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SYSTEMS ANALYSIS DIRECTORATE
ACTIVITIES SUMMARY

JULY 1977

AUGUST 1977

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US ARMY ARMAMENT MATERIEL READINESS COMMAND
SYSTEMS ANALYSIS DIRECTORATE
ROCK ISLAND, ILLINOIS 61201

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This monthly publication contains Memoranda for Record (MFR's) and other technical information that summarize the activities of the Systems Analysis Directorate, US Army Materiel Readiness Command, Rock Island, IL (The most significant MFR's and other data will be published as notes or reports at a later date.) The subjects dealt with are M44 Periscope, XM204 Howitzer, and M110A1 SP Howitzer.		

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*Memorandum for Record and other technical information are grouped according to subject, when applicable, and in chronological order.

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DRSAR-SAA

MEMORANDUM FOR RECORD:

SUBJECT: Cost Analysis of M44 Periscope Product Improvement Proposals

1. The purpose of this study is to determine the most cost effective product improvement proposal (PIP) for the M44 periscope. The alternatives considered were:

alternative 1. Continue with the existing periscope design.

alternative 2. Improve the prism bonding area, convert power supply, install a reset relay to prevent image intensifier tube damage and improve the sealing and purging system.

alternative 3. Modify the M44 periscope body and use the M32E1 night vision elbow.

alternative 4. Replace the M44 periscope with the M32E1 periscope.

2. The M44 Periscope was the first periscope to use the passive night vision image tube. Because of the length of this first generation tube, periscope designers were forced to utilize a complex optical design. Poor maintainability because of the complexity has resulted in high failure rates and high logistic support costs. Alternative 2 proposes to correct these problems by improving the existing M44 design. Advancements in the design of night vision devices have occurred since the M44 periscope was fielded. Second generation image intensifier tubes are more compact and have self-contained optical alignment and electrical controls. These advancements have enabled the night vision portions of the newer passive periscopes to be easily replaceable modules. One of these designs is the M32E1 periscope. The third alternative proposes to modify the M44 body to accept the M32E1 night vision elbow. The fourth alternative proposes to replace the entire M44 periscope with the M32E1 periscope. This alternative requires modification of the hull as the openings for the M44 and the M32E1 are not the same size.

3. The cost of ownership was determined for each of the alternatives. It was assumed that each alternative had been implemented at the beginning of the time period. It was further assumed that 1575 Sheridans would be in use. The one time PIP cost and the yearly maintenance cost was determined using the following equation.

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SUBJECT: Cost Analysis of M44 Periscope Product Improvement Proposals

$$Y = PT(B (B\$) + R (R\$))$$

where:

P = fraction of periscopes replaced due to usage
B = fraction of replaced items purchased
B\\$ = purchase cost for one periscope
R = fraction of units rebuilt
R\\$ = cost of rebuilding one periscope
T = total number of periscopes to be in use

The percent of items replaced, the percent replacements purchased, and the percent of items rebuilt were determined for the M44, equipment used with the M44, and for the M32 periscope. These values and the cost associated with purchase and overhaul are presented in Table 1. The actual determination of these values is presented in the appendix. These values were used for alternatives 1, 3 and 4. The replacement rate for alternative 2 is not known. It was assumed that the improved M44 would require 20 percent fewer replacements than the existing design. Comparing the M44 and the M32 replacement rates indicates this assumption provides an optimistic estimate of the PIP's effectiveness. The M32's replacement rate is 12.78 percent (i.e., the sum of total periscope replacements, head replacements and body replacement). A twenty percent reduction of M44 replacement rate results in a replacement rate of 11.58 percent. Therefore assuming a 20 percent reduction in replacement rate results in the lowest replacement rate for all alternatives considered. The yearly replacement costs and the one time implementation costs are presented in Table 2. The determination of the yearly replacement costs is presented in the appendix. The Cumulative Cost in FY77 Discounted Dollars associated with each alternative was determined for ownership periods for as long as 25 years. These data are presented in Table 3 and Figure 1.

4. Comparing the costs of ownership for each alternative can be accomplished by reviewing Figure 1. The following statements can be made:

a. Alternative 1 is the least costly alternative for the first eight years of consideration, at which time alternatives 1, 2 and 3 are equal in total cost.

b. Alternative 2 breaks even in the ninth year and shows a cost savings when compared to alternative 1 in the subsequent years. However, after nine years alternative 2 shows higher costs than alternative 3, even with the optimistic assumption that alternative 2 would require 20% fewer replacements than the existing design.

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SUBJECT: Cost Analysis of M44 Periscope Product Improvement Proposals

c. Alternative 3 breaks even in the ninth year and in the subsequent years is the least costly when compared to the other alternatives.

d. Alternative 4 is always more costly than the other alternatives.

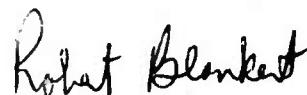
It should be noted that two of the assumptions made in this analysis could affect the breakeven point for alternatives 2 and 3. Firstly, it was assumed that each alternative had been implemented at the beginning of the time period. In actuality, the product improvements would have to be purchased and then phased into the systems. This will make the break-even point greater than nine years. Secondly, it was assumed that all 1575 Sheridans would be in use during the entire period of consideration, even though only 812 were operating at the end of 1975. The projected overhaul of Sheridans could have been phased in or an estimate of the average number of Sheridans could have been used. In either case, the breakeven point would probably be extended past nine years.

Furthermore, it is important to consider the economic life of the Sheridans. If the Sheridans are going to be replaced in 5 to 10 years, then it would not be economical to implement any of the PIPs.

In addition to cost considerations, other areas that could be considered are:

a) If alternative 3 is selected, maintainability will be enhanced because of the modular construction provided by this alternative and the night vision elbow in the M551 will be interchangeable with the night vision elbows in the M60 tanks.

b) If alternative 1 or 2 is selected, difficulty may be experienced in obtaining replacement image intensifier tubes as these first generation image intensifier tubes are no longer in production.



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Methodology Division

TABLE 1

Description	Percent Replaced/Yr	Percent Replacements Purchased	Percent Replacements Overhauled	Purchase Cost	Overhaul Cost
M44 Periscope	14.47	34.80	65.20	15,524	1,876
Panel FSN (1240-181-5612)	1.14	100.00	0	241	-----
Panel FSN (1240-916-5914)	7.79	100.00	0	209	-----
Cable	10.48	100.00	0	33	-----
Circuit Card	16.66	100.00	0	22	-----
M32 Periscope (total)	4.11	14.96	85.04	4,400	808
M32 Head	4.48	37.40	62.60	1,450	368
M32 Body	4.19	30.56	69.44	2,852	440

TABLE 2

Alternative	Initial PIP Cost	Yearly Maintenance Cost
1. Do nothing to existing design	0	1,551,157
2. Improve M44	\$ 1,765,417	1,240,926
3. Install M32 elbow on M44	7,500,000	202,555
4. Replace M44 with M32 periscope	13,500,000	202,555

TABLE 3
CUMULATIVE COST OF IMPLEMENTING ALTERNATIVES
FY77 CONSTANT DISCOUNTED DOLLARS
ASSUMED DISCOUNT RATE 10%

Years of Ownership	Do Nothing	To Existing Design	Improve M44 Periscope	Install M32 Elbow On M44 Periscope	Replace with M32 Periscope
0	0.0	\$1.77M	\$7.5M	\$13.5M	
1	\$1.41M	2.89	7.68	13.68	
2	2.69	3.92	7.85	13.85	
3	3.86	4.85	8.00	14.00	
4	4.91	5.70	8.14	14.14	
5	5.88	6.47	8.26	14.26	
6	6.75	7.17	8.38	14.38	
7	7.55	7.80	8.48	14.48	
8	8.27	8.38	8.58	14.58	
9	8.93	8.91	8.66	14.66	
10	9.53	9.39	8.74	14.74	
11	10.07	9.82	8.81	14.81	
12	10.56	10.22	8.88	14.88	
13	11.01	10.58	8.93	14.93	
14	11.42	10.90	8.99	14.99	
15	11.79	11.20	9.04	15.04	
16	12.13	11.47	9.08	15.08	
17	12.44	11.71	9.12	15.12	
18	12.72	11.94	9.16	15.16	
19	12.97	12.14	9.19	15.19	
20	13.20	12.32	9.22	15.22	
21	13.41	12.49	9.25	15.25	
22	13.60	12.64	9.28	15.28	
23	13.77	12.78	9.30	15.30	
24	13.93	12.91	9.32	15.32	
25	14.07	13.02	9.34	15.34	

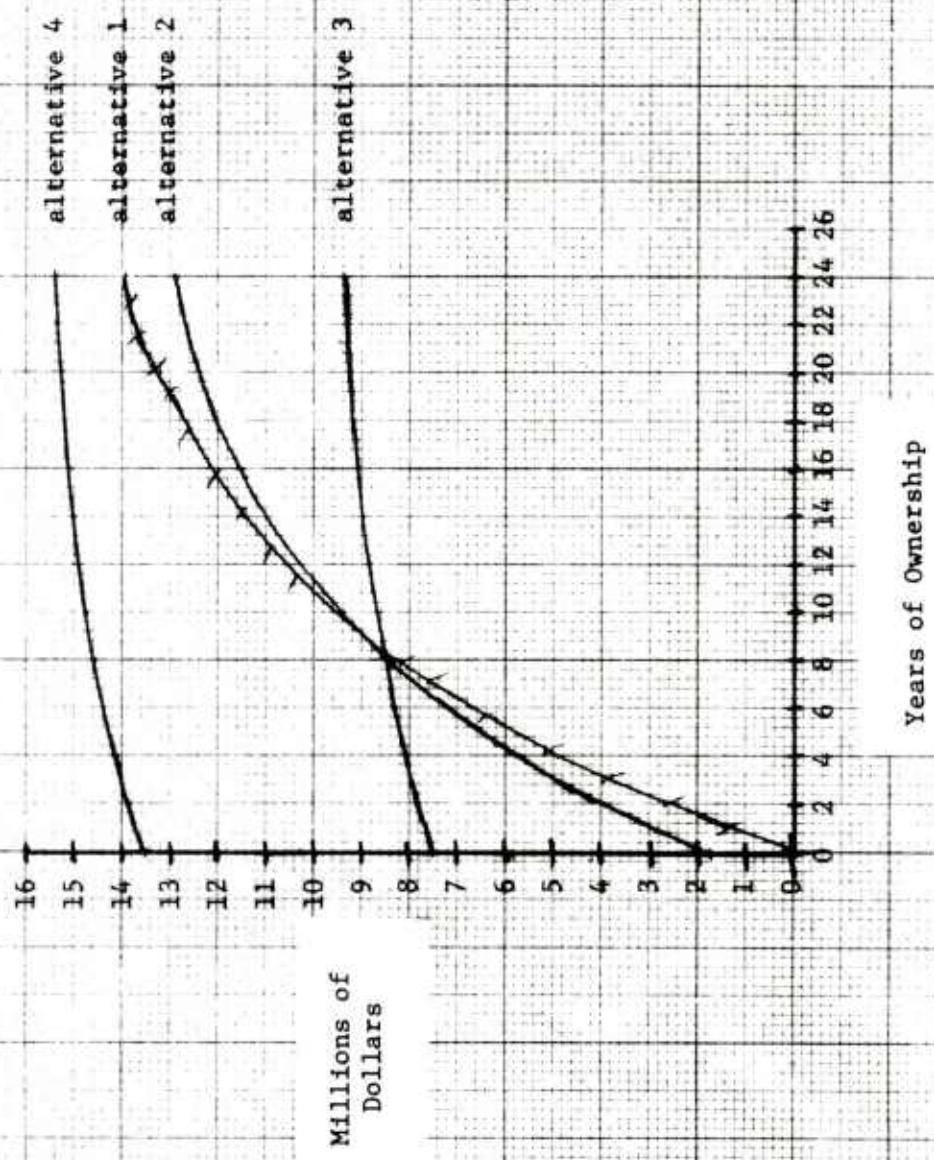


TABLE A-1

M551 Overhaul Program

<u>Rebuild Period</u>	<u>Combat Damaged Overhauls at Anniston</u>	<u>M551 CONUS Milage Overhauls at Anniston</u>	<u>M551 Europe Overhauls at Mainz</u>
73-74	43	0	61
75-76	159	0	78
77	10	61	42
77-78 (Projected)	23	192*	56
TOTAL	335	253	237

* 50 rebuilt from Europe

TABLE A-2

Recurring Demands for
M44 Periscopes

<u>Period</u>	<u>Demand</u>
73-74	87
75-76	104

TABLE A-3

Demands for M44 Periscope
Related Equipment

<u>Description</u>	<u>Non Recurring</u>	<u>Recurring</u>	<u>Purchase Cost</u>
Panel FSN 1240-181-5612	12	3	\$241
Panel FSN 1240-916-5914	96	12	209
Cable FSN 1240-906-7948	96	36	33
Circuit Card FSN 1240-946-8829	48	120	22

TABLE A-4

M44 Periscopes in Use

YEAR	1974	1975
TOTAL IN USE	974	812

TABLE A-5

Tank Overhaul Program

<u>Period</u>	<u>M60</u>	<u>M60A1</u>
75	376	163
76	343	74
77-7T	255	72
78	215	185
79	62	130
80	0	101
TOTALS	1251	725

TABLE A-6

Vehicles and M32 Periscopes in Use

<u>Vehicle</u>	<u>Number</u>	<u>Periscopes</u>
M60	3,527	7,054
M60A2	288	576
M48	963	963
TOTAL		8,593

TABLE A-7

Number of Periscopes Rebuilt and Purchased
with Respective Costs

<u>Item</u>	<u>Number Purchase/Yr</u>	<u>Purchase Cost</u>	<u>Number Rebuilt/Yr</u>	<u>Rebuilt Cost</u>
M44	64	15,524	120	1,876
M32 Periscope	60	4,400	341	808
M32 Head	144	1,450	241	368
M32 Body	110	2,852	250	440

TABLE A-8

Recurring Demands for M32
Periscopes & Related Equipment

Complete M32 Periscope	24/Yr
M32 Head	385/Yr
M32 Body	360/Yr

1. Determination of percent of M44 periscope replaced per year.

$$P = (\bar{R} + \bar{D})/T \quad \text{EQ 1}$$

where

P = Fraction of M44's replaced each year.

\bar{R} = Average number of periscopes rebuilt with the mileage rebuild vehicles. (from Table A-1)

\bar{D} = Average number of periscopes requested for field replacement per year. (from Table A-2)

T = Total number of M44's in use. (from Table A-4)

$$P = \left[\frac{253 + 237}{6} + \frac{87 + 104}{4} \right] / \left[\frac{974 + 812}{2} \right]$$

$$= .1447$$

2. Determination of fraction of M44 periscopes replacements purchased and rebuilt.

$$R_p = \frac{N_p}{N_p + N_r} \quad \text{EQ 2}$$

where

R_p = Fraction purchased

N_p = Number purchased each year from Table A-7

N_r = Number rebuilt each year from Table A-7

$$R_p = \frac{64}{120 + 64}$$

$$= .348$$

$$R_r = 1 - R_p$$

EQ 3

where

$$R_r = \text{Fraction rebuilt}$$

$$R_r = 1 - .348$$

$$= .652$$

3. Now determining panel replacement rate. To get peacetime usage of panels from Table A-1:

$$\begin{aligned} \text{Fraction M551 mileage overhauls} &= \frac{\text{Mileage overhauls}}{\text{All overhauls}} \\ &= \frac{253 + 237}{335 + 253 + 237} \\ &= .6 \end{aligned}$$

Using equation 1 and data from Table A-3 to determine the fraction of panel (FSN 1240-181-5612) replaced.

$$P = \frac{(.6)(12) + 3}{893}$$

$$= .0114$$

Using a similar technique for panel (FSN 1240-916-5914)

$$P = \frac{(.6)(96) + 12}{893}$$

$$= .0779$$

4. Determining cable replacement rate using equation 1 and data from Table A-3.

$$P = \frac{(.6)(96) + 36}{893}$$

$$= .1048$$

5. Determining circuit card replacement rate using equation 4 and data from Table A-3.

$$P = \frac{(.6)(48) + 120}{893}$$
$$= .1666$$

6. Determining the yearly replacement costs for the M44 periscopes.

Cost of M44 purchased for replacement (.1447)(.348)(1575)(\$15,524)	=	\$1,231,209
Cost of M44 rebuild for replacements (.1447)(.652)(1575)(\$1,876)	=	278,759
Cost of panel replacement (FSN-1240-181-5612) (.0114)(1575)(\$241)	=	4,327
Cost of panel replacement (FSN-1240-916-5914) (.0779)(1575)(\$209)	=	25,642
Cable Costs (.1048)(1575)(\$33)	=	5,447
Circuit card costs (.1666)(1575)(\$22)	=	5,773
TOTAL		\$1,551,157

7. Using Equation 1 and data from Tables A-5, A-6 and A-8 to calculate the fraction of M32 periscopes replaced.

$$P = \frac{(1251 + 725)/6 + 24}{8593}$$
$$= .0411$$

8. Using equations 2 and 3 and data from Table A-7 to determine percent purchased and percent rebuilt.

$$R_p = \frac{60}{60 + 341}$$
$$= .1496$$
$$R_r = .8504$$

9. Using Equation 1 and data from Table A-7 to determine the fraction of M32 heads replaced per year.

$$P = \frac{144 + 241}{8593}$$
$$= .0448$$

10. Determining the fraction purchases & fraction rebuild using equations 2 & 3 and data from Table A-7.

$$R_p = \frac{144}{385}$$
$$= .374$$
$$R_R = 1 - .374$$
$$= .626$$

11. Using equation 1 and data from Table A-7 to determine the number of M32 bodies replaced.

$$P = \frac{110 + 250}{8593}$$
$$= .0419$$

12. Using equations 2 & 3 and data from Table A-7 to determine the fraction of M32 bodies purchased and the fraction rebuilt.

$$R_p = \frac{110}{110 + 250}$$
$$= .3056$$
$$R_R = 1 - .3056$$
$$= .6944$$

13. Determining the yearly replacement costs if the M32 periscope is used in place of the M44 periscope.

Cost of purchasing M32 periscopes (.0411)(.1496)(1575)(\$4400)	=	\$42,610
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Cost of rebuilding M32 periscopes (.0411)(.8504)(1575)(\$808)	=	44,479
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Cost of purchasing M32 periscope heads (.0448)(.374)(1575)(\$1450)	=	\$38,265
Cost of rebuilding M32 periscope heads (.0448)(.626)(1575)(\$368)	=	16,255
Cost of purchasing M32 periscope bodies (.0419)(.3056)(1575) (\$2582)	=	52,072
Cost of rebuilding M32 periscope bodies (.0419)(.3056)(1575)(\$440)	=	8,874
Total cost of replacement on M32		\$202,555

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For use of this form, see AR 340-15; the proponent agency is The Adjutant General's Office.

REFERENCE OR OFFICE SYMBOL

SUBJECT

DRSAR-SAA

XM204 Howitzer Production Trade-Off Analysis

TO DRSAR-AS

FROM DRSAR-SA

DATE

8 5 JUL 77

CMT 1

Mr. Trier/plb/6370

1. Reference is made to DF, DRSAR-AS to DRSAR-SAA and eight other Directorates, subject: 105mm Howitzer Production, XM204, dated 29 Mar 77.
2. Systems Analysis was tasked (ref 1) to provide a cost analysis on the possible procurement of XM204 Howitzers and the subsequent potential revenues received by selling overhauled M101A1 and M102 Howitzers via Foreign Military Sales (FMS). Several alternative plans were addressed which considered replacing all Army 105mm Howitzer assets with XM204 Howitzers, replacing only those 105mm Howitzers in Active Army units, or replacing either all M101A1 Howitzers or all M102 Howitzers. In addition, the FMS selling price was parameterized to show how potential revenues increase/decrease as the FMS selling price increases/decreases. Attached MFR (Incl 1) contains the results of this study.
3. Point of contact is Mr. Norman H. Trier, extension 6370.



M. RHIAN
Director, Systems Analysis Directorate

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MEMORANDUM FOR RECORD

SUBJECT: XM204 Production Trade-Off Analysis

1. Objective: Systems Analysis was tasked^{1,2} to determine:

a. the cost of producing XM204 Howitzers to replace the Army's current assets of M101A1 and M102 Howitzers, and

b. the potential net revenues (total revenues minus overhaul costs) of selling overhauled M101A1 and M102 Howitzers via Foreign Military Sales (FMS).

2. Introduction: The Development Acceptance (DEVA) In-Process Review (IPR) for the XM204 Howitzer, a soft recoil 105mm Towed Howitzer, is scheduled for December 1977. Depending on the Development and Operation testing, and other considerations such as the availability of funds and other higher priority systems, the Research, Development and Acquisition Committee (RDAC) could decide to support the production of the XM204 Howitzers. If the XM204 Howitzers are produced and fielded, the current Army assets of 105mm Howitzers (Table 1)^{3,4} would be replaced, and, according to the SAMPAM⁵, the potential distribution of Army 105mm Howitzer assets in FY83 would be similar to that shown in Table 2. If the XM204's are fielded, there is the possibility of overhauling and selling existing Army 105mm Howitzers to FMS customers and diverting that revenue to production of XM204 Howitzers. This report addressed the potential net revenues which could be received from FMS of existing 105mm Howitzers assets and the investment which would be required to produce and field XM204 Howitzers.

3. Alternatives: Four alternatives (ALT 1, 2, 3, and 4) were identified for this analysis and are listed in Table 3. Each alternative addresses the replacement of the current Army assets of 105mm Howitzers with new production of XM204 Howitzers.

ALT 1 addresses the replacement of 105mm Howitzers in Active Army, Reserves, and National Guard units with XM204 Howitzers. This is done in accordance with potential distribution of 105mm Howitzers as found in the 3 Jan 77 SAMPAM (refer to Table 2).

ALT 2 addresses the replacement of 105mm Howitzers in Active Army only with XM204 Howitzers, while retaining a mix of M101A1 and M102 Howitzers in the Reserve and National Guard units.

TABLE 1. CURRENT ARMY ASSETS OF 105MM HOWITZERS^{a,b}

	<u>Active Army</u>	<u>Reserves & National Guard</u>	<u>Totals</u>
M101A1	300	445	745
M102	449	135	584
Totals	749	580	1,329

^aDRSAR-MMH DF to DRSAR-AS, subject: 105mm Howitzer Production, XM204, dated 27 Apr 77. CONFIDENTIAL

^bMeeting between Mr. Aukland, DRSAR-MMH, and Mr. Trier, DRSAR-SA, subject: Quantity of M101A1 and M102 Howitzers in Reserves and National Guard, dated 28 Apr 77.

TABLE 2. POTENTIAL DISTRIBUTION OF ARMY ASSETS^a
OF 105MM HOWITZERS

	<u>Active Army</u>	<u>Reserves & National Guard</u>	<u>Totals</u>
M101A1	--	--	--
M102	248	30	278
XM204	545	573	1,118
Totals	793	603	1,396

^aArmy Materiel Plan Summary, 3 January 1977, Printout numbers G0180000M00, G0180100M00, G0180200M00, and G0180300M00. CONFIDENTIAL

TABLE 3. ALTERNATIVES

ALT 1:

- a. Produce 1,118 XM204 Howitzers for Active Army, Reserves, and National Guard.
- b. Overhaul 745 M101A1 Howitzers and 306 M102 Howitzers.
- c. Sell, via FMS, the overhauled M101A1 and M102 Howitzers.

ALT 2:

- a. Produce 793 XM204 Howitzers for Active Army only.
- b. Overhaul 300 M101A1 and 426 M102 Howitzers from current Active Army assets.
- c. Sell, via FMS, the overhauled M101A1 and M102 Howitzers.

ALT 3:

- a. Produce 812 XM204 Howitzers for Active Army, Reserves, and National Guard.
- b. Overhaul 745 M101A1 from current Army assets.
- c. Sell, via FMS, the overhauled M101A1 Howitzers.

ALT 4:

- a. Produce 651 XM204 Howitzers for Active Army, Reserves, and National Guard.
- b. Overhaul 584 M102 Howitzers from current Army assets.
- c. Sell, via FMS, the overhauled M102 Howitzers.

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SUBJECT: XM204 Production Trade-Off Analysis

ALT 3 addresses the replacement of all M101A1 Howitzers in current Army assets with XM204 Howitzers, while retaining the current assets of M102 Howitzers.

ALT 4 addresses the replacement of all M102 Howitzers in current Army assets with XM204 Howitzers, while retaining the current assets of M101A1 Howitzers.

For each of the four alternatives, the potential distribution of Army 105mm Howitzers is displayed in Table 4. In addition, for each alternative, the production schedules of XM204 Howitzers, the overhaul schedules for the M101A1 and M102 Howitzers, and the FMS schedules for overhauled M101A1 and M102 Howitzers which were used in this analysis are displayed in Appendix A, Tables A-1, A-2, A-3, and A-4.

4. Approach: The analysis was consistent with guidelines in AR 11-28, Economic Analysis and Program Evaluation for Resource Management⁶, in that all input data was converted to constant FY77 dollars and all monies laid out in the out years were discounted to FY77 by applying the 10% discount factors.

The investment costs of XM204 Howitzers include the Initial Production Facilities (IPF), production costs, initial provisioning and training, and publications. The per unit production cost estimate includes the hardware and support costs, test ammunition, and first destination transportation.

The per unit overhaul cost estimate for both the M101A1 and M102 Howitzers includes labor expenses, general and administration (G&A) expenses, indirect maintenance expense (IME), materiel, test ammunition, and transportation charges.

The selling price of overhauled M101A1 and M102 Howitzers for Foreign Military Sales (FMS) was calculated by applying the methodology used for the FMS of M101A1 Howitzers in 1976.^{7,8} That is, the FMS selling price was determined as 80% of their respective standard prices plus the cost of overhaul and test ammunition. Then, since FMS prices are subject to change, the FMS prices were parameterized to demonstrate how changes in selling price affect the potential revenue received.

5. Assumptions: It was assumed that:

a. The production schedule for XM204 Howitzers is feasible when considering the workload of the appropriate manufacturing facilities.

b. The XM204 Howitzer production and delivery schedules, the M101A1 and M102 Howitzer overhaul schedules, and the FMS delivery schedules shown in Tables A-1, A-2, A-3, and A-4 are valid for this analysis.

TABLE 4. POTENTIAL DISTRIBUTION OF ARMY 105MM HOWITZER ASSETS
FOR EACH ALTERNATIVE

	<u>Active Army</u>	<u>Reserves & National Guard</u>	<u>Totals</u>
<u>ALT 1:</u>			
XM204s	545	573	1,118
M102s	248	30	278
M101A1s	--	--	--
Total	<u>793</u>	<u>603</u>	<u>1,396</u>
<u>ALT 2:</u>			
XM204s	793	--	793
M102s	--	158	603
M101A1s	--	<u>445</u>	--
Total	<u>793</u>	<u>603</u>	<u>1,396</u>
<u>ALT 3:</u>			
XM204s	344	468	812
M102s	449	135	584
M101A1s	--	--	--
Total	<u>793</u>	<u>603</u>	<u>1,396</u>
<u>ALT 4:</u>			
XM204s	493	158	651
M102s	--	--	--
M101A1s	<u>300</u>	<u>445</u>	<u>745</u>
Total	<u>793</u>	<u>603</u>	<u>1,396</u>

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SUBJECT: XM204 Production Trade-Off Analysis .

c. For FMS, the M101A1 and M102 Howitzers will be delivered the same year in which they are overhauled.

d. Cost of the test ammunition for the overhauled M101A1 and M102 Howitzers is equal to the cost of test ammunition for the XM204 Howitzer.

e. The per unit production cost for the XM204 Howitzers is valid for production of 1,118 howitzers for ALT 1, as well as for production of lesser quantities of howitzers for ALT 2, 3 and 4.

f. The cost for IPF, initial provisioning and training, and publications for the XM204 Howitzers are applied equally to all four alternatives.

g. Transportation costs, estimated as 3% of the Hardware and Support (Engineering and Production) Costs of the new production of XM204 Howitzers, are applied equally to the M101A1, M102, and XM204 Howitzers.

h. Transportation costs for FMS will be paid by the foreign country and are, therefore, not included in the estimation of net revenues received from FMS of M101A1 and M102 Howitzers.

6. Data: The following data were used in this analysis:

a. Current Army assets of 105mm Howitzers (Table 1) are 745 M101A1 and 584 M102 Howitzers.

b. XM204 Howitzer production and delivery schedules, M101A1 and M102 Howitzer overhaul schedules, and FMS schedules for FY81 through FY87 (Tables A-1, A-2, A-3 and A-4).

c. FMS selling prices for overhauled M101A1 and M102 Howitzers (Table A-5) are \$31,193 and \$126,040, respectively.

d. Overhaul costs for M101A1 and M102 Howitzers⁹ (Table A-6) are \$12,820 and \$36,760, respectively.

e. XM204 Howitzer estimates are \$121.5K for new production costs per unit, \$6.29M for Initial Production Facilities (IPF), \$2.9M for initial provisioning and training, and \$3.4M for publications (Table A-7).

f. Estimated transportation cost is \$3.6K for the XM204 Howitzer, the M101A1 Howitzer, and the M102 Howitzer.

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7. Results: Table 5 displays the investment costs that would be incurred to procure and field XM204 Howitzers for each alternative. Production costs were calculated each year according to the number of howitzers produced (refer to production schedules in Tables A-1, A-2, A-3, and A-4). All costs were then discounted to constant FY77 dollars.

The costs of overhauling the M101A1 and M102 Howitzers in preparation for FMS customers are displayed in Table A-8. These overhaul costs would be paid out of the revenues obtained from the FMS customers. Figures 1, 2, 3 and 4 display the potential net revenues (total revenues (Figures A-1,A-2, A-3 and A-4) minus overhaul costs (Table A-9)) which could be received from FMS of M101A1 and M102 Howitzers for ALT 1, 2, 3 and 4, respectively. Each figure displays two curves (straight lines); one shows the potential net revenues obtained by selling M101A1 Howitzers, and the other shows the potential revenues obtained by selling M102 Howitzers.

In order to exemplify the use of the figures, two cases shall be discussed. In the two cases, different FMS selling prices will be used to show how revenue varies with selling prices. The selling prices used are:

	<u>M101A1</u>	<u>M102</u>
Case 1	~\$31K	~\$126K
Case 2	~\$97K	~\$ 97K

The values for Case 1 were determined as 80% of their respective standard prices plus the cost of overhaul and test ammunition (see Table A-5). The values for Case 2 were determined as 80% of new production costs of XM204 Howitzers. Net FMS revenues corresponding to the selling prices were obtained from Figures 1, 2, 3 and 4 and are displayed in Table 6.

TABLE 6. NET FMS REVENUE (\$M)
(In Constant Discounted FY77 Dollars)

	Quantity sold		Revenues for Case 1			Revenues for Case 2	
	M101A1	M102	M101A1 + M102 = TOTAL		M101A1 + M102 = TOTAL		
ALT 1	745	306	4.8	+ 13.0 = \$17.8M		28.5	+ 8.6 = \$37.1M
ALT 2	300	426	2.0	+ 18.6 = \$20.6M		12.2	+ 12.2 = \$24.4M
ALT 3	745	-	5.1	+ 0.0 = \$ 5.1M		30.4	+ 0.0 = \$30.4M
ALT 4	-	586	0.0	+ 26.0 = \$26.0M		0.0	+ 17.1 = \$17.1M

TABLE 5. XM204 HOWITZER FIELDING COSTS
 (In Constant Discounted FY77 Dollars)

ALT 1

XM204 Production (Qty = 1,118)	\$71.9M
Initial Production Facilities	4.6M
Initial Provisioning and Training	2.2M
Publications	2.4M
 TOTAL	 \$81.1M

ALT 2

XM204 Production (Qty = 793)	\$53.7M
Initial Production Facilities	4.6M
Initial Provisioning and Training	2.2M
Publications	2.4M
 TOTAL	 \$62.9M

ALT 3

XM204 Production (Qty = 812)	\$54.8M
Initial Production Facilities	4.6M
Initial Provisioning and Training	2.2M
Publications	2.4M
 TOTAL	 \$64.0M

ALT 4

XM204 Production (Qty = 651)	\$45.0M
Initial Production Facilities	4.6M
Initial Provisioning and Training	2.2M
Publications	2.4M
 TOTAL	 \$54.2M

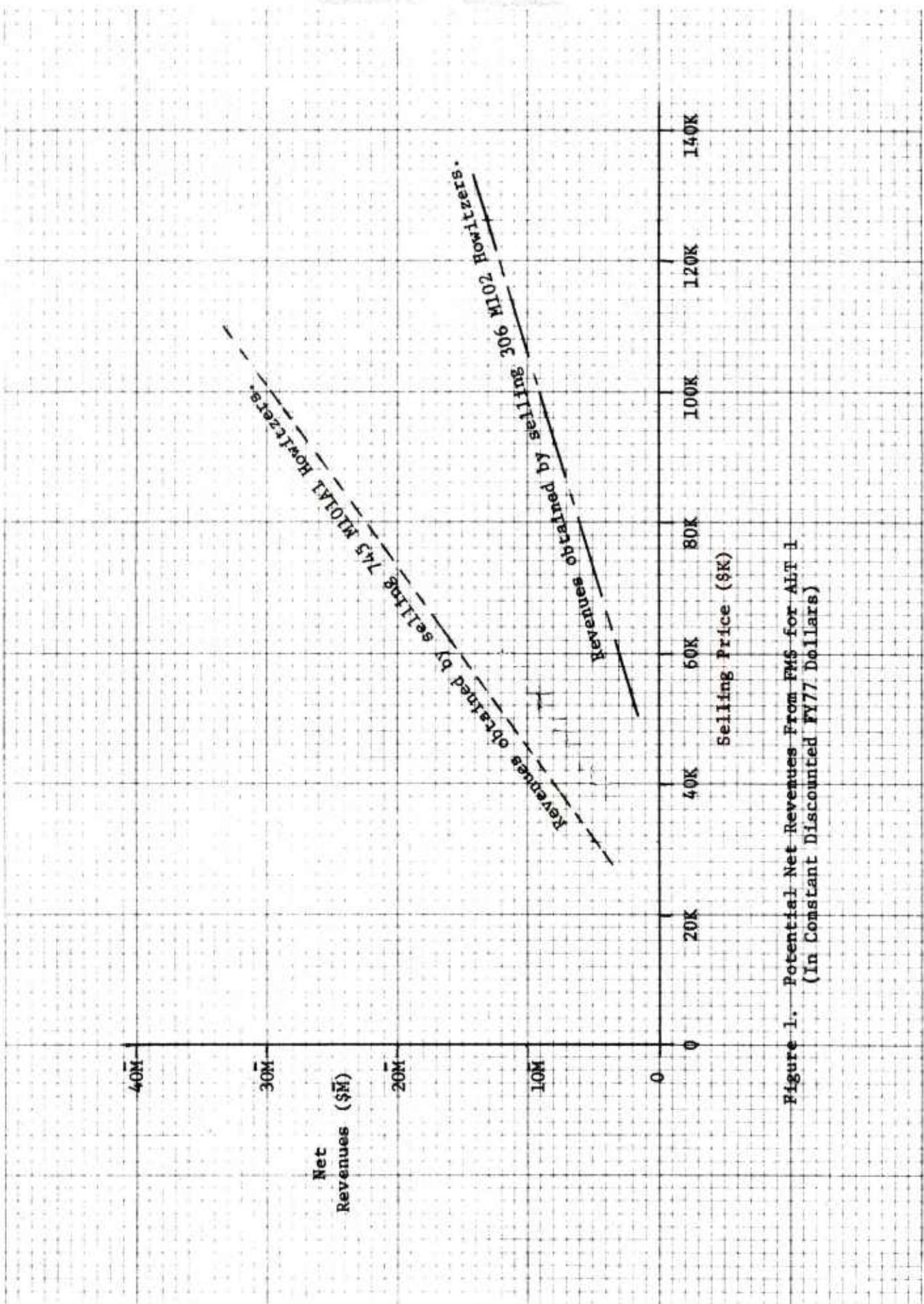


Figure 1. Potential Net Revenues From FMS for ALT 1
(In Constant Discounted FY77 Dollars)

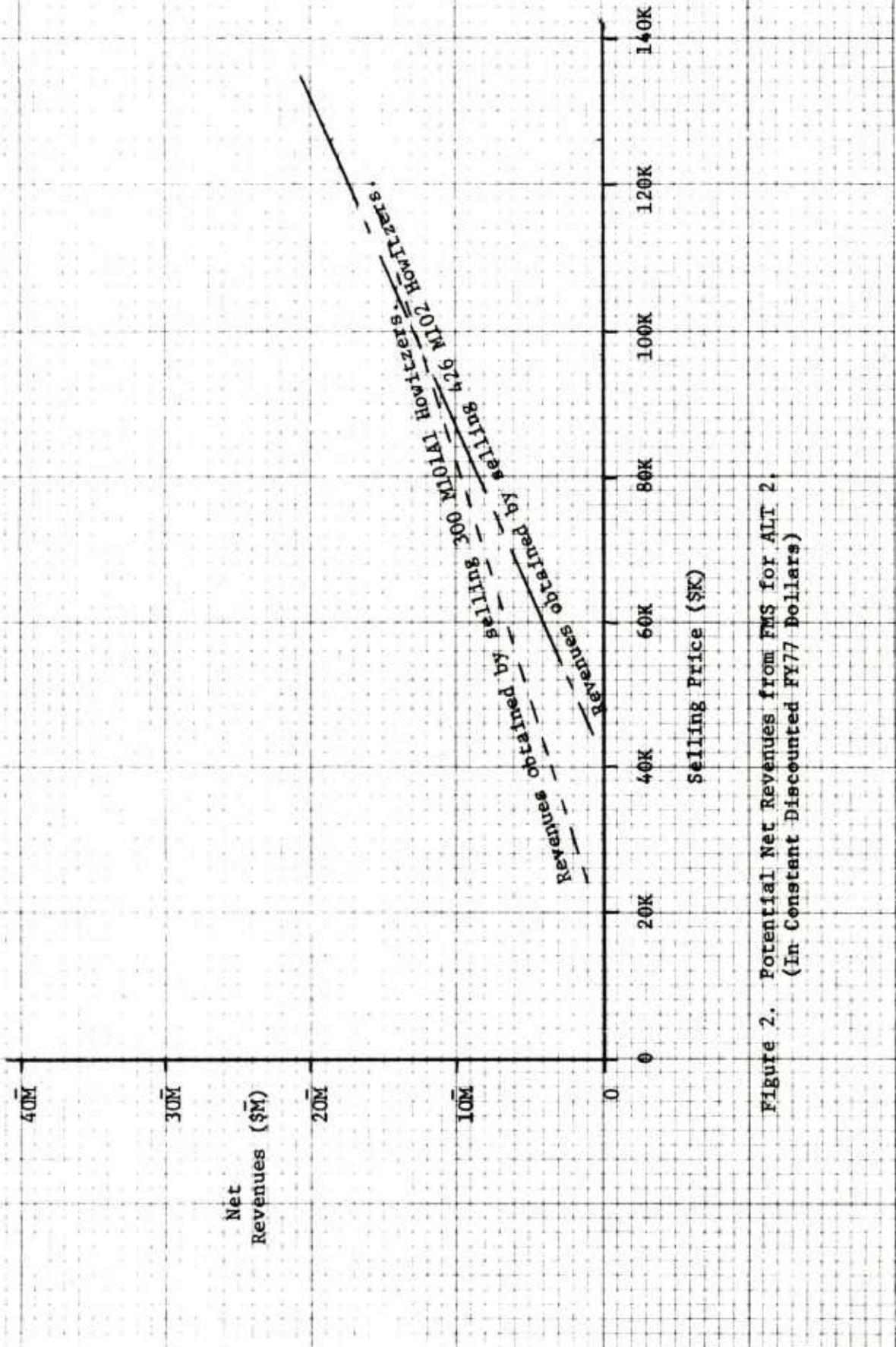


Figure 2. Potential Net Revenues from FMS for ALT 2
(In Constant Discounted FY77 Dollars)

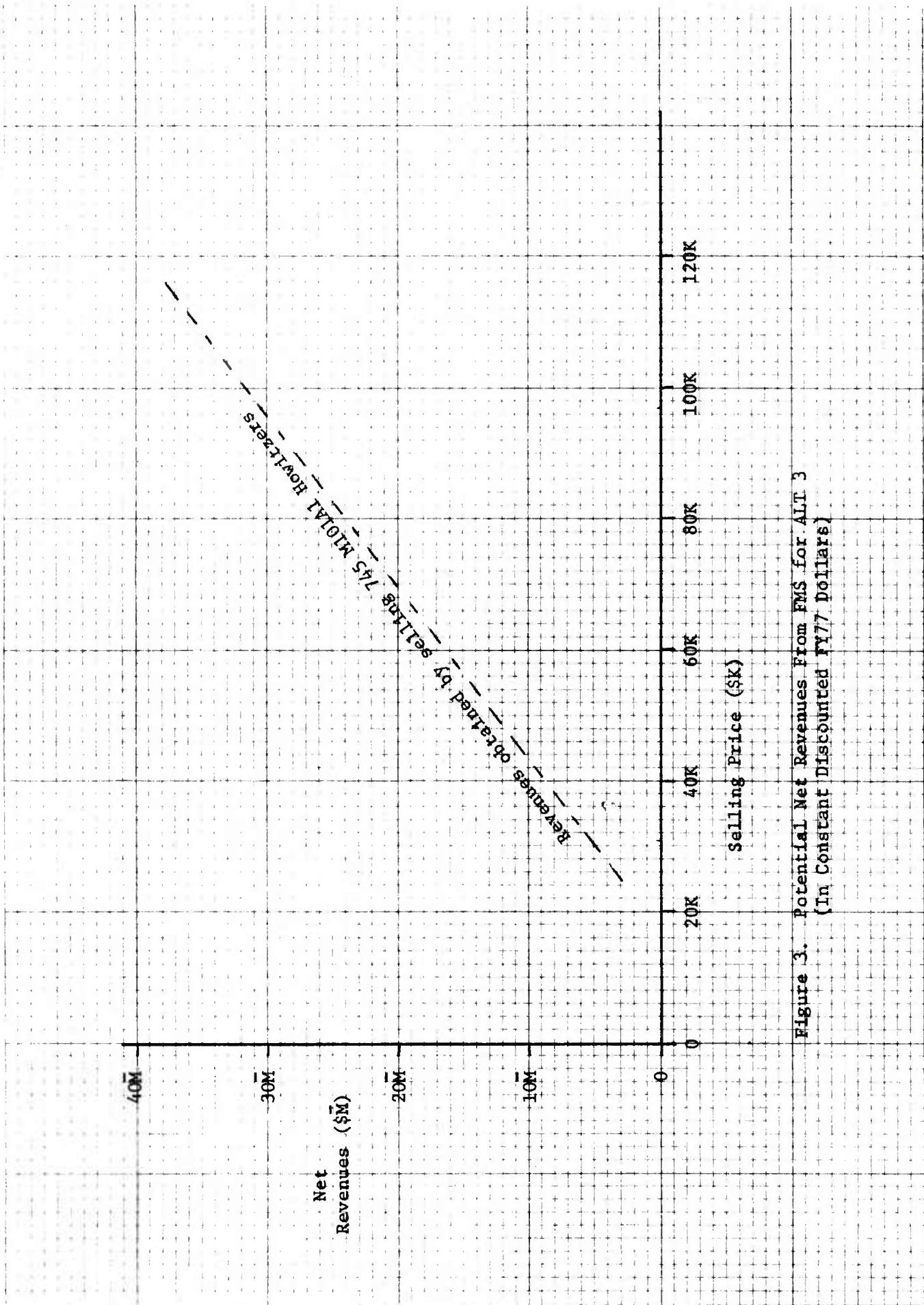


Figure 3. Potential Net Revenues From FMS For ALT 3
(In Constant Discounted FY77 Dollars)

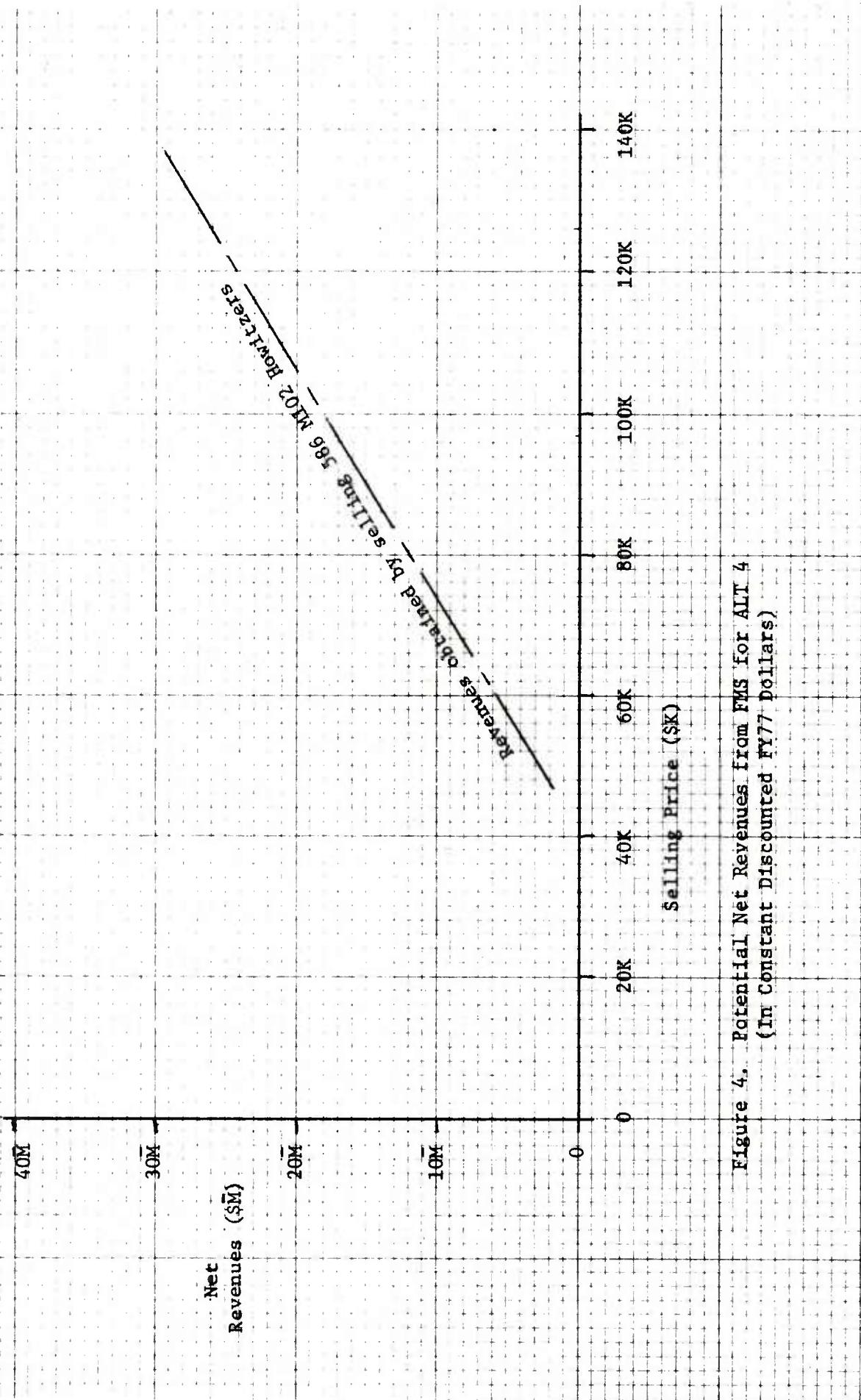


Figure 4. Potential Net Revenues from FMS For ALT 4
(In Constant Discounted FY77 Dollars)

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SUBJECT: XM204 Production Trade-Off Analysis

The net revenues shown in Table 6 would probably go to the US Government General Revenue Fund for subsequent Congressional appropriation. If these funds were reverted to the XM204 program, the net costs of each alternative could be calculated as is done in Table 7.

TABLE 7. ALTERNATIVE NET COSTS FOR XM204 HOWITZERS
(In Constant Discounted FY77 Dollars)

<u>Case 1:</u>	<u>ALT 1</u>	<u>ALT 2</u>	<u>ALT 3</u>	<u>ALT 4</u>
XM204 Fielding Costs	\$81.1M	\$62.9M	\$64.0M	\$52.2M
Net FMS Revenues	17.8	20.6	5.1	26.0
Net Costs	\$63.3M	\$42.3M	\$58.9M	\$26.2M

Case 2:

XM204 Fielding Costs	\$81.1M	\$62.9M	\$64.0M	\$52.2M
Net FMS Revenues	37.1	24.4	30.4	17.1
Net Costs	\$44.0M	\$38.5M	\$33.6M	\$35.1M

8. Summary: For each alternative plan of fielding XM204 Howitzers, the discounted investment costs were determined. These costs included Initial Production Facility (IPF) costs, production and transportation, initial provisioning and training, and publications. It was determined that:

- a. For ALT 1, if 1,118 XM204 Howitzers were produced and delivered to Active Army, Reserve, and National Guard units, an investment of \$81M will be required.
- b. For ALT 2, if 793 XM204 Howitzers were produced and delivered to Active Army units only, an investment of \$63M would be required.
- c. For ALT 3, if 812 XM204 Howitzers are produced and delivered to Active Army, Reserve, and National Guard units to replace all M101A1 Howitzers, an investment of \$64M would be required.

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d. For ALT 4, if 651 XM204 Howitzers were produced and delivered to Active Army, Reserve, and National Guard units to replace all M102 Howitzers, an investment of \$54M would be required.

For each of the four alternative plans addressed in this analysis, potential net revenues (total revenues minus overhaul costs) were calculated for the sale of overhauled M101A1 and M102 Howitzers to Foreign Military Sales (FMS) customers. Figures 1, 2, 3 and 4 display those net revenues for ALT 1, 2, 3 and 4, respectively.

According to current policy, the FMS selling price for overhauled M101A1 and M102 Howitzers would be ~\$31K and ~\$126K, respectively (Table A-5). At these selling prices, the potential net revenues which could be received for ALT 1, 2, 3 and 4 are \$18M, \$21M, \$5M, and \$26M respectively. It should be noted that potential revenues depend directly on the quantities of howitzers sold. For example, if M102 Howitzers could not be sold (say, for example, due to too high a price or low desirability), and only M101A1 Howitzers were sold, the potential net revenues for ALT 1, 2, 3 and 4 would be only \$5M, \$2M, \$5M, and \$0M respectively. Lastly, if different selling prices could be justified, the subsequent potential net revenues could be obtained from Figures 1, 2, 3 and 4 as demonstrated in this report.



NORMAN H. TRIER
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REFERENCES

1. DRDAR-XM DF to DRSAR-AS, subject: XM204 Review Project, dated 23 Mar 77.
2. DRSAR-AS DF to 9 Directorates, subject: 105mm Howitzer Production, dated 29 Mar 77.
3. DRSAR-MMH DF to DRSAR-AS, subject: 105mm Howitzer Production, XM204 (U), dated 27 Apr 77, classified CONFIDENTIAL.
4. Meeting between Mr. Aukland, DRSAR-MMH, and Mr. Trier, DRSAR-SA, subject: Quantity of M101A1 and M102 Howitzers in Reserves and National Guard, dated 28 Apr 77.
5. Army Materiel Plan Summary, 3 January 1977, Printout numbers G0180000M00, G0180100M00, G0180200M00, and G0180300M00. CONFIDENTIAL.
6. AR 11-28, Economic Analysis and Program Evaluation for Resource Management, dated 15 Jan 76.
7. FONECON, Mr. Aukland, DRSAR-MMH and Mr. Trier, DRSAR-SA, subject: Standard Price of M101A1 and M102 Howitzers and Determination of FMS Selling Price, dated 25 Apr 77.
8. DALO-ILP Message, 132055Z Sep 76. CONFIDENTIAL.
9. DRSAR-CPE DF to DRSAR-ASA, subject: 105mm Howitzer Production, XM204, dated 12 Apr 77.

TABLE A-1. SCHEDULES FOR ALTERNATIVE 1

	FY81	FY82	FY83	FY84	FY85	FY86	FY87	TOTAL
<u>AL-1:</u>								
XM204 production schedule ^a								
delivery sch.: Active Army ^b	8	50	168	288	288	316	--	1,118
Res. & Nat. Guard ^b	-	33	109	228	175	--	--	545
Overhaul sch.: Act. Army ^c	-	30	100	210	161	--	--	573
Res. & N.G.	-	--	--	--	108	290	152	550
M101A1: from Act. Army ^d	-	18	60	126	96	--	--	300
Res. & N.G.	-	--	--	--	87	235	123	445
M102 : from Act. Army ^d	-	12	40	84	65	--	--	201
Res. & N.G.	-	--	--	--	21	55	29	105
FMS Delivery sch.: M101A1 ^e	-	18	60	126	183	235	123	745
M102 ^e	-	12	40	84	86	55	29	306

^aObtained from MAJ Roddy, DRDAR-XM (RIA).

^bNumber of Howitzers delivered in a given year equals 1/2 of the number of XM204 Howitzers produced the prior year plus 1/2 of the number of XM204 Howitzers produced that same year. E.g., in FY83, the number of Howitzers delivered = $1/2(501 + 1/2(168)) = 109$.

^cThe overhaul schedule is calculated by multiplying the ratio of the number of M101A1 and M102 Howitzers replaced and the number of XM204 Howitzers fielded times the delivery schedule. E.g., for FY83, the number of Howitzers overhauled from the Active Army equals $(501 \div 545) \times 109 = 100$.

^dM101A1 Howitzers and M102 Howitzers are overhauled concurrently according to the ratio in which they are replaced in Active Army, and then in the Reserves and National Guard. E.g., the number of M101A1 Howitzers overhauled in FY83 equals $(300 \div 501) \times 100 = 60$; the number of M102 Howitzers equals $(201 \div 501) \times 100 = 40$.

^eFor FY83, the M101A1 and M102 Howitzers will be delivered the same year in which they were overhauled.

TABLE A-2. SCHEDULES FOR ALTERNATIVE 2

	FY81	FY82	FY83	FY84	FY85	FY86	FY87	TOTAL
<u>ALT 2:</u>								
XM204 Production Schedule	8	50	168	288	279	--	--	793
Delivery Schedule ^a	-	33	109	228	284	139	--	793
Overhaul Sch.: from Act. Army ^b	-	30	100	209	260	127	--	726
M101A1 ^c	-	12	41	86	108	53	--	300
M102 ^c	-	18	59	123	152	74	--	426
FMS Delivery Sch.: M101A1 ^d	-	12	41	86	108	53	--	300
M102 ^d	-	18	59	123	152	74	--	426

^aNumber of Howitzers delivered in a given year equals 1/2 of the number of XM204 Howitzers produced the prior year plus 1/2 of the number of XM204 Howitzers produced that same year. E.g., in FY83, the number of Howitzers delivered equals $1/2(50) + 1/2(168) = 109$.

^bThe overhaul schedule is calculated by multiplying the ratio of the number of M101A1 and M102 Howitzers replaced and the number of XM204 Howitzers fielded times the delivery schedule. E.g., for FY83, the number of Howitzers overhauled equals $(726 + 793) \times 109 = 100$.

^cM101A1 and M102 Howitzers are overhauled concurrently according to the ratio in which they are replaced. E.g., the number of M101A1 Howitzers overhauled in FY83 equals $(300 + 726) \times 100 = 41$: the number of M102 Howitzers equals $(426 + 726) \times 100 = 59$.

^dFor FMS, the M101A1 and M102 Howitzers will be delivered the same year in which they were overhauled.

TABLE A-3. SCHEDULES FOR ALTERNATIVE 3

	FY81	FY82	FY83	FY84	FY85	FY86	FY87	TOTAL
<u>ALT 3:</u>								
XM204 Production Schedule	8	50	168	288	288	10	--	812
Delivery Sch.: Active Army ^a	-	33	109	202	--	--	--	344
Res. & N.G. ^a	-	--	--	26	288	154	--	468
Overhaul Sch.: from Act. Army ^b	-	29	95	176	--	--	--	300
Res. & N.G. ^b	-	--	--	25	274	146	--	445
FMS Delivery Sch: M101A1 ^c	-	29	95	201	274	146	--	745

^aNumber of Howitzers delivered in a given year equals 1/2 of the number of XM204 Howitzers produced the prior year plus 1/2 of the number of XM204 Howitzers produced that same year. E.g., in FY83, the number of Howitzers delivered equals $1/2(50) + 1/2(168) = 109$.

^bThe overhaul schedule is calculated by multiplying the ratio of the number of M101A1 and M102 Howitzers replaced and the number of XM204 Howitzers fielded times the delivery schedule. E.g., for FY83, the number of Howitzers overhauled equals $(300 + 344) \times 109 = 95$.

^cFor FMS, the M101A1 and M102 Howitzers will be delivered the same year in which they were overhauled.

TABLE A-4. SCHEDULES FOR ALTERNATIVE 4

	FY81	FY82	FY83	FY84	FY85	FY86	FY87	TOTAL
<u>ALT 4:</u>								
XM204 Production Schedule	8	50	168	288	137	--	--	651
Delivery Sch.: Active Army ^a	-	33	109	228	123	--	--	493
Res. & N.G. ^a	-	--	--	--	90	68	--	158
Overhaul Sch.: from Act. Army ^b	-	30	99	208	112	--	--	449
Res. & N.G. ^b	-	--	--	--	77	58	--	135
FMS Delivery Sch: M102 ^c	-	30	99	208	189	58	--	584

^a Number of Howitzers delivered in a given year equals 1/2 of the number of XM204 Howitzers produced the prior year plus 1/2 of the number of XM204 Howitzers produced that same year. E.g., in FY83, the number of Howitzers delivered equals $1/2(50) + 1/2(168) = 109$.

^bThe overhaul schedule is calculated by multiplying the ratio of the number of M101A1 and M102 Howitzers replaced and the number of XM204 Howitzers fielded times the delivery schedule. E.g., for FY83, the number of Howitzers overhauled equals $(449 + 493) \times 109 = 99$.

^cFor FMS, the M101A1 and M102 Howitzers will be delivered the same year in which they were overhauled.

TABLE A-5. ESTIMATED FMS SELLING PRICE^{a,b}

M101A1 Howitzer:

80% of the standard price of \$21,254	=	\$17,003	
Overhaul cost ^c	=	12,820	
Test ammunition ^c	=	1,370	
FMS Selling Price		=	\$31,193

M102 Howitzer:

80% of the standard price of \$109,887	=	\$ 87,910	
Overhaul cost ^c	=	36,760	
Test ammunition ^c	=	1,370	
FMS Selling Price		=	\$126,040

^aMethod to compute FMS selling price and standard prices for the M101A1 and M102 Howitzers were obtained via FONECON between Mr. Aukland, DRSAR-MM and Mr. Trier, DRSAR-SA on 25 April 1977.

^bDALO-ILP MSG 132055z Sep 76 (C).

^cData obtained from DRSAR-CPE DF to DRSAR-ASA, subject: 105mm Howitzer Production, XM204, dated 12 April 1977. Cost of test ammunition for the M101A1 and M102 Howitzers was assumed equal to the cost of test ammunition that was estimated for the XM204 Howitzer.

TABLE A-6. OVERHAUL COSTS ESTIMATES FOR M101A1 AND M102 HOWITZERS^a
 (In Constant FY77 Dollars)

M101A1 OVERHAUL - Pron M17 OE 3020210H3

Labor	\$ 2,894.52
General & Administrative (G&A)	709.81
Indirect Maintenance Expense (IME)	2,447.98
Materiel	6,767.98
TOTAL	<u>\$12,820.29</u>

M102 OVERHAUL - Pron M16 DF 3010910H3

Labor	\$ 3,025.10
G&A	544.77
IME	2,834.59
Materiel	27,791.13
FY76 TOTAL	<u>\$34,195.59</u>
	x 1.0750
FY77 TOTAL	<u>\$36,760.20</u>

^aDRSAR-CPE DF to DRSAR-ASA, subject; 105mm Howitzer Production, XM204, dated 12 Apr 77.

TABLE A-7. UNIT AND PROGRAM COSTS OF THE XM204 HOWITZER^a
 (In Constant FY77 Dollars)

Per Unit Cost of XM204 Howitzer Production

Hardware and Support	\$120,123.20
Test Ammunition	1,370.35
	<hr/>
	\$121,493.65

	FY79	FY80	FY81
Initial Production Facilities	--	\$1.0M	\$5.29M
Initial Provisioning	\$0.4M	\$0.9M	\$1.6M
Publications	--	--	\$3.4M

^aDRSAR-CPE DF to DRSAR-ASA, subject: 105mm Howitzer Production, XM204, dated 12 Apr 77.

TABLE A-8. M101A1 and M102 HOWITZER OVERHAUL COSTS
 (In Constant Discounted FY77 Dollars)

	M101A1		M102	
	<u>Qty</u>	<u>Cost</u>	<u>Qty</u>	<u>Cost</u>
ALT 1	745	\$6.4M	306	\$ 6.5M
ALT 2	300	2.8M	426	9.2M
ALT 3	745	6.8M	-	-
ALT 4	-	-	586	12.9M

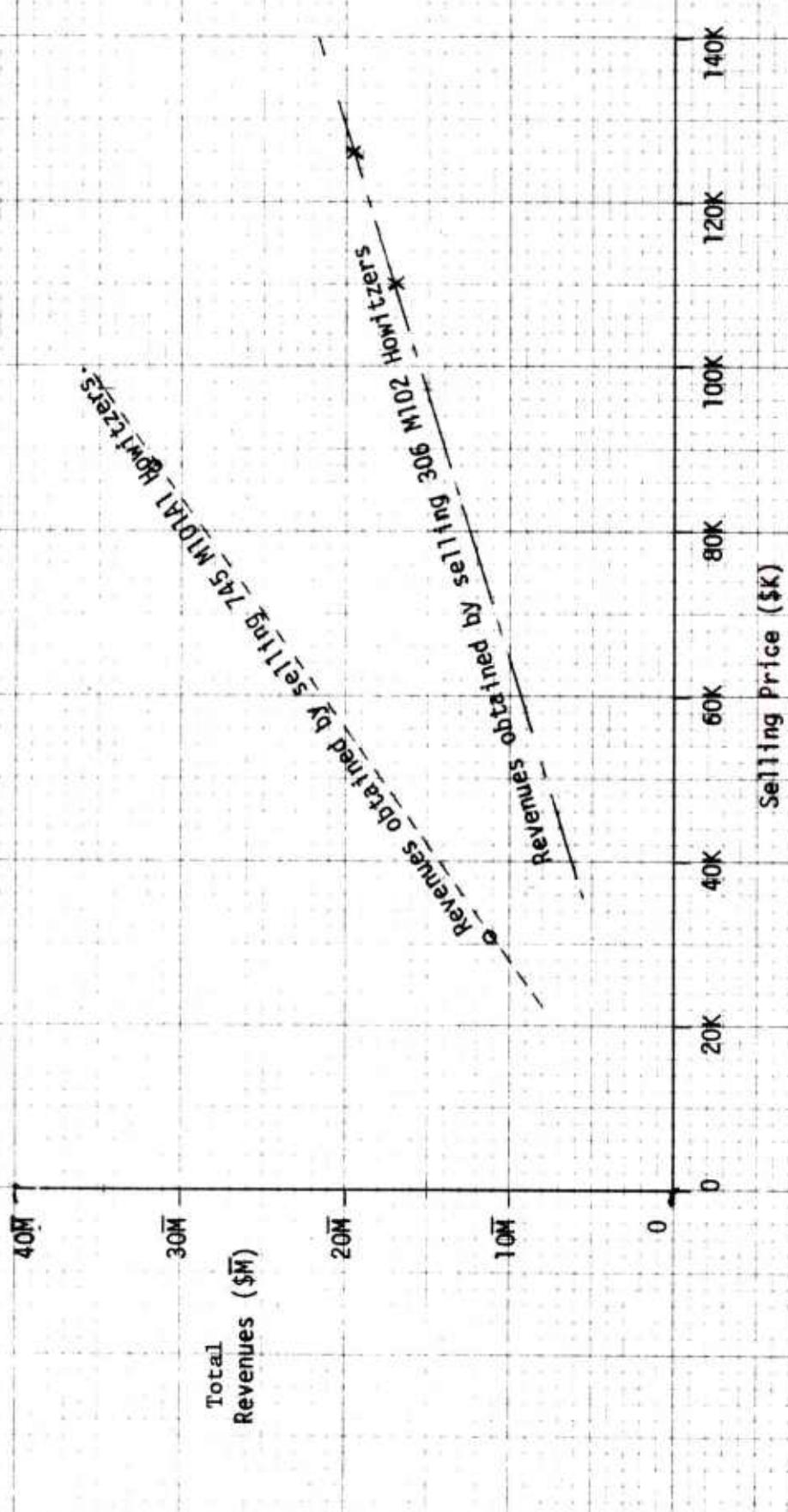


Figure A-1. Potential Revenues From FMS For ALT 1
(IN Constant Discounted FY77 Dollars)

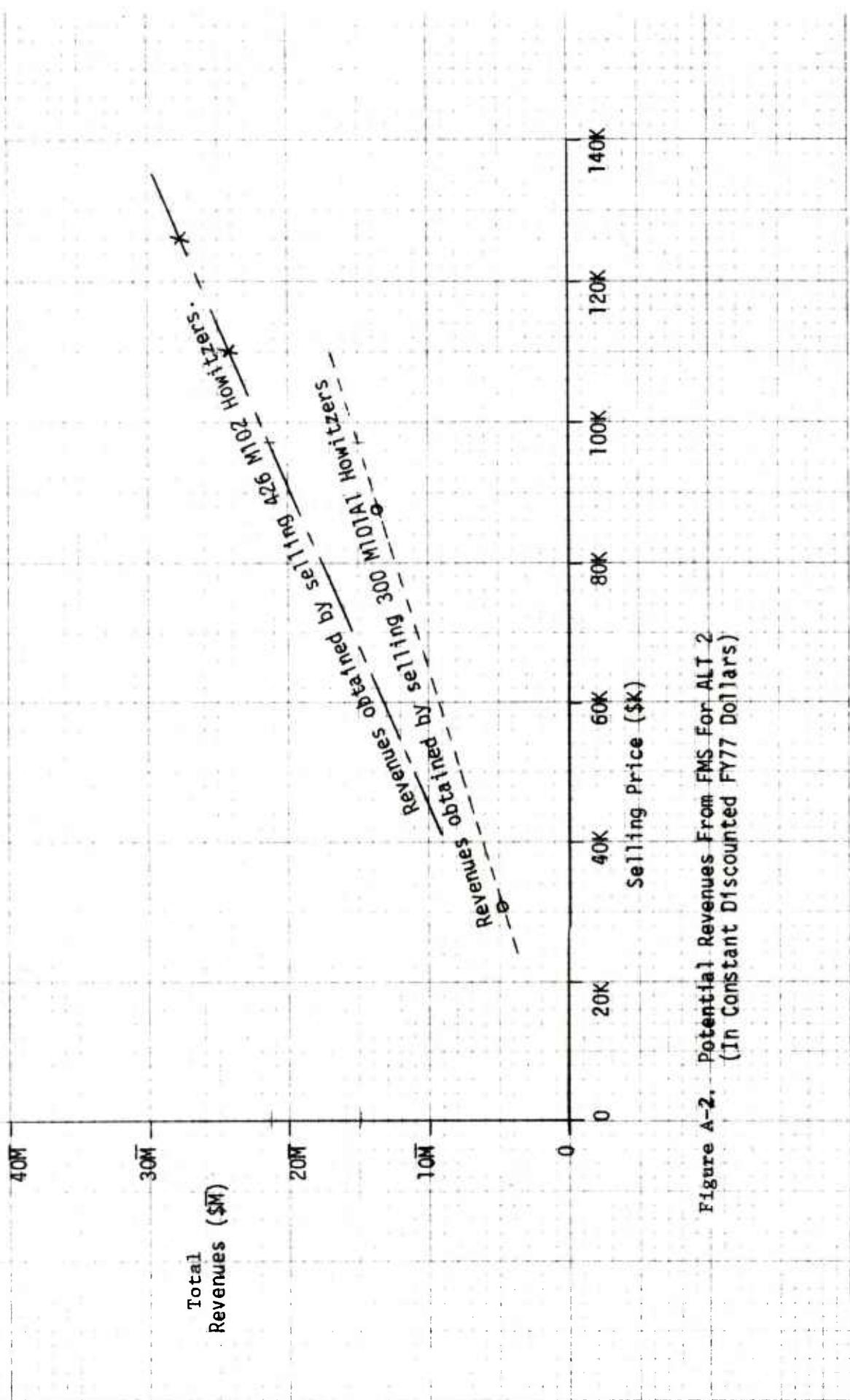


Figure A-2. Potential Revenues From FMS For ALT 2
(In Constant Discounted FY77 Dollars)

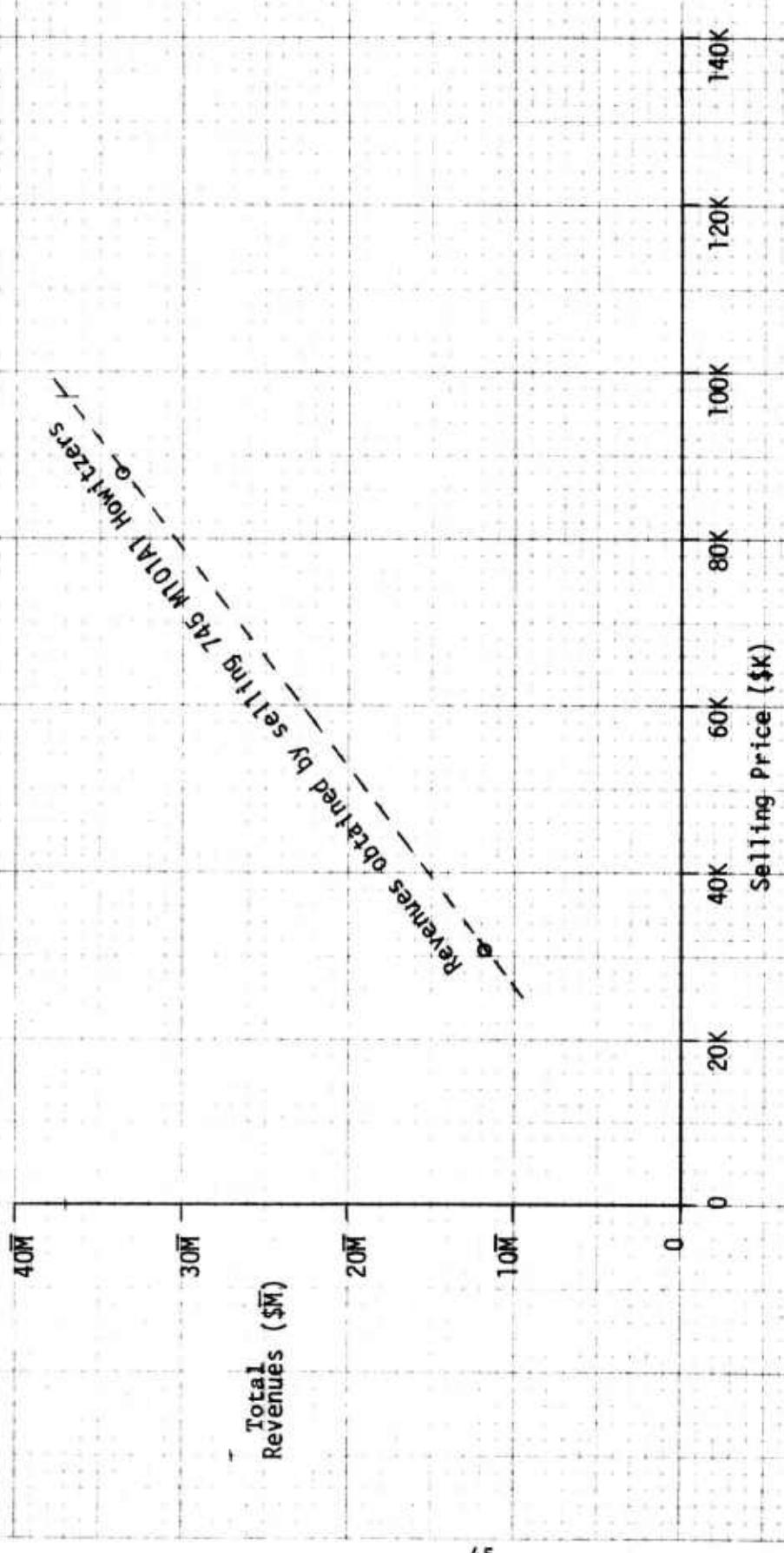


Figure A-3. Potential Revenues From FMS For ALT 3
(In Constant Discounted FY77 Dollars)

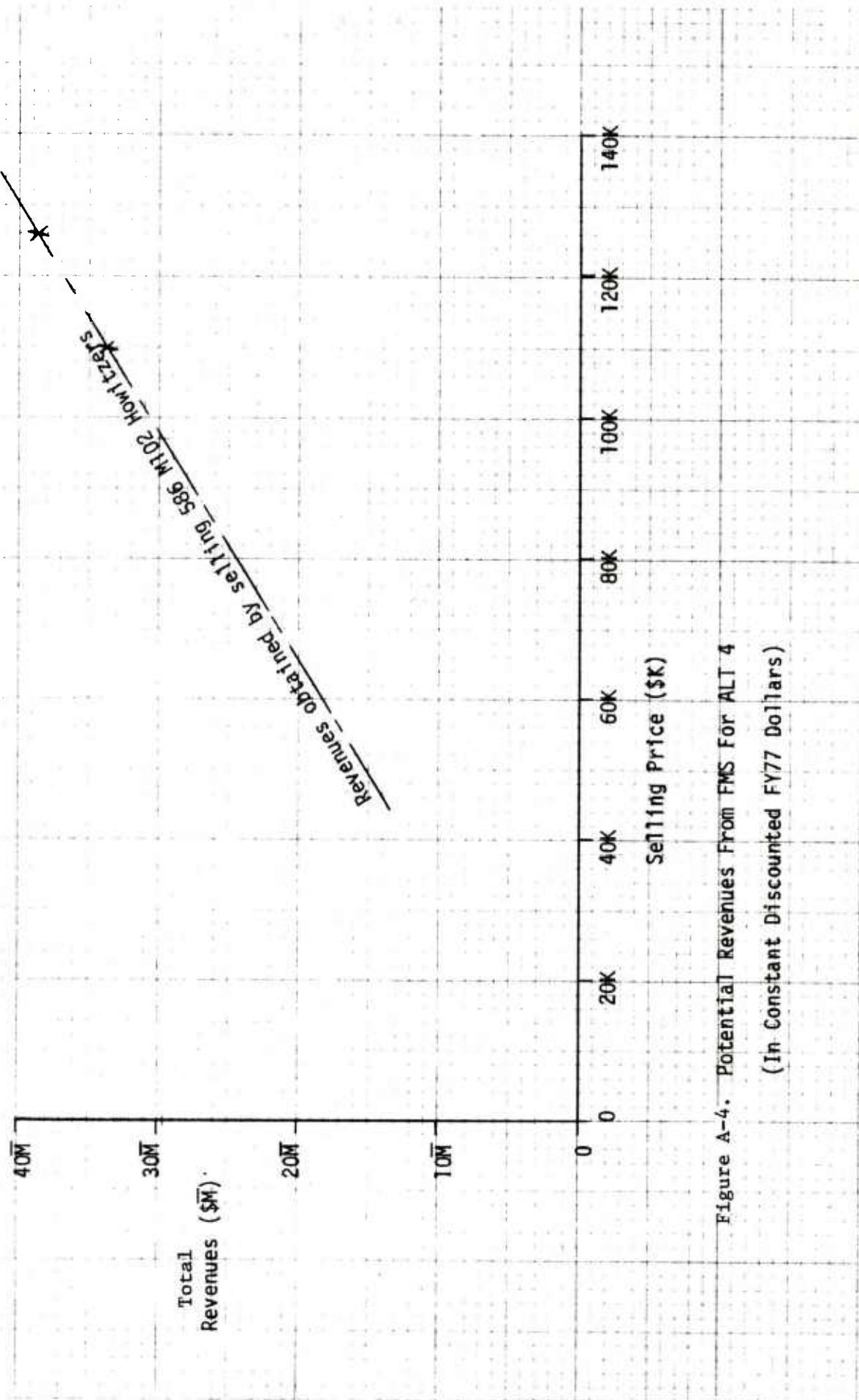


Figure A-4. Potential Revenues From FMS For ALT 4
 (In Constant Discounted FY77 Dollars)



DEPARTMENT OF THE ARMY
HEADQUARTERS, UNITED STATES ARMY ARMAMENT /MATERIEL READINESS
COMMAND
ROCK ISLAND, ILLINOIS 61201

REPLY TO
ATTENTION OF:

DRSAR-SAM

1 AUG 1977

SUBJECT: Analysis of Interior Ballistic Safety Test Data from the M110A1
Using the M188E1 Propelling Charge Subjected to Several Treatments

Project Manager
Cannon Artillery Weapons Systems
ATTN: DRCPM-M110E2 (Mr. B. Walters)
Rock Island, IL 61201

1. References:

a. Conversations between Mr. B. Walters (DRCPM-M110E2) and
Mr. G. Schlenker (DRSAR-SAM), during Jun 77, subject: firing safety of
the M188E1 propelling charge.

b. MFR, DRSAR-SAM, 29 Jul 77, subject as above (Incl 1).

2. Pursuant to your request (Ref a) to DRSAR-SA to investigate various aspects of a potential firing safety problem with the M188E1 propelling charge, this office has completed an analysis of the subject data and has formed certain conclusions. Details concerning the methods of analysis and findings are contained in the attached memorandum (Ref b). These conclusions have implications for technical management of the M188E1 charge to include product improvements and are given below.

3. The principal finding is that a significant statistical difference exists between the interior ballistics of sequentially rough handled charges (set A) and those which are not, i.e., all others (set B). A difference exists in the functional relationship between maximum chamber pressure, P_{max} , and chamber pressure differential, Δp . An additional difference was discovered in the probability distribution of the random variable Δp . Together these differences produce quite different risks of a catastrophic failure for sets A and B.

4. Based upon a goal for the failure rate of 10^{-6} , it is estimated that the rate for sequentially rough handled charges (set A) exceeds this goal by a factor of 64, at low temperatures and by a factor of 22 at high temperatures, whereas charges in set B meet this goal. It is inferred that certain physical changes, possibly defects, are produced in the M188E1 charge due to rough handling.

1 AUG 1977

DRSAR-SAM

SUBJECT: Analysis of Interior Ballistic Safety Test Data from the M110A1
Using the M188E1 Propelling Charge Subjected to Several Treatments

5. It is fair to assert that if the sequential rough handling procedure is representative of the treatment received in typical transportation and use, that this charge would fail to achieve its safety goal. In the light of the differences between the performance of charges in sets A and B and of defects discovered in a breakdown of rough-handled charges, it is recommended that the PM110E2 pursue the goal of identifying and remedying the physical causes for these differences.

6. Clearly, a product improvement must be initiated if the risk of a catastrophic failure is to be reduced to 10^{-6} . Until this improvement is accomplished and demonstrated, it is prudent to restrict the firing of M188E1 charges to those which demonstrably have not been rough handled. It is also recommended that a firing test program (to be defined) be conducted on future product-improved, unmodified charges which have been sequentially rough handled to assess the risk of failure in this charge. Inferences with respect to firing safety of a particular charge design drawn from a different charge are not warranted.

1 Incl (2 cy)
as

M. R. Hian
M. RHIAN
Director
Systems Analysis Directorate

CF:

CDR, ARRADCOM, ATTN: Mr. Costa, Dover, NJ 07801 w incl
Com/Dir, Ballistics Research Lab, ATTN: DRDAR-BLP (Dr. I. May), Aberdeen
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DRSAR-LEA, ATTN: Mr. C. Schneider w incl
DRSAR-EN, ATTN: Dr. Ambrosini w incl

29 JUL 1977

MEMORANDUM FOR RECORD

SUBJECT: Analysis of Interior Ballistic Safety Test Data from the M110A1 Using the M188E1 Propelling Charge Subjected to Several Treatments

1. References:

- a. Informal Test Data Sheets, acquired from DRCPM-M110E2, subject: Maximum Pressure Data DT II Test of the 8-Inch Howitzer, M188E1 Charge (Safety Phase).
- b. MFR, STEAP-MT-G, 11 Apr 77, subject: M188E1 Charge--Max Negative ΔP Results.
- c. MFR, DRSAR-SAM, 23 Jun 77, subject: Statistical Methods Pertinent to a Potential Ignition Problem in the M188E1 Propelling Charge.
- d. Extracts from a Presentation on Charge Safety by BRL Representatives: I. May, et.al., acquired from DRCPM-M110E2.

2. Background

The author was asked by the PM-110E2 to review a potential safety problem in the M110A1 SP howitzer when using the M188E1 propelling charge. A catastrophic failure of this system can occur if the maximum chamber pressure, p_{max} , exceeds a critical value, beyond which the base of projectile fails causing combustion gases to enter the warhead cavity. Of course, this potential problem is not unique to the M110 system; however, the quantification of risk of failure and causes of failure may be peculiar to this system. The latter details, discussed in this memorandum, are derived from the safety test data of Ref a.

3. During ignition and before shot start, the pressure waves within the combustion chamber produce a transient pressure difference between the

8 9 JUL 1977

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front and rear of the chamber. The maximum algebraic value of the front minus rear pressure differential, Δp , occurring during ignition has been found to correlate with p_{max} . Although random variation of p_{max} from round to round occurs at a constant value (level) of Δp , additional variation of p_{max} occurs due to the stochastic nature of Δp and the functional dependence of p_{max} on Δp .

4. The data of Ref a had previously been analyzed by STEAP-MT-G (Ref b) with the intention of discovering the relationship(s) between p_{max} and Δp and identifying the probability distribution function of the random variable Δp . Several candidate types of cumulative distribution functions (c.d.f.) on Δp were examined. Parameters for each type of c.d.f. were estimated from the data. Goodness-of-fit tests (Chi-squared and Kolmogorov-Smirnov) were applied; and, on the basis of minimum risk of error, it was concluded that the two-parameter Weibull distribution best fits the Δp data. The present analysis supports this conclusion. Within its scope the previous analysis appears to be well done. Additionally, Ref b indicated that further analysis would be conducted pending the acquisition of more firing data. It is noted that the only division or segregation of the data for analysis purposes made in Ref b was the separate analysis of cold (-50 deg F) and hot (145 deg F) temperature-conditioned charges. Although a variety of charge preconditions exist--secured cargo, temperature soak, sequential rough handling, and no special treatment--these data were pooled to assess the c.d.f. of Δp . The data from each of these charge treatments were treated discretely in our analysis, and a variety of powerful statistical tests applied.

5. One of the points made in this memorandum is that the aggregation of data from all charge treatments obscures important differences in the effect of treatment. Although it is not obvious from an initial

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inspection of the data, it will be shown that the type of treatment (charge precondition) affects not only the c.d.f. of Δp but the functional relation: $p_{max}(\Delta p)$. Since these relationships are essential ingredients to a risk analysis of the M110A1-M188E1 system, the risk of a catastrophic failure will be shown to depend upon charge treatment. This point is considered significant to possible future product improvement proposals (PIP's) to the M188E1 propelling charge. The author regards this memorandum as an extension of the analysis begun by DRSAR-SA and reported in Ref c. The primary thrust of Ref c is to suggest appropriate statistical tests and sample sizes for determining the effect of charge temperature on the distribution of Δp derived from tests of the standard, unmodified M188E1 propelling charge. By contrast, this memorandum is principally concerned with the exposition of information contained in extant data.

6. Purpose of this Analysis

There are several objectives for analyzing the data in Ref a in greater detail. First, it is desired to distinguish the effect of charge preconditioning treatment on the interior ballistic results. Second, there is a need to identify all interior ballistic variables to which p_{max} is functionally related. Third, there is a need for a statistical (mathematical) model suitable for predicting catastrophic failure of this system. The author feels that these objectives have been met and, as a by-product of the analysis, computer programs exist which can facilitate future analyses of this sort. These are contained in Annex 2.

7. Methodology

The data analyzed consist of values of p_{max} , Δp , and ignition delay, Δt , obtained by firing unmodified M188E1/Z9 propelling charges which had been subjected to a particular preconditioning treatment and then temperature conditioned prior to firing. Typically, approximately twenty to thirty charges of a given treatment were fired sequentially before changing to charges with a different treatment. For purpose of analysis each

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such homogenous batch was assigned a set number, for example, "secured cargo (cold)" is set C1. Shots on which one or more of the data items was lost were deleted from the sample.

8. The analysis performed on each of the sets and on various merged data sets consisted of the following:

- a. calculating marginal statistics, i.e., mean and standard deviation of p_{max} , Δp , and Δt .
- b. correlation analysis
 - (1) pairwise correlation coefficients of all of the variables
 - (2) point estimate of the slope of a simple (univariate) linear regression of p_{max} on Δp
 - (3) 95% confidence interval for (2)
 - (4) multiple linear regression treating p_{max} as a function of both Δp and Δt
 - (5) standard error of the estimate in (2) and conditional standard error in (4) above
- c. stepwise polynomial regression of:
 - (1) p_{max} on Δp
 - (2) p_{max} on Δt
- d. constrained quadratic regression of p_{max} on Δp with the constraint of positive slope for all Δp
- e. analysis of residuals of p_{max} - Δp regression
 - (1) calculation of median rank statistics and estimation of the c.d.f. of the residuals

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- (2) test for normality of the residuals using the Finkelstein-Schafer test* and Lilliefors (K-S) test.
- f. estimation and goodness-of-fit testing of the distribution of Δp
- (1) estimation of a negative exponential distribution function
- (2) estimation of the two parameters of a Weibull distribution by (a) matching moments and (b) maximum likelihood with estimation of the standard errors and 95% confidence intervals
- (3) calculation of the Finkelstein-Schafer test statistics using the above hypothesized distributions
- g. automatic plots of all regressions and all c.d.f.'s
- h. calculation of the risk of a catastrophic failure. The theory for this calculation is derived in Annex 1.

9. Results and Conclusions

The data from both low and high temperature tests show that p_{max} exhibits a great deal of random variation from shot to shot which is not explained by its dependence on either Δp or Δt , separately or jointly. For example, the results of the secured cargo (cold) test, set C1, with sample of 27, show an average value of p_{max} of 37.596 ksi with a standard deviation of 0.772ksi. Linear regressions of p_{max} on Δp and p_{max} on Δt show slopes that are not significantly different from zero at a reasonable level of risk. In fact, the standard error of the estimate of p_{max} given Δp is 0.786 ksi. In this case, essentially no information concerning p_{max} is obtained from knowledge of Δp or Δt . If one were to perform a quadratic regression of p_{max} on Δp (in spite of the lack of a significant linear dependence), the residuals would have a standard deviation of 0.757 ksi.

*The Finkelstein-Schafer test is a non-parametric goodness-of-fit test considerably more powerful than the modified Kolmogorov-Smirnov test. See Finkelstein, J.M. and Schafer, R.E., "Improved Goodness-of-fit Tests," Biometrika (1971), 58, 3, p. 641.

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Thus, the fraction of the variance explained by the quadratic regression is less than 4% in this case. Similar types of statistics for the cold (-50 deg F) tests are shown in Table 1. Table 2 displays the analytical results for the hot (145 deg F) tests. The identity of the various statistics shown in Tables 1 and 2 will be presently clarified. The results of the correlation analysis of p_{max} on Δt and of Δp on Δt are not shown in Tables 1 or 2 since these correlations are not statistically different from zero. Additionally, partial correlation coefficients of p_{max} on Δp , given Δt , and of p_{max} on Δt , given Δp , are not very different from the corresponding unconditional correlations. Stated differently, knowledge of Δt does not enhance the predictability of either p_{max} or of Δp . Because of its lack of predictive capability, Δt will not be discussed further.

10. Inspection of the data shows that the joint occurrence of exceptionally large values of Δp and p_{max} are derived from the charges preconditioned by sequential rough handling (seq. r.h.). This fact suggests that one pool the data selectively. Note that in both Tables 1 and 2 individual tests are analyzed separately and then progressively pooled or merged. For example in Table 2, the two secured cargo tests, sets H1 and H2, are merged and re-analyzed and then merged again with the hot cycle test, set H4, and analyzed again. Similarly, the sequential rough handling data, set H3 and set H5, is merged and analyzed as a single set.

11. Regression analyses of p_{max} on Δp at both cold and hot conditions show markedly different behavior between two different sets of data:
(A) those representing charges which have been preconditioned by sequential rough handling, and (B) all others, i.e., those not subjected to sequential rough handling. The slope of a linear regression for set A (or any subset) is significantly positive (at the 97.5% confidence level) whereas that from set B is not. This observation applies at both cold and

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hot conditions. This is seen from the results extracted from Tables 1 and 2 shown below in Table 3.

12. Additionally, stepwise polynomial regression performed on the $\Delta p - P_{max}$ data consistently shows that set A requires* a quadratic or cubic regression to best fit the data, whereas set B does not support any regression above a linear one for the cold condition with a possible quadratic for the hot condition. The most striking aspect of these regressions is that if quadratic regressions are chosen for both sets A and B, the fraction of the variance explained by the regression function (R^2) distinguishes the two sets. This point is illustrated in Table 4. Note that a relatively tiny portion of the variance is explained by the regression for set B (non-seq. r.h.)--less than 3%--whereas almost half the variance is explained by set A (seq. r.h.).** Another indication of the difference in the $P_{max}(\Delta p)$ relationship for sets A and B (or selected subsets) is obtained by applying constrained quadratic regression to both sets. For set A the positive slope constraint is not binding and the mean squared residual for the constrained analysis is identical to that of the unconstrained regression. By contrast, for both cold and hot

*In this context the word "requires" implies a minimum mean squared residual for the required degree of the polynomial. Additionally, the value of R^2 does not change appreciably with further increases in the degree.

**This distinction in R^2 between sets A and B could be caused by more frequent occurrences of large values of Δp in set A (rather than a difference in the $P_{max}(\Delta p)$ function). Then, assuming that P_{max} is a monotonically increasing function of Δp for both sets, a greater contribution to the variance of P_{max} would be made by the regression in set A. Were this hypothesis correct, one would also expect a greater variance of P_{max} from set A than from set B. In fact, this is not always the case. For the cold condition, the variance of set A is somewhat larger, with an F-statistic of 1.638, which is just significant at the 10% level; however, for the hot condition the F-statistic is 1.017 which is not plausibly significant at all. Therefore, this hypothesis is presently tenuous.

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conditions for set B a constrained regression produces a greater mean squared residual than the corresponding unconstrained value, suggesting a different functional form for set B than for set A.

13. Aside from the differences revealed in sets A and B by regression analysis, a distinction also appears in the c.d.f. of Δp . Analyzing the data from each preconditioning treatment separately showed that, at a 5% risk level, all of the sets were accepted by the Finkelstein-Schafer (F-S) test as Weibull in form with the two parameters β and η in the c.d.f.:

$$F(x) = 1 - \exp[-(x/\eta)^\beta], *$$

estimated (where feasible) by maximum likelihood. After pooling all seq. r.h. data at a given charge temperature to form set A, and all other data to form set B, re-estimation of β and η -- $\hat{\beta}$ and $\hat{\eta}$ with the larger samples also showed that the distribution of sets A and B were Weibull but have different parameter values. The parameter estimates and their standard errors are shown in Table 5. Assuming asymptotic normality and applying a two-sided t-test to the difference:

$$\hat{\beta}(\text{set B}) - \hat{\beta}(\text{set A}),$$

demonstrates that the Weibull shape parameter for set A (cold) is statistically distinguishable from that for set B (cold) with 99% confidence. Although the difference for the hot charge:

$$\hat{\beta}(\text{set B}) - \hat{\beta}(\text{set A})$$

is also positive, a t-test does not reveal a distinguishable difference.

14. However, for the cold charge condition, additional evidence of a difference in sets A and B with respect to the c.d.f. of Δp was obtained

*An alternative form of the distribution was also used:

$$F(x) = 1 - \exp - \lambda x^\alpha$$

with $\lambda = (1/\eta)^\beta$ and $\alpha = \beta$. Maximum likelihood estimates for α and λ and standard errors of $\hat{\alpha}$ and $\hat{\lambda}$ are found in Lloyd, D.K. and Lipow, R. Reliability (1962), pp. 177-181.

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by merging sets A and B, re-estimating parameters and applying the F-S test. For the pooled data, the test rejected the Weigull hypothesis at a 95% confidence level. All of the above evidence strongly suggests that sequential rough handling occasionally produces a change in the structure of the M188E1 propelling charge which affects both the probability distribution of Δp and the functional relation $p_{\max}(\Delta p)$.

15. Analysis of the residuals from a quadratic regression of p_{\max} on Δp by F-S and K-S tests (95% confidence) consistently showed a normal (gaussian) c.d.f. The standard deviation of residuals, σ_z , and the regression coefficients are shown in Tables 1 and 2. Using the theory of Annex 1, these parameters were used to estimate the probability of a catastrophic failure in the M110A1 - M188E1 system. This risk is equated to the probability that p_{\max} exceeds a critical value. The risks are shown in Table 6, in units of 10^{-6} , for sets A and B at both low and high temperature. Numerical uncertainty in the calculation of risk is shown under "integration relative error." This error is principally due to inaccuracy in the standard normal integral. Note that the critical value of p_{\max} was assigned two values--50 and 53 ksi. Doubtless there is some uncertainty in p_{\max} (critical) itself. This range in the critical value may be somewhat excessive but demonstrates the sensitivity of the risk to this parameter. Even for the larger value--53 ksi, which slightly exceeds an estimate by the BRL (Ref d)--the risk of failure is prohibitively large for charges which have been sequentially rough handled. For cold charges, where the risk is greatest, the probability of failure is 64 times the risk goal of 10^{-6} , using a critical pressure of 53 ksi.* However, without sequential rough handling the risk is substantially less than 10^{-6} .

*As a representative example of the wartime consequence of a failure rate of $64 \cdot 10^{-6}$ per shot, the following calculation is given. Suppose that an average of 200 weapons are operating in Europe for 90 days of combat. Let us suppose that the average consumption of M188 charges for this period is only 15 per weapon per day. Using these figures, about 17 catastrophic failures are expected in 90 days of combat.

TABLE 1. PARAMETER VALUES FOR RISK ASSESSMENT IN THE M110A1 5.P. HOW.
USING THE M188E1 PROP. CHARGE AT -50 DEG. F.

Case Description	Sample Size	Regression Params. (ks1/ks1 ⁿ)		$\hat{\alpha}_z$ (ks1)	$\hat{\beta}$ (ks1)	$\hat{\alpha}_1$ (ks1)	$\hat{\alpha}_2$ (ks1)	Resid. Mean Sqr. (ks1) and R^2 for Degree: 3	R^2	MS	R^2	Slope of Linear Reg. (ks1/ks1)	Slope (ks1/ks1)
		$\hat{\alpha}_0$	$\hat{\alpha}_1$										
seq. rough hand. (cold) 28 Jan, set C3	15	36.944	0.15531	0.13410	0.6307	0.8940	0.6846	0.4403	0.3190	0.4641	0.3373	0.4544	0.4053
seq. rough hand., sets C2 and C3	27	36.798	0.34983	0.030178	0.6227	0.6211	0.4688	0.4201	0.4201	0.4525	0.4205	0.4748	0.27
secured cargo (cold), set C1	27	37.344	1.0030	-0.52954	0.7568	1.0461	0.5226	0.6183	0.0021	0.6205	0.0385	0.6940	0.0548
cold soak (-50° F.), set C4	23	37.255	0.334472	-0.42884	0.5138	1.7586	0.5248	0.2904	0.0066	0.2680	0.1289	-0.95	0.76
no precond. (cold), set C5	10	37.768	-0.69356	-0.054821	0.4707	1.4711	0.6404	0.2494	0.3083	0.2848	0.3087	0.4164	-1.74
merge of sets C1, C4, C5	60	37.420	0.14045	-0.13593	0.6560	1.2750	0.5464	0.4389	0.0023	0.4455	0.0049	0.4529	0.0061
merged data from all cold tests, C1 - C5	87	37.238	0.061270	0.066785	0.6856	0.7930*	0.4902*	0.4844	0.1090	0.4813	0.1251	0.4869	0.1254

* The parameters from the merged data produce a distribution rejected by the Finklestein-Schafer test as not fitting the data.

TABLE 2. PARAMETER VALUES FOR RISK ASSESSMENT IN THE M10A1 S.P. HOW.
USING THE M1861 PROP. CHARGE AT 145 DEG. F.

Case Description	Sample Size	Regression Params. (ksi/ksi ^{1/2})			$\hat{\beta}$	σ_{E}	$\hat{\eta}$ (ksi)	Resid. Mean Sqr., (ksi) and R^2 for Degree:			95% Conf. Interval on Slope of Linear Reg. (km/km)			Slope of Linear Reg. (km/km)		
		\hat{a}_0	\hat{a}_1	\hat{a}_2				MS	R^2	MS	R^2	MS	R^2			
secured cargo (hot), set H1	26	42.393	-0.248854	0.306554	0.6701	1.278	0.1940	1.511		0.4881	0.0016			-0.28	0.23	-0.02
secured cargo (hot), set H2	21	42.586	-0.15656	0.034356	0.7401	1.128	0.1851	2.452		0.6086	0.0458			-0.17	0.31	0.07
seq. rough hand. (hot), set H3	12	42.528	-2.5825	1.6719	0.5112	1.783	0.4311	0.8204		0.3194	0.1871			-1.03	0.83	-0.10
hot cycle, set H4	29	42.070	-0.53518	0.17826	0.7013	1.310	0.1914	1.267	0.5455	0.0074	0.5297	0.0718		-0.25	0.39	0.07
seq. rough hand. (hot), set H5	17	42.005	0.18880	0.04820	0.5562	1.011	0.1923	1.348		0.3535	0.5327			0.20	0.67	0.43
secured cargo (hot), sets H1 + H2	47	42.507	-0.14951	0.033471	0.6981	1.200	0.1323	1.811	0.5091	0.0040	0.5095	0.0253		-0.13	0.20	0.03
seq. rough hand. (hot), sets H3 + H5	29	41.888	0.11657	0.067996	0.5839	1.081	0.1521	1.331		0.3672	0.4290	0.3617	0.4292	0.23	0.66	0.45
merge of sets H1, H2, H4 non-sec., r. h.	76	42.223	-0.11881	0.037625	0.7551	1.222	0.1065	1.570	0.5883	0.0111	0.5857	0.0287		-0.08	0.22	0.07
merged data from all hot tests, H1 - H5	105	42.118	-0.038302	0.040708	0.7341	1.176	0.0872	1.471		0.5495	0.0774	0.5520	0.0823	0.04	0.29	0.16

TABLE 3. COMPARISON OF REGRESSION ESTIMATES FROM TWO SETS OF M188E1 PROPELLING CHARGES HAVING DIFFERENT TREATMENTS

Set/ Treatment	Charge Temperature (deg F)			
	-50		145	
	slope (ksi/ksi)	95% C.I.	slope (ksi/ksi)	95% C.I.
Set A, seq. r.h.	0.50	0.27, 0.72	0.45	0.23, 0.66
Set B, non-seq. r.h.	-0.08	-0.51, 0.35	0.07	-0.08, 0.22

TABLE 4. FRACTION OF VARIANCE EXPLAINED BY A QUADRATIC REGRESSION OF PMAX ON DELP (R^2), DISTINGUISHED BY CHARGE TREATMENT

Set/ Treatment	Charge Temperature (deg F)	
	-50	145
Set A seq. r.h.	0.4525	0.4290
Set B non-seq. r.h.	0.0049	0.0287

TABLE 5. WEIBULL SHAPE PARAMETER FOR THE DISTRIBUTION FUNCTION OF ΔP STATISTICS, DISTINGUISHED BY CHARGE TREATMENT

Set/ Treatment	Charge Temperature (deg F)			
	-50		145	
	$\hat{\beta}$	$\sigma_{\hat{\beta}}$	$\hat{\beta}^*$	$\sigma_{\hat{\beta}}^*$
Set A, seq. r.h.	0.6211	0.132	1.081	0.152
Set B, non-seq. r.h.	1.275	0.154	1.222	0.106

*maximum likelihood estimates used

-

TABLE 6. RISK OF CATASTROPHIC
FAILURE IN THE M110A1-M188E1/Z9 SYSTEM

Set/ Treatment	Charge Temp (°F)	Crit p max (ksi)	Risk (10^{-6})	Integration Rel. Error
Set A, seq. r. h.	-50	50	134	0.026
		53	64	0.016
	145		22	$< 1.3 \cdot 10^{-3}$
Set B, w/o seq. r. h.	-50		0	$< 10^{-4}$
	145		0	$< 10^{-3}$

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16. Recommendations

In view of the statistical differences in interior ballistics observed between M188E1 charges which have been sequentially rough handled (set A) and those which have not (set B), it is recommended that the PM110E2 pursue the present testing program with a goal of identifying in detail the physical causes for the difference. The author recently was informed that defects such as torn propellant bags and cracked igniter tubes had been detected in rough handled charges. This physical evidence supports the conclusions based upon our analysis that physical (geometrical) changes occur due to sequential rough handling. Clearly, a product improvement must be initiated if the risk of a catastrophic failure is to be reduced to 10^{-6} . Until this improvement is accomplished and demonstrated, it is prudent to restrict the firing of M188E1 charges to those which demonstrably have not been rough handled. It is further recommended that a firing test program be conducted using unmodified, product-improved charges which have been sequentially rough handled to assess risk of failure. The present evidence suggests subtle effects on the c.d.f. of Δp and on the $p_{max}(\Delta p)$ relationship due to igniter/charge geometry. Therefore, inferences with respect to firing safety of a particular charge drawn from grossly altered or different charges are shakey at best.

George Schlenker

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ANNEX 1.

Probability that p_{\max} Exceeds a Critical Value

The risk of having a catastrophic failure of some sort in the system, e.g., inbore premature or breech blow, is equated to the probability that the maximum chamber pressure exceeds a critical value. Having investigated several alternative mathematical models for the random variable p_{\max} and having selected an optimum, one assumes that this model can be extrapolated to large values of Δp , i.e. that the statistics at extreme pressure have the same mathematical form as that determined for lower values. The necessary assumptions for the calculation of this risk are given below.

Assumptions

(1) In the standard M188E1 propelling charge subjected to the expected rough handling, the maximum chamber pressure depends only on the absolute negative pressure differential during ignition, i.e.,

$$p_{\max} = p_{\max}(\Delta p),$$

(2) The dependence in (1) is quadratic at every charge temperature.

(3) For any value of Δp , p_{\max} has an additive, random component which is normally (gaussian) distributed with mean zero and constant variance and is uncorrelated with Δp .

(4) The pressure differential, Δp , is stochastic having a two-parameter Weibull distribution.

(5) The critical value of p_{\max} is a constant, viz. 53 ksi.

Derivations

Notationally, let y be the dependent variable, x the independent variable-- Δp , in this case--and Z the gaussian noise. Then, the random variable Y is given by

$$Y = a_0 + a_1 X + a_2 X^2 + Z, \quad (1)$$

with X having the p.d.f. $f_X(x)$ and with Z having the p.d.f. $f_Z(z)$.

Notationally,

$$F_X(x) = \int_0^x f_X(u) du .$$

Using assumption (1), (2), and (3), the probability that Y is less than a particular value y is

$$\begin{aligned} P\{Y < y\} &= F_y(y) \\ &= P\{a_0 + a_1 X + a_2 X^2 + Z < y\} \end{aligned} \quad (2a)$$

$$F_y(y) = \int_{\text{all } x} P\{x < X < x + dx\} \cdot P\{Z < y - a_0 - a_1 x - a_2 x^2\}. \quad (2b)$$

$$F_y(y) = \int_0^\infty f_x(x) F_z(y - a_0 - a_1 x - a_2 x^2) dx. \quad (3)$$

By assumption (4),

$$f_x(x) = \frac{\beta}{n} \left(\frac{x}{n}\right)^{\beta-1} e^{-(x/n)^\beta} \quad (4)$$

Assumption (3) yields

$$F_z(z) = \frac{1}{\sqrt{2\pi} \sigma_z} \int_{-\infty}^z e^{-t^2/(2\sigma_z^2)} dt. \quad (5)$$

The risk of exceeding the critical value y_c is given from (3, 4, 5) as $1 - F_y(y_c)$. However, the above equations do not have an analytic solution. Therefore, numerical integration is employed using parameter values given in Table 1.

The integrand in equation (3):

$$g(x) = f_x(x) F_z(y - a_0 - a_1 x - a_2 x^2) \quad (6)$$

can be evaluated using existing subroutines. Integration of (3) is accomplished using the trapezoidal rule:

$$F_y \approx \frac{g(x_1)h}{2} + \frac{h}{2} \sum_{i=1}^n g(x_i) + g(x_{i+1}), \quad (7)$$

with step size h given by

$$h = \min (0.005 \sigma_z, 0.005 n) \quad (8)$$

with

$$x_1 = 0$$

and with truncation at x_n where

$$(x_n/n)^{\beta} > -\ln \epsilon$$

and where ϵ is the largest permissible error in the integrand. Generally, a suitable value of $\epsilon \sim 10^{-7}$.

Since the desired computational quantity is actually the risk ρ

$$\rho = 1 - F_y(y_c), \quad (9)$$

rather than first calculate $F_y(y_c)$ it is numerically more accurate to solve the following equation directly. From (3),

$$\rho = \int_0^\infty f_x(x)[1 - F_z(z)]dx \quad (10a)$$

with

$$z = y_c - \max(0, a_0 + a_1 x + a_2 x^2). \quad (10b)$$

The numerical approximation is

$$\rho \approx \frac{g'(x_1)h}{2} + \frac{h}{2} \sum_{i=1}^n g'(x_i) + g'(x_{i+1})$$

where

$$g'(x) = f_x(x)[1 - F_z(z)]. \quad (11)$$

Simultaneous integration of (3) via (7) provides an estimate of the integration error.

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ANNEX 2.

COMPUTER PROGRAMS USED IN A STATISTICAL ANALYSIS OF INTERIOR BALLISTIC SAFETY TEST DATA

Several source program listings are given in this annex. All programs are written in FORTRAN 4. The first main program and associated subroutines perform all of the analyses outlined in the body of this memorandum exclusive of constrained regression and risk analysis, which are listed separately. Comments provided in the listings indicate the program operations to be performed. The statistical analysis main program and subroutines require approximately 250 K bytes of core storage using the WATFIV diagnostic compiler with the IBM 360 system. A sample run consisting of the analysis of several data sets follows the program listing. Input control parameters are echoed in the output.

The second main program presented here performs a quadratic regression constrained to have positive slope for all values of the independent variable. Examples of program output follow the listing.

The third main program calculates the risk of a catastrophic failure in the M110A1-M188E1 system under the conditions implied by the input parameters. The algorithm of Annex 1 is employed in this calculation. Several examples are provided.

STATISTICAL ANALYSIS OF INTERIOR BALLISTIC DATA--PMAX, DELP, DELAY
UNITS: PMAX (KSI), DELP (PSI), DELAY (MS)

THIS PROGRAM CALCULATES THE MARGINAL STATISTICS AND CORRELATIONS OF THE MAX CHAMBER PRESSURE, PMAX, THE ABSOLUTE PRESSURE DIFFERENTIAL ACROSS THE CHAMBER, DELP, AND THE IGNITION DELAY. REGRESSION ANALYSES OF PMAX ON DELP AND OF PMAX ON DELAY ARE CALCULATED TO A PRESCRIBED DEGREE. AN ANALYSIS OF RESIDUALS FOR NORMALITY IS PERFORMED USING BOTH THE LILLIEFORS (K-S) TEST AND THE FINKELSTEIN-SCHAFER TEST. THE DATA ARE ORDERED FROM SMALLEST TO LARGEST FOR EACH VARIABLE AND SAMPLE C.D.F.'S ARE PRINTED AND PLOTTED. FINALLY, THE FINKELSTEIN-SCHAFER TEST IS APPLIED TO A BEST ESTIMATE OF THE PROBABILITY DISTRIBUTION FUNCTION OF DELP.

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C INPUTS:
C CARD 1      DESCRIPTIVE ALPHAMERIC TITLE
C CARD 2      SAMPLE SIZE, PLOT SWITCH, AND CRIT. VALUE AND RISK FOR F-S TEST
C CARD 3FF     ENTRIES IN THE DATA ARRAY: PMAX(I), DELP(I), DELAY(I), I=1..NSAMP
C OUTPUTS:
C 1.          MEAN VALUES
C 2.          STD. DEVS. OF PMAX, DELP, DELAY
C 3.          CORRELATION COEFS., LINEAR SLOPES, AND STD. ERRORS
C 4.          REGRESSION COEFFICIENTS ETC. FOR PMAX ON DELP AND PMAX ON DELAY
C 5.          ORDER STATISTICS FOR THE DISTRIBUTION FUNCTIONS OF DATA VARS.
C 6.          GOODNESS-OF-FIT TEST OF A PROPOSED DISTRIBUTION--DISTF--.
C           USING THE FINKLESTEIN-SCHAFFER TEST STATISTIC.
C           SEE PAGES 336 FF. MANN, N. ET AL. METHODS FOR STATISTICAL
C           ANALYSIS OF RELIABILITY AND LIFE DATA, C. 1974.

C DIMENSION TITLE(20),DATA(400,3),REGM(400,4),PMAX(400),DELP(400),
C 1 DELAY(400),COVM(3,3),RHO(3,3),SUM(9),CI(4),CJ(4),IVCHAR(10),
C EQUIVALENCE (DATA(1,1),PMAX(1)),(DATA(1,2),DELP(1)),
C 1 (DATA(1,3),DELAY(1))
C DATA ICHAR,ISTAR/0,**/,
C DATA IVCHAR/1,2,3,4,5,6,7,8,9,0/X/*
C 1 CONTINUE
C READ (5,10,END=3) TITLE
C 10 FORMAT (20A4)
C WRITE (6,12) TITLE
C 12 FORMAT (1H1,20A4)
C READ (5,14) NSAMP,IPLOT,NDEG,FSTST,FSRISK
C 14 FORMAT (3I3,1X,2F10.0)
C NDF1=NDFG+1
C IF (FSTST.EQ.0.0) FSTST=(FLOAT(NSAMP)/3.03)**0.37
C IF (FSTST.LT.0.0) FSTST=(FLOAT(NSAMP)/2.506)**0.383

C DEFAULT CRITICAL VALUES FOR THE F-S TEST ARE OBTAINED BY PROVIDING
C ZERO FOR A 10% RISK AND ANY NEGATIVE VALUE FOR A 5% RISK.
C THE ABOVE DEFAULT APPROXIMATIONS ARE GOOD FOR A SAMPLE GT. 6.

C WRITE (6,16) NSAMP,FSTST,FSRISK,NDEG
C 16 FORMAT (1H0,'SAMPLE = ',I3,' F-S CRITICAL VALUE = ',F10.3,4X,
C 1   ' F-S LEVFL OF RISK = ',F10.4,X,' DEG. U, POLY. REGRES. = ',I3)

C DATA INPUT SECTION
C READ DATA ARRAYS

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C DO 15 I=1,NSAMP
17   READ (5,17) PMAX(I),DELP(I),DELAY(I)
18   FORMAT (5,17)
19   IF (PMAX(I).GT.57.0.OR.DELAY(I).GT.1000..OR.DELP(I).GT.9000.) GO TO
20   14
21   15 CONTINUE
21   C END OF DATA INPUT SECTION
C
C CALCULATE MARGINAL STATISTICS
C
C FN=NSAMP
22   FN=NSAMP
23   DO 18 J=1,3
24   SUM(J)=0.0
25   DO 20 I=1,3
26   COVM(1,J)=0.0
27   RHO(I,J)=0.0
28   20 CONTINUE
29   18 CONTINUE
30   DO 22 J=1,3
31   DO 24 I=1,NSAMP
32   SUM(J)=SUM(J)+DATA(I,J)
33   24 CONTINUE
34   SUM(J)=SUM(J)/FN
35   22 CONTINUE
36   DO 26 J=1,3
37   DO 28 I=1,NSAMP
38   REGM(I,J)=DATA(I,J)-SUM(J)
39   28 CONTINUE
40   26 CONTINUE
C
C WRITE MEAN VALUES
C
C   WRITE (6,30) SUM(1),SUM(2),SUM(3)
41   30 FORMAT (1H0,3X,12HAVG PMAX,KSI,3X,12HAVG DELP,PSI,3X,
42   1 12HAVG TMODEL,MS/1H ,F15.4,2F15.1)
43   DO 32 I=1,3
44   DO 34 J=1,3
45   DO 36 K=1,NSAMP
46   COVM(I,J)=COVM(I,J)+REGM(K,I)*REGM(K,J)
47   36 CONTINUE
48   COVM(I,J)=COVM(I,J)/FLOAT(NSAMP-1)
49   34 CONTINUE
50   32 CONTINUE
51   DO 38 I=1,3
52   DO 40 J=1,3
53   RHO(I,J)=COVM(I,J)/FLOAT(NSAMP-1)
54   40 CONTINUE
55   38 CONTINUE
56   SUM(4)= SQRT(COVM(1,1))
57   SUM(5)= SQRT(COVM(2,2))
58   SUM(6)= SQRT(COVM(3,3))
59   FNP1=FLOAT(NSAMP+1)
60   FNM1=FLOAT(NSAMP-1)
C
C CALCULATE THE SLOPE OF A SIMPLE LINEAR REGRESSION OF PMAX ON DELP
C
C SLOPE=SUM((4)*RHO(1,2)/SUM(5)

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C CALCULATE THE STANDARD ERROR OF THE ESTIMATE OF PMAX, GIVEN DELP
C
C SEPMAX=SUM(4)*SQRT((1.-RHO(1,2)**2)*FNML/(FNML-1.))
62 C STD. DEV. OF THE SLOPE AND ASSOCIATED 95% CONFIDENCE INTERVAL
C
C SDSLOP=SEPMAX/SUM(5)/SQRT(FNML)
63 C
C CALCULATE THE T-STATISTIC AND 95% CONFIDENCE LIMITS
C
C NU=NSAMP-2
64 C
T=STUDENT(0.025*NU)
65 C
SLO=SLOPE-T*SDSL0P
66 C
SHI=SLOPE+T*SDSL0P
67 C
C CALCULATE PARTIAL CORRELATION COEFFICIENTS
C
C RY1G2=(RHO(2,1)-RHO(3,1)*RHO(3,2))/ SQRT((1.-RHO(3,1)**2)*
68 C (1.-RHO(3,2)**2))
RY2G1=(RHO(3,1)-RHO(2,1)*RHO(3,2))/ SQRT((1.-RHO(2,1)**2)*
69 C (1.-RHO(3,2)**2))
C
C RY1G2 IS THE PARTIAL CORRELATION OF PMAX ON DELP, GIVEN DELAY
C RY2G1 IS THE PARTIAL CORRELATION OF PMAX ON DELAY, GIVEN DELP
C
VDTDP=RY1G2**2
VDTOLY=RY2G1**2
70 C
71 WRITE ((6.42) *SUM(4)*SUM(5)*SUM(6)
72 WRITE ((6.42) *SUM(4)*SUM(5)*SUM(6)
73 42 FORMAT(1H0,2X,13HSD: PMAX*KSI*7X,8HDELAY,MS/IH,
1 3F15.4/1H0,*CORRELATION MATRIX:,1H0,1IX,4HMAX,11X,4HDEL,10X,
2 5HDELAY)
C
C WRITE CORRELATION MATRIX
C
C WRITE ((6.44) *((RHO(I,J)*J=1,3)*I=1,3)
74 C
44 FORMAT(1H *3F15.4)
75 C
76 WRITE ((6.43) *SLOPE,SEPMAX,SDSL0P,SL0,SHI,*
77 43 FORMAT(1H0,*ANALYSIS BASED ON SIMPLE LINEAR REGRESSION OF PMAX ON
1DELP:/1H0,*SLOPE =,F10.5,* KSI/IH0,*STD. ERR. OF EST. OF PMAX
2X GIVEN DELP =,F10.5,* KSI/IH0,*STD. DEV. OF SLOPE =,F10.5*X*
3.95% CONF. LIMITS: ,2F10.5,X,*T-STATISTIC (CRITICAL) =,F10.5)
78 C
79 45 FORMAT(1H0,*PARTIAL CORRELATION COEFS. WITH DEPENDENCE OF PMAX ON
IDELP AND DELY ASSUMED,/1H0,15H DELP. GIVEN DT,ISH DT, GIVEN DELP/
2 1H *2F15.4/1H0,*FRACTION OF VARIANCE DUE TO DELP =,F15.4/
3 1H0,*FRACTION OF VARIANCE DUE TO DELAY =,F15.4)
C
C FILL REGRESSION MATRIX FOR REGRESSION ANALYSIS OF PMAX ON DELP
C
C DO 48 J=1,NODEG
80 DO 50 I=1,NSAMP
81 PEGM(I,J)=(DELP(I))**
82 50 CONTINUE
83 48 CONTINUE
84 DO 52 I=1,NSAMP
85 PEGM(I,I)=PMAX(I)
86 52 CONTINUE
87

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88      C CALL MLR (RFGM,CI,400,4,NSAMP,NDP1,1,TRUE,RSQ)
C
C      C CALCULATE FRACTION OF VARIANCE EXPLAINED BY REGRESSION
C      C FRACT=RSQ
C
C      C WRITE REGRESSION COEFFICIENTS
C
C      C WRITE (6,54) (CI(J),J=1,NDP1)
C      54 FORMAT(1H0,REGRESSION COEFS. FOR PMAX ON UELP:'/1H0,9X,
C      1 6HZERO TH.10X,5HF1HST.12X,3H2NU.12X,3H3RD/1H ,4E15.5)
C      WRITE (6,56) FRACT
C      56 FORMAT(1H0,'FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION: '' ,
C      1 F15.5)
C
C      C CALCULATE, SORT, AND PRINT (PLOT) THE RESIDUALS
C
C      C RMAX=-1.E20
C      94     RMIN=1.E20
C      95     SR=0.
C      96
C      97     SSK=0.
C      DO 57 I=1,NSAMP
C      98     REGM(I,1)=PMAX(I)-CI(I)
C      99     DO 59 J=2,NDP1
C      100    REGM(I,1)=REGM(I,1)-C1(J)*UEL(I)**(J-1)
C      59    CONTINUE
C      101    SR=SR+REGM(I,1)
C      102    SSR=SSR+(REGM(I,1))**2
C      103    IF (REGM(I,1).GT.RMAX) RMAX=REGM(I,1)
C      104    IF (REGM(I,1).LT.RMIN) RMIN=REGM(I,1)
C      105    CONTINUE
C      106    SR=SR/FN
C      107    SSR=SQR((SSR/FN-SR)**2)*FN/FN)
C      108    IF (IPLOT.EQ.1) CALL PSCALE(1,1,RMIN,RMAX,XMIN,XMAX)
C      109    IF (IPLOT.EQ.1) CALL GPPLT(1,XMIN,XMAX,0.,1.)
C      110    NM1=NSAMP-1
C      111    DO 159 I=1,NM1
C      112    IP1=I+1
C      113    DO 160 II=IP1,NSAMP
C      114    IF (REGM(I,1).LE.REGM(II,1)) GO TO 161
C      115    HOLD=REGM(I,1)
C      116    REGM(I,1)=REGM(II,1)
C      117    REGM(II,1)=HOLD
C      118    REGM(II,1)=HOLD
C      119    CONTINUE
C      120    CONTINUE
C      121    CONTINUE
C      122    CONTINUE
C
C      C END OF SORT OF RESIDUALS
C
C      C WRITE (6,162)
C      123   FORMAT(1H1,DISTRIBUTION OF RESIDUALS FROM PMAX-DELP REGRESSION'/
C      1 1H0,5HINDEX,10H RESID,KS1,10H MED RANK,10H NORM D.F.,
C      2 5X,5HSTAR,5X,5HSTAR)
C
C      C INITIALIZE LILLIEFORS TEST STATISTIC AND CALCULATE THE CRITICAL VALUE
C
C      C SRFNP1=SQR(FLOAT(NSAMP+1))
C      125   IF (FSRISK.LE.0.01) CLFOR5=1.04/SRFNP1
C      126   IF (FSRISK.FG.0.05) CLFOR5=0.881/SRFNP1
C      127

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28 IF (FSRISK .GT. 0.1) CLFURS=0.805/SRFNP1
29 TLFORS=0.0
30 SSTAR=0.0
31 DO 163 I=1,NSAMP
32 Y=FLUAT(1,I)/FNP1
33 X=XEGM(1,1)
34 Z=SNORM((X-SR)/SSR)
35 F1=FLOAT(1)/FN
36 F2=FLOAT(1-1)/FN
37 T1=F1-2
38 T2=Z-F2
39 DSTAR=AMAX1(T1,T2)
40 IF (DSTAR.GT.TLFORS) TLFORS=DSTAR
41 SSTAR=SSSTAR+AES(DSTAR)
42 IF (IPLOT.EQ.1) CALL GPLOD1(X,Y,ISTAR)
43 WRITE(6,164) I*X*Y*Z*DSTAR,SSTAR
44 FORMAT(1H ,15.5F10.4)
45 163 CONTINUE
46 IF (SSTAR.GT.FSTST) GO TO 175
47 WRITE(6,180) SSTAR,FSTST
48 180 FORMAT(1H0,'RESIDUALS ARE PLAUSIBLY GAUSSIAN.'//1H0,
1 'SSTAR IN F-S TEST.',F10.4,' IS LESS THAN THE CRITICAL VALUE.',/
2 F10.4)
49 GO TO 172
50 175 CONTINUE
51 WRITE(6,182) SSTAR,FSTST
52 182 FORMAT(1H0,'RESIDUALS ARE NOT PLAUSIBLY GAUSSIAN.'//1H0,
1 'SSTAR IN F-S TEST.',F10.4,' EXCEEDS THE CRITICAL VALUE.',/F10.4)
53 172 CONTINUE
54 1F (TLFORS.GT.CLFORS) GO TO 184
55 WRITE(6,190) TLFORS,CLFORS,FSRISK
56 190 FORMAT(1H0,'LILLIEFORS (K-S) TEST SHOWS RESIDUALS ARE GAUSSIAN.'/
1 H , 'TEST STATISTIC ',F10.4,' IS LESS THAN THE CRITICAL VALUE ',
2 F10.4,' WITH A RISK OF ',F10.4)
57 GO TO 173
58 184 CONTINUE
59 WRITE(6,192) TLFORS,CLFORS,FSRISK
60 192 FORMAT(1H0,'LILLIEFORS (K-S) TEST SHOWS RESIDUALS ARE NOT GAUSSIAN
1 , '1H , 'TEST STATISTIC ',F10.4,' IS GREATER THAN THE CRITICAL VALUE
2E , 'F10.4,' WITH A RISK OF ',F10.4)
61 173 CONTINUE
62 WRITE(6,165) SR,SSR
63 165 FORMAT(1H0,'MEAN AND STD. DEV. OF RESIDUALS (KSI) :',2F15.5)
64 IF (IPLOT.NE.1) GO TO 170
65 WRITE(6,166)
66 166 FORMAT(1H1,'PLOT OF CUMULATIVE DISTRIBUTION FUNCTION OF PMAX RESID
UALS.')
67 CALL GPPRNT
68 170 CONTINUE
C   FILL REGRESSION MATRIX FOR REGRESSION OF PMAX ON DELAY
C   C
69 00 58 J=1,NDERG
70 DO 60 I=1,NSAMP
71 REGM(I,J)=(NFLAY(1))**J
72 60 CONTINUE
73 58 CONTINUE
74 DO 62 I=1,NSAMP

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I75      REGM(I,NOP1)=PMAX(I)
I76      CONTINUE
I77      CALL MLR( REGM,CJ,400,4,NSAMP,NOP1,1,TRUE,S,RSQ )
I78      C
C      WRITE REGRESSION COEFFICIENTS
C
I79      WRITE (6,64) (C(J,J),J=1,NDPI)
I80      64 FORMAT(1H0,REGRESSION COEFS FOR P MAX ON UELAY::1H0,9X,
I     1 6HZERO,I12X,5HFIRST,I2X,3H2ND,I2X,3H3RD/I4,4E15.5)
I81      C      WRITE (6,56) FRACT
C
C      PRESERVE UNSORTED DATA
C
I82      DO 19 I=1,NSAMP
I83      REGM(I,1)=PMAX(I)
I84      REGM(I,2)=DELP(I)
I85      REGM(I,3)=DELAY(I)
I86      19 CONTINUE
C
C      REGRESSION ANALYSIS COMPLETE; NOW SORT DATA
C
I87      NM1=NSAMP-I
I88      00 66 J=1,3
I89      DO 68 I=1,NM1
I90      IPI=I+I
I91      00 70 II=IPI,NSAMP
I92      IF (DATA(I,J).LE.DATA(II,J)) 60 TU 72
I93      HOLD=DATA(I,J)
I94      DATA(I,J)=DATA(II,J)
I95      DATA(II,J)=HOLD
I96      72 CONTINUE
I97      70 CONTINUE
I98      68 CONTINUE
I99      C      END OF I LOOP
C
C      66 CONTINUE
C
C      END OF VARIABLES (JJ)-LOOP AND END OF SORT
C
C      WRITE SORTED STATISTICS
C
I200     WRITE (6,74)
I201     74 FORMAT(1H0,5HINDEX,10H MED RANK,7X,8HPMAX,KSI,7X,8HDEL,P,PSI,
I     1 7X,8HOFLAY,MS)
I202     00 78 I=1,NSAMP
I203     RANK=FLUAT(I)/FLOAT(NSAMP+I)
I204     WRITE (6,76) I,RANK,PMAX(I),DEL(P(I),DELAY(I))
I205     76 FORMAT(1H,2X,13,F10.4,F15.4,2F15.2)
I206     78 CONTINUE
I207     SSTAR=0.0
I208     FN1=NSAMP+I
I209     IF (IPLOT.NE.I) GO TO 94
C
C      PLOT REGRESSION FUNCTION AND DATA OF PMAX ON DELP
C
C      DETERMINE PLOT LIMITS
C

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C      CALL PSCALF(1,1,0.,DELFP(NSAMP),XMIN,XMAX)
210     CALL PSCALF(3,2,PMAX(I),PMAX(NSAMP),YMIN,YMAX)
211     CALL GPPLOT(2,XMIN,XMAX,YMIN,YMAX)
212     X=0.0
213     DX=DELFP(NSAMP)/100.
214
215     DO 71 I=1,100
216       X=X+DX
217       Y=0.0
218       DO 171 J=1,NDP1
219         Y=Y+CI(J)*X**(J-1)
220         CONTINUE
221         CALL GPL0D1(X,Y,ICHAR)
222         71 CONTINUE
223
224       LOAD SECOND LAYER
225       DO 73 I=1,NSAMP
226         X=REGM(I,2)
227         Y=REGM(I,1)
228         CALL GPL0D2(X,Y)
229         73 CONTINUE
230
231       PLOT OUT REGRESSION
232       WRITE(6,75)
233       75 FORMAT(1H1,'REGRESSION OF PMAX ON DELP')
234       CALL GPCONV(IVCHAR,10)
235       CALL GPPRNT
236
237       PLOT REGRESSION FUNCTION AND DATA OF PMAX ON DELAY
238       DO 77 I=1,100
239         X=X+DX
240         Y=0.0
241         DO 177 J=1,NDP1
242           Y=Y+CI(J)*X**(J-1)
243           CONTINUE
244           CALL GPL0D1(X,Y,ICHAR)
245           77 CONTINUE
246
247       LOAD SECOND LAYER
248       DO 79 I=1,NSAMP
249         X=REGM(I,3)
250         Y=REGM(I,1)
251         CALL GPL0D2(X,Y)
252         79 CONTINUE
253
254       PLOT OUT REGRESSION
255       WRITE(6,81)

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      H1 FORMAT(1H0,'REGRESSION OF PMAX (KS1) ON DELAY (MS) .')
      CALL GPCNIV(LVCHAR,10)
      CALL GPRINT
      CALL PSCALE(1.0,1.0,0.0,DEL((NSAMP)),XMIN,XMAX)

C PROVIDE CONTROL INFORMATION FOR PLOTTING
C CALL GPPLT(1.0,XMAX,0.0,1.0)

C ESTIMATE THE PARAMETERS OF THE C.D.F. OF DELP
C CALL DIST1(SUM(2)*SUM(5)*NSAMP,DELP)

C LOAD THE PLOT CHARACTERS FOR THE CDF INTO A PLOTTING ARRAY
C

C X=0.0
C DX=DEL((NSAMP))/100.
C DO 93 1=1,100
C   X=X+DX
C   CALL DISTF(X,Y)
C   CALL GPLOD1(X,Y,1CHAR)
C   93 CONTINUE
C   94 CONTINUE

C APPLY THE FINKLESTIN-SCHAFFER TEST AND LILLIEFOR'S (K-S) TEST
C WRITE HEADINGS
C

C WRITE (6,90)
C 90 FORMAT(1H0,5HINDEX,2X,8HDELP,KS1,7X,3HCDF,5X,5HSTAR,5X,5HSSTAR)
C
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294      290 FORMAT(1H0,'LILLIEFOR'S (K-S) TEST SHOWS SAMPLE IS PLAUSIBLE FROM T
1HE HYPOTH. C.D.F. '1H ' TEST STATISTIC ',F10.4,' IS LESS THAN THE
2CRITICAL VALUE ',F10.4., WITH A RISK OF ',F10.4)
295      GO TO 288
284      CONTINUE
297      WRITE (6,242) TLFOR5,CLFOR5,FSRISK
292      FORMAT(1H0,'LILLIEFOR'S (K-S) TEST SHOWS THAT SAMPLE IS NOT PLAUSIB
1LE FROM THE HYPOTH. C.D.F. '1H ' TEST STATISTIC ',F10.4,' IS GREAT
2ER THAN THE CRITICAL VALUE ',F10.4., WITH A RISK OF ',F10.4)
288      CONTINUE
299      IF(IFLOT.NE.1) GO TO 1
300      C PLOT DISTRIBUTIONAL DATA
301      C WRITE (6,89)
302      89 FORMAT(1H1,'PLOT OF HYPOTH. AND SAMPLE C.D.F.S OF DELP')
303      CALL GPPRT
304      GO TO 1
305      4 CONTINUE
306      C WRITE ERROR MESSAGE AND STOP
307      400 FORMAT(1H0,'ERROR IN INPUT--PMAX,DELP,DELAY: ',3F15.4)
308      3 CALL EXIT
309      STOP
310      C END *****
311      C SUBROUTINE DIST1(XMEAN,XSTD,N,T)
312      C ESTIMATION OF PARAMS OF THE TWO-PARAM WEIBULL C.D.F.
313      C PARAMETERS ARE ESTIMATED BY THE METHOD OF MATCHING
314      C MOMENTS FROM THE GIVEN MEAN AND STANDARD DEVIATION.
315      C ALTERNATIVE ESTIMATES USING MAX LIKELIHOOD ARE ALSO OBTAINED
316      C
317      C DIMENSION T(400)
318      C BETA=BETA1
319      C KOUNT=0
320      C NRLEV=0
321      C 1 CONTINUE
322      C RETURN OF ITERATION LOOP
323      C KOUNT=KOUNT+1
324      C IF (KOUNT.GT.40) GO TO 20
325      C CALCULATE THE TEST FUNCTION OF BETA
326      C

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324      FH=GAMMA(1.+2.*BETA)/(GAMMA(1.+1./BETA)
325      DF=FB-A
326      IF ( ABS(DF).LT.1.0E-4.NR,DBETA.LT.1.E-3) GO TO 60
327      IF (KOUNT.GT.1) GO TO 10
328      IF (DF.GT.0.0) GO TO 12
329      SIGN=-1.
330      BETA=BETA/2.0
331      GO TO 1
332      12 CONTINUE
333      SIGN=1.
334      BETA=I.5*BETA
335      GO TO 1
336      10 CONTINUE

C      COUNT IS GREATER THAN 1 AND ITERATION CONTINUES

337      IF (DF.GT.0.0) GO TO 14
338      IF (SIGN.GT.0.0) GO TO 5

C      CONTINUE HALVING OR DECREMENTING BETA

339      IF (NREV.GT.0) GO TO 4
340      BETA=BETA/2.0
341      GO TO 40
342      4 BETA=BETA-DBETA
343      IF (BETA.LE.0.0) BETA=DBETA/2.0
344      40 CONTINUE
345      GO TO 1
346      5 CONTINUE

C      SIGN REVERSAL HAS OCCURRED

347      SIGN=-1.
348      NREV=NREV+1
349      IF (NREV.GT.1) DBETA=DBETA/2.0
350      BETA=BETA-DBETA
351      IF (BETA.LE.0.0) BETA=DBETA/2.0
352      GO TO 1
353      14 CONTINUE

C      DF IS POSITIVE; BETA MUST INCREASE.

354      IF (SIGN.GT.0.0) GO TO 2
355      C      A SIGN REVERSAL HAS OCCURRED.

C      SIGN=1.
356      NREV=NREV+1
357      IF (NREV.GT.1) DBETA=DBETA/2.0
358      BETA=BETA+DBETA
359      GO TO 1
360      2 CONTINUE

C      CONTINUE DOUBLING OR INCREMENTING BETA

361      IF (NREV.GT.0) GO TO 45
362      BETA=I.5*BFTA
363      GO TO 1

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364 45 CONTINUE
365  DETA=BETA+DBETA
366  GO TO 1
367  20 CONTINUE
C PRINT ERROR MESSAGE
C
368  WRITE (6,50) DETA
369  50 FORMAT (1H0, *ERROR. COUNT LIMIT OF 40 EXCEEDED. BETA = *,F10.4)
370  CALL EXIT
371  STOP
372  60 CONTINUE
C CONVERGENCE OF BETA ACHIEVED
C
373  ETA=A1/GAMMA(1.+1./BETA)
374  FN=FLOAT(N)
375  SUBETA= SORT (BETA*(2.0*BETA-1.)/FN)*(FN-2.)/(FN+2.)
376  WRITE (6,69)
377  69 FORMAT (1H0, *PARAMETER ESTIMATES OF THE C.O.F. OF DELP OBTAINED BY
1 MATCHING MOMENTS*)
378  WRITE (6,70) BETA,ETA,DF,DBETA,KOUNT,DBETA
379  70 FORMAT (1H0, *BETA = *,F10.4, *ETA = *,F10.4, *DF = *,F10.5,
1 , *DBETA = *,F10.5, *KOUNT = *,I3, *1H0,
2 , *APPROXIMATE STD. DFV. OF ESTIMATE OF BETA = *,F10.5)
C OBTAIN MAX LIKELIHOOD ESTIMATES
C
380  LOOP=1
381  ALPHA=BETA
382  ALPHA1=BETA
383  79 CONTINUE
384  SUM1=0.
385  SUM2=0.
386  SUM3=0.
387  SUM4=0.
388  DO 80 I=1,N
389  IF (T(I).LE.0.0) GO TO 100
390  TIA=T(I)**ALPHA
391  ALTI=ALOG(T(I))
392  SUM1=SUM1+TIA
393  SUM2=SUM2+TIA*ALTI
394  SUM3=SUM3+ALTI
395  SUM4=SUM4+TIA*ALTI**2
396  CONTINUE
397  HLAMB=FN/SUM1
398  ALPHA=FN/(HLAMB*SUM2-SUM3)
399  LOOP=LOOP+1
400  DA=ABS(ALPHA-ALPHA1)
401  ALPHA1=ALPHA
402  IF (DA.LE.1.E-3.OR.LOOP.GE.9) GO TO 81
403  GO TO 79
404  81 CONTINUE
C ALPHA CONVERGENCE ACHIEVED
C
C CALCULATE CONFIDENCE INTERVALS FOR MAX LIKELIHOOD PARAM. ESTIMATES.
C SEE P. 178, LLOYD AND LIPOK, RELIABILITY, C. 1962.

```



```

C INPUTS TO GPPLT, WHICH CLEARS AND SCALES THE PLOT ARRAY:
C NLAYERS NUMBER OF LAYERS IN THE PLOT ARRAY TO BE USED.
C XMIN,XMAX,YMIN,YMAX
C LIMITS OF GRID SCALES.
C
467      DIMENSION XLABEL(6), YLABEL(9)
468      INTEGER ARRAY(51,101,2)
469      DATA IBLANK,IHASH,IDASH / * * * * * / *
C
C CLEAR LAYER 1, CREATE GRID, DEFINE LABELS
C
470      DO 105 I=1,51
471      DO 105 J=I,101
472      105 ARRAY(I,J,1) = IBLANK
473      DRANGE = 0.125 * (YMAX-YMIN)
474      DO 110 K=1,9
475      I = 6*K - 4
476      YLABEL(K) = YMIN + (K-1) * DRANGE
477      DO 110 J=1,101
478      110 ARRAY(I,J,1) = IDASH
479      DO 115 K=1,11
480      J = 10*K - 9
481      DO 115 I=I,51
482      115 ARRAY(I,J,1) = IHASH
483      DRANGE = (XMAX-XMIN) / 5.0
484      DO 120 K=I,6
485      120 XLABEL(K) = XMIN + (K-1) * DRANGE
486      X0 = XMIN
487      RX = XMAX-XMIN
488      Y0 = YMIN
489      RY = YMAX-YMIN
490      LAYERS = NLAYRS
491      IF (LAYERS.EQ.1) RETURN
C
C CLEAR LAYER 2
C
492      DO 155 I=1,51
493      DO 155 J=I,101
494      155 ARRAY(I,J,2) = 0
495      RETURN
C
C ENTRY GPLOD1 (X, Y, ICHAR)
C-- LOAD THE PLOT CHARACTER "ICHAR" AT THE (X,Y) POINT IN LAYER 1.
C
496      LINE = ILINE(Y, Y0, RY)
497      LINE = ILINE(Y, Y0, RY)
498      KOL = IKOLUMN(X, X0, RX)
499      ARPAY(LINE,KOL,1) = ICHAR
500      RETURN
C
C ENTRY GPLINE(X,Y,X2,Y2,ICHAR)
C-- PLOT A "STRAIGHT LINE" USING "ICHAR" FROM (X,Y) TO (X2,Y2) IN LAYER
C NUMBER 1.
C
501      LINE = ILINE(Y, Y0, RY)
502      KOL = IKOLUMN(X, X0, RX)
503      LINE2 = ILINE(Y2, Y0, RY)
504      KOL2 = IKOLUMN(X2, X0, RX)
505      ARRAY(LINE,KOL,1) = ICHAR
506      ARRAY(LINE2,KOL2,1) = ICHAR
507      LINES = LINE - LINE2
508

```

```

KOLS = KOL - KOL2    LINES = -LINES
510  IF (LINES.LT.0)    KOLS = -KOLS
511  IF (KOLS.LT.0)    KOLS = -KOLS
512  IF (LINS.GT.KOLS) GO TO 430
513  IF (X2.EQ.X)      RETURN
514  IF (KOL.LT.KOL2)  GO TO 400
515  K1 = KOL2 + 1
516  K2 = KOL - 1
517  GO TO 410
518  400  K1 = KOL + 1
519  K2 = KOL2 - 1
520  410 CONTINUE
521  IF (K1.GT.K2)     RETURN
522  00 420 K=K1,K2
523  XK = FLOAT(K)/100.*RX + X0
524  YK = Y + (Y2-Y) * (XK-X) / (X2-X)
525  LINE = ILINE(YK,Y0,RX)
526  420 ARRAY(LINE,K,1) = ICHAR
527  RETURN
528  430 CONTINUE
529  IF (LINE.LT.LINE2)  GO TO 440
530  K1 = LINE2 + 1
531  K2 = LINE - 1
532  GO TO 450
533  440 K1 = LINE + 1
534  K2 = LINE2 - 1
535  450 CONTINUE
536  IF (K1.GT.K2)     RETURN
537  00 460 K=K1,K2
538  XK = FLOAT(50-K)/48.*RY + Y0
539  X = X + (X2-X) * (YK-Y) / (Y2-Y)
540  KOL = IKOLUM(XK,X0,RX)
541  460 ARRAY(K,KOL,1) = ICHAR
542  RETURN
C...
C
543  ENTRY GPLOD2 (X, Y)
544  C-- ACCUMULATE AT THE (X, Y) POINT IN LAYER 2.
545  LINE = ILINFO(Y, Y0, RY)
546  KOL = IKOLUM(X, X0, RX)
547  ARRAY(LINE,KOL,2) = ARRAY(LINE,KOL,2) + 1
RETURN
C...
C
548  C-- CONVERT NUMERIC DATA IN LAYER 2 TO ALPHA FOR PRINTOUT
C-- IVECTOR OF PLOT CHARACTERS TO BE USED IN LOADING LAYER
C-- NUMBER 2.
C-- NCHAR DIMENSION AND NUMBER OF CHARACTERS IN IVECTOR.
549
C-- DIMENSION IVECTOR(NCHAR)
DO 225 I=1,51
DO 225 J=1,101
K = ARRAY(I,J,2)
IF (K.GT.0)      GO TO 215
ARRAY(I,J,2) = IRLANK
GO TO 225
215 CONTINUE
550
551
552
553
554
555
556

```



```

C C SUBROUTINE TO DEFINE PLOT SCALE LIMITS. USED OPTIONALLY IN CONJUNC
C TION WITH SUBROUTINE GPPLT
C
C INPUTS:
C   ISCALE CONTROL PARAMETER:
C     1 => USE GIVEN DATMIN AS XMIN; DEFINE XMAX ON BASIS
C           OF DATMAX
C     2 => USE GIVEN DATMAX AS XMAX; DEFINE XMIN ON BASIS
C           OF DATMIN
C     3 => DEFINE XMIN, XMAX ON BASIS OF DATMIN, DATMAX
C
C   IXY CONTROL PARAMETER:
C     1 => SCALING X-AXIS OF GPPLT
C     2 => SCALING Y-AXIS OF GPPLT
C
C   DATMIN,DATMAX
C
C   LIMITS OF DATA TO BE PLOTTED
C
C OUTPUTS:
C   XMIN,XMAX PLOT SCALE LIMITS
C
C
C   DIMENSION RMULT(4), MDIVS(2)
C   DATA RMULT / 2., 5., 10., 20. /, MDIVS / 10, 8 /
C
C   1 FORMAT(' ***PLOT SCALE ROUTINE FAILED. RUN ABORTED.')
C
C   NDIVS = MDIVS(IXY)
C   DRANGE = (DATMAX-DATMIN) / NDIVS
C   IEXPON = ALOG10 (DRANGE)
C   IF (DRANGE.LT.1.0) IEXPON = IEXPON - 1
C   TENS = 10.0 ** IEXPON
C
C   K = 1
C   DO 100 I=1,2
C     TEST = RMULT(I) * TENS
C     IF (TEST.GE.DRANGE) GO TO 110
C   100 CONTINUE
C   I = 3
C   110 TEST = RMULT(I) * TENS
C   613 GO TO (120,160,170), ISCALE
C   120 XMIN = DATMIN
C   130 XMAX = XMIN + NDIVS*TEST
C   616 IF (XMAX.GE.DATMAX) RETURN
C   617 IF (K.EQ.1) GO TO 150
C   140 WRITE (6,I)
C   620 STOP
C   150 K = 2
C   621 I = 1 + 1
C   622 GO TO 110
C   623 XMAX = DATMAX
C   624 XMIN = XMAX - NDIVS*TEST
C   625 IF (XMIN.LE.DATMIN) RETURN
C   626 IF (K-1) 150,150,140
C   170 N = DATMIN/TEST
C   628 IF ((DATMIN.LT.0.0) N = N - 1
C   629 XMIN = N*TENS
C   630 GO TO 130
C   631
C   632

```

```

156      SENTRY      SUBROUTINE MLR(Y,X,NR,NC,NDATA,N,LZERO,PRINT,S,RSQ)
157      C           IMPLICIT REAL *8 (A-H,O-Z)
158      C
159      C           Y=DATA MATRIX. EACH OF THE FIRST N-1 COLUMNS REPRESENTS
160      C           THE VECTOR OF VALUES OF ONE OF THE INDEPENDENT VARIABLES.
161      C           THE N-TH COL. IS FOR THE DEPENDENT VARIABLE.
162      C           CJ=SOLUTION VECTOR. C(2) IS THE COEFFICIENT CORRESPONDING
163      C           TO THE FIRST INDEPENDENT VARIABLE.
164      C           C(1)=AVG. DEPENDENT VAR.
165      C           NR=NUMBER OF ROWS IN STORAGE ALLOCATED FOR THE DATA MATRIX.
166      C           NC=NUMBER OF COLUMNS ALLOCATED IN THE DATA MATRIX STORAGE.
167      C           NOATA=NUMBER OF VALUES OF EACH INDEPENDENT VARIABLE,
168      C           IE, NUMBER OF DATA POINTS.
169      C           N=NUMBER OF COLUMNS IN THE DATA MATRIX=TOTAL NO. OF VARS.
170      C           IF LZERO IS ZERO, THE LEADING (CONSTANT) COEFFICIENT IN EQ. WILL
171      C           BE SET TO ZERO.
172      C           PRINT=LOGICAL SWITCH SET TO .TRUE. FOR PRINT OF
173      C           FITTED FUNCTION AND SET TO .FALSE. FOR NO PRINT.
174      C           MEAN SQUARES=SUM OF SQUARED OEVATIONS FROM FITTED FUNCTION
175      C           DIVIDEO BY DEGREES OF FREEDOM. RETURNED BY SUBROUTINE.
176      C           RSQ IS THE R-SQUARED STATISTIC RETURNED BY SUBROUTINE.
177      C
178      DIMENSION A(10,11)
179      DIMENSION X(NC),Y(NR,NC),B(10,11),XBAR(11),SIGMA(11)
180      REAL *8 SUM,SUMSQ,DARS,DSQRT
181      NA=10
182      NB=11
183      LOGICAL PRINT

```

```

NPO=N+1
NMO=N-1
FN=NDATA
DO 1 J=1,N
167 SUM=0.
168 DO 18 I=1,NDATA
169 18 SUM=SUM+Y(I,J)
170 XBAR(J)=SUM/FN
171 SUMSQ=0.0
172 DO 8 I=1,NDATA
173 8 SUMSQ=SUMSQ+(Y(I,J)-XBAR(J))***2
174 1 SIGMA(J)=DSQRT(DABS(SUMSQ)/(FN-1.0))
175 LONE=0
176 IF (LZERO.EQ.0) LONE=1
177 ILOW=LONE+1
178 DO 4 II=ILOW,N
179 IM=II-1
180 IF (IM.NE.0) GO TO 2
181 A(1,1)=FN
182 DO 3 J=2,NPO
183 3 A(1,J)=0.0
184 GO TO 4
185 2 I=II-LONE
186 DO 5 JJ=II,NPO
187 J=JJ-LONE
188 JM=JJ-1
189 A(I,J)=0.0
190 DO 5 K=1,NDATA
191 5 A(I,J)=A(I,J)+(Y(K,IM)-XBAR(IM))/SIGMA(IM)
          * (Y(K,JM)-XBAR(JM))/SIGMA(JM)
192 4 CONTINUE
193 N1=N-LONE
194 N2=N1+1
195 DO 6 I=2,N1
196 K=I-1
197 DO 6 J=1,K
198 6 A(I,J)=A(J,I)
199 DO 7 I=1,N1
200 DO 7 J=1,N2
201 7 B(I,J)=A(I,J)
202 CALL AXBSOL(B,X,N1,NA,NB,1.0E-10*SIGMA(N))
203 IF (.NOT.PRINT) GO TO 9
204 PRINT 10
205 10 FORMAT (1H04X1H14X1HNORM. COEF.8X7HXBAR (I) 7X8HSIGMA(I)2X
          13HUNIT RESIDUAL)

```

00007400
00007500
00007600

```

206 DO 11 I=1,N1
207 R=0.
208 DO 12 J=1,N1

```

```

209      12 R=R*A(I,J)*X(J)      000007700
210      IF (A(I,N2).EQ.0.0) GO TO 11      00007800
211      R=(R-A(I,N2))/A(I,N2)      00007900
212      PRINT 16,I,X(I)*XBAR(I),SIGMA(I)*R      00008000
213      FORMAT (1H 15,1P4E15.6)      00008100

214      9 IF (LZERO.NE.0) GO TO 21      00008200
215      DO 20 J=1,N1      00008300
216      X(NP0-J)=X(N2-J)      00008400
217      X(1)=0.0      00008500
218      SUM=X(1)      00008600
219      DO 19 J=1,NMO      00008700
220      J2=J+1      00008800
221      SUM=SUM-X(J2)*XBAR(J)/SIGMA(J)      00008900
222      X(J2)=X(J2)*SIGMA(N)/SIGMA(J)      00009000
223      IF (LZERO.NE.0) X(1)=SIGMA(N)*SUM*XBAR(N)      00009100
224      IF (PRINT) PRINT 22,(I*X(I)*I=1,N)      00009200
225      FORMAT (*ODIMENSIONALIZED COEFFICIENTS,* X(*I2,*')=1PE15.8)      00009300

226      S=0.      00009400
227      DO 13 K=1,NDATA      00009500
228      YC=X(1)      00009600
229      DO 14 I=2,N      00009700
230      YC=YC+Y(K,I-1)*X(I)      00009800
231      RES=YC-Y(K,N)      00009900
232      S=S+RES**2      00010000
233      RSQ=(SUMSQ-S)/SUMSQ      00010100
234      DF=NDATA-N      00010200
235      IF (LZERO.EQ.0) DF=DF+1.0      00010300
236      IF (DF.LE.0.0) RETURN      00010400
237      S=S/DF      00010500
238      IF (PRINT) PRINT 15,S,RSQ      00010600
239      15 FORMAT (1H 5X9HRES. M.S.5X9HR-SQUARED/1H 1PE15.6,0PF15.6)      00010700

240      RETURN      00010800
241      END      00010900

242      C      SUBROUTINE AXBSOL (A,X,NA,NB,EPSSIL)      00011000
243      C      IMPLICIT REAL *8 (A-H-O-Z)      00011100
244      C      DIMENSION A(NA,NB),X(N)      00011200
245      C      NPO=N+1      00011300
246      C      NMO=N-1      00011400
247      C      SET MATRIX SIZE. COUNTER      00011500
248      C      DO 2 J=1,NMO      00011600
249      C      B=EPSIL      00011700
250      C      JROW=0      00011800
251      C      D=A(J,J)      00011900
252      C      LOOK FOR LARGEST PIVOTAL ELEMENT OR ZERO HOW      00012000
253      C      DO 3 I=J,N      00012100
254      C      IF (DABS(A(I,J))-DABS(B)) 3,3,4      00012200
255      C      IF ( ABS(A(I,J))- ABS(B)) 3,3,4      00012300
256      C      4 JROW=I      00012400
257      C      B=A(I,J)      00012500

```

```

0=6          00012600
255         C   3 CONTINUE UNTIL ZERO, MINOR IS ZERO. IF GTR THAN J, SWITCH ROWS.
256         C   IF JROW STILL ZERO, MINOR IS ZERO. IF GTR THAN J, SWITCH ROWS.
257         C   IF (JROW-J)5,6,7
258         7 DO 8 L=J,NPO
259         C=A(J,L)
260         A(J,L)=A(JROW,L)
261         8 A(JROW,L)=C
262         C   DIVIDE ROW J BY PIVOTAL ELEMENT
263         6 DO 9 L=J,NPO
264         9 A(J,L)=A(J,L)/D
265         C   GET ZEROS INTO ALL ROWS OF COLUMN J BELOW PIVOT
266         DO 2 IK=J,NMO
267         B=A(IK+1,J)
268         DO 2 JK=J,NPO
269         A(IK+1,JK)=A(IK+1,JK)-B*A(J,JK)
270         GET SOLUTION VECTOR BY BACK-SUBSTITUTION
271         X(N)=A(N,NPO)/A(N,N)
272         DO 10 IK=1,NMO
273         I=N-IK
274         I=N-IK
275         X(I)=A(I,NPO)
276         10 X(I)=X(I)-X(J)*A(I,J)
277         RETURN
278         5 PRINT 15,J,J
279         15 FORMAT (20HMINOR OF COFACTOR (I1,IH,I1,9H) IS ZERO)
280
281         CALL EXIT
282         END

```

TEST DATA FOR 8 IN HOW, MIREI PROP CHG--SECURED CARGO (COLD) SET C1

SAMPLE = 27 F-S CRITICAL VALUE = 2.485 F-S LEVEL OF RISK = 0.0500 DEG. OF POLY. REGRES. = 1

Avg Pmax,KSI Avg DELP,PSI Avg Todel,MS
37.5962 513.3 145.4

SD: Pmax,KSI DELP,PSI DELAY,MS
0.7719 490.8469 44.9309

CORRELATION MATRIX:

PMAX	DELP	DELAY
1.0000	0.0456	0.0134
0.0456	1.0000	-0.1956
0.0134	-0.1956	1.0000

ANALYSIS BASED ON SIMPLE LINEAR REGRESSION OF PMAX ON DELP:

SLOPE = 0.00007 KSI/PSI STU. ERR. OF EST. OF PMAX GIVEN DELP = 0.78632 KSI

STD. DEV. OF SLOPE = 0.00031 95% CONF. LIMITS: -0.00058 0.00072 T-STATISTIC (CRITICAL) = 2.05957

PARTIAL CORRELATION COEFS. WITH DEPENDENCE OF PMAX ON DELP AND DELAY ASSUMED

DELP, GIVEN DT DT, GIVEN DELP
0.0492 0.0227

FRACTION OF VARIANCE DUE TO DELP = 0.0024

FRACTION OF VARIANCE DUE TO DELAY = 0.0005

I	NORM. COEF.	XBAR(I)	SIGMA(I)	UNIT RESIDUAL
1	-0.000000E-01	5.132590E-02	4.908474E-02	0.000000E-01
2	4.561469E-02	3.759628E-01	7.718509E-01	-8.041248E-07

DIMENSIONALIZED COEFFICIENTS

X(1)= 3.7559460E 01
X(2)= 7.1728470E-05
RES. M.S. R-SQUARED
6.182953E-01 0.002080

REGRESSION COEFS. FOR PMAX ON DELP:

ZEROTH	FIRST	2ND	3RD
0.37559E 02	0.71728E-04		

FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION: 0.00208

DISTRIBUTION OF RESIDUALS FROM PMAX-DELP REGRESSION

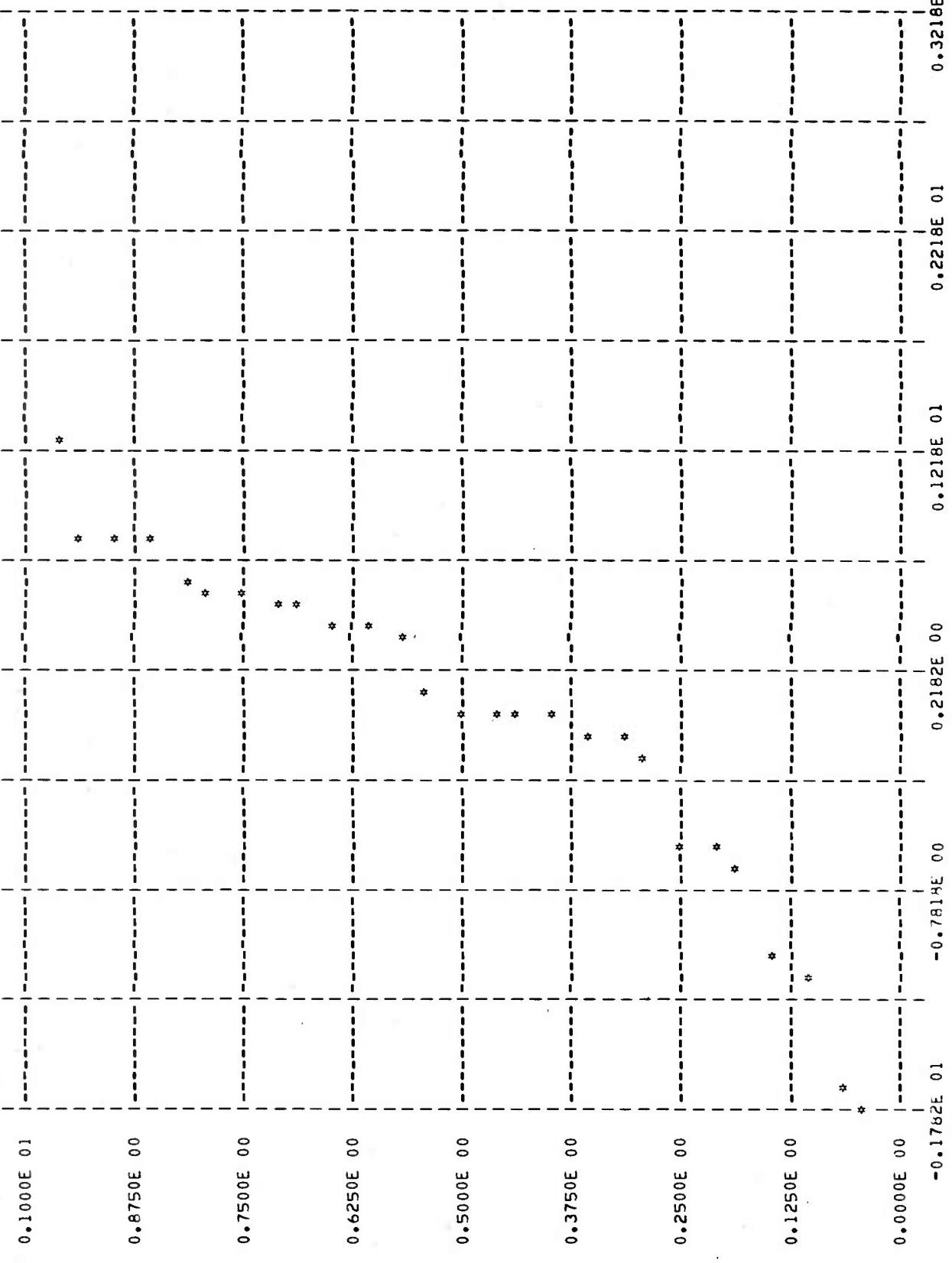
INDEX	RESID. KSI	MED RANK	NORM D.F.	DSTAR	SSTAR
1	-1.7818	0.0357	0.0104	0.0266	0.0266
2	-1.6850	0.0714	0.0144	0.0596	0.0863
3	-1.1924	0.1071	0.0610	0.0501	0.1364
4	-1.0674	0.1429	0.0831	0.0650	0.2014
5	-0.7050	0.1786	0.1803	0.0321	0.2335
6	-0.5801	0.2143	0.2259	0.0407	0.2742
7	-0.5765	0.2500	0.2273	0.0320	0.3062
8	-0.1681	0.2857	0.4137	0.1545	0.4606
9	-0.0990	0.3214	0.4489	0.1526	0.6133
10	-0.0861	0.3571	0.4555	0.1222	0.7355
11	0.0108	0.3929	0.5056	0.1352	0.8707
12	0.0123	0.4286	0.5063	0.0989	0.9696
13	0.0342	0.4643	0.5177	0.0732	1.0429
14	0.0405	0.5000	0.5210	0.0395	1.0823
15	0.1405	0.5357	0.5723	0.0538	1.1361
16	0.3927	0.5714	0.6947	0.1392	1.2753
17	0.3943	0.6071	0.6955	0.1029	1.3782
18	0.4040	0.6429	0.6999	0.0702	1.4484
19	0.5210	0.6786	0.7504	0.0837	1.5321
20	0.5346	0.7143	0.7559	0.0522	1.5843
21	0.5481	0.7500	0.7614	0.0207	1.6050
22	0.5694	0.7857	0.7699	0.0449	1.6500
23	0.6299	0.8214	0.7930	0.0588	1.7088
24	0.8048	0.8571	0.8517	0.0372	1.7460
25	0.8141	0.8929	0.8545	0.0715	1.8175
26	0.8207	0.9286	0.8564	0.1065	1.9240
27	1.2697	0.9643	0.9502	0.0498	1.9738

RESIDUALS ARE PLAUSIBLY GAUSSIAN.

SSTAR IN F-S TEST, 1.9738 IS LESS THAN THE CRITICAL VALUE, 2.4854

LILLIEFORS (K-S) TEST SHOWS RESIDUALS ARE GAUSSIAN.
TEST STATISTIC 0.1545 IS LESS THAN THE CRITICAL VALUE 0.1665 WITH A RISK OF 0.0500

MEAN AND STD. DEV. OF RESIDUALS (KSI): 0.00002 0.77105

PLOT OF CUMULATIVE DISTRIBUTION FUNCTION OF P_{MAX} RESIDUALS

	NORM. COEF.	XBAR(I)	SIGMA(I)	UNIT RESIDUAL
1	-0.000000E-01	1.454074E-02	4.493092E-01	0.000000E-01
2	1.335169E-02	3.759628E-01	7.718509E-01	-1.717001E-07

DIMENSIONALIZED COEFFICIENTS

 $X(1) = 3.75629200E+01$ $X(2) = 2.29363500E-04$

RES. M.S. R-SQUARED

6.194732E-01 0.000179

REGRESSION COEFS. FOR PMAX ON DELAY:

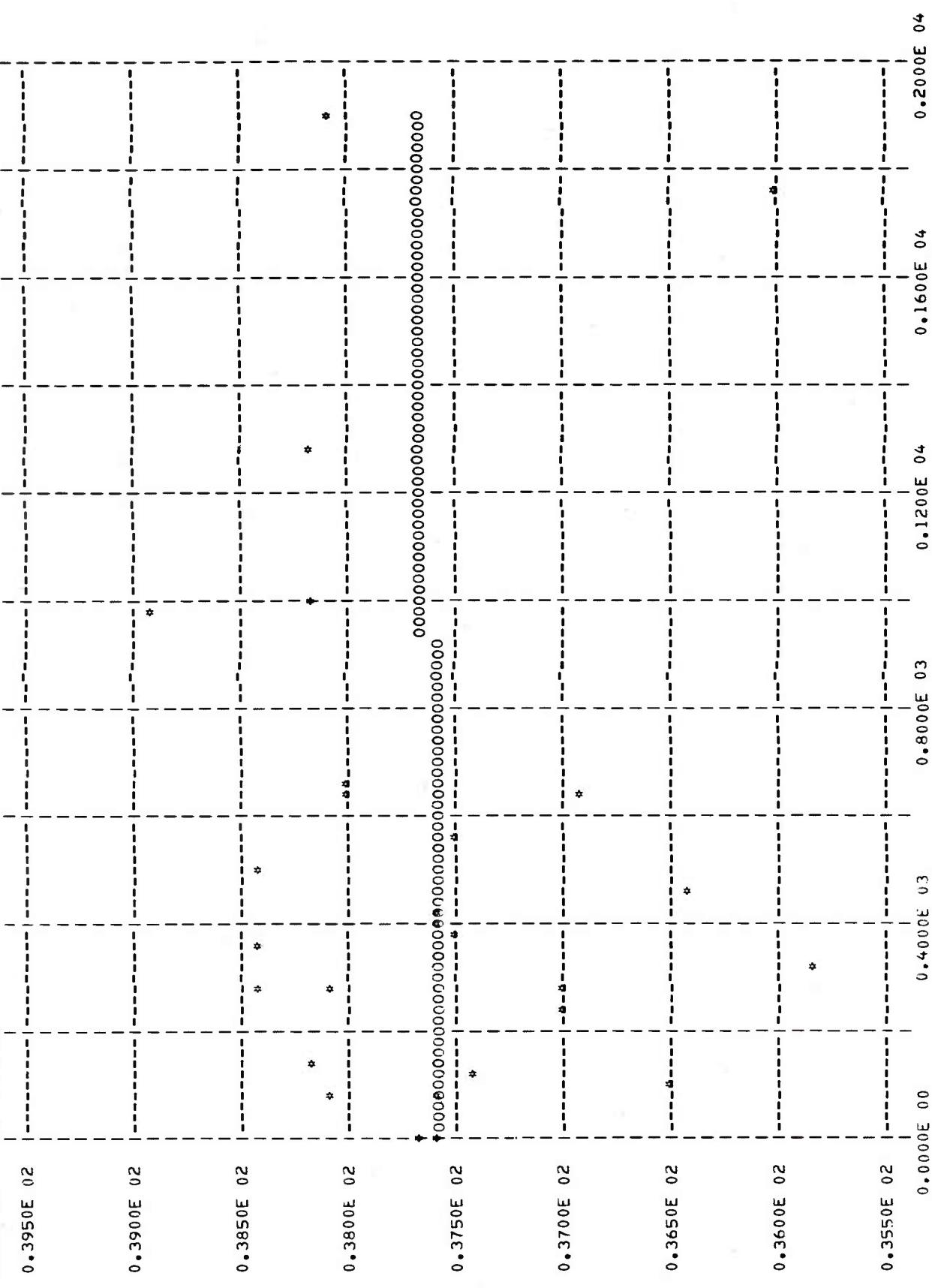
ZEROTH	FIRST
0.37563E-02	0.22936E-03

FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION:

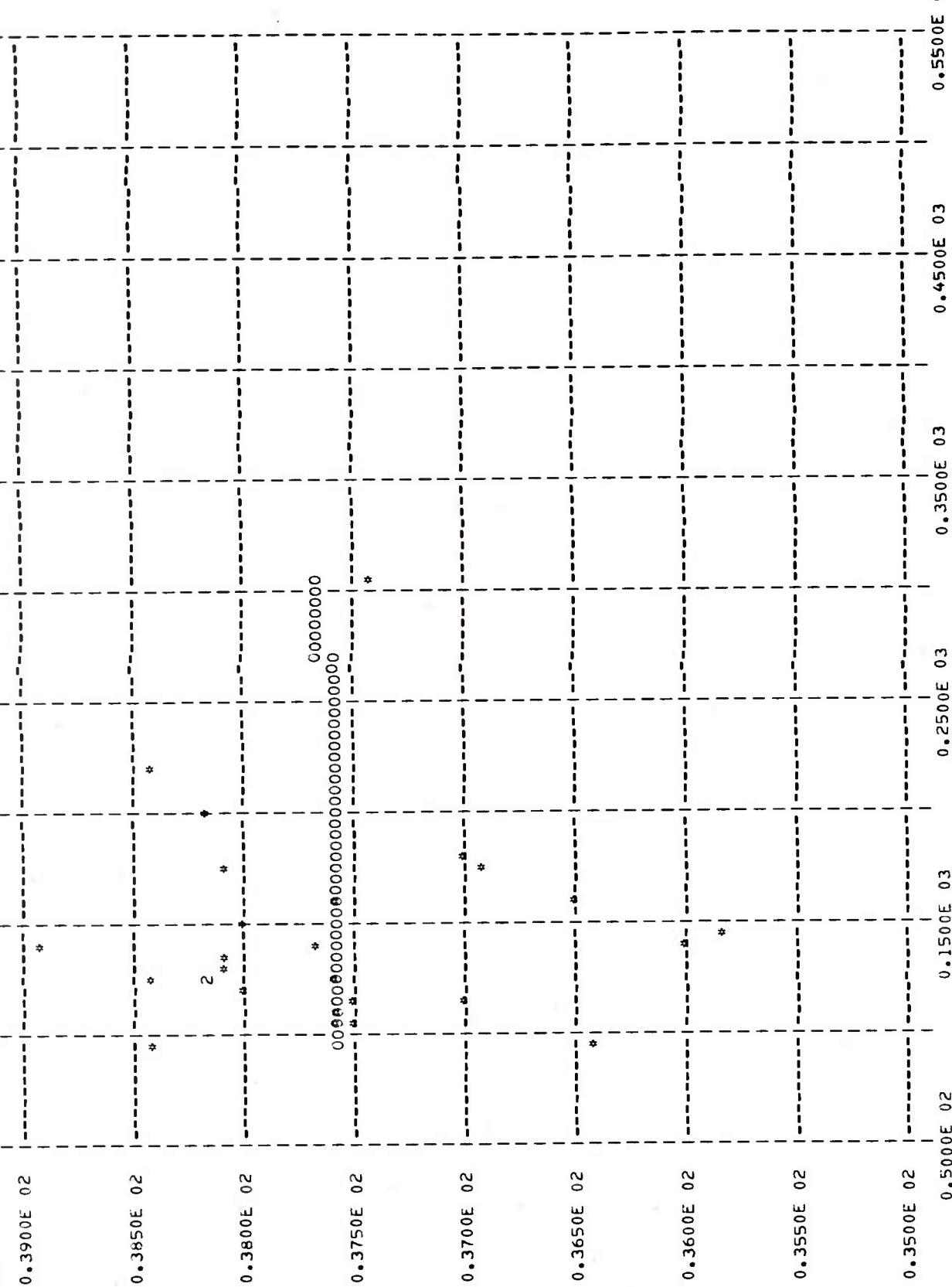
INDEX MED RANK PMAX.KSI

1	0.0357	35.8000	DELP.PSI	DELAY.MS
2	0.0714	36.0000	0.00	93.00
3	0.1071	36.4000	0.00	95.00
4	0.1429	36.5000	83.00	105.00
5	0.1786	36.9000	89.00	106.00
6	0.2143	37.0000	110.00	108.00
7	0.2500	37.0000	120.00	113.00
8	0.2857	37.4000	148.00	114.00
9	0.3214	37.5000	238.00	120.00
10	0.3571	37.5000	272.00	125.00
11	0.3929	37.6000	276.00	126.00
12	0.4286	37.6000	288.00	126.00
13	0.4643	37.6000	312.00	127.00
14	0.5000	37.6000	369.00	130.00
15	0.5357	37.7000	371.00	135.00
16	0.5714	38.0000	394.00	142.00
17	0.6071	38.0000	414.00	142.00
18	0.6429	38.1000	459.00	142.00
19	0.6786	38.1000	498.00	145.00
20	0.7143	38.1000	551.00	150.00
21	0.7500	38.2000	635.00	160.00
22	0.7857	38.2000	644.00	162.00
23	0.8214	38.2000	667.00	176.00
24	0.8571	38.4000	987.00	177.00
25	0.8929	38.4000	992.00	178.00
26	0.9286	38.4000	1288.00	202.00
27	0.9643	38.9000	1750.00	222.00
			1903.00	305.00

REGRESSION OF PHMAX ON DEEP



REGRESSION OF PMAX (KSI) ON DELAY (MS)



PARAMETER ESTIMATES OF THE C.O.F. OF DELP OBTAINED BY MATCHING MOMENTS

BETA = 1.0461 ETA = 522.5786 UF = -0.00023 DBETA = 0.00078 KOUNT = 15

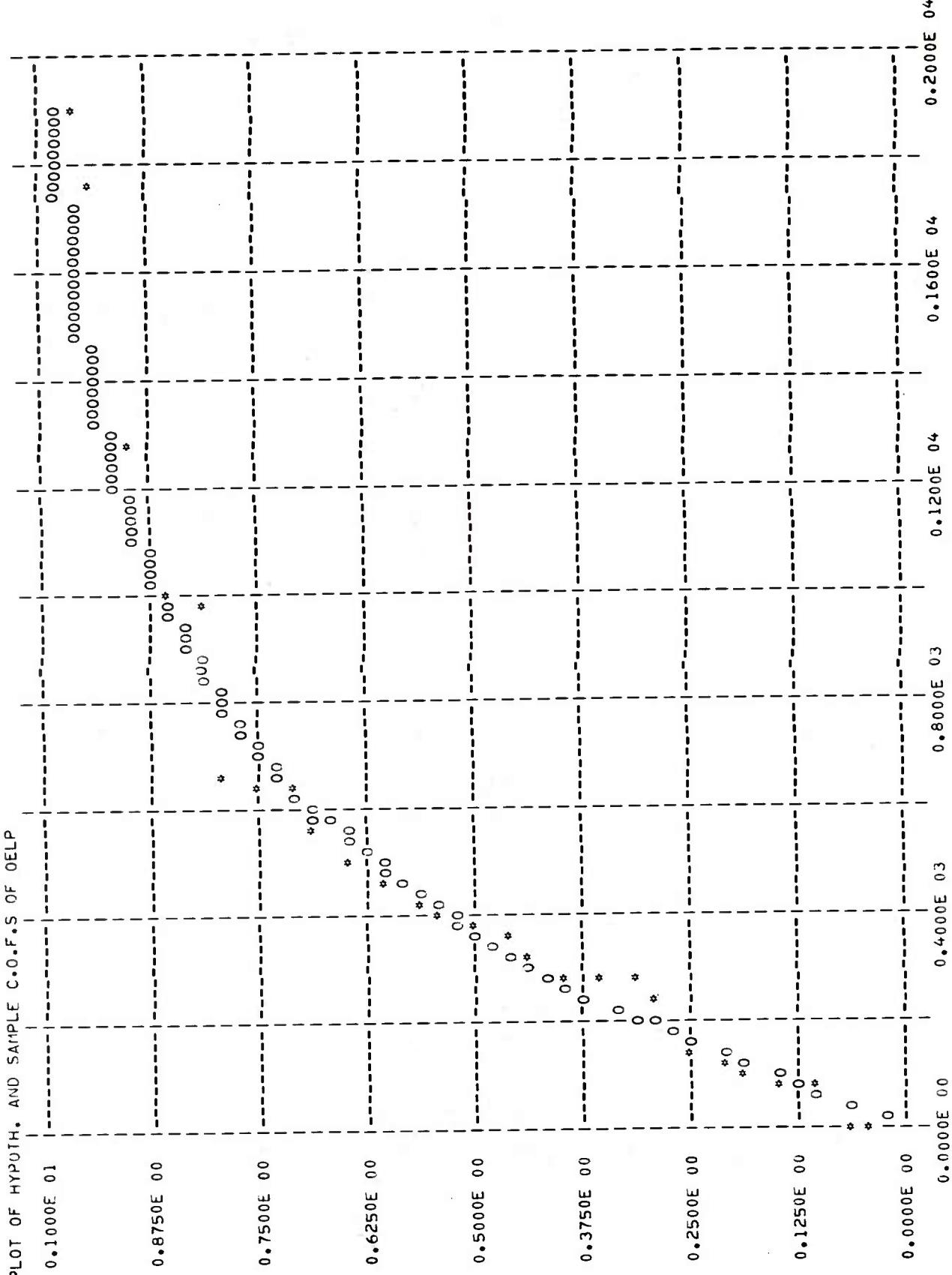
APPROXIMATE STD. DEV. OF ESTIMATE OF BETA = 0.17733

ZERO VALUES ENCOUNTERED PRECLUDES THE CALCULATION OF MAXIMUM LIKELIHOOD ESTIMATES. MATCHING MOM. PARAMS. ARE KEPT.

INDEX	DELP, KSI	CDF	DSTAR	SSTAR
1	0.000	-0.0000	0.0370	0.0370
2	0.0000	-0.0000	0.0741	0.1111
3	83.0000	0.1358	0.0617	0.1728
4	89.0000	0.1453	0.0342	0.2070
5	110.0000	0.1779	0.0298	0.2367
6	120.0000	0.1931	0.0291	0.2658
7	148.0000	0.2345	0.0248	0.2906
8	238.0000	0.3555	0.0962	0.3868
9	272.0000	0.3965	0.1002	0.4870
10	276.0000	0.4012	0.0679	0.5549
11	288.0000	0.4150	0.0447	0.5996
12	312.0000	0.4418	0.0344	0.6339
13	369.0000	0.5009	0.0564	0.6904
14	371.0000	0.5028	0.0213	0.7117
15	394.0000	0.5249	0.0307	0.7424
16	414.0000	0.5433	0.0493	0.7917
17	459.0000	0.5823	0.0473	0.8389
18	498.0000	0.6136	0.0531	0.8920
19	551.0000	0.6525	0.0512	0.9432
20	635.0000	0.7066	0.0342	0.9774
21	644.0000	0.7118	0.0659	1.0433
22	667.0000	0.7249	0.0899	1.1332
23	987.0000	0.8570	0.0422	1.1754
24	992.0000	0.8585	0.0304	1.2058
25	1288.0000	0.9234	0.0345	1.2403
26	1750.0000	0.9710	0.0451	1.2854
27	1903.0000	0.9790	0.0210	1.3064

SAMPLE IS PLAUSIBLE FROM THE HYPOTH. C.D.F. USING THE F-S TEST S STAR = 1.3064

LILLIEFORS (K-S) TEST SHOWS SAMPLE IS PLAUSIBLE FROM THE HYPOTH. C.D.F.
TEST STATISTIC 0.1002 IS LESS THAN THE CRITICAL VALUE 0.1665 WITH A RISK OF 0.0500



TEST DATA FOR 8 IN. HOW. • M188E1 CHG. • MERGE OF SFTS C2+C3+SEQ. ROUGH HAND. (COLD)

SAMPLE = 27 F-S CRITICAL. VALUE = 2.485 F-S LEVEL OF RISK = 0.0500 DEG. OF POLY. REGRES. = 3

AVG PMAX•KSI AVG DELP•PSI AVG TIME•MS
37.0851 675.3 166.8

SD: PMAX•KSI DELP•PSI DELAY•MS
0.8416 1136.6830 65.4170

CORRELATION MATRIX:

PMAX	DELP	DELAY
1.0000	0.6697	-0.0943
0.6697	1.0000	0.1489
-0.0943	0.1489	1.0000

ANALYSIS BASED ON SIMPLE LINEAR REGRESSION OF PMAX ON DELP:

SLOPE = 0.00050 KSI/PSI STU. ERR. OF EST. OF PMAX GIVEN DELP = 0.63732 KSI

STD. DEV. OF SLOPE = 0.00011 95% CONF. LIMITS: 0.00027 0.00072 T-STATISTIC (CRITICAL) = 2.05957

PARTIAL CORRELATION COFFS. WITH DEPENDENCE OF PMAX ON DELP AND DELAY ASSUMED

DELP, GIVEN DT DT, GIVEN DELP
0.6946 -0.2642

FRACTION OF VARIANCE DUE TO DELP = 0.4824

FRACTION OF VARIANCE DUE TO DELAY = 0.0698

I	NORM. COEF.	XBAR(I)	SIGMA(I)	UNIT RESIDUAL
1	-0.00000E+01	6.752590E-02	1.136687E-03	0.00000E-01
2	-2.945518E-01	1.700179E-06	5.773493E-06	-8.762936E-07
3	2.865553E-00	7.168160E-09	3.038551E-10	-1.786141E-06
4	-1.947622E-00	3.708517E-01	8.415649E-01	-9.438726E-07

DIMENSIONALIZED COEFFICIENTS

X(1) = 3.69089300E-01

X(2) = -2.18076200E-04

X(3) = 4.17693100E-07

X(4) = -5.39418300E-11

RES. M.S. R-SQUARED
4.204599E-01 0.474825

REGRESSION COFFS. FOR PMAX ON DELP:

ZEROTH FIRST 2ND 3RD
0.36909E-02 -0.21808E-03 0.41769E-06 -0.53942E-10

FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION: 0.47483

DISTRIBUTION OF RESIDUALS FROM PMAX-UELP REGRESSION

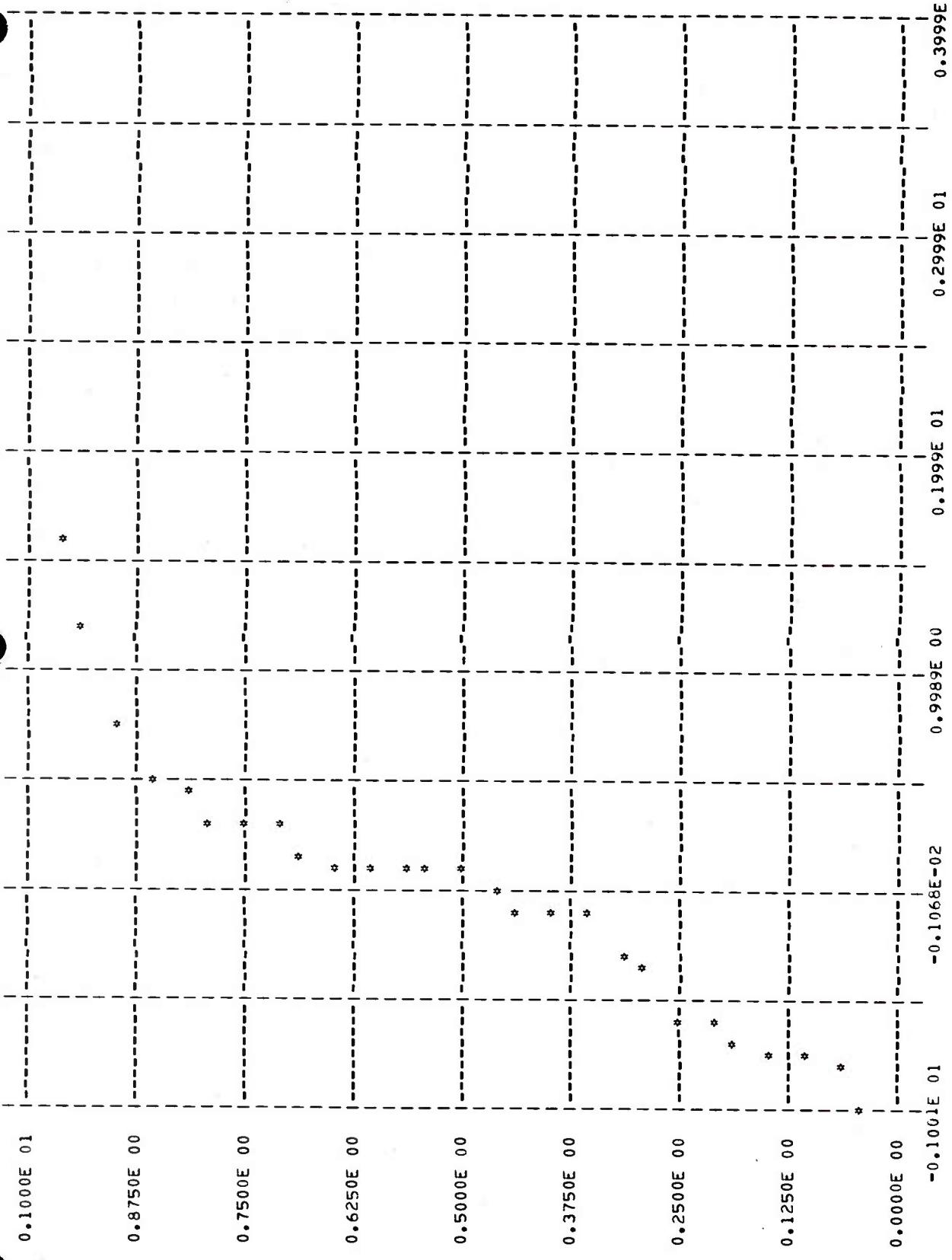
INDEX	RESID-KSI	MED RANK	NORM U.F.	DSTAR	SSTAR
1	-1.0011	0.0357	0.0504	0.0504	0.0504
2	-0.7822	0.0714	0.0998	0.0628	0.1131
3	-0.7624	0.1071	0.1056	0.0315	0.1447
4	-0.7501	0.1429	0.1094	0.0388	0.1835
5	-0.7075	0.1786	0.1230	0.0622	0.2457
6	-0.5861	0.2143	0.1683	0.0540	0.2996
7	-0.5797	0.2500	0.1709	0.0883	0.3880
8	-0.3273	0.2857	0.2957	0.0365	0.4244
9	-0.3089	0.3214	0.3062	0.0271	0.4515
10	-0.1089	0.3571	0.4291	0.0958	0.5473
11	-0.0939	0.3929	0.4398	0.0684	0.6157
12	-0.0833	0.4286	0.4456	0.0382	0.6540
13	-0.0224	0.4643	0.4853	0.0409	0.6948
14	0.0744	0.5000	0.5486	0.0671	0.7619
15	0.0867	0.5357	0.5565	0.0380	0.7999
16	0.0972	0.5714	0.5633	0.0293	0.8292
17	0.1085	0.6071	0.5706	0.0590	0.8882
18	0.1121	0.6429	0.5729	0.0937	0.9820
19	0.1478	0.6786	0.5957	0.1080	1.0899
20	0.2911	0.7143	0.6834	0.0573	1.1473
21	0.3095	0.7500	0.6941	0.0837	1.2309
22	0.3118	0.7857	0.6954	0.1194	1.3503
23	0.4538	0.8214	0.7716	0.0803	1.4306
24	0.5182	0.8571	0.8023	0.0866	1.5173
25	0.7717	0.8929	0.8971	0.0288	1.5461
26	1.2204	0.9286	0.9773	0.0514	1.5975
27	1.6112	0.9643	0.9959	0.0329	1.6304

RESIDUALS ARE PLAUSIBLY GAUSSIAN.

SSTAR IN F-S TEST. 1.6304 IS LESS THAN THE CRITICAL VALUE. 2.4854

LILLIEFORS (K-S) TEST SHOWS RESIDUALS ARE GAUSSIAN.
 TEST STATISTIC 0.1194 IS LESS THAN THE CRITICAL VALUE 0.1665 WITH A RISK OF 0.0500
 MEAN AND STD. DEV. OF RESIDUALS (KSI) : 0.00002 0.60987

PLOT OF CUMULATIVE DISTRIBUTION FUNCTION OF PMAX RESIDUALS



```

1 NORM• CUEF• XBAR(I) SIGMA(I) UNIT RESIDUAL
1 -0.00000E-01 1.667778E 02 6.541719E 01 0.000000E-01
2 -6.137496E 00 3.193574E 04 2.934265E 04 8.751107E-05

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3 1.220910E 01 7.138332E 06 1.119845E 07 9.293784E-05
 4 -6.349072E 00 3.708517E 01 8.415649E-01 1.207029E-04

DIMENSIONALIZED COEFFICIENTS

$x(1) = 4.24765100E 01$
 $x(2) = -7.89563000E-02$
 $x(3) = 3.50164200E-04$
 $x(4) = -4.77133400E-07$

RES. M.S. R-SQUARED
 7.337421E-01 0.083521

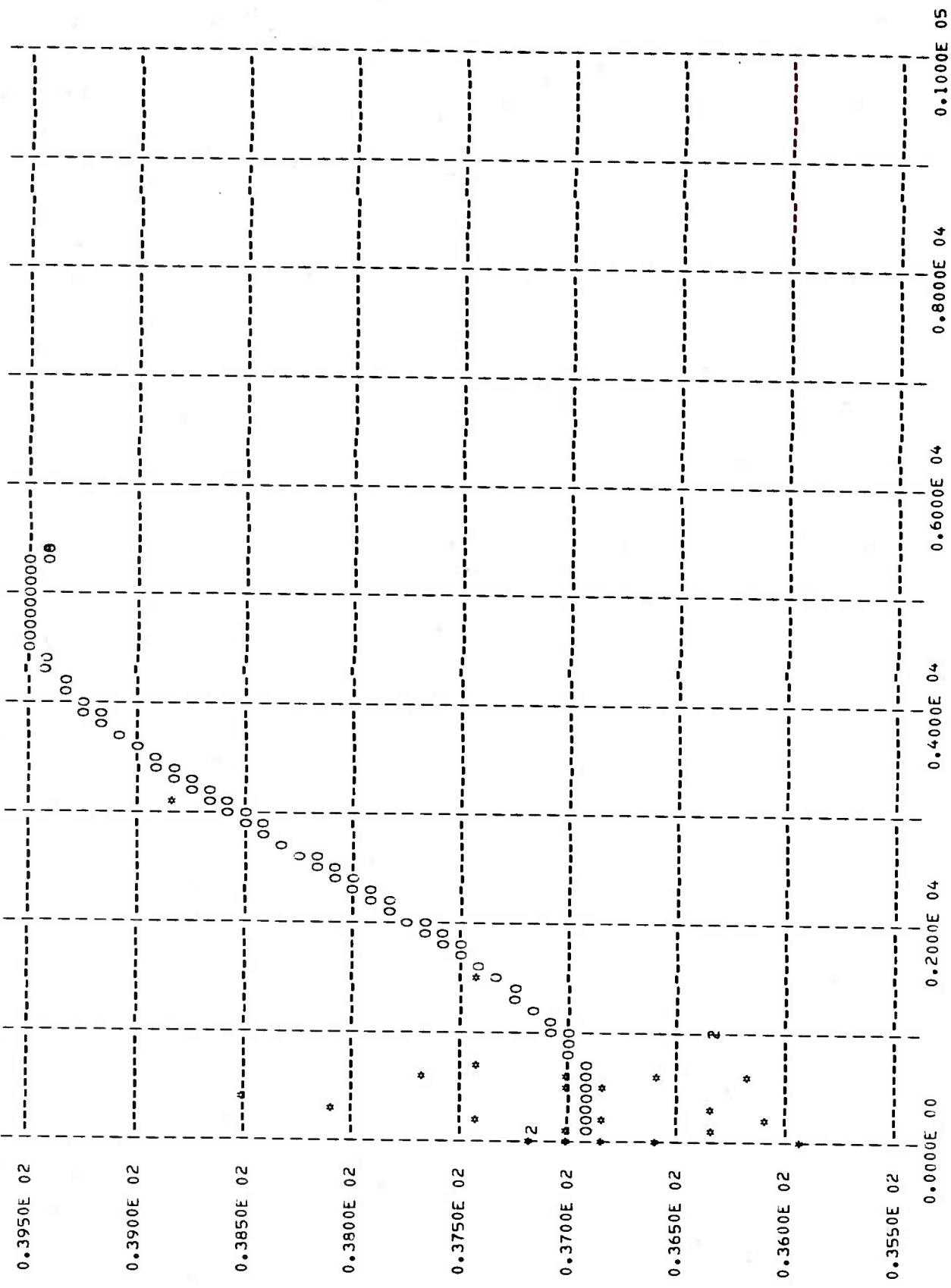
REGRESSION COEFS. FOR PMAX ON DELAY:

ZEROTH	FIRST	2ND	3RD
0.42477E 02	-0.78956E-01	0.35016E-03	-0.47713E-06

FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION:

INDEX	MED RANK	PMAX,KSI	DELP,PSI	DELAY,MS
1	0.0357	35.9000	0.00	93.00
2	0.0714	36.1000	0.00	105.00
3	0.1071	36.2000	0.00	105.00
4	0.1429	36.3000	30.00	117.00
5	0.1786	36.3000	39.00	120.00
6	0.2143	36.3000	106.00	120.00
7	0.2500	36.3000	124.00	121.00
8	0.2857	36.6000	127.00	125.00
9	0.3214	36.6000	143.00	127.00
10	0.3571	36.8000	174.00	135.00
11	0.3929	36.8000	190.00	136.00
12	0.4286	36.8000	197.00	137.00
13	0.4643	37.0000	296.00	140.00
14	0.5000	37.0000	302.00	143.00
15	0.5357	37.0000	436.00	150.00
16	0.5714	37.0000	458.00	154.00
17	0.6071	37.2000	476.00	160.00
18	0.6429	37.2000	556.00	171.00
19	0.6786	37.2000	584.00	173.00
20	0.7143	37.4000	644.00	175.00
21	0.7500	37.4000	648.00	205.00
22	0.7857	37.4000	713.00	211.00
23	0.8214	37.7000	990.00	212.00
24	0.8571	38.1000	1017.00	232.00
25	0.8929	38.5000	1479.00	253.00
26	0.9286	38.8000	3115.00	303.00
27	0.9643	39.4000	5388.00	380.00

REGRESSION OF PMAX ON DELP



REGRESSION OF PMAX (KSI) ON DELAY (MS)

A grid of 16 dashed boxes representing a 4x4 matrix. The diagonal elements are labeled with scientific notation values: 0.3950E 02, 0.3900E 02, 0.3850E 02, 0.3800E 02, 0.3750E 02, 0.3700E 02, 0.3650E 02, 0.3600E 02, 0.3550E 02, 0.3500E 02, 0.3450E 02, 0.3400E 02, 0.3350E 02, 0.3300E 02, 0.3250E 02, and 0.3200E 02. The off-diagonal elements are mostly zero, with some non-zero entries marked by asterisks (*).

PARAMETER ESTIMATES OF THE C.D.F. OF DEEP OBTAINED BY MATCHING MOMENTS

THE ESTATE OF THE LATE MR. C. D. T. OR
SELF OBTAINED BY MATCHING MOMENTS

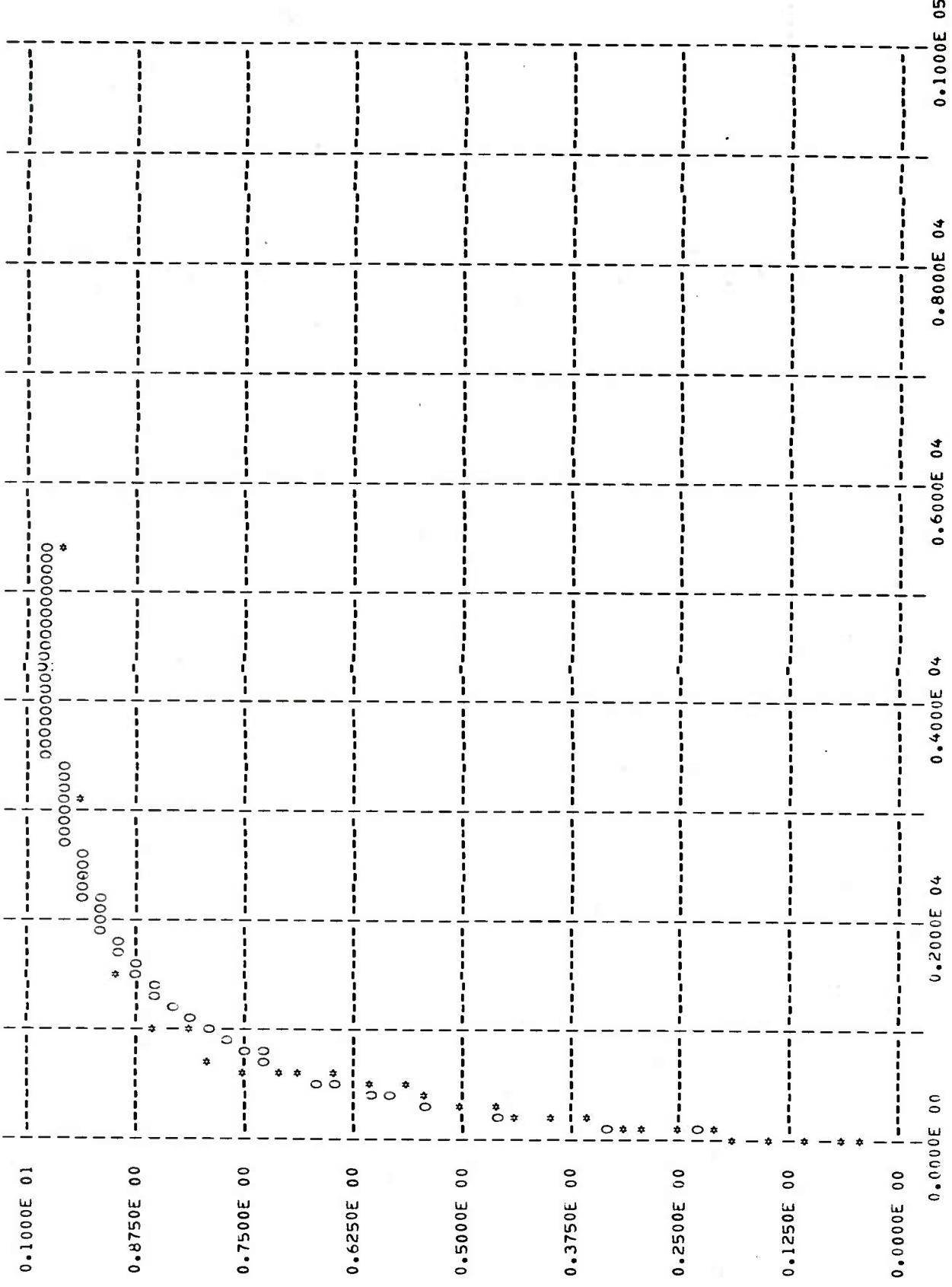
APPROXIMATE STD. DEV. OF ESTIMATE OF BETA = 0.06434
 ZERO VALUES ENCOUNTERED PRECLUDES THE CALCULATION OF MAXIMUM LIKELIHOOD ESTIMATES. MATCHING MOM. PARAMS. ARE KEPT.

INDEX	DELP,KS1	CDF	DSTAR	SSTAR
1	0.0000	-0.0000	0.0370	0.0370
2	0.0000	-0.0000	0.0741	0.1111
3	0.0000	-0.0000	0.1111	0.2222
4	30.0000	0.1659	0.0547	0.2770
5	39.0000	0.1922	0.0441	0.3210
6	106.0000	0.3278	0.1426	0.4636
7	124.0000	0.3546	0.1323	0.5960
8	127.0000	0.3588	0.0995	0.6955
9	143.0000	0.3802	0.0639	0.7794
10	174.0000	0.4175	0.0841	0.8635
11	190.0000	0.4349	0.0645	0.9280
12	197.0000	0.4422	0.0347	0.9627
13	296.0000	0.5284	0.0839	1.0467
14	302.0000	0.5328	0.0513	1.0980
15	436.0000	0.6156	0.0971	1.1951
16	458.0000	0.6268	0.0713	1.2663
17	476.0000	0.6356	0.0430	1.3094
18	556.0000	0.6710	0.0414	1.3508
19	584.0000	0.6822	0.0215	1.3723
20	644.0000	0.7042	0.0365	1.4088
21	648.0000	0.7056	0.0722	1.4810
22	713.0000	0.7268	0.0880	1.5690
23	990.0000	0.7963	0.0556	1.6246
24	1017.0000	0.8017	0.0872	1.7119
25	1479.0000	0.8702	0.0558	1.7676
26	3115.0000	0.9609	0.0350	1.8026
27	5388.0000	0.9895	0.0265	1.8292

SAMPLE IS PLASIBLE FROM THE HYPOTH. C.D.F. USING THE F-S TEST S STAR = 1.0292

LILLIEFORS (K-S) TEST SHOWS SAMPLE IS PLASIBLE FROM THE HYPOTH. C.D.F.
 TEST STATISTIC 0.1426 IS LESS THAN THE CRITICAL VALUE 0.1665 WITH A RISK OF 0.0500

PLOT OF HYPOTH. AND SAMPLE C.D.F.S OF DELP



TEST DATA FOR 8 IN. HDW. N188E1 CHG.--SET C4,COLD SOAK (-50 DEG F)

SAMPLE = 23 F-S CRITICAL VALUE = 2.337 F-S LEVEL OF RISK = 0.0500 DEG. DF PDLY. REGRES. = 3

Avg Pmax,KSI 37.2869	Avg DELP,PSI 467.3	Avg Todel,MS 153.7
SD: Pmax,KSI 0.5155	DELP,PSI 274.3997	DELAY,MS 35.2995

CORRELATION MATRIX:

Pmax	DELP	DELAY
1.0000	-0.0499	0.3734
-0.0499	1.0000	0.0773
0.3734	0.0773	1.0000

ANALYSIS BASED ON SIMPLE LINEAR REGRESSION OF PMAX DN DELP:

SLDPE = -0.00009 KSI/PSI STD. ERR. OF EST. OF PMAX GIVEN DELP = 0.52696 KSI

STD. DEV. DF SLOPE = 0.00041 95% CONF. LIMITS: -0.00095 0.00076 T-STATISTIC (CRITICAL) = 2.07965

PARTIAL CORRELATION CDEFS. WITH DEPENDENCE DF PMAX ON DELP AND DELAY ASSUMED

DELP, GIVEN DT DT, GIVEN DELP
-0.0852 0.3789

FRACTION OF VARIANCE DUE TD DELP = 0.0073

FRACTION OF VARIANCE DUE TO DELAY = 0.1436

I	NORM. CDEF.	XBAR(I)	SIGMA(I)	UNIT RESIDUAL
1	-0.00000E-01	4.672607E-02	2.744001E-02	0.00000E-01
2	2.968628E-00	2.903544E-05	2.848810E-05	-1.735842E-05
3	-7.212316E-00	2.076444E-08	2.754061E-08	3.471966E-05
4	4.369547E-00	3.7288694E-01	5.154914E-01	-1.106674E-04

DIMENSIONALIZED COEFFICIENTS

X(1)= 3.67721200E-01
X(2)= 5.57689700E-03
X(3)=-1.30506600E-05
X(4)= 8.17869800E-09
RES. M.S. R-SQUARED 2.680200E-01 0.128926

REGRESSION COEFS. FOR PMAX ON DELP:

ZEROTH FIRST 2ND
0.36772E-02 0.55769E-02 -0.13051E-04 0.81787E-08

FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION: 0.12893

DISTRIBUTION OF RESIDUALS FROM PMAX-DELP REGRESSION

INDEX	RESID.KSI	MED	RANK	NORM	D.F.	DSTAR	SSTAR
1	-0.7785	0.0417	0.0528	0.0528	0.0528	0.0528	0.0528
2	-0.7470	0.0833	0.0602	0.0602	0.0267	0.0795	0.0795
3	-0.6838	0.1250	0.0776	0.0776	0.0528	0.1324	0.1324
4	-0.4234	0.1667	0.1894	0.1894	0.0589	0.1913	0.1913
5	-0.3683	0.2083	0.2220	0.2220	0.0481	0.2394	0.2394
6	-0.2904	0.2500	0.2730	0.2730	0.0556	0.2950	0.2950
7	-0.2651	0.2917	0.2908	0.2908	0.0300	0.3250	0.3250
8	-0.2194	0.3333	0.3241	0.3241	0.0237	0.3486	0.3486
9	-0.1721	0.3750	0.3602	0.3602	0.0311	0.3797	0.3797
10	-0.1531	0.4167	0.3752	0.3752	0.0596	0.4393	0.4393
11	-0.0388	0.4583	0.4678	0.4678	0.0331	0.4724	0.4724
12	-0.0361	0.5000	0.4700	0.4700	0.0517	0.5241	0.5241
13	0.0098	0.5417	0.5081	0.5081	0.0571	0.5812	0.5812
14	0.0134	0.5833	0.5111	0.5111	0.0976	0.6788	0.6788
15	0.1136	0.6250	0.5933	0.5933	0.0589	0.7377	0.7377
16	0.2127	0.6667	0.6708	0.6708	0.0249	0.7625	0.7625
17	0.2240	0.7083	0.6792	0.6792	0.0599	0.8225	0.8225
18	0.3229	0.7500	0.7489	0.7489	0.0337	0.8561	0.8561
19	0.3244	0.7917	0.7499	0.7499	0.0762	0.9323	0.9323
20	0.3329	0.8333	0.7555	0.7555	0.1141	1.0464	1.0464
21	0.5798	0.8750	0.8859	0.8859	0.0271	1.0735	1.0735
22	0.8894	0.9167	0.9677	0.9677	0.0547	1.1282	1.1282
23	1.1537	0.9583	0.9918	0.9918	0.0352	1.1634	1.1634

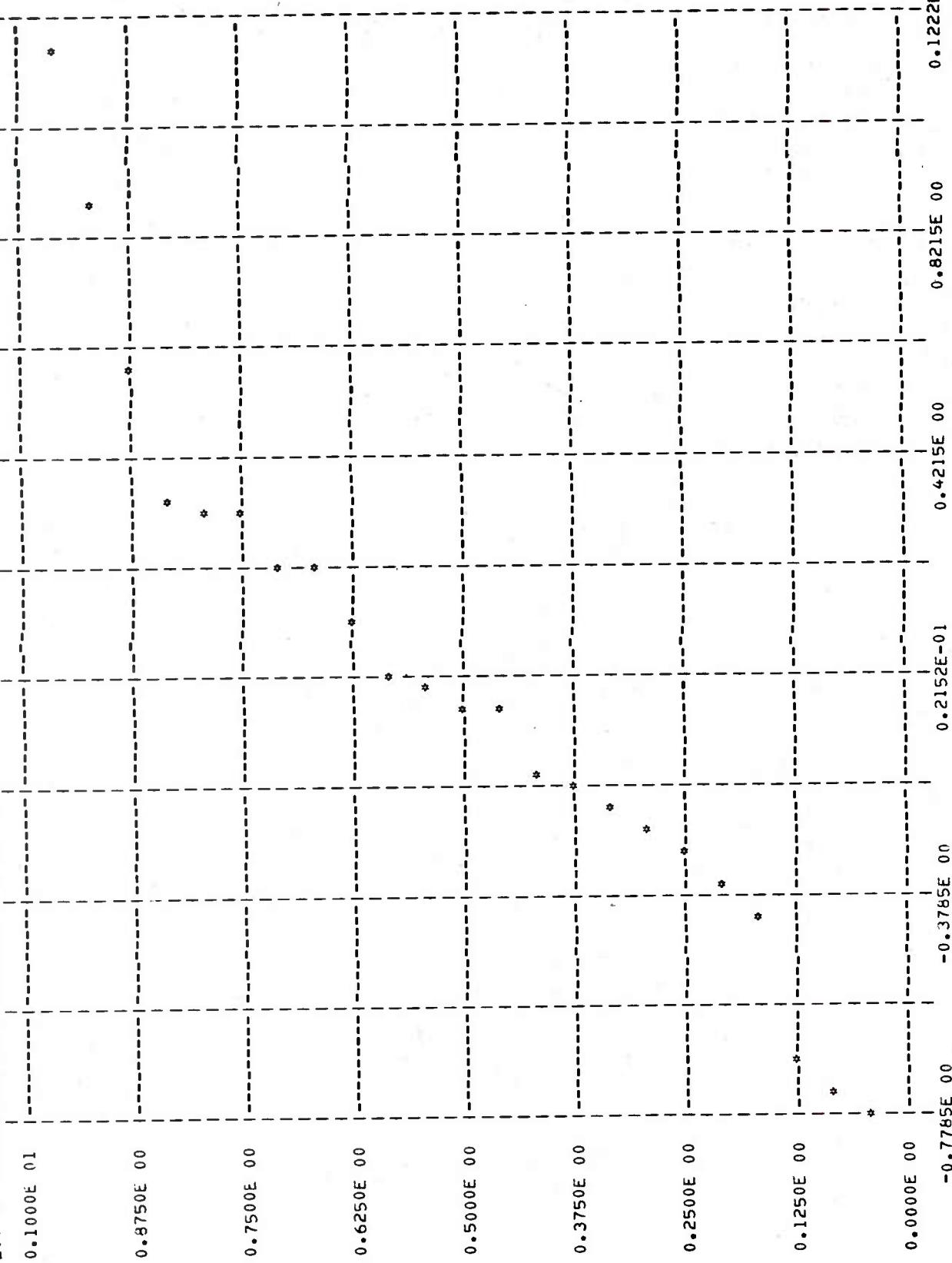
RESIDUALS ARE PLAUSIBLY GAUSSIAN.

SSTAR IN F-S TEST, 1.1634 IS LESS THAN THE CRITICAL VALUE, 2.3374

LILLIEFORS (K-S) TEST SHOWS RESIDUALS ARE GAUSSIAN.
TEST STATISTIC 0.1141 IS LESS THAN THE CRITICAL VALUE 0.1798 WITH A RISK OF 0.0500

MEAN AND STD. DEV. OF RESIDUALS (KSI): 0.00002 0.48112

PLOT OF CUMULATIVE DISTRIBUTION FUNCTION OF PMAX RESIDUALS



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I   NORM. COEF.      XBAR(I)      SIGMA(I)      UNIT RESIDUAL
1   -0.00000E-01     1.536522E 02    3.529950E 01    0.000000E-01
2   1.140126E 01     2.480087E 04    1.164159E 04    -3.076172E-05

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3 -2.149130E 01 4.199822E 06 3.054946E 06 6.371963E-07
 4 1.063285E 01 3.729694E 01 5.154914E-01 -9.620146E-06

DIMENSIONALIZED COEFFICIENTS

X(1) = 2.77705300E 01
 X(2) = 1.06496600E-01
 X(3) =-9.51638200E-04
 X(4) = 1.79418400E-06
 RES. M.S. R-SQUARED
 2.445485E-01 0.205209

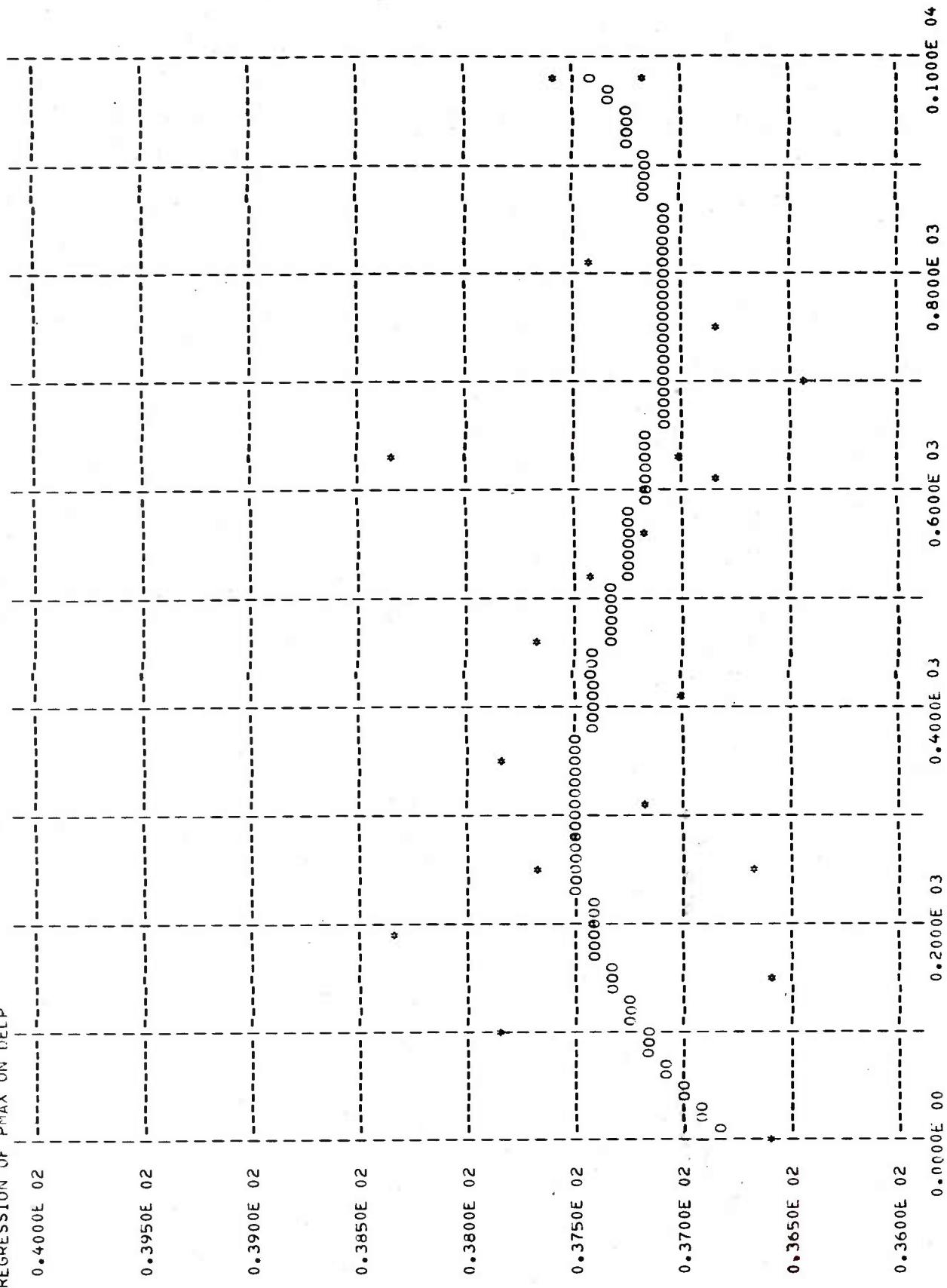
REGRESSION COEFS. FOR PMAX ON DELAY:

ZERO TH	FIRST	2ND	3RD
0.27771E 02	0.16650E 00	-0.95164E-03	0.17942E-05

FRACTION OF VARIANCE EXPLAINED BY THE REGRESSION:

INDEX	MED	RANK	PMAX, KSI	DELP, PSI	DELAY, MS
1	0.0417		36.4000	0.00	98.00
2	0.0833		36.6000	104.00	106.00
3	0.1250		36.6000	152.00	108.00
4	0.1667		36.7000	186.00	110.00
5	0.2083		36.8000	204.00	115.00
6	0.2500		36.8000	246.00	135.00
7	0.2917		37.0000	250.00	136.00
8	0.3333		37.0000	281.00	137.00
9	0.3750		37.2000	310.00	148.00
10	0.4167		37.2000	348.00	151.00
11	0.4583		37.2000	415.00	154.00
12	0.5000		37.2000	464.00	155.00
13	0.5417		37.4000	525.00	157.00
14	0.5833		37.4000	560.00	160.00
15	0.6250		37.4000	600.00	160.00
16	0.6667		37.5000	615.00	160.00
17	0.7083		37.6000	628.00	164.00
18	0.7500		37.7000	634.00	168.00
19	0.7917		37.7000	704.00	169.00
20	0.8333		37.8000	746.00	180.00
21	0.8750		37.8000	814.00	201.00
22	0.9167		38.3000	976.00	230.00
23	0.9583		38.3000	985.00	232.00

REGRESSION OF PMAX ON DELP



REGRESSION OF PMAX (KSI) ON UDELAY (MS)

0.4000E 02

0.3950E 02

0.3900E 02

0.3850E 02

0.3800E 02

0.3750E 02

0.3700E 02

0.3650E 02

0.3600E 02

$$11.7586 \text{ ETA} = 524.7942 \text{ DF} = -0.00014$$

COUNT = 21

0.3685

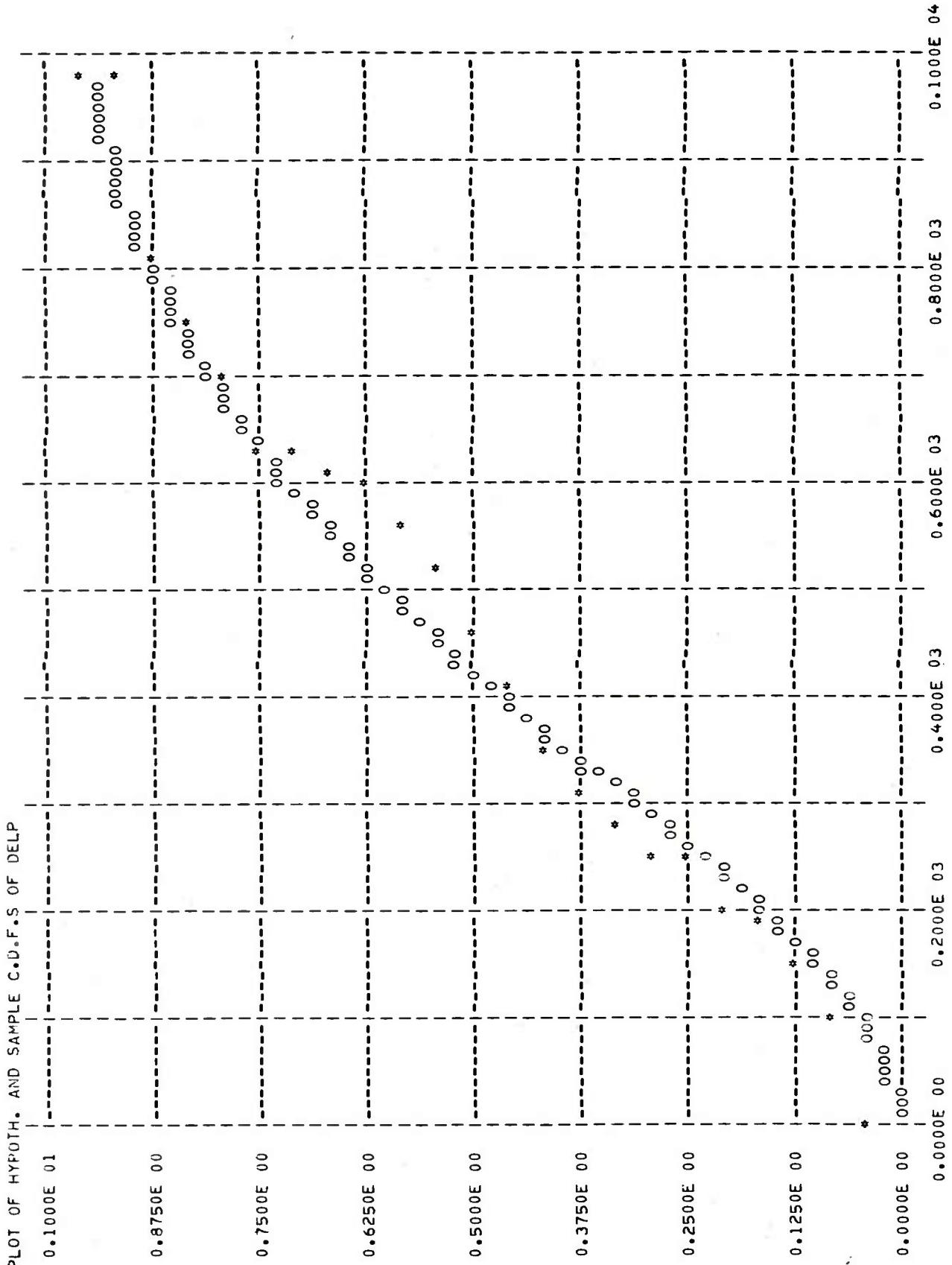
PROXIMATE STD. DEV. OF ESTIMATE OF BETA = 0.3685
ZERO VALUES ENCOUNTERED PRECLUDES THE CALCULATION OF MAXIMUM LIKELIHOOD ESTIMATES.

MATCHING MOM. PARAMS. ARE KEPT.

INDEX	DELP, KSI	CDF	USTAR	SSTAR
1	0.0000	-0.0000	0.0435	0.0435
2	104.0000	0.0564	0.0306	0.0740
3	152.0000	0.1070	0.0235	0.0975
4	166.0000	0.1490	0.0249	0.1224
5	204.0000	0.1729	0.0445	0.1669
6	246.0000	0.2319	0.0290	0.1959
7	250.0000	0.2377	0.0666	0.2625
8	281.0000	0.2835	0.0643	0.3268
9	310.0000	0.3271	0.0642	0.3910
10	348.0000	0.3847	0.0501	0.4411
11	415.0000	0.4841	0.0493	0.4904
12	464.0000	0.5531	0.0748	0.5652
13	525.0000	0.6324	0.1106	0.6758
14	560.0000	0.6740	0.1088	0.7847
15	600.0000	0.7179	0.1092	0.8939
16	615.0000	0.7333	0.0812	0.9750
17	628.0000	0.7462	0.0506	1.0256
18	634.0000	0.7520	0.0306	1.0562
19	704.0000	0.8129	0.0303	1.0865
20	746.0000	0.8437	0.0258	1.1124
21	814.0000	0.8851	0.0279	1.1403
22	976.0000	0.9491	0.0360	1.1763
23	985.0000	0.9515	0.0485	1.2248

SAMPLE IS PLAUSIBLE FROM THE HYPOTH. C.D.F. USING THE F-S TEST S STAR = 1.2248

LILLIEFOR'S (K-S) TEST SHOWS SAMPLE IS PLAUSIBLE FROM THE HYPOTH. C.D.F.
TEST STATISTIC 0.1106 IS LESS THAN THE CRITICAL VALUE 0.1798 WITH A RISK OF 0.0500



```

C CONSTRAINED QUADRATIC REGRESSION
1 IMPLICIT REAL*8(A-H,O-Z)
2 DIMENSION TITLE(20),DATA(400,3),Y(400),X1(400),X2(400),XMS(4),
3   R(4),CU(4),C1(4),C2(4),R(4),S(4)
4 EQUIVALENCE (DATA(1,15,Y(1)),(DATA(1,2),X1(1)),(DATA(1,3),X2(1)),
5 COMMON/GCO/RU,R1
6 CONTINUE
7 READ (5,10) NSAMP
8 FORMAT(20H4)
9 WRITE (6,12) TITLE
10 FORMAT(1H1,20A4)
11 READ (5,14) NSAMP,A0,A1,A2,A3
12 FORMAT(1I3,7X,4F10.0)
13 WRITE (6,114) A0,A1,A2,A3
14 FORMAT(1H0,8X,2H40,8X,2H1,8X,2H2,8X,2H3/1H .,4F10.4)
15 X=0.0D0
16 DX=0.1D0
17 WRITE(6,13) NSAMP
18 FORMAT(1H0,NSAMP =,13/1H0.9X,1HY,8X,2HX1,8X,2HX2)
19 READ DATA ARRAYS
20 DO 15 I=1,NSAMP
21   READ (5,18) Y(I),X1(I),X2(I)
22   WRITE (6,17) Y(I),X1(I),X2(I)
23   CONTINUE
24 CALCULATE R AND S COEFFICIENTS FROM THE DATA
25 DO 20 J=1,4
26   R(J)=0.0D0
27   S(J)=0.0D0
28   SO=0.0D0
29   DO 22 I=1,NSAMP
30     SO=SO+Y(I)
31   DO 24 J=1,n,
32     R(J)=R(J)+X1(I)**J
33     IF (J.GT.2) GO TO 21
34     S(J)=S(J)+X1(I)*J**Y(I)
35   CONTINUE
36   CONTINUE
37   CONTINUE
38   RO=NSAMP
39   R1=R(1)
40 CALCULATE ELEMENTS OF THE A MATRIX
41   A11=R(2)-R(1)**2/R0
42   A21=A12
43   A22=R(4)-R(2)**2/R0
44   R1=S(1)-R(1)*SO/R0
45   R2=S(2)-R(2)*SO/R0

```

```

C CASE 1, ... CO-JSTRAINTS: LAMBDA1(ELS1)=LAMBDA2(ELS2) = 0.
C
C DENO=M=A11*A22-A12*A21
C C1(1)=(A22*B1-A12*B1)/DENOM
C C2(1)=(A11*B2-A12*B1)/DENOM
C C0(1)=S0/R0-C1(1)*C1(2)/(R0-C2(1)*R(2))/RO
C CALL GRANGE(CU(1),C1(1),C2(1),0.000,0.000,X1,Y1)
C XMS(1)
C
C CASE 2, C1=0, C2=NE.0 (LAMBDA2=0)
C
C C1(2)=0.000
C C2(2)=B2/A22
C ELS1=2.000*(C2(2)*A12-B1)/RO
C ELS2=0.000
C C0(2)=S0/R0-C2(2)*R(2)/RO
C CALL GRANGE(CU(2),C1(2),C2(2),ELS1,ELS2,NSAMP,4000,X1,Y1)
C XMS(2)
C
C CASE 3, C1.NE.0 (LAMBDA1=0), C2=0
C
C C2(3)=0.000
C C1(3)=B1/A11
C ELS1=0.000
C ELS2=(C1(3)*A21-B2)/R(1)
C C0(3)=S0/R0-C1(3)*R(1)/R0
C CALL GRANGE(CU(3),C1(3),C2(3),ELS1,ELS2,NSAMP,4000,X1,Y1)
C XMS(3)
C
C CASE 4, C1 = C2 = 0. LAMBDA1.NE.0, LAMBDA2.NE.0.
C
C C1(4)=0.000
C C2(4)=0.000
C C0(4)=S0/R0
C ELS1=-2.000*B1/RO
C ELS2=-B2/R(1)
C CALL GRANGE(CU(4),C1(4),C2(4),ELS1,ELS2,NSAMP,4000,X1,Y1)
C XMS(4)
C
C FIND A FEASIBLE CASE FOR WHICH THE LAGRANGIAN IS MINIMAL
C
C IF(C1(1).LT.0.000.OR.C2(1).LT.0.000) GO TO 48
C HMIN=H(1)
C GO TO 50
C 48 CONTINUE
C IF(C1(2).LT.0.000.OR.C2(2).LT.0.000) GO TO 52
C IF(C1(3).LT.0.000.OR.C2(3).LT.0.000) GO TO 54
C HMIN=DMIN1(H(2),H(3),H(4))
C GO TO 50
C 52 CONTINUE
C
C 0-IT CASE 2 AS FEASIBLE
C
C IF(C1(3).LT.0.000.OR.C2(3).LT.0.000) GO TO 56
C HMIN=DMIN1(H(3),H(4))
C GO TO 50
C 56 H(4)=H(4)
C GO TO 50

```

```

83      54 CONTINUE
84      C CASE 2 IS FEASIBLE; OMIT CASE 3
85      C MIN=L1*(Z)+M(+)
86      50 CONTINUE
87      C WRITE HEADINGS FOR THE OUTPUT OF ALL CASES
88      C
89      WRITE (6,23)
90      26 FORMAT(1H0,10H CASE NO.,13X,2HC0,13X,2HC1,13X,2HC2,5X,
91      1 10HLAGRANGIAN,SX,10HMEAN SGR(S.) )
92      DO 30 J=1,4
93      IF (H(J)*E.Q.MIN) JOPTI=J
94      WRITE (6,32) J,C0(J),C1(J),C2(J),H(J),XMS(J)
95      32 FORMAT(1H ,7X,I3,5U15.5)
96      30 CONTINUE
97      WRITE (6,34) JOPTI
98      34 FORMAT(1H0,'THE OPTIMAL CASE UNDER CONSTRAINTS IS ',I3)
99      GO TO 1
C
C RETURN FOR PROCESSING OF ANOTHER DATA SET
C
C 3 CONTINUE
C 96 3 CONTINUE
C 97 CALL EXIT
C 98 STOP
C 99 END
C
C SUBROUTINE GRANGE(C0,C1,C2,ELS1,ELS2,N,NDIM,X,Y,H,XMS)
C
C THIS PROGRAM CALCULATES THE LAGRANGIAN AND MEAN SQUARED
C ERROR FOR A CONSTRAINED QUADRATIC REGRESSION OF Y ON X.
C CONSTRAINTS ARE: POSITIVE Y(X) AND POSITIVE SLOPE EVERYWHERE.
C
C IMPLICIT REAL*8 (A-H,O-Z)
C DIMENSION X(NDIM),Y(NDIM)
C COMMON/GCOM/RO,R1
C XMS=0.0D0
C H=0.0D0
C DO 1 I=1,N
C 101  TE*P=(Y(I)-C0-C1*X(I)-C2*X(I)**X(I))**2
C 102  XMS=XMS+TE*P
C 103  R1=R1+1
C 104  H=H+TE*P
C 105  106  DO 1 I=1,N
C 107  TE*P=(Y(I)-C0-C1*X(I)-C2*X(I)**X(I))**2
C 108  XMS=XMS+TE*P
C 109  R1=R1+1
C 110  H=XMS-ELS1*R1*C1-2.0D0*ELS2*R1*C2
C 111  XMS=XMS/(I-3)
C 112  RETURN
C 113  END

```

ENTRY

SECURED CARGO (NOT) -- SET 41

	A1	A1	A2	A3
0.0000	0.0000	0.0000	0.0000	0.0000

NSAMP = 26

	X1	X2
42.80	2740.00	60.00
42.70	843.00	64.00
41.50	531.00	54.00
42.60	1886.00	51.00
43.00	813.00	57.00
43.50	641.00	123.00
41.00	226.00	38.00
41.20	889.00	104.00
42.00	903.00	90.00
42.40	68.00	102.00
43.00	650.00	81.00
42.50	1681.00	78.00
43.20	227.00	103.00
43.00	459.00	102.00
42.20	424.00	93.00
42.10	1661.00	79.00
42.60	744.00	98.00
43.00	2321.00	79.00
42.90	4008.00	57.00
42.30	2171.00	84.00
41.80	4200.00	66.00
41.30	2512.00	67.00
41.60	1944.00	104.00
41.60	733.00	103.00
42.60	1193.00	106.00
42.60	697.00	93.00

CASE NO.	LAGRANGIAN			MEAN SQR'S.
	C0	C1	C2	
1	0.42393D 02	-0.46860D-04	0.65557D-08	0.11227D 02
2	0.42360D 02	0.00000D 00	-0.465592D-08	0.11233D 02
3	0.42377D 02	-0.22775D-04	0.00000D 00	0.11229D 02
4	0.42346D 02	0.00000D 00	0.00000D 00	0.11245D 02

THE OPTIMAL CASE UNDER CONSTRAINTS IS 4

SECURED CATALOG (HUT) -- SET 142

A ₀	0.0000
A ₁	0.0000
A ₂	0.0000
A ₃	0.0000

NSAMP = 21

	X1	X2
Y	1591.00	60.00
43.20	736.00	87.00
42.90	525.00	51.00
43.60	3187.00	62.00
42.40	1865.00	72.00
43.30	1540.00	40.00
41.80	1760.00	60.00
43.40	6973.00	78.00
43.20	1883.00	46.00
42.00	2020.00	59.00
41.40	2098.00	63.00
43.20	92.00	110.00
42.30	341.00	83.00
41.80	344.00	75.00
42.50	1067.00	92.00
42.20	1064.00	82.00
43.00	1847.00	85.00
42.90	270.00	110.00
40.80	313.00	105.00
42.40	1737.00	60.00
42.80	621.00	110.00

CASE NO.	C0	C1	C2	MEAN SQRS.
1	0.42586D-02	-0.15655D-03	0.34355D-07	0.10955D-02
2	0.42441D-02	0.00000D-00	0.13422D-07	0.11090D-02
3	0.42396D-02	0.68355D-04	0.00000D-00	0.11273D-02
4	0.42500D-02	0.00000D-00	0.00000D-00	0.11480D-02

THE OPTIMAL CASE UNDER CONSTRAINTS IS 2

```

***** *RISK M110A1*****
C PROGRAM TO CALCULATE THE PROBABILITY THAT THE MAX CHAMBER
C PRESSURE, PMAX, EXCEEDS A CRITICAL VALUE
C
C DIMENSION TITLE(20)
C
C 1 2 1 CONTINUE
C
C READ DESCRIPTIVE ALPHAMERIC TITLE
C
C 3 4 READ (5,10,END=3) TITLE
C 10 FORMAT(20A4)
C 11 WRITE (6,12) TITLE
C 12 FORMAT(1H1,20A4)
C 13 READ (5,14) A0,A1,A2,SIGZ,BETA,ETA,PMCRIT,EPS
C 14 FORMAT(7F10.0,1E10.3)
C 15 WRITE (6,16) A0,A1,A2,SIGZ,BETA,ETA,PMCRIT,EPS
C 16 FORMAT(1H0,10X,2HA0,10X,2HA1,10X,2HA2,4X,8HSIGZ,KSI,8X,4HBETA,
C 15X,7HETA,KSI,2X,10HPMCRT,KSI,9X,3HEPS/1H ,7F12.5,E12.3)
C
C CALCULATE STEP SIZE FOR NUMERICAL INTEGRATION AND THE
C INITIAL VALUE OF THE INDEPENDENT VARIABLE, DELP (KSI)
C
C XLIM=50.0E0
C H=FMIN1(0.002*SIGZ,0.002*ETA)
C HO2=H/2.0E0
C ALNE=-ALOG(EPS)
C XN=ETA*(ALNE)**(1.0E0/BETA)
C IF (XN.GT.XLIM) XN=XLIM
C Y=PMCRIT
C
C 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37
C
C START INTEGRATION AT X=0.
C
C X1=H
C 22 CONTINUE
C 21 WRITE (6,21) X1,XN,H
C 21 FORMAT(1H0,'LIMITS OF INTEGRATION ON DELP (KSI) ARE: ',2F12.5,
C 1 4X,'STEP SIZE IS ',F12.5)
C
C START INTEGRATION
C
C CALL GINT(Y,A0,A1,A2,SIGZ,BETA,ETA,X1,G1,GL1)
C RISK=GL1
C FY=G1
C X=X1
C
C 24 CONTINUE
C X=X+H
C CALL GINT(Y,A0,A1,A2,SIGZ,BETA,ETA,X,G2,GL2)
C RISK=RISK*GL1*GL2
C FY=FY+G1*G2
C G1=G2
C GL1=GL2
C IF (X.LE.XN) GO TO 24
C FY=FY*HO2
C RISK=RISK*HO2
C RISK2=1.0E0-FY

```

```

38     ERR=(GL1+GL2)*H02
39     WRITE(6,30) RISK,FY,RISK2,ERR
40     30 FORMAT(1H0,20H RISK PMAX,6T.PMCRT,6X,14HC,D.F. (PMCRIT),
41           1 10X,10H1 - C.D.F.,8X,12HSTEP IN RISK/1H ,4E20.5)
42     GO TO 1
43     3 CONTINUE
44     CALL EXIT
45     STOP
46     END
***** GINT *****
46     C   SUBROUTINE GINT(Y,A0,A1,A2,SIGZ,BETA,ETA,X,G,GL)
47     C   SUBROUTINE EVALUATES THE INTEGRAND IN THE M110A1 RISK ASSESSMENT
48     FX=(BETA/ETA)*(X/ETA)**(BETA-1.0E0)* EXP(-(X/ETA)**BETA)
49     PMBAR=A0+A1*X+A2*X*X
50     IF (PMBAR.LT.0.0E0) PMBAR=0.0E0
51     Z=Y-PMBAR
52     ARGZ=Z/SIGZ
53     IF (ARGZ.LT.-5.0E0) GO TO 1
54     IF (ARGZ.GT.5.0E0) GO TO 2
55     FZ=SNORM(ARGZ)
56     IF (FZ.LT.0.0E0) GO TO 4
57     IF (FZ.GT.1.0E0) FZ=1.0E0
58     1 FZ=0*0E0
59     2 FZ=1.0E0
60     3 FZ=1.0E0-FZ
61     G=FX*FZ
62     GL=FX*FZ1
63     RETURN
64
65     4 CONTINUE
66     WRITE(6,5)
67     5 FORMAT(1H0,'ERROR. FZ IS NEGATIVE')
68     CALL EXIT
69     STOP
70     END

```

\$ENTRY

RISK OF A CAT. FAILURE IN THE M110A1 SP HOW USING THE M188E1 CHG AT 145F W/ R.H.

A0	0.11657	A1	0.06800	A2	0.58390	SIGZ-KSI	1.08100	BETA	1.33100	PMCRIT-KSI	53.00000	EPS	0.100E-05
LIMITS OF INTEGRATION ON DELP (KSI) ARE:													
RISK PMAX.GT.PMCRIT	0.22172E-04	C.D.F.(PMCRIT)	0.99863E 00	1 - C.D.F.	0.13714E-02	STEP IN RISK	0.11535E-08	STEP SIZE IS	0.00117				

RISK OF A FAILURE IN THE M110A1 SP HOW USING THE M188E1 CHG AT 145 F W/O R. H.

A0 A1 A2 SIGZ*KSI BETA ETA*KSI PMCRIT*KSI
42.22301 -0.11881 0.03762 0.75510 1.22200 1.57000 53.00000 0.100E-05

LIMITS OF INTEGRATION ON DELP (KSI) ARE:

RISK PMAX.GT.PMCRIT C.D.F.(PMCRIT)
0.00000E 00 0.99889E 00
 1 - C.D.F.
 0.11116E-02 STEP IN RISK
 0.00000E 00

RISK OF FAILURE IN THE M110A1 USING THE M188E1 CHG AT -50 F W/ R. H.

	A0	A1	A2	SIGZ-KSI	BETA	ETA-KSI	PMCRIT-KSI	EPS
36.79800	0.34983	0.03018	0.62270	0.62110	0.46880	53.00000	0.100E-06	

LIMITS OF INTEGRATION ON DELP (KSI) ARE:

RISK PMAX*GT*PMCRIT	C.D.F.(PMCRIT)	1 - C.D.F.	STEP IN RISK
0.63789E-04	0.98399E 00	0.16007E-01	0.22782E-10

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