

SHIPSIM/OPTSIM: SIMULATION PROGRAM FOR STATIONARY LINEAR OPTIMAL STOCHASTIC CONTROL SYSTEMS

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These two program groups are described; User's Documentation, Programmer's Documentation, and listings are included as appendices. A simulation of an optimal stochastic path controller for a tanker operating in shallow water is presented as an example. The programs are written in FORTRAN IV and with the exception of the plotting portion of SHIPSIM, they are essentially independent of the Michigan Terminal System (MTS).



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SHIPSIM/OPTSIM: Simulation Program for Stationary, Linear Optimal Stochastic Control Systems

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ABSTRACT

The SHIPSIM/OPTSIM computer program for the simulation of stationary, linear optimal stochastic control systems is presented. This program consists of two separate entities:

- SHIPSIM is a general continuous system simulation program designed to provide a versatile simulation capability with simple user input. This program can be used for any continuous systems simulation problem which can be defined in the three user-supplied subroutines.
- OPTSIM is a group of subroutines which are run under SHIPSIM for the simulation of the response of stationary, linear optimal stochastic control systems to initial condition errors and specific user-supplied process disturbances while subject to measurement white noise.

These two program groups are described; User's Documentation, Programmer's Documentation, and listings are included as appendices. A simulation of an optimal stochastic path controller for a tanker operating in shallow water is presented as an example. The programs are written in FORTRAN IV and with the exception of the plotting portion of SHIPSIM, they are essentially independent of the Michigan Terminal System (MTS).

TABLE OF CONTENT

		Page
	Abstract	i
ı.	Introduction	1
II.	Optimal Control of Stochastic Linear Systems	2
III	. Description of SHIPSIM	. 8
ıv.	Description of OPTSIM	13
v.	Tanker Path Control Example	20
vi.	Closure	35
VII	. References	36
1	Appendices	
Α.	User's Documentation for SHIPSIM	A-1
в.	User's Documentation for OPTSIM	B-1
c.	User's Documentation for OPTSYS	C-1
D.	Programmer's Documentation for SHIPSIM	D-1
E.	Programmer's Documentation for OPTSIM	E-1
F.	Source Listing of SHIPSIM	F-1
G.	Source Listing of OPTSIM	G-1

I. INTRODUCTION

The computer programs presented in this report have been developed in support of research performed on the optimal stochastic path control of surface ships in shallow water. 1 The programs were written to have general utility and with the documentation provided here should be of value to others. The SHIPSIM program has already been used in other research and teaching applications in the Department of Naval Architecture and Marine Engineering. The SHIPSIM/OPTSIM program has been written to be used in conjunction with the Department's OPTSYS program which can very quickly and cheaply provide the design of the optimal controller and Kalman-Bucy filter for a stationary, linear system subjected to white noise process disturbances and measurement noise. The OPTSYS program was originally written by W. Earl Hall, Jr. 2 at Stanford University; a version of this program has been utilized in our research on the path control of ships. The OPTSYS program can evaluate the Root Mean Square (RMS) response of the optimal system to the design disturbances and noise. It is also often desirable to simulate the response of the controlled system to other specific process disturbances and/or initial condition errors. The SHIPSIM/OPTSIM program allows this simulation with a minimum of additional effort and expense.

To provide the maximum utility, the SHIPSIM and SHIPSIM/OPTSIM programs have been written to be completely separate. Users without an interest in stochastic control systems can use SHIPSIM alone for any continuous system simulation problem which can be defined in the user-supplied subroutines. This report has, therefore, been written so that a reader interested only in SHIPSIM need only to consult Section III "Description of SHIPSIM" and Appendices A,D, and G which contain the SHIPSIM documentation and listing. For the general reader, Section II contains a brief review of the stochastic control of linear systems, Section IV contains a description of OPTSIM as run under SHIPSIM, and Section V contains a short example use of the SHIPSIM/OPTSIM program for the simulation of the stochastic path control of a tanker. Appendices B, E, and G include the documentation and listing for OPTSIM. Appendix C includes the User's Documentation for our version of the OPTSYS program for additional reference. The documentation Appendices have been written to be essentially self-contained so they can be reproduced separately for subsequence use with the programs.

II. OPTIMAL CONTROL OF LINEAR STOCHASTIC SYSTEMS

Many physical control problems can most realistically be represented using stochastic disturbances and measurement noise. The response of such a system may then also be treated as a stochastic quantity. The optimal control of linear stochastic systems^{3,4,5} will be reviewed very briefly here as an introduction to the description of the SHIPSIM/OPTSIM program which follows. The engineering approach can be to model stochastic physical systems as Gauss-Markov processes which can be represented by the state vector of a linear dynamical system forced by a gaussian purely-random process where the initial state vector is also gaussian or normally distributed. Thus, we can represent the system by the following:

where en-loop dynamics matrix F, the control distribution matrix G, and sturbance distribution matrix Γ are assumed stationary (constant) here. The condition of the system is completely represented by the mean value n-vector $\overline{\mathbf{x}}$ and covariance matrix X for the n state (differentiated) variables; i.e.,

$$\underline{\underline{x}}(t) \equiv \underline{E}[\underline{x}(t)] \quad \text{with} \quad \underline{\underline{x}}(t_0) = \underline{x}_0 ,$$
 (2)

$$X(t) \equiv E[(\underline{x}(t) - \overline{x}(t)) (\underline{x}(t) - \overline{x}(t))^{T}] \text{ with } X(t_{O}) = X_{O},$$
 (3)

where E[...] is the expected value or ensemble average over the many possible observations at time t. The m non-differentiated variables in \underline{u} are the control variables. The q variables in \underline{w} are the process disturbances which are gaussian purely-random processes or white noise. White noise is an idealized, very-jittery process which can be viewed as the limit of a sequence of impulses with random magnitude and random time of occurence. The impulses average zero over time but have an average square magnitude given by $\sigma(t)$ squared. We thus have,

$$E[w(t)] = 0 , \qquad (4)$$

$$E[(\underline{w}(t) - \underline{w}(t)) (\underline{w}(\tau) - \underline{w}(\tau))^{T}] = Q(t) \delta(t - \tau) , \qquad (5)$$

where Q is the power spectral density matrix and $\delta(t-\tau)$ is the Dirac delta function. It is also assumed that there is no correlation between the process disturbance and the initial condition of the system; i.e.

$$E[(\underline{w}(t)-\overline{w}(t))(\underline{x}(t_0)-\overline{x}_0)^T] = 0.$$
 (6)

The control problem is to develop the optimal state variable feedback control,

$$\underline{\mathbf{u}} = \mathbf{C}\underline{\mathbf{x}} \quad , \tag{7}$$

where C is the control feedback gain matrix. In general, not all of the needed states in \underline{x} are readily measured. Further, it is not necessary to measure all the states if it is possible to estimate the remaining states from those which are most easily measured. In the stochastic case we may have p measurements available represented by,

where H is the measurement distribution matrix (assumed constant here) and $\underline{\mathbf{v}}$ is a vector of white measurement noise with statistical properties,

$$E[\underline{v}(t)] = 0 , \qquad (9)$$

$$E[\underline{v}(t)\underline{v}(\tau)^{T}] = R(t)\delta(t-\tau) , \qquad (10)$$

$$E[\underline{v}(t)\underline{w}(t)^{T}] = E[\underline{v}(t)(\underline{x}(t_{O})-\overline{\underline{x}_{O}})^{T}] = 0.$$
(11)

The matrix R is the power spectral density of the measurement noise. Equation (11) states that there is no correlation between the measurement noise and the process disturbance or the initial state of system. The elements of \underline{z} may be measurements of specific states or linear combinations of the states.

The Separation Theorem³ states that the optimal way to control the system eq. (1) using the information available in the noisy measurements eq. (8) is to design the controller gains eq. (7) neglecting \underline{w} and \underline{v} and thus assuming perfect knowledge of \underline{x} . The noisy measurements \underline{z} can be utilized in an optimal stochastic observer (state estimator) or Kalman-Bucy filter to produce a maximum-likelihood estimate of the state \hat{x} and the optimal control will then be,

$$\underline{\mathbf{u}} = \mathbf{C}\hat{\mathbf{x}} \quad . \tag{12}$$

Thus, the controller design is completely separated from the processing of the noisy measurements to produce the best estimate of the current state of the system. An overall schematic of such a stochastic control system is shown in Figure 1. The measurements \underline{z} from the sensors are used in the optimal stochastic observer to produce an estimate of the states $\hat{\underline{x}}$ which are then used in the optimal controller to produce the control signals \underline{u} given to the actuators.

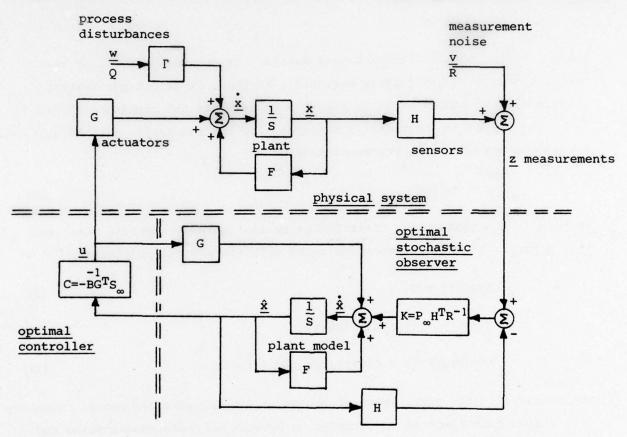


Figure 1. Overall Schematic of Optimal Stochastic Control System

An optimal control can be defined in many ways. The most common when we want to control \underline{x} near zero using reasonable values of control \underline{u} is to use the control which minimizes a linear quadratic cost function,

$$J = \frac{1}{2} \int_{t_0}^{t_f} (\underline{x}^T \underline{A}\underline{x} + \underline{u}^T \underline{B}\underline{u}) dt , \qquad (13)$$

where the A and B matrices are initially established by the designer to reflect the relative weighting of errors in the various states and the use of the various controls. The A and B matrices are usually diagonal with at least some nonzero diagonal elements selected to be,

$$A_{ii} = \frac{1}{x_{0i}^2}$$
 and $B_{jj} = \frac{1}{u_{0j}^2}$, (14)

where u_{oj} is an acceptable amount of control j to be used when the state i deviates x_{oi} from zero. It is usually necessary to modify the weighting matrices A and B and iterate on the design based on the evaluated response of the controlled system. The calculus of variations^{3,8} can be utilized to show that the control which minimizes eq. (13) for a stationary system is given by,

$$C = -B^{-1}G^{T}S_{m} , \qquad (15)$$

where S_{∞} is the steady-state solution of a matrix Riccati equation which is independent of w(Q) and v(R); i.e.,

$$\dot{S} = -SF - F^{T}S + SGB^{-1}G^{T}S - A. \tag{16}$$

An efficient way to obtain the steady-state solution, S_{∞} , is to utilize the technique of eigenvector decomposition first proposed by MacFarlane⁶ and Potter.⁷ This method was developed into a practical design computer program by Bryson and Hall² in Hall's OPTSYS program which uses the QR algorithm to solve the eigensystem. User's Documentation for the Michigan version of this program is included in Appendix C for information.

The second half of the design problem is to develop the optimal stochastic observer. Again, the calculus of variations and be utilized to show that the maximum-likelihood estimate of the state is produced by the filter given by,

$$\frac{\hat{\mathbf{x}}}{\hat{\mathbf{x}}} = \mathbf{F}\hat{\mathbf{x}} + \mathbf{G}\underline{\mathbf{u}} + \mathbf{K}(\underline{\mathbf{z}} - \mathbf{H}\hat{\mathbf{x}}) \; ; \; \hat{\mathbf{x}}(\mathsf{t}_0) = \overline{\mathbf{x}}_0 \; , \tag{17}$$

where the filter feedback gain matrix K for a stationary system is given by,

$$K = P_m H^T R^{-1} , \qquad (18)$$

where P is the steady-state solution of the matrix Riccati equation,

$$\dot{\mathbf{P}} = \mathbf{F}\mathbf{P} + \mathbf{P}\mathbf{F}^{\mathbf{T}} + \mathbf{\Gamma}\mathbf{Q}\mathbf{\Gamma}^{\mathbf{T}} - \mathbf{P}\mathbf{H}^{\mathbf{T}}\mathbf{R}^{-1}\mathbf{H}\mathbf{P} \quad . \tag{19}$$

The matrix P is the covariance of the error of the estimate of the state; i.e.,

$$P(t) = E[(\hat{x}(t) - x(t)) (\hat{x}(t) - x(t))^{T}] . \qquad (20)$$

In eq. (17), it can be seen that the estimate $\hat{\mathbf{x}}$ is assumed to follow the same dynamics as \mathbf{x} (excluding $\Gamma_{\mathbf{w}}$) and that if the measurement which would result from $\hat{\mathbf{x}}$ (excluding $\underline{\mathbf{v}}$) deviates from the actual measurement $\underline{\mathbf{z}}$ a correction is introduced to drive $\hat{\mathbf{x}}$ closer to $\underline{\mathbf{x}}$. In eq. (19), it can be seen that, as expected, large process disturbances (high Q) and large measurement noise (high R) will increase P, the error in the estimate produced by the stochastic observer. An efficient way to obtain the steady-state solution to eq. (19), P_{∞} , is again by eigenvector decomposition as implemented in the OPTSYS program described in Appendix C.

In modeling physical systems, it is not always realistic to assume that the process disturbance or measurement noise is white noise. If the process disturbance is a random quantity which changes very rapidly compared to the time response of the system, it is reasonable to assume the process disturbance is white noise as in Eq. (1). However, if the process disturbance is a random quantity which changes very slowly compared to the time response of the system (perhaps a tidal current effect on a passing ship), it is reasonable to assume the process disturbance to be a random bias or constant. This can be incorporated into the above treatment by defining an additional state variable or variables such that,

$$\dot{\mathbf{x}}_{n+1} = 0 , \qquad (21)$$

and $x_{n+1}(t_0)$ is random. This state variable is included in an augmented state vector of length n+1 and \underline{w} might then be zero.

If the process disturbance is a random quantity which changes on about the same time scale as the response of the system, it must be modeled as something between white noise and a random bias. This is accomplished by the use of various shaping filters and again augmenting the state vector. The simplest shaping filter produces an exponentially correlated disturbance³ by driving

a first-order system by white noise. A new state variable is defined as follows:

$$\tau_{c} \dot{x}_{n+1} + \dot{x}_{n+1} = w$$
 , (22)

where τ_C is the correlation time and w is white noise. The state vector can then be augmented to an n+1 vector and the total system is still disturbed by white noise as in eq. (1). The shaping filter processes the white noise to produce a new disturbance \mathbf{x}_{n+1} which is random but with a characteristic time constant τ_C of about the same order as the response time of the system. Other higher-order shaping filters are possible to model more complex disturbances. 3,5,9

If a physical system, its disturbances, and the noise in its measurements are modeled as described above, a design program such as the OPTSYS program can be used to produce the optimal control gains C and the optimal filter gains K. The OPTSYS program can also produce the Root Mean Square (RMS) response of the system to the design disturbances as represented in the power spectral densities Q and R. The RMS response is, however, not that meaningful to many engineers. Also, specific physical disturbances will often be modeled through the use of shaping filters and the designer may want to know the response of the controlled system to the specific disturbances. Thus, there is often a need to simulate the response of the optimal stochastic control system to specific process disturbances and initial condition errors while subject to the measurement noise. The SHIPSIM/OPTSIM simulation program was developed to allow the simulation of these systems with a minimum of effort and computer programming. This simulation program is a valuable complement to the OPTSYS program for use in control system design.

III. Description of SHIPSIM

In developing a simulation of the optimal stochastic control systems for the path control of surface ships¹, it was decided to develop and document these programs so they could be of general use in the future. Further, it was decided to separate the input/output and numerical integration portions of the program from those portions specifically related to the stochastic control problem. This is the SHIPSIM-OPTSIM dividing point and makes SHIPSIM a general continuous systems simulation program which has a very wide range of applications and usefulness. It has already been used in a number of additional research and teaching applications within the Department of Naval Architecture and Marine Engineering at the University of Michigan.

The authors have research and teaching experience with continuous system simulations written from scratch using existing numerical integration subroutines 10 and with the use of higher-level, problem-oriented continuous systems simulation languages 11 specifically IBM's Continuous Systems Modeling Program (CSMP). 12 Based on this experience, it was felt that a valuable compromise between these two approaches would be a FORTRAN IV batch-type program with flexible input, output, and integration specification and control features to which the user would only have to add a few user-supplied subroutines which define his particular simulation problem in a standard form. This is similar to the modular approach taken in the development of our nonlinear, constrained, parameter optimization program¹³ which has proven very useful in research and teaching applications. The user can work at the FORTRAN level without the need to learn a new, higher-level language but can still have available many of the labor saving features of a higher-level language such as CSMP. We have not conducted a specific test but SHIPSIM should also be significantly cheaper to run than CSMP since the CSMP-to-FORTRAN translation step is not needed.

The only computational function of SHIPSIM is to integrate a set of $n \le 25$ coupled, nonlinear, first-order differential equations from an initial condition,

$$\underline{\dot{Y}}(t) = \underline{f}(\underline{Y}(t), t) , \qquad \underline{Y}(t_0) = \underline{Y}_0 , \qquad (23)$$

and to perform a set of m≤5 nonlinear auxiliary calculations,

at each program output point. The output can be printed output of any selected or all elements of \underline{Y} and all elements of \underline{z} at specified points in t; CALCOMP plots can also be easily obtained for any selected elements of \underline{Y} and \underline{z} as functions of t. The user can select either a fixed step-size Euler (rectangular) integration or a variable step-size, guaranteed-error, fourth-order Kutta-Merson integration method. He simulation can be performed in a series of sequential pre-specified integration segments using a different integration method and different integration and output specifications in each segment. The overall integration can be stopped based on the value of one of the elements of \underline{Y} as well as on the value of the independent variable. Multiple runs can be made by changing the entire SHIPSIM and/or model input data sets for subsequent runs or by changing only specific values in the data sets used in the previous run. This substantial flexibility is achieved with fairly brief and simple SHIPSIM input data.

Euler or rectangular integration gives the value of Y at time t+At as,

$$\underline{Y}(t+\Delta t) = \underline{Y}(t) + \underline{\mathring{Y}}(t) * \Delta t ; \qquad (25)$$

i.e., it evaluates the derivatives once at time t and assumes them constant over the integration step Δt . Euler integration is thus very simple and efficient. For processes with generally small and/or smooth variations in Y it can yield acceptable answers when a suitably small integration step-size, At, is used. When the step-size is too large it is possible for the integration results to completely diverge from the correct results. Euler integration can also successfully handle discrete changes in \dot{Y} when Δt is kept small. If Y experiences large and rapid changes in magnitude, the acceptable value of Δt may be so small that excessive CPU time will be needed to complete the integration. The integration step-size used in a region where Y changes rapidly would be very wasteful if also used in regions where Y changes more slowly. For this reason (and to facilitate variations in output), SHIPSIM allows a specific integration run to be specified with up to five integration segments each with a separate integration method and/or step-size. Euler integration has the disadvantage that the error of the integration results is unknown. It is therefore essential to perform test integration runs with a

reduced step-size to verify that the results are acceptably accurate.

Kutta-Merson integration 14,15 is much more complex than Euler integration but provides a dynamically varying integration step-size which is automatically doubled or halved as necessary to produce guaranteed, user-specified absolute and/or relative error in the results. This step-size will be short where Y changes rapidly and much larger where Y changes more slowly. There is much more computational overhead than with Euler integration but guaranteed error is provided and the integration step-size is never any shorter than necessary. Improved integration cost is thus possible in some cases. A major problem with Kutta-Merson integration is that it may be very difficult to meet the specified error limits (particularly at points where Y is discontinuous in value or slope) without shortening the integration step-size to the point where excessive CPU time is used. To protect against excessive reduction in step-size without user interaction to relax error specifications, SHIPSIM includes capability to limit the number of times the initially specified step-size will be automatically halved (cut). If this number of cuts is exceeded, the integration is terminated and an error message is printed. Kutta-Merson integration is able to predict the integration error by evaluating the derivatives at five points in each integration step as compared to Euler integration which evaluates the derivatives only once for each integration step.

To define a particular problem for SHIPSIM, the user must provide a subroutine DERIV to evaluate the derivatives eq. (23) and a subroutine INPUT to provide the problem dependent input to the program. If the user also wants to output quantities in addition to the n integrated variables; i.e., if m>0, the user must also provide a subroutine ACALC to perform the auxiliary calculations eq. (24). If m=0, a file containing a dummy version of ACALC without executable code is available to be called in order to allow program loading without an error message. Files containing the object code (compiled) versions of these user-supplied subroutines must be concatenated with the SHIPSIM object file on the Michigan Terminal System (MTS) \$RUN command to link the entire program together. The program can be easily run from the terminal using data files. Printed output can be taken on the terminal or line printer as specified. CALCOMP plots can be generated off-line using a SHIPSIM produced plotfile.

The macro structure of SHIPSIM is shown in Figure 2. The three usersupplied subroutines are shown across the bottom. It is important to emphasize how each of these subroutines are called by SHIPSIM since this establishes what the user may and should put in each subroutine. Subroutine INPUT is called once at the beginning of the simulation run. It must input or assign NEQ, the number of equations to be integrated by SHIPSIM (n in equation (23)). It must also obtain any problem dependent input and perform any problem input verification output and initialization needed by the user. The input must be transmitted to the remainder of the user-supplied subroutines by separate subroutine calls (as in OPTSIM which follows) or by labeled COMMON. The COMMON must be labeled since SHIPSIM already utilizes unlabeled COMMON. Subroutine DERIV is called at least once per integration step by whichever integration subroutine has been selected. It may thus be called hundreds or thousands of times in a simulation run. Subroutine ACALC is used to calculate the value of those non-integrated quantities which the user wishes to see in the printed or plotted output. It is thus called only at the specified print and plot points. Often these calculations (perhaps the value of a control) will duplicate those performed in DERIV but they should be repeated again in ACALC since the most recent value established in DERIV will be prior to the actual print or plot point of interest. The example in Appendix A User's Documentation for SHIPSIM illustrates such a case.

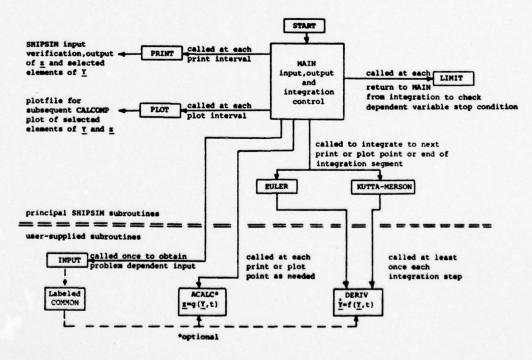


Figure 2. Macro Flow Chart for SHIPSIM

The SHIPSIM program has been written to be independent of the Michigan Terminal System (MTS) as much as possible. The principal exception is the plot option which uses many subroutines from the *PLOTSYS public file on MTS¹⁶ to prepare the CALCOMP plotfile. Most computer installations have comparable software or the program can be used with the plot option removed. Appendix A contains the User's Documentation for SHIPSIM. Appendix D contains the Programmer's Documentation for SHIPSIM. Appendix F contains a source code listing for SHIPSIM. The plot option portions of the code which must be altered or removed to implement the program on another system without the plot capability are identified in Appendix D.

IV. Description of OPTSIM

OPTSIM is a group of subroutines which constitute the INPUT and DERIV subroutines needed by SHIPSIM. OPTSIM running under the control of SHIPSIM allows the simulation of the response of stationary, linear optimal control systems to specific user-specified process disturbances and/or initial condition errors while subject to measurement white noise. The input data set is constructed so that input used for system design using our version of the OPTSYS program (Appendix C) and the gain matrices as output by OPTSYS can be used directly with OPTSIM. The simulations can thus be obtained with a minimum of additional data preparation and programming by the user. The macro structure of OPTSIM running under the control of SHIPSIM is shown in Figure 3.

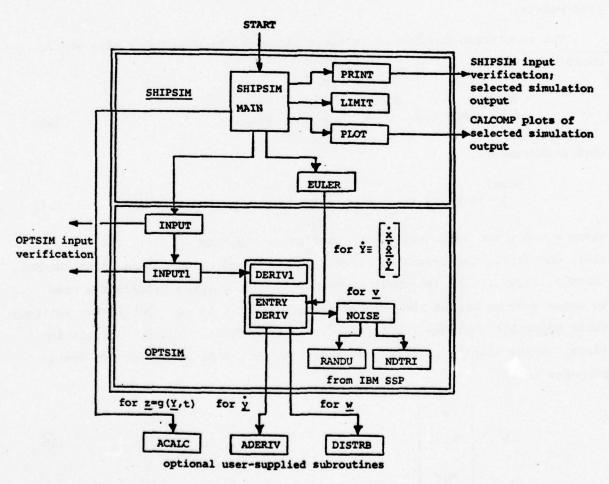


Figure 3. Macro Flow Chart for SHIPSIM/OPTSIM

A control system response to initial condition errors while subject to measurement noise can be simulated without any additional programming by the user. The initial conditions can be input as part of the SHIPSIM input. Measurement white noise \underline{v} with user-specified standard deviation $\underline{\sigma}'$ is calculated within OPTSIM by subroutine NOISE which utilizes two subroutines from the IBM Scientific Subroutine Package¹⁷ for randum number generation (RANDU) and transformation to normally-distributed quantities (NDTRI). If the user wishes to subject the system to a specific process disturbance \underline{w} , he must prepare a subroutine DISTRB which defines the process disturbance as a function of the states and/or time. The user can also include a subroutine ADERIV if quantities \underline{v} in addition to the states \underline{x} and estimates \hat{x} are to be integrated. Finally, the user can also include a subroutine ACALC (defined as part of SHIPSIM) if additional non-integrated quantities are desired at the print or plot points.

The simulation problem of interest includes the physical system which could be given by,

NSxl NCxl NGxl
$$\underline{\dot{x}} = F_S \underline{x} + G_S \underline{u} + \Gamma \underline{w} , \underline{x}(t_O) = \underline{x}_O,$$
 (26)

with measurements,

$$NOBx1 \\ \underline{z} = H_{\underline{S}}\underline{x} + \underline{v} , \qquad (27)$$

where \underline{w} and \underline{v} are white noise with statistics given by eq. (4), (5), (9), (10), and (11). The system matrices F_S , G_S , Γ , and H_S have dimensions (NSxNS), (NSxNC), (NSxNG), and (NOBxNS), respectively. If shaping filters are used to model some or all of the process disturbances, \underline{w} in eq. (26) is not entirely white noise but includes random quantities with finite, nonzero correlation times. Using shaping filters, the state vector can be augmented for design purposes to be,

$$\underline{\mathbf{x}'} \equiv \begin{bmatrix} \underline{\mathbf{x}} \\ \mathbf{x}_{NS+1} \\ \vdots \\ \mathbf{x}_{NE} \end{bmatrix}$$
 (28)

and the design system equation or estimator design equation is given by,

$$\frac{\mathbf{NEx1}}{\underline{\mathbf{x}'}} = \mathbf{F_{e}}\underline{\mathbf{x}'} + \mathbf{G_{e}}\underline{\mathbf{u}} + \mathbf{\Gamma'}\underline{\mathbf{w}'} , \qquad (29)$$

with measurements,

$$\underline{z} = H_{e}\underline{x}' + \underline{v} \quad , \tag{30}$$

where \underline{w}^{\prime} is now white noise with statistics given by eq. (4), (5), and (11). The estimator design matrices F_{e} , G_{e} , and H_{e} now have dimension (NEXNE), (NEXNC), and (NOBXNE), respectively.

The optimal state estimator design produces the Kalman-Bucy filter equation,

$$\frac{\dot{\hat{\mathbf{x}}}}{\dot{\mathbf{x}}} = \mathbf{F}_{e}\hat{\mathbf{x}} + \mathbf{G}_{e}\underline{\mathbf{u}} + \mathbf{K}(\underline{\mathbf{z}} - \mathbf{H}_{e}\hat{\mathbf{x}}) \quad , \tag{31}$$

where the filter gain matrix has dimension (NEXNOB). The optimal controller design produces the control equation,

$$\underline{\mathbf{u}} = \mathbf{C}\hat{\mathbf{x}} \quad , \tag{32}$$

where the control gain matrix has dimension (NCxNE). Substituting eq. (27) and (32) into eq. (26) and (31) yields the system of equations to be simulated; i.e.,

$$\frac{\dot{\mathbf{x}}}{\mathbf{x}} = \mathbf{F}_{\mathbf{S}} \mathbf{x} + \mathbf{G}_{\mathbf{S}} \mathbf{C} \hat{\mathbf{x}} + \mathbf{\Gamma} \mathbf{w} \quad , \tag{33}$$

$$\frac{\dot{\hat{\mathbf{x}}}}{\hat{\mathbf{x}}} = \mathbf{F}_{e} \hat{\mathbf{x}} + \mathbf{G}_{e} \mathbf{C} \hat{\mathbf{x}} + \mathbf{K} \mathbf{H}_{s} \mathbf{x} + \mathbf{K} \mathbf{v} - \mathbf{K} \mathbf{H}_{e} \hat{\mathbf{x}} \quad . \tag{34}$$

Rearranging these gives,

$$\begin{bmatrix} \underline{x} \\ \underline{\dot{x}} \end{bmatrix} = \begin{bmatrix} F_{S} & G_{S}C \\ KH_{S} & F_{e} + G_{e}C - KH_{e} \end{bmatrix} \begin{bmatrix} \underline{x} \\ \underline{\hat{x}} \end{bmatrix} + \begin{bmatrix} \Gamma \underline{w} \\ \underline{K}\underline{v} \end{bmatrix} = A \begin{bmatrix} \underline{x} \\ \underline{\hat{x}} \end{bmatrix} + \underline{b} . \tag{35}$$

If no shaping filters are used, NS=NE and eq. (26) and (29) are identical so $F_S=F_e$, $G_S=G_e$, and $H_S=H_e$.

The simulation problem may also include integration of a number of manditional quantities given by,

$$\frac{NAx1}{\underline{y}} = \underline{h}(\underline{x}(t), \underline{\hat{x}}(t), \underline{y}(t), t) .$$
(36)

SHIPSIM integrates the total system of NEQ=NS+NE+NA equations given by eq. (35) and (36) grouped as follows:

$$\frac{\mathbf{NEQx1}}{\underline{\mathbf{Y}}} \equiv \begin{bmatrix} \frac{\mathbf{x}}{\underline{\mathbf{X}}} \\ \frac{\mathbf{x}}{\underline{\mathbf{Y}}} \end{bmatrix} .$$
(37)

The derivatives eq. (35) are calculated by OPTSIM using the user-supplied disturbance \underline{w} from subroutine DISTRB. The derivatives eq. (36) are calculated in the user-supplied subroutine ADERIV. The combined vector of derivatives eq. (37) is loaded in OPTSIM and returned to the SHIPSIM integration subroutine.

The selection of integration method and step-size and the specification of white noise standard deviation $\underline{\sigma}'$ must be done carefully when simulating stochastic systems. In design, the usual approach in modeling random disturbances or noise which vary rapidly compared to the dominant time constants of the system is to first assume they are exponentially correlated. The correlation time τ_C and standard deviation σ are then obtained or approximated. For an exponentially correlated quantity the power spectral density is given by, 5

$$Q = \frac{2\sigma^2\beta}{\omega^2 + \beta^2} \quad , \tag{38}$$

where $\beta=\tau_c^{-1}$. This power spectral density is approximately constant for $\omega<<\beta$. The power spectral density can therefore be approximated by,

$$Q \cong 2\sigma^2/\beta = 2\sigma^2\tau_G \quad , \tag{39}$$

since τ_C is small compared to the dominant time constants of the system; i.e. $\omega << \beta$. The noise is thus considered white noise with constant power spectral density given by eq. (39).

In simulating stochastic control systems, the continuous gauss-markov process eq. (35) is usually approximated by a discrete gauss-markov sequence

through the use of Euler or rectangular integration. In this approximation, care must be execised to ensure that the system covariances are preserved. The discrete gauss-markov sequence can be given by,

$$\underline{\mathbf{x}}_{i+1} = \Phi_{i}\underline{\mathbf{x}}_{i} + \Gamma_{i} \underline{\mathbf{w}}_{i} , \qquad i = 0,1,...,N$$
 (40)

$$\underline{z}_{i} = H_{i}\underline{x}_{i} + \underline{v}_{i} , \qquad i = 0,1,...,N$$
 (41)

$$E[(\underline{\mathbf{w}}_{i} - \underline{\overline{\mathbf{w}}}_{i}) (\underline{\mathbf{w}}_{j} - \underline{\overline{\mathbf{w}}}_{j})^{T}] = Q_{i} \delta_{ij} , \qquad (42)$$

$$E[v_{i}v_{j}^{T}] = R_{i}\delta_{ij} , \qquad (43)$$

$$E[(\mathbf{w}_{\underline{\mathbf{i}}} - \underline{\overline{\mathbf{w}}}_{\underline{\mathbf{i}}}) \mathbf{v}_{\underline{\mathbf{j}}}^{T}] = E[(\underline{\mathbf{w}}_{\underline{\mathbf{i}}} - \underline{\overline{\mathbf{w}}}_{\underline{\mathbf{i}}}) (\underline{\mathbf{x}}_{\underline{\mathbf{o}}} - \underline{\overline{\mathbf{x}}}_{\underline{\mathbf{o}}})^{T}] = E[\mathbf{v}_{\underline{\mathbf{i}}} (\underline{\mathbf{x}}_{\underline{\mathbf{o}}} - \underline{\overline{\mathbf{x}}}_{\underline{\mathbf{o}}})^{T}] = 0 , \qquad (44)$$

where δ_{ij} is the Kronecker delta function. The control can be omitted in this discussion without loss of generality. If we take P_i as the error covariance of the discrete Kalman filter estimate at point i, the covariance can be propagated to the next measurement point i+1 using a time update to give the error covariance prior to the measurements M_{i+1} and then the measurements can be processed in the measurement update to give P_{i+1} . Governing update equations can be expressed as,

$$M_{i+1} = \Phi_i P_i \Phi_i^T + \Gamma_i Q_i \Gamma_i^T \quad \text{(time update)}$$
 (45)

$$P_{i+1} = M_{i+1} - K_{i+1}H_{i+1}M_{i+1}$$
 (measurement update) (46)

where,

$$K_{i} = P_{i}H_{i}R_{i}^{-1} = M_{i}H_{i}^{T}(H_{i}M_{i}H_{i}^{T}+R_{i})^{-1} . (47)$$

(See Bryson and Ho, Applied Optimal Control, 3 pp. 349-351, 357, 360-361)

The corresponding equations for the continuous gauss-markov process and the error covariance are given by,

$$\underline{\dot{\mathbf{x}}} = \mathbf{F}\underline{\mathbf{x}} + \mathbf{\Gamma}\underline{\mathbf{w}} \quad , \qquad \underline{\mathbf{x}}(\mathbf{t}_0) = \underline{\mathbf{x}}_0 \quad , \tag{48}$$

$$\underline{z} = H\underline{x} + \underline{v} \quad , \tag{49}$$

$$E[(\underline{w}(t) - \underline{\overline{w}}(t)) (\underline{w}(\tau) - \underline{\overline{w}}(\tau))^{T}] = Q\delta(t - \tau) , \qquad (50)$$

$$E[\underline{v}(t)\underline{v}(\tau)^{T}] = R\delta(t-\tau) , \qquad (51)$$

$$\dot{P} = FP + PF^{T} + \Gamma Q \Gamma^{T} - KHP , \qquad (52)$$

where eq. (18) has been used in eq. (19) and eq. (4), (6), (9), and (11) also apply. When Euler integration with integration step-size Δt is utilized, $x(t+\Delta t)$ is approximated using eq. (48) to be,

$$x(t+\Delta t) = x(t) + Fx(t)\Delta t + \Gamma w(t)\Delta t.$$
 (53)

By comparison between eq. (40) and eq. (53) we must then have,

$$\Phi_{i} = [I + F\Delta t] , \qquad (54)$$

$$\Gamma_{i} = \Gamma \Delta t$$
 (55)

Again when using Euler integration, the error covariance $P(t+\Delta t)$ is in effect approximated using eq. (52) to be,

$$P(t+\Delta t) = P(t) + FP(t) \Delta t + P(t) F^{T} \Delta t + \Gamma Q \Gamma^{T} \Delta t - K(t) HP(t) \Delta t.$$
 (56)

This should produce the same error covariance as eq. (45) and (46) for the simulation to be correct.

Using eq. (54) and (55) in eq. (45) yields,

$$M_{i+1} = P_i + FP_i \Delta t + P_i F^T \Delta t + FP_i F^T \Delta t^2 + \Gamma(Q_i \Delta t) \Gamma^T \Delta t, \qquad (57)$$

where the term in Δt^2 can be neglected since the integration step-size Δt is kept small. Using eq. (57) in eq. (46) now yields,

$$P_{i+1} = P_i + FP_i \Delta t + P_i F^T \Delta t + \Gamma(Q_i \Delta t) \Gamma^T \Delta t - \frac{K_{i+1}}{\Delta t} H(P_i + \text{higher order terms in } \Delta t) \Delta t.$$
(58)

In the limit as $\Delta t \rightarrow 0$, $K_{i+1} \rightarrow K_i$ so we have,

$$\frac{K_{i+1}}{\Delta t} = \frac{K_i}{\Delta t} = P_i H^T (R_i \Delta t)^{-1} , \qquad (59)$$

and eq. (56) will equal eq. (58) if we take,

$$Q_{i}\Delta t = Q, \tag{60}$$

$$R_{i}\Delta t = R. (61)$$

The correct measurement noise covariance R_i to use in the simulation therefore depends on the integration step-size Δt . If σ_i' is the standard deviation for noise element i (square root of element i of R_i), a correct simulation must utilize,

$$\sigma_{i}' = \left[\frac{R_{ii}}{\Delta t}\right]^{1/2}, \tag{62}$$

where R_{ii} is the i-th diagonal element of R used in the design of the continuous stochastic control system and Δt is the fixed integration step-size used with Euler integration. Notice that the standard deviation used in eq. (39) to approximate the power spectral density for the measurement noise in the design of the continuous system; i.e.,

$$R_{ii} \stackrel{\Omega}{=} 2\sigma_{i}^{2}\tau_{c} , \qquad (63)$$

is not the same as the standard deviation $\sigma_{\dot{1}}^{\prime}$ which must be used in the simulation using Euler integration.

User's Documentation for OPTSIM is included in Appendix B; Programmer's Documentation for OPTSIM is included in Appendix E; a source code listing of the OPTSIM subroutines is included in Appendix G. An example simulation of the response of an optimal stochastic path controller for a tanker using SHIPSIM/OPTSIM is described in the next section.

V. Tanker Path Control Example

This section will briefly present the simulation of an optimal stochastic path controller for a tanker operating in shallow water as an example of the use of the SHIPSIM/OPTSIM simulation program. For a complete development and extensive results concerning this problem the reader should consult our research report on the optimal stochastic path control of surface ships in shallow water. Considering the small-deviation control of a ship along a path using the coordinate system shown in Figure 4, the equations of motion in the horizontal plane can be written as follows in non-dimensional form:

$$\frac{\mathrm{d}\psi'}{\mathrm{d}t'} = r',\tag{64}$$

$$(I'_{zz}+J'_{zz})\frac{dr'}{dt'} = N_{\beta}, \beta' + N_{r}, r' + N_{\delta}, \dot{\beta}' + N_{\delta}, \delta',$$
 (65)

$$-(m'+m_{Y}')\frac{d\beta'}{dt'} = Y_{\beta'}\beta' + (-m'+Y_{r}')r' + Y_{r}'\dot{r}' + Y_{\delta'}\delta' , \qquad (66)$$

$$\frac{d\eta'}{dt'} = \psi' - \beta' . \tag{67}$$

Numerical values for the coefficients in eq. (65) and (66) for the 150,000 DWT tanker *Tokyo Maru* at 12 knots were given by Fujino¹⁸ for various values of water depth to draft ratio (H/T). Equations (65) and (66) can be solved simultaneously¹ to produce two equivalent equations without the coupling in \dot{r} ' and $\dot{\beta}$ '. Finally the rudder control system can be modeled by a first-order system,

$$\frac{d\delta'}{dt'} = \frac{1}{T_r} \left(\delta_c' - \delta' \right) , \qquad (68)$$

where $\delta_{\rm C}^{\prime}$ is the commanded rudder angle. These equations yield the system equations,

$$\frac{d}{dt}, \begin{bmatrix} \overline{\psi}' \\ r' \\ \beta' \\ n' \\ \delta' \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & f_{22} & f_{23} & 0 & f_{25} \\ 0 & f_{32} & f_{33} & 0 & f_{35} \\ 1 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1/T_r \end{bmatrix} \begin{bmatrix} \overline{\psi}' \\ r' \\ \beta' \\ \eta' \\ \delta' \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1/T_r \end{bmatrix} \delta_c' .$$
(69)

We also have the equation for the movement along the path which when nondimensionalized becomes just,

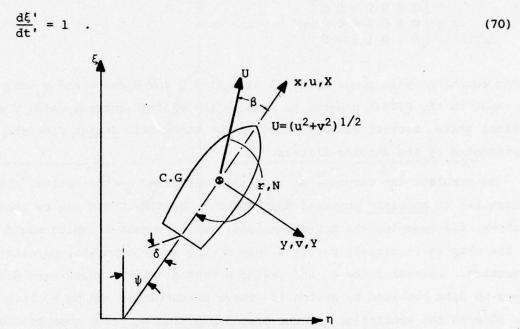


Figure 4. Ship Path Control Coordinate System

The effects of disturbances such as passing ships, bank effects, spatial current changes, etc. can be modeled as exponentially correlated disturbances with the use of first-order shaping filters,

$$T_{Ndt}^{dN'} + N' = w_{N} , \qquad (71)$$

$$T_{Y}\frac{dY'}{dt'} + Y' = w_{Y} , \qquad (72)$$

where N' is a yawing moment and Y' is a lateral force acting on the ship. Augmenting the state vector, the estimator design equation eq. (29) becomes,

and the measurements could be ψ' from a compass, r' from a rate gyro and η' from radar (or DECCA) to give the measurement equation eq. (30),

$$\underline{\mathbf{z}} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \underline{\mathbf{x}}' + \underline{\mathbf{v}} . \tag{74}$$

These equations with power spectral densities Q and R for \underline{w} and \underline{v} were used as input to the OPTSYS program to produce the optimal control gains C and the optimal state observer gains K based on the stochastic <u>design</u> disturbances represented by the shaping filters.

To simulate the response of the ship controlled by the optimal stochastic controller to <u>specific</u> physical disturbances SHIPSIM/OPTSIM can be used. Figure 5 shows, for example, the non-dimensional yawing moment N' which would act on the ship as it closely passes a ship moving in an opposite, parallel direction. Lateral force Y' and yawing moment N' disturbances were developed based on data obtained by Newton. 19 These disturbances can be applied to the ship in the simulation and the system equation eq. (26) then becomes,

$$\frac{d}{dt} \begin{bmatrix} \psi' \\ r' \\ \beta' \\ \eta' \\ \delta' \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & f_{22} & f_{23} & 0 & f_{25} \\ 0 & f_{32} & f_{33} & 0 & f_{35} \\ 1 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1/T_r \end{bmatrix} \begin{bmatrix} \psi' \\ r' \\ \beta' \\ \eta' \\ \delta' \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 0 \\ 0 \\ 0 \\ 1/T_r \end{bmatrix} \delta_C' + \begin{bmatrix} 0 & 0 \\ f_{26} & f_{27} \\ f_{36} & f_{37} \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} N' \\ Y' \end{bmatrix} ,$$
(75)

with the measurement equation eq. (27),

$$\underline{\mathbf{z}} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix} \underline{\mathbf{x}} + \underline{\mathbf{v}} \quad . \tag{76}$$

Eq. (73), (74), (75), and (76) define the system and estimator design matrices F_s , G_s , H_s , F_e , G_e , H_e , and Γ . The OPTSYS output defines the gain matrices Γ 0 and Γ 1. The measurement noise simulation standard deviations Γ 2 were derived from Γ 1 using eq. (62). The simulation equation eq. (35) is thus fully defined. Equation (70) must be treated as an additional derivative to be integrated along with eq. (35).

To set up the SHIPSIM/OPTSIM simulation subroutines DISTRB and ADERIV must be prepared. The disturbances as in Fig. 5 were curve fit with piece-

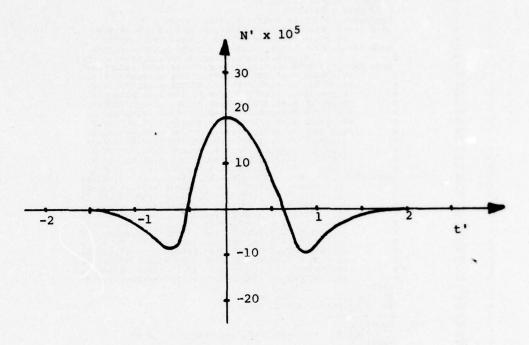


Figure 5. Yawing Moment N' due to Passing Ship

wise cubic splines. The subroutine DISTRB can then take the current value of non-dimensional t=TIME, locate which segment K of each spline is applicable by testing for $t'_{K} \le TIME < t'_{K+1}$, and then evaluate the splines to produce N'(TIME) and Y'(TIME). These disturbances can then be returned in \underline{w} . A listing for the DISTRB subroutine for a passing ship disturbance is shown in Fig. 6. The subroutine ADERIV for NA=1 to implement eq. (70) requires only one line of executable code YDOT(1)=1. A listing will not be included here. There is no need to prepare the optional subroutine ACALC for this simulation.

The SHIPSIM input data set for a simulation of the tanker beginning with zero initial conditions and then sailing past a ship at t'=7. is shown in Fig. 7. This data should be reviewed in conjunction with reference to Appendix A User's Documentation for SHIPSIM. Three integration segments are utilized to obtain more closely spaced printed output over the interval $4.0 \le t' \le 9.0$ where the disturbance occurs. The Euler integration step-size is 0.005 t' units (time to travel one ship length, t'=t/U). Printed output of ψ' , r', β' , η' , δ' , $\hat{\psi}'$, \hat{N}' , \hat{Y}' , and X' are requested. Plots of η' , \hat{N}' ,

```
SUBROUTINE DISTRECT.X.W.NG.NFQ)
IMPLICIT REALES (A-H.O-S)
                                                                DIMENSION W(2),x(25)
DIMENSION TN(13),CN(4,12),TY(13),CY(4,12)
                                                                 DATA TN/-0.2E1,-0.15F1,-0.125E1,-0.10E1,-0.9E0,-0.5E0,
                                                                -0.180,0.280,0.480,0.580,0.680,0.181,0.1581/

-0.180,0.280,0.480,0.580,0.680,0.181,0.1581/

DATA TY/-0.281,-0.1581,-0.1081,-0.7580,-0.5080,-0.2580,

0.080,0.2580,0.5080,0.7080,0.9080,0.12581,0.1581/

DATA CN/0.293708-4,+0.212618-4,-0.73428-5,+0.146858-4,

+0.425228-4,+0.587398-3,+0.373428-4,+0.832888-4,
                                                                                          +0.58739E-3,-0.47209E-3,+0.93288E-4,+0.34951E-3,
-0.11802E-2,-0.54097E-2,+0.81180F-3,+0.95410E-3,
                 12
                                                                                           -0.13524E-2.+0.32983E-3.+0.44139E-3.-0.22777E-3.
                                                                                          +0.32983F-3.+0.50187E-3.-0.22777E-3.-0.58030E-3.+0.66916E-3.+0.17539E-2.-0.72689E-3.-0.65785E-3.
                 14
                 16
                                                                                          +0.26308E-2,-0.76323E-4,-0.85523E-3,+0.30529E-5,
                                                                                          -0.15265E-3,-0.14607E-1,+0.15265E-5,+0.84607E-3,
-0.14607E-1,-0.14179F-2,+0.84607E-3,+0.81418F-3,
                 18
                                                               -0.13647E-3,+0.23664E-3,+0.23757E-3,+0.2138E-4,

-0.3547E-3,+0.23664E-3,+0.27367E-3,+0.12138E-4,

+0.18931E-3,-0.14655E-4,-0.73275E-5,+0.36638E-5/

DATA CY/-0.66367E-4,-0.27267E-4,+0.16592E-4,-0.33183E-4,

-0.27267E-4,-0.30457F-3,-0.33183E-4,-0.12386E-3,

-0.60913E-3,+0.24839E-2,-0.36193E-3,-0.79524E-3,
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                                                                                              +0.24839E-2+0.47536E-2+0.79524E-3+0.29710E-3+0.47536E-2+0.61385E-2+0.29710E-3+0.19837E-2+0.61385E-2+0.19837E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2+0.19625E-2
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                                                                                              -0.6793E-3,-0.13822E-2,+0.19625E-2,+0.16864E-2,
-0.13822E-2,-0.14712E-2,+0.16864E-2,+0.89195E-3,
-0.18390E-2,+0.54353E-2,+0.10736E-2,-0.21741E-3,
                                                                                              +0.54353E-2,+0.97685E-4,-0.21741E-3,-0.20391E-3,+0.55820E-4,+0.14889E-3,-0.12112E-3,-0.75382E-4,
                 32
33
34
                                                                                              +0.20844E-3,-0.74422E-3,-0.93028E-4,+0.46514E-4/
                                                                TP=7.
                                                                 IF (T.LT.TP+TN(1)) GO TO 30
                                                                 IF (T.GT.TP+TN(13)) GO TO 30
                 35
                 36
37
                                                                 K=1
                                                                 CONTINUE
                 38
                                                                IF (T.GE.TP+TN(K).AND.T.LE.TP+TN(K+1)) GO TO 20 K=K+1
                 40
41
42
                                                                 GO TO 10
                                              20
                                                                CONTINUE
                                                                WH=CN(1,K)*(TP+TN(K+1)-T)**3+CN(2,K)*(T-TP-TN(K))**3

+ CN(3,K)*(TP+TN(K+1)-T)+CN(4,K)*(T-TP-TN(K))

GO TO 40
                 43
44
45
                                              30
                                                                 CONTINUE
                 46
                                                                  UN=O.
                                                                 CONTINUE
                                               40
                                                                 IF (T.LT.TP+TY(1)) GO TO 70
IF (T.GT.TP+TY(13)) GO TO 70
                 49
                                                                 K=1
                                                                 CONTINUE
                                                                 IF (T.GE.TP+TY(K).AND.T.LE.TP+TY(K+1)) GO TO 60
                 52
53
54
55
                                                                 K=K+1
                                                                 GO TO 50
                                                                 CONTINUE
                 56
57
58
                                                                WY=CY(1,K)*(TP+TY(K+1)-T)**3+CY(2,K)*(T-TP-TY(K))**3
+ CY(3,K)*(TP+TY(K+1)-T)+CY(4,K)*(T-TP-TY(K))
GO TO 80
                                                             *
                                              70
                                                                 CONTINUE
                  60
                                                                 WY=0.
CONTINUE
                  61
                                                                  W(1)=WN
                 63
                                                                 U(2)=UY
                                                                  RETURN
                                                                  END
SEND OF FILE
```

Figure 6. Subroutine DISTRB for Passing Ship Disturbance

```
T-M, NOISE, PASSING SHIP, H/T=1.89, OPTIMAL, SHAPING FILTER
                                  ETA
YS
0.0
                      BETA
N$
                                             DELTA
                                                         PSI$
           PSIDOT
           DELTAS
ETA$
8.8
NONE
                                                      NS
                                    DELTA
                                             PSIS
PSI
         PSIDOT
                  BETA
                           ETA
                       N$
           DELTA
ETA
            4.0
                     .0050
```

Figure 7. SHIPSIM Input Data Set for Example Simulation

and 6' are requested using a scale factor SF=1.0 to produce 8-1/2"x11" CALCOMP plots. The OPTSIM input data set for the simulation is shown in Fig. 8.

This data should be reviewed in conjunction with reference to Appendix B
User's Documentation for OPTSIM.

1																						
5 1	3	2	1	7																		
	0.0	EØ			1.0	EØ				0.	BE	3		1	3 .	ØE	,			0.	ØE	9
0.0			-0.	1765	7E+	01	3.	57	35	9E	+01	1 :	0.0					. 88				
0.0			0.	1719	9E+	99	-3.	52	76	6E	+32		1.3					15				
	1.0	EØ			0.0	EØ			-	1.	DE			-	. 6	0E					ØE:	
	0.0	EØ			0.0	EØ				0.	BE	,				DE		-1	3 .	43	9E	9
	0.0				1.0	EØ				0.	BEE	3			0 .	ØE	,			0.	ØE	9
	0.0																					
0.0			-0.	1765	7E+	01	0.	57	35	9E	+31	1 6	3.0				-0.	88	37	4E	+01	8
-0.500	43E+	-01															-			1		
0.0			0.	1719	9E+	30	-0.	52	76	6E	+00	3 6	3.0				-0.	15	50	7E	+01	8
-0.282	33E+	102																				
	1.0				0.0	EØ			-	1.	BE	,		-	3 .	ØE	,			0 .	ØE	0
	0.0	BEØ																				
	0.0	BEO			0.0	EØ				0.	BE	3		1	0 .	BE	3	-	0.	43	9E	0
	0.0	EØ																				
	0.0	EØ			0.0	EØ				Ø.	DE	3		1	0 .	ØE	3			ø.	ØE	0
	0.0	EØ																				
	0.8	BE			0.0	E				0.	DE	3		1	Ø.	DE	3			ø.	ØE	0
	-1.6	BEØ																				
	0.0	EØ			0.0	E				0.	ØE	3		1	0 .	ØE	•	1	0.	43	9E	0
	0.6	EØ			0.0	E				0.	DE	9			0.	ØE	3	1	0.	43	9E	0
	0.8	BEO																				
7.746	21E+	-00	4.	623	70E+	00	1.	70	00	9E	+0]	1 :	2.42	52	3E	+06	-4	.71	32	ØE	+0	Ø
-2.257	97E+	-02																				
0.0			0.	0			0.	47	76	8E	+03	3-6	.50	04	3E	+01	0.	21	14	1E	+0	2
0.0			0.	0			0.						0.0									
	1.0	BEO			0.0	EØ				0.	ØE	,		-	0 .	DE	,			0.	ØE	0
	1.0	EØ			0.0	EØ				0.	ØE	3		-	ð .	ØE	,			0.	ØE	0
	0.0	EØ			1.0	EØ				0.	DE	3										
	1.0	EØ			0.0	EØ				0 .	ØE	7		4	ð .	ØE	,			0.	96	a
	0.0	EØ			0.0	E				1.	0E	,				BE					ØE	
	0.0	EO			0.0	E				9.	ØE.	3		-	3 .	ØE:	,		0	. 0	EA	
	0.0				0.0						ØE.				•				-	-	-	
2.188	63E-	-01	1.	005				42					4.83	58	7 E	-02	2 3.	. 29	59	6E	+0	1
7.544	79E-	-02		0809									1.39									
0.0			0.				_						5.94									
-6.313	52E-	-34			34E-	01			86	9E	-0:			-	_							
	541E			2.3							E-1											
				-				- •			-											

Figure 8. OPTSIM Input Data Set for Example Simulation

The printed output from the simulation is shown in Fig. 9. The output consists of the title printed by SHIPSIM, input verification of the OPTSIM input data produced by subroutines INPUT and INPUT1 in OPTSIM, input verification of the SHIPSIM input data, and then the actual simulation results. The plot output from the simulation is shown in Figures 10, 11, and 12. These plots are reduced here in size from the 8-1/2"x11" plots actually produced by the CALCOMP plotter. Figure 10 shows effective control system response to return the ship to the desired path $(\eta'=0)$ following the disturbance

caused by the ship passing at t'=7. The maximum lateral offset is about 19 feet full scale. Figure 11 shows the estimate of the yawing moment disturbance \hat{N} ' produced by the Kalman-Bucy filter. This can be compared with the actual disturbance produced by DISTRB as shown in Figure 5. The validity of using first-order shaping filters to produce design disturbances which model this type actual disturbance is confirmed by a detailed comparison. Figure 12 shows the rudder usage during the simulation. Maximum value is about 4°. The cost of this simulation run was \$3.07 with an additional \$1.86 for the three plots.

Figure 9. SHIPSIM/OPTSIM Printed Output for Example Simulation

ØRUN SGWY:SHIPSIM.OHOFTSIM.OHADERIV.OHDISTRBP.OHACALC.DHNAAS:SSP+#FLOTSYS 4≈DATA41 5=DATA51 9≈-PLOTFILE ØEXECUTION BEGINS

UNIVERSITY OF MICHIGAN DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING SHIPSIM CONTINUOUS SYSTEMS SIMULATION PROGRAM

OPTSIM OPTIMAL STOCHASTIC CONTROLLER SIMULATION PROGRAM

INFUT VERIFICATION NED = 13

ORDER OF SYSTEM = 5

NUMBER OF CONTROLS = 1

NUMBER OF OBSERVATIONS = 3

NUMBER OF PROCESS NUISE SOURCES =

NUMBER OF AUXILIARY STATES = 1

ORDER OF ESTIMATOR - 7

SYSTEM OPEN LOOP DYNAMICS MATRIX....FS(NS.NS)

-0.88074E+00	-0.15607E+00	0.0	-0.43900E+00
0.0	0.0	0.0	0.0
0.57359E+01	-0.52766E+00	-0.10000E+01	0.0
-0.17657E+01	0.17199E+00	0.0	0.0
0.0	0.0	0.10000E+01	0.0
	-0.17657E+01 0.57359E+01 0.0	-0.17657E+01 0.57359E+01 0.0 0.17199E+00 -0.52766E+00 0.0	0.0 -0.17457E+01 0.57359E+01 0.0 -0.88074E+00 0.0 0.0 17199E+00 -0.052746E+00 0.0 -0.15607E+00 0.0 0.0 0.052746E+00 0.0 0.0 0.0

ESTIMATOR OPEN LOOF DYNAMICS MATRIX....FE(NE,NE)

0.0	-0.50043E+01	-0.28233E+02	0.0	0.0	0.0	-0.10000E+01
0.0	0.47768E+03	0.21141E+02	0.0	0.0	-0.10000E+01	0.0
0.0	-0.88074E+00	-0.15607E+00	0.0	-0.43900E+00	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.57359E+01	-0.52766E+00	-0.10000E+01	0.0	0.0	0.0
0.10000E+01	-0.17657E+01	0.17199E+00	0.0	0.0	0.0	0.0
0.	0.1	0.	. 10000E+01	0.	0.0	

BYSTEM CONTROL DISTRIBUTION MATRIX.... GS(NS,NC)

0.0 0.0 0.0 0.43900E+00

SHIPSIM/OPTSIM Printed Output for Example Simulation... Continued Figure 9.

ESTIMATOR CONTROL DISTRIBUTION MATRIX....GE(NE.NC)

0.0 0.0 0.0 0.43900£+00 FEEDBACK CONTROL GAINS ... C(NC,NE)

0.14691E+04 -0.22580E+03 -0.47132E+01 0.24252E+01 SYSTEM DISTURBANCE DISTRIBUTION MATRIX....GAMMA(NS,NG) 0.17001E+02 0.46237E+01 0.77462E+01

0.0 0.47768E+03 -0.50043E+01 . 0.21141E+02 -0.28233E+02 0.0 SYSTEM MEASUREMENT SCALING MATRIX....HS(NOB,NS)

0.10000E+01 0.0 0.0 0.0 0.10000F+01 0.0 0.0 0.0 0.0 KALMAN-FUCY FILTER GAINS....K(NE.NUB)

000

000

000

0.0 0.0 0.10000E+01

0.218846£400 0.10054£401 0.14241E-02 0.48359E-01 0.32940£402 -0.25429E-02 0.75448E-01 0.10809£402 -0.33427£400 0.13917£400 0.051590£401 0.82120£400 0.0 0.0 0.0 -0.49461E-03 0.11229£401 0.40023E-02 -0.43135E-03 -0.59850£400 0.463387E-02

MEASUREMENT NOISE STANDARD DEVIATIONS....SIGMA(NOB)

0.10541E-01 0.23116E-02 0.10413E+00 T-M.NOISE.PASSING SHIP.H/T=1.89,OPTIMAL,SHAPING FILTER

Figure 9. SHIPSIM/OPTSIM Printed Output for Example Simulation... Continued

11 = 0.0 BETA = 0.0 ETA = 0.0 = 0.0 PSIDOT\$ = 0.0 BETA\$ = 0.0 1\$ = 0.0 N\$ = 0.0 Y\$ = 0.0	PSI PSIDOT BETA ETA DELTA Ne Ys X	ETA DELTA NS	ERS:	PRD PLD FIRSTP EPS	0.5000E+00 0.1000E+00 0.5000E-02 0.1000E+00 0.1000E+00 0.5000E-02
# 0.0 PSINT # 0.0 PSI\$ # 0.0 DELTA	# # WARIABLES TO BE PRINTED:	* * * VARIABLES TO BE PLOTTED:	* * * INTEGRATION CONTROL PARAMETERS:	SEGMENT METHOD TF	EULER 0.4000E+01

-	-	21
4440444	91E-0	0.3335E-03 0.8376E-04 0.2010E-03 0.637E-04 8333E-04 0.7526E-05 0.1840E-03 0.4060E-04 0.2388E-03 0.4721E-04 0.6889E-04 0.3387E-04

	# # INTEGRATION SE	SEGMENT 2							
TIME	PSI	PSIDOT	BETA	ETA	DFI TA	PS1\$	\$ 2	*	*
0.4000E+01	-	0.68B9E-04	0.3382E-04	0.8371E-03	0.2869E-03	0.1125E-03	8173E-05	0.6329E-05	0.4000E+01
0.4100E+01	_	0.3550E-04	0.2596E-04	0.8907E-03	0.8919E-03	0.3332E-04	0.1665E-04	6225E-05	0.4100E+01
0.4200E+01	_	4699E-04	0.8479F-05	0.9461F-03	0.1473F-02	0.1495E-03	0.3854E-05	0.3833E-06	0.4200E+01
0.4300E+01	_	1729E-03	1330E-04	0.1003E-02	0.2014E-02	0.2063E-03	0.6913E-05	1010F-05	0.4300E+01
0.4400E+01	_	2957E-03	4655E-04	0.1061E-02	0.9563E-03	0.2283E-03	2733E-04	0.170BE-04	0.4400E+01
0.4500E+01	_	3015E-03	5443E-04	0.1119E-02	1861E-03	0.2229E-03	0.1559E-04	5956E-05	0.4500E+01
0.4600E+01	0.4763E-03	3074E-03	6117E-04	0.1174E-02	0.5830E-03	0.1569E-03	2414E-05	0.4012E-05	0.4600E+01
0.4700E+01	_	3309E-03	7063E-04	0.1226E 02	0.5282E-03	0.3874E-04	1184E-04	0.9358E-05	0.4700E+01
0.4800E+01	_	3357E-03	7637F-04	0.1277E-02	0.369BE-04	4255E-04	1879E-04	0.1319E-04	0.4800E+01
0.4900E+01	_	3643E-03	8561E-04	0.1324E-02	0.176BE-02	0.3879E-04	0.2250E-04	8661E-05	0.4900E+01
0.5000E+01	_	4750E-03	1107E-03	0.1370E-02	0.3443E-03	1323E-04	3671E-04	0.2283E-04	0.5000E+01
0.5100E+01	•	4426E-03	1102E-03	0.1412E-02	0.1171E-03	0.5135E-04	0.6059E-05	3729E-06	0.5100E+01
0.5200E+01	•	4084E-03	1084E-03	0.1450E-02	0.5683E-03	1032E-04	0.1424E-05	0.2341E-05	0.5200E+01

SHIPSIM/OPTSIM Printed Output for Example Simulation... Continued Figure 9.

0.1802E-04	43096E-04 0.5500E+01	0.2769E-05	A - 27195-04 0 59005401	4167F-04	2510E-04	4341E-04	42571E-04 0.6300E+01	1381E-04	0.8294E-06	4 0.2947E-04 0.6500E+01	0.7146E-04	0.1206E-03	3 0.8498E-04 0.7000E+01	0.7196E-04	0.1057E-03	0.6055E-04	0.5454E-04	0.4708E-06	4315E-05	0.5488E-05	5195E-05	5776E-05	A 0.2074E-04 0.8000E+01	0.1157E-04	0.1481E-04	5 0.1160E-04 0.8400E+01	4 0.2480E-05 0.8500E+01	4 0.2960E-04 0.8600E+01	4 0.3176E-05 0.8700E+01	4 0.2317E-04 0.8800E+01	5 0.1493E-04 0.8900E+01	_
-042847E	1457E-03 0.1018E-04	0.1304E-03 0.1005E-05	0.4909F-03 0.5490F-04			0.2721E-02 0.8716E-04	0.3895E-02 0.5419E-04			0.5231F-025083F-04		0.2002E-022278E-03	.5980E-031522E-03						_				1879F-01 0.1556E-04		1639E-016866E-05	1525E-01 0.1564E-05	1413E-01 0.2121E-04	.1293F-012739F-04	.1160F-01 0.2323E-04	.1025E-011315E-04	8847E-02 0.2464E-05	7391E-02 0.1523E-04
	0.1866F-021443F	0.3858E-02 0.130								0.9038F-07 0.523		1827E-01 0.200						'	1	1	•		3616F-01 183		3021E-01163	2602E-01152	2352F-01141	1998E-01179	1792E-01116	1429E-01102	•	8016E-02 739
0.1483F	3 0.15474-02	3 0.1562E-02			_	0.1BOOF-02	0.1965E-02	0.2212E-02	2 0.2550E-02			12 0.4714E-02	_		Ī						0.1427E-02	/4//E-04	2 1060E-02		3 6552E-02	38143F-02	129682E-02	2 -,1115E-01	10 1254F-01	12 1384F-01	1503E-01	1611F-01
	F-03 0.11391-03	E-02 0.2006E-03			_		_		E-02 0.1778E-02			E-013771E-02	'	1	•			'	' - '	1			E-021337F-02	'	E-01 0.2096E-03		F-01 0.1366F-02	E-01 0.1826E-02	_	_	_	E-01 0.3142E-02
0.2080E-032980E-03 0.1909E-033310E-04	0.2591E-03 0.8272E-03	0.3637E-03 0.1321E-02		_		Ĭ			0.55576-02 0.41446-02		Ċ								1			-1887E-01 0.3380E-02		_	1590E-01 0.1021E-01	1483F-01 0.1111E-01		1246E-01 0.1254E-01	•		_	7056E-02 0.1410E-01
0.5400F 101 0.		0.5700E+01 0.		_			_		0.6500E101 0.		_	_	•	•			•			•		0.7900E101			0.8300E+01	0.8400E+01	0.8500E401	•				0.9000E+01

NI * * *	* * * INTEGRATION SF	SFGMENT 3							
1 I'ME	PST	PSTDOT	нета	ETA	DELTA	PS1\$	*2	¥.	×
0.9000F101	706AF-02	0.1410F-01	0.3142E-02	1611F-01	8016F-02	7391F-02	0.1523E-04	0.8622E-05	0.9000F+01
0.9500E+01	-,1955F-03	0.179AF-01	0.3602F-02	1945F-01	0.2239E-02	6604E-03	0.2881E-05	0.1560E-04	0.9500E+01
0.1000E 402	0.5551F-02	0.9598F-02	0.3134F-02	1999F-01	0.1216E-01	0.5141E-02	0.3556E-05	0.1311F-04	0.1000E+02
0.1050E 102	0.9249F-02	0.5099F-02	0.2089E-02	1757E-01	0.1344F-01	0.8904F-02	0.1093E-04	0.6098F-05	0.1050E+02
0.1100E+02	0.1065E 01	0.6978F-03	0.8551F-03	1319E-01	0.1237F-01	0.1044E-01	0.8350E-05	0.4309E-05	0.1100E+02
0.1150E+02	0.1013F-01	2560E-02	2089F-03	8071F-02	0.1095F-01	0.1007E-01	0.2869E-04	-,9718E-05	0.1150E+02
0.1200E+02	0.8227E-02	4669E-02	1005F-02	3110E-02	0.5040E-02	0.7991F-02	0.2189E-04	8207E-05	0.1200E+02
0.127.0F +02	0.56745-02	5425E-02	1426E-02	0.1004E-02	0.2540E-02	0.5363E-02	7800F-05	0.3751E-05	0.1250E+02
0.1300E +02	0.3038F-02	4895F-02	1465F-02	0.3904E-02	1230E-02	0.2429E-02	0.1342F-05	0.1383F-05	0.1300E+02
0.1350E +02	0.7788103	3949E-02	1304E-02	0.5553E-02	3939F-02	0.1488F-03	7810F-05	0.5420E-05	0.1350E+02
0.140GE 102	-,8216E-03	2353E-02	9241F-03	0.4079F-02	5079E-02	1685E-02	0.4856E-05	0.1558E-06	0.1400E+02
0.14-0E+02	1682E-02	1117E-02	5529F-03	0.5799E-02	3770F-02	2577E-02	4531E-04	0.2783E-04	0.1450E+02
0.1500E+02	1976F-02	1261F-03	2215E-03	0.5055F-02	4275E-02	2700F-02	2463E-04	0.1685E-04	0.1500F+02
0.15501102	1737F-02	0.9296F-03	0.1107F-03	0.4136E-02	3436F-02	2767F-02	0.3509E-04	1407E-04	0.15505+02
0.1600E +02	1253F-02	0.958BF-03	0.7160F-07	0.3302F-02	0.3552F-03	1893F-02	-,1281E-05	0.5532E-05	0.1600E+02

Figure 9. SHIPSIM/OPTSIM Printed Output for Example Simulation... Concluded

0.1330E-04 0.1650E+02 0.9221E-05 0.1700F+02 0.1632E-04 0.1750F+02 1839E-04 0.1850E+02 0.2264E-04 0.1850E+02	0.5740E-06 6.1900E+02 8188E-05 0.1950E+02 1749E-04 0.2050E+02 0.4464E-05 0.2050E+02	60000	00000	1005E-04 0.250E+02 4389E-05 0.270E+02 1471E-04 0.280E+02 0.2277E-05 0.2850E+02 0.4379E-05 0.2950E+02 0.6921E-05 0.2950E+02
1551E-04 0.1 1047E-04 0.9 2421E-04 0.1 0.3H77E-041	0.2143E-05 0.5 0.1859E-048 0.3591E-041 5409E-05 0.4			0.2238-04
1485E-02 4510E-03 4750E-03 2239E-03	1209F-03 8246E-04 1494E-03 2735E-03	7153E-03 8063E-03 9215E-03 8656E-03	1002E-02 8059E-03 4988E-03 3305E-03 1825E-03	0.1218E-03 0.2964E-03 0.5261E-03 0.1596E-03 4872E-03 3985E-03
6680F-03 0.3271F-03 0.7478E-03 0.4726E-03 0.4982F-03	0.6774F-03 0.1623E-07 0.2742E-03 0.6775E-03	0.55996-02 0.59996-04 12026-02 0.11986-02	1731E-02 8557E-03 2820E-03 8694E-04 0.1097E-02	9.2604E-02 1078E-02 0.2087E-02 0.1744E-02 1319E-03 1423E-02
0.2672F-02 0.278F-02 0.208F-02 0.2067F-02	0.2321E-02 0.2514E-02 0.2682E-02 0.2769E-02	0.2554E-02 0.2279E-02 0.1944E-02 0.1565E-02	0.1188E-02 0.8234E-03 0.4920E-03 0.2566E-03 0.1385E-03	0.2623E-03 0.4767E-03 0.7077E-03 0.9127E-03 0.9590E-03 0.7575E-03
0.2494E-03 0.2378E-03 0.1820E-03 0.1430E-03	0.2397F-04 3549E-04 9081E-04 1548E-03	1217E-03 6671E-04 3689E-04 1137E-04	0.2264E-04 0.5500E-04 0.1185E-03 0.1338E-03 0.1551E-03	0.9134E-04 0.2184E-04 6130E-04 1267E-03 1934E-03 9015E-04
0.9939E-03 0.7307E-03 0.5071F-03 0.3851F-03	2235E-03 3669E-03 6301E-03	3275E-03 1411E-03 2834E-04 8877E-06	0.2546E-03 0.2546E-03 0.4709E-03 0.4548E-03 0.5318E-03	0.1986E-03 2577E-04 3647E-03 5347E-03 7301E-03 1962E-03 0.6398E-04
.,7652E-03 -,3081E-03 -,1703E-04 0,2072E-03 0,3636F-03	0.4058F -03 0.3439E -03 0.1401E -03 8440F -04	6032E-03 6911E-03 7566E-03	-,7349E-03 -,6584E-03 -,4625E-03 -,2095E-03 0,3360E-04	0.4594E-03 0.4701E-03 0.1964E-03 1308E-03 5908E-03
0.1470E407 0.1750E407 0.1750E402 0.1800E402	0.1950F 102 0.1950E 102 0.7000E 102	0.2150L102 0.2250E402 0.2250E402	0.250E+02 0.2450E+02 0.250E+02 0.2550E+02	0.2650F+02 0.2750E+02 0.2750E+02 0.2850E+02 0.2950E+02 0.2950E+02

PDS: PLOT DESCRIPTION GENERATION BEGINS ***

*** END OF FILE ENCOUNTERED ON 4. **EXECUTION TERMINATED

#RUN #CEGUFUE FAR*-PLOTFILE
#EXECUTION BEGINS
##*-F101FILE
#CONTION TERMINATED
#COPY -PLOTFILE PLOTFILE4
#COUNT *CCCUCUE
#EXECUTION BEGINS
ENTER PLOT REQUEST:
PLOTFILE4
3 PLOTS: PLOTTING REQUIRES 670 SEC. AND 39 IN. # \$1.86 #DISFLAY COST #COST = \$3.07. TERM.NORMAL.UNIV

\$1.86

PLOT ASSIGNED RECEIPT # 510132. ENTER PLOT REQUEST:

EXECUTION TERMINATED

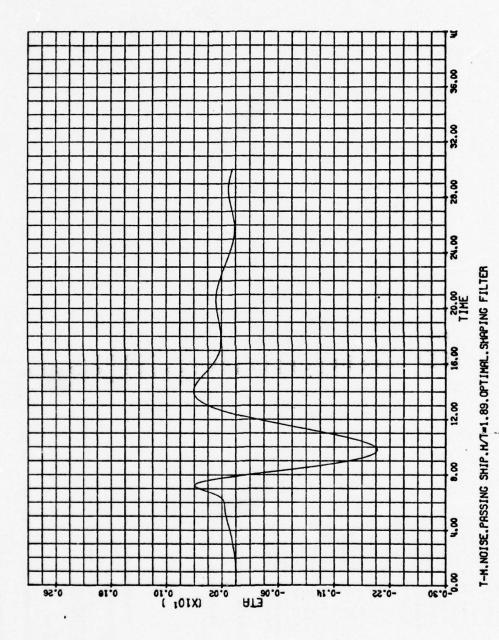


Figure 10. Plot of Lateral Offset n' from Example Simulation

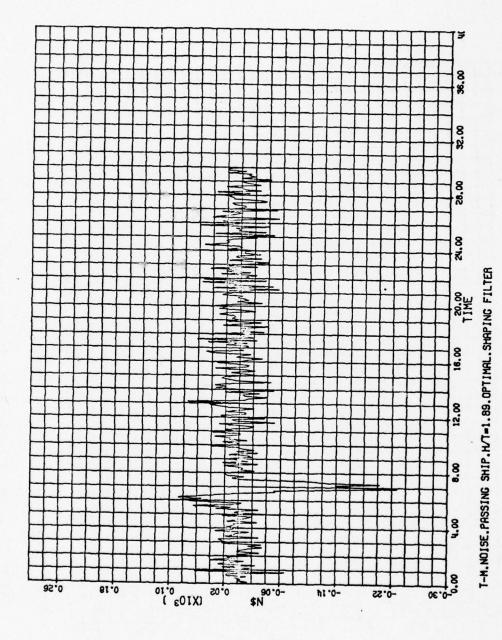
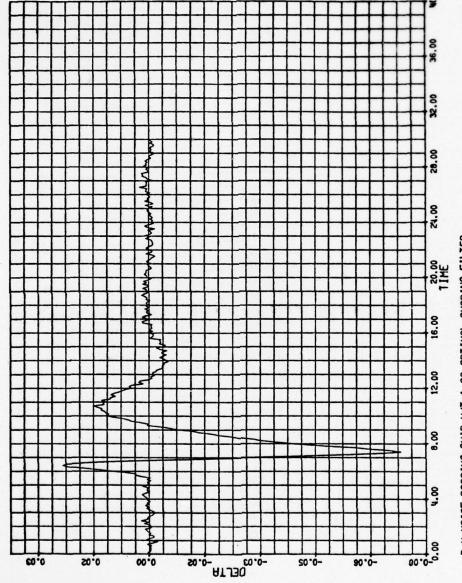


Figure 11. Plot of Yawing Moment Estimate N' from Example Simulation



T-M.NOISE.PRSSING SHIP.H/T=1.89.0PTIMAL.SHAPING FILTER

Figure 12. Plot of Rudder Angle 6' from Example Simulation

VI. Closure

The SHIPSIM/OPTSIM program used in conjunction with the OPTSYS program provides a useful and efficient design tool for the development of optimal stochastic control systems for stationary, linear systems. The SHIPSIM program used alone provides a useful continuous system simulation program with a wide range of applications. The program provides a compromise between writing simulation programs from scratch using existing integration subroutines and using higher-level, problem-oriented simulation languages such as IBM's CSMP. Both these programs can be utilized with a minimum of user programming and data preparation.

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Appendix A: User's Documentation for SHIPSIM

UNIVERSITY OF MICHIGAN

DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING

Rev. 2 5/27/77

IDENTIFICATION: SHIPSIM Program

PROGRAMMER: Ass't. Prof. Michael G. Parsons and J.E. Greenblatt of the University of Michigan, Department of Naval Architecture and

Marine Engineering, under ONR Contract N00014-76-C-0751.

PURPOSE:

This continuous system simulation program integrates a system of up to 25 first-order differential equations. Flexible input, output, and integration control is provided. Up to five auxiliary quantities may be computed and displayed with the integration output. The system definition and auxiliary calculations are handled through user-supplied subroutines. Integration methods available are a fixed step-size Euler or rectangular integration and a fourth-order, variable step-size Kutta-Merson integration with optional absolute and relative error control. Integration method and integration and output control parameters can be changed at up to four user-specified points within the integration. The integration can be terminated based on the value of the independent variable or based on the value of one of the integrated dependent variables.

METHOD:

References: 1. Fox, L., <u>Numerical Solution of Ordinary and Partial</u>
Differential Equations, 1962, p. 24.

- MTS Volume 11: Plot Description System, University of Michigan Computing Center, 1971.
- IBM System/360 and System/370 FORTRAN IV Language, IBM Manual Number GC28-6515-10, May, 1974.

The only computational function of SHIPSIM is to integrate a set of $MEQ(\leq 25)$ coupled, first-order differential equations,

NEQxl

$$\underline{\dot{Y}}(t) = \underline{f}(\underline{Y}, t)$$
 , $\underline{Y}(t_0) = \underline{Y}_0$,

from an initial condition through time and to perform a set of NAC(\leq 5) auxiliary calculations,

NACx1

$$z(t) = q(Y,t)$$
,

at each program output point. The integration can be performed using a rectangular or Euler integration or using a Kutta-Merson integration technique.

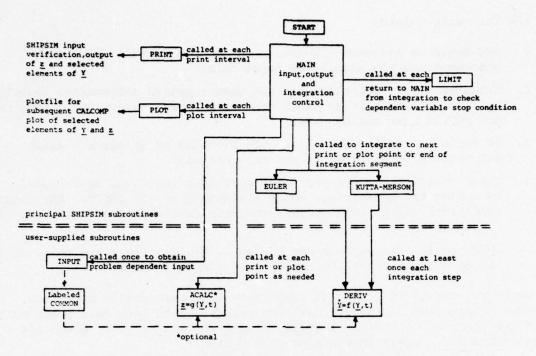
Euler integration gives the value of Y at time t+∆t as,

$$\underline{Y}(t+\Delta t) = \underline{Y}(t) + \underline{\dot{Y}}(t) * \Delta t$$
;

i.e., it evaluates the derivatives once at time t and assumes them contant over the integration step Δt . Euler integration is thus very simple and efficient. For processes with generally small and/or smooth variations in Y it can yield acceptable answers when a suitably small integration step-size, $\overline{\Delta}$ t, is used. When the step-size is too large it is possible for the integration results to completely diverge from the correct results. Euler integration can also successfully handle discrete changes in Y when Δt is kept small. If Y experiences large and rapid changes in magnitude, the acceptable value of Δt may be so small that excessive CPU time will be needed to complete the integration. The integration step-size used in a region where \dot{Y} changes rapidly would be very wasteful if also used in regions where Y changes more slowly. For this meason (and to facilitate variations in output), SHIPSIM allows a specific integration run to be specified with up to five integration segments each with a separate integration method and/or step-size. Euler integration has the disadvantage that the error of the integration results is unknown. It is therefore essential to perform test integration runs with a reduced step-size to verify that the results are acceptably accurate.

Kutta-Merson integration $^{
m l}$ is much more complex than Euler integration but provides a dynamically varying integration step-size which is automatically doubled or halved as necessary to produce guaranteed, user-specified absolute and/or relative error in the results. This step-size will be short where $\underline{\dot{Y}}$ changes rapidly and much larger where $\underline{\dot{Y}}$ changes more slowly. There is much more computational overhead than with Euler integration but guaranteed error is provided and the integration step-size is never any shorter than necessary. Improved integration cost is thus possible in some cases. A major problem with Kutta-Merson integration is that it may be very difficult to meet the specified error limits (particularly at points where Y is discontinuous in value or slope) without shortening the integration step-size to the point where excessive CPU time is used. To protect against excessive reduction in stepsize without user interaction to relax error specifications, SHIPSIM includes capability to limit the number of times the initially specified step-size will be automatically halved (cut). If this number of cuts is exceeded, the integration is terminated and an error message is printed. Kutta-Merson integration is able to predict the integration error by evaluating the derivatives at five points in each integration step as compared to Euler integration which evaluates the derivatives only once for each integration step.

PROGRAM DESCRIPTION: The basic organization of SHIPSIM is shown in the following macro flow chart which includes only the principal SHIPSIM subroutines:



The MAIN program regulates the integration and controls output processing. User-supplied, double-precision subroutines, INPUT, DERIV, and ACALC define the system and any auxiliary calculations of interest. Subrouting PRINT writes the requested simulation results. Subroutine PLOT prepares a plotfile which can be used for subsequent generation of CALCOMP plots of selected simulation results. Subroutine LIMIT checks integration progress and terminates the run if an element of \underline{Y} reaches a user-prescribed value. Subroutines EULER and KUTTA-MERSON conduct the requested integration.

<u>USER-SUPPLIED SUBROUTINES:</u> The following user-supplied, double-precision, subroutines should be compiled and then loaded into an object file(s) which can be referenced on the MTS RUN command.

Subroutine INPUT is called once at the beginning of a simulation run to read any needed problem dependent input on logical I/O device 5 and to transmit this data to the other user-supplied subroutines. It must also return the number of equations to be integrated (NEQ) to the main program. Input should appear as follows:

```
SUBROUTINE INPUT(NEQ,*)
COMMON/MODEL/...[data transfer to DERIV and/or ACALC]
READ(5,1ØØ,ERR=2ØØ)NEQ

1ØØ FORMAT(12)
:
code to read any problem dependent input
:
RETURN

2ØØ WRITE(6,21Ø)

21Ø FORMAT('-ERROR IN READING NEQ')
RETURN 1
END
```

Note the following points:

- NEQ could be assigned a value, thus avoiding a READ and FORMAT statement and the associated input data.
- Transfer of variables between the user-supplied subroutines must be by labeled COMMON. The label name is optional except that COM1, COM2, and OUTPUT must not be used.
- 3. An error in reading NEQ causes the printing of an error message and program termination in the main program.
- 4. Input verification for the model dependent input may be included by coding the appropriate WRITE statements within INPUT. Any output produced by INPUT will appear after the program title in the SHIPSIM output stream.
- 5. INPUT could also perform any needed initialization since it is only called once at the beginning of each simulation run.

Subroutine DERIV is called at least once each integration step from whichever integration subroutine has been selected. At each call DERIV must return the first NEQ elements of $d\underline{Y}/dT$ through the vector YDOT, given the values of T and Y. DERIV should appear as follows:

SUBROUTINE DERIV(T,Y,YDOT)

REAL*8 T,Y(25), YDOT(25)

COMMON/MODEL/...[data from INPUT]

:

code to define first NEQ elements of YDOT

:

RETURN
END

Subroutine ACALC is an optional subroutine which is called as needed at each print or plot point to calculate up to five non-integrated auxiliary variables,

NACx1 $\underline{z} = \underline{z}(\underline{Y}, \underline{T})$.

This subroutine is called only if a number of auxiliary calculations are specified by the input variable NAC> \emptyset . All NAC elements of \underline{z} will automatically appear in the SHIPSIM printed output. If NAC=0, the user can call a dummy subroutine as part of the MTS RUN command as described below and there is no need to write ACALC. When NAC>0, ACALC should appear as follows:

SUBROUTINE ACALC(T,Y,Z,NAC)

REAL*8 T,Y(25), z(5)

COMMON/MODEL/...[Parameters from INPUT]

:
code to calculate first NAC elements of z

:

RETURN

END

OUTPUT Options: Three output options are available. Printed output is written on logical I/O channel 6. Format may be selected by the input variable IOUT. If IOUT=1, up to nine quantities plus the time are printed in tabular form across 120 columns, for each integration output point. These nine quantities are the NAC elements of z preceded by up to any (9-NAC) elements of Y. The elements of Y must be specified by the input vector CPRINT. If IOUT=2, output is given in a vector format. All NEQ elements of Y and the NAC elements of z are printed.

SHIPSIM will also generate a plot file for MTS graphic post-processing if the input variable PLN (number of plots) is greater than zero. Use is made of the MTS plotting subroutine library contained in *PLOTSYS.² Variables for which plots are desired must be specified by the input variable CPLOT. The plot time increment PLD should be selected to give no more than 300 data points per plot.

<u>USER'S INSTRUCTIONS</u>: As described above, the MAIN program reads various simulation specification and control input in addition to the input which is brought in by the user-supplied subroutine INPUT. All MAIN program input is read on logical I/O device 4. Initial runs must be specified by a complete set of fixed-format input data as specified below. Subsequent runs may be specified either by inputting a completely new set of fixed-format data or by changing only specific values in the data for the previous run by using free-format NAMELIST data sets.

The data sets for multiple simulation runs would be $\underline{\text{read}}$ in the following sequence:

- a complete set of user's problem dependent data for subroutine INPUT on I/O channel 5.
- 2. a complete set of SHIPSIM data on I/O channel 4.
- 3. SHIPSIM input NEXT on I/O channel 4.
- if NEXT=1, SHIPSIM NAMELIST data; existing model dependent data will be reused
 - if NEXT=2, SHIPSIM NAMELIST data followed by new model dependent INPUT data
 - if NEXT=3, SHIPSIM fixed-format input data; existing model dependent data will be reused
 - if NEXT=4, new model dependent INPUT data followed by SHIPSIM fixedformat data
 - if NEXT=5, new model dependent INPUT data only
- 5. a new value of NEXT for third run, etc.

Fixed-format SHIPSIM data consists of the following in the specified sequence including only those required:

Record Type	Variables	Format	Comments
1	NIS	15	Number of integration segments Ø <nis≤5< td=""></nis≤5<>
	NAC	15	Number of auxiliary quantities Ø≤NAC≤5
	IOUT	15	=1 for tabular output =2 for vectorial output
	PLN SF*	15 Dlø.4	Number of plots desired $\emptyset \le PLN \le 9$ Scale factor for plots. With SF=1.0,
			plots are 8-1/2" x 11". Ø <sf≤1.ø omit if PLN=Ø</sf≤1.ø
2	TITLE	9A8	Any 72 character user's title for printout and plot labeling
3	YLABLE	8(A8,2X) repeated as required	Labels for NEQ elements of Y
4	ΥØ	7D1Ø.4 repeated as required	Initial values for \underline{Y} .
5	YTEST	A 8	Name of Y variable to be tested for limiting value. The first time the limiting value is reached from either direction the run stops. If no limiting value is desired enter "NONE"
	YTERM*	DlØ.4	Limiting value of YTEST. May be omitted if NONE is entered for YTEST
6*	ZLABLE	(A8,2X)	Labels for NAC elements of \underline{z} . This record should be omitted if NAC= \emptyset .
7*	CPRINT	9 (88)	Names of Y variables for which printed tabular output is desired. This record should be omitted if IOUT=2
8*	CPLOT	7 (A8,2X)	Names of \underline{Y} and \underline{Z} variables for which plots are desired. The number of names must equal PLN. This record should be omitted if PLN= \emptyset .

Record Type	Variables	Format	Comment
9 repeated NIS times	METHOD	15	Integration method: =1 for Euler
defining each inte-	TF	D1Ø.2	=2 for Kutta-Merson Termination time for the integration segment.
gration segment in succes-	FIRSTP PRD	D1Ø.2 D5.2	Initial integration step size Time increment at which printed output is desired
sion. Each input vari- able is a	PLD EPS*	D5.2 D1Ø.6	Time increment between plotted points Relative error limit for Kutta-Mer-son integration. Omit if METHOD=1
vector NIS long.	AB*	D1Ø.6	Absolute error limit for Kutta-Mer- son integration. Omit if METHOD=1
	NCUTS*	15	Number of times the integration step size may be halved during Kutta-Merson integration. A value of 20 is suggested. Omit if METHOD=1.
10*	NEXT	Τl	input switch for next run. Omit if no further runs are desired. NEXT=1, SHIPSIM NAMELIST data on I/O channel 4; existing model dependent data will be reused NEXT=2, SHIPSIM NAMELIST data on I/O channel 4; new model dependent data for user's INPUT subroutine on I/O channel 5. NEXT=3, SHIPSIM fixed-format input on I/O channel 4; existing model dependent data will be reused. NEXT=4, new model dependent data for user's INPUT subroutine on I/O channel 5; SHIPSIM fixed-
			format data on I/O channel 4 NEXT=5, new model dependent data for user's INPUT subroutine on I/O channel 5; existing SHIPSIM data will be reused. INPUT data only.

^{*} These records or variables may be omitted under the specified conditions.

For runs where the NAMELIST input option is specified, (NEXT=1 or 2) the data should consist of one (or more) lines of the form,

column 2 &DATA TF(2)=2Ø., PRD(2)=1.Ø, METHOD(2)=2, &END

If all changes can be made on one line MTS permits the omission of the &DATA and &END delimiters. The user should review the use of NAMELIST in the <u>IBM</u>

FORTRAN IV language manual. Note that any variable input as an alpha-numeric string must be enclosed in apostrophes, as:

... CPLOT(1) = 'VELOCITY', ...

Both the Euler and Kutta-Merson integration subroutines are called several times within each specified integration segment. Each call specifies an integration interval equal to the smaller of the printing interval PRD and the plotting interval PLD. If the smaller of PRD and PLD is not an integer multiple of FIRSTP the output may be shifted slightly from that expected when Euler integration is used. Further, if the final time for this segment (TF) is not an integer multiple of the smaller of PRD and PLD, it also will be shifted slightly by the program. The larger of PLD and PRD must be an integer multiple of the small of these two quantities. For best results, the smaller of PLD and PRD should be an integer multiple of FIRSTP when Euler integration is specified. With either integration method, TF and the larger of PLD and PRD should be an integer multiple of the smaller of PLD and PRD. The following specification would thus be consistent: FIRSTP=0.01, PRD=1.0, PLD=5.0, TF=100.0.

MTS RUN INFORMATION: Object code for SHIPSIM is currently in file SGTA:SHIPSIM.O (subject to change, see Prof. Michael Parsons). If no auxiliary calculations are required object code for a dummy ACALC subroutine is available in file SGTA:ACALC.D. A run using this dummy subroutine would be initiated with the command:

\$RUN SGTA:SHIPSIM.O+SGTA:ACALC.D+*PLOTSYS+(user's INPUT and DERIV object file) 4=(user's SHIPSIM data file) 5=(user's INPUT data file) 9=(user's plotfile)

If no plots are required (PLN=Ø), device 9 may be assigned to *DUMMY*. If plots are required each one will require approximately three pages of file space and cost approximately \$.65. If a CALCOMP plot is desired the following commands could follow.

- \$ PERMIT (User's plotfile) READ OTHERS
- \$ RUN *CCQUEUE PAR=(User's plotfile)

For a description of *CCQUEUE see MTS volume 11.2 The plotfile can be examined on an interactive graphics terminal by issuing the following command:

SRUN *PLOTSEE

and then responding with the user's plotfile name.

If a large amount of printed output is anticipated, the SHIPSIM printed output channel 6 may be assigned to the high-speed line printer *PRINT* or to a user file for later copying to *PRINT*.

EXAMPLE PROBLEM: The following problem illustrates the use of SHIPSIM to simulate the straight line crash stop of a gas turbine powered escort vessel with a controllable pitch propeller. Suppose we wish to investigate the effect of a throttle application ramp on engine and shaft torque and stopping distance.

Our simplified ship model has the following characteristics:

M = 4000 L.T. = 8,960,000 lbm.

 M_O (added mass) = 8%

 J_e (engine inertia) = 108,864 lbf-ft-sec²

 $J_p + J_o$ (propeller inertia plus added inertia) = 50,000 lbf-ft-sec²

V_O = steady-state ahead speed

= 25 knots = 42.225 ft/sec

Npo = steady-state shaft speed

 $= 4.16667 \text{ sec}^{-1}$

w' = wake fraction = .06

t' = thrust deduction = .10

 η_r = relative rotative efficiency = 1.0

D = propeller diameter = 13.37 ft.

DAR = developed area ratio = .70

P = pitch/diameter, $-1.0 \le P \le 1.4$

P = pitch/diameter change rate = 0.1 sec⁻¹

Machinery characteristics are:

drive train frictional torque = -3% of Qe

TH = throttle, $.18 \le TH \le 1.0$

Engine torque characteristics are given by

$$\frac{Qe}{Qeo}$$
 = (-.2928 TH² + .16260 TH - .01332) $\left(2 - \frac{Ne}{Neo}\right)$ - 0.20

The normalized equations of motion are:

$$\dot{\tilde{x}} = (v_0/x_0) \tilde{v} ,$$

$$\dot{\tilde{\mathbf{v}}} = \frac{\mathbf{T}_{pog_C}}{(\mathbf{M} + \mathbf{M}_O) \, \mathbf{v}_O} \quad [\tilde{\mathbf{T}}_p - \tilde{\mathbf{v}}^2] \quad ,$$

$$\dot{\tilde{N}} = \frac{Q_{\text{eo}}}{2\pi \left(\text{Je+Jp+J}_{\text{O}}\right) N_{\text{O}}} \quad \left[\tilde{Q}\text{e+}\tilde{Q}\text{p-}\tilde{Q}\text{F}\right] \; ,$$

where,

x_o = normalizing value of head reach = 1000 ft.

Qeo = normalizing value of engine torque = 625,580.6 ft. lbf.

 N_O = normalizing value of shaft revolution rate = 4.1667 sec⁻¹

 \tilde{x} = normalized ship position

 $\tilde{\mathbf{v}}$ = normalized ship velocity

 \tilde{N} = normalized shaft speed

 \tilde{T}_{p} = normalized propeller thrust

 \tilde{Q}_e = normalized engine torque

 \tilde{Q}_{p} = normalized propeller torque

 \tilde{Q}_f = normalized frictional torque

The user-supplied subroutines INPUT, DERIV, and ACALC are shown below. These subroutines were compiled and loaded into file PS8.0. Subroutine CRPROP is an external subroutine which returns propeller thrust, torque, and efficiency given speed of advance, rotation rate, wake characteristics and propeller geometry. Subroutine CRPROP will not be listed here.

```
SUBROUTINE INPUT(NEQ,*)
IMPLICIT REAL*8 (A-H,O-S)
COMMON/MODEL/PZ,S
READ(5,180,ERR=150) PZ, S

186 FORMAT(2015.9)
WRITE(6,110) PZ, S

118 FORMAT('-INPUT VERIFICATION: STEADY STATE PITCH=',
F6.3, 'D(THROTTLE)/DT=', F6.4)
NEQ=3
RETURN

156 WRITE(6,160)
FORMAT('ERROR IN READING PZ OR S')
RETURN1
END

C

SUBROUTINE DERIV(T,Y,YDOT)
IMPLICIT REAL*8 (A-H,O-S)
COMMON/MODEL/PZ,S
DIMENSION Y(25),YDOT(25)

C

C CALCULATE PITCH FOR CRPROP

IF (T.LT. 5.) P=PZ
IF (5. .LE. T.AMD. T.LT. 26.5) P=PZ-0,1*(T-5.)
IF (26.5 .LE. T) P=-1.8
```

```
OBTAIN NORMALIZED PROP THRUST AND TORQUE
          CALL CRPROP(Y(2),Y(3),P,.7D40,0,0,0,TPN,QPN,EFFO,
A,B,C,D,E,F,1.99D40,1.337D41,0.9D40,0.94D40,
6.25361D45,1.804040D45,4.2225D41,4.165556667D40)
           CALCULATE ENGINE THRUST (TEN) AND THROTTLE (TH)
           IF (T .LT. 5.) TH=1.0
           IF (T.LT. 5.) TH=1.6

IF (5. LE. T. AND. T.LT. 16.5) TH=.18

IF (16.5 .LE. T) TH=0.18+S*(T-16.5)

IF (TH .GT. 1.0) TH=1.0

QEN=(-.2928*TH**2+1.626*TH-0.1332)*(2.0-Y(3))-0.2
C
           YDOT(1)=0.042225*Y(2)
YDOT(2)=0.0141849*(TPN-Y(2)**2)
           YDOT (3) =0.150267054* (QPN+3.97*QEN)
           RETURN
           SUBROUTINE ACALC(T,Y,Z,NAC)
IMPLICIT REAL*8 (A-H,O-$)
COMMON/MODEL/PZ,S
           DIMENSION Z(5),Y(25)
           CALCULATE PITCH FOR CRPROP
           IF (T .LT. 5.) P=PZ
IF (5. .LE. T .AND. T .LT. 26.5) P=PZ-0.1*(T-5.)
IF (26.5 .LE. T) P=-1.0
           OBTAIN NORMALIZED PROP THRUST AND TORQUE
           CALL CRPROP(Y(2),Y(3),P,.7D00,0,0,0,TPN,QPN,EFFO,
A,B,C,D,E,F,1,99D00,1,337D01,0,9070,0,94D00,
6.25361D05,1.80000D05,4.2225D01,4.165566667D00)
           CALCULATE ENGINE THRUST (TEN) AND THROTTLE (TH)
           IF (T .LT. 5.) TH=1.0

IF (5. LE. T .AND. T .LT. 16.5) TH=.18

IF (16.5 .LE. T) TH=7.18+S*(T-16.5)

IF (TH .GT. 1.0) TH=1.0

QEN=(-.2928*TH**2+1.626*FH-0.1332)*(2.0-Y(3))-0.2
           2(1) = P
2(2) = TH
           Z (3) =QEN
           Z (4) =QPN
           RETURN
            END
```

The data for SHIPSIM, shown below, calls for plotting of shaft speed and throttle in the first run. For the second run (NEXT=2) SHIPSIM NAMELIST input alters the title, eliminates plot generation, and changes IOUT to 2 to produce the vectorial form output. This data was loaded into file D4.

```
2 4 1 2 1.0

CRASH STOP SIMULATION: IDLE TO FULL THROTTLE IN 20 SECONDS

ADVANCE VELOCITY SHAFT N
0.0 1.0 1.0

VELOCITY -0.001

PITCH/D THROTTLE ENGINE Q PROP Q

ADVANCE VELOCITYSHAFT N

SHAFT N THROTTLE
1 30. 0.1 1.0 1.0
1 60. 1.0 1.0 1.0
2

6DATA TITLE='CRASH STOP SIMULATION: IDLE TO FULL THROTTLE IN 10 SEC.',
PLN=0, IOUT=2, 4END
```

Data for subroutine INPUT consists of two lines, one for each run. The first value (PZ) is the steady-state ahead pitch. The second (S) is the slope of the throttle return ramp. This data was loaded into file D5.

1.14778 6.841D88 1.14778 6.882D88

The program output follows.

#RUN SHIPSIM.O+P88.O+CRPROP.O+#PLOTSYS 4=N4 5=D5 9=PLOTFT/F

DEXECUTION BEGINS

UNIVERSITY OF MICHIGAN DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING SHIPSIM CONTINUOUS SYSTEMS SIMULATION PROGRAM

INPUT VERIFICATION: STEADY STATE PITCH= 1.148 B(THROTTLE)/DT= 0.0410

CRASH STOP SIMULATION: IBLE TO FULL THROTTLE IN 20 SECONDS

* * * VARIABLES AND INITIAL VALUES:

ADVANCE = 0.0 VELOCITY = 0.100E+01 SHAFT N = 0.100F+01

* * * AUXILIARY VARIABLES:

PITCH/D THROTTLE FNGINE O PROP O

* * * VARIABLES TO BE PRINTED: ADVANCE UFLOCITY SHAFT N

* * * VARIABLES TO BE PLOTTED: SHAFT N THROTTLE

* * * LIMITING VALUE OF VELOCITY IS -. 1000E-02

* * * INTEGRATION CONTROL PARAMETERS:

SEGMENT METHOD TF PRO PLO PLO PROTESTP FFS AR NOUTS

1 FULFR 0.3000F+02 0.1000F+01 0.1000F+01 0.1000F+00 2 EULFR 0.6000E+02 0.1000F+01 0.1000F+01 0.1000F+01

* * * INTEGRATION SEGMENT 1

TIME ADVANCE VELOCITY SHAFT N PITCH/O THRUITIF FNOTNE O PROP D 0.1000F+01 0.1000F+01 0.1000F+01 0.1148F+01 0.1000F+01 0.9999F+00 -.9699E+00

```
0.1 %/1 100
                          0.1000F +01
0.1000F +01
                                                    0.1148 +01
0. 10000 101
                                       0.10001 101
                                                                  0.10001 101
                                                                               0.99991 100
                                                                                             - . YAYYI 100
0.4000t +01
                                       0.10001 101
                                                                  0.10001 +01
                                                                               0.4444+ +00
                                                                                             -. YAYYF +00
0.5000F+01
             0.2111F+60
                          0.1000F+01
                                       0.1000F+01
                                                     0.114RF+01
                                                                  0.10001+01
                                                                               0.99995+00
                                                                                             -. 9499F+00
                                                                               -.3521F-01
-.2729E-01
             0.2533E+00
                                        0.9014F+00
                                                                  0.1800F+00
                                                                                             -. 4491F+00
0.6000F+01
                          0.99ATF100
                                                     0.1048F+01
0.7000E+01
             0.2952E+00
                          0.9863F+00
                                       0.848AF+00
                                                     0.9478E+60
                                                                  0.1800F+00
                                                                                             -. 1966E+00
                                                                               -.2382E-01
0.8000E+01
             0.3366E+00
                          0.9734E+00
                                       0.8254E+00
                                                     0.8478F+00
                                                                  0.1800F+00
                                                                                             -.6132E-01
                                                                               -.2281E-01
                                                                                             0.1830F-01
0.9000F+01
             0.3774E+00
                          0.9587E+00
                                       0.8187F+00
                                                     0.7478F+00
                                                                  0.1800F+00
                                                                  0.1800F+00
             0.4176F+00
                                                     0.6478F+00
                                                                               -.2324E-01
0.1000E+02
                          0.9427E+00
                                       0.8216E+00
                                                                                             0.6486E-01
                                                                               -.2445F-01
0.1100E+02
             0.45718+00
                          0.925AE+00
                                        0.829AF+00
                                                     0.5478F+00
                                                                  0.1800F+00
                                                                                             0.8727F-01
                                                                               -.2592F-01
             0.4958E+00
                          0.9073E+00
                                       0.83946+00
                                                                  0.1800F+00
0.1200F+02
                                                     0.4478F+00
                                                                                             0.8865E-01
                                                                               -.2719F-01
-.2779F-01
                                                                  0.1800F+00
0.1300E+02
             0.5338E+00
                          0.8878F+00
                                       0.8479E+00
                                                     0.3478F+00
                                                                                             0.6960E-01
0.1400E+02
             0.5709E+00
                          0.8670F+00
                                        0.8519F+00
                                                     0.2478F+00
                                                                  0.1800F+00
0.1500F+02
                                                                               -.2729F-01
-.2528F-01
                                                                                             -.2993F-01
-.1076F+00
             0.6071E+00
                          0.8447F+00
                                       0.8485F+00
                                                     0.1478F+00
                                                                  0.1800F+00
             0.6423E+00
0.1600E+02
                          0.8209F+00
                                       0.8351F+00
                                                     0.4778F-01
                                                                  0.1800F+00
0.1700E+02
             0.6765E+00
                          0.7958E+00
                                        0.8106F+00
                                                     -.5222E-01
                                                                  0.2005E+00
                                                                               0.1533F-01
                                                                                             -.1980E+00
                                                    -.1522F+00
-.2522F+00
0.1800F+02
            0.7096E+00
                          0.7694E+00
                                       0.7817F+00
                                                                  0.2415F+00
0.2825F+00
                                                                               0.9533F-01
                                                                                             -.2968E+00
                          0.7423F+00
                                       0.7495F+00
             0.7416F+00
0.1900E+02
                                                                               0.178AF+00
0.2000E+02
             0.7724E+00
                          0.7148E+00
                                       0.7145F+00
                                                     -.3522E+00
                                                                  0.3235E+00
                                                                               0.265AF+00
                                                                                             -.4978F+00
                          0.6872E+00
0.6599E+00
                                                    -.4522F+00
-.5522F+00
0.2100E+02
             0.8021E+00
                                       0.6780F+00
                                                                  0.3645F+00
                                                                               0.3560F+00
                                                                                             -.5905E+00
                                       0.6414F+00
0.2200E+02
             0.8306F+00
                                                                  0.4055F+00
                                                                               0.4494F+00
                                                                                             -. 6750F+00
0.2300E+02
             0.8579E+00
                          0.6332E+00
                                                     -.4522E+00
                                                                               0.5448F+00
                                       0.4064F+00
                                                                  0.4465F+00
                                                                                             -.7516E+00
                          0.6072F+00
0.5822E+00
                                                     -.7522E+00
-.8522E+00
                                                                                             -.8220E+00
0.2400E+02
             0.8841E+00
                                        0.5744E+00
                                                                  0.4875E+00
                                                                               0.6410E+00
0.2500F+02
             0.9093F+00
                                       0.5461F+00
                                                                  0.5285E+00
                                                                               0.7369F+00
             0.9334E+00
                          0.5582F+00
                                        0.5218F+00
                                                     -.9522E+00
                                                                  0.5A95E+00
                                                                               0.8315F+00
0.2600E+02
                                                                                             -.9530E+00
                                       0.503RE+00
0.5039E+00
                                                                               0.9276F+00
0.9996E+00
0.2700E+02
             0.9566E+00
                          0.5354E+00
                                                     -.1000F+01
                                                                  0.6105F+00
                                                                                             -. 9480E+00
             0.9788E+00
0.2800E+02
                          0.5140E+00
                                                     -.1000F+01
                                                                  0.6515E+00
                                                                                             -.9129E+00
                                                     -.1000F+01
0.2900E+02
             0.1000E+01
                          0.4937E+00
                                       0.5175E+00
                                                                  0.6925E+00
                                                                               0.1064F+01
                                                                                             -.9071E+00
0.3000E+02
             0.1021E+01
                          0.4740E+00
                                        0.5391E+00
                                                     -.1000F+01
                                                                  0.7335E+00
                                                                               0.1118E+01
                                                                                             -.9213E+00
```

* * * INTEGRATION SEGMENT 2

TIME	ATIVANCE	VELOCITY	SHAFT N	PITCH/D	THROTTI F	FNGINF Q	PROP 0
0.3000E+02	0.1021E+01	0.4740F+00	0.5391E+00	1000F+01	0.7335E+00	0.1118F+01	9213E+00
0.3100E+02	0.1041E+01	0.4547E+00	0.5A3AF+00	1000F+01	0.7745F+00	0.11A5E+01	9465E+00
0.3200E+02	0.1060E+01	0.4357E+00	0.5912E+00	1000F+01	0.8155F+00	0.1206E+01	9858E+00
0.3300E+02	0.1078E+01	0.4168E+00	0.6188F+00	1000F+01	0.8565E+00	0.1243E+01	1033E+01
0.3400E+02	0.1096E+01	0.3980E+00	0.5448F+00	1000F+01	0.8975E+00	0.1278E+01	1084F+01
0.3500E+02	0.1113E+01	0.3789E+00	0.5681E+00	1000F+01	0.9385F+00	0.1312F+01	1135E+01
0.3600E+02	0.1129E+01	0.3597E+00	0.6888F+00	1000E+01	0.9795F+00	0.1345F+01	1184E+01
0.3700E+02	0.1144E+01	0.3403F+00	0.7070E+00	1000F+01	0.1000E+01	0.1352E+01	1231E+01
0.3800E+02	0.1158E+01	0.3206E+00	0.7191F+00	1000E+01	0.1000F+01	0.1337E+01	1262E+01
0.3900E+02	0.1172E+01	0.3009F+00	0.7242F+00	1000F+01	0.1000F+01	0.1331F+01	1274E+01
0.4000E+02	0.1184E+01	0.2813E+00	0.7268E+00	1000F+01	0.1000F+01	0.1328F+01	1279E+01
0.4100E+02	0.1196F+01	0.2619F+00	0.7281F+00	1000F+01	0.1000F+01	0.1326F+01	1282E+01
0.4200E+02	0.1207F+01	0.2427F+00	0.7288F+00	1000E+01	0.1000E+01	0.1325F+01	1284E+01
0.4300E+02	0.1218F+01	0.2237E+00	0.7291F+00	1000E+01	0.1000F+01	0.1325F+01	1286F+01
0.4400E+02	0.1227E+01	0.2048F+00	0.7290F+00	1000F+01	0.1000F+01	0.1325F+01	1288F+01
0.4500E+02	0.1236E+01	0.1861E+00	0.7284E+00.	1000F+01	0.1000E+01	0.1324F+01	1290E+01
0.4600E+02	0.1243F+01	0.1675F+00	0.7279F+00	1000E+01	0.100GF+01	0.1326F+01	1292E+01
0.4700E+02	0.1251E+01	0.1489F+00	0.7271F+00	1000F+01	0.1000F+01	0.1328F+01	1295E+01
0.4800E+02	0.1257E+01	0.1305F+00	0.7260E+00	1000F+01	0.1000F+01	0.1329E+01	1297F+01
0.4900E+02	0.1262E+01	0.1120E+00	0.7248E+00	1000F+01	0.1000F+01	0.1330F+01	1299F+01
0.5000E+02	0.1267E+01	0.9363E-01	0.7235E+00	1000E+01	0.1000F+01	0.1332E+01	1301F+01
0.5100E+02	0.1271E+01	0.7526E-01	0.7221F+00	1000F+01	0.1000E+01	0.1333F+01	1303E+01
0.5200E+02	0.1274E+01	0.5690E-01	0.7207E+00	1000F+01	0.1000E+01	0.1335F+01	1305E+01
0.5300E+02	0.1277E+01	0.3853F-01	0.7192E+00	1000E+01	0.1000F+01	0.1337F+01	1306E+01
0.5400E+02	0.1278E+01	0.2015E-01	0.7178E+00	1000E+01	0.1000E+01	0.1339F+01	1308E+01
0.5500E+02	0.1279E+01	0.1761E-02	0.7164E+00	1000F+01	0.1000E+01	0.1340E+01	1309F+01
0.5600E+02	0.1279E+01	1665E-01	0.7151E+00	1000E+01	0.1000E+01	0.1342E+01	1310E+01

^{***} VALUE OF VELOCITY HAS REACHED THE LIMITING VALUE OF -0.100000F-02

PDS: PLOT DESCRIPTION GENERATION REGINS ***

INPUT VERIFICATION: STEADY STATE PITCH= 1.148 D(THROTTLE)/DT= 0.0820

CRASH STOP SIMULATION: IDLE TO FULL THROTTLE IN 10 SEC.

* * * VARIABLES AND INITIAL VALUES:

ADVANCE = 0.0 VELOCITY = 0.100E+01 SHAFT N = 0.100E+01

* * * AUXILIARY VARIABLES:

PITCH/D THROTTLE ENGINE Q PROP Q

* * * VARIABLES TO BE PRINTED: ADVANCE VELOCITY SHAFT N

* * * LIMITING VALUE OF VELOCITY IS -. 1000E-02

* * * INTEGRATION CONTROL PARAMETERS:

SEGMENT METHOD TF PRD PLD FIRSTP EPS AB NEUTS

1 EULER 0.3000E+02 0.1000E+01 0.1000E+01 0.1000E+02 EULER 0.6000E+02 0.1000E+01 0.1000E+01 0.1000E+01

* * * INTEGRATION SEGMENT 1

THE OUTPUT VECTOR IS:		ELOCITY SHA	FT N PITCH	/D THROTTL	E
T= 0.0	0.0 0.1000E+01	0.1000E+01 9697E+00	0.1000E+01	0-1148E+01	0.1000E+01
T= 0.1000E+01	0.4222E-01 0.1000E+01	0.1000E+01 9698E+00	0.1000E+01	0.1148F+01	0.1000E+01
T= 0.2000E+01	0.8445E-01 0.9999E+00	0.1000E+01 9699E+00	0.1000E+01	0.1148E+01	0.1000E+01
T= 0.3000E+01	0.1267E+00 0.9999E+00	0.1000E+01 9699E+00	0.1000E+01	0.1148E+01	0.1000E+01
T= 0.4000E+01	0.1689E+00 0.9999E+00	0.1000E+01 9699E+00	0.1000E+01	0.1148E+01	0.1000E+01
T= 0.5000E+01	0.2111E+00 0.9999E+00	0.1000E+01 9699E+00	0.1000E+01	0.1148E+01	0.1000E+01
T= 0.6000E+01	0.2533E+00 3521E-01	0.9962E+00 4491E+00	0.9014E+00	0.1048E+01	0.1800E+00
T= 0.7000E+01	0.2952F+00 2729E-01	0.9863E+00 1966E+00	0.3486E+00	0.9478E+00	0.1800E+00
T= 0.8000E+01	0.3366E+00 2382E-01	0.9734E+00 6132E-01	0.8254E+00	0.8478E+00	0.1800E+00
T= 0.9000E+01	0.3774E+00 2281E-01	0.9587E+00 0.1830E-01	0.8187E+00	0.7478E+00	0.1800E+00
T= 0.1000E+02	0.4176E+00 2324E-01	0.9427E+00 0.6486E-01	0.8216E+00	0.6478E+00	0.1800E+00
T= 0.1100E+02	0.4571E+00 2445E-01	0.9256E+00 0.8727E-01	0.8296E+00	0.5478E+00	0.1800E+00
T= 0.1200E+02	0.4958E+00 2592E-01	0.9073E+00 0.8865E-01	0.8394E+00	0.4478E+00	0.1800E+00
T= 0.1300E+02	0.5338E+00 2719E-01	0.8878E+00 0.6960E-01	0.8479E+00	0.3478E+00	0.1800E+00

					*	
T= 0.1400	E+02	0.5709E+00 2779E-01	0.8670E+00 0.2992E-01	0.8519E+00	0.2478E+00	0.1800E+00
T= 0.1500	E+02	0.6071E+00 2729E-01	0.8447E+00 2993E-01	0.8485E+00	0.1478E+00	0.1800E+00
T= 0.1600	E+02	0.6423E+00 2528E-01	0.8209E+00 1076E+00	0.8351E+00	0.4778E-01	0.1800E+00
T= 0.1700	E+02	0.6765E+00 0.5175E-01	0.7958E+00 1984E+00	0.8116E+00	5222E-01	0.2210E+00
T= 0.1800	E+02	0.7096E+00 0.2016E+00	0.7694E+00 3020E+00	0.7924E+00	1522E+00	0.3030E+00
T= 0.1900	E+02	0.7416E+00 0.3490E+00	0.7420E+00 4172E+00	0.7784E+00	2522E+00	0.3850E+00
T= 0.2000	E+02	0.7724E+00 0.4929E+00	0.7138E+00 5419E+00	0.7678E+00	3522E+00	0.4670E+00
T= 0.2100	E+02	0.8020E+00 0.6333E+00	0.6848E+00 6735E+00	0.7586E+00	4522E+00	0.5490E+00
T= 0.2200	E+02	0.8303E+00 0.7706E+00	0.6555F+00 8090E+00	0.7496E+00	5522E+00	0.6310E+00
T= 0.2300	E+02	0.8574E+00 0.9054E+00	0.6259E+00 9453E+00	0.7400E+00	6522E+00	0.7130E+00
T= 0.2400	E+02	0.8833E+00 0.1038E+01	0.5966E+00 1080E+01	0.7295F+00	7522E+00	0.7950E+00
T= 0.2500	E+02	0.9079E+00 0.1169E+01	0.5677E+00 1212E+01	0.7181E+00	8522E+00	0.8770E+00
T= 0.2600	E+02	0.9314E+00 0.1297E+01	0.5396E+00 1339E+01	0.7061E+00	9522E+00	0.9590E+00
T= 0.2700	E+02	0.9536E+00 0.1366E+01	0.5127E+00 1364E+01	0.6953E+00	1000E+01	0.1000E+01
T= 0.2800	DE+02	0.9748E+00 0.1369E+01	0.4872E+00 1321E+01	0.6929E+00	1000E+01	0.1000F+01
T= 0.2900	E+02	0.9949E+00 0.1366E+01	0.4631E+00 1298E+01	0.6954E+00	1000E+01	0.1000E+01
T= 0.3000	E+02	0.1014E+01 0.1360E+01	0.4399E+00 1285E+01	0.7000E+00	1000E+01	0.1000E+01

* * * INTEGRATION SEGMENT 2

THE OUTPUT VECTOR IS:	LOCITY SHA	FT N PITCH	/D THROTTL	E
T= 0.3000E+02	0.4399F+00 1285E+01	0.7000E+00	1000E+01	0.1000E+01
T= 0.3100E+02	0.4172E+00 1278E+01	0.7051E+00	1000E+01	0.1000E+01
T= 0.3200E+02	 0.3952F+00 1276E+01	0.7103F+00	1000E+01	0.1000E+01

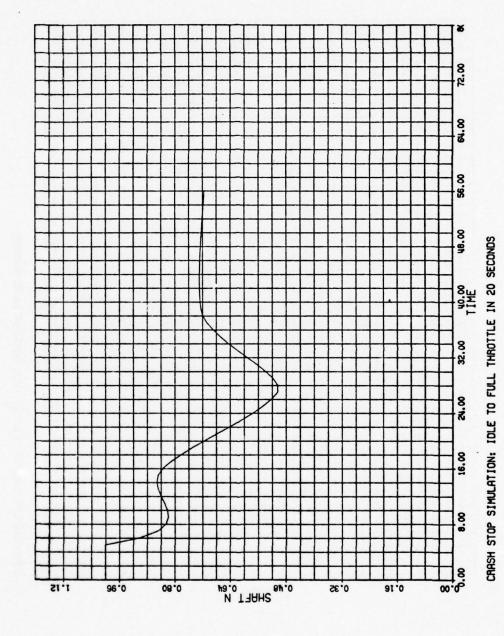
*** END OF FILE ENCOUNTERED ON 4. *EXECUTION TERMINATED

#RUN *CCQUEUE

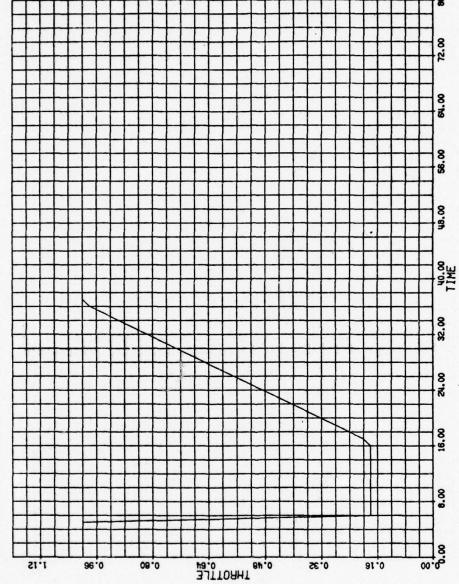
#EXECUTION BEGINS
ENTER PLOT REQUEST:
PLOT
2 PLOTS; PLOTTING REQUIRES 450 SEC. AND 27 IN.; \$1.25
OK?
OK
PLOT ASSIGNED RECEIPT # 510133.
ENTER PLOT REQUEST:

EOF

SEXECUTION TERMINATED DISPLAY COST SCOST = \$4.40, TERM, NORMAL, UNIV #SIG #SGWY 09:54:35-10:13:32 FRI JUN 10/77 STERM, NORMAL, UNIV #ELAPSED TIME #CPU TIME USED #CPU STOR VMI #WAIT STOR VMI 18.933 MIN. 6.636 SEC. 5.25 PAGE-MIN. \$.4R \$2.18 10.201 PAGE-HR. DRUM READS
PLOT TIME
PLOT PAPER 406 7.5 PPLOT TIME 7.5 MIN.
PPLOT PAPER 2.25 FEET
PAPPROX. COST OF THIS RUN IS \$4.43
PDISK STORAGE 66 PAGE-HR. \$1.04 \$.01



A-17



CRASH STOP SIMULATION: IDLE TO FULL THROTTLE IN 20 SECONDS

APPENDIX B: User's Documentation for OPTSIM

UNIVERSITY OF MICHIGAN

DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING

Rev. 1 5/27/77

IDENTIFICATION: OPTSIM: A group of subroutines

PROGRAMMER: Ass't Professor Michael G. Parsons and H.T. Cuong, Dept. of Naval Architecture and Marine Engineering, Univ. of Michigan,

under ONR Contract N00014-76-C-0751.

PURPOSE: These subroutines are designed to be used in parallel with the OPTSYS program to simulate the response of stationary, linear

optimal control and filter systems (developed using OPTSYS) to randomly generated measurement noise, initial condition errors, and specific process disturbances. These subroutines operate under the SHIPSIM continuous systems simulation program. The user inputs the system, estimator, control gain, and filter gain matrices and the standard deviations of the measurement noise. Initial condition errors can be input through SHIPSIM. A subroutine DISTRB is provided by the user to generate the specific process disturbance of interest. A second subroutine ADERIV can also be provided by the user if additional variables must

be integrated to generate the desired output.

METHOD:

References: 1. University of Michigan, Department of Naval Architecture and Marine Engineering, OPTSYS Program, Rev. 2, 5/27/77

- 2. University of Michigan, Department of Naval Architecture and Marine Engineering, SHIPSIM Program, Rev. 2, 5/27/77
- "IBM System/360 and System/370 FORTRAN IV Language," IBM Manual GC28-6515-10.

This set of double precision subroutines provides a general way to simulate the response of a stationary, linear optimal controller and Kalman-Bucy filter system to randomly generated measurement noise, initial condition errors, and specific process disturbances. These systems are designed for stochastic process noise models such as white noise or the output of various shaping filters. The OPTSYS program¹ can be used to design the controller and filter and evaluate the RMS response of the controlled system when subjected to the design measurement noise and process disturbances. It is often desirable to also simulate such a system to establish the response of the controlled system to specific, realistic initial condition errors and process disturbances.

For the stationary, linear system disturbed by Gauss-Markov noise,

$$\dot{\mathbf{x}} = \mathbf{F}\mathbf{x} + \mathbf{G}\mathbf{u} + \mathbf{\Gamma}\mathbf{w} \tag{1}$$

$$\underline{z} = H\underline{x} + \underline{v} \quad , \tag{2}$$

where \underline{x} may be augmented to include the process noise generated by shaping filters as additional states, the OPTSYS program provides the optimal control,

$$\underline{\mathbf{u}} = \mathbf{C}\underline{\hat{\mathbf{x}}} \quad , \tag{3}$$

which uses the estimate of the state produced by the Kalman-Bucy filter given by,

$$\frac{\dot{\hat{\mathbf{x}}}}{\hat{\mathbf{x}}} = \mathbf{F}\hat{\mathbf{x}} + \mathbf{G}\mathbf{u} + \mathbf{K}(\mathbf{z} - \mathbf{H}\hat{\mathbf{x}}) \quad . \tag{4}$$

OPTSYS can also be used to establish the RMS response of this controlled system when subjected to the design white noise sources \underline{w} and \underline{v} . It may also be desirable to establish the controlled system response to initial condition errors $\underline{x}(t_0)$ or $(\underline{x}(t_0)-\hat{\underline{x}}(t_0))$ and specific process disturbances \underline{w} while experiencing the measurement white noise \underline{v} .

The OPTSIM subroutines are designed to perform this simulation under the control of the SHIPSIM continuous systems simulation program². OPTSIM constitutes the INPUT and DERIV subroutines required by SHIPSIM so these do not need to be provided by the user. To the extent possible the input formats are the same as those used by OPTSYS so the same data sets can be utilized. For the most general case where shaping filters are used to model the process disturbances, the estimator estimates both the states and the disturbances (augmented states). In this situation, the filter is of higher order than the system and the formulation can be as follows:

$$\frac{\dot{x}}{\ddot{x}} = F_{S} x + G_{S} C \hat{x} + \Gamma w , \qquad (5)$$

$$\frac{\mathbf{\hat{x}}}{\mathbf{\hat{x}}} = KH_{S}\mathbf{x} + (F_{e} + G_{e}C - KH_{e})\hat{\mathbf{x}} + K\mathbf{v} , \qquad (6)$$

where:

x = system state vector without augmented states (NSx1)

 \hat{x} = estimator state vector with augmented states (NEx1)

w = process disturbance vector (NGx1)

 \underline{v} = measurement noise vector (NOBx1) with standard deviations $\sigma(\text{NOBx1})$

Fs = system open-loop dynamics matrix (NSxNS)

Fe = estimator open-loop dynamics matrix (NEXNE)

Gs = system control distribution matrix (NSxNC)

Go = estimator control distribution matrix (NEXNC)

 Γ = system disturbance distribution matrix (NSxNG)

H_S = system measurement scaling matrix (NOBxNS)

Ho = estimator measurement scaling matrix (NOBxNE)

C = feedback control gains (NCxNE)

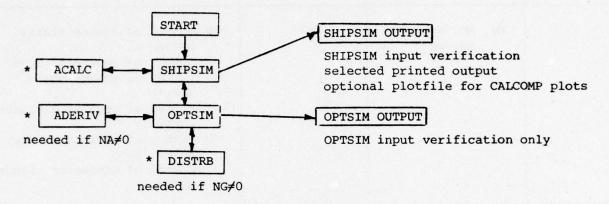
K = Kalman-Bucy filter gains (NEXNOB)

If no shaping filters are used NS=NE and Fs=Fe,Gs=Ge and Hs=He.

If it is desired to integrate variables in addition to \underline{x} and $\hat{\underline{x}}$, these derivatives can be included by adding an optional subroutine ADERIV which calculates,

$$\dot{\underline{\mathbf{y}}} = \underline{\mathbf{f}}(\mathsf{t}, \underline{\mathbf{x}}, \hat{\underline{\mathbf{x}}}, \underline{\mathbf{y}}) \tag{7}$$

where \underline{y} is the vector of additional variables (NAx1). If it is desired to perform calculations at any print or plot point to produce output in addition to $t, \underline{x}, \hat{\underline{x}}$, and \underline{y} , this can be accomplished by adding an optional, user provided subroutine ACALC as defined by SHIPSIM. If NG \neq 0, the user must provide a subroutine DISTRB which will provide the process disturbance \underline{w} as a function time. The general structure of the entire program, OPTSIM running under control of SHIPSIM, is as follows:



*optional user supplied subroutines; with dummy subroutines available

The input is structured so that multiple runs can be made using a completely new data set, by changing only SHIPSIM integration control parameters, or by changing only specific terms within any of the matrices in equations (5) or (6).

USER'S INSTRUCTIONS: The input data sets consist of simulation specification and control input required by SHIPSIM² (which will not be detailed here) on I/O device 4 and the OPTSIM input described below in I/O device 5. Multiple runs can be made by following these with additional data for SHIPSIM and OPTSIM. Data sets for two runs are read in the following order:

- .OPTSIM data for first run
- ·SHIPSIM data for first run
- input control variable NEXT for SHIPSIM
- new OPTSIM data or changes to first run OPTSIM data for second run
- new SHIPSIM data or changes to first run SHIPSIM data for second run

The OPTSIM data for an initial run or a completely new run (SWITCH=1) should consist of the following in the specified sequence including only those required:

Record Type	Input	Format	Comments		
1.	SWITCH (must equal l for an initial run)	13	SWITCH=1 if a completely new set of data will be given SWITCH=2 if only specific changes will be given using NAMELIST		
2.	NS, NC, NOB, NG, NA, NE	613	NS=number of system states, NS≤10 NC=number of controls, NC≤8 NOB=number of measurements, NOB≤10 NG=number of process disturbances, NG≤10 NA=number of additional variables, NA≤5 NE=number of estimator states, NE≤10		
3.	FS	6El2.5 repeated as required	F _S matrix input by rows begin- ning with a <u>new</u> record for each row		
4.*	FE (only if NE≠NS)	6E12.5 repeated as required	F _e matrix input by rows begin- ning with a <u>new</u> record for each row		
5.	GS	6E12.5 repeated as required	G _s input by rows <u>without</u> a new record for each row		
6.*	GE (only if NE≠NS)	6E12.5 repeated as required	Ge input by rows without a new record for each row		
7.	С	6E12.5 repeated as required	C input by rows without a new record for each row		
8.*	GAMMA (only if NG≠0)	6E12.5 repeated as required	Γ input by rows without a new record for each row		

Record Type	Input	Format	Comments	
9.	HS	6E12.5 repeated as required	H _S input by rows <u>without</u> a new record for each row	
10.*	HE (only if NE≠NS)	6E12.5 repeated as required	H _e input by rows <u>without</u> a new record for each row	
11.	K	6E12.5 repeated as required	K input by rows without a new record for each row	
12.	SIGMA	6E12.5 repeated as required	σ'; input a zero vector if no measurement noise is desired See discussion beginning at the bottom page B-6 concerning the specification of σ'.	

*included only if required by input on Card 2.

The form of OPTSIM data for subsequent runs is controlled by the variable SWITCH. If SHIPSIM data is changed but the existing (previous run) OPTSIM data is to be used again, SHIPSIM variable NEXT should equal 1 or 3 and no OPTSIM data is needed. If SWITCH is set equal to 1 on record type 1, a completely new data set must be supplied as described above. If SWITCH is set equal to 2 on record type 1, any specific elements of F_S , F_e , G_S , G_e , C, Γ , H_S , H_e , K, and σ can be changed in the existing OPTSIM data using the format-free NAMELIST input. This input would consist of a record type 1 followed by a record or records as follows:

column 123456789 &LIST1 F(1,3)=0.0,C=1.0,5*0.0,...&END

In this example, element F(1,3) is zeroed and the control gains matrix C(2x3) is changed to 1.0 in the first element with the remaining elements zero. The input can be continued to additional records provided each continued record ends with a comma and each continuing record begins with a new variable name. If all data alterations can be made on a <u>single</u> record, the £LISTl and the £END can be omitted and the first variable name can begin in column 1. A user should review the use of NAMELIST input in the IBM FORTRAN IV language manual. 3

Subroutine ADERIV. IF NA=0, the user can call a dummy subroutine as part of the MTS RUN command as described below and there is no need to write ADERIV. If NA≠0, the user must write ADERIV and load the compiled subroutine into a file to be referenced on the MTS RUN command. This subroutine should

appear as follows:

SUBROUTINE ADERIV(TIME,X,YDOT,NA,NEQ)
IMPLICIT REAL*8(A-H,O-\$)
DIMENSION X(NEQ),YDOT(NA)

code which calculates the vector of NA additional derivatives YDOT(NA)

RETURN END

Here TIME is the independent variable, X(NEQ) is the full vector of variables being integrated (NEQ=number of equations) in which \underline{x} occurs first, $\hat{\underline{x}}$ occurs next, and the additional variables \underline{y} appear last. Thus NEQ=NS+NE+NA. This information can be used if needed to calculate the YDOT at any point in time.

Subroutine DISTRB. If NG=0, the user can call a dummy subroutine as part of the MTS RUN command as described below and there is no need to write DISTRB. If NG≠0, the user must write DISTRB and load the compiled subroutine into a file to be referenced on the MTS RUN command. This subroutine should appear as follows:

SUBROUTINE DISTRB (TIME, X, W, NG, NEQ)
IMPLICIT REAL*8(A-H, O-\$)
DIMENSION W(NG), X(NEQ)

code which calculates the process disturbance vector W(NG)

: RETURN END

Here TIME and X(NEO) are as defined above.

The user will also have to prepare SHIPSIM input as described in the User's Documentation for SHIPSIM.² This will include the selection of integration method and specification of integration control parameters. For a system subjected to white noise disturbances or measurement noise, the integration method choice, step size choice, and specification of measurement noise standard deviation (σ in OPTSIM input) must be done with care. First, only fixed step-size Euler or rectangular integration should be specified. This has the effect of approximating the gauss-markov continuous process by a discrete gauss-markov sequence. (See Bryson and Ho, Applied Optimal Control, Blaisdell, 1969, pp. 342-344 and pp. 364-366). In order for this approximation to preserve the correct system response covariance, the white noise for measurement i must have a standard deviation given by,

$$\sigma_{i}' = \left[\frac{R_{ii}}{\Delta t}\right]^{1/2}$$

where R_{ii} is the corresponding power spectral density used for measurement i in the OPTSYS design and Δt is the simulation integration step-size specified in the SHIPSIM input. Since σ_i' depends on Δt , the variable step-size Kutta-Merson integration available in SHIPSIM must not be used.

MTS RUN INFORMATION: The object code for OPTSIM and the dummy subroutines ADERIV and DISTRB are in files under account SGTA (subject to change; check with Prof. Michael G. Parsons). The RUN is actually made using SHIPSIM so reference should also be made to its description and user's instructions. It is also necessary to utilize two subroutines out of the IBM Scientific Subroutine Package in calculating the random measurement noise. A run using the three dummy subroutines would appear as follows:

\$RUN SGTA:SHIPSIM.O+SGTA:ACALC.D+SGTA:OPTSIM.O+SGTA:ADERIV.D+SGTA:DISTRB.D +NAAS:SSP+*PLOTSYS 4=(SHIPSIM input data file) 5=(OPTSIM input data file) 9=(output file for input to *PLOTSYS)

Appropriate user supplied object code files should be referenced if the optional subroutines ACALC (see SHIPSIM description²), ADERIV, and/or DISTRB are utilized. If device 9 is not used it can be set equal to *DUMMY* or a temporary file.

A complete example will not be included here; example runs can be made available upon request. A sample OPTSIM input data file and the corresponding input verification output produced by OPTSIM for a case where NS=NE follows. Sample output from SHIPSIM is included in the SHIPSIM User's Documentation.²

OPTSIM input file:

P _s	0.0E0	1.0E0 -0.17657E+01	0.050		The second secon	
	0.0		-0.52766E+00		-0.88074E+00 -0.15607E+00	
	1.050	0.0E0	-1.0E0	0.0E0	0.0F0	
	0.0E0	0.0E0	0.0E0	0.0E0	-0.439E0	
G _s	0.0F0	0.050	0. 0E 0	0.0E0	0.43950	
C	7.74621E+00	4.62370E+00	1.70009E+01	2.42523E+00	-4-71320F+00	
r	0.0	0.0	0.47768E+03	-0.50043E+01	0.21141E+02-	0.28233E+02
	0.0	0.0	0.0	0.0		
Hs	1.0E0	0.0E0	0.0E0	0.0E0	0.0F0	0.0E0
	1.0E0	0.050	0.0E0	0. 0E 0	0.0E0	0.0E0
	0.0E0	1.0E0	0.0F0			***************************************
ĸ	2.188975-01	1.009735+00	1.35941E-03	4.85688E-02	6.18658E+02-	4.43003E-03
	6.71746E-02	4.56445E+01-	-4.76066E-01	1.32662F-01-	-8.98771E+00	9-56480F-01
	0.0	0.0	0.0			
ø	3.4904E-3	7.6544E-4	3.4480E-2			

OPTSIM input verification output:

```
OPTSIM OPTIMAL STOCHASTIC CONTROLLER SIMULATION PROGRAM
IMPUT VERIFICATION MEQ = 11
ORDER OF SYSTEM = 5
BUSBER OF CONTROLS = 1
NUMBER OF OBSERVATIONS = 3
NUMBER OF PROCESS NOISE SOURCES = 2
NUMBER OF AUXILIARY STATES - 1
ORDER OF ESTIMATOR = 5
SYSTEM OPEN LOOP DYNAMICS MATRIX.... PS (MS, MS)
                                 0.0
0.57359E+01
-0.52766E+00
-0.10000E+01
   0.0
                   0.10000E+01
-0.17657E+01
0.17199E+00
                                                     0.0
                                                                     0.0
-0.88974 E+00
-0.15607E+00
                                                                     0.0
-0.43900E+00
   0. 10000E+01
                    0.0
SYSTEM CONTROL DISTRIBUTION MATRIX....GS (MS, MC)
   0.0
   0.0
   0.0
   0.43900E+00
PREDBACK CONTROL GAINS .... C (NC, NS)
   0.77462E+01
                    0.46237E+01 0.170C1E+02
                                                   0.24252E+01 -0.47132E+01
SYSTEM DISTURBANCE DISTRIBUTION MATRIX.... GAMMA (MS, NG)
   0.0
                   0.0
-0.50043E+01
   0.477682+03
   0.21141E+02
                   -0.28233E+02
SYSTEM MEASUREMENT SCALING MATRIX.... HS (NOB, NS)
                    0.0
0.10000E+01
                                                     0.0
   0. 1C000E+01
                                     0.0
                                                     0.10000E+01
KALMAN-BUCY PILTER GAINS .... K (NS, NOB)
    0.21890E+00
```

MEASUREMENT MOISE STANDARD DEVIATIONS....SIGNA (NOB)

0.34904E-02 0.76544E-73 0.34480E-01

Appendix C: User's Documentation for OPTSYS

UNIVERSITY OF MICHIGAN

DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING

Rev. 2 5/27/77

IDENTIFICATION: OPTSYS Program

PROGRAMMER: original version by W. Earl Hall, Jr., Dept. of Aeronautics

and Astronautics, Stanford Univ., 1971, (now Systems Control, Inc., Palo Alto, CA.); adapted to MTS by Ass't Professor Michael G. Parsons, Dept. of Naval Architecture and Marine

Engineering, Univ. of Michigan, June, 1976.

PURPOSE: The program provides fast and efficient solutions to the steadystate, linear optimal control and filter problems using the usual

quadratic penalty function on the state and control variables. With user inputs of penalty function, constant coefficient state and measurement equations, and noise spectra, the various program options will provide optimal feedback gains, Kalman-Bucy filter gains, RMS state and control response, response to a constant disturbance, and an evaluation of controllability, disturbability and observability via modal decomposition of the state and measurement equations. It is also possible to evaluate RMS state and control response when feedback gains and filter gains are provided externally.

METHOD:

References: 1. Bryson, A.E. Jr., and Ho, Y.C., Applied Optimal Control, Blaisdell Publ., 1969.

- Bryson, A.E. Jr., "Control Theory for Random Systems," <u>Proceedings</u> of the Thirteenth International Congress of Theoretical and Applied Mechanics, Moscow, August 1972.
- 3. MacFarlane, A.G.J., "An Eigenvector Solution of the Optimal Linear Regulator Problem," <u>Journal of Electronics</u> and Control, Vol. 14, No. 3, May, 1963, pp. 643-654.
- 4. Potter, J.E., "Matrix Quadratic Solutions," SIAM <u>Journal</u> of Applied Mathematics, Vol. 14, No. 3, May, 1966, pp. 496-501.
- 5. Bryson, A.E., Jr., and Hall, W.E. Jr., "Optimal Control and Filter Synthesis by Eigenvector Decomposition," Stanford Univ. Guidance and Control Lab. SUDAAR #436, Nov., 1971.

This program treats the problem of designing optimal controllers for stationary, linear systems disturbed by Gauss-Markov noise. The system must be represented by the model,

 $\frac{\dot{x}}{x} = Fx + Gu + \Gamma w , \qquad (1)$

 $\underline{z} = H\underline{x} + \underline{v} \quad , \tag{2}$

where:

x = state vector (nxl),

 $\bar{u} = control \ vector \ (mxl),$

 $\overline{\underline{w}}$ = white disturbance noise (qxl) with zero mean and power spectral density matrix Q (qxq); or separately a constant disturbance w_C ,

z = measurement vector (pxl),

 \overline{y} = white measurement noise (pxl) with zero mean and power spectral density matrix R(pxp),

F = open-loop dynamics matrix (nxn),

G = control distribution matrix (nxm),

 Γ = state disturbance distribution matrix (nxq),

H = measurement scaling matrix (pxn).

An optimal controller can be defined as the one which minimizes the expected value of the quadratic penalty function,

$$J = \frac{1}{2} \underline{\mathbf{x}}^{\mathrm{T}} A \underline{\mathbf{x}} + \frac{1}{2} \underline{\mathbf{u}}^{\mathrm{T}} B \underline{\mathbf{u}}, \tag{3}$$

where:

A = positive semi-definite state weighting matrix (nxn)

B = positive definite control weighting matrix (mxm).

This program utilizes the certainty-equivalence principle or separation principle which states that the optimal feedback in the ensemble average sense for the above system is the optimal deterministic controller preceded by the optimal estimator (or filter) of the states. The program can in sequence or individually design the optimal deterministic controller, design the Kalman-Bucy filter, and evaluate the RMS state and control response.

State-feedback Controller: The calculus of variations can be used to show $\frac{1}{2}$ that the state-feedback controller which minimizes eqn. (3) is given by,

$$\underline{\mathbf{u}} = \mathbf{C}\underline{\mathbf{x}} = -\mathbf{B}^{-1}\mathbf{G}^{\mathrm{T}}\mathbf{S}_{m}\underline{\mathbf{x}},\tag{4}$$

where S is the steady-state solution of the backward matrix Riccati equation,

$$\dot{S} = -SF - F^{T}S + SGB^{-1}G^{T}S - A, \quad S(t_{f}) = 0.$$
 (5)

Most methods for solving for S_{∞} (integrating eqn, (5) to steady-state or solving simultaneous quadratic equations) are expensive and subject to numerical difficulties for large n. This program utilizes a technique called eigenvector decomposition which was first proposed by MacFarlane³ and Potter⁴ and which is both fast and well-behaved. Earl Hall⁵ used the QR algorithm for finding eigenvalues and eigenvectors to develop a practical and efficient means of utilizing the MacFarlane-Potter method. Hall's work was extended by other students at Stanford Univ. to produce this program.

The eigenvector decomposition method is based on finding the eigenvectors of the Euler-Lagrange equations (2n) for minimizing eqn. (3) subject to eqn. (1):

$$\begin{bmatrix} \frac{\dot{\mathbf{x}}}{\dot{\underline{\lambda}}} \end{bmatrix} = \begin{bmatrix} \mathbf{F} & -\mathbf{GB}^{-1}\mathbf{G}^{\mathbf{T}} \\ -\mathbf{A} & -\mathbf{F}^{\mathbf{T}} \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \underline{\lambda} \end{bmatrix}. \tag{6}$$

The eigenvalues of this system are in pairs which are symmetric about the imaginary axis in the complex plane. If these eigenvalues are grouped into those with positive real parts and those with negative real parts, the associated eigenvectors can likewise be grouped as follows.

$$\widetilde{\lambda} = \left[\frac{x_{+} + x_{-}}{\lambda_{+} + \lambda_{-}} \right], \tag{7}$$

where the eigenvectors with minus subscript are associated with the eigenvalues with negative real parts, etc. The steady-state solution to eqn. (5) is given by,

$$s_{\infty} = \Lambda_{-} (x_{-})^{-1}$$
 (8)

the eigenvalues of the controlled system (F-GC) are the eigenvalues of eqn. (6) with negative real parts, and the eigenvectors of the controlled system are the columns of X. Similarly, if eqn. (5) were a forward matrix Riccati equation the steady-state solution would be given by -X (Λ) as will be utilized below in the filter problem.

<u>Kalman-Bucy Filter</u>: The calculus of variations can be used to show ^{1,2} that the maximum likelihood filter for estimating the state of a system disturbed by white noise from measurements which contain white noise is given by,

$$\frac{\dot{\hat{x}}}{\hat{x}} = F\hat{x} + G\underline{u} + K(\underline{z} - H\hat{x}), \tag{9}$$

where the filter gain matrix K is given by,

$$K = P_{m}H^{T}R^{-1}.$$
 (10)

The matrix P_{∞} is the steady-state solution of the forward matrix Riccati equation,

$$\dot{P} = FP + PF^{T} - PH^{T}R^{-1}HP + \Gamma Q\Gamma^{T}, \quad P(t_{o}) = X(t_{o}). \quad (11)$$

Here P (nxn) is the covariance matrix of the error of the state estimate and X (nxn) is the covariance matrix of the state.

The steady-state solution of eqn. (11) may be found by using the eigenvector decomposition of the Euler-Lagrange equations (2n) for the filter problem 1,2; i.e.,

$$\begin{bmatrix} \frac{\dot{\mathbf{x}}}{\dot{\lambda}} \end{bmatrix} = \begin{bmatrix} \mathbf{F} & -\mathbf{\Gamma}\mathbf{Q}\mathbf{\Gamma}^{\mathbf{T}} \\ -\mathbf{H}^{\mathbf{T}}\mathbf{R}^{-1}\mathbf{H} & -\mathbf{F}^{\mathbf{T}} \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \underline{\lambda} \end{bmatrix} + \begin{bmatrix} \mathbf{0} \\ \mathbf{H}^{\mathbf{T}}\mathbf{R}^{-1}\mathbf{Z} \end{bmatrix}.$$
(12)

Since eqn. (11) is a forward matrix Riccati equation, the steady-state solution is given by,

$$P_{\infty} = -X_{\perp} \left(\Lambda_{\perp} \right)^{-1} \tag{13}$$

where X and Λ_+ are partitions of the eigenvectors associated with the eigenvalues of eqn. (12) having positive real parts. The eigenvalues of the estimate errors $\frac{\tilde{\mathbf{x}}}{\tilde{\mathbf{x}}} = \frac{\hat{\mathbf{x}}}{\tilde{\mathbf{x}}} - \frac{\hat{\mathbf{x}}}{\tilde{\mathbf{x}}}$ are the eigenvalues of eqn. (12) with negative real parts and the eigenvectors of the estimate errors are the columns of $(\Lambda_+)^{-1}$.

RMS State and Control Response: If perfect measurements are available (no filter), the stationary statistical response of the states is determined by the linear matrix equation 1,

$$(F+GC)X + X(F+GC)^{T} + \Gamma O \Gamma^{T} = 0$$
(14)

where again X is the covariance matrix of the states. The RMS response of each state is the square root of the associated diagonal element of X. The covariance matrix for the control will be,

$$E(\underline{u}\underline{u}^{T}) = CXC^{T}, \tag{15}$$

with the RMS control the square root of the associated diagonal element of this matrix.

If filtered estimates of the state are used, the covariance matrix for the state is given by, $^{\rm l}$

$$X = \hat{X} + P_{\perp} , \qquad (16)$$

where \hat{X} is the covariance matrix for the state estimate given by the linear matrix equation,

$$(F+GC)\hat{X} + \hat{X}(F+GC)^{T} + KRK^{T} = 0$$
 (17)

In this case, covariance matrix for the control is given by,

$$E(uu^{T}) = C\hat{X}C^{T}. (18)$$

Steady-state Response: The stochastic control and RMS response are with respect to zero mean disturbances. The program will also separately calculate state and control response to a constant disturbance, if desired, by using,

$$\underline{\mathbf{x}}_{SS} = -(\mathbf{F} + \mathbf{GC})^{-1} \Gamma \underline{\mathbf{w}}_{C} , \qquad (19)$$

and,

$$\underline{\mathbf{u}}_{SS} = \mathbf{C}\underline{\mathbf{x}}_{SS} . \tag{20}$$

The calculated RMS response would then be with respect to or additive to these steady-state values.

Controllability, Disturbability, and Observability: This program can also be used to determine the relative effectiveness of selected control inputs, the relative coupling of state disturbances to the dynamic plant modes, and the relative detectability of the dynamic plant modes from selected measurements. The state and measurement equations can be displayed in modal (normal-coordinate or Jordon canonical) form; i.e.,

$$\frac{\dot{\xi}}{\xi} = F' \underline{\xi} + G' \underline{u} + \Gamma' \underline{w} \tag{21}$$

$$z = H'\xi + v \tag{22}$$

where:

 $\begin{array}{l} \underline{x} = T\underline{\xi} \ , \\ \overline{T} = \text{matrix of right eigenvectors of } F; \text{ columns are eigenvectors} \\ \text{ of } F\underline{t}_i = \underline{t}_i \ \lambda_i \ , \\ F' = T^{-1}FT \text{ is the diagonal eigenvalue matrix for distinct} \\ \text{ eigenvalues}, \\ T^{-1} = \text{matrix of left eigenvectors of } F; \text{ rows are eigenvectors} \\ \text{ of } \underline{t}_iF = \underline{t}_i \ \lambda_i \ , \\ G' = T^{-1}G, \\ \Gamma' = T^{-1}\Gamma, \\ H' = HT. \end{array}$

The degree of controllability (by control inputs) and disturbability (by state disturbances) are shown by displaying the degree of orthogonality between the control distribution vector(s) and disturbance distribution vector(s), respectively, and the left eigenvector of each open-loop mode. Thus for controllability of mode i with control j the program displays,

$$\cos \Theta_{ij} = \frac{\left|\underline{t}_{1i}\underline{g}_{j}\right|}{\left|\underline{t}_{1i}\right| \left|\underline{g}_{j}\right|},$$
(23)

where $\underline{t_{1i}}$ is the left eigenvector associated with mode i and $\underline{g_j}$ is the vector (column) of G associated with control j. A result 1.0 indicates maximum coupling or controllability and a result of 0.0 indicates complete uncontrollability. Similarly, the degree of disturbability is shown by displaying,

$$\cos\phi_{ij} = \frac{\left|\underline{t_{1i}} \ \underline{\gamma_{j}}\right|}{\left|\underline{t_{1i}}\right| \left|\underline{\gamma_{j}}\right|} \,, \tag{24}$$

where γ_j is the vector (column) of Γ associated with state disturbance j. And the state disturbance j.

The degree of observability is shown by displaying the degree of orthogonality between the right eigenvector of each open-loop mode and the measurement distribution vector(s). Thus for observability of mode i with measurement j the program displays,

$$\cos \beta_{ij} = \frac{\left| \underline{h}_{j} \underline{t}_{ri} \right|}{\left| \underline{h}_{i} \right| \left| \underline{t}_{ri} \right|}, \tag{25}$$

where \underline{t}_{ri} is the right eigenvector associated with mode i and \underline{h}_j is the vector (row) of H associated with measurement j. A result 1.0 indicates maximum observability and a result 0.0 indicates that mode i is not observable with measurement j. If mode i is not observable from any measurement, the system is not observable.

For complex eigenvalues of F, the eigenvectors in T and T^{-1} are also complex. The elements of G´, Γ ´, and H´ will also be complex. The eigenvector matrices and G´, Γ ´, and H´ are then presented in a real form; i.e.,

$$T = [t_{1r}, t_{1i}, t_{2r}, t_{2i}, ...],$$

where \underline{t}_{1r} and \underline{t}_{1i} are, for example, the real and imaginary parts, respectively, of the first conjugate pair of right eigenvectors. Likewise, for complex eigenvalues the degree of controllability, disturbability, and observability are presented for the real and imaginary parts of the associated left (or right) eigenvector conjugate pair. Thus, $\cos\theta_{1j}$ and $\cos\theta_{2j}$ will be the results for the orthogonality of the real and imaginary part, respectively, of first pair of conjugate eigenvectors and the jth control distribution vector.

PROGRAM OPTIONS: This program is very flexible with a number of options which control output and needed input. These will be presented prior to defining the input details.

- - = 1, if A and Q will be input as full matrices; B and R input as diagonals only, off-diagonal elements assumed zero;
- IR = 0, if optimal feedback controller and filter are to be determined
 with C and K output;
 - = 1, if C is to be provided as input; optimal filter to be determined and K output;
 - = 2, if K is to be provided as input; optimal feedback controller to to be determined and C output;
 - = 3, if both C and K are to be provided as input;
- ISS = 1, if steady-state values for states and control for a steady
 disturbance w_C are to be determined and output; = 0, if not;
- IM = 1, if modal equations (G', Γ', and H'), controllability, disturbability, and observability are to be determined and results output (IOL = 1, required); = 0, if not.

IP = 1, program calculated C and K matrices are to be output to I/O
 device 7 using format 6E12.5 repeated as required but beginning
 C and K with a new record; = 0, if not.

These options will allow the design and evaluation of an optimal controller and filter (IQ = 1, IR = 0); study of controllability, disturbability, and observability of a system (IOL = 1, IM = 1); evaluation of controller and filter performance when system characteristics change (IQ = 1, IR = 3, with new state equations F and G); etc. When control gains are provided as input the program checks the closed loop system for stability. Likewise, when filter gains are provided as input the filter is checked for stability. In each case, only that input necessary for the selected options must be provided.

USER'S INSTRUCTIONS: Input records should consist of the following in the specified sequence including only those required.

Record Type Number	Input	Format	Comments
1.	"title"	18A4	Any 72 character title for the output.
2.	IOL, IQ, INQ, IR, ISS, IM, IP	712	Program option control integers as defined above.
3.	NS, NC, NOB, NG	413	NS = number of states, n≤25 NC = number of controls, m≤8 NOB = number of measurements, p≤25 NG = number of state disturbances, q≤25
4.	F	6E12.5 repeated as required	F matrix input by rows beginning with a <u>new</u> record for each row.
5.*	A	6E12.5 repeated as required	A input as a diagonal only or input as an entire matrix as set by INQ. Matrix input by rows without a new record for each row.
6.*	G	6E12.5 repeated as required	G input by rows without a new record for each row.

Record Type Number	Input	Format	Comments
7.*	В	<pre>6E12.5 repeated as required</pre>	B input as diagonal only
8.*	С	6E12.5 repeated as required	C input by rows without a new record for each row if IR = 1 or 3.
9.*	Г	6E12.5 repeated as required	I input by rows without a new record for each row.
10.*	Q	6E12.5 repeated as required	Refer to A above. This power spectral density defines $\underline{\mathbf{w}}$.
11.*	н	6E12.5 repeated as required	H input by rows without a new record for each row.
12.*	R	6E12.5 repeated as required	R input as diagonal only. This power spectral density defines v.
13.*	K	6E12.5 repeated as required	K input by rows without a new record for each row if IR = 2 or 3.
14.*	¥ _C	6E12.5 repeated as required	steady disturbance vector only if ISS = 1.
15.	"job control"	A2	「!* if another case follows /* if no case follows

*included only if required by input on records 2 or 3.

To clarify which of the input record types 5 through 14 must be provided note that the input sequence is as follows:

Portions of this sequence should be deleted as follows:

if NC = 0, delete A,G,B,C, if NOB = 0, delete H,R,K if NG = 0, delete Γ,Q,H,R,K if ISS = 0, delete WC C,K if IR = 0, delete = 1, delete A,B,K = 2, delete C = 3, delete A,B

MTS RUN INFORMATION: The object code for the OPTSYS program is on file under account SGTA (subject to change; check with Ass't Prof. Michael G. Parsons). The program can therefore be run on MTS by using:

\$RUN SGTA:OPTSYS.O 7=(user's file for output of C and K)
:
input data cards
:
\$ENDFILE

If the data is in an MTS file, I/O device 5 can be set equal to the file name on the \$RUN command. If no output is to be made to I/O device 7, device 7 should be set equal to *DUMMY* on the \$RUN command. If I/O device 7 is to be set equal to *PUNCH* remember to include on appropriate card number specification (C=...) on the MTS job card. The compilation cost for the entire program under MTS is about \$3.60. The run cost for the NS = 5 example using all options which follows was \$.50.

EXAMPLE INPUT AND OUTPUT: The following example is a NS = 5 test problem for the control of a tanker along a straight line when subject to a white noise current disturbance normal to the ship's path. The states are heading, yaw rate, offset from the line, offset rate, and rudder angle. A single control is the rudder command. Measurements are the heading, yaw rate and offset, each contaminated by white noise. The non-dimensionalized input is as follows:

SSIGNON SGTA	BI = IR I & A	C=20			
SRUN OPTSYS.O	7=*P	OBCH.			
TANKER N=5	EST PROBLEM	PRCH MILLERS'	PAPER		
110011	1				
5 1 3 1					
0.020	1.020	0.020	0.020	0.0E0	
6.25220	-1.72750	0.000	-6.25220	-6.776E0	
0.020	0.020	0.0EC	1.080	0.0E0	
G. 622ED	0.69920	0.020	-0.62220	0.84620	
0.620	0.020	0.029	0.020	-1.021	
0.27423	0.130E2	0.20824	0.27423	0.69420	
C.030	0.0E0	0.030	0.020	1.021	
0.21322					
0.020	6.25220	0.020	0.62220	0.020	
0.441-6					
1.020	0.020	0.020	0.020	0.080	0.030
1.020	3.020	0.080	0.080	0.030	0.0 BO
1.023	0.020	0.0E0			
0.240 E-6	2.3482-5	2.0008-5			
0.12-2					
**					

The resulting output with all options selected is as follows:

UNIVERSITY OF MICHIGAN DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING OPTSYS STATIONARY, LINEAR OFTIMAL CONTROLLEM DESIGN PROGRAM ADAPTED FROM STANFORD UNIVERSITY OPTSYS PROGRAM JUNE 1976

TABRER N=5 TEST FROBLEN FFCE HILLERS' PAPER

CROLE OF SYSTEM = 5

MUMBER OF CONTROLS = 1

MUMBER OF OBSERVATIONS = 3

MUMBER OF PROCESS NCIST SCURCES = 1

OPEN LOOP DYNAMICS MATRIX....P

0.0	1.0003+00	C.C	0.0	0.0
6.2522+00	-1.727E+00	C.C	-6.252E+^G	-6.776 =+ 39
0.0	0.)	0.0	1.0001+00	0.0
6.2205-01	6.9902-01	0.6	-6.227E-01	9.460E-01
0.0	C.3	C.C	6.0	-1.000 E+01

EIGENSYSTEM OF OPEN LOUP SYSTEM

RIGHT EIGENVECTORS REAL EIGENVALUE (1) PEAL EIGENVECTOR (1) (0.0)+3(0.0) (0.0 (1.0000000) (0.0) REAL EIGENVALUE (2) FEAL EIGENVECTOR (2) (-0.3437854) (-2.653388Z+0C)+J (0.0 (0.9121995) (-9.2086217) REAL EIGENVALUE (3) PEAL EIGTNVECTOR (3) (0.3061612) (3.043875E-01)+J (0.0 (0.9063478) (C.275981-) REAL EIGENVALUE (4) FEAT FIGURATION (4) (**.00716.0 **) (-0.0076.0 **) (-1.00707070) (**.007070**) (**.007070**) (-3.539095E-15)+J(3.3 REAL EIGENVALUE (5) ETAL EIGENVECTOR (5) (-1.00000CE+91)+J(9.0 (-0.06:4863) (0.6646677) (0.311124') (-0.1114735) (2.795:099)

```
-1.852E+16 -2.1163+15 1.CCCE+30 2.127F+15 3.2342+15
-2.317E+00 7.529E-01 0.C 2.317E+01 -4.276E-01
2.268E+01 3.3615+00 -4.C -2.268E+01 -4.C72E+30
-1.852E+16 -2.1162+15 -C.C 2.127Z+16 3.234E+15
0.0 0.0 1.272E+06
  STATE WEIGHTING MATRIX....A
   2.740E+02
0.0
                    0.0
1.3008+01
0.0
0.0
0.0
0.0
0.0
0.0
                                                         C.C
C.O
O.C
2.7403+02
O.C
                                                                          0.0
                                                                           0.0
6.9402-01
  CONTROL DISTRIBUTION MATFIX....G
   0.0
    0.0
    1.000E+01
  MODAL CONTROL DISTRIBUTION EATRIX.... G PRIME
  3.234E+16
-4.276E+00
  -4.072E+01
   3.234E+16
1.2725+C1
 RELATIVE CONTROLLABILITY OF NORMAL MODES....COS (THETA (I,J))
        POR MODE I WITH CONTECT J
   1.1365-01
   1.264E-01
1.253E-01
   1.1365-01
 CONTROL WRIGHTING MATRIX....B
   2.19CE+C1
 EIGESSYSTEM OF OPTIMAL CLOSED LOOP SYSTEM ..
COMPLEX EIGENVALUE ( 1) ......
                                                               COMPLEX EIGENVECTOR ( 1) ......
(-5.207049E+00) +J ( 2. #15923E+00)
                                                                   (-0.1485912)+3 (-0.0923567)
                                                                   ( 1.30(007) +J ( 0.0 )
( 0.029(061) +J ( 0.022875))
(-0.21545(4) +J (-0.0374324)
( 0.5752734) +J (-0.4551780)
CCMPLEX SIGESVALTE ( 2) ......
                                                               CCEPLEX EIGENVECTOR( 2) ......
(-1.723152E+CG) +J ( 5.2056642-C1)
                                                                    (-0.5317973) +J(-0.1676566)
                                                                   ( 1.0)((703)+J( 7.0
( 0.244,401)+J(-0.1297732)
(-0.3637383)+J( 7.3149987)
                                                                   (-9. 1556 376) +J (-0. 5156 879)
```

MODAL MATRIX INVERSE: LEFT EIGENVECTOR MATRIX.... INVERSE

```
REAL BIGBHVALUE ( 1) ......
                                                                   BRAL EIGENVECTOR ( 1) ......
 (-8.1570632+00) € ( 0.0
                                                                       (-0.6917690)
                                                                       (-0.0166971)
( 0.1361995)
CONTROL GAINS .... C
   7.0770642+00 2.5952492+00 9.7456232+00 4.0206015+00 -9.6694642-01
CLOSED LOOP DYNASICS MATRIX....F+GC

    0.0
    1.00∪0005€€€
    0.0
    0.0

    6.252€0€€€60
    -1.7270005€€
    0.0
    -6.252€0€€€0
    -6.7750008€0

    0.0
    0.0
    1.0000005€0
    0.0

    6.220€00€=01
    6.99€000E=01
    0.0
    -6.220€005€-01
    9.460€008=01

    7.077054E€01
    2.595249E±01
    9.785623E±01
    4.0206012±01
    -1.966846E±01

 STATE DISTURBANCE DISTRIBUTION HATRIX....GAMMA
   0.0
6.252E+00
   0.0
6.220E-01
0.0
 MODAL STATE DISTURBANCE DISTFIBUTION MATFIX....GAMEA PRIME
 -4.000E+C0
6.148E+00
6.904E+00
   2.000E+00
 RELATIVE DISTURBABILITY OF HORMAL MODES....COS (PHI (I,J))
         FCR MODE I BY DISTUREANCE J
   2.236E-17
   2.887E-01
3.380E-02
   1.118E-17
 POWER SPECTRAL DEMSITY - STATE DISTUFFANCE....Q
   4.400E-07
 BEASUREMENT SCALING MATEIX....
                                                                            0.0
                     1.0003+00
MODAL MEASUREMENT SCALING MATRIX.... PRIME
  0.0 -3.33EE-01 3.662E-01 3.635E-16 -6.049E-02
0.0 9.122E-01 9.319E-02 -1.22E-31 6.049E-01
1.300E+00 7.962E-02 9.063E-01 -1.000E+00 1.120E-02
```

RELATIVE OBSERVABILITY OF MOREAL HODES....COS(BETA(J,I)) POR MODE I PROM MEASUREMENT J 3.0629-01 3.6391-16 0.0 3.4362-01 6.C49E-02 9.319=-52 1.2221-31 1.00CB+00 7.862E-02 9.C63E-01 1.CCDE+00 1.120E-02 POWER SPECTRAL DENSITY - MEASUREMENT NCISE B 2.40CE-07 0.0 3.4863-06 0.0 0.0 EIGENSYSTEM OF ESTIMATE ERECE EQUATION COMPLEX EIGENVALUE (1) COMPLEX EIGENVECTOR(1) (-0.0873291)+J(0.0131527) (-2.595447E+90) +J (1.119110E+00) (0.4339821)+J(-0.0199352) (0.8074845)+J(0.0013291) (-0.1456895)+J(0.0095797) (1.0000702)+J(0.0 PEAL EIGENVALUE (1) FEAL FIGEN VECTOR (1) (-9.5027913-02)+J(0.0 (1.4558396) (0.7526974) (0.0550158) (0.4716369) (0.0 REAL EIGENVALUE (2) REAL EIGENVECTOR (2) (-0.7357525) (-6.261854Z-07)+J (0.6 (0.0016184) (0.9999704) REAL EIGENVALUE (3) PIAL RIGINVICTOR (3) (1.0511230) (-1.000000E+01)+J(0.0) (0.1443075) (-1.9574144) 10.0 COVARIANCE OF THE ESTIMATION FREDE....P 5.2412483-07 6.3135751-67 2.6582161-07 5.1922942-07 2.930778E-36 1.090007E-07 1.090007E-07 1.930454E-36 8.463483E-07 2.431576E-37 6.313576E-07 2.668216E-07 8.463463E-07 2.431976E-07 5.363545E-07 5.1322882-07 PILTER STEADY STATE GAINS....K 2.183853E+00 1.914246E-01 1.334108E-02 2.630657E+00 8.565454E-01 5.450034E-03 1.11757E+00 3.132204E-02 9.652471E-02 2.163454E+00 2.432035E-01 1.215988E-02 0.0 0.0 COVAPIANCE OF THE ESTIMATE.... X HAT 1.9757765-06 -6.3135762-07 -1.0532692-06 .435350E-06 3.5731025-06 -6.3135762-07 1.644640E-05 -2.063580E-04 -4.146194E-05 -1.147418E-06 -7.144734E-07 1.9257870E-06 1.235787E-06 -2.4315762-07 -7.144734E-07 2.997360E-06 1.3929632-05 1.3929632-05

STATE COVABIANCS MATRIX.... = I HAT + P

2.399903E-06 2.734064E-19 -7.864673E-07 1.954579F-06 3.573102E-06
2.184622E-19 2.142717E-05 -1.954579E-06 -3.299836E-06 -1.147418E-06
-7.864673E-07 -1.954574E-06 3.170282E-06 7.14287(E-20 -7.144734E-07 2.997360E-06 1.392963E-05

CONTROL COVARIANCE.... E (0.01)

3.0308342-05

STATE RMS RESPONSE . CONTROL PAS PESPONSE

1.54916209-03 4.62994958-03 1.56839993-03 3.7322415E-03

5.50530142-03

STEADY DISTURBANCE.... W SUE C

1.0000002-03

STEADY STATE VALUES OF STATES....

-1.000E-C3 -0.0 7.262E-C4 -0.0 -1.626E-19

STEADY STATE CONTROLS....

-7.101E-19

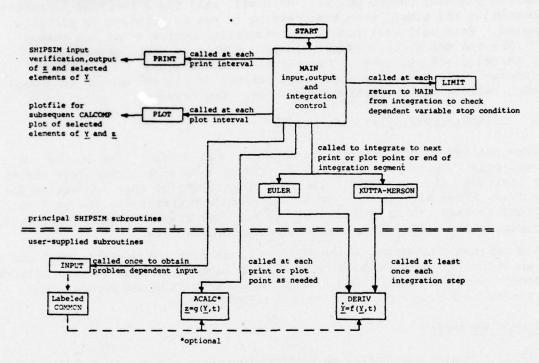
EXECUTION TERMINATED 11:14:11 T=.321 FC=C \$.31

Appendix D. Programmer's Documentation for SHIPSIM

I. Program Organization

This programmer's documentation does not duplicate the User's Documentation for SHIPSIM which is included as Appendix A. The reader should consult Appendix A before proceeding.

The macro-flow chart for SHIPSIM is shown below.



II. Main Program

The main program may be divided into the following sections: input, initialization, input verification, integration control, and error processing.

The input portion calls the user-supplied subroutine INPUT for acquisition of problem dependent data and reads those SHIPSIM integration and output control parameters given in the User's Instructions (Appendix A).

Initialization begins with the assignment of initial values to the NEQ2 elements of Y. (NEQ2 is the SHIPSIM equivalent of the INPUT subroutine variable NEQ.) In the same loop LY, the subscript of the element of Y to be tested against YTERM for the dependent variable integration stopping condition, is assigned. The value of LY is found by matching the character variable YTEST against the vector of Y-element names YLABLE. This technique is utilized frequently throughout the program. PLY and PLZ, vectors containing the subscripts of the Y and z elements to be plotted, are loaded next using a similar character matching technique.

All SHIPSIM input is written on I/O channel 6 for user verification.

Integration control begins with a call to PLOT1 for loading of the plot vector with the initial values of \underline{Y} . All remaining integration control operations are enclosed in the DO loop beginning at statement 400. They are executed once for each integration segment.

The call to entry PRINTl in subroutine PRINT results in the printing of all or selected \underline{Y} and all \underline{z} values at the beginning of each segment. For the first segment these will be, for \underline{Y} , the values of $\underline{Y}\emptyset$. NST is the number of steps (STEP) in the segment, each step being the minimum of the times between printing and plotting output points. MAIN will call the appropriate integration subroutine NST times, each time testing to see if printing or plotting is required. Each call will result in integration over a Δt of one step (STEP). NPR and NPL are the nearest integer number of steps between each pair of printing and plotting output points, respectively. One of these variables must have the value one. Thus printed or plotted output will occur after each call to an integration subroutine. The statement

IF (MOD (J, NPR) . EQ.Ø) CALL PRINT2 ...

determines whether or not printing is needed at the current time in the run and if so, prints the values of \underline{Y} and \underline{z} . The call to subroutine LIMIT checks for the limiting value of YTEST. (See the description of this subroutine in section IV.) After all NIS integration segments are completed, the call to entry PLOT2 invokes the subroutines in the PLOT DESCRIPTION SYSTEM (*PLOTSYS) which generate plot files from the integration output data.

MAIN program statements in the 600-699 range read the variable NEXT and branch accordingly. Statements in the 700-999 range deal with various program error conditions. As SHIPSIM was written as a batch-oriented program, any error results in a diagnostic message and termination.

III. COMMON Variables

SHIPSIM contains the following COMMON blocks:

(unlabeled) NEQ2
/OUTPUT/ YLABLE, ZLABLE, TITLE
/COM1/ CPRINT, IOUT, NAC

/COM2/ CPLOT, PLY, PLZ, PLN

These COMMON variables have the following definitions:

CPLOT vector of labels of variables for which plots are

desired, dimension (9) with only (PLN) used.

CPRINT vector of labels of variables to be printed, dimension

(9).

IOUT output format switch,

=1 for tabular output

=2 for vectorial output

NAC dimension of z

NEQ2 dimension of Y

PLN number of plots desired, dimension of CPLOT

PLY vector of subscripts of the elements of \underline{Y} to be

plotted, dimension (9).

PLZ vector of subscripts of the elements of \underline{z} to be plotted, dimension (5).

TITLE User's 72 character title, dimension (9).

YLABLE labels for NEQ elements of Y, dimension (25).

ZLABLE labels for NAC elements of z, dimension (5).

All real variables above are double precision. As the library subroutines used in SHIPSIM subroutine PLOT require single precision arguments, the /COM2/ variables in that subroutine will have dimensions of two times those given above.

IV. Subroutine Descriptions

The SHIPSIM subroutines are described here in alphabetical order. The designation (I) after a subroutine calling argument indicates that the quantity is input to the subroutine; (O) indicates that the quantity is returned to the calling program.

1. NAME: DFEQKD

PURPOSE: This subroutine integrates from T to T+STEP by

Kutta-Merson variable step-size integration.

CALLING SEQUENCE: MAIN, DFEQKD

ARGUMENTS: NEQ dimension of Y (I)

X independent variable (I) FIRSTP initial integration (I)

step-size

STEP time interval through which the equations

are to be integrated. (I)

Y vector of dependent variables (I/O)

FUNCT name of subroutine which calculates

derivatives of Y. (I)

EPS maximum permissable relative

error. (I)

AB maximum permissible absolute error. (I)

NCUTS maximum number of times the step-size may be halved before the error return

is taken. (I)

STPSZ =.TRUE., integration progress is

printed at each step.

=.FALSE., printing is suppressed. (I)

SUBPROGRAMS CALLED: FUNCT

COMMENTS: An initial call to DFEQKD with EPS=Ø initializes

HC, the integration step-size.

2. NAME:

EULER

PURPOSE:

To perform rectangular integration of Y from X to

X+STEP

CALLING SEQUENCE:

MAIN, EULER

ARGUMENTS:

X independent variable (I)

dependent variable vector (I/O)

STEP

time interval through which the equations

are to be integrated (I) FIRSTP integration step-size (I)

SUBROGRAMS CALLED:

TEST, DERIV

COMMENTS:

Euler integration is described in Appendix A.

3. NAME:

LIMIT

PURPOSE:

To terminate the simulation run if Y(LY) has

reached the user-specified limit YTERM

CALLING SEQUENCE:

MAIN, LIMIT

ARGUMENTS:

Y the dependent variable vector. (I)

initial values for Y. (I) YØ

YTERM

name of the element of Y to be tested.

(I)

COMMENTS:

None

4. NAME:

PLOT, PLOT1, PLOT2

PURPOSE:

To generate linear-rectangular plots of selected elements of Y for MTS graphic post-processing.

CALLING SEQUENCE:

MAIN, PLOT

ARGUMENTS:

T independent variable. (I) dependent variable vector. (I) Y

NAC

dimension of z (I)

SF

scaling factor for plot size. (I)

SUBROUTINES CALLED:

ACALC, PLTSIZ, PLTXMX, PSCALE, PAXIS, PGRID, PLTOFS, PLTREC, PLIN2, PSYMB, PLTEND, PXMARG

COMMENTS:

This subroutine utilizes the MTS graphic subroutine library contained in the file *PLOTSYS. The sub-

routines in this library perform such functions as axis definition, plot scaling, labeling, and grid definition. For a complete description see MTS Vol. 11.

The library subroutines require two vectors for construction of a plot, one of values of the independent variable, and one for the dependent variable. The SHIPSIM independent variable is T, the dependent variables are selected elements of Y and z. Values of T are loaded into the vector TP through ENTRY PLOT1, one value at each call. This program segment also loads the PLNY elements of \underline{Y} and PLNZ elements of \underline{z} into YPLOT. MP is the current subscript for TP, LP is the subscript of YPLOT corresponding to the first element of Y and z to be loaded. To clarify, if Y(2), Y(3), and Z(2) are to be plotted the variables and vectors used in PLOT would appear as:

PLY. . . . 2, 3, Ø, Ø, Ø, Ø, Ø, Ø, Ø

PLZ. . . . 2, Ø, Ø, Ø, Ø

PLNY . . . 2 PLNZ . . . 1

TP (MP)	LP	n	YPLOT (n) contains
MP = 1	1	1 2	Y(2) at T = TP(1) Y(3) at T = TP(1)
2	3 4	3	z(1) at $T = TP(1)z(1)$ at $T = TP(1)Y(2)$ at $T = TP(2)$
	6	5 6	Y(3) at $T = TP(2)z(3) at T = TP(2)$
3	7	7	Y(2) at T = TP(3)
		•	

Entry at PLOT2 occurs after a run has ended. TP(MP) contains the final value of T, while MP indicates the number of points for each plot. The *PLOTSYS subroutines are described in MTS Vol. 11 and will not be included here.

5. NAME:

PRINT, PRINT1, PRINT2

PURPOSE:

To print the integration results.

CALLING SEQUENCE:

MAIN, PRINT

ARGUMENTS:

IS integration segment number (I)

T

independent variable. (I)

Y

dependent variable vector (NEOx1). (I)

SUBROUTINES CALLED:

ACALC

COMMENTS:

The initial call to PRINT results in the loading of

the vector PRY, with the subscripts of \underline{Y} to be printed. This is accomplished in a manner similar to that used for loading PLY in the main program (see section II of this appendix). PRN is the number of elements of Y to be printed.

Entry at PRINTl occurs at the beginning of each integration segment.

Entry at PRINT2 results in the printing of the current value of the independent variable T and the corresponding values of the selected elements of \underline{Y} and \underline{z} .

V. SHIPSIM in MTS

SHIPSIM was written for the Michigan Terminal System (MTS). The program was deliberately structured so as to be as system-independent as possible to aid in its adaptation to other systems. Only two areas of system dependency exist.

Source code was written for the IBM FORTRAN IV-G (Extended) compiler. If this compiler is unavailable, program alterations must be made to suit the user's system capability.

Reference was made in sections II and IV of this appendix to the Plot Description System graphics subroutine library contained in the MTS public file *PLOTSYS. If the user's system has a similar graphics subroutine library, SHIPSIM subroutine PLOT may be adapted to suit. If it is necessary to delete the plotting capability altogether, the following changes should be made:

Line Number	Changes
10	delete
29	delete "PLN" and "SF"
35	delete
36	delete "PLD(I)"
39	change "415" to "315"
	delete "Dlø.r"
45	delete
56-77	delete
92	delete
96	delete
116,118	delete "PLD(I)"
125	change "6" to "5"
129	delete
132,133	delete
135-138	delete
144,152	change "STE" to "PRD(I)"
146,153	delete "IF (MOD (J, NPR) .EQ. Ø) "
147,154	delete
161	delete

In addition, the entire subroutine PLOT (lines 286-377) should be deleted.

Program size statistics given below apply to SHIPSIM with the plotting capability, as compiled on the Amdahl 470/V-6 computer:

Main program	221	source	lines
	166	source	statements
	733Ø	object	bytes
Subroutine PRINT	61	source	lines
	39	source	statements
	2492	object	bytes
Subroutine PLOT	93	source	lines
	66	source	statements
	14,480	object	bytes

Subroutine EULER	22 17 810	source source object	statements
Function TEST	11 6 404	source source object	statements
Subroutine LIMIT	17 11 642	source source object	statements
Subroutine DFEQKD	99 97 4ø8ø	source source object	statements
Total	530 385 30328	source source object	statements

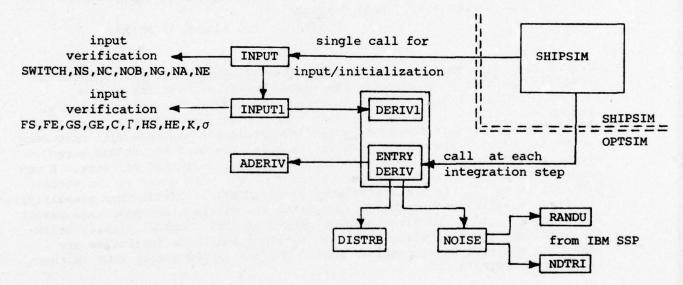
Appendix E: Programmer's Documentation for OPTSIM

I. Program Organization

This programmer's documentation does not duplicate the User's Documentation for OPTSIM which is included in Appendix B. The reader should consult both Appendix A: User's Documentation for SHIPSIM and Appendix B prior to reading this appendix.

OPTSIM is a group of eight double-precision subroutines which are run under the control of the SHIPSIM continuous systems simulation program described in Appendices A and D. These subroutines constitute the INPUT and DERIV subroutines needed by SHIPSIM. Two of the OPTSIM subroutines RANDU and NDTRI are taken from the IBM Scientific Subrouting Package available on the Michigan Terminal System (MTS) under NAAS:SSP.

A macro-flow chart for the OPTSIM subroutines running under SHIPSIM is as follows:



To obtain input to OPTSIM and perform necessary initialization, SHIPSIM calls INPUT once per integration run. Subroutine INPUT reads control and dimensioning variables and writes the input verification of these quantities. It then calls INPUT1 which reads the ten matrices and vectors which define the system, controller, and estimator (if SWITCH=1) or reads changes to these quantities (if SWITCH=2). INPUT1 writes input verification for all data or changes it reads. INPUT1 then calls DERIV1 to transmit the input data. DERIV1 initializes the integer seed XI for the random number generator and calculates the matrix A from the input data; i.e.,

$$\begin{bmatrix}
\frac{\dot{\mathbf{x}}}{\dot{\mathbf{x}}} \\
\frac{\dot{\mathbf{x}}}{\dot{\mathbf{x}}}
\end{bmatrix} = \begin{bmatrix}
\mathbf{F}_{\mathbf{S}} & \mathbf{G}_{\mathbf{S}}^{\mathbf{C}} \\
\mathbf{K}\mathbf{H}_{\mathbf{S}} & (\mathbf{F}_{\mathbf{e}} + \mathbf{G}_{\mathbf{e}}^{\mathbf{C}} - \mathbf{K}\mathbf{H}_{\mathbf{e}})
\end{bmatrix} \begin{bmatrix}
\mathbf{x} \\
\hat{\mathbf{x}}
\end{bmatrix} + \begin{bmatrix}
\mathbf{\Gamma}_{\mathbf{w}} \\
\mathbf{K}_{\mathbf{v}}
\end{bmatrix} = \mathbf{A} \begin{bmatrix}
\mathbf{x} \\
\hat{\mathbf{x}}
\end{bmatrix} + \mathbf{b}$$
(1)

This completes the problem initialization and control is then returned to SHIPSIM through INPUT1 and INPUT.

SHIPSIM calls subroutine DERIVI at ENTRY DERIV once during each integration step throughout the simulation. This call is to obtain the derivative vector YDOT(NEQ) given current values of Y(NEQ) and TIME. The number of integrated equations NEQ equals the number of system states in $\underline{\mathbf{x}}$ (NS) plus the number of estimator states in $\underline{\mathbf{x}}$ (NE) plus the number of additional derivatives in $\underline{\mathbf{y}}$ (NA). The correspondence between SHIPSIM and OPTSIM variables and derivatives is as follows:

$$\frac{\text{SHIPSIM}}{Y \text{ (NEQ)}} = \frac{\text{OPTSIM}}{X \text{ (NEQ)}} = \begin{bmatrix} \frac{\mathbf{x}}{\hat{\mathbf{X}}} \text{ (NS)} \\ \frac{\hat{\mathbf{x}}}{\hat{\mathbf{X}}} \text{ (NE)} \\ \frac{\hat{\mathbf{x}}}{\hat{\mathbf{Y}}} \text{ (NA)} \end{bmatrix}$$

$$\text{YDOT (NEQ)} = \text{XDOT (NEQ)} = \begin{bmatrix} \frac{\mathbf{x}}{\hat{\mathbf{X}}} \text{ (NS)} \\ \frac{\hat{\mathbf{x}}}{\hat{\mathbf{X}}} \text{ (NE)} \\ \frac{\hat{\mathbf{x}}}{\hat{\mathbf{Y}}} \text{ (NA)} \end{bmatrix}$$
 calculated in ADERIV calculated in ADERIV

At each call from SHIPSIM, DERIV1 calls the user-supplied DISTRB subroutine to obtain the current values for the system disturbance vector $\underline{\mathbf{w}}$ (if NG \neq 0) and calls subroutine NOISE to obtain the measurement noise vector $\underline{\mathbf{v}}$. Subroutine NOISE calls RANDU to obtain a random number $0.\leq \text{YFL}\leq 1$. and then calls NDTRI to produce a random, normally distributed variable with zero mean and variance one. The standard deviation σ is then used to produce a random, normally distributed variable with zero mean and the desired variance. A new random number is generated for each element of $\underline{\mathbf{v}}$. With $\underline{\mathbf{w}}$ and $\underline{\mathbf{v}}$, the vector $\underline{\mathbf{b}}$ (NS+NE) in eq. (1) is then calculated within DERIV1. DERIV1 then premultiplies the first NS+NE element vector of X(NEQ) by the matrix A and adds this result to vector $\underline{\mathbf{b}}$ to form the first NS+NE elements of XDOT. DERIV1 finally calls the user-supplied subroutine ADERIV to obtain $\underline{\mathbf{v}}$ and these derivaties are loaded as the last NA elements of XDOT. The derivative vector XDOT is then returned to SHIPSIM.

II. COMMON Variables

The OPTSIM subroutines utilize two labeled COMMON blocks which are unique to these subroutines. These blocks appear as follows:

COMMON/ONE/SWITCH
COMMON/TWO/FS,FE,GS,GE,C,GAMMA,HS,HE,K,SIGMA

These COMMON variables have the following definitions:

- C feedback control gains matrix; dimension (8,10) with only (NCxNE) utilized.
- FE estimator open-loop dynamics matrix; dimension (10,10) with only (NEXNE) utilized; equals FS if NE=NS.

FS	system open-loop dynamics matrix; dimension (10,10) with only (NSxNS) utilized.
GAMMA	system disturbance distribution matrix; dimension (10,10) with only (NSxNG) utilized.
GE	estimator control distribution matrix; dimension (10,8) with only (NEXNC) utilized; equals GS if NE=NS.
GS	system control distribution matrix; dimension (10,8) with only (NSxNC) utilized.
HE	estimator measurement scaling matrix; dimension (10,10) with only (NOB,NE) utilized; equals HS if NE=NS.
HS	system measurement scaling matrix; dimension (10,10) with only (NOB,NS) utilized.
K	<pre>Kalman-Bucy filter gains matrix. Dimension (10,10) with only (NEXNOB) utilized.</pre>
SIGMA	Vector of standard deviations for zero mean measurement noise vector $\underline{\mathbf{v}}$ (NOB). Dimension (10) with only (NOB) utilized.
SWITCH	Input control <u>integer</u> . If SWITCH=1 all input data is read in INPUT1. If SWITCH=2 only changes to data are read in INPUT1 using a NAMELIST read where LIST1 is defined as:

NAMELIST/LIST1/FS,FE,GS,GE,C,GAMMA,HS,HE,K,SIGMA

III. SUBROUTINE Descriptions

The OPTSIM subroutines are described here in alphabetical order. The designation (I) after a subroutine argument signifies that the quantity is input to the subroutine; (O) signifies that the quantity is output of the subroutine.

1.	NAME:	ADERIV
	PURPOSE:	This subroutine calculates up to 5 additional time derivatives YDOT= $f(t,\underline{x},\underline{\hat{x}},\underline{y})$ which are to be integrated as part of the simulation but which are not in \underline{x} or $\underline{\hat{x}}$ in eqn. (1). This is a user-supplied subroutine as defined in the User's Documentation for OPTSIM. A dummy version without executable code is in file ADERIV.D to allow program loading without an MTS error message.
	CALLING SEQUENCE:	SHIPSIM, ENTRY, DERIV, ADERIV
	ARGUMENTS	TIME simulation independent variable (I) X NEQ vector of integrated dependent variables consisting of $\underline{x}(NS)$, $\hat{\underline{x}}(NE)$, and $\underline{y}(NA)$. (I) YDOT NA vector of additional derivatives (O) NA dimension of YDOT. (I)
		NEO dimension of X: NS+NE+NA (I)

SUBROUTINES CALLED: Defined by user.

COMMENTS: See User's Documentation for OPTSIM

2. NAME: ENTRY DERIV

PURPOSE: This entry point in SUBROUTINE DERIV1 calculates

and/or loads the vector of derivatives which are

integrated by SHIPSIM.

CALLING SEQUENCE: SHIPSIM, ENTRY DERIV

ARGUMENTS: TIME simulation independent variable. (I)

Y vector of integrated dependent variables consisting of $\underline{x}(NS)$, $\hat{\underline{x}}(NE)$, and $\underline{y}(NA)$; this is vector Y in SHIPSIM; dimension (25) with only (NEQ) utilized. (I)

XDOT vector of dependent variable first

derivatives with respect to TIME; this is vector YDOT in SHIPSIM; dimension (25)

with only (NEQ) utilized. (0)

SUBROUTINES CALLED: ADERIV, DISTRB, NOISE

COMMENTS: See Program Organization. See eqn. (1) for definition

of internal matrix A (20,20) and vector B (20). Only (NS+NE, NS+NE) of A and only (NS+NE) of B are utilized

in any particular run.

3. NAME: DERIVI

PURPOSE: This portion of SUBROUTINE DERIV1 obtains system,

controller, and estimator input from INPUT1 via COMMON/TWO/, initializes the random number seed XI for use in RANDU, and loads the matrix A in

eqn. (1).

CALLING SEQUENCE: SHIPSIM, INPUT, INPUT1, DERIV1

ARGUMENTS: NS dimension of state vector x (I)

NC dimension of control vector u. (I)

NOB dimension of measurements vector z. (I)

NG dimension of system disturbance vector w. (I)

NA dimension of additional variable vector y. (I)

NE dimension of estimate vector x. (I)

NSE NS+NE (I)

NEQ NS+NE+NA (I)

SUBROUTINES CALLED: none

COMMENTS: see ENTRY DERIV.

. NAME: DISTRB

PURPOSE: This subroutine calculates the system disturbance

vector w using current values of simulation indepen-

dent and dependent variables. This is a usersupplied subroutine as defined in the User's

Documentation for OPTSIM. A dummy version without

executable code is in file DISTRB.D to allow program

loading without an MTS error message.

CALLING SEQUENCE: SHIPSIM, ENTRY DERIV, DISTRB

ARGUMENTS: TIME simulation independent variable (I)

X NEQ vector of integrated dependent variables

consisting of $\hat{\mathbf{x}}(NS)$, $\mathbf{x}(NE)$, and $\mathbf{y}(NA)$. (I)

W NG vector of system disturbances w (0)

NG dimension of W (I)

NEQ dimension of X; NS+NE+NA (I)

SUBROUTINES CALLED: Defined by user.

COMMENTS: See User's Documentation for OPTSIM.

5. NAME: INPUT

PURPOSE: Reads and writes input verification for input control

integer SWITCH and problem dimensions NS, NC, NOB,

NG, NA, and NE.

CALLING SEQUENCE: SHIPSIM, INPUT

ARGUMENTS: NEQ dimension of integrated dependent variable

vector; NS+NE+NA (O)

* error return for END OF FILE on I/O device 5

or data input problem.

SUBROUTINES CALLED: INPUT1

COMMENTS: none

6. NAME: INPUT1

PURPOSE: Reads and writes input verification for matrices FS,

FE, GS, GE, C, GAMMA, HS, HE, K, and SIGMA. Loads these matrices into COMMON/TWO/. If NS=NE, the subroutine reads only FS, GS, C, GAMMA, HS, K and

SIGMA and sets FE=FS, GE=GS, and HE=HS.

CALLING SEQUENCE: SHIPSIM, INPUT, INPUT1

ARGUMENTS: NS dimension of state vector x (I)

NC dimension of control vector <u>u</u>. (I)

NOB dimension of measurements vector z. (I)

NG dimension of system disturbance vector $\underline{\mathbf{w}}$. (I)

NA dimension of additional variable vector y. (I)

NE dimension of estimate vector x̂. (I)

NSE NS+NE (I)

NEQ NS+NE+NA (I)

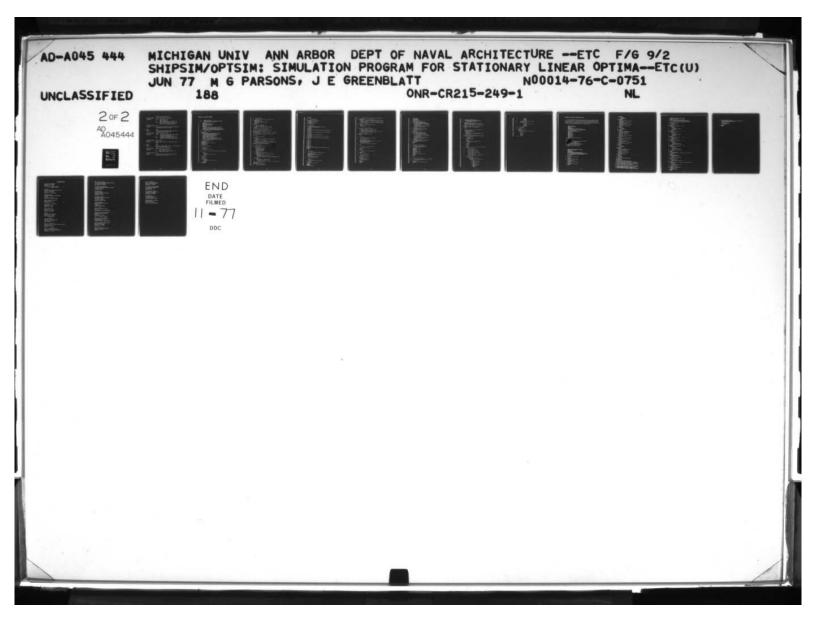
SUBROUTINES CALLED: DERIVI

COMMENTS: none

7. NAME: NDTRI

PURPOSE: Returns a zero mean, normally distributed variable

with variance one given O. < YFL < 1.0. IBM Scientific



Subroutine Package subroutine.

CALLING SEQUENCE: SHIPSIM, ENTRY DERIV, NOISE, NDTRI

ARGUMENTS: YFL input variable (I)

X output variable (0)

D output density F(x); not used here (0)

IER error code which equals 1 if YFL<0, or

YFL>1.; not used here since RANDU will

return YFL in the required range (0)

SUBROUTINES CALLED: none

COMMENTS: See IBM Scientific Subroutine Package documentation

for additional details and listing.

8. NAME: NOISE

PURPOSE: Calculates random measurement noise vector with

standard deviations given by SIGMA.

CALLING SEQUENCE: SHIPSIM, ENTRY DERIV, NOISE

ARGUMENTS: SIGMA NOB vector of measurement noise standard

deviations from zero mean (I)

V NOB vector of measurement noise (O)
NOB dimension of measurement vector (I)
IX integer seed for random number generator

(I)

SUBROUTINES CALLED: RANDU, NDTRI

COMMENTS: Updates integer seed IX to IY after each call to

RANDU.

9. NAME: RANDU

PURPOSE: Generates a random number 0.Generates Generates

Subroutine Package subroutine.

CALLING SEQUENCE: SHIPSIM, ENTRY DERIV, NOISE, RANDU

ARGUMENTS: IX input integer seed (I)

IY output integer seed for next call (0)

YFL random number 0. <YFL<1.0 (0)

SUBROUTINES CALLED: none

COMMENTS: See IBM Scientific Subroutine documentation for

additional details and listing.

Appendix F: Listing of SHIPSIM

```
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                                                                                  UNIVERSITY OF MICHIGAN
                                                                                       DEPARTMENT OF NAVAL ARCHITECTURE AND MARINE ENGINEERING CONTINUOUS SYSTEMS SIMULATION PROGRAM
                                                                   IMPLICIT REAL*8 (A-H,O-$)
                                                                  COMMON NEQ2
COMMON/OUTPUT/YLABLE, ZLABLE, TITLE
COMMON/COM1/CPRINT(9).IOUT, NAC
COMMON/COM2/CPLOT, PLY.PLZ, PLN
                                                                   INTEGER PRN.PLY.PRY.PLN.PLZ
LOGICAL TEST
                                                                    EXTERNAL DERIV
                                                             DIMENSION TF(5), METHOD(5), PRD(5), PLD(5), AB(5), EPS(5),

* NCUTS(5), Y(25), Z(5), Y0(25), FIRSTP(5), DY(25),

*YLABLE(25), TITLE(9), ZLABLE(5), CPLOT(9), PLY(9), PLZ(5)

DATA T,Y,Z/31*0./, METHOD/5*0/,AB,EPS/10*0./, NCUTS/6/,NEXT/4/

NAMELIST/DATA/TITLE, ZLABLE,Z,NAC,Y,TF,METHOD,PRD,PLD,AB,EPS,NCUTS

*, Y0,FIRSTP,NIS,SF,YTEST,YTERM,CPRINT,CPLOT,PLN,IOUT
                                                                                       FORMATTED DATA INPUT
                                      188 CONTINUE
WRITE (6, 2800)

2880 FORMAT('lUNIVERSITY OF MICHIGAN DEPARTMENT OF NAVAL',

* 'ARCHITECTURE AND MARINE ENGINEERING'/

* '8SHIPSIM CONTINUOUS SYSTEMS SIMULATION PROGRAM'/)

IF (NEXT :EQ. 4) CALL INPUT(NEQ2, 6999)

READ(4,120,ERR=800)NIS,NAC,IOUT.PLN.SF,TITLE

READ(4,121,ERR=810) (YLABLE[I), I=1, NEQ2)

READ(4,125,ERR=820) (Y0(I),I=1,NEQ2)

READ(4,126,ERR=830) YTEST, YTERM

IF (NAC.GT. 0) READ(4, 121, ERR=840) (ZLABLE(I), I=1, NAC)

IF(IOUT .EQ. 1) READ(4,122,ERR=850) CPRINT

IF (PLN .GT. 0) READ(4,128,ERR=860) (CPLOT(I), I=1,PLN)

READ(4,123,ERR=870) (METHOD(I),TF(I),FIRSTP(I),PRD(I),PLD(I),

* EPS(I),AB(I),NCUTS(I), I=1,NIS)
                                              100 CONTINUE
                                             120 FORMAT (415, D10.4/9A8)
121 FORMAT (8 (A8, 2X))
                                             122 FORMAT(9A8)
123 FORMAT(15,D10.2,D10.6,2D5.2,2D10.6,I5)
125 FORMAT(7D10.4)
                                             126 FORMAT (A8, D10.4)
128 FORMAT (7 (A8, 2X))
                                             130 CONTINUE
                                                                                ASSIGN INITIAL VALUES
                                              200 DO 250 I=1,NEQ2
                                                                             Y(I)=Y0(I)
IF(YLABLE(I) .EQ. YTEST) LY=I
                                              250 CONTINUE
   55
 56
57
58
59
60
61
62
63
64
65
66
67
71
72
73
74
75
                                                                                   CONSTRUCT PLY AND PLZ VECTORS (SUBSCRIPTS OF Y AND 2 TO BE PLOTTED).
                                                                     K=8
                                                                     DO 260 I=1.9
                                                                             PLY(I)=0
DO 255 J=1,NEQ2
                                                                                        IF (CPLOT(I) .NE. YLABLE(J)) GO TO 255
                                                                                         PLY (K) =J
                                                                             CONTINUE
                                                 260 CONTINUE
                                                                     K=0
DO 262 I=1,5
PLZ(I)=0
                                                262 CONTINUE
DO 270 I=1,PLN
DO 265 J=1,NAC
                                                                                       IF (CPLOT(I) .NE. ZLABLE(J)) GO TO 265
K=K+1
                                                PLZ(R)=J
265 CONTINUE
278 CONTINUE
```

```
INPUT VERIFICATION
 89
81
82
83
84
85
86
87
                  IF (NEXT .EQ. 2 .OR. NEXT .EQ. 5) CALL INPUT(NEQ2, £999)
WRITE(6,2840) TITLE
2848 FORMAT(1H-,9A8)
                    WRITE (6, 2003) (ZLABLE (I), Y0 (I), I=1, NEQ2)

IF (NAC .EQ. 0) GO TO 203

WRITE (6, 2002)

WRITE (6, 2003) (ZLABLE (I), I=1, NAC)

203 CONTINUE
 88
89
90
91
92
93
94
95
                    205 CONTINUE
                    218 IF (IOUT .EQ. 1 ) CALL PRINT
    IF (PN .GT. 0) CALL PLOT
    IF (IOUT .EQ. 1) WRITE(6,2010) CPRINT
    IF (IOUT .EQ. 2) WRITE(6,2010) (YLABLE(I). I=1,NEQ2)
                    215 CONTINUE
                    220 IF (PLN .GT. 0) WRITE(6,2020) (CPLOT(I), I=1,PLN) 225 CONTINUE
 96
98
99
100
                            IF (LY .GT. 0) WRITE(6,2030) YTEST, YTERM
                 101
103
184
105
106
107
                   300 CONTINUE
110
111
                                  INTEGRATION PARAMETER CHECK
113
114
115
116
                    330 WRITE (6,3030)
                            DO 332 I=1, NIS
IF (METHOD(I) .EQ. 1) WRITE(6,3032) I, TF(I), PRD(I), PLD(I),
117
                                FIRSTP(I)
118
119
120
121
122
                            IF (METHOD(I) .EQ. 2) WRITE(6.3034) I, TF(I), PRD(I), PLD(I),
    FIRSTP(I), EPS(I) AB(I), NCUTS(I)
                  123
124
125
126
127
128
129
                                  INTEGRATION CONTROL
                    IF(PLN .GT. 8) CALL PLOT1(T,Y8,NAC)
400 DO 420 I=1, NIS
CALL PRINT1(I,T,Y)
STEP=DMIN1(PRD(I), PLD(I))
130
131
132
133
134
135
                                   IF (LN .EQ. 0) STEP=PRD(I)
NST=(TF(I)-T+STEP/2.)/STEP
NPR=(PRD(I)+STEP/2.)/STEP
                                  NPL=(PLD(1)+STEP/2.)/STEP
IF (NPR .EQ. 0) NPR=1
IF (NPL .EQ. 0) NPL=1
136
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                    484
                                   CONTINUE
                                  CONTINUE

IF (METHOD(I) .EQ. 1) GO TO 410

CALL DFEQKD(0, T, FIRSTP(I), Y, DERIV, EPS(I). AB(I).

NCUTS(I). 6704, .FALSE.)

DO 406 J=1,NST

CALL DFEQKD(NEQ2, T, STEP, Y, DERIV, EPS(I). AB(I).

NCUTS(I).4704,.FALSE.)

IF (MOD(J,NPR) .EQ. 0) CALL PRINT2(T,Y)

IF (MOD(J,NPL) .EQ. 0 .AND. PLN .GT. 0) CALL PLOT1(T,Y,NAC)

IF (LY .GT. 0 .AND. MOD(J,NPR) .EQ. 0) CALL LIMIT(Y,Y0,YTERM,LY.6463)

CONTINUE
                    486
                                  CONTINUE
                          GO TO 468
DO 428 J=1,NST
                    418
                                        428 J=1,NST

CALL EULER(T,Y, STEP, FIRSTP(I), $738)

IF (MOD(J,NPR) .EQ. 8) CALL PRINT2(T,Y)

IF (MOD(J,NPL) .EQ. 8 .AND. PLN .GT. 8)

CALL PLOT1(T,Y,NAC)

IF (LY .GT. 8 .AND. MOD(J,NPR) .EQ. 8) CALL LIMIT(Y,Y8,YTERM,LY,$462)
152
153
154
155
156
157
                    419 IF (LY .GT. 0 .AND. MOD (J
420 CONTINUE
440 FORMAT(12/9A8/(8(A8,2X)))
450 FORMAT(5(D12.4,2X))
460 IF (PLN .GT. 0) CALL PLOT2(SF)
158
159
160
161
162
163
                c...
                                     RESET VARIABLES FOR NEXT RUN
```

```
164
165
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181
                 500 CONTINUE
                       T-8.
              c ...
                            INPUT OPTION SELECTION
                 688 READ(4,692,END=728,ERR=712) NEXT
682 FORMAT(11)
IF (NEXT .EQ. 5) GO TO 138
IP (NEXT .GT. 2) GO TO 188
685 CONTINUE
618 READ(4,DATA,ERR=716)
GO TO 288
             c . . .
                             ERROR MESSAGES
                 182
                       GO TO 600
 183
                 768 CONTINUE
184
                 GO TO 600
712 WRITE (6,714)
                 714 FORMAT (60H-*** DATA INPUT ERROR WHILE READING NEXT AT PROGRAM STEP *600 )
 186
187
 188
                       GO TO 999
189
190
191
                 716 WRITE (6,718)
718 FORMAT (57H-*** ERROR IN UNFORMATTED DATA INPUT AT PROGRAM STEP 618
                 *. )
GO TO 999
728 WRITE(6,722)
722 FORMAT(35H-*** END OF FILE ENCOUNTERED ON 4. )
192
193
194
195
                 GO TO 999
724 WRITE (6,726)
196
197
198
                 726 FORMAT (51H-*** ILLEGAL METHOD SPECIFICATION. RUN TERMINATED. )
GO TO 600
                 888 WRITE(6.881)
881 FORMAT(' *** DATA INPUT ERROR ON 4 WHILE READING RECORD TYPE 1')
GO TO 999
 199
208
 202
                 810 KC=3
283
                       GO TO 988
204
205
206
                820 KC=4
GO TO 900
830 KC=5
287
288
289
218
211
212
                 GO TO 900
840 KC=6
                848 KC=6
GO TO 988
858 KC=7
GO TO 988
868 KC=8
GO TO 988
878 KC=9
213
214
215
                988 WRITE(6,918) KC
918 FORMAT(' *** DATA INPUT ERROR ON 4 WHILE READING RECORD TYPE',14)
216
217
218
219
                      CONTINUE
               1000 CONTINUE
                       STOP
220
221
222
223
224
225
                       END
             c
                       SUBROUTINE PRINT
             c ...
                            THIS SUBROUTINE PRINTS THE INTEGRATION RESULTS.
226
227
228
229
230
231
                      IMPLICIT REAL*8 (A-H,Q-S)
IMPLICIT INTEGER (O-P)
DIMENSION PRY(9),TITLS(9),Y(25),YLABLE(25),
* Z(5),ZLABLE(5)
COMMON NEQ2
232
233
234
235
236
237
                       COMMON/OUTPUT/YLABLE, ZLABLE, TITLE
                       COMMON/COM1/CPRINT (9) , IOUT . NAC
             c ...
                             COMPUTE PRN AND LOAD PRY
                  DO 20 I=1,9
PRY(I)=3
DO 10 J=1,NEQ2
IF (CPRINT(I) .EQ. YLABLE(J)) PRY(I)=J
10 CONTINUE
20 CONTINUE
238
239
240
241
242
243
244
245
246
247
248
                  DO 36 PRN=1,9
IF (PRY(PRN) .EQ. 8) GO TO 40
36 CONTINUE
PRN=18
46 PRN=PRN=1
                       RETURN
                 166 ENTRY PRINTI(IS.T.Y)
249
```

```
250
251
252
253
254
255
256
257
258
259
260
261
262
263
264
265
                              PRINT INTEGRATION SEGMENT NUMBER AND LABELS FOR OUTPUT VECTOR
                 WRITE (6,105) IS

105 FORMAT (1H4,3X,'* * * INTEGRATION SEGMENT ',11)

IF (IOUT .EQ. 1 .AND. NAC .EQ. 0) WRITE (6,110) (CPRINT(I), I=1,PRN)

IF (IOUT .EQ. 1 .AND. NAC .GT. 0) WRITE (6,110) (CPRINT(I), I=1,PRN),

* (ZLABLE(I), I=1,NAC)

IF (IOUT .EQ. 2 .AND. NAC .EQ. 0) WRITE (6,115) (YLABLE(K),K=1,NEQ2)

IF (IOUT .EQ. 2 .AND. NAC .GT. 0) WRITE (6.115) (YLABLE(K),K=1,NEQ2),

* (ZLABLE(L),L=1,NAC)
                  110 FORMAT('0 TIME',6x,9(A8,4x)/1H)
115 FORMAT('0THE OUTPUT VECTOR IS:', (T25,5(A8,2x)))
GO TO 120
                         ENTRY PRINT2 (T,Y)
              c...
266
267
                              PRINT VALUES FOR T. Y. AND Z
 268
269
278
271
272
                 " (Y(PRY(K)),K=1,PRN)
IF (IOUT .EQ. 1 .AND. NAC .GT. 0) WRITE (6,125) T,

" (Y(PRY(K)),K=1,PRN), (Z(K),K=1,NAC)
IF (IOUT .EQ. 2 .AND. NAC .EQ. 0) WRITE (6,130) T, (Y(K),K=1,NEQ2)
IF (IOUT .EQ. 2 .AND. NAC .GT. 0) WRITE (6,130) T,

" (Y(K),K=1,NEQ2), (Z(L),L=1,NAC)
273
274
275
276
277
278
279
280
                 125 FORMAT(1H .10(D10.4.2X))
130 FORMAT('0T= ',D10.4,(T25,5(D10.4,2X)))
                  999 RETURN
281
                          END
282
283
              CC
284
                        SUBROUTINE PLOT
             c . . . c c c
285
286
                              THIS SUBROUTINE GENERATES A PLOTFILE FOR MTS
287
                              GRAPHIC POST PROCESSING.
288
289
                        IMPLICIT INTEGER (O-P)
REAL*8 T,Y,YLABLE,CPLOT,ZLABLE,Z
290
                        DIMENSION CPLOT(9), PLY(9), PLZ(5), TITL(18), TP(300), Y(25), YLA(2), YLAB(50), ZLAB(10), YPLOT(2700), Z(5)

COMMON/OUTPUT/YLAB, ZLAB, TITL
291
292
293
294
295
                        COMMON/COM2/CPLOT.PLY.PLZ.PLN
              c...
296
                              INITIALIZE PLOT VECTOR (TP AND YPLOT) SUBSCRIPTS
297
298
                        LP=Ø
299
                        MP=0
300
                             COUNT NUMBER OF Z ELEMENTS TO BE PLOTTED
302
303
                        DO 125 PLNZ=1,5
                              IF (PLZ(PLNZ) .EQ. 0) GO TO 130
3Ø5
3Ø6
                  125 CONTINUE
                         PLNZ=6
307
                  130 PLNZ=PLNZ-1
              c . . . c
308
309
                              COMPUTE NUMBER OF Y ELEMENTS TO BE PLOTTED
311
312
313
                        PLNY=PLN-PLNZ
                        RETURN
ENTRY PLOTI (T,Y,NAC)
314
                              LOAD TP AND YPLOT VECTORS
                         317
318
319
                  140 CONTINUE
 320
                         LP=LP+PLNY
                        IF (PLNZ .EQ. 8) GO TO 158

CALL ACALC(T,Y,Z,NAC)

DO 158 K=1,PLNZ

YPLOT(LP+K)=SNGL(Z(PLZ(K)))
 322
 323
325
                  158 CONTINUE
                         LP=LP+PLNZ
MP=MP+1
 328
                         TP (MP) = SNGL (T)
                          RETURN
```

```
ENTRY PLOT2 (SF)
                           CALL PLTSIS(SF)
CALL PLTXMX(10.75)
CALL PXMARG(0.25)
333
334
                            DO 200 K=1, PLNY
PLOT IN LINEAR-RECTANGULAR COORDINATES
 335
336
337
                           DEFINE X AND Y AXES AND GRID

CALL PSCALE (10.,0.5, XMIN,DX,TP(1),MP,1)

CALL PSCALE (7.50,0.5, YMIN,DY,YPLOT(K),MP,PLN)

CALL PAXIS (.75,.75, 'TIME',-4.10..0, XMIN,DX,1.9)

YLA (1)=YLAB (2*PLY(K)-1)

YLA (2)=YLAB (2*PLY(K))
338
339
340
341
342
343
344
345
346
                                 CALL PAXIS (.75, .75, YLA(1), 8,7.5,90., YMIN, DY, 1.0)
                                 CALL PGRID(.75,.75,.25,.25,40,30)
CALL PLTOFS (XMIN,DX,YMIN,DY,.75,.75)
                                  CALL PLTREC
               C... DRAW CURVE
CALL PLIN2(TP(1),YPLOT(K),MP,1,PLN,8,9,1)
C... PRINT USER SUPPLIED TITLE
CALL PSYMB(.75,8.9,.125,TITL(1),8.,72)
CALL PLIEND
348
349
350
351
 352
353
                    299 CONTINUE
354
355
                           IF (PLNZ .EQ. 0) GO TO 300
DO 300 K=1,PLNZ
356
357
                           PLOT IN LINEAR-RECTANGULAR COORDINATES
               C... DEFINE X AND Y AXES AND GRID

CALL PSCALE (10..0.5, XMIN.DX.TP(1), MP,1)

CALL PSCALE (7.56,0.5, YMIN.DY, YPLOT (PLNY+K),
358
 359
                                 MP, PLN)

CALL PAXIS (.75, .75, 'TIME', -4, 10., 0., XMIN, DX, 1.0)

YLA (1) = ZLAB (2*PLZ (K) -1)
368
 361
 362
                                YLA(1)=ZLAB(2*PLZ(K))

CALL PAXIS(.75,.75,YLA(1),8,7.5,98.,YMIN,DY,1.8)

CALL PGRID(.75,.75,.25,.25,48,38)

CALL PLTOFS(XMIN,DX,YMIN,DY,.75,.75)

CALL PLTREC
363
364
 365
366
367
 368
               C... DRAW CURVE
               CALL PLIN2(TP(1),YPLOT(PLNY+K),MP,1,PLN,8,8,1)

C... PRINT USER SUPPLIED TITLE

CALL PSYMB(.75,8.8,.125,TITL(1),8.,72)

CALL PLTEND
369
370
372
373
                   388 CONTINUE
374
375
                           RETURN
                           END
376
377
378
379
               CC
                           SUBROUTINE EULER (X.Y.STEP, FIRSTP, *)
               c
380
               c ...
                           ... INTEGRATES Y(X) FROM X TO X+STEP USING
381
382
383
384
385
386
387
388
389
390
391
                                 RECTANGULAR (EULER) INTEGRATION.
                           IMPLICIT REAL*8 (A-H.O-$)
                           LOGICAL TEST
COMMON NEQ2
DIMENSION Y(25), YDOT(25)
                     FINAL=X+STEP
10 CONTINUE
                           CALL DERIV(X, Y, YDOT)
DO 20 I=1, NEQ2
Y(I)=Y(I)+YDOT(I)*FIRSTP
392
393
394
395
396
397
398
399
400
                      26 CONTINUE
                           X=X+FIRSTP
IF (TEST(X, FINAL, FIRSTP/2.)) GO TO 30
GO TO 10
                     30 CONTINUE
RETURN
               CC
461
462
463
                           LOGICAL FUNCTION TEST(A, B, TOL)
               c...
                           ...TESTS FOR EQUALITY OF DOUBLE PRECISION REAL VARIABLES WITHIN SPECIFIED TOLERANCE "TOL"
484
486
487
488
                           TEST=.FALSE.

IF (DABS(A-B) .LT. DABS(TOL)) TEST =.TRUE.
RETURN
                            END
```

```
CC
412
413
414
415
416
417
418
419
428
                           SUBROUTINE LIMIT(Y,Y0,YTERM,LY,*)
...THIS ROUTINE TERMINATES THE RUN IF THE VALUE OF
A SPECIFIED ELEMENT OF Y CROSSES YTERM.
                                       YTERM=LIMITING VALUE OF Y(LY)
                           IMPLICIT REAL*8 (A-H.O-S)
                           DIMENSION Y (25) , YLABLE (25) , Y0 (25) . ZLABLE (5) . TITLE (9)
                           COMMON/OUTPUT/YLABLE, ZLABLE, TITLE

IF (Y(LY) .GE. YTERM .AND. Y0(LY) .LE. YTERM) GO TO 100

IF (Y(LY) .LE. YTERM .AND. Y0(LY) .GE. YTERM) GO TO 100
421
422
423
424
                            RETURN
                   100 WRITE(6,200) YLABLE(LY), YTERM
200 FORMAT('-*** VALUE OF ',A8,' HAS REACHED THE LIMITING',

* 'VALUE OF ',D15.6/' *** RUN TERMINATED. ')
425
426
427
                           RETURN 1
428
               CC
438
431
432
433
                           SUBROUTINE DFEQKD(NEQ,X,STEP,Y,F,EPS,AB,NCUTS,*,STPSZ)
IMPLICIT REAL*8 (A-H.O-$)
INTEGER NEQ, NCUTS
REAL*8 X,STEP,Y(3),F,EPS,AB,YY(3)
EXTERNAL F
434
435
                    INTEGER I, CUT
LOGICAL DBL

50 FORMAT (' THE STEPSIZE HAS BEEN HALVED ',13,' TIMES')
IF (NEQ.NE.0) GO TO 10
HC = STEP
RETURN

16 IF (STEP.EO.8)
                           LOGICAL STPSZ

REAL*8 HC/0.0D0/,FINAL,H2,H3,H6,H8,ERR,TEST,T,H,EPSL,TEMP

REAL*8 Y1 (30),Y2 (30),F0 (30),F1 (30),F2 (30)
436
437
438
439
448
441
442
443
444
445
                                   IF(STEP.EQ.0) RETURN
IF(HC.EQ.0) HC = STEP
447
448
                                   FINAL = X+STEP
449
450
451
                                   H = STEP
                                   EPSL = EPS

IF(EPS.EQ.0 .OR.DABS(H) .LE.DABS(HC)) GO TO 15

IF(H*HC.LE.0) HC = -HC
453
                                            H = HC
                     15
                                   T = X+H
                                   CUT = NCUTS
X = FINAL
H2 = H/2.
456
                                   H3 = H/3.

H6 = H/6.
459
                                   H8 = H/8.
461
462
                     20
                                   IF (H.GT.0 .AND. T.GT.FINAL .OR. H.LT.0 .AND. T.LT.FINAL)
                                   GO TO 40
CALL F(T-H,Y,FØ,H,T-H,Y)
                        C
463
464
465
                     21
                                             DO 22 I = 1,NEQ
Y1(I) = FØ(I)*H3+Y(I)
CALL F(T-2.*H3,Y1,F1,H,T-H,Y)
                     22
                                  467
                     23
469
472
473
475
476
                     26
478
479
481
482
483
484
485
486
487
488
489
                                                       IP(ERR.LE.TEST .OR. ERR.LT.AB) GO TO 34
                                                                H = H2
T = T-H2
                                                                T = T-B2

IF (.NOT.STPS2) GO TO 30

TEMP = T-H2

WRITE (6,52) H, TEMP

CUT = CUT - 1

IF (CUT.GE. 0) GO TO 31

X = T - H2

WRITE (6,62) NCUTS

RETURN 1

IF (T+H.ME.T) GO TO 33
                      30
491
492
493
                                                                 IF (T+H.NE.T) GO TO 33

X = T

RETURN 1
                      31
```

Appendix G: Listing of OPTSIM Subroutines

SUBROUTINE INPUT (NEQ, *

The two IBM Scientific Subroutine Package subroutines RANDU and NDTRI are not included here. See IBM documentation for source code listings for these subroutines. Requirements for the two user-supplied subroutines are included in the User's Documentation for OPTSIM. The source code listing of the four remaining OPTSIM subroutines are included here.

```
SUBROUTINE INPUT(NEQ,")
IMPLICIT REAL*8 (A-H,O-$)
REAL*8 K
INTEGER SWITCH
COMMON/ONE/SWITCH
COMMON/TWO/FS,FE,GS,GE,C,GAMMA,HS,HE,K,SIGMA
DIMENSION FS(10,10),FE(13,10),GS(10,8),GE(10,8),C(8,10
GAMMA(10,10),K(10,10),HS(10,10),HE(10,10),SI
PRAD(5,140,FM)FS(4),SWITCH
                READ(5,100,END=500) SWITCH
IF (SWITCH.EQ.2) GO TO 10
                READ (5,110,END=500) NS,NC,NOB,NG,NA,NE
                NEQ=NS+NE+NA
               MEQ=NS+NE+NA
WRITE (6,201)
WRITE (6,210) NEQ
WRITE (6,220) NS
WRITE (6,230) NC
WRITE (6,230) NG
WRITE (6,250) NG
WRITE (6,250) NG
WRITE (6,270) NE
NSE=NS+NE
   10
                CALL INPUT! (NS, NC, NOB, NG, NA, NE, NSE, NEQ)
                WRITE (6.280)
   500
                REPURN1
                       MAT (13)
                          AT (613)
AT (100PTSIM OPTIMAL STOCHASTIC CONTROLLER SIMULATION
AT (100PTSIM OPTIMAL STOCHASTIC CONTROLLER SIMULATION NEO = 1.13)
   110
                AT('SOPTSIM OPTIMAL STOCHASTIC CONTROLLER S:
AT('SINPUT VERIFICATION NEO =',13)
AT('SONDER OF SYSTEM =',13)
AT('SOUMBER OF CONTROLS =',13)
CHART('SOUMBER OF OBSERVATIONS =',13)
FORMAT('SOUMBER OF PROCESS NOISE SOURCES =',13)
FORMAT('SONDER OF AUXILIARY STATES =',13)
FORMAT('GORDER OF ESTIMATOR =',13)
FORMAT('GEND OF FILE OR DATA ERROR')
END
   280
              SUBROUTIBE IMPUT 1 (MS, MC, MOB, MG, MA, ME, MSE, MEQ)
              IMPLICIT REAL+8 (A-B,C-S)
               INTEGER SUITCH
             INTEGER SWITCH
COMMON/ONE/SWITCH
COMMON/THO/PS, PE, GS, GE, C, GAMMA, MS, ME, K, SIGMA
DIRENSION PS (10, 10), PE (10, 10), GS (10, 8), GE (10, 8), C (8, 10),
GAMMA (10, 10), MS (10, 10), HE (10, 10), K (10, 10), SIGMA (10)
MASELIST/LIST1/PS, PE, GS, GE, C, GAMMA, MS, HE, K, SIGMA
GO TO (10, 160), SWITCH
WRITE (6, 200)
CALL ZIIT
DO 20 I=1. MS
             DO 20 I=1, NS
READ (5,100) (FS(I,J),J=1,NS)
              WEITE (6,201)
DO 25 I=1,85
WEITE (6,101) (PS (I,J),J=1,85)
              CONTINUE
            30
                   WPITE (6, 101) (PE (I,J) ,J=1,BE)
            CONTINUE
```

```
CONTINUE

00 40 1-1, MS

00 50 3-1, MS

FE (I,J) =PS (I,J)

CONTINUE
    ..
    50
60
70
                  CORLIERS
                  CONTINUE
                 CONTINUE

READ (5,100) ((GS(I,J),J=1,HC),I=1,HS)

WRITE(6,203)

DO 73 I=1,HS

WRITE(6,101) (GS(I,J),J=1,HC)
                  CONTINGE
                 TP (MS.EQ.ME) GO TO 80

READ (5,100) ((GE(I,J),J=1,MC),I=1,ME)

WRITE(6,204)

DO 76 I=1,ME

WRITE(6,101) (GE(I,J),J=1,MC)
   76
                 CONTINUE
                 GO TO 110
    80
                 CONTINUE
                 DO 104 I=1, NB
DO 90 J=1,NC
GE(I,J)=GS(I,J)
                          CONTINUE
                CONTINUE
               CONTINUE

CONTINUE

READ (5,100) ((C(I,J),J=1,NE),I=1,NC)

IP (NS.NE.NE) WRITE(6,205)

IP (NS.EQ.NE) WRITE(6,206)

DO 112 I=1,NC

WRITE(6,101) (C(I,J),J=1,NE)
                IF (NG.EQ.0) GO TO 115

READ (5,100) ((GAEMA(I,J),J=1,NG),I=1,NS)

WRITE(6,207)

DO 114 I=1,NS
                         WRITE (6, 101) (GAMMA (I,J) ,J=1, HG)
                CONTINUE
                CONTINUE
                READ (5,100) ((HS(I,J),J=1,HS),I=1,HOB)
WPITE(6,200)
DO 116 I=1,MOB
WRITE(6,101) (HS(I,J),J=1,HS)
                CONTINUE
                IF (NS.EQ.NE) GO TO 120
READ (5,100) ((HE(I,J),J=1,HE),I=1,HOB)
WRITE(6,209)
                DO 118 I=1, HOB
WRITE (6,101) (HE (I,J),J=1,HE)
  118
               CONTINUE
               GO TO 150
CONTINUE
                DO 140 I=1, WOB
DO 130 J=1, MS
HE (I,J) =HS (I,J)
                        CONTINUE
               CONTINUE
  150
                CONTINUE
               TREAD (5,100) ((K(I,J),J=1,N0B),I=1,NE)

IF (NS.NE.NE) WRITE(6,210)

IF (NS.EQ.NE) WRITE(6,211)

DO 153 I=1,NE

WRITE(6,101) (K(I,J),J=1,N0B)
              WRITE(6,100) (SIGHA(I),I=1,HOB)
WRITE(6,212)
DO 156 I=1,HOB
WRITE(6,101) SIGHA(I)
 153
               WRITE (6, 102)
GO TO 170
               READ (5, LIST1)
WRITE (6, LIST1)
WRITE (6, 102)
               CALL DERIVI (#S. MC. MOB, MG, MA, ME, MSE, MEQ)
 170
             PETURN

FORMAT (6212.5)

FORMAT (6212.5)

FORMAT (*0')

FORMAT (*CESTIFATOR OPER LOOP DYNAMICS MATRIX....FS (#S, #S)',//)

FORMAT (*CESTIFATOR OPER LOOP DYNAMICS MATRIX....FE (#L, #Z)',//)

FORMAT (*CESTIFATOR CONTROL DISTRIBUTION MATRIX....GS (#S, #C)',//)

FORMAT (*OFFIDMACK CONTROL GAINS....C (#C, #Z)',//)

FORMAT (*OFFIDMACK CONTROL GAINS....C (#C, #S)',//)

FORMAT (*OSYSTZM DISTURBBANCE DISTRIBUTION MATRIX....GAMMA (#S, #G)',

**//)
                PETURN
 101
 200
201
203
 200
          PORRAY ("OSISTED DISTORBRECK CALING MATRIX...RS (NOB, MS) ",//)
PORRAY ("CESTIMATOR MEASUREMENT SCALING MATRIX...RE (NOB, ME) ",//)
PORRAY ("CESTIMATOR MEASUREMENT SCALING MATRIX...RE (NOB, ME) ",//)
PORRAY ("CRALMAN-NOCY FILTER GAIRS...R (NE, NOB) ",//)
228
```

```
SUBROUTINE DERIVY(US, NC, NOB, NG, NA, NE, NSE, NEQ)
ISPLICIT REAL+8 (A-H, O-$)
         TEAL'S K

COHMON'THO/PS, PE, GS, GE, C, GAHHA, HS, HE, K, SIGHA

DIHERSION FS (10, 10), FE (10, 10), GS (10,8), GE (10,8), C (8,10),

GAMMA (10, 10), HS (10, 10), HE (10, 10), K (10, 10), SIGHA (10),

W (10), V (10), A (20,20), B (20), I (25), XDDT (25), IDDT (5)
TX = 1001

C ***** PUT PS IN PARTITION 1 OF A

DO 20 I=1,MS

DO 10 J=1,MS
              A(I,J)=PS(I,J)
CONTINUE
10
20 CONTINUE
C ***** PUT +GS*C IN PARTITION 2 OF A
                                                                              *****
         DO 50 I=1, MS
DO 40 J=1, ME
                    SUN=0.
                    DO 30 JE=1, MC
SUM=SUM+GS(I,JM) *C(JM,J)
                    CONTINUE
30
                     A (I, J+NS) = SUM
               CONTINUE
          CONTINUE
         DO 80 I=1, ME
DO 70 J=1, MS
SUM=0.
DO 60 IP=1, MOB
SU3=SUM+K(I,IP) *HS(IP,J)
CONTINUE
C ****
                    CONTINUE
60
                     A (I+NS, J) = SUM
70
               CONTINUE
         CONTINUE
80
               PUT PE IN PARTITION 4 OF A
         DO 103 I=1, HE
DO 90 J=1, HE
A (I+HS, J+HS) =FE (I, J)
CONTINUE
 100 CONTINUE
    ***** PUT +GE*C IN PARTITION 4 OF A
                                                                              ****
         DO 130 I=1,NE
DO 120 J=1,NE
                    SUB=0.
DO 117 JM=1, MC
SUB=SUB+GE(I,JE)+C(JB,J)
110
                    A (I+N5, J+NS) = A (I+NS, J+NS) +SUB
120
               CONTINUE
130 CONTINUE
C ***** PUT
               PUT -K+HE IN PARTITION 4 OF A
                                                                               ****
         DO 160 I=1, NE
              DO 150 J=1, HE
SJH=0.
DO 140 IP=1, HOB
                    SUM=SUM+K(I,IP) *HE(IP,J)
CONTINUE
140
                     A (I+MS, J+MS) = A (I+MS, J+MS) - SUM
               CONTINUE
150
          CONTINUE
 160
          RETURN
         ENTRY DERIV(IIEZ,I,IDOT)

CALCULATE B VECTOR

DO 170 I=1,85E

B(I)=0.

CONTINUE
C
         CONTINUE
1F (MG.EQ.C) GO TO 190
CALL DISTRB(TIME,X,W,MG,MEQ)
DO 190 I=1,MS
DO 180 JQ=1,MG
B(I)=3(I)+GASHA(I,JQ)*W(JQ)
               SURITEOS
190 CONTINUE
         CONTINUE
CALL NOISE (SIGHA, V, NOP, IX)
DO 210 I=1, NE
DO 200 JP=1, NOB
B (I+HS) = B (I+HS) + K (I, JP) + V (JP)
               CONTINUE
200
        CONTINUE
          DO 230 I = 1, MSE

NDOT (I) = 0.

DO 220 J= 1, MSE

XDOT (I) = XDOT (I) + A (I, J) = I (J)
 220
                CONTINUE
          CONTINUE
          TF (M. EQ. 0) GO TO 235
CALL ADERIT(THE, I, TDOT, MA, FEQ)
CONTROT
DO 240 1-1, MA
IDOT(I+HSE)-TBOT(I)
 240
          CONTINUE
          RETURN
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