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DEFENCE RESEARCH ESTABLISHMENT SUFFIELD RALSTON ALBERTA

SUFFIELD TECHNICAL PAPER NO. 447

NUMERICAL SIMULATION OF THE AIR BLAST RESPONSE

OF TAPERED CANTILEVER BEAMS (U)

by

G.V. Price

ABSTRACT

A numerical procedure is developed to predict the elastic response of variable cross-section cantilever beams when subjected to a transient air blast load. Computed natural frequencies and transient strains were in reasonable agreement with experimentally obtained values.

(U)

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by

G.V. Price

1. Introduction

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The Defence Research Establishment Suffield (DRES), in support of Canadian Forces (Maritime) requirements, is conducting a series of tests to determine the ability of certain antenna designs to withstand blast overpressures of various intensities. Two of the antennas to be evaluated are a 35 ft fibreglass Whip Antenna and a 23 ft UHF Polemast Antenna. The objective of this study is to develop a numerical procedure to predict the time response of antennas of the above type when subjected to a transient air blast load.

The numerical procedure begins with the Bernculli-Euler equation for a tapered cantilever beam subjected to a transient distributed force. This equation is based on linear elastic theory and assumes small beam deflections [1]. The normal modes and natural frequencies of the beam are determined by solving the difference equations for free vibration using successive relaxation, Rayleigh quotient and Gram-Schmidt orthogonalization numerical techniques [2,3]. The forced vibration solution is determined using normal mode coordinates and Laplace transforms [4]. In this calculation,

the transient air blast load is computed using the classical gas dynamics equations describing air shock waves [5,6,7] and recent empirical drag loading relations developed at DRES [8,9].

The Bernoulli-Euler equation for a vibrating beam of length L may be written in the form [1]

$$\rho A \frac{\partial^2 y}{\partial t^2} + \frac{\partial^2}{\partial x^2} \left(EI \frac{\partial^2 y}{\partial x^2} \right) = w, \ 0 \le x \le 1,$$
(1)

where x is distance from the base of the beam, t is time, y(x,t) is the beam deflection in the transverse direction, ρ is the beam density, A(x) is the beam cross-sectional area, E is Young's modulus for the beam material, I(x)is the second moment of the cross-sectional area with respect to the neutral axis, and w(x,t) is the load per unit length on the beam in the transverse direction. The discussion which follows considers a numerical solution to the above equation at N prescribed points

$$x_i = i \Delta x, \Delta x = LN^{-1}, i = 1, ..., N,$$
 (2)

subject to specified initial conditions and boundary conditions.

2. Free Vibration of a Tapered Cantilever Beam

The normal modes and natural frequencies are obtained by solving equation (1) with w=0. Assuming a sinusoidal time response, the free vibration solution may be written in the form

$$y(x,t) = Y^{(r)}(x)e^{i\omega}r^{t}$$
, (3)

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where ω_r is the r'th circular frequency of the time response, $Y^{(r)}(x)$ is the normal mode corresponding to ω_r , and i is $\sqrt{-1}$. With the results (2) and (3), equation (1) with w=0 reduces to the form

$$\rho A_{i} \omega_{r}^{2} \gamma_{i}^{(r)} = \frac{d^{2}}{dx^{2}} \left(E I_{i} \frac{d^{2}}{dx^{2}} \gamma_{i}^{(r)} \right)$$
(4)

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at point x_i . Expanding the derivative in (4) using central finite differences, the difference equation for free vibration becomes

$$I_{i-1} Y_{i-2}^{(r)} - 2(I_{i-1} + I_i)Y_{i-1}^{(r)} + (I_{i-1} + 4I_i + I_{i+1} - \rho A_i \omega_r^2 \Delta x^4 E^{-1})Y_i^{(r)}$$
(5)

$$-2(I_{i} + I_{i+1})Y_{i+1}^{(r)} + I_{i+1}Y_{i+2}^{(r)} = 0, \quad i = 1, 2, \dots, N.$$

The four unknowns $Y_{-1}^{(r)}$, $Y_{0}^{(r)}$, $Y_{N+1}^{(r)}$ and $Y_{N+2}^{(r)}$ are eliminated from this system of equations through the application of boundary conditions. Several possibilities are considered below.

(a) clamped at x = 0, zero displacement and slope:

y(0) = 0	3	$Y_0^{(r)} = 0;$		(6)
$\frac{\partial x}{\partial A}\Big _{0} = 0$,	$Y_{-1}^{(r)} = Y_{1}^{(r)}.$)	(0)

(b) free at x = L, zero moment and shear:

$$\frac{\partial^{2} y}{\partial x^{2}}\Big|_{L} = 0 , \qquad Y_{N+1}^{(r)} = 2Y_{N}^{(r)} - Y_{N-1}^{(r)} ;$$

$$\frac{\partial^{3} y}{\partial x^{3}}\Big|_{L} = 0 , \qquad Y_{N+2}^{(r)} = 4Y_{N}^{(r)} - 4Y_{N-1}^{(r)} + Y_{N-2}^{(r)} .$$
(7)

(c) pinned at x = 0 and $x = I\Delta x$, zero displacement and moment at x = 0, and zero displacement at $x = I\Delta x$:

$$y(0) = \frac{\partial^2 y}{\partial x^2} \bigg|_{0}^{2} = 0, \quad Y_{0}^{(r)} = 0, \quad Y_{-1}^{(r)} = -Y_{1}^{(r)};$$

$$y(I_{0}x) = 0, \quad Y_{I}^{(r)} = 0.$$
(8)

With a suitable combination of the boundary conditions (6) to (8), equation (5) becomes an eigenvalue problem for an n-rowed square matrix. In matrix form, the eigenvalue problem may be written in the form

$$\omega_{\mathbf{r}}^{2} \beta_{\mathbf{v}}^{\mathbf{r}}(\mathbf{r}) = \alpha_{\mathbf{v}}^{\mathbf{r}}(\mathbf{r}) , \qquad (9)$$

where α is a five-diagonal matrix which depends on the coefficients I_i , i=1,...N, and β is a diagonal matrix for which the i'th diagonal element is the value $\rho A_i \Delta x^4 E^{-1}$. If the frequencies ω_r are all distinct, it may be readily verified that the normal modes are orthogonal with respect to the matrix β , according to

$$\frac{\gamma^{(r)} \beta \gamma^{(s)}}{\delta_{rs}} = \delta_{rs} M_{r}, \qquad (10)$$

$$\delta_{rs} = \begin{cases} 0, r \neq s, \\ 1, r = s. \end{cases}$$

A numerical solution procedure for the eigenvalue problem (9) will now be considered. The procedure begins with an initial guess for the smallest circular frequency a_1 . The corresponding normal mode is obtained by successive relaxation [2,3] according to the iteration equation

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$$Y_{i}^{(1)} = (\omega_{1}^{2} \beta_{11} - \alpha_{11})^{-1} \sum_{j=1}^{N} \alpha_{ij} Y_{j}^{(1)}.$$
(11)
n+1 guess) $j=1$ (n guess)
 $(j \neq i)$

This iteration is inherently unstable since the system of equations is homogeneous. However, convergence to a stationary $\Upsilon^{(1)}$ is achieved by normalizing $\Upsilon^{(1)}$ after each complete repetition of the iteration. An improved estimate for ω_1 is then obtained by the Rayleigh quotient [2,3] technique.

The complete iteration is repeated until a stationary value for the circular frequency ω_1 is obtained, at which point the corresponding normal mode, in normalized form, will be $Y^{(1)}$.

Higher natural frequencies ω_r and normal modes $Y^{(r)}$ are obtained using the above procedure with but one modification: between repetitions of the successive relaxation iteration (equation 11), the latest guess $Y_j^{(r)*}$ is modified to extract any component in the direction of previously evaluated normal modes $Y_j^{(s)}$, s<r. This operation is termed Gram-Schmidt orthogonalization [2,3], and is based on the orthogonality property (10).

$$\frac{\gamma(r)}{(\text{new guess})} = \frac{\gamma(r)}{s=1} \frac{r-1}{\gamma(s)} \left\{ \frac{\langle \gamma(r), \gamma(s) \rangle}{\langle \gamma(s), \gamma(s) \rangle} \right\}.$$
(13)

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In this equation, the inner product, denoted $\langle u, v \rangle$ for two arbitrary vectors u and v, is weighted with respect to the matrix β according to

$$\langle u, v \rangle = u^{T} \beta v$$
, (14)

where superscript I denotes the transpose of the indicated vector. A computer program which determines the natural frequencies and normal modes according to the techniques described above is given in the Appendix.

3. Forced Vibration of a Tapered Cantilever Beam

The forced vibration solution begins with an expansion of the displacement vector y in terms of normal mode coordinates n, according to

$$y = \sum_{r=1}^{N} n_r y(r) , \qquad (15)$$

or

y = Φη,

where ϕ is a matrix formed by the normal modes.

$$\Phi = \begin{pmatrix} Y_1^{(1)} & \dots & Y_1^{(N)} \\ \vdots & \vdots \vdots & \vdots \\ Y_1^{(1)} & & Y_1^{(N)} \end{pmatrix} ...$$
(16)

Using the general techniques outlined in [4], substituting (15) into (1) and pre-multiplying the resulting equation by ϕ^{T} , the governing equation becomes

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$$\Phi^{\mathsf{T}}_{\beta}\Phi_{\eta}^{\mu} + \Phi^{\mathsf{T}}_{\alpha}\Phi_{\eta} = \Phi^{\mathsf{T}}_{\psi}, \qquad (17)$$

where " denotes the time derivative d^2/dt^2 . The r'th equation in the system of equations (17) is

$$\underline{\gamma}^{(r)}{}^{T}{}_{\beta}\underline{\gamma}^{(r)}{}^{T}{}_{n}{}_{r} + \underline{\gamma}^{(r)}{}^{T}{}_{\alpha}\underline{\gamma}^{(r)}{}_{n}{}_{r} = \underline{\gamma}^{(r)}{}^{T}\underline{\psi} . \qquad (18)$$

Since the normal modes satisfy equations (9) and (10), the above result simplifies to the form

$$\ddot{\eta}_{r} + \omega_{r}^{2} \eta_{r} = \frac{\underline{\gamma}^{(r)^{T}} \underline{w}(t)}{\underline{M}_{r}} .$$
 (19)

The normal mode coordinates n_r , $r \approx 1, ... N$ are obtained by solving equation (19) using Laplace transforms and the convolution theorem. With specified initial conditions in the form

$$y(x,0) = f(x)$$
,
 $\dot{y}(x,0) = g(x)$, (20)

The solution to equation (19) becomes

$$n_{r}(t) = M_{r}^{-1} \gamma^{(r)} \left(\beta f \cos \omega_{r} t + \beta g \omega_{r} - \sin \omega_{r} t \right) + \frac{\omega_{r}^{-1}}{2} \int_{0}^{t} W(\tau) \sin \omega_{r}(t-\tau) d\tau$$
(21)

The parameter M_r appearing in this equation is evaluated according to equation (10).

$$M_{\gamma} = \underline{\gamma}^{(r)^{T}} \beta \underline{\gamma}^{(r)} . \qquad (22)$$

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Combining the results (21) and (15), the beam displacement at position x_i becomes

$$y_{j}(t) = \sum_{r=1}^{N} Y_{j}^{(r)} M_{r}^{-1} \left\{ \cos \omega_{r} t \left(\sum_{j=1}^{N} Y_{j}^{(r)} \rho A_{j} f_{j} \right) + \omega_{r}^{-1} \sin \omega_{r} t \left(\sum_{j=1}^{N} Y_{j}^{(r)} \rho A_{j} g_{j} \right) + \omega_{r}^{-1} \sin \omega_{r} t \left(\sum_{j=1}^{N} Y_{j}^{(r)} \rho A_{j} g_{j} \right) \right\}$$

$$(23)$$

$$+ \omega_{r}^{-1} \int_{0}^{t} \left\{ \sum_{j=1}^{n} Y_{j}^{(r)} w_{j}(\tau) \right\} \sin \omega_{r} (t-\tau) d\tau \bigg\},$$

$$M_{r} = \sum_{j=1}^{N} Y_{j}^{(r)} \rho A_{j} Y_{j}^{(r)}.$$
(24)

where

The time integral in (23) may be readily evaluated by numerical integration using a time step Δt of specified duration.

A computer program which determines the forced vibration solution according to the techniques described above is given in the Appendix.

4. <u>Transient Drag on Circular Cylinders from Air Blast Waves</u>

The accuracy of the forced vibration solution is strongly dependent on the procedure used to calculate the air blast load on the tapered cantilever beam. The transient air blast load on circular cylinders has been investigated extensively at DRES over the period 1968 to 1975. The discussion which follows is based on the more recent DRES reviews of empirical relations for the prediction of drag loading [8,9] and on the classical gas dynamics equations describing air shock waves [5,6,7].

The air blast load arising from the interaction of a blast wave with a circular cylinder may be expressed in the form

$$F = P^*A + C_D q_I A, \qquad (25)$$

where A is the projected area of the cylinder, P^* is an empirical pressure parameter which accounts for the load on the cylinder over the short period of time during which the blast wave diffracts around and engulfs the cylinder, C_D is an empirical aerodynamic drag coefficient, and q_I is the impact pressure (instantaneous difference between the local stagnation and static pressures).

The following empirical relations have been determined at DRES for the diffraction pressure P* and the drag coefficient C_D [8,9]:

$$P^{*} = \left\{ \begin{array}{c} 1.6 \ t_{T}^{-1} (p_{0} t_{T})^{1.13}, \ 0 \le t \le 5 t_{T}, \\ 0, \ t \ge 5 t_{T}, \end{array} \right\}$$
(26)

$$C_{D} = \left\{ \begin{array}{ccc} 0.7 & , & \underline{M} \ge 0.48, & Re \ge 3x10^{5} \\ 0.6 & , & M < 0.48, & Re \ge 3x10^{5} \\ 1.2 & , & M < 0.48, & Re < 3x10^{5} \end{array} \right\}$$
(27)

In the above equations, p_0 is the peak overpressure of the blast wave, t_T is the transit time required by the blast wave to completely engulf the cylinder, M is the instantaneous Mach number of the flow incident on the cylinder, and Re is the instantaneous Reynolds number of the flow incident on the cylinder.

To complete the transient drag calculation, it remains to evaluate the basic fluid properties of the flow behind the blast wave. The parameters to evaluate include q_I , t_T , M and Re. The evaluation of these parameters requires

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a preliminary evaluation of the temperature T, speed of sound c, static pressure P, dynamic pressure q, fluid particle velocity u, and fluid viscosity v both at the cylinder and immediately behind the shock front. To simplify the presentation, the following notation will be adopted. Variables which apply immediately in front of the shock front will be indicated by a subscript "A", variables which apply immediately behind the shock front will be indicated with a subscript "B", and variables which apply instantaneously at the cylinder itself will have no explicit subscript.



The pressure-time history of the ideal blast wave is most frequently described in terms of the modified Friedlander equation [7],

$$p(t) = p_0(1-t/t_d)e^{-\kappa t/t_d}, \quad 0 \le t \le t_d, \quad (28)$$

where p(t) is the blast wave overpressure, t is the time measured from time of arrival of the blast wave, p_0 is the peak overpressure, t_d is the positive phase duration, and κ is the exponential decay constant. The three parameters p_0 , t_d and κ in this equation make it possible to match the following three experimental characteristics of the real blast wave: p_0 , t_d and I_d , where I_d

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is the positive phase impulse defined by

$$I_{d} = \int_{0}^{t_{d}} p(t) dt . \qquad (29)$$

The region immediately in front of the shock front is assumed to be in an undisturbed state $(u_A=0)$ at a known pressure P_A and temperature T_A . Conditions immediately behind the shock front are determined from the Rankine-Hugoniot and other standard gas dynamics equations describing shock waves in air. Assuming a specific heat ratio $\gamma = 1.4$, and adopting the notation ζ to represent the pressure ratio P_B/P_A across the shock front, the fluid properties immediately behind the shock front may be written in the form

$$P_{B} = P_{A} + P_{0} ,$$

$$T_{B} = T_{A} \zeta (6 + \zeta) (1 + 6\zeta)^{-1} ,$$

$$u_{c} = (1.4 \text{ R } T_{a})^{\frac{1}{2}} (1 + 6P_{0} / (7P_{A}))^{\frac{1}{2}} ,$$
(30)

where R is the gas constant for dry air, and u_s is the speed of the shock front. At the cylinder itself, conditions are determined by assuming isentropic flow in the region behind the shock front.

$$P = P_{A} + p(t) ,$$

$$T = T_{B}(P/P_{B})^{286} ,$$

$$c = (1.4 \text{ RT})^{\frac{1}{2}} ,$$

$$q = 2.5 p_{0}^{2}(p_{0} + 7P_{A})^{-1}(p(t)/P_{0})^{2} ,$$

$$\rho = P(RT)^{-1} ,$$

$$u = (2q/\rho)^{-\frac{1}{2}} .$$
(31)

11.

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With the basic fluid properties known behind the shock front and at the cylinder, it is possible to evaluate the four parameters q_I , t_T , M and Re appearing in the drag equations (25) to (27).

$$M = u c^{-1},$$

$$Re = u D v^{-1},$$

$$t_{T} = D u_{s}^{-1},$$

$$q_{T} = q + .175 PM^{4} + .0175 PM^{6},$$
(32)

where the kinematic viscosity v is a known function of T and P (refer to [10] and [11] for considerations in this regard).

A computer program which determines the air blast load on circular cylinders according to the techniques described above is given in the Appendix.

Numerical Predictions and Comparison with Experiments

The numerical simulation model developed above was used to predict the time response of a 35 ft fibreglass Whip Antenna and a 23 ft UHF Polemast Antenna when subjected to a nominal 7.0 psi peak overpressure blast loading. The two antennas were subsequently exposed to air blast loading in Event Dice Throw, a 620 ton AN/FO free-field blast trial conducted by the United States Defense Nuclear Agency at the Shite Sands Missile Range in New Mexico on October 6, 1976, and strain data were recorded for five pairs of strain gauges measuring bending strain on each antenna. The theoretical predictions and experimental results for the Whip and Polemast Antennas have been examined in detail in references [12] and [13]. The brief discussion which follows considers only representative items from the detailed reports.

The structures of the antennas were represented in the computer model

in such a way as to simulate the mass and projected (normal to blast direction) cross-sectional area profiles of the prototype antennas. Photographs of the two antennas installed at the nominal 7.0 psi peak overpressure location for Event Dice Throw are shown in Figures 1 and 2. The physical features which describe the corresponding computer simulation of the antennas are outlined in Tables 1 and 2. It should be noted that the computer simulations of the antennas of the antennas agree with the actual structures in the following critical areas: weight distribution, total weight, projected (normal to blast direction) cross-sectional area distribution, and total projected cross-sectional area.

Prior to the blast trial, a static load was applied near the top of each antenna using an anchored steel cable at a pull angle of 30° to the horizontal. The load was subsequently released electrically ("Twang Test", see [12,13]) and the strain data for free vibration were recorded. A Fourier analysis was performed for the experimental strain data to determine the natural frequencies of the antennas. A comparison of theoretical (numerical simulation) and experimental ("Twang Test") natural frequencies for the two antennas is presented in Table 3. It is apparent from this comparison that the predicted frequencies are in good agreement with the values obtained experimentally.

A comparison of theoretical (numerical simulation) and experimental (blast trial) bending strain histories is presented in Figures 3 and 4. The theoretical predictions were generated using a Friedlander overpressure wave (Figure 5) which corresponds to the Defense Nuclear Agency (DNA) pre-trial predictions for peak overpressure (7.0 psi), positive duration (242 msec) and positive phase impulse (600 psi-msec). The free-field overpressures at the base of the antennas were measured with four strain-type pressure transducers.

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The Friedlander overpressure wave which corresponds to the average experimental peak overpressure (6.6 psi), positive duration (251 msec), and positive phase impulse (705 psi-msec) is shown in Figure 5 for comparison purposes.

It is apparent from Figure 3 that the Whip Antenna bending strain predictions are generally much larger than the corresponding experimental strains (the differences are within experimental error bands, considering pressure transducer errors, drag coefficient errors, material uncertainties, etc.). The average ratio of peak theoretical to experimental bending strain from all five Whip Antenna gauge pairs is 1.65 (Table 4). This may be compared to the results in Figure 4 for the Polemast Antenna in which there is excellent agreement between the theoretical and experimental strains. The average ratio of peak theoretical to experimental bending strain from all five Polemast Antenna gauge pairs is 1.19 (Table 4). A considerably more detailed evaluation of the above two antenna experiments may be found in references [12] and [13].

6. <u>Conclusions</u>

A numerical procedure was developed to predict the elastic response of variable cross-section cantilever beams when subjected to a transient air blast load. The numerical model was used to predict the time response of a 35 ft fibreglass Whip Antenna and a 23 ft UHF Polemast Antenna when subjected to a nominal 7.0 psi peak overpressure blast loading. The computed natural frequencies and transient strains were in reasonable agreement with values obtained experimentally in Event Dice Throw. A more detailed evaluation of the above two antenna experiments may be found in references [12] and [13].

14.

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x (in)	ID ¹ (in)	OD ^I (in)	OD ² (in)
0.004	4.400	6.500	6.500 ³
41.85	4.288	5.942	5.942
83.70	4.002	4.878	4.878
125.55	3.665	4.459	4.459
167.40	3.403	4.154	4.154
209.25	3.056	3.935	3.935
251.10	2.707	3.241	3.241
292.95	2.298	2.63	2.638
334.80	1.957	2.257	2.257
376.65	1.695	2.030	2.030
418.504	1.500	1.900 ³	1.900 ³

¹ This profile establishes the mass distribution.

² This profile establishes the projected (normal to blast direction) cross-sectional area distribution.

³ Extrapolated value based on data supplied by the manufacturer.

Boundary conditions: clamped at x=0 in, free at x=418.50 in.

Ε 3.9x10⁶ psi z. 0.002298 slugs/in³ = ٥ ΔX = 41.85 in N = 10 418.5 in (34.88 ft) = L PA = 12.58 psi 54.0°F = TA = 7.0 psi po. = 242 msec t_d Id Ŧ 600 psi-msec (κ =1.137, computed)

 $\Delta t = 1.00 \text{ msec}$

The time response is formed using only the lowest 3 natural frequencies and corresponding normal modes.

TABLE 1:Numerical model simulation of a 35 ft fibreglass Whip Antenna.All symbols are defined in the text. The antenna outside
diameter (OD) and inside diameter (ID) data were interpolated
from data supplied by the manufacturer. The air blast predictions
were provided by the United States Defense Nuclear Agency.

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x (in)	ID ¹ (in)	OD ¹ (in)	OD ² (in)
0 ³ 36 ⁹ 72 108 144 180 216 252 288 ³	8.978 8.978 8.978 7.950 8.978 8.600 8.600 8.290 8.290	9.500 9.500 9.500 9.500 9.500 9.500 9.500 9.500 9.500	9.500 9.500 9.500 17.220 9.500 13.360 13.360 13.360 10.080 10.080

This profile is calculated to establish the correct mass distribution, assuming a fixed OD equal to that of the seamless extruded aluminum tubing which constitutes the primary structural portion of the antenna.

This profile is calculated to establish the correct projected (normal to blast direction) cross-sectional area distribution.

Boundary conditions: pin at x=0 in, pin at x=36 in, free at x=288 in.

E 10x10⁶ psi = 0.003044 slugs/in³ ρ ÷ Δx = 36.0 in N Ŧ 8 Ξ L 288.0 in (24.0 ft) PA = 12.58 psi 54.0°F TA Ξ = 7.0 psi Po Ξ 242 msec td I_d z. 600 psi-msec (κ =1.137, computed)

 $\Delta t = 1.00 \text{ msec}$

1

2

The time response is formed using only the lowest 3 natural frequencies and corresponding normal modes.

TABLE 2: Numerical model simulation of a UHF Polemast Antenna. All symbols are defined in the text. The structural datawere obtained from drawings supplied by DMCS-6 (modifications as noted in [13]). The air blast predictions were provided by the United States Defense Nuclear Agency.

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Mada	Whip Frequ	uencies (cps)	Polemast Freque	encies (cps)
mode	Theoretical	Experimental	Theoretical	Experimental
1	1.47	1.27	4.62	4.00
2	4.09	4.20	25.5	24.1
3	9.55	9.50	72.4	

¹ This value represents an average of indistinct frequencies which appear in a band over the range 19.7 to 32.1 cps.

<u>TABLE 3</u>: A comparison of theoretical (numerical simulation) and experimental (Twang Test) natural frequencies for a 35 ft fibreglass Whip Antenna and a 23 ft UHF Polemast Antenna.

		Pe	sak Bending Str	ains (uin/in)			
Gauge		Whip Antenna		Pole	mast Anterna		
	Theoretical	Experimental	Theo./Exp.	Theoretical	Experimental	Theo./Exp.	·
-	2050	2009	1.02	208	132	1.58	
2	3443	2381	1.45	1248	973	1.28	
ę	3112	1335	2.33	2414	2010	1.20	
4	3578	2376	1.51	2008	1917	1.05	
Ϋ́	7171	3713	1.93	774	927	0.83	
			Avg. <u>1.65</u>			Avg.1.19	

rimental bending strains (first cycle o	
etical and exper	tennas.
the peak theor	and Polemast An
Comparison of	for the Whip
3LE 4:	



FIGURE 1: Photograph of the 35 ft fibreglass Whip Antenna installed at the nominal 7.0 psi location in Event Dice Throw.

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FIGURE 2: Photograph of the 23 ft UHF Polemast antenna installed at the nominal 7.0 psi location in Event Dice throw.

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FIGURE 4: Comparison of the Polemast Antenna bending strain predictions (dashed lines) against the measured strains (solid lines). The five gauge pairs are respectively located at distances 0.25, 1.5, 3.25, 4.5 and 12.0 ft from the base of the antenna.



APPENDIX A

COMPUTER PROGRAM FOR THE NUMERICAL SIMULATION MODEL.

Based on the numerical procedures described in Sections 2, 3 and 4, a computer program was prepared to determine the natural frequencies, normal modes and air blast transient response of a tapered cantilever beam. A listing of the computer program is presented in this appendix, together with a description of the initialization procedures.

(a) Free Vibration

The computer program for free vibration consists of a main program and two subroutines, referred to as "ESOR" and "ANORM". The major portion of the computation for the natural frequencies and normal modes is carried out in subroutine ESOR. On completion of the calculation, the program displays the relevant frequencies and modes, and stores the information in a disk file for future use in the forced vibration calculations. The card input data for the free vibration calculation is outlined below, and a listing of the computer program is provided in Figure A1.

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Program Symbol	Text Symbol	Units	Field Type	Description		
CARD 1: I	teration cont	rol parameters	• • • • • • • • • • • • • • • • • • • •			
N	N N		15	number of elements in the beam.		
М	-		15	number of frequencies/modes to be calculated, ascending order (3 is satisfactory).		
FSTOP	-		F10.5	SOR and Rayleigh quotient con- vergence criteria (.001 is satisfactory.		
NSTOP	-		15	iteration loop termination parameter (150 is satisfactory).		
IPRNT	-		15	printout option (l=full, O=partial).		
ALEN	L		F10.5	length of the beam.		
NN	-		15	number of data cards (see Card 2) used to describe the mass distribution along the antenna.		
EMOD	E	psi	F10.5	Young's modulus.		
RHŰ	ρ	slugs/in ³	F10.5	density.		
ANU	-		F10.5	SOR acceleration factor (1.0 is satisfactory).		
IBC	I		15	boundary condition code: O=clamped-free, 1 or larger = pin-pin-free with pin at x=IAx.		
<u>CARD 2</u> : Description of the mass distribution along the beam; NN cards of this type.						
WI,XX	×	ft	F10.2	position from base of the beam.		
W3,DOU	DO	in	F10.2	outside diameter.		
W4,DIN	ID	in	F10.2	inside diameter.		

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State State 1 WRITE (10.102) N.M.FSTOP.NSTOP 102 FORMAT (*1'//10X,*'NATURAL FREQUENCIES AND NORMAL MODES OF A BEAM W 1121 WARIABLE (ROOSS SECTIONAL AREA'//10X,*BEAM IS DIVIDED INTO N EL 1174 WARIABLE (ROOSS SECTIONAL AREA'//10X,*BEAM IS DIVIDED INTO N EL 1946ENTS, N = '.142/ 10X,*NUMBER OF MODES AND FREQUENCIES TO BE CALC 1946ED, IN ASCENDING ORDER, M = '.15' 10X,*'SOR AND RAYLEIGH QUOTI 1014ATED, IN ASCENDING ORDER, M = '.15' 10X,*'SOR AND RAYLEIGH QUOTI 1014ATED, IN ASCENDING FSTOP = '.13' 10X,*'ITERATION LOOP TE 1840INATION PARAVETER, NSTOP = '.13') WAITE (10:109) /LEN,DEL,FMOD,RHO,ANU,NN,IBC 109 FORMAT (1 :, 9X;'LENGTH OF REAM (IN), ALEN = ',F51.3/ 10X,'BEAM I IS DIVUEDS INTO ELEMENTS OF LENGTH (IN), DEL = ',F27.3/10X,'YOUNGS 140DLUG (PSI), EMOD = ',F50.0/ 10X,'BEAM DENSITY (SLUGS/IN+*3), R 140 = ',F45.9/ 10X,'SOR ACCELERATION FACTOR, ANU = ',F48.5/ 10X,' 110UMPER OF SUPPLED BEAM COORDINATE POINTS, NN = ',131/10X,'BOUNDAR 17 CONDITION CODE, IBC = ',148/) WHIP ANTENNA OR UHF/VHF OR OTHER SINGLE ROD MAST OF VARIABLE CROSS Sectional Area 110 FORMAT (' ', 9x,'BEAM PHYSICAL SPECIFICATIONS'//IOX,'X LOCATION (F
11)'+5x+'X LOCATION (IN)'+5x+'INNER DIA (IN)'+6x+'OUTER DIA (IN)'/) NOW CREATE THE INNER AND OUTER DIAMETER VECTORS DIN AND DOU AT THE DIVENSION A(40+10)+B(10)+DIN(44)+DON(44)+W1(44)+W2(44)+W3(44)+W4(4 W1+W2 DATA VECTORS CONTAIN X LOCATION IN FT AND IN RESPECTIVELY W3+W4 DATA VECTORS CONTAIN THE OUTER AND INNER BEAM DIAMETERS IN 5 DIMENSION AREA(44).AMR(10) ALSO NOTE THAT THE DIMENSIONS FOR A AND B HAVE REEN SELECTED PERMIT VALUES OF N .LE. 40 AND VALUES OF M .LE. 10. LARGER DIMENSIONS MAY RE SELECTED AT ANY TIME IF REQUIRED COMMON DEL.EUDPRHOIDNINDOU.WI.W2.W3.W4.AREA.AMR ASSIGN IO DEVICF. NUMBERS READ (IN.100) N.M.FSTOP.NSTOP.IPRNT.ALEN.NN.EMOD.RHO.ANU.IBC 100 FORMAT (215.F10.5,215.F10.5.15.3F10.5.15) 3EL*ALEN/N < ASSIGN NN AND MM TO EQUAL THE DIMENSIONS OF NN=40 IF (IPRNT) 3,3,4 4 WRITE (10+104) W1(1)+W2(1)+W4(1)+W3(1) 04 FORMAT (''+ 4F20=3) LOCATIONS X = [+DEL,] = 0.1.2..... 2 DO 3 [=1,NN REAC (IN.101) %1(1),W3(1),W4(1) 101 FORMAT (3F10.2) DEFINE FILE 1(559,2,U,18) IF (IPRNT) 2.2.1 W2(I)=W1(I)*12" WRITE (I0.110) DO 15 [=1,004 AREA(1)=0. 104 FORMAT (3 CONTINUE INCHES MM=10 υ 0000 000

SUBROUTINE ESOR(N,M,A,B,FSTOP,NSTOP,IPRNT,ANU,IBC)

S <u>نه</u> ب ا RUJISUSED TO STORE THE JIH EIGENVALUE NOTE THAT THE EIGENVALUES * CIRCULAR FREQUENCIES ** 2 ALSO NOTE THAT THE DIMENSIONS FOR A AND B HAVE BEEN SELECTED TO PERMIT VALUES OF N .LE. 40 AND VALUES OF M .LE. 10. LARGER DIMENSIONS MAY BE SELECTED AT ANY TIME IF REQUIRED FSTOP IS THE ITRAATION CONVERGENCE CRITERIA FOR FRACTIONAL DISPLA-CEMENT NORMS IN THE SON PROCEDURE AND FRACTIONAL LAMBDA NORM IN NOTE THAT DIN AND DOU ARE DIMENSIONED N+4 TO ALLOW FOR TWO POINTS AT X= 0 AND -DEL AND TWO POINTS AT X = (N+1)*DEL AND (N+2)*DEL DIMENSION A(40.10).B(10).DIN(44).DOU(44).CK(44).EK(44).FK(44).YK(4 EWOD IS YOUNGS MODULUS (PSI) RHO IS THE REAM DENSITY (SLUGS/IN**3) DIN AND DOU ARE THE INNER AND OUTER CIAMETERS OF THE ROD AT LOCATIONS SMALL I = 0 TO N+ FOR WHICH THE INDEX RANGE IS INDX = g NSTOP IS THE ITERATION TERMINATION PARAMETER FOR ANY ITERATION ADDITIONAL INPUT INFORMATION IS SUPPLIED VIA THE COMMON BLOCK ALL UNITS ARE LAF.SLUGS.INCHES.SEC UNLESS OTHERWISE SPECIFIED THE J TH NORMAL MODE, J=1 TO M [PANT IS THE PRINTOUT OPTION. 1 IS FOR FULL PRINT. 0 IS FOR FRFOUENCIES AND NORMAL MODES (EIGENVALUES AND EIGENVECTORS) Sor, rayleigh duotient, and gram Schwidt methods are used M = NUVBER OF NORMAL MODES AND FREQUENCIES WHICH ARE TO BE Determined COMMON DEL, EMCD, RHO, DIN, DOU, CK, EK, FK, YK, AREA, AMR ANU IS THE SOR ACCELERATION FACTOR DEL IS THE GRID SPACING (INCHES) THE RAYLEIGH QUOTIENT PROCEDURE A(I,J),I=I,N, IS USED TO STORE DIMENSION AREA(44), AMR(10) ASSORTED CONSTANTS IO DEVICE NUMBERS PI=3.14159 2 TO N+2 N2=N+2 PRINT LOOP 4 00000000

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	110 FCAME 1:	I	DIMERSION AREA(44),448(10) Covicy Jellerucd,440,9104,500,664,64,454,476,4864,448
	1545 IIN 101) KI([].K4([)	00	DEL IS THE GRID SPACING (INCHES)
٠		υv	EMOD IS YOUNGS 40DULUS (PSI) RHO IS THE REAM DENSITY (SLUGS/IN++3)
	MINAR VATA VECTURS CUMPIN X LOCATION IN FT AND IN RESPECTIVELY 20144 Data Vectors contain the outer and inner beam diameters in 11/146		DIN AND DOU ARE THE INNER AND OUTER DIAMETERS OF THE ROD AT Locations swall i = 0 to N+ FOR WHICH THE INDEX RANGE IS INDX =
,	F [1994]),),4 4 401F [[0,104] %][],42(1),44(1),43(1)		Z TO N+Z Vote that din and dou are dimensioned n+4 to allow for two points at x= 0 and -def and two points at y - 1
	ICE FORMAT (* ** - 4F20.3)) continue		IO DEVICE AUMARAS
~~	VOW CREATE THE INNER AND OUTER DIAMETER VECTORS DIN AND DOU AT THE	,	
v	LOCATIONS K = 1+00EL+ 1+00+1+2++++N++ DO 15 1=1+MM+	U	ASSORTED CONSTANTS
	AREAL11+0. Divit1+0.	J	PI=3=14159
	15 DOU(1=0. ##=-0fL	, U U	ASSIGNING CK AND EK VECTORS Accise abea useride
	Z-Z-Z 20 z 120X-2.22	,	
			AKED. WTT=0.
			00 1 INDX=2,42 A1=P1/64.**(DOU(INDX)**44.=DIN(INDX)**44.)
			EK(INDX)=EMOD4AI IF (INDX-2) 2.2.3
			7 FNOT=EK(2) 15 (1PRNT) 3,3,4
	0 1 10 1 1 1 1 1 1	10,1	↓ krite (10+100) ENOT) format ('1'//10X+'Normal modes and frequencies using sob. bavifich
	11 ILGMAILDMAL I 12,10,10		I OUOTIENT, AND GRAM SCHMIDT TECHNIQUES'//IOX, FPSILON NOUGHT AT RO 101 OF BEAN (LBF-IN##2), FNOT = 1.514, 5/10X, NOTE TOT DE 2.5
	12 GO TO B 10 MHGHellOW+1		11 = EKENDIT/10X, PHYSICAL DESCRIPTION OF THE BEAM (ALL UNITS
	DOUCINDX1+W3(ILOW)+(W3(IMIGM)-W3(ILOW))/(W2(IMIGM)-W2(ILOW))+(XX-W		WRITE (10,110)
	01111001)=4411L041+14411H1641-4411L0411/4211H1641-4211L04))+(XX-4 01111001)=4411L041+14411H1641-4411L0411/4211H1641-4211L04))+(XX-4	11] FORMAT (' ' ' 2X* 'LOCN' 65*'X (IN) ' 9X*'OUT DIA (IN) ' 2X* 'INN DI Ia ([4]) ' 2X* 'AREA (IN**2)' 2X*' [(IN**4]' 5X* 'WT (LBF) ' 7X* '
١	2 CONTINUE		JEK'+ +X+ 'CK (]/SEC++2)*/) EK([NDX]+EK([NDX)/ENDT
U	2540 A A40 A 50 13 Je1644		AKKAAK Akep1*(DGU([NDX)*+2.=D1%(1NDX!==2.)/A.
	#K#141+0. Prub+0.		
		U	CKITNDATERNOT/KHO*DEL**4.*AK) IN THE ABOVE EQUATION, DUE TO THE UNITS CHOSEN, CK HAS UNITS LEF/
L		00	IIN-SLUGI. TENPORARILY THIS IS CONVERTED INTO FT SO THAT LBF MAY BE PEPLACED WITH SLUG-FT/SEC**2. THEN THE FINAL ANSWER FOR CK
	MORTAL MODES AND FREQUENCIES ARE ORTAINED USING SUBROUTINE ESOR	U	WILL HAVE THE UNITS 1/SEC+*2 CK(INDX)=CK(INDX)+12+
, .	CALL ESO9(N;M:A.A.A.A.FSTOP.NSTOP.IPANT.ANU.18C)		xx=xx+DFL [= NDX-2
			WI=054(4XX)*OFL*RH0*32.2 [f (1) 30+31+30
y	LTEATE THE GENERALIZED MODAL PSEUDO MASS VECTOR IN MODE SPACE		. ¥T=€. • ₩TT=₩TT+⊻T
	DO 91 [MODE#1,W Avrilmode1=0.		IF (IPRVT) 1.1.6 W3TF (10-101) 1.XX-DOU([NDX]-DIN(]NDX)-4K.4[.WI-EK(]NDX).CK(]NDX)
	00 52 Jelsk 52 Avriimodfi=Amriimodfi+A(J,imodfi*A(J,imodfi*Arfa(J+2)	101	FORMAT (* * * 2 <u>x 13.13.113.13.114.3.3114.3.1112.112.114.61</u>
	AMAIIYODEJ=AVA(IWODE)=QHO 51 COMTINUE		IF (IPANT) 32,32,33 HOTTE /// //// 32,33
U	STORE THE NORMAL MODES, EIGENVALUES, AND SELECTED BEAM CONSTANTS An=1.+T++.1		* TILE (10412), WIL * Forwart (* :/lox*!total xeight of the beam (lbf), witt = *.flo.3//) Fripadolate fr one deita
	AX41.474.41 A18641.41864.1		
U	**IIF (1'1) AN*AM*ALEN*DEL*EVOD*RHO*DIN*DOU*A*B*AREA*AMR*AIBC		
v	CALL EXIT	,00	SOR/RAYLFIGH QUOTIENT/GRAM SCHMIDT SOLUTION PROCEDURE
	. ·		
	ETCHDE A1: Euco uthority		
		compu	iter program listing.
C	SELLAVAILABLE (UPT . UNCLASS)	IFIED	
-			
2			

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ASSIFIED 28. RATION (CONT'D)	<pre>Avelia duotient culculation fon a Betten Eldervalue ESTIMATE SUMPLO</pre>	
stp 447 ungi	D0 7 HODE-1.M ESTABLISH STATING ESTIMATES FOR ELGENVALUES AND ELGENVECTORS D0 20 HODE-1.M D0 20 HODE-1.M D0 20 HODE-1.M TF (1967) 5115145 D0 20 HODE-1.M TF (1967) 5115145 D1 HODE-1.M TF (1967) 5115145 D1 HODE-1.M TF (1967) 5115145 D1 HODE-1.M D1 HODE-1.	

WRITE (10.104) FLN.ITLP2.ITLP1.0MEGA.FREQ WRITE (10.104) FLN.ITLP2.ITLP1.0MEGA.FREQ 104 FORMAT (1 '1 9X.IFINAL FRACTIONAL LAMBDA (EIGENVALUE) NORM, FLN = 11. FT7.B. 10X.187KE164 QUOTIENT ITERATION LOOP COUNT. ITLP2 = ' 11. FT7.B. 10X.1908 ITERATION LOOP CUMULATIVE COUNT. ITLP1 = '.121/ 111A/ 10X.1018/10X.1885/1008 COUNT. 11207 = '.121/ 110X.1018/10X.1908 ITERATION LOOP COMULATIVE COUNT. 1107 10X.1006 SHAPE'//) 10X.1006 SHAPE'//) 100 25 HUDX=2.N2 AND', I5,' , WEIGHTED INNER PRODUC FREG=OMEG/2./FI FREG=OMEG/2./FI WRITE (10.103) IMODE,FSTOP.NSTOP,ANU.FIN WRITE (10.103) IMODE,FSTOP.NSTOP,ANU.FIN IO3 FORMAT ('1!'/IOX,WODE ', 15//IOX,SOR / RAYLEIGH QUOTIENT / GRAM I SCHUTDT TERRATION CUMULATIVE PARAMETERS:/IOX.FFDN AND FLN CONVERG I SCHUTDT TERRATION CUMULATIVE PARAMETERS:/IOX.FFDN AND FLN CONVERG I SCHUTDT TERRATION CUMULATIVE I FI2.5/ IOX,SUCCESSIVE OVER RELAXATION ACCELERATION FACTOR. I ANU = '.FI2.5/ IOX,FINAL FRACTIONAL INTERMEDIATE NOR%, FIN = 'FINAL SOR FRACTIONAL DISPLACEMENT NORM. FD WRITE (10-115) IMODE Format (1 1/10x, Orthogonality Check For Eigenvector Mode', 15/) D0 41 Iorto=1,1MODE THIS GUB COMPUTES THE NORM OF Y(I), I = M TO N THE NORM IS RETURNED IN YNORM YNORM = SUM (ABS(Y(I))/ (NUMBER OF ELEMENTS IN Y) WHFN ICODE IS 1, ONLY THE NORM OF Y IS COMPUTED WHEN ICODE IS 2, YNORM IS COMPUTED AND Y ITSELF IS NORMALIZED DIMENSION Y(44) \mathcal{T}_{i}^{n} PRINTOUT OF THE FINAL EIGENVALUES AND EIGENVECTORS IF (IPRNI) 7,97,38 36 OMEGA=SORT(OMEG2) SU41=SU41+A(1+[MODE)*A(1+[0RT0)*AREA(1+2) SU41=SUM1*RH0 SURROUTINE ANORMIY .M. N. YNORM. [CODE] **17 FFDN=F3TOP A7119-19** 47 IF (FLN=F3TOP) 18-19+19 19 CONTINUE WRITE (10,116) IMODE.IORTO.SUMI 116 FORMAT (' ',9X,'MODES'.15.' CON1=A(1,140DE) WRITE (10,109) 1+CON1 FORMAT (' +9X+15+F23+7) YNCRM=YNORM+ARS (CON1) CONTINUE YNORMEYNORM/ (N=M+1) IF (1CODE=2) 3.2.3 ORTHOSONALITY CHECK ARITE (10,217) FDN MRITE (10,217) FDN 117 FORMAT (* *9X* 1N = *•F19.8) 00 4 1=M4N Y(1)=Y(1)/YNORM RETURN F (1) 26.26.27 17 15'+F12+71 :,F19.8) N+[=] N+M+1 1 00 27 CON1=A(1. 26 WRITE (10 109 FORMAT (1 25 CONTINUE 41 CONTINUE 7 CONTINUE CON1=Y(I) YNORM=0. [=1NDX-2 SU41=0. 00V1=C. RETURN 19 CONTINUI 18 IJKLM=1 DO 42 -N 115 42 UNCLASSIFIED 00000 υ 000 GRAM-SCHMIDT ORTHOGONALIZATION See Antenna Notes regarding the Matrix Which The Matural Modes are Orthogonalized Whith respect to a Weighting r S 1 BES Mar and F 2 é DNORM=DNORM+APS(CON1) FK WILL 9E USED TO STORE OLD YK FOR USE BELOW FK(INDX)=YK(INDX) SUM1=SUM1+A([+[MODE]#A(1+IORTO)#AREA(1+2) SUM2=SUM2+A(1+IORTO)#A(1+IORTO)#AREA(1+2) SUCCESSIVE OVER RELAXATION (1508) LOOPS DO 1 LOOP=1.NSTOP 11LP1=11LP1+1 16 YK(1+2)=YK(1+2)-A(1,1)RTO)*SUM1/SUM2 14 CONTINUE DNORMEDNORM/(N+1) Call andry(tk.2,N2,YNORM.2) Fin=DNORM/YNORM STORE YK(INDX) IN. A(1,1MODE) CALL ANORM(FK,2,N2,DNORM,1) FDN=DNORM/YNORM IF (FDN=FSTOP) 9,10,10 CALL ANORM(YK.2.N2.VNORM.2) FK([+2]=FK([+2]=YK([+2]) A([,1MODE]=YK([+2]) YK (INDX) =YK (INDX) +CONI CONTINUE A(1,1MODE)=YK(1+2) YK(2)=0. FK(2)=YK(2) IF (IBC) 53.53.54 \YK(IBC+2)=0. IF (IMM) 12.12.13 DO 14 IORTO=1.1MM CONTINUE DO 16 1-1 .N Nº 17 1=1,N I-JOOMI-WH N. 1. I Nel=1 11 00 YK(1)=YK(3) 10 CONTINUE 9 1JKLM=1 FK(2)=0= FUNCTION EXTEND Y [JKLMe] SUM1=0. SUM2=0. 12 5 17 13 60 1 45 000000 υ U 0000

(b) Forced Vibration

The computer program for forced vibration consists of a main program and three subroutines, referred to as "DRAGC", "YDISP" and "VISCO". The major portion of the computation for the forced vibration response is carried out in the main program. Subroutines DRAGC, YDISP and VISCO respectively deal with computation of the air blast loading on circular cylinders, display of the stresses which correspond to a specified beam displacement profile, and calculation of the kinematic viscosity for air. Input data for this program consists of the natural frequencies and normal modes computed previously (read from a disk file) and data cards identifying the air blast loading and assorted parameters required in the time response calculation. The card input data for the forced vibration calculation is outlined below, and a listing of the computer program is provided in Figure A2.

Program Symbol	Text Symbol	Units	Field Type	Description
Card 1:	Data desci	ribing the	normaì mo	de plots.
INPLT	_		15	plotting option (O=suppress the plot).
ICODE	-		15	printout option in the plot subroutine.
XLEN	-	in	F10.3	length of the abscissa.
YLEN	-	irı	F10.3	length of the ordinate.
YDELL	~		F10.3	scale of the ordinate.

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Program Symbol	Text Symbol	Units	Field Type	Description
Card 2:	Data descr	ibing the a	air blast	loading on the antenna.
PO	р _о	psî	F10.1	peak overpressure.
TPLUS	t _d	sec	F10.1	positive phase duration.
PA	PA	psi	F10.1	atmospheric pressure.
TA	TA	۴F	F10.1	atmospheric temperature.
D	-	in	F10.1	representative antenna diameter (for display of drag pressures only).
AK	к		F10.1	Friedlander decay constant.
TIME	-	sec	F10.1	time step (for display of drag pressures only; .010 is satisfactory).
LOOPS	-		110	limit on the number of display loops (display purposes only; 999 is satisfactory).
<u>Card 3</u> :	Number of (direction)	cards need cross-sec	ed to spec tional_are	ify the projected (normal to blast a profile of the antenna.
NN	-		15	if NN=1, then the OD used in the Free Vibration problem also specifies the projected antenna area profile; if NN>1, then there are NN cards to follow to specify this profile (see Card 4).
Card 4:	Description area_profi	n of the p le_of_the_a	rojected (mantenna:	normal to blast direction) cross-sectional NN_cards_of_this_type_(if_NN>1)
W1,XX	×	fl	F10.2	position from base of the beam.
W3,DIA	<u>OD</u>	in	F10.2	outside diameter.
Card 5: C	ontrol para	ameters fo	r the tran	sient response calculation.
MODES	-		110	number of normal modes used in construc- ting the time response (ascending order in frequency).
DELT	Δt	sec	F10.5	time step used in the numerical integration.
TLIM	-	Sec	110	maximum time to which the time response is carried.
MDISP	-		F10.5	the number of time steps between beam response displays.

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FORCED VIBRATION

 $\langle \cdot \rangle$ ≟4 1.1 601 FORMAT (' '//OX 'EFFECTIVE EXTERNAL "EAM DIAMETER PROFILE FOR THE 10RAG CALCULATION'//IOX,'LOCN'+12X,'DIAMETER (IN)'.7X .'PROJECTED ^{3K*} 1AREA (FT**2) PER LINEAR FOOT OF BEAM'/) 12 G0 T0 8 10 THIGH=ILOW+1 DIA(INDX)=#3(ILOW)+(W3(IHIGH)-W3(ILOW))/(W2(IHIGH)-W2(ILOW))+(XX-W DISPLAY CONSTANTS, DRAG DIAMETERS, ETC. WRITE (10.600) MODES,DELT,TLIM,MDISP 600 FORMAT (11//10x,TIME HISTORY RESPONSE OF VARIABLE AREA BEAM'// 110X,'NUWARE OF NORMAL MODES USED IN CONSTRUCTING THE TIME RESPONSE 1, MODES = '*IIO' 10X,'TIME STEP USED IN THE TIME INTEGRATIONS (SE 10) DELT = '*F27.6C' 10X,'TRANSIENT RESPONSE WILL BE CARRIED CUT 110 THE TIME LIMIT (SEC), TLIM = ',F10.6/ 10X,'NUMBER OF TIME STE 105 FTWE LIMIT (SEC), TLIM = ',F10.6/ 10X,'NUMBER OF TIME STE 105 FTWE LIMIT (SEC), TLIM = ',F10.6/ 10X,'NUMBER OF TIME STE 105 FTWE LIMIT (SEC), TLIM = ',F10.6/ 10X,'NUMBER OF TIME STE ESTARLISH CONSTANTS FOR THE TIME HISTORY READ (IN+500) MODES,DELT,MDISP,TLIM 500 FORMAT (I10,F10,5,I10,F10,5) WPITE (10.6C2) [.DIA(INDX).AAAA FORMAT (' '.113.F23.44.30X.F10.6) LOOPS . O. T.I HEADRAG IF (NTIME-1000) 25,25,26 IF (MODES-M) 27+27+28 DO 29 ILOOP=1.NTIME AAA=DIA(INDX)/12. TREAL=TIME+.5*DELT NTIME=TLIM/DELT+1 00 Z1 INDX=2+42 DO 33 K=1,MODES (10,601) TIME=TIME+DEL1 DO 60 I=1 NN4 Nº 1=1 00 00 CBETA(K)=0. SBETA(K)=0. INITIALIZE NTIME=1000 IMF=DELT I OUT = MDI SP 12(ILOW)) 21 CONTINUE 26 NTIME=10 25 IF (MODE: 28 MODES=M 27 IJKLM=1 CONTINUE YK(1)=0. 1=1NDX-2 5 CONTINU .00PS=1 D=DIA(I WRITE 602 33 60 υυ υ $\mathbf{v} \mathbf{v}$ 0000 DEFINE FILE 1(559,2,0,18) DIMENSION A(40,10),8(10),9DIN(44),0OU(44),YK(44) DIMENSION DIA(44),WI(44),W2(44),0OU(44),YK(44) 310 FORMAT (215,3) 10005, XLEN, YLEN, YLEN, YDELL WRITE (10,311) INPLT, ICODE, XLEN, YLEN, YDELL 311 FORMAT (10,710X, PLOT DATA ... INPLT, ICODE, XLEN, YLEN, YDELL ...', 21 CALL YDISP(IMODE)FREQ+N+YK+DIN+DOU+DEL+EMOD+RHD+ICUDE+XLEN+YD WRITE (10+100) N+M+ALEN+DEL+EMOD+RHO+IBC FORMAT ('1'/10X+'N+M+ALEN+DEL+EMOD+RHO+IBC'+215+2F10+4+2F15+5+15) RETRIEVE NORMAL MODES, GENERATE STRESSES AND PLOTS, AND GENERATE PI=3.14159 Read Normal Modes and Frequencies etc. Read (1'1) An\$AM\$ALEN\$CEL\$EMOD\$RHO\$DIN\$DOU\$A\$B\$AREA\$AMR\$AIBC NORMAL MODE/ FREOUENCY DISPLAY INPUT PLOT DATA, NOTE THAT INPLT * 0 MEANS PLOTTING WILL BE WRITE (IO+101) 1.4DIN(INDX).4DOU(INDX).4REA(INDX) FORMAT (' ',9X,'I.4DIN.6DOU.4REA'.15.3F12.6) READ (IN. 310) INPLT, ICCOE, XLEN, YLEN, YDELL COMMON PO.TPLUS.PA.TA.D.AK.GAMMA.R IO DEVICES ESTABLISH THE CIRCULAR FREQUENCIES D0 22 140DE=1,4 C041=R(1M0DE) WRITE (IO+105) (1+AMR(1+)|=1+M) 105 FORMAT (+0++7×+15+F20+10) 10) DIMENSION AREA(44) .AMR(10) THE TIME HISTORY RESPONSE YK (INDX) = A (INDX-2, IMODE) E (IMODE) "SORT (CONI) FREQ=B(1MODE)/PI/2. IF (INPLT) 71,72,71 DO 2 IMODE=1.M DO 3 INDX=3.N2 DO 1 INDX=2,N2 15,3F10,3//) SUPPRESSED 18C=A18C I=INDX-2 CONTINUE CONTINUE · IRCI [JKLM=] 42=N+2 44=4NN N = N MAHM いま 100 101 22 1 401-1124 υυι U 000 υυ 0000

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WINCELTAIN WINCE (1000) TASEC.(FACTKII)(F#1,WODES) BOD FORMAT (* '//IOX,'TIME (MSEC)',F9,3 // IOX,'NORMAL MODES RELATIV IE CONTRIPUTION (ASCENDING ORDER)',F7F10,4/1 ALL YDISP11MODE,FREG,N,YK,D1N,DOU,DEL,EMOD,RHO,ICODE,XLEN,YL LL,1EC) CHETAI(HODE)+CHETAI(HODE)+CON1*HETAK*COS(ARG) SHETAI(HODE)+SHETAI(HODE)+CON1*HETAK*SIN(ARG) SHETS(HODE)+TEELA SHETS(HODE)+TEELA FACTK(HODE)+TEELA+SIN(ARG)+COS(ARG)*SHETA(IMODE))/B(1MODE) iB NOTE ... DISPLACEMENTS Y AS A FUNCTION OF TIME ARE GENERATED OR THE TIME T = TREAL (NOT FOR THE TIME T = TIME) CALL DAAĞC(LOOPS.0.TIME.DRAG) WICII-ORAĞAD/12. WICII-ORAĞAD/12. WICII-ORAĞAD/12. WICIION OF LOADING DUE TO REDUCED PROJECTED AREA WHEN THE ANDUCTION OF TOADING DUE TO REDUCED PROJECTED AREA WHEN THE ANDUCTION OF TA TA FINITE SLOPE RELATIVE TO THE VERTICAL CONL=YYK(1+3)-YK(1+1))#12./2./DEL GENERATE Y AT'THIS LATER TIME AND DISPLAY PRINTOUT THE CALCULATION TIME IS T = TREAL YK(INDX)=YK(INDX)=A(I.IMDDE)=FACTK(IMODE) CONVERT YK FRCM INCHES TO FEET YK(INDX)=YK(INDX)/12. CO 32 [=1.N BFTAK+BFTAK+A([,[MODE]*W]([) 32 CNTINUE ARG=B([NODE]*TIME IF (IOUT-MDISP) 29,39,39 IOUT=0 WILLS=WILLSCOS(CON1) (ILCOP-1) 34.34.35 Forced vibration computer program listing. 1 NODE=1 MODES IMODE=1,MODES ILOOP=1 +NT IME ME+.5*DELT "MSEC=TREAL+1000. LOUP5*1 TIMF=-DELT DO 33 K#1+MODES CBETA(K)=0. SBETA(K)=0. +DEL I=1 *NN 1) / AMR (IMODE) 30 I-1.N N. [=] 0UT=10UT+1 CONTINUE IOUT=MDISP INITIALIZE DO 60 I=1+N CON1=.5*DEL YK(IADX)=0. CALL EXIT 00 29 IL 41 CONTINUE 29 CONTINUE 60 YK(1)=0. TRFAL=T(D0 30 1= 0=D[A([+ CON1=ARS BETAK=0 +1=X0v] CONTINU CON1=DE 16 00 14 00 00 47 UNCLASSIFIED 93 30 45 31 66 42 υu υu υu 000 A STATE OF A if (inplf) 71.72.71
71 [JkLM=1
72 [JkLM=1
74 [JkLM=1
74 [JkLM=1
75] JkLM=1
75] JkLM MITE (10:311) INPLT.ICODE.XLEN.YLEN.YDELL
311 FORMAT {'0'/10X+'PLOT DATA ... INPLT.ICODE.XLEN.YLEN.YDELL ...',21 THEN THE DIAMETERS FOR THE DRAG LOADING CALCULATION ARE AT THE THE OUTER DIAMETER VECTOR DIA If NN .61. I. THEN THE DIAMETERS TO BE READ IN BELOW SPECIFY THE Face-on diameters for use in the orag loading calculation WIW2 DATA VECTORS CONTAIN X LOCATION IN FT AND IN RESPECTIVELY W3 DATA VECTOR CONTAINS THE OUTER BEAM DIAMETER IN NORMAL MODE/ FREQUENCY DISPLAY INPUT PLOT DATA. NOTE THAT INPLT * 0 MEANS PLOTTING WILL BE READ IN OR ASSIGN DIAMFTERS FOR DRAG LOADING CALCULATION and the second second second with the second s LOCATIONS X = 1*DEL, 1=0,1,2,...,N. DO 15 1=1,NN4 15 DIA(1)=0. FIGURE A2: RASIC BLAST WAVE PROFILE AND SCAN OF DRAG LOADING READ (IN.300) PO.TPLUS.PA.TA.D.AK.TIME.LODPS Forwat (TF10.1.110) Gamma=1.4 SUPPRESSED READ (IN:310) INPLT.ICODE.XLEN.YLEN.YDELL 310 FORWAT (215.3F10.3) W3(1) CALL DRAGC (LOOPS, 1, TIME, DRAG) WRITE ([0,104) W1(1),W2(1), 104 Format (+ ', ', 3F20.3) 20 Continue G0 T0 10 IF (XX-W2(ILOW+1)) 10,10,11 ILOW-ILOW+1 IF (ILOW-NN+1) 12,10,10 READ (IN.401) WI(I).W3(I) FORMAT (2F10.2) W2(I)=W1(I)*12. 3 YK(INDX)=A(INDX-2,IMODE) FREQ=B(IMODE)/PI/2. (X0N]) nog= () 16.16.17 READ (IN.400) NN 400 FORMAT (15) 00 \$ INDX=2,V2 XX=XX+DEL I=INDX-2 INDX=2,N2 DO 2 [MODE=1.M DO 3 [NDX=3.N2 IF (1-N) 8,9,8 TO 19 20 1=1.NN (1) 61716 Same alter and a later all a state was to an 15.3F10.3//) 9 2 CONTINUE 12 [JKLM=1 XON I - NN LI 401 FORMAT 130-1 NCHES NN=NO 16 DO 18 18 DIA(1N LOV=1 ÷z. 5 38 300 • 1 00 0000 000 υυυ

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(CONT'D) VIBRATION FORCED

SUBROUTINE DRAGCIJCODE, JPRNT, TIME, DRAG)

SUBROUTINE YDISP(IMODE,FREQ,N,YK,DIN,DOU,DEL,EMOD,RHO,ICODE,XLEN,Y

NORMAL MODE OR GENERAL CURVE DISPLAY

LEN.YDELL.IBC)

FRANSIENT DRAG ON CIRCULAR CYLINDERS

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LOCATION A REFERS TO AMBIENT CONDITIONS Location B refers to the region immediately behind the shock front Location C refers to the immediate vicinity of the cylinder ZETA=PB/PA Note that several of the fquations which follow assume gamma =1.4 TB=TA*ZETA*(6.*ZETA)/(6.*ZETA+1.) CR=CA*SORT(TB/TA) INPUT INFORMATION P0.TPLUS. ETC PARAMETERS IN COMMON MUST BE SUPLIED P0.TPLUS. ETC PARAMETERS IN COMMON MUST BE SUPLIED ICODE IS THE NUMBER OF TIMES THE DRAG CALCULATION IS PERFORMED IPRNT IS THE OUTPUT OPTION. 0 = NO OUTPUT. 1 = FULL PRINTOUT TIME IS' THE TIME IN SEC AT WHICH THE DRAG CALCULATION IS TO BE PERFORMED IF ICODE IS 1. OR TIME IS THE TIME INTERVAL IN SECONDS BETWEEN SUCCESIVE DRAG CALCULATIONS IF ICODE .0T. 1 DRAG IS THE FINAL CALCULATIONS IF ICODE .0T. 1 DRAG IS THE FINAL CALCULATIONS IF POUNDS/FT**2 ASSIGNMENT OF INPUT/OUTPUT DEVICE NUMBERS (IN. 10) COMMON PO.TPLUS.PA.TA.D.AK.GAMMA.R AMACS =SQRT(1.+6.*PO/(7.*PA)) U8=5.*PD*CA/(7.*PA*AMACS) 00=2.5*P0**2./(P0+7.*PA) ANUE=VISCO (TB.PR.PA.PB) RER=UB+D/ANUB QIC=00+00**2*/{2*8*P8} CA=SORT (GAMMA+R+TA) US=AMACS *CA AMACB =UR/CB TA=TA+461. PB=PA+P0 0=D/12, 11=0/US [N=2 0=00 5=C]

IRC IS THE ROUNDARY CONDITION PARAMETER INC = 0 ... CLAMPED - FREE (CANTILEVER) BC. AS IN THE WHIP ANTENNA INC = NO. 467. 0 ... PIN - FILE CONTILEVER) BC. AS IN THE WHIP ANTENNA INC = NO. 467. 0 ... PIN - FILE END CONDITION AT X = L AND AT X = IJAC#PELTAX AND THE FREE END CONDITION AT X = L. INCCE IS EITHER THE NORMAL MODE NUMBER OR THE CURVE IDENTIFICA-TTOW NUMBER TCORE = 1. PRINTOUT AND STRESSES ONLY TCORE = 2. APOVE PRINTOUT AND STRESSES ONLY TCODE = 2. APOVE PRINTOUT ONLY DISPLACEMENTS YK ARE IN FET ALL OTHER DIMENSIONS ARE LEFSLUGS.IN.SEC ALL OTHER DIMENSIONS ARE LEFSLUGS.IN.SEC XLEN AND YLEN ARE THE PLOT XLEN AND YLEN ARIABLE RANGE BETWEEN UNITS ON THE Y AXIS TF YDELL .LT. 0. THEN A VALUE IS AUTOMATICALLY SELECTED WITHIN THE PROGRAM TO SCALE DATA TO FIT ON THE PLOT IF (ICODE-2) 2.2.1 2 WRITE (10.100) IMODE.FREG 100 FORMAT ('1'//IOX.'MODE/CURVE NUMMER '.15 [=b[/@d**(\DON])***d**0]N[]N[]N]]**d**] {DOU(INDX)**2.-DIN(INDX)**2.)/4. YK { N+4 } = 4 * YK { N+2 } - 4 * YK { N+1 } + YK { N } DIMENSION YK (44) . DIN (44) . DOU (44) . 10 ^EVICES 1N=2 YK (N+3)=2°*YK (N+2)-YK (N+1) /K(1)=YK(3) IF (IBC) 51+51+52 DO 3 INDX=2,N2 YK(1)=-YK(3) PI=3.14159 BCIS ON YK AMOLD=0. AKOLD=0. /X (2) = 0 (-XONI-32 IJKLM=1 N2=N+2 5 25 ~~~~~ υ J

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FD1FR=5.*T1

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if (IPRMT)2,2,1 WRITE (IO+101) PA,TA,DD,PO,TFLUS,AK WRITE (IO+101) PA,TA,DD,PO,TFLUS,AK FORWAT ('1://JOX+)TRANSIENT DRAG ON CYLINDERS DUE TO AIR BLAST'// IIOX*'AMBIENT PRESSURE (PSI), PA = ',FIA,2' IOX*'AMBIENT TEMPERATUR IE (NEG R), TA = ',FI1,2' IOX*'CYLINDER DIAMETER (IN), D = ',FIT*' IIOX*'PEAK OVERPRESSURE (PSI), PO = ',FI5,3' IOX*'POSITIVE DURATI ION (SEC), TPLUS = ',FI1,2' IOX*'DECAY CONSTANT, AK = ',F24,2) WRITE (IO)+104) CA,US,TI+TDIFR

104 FORMAT ('

'AMBIENT SPEED OF SOUND (FPS). CA = '+F10.2' 10X.'SPEED OF CK FRONT (FPS). US = '+F8.2' 10X.'TIME OF ENGULFMENT (SEC) '+E-14.8' 10X.'LENGTH OF TIME FOR WHICH THE DIFRACTION PRESS いたのでは、「「「「」」」 THE SHOCK

1))*12•/DEL/DEL*EMOD*

- WK UNDX+111-24 HX

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υU υυ 000000 $\mathbf{U}\mathbf{U}$ υ 17000 1 WPITE (10:101) PA.FA.DD.PO.FPLUS.AK 101 FORWAT (11://10X, TRANSIENT DRAG ON CYLINDERS DUE TO AIR BLAST'// 110X ** AMBIENT PRESSURE (PSI). PA = '*F16.2/ 10X, *AMBIENT TEMPERATUR 110X ** AMBIENT PRESSURE (PSI). PA = '*F16.2/ 10X, *AMBIENT TEMPERATUR 101 10X ** PEAX OVERPRESSURE (PSI). PO = '*F15.3/ 10X, *POSITIVE DURATI 10N (SEC). TPLUS = '*F12.5/ 10X, *DECAY CONSTANT. AK = '*F24.2) **RIFE (10:104) CA.US, TT, *DIFR 104 FORMAT (' */10X, 1 'AWBIENT SPEED OF SOUND (FPS), CA = ',F10.2' 10X,'SPEED OF 17HE SHOCK FRONT (FPS), US = ',F8.2' 10X,'TIME OF ENGULFMENT (SEC) 1, TT = .,F14.5' 10X,'LENGTH OF TIME FOR WHICH THE DIFRACTION PRESS 1URE APPLIES (SEC), TDIFR = ',F8.5//) WAITE (10,102) 102 FORMAT (' ',' 10X,'ALT OF THE FOLLOWING DATA APPLIES AT THE CYLIND 168 (STATION C) '/10X,'UNITS ... PRESSURE IN PS1, FEMPERATURE IN D 15G R, VELOCITY IN FTSEC, TIME IN SSCURE IN PS1, FEMPERATURE IN D 17EMP',7X,'Q',98X,'OI',6XX,'U',98 25 WRITE 110+103) TIME, POVER, TC+QC, QIC+UC+CC+AMACC , REC, PDIFR, PDRAG, P 103 FORMAT (' '.IX+F9+5+F9.3+F9.2+2.2F9.3+2F9.2+F9.3+F11.0+3F9.3+F9.2} IF (AMACC --48)10+10+11 New DRAG COEFFICIENTS INTRODUCED FEBRUARY 2, 1977-7 TIME=TIME+DELTA 4 F=11.~TIME/TPLUS)*EXP(-AK*TIME/TPLUS) RESTCRF DIAMETER D TO ORIGINAL UNITS CON1=8.*(PO*TT)**1.13/(5.*TT A STRAND STRAND STRAND STRAND AMACB =UB/CB Anur=VISCO (TR,PR,PA,PB) Ref=ur+D/Anur ANUC=VISCO (TC.PC.PA.PB) REC=UC*D/ANUC (TIME-TPLUS)14,14,13 TC=TB+{PC/PB)++.286 CC=CA+SQRT(TC/TA) UC=UB+F+{P0/PC)++.3571 [REC-4.E5)12.11.11 IF (TIME=TOIFR)8,8,9 PDIFR=CONI DO 3 I=1.ICODE IF (ICODE-1)4.4.5 IF (I-1)6.6.7 PLOAD=PDIFR+PDRAG IF (1PRNT) 3,3,25 DRAG=PLOAD#144. ([PRNT)2.2.1 0C=00*F**2 0IC=0I0*F**2. P0IFR=0. PDRAG=CON2+01C AMACC =UC/CC US=AMACS *CA C=PA+POVER 01FR#5.4T 6 DELTA=TIME TIME=-DELT POVER=PO*F 1LOAD DRAG 3 CONTINUE CON2 = 3 CON2=+6 TT=C/US DRAG=0. CON2=+7 RETURA 0-00 220 <u>ل</u> 5 13 4 20 112 υ

-4 C 1 1 //IOX:"MOMENTS ARE COMPUTED AT THE GRID POINTS USING 3-POINT OPERATOR 15:/IOX."SHEAR FORCES ARE COMPUTED .**ELE BEHIND THE INDICATED GRID 1 POINT'//5X."LOCN'.5K!'Y SHAFE (FT)'.*3X."SHEAR (LBF)'.*4X."MOMENT I 11N-LRF)'.*5X."SHEAR (PS1)'.*4X."FLEXURE (PS1)'/) GO TO 32 1 WRITE (10.109) IMODE 1 WRITE (10.109) IMODE 109 FORMAT (' '.100%, TIME (MSEC)', I7// 109 FORMAT (' '.100%, 6X, 'Y SHAPE (FT)', 3X, 'SHEAR (LBF)', 4X, 'MOMENT ' 11-LRF)', 9X, 'SHEAR (PSI)', 4X, 'FLEXURE (PSI)'/) FSTARLISH CRIGIN 2 INCHES ABOVE BOTTOM OF PAGE, AND LEAVE SCALES at 1 inch = 1 unit for plotting purposes CALL SCALF(1.0.1.0.-2.0)-2.0) CHOOSE THE NUMBER OF INTERVALS ALONG THE X AXIS TO BE AN INTEGER WULTIPLE OF 5 FT. AT=PI/64.*(DOU(INDX)+*4.=DIN(INDX)**4.) AK=PI*(DOU(INDX)**2.=DIN(INDX)**2.)/4. ANOM=(YK!INDX+1)-2.*YK(INDX)+YK(INDX-1))*12./DEL/DEL+EMOD*AI NOTE THAT YK IS IN FT. E IS IN PSI. DEL IS IN INCHES. AND THE HOMENT IS IN IN-LBF SHEAR=-(ANOM-ANOLDI/DEL and the second second second second second NY IS THE NUMBER OF Y AXIS INTERVALS (EVEN NUMBER) Ydfl=Cony/nny++99 FLSTR=ANDM=DOU(INDX)/2./AI WRITE (10.101) 1.VK(INDX).SHEAR.AYOM.SHSTR.FLSTR 101 FORMAT (' '.17.1X.F15.3.F14.0.F18.0.F16.0.F17.0) 3 CONTINUE TENTHS OF AN INCH CON2=CCN2=10. Conz is the range of Abs(Y) in tenths of a foot 100 FORWAT ('1'//IOX + MODE/CURVE NUMBER ', IS FEET IYDEL IS THE YAXIS INTERVAL IN YDEL IS THE Y AXIS INTERVAL IN 2 WALTER (101100) INCORTFRED (ICODE-2) 33+33+34 CON1=N*DEL/12./5.+.99 F (CON1-CON2) 7.7.8 IF (YDELL) 30.30.31 IYDEL=YAELL+10.+.99 AKK=(4K0LD+AK)/2. PLOT THE Y CURVE DO 3 [NDX=2+N2 CONZ=0. DC 7 INDX=2.VZ CON1=APS(CON1) YDEL=.1*IYDEL CON1=YK(INDX) [F ([) 5.5.4 NY=YLEN+2. I YDEL=YDEL AMOLD=A40M CONZECONI AHOLD=0. =[v0x-2 5 SHEAR=0. 4 AMOLD=AVC AKOLD=AK CONTINUE 71×2×2×2 2/AN#ANN AKOLD=0. NNS=CON1 33 IJKLM-1 301 •• ••

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VIBRATION (CONT'D) FORCED

ć. HTIC=.06 PLOTTING THE BOX AND TICK MARKS NUMBERING AND LABELING THE AXES CALL FPLOT(0,X1,Y1) IF (J-NY) 20,14,20 OCALL FPLOT(0,X2,Y1) CALL FPLOT(0,X1,Y1) CALL FPLOT(0,X1,Y1) 4 CONTINUE IF (J-NY) I7912417 7 CALL FPLOT(0,X2,Y1) CALL FPLOT(0,X1,Y1) 2 CONTINUE DY=YLEN/NY CALL FPLOT(1:0.00) CALL FPLOT(-2:0.00) IF (I-NX) 19.15.19 CALL FPLOT(0.X1.Y2) CALL FPLOT(0.X1.Y1) CALL FPLOT(0.X1.Y1) I CONTINUE CALL FPLOT(0.X1.Y1) IF (1-NX) 16.11.16 CALL FPLOT(0.X1.Y2) CALL FPLOT(0.X1.Y1) CALL FPLOT (0, X1, Y1) CALL FPLOTIO X1 + Y1 Y2=Y1+HTIC D0 11 1=1,NX X1=X1+DX X2=X1+HTIC D0 14 J=1+NY VN. 1- 1 51 00 XN+1=1 EI 00 X2=X1-HTIC Y2=Y1-HTIC DX=XLEN/NX Y1=Y1-DY CONTINUE č Y1=Y1+DY HT=.11 (1=0+ X1=X1 ů ľ 19 20 4 13 16 11 17 12

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CALL FPLOT(1,x1,-2.0) CALL SCALF(1.0)1.00.0.0.0) ORIGIN HAS NOW BEEN RESTORED TO BOTTOM OF PAGE BEYOND PLOT. READY FOR FUTURE CALLS TO THIS SUBROUTINE YI=YLEN/2,-NLAR/2*XHTT CALL FCHAR(X1,Y1,XHTT,HTT,PI/2.) WRITE (7,203) FORMAT ('DISPLACEMENT Y (FT)'I YSHIF=YLEN/2. ANUM=(I-1-NNY)*!YDEL*. Call FCHAR(X1.Y1.XHT.HT.O.) WRITE (7.202) ANUM FORMAT (54.1) XX1=X1/SCAX XY1=YK(INDX)/SCAY+YSHIF YY1=YK(INDX-2) ZCAY+YSHIF IF (INDX-2) ZCA2,23 ZCALL FPLOT(1,XX1,YY1) CALL FPLOT(0,XX1,YY1) 23 CALL FPLOT(0,XX1,YY1) CALL POINT(1) IF (X1-8.5) 24,24,25 SCAX=NX*5.*12./XLEN SCAY=NY*YDEL/YLEN DO 21 INDX=2.N2 X1=-5.5*XHT NLAP=19 X1=XLEN+1. X1=X1+DEL 21 CONTINUE CONTINUE X1=-DEL RETURN X1=8•5 on Ng 36 4 E 202 203 18

FUNCTION VISCO (TC+PC+PB)

DYNAMIC VISCOSITY FOR AIR . NU . SEE STN 249

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SUM = 90.27754-0.32934]3*TC+0.000874]*TC*TC VISCO =14.77PA*(6.+PB/PA)/(1.+6.*PR/PA) VISCO =VISCO *((PB/PC)**.714)*SUM*1.E=6 RFTURN

END

THX**1-XG-#1X

Itxx=xxx

NXXX=NXX/2+1

XHT=HT*6./7.

Y1=-2+#HT

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STP 447

3 CALL FPLOTIO:XXI.YYI) 21 CONTINUE X1=XLEN+1. 21 CONTINUE X1=XLEN+1. 21 CONTINUE X1=XLEN+1. 21 CONTINUE X1=XLEN+1. 21 CONTINUE X1=XLEN+1. 21 CONTINUE X1=XLEN+1. 21 CONTINUE 21 CONTINUE 22 CALL FPLOT(1).01.000.00.) 23 CALL SCALF(1).01.000.00.) 23 CALL SCALF(1).01.000.00.) 24 RETURN 34 RETURN 50 RET	FUNCTION VISCO (TC.PC.PA.PB) C DYNAMIC VISCOSITY FOR AIR • NU • SEE STN 249 C SUM = 90.27754-0.3293413#TC+0.0008741#TC#TC VISCO =14.77PA#(6.+PB/PA)/(1.+6.*PA/PA) VISCO =VISCO *((PB/PC)**.714)*SUM*1.E-6 AFTUPN END				UNCLASSIFIED
17 CALL FPLOT(0,X1,Y1) CALL FPLOT(0,X1,Y1) 12 CONTINUE 72=Y1-HTIC 50 13 1=1.NX X1=X1-DX X1=X1-DX CALL FPLOT(0,X1,Y1) 19 CALL FPLOT(0,X1,Y1) 13 CONTINUE 13 CONTINUE 13 CONTINUE 13 CONTINUE 13 CONTINUE 14 J=1.NY 71=Y1-DY 15 (J-NY) 20:14+20	<pre>20 CALL FPLOT(0.x2.Y1) CALL FPLOT(0.x1.Y1) 14 CONTINUE NUMBERING AND LABELING THE AXES HT=.11 Y1=-2.*HT XTT=HT*6./T. XTT=HT*6./T. XTT=NX+1 NXX=NX/1 NXX=NX/1 NUM=-5 00 15 1=1.NX X1=X1=DX</pre>	ZOD FORMAT (12) CALL FCHAR(X1,Y1,XHT,HT.00.) WRITE (7.200) INUM 200 FORMAT (12) 15 CONTINUE XHTT=1.2*XHT XHTT=1.2*XHT XHTT=1.2*HT XHTT=1.2*HT XHTT=1.2*HT XHTT=1.2*HT XHTT=1.2*HT XHTT=1.2*HT XHTT=1.2*HT 201 FCHAR(X1,Y1,XHTT,HTT,0.) 201 FCHAR(X1,Y1,XHTT,HTT,0.) 201 FCHAR(X1,Y1,XHTT,HTT,0.)	YI=-JC.*HT XI=-JC.*HT CALL FCHAR(X1.*XHTT.HTT.00.) WRITE (7.204) IMODE WRITE (7.204) IMODE VI=-DY YI=-DY XI=-5.*XHT WYY=NY+I DO 18 I=1.NYY YI=YI-DY	J	

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