ARBRI -TR-02037

BRL

AD

TECHNICAL

TECHNICAL REPORT ARBRL-TR-02037

NUMERICAL PREDICTIONS FOR IGNITION OF A CONFINED REACTIVE GAS

Douglas E. Kooker

January 1978

Approved for public release; distribution unlimited.

USA ARMAMENT RESEARCH AND DEVELOPMENT COMMAND USA BALLISTIC RESEARCH LABORATORY ABERDEEN PROVING GROUND, MARYLAND

Destroy this report when it is no longer needed. Do not return it to the originator.

Secondary distribution of this report by originating or sponsoring activity is prohibited.

Additional copies of this report may be obtained from the National Technical Information Service, U.S. Department of Commerce, Springfield, Virginia 22161.

The findings in this report are not to be construed as an official Department of the Army position, unless so designated by other authorized documents.

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION P	READ INSTRUCTIONS BEFORE COMPLETING FORM				
1. REPORT NUMBER 2.	. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER			
TECHNICAL REPORT ARBRL-TR-02037	ļ	·			
4. TITLE (and Subtitle)		5. TYPE OF REPORT & PERIOD COVERED			
Numerical Predictions for Ignition of	f a Confined	BRL Report 6. PERFORMING ORG. REPORT NUMBER			
Reactive Gas	I a contined	B. PERFORMING ONG. NEFON, NUMBER			
7. AUTHOR(*)		8. CONTRACT OR GRANT NUMBER(s)			
Develop F. Vocker					
Douglas E. Kooker 9. PERFORMING ORGANIZATION NAME AND ADDRESS		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS			
US Army Ballistic Research Laboratory	у	AREA & WORK UNIT NUMBERS			
(ATTN: DRDAR-BLP)	<u></u>	1T161102AH53			
Aberdeen Proving Ground, MD 21005	·				
11. CONTROLLING OFFICE NAME AND ADDRESS US Army Armament Research & Developme	ent Command	JANUARY 1978			
US Army Ballistic Research Laboratory (ATTN: DRDAR-BL)	у	13. NUMBER OF PAGES			
Aberdeen Proving Ground, MD 21005		68			
Aberdeen Proving Ground, MD 21005 14. MONITORING AGENCY NAME & ADDRESS(If different to	from Controlling Office)	15. SECURITY CLASS. (of this report)			
		Unclassified 15a DECLASSIFICATION/DOWNGRADING			
	l	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE			
16. DISTRIBUTION STATEMENT (of this Report)					
Approved for public release; distribu	ution unlimited				
		- %			
17. DISTRIBUTION STATEMENT (of the abetract entered in	Block 20, if different from	m Report)			
18. SUPPLEMENTARY NOTES					
ł					
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)					
issition of any mined access Navion Steles equations for reseting flavo					
ignition of pre-mixed gases; Navier-Stokes equations for reacting flow; numerical integration					
ssv/4589					
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) Ignition of a reactive gas					
in a closed chamber is investigated by numerically solving the one-dimensional,					
compressible Navier-Stokes Equations for a multi-species reacting flow. The full momentum equation is retained in order to model the influence of the finite-					
size chamber. Ignition is studied on a go/no-go basis when the external heat					
flux is interrupted. The results for a simple premixed reaction show a complex					
interaction with the acoustic modes, a hang-fire ignition separating go/no-go,					
and the possibility of a shock wave once ignition occurs. Dependence of ignition					

TABLE OF CONTENTS

	<u>Pag</u>	e
	LIST OF TABLES	5
	LIST OF FIGURES	7
	NOMENCLATURE	9
I.	INTRODUCTION AND MOTIVATION	L
II.	ANALYSIS	2
	Assumptions	3
	Governing Equations	4
	Boundary Conditions	5
	Method of Solution	7
III.	RESULTS	9
	Correlation of Results	3
IV.	CONCLUSIONS	4
٧.	ACKNOWLEDGMENT	5
	REFERENCES	7
	APPENDIX A	9
	APPENDIX B	7
	DISTRIBUTION LIST	3

LIST OF TABLES

		Pa	age
Table 1.	Parameters Held Constant	. 1	L9
Table 2.	Results of Parametric Study	. 2	20

LIST OF FIGURES

			<u>P</u>	age
Figure	1.	Problem Configurations - (a) Solid Propellant in Closed Chamber; (b) Reactive Gas in Closed Chamber		12
Figure	2.	Physical Boundary Conditions	•	15
Figure	3.	Time-Dependent Heat Flux Imposed at z=0	•	16
Figure	4.	Control Volume Nomenclature	•	17
Figure	5.	Temperature Distribution for Standard Case (No Reaction)		21
Figure	6.	Temperature Distribution for Standard Case	•	22
Figure	7.	Velocity Distribution for Standard Case At Time ~107	•	24
Figure	8.	Density Distribution for Standard Case	•	25
Figure	9.	Reactant Mass Fraction Distribution for Standard Case		26
Figure	10.	Temperature Distribution for Standard Case (t = 127.0)		27
Figure	11.	Velocity Oscillation Pattern for Standard Case (t =127.0) At Time ~132		28
Figure	12.	Density Distribution for Standard Case (t $_{mq}$ =127.0)		29
Figure	13.	Reactant Mass Fraction Distribution for Standard Case (t_{mq} =127.0)		30
Figure	14.	Temperature-Time History At Heated Wall (Varying t_{mq}) for Standard Case		31
Figure	15.	Temperature Distribution for Standard Case (t _{mq} =127.87) Showing Flame Formation		33

LIST OF FIGURES (Continued)

			Page
Figure	16.	Pressure Distribution for Standard Case (t = 127.87) Showing Shock Wave Formation	. 34
Figure	17a.	Temperature Distribution for Standard Case (t =128.0) As Runaway Reaction Begins	. 35
Figure	17b.	Velocity Distribution for Standard Case (t =128.0) As Runaway Reaction Begins	. 36
Figure	17c.	Temperature Distribution for Standard Case (t_{mq} =128.0) As Runaway Reaction Accelerates	. 37
Figure	17d.	Velocity Distribution for Standard Case (t =128.0) As Runaway Reaction Accelerates	38
Figure	18.	Temperature-Time History At Heated Wall (Varying t_{mq}) for Case CV2	. 39
Figure	19.	Temperature Distribution for Case CV2 (t = 185.5) Showing Flame Formation	40
Figure	20.	Reactant Mass Fraction Distribution for Case CV2 (t =185.5) Showing Flame Formation	. 41
Figure	21.	Pressure Distribution for Case CV2 (t _{mq} =185.5)	. 42

NOMENCLATURE

NOMENCLATURE (Continued)

u*/ar*; velocity u ρ_{i}/ρ_{i} mass fraction of species i Y z*/L*; axial coordinate z z* pre-exponential factor (sec⁻¹) $^*/^*_r$; coefficient of viscosity μ $(4/3)\mu/Re$ $\mu_{\mathbf{R}}$ reference value of coefficient of viscosity (gm/cm-sec) ρ^*/ρ_r^* ; density density of species i ρį reference value of density (gm/cm^3) a constant, $0 \le \theta \le 1$ $\tilde{\omega}^{i}L^{*}/\rho_{r,}^{*}a_{r}^{*}$; chemical production rate of species i

Subscripts

- i pertaining to species i
- j location of grid point
- r reference value
- t derivative with respect to time
- z derivative with respect to axial coordinate

Superscripts

- * dimensional quantity
- n current time level
- n+1 new time level

I. INTRODUCTION AND MOTIVATION

Any attempt to construct a mathematical model of solid propellant ignition and/or unsteady combustion is faced with the difficulty of describing the gas-phase reaction zone. Unless it can be assumed that solid-phase reactions dominate completely, a prediction of solid propellant decomposition rate is heavily dependent upon events occurring in the gas phase. Competition between convection, heat conduction, species diffusion, and chemical reaction rates will establish the instantaneous energy flux to the surface of the reactive solid. The ability to describe this interaction is a prerequisite for mathematical models designed for transient calculations.

The study of transient solid propellant combustion in Ref. 1 examined several combustion models which assume the flame region to be quasi-steady. This affords a tremendous simplification in the analysis, if it also can be assumed that the spatial distributions of heat release and chemical production rate are known and remain unchanged. The latter assumption effectively uncouples the energy equation from the species continuity equations, and thus any fixed distribution is hard to defend. Furthermore, the basic quasi-steady assumption is difficult to justify for problems related to a gun combustion chamber where the entire ignition and unsteady combustion process is completed within milliseconds.

Four recent models^{2,3,4,5} of the solid propellant ignition process have analyzed the gas-phase reaction zone in much greater detail. These studies have led to considerable insight into the competing processes which control ignition of a reactive solid. However, all have dealt with a constant-pressure "isolated" ignition problem. The isolation is a consequence of applying vanishing gradient boundary conditions to the

¹ Kooker, D. E., and Nelson, C. W., "Numerical Solution of Three Solid Propellant Combustion Models During a Gun Pressure Transient", BRL Report No. 1953 (AD #A035250), USA Ballistic Rsch Lab, APG, MD, Jan 77 (see also 12th JANNAF Combustion Meeting, Newport, RI, CPIA Publication 273, pp 173-197, Dec 75).

Hermance, C. W., and Kumar, R. K., "Gas Phase Ignition Theory for Homogeneous Propellants Under Shock Tube Conditions", AIAA J., Vol. 8, No. 9, pp 1551-1558 (Sep 70).

³ Kashiwagi, T., "A Radiative Ignition Model of a Solid Fuel", <u>Comb.</u> Sci. Tech., Vol. 8, pp 225-236 (1974).

⁴ Bradley, H. H., Jr., "A Unified Theory of Solid Propellant Ignition, Part 1, Development of Mathematical Model", NWC TP5618 (Aug 74).

⁵ Kindelan, M., and Williams, F. A., "Radiant Ignition of a Combustible Solid with Gas-Phase Exothermicity", <u>Acta Astronautica</u>, Vol. 2, No. 11/12 Nov/Dec 75).

gas-phase dependent variables at an infinite distance from the propellant surface; thus, changes in the outside environment cannot influence the ignition process. Additionally, each analysis is constrained by various combinations of assumptions such as a unity Lewis number, negligible kinetic energy, multiple species with identical molecular weights and specific heats, etc.

The current study is motivated by a desire to model the ignition and unsteady combustion process of an end-burning solid propellant grain confined in a one-dimensional chamber, as shown in Fig. la. The model must be sufficiently general to allow variable transport properties, various chemical decomposition schemes, etc., without the restriction of constant pressure. The objective is two-fold: (a) predict the instantaneous regression rate of the reactive solid as a function of the self-generated pressure, and (b) look for potential instabilities in both regimes—ignition and unsteady combustion.

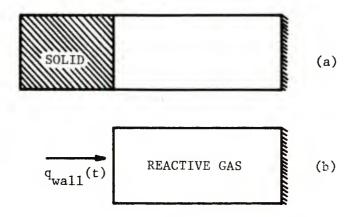


Figure 1. Problem Configurations - (a) Solid Propellant in Closed Chamber; (b) Reactive Gas in Closed Chamber

The present investigation is the first step in the above model and has the limited objective of describing the ignition sequence of a reactive gas confined in a rigid, one-dimensional chamber. As shown in Fig. 1b, one boundary is assumed to be insulated and the other is subjected to an externally-prescribed, time-dependent heat flux. The imposed heat flux, as used here, serves as the ignition stimulus and is not intended to represent the response of the solid in the full propellant ignition problem of Fig. 1a. The remainder of this report is concerned with the solution of the gas-phase ignition problem shown in Fig. 1b.

II. ANALYSIS

The gas-phase ignition problem described above requires the numerical solution to the one-dimensional, time-dependent, compressible

Navier-Stokes Equations for a multi-species reacting flow field. To correctly model the influence of the finite-size chamber, the system must retain the full momentum equation, as opposed to the trivial constant-pressure form. At no time will the analysis employ an externally specified value of "Tignition"; thus, no artificial boundary is drawn between ignition and unsteady combustion. Ignition will be determined by a go/no-go response when the external heat flux is terminated.

Assumptions

The reactive gas confined in the chamber is assumed to be a mixture of perfect gases, each of which may have a different molecular weight, specific heat capacity, and heat of formation. It is assumed that the mixture viscosity, thermal conductivity, and species diffusion coefficients can be described at the molecular level, i.e., all transport is laminar. Admittedly, turbulent transport is the dominant mode in many combustion situations. However, the gas-phase ignition problem posed here should not be controlled by turbulence. In the event of a violent unsteady flame propagation in the chamber, this assumption would have to be re-examined. The numerical solution procedure assumes variable laminar transport properties, with no constraints on the magnitude or variability of the mixture Lewis number or Prandtl number. The influence of radiation, gravity, bulk viscosity, the Dufour effect, the Soret effect, and diffusion due to pressure gradients will be neglected.

The current results are based on the additional assumption that the chamber initially contains a reactive gas composed of the single species A, capable of undergoing the one-step, irreversible reaction

 $A \rightarrow 2B$.

Fick's Law is then used to describe the diffusion mass flux in this binary system. It should be noted that extending Fick's Law to a generalized multi-component mixture, and then assigning unequal diffusion coefficients, will lead to a violation of the basic identity that the sum of the diffusion mass fluxes must be zero. Although this has been done⁶,⁷, the

Rivard, W. C., Farmer, O. A., and Butler, T. D., "RICE: A Computer Program for Multicomponent Chemically Reactive Flows at All Speeds", LA-5812, Los Alamos Scientific Laboratory, Los Alamos, NM, Mar 75.

Kothari, A. P., Anderson, J. D., Jr., and Jones, E., "Navier-Stokes Solutions for Chemical Laser Flows", AIAA J., Vol. 15, No. 1, pp 92-100 (Jan 77).

correct procedure requires the solution of the coupled equations relating all diffusion mass fluxes and mass fraction gradients, as described by $Edelman^8$.

Governing Equations

Based on the foregoing assumptions, the conservation equations in an inertial frame of reference can be written as:

Global Continuity
$$\rho_{t} + (\rho u)_{z} = 0$$
 (1)

Momentum
$$\omega_{t} + [\omega u + p]_{z} = [\mu_{R}(\frac{\omega}{\rho})_{z}]_{z}$$
 (2)

Energy
$$(\rho E)_{t} + [\omega E + pu]_{z} = \left\{ k_{g} T_{z} + \mu_{R} u u_{z} + (\sum_{i=1}^{N} h_{i} \rho D_{12} Y_{i}) \right\}_{z}$$
 (3)

Species Continuity
$$\rho Y_{i_{t}} + \omega Y_{i_{z}} = (\rho D_{12}Y_{i_{z}})_{z} + \tilde{\omega}^{i} \qquad (4)$$

$$i=1,\dots,N-1$$

State
$$p = \rho RT , R = R_{o} \sum_{i=1}^{N} (Y_{i}/M_{i})$$

$$h = \sum_{i=1}^{N} Y_{i}h_{i} , h_{i} = \int_{T^{o}}^{T} c_{p_{i}} d\hat{T} + h_{i}^{o}$$

$$\text{where } \omega = \rho u, E = h + \frac{u^{2}}{2} - p/\rho, Y_{i} = \rho_{i}/\rho$$
(5)

Equations (1) - (3) are solved numerically in their strict conservation form. Attempts to solve the species continuity equation written in terms of partial densities led to numerical instabilities when forming a mass fraction with a value very close to unity. The origin of this instability appears to be machine inaccuracy in division of two nearly identical numbers, and is not attributable to the stiffness of the equation. Use of the form shown in Eq. (4) eliminated the difficulty.

The common practice of transforming the axial coordinate (using an integral of density) to eliminate direct dependence on the global continuity equation is unworkable here because the computational domain is enclosed by two boundaries at finite locations.

⁸ Edelman, R. B., Fortune, O. F., and Weilerstein, G., "An Analytical and Experimental Investigation of Gravity Effects Upon Laminar Gas Jet-Diffusion Flames", 14th Symposium (International) on Combustion, Aug 72, Penn State University, pp 399-412.

Boundary Conditions

Boundary values of the dependent variables must be specified at both the heated boundary, z=0, and the insulated boundary, z=1 (see Fig. 2).

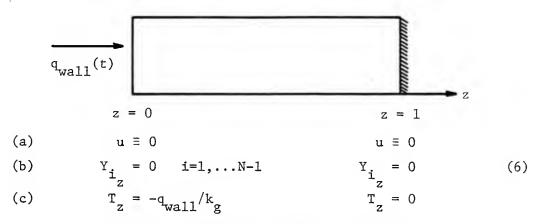


Figure 2. Physical Boundary Conditions

The assumption of impenetrable walls requires the mean flow velocity to vanish at z=0 and z=1 [Eq. (6a)]. The individual species velocities must also vanish at the solid boundary, which means that all diffusion velocities are zero. Since by Fick's Law the diffusion velocity is linearly dependent upon the spatial gradient of the mass fraction, each mass fraction gradient must vanish at z=0 and z=1 [Eq. (6b)]. Combining Eqs. (6a) and (6b) with the energy balance at the boundaries results in a zero temperature gradient at z=1 and a time-dependent temperature gradient at z=0 governed by $q_{wall}(t)$ [Eq. (6c)]. At each boundary, there are N+3 dependent variables, but only N+2 conditions given by Eq. (6) along with the equation of state. However, no physical boundary condition is missing. The situation is directly analogous to the simpler, inviscid acoustic problem at a boundary; a value of the velocity perturbation (or an equivalent admittance condition) can be specified but the value of the pressure perturbation must follow from the solution. To specify both values would over-determine the system of equations.

The numerical solution procedure requires values of all dependent variables at both boundaries for every time step. In a complex system of equations, the manner in which the "extraneous" boundary values are determined is usually the difference between success and failure. An accurate method to solve the inviscid acoustic problem is based on the fact that the system of equations is hyperbolic. Because of the finite propagation velocity, one characteristic line in the t-z plane will intersect the boundary at the new time level. The compatibility condition along this line provides the missing information which relates the unknown boundary values to the known solution at the previous time level.

In the present gas-phase ignition problem, the governing equations are parabolic. All characteristic directions have essentially collapsed to the single line t=constant, which implies an infinite speed of propagation. The potential benefit from a method-of-characteristics solution at the boundary is now lost.

The present investigation attempted several different methods to determine the boundary value of pressure consistent with the interior numerical solution. The only successful one is based on the idea of mechanical equilibrium at the boundary. Since the mean velocity is constrained to be zero at all times, the momentum equation reduces to the statement that the gradient of the stress tensor must vanish. Thus, at the boundary, the gradient of thermodynamic pressure must balance the gradient of the viscous normal stress, viz.,

$$P_z = (\mu_R u_z)_z \tag{7}$$

Equation 7 is enforced at a boundary by fitting a cubic profile (in velocity and pressure) through the adjacent nearest neighbors, and appropriately differentiating. This provides the value of pressure, and then the value of density follows directly from the equation of state [Eq. (5)].

The boundary conditions are completed by specifying the time-dependent heat flux imposed at z=0. All computations discussed in the present study are based on $q_{\rm wall}(t)$ shown in Fig. 3, where the duration of heating is altered by varying the cut-off time, $t_{\rm mq}$. The shut-down portion of the heating profile (after $t_{\rm mq}$) is necessary to keep a discontinuous gradient from destroying the numerical solution; its shape remained unchanged throughout the study. Unless otherwise stated, the constant portion of the heating curve was held at the value 10 cal/cm^2-sec. Note that for t > t $_{\rm mg}$ +5, the heated wall becomes adiabatic.

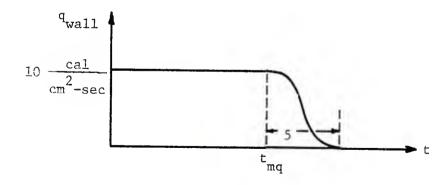


Figure 3. Time-Dependent Heat Flux Imposed at z=0

Method of Solution

The numerical integration technique used to solve Eqs. (1) - (4) is constructed on the basis of a control volume of length Δz centered about each grid point (see Fig. 4).

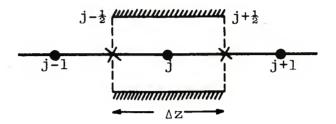


Figure 4. Control Volume Nomenclature

Each term in the equation, other than the time derivative, is weighted between its value at the old time level "n" and the new time level "n+1". Using global continuity [Eq. (1)] as an example,

$$\frac{\rho_{j}^{n+1} - \rho_{j}^{n}}{\Delta t} + \frac{\theta}{\Delta z} \left(\rho u_{j+\frac{1}{2}} - \rho u_{j-\frac{1}{2}}\right)^{n+1} + \frac{1-\theta}{\Delta z} \left(\rho u_{j+\frac{1}{2}} - \rho u_{j-\frac{1}{2}}\right)^{n} = 0$$
 (8)

where θ is a constant, $0 \le \theta \le 1$, and the subscripts indicate grid point location. The accuracy of the integration is $0(\Delta t^2)$ if $\theta = \frac{1}{2}$. However, with the competing effects of convection and diffusion, stability can be assured only when $\theta > \frac{1}{2}$. All solutions discussed in this report are based on $\theta = 0.55$. Values of the dependent variables are stored only at the integer grid point location; values required at the midpoints are found from

$$\rho u_{j+\frac{1}{2}} = \frac{1}{2} (\rho u_{j+1} + \rho u_{j}), \text{ etc.}$$
 (9)

Similarly, flux terms which depend on a spatial gradient are represented as

$$k_{g_{z}} = \frac{1}{2} (k_{g_{j+1}} + k_{g_{j}}) (\frac{T_{j+1} - T_{j}}{\Delta z})$$
 (10)

using the internal heat flux as an example. This procedure insures strict conservation, i.e., the flux value entering control volume j+l across the interface located at $j+\frac{1}{2}$ will be exactly the value which left control volume j across the same interface.

Equations (2) - (4) are each written in a form analogous to Eq. (8), such that the terms representing time storage, convection, diffusion, and production are coupled at the new time level "n+1". The result, after applying the boundary conditions, is a tri-diagonal matrix which can be inverted with the standard Thomas Algorithm. The solution then proceeds by successive substitution, not quasi-linearization. A series of tri-diagonal matrix inversions is performed in the following sequence, where each step incorporates the latest dependent variable estimates from the previous steps:

- 1. Solve the species continuity equations for the $Y_{i}^{\dagger}s$,
- 2. Solve the energy equation for the E's,
- 3. As a provisional step, solve the global continuity equation for the ρ 's and update the pressure array,
 - 4. Solve the momentum equation for the ω 's,
- 5. Re-solve the global continuity equation for the ρ 's and again update the pressure array.

Steps 1-5 constitute one iteration; the values of the dependent variables at the new time level are taken to be those obtained on the third iteration. Of the flow field points investigated, the third iteration produced convergence to at least five significant digits.

Stability of this integration could be maintained only by observing the well-known Courant condition,

$$\Delta t < \Delta x/(a+u)_{max}$$

which is normally applicable to explicit techniques. Furthermore, the cell Reynolds number limitation,

$$Re_{cell} \equiv uRe\Delta z < 2$$

became a major barrier. All attempts to circumvent these two restrictions ended in failure. The difficulty stems primarily from the type of problem posed here. A system of coupled parabolic partial differential equations, exhibiting an infinite speed of propagation (all characteristic directions collapse to t=constant), is solved between two fixed boundaries. The closed computational domain traps (and retains) numerical errors as well as the desired physical quantitites. Furthermore, rapid heating of the chamber excites nonlinear acoustic oscillations in the gas which change significantly on a short time scale. This combination presents a formidable challenge to any numerical method based on large time steps.

III. RESULTS

Numerical predictions for ignition behavior are presented for a simple two-species system representing the ultimate in a premixed reaction. Initially, the chamber contains only species A which is capable of the single, one-step, irreversible reaction,

$$A \rightarrow 2B$$
.

As would be the case for an elementary reaction, the reaction rate is assumed linearly proportional to the concentration of A. Hence, the chemical production rate term required in Eq. (4) can be written as

$$\tilde{\omega}^{A} = -Z^{*} \rho Y_{A} (L^{*} / a_{r}^{*}) \exp[-E^{*} / R_{o}^{*} T^{*}].$$

In keeping with the simplicity of this example, the thermal conductivity, viscosity, diffusion coefficient, and specific heats were all held constant at the representative values shown in Table 1.

Table 1. Parameters Held Constant

$$M_{A}^{*}$$
 = 30 gm/gm-mole M_{B}^{*} = 15 gm/gm-mole c_{P}^{*} = .331 ca1/gm-°K c_{P}^{*} = .662 ca1/gm-°K k_{g}^{*} = 2.0 x 10⁻⁴ ca1/cm-sec-°K c_{P}^{*} = 5.0 x 10⁻¹ cm²/sec c_{P}^{*} = 5.0 x 10⁻⁴ gm/cm-sec ; c_{P}^{*} = 1 c_{P}^{*} = 3.2238 x 10⁴ cm/sec c_{P}^{*} = 3.00 °K c_{P}^{*} = 300 °K c_{P}^{*} = 1965.4

A parametric study was conducted to estimate the influence of the three important kinetic parameters, Z^* the pre-exponential factor, \hat{E}^* the activation energy, and ΔH^* the heat of reaction. The values considered are listed in Table 2.

Table 2. Results of Parametric Study $(q_{wal1}^* = 10 ca1/cm^2 - sec)$

Case	E* kcal mole	Z [*] sec ⁻¹	ΔH^* (exothermic) $\frac{kcal}{mole}$	t _{mq} at go/no-go (n-d)
Std.	35	10 ¹³	35	127.87
CV1	35	10 ¹²	35	174.7
CV2	35 ,	10 ¹²	25	185.4
CV3	35	10 ¹²	30	179.3
CV4	35	10 ¹³	30	131.0
CV5	35	10 ¹⁴	30	97.6
CV6	30	10 ¹²	30	115.8
CV7	30	10 ¹³	30	83.0

The results to follow are displayed in machine-drawn plots, constructed by connecting two points with a straight line segment. None of the curves were smoothed or fitted with polynomials or splines. The non-dimensional axial distance, $0 \leqslant z \leqslant 1$, is divided into 50 cells.

For reference purposes, Fig. 5 shows the temperature distribution in the chamber for the special case when q_{wall} is held constant at $10~cal/cm^2$ -sec and the reaction rate is set to zero. The parameter values listed on the right-hand side of the figure are non-dimensional times from the onset of heating; one non-dimensional time unit is the time required for a small amplitude disturbance to travel the length of the chamber, assuming a uniform temperature of 300°K and $Y_{\text{A}} \equiv 1$. Initial conditions are $u^* \equiv 0$, $p^* = 1$ atm., and $Y_{\text{A}} \equiv 1$. The results show that 850°K is the maximum temperature achieved during a heating time of 145 time units when species A is inert.

Figure 6 shows the temperature distribution in the chamber for the kinetic parameters denoted as the standard case. The heating rate remained constant at 10 ca1/cm^2 -sec. The temperature at z=0 exceeds 850°K at a time of 128, and the distribution shows evidence of the classic

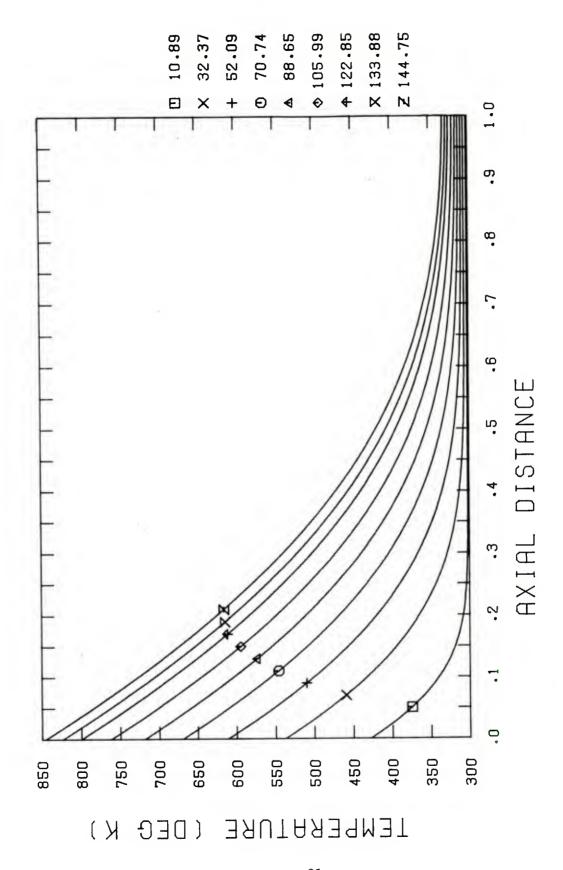


Figure 5. Temperature Distribution for Standard Case (No Reaction)

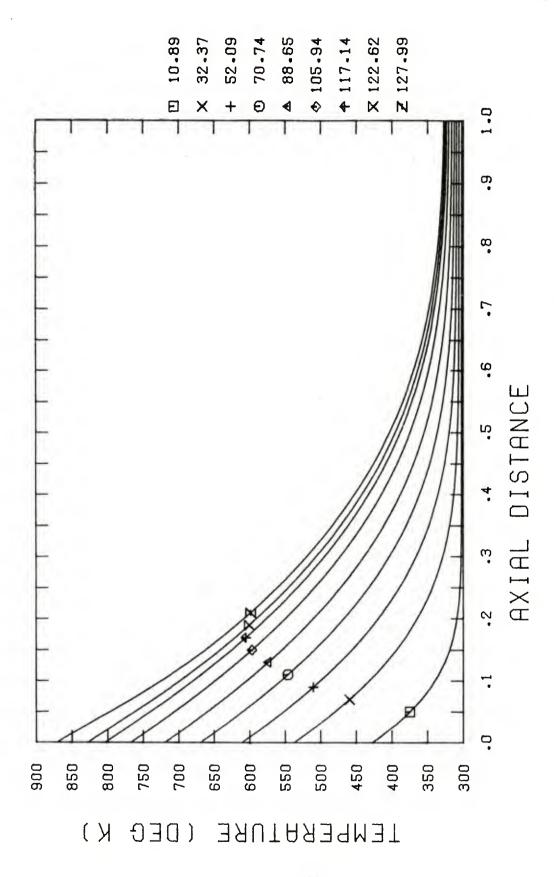


Figure 6. Temperature Distribution for Standard Case

"bulge" near the heated wall as discussed by Merzhanov and Averson . This indicates the onset of the reaction. These temperature profiles, however, give no indication of the oscillatory nature of the confined gas. Rapid heating of the chamber leads to a thermally-driven convection process which creates the velocity oscillation pattern shown in Fig. 7. The plot shows the development of the wave over one-half of the cycle; as indicated by the shape of the profile, the frequency is close to that of the fundamental. Note that all velocities are positive. Hence, hot gas is continuously carried away from the heated end of the chamber. This is verified by the development of the density distribution shown in Fig. 8. The counterpart of the bulge in the temperature distribution near z=0 is visible in the density distribution at t=128. The extent of the chemical reaction at this time can be visualized with the reactant mass fraction distribution displayed in Fig. 9. The results indicate the reaction at the boundary is approximately two percent complete.

As a first step toward establishing the critical go/no-go ignition point, the time t_{mq} which begins the shut-down portion of the external heat flux curve (see Fig. 3) was set to 127.0. The temperature distribution in Fig. 10 clearly shows the reaction was not self-sustaining, and the temperature profiles decay between two adiabatic walls. teresting aspect of this cooling process is the effect on the velocity oscillation pattern. The pressure near the heated boundary immediately senses the falling temperatures and sends an expansion wave across the chamber. This expansion wave inverts the velocity oscillation to create the pattern in Fig. 11, which shows the development of the distribution during one-half of the oscillation cycle. The negative velocities mean the direction of the flow is toward the heated boundary; thus, cold gas is brought in to help "put out the fire." This is again confirmed by the density distribution displayed in Fig. 12. The progress of the reaction can be followed in Fig. 13 which shows the reactant mass fraction distribution during the same time interval. The reaction near the wall continues to three percent completion (at t~133) even though the temperatures are decreasing, but then convection and diffusion begin to dominate. The result is an increase in the mass fraction of A near the wall, as the product B is spread throughout the chamber.

The behavior near the critical ignition point can be seen more clearly by plotting the temperature of the gas at z=0 as a function of time, for a series of runs varying only t_{mq} . Such a plot is shown in Fig. 14. The extreme sensitivity of this pre-mixed reaction to the cut-off time of the external stimulus is evident; the critical time of 127.87 leads to a hang-fire situation where the runaway reaction occurs 36 time units after t_{mq} . A nearly identical phenomenon was predicted

⁹ Merzhanov, A. G., and Averson, A. E., "The Present State of the Thermal Ignition Theory: An Invited Review", Comb. Flame, Vol. 16, pp 89-124 (1971).

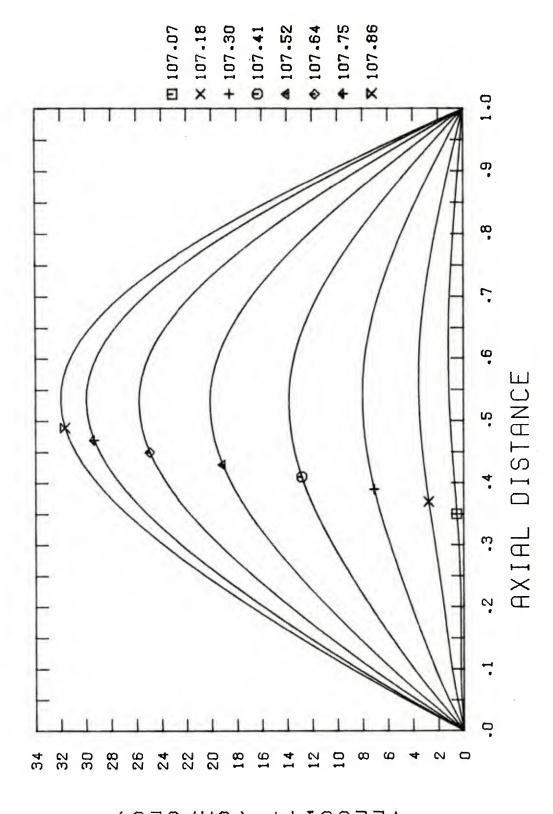


Figure 7. Velocity Distribution for Standard Case At Time ~107

VELOCITY (CM/SEC)

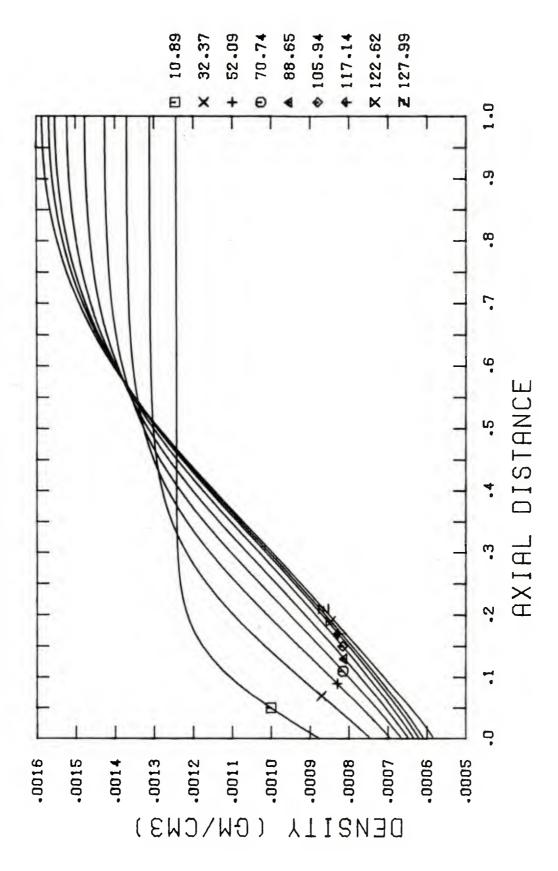
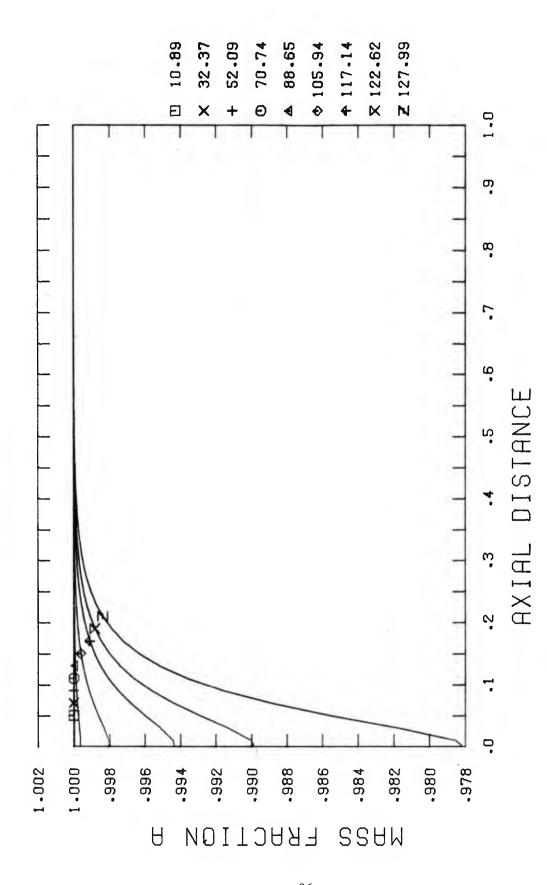


Figure 8. Density Distribution for Standard Case



Reactant Mass Fraction Distribution for Standard Case Figure 9.

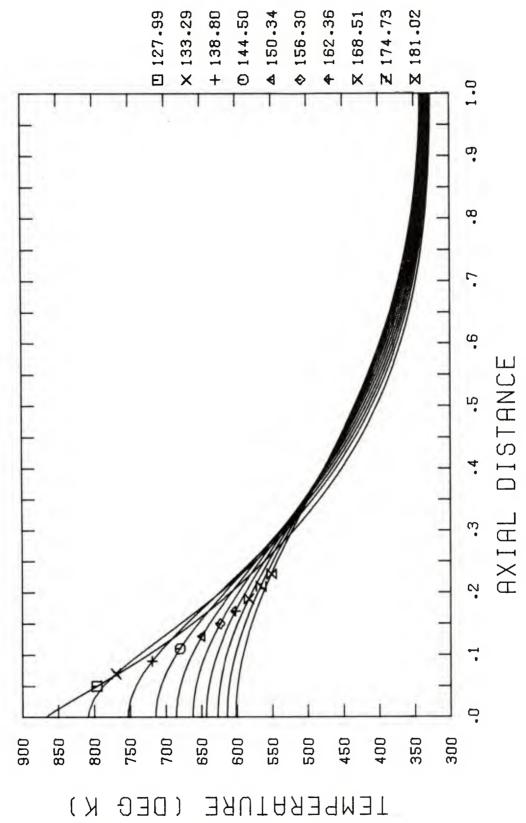


Figure 10. Temperature Distribution for Standard Case (t $_{\rm mq} = 127.0)$

27

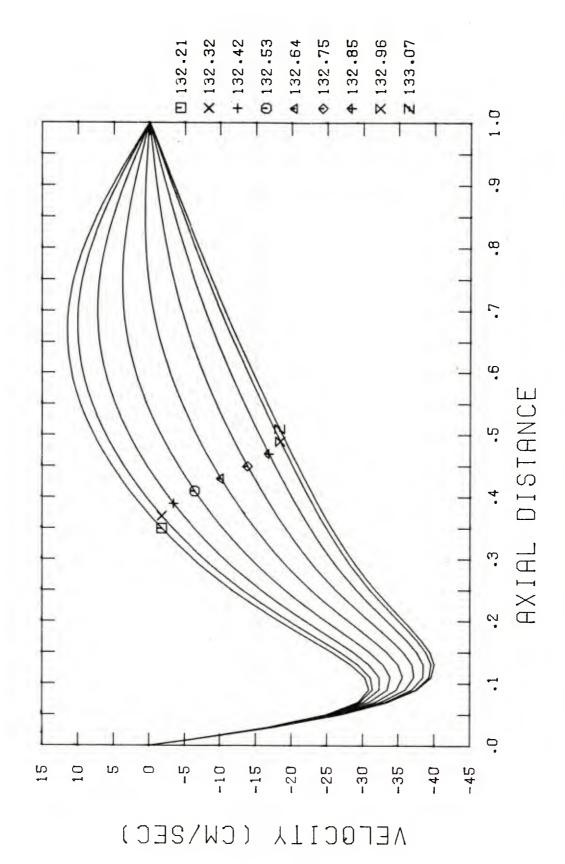


Figure 11. Velocity Oscillation Pattern for Standard Case (t $_{mq}\!=\!127.0)$ At Time ~132

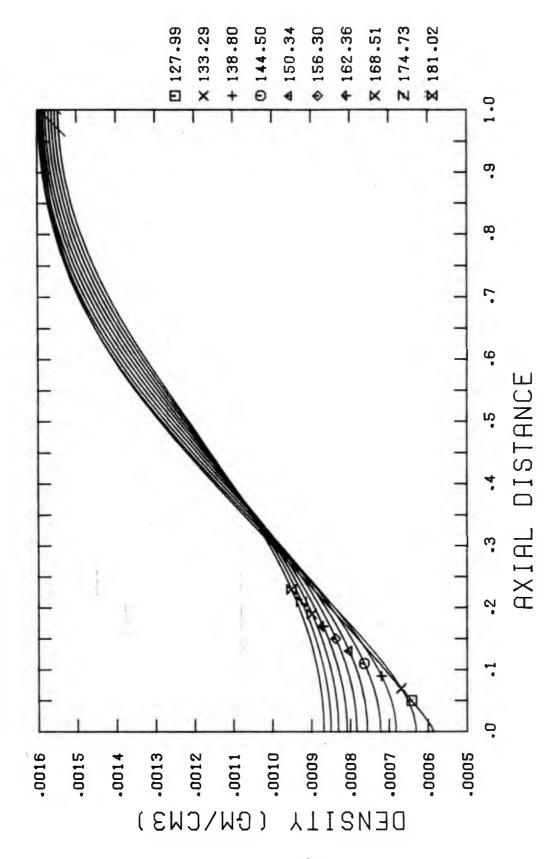
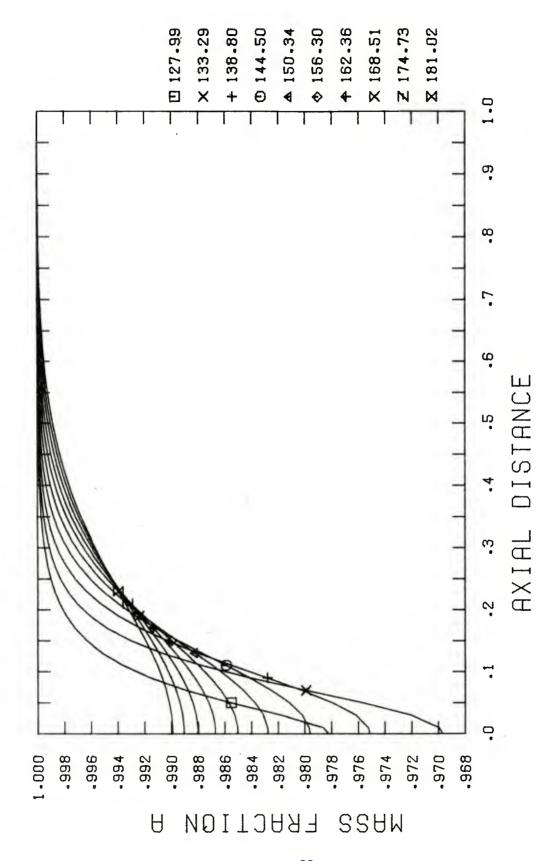
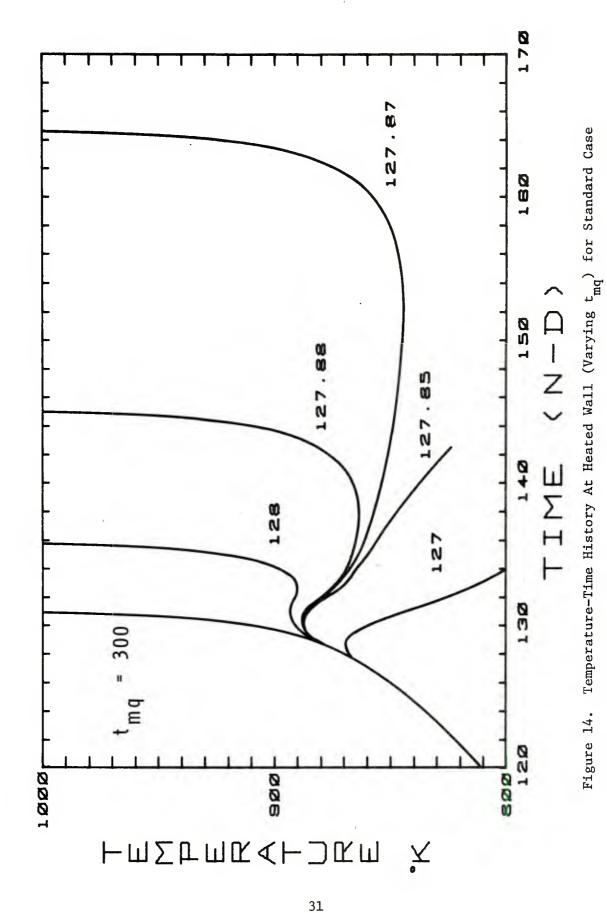


Figure 12. Density Distribution for Standard Case (t $_{\rm mq} = 127.0)$



Reactant Mass Fraction Distribution for Standard Case (t $_{\rm mq}$ =127.0) Figure 13.



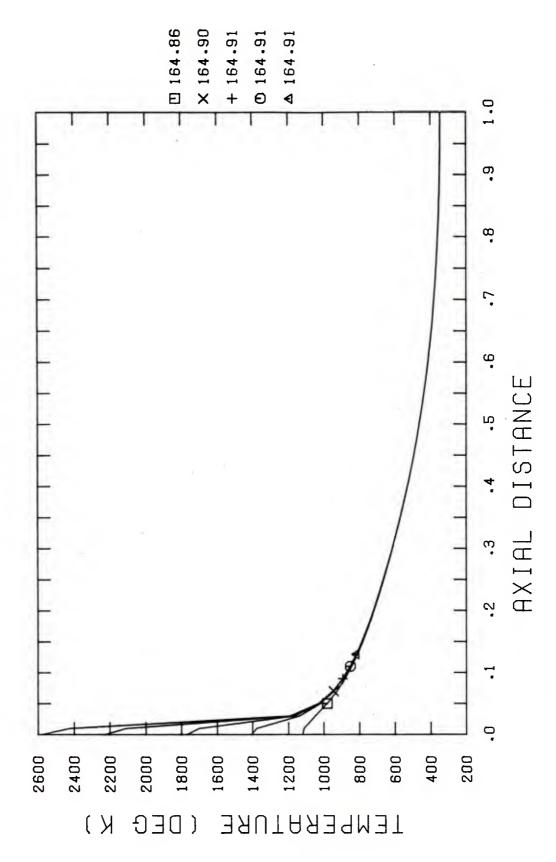
by $\operatorname{Bradley}^{10}$ in his ignition study of a reactive solid with no contribution from the gas-phase.

Evidence that the runaway reaction is self-sustaining after the long hang-fire (t_{mq} =127.87) is given by the temperature distribution plotted in Fig. 15 at a time of approximately 164. The results indicate a rapid rise to nearly 2600°K as the flame forms at the z=0 boundary. In this short time interval, the temperature is increasing much faster than the density can decrease. Hence, a significant change in pressure should occur. This is indeed the case, as shown in Fig. 16. The rapidly increasing pressure profiles coalesce into a shock wave. Unfortunately, the numerical integration method is sensitive to the fact that continuous differential equations cannot be integrated directly across a discontinuity and this halts the solution. It is concluded, however, that successful ignition of a pre-mixed gas with the kinetic parameters of the standard case will lead to a detonation wave.

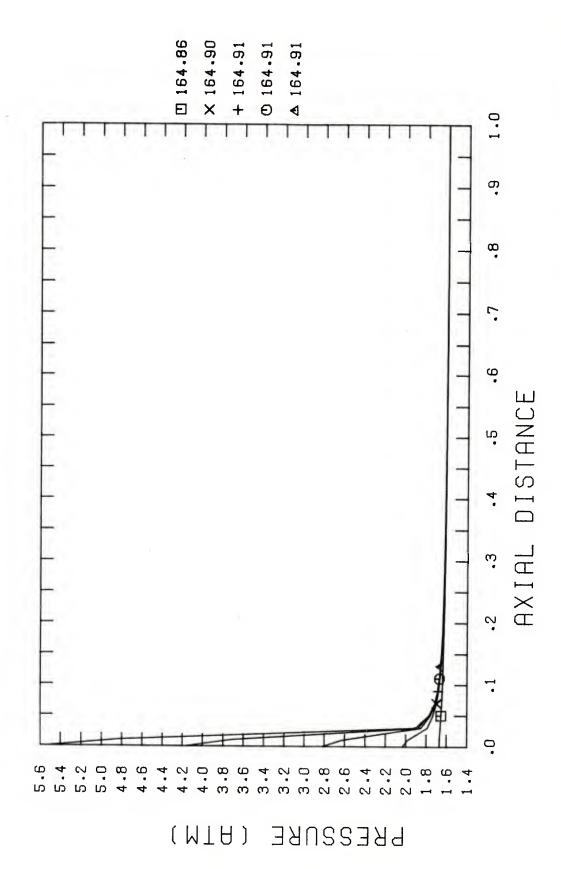
The rapid heat release which drives the shock wave formation, displayed in Figs. 15 and 16, has a dramatic influence on the gas velocity oscillation pattern in the chamber. This is shown in the multiple plots of Fig. 17 for the standard case when t_{mq} =128.0 (see Fig. 14 for the wall temperature-time history). Temperature and velocity distributions are plotted in Figs. 17(a) and 17(b) for the time interval when the runaway reaction is just beginning. At the time of 133.14, the velocity distribution is a low amplitude oscillation pattern similar to that shown in Fig. 7. However, the internal heat generation near the z=0 boundary creates an increasing temperature and pressure field which halts the oscillation and forces a monotonically swelling velocity profile. This continues at an accelerated pace, as shown in Figs. 17(c) and 17(d), and the maximum velocity moves closer toward the boundary. This will become a "blast-wave" velocity profile which must follow behind the forming detonation wave.

A set of kinetic parameters which does not create a detonation wave can be found in Case CV2. Compared to the standard case, the pre-exponential factor is reduced by a factor of 10 and the exothermic heat release is 10 kcal/mole lower. This combination significantly increases the time to ignition as shown in the temperature-time history plot of Fig. 18. Once ignited, this case produces a much less severe temperature distribution as shown in Fig. 19. The flame temperature is approximately 1800°K, compared to 2600°K for the standard case. Figure 20 shows the reactant mass fraction distribution as the flame is forming. An estimate of the thickness of this pre-mixed flame is about 50 microns. This may be reasonable considering that a complex methane-air diffusion flame is 600-800 microns. Figure 21 is a plot of the pressure distribution during flame formation. The last profile is similar to the

Bradley, H. H., Jr., "Theory of Ignition of a Reactive Solid by Constant Energy Flux", Comb. Sci. Tech., Vol. 2, pp 11-20, (1970).



Temperature Distribution for Standard Case (t $_{mq}$ =127.87) Showing Flame Formation Figure 15.



Pressure Distribution for Standard Case (t $_{\rm mq}$ =127.87) Showing Shock Wave Formation Figure 16.

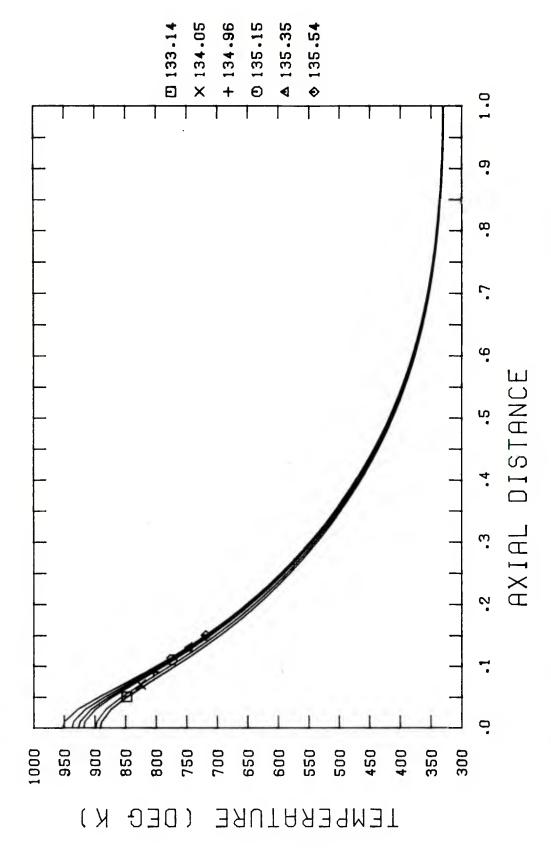
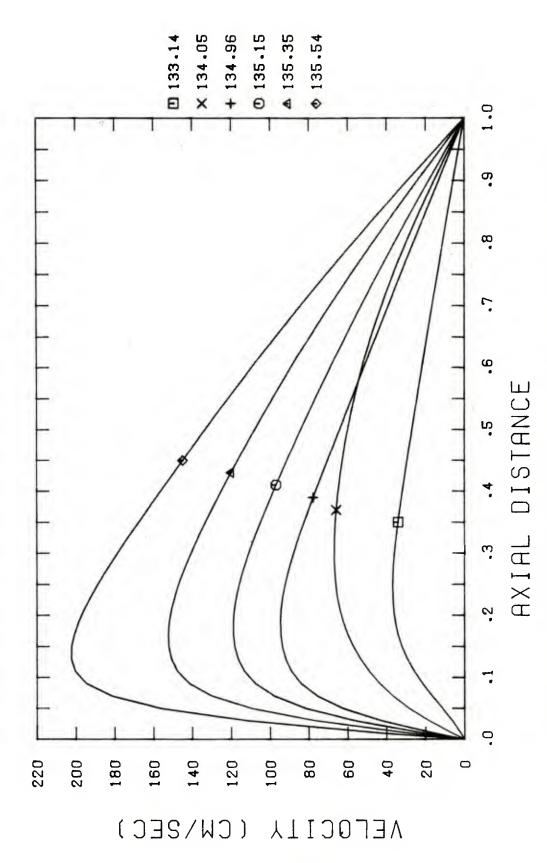
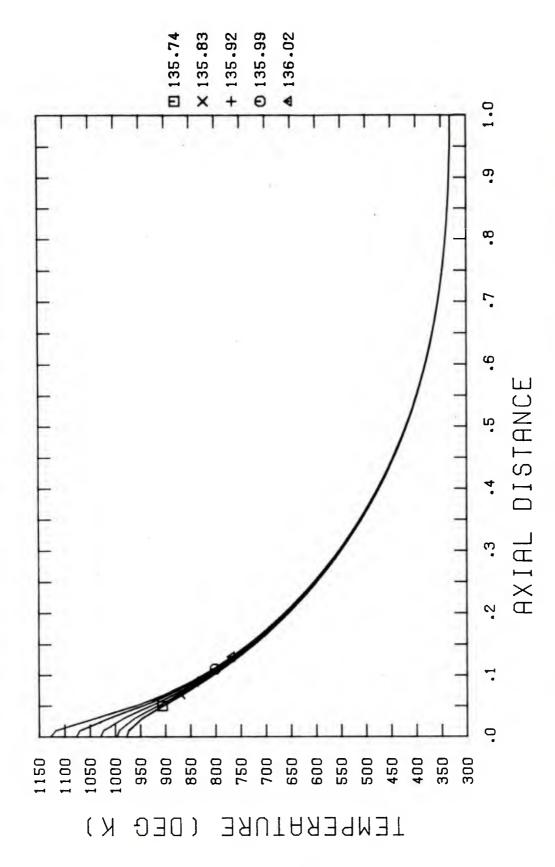


Figure 17a. Temperature Distribution for Standard Case (t =128.0) As Runaway

Reaction Begins



Velocity Distribution for Standard Case (t $_{\rm mq} = \! 128.0)$ as Runaway Reaction Begins Figure 17b.



Temperature Distribution for Standard Case (t =128.0) As Runaway

Figure 17c.

Reaction Accelerates

37

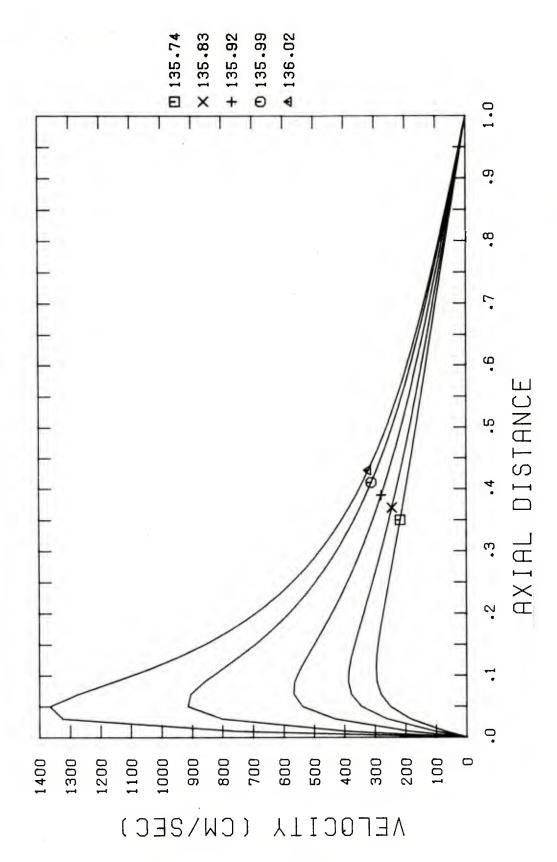


Figure 17d. Velocity Distribution for Standard Case (t $_{\rm mq} = 128.0)$ As Runaway Reaction Accelerates

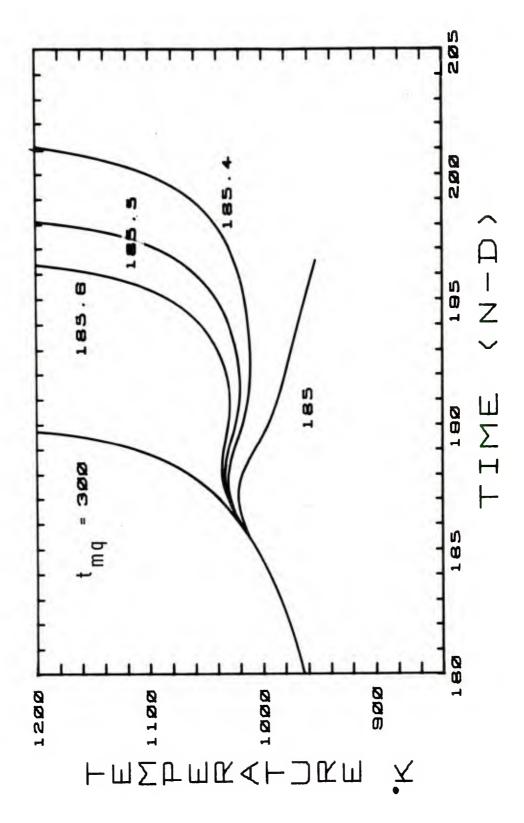


Figure 18. Temperature-Time History At Heated Wall (Varying tmg) For Case CV2

Temperature Distribution for Case CV2 (t =185.5) Showing Flame Formation Figure 19.

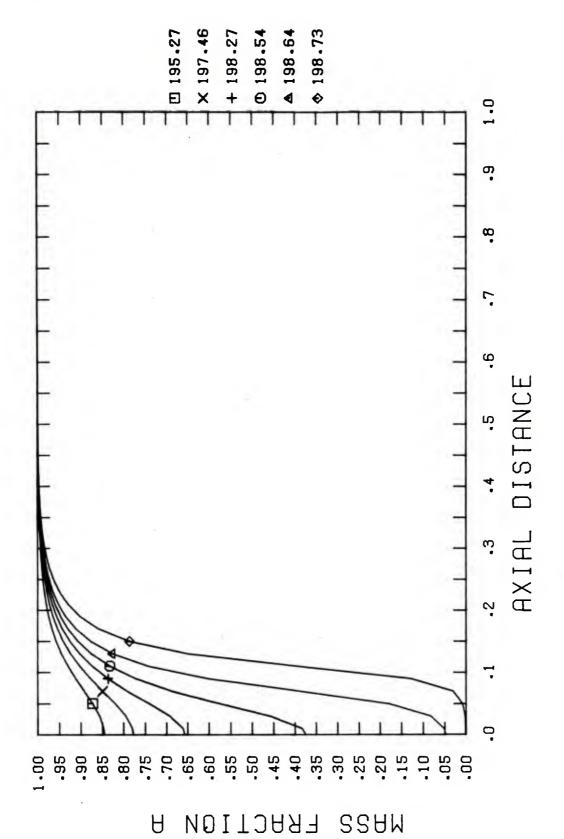


Figure 20. Reactant Mass Fraction Distribution for Case CV2 (t $_{\rm mq}$ =185.5) Showing Flame Formation

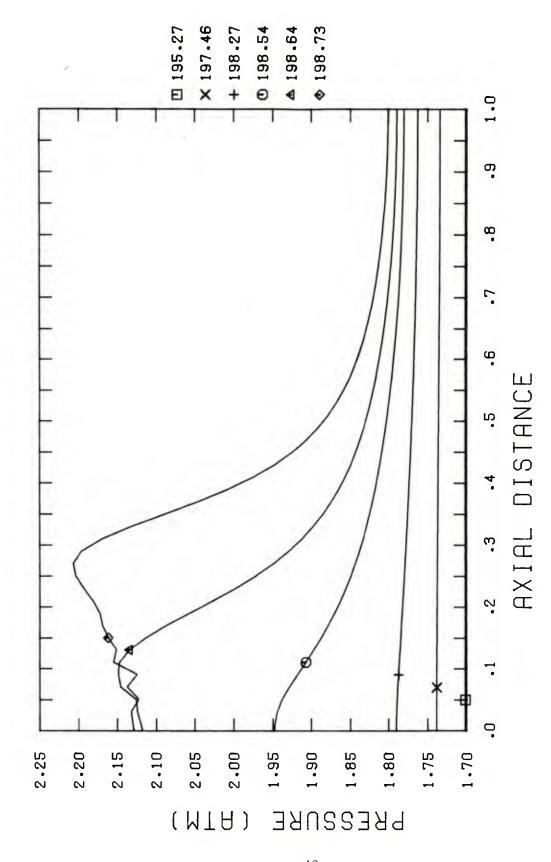


Figure 21. Pressure Distribution for Case CV2 (t $_{mq} = \! 185.5)$

classical description of a laminar deflagration wave in which the pressure decreases slightly across the combustion front. Of course, a compression wave must precede the subsonic deflagration in order to satisfy the wall boundary condition at z=0. The slight "raggedness" of the predicted pressure in this region is non-physical, and is the direct result of violating the cell Reynolds number limitation discussed earlier. Increased grid point resolution would eliminate the problem.

Correlation of Results

The results obtained in the parametric study for time to ignition are summarized in Table 2. The critical value of ignition time for each case is taken to be the value of t_{mq} which yields the longest hang-fire. The temperature-time history for each case can be found in Appendix A. A better perspective of the sensitivity of ignition time to a change in one of the kinetic parameters can be seen with a simple power law correlation. These correlations are given below:

(a) ignition time vs. activation energy

$$t_{mq} \alpha (E^*)^{2.9}$$

(b) ignition time vs. heat of reaction

$$t_{mq} \propto (\Delta H^*)^{-.178}$$

(c) ignition time vs. pre-exponential factor

$$t_{mq} \propto (Z^*)^{-.132}$$

Thus, an increase in activation energy will substantially increase the time to ignition, while an increase in the heat of reaction and/or the pre-exponential factor will decrease the time to ignition.

In ignition studies of all types, the question most frequently addressed concerns the dependence of ignition time on external heat flux. To answer this question for a confined pre-mixed gas, the present investigation conducted a special series of runs based on the standard case. (The results for temperature-time history are included in Appendix B). The constant portion of $q_{\rm wall}(t)$ was varied in small increments over the limited range of 10-25 cal/cm²-sec. The predictions for $t_{\rm mq}$ at go/no-go as a function of the constant portion of $q_{\rm wall}$ correlated exactly as the power law,

$$t_{mq} \propto q_{wall}^{-m}$$
, m=1.89

An interesting comparison can be made with the results of two different solid propellant ignition theories. Bradley and Williams 11 postulated a heterogeneous reaction between a gas-phase oxidizer and the surface of the solid propellant. Their correlation produces the above result with m=1.86, for the activation energy used in the standard case of this paper. Kashiwagi postulated a two reaction model; the solid fuel pyrolyzes (endothermically) at the surface and then reacts in a gas-phase diffusion flame with the ambient oxidizer. The result of his correlation produces the exponent m=1.9, in the heat flux range quoted above.

All three correlations yield nearly the same value for the exponent. In fact, this value is close to 2.00 which is the value obtained from the well-known solution to the heat conduction equation for an inert solid (e.g., see discussion in Ref. 3). The important implication here is that a plot of ignition time versus external heat flux cannot be used to distinguish the mechanism controlling ignition.

IV. CONCLUSIONS

- 1. Numerical predictions of the gas-phase ignition sequence seem qualitatively correct. In general, the results show that:
- a. A confined premixed gas capable of a single, one-step, irreversible, chemical reaction can sustain a hang-fire ignition, i.e., the runaway reaction occurs many time units after the external heat source (ignition stimulus) is terminated.
- b. A hang-fire ignition forms the boundary separating "go" and "no-go".
- c. The acoustic response of the chamber plays a definite role in the ignition of a confined reactive gas.
- d. Successful ignition of the confined premixed gas leads to a thin flame zone, assuming that all transport processes are laminar and that the controlling chemical reaction is a single, one-step, irreversible decomposition. When the exothermic heat of reaction is sufficiently large, the numerical solution predicts the formation of a detonation wave.

Bradley, H. H., Jr., and Williams, F. A., "Theory of Radiant and Hypergolic Ignition of Solid Propellants", <u>Comb. Sci. Tech.</u>, Vol. 2, pp 41-52 (1970).

- 2. Correlations of the numerical results were established to show that:
- a. An increase in activation energy (E *) will substantially increase the time to ignition.
- b. An increase in the exothermic heat of reaction (ΔH^*) will decrease the time to ignition.
- c. An increase in the pre-exponential factor (\boldsymbol{Z}^*) will decrease the time to ignition.
- 3. The dependence of ignition time on external heat flux cannot be used to distinguish a simple premixed gas-phase reaction from other mechanisms which may control ignition.

V. ACKNOWLEDGMENT

The author gratefully acknowledges the substantial contribution of R. D. Anderson who executed the computer program and constructed the CALCOMP plots.

REFERENCES

- Kooker, D. E., and Nelson, C. W., "Numerical Solution of Three Solid Propellant Combustion Models During a Gun Pressure Transient", BRL Report No. 1953 (AD No. A035250), Ballistic Research Lab, Aberdeen Proving Ground, MD, January 1977 (see also 12th JANNAF Combustion Meeting, Newport, RI, CPIA Publication 273, pp 173-197, Dec 75).
- 2. Hermance, C. W., and Kumar, R. K., "Gas Phase Ignition Theory for Homogeneous Propellants Under Shock Tube Conditions", AIAA J., Vol 8, No. 9, pp 1551-1558 (Sep 70).
- 3. Kashiwagi, T., "A Radiative Ignition Model of a Solid Fuel," <u>Comb. Sci. Tech.</u>, Vol. 8, pp 225-236 (1974).
- 4. Bradley, H. H., Jr., "A Unified Theory of Solid Propellant Ignition, Part 1, Development of Mathematical Model," NWC TP5618 (Aug 74).
- 5. Kindelan, M., and Williams, F. A., "Radiant Ignition of a Combustible Solid with Gas-Phase Exothermicity," Acta Astronautica, Vol. 2, No. 11/12 (Nov/Dec 75).
- 6. Rivard, W. C., Farmer, O. A., and Butler, T. D., "RICE: A Computer Program for Multicomponent Chemically Reactive Flows at All Speeds," LA-5812, Los Alamos Scientific Laboratory, Los Alamos, NM, Mar 75.
- 7. Kothari, A. P., Anderson, J. D., Jr., and Jones, E., "Navier-Stokes Solutions for Chemical Laser Flows", AIAA J., Vol. 15, No. 1, pp 92-100 (Jan 77).
- 8. Edelman, R. B., Fortune, O. F., and Weilerstein, G., "An Analytical and Experimental Investigation of Gravity Effects Upon Laminar Gas Jet-Diffusion Flames", 14th Symposium (International) on Combustion, Aug 72, Penn State University, pp 399-412.
- 9. Merzhanov, A. G., and Averson, A. E., "The Present State of the Thermal Ignition Theory: An Invited Review," <u>Comb. Flame</u>, Vol. 16, pp 89-124 (1971).
- 10. Bradley, H. H. Jr., "Theory of Ignition of a Reactive Solid by Constant Energy Flux," Comb. Sci. Tech., Vol. 2, pp 11-20 (1970).
- 11. Bradley, H. H. Jr., and Williams, F. A., "Theory of Radiant and Hypergolic Ignition of Solid Propellants", <u>Comb. Sci. Tech.</u>, Vol. 2, pp 41-52 (1970).

APPENDIX A

Ignition Results for Parametric Study

This appendix contains the numerical results obtained near the critical ignition point for each case considered in the parametric study (for the Standard Case, see Fig. 14, page 31). Each of the figures to follow pertains to a single case and displays multiple curves of gas temperature adjacent to the heated wall (z=0) as a function of time; the only parameter varied is the cut-off time, t_{mq} , of the external heat flux. The constant portion of the external heat flux, $q_{wall}(t)$, is held constant at 10 cal/cm²-sec. The value of t_{mq} which yields the longest hang-fire is taken as the "time to ignition" and was recorded in Table 2 on page 20.

Case	Ê* kcal mole	z* sec ⁻¹	ΔΗ [*] (exothermic) <u>kcal</u> mole
Std.	35	10 ¹³	35
CV 1	35	10 ¹²	35
CV 2	35	10 ¹²	25
CV 3	35	10 ¹²	30
CV 4	35	10 ¹³	30
CV 5 .	35	10 ¹⁴	30
CV 6	30	10 ¹²	30
CV 7	30	10 ¹³	30

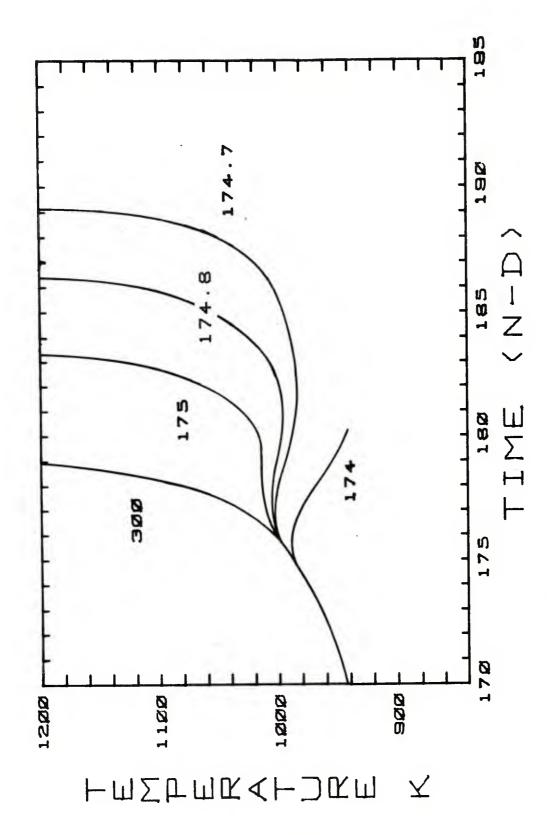


Figure A-1 Temperature-Time History at Heated Wall (Varying t $_{\rm mq}$

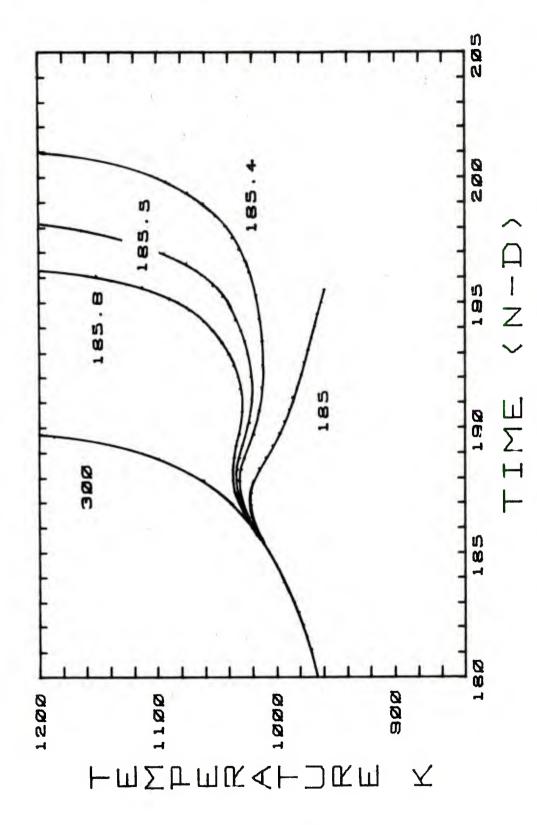


Figure A-2 Temperature-Time History at Heated Wall (Varying t $_{\rm mq}$

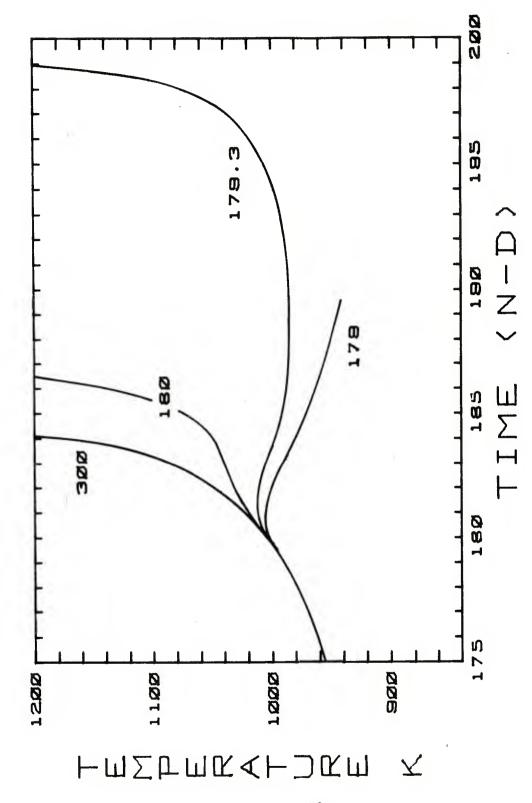


Figure A-3 Temperature-Time History at Heated Wall (Varying t $_{\rm mq}$

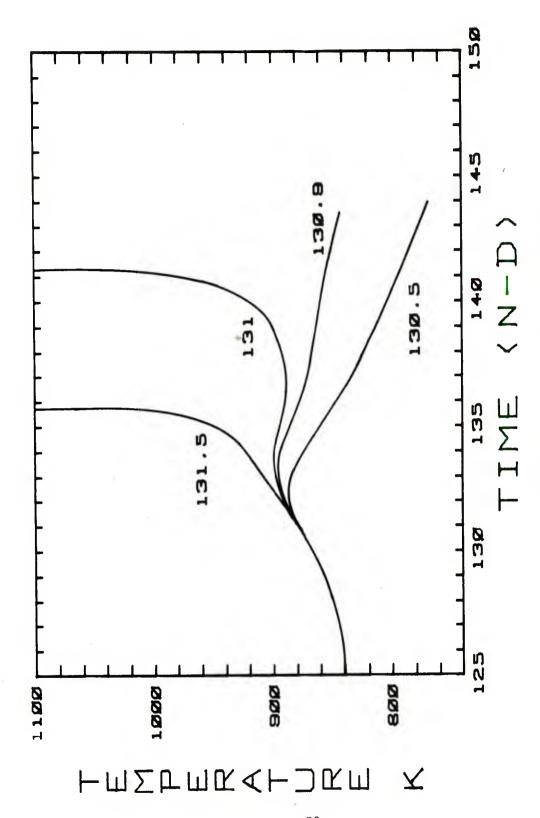


Figure A-4 Temperature-Time History at Heated Wall (Varying t_{mq})

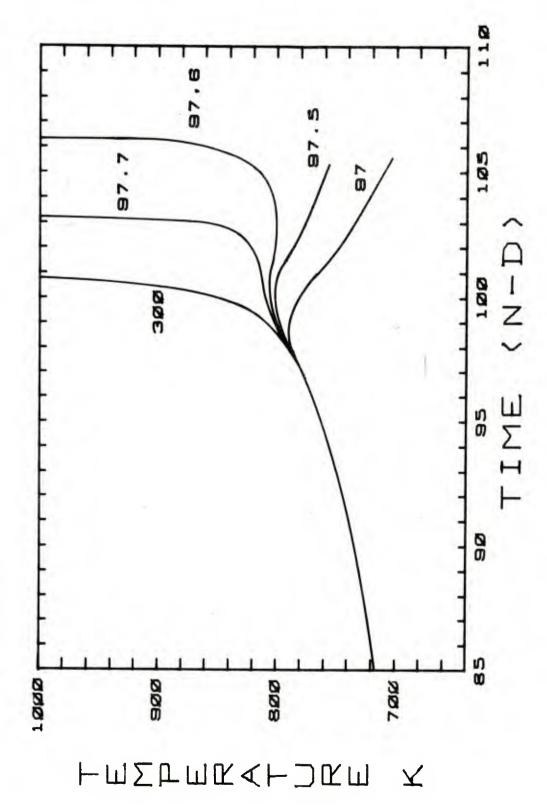


Figure A-5 Temperature-Time History at Heated Wall (Varying t $_{\rm mq}$

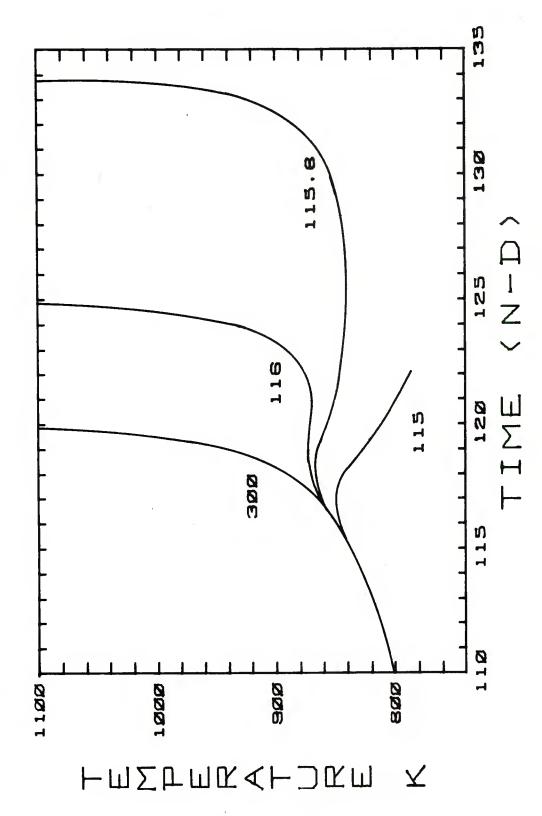
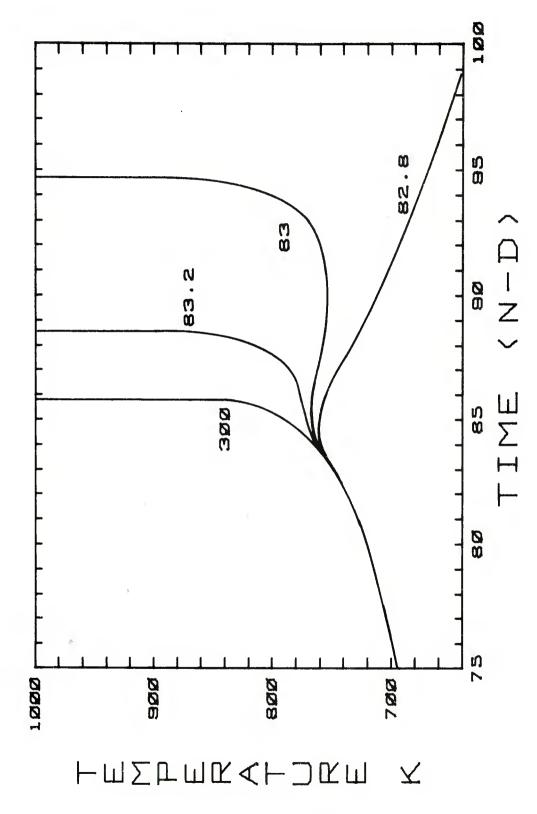


Figure A-6 Temperature-Time History at Heated Wall (Varying t $_{\rm mq}$



Temperature-Time History at Heated Wall (Varying t mq' for Case CV 7 Figure A-7

APPENDIX B

Ignition Results for Variable External Heat Flux

This appendix contains the numerical results obtained near the critical ignition point for the study of ignition time dependence on external heat flux level. All of the figures to follow are based on the set of parameters denoted as the Standard Case. Each figure corresponds to a particular value for the constant portion of the external heat flux, $q_{\rm wall}(t)$ (see Fig. 3, page 16). The value of this constant portion is varied over the range 10-25 cal/cm²-sec. Similar to Appendix A, the results are displayed as multiple curves of gas temperature adjacent to the heated wall (z=0) as a function of time; the only parameter varied is the cut-off time, $t_{\rm mq}$, of the external heat flux. The value of $t_{\rm mq}$ which yields the longest hang-fire is taken as the "time to ignition" and was used to obtain the correlation,

$$t_{mq} \propto q_{wall} -1.89$$

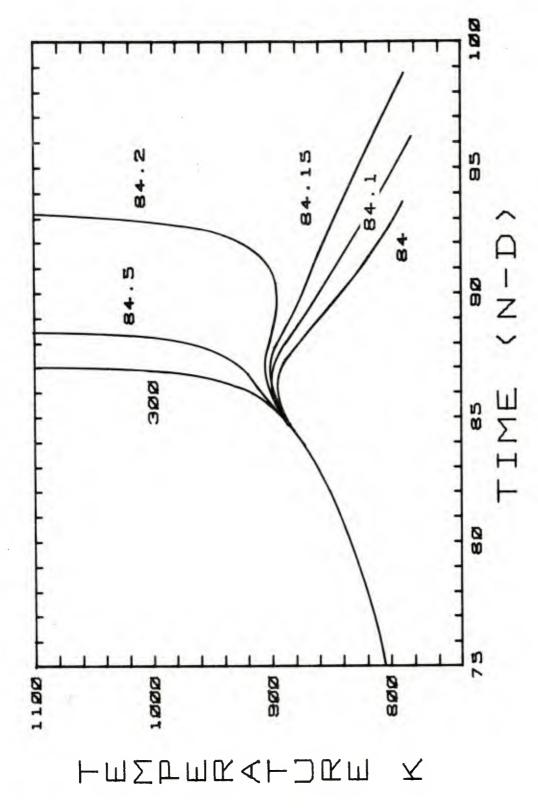


Figure B-1 Temperature-Time History at Heafed Wall (Varying t properties of for $q_{\rm Wall_o} = 12.5~{\rm cal/cm}^2$ -sec

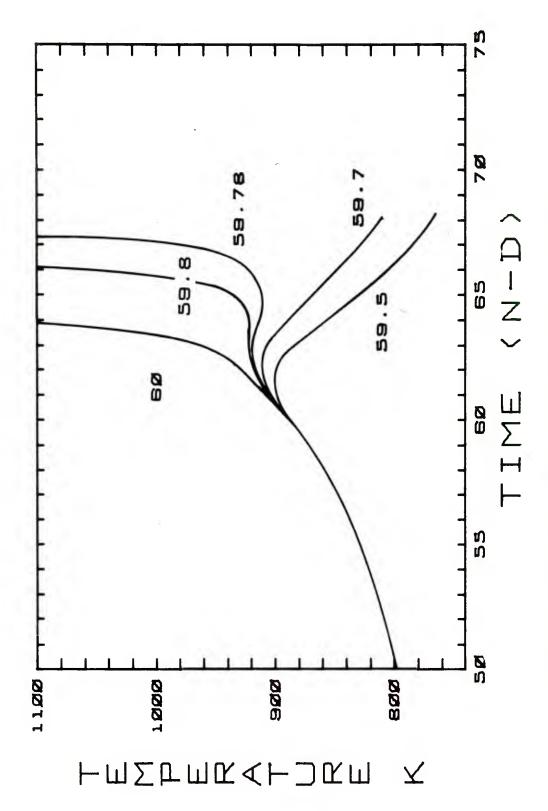


Figure B-2 Temperature-Time History at Heated Wall (Varying t propertion for $q_{wall} = 15.0 \text{ cal/cm}^2$ -sec

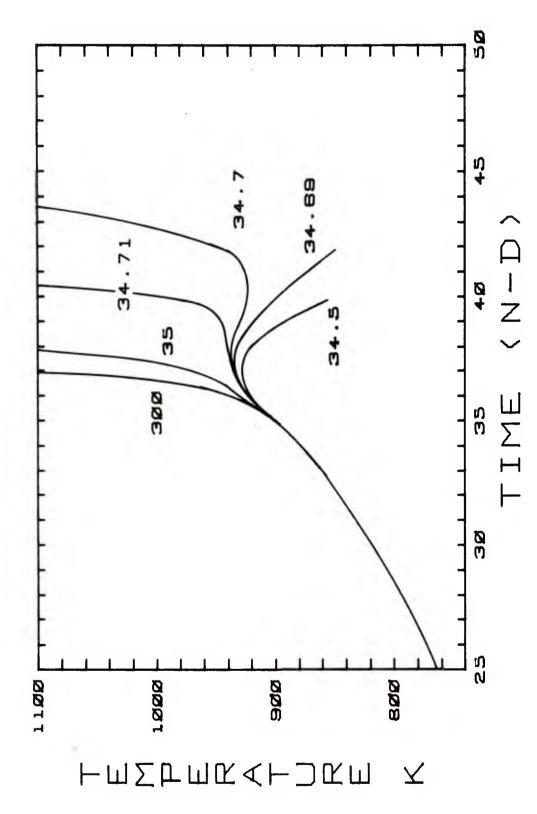


Figure B-3 Temperature-Time History at Heafed Wall (Varying t por qwall $_{\rm mq}$ = 20.0 cal/cm -sec

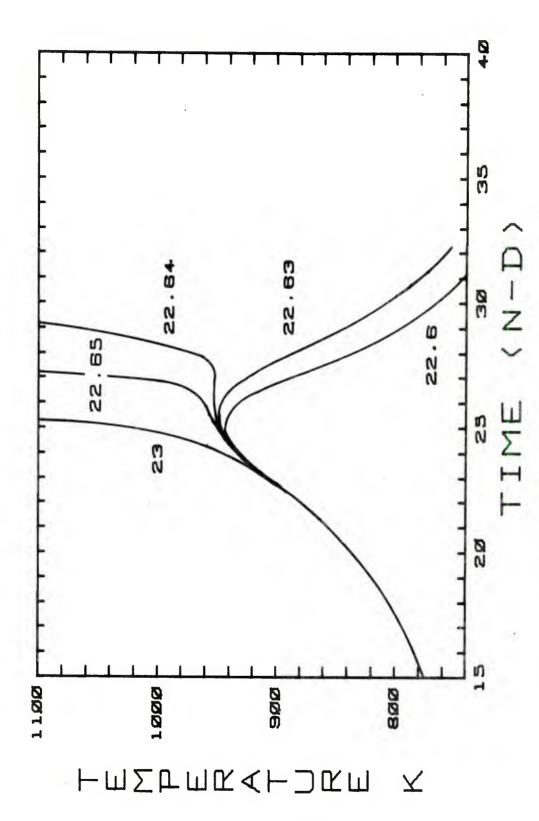


Figure B-4 Temperature-Time History at Heated Wall (Varying t properties for $q_{\rm u,a}$) for $q_{\rm u,a}$, $q_{\rm c}$ = 25.0 cal/cm -sec for qwall =

No. of No. of Copies Organization Copies Organization 12 Commander 1 Commander Defense Documentation Center US Army Missile Research and ATTN: DCC-TCA Development Command Cameron Station ATTN: DRDMI-R Alexandria, VA 22314 Redstone Arsenal, AL 35809 1 Director 1 Commander Defense Advanced Research Pro-US Army Tank Automotive Developjects Agency ment Command ATTN: C. R. Lehner ATTN: DRDTA-RWL 1400 Wilson Boulevard Warren, MI 48090 Arlington, VA 22209 2 Commander 2 Director US Army Mobility Equipment Re-Institute for Defense Analyses search & Development Command ATTN: Dr. H. Wolfhard Tech Doc Ctr, Bldg 315 R. T. Oliver DRSME-RZT 400 Army-Navy Drive Ft. Belvoir, VA 22060 Arlington, VA 22202 1 Commander 1 Commander US Army Armament Materiel Readi-US Army Materiel Development ness Command and Readiness Command ATTN: DRSAR-LEP-L, Tech Lib ATTN: DRCDMA-ST Rock Island, IL 61299 5001 Eisenhower Avenue Alexandria, VA 22333 4 Commander US Army Armament Research and 1 Commander Development Command US Army Aviation Research and ATTN: C. Lenchitz Development Command J. Lannon ATTN: DRSAV-E D. Downs 12th and Spruce Streets H. Fair St. Louis, MO 63166 Dover, NJ 07801 1 Director 1 Commander US Army Air Mobility Research US Army White Sands Missile and Development Laboratory Range Ames Research Center ATTN: STEWS-VT Moffett Field, CA 94035 WSMR, NM 88002 1 Commander 1 Commander US Army Electronics Command US Army Watervliet Arsenal ATTN: DRSEL-RD ATTN: R. Thierry/Code SARWV-RD Ft. Monmouth, NJ 07703 Watervliet, NY 12189

No. Copi		lo. Copi	
1	Commander US Army Materials and Mechanics Research Center ATTN: DRXMR-ATL Watertown, MA 02172	1	Commander US Naval Surface Weapons Center ATTN: Library Br, DX-21 Dahlgren, VA 22448
1	Commander US Army Natick Research and Development Command ATTN: DRXRE, Dr. D. Sieling Natick, MA 01762	1	Commander US Naval Underwater Systems Center Energy Conversion Department ATTN: R. S. Lazar/Code 5B331 Newport, RI 02840
1	Director US Army TRADOC Systems Analysis Activity ATTN: ATAA-SL, Tech Lib WSMR, NM 88002	2	Commander US Naval Weapons Center ATTN: Dr. R. Derr Mr. H. Bradley China Lake, CA 93555
1	Commander US Army Research Office ATTN: Tech Lib P.O. Box 12211 Rsch Triangle Park, NC 27706		Commander US Naval Research Laboratory ATTN: Code 6180 Washington, DC 20375
1	Chief of Naval Research ATTN: Code 473 800 N. Quincy Street Arlington, VA 22217	3	Superintendent US Naval Postgraduate School ATTN: Tech Lib Dr. David Netzer Dr. Allen Fuhs Monterey, CA 93940
1	Commander US Naval Sea Systems Cmd ATTN: J. W. Murrin (NAVSEA-033 National Center Bldg 2, Rm 6E08 Washington, DC 20360		Commander US Naval Ordnance Station ATTN: S. E. Mitchell C. B. Dale Tech Lib Indian Head, MD 20640
2	Commander US Naval Surface Weapons Ctr White Oak Laboratory ATTN: S. J. Jacobs R. R. Bernecker, R13 Silver Spring, MD 20910	2	AFOSR ATTN: J. F. Masi Dr. B. T. Wolfson Bolling AFB, DC 20332

No.	of	No.	of
Copie	es <u>Organization</u>	Copie	organization 0rganization
	AFRPL (DYSC) ATTN: Dr. D. George Mr. J. N. Levine Edwards AFB, CA 93523	1	General Electric Company Armament Department ATTN: M. J. Bulman Lakeside Avenue Burlington, VT 05402
1	Lockheed Palo Alto Rsch Labs ATTN: Tech Info Ctr 3251 Hanover Street Palo Alto, CA 94304	1	General Electric Company Flight Propulsion Division ATTN: Tech Lib Cincinnati, OH 45215
1	Aerojet Solid Propulsion Co. ATTN: Dr. P. Micheli Sacramento, CA 95813	1	Paul Gough Associates, Inc. ATTN: Dr. P. S. Gough P.O. Box 1614
1	ARO Incorporated ATTN: Mr. N. Dougherty Arnold AFS, TN 37389	2	Portsmouth, NH 03801 Hercules Incorporated Alleghany Ballistic Lab
1	Atlantic Research Corporation ATTN: Dr. M. K. King 5390 Cherokee Avenue Alexandria, VA 22314	2	ATTN: Dr. R. Miller Tech Lib Cumberland, MD 21501 Hercules Incorporated
1	AVCO Corporation AVCO Everett Research Lab Div ATTN: D. Stickler 2385 Revere Beach Parkway Everett, MA 02149		Bacchus Works ATTN: Dr. D. Pilcher Dr. R. Simmons Magna, UT 84044
2	Calspan Corporation ATTN: Dr. E. B. Fisher A. P. Trippe P.O. Box 235	1	ATTN: Dr. M. J. Klein 10 West 35th Street Chicago, IL 60615
1	ENKI Corporation ATTN: M. I. Madison 9015 Fulbright Avenue	1	Olin Corporation Badger Army Ammunition Plant ATTN: J. Ramnarace Baraboo, WI 53913
1	Chatsworth, CA 91311 Foster Miller Associates, Inc ATTN: A. J. Erickson 135 Second Avenue Waltham, MA 02154	2	Olin Corporation New Haven Plant ATTN: R. L. Cook D. W. Riefler 275 Winchester Avenue New Haven, CT 06504

No. of Copies	Organization	No. of	
2	Physics International Company 2700 Merced Street Leandro, CA 94577	2	Thiokol Corporation Wasatch Division ATTN: Dr. John Peterson Tech Lib
<i>I</i> 8	Pulsepower Systems, Inc. ATTN: L. C. Elmore B15 American Street		P. O. Box 524 Brigham City, UT 84302
	San Carlos, CA 94070	1	TRW Systems Group ATTN: Dr. H. Korman
I	Rockwell International Corp Rocketdyne Division ATTN: Dr. C. Obert		One Space Park Redondo Beach, CA 90278
	Dr. J. E. Flanagan 6633 Canoga Avenue Canoga Park, CA 91304	2	United Technology Center ATTN: Dr. R. Brown Tech Lib P. O. Box 358
	Rockwell International Corp Rocketdyne Division		Sunnyvale, CA 94088
,	ATTN: Mr. W. Haymes Tech Lib McGregor, TX 76657	1	Universal Propulsion Co ATTN: H. J. McSpadden P. O. Box 546
1 :	Science Applications, Inc.		Riverside, CA 92502
	ATTN: Dr. R. B. Edelman 23146 Cumorah Crest Woodland Hills, CA 91364	1	Battelle Memorial Institute ATTN: Tech Lib 505 King Avenue Columbus, OH 43201
	Shock Hydrodynamics, Inc. ATTN: Dr. W. H. Anderson 4710-16 Vineland Avenue North Hollywood, CA 91602	1	Brigham Young University Dept of Chemical Engineering ATTN: Dr. M. Beckstead Provo, UT 84601
	Thiokol Corporation Elkton Division ATTN: E. Sutton Elkton, MD 21921	1	California Institute of Tech ATTN: Prof. F. E. C. Culick 204 Karman Lab, Mail Stop 301-46 1201 E. California Street
	Thiokol Corporation Huntsville Division		Pasadena, CA 91125
	ATTN: Dr. D. Flanigan Dr. R. Glick Tech Lib	1	Case Western Reserve Univ Division of Aerospace Sciences ATTN: Prof. J. Tien
	Huntsville, AL 35807		Cleveland, OH 44135

No. (No.	

3	Georgia Institute of Technolog School of Aerospace Engineerin ATTN: Prof. B. T. Zinn Prof. E. Price Prof. W. C. Strahle Atlanta, GA 30332		Rutgers State University Dept of Mechanical and Aero- space Engineering ATTN: Prof. S. Temkin University Heights Campus New Brunswick, NJ 08903
1	Johns Hopkins University Applied Physics Laboratory Chemical Propulsion Informatio Agency ATTN: Mr. T. Christian Johns Hopkins Road Laurel, MD 20810	on	Southwest Research Institute Fire Research Section ATTN: W. H. McLain P.O. Drawer 28510 San Antonio, TX 78228 Stanford Research Institute
	nadici, in 20010		Propulsion Sciences Division
1	Massachusetts Institute of Technology Dept of Mechanical Engineering	5	ATTN: Tech Lib 333 Ravenswood Avenue Menlo Park, CA 94024
	ATTN: Prof. T. Toong Cambridge, MA 02139	1	Stevens Institute of Technology Davidson Laboratory
1	Pennsylvania State University Dept of Mechanical Engineering ATTN: Prof. K. Kuo		ATTN: Prof. R. McAlevy III Hoboken, NJ 07030
	University Park, PA 16801	T	University of California San Diego
3	Princeton University		AMES Department
	Forrestal Campus Library ATTN: Prof. M. Summerfield		ATTN: Prof. F. Williams
	Dr. L. Caveny Tech Lib		P.O. Box 109 La Jolla, CA 92037
	P.O. Box 710	1	University of Illinois
	Princeton, NJ 08540		Dept. of Aeronautical Engineering ATTN: Prof. H. Krier
2	Purdue University School of Mechanical Engineeri ATTN: Prof. J. Osborn	.ng	Transportation Bldg, Rm 105 Urbana, IL 61801
	Prof. J. D. Hoffman TSPC Chaffee Hall West Lafayette, IN 47906	1	University of Minnesota Dept. of Mechanical Engineering ATTN: Prof. E. Fletcher Minneapolis, MN 55455

No. of Copies Organization

Aberdeen Proving Ground

Marine Corps LnO Dir, AMSAA