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RESOURCE ALLOCATION IN THE PIPELINED SYSTEM



FINAL REPORT

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Abstract (cont.) organized programs is also developed. Finally, a scheme using intelligent buffers to improve the performance of interleaved memory is developed and analyzed. White Section C ACCESSION for Bull Section D NTIS UNANNOUNCED DOC JUSTIFICATION DISTRIBUTION AVAILABILITY POPTS BY Dist

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1. Introduction

This report summarizes the findings of our research supported by the U. S. Army Research Office through grant DA-ARO-D-31-124-73-G157. Most of the results reported here are published in the technical papers, Ph.D. dissertations and M.S. theses given in the References. Eleven graduate students have been supported by the grant to pursue advanced degrees at the University of California, Berkeley.

This investigation has been an attempt to establish some foundation for solving design and operational problems related to computer architectures which utilize concurrency in computation to attain more computing power than is allowed by today's electronic technology. The emphasis of our research under the grant has been on pipeline architectures [Ram 77]. But in the course of our research, some new results in parallel processing and memory organization are developed. Parallel processing complement pipelining in increasing the capability of a processing system and the memory bottleneck must be solved if all the advantages of pipelining and parallel processing are to be realized.

We shall briefly discuss our findings in these research areas in three separate sections, one for each topic. A summary section is given at the end.

2. Pipeline Systems

2.1. Overview

Pipelining can be viewed as a mode of exploiting computational parallelism. It can be roughly defined as a technique of imbedding concurrency in execution by constructing a system configuration composed of independent autonomous units each dedicated to perform a specific

-1-

subfunction in an overlapped mode with the others [Ram 74b]. Such an autonomous unit is sometimes called a pipeline segment or facility. A task once initiated flows from segment to segment inside the pipe to be processed. As an illustration, the schematic of a pipelined instruction unit is shown in Fig. 1.



Fig. 1. An example pipelined instruction unit.

It is easy to see that if an uninterrupted stream of instructions is allowed to flow through the pipeline shown in Fig. 1, the throughput rate of the system will be one instruction per 600 nanosecond. The basic objective of pipelining is to maximize throughput through efficient utilization of resources. Compared with parallel processing, pipelining is not geared to shorten response time, but it increases system throughput rate in a more economical way. Furthermore, the effect of overhead on system throughput rate in operating a pipeline system is almost invisible. This is mainly because this overhead can also be overlapped with the other useful operations. Many modern computers (e.g. IBM 360/195, Amdahl 470 and the Cray computers) have extensively utilized pipelining in their processor architecture.

The structure of a pipeline system can be quite complicated. A segment may be used at different times to complete the processing of a task (see Fig. 2). Sometimes there may be several pipelines in the system sharing certain facilities. The TIASC arithmetic unit as shown in Fig. 3 is a notable exampel of such systems. To complicate the issues further, the tasks to be processed may have different processing and resource

-2-



Fig. 2. A single function pipeline with feedback.



RESULTS

Fig. 3. Pipelined arithmetic unit in TIASC. An example of multifunction pipeline.

requirements. The tasks may require different amounts of time to be processed in a segment; they may be tightly coupled by some precedence relations; and if not appropriately controlled they may race for the service of shared segments and resources (e.g. registers). The difficulty of most effectively designing and controlling the operation of a pipeline system has presented a very challenging area of fruitful research. We have extensively surveyed existing theoretical results and practices of pipelining in [Ram 77a].

The results we obtained in tackling some problems in pipelining can be grouped into four areas: (1) modeling of pipeline systems for effective control and performance evaluation; (2) sequencing strategies and their inherent complexity; (3) design methods to optimize cost-effectiveness; (4) program restructuring and optimal register assignment for pipelined processors. These results are summarized in the following four sections.

2.2. Modeling of pipeline system

The objective of our earlier pipelining studies was aimed at establishing an unified analytical model for the design and control of pipeline systems. In [Red 72], we developed a scheme for categorizing various types of pipeline systems based on the flow pattern of tasks in the pipeline, amount of intermediate storage and the nature of the tasks (e.g. absence or presence of dependence). Subsequently, a study was made on the various scheduling algorithms for each category [Red 73].

In [Ram 74a], reconfigurable shared resource pipeline (RSRP) systems were considered in full generality. A useful concept of efficiency measure which considers cost, speed and space-time span of the segments of a pipeline system was established so that the effectiveness and feasibility of a pipeline system can be analyzed. A RSRP system can be

-4-



P₁: 1-2-3-4
P₂: 1-5-3-6
(Speed of each facility
is as labeled.)
Collision matrix:

$$t_{11} = (15, \infty)$$

$$t_{12} = ((4, 10), (16, \infty))$$

$$t_{21} = (4, \infty)$$

$$t_{22} = (4, \infty)$$

Fig. 4. Example collision matrix.

modeled by a digraph where a node represents a segment and an arc indicates the flow of control from one segment to the other. A collision matrix was introduced in [Ram 74a]. It can be used to avoid collisions inside a RSRP system. (A collision occurs when more than one task attempts to use a shared segment at the same time.) Figure 4 shows a RSRP system with its corresponding collision matrix. The (i,j)th entry of the matrix represents the time intervals after the initiation of a task to flow through pipe i so that the excitation of a task to flow through pipe j will not casue a collision.

Concurrently with the research reported above a scheme called the dynamic sequencing and segmentation model (DSSM) was developed with the objective of concealing the run-time overhead required to control the operation of a general parallel and pipeline system [Ram 74b]. A simulation study [Ram 73] showed the steady and high performance of the DSSM and the high feasibility for implementation.

2.3. Sequencing in pipeline systems

In general, the major obstacles to high efficiency in pipeline systems are caused by: (1) the inherent relationship between the tasks, (2) the scarcity of some expensive facilities, (3) the unequal and sometimes unpredictable execution time of the tasks in a given segment; and (4) the conflicts at some shared resource in the system. These factors indicate one critical problem to be solved: the optimal sequencing of the tasks to be admitted into the pipeline system. A sequencing strategy is optimal in the sense that maximum throughput is achieved while collisions on shared resources are avoided.

For simple RSRP systems with a bounded queue of ready tasks, an

-6-

efficient lookahead scheme to produce locally optimal sequences was developed in [Ram 74a]. The method can be extended to the dynamic case where huge tasks are involved, for example, in a computer network. The inherent complexity of sequencing tasks in a RSRP system was studied in [Ram 75b]. It was found that even under very strong assumptions when we have a static set of ready tasks and the execution time of the pipeline segments are deterministic, the optimal sequencing problem of pipeline system is NP-complete. This implies that its complexity is in the same class as the classical traveling salesman problem. From this result, the semi-exhaustive nature of an optimal strategy for pipeline system sequencing is justified. One implication is that for low level pipeline implementations, faster heuristics are necessary. Some efficient heuristics were proposed in [L1 75] and simulation experiments have demonstrated their effectiveness.

2.5. Design methods

The design problem can be informally stated as the following: Given an application, its throughput, reliability, cost and other requirements, how to most cost-effectively design a pipeline system for the application. In [Li 75], we developed a set of algorithms so that the design problem can be approached in a systematic way rather than using pure instinct, experience and ad hoc solutions. The design of a pipeline system can be approached in the following manner. First a basic skeleton machine and some relevant cost and effect functions can be derived based on the system and application objectives. A set of semi-dynamic programming strategies developed in [Li 75] can then be applied to obtain analytically the most cost-effective pipeline design without exhaustive enumeration. Further by appropriate duplication of some shared resources, a complex RSRP System

-7-

can be partitioned into simplier system. The result of the appropriate partitioning will lead to reduced control complexity, improved throughput and reliability. The partitioning algorithms are extended from the algorithms of Kerninghan-Lin and Ford-Fulkersen. Details of them can be found in [Li 75]. Another problem of interest is how to introduce redundancy to a ASRP system for improvement in reliability under cost constraints. A semi-dynamic programming algorithms for this problem under weak assumptions was developed also in [Li 75].

It should be mentioned here that these analytical design algorithm are developed not for the decision making, but as a tool to test decision and justify prediction or experience. In all cases it is recommended that both analytical and simulation evaluations be used to search for a good design.

2.5. Program restructuring and register allocation

The characteristics of a program have significant influence on the effectiveness and applicability of pipelining. In general, a program must possess suitable structures as well as abundant parallelism in order to fully utilize the multi-pipelines available. Restructuring a program is the process of organizing the original program in such a way that the final code has "good" characteristics with respect to the system configuration available. These characteristics would simplify the control procedure and thus improve the performance of the system. In general, how to best restructure a program is a difficult problem and it is intimately related to the pipeline configuration and the sequencing scheme used. Some efficient program restructuring strategies were developed in [Li 75] and they are studied, using simulation experiments, in the context of

-8-

some sequencing heuristics on systems whose models were based on some existing machines. (They include the STAR 100 and TIASC pipes).

A closely related problem is how to most effectively assign pipeline resources to tasks. We looked into the special case of assigning registers to instructions to be executed in a pipeline processor. In a pipeline processing system, the operand fetch and preparation phase of one instruction can be overlapped with the actual execution phase of some preceding instructions. While the latter time varies from instruction to instruction, the former is also variable depending on the register assignment. It is crucial for pipeline processors to employ a good register assignment that is not completely insensitive to the processor architecture, otherwise the overlapping power can be severely damaged. This problem is formulated in detail in [Li 77]. In general the problem is also inherently difficult. A non-exhaustive optimal algorithm is found under some strong assumptions. Efficient heuristics with certain performance bounds are proposed for other cases.

3. Parallel Processing

The term parallel processing can be defined as the mode of operation in which different sections of a program are processed by several units of a multi-processing system. The fundamental objective of parallel processing is to execute a program as fast as possible often at all costs which may be incurred. Although parallel processing is quite different from pipelining in the means used to achieve high computing power, these two techniques complement each other in imporving the performance of a processing system. Modern computers, almost without exception, utilize both techniques in their architecture. The parallel

-9-

execution unit of the instruction pipeline of the IBM360/91 is a notable example.

Under this grant, we have considered two different approaches to the identification of parallelism in a program. A set of language constructs were developed by which the programmer can explicitly indicate parallelism. On the execution level, a scheme was also developed to detect and control parallelism at run time.

In [Ram. 75a], control parts of parallel programming constructs, one at the machine level and the other at the source level were defined. With respect to these constructs technical foundation is established for detecting useful parallelism hidden in a source parallel program as well as for restructuring a program into the one leading itself to easier analysis and more effective execution. Another objective of these language construct is to impose constraints on the program structure so that the program reliability can be improved. Details of these constructs can be found in [Kim 74].

More recently, we developed a scheme to detect and control the execution of parallel tasks in run time [Ram. 76]. Unlike the traditional lookahead approach, parallelism detection is done by controls local to the processors in the new scheme. With information about how variables are used in the program and the status of tasks being executed, these local controls cooredinate with each other and synchronize the action of the processors so that precedence among tasks are preserved. The scheme minimized the overhead time before parallel execution and thus in effect removed the parallelism detection procedure as a bottleneck of the parallel processing system.

-10-

Associative search methods are also studied. An algorithm for ordered retrieval was developed in [Ram. 77b]. It is believed that the algorithm is the best one ever presented.

4. Memory Organization

The problem of memory contention has a significant effect on the efficiency of any pipeline and/or parallel system. This problem occurs when more than one task being executed concurrently needs to access the same memory module.

A scheme using intelligent buffers was developed for an interleaved memory in [Wah 76]. The goal there is to improve the performance of the memory by the addition of a small number of buffers. An analytical model based on discrete Markov chains has been developed to evaluate the scheme. The results show that significant improvement can be achieved with a small number of buffers. The analytical result is verified by a trace driven simulation.

5. Summary

This report summarizes the research findings obtained under grant DA-ARO-D-31-123-73-G157. Three related areas of advanced computer architecture are investigated. In pipelining, results obtained pertain to the modelling, sequencing control, design methods and tasks resource allocation problems of generalized pipeline systems. In parallel processing, language constructs which can effectively identify parallel tasks and a new scheme to detect parallelism in run time are developed. An efficient associative search algorithm for ordered retrieval is also proposed. Finally, a scheme using intelligent buffers to improve the performance of interleaved memory is developed and analyzed.

-11-

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-13-

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3