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Research Report CCS 195 ✓
**IMPORTANT PRACTICAL
 MISCONCEPTIONS OF OPTIMIZING
 LARGE SCALE ASSIGNMENT AND
 TRANSPORTATION PROBLEMS**

by

F. Glover*
 D. Klingman

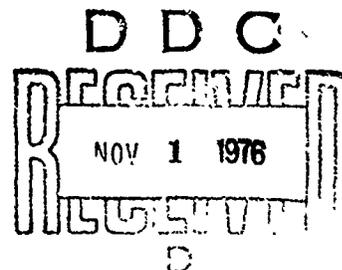
October 1974

* University of Colorado, Boulder, Colorado 80302.

This research was partly supported by the Navy Personnel Research and Development Laboratory Contract N00123-74-C-2272 with the Center for Cybernetic Studies, The University of Texas, Austin, Texas, and by the Alexander Von Humboldt Stiftung, Bonn, Germany. Reproduction in whole or in part is permitted for any purpose of the United States Government.

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INTRODUCTION

Modelling and solving large scale networks are crucial to many practical military applications. The purpose of this note is to identify important elements of successful models and methods that were incompletely or inaccurately portrayed in recent presentations at O.R. meetings such as that in [16]. Our observations result from breakthroughs in network areas that have been validated in over a hundred computer hours of empirical testing and 15 man years of code development. They particularly apply to modelling large scale military manpower assignment problems and designing computer codes for solving large scale assignment, transportation, and transshipment problems. To focus our remarks we shall address chiefly the misconceptions presented in [16].

MEMORY AND SOLUTION CAPACITIES

A major oversight of [16], which unfortunately is transmitted throughout the paper, concerns a confusion between computer codes for capacitated and uncapacitated network problems (and a secondary confusion between early codes and more recent ones). One manifestation of this confusion occurs in the formula given in [16] for computing memory requirements for the recently developed network code PNET [7]:

$$3(mnd) + 8m + 7n + 10,000$$

where

m = number of source nodes

n = number of sink nodes

d = cost matrix density

This is not the formula for PNET, but is the formula for the somewhat earlier transportation code PTRANS [9], and applies to a version for solving capacitated

transportation problems. The correct formula for PNET is

$$2(\text{rmd}) + 5m + 5n + 8,000$$

The errors resulting from this misunderstanding cause the entries in Table 1 and Figure 1 to be drastically distorted. While it appears in Table 1 and Figure 1 that PNET can not solve as large a problem as the other in-core codes listed, PNET can in fact solve larger problems than any other in-core codes in existence. In addition, PNET is capable of solving general transshipment problems as well as assignment and transportation problems. None of the other codes discussed in [16] has this ability. (Ironically, the difficulties of optimal quota accommodation--for "fill" optimization--discussed at length in [16] are in fact due to this inability of the other codes to solve transshipment problems. PNET's ability to handle such problems eliminates the need for a nonlinear optimization routine.)

Our research over the past five years has solidly demonstrated that simplex-based computer codes are more efficient and require less memory than primal-dual (out-of-kilter) computer codes. This empirical fact has been derived scientifically by developing and implementing a wide variety of improved algorithmic procedures for network [1, 3, 7, 9, 10, 15, 17, 18, 19, 23]. (Our findings concerning the superiority of simplex-based codes are not biased by inattention to primal-dual methods. In fact, our primal-dual code SUPERK [1] has never been beaten by any other primal-dual code.)

To verify the practical merit of these developmental efforts, we have conducted extensive computational testing (in excess of 100 central processing hours on a CDC 6600) against all available codes and on all types of assignment, transportation, and transshipment problems [7, 9, 10, 15, 17, 18, 19, 23].

The outcomes of this testing were then validated across different types and sizes of computer; e.g., CDC 3100, UNIVAC 1108, Burroughs 4700, CDC 6600, IBM 360/65, IBM 370/155, CDC 6400, Burroughs 6700, PDP-10, and IBM 370/145. Subsequently, the efficiency of our codes and the accuracy of our conclusions have been independently substantiated by researchers around the world.*

These developments uncover a serious omission in the hypothetical codes considered in [16], which astonishingly fail to include simplex-based codes. The eligibility and cost storage schemes mentioned in [16] are all easily accommodated by a simplex-based code. As a consequence, a simplex-based network code can be designed whose memory requirement is only $2n + 2m$ words beyond that required by the cost storage scheme. This memory requirement is less than any of the hypothetical or existing codes discussed in [16].

We are quite skeptical of the value of in-core codes utilizing such minimal memory requirements (independent of whether the underlying method is a primal-dual or simplex based algorithm). These doubts stem from the fact that a code using implicit eligibility and cost storage schemes exhibit two notable defects. First, the code is immediately problem specific. That is, as soon as the rules for eligibility or cost relevant information are changed, the code is obsolete and must be revised. Second, the code is computer dependent-- i.e., the code can only be used on one manufacturer's computer (and possibly even only one of his computer models). In the age of rapid technology and social change, it is highly doubtful that any organization should be tied to a problem specific and computer dependent solution code.

*To enable researchers to make meaningful comparisons of alternative solution codes we developed a computer program for generating test networks called NETGEN [19]. The NETGEN code documentation also provides the user with benchmarks (solution times on current codes and objective function values) on 40 assignment, transportation, and transshipment problems.

OUT-OF-CORE METHODS

A closely related, but even more serious misconception of the paper concerns the application of out-of-core methods. According to [16]:

Out-of-core approaches are considered prohibitively expensive. During the solution these approaches repeatedly access information stored on peripheral devices and can be shown to be impractical from the standpoint of computer time required. . . .

It is estimated that out-of-core approaches incur a penalty resulting in a 10 to 1000 times increase in computer costs.

These speculations are contradicted by our results from testing both in-core and out-of-core codes [17]. Based on these results, we conclude that an appropriately designed out-of-core code is only 2 to 5 times slower than an in-core code. This is based on the premise that the in-core code does not pack information within one word. If the in-core code does pack information, then the out-of-core code may be faster than the in-core code.

Our findings also document the following major advantages of an out-of-core code over an in-core code:

1. Vastly larger problems can be solved by an out-of-core code. For example, we have recently implemented an Extended Transportation System for the U. S. Treasury Department which is capable of solving transportation problems with 50,000 nodes and 62 million arcs on a UNIVAC 1108. Larger problems can be solved by this system on an IBM 360/65, IBM360/155, IBM 360/165, CDC 6600, etc.

2. Out-of-core codes require less central memory for problems of all size ranges--including those that in-core codes can handle. This is critical for fast job handling on multi-processing computer systems. (All of the computer systems discussed in [16] are of this type.) Thus, if turn-around time is the

criterion of efficiency, then out-of-core codes will be substantially faster due to the bias of multi-processing systems against jobs requiring a large amount of core.

3. An out-of-core code can in fact operate as an in-core code simply by allocating the code sufficient core space to bring all problem data into core. In this mode, an appropriately designed out-of-core code runs less than 10% slower than an in-core code [17].

In conclusion, extensive research and testing has established that practical network problems can now be handled routinely at efficiencies and memory capabilities dramatically beyond those imagined possible a few years ago. These achievements^{s!} and the innovations that have brought them about have upended a number of notions that unfortunately are still disseminated as folklore by papers such as [16].

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Unclassified

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and reference numbers is entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author)

Center for Cybernetic Studies
The University of Texas

2a. REPORT SECURITY CLASSIFICATION

Unclassified

2b. GROUP

3. REPORT TITLE

⑩ Important Practical Misconceptions of Optimizing Large Scale Assignment and Transportation Problems

4. DESCRIPTIVE NOTES (Type of report and, inclusive dates)

⑨ Research Rept.

5. AUTHOR(S) (First name, middle initial, last name)

⑩ Fred Glover
Darwin Klingman

⑭ CCS-195

6. REPORT DATE

⑮ Oct 74

⑫ 11p.

7a. TOTAL NO. OF PAGES

8

7b. NO. OF REFS

24

8a. CONTRACT NUMBER

⑮ N00123-74-C-2272

9a. ORIGINATOR'S REPORT NUMBER(S)

Center for Cybernetic Studies
Research Report CCS 195

c.
d.

9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)

9. DISTRIBUTION STATEMENT

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10. SUPPLEMENTARY NOTES

11. SPONSORING MILITARY ACTIVITY

Office of Naval Research (Code 434)
Washington, D.C.

11. ABSTRACT

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resulting in the

Unclassified

Security Classification

14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
Networks						
Assignment problems						
Linear programming						
Software development						