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# PENETRATION OF HIGH EXPLOSIVES BY INERT PROJECTILES

FINAL REPORT

M. H. RICE

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#### I. INTRODUCTION

The two-dimensional, Eulerian computer code HELP (Hydrodynamics ELastic Plastic) developed at Systems, Science and Software (S<sup>3</sup>) has been modified to allow for the inclusion of an explicit reaction rate for modeling partially reacted states of high explosives. Calculations of the detonation thresholds and velocity losses of steel spheres penetrating slabs of Composition B and PBX-9404 have been carried out. Empirical reaction-rate models based on experimental, onedimensional run-to-detonation data (Reference 1) give good correlations with the experimental thresholds and velocityloss data as obtained at the Ballistic Research Laboratories (BRL).

The new capability provided by the code should be of use in several problem areas of interest to the Army. In particular, work is already underway to determine the effect of explosive reaction rates on shaped-charge jet formation.

Section II of this report contains a description of the reaction-rate models and the correlations of calculated and experimental velocity-loss and detonation threshold data. The equation of state and constitutive models used in the calculations are described in Section III. The reactionrate models and their experimental basis are discussed in Section IV.

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#### II. HELP CODE CALCULATIONS

The two-dimensional, Eulerian HELP code (Reference 2) has been employed extensively in a variety of studies to calculate the material flow associated with both the impact process and the detonation of high explosives as well as the interaction between detonated products and inert material. However, prior to the present work, the explosive computational cell was treated as either completely unreacted or completely reacted. In addition, it had to be decided before hand whether a given cell was to detonate, and if so, at what time. The modification to allow for the use of an explicit reaction rate enables one to treat partially reacted states of the HE. Correlations can be made of the degree of decomposition with the impact velocity of a projectile, the initial projectile/target configuration and the material properties of both the HE and the projectile. In particular, the use of a realistic rate law enables one to determine whether a given impact and configuration will lead to only partial decomposition or to complete detonation.

#### 2.1 CORRELATIONS WITH EXPERIMENT

In the present work the modified HELP code was used for a series of calculations consisting of a 1.3 cm diameter steel sphere striking at normal incidence a 10 cm diameter, 2.5 cm thick cylindrical slab of Composition B or PBX-9404. The initial calculational configuration is shown in Figure 1. The quantities of particular interest are the velocity loss of the projectile,  $V_{l} \equiv V_{s} - V_{f}$ , as a function of the initial striking velocity,  $V_{s}$ , and the minimum striking velocity required to produce complete detonation of the slab. A comparison of calculated velocity losses with experimental data as supplied by the BRL (Reference 3) is given in Figure 2. Several of the calculations, as indicated in the figure, were



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performed using the completely unreacted equation of state for the HE, as given in Section 3.2. The agreement of these points with the experimental curves is completely satisfactory. Four of the points in Figure 2 are the result of calculations using the reactive equation of state for HE (Section 3.2) and the reaction rate models as given in Figure 3, which is a plot of the fractional rate of decomposition as a function of pressure. As can be seen from Figure 2, the results of these calculations are also in good agreement with the experimental results.

A summary of the results of the calculations for PBX-9404 is given in Table I. The reaction rates used in these calculations are those as given by the "Forest Fire" model, proposed by Mader and Forest (Reference 1). A brief description of the model is given in Section 4.1. The reaction rates are obtained from experimental, one-dimensional run-todetonation data and are a function of a single equation of state variable which may be taken either as the pressure or the temperature. In the present calculation pressure was used as the independent variable. The Forest Fire reaction rates for PBX-9404 are plotted as a function of pressure in Figure 3. The use of this model in the HELP code calculations results in a transition from partial to complete reaction for striking velocities in the range 1.0 to 1.1 km/sec, in good agreement with the experimental results.

A summary of the results of calculations for Composition B is given in Table II. For Composition B, the use of the Forest Fire reaction rates results in only partial decomposition at a striking velocity of 2.0 km/sec. Increasing the reaction rates by a factor of 1.5 at each pressure brings the calculated detonation threshold to between 1.7 and 1.8 km/sec, in agreement with the experimental results. These modified reaction rates for Composition B are plotted in Figure 3.

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Figure 3. Reaction rate versus pressure as used in the HELP code calculations, where w is the mass fraction of unreacted explosive.

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## TABLE I

# HELP CODE RESULTS FOR THE PENETRATION OF PBX-9404 BY A 1.3 CM DIAMETER STEEL SPHERE

REACTION RATE MODEL	INITIAL VELOCITY (km/sec)	VELOCITY LOSS (km/sec)	DETONATION?
Inert	0.35	0.125	
Inert	0.7	0.23	
Inert	1.4	0.41	
Forest Fire	0.9		No
Forest Fire	1.0		No
Forest Fire	1.1		Yes
Forest Fire	1.4	0.86	Yes

## TABLE II

## HELP CODE RESULTS FOR THE PENETRATION OF COMPOSITION B BY A 1.3 CM DIAMETER STEEL SPHERE

REACTION RATE MODEL	INITIAL VELOCITY (km/sec)	VELOCITY LOSS (km/sec)	DETONATION?
Inert	2.0	0.56	
Forest Fire	2.0		No
FF × 1.5	2.0	1.0	Yes
FF × 1.5	1.8	0.85	Yes
FF × 1.5	1.75		Yes
FF × 1.5	1.70		No
FF × 1.5	1.6	0.39	No
FF × 1.5			
Y × 10	1.6	0.28*	No
FF × 1.5			
$Y_s = 0$	1.6	0.28*	No

\*Velocity loss at 10 µsec

In summary, the equations of state and constitutive models described in Section III together with the Forest Fire reaction rate model give good agreement between calculated velocity-loss and detonation threshold data for PBX-9404. For Composition B it is necessary to increase the Forest Fire reaction rates by a factor of 1.5 in order to obtain agreement between the calculated and experimental detonation thresholds. With regard to the factor of 1.5, since the Forest Fire reaction rates were obtained with the HOM equation of state for partially reacted explosive (Reference 4) instead of the models used in the HELP code calculations, a study was undertaken to determine the sensitivity of the reaction rates to the particular equation of state models used in their calculation. The results of this investigation are given in Section 4.2.

#### 2.2 SENSITIVITY TO UNREACTED EXPLOSIVE YIELD STRENGTH

Two calculations for Composition B were performed in order to determine the sensitivity of the calculated detonation threshold to the value of the yield strength used for the unreacted explosive. For one calculation the yield strength was increased by a factor of 10 over the nominal value of 0.512 kbar (Section 3.2.1), and for the other calculation the yield strength was reduced to zero. There was no discernible effect on the detonation threshold and a negligible, if any, effect on the calculated velocity loss. It should be emphasized that this insensitivity to the value of the yield stress is for an <u>unconfined</u> explosive geometry at a rather high striking velocity. For a cased configuration at lower impact velocities, the value of the yield strength and its effect on the amount of plastic deformation would probably be significant.

#### III. MATERIAL MODELS

#### 3.1 INERT MATERIAL MODEL AND PARAMETERS FOR STEEL

The inert material model employed in HELP includes an equation of state, a deviatoric constitutive relation for elastic and plastic deformations, and a failure criterion, as discussed in the following paragraphs.

For steel, the Tillotson (Reference 5) equation of state, modified to give a smooth transition between compressed and expanded states was used. For compressed states, i.e., when  $\rho/\rho_0 > 1$ , or for any cold states,  $E < E_s$ , where  $E_s$  is the specific internal energy at incipient vaporization, the equation of state has the form

$$P = P_{c} = \left[a + \frac{b}{\frac{E}{E_{0}\xi^{2}} + 1}\right] E\rho + A\eta + B\eta^{2}$$
(3.1)

where  $\xi \equiv \rho/\rho_0$  and  $\eta \equiv \xi - 1$ . For expanded hot states, i.e., when  $\rho/\rho_0 < 1$  and  $E > E'_s$ , the equation of state has the form

$$P = P_{E} = aE\rho + \left[\frac{bE\rho}{\frac{E}{E_{0}\xi^{2}} + 1} + A\eta e^{-\beta \left(\frac{V}{V_{0}} - 1\right)}\right]$$
$$-\alpha \left(\frac{V}{V_{0}} - 1\right)^{2}$$
$$(3.2)$$

A smooth transition between the compressed and expanded states is insured by a transition equation for the intermediate region defined by  $E_s < E < E'_s$  and  $\rho/\rho_0 < 1$ , where  $E'_s$  is the specific internal energy at complete vaporization. This blended portion of the equation of state has the form

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$$P = \frac{(E-E_{s})P_{E} + (E_{s}'-E)P_{c}}{(E_{s}' - E_{s})} .$$
(3.3)

The values of the parameters as used for steel in the above equations are

A = 1280 kbar B = 650 kbar a = 0.5 b = 1.5 E<sub>0</sub> = 9.5 × 10<sup>10</sup> erg/g E<sub>s</sub> = 2.44 × 10<sup>10</sup> erg/g E's = 10.2 × 10<sup>10</sup> erg/g  $\alpha$  = 5.0  $\beta$  = 5.0

The deviatoric stress increments, dS'<sub>ij</sub> are calculated from the elastic relation

 $dS'_{ij} = 2\mu d\varepsilon'_{ij}, \qquad (3.4)$ 

where  $\mu$  is the shear modulus and define are the increments of deviatoric strain. When such an increment of stress causes the von Mises yield criterion,

$$s'_{ij} s'_{ij} \leq 2Y_s^2$$

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to be violated, each stress component is proportionately reduced to bring the stress back (normally) to the yield surface. A variable yield strength

$$Y_{s} = (Y_{0} + Y_{1}\eta + Y_{2}\eta^{2}) (1 - \frac{E}{E_{m}})$$
 (3.5)

can be used to account for the increase in strength at high pressures and the decrease in strength at elevated values of the specific internal energy, where  $E_m$  is the internal energy at the melt point. The values of the parameters as used for steel are

 $\mu = 800 \text{ kbar}$   $Y_0 = 6.0 \text{ kbar}$   $Y_1 = 0$   $Y_2 = 0$  $E_m = 1.3 \times 10^{10} \text{ erg/g}$ 

The failure criterion employed in the HELP code is based upon a minimum allowable compression ratio,  $\eta_{min}$ . When the material in a computational cell is subjected to conditions such that the failure criterion is violated, i.e.,

n < nmin'</pre>

the material is considered failed, and the stresses in that cell are set to zero. For steel, the value used for the minimum compression ratio was

 $\eta_{min} = -0.02$ 

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#### 3.2 HIGH-EXPLOSIVE EQUATION OF STATE

Partially reacted explosive is treated as a mixture of completely reacted and completely unreacted components in pressure equilibrium. Separate equations of state of the general form

 $P_1 = f_1 (\rho_1, E_1)$ 

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$$P_{2} = f_{2} (\rho_{2}, E_{2})$$
(3.6)

are used for the unreacted and reacted components, respectively, where  $\rho_1$ ,  $\rho_2$  and  $E_1$ ,  $E_2$  are the densities and specific internal energies. The equations of state are described in detail in the following sections.

The pressure is calculated as follows: at the end of a computational cycle the overall density  $\rho$  and the specific internal energies of the unreacted and reacted components are known. The general expression relating the overall density to the individual densities of the unreacted and reacted components is

 $\frac{1}{\rho} = \frac{w}{\rho_1} + \frac{(1-w)}{\rho_2} , \qquad (3.7)$ 

where w is the mass fraction of unreacted explosive in the computational cell. The individual densities are varied in an iterative procedure, subject to the above constraint, until the calculated pressures of the unreacted and reacted components are equal. Thus, the determination of the pressure in a cell containing partially reacted high-explosive is formally the same as that for a cell containing a mixture of any other two material constituents, and the computational machinery developed previously for use in the HELP code was immediately applicable. The determination of the mass fraction of unreacted explosive in a computational cell is a two-step procedure. The first possible variation is due to the mass flow into and out of a given cell from neighboring cells with different unreacted mass fractions. This increment is calculated at the same time that the cell mass is updated, a mass-weighted average of the appropriate contributions being used. The second variation is explicit change as calculated from the assumed reaction rate of the explosive decomposition. A separate subroutine was written to perform this part of the update.

3.2.1 Unreacted Composition B

For compressed states,  $\rho > \rho_0$ , a Mie-Gruneisen equation of state was used,

$$P_{c} = f(\rho) + \rho GE, \qquad (3.8)$$

where

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$$f(\rho) = \left(1 - \frac{G}{2} \xi \varepsilon\right) P_{H}(\rho) \qquad (3.9)$$

in terms of the Hugoniot pressure  $P_{\mu}\left(\rho\right)$  , and

$$\xi \equiv \frac{\rho}{\rho} , \quad \varepsilon \equiv 1 - \frac{v}{v_0} . \quad (3.10)$$

The Hugoniot pressure is determined from the straight line  $U_s$ ,  $U_p$  fit,

 $u_{s} = C_{0} + SU_{p}$ , (3.11)

or equivalently,

$$P_{\rm H} = \rho_0 C_0^2 \epsilon / (1 - S\epsilon)^2 . \qquad (3.12)$$

For negative pressures the Hugoniot was extrapolated as a straight line. Values of the parameters in the above equations as obtained from Reference 1 are

$$\rho_0 = 1.715 \text{ g/cm}^3$$
 $C_0 = 2.31 \times 10^5 \text{ cm/sec}$ 
 $S = 1.83$ 
 $G = 1.5$ 

Other parameters as obtained from the Ballistic Research Laboratories (Reference 6) are the shear modulus,

 $\mu = 50.3$  kbar

the yield stress in simple tension of

 $Y_{\rm T} = 0.887$  kbar

from which the von Mises yield criterion is

 $Y_{s} = Y_{T}^{1}/\sqrt{3} = 0.512$  kbar,

and the tensile strength of

0

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 $-S^* = 0.1042$  kbar.

The volumetric strain at failure as used in the HELP code is

then

$$\varepsilon_{\min} = S^* / (\rho_0 C_0^2) = - 0.00114$$

For expanded hot states the equation of state used was

$$P_{E} = \rho GE + \rho_{0} C_{0}^{2} \left(\frac{\rho}{\rho_{0}} - 1\right) \exp \left[-\beta \left(\frac{V}{V_{0}} - 1\right)\right]$$

$$\times \exp \left[-\alpha \left(\frac{V}{V_{0}} - 1\right)^{2}\right] . \qquad (3.13)$$

For intermediate states, the blend as described in Section 3.1 was used. For Composition B, the energy at the melt point was taken as

$$E_{m} = 8.29 \times 10^{8} \text{ erg/g}$$

and the energy at incipient vaporization and complete vaporization were estimated as

$$E_{e} = 9.19 \times 10^{9} \text{ erg/g}$$

$$E'_{=} = 3.0 \times 10^{10} \text{ erg/g}$$

The standard values  $\alpha = \beta = 5.0$  were used in Equation (3.13).

## 3.2.2 Unreacted PBX-9404

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The Mie-Gruneisen equation of state, as described in the preceding section, was also used for compressed states of PBX-9404. Values of the parameters as obtained from Reference 7 are

$$\rho_0 = 1.83 \text{ g/cm}^3$$
  
 $C_0 = 2.423 \times 10^5 \text{ cm/sec}$   
 $S = 1.883$   
 $G = 0.675$ 

The shear modulus, as calculated from the shear wave velocity of  $1.62 \times 10^5$  cm/sec (Reference 8) is

$$\mu = \rho_0 C_t^2 = 48.0$$
 kbar.

The form of the expanded phase equation of state was taken to be the same as that for Composition B, Equation (3.13), with  $\alpha = \beta = 5.0$ . The melt temperature was taken as 280°C, which together with specific heat data from Reference 9 gives for the energy at melt,

$$E_{\rm m} = 3.21 \times 10^9 \, {\rm erg/g}.$$

The energies for incipient vaporization and complete vaporization were estimated as

$$E_s = 1.16 \times 10^{10} \text{ erg/g}$$
  
 $E_s' = 3.25 \times 10^{10} \text{ erg/g}$ 

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The yield and failure parameters were taken to be the same as those for Composition B, i.e., the shear yield stress for use in the von Mises yield criterion is

$$Y_{s} = 0.512$$
 kbar,

and the tensile strength as

$$-S^* = 0.1042$$
 kbar.

The resulting volumetric strain at failure is then

$$\epsilon_{\min} = S^* / (\rho_0 C_0^2) = - 0.00097$$

3.2.3 Reacted Composition B

The Jones-Wilkins-Lee (JWL) equation of state was used for both Composition B and PBX-9404 for the completely reacted state. It had already been coded for use in the HELP code and is of the form

$$P = A \left(1 - \frac{\omega}{R_1 V}\right) \exp \left(-R_1 V\right) + B \left(1 - \frac{\omega}{R_2 V}\right) \exp \left(-R_2 V\right)$$
$$+ \frac{\omega E}{V}, \qquad (3.14)$$

where V is the volume of the detonation products relative to that of the undetonated explosive, and E is the internal energy per  $cm^3$  of undetonated explosive.

The values of the parameters for Composition B as taken from Reference 10 are

$$A = 5.242 \text{ Mbar}$$

B = 0.07678 Mbar  $R_1 = 4.20$   $R_2 = 1.10$   $\omega = 0.34$  $E_0 = 0.085$  Mbar-cc/cc

3.2.4 Reacted PBX-9404

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The parameters for the JWL equation of state as obtained from Reference 10 are

A = 8.545 Mbar B = 0.2049 Mbar R<sub>1</sub> = 4.60 R<sub>2</sub> = 1.35  $\omega$  = 0.25 E<sub>0</sub> = 0.102 Mbar-cc/cc

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#### IV. REACTION-RATE MODEL

#### 4.1 FOREST FIRE REACTION-RATE MODEL

A brief description of the model is given here; a detailed discussion is given by Mader and Forest (Reference 1).

The basic assumption is that the build-up to complete detonation takes place along a unique curve in distance, time and state space, regardless of the initial driving pressure. The shock pressure as a function of distance run is then given by the so-called "Pop plot", which is a fit to the experimental data for initial shock pressure as a function of run to detonation. The Pop plot for Composition B is shown in Figure 4 along with the assumed growth of the shock pressure as complete detonation is approached. A second assumption, as indicated in Figure 4, is that the pressure gradient immediately behind the shock front is zero.

The additional information required for the determination of the reaction rates are the Hugoniot curve for shocks to the intermediate, partially reacted states, and an equation of state of the form

$$P = f(\rho, E, w),$$
 (4.1)

where  $\rho$  is the density, E the specific internal energy, w the mass fraction of unreacted explosive. The calculational procedure is as follows:

For a given shock pressure  $P_{H}$ , the experimental curve of U<sub>s</sub> versus U<sub>D</sub> for the partially reacted Hugoniot,

$$U_{s} = C + S'U_{p},$$
 (4.2)

and the Hugoniot relations are used to determine the state at the shock front,

$$P_{H} = \rho_{0} U_{s} U_{p} = \rho_{0} (C + s' U_{p}) U_{p}$$
(4.3)



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$$W_{\rm H} = V_0 (U_{\rm s} - U_{\rm p}) / U_{\rm s}$$
 (4.4)

$$E_{\rm H} = \frac{1}{2} U_{\rm p}^2 . \tag{4.5}$$

These values are used with the equation of state to determine the mass fraction of unreacted explosive at the shock front,

$$P_{\rm H} = f (\rho_{\rm H}, E_{\rm H}, w_{\rm H}).$$
 (4.6)

The reaction rate itself is then obtained from the Lagrangian time derivative of the above expression,

$$\left(\frac{\partial P}{\partial t}\right)_{m} = f_{1} \left(\frac{\partial \rho}{\partial t}\right)_{m} + f_{2} \left(\frac{\partial E}{\partial t}\right)_{m} + f_{3} \left(\frac{\partial w}{\partial t}\right)_{m}, \qquad (4.7)$$

where the subscript m denotes the time derivative at a fixed mass element, and  $f_{1,2,3}$  are the partial derivatives of the equation of state function with respect to its arguments.

At this point, the assumption of a zero pressure gradient at the shock front is used to evaluate the partial derivatives. The general expression

$$\left(\frac{\partial P}{\partial t}\right)_{m} \equiv \left(\frac{\partial P}{\partial t}\right)_{x} + \left(\frac{\partial P}{\partial x}\right)_{t} \left(\frac{\partial x}{\partial t}\right)_{m}$$

reduces to

$$\left(\frac{\partial P}{\partial t}\right)_{m} = \left(\frac{\partial P}{\partial t}\right)_{x} = \frac{dP_{H}}{dt} = -\frac{dP_{H}}{dR} U_{s}$$
(4.8)

where the derivatives of the Hugoniot pressure with respect to R (run to detonation) is obtained from the Pop plot. The Lagrangian equation for conservation of momentum

$$\left(\frac{\partial \mathbf{u}}{\partial \mathbf{t}}\right)_{\mathbf{m}} = - \left(\frac{\partial \mathbf{P}}{\partial \mathbf{m}}\right)_{\mathbf{t}} = \mathbf{0}$$

allows one to write for the rate of change of particle velocity at the shock front

$$\frac{dU_{p}}{dt} \equiv \left(\frac{\partial u}{\partial t}\right)_{m} + \left(\frac{\partial u}{\partial m}\right)_{t} \frac{dm}{dt} = \rho_{0}U_{s} \left(\frac{\partial u}{\partial m}\right)_{t}, \qquad (4.9)$$

and the Lagrangian equation for conservation of mass yields

$$\left(\frac{\partial V}{\partial t}\right)_{m} = \left(\frac{\partial u}{\partial m}\right)_{t} = \frac{1}{\rho_{0} U_{s}} \frac{dU_{p}}{dt}, \qquad (4.10)$$

for use in Equation (4.7), where the time derivative on the right in the above expression is evaluated from the pressure time derivative by

$$\frac{dU_{p}}{dt} = V_{0} \frac{dP_{H}}{dt} / (S'U_{p} + U_{s}).$$
 (4.11)

The energy derivative in Equation (4.7) is obtained from the Lagrangian equation for conservation of energy,

$$\left(\frac{\partial E}{\partial t}\right)_{m} = -P \left(\frac{\partial V}{\partial t}\right)_{m} = -P_{H} \left(\frac{\partial V}{\partial t}\right)_{m} . \qquad (4.12)$$

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## 4.2 SENSITIVITY OF REACTION RATE TO EQUATION OF STATE

Since the Forest Fire reaction rates were obtained using the HOM equation of state (Reference 4) in Equation (4.1) to evaluate the pressure for a partially reacted state, it seemed worthwhile to recompute them using the HELP models in order to check the sensitivity to variations in the explosive equation of state. Such a calculation was done for Composition B.

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As a first step, the Fortran lisings given in Reference 1 were punched, and the program was run using the original HOM equation of state in order to insure that there were no coding errors. The reaction rates for Composition B were then recalculated using the equation of state models described in Section III and the appropriate subroutines from the HELP code. Comparison of Hugoniots for several unreacted mass fractions is given in Figure 5, and a comparison of the reaction rates as calculated from the two equations of state is given in Figure 6. As the figure shows, the differences of the equations of state are enough to very nearly account for the factor of 1.5 necessary to bring the experimental and calculated detonation thresholds for Composition B into agreement.



Figure 5. A comparison of several Hugoniots for Composition B as given by the HOM equation of state and the models used in the HELP code calculation, where w is the mass fraction of unreacted explosive.

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Figure 6. Comparison of Forest Fire reaction rates for Composition B as calculated with the HOM equation of state and the HELP equation of state models.

#### V. CONCLUSIONS

For the explosives PBX-9404 and Composition B the use of the equation-of-state models presented here and the Forest Fire reaction rates (modified for Composition B to account for the sensitivity to the equation of state) results in good agreement between calculated and observed velocity losses and detonation thresholds for the penetration of unconfined explosive slabs by steel spheres. The reaction-rate model (Reference 1), which was published after the start of the present contract, has also been used with success at the Los Alamos Scientific Laboratory to describe the detonation process in heterogeneous explosives.

However, as pointed out in Reference 1, the use of this reaction-rate model is not realistic at very low pressures. For example, in the calculations reported here, the reaction rates are assumed to be a function of pressure only, and they are set to zero for pressures less than 15 kbar in PBX-9404 and 20 kbar in Composition B. Consequently, the model as described here would not be useful for confined geometries at low pressures, in which the explosive has a chance to "cook", or for configuration in which the initial heating is due principally to plastic deformation associated with macroscopic shear.

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