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RESEARCH IN CALCULUS OF VARIATIONS NUMERICAL ANALYSIS AND RELAT--ETC(U)
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RESEARCH IN CALCULUS OF VARIATIONS
NUMERICAL ANALYSIS AND RELATED FIELDS

Final Report

M. R. Hestenes

August 31, 1975

U. S. ARMY RESEARCH OFFICE

Contract DA-31-124-ARO-D-355

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UNIVERSITY OF CALIFORNIA

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