NUSC Technical Report 4860

# A Study of the Drag Characteristics and Polymer Diffusion in the Boundary Layer of an Axisymmetric Body

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John E. Sirmalis

Wersons Department



12 March 1976

# NAVAL UNDERWATER SYSTEMS CENTER

Newport Laboratory

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## PREFACE

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C. A. Spero, Jr. Director, Systems Development

The author of this report is located at the Newport Laboratory, Naval Underwater Systems Center, Newport, Rhode Island 02840.

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Extension to axisymmetric flow could result in significant achievable gains in volume utilization.

This study examines these polymer ejection processes through measurement of wall and boundary layer concentration profiles and through a photographic study of the boundary layer. Tests performed with fresh water ejection and solutions of the drag reducing polymer, Polyox WSR-301, lead to the hypothesis that optimal ejection for minimum polymer usage requires ejection into a laminar boundary layer prior to turbulent flow transition.

Analytical routines are developed which predict boundary layer parameter and polymer wall concentrations for this postulated optimal ejection process or the suboptimal case. Limited verification of the model is made.

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#### SUMMARY

Drag reduction by ejection of high molecular weight polymers on free-running bodies of revolution has been demonstrated repeatedly. The quantities of polymer required have made the gains achieved marginal from a volume utilization tradeoff. The ejection process is hypothesized to be the controlling factor. Limited data obtained in pipe flow and flat plate flow experiments on ejection into developing boundary layers indicate a drastic reduction in polymer requirements for equivalent percent drag reductions. Extension to axisymmetric flow could result in significant achievable gains in volume utilization.

The object of the research described merein was to examine the processes described above through measurement of wall and boundary layer concentration profiles and through a photographic study of the boundary layer. Tests were performed with fresh water ejection and solutions of the drag reducing polymer, Polyox WSR-301. Predictive analytical routines were developed and experimentally verified.

The experimental apparatus used in this experiment was a drop tank with several velocity measurement stations and photographic equipment. Several specially designed axisymmetric bodies were constructed. Three of these ejected dye by aspiration at the minimum pressure point near the nose. The fourth had a capability to eject through a nose-screen type orifice at a constant rate

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and withdraw wall or boundary layer samples at four stations along the body. All bodies had a maximum diameter of three inches and applied a half-body forebody. The three dye ejecting bodies incorporated different tail configurations:  $6^{\circ}$  cone tail, L/D = 8.33;  $12^{\circ}$  cone tail, L/D = 6.7; and spherical tail, L/D = 5.54. The polymer ejection body was similar in configuration to the  $6^{\circ}$  tail body.

Tests were performed in a Reynolds number range of one to five million. The first series of tests were performed in fresh water and in a polymer "ocean" of various concentrations; 1.25, 2.5, 5, 10, 20, 50, and 60 WPPM. Skin friction reduction obtained on all bodies approached 70 percent at polymer concentrations of 20 WPFM, agreeing well with data from other experimenters. Total drag reductions of 33 percent for the 6<sup>o</sup> body, 16 percent for the 12<sup>o</sup> body, and 10 percent for the spherical tail body were obtained, the effect of higher percentage form drag being evident.

Photographic studies of dyed boundary layers in these tests and in ejection tests with 50 WPPM, 500 WPPM, and 1000 WPPM displayed several interesting characteristics. Addition of small quantities of polymer, 2.5 WPPM, eliminated the fine-scale turbulent structure leaving only coarse turbulence. Higher concentrations resulted in suppression of the coarse turbulence and extreme thinning of the boundary layer. In the ejection tests, concentrations of 500 WPPM and 1000 WPPM displayed no turbulent structure or

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mixing. A dye streaking phenomenon with spacing equivalent to that characteristic of laminar sublayer streaks was displayed. The number of streaks was also approximately equal to the number of ejection holes, approximately 700, supporting the fact that mixing had essentially ceased.

Concentration profiles were measured in the ejection tests using a fluorometric method. Tracer-contaminated water, 5 WPPM, 10 WPPM, 20 WPPM, 50 WPPM, 500 WPPM, and 1000 WPPM solutions, were ejected. Four measurement stations, the last at an x/Lof .48, were sampled. The water data displayed expected concentration profiles, agreeing well with those of other investigators. At all polymer concentrations tested, unexpected results were achieved. Wall concentrations remained at levels predicted by molecular diffusion. As evidenced from the photographs, no diffusion was occurring. An initial mixing zone neglected by most investigators was the controlling zone in these tests. Only for the 5 WPPM case did a higher diffusion rate begin part way along the body. The data for this axisymmetric case were compared with data from the single flat plate experiment evidencing the same phenomenon. A dimensionless distance developed in the flat plate experiment used to predict the extent of this initial zone was modified and compared favorably with this experiment. It is hypothesized from these tests that optimal ejection for minimum polymer usage requires ejection into a laminar boundary layer prior to transition to turbulent flow.

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Analytical routines are developed which predict boundary layer parameters and polymer wall concentrations for this postulated optimal ejection process or the suboptimal case. Limited verification of the model is made.

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# LIST OF SYMBOLS

A = body area	ft <sup>2</sup>
$A_e$ = ejection area	ft <sup>2</sup>
A <sub>f</sub> = body frontal area	ft <sup>2</sup>
A <sub>s</sub> = body surface area	ft <sup>2</sup>
a = acceleration	ft/sec
b = Batchelor's Constant	dimensionless
B = Buoyant force on body	lbs
c = concentration	WPPM
c <sub>i</sub> = ejected concentration	WPPM
cf = local skin friction coefficient	dimensionless
C <sub>F</sub> = skin friction coefficient	dimensionless
c <sub>w</sub> = wall concentration	WPPM
C <sub>D</sub> = total drag coefficient	dimensionless
C <sub>p</sub> = pressure coefficient	dimensionless
D = body diameter	ft
D <sub>c</sub> = Eddy diffusivity	$\frac{1b \text{ sec}^2}{\text{ft}^2}$
$D_{POLY} = total drag with polymer$	lbs
$D_{W}$ = total drag in water	lbs
F = force	lbs
g = gravitational acceleration	ft/sec <sup>2</sup>
k = gas constant	dimensionless
K = mixing length constant	dimensionless
$K_2$ = defined by equation (114)	dimensionless

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$K_3$ = defined by equation (119)	dimensionless
$K_5 =$ defined by equation (117)	dimensionless
l = length dimension	ft
L = body length	ft
M = mass	$\frac{1b_{f} \sec^{2}}{1b_{w} ft^{2}}$
p = pressure	lb/ft <sup>2</sup>
p <sub>c</sub> = pressure at edge of boundary layer	lb/ft <sup>2</sup>
q <sub>z</sub> = flux of diffused matter	lb sec ft <sup>3</sup>
Q = volume flow rate	ft <sup>3</sup> /sec
Q <sub>i</sub> = ejection rate	ft <sup>3</sup> /sec
r = radial distance from body centerline	ft
r <sub>h</sub> = distance from origin for body coordinate	
generation	ft
r <sub>o</sub> = radius of body	ft
$r^+ = \frac{r v^*}{v}$	dimensionless
$r^{+} = \frac{r v^{*}}{v}$ $r^{+}_{o} = \frac{r_{o} v^{*}}{v}$	dimensionless
R <sub>e</sub> = Reynold's number	dimensionless
$R_L = \frac{U_O L}{V}$	dimensionless
SD <sub>POLY</sub> = shear drag with polymer	lbs
SD <sub>w</sub> = shear drag with water	lbs
SFR = total skin friction reduction	o/ /o
t = time	second
T = temperature	٥ <sub>R</sub>

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$T_{i}$ = temperature of injected fluid	° <sub>R</sub>
TDR = total drag reduction	9/ / 3
u(z) = local boundary layer velocity	ft/sec
$u^+ = u/v^*$	dimensionless
$u(\overline{Y}) = velocity at \overline{Y}$	ft/sec
U = U <sub>0</sub> freestream or body velocity	ft/sec
U <sub>e</sub> = velocity at edge of boundary layer	ft/sec
v = velocity	ft/sec
$v_i$ = ejection velocity	ft/sec
v* = characteristic or friction velocity	ft/sec
$v_0^*$ = critical shear velocity = $t_w/\rho$	ft/sec
$V = U_e/U_o$	dimensionless
V <sub>S</sub> = storage volume	ft <sup>3</sup>
W = body weight in air	lbs
x = linear dimension	ft
x <sub>s</sub> = surface length	ft
$x \star = x/L$	dimension <b>le</b> ss
y = distance normal to body	ft
$y^+ = \frac{y \cdot v^*}{v}$	dimensionless
$\overline{y}$ = mean vertical position of particles	ft
$\overline{Y}$ = mean vertical position of single particle	ſť
Y = RAO variable defined by equation (15)	ft
$Y^+ = \frac{Y v^*}{v}$	dimensionless
$\alpha$ = defined by equation (29)	dimensionless
$\beta$ = defined by equation (10)	dimensionless

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$\gamma$ = defined by equation (43)	dimensionless
i ⇒ Eddy viscosity	$\frac{1b \text{ sec}}{ft^2}$
$\Delta B$ = defined by equation (42)	dimensionless
$\delta$ = boundary layer thickness	ft
δ」 = diffusion boundary layer thickness	ft
$\phi$ = angle for definition of half body	degrees
$\theta$ = angle from normal to bad	degrees
II = defined by equation (11)	dimensionless
$\psi$ = stream function	seconds
$\lambda = \left(\frac{2}{c_f}\right)^{\frac{1}{2}}$	dimensionless
w = gas flow rate	lb/sec
$\rho$ = density	slugs/ft <sup>2</sup>
$\mu$ = viscosity	lb sec/ft <sup>2</sup>
τ <sub>w</sub> = wall shear stress	lb/sec <sup>2</sup>
v = kinematic viscosity	ft <sup>2</sup> /sec

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#### 1. INTRODUCTION

#### A. General Considerations

High speed flow of both gases and liquids past a fixed boundary generates a turbulent boundary layer which exerts both a fluctuating normal stress (flow noise) and fluctuating shear stress (whose average is drag) on the body. The reduction of resistance to the turbulent shear flows of liquids through the addition of small quantities of high molecular weight polymers into the boundary layer of the flow has been demonstrated repeatedly. This phenomenon of drag reduction has far-reaching importance in the reduction of power required for pumping of fluids or transport of bodies through liquids.

Until recently, the phenomenon of drag reduction was confined essentially to characterizing the manner in which the boundary layer velocity profiles were affected, thus allowing predictions of boundary layer thickness and shear drag. Additionally, the early work primarily dealt with well-developed pipe flows where the observation of drag reduction was first made. An added complication results from the fact that data obtained with commonly used instrumentation have been found to be affected by the polymers resulting in erroneous readings. As a result, the mechanism of shear stress reduction remains undefined although emperical techniques predicting the benefits of application of the phenomenon have been developed.

Interest in the problem has expanded with recent investigators examining the effect of polymers on external flows, as over flat plates. Similar results as in the pipe flows have been achieved. The magnitude of the turbulent fluctuations have been found to decrease with a thickening of the laminar sublayer and a lowering of the shear stress.

Shear stress reduction for external flows over bodies can be achieved by proper ejection of polymer solutions. A limit to the amount of drag reduction achievable with polymer use has been demonstrated and increases in shear stress has been obtained when excess polymer is used.

It is evident that a better understanding of the mechanisms of drag reduction in developing flows with polymer ejection is required if an advantage is to be taken of the phenomenon. For most cases, of interest in external flows, a carried polymer supply would be used for ejection into the boundary layer. Limits on diffusion result in  $\varepsilon$  far too high concentration initially – with, possibly, shear drag increases – and then, further downstream on the body, too little polymer resulting in insignificant gains in drag reduction. One might envision, to circumvent the problem, multiple ejection ports to optimize the polymer wall concentration and maximize the drag reduction.

Many investigators have addressed portions of the problem outlined above as discussed in the following chapter. The

effect of long chain polymers on suppressing boundary layer turbulence has been investigated for pipe flows and external flows; methods of characterizing the boundary layer velocity profiles with polymers present have been developed and methods for prediction of flow separation have been postulated.

The object of the research described herein was to develop predictive methods for design of polymer ejection system for bodies of revolution and to perform experiments to verify the predictive methods. Additionally, a study of the effects of polymers on boundary layer separation was made. Several "half body" configurations were used in the testing, differing in their conical to hemispherical tail configurations. The bodies were dropped in a twenty-foot long cylindrical tank and allowed to achieve a steady state velocity. On three of the bodies, dye was ejected in the boundary layer and photographic records of the growth and separation of the boundary layer at several velocities were made. For these tests, the ambient fluid was water and a water polymer mix (polymer ocean) of several concentrations. Another series of tests were made with a body having a significantly different internal configuration. This body has the capability to store and eject concentrated polymer solution from its nose and withdraw boundary layer samples at four stations along its length. The boundary layer samples in turn were either wall samples or samples at three heights within the boundary layer. The stored

polymer was contaminated with a fluorescent dye which was later used in analyzing the concentrations from these boundary layer samples. Thus, it was possible to measure the change in wall concentration and concentration profile in the boundary layer, measure steady state body velocity and compare simultaneously with computed results. This research, therefore, concentrates on the prediction and verification of the drag reduction mechanism on bodies of interest for underwater application to gain insight which will help in the design of vehicle ejection systems.

B. Selection of Experimental Apparatus

The intended research could be carried out in water tunnels, towing tanks, ring channels, in buoyant vehicle experiments, or in drop tank tests.

For the desired research, the drop tank has a number of attractive features. Conceptually, it is a relatively simple experimental tool. The ambient turbulence level is very low, flow visualization is easily achieved and velocity measurements readily made. Tests over a reasonable range of Reynolds numbers are achieved by weighting the body being dropped.

One of the chief drawbacks of the drop tank facility as compared to a water tunnel, ring channel or towing tank is the inability to easily measure velocity profiles since the body being measured is moving. Since flow visualization gives an approximate boundary layer thickness, this limitation was not considered to be an important drawback.

Fortunately, the author's employer, Naval Underwater Systems Center, had available a drop tank with suitable dimensions for this research. The potential for meaningful research and the availability of the capital equipment led to the decision to proceed with axisymmetric boundary layer research described herein.

#### C. Results

Tests were performed in a Reynolds number range of one to five million. The first series of tests were performed in fresh water and in a polymer "ocean" of various concentrations; 1.25, 2.5, 5, 10, 20, 50, and 60 WPPM. Skin friction reduction obtained on all bodies approached 70 percent at polymer concentrations of 20 WPPM agreeing well with data from other experimenters. Total drag reductions of 33 percent for the 6<sup>o</sup> body, 16 percent for the 12<sup>o</sup> body, and 10 percent for the spherical tail body were obtained, with the effect of higher percentage form drag being evident.

Photographic studies of dyed boundary layers in these tests and in ejection tests with 50 WPPM, 500 WPPM, and 1000 WPPM displayed several interesting characteristics. Addition of small quantities of polymer, 2.5 WPPM, eliminated the fine-scale turbulent structure leaving only coarse turbulence. Higher concentrations resulted in suppression of the coarse turbulence and extreme thinning of the boundary layer. In the ejection tests, concentrations of 500 WPPM and 1000 WPPM displayed no turbulent structure or mixing. A dye streaking phenomenon with spacing equivalent to that characteristic of laminar sublayer streaks was displayed. The number of streaks

-5

was also approximately equal to the number of ejection holes, approximately 700, supporting the fact that mixing had essentially ceased.

Concentration profiles were measured in the ejection tests using a fluorometric method. Tracer-contaminated water, 5 WPPM, 10 WPPM, 20 WPPM, 50 WPPM, 500 WPPM, and 1000 WPPM solutions, were ejected. Four measurement stations, the last at an x/L of .48, were sampled. The water data displayed expected concentration profiles, agreeing well with those of other investigators. At all polymer concentrations tested, unexpected results were achieved. Wall concentrations remained at levels predicted by molecular diffusion. As evidenced from the photographs, no diffusion was occurring. An initial mixing zone neglected by most investigators was the controlling zone in these tests. The data for this axisymmetric case were compared with data from the single flat plate experiment evidencing the same phenomenon. A dimensionless distance developed in the flat plate experiment used to predict the extent of this initial zone was modified and compared favorably with this experiment. It is hypothesized from these tests that optimal ejection for minimum polymer usage requires ejection into a laminar boundary layer prior to transition to turbulent flow.

Analytical routines are developed which predict boundary layer parameters and polymer wall concentrations for this postulated optimal ejection process or the suboptimal case. Limited verification of the model is made.

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### 11. LITERATURE REVIEW

The reduction of resistance to the turbulent shear flows of liquids through addition of small quantities of polymer into the boundary layer flowing over a body has received considerable attention. The first reportings occurring independently by Mysel (1949), Toms (1949), and Oldroyd (1949). Although extensive theoretical and experimental work has been carried out with steady pipe flows where the resistance is due to turbulent skin friction alone, relatively few studies have been conducted on the effect of additives on the flow about axisymmetric bodies where the development of the boundary layer, the position of the separation point, and the unsteady wake significantly contributes to the total resistance. Polymer injection in developing boundary layers has only recently come under study. Polymer ejection type data for external flows with pressure gradients are virtually non-existent. Hoyt (1972) presents an encellent summary of the research efforts and results available in the field of drag reduction.

Literature pertaining to the current study will be reviewed under four separate headings:

- 1. Bluff body experiments with polymer solutions,
- 2. Turbulent boundary layer theory,
- 3. Homogeneous polymer flow, and
- 4. Polymer ejection studies.

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### Bluff Body Experiments With Polymer Solution

The earliest known experiment with bluff bodies in drag reducing polymers was carried out by Crawford and Pruitt (1963). Additional experiments with different sizes and shapes of bodies (mostly spheres cones and cylinders) in various types and concentration of polymers were conducted by others. Work performed by Lang and Patrick (1966) is representative of much of the effort. They found, as did many of the other investigators, that the drag on a sphere was considerably reduced probably due to the rearward movement of the point of boundary layer separation. These experiments were performed in a drop tank where the fluid ahead of the ball was stationary. A drag reduction of 69% was attained for a 2-inch diameter steel sphere dropped in a 1000 WPPM solution of Polyox at a water Reynolds number of 1.4 x  $10^{2}$ . It was also shown that the polymer produced little or no drag reduction on stable bluff-based bodies whose point of boundary layer separation is fixed. The additives produced an apparent decrease in turbulent mixing in the mean wake and had a tendency to display a stringiness in the wake at high polymer concentration.

Contradictory results were achieved by Stow and Elliot, 1970, who demonstrated no significant drag reduction on a tethered ball suspended in a fully developed turbulent pipe flow. This is not surprising, if the flow about the sphere exhibits a turbulent type rearward movement of the separation point.

The performance of additives in reducing drag on an immersed body is complicated by a number of factors. Certainly, with well streamlined bodies, drag reduction is effected through reduced skin friction

just as with internal flow. With blunter bodies, however, the drag consists primarily of form drag and is dominated by the wake size and point of flow separation, skin friction frequently being negligible in comparison. On typical free-running underwater bodies of revolution, the form drag can represent 25% of the total drag. The two investiga-tions previously reported demonstrate the importance of the "free stream" condition on the movement of the separation point with polymers. The effect of polymers on boundary layer separation for bodies of revolution warrants further study to define if reduction in the form drag as well as the skin friction drag can be affected by application of polymers.

#### Turbulent Boundary Layer Theory

Since the concept of transition from laminar to turbulent flow was demonstrated by Osborne Reynolds, in his classic original transition experiment in pipe flow, many attempts have been made to predict the conditions at which laminar to turbulent flow transition will take place. Many attempts have also been made to predict velocity profiles and wall shear. So many, in fact, that in 1968 the Stanford conference was called in which a total of 29 methods for performing turbulent boundary layer analysis were graded. These proceedings have been edited by Kline (1968). Such general analysis can be divided into two types: (1) integral methods averaged across the boundary layer, and (2) finite difference, or differential methods which attempt to solve the full partial differential equations of the boundary layer. A text by F. M. White (1974) neatly summarizes and discusses many of the competing analysis methods.

By considering the relative importance of viscous and turbulent shear, the velocity distribution in a turbulent boundary layer follows a three-layer concept. The layers are:

Inner Layer: Viscous shear dominates

Outer Layer: Turbulent shear dominates

Overlap Layer: Both types of shear important

The mean velocity distribution in a two-dimensional turbulent boundary layer, u(y), depends upon four local parameters --  $\pi_w$ , the local wall shear stress;  $\mu$ , the fluid density;  $\mu$ , the fluid viscosity; and  $\delta$ , the boundary layer thickness. Prandtl (1933) deduced for the inner law that the mean velocity did not depend on  $\delta$  resulting in a functional expression for the inner law of

$$u = f(\tau_{y}, \mu, \mu), \quad (1)$$

Karman (1930) deduced that the wall acts as a source of retardation reducing the local velocity, u, below the freestream velocity  $U_e$ , in a manner independent of viscosity,  $\mu$ . The outer or velocity defect relationship is then

$$U_{e} - u = f(\tau_{w}, \rho, y, \delta).$$
 (2)

Coles (1954) performed a dimensional analysis on these relationships resulting in

Inner Law 
$$\frac{u}{v^*} = f(\frac{yv^*}{v})$$
 (3)

Outer Law 
$$\frac{U_e - u}{v^*} = g(y/\delta)$$
 (4)

where v\* is a characteristic velocity called the wall shear velocity defined as

$$\mathbf{v}^{\star} = \left(\frac{\tau}{\rho}\right)^{\frac{\tau}{2}}.$$
 (5)

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By equating equations (3) and (4) in the overlap region, one may obtain the commonly known relation for the "law of the wall" based on inner variables

$$\frac{u}{v^{\star}} = \frac{1}{K} \ln \frac{yv^{\star}}{v} + B$$
(6)

where K and B are constants determined by the data of Nikuradse (1930), to be .4 and 5.5, respectively. Coles (1954) displays the correlation of the dimensionless velocity profile,  $u/v^*$  with the dimensionless distance for the wall  $\frac{uv^*}{v}$  up to a wake of about 300. With the exception of separating flows, all the data nicely collapse into regions defined by the inner and logarithmic laws having dimensions

nner Law 
$$\frac{u}{v^*} = \frac{yv^*}{v} \quad 0 < \frac{yv^*}{v} < 10$$
 (7)

Logarithmic Law 
$$\frac{u}{v^*} = 2.5 \ln \frac{yv^*}{v} + 5.5 \quad 35 < \frac{yv^*}{v} < 300.$$
 (8)

For regions beyond  $\frac{yv^*}{v}$  = 300, the outer region or wake region, Coles (1956) postulates a function defined as

$$\frac{11}{K} W(\frac{y}{\delta})$$

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be added to the equation (6) resulting in

$$u^{+} = \frac{1}{K} \ln y^{+} + B + \frac{\Pi}{K} W(\frac{y}{\delta})$$
(9)

where II is related to Clauser's (1954, 1955) equilibrium parameter

$$\beta = \frac{\delta^{\star}}{\tau_{w}} \frac{dp_{e}}{dx}.$$
 (10)

A reasonable fit to data is given by the relationship

$$II \stackrel{<}{\sim} 0.8 (\beta + 0.5)^{0.75}$$
(11)

Coles (1956) proposed the following curve fit to the wake function W:

$$W(\frac{y}{\delta}) = 2 \sin^2 \left(\frac{\pi}{2} \frac{y}{\delta}\right)$$
(12)

Thus, for two-dimensional flow, empirical relations for the velocity profile in the boundary layer are available. These relations will 

Rao (1967) observed that in the viscous sublayer of a thick axisymmetric turbulent boundary layer the momentum equation reduces to

$$\frac{\partial}{\partial \mathbf{r}}$$
 (r)  $z = 0 = \frac{\partial}{\partial \mathbf{r}} (\mu \mathbf{r} \frac{\partial \mathbf{u}}{\partial \mathbf{r}}).$  (13)

Integrating with u = 0 at  $r = r_0$ , an inner law for the sublayer results

$$u^{\dagger} = r_{0}^{\dagger} \ln \frac{r}{r_{0}}$$
(14)

where  $r = r_0 + y$ .

When  $\frac{y}{r_0} <<1$ , the familiar  $u^+ = y^+$  relationship returns since the ln(1 +  $\frac{y}{r_0}$ ) approaches  $y/r_0$ .

Rao also postulated that by defining

$$Y^{+} = r_{o}^{+} \ln \frac{r}{r_{o}}$$
(15)

and inserting  $Y^+$  into the familiar law of the wall (6) in place of y, a correlation with the two-dimensional case would result. The final relations are

$$u^+ = \chi^+$$
  $\chi^+ < 5.0$  (16)

$$u^{+} = \frac{1}{K} \ln Y^{+} + B \qquad Y^{+} > 30.$$
 (17)

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Figure 1, reproduced from Rao's paper, displays this correlation with data obtained by Richmond (1957) and Yu (1958). As the body curvature effects become greater, the agreement improves since the wake tends to disappear. For axisymmetric cases where  $y/r_0$  may not be considerably less than 1, equation (15) must be corrected to account for the outer wake region. White, et al (1972), accounts for the wake region using an inner variable approach. The basic idea of the method is that in inner variables, the velocity profile is approximately a logarithmic function of  $Y^+$  plus a wake which depends on  $Y^+$  and a single dimension-less parameter  $\xi(x)$ . For example,

$$u^{+} - \frac{1}{K} \ln y^{+} + B + f[y^{+}, f(x)]$$
 (18)

for the two-dimensional case. The derivation of the functional relation for the axisymmetric case is carried through here, since the resulting velocity relationship is not in a form readily recognizable. Recalling Prandtl's mixing length theory:

$$\tau = \varepsilon \frac{\partial u}{\partial y}.$$
 (19)

Consistent with equation (17) for the axisymmetric case,  $\varepsilon$ , the eddy viscosity, equals

$$\epsilon = \rho \ \ell^2 \ \left| \frac{\partial u}{\partial Y} \right| \tag{20}$$

where 1 is the mixing length.

Now 
$$\frac{\partial u}{\partial Y} = \frac{r}{r_0} \frac{\partial u}{\partial y}$$
 (21)

substituting in (20)

$$\varepsilon = \rho \, \varrho^2 \, \frac{\mathbf{r}}{\mathbf{r}_o} \, \left| \frac{\partial \mathbf{u}}{\partial \mathbf{y}} \right| \,. \tag{22}$$

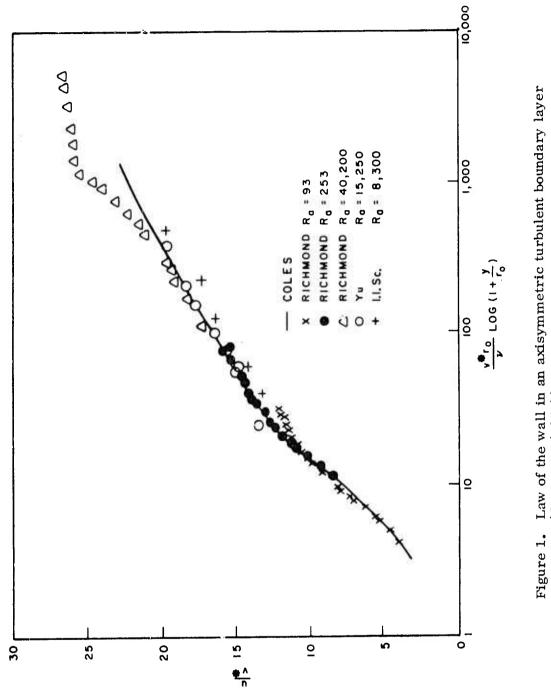


Figure 1. Law of the wall in an axisymmetric turbulent boundary layer (from Rao (1971))

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Fairly near the wall in the overlap layer

 $\ell = KY$ (23)

resulting in an eddy viscosity which is

$$\epsilon = \rho K^2 Y^2 \frac{\mathbf{r}}{\mathbf{r}_0} \left| \frac{\partial \mathbf{u}}{\partial \mathbf{y}} \right|$$
 (24)

Finally, upon substitution in (19):

$$\tau = \rho K^2 Y^2 \frac{r}{r_o} \left(\frac{\partial u}{\partial y}\right)^2.$$
 (25)

Equation (25) may be used to derive an axisymmetric law of the wall, using a Couette flow approximation for the near wall momentum:

$$\left(\frac{\partial}{\partial r}\right)(r\tau) - r \left(\frac{dp_e}{dx}\right) = 0.$$
<sup>(26)</sup>

Integrating with

$$r = r_{0}, \quad r\tau = r_{0}\tau_{w},$$

$$r = r, \quad r\tau = r\tau,$$

$$r\tau = r_{0}\tau_{w} + \frac{1}{2} \left(\frac{dp_{e}}{dx}\right)(r^{2} - r_{0}^{2}).$$
(27)

Substituting (25) into (27) gives

$$\mathbf{r}_{o} \mathbf{\tau}_{W} + \frac{1}{2} \left( \frac{\mathrm{d}\mathbf{p}}{\mathrm{d}\mathbf{x}} \right) \left( \mathbf{r}^{2} - \mathbf{r}_{o}^{2} \right) = \rho \mathbf{K}^{2} \mathbf{Y}^{2} \left( \frac{\mathbf{r}}{\mathrm{r}_{o}} \left( \frac{\partial \mathbf{u}}{\partial \mathbf{y}} \right)^{2} \right)$$
(28)

The pressure gradient parameter  $\alpha$  is defined as

$$\alpha = \left(\frac{v_{W}}{\tau_{W}}v^{*}\right) \frac{dp_{e}}{dx}$$
 (29)

Solving (29) for  $\frac{dp_e}{dx}$  and substituting in equation (28) and rearranging results in

$$\tau_{\mathbf{w}} \left[1 + \frac{1}{2} r_0 \frac{\mathbf{v}^{\star}}{\mathbf{v}_{\mathbf{w}}} \alpha \left(\frac{\mathbf{r}^2}{\mathbf{r}_0^2} - 1\right)\right] = \rho K^2 Y^2 \frac{\mathbf{r}^2}{\mathbf{r}_0^2} \left(\frac{\partial \mathbf{u}}{\partial \mathbf{y}}\right)^2.$$
(30)

Equation (30) may be placed in law of the wall variables by applying equations (5), (15), and (16) and equalities from Figure 2. Equation (30) becomes

$$\frac{du^{+}}{dy^{+}} = \frac{1}{Ky^{+}} \begin{bmatrix} 1 + \frac{\alpha}{2} r_{o}^{+} (e^{-1}) \end{bmatrix}^{\frac{1}{2}} \cdot$$
(31)

This equation reduces in the limit of large radius to the law of the wall

$$u^+$$
 (Y<sup>+</sup>, 0, 0) =  $\frac{1}{K}$  1n (Y<sup>+</sup>) + B

where  $u^+ = 0$  at  $Y_0^+ = e^{-KB}$ 

= 0.1108 for K = 0.4

Integrating across the boundary layer from  $Y_0^+ = 0.1108$  to  $Y_0^+$  (the edge of the boundary layer) yields

$$u^{+} = \frac{1}{K} \int_{0.1108}^{Y^{+}} \frac{1}{Y^{+}} \left[1 - \frac{\alpha}{2} r_{o}^{+} (1 - e^{2Y^{+}/r_{o}^{+}})\right] dY^{+}.$$
 (32)

Equation (32) represents the law of the wall relation for the velocity profile accounting for pressure gradient. This relation holds throughout the boundary layer with the exception of the viscous sublayer region. Figure 3 reproduced from White's paper shows some velocity profiles obtained by integrating equation (32). The effect of positive (adverse pressure gradient) raising the curve above the incompressible log law and the effect of changes in  $r_0^+$  with finite  $\alpha$  are evident.

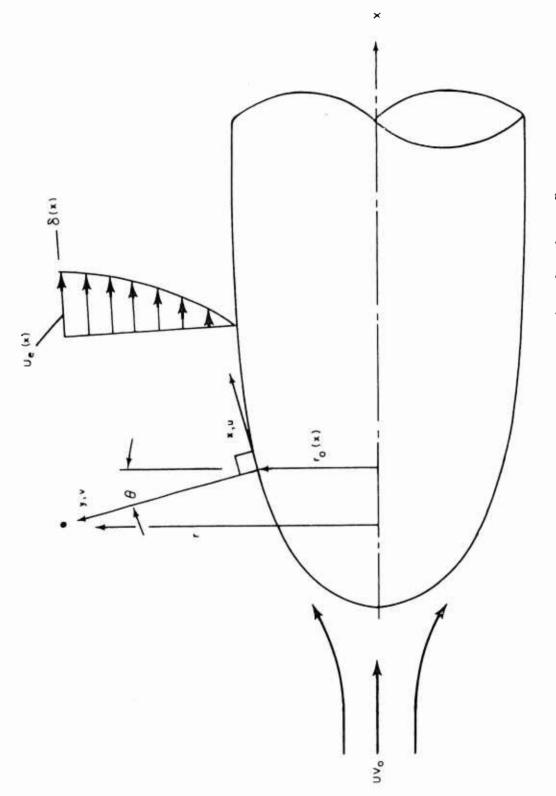
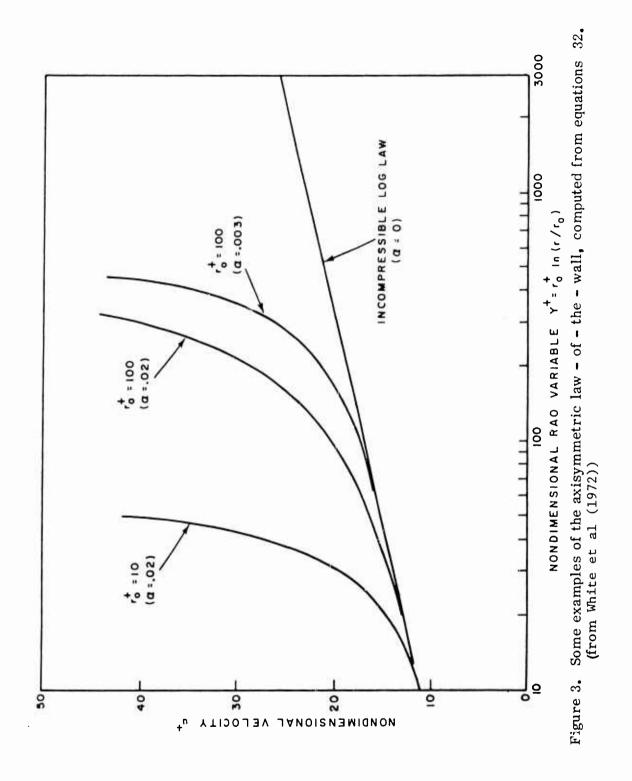


Figure 2. Coordinates for axisymmetric boundary layer flow

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As mentioned previously, many methods have been postulated to predict skin friction. White, F. M. et al (1972, 1973) extended an earlier integral technique developed for flat plate flows (White, F. M., 1968) to the case of thick axisymmetric boundary layer. The method concentrates on the boundary layer equations using inner law variables and is interesting in that boundary layer separation is automatically predicted. The integral technique provides for relatively simple computer solution minimizing required computer time and has been demonstrated by White, to quite accurately predict skin friction. A drawback of the method, as with most integral methods, is that thickness calculations are not very accurate. This is not a serious drawback for the intended calculations since nondimensionalized boundary layer thickness can be applied. A priori specification of the velocity profile is required with this integral technique, as with others. The boundary layer continuity and momentum equations for turbulent axisymmetric flow are given by

$$\frac{\partial}{\partial \mathbf{x}} (\rho \mathbf{u} \mathbf{r}) + \frac{\partial}{\partial \mathbf{y}} (\rho \mathbf{v} \mathbf{r}) = 0$$
(33)

and

$$\rho ur \left(\frac{\partial u}{\partial x}\right) + \rho vr \left(\frac{\partial u}{\partial y}\right) = -r \left(\frac{dp_e}{dx}\right) + \frac{\partial}{\partial y} (r\tau).$$
(34)

where x and y are normal to the body surface as shown in Figure 2. For the portions of the body to which the equations are applied, the angle 0 between the normal to the surface and the normal to the body axis is small and is, therefore, neglected. Assuming the law of the wall (32) is valid across the entire boundary layer, equations (32) through (34) form a closed system that can be solved for the skin friction. The only additional relations required for the present study are those necessary to provide a definition of the polymer wall concentration,

°w.

Appendix A presents a complete development of the equations related to this method along with the additional terms required for solution of the polymer ejection and dilution.

The resulting boundary layer equation, after considerable algebraic manipulation, is

$$\frac{d\lambda}{dx^{\star}} (3_{\alpha} H - G_{1}) + \frac{V}{V} \lambda G_{1} - \frac{\lambda^{2} r_{0}}{2} (e^{2Y_{e}^{\dagger}/r_{0}} - 1)$$

$$+ \frac{\lambda^{\prime \prime}}{R_{1}} (\frac{1}{V})^{\prime \prime} H = -R_{L} V - \lambda \frac{dr_{0}^{\dagger}}{dx^{\star}} I$$
(35)

where

$$\lambda = \frac{U_{e}}{v^{*}} = \left(\frac{2}{c_{f}}\right)^{\frac{1}{2}},$$
(36)

$$X^{\star} = \frac{X}{L}, \qquad (37)$$

$$V = \frac{U}{U_o},$$
(38)

$$R_{\rm L} = \frac{U_{\rm o}L}{v}, \qquad (39)$$

$$\alpha = \left(\frac{v_{w}}{\tau_{w}v^{\star}}\right) \frac{dp_{e}}{dx}, \qquad (40)$$

and the definition of  $G_1$ , H, and I may be found in Appendix A.

Other integral and finite difference techniques for solution of the boundary layer problem although applicable will not be reviewed since they are not of central interest to the work being presented.

## Homogeneous Polymer Flow

Since the early experiments of Toms and Olroyd (1949), a large number of high molecular weight polymers have been shown to be effective drag reducers. Polysaccharides (Guar), polyethylene oxide, polyacrylamides, and sodium carboxymethyl cellulose have received most attention. The data of Hoyt and Fabula (1964) and Virk (1971) show that there is a maximum drag reduction asymptote. This asymptote, for a smooth pipe, corresponds to 80% of the friction reduction that would be attained if completely laminar flow were sustained at a given Reynolds number.

The efficiency of several of these high molecular weight polymers is evidenced in Table 1 from Hoyt (1972).

### TABLE 1

Concentrations (WPPM) of Material Required to Achieve 67-Percent Drag Reduction in Pipe Flow at  $R_e = 14 \times 10^3$  (from Hoyt (1972))

Guar	400
Gum Karaya	850
Polyox WSR 301	10
Polvacrvlamide.	Polyhal1-250 20

Meyer (1966) and Elata, et al (1966) have shown that drag reduction in pipes is due to a thickening of the laminar sublayer. It was shown that the constant B in the law of the wall (6) to remain constant and equal to the Newtonian value until a critical threshold value of the shear velocity was reached  $(v_0^*)$  after which B increased logarithmically with v\*

$$B = 5.5 + \gamma \ln \left(\frac{\mathbf{v}^{\star}}{\mathbf{k}}\right) \tag{41}$$

where 
$$\Delta B = \gamma \ln \frac{v^*}{v_o^*}$$
. (42)

White, F. M. (1968) has plotted data from several investigators and found that

$$\gamma = 2.3 C_w^{1/2}$$
 (43)

Further, the data indicate a maximum value of  $\gamma$  of approximately 11 and a critical shear velocity,  $v_0^*$ , for the onset of Jrag reduction of .08 ft/sec. Many authors have described drag reduction as a "negative roughness effect" since the polymers appear to thicken the sublayer while maintaining the same slope of the u/v\*vs ln  $\frac{yv*}{v}$  curve in the overlap region.

In the outer region, where the wake law holds, polymer additives appear to have no effect on the flow.

Nadolink (1968) demonstrated the existence of the thickened sublayer directly, using a high speed motion picture camera and a microscope.

Virk (1966) presents evidence indicating that the onset shear stress is inversely proportional to polymer molecular radius of gyration. Based on experimental data, the critical wall shear stress,  $\tau_{yr}^{c}$ , which must be exceeded for drag reduction to occur is given by

$$\tau_{w}^{c} = \rho \left(0.625 \text{ x } 10^{6} \text{ } \mu/\text{R}_{\text{G}}\right)^{2} = \frac{\text{constant}}{\text{R}_{\text{G}}^{2}}$$
(44)

where  $R_{C}$  is the rms radius of gyration of the molecule as deduced from light scattering data.

Fabula et al (1969) have pointed out that the small value of the ratio of the polymer molecule scale to the scale of the turbulent eddier at onset indicates that individual molecules are too small by several orders of magnitude to interfere with the turbulence structure. To circumvent this problem of length scales, Fabula postulated an interaction between the time scales of the periodic molecular deformation in the viscous sublayer, given by  $\dot{\gamma}/2\pi$ , where  $\dot{\gamma}$  is the shear rate, and a molecular characteristic relaxation time  $\tau_1$ .  $\tau_1$  is determined by the Zimm or Rouse theories which relate a characteristic relaxation time of the solution,  $\tau_1$ , to the solvent viscosity,  $\mu_s$ , the solution viscosity,  $\mu$ , the polymer molecular weight, M, temperature, T, and the concentration, C

$$\tau_1 = a \frac{(\mu - \mu_s)M}{CRT}$$
(45)

where a is a constant having a value between .4 and .6.

The result is a criteria for the critical wall stress for onset given by

$$2\pi(\dot{\gamma}/2\pi) = 1$$
 (46)

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$$\frac{c}{w} = \frac{\mu}{\tau_1} = \frac{\mu RT}{a\mu_s \mu M} .$$
(47)

Equation (47) may be rewritten applying a relation between intrinsic viscosity, molecular weight and molecular dimensions resulting in

$$u_{w}^{c} = \frac{constant}{R_{c}^{3}}$$
 (48)

Equation (48) of Fabula provides a better estimate of magnitude of onset shear stress whereas Virk's equation (44) gives a better representation when the constant is determined by a best fit of the data.

As an explanation of the effectiveness of very dilute solutions, Fabula postulated that entanglements or "blobs" of macromolecules, rather than individual molecules, are responsible for drag reduction. This explanation has also been proposed by Kowalski and Brundrett (1974). In their work, a formula has been developed connecting the size of the entangled molecules with the size of a dissipative eddy. The macromolecules entanglement hypothesis was tested to predict the so-called onset of drag reduction in pipe flows of homogeneous polymer solutions.

Darby (1972) presents a comprehensive review of drag reduction theories in which comparison of molecular hypotheses, such as Virk's time scale hypotheses, of which Fabula's and Kowalski's are examples; continuum approaches and conventional length scale boundary layer

modifications are made. The continuum mechanics approach results in the conclusion that the presence of elastic properties in dilute solutions being a sufficient criteria for drag reduction. This is accounted for by the inclusion of a dimensionless time parameter (the Deborah number), which is qualitatively the ratio of a characteristic time of the fluid to a characteristic time of the flow system. A presentation of a dozen different forms of the Deborah number is made illustrating the problems encountered with the present "state-ofthe-art" of this approach.

Transition delay from Jaminar to turbulent flow has been reported by White and McEligot (1970) and is found to depend on where the onset shear stress is reached. If the onset shear stress occurs in the laminar flow region, a delay in transition to turbulent flow can occur.

Extension of the pipe flow data to provide insight into flow over flat plates has been successfully performed by many investigators. Granville (1971) has computed the maximum possible drag reduction on a flat plate of 80% at Reynolds numbers of 10<sup>9</sup>. Data on flow over cylindrical bodies are somewhat sparse but evidence of 35% drag reduction by Nadolink et al (1968) for a cylindrical body dropped in a homogeneous polymer solution is representative of the results to be expected.

### Polymer Ejection Studies

Practical applications of polymer solutions imply the necessity for injection whether it be for internal or external flows. Since the polymers have been shown to effect the sublayer resulting in drag reduction, the mechanism of injection, the diffusion process and the quantities of polymers required as compared to the homogeneous flow cases treated previously are of extreme practical importance.

Two approximate methods have been used to treat diffusion patterns in turbulent shear flows. The most widely known method employs the eddy diffusivity model which assumes that the flux of the diffused matter by the turbulent fluctuations is proportional to an eddy diffusivity term, D<sub>p</sub>, multiplied by the local concentration gradient

$$q_y = -D_e \frac{\partial c}{\partial y} .$$
 (49)

Poreh and Hsu (1971) point out that the assumption in this model is that  $D_e$  is a function of the flow field. The fact that its value at a point can be specified regardless of the position of the source only holds true for distances from the source that are large compared to the lagrangian integral scale. Measurements made by Poreh and Cermak (1964) indicate that this characteristic holds for turbulent shear flows and the Lagrangian integral scale is of the order of 10 boundary layer thicknesses.

The second method is based on Batchelor's (1957) lagrangian similarity hypothesis. The hypothesis is used to predict the turbulent motion of particles in steady, self preserving shear flows. Cermak (1962) applied the Lagrangian similarity hypothesis to predict diffusion from a continuous point and line source. He concluded that results from application of the Lagrangian similarity hypothesis were significant for the modeling of diffusion.

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Hsu (1971) and Poreh and Hsu (1971) applied the technique to predict the diffusion boundary layer growth in the intermediate, transition and final zones for polymer flows. Applying the Lagrangian similarity hypothesis, the following equations resulted describing the change of the mean vertical position  $\overline{y}$ , and the mean longitudinal position  $\overline{x}$ , for an ensemble of single particle releases

$$\frac{d\bar{y}}{d\tau} = bv \star$$
(50)

where b is Batchelor's constant, and

$$\frac{\mathrm{d}\bar{x}}{\mathrm{d}\tau} = u(\bar{y}). \tag{51}$$

Combining yields

$$\frac{\mathrm{d}\overline{y}}{\mathrm{d}\overline{x}} = \frac{\mathrm{b}v^{\star}}{\mathrm{u}(\overline{Y})} , \qquad (52)$$

Ellison (1959) estimated Batchelor's constant to be given by b = K. His analysis further suggests that  $\overline{y}$ , the mean position of particles at a given cross section x, is equal to  $\overline{Y}$ , the mean position of single particle releases when  $\overline{x} = x$ . The mean position of particle at any cross section x may be defined as

$$\overline{y} = \frac{\int cy \, dy}{\int c \, dy}.$$
(53)

By replacing y with y/ $\delta_d$  where  $\delta_d$  equals the value of y when C/C  $_{\rm max}$  is .5 and c by

$$\frac{C}{C_{\max}} = f(\frac{y}{\delta_d}).$$

Equation (53) may be integrated to yield

$$\overline{\mathbf{y}} = a_1 \cdot \delta_d \,. \tag{54}$$

Substituting (54) into (52) results in an expression for the development of the diffusion boundary layer with distance x

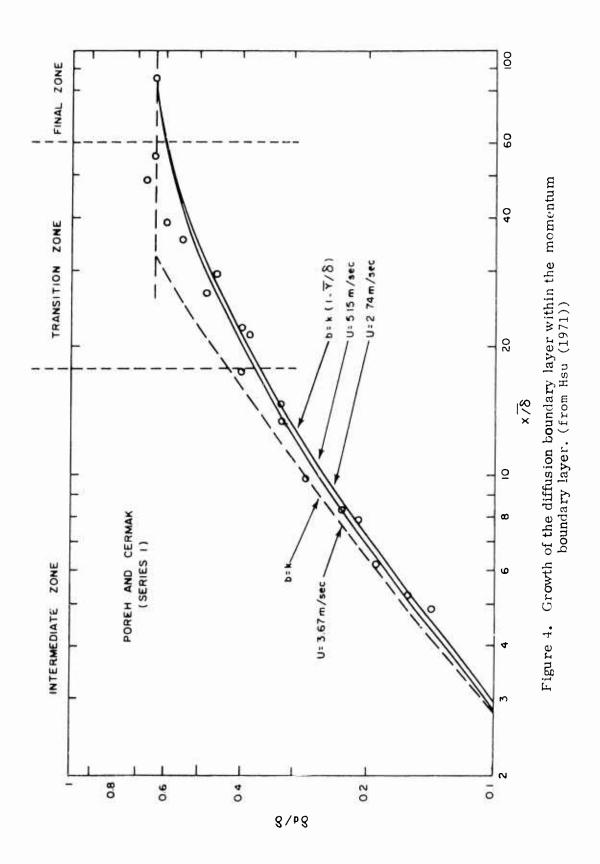
$$a_{1} \cdot \frac{d \delta_{d}}{dx} = \frac{bv \star}{u(\overline{Y})} , \qquad (55)$$

Hsu (1971) has found that better agreement with data occurs if the constant b in (47) is replaced with

$$b = K(1 - \frac{\overline{y}}{\delta})$$
 (56)

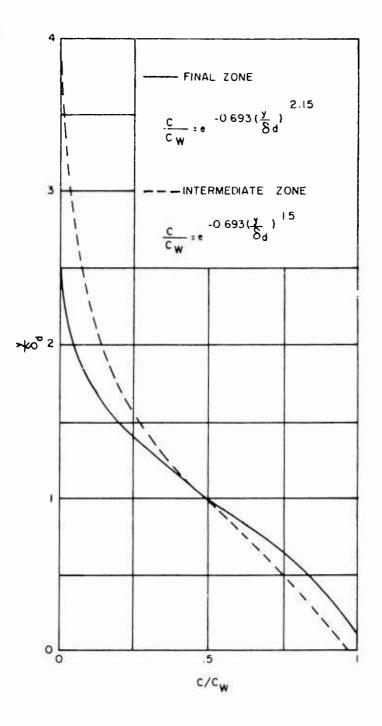
Figure 4 displays a plot showing the growth of the diffusion boundary layer within the momentum boundary layer and depicting the several zones of diffusion.

The above method was applied assuming similarity in concentration profiles with those observed by Poreh and Cermak (1964) for two-dimensional turbulent mixing of ammonia gas from a wall line source. Porch and Cermak envisioned a four-zone process which is worthy of description since the concentration profiles have come under much study as being representative for polymer diffusion. The four zones as defined by Poreh and Cermak are: (1) the initial zone - very little reliable data were obtained in this region due to very large velocity and concentration gradients. The extent of the zone  $(x/\delta)$  was not determined. (2) The intermediate zone - the diffusing plume is submerged in the boundary layer, but its thickness is large compared to that of the laminar sublayer. Diffusion in this zone depends only



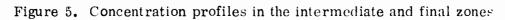
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slightly on the rate of the boundary layer growth. The upper limit of the zone is about  $x/\delta = 18$ . (3) The transition zone - this zone provides for a decrease in the rate of growth of the diffusing plane and to gradually change the shape of the concentration profile. Within this zone  $18 < \frac{x}{\delta} < 60$ . Downstream of this zone,  $\frac{x}{\delta} > 60$ , the diffusion plane grows at the same rate as the boundary layer. (4) The final zone - diffusion is again controlled by molecular action.

Morkovin (1963) described the data taken by Poreh and Cermak as shown below:

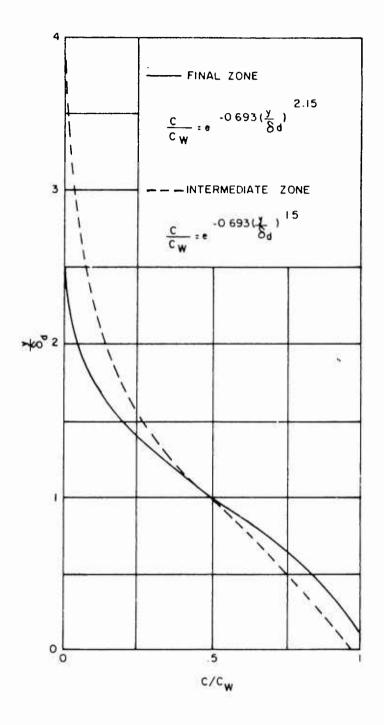
$$\frac{c}{c_{w}} = e^{-0.693(y/\delta_{d})^{1.5}}$$
 intermediate zone (57)

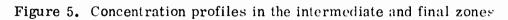
$$\frac{c}{c_{w}} = e^{-0.693(y/\delta_{d})^{2.15}}$$
 (58)

Figure 5 displays a plot of the concentration profiles in the intermediate and final zones.

Wells (1968) suggested uniform injection through a porous wall since it raises the additive concentration to the drag reducing level in the wall region only. Using a Reynolds - Prandtl analogy to analyze the diffusion process, he calculated that distributed ejection would require 40 to 140 times less additive than slot ejection for equivalent drag reductions.

Walters and Wells (1971) conducted tests using uniform ejection of polymer solution through sintered stainless steel smooth cylinders. Fully developed turbulent flow was achieved in the test section. Concentration and velocity profiles measurements were made at





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several different downstream distances. Pressure drops were also measured in the facility to give information on the friction reduction. The concentration measurements were made by using a fluorometric method. Uranine B was used as the fluorescent dye rather than several other dyes, since the laboratory apparatus could be easily decontaminated. The dye was mixed with the ejection fluid and then the tracer sample concentration measured with a fluorometer. Accuracies of the measurement instrumentation of two parts per billion are reported. The conclusions from the study are very interesting. The study showed that the porous wall approach to injection required lower quantities of additives for equivalent drag reduction than by slot ejection. For certain conditions of high polymer mass flux, a wall friction increase possibly due to the higher viscosity in this region was noted. As compared to water injection, a one or two order of magnitude reduction in total diffusivity in the ejection region was evidenced. Downstream of the ejection, an order of magnitude reduction of total diffusivity was noted along with a significant reduction in wall friction.

Latto and Shen (1970) performed an experiment of slot ejection over a flat plate positioned in a flume. Using hot film anemometry, it was found that the momentum diffusivity was less than for pure water. The velocity of injection was also found to be important. It was found to be desirable to keep the injection velocity as low as possible, and tangential to the surface.

Wetzel and Ripkin (1970) experimentally studied polymer injection into a developing boundary layer in a 9-ft-wide open channel. Polymer solutions were injected parallel to the flow near the bottom wall. Pitot tubes were located at positions 16, 28, and 40 feet downstream of the injection slot. Measurements indicated similar velocity profiles at each station. Several methods of polymer concentration determination were investigated. The fluorometric method was found to give satisfactory results. The resulting concentration profiles for water, 1000 WPPM, 2000 WPPM, and 3000 WPPM were found by the author to be in good agreement with the curves developed by Morkovin (1963) described previously.

A maximum drag reduction of 35% was achieved over 40-ft boundary length. Further, at a distance of 16 ft from the slot, greater drag reduction was attained for the low quantities ejected than for the higher. At further downstream distances, the reverse was true. The behavior was attributed to more complete mixing. Large wavering parallel streakes were evidence shortly after injection when the polymer was color dyed. The streaking was reported to be a secondary three-dimensional vortex motion superimposed on the two-dimensional flow.

Fabula and Burns (1970) invoked the negative roughness analogy to flat plat flow with polymers so that the outer layer mean velocity similarity is unaffected by friction reduction. The similarity law of mixing with polymeric friction is predicted to be the same as without polymeric friction reduction. Proceeding with this assumption, a relation for calculating the local additive concentration at downstream stations along the wall was developed. The study includes the effects

of turbulent intermittency and the similarity profile for the local additive concentration as formulated by Poreh and Cermak.

Lessmann (1970) extended this work to the case of a body of revolution with the final result:

$$Q_{i}C_{i} = 2\pi r_{0} = \int_{0}^{\infty} \frac{\overline{u} \overline{c}}{c} \left(\frac{1 + y \cos \theta}{r_{0}}\right) dy$$
(59)

where the terms are in accordance with Figure 2.

Wu and Tulin (1970) presented experimental data obtained by injection of various polymer concentrations along a smooth and rough flat plate. The general conclusions were that the slot ejection angle should be small with respect to the flow direction and the slot width should be comparable with the thickness of the viscous sublayer. It was also shown that a large drag reduction was obtained by ejecting the additive solution at a rate comparable to the normal viscous discharge. The choice of additive concentration of the ejected solution is governed by the length of the boundary and its roughness. These findings suggest that smaller amounts of additives are needed for injection than are usually estimated.

Tullis and Ramu (1973) studied the characteristics of mean turbulent flow in the entrance region of a rough pipe for water flow and for polymer injection into a boundary layer. A 12-inch diameter, 200-ft-long steel pipe was used for the study. Polymer was injected through a perforated wall pipe section. Drag reduction of up to 80% in the fully developed region and 90% in the inlet region were measured. Comparison between water and dilute polymeric solution injection showed that polymer concentration profiles developed slower

than that of dye in water, indicating lower diffusivity. The inlet length needed for flow to fully develop was found to be greater for polymer injected flows than for the case of no injection.

Fruman and Tulin (1974) performed a study of diffusion of a thin tangential jet of polymer solution injected into the turbulent boundary layer of a flat plate suspended in a high speed channel. Free-stream Reynolds number in the order of 3.6 x  $10^7$  were achieved. Drag measurements by reluctance force guages and wall concentrations measured by a light intensity dyed additive method were taken. The concentration distribution along the wall was found to be represented by two regions. Within the first region the wall concentration is practically constant and equal to the injected polymer concentration. In the second region, the concentration varied inversely with the distance from the injection slit. The length of this first zone was some 15 to 20 times that of water injection. The length of this first zone appears to be directly related to the thickening of the viscous sublayer, the reduction of shear stress and the decrease of molecular diffusivity. The data taken correlates well when formulated using a heat transfer analogy to the temperature distribution over a flat plate. The distribution of the wall temperature, T, as given by Seban (1960)

$$\frac{T}{T_{i}} = 25.0 \left(\frac{\rho_{i} v_{i}}{\rho u}\right)^{1.2} \left(\frac{x}{s}\right)^{-0.8}$$
(60)

Tulin's data for  $\rho = \rho_1$  yields

$$\frac{c}{c_{i}} = 17.01 \left(\frac{v_{i}}{U}\right)^{1.06} \left(\frac{x}{s}\right)^{-0.711}$$
(61)

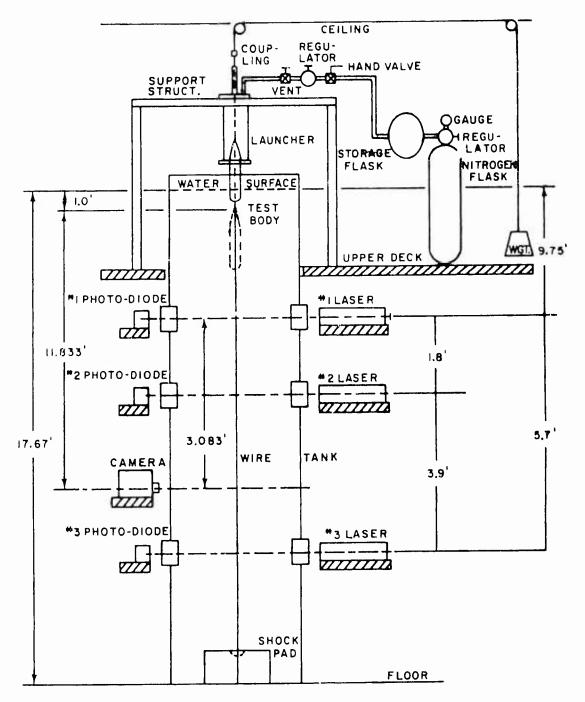
These results reported by many investigators represent clear evidence of the need for additional information regarding i: jection of polymers in external flows and their effect on the diffusion process. There appears to be some discrepancy in the measured concentration profiles between investigations and to the definition of the zones where the diffusion process for polymer flows varies from that of water. This will be the central thought guiding this study.

#### 111. EXPERIMENTAL APPARATUS

The experimental apparatus used in this research consists of a clear plastic drop tank, a launcher, several test models and appropriate instrumentation and photographic equipment to measure model velocity, to deduce boundary layer thickness and to measure boundary layer concentration profiles. Figures 6 and 7 show the major elements of the experimental apparatus. The characteristic of each of the above elements is discussed below.

## Drop Tank

The drop tank facility consists of a 20-ft long clear plastic cylinder 2 ft in diameter. Several viewing collars are available as noted in Figure 7 which may be positioned where desired. These viewing collars, when filled with water, minimize optical distortion due to the tank wall curvature. The liquid in the tank is continuously filtered, excepting during testing periods, to maintain high clarity. Located to either side of the tank are instrumentation platforms which may be set in any vertical position desired. A shock pad consisting of several layers of dense rubber topped with rubberized horsehair pads totalling approximately 1-ft thick is installed at the bottom to absorb the energy of models being dropped. An .062-inch diameter stainless steel wire is suspended down the center of the tank with the other end weighted to approximately 75 lbs. All models were guided down the tank by this wire. The drag of the wire on the bodies has been determined

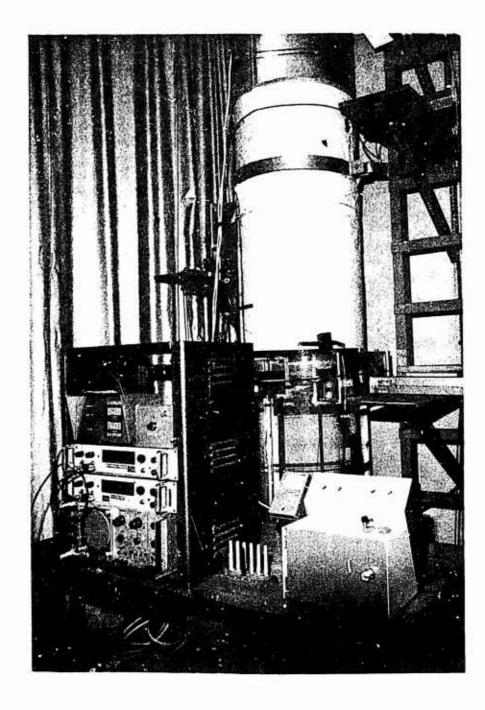


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Figure 6. Experimental apparatus



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Figure 7. Experimental apparatus photograph

by a free fall sphere experiment with similar guide bearings installed in the sphere. The bearing drag force determined is approximately .1 lbs.

# Launcher Assembly

A launcher was deemed necessary in order to obtain steady state velocities in the short drop tank and avoid the problem of predicting boundary layers under a transient condition. Figure 6 schematically shows the launcher components and Figure 8 displays the actual launcher used in many of the tests. As can be seen in Figure 8, the launcher is required to accelerate the test bodies very quickly in a very short distance resulting in high accelerations and, to the dismay of occupants of the building, the launcher ram must stop in a shorter distance with even higher deaccelerations.

The launching problem consists of accelerating a body of approximately 10 lbs weight, plus accelerating launcher components weighing approximately 20 lbs to a desired velocity of 30 ft/sec, the maximum velocity considered for the tests to be performed, in a distance of 24 inches. Applying the impulse momentum relation

$$\int \mathbf{F} \, \mathrm{d}\mathbf{t} = \int \mathbf{M} \, \mathrm{d}\mathbf{v} \tag{62}$$

where F = the force required (neglecting drag on the body)

- t = time for acceleration
- v = velocity

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M = mass of launcher components and body under acceleration.

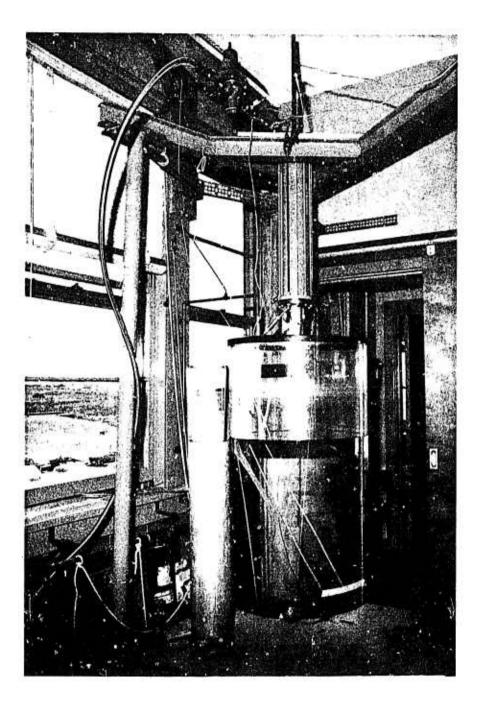


Figure 8. Launcher assembly photograph

: ; The time for an acceleration, a, to 30 ft/sec velocity in 2 feet is given by

$$t = \frac{v}{a} , \tag{63}$$

Determining the acceleration

$$x = \frac{1}{2} at^{2} = \frac{1}{2} \frac{v^{2}}{a}, \qquad (64)$$

Rearranging and solving

$$a = \frac{1}{2} \frac{v^2}{x} = 225 \text{ ft/sec}^2.$$
 (65)

Substituting in (63) yields

$$t = .1333 \text{ sec}$$
 (66)

Integrating (62) with the established limits gives

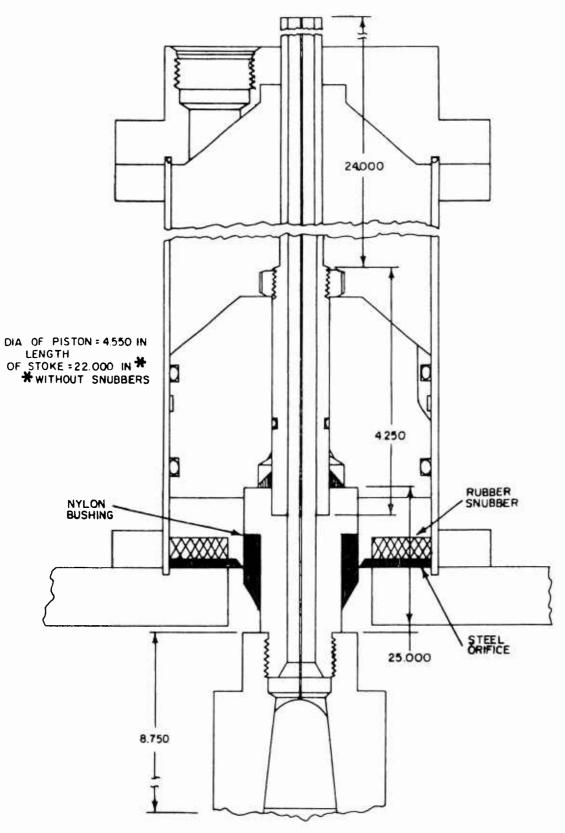
$$t = 0$$
  $v = 0$   
 $t = .1333$  sec  $v = 30$  ft/sec

$$.1333 F = \frac{30}{32.2} (30)$$

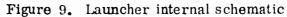
$$F = 210$$
 lbs.

A steady force, therefore, of 210 lbs would do the job. Figure 9 is an assembly drawing of the launcher constructed. The chief components of the launcher come from a high pressure hydraulic damper cylinder normally operated at 3000 psi. For safety reasons, this was satisfying since the pressures that the cylinder would be subjected to in this work were low but the shock loads high. The overall cylinder length was about 2 feet with a working piston diameter of 4.550 in. Fitted to the end of the piston was a conical

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adapter which would mate with the 6<sup>o</sup> tailcone of the prime test model. The total piston assembly including upper guide, piston and lower extension pieces was approximately 62 inches. All pieces were designed to minimize weight. A pressure over the piston of 14 psi should then provide the necessary acceleration force. The problem was to get the working fluid safely to the piston quickly enough.

The remainder of the launcher system, Figure 6, consisted of a high pressure nitrogen supply (2200 psi) regulated down to 150 psi, stored in a 4-cubic ft storage flask whose contents in turn were allowed to pass through a hand operated "fire" valve through a high flow low pressure regulator to the launcher itself. All pressure lines were maintained as large as possible (#12 AN) where equipments permited. The launcher chamber pressure was recorded on a Sanborn recorder so that launch velocities could be varied by varying the low pressure regulator output pressure in a predetermined fashion.

Through tests, it was found that a much higher final pressure was required to achieve 30 ft/sec ejection velocity. A final pressure of about 60 psi was required to account for the inertia of the low pressure regulator and the losses in the delivery line. The launcher has successfully been used in several hundred launches.

## Velocity Measurement Instrumentation

The velocity measurement instrumentation consists of three laser photo-diode stations with known separation as shown in Figures 6 and 7. The lasers are 5 milliwatt helium neon lasers manufactured by Spectra Physics (Model 120). Lasers were used rather than a conventional light source to insure that a sharp cutoff of light by the body would occur. This was especially critical where measurements across the body length dimensions were made. The silicon photo-diodes used to detect the light cutoff were United Detector Technology, Model PIN-020A. Their response time is in the order of 5 nanoseconds, well exceeding the requirements of this investigation.

The outputs of these diodes when amplified was used to trigger two Hewlett Packard counters and a special purpose dual counter. These may be seen in Figure 6 in the instrumentation rack. The bottom instrument was only used for troubleshooting work with the equipment. The instrumentation was so arranged to allow measurement of the velocities, referring again to Figure 6, between stations 1 and 2, 2 and 3, 1 and 3, and across the body (nose to tail) at station 3. Four velocities in all were measured across a total span of 5.7 feet to less than 2 feet. For all except the last measurement, only the breaking of the light beam by the nose of the model was used to start the counters. This is rather important since although the model travelled down the center of the

tank guided by a wire, small lateral movements, especially with the 6° tapered tail model, would result in rather large unknown discrepancies in effective length of the model (where the laser intercepts the model on entrance and exit) and as a result, in the velocity measurements. Lateral motions did not seriously effect measurements taken from the nose of the model at subsequent stations since the curvature of the nose is gradual, introducing less error, and since all lasers were positioned on one side of the wire, at about .25 inches offset, resulting in approximately the same lateral offset at each station if such occurred.

#### Boundary Layer Thickness Measurements

The title of this section is a misnomer of sorts since actual boundary layer measurements in a drop tank experiment of this type could only be performed with extreme difficulty. Especially in the size of free falling model being tested (3-inch diameter x 25 inches long). In fact, what has been done is eject from the test bodies a visible opaque dye and photograph the body and its "boundary layer" at a given position. The assumption is that for a dilute polymer solution, the molecular diffusivity and viscosity are very close to those of the solvent. As concluded by Fabula and Burns (1970) for a far downstream case, the similarity law of mixing with polymeric friction reduction is predicted to be the same as it is without polymeric friction reduction. Two types of dyes

were used; the first, a food coloring, gave excellent results and photographic records but reduced the number of tests to 3 to 4 per day due to the resulting opaqueness of the tank. The second, phenolphthalein solution, was used as an alternative. The solution PH was kept sufficiently low, below 10, so as to not effect the polymers used (this was verified by drag reduction measurements no velocity changes noted with or without the dye). The dye gave excellent photographic results and disappeared within seconds due to the mixing with the water and the resultant lowering of the dye PH. It is assumed for the dye as with polymers that the diffusivity would be equal to that of the solvent.

Figures 6 and 7 show the camera station. A graphic camera and Polaroid, 4" x 5" colored film was used for the photographic records. The shutter of the camera was fixed open just prior to launch and a signal from the first laser station adjustably delayed from the instrumentation console would trigger three flash units exposing the film. The adjustable delay allowed for correction for velocity changes on different tests or to photograph different segments of the body on subsequent but similar tests. Velocity of the vehicle on a run-to-run basis for the same conditions was found to be in the order of 2% allowing for accurate presetting of the delay by a calibrated vernier.

## Test Models

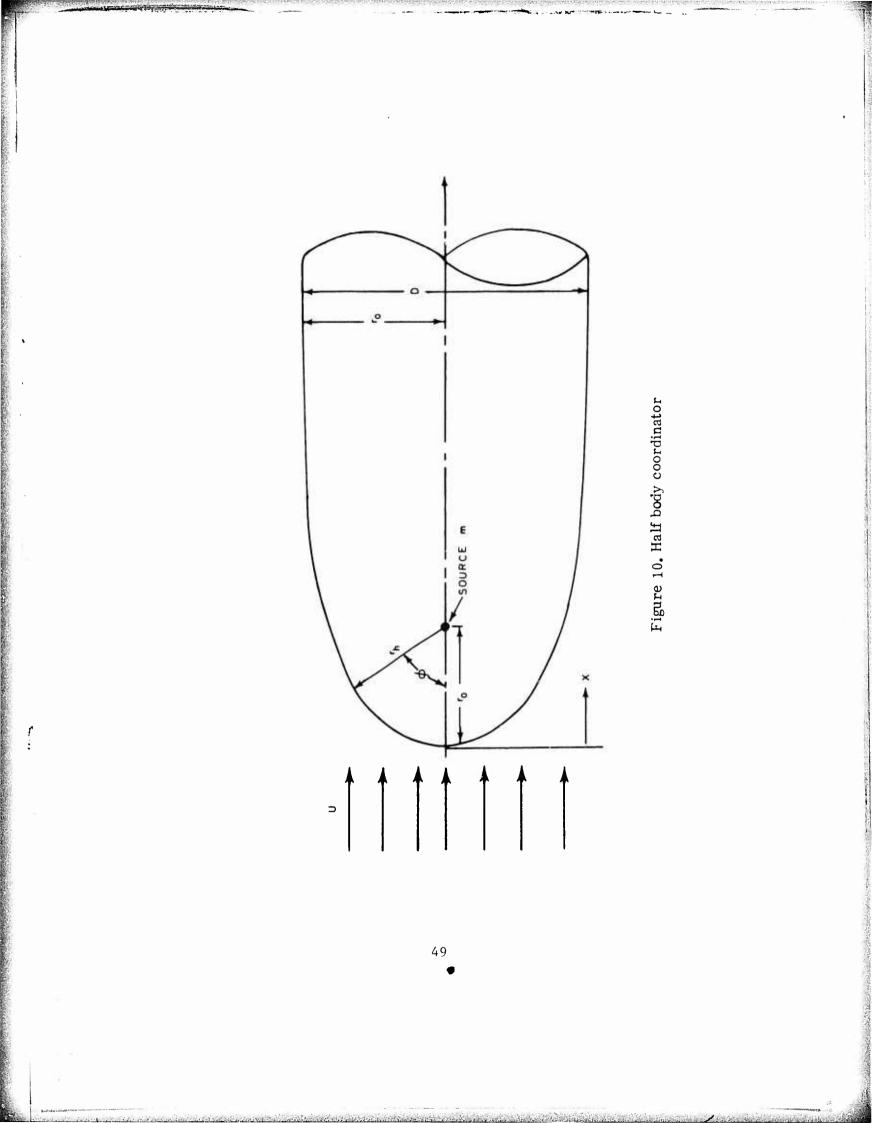
Four axisymmetric models were constructed for use in the test program. Three of these are called the dye ejecting bodies and the fourth, the polymer ejecting body. Their purposes are different in that the dye ejecting bodies are used for drag measurements and for boundary layer photographs and the polymer ejecting body is used for polymer ejection, boundary layer concentration measurement studies. This latter body could also be used, when loaded with visible dye, for boundary layer photographic studies. The models all had a maximum diameter of three inches and an identical forebody design. In fact, the dye ejecting models all used the same forebody with replaceable tail pieces. The forebody chosen for application is a classical "half body" with a length-todiameter ratio of 3.88. The classical half body shape is defined by placing a source, of strength m, in a uniform stream. The resulting shape is defined by the equation

$$r_{\rm h} = R_{\rm o} \sec \frac{\phi}{2} \tag{67}$$

where  $R_0 = \frac{D}{4}$ 

and the coordinates are defined from the source as shown in Figure 10. The body normally extends to infinity but was terminated at 11.65 inches for the models constructed. The half body was chosen for use since it presented a very streamlined, tractable shape for the prediction of pressure coefficients. The equation for the bodies, in x and  $r_0$  coordinates will be given in subsequent sections.

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# Dve Ejecting Bodies

Three different configurations of dye ejecting bodies were constructed. Each uses the same half body forebody discussed previously followed by a three-inch long spacer section of constant three-inch diameter. The various tail pieces were assembled to this assembly. The tail pieces constructed were a 6° tapered tail (12° included angle) terminating in a .5-inch diameter sphere, a 12° tapered tail (24° included angle) terminating in a .5-inch diameter sphere and a 3-inch diameter hemispherical tail piece. Figures 11, 12 and 13 are photographs of the three test models. The equations for the external shape of the bodies measured from the nose as shown in Figure 10 are given by:

Half Body Section

$$r_0 = .079 + 4.346x - .1022x^2 + .122x^3 - 5.29x^4$$
 (68)  
for  $0 \le x \le .981$  inches

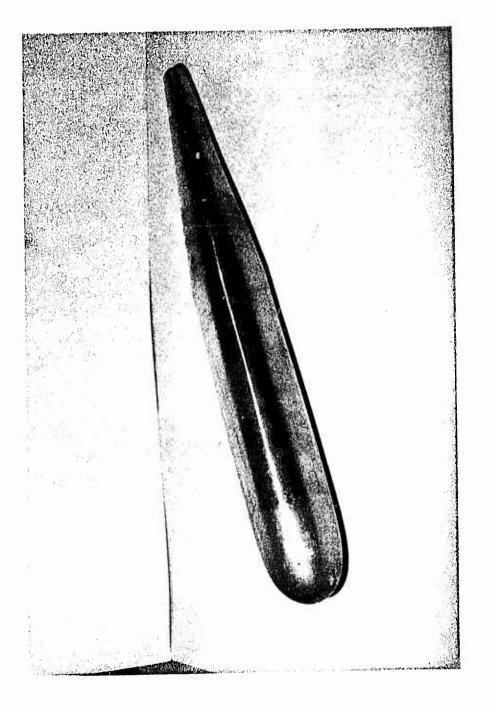
and

$$f_0 = .924 + .3296x - .0669x^2 + .000555x^3 - .000161x^4$$
 (69)  
for .981 < x  $\leq$  11.65 inches.

Constant Diameter Section

$$r_0 = 3$$
 inches for 11.65 < x < 14.65 inches (70)

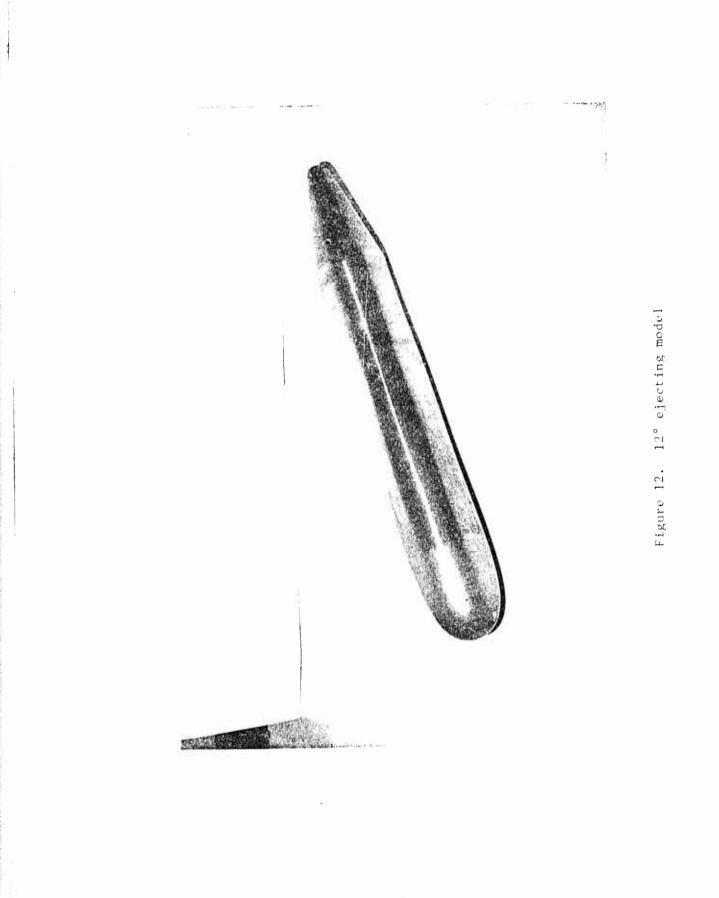
60 Tapered Tail



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Figure 11. 6° ejecting model

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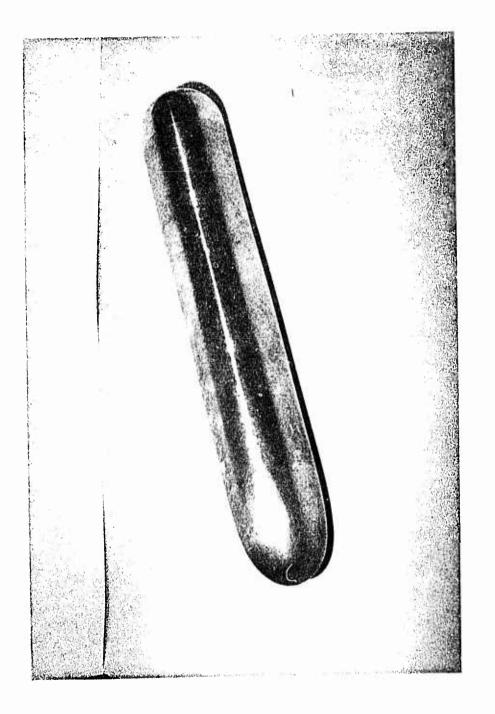


Figure 13. Hemispherical tail dye ejecting model

Natural Contain

Hemispherical Tail for 60 Cone

$$\mathbf{r}_{0} = \left[ 25 - (\mathbf{x} - 24.58)^{3} \right]^{\frac{1}{2}}$$
 (72)  
for 24.58 <  $\mathbf{x} \le 25.04$ .

Equations (68) through (72) described the boundary for the 6<sup>0</sup> model. The conical tail assembly was blended to the cylindrical section to remove the abrupt change in contour at that point. Continuing with the body equations:

12<sup>0</sup> Taper Tail

$$\mathbf{r}_{0} = -.20842 \ \mathbf{x} + 4.6145 \tag{73}$$

for 14.65  $\leq x \leq$  19.65 inches.

Hemispherical Tail for 120 Cone

$$r_0 = \left[.25 - (x - 24.58)^2\right]^{\frac{1}{2}}$$
 (74)  
for 19.65 < x < 20.15 inches.

Equations (68), (69), (70), (73) and (74) describe the external boundary for the  $12^{\circ}$  model.

Hemispherical Model

Constant Diameter Section

 $r_0 = 3$  inches for 11.65 < x < 15.132 inches. (75)

Hemispherical Tail

$$r_{o} = \left[2.25 - (x - 15.132)^{2}\right]^{\frac{1}{2}}$$
 (76)

for  $15.132 \le x \le 16.632$  inches,

Equations (68), (69), (75) and (76) form the equation for the hemispherical tail model.

All bodies were constructed of aluminum and allowed for the addition of weights for matching of velocities when testing the

models under increased drag conditions. Figures 14 and 15 describe the body components and features. Referring to the figures, an explanation of the operation of the model will b ... describe the function of the various pieces. The model is made ready for a launch by inserting the tank guide wire through the body guide tube, (9), the wire bears on a nylon bearing at either end of the model to minimize friction. The tail, (10), of the model is removed (separated sufficiently) and the internal cavity filled with dye. The dye ejection ports (6) being previously taped over to insure no loss of dye. The model is reassembled and the vent screw (unmarked) in the tail is removed and the model placed under the water level in the tank to back fill the cavity totally with water. The model may now be fired upon removal of the tape over the ejection holes. When fired, stagnation pressure enters the 4 stagnation ports, (1), is transmitted through the body guide tube and pressurizes the bladder, (4), forcing the dye out the four dye ejection ports located at the minimum pressure point of the forebody as determined by a potential flow program. After several tests, the bladder was found to be not necessary simplifying the operation. The stagnation ports consisted of 8, .050 inch diameter holes located on a .625 inch circle at the nose of the body. The four ejection ports were also .050 inch diameter placed on a 1.125-inch diameter circle, normal to the surface of the body. Table 2 summarizes the pertinent information about the bodies.

STAGNATION PRESSURE INLET PORTS  $\begin{array}{c}
1 \\
2 \\
3 \\
4 \\
5 \\
6 \\
7 \\
8 \\
9 \\
10
\end{array}$ 

BODY WEIGHTS

DYE STORAGE VOLUME

BLADDER FOR DYE EXPULSION

REPLACEABLE TAIL CONFIGURATIONS

DYE EJECTION PORTS

HALF BODY CONTOUR

SPACER SECTIONS

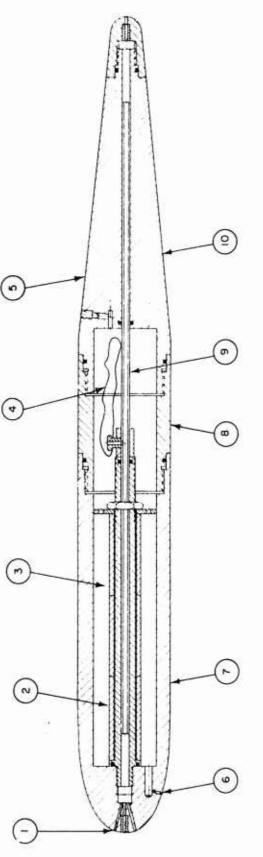
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REPLACEABLE TAIL CONFIGURATIONS

Figure 14. Dye ejecting axisymmetric body description



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## TABLE 2

LENGTH (FT)	60 TAIL 2.0833	<u>12<sup>0</sup> TA1L</u> 1.679	HEMISPHERICAL TAIL 1.386
DIAMETER (FT)	. 25	.25	.25
L/D	8.33	6.7	5.54
FRONTAL AREA (FT <sup>2</sup> )	.0491	.0491	.0491
WEIGHT IN WATER (LBS) WEIGHTED	4.43	7.109	3.95
UNWEIGHTED	3.47	-	2.94

Dye Ejecting Axisymmetric Body Information

## Polymer Ejecting Body

The polymer ejecting body is similar in external configuration to the  $6^{\circ}$  dye ejecting body. The equations for the external shape hold for this body. The body has been designed to perform two functions while traversing the length of the drop tank. These functions are:

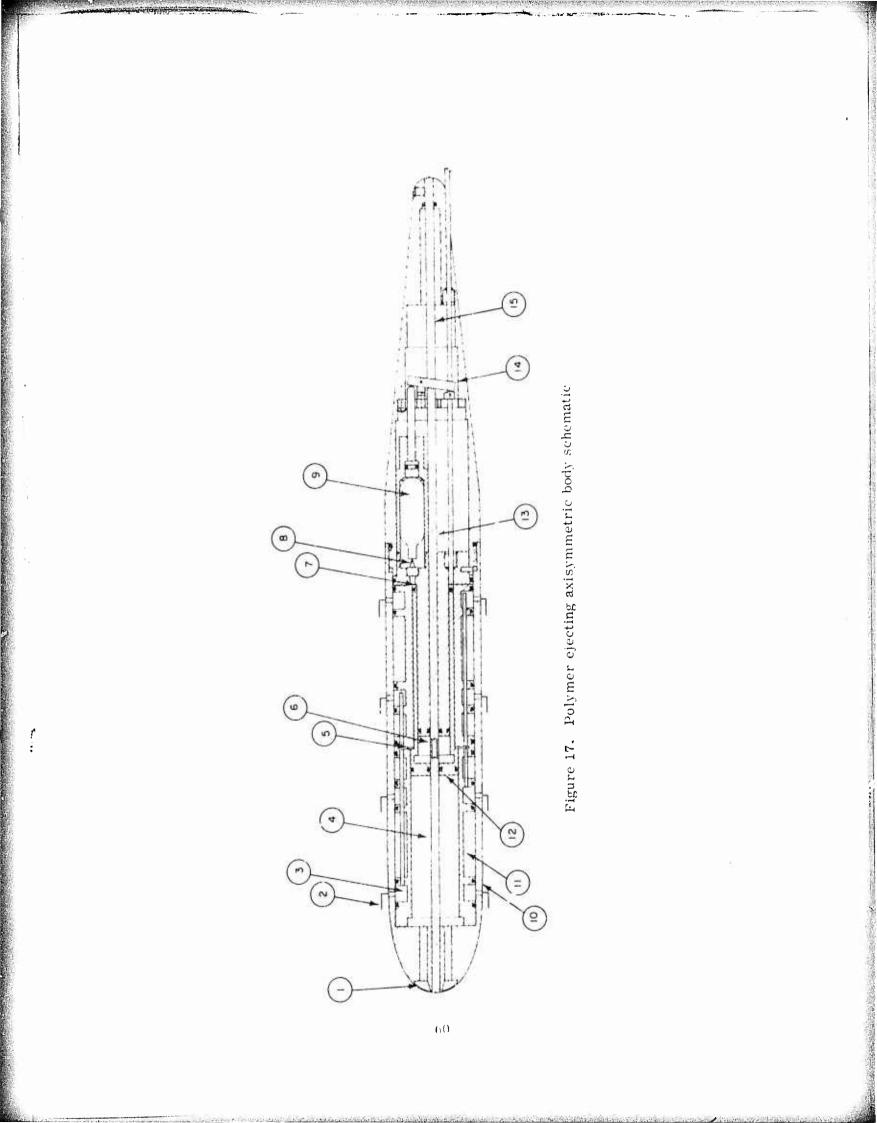
- 1. Eject polymer or other fluids at a constant rate
- 2. Withdraw samples from the boundary layer at

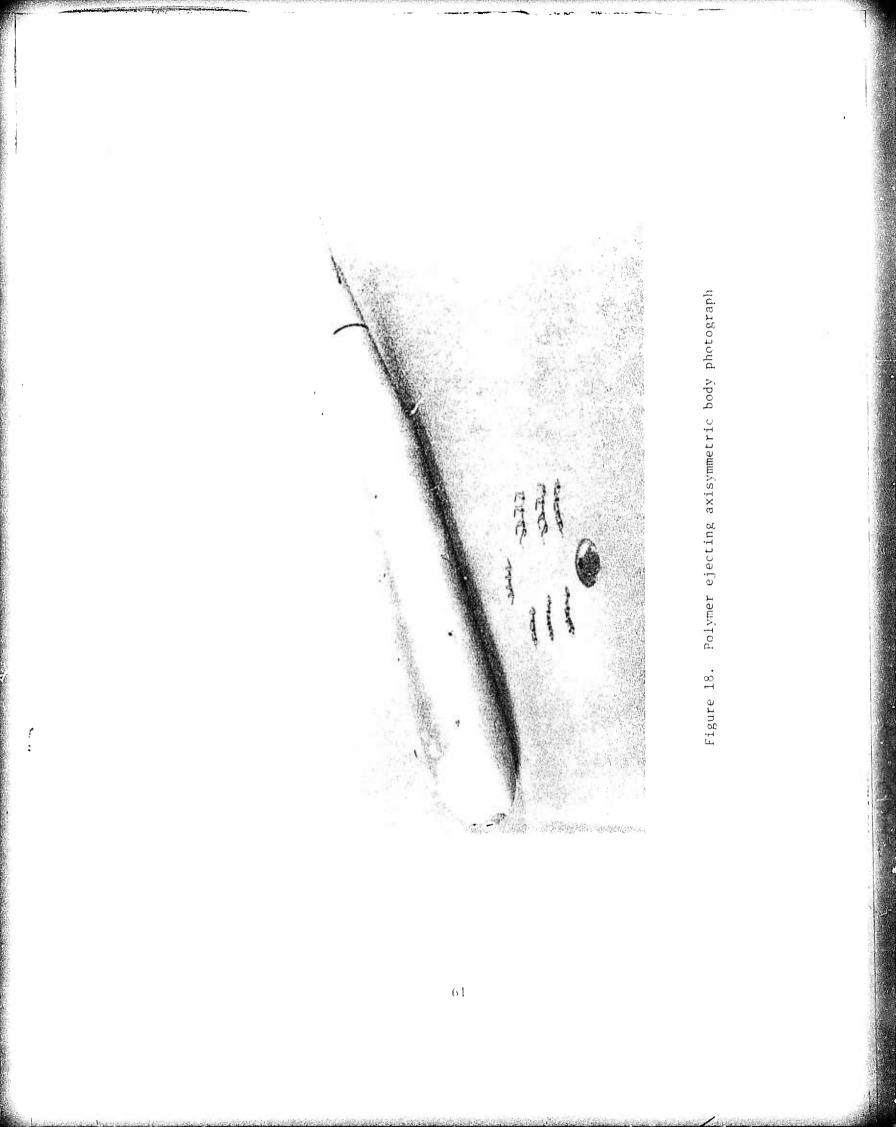
four axial stations

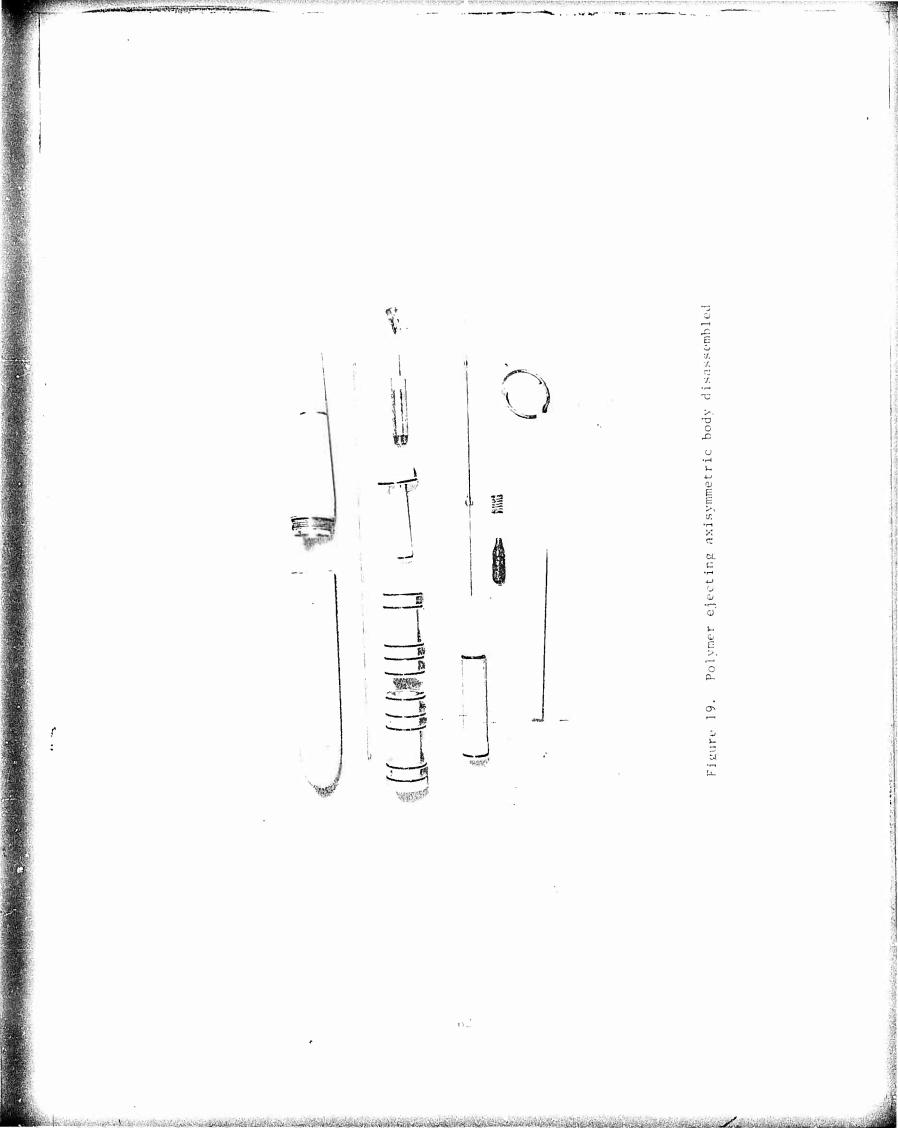
Figures 16 and 17 describe the various elements of the ejecting body. These elements may be viewed in assembled and disassembled form in Figures 18 and 19, respectively. The overall dimensions of the model are 25 inches in length by 3 inches in diameter. Prior to discussing the design values of the various elements, a

POLYMER EJECTION SCREEN BOUNDARY LAYER SAMPLE TUBES BOUNDARY LAYER SAMPLE COLLECTION CHAMBER POLYMER SOLUTION STORAGE VOLUME SUCTION PISTON FOR BOUNDARY LAYER SAMPLING POLYMER EJECTOR PISTON AMBIENT PRESSURE BACKFILL VOLUME POLYMER EJECTOR PISTON PRESSURIZATION AREA CO<sub>2</sub> ORIFICE AND PUNCTURE NEEDLE CO<sub>2</sub> SUPPLY HALF BODY CONTOUR VOLUME AVAILABLE FOR WEIGHT POLYMER EJECTOR PISTON STROKE MEASUREMENT ROD CO<sub>2</sub> SUPPLY ACTIVATION DEVICE BODY GUIDE TUBE

Figure 16. Polymer ejecting axisymmetric body description







description of the operation of the model will serve to identify all the major components. Referring to Figures 16 and 17, the model is assembled for a launch with polymer or other fluid in the storage volume, (4) and a fresh energy source, (9), a CO<sub>2</sub> cartridge installed. The model is placed on the guide wire in the drop tank, (15), and inserted in the launcher. A nylon shear screw is attached through the launcher to the polymer ejector piston stroke measurement rod, (13). This rod serves to hold the model in the launcher and, upon impulsing the launcher, triggers the CO<sub>2</sub> supply activation device, (14), puncturing the CO<sub>2</sub> cartridge and releasing the constant pressure (800 psi) gas supply. The model leaves the launcher shearing the nylon screw allowing the spring loaded stroke measurement rod, (13), to bear against and follow the polymer ejector piston, (12), in its travel. The gas from the  $CO_2$  supply passes through an orifice, ( 8 ), and pressurizes the annular piston area, (7), of the polymer ejector piston driving it forward. This action results in ejecting the polymer from the storage volume, (4), through the ejection screen, [1], and providing a suction in the annular area, (5). This area is connected to four equal sampling chambers, (3), through tubes located within  $30^{\circ}$  of the arbitrarily chosen top of the model. The suction then draws either a wall sample or a sample, As the piston, (12), is moving, ambient pressure, from a probe, (2) which varies from atmospheric at the surface of the tank to near 9 psi above atmospheric at the bottom of the tank, enters the guide

tube, (16), and is transmitted to the ambient pressure backfill volume, (6). Finally, at the end of the piston, (12), travel, the CO<sub>2</sub> gas is vented to the backfill volume chamber, (6), and out the guide tube, (15). The model at the end of a test is thoroughly vented of gas and readily handled.

The model was designed with several thoughts in mind. First, it would be desirable to eject at as low a velocity as practical so as not to disrupt the flow. Secondly, ejection in the nose stagnation region forward of the minimum pressure point would be desired to minimize the possibility of early tripping of the boundary layer to turbulent flow. The volume ejection rate should result in an annular flow of about the same dimensions as the laminar boundary layer thickness to minimize the disturbance on the flow field. The stroke and suction process should be at a constant The suction process should be at a low enough rate to minirate. mize the disturbance on the boundary layer and, for the wall suction case, to insure a sample is withdrawn near the wall and not penetrating the boundary layer too far. Finally, all processes should be completed prior to the model impacting the bottom so as not to be either ejecting or sampling under a zero velocity condition. Conversely, it is desirable to delay sampling until the boundary layer has been established at launch. This requirement was difficult to achieve and attempts discarded early in the design process. The errors introduced are less than 8% for the worse case.

The first design parameter fixed was that of deciding on the required polymer ejector volume. After deciding to keep the model as light as possible, constructing with aluminum, a guessed weight in water, based on some calculations for a hemispherical nose, a cylindrical section and a tail, of 4.43 lbs resulted for a 24-inch long body of 3-inch diameter. Assuming drag coefficients of .22 and .11, the velocity of the body was determined by the equation:

$$U = \left(\frac{W-B}{1/2 C_{\rm D} \rho A}\right)^{1/2}.$$
 (77)

The calculated velocities for 70° water were

U = 20.6 ft/sec for  $C_D = .22$ U = 29.0 ft/sec for  $C_D = .11$ .

The Reynolds numbers for these velocities were

 $R_e = 3.9 \times 10^6$  @ U = 20.6 ft/sec  $R_e = 5.5 \times 10^6$  @ U = 29.0 ft/sec.

The Laminar boundary layer thickness may be calculated using flat plate approximations and assuming a position 2 inches back along the body surface. From Schlichting (1968)

$$\frac{\delta}{x_{\rm s}} = \frac{5.2}{(R_{\rm e})^{1/2}}.$$
(78)

Now  $R_{e_x} = 3.25 \times 10^5$  U = 20.0 ft/sec  $R_{e_x} = 4.6 \times 10^5$  U = 29.0 ft/sec.

Therefore,

 $\delta = 1.52 \times 10^{-3} \text{ ft}$  U = 20.0 ft/sec.

$$\delta = 1.27 \times 10^{-3} \text{ ft}$$
 U = 29.0 ft/sec.

Now, the volume flow through the annulus around the body is given by

$$Q_{\delta} = .6 U_{\parallel} \Pi D \delta$$
(79)

where .6U is used as an approximation to an average velocity in the region. For the two conditions being calculated

> Q = .0148 ft<sup>3</sup>/sec = 25.5 in<sup>3</sup>/sec for U = 20.6 ft/sec Q = .0174 ft<sup>3</sup>/sec = 29.9 in<sup>3</sup>/sec for U = 29.0 ft/sec.

The usable tank length for model tests is about 13 ft; therefore, the time of ejection will be about

$$t_1 = \frac{18}{20.6} = .63$$
 seconds  
 $t_2 = \frac{18}{29} = \frac{1}{.448}$  seconds,

Required volumes for storage are

 $U_s = 16.0 \text{ in}^3$  U = 20.6 ft/sec $U_s = 13.4 \text{ in}^3$  U = 29.0 ft/sec

Comparing these volume flux rates with expected velocities from the nose, assuming a one-inch diameter ejection port with a 30% open area screen installed

$$\frac{Q_{\delta}}{(A_{e})(.30)} = 9 \text{ ft/sec} \text{ for } U = 20.6 \text{ ft/sec}$$
$$\frac{Q_{\delta}}{(A_{e})(.30)} = 10.6 \text{ ft/sec}$$

for U = 29.0 ft/sec.

These velocities are high. Velocities in the order of 5 ft/sec would be much more desirable. Reduction of velocities by 1/2 would result in a storage volume goal of about 8 cubic inches. This reduction would also result in smaller thicknesses of flow in the boundary layer as compared to the laminar layer thickness.

The effective polymer storage volume designed into the model is 8.25 in<sup>3</sup> with a stroke of 4.67 in. and a stroking time of .4 secs.

The ejector screen used in the model, Figure 18, was formed to the contour of the forebody nose. The screen contained 517 .024 inch diameter holes per square inch with a 24% open area. The outside diameter of the screen is 1.37 inches and the inside diameter .3 inches. The projected area is  $1.4 \text{ in}^2$  with an open orifice area of .337 in<sup>2</sup>. This ejection area resulted in a 5-ft per second ejection velocity.

The screen used is a No. O straight screen from Harrington and King Perforating Company.

The suction time was next to be determined. Since the single piston approach was decided upon, the stroke available and the stroking time for use was equivalent to that for the ejector piston, 4.67 inch and a time of .4 seconds. The suction rate for the design of the suction piston is 11.675 in<sup>3</sup>/sec. Applying a method defined by Dowdell (1973) for correction of the measured "wall concentrations" due to the sampling process

drawing further out in the boundary layer, an estimation of a reasonable sample rate and sample probe orifice size were made. It was first decided that samples would be made at stations 3, 6, 9, and 12 inches back from the nose of the body. This selection was somewhat governed by the need in the tail for other machinery space. From a measurement standpoint, it was desirable to maximize sample size but from a correction standpoint, minimal flow velocity is desirable. As a result, four suction ports 90° apart, were located at each measurement plane. Additionally, at each subsequent plane the port locations were rotated 22° 30' so as not to be affected by the flow entering the ports in the previous place, Figure 18. The next step was to define the approximate boundary layer thickness at the most forward probe station for the highest Reynolds number case as used before. This would give the thinnest boundary layer which is the worst case. Using a flat plate turbulent boundary layer thickness expression from Schlichting (1968)

$$\frac{\delta}{x} = \frac{0.37}{(R_{\rm o})^{1/5}} \,. \tag{80}$$

From (80),  $\delta = .05$  inches.

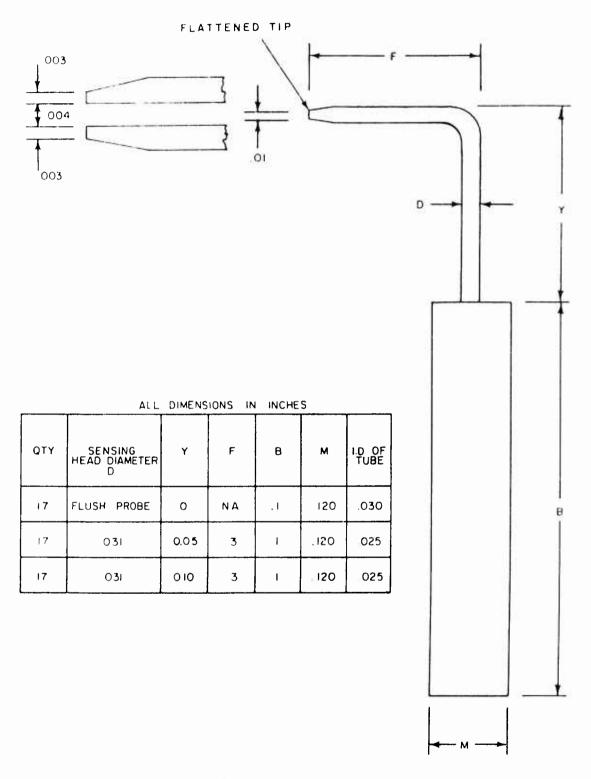
A matrix of probe sizes (inside diameter) and suction volumes were examined for the piston rates calculated, body velocities and the boundary layer thickness calculated above. This was also performed for a boundary layer thickness of .025 inches, postulated to be the thickness that might occur when polymers

were added. The result was that a .760 cubic inch suction volume and sampling tube inside diameter of .030 inches would give acceptable results. A worst case correction factor of

## $\frac{C}{C}$ measured = .54 $\frac{C}{W}$ actual

was calculated for a .025-inch thick boundary layer. This correction reduced to about .8 at a boundary layer thickness of .05 inches. Although a lower correction factor would be desirable, an ample sample volume of fluid is necessary for concentration determination. This suction rate and flush wall sample tube size had an inflow rate per tube of approximately 14 ft/sec.

The pitot probes to be used in sampling the boundary layer away from the wall were designed to minimize the effects on the flow. Two heights were chosen for measurement, .025 inches from the wall and .055 inches. These selections came about, in part, due to physical limitations. With the physical dimensions of the probes, it is difficult to get closer to the wall and with the projected boundary layer thickness for the first station, it is not desirable to get any further from the wall. These heights would allow for a reasonable three-point plot of boundary layer concentrations. Figure 20 displays the salient features of the probes. As is noted, a thin wall tubing is used which allows for flattening of the tip to .01-inch thickness. The resulting inner dimension for sampling is .004 inches high. Sampling



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Figure 20. Special boundary layer probes

velocities in the tube are approximately 20 ft/sec. Sixteen probes were used in each test replacing the sixteen flush wall probes.

The model design, as can be seen from the schematic, Figure 17, contained void volumes in the suction lines which were prefilled with liquid. The void volume is 1.4316 cubic inches resulting in a sample dilution factor of .1327.

The stroking piston pressurization system consists of the carbon dioxide (CO2) cartridge, a puncture device and an orifice. Since the goal is a constant rate ejection process, the use of a CO<sub>2</sub> cartridge as the gas source was chosen since the substance is stored in liquid form with a vapor pressure of 800 psi at about 65<sup>o</sup>F. Little change in the vapor pressure would occur during the use cycle as the gas is drawn off. The system was designed to minimize the free volumes in the high pressure area to insure a sufficient gas supply for the stroking process, Figure 17. The CO<sub>2</sub> cartridge in the final version of the model is inverted from that shown in Figure 16, with the puncturing needle placed on the opposite end also. This was done to achieve reproducibility in the stroking of the piston. Apparently, either freezing of the orifice or slight contaminants would plug the metering orifice resulting in extreme variability of stroking times. The reversal corrected the situations. The pressurization area and orifice area size for metering the CO<sub>2</sub> gas were

selected to provide the stroking rate previously determined. The area was somewhat governed by the desire to maximize the drop tank depth pressure balance area, 6, Figure 17. The volume in this area, besides providing for balancing of the depth pressure also minimizes the weight change during a launch by water backfilling the volume. The CO<sub>2</sub> piston pressurization area designed was .785 in<sup>2</sup> with a resultant total volume of 3.68 in<sup>3</sup>. The orifice size was determined to achieve the .4 second stroking time. Considering that the orifice is small enough such that choked flow conditions exist, the pressure ratio across the nozzle is given by, Shapiro (1953),

$$\frac{p_2}{p_1} = \left(\frac{2}{k+1}\right)^{\frac{k}{k+1}}$$
(81)

Which for k = 1.29 for  $CO_2$  gas @  $68^{O}F$  yields

$$\frac{p_2}{p_1} = 0.55.$$
(82)

Therefore, flow will be a maximum for downstream pressures less than or equal to 440 psi with an upstream pressure of 800 psi. The flow rate is given by, Shapiro (1953)

$$\left(\frac{w}{A_{1}}\right)_{\text{max.}} = \sqrt{\frac{2gk}{k-1}} \left(p_{1}\rho_{g}\right) \left[\left(\frac{2}{k+1}\right)^{\frac{2}{k-1}} - \left(\frac{2}{k+1}\right)^{\frac{k+1}{k-1}}\right]$$
(83)

where  $p_g = .114 \text{ lbs/ft}^3 @ 68^\circ \text{F}.$ Substituting in (83):

$$\frac{w}{A_1} = 4.28 \times 10^2 \text{ lbs/ft}^2 \text{ sec.}$$
 (84)

Converting to match the volume flow requirements

$$\frac{Q}{\Lambda_1} = \frac{w}{\rho_g \Lambda_1} = 37.54 \text{ x } 10^2 \text{ ft/sec.}$$
(85)

To achieve the 9.2 in<sup>3</sup>/sec volume stroking rate for the pressurizing gas volume, Q must equal 9.2 in<sup>3</sup>/sec and  $A_1$  is determined. Substituting in (85)

$$A_{1} = 1.418 \times 10^{-6} \text{ ft}^{2}$$

$$= 2.04 \times 10^{-4} \text{ in}^{2}$$
(86)

Therefore, the orifice diameter must be .016 inches. This diameter orifice has been used in the model.

The important characteristics of the 6<sup>o</sup> ejecting model as finally designed and constructed are displayed in Table 3.

## TABLE 3

## Characteristics of 6<sup>0</sup> Ejecting Model

Length	2.0833 ft
D	.25 ft
L/D	8.33
Weight in Water	4.46 lbs
Polymer Solution Storage Volume	8.25 in <sup>3</sup>
Stroke	4.67 in
Stroke Time	.400 sec
Suction Volume	.760 in <sup>3</sup>
Suction Volume Per Sampling Chamber (4 Chambers)	.19 in <sup>3</sup>
Sample Dilution Factor	.1327
Ejection Velocity	5 ft/sec

## Boundary Layer Concentration Measurements

Several methods exist for the measurement of the concentration of polymer in a sample solution. These include polarographic, turbidity, simple opaqueness and fluorometric methods. A comparison of all but the opaqueness is given in Wetzel and Ripkin (1970). The opaqueness method, which relies upon a measurement of light cransmission through a portion of the boundary layer, cannot be applied to the moving body case since short time measurements and accurate body position with time would have to be known. The remaining methods are all applicable to the conditions of this study since they deal with a sample of solution. The method chosen for use is the fluorometric method. This method has been used successfully by Walters and Wells (1971), Wetzel and Ripkin (1970) and Tullis and Ramu (1973). The method consists of injecting a tracer dye into the fluid being analyzed and capturing a sample of the fluid for analysis. This assumes, of course, that the diffusion of the tracer dye is identical to that of the boundary layer mixture. A reasonable assumption as data comparing various measurement methods by Wetzel and Ripkin (1970) display. The tracer dye, which may be colorless, fluoresces when radiated with an ultraviolet source. This reradiation is measured with a photomultiplier tube and is proportional to the concentration of dye in the sample. The fluorometer used in these tests is a G. K. Turner Associates Model 111 Fluorometer.

Several tracer dyes may be used. Two prime candidates are Rhodamine-B and Uranine-B. Both are compatible with polymer solutions in that the mixture was stable and the drag characteristics were unaffected when measured in a Turbulent Flow Rheometer similar to that described in Hoyt (1966). The Rhodamine-B gives excellent results with solution concentration of 1 part in 10 inches on a weight basis but is very difficult to cleanse from the apparatus. The Uranine-B dye was readily adaptable to laboratory use and gave reproducible readings to about 1 part in  $10^9$ on a weight basis. This was sufficient for the experiment to be performed since the dye concentration in the solution to be ejected could be adjusted to produce samples along the body sufficiently above the background levels to give reproducible results. Calibration curves were experimentally developed for the instrument using known concentration of Uranine-B dye in the tap water to be used in the experiment. The Model 111 Fluorometer has four sensitivity settings allowing calibration curves to be drawn over a range of about 1 part per  $10^6$  to 1 part per  $10^9$ , on a weight basis. For concentrations greater than the lower value, dilution prior to measurement was performed. The calibration charts for this experiment are shown in Figures 21. and 22. Approximately a 3.5 to 4.5 ml sample is required for measurement. This sample is placed in a cuvette (a small test tube) and placed in the instrument and the measurement taken.

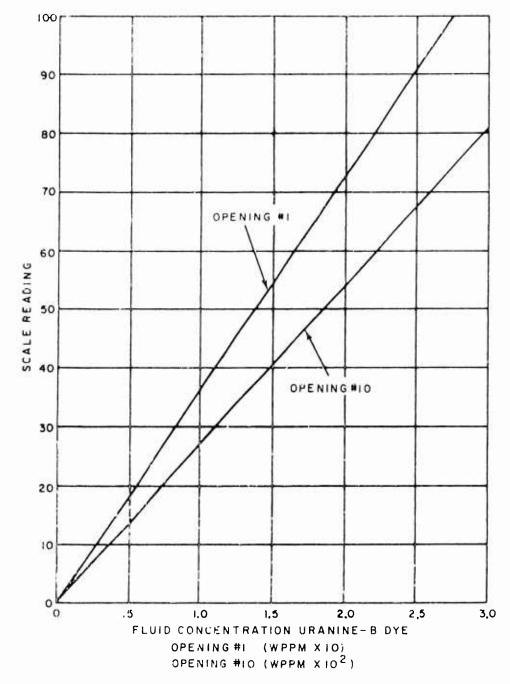


Figure 21. Calibration curves for model 111 fluorometer - openings 1 and 10

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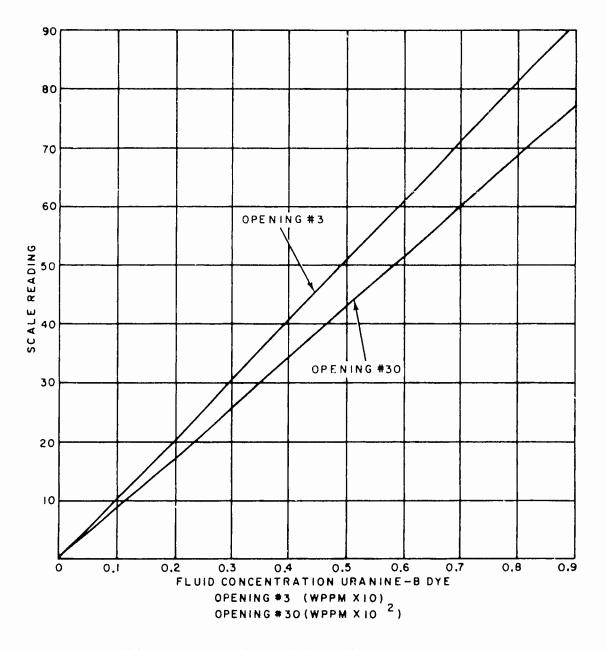


Figure 22. Calibration curves for model 111 fluorometer – openings 3 and 30  $\,$ 

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Can wave to tak a constraint outside of the empiric clean prior to measurement since these prints do effect the readings. Wiping with a paper cowel was found to be sufficient. All samples were allowed to achieve room temperature prior to reading.

## Model Calibration

### Concentration Measurement Calibration

The ejecting model, as designed contained four sample collection charbers drawing simples through four flush will or four pitet probes per sample chamber. These diffection chambers are all connected by 3/32 inch inside diameter tubing to the suction piston. The transfer tubes are of unequal lengths resulting in an interesting transient analysis problem of defining the suction rate differences per sample chamber. The problem was circumvented by calibrating the model through a series of experiments. Additionally, a calibration was desirable since it was difficult to determine the exact word volume per sample chamber previously stated at 1.4318 (which inches which resulted in a dilution factor of .1327. This resulted in a sample concentration lower than the boundary layer sample concentration. It was first thought to leave these void spaces air filled eliminating the dilution factor. Early tests showed that with the body in the tank in the vertical position, the water pressure head difference would result in a venting of the air in these chambers, since they were interconnected, out the uppermost chamber and a filling with tank water through the lower chambers. Prefilling with water, as will be

discussed later, eliminated the problem. To calibrate the model, an assembly and calibration tank was constructed. The tank is displayed in Figure 8 in the foreground having dimensions of 8-inch diameter by 3 feet height. The model is installed in the tank tail first as shown in Figure 23 and fired by pulling on a preattached lanyard. The following procedure was followed in calibrating the model. The model was assembled excepting for the half body nose and placed in the tank after connecting the lanyard to the firing rod. Tap water was placed in the tank just below the level of the polymer ejection volume completely filling all sample chamber volumes. The nose is then installed and a sample background reading of the water taken. The water was then contaminated with the Uranine-B tracer to one of three concentration levels called the Ocean Concentration. These were approximately  $.3 \times 10^{-7}$ , .8 x  $10^{-7}$  and 2 x  $10^{-7}$  WPPM, which were determined to result in an appropriate spread of chamber concentration levels. The model was ther fired. The samples were withdrawn and measured in the Fluorometer. The samples were withdrawn by removing the model from the calibration tank, wiping the outside dry while holding in a horizontal position with the top, as defined by the position of the internal suction transfer tubes, being in the uppermost position and placing the model over individual collection trays. The samples would drain into these four separate trays for analysis. It is necessary to keep the suction transfer tubes in the uppermost position to insure no transfer of liquid between the chambers. The

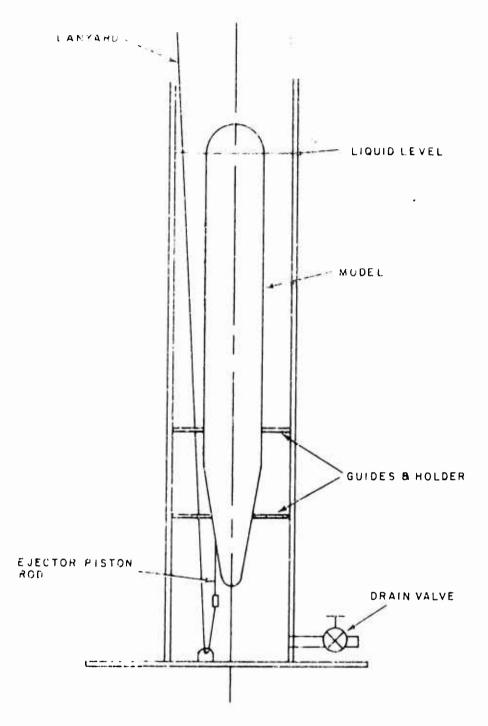


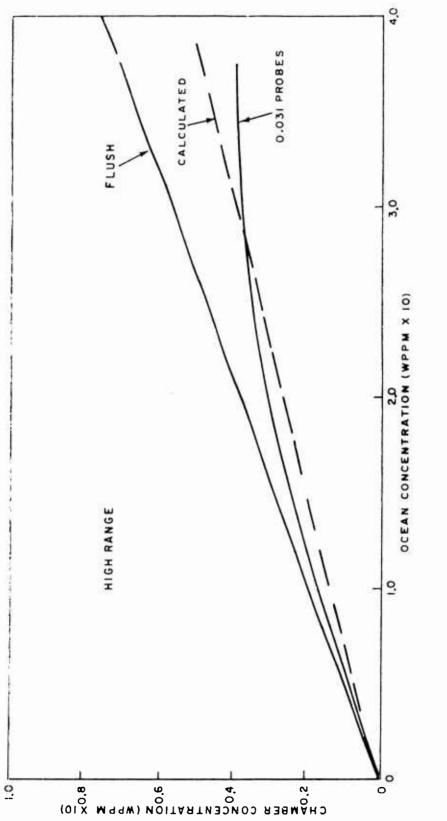
Figure 23. Assembly and calibration tank

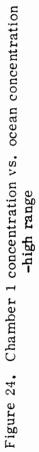
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procedure was similar for the probe case excepting that an uppermost row of probes was removed and then a bottom row to facilitate the liquid withdrawal. A minimum of four calibration tests were run at each concentration with the flush probes and also with the pitot probes. A least squares fit was performed on the data which are plotted for each sample chamber in Figures 24 through 31 for high and low chamber concentrations. Deviations of  $\pm 5\%$  were noted in the data. Several tests were performed with a 50 WPPM polymer solution in the tank with no significant change in the data.

## Stroking Time Verification

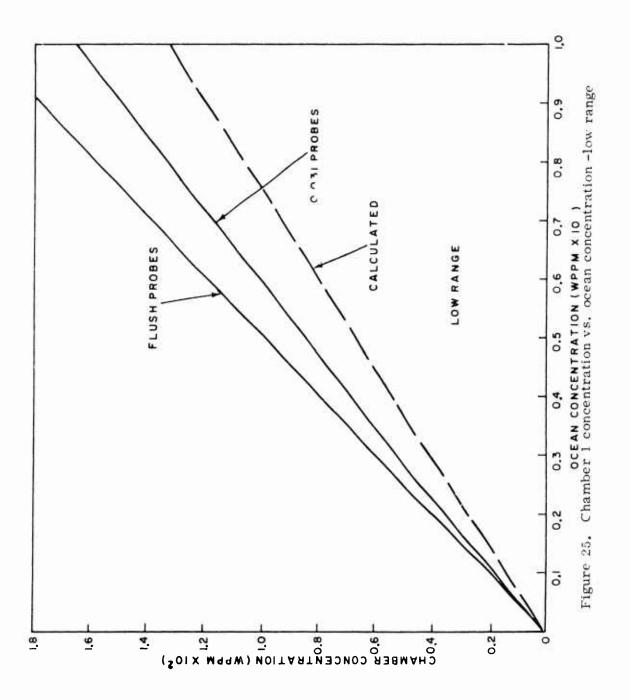
Verification of the stroking time was necessary to insure that the appropriate volume flow rates were being achieved. The facility shown schematically in Figure 32 was used for this purpose. To calibrate, the model was loaded with liquid and clamped to the bench. A calibration spacer was placed on the ejector follower and the rod clamped with a nylon shear screw to the facility firing arm. When fired by moving the firing arm in a counterclockwise direction and shearing the shear screw, the follower rod would move into the model following the ejector piston. The calibration spacer would interrupt the laser beam for the length of the spacer, starting the counters, discussed previously, giving a time over the known distance and the velocity of the rod. It was found, by test, that the velocity of the rod was approximately 5 times faster than the stroking time, therefore not influencing the results. A .5-inch long

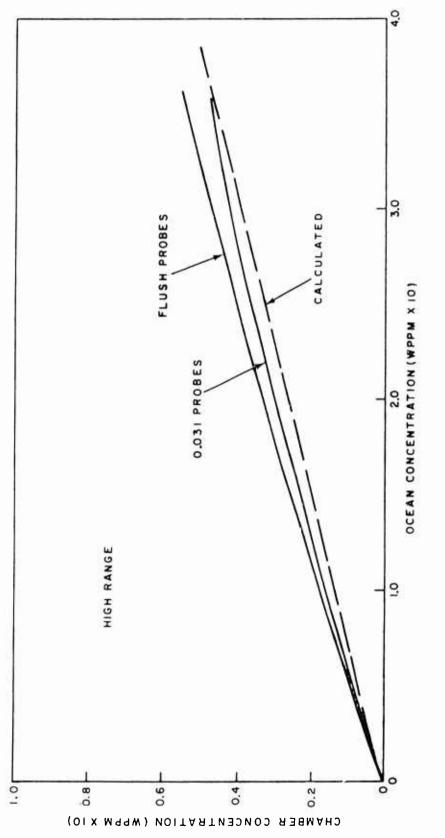




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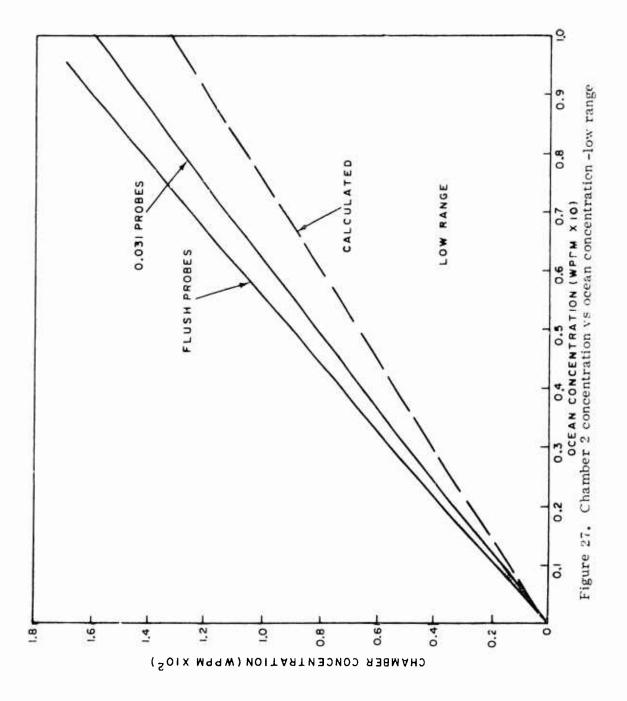
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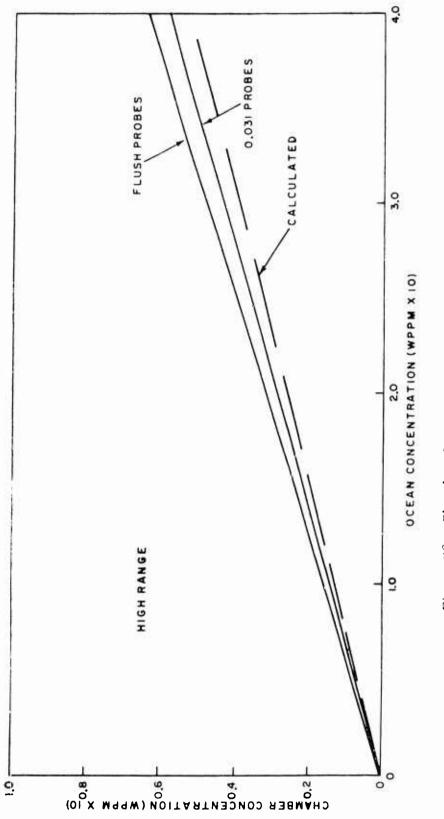




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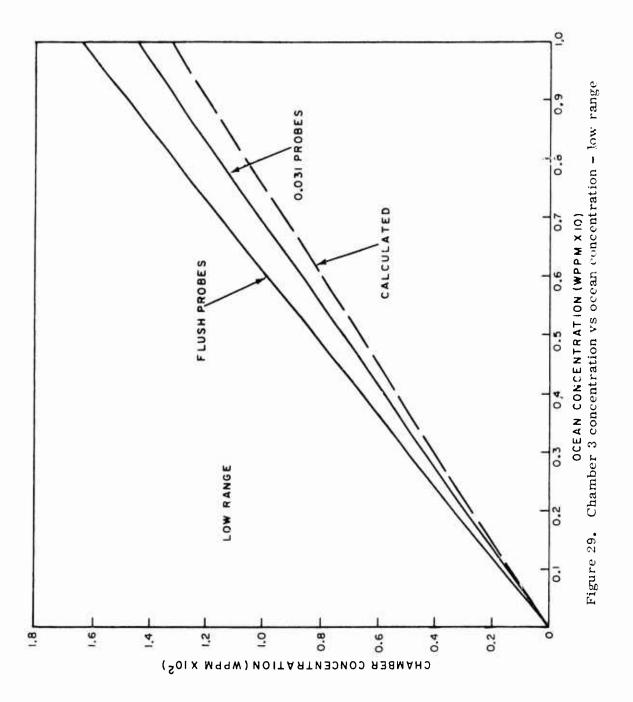


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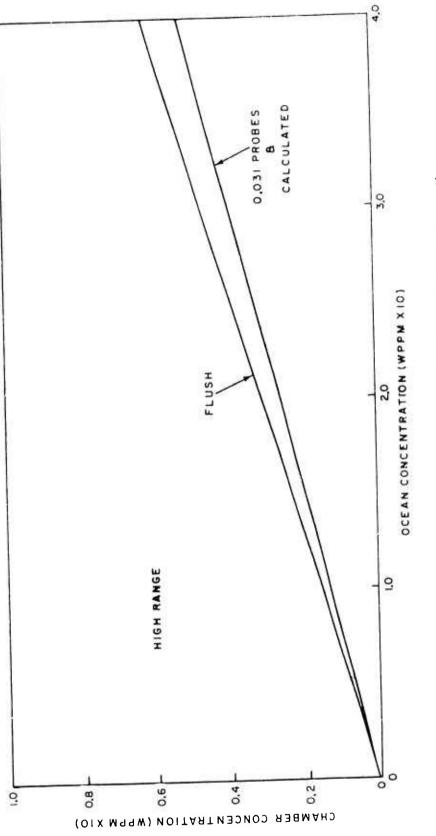


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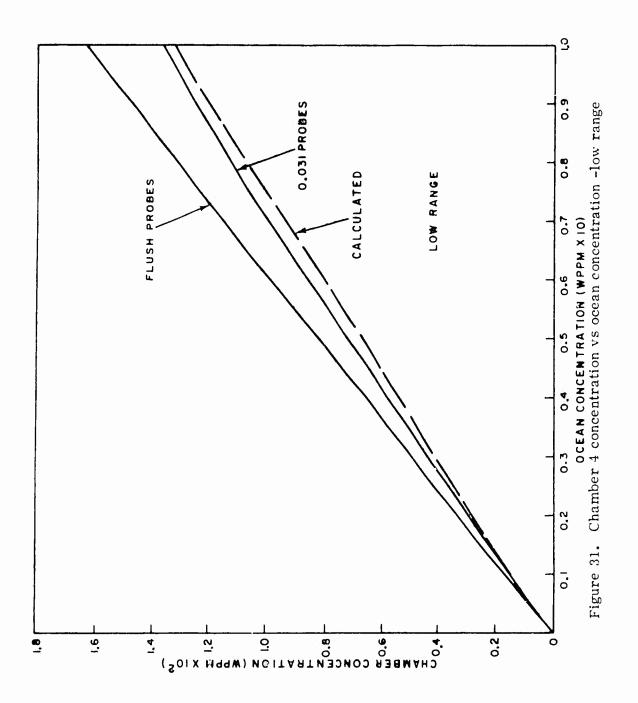




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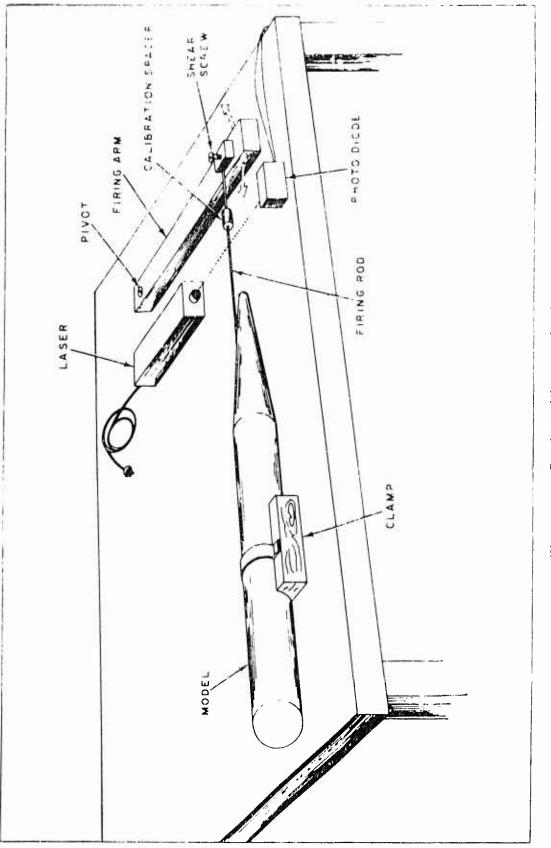


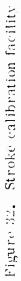


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calibration spacer was used in the test and placed at several positions on the follower rod to detect any acceleration of the rod. None was evident. Nineteen calibration runs were made. The stroke rate resulting was 12.1 in/sec  $\pm 6\%$  as compared to the calculated value of 11.7 in/sec.

## IV. ANALYTICAL CONSIDERATIONS

## Boundary Layer Model

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This section presents the analytical approach for the analysis of developing turbulent flow over an axisymmetric body for the cases of no polymer, polymer ocean and polymer injection. A model is developed for predicting growth of the boundary layer, diffusion of tracers within the boundary layer and prediction of skin friction coefficients and total drag.

From the literature review, the features of previous studies for turbulent flows can be summarized as follows:

- A modified law of the wall type velocity profile with pressure gradient terms was developed for the thick axisymmetric boundary layer case.
- Inner variable integral equations were developed for the thick axisymmetric boundary layer and verified for certain parameters.
- 3. Porous wall pipe flow studies with injection of polymers have suggested significantly reduced diffusion characteristics. This representing the ideal case of introducing polymers into the viscous sublayer.
- External flow studies demonstrate the importance of the ejection process on polymer efficiency.

- Far downstream dilution laws for polymer follow those for water diffusion.
- Similarity concentration profile relations have been established for the downstream case.
- 7. The extent of the initial mixing zone is considerably extended by nearly a factor of 20 with polymer flows. Most investigators have obtained data in far downstream conditions only.
- Data on concentration profiles on axisymmetric bodies are desirable to extend and/or verify dilution laws presently available.

In the analysis that follows, the velocity profile, continuity equation, momentum equation, a Lagrangian similarity hypothesis for the turbulent diffusion boundary layer growth, and a conservation of polymer equations for the intermediate and final zones of diffusion are combined to yield expressions for the growth of the turbulent boundary layer with poly er ejection. Additionally, terms are added to predict the initial zone region where molecular diffusion predominates for an optional ejection process. An alternate analytical model is postulated which would eliminate the need for the concept of an initial, intermediate and final zone concept.

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## Velocity Profile Relation

Equation (32) provided a relation for the law of the wall accounting for pressure gradients. Rewriting equation (32) accounting for the Meyer (1966) correction for polymers,  $\Delta B$ , yields:

$$u^{+} = \frac{1}{K} \int_{0.1108}^{Y^{+}} \frac{1}{Y^{+}} \left[ 1 - \frac{\alpha}{2} r_{0}^{+} \left( 1 - e^{2Y^{+}/r_{0}^{+}} \right)^{1/2} dY^{+} + \Delta B \right]$$
(87)

An alternate method for accounting of the polymer effect would be by adjustment of the mixing length constant, K. As noted by Virk (1971), a change in K by a factor of 5 is possible and in full agreement with data. This would only apply for the case of maximum drag reduction along the ultimate asymptote line, however. <u>Skin Friction Relations</u>

The boundary layer continuity and momentum equations, equations (33) and (34), for turbulent axisymmetric flow

$$\frac{\partial}{\partial \mathbf{x}} (\rho \mathbf{u} \mathbf{r}) + \frac{\partial}{\partial \gamma} (\rho \mathbf{v} \mathbf{r}) = 0$$
(33)

and

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$$\rho \, u \, r \, \left(\frac{\partial u}{\partial x}\right) \, + \, \rho \, v \, r \, \left(\frac{\partial u}{\partial y}\right) \, = \, - \, r \, \left(\frac{d p_e}{d x}\right) \, + \, \frac{\partial}{\partial_y}(r\tau) \tag{34}$$

are applied to the polymer flow case studied here. The x derivatives must be handled by the chain rule, since each of the parameters  $(Y^+, \alpha, r_0^+, C_w)$  in the law of the wall is a function of x. Thus, we substitute

$$\frac{\partial}{\partial x} = \frac{\partial Y^{+}}{\partial x} \frac{\partial}{\partial Y^{+}} + \frac{\partial \alpha}{\partial x} \frac{\partial}{\partial \alpha} + \frac{\partial r_{0}^{+}}{\partial x} \frac{\partial}{\partial r_{+}^{+}} + \frac{\partial C_{w}}{\partial x} \frac{\partial C_{w}}{\partial C_{w}}$$
(88)

As may be noted in (88), concentration derivatives are added. It is assumed throughout that  $\rho_{\rm W}$  and  $\mu_{\rm W}$  are constant in this analysis.

The resulting boundary layer equation, after considerable algebraic manipulation is:

$$\frac{d\lambda}{dx^{\star}} (3 \alpha H - G_{1}) + \frac{v'}{v} \lambda G_{1} - \frac{\lambda^{2}r_{o}^{+}}{2} (e^{2Y_{e}^{+}/r_{o}^{+}} 1)$$

$$+ \frac{\lambda^{4}}{R_{L}} (\frac{1}{v})'' H = - R_{L}v - \lambda \frac{dr_{o}^{+}}{dx^{\star}} I - \lambda \frac{dc_{w}}{dx^{\star}} J$$
(89)

where G, H, I, J are given in the appendix.

The prime difference between equations (89) and (35), for the polymer case, is the last term accounting for the change of concentration with x.

Appendix A presents a complete development of the equation related to this method.

Prior to solution of equations (87) and (89), it is necessary to determine a means of calculating  $C_w$ . Test (1974) applied techniques developed by Lessmann (1970), and Fabula and Burns (1970) to provide a solution for  $C_w$ . This technique satisfied the case of final zone of mixing but did not account for the development of a diffusion boundary layer in a similar tashion to the development of a hydrodynamic boundary layer. Nevertheless, the results of the work are significant. With the application of the hypothesis suggested by Batchelor (1957), describing the development of the diffusion boundary layer and data by Poreh and Cermak (1964) and Poreh and Hsu (1971), empirical relations are developed which provide the values  $C_w$  necessary to determine the friction coefficients for the intermediate and final zone.

For the case of no polymer present, equations (87) and (89) may be solved setting all terms containing  $C_w$  equal to zero. It is only necessary, as pointed out in White (1972), to assume an initial  $\lambda_0$  and prescribe the flow condition ( $U_e$ ,  $r_0$ ) as a function of x. Additionally, for the case of operation in a polymer ocean, that is  $C_w$  is everywhere constant, all derivatives of  $C_w$  and with respect to  $C_w$  are set equal to zero and again a solution can be obtained as for the case of  $C_w$  equal to zero but instead inserting a constant value of  $C_w$  into equation (87).

Many of the previous investigators have neglected the contribution of the initial zone in the process of diffusion and resulted in good agreement with data. The suggestion being that the diffusing process with polymers is similar to that with water. This is true in the intermediate and final region of the diffusion process where molecular diffusion is not the controlling factor. Experimental methods and apparatus used significantly control the results. For the external flow case studied here, ejection in a laminar

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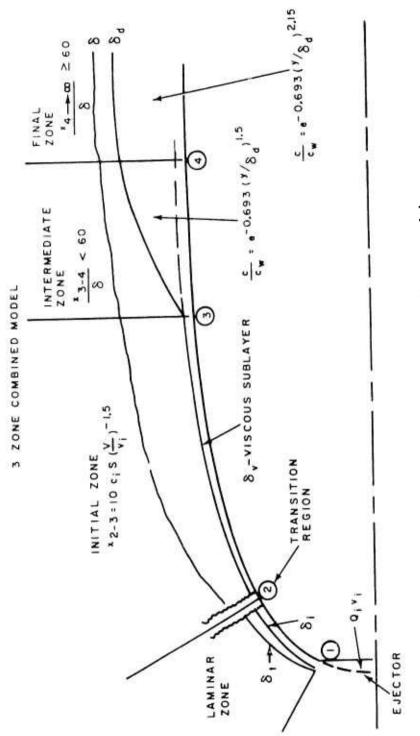
flow region prior to transition to turbulent flow may significantly influence the process. Data by Walters and Wells (1971) and Fruman and Tulin (1974) suggest the initial zone becomes very large. It is hypothesized, here, that by injection prior to transition, the turbulence intensity levels are extremely subdued resulting in elimination of the high level mixing process associated with the turbulent eddies penetrating the viscous sublayer. When injecting into established flows, as performed by many investigators, the dampening of the turbulent intensity does occur, but not before the polymer is dispersed at a rather normal diffusion rate consistent with other fluids (water). This results in low wall concentration, rather quickly, and therefore low drag reduction efficiency. The sections that follow describe an analytical model which includes an initial zone. Figure 33 schematically describes the model.

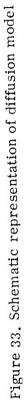
Considering first the initial zone where molecular diffusion is presumed to predominate, an approximation to the concentration entering the turbulent transition zone is made. Writing a simplified polymer conservation relation:

$$Q_1 C_1 = (Q_t + Q_2) C_t$$
 (90)

where  $Q_t$  and  $C_t$  are the flow rate and concentration at the transition point, respectively, and  $Q_2$  is an initial condition correction factor. The volume flow rate  $Q_t$  is given by the mean local laminar flow velocity, .6U<sub>e</sub>, at the transition position radius  $r_{ot}$  and a

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laminar layer thickness,  $\delta_t$ , determined from equation (78)

$$Q_{t} = .6U_{e} 2\pi r_{o} \delta_{t}. \tag{91}$$

The initial condition to the laminar flow boundary layer must be applied if the ejected volume of fluid exceeds the fluid in the laminar boundary layer at the periphery of the ejector. In equation form

$$Q_1 - Q_e = Q_2$$

where  $Q_e$  is the volume flux through the laminar thickness calculated at the ejector periphery in a similar fashion to equation (91), and  $Q_2$  is the volume flux difference which provides an "initial condition" and must be added to the boundary thickness at each station. The assumption is made that the polymer solution is uniformly mixed within this laminar layer. The local concentration at the transition point is then determined from (90). The volume flow rate into the viscous sublayer is determined by simple ratio of the thickness of the viscous sublayer height to the laminar layer height at transition.

$$Q_v = (Q_t + Q_2) \frac{\delta_v}{\delta_t} .$$
(92)

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Approximating in this manner would tend to overpredict the flow into the viscous sublayer while underpredicting the flow in the region above the sublayer. The flow rate into the viscous region,  $Q_v$ , and the concentration,  $Q_t$ , are the parameters applied to the drag reduction and boundary layer calculations. This approxima-

mation allows for an excess quantity of fluid being introduced above the viscous sublayer. The portion of flow injected into the intermediate layer of the turbulent flow is given by

$$(Q_{t} + Q_{2}) - Q_{v} = Q_{3}.$$
(93)

This fluid will undergo a rapid diffusion characteristic of intermediate and far downstream diffusion as discussed earlier. The concentration of polymer at the transition point is as given previously,  $C_t = \frac{Q_i C_i}{Q_t + Q_2}$ .

Considering equation (59), the relation for this diffusion process is given by

$$Q_{3}C_{t} = 2\pi (r_{0} + y_{v}) C_{t} \int_{y_{11}}^{\infty} u \frac{C}{C_{t}} (1 + \frac{y}{r_{0} + y_{v}}) dy$$
 (94)

where, for the assumption of uniform concentration in the sublayer,  $C_t = C_w$  on the right side of (94). For  $y_v << r_o$  equation (94) becomes

$$Q_{3}C_{t} = 2\pi r_{0} C_{w} \int_{0}^{\infty} u \frac{C}{C_{w}} (1 + \frac{y}{r_{0}}) dy.$$
 (95)

Equation (95) may be integrated across the boundary layer at each x station resulting in a measure of the concentration profile above the viscous sublayer. It is suggested that this relation, (95), be solved as described in subsequent sections, as an independent solution to the two-zone diffusion process with flow and concentration inputs of  $Q_3$  and  $C_t$ , respectively, but other boundary layer

and polymer wall concentration parameters governed by the basic initial zone calculations. This will avoid additional computer programming complexity. This calculation is only required if a measure of boundary layer concentration at particular heights in the boundary layer is desired. The extent of the initial zone has yet to be determined. Fruman and Tulin (1974) postulate a model for prediction of the extent of the initial zone for flat plates, based on an analogy to heat transfer. They show, for a near optimal ejection process, that the initial zone terminates for values of dimensionless distance greater than 8. The dimensionless distance used to correlate these data is:

$$\left[\left(\frac{U_{o}}{v_{i}}\right)^{1.5} \frac{x}{s} \frac{1}{C_{i}}\right]$$
(96)

where s is the slot width. For the axisymmetric case with nose ejection, an effective slot width may be defined as the ejection orifice area divided by the ejection circumference. For the model being applied in this study, the effective slot width is .07837 inches and  $C_i$  is replaced with  $C_t$ . No correction will be made to this relation for application to the axisymmetric case pending results of the test program. It should be reiterated that the initial zone length will normally be very small for dilute solutions of polymer as would occur if ejection were initiated in a highly turbulent region. For this type of ejection process, an intermediate and final zone model would be quite adequate. Upon leaving the initial zone, relations for the prediction of wall concentration are required. Application of the Lagragian similarity hypothesis and the concentration similarity profiles discussed earlier coupled with the axisymmetric boundary layer relations and velocity profile provide the necessary relations.

A relation for solution of  $C_w$  in the highly turbulent flow field may be extracted by application of equations (57), (58) and (59)

$$Q_{i}C_{i} = 2\pi r_{o} C_{w} \int_{0}^{\infty} u \frac{\overline{C}}{C_{w}} (1 + \frac{y}{r_{o}}) dy \qquad (97)$$

where, for the case of polymer flows with an initial zone,  $Q_i C_i$ would be replaced with  $Q_v C_t$ . Changing to law of wall variables and dropping the overbars since we are dealing with average values throughout the turbulent flow field analysis

$$Q_{i}C_{i} = 2\pi r_{o} \vee C_{w} \int_{0}^{Y_{e}^{+}} u^{+} \frac{C}{C_{w}} e^{2Y^{+}/r_{o}^{+}} dY^{+}.$$
(98)

Solving for C<sub>w</sub>

$$C_{w} = \frac{Q_{1}C_{1}}{\begin{array}{c} Y^{+} & 2Y^{+}/r_{o}^{+} \\ 2\pi r_{o} & v & \int_{0}^{e} u^{+} \frac{C}{C_{w}} & dY^{+} \end{array}}$$
(99)

Equation (99) for polymer concentration is analogous to equation (34) for momentum. It is necessary to define a relation for C to solve equation (99) as it was necessary to develop an expression for u to solve equation (34). The similarity relations given by equations (57) and (58) provide the needed concentration expressions

$$C/C_{w} = e^{-0.693} (y/\delta_d)^{1.5}$$
 Intermediate Zone (57)

and

$$C/C_{w} = e^{-0.693} (y/\delta_{d})^{2.15}$$
 Final Zone. (58)

Within the final zone, for zero pressure gradient flows,  $\delta_d/Y_e$ remains constant at 0.64. If there is a pressure gradient, data by Mellor (1966) indicate that the value of  $\delta_d/Y_e$  changes to .53 in this zone.

The expression for the growth of the diffusion boundary layer,  $\delta_d$ , equation (55), completes the analysis

$$a_1 \frac{d\delta_d}{dx} = \frac{b v^*}{u(\overline{Y})}.$$
 (55)

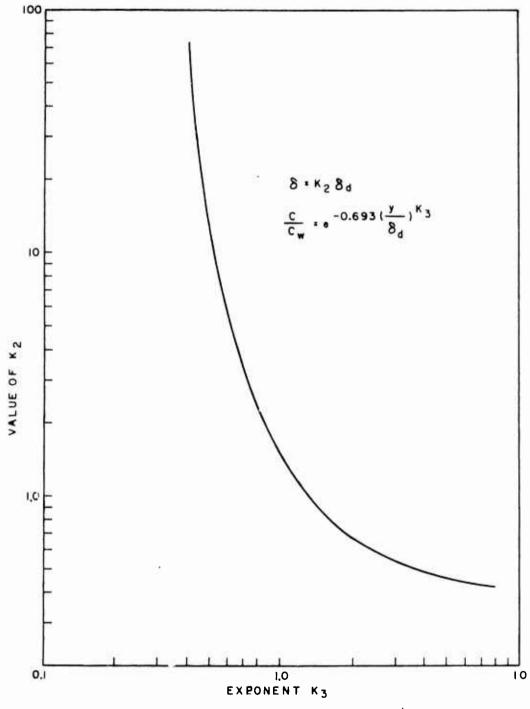
It is only necessary to determine the constant,  $a_1$ , in equation (55). Applying equation (48), changing variables and inserting a similarity concentration profile with variable exponent

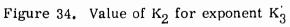
$$\overline{Y} = \frac{\int_{0}^{\infty} \int_{0}^{-0.693(y/\delta_{d})K3} y/\delta_{d} d(y/\delta_{d})}{\int_{0}^{\infty} C_{w} e^{-0.693(y/\delta_{d})K3} d(y/\delta_{d})}$$
(100)

which results in

$$Y = K_2 \delta_d = a_1 \delta_d. \tag{101}$$

Numerically integrating (100) for various values of  $K_3$  between .5 and 5 yields values of  $K_2$  which may be applied to (101) Figure 34 displays the results. Substituting (101) into (55)





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yields a relation for  $\boldsymbol{\delta}_d$ 

$$K_2 \frac{d\delta_d}{dx_g} = K \frac{v*}{u_1}$$
(102)

where  $u_1$  is the value of u at  $K_2\delta$  and  $x_s$ , and K is the Karman constant. Virk (1971) has shown that the constant, K, used in the law of the wall varies with polymer addition resulting in an ultimate asymptote for the velocity profile in drag reduction cases. An effective value of Karman's constant may be determined. This new "constant," which is a function of  $\Delta B$ , will be called K<sub>5</sub>. The manner in which the modification of K to K<sub>5</sub> is determined relates to the basic equations for the velocity profiles with and without polymers, equation (87) and (32), respectively. Equating these equations

$$\frac{1}{K} \int_{0}^{Y_{e}^{+}} \frac{1}{Y_{e}^{+}} \left[ 1 - \frac{\alpha}{2} r_{o}^{+} (1 - e^{2Y_{e}^{+}/r_{o}^{+}}) \right]^{1/2} + \Delta B =$$

$$\frac{1}{K_{5}} \int_{0}^{Y_{e}^{+}} \frac{1}{Y_{e}^{+}} \left[ 1 - \frac{\alpha}{2} r_{o}^{+} (1 - e^{2Y_{e}^{+}/r_{o}^{+}}) \right]^{1/2} dY^{+}.$$
(103)

Solving for K<sub>5</sub> yields

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$$K_{5} = \frac{Y_{e}^{+} \frac{1}{Y^{+}} \left[1 - \frac{\alpha}{2} r_{o}^{+} (1 - e^{2Y^{+}/r_{o}^{+}})\right]^{1/2} dY^{+}}{\frac{1}{K} \int_{0}^{Y^{+}} \frac{1}{Y^{+}} \left[1 - \frac{\alpha}{2} r_{o}^{-} (1 - e^{2Y^{+}/r_{o}^{+}})\right]^{1/2} dY^{+} + \Delta B}$$
(104)

The effect is apparent.  $K_5$  is reduced dependent on the value of  $\triangle B$ . In effect, reduction of the eddy viscosity through the mixing length is occurring. Depending on the value of u<sup>+</sup> and  $\triangle B$  chosen,  $K_5$ values approaching those of Virk's (1971) ultimate asymptote can be achieved. The effect of this change in K to some smaller value  $K_5 = f(\triangle B)$  is to lengthen the intermediate mixing zone.

Equations (102), and (57) or (58) provide relation for the solution of  $C/C_w$  which, in turn, may be substituted into (99) yielding an expression for  $C_w$ . Equations (87) and (89), the boundary layer velocity profile and momentum equations, respectively, may then be solved. These relations apply for the intermediate and final zones of the diffusion process. Within the initial zone, equations (90) and (92) define the polymer wall concentration and flow, respectively. The equations for the intermediate and final zone are summarized below:

$$K_2 \frac{d\delta_d}{dx_s} = K_5 \frac{v^*}{u_1}$$
(102)

$$\frac{C}{C_{w}} = e^{-0.693(Y/\delta_{d})^{2.15}}$$
 For  $x_{s}/Y_{e} > 60$  (58)

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$$\frac{C}{C_{w}} = e^{-0.693(Y/\delta_{d})^{1.5}}$$
 For  $x_{s}/Y_{e} < 60$  (57)

$$C_{w} = \frac{Q_{1}C_{1}}{2\pi r_{o} \vee \int_{0}^{Y^{+}} u^{+} \frac{C}{C_{w}} e^{2Y^{+}/r_{o}^{+}} dY^{+}}$$
(99)  
$$u^{+} = \frac{1}{K} \int_{0.1108}^{Y^{+}} \frac{1}{Y^{+}} \left[1 - \frac{\alpha}{2} r_{o}^{+} (1 - e^{2Y^{+}/r_{o}^{+}})\right]^{1/2} dY^{+} + \Delta B (87)$$
$$\frac{d\lambda}{dx^{*}} (3 \alpha H - G_{1}) + \frac{V}{V} \lambda G_{1} - \frac{\lambda^{2}r_{o}^{+}}{2} (e^{2Y^{+}_{e}/r_{o}^{+}} - 1)$$
(89)

$$+ \frac{\lambda^4}{R_{\rm L}} \left(\frac{1}{4}\right)^{\prime\prime} H = - R_{\rm L} V - \lambda \frac{dr_{\rm O}^+}{dx^*} I - \lambda \frac{dC_{\rm W}}{dx^*} J$$

where the terms are as defined previously.

An alternate approach may be applied to attack the problem for developing flow. It is assumed the similarity expression for the concentration profile holds throughout the boundary layer. Lacking data for the effect of turbulence intensity changes in developing flow with polymer ejection, it is hypothesized that the similarity relation is functionally related to the boundary layer thickness,  $\delta$ , the diffusion boundary layer thickness,  $\delta_d$ , the Karman constant, K, and a distance from the inception of turbulence to the ejection slot,  $x_e$ , (set equal to 1 for cases of the ejection being at the transition to turbulent flow point or before). The exponent in the similarity expression is the controlling parameter since it indicates the diffusion rate. The expression for the similarity profile may be written as

$$\frac{C}{C_{w}} = e^{-0.693} (Y/\delta_{d})^{K3}$$
(105)

where  $K_3 = f(\delta, \delta_d, K, x_e)$ .

Porch and Cermak (1964), as discussed, have empirically assigned specific zones relating downstream distance and the boundary layer thickness to establish the exponent value. It seems apparent, that in the intermediate zone, the value  $r\bar{t}$  the exponent should not be constant. Concentration profiles as a function of downstream distance by Walters and Wells (1971) bear this out. Rewritting (105) in terms of K<sub>5</sub>

$$K_3 = f(\delta, \delta_d, K_5, x_e).$$
 (106)

Assuming a nondimensional relationship which allows the exponent to grow as the diffusion boundary layer grows results in

$$K_3 = C K_5 \frac{\delta_d}{\delta} \frac{\mathbf{x}_e}{L} .$$
 (107)

For final zone of diffusion where the characteristic diffusion rates of polymer and water have been shown to be the same,

> $K_5 = K = .4$   $\frac{\delta_d}{\delta} = .64$  for zero pressure gradient flows  $\frac{x_e}{L} = 1$  since ejection preceeds the turbulent transition point and  $K_3 = 2.15$ .

Solving for C in (107) yields

$$C = 8.4$$
 (108)

From which (107) is defined as

$$K_3 = 8.4 K_5 \frac{\delta_d}{\delta}$$
 (109)

For developing polymer flows with the ejector at or preceeding the point of transition to turbulent flow (using the test model described earlier),

$$K_5 = .2$$
  
 $\delta_d = .0008$  ft (for the model flow rates)  
 $\delta = .003$  ft (equation (80))

the value of  $K_3$  becomes

and

 $K_3 = .45$ 

and the value of the moment,  $K_2$ , may be determined from Figure 34. The constant  $K_3 = .45$  implies an extremely suppressed diffusion process, which in fact, on computation, occurs. Application of (105) with the Lagrangian similarity hypothesis for predicting the diffusion boundary layer growth would eliminate the need for a multi-zone. The exponent,  $K_3$ , would be self-adjusting throughout the boundary layer. The simple form chosen for  $K_3$  may be incorrect. Sufficient data would be required in all diffusing zones to properly define whether the similarity profile extends to the boundary layer and to define the proper functional form. Application of this method would require integration of equation (100) rather than use of Figure 34. This is required since equation (100), although

integrated between 0 and  $\infty$  in reality reaches final values for values nearer 4 or 5. For cases where  $\delta_d$  may be small, as for much reduced diffusion, the value may become quite large and should be bounded by the viscous sublayer thickness, for  $\delta_{d_{\min}}$ , and the boundary layer, thickness for  $\delta_{\max}$ . This will prevent the moment, K<sub>2</sub>, from becoming very large for low values of K<sub>3</sub> as implied by Figure 34. Extensive effort in pursuing this approach was not expended since the molecular diffusion coupled with the two zone model is believed to represent a sounder approach.

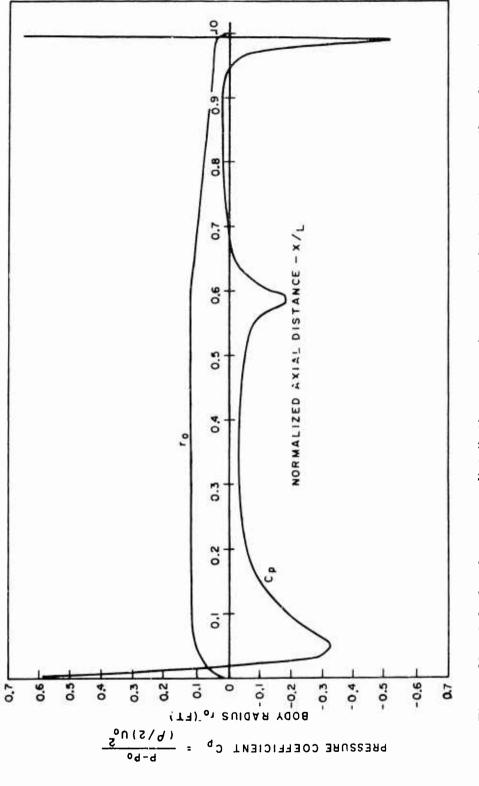
The equations may be solved for the skin friction distribution  $C_f(x)$ , the boundary layer thickness,  $\delta$ , and the diffusion boundary layer thickness,  $\delta_d$ . Additionally, the concentration at the wall,  $C_w$ , and at any position in the boundary layer, C, for a given polymer or tracer flow and ejection concentration and ejection rate can be determined. The initial conditions required are an estimation of  $\lambda_0$ , and the known flow condition  $U_e$  and  $r_o$ as functions of x. Inputs of velocity, temperature and related parameters, ejection rate and polymer concentration are required. It has been assumed that the flow becomes turbulent at the minimum pressure point and all initial conditions are determined at this point. From these input conditions,  $\delta_{do}$  may be determined from a mass balance at  $r_o(x)$  and  $\delta_o$  may be calculated from (80).  $\Delta B_o$  may be calculated from (42). An estimate for the skin friction term  $\lambda_0$  comes from the flat plate relation.

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$$C_{f} = 0.0592 R_{e_{x}}^{-1/5} = \frac{2}{\lambda^{2}}$$
 (110)

Figures 35, 36 and 37 present the pressure coefficients vs normalized axial distance for the three bodies discussed earlier. The pressure coefficients and other flow conditions,  $U_{\rm p}/U_{\rm o}$ , have been determined using the Douglas-Neumann Potential Flow Program (1958) and are required for solving the previous system of equations. The total drag on the body has been determined by integrating the calculated skin friction and by integrating the pressure distribution over the body to the point of separation. As pointed out by White (1972), equation (89) provides a distinct test for separation when the coefficient (3 $\alpha$ H-G<sub>1</sub>) vanishes which causes  $\lambda$  to approach  $\infty$  and Cf approaches 0. At this point, the pressure is determined and multiplied by the projected area at the radius,  $r_o(x)$  of separation. Thus, both friction and form drag are accounted for. The form drag calculated in this manner may exhibit large errors due to the steepness of the calculated pressure coefficient in the tail region as seen in Figures 36 through 37. Data on pressure coefficients for similar bodies, Nadolink (1968), do not exhibit this steepness. The calculation is simple, however, and does provide an indication of the total drag.

The equations have been programmed on a Control Data Corporation Computer, CDC 3300. All numerical integrations use the standard RUNGE-KUTTA subroutine. Appendix B contains a sample of the computer program and solution for the combined model. A difficulty does occur in the formulation when a favorable pressure is encountered

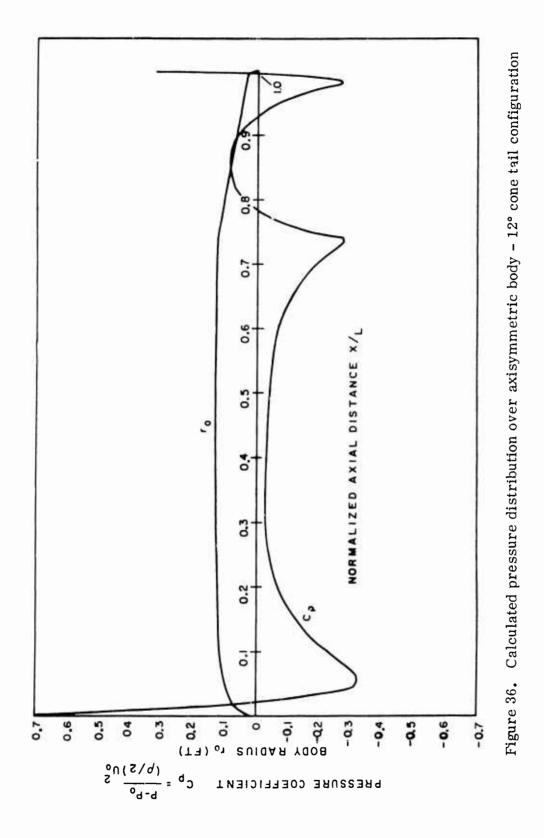


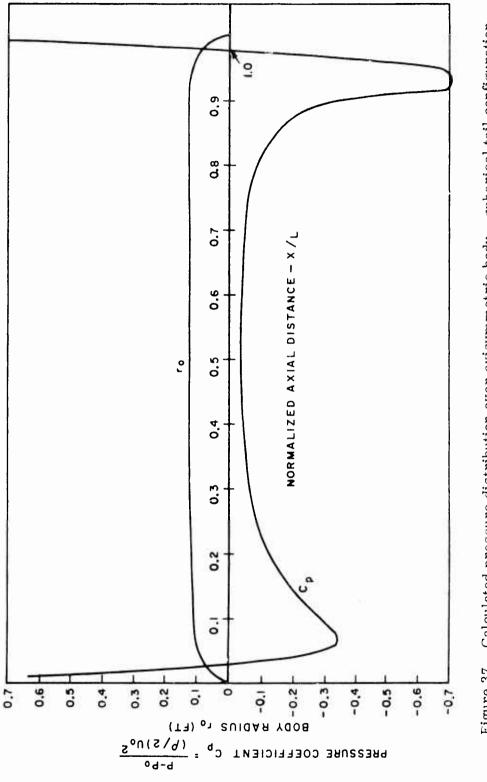


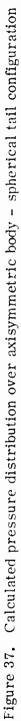
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(negative  $\infty$ ). Equation (89) diverges resulting in no solution. The problem is resolved by not allowing  $\alpha$  to become negative. This does introduce a discontinuity into the solution but recovery from the discontinuity is rapid. Two methods of solution are possible for the determination of  $\lambda$  in equation (89). The full equation may be used, which for small polymer wall concentration gradients  $\frac{dC_w}{dx}$ , provides for stable solution. For higher concentration gradients, an alternate approach is recommended. A solution for  $\lambda$  may be obtained neglecting the last term in equation (89). The value of  $\lambda$  is then corrected at each calculation interval as noted below:

$$\lambda = \lambda_{calculated} - (\Delta B_{o} - \Delta B)$$
(111)

where  $\Delta B_0$  is the previous calculated value of  $\Delta B$ . In this manner, the new calculated value of  $\lambda$  is corrected for an updated  $\Delta B$ resulting in the appropriate  $\lambda$ . The full equation (89) does provide a solution at the higher concentration gradients but the solution tends to become oscillatory requiring a large number of calculation points to minimize the oscillations.

The analytical model has been exercised in several different ways to test the results that may be obtained. For purposes of ease in discussing these models, they will be given specific names. First, the <u>molecular diffusion model</u> only contains the molecular diffusion portion of the analytical program and never switches to a higher diffusion two-zone model. The second model is called

the <u>two zone model</u>, the initial zone is very small and not included. This model is applicable to water diffusion or to polymer diffusion if the ejector were placed in an established turbulent flow. The third model will be called the <u>combined model</u> and represents the near optimal external flow process for polymer ejection, ejecting into the laminar region prior to turbulent flow transition. The postulated model, with variable K<sub>3</sub> is tested, in a single case, for comparison. The total model is shown schematically in Figure 33.

The calculations were all made using the  $6^{\circ}$  tail model, a velocity of 27 ft/sec, an ejection rate of 20.6 in<sup>3</sup>/sec, unless otherwise noted, and a medium temperature of  $60^{\circ}$ F. The length Reynolds number is 4.5 x  $10^{6}$ . The primary emphasis in these calculations has been on the concentration profiles and, more specifically, wall concentration profile. It should be remembered, however, that the computer routine and analytical model allow determination of concentration throughout the boundary layer, the growth of the diffusion boundary layer within the hydrodynamic boundary layer and other boundary layer parameters. Skin friction and total drag is also determined and a comparison of the drag reduction resulting from the different diffusion processes as the three models (really one applied differently excepting the variable K<sub>3</sub> model) predict are compared in Table 4.

Figure 38 displays polymer wall concentration ratios vs axial distance calculated using the molecular diffusion model and the two-zone model. For comparison purposes in the drag reduction calculations, the water case for the two zone model is considered to be the baseline. This model, for water, is accurate as will be shown in subsequent sections. The molecular diffusion model presents the optimal case for drag reduction on external flows. The viscous sublayer growth is rather small over the body length, a growth of less than .001 inches over the x/L distance displayed, resulting in the flat concentration profile. The prime reason for the reduced concentration to that ejected is due to the diameter ratio from the ejection diameter to the near maximum body diameter. Since, for molecular diffusion, the concentration at the wall does not change appreciably, the single line shown applies to all polymer concentration so long as  $\gamma$  equals 11.5. For values of polymer concentration less than 50 WPPM,  $\Delta B$  in the model would change resulting in a wall concentration variation. For this case, only v\* affects the calculations. The two zone model for 50 and 500 WPPM shows rapid dispersion of the polymer resulting in less than 1/10 the ejected concentration at about 1/2 the body length. This type of diffusion process would predict high polymer concentration or ejection rates required for reasonable drag reduction. The model would be reasonably accurate for long bodies where the initial zone is small compared to the body length.

The effect of concentration is evident with a maximum wall concentration, over the portion of the body shown exceeding that required for maximum drag reduction for ejected concentration above approximately 200 WPPM. The model, as implemented, does not include changes in viscosity for high polymer concentrations. The effects must be accounted for if large concentrations are applied.

Figure 39 displays the two-zone model compared to a data adjusted model based on data generated in the test program. Essentially, the two-zone model is reduced to a single zone model with the exponent value in the similarity expression (58) being that determined from the experimental data, .75. The effect of suppressed diffusion is apparent with concentration levels being much higher. Care must be taken in interpreting this figure, as will be discussed in the experimental section where the data is qualified. For the moment, the effect of a change in the exponent is the important factor shown here.

Figure 40 displays the variable K3 model predicting very low diffusion and therefore high wall concentrations as compared to the two-zone model. The results are interesting warranting further development of the functional form of the K3 function (106).

Figure 41 displays the results from the combined model compared to the two-zone model. The transition from the molecular model to the two-zone model is clearly evident as controlled by the effect of concentration on the initial zone length in equation

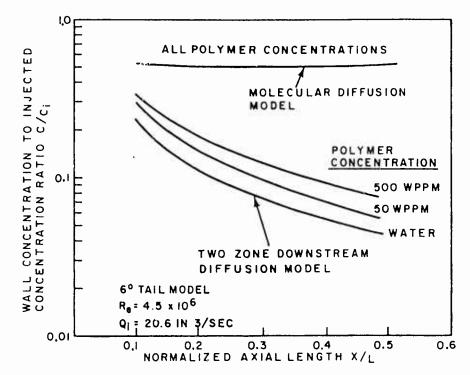
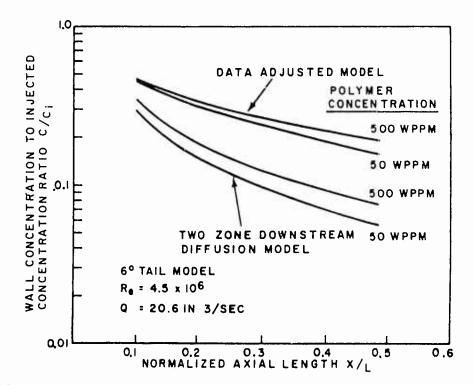


Figure 38. Comparison of predictions of wall concentration ratio of two-zone downstream diffusion model with molecular diffusion model



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Figure 39. Comparison of predictions of wall concentration ratio of two-zone downstream diffusion model and experimental data adjusted model

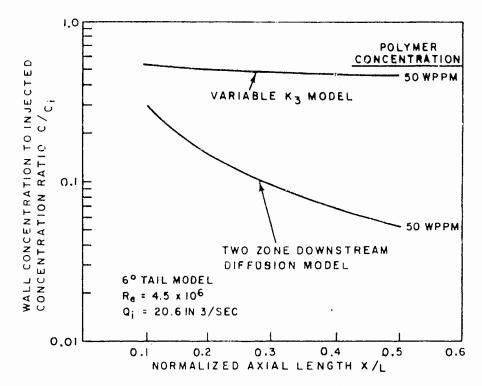
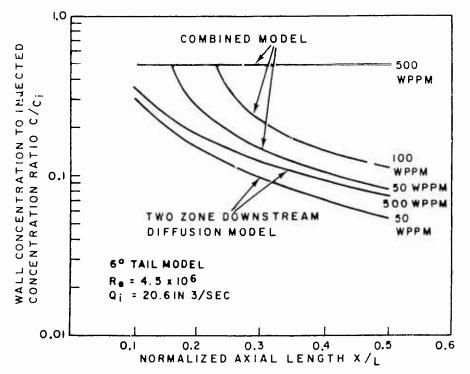


Figure 40. Comparison of predictions of wall concentration ratio of two-zone downstream diffusion model and variable K3 model



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Figure 41. Comparison of predictions of wall concentration ratio of two-vone downstream diffusion model and combined model

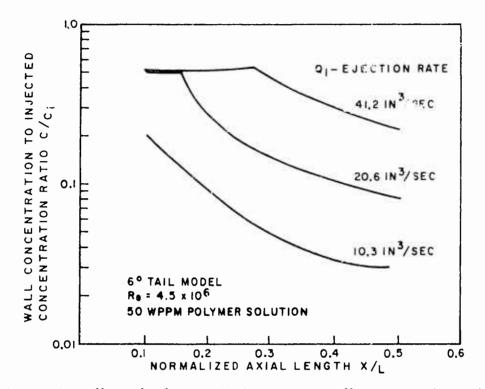
(96) and data from Fruman and Tulin (1974). This model should adequately predict the polymer diffusion process for the initial, intermediate, and final zone of diffusion subject only to verification of the abrupt transition from the initial to intermediate zone similarity profile. Quite possibly a more gradual transition, as suggested by the variable K3 model, would be appropriate. Figure 42 displays the effect of the ejection rate, for a fixed 50 WPPM polymer concentration, on the wall concentration ratio. The shift in the transition from the initial zone to the intermediate zone is apparent and governed by the changed ejection velocity in equation (96). Figure 43 taken from Fruman and Tulin (1974) displays wall concentration data calculated from the combined model plotted against the reduced dimensionless distance, equation (96). As may be seen, the combined model, applying the Lagrangian similarity hypothesis, results in good agreement with data obtained by Tulin.

The percent total drag reduction and percent skin friction reduction have been calculated for the cases discussed using the relations

% TDR = 100 
$$(1 - \frac{D_{POLY}}{D_w})$$
 (112)

and

% SFR = 100 (1 - 
$$\frac{SD_{POLY}}{SD_{w}}$$
) (113)



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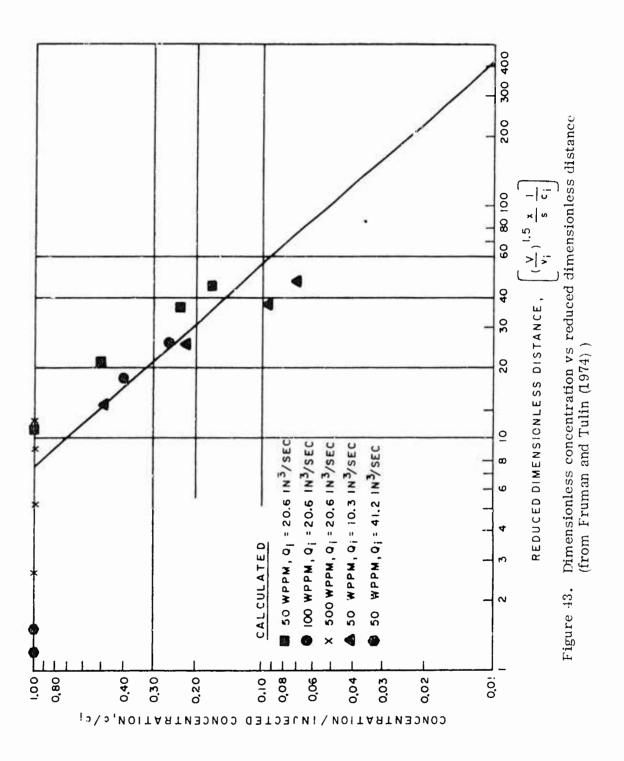
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Figure 42. Effect of polymer ejection rate on wall concentration ratio - combined model - 50 WPPM polymer concentration

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where

 $D_{POLY}$  = total calculated drag with polymer ejection  $D_w$  = total calculated drag with water ejection  $SD_{POLY}$  = shear drag calculated with polymer ejection  $SD_W$  = shear drag calculated with water ejection.

Table 4 lists these results. A discussion of the table will not be given since the results are as would be expected for the wall concentration shown in the previous figures.

The system of equations presented herein is believed to have several unique qualities. First, presuming that a reasonable ejection process occurs, the equations account for a change in the mixing length constant resulting in a significantly reduced diffution process. This should represent a near-optimum case for developing flow. Secondly, by maintaining the mixing length constant equal to that of water, the model represents the ejection of polymers in a fully developed turbulent flow where the similarity concentration profiles are equivalent to those of water. Thirdly, the model accounts for the initial zone of diffusion as well as the subsequent zones, which should provide an accurate prediction of the wall concentration. These beliefs will be tested in subsequent sections.

# TABLE 4

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# Calculated Drag Reductions

Model Applied 2 zone	Conditions Polymer CONC/Q <sub>4</sub> (in <sup>3</sup> /sec) Water/20.6	<u>% TDR</u> 0	χ sfr 0
Molecular Diffusion	50,500/20.6	32.6	65
Variable K3	50/20.6	31.2	62.3
Data Adjusted	50/20.6	27	55
	500/20.6	32	65
2 zone	50/20.6	22.6	44.6
	500/20.6	32.6	65
Combined	50/41.2	30.3	60.6
	50/20.6	24.6	50.3
	50/10.3	17.8	37.8
	100/20.6	30.1	60.4
	500/20.6	32.3	64.2

#### V. EXPERIMENTAL PROCEDURES

Two types of tests were performed in this research. These were: (1) polymer ocean, drag reduction and flow visualization tests and (2) polymer ejection boundary layer sampling tests. Both series made use of the full experimental apparatus but in slightly different ways. The experimental procedure for the polymer ocean tests will be discussed first.

# A. Polymer Ocean Tests

## General

The polymer ocean tests made use of the three dye ejecting bodies described previously and displayed in Figures 11, 12 and 13. The test series is called polymer ocean since for these tests the entire drop tank is filled with either fresh water or filled with a polymer solution. The model, therefore, is operating under conditions of uniform polymer concentration. A visible dye was ejected, by aspiration in many of the tests.

# Polymer Addition

The polymer used in these tests was polyethylene oxide (Polyox-WSR-301, Union Carbide Corp.). Polyox is a long, 3 million molecular weight, water soluble polyether. Due to its considerable size and the sensitive ether linkage, the mixing of highly concentrated solutions must be undertaken with great care. A 25% by weight

polymer slurry was made up for mixture with the water in the tank. The test program called for polymer ocean concentrations of 60 WPPM to 1.25 WPPM. Since the water tank weight of water equaled 3452.5 lbs, 3452.5 x  $10^{-6}$  lbs of polymer addition were required for each WPPM of polymer concentration desired (or 13810 x  $10^{-6}$  lbs of 25% polymer slurry by weight). The tank was first brought to 60 WPPM concentration level, tests performed, and then drained to a predetermined level and refilled with fresh water to obtain 50 WPPM. After testing at this level, the procedure was repeated to obtain 20 WPPM and 5 WPPM. The tests requiring concentrations down to 1.25 WPPM and 2.5 WPPM were begun with a 20 WPPM concentration.

The mixing procedure consisted of premixing the preweighed 25% polymer slurry in a 25-gallon drum by slowly pouring the slurry against a wall of the drum, and spraying a high intensity fan shape spray of water on the polymer. Gentle stirring followed for approximately 1/2 hour and the mixture left to stand for 2 to 4 hours. The clear solution was then poured into the partially empty drop tank and the tank refilled. The tank was gently mixed by raising and lowering the retrieval net to insure a homogeneous mixture. Samples were taken at each concentration and measured in a Hydrat apparatus similar to that described in Hoyt (1966).

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# Model Preparation

The models for testing were configured in the  $6^{\circ}$  tail,  $12^{\circ}$ tail or spherical tail configuration as discussed previously. The model preparation for test was as described previously. It is repeated here for completeness. Referring to Figures 14 and 15, the model is made ready for a launch by inserting the tank guide wire through the body guide tube, (9), the wire bears on a nylon bearing at either end of the model to minimize friction. The (10), of the model is removed (separated sufficiently) and tail, the internal cavity filled with dye. The dye ejection ports, (6 being previously taped over to insure no loss of dye. The model is reassembled and the vent screw (unmarked) in the tail is removed and the model placed under the water level in the tank to back fill the cavity totally with water. The model may now be fired upon removal of the tape over the ejection holes. When fired, stagnation pressure enters the 4 stagnation ports, is transmitted through the body guide tube and pressurizes the bladder, (4), forcing the dye cut the four dye ejection ports located at the minimum pressure point of the forebody as determined by a potential flow program. After several tests, the bladder was found to be not necessary simplifying the operation. The tail of the model was then inserted into the launcher in preparation for launching. The launcher receptacle, as designed, mates with the  $6^{\circ}$  tail only. The other models are butted to the

launcher. The models are held in place by fishline that is tied to one side of the launcher, wrapped around the wire in front of the nose of the model and tied to the other side of the launcher. At launch, the string is severed by the forward motion. When in the ready to fire condition, all except the tail is underwater. After firing, the model is maintained on the wire in the tank, the ejection holes retaped underwater, the tail removed and the internal chamber drained and refilled with dye. The model is reassembled as before and made ready for a launch.

# Launch Procedures

The launcher operation was quite simple. The low pressure regulator on the launcher was preset to some known pressure level. The hand firing valve was opened, firing the launcher. The launcher chamber pressure was recorded during this operation. The model velocity was measured at the several stations and noted for acceleration or deacceleration. The launcher pressure was then adjusted to obtain steady state velocities during the model travel down the tank. After fire, the firing valve is closed, the launcher piston chamber vented, and the firing piston retracted in preparation for the next test.

## Velocity and Photographic Measurements

Little needs to be said regarding procedures here. It was only necessary to reset the counter and set the camera flash guns delay circuitry to the appropriate value. At launch, the camera shutter was held open. The appropriately delayed flash would

expose the film. Transit times through the various stations were automatically recorded.

# Polymer Ocean Test Series

Two types of tests were performed. Launch tests in which the launcher was used and free drop tests, in which the model was held just underwater and allowed to gravity drop down the tank. The launch tests were all performed with the  $6^{\circ}$  tail model. The free drop tests were performed with the  $12^{\circ}$  tail and spherical tail model. This type of test was initiated since gross instabilities in trajectory of the models ( $12^{\circ}$  and spherical tail) occurred when launchings were attempted. Undoubtedly due to the launche: receptacle having a  $6^{\circ}$  taper design to fit that model.

The test series are summarized in Table 5. For the launch tests, only those tests at which terminal velocity was achieved are noted. A total of 491 tests were run of which 135 tests are reported.

# TABLE 5

#### POLYMER CONCENTRATION LAUNCH TESTS FREE DROP TESTS 120 TAIL SPHERICAL PPMW 60 TAIL TAIL 8 7 7 FRESH WATER 1.25 8 \_ 2.5 4 5 10 6 7 10 9 20 7 6 11 2 50 6 ----12 19 60 6

# Summary of Tests Performed Polymer Ocean Series-Number of Tests

# B. Polymer Ejection Tests

# General

The polymer ejection tests made use of the polymer ejecting body described previously and displayed in Figure 18. In these tests, varied polymer concentrations as well as pure water all dyed with a fluorescent dye, Uranine-B, were employed. Simultaneously, either wall samples or samples at two different distances from the wall in the boundary layer were taken at four axial positions. Visible dye was also mixed with the polymer on specific tests for boundary layer photographs.

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### Polymer Preparation

The polymer used in this series of tests was also polyethylene oxide (Polyox-WSR-301).

The test matrix called for solutions in the 50 to 1000 PPMW range. A master solution was prepared at 2000 ppmw and diluted to the required concentration.

The master solution was prepared by sifting the premeasured polyox powder onto the surface of the carefully weighed water which was being slowly stirred by a magnetic mixing bar. After a clear solution resulted (approximately 1 hr.), the solutions were left to stand for approximately 40 hrs. to minimize the high viscoelastic effects of freshly mixed solutions, and to assure homogeneity. The master solution was kept in a dark, cool place after initial mixing to reduce the auto-oxidation problem with polyethers. When required, the proper amount was pipetted out of the master solution and diluted to the required concentration. These dilute solutions were used within 24 hrs. of the make-up time.

The uranine master solution was prepared in the same manner. Thus, when a test solution was required, the proper amount of each constituent was added to enough water to make one liter of solution. This was poured back and forth into the container ten times to assure complete mixing, and then let stand for one hour to achieve homegeneity.

A series of calibration tests with the fluorometer indicate that this procedure is adequate to obtain accurate results.

The phenolphthalein solution was also mixed with the polymer solution in the same manner as the uranine to provide a visible dye for photographic record purposes. Fluorometric readings were not taken during these tests since the slight opaqueness of the phenolphthalein resulted in erroneous fluoressence readings were attempted.

The test series conducted required polymer solutions of 5 PPMW, 10 PPMW, 20 PPMW, 50 PPMW, 500 PPMW and 1000 PPMW.

# Model Preparation and Data Retrieval

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The ejecting 6° tail model has been previously described. The assembly for a test and the subsequent withdrawal of samples is discussed below. The model is assembled, as described previously, excepting for the half-body nose and placed in the assembly tank, Figure 23. The appropriate flush-mounted probes or boundary layers pitot tubes are installed. The installation procedure for the flush probes consists of partially inserting the flush probes, placing a small amount of wax around their periphery, heating lightly with a propane torch and pressing the probes flush with the surface. The pitot-like probes were installed in a similar fashion excepting that a feeler gauge set at either .020 inches or .050 inches, depending on probe set, was placed under the flattened tip of the probe, Figure 20. The probe area at the surface of the body

was filled with wax and flaired in with a razor blade. The height could be reasonably set within .003 inches by this method. The axial orientation was set by eye, but with the extent of the probes, .03 inches, an officiet of several degrees was easily noticed and corrected.

The assembly tank was now filled with water to just below the polymer storage volume level. A background sample of the assembly tank water and drop tank water was taken at this time to correct sample fluorence readings. The solution to be ejected was then poured carefully into the polymer storage volume, Figure 17, and the halfbody nose carefully installed. The model now resides in the assembly tank, nose up, and must be transferred to the drop tank, nose down. The ejector screen was then taped with electrical tape to insure no leakage occurred on transfer to the The guide wire was threaded through the model and the drop tank. model transferred to the drop tank. The model is now inserted into the launcher receptacle and a nylon shear screw affixed through the launcher to the firing rod on the model. This holds the model in place and fires the CO<sub>2</sub> cartridge ejecting the polymer and withdrawing boundary samples at launch. After firing and the launcher retracted, the model is kept underwater while preparations are made to quickly wipe it dry on removal from the tank prior to placing on four separate collection trays. The model is removed from the wire, wiped dry and placed on a stand, horizontally, over

four collection trays, (keeping the top uppermost for reasons explained under the calibration section). After the samples have drained into the collection trays, the model was totally disassembled and washed prior to the next test. The chamber samples were then tested applying the fluorometric techniques described previously. The fluorometer readings were transferred to fluorescent dye concentration measurements in PPMW using the appropriate calibration curve, Figure 21 or 22, and then converted to undiluted values applying the external to internal calibration curves, Figures 24 through 31. These values, when nondimensionalized with the ejected dye concentration, represent the normalized concentration of any ejected tracer, or the polymer, at that particular station or boundary layer height under the assumption of similar diffusion qualities.

#### Launch Procedure

The launch procedure is the same as for the previous tests. No attempt was made to achieve terminal velocity since a significant number of tests are required to do this. The ejector type tests took approximately one hour per complete test cycle as compared to 15 minutes for the polymer ocean tests (when photographic records were desired).

#### Velocity and Photographic Records

The procedures for these tests were as described for the polymer ocean tests.

# Polymer Ejection Test Series

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The polymer ejection tests were performed with fresh water and six polymer concentrations. As previously mentioned, no attempt was made to control velocity. The test series is summarized in Table 6. The ejection rate for all tests was held constant at 20.625  $in^3/sec$ .

# TABL<sup>v</sup> 6

# Summary of Tests Performed Polymer Ejection Series-Number of Tests

POLYMER CONCENTRATION PPMW	FLUSH	PROBE HEIGHTS .020 IN.	.050 IN.	PICTURE TESTS
FRESH WATER	4	3	7	5
50	4	4	4	l
500	6	4	3	1
1000	3	-	-	2
20	1	-	-	_
10	2	-	-	-
5	2	-	-	

#### VI. EXPERIMENTAL RESULTS AND DISCUSSION

#### A. General

The test series were directed towards providing information in several areas. These were, for the axisymmetric turbulent flow case (1) does the polymer affect the point of separation thereby affecting the form drag, (2) qualitatively, is there any change in the boundary layer characterization and lastly, (3) what is the wall concentration necessary to achieve a maximum skin friction reduction and what is the diffusion process for an ejector ejecting into the laminar nose region. A discussion of the effects of polymers on the separation region and the effects of polymer on the boundary layer characteristics will be performed simultaneously since they relate to the flow visualization portion of the study.

# B. Boundary Layer Characterization

#### and Separation Tests

Both the simple dye ejecting body and the polymer ejecting body were used in this series of tests. The mechanism of maintaining a high wall concentration was different in these tests The dye ejecting body was operated in the drop tank with a uniform polymer concentration throughout the tank. The polymer ejecting body depended on a diffusion process for wall concentration control. Direct comparison can be made which clearly displays the effect of the polymers on the character of the boundary layer.

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Brady (1973) summarized the work of Kline et al (1963) quite nicely. He states:

"Kline et al found the 'laminar sublayer' to be made up of a regular structure of low and high velocity longitudinal streaks which meander transverse and normal to the wall. A dimensionless streak spacing  $\lambda^+ = \frac{\lambda v^*}{2} = 76.5$  was found for zero pressure gradient. These streaks either break up or randomly burst from the sublayer into the fully turbulent region.

The fully turbulent region is one of intense mixing and high dissipation of energy. Protruding from this region are intermittent large eddies -- visualized as peninsulas of turbulence.

The peninsulas of turbulence which extend into the third boundary layer zone -- the outer turbulent region -- gives it a characteristic not unlike the wake behind a cylinder. It has rather large lumps of turbulence at intermittent spacings.

It is clear that the driving force for the entire turbulent boundary layer is the generation of velocity streaks in the sublayer and their subsequent bursting outwards. Kline presents the results of many other investigators, as well as his own, in support of this hypothesis."

Figure 44 is a pictorial sketch of the boundary layer flow taken from Kline (1963) displaying the process quite nicely. The subsequent test results bear this process out quite well and display the effects of polymers on the process.

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The first series of tests were made with the dye ejecting bodies. In this series, one or more of the four dye ejecting

FLOW STRUCTURE, VELOCITY PROFILE ) t, 80 370 30 0 8/7 86:0 003 0.01 0.4 PRIMARILY DECAY OF LARGE RANDOM INTER-Action of Eddies UNIFORM FREE STREAM FLOW WALL FLOW BREAK-UPS TURBULENT EDDIES IRREGULAR EDGE OF WAKE REGION 11111 EDGE OF BOUNDARY LAYER PHYSICAL PICTURE OF FLOW -WALL PATH OF EJECTED EDDIESA ZITTITITITITI INTERMITTENT WAKE REGION FULLY TURBULENT REGION FREE STREAM AYER FLOW REGIONS OF BOUNDARY

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Figure 44. Pictorial sketch of boundary layer flow (from Kline, (1963))

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holes was plugged to attempt to minimize tank contamination. The tests were of the launcher or free drop type depending on the tail configuration.

Figure 45 displays the boundary layer character for the  $6^{\circ}$ tail configuration operating in water at a Reynold's number of 4.94 x  $10^6$ . The highly turbulent character with the ejected eddies is clearly evident. Measurements of the boundary layer taken from this picture and others not displayed, at a mean position of the ejected eddies, is shown in Figure 46. The analytical program previously discussed was exercised to predict the boundary layer thickness. This is shown in Figure 46 also. Good agreement occurs, within 10% for this case, if one considers that the measured position was the mean of the eddies and not the tips as theorized by Kline (1963). Figure 47 presents a normalized version of this same information. Both the calculated and measured values were normalized by their respective values at x/L = .5. As is shown in the figure, an excellent prediction of the boundary layer shape as a function of distance down the body results for this body by the analytical routine.

A second test was performed with the  $12^{\circ}$  tail configuration at a length Reynold's number of 3 x  $10^{6}$  and a polymer concentration of 2.5 WPPM. The forebody portion, shown in Figure 48 displays the same character as the no-polymer case seen previously. The ejected eddy height seems somewhat larger in this case probably

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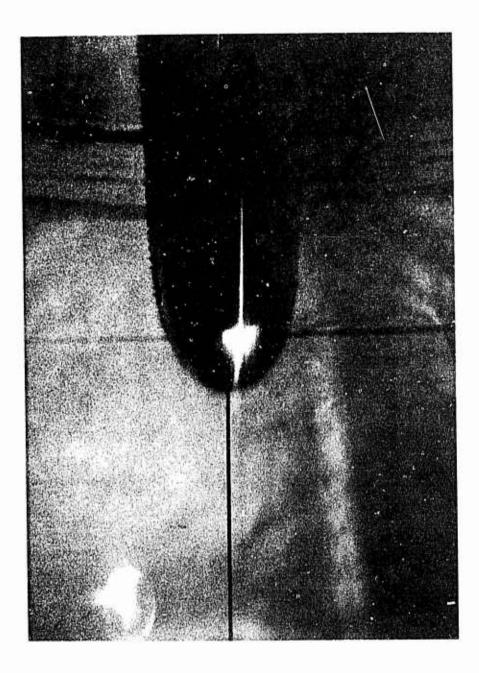


Figure 45. Photograph of dye ejection into the boundary layer -  $6^{\circ}$  tail - no polymer  $R_e = 4.94 \times 10^{6}$ 

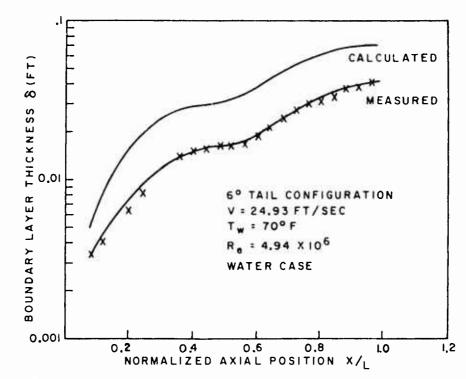


Figure 46. Boundary layer thickness vs normalized axial position - 6° tail configuration water case

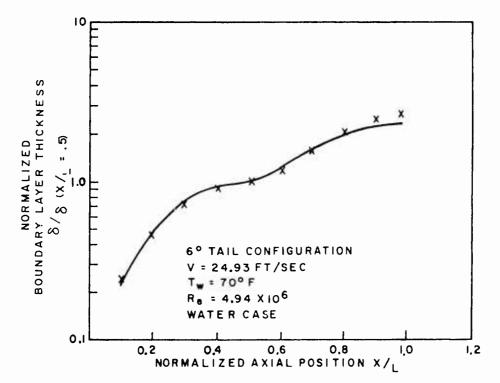


Figure 47. Normalized boundary layer thickness vs normalized axial position - 6° tail configuration water case

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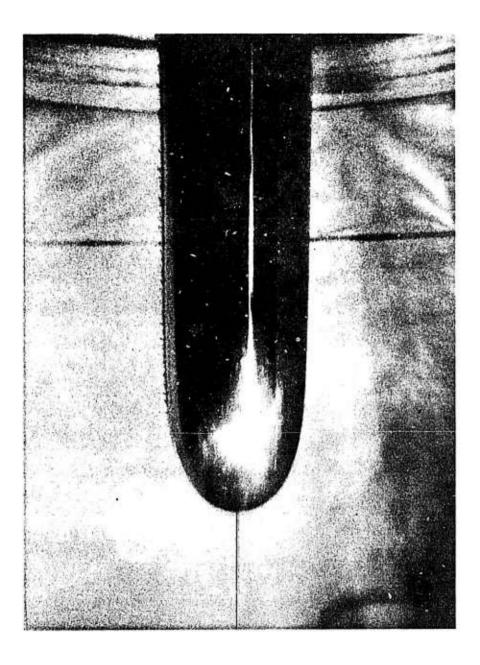


Figure 48. Photograph of dye ejection into the boundary layer - 12° tail configuration - 2.5 WPPM polymer  $R_e = 3 \times 10^6$ 

due to the suppression of the smaller scale turbulence as displayed by White, A. Figure 49 displays the measured and calculated boundary layer thickness again using the mean eddy height for measurement purposes. The thickness measured in this test is believed to be in error (the body rotated) since the first visible position of the dye is too far for the nose. The shape of the profile should be correct, however. The normalized values are displayed in Figure 50 again showing reasonable shape agreement.

The effect of polymer suppression of the small scale turbulence was much more apparent in the tests with the polymer ejecting body. The polymer solutions used in these tests were all made up within a 24-hour period. Table 7 lists the pertinent data for this test series.

Figures 51, 52 and 53 display photographs of the polymer ejecting body ejecting visible dye and water.

## Table 7

Polymer Ejecting Body - Boundary Layer Visualization and Measurement Tests - Test Parameters

POLYMER CONCENTRATION (WPPM)	VELOCITY (FT/SEC)	LENGTH REYNOLDS NUMBER
Water	26.9	5.33 x 10 <sup>6</sup>
50	28.33	4.67 x 10 <sup>6</sup>
500	29.1	5.31 x 10 <sup>6</sup>
1000	29.2	4.9 x $10^{6}$

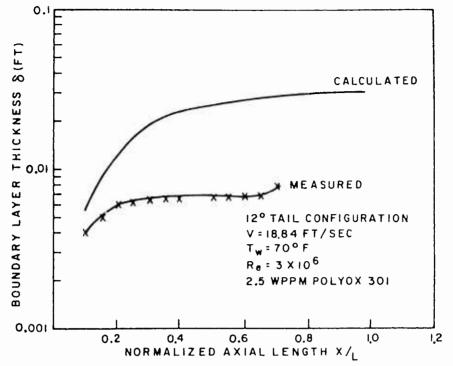


Figure 49. Boundary layer thickness vs normalized axial position - 12° tail, 2.5 WPPM polymer

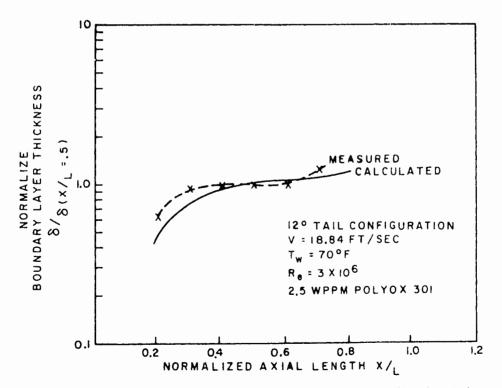


Figure 50. Normalized boundary layer thickness vs normalized axial position - 12° tail configuration, 2.5 WPPM

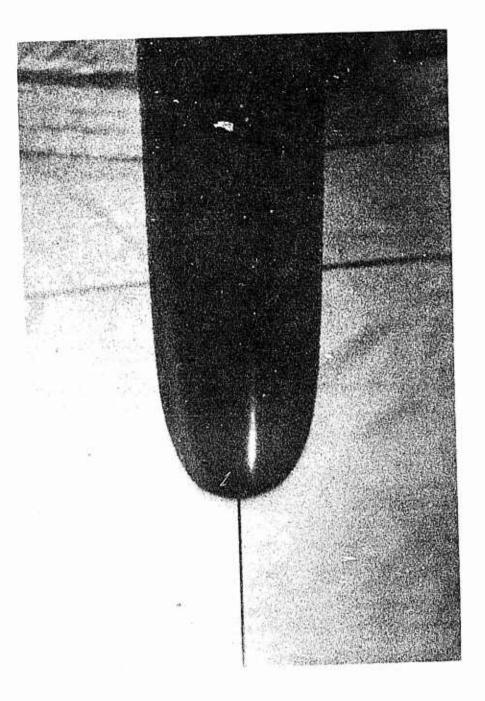


Figure 51. Photograph of polymer ejecting body - forebody view - water ejection  $R_e = 5.33 \times 10^6$ 

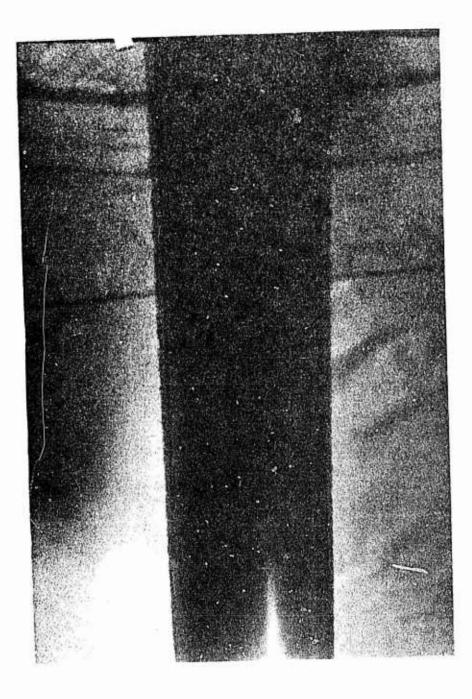


Figure 52. Photograph of polymer ejecting body - midbody view - water ejection Re = 5.33 x 106

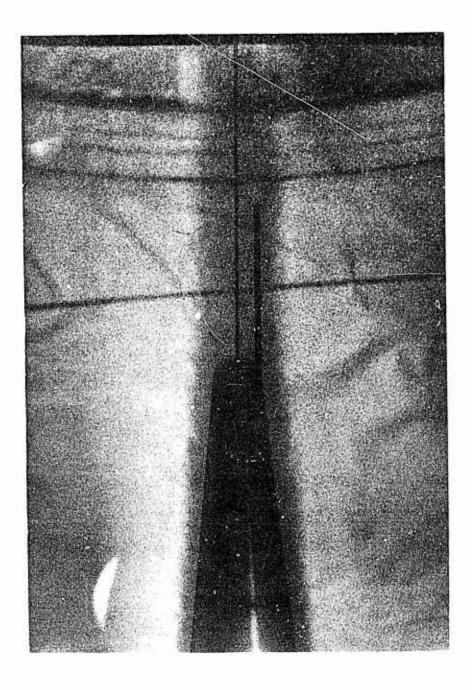


Figure 53. Photograph of polymer ejecting body - tail view - water ejection  $R_e = 5.33 \times 10^6$ 

These views clearly show the coarse and fine scale turbulent type flow. Measurements of the boundary layer are plotted in Figure 60. Also to be noted in Figure 51 is the uniform ejection process which apparently is not seriously effecting the flow. From these views, the flow is apparently fully turbulent near the nose of the body.

The tests were repeated, this time ejecting a 50 WPPM polymer solution. Figures 54 and 55 display the results. The fine scale eddy structure is apparently missing leaving only the coarse structure. More interestingly, the boundary layer thickness has decreased a disproportionate amount in the midbody region as compared to the tail suggesting, as it should be, higher effective wall concentrations forward on the body which result in thinner boundary layers in this region and a rapid growth in the tail region. Since the boundary layer is beginning to get rather thin in the forebody region, the measurement method used should be described. Slides have been made of the figures presented in this study, these were projected on a screen such that the body diameter (3 inches) projected to about 2 feet in diameter. The resultant boundary layer thicknesses near the nose were a projected .2 inch. An overlay slide with one inch axial marks was used as an overlay (with 2 projectors to insure proper scale). This was required since the body does not reach 3 inch diameter for some distance form the nose.

The last two groups of tests in this series were with 500 WPPM and 1000 WPPM. Figures 56 and 57 show the forebody view

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Figure 54. Photograph of polymer ejecting body - midbody view - 50 WPPM polymer ejection  $R_e = 4.67 \times 10^6$ 

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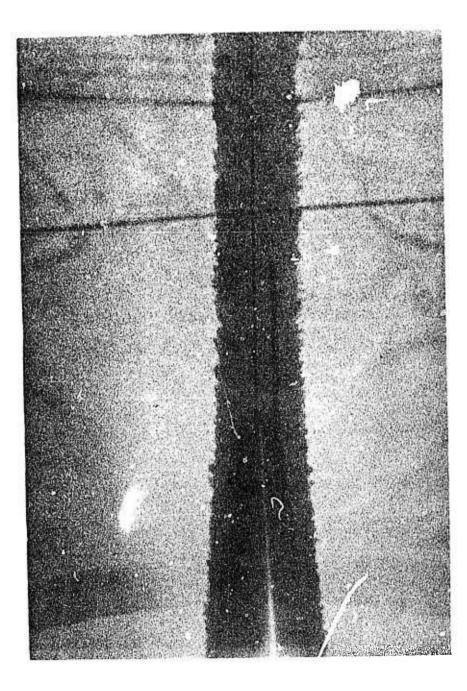


Figure 55. Photograph of polymer ejecting body - tail view - 50 WPPM polymer ejection  $R_e = 4.65 \times 106$ 

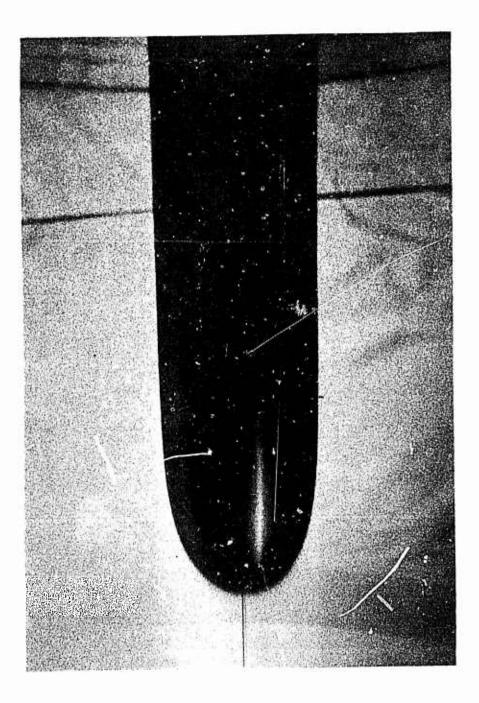


Figure 56. Photograph of polymer ejecting body - forebody view - 500 WPPM polymer ejection  $R_e = 5.31 \times 10^6$ 

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Figure 57. Photograph of polymer ejecting body - tail view - 500 WPPM polymer ejection  $R_e = 5.3i \times 106$ 

and tail view for the 500 WPPM case and Figures 58 and 59 show similar views for the 1000 WPPM case. Apparently, a limit of drag reduction is being reached, presuming this may be inferred from the fact that there is little difference in the boundary layer reduction between these cases as seen in Figure 60. Moreover, an additional phenomenon is occurring. It is first noticeable in Figure 57 and readily apparent at the 1000 WPPM level of Figures 58 and 59. A significant number of streaks are evident in the flow. The approximate streak spacing is about .015 inches. The number of ejector holes is approximately 700. For the body diameter of 3 inches, the number of streaks would be about 620. Additionally, applying the dimensionless streak spacing found by Kline et al (1963) in the laminar sublayer, for a  $v^*$  of approximately .6 ft/sec and viscosity of about that of water, results in a "laminar sublayer" streak spacing of the order of .015 inches. Apparently, at these concentration levels, the turbulence intensity is so damped that the streaks become well ordered and have difficulty in bursting out into the other layers of the boundary layer. It is not until the tail region that a very filamentary bursting is occuring suggestive of the long stringiness associated with elastic polymers. Even the angle of the streaks, essentially in the axial direction, are suggestive of very low energy levels bursting the streaks outward as compared to the water case. The implication of these photographs is that turbulent diffusion has ceased and a molecular

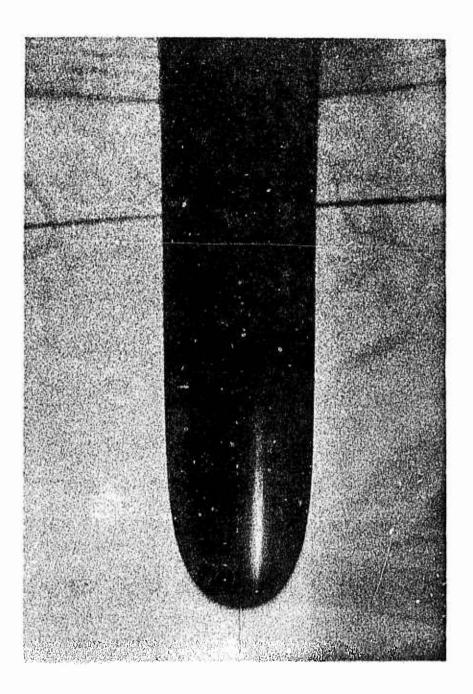


Figure 58. Photograph of polymer ejecting body - forebody view - 1000 WPPM polymer ejection  $R_e = 4.9 \times 106$ 

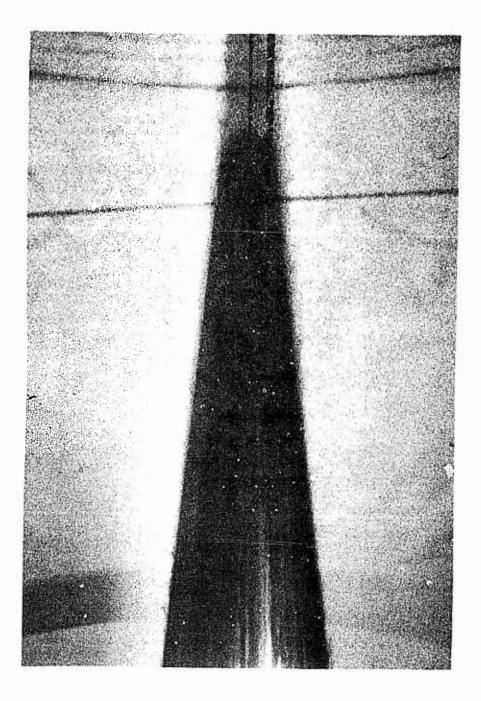


Figure 59. Photograph of polymer ejecting body - tail view - 1000 WPPM polymer ejection  $R_e = 4.9 \times 10^6$ 

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diffusion only in the sublayer is occurring. This would suggest extremely long mixing lengths. Tests by Nadolink (1968) displayed the same characteristic but for polymer ocean type tests. Figure 61 displays a normalized plot of the boundary layer growth for these tests. The polymer cases clearly show a delayed growth trend indicative of suppressed diffusion.

The last series of visual observations centered around the question of whether application of polymers effected the separation point at the tail. Several tests were run with the dye ejecting body with the hemispherical tail in fresh water and in a 20 WPPM polymer ocean. The length Reynolds number for both cases was  $1.877 \times 10^6$ .

Figure 62, the test with plain water, displays a thick boundary layer near the tail and a separation angle measured from the vertical of approximately  $62^{\circ}$  to  $65^{\circ}$ . Figure 63 displays the results of a similar test with 20 WPPM polymer concentration in the tank. The boundary layer is characteristically thin but the separation point resulting in an angular measurement of  $80.6^{\circ}$  for either polymer case or water case. On a nondimensional basis, the computer program predicted separation at x/L = .925 while the data indicate x/L = .948 for separation. Nonetheless, the polymer, for the case tested, did not apparently change the separation point. Similar tests with the  $12^{\circ}$  tail configuration also showed no effect on the separation point. Since sphere tests conducted by Lang and Patrick (1967) indicated that sphere

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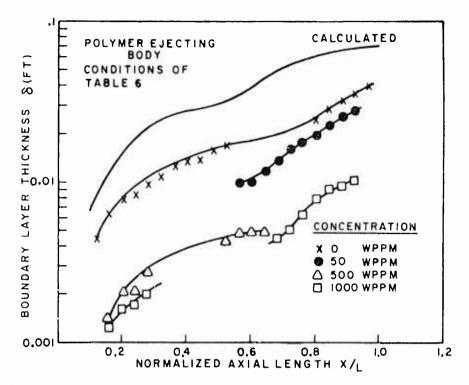
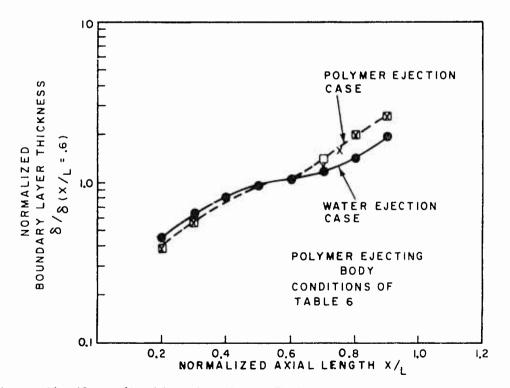


Figure 60. Boundary layer thickness vs normalized axial length - polymer ejecting body



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Figure 61. Normalized boundary layer thickness vs normalized axial length - polymer ejecting body

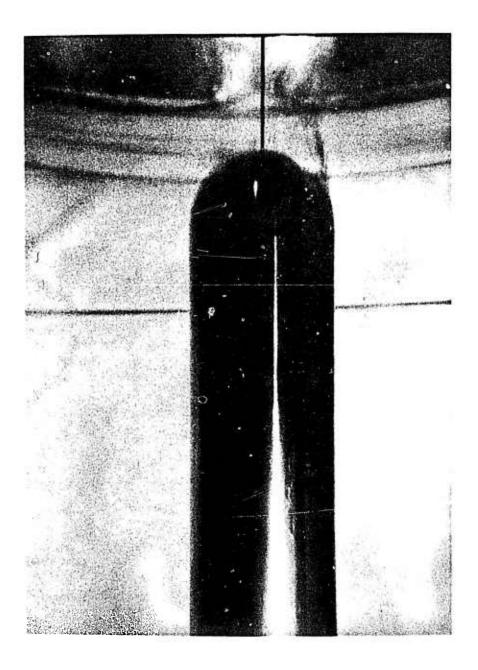


Figure 62. Photograph of dye ejecting body - 20 WPPM polymer ocean  $R_e = 1.877 \times 10^6$ 

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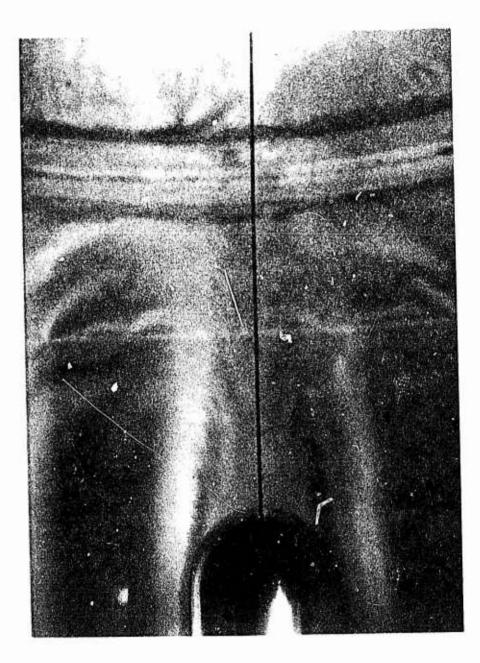


Figure 63. Photograph of dye ejecting body - spherical tail - tail view - water case  $R_e = 1.877 \times 10^6$ 

drag was reduced by a movement of the separation point from the laminar separation point to a further back turbulent separation point. These results are not surprising for the case of a turbulent separation point initially. These results are consistent with those of Stone and Elliott (1970). Unfortunately, this small change in predicted separation point places the separation at the extreme of the negative pressure coefficient, Figure 37, resulting in a very high calculated form drag.

### C. Drag Reduction Tests

The next series of tests were directed towards determining drag reduction efficiency for various polymer concentrations and tail configurations and to test the analytical model for the 6<sup>o</sup> tail case. The form drag calculation for this case are simpler due to the geometry and pressure coefficient profile. The test matrix run was as outlined in Table 5. A total drag coefficient was calculated for each series of tests using the relation

$$C_{\rm D} = \frac{W - B}{1/2 \rho A_{\rm f} U_{\rm o}^2}$$
(114)

where the frontal area,  $A_f = 0.0491 \text{ ft}^2$ . From the drag coefficient,  $C_D$ , the percentage total drag reduction was then calculated for each polymer concentration tested. The percentage total drag reduction is given by

f

% TDR = 100 (1 - 
$$\frac{C_{D_{POLY}}}{C_{D_{uf}}}$$
) (115)

where

$$C_{D_{POLY}}$$
 = Drag coefficient for polymer tests  
 $C_{D_W}$  = Drag coefficient for water tests.

A calculation of percent skin friction reduction was also made for each test. The relation for percent skin friction reduction are.

% SFR = 100 
$$(1 - \frac{C_{fPOLY}}{C_{f_{W}}})$$
 (116)

where.

$$C_f = C_D \frac{D_f}{D_t}$$

and

 $C_D$  = measured drag coefficient

 $D_f$  = total shear drag analytically calculated  $D_t$  = W-B = body weight in water.

It is noted here that  $D_t$ , the actual drag, is used in the % SFR calculation and not the total calculated drag. This is done since the skin friction as calculated by this method has been shown by White (1972) to be accurate. The addition of the term for calculating form drag is only considered to be an indicator and may be considerably in error due to the pressure coefficient inaccuracies. The  $6^{\circ}$  tail tests were the only tests where the launcher could be used. These tests, therefore, were the only ones in this seties where terminal velocities were achieved.

Extreme instabilities were noted when launch tests were attempted with the 12<sup>0</sup> tail and spherical tail models. This is attributed to the launcher receptacle being designed to accept the 6<sup>0</sup> tail. As

a result, the 12° tail and spherical tail were not properly guided during the launch phase. Even with the weighted guide wire, photographs of the test models travelling at angles of near 10° relative to the wire were obtained. Drag data obtained in this manner were not of any use. Additionally, velocity measurements were never achieved when this occurred since the guide wire would generally trip the lasers during the launch transient.

The free drop 12° and spherical tail tests were projected to terminal velocity using a procedure outlined in Nadolink (1968). The procedure solves the equation of motion for an accelerating body having as knowns the weight in air, the weight in water, the velocity at a particular distance and an entrained mass coefficient emperically determined and plotted in the report as a function of L/D. The procedure, because of the form of the final relation is iteratively solved for terminal drag coefficient, which will predict the velocity at the station which is being measured. From this, equation (114) is used to calculate the terminal velocity.

Tables 8, 9 and 10 present the data obtained in this series of tests as well as the percent total drag reduction and skin friction reduction calculated. Other pertinent information noted is the total drag calculated from the analytical routine for the identical test conditions. As may be noted from Table 8, the total drag predicted by the analytical routine is within 10% for the  $6^{\circ}$  tail case. Additionally, the total skin friction determined from equation (89) results in a friction drag coefficient based

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DATA SUMMARY 6° TAIL TESTS

	CALC. D <sub>t</sub>	(001)	4.70		3.75		3.49	3.46		
	CALC. Df	(egr)	2.598	1.508	1.422	.9206	.998	.958		
	و د تیا و	NIC 4	ł	39.8	49.25	67.1	68.8	68.8		
	ه ۲۰۰۲	YULL &	ł	18.73	27.70	33.00	30.29	33.06		
	$c_{D_{A}}$		0.1479	0.1202	0.1068	0.0991	0.1031	0660.0		
	ReL	OTY	5.37	4.56	4.68	4.85	5.27	5.12		
	TANK TEMP.	(UF)	76	68	62	64	70	71		
POLYMER	CONCEN- TRATION		0	2.5	5.0	20.0	50.0	60.0		
	AVERAGE VELOCITY (PT/SPC)	111000	25.1 <u>+</u> 3%	24.64 +2%	26.17 +2%	$27.14 \pm 2\%$	26.61 <u>+</u> 2%	27.2 <u>+</u> 2%	TESTS	-
	NUMBER OF TESTS		8	4	10	7	2	12	LAUNCHER TESTS	7000 C - 1

L = 2.0833 FT.

 $A_{f} = 0.0491 \text{ FT}^2$  (Frontal area)

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 $A_{S} = 1.3685 \text{ FT}^{2}$  (surface area)

D = 0.25 FT.

W-B = 4.43 LBS. WATER TESTS (WEIGHT IN WATER) W-B = 3.47 LBS. POLYMER TESTS (WEIGHT IN WATER)

TABLE 9 DATA SUMMARY 12<sup>0</sup> Tail Tests

					1		1					
NUMBER OF TES'IS	AVERAGE (F)	AVERAGE VELOCITIES (FT/SEC) V12 V22 V1	IES V; 2	PROJECTED TERMINAL VELOCITY (FT/SRC)	POLYMER CONCEN- TRATION (WPPM)	TANK TEMP.	ReL *10 <sup>-6</sup>	c <sub>DA</sub>	PROJECTED %TDR %5E	CTED %SER	CALC. Df	CALC. D <sub>t</sub>
		67.	CT.		(11111)	101/	014		NULL &	WHUN	(007)	
7	17.1	19.36	18.6	25.58	0	70	4.08	.2292	I	1	2.39	4.22
80	17.1	19.36	18.6	26.07	1.25	69	4.1	.2208	3.7	32.9	1.66	3.57
9	17.284	19.756	18.895	27.15	Ŋ	68	4.22	.2066	10.2	50.0	1.33	3.39
6	17.284	19.756	18.895	27.51	10	69	4.33	.1986	13.4	59.6	1.113	3.23
9	17.279	19.727	18.875	27.41	20	69	4.32	.1979	12.8	68	.888	2.99
9	17.359	19.813	18.986	27.92	50	69	4.39	.1928	15.9	69.2	.875	3.06
9	17.302	19.755	18.907	27.57	60	70	4.39	.1978	13.8	69.0	.863	2.99
FREE DR	FREE DROP TESTS											
L = 1.679 FT.	.79 FT.											
$A_{f} = 0.$	$A_{f}$ = 0.0491 FT <sup>2</sup> (Frontal	(FRONTA	L AREA)									
A <sub>S</sub> = 1.	1.1741 FT <sup>2</sup> (SURFACE	(SURFAC	E AREA)									
D = 0.2	0.25 FT.											
W = 9.4	9.418 LBS.	(WEIGHT IN AIR)	IN AIR)									

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W-B = 7.109 LBS. (WEIGHT IN WATER)

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	CALC. Dt (LBS)	7.09	6.8	7.09	7.43					
	CALC. Df (LBS)	.665	.376	. 28	.283					
	%SFR	ł	7*77	60.4	61.8					
sts	%TDR	i	1.5	9	10.3					
Tail Tea	c <sub>DA</sub>	.34	.335	.32	.305					
Spherical Tail Tests	R <sub>eL</sub> x10 <sup>-6</sup>	1.66	1.6	1.64	1.68					
Spł	TANK TEMP. (OF)	65	62	62	62					
Data Summary	POLYMER CONCEN- TRATION (WPPM)	0	5	20	60					
Data S	PROJECTED TERMINAL VELOCITY (FT/SEC)	13.5	13.5	13.9	14.24			L AREA)	E AREA)	
	AVERAGE VELOCITY V12 (FT/SEC)	12.23	12.24	12.44	12.67	? TESTS	5 FT.	$A_{f} = 0.0491 \text{ FT}^{2}$ (Frontal Area)	$A_{s} = 1.1044 \text{ FT}^2$ (SURFACE AREA)	гт.
	NUMBER OF TESTS	7	7	11	19	FREE DROP TESTS	L = 1.386 FT.	$A_{f} = 0.0^{1}$	$A_{S} = 1.10$	D = 0.25 FT.

W = 4.9 LBS. (WEIGHT IN AIR)

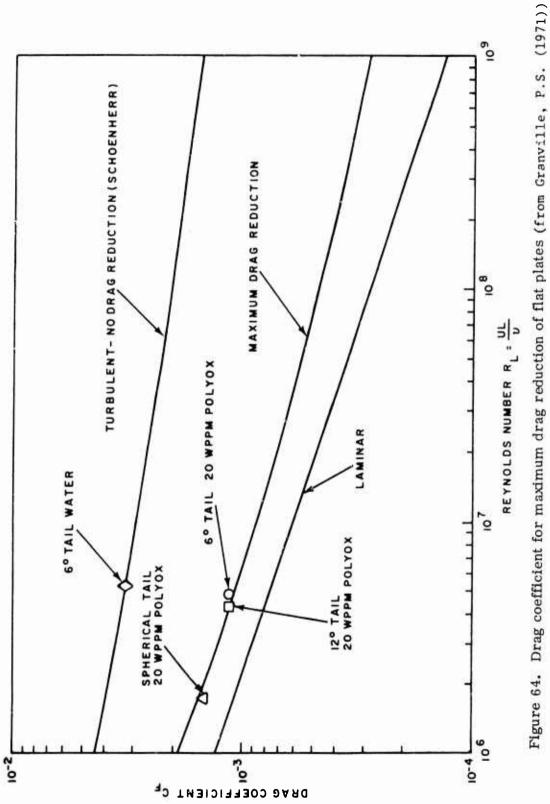
W-B = 2.94 LBS. (WEIGHT IN WATER)

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on surface area of  $C_f = .00311$  which compares very favorably with that determined from the accepted formulas for flat plates of .00336 at the same length Reynolds number. The calculated skin friction coefficient is plotted in Figure 64 taken from Granville (1971). For the  $\delta/r_0$  being worked with in this study and for a mild pressure gradient, a comparison is considered reasonable.

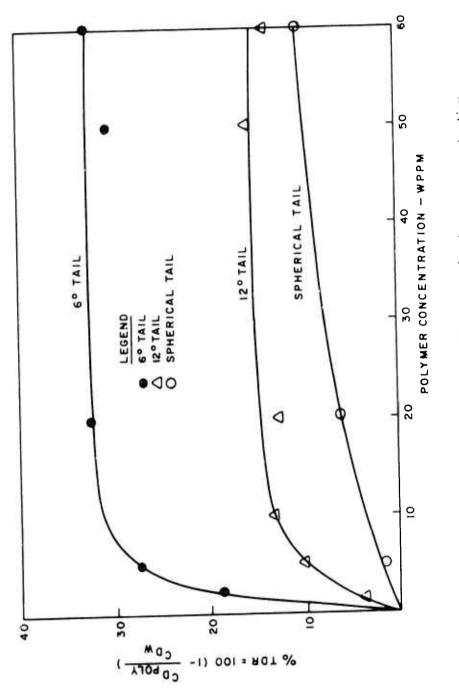
Figure 65 presents a plot of the percent total drag reduction for the various tail configurations. As noted in the figure, peak drag reductions are occurring for the  $6^{\circ}$  and  $12^{\circ}$  tail case at polymer concentrations of between 15 and 20 WPPM. The effect of increased form drag with the 12° and spherical tail models results in a decreased total drag reduction since the polymer only reduces the skin friction. Figure 66 is a plot of percent skin friction reduction. This plot clearly displays the achievement of equal skin friction reduction on all the bodies tested as would be expected. Calculation of the skin friction coefficient based on surface area for the 20 WPPM case with the  $6^{\circ}$  tail results in a C<sub>f</sub> of .0011 at a length Reynolds number of  $4.85 \times 10^6$ . This point is plotted on Figure 64 and is in good agreement with the maximum drag reduction value given by Granville. Plotted on Figure 64 also are the skin friction coefficients calculated for the 12° and spherical tail. These also are in reasonable agreement with the maximum drag reduction line as proposed by Granville.





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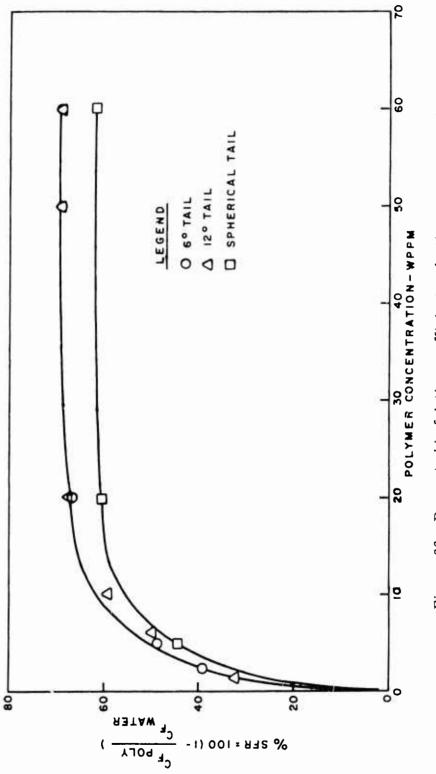


Figure 66. Percent skin friction coefficient reduction vs concentration

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### D. Polymer Concentration Profile Tests

The polymer ejecting body was used throughout this entire series of tests. The primary emphasis in these tests was to obtain polymer concentration measurements at the wall and at two heights in the boundary layer. These heights were selected to be .025 inches from the body to the centerline of the probes and .055 inches from the body to the probe centerline of the probes for reasons previously discussed. The probes are as described previously and shown in Figure 20. Only one stroke rate was used in these tests although other stroke rates are possible with the model through an orifice change. The stroke rate selected resulted in a volume rate of flow of 20.6 in $^{3}$ /sec. Polymer concentrations of 50 and 500 WPPM of Polyox-WSR-30 were ejected and samples taken at the wall and the two probe heights. Testing with 5 WPPM, 10 WPPM, 20 WPPM and 1000 WPPM was also performed but only with the flush probes installed. Tests were also performed with fresh water dyed with the fluorescent dye to determine what differences in diffusion exist between the polymer contaminated solution being ejected and the water. All tests were run using the launcher and no attempt was made to attain terminal velocity. The tests were all made at a high enough initial velocity that near terminal velocities existed and transient characteristics were deemed to be unimportant. The tests could not be used, however, to determine drag reduction or drag coefficients. The tests went very smoothly

with only one or two failures in the entire test series when a launch was made. Velocity variations for similar tests were within one percent. Unfortunately, concentration measurements were more diverse with 10 to 15% variations not uncommon although the bulk of the data fell in a narrowband. The test operation was very procedure oriented with deviations generally resulting in an aborted attempt at a launch. The long hours spent in calibrating the model was key to the smooth test series since carefully followed procedures resulted. The test matrix run is that shown in Table 6. In general, each test series, a series being either no polymer or a specific polymer concentration, began with the flush probes installed. The .025 inch probes were next installed and finally the .055 inch probes. No intermixing of probe heights occurred, even on a per station basis. The test model functioned perfectly, as designed, with over several hundred firings being accounted for considering stroke rate calibration tests, polymer concentration tests, photographs firings and actual data gathering firings. The only malfunction occurring was in the firing rod. One of the functions of this rod was to follow the polymer ejection piston during the ejection process. A photograph of the tail region of the model could then be analyzed to reveal the position of the firing rod still external to the body. This information combined with body velocity and distance to the camera station would allow a continual check on

the stroking rate to be made. Unfortunately, the launch process proceeded to distort the rod slightly on each launch resulting in it becoming stuck and not properly following the ejection piston.

By inserting a spacer in the ejector piston volume to limit its stroke, an independent check on stroke rate was made. With the appropriate spacer size for the body velocity, camera station and stroke rate installed, a test was made with visible dye and a photograph taken. The photograph displayed several inches of the forebody free from dye while the remainder of the body uniformly covered with dye. This verified that the proper ejection rate was occurring under test conditions.

The effects of the probes on the boundary layer flow was also of concern. The rotation of subsequent sampling stations on the body was a result of this concern. Figure 67 displays a photograph of a .025 inch probe within a dyed boundary layer for a water test case. No significant distortion of the boundary layer is apparent. The velocity in this case was 20.5 ft/sec.

The results of the test series are tabulated in Tables 11, 12, 13, 14, 15, 16 and 17. Although polymer concentrations were not directly measured, the assumption that the Uranine-B in solution reacts and diffuses in the same manner, as previously discussed, allows direct translation to polymer concentration to be made. Only for the water case is the tracer concentration discussed.



Figure 67. Photograph of .025-inch probe within the boundary layer

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Water Ejection Test Results

R <sub>eL</sub> x10 <sup>-6</sup>	4.78 4.78 4.78 4.78 4.78	4.67 4.67 4.67 4.67	· · · · · · · · · · · · · · · · · · ·
TEMPERA- TURE T ( <sup>O</sup> F)	62.5 62.5 62.5 62.5	65 65 65	70 70 70
BODY VELOC_TY FT/SEC	$\begin{array}{c} 26.5 \\ \pm 1\% \\ 26.5 \\ \pm 1\% \end{array}$	$\begin{array}{c} 25.23 \pm 1\%\\ 25.23 \pm 1\%\\ 25.23 \pm 1\%\\ 25.23 \pm 1\%\\ 25.23 \pm 1\%\end{array}$	$\begin{array}{c} 27.81 \\ 27.81 \\ 27.81 \\ 11\% \\ 27.81 \\ 11\% \\ 27.81 \\ 11\% \\ 27.81 \\ 11\% \end{array}$
EJECTED CONCEN- TRATION C <sub>1</sub> (WPPM)	.588 .588 .588 .588	1.105 1.104 1.104 1.104	.560 .560 .560 .560
RMS CONCEN- TRATION RATIO C/C <sub>1</sub>	.077 .048 .051 .035	.069 .045 .049 .046	.0188 .0272 .0273 .0312
MEASURE- MENT STATION ×/L	.120 .240 .360	.108 .228 .348	.108 .228 .348 .468
NO. OF TFSTS		m	2
PROBE HEIGHT	Flush	.025	.055
	SERIES 1	2	m

NOTE: Ejection Rate 20.6 in<sup>3</sup>/sec L = 2.0833 ft W-B = 4.46 lbs (Weight in Water) Af = 0.0491 ft<sup>2</sup> (Frontal Area) As = 1.3685 ft<sup>2</sup> (Surface Area)

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50 WPPM Ejection Test Results

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ReL x10-6	4.54 4.54 4.54 4.54 4.54	4.79 4.79 4.79 4.79	4. 4 4. 4 4. 4 4. 4 4. 4 4. 4 4. 4 4. 4
TEMPERA- TURE T( <sup>O</sup> F)	5 5 8 8 8 8 8	62 62 62 62	60 60 60
BODY (FT/SEC)	$\begin{array}{c} 27.33 +1\%\\ 27.33 +1\%\\ 27.33 +1\%\\ 27.33 +1\%\\ 27.33 +1\%\end{array}$	27.0 +1.5% 27.0 +1.5% 27.0 +1.5% 27.0 +1.5% 27.0 +1.5%	$\begin{array}{c} 27.0 \\ 27.0 \\ 11\% \\ 27.0 \\ 11\% \\ 27.0 \\ 11\% \\ 27.0 \\ 11\% \end{array}$
EJECTED CONCEN- TRATION (WPPM)	50 50 50	50 50 50	5 5 5 5
RMS CONCEN- TRATION RATIO C/C <sub>1</sub>	.507 .42 .406 .490	.05 .075 .086 .098	.0104 .0126 .0126 .0366
MEASURE- MENT STATION ×/L	.120 .240 .360 .480	.108 .228 .348 .468	.108 .228 .348 .468
NO. OF TESTS	4	4	4
PROBE HEIGHT (IN.)	Flush	.025	.055
SERIES	4	<u>س</u>	Q

SEE NOTE TABLE 10

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## 500 WPPM Ejection Test Results

		1990 - 10 - 11	
ReL x10 <sup>-5</sup>	5.27 5.27 5.27 5.27	4.73 4.73 4.73 4.73	5.32 5.32 5.32 5.32
TEMPERA- TURE T ( <sup>O.F.</sup> )	444 6666	60 60 60	70 70 70
BODY VELOCITY (FT/SEC)	$\begin{array}{c} 28.9 \\ +1\% \\ 28.9 \\ +1\% \\ 28.9 \\ +1\% \\ 28.9 \\ +1\% \\ 28.9 \\ +1\% \end{array}$	27.4 + 1% $27.4 + 1%$ $27.4 + 1%$ $27.4 + 1%$ $27.4 + 1%$	26.85 26.85 26.85 26.85
EJECTED CONCEN- TRATION (WPPM)	200 200 200 200	200 200 200 200 200	200 200 200 200
RMS CONCEN- TRATION RATIO C/C <sub>1</sub>	.45 .45 .555	.0222 .031 .046 .056	.021 .0097 .02 .024
MEASURE- MENT STATION x/L	.120 .240 .360 .480	.108 .228 .348 .468	.108 .228 .348 .468
NO. OF TESTS	4	4	£
PROBE HEIGHT (IN.)	Flush	.025	.055
SERIES	2	ω	6

SEE NOTE TABLE 10

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# 1000 WPPM Ejection Test Results

			MEASURE-	RMS	EJECTED			
	PROBE	.ov	MENT	CONCEN-	CONCEN-	BODY	TEMPERA-	еč.
	HEICHT	OF	STATION	TRATION	TRATION	VELOCITY	TURE	1
SERIES	(IN.)	TESTS	x/L	RATIO C/C <sub>1</sub>	(MPPM)	(FT/SEC)	T( <sup>O</sup> F)	6-01x
	Flush		.120	. 45	1000	<del>6</del> 3	58	4.841
			.240	.35	1000	63	58	4.844
10			.360	. 437	1000	28.93 +2%	58	4.844
		e	. 480	.352	1000	28.93 + 2%	58	4.844
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SEE NOTE TABLE 10

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20 WPPM Ejection Test Results

T	
ReL ×10 <sup>-6</sup>	6.04 6.04 6.04
TEMPERA- TURE T( <sup>O</sup> F)	79 79 79
BODY VELOCITY (FT/SEC)	27.2 27.2 27.2
EJECTED CONCEN- TRATION (WPPM)	20 20 20
RMS CONCEN- TRATION RATIO C/C <sub>1</sub>	.39 .431 .463
MEASURE- MENT STATION x/L	.120 .240 .360
NO. OF TESTS	F
PROBE HEIGHT (TN_)	Flush
250 250 250 250 250 250 250 250 250 250	11

SEE NOTE TABLE 10

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10 WPPM Ejection Test Results

ReL x10-6	6.02 6.02 6.02
TEMPERA- TURE T( <sup>o</sup> F)	79 79 79
BODY VELOCITY (FT/SEC)	$\begin{array}{c} 27.1 \\ 27.1 \\ 112 \\ 27.1 \\ 112 \\ 27.1 \\ 113 \\ 1$
EJECTED CONCEN- TRATION (WPPM)	100
RMS CONCEN- TRATION RATIO C/C <sub>1</sub>	.390 .390 .355
MEASURE- MENT STATION ×/L	.120 .240 .360
NO. OF TESTS	7
PROBE HEIGHT (IN.)	Flush
SERIES	12

SEE NOTE TABLE 10

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### 5 WPPM Ejection Test Results

ReL x10-6	6.011 6.011 6.011
TEMPERA- TURE T(OF)	79 79
BODY VELOCITY (FT/SEC)	27.05 27.05 27.05
EJECIED CONCEN- TRATION (WPPM)	יט וט ע
RMS CONCEN- TRATION RATIO C/CI	.378 .378 .260
MEASURE- MENT STATION ×/L	.120 .240 .360
NO. OF TFSTS	5
PROBE HEIGHT	Flush
	13 13

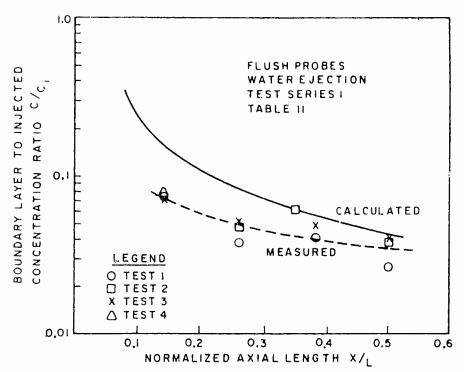
SEE NOTE TABLE 10

### Water Ejection Test Results

Figures 68, 69 and 70 display the data obtained in test series 1, 2 and 3 of Table 10. Referring first to Figure 10, it can be reticed that for this water diffusion case, the wall dye concentration has decreased to .1 of the ejected concentration in a distance of slightly less than one body diameter. The diffusion over the next nine inches of body length near halves again the concentration level. The diffusion process is quite rapid, characteristic of turbulent mass transport. The predicted curve on this figure applies the two zone diffusion boundary layer growth model combined with the axisymmetric boundary layer model as discussed earlier. The concentration similarity profiles for water were applied for the two-zone process quite successfully.

Figure 69 displays the data from the series 2 experiment with the .025 inch probes sampling the boundary layer. Again, comparison with the model for the water case seems quite good. Although not apparent in the data, the computer solutions shows the concentration growth prior to the sampling station and then a normal decay as the dye diffuses outward in the boundary layer.

Figure 70 displaying series 3 tests with water ejection and the .055 inch probes, the rise in the concentration levels between the first and second probe stations is evident in the data and predicted by the theory.



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Figure 68. Boundary layer to injected concentration ratio vs normalized axial length Test Series 1

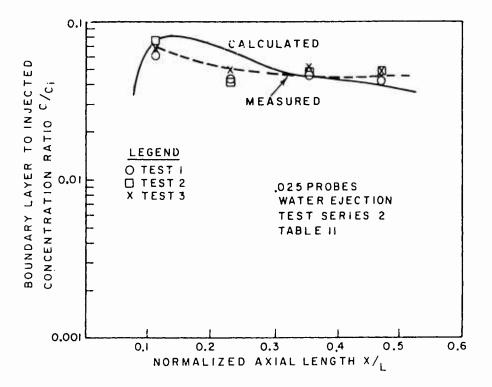
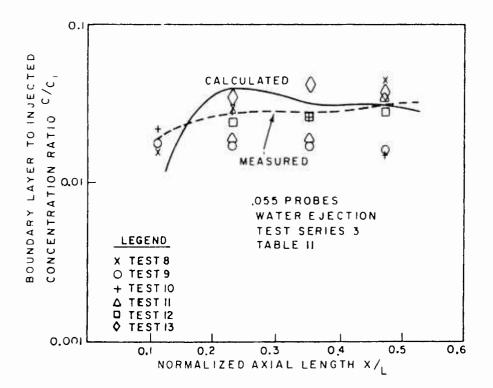


Figure 69. Boundary layer to injected concentration ratio vs normalized axial length Test Series 2



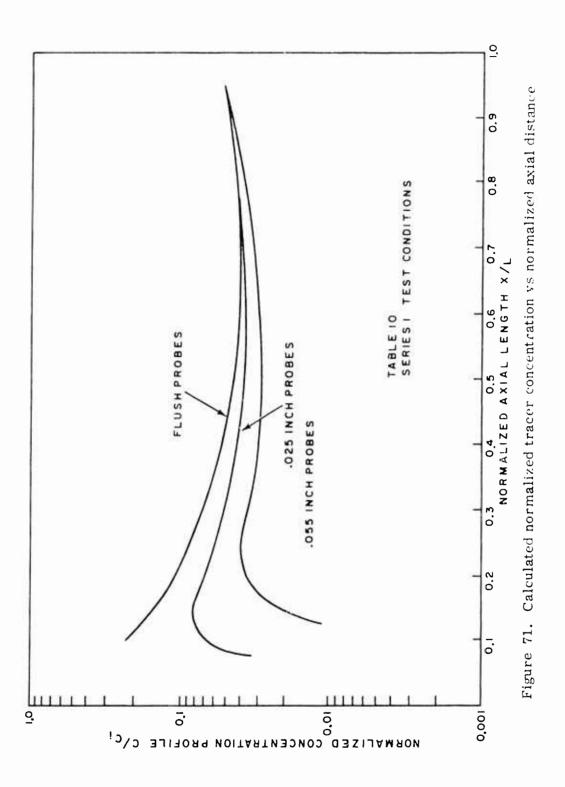
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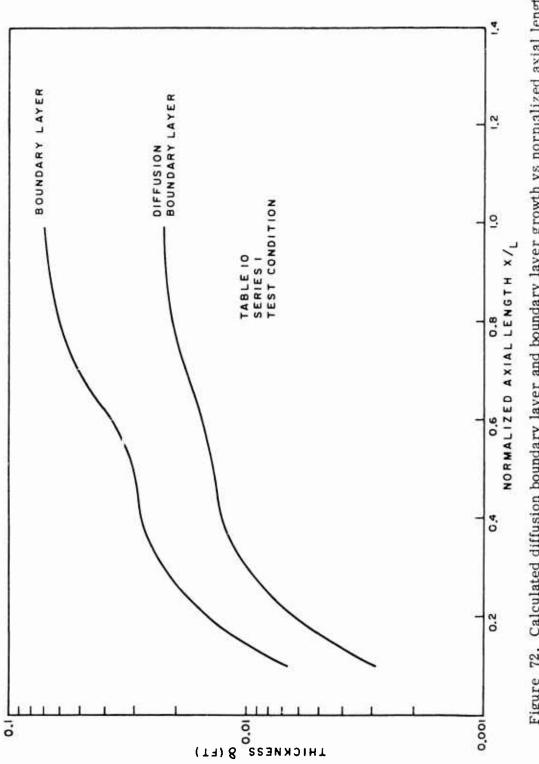
Figure 70. Boundary layer to injected concentration ratio vs normalized axial length Test Series 3

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Figure 71, a composite plot of the calculated flush, .025-inch and .055-inch probes displays an interesting result. First, the increase in concentration initially for the probes away from the wall is evident. The decay in concentration as the fluorescent dye diffuses outward is as expected in the approximately constant diameter section. At x/L of approximately .6, however, the concentration ratio begins to increase. The boundary layer in this region is growing very rapidly as both the photograph for this case, Figure 53 and the calculated and measured boundary layers indicate, Figure 60. The cause of this rise is the decreasing diameter resulting in a smaller boundary layer flux area within which the tracer resides. This is a rather interesting result since in external flows one would expect a uniform decrease in concentration with length due to boundary layer growth, Figure 72 displays the growth of the diffusion boundary layer, defined as height at which the concentration is .5 of the wall concentration, within the normal boundary layer. The growth of the diffusion boundary layer is reduced as compared to the normal boundary layer in the tail region, x/L > .6.

Figure 73 displays a plot of the concentration profile for the first two probe stations normalized to the wall concentration. The remaining two stations were not plotted since only the .055 probe height gave a value of  $C/C_w$  different from one. A single point curve would have resulted. Table 18 provides a tabulation of the experimental data used in generating this figure. As noted in the







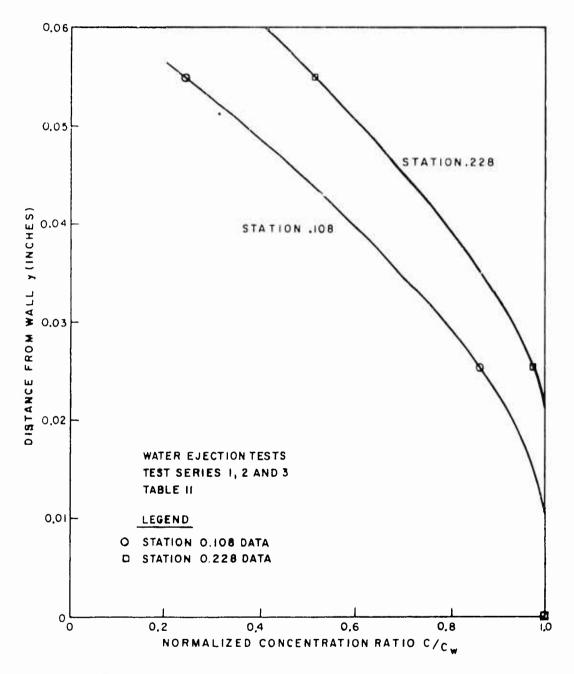


Figure 73. Distance from wall vs normalized concentration ratio water case

# TABLE 18

					БТАТ	JON			
		.108		.228		.348		.468	
y (IN	)	c/c <sub>i</sub>	c∕c <sub>w</sub>	c/c <sub>i</sub>	C/Cw	c/c <sub>i</sub>	C/Cw	C/Ci	c/c <sub>w</sub>
Water	0	.082	1	.051	1	.041	1	.035	1
	.025	.07	.854	.051	1.48	.045	1	.045	1
	.055	.019	.23	.027	.53	.028	.68	.031	.88
50 WPPM	0	. 49	1	.42	1	.406	1	.48	1
	.025	.05	.102	.075	.178	.088	.216	.095	.2
	.055	.01	.02	.012	.028	.013	.032	.034	.07
500 WPPM	0	.45	1	. 45	1	.48	1	.57	1
	.025	.023	.05	.034	.076	.047	.1	.057	.1
	.055	.001	.002	.01	.02	.02	.042	.022	.04

# Concentration Profile Determination (Using Smoothed Profile)

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figure, the diffusion process is quite rapid with wall concentration being approached quite far out into the boundary layer a short distance back on the body. By defining the diffusion boundary layer thickness as that value of y at which  $C/C_w$  equals .5, a normalization height is determined for plotting this data on a similarity concentration profile plot. Table 19 presents these data, along with data from subsequent tests with polymers. A comparison of these data (water case) with that from other experimentators is done on the similarity profile plot of Figure 74. The dotted line on this figure taken from Hsu (1971) has been generated from data by Poreh and Cermak (1964) and verified by Wetzel and Ripkin (1970). The equation for this line is as shown on the figure. The limited data obtained in this experiment verify, for the axisymmetric case, the applicability of this similarity profile for the downstream region. The water ejection line, although falling slightly higher resulting in a higher value of the exponent in the  $C/C_w$  relation, is in good agreement with the previous investigation. The applicability of the model in predicting the wall concentration and concentration profiles in the boundary layer seems apparent.

## Polymer Ejection Test Results

Figures 75, 76 and 77 display the data obtained in test series 4, 5 and 6 of Table 12. In this series, 50 WPPM polymer concentration was ejected. The results were not as expected. At all probe stations the polymer concentration remained high indicating no diffusion occurring. As may be seen in Figure 75, the combined model

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			1	
	y/8d		2.79 1.38 .723 .298	2.6 1.37 .68 .28
.468	Y		.0263 .013 .0068 .0028	.0153 .0081 .0004 .0016
	δđ		.0094 .0094 .0094 .0094 .0094	.0059 .0059 .0059 .0059 .0059
	y/ôd		2.79 1.38 .723 .298	2.6 1.37 .68 .28
.348	У		.0263 .013 .0068 .0028	.0153 .0081 .0004 .0016
N 0 I	Pγ		4000. 4000. 4000. 4000.	.0059 .0059 .0059 .0059
STAT	y/ôd	1.09 .89 .68	.275 1.375 .712 .275	2.7 1.38 .69 .27
. 228	У	.0625 .0510 .039	.022 .011 .0057 .0022	.014 .0072 .0036 .0014
	Ρŷ	.057 .057 .057 .057 .057	.008 .008 .008 .008 .008	.0052 .0052 .0052 .0352 .0352
	y/ôd	1.09 .89	18 2.76 1.42 .67 .25	2.7 1.45 .65
108	y	.048 .039 .029	.1 .0152 .0078 .0037 .0014	.012 .0064 .0029 .001
	þđ	044 044 044 044 044	.0055 .0055 .J055 .J055 .0055	.0044 .0044 .0044 .0044 .0044
c/c	*	.1 .2 .4 .6 .8	.1 .2 50 .4 WPPM .6	.1 .2 500 .4 WPPM .6

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TABLE 19 Normalized Concentration Profile for Several Concentration Ratios

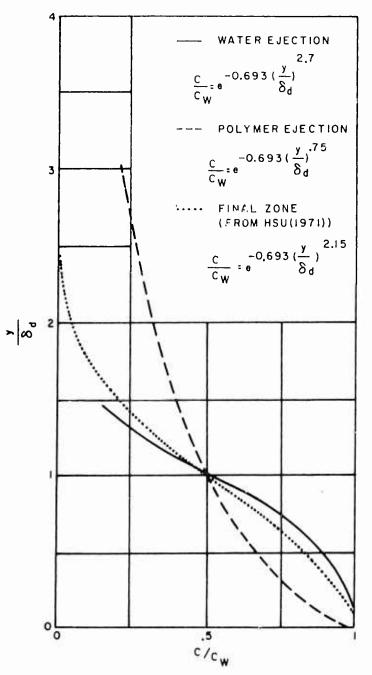


Figure 74. Concentration profiles determined for water and polymer ejection

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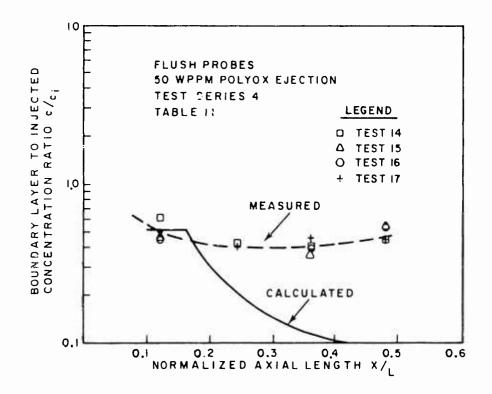


Figure 75. Boundary layer to injected concentration ratio vs normalized axial length Test Series 4

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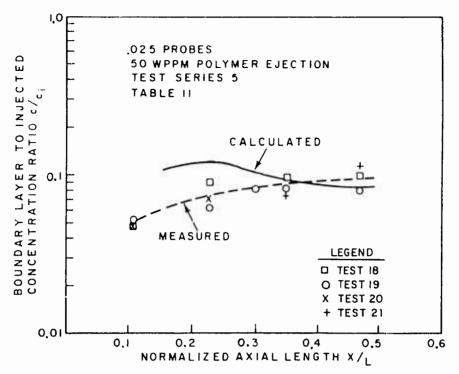
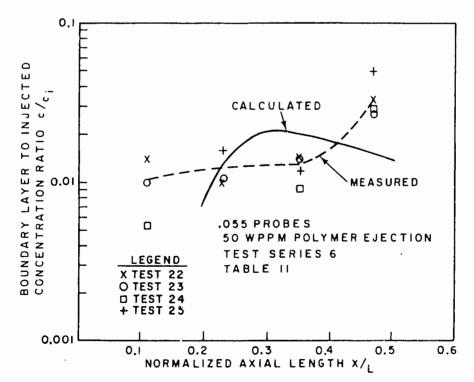


Figure 76. Boundary layer to injected concentration ratio vs normalized axial length Test Series 5



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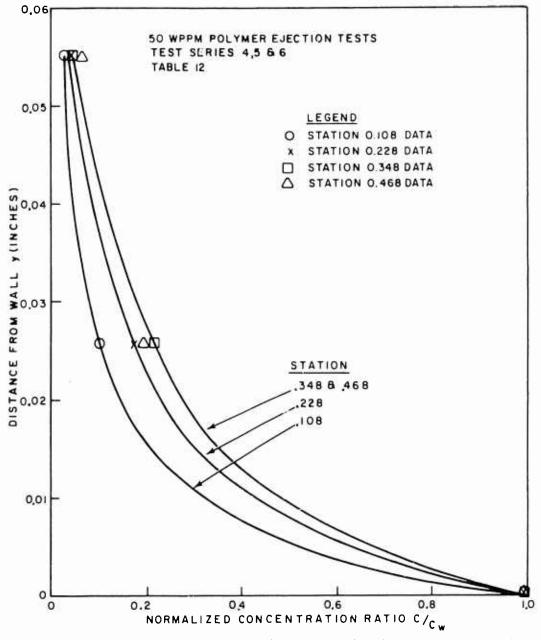
Figure 77. Boundary layer to injected concentration ratio vs normalized axial length Test Series 6

predicts a short initial zone. Figures 76 and 77 show the concentration measured with the .025-inch probes and the .055-inch probes. The experimental data display a slow build up of the concentration. The .055-inch probes which should be well outside the sublayer, display much scatter expecially at the first station. Apparently there is diffusion from the surface of the viscous layer otherwise the measured value would be much lower. The calculations do not account for diffusion from the viscous layer. There may still be some bursting occurring at this concentration level as some of the polymer in the ejection process is being hurled to regions further from the wall. The calculated values displayed in this figure show the characteristic rise and fall off of the rapid diffusion process as is predicted by the intermediate and final zone models. Figure 77 shows a sudden rise in the data at the last measurement station. Quite possibly, the end of the initial zone is being reached and the more rapid diffusion is beginning to occur.

Table 18 summarizes the concentration profile data taken for the 50 WPPM case from which Figure 78 is plotted. This figure displays the totally changed character of the concentration profile from the water case, Figure 73. Comparing,  $\delta_d$ , the value of y at  $C/C_w$  equal to .5, for the water case  $\delta_d$  is .044 inches at the first measurement station, while for the 50 WPPM case it is .0055 inches. (nearly a factor of 10 difference). Table 19 presents the data taken from Figure 78 from which a redefinition of the distance from the

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Figure 78. Distance from wall vs normalized concentration ratio 50 WPPM case

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wall, y, to a nondimensional distance,  $y/\delta_d$ , is made. This nondimensional height is plotted in Figure 74 and a curve fit made. The result, is a similarity profile with an exponent of .75 for all measurement stations. This exponent implies significantly reduced diffusion but not to the level which the data display. The discrepancy lies in the fitting of the curve in Figure 78. Three points are available. These are at y = .025 inches, y = .055inches and y = 0 inches. Clearly, the curve could be drawn a number of ways which would significantly reduce the exponent value by reducing  $\delta_d$ . The information demonstrating low diffusion rate is contained in the wall concentration measurement, however, so no attempt was made to match the curves to the data through the computer routine. In fact, the variable K3 model which resulted in a steady wall concentration profile calculated an exponent value of about .15. Let it suffice that Figure 78 displays markedly reduced diffusion to that of water and recommend for future work that a probe be tested at .01-inch height. Another interesting facet of these tests were that the exponent did not change with measurement station. This implies that the diffusion rate does not change, in these tests, with downstream distance. Again this may be a function of the curve fit only since, unless only molecular diffusion is occurring, it would be expected that the diffusion rate would increase.

Figures 79, 80 and 81 present similar test results for the test series 7, 8 and 9 of Table 13. As can be seen in Figure 79, for the

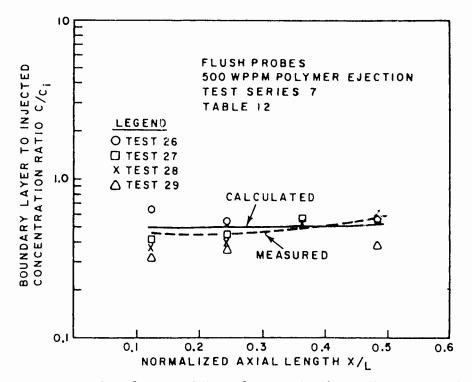


Figure 79. Boundary layer to injected concentration ratio vs normalized axial length Test Series 7

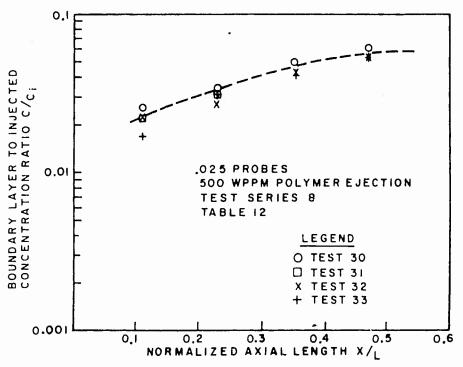


Figure 80. Boundary layer to injected concentration ratio vs normalized axial length Test Series 8

500 WPPM case, both the calculated and experimental data clearly indicate little diffusion is occurring. The .025-inch probes display the same gentle rise in concentration, Figure 80, as compared to the decay in concentration noted for the water case, Figure 69, resulting from the higher diffusion in that case. The .055-inch probes again display a slow rise with low levels indicative of low diffusion. It is interesting to note the scatter at the first station implying some anomaly in the ejection process. No calculations are evident for the concentration ratio in these probe figures since the molecular diffusion portion of the model does not incorporate a similarity concentration profile. The variable K3 model would account for this. Before turning to a concentration profile discussion, a test, test series 10, Table 14, was performed with 1000 WPPM ejected. Figure 82 displays the results. Again a nearly constant concentration with body distance results indicating little or no diffusion. This is not surprising considering the photographs taken showing the boundary layer structure, Figures 58 and 59.

The data for the 500 WPPM series have also been normalized for plotting as concentration ratio vs height, Table 18. Figure 83 displays this plot. Again an extremely low diffusion rate is evident compared to the water case, Figure 73. The 500 WPPM case is much steeper in profile than that of the 50 WPPM case, Figure 78, implying an even greater decrease in diffusion rate. Interestingly, wher. the height, y, is nondimensionalized with  $\delta_d$ , Table 19, the

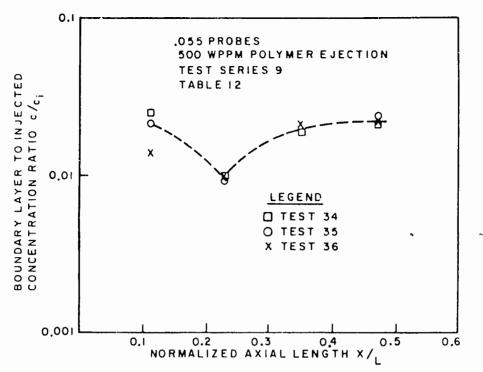


Figure 81. Boundary layer to injected concentration ratio vs normalized axial length Test Series 9

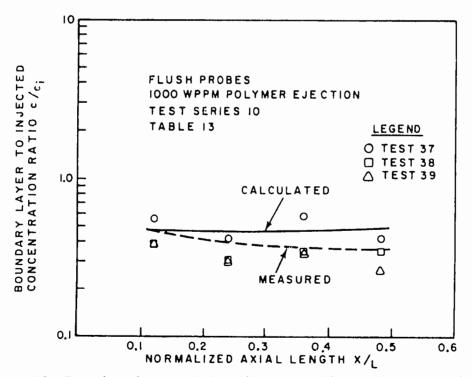


Figure 82. Boundary layer to injected concentration ratio vs normalized axial length Test Series 10

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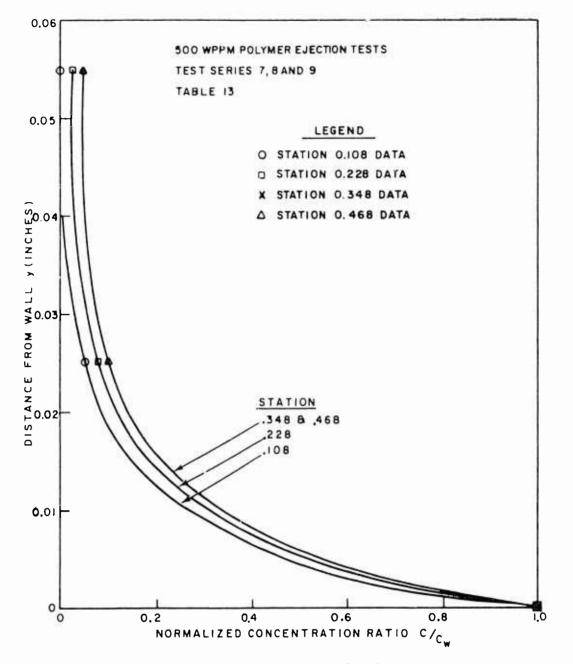


Figure 83. Distance from wall vs normalized concentration ratio 500 WPPM case

the similarity profile is the same as for the 50 WPPM case. The results are plotted in Figure 74 where the polymer ejection case applies to both the 50 WPPM and 500 WPPM test series. Again, the frailties of this plot are similar to those of Figure 78.

Additional tests were performed with reduced polymer concentrations in an attempt to define the position at which the initial diffusion zone terminated. These test results are displayed in Figure 84, for 20 WPPM polymer solution, Figure 85, 10 WPPM polymer solution and Figure 86, 5 WPPM polymer solution ejected. For both the 20 WPPM and 10 WPPM case, no drastic change to a higher diffusion rate is evident. The wall concentration to injected concentration ratio remaining about constant throughout the sampling region of the body. The 5 WPPM ejected concentration did display the result being sought. As shown in Figure 86, a definite reproducible shift to a lower concentration has occurred between the second and third sampling stations. From the flat plate data of Fruman and Tulin (1974) a projected transition to a higher diffusion process would have been projected to occur at concentration below 36 WPPM. These limited results indicate, for the axisymmetric case, a delay in transition to higher diffusion occurs at a significantly reduced concentration level.

The test series performed in this study may be compared directly with those of Fruman and Tulin (1974) if corrected for the axisymmetric influence by multiplying the concentration ratio by  $D_0/D_1$ . The

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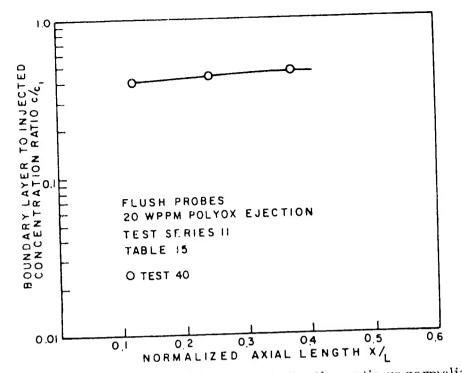
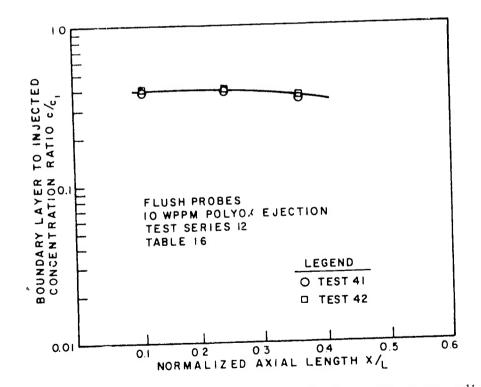


Figure 84. Boundary layer to injected concentration ratio vs normalized axial length Test Series 11



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Figure 85. Boundary layer to injected concentration ratio vs normalized axial length Test Series 12

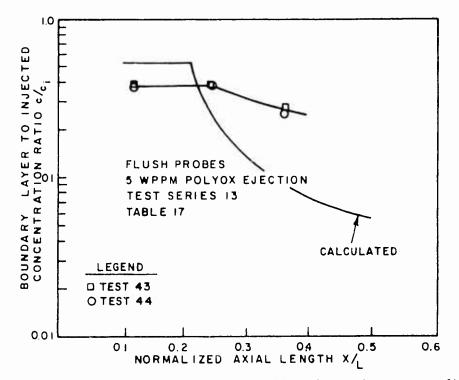
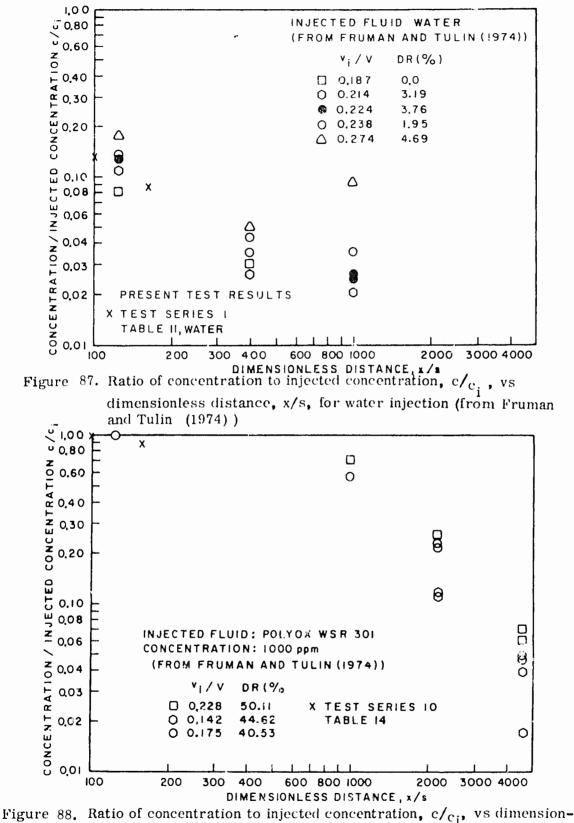
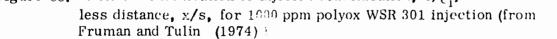


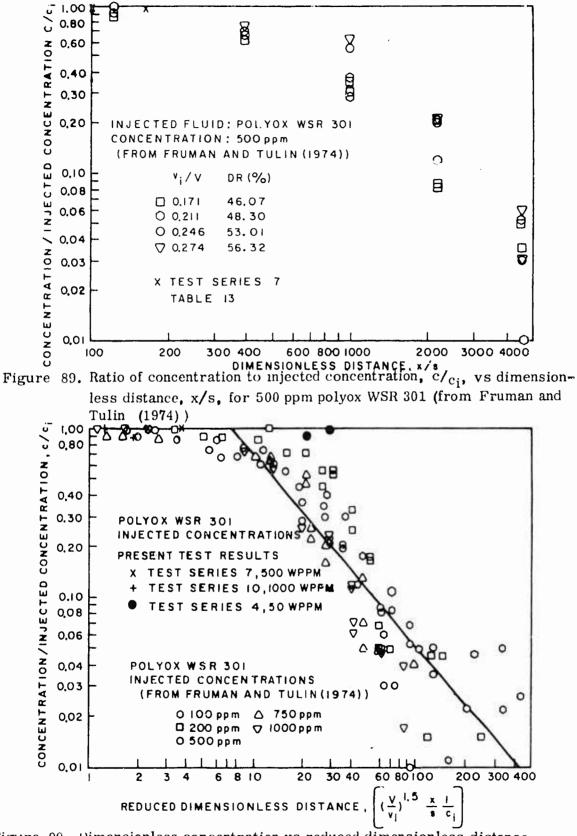
Figure 86. Boundary layer to injected concentration ratio vs normalized axial length Test Series 13

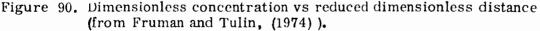
Reynolds pumber range for this test series was about 5 million whereas the Proposal and Tulin experiments were approximately 10 million. The ratio of ejection velocity to free stream velocity (body velocity in this case) is .185 in this study and ranges from .187 to .274 in the Fruman and Tulin experiments. Figure 87 displays a plot of the concentration to injected concentration ratio vs a dimensionless distance for a water ejected case taken from Fruman and Tulin (1974). The data from this experiment compare well. Similar plots for 1000 WPPM Figure 88, and 500 WPPM, Figure 89 show similar agreement. The data from this experiment are believed to be well qualified and displaying similar trends.

Figure 90, from Fruman and Tulin (1974), displays the departure from the initial zone of diffusion as was predicted from equation (96) from that reference. Data from this experiment are plotted on this figure. As is noted, all data for concentration fall in the initial zone region of molecular diffusion and have a corrected concentration ratio of about 1. The test series 4 data, 50 WPPM<sup>-</sup> case, falls to the right of the departure from the initial zone region. The reason is suspected to be that equation (96), which applies to slot ejection, should be modified to the case of ejection into the free stream and becoming a part of the laminar boundary layer. The ejection velocity becomes meaningless for this case and should be replaced with some other velocity which may be the mean laminar flow velocity or approximately .6 of the local









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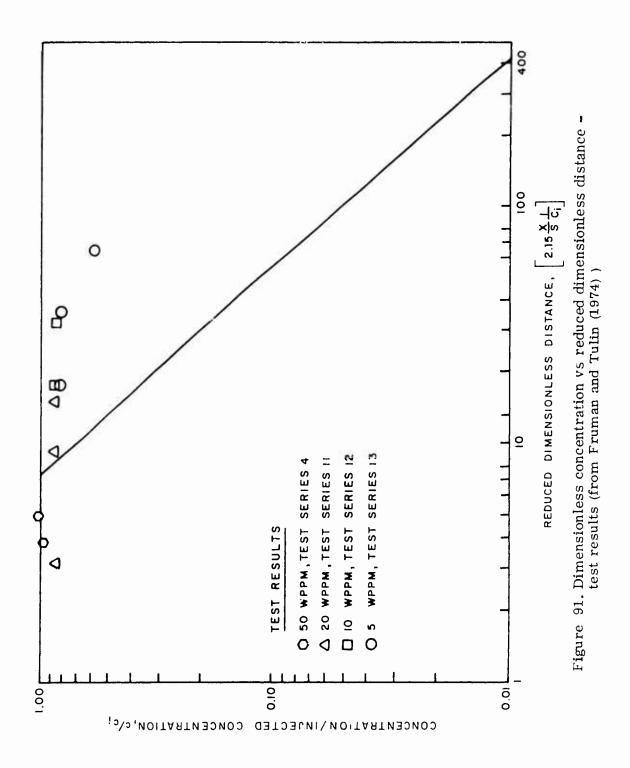
free stream velocity. For this case, equation (96) reduces to

2.15 
$$\frac{x}{s} = \frac{1}{C_1}$$
 (117)

For the 50 WPPM case, the reduced dimensionless distance for the 50 WPPM point would now be placed at 5.87 rather than near 30 where it presently is. In fact, all the points for the present test would shift to the left indicating a large initial length as the data indicate.

Figure 91 presents the corrected experimental data plotted against the modified dimensionless distance give by equation (117). The extended initial zone compared to the flat plate experiment is apparent in this figure. The analytical model was exercised for the condition of the test shown in Figure 86 with a transfer from the initial to intermediate zone occurring at 30. The dimensionless distance given by equation (117) was used to determine the change to the intermediate diffusion zone. The calculated values are displayed in Figure 86. As may be seen, the calculated intermediate zone diffusion process is much greater than the experimental data indicate warranting further study of this zone.

The extended initial zone for the ejection method applied is significant in that no special care is needed in the ejection process. Additionally, this ejection process most likely represents the optimal case since higher ejection velocities would quickly be reduced to the mean viscous sublayer velocity through viscous drag and, for a slot ejection case, could result in flow disruption.



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#### A. CONCLUSION

### 1. General

The object of this research was threefold: 1) to develop methods for wall concentration and drag reduction prediction for bodies of revolution with a polymer ejection process, 2) to qualitatively define the effects of polymer on boundary layers in external flows, and 3) to verify the predictive techniques by experiment. Drop tank testing was performed with several especially designed bodies of revolution. One of these bodies was capable of simultaneous ejection and boundary layer sampling at several heights in the boundary and at several axial stations. The ejection process for this model was considered optimal in that ejection occurred directly forward of the body in a laminar flow region thus affecting the developing flow region of turbulent flow. The experimental apparatus is capable of testing a wide variety of ejectors at different locations and over a range of Reynold's number to about 5 x  $10^6$ . Variable ejection rates and polymer concentrations may be applied as well as boundary layer sampling at selected heights and at the wall. The drop tank facility provided a very low turbulence level apparatus in which the external flow experiment could be carried out.

2. Analytical Prediction Methods

Much of the past work in the diffusion of polymer boundary layers

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has centered in the far downstream zone where the polymer attained the same diffusion characteristics as the medium. Postulates of an intermediate zone have been made but not reasonably tested for polymer cases. The case of developing flow with polymer ejection has received little attention for external flows and especially so for bodies of revolution. Predictive methods are, therefore, not well developed.

Several analytical models were developed for comparison with experimental data. The models were based upon a proven integral boundary layer analysis for thick axisymmetric boundary layers combined with a velocity profile relation accounting for pressure gradients. The models made use of a Lagrangian similarity hypothesis which predicts a diffusion boundary layer growth within the boundary layer. Two versions of the model are proposed but only one extensively used in the comparison. The first version, combined model, presently recommended as capable of accurate prediction of skin friction, polymer wall concentration and indicating total drag if provided with an experimental pressure profile, incorporates an initial diffusion zone where molecular diffusion is predomanate. Based upon a nondimensional distance, given by

$$\left(\frac{U}{v_{i}}\right)^{1.5} = \frac{X}{S} \frac{1}{C_{i}} = 8$$
 (96)

a change to an intermediate zone diffusion process is made. Within this region, determined by experimental data for ammonia diffusion in air to extend to  $X/\delta$  < 60, a similarity concentration profile exists having the form

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$$\frac{C}{C_{W}} = e^{-0.693 (y/\delta_d) K_3}$$

where the exponent is adjusted to a given value dependent on the region of diffusion. Proceeding to  $X/\delta > 60$  places the diffusion process in the final zone where the second value of K<sub>3</sub> is applied. The Lagrangian analysis provides for the determination of,  $\delta_d$ , the diffusion boundary layer. The equation for the diffusion boundary layer development incorporates the Karman constant, K, which is adjusted for the polymer flow case resulting in suppressed diffusion.

The analytical model has been compared to experimental data and found to predict proper levels of wall and concentration profiles but predicts an early increase in the diffusion process. It is hypothesized that the ejection velocity for the forward ejector, ejecting into the laminar region, is not the valid velocity for application into the nondimensional distance relation  $(v_i)$ . A mean laminar velocity is believed to be the correct velocity for this ejection process. When applied, the predictive techniques properly reproduces the experimental data. Unfortunately, only limited data are available displaying the initiation of the intermediate diffusion zone.

The second postulated model, the variable  $K_3$  model, eliminates the need for the molecular diffusion portion of the previous model and adjusts,  $K_3$ , as a function of  $\delta$ ,  $\delta_d$ , x/L, and  $c_w$  to account for this region. Unfortunately, insufficient data were available to perfect this model. A simplified functional relationship of  $K_3$  was found to predict the limited experimental data

$$K_3 = C K_5 \frac{\delta d}{\delta} \frac{x}{L} \cdot$$

The combined model is considered valid for use in prediction of various flow parameters for axisymmetric bodies of revolution. The model should be exercised in several ways depending on the ejection process. If ejection occurs prior to or at the point of transition to turbulent flows, the full model should be applied. If the ejector is placed in a region of a developed turbulent boundary layer, the initial zone should be eliminated and the Karman constant reduction removed.

#### 3. Boundary Layer Characterization and Separation Tests

Several test bodies were applied in this series of experiments covering a Reynolds number range of one to five million. One series of tests were conducted in a polymer ocean, where the drop tank was uniformly mixed to a polymer concentration level of 1.23, 2.5, 5, 10, 20, 50, and 60 WPPM using Polyox-WSR-301 polymer. In this series, models having  $6^{\circ}$  tail cone,  $12^{\circ}$  tail cone, and a spherical tail were tested. The photographic study displayed several interesting results. The turbulent nature of the boundary layer was apparent from the dye aspirated from these bodies at the minimum pressure point. At very low concentration levels, 2.5 WPPM, the fine structure turbulence was absent and only the large scale turbulence remained. At higher concentration, extreme boundary layer thinning occurred. Measurements of the boundary layer thickness were made from photographs and compared to computer predictions. The computer routines predicted the proper boundary layer growth shape for these tests but tended to overpredict the thickness. This was probably due to the mean height of the eddies being used for measurement purposes.

No shift in the boundary layer separation region was noted by application of the polymer. This was undoubtedly due to the large adverse pressure gradient conditions for these tail configurations. Computer predictions also indicated no shift in separation point for the test conditions.

The testing in fresh water with the polymer ejection body showed similar results but provided much better visual representations at the higher polymer concentrations. The characteristic coarse and fine scale turbulence was noted on dyed water ejection. Ejection of 50 WPPM dyed polymer solution eliminated most of the fine structure turbulence leaving only the coarse structure and somewhat the rapid boundary layer growth in the tail region. Application of 500 WPPM and 1000 WPPM of ejected polymer resulted in extremely thin boundary layers, even in the tail region with little evidence of turbulent action. In the tail region, bursting of the eddy structure is evident but with very low energy levels as evidenced by their vectors being in a near axial direction.

At the higher concentration levels, dye streaking is apparent. The streaking spacing is consistent with laminar sub layer streaks but also, for this case, agrees well with the number of ejection holes in the screen ejector in the nose of the body. In any event, turbulent mixing is not apparent at the 500 WPPM and 1000 WPPM concentrations. Boundary layer measurements were made for each case tested. A normalization of the thickness measurements shows an increased rate of growth for all concentrations tested, in the tail region. This suggests higher diffusion rates lowering the wall concentrations and reducing the subdued growth in this region.

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### 4. Drag Reduction Tests

Drag reduction tests were performed with the  $6^{\circ}$ ,  $12^{\circ}$ , and spherical tail bodies in a polymer ocean. The concentration levels were as discussed previously. A total drag reduction of 33% was achieved with the  $6^{\circ}$  tail body at polymer concentrations of 20 WPPM and greater. This compared favorably, within 10% of calculated values. Percent skin friction reduction of near 70% were achieved, comparing well with optimal total shear drag reduction for flat plates as determined by other investigators. The maximum total drag reduction achieved with the  $12^{\circ}$ tail and spherical tail bodies was less due to the reduced surface area and, therefore, increased percentage of form drag. Maximum total drag reductions of 16% and 10% were achieved respectively for the 12° tail and spherical tail configuration. The skin friction reduction remained near 70% as it should. Computer predictions for total drag with the  $12^{\circ}$  and spherical tail models was considerably in error due to the very large pressure coefficients predicted near the separation region for these cases from potential flow.

### 5. Polymer Diffusion Tests

The polymer ejecting body was applied for all tests with a fixed ejection rate of 20.6 in<sup>3</sup>/sec and nominal velocity of 27 ft/sec. Wall samples and boundary layer samples at .025 inches and .055 inches were taken and analyzed applying a fluorometric technique. Testing with water ejection and 5 WPPM, 10 WPPM, 20 WPPM, 50 WPPM, 500 WPPM, and 1000 WPPM were performed. The water tests compared well with available predictive methods displaying appropriate concentration profiles as

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achieved by other investigators. The tests with all polymer concentrations displayed an unexpected drastically reduced diffusion resulting in a considerably extended initial mixing zone. Application of a molecular diffusion model in this region agrees well with data. Boundary layer concentration profile data when plotted nondimensionally as  $y/\delta_d$  vs c/c result in similarity profile exponent coefficients,  $K_3$ , of .75. It is believed, however, the value is below this since data were not obtained in the critical region of approximately .01 inches from the wall in these tests. These results are significant in that they imply significantly reduced polymer quantities may be required with proper ejection techniques. Apparently ejection into the laminar, and in this case stagnation region, of developing flow substantially reduces the turbulence levels associated with turbulent flow and reduces, therefore, diffusion. It is believed that ejection in a developed flow would result in an extremely short initial zone and rapid mixing.

## 6. Conclusion Summary

An experimental apparatus has been developed which allows laboratory measurement of polymer drag reduction wall concentration profiles and ejector geometries at various ejection rates on axisymmetric bodies. Experiments have displayed reduced fine scale turbulence structure with polymer and a significantly reduced diffusion process if ejection is performed upstream of the turbulent transition point. Maximum skin friction reductions were achieved. Predictive methods were developed, building on available theories, for prediction of the wall concentration on an axisymmetric body. Comparison with experiment has been performed.

#### **B. RECOMMENDATIONS**

1. The variable K<sub>3</sub> analytical model should be developed to more adequately describe the diffusion process. As presently configured, the model abruptly changes from molecular diffusion to a diffusion process which is believed to be too high a rate for polymer. Application of the Lagrangian approach with modified Karman constant should provide an input to the functional relationship.

2. Additional data should be obtained at boundary layer heights below the .025-inch level with this experimental model. These data are required to adequately define the concentration curves and provide the data necessary for developing the  $K_3$  model. The variation in the similarity profile exponent,  $K_3$ , with axial length should also be defined by these data and would provide information on the intermediate and final zone similarity profile exponents.

3. Additional testing should be performed at lower concentration levels, below 50 WPPM, with the ejecting experimental model. This would clearly establish the extent of the initial mixing zone and verify the relation used for the extent of the initial zone and the hypothesis for the ejection velocity equaling a mean laminar velocity for the type of ejection process used here.

4. The experimental model should be modified for ejection into the established turbulent boundary layer region to clearly demonstrate the elimination (or drastic reduction) of the initial zone length with the

resulting high diffusion process. Significantly higher concentrations of polymers are believed to be required (higher flow rates and/or higher concentrations) for this case. Model modifications are extremely simple.

5. Drag reduction measurements should be made with this model during the ejection process. Correlations with wall concentration measurements and polymer ocean data would lend further credence to the results.

W. Sterner and Market

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#### APPENDIX A

### SKIN FRICTION RELATIONS

The conservation of mass and the momentum equation for axisymmetric flow are given by

$$\frac{\partial}{\partial \mathbf{x}} (\rho \mathbf{u} \mathbf{r}) + \frac{\partial}{\partial y} (\rho \mathbf{v} \mathbf{r}) = 0$$
 (A1)

and

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pur 
$$\left(\frac{\partial u}{\partial x}\right) + \rho vr \left(\frac{\partial u}{\partial y}\right) = -r \left(\frac{dp}{dx}\right) + \frac{\partial}{\partial y}(r\tau)$$
. (A2)

White's derivation is reproduced here to show the incorporation of the polymer concentration terms.

Defining a stream function which satisfies equation (Al) to eliminate  $\boldsymbol{v}$ 

$$\frac{\partial \Psi}{\partial y} = \rho u r \qquad \qquad \frac{\partial \Psi}{\partial x} = -\rho v r . \tag{A3}$$

Solving (A3) for  $\Psi$  yields

$$\Psi = \int_{y_0}^{y} \rho ur \, dy \,. \tag{A4}$$

Rewriting in law of the wall variables

$$\Psi = \int_{y_0^+}^{y_0^+} \rho r v u^+ dy^+ \qquad (A5)$$

or, in terms of  $Y^+$ 

A-1

$$\frac{\Psi}{\mu r_{0}} = \int_{0.1108}^{Y_{e}^{+}} \frac{(r_{0})^{2}}{(r_{0})^{2}} u^{+} dY^{+}$$
 (A6)

Writing equation (A2) in wall variables and substituting in equation (A3) to eliminate v

$$\rho \mathbf{r} \mathbf{v}^{\star} \mathbf{u}^{\dagger} \frac{\partial}{\partial \mathbf{x}} (\mathbf{v}^{\star} \mathbf{u}^{\dagger}) - \frac{\partial \Psi}{\partial \mathbf{x}} \frac{\mathbf{v}^{\star}}{\mathbf{v}} \frac{\partial}{\partial \mathbf{y}^{\dagger}} (\mathbf{v}^{\star} \mathbf{u}^{\dagger}) = -\mathbf{r} \frac{d\mathbf{p}}{d\mathbf{x}} + \frac{\mathbf{v}^{\star}}{\mathbf{v}} \frac{\partial}{\partial \mathbf{y}^{\dagger}} (\mathbf{r} \tau). \quad (A7)$$

The x derivatives must be handled by the chain rule, since each of the parameters  $(Y^+, \alpha, r_o^+, c_w)$  in the law of the wall is a function of x. Thus, we substitute

$$\frac{\partial}{\partial x} = \frac{\partial V}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial x} + \frac{$$

It is assumed throughout that  $\rho_W$  and  $\nu_W$  are constant in this analysis. Differentiating u

$$u = v^{*}(x) u^{+}(Y^{+}, \alpha, r_{o}^{+}, c_{w})$$
 (A9)

$$\frac{d(v \star u^{+})}{dx} = (u^{+} \frac{dv \star}{dx} + v \star \frac{\alpha Y^{+}}{dx} \frac{\partial u^{+}}{\partial Y^{+}} + v \star \frac{d\alpha}{dx} \frac{\partial u^{+}}{\partial \alpha} + v \star \frac{dr_{o}}{dx} \frac{\partial u^{+}}{\partial r_{o}} + v \star \frac{dC_{w}}{dx} \frac{\partial u^{+}}{\partial C_{w}})$$
(A10)

$$\frac{\partial(\Psi)}{\partial \mathbf{x}} = \frac{dY^{+}}{dx} \frac{\partial\Psi}{\partial Y^{+}} + \frac{d\alpha}{dx} \frac{\partial\Psi}{\partial \alpha} + \frac{dr_{o}^{+}}{dx} \frac{\partial\Psi}{\partial r_{o}^{+}} + \frac{dC_{w}}{dx} \frac{\partial\Psi}{\partial C_{W}}.$$
 (A11)

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Substituting in (A7)

$$\rho \mathbf{r} \mathbf{v}^{\star} \mathbf{u}^{\dagger} \left(\mathbf{u}^{\dagger} \frac{d\mathbf{v}^{\star}}{d\mathbf{x}} + \mathbf{v}^{\star} \frac{d\mathbf{Y}^{\dagger}}{d\mathbf{x}} \frac{\partial \mathbf{u}^{\dagger}}{\partial \mathbf{Y}^{\dagger}} + \mathbf{v}^{\star} \frac{d\mathbf{u}}{d\mathbf{x}} \frac{\partial \mathbf{u}^{\dagger}}{\partial \mathbf{a}} + \mathbf{v}^{\star} \frac{d\mathbf{r}^{\dagger}}{d\mathbf{x}} \frac{\partial \mathbf{u}^{\dagger}}{\partial \mathbf{r}^{\dagger}} \right)$$

$$+ \mathbf{v}^{\star} \frac{d\mathbf{C}_{\mathbf{w}}}{d\mathbf{x}} \frac{\partial \mathbf{u}^{\dagger}}{\partial \mathbf{C}_{\mathbf{w}}} - \frac{\mathbf{r}_{\mathbf{o}}}{\mathbf{r}} \frac{\mathbf{v}^{\star 2}}{\mathbf{v}_{\mathbf{w}}} \frac{\partial \mathbf{u}^{\dagger}}{\partial \mathbf{Y}^{\dagger}} \left(\frac{d\mathbf{Y}^{\dagger}}{d\mathbf{x}} - \frac{\partial \Psi}{\partial \mathbf{Y}^{\dagger}} + \frac{d\mathbf{u}}{d\mathbf{x}} \frac{\partial \Psi}{\partial \mathbf{u}} \right)$$

$$+ \frac{d\mathbf{r}_{\mathbf{o}}^{\dagger}}{d\mathbf{x}} \frac{\partial \Psi}{\partial \mathbf{C}_{\mathbf{w}}} - \frac{\mathbf{r}_{\mathbf{o}}}{\mathbf{v}} \frac{\mathbf{v}^{\star 2}}{\mathbf{v}_{\mathbf{w}}} \frac{\partial \mathbf{u}^{\dagger}}{\partial \mathbf{Y}^{\dagger}} \left(\frac{d\mathbf{Y}^{\dagger}}{d\mathbf{x}} - \frac{\partial \Psi}{\partial \mathbf{Y}^{\dagger}} + \frac{d\mathbf{u}}{d\mathbf{x}} \frac{\partial \Psi}{\partial \mathbf{u}} \right)$$

$$+ \frac{d\mathbf{r}_{\mathbf{o}}^{\dagger}}{d\mathbf{x}} \frac{\partial \Psi}{\partial \mathbf{r}_{\mathbf{o}}^{\dagger}} + \frac{d\mathbf{C}_{\mathbf{w}}}{d\mathbf{x}} \frac{\partial \Psi}{\partial \mathbf{C}_{\mathbf{w}}} = -\mathbf{r} \frac{d\mathbf{p}_{\mathbf{e}}}{d\mathbf{x}} + \frac{\mathbf{r}_{\mathbf{o}}}{\mathbf{r}} \frac{\mathbf{v}^{\star}}{\mathbf{v}_{\mathbf{w}}} \frac{\partial(\mathbf{r}\tau)}{\partial \mathbf{Y}^{\dagger}} .$$

$$(A12)$$

Terms (a) and (b) cancel using equation (A6). Multiplying out, cross multiplying by  $r/r_o^2$  and integrating with respect to  $Y^+$  gives

$$\rho \mathbf{v} \star \frac{d\mathbf{v} \star}{d\mathbf{x}} \int_{0}^{\mathbf{r}_{e}^{+}} \frac{\mathbf{r}_{2}^{2}}{\mathbf{r}_{0}^{2}} u^{+2} d\mathbf{Y}^{+} + \rho \mathbf{v} \star^{2} \frac{d\alpha}{d\mathbf{x}} \int_{0}^{\mathbf{r}_{e}^{+}} \frac{\mathbf{r}_{2}^{2}}{\mathbf{r}_{0}^{2}} u^{+} \frac{\partial u^{+}}{\partial \alpha} d\mathbf{Y}^{+}$$

$$+ \rho \mathbf{v} \star^{2} \frac{d\mathbf{r}_{0}^{+}}{d\mathbf{x}} \int_{0}^{\mathbf{r}_{e}^{+}} \frac{\mathbf{r}_{2}^{2}}{\mathbf{r}_{0}^{2}} u^{+} \frac{\partial u^{+}}{\partial \mathbf{r}_{0}^{+}} d\mathbf{Y}^{+} + \rho \mathbf{v} \star^{2} \frac{d\mathbf{c}_{w}}{d\mathbf{x}} \int_{0}^{\mathbf{r}_{e}^{+}} \frac{\mathbf{r}_{2}^{2}}{\mathbf{r}_{0}^{2}} u^{+} \frac{\partial u^{+}}{\partial \mathbf{c}_{w}} d\mathbf{Y}^{+}$$

$$- \frac{\mathbf{v} \star^{2}}{\mathbf{r}_{0}^{-} \mathbf{v}_{w}} \frac{d\alpha}{d\mathbf{x}} \int_{0}^{\mathbf{r}_{e}^{+}} \frac{\partial u}{\partial \alpha} \frac{\partial u}{\partial \mathbf{v}^{+}} d\mathbf{Y}^{+} - \frac{\mathbf{v} \star^{2}}{\mathbf{r}_{0}^{-} \mathbf{v}_{w}} \frac{d\mathbf{r}_{0}^{+}}{\mathbf{r}_{0}^{-}} \frac{\partial \Psi}{\partial \mathbf{r}_{w}^{+}} \frac{\partial u^{+}}{\partial \mathbf{r}_{v}^{+}} d\mathbf{Y}^{+}$$

$$- \frac{\mathbf{v} \star^{2}}{\mathbf{r}_{0}^{-} \mathbf{v}_{w}} \frac{d\alpha}{d\mathbf{x}} \int_{0}^{\mathbf{r}_{e}^{+}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial \mathbf{r}_{v}^{+}} d\mathbf{Y}^{+} = - \frac{d\mathbf{p}}{\mathbf{r}_{0}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{0}^{-}} \frac{\partial \Psi}{\mathbf{r}_{v}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{w}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{w}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{w}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{w}^{-}} \frac{d\mathbf{r}_{v}^{+}}{\mathbf{r}_{v}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{v}^{-}} \frac{d\mathbf{r}_{v}^{+}}{\mathbf{r}_{v}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{w}^{-}} \frac{\mathbf{v}}}{\mathbf{r}_{w}^{-}} \frac{\mathbf{v}}{\mathbf{r}_{w}^{-$$

Where the integral of the last term is  $-\frac{v^*}{v}r_{ow}\tau$  and the term

$$\frac{dp_{e}}{dx} \int_{0}^{Y^{+}} (\frac{r}{r_{o}})^{2} dY^{+} = -\rho_{w} U_{e} \frac{dU_{e}}{dx} \int_{0}^{Y^{+}} (\frac{r}{r_{o}})^{2} dY^{+}$$
(A14)

A-3

may be simplified by substituting in  $e^{2Y^+/r_0^+}$  for  $(\frac{r}{r_0})^2$  and integrated resulting in

$$-\rho_{w} U_{e} \frac{dU_{e}}{dx} \frac{r_{o}^{+}}{2} (e^{-1}).$$
 (A15)

Rearranging (A13) yields  

$$\rho v \star \frac{dv \star}{dx} \int_{0}^{v_{e}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+^{2}} dY^{+} + \rho v \star \frac{d\alpha}{dx} \int_{0}^{v_{e}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial \alpha}$$

$$- \frac{1}{\rho v r_{o}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} dY^{+} + \rho v \star^{2} \frac{dr_{o}^{+}}{dx} \int_{0}^{v_{e}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial r_{o}^{+}}$$

$$- \frac{1}{\rho v r_{o}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} dY^{+} + \rho v \star^{2} \frac{dc_{w}}{dx} \int_{0}^{v_{e}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial r_{o}^{+}}$$

$$- \frac{1}{\rho v r_{o}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} dY^{+} + \rho v \star^{2} \frac{dc_{w}}{dx} \int_{0}^{v_{e}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial c_{w}^{+}}$$

$$- \frac{1}{\rho v r_{o}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} dY^{+} + \rho v \star^{2} \frac{dc_{w}}{dx} \int_{0}^{v_{e}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial c_{w}^{+}}$$

$$- \frac{1}{\rho v r_{o}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} dY^{+} = \rho U_{e} \frac{dU_{e}}{dx} \frac{r_{o}^{+}}{2} (e^{2Y^{+}/r_{o}^{+}} -1) - \frac{v \star}{v} \tau_{w}. \quad (A16)$$

Dividing by  $\rho$  and remembering that  $\rho\nu$  =  $\mu$  yields

$$\mathbf{v} \star \frac{d\mathbf{v} \star}{d\mathbf{x}} \mathbf{G}_{1} + \mathbf{v} \star^{2} \frac{d\alpha}{d\mathbf{x}} \mathbf{H} + \mathbf{v} \star^{2} \frac{d\mathbf{r}_{0}^{+}}{d\mathbf{x}} \mathbf{I} + \mathbf{v} \star^{2} \frac{d\mathbf{c}_{w}}{d\mathbf{x}} \mathbf{J}$$
  
=  $U_{e} \frac{dU_{e}}{d\mathbf{x}} \frac{\mathbf{r}_{0}^{+}}{2} (e^{2\mathbf{Y}_{e}^{+}/\mathbf{r}_{0}^{+}} -1) - \frac{\mathbf{v} \star}{\mathbf{v}} \tau_{w}$ . (A17)

A-4

$$\frac{\text{Where}}{G_1} = \int_{0}^{Y_e} \frac{2Y'}{r_o} + \frac{1}{u^2} \frac{1}{dY'}$$
(A18)

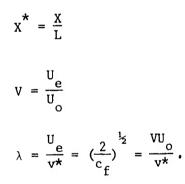
$$H = \int_{0}^{Y^{+}} \{e^{2Y^{+}/r_{0}^{+}} u^{+} \frac{\partial u^{+}}{\partial \alpha} - \frac{1}{\mu r_{0}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} \} dY^{+}$$
(A19)

$$I = \int_{0}^{Y_{e}^{+}} \{e^{2Y_{o}^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial r_{o}^{+}} - \frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial r_{o}^{+}} \frac{\partial u^{+}}{\partial Y^{+}} \} dY^{+}$$
(A20)

$$J = \int_{0}^{Y^{+}} \left\{ e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial c_{w}} - \frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial c_{w}} \frac{\partial u^{+}}{\partial Y^{+}} \right\} dY^{+}.$$
 (A21)

Defining dimensionless parameters

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Rewriting terms of equation (Al7) with these nondimensional parameters

$$\mathbf{v^*} = \frac{\mathbf{VU}}{\lambda} = \frac{\mathbf{U}}{\lambda}$$

$$\frac{1}{L}\frac{d\mathbf{v}^{\star}}{d\mathbf{x}^{\star}} = \frac{d(\underline{U}_{e}/\lambda)}{d\mathbf{x}^{\star}} = \frac{1}{L}\left(\frac{U}{\lambda}\frac{dV}{d\mathbf{x}^{\star}} - \frac{U}{\lambda^{2}}\frac{dV}{d\mathbf{x}^{\star}}\right)$$

$$\alpha = \left(\frac{v}{v}\frac{w}{v}\right) \frac{dP_e}{dx} = -\frac{v}{v}\frac{w}{v^*} \quad U_e \frac{dU_e}{dx}$$

$$\alpha = -\frac{v}{v}\frac{w}{v^*} \quad \lambda \frac{dU_e}{dx} = -\frac{v}{u}\frac{w}{v} \quad \lambda^3 \frac{dU_e}{dx} = -\frac{v}{u}\frac{w}{v} \quad \lambda^3 \frac{dV}{dx} = -\frac{v}{u}\frac{\lambda^3}{v} \frac{dV}{dx}$$
now  $R_0 = \frac{U_o L}{v}$ .

Therefore,

$$\alpha = - \frac{\lambda^3}{R_L V^2} \frac{dV}{dx^*}$$

but 
$$-\frac{1}{V^2}\frac{dV}{dx^*} = (\frac{1}{V})$$

where ' denotes first derivative with respect to  $x^*$ , resulting in

$$\alpha = \frac{\lambda^3}{R_L} \left(\frac{1}{V}\right)'.$$

Finally

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$$\frac{1}{L}\frac{d\alpha}{dx^{\star}} = \frac{1}{L} \begin{bmatrix} \frac{3\lambda^2}{R_L} & (\frac{1}{V})' & \frac{d\lambda}{dx^{\star}} + \frac{\lambda^3}{R_L} & (\frac{1}{V})'' \end{bmatrix}.$$

Substituting in (A-17)

$$\frac{U_{o}V}{L\lambda} \left(\frac{U_{o}}{\lambda}V' - \frac{U_{o}V}{\lambda^{2}}\frac{d}{dx^{*}}\right) G_{1} + \frac{V^{2}U^{2}}{L\lambda^{2}}\frac{3\lambda^{2}}{R_{r}} \left(\frac{1}{V}\right)' \frac{d\lambda}{dx^{*}}.$$

Multiply through by  $\lambda$  and rearranging setting  $\alpha = \frac{\lambda^3}{R_L} \left(\frac{1}{V}\right)'$ 

$$\frac{d\lambda}{dx^{\star}} (3\alpha H - G_1) + \frac{V}{V} \lambda G_1 - \frac{\lambda^2 r_0^{\star}}{2} (e^{-1})$$
(A22)

$$+ \frac{\lambda^{\prime 4}}{R_{L}} \left(\frac{1}{V}\right)^{\prime \prime} H = 1 R_{L} V - \lambda \frac{dr^{+}}{dx^{\star}} I - \lambda \frac{dc}{dx^{\star}} J \qquad (A22)$$

where G, H, I, J are given by

$$G_{1} = \int_{0}^{Y_{e}^{+}} e^{2Y_{o}^{+}/r_{o}^{+}} u^{+} dY^{+}$$
(A23)

$$H = \int_{0}^{Y_{e}^{+}} \left\{ e^{2Y_{o}^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial \alpha} - \frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial \alpha} \frac{\partial u^{+}}{\partial Y^{+}} \right\} dY^{+}$$
(A24)

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$$\frac{\partial u^{+}}{\partial \alpha} = \int_{0}^{Y^{+}} \frac{r_{o}^{+}}{4KY^{+} \left[1 + \frac{\alpha}{2} r_{o}^{+} \left(e^{-1}\right)\right]^{\frac{1}{2}}} dY^{+}$$
(A25)

$$\frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial \alpha} = \int_{0}^{Y^{+}} e^{2Y^{+}/r_{o}^{+}} \frac{\partial u^{+}}{\partial \alpha} dY^{+}$$
(A26)

and

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$$\frac{\partial u^{+}}{\partial Y^{+}} = \frac{1}{KY^{+}} 1 + \frac{\alpha}{2} r_{0}^{+} (e^{2Y^{+}/r_{0}^{+}} -1)^{\frac{1}{2}}$$
(A27)

$$I = \int_{0}^{Y_{e}^{+}} e^{2Y'/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial r_{o}^{+}} - \frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial r_{o}} \frac{\partial u^{+}}{\partial Y^{+}} dY^{+}$$
(A28)

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where  $\frac{\partial u^{+}}{\partial r_{o}^{+}} = \int_{0}^{Y_{e}^{+}} -\frac{1}{2KY^{+}} \frac{\left[-\frac{\alpha}{2} + \frac{\alpha}{2} e^{2Y^{+}/r_{o}^{+}} - \frac{\alpha Y^{+}}{r_{o}^{+}} e^{2Y^{+}/r_{o}^{+}}\right]}{\left[1 - \frac{\alpha}{2} r_{o}^{+} (1 - e^{-2Y^{+}/r_{o}^{+}})\right]} dY^{+}$ 

$$= \int_{0}^{Y_{e}^{+}} \frac{\alpha}{4\kappa Y^{+}} \frac{\left[(1 - e^{2Y^{+}/r_{o}^{+}}) + \frac{Y^{+}}{2r_{o}^{+}} + e^{2Y^{+}/r_{o}^{+}}\right]}{\left[1 + \frac{\alpha}{2}r_{o}^{+} + (e^{2Y^{+}/r_{o}^{+}} - \frac{1}{2})\right]} dY^{+}$$
(A29)

and

$$\frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial r_{o}^{+}} = \frac{\partial}{\partial r_{o}^{+}} \int_{0}^{Y^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} dY^{+}$$
$$= \int_{0}^{Y^{+}} \left\{ -\frac{2Y^{+}}{r_{o}^{+}} e^{2Y^{+}/r_{o}^{+}} u^{+} + e^{2Y^{+}/r_{o}^{+}} \frac{\partial u^{+}}{\partial r_{o}^{+}} dY^{+} \right\}$$
(A30)

$$J = \int_{0}^{Y^{+}} \left\{ e^{2Y^{+}/r_{o}^{+}} u^{+} \frac{\partial u^{+}}{\partial c_{w}} - \frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial c_{w}} \frac{\partial u^{+}}{\partial Y^{+}} \right\} dY^{+}$$
(A31)

where

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$$\frac{\partial u^{+}}{\partial c_{w}} = \frac{2.3}{2(c_{w})^{\frac{1}{2}}} \ln \frac{v^{*}}{v_{o}^{+}} = \frac{1.15}{c_{w}} \ln \frac{v^{*}}{v_{o}^{+}}$$
(A32)

and

$$\frac{1}{\mu r_{o}} \frac{\partial \Psi}{\partial c_{w}} = \int_{0}^{Y^{+}} e^{2Y^{+}/r_{o}^{+}} \frac{\partial u^{+}}{\partial c_{w}} dY^{+}.$$
 (A33)

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## APPENDIX B

# COMPUTER PROGRAM SAMPLES

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05.5     Distriction       05.5     Filter       05.5	05.5       0.5		
0.2.1     0.1.1     0.1.1     0.1.1     0.1.1       0.2.2     0.1.1     0.1.1     0.1.1       0.2.3     0.1.1     0.1.1     0.1.1       0.2.4     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5     0.1.1     0.1.1     0.1.1       0.2.5 <td>0.4.1     0.4.1     0.4.1     0.4.1       0.4.2     0.4.1     0.4.1       0.4.3     0.4.1     0.4.1       0.4.4     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.6     0.4.1     0.4.1       0.4.7     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1</td> <td></td> <td></td>	0.4.1     0.4.1     0.4.1     0.4.1       0.4.2     0.4.1     0.4.1       0.4.3     0.4.1     0.4.1       0.4.4     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.5     0.4.1     0.4.1       0.4.6     0.4.1     0.4.1       0.4.7     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1       0.4.1     0.4.1     0.4.1		
055     055     055       055     055     055       055     055     055       055     055     055       055     055     056       055     056     050       055     056     050       055     056     050       055     056     050       055     056     050       055     056     050       055     056     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       056     050     050       057     050     050       058     050     050       059     050     050       050     050     050       050     050	000000000000000000000000000000000000		τ.
05:0     1111       05:1     1111       05:1     1111       05:2     1111       05:3     1110       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:5     1100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0     100       05:0 </td <td>0000     0000       0000     0000    <t< td=""><td></td><td></td></t<></td>	0000     0000       0000     0000 <t< td=""><td></td><td></td></t<>		
0550     FULLE-FULK       0551     FULLE-FULK       0553     FULLE-FULK       0554     FULLE-FULK       0555     FULLE-FULK       0555     FULLE-FULK       0556     FULK       0557     FULK       0558     FULK       0559     FULK       0550     FULK       0551     FULK       0553     FULK       0554     FULK       0555     FULK       0556     FULK       0557     FULK       0558     FULK       0559     FULK       0551     FULK       0553     FULK       0554     FULK       0555     FULK       0556     FULK       0557     FULK       0558     FULK       0559     FULK       0511     FULK       055     FULK       0550     FULK       0511     FULK       0558     FULK       0559     FULK       0550     FULK       0551     FULK       0551     FULK       0551     FULK       0551     FULK       0551     FULK       0551<	0551     FTUGETERIA       0551     FTUGETERIA       0551     FTUGETERIA       0551     FTUGETERIA       0551     FTUGETERIA       0551     FTUGETERIA       0552     FTUGETERIA       0553     FTUGETERIA       0554     FTUGETERIA       0555     FTUGETERIA       0555     FTUGETERIA       0555     FTUGETERIA       0555     FTUGETERIA       0555     FTUGETERIA       0556     FTUGETERIA       0557     FTUGETERIA       0558     FTUGETERIA       0559     FTUGETERIA       0550     FTUGETERIA       0551     FTUGETERIA		
0550 FRUESCIVERIES FUNCTIONE 1000-06-110/11-1.000 1000-06-1100	0550     FTUESCIVENTER       0551     FTUESCIVENTER       0553     FTUESCIVENTER       0554     FTUESCIVENTER       0555     FTUESCIVENTER <t< td=""><td></td><td>1. In the second s</td></t<>		1. In the second s
0551       Treasence         0553       Treasence         0554       Treasence         0555       Treasence         0556       Del tao         0557       Del tao         0561       Doi 70 206         0561       Doi	0551       FFERENCE         0553       FFERENCE         0554       FFERENCE         0555       FFERENCE         0556       FFERENCE         0557       FFERENCE         0561       B070         0571       B070         0551       FFERENCE         0552       FFERENCE         0553       FFERENCE         0561       B070         0571       B070         0551       FFERENCE         0552       FFERENCE         0553       FFERENCE         0561       FFERENCE         0573       FFERENCE         0573       FFERENCE         0573       FFERENCE         0574       FFERENCE         0575       FFERENCE         0576       FFERENCE         0577		YPLUSC#YPLUS
7551     If the UNIT AT A TANK A	2551       FFEGRATIATION         2553       FFEGRATIATION         2554       FFEGRATIATION         2555       FELORETA         255       FELORETA         256       FELORETA <t< td=""><td></td><td></td></t<>		
0555       TETULERTITIE         0554       TETULERTITIE         0555       TETULERTITIE         0556       TETULERTITIE         0557       TETERSTE         0558       TETERSTE         0559       TETERSTE         0559       TETERSTE         0559       TETERSTE         0559       TETERSTE         0559       TETERSTE         0551       TETERSTE         0553       TETERSTE         0541       TETERSTE         0551       DELTERS         0552       TETERSTE         0553       TETERSTE         0564       TETERSTE         0555       TETERSTE         0565       TETERSTE	0555     TETELUSTIONE       0555     ATELENTIAL       0555     ATELENTIAL       0555     ATELENTIAL       0555     DELEGONELIOVE       0555     DELETAO       0555     DELET		
0533       XCHECKARITTIAL MARTIN         0555       XCHECKARITTIAL MARTIN         0557       XCHECKARITTIAL MARTIN         0557       MICEONER         0558       MICEONER         0559       MICEONER         0559       MICEONER         0550       MICEONER         0551       MICEONER         0553       MICEONER         0554       MICEONER         0555       MICEONER         0551       MICEONER         0553       MICEONER         0554       MICEONER         0555       MICEONER         0551       MICEONER         0553       MICEONER         0554       MICEONER         0555       MICEONER         0555       MICEONER         0556       MICEONER         0557       MICEONER         0571       MIC	0535       TCHERCHICKTONE         0555       TCHERCHICK         0556       TCHERCHICK         0557       TCHERCHICK         0558       TCHERCHICK         0559       TCHERCHICK         0550       TCHERCHICK         0551       TCHERCHICK         0552       TCHERCHICK         0553       TCHERCHICK         0554       TCHERCHICK         0555       TCHERCHICK	2020 N	
0554       XCHECKTRUTH       ATOL-ANLINATION         0255       XCHECKTRUTK       0010-06L10/K         0255       ATOL-ANLINATION       0010-06L10/K         0256       TriXX:IT.300.01 3070 200       0010 200         0261       VITCARFE COUNTON       0010 200         0263       VITLAR       0010 201         0264       VITLAR       0010 201         0265       VITLAR       0010 201         0266       VITLAR       0010 201         0266       VITLAR       0010 201         0267       VITLAR       0010 201         0271       DEPRIVIALSCAR       010 202         0272       DEPRIVIALSCAR       010 202         0273       DEPRIVIAL       010 201         0274       DEPRIVIAL       010 202         0274       DEPRIVIAL       010 201         0274       DEPRIVIAL       010 202         0274	655       XCHC+AKI (1) ALL       ACDC+AKI (1) ALL         675       XCHC+AKI (1) ALL       ACDC+AKI (1) ALL         675       Dit (1000) (100 - 100) (100		34 # # # # # # # # # # # # # # # # # # #
0555       AX10-mELIAVYE         0557       CFL0AMELIAVYE         0559       FXXX:TX.001 B0 TO 200         0550       TXXX:EFA.001 B0 TO 200         0550       DELTA-0         0551       TXXX:TX.01 B0 TO 200         0553       TXXX:TX.01 B0 TO 200         0550       DELTA-0         0551       DELTA-0         0552       DELTA-0         0553       DELTA-0         0554       DELTA-0         0555       DETTA-0         0556       DETTA-0         0557       DETTA-0         0558       DETTA-0         0579       DETTA-0         0571       DETTA-0         0571       DETTA-0         0571       DETTA-0         0571       DETTA-0         0571       DETTA-0         0571       DETTA-	2555       Artionactinover         2550       CLANALINALINATION         2551       CLANALINATION         2553       FLANALINATION         2554       TIXXIIIION         2555       TIXXIIIION         2550       TIXXIIIION         2551       DELTAD         2550       DELTAD         2551       DELTAD         2552       TIXXIIIION         2553       STEPOS         2551       DELTAD         2553       STEPOS         2554       STEPOS         2555       STEPOS         2551       STEPOS         2552       STEPOS         2553       STEPOS         2554       STEPOS         2555       STEPOS         2555       STEPOS         2555       STEPOS         2551		XCHECK# (XL (]+1)14570)/YE
0250       Dailorditiont         0251       Chonchine         0253       Principate         0254       Prixt.LT.30.00 60 TO 200         0255       Principate         0255       Principate         0255       Principate         0256       Prixt.LT.30.00 60 TO 200         0251       Prixt.LT.30.00 60 TO 200         0252       Prixt.LT.30.00 60 TO 200         0253       Prixt.LT.30.00 60 TO 200         0254       Prixt.LT.30.00 60 TO 200         0255       Prixt.LT.400         0255       Prixt.LT.400         0255       Prixt.LT.400         0256       Prixt.LT.400         0257       Prixt.LT.400         0258       Prixt.LT.400         0251       Prixt.LT.400         0252       Prixt.LT.400         0253       Prixt.LT.400         0251       Prixt.LT.400         0252       Prixt.LT.400         0253       Prixt.LT.400         0254       Prixt.LT.400         0257       Prixt.LT.400         0258       Prixt.LT.400         0259       Prixt.LT.400         0250       Prixt.LT.400         0251	0750       BATTOPECTALINYE         0757       C         1       INTEGRATE GUARTON 5 TO DETERMINE CU         0759       U         0751       UT (XX.IT'.30.0) 30 TO 200         0753       UT (XX.IT'.30.0) 30 TO 200         0753       UT (XI.0) 1100         0753       UT (XI.0) 1100         0753       UT (XI.0) 1100         0753       UT (XI.0) 201         0753       UT (XI.0) 1100         0753       UT (XI.0) 1100         0753       UT (XI.0) 1100         0753       UT (XI.0) 1100         0754       UT (XI.0) 1100         0755       UT (XI.0) 1100         0750       UT (XI.0) 1100         0751       UT (XI.0) 1100         0751 <td< td=""><td></td><td></td></td<>		
0557     DELADORELADITE       0558     TEXX.LT.30.0) 60 TQ 200       0559     TEXX.LT.30.0) 60 TQ 200       0551     TEXX.LT.30.0) 60 TQ 200       0553     TEXX.LT.30.0) 60 TQ 200       0554     DELLAD       0555     TEXX.LT.30.0) 60 TQ 200       0556     TEXX.LT.30.0) 60 TQ 200       0551     DELLAD       0552     DELLAD       0553     DELLAD       0554     DELLAD       0555     DELLAD       056     DELLAD       0571     DELLADOL       0573     DELLADOL       0574     DELLADOL       0575     DEVILLAD       0576     DELLADOL       0577     DELLADOL       0578     DELLADOL       0579     DELLADOL       0570     DELLADOL       0571     DELLADOL       0573     DELLADOL       0574     DELLADOL       0575     DELLADOL       0576     DELLADOL       0577     DELLADOL       0578     DELLADOL       0579     DELLADOL       0570     DELLADOL       0570     DELLADOL       0570     DELLADOL       0570     DELLADOL       0570     DELLA	0259     CELLBONCEL       0259     FF 17:30:01 00'10 266       0250     FF 17:30:01 00'10 266       0251     VITEGATE FOULTION 5 TO DETERMINE CN       0253     VITEGATE FOULTION 5 TO DETERMINE CN       0254     VITEGATE FOULTION 5 TO DETERMINE CN       0255     VITEGATE FOULTION 5 TO DETERMINE CN       0251     VITEGATE FOULTION 5 TO DETERMINE CN       0252     VITEGATE FOULTION 5 TO DETERMINE CN       0253     VITEGATE FOULTION 5 TO DETERMINE CN       0254     VITEGATE FOULTION 5 TO DETERMINE CN       0255     VITEGATE FOULTION 5 TO DETERMINE CN       0257     VITEGATE FOULTION 5 TO DETERMINE CN       0251     VITEGATE FOULTION 5 TO DETERMINE CN       0251     VITEGATE FOULTION 5 TO DETERMINE CN       0251     VITEGATE FOULTION 5 TO TO ZOT       0252     VITEGATE FOULTION 5 TO TO ZOT       0253     VITEGATE FOULTION 5 TO TO ZOT       0254 <t< td=""><td></td><td></td></t<>		
0557 0559 0550 0551 0551 0551 0551 0551 0551	0255 C         Differet Traxt.[r.30.0] 60 TO 200         Offerentive Color           0.553 C         Traxt.[r.30.0] 60 TO 200         00 for teamive cv           0.554 C         VIEGATE SITA-0         00         00           0.555 C         VIEGATE SITA-0         00         00           0.555 C         VIECATA-0         200         00           0.555 C         VIECATA-0         00         00           0.557 C         VIECATA-0         00         00           0.557 C         VIECATA-0         00         00           0.575 C         VIECATA-0         00         00 <tr< td=""><td></td><td></td></tr<>		
C INTEGARTE GUUTTON 5 TO DETERMINE CM TFIXX.TT.30.01 TO 706 TFIXX.TT.30.01 TO 706 TFIXX.TT.30.01 TO 706 TFIXX.TT.30.01 TO 706 TFIXX.TT.30.01 TO 706 TO 200 TO 2	C INFGGATE EQUATION 5 TO OFTERMINE CM C ITTXX.LT.30.00 60 TO 206 C ITTXX.LT.30.01 60 TO 206 C C C C C C C C C C C C C C C C C C C	1520	DEL POEDELB
0250       FFIXX.IT.30.01 60 T0 206         0261       U2         0262       Na         0263       STP=0.5         0264       V11.0-0.10         0265       V11.0-0.10         0265       V11.0-0.10         0265       V11.0-0.10         0265       V11.0-0.10         0265       V11.0-0.10         0265       V11.0-0.10         0264       V11.0-0.10         0265       V11.0-0.10         0265       V11.0-0.10         0266       V11.0-0.10         0267       DBHT(1.0-0.10         0273       DBHT(21.V0C         0274       DBHT(21.V0C         0275       DBHT(21.V0C         0276       DBHT(21.V0C         0277       DBHT(21.V0C         0278       DD14.5         0278       DD14.5         0278       DD14.5         0278       DD14.5         0278       DD14.5         0279       DD14.5         0271       DFL(V=0.00.7         0278       DD14.5         0279       DD14.7         0271       DC10.05         0271       DC10.05 <td>0250       HTXX.LT.30.01 30 T0 266         0251       UELT4-0         0252       VT71-0.5         0253       VT71-0.5         0254       VT71-0.5         0255       VT0         0251       PAHT(1)=5.104         0253       PAHT(1)=5.104         0254       PAHT(1)=5.105         0271       PAHT(1)=5.105         0272       PAHT(1)=5.105         0273       PAHT(1)=5.105         0274       PAHT(1)=5.105         0275       PAHT(1)=5.105         0274       PAHT(1)=5.105         0275       PAHT(1)=5.105         0276       PAHT(1)=5.105         0277       PAHT(1)=5.105         0278       PAHT(1)=5.105         0279       PAHT(1)=5.105         0271       PAHT(1)=5.100         0272       PAHT(1)=5.100         0273       PAHT(1)=5.100         0274       PAHT(1)=5.100         0275       PAHT(1</td> <td>0254</td> <td>INTEGPATE EQUATION 5 TO DETERMINE CM</td>	0250       HTXX.LT.30.01 30 T0 266         0251       UELT4-0         0252       VT71-0.5         0253       VT71-0.5         0254       VT71-0.5         0255       VT0         0251       PAHT(1)=5.104         0253       PAHT(1)=5.104         0254       PAHT(1)=5.105         0271       PAHT(1)=5.105         0272       PAHT(1)=5.105         0273       PAHT(1)=5.105         0274       PAHT(1)=5.105         0275       PAHT(1)=5.105         0274       PAHT(1)=5.105         0275       PAHT(1)=5.105         0276       PAHT(1)=5.105         0277       PAHT(1)=5.105         0278       PAHT(1)=5.105         0279       PAHT(1)=5.105         0271       PAHT(1)=5.100         0272       PAHT(1)=5.100         0273       PAHT(1)=5.100         0274       PAHT(1)=5.100         0275       PAHT(1	0254	INTEGPATE EQUATION 5 TO DETERMINE CM
0250 42 0251 JELT4-0 0253 YIJP0.0 0265 YIJP0.0 0265 PWT(1)-0.1108 0265 PWT(1)-0.1108 0265 PWT(1)-0.1108 0265 PWT(1)-0.1108 0270 PWT(1)-0.1108 0271 PWT(4)-5.06-2 0271 PWT(4)-5.06-2 0271 PWT(4)-5.06-2 0271 PWT(4)-5.06-2 0272 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 001-10.00 0271 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 0273 PWT(4)-5.06-2 001-10.00 061 PWT(4)-5.06-2 072 PWT(4)-5.06-2 001-10.00 061 PWT(4)-5.06-2 001-10.00 061 PWT(4)-5.06-2 001-10.00 061 PWT(4)-5.06-2 001-10.00 061 PWT(4)-5.06-2 001-10.00 061 PWT(4)-5.06-2 072 PWT(4)-5.06-	0250 42 0251 JELT4-0 0253 Signature 0255 Signature 0256 Partition 0258 Partition 0258 Partition 0258 Partition 0258 Partition 0251 Pa		TF XXX, LY, 30.0) 60 TO 260
0251 JDELTA-0 0252 No 0255 No 0255 STPP-5 0255 STPP-5 0255 STPP-6 0255 STPP-6 0255 STPP-10 0255 STPP-10 0255 STPP-10 0255 STPP-105 0255 STPP-105 0255 STPP-105 0251 STPP-05 0275 STPP-105 0275 STPP-105 075 STPP-	0551       JDELTA-0         0252       STFP-0.5         0253       STFP-0.5         0254       V111-0.0         0255       V111-0.0         0256       PWT(1)-0.10         0256       PWT(1)-0.0         0256       PWT(1)-0.10         0256       PWT(1)-40.0         0271       PWT(1)-51.0         0272       PWT(1)-51.6         0273       PWT(1)-51.6         0274       PWT(1)-51.6         0275       PWT(1)-51.6         0276       PWT(1)-51.6         0277       PWT(1)-51.6         0278       PWT(1)-51.6         0279       PWT(1)-51.6         0271       PWT(1)-51.6         0273       PWT(1)-51.6         0274       PWT(1)-51.6         0275       PWT(1)-51.6         0275       PWT(1)-51.6         0275       PWT/10.7         0275       PWT/10.7         0275       PWT/10.7         0275       PWT/10.7         0275       PWT/10.7         0276       PWT/10.7         0277       PWT/10.7         0278       PWT/10.7         0279		C=7
0262 0265 0265 0265 0265 0265 0265 0265	0262 0265 0265 0265 0265 0265 0265 0265		
0200 0200 0200 0200 0200 0200 0200 020	0200 0200 0200 0200 0200 0200 0200 020		
0250       517-0.5         0255       717-0.0         0265       717-0.0         0265       702         0265       702         0265       702         0270       100-1104         0265       702         0271       100-1104         0272       100-1104         0273       100-1104         0271       100-1104         0272       100-1104         0273       100-1104         0273       100-1104         0273       100-1104         0273       100-1104         0273       100-1104         0273       100-1104         0273       100-1104         0273       101-1104         0273       101-1104         0274       110-100         0275       110-100         0278       110-100         0279       1110-100         0279       1110-100         0271       100-100         0273       1110-100         0274       1110-100         0275       111-100         0276       100-100         0277       100-100<	0253       517-0.5         0255       717-0.6         0255       717-0.6         0256       707         0258       702         0269       702         0270       201         0271       201         0271       201         0271       201         0271       201         0271       201         0271       201         0273       201         0274       201         0275       201         0276       201         0277       201         0278       200         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0279       201         0271       201         0271       201         0271       201         201       202		
0264       Y(1)=0.0         0265       Y(1)=0.106         0265       Part(1)=0.1106         0265       Part(1)=0.1106         0265       Part(1)=21         0265       Part(1)=21         0265       Part(1)=21         0265       Part(1)=21         0269       Part(1)=51         0271       Part(1)=516-2         0272       Part(1)=516-2         0273       Part(1)=516-2         0274       Part(1)=516-2         0275       Part(1)=0.5         0271       Part(1)=0.5         0272       Part(1)=0.5         0273       DEPT(1)=0.5         0274       DEPT(1)=0.5         0275       DETL PASS(1) 60 TO 202         0278       CONTINUE         0279       DEL(V=6VC/T)         0271       DEL(V=90LuSC)) 60 TO 202         0273       DEL(V=90LuSC)) 60 TO 202         0274       DEL(V=90C/C)         0274       DEL(V=90C/C)         0274       DEL(V=90C/C)         0274       DEL(V=90C/C)	0264       Y(1)=0.0         0265       Y(1)=0.100         0265       Part(1)=0.1106         0265       Part(1)=0.1106         0265       Part(1)=0.1106         0269       Part(1)=0.1106         0270       Part(1)=YFUG         0271       Part(2)=YFUG         0272       Part(2)=YFUG         0273       Part(2)=YEF         0274       Part(2)=YEF         0275       Part(2)=YEF         0271       Diput(2)=Q         0273       Diput(2)=Q         0274       Diput(2)=Q         0275       Diput(2)=Q         0276       CALL RKGS(FEMT-NDIM-INLANX)         0277       Diput(2)=Q         0278       COUTUNUE         0279       Diput(2)=Q         0278       COUTUNE         0279       Diput(1)=0.5         0271       Diput(1)=0.5         0278       COUTUNUE         0279       Diput(1)=0.5         0278       COUTUNUE         0279       COUTUNUE         0271       Dict(Y=SUCC)         0273       Dict(Y=SUCC)         0274       Dict(Y=SUCC)         0275       Dict		STEP=0.5
0265 PYT7T60 0 0268 PYT7T9 0 0269 201 20110 0269 201 20110 0269 201 20110 0270 2011155FF 0271 2011(1):5FF 0271 2011(1):5FF 0271 2011(1):5FF 0273 200 2011(1):5FF, MDIM.; MLF, BOLAFE.HOUTPUT.AUX) 1617FLUS5.17.16 0278 200 2011-0.5 0278 200 2011-10.5 0278 200 2011-10.5 0279 200 2011-10.5 0279 200 2011-10.5 0279 200 2011-10.5 0279 200 2011-10.5 0279 200 2011-10.5 0279 200 2011-10.5 0270 2011-10.5 0271 200 2011-10.5 0271 200 2011-10.5 0271 200 2011-10.5 0271 200 2011-10.5 0272 2011-10.5 0273 200 2011-10.5 0273 200 2011-10.5 0273 2011-10.5 0273 2011-10.5 0274 2011-10.5 0275 2011-2012 2012 2012 2012 2012 2012 2012	0265       717760       0         010       010       010         0269       702       0010         0269       702       0010         0269       702       0010         0269       701       0010         0270       0010       001         0271       0010       001         0273       0010       001         0274       0010       001         0275       0010       001         0275       0010       001         0275       0010       001         0275       0010       001         0279       00010       001         0279       00010       001         0279       00010       001         0279       00010       001         0279       0010000       001         0279       0010000       001         0279       0010000       001         0279       0010000       001         0279       00010000       001         0270       00010000       001         0270       00010000       001         0271       001000       <		Y(1)=0.0
0260       0201       0201         0261       001       001         0265       001       001         0266       201       001         0265       201       001         0265       201       001         0265       201       001         0271       0011       001         0272       0011       001         0273       0011       001         0274       0011       001         0275       0011       001         0275       0011       001         0275       0011       001         0275       0011       001         0276       0011       001         0277       0011       001         0278       001       001         0278       00       001         0279       001       01         0270       001       01         0271       01       01         0271       01       01         0271       01       01         0271       01       01         0271       01       01         0271	0265       001       001         0263       001       001         0264       001       001         0265       201       0011         0270       001105       001         0271       001105       001105         0272       001145       001145         0273       001145       001145         0274       001145       001145         0275       001145       001145         0275       001145       001145         0275       001145       001145         0275       001145       001145         0276       001145       001145         0277       001145       001145         0278       001145       001201         0279       001145       001201         0279       001145       001205         0279       001145       001205         0270       001145       001205         0271       001145       001205         0271       001145       001205         0271       001145       001205         0271       001145       001205         0271       0010125       001010		Υ(7)1=0.6
0269       702       2010       201         0268       702       2011       101         0269       701       2011       101         0270       2011       101       101         0271       2011       101       101         0273       2011       201       201         0274       2011       201       201         0275       2011       201       201         0275       0211       201       201         0275       0211       201       207         0275       0211       201       207         0278       0211       201       207         0279       161       105       107         0278       000       105       107         0279       001       107       107         0279       001       107       107         0279       001       107       107         0279       001       107       107         0279       001       105       107         0279       001       105       107         0270       001       105       107       101 <td>0269       701       201         0268       702       501         0269       701       501         0261       501       501         0270       5041(2)*FULG       50         0271       5041(2)*FULG       50         0273       5041(2)*GE       50         0274       501(2)*GE       50         0275       500(1)*GE       50         0278       500       501(2)*GE         0279       500(1)*GE       50         0279       50(1)*GE       50     <td></td><td></td></td>	0269       701       201         0268       702       501         0269       701       501         0261       501       501         0270       5041(2)*FULG       50         0271       5041(2)*FULG       50         0273       5041(2)*GE       50         0274       501(2)*GE       50         0275       500(1)*GE       50         0278       500       501(2)*GE         0279       500(1)*GE       50         0279       50(1)*GE       50 <td></td> <td></td>		
0260       702       504 113 FPLUS         0260       701       504 113 FPLUS         0260       701       504 113 FPLUS         0271       504 113 FPLUS       504 113 FPLUS         0272       504 113 FPLUS       504 113 FPLUS         0273       504 115 FPLUS       504 113 FPLUS         0274       504 113 FPLUS       504 113 FPLUS         0275       504 113 FPLUS       504 113 FPLUS         0275       504 113 FPLUS       505 104 FPLUS         0275       504 113 FPLUS       507 103 FPLUS         0275       504 113 FPLUS       507 103 FPLUS         0276       504 113 FPLUS       500 100 202         0277       500 100 110 FPLUS       500 100 202         0278       500 100 110 FPLUS       500 100 202         0279       501 110 (FEXP (TPLUSV/ROPLUSE) 11.0)       500 100 202         0280       501 110 (FEXP (TPLUSV/ROPLUSE) 11.0)       501 100 202	0260       202       001       000         0270       0011117400       001         0271       0011155170       001155170         0271       001145100       001145100         0271       001145100       001145100         0271       001145100       001145100         0271       001145100       001145100         0271       0011451000       0011451000         0271       0011451000       0011451000         0271       0011451000       00114500         0273       0011451000       00114500         0274       00114500       0011400         0275       00114500       0011400         0278       0011400       0010000000000000000000000000000000000		
0268 702 BANT(2)*PUUS 0270 PANT(2)*PUUS 0270 PANT(2)*PUUS 0271 PANT(2)*FUUS 0271 PANT(2)*FUS 0273 PANT(1)*56F2 0273 PANT(1)*56F2 0274 CALL PSOS (PANT V.0FPY.MD1%.1MLF.90LAYER.HOUTPUT.AUX) 16TYPLUS.TT.10.499*PFLUSC)7 60 T0 202 0278 CALL PSOS (PANT V.0FPY.MD1%.1MLF.90LAYER.HOUTPUT.AUX) 16TYPLUS.TT.10.499*PFLUSC)7 60 T0 202 0278 CONTINUE 0278 CONTINUE 0	0268 702 DBWT(2)*PUUS 0270 DBWT(2)*PUUS 0271 DBWT(2)*FUSC 0271 DBWT(1)=516 2 0273 DBWT(1)=516 2 0273 DBWT(1)=5.06 2 0275 DEP(1)=0.5 0275 DEP(1)=0.5 0279 CONTINUE 0279 CONTINUE	1920	CO 10 201
2000 POHT(12:14*PLUSC 2010 POHT(12:14*PLUSC 2011 POHT(15:10:0 2012 POHT(15:10:0 2013 POHT(15:10:0 2014	0269       201       PAHT(1):STFUSC         0271       PAHT(1):STFUSC         0272       PAHT(1):STFUSC         0273       PAHT(1):STFUSC         0274       PAHT(1):STFUSC         0275       PAHT(1):STFUSC         0275       PAHT(1):STFUSC         0275       PAHT(1):STFUSC         0275       PAHT(1):STFUSC         0276       CALL RAGS (FPHT, V.DFRY, ND14, IMLF, BOLAVER, MOUTPUT, AUX)         0277       PAHT (STSTO, STSUSC)         0278       COLL RAGS (FPHT, V.DFRY, ND14, IMLF, BOLAVER, MOUTPUT, AUX)         0279       CALL RAGS (FPHT, V.DFRY, ND14, IMLF, BOLAVER, MOUTPUT, AUX)         0279       COLL RAGS (FPHT, V.DFRY, ND14, IMLF, BOLAVER, MOUTPUT, AUX)         0279       COLL RAGS (FPHT, V.DFRY, ND14, IMLF, BOLAVER, MOUTPUT, AUX)         0271       DFLY/STO, TO, GATAPELUSC) TO, TO, Z02         0271       COLL RAGE (FPLUSCVR POLUSC) TO, TO, Z02         0271       DFLY/STO, TO, GATAPELUSC) TO, TO, Z02         0272       DFLY/STO, TO, GATAPELUSC) TO, TO, Z02         0273       DFLY/STO, TO, GATAPELUSC) TO, TO, Z02	0269	DRM ( 1) * YPLUS
0270 PPW1(1):STFP 0271 PPW1(1):S.0F-2 0273 PW1(5):0.0 0273 PW1(5):0.0 0275 PW1(5):0.5 0275 PW1(5):0.6 0275 PW1(5):0.6 0275 PW1(1):0.5 0275 PW1(1):0.6 0278 PW1(1):0.6	0270 PPW1(1)=5FP 0271 PW1(1)=-106-2 0273 PW1(5)=0.0 0273 PW1(5)=0.0 0275 PW1-F2 0275 PW1-F2 0275 PW1-F2 0275 PW1-F2 0276 PW1-F2 0279 PW1(10,0 0279 PW1(10,0 0279 PW1(10,0 0279 PW1(10,0 0279 PW1(10,0 0279 PW1(10,0 0279 PW1(1)=0(EXP(1USV/B0PLUSE)-1,0) 0279 PW1(1)=0(EXP(1USV/B0PLUSE)-1,0) 0279 PW1(1)=0(EXP(1USV/B0PLUSE)-1,0) 0270 PW1(1)=0(EXP(1USV/B0PLUSE)-1,0) 0271 PW1(1)=0(EXP(1USV/B0PLUSE)-1	0269	DAWT (2) # VDI IISC
0272       DFWT (4)=2.06         0272       DPWT (4)=2.06         0273       DFWT (5)=0.0         0274       DEWT (5)=0.6         0275       DEWT (2)=0.5         0276       CALL RKGS (PPWT, VDERY-NDIM-1HLF. BOLAYER-MOUTPUT.AUX)         0278       200         0279       CONTINUE         0279       CONTINUE         0279       CONTINUE         0279       CONTINUE         0279       CONTINUE         0279       DELTV=ROLL-LUSV/ROPLUSE) 1.0.0         0279       DELTV=ROLL-LUSV/ROPLUSE)-1.0)	0272       DFWT (4)=2.06         0273       DFWT (5)=0.0         0274       DFWT (5)=0.6         0275       DFWT (5)=0.6         0275       DFWT (5)=0.6         0275       DFWT (2)=0.5         0275       DFWT (2)=0.5         0275       DFWT (2)=0.5         0276       DEWT (1)=0.5         0277       DFWT (2)=0.5         0278       DFWT (2)=0.5         0279       COLL RAGS (FPWT - VDFWT - MUX )         0279       DFWT (2)=0.5         0279       COLL HAGE         0279       CONTINUE         0270       CONTINUE         0271       DFL YV=ROT(1=1)= (EXP (YPLUSC)) GO TO 202         0278       DFL YV=ROT(1=1)= (EXP (YPLUSV/ROPLUSE)=1.0)         0278       DFL YV=ROT(1=1)= (EXP (YPLUSV/ROPLUSE)=1.0)	0200	
0271 PENT 153-9.0F-Z 0273 PENT 153-9.0 0273 PENT 153-9.0 0275 PENT 153-9.0 0275 PENT 123-9.0 0275 CALL PASS PENT 17.0FRY.MD14.1HLF.80LAYEP.HOUTPUT.AUX) 0278 CALL PASS PENT 17.0FRY.MD14.1HLF.80LAYEP.HOUTPUT.AUX) 0278 CALL PASS PENT 17.0FRY.MD14.1HLF.80LAYEP.HOUTPUT.AUX) 0278 CALL PASS PENT 17.0FRY.MD14.1HLF.80LAYEP.HOUTPUT.AUX) 0278 CALL PASS PENT 17.0FRY.MD14.1HLF.80LAYEP.HOUTPUT.AUX) 0279 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0278 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0278 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0279 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0270 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0270 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0270 CALL PASS PENT 17.0FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.90LAYEP.HOUTPUT.AUX) 0770 FRY.MD14.1HLF.	0271 PPW115)=0.0-2 0273 PW115)=0.0 0274 DM1#2 0275 DF910.5 0275 DF912]=0.5 0276 C412]=0.5 0278 C412]=0.5 0278 C412[-0.4 0278 C412[-0.4] 0278 C		
0272 PPW151=0.0 0273 DEW1251=0.5 0274 DESV(1)=0.5 0275 DEV(1)=0.5 0275 DEV(1)=0.5 0275 DEV(1)=0.5 0276 Call RKG5(947+ND14.1HLF.80LAYER.HOUTPUT.AUX) 0279 COLL RKG5(9474FUUSC)) 60 TO 202 0278 COLLIAUC 0278 COLLIAUC 0279 COLLIAUC 0279 COLLIAUC 0270 COLLIAUC 0271 COLLIAUC 0270 COLLIAUC 0271 COLLIAUC 0270 COLLIAUC 0271 COLLIAUC 071 C	0272 PPHTES:=0.0 0273 DEPTIS:=0.0 0274 DEPTIS:=0.5 0275 DEPTIS:=0.5 0275 DEPTIS:=0.5 0278 CALL RKGS (PPHT: +.0014-11.4.0.X) 0279 CONTINUE 0279 CONTINUE 0279 CONTINUE 0279 CONTINUE 0270 CONTINUE 0271 CONTINUE 071 CONTIN		PP41(4)145-06-2
0274 ND14-2 0274 DETV11-0.5 0275 DETV21-0.5 0276 CALL RKGS(EPM1-Y-DERY-ND14.1MLF.BOLAYER.HOUTPUT.AUX) 0279 CALL RKGS(EPM1-Y-DERY-ND14.1MLF.BOLAYER.HOUTPUT.AUX) 0279 CALL RKGS(EPM1-Y-DETUSCI) GO TO ZOZ 0279 CODCI=CU/CI 0279 DELYV=D0(1:1)*(EXP(YPLUSV/R0PLUSE)-1.0) 0214 DELYV=D0(1:1)*(EXP(YPLUSV/R0PLUSE)-1.0)	0271 ND1#27 0274 DE7(1)=0.5 0275 DE7(1)=0.5 0275 CALL PSC1 POL 0278 CALL V.C. (0,9947PLUSC) 1 60 T0 202 0278 200 CONTAUE 0278 200 CONTAUE 0278 200 CONTAUE 0279 CUCLI-CVCC1 0279 CUCLI-CVCC1 0279 CUCLI-CVCC1 0270 DELTV=D0(1:1)=(EXP(YPLUSV/B0PLUSE)-1.0)		PPW1 (5)=0.0
0275 0EPY(1)=0.5 0275 0EPY(1)=0.5 0275 0EAL RKGS(PAHI-Y-0ERY-NDIN-1HLF.80LAYEP-HOUTPUT.AUX) 0279 0278 0EAL RKGS(PPHI-V-0ERY-NDIN-1HLF.80LAYEP-HOUTPUT.AUX) 0278 0278 0EOHI-1-1-05 0278 0EOHI-1-05 000000000EOHI-1-05 000000000000000	0275 06711=0.5 0275 06711=0.5 0275 074L RKGS (PPHI-Y-06FY-MD1M-1HLF-80LAYEP-MOUTPUT-AUX) 0278 0216 0278 200 CONTINUE 0278 200 CONTINUE 0278 0278 0011=1)=(EXP(YPLUSC)) GO TO 202 0278 0278 0011=1)=(EXP(YPLUSC)) GO TO 202 0278 0278 0279 0511=1)=(EXP(YPLUSC)) GO TO 202 0278 0278 0278 0511=1)=(EXP(YPLUSC)) GO TO 202 0278 0278 0278 0511=1)=(EXP(YPLUSC)) GO TO 202 0278 0278 0278 0511=1)=(EXP(YPLUSC)) GO TO 202 0278 0511=1000000000000000000000000000000000		
0276 DEPY(21-0.5 0276 DEPY(21-0.5 0276 CALL RKGS(EPW1-Y.0ERY.MD14.1MLF.BOLAYER.HOUTPUT.AUX) 0279 CALL RKGS(EPW1-Y.0ERY.MD14.1MLF.BOLAYER.HOUTPUT.AUX) 0279 CALL RKGS(EPW1-Y.0ERY.MD14.1MLF.BOLAYER.HOUTPUT.AUX) 0279 CALL VCB (011-11-0(EXP(USV.R0PLUSE)-1.0) 0279 DELYV=D0(11-11-0(EXP(VPLUSV.R0PLUSE)-1.0)	0275 DEPT(11+0.5 0275 DEPT(11+0.5 0276 TALLUS(11+0.5 0278 TALLUS(1) 60 TO 202 0278 200 CONTINUE 0278 200 CONTINUE 0279 CODET-CV/C1 0279 00 CONTINUE 0270 DELVY=D0(11)+(EXP(YPLUSV/B0PLUSE)-1.0)		
0275 DEPT (2:1-0.5 0275 Call Ress (PPM1 - 1.0 F - 80LAYEP. HOUTPUT. AUX) 0279 Call Ress (PPM1 - 1.0 - 993 YPLUSC)) 60 T0 202 0278 200 Continue 0279 Continue 0279 051 - 10 - (EXP (YPLUSV/R0PLUSE) - 1.0) 0280 05LYV=R0(1+1)+ (EXP (YPLUSV/R0PLUSE) - 1.0)	0275 DEPT (21-0.5 0276 CaLL Recs (PPM1, V.0EPT, V.0EPT, V.0EPT, AUX) 0279 CALL Recs (PPM1, V.0EPT, V.0EPT, AUX) 0278 200 CONTINUE 0278 CONTINUE 0278 0279 CONTINUE 0280 DELTV=R0(1-1)*(EXP(VPDLUSE)-1.0) 0280 DELTV=R0(1-1)*(EXP(VPDLUSE)-1.0)		0EPY(1)=0.5
0276 CAL REGS (PPMT.Y.OFRY.MDIM.IMLF.BOLAFER.HOUTPUT.AUX) 0277 IFYPLUS.CT.T.0.9994PLUSCHT 60 TO 202 0279 CONTINUE 0279 CUDCI-CV/CT 0280 DELYV=B0(1-1)*(EXP(YPLUSV/R0PLUSE)-1.0) 0280 DELYV=P0(1-1)*(EXP(YPLUSV/R0PLUSE)-1.0)	0276 CALL REGS (PPMT.Y.0FRY.NDIM.IMLF.BOLAFER.HOUTPUT.AUX) 1614PLUS.CT.T.0.4947PLUSCHT 60 TO 202 0279 200 CONTINUE 0279 CUDCI-CV/CT 0280 DELTV=B0(1-1)+(EXP[YPLUSV/B0PLUSE)-1.0) 0280 DELTV=B0(1-1)+(EXP[YPLUSV/B0PLUSE)-1.0)		0697 (2)=0.5
0279 1617PLUS.CT0.999*PPLUSCJJ 60 T0 202 0278 200 CONTINUE 0279 CONTINUE 0280 0ELTV=#0(1+1)*(EXP(YPLUSV/R0PLUSE)-1.0) 0280 0ELTV=#0(1+1)*(EXP(YPLUSV/R0PLUSE)-1.0)	0279 1617PLUS-LT.10.04947PLUSC1) G0 T0 202 0278 200 CONTINUE 0279 CONTINUE 0280 0ELTV-R0(1-1)•(EXP(YPLUSV/R0PLUSE)-1.0) 0280 0ELTV-R0(1-1)•(EXP(YPLUSV/R0PLUSE)-1.0)		C 41 1 DKGC (DDW1 - Y - DEDY - ND14 - 141 F - 901 AYED - 40117041 - 4414 -
0280 0011WUE CONTINUE 0279 CUDIT=C#/CT 0279 0ELTV=B0(1:1)•(EXP(YPLUSV/R0PLUSE)=1.0)	0219 200 CONTINUE 0279 CUDCI=C#/CT 0219 DELYV=00(1-1)•(EXP(YPLUSV/R0PLUSE)-1.0) 0280 DELYV=00(1-1)•(EXP(YPLUSV/R0PLUSE)-1.0)		
0278 200 CONTINUE 0279 CONTINUE 0280 DELTV=R0(1+1)*(EXPTVPDLUSE)-1.0) 0280 DELTV=R0(1+1)*(EXPTVPDLUSE)-1.0)	0278 200 CONTINUE 0279 CONTINUE 0280 DELTY=R0(1:1)•(EXP[VS/R0PLUSE)-1.0) 0281 DELTY=R0(1:1)•(EXP[VPLUSY/R0PLUSE)-1.0)	1120	
0279 CuDCT=C#/CT 0280 DELTV=R0(1-1)+(EXP(YPLUSV/R0PLUSE)-1.0)	0279 CuDCT=C#/CT 0280 DELTV=R0(1+1)+0(EXP(YPDPLUSE)-1.0)	8750	
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0015       TF(F-EQ.S)       00 TO A.         0019       TF(F-EQ.S)       00 TO A.         0021       TF(T-EVLS)       00 TO A.         0022       TF(LEC.S)       00 TO 13         0022       TF(L.EO.S)       00 TO 13         0023       TF(L.EO.S)       00 TO 13         0023       TF(L.EO.S)       00 TO 13         0023       TF(L.EO.S)       00 TO 2         0033       TF(L.EO.S)       00 TO 2         0033       TF(L.EO.S)       00 TO 2         0033       TF(R-LUS.LF.20.0)	FF(W-EC, 5)       G0 T0 **         FF(W-EC, 5)       G0 T0 **         UPUUS=Y(1)       00 T0 **         FF(W-EC, 5)       G0 T0 **         FF(US=X)       FUUS=X         FF(US=X)       FUUS=X         FF(CFC=1)       FO T0 **         FF(US=X)       FUUS=X         FF(US=X)       FUUS=X         FF(US=X)       FUUS=X         FF(N=E0.1)       G0 T0 1         FF(N=E0.2)       G0 T0 2         FF(N=US_LE_E00.0)       G0 T0 2         FF(N=E0.2)       G0 T0 2     <	0015       TF(F*-EQ.5)       00 TO 4.         0019       TF(F*-EQ.5)       00 TO 4.         0019       H=Y(5)       00 TO 4.         0021       YPLUSY=T       0.0         0022       TF(FECKSL1_LUPLUS) 60 TO 1         10022       TF(1.E0.15)       YPLUSY=PLUSY         0022       TF(1.E0.15)       60 TO 1         0022       TF(1.E0.15)       60 TO 1         0022       TF(1.E0.15)       60 TO 1         0023       TF(1.E0.21)       60 TO 1         0023       TF(1.E0.21)       60 TO 1         0033       TF(1.E0.21)       60 TO 1         0033       TF(1.E0.21)       60 TO 2         0033       TF(1.E0.21)       60 TO 2         0033       TF(1.E0.21)       60 TO 2         0033       TF(1.E0.2.20.0)       60 TO 2			3
0013       UPLUSSY(11)       DELA         0014       UPLUSSY(11)       DELA         0013       YFUUSSY(11)       DELA         0014       YFUUSSY(11)       DELA         0022       TF(TCHECK-FQ.1)       GO TO 31         0022       TF(TCHECK-FQ.1)       GO TO 31         0022       TF(TCHECK-FQ.1)       GO TO 31         0022       TF(TCHECK-FQ.1)       GO TO 12         0022       TF(11.EQ.35)       VPLUSSSEVPLUSS         0023       TF(11.EQ.35)       VPLUSSSEVPLUSS         0033       TF(11.EQ.35)       VPLUSSSEVPLUSS         0033       TF(11.EQ.35)       VPLUSSSEVPLUSS         0033       TF(11.EQ.35)       VPLUSSSEVELSS         0033       TF(11.EQ.35)       TO         0033       TF(11.EQ.35)       TO         0033       TF(11.EQ.35)       TO         0033       TF(11.EQ.35)       TO         0033       TF(11.EQ.35)       TO <t< td=""><td>UPULS=Y(1) - DELA UPULS=Y(1) - DELA UPULS=Y(1) - DELA TETETES TETETES TETETES TETETES TETETES TETETES TETETES TETETS</td><td>0013       UPLUSST(11)       001         00119       UPLUSST(11)       001         00121       FILUSST(11)       001         00121       FILUSST(11)       001         00121       FILUSST(11)       001         00121       FILUSST(11)       001         00221       FILUSST(11)       001         00221       FILUSST(11)       001         00221       FILUSST(11)       001         00221       FILUSST(11)       001         00222       FILUSST(11)       001         00223       FILUSST(11)       001         00224       FILUSST(11)       001         00225       FILUSST(11)       001         00226       FILUSST(11)       001         00227       FILUSST(11)       001         00231       FILUSST(11)       001         00232       FILUSST(11)       001         0033       FILUSST(11)       001         0033       FILUSST(12)       001         0033       FILUSST(12)       001         0033       FILUSST(12)       001         0033       FILUSST(12)       001         0033       FILUSST(12)</td><td></td><td></td><td>3</td></t<>	UPULS=Y(1) - DELA UPULS=Y(1) - DELA UPULS=Y(1) - DELA TETETES TETETES TETETES TETETES TETETES TETETES TETETES TETETS	0013       UPLUSST(11)       001         00119       UPLUSST(11)       001         00121       FILUSST(11)       001         00121       FILUSST(11)       001         00121       FILUSST(11)       001         00121       FILUSST(11)       001         00221       FILUSST(11)       001         00221       FILUSST(11)       001         00221       FILUSST(11)       001         00221       FILUSST(11)       001         00222       FILUSST(11)       001         00223       FILUSST(11)       001         00224       FILUSST(11)       001         00225       FILUSST(11)       001         00226       FILUSST(11)       001         00227       FILUSST(11)       001         00231       FILUSST(11)       001         00232       FILUSST(11)       001         0033       FILUSST(11)       001         0033       FILUSST(12)			3
00119     ULUS-11	1       1	00119     ULUS-11(1)			3
0018     H=YY51       0022     F(TUEKCK-1, LPLUS) 60 T0 3       0022     F(TUEKCK-1, LPLUS) 60 T0 3       0022     F(TUEKV-10       0022     F(TUEKV-10       0022     F(TUEK-10       0022     F(TUEK-10       0022     F(TUEK-10       0022     F(TUEK-10       0022     F(TUEK-10       0023     F(TUEK-20.1) 60 T0 13       0029     FF(TUEK-20.1) 60 T0 13       011     F(TUEK-20.1) 60 T0 13       0023     FF(TUEK-20.1) 60 T0 2       0033     FF(TUES-15.00 0) 13       0033     FF(TUES-15.00 0) 60 T0 2       0034     FF(TUES-15.00 0) 60 T0 2       0035     FF(TUES-15.00 0) 60 T0 2       0043     FF(TUES-15.00 0) 60 T0 2       0043     FF(TUES-15.00 0	Trivici         xiav(s)         xiav(s)         xiav(s)         reves         reves </td <td>0018     H=Y(5)       0022     TF(TUES.LT.UPLUS) G0 T0 3       0022     TF(TUES.LT.UPLUS) G0 T0 3       0022     TF(TELUS.LT.UPLUS) G0 T0 3       0022     TF(11.E0.35) YPLUSSYPELUS       0023     TF(11.E0.35) YPLUSSYPELUS       0023     TF(11.E0.35) YPLUSSYPELUS       0023     TF(11.E0.35) YPLUSSYPELUS       0033     TF(12.E0.30) YPLUSSYPELUS       0034     TF(12.E0.30)</td> <td></td> <td></td> <td>9</td>	0018     H=Y(5)       0022     TF(TUES.LT.UPLUS) G0 T0 3       0022     TF(TUES.LT.UPLUS) G0 T0 3       0022     TF(TELUS.LT.UPLUS) G0 T0 3       0022     TF(11.E0.35) YPLUSSYPELUS       0023     TF(11.E0.35) YPLUSSYPELUS       0023     TF(11.E0.35) YPLUSSYPELUS       0023     TF(11.E0.35) YPLUSSYPELUS       0033     TF(12.E0.30) YPLUSSYPELUS       0034     TF(12.E0.30)			9
0019       YIIA(8)         0021       YELUS-LT : JELUS) 60 T0 3         0022       YELUS-LT : JELUS) 60 T0 3         0022       YELUS-TELT : JELUS) 60 T0 3         0022       YELUS-TELT : JELUS) 60 T0 3         0027       31 T616.50 30 YELUSS-FPLUS         0027       1611.60.36) YELUS35-YELUSY         0027       1611.60.36) YELUS35-YELUSY         0027       1611.60.36) YELUS35-YELUSY         0027       1611.60.36) YELUS35-YELUSY         0023       1611.60.36) YELUS35-YELUSY         0023       1611.60.36) YELUS35-YELUSY         0033       1611.60.36) YELUS35-YELUSY         0033       1611.60.36       17         0033       1611.61.0       60 T0 13         0033       10       1614.61.0       60 T0 2         0033       10       1614.61.0       60 T0 2         0033       10       1610.10       60 T0 2         0033       10       16.41.0       60 T0 2         0033       10       16.41.0       60 T0 2         0033       10       16.41.0       60 T0 2         0034       10       16.41.0       60 T0 2         0044       10       16.10       60 T0 2	X13Y (8) X13Y (8) Y10254 F(1CHECK.F0.1) 60 T0 31 F(1CHECK.F0.1) 60 T0 31 F(1ECHECK.F0.1) 60 T0 31 F(1ECHECK.F0.3) 60 T0 12 F(1.E0.3) 60 T0 2 F(1.E0.3) 60	0019       Y114(18)         VPLUSS-LT TUPLUS       F(1CHECK-F0.1) 60 70 31         0022       F(1CHECK-F0.1) 60 70 31         0022       F(1ECHECK-1)         0022       F(1ECHECK-1)         0022       F(1ECHECK-1)         0022       F(1EC-35)         0022       F(1E-0.36)         0022       F(1E-0.36)         0023       F(1E-0.36)         013       F(1E-0.36)         013       F(1E-0.36)         013       F(1E-0.36)         013       F(1E-0.36)         013       F(1E-0.36)         013       F(1E-0.36)         014       F(1E-0.36)         015       F(1E-0.36)         013       F(1E-0.36)         014       F(1E-0.36)         015       F(1E-0.36)         015       F(1E-0.36)         015       F(1E-0.36)         016       F(1E-0.36)         017       F(1E-0.36)         018       F(1E-1.20.0)         019       F(1E-1.20.0)         010       F(1E-1.20.0)         011       F(1E-1.20.0)         012       F(1E-1.20.0)         013       F(1E-1.20.0) <td></td> <td></td> <td>H#Y (5)</td>			H#Y (5)
00220         FFLUS.LT.UPLUS1         60 T0 31           00221         FF(TELEK.FQ.1) 60 T0 31           00223         FF(TELEG.J5) FEUUS160 T0 30           00223         FF(TE.FQ.1) 60 T0 12           00223         FF(TE.FQ.1) 60 T0 12           00223         FF(TE.FQ.2) 60 T0 12           00223         FF(TE.FQ.2) 60 T0 12           00230         FF(A.FG.2) 60 T0 12           00311         FF(A.FG.2) 60 T0 12           0133         FF(A.FG.2) 60 T0 12           0134         FF(A.FG.2) 60 T0 2           0135         FF(A.FG.2) 60 T0 2           014         A           015         FF(A.FG.2) 60 T0 2           016         FF(A.FG.2) 60 T0 2           017         FF(A.FG.2) 60 T0 2	FULSELT: UPLUS: 160 T0 31         F(TCHEKK, F02,1) 60 T0 31         F(TCHEKK, F02,1) 60 T0 31         F(TERES)         F(TERES)      <	00220       FFLUS-LT_UPLUS1       60 T0 31         00221       FF(TELES.TS)       FEUS-LT_UPLUS1       60 T0 31         00223       FF(TELES.35)       FEUSS4       FEUSS4         00223       FF(TELES.35)       FEUSS4       FEUSS4         00223       FF(TELES.35)       FEUSS4       FEUSS4         00224       FF(TELES.35)       FEUSS4       FEUSS4         00224       FF(TELES.35)       FEUSS4       FEUSS4         00224       FF(TELES.35)       FEUSS4       FEUSS4         00231       FF(TELES.35)       FEUSS4       FEUSS4         00331       FF(TELES.35)       60 T0 12       FEUSS4         00333       FF(TELES.1E.200.0)       60 T0 2       2         00334       VALUS.1E.200.0)       60 T0 2       2         00335       FF(TELUS.1E.200.0)       60 T0 2       2         00334       VALUS.1E.2000.0)       60 T0 2       2         00335       FF(TELUS.1E.2000.0)       60 T0 2       2         00335       FF(TELUS.1E.2000.0)       60 T0 2       2         00335       FF(TELUS.1E.2000.0)       60 T0 2       2         0044       FF(TELUS.1E.2000.0)       60 T0 2       2			X1#7(8)
00221         F(TCHEUS_LT_JUPLUS) 60 T0 1           00223         F(TEREUS_LT_JUPLUS) 60 T0 1           00273         F(TEREUS_LT_JUPLUS) 60 T0 1           00273         F(TEREOS_1) 60 T0 1           00273         F(TERES_LT_JUPLUS) 60 T0 1           00231         F(TERES_LT_JUPLUS) 60 T0 1           00333         F(TERES_LT_200) 60 T0 2           00334         FF(TERES_LE_20.0) 60 T0 2           00335         FF(TERES_S_0 0           00335         FF(TERES_S_0 0           00335         FF(TERES_S_0 0           00335         FF(TERES_S_0 0           0033         FF(TERES_S_0 0           0033         FF(TERES_S_0 0	11       F(1(EC.15)       0       0       0         12       F(1(EC.15)       0       10       0       0         13       F(1(EC.15)       0       10       11       0       0       0         14       F(1(EC.15)       0       10       11       0       0       10         14       F(1(EC.15)       0       10       11       11       0       0       10         17       F(1(EC.15)       0       10       11 <td< td=""><td>00221     F(TCHEUS.LT.UPLUS) 60 10       00223     F(TELUS.LT.UPLUS) 60 10       00224     F(TEC.35) YPLUSSSPPLUSY       0027     F(TEC.35) YPLUSSSPPLUSY       0027     F(TEC.35) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0031     F(TEC.25) YPLUSSSPPLUSY       0033     F(TPLUS.LF.20.0) G0 T0       00335     FF(TPLUS.LF.20.0) G0 T0       0044     PART(5)=1.0       0045     FF(TPLUS.LF.2000.0) G0 T0       0045     FF(TPLUS.LF.2000.0) G0 T0</td><td>LN 0020</td><td></td><td></td></td<>	00221     F(TCHEUS.LT.UPLUS) 60 10       00223     F(TELUS.LT.UPLUS) 60 10       00224     F(TEC.35) YPLUSSSPPLUSY       0027     F(TEC.35) YPLUSSSPPLUSY       0027     F(TEC.35) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0027     F(TEC.25) YPLUSSSPPLUSY       0031     F(TEC.25) YPLUSSSPPLUSY       0033     F(TPLUS.LF.20.0) G0 T0       00335     FF(TPLUS.LF.20.0) G0 T0       0044     PART(5)=1.0       0045     FF(TPLUS.LF.2000.0) G0 T0	LN 0020		
0025     TCHECKEL     COUNCE       0025     TCHECKEL     CUUS35=YPLUSY       0027     TF(1.E0.15)     YPLUS3=YPLUSY       0027     TF(1.E0.15)     FUUSY       0027     TF(1.E0.15)     FO     T       0027     TF(1.E0.15)     FO     T       0027     TF(1.E0.15)     FO     T       0021     TF(1.E0.15)     GO     T       0023     TF(1.E0.21)     GO     T       0033     T	TCHECKT     TCHECKT     TCHECKT       TCHECKT     TCHECKT     TCHECKT       TFULSSS+PLUS       TFULSSS+PLUS       TFULSSS+PLUS       TFULSSS+PLUS       TFULSSS+PLUS       TFULSS       TT       <	0025     TCHECKEL     COUNCE       0025     TCHECKEL     COUNCE       0025     TFILUSYMPPLUS       0026     TFILUSYMPPLUS       0027     TFILUSYMPPLUS       0027     TFILUSYMPPLUS       0027     TFILUSYMPPLUS       0029     TFILUSYMPPLUS       0029     TFILUSYMPPLUS       0029     TFILUSYMPPLUS       0029     TFILUSS       0011     TFILUSS       0012     TFILUSS       0013     TFILUSS       0010     TTIL <t< td=""><td>LN 0021</td><td></td><td></td></t<>	LN 0021		
0022     YPLUSSWERUS       0022     1511.80.151       0022     1511.80.151       0022     1511.80.151       0023     1511.80.151       0031     1514.80.151       0032     1514.80.151       0031     1514.80.151       0032     1514.80.151       0033     1514.80.151       0033     1514.80.151       0033     1514.80.151       0033     1614.80.151       0033     1614.80.151       0033     1614.80.151       0033     10       117.14.105.15.20.01     60 TO 2       0033     10       117.14.105.15.10     0       0033     11       117.14.105.11.0       0033     11       117.14.105.11.0       0044     12       0045     11       117.14.105.11.0       0044     12       0045     11       117.14.100.0.01     60 TO 2       0044     12       0045     11       117.14.100.0.01     60 TO 2       0045     11       117.14.100.0.01     60 TO 2       0045     12       0045     12       0045     12       0045 <td< td=""><td>Tritice       Tritice       Tritice</td><td>0022     7PLUSY-FULUS       0022     1F(1.E0.35) YPLUS35-YPLUSY       0022     1F(1.E0.35) YPLUS35-YPLUSY       0022     1F(1.E0.35) GO TO 12       0023     1F(1.E0.25) GO TO 12       0023     1F(1.E0.25) GO TO 12       0023     1F(1.E0.25) GO TO 12       0033     1F(1.E0.25) GO TO 2       0033     1F(1.E0.2.1.0       0044     17       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     12       0045     12       <t< td=""><td></td><td></td><td></td></t<></td></td<>	Tritice	0022     7PLUSY-FULUS       0022     1F(1.E0.35) YPLUS35-YPLUSY       0022     1F(1.E0.35) YPLUS35-YPLUSY       0022     1F(1.E0.35) GO TO 12       0023     1F(1.E0.25) GO TO 12       0023     1F(1.E0.25) GO TO 12       0023     1F(1.E0.25) GO TO 12       0033     1F(1.E0.25) GO TO 2       0033     1F(1.E0.2.1.0       0044     17       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     11       0045     12       0045     12 <t< td=""><td></td><td></td><td></td></t<>			
0025     If(1.E.055)     YELU535=YELUSY       0027     31     F(1.E.015)     YELU535=YELUSY       0029     1F(1.E.015)     F(1.E.015)     F(1.E.015)     F(1.E.015)       0030     1F(1.E.015)     F(1.E.015)     F(1.E.015)     F(1.E.015)       0031     1F(1.E.E.015)     F(1.E.015)     F(1.E.015)     F(1.E.015)       0031     1F(1.E.E.015)     F(1.E.015)     F(1.E.015)     F(1.E.015)       0031     1F(1.E.E.015)     F(1.0.12)     F(1.E.015)     F(1.20.0.0)     F(1.20.0.0)       0033     10     1F(1.E.015)     F(1.E.015)     F(1.E.0.0.0)     F(1.20.0.0)     F(1.20.0.0)       0033     10     17     17     F(1.E.20.0.0)     F(0.10     F(1.20.0.0)       0033     10     17     17     F(1.E.1.0.0)     F(1.20.0.0)     F(1.20.0.0)       0043     11     17     11     F(1.20.0.0.0)     F(0.10     F(0.10)       0044     9045     9040     9040     9040     F(1.20.0.0)     F(0.10       0044     9044     9040     9040     9040     9040     F(1.20.0.0)     F(0.10       0045     11     11     11     11     F(1.20.0.0)     F(0.10     F(0.10)       004	If (1: E0.35) % PLU355-% PLUS         If (1: E0.35) % PLU355-% PLUS         If (1: E0.36) % PLU355-% PLUS         If (1: E0.36) % 0 10         If (1: E0.31) % 0 10         StEP=5.0         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         0 10 2         11         12         13         14         15         16         17         18         19         10         11         12         13         14         15         16 <td>0025     If(1.E.055) YELUS35=YELUSY       0027     31     F(1.E.015) YELUS35=YELUSY       0029     IF(1.E.E.015) GO TO 12       0020     IF(1.E.E.015) GO TO 12       0020     IF(1.E.E.015) GO TO 12       0021     IF(1.E.E.015) GO TO 12       0023     IF(1.E.E.015) GO TO 12       0023     IF(1.E.E.015) GO TO 2       0023     IF(1.E.E.015) GO TO 2       0033     IF(1.E.E.015) GO TO 2       0033     IF(1.E.E.015) GO TO 2       0033     IF(1.E.E.016) GO TO 2       0033     IF(1.E.E.20.0.0) GO TO 2       0045     IF(1.</td> <td>LN 0024</td> <td></td> <td>YPLUSV=YPLUS</td>	0025     If(1.E.055) YELUS35=YELUSY       0027     31     F(1.E.015) YELUS35=YELUSY       0029     IF(1.E.E.015) GO TO 12       0020     IF(1.E.E.015) GO TO 12       0020     IF(1.E.E.015) GO TO 12       0021     IF(1.E.E.015) GO TO 12       0023     IF(1.E.E.015) GO TO 12       0023     IF(1.E.E.015) GO TO 2       0023     IF(1.E.E.015) GO TO 2       0033     IF(1.E.E.015) GO TO 2       0033     IF(1.E.E.015) GO TO 2       0033     IF(1.E.E.016) GO TO 2       0033     IF(1.E.E.20.0.0) GO TO 2       0045     IF(1.	LN 0024		YPLUSV=YPLUS
0027       31       F(1.E.0.16)       YPLUSSS=YPLUSV         0027       31       F(1.E0.1)       60       71         0030       F(N.E0.1)       60       71         0031       F(N.E0.1)       60       71         0031       F(N.E0.2)       60       71         0031       F(N.E0.2)       60       71         0032       F(N.E0.2)       60       72         0033       F(N.E0.2)       60       70         0034       YPLUS.LF.20.0)       60       70         0035       F(YPLUS.LF.20.0)       60       70         0033       10       F(YPLUS.LF.20.0)       60       70         0033       10       F(YPLUS.LF.200.0)       60       70         0045       STEP5.0       90       70       70         0043       11       F(YPLUS.LF.200.0)       60       70         0044       12       F(YPLUS.LF.200.0)       60       70         0045       11       F(YPLUS.LF.200.0)       60       70         0045       11       F(YPLUS.LF.200.0)       60       70         0045       11       F(YPLUS.LF.200.0)       60       70	1 $f(1, \epsilon, 5)$ $Pelusservelusvelusvelusvelusvelusvelusvelusvelus$	0027     31     Ff(1, F0, 1)     F(1, F0, 1)	LN 0025		If(I.EQ.35) YPLUS35=YPLUSV
0027     31     CCNTINE     00       0029     17(N+E0.2)     60     10       0031     17(N+E0.2)     60     11       0032     17(N+E0.2)     60     11       0033     17(N+E0.2)     60     12       0033     17(N+E0.2)     60     12       0033     17(N+E0.2)     60     12       0033     17(N+E0.2)     60     12       0034     N=1     12     10       0035     17(N+LUS.LF.200.0)     60     10       0031     17(Y-LUS.LF.200.0)     60     10       0031     17(Y-LUS.LF.200.0)     60     10       0031     17(Y-LUS.LF.200.0)     60     10       0041     17(Y-LUS.LF.200.0)     60     10       0042     11     17(Y-LUS.LF.200.0)     60     10       0041     17(Y-LUS.LF.200.0)     60     10     2       0042     11     17(Y-LUS.LF.200.0)     60     10       0043     11     17(Y-LUS.LF.200.0)     60     10       0044     12     14     10     10       0044     12     14     10     10       0044     12     10     10     10       0045	3) CONTURE CONTUNE CONTURE CONTURE CONTURE CONTURE CONTURE CONTURE CONTURE CONTUNE CONTUNE CONTURE CONTUNE CON	0027     31     CCNTINE     60     70     10       0029     1     1     1     1     1       0029     1     1     1     1     1       0029     1     1     1     1     1       0021     1     1     1     1     1       0011     1     1     1     1     1       0013     1     1     1     1     1       0013     1     1     1     1     1       0013     1     1     1     1     1       0014     1     1     1     1     1       0013     1     1     1     1     1       0014     1     1     1     1     1       0015     0     1     1     1     1       0015     0     1     1     1     1       0015     0     1     1     1     1       0015     0     1     1     1     1       0010     1     1     1     1     1       0010     1     1     1     1     1       0010     0     0     0     0     <	LN 0026		If (1.EG.36) VPLUS35=YPLUSV
0029         1F(Ax:EG.1)         60 70         10           0011         F(Ax:EG.1)         60 70         12           0011         F(Ax:EG.1)         60 70         2           0013         F(Ax:EG.1)         60 70         2           0014         F(Ax:EG.1)         60 70         2           0015         F(F(A:LUS.LE.200.0)         60 70         2           0014         F(F(PLUS.LE.2000.0)         60 70         2           0015         F(F(PLUS.LE.2000.0)         60 70         2           0015         F(F(PLUS.LE.2000.0)         60 70         2           0045         F(F(PLUS.LE.2000.0)         60 70         2           0045         F(F(FUS.LE.2000.0)         60 70         2           0045         F(F(FUS.LE.2000.0)         60 70	IF(N=E0.2)     60     70     10       IF(N=E0.2)     60     70     12       Nait     Nait     10     12       Nait     Nait     10     10       Nait     10     10     10       Nait     10     10     10       Nait     11     11     11       Nait     10     10     10       Nait     11     11     10       Nait     11     11     10       Nait     11     10     10       Nait     10     2     10       Nait     10     2     10       Nait     10     2     10       Nait     10     2<	0029     1F(Ax:EQ.1) 60 70 10       0011     F(Ax:EQ.1) 60 70 12       0011     F(Ax:EQ.1) 60 70 2       0013     F(Ax:EQ.1) 60 70 2       0014     F(Ax:EQ.1) 60 70 2       0015     F(Ax:EQ.1) 60 70 2       0015     F(Ax:EQ.1) 60 70 2       0013     F(Ax:EQ.1) 60 70 2       0013     F(Ax:EQ.1) 60 70 2       0014     F(Ax:EQ.1) 60 70 2       0015     F(Ax:EQ.1) 60 70 2       0016     F(Ax:EQ.1) 60 70 2       0017     F(Ax:EQ.1) 60 70 2       0018     F(Ax:EQ.1) 60 70 2       0019     F(Ax:EQ.1) 60 70 2       0019     F(Ax:EQ.1) 60 70 2       0010     F(Ax:EQ.1) 60 70 2       0011     F(Ax:EQ.1) 60 70 2       0012     F(Ax:EQ.1) 60 70 2       0013     F(Ax:EQ.1) 60 70 2       0014     F(Ax:EQ.1) 60 70 2       0015     F(Ax:EQ.1) 60 70 2       0018	LN 0027	5	
0031     FF(NEUS.1F 60 70 12       0033     FF(NEQ.4) 60 70 12       0034     FF(NEQ.4) 60 70 12       0035     FF(NEQ.4) 60 70 12       0031     FF(NEQ.4) 60 70 12       0033     FF(NEQ.4) 60 70 12       0033     FF(NEQ.4) 60 70 2       0033     FF(NEUS.LE.20.0) 60 70 2       0033     FF(NEUS.LE.200.0) 60 70 2       0033     FF(NEUS.LE.200.0) 60 70 2       0043     FF(NEUS.LE.200.0) 60 70 2       0044     FF(NEUS.LE.200.0) 60 70 2       0045     FF(NEUS.LE.2000.0) 60 70 2       0055     FF(NEUS.LE.2000.0) 60 70 2	IF(N:EC.3) 60 70 12 IF(N:EC.4) 60 70 13 IF(N:EC.4) 60 70 13 IF(N:EC.4) 60 70 13 IF(N:EC.4) 60 70 2 STEP=5.0 60 70 2 10 IF(PLUS.LE.200.0) 60 70 2 STEP=10.0 STEP=10.0 11 IF(PLUS.LE.200.0) 60 70 2 STEP=2.0 12 60 70 3 PM47(5)=1.0 STEP=2.0 13 17(5)=1.0 STEP=2.0 13 17(5)=1.0 STEP=2.0 13 17(5)=1.0 STEP=2.0 13 17(5)=1.0 STEP=2.0 13 17(5)=1.0 STEP=2	0033     FF(NEUS.15, 60 T0 12)       0133     FF(NEC.15, 60 T0 12)       0134     FF(NEC.15, 60 T0 13)       0135     FF(NEC.15, 60 T0 13)       0136     FF(NEC.15, 60 T0 13)       0137     FF(NEC.15, 60 T0 13)       0136     FF(NEC.15, 60 T0 13)       0137     FF(NEC.15, 60 T0 13)       0136     FF(NEC.15, 60, 10)       0139     10       0139     10       0139     10       014     PRHT(5)=1.0       0041     N=2       0043     11       014     PRHT(5)=1.0       0043     11       0044     N=2       0044     N=2       0045     FF(NEUS.LE.500.0)       0045     FF(NEUS.LE.500.0)       0045     FF(NEUS.LE.2000.0)       0055     FREP.20.0       0055     FREP.20.0       0055     FREP.20.0       0055     FF(NEUS.LE.200.0) </td <td></td> <td></td> <td></td>			
0011         IF(N.E0.4)         00         01           0132         IF(N.E0.5)         60         70         2           0134         N=1         N=1         00         2         0         2           0035         F(N.E0.5)         60         70         2         0         2         0         2           0035         F(PLUS.LE.200.0)         60         70         2         0         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         2         2         0         0         2         2         0         0         2         0         0         0         0         0         0         <	If (N.E0.4) G0 T0 2         IF (N.E0.4) G0 T0 2         IF (N.E0.5) G0 T0 2         NH1         STEP=5.0         G0 T0 2         STEP=5.0         G0 T0 2         STEP=1.0         STEP=5.0         STEP=1.0         STEP=5.0         PANT (5)=1.0         STEP=1.0         STEP=2.0         PANT (5)=1.0         STEP=2.0         PANT         PANT         PA	0011     Ff(x,E0.4)     60 T0 13       15     Ff(x,E0.4)     60 T0 2       0033     PHAT     Ff(x,E0.4)     60 T0 2       0034     PHAT     Ff(x,E0.4)     60 T0 2       0035     STEP=5.0     60 T0 2     7       0039     10     Ff(xPLU5.LE.200.0)     60 T0 2       0040     STEP=16.0     7     7       0041     Ff(xPLU5.LE.200.0)     60 T0 2       0041     Ff(xPLU5.LE.200.0)     60 T0 2       0041     Ff(xPLU5.LE.200.0)     60 T0 2       0041     Ff(xPLU5.LE.2000.0)     60 T0 2       0042     Ff(xPLU5.LE.2000.0)     60 T0 2       0043     Ff(xPLU5.LE.2000.0)     60 T0 2       0044     Ff(xPLU5.LE.2000.0)     60 T0 2       0045     Ff(xPLU5.LE.2000.0)     60 T0 2       0055     FMAT(5)=1.0     60 T0 2       0055     FMAT(5)=1.0     60 T0 2       0055     FF     FF       0055     FMAT(5)=1.0     60 T0 2       0055     FMAT(5)=1.0     60 T0 2       0055     FF     FF			0000
0012         FF(N=0.5)         G0         TO         Z           0013         FF(N=0.5)         G0         TO         Z           0013         FF(N=US.LF.20.0)         G0         TO         Z           0013         FF(N=US.LF.20.0)         G0         TO         Z           0013         FF(N=US.LF.200.0)         G0         TO         Z           0014         FF(N=US.LF.200.0)         G0         TO         Z           0014         FF(N=US.LF.200.0)         G0         TO         Z           0014         M=         FF         FF         G0         TO           0015         FF         FF         FF         G0         TO         Z           0015         FF         FF         FF         FF         FF         FF         FF           0015         FF         FF         FF	Ff. A.: E05)     G0     C0     Z       FF. YPLUS.LF.20.0)     G0     C0     Z       STEP=S.0     STEP=S.0     G0     Z       STEP=S.0     G0     C0     Z       PAHTSJ=1.0     STEP=10.0     G0     Z       STEP=10.0     G0     C0     Z       STEP=10.0     STEP=20.0     G0     G0       STEP=20.0     STEP=20.0     G0     G0       STEP=20.0     STEP=20.0     G0     G0       STEP=200.0     STEP=200.0     G0     G0	0012     FF(N=0.5) G0 T0 2       0013     FF(N=0.5) G0 T0 2       0013     N=1       0013     FF(N=LUS.LF.20.0) G0 T0 2       0013     STFPT(5)=1.0       0013     FF(N=LUS.LF.200.0) G0 T0 2       0014     FF(N=LUS.LF.200.0) G0 T0 2       0042     STFPT(5)=1.0       0042     STFPT(5)=1.0       0043     H1 F(N=LUS.LF.2000.0) G0 T0 2       0044     H2 F(N=LUS.LF.2000.0) G0 T0 2       0045     STFP=25.0       0045     STFP=25.0       0045     STFP=20.0       0055     STFP=100.0       0055     STFP=100.0       0055     STFP=100.0       0055     STFP=100.0			If (N.EQ.4) GO TO 13
00133 FF (YPLUS.LF.20.0) G0 T0 2 00134 Nat 00135 FF (YPLUS.LF.20.0) G0 T0 2 00139 10 FF (YPLUS.LE.200.0) G0 T0 2 00139 Nat 0013 11 F(YPLUS.LF.200.0) G0 T0 2 0013 11 F(YPLUS.LF.200.0) G0 T0 2 0014 Nat 0015 11 F(YPLUS.LF.1000.0) G0 T0 2 0015 11 F(YPLUS.LF.2000.0) G0 T0 2 0015 12 FF (YPLUS.LF.2000.0) G0 T0 2 0015 13 FF (YPLUS.LF.2000.0) G0 T0 2 0015 14 FF (YPLUS.LF.2000.0) FF (Y		00133 FF (YFULS.LF.20.0) G0 T0 2 00134 N=1 00135 STEP=1.0 00139 10 TE (YFULS.LE.200.0) G0 T0 2 00139 10 TE (YFULS.LE.200.0) G0 T0 2 0014 15 10 0 0014 15 10 0 0014 12 TE (YFULS.LF.200.0) G0 T0 2 0014 12 TE (YFULS.LF.200.0) G0 T0 2 0014 12 TE (YFULS.LF.200.0) G0 T0 2 0015 13 TE (YFULS.LF.2000.0) G0 T0 2 0015 14 TS 10 0 0015 14 TS 10 0 0015 15 TE (YFULS.LF.2000.0) G0 T0 2 0015 14 TS 10 0 0015 1			- - 
0035         FRHT(5)=1.0           0035         STEP=5.0           010         STEP=16.3           0040         STEP=16.3           0041         STEP=16.3           0041         STEP=16.3           0041         STEP=16.3           0041         STEP=16.3           0041         STEP=16.3           0045         STEP=16.3           0045         STEP=16.3           0045         STEP=25.0           0045         STEP=25.0           0045         STEP=26.0           0045         STEP=26.0           0045         STEP=26.0           0045         STEP=26.0           0055         STEP=26.0           0055         STEP=20.0           0055         STEP=20.0           0055         STEP=20.0           0055         STEP=20.0           0055         STEP=20.0           0055         STEP=20.0	FPHYT(5)=1.0       STEP=5.0       STEP=5.0       G0 T0 2       Hard       Part (5)=1.0       STEP=10.3       STEP=10.4       G0 T0 2       STEP=25.0       PART (5)=1.0       STEP=20.0       PART (5)=1.0       STEP=20.0       PART (5)=1.0       STEP=200.0       STEP=20.0	0035     PRHT(5)=1.0       0036     STEP=5.0       0039     10 2       0139     10 2       0139     10 2       0139     10 2       0139     10 2       0139     11 15.1       0140     210 2       0141     210 16.0       0141     210 2       0141     11 15.1       0141     11 15.1       0141     11 15.1       0141     210 2       0141     210 2       0141     11 15.1       0141     12 10.0       0141     12 11.0       0141     12 11.0       0141     12 11.0       0141     12 10.0       0141     12 10.0       0141     12 10.0       0141     12 11.0       0142     13 11 15.1       0145     14 15.1       0145     13 11.5       0145     14 15.1       0155     13 11.5       0155     13 11.5       0155     14 15.1       0155     13 11.5       0155     14 15.1       0155     14 15.1       0155     13 11.5       0155     14 15.1       0155     10 0.0    1	LN 0033		YPLUS.LF.20.0) 60 TO
0035         STEPF5.0         00         2           0036         STEPF5.0         0         70         2           0039         10         F(TPLUS.LE.200.0) G0 T0 2         2           0040         STEP16.0         0         7         2           0041         F(TPLUS.LE.200.0) G0 T0 2         0         7         2           0042         STEP16.0         0         7         7         7           0043         TF(TPLUS.LE.200.0) G0 T0 2         0         7 <t< td=""><td>10 5751110 56702 60702 942715110 942715110 942715110 5771516.0 11 177122.5 60702 12 177225.0 12 177225.0 12 177225.0 12 177225.0 12 177225.0 12 177225.0 13 177725.0 13 177725.0 10 2 10 2 10 2 10 2 10 2 10 2 10 2 10</td><td>0035     STEPIS.0       0037     50 10 2       0039     IF (YPLUS.LE.200.0) 60 10 2       0040     F(YPLUS.LE.200.0) 60 10 2       0041     F(YPLUS.LE.200.0) 60 10 2       0042     IF (YPLUS.LE.200.0) 60 10 2       0043     IF (YPLUS.LE.200.0) 60 10 2       0044     N=2       0045     IF (YPLUS.LE.200.0) 60 10 2       0055     IF (YPLUS.LE.200.0) 60 10 2</td><td></td><td></td><td></td></t<>	10 5751110 56702 60702 942715110 942715110 942715110 5771516.0 11 177122.5 60702 12 177225.0 12 177225.0 12 177225.0 12 177225.0 12 177225.0 12 177225.0 13 177725.0 13 177725.0 10 2 10 2 10 2 10 2 10 2 10 2 10 2 10	0035     STEPIS.0       0037     50 10 2       0039     IF (YPLUS.LE.200.0) 60 10 2       0040     F(YPLUS.LE.200.0) 60 10 2       0041     F(YPLUS.LE.200.0) 60 10 2       0042     IF (YPLUS.LE.200.0) 60 10 2       0043     IF (YPLUS.LE.200.0) 60 10 2       0044     N=2       0045     IF (YPLUS.LE.200.0) 60 10 2       0055     IF (YPLUS.LE.200.0) 60 10 2			
0037         00102         00102         00102           0039         17 (F (YELUS.LE.200.0)) GO TO 2           0040         257 (F 16.0)         00 TO 2           0041         257 (F 16.0)         00 TO 2           0042         260 TO 2         00 TO 2           0044         260 TO 2         00 TO 2           0045         11 F (YELUS.LE.500.0) GO TO 2           0045         260 TO 2         00 TO 2           0045         271 F 16.0         00 TO 2           0045         12 F (YELUS.LE.1000.0) GO TO 2         00 TO 2           0045         12 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0045         12 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0045         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13 F (YELUS.LE.2000.0) GO TO 20         00 TO 2           0055         13	10 17 220 10 17 72 20 11 17 77 12 10 2 11 17 77 12 10 2 11 17 77 12 10 2 12 17 70 2 12 17 70 2 12 17 70 2 13 17 70 2 14 17 1000.01 60 70 13 17 70 2 10 00.01 60 70 10 10 0 10	0037 00 10 2 0039 10 TE (YELUS-LE-200.0) 60 TO 2 0039 HE (YELUS-LE-200.0) 60 TO 2 0047 5TEP-16.7 0045 11 TE (YELUS-LE-500.0) 60 TO 2 0045 00 0 2 0045 00 0 2 0045 00 0 0 0045 12 TE (YELUS-LE-1000.0) 60 TO 2 0045 00 0 2 0045 12 TE (YELUS-LE-2000.0) 60 TO 2 0045 00 0 2 0045 00 0 2 0045 00 0 2 0045 00 0 0 0055 00 0 2 0055 00 0 0 0055 00 0 0050 0 0055 00 0 0050 0 0055 00 0 0050 0 0000 0 0000 0 0050 0 0000 0			
0038     10     If (YPLUS.LE.200.0) G0 T0 2       0040     204       0041     204       0043     11       014     21       0044     21       0045     11       11     11       11     11       11     11       11     11       11     11       11     11       11     11       11     11       11     11       11     12       12     12       0045     17       0045     12       0045     12       12     16       0045     12       12     16       0045     12       010     01       010     01       025     13       15     16       025     13       16     10       025     13       16     10       025     13       16     10       025     13       16     10       025     13       16     10       025     13       16     10       17     10   <	10 TF(YPLUS.LE.200.0) GO TO 2 N=2 PRH1(5)=1.0 CO TO 2 CO TO 2 CO TO 2 PRH2(5)=1.0 PRH2(5)=1.0 STEP=25.0 PRH2(5)=1.0 STEP=25.0 PRH2(5)=1.0 STEP=20.0 CO TO 2 PRH2(5)=1.0 STEP=100.0 STEP=100.0	0038 10 IF(YPLUS.LE.200.0) G0 T0 2 0040 82 0044 82 0044 9841(5)=1.0 0045 974716.0 0045 974716.0 0045 974715)=1.0 0045 97475)=1.0 0045 97475)=1.0 0045 97475)=1.0 0045 97475)=1.0 0055 984775)=1.0 0055 98475)=1.0 0055 98475)=1.0			
0000         0000 <th< td=""><td>Har (2) (2) (2) (2) (2) (2) (2) (2) (2) (2)</td><td>0041     N=2     N=2     N=2       0041     STEP=16.0     004       0041     STEP=16.0     00       0044     STEP=16.0     00       0044     N=3     004       0045     STEP=16.0     00       0045     STEP=16.0     00       0045     STEP=25.0     0       0045     STEP=25.0     0       0045     STEP=50.0     0       0045     STEP=10.0     00       0045     STEP=10.0     0       0045     STEP=10.0     0       0045     STEP=10.0     0</td><td></td><td>5</td><td>5.15.200.01 GO TO</td></th<>	Har (2) (2) (2) (2) (2) (2) (2) (2) (2) (2)	0041     N=2     N=2     N=2       0041     STEP=16.0     004       0041     STEP=16.0     00       0044     STEP=16.0     00       0044     N=3     004       0045     STEP=16.0     00       0045     STEP=16.0     00       0045     STEP=25.0     0       0045     STEP=25.0     0       0045     STEP=50.0     0       0045     STEP=10.0     00       0045     STEP=10.0     0       0045     STEP=10.0     0       0045     STEP=10.0     0		5	5.15.200.01 GO TO
0000         Desir(5)=1.0           0001         STEP=15.0           0002         STEP=15.0           0004         I           0004         I           0004         I           0004         I           0004         I           0004         I           004         I           10         I           11         I           12         I           13         I           14         I           15         I           16         I           17         I           18         I           19         I           10         I           11         I           12         I           13         I           14         I           15         I           16         I           17         I           18         I           19         I           10         I           11         I           12         I           13         I           14 <td>PANT (5)=1.0       STEPE 10.0       STEPE 10.0       60 T0 2       PANT (5)=1.0       STEPE 25.0       00 T0 2       12 If (YPLUS.LF.1000.0) 60 T0       PANT (5)=1.0       STEPE 25.0       12 If (YPLUS.LF.2060.0) 60 T0       13 If (YPLUS.LF.2060.0) 60 T0       13 If (YPLUS.LF.2060.0) 60 T0       PANT (5)=1.0       STEP=100.0</td> <td>0000         Dent(5)=1.0           0001         STEP=16.0           0002         00102           0004         12           0004         12           0004         12           0004         12           0004         12           0004         12           004         12           004         12           004         12           004         04           004         04           004         04           004         04           004         12           004         12           004         12           004         04           004         04           004         12           12         14           12         14           004         07           005         00           005         00           005         00           005         13           005         14           005         13           005         14           005         14           005</td> <td></td> <td></td> <td></td>	PANT (5)=1.0       STEPE 10.0       STEPE 10.0       60 T0 2       PANT (5)=1.0       STEPE 25.0       00 T0 2       12 If (YPLUS.LF.1000.0) 60 T0       PANT (5)=1.0       STEPE 25.0       12 If (YPLUS.LF.2060.0) 60 T0       13 If (YPLUS.LF.2060.0) 60 T0       13 If (YPLUS.LF.2060.0) 60 T0       PANT (5)=1.0       STEP=100.0	0000         Dent(5)=1.0           0001         STEP=16.0           0002         00102           0004         12           0004         12           0004         12           0004         12           0004         12           0004         12           004         12           004         12           004         12           004         04           004         04           004         04           004         04           004         12           004         12           004         12           004         04           004         04           004         12           12         14           12         14           004         07           005         00           005         00           005         00           005         13           005         14           005         13           005         14           005         14           005			
0041 516.0 5178-16.0 0045 11 15(7PLUS.LE.500.0) 60 70 2 0045 001 2 0045 001 12 0045 001 2 0045 00 2 0045 12 15(7PLUS.LF.1000.0) 60 70 0051 12 15(7PLUS.LF.2000.0) 60 70 0051 00 2 0051 13 15(7PLUS.LF.2000.0) 60 70 0055 00 2 0055 00 2 00 2 0 0 0 0 0 0 0 0 0 0 0 0 0	STFF=10.0 GO TO 2 GO TO 2 PAHT(5)=1.0 PAHT(5)=1.0 STFP=55.0 STFP=55.0 STFP=55.0 STFP=55.0 PAHT(5)=1.0 STFP=100.0 STFP=100.0 STFP=100.0	0041 516.0 5167-16.0 0045 11 15(17PLUS.LE.500.0) 60 70 2 0045 0045 0041 0 0045 0045 0040 0 0045 017 0 0045 15 15(17PLUS.LF.1000.0) 60 70 0050 0050 0041 0 0050 0050 007 2 0050 0050 007 0 0050 0050 0050 0 0050 0050 0 0050 0050			PRW1 (5) = 1.0
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0044 NET (VELUS-LE-S00.0) GO TO 2 0044 NET (VELUS-LE-S00.0) GO TO 2 0045 NET (VELUS-LE-1000.0) GO TO 2 0046 12 TET (VELUS-LE-1000.0) GO TO 0 0040 NET (VELUS-LE-2000.0) GO TO 0 0051 13 TET (VELUS-LE-2000.0) GO TO 0 0055 13 TET (S)=1.0 0055 STEP=100.0	11 I FYPLUS.LE.500.0) 60 T0 2 Has part(5)=1.0 5 TEP=23.0 5 TEP=23.0 6 T 0 2 12 If(YPLUS.LF.1000.0) 60 T0 Has (5)=1.0 5 TP = 20.0 5 TP = 20.0 5 TP = 100.0 5 TEP=100.0	0044 NET (VIS.LF.500.0) 60 T0 2 0044 NET (VIS.LF.500.0) 60 T0 2 0045 PENT(5)=1.0 0045 12 TEP=25.0 0046 12 TEP=25.0 0046 12 TEP=25.0 0046 12 TEP=25.0 0051 13 TEP=20.0 0052 13 TEP=20.0 0055 13 TEP=100.0 0055 5TEP=100.0			
0044 M=3 0045 PHT(5)=1.0 0045 STEP=25.0 0049 12 GT(70.2 0050 0050 PHT(5)=1.0 0055 PHT(5)=1.0 0055 13 HE(79LU5.LF.2000.0) GO TO 0055 13 HE(79LU5.LF.2000.0) GO TO 0055 PHT(5)=1.0 0055 PHT(5)=1.0 0055 STEP=100.0	PH43 PH43 STEP=25.0 STEP=25.0 FQ T05 FT PLUS.LF.1000.01 G0 T0 PH44 PH47 (5)=1.0 G0 T0 5 FT PFUS.LF.2060.01 G0 T0 FM (5)=1.0 STEP=100.0 STEP=100.0	0044 M=3 0045 PHT(5)=1.0 0045 STEP=25.0 0049 12 TF(70-25.0 0049 12 TF(70-25.0 0050 PHT(5)=1.0 0051 13 TF(70-10.0 0052 00 10 2 0055 PHT(5)=1.0 0055 PHT(5)=1.0 0055 PHT(5)=1.0 0055 PHT(5)=1.0		=	YPLUS.LE.500.0) 60 TO
0045 5 12 10 0045 5 12 10 0048 12 15 (19 US.LF.1000.0) 60 10 0048 12 15 (19 US.LF.1000.0) 60 10 0051 5 13 15 10 0 0051 13 15 (19 US.LF.2000.0) 60 10 0055 13 15 (19 US.LF.2000.0) 60 10 0054 984 75 910.0	12     15     10     50     70       12     15     15     15     10       14     15     15     10     10       15     15     10     10     10       13     15     15     10     60     10       13     15     15     10     10       13     15     15     10     60     10       13     15     15     10     60     10       15     15     10     0     10       15     15     10     0     10	0045 PENT (3) = 1.0 0046 STEP 75) = 1.0 0046 12 F(YPLUS.LF.1000.0) 60 T0 0048 PENT (5) = 1.0 0051 STEP 50.0 0051 13 F(YPLUS.LF.2000.0) 60 T0 0055 13 F(YPLUS.LF.2000.0) 60 T0 0055 PENT (5) = 1.0 0056 STEP = 100.0			
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00053 00059 0070 0071 0071 0071 0071 0071 0071	
00000 00000 0070 0071	
0071 0071	REMOVE THE ENCLOSED CARDS FOR NO FOLTMER CASES
1200	
1.00	D0ELTCH011) * (EXPTTPUS/B0PLUSE )-1.6)
1	
0074	0 100
0015 110	TF(DELVC.GF.0.336/12.0) 60 TO 112
0076	60 T0 100
0077 112	C030DCT*C/CT
0078	
0079	PHYNT 103.C0300CT
0040 103	COPAT(94 C0300C1=.F7.4)
0081	
111 2000	P UDELYC-6F .0.100/12.01 60 10 113
0085	
0096 102	FORMAT(94 F10005C1++F7_4)
0087	
0018 100	CONTINUE
0080	64H#4=2.3=50PT (CV)
0600	Def et an (0, 1) (5) (54 MH + 1) (5)
1400	
9004	
2000	TETECHER I I ARGENELIAN) 60 TO 30
9004	
0001	Ū]=ŪPEŪŠ=V <tape< td=""></tape<>
30 00	CONTINUE
0099 0	RÉMOVE THE ENCLOSED CARDS FOR NO POLYMER CASES
0100 A0 UPL	S=r(1) • OELa
0101	IF(M.EQ.2) 60 TO 6]
LN 0102 DISP	015PL & C=Y (2)
0103	HOHENTSY (1)
0104	If (UPLUS.GF. (0.99°*LAMDAC)) PRMT (5) = 1.0
0105 61	
0106	
0107	
112	
5710	

10011     Service:10       10011     Service:10 <td< th=""><th>111     20     Filestill       111     20     Filestill       111     20     Filestill       111     20     Filestill       111     21     Filestill       121     22     Filestil</th><th>111     Tentission       111     1       1111     1       <t< th=""><th>0113 0115 0115 0116 0119 0119 0120 0121 212 0122 212</th><th></th></t<></th></td<>	111     20     Filestill       111     20     Filestill       111     20     Filestill       111     20     Filestill       111     21     Filestill       121     22     Filestil	111     Tentission       111     1       1111     1 <t< th=""><th>0113 0115 0115 0116 0119 0119 0120 0121 212 0122 212</th><th></th></t<>	0113 0115 0115 0116 0119 0119 0120 0121 212 0122 212	
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1115       20       HT PULLE. 200.01       60 T 2         111       201151.1.0       2010 2       2010 2         111       21101.1.1       2010 2       2010 2         112       21101.1.1       2010 2       2010 2         113       21101.1.1       2010 2       2010 2         113       21101.1.1       2010 2       2010 2         113       21101.1.1       2010 2       2010 2         113       21101.1.1       2010 2       2010 2         113       21101.1.1       2010 2       2010 2         113       21101.1.1       2110 2       2010 2         113       21101.1.1       2110 2       2010 2         113       21101.1       2110 2       2010 2         113       21101.1       2110 2       2010 2         113       21101.1       2110 2       2010 2         113       21101.1       2110 2       2010 2         113       21101.1       2110 2       2110 2         113       21101.1       2100 3       2100 3         113       21101.1       2110 3       2110 3         113       21101.1       2100 3       2100 3	111     20     Trreuts.tr.200.01 60 fr 2       11     11     11       11     11     11       11     11     11       11     11     11       11     11     11       11     11     11       12     11     11       13     11     11       14     11     11       15     11     11       16     11     11       17     11     11       18     11     11       19     10     11       10     11     11       11     11     11       12     13     14       14     15     14       15     10     10       16     10     10       17     11     11       18     11     11       19     10     10       10     11     11       11     11     11       12     13     14       14     15     14       15     10     10       16     10     10       17     10     10       18     14     11 <t< td=""><td>111     20     Trreutus.tr.son.on 60 fr 2       11     Trreutus.tr.son.on 60 fr 2       12     Trreutus.tr.son.on 60 fr 2       13     Trreutus.tr.son.on 60 fr 2       14     Trreutus.tr.son.on 60 fr 2       15     Trreutus.tr.son.on 60 fr 2       16     Trreutus.tr.son.on 60 fr 2       17     Trreutus.tr.son.on 60 fr 2       18     Trreutus.tr.son.on 60 fr 2       19     Trreutus.tr.son.on 60 fr 2       10     Trreutus.tr.son.on 60 fr 2       11     Trreutus.tr.son.on 60 fr 2       12     Trreutus.tr.son.on 60 fr 2       13     Trreutus.tr.son.on 60 fr 2       14     Trreutus.tr.son.on 60 fr 2       15     Trreutus.tr.son.on 60 fr 2       16     Trreutus.tr.son.on 60 fr 2       10     Trreutus.tr.son.on 60 fr 2       11     Trreutus.tr.son.on 60 fr 3       12     Trreutus.tr.son.on 60 fr 3       13     Trreutus.tr.son.on 60 fr 3       14     Trreutus.tr.son.on 60 fr 3       15     Trreutus.tr.son.on 60 fr 3       16     Trreutus.tr.son.on 60 fr 3       17     Trreutus</td><td>0116 20 0117 0118 0119 0121 0121 21 0122</td><td></td></t<>	111     20     Trreutus.tr.son.on 60 fr 2       11     Trreutus.tr.son.on 60 fr 2       12     Trreutus.tr.son.on 60 fr 2       13     Trreutus.tr.son.on 60 fr 2       14     Trreutus.tr.son.on 60 fr 2       15     Trreutus.tr.son.on 60 fr 2       16     Trreutus.tr.son.on 60 fr 2       17     Trreutus.tr.son.on 60 fr 2       18     Trreutus.tr.son.on 60 fr 2       19     Trreutus.tr.son.on 60 fr 2       10     Trreutus.tr.son.on 60 fr 2       11     Trreutus.tr.son.on 60 fr 2       12     Trreutus.tr.son.on 60 fr 2       13     Trreutus.tr.son.on 60 fr 2       14     Trreutus.tr.son.on 60 fr 2       15     Trreutus.tr.son.on 60 fr 2       16     Trreutus.tr.son.on 60 fr 2       10     Trreutus.tr.son.on 60 fr 2       11     Trreutus.tr.son.on 60 fr 3       12     Trreutus.tr.son.on 60 fr 3       13     Trreutus.tr.son.on 60 fr 3       14     Trreutus.tr.son.on 60 fr 3       15     Trreutus.tr.son.on 60 fr 3       16     Trreutus.tr.son.on 60 fr 3       17     Trreutus	0116 20 0117 0118 0119 0121 0121 21 0122	
1       Tripeston         1<	1       1	31     Tripical       32     Tripical       33     Tripical       34     Tripical       35     Tripical       35     Tripical       36     Tripical       37     Tripical       38     Tripical       39     Tripical       31     Tripical       32     Tripical       33     Tripical       34     Tripical       35     Tripical       35     Tripical       36     Tripical       37     Tripical       36     Tripical       37     Tripical       37     Tripical       36     Tripical       37     Tripical       37     Tripical       38     Tripical       39     Tripical       31     Tripical       32     Tripical       33     Tripical       34     Tripical       35     Tripical       36     Tripical       37     Tripical       38     Tripical       39     Tripical       31     Tripical       32     Tripical       33     Tripical       34 <td< td=""><td>0115 0119 0120 0121 21</td><td>٤,</td></td<>	0115 0119 0120 0121 21	٤,
21       71       72       71       72         22       27       71       71       71         23       27       71       71       71         24       27       71       71       71         25       71       71       71       71         26       71       70       71       71         27       71       71       71       71         28       71       70       71       71         29       71       70       71       71         21       71       70       71       71         21       70       71       71       71       71         21       70       70       71       71       71         21       70       70       71       71       71         21       70       70       70       71       71         21       70       71       71       71       71       71         21       70       70       70       70       71       71         21       70       70       70       71       71       71	31       Titelate.coo.01 60 T0 2         32       Titelate.coo.01 60 T0 2         33       Titelate.coo.01 60 T0 2         34       Titelate.coo.01 60 T0 2         35       Titelate.coo.01 60 T0 2         36       Titelate.coo.01 60 T0 2         37       Titelate.coo.01 60 T0 2         38       Titelate.coo.01 60 T0 2         39       Titelate.coo.01 60 T0 2         31       Titelate.coo.01 60 T0 2         33       Titelate.coo.01 60 T0 2         34       Titelate.coo.01 60 T0 2         35       Titelate.coo.01 60 T0 2         36       Titelate.coo.01 60 T0 2         37       Titelate.coo.01 60 T0 2         38       Titelate.coo.01 60 T0 2         39       Titelate.coo.01 60 T0 3         31       Titelate.coo.01 60 T0 3         33       Titelate.coo.01 60 T0 3         34       Titelate.coo.01 60 T0 3         35       Titelate.coo.01 50 T0 3         36       Titelate.coo.01 50 T0 3         37       Titelate.coo.01 50 T0 3         38       Titelate.coo.01 50 T0 3         39       Titelate.coo.01 50 T0 3         39       Titelate.coo.01 50 T0 3         39       Titelate.coo.01 50 T0	31       1000-50       600-50         32       1000-50       600-50         33       1000-50       600-50         34       100-50       600-50         35       100-50       600-50         36       100-50       600-50         37       100-50       600-50         30       100-50       600-50         31       100-50       600-50         32       100-50       600-50         33       100-50       600-50         34       100-50       600-50         35       100-50       600-50         36       100-50       600-50         36       100-50       600-50         37       100-50       600-50         36       100-50       600-50         37       100-50       600-50         38       100-50       700-50         39       100-50       700-50         30       100-50       700-50         30       100-50       700-50         30       100-50       700-50         30       100-50       700-50         30       100-50       700-50 <t< td=""><td>0119 0120 0121 21 0122</td><td>(2)= •0</td></t<>	0119 0120 0121 21 0122	(2)= •0
21     71     71     71       22     71     71     71       23     71     72     72       24     70     7     7       25     72     70     7       26     70     7     7       27     70     7     7       28     75     70     7       29     75     75     7       20     7     7     7       21     7     7     7       22     75     7     7       23     75     7     7       24     7     7     7       25     7     7     7       26     7     7     7       27     7     7     7       27     7     7     7       28     7     7     7       29     7     7     7       20     7     7     7       20     7     7     7       20     7     7     7       20     7     7     7       20     7     7     7       20     7     7     7       20     7     7<	2)       "FireUs.LF.500.01 60 10 2         2)       "FireUs.FF.100.01 60 10 2         2)       "FireUs.FF.200.01 60 10 2         2)       "FireUs.FF.10.01 10 10 10 10 10 10 10 10 10 10 10 10 1	2)       Trivuls.LF.500.01 60 T0 2         2)       Trivuls.LF.500.01 60 T0 2         2)       Trivuls.LF.1000.01 60 T0 2         2)       Trivuls.LF.2000.01 60 T0 2         2)       Trivuls.LF.111 00 T0 T0         3)       Trivuls.LF.111 00 T0 T0         4)       Trivuls.LF.111 00 T0 T0         4)       Trivuls.LF.111 00 T0 T0         1)       Trivuls.LF.111 00 T0 T0         1)       Trivuls.LF.111 00 T0 T0	0122 21	
0123       WHITS:-1.0         0124       60 10 2         0103       60 10 2         0103       60 10 2         0103       60 10 2         0103       60 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0103       61 10 2         0104       10 00 10         0105       61 10 2         0104       10 00 10         0105       11 000 10         0104       11 000 10         0105       11 000 10         0104       11 000 10         014       11 000 10         014       11 10 00 10         015       11 10 00 10         016       11 10 00 10         016       11 10 00 10         016       11 10 00 10         016       11 10 00 10         016       11 10 00 10         016       11 10 00 10         016       11 10 10	0122     PHATTST-L0       0123     PHATTST-L0       0123     FX       0124     PX       0131     FX       0132     FX       0133     PX       0133     FX       0134     FX       0134     FX       0134     FX       0134     FX       0134     FX       0135     FX       0134     FX       0135     FX       0135	0122     PHIT[5]:1.0       0123     PHIT[5]:1.0       0123     TP100.01 GO TO 2       0123     TP100.01 GO TO 2       0131     TP100.01 GO TO 2       0102     TP100.01 GO TO 2       0103     TP100.01 GO TO 3       0103     TP100.01 TO 10       0104     TP100.01 TO 10       0105     TP100.01 TO 10       0104     TP100.01 TO 10       0105     TP100.01 TO 10       0104     TP100.01 TO 10       0105     TP100.01 TO 10       0104     TP100.01 TO 10	0122	PLÚS-LF-500.0) GO TO 2
375       377       377       377         103       377       177       100.00       100       10         103       377       1710       100.00       100       10       10         103       377       1710       101.00       10<	22       III (PULS.LE.1000.01) 60 10 2         103       23         103       23         103       23         103       23         103       21         103       23         103       24         103       24         103       24         103       24         103       24         103       24         103       24         104       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         105       24         106       24         107       24         108       24         108       24         108       24	22       If (PULS, LE, 1000, 0)       60       2         103       STEPTSS, 10       0       10         103       STEPTSS, 10       11       10       10         104       STEPTSS, 10       10       10       10         105       STEPTSS, 10       11       10       10         105       STEPTSS, 10       10       10       10         105       STEPTSS, 10       11       10       10         105       STEPTSS, 10       11       10       10         105       STEPTSS, 10       10       10       10         106       STEPTSS, 10       11       10       10         107       STEPTSSS, 10       10 <td></td> <td>12:21 N</td>		12:21 N
27 FULLE.100.01 60 T0 2 28 FITULE.100.01 60 T0 2 29 FITULE.200.01 60 T0 2 29 FITULE.200.01 60 T0 2 20 FITULE.200.01 60 T0 2 20 FITULE.200.01 60 T0 2 20 FITULE.200.01 60 T0 2 20 FITULE.111 60 T0 20 20 FITULE.111 60 FITU	22 FUSLES.F. 1000.01 60 TO 2 23 FUSLES.100.01 60 TO 2 24 FUSLES.000.01 60 TO 2 25 FUSLES.200.01 60 TO 2 26 FUSLES.200.01 60 TO 2 27 FUSLES.200.01 60 TO 2 28 FUSLES.200.01 60 TO 2 29 FUSLES.200.01 60 TO 2 20 FUSLES.200.01 F	22 60 10 2 23 10 2 24 10 2 25 10 2 26 10 2 27 10 2 28 10 10 28 10 2 28 10 10 28 10 10 28 10 10 28 10 10 29 10 10 20 10 20 10 10 20	0124	0.52
23     Mr. FULS.LE.2000.01 60 T0 2       133     1577LUS.LE.2000.01 60 T0 7       133     1571LUS.LI.11 60 T0 70       133     1571LUS.LI.11 60 T0 70       134     7004170       135     1704170       135     1704170       135     1704170       135     1704170       135     1704170       135     1704170       135     104070       135     1704170       135     1704170       135     1704170       135     104070	2.4     Mr. Full     Mr. Full </td <td>13     24     Marrowstr.1000.01 60 10 2       13     27155.1.0       13     27155.1.0       13     17751.0.0       13     17751.0.0       14     1751.0.0       15     17751.0.0       15     17751.0.0       16     171.1.1.0       17     171.1.1.1.0       18     171.1.1.1.0       19     7001.1.1.1.1.1.1.0       101     17       101     17       101     17       101     17       11     100 10.0       11     100 10.0       12     111.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.</td> <td>0125</td> <td></td>	13     24     Marrowstr.1000.01 60 10 2       13     27155.1.0       13     27155.1.0       13     17751.0.0       13     17751.0.0       14     1751.0.0       15     17751.0.0       15     17751.0.0       16     171.1.1.0       17     171.1.1.1.0       18     171.1.1.1.0       19     7001.1.1.1.1.1.1.0       101     17       101     17       101     17       101     17       11     100 10.0       11     100 10.0       12     111.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.	0125	
Diff         Dest (5)=1.0           010         010.2         010.2           0113         15.11         0.10.2           113         15.11         0.10.2           113         15.11         0.10.2           113         15.11         0.10.2           113         15.11         0.10.2           113         0.10.2         0.10.2           113         0.10.7         0.10.7           113         0.10.7         0.10.7           113         0.10.7         0.10.7           114         15.11.1         0.10.7           115         0.10.7         0.10.7           114         15.6         0.10.7           117         14.1         15.6           114         15.6         0.10.7           114         15.6         0.10.7           114         15.6         0.10.7           115         0.10.7         0.10.7           114         15.6         0.10.7           115         0.10.7         0.10.7           115         0.10.7         0.10.7           115         0.10.7         0.10.7           115         0.10.7	01228         Dentification           0131         23         17         10.2         10.2         10.2         10.3	1128     Perif (5)=1.0       1129     (0) 10 2       113     17 PLUS.LE.2000.0) 60 10 2       113     17 PLUS.LE.10       113     17 PLUS.LE.10       114     15 GBEATEP THAN 10 *)       115     10 FBEATEP THAN 10 *)       115     10 FBEATEP THAN       115     10 FBEATEP THAN       115     10 FBEATE	0127 22	(4) The data is a maximum of the state of the same shares being the state of the same is a sub-
0120 0120 0131 0131 0132 0132 0132 0135 0135 010 0135 010 0135 010 0135 010 014 014 014 014 014 014 014	0120 0120 0131 0132 0132 0133 0134 0135 0135 0135 0137 0137 0137 0137 0147 0137 0147	0100       00100       001000       001000         0111       0110000       0010000       0010000         01110       01000000       0100000       0100000         0111000000000000000000000000000000000	0128	(5)=1.0
0131       23       If (rPLUS.LE.2000.01 60 T0 2         0133       40       577P-100.0         0134       570 7       5         0135       40       70         0135       40       71         0136       70 7       5         0137       5       70 7         0138       71 20       100.0         139       71 1100.0       60 70         139       71 1100.0       70         139       71 1100.0       60 70         141       71       70         131       70       70         141       71       70         141       70       70         141       71       70         141       70       70         170       70       70         141       70       70         141       70       70         141       70       70         141       70       70         141       70       70         141       70       70         141       70       70         142       70       70         141	0131       23       If (rPLUS.LE.2000.01 60 T0 2         0133       40       577 P100.0         0134       577 P100.0         0135       40         0135       50 T0 2         0136       577 P100.0         0137       50 T0 2         0138       517 P100.0         0139       71 F100.0         0139       71 F1110.0         014       71         11       70 CONTINUE         014       71         11       70 CONTINUE         014       71         11       70 CONTINUE         014       70 CONTINUE         014       70 CONTINUE         015       70 CONTINUE         014       70 CONTINUE         014       70 CONTINUE         015       70 CONTINUE         014       70 CONTINUE         015       70 CONTINUE         015       70 CONTINUE         015       70 CONTINUE         014       70 CONTINUE         015       70 CONTINUE         015       70 CONTINUE         015       70 CONTINUE         016       70 CONTINUE	113)       23       If (rPLUS.LE.2000.01 60 T0 2         113       40       517 FLUS.LE.2000.01 60 T0 2         113       40       517 FLUS.LE.2000.01 60 T0 2         113       40       71 FLUS.LE.2000.01 60 T0 70         113       50 FLID.00.01       51.4X2*DELV1 DELTAD-AK2*DELV         113       71 FLUS.LE.111 60 T0 70       70         114       71 5 GREATER FLAN 10 *1       70         113       70 CONTAULE       70         114       71 5 GREATER FLAN 10 *1       70         114       71 5 GREATER FLAN 10 *1       70         115       70       70       70         114       71 5 GREATER FLAN 10 *1       70         114       71 5 GREATER FLAN 10 *1       70         115       70       70       70         115       70       70       70         115       70       70       70         115       70       70       70         115	0130	5000 50 1 50 1
0132 PWF(5)-1.0 517 00.0 134 00 70 135 40 FLIAD-6T.(1X720ELY1) DELTAD-AK70ELY 135 2017440 141 71 141 71	0133 PWF(5)-1.0 5170 01 01 00.0 1134 40 101 01 01 01 01 01 01 01 01 01 01 01 0	0133 PWF(5)=1.0 5170 010 5170 010 5170 010 5170 010 5170 010 5170 010 5170 010 5170 010 5170 01 5170	0131 23	PLUS.LE.2000.0) 60 TO 2
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NIS TO CONTINUE THE IS OFFICE THAN TO RETURN USASI FORFAN DIAGNOSTIC RESULTS FOR HOUTPUT NO EAROAS	NIN EARDAST FORTANCE THE IS OFFICE THAN TO BETURN USAST FORTAAN DIAGNOSTIC RESULTS FOR HOUTPUT	NIN EARDAST FORTANTE THE IS OFFICIENTIAN TO USAST FORTAN DIAGNOSTIC RESULTS FOR HOUTPUT	0140	
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AL PHA	-1-01733	-0-32690	-0-21956	-0.19763	-0.18542	-0.16489	20231-0-	-0.13430	20521 0-	-0.13462	28501 0-		15250.6-	P0180 D+	-0.07586	-16010-0-	-0.00445		12740-0-	-9.04210	-0.03746	-0.07255	-0.02760	-0.02350		211000-	-0.00717	-0.00419	-0.60110		0.00071	2000000	02100.0	0.70171	001	0.00125	02100"0	0.60117	01130.0	0.00097	24000.0		0.00045	5E030.0	0.00022	0.00013		-0.00019	-0-00063	-0.00256	0.0000.0	0.00020
061.	1.7		0.00	3.51	35.5	1 ° 85	2.24	4	9.64	47.3	0.94		53.0	1.12	55.7	56.9			51.5	62.5	63.5	54°.	65°E	-1-2			0.00	70.7	71.6 2.072		577.0	1.992	611.5	1.1.4	451.4	1.000	1.140	115.4	751.3	9.277	804°2		E 96	1040.9	1142.3	6°1821	1 755	1875.1	1986.9	2129.0	1.1555	1 E222
R0.			64143	5.1.20	1060.5	r leel	1749.6	1967.5	2.169.2	2411.4	2670.9	0.000 0.0707	1.2956	P-0521	1.4676	3440.0			100.5	4868.	5026.3	5175.3	5312.1	4°1645		5744	5820.4	5645	1-128521	12505.7	12662.1	: 2775	12803.0	L DEAL	12635.0	1.25521	12787 4	12749.1	12685.7	12605.4	00221	5 * 66CJI	12135.4	TTGRU.F	11808.0	11612.8	2 19611	11145.9	3.84111	6-24611	11624.4	11615.5
DELY	0.0164	1010.0	0100	0.0105	0.0105	0.0105	0100	0.0107	1010.0	0.0108	0.0108	1110.0	0.0112	- EIID-0	0.0114	2112	/ 110.0	0110-0	1210.0	6-0123	5210-0	0.0127	0.0129	1610.0		0.0134	2410.0	0.0145	0.01.6	2420.0	0.0606	0.0634	0.052	1290.0	9.0712	2.0735		0.0812	J-DESK	0.0905	0.0454 0.1031		0.1215	0.1341	0.1507	5.138 5.138	0.00M	0.2741	2262.0	0.3090	0.3144	0.3151
SDRAGS	0000°e		2000.0	0.0605	0.000	0.0012	0.0022	0.0028	0.0035	0.0043	0.0052	5400.0	0.0088	2010.0	0.0116	0.0136	2510.0		0.0771	0.0246	0.0773	2969,0	2660.0	2460 0		0.0473	0.0513	5.0555	0.0599	6150.0	0.1340	0.1637	0.1770	1122.6	70	0.2653	22020 7115 D	0 ]+19	TTHE D	1264-0			0127.0	ENER.0	0.9880	2651.1		2.0645	E1.22.2	2,3850		2.4578
9	1.000		0.915	0.882	0.837	0 179	0.685	0.633	0.578	£25°0		255-0	6.296	162.0	0.174	0.119	400 0		-0.052	-0.124	-0.163	-0.199	-0-230	195.0-	100.01	-0.315	-0.325	166.0-	201-0-	10.0-	-0.310	-0.302	162.0-	-0.26H	+0-2-0+	272.0-	-0.015	1020-	081-0-	-0.156	-0-137		-0.076	-0.062	-0-047	-0.036		-0.036	-0.051	-0-105	-0-1-0-	-0-178
LANDA	4.306	11.17	18.032	19.652	21.363	211.65	25.408	26.476	107.12	194.92	165.95	11.136	31.955	201.55	33.564	34 . 304	970.01	101 11	37.841	012.16	36.279	38.874		40.00F	1.035	+1.610	-2.118	42.520	11.64	21.141	PE.15	21.452	21.514	21.640	21.705	144.15		21.984	22.040	22.215	25.355	77.4 66	22.871	101.65	23.377	517 °E2	201.42	248.42	210-52	25.215	1.6.55	25.343
PDRAG	100.0	104	0.720	1.006	1.378		2.509	2.863	1.21		CT -		4.670	*L8.*	5.035 1		176 3		5.202	5.109	4.977		÷ 511	197.14	1.867	3.584	0°2°0	2 907	101-1	2.125	1.663	1.340	1.228	120.0	524.0	0.715	1 2 2 2	16.0	0.324	0.235	191.0	A 154	0.023	100.0-	-0.017	120.0-	220-0-	-0.037	-0-037	-0.037	-0.012	400.0-
XX XX	010.0		162.0	6.36.9	101 0	0.414	0.562	0.636	0.649			0.505	0.839	113.0	606.0	6 E E O		810 1	1.020	1.060	1.078	1.095	109	1.121		1-147	1.151	1.1.74	21. 251.	1.154	1.144	1.141	46 T • 1	174	1.121	1.115	1107	1.096	T. 546	1.076	1.065	270	1.018	5	1.023					1.052		
0 a a	100.0	210.0	0.018	0.022	0.026	0.000	0.036	0.039	270 0	040.0		0.055	0.057	0.060	0 0 3	0.050	0.071	0.074	0.077	0.079	280.0	0 0 B4	0.087		10000	0.096	800°0	0.100	0.102	0.105	0.108	0.110	111.0	6.113	0.11.	0.115	1110	0.117	9.118	0.119	0.120	221.0	9.123	0.123	0.124	121.0		0.125	0.125	0.125	0.124	0.124
XLSTAR COOLO	225.00.0	0.00618	0.00047	0.01014	0.01207	0.01572	16710.0	0.01892	0.02054	01220-0	000000	0.07721	0.02899	14010.0	0.03258			12070 0	0.04223	0.04432	0.04546	0.04457	0.05096	01220 0	0.05474	0.04101		0.04673	0.07305	0.07651	416 BO.0	0.08797	0.04040	0.94746	10101.0	0.10490		CP711.0	0.12510	0.11395	0.14412		0.14966	0.21319	٠	17642.0	10237.0	41604.0	5-145.0	0.57011	10.54.0	0.5A468 0.5A735
S-AREA	0.000.0	0.00056	50100.0	0.00150	0.00213	0.00159	4E400 0	0.00517	0.00607	0,000,0	51000°0	0.01051	0.01184	0.01327	0.01478		10010 0	10100	0.02401	22420-0	15820.0	1010.0	ELEED.O	130E0 0	0.04278	0.04521	10.049AF	0.05381	12240.0	0.00747	0.0770.0	0.08424	1250.0	0.04459	0.10417	10011.0		0.13061	1:531.0	0.15464	745/1.0		0.24450	0.29783	14074	12414.0	1164.0	0.74120	0.42649	0.89]78 0 91759	52416-0	0.92100
SUPF-X	0.00761	91119	26910.0	0.02195	0.02614		0.03749	0.04047	0.04448			0.05900	0.05279	0.06663	0.07055			0.04707	0.09146	1,09597	2 1001 0	14501.0	0.11036	100110	0.12635	0.13212	71961.0		12851.0	0.14570	0.14004	0.19052	20102-0		0.21974	25422.0	1.24518	0.25534	10010.0	1002.0			0.41074	0.46158			04440-0	1.04744	1.15129	1.27453	1.25995	1.27197
AX TAL-X	10,000.0	0100-0	10200.0	0.00287	0.00405	0.00680	0.00920	0.00974	14110-0	0.01517	01776	0.01947	0.07194	27720.0	0.02711			0.03949	20640.0	0-0-673	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.450.0	01650.0	0.05460	73570.0	FPAT0.0	0.08461		0.10360	0.11105	0.12505	0.13539	4541-0	0.15572	0.1-335	161/1.0	14041 0	6.199AA	0.21534	0.23457		1515 0	0.35504	0,40403	0.47427		22120.0	1.01230	1.09563	1.21194	1.21340	1.21485

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0.00020	02000*0	0-00050		0.000.0	02000.0	0.00018	0.000.5	0.00330	100000		0.00040	15000.0	0.00025	0.00021	0.00016	0.00019	1000010	12000-0-	10,00,01	05520-0-	17610.0-	95500-0	0.010.0	15140.0	0.05510	H0250"0	0.22827	14715"0	3.80983										
2220.1	8222	1.0525		2235.1	2736.5	2238.4	1-0+22	2232.6	2.8755		6.1665	2372.0	2413.6	2455.7	2448.0	2657.4	2742.8	2830-6	1152.4	34.35.4	3505.6	3515.4	3483.5		B.971E	2957.4	2278.4	1697.6	1.677									ł	
11597.1	8-98511	6*67211		11553.2	11544.3	11535.4	11526.9	9-26211	9.85501	9576	9143.0	8728.5	8326.2	7932.5	1545-4 4 H H I - 4	6139.9	5410.9	4699.3	3779.4	1032.4	4062.9	3472.6	3791-9	5-191E	5140.3	2310.2	0.6211	504.4	58.7							ľ		1	
0, 3154 2225	0.315/	1915.0		1716.0	0.3175	0.3178	1416.0	0.3228	1445 0	1277	0.3656	7195.0	1.941	0.4070	0.4205	E # 7 # 0	0.5166	0.5636	0.6668	0.6633	0.4648	0.6738	0.5899	0.7512	0.8075	0.9004	1-5621	4.3416	027.9939				1						
2.4639		2.4699		0413 0	7.4814	2.4849	2.4779	2.5175	2.55A0	1924 6	2767.2	2.8557	1-10-5	2.9694	1/01.1	6761.6	5.2713	3.3383	2464.6	75.22.6	3.4463	3.4490	3.4515	3.4545	3. 4587	J.4695	3.4631	3.4637	3.46382602										
-0.178				-0-177	-0.177	-0-177	-0-176	0 - 1 3 d	-0.040	-0.076	-0.015	-0.006	0.000	500.0	0.010	0.021	0.075	0.025	-0.135	267-0-	-0.510	-0.517	10.474	-0.269	-0.112	0.070	0.559	0.808	0.979			1							
25.347				25.358	75.360	25.363	25,365	22.155	20.186	21-2-2C	26.4.52	25.533	25.584	25.635	111.22	25.856	25.059	26.051	26.357	26.617	26.676	26.685	26.658	26.508	ETE. 35	26.179	25.415	24.549	512.22							I		1	
0.011	110.0	20°0		0.047	0.054	0.062	0.063	6/1.0		102.0	0.633	0.653	0.659	0.654	0.605	0.550	0.489	0.40	0.475	0.569	0.629	0.719	0.832	1.060	1.133	1.140	0.818	5	0.170					-					
1.045				1.085	1.085	1.085	1.045	140.1			1.007	1.003	1.000	100.07	266.0	0.949	0.988	845 0	1-066	1.197	1.229	1.231	1.214	1.126	1.054	0.960	0.564	0.439	0.14.		-								
0.124		1010	124	0.124	721.0	0.124	7210	0.122	1110	0110	0.106	0.102	990.0	660-0	280.0	0.074	0.045	0.057	140.0	0.041	0.040	0.039	0.038	0.035	0.032	0.029	0.020	E10-0	100.0		-			-			4		
0.58802			0.59071	9-192.0	0.59705	615923	0.59340	51000°D	0.414.0	0.65613	0.67547	18496.0	0.71414	0.73348	0.78646	9.42533	0-96400	0.90255	64749.0	0.974.94	0.97641	10879.0	0.97956	0.9631	0.94511	0.98721 n 98950	0.99746	0.99547	1.00000					l					
0.92214		0.92554	0.97668	0.92781	76826-0	0.93007	0.93120	H5295 0		80160-1	1.05954	1.08689	41611.I	1.13829	1.20175	1.24269	1.27920	TELLE I	1.35509	1.35944	1.36031	1.36118	1.36205	1.36380	1.36467	1.36554	1.36728	1.36804	1.36852										
67672°I		27770	1.27425	1.24070	1.24216	1.28342	1.28507		11005	FP044	1.46240	1.50464	1.54656	1.5444J	1.70359	1.78735	1.47110	1.95425	10000.2	211112	2.11453	2.11800	2.12157	2.12919	2.13336	20161.5	2.14930	2.15666	2 1 1 5 2 6 1					1					
21776	13412	100022	72555	52503	.22649	. 22793	66622	20190	12242	16459	40625	\$4192	*895s	-53125	.64583	71957.	.91250	ERSPH.	26760	65139	.05464	05798	2,06131	0479A	16170.	40%L0	ICIRO.	E54R0.	04560					-					

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THOMEN' DELP	0.000816 24.968212	0.000949	0.000979 9.709989	0.000945 9.484663	0.000984 9.478769	0.001021	0.101058 9.422734	0.001067 9.397919	0.001167 9.369180	0.001147 9.340944	0.001219 0.31254P	0.001300 9.282995	0.0014°6 9.239306	0.001536	0.001693	0.001+73 9.107894	0.002178 9.065078	9.002452 9.025452	0, 002885 8.985597	742558.8 9°4600.0
015PLAC DELY (FT)	184200.0	0.001586 0.004094	0.001726	0.001661 0.003966	0-001725	0.001784 9.004290	0.001843 0.004451	0.001361 0.004486	0.001927	0.001994	0.005141	0.002236	0.002423	0.302615 0.006476	0.002865	146800.0	0.003614 0.009191	0-00-080 0-010-0	0.004701	0.005495 0.014300
DELTAD PUPAG	0.000716 2.125157	0.000452	0.000247	0.000315	0.000316	0.000318 0.452701	05000.0 175958.0	0.715408	0.000325 0.000325	0-000327	0.000330	0.328505	0.235899	0.000340	0.000344	0.000348	0.000352 0.022585	0.000356	0.000360	0.001433 -0.027027
	190.1 0.085268	340.15 1.0401.0	320.1 0.114896	1.016 177651.0	320.1	1.0EE 1.0E541.0	340.1	340.1	350.1 0.174455	360.1 0.187106	1.086 0.200220	400.1 0.219955	1.05445.0	460-1	1.002	575.1 0.341986	625.1 0.388648	700.1 0.447570	800.1 0.525205	5*9219 1*526
LDGHD 3Sn1408	-0-0 0.533683	0,9 0,533683	1.6 0.533683	2.1 0.533683	2.5	0~533663 0.533663	3.5 0.533683	0.533683	4.6 0.533683	5°5 5°5	5.9 0.533683	6.9 0.533683	8.2 0.533683	0.533683	11.4	13.5 0.533683	16.1 0.533683	19.5 0 <u>533683</u>	24.43 0.5336A3	30.4
VSTARF AKJ AK5	0.02 0.18	1.060455 0.07 0.28	0.998725 0.02 0.27	0.07150 0.02 0.28	0.02 0.28	0.02 0.28	0.02 0.26	0.968495 0.02 0.23	0.02 0.24	0.054006	0.02 0.28 0.02 0.28	0.02 0.28	0.924602	0.02 0.29	0.903430 0.02 0.24	0.05103 7.0 20.0	0.02 0.29	0.074496 0.02 0.29	0.865415 0.02 0.29	0.855458 0.02 0.29
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ацриа Ахс	0.05098835	0.001873319	0.002845797	0.003634808 0.14177750	0.003741714 0.14954000	0.003683294 0.15572000	0.003716161 0.16335000	0.103901948 0.17150750	0.03675922	0.003583555 0.18966250	0.003485544	0.003267495 0.71533500	0.002856733	0.002472128 0.25692250	31.9610~ 0.002066930 00195789 ^.28338500	32.041215 0.001652269 .00194810 0.31537750	0.001252639	0.000892453 0.40602750	0.00580099	0+000323272 0+57122500
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