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AFAL-TR-77-74

SOLAR CELL DESIGN STUDY

CENTER FOR THE SYNTHESIS AND STUDY OF SEMICONDUCTING COMPOUNDS (CSSSC) RESEARCH TRIANGLE INSTITUTE RESEARCH TRIANGLE PARK, N.C. 27709



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FOREWORD

This report was prepared by the Center for the Synthesis and Study of Semiconducting Compounds (CSSSC), Research Triangle Institute, Research Triangle Park, North Carolina, under Air Force Contract No. F33615-76-C-1283. The contract was administered under the direction of the Air Force Avionics Laboratory, Wright-Patterson Air Force Base, Ohio. Mr. Russell W. Runnels (AFAL/DHO-3) was the Air Force Project Engineer.

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LIST OF SYMBOLS

	2
D	minority carrier diffusion coefficient, cm ² /sec
E _G	bandgap values, volts (eV)
E	electric field strength, volt/cm
F	V-I Solar Cell Fill Factor
g	minority carrier generation rate, $cm^{-3} sec^{-1}$
J sc	short circuit current density, ma/cm ²
Jmax	terminal current density at maximum power, ma/cm ²
J	diode saturation current density, ma/cm ²
J	minority carrier current density, ma/cm ²
JJ	minority carrier current density to the dark current, ma/cm^2
k	Boltzman constant, 1.38x10 ⁻²³ joules/K
L	minority carrier diffusion length, cm
n _{po} ,	
n,p	excess minority carrier electron or hole concentration, cm^{-3}
ⁿ i	intrinsic carrier concentration, cm^{-3}
ND	donor concentration in n-type material, cm^{-3}
NA	acceptor concentration in p material, cm^{-3}
No	incident solar photon flux, cm ⁻² sec ⁻¹ λ^{-1}
-P _{ma}	maximum power
q	electronic charge, 1.óx10 ⁻¹⁹ coulombs
R	reflectivity at x=0 surface
s	surface recombination velocity, cm/sec
s _c	bottom contact recombination velocity, cm/sec
т	temperature, kelvin

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LIST OF SYMBOLS (continued)

v _{0c}	open circuit voltage, volts
V _{max}	terminal voltage at maximum power, volts
x _i -x _{i-x}	thickness of ith layer, cm
μ	minority carrier mobility, cm ² /volt sec
τ	minority carrier lifetime, sec
λ	wavelength µm
λ _c	band gap cut-off wavelength, μm
α	absorption coefficient, cm^{-1}
$\Delta \mathbf{E}$	band edge discontinuity, volts (eV)
^C _{i1} , ^C _{i2}	constants of integration of ith layer, cm^{-3}

Subscripts

P	associated with minority hole carrier properties in n-type material
n	associated with minority electron carrier properties in p-type material
1,2,3,4	refers to parameters of layer 1, 2, 3, or 4, respectively.

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1.0 INTRODUCTION

The purpose of this work has been 1) to review the present state-ofthe-art of III-V solar cells and 2) to determine which III-V materials and solar cell designs can be advanced most effectively in the development of high efficiency solar cells for use in the near-earth space environment. This work has been accomplished through extensive literature surveys, in-house modeling and design optimization studies, and evaluation of the design tradeoffs and technical risks associated with the development and fabrication of specific material systems and device configurations.

In general, III-V compound semiconductors exhibit electrical and optical properties of considerable promise for photovoltaic conversion applications, and several of these compounds are prominent among the alternatives to silicon. The principal advantages of III-V solar cells over silicon cells are the higher theoretical efficiency values, increased radiation resistance, and improved high temperature performance. Because of these features, considerable effort has recently been directed toward the design, development, and fabrication of cells using III-V materials. Theoretical and experimental studies have resulted in a variety of proposed cell designs and III-V material combinations. Added impetus to these efforts has been provided by recent advances in III-V technology associated with the development of microwave and laser devices.

During this study consideration has been given to a number of III-V binary, ternary, and quaternary alloys having properties deemed particularly attractive to a specific solar cell configuration or fabrication process.

Special emphasis was placed on the following materials: GaAs, GaP, $Ga_xAl_{1-x}As$, $GaAs_xP_{1-x}$, $Ga_xIn_{1-x}As$, and $Ga_xAl_{1-x}Sb$. Typically, alloy ratios (x) were varied in order to determine the optimum bandgap for the solar spectrum or to optimize lattice match between dissimilar alloys. In general, GaAs served as a reasonably well-characterized base material for comparison with other III-V compounds. Solar cell configurations evaluated included homojunctions, heterojunctions, Schottky barriers, graded-structures, and multi-junction or cascaded devices.

Section 2.0 reviews homojunction, heterojunction and graded bandgap cells and presents the results of optimization studies on heterojunction and graded bandgap devices. Schottky barrier and MIS cells are discussed in Section 3.0, which also includes the results of optimum Schottky barrier performance calculations. Section 4.0 outlines a closed form analytical technique developed to calculate solar cell characteristics. This technique is then used in the development of optimized "potential well" and "cascade" configurations as presented in Section 5.0 and 6.0, respectively. A comparative assessment of the major III-V material and solar cell configurations is then summarized in Section 7.0.

2.0 BASIC SINGLE JUNCTION SOLAR CELL STRUCTURES

2.1 Homojunction Devices

A homojunction solar cell is a device consisting of a single semiconductor material and having a single p-n junction. For many years this was the only device considered for solar cells and the silicon homojunction solar cell remains to date the most successful solar cell.

A cross sectional view of the typical homojunction solar cell is shown in Figure 2.1. The important elements of the cell are (1) the anti-reflecting layer to reduce optical losses at the surface, (2) the collecting p-n junction located near the surface and (3) ohmic contacts to both the back surface (shown) and the front surface (not shown). Because the diffusion length for electrons is longer in most materials than the diffusion length for holes, cells with an n^+ layer near the surface are typically of higher efficiency than p^+ -n cells.

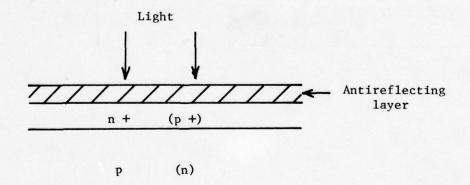


Figure 2.1. Homojunction Solar Cell

The efficiency of a solar cell is determined by the terminal parameters of short circuit current (I_{SC}) , open circuit voltage (V_{OC}) and fill factor

(F) in an equation of the form

$$\eta = \frac{I_{SC} \cdot V_{OC} \cdot F}{P_{O}} , \qquad (2-1)$$

where P_0 is the incident optical power. In achieving maximum efficiency, the product $I_{SC} \cdot V_{OC} \cdot F$ should be maximized for a given cell design. The maximization of efficiency is not easily achieved because of the cell's internal competing process giving rise to rather complex relationships on which the terminal characteristics depend. Ideally, the maximum power point on the solar cell V-I curve should be maximized. This is equivalent to maximizing the product given in Eq. (2-1).

The internal steady-state operation of any semiconductor device is governed by the device equations given by

$$J_n = q\mu_n nE + qD_n \frac{dn}{dx} , \qquad (2-2)$$

$$J_{p} = q\mu_{p}PE - qD_{p}\frac{dp}{dx}, \qquad (2-3)$$

$$0 = G_{e} - U + \frac{1}{q} \frac{dJ_{n}}{dx}, \qquad (2-4)$$

$$0 = G_{e} - U - \frac{1}{q} \frac{dJ_{p}}{dx} , \qquad (2-5)$$

$$\frac{dE}{dx} = \frac{q}{\varepsilon} (n-p + N_N) . \qquad (2-6)$$

In these equations N_{N} is the net impurity doping density, U is the internal recombination rate which is usually modeled by the Shockley-Read-Hall theory of

$$U = \frac{pn - n_i^2}{\tau_{no}(p + p_1) + \tau_{po}(n + n_1)} , \qquad (2-7)$$

and G is the external optical generation of

$$G_e = \int T\alpha N_p \exp(-\alpha x) d\lambda$$
, (2-8)

where T is the transmission coefficient, α is the absorption coefficient and N is the incident photon density per wavelength interval. The solution of this set of equations with appropriate boundary conditions give relationships between internal device parameters and the terminal characteristics.

Many of the major factors influencing steady state solar cell operation can be seen from expressing Equations (2-2) and (2-3) in integral form. Equation (2-2) is applied to the p-type side of the p-n junction while Equation (2-3) is applied to the n-type side of the p-n junction. The integrals lead to the equation for the terminal current represented by

$$J = \int_{e}^{b} G_{e} dx - q \int_{e}^{b} \frac{\Delta n}{\tau_{n}} dx - q \int_{e}^{b} \frac{\Delta p}{\tau_{p}} dx - q \int_{e}^{b} U dx - J_{ns} - J_{ps} .$$
 (2-9)
entire pregion n region depletion
device region

Each term on the right can be related to specific physical processes within the solar cell. The $\int G_e dx$ term across the entire device gives the available optically generated current in the absence of any losses. The second and third terms represent the integrated electron and hole recombination losses in the p- and n-region, respectively. In these integrals the recombination rate, has been replaced by $\Delta p/\tau_p$ or $\Delta n/\tau_n$, where $\Delta n, \tau_n$ and $\Delta p, \tau_p$ are the excess carrier densities and the corresponding lifetimes in the p- and n-region, respectively. The term /Udx is the depletion region loss. The final two terms J_{ns} and J_{ps} represent surface recombination currents at the p- and n-type surfaces, respectively, corresponding to the back and front surfaces

in Figure 1. These terms are usually expressed as $q\Delta p \underset{s p}{S}$ and $q\Delta n \underset{s n}{S}$, where Δn_s , $\underset{n}{S}$ and Δp_s , $\underset{p}{S}$ are the surface excess carrier densities and surface recombination velocities at the p- and n-type surfaces, respectively.

In order to obtain a large external current it is obvious from Equation (2-9) that the $\int G_{e} dx$ should be as large as possible and all recombination losses - bulk, depletion and surface - should be minimized. Equation (2-9) explicitly shows the importance of generation rate, lifetime and widths of the various regions on terminal current. However, several other important factors are not explicitly shown. Under forward bias conditions, the Δp and Δn terms in a solar cell can be thought of as arising from two sources. One contribution comes from the optical carrier generation rate, and a second contribution comes from the forward bias of the p-n junction. It is the forward bias contribution to Δn and Δp which constitutes the dark current. The dependency of this term on voltage is obtained from an approximate analytical solution or from a numerical solution of the device equations with G_{e} equal to zero [(Equations (2-2) to (2-6)].

Consider the excess carrier densities as expressed in terms of a contribution from the incident solar flux and a contribution from the terminal voltage as¹

$$\Delta \mathbf{p} = \Delta \mathbf{p}_{\mathrm{L}} + \Delta \mathbf{p}_{\mathrm{V}} \tag{2-10}$$

$$\Delta n = \Delta n_{\rm r} + \Delta n_{\rm w} \tag{2-11}$$

where the subscript L indicates the solar flux contribution and V indicates

¹These equations are exact representations only when superposition of solar flux and voltage effects holds for the transport equations. Linearity of the basic equations holds only at low injection levels and/or low light levels and thus these equations are not always valid. However, they can be used to illustrate the approximate dependence of solar cell properties on device parameters.

the voltage contribution. Then Equation (2-9) becomes of the form

$$J = J_{SC} - J_D(V)$$
, (2-12)

where $\boldsymbol{J}_{\mbox{SC}}$ is the short circuit current expressed as

$$J_{SC} = \int G_e \, dx - q \int \frac{\Delta p_L}{\tau_p} \, dx - q \int \frac{\Delta n_L}{\tau_n} \, dx - q \int U_L \, dx$$

entire n-region p-region depletion region
device

$$- q \Delta p_{LS} S_{p} - q \Delta n_{LS} S_{n} , \qquad (2-13)$$

and $\boldsymbol{J}_{D}^{}\left(\boldsymbol{V}\right)$ is the dark current expressed as

$$J_{D}(V) = J_{n}(V) + J_{p}(V) + J_{u}(V)$$
, (2-14)

with

$$J_n(V) = dark$$
 current contribution from n-type region

$$= q \int \frac{\Delta p_{v}}{\tau_{p}} dx + q \Delta p_{vs} S_{p} , \qquad (2-15)$$

n region

 $J_n(V)$ = dark current contribution from p-type region

$$= q \int \frac{\Delta n_v}{\tau_n} dx + q \Delta n_{vs} S_n , \qquad (2-16)$$

p-region

 $J_{ij}(V)$ = dark current contribution from depletion region

$$= q \int_{v} U_{v} dx .$$
 (2-17)
depletion region

The current contributions from the n- and p-type regions are seen to arise from two terms — bulk recombination and surface recombination.

Equations (2-13) to (2-17) aid in the identification of the important solar cell parameters for single p-n junction solar cells. In general, the short circuit current should be maximized and the dark forward current minimized. The important parameters which influence short circuit current are

1. Solar spectrum

- 2. Transmission efficiency
- 3. Absorption coefficient
- 4. Lifetime in n- and p-regions and in the depletion region
- 5. Doping density and doping gradients
- 6. Diffusion coefficient and mobility
- 7. Thicknesses of n- and p-type regions and depletion region

8. Surface recombination

Of these factors, the solar spectrum and absorption coefficient are fixed for a given cell design and semiconductor material. The diffusion coefficient and mobility are also fixed once a doping density profile is selected. Thus to maximize efficiency for a given material the device designer has at his disposal the transmission efficiency into the semiconductor, the doping densities, thicknesses of the layers and perhaps lifetime. The doping density, mobility and diffusion coefficient dependence is not

explicitly shown in Equation (2-13). However, it is obvious from the basic device equations [(Equations (2-2) to (2-6)] that Δn and Δp depend on these parameters.

The important parameters determining dark current for a given material are

1. Lifetime in the n- and p-type regions and in the depletion region

2. Doping density and doping gradients

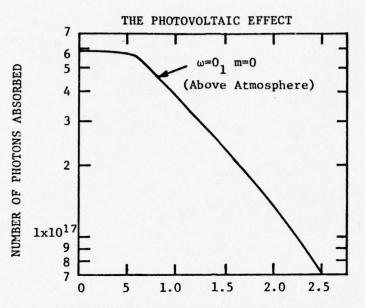
3. Diffusion coefficients and mobility

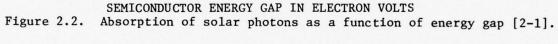
- 4. Thicknesses of n- and p-type regions and depletion region
- 5. Surface recombination

6. Terminal voltage

These parameters are all included in the list for short circuit current parameters except for the terminal voltage.

The parameters discussed above are those which influence solar cell performance for a given semiconductor material. When the broad spectrum of available semiconductor materials is considered the bandgap of the semiconductor becomes one of the dominant factors determining efficiency. The energy bandgap is important for two reasons. First, it determines the optical absorption edge and to a large extent the absorption coefficient. This in turn determines the maximum available optical current from the $fG_e^{}$ dx term. As the bandgap is increased the available optical current decreases as less photons which are capable of producing electron-hole pairs are absorbed in the material. This is illustrated in Figure 2.2 which shows the number of photons absorbed as a function of energy gap for an AMO spectrum [2-1]. This effect alone tends to decrease efficiency as the energy bandgap is increased.





The second major effect of increasing the bandgap is a reduction in the dark current. The ideal dark current density for a p-n junction which has regions on each side of the junction which are wide compared with a diffusion length is

$$J_{\rm D}(V) = J_{\rm O} \left[\exp \left(\frac{qV}{kT} \right) - 1 \right],$$
 (2-18)

where

$$J_{0} = qn_{i}^{2} \left[\frac{1}{N_{D}} \sqrt{D_{p}/\tau_{p}} + \frac{1}{N_{A}} \sqrt{D_{n}/\tau_{n}} \right] . \qquad (2-19)$$

In the above N_D is the donor density on the n-side and N_A is the acceptor density on the p-side. The bandgap enters through the n_i^2 term as

$$n_i^2 = N_c N_v \exp(-E_g/kT)$$
, (2-20)

where N_c and N_v are the conduction and valence bands effective density of states, respectively.

The open circuit voltage is determined from the dark current density, short circuit current density, and temperature as

$$V_{\rm OC} \simeq \frac{kT}{q} \ln \left(\frac{J_{\rm SC}}{J_{\rm O}}\right)$$
 (2-21)

In terms of the semiconductor bandgap this can be expressed as

$$V_{\rm OC} = \frac{E_g}{q} - \frac{kT}{q} \ln \left(\frac{J_{\rm OO}}{J_{\rm SC}}\right)$$
, (2-22)

where

$$J_{00} = qN_{c}N_{v} \left[\frac{1}{N_{D}} \sqrt{D_{p}/\tau_{p}} + \frac{1}{N_{A}} \sqrt{D_{n}/\tau_{n}}\right] .$$
(2-23)

This illustrates the direct dependence of open circuit voltage on bandgap (all other factors being constant). Thus, the general trend with increasing bandgap is for the short circuit current to decrease, but for the open circuit voltage to increase. These two effects cause overall cell efficiency to peak at some particular bandgap.

The above idealized discussion has to be modified somewhat for actual solar cells. First, many solar cell designs have a surface layer thickness which is less than a diffusion length. This modifies the dark current expression [(Equation (2-19)] and introduces the surface recombination velocity into the analysis as a design parameter. This however does not affect the dependence of J_0 on n_i^2 as in Equation (2-19) but does change the factor multiplying n_i^2 .

Another factor which has to be considered for real devices and especially for wide bandgap materials is the non-ideal components of dark current such as depletion region current as expressed in Equation (2-17). The depletion region current tends to become the dominant dark current component in wide bandgap materials. Under many conditions, the depletion region current can be approximated as

$$J_{U} \simeq \frac{qn_{i}W_{J}}{(\tau_{po} + \tau_{no})} \exp (qV/2kT) , \qquad (2-24)$$

where W_J is the width of the junction depletion region. When this is the dominant component of dark current the open circuit voltage can be expressed as

$$V_{OC} \simeq \frac{E_g}{q} - \frac{2kT}{q} \ln \left(\frac{J_{OO}}{J_{SC}}\right) , \qquad (2-25)$$

with

$$J_{00} = \frac{q\sqrt{N_cN_v}}{(\tau_{po} + \tau_{no})} \frac{W_J}{(\tau_{po} + \tau_{no})} .$$
 (2-26)

This has a similar dependence on bandgap as for the ideal diffusion current. However the magnitude of the open circuit voltage is reduced when the depletion region current dominates the dark current. Also, the fill factor is reduced when the current exhibits the exp (qV/2kT) dependency.

The peak efficiency of homojunction solar cells has been studied by many investigators [2-2]. The maximum available efficiency for homojunctions as a function of the bandgap of the semiconductor has also been calculated many times. The results of five reported studies are shown in Figures 2.3 through 2.7. The major predictions of the various curves are very similar although the details vary somewhat depending on the assumptions made in the calculations. Figure 2.3 shows an early calculation by Prince [2-3] which predicts a maximum efficiency of about 22.5% at a bandgap of around 1.3 eV.* The curves shown in Figures 2.3 through 2.7 show peak efficiency

The calculated power density values in Figure 2.3 can be divided by the assumed solar power density of 108 mW/cm² to obtain the corresponding efficiency values.

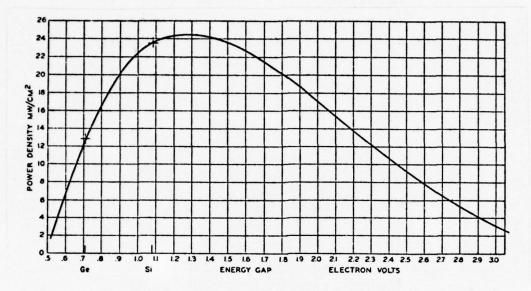
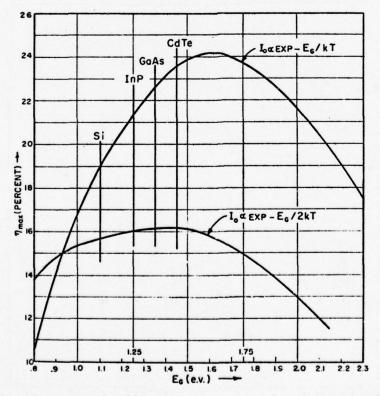
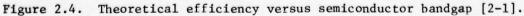


Figure 2.3. Maximum converted power density in bright sunlight as a function of energy gap of semiconductor [2-3].





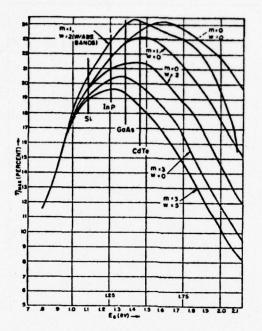
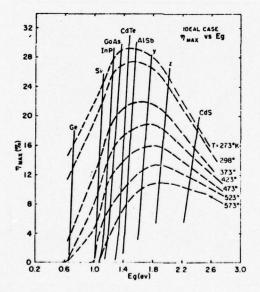
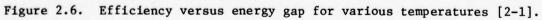


Figure 2.5. Maximum efficiency for different optical spectra conditions [2-4].





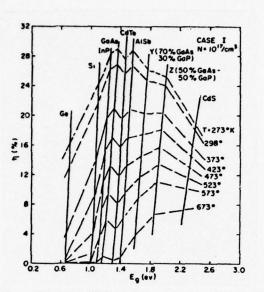


Figure 2.7. Ideal efficiency versus energy gap [2-5].

values at room temperature of about 22% to 27% with the energy at which the peak occurs ranging from about 1.3 eV to about 1.6 eV. These differences are due to different assumptions in the various models with regard to lifetime, optimum doping densities, etc.

All of the reported studies of peak efficiency as a function of bandgap contain certain important assumptions and approximations which should be understood. First, the calculations typically assume that all of the available photons above the bandgap create electron-hole pairs which are collected by the p-n junction. This over-estimates the short circuit current because of the neglect of reflection losses at the surface and internal recombination processes. Second, the calculations typically assume that the dark current is an ideal diffusion current. The lower curve in Figure 2.4 shows calculated values when the depletion region recombination current is assumed to dominate the dark current. This is seen to reduce considerably the peak efficiency for wide bandgap cells

resulting in a peak efficiency of only about 16% at a bandgap of about 1.4 eV. Finally, in making the calculations, assumptions must be made with respect to diffusion coefficients, lifetimes and doping densities. The selection of lifetime values is especially difficult because it varies greatly from one material to another and with doping density. For example, the lifetime in direct bandgap semiconductors such as GaAs and other III-V materials is typically much lower than in indirect bandgap semiconductors such as Si and Ge. These differences are not taken into account in most of the reported efficiency calculations.

Figure 2.5 includes calculated efficiency values for different solar spectra conditions incident on a cell. The curves from m = 0, w = 0 to m = 3, w = 5 show calculated efficiency values corresponding to increasing losses within the atmosphere. The peak efficiency and the bandgap at which the peak occurs is seen to both decrease with increasing absorption in the atmosphere.

Figures 2.6 and 2.7 show the effects of temperature on predicted efficiencies. Increasing the temperature lowers the available efficiency and shifts the bandgap energy for peak efficiency to larger values. This reduction in efficiency with increasing temperatures is due largely to a decreasing open circuit voltage [(see Equation (2-22)] with temperature.

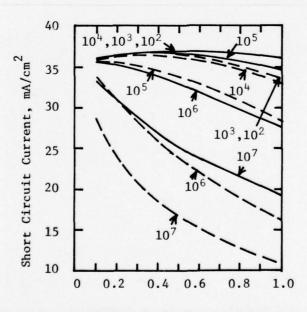
The approximations made in obtaining the peak efficiency curves of Figures 2.3 to 2.7 are such that the predicted values tend to be considerably larger than experimentally observed values. The various curves predict about 19%-20% for silicon and after many years of work the peak efficiencies are beginning to pass the 15%-16% range [2-6]. The second most extensively studied homojunction cell is the GaAs cell. The best efficiencies which

have been obtained to date for GaAs homojunction cells are around 11%-12% for AMO conditions [2-6]. Thus the actual efficiencies of homojunction cells remains considerably below the ideal efficiency calculations. The major reasons for this are now briefly discussed.

In terms of the terminal properties, low short circuit current and low open circuit voltage are the two major causes of the reduced efficiency of homojunction solar cells. The short circuit current can be low because of optical losses at the surface and because of internal carrier recombination. Surface optical losses occur because of reflection from or absorption within the anti-reflecting layer. With a single layer anti-reflection film, surface optical losses are typically 10%-15% of the available photons. This loss has been reduced in silicon cells through the use of multiple layer antireflection films and textured surfaces. Similar techniques have not been developed for GaAs and other III-V homojunction cells.

Internal to the solar cell, short circuit current losses occur from bulk recombination, depletion region recombination, and surface recombination. These losses are all directly related to bulk lifetime and surface lifetime. Fundamental differences exist in terms of internal losses between direct bandgap and indirect bandgap semiconductors. First for indirect bandgap materials such as Si and GaP, the optical absorption coefficient increases rather slowly for photon energies above the bandedge. This causes appreciable carrier generation to occur deep within the semiconductor to depths of several hundred µm in silicon, for example. On the other hand, for direct bandgap materials the absorption coefficient increases much faster and carrier generation occurs much closer to the surface - in about 10 µm of GaAs for example.

Design considerations for maximum short circuit current are somewhat different depending on whether the semiconductor is a direct or indirect bandgap material. For the indirect bandgap designs, the diffusion length and material thickness must be much larger than for the direct bandgap designs. When using indirect materials, the base layer becomes of major importance in achieving a high short circuit current. Losses to recombination at the back contact become important and these are minimized in silicon cells by the use of a back surface field or high-low junction at the back contact. For direct bandgap cells, the region near the surface becomes of dominant importance. The lifetime and thickness of the thin surface layer (see Figure 2-1) becomes very important. Also surface recombination becomes much more important than for the indirect bandgap cells. Figure 2.8 shows calculated short circuit current for p on n GaAs cells as a function of p-n junction depth at various surface recombination velocities [2-7]. A



Junction Depth (µm)

Figure 2.8. Calculated AMO short circuit current for p or n GaAs solar cells [2-7].

surface recombination velocity in the range of 10^6 cm/sec, as is typical of a GaAs surface, is seen to greatly reduce the short circuit current unless the junction depth is below 0.1 μ m.

Low open circuit voltages are caused both by low short circuit currents and by high dark currents. The major factors determining dark current have been presented in Equation (2-14). Low dark currents require long bulk lifetimes and low surface recombination velocities. One of the major factors increasing the dark current in wide bandgap semiconductors is the junction depletion region recombination. This is typically identified as a dark current which varies with voltage as exp (qV/2kT). Figure 2.4 shows that when this current component dominates the theoretical efficiency is greatly reduced. This non-ideal current reduces the fill factor as well as reducing the open circuit voltage. Figure 2.9 illustrates how the efficiency versus bandgap might appear when account is taken of the change from an ideal diffusion current for small bandgaps to purely depletion region current for wide bandgap semiconductors. Silicon p-n junctions can be readily fabricated in which the dark current is essentially the ideal current around the open circuit voltage value. GaAs diodes typically tend to be dominated by depletion region recombination current. However, devices have recently been built in which it appears that the ideal current dominates near open circuit voltage conditions [2-7]. As discussed by Hovel [2-7], this appears to require diffusion lengths of 3 µm or more.

The major differences between the ideal and the experimentally realized efficiencies of homojunction cells appear to be understood. The major problems are achieving conditions sufficiently close to the ideal conditions

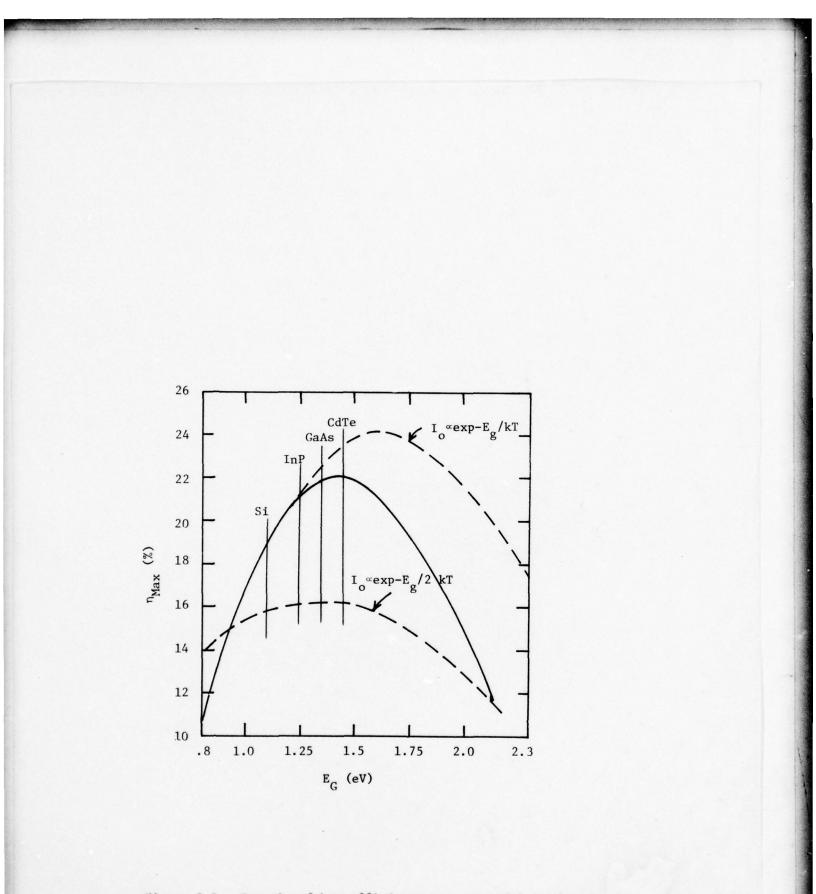
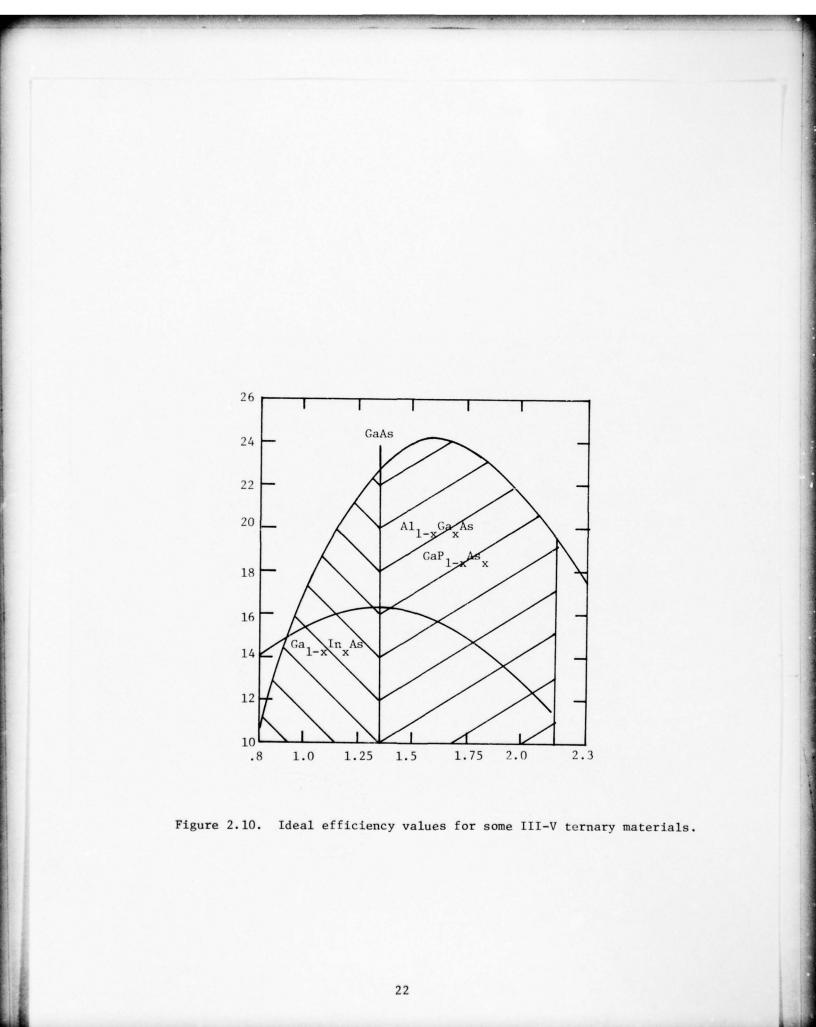


Figure 2.9. Example of how efficiency may vary with bandgap as dark current changes from the ideal diffusion current to depletion region recombination.

to approach the theoretical values given in Figures 2.4 through 2.7. Because of the presence of depletion region current in wide bandgap devices the maximum efficiency for homojunction cells almost certainly occurs at a bandgap value below the 1.3 eV to 1.6 eV value shown in Figures 2.4 to 2.7. Thus for operation near room temperature there is probably little reason to explore III-V materials with bandgaps larger than GaAs. For high temperature operation (above 100°C) other materials may have somewhat higher efficiencies as seen from Figures 2.6 and 2.7.

Of the binary III-V semiconductors, only AlSb (1.52 eV bandgap), GaAs (1.44 eV bandgap) and InP (1.34 eV bandgap) have bandgap values close to that predicted for maximum efficiency. GaAs is the natural material because it is close to the peak efficiency and because of the advanced state of technology. Of the other two materials only InP appears to be worthy of further study because of its slightly smaller energy bandgap. As the materials technology for InP advances, it should probably be looked at more seriously as a solar cell material.

There are a large number of ternary III-V materials for possible homojunction solar cells. Of these materials those with bandgaps slightly above or slightly below GaAs appear to have the most promise for solar cells. The most extensively studied of these are $Al_{1-x}Ga_xAs$, $GaP_{1-x}As_x$ and $Ga_{1-x}In_xAs$. The first two have similar properties and have bandgaps larger than GaAs, while the last material covers bandgap values below GaAs. The range of bandgap values covered by these materials is shown on the ideal efficiency curves of Rappaport in Figure 2.10. According to the ideal theory, the $Al_{1-x}Ga_xAs$ or $GaAs_{1-x}P_x$ cells should have slightly higher efficiencies than pure GaAs. If depletion region recombination dominates, the $Ga_{1-x}In_xAs$



cell may be a better choice. Thus the ternaries offer the ability to select the truly optimum bandgaps for a particular solar cell design. However, all of this will remain speculative until means are found to achieve III-V homojunction solar cells with efficiencies exceeding that of silicon.

One of the major (if not dominant) limitations of present GaAs homojunction solar cells is the short circuit current losses to surface recombination. The dark current may also be significantly enhanced by surface recombination. The two approaches to minimizing this problem have been to reduce the junction depth or to go to a heterojunction structure. The reduction of the junction depth has the problem of increasing the sheet resistance and, therefore, the series resistance of the cells. This limits the junction depth reduction which can be achieved. At present almost all research on III-V p-n junction solar cells is directed toward the heterojunction cell and impressive results have been achieved as discussed in the next section. Another approach which does not appear to have been extensively explored is to reduce the value of the surface recombination velocity. It may be possible to significantly reduce surface recombination by the formation of some type of native oxide at the surface, such as formed by anodic oxidation techniques. MOS devices have been constructed on GaAs through the use of such techniques and these devices generally require good surface properties. The use of a semiconductor heterojunction is simply one means of providing an improved GaAs surface interface. Improvements in surface recombination could make homojunction III-V cells competitive with heterojunction cells.

Because of the wide bandgap of GaAs, the reduction in efficiency with temperature is less than that of silicon cells. Figure 2.11 shows the terminal

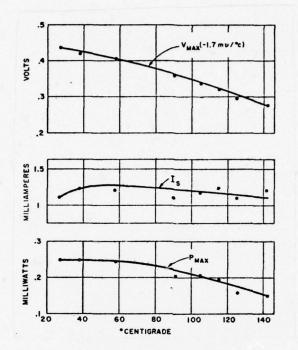


Figure 2.11. Variation of GaAs alloy-junction-solar-cell parameters with temperatures.

parameters of an early GaAs cell as a function of temperature. The short circuit current is seen to remain almost constant with the open circuit voltage changing at about -1.7 mV/°C. The improved temperature performance of III-V cells is one of the major attractive features of such cells.

Another important performance parameter is radiation resistance. Because of the short lifetime and diffusion length, GaAs homojunction cells are more resistant to penetrating radiation than silicon cells. For both high energy electrons and protons the radiation resistance of GaAs cells has been found to be about an order of magnitude larger than silicon cells [2-7, 2-8]. For low energy particles little or no improvement over silicon was observed. However low energy particles can be removed by a thin cover glass so that an overall improved radiation resistance results.

A summary of some of the results and potential performance of various III-V homojunctions is given in Table (2.1). As previously discussed the ideal efficiencies are much larger than can be expected in actual practice. Although GaAs is the only material extensively explored, other materials as shown have equivalent or slightly better efficiency potential. The major problem with all the homojunction III-V cells is the surface recombination. The development of a simple, practical means of greatly reducing the surface recombination velocity on any of the materials in Table 2.1 could catapult the III-V homojunction solar cell back into the picture for some solar cell applications.

The efficiency values in this section are all taken from very idealized studies of general trends of efficiency as a function of semiconductor bandgap which have appeared in the literature. These idealized studies give efficiency values which are larger than typically predicted by more complete studies of particular materials and devices. The results are useful for predicting general trends of efficiency with bandgap. However, the efficiency values reported can not be directly compared with the efficiency values reported in subsequent sections of this report because of the idealized nature of the calculations.

Table 2.1. III-V Homojunction Solar Cells

	22%-26% 21%-25%	11%-12%	Limited in collection efficiency by surface recombination. Long diffusion
	.%-25%		lengths required for low dark current and for ideal dark current.
			Potentially about as good as GaAs with similar problems.
	23%-27%		Little development of materials technology. May be lower in practical efficiency than GaAs even if developed.
GaP _{1-x} x (large x	23%-27% (large x values)		These have advanced materials technology and cover the peak in ideal efficiency. Practical efficiency may not exceed GaAs if dark current is dominated by depletion region recombination.
Ga _{1-x} In _x As (small:	21%-25% (small x values)		Small In concentrations may have slightly higher efficiencies than GaAs if depletion region recombination is important in GaAs.

*Highly idealized values reported in literature (surface recombination neglected). These values are based upon more idealized models than the results of subsequent sections of this report and should not be compared directly with the more complete device calculations.

2.2 Heterojunction Devices

The heterojunction solar cell represents a practical means of eliminating or minimizing the surface recombination loss of III-V homojunction cells discussed in the previous section. It was the development of this type of cell [2-9,2-10] that generated renewed interest in all types of III-V solar cells. In the heterojunction solar cell, a thin layer of a wide bandgap semiconductor is placed at the surface on which the solar flux is incident. Ideally the wide bandgap material, as illustrated in Figure 2.12, acts as a window to pass the incident light into the narrow bandgap semiconductor.

There are basically two types of heterojunction solar cells. In the first type the p-n junction is located at the heterojunction while in the second type the p-n junction is located some distance below the heterojunction. Energy band diagrams for these two types of cells are shown in Figure 2.13. The diagrams show n-on-p cells, but p-on-n cells are also possible. In fact, cells which have been fabricated with the junction below the interface are typically p-on-n cells. When the p-n junction is located below the heterojunction interface, the cell is frequently referred to as a "heteroface" cell [2-6] since the heterojunction plays a more passive role in the operation of the cell. In the present study, the term heterojunction cell will be used for both types of cells, since these can exist as a continuous variety of cells between the cases shown in Figure 2.13.

The heterojunction cell has two major advantages over the homojunction solar cell. First, the optical absorption occurs strongly within the narrow bandgap material beginning at the heterojunction interface. The calculated generation rate, G_e , for an AlAs-GaAs heterojunction of 1 μ m

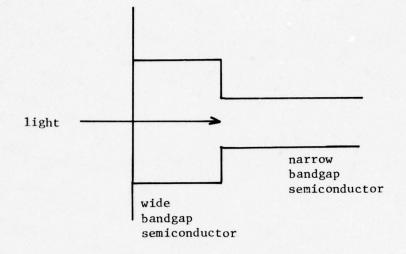


Figure 2.12. Illustration of wide bandgap window on a narrow bandgap semiconductor.

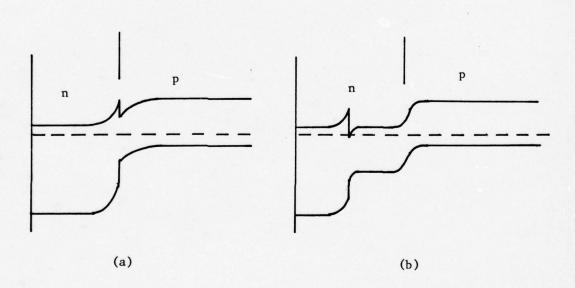


Figure 2.13. Energy band diagrams for the two types of heterojunction cells.

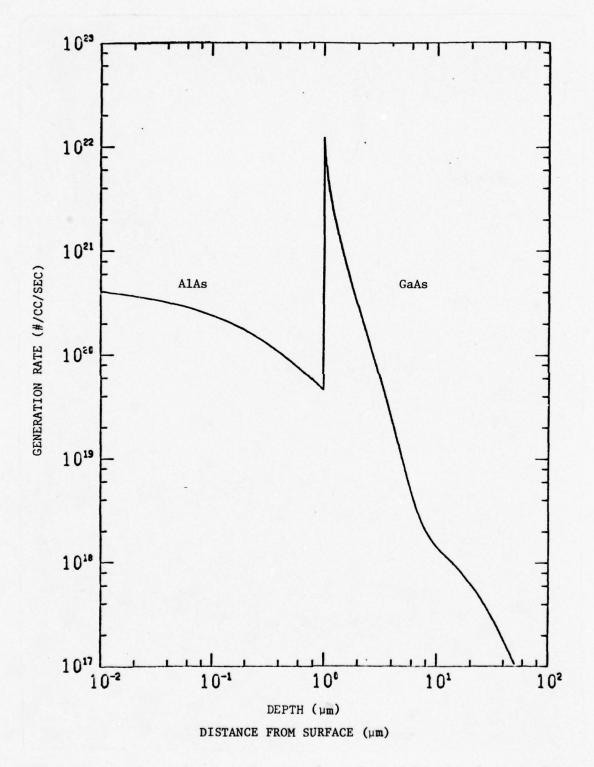
(a) p-n junction at interface.

(b) p-n junction below interface.

depth is shown in Figure 2.14. The generation rate shows an increase of over two orders of magnitude in value at the heterojunction interface compared to the window region. The advantage of the heterojunction cell is that the generation occurs away from the physical surface and there is an energy barrier between the generated minority carriers and the surface. Carriers are thus prevented from reaching the surface and surface recombination loss becomes relatively unimportant in the solar cell operation.

A second advantage of the heterojunction cell arises from the fact that little of the light is absorbed in the wide bandgap region. This allows the surface layer to be relatively wide compared with the surface layer of a homojunction cell. The wider region can be used to lower the sheet resistance of the surface layer and subsequently lower the series resistance of a solar cell. This, however, conflicts somewhat with high efficiency and compromises must be made between high efficiency and low series resistance.

The limitations to efficiency for a heterojunction solar cell are very similar to those of a homojunction cell of the narrower bandgap material. The dark current and short circuit considerations of Equations (2-13)to (2-17) also apply to the heterojunction cell. The short circuit current is limited by transmission into the cell, by bulk recombination, depletion region recombination and surface recombination. As previously discussed the heterojunction cell greatly reduces the front surface recombination. However, it introduces another recombination process which may be almost as severe in some heterojunction cells as surface recombination. This is the introduction of lattice mismatch recombination states at the heterojunction interface due to dangling bonds.



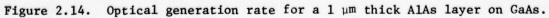


Table 2.2. Density of	Interface Dangling Bon	ds for Various I)	Density of Interface Dangling Bonds for Various III-V Heterojunctions [2-11].
Heterojunction (deposit/substrate)	Lattice parameters (A)	Plane	Dangling $\Delta N = \frac{\Delta N}{(cm^2)}$
InSb/GaSb	6 • 4787 / 6 • 0954	(100)	$1 \cdot 2 \times 10^{14}$ $7 \cdot 1 \times 10^{13}$
InSb/GaAs	6 •4787/5 •6531	(001)	3×10^{14} 1 · 7 × 10 ¹⁴
InAs/GaSb	6.0583/6.0954	(100)	$1 \cdot 3 \times 10^{13}$ 7 \cdot 4 × 10^{12}
InAs/GaAs	6.0583/5.6531	(100)	1 • 6 × 10^{14} 9 • 4 × 10^{12}
GaSb/GaAs	6.0954/5.6531	(111)	$1 \cdot 7 \times 10^{14}$ 1×10^{14}
InP/GaAs	5.8687/5.6531	(100)	9 • 1 × 10^{13} 5 • 2 × 10^{13}
GaAs/GaP	5.6531/5.4505	(100)	9 · 5 × 10^{13} 5 · 5 × 10^{13}
AlAs/GaAs	5.6622/5.6531	(100)	$4 \cdot 3 \times 10^{12}$ 2 $\cdot 5 \times 10^{12}$
AIP/GaAs	5.451/5.6531	(111)	9 • 4 × 10^{13} 5 • 4 × 10^{13}
A1P/GaP	5•451/5•4505	(100)	9 · 1 × 10^{11} 5 · 2 × 10^{11}

. .

The density of dangling bonds has been worked out for a wide range of heterojunctions [2-12] and some of the results are shown in Table (2.2). To obtain an appreciation for the magnitude of the interface recombination the following simple model can be considered. The equivalent surface recombination velocity of the interface states can be written as

$$S = N_{I} \sigma v_{th} , \qquad (2-27)$$

where N_I is the number of recombination states per unit area, σ is the capture cross-section and v_{th} is the thermal carrier velocity. For charged recombination centers $\sigma \sim 10^{-14}$ cm² [12] and taking v_{th} $\sim 10^7$ cm/sec gives

$$S \sim (10^6 \text{ cm/sec}) [N_T / (10^{13}/\text{cm}^2)]$$
. (2-28)

From this estimation, an interface density of recombination centers of $10^{13}/\text{cm}^2$ would give an equivalent interface recombination velocity of 10^6 cm/sec or a value which is about equivalent to that of a bare GaAs surface. If every dangling bond contributes one recombination site then Table 2.2 shows that many potential heterojunction systems will have very large interface recombination and probably offer no advantage over a homojunction cell. Not all of the dangling bonds may be active as recombination centers or the capture coefficient may be smaller than that assumed in this simple calculation. The advantage of the AlAs-GaAs or $Al_{1-x}Ga_x$ As-GaAs system, as seen from Table (2.2), is the very low density of dangling bonds due to the small lattice mismatch between AlAs and GaAs.

Experimental measurements by Ettenberg and Kressel on an $Al_{0.5}Ga_{0.5}As$ -GaAs heterojunction have indicated an interface recombination velocity of about 8 x 10³ cm/sec for this heterojunction [2-13]. This is considerably less than would be estimated from Equation (2.28) assuming that every dangling bond acts as a recombination center. However it shows that even for this near ideal lattice match there is still a fairly large interface recombination. To show a significant improvement over a bare GaAs surface the density of dangling bonds may be limited to values no greater than about ten times the density present at the AlAs-GaAs interface. The actual influence of interface recombination on solar cell efficiency is discussed later in this section.

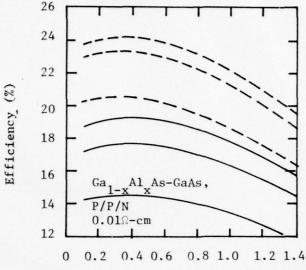
The dark current of a heterojunction is determined by minority carrier injection across the p-n junction and by depletion region and interface recombination. Because of the wider bandgap of the window surface layer, minority carrier injection is small into the surface layer. Neglecting interface recombination states, the dark current of a heterojunction cell should be somewhat less than that of a corresponding homojunction cell. However as shown later, interface recombination may greatly enhance the dark current if the p-n junction depletion region extends into the heterojunction.

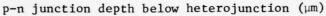
Because the same fundamental factors limit both homojunction and heterojunction solar cells, the ideal efficiency limits discussed for homojunctions in the previous section may also be considered as upper limits to the efficiency of heterojunction cells. From these curves, the efficiency of heterojunction cells on GaAs substrates can be estimated as below the 22%-24% range. More complete calculations have given better estimates of the efficiency limits of selected heterojunction cells.

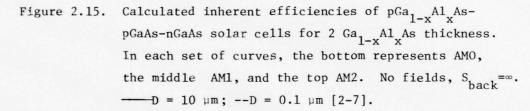
The most extensively studied heterojunction cells are the AlAs-GaAs [2-14,2-15] cell and the Ga_{1-x}Al_xAs-GaAs cell with x in the range of 0.8-1.0 [2-9,2-10]. Figure 2.15 [2-7] shows calculated efficiency values (x values close to unit) as a function of the depth of the p-n junction below the heterojunction. Two thicknesses (10 µm and 0.1 µm) of window material are shown as well as calculated values for AMO, AMI and AM2 spectral conditions. The peak efficiencies for AMO are around 14.5% for a 10 µm window and 20.5% for a 0.1 µm window. These values are lower than the ideal efficiencies of Figure 2.3-2.7 because of more realistic approximations used in the calculations. The effect of the window thickness is seen in Figure 2.16. It is seen that the window thickness must be less than 0.1 µm if the highest efficiency values are to be achieved.

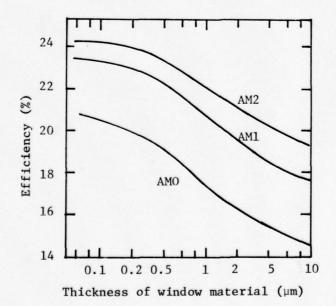
The results shown in Figures 2.15 and 2.16 are based upon closed form solutions to the approximate transport equations as discussed in Appendix A. Exact numerical calculations have also been made for AlAs-GaAs heterojunction cells using the method discussed in Appendix A. The peak efficiency values obtained by this exact numerical analysis are shown as a function of p-n junction depth in Figure 2.17 [2-16]. The doping densities used in the calculations were $2 \times 10^{17}/\text{cm}^3$ for the surface layer and $4 \times 10^{17}/\text{cm}^3$ for the base layer. The optimum p-n junction depth has been identified as about 0.3 µm to 0.4 µm in both calculations. The resulting efficiency values are very similar to those of Figure 2.15 obtained by the simpler analysis.

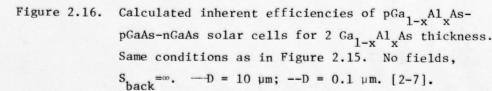
The calculations for (Al,Ga)As heterojunction cells in this and the next section were done on a separate NASA Langley Research Grant to N. C. State University.











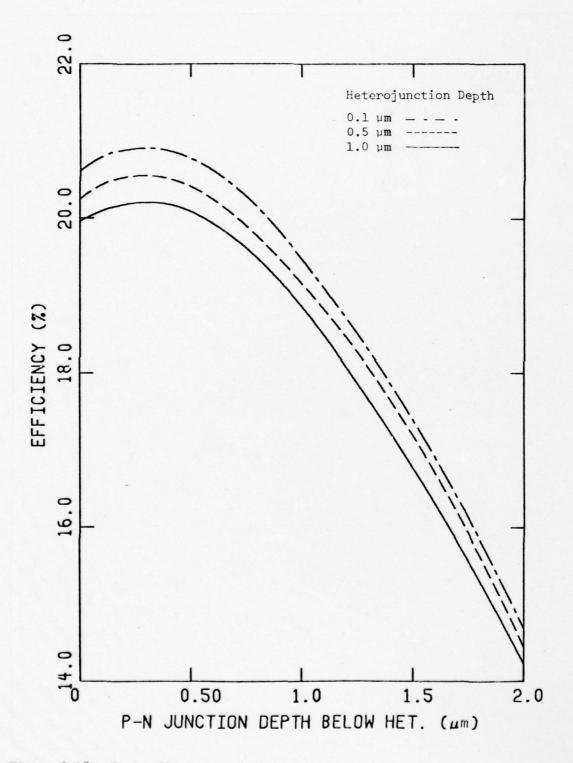


Figure 2.17. Peak efficiency of AlAs-GaAs heterojunction cells as a function of p-n junction depth below the heterojunction from numerical analysis.

This is especially interesting since the results in Figures 2.15 and 2.16 are for p-on-n cells while the results of Figures 2.17 are for n-on-p cells. These results indicate that little theoretical differences are to be expected in peak efficiency between n-on-p and p-on-n cells and the choice must be made from practical fabrication considerations.

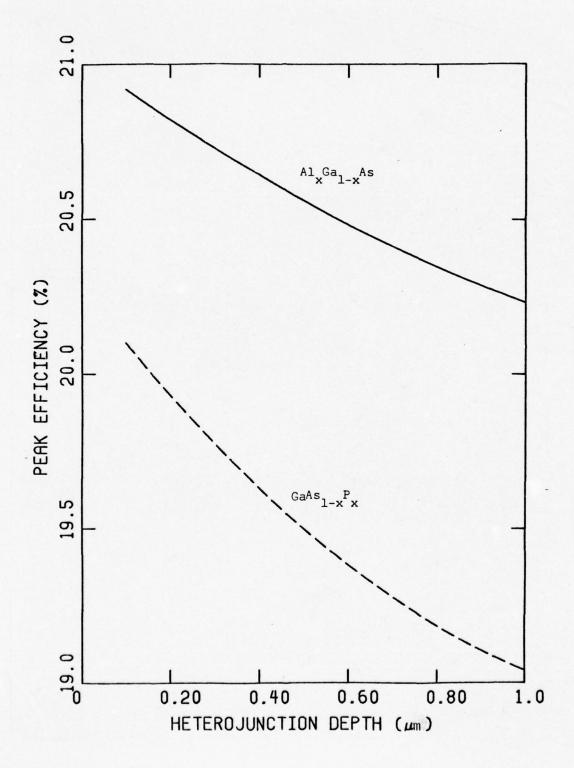
Figure 2.18 shows the results of the detailed analysis for peak efficiency as a function of heterojunction depth. This again for the $Al_xGa_{1-x}As$ system is very similar to Figure 2.16. (The results for $GaAs_{1-x}P_x$ are discussed subsequently.) The results in general illustrate the importance of a very thin window region and indicate that the theoretical efficiency values are in the range of 20%-21%.

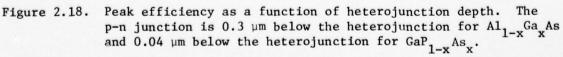
In addition to the (AlGa)As system, the Ga(P,As) system is probably the next most extensively explored III-V ternary system because of its applications in LEDs. GaP has similar electrical and optical properties to AlAs and should in principle behave similarly in heterojunction solar cells. This conclusion has been confirmed to a certain extent by solar cell calculations, but a problem arises with the GaP-GaAs heterojunction system which has also been identified. Calculations have been made for GaP-GaAs heterojunction cells with dimensions and doping densities identical to those used in obtaining the results of Figure 2.17. A comparison of some of the results is shown in Table (2.3). The first three lines in the table are for AlAs-GaAs heterojunctions under different conditions. Device number 1 does not include the lattice mismatch interface states while devices number 2 and 3 do include these. For the AlAs-GaAs devices, heterojunction interface states were found to reduce the efficiency only by about 0.1-0.2 percentage points.

A comparison of devices number 1 and 4 gives a direct comparison of the AlAs-GaAs cell and the GaP-GaAs cell before interface states are included. The GaP-GaAs cell has a slightly lower efficiency of 19.24% as compared with 19.95%, but the predicted performance is almost identical as expected. Device number 5 shows the results of including the interface states on the efficiency of the GaP-GaAs cells. The efficiency decreases from 19.24% to 15.04%. The reduced efficiency is due almost entirely to the drop in open circuit voltage from 0.985V to 0.831V. These predictions are based upon the assumption that the interface recombination velocity is directly proportional to the density of dangling bonds at the interface. This has not been experimentally verified but appears to be a reasonable assumption.

The variation in efficiency with p-n junction depth for GaP-GaAs cells is shown in Figure 2.19. As contrasted with the AlAs-GaAs cells of Figure 2.17, the efficiency was observed to increase rapidly as the p-n junction was moved to small distances below the heterojunction. Efficiencies of 19% or slightly above were calculated for junction depths of around 0.04 μ m below the heterojunction. The efficiency was then observed to decrease rapidly for junction depths beyond 0.1 μ m. This behavior is directly due to the large density of interface states.

Consider first the rapid increase in efficiency as the junction is moved below the heterojunction. This has the effect of moving the interface recombination states out of the center of the junction depletion region. Recombination states within a depletion region are most effective when they occur near the center of the energy bandgap. Thus moving the junction slightly below the heterojunction greatly reduces the dark





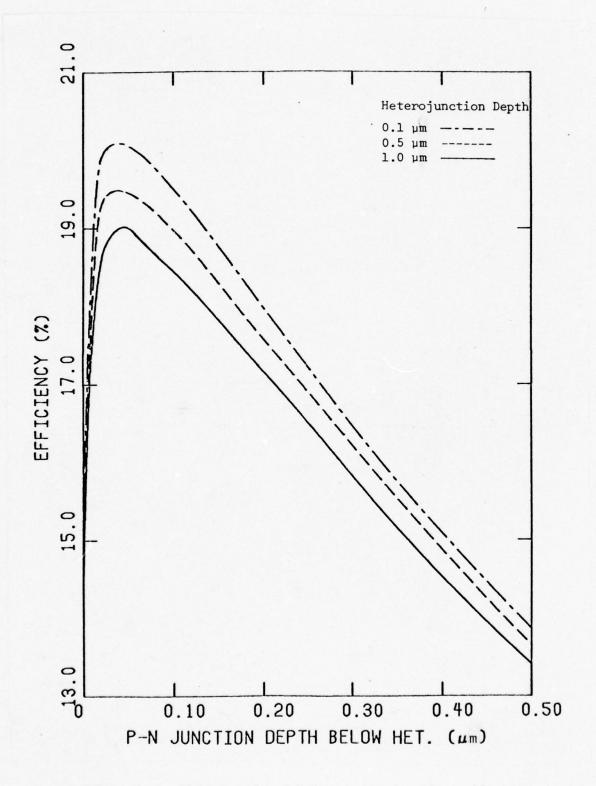


Figure 2.19. Peak efficiency for GaP-GaAs heterojunction cells as a function of p-n junction depth below the heterojunction. Analysis includes interface recombination.

current from these recombination states. This conclusion is verified in Figure 2.20 which shows the dark current for three GaP-GaAs cells. The lowest current curve is for the p-n junction at the heterojunction but without interface states. Keeping the junction at the interface and including the interface states results in the largest current curve $(x_J = 0)$. The interface states result in an increase of about two order of magnitude in dark current. This is responsible for the decrease in V_{OC} shown in Table 2.3. Moving the p-n junction only 0.04 µm below the interface is seen to reduce the dark current back almost to its original value.

The rapid decrease in efficiency for junction depths beyond the peak in Figure 2.19 is due to a second physical effect. This is the loss of short circuit current to the interface states as the p-n junction depth increases. The large density of interface states acts in much the same way as recombination at the surface of a homojunction solar cell.

It can be concluded from these studies that interface recombination states can severely degrade the performance of heterojunction solar cells. For large densities of interface states, the heterojunction cell probably offers no advantages over a homojunction solar cell. High efficiency abrupt heterojunction cells can probably be made only in a few selected material combinations such as AlAs-GaAs where the lattice mismatch is small between the two semiconductor materials. The possibility may still exist in devices such as GaP-GaAs of slowly grading the material so that the lattice mismatch states can be spread

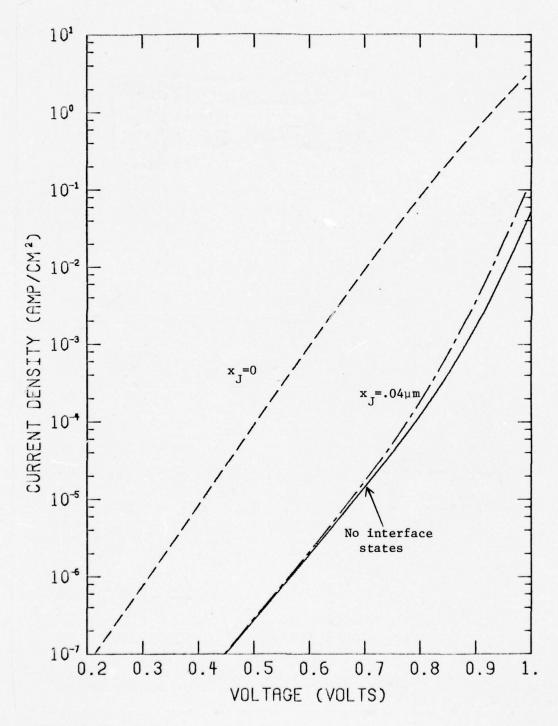


Figure 2.20. Influence of interface states and junction depth on dark current.

Table	Table 2.3. Computer Results for Several $A_{x}^{1}Ga_{1-x}^{1}As$ and GaAs $_{1-x}^{1}x_{x}^{1}$ Solar Cells	ter Results	for Sev	eral Al _x	Ga _{1-x} As	and GaAs.	l-x x Sola	ır Cells	
evice #	Alloy	Comp. Change	Het. Depth (µm)	p-n Depth (µm)	voc (V)	J sc (mA)	Fill Factor	Peak Eff. (%)	Interface States
1	$A1_{x}Ga_{1-x}As$	abrupt	1.0	1.0	.998	31.40	.861	19.95	No
2	$A1_{\mathbf{x}}Ga_{\mathbf{1-x}}As$	abrupt	1.0	1.3	.998	31.79	.862	20.21	Yes
S	$A1_{x}Ga_{1-x}As$	abrupt	0.1	0.4	666.	32.83	.863	20.91	Yes
4	GaAs _{1-x} ^P x	abrupt	1.0	1.0	.985	30.64	.862	19.24	No
5	GaAs _{1-x} x	abrupt	1.0	1.0	.831	30.64	.799	15.04	Yes

over a larger volume and perhaps degrade less the performance. This is considered in more detail in the next section on graded bandgap solar cells.

The results of Figure 2.19 indicate that the detrimental effects of the interface states can be minimized if the p-n junction depth is selected at about 0.04 μ m below the heterojunction. The peak efficiency for this junction depth is shown in Figure 2.18 as a function of the thickness of the GaP window material. The results are similar to the AlAs-GaAs cells except that the efficiency is about 1 percentage point lower in value. This solution to the interface problem may not be practical on a production basis because of the critical selection required of p-n junction depth.

In addition to the AlAs-GaAs and GaP-GaAs systems, other materials can be considered for heterojunction cells. Several other such heterojunctions have been considered by Milnes and Feucht [2-17] and by Sneedhor, <u>et al</u>. [2-18]. Of the possible III-V materials, it appears that highest efficiency will be achieved with a base layer of GaAs or some other material with a bandgap close to GaAs such as InP, $Ga_{1-x}In_xAs$, $Al_{1-x}Ga_xAs$ or $GaP_{1-x}As_x$. The ternary III-V materials such as $Ga_{1-x}In_xAs$ and $Al_{1-x}Ga_xAs$ are especially interesting since they make possible the potential of adjusting the bandgap of the base layer for peak efficiency. Calculations for $AlAs-Al_{1-x}Ga_xAs$ heterojunctions have indicated that the efficiency decreases as the Al content of the base layer is increased. The $AlAs-Ga_{1-x}In_xAs$ heterojunction should then be more efficient than pure GaAs for the base layer. This has been verified by calculations. However the increased efficiency appears to

be less than 1 percentage point at an In concentration of around 10%. This small increase in efficiency probably does not justify the development of this type of device considering the additional fabrication problems of the ternary base layer solar cell.

The temperature performance of heterojunction solar cells has not been extensively investigated. However the heterojunction cell can be expected on theoretical grounds to have essentially the same temperature performance as a homojunction cell made of the base layer material. When the p-n junction is below the heterojunction the wide bandgap layer acts mainly as a low surface recombination boundary for what otherwise looks like a homojunction solar cell. Even when the p-n junction coincides with the heterojunction, the dark current which controls to a major extent the temperature performance is still determined essentially by the properties of the narrow bandgap material.

In summary the AlAs-GaAs or (Al,Ga)As-GaAs heterojunction cell is the most highly developed III-V solar cell. The ultimate efficiency performance does not exceed that of p-n homojunction cells. However it has so far come much closer to achieving the theoretically predicted performance because of problems in achieving a low surface recombination velocity on homojunction cells. The highest efficiency heterojunction cells require the thinnest window materials which can be partically achieved and can be said to be approaching the homojunction solar cell case.

It appears that lattice mismatch interface recombination will be a real problem in any heterojunction cell which does not have close

lattice matching between the layers such as occurs in the AlAs-GaAs cell. The advantage of the heterojunction cell is eliminated unless the interface has a low surface recombination velocity (below 10^4 cm/sec).

A summary of the most promising III-V heterojunction solar cells is given in Table (2.4). At present none of the other possibilities appear to offer a real challenge to the AlAs-GaAs solar cell. The calculated efficiency values given in Table (2.4) are somewhat lower than the ideal efficiency values of Table (2.1) for homojunction cells. This results from the more realistic assumptions incorporated into our calculations for heterojunction cells and is not due to an inherent limitation in heterojunction efficiency which is not present with homojunction cells.

	Table 2.4.	III-V Heterojunction Solar Cells	r Cells
Material	Ideal Efficiency*	Achieved Efficiency	Remarks
(Al, Ga)As-GaAs	20%-21%	18.5%	Best cells require compositions close to pure AlAs for the surface layer. Highly developed materials technology. Thin surface layers required.
AlAs-GaAs	20%-21%		Ideal case of above general cell. Pure AlAs is more difficult to achieve than (Al,Ga)As layers.
AlAs-(Al,Ga)As	Below above values		Theoretical efficiency decreases as band gap of base layer increases.
AlAs-(Ga,In)As	21%-22%		Slightly higher theoretical efficiency than GaAs base layer for small In compositions in base layer. Difficult to achieve required base layer.
GaP-GaAs	19%-20%		Interface recombination greatly reduces efficiency unless location of p-n junction is carefully selected. Difficult to achieve efficiency values as high as for AlAs-GaAs.
AlAs-InP or GaP-InP *			Lattice mismatch is large. Similar problems to GaP-GaAs.

These efficiencies are theoretical values based upon active area only and including a single layer anti-reflecting film. Low loss (5% or less) antireflecting layers would increase these theoretical values for active area efficiency by 1.5 - 2.0 percentage points.

2.3 Graded Bandgap Devices

The use of a graded band gap in a solar cell gives an additional degree of freedom in solar cell design which is not present in homojunction or abrupt heterojunction solar cells. The current density equations for a graded bandgap semiconductor are (see APPENDIX A).

$$J_n = q\mu_n nE_n + q D_n \frac{dn}{dp} , \qquad (2-29)$$

$$J_{p} = q \mu_{p} p E_{p} - q D_{p} \frac{dp}{dp} , \qquad (2-30)$$

where $\underset{n}{E}$ and $\underset{p}{E}$ are the total fields acting on electrons and holes. Explicit expressions for these are

$$E_{n} = E - \frac{1}{q} \frac{d\chi_{c}}{dx} - \frac{kT}{q} \frac{1}{N_{c}} \frac{dN_{c}}{dx} , \qquad (2-31)$$

$$E_{p} = E - \frac{1}{q} \frac{d\chi}{dx} - \frac{1}{q} \frac{dEg}{dx} + \frac{kT}{q} \frac{1}{N_{v}} \frac{dN_{v}}{dx} . \qquad (2-32)$$

Contributions to E_n arise from the electric field E, changes in electron affinity X_c with position and changes in the condition band density of states N_c with position. Similar terms occur in E_p with an additional term due to band gap E_g changes with position.

There are at least three basic reasons for considering graded bandgap solar cells. First, the built-in fields may aid in collecting the generated carriers. Second, the built-in fields might reduce the dark current (in comparison with homojunction structures) and third, by using a graded as opposed to abrupt transition between a wide bandgap and narrow bandgap region, recombination from the interface recombination states discussed in the previous section may be minimized. The first two reasons relate to the presence of the built-in field due to the bandgap grading.

The most logical use of the graded bandgap layer is in the surface layer to aid in carrier collection from this region. Figure 2.21 shows the energy band diagram near the surface of an (Al,Ga)As graded bandgap cell. This is an exact solution of the energy bands for a device which is linearly graded in composition from pure AlAs at the surface to pure GaAs at 1 μ m where the p-n junction is located. Because the graded bandgap region is doped n-type, almost all of the band gap change occurs at the edge of the valence band. The change in E at about 0.6 μ m is due to the transition of (Al,Ga)As from a direct bandgap to an indirect bandgap material and the subsequent change in N. The valence band edge also shows a change in slope at this point which is also due to the transition from a direct to indirect bandgap material. The effective fields of Eqs. (2-31) and (2-32) in equilibrium are the slopes of the conduction and valence band edges in Figure 2.21. As shown in the figure, the bandgap grading gives a field acting on the minority carriers (holes) forcing them toward the collecting p-n junction. The resulting increased collection efficiency is one of the major reason for considering such graded bandgap cells.

An exact analysis of graded bandgap cells requires a numerical solution because of the nonlinear nature of the equations. However, Figure 2.21, which was obtained from such an analysis, shows that good approximations are possible for the minority carriers. For the linearly graded composition case the field acting on the minority carriers is approximately constant in both the direct and indirect bandgap regions but is much larger in magnitude in the direct bandgap region. Thus a good approximation can be made to the transport equations by assuming a constant field—— E_p for example in Eq. (2-30). With other simplifying approximations, as discussed in APPENDIX A, approximate

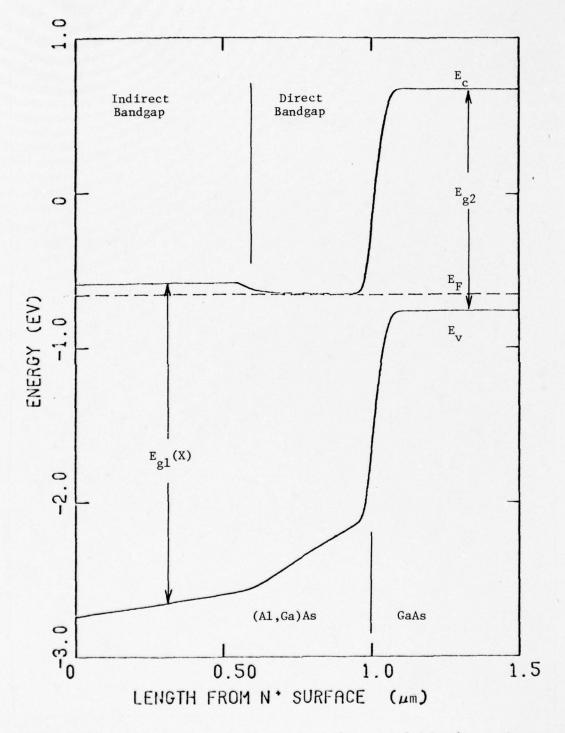


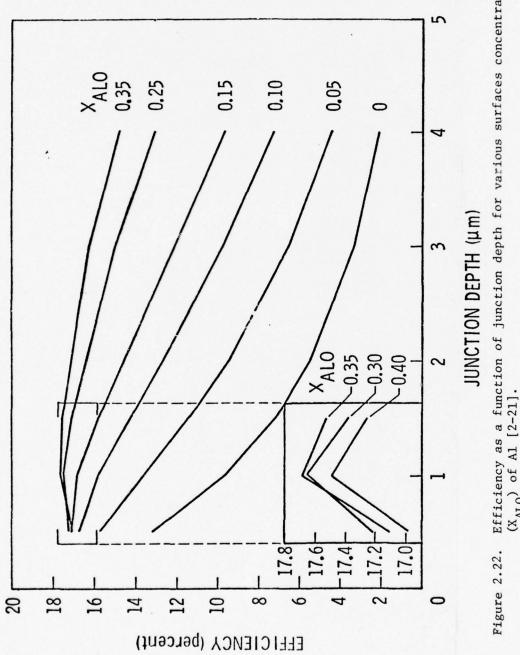
Figure 2.21. Typical energy band structure for a graded bandgap solar cell. AlAs is at the surface, and is graded linearly to GaAs for distances beyond 1 μm.

closed form solutions can be obtained. The details of the resulting solutions are given in other parts of this report.

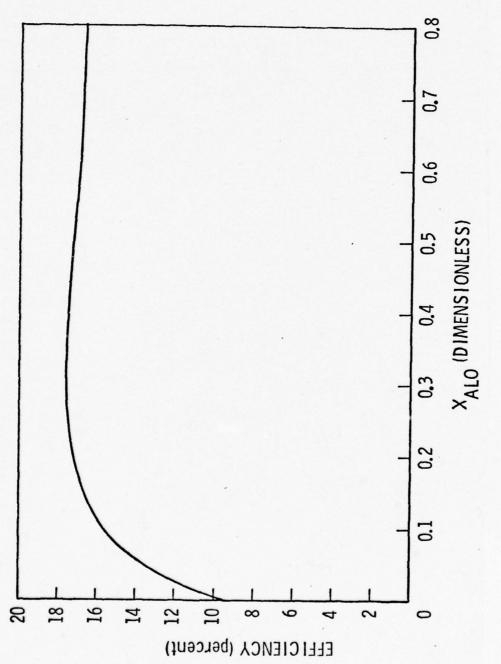
Using an approximate analysis as outlined above, Hutchby has studied the design and performance of graded bandgap n-on-p (Al,Ga)As solar cells [2-19--2-21]. Shown in Figure 2.22 is the calculated efficiency as a function of junction depth (and also graded region depth) for various surface concentrations (X_{ALO}) of Al in the (Al,Ga)As graded layer. The efficiency is seen to be greatly increased at large junction depths by the graded bandgap as compared with the $X_{ALO} = 0$ curve which is a homojunction GaAs solar cell. These particular calculations are for doping densities of $N_A = 2 \times 10^{17}/cm^3$ and $N_D = 4 \times 10^{17}/cm^3$.

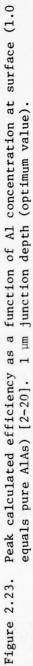
The highest curve in Figure 2.22 which is for an Al composition of 35% at the surface is just below the composition for the direct to indirect bandgap cross-over. The maximum efficiency as a function of Al composition at the surface is seen in Figure 2.23. It is seen that the efficiency tends to saturate at around 35% Al and in fact decreases slightly for larger compositions. From this it can be concluded that the peak efficiency occurs at approximately the point where the material changes from a direct band gap to an indirect bandgap material. As previously discussed in connection with Figure 2.21 the field acting on the minority carriers is small in the direct band gap region and this small field is responsible for the saturation in efficiency.

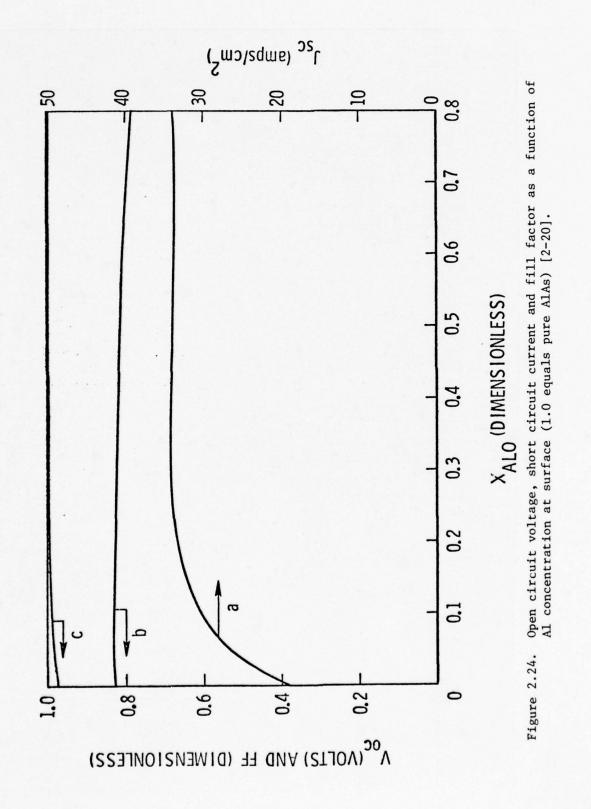
The increase in efficiency of the graded band gap cell over the homojunction cell is largely due to an increase in short circuit current. This is seen in Figure 2.24 which shows the three terminal parameters for the same conditions as for Figure 2.23. Very little change is seen in open circuit voltage or fill factor. However, a very significant increase is seen in short circuit current due to the increased collection efficiency of the surface layer.



Efficiency as a function of junction depth for various surfaces concentrations $(X_{\rm ALO})$ of Al [2-21].





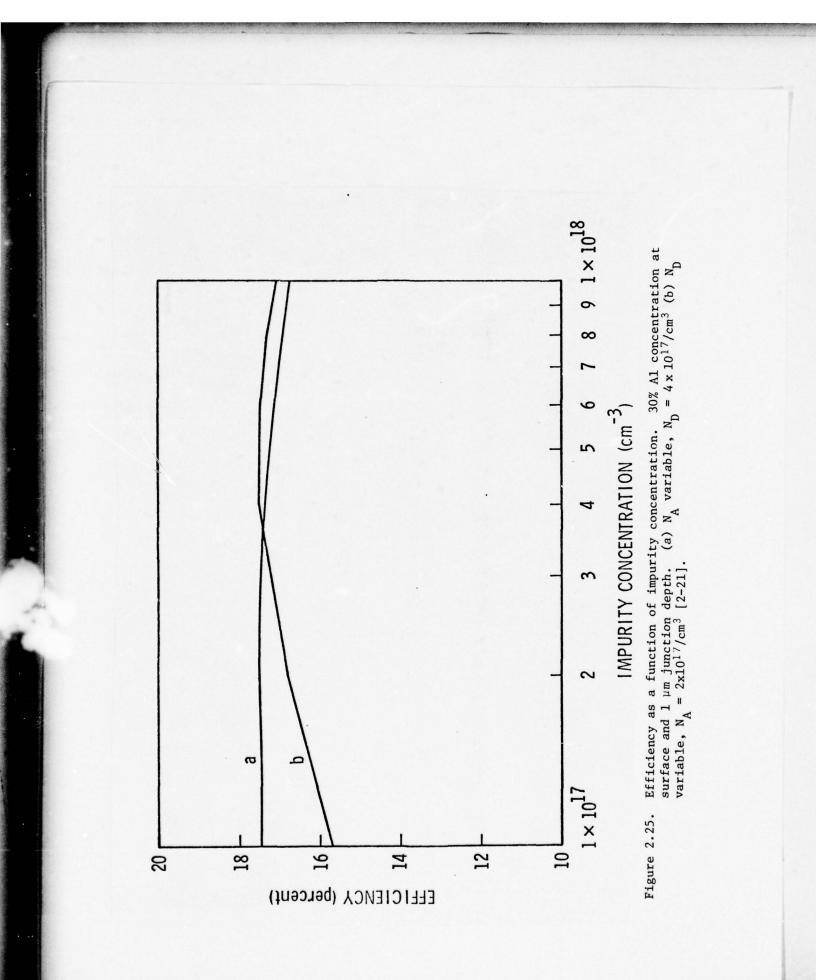


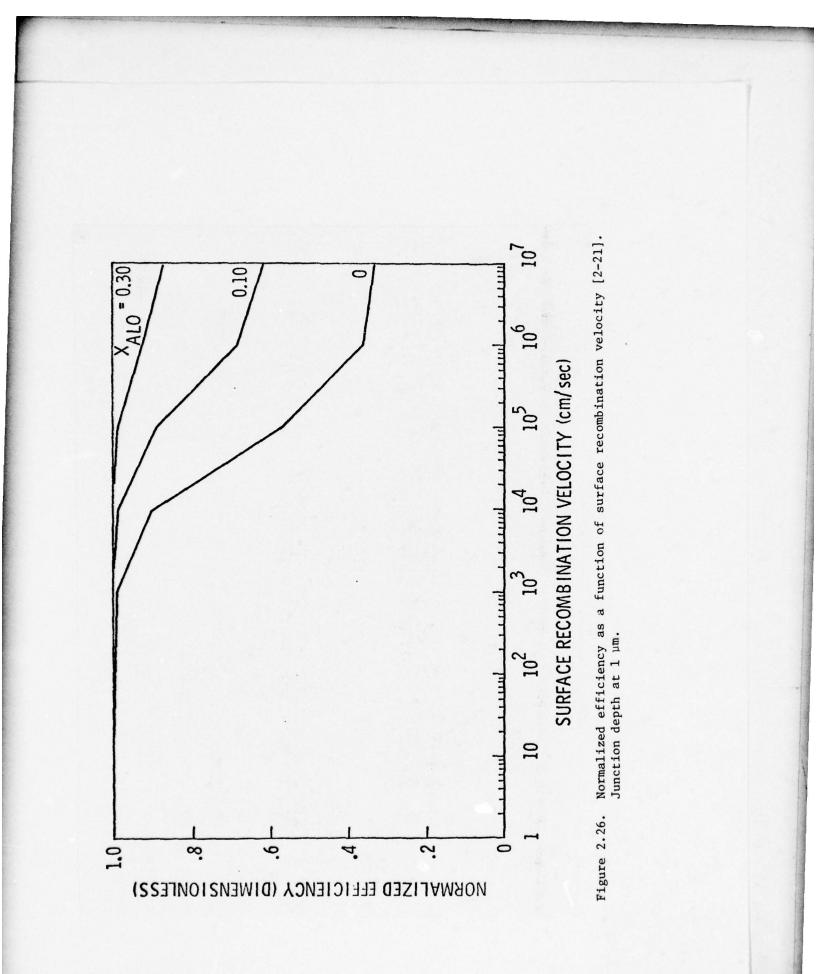
The effect of impurity doping density on peak efficiency is shown in Figure 2.25. Over the range of $10^{17}/\text{cm}^3$ to $10^{18}/\text{cm}^3$, the efficiency is not a strong function of doping density. However, optimum doping densities were found to be $4 \times 10^{17}/\text{cm}^3$ on the n-side and $2 \times 10^{17}/\text{cm}^3$ on the p-side.

Finally the effect of surface recombination velocity on efficiency for different degrees of grading is shown in Figure 2.26. For the homojunction case ($X_{ALO} = 0$) the surface recombination velocity must be below $10^4/\text{cm}^3$ if it is not to greatly reduce the efficiency. For the optimum graded bandgap cell ($X_{ALO} > 0.3$), surface recombination velocities of even 10^7 cm/sec reduce the efficiency only about 10%. The graded bandgap cell has the same desirable features of the abrupt heterojunction cell with regard to surface recombination velocity.

The efficiency values calculated by Hutchby and discussed above can not be directly compared with the heterojunction efficiency values given in the previous section. Hutchby's values have been corrected for series resistance and for ohmic contact stripes. The assumed contact coverage was 13% so the values must be increased by this factor to compare with the values in the previous section. Also the series resistance used by Hutchby has further reduced the efficiency. An 18% efficiency value after correcting for these, corresponds to at least a 20.5% initial efficiency. Thus the graded bandgap efficiency values are very similar in magnitude to the abrupt heterojunction values.

An analysis of the efficiency of graded bandgap cells has also been made using the detailed numerical analysis outlined in APPENDIX A. This is a more accurate analysis than that of Hutchby but the results are very similar. Table 2.5 shows a comparison of the calculated performance of graded bandgap





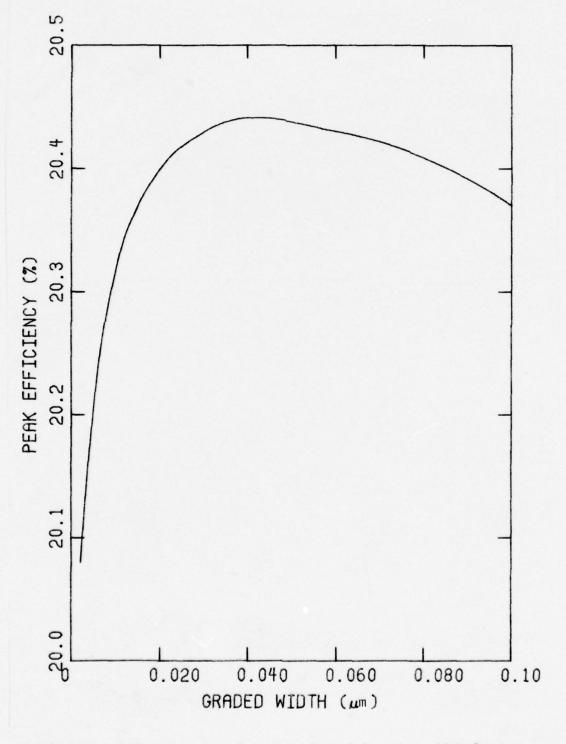
(A1,Ga)As-GaAs and abrupt heterojunction solar cells. Device No. 1 is for 35% Al composition at the surface while devices No. 2 and 3 are for 100% Al composition at the surface. Devices No. 4 and 5 give results for abrupt AlAs-GaAs solar cells for comparison. First it is seen that the graded bandgap cells have slightly larger short circuit currents as expected from the built-in fields. The largest efficiency of 20.75% occurred for a grading to pure AlAs at the surface and is 0.8 of a percentage point larger in efficiency than a similar heterojunction device [(No. 4 of Table 2.5)].

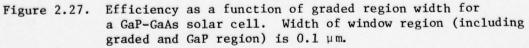
These results discussed above are for (A1,Ga)As solar cells where lattice mismatch interface recombination is relatively unimportant. For other solar cells such as Ga(P,As) it may be argued that a graded bandgap region rather than an abrupt heterojunction can be used to greatly reduce the effect of the lattice mismatch states. To study this effect, a series of calculations have been made on Ga(P,As) solar cells. The devices studied have a p-n junction located at 0.1 µm from the surface and a constant GaP region near the surface. Between these constant bandgap regions is a linearly graded composition region of varying width, with the width varying from zero to the complete surface layer width of 0.1 µm. The calculations include lattice mismatch recombination states which are assumed to be uniformly distributed throughout the graded layer. The resulting efficiency values as a function of the width of the graded layer are shown in Figure 2.27. The results show that the use of a graded layer does in fact lead to an increased efficiency. However, the peak efficiency is still lower than that which could be achieved without the interface recombination series.

From the studies which have been made here and elsewhere on graded bandgap solar cells, it can be expected that such cells can have slightly larger efficiency values than abrupt heterojunction cells of similar material

r Cell	face tes	0	0	0	0	0
n Solai	Interface States	NO	No	No	No	No
ojunctio	S cm/sec	10 ⁵	10 ⁵	20.60 10 ⁵	10 ⁵	10 ⁵
ot Heter	Fill Peak actor Eff. (%)	20.46 10 ⁵	20.75 10 ⁵	20.60	19.95	20.21
GaAs Abrug	Fill Factor	.864	.863	.863	.861	.862
and AlAs-	J _{sc} (mA/cm ²)	32.07	32.55	32.37	31.40	31.79
As-GaAs	v _{oc} (v)	1.0 .999	666.	866.	.998	.998
(A1, Ga)	p-n Depth (µm)	1.0	1.0	1.5	1.0	1.3
Band Gap	Het. Depth (µm)	1.0	1.0	1.0	1.0	1.0
f Graded	Comp. Change	linear (to 35% AlAs)	linear	linear	abrupt	abrupt
Table 2.5. Comparison of Graded Band Gap (A1,Ga)As-GaAs and A1As-GaAs Abrupt Heterojunction Solar Celli	Alloy	A1 _x Ga _{1-x} As	$A1_{x}Ga_{1-x}As$	$A1_{x}Ga_{1-x}As$	$A1_{x}Ga_{1-x}As$	$A1_{x}Ga_{1-x}As$
Table 2.5.	Device #	1	2	в	4	S

11s





compositions. These improvements result basically from an increase in carrier collection efficiency of the surface layer. However, the predicted improvements are typically less than one percentage point in overall efficiency. These improvements must be weighed against the increased difficulty of fabricating such solar cells.

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3.0 SCHOTTKY BARRIER AND METAL-INSULATOR-SEMICONDUCTOR SOLAR CELL STRUCTURES3.1 Schottky Barrier

3.1.1 Introduction

The metal-semiconductor or Schottky barrier solar cell has received attention primarily becuase of the relative simplicity of the structure compared to other fabricational techniques [3-1]. In addition, when interfacial layers are introduced between the metal and semiconductor, increased conversion efficiencies are feasible due to a variety of physical mechanisms [3-2, 3-3].

Physical modeling of the characteristics of Schottky barrier solar cells has included first order limit calculations [3-4], more detailed closedform analytical solutions [3-1], and even more detailed computer-generated solutions of the transport equations [3-5]. Other investigators have contributed to the literature on physical modeling, treating specific physical effects and including other aspects of importance in the overall cell performance [3-6, 3-7].

In general, the approach in discussing the results of these physical models has been either to present the calculations for specific materials such as silicon or gallium arsenide, or to discuss the results in terms of general fundamental material parameters, such as energy bandgap or Schottky barrier height. The latter approach usually assumes unity internal collection efficiency for energies above the bandgap; this eliminates the need for a knowledge of material parameters which influence the photocurrent. These calculations have been used to establish upper limits to conversion efficiency of Schottky barrier solar cells for the general class of semiconductor materials, and to examine performance characteristics of specific materials with known energy bandgaps and barrier heights.

The importance of energy bandgap and barrier height in determining the performance of Schottky barrier solar cells is well known and verified [3-1 to 3-7]. The ternary alloys of the binary III-V semiconductor compounds provide the means for continuously adjusting the energy bandgap and barrier height in order to optimize this performance. For example, Yeh and Stirn [3-3] have reported a 20% improvement in cell conversion efficiency for the ternary GaP_{.22}As_{.78} as compared to GaAs. At the same time, recent theoretical treatments [3-8, 3-9] provide a means whereby the important material parameters of the ternary alloys can be calculated from a knowledge of material parameters for the binary constituents. Thus, unity internal collection efficiency is not a necessary assumption. In addition, experimental data for barrier heights in ternary alloy systems of interest for Schottky barrier solar cells have been reported [3-10], and this is a subject of specific interest for many other device applications.

This section discusses Schottky barrier solar cell calculations for the GaP_xAs_{1-x} , $Ga_{1-x}Al_xAs$, $Ga_{1-x}In_xAs$, and $GaAs_{1-x}Sb_x$ ternary alloy systems. The device modeling approach used is similar to that discussed by Hovel [3-1], whereby an analytical transport model which takes into account important material properties is used to calculate the photocurrent. Experimental data for the energy bandgaps as a function of alloy composition x are used. Theoretical models are used to calculate the compositional dependence of other important material parameters in terms of known experimental parameters for the binary consituents, with special attention being given to the absorption coefficient. Both experimental and empirical values of the barrier height are used in the calculations. An attempt has been made to accurately

describe the compositional dependence of all significant material parameters which determine cell performance, and to include these material parameter variations in a device model which gives reasonable performance characteristics for cells using materials with accurately known parameters (such as silicon and gallium arsenide).

3.1.2 Device Model

A brief summary of the device equations used in the calculations will be given [3-1]. The voltage-current characteristic for the solar cell is given by

$$J_{T}(V_{a}) = J_{0}(V_{a}) - J_{sc}$$
(3-1)

where

$$J_{T}(V_{a})$$
 = the terminal current density as a function of applied voltage

 J_{sc} = the short circuit (V =0) photocurrent density due to the solar spectrum

 $J_D(V_a)$ = the dark current density as a function of applied voltage

The photocurrent density $J_{\mbox{sc}}$ is composed of two integrated terms through the relation

$$J_{sc} = \int_{0}^{\infty} \left[J_{DR}(\lambda) + J_{p}(\lambda) \right] d\lambda$$
(3-2)

where λ = optical wavelength, and

 $J_{DR}(\lambda)$ = Depletion region photocurrent density per unit optical band width

 $J_p(\lambda) = Minority carrier (hole) photocurrent density per unit optical band width$

Here an n-type semiconductor has been assumed for convenience.

The dark current density is taken to be composed of three terms as follows:

$$J_{\rm D} = J_{\rm SB} + J_{\rm R} + J_{\rm Diff}$$
(3-3)

where

$$J_{SB}$$
 = Schottky barrier current density

$$R_R$$
 = Recombination current density integrated
over the depletion region

J_{Diff} = Minority carrier (hole) current density at the depletion region-quasi neutral semiconductor boundary

The only difference between the model given by Eqn. (3-1) and that used in Hovel's calculations [3-1] is the term involving J_R included in the dark current. Usually $J_{SB}+J_{Dif}>>J_R$ and this term can be neglected. However, in this work the term was included because its importance is not readily ascertainable when the complicated compositional dependence of the ternary material parameters is considered.

The dependence on material parameters of each of the terms in Eqns. (3-1) and (3-3) is presented in APPENDIX C.

These device equations are used along with the standard equation

$$\eta = \frac{P_o}{P_{in}} = \frac{V_a J_T (V_a)}{P_{in}}$$
(3-4)

to calculate the cell conversion efficiency, η . The fill factor, F.F. is also calculated from

$$F.F. = \frac{P_{max}}{V_{oc}J_{sc}}$$
(3-5)

where P_{max} is the maximum output power, V_{oc} is the open-circuit voltage, and J_{sc} is the short-circuit current density. The input power, P_{in} , is based on both the AMO spectral conditions. The optical generation rate used in the device equations for calculating $J_{DR}(\lambda)$ and $J_{P}(\lambda)$ is based on the calculations presented by Sutherland and Hauser [3-11].

3.1.3 Material Parameters

The following list shows the parameters identified from the device models which are needed for the solar cell calculations.

D p	minority carrier diffusion constant
P _o	equilibrium minority carrier concentration
L p	minority carrier diffusion length
Wn	depletion region width
N _D	majority carrier doping concentration
** A	Schottky barrier effective Richardson constant
Ø _B	Schottky barrier energy
ⁿ i	intrinsic carrier concentration
τ _p	minority carrier lifetime
^τ po, ^τ no	Shockley-Read recombination model lifetimes
Et	Shockley-Read recombination center energy level
α	photon absorption coefficient
S	back surface recombination velocity
W	total cell length

All of these parameters are required to be known as a function of alloy composition, and the relations which describe this dependence are given in APPENDIX B. The diffusion constant is calculated from the mobility by using the Einstein relation $D_p = \frac{kT}{q} \mu_p$. The diffusion length is then calculated from $L_p = \sqrt{D_p \tau_p}$. The dependence of hole mobility on doping level and alloy composition is described in APPENDIX B. The depletion layer width is calculated from the equation

$$V_{\rm n} = \sqrt{\frac{2\varepsilon_{\rm r}\varepsilon_{\rm o}}{q\,N_{\rm D}}} \left(V_{\rm D} - V_{\rm a} - \frac{kT}{q} \right), \qquad (3-6)$$

where \boldsymbol{V}_{D} is the diffusion potential, given by

$$W_{\rm D} = \frac{E_{\rm G}}{q} - \frac{kT}{q} \ln \left(\frac{N_{\rm c}}{N_{\rm D}} \right) , \qquad (3-7)$$

where E_{G} is the band gap and N_{c} is the conduction band density-of-states. The minority carrier density is calculated from $P_{o} = \frac{n^{2}}{i/N_{D}}$, where the intrinsic concentration, n_{i} , is given by

$$n_i^2 = N_c N_v \exp\left(\frac{-E_c}{kT}\right)$$
 (3-8)

Here N_V is the valence band density-of-states. Most of these parameters are used in the more detailed computer calculations described in this report, and these are discussed in more detail in these sections, and in APPENDIX B. It should also be mentioned that the absorption coefficient versus wavelength data used in these calculations was obtained by the method of Sutherland and Hauser [3-10].

3.1.4 Results

The purpose of this study was to examine the performance of Schottky barrier solar cells in ternary III-V alloys to see if improved performance could be achieved compared with the performance of GaAs. In this study, four materials were examined. These materials were GaP_xAs_{1-x} , $Ga_{1-x}Al_xAs$, $Ga_{1-x}In_xAs$ and $GaAs_{1-x}Sb_x$. Of these four, GaP_xAs_{1-x} and $Ga_{1-x}Al_xAs$ have bandgaps which are greater than that for GaAs (1.439 eV) as x increases, while $Ga_{1-x}In_xAs$ and $GaAs_{1-x}Sb_x$ have bandgaps which are smaller than that for GaAs as x increases.

In order to check the computational technique, a detailed study of the GaAs system was made so that comparison with previous calculations [3-1] could be made. The results of this study are summarized in Table 3-1.

The standard material parameters used for GaAs are listed in Table 3-2. Any deviation from these is listed as a footnote in Table 3-1. The influence of all material parameters was studied, and if no changes in the parameters are indicated in Table 3-1, then there were no changes in cell performance due to these parameters. The AMO conversion efficiencies are in good agreement with those calculated by other authors [3-1 to 3-3]. It should be noted that the transmission coefficient data used in these calculations is representation of that for thin gold films [3-6], and the barrier heights are typical of that for gold on GaAs (0.898 eV) [3-1 to 3-3].

In beginning the calculations, very little experimental data on metalsemiconductor barrier heights was found. Thus, calculations were first made using the emperical relation $\phi_{\rm B} = \frac{2}{3} E_{\rm G}$ [3-12]. Figure 3.1 shows the results of these calculations for ${\rm GaP}_{\rm X} {\rm As}_{1-{\rm x}}$. It can be seen that as temperature increases the conversion efficiency decreases for a given alloy of composition x. Also, for a given cell temperature, the composition for maximum conversion efficiency increases the higher the cell temperature. At 300K, the maximum efficiency is $n_{\rm max} = 11.92\%$ for x = 0.2, compared to the 300K conversion efficiency of 11.66\% for GaAs. This is far below the 20\% improvement

	n _{max} (AMO)	J _{sc} (ma/cm ²)	V _{oc} (V _o H _s)	F.F.
0.898	10.0	36.96	0.463	0.791
0.898	9.96 ^a	36.94	0.462	0.792
0.898	9.93 ^b	36.70	0.462	0.792
0.898	9.57 ^c	35.47	0.461	0.792
0.898	10.36 ^d	35.84	0.463	0.793
0.800	7.51	36.96	0.364	0.756
1.00	12.63	39.96	0.565	0.818
1.00	10.24 ^e	37.06	0.483	0.774
0.898	7.67 ^f	37.06	0.381	0.735
$0.959(\frac{2}{3} E_{G})$	11.66	36.97	0.530	0.810
0.959	10.13 ^g	32.36	0.523	0.812
0.959	13.38 ^h	23.79	0.516	0.806
0.898	8.66 ¹	32.30	0.459	0.791
0.959	4.93 ^j	16.40	0.506	0.804
0.898	11.62 ^k	369.73	0.525	0.810
		16.40	0.444	0.787
a. $W = 10 \ \mu m$	e. T = 3	350K	i. $\tau_p = 1$	0 ⁻¹⁰ sec
b. $W = 5 \mu m$	f. T = 3	350K	j. $T_R = T$	$R^{(\lambda)}$
c. $N_{\rm D} = 10^{17} {\rm cm}^{-7}$	-3 g. τ _{no} =τ	$\tau_{po} = \tau_{p} = 10^{-10} \text{sec}$	k. Concen	tration Ratio

Table 3.1. Summary of Schottky Barrier Solar Cell Performance for GaAs

 ${\tt T}_R(\lambda)$ is the experimentally measured transmission coefficient for thin Au films.

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Table 3.2. Standard GaAs Material Parameters Used in Calculations

$\tau_{po} = 8.5 \times 10^{-9} [3-11]$	$\tau_{no} = 5.3 \text{ x}$ (3-11]	$E_{T} - E_{i} = 0.7 eV$	$p_p = 9.13 cm^2/sec$	$n_i = 1.95 \times 10^6 cm^{-3}$
T = 300K	$N_{\rm D} = 10^{16} {\rm cm}^{-3}$	S = 10 ⁶ cm/sec	W = 100 µm	$r_{\rm p} = 10^{-8} sec$
$A^{**} = 7.63 \text{ amps/cm}^2 \text{ K}^2$	E _G = 1.439 eV	$m_n^* = 0.0636 m_o$	$m_{p}^{*} = 0.68 m_{o}$	$\varepsilon_r = 13.2$

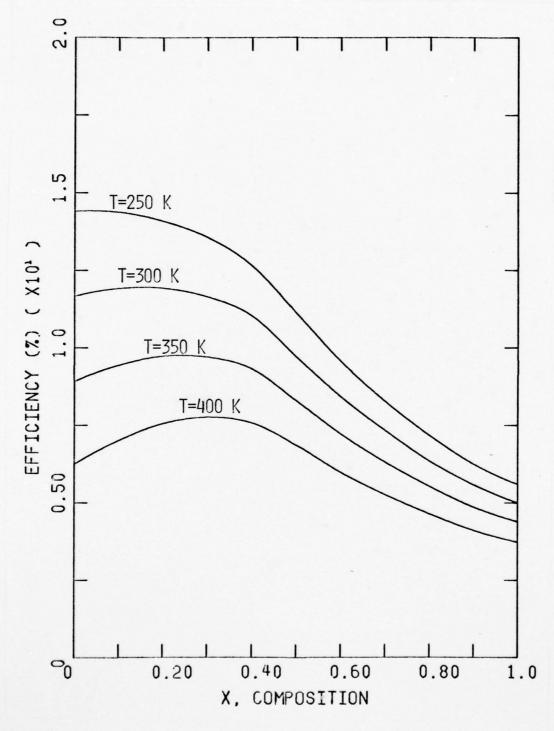


Figure 3.1. AMO conversion efficiency for $GaAs_{1-x} P_x$ Schottky Barrier solar cells as a function of alloy composition X for $\phi = \frac{2}{3} E_G$ and concentration ratio = 1.

experimentally determined for GaP.22^{As}.78 [3-3]. These calculations have all assumed unity transmission coefficient.

Recent experimental measurements of barrier heights for Au Schottky barriers on $\text{GaP}_x \text{As}_{1-x}$ show that instead of $\phi_B = \frac{2}{3} E_G$ the data is best fit by the expression $\phi_B = E_G^{-0.55} \text{ eV} [3-10]$. The cell conversion efficiencies were calculated using this relation and the results are shown in Figure 3.2. In this case, the trends are still the same, although the maximum efficiency as a function of composition is much more pronounced. Here, the efficiency at room temperature for GaP_{.22}As_{.78} is 12.16% while that for GaAs is 9.85%. Thus, the model predicts a 23% improvement in cell efficiency. The quoted experimental values of AMO conversion efficiencies given by Stern and Yeh [3-3] are 10% for GaAs and 12% for GaP_{.22}As_{.78}, or an improvement of 20%. The calculations predict a maximum conversion efficiency of 12.6% for x \approx 0.3.

Figure 3.3 shows a plot of the energy bands (both direct and indirect bands) as a function of composition, along with values for the barrier heights according to the two relations used to calculate the conversion efficiencies in Figures 3.1 and 3.2. Also shown are some experimental values for the barrier height. The experimental values are not in good agreement for the P-rich ternary with x > 0.5.

Tables 3.3 and 3.4 summarize the results of the calculations for both GaP_xAs_{1-x} and $Ga_{1-x}Al_xAs$ ternary alloys as both temperature and solar concentration ratio is varied. As concentration ratio is increased the value of x for maximum efficiency decreases, while the converse is true when temperature increases. Thus, for concentration systems, it seems that there is an optimum value of x in these ternaries which will yield

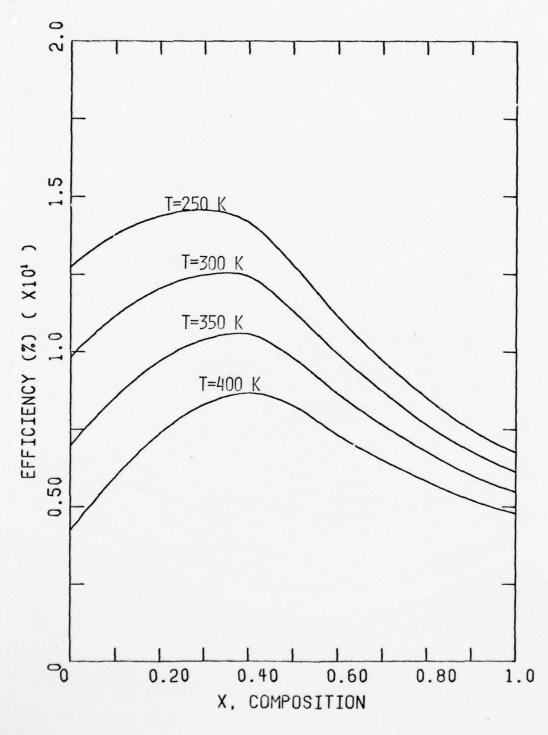


Figure 3.2. AMO conversion efficiency for GaP_xAs_{1-x} as a function of alloy composition for $\phi_B = E_G - 0.55$ eV and concentration ratio = 1.

	<u>A.</u>	GaP _x As _{1-x}	
Temperature °K	Concentration Ratio	Maximum Efficiency, %	x, Composition at
<u> </u>	Katio	Efficiency, %	Maximum Efficiency
250	1	14.455	0.06
	10	15.721	0.0
	100	17.028	0.0
	1000	18.337	0.0
300	1	11.99	0.160
	10	13.321	0.11
	, 100	14.772	0.03
	1000	16.319	0.0
350	1	9.744	0.2
550	10	11.156	0.18
	100	12.651	0.13
	1000	14.294	0.03
400	1	7.782	0.3
	10	9.184	0.27
	100	10.716	0.20
	1000	12.40	0.11

Table 3.3. Summary of Conversion Efficiency Calculations for GaP_xAs_{1-x} and $Ga_{1-x}Al_xAs$ Schottky Barrier Solar Cells Using $\phi_B = \frac{2}{3}E_G$.

B. $Ga_{1-x}A1_xAs$

emperature	Concentration	Maximum	x, Composition at
°K	Ratio	Efficiency, %	Maximum Efficiency
250	1	14.443	0.05
250	10	15.720	0.03
	100	17.026	0.0
	1000	18.335	0.0
300	1	11.960	0.149
	10	13.301	0.08
	100	14.759	0.0
	1000	16.317	0.0
350	1	9.719	0.2
330	10	11.124	0.18
	100	12.623	0.13
	1000	14.281	0.03
400	1	7.777	0.30
	10	9.160	0.23
	100	10.676	0.21
	1000	12.379	0.11

$\frac{A. GaP_{x}As_{1-x}}{x}$								
Temperature °K	Concentration Ratio	Maximum Efficiency, %	x, Composition at Maximum Efficiency					
250	1	14.63	0.29					
	10	15.54	0.25					
	100	16.50	0.23					
	1000	17.48	0.21					
300	1	12.60	0.33					
	10	13.62	0.31					
	100	14.68	0.29					
	1000	15.78	0.25					
350	1	10.63	0.38					
	10	11.73	0.33					
	100	12.90	0.31					
	1000	14.13	0.29					
400	1	8.69	0.38					
	10	9.932	0.36					
	100	11.208	0.36					
	1000	12.514	0.34					

Table 3.4. Summary of Conversion Efficiency Calculations for GaP_xAs_{1-x} and $Ga_{1-x}Al_xAs$ Schottky Barrier Solar Cells Using $\phi_B = E_G - 0.55$ eV.

B. Ga_{1-x}A1_xAs

Temperature °K	Concentration Ratio	Maximum Efficiency, %	x, Composition at Maximum Efficiency
250	1	14.561	0.30
	100	16.430	0.24
300	1	12.537	0.33
	100	14.595	0.29
350	1	10.559	0.35
	100	12.867	0.31
400	1	8.644	0.36
	100	11.153	0.34

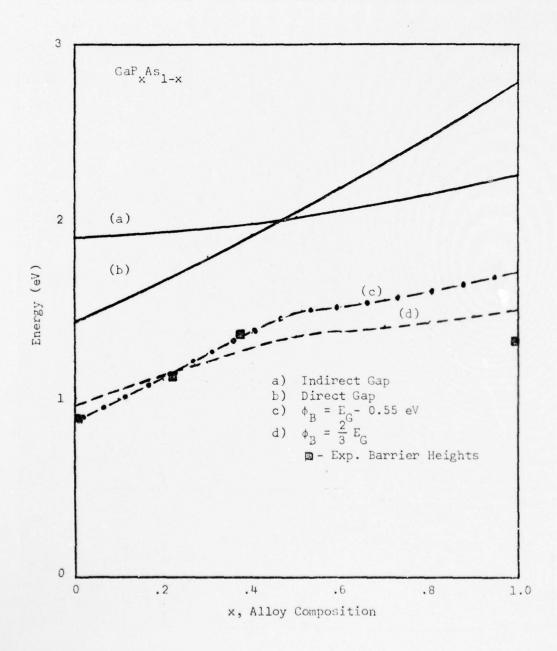


Figure 3.3. Energy bandgaps and barrier heights as a function of alloy composition for ${\rm GaP}_x{\rm As}_{1-x}$

AD-A048 042	SOLAR	RESEARCH TRIANGLE INST RESEARCH SOLAR CELL DESIGN STUDY.(U) AUG 77 M F LAMORTE, J R HAUSER RTI-41U-1259					E PARK	F336	15-76-(F/G 1 C-1283 NL	0/2	2	
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maximum efficiency. The ternaries which seem to offer near optimum conditions are $GaP_x As_{1-x}$ with $x \approx 0.3$ or $Ga_{1-x} Al_x As$ with $x \approx 0.27$.

The ternaries $GaAs_{1-x}Sb_x$ and $Ga_{1-x}In_x$ were also extensively studied. However, all of the calculations showed that GaAs was superior to either of these two alloys, and further discussion of these materials will not be presented.

3.2 MIS Solar Cells

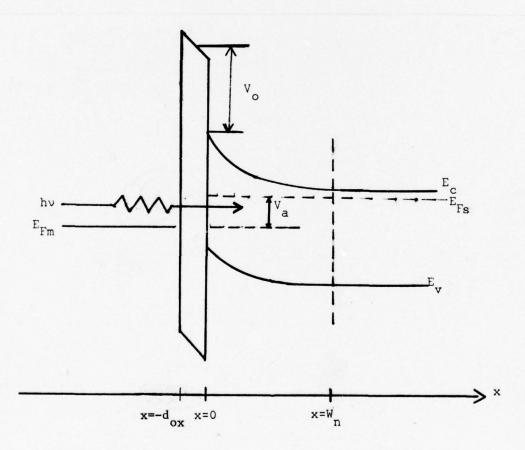
The discussion in the previous section indicates that practical barrier heights for metal-semiconductor Schottky barrier solar cells are limited to a certain fraction of the energy bandgap ($\approx \frac{2}{3} E_{\rm G}$). This factor further places a lower bound on the dark current of the Schottky barrier solar cell, which in turn limits the achievable photovoltaic conversion efficiency. If barrier heights approaching the bandgap could be achieved then conversion efficiencies approaching those p-n junction cells could also be achieved.

There have been several experimental papers published in the last two years [3-13 to 3-17] which indicate that an interfacial layer (oxide layer) purposely introduced between the metal and semiconductor of a Schottky barrier solar cell structure can increase the conversion efficiency of such cells. This interfacial layer is very thin (on the order of a few atomic layers or approximately 20Å-50Å thick) and, in effect, reduces the dark current over that for the Schottky barrier while absorbing essentially none of the incident solar radiation. One can conclude that this physical effect is equivalent to an increase in the barrier height of the structure.

There have been several theoretical discussions of the physics of the MIS solar cell [3-16, 3-18 to 3-20], which elaborate the details of the transport mechanisms. In this paper, a brief discussion will be given which

summarizes these published results and demonstrates the basic nature of the structure.

Figure 3.4 illustrates schematically the band structure of an MIS solar cell. Here $E_{\rm Fm}$ and $E_{\rm FS}$ are the quasi-Fermi levels in the metal and semiconductor, respectively. The total current flow is given by



$$J_{T} = J_{n}(0) + J_{n}(0)$$
(3-9)

Figure 3.4. Schematic Illustration of MIS Solar Cell.

where $J_n(0)$ and $J_p(0)$ are the electron and hole currents, respectively, at x = 0. Now,

$$J_{p}(0) = J_{p}(W_{n}) + J_{u}$$
 (3-10)

Here J_u is the total recombination current in the depletion region, and in general will involve a term due to the optical generation in this region (i.e. $-J_{DR}$ of Eqn. 3-2), a term due to thermal generation-recombination in this region (i.e. J_R of Eqn. 3-3), as well as a term due to recombination through interface states. Also, $J_p(W_n)$ would normally be calculated using a first-order diffusion model, and will be equal to the sum of the terms given by the equations in APPENDIX C, if the insulator does not influence the Boltzmann boundary condition on the minority carriers.

The most important term in establishing the major effect of the insulator on the conversion efficiency of MIS solar cells is $J_n(0)$. Here, Card and Rhoderick [3-18] show that

$$J_{n}(0) = J_{MIS} = A^{**}T^{2} \exp\left(\frac{-\phi_{B}}{kT}\right) \exp\left(\frac{-2\sqrt{2m_{n}^{*}V_{o}}}{\sqrt{n}}d_{ox}\right) \left\{ \exp\left(\frac{qV_{a}}{nkT}\right) - 1 \right\} (3-11)$$

The term exp $(-2\sqrt{2m^*V_o} d_{ox}/\hbar)$ is the transmission coefficient through the oxide based on a WKB approximation to the quantum tunneling problem, and the factor n (the ideality factor) takes into account the fact that part of the applied voltage, V_a , is dropped across the oxide. Ponpon and Siffert [3-16] show that n obeys three different analytical expressions, depending on the nature of the interface states. It is apparent from Eqn. (3-11) that an effective barrier height can be defined as

$$\phi_{\rm BE} = \phi_{\rm B} + \left(\frac{2\sqrt{2m_{\rm n}^*V_{\rm o}}}{\sqrt{n}}\right) kT d_{\rm ox}$$
(3-12)

where V_o is the average surface tunneling barrier height, as shown in Figure 3.4. Also, for investigative purposes the device current can be expressed as

$$J_{\rm T} = J_{\rm MIS} - J_{\rm sc} \tag{3-13}$$

where J_{sc} is defined in Eqn. 3-2. However, this equation holds only as long as $J_{MIS} >> J_R + J_{Diff}$. This may or may not be violated before $\emptyset_{BE} \cong E_G$, and the importance of these terms has not been fully investigated for different materials.

If one takes
$$\phi_{B} = \frac{2}{3} E_{G}$$
 and requires $\phi_{BE} = E_{G}$, then

$$\frac{2\sqrt{2m_{n}^{*}V_{o}}}{\pi} kT d_{ox} = \frac{E_{G}}{3}$$
(3-14)

For GaAs, this requires that

$$V_o d_{ox}^2 \approx 400 \text{ eV}(\text{\AA})^2$$

which for 20Å oxide thickness requires V_0 to be 1 eV, which is a reasonable value. In general for $\phi_{BE} = E_G$, then

 $v_o d_{ox}^2 = 157 \left[E_G(eV) \right]^2, eV(Å)^2$ (3-15)

for $m_n^* = m_o$. Using this model, then one can predict the limit conversion efficiencies originally given by Pulfrey and McQuart [3-4] for Schottky barrier solar cells. For example, these authors predict a maximum conversion efficiency of approximately 25% for a Schottky barrier solar cell with $\phi_B = E_G \simeq 1.4 \text{ eV}.$

Figure 3.5 shows a plot of some recent calculations made by Olsen [3-20], for MIS solar cells designed for optimum oxide thickness. These calculations are discussed in detail in this reference. The results again show the prediction that large efficiencies are possible with MIS solar cells. Much experimental work needs to be done to elucidate these structures, although efficiencies of 15% for GaAs cells have already been reported [3-15].

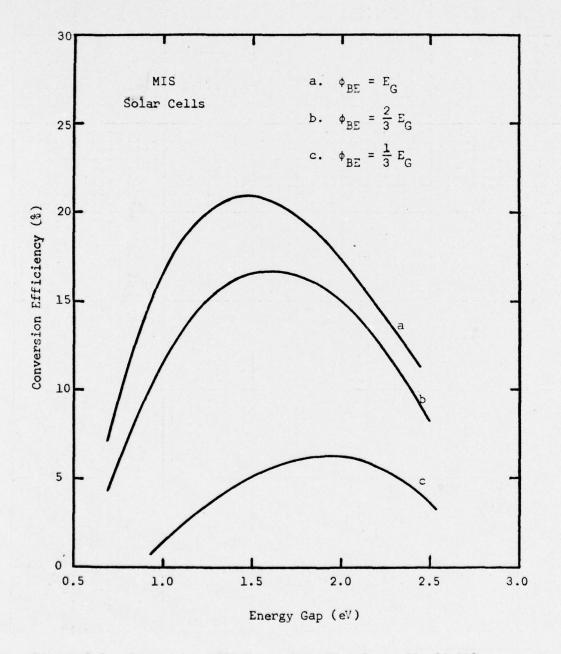


Figure 3.5. Conversion efficiency for MIS solar cells [3-20].

3.3 Assessment of Schottky Barrier and MIS Solar Cell Technologies

At the present time AMO conversion efficiencies of 10% for Schottky barrier cells and 15% for MIS cells have been reported in the literature. These results are for GaAs or GaAs-based ternary compounds. There is currently a significant amount of research activity, both experimental and theoretical, which is being carried out to improve the performance of these cells.

The primary consideration in discussing the utility of these cells is the relationship of total cell cost to total system cost. If cell cost is a small fraction of the total system cost then Schottky barrier solar cells probably do not deserve attention in such systems. The MIS solar cell, in principle, could receive consideration for such systems if the theoretical predictions prove feasible. However, the comparative cost of a high efficiency MIS cell to other high efficiency cells discussed in this report cannot be ascertained at this time. Although the MIS cell seems to be cost competitive with other high efficiency technologies, any discussion of this point seems to be only conjecture.

The ultimate efficiency of MIS cells is uncertain because it is not clear as to how large the energy barrier can be made by the use of various insulating layers. If the barrier height can be made to approach the values obtained with p-n junctions, then the calculated efficiencies are in the same range as those of homojunctions and heterojunctions. However, barriers this large have not so far been experimentally achieved.

When cell cost is a major part of system cost the Schottky barrier and MIS solar cells deserve much consideration. Progress in achieving both low cost silicon and GaAs make MIS cells viable alternatives in

these systems. Although progress has been made in increasing efficiency and solving stability problems in such low cost technologies as the CdS cell, it is possible that silicon and GaAs Schottky barrier cells can become cost competitive with these technologies due to higher achievable efficiencies.

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4.0 GENERALIZED SINGLE AND MULTI-JUNCTION SOLAR CELL CLOSED FORM ANALYSIS

4.1 <u>Steady-State Integral - Differential Continuity Equations for</u> <u>Electro-optical Devices</u>

In order to avoid some of the assumptions made in the conventional analysis of solar cells, an effort was made to obtain the V-I solar cell curve equation in closed form. The first step necessary to accomplish this was to derive a continuity equation (for electrons and holes) which includes the external excitation of the entire solar spectrum. This results in an integral-differential (2nd order) continuity equation. The second step requires the determination of the general solution (the homogeneous and nonhomogeneous parts) to the integral-differential equation. With the appropriate boundary conditions imposed on the general solution, the minority carrier distribution and the diffusion and drift components of electron and hole currents as a function of the photovoltage(s) are obtained. All the device characteristics may now be derived from the V-I cell equation.

In the conventional analysis the steady-state continuity equation that is employed to determine the collection efficiency is given by [4-1]

$$o = \alpha [1-R] N_o e^{-\alpha x} + D_n \frac{d^2 n}{dx^2} + \mu_n E \frac{dn}{dx} - r_n, \qquad (4-1)$$

for electrons in p-type material and

$$o = \alpha [1-R]N_o e^{-\alpha x} + D_p \frac{d^2 p}{dx^2} - \mu_p E \frac{d p}{dn} - r_p$$
 (4-2)

for holes in n-type material.

The equations appropriate for a general electric field and complete solar spectrum generation rate can be derived from the current density and continuity equations. For electrons these are

$$J_{n} = q\mu_{n} nE + qD_{p} \frac{dp}{dx} , \qquad (4-3)$$
$$0 = G_{e} - r_{n} + \frac{1}{q} \frac{dJ_{n}}{dx} . \qquad (4-4)$$

Combining these and using $r_n = \frac{n-n_o}{\tau_n}$ gives

$$0 = G_{e} - \frac{n - n_{o}}{\tau_{n}} + \mu_{n} n \frac{dE}{dx} + \mu_{n} E \frac{dn}{dx} + D_{n} \frac{d^{2}n}{dx^{2}} .$$
 (4-5)

Combining this with the generation rate due to the complete solar spectrum of

$$G_{e} = \int_{0}^{\lambda_{c}} -\frac{n-n_{o}}{\tau_{n}} \alpha (1-R) N_{o} e^{-\int_{0}^{x} \alpha dx'} d\lambda , \qquad (4-6)$$

then finally gives

$$o = \int_{0}^{\lambda_{c}} \alpha (1-R) N_{o} e^{-\int_{0}^{x} \alpha dx'} d\lambda + D_{n} \frac{d^{2}n_{p}(x)}{dx^{2}} + \mu_{n} E(x) \frac{dn_{p}(x)}{dx} + \mu_{n} n_{p}(x) \frac{dE(x)}{dx} - \frac{n_{p}(x) - n_{po}}{\tau_{n}}, \qquad (4-7)$$

where $\alpha(\lambda, \mathbf{x})$ and $E(\mathbf{x})$ are position-dependent. A similar equation exists for holes

$$o = \int_{0}^{\lambda c} \alpha (1-R) N_{o} e^{-\int_{0}^{x} \alpha dx'} d\lambda + D_{p} \frac{d^{2} p_{n}(x)}{dx^{2}} - \mu_{p} E(x) \frac{d p_{n}(x)}{dx} - (4-8)$$
$$- \mu_{p} p_{n}(x) \frac{d E(x)}{dx} - \frac{p_{n}(x) - p_{no}}{\tau_{p}}.$$

For constant field dE(x)/dx vanishes and Eqs. (4-7) and (4-8), which are the equations that will be used in the analytical work, become

$$o = \int_{0}^{\lambda} c \alpha (1-R) N_{o} e^{-\int_{0}^{X} \alpha dx'} d\lambda + D_{n} \frac{d^{2}n_{p}(x)}{dx^{2}} + \mu_{n} E_{o} \frac{dn_{p}(x)}{dx} - \frac{n_{p}(x) - n_{p}}{\tau_{n}}, (4-9)$$

$$o = \int_{0}^{\lambda} c \alpha (1-R) N_{0} e^{-\int_{0}^{X} \alpha dx'} d\lambda + D_{p} \frac{d^{2} p_{n}(x)}{dx^{2}} - \mu_{p} E_{0} \frac{d p_{n}(x)}{dx} - \frac{p_{n}(x) - p_{n0}}{\tau_{p}} \cdot (4-10)$$

The equations for zero field are also required in the analytical work and are obtained by setting $E_0 = 0$. This results in the continuity equation for electrons

$$o = \int_{0}^{\lambda} c_{\alpha}(1-R) N_{o} e^{-\alpha x} d\lambda + D_{n} \frac{d^{2} n_{p}(x)}{dx^{2}} - \frac{n_{p}(x) - n_{po}}{\tau_{n}}$$
(4-11)

and for holes

$$o = \int_{0}^{\lambda_{c}} \alpha (1-R) N_{o} e^{-\alpha x} d\lambda + D_{p} \frac{d^{2} p_{n}(x)}{dx^{2}} - \frac{p_{n}(x) - p_{n0}}{\tau_{n}}. \qquad (4-12)$$

The absorption coefficient has been made to be position-independent in the absence of a non-graded bandgap material in the manipulation of Eqs. (4-9) and (4-10) to obtain Eqs. (4-11) and (4-12). However, the position-dependent absorption coefficient could remain as such in Eqs. (4-9) and (4-11).

4.2 General Solutions to the Steady-State Continuity Equations

In this discussion the general solutions to Eqs. (4-9) through (4-12) are given. Eqs. (4-9) and (4-10) are the electron and hole continuity equations, respectively, for which the established built-in field is constant. The built-in field may be established by grading the bandgap (in a ternary or quaternary) or by grading the net impurity concentration. If the mobility and/or lifetime are position dependent, average values are used. Eqs. (4-11) and (4-12) are obtained from the electron and hole continuity equations, respectively, for which no built-in field is present. The general solution for electrons will be presented since the hole solution may be obtained by inspection.

The general solutions to Eqs. (4-9) through (4-12) contain homogeneous and nonhomogeneous parts. The homogeneous parts represents the general solution to the continuity equation when the generation term arising from the solar flux is zero. Both homogeneous and nonhomogeneous parts, are necessary when the generation term is present.

The general solutions are required to satisfy their respective continuity equations for all x and λ in the range 0 to λ_c , and must satisfy the imposed boundary conditions of the solar cell band structure model. Not all general solutions will satisfy the continuity equation and boundary conditions. The general solutions discussed below satisfy the continuity equation and the imposed boundary conditions. A general solution to Eq. (4-9) for electrons is given by

$$n_{p}(x) = C_{1}e^{\omega_{1}x} + C_{2}e^{\omega_{2}x} + \frac{1}{\omega_{2}-\omega_{1}}[G_{1}(x)e^{\omega_{1}x} + G_{2}(x)e^{\omega_{2}x}]. \quad (4-13)$$

The functions $G_1(x)$ and $G_2(x)$ are defined by

$$G_{1}(x) = \frac{1}{D_{n}} \int_{0}^{x} e^{-\omega_{1}x'} \int_{0}^{\lambda_{c}(x')} \alpha(1-R)N_{o}e^{-\int_{0}^{x'} \alpha dx'} d\lambda dx', \quad (4-14)$$

and

$$G_{2}(x) = -\frac{1}{D_{n}} \int_{0}^{x} e^{-\omega_{2}x'} \int_{0}^{\lambda_{c}(x')} \alpha(1-R)N_{o}e^{-\int_{0}^{x'} \alpha dx''} d\lambda dx' \quad . \quad (4-15)$$

The constants ω and $\omega^{}_2$ are given by

$$\omega_{1} = \frac{\mu_{n} E_{o}}{2 D_{n}} + \sqrt{\left(\frac{\mu_{n} E_{o}}{2 D_{n}}\right)^{2} + L_{n}^{-2}}, \qquad (4-16)$$

$$\omega_{2} = \frac{\mu_{n} E_{o}}{2 D_{n}} - \sqrt{\left(\frac{\mu_{n} E_{o}}{2 D_{n}}\right)^{2} + L_{n}^{-2}} .$$
(4-17)

A similar set of equations exists for the general solution to Eq. (4-11) for holes.

A general solution to Eq. (4-11) for electrons is given by

$$n_{p}(x) = C_{1} \cosh \frac{x}{L_{n}} + C_{2} \sinh \frac{x}{L_{n}} - \int_{0}^{\lambda_{c}} C_{3} e^{-\alpha x} d\lambda$$
, (4-18)

where

$$C_{3} \equiv \frac{\alpha L_{n}^{2} (1-R) N_{o}}{D_{n} (\alpha^{2} L_{n}^{2} - 1)} .$$
 (4-19)

A similar set of equations exists for the general solution to Eq. (4-12) for holes.

Each of the general solutions, Eqs. (4-13) and (4-18) contain two constants of integration, C_1 and C_2 . Since the continuity equations are of the second order, two boundary conditions must be imposed on each solution in order to define a physically realizable model. The two constants are therefore required to satisfy the two boundary conditions.

4.3 Requirements to Interchange Sequence of Integration Between Wavelength and Position in the G_1 and G_2 Integrals

To calculate the solar cell device characteristics, it is necessary to integrate the functions G_1 and G_2 numerically, because the NASA measured solar flux spectrum cannot easily be represented by a mathematical function. The forms given for G_1 and G_2 in Eqs. (4-14) and (4-15), respectively, are time consuming and costly to integrate even when performed on a computer. This may be avoided if G_1 and G_2 are represented in the following forms:

$$G_{1}(\mathbf{x}) = \frac{1}{D_{n}} \int_{0}^{\lambda} c \int_{0}^{\mathbf{x}} e^{-\omega_{1} \mathbf{x}'} \alpha (1-R) N_{0} e^{-\int_{0}^{\mathbf{x}'} \alpha d\mathbf{x}' d\lambda} \qquad (4-20)$$

$$G_{2}(x) = \frac{1}{D_{n}} \int_{0}^{\lambda} c \int_{0}^{x} e^{-\omega_{2} x'} \alpha (1-R) N_{0} e^{-\int_{0}^{x'} \alpha dx''} dx' d\lambda . \quad (4-21)$$

where the integration of x and λ have been interchanged.

It is readily seen in the following manner that this interchange is possible. Since $\alpha = 0$ for wavelengths larger than the bandgap, the upper limit on λ in Eq. (4-14) may be extended to ∞ without a change in value. Then

$$G_{1}(x) = \frac{1}{D_{n}} \int_{0}^{x} e^{-\omega_{1}x'} \int_{0}^{\infty} \alpha(1-R)N_{0} e^{-\int_{0}^{x'} \alpha dx''} d\lambda dx' . \quad (4-22)$$

Since the limits on the λ integration are independent of x the above integrations can be interchanged to

$$G_{1}(x) = \frac{1}{D_{n}} \int_{0}^{\infty} \int_{0}^{x} e^{-\omega_{1}x'} \int_{0}^{\infty} \alpha (1-R)N_{0} e^{-\int_{0}^{x'} \alpha dx''} dx' d\lambda . \quad (4-23)$$

The upper limit on the λ integration may now be reduced to λ_{c} as in Eq. (4-20) where λ_{c} is the wavelength of the smallest bandgap material in the layer under consideration. Similar considerations lead to Eq. (4-21).

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5.0 "POTENTIAL WELL" SOLAR CELL STRUCTURE USING THE A1 Ga As-GaAs MATERIALS SYSTEM

5.1 Introduction

The potential advantages of GaAs over Si for solar cells were recognized early [5-1, 5-2]. Conversion efficiency values of 11 to 12% were reported in 1962 [5-3, 5-4], which at that time were equivalent to or greater than Si cell values. Unpublished data demonstrated GaAs efficiency values exceeding 16% [5-5]. Device parameters limiting efficiency in GaAs cells were also reported [5-6, 5-7]. The recent advances in III-V materials and device technology and their application to solar cells has resulted in significant increases in GaAs efficiency [5-8 to 5-26]. The use of these cells has been extended to concentrator systems [5-22]. These results have stimulated solar cell design in the light of recent advances in technology.

In this Section the Potential Well or PW cell structure, pAlGaAs/ pGaAs/nGaAs/nAlGaAs, is analyzed and the calculation of cell characteristics are accomplished by means of a computer. In each of the 4 distinct subregions, the general solution of the excess minority carrier distribution is obtained from the integral form of the continuity equation. This form of the continuity equation considers the perturbation of the entire solar flux distribution in the cell. Imposing the appropriate boundary conditions gives, in addition to the usual quantities, the solar cell V-I curve from which P_{max} , J_{max} , V_{max} , F, J_{Jn} , and J_{Jp} are calculated. Moreover, from J_{Jn} and J_{Jp} it can be determined whether charge carrier confinement for electrons and holes, respectively, occurs.

This work represents the first attempt to solve for the V-I solar cell curve, in closed form, from the integral form of the continuity

equation. It also represents the first attempt to solve in closed form for electron and hole concentrations in the case where both a built-in field and a barrier to minority carrier flow are both present. The analytical result of this model allows for the determination of the design conditions to optimize overall cell performance.

The absorption coefficient rises sharply at the band edge of direct transition materials, attaining values in excess of 10^5 cm⁻¹ over a significant portion of the solar spectrum [5-24]. For example, 95% of the photon flux above the band edge energy is absorbed at AMO in less than 2 µm of GaAs. At the same time, however, the high surface recombination velocity (S) in conjunction with the high absorption results in a significant reduction in spectral response at short wavelengths. Several approaches have been employed to reduce surface recombination losses: a built-in aiding electric field established by an impurity gradient [5-7, 5-27]; a wide, constant bandgar surface layer serving as an optical window [5-8, 5-8a]; or bandgap grading which also establishes an aiding built-in drift field [5-28 to 5-31]. The first technique does not significantly reduce surface losses. The latter two structures have been effective in improving the spectral response of GaAs homojunction and heterojunction cells. As a result of the application of the recently developed structures. the conversion efficiencies of p-AlGaAs/p-GaAs/n-GaAs [5-30, 5-31] and nAlGaAs/pGaAs [5-31] cells have been calculated and show an improvement over earlier GaAs homojunction cells. In a concentration system of 1700 at AM1.5, similarly constructed cells have yielded 19% efficiency [5-22].

At the other extreme, the absorption coefficient in indirect transition materials rises less sharply at the band edge. In Si, for example, the absorption coefficient is less than 10^4 cm⁻¹ over the portion of the solar spectrum of highest photon flux at AMO [5-23]. A Si layer of 205 µm is required to absorb 95% of the photon flux of energy above its band edge. Typically, solar cells fabricated from indirect transition materials do not exhibit high surface recombination loss. However, indirect transition materials do give rise to other losses--incomplete absorption, high base region recombination, recombination loss at the base region-base contact interface [5-27]. The latter two also affect the photovoltage. Base region recombination may be reduced by increasing the minority carrier diffusion length, while the recombination loss at the base contact is reduced by the low-high junction (LHJ) or back surface field cell (BSF) [5-32].

The Back Surface Field (BSF) n^+pp^+ Si solar cells result in a measurable and reproducible increase in V_{oc} [5-32]. This increase typically lies in the range 30 to 50 mV. The short-circuit current (though apparently more difficult to quantify and less reproducible) and the fill factor also increase [5-33]. In n^+p cells, V_{oc} decreases with decreasing p-region width. In contrast, V_{oc} is insensitive to the p-region width in the n^+pp^+ structure at least in the range 100 to 400 µm [5-33]. These improvements have been shown experimentally to be attributed directly to the barrier established by the heavily doped p^+ region [5-32 to 5-34].

Gunn studied the effects of a barrier such as is represented by the pp⁺ junction [5-35]. For sufficiently long diffusion length, Gunn concluded that minority carrier accumulation may take place [5-35]. Minority carrier

accumulation or carrier confinement serves to reduce dark current and correspondingly increase the photovoltage and fill factor [5-32, 5-33].

Even though the minority carrier diffusion length is inherently short in direct transition materials, the high absorption coefficient allows fabrication of practical structures in which a large fraction of the photon flux generates electron-holes pairs in a region less than one diffusion length from the p-n junction. Correspondingly, the base region-contact interface recombination loss is negligible in typical solar cell structures fabricated from direct transition materials. Thin film, direct transition solar cell structures are receiving increased attention because material costs may be reduced by more than two orders of magnitude where the substrate seed can be eliminated. Technology has been developed for the III-V materials systems from which solar cells of several micrometers thickness may be fabricated. Moreover, due to the versatility and compatibility of the AlGaAs graded bandgap regions to establish aiding drift fields and junction barriers, such as the pp barrier in Si cells, to achieve minority carrier confinement in both regions su-rounding the GaAs p-n junction to increase the photovoltage and fill factor.

5.2 "Potential Well" (PW) Structure

Figure 5.1 shows the band structure of the PW cell. The GaAs homojunction is sandwiched between graded bandgap layers of $Al_xGa_{1-x}As$. The ternary AlGaAs is chosen because it exhibits a bandgap range required to optimize cell performance, and it forms the best lattice match with GaAs over a wide range of alloy compositions [5-36]. Double-heterostructure GaAs-Al_xGa_{1-x}As laser diodes reduced threshold current density for lasing

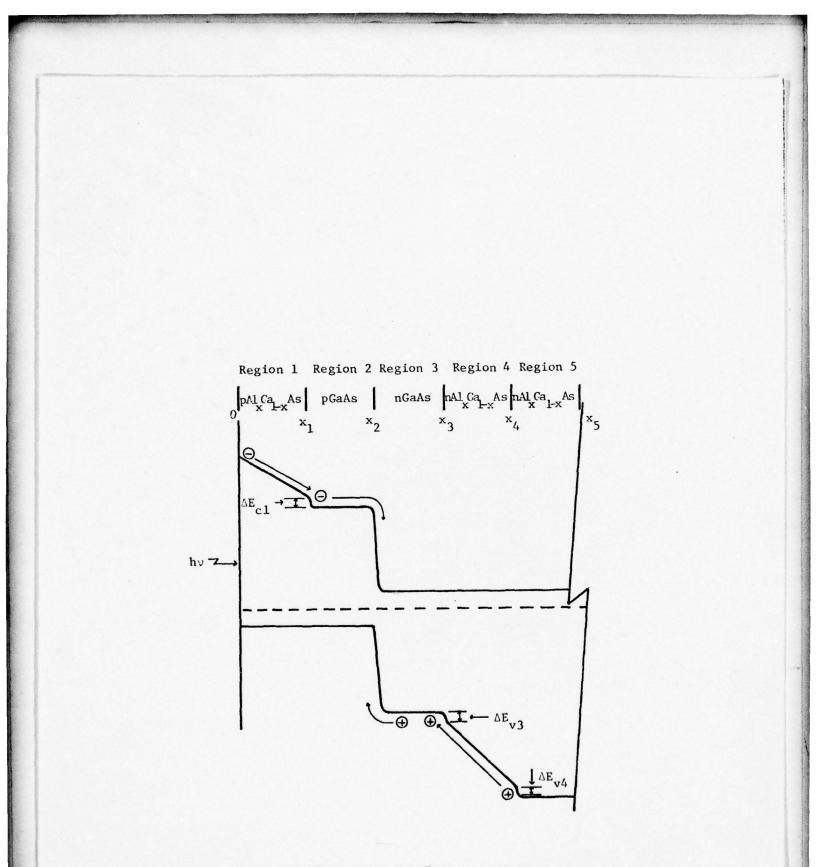


Figure 5.1. "Potential Well" Solar Cell Structure

through carrier confinements [5-37]. This behavior is further strengthened by the low recombination rate measured at AlGaAs-GaAs interfaces [5-38]. <u>REGION 1</u>: The Al_xGa_{1-x}As bandgap is made to decrease linearly such that a constant negative built-in electric field is established. This negative field accelerates electrons flowing toward the p-n junction, thereby reducing bulk recombination in this region. Surface recombination loss is also reduced due to the drift field. In addition, the bandgap (being larger than for GaAs) serves as a window for the majority of the solar flux.

The layer also serves as an additional conducting path for the terminal load current. By highly doping this layer, the sheet resistance may be reduced to very low values. The high doping level and the corresponding low minority carrier diffusion length in this region is not as critical to spectral response because of the presence of an aiding field. REGION 2: Due to the presence of Region 1 and its high doping level, the design of Region 2 does not need to have imposed on it the conditions for a low conducting path for the terminal current. As a result, Region 2 may be more lightly doped (i.e., 10^{16} to 10^{17} cm⁻³) in order to realize higher lifetime, mobility and absorption coefficient as well as to obtain a superior quality metallurgical and electronic p-n junction. Typically, solar cells without a window layer require surface concentration values in excess of 5 x 10^{19} (usually 5 x 10^{19} to 10^{21} cm⁻³) to minimize resistive losses. In Si this may result in a "dead layer" in which the lifetime is estimated to be 100 psec or less [5-39]. In such cases, the efficiency is reduced because of lower spectral response and a high dark current is observed with a consequence that V oc, J sc and F decrease.

In the case where the p-GaAs is lightly doped, the mobility and lifetime are higher and its absorption coefficient rises more rapidly and attains higher values than more heavily doped material. This allows for a thinner p-GaAs layer without suffering bulk recombination or incomplete absorption loss. Moreover, in conjunction with the aiding built-in field in Region 1 and the barrier, ΔE_{c1} , at x_i (both of which restrict electrons in Region 2 from entering Region 1 and then recombining) and a thinner Region 2, the conditions are established to obtain carrier confinement in Region 2. This reduces the dark current and increases V_{oc} and F.

REGION 3: The design considerations for Region 3 are similar to those for Region 2. The doping level may also be in the same range as for Region 2 (i.e., 10^{16} to 10^{17} cm⁻³) and inherently higher lifetime, mobility and absorption coefficient are realized. As in Region 2, this contributes to a superior metallurgical and electronic p-n junction. Due to the high absorption coefficient, the layer may be made thin (i.e., micron range) without incurring incomplete absorption loss. Analogous to Region 2, the excess holes in Region 3 are restrained from entering Region 4 and recombining due to the aiding built-in field in Region 4 and the barrier ΔE_{y3} , formed by the discontinuity in the valence band at x3. These all combine to increase the probability of making the Shockley diffusion the dominant transport mechanism. Together with hole accumulation in the n-GaAs region, the dark current is reduced with a consequent increase in V_{oc} and F. This portion of the PW structure has similarities to the BSF Si solar cell, except in the PW band edge structure the barrier height, ΔE_{v2} , may be made greater than the pp barrier of the BSF Si cell and to serve as a more effective

barrier for carrier confinement. Moreover, the drift field in Region 4 may be made greater and also aid to confine holes to Region 3. <u>REGION 4</u>: The bandgap increase is manifested through a negative slope in the valence band edge. This results in a negative field which serves to accelerate holes toward the p-n junction and to confine holes to Region 3. This aids in reducing the dark current and increasing $V_{\rm oc}$ and F.

5.3 Results and Discussion

In this section the results of the calculations are discussed. Calculations are made on the PW structure for which each of the regions is 10^{-4} cm thick and for which the bandgap of the AlGaAs at the surface and at the base is 1.739eV (0.713 micrometers) giving a value of x = 0.258 [5-40, 5-41]. The material parameters used in the calculations are taken from the literature. There is general agreement in the GaAs data for electron and hole lifetime and diffusion length [5-42 to 5-51], and mobilities [5-52 to 5-54]. The AlAs data, while not as extensive, is also available [5-52]. To obtain alloy parameters, an interpolation method is used [5-54], where data is not available (See APPENDIX B). The ternary direct and indirect bandgap values are determined by well known relationships [5-40, 5-41]. All calculations have been performed at AMO [5-55].

$p-A1_xGa_{1-x}$ As Layer Acceptor Concentration

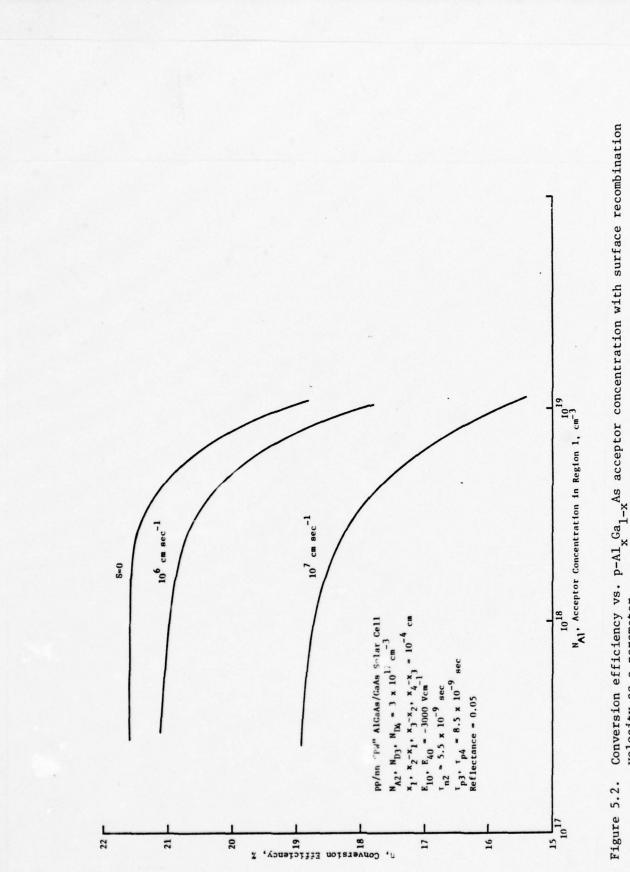
In Section 5.2 we discussed the useful design functions which Region 1 (AlGaAs) serve. One of these is the conduction path for terminal current. In this connection, a low resistance conducting path (obtained through optimized design of doping level and thickness of Region 1) is desired.

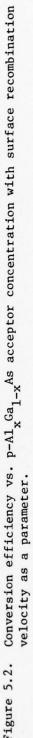
The competing design parameters are electrons diffusion length, photon flux absorbed through the layer and sheet resistance or impurity concentration, with surface recombination velocity as a parameter. These calculations show that efficiency drops significantly when the acceptor concentration exceeds 3×10^{18} cm⁻³.

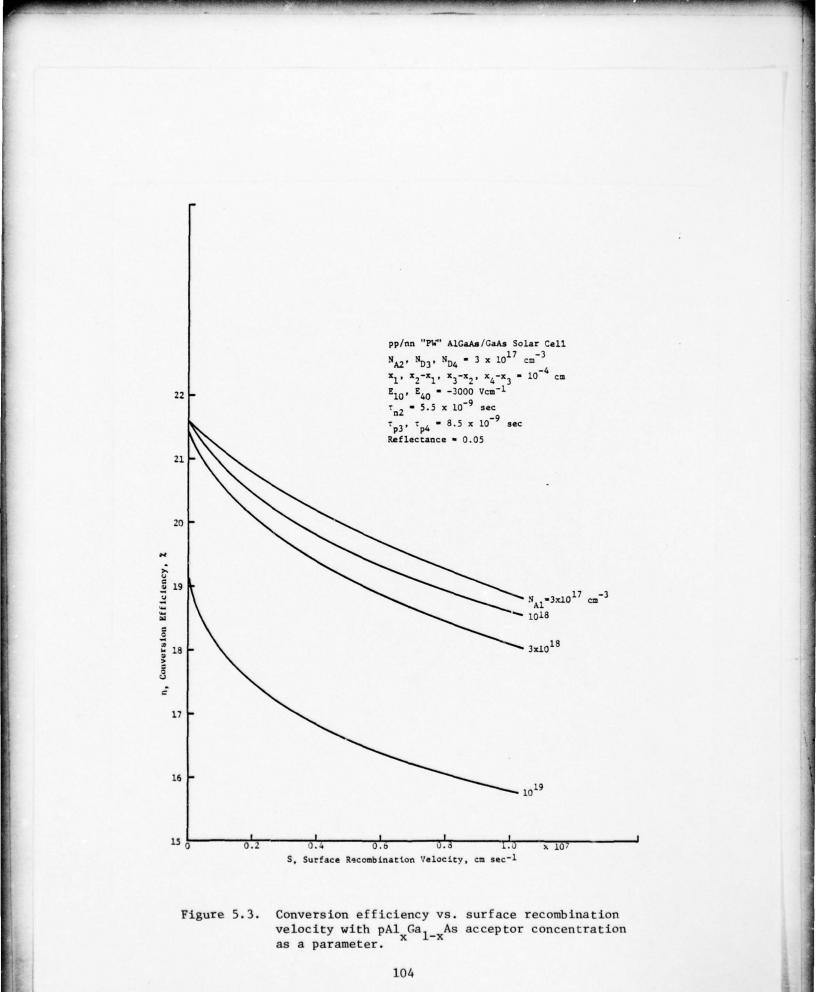
Figures 5.2 and 5.3 summarize the results of nine computer runs for which the V-I curve, maximum power, short-circuit current density, open circuit voltage, form factor, voltage at maximum power point and spectral response were calculated. These curves show that efficiency decreases markedly above 3 x 10^{18} cm⁻³ acceptor concentration in the p-A1_xGa_{1-x}As. This results because of a decrease in both electron lifetime (due to the introduction of recombination centers) and electron mobility (due to increased ionized impurity scattering) with increasing acceptor concentration. The efficiency is also reduced with increasing surface recombination velocity. These calculations are presented in Figure 5.3 in which the independent variable (N_{A1}) and the surface recombination velocity (S) are interchanged in order to more clearly exhibit the effect of surface recombination velocity.

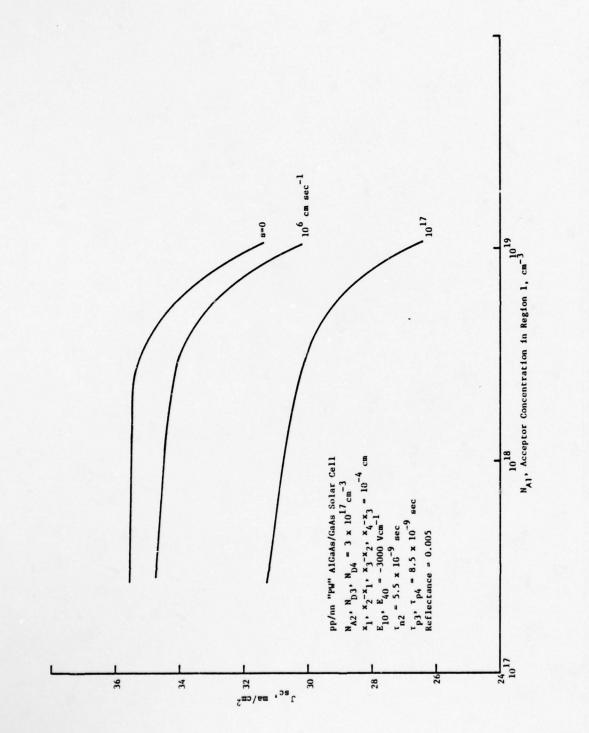
For completeness the short-circuit current density vs. the acceptor concentration in the $p-Al_xGa_{1-x}As$ layer is shown in Figure 5.4. The shape of the family of curves is similar to those in Figure 5.2.

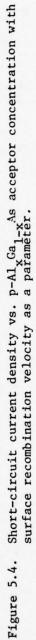
Figure 5.5 shows the reciprocal of the carrier confinement factor, R_n , for electrons in the p-GaAs layer and the dark current vs. $p-Al_xGa_{1-x}As$ acceptor concentration. R_n is the factor by which dark current is decreased as compared with the case of pure diffusion away from the junction into an infinitely thick layer. The R_n coefficient (APPENDIX

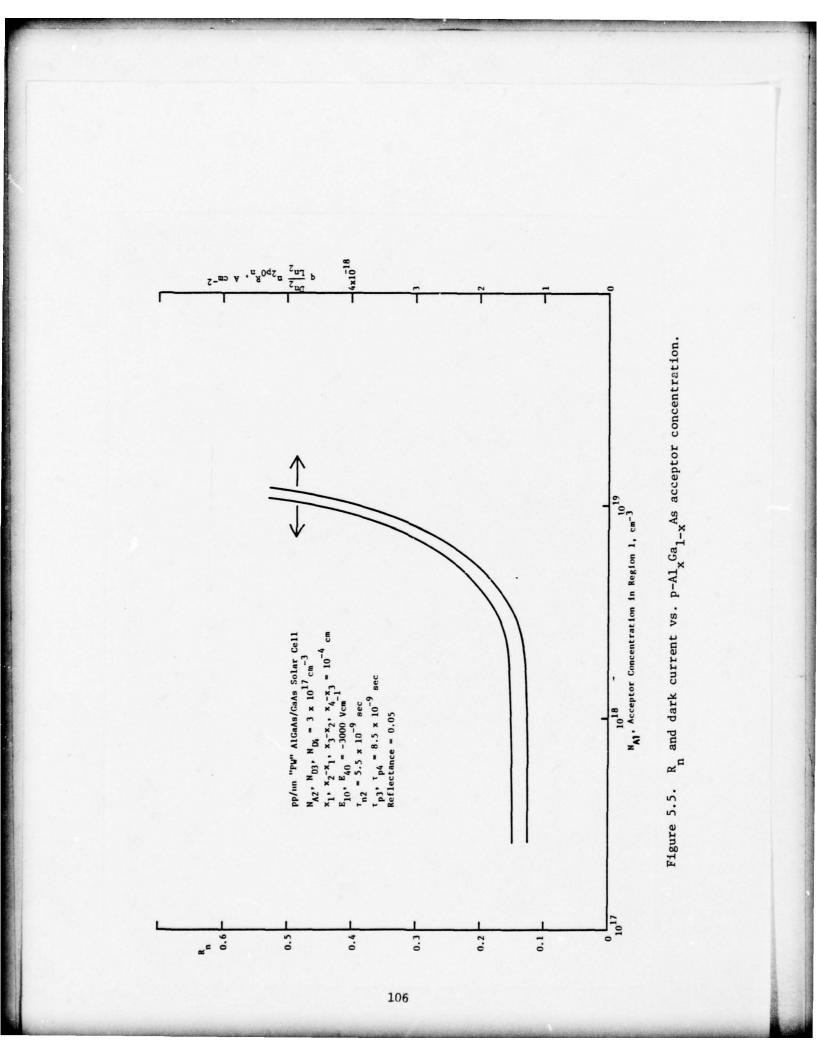








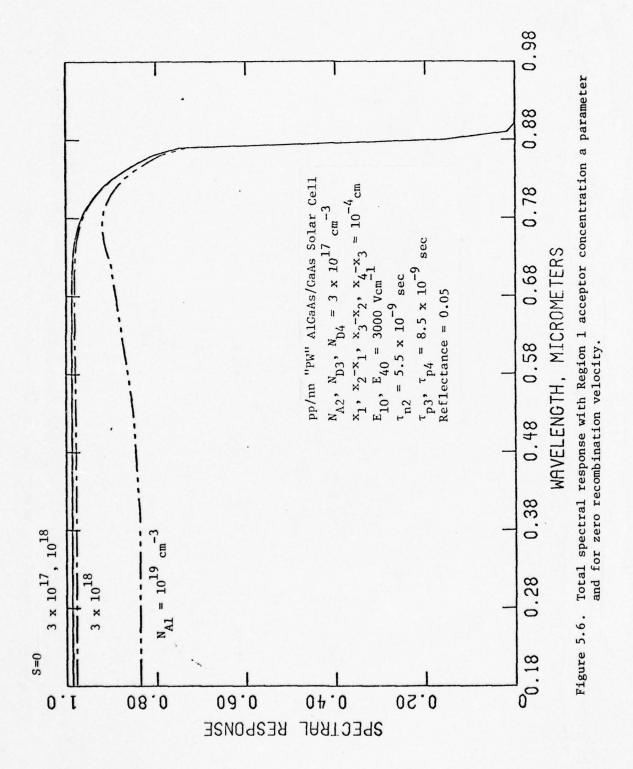


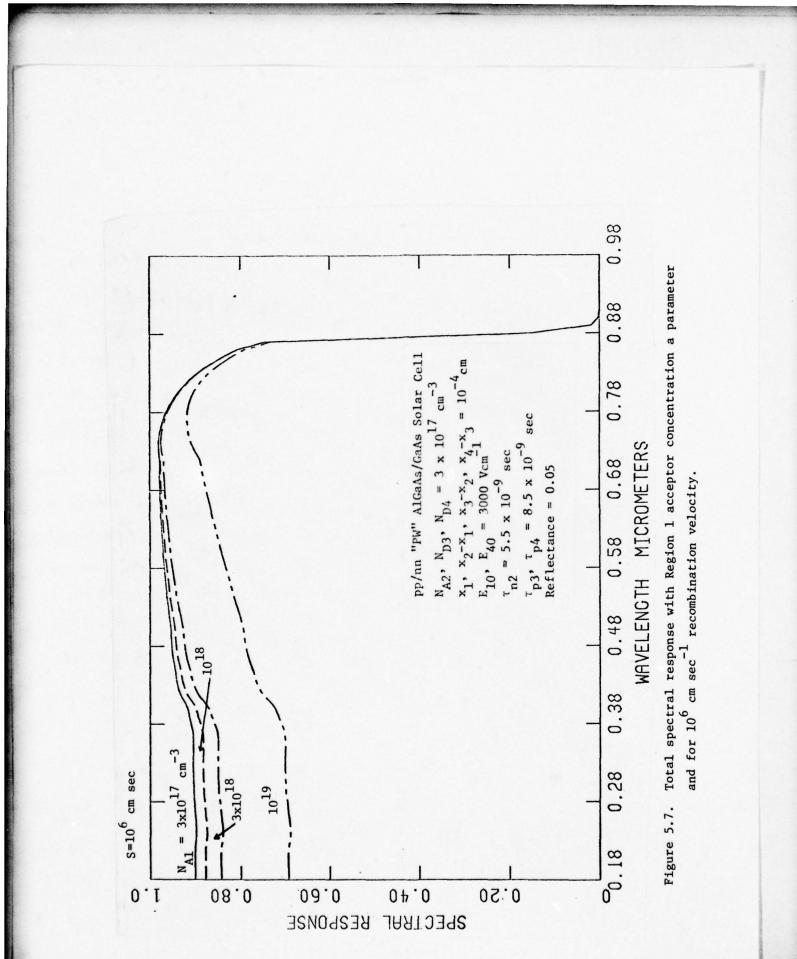


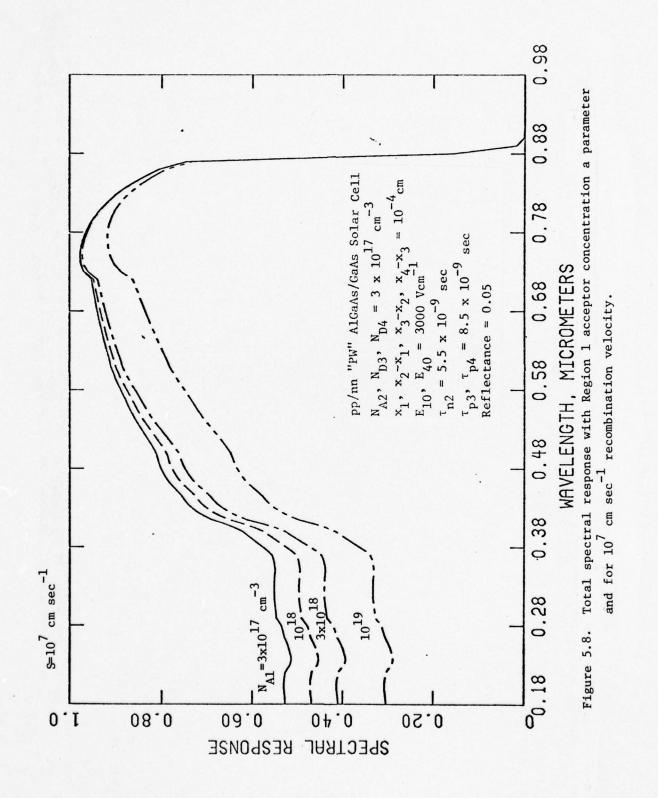
F, Eqs. (F-27) and (F-28)) is unity when the minority carrier diffusion length is small compared to the semiconductor thickness. Figure 5.5 shows that below 3×10^{18} cm⁻³ the dark current and the R_n coefficient are constant and that the dark current is lower by nearly an order of magnitude than that obtained when carrier confinement does not occur. For concentration levels in the p-AlGaAs layer of 3×10^{18} cm⁻³ and lower, the carrier confinement in the p-GaAs layer is high enough to significantly reduce the dark current.

With increasing acceptor concentration in the p-AlGaAs layer, the electron recombination in this layer increases. Because $\Delta E_{cl} = 0$ in this calculation, minority carriers injected into Region 2 from Region 3 (due to the photovoltage) traverse Region 2, without appreciable recombination, and enter Region 1 where they experience an increased recombination rate. This results in reducing the carrier confinement in Region 1 as is shown in Figure 5.5 and increasing the electron contribution to dark current.

As further support of the above results and the interpretation, the spectral response is shown in Figures 5.6, 5.7 and 5.8 for zero, 10^6 and 10^7 cm sec⁻¹ surface recombination velocity, respectively, with Region 1 acceptor concentration as a parameter. The three sets of curves show reduced collection efficiency for increasing S over the spectral range, except at the band edge. However, the percentage change is greatest and relatively constant in the range $\lambda < 0.38 \ \mu m$ in each of the curve sets. The spectral response curves, in Figure 5.6 for zero recombination velocity, show a small change in the concentration range 3×10^{17} to 3×10^{18} cm⁻³. This small change is due to the value of the ratio L_{n1}/x_1 being considerably







greater than unity over this concentration range which results in an imperceptible change in efficiency as shown in Figure 5.2. For 10^{19} cm⁻³ the ratio L_{n1}/x_1 is of the order of unity or less due to the marked decrease in electron mobility and lifetime, resulting in increased bulk recombination over the entire spectral range. However, the spectral response change is discernible over the entire concentration, 3×10^{17} to 10^{19} cm⁻³, for 10^6 and 10^7 cm sec⁻¹ SRV as Figures 5.7 and 5.8 show. This is reflected in a detectable change in efficiency for high surface recombination velocity and shown in Figure 5.2.

The curves in Figures 5.6, 5.7, and 5.8 generally show a drop in spectral response in the spectral range $\lambda \leq 0.38 \ \mu\text{m}$. For convenience we may define $\lambda_w = 0.38 \ \mu\text{m}$ as the window wavelength over which the largest portion of the photon flux is absorbed in Region 1, and, therefore most sensitive to the electron diffusion length decrease as the acceptor concentration increases.

Table 5.1 shows the electron mobility and lifetime used in the device characteristic calculations; it also lists the calculated values of L_{n1} and L_{n1}/x_1 . The latter ratio is seen to be greater than unity for 3×10^{18} cm⁻³ and lower.

And a state we shall be a state of the state				
NAL	^µ n1	τ _{nl}	^L n1	L _{n1} /x ₁
$3 \times 10^{17} \text{ cm}^{-3}$	$3150 \ \frac{\mathrm{cm}^2}{\mathrm{v-sec}}$	$5.5 \times 10^{-9} sec$	6.58×10^{-4} cm	6.58
10 ¹⁸	2425	5×10^{-9}	5.5 $\times 10^{-4}$	5
3×10^{18}	1875	1.9×10^{-9}	3.0×10^{-4}	3.0
10 ¹⁹	1400	1.8×10^{-10}	7.9 x 10^{-5}	0.79

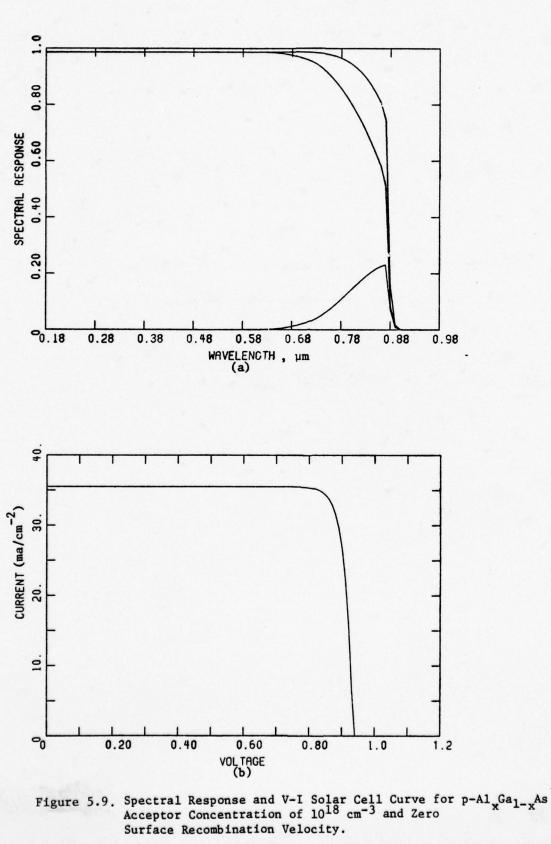
Table 5.1. Region 1 material parameters used in the calculation.

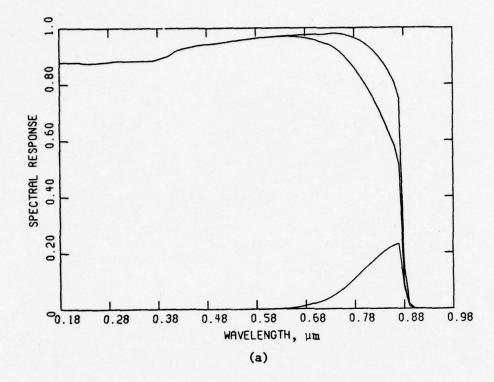
A concentration of 10^{18} cm⁻³ has been selected for Region 1 as a compromise device parameter. The electron, hole and the electron plus hole collection efficiency and the corresponding V-I solar cell curve are presented in Figures 5.9, 5.10 and 5.11 for zero, 10^6 and 10^7 cm sec⁻¹ surface recombination velocity. The hole spectral response is independent of surface recombination velocity. From Figure 5.5 we see that the dark current is in the neighborhood of its minimum for 10^{18} cm⁻³, therefore, there is an imperceptible change in V_{oc} with increasing surface recombination velocity. However, the V-I curves shows J_{sc} to decrease with increasing recombination velocity. This is reflected in the decrease of electron spectral response.

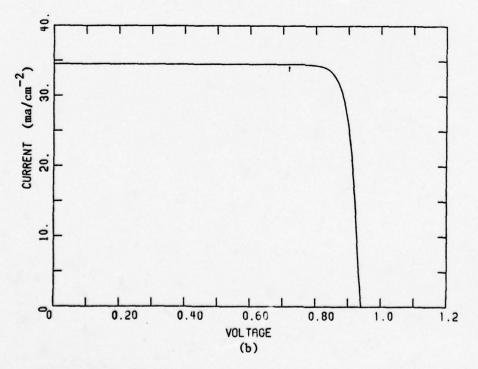
Window Layer, Region 1, Built-in Aiding Electric Field

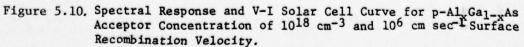
In the preceding discussion the window layer acceptor concentration was optimized with a built-in field strength of -3000 V cm⁻¹. Accepting the optimized value of 10^{18} cm⁻¹, the influence of the electric field strength (and correspondingly, ΔE_{c1} , APPENDIX F, Eq. (F-3)) on efficiency has been studied.

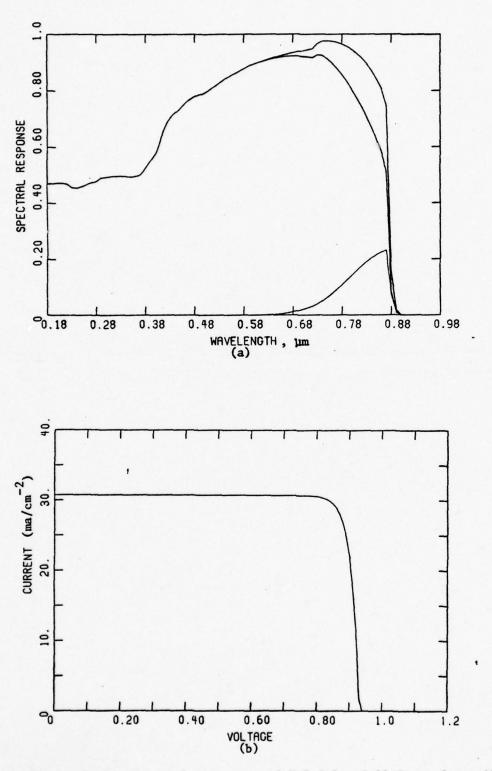
Figure 5.12 shows the conversion efficiency dependency on the aiding built-in drift field present in Region 1 with the recombination velocity a parameter. In this calculation the bandgap at the surface was maintained constant at 1.739 eV and ΔE_{c1} was changed from 0 to 0.3 volt to achieve the desired field strength. The efficiency is 22% and constant for zero recombination velocity. This arises because the diffusion length in Region 1 is greater than the Region 1 thickness and, in the absence of recombination velocity, the majority of the excess electrons diffuse into Region 2.

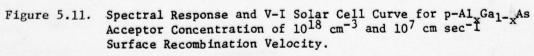


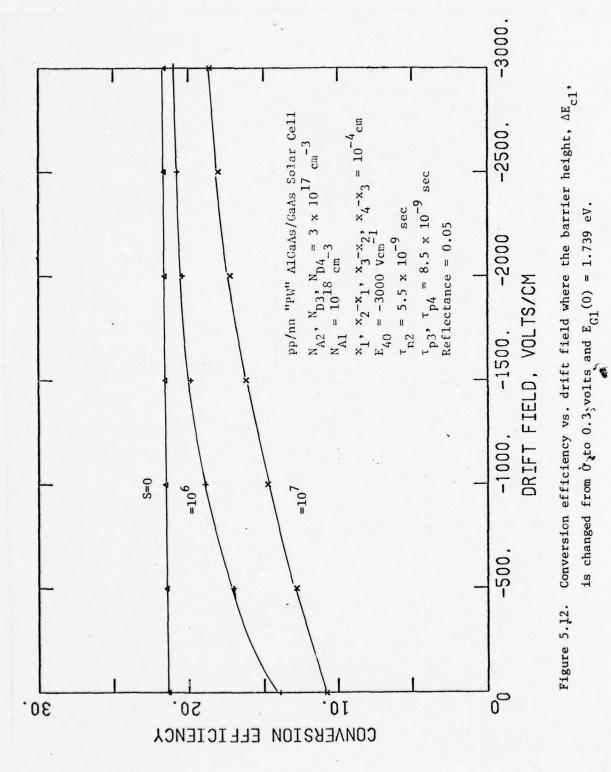










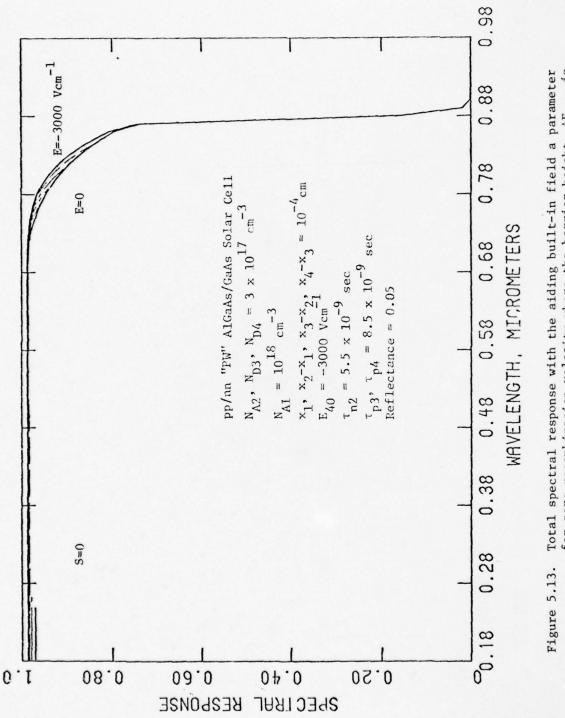


The electron diffusion length in Region 2 is also greater than the Region 2 thickness and therefore, most of the electrons in Region 2 (whether produced there or not) are collected by the p-n junction.

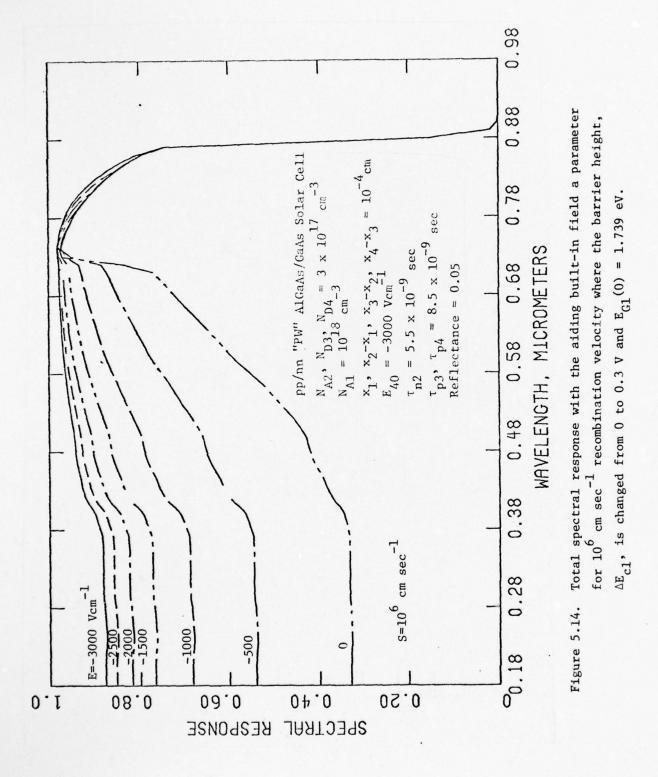
Increasing the surface recombination velocity to 10^6 and 10^7 cm sec⁻¹ results in a significant reduction in efficiency for all field strengths, particularly at low field strengths. Efficiency increases for increasing field values. At field strengths less than 500 Vcm⁻¹ and 10^7 cm sec⁻¹ SRV, the efficiency is reduced by 50% or more.

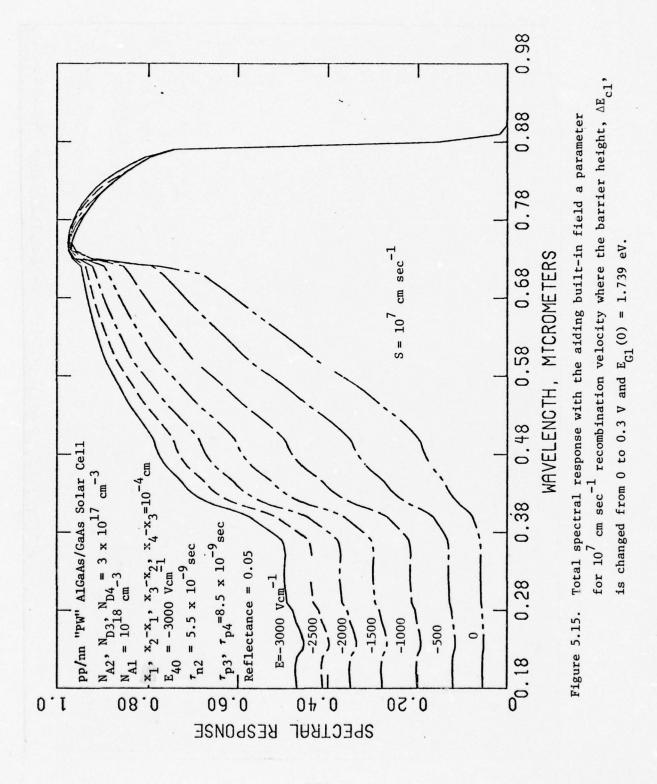
Figures 5.13, 5.14, and 5.15 show the total spectral response, electrons plus holes, with the field varying from 0 to -3000 Vcm⁻¹, for surface recombination velocity values of 0, 10^6 and 10^7 cm sec⁻¹, respectively. In the spectral region $\lambda < 0.73$ micrometers, the field strength has only a small influence on the spectral response up to 10^7 cm sec⁻¹. This is due to the window-effect of the AlGaAs Region 1. The wavelength for which the spectral response increases sharply for $E_{10} = 0$ is denoted λ_w , the window wavelength. In Figures 5.14 and 5.15, $\lambda_w = 0.73$ micrometers. It is the shortest wavelength which is not absorbed appreciably in Region 1 allowing photons at longer wavelengths to pass through unattenuated to the pGaAs Region 2 layer. Thus, in this spectral region the recombination velocity has almost no influence.

In Figure 5.13, for which the surface recombination velocity is zero, the spectral response exhibits only small changes. However, for high recombination velocity, there is a strong field dependency in the spectral region $\lambda < \lambda_w$ as indicated in Figures 5.14 and 5.15. Moreover, for a given recombination velocity the influence of the field strength on the response in the region $\lambda < 0.38$ micrometers is very nearly uniform. In



Total spectral response with the aiding built-in field a parameter for zero recombination velocity where the barrier height, $\Delta E_{c1},$ is changed from 0 to 0.3 V and $E_{G1}(0) = 1.739 \text{ eV}$.

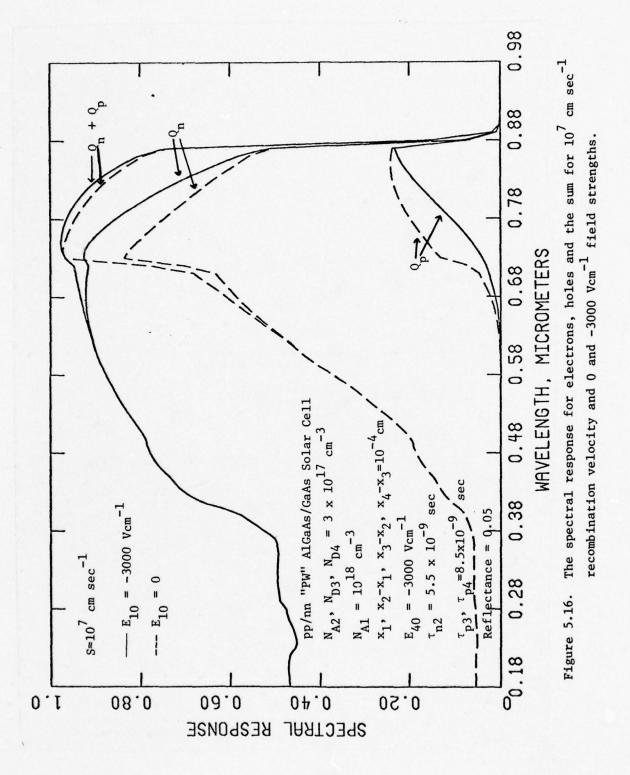




this spectral region of Figure 5.14 for which the recombination velocity is 10^{6} cm sec⁻¹, there is nearly a 300% improvement as the field strength is increased to -3000 Vcm^{-1} . In contrast, when the recombination velocity is increased to 10^{7} cm sec⁻¹, Figure 5.15 shows an order of manitude improvement in response between 0 and -3000 Vcm^{-1} in this spectral region. This spectral region, $\lambda < 0.38$ micrometers, represents the region over which the absorption coefficient is greater than 10^{6} cm^{-1} in Region 1. This suggests that excess electrons produced in the range 100 to 300 Ű from the surface are those which are greatly affected by the surface recombination velocity and the field strength. The estimate of the thickness over which surface recombination losses occur is consistent with the discussion in APPENDIX F (Eq. (F-19)).

The influence of field on electron and hole spectral response is shown in Figure 5.16 for 10^7 cm sec⁻¹ surface recombination velocity. The structure of the -3000 Vcm⁻¹ field case has the bandgap linearly decreasing from 1.739 eV at the surface to 1.439 eV at x_1 . The 0.3 volt drop over one micrometer results in the -3000 Vcm⁻¹ field strength. For the zero field case, the bandgap in the AlGaAs Region 1 layer is constant at 1.739 eV. The latter case results in greater absorption in Region 1 in the photon energy range above 1.739 eV (0.713 micrometers), while this wavelength the photons traverse Region 1 unattenuated.

Due to the increased flux beyond λ_{w} for the zero field case, the hole spectral response in the n-type Region 3 is greater than for the high field case. The difference between the hole response curves in Figure 5.16 is a measure of the higher incident flux on Region 3. At the same time, recombination losses (surface and bulk) are higher in Region 1 in the absence



of an aiding field. Therefore, the difference between electron response curves in Figure 5.16 in the range $\lambda < \lambda_w$ is a measure of the increased losses. The increase in electron response for the high field case in the range $\lambda < \lambda_w$ is due to the collection of excess electrons in Region 1. In the region $\lambda < \lambda_w$ the net electron and hole responses do not compensate and result in a slightly higher response for the high field case.

In Section 2.0 we discussed the useful design functions which the Region 1 AlGaAs serve. One of these is a conduction path for terminal current. In this connection, a low resistance conducting path, obtained through optimized design of doping level and thickness in Region 1, is desired. The competing design parameters are electrons diffusion length, photon flux absorbed through the layer and sheet resistance. Figure 5.2 shows the conversion efficiency vs. Region 1 acceptor concentration, with surface recombination velocity as a parameter. These calculations show that efficiency drops significantly when the acceptor concentration, approaches 10^{19} cm⁻³. The percentage change is approximately 10% for all values of S. At lower field strengths the percentage change is greater for a given S value.

Temperature Behavior

High temperature operation is one of the advantages of GaAs and other wide bandgap III-V solar cells over Si cells. This is especially important in concentrator systems.

The maximum power output from a solar cell can be written as

$$P = F V I (5-1)$$

where V_{oc} and I_{sc} are the open circuit voltage and short circuit current, respectively, and F is the V-I curve fill factor. The change in power output with respect to temperature may be written as [3]

$$\frac{dP}{dT} = P \left[\frac{d\ln F}{dT} + \frac{d\ln V_{oc}}{dT} + \frac{d\ln I_{sc}}{dT} \right]$$
(5-2a)

or in normalized form as

$$\frac{d\ln P}{dT} = \frac{d\ln F}{dT} + \frac{d\ln V_{oc}}{dT} + \frac{d\ln I_{sc}}{dT}$$
(5-2b)

The change in conversion efficiency at AMO is given by

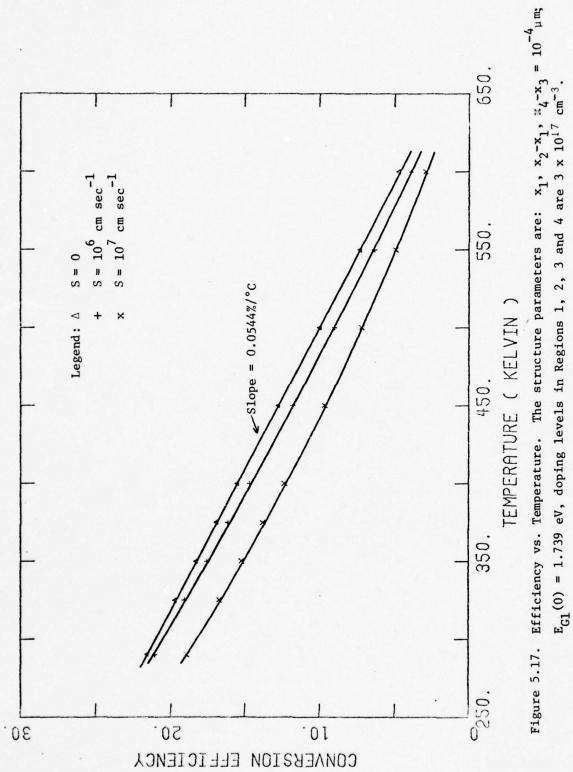
$$\frac{d\eta}{dT} = \frac{1}{0.1353} \frac{dP}{dT}$$
 (5-3)

where P is given in watts per cm². The first and second terms in Eqs. (5-2a) and (5-2b) are almost always negative while the third term tends either to increase slightly or remain constant (it is almost never negative). The typical increase in I_{sc} with increasing temperature, however, is usually not sufficient to offset the decrease in V_{oc} and F, leading to decreasing power output with increasing temperature. The temperature coefficients for power output, Eq. (5-2a), and for conversion efficiency, Eq. (5-3), are convenient and practical figure-of-merits for solar cells. From Eqs. (5-2a) and (5-3) we note that both temperature coefficients are linearly proportional to the power. Therefore, higher efficiency cells and/or cells subjected to concentrated incident solar energy will exhibit higher temperature coefficients. Thus, in comparing cells the normalized form, Eq. (5-2b) may be enlightening.

Table 5.2 shows the temperature coefficients for GaAs and Si cells [5-3, 5-4]. The efficiency of these cells at ambient temperature is comparable (\approx 11%) so that the terms in Eq. (5-2a) are listed. These data show that the temperature coefficient for output power of the GaAs cell is only one-half of the Si cell value. The logarithmic changes of V_{oc} and F are of a smaller magnitude for GaAs than for Si. On the other hand the short circuit current increase is greater for Si than it is for GaAs.

	Table 5.2.	Temperature cha	inges in power	output [5-3, 5-4].	
•	$P \frac{dln(I_{sc})}{dT}$	$P \frac{d\ln(V_{oc})}{dT}$	$P \frac{d \ln(F)}{dT}$	$(\frac{dP}{dT})$ Meas.	
GaAs	+ 0.018	- 0.044	- 0.030	- 0.050 mw/°C	
Si	+ 0.024	- 0.091	- 0.046	- 0.095 mw/°C	

Figure 5.17 shows the PW calculated cell efficiency as a function of temperature where the initial efficiency at 290°K is approximately 20%. The slope of the S = 0 curve is constant at 0.0544%/°C or 0.074 mw/°C. This calculated value is approximately 50% higher than the measured GaAs value in Table 5.2. However, if the temperature coefficient is normalized with respect to power output, the measured normalized coefficient is 0.0034/°C while the PW cell calculated value is 0.0027/°C which is in fair agreement considering that the cells are of different structure. While the curves for 10^6 and 10^7 cm sec⁻¹ surface recombination velocity show a slight bowing, they are represented to a fair approximation by the same



slope as for the zero recombination velocity. The slopes of the 10° and 10^{7} compared to zero recombination velocity are slightly higher in the region < 450°K but smaller in the region > 450°K.

The major material and structural parameters which give rise to the efficiency decrease have also been studied. As shown in the analysis of APPENDIX E, temperature affects the V-I curve. The effect of temperature is observed through I_{sc} , V_{oc} and F in the power relationship, Eq. (5-1). The V-I curve, I_{sc} , V_{oc} and F are all greatly influenced by the diffusion length. Diffusion length almost always decreases with increasing temperature above ambient. The decrease in diffusion length arises directly from the mobility dependence on temperature, since in general the diffusion length is given by

$$L = \sqrt{\frac{kT}{q}} \mu \tau \qquad (5-4)$$

In the calculation of temperature behavior, the electron mobility temperature dependency was taken to be $T^{-2.3}$ for electrons and T^{-2} for holes [5-52]. While the lifetime usually increases with increasing temperature above ambient, in these calculations the lifetime value reported at 290°K was used throughout the range 290 to 600°K. To the degree that this occurs, the temperature calculations are conservative. Therefore, in Eq. (5-4) the diffusion length for electrons is proportional to $T^{-1.15}$ and for holes at T^{-1} . This functional dependence is shown in Figure 5.18 for electron and hole diffusion length in their respective regions, denoted by the subscripts 1, 2, 3 and 4.

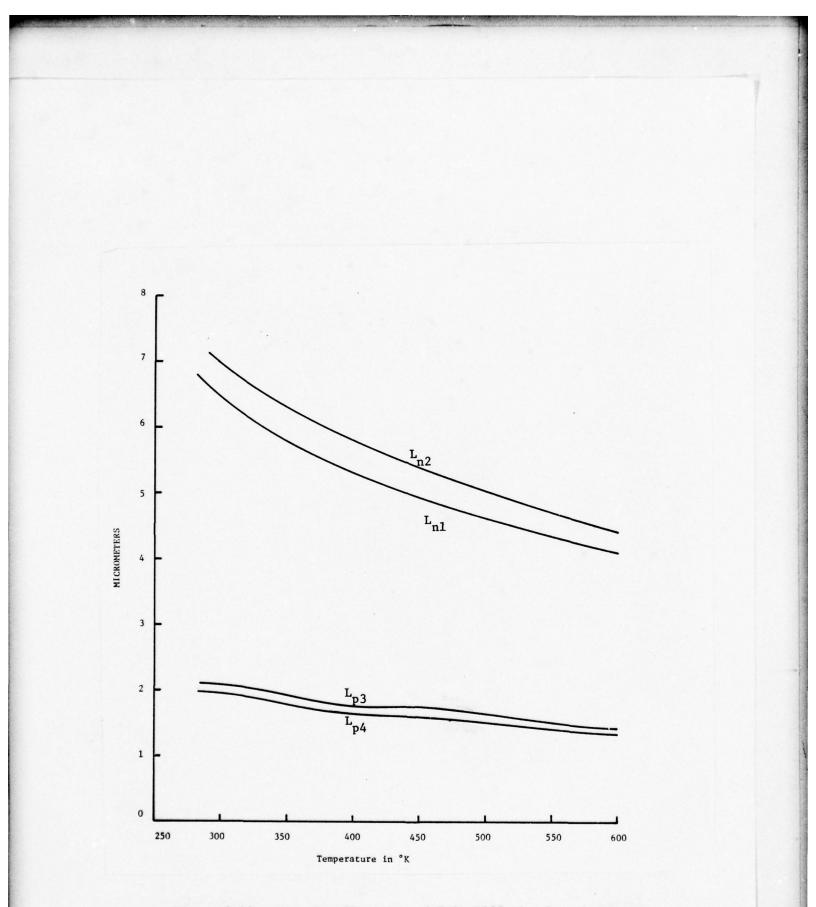


Figure 5.18. Minority Electron and Hole Diffusion Length vs. Temperature in each of the Regions of the PW Cell Structure.

The short circuit current may be sensitive to temperature through the minority carrier diffusion length and bandgap narrowing. Figure 5.19 shows the short circuit current vs. temperature for 0, 10^6 and 10^7 cm sec⁻¹ surface recombination velocity. In the absence of surface recombination loss, the short circuit current increases due to bandgap narrowing, and is the dominant mechanism with increasing temperature. As the surface recombination loss increases, SRV increasingly compensates for the current increase due to bandgap narrowing. For 10^6 cm sec⁻¹ recombination velocity the short circuit current is shown to decrease slightly with increasing temperature while at 10^7 cm sec⁻¹ the current decrease is greater than for 10^6 cm sec⁻¹.

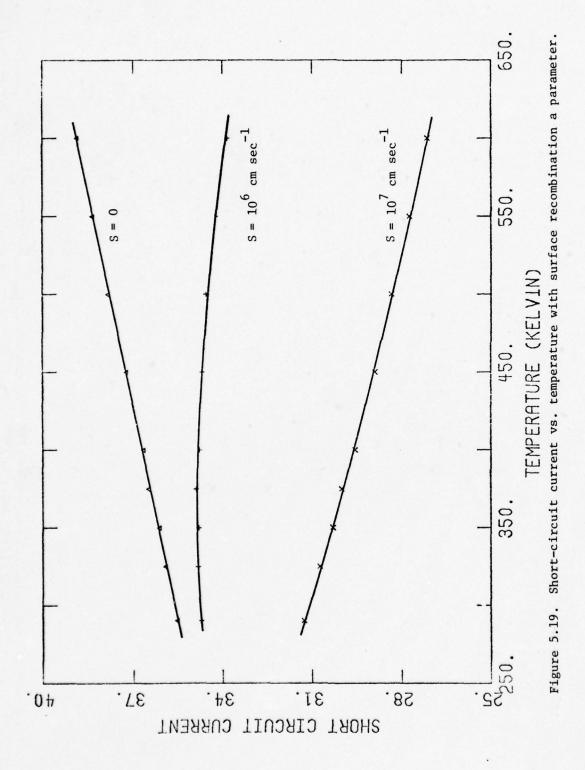
The assumed general expression for the direct bandgap temperature dependency is

$$E_{Gd}(x,T) = E_{Gd}(x,0^{\circ}K) - \left(\frac{dE_{Gd}}{dT}\right)_{x} T \qquad (5-5)$$

where x is the alloy composition, E_{Gd} (x,0°K) the extrapolated direct bandgap value at 0°K and of composition x and $\left(\frac{dE_{Gd}}{dT}\right)_x$ is the direct bandgap temperature coefficient in the region 250 to 600°K. The bandgap of the alloy at 0°K is given by [5-41].

$$E_{cd} = 0.468 x^2 + 1.042 x + 1.544$$
 (5-6)

This expression is similar to the relationship used at elevated temperature in which the constant term, 1.544, has been determined to give consistent results over the temperature range of interest. The temperature coefficient



for GaAs is 3.6 x 10^{-4} eV/°K [5-48] and for AlAs, it is 4 x 10^{-4} eV/°K [5-48]. The coefficient for the alloy Al_xGa_{1-x}As is assumed to be a linear extrapolation given by

$$\left(\frac{dE_{Gd}}{dT}\right)_{x} = \left(\frac{dE_{Cd}}{dT}\right)_{AlAs} - \left[\left(\frac{dE_{Gd}}{dT}\right)_{AlAs} - \left(\frac{dE_{Gd}}{dT}\right)_{GaAs}\right](1-x). \quad (5-7)$$

The bandgap relationship for GaAs becomes

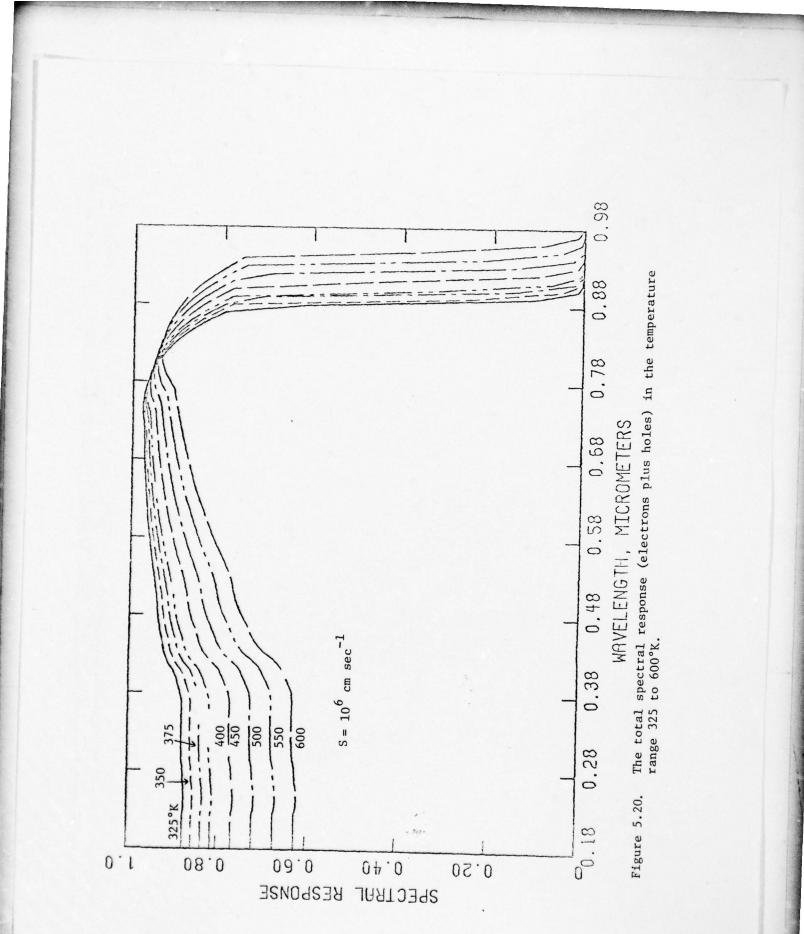
$$E_{Gd}$$
 (T) = 1.544 - 3.63 x 10⁻⁴ T. (5-8)

For the alloy, E_{Gd} is calculated from Eq. (5-6) and $\left(\frac{dE_{Gd}}{dT}\right)_{x}$ from Eq. (5-7) and substituted into Eq. (5-5). The bandgap values at a given temperature, T, are then entered as input parameters into the computer program. Moreover, the bandgap changes are also required in the calculation of the intrinsic carrier concentration given by

$$n_{i}(x,T) = n_{i}(x,T_{1}) e^{-\frac{1}{2} \left[E_{Gd}(x,T)/kT - E_{Gd}(x,T_{1})/kT_{1} \right]}.$$
 (5-9)

Due to the different rates of bandgap narrowing with temperature, the built - in field values in Regions 1 and 4 may decrease slightly to -2900 from -3000 Vcm^{-1} .

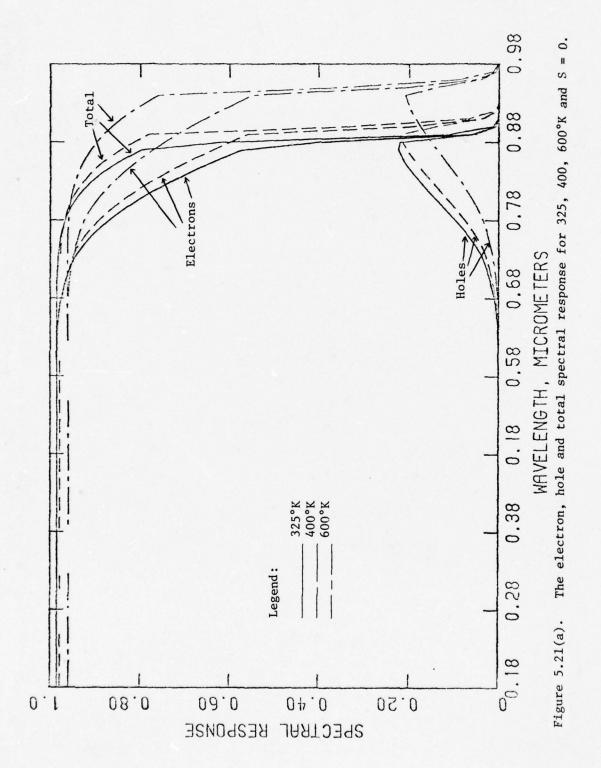
The total spectral response (electrons plus holes) of the solar cell is shown in Figure (5.20) with temperature as a parameter. This family of curves shows that while the response decreases in the spectral region $\lambda < 0.8 \ \mu\text{m}$ it increases in the region $\lambda > 0.8 \ \mu\text{m}$. The wavelength point at which this crossover occurs increases with increasing temperature. In the region $\lambda < 0.38 \ \mu\text{m}$ the response decreases by 30% from 325 to 600°K.

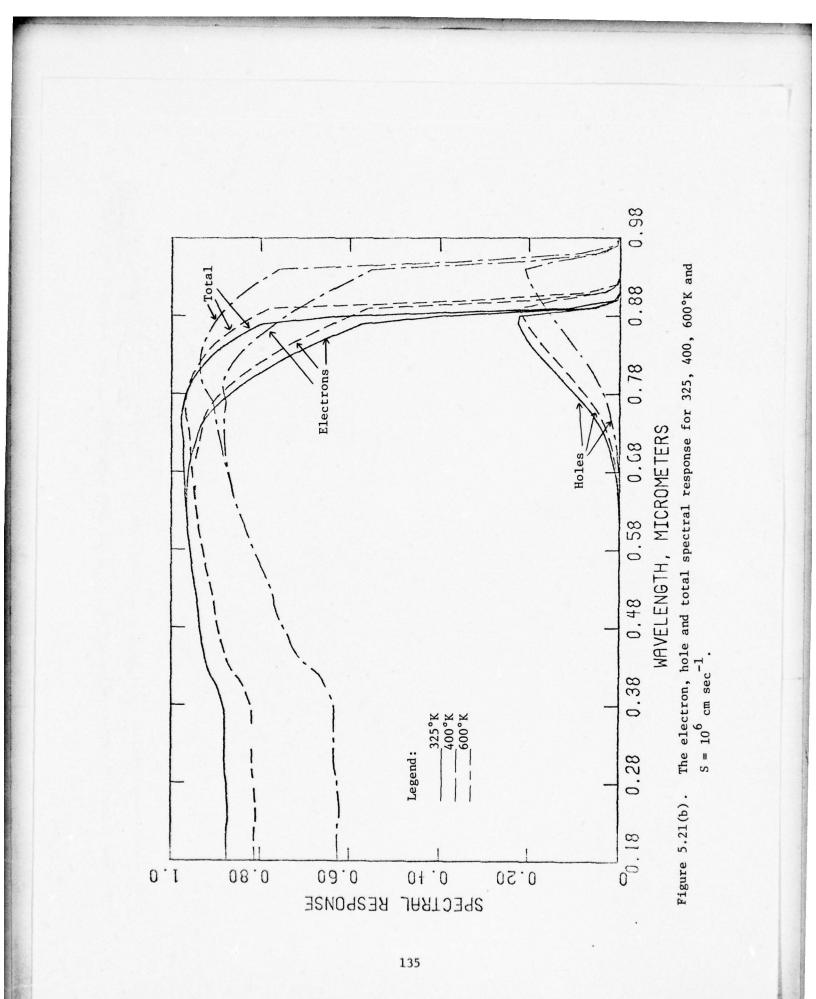


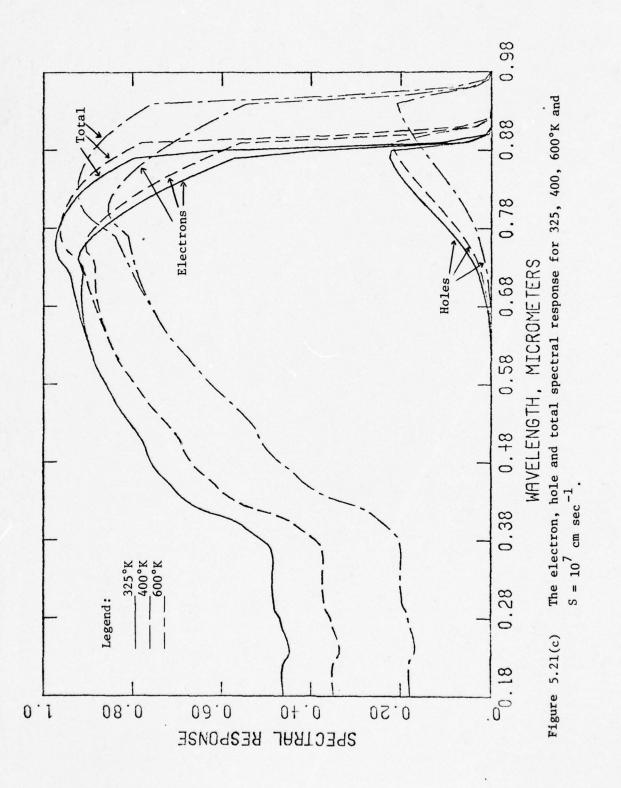
Similarly, it is seen in Figure (5.18) that each of the diffusion lengths also decrease, approximately, 30% in this temperature range. Thus, we can attribute the decrease in response in the region $\lambda < 0.8 \ \mu\text{m}$ to the decrease in diffusion length. On the other hand, the increase in the range $\lambda < 0.8 \ \mu\text{m}$ is due entirely to bandgap narrowing and the increased photon absorption. This is clearly seen in Figure (5.20) by the cut-off wavelength increasing to higher values with increasing temperature, from 0.90 to 0.98 \ mm. The response for 290°K is only slightly better than the 325°K and was not shown for that reason.

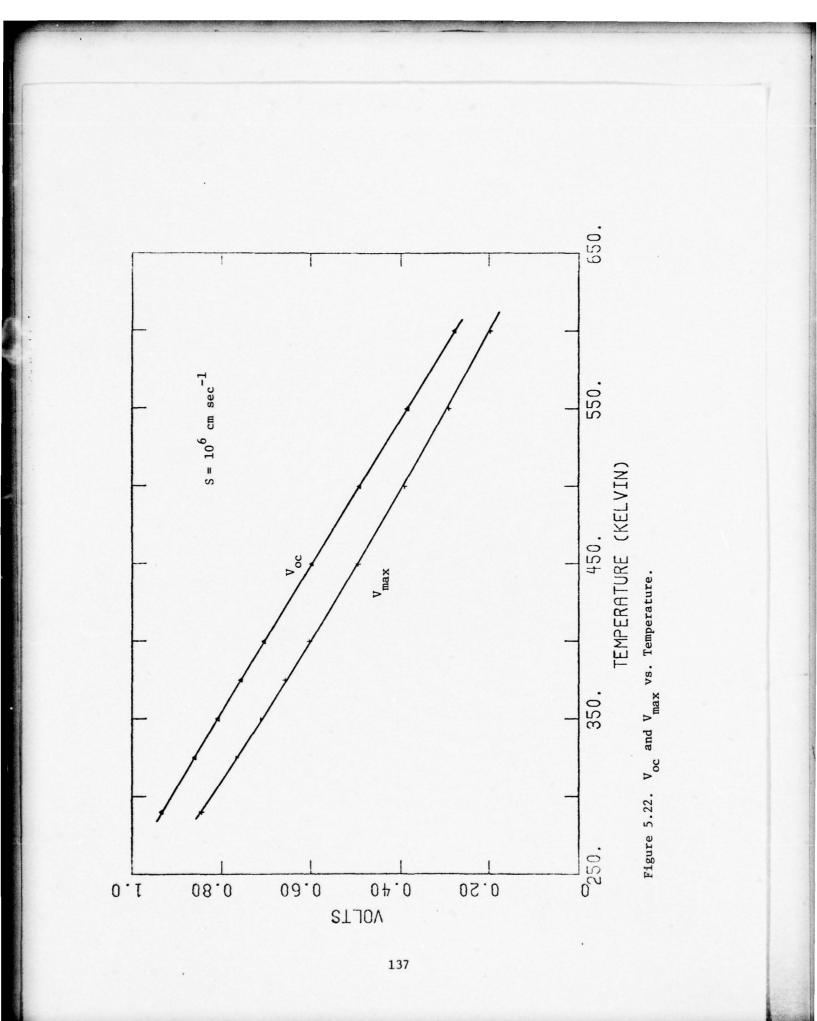
Figures (5.21(a)), (5.21(b)), and (5.21(c)) show the electron, hole and total response for 325, 400 and 600°K and surface recombination velocities of 0, 10^6 , and 10^7 cm sec, respectively. In general for $\lambda < 0.38$ µm, the change from 290 to 325°K is only of the order of 1 to 3%.

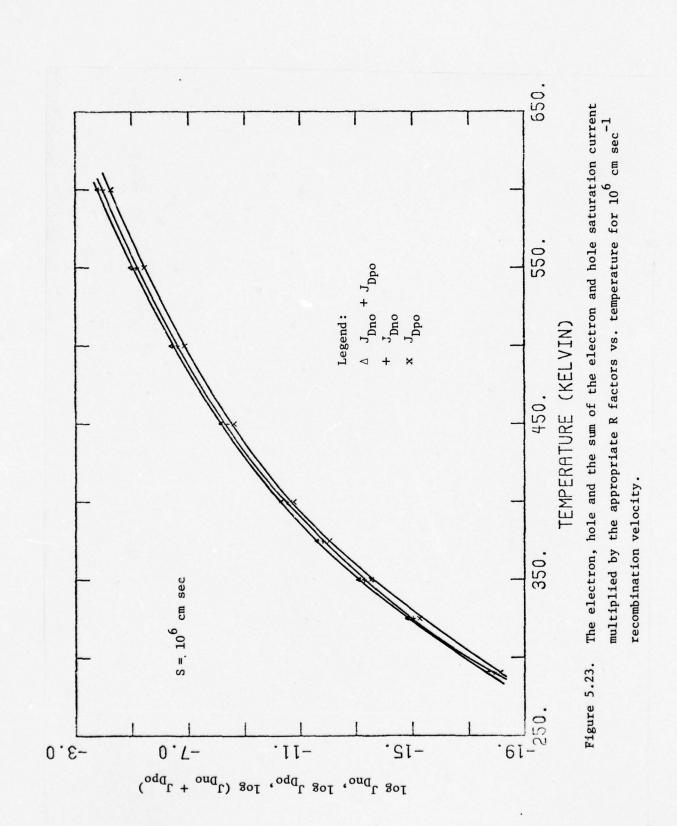
The voltage at the maximum power point on the V-I curve, V_{max} , and V_{oc} are plotted as a function of temperature in Figure (5.22) for 10⁶ cm sec⁻¹ recombination velocity. These calculations show the rapid drop off in photovoltage with increasing temperature. Since the short circuit current for 10^{6} cm sec⁻¹ is not very sensitive to temperature, the dark current is the device parameter with is responsible for the decrease in voltage. This is seen in Figures (5.23) where the sum of the saturation currents multiplied by the appropriate R- factors, R_n or R_p , for electrons and holes are calculated as a function of temperature. (Referring to the analysis in APPENDIX E, the ordinate is the sum of Eqs. (E-27) and (E-63) divided by $(e^{qV_2/kT}-1)$ where V_2 is the photovoltage at the homojunction.) The sum increases by many orders of magnitude which serves to greatly reduce the photovoltage.





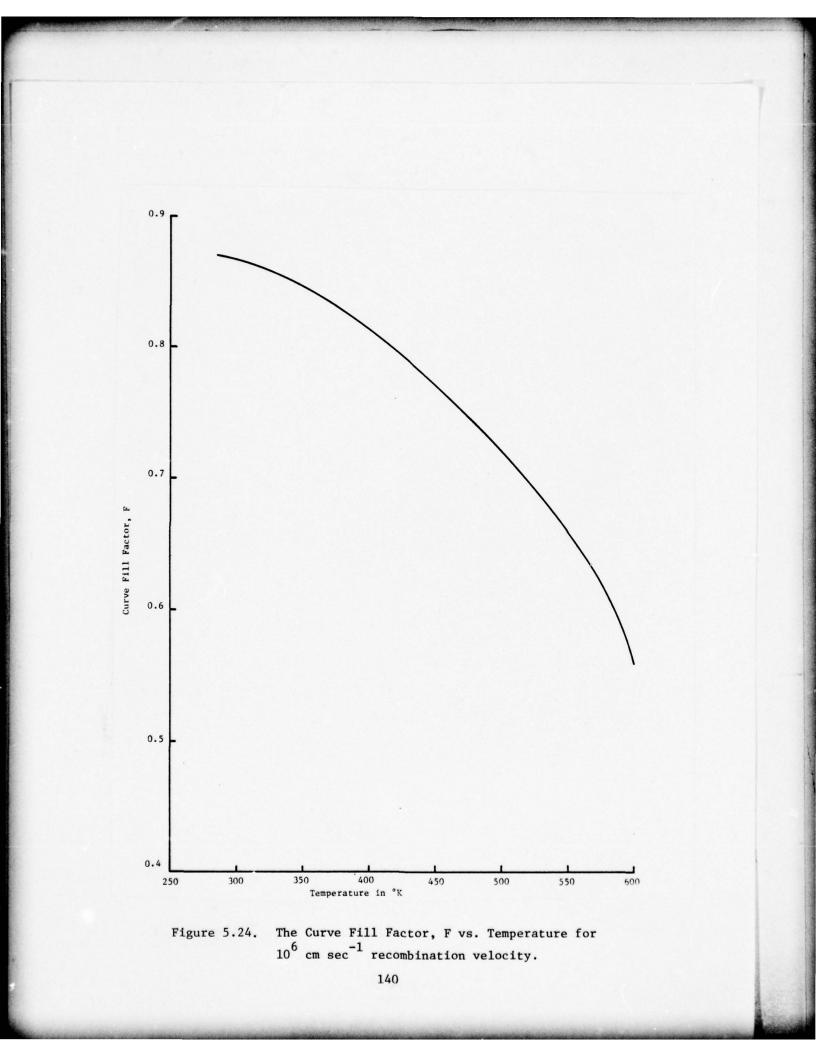


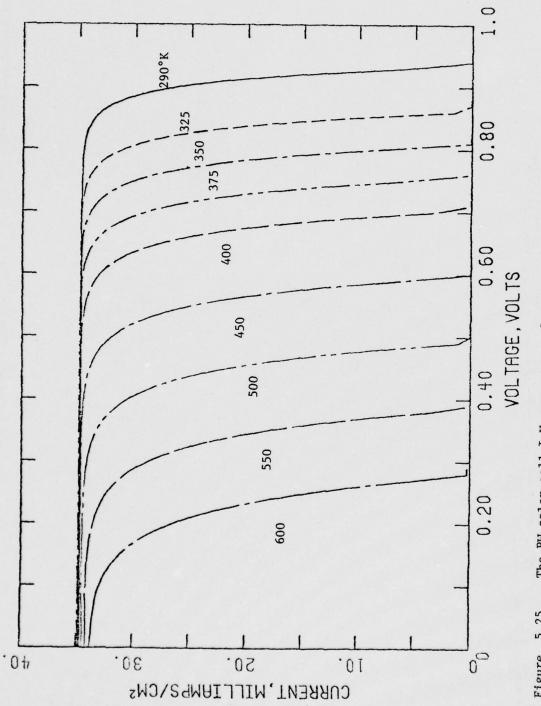


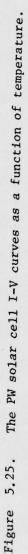


Finally, we have calculated the curve fill factor as a function of temperature for 10^6 cm sec⁻¹ recombination velocity and as shown in Figure (5.24). These calculations show that F changes from 0.87 at 290°K to 0.56 at 600°K, a 36% decrease which further reduces conversion efficiency.

Figure (5.25) illustrates PW solar cell I-V curves with temperature as a parameter. These calculations show that the combination of decreased V_{max} and F results in a decrease in conversion efficiency.







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6.0 MONOLITHIC, CASCADE SOLAR CELL

6.1 Introduction

The maximum theoretical energy conversion efficiency which may be obtained from a single junction photovoltaic solar cell is determined by the semiconductor bandgap. The bandgap determines the lower photon energy limit of the solar spectrum flux which may produce electron-hole pairs and, as a consequence, the maximum photon flux which may affect energy conversion. The maximum theoretical efficiency calculated from the bandgap model assumes that each solar photon possessing an energy equal to or greater than the bandgap energy produces an electron-hole pair and therefore contributes to energy conversion. This calculated efficiency is independent of material parameters because they do not enter the calculation of this simple model. The bandgap model assumes unity collection efficiency; i.e., that all electron-hole pairs produced are separated and collected by the p-n junction. Thus, the model assumes that all the photons having an energy greater than the bandgap are absorbed in a layer thickness, surrounding the p-n junction, smaller than either the electron and hole diffusion lengths. However, when a more detailed model is employed which includes the cell structure parameters with a specific semiconductor and its material parameters, the calculated collection and conversion efficiencies are usually lower than the maximum theoretical values. The material parameters which may affect efficiency values are: lifetime, minority carrier mobility, direct/indirect optical transition characteristics, and junction transport mechanisms.

By its very simplicity, the bandgap model is not encumbered by the details of device structure and material parameters. While the calculated

efficiency gives a higher value than can be attained in a practical case, from an overall point of view, the bandgap model does consider the more fundamental loss factors. It is, therefore, convenient to use the model as a crutch in order to explore new and fundamental methods to increase efficiency beyond the values attainable with single p-n junction solar cells.

There are three major losses incorporated in the bandgap model: dark current - forward bias current or dark current which subtracts from the photocurrent; excess photon energy - the energy difference between the individual photon energy and the bandgap energy of the material; long wavelength - that portion of the solar flux whose photon energy is lower than the bandgap and is not capable of producing electron-hole pairs. The dark current loss is largely dependent on technology and a lower limit exists due to the Shockley ideal forward current diffusion transport mechanism and to any associated carrier confinement. The excess photon energy loss cannot be reduced in conventional single junction cells. The long wavelength loss may be reduced, provided the long wavelength portion of the spectrum may be made to produce electron-hole pairs and take part in the energy process. We conclude that to obtain higher efficiency from photovoltaic devices, a cell structure is required which incorporates two or more p-n junctions in a monolithic, cascade arrangement. The structure consists of the widest bandgap junction at the surface with progressively smaller bandgap junctions into the material away from the surface. In this way, progressively larger and larger portions of the solar spectrum may be made to take part in an energy conversion process. Consequently, efficiency is increased substantially beyond the maximum theoretical value predicted by the bandgap model for a single p-n junction solar cell.

In properly designed cascade structures, the material for the first cell possesses the largest bandgap and the materials for succeeding cells deeper into the structure have progressively smaller bandgaps. Photons of energy equal to or greater than the first cell's bandgap energy are absorbed mostly in the first cell, while the free carrier absorption for photons of lower energy is small and this photon flux passes almost unattenuated onto the second cell. Photons of energy equal to or greater than the second cell's bandgap energy but less than the first cell's bandgap are absorbed mostly in the second cell, while the free carrier absorption for photons of lower energy is small and this photon flux passes almost unattenuated on to the third cell. This is repeated for as many cells as are in the structure. In this manner, the cascade structure presents a greatly improved spectral match to the solar spectrum.

Efficiency calculations using the simple bandgap model have been made for cascade cell structures. One result gives 31% efficiency at AM2 for a two terminal, two junction structure in which the top cell bandgap is 1.65 eV and the other is approximately 1.2 eV [6-1]. Calculations by other workers have reported similar results.

By the very nature of the bandgap model, structure design and material parameters are not provided. Moreover, the conventional closed form analytical method as well as the computer modeling technique involve approximations which do not give significantly improved design information for cascade cells, with respect to structure design and material parameters. In addition, development of improved efficiency calculations for practical use requires an analytical method from which the V-I curve equation is obtained. Therefore, it seemed appropriate to develop an analytical

method which derives the V-I solar cell curve which can be applied to the cascade structure in the case of a two-terminal device and the V-I curves of each cell in the cascade structure of a three-terminal device.

Section 4.0 outlines an improved analytical method to calculate solar cell device characteristics. This is particularly useful for cascade structures where design optimization studies of structure design and material parameters are to be made. This analysis obtains a solution for minority carrier concentration for the steady-state integraldifferential continuity equation in each distinct region of the structure. Once the minority carrier solutions satisfy the imposed boundary conditions in each distinct layer, all solar cell phenomena may be recovered, consistent with the approximations used (APPENDIX D).

There are two generic types of cascade structures with respect to construction. The first is where two separately fabricated cells are mechanically attached one behind the other in a stacked manner. The second is where the cells are fabricated monolithically by sequentially fabricating on a substrate the bottom p-n junction followed by the top p-n junction. Obviously the monolithic construction may be most conveniently fabricated by a sequential epitaxial growth process, ideally by the LPE process. In each of these types, the p-n junctions may be connected so that the voltages aid or oppose each other. The most convenient way to operate the former is as a two-terminal device which requires that the same terminal current flows through each p-n junction. However, it may also be operated as a three-terminal device in which each cell delivers power to its own load. The latter configuration, in which the voltages oppose each other, is a three-terminal device (See APPENDIX H).

The optimized two-terminal voltage aiding cell may exhibit a lower efficiency than the three-terminal voltage opposing cell. This results because of the imposition on the former that the same terminal current flows through each junction. For most applications the two-terminal cell may be preferred and, in addition, it will be simpler to fabricate. The three-terminal cell is more difficult to fabricate because of the placement of the common contact between the two cells. Moreover, power conditioning of voltage opposing cells will be less efficient since additional cells must be stacked in parallel (rather than series) and the resultant low voltages converted externally to useable levels (See APPENDIX J). The two-terminal, voltage aiding solar cell structure appears to have a number of compelling advantages over the three-terminal, voltage opposing structure.

Since the efficiency of such stacked layers is less than doubled when comparing conventional single junction cells to a two-junction cascade cell, the cascade cell will only be economical when the cost of the second cell is small. It may be possible to construct the monolithic, twojunction cascade junction solar cell with a small incremental cost over single junction, homojunction and heterojunction cells. This results because multi-layered III-V devices are fabricated by means of the multiple well LPE technique and all layer thicknesses are of the order of 1 µm.

Over the last 25 years, little has been done to fabricate cascade solar cells. A two-terminal GaAs/Si cascade solar cell was fabricated in 1961 [M. F. Lamorte, unpublished]. The GaAs cell was mechanically thinned to 25 µm and attached with epoxy to the Si cell surface. The

combined efficiency of the cell was lower than the efficiency of either cell operated separately. The poor results were shown to be due to free carrier absorption in the spectral range 1.1 to 1.4 μ m and to reflection losses at the GaAs/epoxy and to the epoxy/Si interfaces. Recently, a stacked junction Si solar cell composed of eight layers was reported [6-2]. This yielded an efficiency of 13.5% at a concentration of 20 suns, which is not overly impressive. Moreover, apart from the efficiency calculations made using the bandgap model, cascade cell design optimization studies have not been conducted. In Section 6.0 the analytical method presented in Section 4.0 and expanded in APPENDIX G is applied to a two p-n junction monolithic, cascade solar cell.

6.2 <u>Two-junction Cascade Cell Structure - Voltage Aiding Configuration</u>

Figure 6.1 shows an idealized cascade cell structure which is to be optimized for maximum efficiency. The cell contains three substructures: the top and bottom cells, and the tunnel junction separating the cells. The tunnel junction also serves as the electrical contact between the cells. There are a total of 10 distinct layers in this structure. Each cell is effectively a "Potential Well" (PW) cell. (For PW cell structure details see Section 5.2).

The optimum acceptor concentration of the "Window" layer is taken to be 10^{18} cm⁻³ as was determined from the PW cell optimization studies (Section 5.3). The bandgap values of the top cell (1.590 eV) and the bottom cell (1.030 eV) were determined from calculations based on the bandgap model.

The Al_xGa_{1-x} As "Window" bandgap is made to decrease linearly such that a constant negative built-in electric field is established. This

negative field accelerates electrons flowing toward the p-n junction, thereby reducing bulk recombination in this region. Surface recombination loss is also reduced due to the drift field which is present at the surface.

The "Window" layer also serves as an additional conducting path for the terminal load current. By highly doping this layer, the sheet resistance may be reduced to very low values. The high doping level and the correspondingly low minority carrier diffusion length in this region is not as critical to spectral response because of the presence of an aiding field.

6.3 Results and Discussion - Voltage Aiding Configuration

The analytical method used in Section 4.0 and APPENDIX G allows for a definitive design optimization, within the bounds of the approximations employed. As a result of the preliminary first and second iterative optimization studies, which are not presented here, a number of structural parameters were nearly optimized and are included in the band structure of Figure 6.1. They are: the impurity concentration in the p- and n-regions surrounding the homojunctions is taken at 10^{17} cm⁻³ for no other reason than to insure that depletion region space charge recombination is minimized; the sum of the p- and n-region thickness surrounding each homojunction^{*} was selected at the minimum thickness for which the normalized spectral response^{**} exceeded 98%, so that incomplete absorption loss is not a major factor; the p- and n-region thickness should be nearly equal; in graded regions an assumed alloy composition gradient

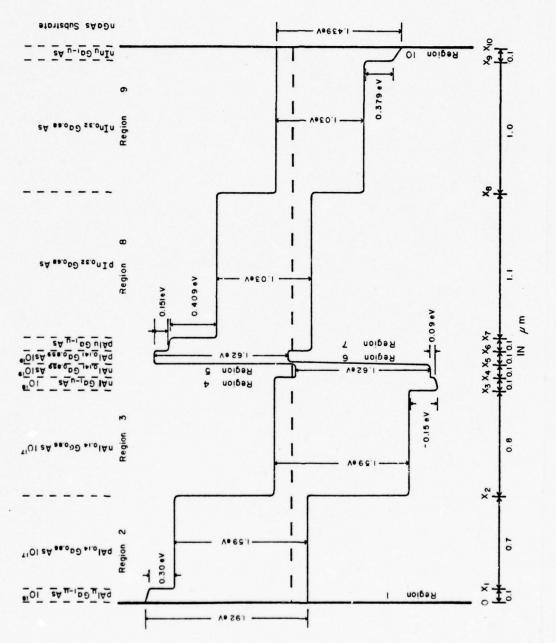
A p-n junction residing in a material of uniform alloy composition and uniform bandgap.

The contribution to short circuit arising in a layer produced from the absorbed flux in that layer.

is imposed to establish a constant 3,000 V cm⁻¹ field strength at 290°K which accelerates minority carriers toward the nearest homojunction cell; the barrier height in the minority carrier band edge is always equal to or greater than 4 kT to 5 kT volts for the purpose of achieving effective carrier confinement to reduce dark current; the top cell bandgap value was taken at the value, 1.590 eV, which on average, appears to give maximum efficiency for a conventional single junction cell; the p- and n-region thickness values were selected and shown in Figure 6.1.

The general optimization procedure found to be most suitable in a multiple layer device is to begin the optimization in the bottom cell followed by that of the top cell. The tunnel junction is made to be optically inactive because its bandgap value is greater than the value of the top cell. In the work described below, the study begins by optimizing the bottom cell bandgap. Having established the optimum bandgap for the bottom cell, this value is then imposed in all subsequent calculations. This is then followed by optimizing the n- and p-layer thickness of the bottom cell and these two parameters are imposed in all subsequent calculations. Finally, the n- and p-layer thicknesses of the top cell are optimized. The temperature characteristics of the cascade structure is then determined.

The optimization study presented here by no means exhausts the optimization. There remains to optimize the bandgap of the top cell, impurity concentration of the optically active and inactive portions of the structure, and the layer thickness of the inactive regions as well as of the "window" layer.





The design optimization study discussed below is a third iterative calculation. The first and second iterations are not presented here since the third calculation exhibits all the features of interest to a design engineer. The design optimization sequence to be described is as follows:

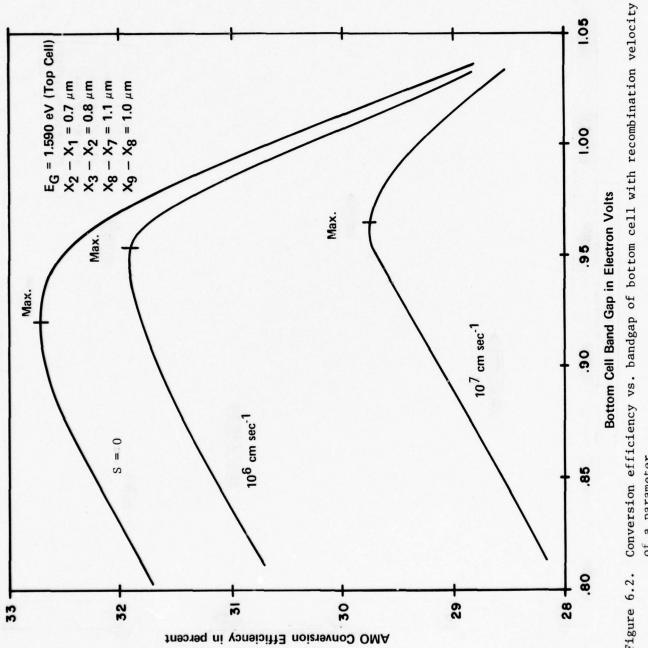
- 1. bottom cell bandgap,
- 2. ratio of the n- to p-region thickness of the bottom cell,
- sum of the p-region plus the n-region thickness of the bottom cell,
- 4. ratio of the n- to p-region thickness of the top cell,
- 5. sum of the p-region plus the n-region thickness of the top cell.

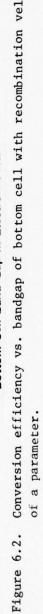
The optimization is conducted on the basis that the sum of the efficiencies of the top and bottom cells is maximized.

6.3.1 Bottom Cell

To calculate the bottom bandgap value to maximize the cascade efficiency, four bandgap values of the ternary $In \ Ga_{1-x}$ As were used. The bandgap values are: 1.030 (1.2 µm), 0.954 (1.3 µm), 0.886 (1.4 µm) and 0.827 (1.5 µm) eV.

Figure 6.2 shows the results of computer calculations of the AMO total efficiency to determine the bottom cell optimum bandgap. The calculations were performed using 0, 10^6 and 10^7 cm sec⁻¹ surface recombination velocity (SRV) at the window-air interface. The total efficiency was calculated by obtaining the V-I curve at the terminals of the cascade structure of both cells operating as a unit. The tunnel diode voltage drop was taken to be 0.050 volts and this was subtracted from the V-I curve.





There are a number of interesting observations to be made from this set of curves. The first observation is that the total efficiency is markedly sensitive to the bottom cell bandgap. The initial bandgap, 1.030 eV, gives an efficiency less than 29% for all three SRV values. For example, the efficiency increases to nearly 32% for 10^6 cm sec⁻¹ and 0.954 eV. Similar increases are obtained for 0 and 10^7 cm sec⁻¹ SRV.

The second is that the rate of decrease of efficiency on the high energy side is approximately three times faster than on the low energy side. A 10% increase in the bandgap energy above the optimum bandgap value results in approximately a 10% decrease in total efficiency, while a 10% decrease in bandgap below the optimum results in less than a 3% drop in efficiency.

The third observation is that while the bottom cell junction is physically remote from the cell surface, the bottom cell optimum bandgap is sensitive to SRV. Table 6.1 lists the bottom cell optimum bandgap and the corresponding calculated efficiency for each of the SRV values used. The optimum bandgap increases with increasing SRV.

	maxima efficiency				
of the cascade structure in Figure 6.1.					
Optimum					
Band	Efficiency				
Gap					
0.920 eV	32.7%				
0.954	32.0				
0.965	29.9				
	Optimum Band Gap 0.920 eV 0.954				

Table 6.1. Optimum bandgap and the corresponding and

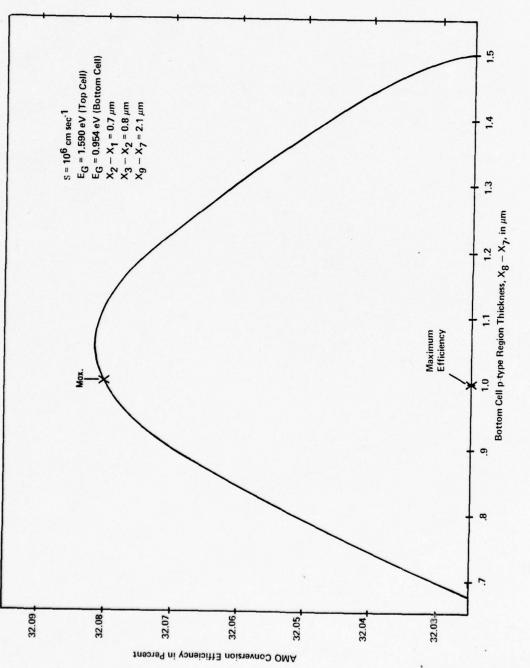
With increasing surface recombination velocity the terminal current and voltage at the maximum efficiency on the V-I curve of the top cell shift to lower values. Due to the imposition that the terminal current must be the net current passing through each cell, the current in the lower cell is shifted by the same amount. Therefore, the bandgap of the bottom cell may be increased to allow the terminal voltage of this cell to increase along its V-I curve to the point where the terminal current is equal to the current at the maximum power point on the V-I curve. This results in a higher photovoltage in the bottom cell.

The calculations show that even though the bottom cell is located away from the surface and from direct coupling phenomena, the design parameters of the bottom cell are very sensitive to the surface recombination velocity.

In Figure 6.2 the efficiency decreases at low bandgap values because the dark current in the bottom cell increases; at high bandgap, the efficiency decreases because the terminal current of the bottom cell decreases.

From Figure 6.2 we observe that the optimum bandgap for 10^6 cm sec⁻¹ recombination velocity is 0.954 eV. Therefore, in the further optimization studies we impose these two parameters on the band structures in Figure 6.2 for all further calculations. The 0.954 eV results in the alloy In_{0.388}Ga_{0.612}As.

The efficiency, short circuit current, and dark current are calculated and plotted in Figures 6.3, 6.4, and 6.5, respectively, for six thickness values of the bottom cell p-region. The thickness of the p-region plus





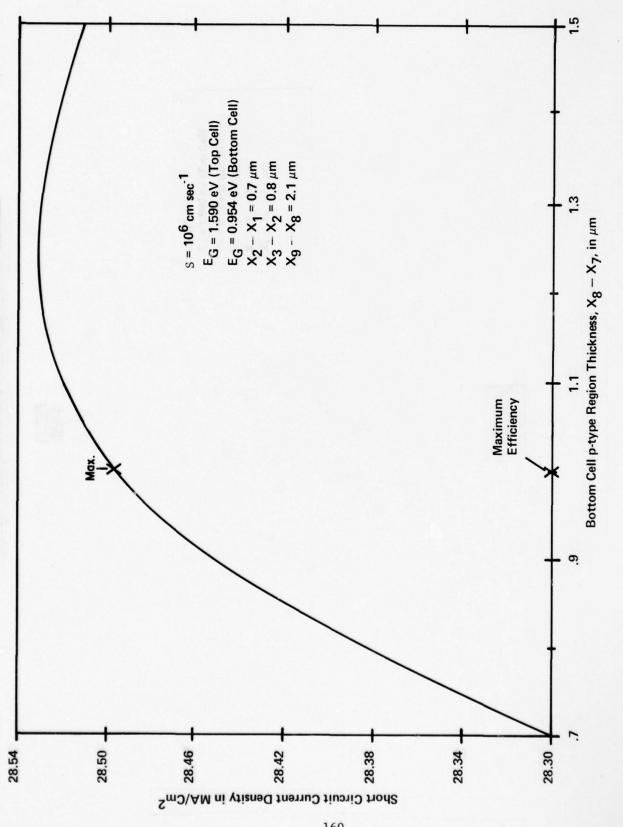
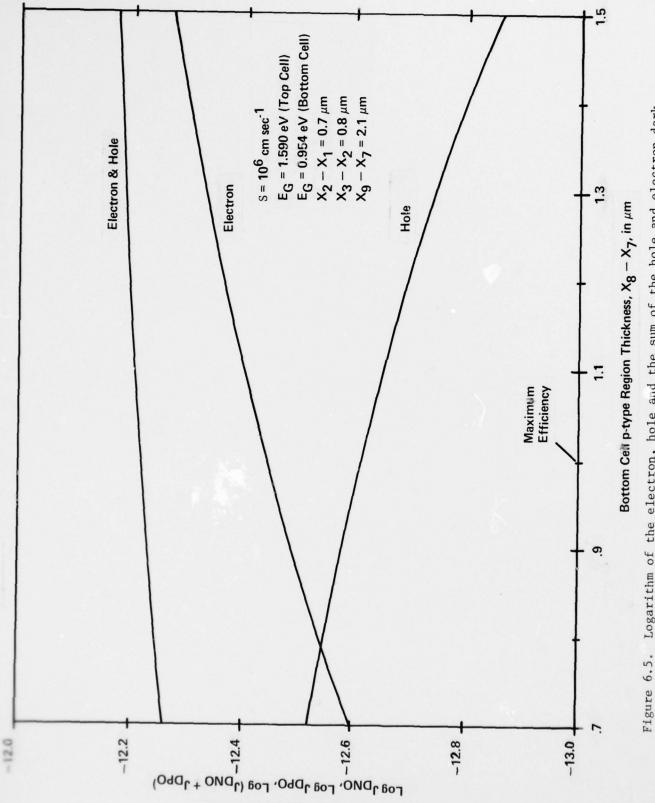


Figure 6.4. Short circuit current density vs. bottom p-type thickness.



Logarithm of the electron, hole and the sum of the hole and electron dark current vs. bottom p-type thickness.

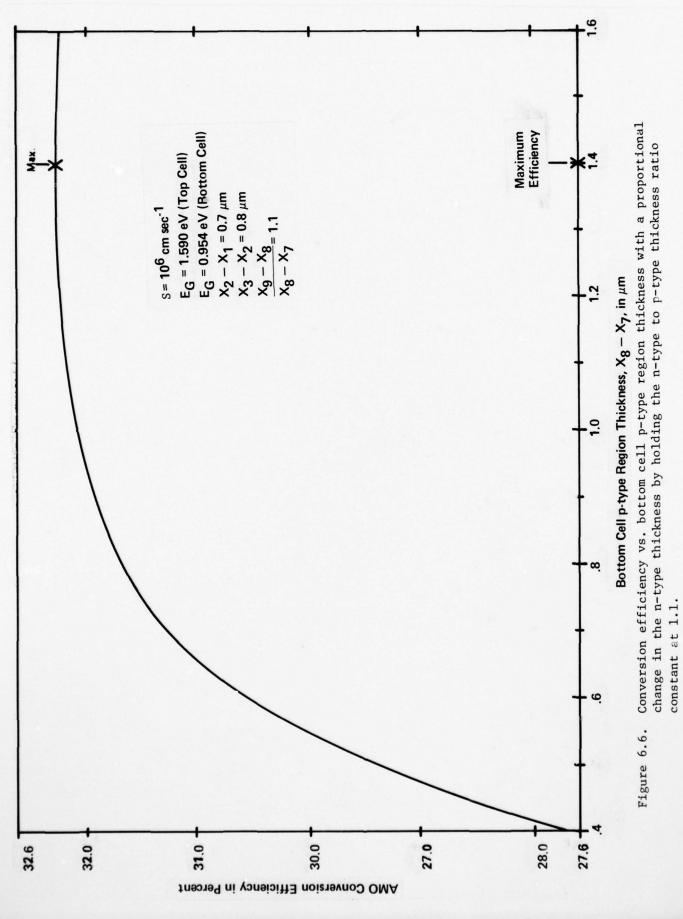
the n-region is maintained constant at 2.1 μ m. From previous studies we are assured that this results in a small incomplete absorption loss in the bottom cell. The cascade efficiency peaks at 32.08% for the pregion thickness range 1.0 μ m.

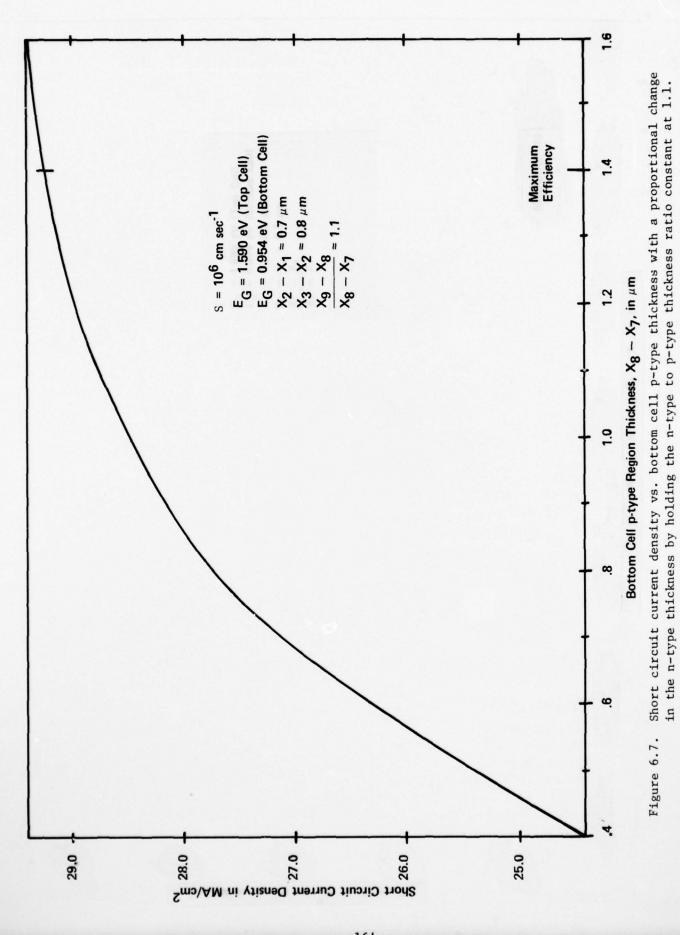
In Figure 6.4 the maximum short circuit current occurs in the region of 1.3 μ m where the efficiency has decreased to 32.06% from its maximum of 32.08% at 1.0 μ m. It is seen that the maximum efficiency does not occur at the maximum short circuit current, as is sometimes assumed.

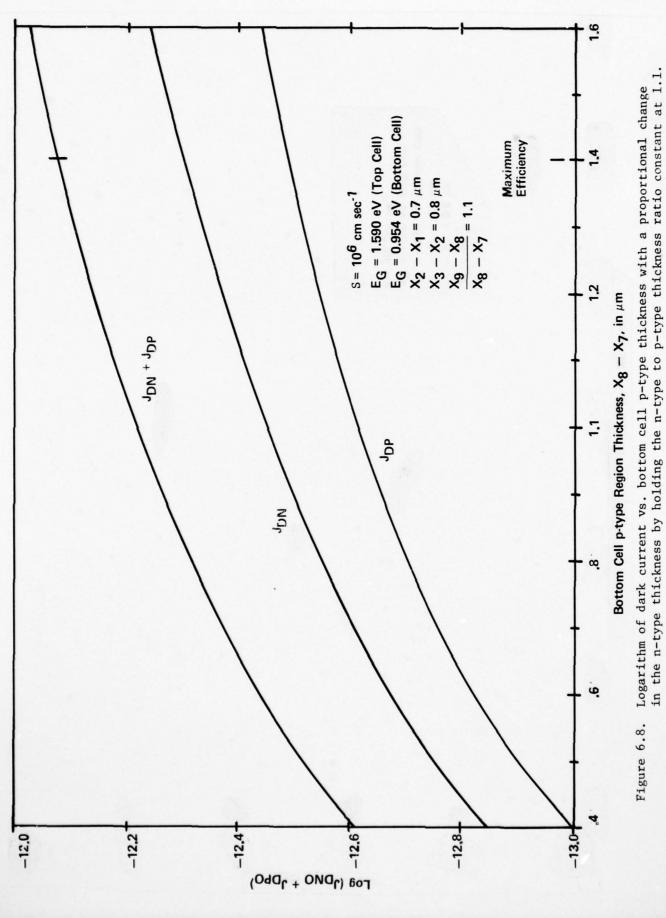
The total dark current and its components are shown in Figure 6.5. Due to the completeness of the model analyzed, the influence of carrier confinement on dark current is also manifested in Figure 6.5. With increasing p-region thickness, electron carrier charge confinement is reduced, thereby, increasing the electron contribution to dark current. Contrarywise, the n-region thickness decreases with increasing p-region thickness resulting in an increase in hole carrier charge confinment in the n-region, thereby, reducing the hole contribution to dark current. As seen in Figure 6.5, the total dark current increases only slightly with increasing p-region thickness attesting to the compensating electron and hole contributions to dark current.

We now add to the band structure in Figure 6.1 that the ratio of the n- to the p-region thickness is to be maintained at 1.1 in all further design optimization calculations.

In a similar way, the efficiency, short circuit current and the dark current are calculated and plotted in Figure 6.6, 6.7, and 6.8, respectively, for six values of p-region thickness. But, in this calculation the n-region







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thickness is changed proportionally with respect to the p-region thickness, thereby, maintaining a ratio for the n- to p-region thickness at 1.1. In Figure 6.6 maximum efficiency occurs at a value of 1.40 μ m for x₈-x₇. This results in the optimum n-region thickness, x₉-x₈ = 1.54 μ m.

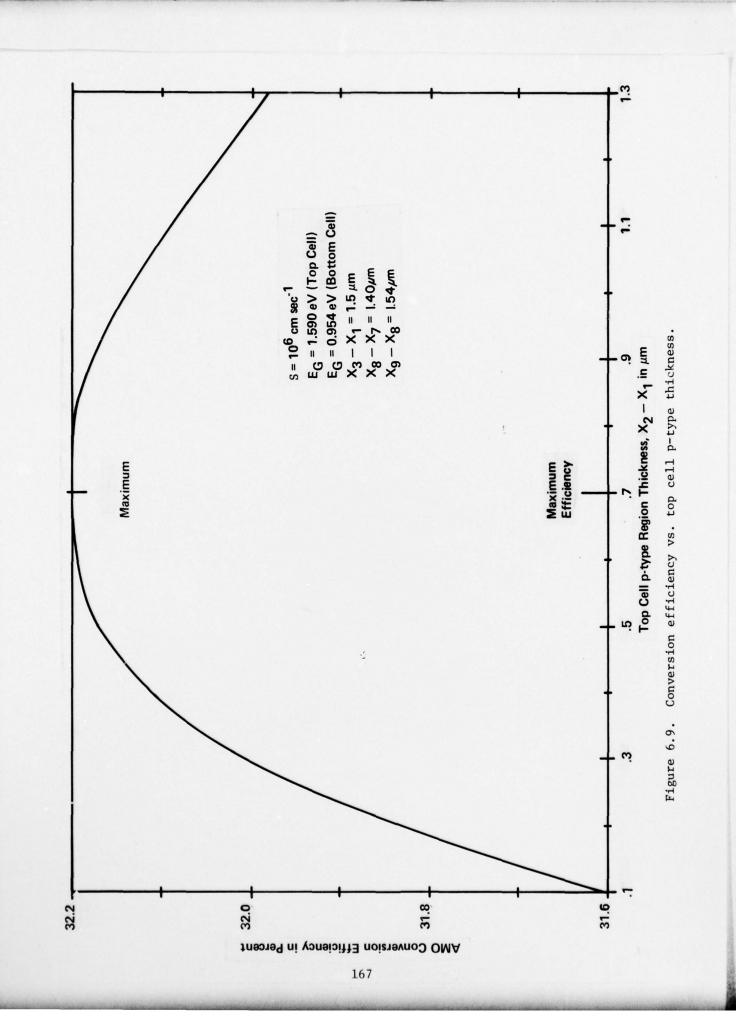
Again we observe that the short circuit current and dark current continue to increase beyond 1.40 μ m, the value of the p-region thickness for maximum efficiency. Below the 1.40 μ m thickness, terminal current increases more rapidly than the terminal voltage decreases resulting in efficiency increasing at a greater rate than the terminal current increases; therefore, the efficiency shows a decreasing trend.

Having determined the optimum p- and n-region thickness of the $In_{0.388}Ga_{0.612}As$ homojunction, these values for $x_8-x_7 = 1.40 \ \mu m$ and $x_9-x_8 = 1.54 \ \mu m$ are now imposed on the band structure in Figure 6.1 for all subsequent calculations.

6.3.2 Top Cell

We now turn our attention to the ternary $A1_{0.14}^{Ga}_{0.86}^{As}$ homojunction which makes up the top solar cell. The optimization details are identical to those which are presented for the lower junction.

Figures 6.9, 6.10, and 6.11 show the efficiency, short circuit current and dark current for the $Al_{0.14}Ga_{0.86}As$ homojunction as a function of the p-region thickness, x_2-x_1 . The sum of the p- and n-region thickness is held constant at 1.5 µm in this calculations. Efficiency peaks at 32.21% for $x_2-x_1 = 0.7$ µm and $x_3-x_2 = 0.8$ µm. This results in the optimum ratio of 1.1 µm of n- to p-region thickness, which was also obtained for the In_{0.388} Ga_{0.612}As homojunction.



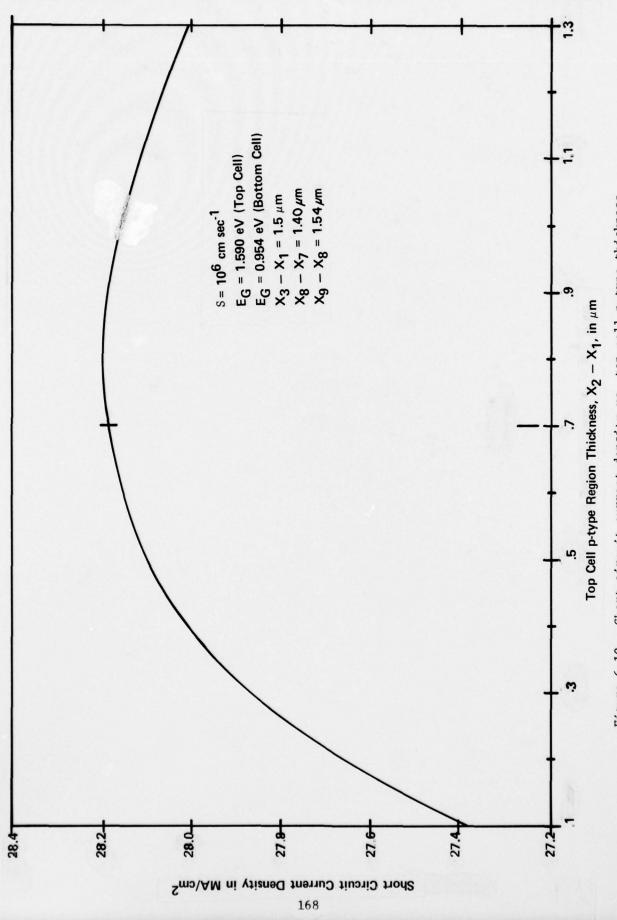
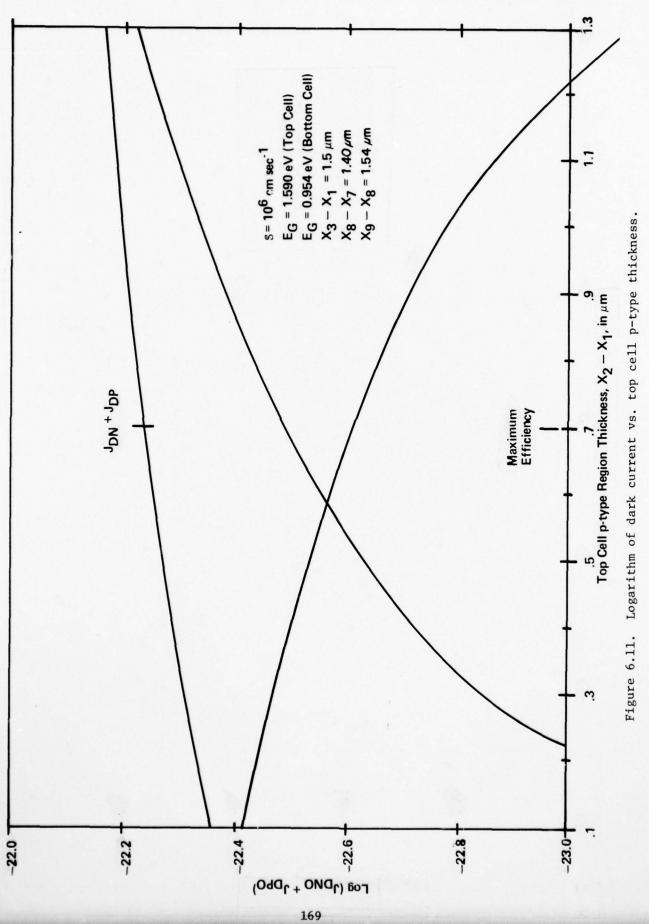


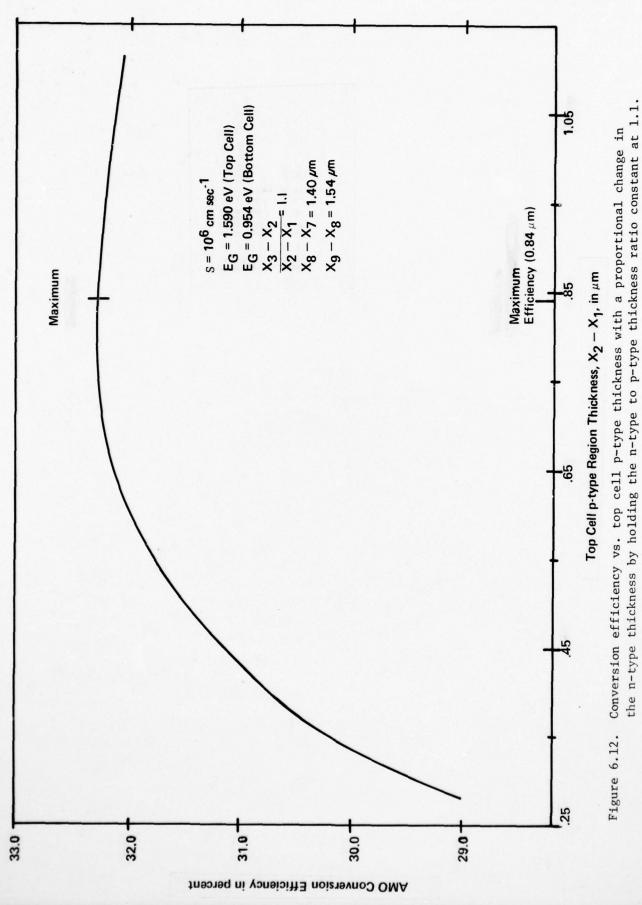
Figure 6.10. Short circuit current density vs. top cell p-type thickness.

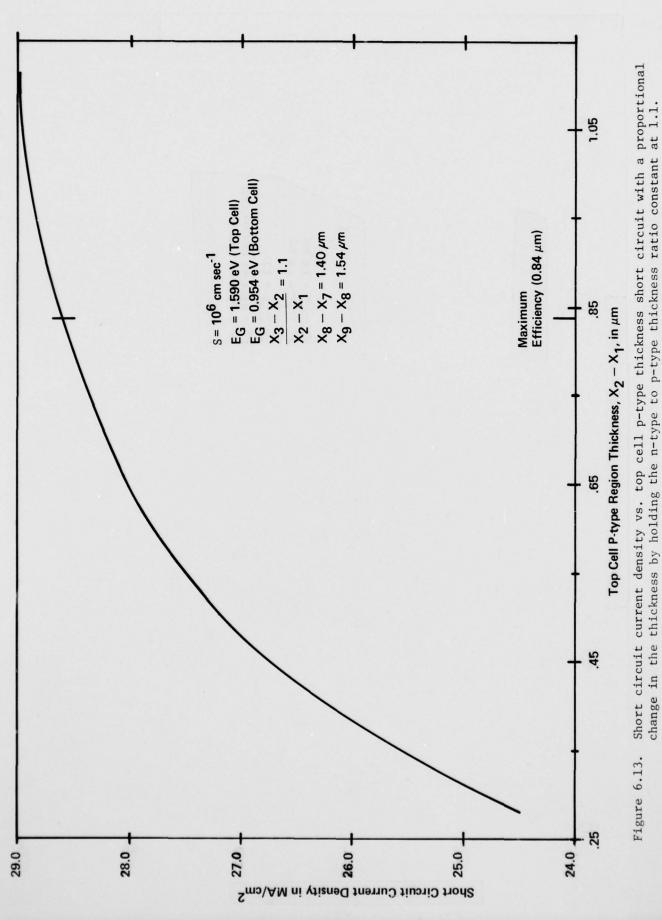


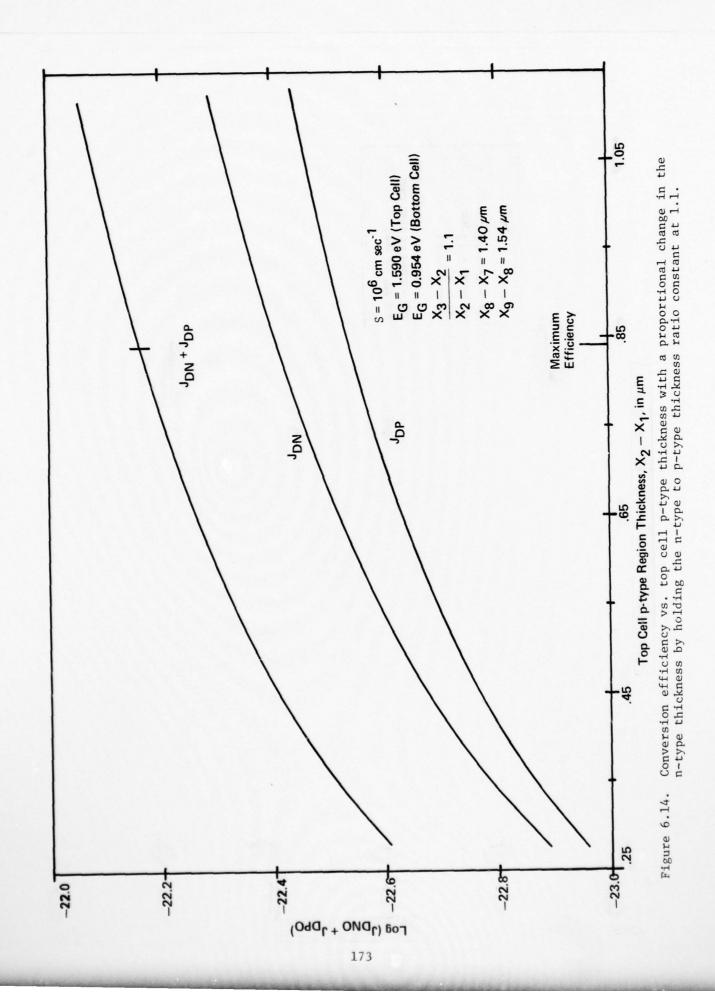
The short circuit current in Figure 6.10 is seen to peak at 0.8 µm, while the dark current in Figure 6.11 is seen to increase monotonically with increasing x_2-x_1 . The general shapes of these curves are strikingly similar to the corresponding curves represented in Figures 6.4 and 6.5 for short circuit current and dark current, respectively, for the $In_{0.388}Ga_{0.612}As$ homojunction. We now impose the additional design constrant on the band structure in Figure 6.1 that the ratio $(x_3-x_2)/(x_2-x_1)$ is to be held at 1.1.

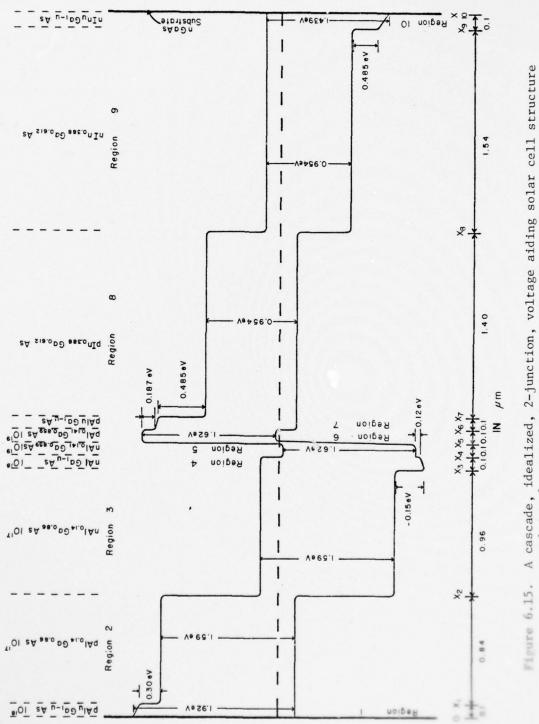
Efficiency is finally calculated for seven values of $x_2 - x_1$ maintaining the ratio of the n- to p-region thickness at 1.1. The curve drawn through the seven points is shown in Figure 6.12 where the efficiency peaks at 32.31% at $x_2 - x_1 = 0.84 \ \mu\text{m}$ and $x_3 - x_2 = 0.92 \ \mu\text{m}$. The short circuit current is shown in Figure 6.13 to increase and appears to have a broad maximum beyond 1.05 μm . The dark current is also shown to increase with increasing $x_2 - x_1$. All three curves show strikingly similar shapes with their corresponding curves in Figures 6.6, 6.7, and 6.8 for $\text{In}_{0.388}\text{Ga}_{0.612}\text{As}$ homojunction.

The last of the parameters to be imposed on the structure in Figure 6.1 are $x_2-x_1 = 0.84 \ \mu m$ and $x_3-x_2 = 0.92 \ \mu m$, giving a total thickness of 1.76 μm for the p- and n-regions of the ternary $Al_{0.14}Ga_{0.86}As$. The resultant cascade structure of the third iterative process is shown in Figure 6.15. The efficiency of the cascade structure represented in Figure 6.15 is 32.31%, while the efficiency represented by the structure in Figure 6.1 is 29%. This represents more than an 11% increase. A further optimization with respect to the bandgap of the top cell has not been completed.









resulting from the third iterative design optimization.

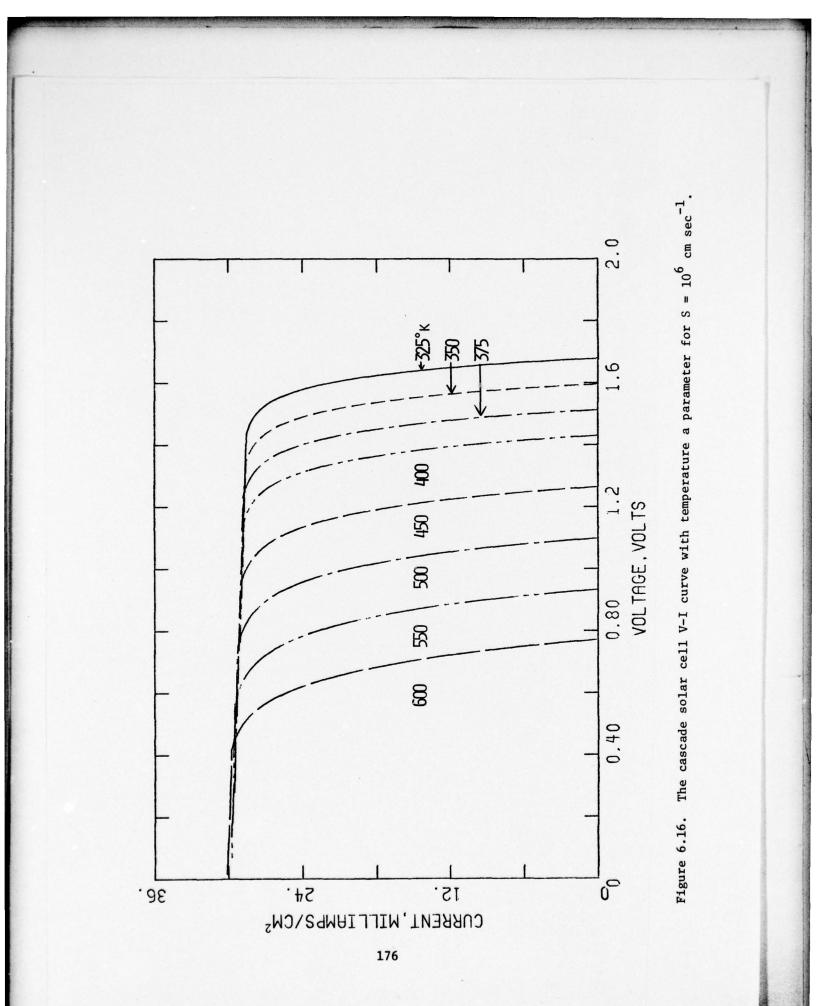
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6.3.3 Temperature Behavior

To fully characterize the cascade structure under study and to compare its performance to GaAs and Si cells, temperature characteristics must be obtained. Temperature studies were conducted on the "optimized" structure given in Figure 6.15. The calculation of temperature characteristics was done using the identical Fortran IV computer program as was used for the PW cell. This provides for an excellent basis on which to compare the temperature behavior of the PW cell and the cascade cell of Figure 6.15. The latter is essentially two PW cells in series. While calculations have been done for 0, 10^6 and 10^7 cm sec⁻¹ surface recombination velocity, in this discussion only the calculations for 10^6 cm sec⁻¹ will be presented.

Figure 6.16 shows the cascade V-I curves with temperature a parameter up to 600°K. Each point on the V-I curve represents the sum of the photovoltaic voltages (top and bottom cells) minus 0.050 volts due to the voltage drop across the tunnel junction, all for a given terminal current. This family of curves shows that the open circuit voltage at 325°K is nearly twice that of the PW GaAs homojunction cell and more than three times the value of Si cells. The short circuit current is approximately equal to that of the PW cell.

The V-I curves show that the voltage at the maximum power point and open circuit voltage decrease with increasing temperature, while the current is relatively independent of temperature. Thus, the cascade cell V-I characteristics behave like a single junction solar cell except that the magnitudes of the device parameters are different.



The computer program calculates the maximum power from the V-I curve for each temperature, determines the AMO efficiency and plots efficiency vs. temperature given in Figure 6.17. In addition, Figure 6.17 also shows a plot of the efficiency for the top and bottom cells also calculated by the program, from the V-I curves of the individual cells. The cascade cell efficiency exhibits a temperature coefficient of 0.0733%/°C or 0.099 mw/°C, which is approximately 50% higher than for the PW cell and nearly double the value of GaAs experimental values. The comparison between the PW and cascade temperature characteristics is made in Table 6.2. The most important temperature coefficient is that listed in the last column - the normalized power output temperature coefficient. It shows that the PW cell and cascade cells are approximately equivalent with the cascade having a slight edge. On a similar basis it can be shown that the normalized power temperature coefficient is lower for the top cell and higher for the bottom cell compared to the cascade as a unit. This arises because the photovoltage of the top cell is less sensitive to temperature than that of the bottom cell due to the larger bandgap of the top cell.

Figure 6.18 shows the total spectral response of the cascade solar cell with temperature as a parameter. The total spectral response is the sum of the spectral responses of electrons and holes of both the top and bottom cells. The short wavelength response decreases with increasing temperature because surface recombination loss increases at the window-atmosphere interface. At the long wavelength edge the response increases with increasing temperature because of bandgap shrinkage.

The component parts of the spectral response curves of Figure 6.18 may also be plotted as shown in Figure 6.19. These curves show that the

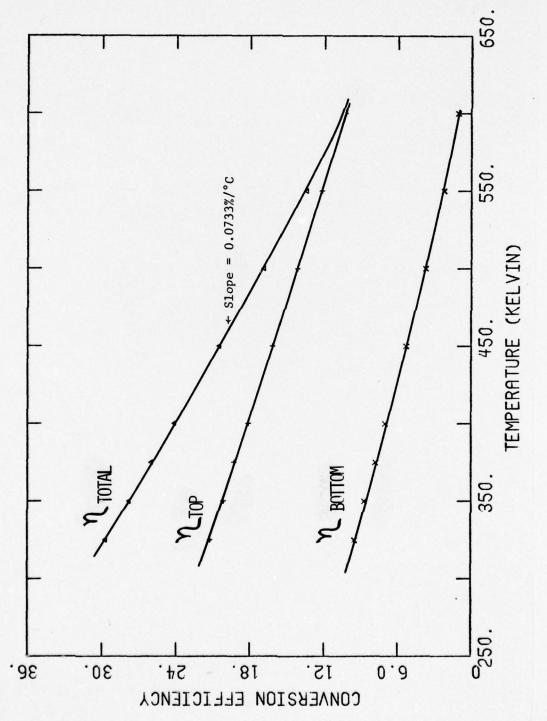
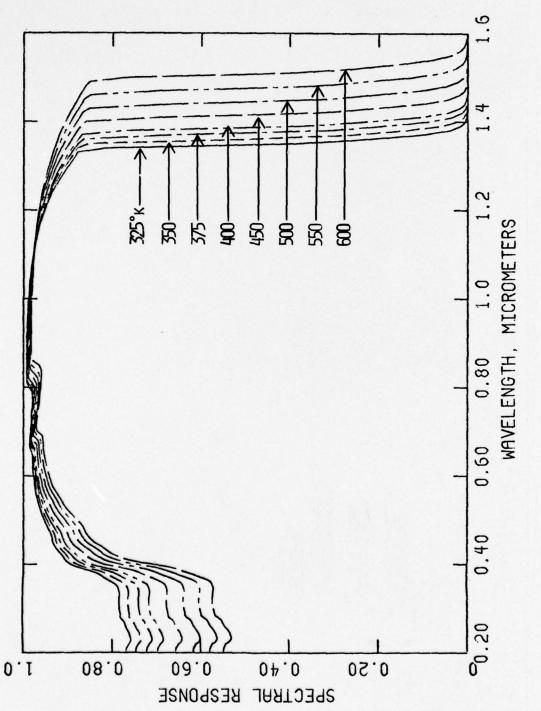


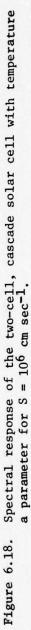


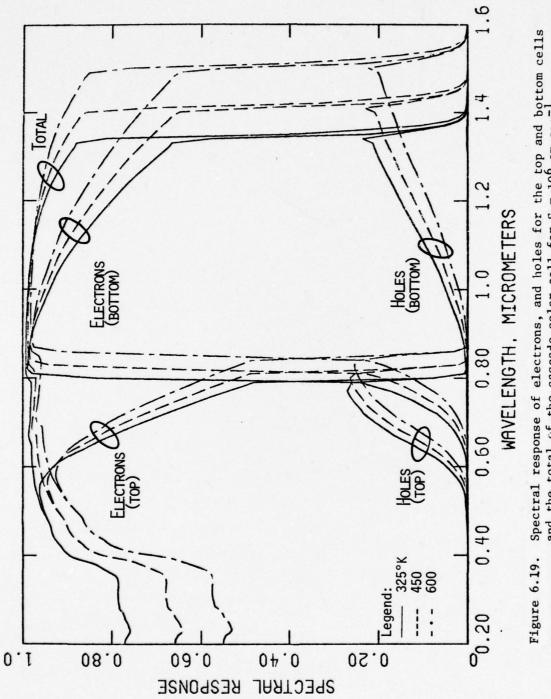
Table 6.2. Comparison of PW and Cascade cell temperature characteristics at AMO and 10^6 cm eac⁻¹ SRV.

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and	TO CII S	and IU' cm sec - akv.			
	F	Ч Ц	dn/ _{dT}	dP _{m/dT}	d(Pm/Po)/dT
Potential Well	21.5%	21.5% 29.1 mw/cm ²	0.0544%/°C	0.074 mw/°C	0.0025/°C
Cascade	32.0 43.3	43.3	0.0733	0.099	0.0023









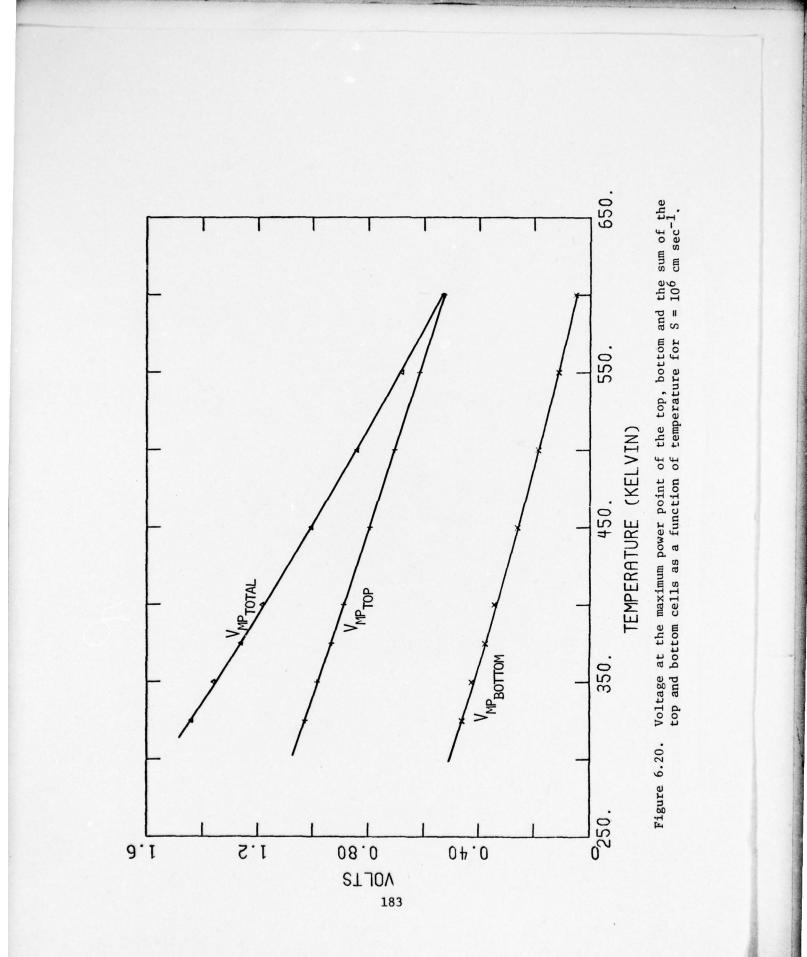
electron response is substantially higher in both cells. This arises because the incident flux falls first on the p-region and then on the n-region for both top and bottom cells. Therefore, the total photon flux absorbed by each p-region of the homojunctions is substantially greater than in the corresponding n-regions.

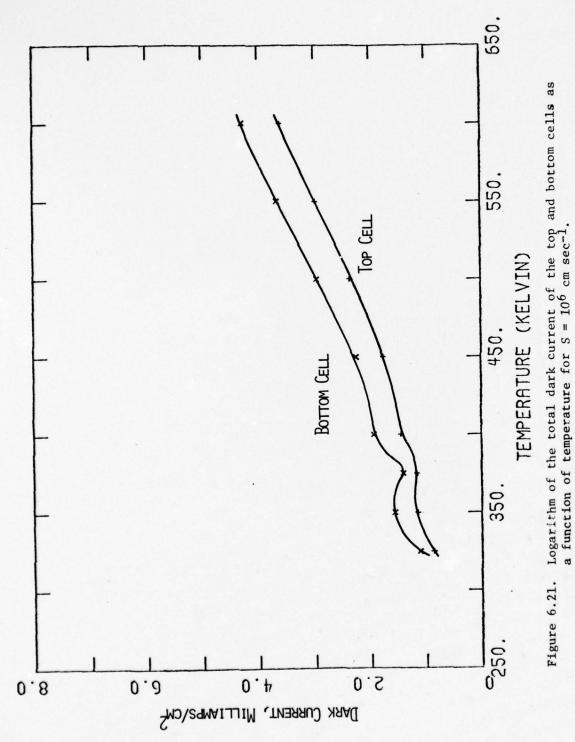
Figure 6.20 shows the temperature behavior of the photovoltage at the maximum power point of the cascade, top and bottom cells. The normalized temperature coefficient of the top cell is smaller than either the cascade and bottom cells. This arises because the bandgap of the top cell is larger than the bottom cell.

The dark current increases with increasing temperature for both the top and bottom cells as shown in Figure 6.21. These calculations show that for the optimized configuration of Figure 6.15 the magnitude and temperature behavior of the dark current for the two cells are nearly equal, even though the bandgap of the top cell is substantially larger than the bottom cell. If the structure in Figure 6.15 were further optimized, the dark currents of the two cells would show a smaller differential.

6.4 <u>Two-Junction Cascade Cell Structure - Voltage Opposing Configuration</u>

The photovoltages are of opposite polarity in the voltage opposing configuration. This cascade cell configuration should be operated as a three-terminal device. If operated as a two-termination device, with the middle contact floating, the cascade cell efficiency is less than either cell operated as a conventional single junction solar cell.

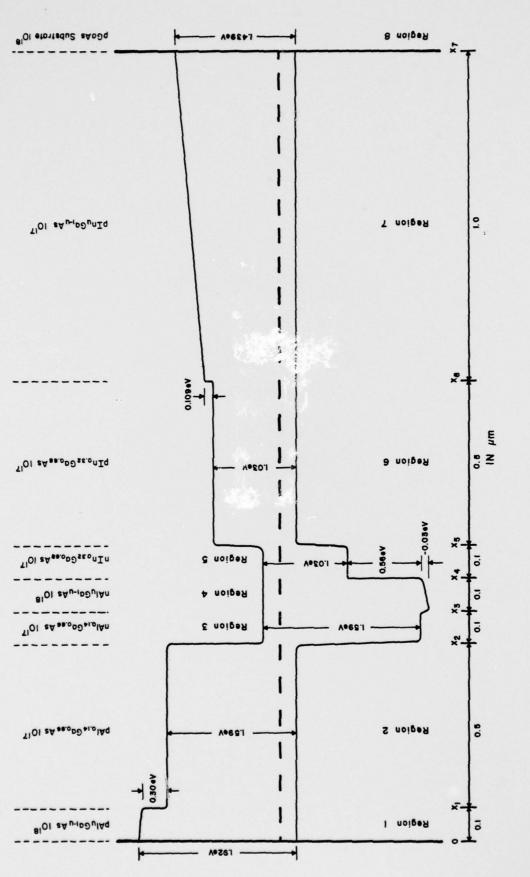




Neglecting contact problems for the center layer, the optimized cascade cell voltage opposing (CCVO) configuration will always exhibit an efficiency equal to or higher than the cascade cell voltage aiding (CCVA) configuration. This results because in the CCVA case equal photocurrents must flow through each cell and the voltage drop across the tunnel junction. Area lost in making contact to the center layer will reduce somewhat the advantage of the voltage opposing case.

The computer program written for the closed form analysis has been modularized so that it may be applied for single junction and up to n-junctions in a cascade solar cell. On each side of a junction, the program provides for up to three distinct layers. This allows for input structure and material parameters for each of three layers such as described in APPENDIX F for the PW cell and in APPENDIX G for cascade cells. Moreover, the modularization allows for the program to be applied to simple Si and III-V materials cells with or without the low-high junction (LHJ), to the PW cell and to cascade cells with voltage aiding or opposing.

Figure 6.22 shows the idealized CCVO structure which is to be optimized for maximum efficiency. It contains seven (7) distinct layers plus a GaAs substrate. The latter is optically and electronically inactive in a properly designed cascade structure. Regions 1, 2 and 3 serve the same functions as for the corresponding layers of the PW cell described in Section 5.0. Region 4 is graded to accelerate holes toward the bottom cell. Regions 5, 6 and 7 serve the same functions as described in Section 5.0 for the corresponding layers of the PW cell. The cell



A cascade, idealized, 2-junction, voltage opposing solar cell structure. Figure 6.22.

design provides for the built-in electric field intensity at 290°K to be 3000 volts per cm in Regions 1, 4 and 7. The field in Region 1 accelerates electrons toward Region 2, while the field in Region 4 accelerates holes toward Region 5 and the field in Region 7 accelerates electrons towards Region 6.

The design optimization represents a preliminary effort. The bandgap at the surface was chosen to be 1.92 eV, while the top and bottom homojunction chosen are 1.590 and 1.030 eV, respectively. These bandgap values selected were only educated guesses and do not represent optimized values. Similarly the layer thickness of Regions 1, 3, 4 and 5 were chosen to be 0.1 μ m. None of these thicknesses were optimized, but, only represent arbitrarily chosen values. Further optimization studies of thickness and bandgaps beyond that reported here will result in higher efficiency values. The bandgap of Region 4 was selected so that it is optically inactive. The materials of the top cell was chosen to be $Al_{0.14}Ga_{0.86}As$ and that of the bottom cell $In_{0.32}Ga_{0.68}As$ because of their high mobility values and reasonable lifetime values. Lattice misfit and the resultant recombination centers which may be introduced in this structure are not included in this model.

The design optimization described below is based on the band structure given in Figure 6.22 and the sequence is as follows:

- 1. Bottom cell p-layer thickness
- 2. Valence band edge discontinuity, ΔE_{v3} , at x_3
- 3. Top cell p-layer thickness

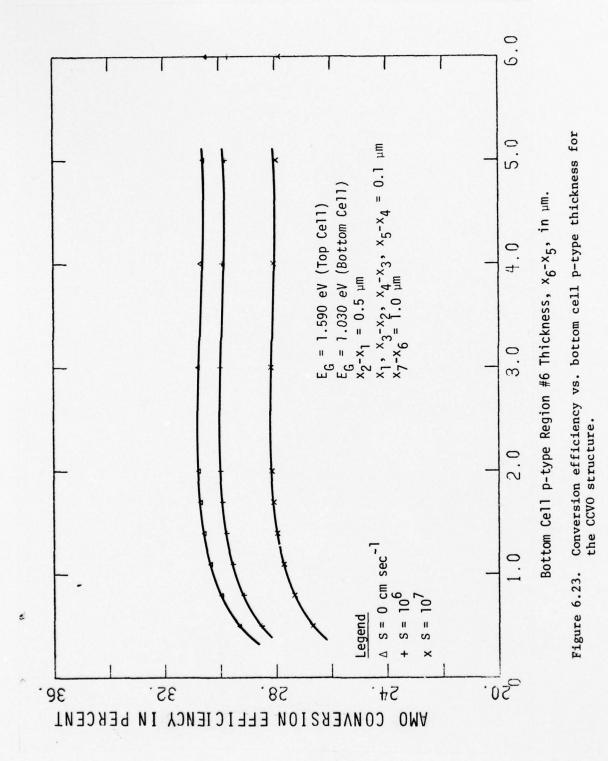
The cascade optimization is conducted on the basis that the sum of the efficiencies of the top and bottom cells is maximized.

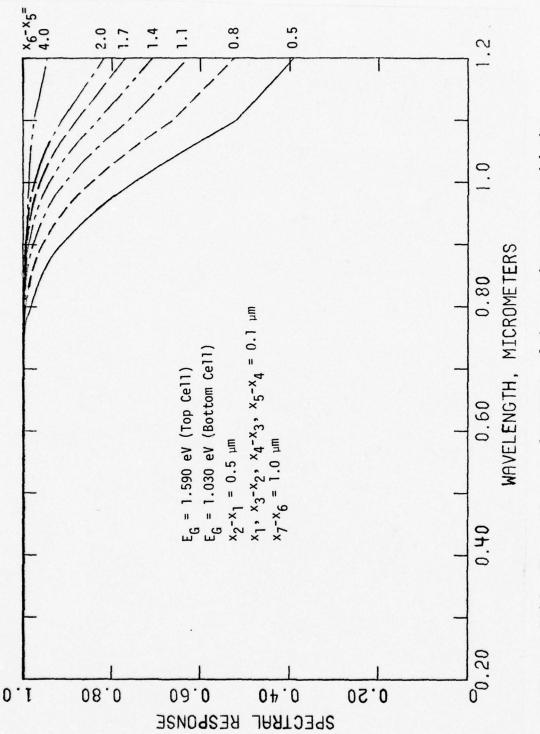
6.5 Results and Discussion - Voltage Opposing Configuration

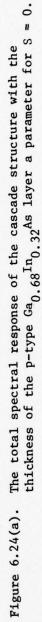
6.5.1 Bottom Cell

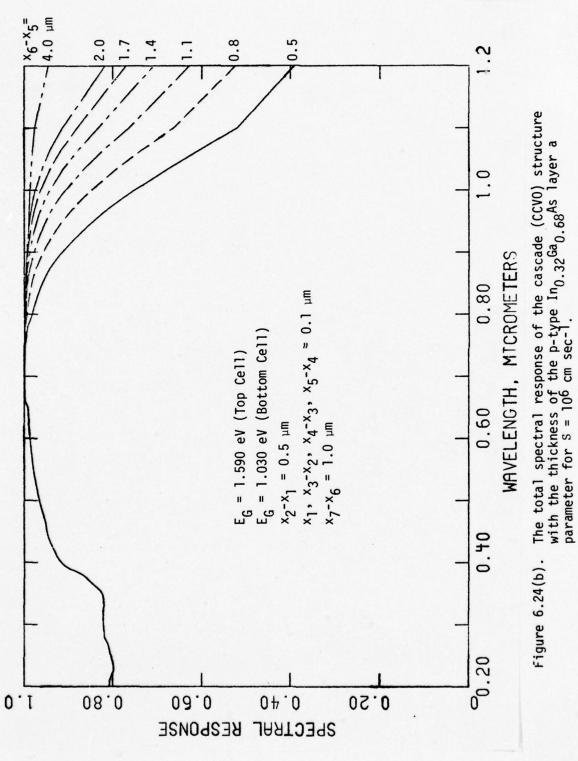
The optimization study commenced with the determination of the thickness of the p-type $In_{0.32}Ga_{0.68}As$ layer, x_6-x_5 . Figure 6.23 shows the results of the cascade cell (sum of efficiencies of the top plus the bottom cells) efficiency calculation as a function of x_6-x_5 . The surface recombination velocity (SRV) which is present at x = 0 is a parameter. The maximum efficiency occurs at approximately 2.0 µm for all three values of SRV. However, the efficiency is not a strong function of thickness over the range 1.5 to 4.0 µm. This arises because the diffusion length in $In_{0.32}Ga_{0.68}As$ is greater than 10 µm and the spectral response and dark current nearly compensate and there is little change in efficiency.

Figures 6.24(a), (b) and (c) show the total cascade spectral response for SRV values 0, 10^6 , 10^7 cm sec⁻¹. The response was calculated over the wavelength range 0.2 to 1.2 µm. Each spectral response curve represents the sum of the electrons and holes of both the top and bottom cells. The p-type In_{0.32}Ga_{0.68}As layer thickness is a parameter, using the following values: 0.5, 0.8, 1.1, 1.4, 1.7, 2.0 and 4.0 µm. The response increases in the spectral region $\lambda > 0.75$ µm with increasing $x_6^{-x_5}$ because of increased photon absorption at longer wavelengths. This behavior is almost independent of the SRV. Even though the p-type In_{0.32}Ga_{0.86}As layer thickness increases to 4.0 µm, the electron diffusion length in this region is greater than 10 µm and the bulk recombination increase is not a major factor. At the same time, however, carrier confinement in this region is monotonically









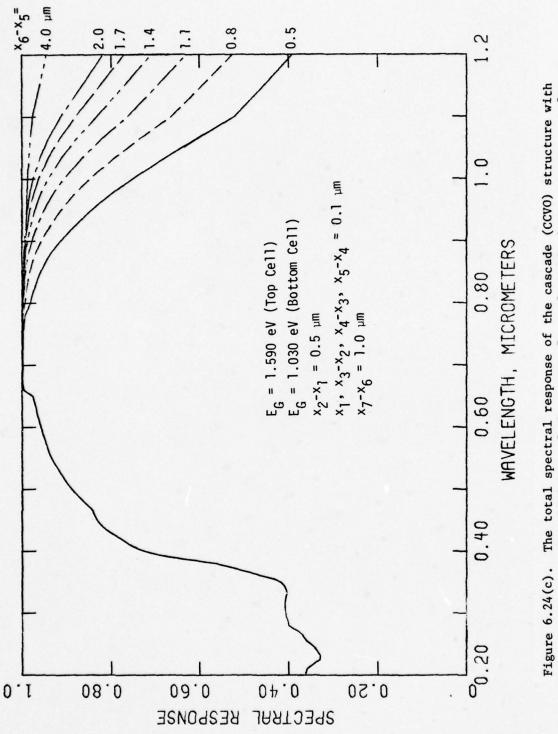


Figure 6.24(c). The total spectral response of the cascade (CCVO) structure with the thickness of the p-type $In_{0.32}Ga_{0.68}As$ layer a parameter for $S = 10^7 \text{ cm sec}^{-1}$.

decreasing with increasing x_6-x_5 resulting in an increase in the dark current. This is shown in Figure 6.25 where the reciprocal of the electron charge accumulation, R_{n6} , in Region 6 is shown to increase with increasing x_6-x_5 . Therefore, beyond $x_6-x_5 = 2.0$ µm the dark current begins to show a significant increase and to more than overcome the increase in spectral response. R_{n6} increases by nearly an order of magnitude when x_6-x_5 increases from 0.8 to 4.0 µm and results in the dark current increasing by the same factor. The electron dark current obtained is of the form

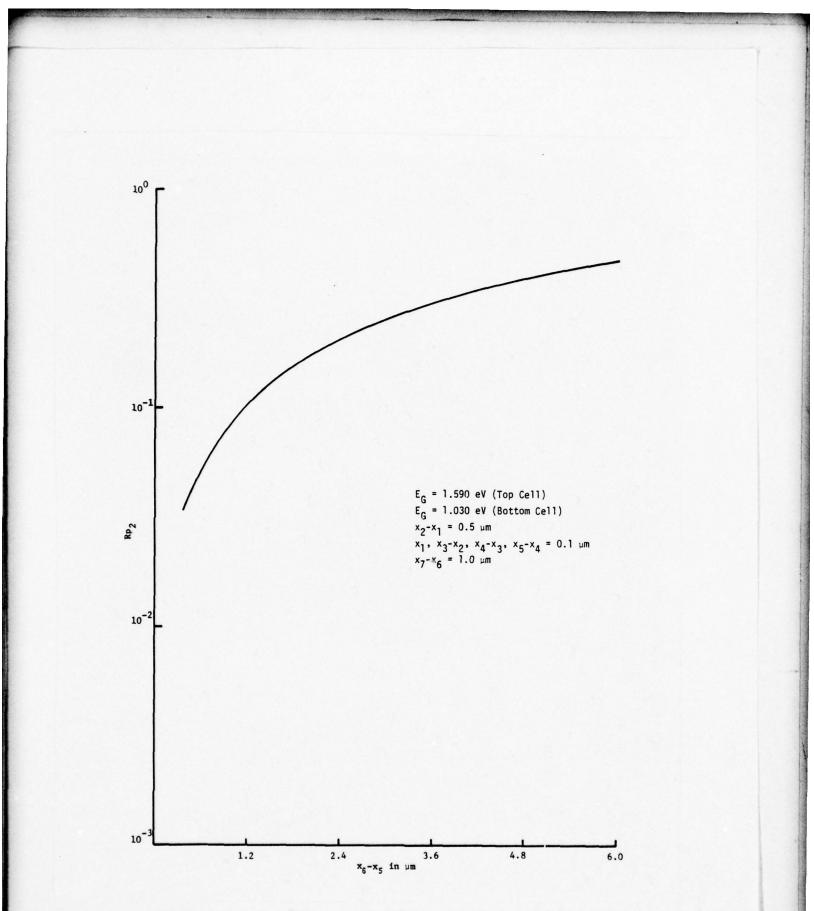
$$J_{Dn6} = q \frac{D_{n6}}{L_{n6}} n_{p60} \left(e^{qV_2/kT} - 1 \right) R_{n6}$$
(6-1)

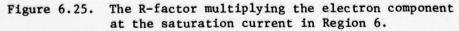
where V_2 is the photovoltage of the bottom cell, R_{n6} is given in closed form in Appendix G as a function of structure and material parameters as well as temperature and where q, D_{n6} , L_{n6} and n_{p60} have the usual meaning pertaining to Region 6.

For values of $x_6-x_5 < 2.0 \ \mu m$ the incomplete absorption loss more than compensates for the increased carrier confinement and increased collection efficiency which results in a decrease in spectral response and efficiency.

In Figures 6.24(a), (b) and (c) the spectral response decreases with increasing SRV in the range $\lambda < 0.65$ because of increase surface losses. In the spectral region 0.65 < $\lambda < 0.75$ the spectral response is not sensitive to SRV or to x_6-x_5 .

In all subsequent calculations in this study, the optimized value for $x_6-x_5 = 2.0 \ \mu m$ is imposed on the structure in Figure 6.22.



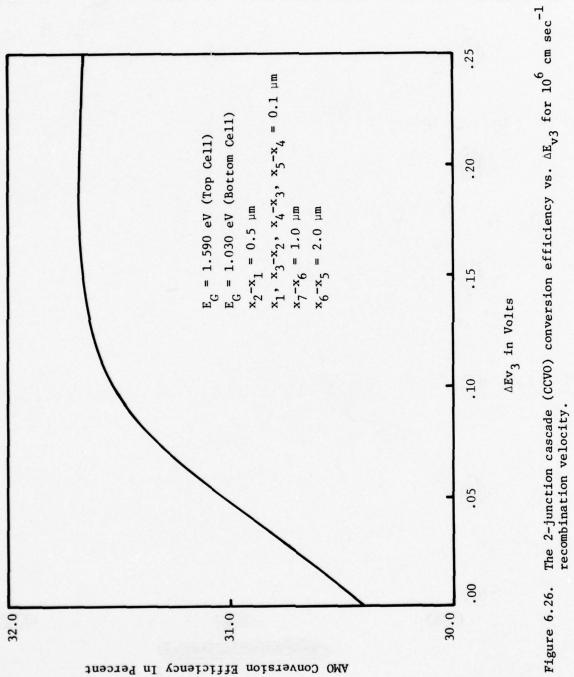


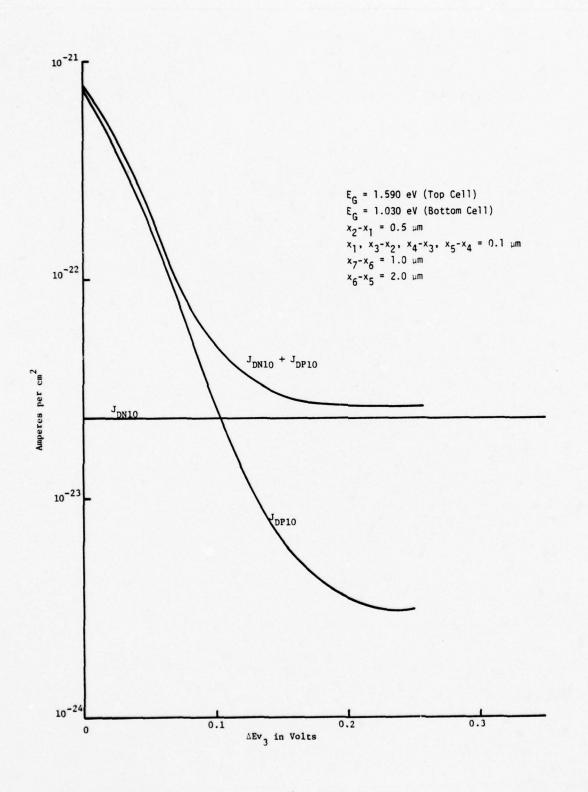
6.5.2 Top Cell

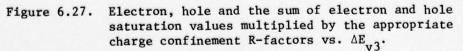
A study was conducted to determine the valence band barrier height, ΔE_{v3} , at x_3 which results in sufficient hole charge confinement in Region 3 to significantly increase efficiency by reducing the hole component of dark current in the Al_{0.14}Ga_{0.86}As homojunction. Here the conversion efficiency was calculated for 8 values of ΔE_{v3} in the range 0 to 0.25 volts. The calculated values are shown in Figure 6.26 with a curve drawn through the points. It is seen that the efficiency increases from 30.7% at $\Delta E_{v3} = 0$ and asymptotically approaches 31.6% at $\Delta E_{v3} = -0.25$. Further, it is seen that at -0.12 volts the efficiency is within 0.3% of the asymptotic value. Therefore, the barrier height, in all subsequent work, was generally chosen at the 0.12 volt level.

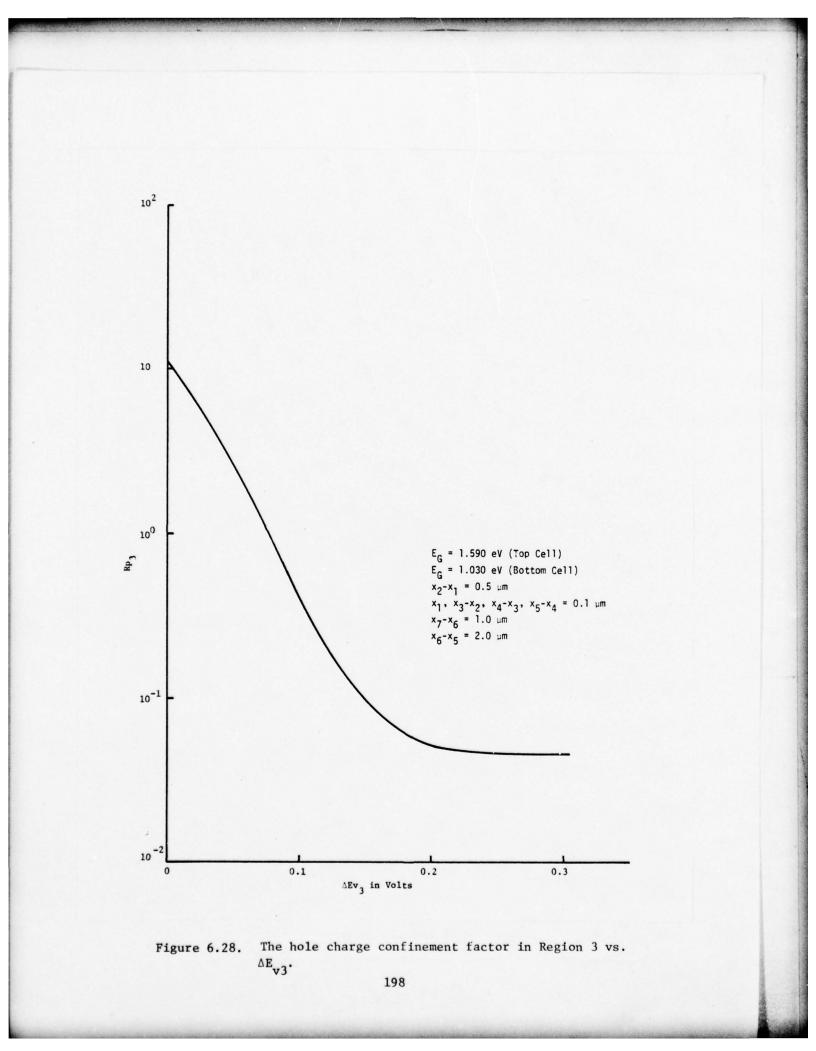
The influence of ΔE_v on the Al_{0.14}Ga_{0.68}As hole contribution to dark current in Region 3 is shown in Figure 6.27. In Figure 6.27 the electron, hole and the sum of the electron plus hole saturation currents multiplied by the appropriate R- factors are plotted vs. $-\Delta E_{v3}$ for the Al_{0.14}Ga_{0.68}As homojunction. The electron contribution to dark current, which arises in Region 2, is independent of ΔE_{v3} and is represented by the horizontial line, J_{Dn10} . In contrast, the hole contribution for $\Delta E_{v3} = 0$ is higher by approximately 30 times than the electron contribution. The hole contribution is reduced by approximately 200 times between $\Delta E_{v3} = 0$ to $\Delta E_{v3} = -0.25$ volts. The sum of the electron and hole contribution shows a reduction by approximately 30 times, approaching the horizontal line, representing the electron contribution, asymptotically.

Figure 6.28 shows the reciprocal of hole charge confinement factor, R_{p3} , vs. E_{v3} . It shows a reduction of approximately 200 between $\Delta E_{v3} = 0$ to







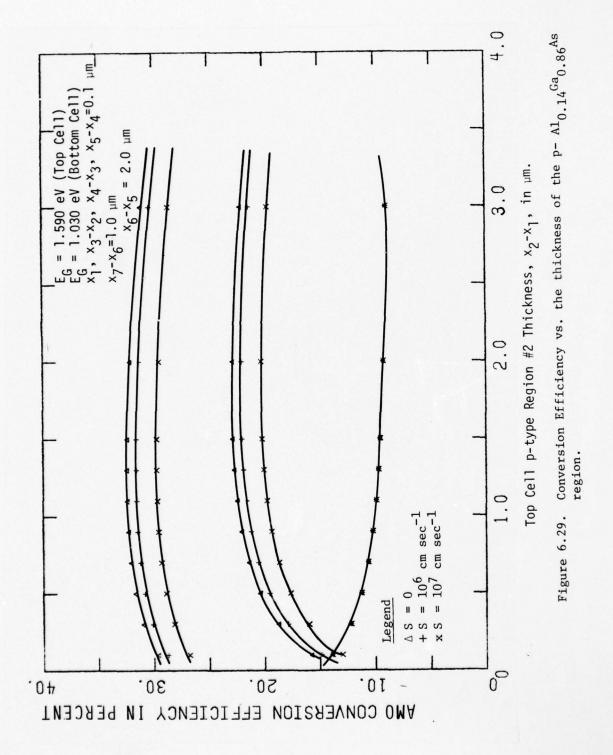


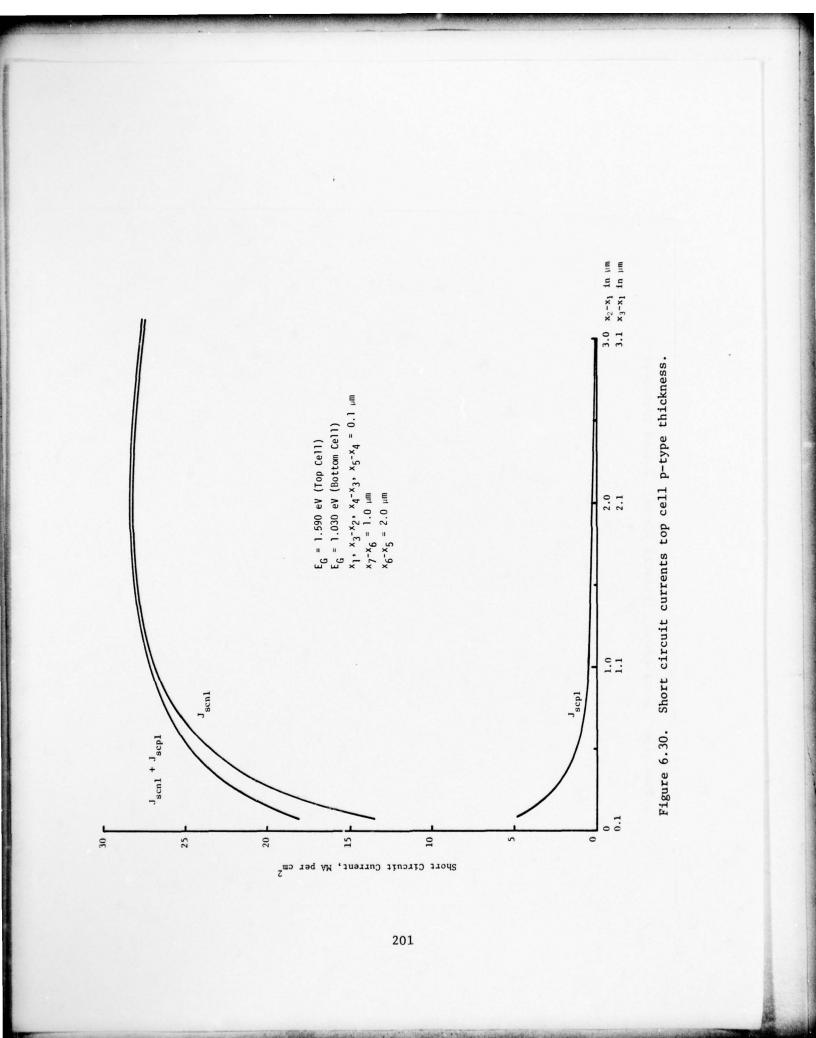
-0.25 volts. It is seen to have the correct magnitude and shape to completely describe the hole dark current change in Region 3.

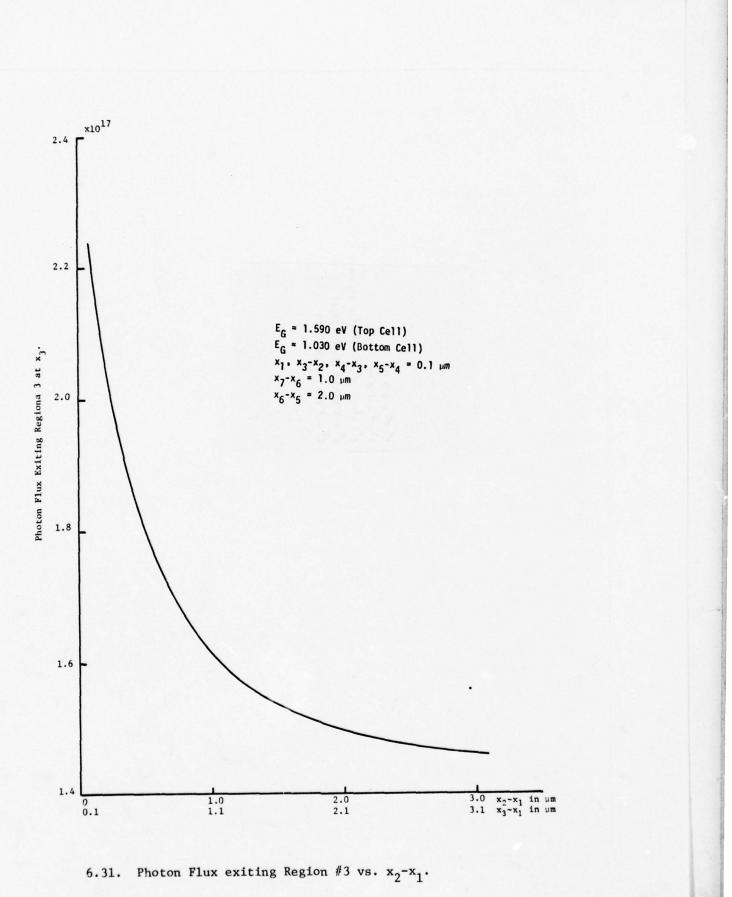
The optimum thickness of the p-type Al_{0.14}Ga_{0.86}As was studied for three SRV values. The results are shown in Figure 6.29. The bottom cell efficiency, n_2 , is independent of SRV because it is isolated from direct and indirect coupling phenomena. The top cell efficiency, n_{τ} , of the CCVO is influenced by SRV and is represented by a curve for each SRV used. The maximum for n_{τ} occurs at approximately 1.4 to 1.5 µm where the efficiency curves are relatively flat with respect to x_2-x_1 . In the range 1.4 to 1.5 µm for x_2-x_1 , the efficiency is 29.7 and 32.4% for 10⁷ and 0 cm sec⁻¹ SRV, respectively.

Figure 6.30 shows the electron, hole and the sum of the electron and hole contributions to the short circuit current density of the top cell as a function of the p-type layer thickness. The hole contribution decreases with increasing x_2-x_1 , while both the total and the electron contributions to short circuit current increase. This occurs because while the n-type thickness is held constant at 0.1 µm the p-type thickness increases. This results in increased photon absorption in the p-type and a decrease in absorption in the n-type. For $x_2-x_1 = 0.1$ µm the electron contribution to the short circuit current is less than 15 mA/cm² while the hole contribution is less than 5 mA/cm². J_{scn1} increases sharply with increasing x_2-x_1 , rising to 28 mA/cm² at approximately 2.0 µm.

Figure 6.31 shows the solar flux exiting Region 3, the top cell n-type layer decreasing sharply with increasing p-type layer thickness, $x_2^{-x_1}$. This is a measure of the increased absorption occurring in Region 2.







The normalized spectral response for Region 1 plus Region 2 is defined by

$$Q_{\rm N12} = \frac{J_{\rm scn1}}{q[N_{\rm ph}(0) - N_{\rm ph}(x_2)]}$$
(6-2)

where J_{scn1} is the electron contribution to short circuit current arising in Regions 1 plus Region2, $N_{ph}(0)$ is the photon flux entering Region 1, $N_{ph}(x_2)$ is the flux exiting Region 2, and q is the electronic charge. The normalized spectral response (NSR) for Regions 1 and 2 is shown in Figure 6.32 for 0, 10^6 and 10^7 cm sec⁻¹ SRV. The NSR decreases monotonically for zero SRV with increasing x_2-x_1 , while it increases and peaks for 10^6 cm sec⁻¹ up to 0.75 µm and for 10^7 cm sec⁻¹ up to 1.3 µm. For non-zero values of SRV the NSR decreases. For zero SRV, increasing x_2-x_1 results in increased bulk recombination with a consequent reduction in NSR. For high SRV, NSR increases for small SRV because the increased absorption in Region 2 more than compensates for the surface losses. At x_2-x_1 values beyond the peak, NSR is reduced with increasing x_2-x_1 values because of increased bulk recombination.

Figure 6.33 shows the electron, hole, and the sum of the electron plus hole saturation currents with each component multiplied by its appropriate charge confinement factor vs. x_2-x_1 . Since x_3-x_2 , the n-type region of the top cell, is maintained constant, the hole contribution, J_{Dp10} , to dark current is independent of x_2-x_1 and is shown as a horizontal line. Decreasing x_2-x_1 results in increased electron charge confinement and, therefore, in decreasing dark current arising from electrons in Region 2. This is shown in Figure 6.33. The total of the electron and hole contributions is also shown and it is always greater than J_{Dp10} .

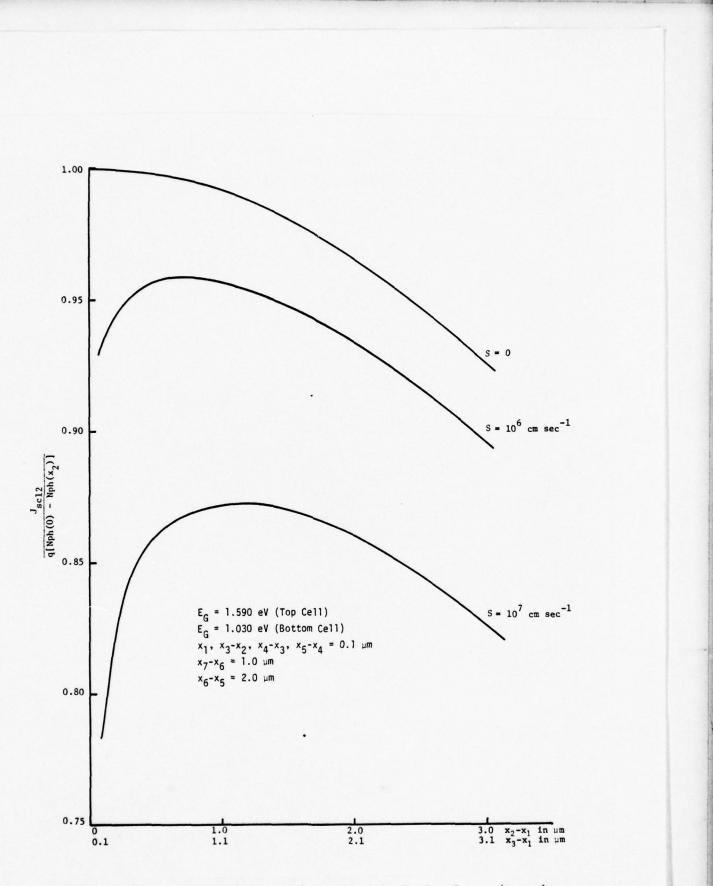
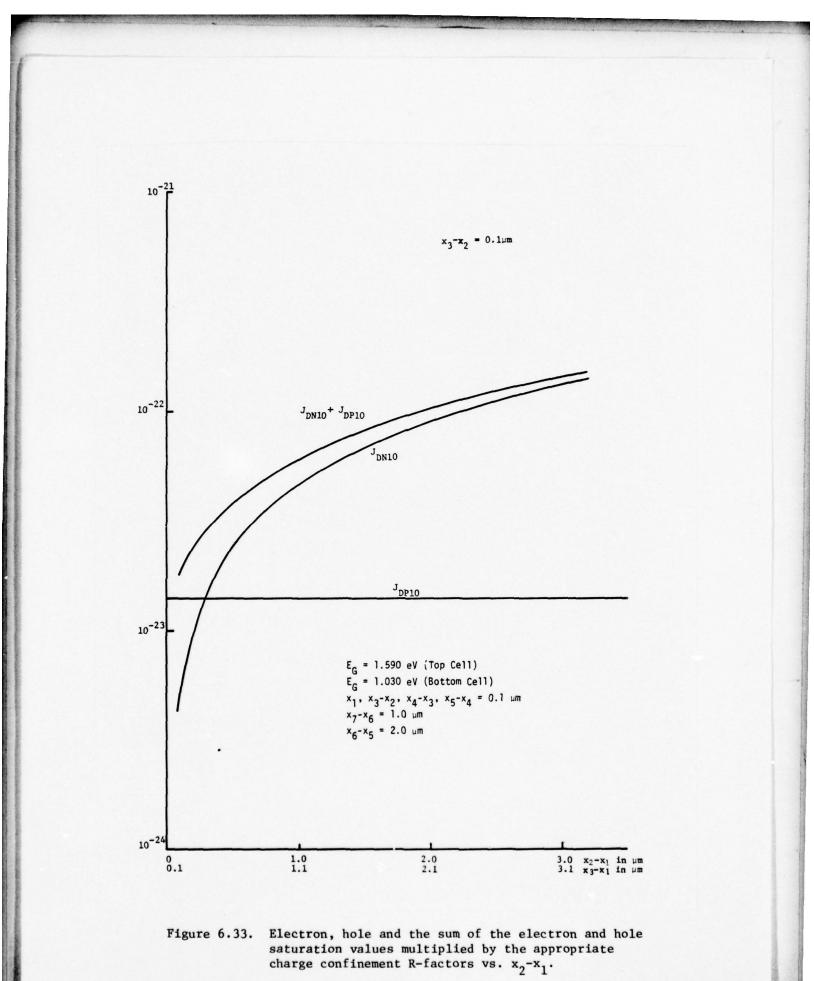
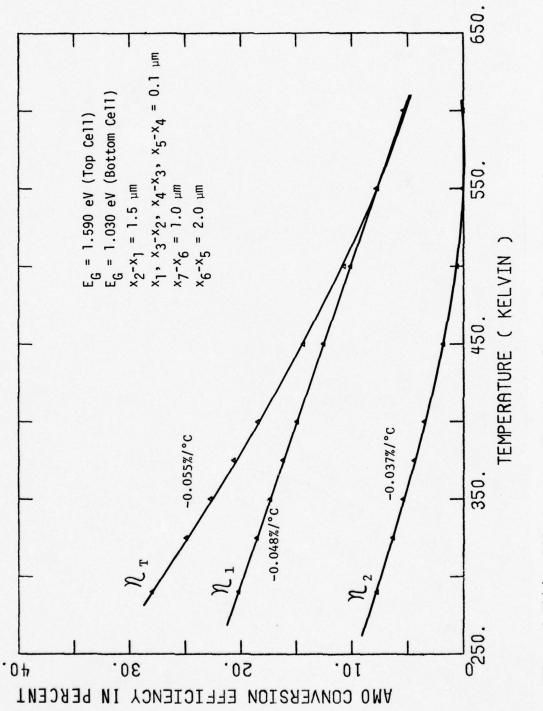
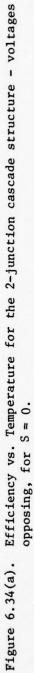


Figure 6.32. Normalized spectral response in Region 2 vs. (x_2-x_1) with surface recombination velocity a parameter.





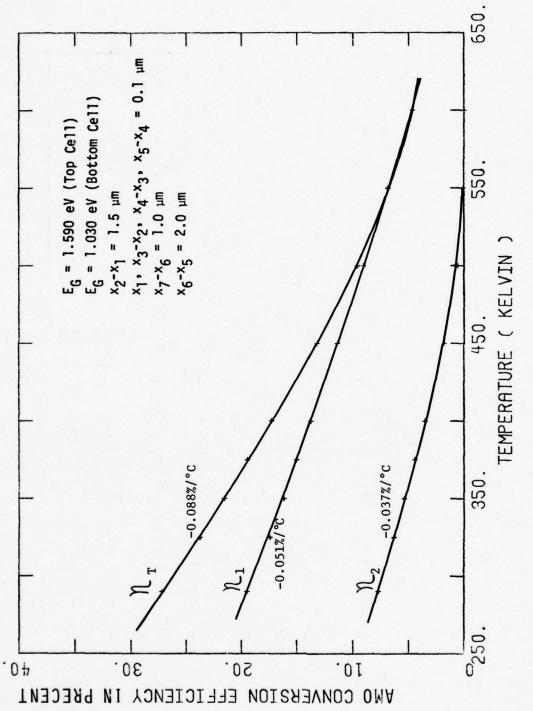


In Figure 6.29 we have seen that the efficiency is maximum in the range 1.4 to 1.5 μ m for x_2-x_1 and not at 2.0 μ m as it is for the short circuit current, in Figure 6.30. This arises because at 1.4 to 1.5 μ m the incomplete absorption loss is more than compensated by the reduced dark current arising from electron confinement in Region 2, and, therefore, the maximum efficiency occurs at 1.4 to 1.5 μ m and not at 2.0 μ m. 6.5.3 Temperature Studies

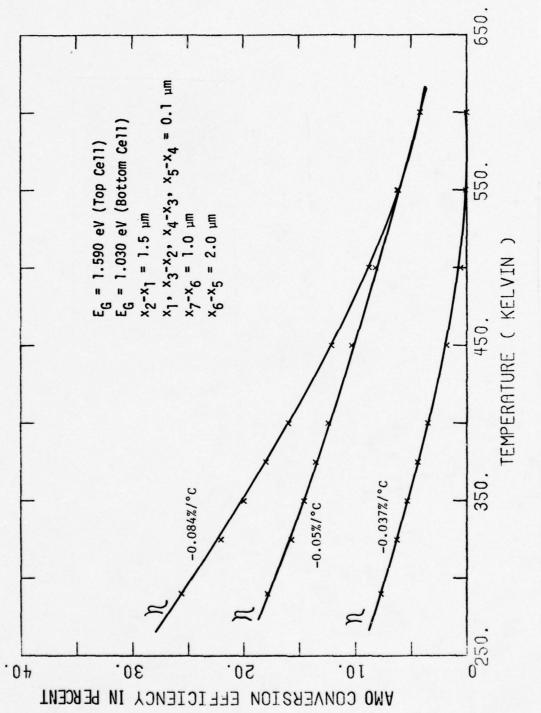
The optimization studies presented in Section 6.5.2 was conducted for 290°K. In this discussion the calculations with respect to temperature are presented.

In Figures 6.34(a), (b) and (c) the individual and the total AMO efficiency are shown as a function of temperature for surface recombination velocities of 0, 10^6 and 10^7 cm sec⁻¹, respectively. The efficiency of the bottom cell, η_2 , is independent of SRV since there are no direct or indirect coupling phenomena. The conversion efficiency temperature coefficient for these curves show them to be relatively constant up to 450°K, and the slope is nearly independent of SRV. The total efficiency temperature coefficient lies in the range of GaAs and Si.

Due to the bandgap shrinkage with increasing temperature, the distribution of the absorbed photon flux through the cascade cell is a function of temperature. The curves in Figure 6.35 show the change in distribution. The sum of the photon flux absorbed in the top cell p-type layers, Regions 1 and 2, shows the largest increase with increasing temperature due to bandgap shrinkage. Regions 3, 4 and 5 show a slight decrease in photon absorption. The reason for this is not clear and more work is required to make any statements regarding this behavior. There is a small increase in photon absorption in Regions 6 and 7.









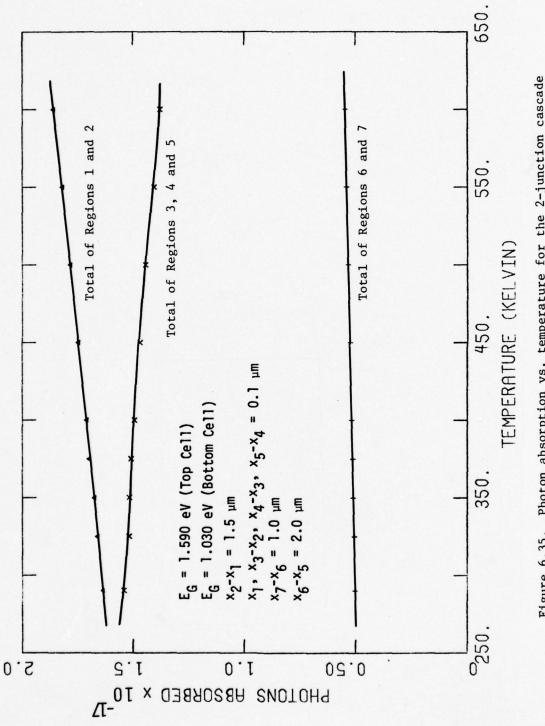


Figure 6.35. Photon absorption vs. temperature for the 2-junction cascade structure - voltages opposing.

6.6 Cascade Cell Fabrication -- Parameter Control

In this section percent changes in efficiency resulting from an imposed +10% change in various structural parameters of the optimized CCVA structure (Figure 6.15) are calculated. These parameters include the bandgap and the alloy composition of the bottom junction, the p- or n-region thickness surrounding the homojunction cells and the sum of the p-region thickness surrounding the homojunction cells. The curves in Figures 6.2, 6.3, 6.6, 6.9 and 6.12 have been employed to determine the efficiency percent changes. Table 6.3 lists the parameters and the corresponding efficiency changes. The efficiency change is greatest for a $\pm 10\%$ change in the bandgap of the In Ga_{1-As} alloy. However, this represents as much as a 24% change in alloy composition. LPE technology has been sufficiently developed for alloy composition control to better than +5%. Therefore, the second listing in efficiency to be less than 6% for a $\pm 10\%$ change in alloy composition is a more reasonable production variance. All efficiency changes are less than 0.19% for impositions of +10% changes on p- and n-region thicknesses. It is also observed that in this optimized design, thickness control of the active regions of each cell is reasonable to achieve high conversion efficiency.

The surface layer window thickness is specified at 0.1 µm in Figure 6.15, but this thickness value should be viewed as a minimum rather than an optimum value. Its only purpose is to reduce surface recombination losses because of the built-in field and the reduced flux absorbed in the surface region due to its wider bandgap value at the surface. This can be accomplished by means of a thin layer and, in fact, a thicker AlGaAs

Parameter	Lim:	its	Effici	ency	Effic Percent	
	Low	High	Low	High	Low	High
Band Gap	0.859 eV u = 48%	1.049 eV u = 33%	31.2%	~28%	-2.5%	~12.5%
Alloy Composition	u = 35% 1.00 eV	u = 43% 0.91 eV	30.3%	31.7%	-5.3	0.9%
x ₈ -x ₇ x ₉ -x ₈	0.95 0.94	1.16 1.15	32.07%	32.07%	-0.03%	0.03%
x9 ^{-x} 7 x8 ^{-x} 7 x9 ^{-x} 8	2.65 1.26 1.39	3.23 1.54 1.69	32.2%	32.2%	-0.03%	0.03%
x ₂ -x ₁ x ₃ -x ₂	0.63	0.77 0.87	32.2%	32.2%	-0.03%	0.03%
$ \begin{array}{c} x_{3} - x_{1} \\ x_{3} - x_{2} \\ x_{2} - x_{1} \end{array} $	1.58 0.825 0.755	1.94 1.02 0.92	32.25%	32.30%	-0.19%	0.03%

Table 6.3. Risk assessment relative to the fabrication of the cascade structure shown in Figure 6.15 for 10^6 cm⁻¹ surface recombination velocity.

layer only absorbs more photons that would be otherwise absorbed in the $1_{0.14}$ Ga_{0.86}As homojunction. This may reduce the efficiency slightly. A variation of $\pm 10\%$ in the surface layer thickness affects the efficiency less than 1%. In addition, the layers forming the tunnel diode portion of the cascade structure affect the conversion efficiency even less, because these layers are designed with materials for which the bandgap value is 1.62 eV. Therefore, they can neither aid or oppose the photoelectronic processes occurring in cell, provided free carrier absorption is small.

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- 6-1. L. W. James, "III-V Compound Heterojunction Solar Cells", 1975 IEEE Electron Devices Meetings, Washington, D.C., December 1-3, 1975.
- 6-2. T. Matsushuta and T. Mamine, "A New Class of Solar Cell with Multilayer Structure", Technical Digest, 1975, Inter. ED Meeting, IEEE, New York, New York.

7.0 RISK ASSESSMENT AND CONCLUDING SUMMARY

In this study, an effort has been made to assess the state-of-theart of III-V solar cells and to illuminate those areas offering the greatest potential for the development of high efficiency solar cells for military space applications. This has been accomplished through a review of the work of other investigators and through computer modeling and design optimization studies of existing as well as novel solar cell designs.

A tabulation of the more promising III-V solar cell configurations and materials combinations (discussed in Section 2.0 through 6.0 of this report) and a comparative summary of their major properties are shown in Table 7.1. Considerations of these and other factors previously discussed have resulted in the following overall assessment of III-V solar cells.

All III-V homojunction cells presently suffer surface recombination problems which seriously limit conversion efficiency values in actual structures. While some method for greatly reducing surface recombination velocity in III-V materials may ultimately be developed (native oxides, for example), it is felt that the chances of a breakthrough are too small to warrant major committments to III-V homojunction cell development.

The heterojunction configuration significantly reduces the front surface recombination problem and is an attractive alternative to the simple homojunction structure. It seems highly likely that active area efficiencies of 20% or more can be achieved in optimized^{*} heterojunction cells fabricated from materials carefully chosen to minimize

Optimized layer thickness and doping levels and introduction of appropriate bandgap grading as discussed in Section 2.0.

	Tabl	Table 7.1. Summary of	Summary of Solar Cell Properties	perties			
Cell Configuration	Fabrication Technology	Special Problems	Relative Cost Unit Area ^l	Projected Efficiency at Maturity ²	Temperature Coefficient (mw/°C)	Radiation Hardness (1 MeV e/cm ²) ³	Years to Maturity ⁴
Homojunction							
Si GaAs AIAIAs GaINAs	Diff Diff/EPI LPE VPE/LPE		0.1 1.0 1.0-1.2 1.0-1.2	17-19 15-17 15-17 15-17	0.09-0.1 0.05-0.06 0.05-0.06 0.05-0.06	10^{16}_{1017} 10^{17}_{1017} 10^{17}_{1017}	 1-4 2-5 3-6
Heterojunction/Graded/PW	Md/p						
GaAlAs-GaAs AlAs-GaAlAs AlAsGaInAs GaAsP-GaAs	LPE LPE VPE/LPE VEP/LPE	Lattice fabri- matching cation	1.0-1.2 1.2-1.5 1.2-1.5 1.0-1.2	20-21 20-21 21-22 19-20	0.05-0.06 0.05-0.06 0.05-0.06 0.05-0.06	$10^{17}_{10^{17}}_{10^{17}}_{10^{17}}_{10^{17}}$	2-5 3-6 3-6 3-6
Shottky Barrier							
GaAs GaAlAs GaPAs	LPE VEP/LPE	Achieving large barrier heights	1.0-1.2 1.0-1.2 1.0-1.2	10-12 11-13 11-13	0.05-0.06 0.05-0.06 0.05-0.06	$\geq 10^{17}$ $\geq 10^{17}$ $\geq 10^{17}$	2-6 2-6 2 6
MIS							
GaAs InP	Oxidation Oxidation	Insulation re-	1.0-1.2 1.2-1.5	15-17 15-17	0.05-0.06	$10^{17}_{10^{17}}$	2-6 2-6
Cascade (two jctn.)							
Ternary or Quaternary	LPE/VPE	Lattice matching	1.5-2.0	28-30 ⁵	0.08-0.09	10 ¹⁷	5-10
¹ Present material costsIII-V costs	stsIII-V o	costs will be reduce	will be reduced with increased production.	sed production	on.		

¹Present material costs--III-V costs will be reduced with increased production. ²AMO, 5% reflection, active area. ³For 50% power reduction ⁴Assumes concentrated effort. ⁵Reduced below calculated values in recognition of increased complexity of fabrication.

lattice mismatch recombination. At present, the AlAs-GaAs or GaAlAs-GaAs heterojunction is the most highly developed III-V solar cell; this cell is judged to be the leading candidate among single-junction III-V cells when evaluated in terms of its overall performance in the space environment and the technical risk associated with its fabrication in production quantities.

Schottky barrier cells, though relatively inexpensive and simple to fabricate, can be ruled out of the competition solely on the basis of extremely low projected efficiency values--lower even than present commercial silicon cells. MIS cells, on the other hand, are characterized by somewhat higher efficiencies than Schottky barrier cells but are more complex than simple Schottky barrier structures and are certainly more difficult to fabricate. Experimental efforts designed to refine MIS fabrication techniques and demonstrate theoretically predicted efficiencies are presently being funded by ERDA, and major Air Force support does not appear warranted.

The most promising avenue toward the realization of appreciably higher efficiency solar cells appears to be in the direction of multijunction III-V structures. The two-junction, voltage-aiding cascade cell, described in detail in Section 6.0 of this report, is highly attractive from the standpoint of both theoretical efficiency and high temperature performance; also, it will very likely offer an improvement in radiation hardness over contemporary silicon cells. Although the particular materials system discussed in Section 6.0 is not lattice-matched, there are several alternative ternary and quaternary systems having essentially the same electrical properties and which avoid lattice mismatch between

the top and bottom cells. We believe that a monolithic two-junction cascade device of the type described can be fabricated via state-ofthe-art liquid-phase epitaxial (LPE) techniques, which have been used successfully in fabricating multi-layer structures and which can be adapted to a production process.

For improved high temperature performance and improved radiation resistance of solar cells at efficiencies as good as or slightly better than silicon cells, it appears that the III-V heterojunction offers the highest probability of achieving these goals. Over the long term, however, it appears that the cascade type of solar cell in a monolithic, lattice matched configuration offers the most promise for significant increases in efficiency as well as good radiation hardness.

It is recommended that major Air Force solar cell programs be directed toward the heterojunction and cascade types of solar cells; smaller developmental efforts could focus on such areas as homojunction III-V cells and MIS cells.

APPENDIX A. SOLUTION OF SEMICONDUCTOR DEVICE EQUATIONS

The internal phenomena governing the operation of a solar cell are described in steady state by the following set of device equations:

$$J_{n} \approx \mu_{n} n \left[qE - \frac{d\chi}{dx} + \frac{kT}{n} \frac{dn}{dx} - \frac{kT}{N_{c}} \frac{dN_{c}}{dp} \right], \qquad (A-1)$$

$$= q \mu_n n \frac{d\phi_n}{dx} , \qquad (A-2)$$

$$J_{p} = \mu_{p} p \left[qE - \frac{dX_{c}}{dx} - \frac{dE_{g}}{dx} - \frac{kT}{p} \frac{dp}{dx} + \frac{kT}{N_{v}} \frac{dN}{dx} \right] , \qquad (A-3)$$

$$= q\mu_{p} p \frac{d\phi_{p}}{dx} , \qquad (A-4)$$

$$0 = G_{e} - U + \frac{1}{q} \frac{dJ_{n}}{dx} , \qquad (A-5)$$

$$0 = G_{e} - U - \frac{1}{q} \frac{dJ_{p}}{dx} , \qquad (A-6)$$

$$\frac{d}{dx} (\varepsilon E) = q(p-n+N)$$
 (A-7)

$$U = \frac{pn - n_{1}^{2}}{\tau_{po}(n + n_{1}) + \tau_{no}(p + p_{1})} , \qquad (A-8)$$

$$G_{e} = \int T \alpha N_{p} \exp \left(\int_{0}^{x} \alpha dx \right) d\lambda . \qquad (A-9)$$

In this form, the equations are valid for graded bandgap materials as well as homogeneous materials. In the special cases of constant bandgap (E_g) and constant electron affinity (X_c) the current density equations reduce to the more familiar form of

$$J_n = q \mu_n E + q D_n \frac{dn}{dx} , \qquad (A-10)$$

$$J_{p} = q \mu_{p} p E - q D_{p} \frac{dp}{dx} . \qquad (A-11)$$

Exact closed form solutions of the general set of device equations are impossible because of the nonlinear nature of the equations. To circumvent this difficulty two approaches are typically taken. One is to approximate the device equations for certain operating conditions to obtain a set of linear equations which can be solved in closed form. The other approach is to obtain exact numerical solutions of the complete set of device equations without any simplifying approximations. Both of these approaches have their place and when used together can be complementary and provide a complete understanding of device operations.

A-1 Approximate Solutions

In obtaining approximate, closed form solutions of the device equations, the approach is to divide a semiconductor into space charge regions occurring around junctions, surfaces and other interfaces and quasi-neutral regions which constitute the bulk of the device. In the space charge regions, operation is dominated by Poisson's equation and in the quasi-neutral regions only the transport and continuity equations are considered. The approximate boundary conditions appropriate to the space charge regions are well established and are not repeated here.

In the quasi-neutral regions, the current density equations can be written as

$$J_n = q\mu_n n E_n + q D_n \frac{dn}{dx} , \qquad (A-12)$$

$$J_{p} = q\mu_{p} p E_{p} - q D_{p} \frac{dp}{dx} , \qquad (A-13)$$

where

$$E_n = E - \frac{1}{q} \frac{d\chi_c}{dx} + \frac{kT}{q} \frac{1}{N_c} \frac{dN_c}{dx} , \qquad (A-14)$$

$$E_{p} = E - \frac{1}{q} \frac{d\chi_{c}}{dx} - \frac{1}{q} \frac{dE_{g}}{dx} + \frac{kT}{q} \frac{1}{N_{v}} \frac{dN_{v}}{dx} . \qquad (A-15)$$

The terms E_n and E_p represent effective fields which act on electrons and holes and are equal to the electric field for constant band gap devices.

Combining the current density equation and continuity equation for electrons gives

$$\frac{d^2 n}{dx^2} + \frac{1}{D_n} \frac{dn}{dx} \frac{dD_n}{dx} + \frac{\mu}{D_n} \left[E_n \frac{dn}{dx} + n \frac{dE_n}{dx} \right] + \frac{n}{D_n} E_n \frac{d\mu}{dx}$$
$$- \frac{U}{D_n} + \frac{G_e}{D_n} = 0. \qquad (A-16)$$

Further approximations are usually made by neglecting dE_n/dx and approximating U as $(n-n_o)/\tau_n$. If now E_n is assumed to be a known function of position, a linear differential equation is obtained. Closed form solutions are still impossible unless any position dependence of D_n, μ_n and E_n are neglected. The resulting linear equation for which closed form solutions can be obtained is

$$\frac{d^2 n}{dx^2} + \frac{qE_n}{kT} \frac{dn}{dx} - \frac{n-n_o}{D_n \tau_n} + \frac{G_e}{D_n} = 0 , \qquad (A-17)$$

where E_n is taken as a constant and G_e is a known function of x. The closed form solutions of this equation are discussed in other sections of this report. A-2 Exact Computer Solutions

The second general approach to the device equations is to treat the equations as a coupled set of non-linear equations which are to be solved numerically. The complete set of device equations can be written as a set of three non-linear, second order equations in three selected variables. The equations for a graded bandgap material are readily expressed in terms of the two quasi-Femi potentials $\phi_{\rm p}$ and $\phi_{\rm p}$ and the electrostatic

potential ψ as

$$\frac{d^2\phi_n}{dx^2} + \frac{d\phi_n}{dx} \left[\frac{1}{n}\frac{dn}{dx} + \frac{1}{\mu_n}\frac{d\mu_n}{dx}\right] - \frac{U}{\mu_n^n} + \frac{G_e}{\mu_n^n} = 0 \qquad (A-13)$$

$$\frac{d^2\phi_p}{dx^2} + \frac{d\phi_p}{dx} \left[\frac{1}{p}\frac{dp}{dx} + \frac{1}{\mu_p}\frac{d\mu_p}{dx}\right] + \frac{U}{\mu_p p} - \frac{G_e}{\mu_p p} = 0 \qquad (A-19)$$

$$\frac{d^2\psi}{dx^2} + \frac{1}{\varepsilon}\frac{d\psi}{dx}\left(\frac{d\varepsilon}{dx}\right) + \frac{q}{\varepsilon} (p-n+N) = 0 \qquad (A-20)$$

To complete this set of equations only requires that n and p be expressed in terms of ϕ_n , ϕ_p , and ψ . This is readily done as

$$n = n_{io} \exp \left[\frac{q}{kT} \left(\psi - \phi_n + \theta_n \right) \right], \qquad (A-21)$$

$$p = n_{io} \exp \left[\frac{q}{kT} \left(\phi_p - \psi + \theta_p \right) \right], \qquad (A-22)$$

where

$$\theta_{n} = \frac{\chi_{c}}{q} - \psi_{o} + \frac{kT}{q} \ln \left(\frac{N_{i}}{n_{io}}\right) , \qquad (A-23)$$

$$\theta_{p} = \frac{1}{q} \left(\chi_{c} + E_{g} \right) + \psi_{o} + \frac{kT}{q} \ln \left(\frac{N_{v}}{n_{io}} \right) . \qquad (A-24)$$

In these n_{io} is some convenient constant intrinsic carrier density and ψ_o is some reference potential. Both n_{io} and ψ_o can be conveniently selected so that $\theta_n = 0$ and $\theta_p = 0$ at any desired composition.

The solution of Equations (A-18) through (A-24) can be obtained by any appropriate numerical techniques such as finite difference techniques. To obtain solutions, boundary conditions are required for the three variables

 ϕ_n , ϕ_p and ψ at the terminals of the device. These are easily obtained if ohmic boundary conditions are assumed at the terminals. In solar cells, however, the front surface is typically a low surface recombination boundary. This can be taken into account in the solution of the device equations. Techniques used in solving the equations have been discussed elsewhere [A1, A2] and will not be repeated here.

In any modeling of solar cells, the various device parameters such as mobility, fields, etc. must be known. Most of the device parameters depend on doping density and in graded band gap devices also depend on the material composition at any point within the device. The modeling of these device parameters is discussed in Appendix B.

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- A2. P. M. Dunbar and J. R. Hauser, "A Theoretical Analysis of the Current-Voltage Characteristics of Solar Cells", Annual Report on NASA Grant NGR 34-002-195, August 1975.

APPENDIX B. MODELING OF DEVICE PARAMETERS

B-1 Introduction

The material parameter modeling discussed in the following sections makes possible the computer analysis of solar cells made of a spatially varying alloy of two compatible semiconductors. Given the material properties of the two binary semiconductors, the computer program generates approximate parameters for the specified ternary composition. For example, solar cells made of the alloy, $Al_xGa_{1-x}As$, are analyzed by providing the material properties of AlAs and GaAs, along with the desired composition profile, i.e. the mole fraction of AlAs, x, vs. position. Equations of both a theoretical and empirical nature have been used to obtain the alloy material parameters from the binary material parameters. Whenever possible, these approximations have been checked against experimental results and adjusted to improve the agreement with available data. The most important approximations are described in the following sections.

B-2 Dielectric Constant vs. Composition

Given the dielectric constants, ε_1 and ε_2 , for semiconductors 1 and 2, the following interpolation scheme is used to estimate the dielectric constant, ε , for an alloy that has mole fraction, C, of material 1, [B-1]:

$$\varepsilon = \frac{1+2\left[C\left(\frac{\varepsilon_{1}^{-1}}{\varepsilon_{1}^{+2}}\right) + (1-C)\left(\frac{\varepsilon_{2}^{-1}}{\varepsilon_{2}^{+2}}\right)\right]}{1-C\left(\frac{\varepsilon_{1}^{-1}}{\varepsilon_{1}^{+2}}\right) - (1-C)\left(\frac{\varepsilon_{2}^{-1}}{\varepsilon_{2}^{+2}}\right)}$$
(B-1)

^{*} Most of the work reported in this section was performed on a separate NASA Langley Research Grant to N. C. State University (NSG 1116), and is being published elsewhere [B-2, B-3]. It is included here for reference and for completeness.

B-3 Band Structure Parameters vs. Composition

 $Al_xGa_{1-x}As$ and $GaAs_{1-x}P_x$ have both a direct and an indirect bandgap which are important over various alloy compositions, and the solar cell program permits the specification of two valleys, each with its own composition dependent parameters such as band gap, effective mass and mobility. Assuming these two electron populations are at equilibrium with each other, a single electron quasi-Fermi potential, ϕ_n , can be used in the device equations. Then an "effective" electron mobility and "effective" electron mass can be defined such that a single current density equation and a single carrier density equation is sufficient for this two conduction band valley model. The following sections describe the techniques used to determine the resultant band structure parameters (such as electron and hole mobilities) of an alloy, from the band structure parameters for each of the two components.

Band Gap vs. Composition

Experimental studies have shown that the direct energy gap for III-V alloys has an approximately quadratic dependence on composition such as [B-4].

$$E_{gd} = a C^2 + bC + E_{gd2}$$
 (B-2)

where a and b are experimental values. The same form was used to model the indirect variation in $GaAs_{1-x}P_x$, while for $A_x^1Ga_{1-x}Ax$, the indirect gap was estimated by a linear variation with composition. The bandgap is the minimum of the direct or indirect bandgaps.

Effective Masses

The effective masses, m*, for holes and electrons were obtained by interpolating between the effective masses, m* and m*, of the alloy components

in the following manner [B-1]:

$$\frac{1}{m^*} = \frac{C}{m^*_1} + \frac{1-C}{m^*_2} . \tag{B-3}$$

For the direct and indirect conduction bands a single effective mass was obtained through use of the expression

$$n = N_{c} \exp\left(\frac{E_{Fn}-E_{c}}{kT}\right) = N_{cd} \exp\left(\frac{E_{Fn}-E_{cd}}{kT}\right) + N_{ci} \exp\left(\frac{E_{Fn}-E_{ci}}{kT}\right), (B-4)$$

where N_c is an effective density of states for the two valleys and N_{cd} and N_{ci} are the densities of states for the direct and indirect valleys respectively. From the above, a combined density of states effective mass can be defined for use in N_c as

$$m_{n}^{*} = [m_{cd}^{*}]^{3/2} \exp(\frac{E_{g}^{-E}gd}{kT}) + m_{ci}^{*}]^{3/2} \exp(-\frac{E_{g}^{-E}gi}{kT})]^{2/3}$$
(B-5)

where E_{gd} is the direct energy gap, E_{gi} is the indirect gap, E_g is the actual gap (either E_{gd} or E_{gi}) and m_{cd}^* and m_{ci}^* are the direct and indirect valley effective masses respectively.

Hole Mobility

Mobility depends not only on alloy composition, but on the doping level as well. In order to calculate hole mobility for an arbitrary doping and composition, an empirical formula, f_{p2} , was constructed to approximate the doping dependence of hole mobility for one of the alloy components, to be referred to as material 2:

$$\mu_{p2} = f_{p2}(N)$$
 (B-6)

where N = total impurity concentration. The form of f_{p2} was taken to be

$$f_{p2}(N) = \frac{A_p}{(1+N/N_p)^{\alpha}}$$
 (B-7)

Now, because

$$\mu_{p} = \frac{q < \tau^{>}}{m^{*}_{p}} = \mu_{p2} \frac{m^{*}_{p2}}{< \tau_{p2}^{>}} \frac{< \tau^{>}_{p}}{m^{*}_{p}}, \qquad (B-8)$$

it is apparent that if $\langle \tau_p \rangle$ and m_p^* can be specified as functions of composition, then a reasonable approximation to hole mobility for any doping level and composition can be made. In the III-V semiconductors, mobility is controlled primarily by a polar optical phonon scattering process¹ of the form [B-6]

$$<\tau > \frac{K}{m^* (\frac{1}{\varepsilon_h} - \frac{1}{\varepsilon_\ell})}$$
, (B-9)

where K is a proportionality constant for all materials and ε_h and ε_l are the high and low frequency relative dielectric constants.

Combining Equations (B-8) and (B-9) then gives as an approximation to the mobility

$$\mu_{p}(N,C) = \frac{f_{p2}(N) m_{p2}^{*} \frac{3/2}{\varepsilon_{h2}} \left(\frac{1}{\varepsilon_{h2}} - \frac{1}{\varepsilon_{\ell2}}\right)}{m_{p}^{*} \frac{3/2}{\varepsilon_{\ell1}} \left(\frac{1}{\varepsilon_{h2}} - \frac{1}{\varepsilon_{\ell2}}\right)}.$$
 (B-10)

where m_{p2}^{\star} , ε_{l2}^{\star} , and ε_{h2}^{\star} are known parameters of material 2, and ε_{l}^{\star} , ε_{h}^{\star} , and m_{p}^{\star} are given as functions of composition by Equations (B-1) and (B-3).

Electron Mobility

The modeling of electron mobility is more complex than hole mobility because of the indirect and direct bands. Treating the direct and indirect valleys independently, and using the same technique as described for hole mobility, a direct valley electron mobility, μ_d , and an indirect valley electron mobility, μ_i , can be determined approximately as:

¹The validity of this assumption has been questioned for hole mobility in n-type indirect gap and p-type III-V semiconductors [B-5].

$$\mu_{d}(N,C) = \frac{f_{n2}(N) m_{cd2}^{*} \frac{3/2(\frac{1}{\epsilon_{h2}} - \frac{1}{\epsilon_{\ell2}})}{m_{cd}^{*} \frac{3/2(\frac{1}{\epsilon_{h}} - \frac{1}{\epsilon_{\ell2}})}{m_{cd}^{*} \frac{3/2(\frac{1}{\epsilon_{h}} - \frac{1}{\epsilon_{\ell2}})}}$$
(B-11)
$$\mu_{i}(N,C) = \frac{f_{n1}(N) m_{ci2}^{*} \frac{3/2(\frac{1}{\epsilon_{h1}} - \frac{1}{\epsilon_{\ell2}})}{m_{ci}^{*} \frac{3/2(\frac{1}{\epsilon_{h2}} - \frac{1}{\epsilon_{\ell2}})}}{m_{ci}^{*} \frac{3/2(\frac{1}{\epsilon_{h2}} - \frac{1}{\epsilon_{\ell2}})}{m_{ci}^{*} \frac{1}{\epsilon_{Li}} \frac{1}{\epsilon_{$$

where m_{cd2}^{\star} , m_{c11}^{\star} , ε_{k2} , ε_{k1} , ε_{h2} and ε_{h1} are known parameters of materials 1 and 2, $f_{n2}(N)$ is an empirical function relating electron mobility to doping for material 2, $f_{n1}(N)$ is an empirical function relating electron mobility to doping for material 1 and ε_{l} , ε_{h} , m_{cd}^{\star} and m_{c1}^{\star} are given by Equations (B-1) and (B-3). The functions f_{n1} and f_{n2} used the same functional form as Equation (B-7). An "effective" mobility for use in the current density equation can be found by weighing the direct and indirect mobilities by their respective electron populations, as

$$\mu_{n}(N,C) = \mu_{d}R_{d} + \mu_{i}(1-R_{D})$$
(B-13)

where ${\rm R}_{\rm d}$ is the fraction of electrons in the direct valley given by the expression

$$R_{d} = \frac{n_{d}}{n_{d} + n_{i}} = \frac{1}{\frac{m_{d}^{*}(c_{i})}{1 + (\frac{c_{i}}{m_{cd}^{*}})^{3/2}} \exp(\frac{E_{gd} - E_{gi}}{kT})} .$$
 (B-14)

Band Parameters, θ_n and θ_p

In order to model the composition dependence of the band parameters, θ_n and θ_p , some knowledge of the variation of electron affinity, χ_c , and bandgap E_g, must be available. It has been found to be advantageous to select the potential reference, ψ_o , so that $\theta_n = \theta_p = 0$ when the mole fraction of material 1 is zero. In other words, θ_n and θ_p are zero in regions of the solar cell consisting entirely of material 2. Then

$$\psi_{0} = \frac{\chi_{c2}}{q} + \frac{kT}{q} \ln \left(\frac{N_{c2}}{n_{12}}\right) , \qquad (B-15)$$

or equivalently,

$$\psi_{o} = \frac{\chi_{c2} + E_{g2}}{q} - \frac{kT}{q} \ln \left(\frac{N_{v2}}{n_{12}}\right) . \qquad (B-16)$$

Now, inserting Equation (B-15) into Equation (A-23), and Equation (B-16) into Equation (A-24) gives:

$$\theta_n = \frac{\chi_c^{-\chi} c^2}{q} + \frac{kT}{q} \ln \left(\frac{N_{v2}}{n_{i2}}\right) ,$$
(B-17)

$$\Theta_{\rm p} = \frac{\chi_{\rm c2} - \chi_{\rm c}}{q} + \frac{E_{\rm g2} - E}{q} + \frac{kT}{q} \ln \left(\frac{N_{\rm v}}{N_{\rm v2}}\right) .$$
 (B-18)

Finally, in terms of effect mass:

$$\theta_{n} = \frac{\Delta \chi_{c}}{q} + \frac{3}{2} \frac{kT}{q} \ln \left(\frac{m^{*}}{m^{*}}\right)$$
(B-19)

$$\theta_{p} = \frac{-(\Delta \chi_{c} + \Delta E_{g})}{q} + \frac{3}{2} \frac{kT}{q} \ln \left(\frac{m*}{m_{p2}}\right)$$
(B-20)

where $\Delta \chi_c = \chi_c - \chi_{c2}$ and $\Delta E_g = E_g - E_{g2}$.

Equations (B-19) and (B-20) are the forms used to compute the band parameters for an arbitrary alloy of two materials.

Interface Recombination

At an abrupt interface between two semiconductors, lattice mismatch introduces trapping levels due to dangling bonds. For a [100] interface, the density of dangling bonds is given by [B-7].

$$N_{s} = \frac{4(a_{2}^{2}-a_{1}^{2})}{a_{2}^{2}a_{1}^{2}}$$
(B-21)

where a₁ and a₂ are the lattice constants of the two materials. If the composition change is gradual, rather than abrupt, the trapping levels have been assumed in this work to have a volume density that is proportional to the slope of the composition profile as

$$N_{RH} = N_{ST} \frac{dC}{dx} , \qquad (B-22)$$

where N_{ST} is the total density (per unit area) of dangling bonds in going from pure material 1 to pure material 2. These interface states have been incorporated into the Shockley-Read-Hall model by modification of the excess carrier lifetimes:

$$\frac{1}{\tau_{no}} = \frac{1}{\tau_{no}} \left|_{Bulk} + \frac{1}{N_{RH}C_R} \right|$$
(B-23)

$$\frac{1}{\tau_{po}} = \frac{1}{\tau_{po}} \left|_{Bulk} + \frac{1}{N_{RH}C_R} \right|$$
(B-24)

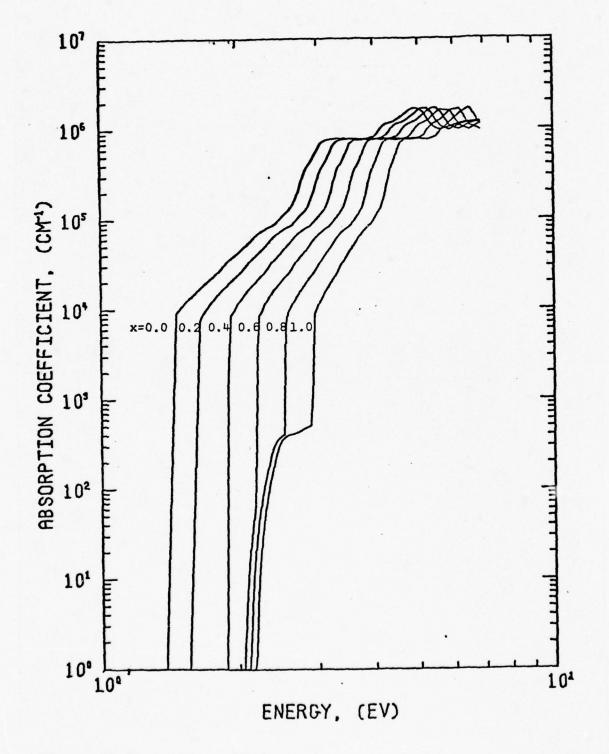
where C_R is the capture coefficient. Ettenberg and Kressel [B-8] obtained a value of 8×10^3 cm/s for the interface recombination velocity at an abrupt $A1_{0.5}Ga_{0.5}As - GaAs$ heterojunction, indicating a value of 5.2 x 10^{-9} cm³/s for C_R . For the lack of further data, this value was used to determine the excess carrier lifetimes for holes and electrons in both $A1_xGa_{1-x}As$ and $GaAs_{1-x}P_x$ solar cells. The density of interface states is increased greatly, however, for the GaAs-GaP heterojunction because of the larger lattice mismatch. The bulk lifetimes, τ_{no} and τ_{po} were assigned values of 5.3 nsec and 8.5 nsec, respectively, as calculated from an estimate of the diffusion lengths as functions of doping [B-9].

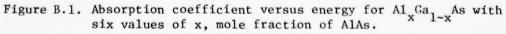
Optical Carrier Generation

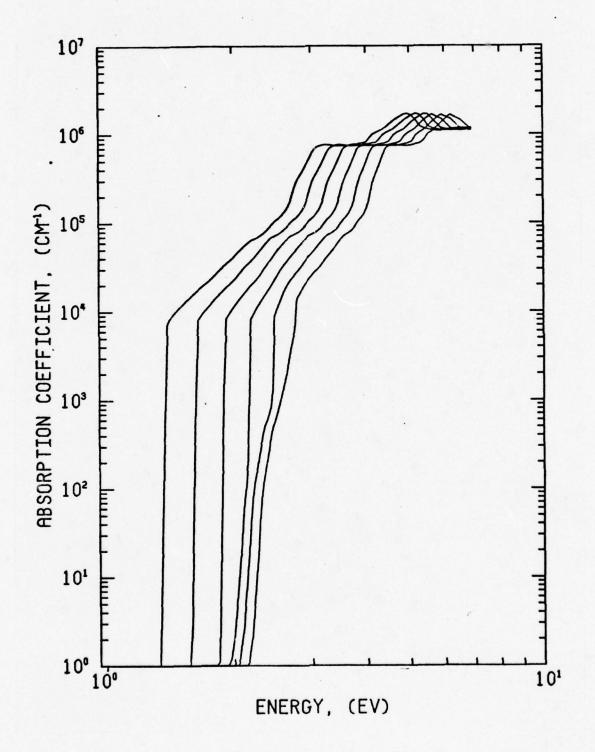
The optical carrier generation rate was determined by the equation

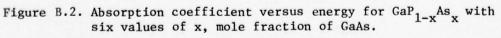
$$G_{e} = \sum_{\lambda} T(\lambda)N(\lambda)\alpha[C(x),\lambda]exp\{-\int_{0}^{x} \alpha[C(y),\lambda]dy\}$$
(B-25)

where $T(\lambda)$ is the antireflection layer transmission coefficient, $N(\lambda)$ is the incident photon density per wavelength interval, C(x) is the composition profile, and $\alpha[C(x),\lambda]$ is the absorption coefficient, which was taken to be the sum of two absorption coefficients, one pertaining to direct transitions and the other to indirect transitions. The direct absorption coefficient for a ternary semiconductor was approximated by shifting the α vs. E profile of GaAs by the amount of the difference between the direct band gaps of the alloy and GaAs. Similarly, the indirect portion of the α vs. E profile of the indirect binary material was approximated by shifting the indirect portion of the α vs. E profile of the indirect binary material (AlAs or GaP) by the amount of the difference between the indirect bandgaps of the alloy and its indirect binary component. This technique is similar to that used by Hutchby [B-10]. The resulting absorption coefficient is shown in Figure B.1 and B.2 for various compositions of Al_{1-x}Ga_As and GaP_{1-x}As_x.









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APPENDIX C. CURRENT COMPONENTS FOR SCHOTTKY BARRIER SOLAR CELLS

This appendix shows the relationships to material parameters and device dimension of each of the dark current density and photocurrent density components used in the device model for Schottky barrier solar cell calculations.

A. Dark Current Components

The three dark current density components given in Eqn. (3-3) are:

1)
$$J_{SB} = A^{**}T^2 \exp\left(\frac{-\phi_B}{kT}\right) \left\{ \exp\left(\frac{qV_a}{kT}\right) - 1 \right\}$$

where

$$A^{**} = 120 \left(\frac{m_{n}}{m_{o}}\right) \text{amps/cm}^2 \text{ K}^2$$

is the effective Richardson constant. Here m_n^* is the electron effective mass, ϕ_B is the barrier height energy, k is Boltzmann's constant (8.62 x 10⁻⁵ eV/K), T is absolute temperature, q is electron charge, and V_a is applied voltage.

2)
$$J_{R} = \frac{q n_{i}^{2} W_{n}}{(\tau_{po} n_{1} + \tau_{no} p_{1}) + (\tau_{po} + \tau_{no}) n_{i} \exp\left(\frac{qV_{a}}{kT}\right)}$$

For a discussion of this model for recombination current see reference [3-21].

3)
$$J_{\text{Diff}} = J_s \left\{ \exp\left(\frac{qV_a}{kT}\right) - 1 \right\}$$

where

$$\mathbf{J}_{s} = \frac{q\mathbf{D}_{p}\mathbf{P}_{o}}{\mathbf{L}_{p}} \frac{\sinh\left(\frac{\mathbf{W}}{\mathbf{L}_{p}}\right) + \frac{\mathbf{SL}_{p}}{\mathbf{D}_{p}} \cosh\left(\frac{\mathbf{W}}{\mathbf{L}_{p}}\right)}{\cosh\left(\frac{\mathbf{W}}{\mathbf{L}_{p}}\right) + \frac{\mathbf{SL}_{p}}{\mathbf{D}_{p}} \sinh\left(\frac{\mathbf{W}}{\mathbf{L}_{p}}\right)}$$

and the terms are defined in the text.

B. Photocurrent Components

The components of photocurrent density per unit optical band width used in Eqn. (3-3) are given by:

1)
$$J_{DR}(\lambda) = \frac{qG_o(\lambda)}{\alpha(\lambda)} \left\{ 1 - \exp\left[-\alpha(\lambda)W_n\right] \right\}$$

where ${\tt G}_{{\tt O}}$ is the surface generation rate and α is the absorption coefficient.

2)
$$J_{p}(\lambda) = \frac{qG_{o}(\lambda)L_{p} \exp \left[-\alpha(\lambda)W_{n}\right]}{\left[\alpha(\lambda)L_{p}\right]^{2} - 1} \left[\alpha(\lambda)L_{p} - F(\lambda)\right]$$

where

3)
$$F(\lambda) = \frac{\frac{SL_p}{D_p} \left\{ \cosh\left(\frac{W}{L_p}\right) - \exp\left[-\alpha(\lambda)W\right] \right\} + \sinh\left(\frac{W}{L_p}\right) + \alpha(\lambda)L_p \exp\left[-\alpha(\lambda)W_n\right]}{\cosh\left(\frac{W}{L_p}\right) + \frac{SL_p}{D_p} \sinh\left(\frac{W}{L_p}\right)}$$

For a discussion of this equation see reference [3-1], p. 112 ff.

APPENDIX D. ASSUMPTIONS USED IN THE CLOSED FORM ANALYSIS

The assumptions used in the derivation of the closed form equations and in the calculations are described below.

D.1 Statistics

Nondegenerate semiconductor material will be assumed over the temperature range of interest. Therefore, Boltzmann statistics will be considered applicable in all cases; i.e., the Fermi level is at least several kT below the conduction band edge in n-type and several kT above the valence band edge in p-type.

D.2. Recombination

The usual single trapping level model is assumed for recombination. While for III-V semiconductor compounds multiple recombination levels are not uncommon, the single level is useful, nevertheless, because it does include the general features of the multilevel model without the increased complexity of a multiple level model analysis.

The recombination rate for a single level recombination center located at energy E_{t} and concentration N_{t} is given by

$$r = \frac{\sigma_n \sigma_p v_{th} (pn - n_i^2) N_t}{\sigma_n \left[n + n_i e^{(E_t - E_i)/kT}\right] + \sigma_p \left[p + n_i e^{-(E_t - E_i)/kT}\right]}, \quad (D-1)$$

where

 $v_{th} = \left[\frac{3kT}{m^*}\right]^{1/2}$: electron and hole capture cross sections, respectively m^* : effective mass

- E_i : intrinsic Fermi energy level
- n, : intrinsic carrier concentration

A simplifying assumption usually made is that

$$\sigma_{n} = \sigma_{p} = \sigma \qquad (D-2)$$

reducing Eq. (D-1) to

$$r = \sigma v_{th} N_t \frac{pn - n_i^2}{n + p + 2n_i \cosh(E_t - E_i)/kT}$$
(D-3)

The recombination rate is a maximum when the recombination energy level, E_t , is at approximately the center of the forbidden bandgap, i.e.,

$$E_{t} = E_{i}, \qquad (D-4)$$

for which

$$\cosh(E_t - E_i)/kT = 1.$$
 (D-5)

Thus, recombination centers located at mid bandgap are most effective in affecting recombination. Equation (D-3) also shows that increasing the concentration of recombination centers also increases the rate.

In solar cells irradiated up to several solar constants, the minority carrier concentrations are low compared to the majority carrier concentrations, i.e.,

$$n_p - n_{po} \ll p_{po}$$
(D-6)

and

$$p_n - p_{no} \ll n_{no}$$
(D-7)

where n po, po, pno, no are the equilibrium values, and n and pn are

the non-equilibrium values of electrons and holes. The low injection level recombination rates are well established and given by

$$r_n = \frac{\frac{n}{p} - \frac{n}{po}}{\frac{\tau_n}{n}}$$
(D-8)

for electrons in p-type, and

$$r_{p} = \frac{p_{n} - p_{no}}{\tau_{p}}$$
(D-9)

for holes in n-type material, where τ_n and τ_p are the electron and hole lifetimes, respectively.

In n-type solar cell semiconductors $n \approx n_{po}$ and $n >> p >> n_i$, and if in Eq. (D-1) we set $E_t = E_i$, the result is the hole recombination given by

$$r_{p} = \sigma_{p} v_{th} N_{t} (p - p_{no}) . \qquad (D-10)$$

Comparing with Eq. (D-9) it is seen that

$$\tau_{p} = \frac{1}{\sigma_{p} v_{th} N_{t}} . \tag{D-11}$$

Similarly, the electron lifetime in p-type is given by

$$\tau_{n} = \frac{1}{\sigma_{n} v_{th} v_{t}} . \qquad (D-12)$$

Therefore, we observe that electron and hole lifetimes are inversely proportional to the recombination center concentration. This has been established many times by experiment. Thus, Eqs. (D-8) and (D-9) will be employed as the recombination rate in the integral-differential continuity equations.

D.3 Junction Recombination/Transport Processes

The junction current mechanisms have been studied extensively and are too numerous to reference. Shockley's ideal diffusion transport model is one in which minority carriers are injected across the space charge of a forward biased junction and the minority carrier flux is not attenuated by depletion region recombination. This results in the smallest dark current and, therefore, the highest open circuit voltage for a given short-circuit current. The dark current is given by

$$I_{D} = q \left[n_{po} \left(\frac{D_{n}}{\tau_{n}} \right)^{1/2} + p_{no} \left(\frac{D_{p}}{\tau_{p}} \right)^{1/2} \right] \left(e^{qV/kT} - 1 \right). \quad (D-13)$$

The space charge recombination model includes a recombination process in the space charge region which attenuates the minority carrier flux, increases the dark current, reduces the open circuit voltage, and also reduces the fill factor, F_c . It is sometimes approximated by

$$I_{rg} = I_{rgo} \left[e^{qV/2kT} - 1 \right]$$
 (D-14)

where

$$I_{rgo} = \frac{qn_i^W}{\sqrt{\tau_p \tau_n}}; \qquad (D-15)$$

W is the depletion width and τ_n and τ_p are the electron and hole lifetimes in the space charge region.

D.4 Carrier Transport

The carrier mobilities are considered as being independent of position through a layer. Where necessary, average values are determined

in the analysis. However, the influence of active impurity concentration on the average carrier mobilities (ionized impurity scattering) is included at the point where the alloy composition changes from a direct to an indirect transition material such as in $Al_xGa_{1-x}As$ and GaP_xAs_{1-x} . When such an alloy is present, the layer may be separated into two layers and solutions obtained in each layer. In those cases where the calculation is improved significantly or pertinent design understanding is enhanced, this has been done.

Changes in mobility are also reflected in the minority carrier diffusion coefficient through the Einstein relationships,

$$D_n = \frac{kT}{q} \mu_n \tag{D-16}$$

$$D_{p} = \frac{kT}{q} \mu_{p} \qquad (D-17)$$

for electrons and holes, respectively, where (kT/q) is the thermal voltage.

In all cases, the electric field values considered are less than the critical field value, 3000 v/cm, so as to avoid the consideration of hot electrons. Exceeding the critical field value results in a decrease in minority carrier diffusion length and is, therefore, to be avoided in solar cells.

D.5 Solar Cell V-I Curve Fill Factor

The power out put of a solar cell is determined experimentally by obtaining the solar cell V-I curve and calculating the maximum power point. The short-circuit current is obtained from the spectral collection efficiency Q as

$$I_{sc} = \int_0^{\lambda_c} (1 - R) N_o Q d\lambda \qquad (D-18)$$

where R is the reflectivity, N the incident solar radiation photon flux

per unit wavelength, and λ_{c} the cut-off wavelength of the material. The open circuit voltage is given by

$$V_{oc} = \frac{1}{\beta} \ln \frac{I_{sc}}{I_o}$$
(D-19)

where $\boldsymbol{\beta}$ and \boldsymbol{I}_{o} are defined in the dark current relationship

$$I = I_{0}(e^{\beta V}-1)$$
 (D-20)

Maximum power is then determined from the equation

$$P_{\max} = F_{c} \frac{I_{sc}}{\beta} \ln \frac{I_{sc}}{I_{o}} . \qquad (D-21)$$

The value of F_c is sensitive to the dark current parameters, I_o and β . F_c may change significantly for cases of dark current arising from diffusion, space charge recombination or tunneling.

In the solutions to the integral-differential equations, the fill factor is not required to determine the maximum power. The maximum power point is obtained directly from the calculated solar cell V-I curve. The maximum power point is dependent on the dark current mechanism used in the boundary conditions, which is the equivalent of determining the appropriate fill factor.

D.6 Current Conventions

The current density equations for the one-dimensional case are

$$J_{n} = q\mu_{n}nE + qD_{n}\frac{dn}{dx}$$
(D-22)

$$J_{p} = q\mu_{p}pE - qD_{p}\frac{dp}{dx}$$
(D-23)

for electrons and holes, respectively, where

q: electronic change,

 μ_n , μ_p : electron and hole mobility

E: electric field,

n, p: minority carrier concentrations,

D_n, D_n: minority carrier diffusion coefficient.

The first terms in Eqs. (D-22) and (D-23) are the drift components to the total current due to the drift field, E, whether externally applied or built-in. The second terms are the diffusion component contribution to total current.

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D.7 Reflectivity

In the multiple layer structures discussed in Section 6.0, the reflectivity is low at the interfaces and the absorption is strong enough within the layers such that multiple reflections are not present.

While reflectivity data between III-V binaries and ternaries is not generally available, there exists some data at vacuum-semiconductor interfaces. These data are shown in Tables D.1 through D.8. With the exception of AlAs and GaP, over the high solar photon flux region, the data show that the reflectance at a vacuum interface is typically 0.35 \pm 0.10. Therefore, the reflectance between most III-V binaries and ternaries is generally less than 0.05 in this region of the solar spectrum. Moreover because a cascade cell design dictates that direct transition materials be used, except for the window material, the absorption is typically very strong. As a result of low reflectivity and strong absorption, multiple reflections in the cascade structure is expected to be minimal.

D.8 Drift Field

Aiding drift fields for minority carriers in solar cells has been demonstrated to provide improvement in conversion efficiency. In this

ż (microns)	R	ک (microns)	R	2 (microns)	R
0.22	0.29	0.36	0.17	0.50	0.14
0.24	0.30	0.38	0.17	0.52	0.13
0.26	0.32	0.40	0.17	0.54	0.13
0.28	0.34	0.42	0.17	0.56	0.12
0.30	0.30	0.44	0.18	0.58	0.12
0.32	0.26	0.46	0.16		
0.34	0.22	0.48	0.15		

Table D.1. REFLECTANCE R OF ALUMINUM ANTIMONIDE AS A FUNCTION OF WAVELENGTH λ^{\bigstar}

*T. E. Fischer, Phys. Ref., <u>139</u>, A1228 (1965).

Table D.2. REFLECTANCE R OF ALUMINUM ANTIMONIDE AS A FUNCTION OF WAVELENGTH $\boldsymbol{\lambda}^{\boldsymbol{\star}}$

λ microns)	R	λ (microns)	R	ż (microns)	R
15.0	0.255	29.0	0.058	31.8	0.580
16.0	0.252	29.2	0.027	31.9	0.558
17.0	0.250	29.4	0.095	32.0	0.541
18.0	0.247	29.6	0.610	32.1	0.522
19.0	0.245	29.8	0.754	32.2	0.517
19.5	0.243	30.0	0.850	32.3	0.492
20.0	0.242	30.1	0.877	32.5	0.473
21.0	0.238	30.2	0.888	32.7	0.454
21.5	0.237	30.3	0.895	33.0	0.436
22.0	0.236	30.4	0.899	33.5	0.412
22.5	0.234	30.5	0.902	34.0	0.392
23.0	0.232	30.6	0.903	34.5	0.378
23.5	0.229	30.7	0.904	35.0	0.368
24.0	0.226	30.8	0.906	35.5	0.359
24.5	0.222	30.9	0.906	36.0	0.353
25.0	0.217	31.0	0.906	36.5	0.344
25.5	0.212	31.1	0.904	37.0	0.338
26.0	0.205	31.2	0.901	37.5	0.331
26.5	0.196	31.3	0.878	38.0	0.326
27.0	0.187	31.4	0.808	38.5	0.320
27.5	0.172	31.5	0.731	39.0	0.318
28.0	0.153	31.6	0.664	40.0	0.317
28.5	0.120	31.7	0.609		

*W.	J.	Turner	and	W.	Ε.	Reese,	Phys.	Rev.,	127,	126	(1962)	•
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λ (microns)	R	Reference	λ (microns	R)	Reference	λ (microns)	R	Reference
0.049	0.007	[1-4]	0.095	0.188	[1-4]	0.194	0.416	[1-4]
0.050	0.010	- -	0.103	0.216		0.207	0.469	1
0.052	0.013		0.113	0.240		0.229	0.580	1
0.054	0.019		0.124	0.273		0.234	0.583	
0.056	0.020		0.135	0.239		0.239	0.568	
0.059	0.019		0.139	0.246		0.264	0.463	
0.063	0.015		0.146	0.286		0.288	0.402	
0.065	0.025		0.157	0.385		0.295	0.398	
0.069	0.045		0.165	0.419		0.302	0.398	
0.073	0.077		0.177	0.455		0.310	0.408	
0.077	0.108	1	0.180	0.459		0.318	0.428	
0.083	0.134		0.188	0.422		0.330	0.480	
0.089	0,161	1	0.190	0.411	1	0.335	0.491	. +
0.344	0.468		19.44	0.195	[5]	27.14	0.924	[5]
0.354	0.435		20.00	0.188	1	27.19	0.903	1
0.375	0.384		20.43	0.183	1	27.26	0.875	
0.413	0.331		21.25	0.172		27.33	0.846	
0.459	0.302		22.34	0.144		27.40	0.806	
0.517	0.280		23.18	0.107		27.46	0.771	
0.620	0.263		23.87	0.069		27.54	0.736	
0.689	0.257		24.19	0.029		27.64	0.700	
0.885	0.251		24.66	0.016		27.76	0.669	
1.240	0.247		24.80	0.077		27.89	0.646	
1.377	0.246		24.86	0.269		28.02	0.627	
2.066	0.244		24.95	0.550		28.49	0.467	
3.099	0.244		25.00	0.669		29.16	0.421	
6.198	0.243	+	25.03	0.736		30.00	0.385	
13.17	0.228	[5]	25.03	0.824		31.30	0.352	
14.00	0.226		25.22	0.906		32.64	0.331	
14.88	0.222	1 1	25.26	0.925		33.95	0.321	
15.75	0.219		25.39	0.957		35.00	0.315	
16.00	0.220		25.79	0.966		35.44	0.313	
16.59	0.217		26.22	0.971		36.27	0.307	
17.40	0.210		26.56	0.973		37.39	0.302	
18.00	0.207		26.80	0.966		38.16	0.299	
18.55	0.202		27.05	0.956		38.95	0.299	÷

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REFLECTANCE R OF GALLIUM PHOSPHIDE Table D.3. AS A FUNCTION OF WAVELENGTH λ

[1] H. R. Philipp and H. Ehrenreich, Phys. Rev. Letters, 8, 92 (1962)

[2] H. R. Philipp and H. Ehrenreich, Phys. Rev., 129, 1550 (1963).

[3] H. Ehrenreich, H.R. Philipp and J.C. Phillips, Phys. Rev. Letters, 8, 59 (1962).

[4] H. R. Philipp and H. Ehrenreich, Chapter 4 of this volume.
[5] D. A. Kleinman and W. G. Spitzer, Phys. Rev., <u>118</u>, 110 (1960)

۱ (microns	R)	Reference	لا (microns	R .)	Reference	λ (microns)	R	Reference
0.049	0.006	[1-4]	0.590	0.350	[1-4]	31.91	0.186	[5]
0.051	0.010	- 1 -	0.653	0.335	- 1	32.08	0.180	
0.054	0.013		0.729	0.323		32.25	0.173	
0.056	0.014		0.827	0.314	1	32.43	0.164	
0.058	0.015		1.00	0.289	[5]	32.60	0.155	
0.059	0.015		2.00	0.289	191	32.78	0.144	
0.062	0.011		3.00	0.289	(32.96	0.132	
0.065	0.014		4.00	0.289		33.14	0.117	
0.068	0.020		5.00	0.289		33.33	0.100	
0.073	0.032		6.00	0.288		33.52	0.080	
0.077	0.053		7.00	0.288		33.70	0.059	
0.083	0.077		8.00	0.287		33.89	0.046	
0.089	0.104		9.00	0.288		34.09	0.080	
0.096	0.131		10.00	0.287		34.28	0.255	
0.103	0.151	1	11.00	0.287		34.48	0.473	
0.115	0.175		12.00	0.286	1.1.1	34.68	0.617	
0.124	0.208		13.00	0.266		34.88	0.704	
0.138	0.265		14.00	0.285		35.08	0.756	
0.155	0.365		15.00	0.284		35.29	0.788	
0.177	0.443		15.78	0.283	1	35.50	0.806	
0.188	0.460		16.66	0.283		35.71	0.812	
0.197	0.419		17.64	0.282		35.92	0.804	
0.200	0.418		18.75	0.280		36.14	0.769	
0.207	0.438		20.00	0.278		36.36	0.699	
0.225	0.510		21.42	0.276		36.58	0.628	
0.248	0.605		23.07	0.272		36.81	0.576	. 1
0.248	0.598		25.00	0.266	1.1	37.03	0.539	
0.233	0.494		27.27	0.256		37.26	0.510	
0.318	0.404		30.00	0.230		37.50	0.487	
0.326	0.404		30.15	0.228		37.73	0.469	
0.344	0.402		30.30	0.225	1 1	37.97	0.454	
0.365	0.400		30.45	0.223		38.21	0.442	
0.305	0.466		30.61	0.220		38.46	0.431	1
0.400	0.465		30.76	0.217		38.71	0.422	
0.409	0.468		30.92	0.214		38.96	0.414	
0.419	0.484		31.08	0.210		39.21	0.407	7
0.423	0.461		31.25	0.206		39.47	0.401	
0.459	0.436		31.41	0.202		39.73	0.395	5
0.496	0.402		31.57	0.197		40.00	0.390)
0.498	0.373	+	31.74	0.192	+			+

Table D.4. REFLECTANCE ${\it R}$ OF GALLIUM ARSENIDE AS A FUNCTION OF WAVELENGTH λ

[1] H. R. Philipp and H. Ehrenreich, Phys. Rev. Letters, 8, 92 (1962).

[2] H. R. Philipp and H. Ehrenreich, Phys. Rev., <u>129</u>, 1550 (1963).

[3] H. Ehrenreich, H.R. Philipp & J.C. Phillips, Phys. Rev. Letters, 8, 59 (1962).

[4] H. R. Philipp and H. Ehrenreich, Chapter 4, Semiconductors and Semimetals:

edited by R.K. Willardson and A.C. Beer, Vol. 3, Academic Press, New York. [5] B.Piriou and F. Cabannes, Compt. Rend., 255, 2932 (1962).

λ (microns)	R	λ (microns)	R	λ R (microns)		
0.245	0.385	0.351	0.434	0.64	0.454	
0.246	0.386	0.360	0.422	0.65	0.456	
0.249	0.393	0.365	0.418	0.66	0.453	
0.252	0.409	0.370	0.414	0.68	0.438	
0.256	0.419	0.380	0.406	0.70	0.432	
0.260	0.430	0.390	0.402	0.75	0.419	
0.265	0.451	0.400	0.400	0.80	0.410	
0.269	0.473	0.409	0.400	0.85	0.399	
0.272	0.500	0.415	0.406	0.90	0.391	
0.276	0.511	0.420	0.405	0.95	0.380	
0.280	0.521	0.423	0.403	1.00	0.370	
0.282	0.526	0.427	0.409	1.06	0.358	
0.285	0.535	0.430	0.413	1.09	0.351	
0.288	0.540	0.440	0.411	1.20	0.346	
0.291	0.536	0.450	0.420	1.26	0.346	
0.295	0.532	0.460	0.425	1.30	0.343	
0.300	0.522	0.470	0.430	1.40	0.340	
0.302	0.520	0.480	0.434	1.55	0.340	
0.303	0.513	0.490	0.439	1.60	0.339	
0.308	0 503	0.500	0.435	1.68	0.338	
0.309	0.497	0.520	0.435	1.80	0.335	
0.311	0.490	0.540	0.434	1.86	0.334	
0.315	0.486	0.560	0.436	2.00	0.333	
0.320	0.475	0.58	0.442	2.15	0.330	
0.327	0.463	0.60	0.448	2.38	0.329	
0.333	0.452	0.62	0.454	A REAL PROPERTY.		
0.340	0.448	0.63	0.453			

Table D.5. REFLECTANCE R OF GALLIUM ANTIMONIDE AS A FUNCTION OF WAVELENGTH λ^{\bigstar}

*M. Cardona, Z. Physik, <u>161</u>, 99 (1960).

λ (microns)	R	λ (microns)	R	ک (microns)	R
0.059	0.091	0.133	0.316	0.194	0.417
0.060	0.087	0.135	0.320	0.197	0.410
0.062	0.083	0.136	0.325	0.200	0.408
0.064	0.080	0.138	0.330	0.203	0.415
0.065	0.075	0.139	0.336	0.207	0.429
0.067	0.072	0.141	0.343	0.210	0.442
0.069	0.069	0.144	0.359	0.214	0.452
0.071	0.068	0.146	0.366	0.217	0.465
0.075	0.075	0.148	0.370	0.221	0.477
0.077	0.094	0.149	0.376	0.225	0.490
0.079	0.111	0.151	0.380	0.229	0.504
0.083	0.132	0.153	0.385	0.234	0.517
0.085	0.162	0.155	0.390	0.238	0.528
0.089	0.178	0.157	0.395	0.243	0.544
0.093	0.194	0.159	0.407	0.248	0.553
0.095	0.205	0.161	0.409	0.253	0.538
0.099	0.210	0.163	0.414	0.258	0.524
0.103	0.218	0.165	0.419	0.264	0.491
0.108	0.232	0.167	0.423	0.269	0.450
0.113	0.246	0.170	0.428	0.275	0.404
0.118	0.266	0.172	0.430	0.282	0.380
0.124	0.298	0.175	9.432	0.288	0.364
0.125	0.300	0.177	0.433	0.295	0.352
0.126	0.301	0.180	0.432	0.302	0.343
0.128	0.303	0.182	0.431	0.310	0.339
0.129	0.305	0.185	0.429	0.318	0.336
0.130	0.309	0,188	0.427	0.326	0.338
0.132	0.311	0.191	0.422	0.335	0.343
0.344	0.351	0.477	0.336	0.729	0.290
0.354	0.361	0.496	0.329	0.775	0.286
0.375	0.406	0.517	0.322	0.826	0.285
0.387	0.424	0.539	0.316	0.885	0.282
0.399	0.416	0.563	0.310	0.953	0.273
0.413	0.394	0.590	0.307	1.033	0.269
0.427	0.375	0.620	0.304	1.126	0.265
0.443	0.356	0.652	0.301	1.240	0.263
0.459	0.346	0.689	0.295		

Table D.6. REFLECTANCE R OF INDIUM PHOSPHIDE AS A FUNCTION OF WAVELENGTH λ^*

λ (microns)	R	λ (microns)	R	λ R (microns)		
0.049	0.010	0.153	0.384	0.443	0.435	
0.052	0.012	0.172	0.432	0.451	0.437	
0.054	0.013	0.180	0.435	0.459	0.435	
0.056	0.014	0.188	0.421	0.468	0.430	
0.059	0.015	0.195	0.433	0.477	0.433	
0.062	0.015	0.211	0.395	0.496	0.443	
0.064	0.014	0.225	0.435	0.517	0.430	
0.067	0.013	0.248	0.501	0.563	0.396	
0.070	0.009	0.259	0.550	0.620	0.373	
0.077	0.020	0.264	0.559	0.689	0.355	
0.082	0.034	0.269	0.550	0.775	0.341	
0.089	0.060	0.282	0.502	0.885	0.330	
0.095	0.108	0.310	0.391	1.033	0.321	
0.103	0.166	0.335	0.354	1.240	0.314	
0.108	0.200	0.344	0.349	1.377	0.311	
0.112	0.219	0.354	0.350	2.066	0.305	
0.123	0.260	0.387	0.360	3.099	0.302	
0.136	0.310	0.413	0.393	6.198	0.300	

Table D.7. REFLECTANCE R OF INDIUM ARSENIDE AS A FUNCTION OF WAVELENGTH λ^*

- H. R. Philipp and H. Ehrenreich, Phys. Rev. Letters, 8, 92 (1962).
 H. R. Philipp and H. Ehrenreich, Phys. Rev., <u>129</u>, 1550 (1963).

- [3] H. Ehrenreich, H. R. Philipp, and J. C. Phillips, Phys. Rev. Letters, 8, 59 (1962).
- [4] H. R. Philipp and H. Ehrenreich, Chapter 4, Semiconductors and Semimetals: Ed. R. K. Willardson and A. C. Beer, Vol. 3, Academic Press, New York.

ر (microns	R .)	Reference	ک (microns)	R	Reference	ک (microns)	R	Reference
0.049	0.010	[1]	0.238	0.442	[1]	1.24	0.376	[1]
0.052	0.012	1	0.243	0.436		1.55	0.369	
0.054	0.013	1	0.248	0.441		2.07	0.364	1
0.056	0.014		0.282	0.530		20.0	0.35	[2]
0.059	0.016		0.302	0.579		25.0	0.34	
0.062	0.016		0.310	0.570		30.0	0.31	
0.065	0.015		0.344	0.465		35.0	0.29	
0.069	0.012	-	0.365	0.438		40.0	0.25	
0.073	0.009		0.413	0.398		45.0	0.21	+
0.080	0.007		0.428	0.400		50.0	0.19	[3]
0.083	0.009		0.443	0.405	* N	50.3	0.18	1
0.089	0.023	1	0.477	0.425	1	50.5	0.17	1
0.095	0.053		0.517	0.460		50.8	0.15	
0.103	0.100		0.539	0.458		51.0	0.14	
0.113	0.160		0.564	0.454		51.3	0.12	
0.124	0.222		0.590	0.448		51.5	0.13	
0.138	0.274		0.620	0.453		51.8	0.17	
0.155	0.332		0.656	0.479	3.60	52.1	0.27	
0.163	0.348		0.677	0.488		52.4	0.42	
0.182	0.380	1 1	0.689	0.480		52.6	0.59	1.1.1
0.207	0.430		0.708	0.466		52.9	0.70	
0.218	0.424		0.775	0.430		53.2	0.76	
0.221	0.429		0.886	0.400		53.5	0.79	
0.234	0.442	+	1.03	0.385	1	53.8	0.81	1

Table D.8. REFLECTANCE R OF INDIUM ANTIMONIDE AS A FUNCTION OF WAVELENGTH λ

H. R. Philipp and H. Ehrenreich, Phys. Rev., <u>129</u>, 1550 (1963).
 H. Yoshiriago and R. A. Oetjen, Phys. Rev., <u>101</u>, 526 (1956).
 R. B. Sanderson, J. Phys. Chem. Solids, <u>26</u>, 803 (1965).

study, drift fields are one of the major parameters studied to determine their effect on efficiency and other solar cell terminal properties. The integral-differential continuity equation has been derived and general solutions obtained with constant or average drift field. No attempt has been made to obtain a general solution with variable drift field. This decision has been reached because when the drift field exceeds 1500 V/cm in optimally designed cells, the improvement in efficiency is within 10% of the saturation level attained at 3000 V/cm in surface layers where surface recombination is high. Therefore, the most interesting cases for those solar cells with optimally designed structures and with drift fields in the range 1500 to 3000 V/cm.

In a practical endeavor to correlate device experimental results with theory, the use of an average, constant built-in field in micrometer thick layers is consistent with the other approximations, typically used in semiconductor analysis, for impurity concentration, minority carrier lifetime, mobility and mobility scattering processes, absorption coefficient, and the interpolation of the absorption coefficient for ternary alloys from the terminal binaries.

Exceeding 3000 V/cm, the critical field value, in many III-V compounds, results in a decrease in carrier velocity and a decrease in efficiency. Therefore, exceeding the critical field value is not of interest for solar cells.

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APPENDIX E. LAMBERT'S ABSORPTION LAW FOR POSITION-DEPENDENT ABSORPTION COEFFICIENT

The absorption law for position-independent absorption coefficient is well known and given by

$$N(x) = N_0 e^{-\alpha x}$$
(E-1)

where the incident flux is N_0 at x=0. In graded bandgap materials the absorption coefficient is position-dependent for a given wavelength. This absorption law expression is derived below.

Consider monochromatic parallel beam of light characterized by wavelength, λ , propogating in the x-direction and incident on an absorbing material whose plane is perpendicular to the beam. The material is assumed to be uniform in composition and properties in the y-z directions and is assumed to absorb, but not to scatter, light. In Figure E.1, N is denoted as the incident flux at x in units of cm⁻² sec⁻¹ (µm)⁻¹. The absorbed flux is proportional to the product

$$dN = -\alpha(x)Ndx$$
 (E-2)

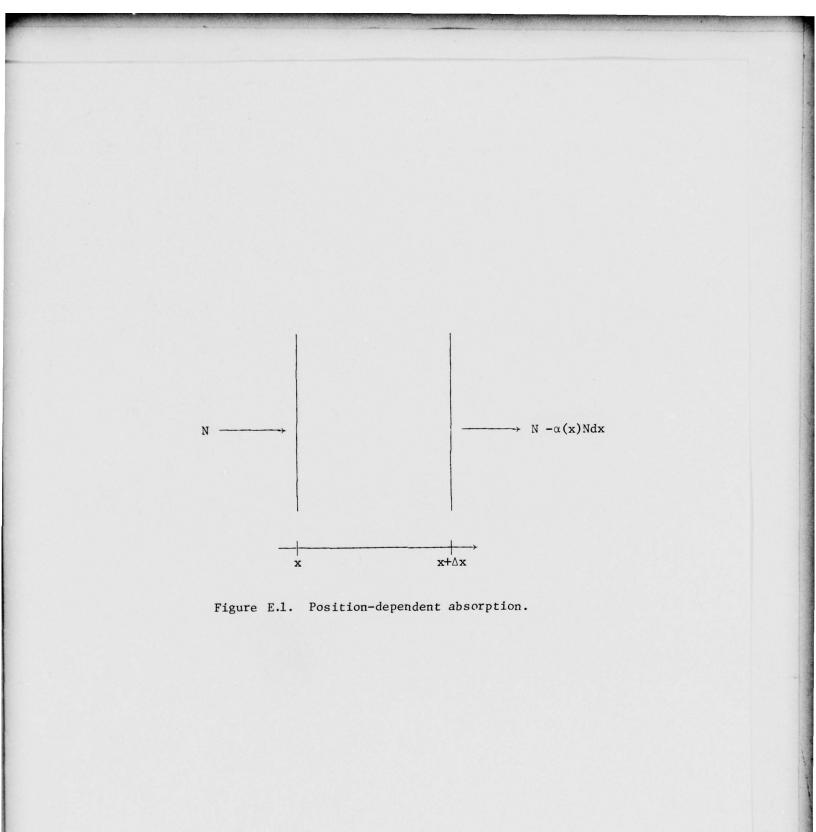
so that the exiting flux is

$$N-\alpha(x)Ndx.$$
 (E-3)

From Eq. (E-2) we obtain the absorption law, after integrating, giving

$$N = N_{O}e^{-\int_{0}^{X} \alpha(x) dx}, \qquad (E-4)$$

for position-dependent absorption coefficient. By setting α independent of x, Eq. (E-1) is recovered.



APPENDIX F. "POTENTIAL WELL" ANALYSIS

In this appendix an analytical solution is obtained for the PW cell. The method employed in the analysis is to establish an integral form of the steady-state continuity equation (See Section 4.0) for excess minority carriers in each of the four regions. A general solution to each of the continuity equations is obtained and the boundary conditions imposed. The approximations employed were discussed in APPENDIX D. The current relationship is then used to calculate cell performance.

The model used in the analysis is shown in Figure 5.1 and described in Section 5.0. The electron current at the p-n junction, arising from Regions 1 and 2, is simultaneously dependent on the constants of integration of the solutions in Regions 1 and 2. Similarly, the hole current is simultaneously dependent on the constants of integration of the solutions in Regions 3 and 4. Therefore, the solutions to Regions 1 and 2 are discussed together and similarly for Regions 3 and 4.

The assumptions made in the solution of the excess minority carrier concentrations are as follows:

1. Each interface bounding a subregion, including the p-n junction, is treated as a line boundary whose thickness is small compared to the subregion width and where the associated boundary condition(s) are considered as a property of the interface [5-7, 5-27].

2. Shockley's diffusion mechanism is the dominant p-n junction carrier transport and space charge recombination is small. This is a good approximation in the PW cell because of the relatively low doping in each of the GaAs subregions which form the p-n homojunction [5-40, 5-41].

3. For the one solar constant perturbation, the excited excess electron and hole concentrations are small compared to the majority carrier concentrations

in their respective regions. Therefore, the recombination rate is assumed linearly proportional to the excess carrier concentration in each subregion [5-40].

4. Each photon of the solar spectrum may not excite more than one hole-electron pair.

5. The ternary alloy composition grading is such that the AlGaAs layers establish a constant built-in field.

6. In the graded layers the bandgap grading is manifested through a slope of the minority carrier band edge. This arises because the majority carrier band edge position is dictated by the energy difference from the equilibrium Fermi level.

7. Uniform doping is assumed in each subregion.

 The absorption coefficient in the graded layers is position dependent.

9. Minority carrier lifetime in AlGaAs is assumed to be the same as in GaAs for the same doping level [5-30].

10. A reflectivity of 5% is taken over the entire solar spectrum of interest.

11. The photovoltage generated across the graded layers and barriers are assumed small compared to that generated at the p-n junction and, therefore, neglected [5-28, 5-29].

12. Recombination at the AlGaAs-GaAs interfaces are assumed small [5-38].

13. The effective masses, hole and effective electron mobilities, density of states and absorption coefficient for AlGaAs are calculated by interpolation between the values of GaAs and AlAs.

14. An average mobility is assumed in the graded layers.

15. The temperature effects in mobility, bandgap, and in the intrinsic concentration have been taken into consideration in the temperature behavior. However, the increase in lifetime with increasing temperature has been neglected, and the ambient temperature value used for all temperatures. Carrier mobility is assumed to be dominated by ionized impurity scattering and by polar optical photon scattering.

In the one-dimensional model used, the value of x increases from the surface into the cell. The general case is solved for which the conduction band discontinuity, ΔE_{c1} , and valence band discontinuities, Δ_{v3} and ΔE_{v4} , are present as parameters in the solar cell V-I expression. The interface boundary lines are denoted x_1 , x_2 , x_3 , and x_4 . REGIONS 1 and 2: Electrons in the p-p regions

The inhomogeneous integral form of the steady-state continuity equation in the Al Ga As graded bandgap layer is given by

$$0 = g_1 + D_{n1} \frac{d^2 n_1}{dx^2} + \mu_{n1} E_{10} \frac{dn_1}{dx} - \frac{n_1}{\tau_{n1}} , \qquad (F-1)$$

where the generation term is

$$g_{1} = \int_{0}^{\lambda_{c1}} \alpha_{1} [1-R] N_{0} e^{-\int_{0}^{X} \alpha_{1} dx'} d\lambda . \qquad (F-2)$$

The symbols are defined in the List of Symbols. The electric field, E_{10} , is constant and is established by an appropriate compositional grading. This results in a nearly linearly decreasing composition in this region. The field is given by

$$E_{10} = -\frac{E_{G0} - E_{G1} - \Delta E_{c1}}{x_1}$$
(F-3)

where E_{G0} and E_{G1} are the bandgap values at the surface and in Region 2, respectively. The value of E_{G0} used in the analysis is 1.739, which gives a value for x of 0.258. In the range of u from zero to 0.3 the electron mobility [5-41], diffusion coefficient, diffusion length [5-43] and lifetime [5-44] are not strong functions of the Al mole fraction. For our considerations here the electron effective mobility is calculated as a function of Al mole fraction in the graded larger and an average value taken for μ_{n1} and D_{n1} in Eq. (F-1). The value of τ_{n1} is taken from GaAs data at the same doping concentration. The value for α_1 in this region is interpolated between the GaAs and AlAs absorption curves, and the reflectance is taken to be 0.05 over the spectrum of interest.

The general solution to Eq. (1) is represented by

$$n_{1}(x) = c_{11}e^{\omega_{11}x} + x_{12}e^{\omega_{12}x} + \frac{1}{\omega_{12}-\omega_{11}} [G_{11}(x)e^{\omega_{11}x} + G_{12}(x)e^{\omega_{12}x}]$$
(F-4)

where $c_{11}^{}$ and $c_{12}^{}$ are constants of integration and where we define

$$G_{11}(x) = \frac{1}{D_{n1}} \int_{0}^{\lambda} c1 \int_{0}^{x} \alpha_{1} N_{01}(x') e^{-\omega_{11}x'} dx' d\lambda, \qquad (F-5)$$

$$G_{12}(\mathbf{x}) = -\frac{1}{D_{n1}} \int_{0}^{\lambda} c_{1} \int_{0}^{\mathbf{x}} \alpha_{1} N_{01}(\mathbf{x'}) e^{-\omega_{12} \mathbf{x'}} d\mathbf{x'} d, \qquad (F-6)$$

$$\omega_{11}, \ \omega_{12} = -\frac{\mu_{n1}E_{10}}{2D_{n1}} \pm \sqrt{\left(\frac{\mu_{n1}E_{10}}{2D_{n1}}\right)^2 + L_{n1}^{-2}}, \tag{F-7}$$

$$N_{01}(x) = (1-R)N_{0}e^{-\int_{0}^{x} \alpha_{1}dx'}.$$
 (F-8)

In Eq. (F-4) the first and second terms represent the homogeneous solution while the third represents the nonhomogeneous solution. The integration over x in G_{11} and G_{12} is a consequence of the position sensitive absorption coefficient due to the bandgap grading. Lambert's absorption law is also modified, as shown in Eq. (F-8), because the absorption is position sensitive and is represented by the integration of α_1 over x. The value of E_{G1} is given by

$$E_{G1} = E_{G2} + \Delta E_{c1}$$
 (F-9)

where

$$\lambda_{c1} = \frac{1.2398}{E_{G1}}$$
(F-10)

and E_{G2} is the GaAs bandgap value.

Both the homogeneous and nonhomogeneous solutions are functions of E_{10} and ΔE_{c1} . By setting E_{10} and ΔE_{c1} to zero the general solution for constant bandgap, the zero field case may be recovered.

The integral form of the continuity equation in Region 2 is

$$0 = g_2 + D_{n2} \frac{d^2 n_2}{dx^2} - \frac{n_2}{\tau_{n2}}$$
(F-11)

where the generation term is given by

$$g_{2} = \int_{0}^{\lambda} c^{2} \alpha_{2} N_{01}(x_{1}) e^{-\alpha_{2}(x-x_{1})} d\lambda.$$
 (F-12)

This continuity equation is similar to that of Region 1 except that it is applicable to the region bounded by x_1 and x_2 , a field is not present, the material constants apply to GaAs of constant bandgap, α_2 is independent of position and the usual form of Lambert's absorption law applies.

The incident flux, $N_{01}(x_1)$, on Region 2 is dimished by the flux absorbed in Region 1 and given by

$$N_{01}(x_1) = (1-R)N_0 e^{-f_0^{X_1} \alpha_1 dx} .$$
 (F-13)

The general solution to Eq. (F-11) is

$$n_2(x) = C_{21} \cosh \frac{x - x_1}{L_{n2}} + C_{22} \sinh \frac{x - x_1}{L_{n2}} - C_{02}(x)$$
 (F-14)

where

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$$C_{02}(\mathbf{x}) = \int_0^{\lambda_{c2}} C_{23} e^{-\alpha_2 (\mathbf{x} - \mathbf{x}_1)} d\lambda$$
 (F-15)

and

$$C_{23} = \frac{\alpha_2^2 L_{n2}^2 N_{01}(x_1)}{D_{n2}(\alpha_2^2 L_{n2}^2 - 1)} \quad . \tag{F-16}$$

The cut-off wavelength, λ_{c2} , is that of GaAs. The homogeneous solution is represented by the first and second term in Eq. (F-14) while the non-homogeneous solution is the third term.

In Regions 1 and 2 there are four boundary conditions that enable us to solve for the four constants of integration, C_{11} , C_{12} , C_{21} , and C_{22} . Due to the nature of the boundary conditions they are inter-related.

The boundary condition at x = 0 describes the electron current arising from surface recombination. Its direction is in the postive x direction. It is represented by the relationship

$$D_{n1} \frac{dn_1}{dx} \bigg|_{0} + n_1(0)\mu_{n1}E_{10} = Sn_1(0)$$
 (F-17)

where the surface recombination velocity, S, is taken to be a positive quantity. The numerical value of E_{10} , for an aiding field, is negative

and represents the electron drift component whose direction opposes that of surface recombination current. For a nonvanishing value of S, the electron concentration gradient within several hundred angstroms of the surface is positive and represents the diffusion component of electron current into surface recombination states. When the built-in field, E_{10} , is sufficiently negative it reduces the surface recombination current to negligible values. Moreover, for indirect transition materials, $n_1(0)$ is smaller than for direct transition materials which also serves to reduce surface recombination current. From a substitution of the Einstein relationship

$$D = \frac{kT}{q} \mu, \qquad (F-18)$$

into Eq. (F-17), it is observed that surface recombination current increases with increasing temperature. Phenomenologically this results because minority carrier diffusion increases with increasing temperature. In order for surface recombination current to vanish the relationship

$$E_{10} = -\frac{kT}{q} \frac{1}{n_1(0)} \frac{dn_1}{dx} \Big|_{0}$$
(F-19)

must be satisfied. The value of n_1 required to satisfy Eq. (F-19) is 13% higher than $n_1(0)$ in a recombination layer thickness of 10^{-6} cm.

The second boundary condition to be satisfied is that the excess electron concentration at x_1 is described by Maxwell-Boltzmann statistics given by

$$n_1(x_1) = n_2(x_1)e^{-\Delta E_{c1}/kT}$$
 (F-20)

This relationship assumes non-degenerate materials and that the metallurgical heterojunction is very narrow compared to the thickness of either Region 1 or 2. The barrier energy, ΔE_{cl} , is assumed to be a positive quantity as shown in Figure 5.1. In the case of a vanishing barrier then, of course, the continuity of charge is evident.

In the absence of heterojunction recombination, the electron current is continuous across the boundary at x_1 . This gives the third boundary condition and is represented by

$$D_{n1} \frac{dn_1}{dx} \bigg|_{x_1} + n_1(x_1) n_1 E_{10} = D_{n2} \frac{dn_2}{dx} \bigg|_{x_1} .$$
 (F-21)

Heterojunction recombination is not considered here because it has been shown to be small at the Al_xGa_{1-x}As-GaAs interface [5-38]. This result is not surprising considering the small mismatch in lattice constant for Al_xGa_{1-x}As over a wide range of alloys compared to the GaAs lattice constant.

The fourth boundary condition relates to the non-equilibrium concentration at x_2 . This boundary condition results in the only term that does not involve an integration over wavelength. In GaAs homojunctions the competing junction transport mechanisms are thermal diffusion and space charge recombination. Imposing thermal diffusion at x_2 , the boundary condition becomes

$$n_2(x_2) = n_{2po} \ (e^{qV/kT} - 1)$$
 (F-22)

where n_{2po} is the equilibrium electron concentration. In the junction current equation we will show that the junction current which results is Shockley's ideal diffusion mechanism multiplied by a coefficient that describes charge confinement.

Having solved for the four constants of integration, the electron contribution to the terminal current may be obtained from

$$J_{n2} = qD_{n2} \left. \frac{dn_2}{dx} \right|_{x}$$
(F-23)

resulting in

$$J_{n2} = -J_{scn1} - J_{scn2} + J_{Jn2}$$
, (F-24)

where J_{scn1} and J_{scn2} are the contributions to the short-circuit current from Regions 1 and 2, respectively, and J_{Jn2} is the contribution to dark current from electron injection across the p-n junction into Region 2. The quantities J_{scn1} , J_{scn2} and J_{Jn2} are positive quantities for all values of material and structural parameters. The presence of the negative signs indicates that the current component is in a direction opposite to the positive x-direction. The current components in Eq. (F-24) are represented by:

$$J_{scn1} = q \frac{N_{12}}{F_{12}} v_{21} \left(1 - \frac{1}{R_n} \tanh \frac{x_2 - x_1}{Ln_2} \right) \frac{e^{(\omega_{11} + \omega_{12})x_1}}{I_{01}} \int_0^\lambda c_1 \int_0^x 1_{\alpha N_{01}} (e^{-\omega_{11}x} - v_{s1} e^{-\omega_{12}x}) dx d\lambda$$
(F-25)

$$J_{scn2} = q \int_{0}^{\lambda} c_{1} \alpha_{2} D_{n2} C_{23} \left[\left(R_{n} cosh \frac{x_{2} - x_{1}}{L_{n2}} - sinh \frac{x_{2} - x_{1}}{L_{n2}} \right) \left(\frac{v_{21}}{v_{\omega 1} e^{-\Delta E_{c1}/kT}} + \frac{1}{\alpha_{2} L_{n2}} \right) - \left(1 + \frac{R_{n}}{\alpha_{2} L_{n2}} \right) e^{-\alpha_{2} (x_{2} - x_{1})} \right] d\lambda$$
(F-26)

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$$J_{Jn2} = q \frac{D_{n2}}{L_{n2}} n_{2po} (e^{qV_2/kT} - 1)R_n$$
 (F-27)

where

$$R_{n} = \frac{N_{12}}{F_{12}} \frac{v_{\omega 1}e}{\cosh \frac{x_{2}^{-x_{1}}}{L_{n2}}},$$
 (F-28)

$$N_{12} = \frac{\frac{\cosh \frac{x_2^{-x_1}}{L_{n2}}}{\sum_{i=1}^{n} \frac{x_2^{-x_1}}{1} \left[v_{21} + v_{\omega 1} e^{-\Delta E_{c1}/kT} \frac{x_2^{-x_1}}{\cos h \frac{L_{n2}}{L_{n2}}} \right], \quad (F-29)$$

$$v_{21} + v_{\omega 1} e^{-\Delta E} c1^{/kT} tanh \frac{x_2 - x_1}{L_{n2}}, \qquad (F-30)$$

$$I_{01} = e^{\omega_{12}x_{1}} - v_{s1}e^{\omega_{11}x_{1}}, \qquad (F-31)$$

$$\mathbf{v}_{1} = \frac{D_{n1}\omega_{12}^{+\mu}n_{1}^{E}10}{D_{n1}\omega_{11}^{+\mu}n_{1}^{E}10} , \qquad (F-32)$$

$$\mathbf{v_{s1}} = \frac{D_{n1}^{\omega} 12^{+\mu} n1^{E} 10^{-S}}{D_{n1}^{\omega} 11^{+\mu} n1^{E} 10^{-S}},$$
 (F-33)

$$\mathbf{v}_{21} = \frac{\frac{D_{n2}/L_{n2}}{D_{n1}\omega_{11}^{+\mu}n_{1}^{E} 10},$$
 (F-34)

$$\mathbf{v}_{\omega 1} = \frac{\mathbf{v}_{1} e^{\omega_{12} \mathbf{x}_{1}} - \mathbf{v}_{s1} e^{\omega_{11} \mathbf{x}_{1}}}{\mathbf{I}_{01}} , \qquad (F-35)$$

$$n_{2po} = \left(\frac{n_{i}^{2}}{N_{A2}}\right)_{GaAs} \qquad (F-36)$$

We observe that the short-circuit contribution from Region 1, J_{scn1} , is characterized by an integration over x. This arises because of the bandgap grading and the position dependent absorption coefficient. An integration over x is not required for J_{scn2} since Region 2 possesses a constant bandgap material and a position-independent absorption coefficient.

The form of the dark current, Eq. (F-27), is illuminating in that it predicts a higher or lower dark current represented by the more common expression of the diode equation

$$J = q \frac{D_{n2}}{L_{n2}} n_{2po} (e^{qV_2/kT} - 1).$$
 (F-37)

The multiplicative factor, R_n , in Eq. (F-27) predicts charge confinement in Region 1 and recombination of electrons in Region 1 and 2. In the absence of surface recombination, R_n asymptotically approaches unity for increasing $(x_2-x_1)/L_{n2}>1$. For decreasing values of $(x_2-x_1)/L_{n2}$ and $\Delta E_{c1}>kT$ charge confinement occurs. R_n is more sensitive to ΔE_{c1} than it is to E_{10} . We conclude that the barrier ΔE_{c1} is more effective in confining electrons to Region 2 when $\Delta E_{c1}>kT$.

In direct transition materials $(x_2-x_1)/L_{n2}$ may be made to take on values between 10^{-2} to 10^{-1} in order to affect a reduction in dark current without suffering incomplete absorption loss. This is particularly true in the PW solar cell where the p-type GaAs in lightly doped and for which mobility and lifetime attain their highest values. Moreover, the additional capability of fabricating a conduction band discontinuity $\Delta E_{c1}^{>>kT}$ results in a more effective barrier in confining electrons to Region 2.

With increasing surface recombination velocity, R_n may attain values greater than unity which indicates increased recombination. This gives a dark current higher than predicted by Eq. (F-37).

REGIONS 3 and 4: Holes in the n-n Regions

The solutions for Regions 3 and 4 are similar to those obtained in Regions 2 and 1, respectively. We briefly outline the analysis below.

The nonhomogeneous continuity equation, generation term, entering flux, general solution, and defined functions are:

$$0 = g_3 + D_{p3} \frac{d^2 p_3}{dx^2} - \frac{p_3}{D_{p3}} , \qquad (F-38)$$

$$g_{3} = \int_{0}^{\lambda_{c2}} \alpha_{2} N_{02}(x_{2}) e^{-\alpha_{3}(x-x_{2})} d\lambda , \qquad (F-39)$$

$$N_{02}(x_2) = N_{01}(x_1)e^{-\alpha_2(x_2^{-x_1})}$$
, (F-40)

$$P_3(x) = C_{31} \cosh \frac{x-x_2}{L_{p3}} + C_{32} \sinh \frac{x-x_2}{L_{p3}} - C_{03}(x)$$
, (F-41)

$$c_{03}(x) = \int_0^{\lambda} c^2 c_{33} e^{-\alpha_3 (x-x_2)} d\lambda$$
, (F-42)

$$C_{33} = \frac{\alpha_{3}L_{p}^{2}N_{02}(x_{2})}{D_{p3}(\alpha_{3}^{2}L_{p3}^{2}-1)}, \qquad (F-43)$$

The cut-off frequency, $\lambda_{\rm c2}^{},$ corresponds to the GaAs bandgap energy.

The set of equations for Region 4 are summarized below:

$$0 = g_4 + D_{p4} \frac{d^2 p_4}{dx^2} - \mu_{p4} E_{40} \frac{d_{p4}}{dx} - \frac{p_4}{\tau_{p4}} , \qquad (F-44)$$

$$g_{4} = \int_{0}^{\lambda_{c3}} \alpha_{4} N_{03}(x_{3}) e^{-\int_{x_{3}}^{x_{\alpha}} 4dx'}, \qquad (F-45)$$

$$N_{03}(x_3) = N_{02}(x_2)e^{-\alpha_3(x_3-x_2)}$$
, (F-46)

$$P_4(x) = C_{41}e^{\omega_{41}(x-x_3)} + C_{42}e^{\omega_{42}(x-x_3)} + C_{42}e$$

$$+\frac{1}{\omega_{42}-\omega_{41}}\left[G_{41}(x)e^{\omega_{41}(x-x_3)}+G_{42}(x)e^{\omega_{42}(x-x_3)}\right], \quad (F-47)$$

$$G_{41} = \frac{1}{D_{p4}} \int_{0}^{\lambda} c^{3} \int_{x_{3}}^{x} \alpha_{4} N_{04}(x') e^{-\omega_{41}(x'-x_{3})} dx' d\lambda , \qquad (F-48)$$

$$G_{42}(x) = -\frac{1}{D_{p4}} \int_{0}^{\lambda} c^{3} \int_{x_{3}}^{x} \alpha_{4} N_{04}(x') e^{-\omega_{42}(x'-x_{3})} dx' d\lambda , \qquad (F-49)$$

$$\omega_{41}, \omega_{42} = \frac{\mu_{p4}E_{40}}{2D_{p4}} \pm \sqrt{\frac{\mu_{p4}E_{40}}{2D_{p4}} + L_{p4}^{-2}} , \qquad (F-50)$$

$$N_{04}(x) = N_{03}(x_3)e^{-\int_{x_3}^{x} \alpha_4 dx'}, \qquad (F-51)$$

$$E_{G3} = E_{G2} + \Delta E_{v3}$$
, (F-52)

$$E_{40} = -\frac{E_{G4}^{-E}G2^{-\Delta E}v3}{x_4^{-x_3}}, \qquad (F-53)$$

$$\lambda_{c3} = \frac{1.2398}{E_{G3}} . \tag{F-54}$$

The cut-off frequency λ_{c3} is represented by the bandgap of the Al_xGa_{1-x}As at x₃.

Again, there are imposed four boundary conditions on the two general solutions from which we determine the four constants of integration. The boundary conditions are:

$$p_3(x_2) = p_{3n0}(e^{-1}),$$
 (F-55)

$$p_3(x_3) = p_4(x_3)e^{\Delta E_{v3}/kT}$$
, (F-56)

$$\left. {}^{D}_{p3} \frac{dp_{3}}{dx} \right|_{x_{3}} = \left. {}^{D}_{p4} \frac{dp_{4}}{dx} \right|_{x_{3}} - p_{4}(x_{3}) \mu_{p4} E_{40},$$
 (F-57)

$$P_4(x_4) = P_{5n0}e^{\Delta E_{v4}/kT}$$
 (F-58)
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The current is determined at x_2 from the relationship

$$J_{p2} = -qD_{p3} \frac{dp_3}{dx} \Big|_{x_2}$$
 (F-59)

resulting in an equation similar in form to Eq. (F-24) and given by

$$J_{p2} = -J_{scp3} - J_{scp4} + J_{Jp2}$$
 (F-60)

The components J_{scp3} and J_{scp4} are contributions to short-circuit current from Regions 3 and 4, respectively, and J_{Jp2} is the contribution to dark current from hole injection across the p-n junction into Region 3. The presence of the minus sign indicates current direction is in the negative x-direction while the plus sign indicates current direction in the positive x-direction.

The expressions for the current components of Eq. (F-60) are represented by:

$$J_{scp3} = q \int_{0}^{\lambda} c^{2} \alpha_{3} D_{p3} C_{33} \left\{ 1 - \frac{R_{p}}{\alpha_{3} L_{p3}} - \left[\cosh \frac{x_{3} - x_{2}}{L_{p3}} - R_{p} \sinh \frac{x_{3} - x_{2}}{L_{p3}} - \frac{R_{p} \sinh \frac{x_{3} - x_{2}}{L_{p3}} - \frac{R_{p} \sinh \frac{x_{3} - x_{2}}{L_{p3}} \right] \right\} d\lambda$$
(F-61)
$$J_{scp4} = q \frac{D_{p3}}{L_{p3}} \frac{1 - v_{v4}}{T_{34}} \frac{e^{\Delta E_{v3}/kT}}{sinh \frac{x_{3} - x_{2}}{L_{p3}}} \frac{1/D_{p4}}{\omega_{41} - \omega_{42}} \int_{0}^{\lambda} c^{3} \int_{x_{3}}^{x_{4}} \alpha_{4} N_{04} (x') \left[e^{\omega_{41}(x_{4} - x')} - e^{\omega_{42}(x_{4} - x')} \right] dx' d\lambda + q \frac{D_{p3}}{L_{p3}} P_{sno} \frac{1 - v_{v4}}{T_{34}} \frac{e^{(\Delta E_{v3} + \Delta E_{v4})/kT}}{sinh \frac{x_{3} - x_{2}}{L_{p3}}}$$
(F-62)

$$J_{Jp2} = q \frac{\frac{D}{P3}}{L_{p3}} p_{3no} (e^{qV_2/kT} - 1)R_p.$$
 (F-63)

APPENDIX G: TWO-JUNCTION CASCADE SOLAR CELL ANALYSIS

In APPENDIX F, "Potential Well Solar Cell Analysis", the details of the closed form analysis were presented. The two-junction cascade analysis is discussed below; but, since the details are similar to the analysis presented for the PW cell, less detail is presented for the cascade cell.

The analysis is based on the band structures given in Figure 6.22 for the voltage opposing configuration. The solution for the minority carrier distributions have been written into a computer program through Fortran IV and using an IBM 370-165 for numerical solution. The analysis, while based on the CCVO configuration, has been generalized such that it can also be applied to Si, GaAs, window structures, PW, CCVA and other cascade structures up to n-junctions. The PW analysis is a simplification of this analysis.

The appropriate continuity equation, Eqs. (4.10) through (4.13) is applied to each of the 10 regions in Figure 6.22. The corresponding general solutions, Eqs. (4-14) and (4-19), are then subjected to the boundary conditions given in Table G.1. The boundary conditions pertaining to excess minority carrier concentration and to minority carrier current density are listed in separate columns in Table G.1.

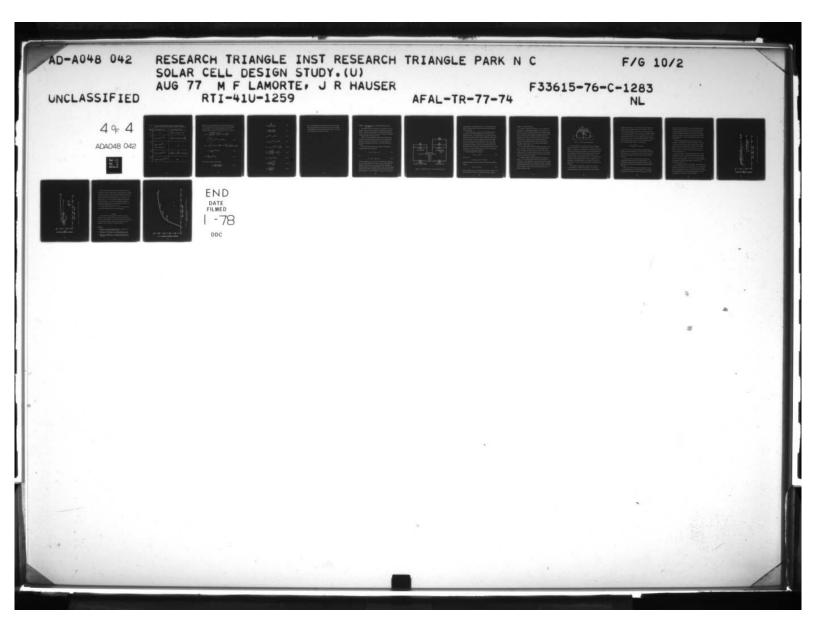
The electron current density, J_{n2} , of the top junction (X = X_2) arising from the absorption of photons in Regions 1 and 2 is given as

$$J_{n2} = -J_{nsc1} - J_{nsc2} + J_{nJ2}$$
(G-1)

where J nsc1 and J nsc2 are the contributions from Regions 1 and 2,

Boundary	Excess Minority Carrier	Minority Carrier Current
X = 0	None	$\left. D_{n1} \frac{dn_1}{dx} \right _0 + n_1(0) \mu_{n1} E_{10} = Sn_1(0)$
= x ₁	$n_1(x_1) = n_2(x_1)e^{-\Delta E_{c1}/kT}$	$D_{n1} \frac{dn_1}{dx} + n_1(x_1)\mu_{n1}E_{10} = D_{n2} \frac{dn_2}{dx}\Big _{x_1}$
= x ₂	$n_2(x_2) = n_{2p0}(e^{\beta_2 1/2} - 1)$ $p_3(x_2) = p_{3n0}(e^{\beta_2 1/2} - 1)$	None
= x ₃	$p_3(x_3) = p_4(x_3)e^{-\Delta Ev_3/kT}$	$ \left \begin{array}{c} D_{p3} \frac{dP_{3}}{dx} \Big _{x_{3}} = D_{p4} \frac{dP_{4}}{dx} \Big _{x_{3}} - P_{4}(x_{3}) \mu_{p4} E_{40} \right $
= X ₄	$p_4(x_4) = p_5(x_4)^{e^{-\Delta E v_3/kT}}$	$D_{p4} \frac{dp_4}{dx} \Big _{x_4} - p_4(x_4) \mu_{p4} E_{40} = D_{p5} \frac{dp_5}{dx} \Big _{x_4}$
= x ₅	$p_5(x_5) = p_{5n0}(e^{\beta_5 V_5} - 1)$ $n_6(x_5) = n_{6p0}(e^{\beta_5 V_5} - 1)$	None
= x ₆	$n_6(x_6) = n_7(x_6)e^{-\Delta E_{c6}/kT}$	$D_{n6} \frac{dn_6}{dx} \Big _{x_6} = D_{n7} \frac{dn_7}{dx} \Big _{x_6} + n_7 (x_6) \mu_{n7} E_{70}$

Table G.1. The list of boundary conditions imposed on the general solutions relating to the CCVO band structure given in Figure 6.22.



Boundary	Excess Minority Carrier	Minority Carrier Current
X = 0	None	$\left D_{n1} \frac{dn_1}{dx} \right _0 + n_1(0) \mu_{n1} E_{10} = Sn_1(0)$
= x ₇	$n_7(x_7) = n_8(x_7)e^{-\Delta E_{c7}/kT}$	$\left. D_{n7} \frac{dn_7}{dx} \right _{x_7} + n_7 (x_7) \mu_{n7} E_{70} = D_{n8} \frac{dn_8}{dx} \Big _{x_7}$
= x ₈	$n_{8}(x_{8}) = n_{8p0}(e^{\beta_{8}V_{8}} - 1)$ $p_{9}(x_{8}) = p_{9n0}(e^{\beta_{8}V_{8}} - 1)$	None
= x ₉	$p_{9}(x_{9}) = p_{10}(x_{9})e^{+\Delta E_{v9}/kT}$	$D_{p9} \frac{dp_9}{dx} \bigg _{x_9} = D_{p10} \frac{dp_{10}}{dx} - p_{10}(x_9) \mu_{p10} E_{100}$
= x ₁₀	$p_{10}(x_{10}) = p_{11}(x_{10})e^{+\Delta E_{v10}/kT}$	None

Table G.1. The list of boundary conditions imposed on the general solutions relating to the CCVO band structures given in Figure 6.22 (Continued).

respectively, to the electron short circuit current density and J_{nJ2} is the electron contribution to dark current arising from the photovoltage of the top junction. The closed form relationships for each of the component currents in Eq. (G-1) are given in Eqs. (G-2), (G-3) and (G-4):

$$J_{nscl} = q \frac{v_{21}^{\cosh \frac{x_2^{-x_1}}{L_{n2}}}}{v_{w1}^{e^{-\Delta}el^{/kT}}} \frac{e^{(w_{11}^{+C0}_{12}x_1)}}{I_{01}} (R_n^{-\tanh \frac{x_2^{-x_1}}{L_{n2}}})$$

$$\times \int_{0}^{\lambda_{c2}} \int_{0}^{x_{1}} \alpha_{1} N_{01} \left[e^{-w_{11x}} - v_{s1} e^{-w_{12x}} \right] dx d\lambda ; \qquad (G-2)$$

$$J_{nsc2} = qD_{n2} \int_{0}^{A_{c2}} \alpha_{2}C_{23} \left[(R_{n} \cosh \frac{x_{2}-x_{1}}{L_{n2}} - \sinh \frac{x_{2}-x_{1}}{L_{n2}}) (\frac{v_{21}}{v_{w1}e^{-\Delta E_{c1}/kT}} + \frac{1}{\alpha_{2}L_{n2}}) \right]$$

$$-(1 + \frac{1}{\alpha_2 L_{n2}})e^{-\alpha_2 (x_2 - x_1)}]d\lambda ; \qquad (G-3)$$

$$J_{n2} = q \frac{D_{n2}}{L_{n2}} n_{2po} (e^{\beta_2 V_2} - 1)R_n . \qquad (G-4)$$

The constants are defined by the following:

$$\mathbf{v_{s1}} = \frac{D_{n1}\mathbf{w_{12}} + \mu_{n1}\mathbf{E_{10}} - S}{D_{n1}\mathbf{w_{11}} + \mu_{n1}\mathbf{E_{10}} - S}, \qquad (G-5)$$

$$v_{21} \equiv \frac{\frac{D_{n2}}{L_{n2}}}{D_{n1}w_{11} + \mu_{n1}E_{10}}$$
, (G-6)

$$\mathbf{v}_{1} = \frac{D_{n1}\mathbf{w}_{12} + \mu_{n1}\mathbf{E}_{10}}{D_{n1}\mathbf{w}_{11} + \mu_{n1}\mathbf{E}_{10}}, \qquad (G-7)$$

$$I_{01} \equiv e^{w_{12}x_1} - v_{s1}e^{w_{11}x_1}$$
, (G-8)

$$v_{w1} \equiv \frac{1}{I_{01}} [v_1 e^{w_{12} x_1} - v_{s1} e^{w_{11} x_1}],$$
 (G-9)

$$F_{12} \equiv v_{21} + v_{w1}^{-\Delta E_{c1}/kT} \tanh \frac{x_{2}-x_{1}}{L_{n2}}$$
, (G-10)

$$N_{12} \equiv \frac{v_{21}^{\sinh \frac{x_{2}-x_{1}}{L_{n2}}}}{v_{w1}^{e}e^{-\Delta E}c^{1/kT}} + \cosh \frac{x_{2}^{-x_{1}}}{L_{n2}}$$
(G-11)

.

$$N_{01} \equiv (1-r)N_{0}(\lambda)e^{-\int_{0}^{x} \alpha_{1}dx'} \qquad (G-12)$$

$$R_{n} = \frac{N_{12}}{F_{12}} \frac{v_{w1}e}{\cosh \frac{x_{2}-x_{1}}{L_{n2}}}$$
(G-13)

$$C_{23} = \frac{\alpha_2 L_{n2}^2 (1-R) N_o}{D_{n2} (\alpha_2^2 L_{n2}^2 - 1)}$$
(G-14)

These are corresponding current equations of holes for the top junction and of electrons and holes for the bottom junction. Due to the length of these equations we will not present them in this report. The results of the calculations are presented in Section 6.0

APPENDIX H. EQUIVALENT CIRCUIT FOR A VOLTAGE-OPPOSING CASCADE SOLAR CELL STRUCTURE

The equivalent circuit of a cascade solar cell structure is not selfevident. Clearly, it must be derived from the solution to the continuity equation. An interesting characteristic of voltage-opposing structures is that a fraction of the dark current of one p-n junction may be converted to electrical energy in an adjacent junction.

Consider a two-junction pp/nnn/pp cascade structure where the load resistance, R_1 , and load voltage, V_1 , relate to the first junction while R_2 and V_2 to the second. We assume that a drift field is present in the middle n-type region which aids holes to flow forward the second p-n junction.

The current solutions obtained from a solution of the continuity equations for each of the junctions are

$$J_{1} = J_{sc1} + \beta_{2} J_{Dp2} - J_{D1}$$
(H-1)

and

$$J_{2} = -J_{sc2} - \beta_{1} J_{Dp1} + J_{D2}$$
(H-2)

where the subscripts refer to the first and second junctions, respectively: J_{sc1} , J_{sc2} are the short-circuit currents; J_{D1} , J_{D2} are the component dark currents - electrons and holes; J_{Dp1} , J_{Dp2} are the hole contributions to the dark currents; β_1 , β_2 are the hole transport factors in the (nnn) regions. From Eqs. (H-1) and (H-2) the equivalent circuit may be constructed and presented in Figure H.1. The current generator, β_2 J_{Dp2} , in Eq. (H-2) is not

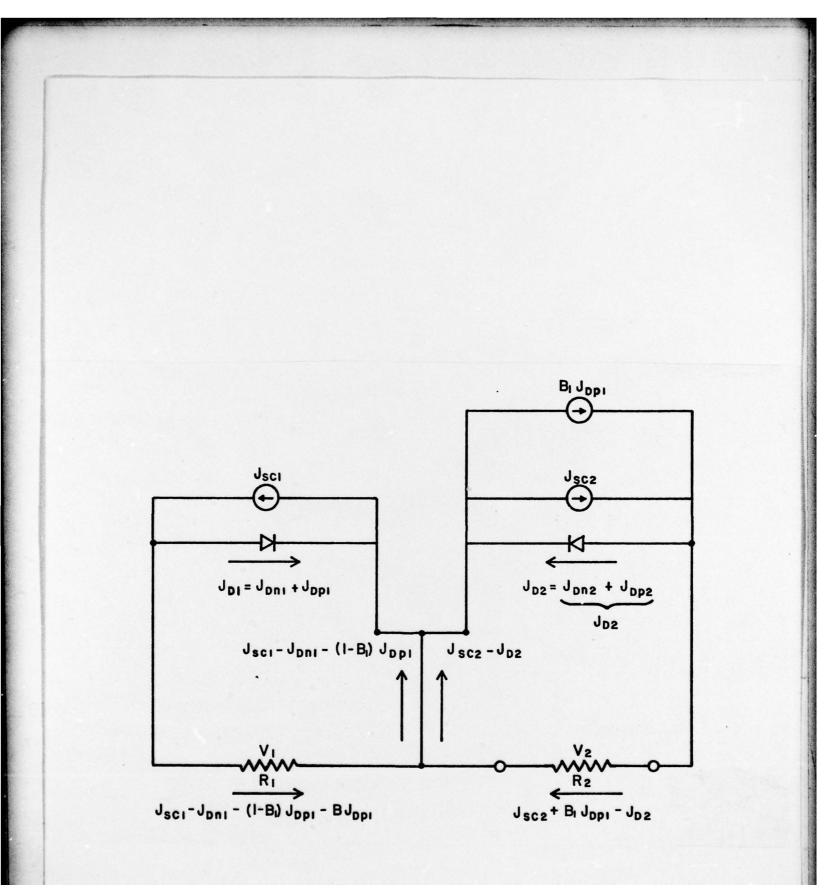


Figure H.1. Equivalent Circuit for 2-Junction Cascade Structure.

included because it is very small since $\beta_2^{<<1}$. This results because the built-in field in the middle n-type region accelerates holes toward the second p-n junction.

The current generators, J_{sc1} and J_{sc2} , and the diode dark currents, J_{D1} and J_{D2} , are the familiar quantities which are present in single junction solar cells. The current generator $\beta_1 J_{Dp1}$ arises from the hole contribution to the dark current of the first p-n junction which is transported to the second. This current component arises from holes flowing in the same direction as those holes produced by photons in the second and third n-type regions. The transport factor, β_1 , can be nearly unity for appropriate cell designs. Therefore, an appreciable portion of this hole dark current may be converted to useful electrical energy by the second p-n junction. For the same reasons that β_1 may be unity, β_2 is much less than unity and the term $\beta_2 J_{Dp2}$ is neglected.

The power dissipated in the load R₁ is

$$P_{1} = (J_{sc1} - J_{D1}) V_{1}$$
(H-3)

and in R₂ it is

$$P_2 = (J_{sc2} - J_{D2}) V_2 + \beta_1 J_{Dp1} V_2 .$$

The power dissipated in the load, R_2 , without the dark current component, $\beta_1 J_{Dp1}$, is

$$P_{20} = (J_{sc2} - J_{D2}) V_2$$
(H-4)

which is identical in form to a single junction solar cell. Therefore, the power converted by the second cell is increased by the amount $\beta_1 J_{Dp1} V_2$.

APPENDIX J. LOW VOLTAGE CONVERSION

The problem of converting low voltages (< 1 Vdc) to a higher, more useful level is a classical problem dating back to the early 1960's. At that time, fuel cells and thermionic generators were promising new energy sources, and efficient voltage converters were urgently needed to exploit their characteristic low output voltages. Consequently, there were numerous, concerted efforts to develop efficient, low voltage converters during the 1960's. These efforts were only marginally successful. Converters for input voltages between 0.5 and 1 volts exhibited peak efficiencies of about 80 percent. Efficiencies decreased sharply as voltages were reduced below 0.5 volts.

The low voltage conversion problem was somewhat circumvented in the mid- to late 1960's. The solar cell, fuel cell, and thermionic energy sources, for example, were placed in series to obtain a higher output voltage and provide for a higher conversion efficiency. The series source connections were generally more complex and less reliable than the single sources or sources connected in parallel.

Low voltage converters are basically configured as illustrated in Figure J.1. The low input voltage is connected across the primary of a transformer. As the transformer core approaches saturation, the switches are operated to apply the MMF (V_{in}) in the opposite direction. Additional circuitry controls the state of the two switches, which must be alternately closed and opened, and provides other desired characteristics, e.g., a filtered, regulated dc output.

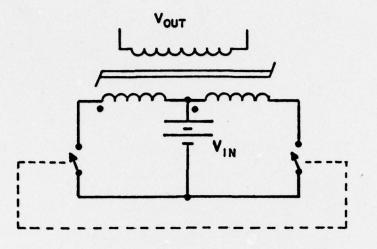


Figure J.1. Basic Converter Configuration.

For a given power input, the converter efficiency is determined by losses in the converter. (n = Power out/Power in = (Power in - Losses)/ (Power in.). These consist of transformer core losses (hysteresis and eddy currents), copper losses, and switch losses. In practical converters for space applications, transistors are most suitable as switches. However, transistor switches have a characteristic threshold loss due to the voltage drop across the collector-emitter circuit. If the converter input voltage is low, this collector-emitter loss is very significant and is detrimental to the collecter efficiency. In contrast, core losses and copper losses vary with the converter output and are relatively small and manageable.

As an illustration, assume that the switches in the circuit of J.1 are transistors. At moderate current levels, e.g., 30-100A, the collector-emitter drop (V_{ce} sat.) will typically be 50 mV for selected

germanium power transistors. (Low voltage converters must handle large currents if a significant power output is to be achieved.) Thus, the collector-emitter circuit loss is estimated to be 0.05 I_c watts where I_c is the collector (transformer) current. Other typical transistor parameters are a dc current gain (h_{FE}) of 10 and a base-emitter drop of 0.5V. Thus, the base-emitter circuit has a loss (0.5 I_c/ h_{FE}) equal to the collectoremitter, and the losses in a conducting switch are estimated as (2)(0.05) I_c. The converter input power is V_{in}I_c. With only the transistor switch losses considered, maximum efficiency can be estimated as

$$n = \frac{V_{in} - (2) (.05)}{V_{in}} \times 100 \text{ percent.}$$

If V_{in} is 0.2, 0.4, or 0.6 volts, for example, the estimated maximum possible converter efficiencies are 50, 75, and 83 percent, respectively. Other losses, e.g., core, copper, switch control circuit, and regulator circuit, have been neglected and these will also reduce the converter efficiency.

A literature search of the NASA and DOD files has been made to determine the state-of-the-art in low voltage converters. It is noteworthy that references from the NASA search show numerous entries between 1962 and 1967, and a sharp curtailment of converter activities after 1967.

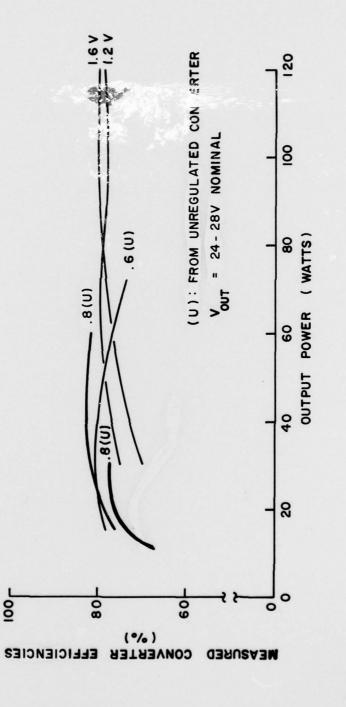
The literature confirms that the basic configuration of Figure J.1 is predominantly used in lwo voltage converters. The switches are special purpose, germanium power transistor with low V sat. values.

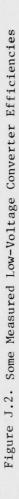
Design features characteristically include current feedback schemes to insure that conducting transistor switches were saturated ON, schemes to minimize excessive base currents which overdrive the conducting transistor, and schemes to eliminate extraneous losses associated with excessive transformer (and switch) currents when the power transformer approaches saturation. Converter operating frequencies tended to be 400 to 1000 Hz.

Figure J.2 shows some measured efficiencies from low voltage converters. The parameters are converter input voltages. The 1.6V and 1.2V curves are from a 150 watt, 28 volt, regulated output converter. The converter efficiency remained above 79 percent for input voltages between 1.2V and 1.6V over the 80 to 155 watt range [J-1]. The other curves in Figure J.2 are from two unregulated converters designed for lower input voltages [J-1].

The curves in Figure J.3 show measured efficiencies from a second regulated-output converter. The output voltages were regulated within \pm 1 percent. For the 0.4V input case, the set point had to be changed to 24 VDC to maintain regulation. The 1.2 and 1.8V curves were obtained by operating from a laboratory power supply, and the others from a thermionic diode source [J-2].

It is interesting to note that the efficiency is a rather complicated function of the power output and the input voltage. For low voltage inputs, particularly, the efficiency tends to peak over a narrow range of output power. This reflects the fact that, for low input voltages, the efficiency is strongly dependent upon certain design considerations that can only be optimized over a small range of operating conditions.





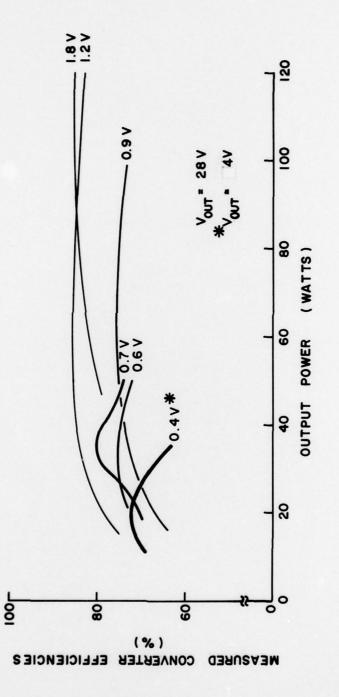




Figure J.4 shows efficiency data from an experimental low voltage converter as a function of input voltage. The input current was a constant average (over each cycle) of 20A. These data are especially interesting in that the efficiency is shown going to zero at about 0.23 volts. This implies that the transistor switches have a V_{ce} sat. parameter of less than 0.23 volts, i.e., it is a very unusual transistor and is probably not readily available. This converter is an unregulated converter. It is basically configured similar to the configuration in Figure J.1 but with a unique, highly efficient innovation [J-3].

The data presented in Figures J.2, J.3, and J.4 are from the more efficient converters described in the literature reviewed.

Conclusions

The data presented in this appendix confirm that the efficient conversion of low, dc voltages from less than one volt to a more useful level is a difficult problem. In the range of 0.5V to 1V input, efficiencies of 70-80 percent are obtained through careful design and selection of components. Below 0.5V inputs, the efficiency decreases.

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