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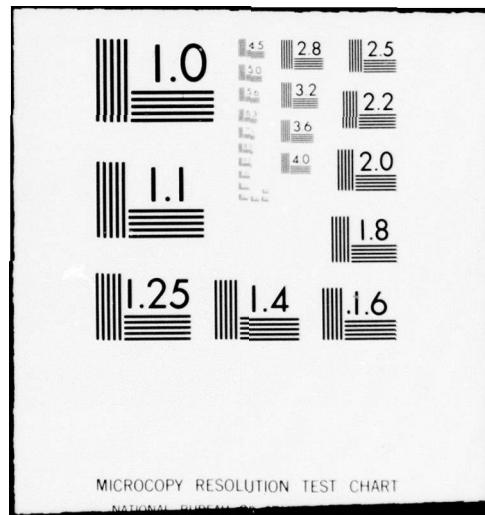
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Geometric Performance of Pseudoranging Navigation Satellite Systems: A Computer Program

Jeannine V. Lamar, L. N. Rowell, J. J. Mate

A Project AIR FORCE report
prepared for the
United States Air Force



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Describes a computer program designed to analyze many aspects of the geometric performance of pseudoranging navigation satellite (navsat) systems for users either on earth or in earth orbit. A navsat system includes a fleet of satellites, each with an accurate clock that transmits ephemeris, time, and other signals. These signals can be received by relatively small, inexpensive equipment, thus enabling the user to compute his position and time accurately. The NAVSTAR/Global Positioning System (GPS) is such a system, and its overall user accuracy can be broken down into two components which, when multiplied together, yield an estimate of the user's position and/or time accuracy. These two components are analyzed in this report; the first depends on the relative geometry among the navsats being employed and the user's location, and the second involves a determination of system errors. This report was performed as part of a Project AIR FORCE study entitled "Space Warfare Issues," and should be of use to military and civilian defense analysts responsible for the design, use, and survivability of GPS and other U.S. space-related systems. Refs. (Hx)

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PREFACE

This report describes a computer program designed to analyze many aspects of the geometric performance of pseudoranging* navigation satellite (navsat) systems for users either on earth or in earth orbit. A navsat system includes a fleet of satellites, each with an accurate clock, which transmits ephemeris, time, and other signals. These signals can be received by relatively small, inexpensive equipment, thus enabling the user to compute his position and time accurately. The NAVSTAR/Global Positioning System (GPS) currently under development is such a system. The overall user accuracy of such a system can be broken into two components which, when multiplied together, yield an estimate of the user's position and/or time accuracy. The first component, addressed in this report, depends on the relative geometry among the navsats being employed and the user's location. The second involves "system" errors, such as the accuracy of the ephemeris data of the navsats, propagation effects, clock accuracies, etc. Convenient computer analysis of the geometric performance aspect is important in addressing questions of alternative orbital configurations for the navsats and the degradation of performance due to failure or destruction of some or many of them.

The impetus for this research came from Lieutenant Colonel Frank A. Paparozzi, Directorate of Space, Hq USAF (AF/RDSA), who requested an analysis of the utility and feasibility of NAVSTAR/GPS navigation support to high-altitude satellites, for which GPS was not designed.

The research formed as a part of a Project AIR FORCE (formerly Project study entitled "Space Warfare Issues." It should be of use to military and civilian defense analysts responsible for the design, use, and survivability of GPS and other U.S. space-related systems. Additional Project AIR FORCE research is in progress to analyze GPS Phase III design features needed to support high-altitude space navigation and user equipment, as well as performance, applications, utility, survivability, and alternatives.

* Ideally, pseudoranging is a one-way measurement of the true range plus the user's unknown time offset with respect to a master reference.

SUMMARY

This report presents a discussion of pseudoranging navigation satellite (navsat) systems (such as the NAVSTAR/Global Positioning System (GPS) satellite system), of Geometric Dilution of Precision (GDOP), and other geometry-related performance parameters, and a computer program which computes them. Included are satellite selection algorithms which were developed to minimize the computational effort required to obtain the best (or nearly best) set of four required satellites for computing the GDOP for either a satellite-based or earth-based user.

A computer program for earth-based users, developed by the Aerospace Corporation, was acquired and extensively modified. Subject to certain constraints, the original program computed the number of navigation satellites within view of a user at any location, selected the set of four of those within view which would minimize navigation errors, and computed the various values of GDOP--namely, the three-dimensional position error, the horizontal position error, the altitude error, and the time error.

At Rand, the program was modified, extended to accommodate users in any earth orbit, and optimized. Further, facilities were added to give the user convenient and powerful input and output control. In short, the program described here is a flexible "production" program.

In addition to the computation of navigation satellite coverage available to any user and the optimum values of GDOP, the Rand program also includes a feature which permits the variation of the navsat antenna beamwidth and determines the effect of this variation on navigational accuracy for satellite users. There are no restrictions on the shape or size of the orbits of either the navigation satellites or the user satellite.

The computer program is written in FORTRAN IV and has been implemented on an IBM 370/158 computer at Rand. Included in this report are: a program listing, an explanation of the variables, a discussion of the operation of the program, and sample results.

ACKNOWLEDGMENTS

The authors wish to acknowledge the cooperation and assistance of A. Bogen and Paul Jorgenson of the Aerospace Corporation, and of Major Gaylord Green and Captain D. A. Flattery of the Space and Missile Systems Organization (SAMSO/YE). Also appreciated are the reviews of this report and helpful suggestions by Mario Juncosa and Richard Frick of The Rand Corporation.

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CONTENTS

PREFACE.....	iii
SUMMARY.....	v
ACKNOWLEDGMENTS.....	vii
I. INTRODUCTION.....	1
II. DISCUSSION.....	7
Navigation Satellite Deployments.....	7
User Locations.....	7
Navigation Satellite Visibility.....	8
User Position Accuracy.....	8
Satellite Selection.....	12
III. COMPUTER PROGRAM OPERATION.....	15
Table 1: Explanation of Variables in Main Program.....	19
Table 2: Explanation of Variables and Calling Sequences of Subroutines.....	23
Table 3: Input Card Setup.....	28
Table 4: Computing Costs (IBM 370/158 Computer).....	30
IV. PROGRAM INPUT AND OUTPUT.....	31
Table 5: Example Data Set for Case I.....	32
Table 6: Example Data Set for Case II.....	37
Table 7: Example Data Set for Case III.....	44
APPENDIX A: NAVSAT SELECTION ALGORITHMS FOR A SATELLITE USER....	56
APPENDIX B: PROGRAM LISTING.....	64
REFERENCES.....	92

I. INTRODUCTION

Pseudoranging navigation satellite systems transmit one-way signals of their ephemeris, time (based on highly accurate and stable onboard clocks that are periodically calibrated by ground command), and other signals that allow a user with fairly simple, lightweight equipment to accurately determine his position, velocity, and time. Such a system, called the NAVSTAR/Global Positioning System (GPS), is being developed by the military services at the Air Force Systems Command Space and Missile Systems Organization. The GPS will eventually consist of 24 satellites with the following configuration:^{*} three orbit planes inclined 63 deg and separated by 120 deg in longitude; eight satellites uniformly distributed in each plane in circular orbits at about 10,900 n mi altitude (12 hr period). (See Fig. 1.) The system is being designed to provide continuous global navigation to terrestrial or near-earth users with accuracies on the order of tens of feet. With modifications, the system could provide high-altitude satellites (above 8000 n mi) with real time navigation support. This navigation support could effect future satellite designs and operations, tracking, telemetry, command and control, and many other space applications.

This report documents a computer program which simulates the orbital motion of a system of pseudoranging navigation satellites (navsats) and the motion of earth-based users or a satellite-based user.^{**} The program computes the number of navigational satellites within view of the user and the Geometric Dilution of Precision (GDOP) values which are dependent primarily on the user/satellite geometry.

The position accuracy provided by such systems can be conveniently divided into two multiplicative factors--GDOP and other "system" errors. The "system" errors depend on the accuracy of the ephemeris data and time transmitted by the navigation satellites, ionospheric and atmospheric effects, and various mechanization, electronic, and processing

^{*} The GPS Joint Program Office is considering alternative orbital configurations.

^{**} Ballistic missiles can be treated as satellites with orbital perigees less than earth radius.

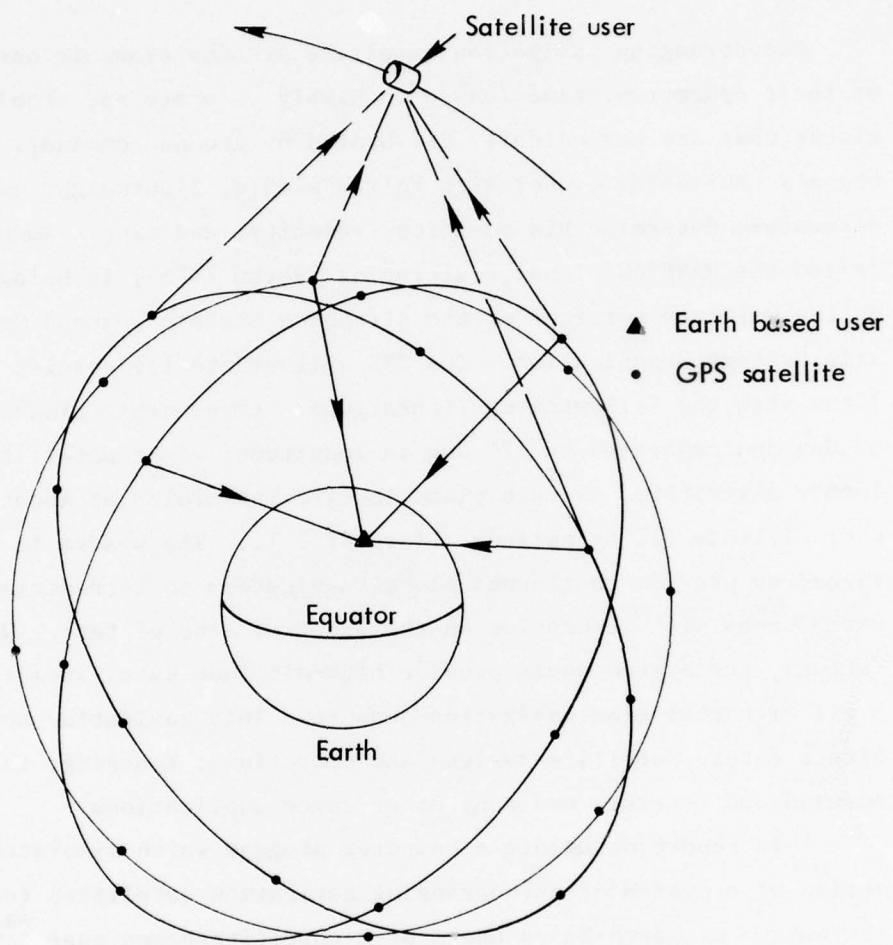


Fig. 1—Typical configuration of GPS satellites and GPS users

errors in the navigation satellite and user equipments. Since the GDOP factors depend predominantly on the user/navigation satellite geometries, they can be analyzed independently of system errors, which depend on cost, technology, and effort. This allows separate analyses of alternative orbital configurations, user motion, and the loss of some of the navigation satellites by interference or negation.

The original computer program was based on the analyses contained in Ref. 1 and was designed with GPS in mind. Both the referenced report and the original computer program were written by A. Bogen of the Aerospace Corporation. The original program was designed to compute the number of NAVSTAR/GPS satellites available to an earth-based user (or users) and the various GDOP values at specified times. It was written so that the set of navigational satellites can be changed simply by changing the initial orbital elements of each satellite. Satellite motion is assumed to be Keplerian, i.e., all perturbing forces are neglected. Both satellite coverage and GDOP values could be determined for a single earth-based user located at any latitude and longitude or on a global basis, which involved an assumed uniform distribution of earth-based users.

At Rand, the original program has been extensively modified and extended to permit the simulation of a satellite-based user and any orbital configuration of navsats. There are no restrictions on a satellite user's orbit. It can be circular or elliptical and can be entirely above or below the altitude of the navsats, or both above and below (e.g., highly elliptic orbits).

The modifications to the original program to accommodate a satellite user include algorithms which remove unneeded navigation satellites that are in view of the satellite user in order to decrease the amount of computation.

A user position fix requires a determination of four unknowns: three components of position plus time, thus requiring pseudoranging information from at least four navigation satellites.^{**} Since the GDOP

^{*} Some combinations of satellite user orbit and navsat orbit configuration are more expensive to run than others; this will be explained later.

^{**} The inclusion of an explicit time calculation reduces the accuracy and stability requirements for the user's clock, thereby making the user equipment simpler, smaller, lighter, more rugged, and cheaper.

values vary primarily with the relative geometry of the user and the navigation satellites, one objective is to select that combination of four navsats, from all those in view of the user, which will yield the minimum (or near minimum) values of GDOP.

The original computer program contained an algorithm which quickly selected the best combination of four GPS satellites from a maximum number of 11 that an *earth-based* user could see with a masking angle of 5 deg.* (See Fig. 2.) The first of the four satellites is the one nearest the user's zenith and the remaining satellites in view are used three at a time to determine the best combination of four. This is an efficient algorithm that results in the selection of the four navsats which will yield the smallest GDOP *almost all of the time*.** For 11 satellites in view, the maximum that GPS would provide to a terrestrial user, 120 combinations of three are possible after the first satellite has been selected, and there are 330 different combinations of four.

For a satellite-based user, assuming sufficient GPS signal strength in all directions, the masking angle depends only on the user's altitude and the dimensions assumed for the earth and atmosphere. Therefore, as the user's altitude increases, so will the number of satellites in view. For a user above about 8000 n mi altitude, about 21 of the 24 GPS satellites would be in view if the satellites were uniformly distributed. In this case, after selecting the first satellite, 1330 different combinations of three satellites are possible, and there are 7315 different combinations of four.

By considering the geometry of the satellite user relative to that of the satellites in view, it is usually possible to eliminate about half

* If the 24 GPS satellites were uniformly distributed on the spherical surface 10,900 n mi above the earth, then the expected number in view of a user with a 5 deg masking angle would be eight. However, since GPS satellites are not uniformly distributed, the maximum number in view can be 11.

** Occasionally, there may be a navsat with a slightly larger zenith angle that would result in a different selection of the other three navsats and a smaller GDOP. A switch is provided in the program to bypass the algorithm and consider all combinations of four navsats in view, but is far more expensive to use.

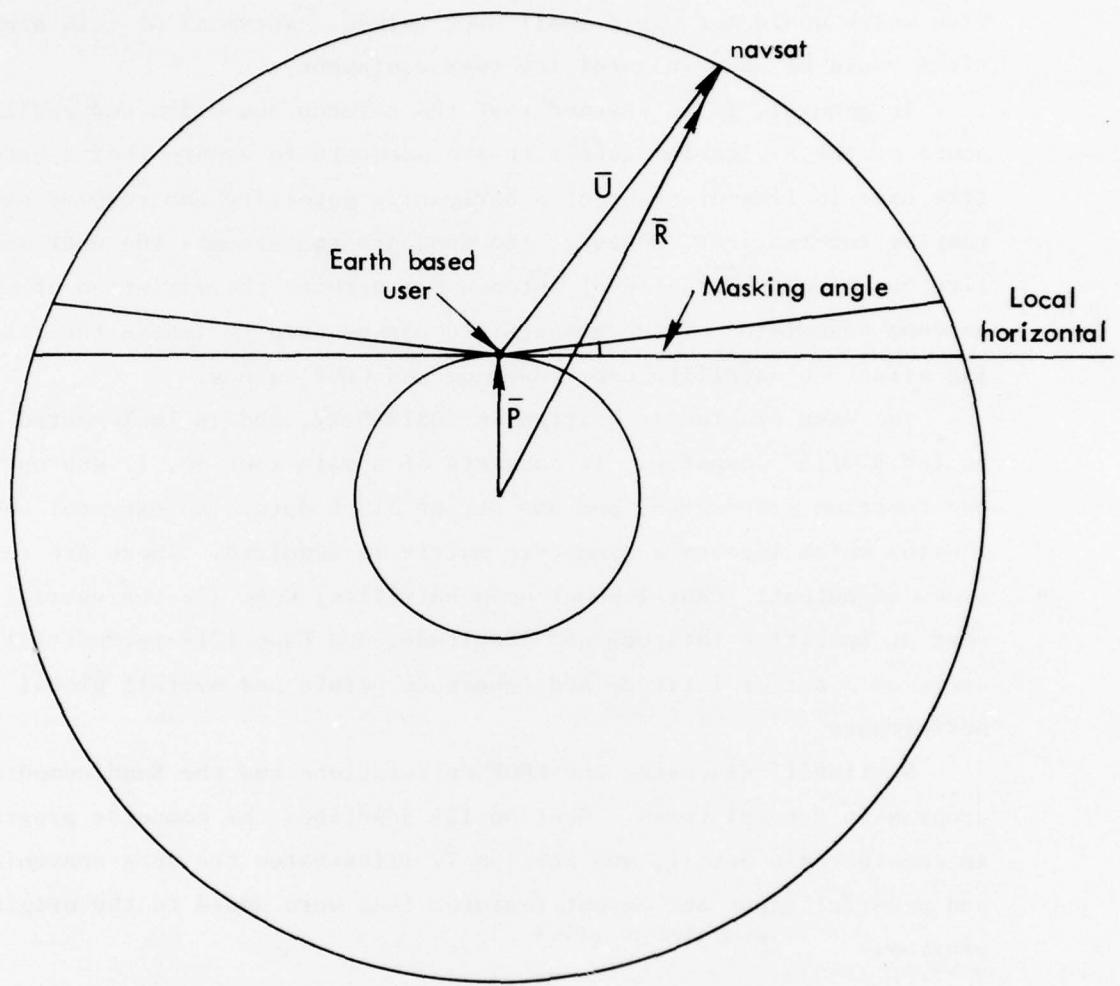


Fig. 2—User on earth

of them from further consideration. Thus, the original program was not only modified to include a satellite user but also contains an algorithm for such a user that eliminates navigation satellites in view which would not yield small GDOP values. Versions of this algorithm could be used in satellite user equipment.

In general, it is assumed that the antenna beamwidth and radiated power of the navigation satellite are adequate to assure that a satellite user in line-of-sight of a navigation satellite can receive pseudo-ranging information. However, the Rand program assumes the user satellite has an omni-directional antenna but permits the variation of the antenna beamwidths of the navsats and can be used to assess the resulting effect on satellite user coverage and GDOP values.

The Rand program is written in FORTRAN IV, and is implemented on an IBM 370/158 computer. It consists of a main routine, 12 subroutines, one function subprogram, and one set of block data. An external subroutine which inverts a symmetric matrix is required. There are three types of output: Case I--user on a satellite; Case II--terrestrial user at specified latitude and longitude; and Case III--terrestrial users on a net of latitude and longitude points and overall global performance.

Section II discusses the GDOP calculations and the Rand computer program in general terms. Section III describes the computer program in considerable detail, and Section IV illustrates the more convenient and powerful input and output features that were added to the original program.

II. DISCUSSION

NAVIGATION SATELLITE DEPLOYMENTS

The Rand computer program, which was partly written with GPS Phase III in mind, will accommodate up to a total of 36 navsats in any orbital arrangement. One additional satellite can be a user.

Current plans for the fully operational GPS Phase III call for 24 satellites deployed in 12-hr (about 10,900 n mi altitude) circular orbits inclined 63 deg to the earth's equatorial plane. The 24 satellites will be uniformly distributed in three orbit planes with ascending nodes separated by a longitude of 120 deg. (Alternative orbital configurations are being considered by the GPS Joint Program Office.) The eight satellites in each plane will be separated by 45 deg, and the phasing of the satellites between planes will be chosen to provide optimum navigation geometry. This system will be referred to frequently in the following text and the example solutions shown later are based on this system of navigational satellites.

USER LOCATIONS

Earth-based users can be located at any earth latitude and longitude. The program will compute the GDOP values for a single user, or for multiple users on a global basis. Currently, the program will accommodate only one satellite-borne user. There are no restrictions on the orbital elements of any of the navsats or the satellite user.

NAVIGATION SATELLITE VISIBILITY

In Ref. 1, it is stated that the number of GPS satellites that would be visible to an earth-based user would never be less than 6 nor greater than 11 if the masking angle (elevation angle of the user's line of sight) is 5 deg. Larger masking angles result in fewer satellites being visible to the user and therefore would probably decrease the accuracy in determining the user's position. Although smaller masking angles would, in general, increase the number of satellites visible, atmospheric effects could result in large errors in the pseudoranging

information that the user receives from GPS satellites near the user's horizon due to propagation errors.

For a satellite user, the masking angle required to avoid large atmospheric propagation effects changes rapidly with the user's altitude so that the number of GPS or other navigation satellites in view increases. In fact, a satellite user above about 8000 n mi altitude would, on the average, see 22 of the 24 GPS satellites. At this altitude, only two satellites, on the average, would be obscured from the user's view by the earth plus 200 n mi of atmosphere above the earth. This increase in the number of GPS satellites visible to a satellite user as a function of the user's altitude is shown in Fig. 3.

USER POSITION ACCURACY*

A user of a pseudoranging navsat system needs measurements from four satellites in order to determine his position (three components) and time. The redundancy afforded by having more than four satellites available permits a choice of the one set of four which will yield small values of GDOP. These values depend on both the pseudorange measurement errors (system errors) and the relative positions of the four GPS satellites selected.

The geometric relationships between the user's position, the positions of the four navigation satellites, and the four pseudorange measurements are given by Ref. 1:

$$\sum_{j=1}^3 (x_{ij} - u_j)^2 = (r_i - b)^2 , \quad (i)$$

where $i = 1, 2, 3, 4$ and is the index of each of the four equations, $j = 1, 2, 3$ and is the index for each of three orthogonal directions centered at the user,

x_{ij} = the j^{th} component of the position of the i^{th} navsat,

u_j = the j^{th} component of the position of the user,

r_i = the pseudorange measurement from the user to the i^{th} navsat, and

b = the user's clock bias in units of distance.

* These formulations are partly based on information from Paul Jorgenson of the Aerospace Corporation.

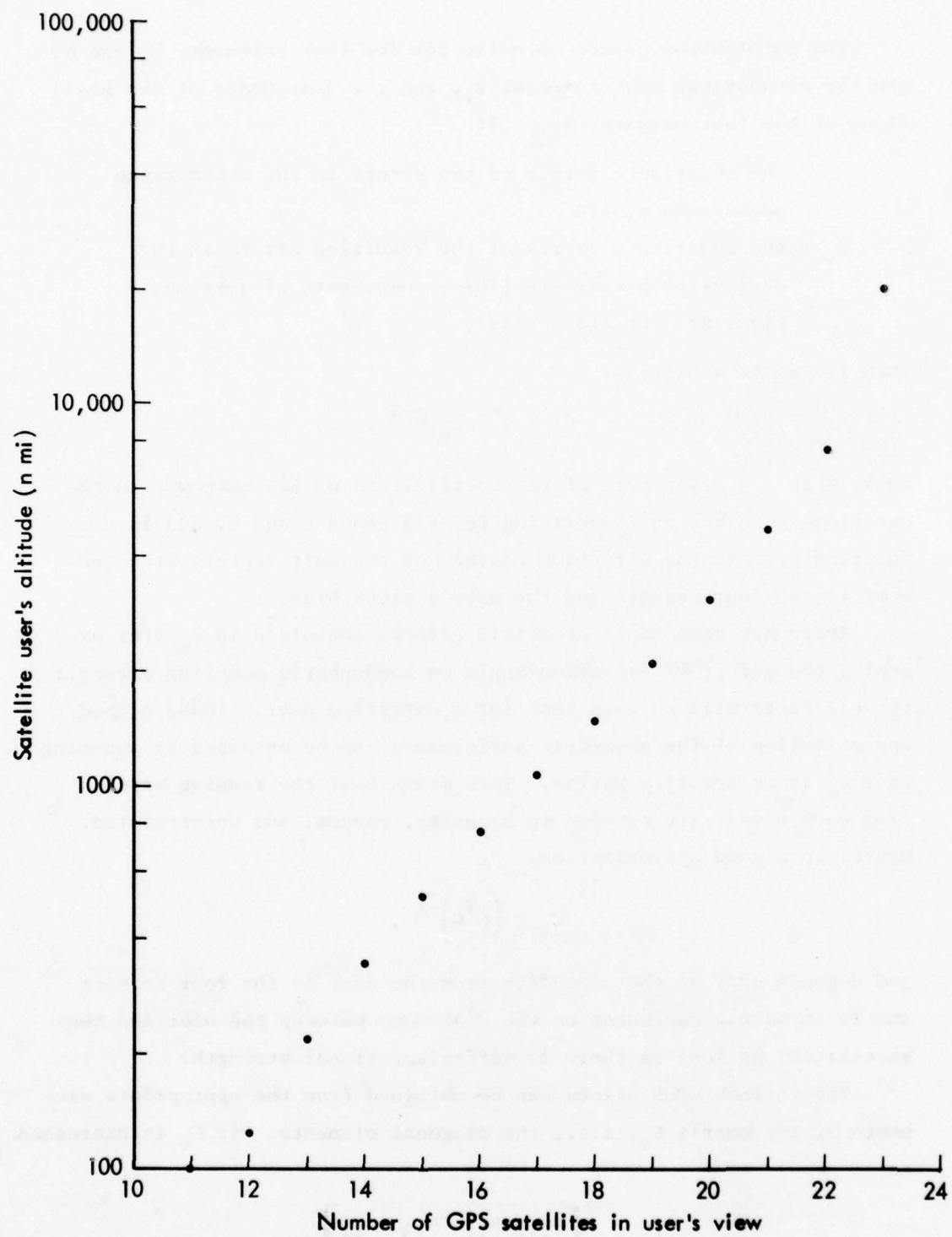


Fig. 3—The average number of GPS satellites visible to satellite users versus user altitude

The information needed to solve for the four unknowns, U_j and b , are the pseudorange measurements, r_i , and the components of the positions of the four navsats, x_{ij} . If

C_m = the covariance matrix of the errors in the pseudorange measurements, and

C_v = the covariance matrix of the resulting errors in the navigation parameters (three components of user position and user clock bias),

then it can be shown that

$$C_v = G^{-1} C_m G^{-T},$$

where G is a 4×4 matrix of the coefficients of the unknowns in the equations obtained by linearizing Eq. (1) about U and b , and is a function of only the direction cosines of the unit vectors from the user to the four navsats and the user's clock bias.

There are some small geometric effects contained in C_m (for example, the effect of elevation angle on ionospheric modeling errors); these effects will be even less for a satellite user. Thus, a good approximation of the geometric performance can be obtained by assuming that C_m is an identity matrix. This means that the ranging errors from each navsat are assumed to be unity, random, and uncorrelated. Hence, to a good approximation,

$$C_v = (G^T G)^{-1},$$

and depends only on the *direction* from the user to the four navsats and is in no way dependent on the *distances* between the user and the satellites, as long as there is sufficient signal strength.

The various GDOP values can be obtained from the appropriate elements of the matrix C_v , i.e., the diagonal elements. If C_v is expressed as

$$C_v = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{bmatrix},$$

an overall measure of geometric effect, GDOP, is obtained from the square root of the trace of the matrix.

$$GDOP = \sqrt{a_{11} + a_{22} + a_{33} + a_{44}},$$

where a_{11} , a_{22} , a_{33} relate to errors in position (x , y , z), and a_{44} to the user's time bias.* This factor includes all four unknowns (three dimensions of position and time) and is the conventional measure of overall performance. The other DOP values are:

$$PDOP = \sqrt{a_{11} + a_{22} + a_{33}},$$

$$HDOP = \sqrt{a_{11} + a_{22}},$$

$$VDOP = \sqrt{a_{33}},$$

$$TDOP = \sqrt{a_{44}},$$

$$MDOP = \text{Max} \left(a_{11}^{1/2}, a_{22}^{1/2} \right),$$

where PDOP, HDOP, VDOP, TDOP, and MDOP are the multiplying DOP factors that apply for the three-dimensional position error, the horizontal position error, the altitude error, the time error, and the larger component of the horizontal position error, respectively.

Because the effects of system errors (those independent of geometry) are multiplied by the DOP factors, it is desirable to select the four navsats of those available that will yield minimum DOP values (generally, PDOP).

The results of many computer runs and analytic approximations show that there is almost total correlation between PDOP and the volume of the tetrahedron formed by lines connecting the tips of the four unit vectors from the user toward the four navsats.** Usually (but rarely

* The origin of the x , y , z coordinate system (a right-handed system) is at the user's position. The z axis is in the direction of the user's vertical; the x axis points north and the y axis points east in a plane normal to the z direction.

** For example, PDOP can be shown to be inversely proportional to six times the volume of the tetrahedron and directly proportional to the trace of a complicated 3×3 matrix.(2)

not), the larger this volume, the smaller the PDOP values. The amount of computational time required to compute this volume is much less than the computation of PDOP itself, which involves a matrix inversion. Thus, the program was designed to first compute the volumes of the tetrahedrons associated with the different combinations of four nav-sats, identify the combination of four which yields the largest tetrahedron volume, and then use that combination to compute the DOP values. Another advantage of computing the tetrahedron volume as a prelude to computing the DOPs is that the time rate of change of the volume, and consequently an estimate of the time rate of change of PDOP, can easily be obtained;⁽¹⁾ however, this is not implemented in the program.

SATELLITE SELECTION

An earth-based user of a 24-satellite GPS system will see a maximum of 11 of the 24 satellites if his masking angle is as low as 5 deg. If it is assumed that 11 satellites are in view, and the one closest to the user's zenith is chosen as one of the four satellites required, there are 120 combinations if the remaining 10 satellites are taken three at a time. This is not a large number of combinations to be investigated, so the original program did not include an algorithm which would reduce the number of combinations to be examined. There is an option in the present program which allows the satellites to be combined four at a time, without the zenith restriction, but still using the tetrahedron volume.

In the case of a high-altitude satellite user of the baseline GPS configuration, 22 of the 24 satellites may be visible at any time. If this occurs, there are 1330 combinations to be investigated, and there is an option in the program which allows all combinations of four to be examined. An algorithm was developed to eliminate from the calculations those satellites which have unfavorable relative locations. This option usually cuts the execution time for the program by about a factor of 10. In general, about half of the satellites in view can be eliminated. The algorithm is derived in Appendix A.

Figure 4 is a plot of PDOP for a satellite user in a highly elliptic orbit versus time and altitude, and the variation of the parameter

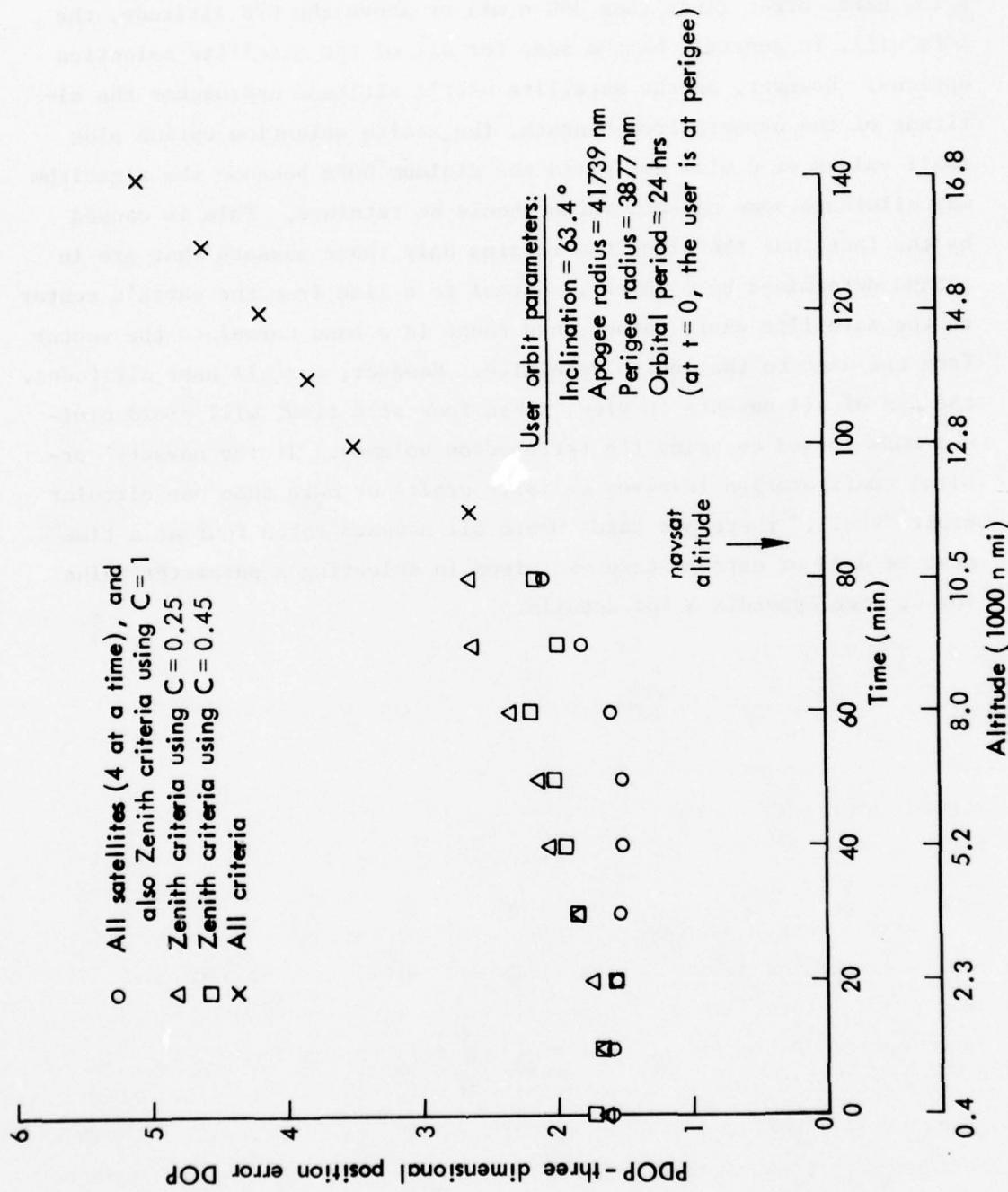


Fig. 4—Comparison of PDOPs using various satellite selection criteria

value for C, as described in Appendix A. If the user satellite is in a low earth orbit (less than 300 n mi) or above the GPS altitude, the DOPs will, in general, be the same for all of the satellite selection options. However, as the satellite user's altitude approaches the altitude of the navsats from beneath, the zenith selection option plus small values of C will not yield the minimum DOPs because the algorithm may eliminate some navsats which should be retained. This is caused by the fact that the algorithm retains only those navsats that are in a band determined by C which is normal to a line from the earth's center to the satellite user, rather than those in a band normal to the vector from the user to the zenith satellite. However, for all user altitudes, the use of all navsats in view, taken four at a time, will yield minimum DOPs (based on using the tetrahedron volume). If the navsats' orbital configuration involves elliptic orbits or more than one circular orbit "shell," there are cases where all navsats taken four at a time must be used or extreme care exercised in selecting a parameter value for C. See Appendix A for details.

III. COMPUTER PROGRAM OPERATION

The first card of the input contains the switch for choosing the case desired (LOC: LOC = 1, satellite user; LOC = 2, earth-based user; LOC = 3, global calculations); the number of navsats (NJL); and the switch for choosing the navsat selection technique (ISCM: ISCM = 0, zenith; ISCM = 1, all satellites, four at a time).

There are three types of calculations performed by the program: in Case I, the user is on a satellite; in Case II, the user is stationed at a specific latitude and longitude on the earth's surface; and, in Case III, a group of users are located at a set of latitudes and longitudes which form a net over the whole surface or a hemisphere of the earth.

Along with each of the three cases, there is a choice of the navsat selection technique to be used. In Case I, when the user is on a satellite, one choice is to use the navsat which is most nearly above or below the user as one of the four satellites in the calculation of the volume of the tetrahedron (zenith or nadir mode); the other choice is to use all of the navsats in view, taken four at a time. In Cases II and III, one choice is to use the navsat most nearly overhead of the earth-based user as one of the four satellites in all calculations of the volume, and the other choice is all of the satellites in view taken four at a time.

In all cases, the basic input to the program is the number of navsats and their orbital elements: eccentricity, argument of perigee, right ascension, inclination, initial true anomaly (at $t = 0$), and period. On the input cards, NJL is the number of satellites in the navsat system. P(N,K) is the array into which the orbital elements are read, where N is the identification number of the navsat, and K = 1 to 5 is the index on the first five orbital elements. The index K is held constant and the orbital element for that index is read in for all navsats (i.e., all eccentricities, then all arguments of perigee, etc.). The final inputs for the navsats are their periods, which are read into the array PER(N). After these inputs, navsat user related data is read in, which varies by case.

For Case I, NJL + 1 is the number of the user satellite. The first satellite user data card of a Case I input contains the eccentricity, argument of perigee, right ascension, inclination, and initial true anomaly of the user satellite at $t = 0$. The second card contains the period of the user, the antenna beamwidth half-angle of the navsats relative to a vector from the navsat to the center of the earth (AIN), and a numerical value (C) used in the calculation of the width of the band on the spherical surface containing the navsats, where the satellites for consideration in the "DOP" calculations will be sought (see Appendix A). The third card contains the time increment, in minutes, at which the calculations are desired (INC), and the total number of these time increments, plus one (ITF).^{*} For each run, the first page of output contains the orbital elements and all other input values. The subsequent output for Case I is the user altitude, VDOP, HDOP, MDOP, TDOP, PDOP, and GDOP at the chosen time increments, plus the identification numbers of the four navsats used and all others in view. If there are less than four satellites in view, there will be no print line for that time step--it is merely skipped and the program continues.

The first navsat user data card for a Case II run contains the latitude (ATL), longitude (ONGL), and masking angle of the user (ELEVAT, see Fig. 2). The second card contains the time increment, in minutes, at which the calculations are desired (INC) and the total number of these time increments required, plus one (ITF).^{*} The output for Case II is identical to Case I--except that the altitude is always zero.

In Case III, the users are located at a set of latitudes and longitudes which form a net over the surface of the earth. The prime objective of this Case is average overall system performance for earth users over a period of time, with a secondary objective of providing a "snapshot" of the DOPs at specified time steps at each longitude and latitude intersection specified. For overall performance, global statistics are calculated for a uniform distribution^{**} of users over the surface of the earth or in the northern hemisphere, and for a full

^{*}The "plus one" accounts for the "zero" time point.

^{**}A uniform distribution of users is approximated by the DOPs of users at a given latitude by the cosine of that latitude.

orbital period or a symmetrical part thereof. The total time input must assure this condition if overall performance for earth users is the objective.

The net of users can be chosen in various combinations. Basically, the calculations can be done at 10 deg steps in both longitude and latitude, covering the whole surface of the earth; or at 10 deg steps of longitude and 5 deg steps of latitude for covering the northern hemisphere. In addition, increments of these basic steps can be chosen so that the calculations will be performed at every 20 or every 30 deg, etc., of longitude and at every 20 or every 30 deg., etc., or at every 5 or every 15 deg, etc., of latitude. Global statistics calculations averaged over time are output at the completion of the calculations, but a "snapshot" of the DOPs at each longitude and latitude selected are available at any time point.

The first navsat user card for a Case III input contains the latitude step size (LATDEG) and the masking angle of the users (ELEVAT). The second card contains the latitude increment (LATIC) and the longitude increment (LONIC). If LATIC = 3 and LATDEG = 5, then calculations will be made at 0, 15, 30 deg, etc., in latitude. If LONIC = 2, then calculations will be made at 0, 20, 40, deg., etc., in longitude. The second card also contains the time increment, in minutes, at which the calculations are desired (INC) and the total number of these time increments, plus one, required to complete a full orbital period or to reach a condition of symmetry (ITF), if overall performance is the objective. The final two variables on the second navsat user card are concerned with the "snapshot" request. If IPFREQ = 0, no "snapshot" calculations are made; if it is greater than 0, then ITIME is set to an integer and "snapshot" calculations will be made and printed. For example, if the user has chosen INC = 10 and ITIME = 5, then "snapshot" output will occur at time = 0, 50, 100, etc. If the "snapshot" calculations are requested, the user will always get output at time = 0.

Since the program is quite costly for global calculations, the computation time step should be small enough to insure a representative global distribution. The size of the time step will depend on the navsat orbital configuration. Output for the average overall global

performance are elevation distribution, latitude elevation distribution, accumulative global distribution of DOPs, maximum and minimum number of satellites seen at the latitudes and longitudes of the net, the probability of seeing exactly N satellites, and the probability of seeing N or more satellites both by latitude and on an average (weighted by the cosine of latitude) global basis.

Table 1 (pages 19-22) contains an explanation of the variables in the MAIN program, and Table 2 (pages 23-27) contains an explanation of the variables in the subroutines *and* in their calling sequences. Table 3 (pages 28-29) shows the manner in which the input cards are set up. Appendix B provides a listing of the entire program.

A few timed runs were made. Table 4 (page 30) shows a comparison of some of the computing parameters.

The program has been dimensioned to accommodate a total of 36 navsats. In Case I, this means 36 navsats and one satellite user. Cases II and III are limited to a maximum of 36 navsats. All cases can evoke the option of using all navsats in view, taken four at a time, but, in Case III and in Case I (for high-altitude satellite users), the run time would be prohibitive. If less than 36 satellites are to be used, the dimensions of matrix KXX(I,4) (in MAIN, and in subroutines TAAT and TALL) should be reduced to cut down core storage. The index I is calculated from the formula

$$I = \frac{n!}{r! (n - r)!} ,$$

where n = number of navsats and r = 4.

For Case I, the calculations become less accurate as the altitude of a user above the navsats increases. The subroutine which inverts the DOP matrix is in double precision in order to alleviate some of this problem. However, above a ratio of satellite user altitude to navsat altitude of about 20, the matrix becomes sufficiently ill-conditioned that errors begin to occur in the DOPs.

Table 1
EXPLANATION OF VARIABLES IN MAIN PROGRAM

A. USER ON SATELLITE

FORTRAN	Equations	Explanation
\overline{R}^{α}	\overline{R}	Vector from the center of the earth to a navsat (where N is the "identification number" of the navsat and "IV" is the index of the components of the vector)
\overline{P}	P	Vector from the center of the earth to a user satellite (where "IP" is the "identification number" of the user satellite and "IV" is as above)
\overline{U}	U	Vector from a user satellite to a navsat
R	\overline{R}	Length of vector \overline{R}
P	\overline{P}	Length of vector \overline{P}
A	r/R	$\cos^{-1}(r/R)$, r = earth radius
B	r/P	$\cos^{-1}(r/P)$
ϕ	θ_n	$\cos^{-1}(r/R) + \cos^{-1}(r/P)$
PHI	\overline{U}	Length of the vector \overline{U}
THETN	β_n	$\cos^{-1}(-\overline{U} \cdot \overline{P}/UP)$
AU	α	Navsat antenna beamwidth half-angle (input) relative to a vector from the navsat to the center of the earth
$BWIDTH$	$\pi - (\theta_n + \beta_n)$	

^aAn overscore denotes a vector.

Table 1 (continued)

FORTRAN	Equations	Explanation
USUV(IINT(N),IV) U(IV)	$\bar{e}_1, \bar{e}_2, \bar{e}_3, \bar{e}_4$	Unit vectors from a user toward 4 navsats (where IINT(N) contains the "identification number" of the satellites which have not been eliminated and "IV" as above)
THETT	θ_T	<p>If $P > R \theta_T = \cos^{-1}(R/P)$</p> <p>If $P \leq R$ and β (of the navsat closest to zenith or nadir) $> \pi/2$; $\theta_T = 109.5^\circ - \sin^{-1}(P \sin 19.5^\circ / R)^b$</p> <p>If $P \leq R$ and β (of the navsat closest to zenith or nadir) $< \pi/2$; $\theta_T = 70.5^\circ - \sin^{-1}(P \sin 19.5^\circ / R)^b$</p>
DELONE	δ_1	<p>If $\sin^2 \theta_T > C \delta_1 = \sin^{-1}(C / \sin \theta_T)$</p> <p>If $\sin^2 \theta_T \leq C \delta_1 = \theta_T$</p>
DELTWO	δ_2	<p>If $\sin^2 \theta_T > C \delta_2 = \delta_1$</p> <p>If $\sin^2 \theta_T \leq C \delta_2 = \cos^{-1}(1 - 2C) - \theta_T$</p>

^b See Appendix A.Note

After the calculations for eliminating satellites which are not to be considered in the set for navigational purposes, the ones to be used are located as follows:

- IOS(I) As I is incremented from 2 to the number of satellites to be included in the navigational calculations, the "identification numbers" of those satellites are stored in IOS.

IOS(1) always contains the "identification number" of the satellite which is closest to zenith or nadir.

Table 1 (continued)

B. USER ON GROUND^c

FORTRAN	Explanation
R, RMX	Vector from the center of the earth to a navsat
UPV	Vector from the center of the earth to a user
STN	Vector from a navsat to a user
SE	Elevation (masking) angle of a satellite
UTS	Vector from a user to a navsat (-STN)
USUV	Unit vector (of UTS)
NSTO	Total number of navsats in view
NSPL(L)	Total number of navsats in view at each latitude
CL(L)	Total number of latitudes when there are four or more navsats in view
Z	Vector in the polar direction \bar{Z} (origin at the earth's center)
YE	Vector in the eastward direction (origin at the user)
XN	Vector in the northward direction (origin at the user)
G(NSGD(N), I)	Direction cosines (where NSGD(N) contains the "identification numbers" of the four selected navsats and I = 1, 4)
SIGT	Dimensioned at 6, contains the dilution of precision (DOP) parameters
CDOP(L, K, IDOP)	Storage for DOPs for each time step; L = latitude index, K = longitude index, IDOP = DOPs index
PIB(IX)	Elevation distribution--the probability that the satellite in view will have specified elevation angles; IX = elevation angle index

^cThis portion of the program is explained in Ref. 1.

Table 1 (continued)

FORTRAN	Explanation
CAGX(LA,LC)	Latitude elevation distribution--the probability that any navsat in view will have an elevation angle greater than or equal to those specified; LA = latitude index, LC = elevation range index
GLEB(IC)	Accumulative elevation distribution--the probability that the elevation angle to a navsat is greater than or equal to those listed; IC = elevation range index
QSRIQSR)	Range into which the printed variable falls; IQSR = 1, 36 in steps of .2
SKEGX(LK,IQSR,JDOP)	Dilution of precision parameters for overall global performance; LK = latitude index, IQSR (see above), JDOP = DOPs index
MAX(IL,IK)	Maximum number of navsats seen at the intersections of latitudes and longitudes; IL = latitude index, IK = longitude index
MIN(IL,IK)	Minimum number of navsats seen at the intersections of latitudes and longitudes; IL = latitude index, IK = longitude index
OBLAT(IL,N)	Probability (in percent) of seeing exactly N navsats; IL = latitude index, N = number of navsats
ACLAT(IL,N)	Probability (in percent) of seeing N or more navsats; IL = latitude index, N = number of navsats
OBDIS(N)	On a global basis, the probability (in percent) that exactly N navsats will be seen (as above)
ACTOT(N)	On a global basis, the probability (in percent) that N or more navsats will be seen (as above)

Table 2
EXPLANATION OF VARIABLES AND CALLING SEQUENCES OF SUBROUTINES

The subroutine call with the variable names in its argument list, as it appears in MAIN, is shown first. The subroutine name, with the variable names in its argument list and an accompanying explanation, appears second.

ORBINI(N)

ORBINI(I)	I, satellite number
P(I,2)=P(I,2)*C(1)	Argument of periapsis x 0.01745
P(I,3)=P(I,3)*C(1)	Right ascension of the node x 0.01745
P(I,4)=P(I,4)*C(1)	Inclination x 0.01745
P(I,5)=P(I,5)*C(1)	Initial true anomaly x 0.01745
P(I,9)=sin i	i, inclination
P(I,10)=cos i	
P(I,11)=sin Ω	Ω, right ascension of node
P(I,12)=cos Ω	
P(I,21)=a	orbit semi-major axis in feet
SAA=earth synchronous satellite radius in feet	
P(I,23)=ratio of synchronous radius to orbit semi-major axis	
P(I,6)=a(1-e ²)	e, eccentricity
P(I,7)= $\sqrt{\mu/[a(1-e^2)]}$	μ, gravitational constant
P(I,8)= $\sqrt{\mu/[a^2(1-e^2)]}$	

Calculated only
to change units
from degrees
to radians

POINT(LONG,LAT,TID,UPV)

POINT(ALO,ALA,TIM,VEC)	ALO, longitude
	ALA, latitude
	TIM, time in days
	VEC, vector from the center of the earth to
	a user at a specific latitude and
	longitude
EW=long(rad)+2π(time)	
SN=lat(rad)	

Table 2 (continued)

VEC(1)=(radius of the earth at the equator)(cos lat)(cos long)
VEC(2)=(radius of the earth at the equator)(cos lat)(sin long)
VEC(3)=(radius of the earth at the equator)(sin lat)

COVNAV(G,NSGD,4 SIGT)

COVNAV(G, ID, NAT, SIG) G, direction cosine matrix
 ID, index of the navsats which were chosen
 as the "best" four
 NAT, the number of them (always four)
 SIG, dilution of precision parameters re-
 turned to MAIN

This subroutine is the only one which requires a local system subroutine--a matrix inversion. This subroutine calculates $[G^T G]^{-1}$ and returns the values in SIG(1-6), which are the DOPs.

TRMATX(TRANS,I)

TRMATX(TR,I) TR, 3 x 3 coordinate transformation matrix
 I, satellite number

TR(1,1)=cos Ω cos u - sin Ω cos i sin u u, argument of
 TR(1,2)=-cos Ω sin u - sin Ω cos i cos u latitude
 TR(1,3)=sin Ω sin i

TR(2,1)=sin Ω cos u + cos Ω cos i sin u
TR(2,2)=-sin Ω sin u + cos Ω cos i cos u
TR(2,3)=-cos Ω sin i
TR(3,1)=sin i sin u
TR(3,2)=sin i cos u
TR(3,3)=cos i

MATMUL(TRANS,Q,R)

MATMUL(TRANS, QEL, VEL)

Table 2 (continued)

MATMUL(TRANS, QC, AC)

MATMUL(T,V,O) T, 3 x 3 coordinate transformation matrix
 V, vector to be transformed
 O, vector returned

VOLUME (USUV, ISIC, VOLUM)

ORBIT(N, TID, PER, RF, VE, AA)

ORBIT(I,T,PER,R,VEL,AC) N, I, satellite number
 TID, T, time in days
 PER, period of a satellite
 RF, R, vector to a satellite from the center
 of the earth
 VE, VEL, velocity } not used
 AA, AC, acceleration due to gravity } at present

This subroutine iterates for the eccentric anomaly and computes the true anomaly. If time = 0, the following is computed:

$V(I) = OP(I, 5) = v$, true anomaly
 $SINE = [\sqrt{1-e^2} \sin v] / [1 + e \cos v]$, sin E
 $E(I) = E$, arcsin E, eccentric anomaly
 $BIGT(I) = \text{time from perigee for satellite}$

If $\text{time} > 0$, $E(I)$ is obtained by iterating, then the following is computed:

$$\begin{aligned} \text{SINV} &= [\sqrt{1-e^2} \sin E] / [1 - e \cos E] = \sin v \\ V(I) &= \arcsin v, \text{ true anomaly} \\ U(I) &= V(I) + OP(I, 2), v + \text{argument of periapsis} = v + w = u, \text{ argument of latitude} \end{aligned}$$

Table 2 (continued)

OP(I,13) = cos u
OP(I,14) = sin u
OP(I,15) = latitude
OP(I,18) = u, argument of latitude
 $Q(1) = [a(1-e^2)]/[1 + e \cos v]$ }
 $Q(2) = 0$ }
 $Q(3) = 0$ } for calculating R
 $QEL(1) = e \sin v \sqrt{\mu}/\sqrt{a(1-e^2)}$ }
 $QEL(2) = \sqrt{\mu}/\sqrt{a(1-e^2)}$ } for calculating VEL
 $QEL(3) = 0$
 $QC(1) = (1 + e \cos v)^2 \mu/[a^2(1-e^2)^2]$ }
 $QC(2) = 0$ } for calculating AC
 $QC(3) = 0$
OP(I,24) = earth rotation
OP(I,16) = longitude of the satellite

TAAT(NSS,KCOM,KXX)

TAAT(MAX,MXX,MATRIX) MAX, 1 less than the number of navsats to be examined for use
MXX, the number of combinations of those navsats
MATRIX, contains indices of the navsats to be examined, three at a time

This subroutine sets up the sequence of navsats which are to be examined, using either the one above or below the user as one of the four in each calculation of the tetrahedron volume.

TALL(KOT,KCOM,KXX)

TALL(MAX,MXX,MATRIX) MAX, the number of navsats to be examined for use
MXX, the number of combinations of those navsats

Table 2 (continued)

MATRIX, contains indices of the navsats
to be examined, four at a time

This subroutine sets up the sequence of navsats which are to be
examined, using all satellites taken four at a time.

BLOCK DATA

Contains various parameter values used in the program, although
not all of them are used in the current version.

VECTOR(V1,I,V2,V3)

This subroutine performs vector additions, subtractions, and
cross products.

UNIVEC(U,UV)

This subroutine calculates unit vectors.

DOT(V1,V2)

This function subprogram calculates dot products.

Table 3
INPUT CARD SETUP

All Cases; Case Type, and Navsat System Description

Card Number	Format	Variable Names	Explanation	Units
1	10I5	LOC NJL ISCM ^a	LOC, case type NJL, number of navsats (maximum of 36) Navsat combination switch ("zenith"/nadir plus 3 others, ISCM ^b = 0, or all combinations of 4, ISCM ^b = 1)	
2, etc.	12F6.0	P(N,1) ^a	Eccentricity	deg
	12F6.0	P(N,2)	Argument of perigee	deg
	12F6.0	P(N,3)	Right ascension	deg
	12F6.0	P(N,4)	Inclination	deg
	12F6.0	P(N,5)	Initial true anomaly	deg
n	12F6.0	PER(N)	Period	hr

^aN is the number of the navsat; the first orbital element for all navsats is read in (eccentricity), then the second orbital element for all satellites is read in, etc. If there are more than 12 satellites, the next cards in sequence contain the rest of that element until NJL is reached. From here on, the cards differ depending on case.

Case I, Satellite User

n+1	12F6.0	P(NJL+1,K)	NJL+1, number of the user satellite; K = 1, 5, indices of elements of the user satellite (as above, in sequence)	deg
n+2	7F10.0	PER(NJL+1) AIN C	PER, period of the user satellite AIN, antenna half beamwidth for the navsats C, numerical constant for navsat selection ^b	hr deg
n+3	10I5	INC ITF	INC, time step ITF, total number of time steps, plus 1	min

^bSee Appendix A.

Table 3 (continued)

Case II, User at Specified Latitude and Longitude

Card Number	Format	Variable Names	Explanation	Units
n+1	7F10.0	ATL ONGL ELEVAT INC ITF	ATL, latitude ONGL, longitude ELEVAT, masking angle above horizontal INC, time increment per step ITF, total number of time steps, plus 1	deg deg deg min
n+2	10I5			

Case III, Global Calculations

n+1	7F10.0	LATDEG ELEVAT LATIC LONIC INC ITF IPFREQ ITIME	LATDEG, latitude step (10 or 5 only) ^c ELEVAT, masking angle above horizontal LATIC, latitude increment LONIC, longitude increment INC, time increment per step ITF, total number of time steps, plus 1 IPFREQ, "DOP" print flag ITIME, print increments for DOP	deg deg
n+2	10I5			

^cThe basic longitude step is always 10 deg. LATDEG = 10 is for northern and southern hemisphere coverage; LATDEG = 5 is for northern hemisphere coverage.

Table 4
COMPUTING COSTS (IBM 370/158 COMPUTER)

Case I, Satellite User

Number of Navsats	Choice ^a	Number of Time Steps	CPU Time (sec)	Amount of Core (bytes)	Costs ^b (MUs)
24	All	48	223	300 K	27.24
24	Zenith/nadir	48	21	300 K	2.68
36	All	57	348	722 K	42.70
36	Zenith/nadir	120	67	300 K	8.31

Case II, Single Earth-Based User

24	All	144	25	300 K	3.91
24	Zenith	144	21	300 K	2.69

Case III, Global Net of Earth-Based Users

24	Zenith	5	1228	300 K	149.29
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^a"All" refers to using all navsats in view, 4 at a time, in all calculations; zenith/nadir refers to using the navsat most directly above or below as one of the 4 in all calculations.

^bCost in Machine Units--a direct measure of computing cost used at Rand, which accounts for core, CPU time, and input/output resources used for a given run; currently, a Machine Unit (MU) costs about \$1.25.

IV. PROGRAM INPUT AND OUTPUT

Table 5 (pages 32-36) is a listing of the input data set for a Case I run (using the navsat most nearly above or below the user in all calculations) and its resulting output. This run treats the user satellite as a very high apogee ballistic missile. Table 6 (pages 37-43) is a listing of the input data set for a Case II run (using all navsats in view, taken four at a time) and its resulting output. Table 7 (pages 44-55) is a listing of the input data set for a global distribution of earth-based users with its output.

Table 5
EXAMPLE: DATA SET FOR CASE I ("ZENITH/NADIR" SATELLITE USED)

INPUT

		CASE NO. OF SATELLITES SWITCH					
1	24	0	0	0	0	0	0
0	0	0	0	0	0	0	0
3	0	3	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
120	120	120	240	240	240	120	120
63	63	63	63	63	63	63	63
63	63	63	63	63	63	63	63
0	45	90	135	180	225	270	315
195	240	285	330	30	75	120	165
12	12	12	12	12	12	12	12
12	12	12	12	12	12	12	12
*81602	11.24	47.5	144.21	69.76			
11.0529	180.						
10	100						
		<u>INITIAL TRUE ANOMALY</u>					
		<u>PERIOD OF NAVSATS</u>					
		<u>USER PARAMETERS</u>					
		<u>PERIOD OF USER BEAM C</u>					
		<u>INCREMENT TOTAL TIME</u>					

Table 5 (Continued)

ORBITAL ELEMENTS

	ECC	ARGP	RASC	INC	ANEM ^a	PER
1	0.0	0.0	0.0	63.00	0.0	12.00
2	0.0	0.0	0.0	63.00	45.00	12.00
3	0.0	0.0	0.0	63.00	90.00	12.00
4	0.0	0.0	0.0	63.00	135.00	12.00
5	0.0	0.0	0.0	63.00	180.00	12.00
6	0.0	0.0	0.0	63.00	225.00	12.00
7	0.0	0.0	0.0	63.00	270.00	12.00
8	0.0	0.0	0.0	63.00	315.00	12.00
9	0.0	0.0	120.00	63.00	15.00	12.00
10	0.0	0.0	120.00	63.00	60.00	12.00
11	0.0	0.0	120.00	63.00	105.00	12.00
12	0.0	0.0	120.00	63.00	150.00	12.00
13	0.0	0.0	120.00	63.00	195.00	12.00
14	0.0	0.0	120.00	63.00	240.00	12.00
15	0.0	0.0	120.00	63.00	285.00	12.00
16	0.0	0.0	120.00	63.00	330.00	12.00
17	0.0	0.0	240.00	63.00	30.00	12.00
18	0.0	0.0	240.00	63.00	75.00	12.00
19	0.0	0.0	240.00	63.00	120.00	12.00
20	0.0	0.0	240.00	63.00	165.00	12.00
21	0.0	0.0	240.00	63.00	210.00	12.00
22	0.0	0.0	240.00	63.00	255.00	12.00
23	0.0	0.0	240.00	63.00	300.00	12.00
24	0.0	0.0	240.00	63.00	345.00	12.00

USER SATELLITE ORBITAL ELEMENTS

25 0.82 11.24 47.50 144.21 69.76 11.05

TOTAL TIME(MIN) = 990
TIME INCREMENT(MIN) = 10
BEAMWIDTH ANGLE(DEG) = 180.00
FRACTION OF NAVSAT SPHERICAL AREA = 0.340

THE SATELLITE MOST NEARLY ABOVE OR BELOW IS USED AS ONE OF THE FOUR
IN ALL CALCULATIONS OF THE VOLUME OF THE TETRAHEDRON

^aDuring final preparation of this report, the authors were informed by the NAVSTAR/GPS Joint Program Office that the planned orbital configuration for GPS had been changed. Users who wish to simulate the currently planned configuration should interchange the anomalies of satellites 9 through 16 with those of satellites 17 through 24, shown above. No other changes are required.

Table 5 (Continued)

TIME (MM)	ALT (NM)	VDDP	HDDP	MDDP	TDDP	PDDP	GDDP	SATELLITES CHOSEN
10	1894.	0.829	1.423	1.165	0.516	1.647	1.726	12 3 5 14 4 6 7 20 23
20	3612.	0.926	1.339	1.061	0.521	1.628	1.709	17 3 8 23 1 2 4 5 6 7 9 14 19
30	5173.	0.967	1.338	1.042	0.533	1.650	1.734	17 3 8 23 1 2 4 5 6 7 9 14 19
40	6584.	1.136	1.394	1.088	0.716	2.226	2.339	16 10 12 23 5 6 13 18
50	7879.	1.674	1.231	0.901	0.837	2.078	2.240	21 10 12 23 4 5 6 17 18
60	9063.	1.792	1.219	0.904	0.972	2.167	2.375	15 10 12 23 4 5 6 11 17
70	10157.	1.937	1.254	0.966	1.116	2.308	2.564	15 10 12 23 4 5 6 11 17
80	11170.	1.698	1.627	1.307	1.048	2.352	2.574	19 12 23 24 4 5 10 11 17
90	12109.	2.432	1.404	1.145	1.563	2.808	3.214	15 10 12 23 4 5 11 17 24
100	12992.	2.735	1.823	1.548	1.887	3.287	3.790	20 10 11 23 4 5 17 22 24
110	13795.	3.526	1.534	1.143	2.557	3.847	4.614	20 9 11 22 4 5 10 23 24
120	14551.	3.882	1.545	1.171	2.856	4.178	5.061	20 9 11 22 3 4 5 10 23 24
130	15256.	4.564	1.635	1.224	3.377	4.848	5.908	18 9 11 22 3 4 5 10 24
140	15912.	4.404	1.678	1.298	3.395	4.713	5.809	18 3 5 10 4 9 11 22 24
150	16521.	4.494	1.673	1.228	3.533	4.796	5.956	18 3 5 10 4 9 11 22 23 24
160	170d7.	4.606	1.702	1.229	3.685	4.910	6.139	18 3 5 10 4 9 11 21 22 23 24
170	17611.	4.973	1.799	1.392	4.009	5.288	6.636	19 3 5 10 4 9 11 21 22 23 24
180	18094.	5.600	1.830	1.347	4.583	5.891	7.464	19 3 5 23 4 9 10 21
190	18539.	6.115	1.848	1.307	5.015	6.388	8.122	19 2 10 21 3 4 5 9 16 23
200	18947.	6.918	1.859	1.384	5.697	7.164	9.153	7 2 4 10 3 9 16 21 23
210	19320.	6.464	1.970	1.563	5.345	6.757	8.616	17 2 4 23 3 9 10 16 21
220	19657.	6.328	1.961	1.550	5.283	6.625	8.474	17 2 4 23 3 9 10 16 21
230	19960.	6.232	1.942	1.447	5.243	6.528	8.373	17 2 4 9 3 10 16 20 21 23
240	20230.	6.188	1.923	1.408	5.242	6.480	8.334	17 2 4 9 3 10 16 20 23
250	20468.	6.738	1.938	1.402	5.114	7.011	9.045	18 2 4 9 3 10 16 20 22 23

Table 5 (Continued)
 TIME (MM) ALT (NM) VDOP HDOP MDOP TDOP PDOP GDOP SATELLITES CHOSEN

260	20674.	7.411	1.996	1.521	6.297	7.675	9.928	18	2	4	9	3	16	20	22		
270	20848.	7.915	2.005	1.467	6.763	8.165	10.603	7	2	4	22	1	3	9	15	16	20
280	20991.	7.952	2.042	1.508	6.817	8.210	10.671	6	2	4	22	1	3	9	15	16	20
290	21103.	7.883	2.115	1.677	6.764	8.162	10.603	6	1	3	22	2	4	9	15	16	20
300	21184.	7.611	2.101	1.676	6.531	7.895	10.246	6	1	3	22	2	9	15	16	19	20
310	21236.	6.875	2.080	1.648	5.921	7.183	9.308	17	1	3	22	2	9	15	16	19	
320	21257.	6.860	2.064	1.595	5.908	7.164	9.286	24	1	3	16	2	15	19	21	22	
330	21247.	7.315	2.049	1.514	6.282	7.596	9.858	6	1	3	16	15	19	21	22		
340	21208.	7.383	2.044	1.482	6.349	7.662	9.951	6	1	3	21	15	16	19			
350	21138.	7.306	2.025	1.473	6.285	7.581	9.848	6	1	3	21	2	8	14	15	16	19
360	21036.	7.484	2.033	1.477	6.452	7.755	10.080	6	1	3	21	2	6	14	15	16	19
370	20907.	7.427	2.046	1.512	6.436	7.704	10.038	5	1	3	21	2	8	14	15	16	19
380	20745.	6.979	2.123	1.696	6.012	7.294	9.453	24	2	8	21	1	3	14	15	18	19
390	20551.	6.878	2.109	1.704	5.887	7.194	9.296	5	2	8	21	14	15	18	19	20	
400	20326.	6.649	2.072	1.516	5.670	6.965	8.981	5	2	8	20	14	15	18	21		
410	20069.	7.104	1.939	1.3d6	5.979	7.364	9.485	24	2	8	20	14	15	18			
420	19778.	7.473	1.928	1.382	6.217	7.717	9.910	24	2	8	20	14	18				
430	19454.	6.749	1.893	1.365	5.606	7.010	8.976	4	8	16	20	2	14				
440	19095.	5.615	1.906	1.393	4.694	5.930	7.563	5	8	18	20	2	7				
450	18701.	5.890	1.936	1.449	4.906	6.200	7.906	23	8	16	20	1	2	7	19		
460	18270.	5.728	1.971	1.610	4.761	6.058	7.705	4	7	18	20	1	2	8	17	19	
470	17801.	5.229	1.781	1.290	4.267	5.524	6.980	22	7	17	19	1	2	8	18	20	
480	17243.	4.602	1.714	1.214	3.674	4.913	6.137	22	7	17	19	1	18				
490	16744.	4.722	1.664	1.206	4.639	5.006	6.189	5	7	17	19	1	18				
500	16151.	4.532	1.611	1.203	3.398	4.812	5.891	5	7	17	19	1	18				

Table 5 (Continued)

TIME(4N) ALT(NM)	VDDP	HDDP	MDDP	TDDP	PDDP	GDDP	SATELLITES CHOSEN
510 15514.	3.589	1.574	1.204	2.700	3.919	4.759	22 7 17 19 1 8 18
520 14629.	3.356	1.537	1.205	2.468	3.691	4.440	22 7 17 19 1 8 18
530 14093.	2.933	1.507	1.102	2.032	3.297	3.873	3 7 17 18 1 8 19 24
540 13303.	2.526	1.479	1.109	1.687	2.927	3.378	3 7 17 18 1 6 8 24
550 12453.	2.363	1.339	0.955	1.546	2.716	3.126	21 7 18 24 1 6 8 17
560 11541.	1.995	1.306	0.980	1.225	2.385	2.681	4 7 1d 24 6 8 17
570 10558.	2.234	1.335	1.014	1.305	2.603	2.912	4 6 18 24 8 10 11 17
580 9496.	1.750	1.389	1.135	0.870	2.235	2.398	21 6 17 24 8 9 10 11 18 23
590 8347.	1.430	1.334	1.085	0.679	1.958	2.073	20 6 17 24 8 9 10 11 18 23
600 7095.	1.615	1.256	0.916	0.683	2.046	2.157	2 6 17 23 8 9 10 11
610 5733.	1.403	1.178	0.861	0.695	1.832	1.954	2 11 17 23 5 6 5 9 10 16
620 4228.	1.128	1.214	0.947	0.556	1.657	1.748	2 10 17 23 5 6 8 9 11 16 22
630 2576.	1.120	1.140	0.816	0.521	1.598	1.681	14 5 22 24 6 7 8 10 16 17
640 784.	0.902	1.376	1.099	0.512	1.645	1.723	9 1 4 17 11

TERMINATION OF RUN, ALTITUDE APPROACHING ZERO *

* Satellite user calculations terminate when and if the orbit intersects the earth's surface.

Table 6 (Continued)

ORBITAL ELEMENTS

	ECC	ARGP	RASC	INC	ANOM	PER
1	0.0	0.0	0.0	63.00	0.0	12.00
2	0.0	0.0	0.0	63.00	45.00	12.00
3	0.0	0.0	0.0	63.00	90.00	12.00
4	0.0	0.0	0.0	63.00	135.00	12.00
5	0.0	0.0	0.0	63.00	180.00	12.00
6	0.0	0.0	0.0	63.00	225.00	12.00
7	0.0	0.0	0.0	63.00	270.00	12.00
8	0.0	0.0	0.0	63.00	315.00	12.00
9	0.0	0.0	120.00	63.00	15.00	12.00
10	0.0	0.0	120.00	63.00	60.00	12.00
11	0.0	0.0	120.00	63.00	105.00	12.00
12	0.0	0.0	120.00	63.00	150.00	12.00
13	0.0	0.0	120.00	63.00	195.00	12.00
14	0.0	0.0	120.00	63.00	240.00	12.00
15	0.0	0.0	120.00	63.00	285.00	12.00
16	0.0	0.0	120.00	63.00	330.00	12.00
17	0.0	0.0	240.00	63.00	30.00	12.00
18	0.0	0.0	240.00	63.00	75.00	12.00
19	0.0	0.0	240.00	63.00	120.00	12.00
20	0.0	0.0	240.00	63.00	165.00	12.00
21	0.0	0.0	240.00	63.00	210.00	12.00
22	0.0	0.0	240.00	63.00	255.00	12.00
23	0.0	0.0	240.00	63.00	300.00	12.00
24	0.0	0.0	240.00	63.00	345.00	12.00

USER LOCATION ON EARTH

LATITUDE = 0.0 DEGREES

LONGITUDE = 0.0 DEGREES

MASKING ANGLE = 5.00 DEGREES

TOTAL TIME(MIN) = 720

TIME INCREMENT(MIN) = 6

ALL SATELLITES, TAKEN FOUR AT A TIME, ARE USED IN
THE CALCULATIONS OF THE VOLUME OF THE TETRAHEDRON

Table 6 (Continued)

TIME (MM) ALT (NM)	VDUP	MDUP	WDUP	DDUP	TOUP	PQUP	GDUP	SATELLITES CHOSEN
0	0.	2.012	1.843	1.554	1.328	2.729	3.035	1 13 14 20 2 8 19
6	0.	1.954	1.810	1.513	1.251	2.664	2.943	1 13 15 20 2 8 14
12	0.	1.968	1.796	1.495	1.217	2.664	2.929	1 13 19 20 2 8 14
18	0.	1.994	1.744	1.437	1.195	2.649	2.905	1 2 13 20 8 14 19
24	0.	1.581	1.318	1.082	0.870	2.058	2.234	1 14 18 20 2 8 13 19
30	0.	1.631	1.343	1.116	0.885	2.113	2.241	1 14 18 20 2 8 13 19
36	0.	1.768	1.251	0.921	0.988	2.166	2.381	1 13 18 20 2 8 14 19
42	0.	1.858	1.227	0.875	1.002	2.226	2.442	1 13 18 20 2 8 14 19
48	0.	1.984	1.216	0.878	1.033	2.327	2.546	1 13 18 20 2 8 14 19
54	0.	1.883	1.181	0.895	0.904	2.223	2.400	7 8 18 20 1 2 13 14 19
60	0.	1.934	1.105	0.996	0.955	2.273	2.465	8 7 18 20 1 2 13 14 19
66	0.	1.824	1.317	0.958	0.860	2.249	2.408	8 2 7 20 1 13 14 18 19
72	0.	2.108	1.208	0.912	1.082	2.430	2.660	8 7 18 20 1 13 14 19
78	0.	2.225	1.237	0.945	1.160	2.546	2.797	8 13 18 20 1 7 14 19
84	0.	2.307	1.277	0.985	1.214	2.637	2.903	8 13 18 20 1 7 14 19
90	0.	2.447	1.336	1.034	1.296	2.788	3.074	8 13 18 20 1 7 14 19
96	0.	2.662	1.419	1.093	1.414	3.016	3.331	8 13 18 20 1 7 14 19
102	0.	2.481	1.536	1.168	1.586	3.354	3.710	8 13 18 20 1 7 14 19
108	0.	3.082	1.420	1.010	1.599	3.394	3.751	1 7 14 19 8 13 18 20
114	0.	2.751	1.328	0.972	1.428	3.055	3.372	1 7 14 19 8 13 18 20
120	0.	2.527	1.266	0.940	1.311	2.826	3.115	1 7 14 19 8 13 18 20
126	0.	2.379	1.225	0.914	1.230	2.676	2.945	1 7 14 19 8 13 18 20
132	0.	2.290	1.200	0.893	1.177	2.585	2.840	1 7 14 19 8 13 18 20
138	0.	1.878	1.267	0.897	0.859	2.265	2.423	1 9 7 17 20 1 8 13 14 18
144	0.	1.566	1.274	1.017	0.862	2.259	2.415	1 8 13 14 19

Table 6 (Continued)

TIME(MN)	ALT(NM)	VDDP	HDDP	MDDP	TDDP	PDDP	GDDP	SATELLITES CHOSEN
150	0.	1.939	1.261	0.949	0.955	2.313	2.503	1b 7 14 17 1 b 13 19
156	0.	1.947	1.286	0.937	0.992	2.334	2.536	1b 7 14 17 1 8 13 19
162	0.	1.954	1.280	0.957	1.044	2.335	2.558	1b 1 7 14 8 13 17 19
168	0.	1.926	1.266	0.933	1.014	2.235	2.454	1b 1 7 14 8 13 17 19
174	0.	1.738	1.307	0.932	0.999	2.175	2.393	1b 1 7 14 8 13 17 19
180	0.	1.992	1.509	1.164	1.137	2.494	2.745	1b 1 7 14 17 8 13 19
186	0.	1.999	1.605	1.292	1.171	2.564	2.819	1b 1 7 14 17 8 13 19
192	0.	2.003	1.720	1.416	1.206	2.640	2.902	1b 1 7 14 17 8 13 19
198	0.	1.812	1.384	1.108	0.949	2.280	2.469	1b 6 8 14 7 13 17 19
204	0.	1.701	1.325	1.049	0.903	2.156	2.338	1b 6 8 14 7 13 17 19
210	0.	1.634	1.286	1.013	0.876	2.050	2.257	1b 6 8 14 7 13 17 19
216	0.	1.602	1.267	0.995	0.864	2.043	2.218	1b 6 8 14 7 13 17 19
222	0.	1.604	1.262	0.994	0.864	2.041	2.217	1b 6 8 14 7 12 13 17 19
228	0.	1.639	1.270	1.007	0.878	2.074	2.252	1b 6 8 14 7 12 13 17 19
234	0.	1.709	1.293	1.035	0.905	2.143	2.326	1b 6 8 14 7 12 13 17 19
240	0.	1.731	1.267	0.971	0.989	2.146	2.363	1b 7 12 14 6 8 13 17 19
246	0.	1.779	1.284	1.034	0.900	2.194	2.371	1b 6 8 19 7 12 13 14 17
252	0.	1.784	1.167	0.917	0.811	2.147	2.295	12 14 17 24 18 6 7 8 13 19
258	0.	1.748	1.231	0.977	0.811	2.138	2.287	1b 6 8 19 7 12 13 14 17 24
264	0.	1.747	1.212	0.957	0.774	2.126	2.262	6 8 18 19 17 7 12 13 14 24
270	0.	1.885	1.231	0.959	0.949	2.251	2.443	17 12 14 24 6 7 8 13 18
276	0.	1.749	1.270	1.034	0.907	2.161	2.344	17 6 12 14 7 8 13 18 24
282	0.	1.677	1.244	1.004	0.881	2.091	2.269	17 6 12 14 7 8 13 18 24
288	0.	1.642	1.241	0.989	0.868	2.058	2.233	17 6 12 14 7 8 13 18 24
294	0.	1.640	1.245	0.990	0.867	2.059	2.234	17 6 12 14 7 8 13 18 24

Table 6 (Continued)

TIME (MM)	ALT (NM)	VDOOP	HDOOP	MDOOP	TDOOP	PDOOP	GDOOP	SATELLITES CHOSEN
300	0.	1.672	1.264	1.006	0.880	2.096	2.273	1/ 6 12 14 7 8 13 18 24
306	0.	1.741	1.299	1.042	0.907	2.172	2.354	1/ 6 12 14 7 8 13 18 24
312	0.	1.855	1.353	1.101	0.953	2.296	2.486	1/ 6 12 14 7 8 13 18 24
318	0.	1.947	1.373	1.115	0.971	2.382	2.573	1/ 6 14 18 7 8 12 13 24
324	0.	1.989	1.351	1.071	0.949	2.404	2.585	1/ 6 14 18 7 8 12 13 24
330	0.	2.033	1.336	1.033	0.926	2.433	2.603	1/ 6 14 18 7 8 12 13 24
336	0.	2.082	1.330	0.999	0.900	2.471	2.630	1/ 6 14 18 7 12 13 24
342	0.	1.781	1.386	1.056	1.036	2.257	2.483	1/ 6 11 13 7 12 18 24
348	0.	1.903	1.391	1.093	1.068	2.357	2.588	1/ 6 11 13 7 12 18 24
354	0.	1.919	1.331	1.005	1.005	2.335	2.563	1/ 6 13 18 7 11 12 24
360	0.	2.431	1.255	1.001	1.174	2.736	2.977	7 11 13 24 17 12 18
366	0.	1.919	1.331	1.005	1.005	2.335	2.542	1/ 8 11 24 7 13 17 18
372	0.	1.903	1.391	1.093	1.069	2.357	2.588	1/ 2 8 18 24 7 11 13 17
378	0.	1.782	1.386	1.056	1.037	2.257	2.484	1/ 8 18 24 7 11 13 17
384	0.	2.082	1.330	0.999	0.900	2.471	2.630	1/ 2 8 11 23 7 13 17 24
390	0.	2.033	1.336	1.032	0.926	2.433	2.603	1/ 2 8 11 23 6 7 13 17 24
396	0.	1.989	1.351	1.071	0.949	2.404	2.585	1/ 2 8 11 23 6 7 13 17 24
402	0.	1.947	1.373	1.114	0.971	2.382	2.573	1/ 2 8 11 23 6 7 13 17 24
408	0.	1.855	1.354	1.101	0.953	2.296	2.486	1/ 2 8 11 23 6 7 11 13 24
414	0.	1.742	1.299	1.042	0.907	2.172	2.354	1/ 2 8 11 23 6 7 11 13 24
420	0.	1.672	1.264	1.006	0.880	2.096	2.273	1/ 2 8 11 23 6 7 11 13 24
426	0.	1.640	1.245	0.990	0.867	2.059	2.234	1/ 2 8 11 23 6 7 11 13 24
432	0.	1.642	1.240	0.989	0.868	2.058	2.233	1/ 2 8 11 23 6 7 11 13 24
438	0.	1.677	1.249	1.004	0.880	2.091	2.269	1/ 2 8 11 23 6 7 11 13 24
444	0.	1.748	1.270	1.034	0.906	2.161	2.363	1/ 2 8 11 23 6 7 11 13 24

Table 6 (Continued)

TIME (W.N.)	ALT (NM)	VDOF	HDOF	MDOF	TDOF	PDOF	GDOF	SATELLITES CHOSEN
450	0.	1.885	1.232	0.959	0.949	2.252	2.443	12 13 17 23 6 7 6 11 24
450	0.	1.747	1.212	0.957	0.774	2.126	2.262	6 8 10 11 12 7 13 17 23 24
452	0.	1.748	1.231	0.977	0.811	2.138	2.287	11 6 8 10 7 12 13 17 23 24
454	0.	1.769	1.187	0.917	0.811	2.147	2.245	12 13 17 23 11 6 7 8 10 24
474	0.	1.779	1.284	1.034	0.900	2.194	2.371	11 6 8 10 7 12 17 23 24
480	0.	1.731	1.267	0.971	0.989	2.146	2.363	11 7 17 23 6 8 10 12 24
486	0.	1.709	1.293	1.035	0.905	2.143	2.326	11 6 8 23 7 10 12 17 24
492	0.	1.639	1.270	1.007	0.878	2.074	2.252	11 6 8 23 7 10 12 17 24
494	0.	1.605	1.262	0.994	0.865	2.041	2.217	11 6 8 23 7 10 12 17 24
504	0.	1.602	1.267	0.995	0.864	2.043	2.218	11 6 8 23 7 10 12 17 24
510	0.	1.633	1.288	1.013	0.876	2.080	2.257	11 6 8 23 7 10 12 24
516	0.	1.701	1.325	1.049	0.903	2.156	2.338	11 6 8 23 7 10 12 24
522	0.	1.812	1.384	1.108	0.949	2.280	2.469	11 6 8 23 7 10 12 24
528	0.	2.003	1.720	1.416	1.206	2.640	2.903	11 7 12 23 6 10 24
534	0.	2.000	1.605	1.292	1.171	2.564	2.619	11 7 12 23 6 10 24
540	0.	1.992	1.509	1.104	1.137	2.499	2.746	11 7 12 23 6 10 24
546	0.	1.738	1.307	0.933	0.999	2.175	2.393	11 5 7 23 6 10 12 24
552	0.	1.828	1.266	0.933	1.014	2.235	2.454	11 5 7 23 6 10 12 24
558	0.	1.953	1.279	0.957	1.044	2.335	2.558	11 5 7 23 6 10 12 24
564	0.	1.947	1.286	0.937	0.992	2.334	2.535	11 7 12 23 5 6 10 24
570	0.	1.939	1.261	0.949	0.955	2.313	2.503	11 7 12 23 5 6 10 24
576	0.	1.866	1.274	1.017	0.862	2.259	2.418	11 7 9 12 5 6 10 23 24
582	0.	1.877	1.267	0.897	0.859	2.265	2.422	10 7 9 12 5 6 11 23 24
588	0.	2.290	1.200	0.893	1.177	2.585	2.841	5 7 10 23 6 9 11 24
594	0.	2.379	1.225	0.914	1.230	2.675	2.945	5 7 10 23 6 9 11 24

Table 6 (Continued)

TIME (HH)	ALT (NM)	VDDP	HDDP	MDDP	TDDP	PDDP	GDDP	SATELLITES CHOSEN
600	0.	2.527	1.266	0.940	1.311	2.826	3.115	5 7 10 23 6 9 11 24
606	0.	2.750	1.326	0.971	1.428	3.054	3.371	5 7 10 23 6 9 11 24
612	0.	3.081	1.420	1.010	1.598	3.393	3.750	5 7 10 23 6 9 11 24
618	0.	2.982	1.536	1.169	1.587	3.354	3.711	6 9 11 24 5 7 10 23
624	0.	2.662	1.419	1.093	1.414	3.017	3.332	6 9 11 24 5 7 10 23
630	0.	2.448	1.336	1.034	1.296	2.789	3.075	6 9 11 24 5 7 10 23
636	0.	2.308	1.278	0.985	1.214	2.638	2.904	6 9 11 24 5 7 10 23
642	0.	2.225	1.237	0.945	1.160	2.546	2.798	6 9 11 24 5 7 10 23
648	0.	2.104	1.206	0.912	1.083	2.431	2.661	6 7 9 11 5 10 23 24
654	0.	1.824	1.317	0.958	0.860	2.249	2.403	6 4 7 9 5 10 11 23 24
660	0.	1.939	1.165	0.896	0.955	2.273	2.465	6 7 9 11 4 5 10 23 24
666	0.	1.884	1.181	0.895	0.904	2.223	2.400	6 7 9 11 5 4 10 23 24
672	0.	1.984	1.215	0.878	1.032	2.327	2.545	5 9 11 24 4 6 10 23
678	0.	1.658	1.227	0.875	1.002	2.227	2.442	5 9 11 24 4 6 10 23
684	0.	1.769	1.251	0.921	0.988	2.166	2.381	5 9 11 24 4 6 10 23
690	0.	1.631	1.344	1.116	0.885	2.113	2.291	5 9 11 23 4 6 10 24
696	0.	1.581	1.316	1.082	0.870	2.058	2.234	5 9 11 23 4 6 10 24
702	0.	1.994	1.744	1.437	1.195	2.049	2.406	5 4 7 24 6 10 23
708	0.	1.969	1.796	1.495	1.217	2.664	2.929	5 9 10 24 4 6 23
714	0.	1.954	1.810	1.513	1.251	2.663	2.943	5 9 10 24 4 6 23
720	0.	2.012	1.843	1.554	1.328	2.729	3.035	5 9 23 24 4 6 10

EXAMPLE: DATA SET FOR CASE III ("ZENITH" SATELLITE USED IN ALL CALCULATIONS)*

* This example is contrived only to show what the global calculations output would look like. There are only two time points in this run--0 and 250 minutes. No "snapshot" calculations were made.

Table 7 (Continued)

ORBITAL ELEMENTS

	ECC	ARGP	RASC	INC	ANOM	PER
1	0.0	0.0	0.0	63.00	0.0	12.00
2	0.0	0.0	0.0	63.00	45.00	12.00
3	0.0	0.0	0.0	63.00	90.00	12.00
4	0.0	0.0	0.0	63.00	135.00	12.00
5	0.0	0.0	0.0	63.00	180.00	12.00
6	0.0	0.0	0.0	63.00	225.00	12.00
7	0.0	0.0	0.0	63.00	270.00	12.00
8	0.0	0.0	0.0	63.00	315.00	12.00
9	0.0	0.0	120.00	63.00	15.00	12.00
10	0.0	0.0	120.00	63.00	60.00	12.00
11	0.0	0.0	120.00	63.00	105.00	12.00
12	0.0	0.0	120.00	63.00	150.00	12.00
13	0.0	0.0	120.00	63.00	195.00	12.00
14	0.0	0.0	120.00	63.00	240.00	12.00
15	0.0	0.0	120.00	63.00	285.00	12.00
16	0.0	0.0	120.00	63.00	330.00	12.00
17	0.0	0.0	240.00	63.00	30.00	12.00
18	0.0	0.0	240.00	63.00	75.00	12.00
19	0.0	0.0	240.00	63.00	120.00	12.00
20	0.0	0.0	240.00	63.00	165.00	12.00
21	0.0	0.0	240.00	63.00	210.00	12.00
22	0.0	0.0	240.00	63.00	255.00	12.00
23	0.0	0.0	240.00	63.00	300.00	12.00
24	0.0	0.0	240.00	63.00	345.00	12.00

GLOBAL DISTRIBUTION CALCULATIONS

MASKING ANGLE = 5.00 DEGREES

LATITUDE STEP = 5.00 DEGREES

LATITUDE INCREMENT = 1

LONGITUDE INCREMENT = 1

DILUTION OF PRECISION PARAMETERS PRINTED AT TIME INCREMENT OF 0

TOTAL TIME(MIN) = 250

TIME INCREMENT(MIN) = 250

THE SATELLITE MOST NEARLY OVERHEAD IS USED AS ONE OF THE FOUR
IN ALL CALCULATIONS OF THE VOLUME OF THE TETRAHEDRON

Table 7 (Continued)

ELEVATION DISTRIBUTION - PROBABILITY THAT THE SATELLITE IN VIEW WILL HAVE ELEVATION ANGLES AS LISTED

ELEVATION ANGLE										
0-5	5-10	10-15	15-20	20-25	25-30	30-35	35-40	40-45	45-50	50-55
0.0	0.0	10.3	9.8	9.2	9.1	7.8	8.2	6.8	6.4	6.2

LATITUDE ELEVATION DISTRIBUTION
PROBABILITY THAT ANY SATELLITE IN VIEW WILL HAVE AN ELEVATION ANGLE GREATER THAN OR EQUAL TO THOSE LISTED

LATITUDE										
ELEVATION ANGLE	90	85	80	75	70	65	60	55	50	45
0	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
5	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
10	0.74	0.72	0.91	0.92	0.90	0.91	0.90	0.87	0.88	0.85
15	0.83	0.85	0.84	0.82	0.82	0.81	0.77	0.75	0.78	0.76
20	0.78	0.77	0.76	0.75	0.73	0.73	0.69	0.67	0.69	0.66
25	0.72	0.69	0.67	0.66	0.65	0.62	0.58	0.56	0.57	0.60
30	0.61	0.61	0.59	0.57	0.54	0.50	0.49	0.49	0.50	0.52
35	0.56	0.52	0.51	0.48	0.42	0.42	0.42	0.43	0.45	0.46
40	0.39	0.43	0.40	0.36	0.35	0.35	0.35	0.37	0.38	0.38
45	0.33	0.34	0.29	0.27	0.28	0.30	0.31	0.31	0.33	0.33
50	0.28	0.20	0.20	0.22	0.23	0.24	0.25	0.26	0.26	0.27
55	0.06	0.10	0.13	0.16	0.17	0.18	0.19	0.21	0.21	0.22
60	0.0	0.02	0.07	0.10	0.12	0.14	0.15	0.16	0.17	0.18
65	0.0	0.0	0.02	0.07	0.08	0.11	0.11	0.13	0.14	0.15
70	0.0	0.0	0.0	0.02	0.05	0.07	0.09	0.07	0.07	0.07
75	0.0	0.0	0.0	0.0	0.03	0.05	0.06	0.05	0.05	0.05
80	0.0	0.0	0.0	0.0	0.02	0.03	0.02	0.02	0.02	0.02
85	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

ACCUMULATIVE ELEVATION DISTRIBUTION
PROBABILITY THAT THE ELEVATION ANGLE IS GREATER THAN OR EQUAL TO THOSE LISTED

ELEVATION ANGLE										
0	5	10	15	20	25	30	35	40	45	50
0.0	1.0	0.9	0.8	0.7	0.6	0.5	0.4	0.3	0.2	0.1

Table 7 (Continued)
DILUTION OF PRECISION - ACCUMULATIVE LATITUDE
PROBABILITY THAT ALTITUDE DOP WILL BE GREATER
THAN NUMBER LISTED

Table 7 (Continued)
 DILUTION OF PRECISION - ACCUMULATIVE LATITUDE DISTRIBUTION
 PROBABILITY THAT POSITION DOP IN HORIZONTAL PLANE WILL BE GREATER THAN NUMBER LISTED

Table 7 (Continued)

DISTRIBUTION OF PRECISION - ACCUMULATIVE LATITUDE DISTRIBUTION THAT LARGER COMPONENT OF POSITION DOP WILL BE GREATER THAN NUMBER LISTED

Table 7 (Continued)
ACCUMULATIVE LATITUDE DISTRIBUTION
PROBABILITY THAT TIME DOP WILL BE GREATER THAN NUMBER LISTED
CONDITION OF PRECISION

Table 7 (Continued)

ILLUSTRATION OF PRECISION - ACCUMULATIVE LATITUDE DISTRIBUTION
PROBABILITY THAT THREE DIMENSIONAL POSITION DOP WILL BE GREATER THAN NUMBER LISTED

Table 7 (Continued)

Table 7 (Continued)

DILUTION OF PRECISION PARAMETERS - ACCUMULATIVE GLOBAL DISTRIBUTION

NUMBER	VDDP	HDDP	MDDP	TDDP	PDDP	GDDP
0.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
0.2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
0.4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
0.6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
0.8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1.2	1.0000	1.0000	0.6939	0.5826	1.0000	1.0000
1.4	0.9973	0.4683	0.1174	0.2360	1.0000	1.0000
1.6	0.9254	0.2297	0.0353	0.1584	1.0000	1.0000
1.8	0.7123	0.0794	0.0173	0.1243	1.0000	1.0000
2.0	0.4915	0.3234	0.0039	0.0175	0.9879	1.0000
2.2	0.3299	0.0039	0.0	0.0	0.8051	0.9786
2.4	0.2375	0.0	0.0	0.0	0.5256	0.7697
2.6	0.1865	0.0	0.0	0.0	0.3519	0.5281
2.8	0.1183	0.0	0.0	0.0	0.2430	0.3888
3.0	0.0875	0.0	0.0	0.0	0.1997	0.3005
3.2	0.0641	0.0	0.0	0.0	0.1529	0.2236
3.4	0.0312	0.0	0.0	0.0	0.1043	0.1913
3.6	0.0113	0.0	0.0	0.0	0.0746	0.1697
3.8	0.0030	0.0	0.0	0.0	0.0262	0.1186
4.0	0.0	0.0	0.0	0.0	0.0084	0.0769
4.2	0.0	0.0	0.0	0.0	0.0059	0.0385
4.4	0.0	0.0	0.0	0.0	0.0046	0.0059
4.6	0.0	0.0	0.0	0.0	0.0	0.0
4.8	0.0	0.0	0.0	0.0	0.0	0.0
5.0	0.0	0.0	0.0	0.0	0.0	0.0
5.2	0.0	0.0	0.0	0.0	0.0	0.0
5.4	0.0	0.0	0.0	0.0	0.0	0.0
5.6	0.0	0.0	0.0	0.0	0.0	0.0
5.8	0.0	0.0	0.0	0.0	0.0	0.0
6.0	0.0	0.0	0.0	0.0	0.0	0.0
6.2	0.0	0.0	0.0	0.0	0.0	0.0
6.4	0.0	0.0	0.0	0.0	0.0	0.0
6.6	0.0	0.0	0.0	0.0	0.0	0.0
6.8	0.0	0.0	0.0	0.0	0.0	0.0
7.0	0.0	0.0	0.0	0.0	0.0	0.0

Table 7 (Continued)

BY A GLOBAL BASIS THE PROBABILITY (IN PERCENT) THAT EXACTLY N SATELLITES WILL BE SEEN

卷之三

Table 7 (Continued)

MAXIMUM AND MINIMUM NUMBERS SEEN AT EACH LATITUDE & LONGITUDE

Appendix A
NAVSAT SELECTION ALGORITHMS FOR A SATELLITE USER

This appendix describes the algorithms used to select, from all of the navsats in view of a satellite user, those most likely to yield small DOP values. These algorithms were developed to reduce computation costs, accomplished by selecting a value for the input parameter C ($0 < C < 1$), which is the fraction of the area of a sphere with radius equal to the orbital radius of the navsats. If the navsat system orbital configuration involves elliptic orbits, these algorithms cannot be used and C should be set equal to one.* Also, computation costs can be reduced further, with little sacrifice in position determination accuracy, if the zenith/nadir satellite selection mode is used to reduce computation time.

If the navsat orbital configuration involves more than one circular orbit altitude (a "multishell" system) and the satellite user is above all of the shells, the algorithm can be used as presented below. If the satellite user is between or below the shells part of the time, the situation is more complex because there are two possible values for θ_T (see below)--one for the "zenith" navsat on the same side of the earth as the user, and one for the "nadir" navsat on the other side of the earth from the user. In this case, suitable values of C can be obtained by careful consideration of the user/navsat system relative geometries. As with elliptic orbit navsats, C can be set equal to one, and the zenith/nadir navsat selection mode can be used to minimize computation time.

The following is a description of the algorithms for use with any satellite user orbit, as long as the navsat system uses a single altitude, circular orbit. The number of navsats considered for use after the zenith/nadir navsat is selected by C; the larger C is, the larger the number of navsats considered. Values of C from 0.4 to 0.6 generally yield good results.

* The algorithms can be used if the satellite user is always above or below all of the navsats and the value of R, which is used in the expression to obtain θ_T , is representative of the navsat orbits. (For example, set R equal to the average of the semimajor axes of the navsat orbits.) This would require a minor modification of the computer program.

The two algorithms derived below, one for the satellite user above the navsats and the other for the satellite user below, use the same criteria for selecting the first navsat of the four to be used for the computation of the DOPs, i.e., the satellite, of those in view of the user, which is closest to the user's zenith or nadir. However, the criteria for selecting the remaining three satellites are not the same for the two algorithms.

SELECTION OF THE FIRST NAVSAT

For convenience of explanation, Fig. A-1 shows the user above the navsats, the spherical surface containing the navsats, and the earth plus 200 n mi of atmosphere (hereafter called earth). Also, the shaded area that is shown will contain the navsats which are retained for the computation of the DOPs, as we will describe later.

At each time point, the angles θ_n and β_n are computed for each user and navsat combination from

$$\theta_n = \cos^{-1} \left(\frac{\bar{R} \cdot \bar{P}}{RP} \right)^* \quad \text{and} \quad (A-1)$$

$$\beta_n = \cos^{-1} \left(\frac{-\bar{U} \cdot \bar{P}}{UP} \right) .$$

If $\theta_n > \phi$, where $\phi = \cos^{-1} \left(\frac{r}{R} \right) + \cos^{-1} \left(\frac{r}{P} \right)$, then the satellite is obscured from the user's view by the earth and is discarded from further consideration until the next step.

If the angle α , which is equal to $\pi - (\theta_n + \beta_n)$, is greater than the navsat antenna beam half-angle, then the user satellite will not be illuminated by the navsat antenna beam and the navsat will not be used in the calculations.

The angle β_1 , corresponding to the first satellite not obscured by the earth, and the number of the satellite are stored. Subsequent β 's are computed and compared to the β in storage, and the satellite yielding the smallest β is the first of the four navsats used for the computation of DOP values.

* $P = |\bar{P}|$ (the length of \bar{P}) and $R = |\bar{R}|$ (the length of \bar{R}).

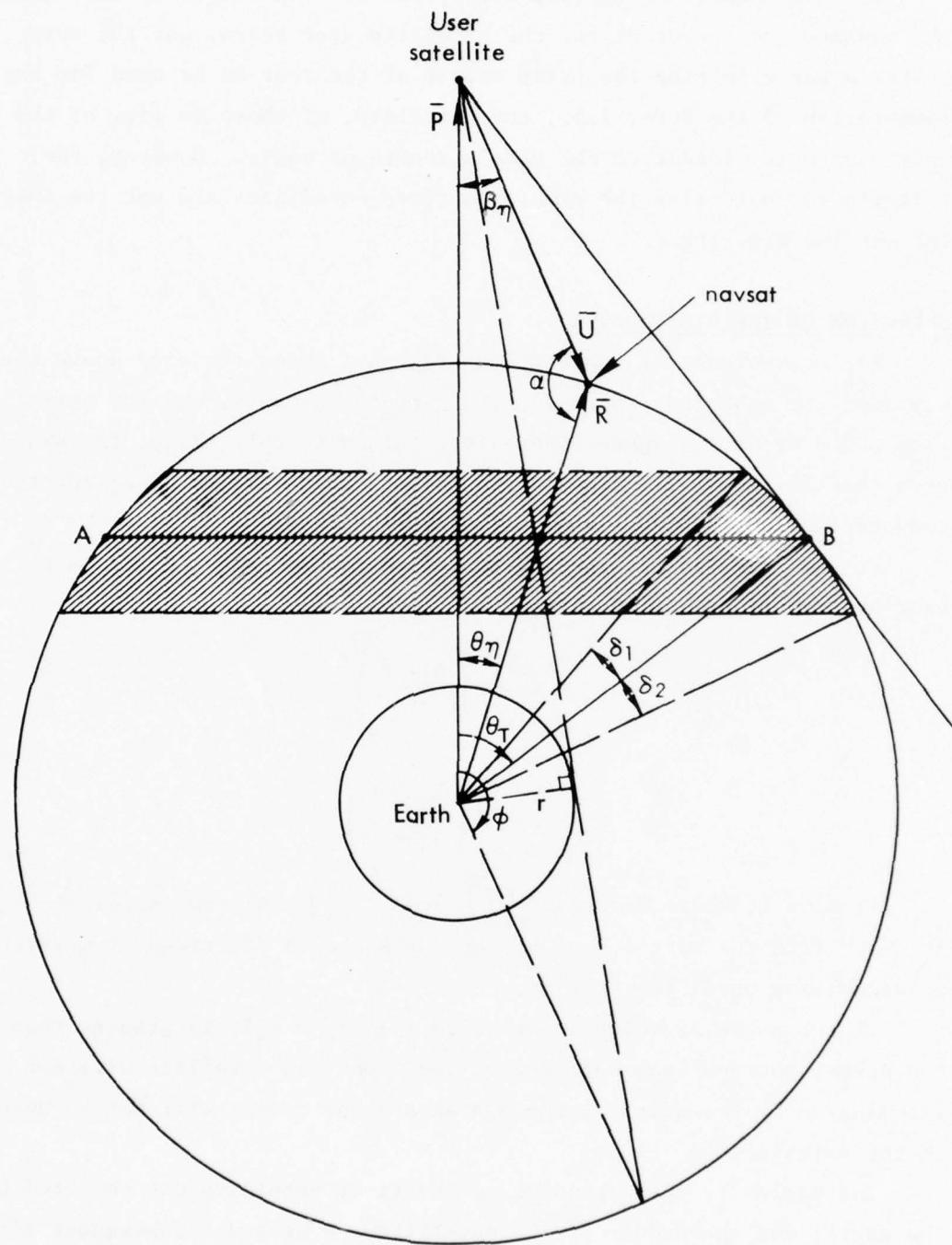


Fig. A-1—Satellite user above the navsat altitude

For the axis of the navsat antenna pointing toward the center of the earth, it is clear that any navsat above the plane represented by line A-B in Fig. A-1 must have an antenna beam with half-angle greater than 90 deg in order to illuminate the satellite user. If the navsat is below the plane, the antenna beam half-angle required will be less than 90 deg.

SATELLITE USER ABOVE THE NAVSAT SYSTEM

If the remaining three navsats needed for the GDOP computations are on or near the tangent circle A-B (Fig. A-1) and are separated in longitude by 120 deg, then the volume of the tetrahedron formed, as shown in Fig. A-2 (a,b,c,d), will be a near maximum and the corresponding PDOP values will (almost always) be minimum.* The probability that the three satellites will be so arranged is small; thus, all of the satellites in a band (similar to a band between two parallels of latitude) containing the tangent circle, and whose width corresponds to the sum of the central angles δ_1 and δ_2 , are retained for the selection of the three remaining satellites. The satellites not in this band are discarded from further consideration until the next time point. The angles δ_1 and δ_2 are obtained from

$$\delta_1 = \sin^{-1} \left(\frac{c}{\sin \theta_T} \right) \quad \text{if } \sin^2 \theta_T > c , \quad (\text{A-2})$$

where $\cos \theta_T = |\bar{R}| / |\bar{P}|$, and $\delta_2 = \delta_1$; or

$$\delta_1 = \theta_T \quad \text{if } \sin^2 \theta_T \leq c , \quad (\text{A-3})$$

and

$$\delta_2 = \cos^{-1} \left(1 - 2c \right) - \theta_T .$$

The central angle $\theta_T = \cos^{-1} \left(\frac{R}{P} \right)$ is shown in Fig. A-1. The quantity $0 < c < 1$ (an input quantity) represents the ratio of the area of

* The tangent circle A-B, between a cone with apex at the user's position and the spherical surface containing the navsats, corresponds to the maximum value β_n can have.

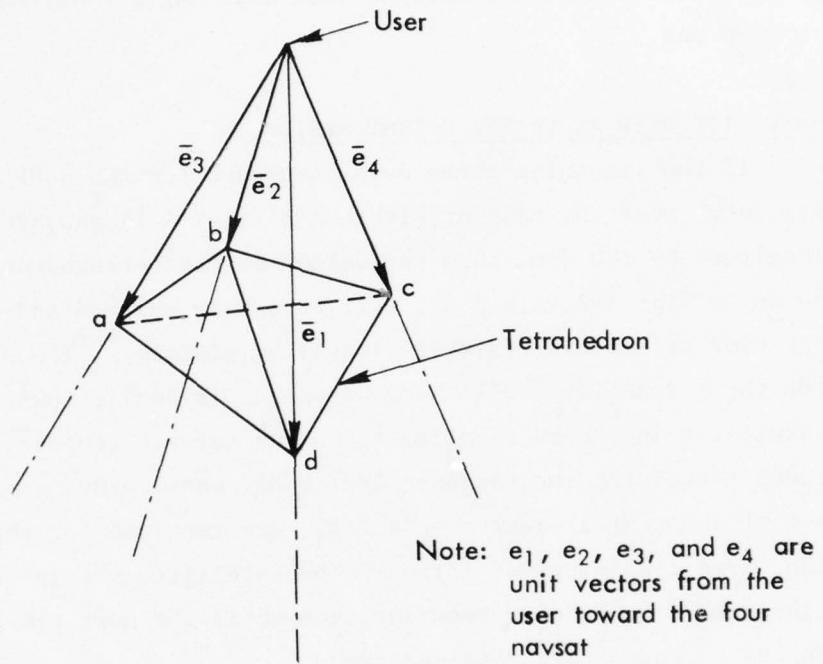


Fig.A-2—Tetrahedron formed by the ends of unit vectors from a satellite user toward four navsats

the band to the area of the sphere containing the navsats. If the satellites are uniformly distributed, the number of navsats in the band will be the product of C times the total number of navsats. Thus, for $C = 0.25$, the number of GPS satellites in the band (on the average) would be 6. Since the navsats are not usually uniformly distributed, $C \approx 0.5$ should ensure that there will be an adequate number of navsats available.

SATELLITE USER BELOW THE NAVSAT SYSTEM ALTITUDE

The characteristics of the algorithm for satellite selection for a satellite user below the navsats, as shown in Fig. A-3, are not readily apparent if it is desirable to reduce the computational effort that results when all satellites in view are taken four at a time. The number of different combinations of four satellites can be large. For example, a user near the altitude of GPS will, on the average, see 22 of the 24 GPS satellites, and the number of different combinations of four will be 7315.

The satellite selection algorithm presented here and used in the program is based on the simplifying assumptions that the first of the four satellites to be used for computing GDOP values is the one nearest the user's zenith (or nadir) and that the other three satellites are in or near a plane which is normal to the vector \bar{P} . The additional program statements required to select the *optimum* orientation of the plane were not used because of singularity problems that could occur when the user is just below the navsat altitude.*

Figure A-3 shows the orbit containing the first of the four navsats chosen for the tetrahedron volume computation and the band, on the spherical surface containing the navsats, which will be used to select the other three navsats.

The angles δ_1 and δ_2 are determined as before, except θ_T is now computed from

$$\theta_T = \rho + \cos^{-1} \left(\frac{|\bar{P}|}{|\bar{R}|} \cos \rho \right),$$

* If obtaining minimum GDOP values is essential, it is recommended that the algorithm be ignored and that all possible combinations of four satellites be examined.

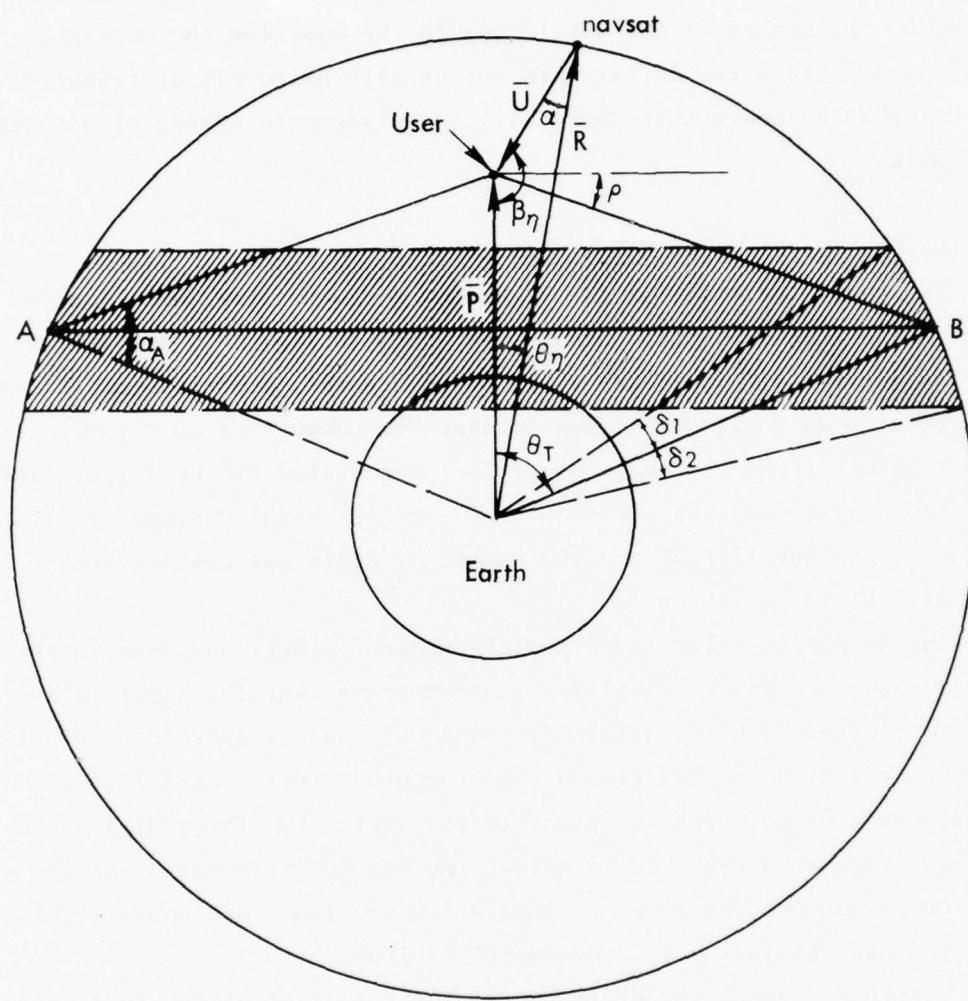


Fig. A-3—Orientation with satellite user
below the navsat altitude

where ρ is the angle between the user's horizontal and a line from the user to the circle represented by the line A-B in Fig. A-3. If the first navsat chosen is on the user's vertical, then it can be shown that the optimum value for ρ is about 19.5 deg. This value of ρ will maximize the volume of the tetrahedron formed by joining the tips of the four unit vectors which point from the user to the four navsats. If the first chosen navsat is above the user's horizontal (as shown in the figure), the angle ρ will be below the user's horizontal--and vice versa.

Figure A-3 shows that the half-angle of the navsat antenna beam, which is directed toward the center of the earth, must be as large as the angle α if the user satellite is to receive ranging information from a navsat located at point A.

Appendix B
PROGRAM LISTING

1. MAIN	[pages 65-77]
2. ORBINI(I)	[page 78]
3. ORBIT(I,T,R,VEL,AC)	[pages 79-80]
4. TRMATX(TR,I)	[page 81]
5. MATMUL(T,V,O)	[page 82]
6. POINT(ALO,ALA,TIM,VEC)	[page 83]
7. TAAT(MAX,KXX,MATRIX)	[page 84]
8. VOLUME(OVEC,IDSAT,VOL)	[page 85]
9. COVNAV(G, ID,NAT,SIG)	[page 86]
10. BLOCK DATA	[page 87]
11. VECTOR(V1,I,V2,V3)	[page 88]
12. DOT(V1,V2)	[page 89]
13. UNIVEC(V,UV)	[page 90]
14. TALL(KOT,KXX,MATRIX)	[page 91]

MAIN

```
COMMON/ORBIS/P(37,25)/CON/C(18)
DIMENSION AA(3),G(37,4),IOS(37),ISIC(4),KXX(58905,4),NSGD(37),R(3)
1,RF(3),RMX(37,3),SIGT(6),U(3),UPV(3),USUV(37,3),UTS(3),VE(3),Z(3),
2 YE(3),XN(3),ISAVE(37),IINT(37),UEL(37),IOUT(37),STN(3)
DIMENSION QSR(36),CAG(19,18),GLEB(18),PIB(18),ACLAT(19,36),
1 ACTOT(36),OBLAT(19,36),UBDIS(36),CL(19),MIN(19,36),MAX(19,36),
2 CAGX(19,18),NSPL(19),SKEG(19,36,6),SKEGX(19,36,6),GLOS(6,36),
3 CDOP(19,36,6),ISAPP(32),PER(36)
REAL LAT,LONG,LATDEG,LADG,LAD
KTR=48
IPRINT=0
Z(1)=0.
Z(2)=0.
Z(3)=1.E+10
C
C LOC=1; USER ON SATELLITE
C LOC=2; USER ON GROUND AT SPECIFIED LATITUDE AND LONGITUDE
C LOC=3; GLOBAL CALCULATIONS
C
READ (5,175) LOC,NJL,ISCMP
GO TO (100,110,120), LOC
C
100 DO 105 K=1,5
READ (5,180) (P(N,K),N=1,NJL)
105 CONTINUE
READ (5,180) (PER(N),N=1,NJL)
NJM=NJL+1
READ (5,180) (P(NJM,K),K=1,5)
READ (5,185) PER(NJM),AIN,CK
READ (5,175) INC,ITF
GO TO 155
C
110 DO 115 K=1,5
READ (5,180) (P(N,K),N=1,NJL)
115 CONTINUE
READ (5,180) (PER(N),N=1,NJL)
READ (5,185) ATL,ONGL,ELEVAT
READ (5,175) INC,ITF
GO TO 155
C
120 DO 125 K=1,5
READ (5,180) (P(N,K),N=1,NJL)
125 CONTINUE
READ (5,180) (PER(N),N=1,NJL)
READ (5,185) LATDEG,ELEVAT
READ (5,175) LATIC,LONIC,INC,ITF,IPFREQ,ITIME
DO 135 MA=1,19
CL(MA)=0.
NSPL(MA)=0
DO 130 MB=1,36
MIN(MA,MB)=30
MAX(MA,MB)=0
DO 130 MC=1,6
SKEGX(MA,MB,MC)=0.
CDOP(MA,MB,MC)=0.
130 SKEG(MA,MB,MC)=0.
DO 135 MD=1,18
CAGX(MA,MD)=0.
```

MAIN

```
135 CAG(MA,MD)=0.  
    DC 140 MA=1.36  
    DO 140 MB=1.6  
140 GLOS(MB,MA)=0.  
    DO 150 MA=1.19  
    ACTOT(MA)=0.  
    OBDIS(MA)=0.  
    DO 145 MD=1.36  
    ACLAT(MA,MD)=0.  
145 OBLAT(MA,MD)=0.  
150 GLEB(MA)=0.  
  
C 155 CONTINUE  
    WRITE (6,195)  
    WRITE (6,190)  
    DO 160 IP=1,NJL  
    WRITE (6,215) (IP,(P(IP,IV),IV=1,5),PER(IP))  
160 CONTINUE  
    IF(LOC.EQ.1) WRITE (6,200)  
    IP=NJL+1  
    IF(LOC.EQ.1) WRITE (6,215) (IP,(P(IP,IV),IV=1,5),PER(IP))  
    IF(LOC.EQ.2) WRITE (6,210) ATL,ONGL,ELEVAT  
    IF(LOC.EQ.3) WRITE (6,205) ELEVAT,LATDEG,LATIC,LONIC,ITIME  
    ITT=(ITF-1)*INC  
    WRITE (6,220) ITT,INC  
    IF(LOC.EQ.1) WRITE (6,225) AIN,CK  
    IF(LOC.EQ.1.AND.ISCMP.EQ.0) WRITE (6,166)  
    IF(LOC.NE.1.AND.ISCMP.EQ.0) WRITE (6,165)  
    IF(ISCMP.EQ.1) WRITE (6,170)  
  
C  THE FOLLOWING FORMATS HAVE TO DO WITH INPUT  
C  
165 FORMAT(1H0,10X,'THE SATELLITE MOST NEARLY OVERHEAD IS USED AS ONE  
1OF THE FOUR',//,11X,'IN ALL CALCULATIONS OF THE VOLUME OF THE TETRAH  
2EDRON')  
166 FORMAT(1H0,10X,'THE SATELLITE MOST NEARLY ABOVE OR BELOW IS USED A  
1S ONE OF THE FOUR',//,11X,'IN ALL CALCULATIONS OF THE VOLUME OF THE  
2TETRAHEDRON')  
170 FORMAT(1H0,10X,'ALL SATELLITES, TAKEN FOUR AT A TIME, ARE USED IN'  
1,//,11X,'THE CALCULATIONS OF THE VOLUME OF THE TETRAHEDRON')  
175 FORMAT(10I5)  
180 FORMAT(12F6.0)  
185 FORMAT(7F10.0)  
190 FORMAT(1H0,22X,' ECC',5X,'ARGP',4X,'RASC',4X,'INC',5X,'ANOM',4X,  
1'PER',//)  
195 FORMAT(1H1,//32X,'ORBITAL ELEMENTS')  
200 FORMAT(1H0,10X,'USER SATELLITE ORBITAL ELEMENTS')//  
205 FORMAT(1H0,10X,'GLOBAL DISTRIBUTION CALCULATIONS',//,  
1 11X,'MASKING ANGLE = ',F6.2,' DEGREES',//,  
2 11X,'LATITUDE STEP = ',F6.2,' DEGREES',//,  
3 11X,'LATITUDE INCREMENT = ',I3,//,  
4 11X,'LONGITUDE INCREMENT = ',I3,//,  
5 11X,'DILUTION OF PRECISION PARAMETERS PRINTED AT TIME INCREMENT 0  
6F ',I5)  
210 FORMAT(1H0,10X,'USER LOCATION ON EARTH',//11X,  
1      'LATITUDE = ',F5.2,' DEGREES',//,11X,'LONGITUDE = ',F5.2,  
2      ' DEGREES',//,11X,'MASKING ANGLE = ',F6.2,' DEGREES')  
215 FORMAT(1H ,15X,I3,1X,6F8.2)
```

MAIN

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220 FORMAT(1H0,10X,'TOTAL TIME(MIN) = ',I5,/ ,11X,
      1  'TIME INCREMENT(MIN) = ',I3)
225 FORMAT(1H ,10X,'BEAMWIDTH ANGLE(DEG) = ',F6.2,/ ,11X,
      1  'FRACTION OF NAVSAT SPHERICAL AREA = ',F6.3)
C
C  SET UP ORBITAL ELEMENTS
C
      DO 230 N=1,NJL
      P(N,22)=22808.*(PER(N)/24.)**(2./3.)
      CALL ORBINI (N)
230 CONTINUE
      IF(LOC.EQ.2.OR.LOC.EQ.3) GO TO 235
      P(IP,22)=22808.*(PER(IP)/24.)**(2./3.)
      CALL ORBINI (IP)
235 CONTINUE
      INCA=0
      NSTO=0
      MAXNSS=0
      DO 625 IT=1,ITF
      TID=FLOAT(INCA)/1440.
      INCA=INCA+INC
      NN=IP
      IF(LOC.EQ.2.OR.LOC.EQ.3) NN=NJL
      DO 240 N=1,NN
      CALL ORBIT (N,TID,PER,RF,VE,AA)
      DO 240 IV=1,3
      RMX(N,IV)=RF(IV)
240 CONTINUE
      IF(LOC.EQ.2) GO TO 335
      IF(LOC.EQ.3) GO TO 330
C
C
      DO 245 IV=1,3
      UPV(IV)=RMX(IP,IV)
245 CONTINUE
      IK=0
      BETAMN=4.000000
      DO 265 N=1,NJL
      DO 250 IV=1,3
      R(IV)=RMX(N,IV)
250 CONTINUE
      CALL VECTOR (R,2,UPV,UTS)
      AR=SQRT(DOT(R,R))
      AP=SQRT(DOT(UPV,UPV))
      A=ARCCOS(2.0926144E+07/AR)
      IF(AP.LE.2.0926144E+07) WRITE(6,251)
251 FORMAT(1H ,/,3X,'TERMINATION OF RUN, ALTITUDE APPROCHING ZERO')
      IF(AP.LE.2.0926144E+07) STOP
      B=ARCCOS(2.0926144E+07/AP)
      PHI=A+B
      DOTRP=DOT(R,UPV)
      THETN=ARCCOS(DOTRP/(AR*AP))
      IF(THETN.GE.PHI) GO TO 265
      IK=IK+1
      ISAVE(IK)=N
      AU=SQRT(DOT(UTS,UTS))
      DOTUP=DOT(UTS,UPV)
      BETAN=ARCCOS(-DOTUP/(AU*AP))
```

MAIN

```
AIWID=AIN/C(2)
BWIDTH=C(3)-(THETN+BETAN)
IF(AIWID.LT.BWIDTH) GO TO 265
BETASV=BETAN
IF(BETAN.GT.C(5)) BETAN=C(3)-BETAN
255 IF(BETAN.LT.BETAMN) GO TO 260
GO TO 265
260 ISATNO=N
BETAMN=BETAN
BETAS=BETASV
265 CONTINUE
DO 285 IK=1,IK
IF(ISAVE(I).EQ.ISATNO) GO TO 270
GO TO 285
270 INDX=I
DO 275 KI=1,INDX
KII=KI+1
IINT(KII)=ISAVE(KI)
275 CONTINUE
INDX=INDX+1
DO 280 KI=INDX,IK
IINT(KI)=ISAVE(KI)
280 CONTINUE
GO TO 290
285 CONTINUE
290 IINT(1)=ISATNO
IF(ISCMP.EQ.1) GO TO 335
C
C THE NUMBERS OF THE SATELLITES WHICH FIT CRITERIA FOR USE, PLUS THE
C ONE NEAREST TO OVERHEAD HAVE BEEN CALCULATED
C
IOS(1)=IINT(1)
NSS=1
DO 295 IV=1,3
R(IV)=RMX(IINT(1),IV)
295 CONTINUE
CALL VECTOR (R,2,UPV,UTS)
CALL UNIVEC (UTS,U)
DO 300 IV=1,3
USUV(IINT(1),IV)=U(IV)
300 CONTINUE
DO 325 N=2,IK
DO 305 IV=1,3
R(IV)=RMX(IINT(N),IV)
305 CONTINUE
CALL VECTOR (R,2,UPV,UTS)
CALL UNIVEC (UTS,U)
DO 310 IV=1,3
USUV(IINT(N),IV)=U(IV)
310 CONTINUE
AR=SQRT(DOT(R,R))
AP=SQRT(DOT(UPV,UPV))
IF(AP.GT.AR) THETT=ARCOS(AR/AP)
IF(AP.LE.AR.AND.BETAS.GT.C(5)) THETT=109.5/C(2)-ARSIN(AP*.33380686
/AR)
IF(AP.LE.AR.AND.BETAS.LE.C(5)) THETT=70.5/C(2)-ARSIN(AP*.33380686/
AR)
DOTRP=DOT(R,UPV)
```

MAIN

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THETN=ARCCOS(DOTRP/(AR*AP))
SINTT=SIN(THETT)
SINTSQ=SINTT**2
IF(SINTSQ.GT.CK) GO TO 315
DELONE=THETT
ANG=1.-(CK/.5)
DELTWO=ARCCOS(ANG)-THETT
GO TO 320
315 CONTINUE
DELONE=ARSIN(CK/SINTT)
DELTWO=DELONE
320 IF(THETN.LT.(THETT-DELONE)) GO TO 325
IF(THETN.GT.(THETT+DELTWO)) GO TO 325
NSS=NSS+1
IOS(NSS)=I INT(N)
325 CONTINUE
IF(NSS.LE.4) GO TO 625
GO TO 335
C
C END OF USER ON SATELLITE
C
C CALCULATIONS FOR USER ON EARTH AT SPECIFIED LAT AND LONG, AND GLOBAL
C DISTRIBUTIONS FOLLOW
330 CONTINUE
LKL=36
LLL=19
335 CONTINUE
IF(LOC.EQ.2.OR.LOC.EQ.1) LKL=1
IF(LOC.EQ.2.OR.LOC.EQ.1) LLL=1
DO 500 K=1,LKL,LONIC
DO 500 L=1,LLL,LATIC
IF(LOC.EQ.1.AND.ISCMP.EQ.0) GO TO 400
IF(LOC.EQ.1.AND.ISCMP.EQ.1) GO TO 375
LONG=FLOAT(K-1)*10.
LAT=90.-FLOAT(L-1)*LATDEG
IF(LOC.EQ.2) LONG=0NGL
IF(LOC.EQ.2) LAT=ATL
CALL POINT (LONG,LAT,TID,UPV)
NSS=0
CL(L)=CL(L)+1.
DO 350 N=1,NJL
DO 340 IV=1,3
R(IV)=RMX(N,IV)
340 CONTINUE
CALL VECTOR (UPV,2,R,STN)
SE=-DOT(STN,UPV)/SQRT(DOT(STN,STN)*DOT(UPV,UPV))
IFI(ABS(SE).GE..9999999) SE=SIGN(1.,SE)
EL=ARSIN(SE)*C(2)
IFI(EL.LT.ELEVAT) GO TO 350
NSS=NSS+1
IINT(NSS)=N
UEL(N)=EL
CALL VECTOR (R,2,UPV,UTS)
CALL UNIVEC (UTS,U)
DO 345 IV=1,3
USUV(N,IV)=U(IV)
345 CONTINUE
350 CONTINUE
```

MAIN

```
IF(NSS.GE.4) GO TO 355
IF(NSS.LT.4) GO TO 500
355 CONTINUE
NSTO=NSTO+NSS
NSPL(L)=NSPL(L)+NSS
NSP=NSS+1
MAXNSS=MAX0(MAXNSS,NSS)
HIGH=0.
DO 365 NUM=1,NSS
IX=IINT(NUM)
AEA=UEL(IX)
IF(AEA.GT.HIGH) GO TO 360
IF(AEA.LE.HIGH) GO TO 365
360 HIGH=AEA
NN=NUM
365 CONTINUE
DO 370 NU=1,NSS
IF(NU.EQ.NN) NX=1
IF(NU.LT.NN) NX=NU+1
IF(NU.GT.NN) NX=NU
IOS(NX)=IINT(NU)
370 CONTINUE
GO TO 400
C
C IOS(NSS) HAS THE SATELLITE NEAREST TO OVERHEAD, THEN ALL OTHERS
C WHICH FIT CRITERIA
C
C NEXT CALCULATIONS ARE CONCERNED WITH FINDING THE COMBINATION OF
C FOUR SATELLITES WHICH HAVE THE GREATEST VALUE OF THE VOLUME OF THE
C TETRAHEDRON FORMED BY THEM
C
375 CONTINUE
DO 390 IKN=1,IK
DO 380 IV=1,3
R(IV)=RMX(IINT(IKN),IV)
380 CONTINUE
CALL VECTOR (R,2,UPV,UTS)
CALL UNIVEC (UTS,U)
DO 385 IV=1,3
USUV(IINT(IKN),IV)=U(IV)
385 CONTINUE
390 CONTINUE
DO 395 IJK=1,IK
395 IOS(IJK)=IINT(IJK)
400 BOX=-10.
IF(ISCMP.EQ.1) GO TO 405
KOT=NSS
NSS=NSS-1
CALL TAAT (NSS,KCOM,KXX)
ISIC(1)=IOS(1)
LPN=2
GO TO 410
405 KOT=IK
IF (LOC.EQ.2.OR.LOC.EQ.3) KOT=NSS
CALL TALL (KOT,KCOM,KXX)
LPN=1
410 DO 430 M=1,KCUM
```

MAIN

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DO 415 LPQ=LPN,4
NUX=KXX(M,LPQ)
ISIC(LPQ)=IOS(NUX)
415 CONTINUE
CALL VOLUME (USUV,ISIC,VOLUM)
IF(VOLUM.GT.BOX) GO TO 420
IF(VOLUM.LE.BOX) GO TO 430
420 BOX=VOLUM
DO 425 MC=1,4
NSGD(MC)=ISIC(MC)
425 CONTINUE
430 CONTINUE
DO 440 N=1,4
DO 435 IV=1,3
R(IV)=RMX(NSGD(N),IV)
435 CONTINUE
CALL VECTOR (R,2,UPV,UTS)
CALL VECTOR (Z,3,UPV,YE)
CALL VECTOR (UPV,3,YE,XN)
AX=SQRT(DOT(XN,XN))
AY=SQRT(DOT(YE,YE))
AP=SQRT(DOT(UPV,UPV))
ALT=AP/6076.116-3444.
AS=SQRT(DOT(UTS,UTS))
G(NSGD(N),1)=DOT(XN,UTS)/(AX*AS)
G(NSGD(N),2)=DOT(YE,UTS)/(AY*AS)
G(NSGD(N),3)=DOT(UPV,UTS)/(AP*AS)
G(NSGD(N),4)=1.
440 CONTINUE
CALL COVNAV (G,NSGD,4,SIGT)
IF(LOC.EQ.3) GO TO 480
IF(LOC.EQ.2) ALT=0.
DO 445 II=1,4
IOUT(II)=NSGD(II)
445 CONTINUE
IL=1
LK=4
DO 455 NN=1,KUT
ITST=NSGO(IL)
IF(ITST.EQ.IOS(NN)) GO TO 450
LK=LK+1
IOUT(LK)=IOS(NN)
GO TO 455
450 IL=IL+1
IF(IL.EQ.5) GO TO 460
455 CONTINUE
460 KOS>NN+1
DO 465 LK=KOS,KOT
IOUT(LK)=IOS(LK)
465 CONTINUE
ITOUT=(IT-1)*INC
KTR=KTR+2
IF(KOT.GT.18) KTR=KTR+1
IF(KTR.GE.50) GO TO 470
GO TO 475
470 WRITE (6,525)
KTR=0
475 WRITE (6,530) ITOUT,ALT,(SIGT(KP),KP=1,6),(IOUT(KP),KP=1,KOT)
```

MAIN

```
C END OF CALCULATION FOR SINGLE USER ON EARTH
C GO TO 625
C FOLLOWING CALCULATIONS FOR GLOBAL DISTRIBUTION
C
480 DO 485 IDOP=1,6
485 CDOP(L,K,IDOP)=SIGT(IDOP)
DO 490 NS=1,6
KA=MAX0(1,MIN0(INT(SIGT(NS)*5.+1.),36))
490 SKEG(L,KA,NS)=SKEG(L,KA,NS)+1.
DO 495 NA=1,KOT
I=IOS(NA)
ELT=UEL(I)
KO=MIN0(INT(ELT/5.)+1,18)
495 CAG(L,KO)=CAG(L,KO)+1.
MAX(L,K)=MAX0(MAX(L,K),KOT)
MIN(L,K)=MIN0(MIN(L,K),KOT)
OBLAT(L,NSP)=OBLAT(L,NSP)+1.
500 CONTINUE
IF(LOC.EQ.3.AND.IPFREQ.EQ.0) GO TO 625
C NO INTERMEDIATE PRINT
IF(IPRINT.EQ.0.AND.IT.EQ.1) GO TO 505
C PRINT FIRST TIME STEP
IPRINT=IPRINT+1
IF(IPRINT.EQ.ITIME) GO TO 505
C PRINT EACH TIME STEP REQUESTED
GO TO 625
505 IPRINT=0
DO 515 IDOP=1,6
IF(IDOP.EQ.1) WRITE (6,535) ITIME
IF(IDOP.EQ.2) WRITE (6,540) ITIME
IF(IDOP.EQ.3) WRITE (6,545) ITIME
IF(IDOP.EQ.4) WRITE (6,550) ITIME
IF(IDOP.EQ.5) WRITE (6,555) ITIME
IF(IDOP.EQ.6) WRITE (6,560) ITIME
IF(LATDEG.EQ.10.) WRITE (6,565)
IF(LATDEG.EQ.5.) WRITE (6,570)
ICT=-10
DO 510 IC=1,36
ICT=ICT+10
IF(ICK.LE.90.OR.ICT.GE.190) WRITE (6,575) ICT,(CDOP(IK,IC,IK),IK
1=1,19)
IF(ICK.EQ.100) WRITE (6,580) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.110) WRITE (6,585) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.120) WRITE (6,590) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.130) WRITE (6,595) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.140) WRITE (6,600) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.150) WRITE (6,605) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.160) WRITE (6,610) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.170) WRITE (6,615) (CDOP(IK,IC,IK),IK=1,19)
IF(ICK.EQ.180) WRITE (6,620) (CDOP(IK,IC,IK),IK=1,19)
510 CONTINUE
515 CONTINUE
DO 520 ICL=1,19
DO 520 ICK=1,36
DO 520 ICD=1,6
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MAIN

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520 CDOP(ICL,ICK,ICD)=0.  
C  
C THE FOLLOWING FORMATS HAVE TO DO WITH A SPECIFIED TIME STEP REQUEST  
C FOR PRINTING  
C  
525 FORMAT(1H1,/,1X,'TIME(MN)',1X,'ALT(NM)',4X,'VDOP',  
1 5X,'HDOP',5X,'MDOP',5X,'TDOP',5X,'PDOP',5X,'GDOP',4X,  
2 'SATELLITES CHOSEN',//)  
530 FORMAT(1H0,I7,F9.0,6(F9.3),1X,18(1X,I2),/,72X,18(1X,I2))  
535 FORMAT(1H1,/,10X,'TIME = ',I6,20X,'VDOP - ALTITUDE')  
540 FORMAT(1H1,/,10X,'TIME = ',I6,20X,'HDOP - POSITION ERROR IN HORIZONTAL PLANE')  
545 FORMAT(1H1,/,10X,'TIME = ',I6,20X,'MDOP - LARGER COMPONENT OF POSITION ERROR')  
550 FORMAT(1H1,/,10X,'TIME = ',I6,20X,'TDOP - TIME')  
555 FORMAT(1H1,/,10X,'TIME = ',I6,20X,'PDOP - THREE DIMENSIONAL POSITION ERROR')  
560 FORMAT(1H1,/,10X,'TIME = ',I6,20X,'GDOP - FOUR DIMENSIONAL POSITION ERROR')  
565 FORMAT(1H0,52X,'LATITUDE',/,9X,' 90',3X,' 80',3X,' 70',3X,' 60',  
1 3X,' 50',3X,' 40',3X,' 30',3X,' 20',3X,' 10',3X,' 0',3X,'-10',  
2 3X,'-20',3X,'-30',3X,'-40',3X,'-50',3X,'-60',3X,'-70',3X,'-80',  
3 3X,'-90',//)  
570 FORMAT(1H0,52X,'LATITUDE',/,9X,' 90',3X,' 85',3X,' 80',3X,' 75',  
1 3X,' 70',3X,' 65',3X,' 60',3X,' 55',3X,' 50',3X,' 45',3X,' 40',  
2 3X,' 35',3X,' 30',3X,' 25',3X,' 20',3X,' 15',3X,' 10',3X,' 5',  
3 3X,' 0',//)  
575 FORMAT(1H ,2X,I3,1X,19F6.2)  
580 FORMAT(1H , 'L',1X,'100',1X,19F6.2)  
585 FORMAT(1H , '0',1X,'110',1X,19F6.2)  
590 FORMAT(1H , 'N',1X,'120',1X,19F6.2)  
595 FORMAT(1H , 'G',1X,'130',1X,19F6.2)  
600 FORMAT(1H , 'I',1X,'140',1X,19F6.2)  
605 FORMAT(1H , 'T',1X,'150',1X,19F6.2)  
610 FORMAT(1H , 'U',1X,'160',1X,19F6.2)  
615 FORMAT(1H , 'D',1X,'170',1X,19F6.2)  
620 FORMAT(1H , 'E',1X,'180',1X,19F6.2)  
C  
625 CONTINUE  
IF(LOC.EQ.1.OR.LOC.EQ.2) GO TO 920  
MNSSPO=MAXNSS+1  
DO 630 LI=1,36  
630 QSR(LI)=FLOAT(LI-1)*.2  
DO 640 IX=1,18  
PIB(IX)=0.  
DO 635 IY=1,19  
635 PIB(IX)=PIB(IX)+CAG(IY,IX)  
640 PIB(IX)=(PIB(IX)/FLOAT(NSTO))*100.  
DO 660 LA=1,19  
IF(CL(LA).EQ.0..OR.NSPL(LA).EQ.0) GO TO 660  
DO 650 N=1,36  
DO 650 I=1,6  
SKEGX(LA,N,I)=0.  
DO 645 J=N,36  
645 SKEGX(LA,N,I)=SKEGX(LA,N,I)+SKEG(LA,J,I)  
650 SKEGX(LA,N,I)=SKEGX(LA,N,I)/CL(LA)  
DO 660 LC=1,18  
CAGX(LA,LC)=0.
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MAIN

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DO 655 LF=LC,18
655 CAGX(LA,LC)=CAGX(LA,LC)+CAG(LA,LF)
CAGX(LA,LC)=CAGX(LA,LC)/FLOAT(NSPL(LA))
660 CONTINUE
WRITE (6,780)
WRITE (6,785) (PIB(IX),IX=1,18)
IF(LATDEG.EQ.5.) WRITE (6,795)
IF(LATDEG.EQ.10.) WRITE (6,800)
ICT=-5
DO 665 LC=1,18
ICT=ICT+5
WRITE (6,815) ICT,(CAGX(LA,LC),LA=1,19)
665 CONTINUE
CVS=0.
DO 680 LM=1,19
IF(CL(LM).EQ.0..OR.NSPL(LM).EQ.0) GO TO 680
CV=COS((90.-FLOAT(LM-1)*LATDEG)*C(1))
CVS=CVS+CV
DO 670 IN=1,6
DO 670 II=1,36
670 GLOS(IN,II)=GLOS(IN,II)+SKEGX(LM,II,IN)*CV
DO 675 LN=1,18
675 GLEB(LN)=GLEB(LN)+CAGX(LM,LN)*CV
680 CONTINUE
DO 685 LN=1,18
685 GLEB(LN)=GLEB(LN)/CVS
WRITE (6,805)
WRITE (6,810) (GLEB(IC),IC=1,18)
DO 690 IN=1,6
DO 690 II=1,36
690 GLOS(IN,II)=GLOS(IN,II)/CVS
DO 695 JDOP=1,6
IF(JDOP.EQ.1) WRITE (6,830)
IF(JDOP.EQ.2) WRITE (6,835)
IF(JDOP.EQ.3) WRITE (6,840)
IF(JDOP.EQ.4) WRITE (6,845)
IF(JDOP.EQ.5) WRITE (6,850)
IF(JDOP.EQ.6) WRITE (6,855)
IF(LATDEG.EQ.10.) WRITE (6,820)
IF(LATDEG.EQ.5.) WRITE (6,825)
DO 695 IQSR=1,36
WRITE (6,775) QSR(IQSR),(SKEGX(LK,IQSR,JDOP),LK=1,19)
695 CONTINUE
WRITE (6,860)
DO 700 IQSR=1,36
WRITE (6,865) QSR(IQSR),(GLOS(IN,IQSR),IN=1,6)
700 CONTINUE
WRITE (6,870)
LADG=90.
IF(LATDEG.EQ.10.) LAD=-10.
IF(LATDEG.EQ.5.) LAD=-5.
WRITE (6,880)
DO 705 IL=1,19
WRITE (6,885) LADG,(MAX(IL,IK),IK=1,36)
LADG=LADG+LAD
705 CONTINUE
WRITE (6,875)
LADG=90.
```

MAIN

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DO 715 IL=1,19
DO 710 IX=1,36
IF(MIN(IL,IX).EQ.30) MIN(IL,IX)=0
710 CONTINUE
WRITE (6,885) LADG,(MIN(IL,IK),IK=1,36)
LADG=LADG+LAD
715 CONTINUE
DO 720 N=1,MNSSPO
OBDIS(N)=0.
DO 720 L=1,19
IF(CL(L).EQ.0..OR.NSPL(L).EQ.0) GO TO 720
OBLAT(L,N)=(OBLAT(L,N)/CL(L))*100.
720 CONTINUE
DO 730 L=1,19
DO 730 N=1,MNSSPO
ACLAT(L,N)=0.
DO 725 M=N,MNSSPO
725 ACLAT(L,N)=ACLAT(L,N)+OBLAT(L,M)
730 CONTINUE
CO=0.
DO 740 L=1,19
IF(CL(L).EQ.0..OR.NSPL(L).EQ.0) GO TO 740
CA=COS((90.-FLOAT(L-1)*LATDEG)*C(1))
CO=CO+CA
DO 735 N=1,MNSSPO
735 OBDIS(N)=OBDIS(N)+OBLAT(L,N)*CA
740 CONTINUE
DO 745 N=1,MNSSPO
745 OBDIS(N)=OBDIS(N)/CO
DO 750 N=1,MNSSPO
ACTOT(N)=0.
DO 750 M=N,MNSSPO
750 ACTOT(N)=ACTOT(N)+OBDIS(M)
DO 755 I=1,32
ISAPP(I)=I-1
755 CONTINUE
NP=1
MNS=MNSSPO
IF (MNSSPO.GT.16) MNS=16
WRITE (6,890) (ISAPP(I),I=1,16)
760 WRITE (6,900)
LADG=90.
DO 765 IL=1,19
WRITE (6,895) LADG,(OBLAT(IL,N),N=NP,MNS)
LADG=LADG+LAD
765 CONTINUE
WRITE (6,905)
LADG=90.
DO 770 IL=1,19
WRITE (6,895) LADG,(ACLAT(IL,N),N=NP,MNS)
LADG=LADG+LAD
770 CONTINUE
WRITE (6,910)
WRITE (6,790) (OBDIS(N),N=NP,MNS)
WRITE (6,915)
WRITE (6,790) (ACTOT(N),N=NP,MNS)
IF(MNSSPO.LT.16) GO TO 920
IF(MNS.GT.16) GU TO 920
```

MAIN

```
MNS=MNSSPO
NP=17
WRITE (6,890) (ISAPP(I),I=17,32)
GO TO 760
C
C THE FOLLOWING FORMATS HAVE TO DO WITH A GLOBAL SYSTEM
C
775 FORMAT(1H ,F4.1,3X,19F6.3)
780 FORMAT(1H1,////1X,'ELEVATION DISTRIBUTION - PROBABILITY THAT THE
1SATELLITE IN VIEW WILL HAVE ELEVATION ANGLES AS LISTED',//,48X,
2 'ELEVATION ANGLE')
785 FORMAT(1H0,6X,'   0-5   5-10  10-15 15-20 20-25 25-30 30-35 35-40 40
1-45 45-50 50-55 55-60 60-65 65-70 70-75 75-80 80-85 85-90',//,2X,
2 'PROB',1X,18F6.1)
790 FORMAT(1H0,3X,'PROB',5X,16F7.2)
795 FORMAT(1H0,///,1X,'LATITUDE ELEVATION DISTRIBUTION',//,
1 1X,'PROBABILITY THAT ANY SATELLITE IN VIEW WILL HAVE AN ELEVAT
2ION ANGLE GREATER THAN OR EQUAL TO THOSE LISTED',//,52X,
3'LATITUDE',//,2X,'ELEV',//,1X,'ANGLE', 1X,'    90      85      80      75
4    70      65      60      55      50      45      40      35      30      25      20
5    15      10       5       0',//)
800 FORMAT(1H0,///,1X,'LATITUDE ELEVATION DISTRIBUTION',//,
1 1X,'PROBABILITY THAT ANY SATELLITE IN VIEW WILL HAVE AN ELEVAT
2ION ANGLE GREATER THAN OR EQUAL TO THOSE LISTED',//,52X,
3'LATITUDE',//,2X,'ELEV',//,1X,'ANGLE', 1X,'    90      80      70      60
4    50      40      30      20      10       0      -10     -20     -30     -40     -50
5   -60     -70     -80     -90',//)
805 FORMAT(1H0,///,1X,'ACCUMULATIVE ELEVATION DISTRIBUTION',//,
1 1X,'PROBABILITY THAT THE ELEVATION ANGLE IS GREATER THAN OR EQUAL
2TO THOSE LISTED',//,48X,'ELEVATION ANGLE')
810 FORMAT(1H0,7X,'   0      5      10     15     20     25     30     35      4
10     45     50     55     60     65     70     75     80     85',//,2X,
2 'PROB',1X,18F6.1)
815 FORMAT(1H ,I3,4X,19F6.2)
820 FORMAT(1H0,52X,'LATITUDE',//,2X,'NUM',5X,
1           ' 90',3X,' 80',3X,' 70',3X,' 60',
2 3X,' 50',3X,' 40',3X,' 30',3X,' 20',3X,' 10',3X,' 0',3X,'-10',
3 3X,'-20',3X,'-30',3X,'-40',3X,'-50',3X,'-60',3X,'-70',3X,'-80',
4 3X,'-90',//)
825 FORMAT(1H0,52X,'LATITUDE',//,2X,'NUM',5X,
1           ' 90',3X,' 85',3X,' 80',3X,' 75',
2 3X,' 70',3X,' 65',3X,' 60',3X,' 55',3X,' 50',3X,' 45',3X,' 40',
3 3X,' 35',3X,' 30',3X,' 25',3X,' 20',3X,' 15',3X,' 10',3X,' 5',
4 3X,' 0',//)
830 FORMAT(1H1,///,1X,'DILUTION OF PRECISION - ACCUMULATIVE LATITUDE D
1ISTRIBUTION',//,1X,'PROBABILITY THAT ALTITUDE DOP WILL BE GREATER T
2HAN NUMBER LISTED',//)
835 FORMAT(1H1,///,1X,'DILUTION OF PRECISION - ACCUMULATIVE LATITUDE D
1ISTRIBUTION',//,1X,'PROBABILITY THAT POSITION DOP IN HORIZONTAL PLA
2NE WILL BE GREATER THAN NUMBER LISTED',//)
840 FORMAT(1H1,///,1X,'DILUTION OF PRECISION - ACCUMULATIVE LATITUDE D
1ISTRIBUTION',//,1X,'PROBABILITY THAT LARGER COMPONENT OF POSITION D
2OP WILL BE GREATER THAN NUMBER LISTED',//)
845 FORMAT(1H1,///,1X,'DILUTION OF PRECISION - ACCUMULATIVE LATITUDE D
1ISTRIBUTION',//,1X,'PROBABILITY THAT TIME DOP WILL BE GREATER THAN
2NUMBER LISTED',//)
850 FORMAT(1H1,///,1X,'DILUTION OF PRECISION - ACCUMULATIVE LATITUDE D
1ISTRIBUTION',//,1X,'PROBABILITY THAT THREE DIMENSIONAL POSITION DOP
```

MAIN

2 WILL BE GREATER THAN NUMBER LISTED',//)
855 FORMAT(1H1,///,1X,'DILUTION OF PRECISION - ACCUMULATIVE LATITUDE D
ISTRIBUTION',/,1X,'PROBABILITY THAT FOUR DIMENSIONAL POSITION DOP
2WILL BE GREATER THAN NUMBER LISTED',//)
860 FORMAT(1H1,///,1X,'DILUTION OF PRECISION PARAMETERS - ACCUMULATIVE
1 GLOBAL DISTRIBUTION',//,8X,'NUMBER',7X,'VDOP',6X,'HDOP',6X,
2 'MDOP',6X,'TDOP',6X,'PDOP',6X,'GDOP',//)
865 FORMAT(1H ,9X,F3.1,3X,6F10.4)
870 FORMAT(1H1,1X,' MAXIMUM AND MINIMUM NUMBERS SEEN AT EACH LATITUDE
1& LONGITUDE')
875 FORMAT(1H0,/,38X,'MINIMUM',/,37X,'LONGITUDE',//,
1 32X,2('1',9X),2('2',9X),2('3',9X),/,22X,3('5',9X,'0',9X),
2 '5',/,5X,'LAT',4X,8('0',9X),/)
880 FORMAT(1H0,/,38X,'MAXIMUM',/,37X,'LONGITUDE',//,
1 32X,2('1',9X),2('2',9X),2('3',9X),/,22X,3('5',9X,'0',9X),
2 '5',/,5X,'LAT',4X,8('0',9X),/)
885 FORMAT(1H ,3X,F4.0,3X,36I2)
890 FORMAT(1H1,40X,'NUMBER OF SATELLITES',//,5X,'LAT',3X,16I7)
895 FORMAT(1H ,3X,F4.0,5X,16F7.2)
900 FORMAT(1H0,/,10X,'PROBABILITY (IN PERCENT) OF SEEING EXACTLY N SAT
1ELLITES',/)
905 FORMAT(1H0,/,10X,'PROBABILITY (IN PERCENT) OF SEEING N OR MORE SAT
1ELLITES',/)
910 FORMAT(1H0,/,1X,'ON A GLOBAL BASIS THE PROBABILITY (IN PERCENT) TH
1AT EXACTLY N SATELLITES WILL BE SEEN')
915 FORMAT(1H0,/,1X,'ON A GLOBAL BASIS THE PROBABILITY (IN PERCENT) TH
1AT N OR MORE SATELLITES WILL BE SEEN')
920 CONTINUE
END

ORBINI

```
SUBROUTINE ORBINI(I)
COMMON/ORBIS/P(37,25)/CON/C(18)
P(I,2)=P(I,2)*C(1)
P(I,3)=P(I,3)*C(1)
P(I,4)=P(I,4)*C(1)
P(I,5)=P(I,5)*C(1)
P(I,9)=SIN(P(I,4))
P(I,10)=COS(P(I,4))
P(I,11)=SIN(P(I,3))
P(I,12)=COS(P(I,3))
P(I,21) = P(I,22)*C(6)
SAA=22808.*C(6)
P(I,23)=(SAA/P(I,21))**1.5
P(I,6)=P(I,21)*(1.-P(I,1)*P(I,1))
P(I,7)=SORT(C(12)/P(I,6))
P(I,8)=C(12)/(P(I,6)*P(I,6))
RETURN
END
```

ORBIT

```
SUBROUTINE ORBIT(I,T,PER,R,VEL,AC)
COMMON/ORBIS/OP(37,25)/CON/C(18)
DIMENSION R(3),VEL(3),AC(3),TRANS(3,3),Q(3),QEL(3),QC(3),U(36),
1   E(36),BIGT(36),LILT(36),V(36),CV(36),SV(36),PER(36)
REAL LILT
IF(T.GT.0.) GO TO 10
V(I)=OP(I,5)
SINE=(SQRT(1.-OP(I,1)**2)*SIN(OP(I,5)))/(1.+OP(I,1)*COS(OP(I,5)))
RAD=(OP(I,22)*(1.-OP(I,1)**2))/(1.+OP(I,1)*COS(OP(I,5)))
E(I)=ARSIN(SINE)
IF(OP(I,1).NE.0.) GO TO 15
IF(V(I).LT.(C(3)/2.)) E(I)=E(I)
IF((V(I).GE.(C(3)/2.)).AND.
1   (V(I).LE.(3.*C(3)/2.))) E(I)=C(3)-E(I)
IF(V(I).GT.(3.*C(3)/2.)) E(I)=C(4)+E(I)
GO TO 20
15 CONTINUE
IF(RAD.LT.OP(I,22).AND.V(I).LE.C(3)) E(I)=E(I)
IF(RAD.GT.OP(I,22)) E(I)=C(3)-E(I)
IF(RAD.LT.OP(I,22).AND.V(I).GT.C(3)) E(I)=C(4)+E(I)
20 CONTINUE
BIGT(I)=(PER(I)*(E(I)-OP(I,1)*SINE))/(24.*C(4))
LILT(I)=BIGT(I)
GO TO 25
10 DEL=.1
LILT(I)=BIGT(I)+T
E(I)=0.
35 E(I)=E(I)+DEL
Y=LILT(I)-(PER(I)*(E(I)-OP(I,1)*SIN(E(I))))/(24.*C(4))
IF(ABS(Y).LE..00001) GO TO 30
IF(Y.GT.0.) GO TO 35
E(I)=E(I)-DEL
DEL=DEL/10.
GO TO 35
30 CONTINUE
IF(E(I).GE.C(4)) E(I)=E(I)-C(4)
SINV=(SQRT(1.-OP(I,1)**2)*SIN(E(I)))/(1.-OP(I,1)*COS(E(I)))
V(I)=ARSIN(SINV)
RP=OP(I,22)*(1.-OP(I,1)*COS(E(I)))
P=OP(I,22)*(1.-OP(I,1)**2)
IF(OP(I,1).NE.0.) GO TO 40
IF(E(I).LT.(C(3)/2.)) V(I)=V(I)
IF((E(I).GE.(C(3)/2.)).AND.
1   (E(I).LE.(3.*C(3)/2.))) V(I)=C(3)-V(I)
IF(E(I).GT.(3.*C(3)/2.)) V(I)=C(4)+V(I)
GO TO 25
40 CONTINUE
IF(RP.LT.P.AND.E(I).LE.C(4)) V(I)=V(I)
IF(RP.GT.P) V(I)=C(3)-V(I)
IF(RP.LT.P.AND.E(I).GT.C(4)) V(I)=C(4)+V(I)
25 CONTINUE
CV(I)=COS(V(I))
SV(I)=SIN(V(I))
U(I)=V(I)+OP(I,2)
OP(I,13)=COS(U(I))
OP(I,14)=SIN(U(I))
SPH=OP(I,14)*OP(I,9)
CPH=SQRT(1.+SPH*SPH)
```

ORBIT

```
OP(I,15)=ARSIN(SPH)*C(2)
OP(I,18)=U(I)
F1=1.+OP(I,1)*CV(I)
Q(1)=OP(I,6)/F1
Q(2)=0.
Q(3)=0.
QEL(1)=OP(I,1)*OP(I,7)*SV(I)
QEL(2)=OP(I,7)*F1
QEL(3)=0.
QC(1)=-OP(I,8)*F1*F1
QC(2)=0.
QC(3)=0.
CALL TRMATX (TRANS,I)
CALL MATMUL (TRANS,Q,R)
CALL MATMUL (TRANS,QEL,VEL)
CALL MATMUL (TRANS,QC,AC)
OP(I,24)=(T- AINT(T+.5))*C(4),
OP(I,16)=ATAN2(R(2),R(1))-OP(I,24)
OP(I,16)=OP(I,16)*C(2)
RETURN
END
```

TRMATX

```
SUBROUTINE TRMATX(TR,I)
DIMENSION TR(3,3)
COMMON/ORBIS/OP(37,25)/CON/C(18)
TR(1,1)=OP(I,12)*OP(I,13)-OP(I,11)*OP(I,10)*OP(I,14)
TR(1,2)=OP(I,12)*OP(I,14)+OP(I,11)*OP(I,10)*OP(I,13)
TR(1,3)=OP(I,11)*OP(I,9)
TR(2,1)= OP(I,11)*OP(I,13)+OP(I,12)*OP(I,10)*OP(I,14)
TR(2,2)=-OP(I,11)*OP(I,14)+OP(I,12)*OP(I,10)*OP(I,13)
TR(2,3)=-OP(I,12)*OP(I,9)
TR(3,1)=OP(I,9)*OP(I,14)
TR(3,2)= OP(I,9)*OP(I,13)
TR(3,3)=OP(I,10)
TR(1,2)=-1.*TR(1,2)
RETURN
END
```

MATMUL

```
SUBROUTINE MATMUL(T,V,O)
DIMENSION T(3,3),V(3),O(3)
DO 10 I=1,3
  O(I)=0.
  DO 10 J=1,3
10  O(I)=O(I)+T(I,J)*V(J)
      RETURN
      END
```

POINT

```
SUBROUTINE POINT(ALD,ALA,TIM,VEC)
COMMON/CON/C(18)
DIMENSION VEC(3)
EW=ALD*C(1)+C(4)*TIM
SN=ALA*C(1)
VEC(1)=C(10)*COS(SN)*COS(EW)
VEC(2)=C(10)*COS(SN)*SIN(EW)
VEC(3)=C(10)*SIN(SN)
RETURN
END
```

TAAT

```
SUBROUTINE TAAT (MAX,MXX,MATRIX)
DIMENSION MATRIX(58905,4)
DO 10 I=1, 58905
DO 10 II=1,4
10 MATRIX(I,II)=0
IF(MAX.LT.3) GO TO 30
MXX=(MAX-2)*(MAX-1)*MAX/6
MMM=MAX-1
MMN=MAX
MMO=MAX+1
NA=0
DO 25 K=2,MMM
KO=K+1
DO 20 L=KO,MMN
KT= L+1
DO 15 M=KT,MMO
NA=NA+1
MATRIX(NA,2)=K
MATRIX(NA,3)=L
MATRIX(NA,4)=M
15 CONTINUE
20 CONTINUE
25 CONTINUE
30 RETURN
END
```

VOLUME

```
SUBROUTINE VOLUME (UVEC,IDSAT,VOL)
DIMENSION UVEC(37,3),IDSAT(4),ONE(3),TWO(3),THREE(3),FOUR(3)
DIMENSION TMF(3),TMT(3),OMT(3),CROSS(3)
KA=IDSAT(1)
KB=IDSAT(2)
KC=IDSAT(3)
KD=IDSAT(4)
DO 10 N=1,3
ONE(N)=UVEC(KA,N)
TWO(N)=UVEC(KB,N)
THREE(N)=UVEC(KC,N)
10 FOUR(N)=UVEC(KD,N)
CALL VECTOR (TWO,2,FOUR,TMF)
CALL VECTOR (THREE,2,TWO,TMT)
CALL VECTOR (ONE,2,TWO,OMT)
CALL VECTOR (TMT,3,TMF,CROSS)
VOL=ABS(DOT(OMT,CROSS))
RETURN
END
```

COVNAV

```
SUBROUTINE COVNAV (G, ID, NAT, SIG)
DIMENSION ID(37), B(4), SIG(6), G(37,4), IPIVOT(4), INDES(4,2)
REAL*8 TRA(4,4), BBB(1,1), DETERM, FPTMAX
DATA FPTMAX/Z7FFFFFFFFFFFFF/
DO 20 I=1,4
DO 15 J=1,I
TRA(I,J)=0.
DO 10 K=1,NAT
L=ID(K)
TRA(I,J)=TRA(I,J)+G(L,I)*G(L,J)
10 CONTINUE
TRA(J,I)=TRA(I,J)
15 CONTINUE
TRA(I,I)=TRA(I,I)+1.E-12
20 CONTINUE
CALL DMATRI (TRA,4,4,BBB,1,0,IPIVOT,INDES,ISING,DETERM)
IF(ISING.NE.0) STOP
IF(DETERM.EQ.FPTMAX) GO TO 25
SIG(1)=DSQRT (TRA(3,3))
SIG(2)=DSQRT (TRA(1,1)+TRA(2,2))
SIG(3)=DMAXI (DSQRT (TRA(1,1)), DSQRT (TRA(2,2)))
SIG(4)=DSQRT (TRA(4,4))
SIG(5)=DSQRT (TRA(1,1)+TRA(2,2)+TRA(3,3))
SIG(6)=DSQRT (TRA(1,1)+TRA(2,2)+TRA(3,3)+TRA(4,4))
RETURN
25 WRITE(6,30)
30 FORMAT(1H ,/,3X,'DETERMINATE REACHED MAXIMUM VALUE')
STOP
END
```

BLK DATA

```
BLOCK DATA
COMMON/CON/C(18)
DATA C/.01745329252,57.295779513,3.1415926536,6.28318530718,
11.57079630,6076.116,0.,0.,0.,2.0926143504E+07,
27.29211585E-05,1.4076380E+16,365.2563835 ,92.91
3E+06,0.0167272,23.44436,-77.7303,5280./
END
```

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GEOMETRIC PERFORMANCE OF PSEUDORANGING NAVIGATION...ETC.(U)
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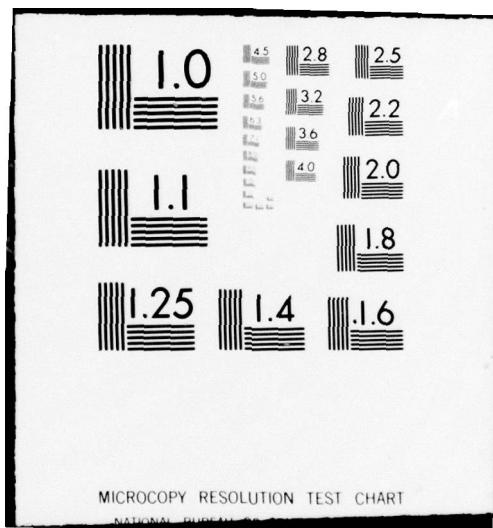
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VECTOR

```
SUBROUTINE VECTOR(V1,I,V2,V3)
DIMENSION V1(3),V2(3),V3(3)
GO TO (10,15,20), I
10 V3(1)=V1(1)+V2(1)
    V3(2)=V1(2)+V2(2)
    V3(3)=V1(3)+V2(3)
    RETURN
15 V3(1)=V1(1)-V2(1)
    V3(2)=V1(2)-V2(2)
    V3(3)=V1(3)-V2(3)
    RETURN
20 V3(1)=V1(2)*V2(3)-V1(3)*V2(2)
    V3(2)=V1(3)*V2(1)-V1(1)*V2(3)
    V3(3)=V1(1)*V2(2)-V1(2)*V2(1)
    RETURN
END
```

DOT

```
FUNCTION DOT(V1,V2)
DIMENSION V1(3),V2(3)
DOT=V1(1)*V2(1)+V1(2)*V2(2)+V1(3)*V2(3)
RETURN
END
```

UNIVEC

```
SUBROUTINE UNIVEC (V,UV)
DIMENSION V(3),UV(3)
DENOM = SQRT(DOT(V,V))
UV(1) = V(1)/DENOM
UV(2) = V(2)/DENOM
UV(3) = V(3)/DENOM
RETURN
END
```

TALL

```
SUBROUTINE TALL (MAX,MXX,MATRIX)
DIMENSION MATRIX(58905,4)
DO 10 I=1,58905
DO 10 II=1,4
10 MATRIX(I,II)=0
IF(MAX.LT.3) GO TO 35
MXX=(MAX-3)*(MAX-2)*(MAX-1)*MAX/24
KK=MAX-3
LL=MAX-2
MM=MAX-1
NN=MAX
NA=0
DO 30 K=1,KK
KO=K+1
DO 25 L=KO,LL
KT=L+1
DO 20 M=KT,MM
KP=M+1
DO 15 N=KP,NN
NA=NA+1
MATRIX(NA,1)=K
MATRIX(NA,2)=L
MATRIX(NA,3)=M
MATRIX(NA,4)=N
15 CONTINUE
20 CONTINUE
25 CONTINUE
30 CONTINUE
35 RETURN
END
```

REFERENCES

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2. Unpublished analysis by J. J. Mate, The Rand Corporation, September 1976.