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A STATISTICAL MODEL OF THE LOWER IONOSPHERE

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MEECN TECHNICAL PAPER

① "A STATISTICAL MODEL OF THE
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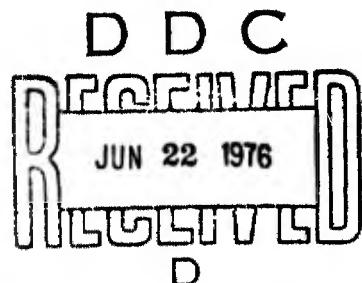
ABSTRACT: This report analyzes, as a group, measurements of the electron density profile in the lower ionosphere. Approximately 15 years of measurements were analyzed and an effort is made to develop a preliminary time-varying ionospheric model for use in determining VLF and LF propagation predictions.

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EXECUTIVE SUMMARY

1. THE NEED AND POTENTIAL FOR A MODEL OF THE LOWER IONOSPHERE

In order to estimate the performance of the Minimum Essential Emergency Communications Network (MEECN), it is necessary to determine the time-availability of each individual link. Some links in the system are LF-VLF radio communications systems, whose time availability depends primarily on the temporal statistics of the signal-to-noise ratio (S/N). The variation of LF-VLF S/N is not sufficiently well known for good system design and analysis, so the Office of MEECN System Engineer has organized the Tri-Service Propagation Program to develop the required information.

The main uncontrollable determinant of LF-VLF signal strength is the profile (height variation) of the electron density in the extreme lower ionosphere, because it is here that the VLF radio waves are reflected. Most of the sophisticated computer programs that have been developed for computing LF and VLF field strength require a model of the lower ionosphere as input. The accuracy of the field strength prediction (and through it, the accuracy of the link time-availability calculation) depends on the accuracy of the ionospheric model used.

There is no available model of the lower ionosphere which depicts realistically the variation of the ionosphere with hour, season, latitude, and sunspot number. However, during the past 15 years, many measurements of the electron density have been made at various locations and times. These measurements have not been analyzed as a group, nor incorporated into a synoptic, statistical model useful for LF-VLF communications link analysis. This report analyzes the available data, assesses its usefulness, and provides a preliminary time-varying ionospheric model.

2. SELECTION AND VALIDATION OF DATA REDUCTION TECHNIQUES

Previous experience has shown that a simple exponential model of the electron density in the lower ionosphere is adequate to describe LF-VLF radio propagation in most cases (see equation (ES-1) in section 3). Rules for scaling the parameters for such a model from measured electron density profiles were developed. They were validated by comparing propagation parameters computed for a sample of ten representative measured profiles with the same parameters computed for the scaled exponential approximation. For these ten

profiles, the magnitude of the principle reflection coefficient errors averaged less than 1 dB for the important angles of incidence for LF-VLF propagation. This resulted in an average error of about 1 dB in field strength for a 5000 km path. The error increases with path length. An error of this size from the scaling procedure is acceptable because it is smaller than the random variation of signal strength.

3. DERIVATION OF THE MODEL

Four hundred and seventy measured profiles of electron density in the D-region were retrieved from the report and journal literature, and were scaled to determine the statistical distribution and correlation that could be derived from emperical data. A multi-parameter linear regression of the model parameters on significant geophysical parameters was performed using a standard statistical approach. The resulting model has the form:

$$N(h) = N_0 \exp (\alpha (h - h_w)) \quad (ES-1)$$

where

$$N_0 = 1.43 (10^7) \exp (-0.15 h_w)$$

so that h_w is the standard reference height. The gradient, α and h_w will depend on time (hour and month), latitude, and solar activity.

$$\alpha = \alpha_c + \alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \alpha_4 x_4 \quad \text{and} \quad (ES-2)$$

$$h_w = h_c + h_1 x_1 + h_2 x_2 + h_3 x_3 + h_4 x_4$$

The α_i and h_i are coefficients determined by a multidimensional linear regression on the independent variables x_i . These variables are:

$$x_1 = \cos \left(\frac{t - 12}{24} 2\pi \right), \text{ where } t \text{ is the local time (hour), } t = 1, 24.$$

$$x_2 = \cos (L), \text{ where } L \text{ is the latitude (radians).}$$

$$x_3 = \pm \cos \left(\frac{m - 1/2}{12} 2\pi \right), \text{ where } m \text{ is the month (January} = 1, \dots \\ \text{December} = 12.)$$

(Use + for northern hemisphere, - for southern hemisphere.)

$$x_4 = S, \text{ where } S \text{ is the sunspot number (12 month running average of Zurich sunspot number).}$$

The analysis was also done for $x_1 = \cos(\text{sun's zenith angle})$ but the residual error in both h and α was greater (slightly) for this set of variables. Table ES-1 gives the resulting values for α_i and h_i .

Table ES-1. Values of Coefficients for Statistical Electron Density Model

i	c	1	2	3	4
h_i	71.8	3.83	6.85	0.085	0.047
α_i	0.210	0.036	0.082	-0.050	0.00045

Statistical tests show that all coefficients except h_3 are significantly different from zero.

4. COMPARISONS OF MODEL VARIATIONS WITH VLF PROPAGATION EXPERIENCE

The model predicts a day-to-night variation in reference height, h_0 , of less than 8 km. Measured VLF propagation data suggests that this variation should be about 15 km. This is the biggest deficiency of the preliminary model. It appears to be caused by too few, or too inaccurate, nighttime profiles.

However, the

- variation of reference height with sunspot number,
 - variation of reference height with latitude, and
 - the day and night values of the slope parameter, α ,
- are all consistent with LF-VLF propagation experience -- at least qualitatively.

5. CONCLUDING REMARKS AND RECOMMENDATIONS

The dependence of lower ionosphere reflection properties on sunspot number, season, and latitude shown by the analysis in this report will be useful for predicting LF-VLF field strength (and thus VLF link time availability). The apparent poor quality of the measurements of electron density at low altitudes at night resulted in unrealistically small day-to-night change in reflection height. To make a practical model useful for LF-VLF signal-to-noise predictions, the following steps are recommended:

1. Remove local time from the list of independent variables, and instead put in a fixed variation with time which has the required day-to-night variation, as determined by propagation data.
2. Filter the data by making subjective, but careful, judgments about the quality of the data, indicated by the experimental method and controls. Discard the profiles judged to be unreliable.
3. Continue to add high quality profiles to the data base as they become available.
4. Then recompute the coefficients for the remaining variables, separately for day and night.

A realistic time-varying model of the lower ionosphere is necessary for reliable calculations of the time-availability of LF-VLF links in the MEECN system.

APPENDIX

The profile data, and sources of the profiles used in the report are listed in the Appendix.

A STATISTICAL MODEL OF THE LOWER IONOSPHERE

ABSTRACT

Four hundred and seventy measured profiles of electron density in the lower ionosphere were retrieved from the literature. Scaling rules were developed for fitting the profiles with an exponential approximation, and were validated by comparing LF-VLF field strengths computed with the approximations and the full measured profiles. The coefficients for a multidimensional linear regression on the parameters of the exponential model were calculated using standard techniques. The seasonal, latitudinal, and sunspot number variations of the reference height are consistent with long-path VLF measurements. The day-to-night variations of reference height and gradient are qualitatively correct, but are not large enough. This discrepancy is traced to the nighttime profiles. Further analysis to improve the model is recommended.

1. THE NEED AND POTENTIAL FOR A MODEL OF THE LOWER IONOSPHERE

In order to estimate the performance of the Minimum Essential Emergency Communications Network (MEECN), it is necessary to determine the time-availability of each individual link. Some links in the system are LF-VLF radio communications systems whose time availability depends primarily on the time distribution of the signal-to-noise ratio (S/N). The main uncontrollable determinant of LF-VLF signal strength is the profile (height variation) of the electron density in the extreme lower ionosphere, because it is here that the VLF radio waves are reflected. So most of the sophisticated computer models that have been developed for computing LF and VLF field strength require specification of a model of the lower ionosphere.

Since the computer field strength is to be compared with the noise, the ionospheric model should vary realistically with the same parameters which affect the noise -- the time (hour, season) and geographic location. No satisfactory time-varying, worldwide model of the lower ionosphere exists. Several attempts have been made to develop "average" profiles for day and night (see, for example, Bain and May, 1967). Berry and Jones (DCA, 1974b, Appendix) made a preliminary attempt at a time-varying model. More recently (DCA, 1974a), Morfitt prepared a table recommending "descriptive electron density profiles" for various latitudes and seasons for day and night. These profiles "describe the limited amount of propagation data to varying degrees

of exactness." However, the table is incomplete, especially at night, and it is clear that the recommended profiles will not reproduce the known seasonal variations in LF-VLF signal strengths.

During the past 15 years, a number of experimenters have attempted to measure the electron density in the lower ionosphere. The measurement methods include direct measurements of electron density by rockets and indirect radio sensing techniques using rockets or ground-based "radar". Two ground-based techniques use HF radio waves: the partial reflection technique (e.g., Gardner and Pawsey, 1953; Belrose, et al., 1967) and the wave interaction or cross-modulation technique (e.g., Smith, 1967). Multi-frequency VLF sounders are used at both steep (e.g., Gossard, 1967) and oblique (e.g., Morfit, 1973) incidence. Finally field strength as a function of distance from the transmitter can be used to deduce the electron density profile (e.g., DCA, 1975). The Appendix lists many more references for each experimental method.

The low values of electron density in the lower ionosphere make its measurement difficult (Booker and Smith, 1970). None-the-less, there have been enough such attempts to make it worthwhile to try to analyze all measurements and integrate them into a synoptic quantitative description.

In this report, all applicable measurements that were found are used. The usual hopeful assumption is made: if the sample is large enough, errors made in individual measurements will "average out" so that the resulting sample mean represents the true mean ionosphere, and the distribution of the data about the mean approximates the true distribution. That assumption should eventually be tested by comparing calculated LF-VLF field strengths with measured values for particular paths.

This appears to be the first attempt to organize all the data into a quantitative model. The usual reasons given for not doing it are that the data are not sufficiently accurate, have not been validated by replication (various experimental methods may give different results), have not been taken in enough different points in space and time, and do not extend low enough in altitude to be useful in long-path VLF propagation studies. Most of the reasons except the last can be tested and perhaps circumvented by statistical analysis. The last reason is the most inhibiting -- but can be tested only after the model has been developed -- by comparing theoretical propagation calculations made with the model with actual measurements.

2. SELECTION AND VALIDATION OF DATA REDUCTION TECHNIQUES

Two measured D-region profiles are shown in Figure 1 (Profiles 70 and 167 of Appendix). The fact that measured D-region electron densities are usually shown in this format emphasizes that the most important variation is with height. Given a large number of profiles like those shown in Figure 1, which were measured at various geographic locations and times, how can the average profile and the variation of profiles with important causative geophysical parameters be summarized? That is the problem being addressed.

A brute force approach might be to consider a four dimensional grid (latitude, longitude, altitude, and time) and to fit some function to the data values we have, recognizing the important time cycles (diurnal, annual, and sunspot cycle). Even a cursory examination of this approach shows that it requires orders of magnitude more data than are available.

A more refined approach is to choose a mathematical form whose values depend on parameters, determine the values of these parameters for the measured data, and analyze the geophysical dependence of these parameters.

Berry and Jones (OCA, 1974b) used a model which consisted of an exponential function of height, plus a Chapman layer. This model required six parameters, and could be fit quite well to profiles like the one labeled A in Figure 1. Scaling the parameters from profiles is quite difficult, especially if the shape is like that of profile B in Figure 1.

2.1 The Exponential Profile

A much simpler model for theoretical purposes was suggested by Wait and Spies (1964). Calculations show that the parameters which most affect VLF propagation are the height of reflection and gradient of electron density at that height. These two parameters are explicit in the "exponential profile"

$$N(h) = N_0 \exp [\alpha(h - h_0)] \quad (1)$$

where N_0 is the electron density at height h_0 and α is the slope on semi-log paper. The rationale is that the lower edge of most profiles can be approximated by a straight line on the semi-log paper for a height range of several kilometers. Theoretical calculations have shown (Crain, 1970; Gambill and Rutherford, 1971) that most of the contribution to reflection of LF and VLF waves occurs within a height range of perhaps 5 kilometers.

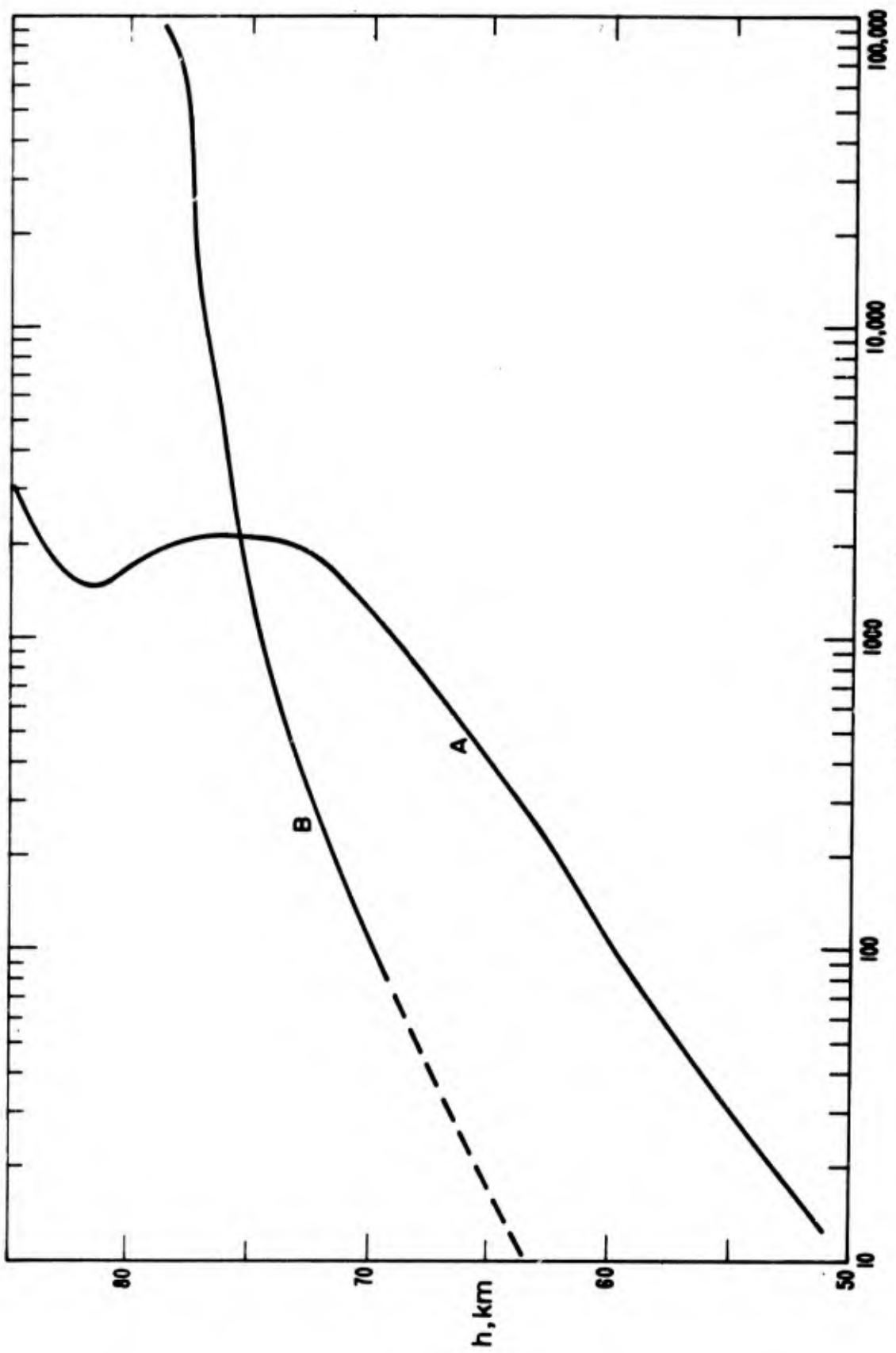


Figure 1. Example of daytime (A) and nighttime (B) electron density profiles.

The Naval Electronics Laboratory has had considerable success matching theoretical propagation calculations to measured field strengths by using such exponential profiles. Thus, this simple model, which requires only three parameters for complete specification, was selected for a first attempt. If it does not prove satisfactory, more complicated models can be tried later.

As will be seen, even profiles such as profile A in Figure 1 can be fitted with an exponential. The argument is that, even for these, the oblique reflection often takes place well below the nose of the profile, so that the departure from an exponential higher up is not significant. Of course, there will be times when electron density in the reflection region is considerably non-linear, but if these times are sufficiently rare, they will not invalidate a statistical model.

2.2 Scaling Rules

Having chosen to fit the profiles with a straight line (on a log scale), the choice of the proper height at which to determine the slope of the line becomes critical, because the slope is an important determinant of the reflection coefficient magnitude. For theoretical work, Wait and Spies (1964) chose to fix N_0 so they could deal with only two parameters -- h_0 and α . They chose the height h_w at which

$$\omega_r(h_w) = 2.5 \times 10^5. \quad (2)$$

$$\text{Here, } \omega_r(h) = 3.18 \times 10^9 N(h)/v(h), \quad (3)$$

N is the electron density, and v is the electron neutral collision frequency. It is important to notice that for a truly exponential profile, such a choice is entirely arbitrary: given one set of N_0 , h_0 , and α , the same profile can be represented at any other height h_1 by finding the corresponding N_1 using formula (1).

However, for determining an exponential electron density profile which adequately represents an experimentally measured profile for propagation calculations, selection of the height at which to determine the slope can be critical, because this slope may change considerably in a distance of 10 or 15 km.

Gambill and Rutherford (1971) have made a number of calculations which show that most of the energy of a VLF or LF wave incident at an angle ϕ on the ionosphere is reflected near the height where

$$\frac{\omega_r}{\omega} = \sqrt{2} \cos^2 \phi, \quad (4)$$

where $\omega = 2\pi f$ is the radio frequency. This was originally suggested by Field and Engle (1965). Unfortunately, this criterion is a function of radio frequency and angle of incidence, and the ionospheric model should not be a function of these parameters. In the next paragraph it is shown that the dependence on f and ϕ is sufficiently weak that average values can adequately represent the range of interest to LF-VLF.

An adequate approximation for the collision frequency is (Wait and Spies, 1964)

$$v = 5 (10^6) \exp [-0.15(h-70)] = 1.8 (10^{11}) \exp (-0.15h) \quad (5)$$

Assume $v = d \exp [-0.15(h - h_0)]$ and that $N(h) = N_0 \exp (\alpha (h - h_0))$. The reflection height, h_r , is found by solving (4) using (3):

$$\frac{3.18(10^9) N_0 \exp (\alpha (h - h_0))}{2\pi f d \exp (-0.15 (h - h_0))} = \sqrt{2} \cos^2 \phi, \text{ or} \quad (6)$$

$$\exp [(\alpha + 0.15) (h - h_0)] = 2.8(10^{-9}) f \frac{\cos^2 \phi}{N_0} d, \quad (7)$$

Taking the natural logarithm of each side and rearranging yields:

$$h = h_0 + \frac{1}{\alpha + 0.15} \ln \frac{2.8(10^{-9})d}{N_0} + \frac{\ln(f \cos^2 \phi)}{\alpha + 0.15}. \quad (8)$$

The radio frequency and angle of incidence affect only the last term on the right. The denominator of the term, $\alpha + 0.15$, varies from 0.3 to 1.2 (DCA, 1975). Choosing 0.5 as a typical value, the reflection height variation with f and ϕ is $2 \ln (f \cos^2 \phi)$ km -- a factor of 2 variation in $f \cos^2 \phi$ changes the reference height only 1.4 km. For example if $f = 30$ kHz, the height would be within 1.4 km of the correct height for frequencies from 15 kHz

to 60 kHz. Similarly, $\phi = 81^\circ$ will cover angles from 77° to 84° -- and these are by far the most important angles of incidence for long-path VLF-LF propagation.

Therefore, equation (4) with $f = 30$ kHz and $\phi = 81^\circ$ was used to determine the scaling height. The scaling procedure was as follows:

1. If the lower portion of the profile shows electron density increasing, or constant, as the height decreases, discard the profile.
2. Otherwise find the lowest height that satisfies equation (4).
If this height exists on the measured profile, use it and go to 3.
If the height is below the measured profile,
 - a. if there is an established slope to the profile near the bottom, extrapolate it to the height that satisfies equation (4), and proceed to 3.
 - b. Otherwise, discard the profile.
3. Record the height and N at the required height.
4. Fit (by observation) a straight line tangent to the profile at the selected height. Determine α for this straight line.

2.3 Validation of Scaling Rules

Since the ionospheric model is being developed for use in propagation predictions, the salient test of the adequacy of this procedure is comparison of propagation parameters computed for the entire measured profile and the exponential fit. From some 280 profiles collected at the time of the test, a stratified sample was selected: one night and one day profile from each season (winter, summer, equinox) from each of three latitude zones (high, medium, low). There were not enough profiles from low latitudes to do this, so the test was made with 10 test profiles (numbers 70, 159, 167, 169, 247, 250, 300, 317, 343, and 372 from the Appendix).

The electron density and the parameters for an exponential fit were scaled from each profile using the rules above. Then ionospheric reflection coefficients for both representations of each profile were computed for radio waves with frequencies of 20, 40, and 60 kHz incident on the ionosphere at angles of 50° , 60° , 70° , 75° , 78° , 82° , and 84° . The three larger angles in this list are the most important for long-distance VLF and LF propagation.

The values for the measured profile and its exponential fit were compared to determine the error caused by the exponential approximation. For the amplitude of the reflection coefficient, the error (in dB) is

$$20 \log \frac{|R \text{ (for exponential fit)}|}{|R \text{ (for measured profile)}|}$$

where R is the computed reflection coefficient for each case.

The phase error was defined to be

$$\phi(\text{exponential fit}) - \phi(\text{measured profile})$$

where ϕ is the computed phase of the reflection coefficients. The errors were computed for each frequency as a function of angle of incidence. To determine if there were any consistent bias in the scaling procedure, the errors were averaged. The results for the most important reflection coefficient ($|R|$) are shown in Figure 2. The fact that the overall average of the error is small indicates that there is no bias in the scaling procedure.

For estimating the effects of the errors on field strength predictions, the average of the absolute value of the errors is more important. This average is shown for each frequency in Figure 3. In general, the errors are larger for smaller angles of incidence. This could be expected from the scaling rules, since the height at which the electron density gradient was scaled was the "correct" one for an angle of 81° . The errors are also larger for the higher frequencies than for the lower frequencies.

The large errors for small angles of incidence are not too disturbing, because the model is to be used for calculation of field strengths at long distances. For these calculations, angles between 80° and 85° are most important, since the limiting grazing angles for wave hop theory are about 81° or 82° and the real part of the eigen angles of the important wave guide modes are greater than 80° also.

The probable error in field strength can be estimated from the error in reflection coefficients using notions from the wave hop theory. In this theory, the reflection coefficient (in dB) is multiplied by the hop number, so the error in a hop would just be the hop number times the error in the reflection coefficient. The first hop is usually the largest for distances from 1000 to about 3000 km, so the error in field strength in this region should be about the same as the error in the grazing reflection coefficient.

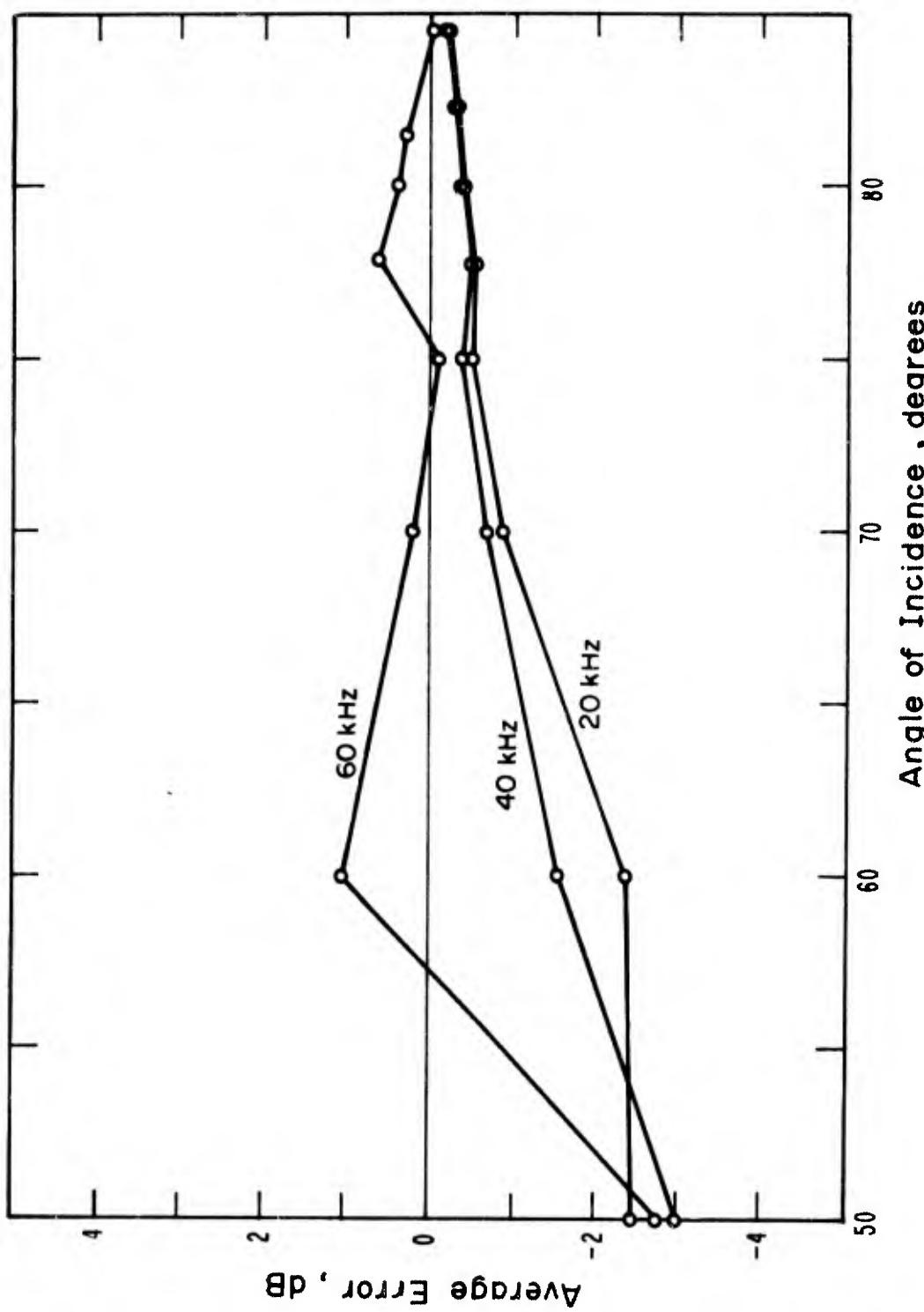


Figure 2. Ten-profile mean of the error in the principle reflection coefficient using the exponential approximation to measured profiles. The mean error, in dB, is shown as a function of angle of incidence for three frequencies.

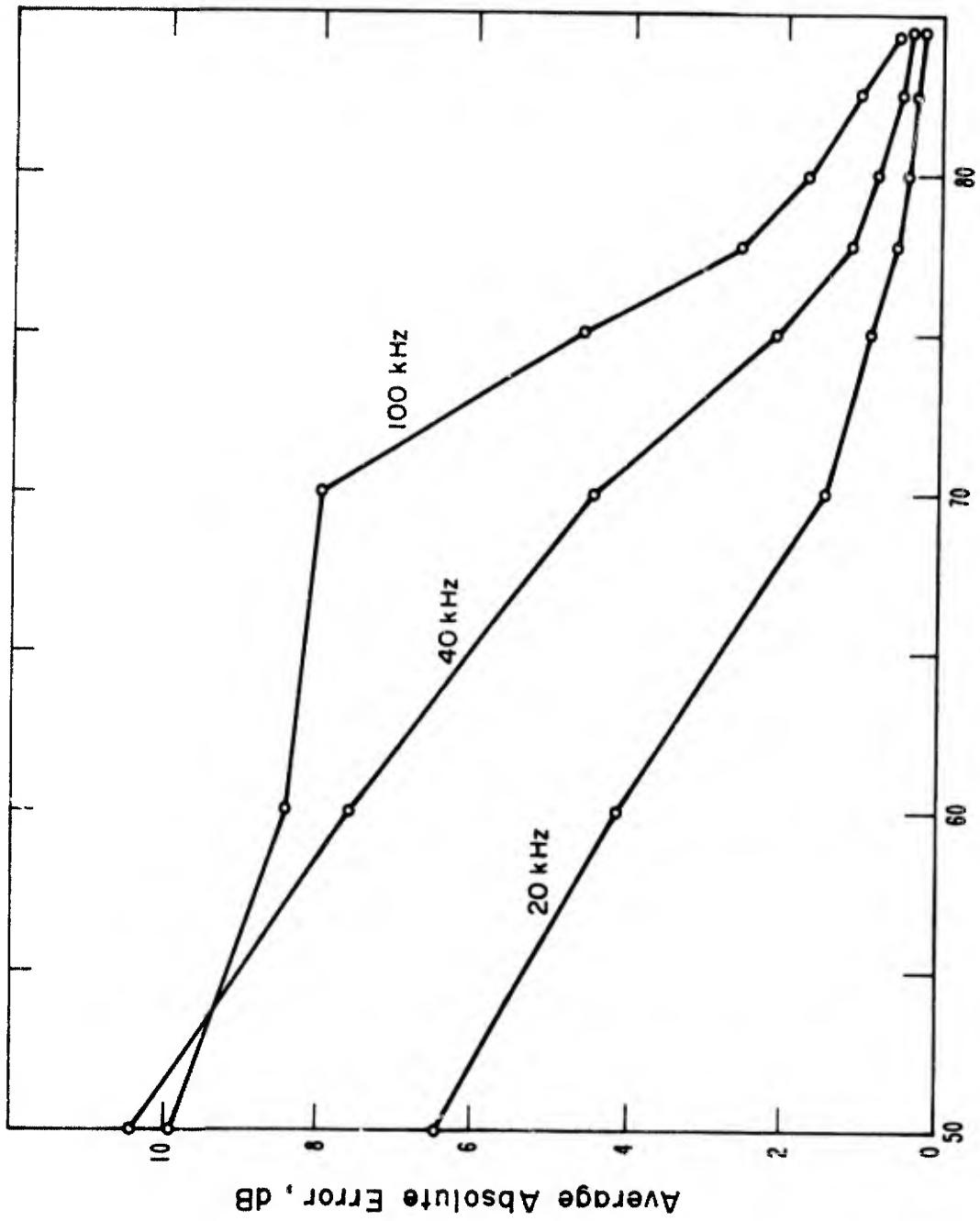


Figure 3. Ten-profile average of the absolute value of the error in the principle reflection coefficient using the exponential approximation to measured profiles. The error in dB is shown as a function of angle of incidence for three frequencies.

From about 3000 km to 5000 km, the second hop predominates, and the error should be twice the error in the reflection coefficient. Between about 5000 km and 7000 km, the error should average about 3 times the error in the reflection coefficient, etc.

Three of the profiles were selected for further testing. One was the profile with the smallest errors in reflection coefficients (profile 167). The second was a profile whose errors most nearly matched the average values (profile 70) and the third was the profile with the largest errors in reflection coefficients (profile 300). The field strength as a function of distance was computed for these three profiles for frequencies of 20, 40, and 60 kHz using the wave hop theory program (Berry and Herman, 1971). The results for 40 kHz are shown in Figures 4, 5, and 6.

Figure 4 is the best case; the field strength curve for the exponential profile can barely be separated from that for the complete profile. The average case is shown in Figure 5. The separation between the two curves gradually increases with distance, but even at 6000 km the difference is acceptable for many practical purposes. The worst case is shown in Figure 6, where the two field strengths are far apart from 5000 km onward.

Notice that in all three cases, even in the worst case, the locations of relative maxima and minima in the two curves are nearly coincident.

The magnitude of errors in field strength can be easily seen in Figure 7, where they are given (in dB) as a function of distance for all three cases. Recall (Figure 3) that the average error in reflection coefficient for grazing incidence was under 1 dB. Thus for the average case (profile 70), the error in field strength from 1000 to 3000 km averages less than 1 dB. From 3000 to 5000 km, the error is between 1 and 2 dB, and so forth. The error in the worst case increases quickly with distance to over 5 dB beyond 5000 km.

The errors in field strength at 20 kHz and 60 kHz are shown in Figures 8 and 9, respectively. These calculations show that the errors in field strength can be estimated accurately from the reflection coefficient errors.

It is interesting to go back and look at the profiles which produced the best, average, and worst results. Profile 167, the best fit, is shown in Figure 10. It is easy to see why the exponential fit (also shown in Figure 10) is an adequate approximation, especially when you note how closely it

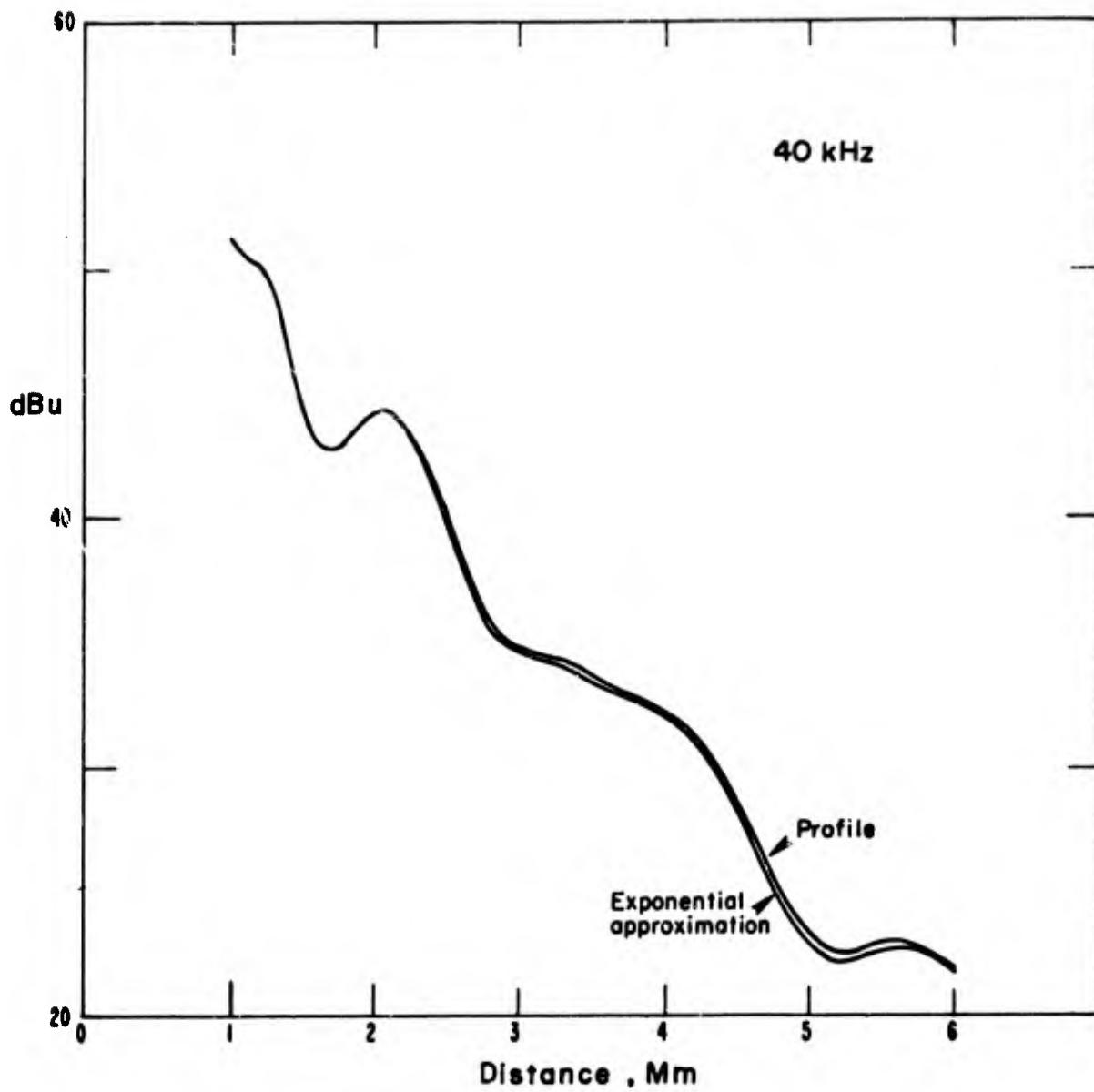


Figure 4. 40 kHz field strength as a function of distance for measured profile 167, and for the exponential approximation to it.

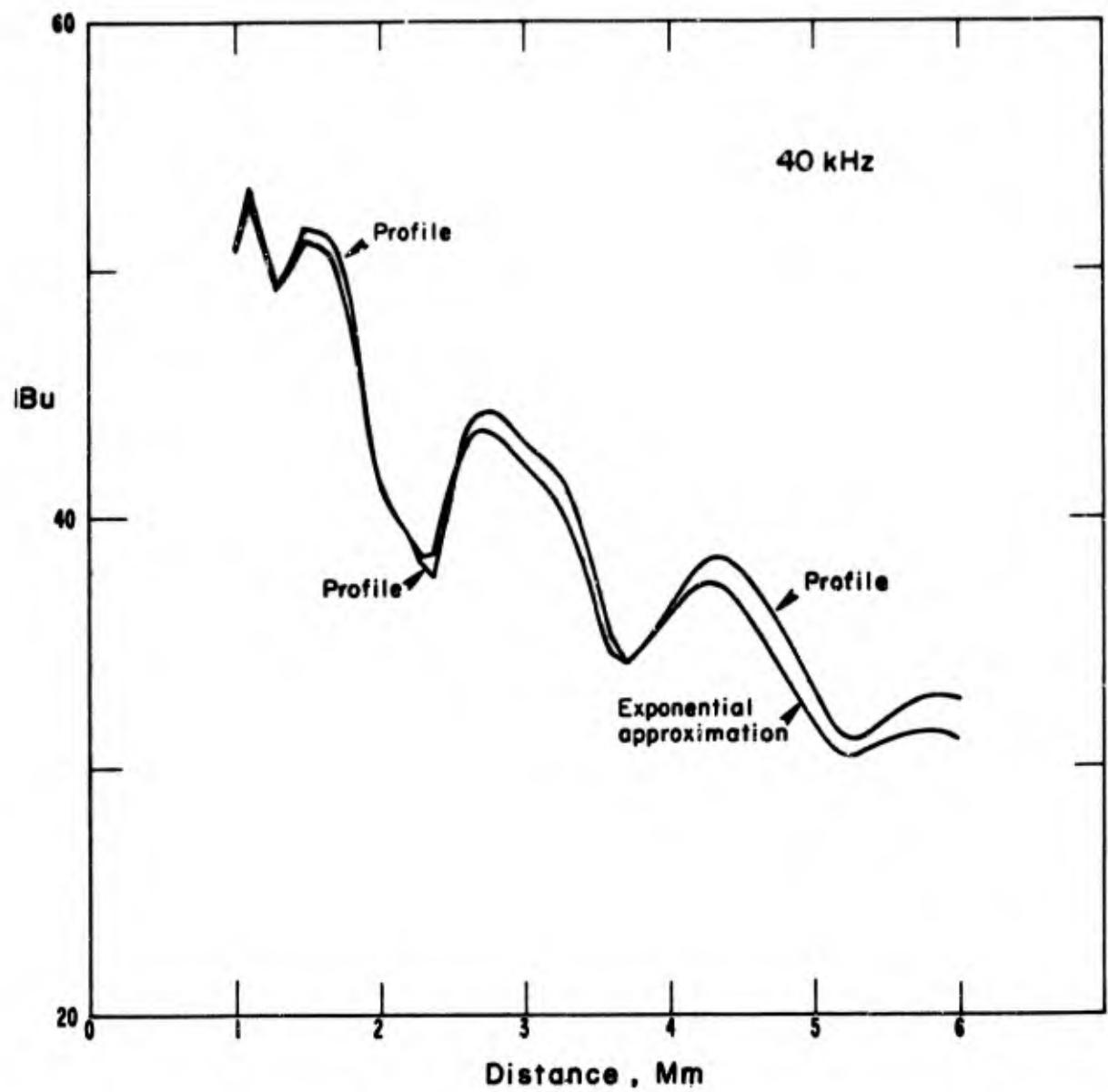


Figure 5. 40 kHz field strength as a function of distance for measured profile 70, and for the exponential approximation to it.

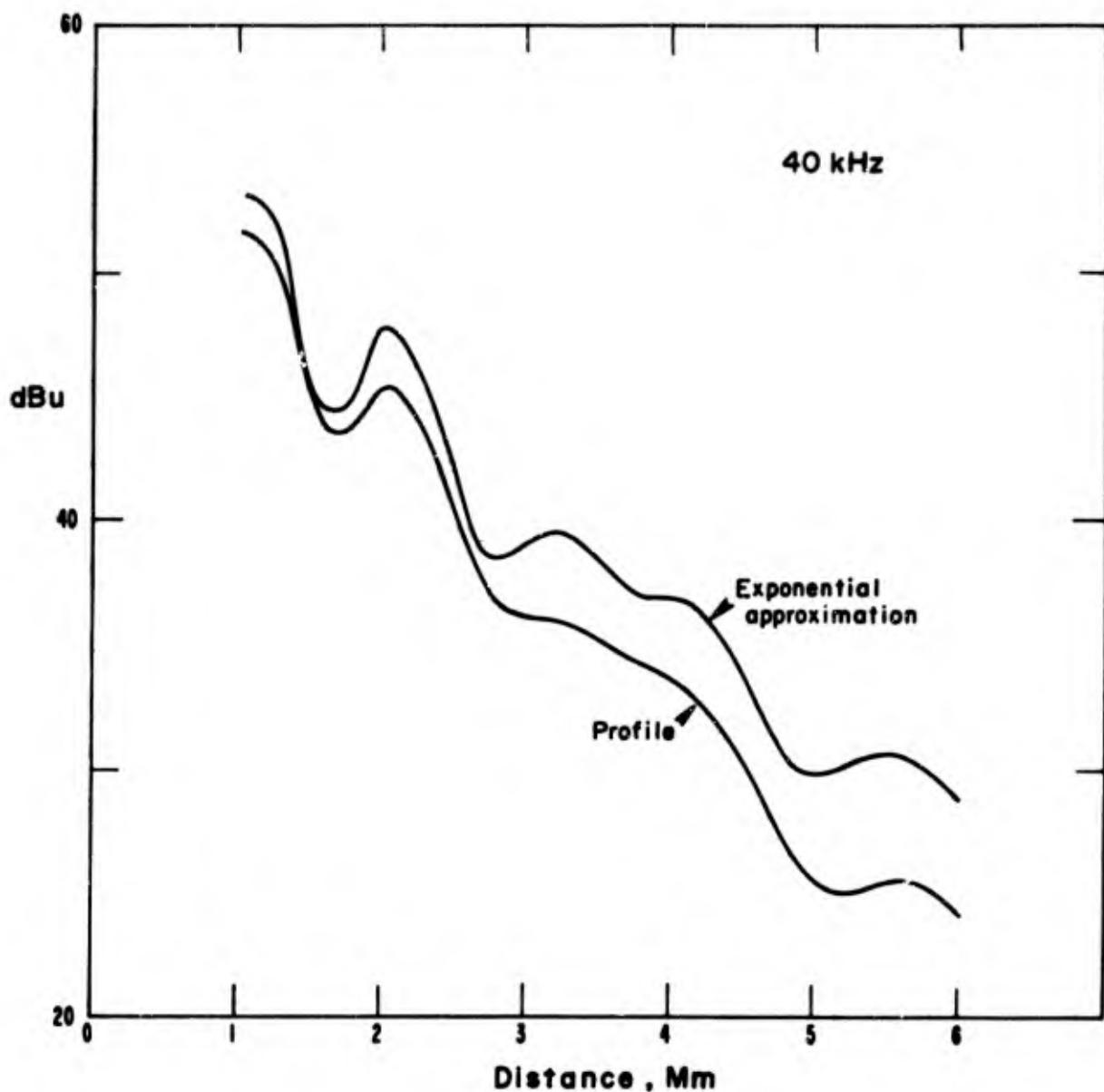


Figure 6. 40 kHz field strength as a function of distance for measured profile 300, and for the exponential approximation to it.

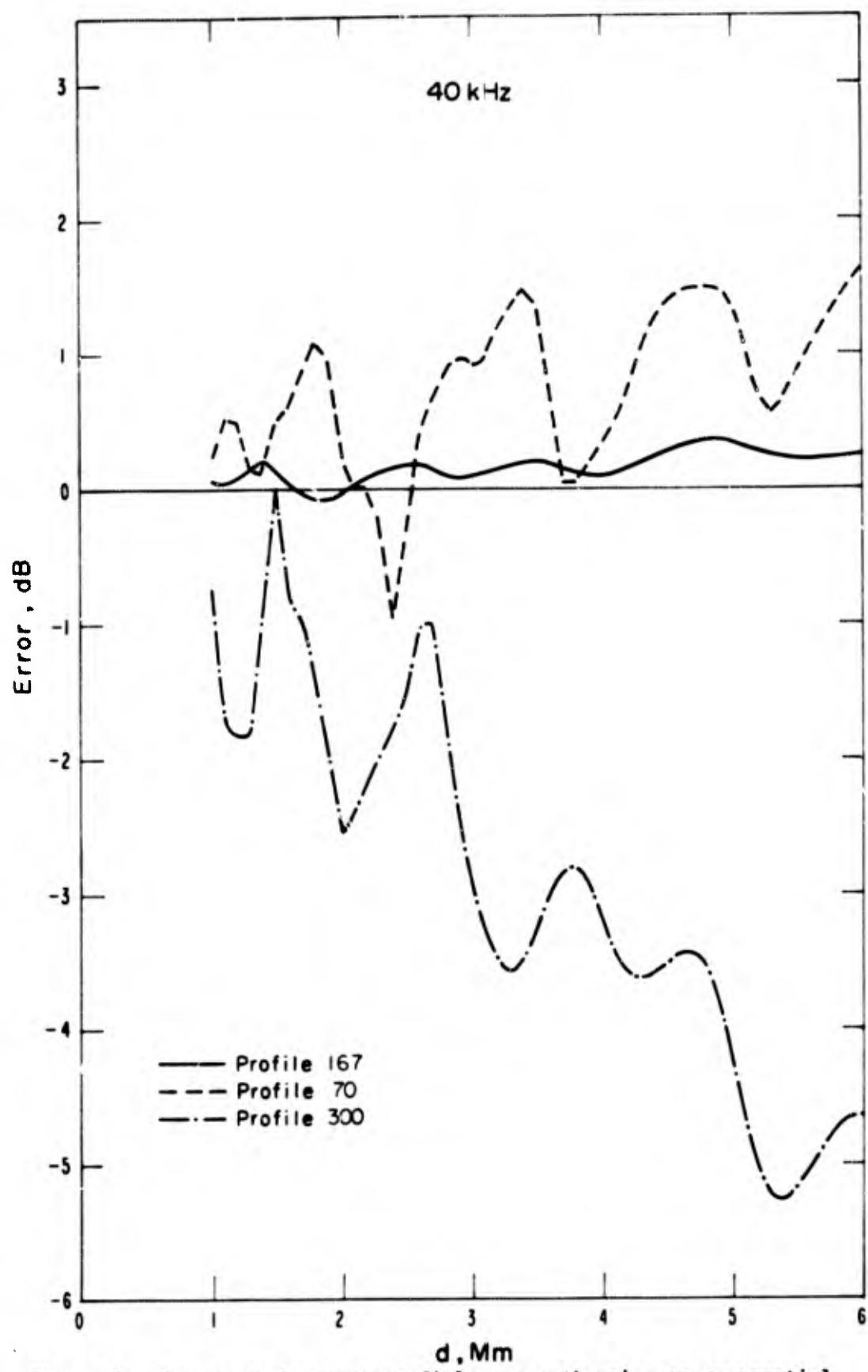


Figure 7. The error in computed field strength using an exponential approximation to a measured electron density profile for a frequency of 40 kHz.

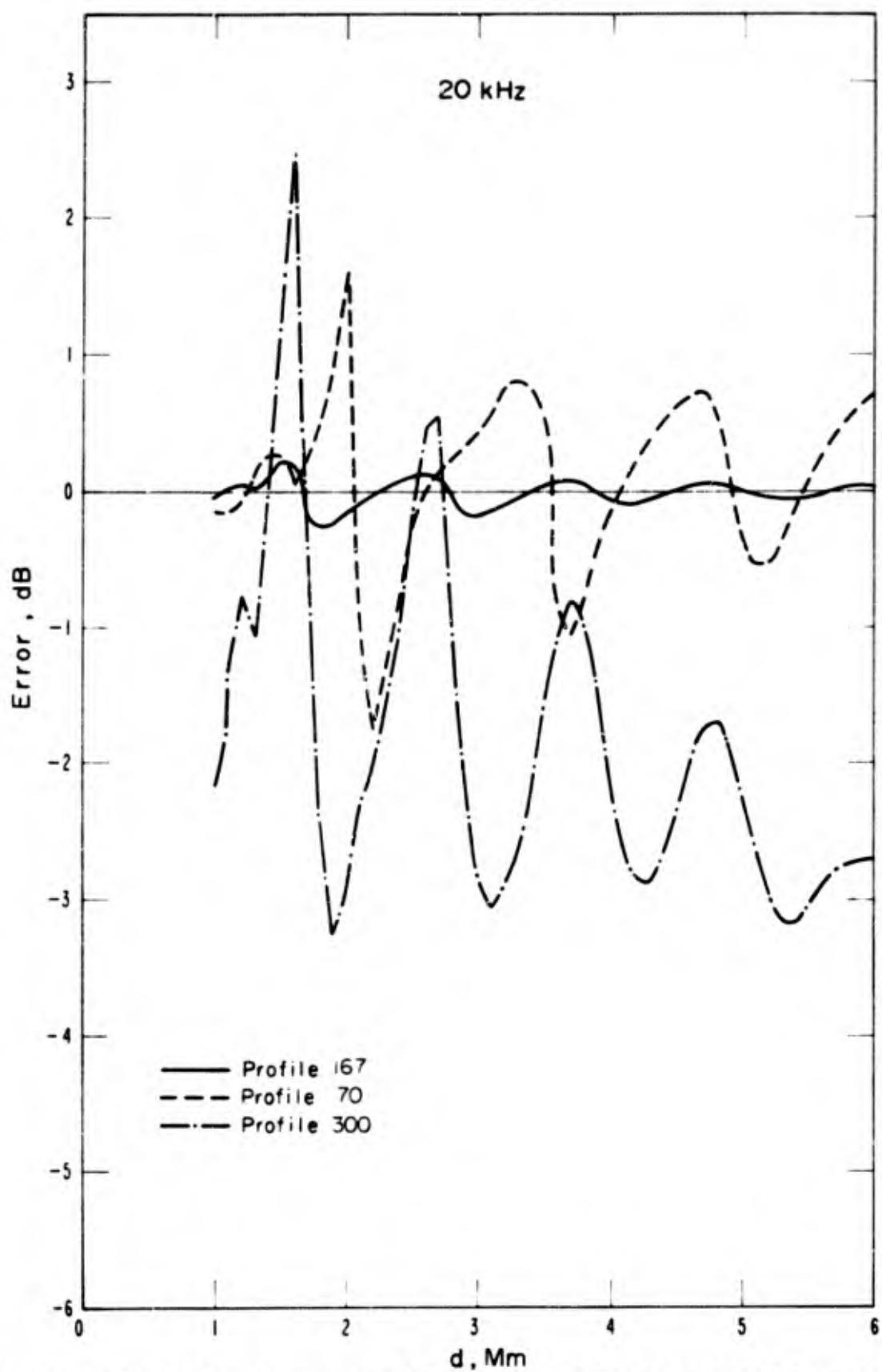


Figure 8. The error in computed field strength using an exponential approximation to a measured electron density profile for a frequency of 20 kHz.

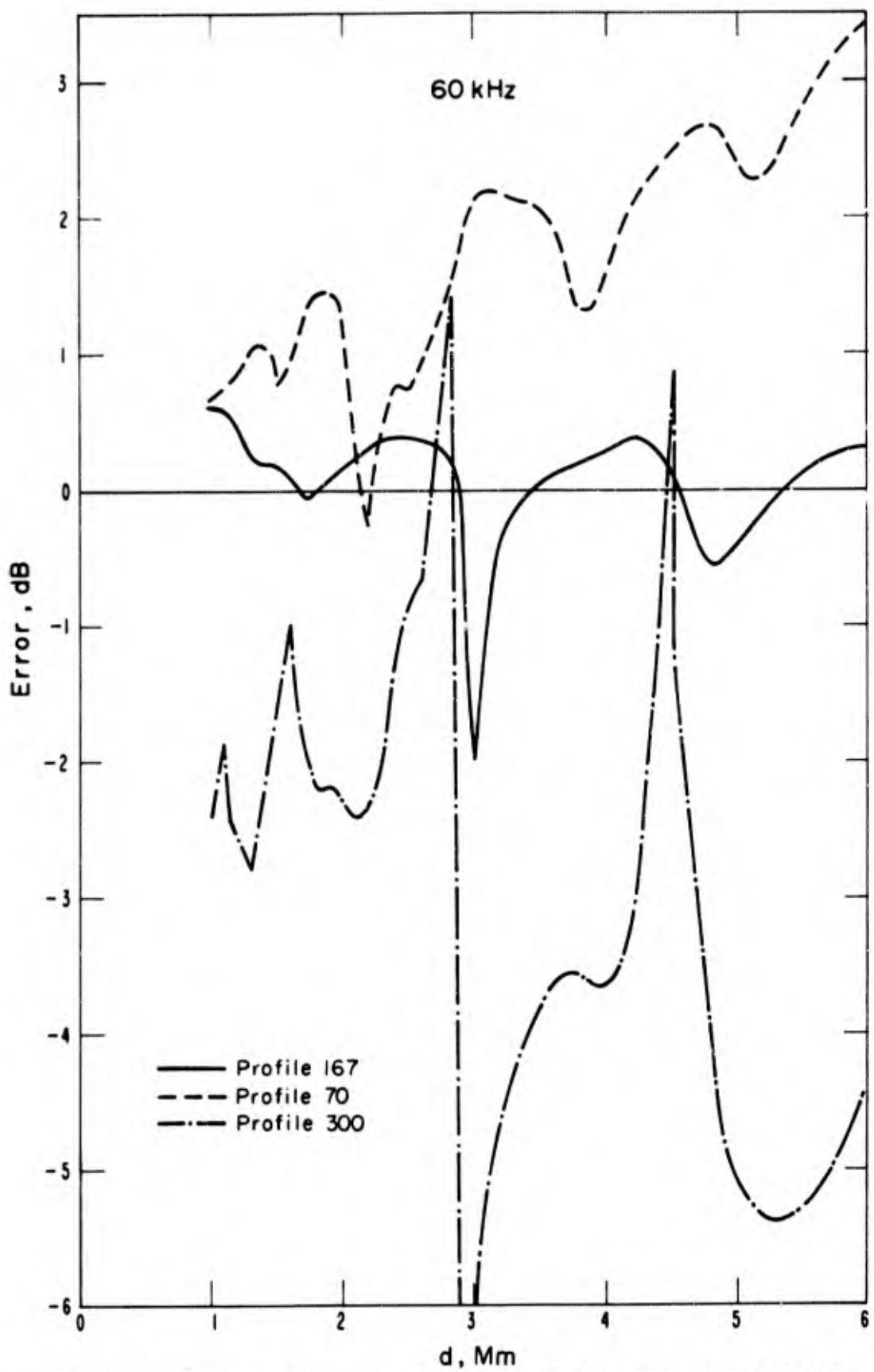


Figure 9. The error in computed field strength using an exponential approximation to a measured electron density profile for a frequency of 60 kHz.

follows the measured profile for many kilometers on each side of the reflection region (marked by an X on the profile).

The fit which produced average errors is shown in Figure 11. The measured profile departs significantly from the straight line fit above 73 km, which leads to larger errors in reflection coefficients for more sharply incident radio waves.

The worst-fit profile is shown in Figure 12. It is obvious that this profile is very unlike the exponential profile also shown on the figure. If all, or even very many, real profiles had the shape of profile 300, the selected scaling process would clearly be inadequate -- and the model would probably need to be more complicated. However, the statistical test conducted with 10 profiles indicates that profiles like the one in Figure 12 are rare.

These tests showed that the exponential model and the scaling procedure are sufficiently accurate, since the average errors in field strength are less than or comparable to the natural variation of VLF-LF propagation over paths less than 6000 km long.

3. DERIVATION OF THE MODEL

The journal and report literature yielded 470 profiles which could be scaled according to the rules in the previous section. The Appendix contains a list of the sources of the profiles, and lists the parameters scaled from the profiles and other necessary information about them such as location, time, and experimental method.

Standardized computer programs exist for performing sophisticated statistical analyses of data. OMNITAB II, produced by the National Bureau of Standards (Hogben, et al., 1971), was used. The analysis is essentially a multidimensional linear regression. The independent variables must be chosen so that, to the extent possible, their influence on the model parameters is linear. Physical reasoning and previous studies of the D region provide clues to the appropriate variables. A final choice follows experimentation with various combinations using the OMNITAB program.

3.1 Selection of Regression Variables

The daytime D region is produced by direct radiation from the sun. Theoretical analysis (Davies, 1965) and experimental analysis (Reid, 1969) have shown that the electron density correlates well with $\cos x$, where x is

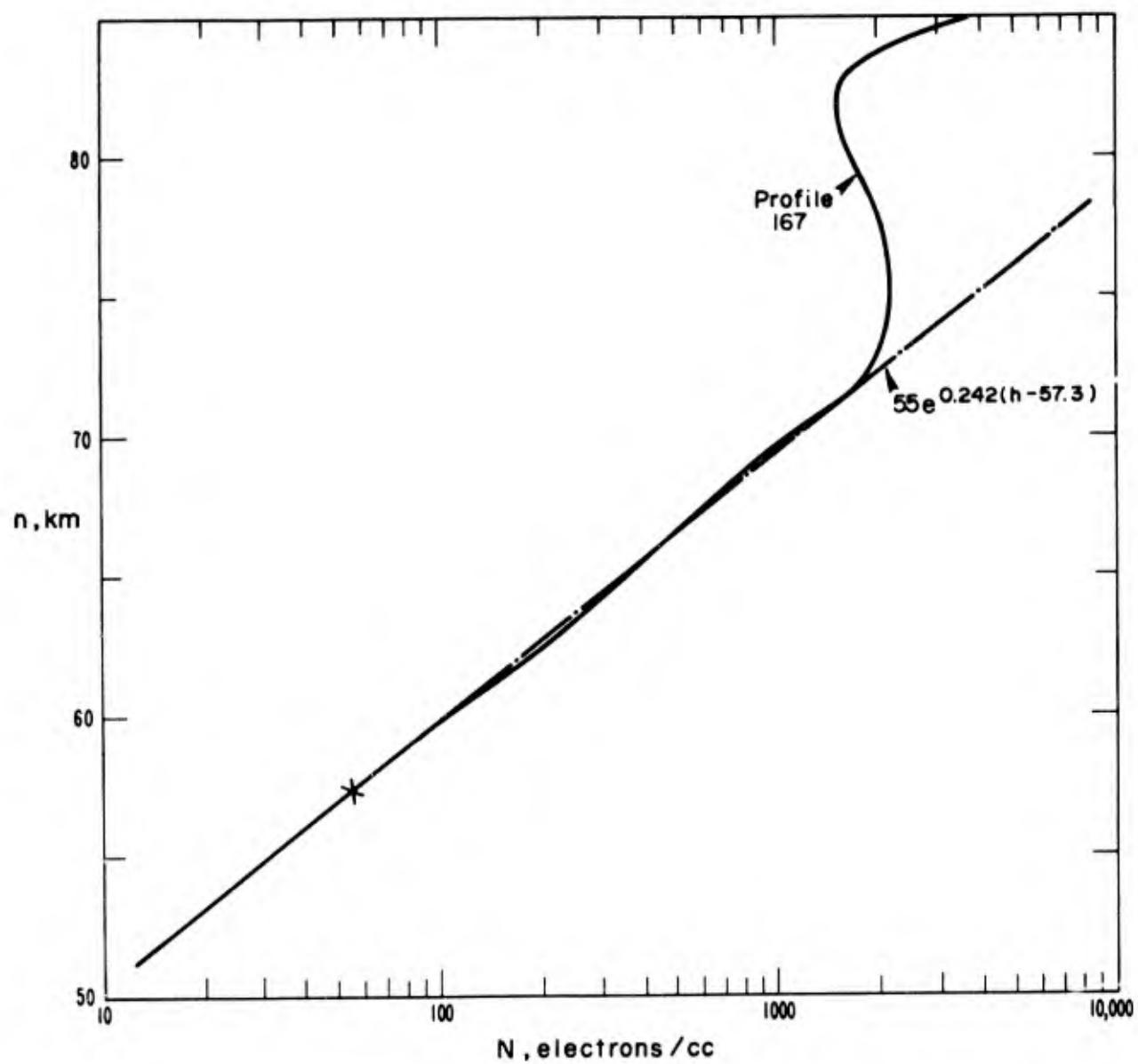


Figure 10. Measured electron density profile 167, and the scaled exponential approximation to it.

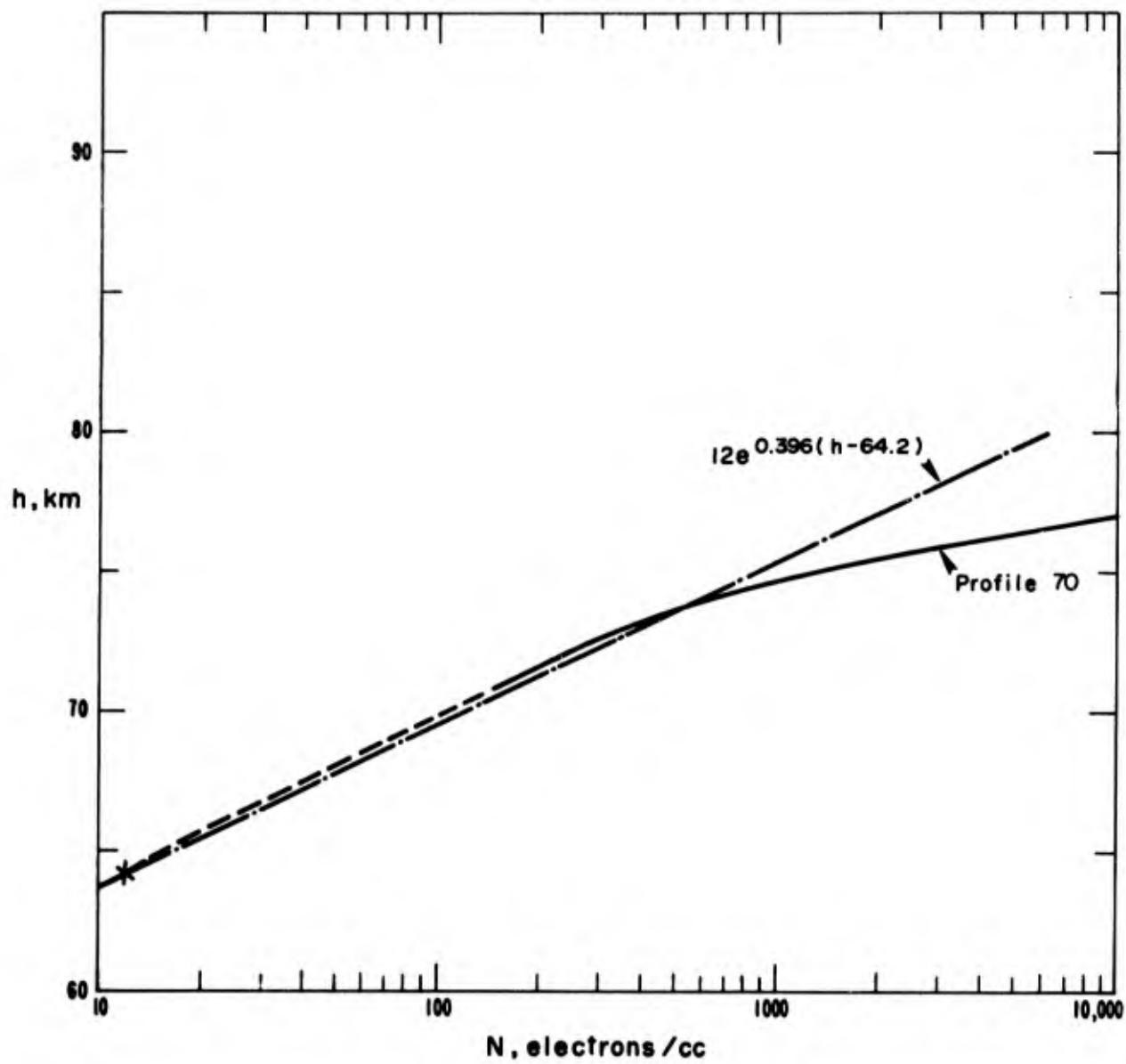


Figure 11. Measured electron density profile 70, and the scaled exponential approximation to it.

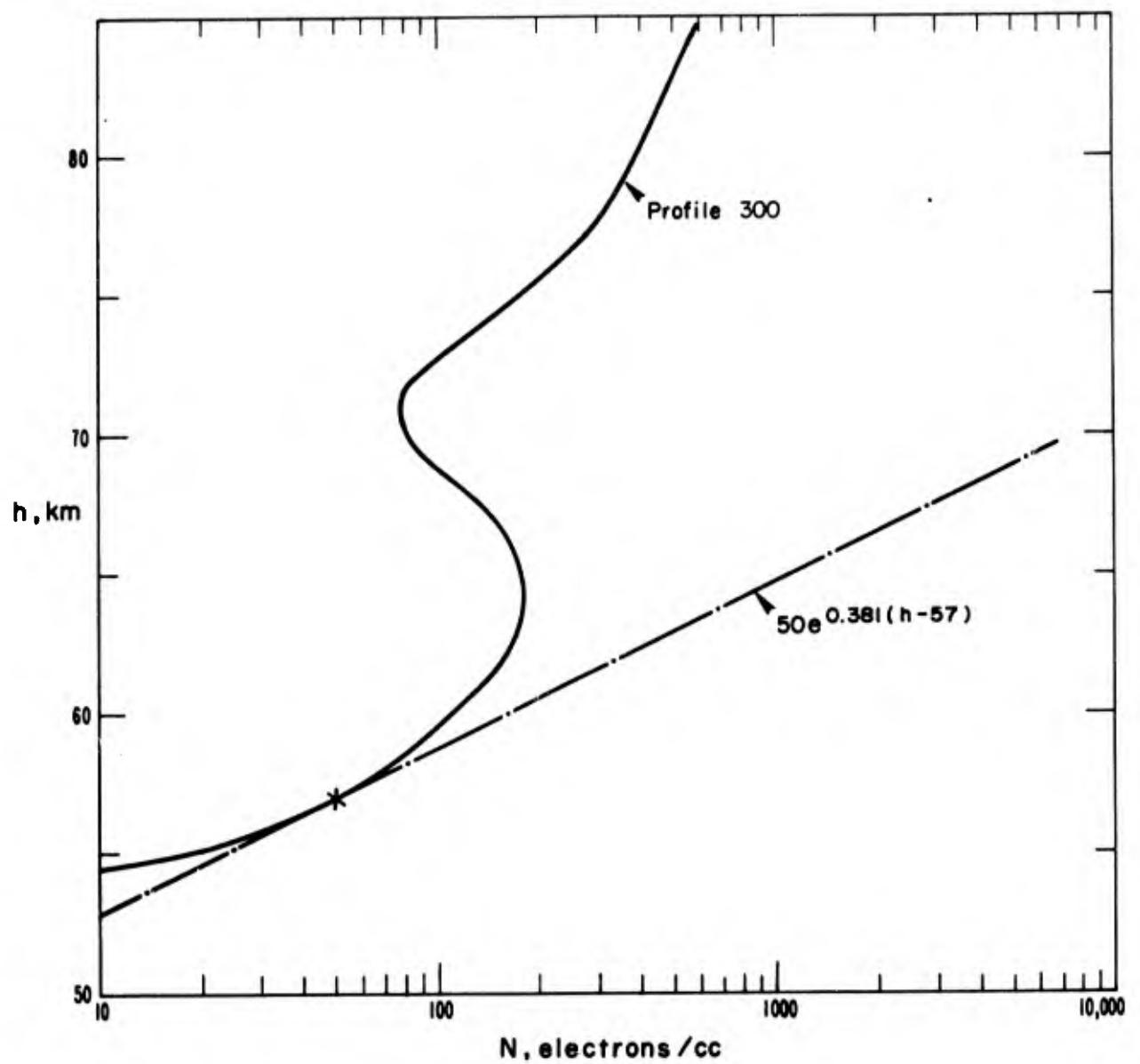


Figure 12. Measured electron density profile 300, and the scaled exponential approximation to it.

the zenith angle of the sun. The zenith angle depends on local time, latitude, and season, so it incorporates in one variable many of the things that influence the D region.

An alternative choice for representing the diurnal variation is the local time. In order to keep the variable cyclic, let the independent variable be $\cos(2\pi(t-12)/24)$ where t is the local hour. This choice has the advantage of being independent of season and latitude, other potential independent variables. Tests with OMNITAB showed that the residual error was smaller if local time rather than sun's zenith angle was used to represent the diurnal variation.

LF-VLF propagation also varies with season, which indicates that the lower ionosphere depends on season. Numbering the months from 1 to 12 beginning with January yields a numerical variable which represents the seasons. A complication is that the year is a cycle, but the month numbers have a discontinuity between December and January. That is, in nature, December and January are very much alike, but in the numbering scheme they are as different as possible, being numbered 12 and 1 respectively. This difficulty is avoided by choosing $\pm \cos(2\pi(m - 1/2)/12)$ as the independent variable instead of the month number. The plus sign is used in the northern hemisphere, and the minus sign in the southern hemisphere so that the seasons will be similar in behavior. January 15 is winter in the northern hemisphere and the variable has the value +1. In order that winter in the southern hemisphere (June 15) have the same value, use the negative sign.

Watt (1967) suggests that VLF phase velocity varies like the cosine of latitude. This also has the advantage of treating north and south latitude the same. So $\cos(\text{latitude})$ was chosen as an independent variable.

Following the practice at high frequencies, the 12 month running average of the Zurich sunspot number was used as an independent variable.

It was necessary to choose carefully the height at which the parameters were scaled as discussed in section 2.2. However, once the three parameters, N_0 , h_r , and α , are known, one of them can be discarded by transforming to the standard reference height h_w (the height where $\omega_r/\omega = 2.5 (10^5)$). This also makes it easier to compare the results with the literature.

3.2 The Regression Model

The model is therefore to have the form

$$N(h) = N_0 \exp (\alpha (h - h_w)) \quad (9)$$

where

$$N_0 = 1.43 (10^7) \exp (-0.15 h_w) \quad (10)$$

so that h_w is the standard reference height. The gradient α and h_w will depend on time (hour and month), latitude, and solar activity.

$$\alpha = \alpha_c + \alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \alpha_4 x_4 \quad \text{and} \quad (11)$$

$$h_w = h_c + h_1 x_1 + h_2 x_2 + h_3 x_3 + h_4 x_4 \quad (12)$$

The α_i and h_i are coefficients determined by a multidimensional linear regression on the independent variables x_i . These variables are:

$$x_1 = \cos \left(\frac{t - 12}{24} 2\pi \right), \text{ where } t \text{ is the local time (hour), } t = 1, 24.$$

$$x_2 = \cos (L), \text{ where } L \text{ is the latitude (radians).}$$

$$x_3 = \pm \cos \left(\frac{m - 1/2}{12} 2\pi \right), \text{ where } m \text{ is the month (January = 1, } \dots \text{December = 12.}$$

(Use + for northern hemisphere, - for southern hemisphere.)

$x_4 = S$, where S is the sunspot number (12 month running average of Zurich relative sunspot number).

The analysis was also done for $x_1 = \cos$ (sun's zenith angle) but the residual error in both h_w and α was greater (slightly) for this set of variables. Table 1 gives the resulting values for α_i and h_i .

Table 1: Values of Coefficients for Statistical Electron Density Model.

i	c	1	2	3	4
h_i	71.8	-3.83	6.85	0.085	-0.047
α_i	0.210	-0.036	0.082	-0.050	0.00045

What is the significance of α_c and h_c ? They are the values of α and h_w at 0600 and 1800 hours on March 15 and September 15 at $\pm 90^\circ$ latitude if the sunspot number is 0.

4. COMPARISONS OF MODEL VARIATIONS WITH VLF PROPAGATION EXPERIENCE

The implications of the regression analysis are shown in Tables 2, 3, and 4. The coefficient of the month term for height is small (not significantly different from zero).

Watt (1967, p. 265) estimates that the phase velocity of a 16 kHz signal increases about one part in 10^{-3} as the sunspot number goes from 0 to 100. This corresponds to a 5 to 10 km decrease in reference height (Wait and Spies, 1964). Coefficient h_4 above would cause a reference height decrease of 4.7 km, which is consistent with the propagation data.

Table 2 shows the values of h_w as a function of hour and latitude. The variation from midnight ($t = 0$) to noon ($t = 12$) is only about 8 km. The mid-latitude noon values of 70 to 72.5 km are consistent with those determined for long path VLF propagation; namely, 70 km (DCA, 1974a) to 75 km (DCA, 1975). However, the nighttime heights are 7-10 km lower than heights deduced from long-path propagation data (DCA, 1974a, 1975). This may be caused by the much smaller data pool for nighttime profiles, by less accurate measurements at night because of the high noise level, or by smoothing of the data in the statistical analysis.

Figure A3 of the Appendix shows the distribution of scaled heights h_w for the nighttime profiles. The mean value is 77.2 km -- much lower than is suggested by VLF propagation data. Measurement of low-level electron density is notoriously difficult. These difficulties are compounded at night by high-noise levels, and perhaps by a more variable (in space and time) lower ionosphere. It is likely that the lower parts of the nighttime profiles used are inaccurate.

Watt (1967, p. 365) estimates an increase at 10 kHz of about $2(10^{-3})$ in phase velocity relative to the speed of light as latitude increases from 0° to 90° . This corresponds to about 7 to 12 km decrease in reference height (Wait and Spies, 1964). Table 2 shows about 7 km decrease in reference height between 0° to 90° latitude.

The other model parameter, α , is equal to $\beta - 0.15$, where β is the parameter most often mentioned in the literature. Propagation measurements lead to daytime estimates of β that range from 0.3 to 0.5 (DCA, 1974a, 1975); that is, α is estimated to range from 0.15 to 0.35. The daytime ($t = 12$) values in Tables 3 and 4 are mostly in this range. The winter

Table 2: Values of h_w computed using equation (4) and Table 1, assuming it is equinox, and that the sunspot number is 30.

Latitude °		Local Time (hours)			
		0	6	12	18
Latitude °	0	81.1	77.2	73.4	77.2
	30	80.1	76.3	72.5	76.3
	60	77.7	73.8	70.0	73.8
	90	74.2	70.4	66.6	70.4

Table 3: Values of α computed using equation (3) and Table 1, and assuming that it is January, and that the sunspot number is 30.

Latitude °		Local Time (hours)			
		0	6	12	18
Latitude °	0	0.293	0.257	0.221	0.257
	30	0.282	0.246	0.210	0.246
	60	0.252	0.216	0.180	0.216
	90	0.211	0.175	0.139	0.175

Table 4: Values of α computed using equation (3) and Table 1, assuming that it is July, and that the sunspot number is 30.

Latitude °		Local Time (hours)			
		0	6	12	18
Latitude °	0	0.376	0.340	0.304	0.340
	30	0.365	0.329	0.293	0.329
	60	0.335	0.299	0.263	0.299
	90	0.294	0.258	0.222	0.258

mid-latitude value of α is about 0.2, and the summer noon value is about 0.27.

Nighttime values of β determined from propagation measurements range from 0.3 to 1.2, corresponding to values of α between 0.15 and 1.05 (DCA, 1975). The ($t = 0$) values in Tables 3 and 4 range from 0.21 to 0.38.

5. CONCLUDING REMARKS AND RECOMMENDATIONS

Summarizing, the multiparameter regression analysis results in variations of the model reference height with latitude and sunspot number that are consistent in direction and magnitude with those deduced from propagation data. However the day-to-night change in reference height is only about half as large as the diurnal change indicated by propagation measurements. The model values for the gradient of electron density, α , are consistent with the most-often-used propagation values, but do not have as large a range.

It is likely that the small number, and/or poor quality of the nighttime profiles caused the day-to-night variation of h_w to be only half as large as is indicated by propagation data. The following recommended steps would probably improve the model:

1. Remove local time from the list of independent variables, and, instead, put in a fixed variation with time which has the required day-to-night variation, as determined by propagation data.
2. Filter the data by making subjective, but careful, judgements about the quality of the data, indicated by the experimental method and controls. Discard the profiles judged to be unreliable.
3. Continue to add high quality profiles to the data base as they become available.
4. Then recompute the coefficients for the remaining variables, separately for day and night.

A realistic time-varying model of the lower ionosphere is necessary for reliable calculations of the time-availability of LF-VLF links in the MEECN system.

6. REFERENCES

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APPENDIX
D-Region Data Base

Table A2 lists the lower ionosphere electron density profiles used in the analysis, along with the parameters N_0 , h_r , and α scaled from the profiles using the scaling rules in Section 2.2. Other relevant data is also listed. (Table A1 defines the column headings of Table A2.) The last column of Table A2 contains a reference to the source of the profile. The full list of references follows Table A2.

Figure A1 shows histograms of the scaled parameter α and the reference height h_w (height satisfying equation (2)) for all the data.

Figures A2 and A3 show histograms of the same parameters for day hours only and night hours only. For figures A2 and A3, sunrise and sunset data have been deleted.

Table A1: Definition of column headings in Table A2.

Column	Heading
A	Profile reference number
B	Year of observation
C	Month of observation
D	Day of observation (00 means unknown or irrelevant)
E	Reference height for scaling α
F	Electron density (electrons/cc) at reference height
G	Exponential profile slope parameter, α
H	Geographic latitude of observation, degrees (south is negative)
I	Local time of observation (hour = 1, 24)
J	Sunspot number for month of observation
K	Methods of observation: 1 = partial reflection 2 = rocket 3 = wave interaction 4 = LF-VLF reflection 5 = other
L	Magnetic disturbance indicator: undisturbed = 1 disturbed = 2
M	Solar eclipse indicator: no eclipse = 1; eclipse = 2
N	Collision frequency profile applicable to observation
O	Geographic longitude of observation (degrees east)
P	Reference to source document

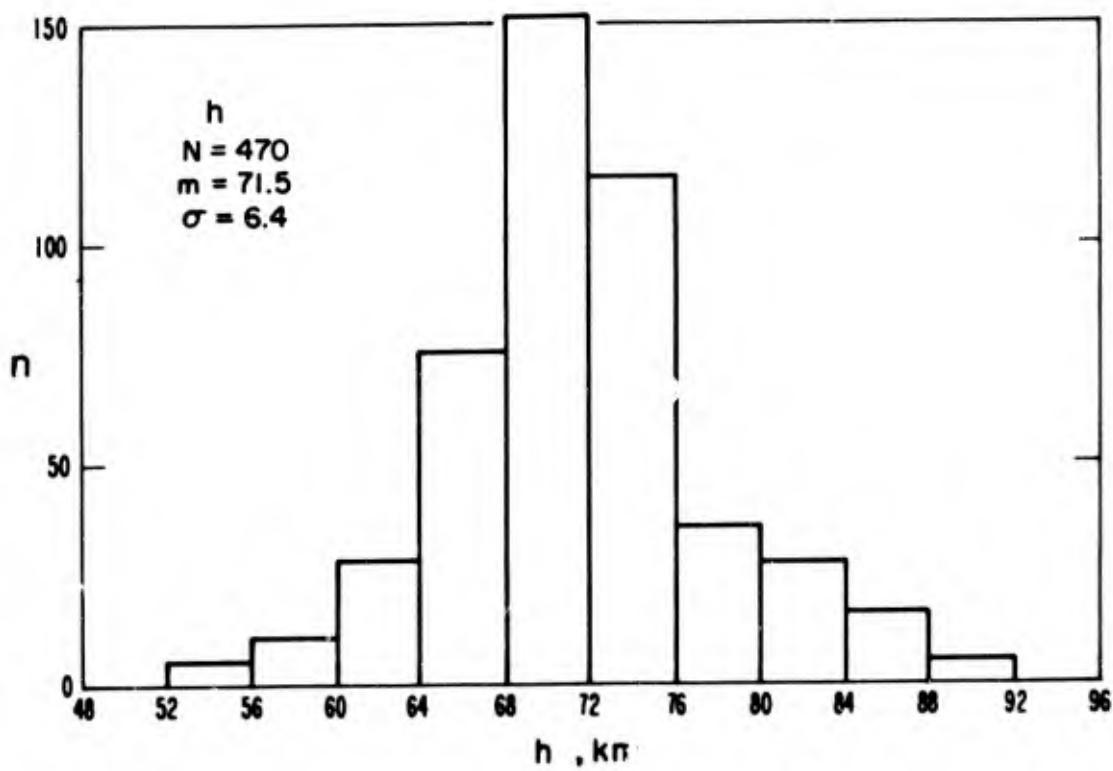
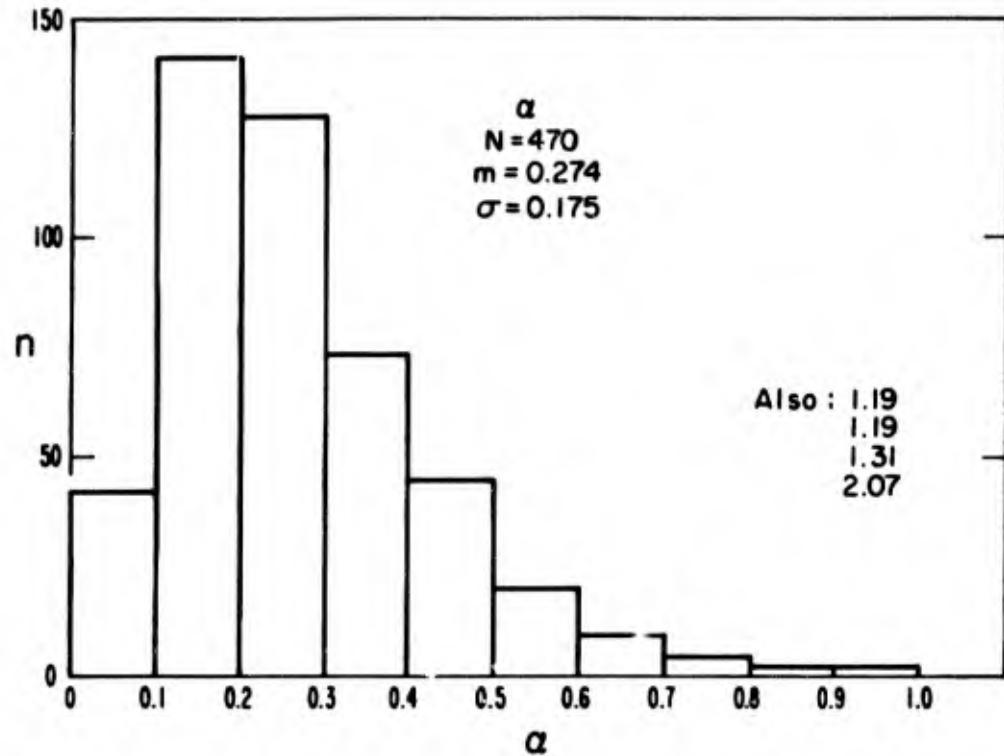


Figure A1. Distribution of scaled α , and reference height h_w for all 470 profiles used in the study. The number of observations, N , the mean, m , and the standard deviation, σ , are shown on the figure.

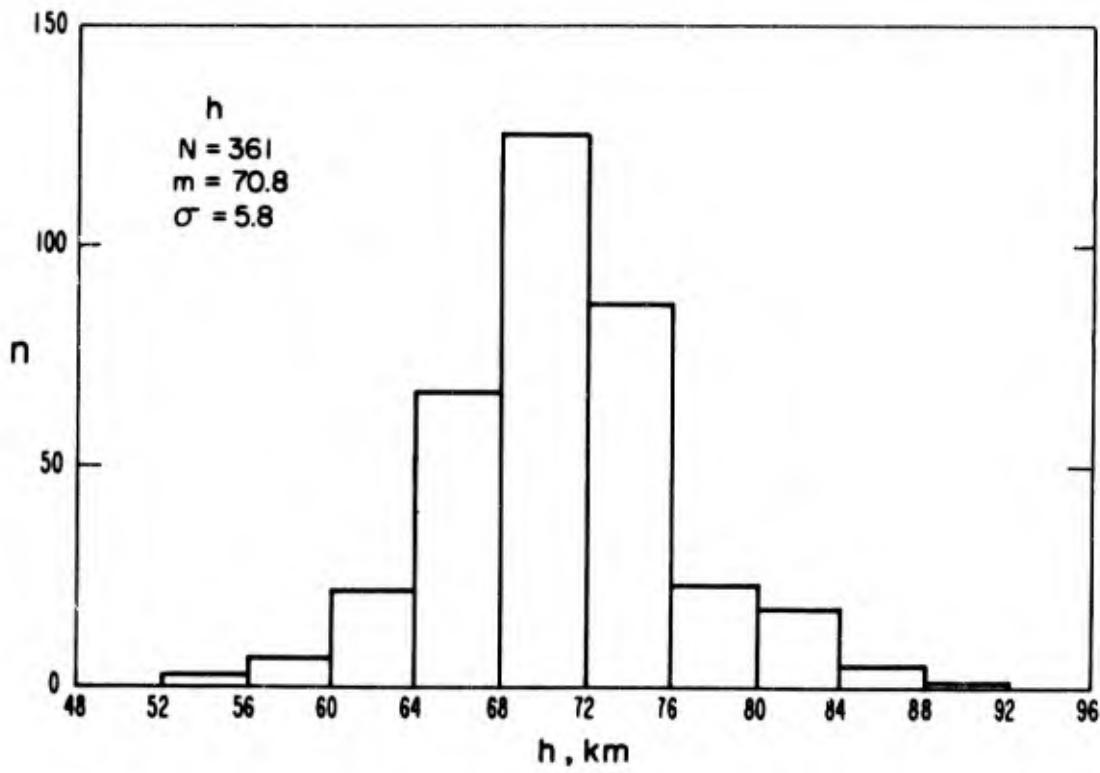
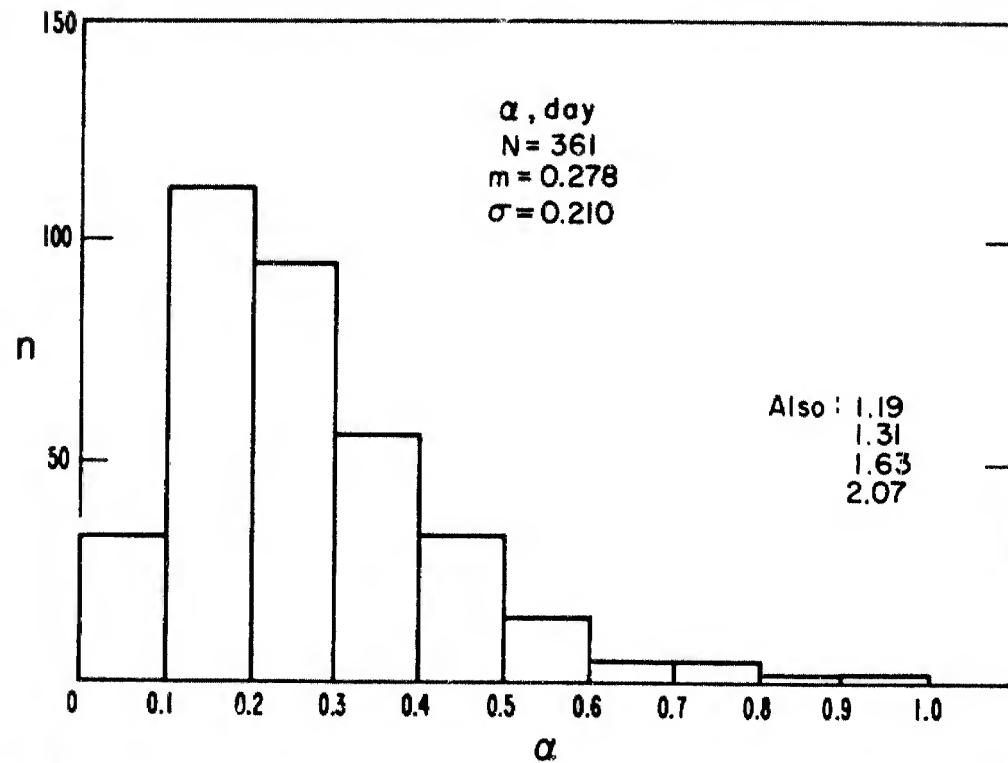


Figure A2. Distribution of scaled α , and the reference height h , for daytime profiles used in the study. The number of observations, N , the mean, m , and the standard deviation, σ , are shown on the figure.

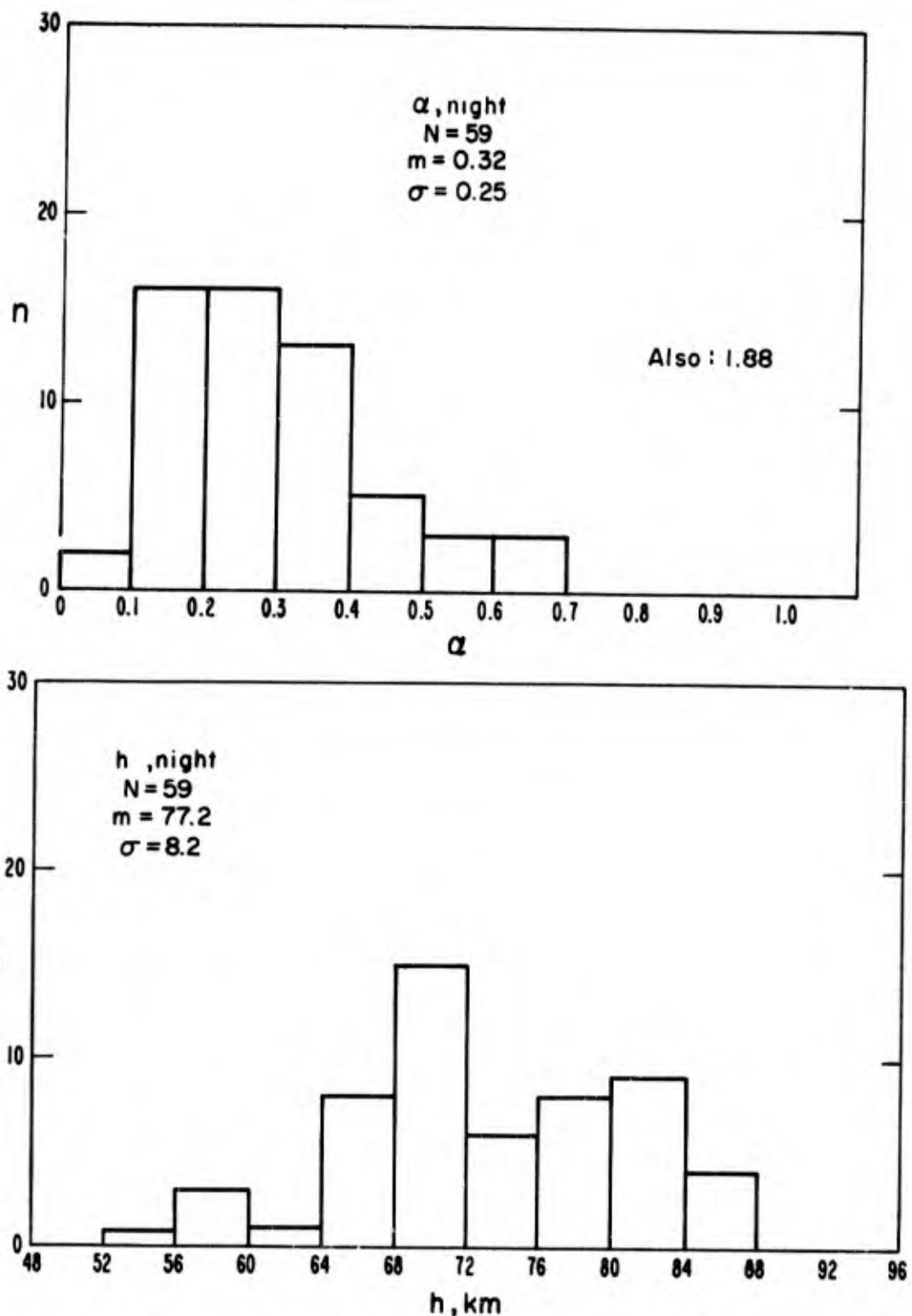


Figure A3. Distribution of scaled α , and reference height h , for night-time profiles used in the study. The number of observations, N , the mean, m , and the standard deviation, σ , are shown on the figure.

TABLE A2: D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

	See Table A1 for Column Headings										P				
	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
A	38	61	03	08	60.0	40.0	22.4	45.4	1200	69	1	1	11	284.1	Belrose and Cetiner (1962)
40	61	05	01	52.0	73.0	0.050	45.4	1040	60	1	1	11	284.1	Belrose and Burke (1964)	
41	61	06	00	59.5	43.0	0.284	45.4	1200	56	1	1	11	284.1	Belrose (1964)	
42	61	07	14	59.5	43.0	0.284	45.4	1130	53	1	1	10	284.1	Belrose (1964)	
43	61	08	17	69.0	8.0	0.204	37.9	2206	52	2	1	20	284.5	Smith (1966)	
44	61	09	20	65.6	82.0	0.157	-31.2	1351	52	4	1	36	136.3	Hall and Bullough (1963)	
45	61	10	27	75.0	3.2	0.174	37.9	0435	51	2	1	20	284.5	Smith (1965)	
46	61	11	00	57.7	55.0	0.132	45.4	1200	50	1	1	11	284.1	Belrose and Bourne (1967)	
47	61	12	00	59.5	39.6	0.115	45.4	1200	49	1	1	11	284.1	Belrose (1965)	
48	61	12	16	61.2	36.0	0.660	45.4	1200	49	1	1	20	284.1	Mechly and Smith (1968b)	
49	61	12	20	68.5	9.5	0.061	45.4	1200	49	1	1	20	284.1	Mechly and Smith (1968b)	
50	61	12	00	65.0	19.0	0.070	45.4	1200	49	1	1	11	284.1	Belrose and Bourne (1967)	
51	62	01	00	61.0	39.0	0.109	45.4	1200	45	1	1	11	284.1	Belrose and Bourne (1967)	
52	62	03	01	53.4	93.0	0.544	45.4	1145	45	1	2	11	284.1	Belrose and Cetiner (1962)	
53	62	03	09	64.8	16.0	0.369	45.4	1200	40	1	1	11	284.1	Belrose and Cetiner (1962)	
54	62	03	00	59.0	52.0	0.136	45.4	1200	40	1	1	11	284.1	Belrose (1965)	
55	62	06	00	58.4	49.0	0.152	45.4	1200	38	1	1	11	284.1	Belrose and Bourne (1967)	
56	62	07	00	56.6	62.0	0.107	45.4	1200	37	1	1	11	284.1	Belrose (1965)	
57	62	07	00	55.1	76.0	0.095	45.4	1200	37	1	1	11	284.1	Belrose and Bourne (1967)	
58	62	08	11	56.8	126.0	0.115	60.0	0450	35	1	1	32	11.1	Holt (1963)	
59	62	08	15	70.4	7.4	0.162	-31.2	0050	35	4	1	34	136.3	Hall and Fooks (1965)	
60	62	08	18	51.4	240.0	0.165	69.3	0809	35	2	2	1	14	16.0	Jesperson, Haug & Landmark (1966)
61	62	08	00	58.0	51.0	0.106	45.4	1200	35	1	1	11	284.1	Belrose and Bourne (1967)	
62	62	09	00	56.2	62.0	0.182	45.4	1200	33	1	1	11	284.1	Belrose (1965)	
63	62	10	21	60.0	135.0	0.221	40.6	1210	31	3	1	16	282.1	Rowe et al. (1970)	
64	62	10	21	56.6	260.0	0.081	40.8	1239	31	3	1	2	16	282.1	Rowe et al. (1970)
65	62	11	07	77.8	2.1	0.406	37.9	0525	30	2	1	20	284.5	Smith (1963)	
66	62	11	30	71.3	5.7	0.197	37.9	0557	30	2	1	20	284.5	Smith (1963)	
67	62	11	30	55.2	78.0	0.120	45.4	1200	30	1	1	11	284.1	Belrose and Bourne (1967)	
68	62	12	05	62.2	27.5	0.131	37.9	1760	30	2	1	20	284.5	Smith (1963)	
69	62	12	11	54.0	39.0	0.166	69.3	0427	30	2	2	14	16.0	Jesperson et al. (1964)	
70	62	12	14	64.2	12.0	0.396	69.3	2152	30	2	2	14	16.0	Jesperson, Haug & Landmark (1966)	
71	63	02	27	55.0	74.0	0.248	37.9	1430	30	2	1	20	284.5	Smith (1963)	
72	63	03	08	63.1	19.0	0.227	37.9	0950	30	2	1	23	284.5	Aikin (1972)	

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters
See Table A1 for Column Headings

	P	N	O	Aikin, Kane and Troim (1964)
J	29	2	1	29
K	29	4	1	20
L	37	1	1	13
M	28	2	1	11
N	28	2	1	11
O	28	2	1	11
P	28	2	1	11
G	302	37.9	1530	284.5 Aikin, Kane and Troim (1964)
F	• 260	37.9	0030	284.5 Cartwright (1964)
E	18.6	60.0	60.0	44.0 1200
D	63.5	56.0	60.0	56.8 1503
C	63.0	56.0	60.0	40.3 1513
B	63.0	56.0	60.0	67.2 1540
A	73	63	70	58.9 50.2
	74	63	67	50.2 100.0
	75	63	67	65.7 17.5
	76	63	67	20 55.2
	77	63	67	20 65.1
	78	63	67	20 67.2
	79	63	67	20 58.9
	80	63	67	20 65.7
	81	63	67	20 55.2
	82	63	67	26 54.5
	83	65	67	0 58.0
	84	63	69	12 55.6
	85	67	63	10 25 67.9
	86	68	63	10 31 51.5
	87	69	65	10 00 59.1
	88	90	63	11 14 61.5
	89	91	65	12 00 77.4
	90	92	65	12 00 54.2
	91	93	64	01 00 65.0
	92	94	64	01 00 67.0
	93	95	64	01 00 65.3
	94	96	64	01 00 64.0
	95	97	64	01 00 64.7
	96	98	64	02 18 65.0
	97	99	64	03 12 57.6
	98	100	64	03 15 64.4
	99	101	64	03 00 22.0
	100	102	64	03 00 59.3
	101	103	64	03 00 57.5
	102	104	64	03 00 72.0
	103	105	64	03 00 73.3
	104	106	64	07 00 80.2
	105	107	64	03 00 75.2
	106	108	64	03 00 60.0

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

	See Table A1 for Column Headings										P
	F	G	H	I	J	K	L	M	N	O	
A											
109	64	03	00	60.0	74.0	•22.3	40.0	000.0	14.4	1.1	0.9
110	64	03	00	60.0	74.0	•25.3	40.0	100.0	14.4	1.1	0.9
111	64	03	00	60.2	76.0	•31.0	40.0	120.0	14.4	1.1	0.9
112	64	04	16	59.5	40.0	•18.8	37.9	160.5	13.2	1.1	2.0
113	64	06	22	62.0	33.0	•20.3	-30.5	142.0	10.3	1.1	3.4
114	64	06	22	61.0	39.0	•07.6	-30.5	144.0	10.3	1.1	3.4
115	64	06	22	61.0	37.5	•12.6	-30.5	154.0	10.3	1.1	3.4
116	64	06	24	63.5	25.0	•41.9	-30.5	123.5	10.3	1.1	3.4
117	64	07	15	79.1	1.8	•61.6	37.9	030.0	16.2	1.1	2.0
118	64	07	15	76.5	2.5	•69.7	37.9	042.0	10.2	1.1	2.0
119	64	07	15	61.2	29.0	•38.4	37.9	052.5	10.2	1.1	2.0
120	64	07	00	64.6	19.0	•12.7	74.7	030.0	10.1	1.1	1.1
121	64	07	00	62.9	26.0	•16.0	74.7	12.0.0	10.1	1.1	1.1
122	64	08	00	57.5	86.0	•08.4	69.5	060.0	10.1	1.1	1.4
123	64	08	00	59.5	66.0	•10.9	69.5	12.0.0	10.1	1.1	1.4
124	64	08	30	61.5	46.0	•15.1	69.5	17.0.0	10.1	1.1	1.4
125	64	08	26	52.8	100.0	•14.3	37.9	12.0.0	10.2	1.1	2.0
126	64	08	00	59.4	55.0	•09.5	40.0	012.0.0	10.4	1.1	1.5
127	64	08	00	60.4	122.0	•26.2	40.0	012.0.0	10.4	1.1	1.9
128	64	09	01	61.2	35.0	•55.9	-30.5	17.15	10.3	1.1	3.4
129	64	09	00	63.3	13.5	•17.6	60.0	12.0.0	10.1	1.1	1.1
130	64	10	00	64.8	18.0	•08.5	35.2	064.5	10.3	1.1	1.8
131	64	10	00	63.0	24.0	•33.1	35.2	081.0	10.3	1.1	1.8
132	64	10	00	61.5	29.0	•29.7	35.2	093.5	10.3	1.1	1.8
133	64	10	00	60.7	43.0	•31.5	35.2	11.0.0	10.3	1.1	1.8
134	64	10	00	60.4	33.0	•34.0	35.2	11.30	10.3	1.1	1.8
135	64	10	00	61.5	30.0	•41.8	35.2	12.30	10.3	1.1	1.8
136	64	10	00	61.5	30.0	•36.2	35.2	13.00	10.3	1.1	1.8
137	64	10	00	62.0	27.0	•35.4	35.2	14.00	10.3	1.1	1.8
138	64	10	00	63.0	23.0	•32.3	35.2	15.00	10.3	1.1	1.8
139	64	10	00	66.2	19.5	•30.7	35.2	16.00	10.3	1.1	1.8
140	64	10	00	65.0	17.0	•09.0	35.2	17.00	10.3	1.1	1.8
141	64	10	07	64.5	17.5	•23.6	37.9	18.04	10.2	1.1	2.0
142	64	10	08	79.5	1.6	•40.5	37.9	052.3	10.2	1.1	2.0

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
143	64	10	27	60.4	41.0	26.7	58.8	120.0	10	2	2	1	11	265.8	Ulwick et al. (1968)	
144	64	10	27	64.4	26.0	.41.0	58.8	120.0	10	2	2	1	11	265.8	Ulwick et al. (1968)	
145	64	11	19	61.3	30.0	.104	37.9	152.0	10	2	1	20	284.5	Mechtly, Bowhill and Smith (1972)		
146	64	11	23	65.0	16.0	.248	37.9	1207	10	2	1	20	284.5	Bourdeau et al. (1966)		
147	65	12	30	62.1	25.0	.085	37.9	1000	10	1	1	20	284.5	Mechtly and Smith (1967b)		
148	64	12	30	74.2	6.5	.169	40.0	0000	12	4	1	1	9	00.0	Deeks (1966)	
149	64	12	30	62.4	50.0	.112	40.0	1200	12	4	1	1	9	00.0	Deeks (1966)	
150	64	03	30	69.2	10.0	.529	58.8	0000	12	2	2	1	11	265.8	Belrose and Bourne (1967)	
151	64	00	00	66.0	15.0	.259	58.8	0000	12	2	1	11	265.8	Belrose and Bourne (1967)		
152	65	01	08	81.0	1.5	.205	-30.5	1935	12	3	1	34	151.5	Smith, Coyne, Loch & Bourne (1967)		
153	65	01	08	66.4	17.0	.490	-30.5	1903	12	3	1	34	151.5	" " "		
154	65	01	08	66.2	16.5	.119	-30.5	1920	12	3	1	34	151.5	" " "		
155	65	01	08	65.9	9.7	.172	-30.5	1925	12	3	1	40	151.5	Smith et al. (1967)		
156	65	01	08	68.1	7.1	.197	-30.5	1930	12	3	1	40	151.5	Smith et al. (1967)		
157	65	01	08	83.5	1.0	.304	-30.5	1941	12	3	1	34	151.5	Smith, Coyne, Loch & Bourne (1967)		
158	65	02	06	53.2	100.0	.137	74.7	1200	12	1	1	11	265.4	Hewitt (1969)		
159	65	02	08	62.0	28.0	.176	74.7	1200	12	1	1	11	265.1	" "		
160	65	02	11	75.0	4.0	.240	74.7	1200	12	1	1	11	265.1	" "		
161	65	03	08	71.8	6.5	.253	58.8	0000	13	1	1	11	265.8	Belrose, Bourne and Hewitt (1967)		
162	65	03	09	63.1	22.5	.219	58.8	0000	13	1	1	11	265.8	Belrose, Bourne and Hewitt (1967)		
163	65	03	16	72.5	5.4	.362	-12.8	1151	13	2	1	18	281.8	Aikin and Blumle (1968)		
164	65	03	18	67.8	13.0	.254	-12.8	0141	13	2	1	18	283.1	" "		
165	65	03	18	74.7	4.3	.432	-12.8	1138	13	2	1	18	282.0	" "		
166	65	03	20	65.0	18.5	.237	-12.9	0820	13	2	1	18	282.0	Hechtly et al. (1969)		
167	65	03	20	57.3	55.0	.242	-13.0	1204	13	2	1	18	282.1	Smiddy and Sagalyn (1967)		
168	65	03	21	53.2	72.0	.136	69.3	0659	13	2	2	14	16.0	Jesperson et al. (1968)		
169	65	03	22	78.8	2.1	.282	-13.0	0349	13	2	1	18	282.2	Smiddy and Joyalyn (1967)		
170	65	03	24	69.6	9.0	.303	-11.4	1207	13	2	1	18	281.6	Aikin and Blumle (1968)		
171	65	03	26	67.6	12.0	.228	-10.2	1113	13	2	1	18	280.6	" "		
172	65	03	27	64.2	20.0	.260	-12.2	2000	13	2	1	18	281.2	Haug and Thrane (1967)		
173	55	03	00	70.5	8.0	.720	-19.3	0730	13	1	1	19	17.7	Belrose, Bourne and Hewitt (1967)		
174	65	03	00	60.4	33.0	.134	58.8	0800	13	1	1	11	265.8	Belrose, Bourne and Hewitt (1967)		
175	65	03	00	69.0	10.0	.727	-19.3	0915	13	1	1	19	17.7	Haug and Thrane (1967)		

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

	See Table A1 for Column Headings										P				
	G	H	I	J	K	L	M	N	O						
A	177	65	0.3	0.0	66.6	15.0	55.1	-19.3	110.0	1.3	1	19	17.7	Haug and Thrane (1967)	
B	178	65	0.3	0.0	69.2	31.6	116	58.8	120.0	1.3	1	11	265.8	Belrose, Bourne and Hewitt (1967)	
C	179	65	0.3	0.0	64.6	20.0	38.8	-19.3	135.0	1.3	1	19	17.7	Haug and Thrane (1967)	
D	180	65	0.3	0.0	65.0	18.5	36.6	-19.3	143.5	1.3	1	19	17.7	" "	
E	181	65	0.3	0.0	65.5	17.5	36.1	-19.3	152.5	1.3	1	19	17.7	" "	
F	182	65	0.3	0.0	69.1	10.0	44.9	-19.3	150.0	1.3	1	19	17.7	" "	
G	183	65	0.3	0.0	70.1	8.0	51.3	-19.3	165.0	1.3	1	19	17.7	" "	
H	184	65	0.3	0.0	75.2	3.7	40.1	-19.3	182.7	1.3	1	19	17.7	Throne et al. (1968)	
I	185	65	0.3	0.0	59.5	40.0	10.3	45.4	151.0	1.3	1	11	284.1	Belrose, Hewitt and Bunker (1969)	
J	186	65	0.3	0.0	70.9	7.4	26.5	74.7	12.0	1.3	1	11	265.1	Belrose, Bourne and Hewitt (1967)	
K	187	65	0.3	0.0	61.0	20.0	11.3	60.0	120.0	1.3	1	2	11.1	Throne et al. (1968)	
L	188	65	0.4	0.5	59.8	40.0	13.4	-29.6	88.6	14	2	1	18	284.8	Mechtly et al. (1969)
M	189	65	0.4	0.6	69.5	67.0	7.5	-44.6	14.1	14	2	1	18	282.2	" "
N	190	65	0.4	1.2	68.6	11.0	38.3	-58.5	121.4	14	2	1	18	282.0	" "
O	191	65	0.4	0.0	77.5	3.8	31.8	-19.3	0.000	14	5	1	9	17.7	Gruschwitz (1974)
P	192	65	0.4	0.0	68.8	19.0	0.59	-19.3	0.000	14	5	1	9	17.7	" "
Q	193	65	0.4	0.0	61.1	62.0	12.4	-19.3	120.0	14	5	1	9	17.7	" "
R	194	65	0.4	0.0	71.5	12.5	11.0	-19.3	190.0	14	5	1	9	17.7	" "
S	195	65	0.4	0.0	66.4	6.3	28.4	60.0	120.0	14	1	1	2	11.1	Throne et al. (1968)
T	196	65	0.5	1.9	59.8	28.0	17.3	-31.2	143.3	15	4	1	21	136.3	Hall (1973)
U	197	65	0.5	2.8	61.0	24.0	12.3	-35.0	120.0	15	1	1	21	173.0	Gregory and Manson (1967)
V	198	65	0.5	2.7	60.5	35.0	15.8	58.6	175.9	15	1	1	21	173.0	Belrose, Bourne and Hewitt (1967)
W	199	65	0.5	2.7	58.7	46.0	23.6	58.8	175.9	15	2	1	11	265.8	Belrose, Bourne and Hewitt (1967)
X	200	65	0.5	3.0	75.0	3.0	23.5	-35.0	173.3	15	2	1	12	175.0	Kane and Troim (1967)
Y	201	65	0.6	1.4	70.6	6.5	62.7	37.9	0.413	15	2	1	20	284.5	Mechtly and Smith (1968a)
Z	202	65	0.6	1.7	59.8	39.0	11.9	37.9	164.1	15	2	1	20	284.5	Mechtly and Smith (1968b)
AA	203	65	0.6	2.2	76.0	29.0	39.9	37.9	230.0	15	2	1	20	284.5	Smith (1970)
AB	204	65	0.6	2.6	56.0	73.0	10.9	45.4	120.0	15	4	1	11	284.1	Belrose and Segal (1967)
AC	205	65	0.9	0.1	70.0	7.4	23.6	37.9	0.617	17	2	1	20	284.5	Heikkila et al. (1967)
AD	206	65	0.9	1.1	66.0	16.0	35.8	35.2	120.0	17	1	1	33	25.0	Throne (1966)
AE	207	65	0.9	1.1	67.9	12.5	36.0	35.2	151.0	17	1	1	33	25.0	" "
AF	208	65	0.9	1.1	68.6	11.0	40.8	35.2	160.4	17	1	1	33	25.0	" "
AG	209	65	0.9	1.1	65.6	16.5	16.1	35.2	161.2	17	1	1	33	25.0	" "
AH	210	65	0.9	1.5	61.2	30.0	14.0	37.9	152.8	17	2	1	20	284.5	Mechtly, Bowhill and Smith (1972)

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
211	65	09	04	64.1	18.8	.225	35.2	0910	17	1	1	19	25.0	Haug and Thrane (1967)	
212	65	09	00	66.0	16.5	.346	35.2	1015	17	1	1	19	25.0	" " "	
213	65	09	00	66.8	14.0	.363	35.2	1200	17	1	1	19	25.0	" " "	
214	65	11	00	63.5	21.0	.252	35.2	1335	17	1	1	19	25.0	" " "	
215	65	09	00	68.9	10.0	.380	35.2	1445	17	1	1	19	25.0	" " "	
216	65	09	00	67.6	12.0	.268	35.2	1535	17	1	1	19	25.0	" " "	
217	65	09	00	68.0	11.5	.280	35.2	1645	17	1	1	19	25.0	" " "	
218	65	11	10	71.3	77.2	.132	30.4	2210	22	2	1	18	273.3	Sagalyn, Smidly & Sullivan (1967)	
219	65	11	17	72.8	55.0	.209	30.4	2320	22	2	1	18	273.3	Sagalyn et al. (1967)	
220	65	12	15	62.8	24.0	.083	37.9	1200	24	2	1	20	284.5	Mechtly and Shirke (1968)	
221	66	01	10	59.2	40.0	.159	37.9	1200	26	2	1	20	284.5	Mechtly and Shirke (1968)	
222	66	02	22	60.2	25.0	.276	69.3	1929	31	2	2	18	16.0	Jesperson et al. (1968)	
223	66	02	24	60.5	24.3	.337	69.3	0015	31	2	2	18	16.0	" " "	
224	66	03	09	62.5	14.9	.234	69.3	2320	34	2	2	18	16.0	" " "	
225	66	03	10	70.0	15.1	.384	69.3	2326	34	2	2	18	16.0	" " "	
226	66	03	22	67.4	7.2	.696	69.3	0004	34	2	2	18	16.0	" " "	
227	66	04	07	70.6	6.2	.203	37.9	2301	37	2	1	20	284.5	Heikkila et al. (1967)	
228	66	05	15	63.2	30.0	.278	38.0	1151	41	2	1	27	23.6	Jesperson and Pederson (1970)	
229	66	05	16	64.2	20.0	.274	35.2	1530	41	2	1	19	25.0	Thrane (1966)	
230	66	05	20	62.6	25.0	.291	36.8	1000	41	2	1	2	21.9	Kane (1969)	
231	66	05	20	65.0	17.5	.359	36.8	1045	41	2	1	18	21.9	" " "	
232	66	05	20	70.5	7.5	.258	36.8	1130	41	2	1	18	21.9	" " "	
233	66	05	20	64.8	19.0	.335	36.8	1215	41	2	1	18	21.9	" " "	
234	66	05	20	61.5	30.0	.261	36.8	1300	41	2	1	18	21.9	" " "	
235	66	05	20	67.2	26.0	.692	35.2	1010	41	1	2	19	25.0	Haug et al. (1970)	
236	66	05	20	64.1	20.0	.464	35.2	1055	41	1	2	19	25.0	" " "	
237	66	05	20	62.8	25.0	.263	35.2	1105	41	1	2	19	25.0	" " "	
238	66	05	20	66.3	15.0	.222	35.2	1137	41	1	2	19	25.0	" " "	
239	66	05	20	57.5	53.0	.061	38.0	1140	41	2	1	19	23.6	" " "	
240	66	05	20	57.6	54.0	.100	35.2	1215	41	1	2	19	25.0	" " "	
241	66	05	20	63.2	24.0	.387	35.2	1225	41	1	2	19	25.0	" " "	
242	66	05	20	57.5	58.0	.104	35.2	1235	41	1	2	19	25.0	" " "	
243	66	05	20	56.0	71.0	.148	38.0	1239	41	2	1	19	23.6	" " "	
244	56	05	20	52.0	143.0	.073	35.2	1255	41	1	2	19	25.0	" " "	

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
245	66	05	20	56.5	22.0	375	35.2	1305	41	1	1	19	25.0	Haug et al. (1970)	
246	66	05	20	56.5	63.5	68.8	38.0	1100	41	2	1	19	23.6	" "	
247	66	06	14	71.8	5.6	567	37.9	0418	45	2	1	20	284.5	Mechtly and Smith (1968a)	
248	66	06	26	+7.8	137.0	177	69.3	1200	45	2	1	14	16.0	Riedler (1969)	
249	66	06	26	52.0	208.0	197	69.3	2247	45	2	2	11	16.0	Pederson, Troim and Kane (1970)	
250	66	07	15	63.3	22.5	195	74.7	1200	50	1	1	11	265.1	Hewitt (1969)	
251	66	07	17	56.0	67.0	108	74.7	1200	50	1	1	11	265.1	Hewitt (1969)	
252	66	07	00	51.3	83.0	057	-43.6	1200	50	1	1	2	172.8	Austin (1971)	
253	66	09	28	69.3	9.0	584	58.8	1200	63	2	2	11	265.5	Ulwick et al. (1968)	
254	66	09	28	66.5	15.0	410	58.8	1200	63	2	2	11	265.8	Ulwick et al. (1968)	
255	66	10	29	52.2	115.0	082	31.6	1728	68	2	1	18	130.5	Oya and Obayashi (1966)	
256	66	10	20	52.0	125.0	382	31.6	1734	68	2	1	18	130.5	Oya and Obayashi (1966)	
257	66	11	05	63.6	17.5	786	-32.2	6955	70	2	1	20	307.8	Ulwick (1972)	
258	66	11	10	60.2	51.0	158	-32.2	1700	70	1	1	20	307.6	Von Biel et al. (1970)	
259	66	11	19	62.5	19.0	285	-32.2	1745	70	1	1	20	307.6	Von Biel et al. (1970)	
260	66	11	12	68.8	8.0	469	-32.2	0954	70	2	1	20	307.8	Ulwick (1972)	
261	66	11	12	68.0	9.4	515	-32.2	1010	70	2	1	18	307.8	Mechtly, Seino and Smith (1969)	
262	66	11	12	69.0	8.2	438	-32.2	1011	70	2	1	18	307.8	Mechtly, Seino and Smith (1969)	
263	66	11	12	75.0	3.3	1.186	-32.2	1014	70	2	1	18	307.8	Mechtly, Seino and Smith (1969)	
264	66	11	12	59.8	39.0	245	-32.2	1200	70	2	1	18	307.8	Mechtly (1972)	
265	66	11	20	57.8	36.0	183	69.3	0138	70	2	1	28	16.0	Jesperson et al. (1968)	
266	66	12	13	51.0	148.0	061	32.3	1200	73	2	1	20	253.5	Hale, Hoult and Baker (1968)	
267	66	00	00	63.9	2.5	458	40.0	0000	50	4	1	15	50.0	Krasnushkin and Knyazeva (1970)	
268	67	01	31	63.7	18.0	357	37.9	1200	75	2	1	20	284.5	Sechrist et al. (1969)	
269	67	03	04	59.6	22.0	204	69.3	0058	82	2	1	2	16.0	Jesperson et al. (1967)	
270	67	03	12	70.0	7.0	338	8.6	1857	82	2	1	20	76.9	Prakash et al. (1968)	
271	67	03	12	75.8	2.7	478	8.6	1857	82	2	1	20	76.9	Prakash et al. (1968)	
272	67	03	15	59.6	22.0	154	69.3	0046	82	2	1	2	16.0	Jesperson et al. (1968)	
273	67	04	27	57.0	56.0	352	45.4	1200	85	1	1	11	284.1	Berrose (1970)	
274	67	05	03	53.0	98.0	279	45.4	1220	87	1	1	11	284.1	Berrose (1970)	
275	67	07	00	61.0	24.0	141	-4.4	01200	92	1	1	21	173.0	Austin and Manson (1969)	
276	67	09	27	62.0	31.0	170	40.0	01432	95	2	1	18	9.0	Sturges (1973)	
277	67	10	07	69.0	10.0	277	40.0	01550	95	2	1	18	9.0	Sturges (1973)	
278	67	10	13	62.2	41.0	289	69.3	05550	95	2	1	14	16.0	Folkestad et al. (1969)	
279	67	10	13	62.2	41.0										

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters
See Table A1 for Column Headings

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
280	67	10	24	63.7	21.0	271	18.5	1314	95	2	1	18	292.8	Sagalyn and Wand (1971)	
281	67	10	27	61.6	31.0	228	18.5	1314	95	2	1	18	292.8	Booker and Smith (1970)	
282	67	11	20	59.5	20.7	183	69.3	0137	97	2	1	2	16.0	Riedler (1968)	
283	67	11	00	63.0	2	19.5	26.0	6.9	1260	97	5	1	23	81.0	Mitro and Chakrabarty (1971)
284	67	12	29	58.4	47.0	247	40.8	1300	101	3	1	25	282.1	Lee and Ferraro (1969)	
285	67	12	30	57.6	59.0	181	45.4	1200	101	1	1	11	284.1	Belrose et al. (1968)	
286	67	12	00	57.3	49.6	132	40.8	0900	102	3	1	25	282.1	Rowe et al. (1969)	
287	67	12	14	57.2	51.2	165	40.8	0900	102	3	1	25	282.1	" "	
288	68	01	08	57.1	51.5	212	40.9	1500	102	3	1	25	282.1	" "	
289	68	01	01	53.9	108.0	222	45.4	1200	103	1	1	11	294.1	Belrose et al. (1968)	
290	68	01	02	47.1	29.0	073	45.4	1200	103	1	1	11	284.1	Lee and Ferraro (1969)	
291	68	01	05	57.5	55.0	330	40.8	1100	103	3	1	25	282.1	Lee and Ferraro (1969)	
292	69	01	15	54.8	82.0	500	45.4	1200	103	1	1	11	284.1	Belrose (1970)	
293	68	01	16	59.0	40.0	230	37.9	1400	103	2	1	2	20	Aikin (1972)	
294	69	01	16	62.1	25.0	289	37.6	1430	103	2	1	2	20	Aikin (1972)	
295	69	01	18	59.2	35.0	211	40.8	0900	103	3	1	25	282.1	Lee and Ferraro (1969)	
296	68	01	18	60.4	29.0	123	40.8	1100	103	3	1	25	282.1	" "	
297	68	01	18	58.0	45.0	338	40.8	1300	103	3	1	25	282.1	" "	
298	68	01	18	59.2	35.0	211	40.8	1500	103	3	1	25	282.1	" "	
299	68	01	22	58.0	45.0	318	40.8	1100	103	3	1	25	282.1	" "	
300	58	01	22	57.0	50.0	381	40.8	1300	103	3	1	25	282.1	" "	
301	68	01	22	59.2	36.0	194	40.8	1500	103	3	1	25	282.1	" "	
302	68	01	23	59.0	39.0	188	40.5	1100	103	3	1	25	282.1	" "	
303	68	01	23	57.7	48.0	277	40.8	1300	103	3	1	25	282.1	" "	
304	68	01	23	57.7	48.0	277	40.8	1500	103	3	1	25	282.1	" "	
305	68	01	30	59.0	38.0	236	40.8	0900	103	3	1	25	282.1	" "	
306	68	01	30	59.0	38.0	239	40.8	1100	103	3	1	25	282.1	" "	
307	68	01	30	55.3	67.0	144	40.8	1300	103	3	1	25	282.1	" "	
308	68	01	30	55.2	46.0	217	40.8	1500	103	3	1	25	282.1	" "	
309	68	01	31	59.2	36.0	183	40.8	0900	103	3	1	25	282.1	" "	
310	68	01	31	59.2	36.0	183	40.8	1100	103	3	1	25	282.1	" "	
311	68	01	31	57.5	50.0	240	40.8	1300	103	3	1	25	282.1	" "	
312	68	01	31	57.5	50.0	240	40.8	1500	103	3	1	25	282.1	" "	
313	69	01	00	59.0	40.0	258	40.8	1200	103	3	1	25	282.1	" "	

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

					G	H	I	J	K	L	M	N	O	P	
A	B	C	D	E	F	3.0	• 331	37.9	3009	103	2	1	20	284.5	Smith (1970)
314	68	02	22	76.0	2.6	• 184	37.9	0130	103	2	1	20	284.5	"	Kane (1969u)
315	68	02	22	76.5	2.5	• 527	37.9	0300	103	2	1	20	284.5	"	Kane (1969b)
316	68	02	22	77.0	6.0	• 184	37.9	0430	103	2	1	20	284.5	"	Cole et al. (1969)
317	68	02	22	72.0	4.0	• 367	37.9	0602	103	2	1	20	284.5	"	282.1
318	68	02	22	73.7	6.0	• 365	40.8	1230	105	1	1	5	282.1	Cole et al. (1969)	
319	68	03	08	57.1	54.0	• 134	8.6	1200	105	2	1	20	284.5	"	Kane (1969u)
320	68	03	08	68.5	9.0	• 216	8.6	1735	105	2	1	20	284.5	"	Kane (1969b)
321	68	03	22	57.0	60.0	• 365	40.8	1230	105	3	1	1	5	282.1	Cole et al. (1969)
322	68	03	22	57.0	60.0	• 365	40.8	1230	105	1	1	5	282.1	Belrose (1969)	
323	68	03	25	61.0	32.0	• 214	45.4	0945	105	1	1	11	284.1	Belrose (1969)	
324	68	03	25	54.2	85.0	• 148	45.4	1010	105	1	1	11	284.1	Belrose (1969)	
325	68	03	25	57.5	50.0	• 243	40.8	1100	105	3	1	1	5	282.1	Cole, Ferraro and Lee (1969)
326	68	03	25	57.2	52.0	• 428	40.8	1130	105	3	1	1	5	282.1	"
327	68	03	25	57.2	52.0	• 428	40.8	1130	105	1	1	1	5	282.1	"
328	68	03	25	56.5	59.0	• 411	40.8	1230	105	3	1	1	5	282.1	Cole et al. (1969)
329	68	03	25	59.6	39.0	• 223	40.8	1230	135	1	1	1	5	282.1	Cole et al. (1969)
330	68	03	25	57.6	55.0	• 416	40.8	1430	105	3	1	1	5	282.1	Cole, Ferraro and Lee (1969)
331	68	03	25	58.0	45.0	• 360	40.8	1430	105	1	1	1	5	282.1	Cole, Ferraro and Lee (1969)
332	68	04	02	57.0	59.0	• 407	40.8	1030	107	3	1	1	5	282.1	Cole et al. (1969)
333	58	04	92	58.0	45.0	• 318	40.8	1030	107	1	1	5	282.1	Cole et al. (1969)	
334	58	07	04	61.0	34.0	• 478	45.4	1200	105	1	1	1	5	284.1	Montbriand and Belrose (1972a)
335	68	07	08	49.5	17.0	• 168	45.4	1240	105	1	1	2	1	284.1	Montbriand and Belrose (1972c)
336	68	07	08	49.5	17.0	• 261	45.4	1300	105	1	1	2	1	284.1	"
337	68	07	08	54.0	100.0	• 233	45.4	1330	105	1	1	2	1	284.1	"
338	68	07	08	57.5	60.0	• 265	45.4	1400	105	1	1	2	1	284.1	"
339	68	07	08	58.0	55.0	• 213	45.4	1455	105	1	1	2	1	284.1	"
340	68	07	24	63.0	23.0	• 190	37.9	0450	105	2	1	2	20	284.5	Mechtly and Smith (1970)
341	68	07	24	61.0	29.0	• 248	37.9	0530	105	2	1	2	20	284.5	"
342	68	07	24	62.0	25.0	• 399	37.9	1636	105	2	1	2	20	284.5	"
343	68	07	24	64.0	16.5	• 308	37.9	1235	105	2	1	2	20	284.5	"
344	68	08	21	52.3	125.0	• 101	37.9	1440	105	2	1	2	20	284.5	Aikin (1972)
345	68	08	21	50.9	150.0	• 105	37.9	1440	105	2	1	2	20	284.5	Aikin (1972)
346	68	08	21	61.5	27.0	• 251	37.9	1440	105	2	1	2	20	284.5	Rowe (1972)
347	68	08	29	36.7	61.0	• 158	8.6	1415	105	2	1	20	284.5	Prakash et al. (1971)	
														76.9	

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	
348	68	08	29	54.6	86.6	• 11.8	6.6	14.15	10.5	2	1	20	76.9	Prakash et al. (1971)		
349	68	07	30	60.4	48.0	• 20.1	40.0	12.66	10.5	4	1	11	55.0	Krasnushkin and Knyazeva (1970)		
350	68	10	21	56.0	65.0	• 17.7	40.0	17.10	11.0	3	1	25	282.1	Rowe et al. (1970)		
351	68	10	21	52.0	122.0	• 091	40.0	17.39	11.0	3	1	25	282.1	" " "		
352	68	10	21	51.4	142.0	• 075	40.0	18.01	11.0	3	1	25	292.1	" " "		
353	68	10	24	54.3	59.0	• 154	67.0	21.50	11.0	2	2	1	28	26.4	Derblom and Ladell (1973)	
354	68	10	25	76.5	15.0	• 442	74.0	12.60	11.0	1	1	11	265.1	Belrose, Hewitt & Bunker (1969)		
355	68	10	26	60.0	37.0	• 17.6	74.0	7	12.00	11.0	1	1	11	" " "	" " "	
356	68	10	29	56.0	62.0	• 146	74.0	7	12.00	11.0	1	2	11	265.1	" " "	
357	68	10	31	51.5	13.5.0	• 453	74.0	7	12.00	11.0	1	1	11	265.1	" " "	
358	68	11	21	55.0	2	71.0	• 359	74.0	7	12.00	11.1	1	11	265.1	" " "	
359	68	11	24	63.4	17.5	• 220	-44.0	12.30	11.1	1	1	21	173.0	Von Briel (1971)		
360	68	11	19	56.5	60.0	• 645	58.0	0.200	11.1	2	2	11	265.0	Ulwick, Baker & Sellers (1970)		
361	68	00	00	63.0	50.0	• 232	51.5	12.00	10.5	4	1	8	359.4	Thrane (1972)		
362	69	01	19	58.5	32.0	• 137	69.0	3	20.24	11.0	2	2	1	28	16.0	Derblom et al. (1973)
363	69	01	31	61.6	27.0	• 227	37.0	9	12.00	11.0	2	1	20	284.5	Mechtly, Bowhill and Smith (1972)	
364	69	02	06	63.3	19.0	• 783	37.0	9	12.09	11.0	2	1	20	284.5	Mechtly, Bowhill and Smith (1972)	
365	69	02	25	46.2	20.0	• 340	50.0	0	15.21	11.0	2	2	1	28	15.0	Jespersen et al. (1969)
366	69	02	25	51.1	42.0	• 351	50.0	0	22.37	11.0	2	2	1	28	15.0	Jespersen et al. (1969)
367	69	03	20	51.7	14.0	• 081	45.4	12.00	10.8	1	1	11	284.1	Belrose (1970)		
368	69	04	14	45.5	34.5	• 112	58.0	8	15.28	10.6	2	2	11	265.8	Megill et al. (1971)	
369	69	04	14	64.0	22.0	• 597	58.0	8	23.19	10.6	2	2	11	265.8	Megill et al. (1971)	
370	69	04	17	61.0	30.0	• 258	37.0	9	16.00	10.6	1	1	20	284.5	Mechtly, Bowhill and Smith (1972)	
371	69	06	19	56.7	5.0	• 257	57.0	2	10.06	10.6	2	1	23	352.7	Bain and Harrison (1972)	
372	69	06	05	73.7	4.7	• 344	58.0	8	21.36	10.6	2	1	11	265.8	Dean (1972)	
373	69	09	10	60.9	32.0	• 475	37.0	9	15.6	10.5	1	1	20	284.5	Mechtly, Bowhill and Smith (1972)	
374	69	10	00	58.1	45.0	• 270	40.0	8	12.00	10.4	3	1	25	282.1	Rowe (1972)	
375	69	11	02	71.2	6.5	• 397	58.0	8	0.500	10.5	1	2	11	265.8	Belrose (1972)	
376	69	11	02	67.0	12.5	• 318	58.0	8	6.00	10.5	1	2	11	265.8	" " "	
377	69	11	02	51.5	14.6	• 403	58.0	8	6.700	10.5	1	2	11	265.8	" " "	
378	69	11	02	49.1	19.4	• 548	58.0	8	0.803	10.5	1	2	11	265.8	" " "	
379	69	11	02	45.0	36.0	• 369	58.0	8	0.900	10.5	1	2	11	265.8	Dean (1972)	
380	69	11	02	46.4	27.5	• 567	58.0	8	15.10	10.5	2	2	11	265.8	Belrose (1972)	
381	69	11	03	62.8	25.0	• 374	58.0	8	0.000	10.5	1	2	11	265.8	" " "	

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
382	69	11	03	52.4	130.6	206	58.3	0005	105	2	2	1	11	265.6	Ulwick (1972)	
383	69	11	33	57.7	50.6	317	58.8	2657	105	2	2	1	11	265.6	Dean (1972)	
384	69	11	03	58.9	51.0	751	58.3	0730	105	2	2	1	11	265.5	Dean (1972)	
385	69	11	03	54.1	85.0	397	58.8	0752	105	2	2	1	11	265.5	Ulwick (1972)	
386	69	11	93	42.0	260.0	140	58.8	1254	105	2	2	1	11	265.5	Dean (1972)	
387	69	11	34	64.7	18.0	343	58.8	0900	105	1	2	1	11	265.5	Belrose (1972)	
388	69	11	04	51.8	150.0	286	58.8	1530	105	2	2	1	11	265.5	Dean (1972)	
389	69	11	04	51.0	90.0	214	58.8	1638	105	2	2	1	11	265.6	Dean (1972)	
390	69	11	04	55.8	68.0	278	58.8	1708	105	2	2	1	11	265.6	Ulwick (1972)	
391	69	11	35	66.8	15.0	317	58.8	0000	105	2	2	1	11	265.6	Belrose (1972)	
392	69	11	18	51.2	150.0	236	45.4	1250	105	1	1	2	11	264.1	Montbriand and Belrose (1972c)	
393	69	11	19	53.7	98.0	177	45.4	1330	105	1	1	2	11	284.1	" " "	
394	69	11	18	55.0	82.0	183	45.4	1400	105	1	1	2	11	264.1	" " "	
395	69	11	18	56.4	67.5	212	45.4	1430	105	1	1	2	11	264.1	" " "	
396	69	12	30	57.9	46.5	182	40.8	0900	106	3	1	1	25	282.1	Rowe (1972c)	
397	69	12	00	57.5	40.0	221	40.8	1030	106	3	1	1	25	282.1	" " "	
398	69	12	00	66.5	57.0	220	40.8	1200	106	3	1	1	25	282.1	" " "	
399	69	12	00	56.6	57.0	234	40.8	1430	106	3	1	1	25	282.1	" " "	
400	69	12	30	56.8	56.5	42C	40.8	1500	106	3	1	1	25	282.1	" " "	
401	69	12	00	67.3	35.0	091	40.0	1200	60	4	1	1	15	50.0	Krashushkin and Knyazeva (1970)	
402	70	01	02	60.4	34.0	247	8.6	1212	106	2	1	1	20	76.9	Somayajulu et al. (1971)	
403	70	01	00	54.7	77.0	135	40.8	1200	106	3	1	1	25	282.1	Rowe (1972c)	
404	70	02	00	57.1	54.0	190	40.8	1200	106	3	1	1	25	282.1	Rowe (1972c)	
405	70	03	01	56.0	74.0	082	45.4	1003	106	1	1	1	264.1	Montbriand and Belrose (1972c)		
406	70	03	01	52.0	145.0	353	45.4	1009	106	1	1	2	11	284.1	" " "	
407	70	03	01	52.9	123.0	273	45.4	1017	106	1	1	2	11	284.1	" " "	
408	70	03	07	63.6	20.0	324	37.9	045	106	2	1	1	20	284.1	Mechtly and Sechrist (1972)	
409	70	03	07	59.9	38.0	126	40.8	1309	106	3	1	2	11	282.1	Rowe et al. (1970)	
410	70	03	07	61.2	30.0	103	40.8	1328	106	3	1	2	11	282.1	Rowe et al. (1970)	
411	70	03	07	71.3	5.6	837	37.9	1339	106	2	1	2	20	284.1	Mechtly, Sechrist & Smith (1972)	
412	70	03	07	63.2	25.0	374	44.3	1340	106	1	1	1	297.7	Belrose et al. (1972)		
413	70	03	07	64.2	26.0	471	44.9	1340	106	2	1	1	297.7	Belrose et al. (1972)		
414	70	03	07	58.8	44.0	240	40.8	1413	106	3	1	2	11	282.1	Rowe et al. (1970)	
415	70	03	07	68.1	12.0	170	44.9	1504	106	2	1	2	11	297.7	Belrose, Ross & McNamara (1972)	

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
416	70	03	07	65.0	18.0	471	44.9	15.0	106	1	1	2	11	297.7	Belrose, Ross & McNamara (1972)
417	70	03	11	58.2	48.5	494	46.8	1310	106	3	1	1	11	282.1	Rowe, Ferraro and Lee (1970)
418	70	03	19	59.3	38.0	149	8.6	827	106	2	1	1	20	76.9	Aikin et al. (1972)
419	70	03	19	58.0	45.0	147	8.6	1017	106	2	1	1	20	76.9	" " "
420	70	03	19	60.1	34.0	223	8.6	1509	106	2	1	1	20	76.9	" " "
421	70	05	22	59.7	38.5	115	45.4	65.5	106	1	1	1	11	284.1	Coyne and Belrose (1972b)
422	70	05	22	57.1	46.0	155	45.4	810	106	1	1	1	11	284.1	Coyne and Belrose (1972)
423	70	05	22	55.9	69.3	185	45.4	1020	106	1	1	1	11	284.1	Coyne and Belrose (1972b)
424	70	05	22	55.0	43.0	225	45.4	1200	106	1	1	1	11	284.1	Coyne and Belrose (1972)
425	70	05	22	56.9	47.0	209	45.4	1600	106	1	1	1	11	284.1	" " "
426	70	35	22	50.8	70.0	045	45.4	1750	106	1	1	1	11	284.1	" " "
427	70	06	24	57.2	51.5	337	40.8	0755	105	3	1	1	5	282.1	Ferraro, Lee and Cohen (1972)
428	70	06	24	60.0	52.0	208	45.4	0755	105	1	1	1	5	284.1	Ferraro, Lee and Cohen (1972)
429	70	06	26	56.9	60.5	350	40.8	1110	105	3	1	1	4	282.1	Belrose and Coyne (1972)
430	70	06	26	58.2	67.5	253	45.4	1200	105	1	1	1	4	284.1	Belrose and Coyne (1972)
431	70	07	00	57.4	60.0	185	40.6	1430	104	3	1	1	25	282.1	Rowe (1972)
432	70	07	00	56.7	57.3	352	40.8	1200	104	3	1	1	25	282.1	Rowe (1972)
433	70	08	04	64.2	25.0	328	59.3	1305	101	2	1	1	26	16.0	Thrane (1972)
434	70	08	10	70.0	10.2	295	67.8	0040	101	2	1	1	26	26.4	Derblom et al. (1973)
435	70	08	00	56.5	58.0	438	40.8	1200	101	3	1	1	25	282.1	Rowe (1972)
436	70	07	00	55.6	58.0	169	40.8	0800	104	3	1	1	25	282.1	Ferraro et al. (1974)
437	70	07	00	56.0	56.5	182	40.8	0630	104	3	1	1	25	282.1	" " "
438	70	07	00	56.7	50.0	280	40.8	0900	134	3	1	1	25	282.1	" " "
439	70	07	00	56.3	52.0	192	40.8	1000	104	3	1	1	25	282.1	" " "
440	70	07	00	57.0	46.0	280	40.8	1230	104	3	1	1	25	282.1	" " "
441	70	09	30	57.0	55.0	449	40.8	1200	97	3	1	1	25	282.1	Rc,je (1972)
442	70	10	00	56.9	55.0	324	40.8	0930	94	3	1	1	25	282.1	" " "
443	70	10	00	59.5	37.0	201	40.8	1000	94	3	1	1	25	282.1	" " "
444	70	10	00	56.9	55.6	066	40.8	1038	94	3	1	1	25	282.1	" " "
445	70	10	00	57.2	52.0	410	40.8	1430	94	3	1	1	25	282.1	" " "
446	70	10	00	58.6	40.0	201	40.8	1500	94	3	1	1	25	282.1	" " "
447	70	10	00	57.5	49.3	293	40.8	1200	94	3	1	1	25	282.1	Ferraro et al. (1974)
448	70	10	00	57.2	52.0	146	40.8	1300	96	3	1	1	25	282.1	" " "
449	70	11	00	57.2	52.5	135	40.8	1200	89	3	1	1	25	282.1	Rowe (1972)

TABLE A2 (continued): D-Region Profiles: Data and Scaled Parameters

See Table A1 for Column Headings

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
450	71	01	22	46.4	265.6	•104	32.3	1200	80	2	1	1	20	253.5	Mitchell et al. (1972)
451	71	61	26	49.0	177.0	•037	32.3	0955	80	2	1	1	20	253.5	Mitchell et al. (1972)
452	71	01	28	64.0	39.0	•341	5.6	1040	80	2	1	1	20	76.9	Prakash (1972)
453	71	01	28	61.9	60.2	•318	8.6	1110	80	2	1	1	20	76.9	Prakash (1972)
454	71	01	00	58.8	41.0	•245	40.8	1200	80	3	1	1	25	282.1	Rowe (1972)
455	71	02	01	47.0	230.0	•143	32.3	1200	78	2	1	1	20	253.5	Mitchell et al. (1972)
456	71	03	27	59.5	50.0	•096	45.4	0930	74	1	1	1	11	284.1	Coyne and Belrose (1972)
457	71	03	27	58.0	58.2	•127	45.4	1200	74	1	1	1	11	284.1	" "
458	71	03	27	55.3	78.0	•057	45.4	1455	74	1	1	11	284.1	" "	
459	71	10	16	59.1	48.0	•175	45.4	1200	66	1	1	1	37	284.1	Tanenbaum et al. (1973)
460	71	10	20	57.2	62.0	•165	45.4	1200	66	1	1	1	37	284.1	" "
461	71	10	25	61.2	34.5	•267	45.4	1200	66	1	1	1	37	284.1	" "
462	71	10	26	55.5	60.0	•244	45.4	1147	66	1	1	1	39	284.1	Belrose et al. (1972)
463	71	10	29	50.2	29.0	•136	45.4	1200	66	1	1	1	39	284.1	Belrose et al. (1972)
464	72	12	05	62.9	21.0	•223	37.9	1200	55	2	1	1	20	284.5	Mechtly et al. (1973)
465	73	01	16	59.5	36.0	•191	37.9	1200	51	2	1	1	20	284.5	Mechtly et al. (1973)
466	67	12	00	57.3	49.0	•132	40.6	1500	102	3	1	1	25	282.1	Rowe et al. (1969)
467	67	12	14	57.2	51.2	•165	40.6	1500	102	3	1	1	25	282.1	" "
468	68	01	08	57.1	51.5	•212	49.6	1500	102	3	1	1	25	282.1	" "
469	69	03	27	60.5	80.0	•054	60.0	1630	122	3	1	1	7	11.1	Barrington et al. (1963)
470	60	03	27	59.8	94.0	•146	60.0	1230	122	3	1	1	7	11.1	" "
471	60	03	27	59.8	94.0	•146	60.0	1330	122	3	1	1	7	11.1	" "
472	64	09	01	61.2	35.0	•559	-30.5	1730	10	3	1	1	34	151.5	Smith, Coyne and Loch (1967)
473	64	09	01	61.2	35.0	•559	-30.5	1742	10	3	1	1	34	151.5	" "
474	64	09	01	61.2	35.0	•559	-30.5	1752	10	3	1	1	34	151.5	" "
475	65	04	00	61.1	62.0	•124	-19.3	0900	14	5	1	1	9	17.7	Gruschwitz (1974)
476	65	04	00	61.1	62.0	•124	-19.3	1500	14	5	1	1	9	17.7	" "
477	65	03	00	60.4	33.0	•134	53.8	1630	13	1	1	1	11	265.8	" "

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