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(continued from front page)

20. Abstract

Specific applications for randomly winned 43m crystals are shown. To form a proper theory for the development of such crystals we have studied the effects of crystal absorption and twin spacing on such crystals. We have also calculated the distribution function of the expected power from randomly twinned crystals and have shown it to take the form

 $\omega(P) = \frac{1}{N} e^{-P/N}$

for large N.

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DEVELOPMENT OF POWERFUL WAVELENGTH-TUNABLE

INFRARED LASER SYSTEM

Technical Report No. 3

For Period Ending December 31, 1975

ARPA Order Number: 2840 Program Code Number: 6E20 Massachusetts Institute of Technology Effective Date: July 1, 1975 Expiration Date: June 30, 1976 Total Value: \$44,987 Contract No.: NCO014-76-C-0431

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TUNABLE LASERS ARPA Contract No. NOOO14-76-C-0431 Technical Report No. 3 For Period Ending 12/31/75

Summary

In our research on nonlinear crystals and processes for frequency mixing in the infrared we have made progress along two fronts.

We have produced tunable infrared from 11µ to 23µ by mixing the outputs from two ruby-pumped dye lasers in proustite. Peak powers of 2 watts were shown for the wavelength range 16-20µ. Analysis of the output power verses wavelength showed that beam convergence at the nonlinear crystal can be responsible for a substantial reduction in output from that which one would expect were the crystal at the beam waste. This effect is studied quantitatively and an excellent agreement is found between theory and experiment.

We show that there are applications where randomly twinned crystals could meet specific needs for crystals to be used in nonlinear mixing processes. In order to lay a proper background for the development of such crystals we have made a preliminary theoretical investigation of the effects of crystal absorption and twin spacing on the power production from a randomly twinned crystal. We have also found the probability distribution function for the power produced by a randomly twinned crystal. This distribution function has the form

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$$\omega(P) = \frac{1}{N} e^{-P/N}$$

where N is the number of twins with spacings larger than the coherence length, and N >> 1. P is normalized so that N twin planes give on the average a power of N. Since the distribution is quite wide there is a substantial probability of getting much less power than expected. The probability of observing an enhancement of N/2 or less for N twins is 40%. Accordingly some crystal selection will be necessary.

DEVELOPMENT OF POWERFUL WAVELENGTH-TUNABLE

INFRARED LASER SYSTEM

ARPA Contract No. NOOOL-76-C-0431 Semi-Annual Technica. Report No. 3 For Period Ending December 31, 1975

Research Program:

In our research program we have been studying in detail, various approaches to the production of tunable infrared power. The emphasis of this program lies with nonlinear mixing in solids. In this vein we are studying traditional phase matchable materials and also materials that are not traditionally phase matchable but are potentially so given the development of techniques to produce controlled twinning. Ramar shifting of dye laser radiation to produce tunable I.R. has great potential. We are not currently pressing this program.

Accomplishments:

A) <u>Phase Matchable Materials</u>. We have studied difference frequency generation in proustite in a frequency range where the crystal shows substantial absorption. The variation of the absorption coefficient with wavelength was used to probe the effective coherence length of the mixing process and show that even a weak beam convergence or divergence at the crystal can produce a substantial reduction in the difference frequency power from that which one would expect were the crystal at the beam waist.

-1-

This work is being written for publication and a draft of this paper appears as Appendix I.

B) Phase Matching by Twin Planes. The coherence length for some nonlinear mixing processes in $\overline{43}$ m materials can be fairly long. For example the coherence length for frequency doubling of 10.6µ radiation is greater than 200µ for both CdTe and ZnTe. This combination of large coherence length, large nonlinear coefficient and high damage threshold means that it is practical to consider synthesizing a crystal from a stack of carefully cut and polished plates, each with a precise orientation and thickness. A relatively few plates (5 or 6) is quite sufficient to cause pump depletion. Such an experiment is currently in progress at Los Alamos using CdTe. In order to assure some strength these plates were cut and polished to a thickness several times the coherence length. The orienting, cutting, and polishing requirements are quite stringent as each plate must be oriented so that both the fundamental and the harmonic beam have the same polarization and can enter and leave the crystals at Brewster's angle. The optical path length inside the crystal must also be very close to n + 1/2 coherence lengths so that the cumulative errors of several plates will not be important.

It occurred to us that the same result could be achieved much more readily by using a <u>randomly</u> twinned crystal with 30 or more twins spaced by at least 200µ. This crystal would have approximately the same thickness as the synthesized crystal but would not have the same orientation

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requirements. It would also have only two surfaces, neither one critical. The power produced by the stack of plates is proportional to the square of the number of plates (ignoring depletion) while for randomly spacing we expect a linear relationship between the number of twins and the power produced. Accordingly 30 randomly spaced twins would produce as much harmonic power as 5 or 6 plates.

Since for such applications randomly twinned crystals appear to have considerable potential we have considered randomly twinned crystals from a theoretical standpoint. Appendices II, III, and IV study briefly three different aspects of this problem.

APPENDIX I

DIFFERENCE FREQUENCY GENERATION IN PROUSTITE FROM 11 TO 23µ

Productite has been shown to be a useful nonlinear material by a multiplicity of authors. Harmonic⁽¹⁾ and difference-frequency generation, ^(2,3,4) parametric oscillation, ^(5,6) and up conversion^(7,8,9) have been successfully accomplished over the wavelength range of about 1 to 12 μ . The high intrinsic absorptivity of this material for wavelengths greater than 12 μ , however, has provided a deterrent for nonlinear mixing experiments at these longer wavelengths. In this experiment we have used difference-frequency generation in product tunable I.R. over the wavelength range 11 to 23 μ . Despite substantial absorption, significant levels of I.R. power are achieved over most of this wavelength range.

A ruby laser was used to end pump two tunable dye lasers operating with orthogonal polarizations. These two lasers operated in the wavelength range .84 \div 1.0 μ using Kodak dye Air 1 and Nippon Kankoh-Shikiso Kenkyusho dye NE 1748. The dye laser outputs were about 5 m_j with a pulse width of about 30 ns. The linewidths were measured to be about 3 Å. By mixing the output of these two dye lasers the entire range of 11 to 23 μ could be phase matched with only a 7° rotation of the proustite crystal. The phase matching angles were found to be close to those calculated from the index of refraction data of Hobden⁽¹⁰⁾. In order to

correlate the generated infrared power with the absorptivity of proustite it was necessary to measure the absorption coefficient of proustite over the wavelength range of interest. Previous measurements of the proustite absorption coefficient in this wavelength range (11, 12, 13)were not sufficiently quantitative for our purposes. Proustite is a negatively birefringent uniaxial crystal, and type 1 phase matching was used. The I.R. signal exists in the crystal as an ordinary wave; accordingly, we measured the ordinary wave absorption coefficient. This measurement was performed on a Beckman IR-12 dual-beam spectrophotometer operated in the single beam mode. Polarization was provided by an AgC1 polarizer. Transmission measurements were made on crystals (14) (grown, cut and polished by R.R.E) with thicknesses of 3 mm, 1.0 mm and 0.3 mm. The results of these measurements are shown on Figure 1.

The absorption peaks at 10μ , 14.5μ , 16.5μ and 22.5μ are readily identifiables as combination and overtons bands by reference to the comprehensive work⁽¹⁵⁾ of Byer, Bobb, Lefkowitz and Deaver. Their notation is used in the absorption peak identifications shown in Fig. 1.

Measurements were made of the infrared power generated by mixing the outputs of the two ruby-pumped dye lasers in a 4 mm thick proustite crystal⁽¹⁴⁾. The crystal was cut 20° to the optic axis in the appropriate quadrant to make the d_{31} and d_{22} contributions to the nonlinear polarizations additive⁽¹⁶⁾. For each wavelength the crystal orientation was adjusted for optimum output. Focusing of the dye laser beams was accomplished with a 35 cm focal length lens. A f:2 mirror was used to focus the infrared radiation leaving the crystal onto HgCdTe detector.

The results of these measurements are shown on Fig. 1. The responsivity of the HgCdTe detector used for these measurements peaked at about 17μ and fell off rapidly at longer wavelengths. The exact shape of the detector response curve is of considerable importance for determining the power levels reached for wavelengths greater than 17μ .

A twinned ZnSe crystal⁽¹⁷⁾ was used in place of the proustite to calibrate the detector. This crystal is transparent out to about 22 μ . Past 17 μ the detected signal was observed to chop off at between a factor of 2.4 and 2.8 per micron. Correcting for the expected λ^2 dependence of the difference frequency generation, and adding an additional factor of λ to compensate for the reduced number of twins available at longer wavelengths we find the detector fall off to be between 2.0 and 2.4 per micron. We have adopted the factor of 2 fall off rate for these measurements as it seems to describe the data most consistently.

In order to see the influence of absorption on the infrared power produced in the experiment we must first remove the wavelength dependence. Besides the explicit λ_{IR}^{-2} power dependence the variation of the indices of refraction and nonlinear coefficient with wavelength must be considered. The refractive index variations are small for the difference frequency wavelength range 10 + 24µ both for the IR beam and the pump beams. This implies by Miller's rule⁽¹⁸⁾ that the nonlinear coefficient will also change only slightly. We consider these wavelengths too far removed from restrahl for resonance effects such as those seen by Faust and Henry⁽¹⁹⁾ to be important. Thus to some reasonable approximation the wavelength dependence only as the usual λ^{-2} term and indirectly

through the absorption coefficient. Thus we find

$$P\lambda^{2} = A L_{eff}^{2}(\alpha)$$
 (1)

where L_{eff} is the effective crystal length taking into account absorption, beam walk off and the like. Figure 2 shows L_{eff}^2 , suitably normalized, plotted against the absorption coefficient α data at all wavelengths we measured. (The normalization of L_{eff}^2 will be apparent later.) Since this plot combines the experimental errors of both the absorption coefficient and I.R. difference frequency experiments, it is not surprising that there is substantial scatter in the data.

The effective length of an absorbing crystal used in a difference frequency generation experiment can be readily derived. Following the approach of Miller and Nordland⁽¹⁸⁾ we find for perfect phase matching

$$\left(\frac{L_{eff}}{L}\right)^2 = \frac{1 + e^{-\alpha L} - 2e^{-1/2} \alpha L}{(\alpha/2)^2}$$
(2)

It is not possible to fit the observed data with this function. This equation appears as the $\Delta K = 0$ curve on Figure 2. The only free parameter in this equation is the normalization which corresponds to an arbitrary displacement of the curve along the vertical axis. It is clear that if the curve is forced to fit the data for large α it will not fit for small α and vice versa. In the limit of strong absorption, we expect an $1/\alpha^2$ dependence of the power regardless of other effects,

and accordingly it is appropriate to match equation (2) to the large α points. The discrepancy between the observed and expected values for small α must be due to a limitation other than crystal length.

Double refraction and beam divergence (20) are not to blame, as for this experiment both the aperture length and the effective length of focus were substantially greater than the crystal length. Nor is it possible that the dye laser linewidths are responsible, as they are only about 4 cm⁻¹, and the phase matching angle varies only very slowly with wavelength. (Indeed at 18µ this change is zero.) However the crystal was not placed at the focus of the lens, and accordingly the crystal spread meant that all parts of the input beams could not be phase matched for the same crystal orientation. This effect was responsible for the early saturation of the power production.

In order to determine quantitatively the effect of this spread of input angles we must return to a more general form of equation 2, leaving in the effect of imperfect phase matching and integrating over a distribution of input angles.

$$\left(\frac{L_{eff}}{L}\right)^{2} = \frac{\int \frac{(1+e^{-\alpha L}-2e^{-1/2\alpha L} \cos(\Delta K(\theta,\phi)L)}{(\Delta K(\theta,\phi)L)^{2} + (\alpha L/2)^{2}} I_{1}(\theta,\phi) I_{2}(\theta,\phi)d\theta d\phi}{\int I_{1}(\theta,\phi) I_{2}(\theta,\phi)d\theta d\phi}$$
(3)

Here $I_1(\theta,\phi)$, $I_2(\theta,\phi)$ are the intensity distribution of the point beams and $\Delta K(\theta,\phi) = 2\pi \left(\frac{n_1(\theta,\phi)}{\lambda_1} - \frac{n_2}{\lambda_1} - \frac{n_3}{\lambda_1} \right)$. We have assumed that the

crystal is far from the focal point of the lens so that $I_1(\theta,\phi)$ and $I_2(\theta,\phi)$ are essentially constant over the length of the crystal.

This integration is not possible to do analytically in general, but can be approximated after some simplifying assumptions are made. First, we assume $I_1(\theta,\phi)$ and $I_2(\theta,\phi)$ are rectangular functions with the same width. This is a good approximation for our case as the dye lasers were run multimode and apertured outside the cavity. Secondly, we consider the distribution of input angles to be the same for both dye beams, appropriate for our case, but not in general as often lenses are used to match beam sizes and are accordingly only used in one beam^(2,4). Since the outputs of the two dye lasers employed in our experiment had nearly identical spatial characteristics, the lens was used to adjust the power density at the crystal. For the phase matching angle used in this experiment, the angular spread in the plane of the optic axis contributed much more to the mismatch than the spread perpendicular toit and we can ignore the contribution due to the beam spread perpendicular to the optic axis.

After defining the full width of the rectangular functions $I_n(\theta,\phi)$ as <u>a</u>; and defining $g = \frac{d(\Delta K)}{d\theta}$ we can look at this equation in a few of its limits:

1) for
$$\alpha L \gg 1$$
, $\alpha L \gg gaL$ $\left(\frac{L_{eff}}{L}\right)^2 \div \frac{4}{(\alpha L)^2}$
2) for $gaL \ll 1$, $\alpha L \ll 1$ $\left(\frac{L_{eff}}{L}\right)^2 \div 1$
3) for $\alpha L \ll 1$, $gaL \gg 1$ $\left(\frac{L_{eff}}{L}\right)^2 \div \frac{2\pi}{gaL}$

Intermediate values can be obtained by machine integration. Where great accuracy is not required the approximation of the integration for gaL >> 1 is given by

$$\left(\frac{L_{eff}}{L}\right)^{2} \sim \frac{4}{\alpha gaL^{2}} \left(1 - e^{-\alpha L/2}\right) \left[\left(1 - e^{-\alpha L/2}\right) \tan^{-1} \frac{gaL}{\alpha L} + \pi e^{-1/2\alpha L}\right]$$
(4)

This equation is plotted in figure 2 for various values of gaL. Best fit to the data is found with gaL = 20. This is in reasonable agreement with experiment as $ga \stackrel{\sim}{=} 40 \text{ cm}^{-1}$ for our experiment and L = .4 cmgiving an anticipated value of gaL of 16.

In conclusion we have shown that reasonable levels of tunable infrared power can be produced in crystals that show strong absorption. In assessing the value of a nonlinear crystal, it is apparent that such terms as transparent and opague should be used with caution. We have also shown the effect of a spread of beam angles on the power produced in a nonlinear crystal. Even a weak beam convergence can lead to a substantial reduction in the difference frequency power generated.

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APPENDIX II

POWER PRODUCED BY HARMONIC GENERATION IN A RANDOMLY TWINNED ABSORBING CRYSTAL

We show here a derivation of equation (1) given without proof in our paper <u>Enhancement of Second-Harmonic Generation in Zinc Selenide</u> by Crystal Defects.

We chose as a comfortable starting point equation 2.41 (page 43) of Zernike and Midwinter's book Applied Nonlinear Optics.

For general $\omega_1 + \omega_2 = \omega_3$ mixing

$$E_{3} = \frac{-8\pi i \omega_{3}^{2} d_{123}}{K_{3} c^{2}} E_{1} E_{2} \int e^{i\Delta Kz} dz \qquad (1)$$

In the special case of frequency doubling $E_1 = E_2$. Also

$$\Delta K = 2\pi \left(\frac{2n_1}{\lambda_1} - \frac{n_3}{\lambda_3} \right) = \frac{4\pi (n_1 - n_3)}{\lambda_1}$$

where the subscript 1 refers to the fundamental and 3 to the harmonic. Thus

$$E_{3} = \frac{-8\pi i \omega_{3}^{2} d_{113}}{K_{3} c^{2}} E_{1}^{2} \int e^{i\Delta Kz} dz \qquad (2)$$

With N twins, the crystal is broken into N + 1 domains with a reversal of sign of the nonlinear coefficient in each domain. If the twins appear at positions L_j

$$E_{3} = \frac{-8\pi i \omega_{3}^{2} d_{113}}{K_{3} c^{2}} E_{1}^{2} \sum_{j=0}^{N} (-1)^{n} \int_{L_{j}}^{L_{j+1}} e^{i\Delta Kz} dz$$

$$= \frac{-8\pi i \omega_{3}^{2} d_{113}}{K_{3} c^{2}} E_{1}^{2} \sum_{j=0}^{N} (-1)^{j} \frac{1}{i\Delta K} \left[e^{i\Delta KL} j + 1 - e^{i\Delta KL} j \right] \qquad (3)$$

$$= \frac{-8\pi i \omega_{3}^{2} d_{113}}{K_{3} c^{2} \Delta K} E_{1}^{2} \left[2 \sum_{j=1}^{N} (-1)^{j} e^{i\Delta KL} j + e^{i\Delta KL} o + (-1)^{N+1} e^{i\Delta KL} N + L \right]$$

R. C. Miller and W. A. Nordland [Phys. Rev., B2, 4896, (1970)] show how to account for absorption:

$$n = n' + \frac{i\lambda_3^{\alpha_3}}{4\pi}$$
 (4)

$$\frac{\Delta K}{2\pi} = \frac{2n_1}{\lambda_1} - \frac{n_3'}{\lambda_3} - \frac{i\lambda_3^{\alpha_3}}{\lambda_3^{4\pi}} = \frac{\Delta K'}{2\pi} - \frac{i\alpha_3}{4\pi}$$
(5)

Here the primed n and K are pure real. Substituting we find:*

$$E_{3} = \frac{-8\pi \omega_{3}^{2}}{K_{3} c^{2}} \frac{d_{113} E_{1}^{2}}{(\Delta K - i\alpha/2)} \left[(-1)^{N+1} + 2 \sum_{j=1}^{N} (-1)^{j} e^{\alpha/2L_{j}} e^{i\Delta K'L} \right]$$
(6)

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* corresponds to the far edge of the crystal so $L_{N+1} = 0$ and $L_0 = -L$ where L is the crystal length. Assume a large number of twins with $\Delta KL >> 1$.

$$P_{3} = \frac{cn_{3}}{2\pi} E_{3} E_{3}^{*} = \frac{64 \pi^{2} \omega_{3}^{4} n_{3} d_{113}^{2} (E_{1}E_{1}^{*})^{2}}{2\pi K_{3}^{2} c^{3} (\Delta K^{*2} + \alpha^{2})^{4}}$$

$$\cdot \left[1 + 2 \int_{j=1}^{N} e^{-\alpha/2} L_{j} \left(+i\Delta K^{*}L_{j} + e^{-i\Delta K^{*}L_{j}} \right) (-1)^{N+j+1} + 4 \int_{j=1}^{N} \sum_{k=1}^{N} (-1)^{j+k} e^{-\alpha/2} (L_{j} + L_{k}) e^{i\Delta K^{*}(L_{j} - L_{k})} \right]$$
(7)

Obviously (7) is of little help when we don't know the values of the L_j , but if we assume they are randomly spaced everything simplifies greatly. For close twin spacings $2\pi \gg (\Delta K(L_j - L_{j+1}))$ the second term contributes nothing as it alternates sign with each twin while the cosine term changes only slightly. For wide twin spacings $\Delta K(L_j - L_{j+1}) > 2\pi$ the cosine term has essentially randomized by the next plane so for randomly spaced twins this term will contribute nothing. The third term will suffer the same cancellations except for the cases j = k. So under this assumption

$$P_{3} = \frac{32 \pi \omega_{3}^{2} n_{3} d_{113}^{2} (E_{1}E_{1}^{*})^{2}}{(n_{3})^{2} \omega_{3}^{2} c(\Delta K'^{2} + \alpha^{2}/4)} \begin{bmatrix} 1 + 4 \sum_{j=1}^{N} e^{-\alpha L_{j}} \end{bmatrix}$$
(8)

If we assume the twins are roughly evenly distributed through the crystal, then the sum can be replaced by an integral for large N

$$\sum_{j=1}^{N} e^{-\alpha L_j} + \frac{N}{L} \int_{0}^{L} e^{-\alpha x} dx = \frac{N}{\alpha L} (1 - e^{-\alpha L})$$
(9)

So

$$P_{3} = 32\pi \frac{c}{\lambda_{3}^{2} n_{3}} d_{113}^{2} \frac{P_{1}^{2} 4\pi^{2}}{\sum (1 - e^{-L})} \left[\frac{1 + \frac{4N}{\alpha L} (1 - e^{-L})}{\Delta K^{2} + \alpha^{2}/4} \right]$$
(10)

But by Miller's rule

$$d_{113} = (n_1^2 - 1)^2 (n_3^2 - 1) \delta_{113}$$

where δ_{113} is a material constant independent of the index (Miller's δ). So

$$P_{3} = \frac{128\pi^{3} P_{1}^{2} (n_{1}^{2}-1)^{4} (n_{3}^{2}-1)^{2} \delta_{133}^{2}}{\lambda^{2} n_{3} n_{1}^{2} c} \left[\frac{1 + \frac{4N}{\alpha L} (1-e^{-\alpha L})}{(\Delta \kappa^{2} + \alpha^{2}/4)} \right]$$
(11)

The key approximation appears in the step between equations 7 and 8. The assumption there is that the phases of the radiation emitted by each segment are randomly correlated. In practice there is some accidental correlation which brings in contributions from those terms. Recently we took one crystal orientation and swept ΔK (by changing λ) and observed large fluctuations in the power produced in a difference frequency measurement. This modulation results from the changing contributions from these terms (which can subtract from the power produced as well as add to it). Periodic twinning with the right spacing would produce positive contributions from all these terms.

APFENDIX III

DIFFERENCE FREQUENCY POWER PRODUCED BY N TWINS WITH AN APBITRARY SPACING IN A NON-ABSORBING 43m CRYSTAL

In this model we consider a crystal with N twin planes separated by distances large compared to a coherence length.



For simplicity we will assume N >> 1 so we can ignore contributions from the ends. We also consider $\alpha L << 1$ so that absorption effects are negligible. In this case for difference frequency generation

$$P_{3} = \frac{128 \pi^{3} d_{123}^{2} P_{1}P_{2}}{\lambda_{3}^{2} n_{3} n_{2} n_{1} c(\Delta K')^{2}} \left[4 \sum_{j=1}^{N} \sum_{k=1}^{N} (-1)^{j+k} e^{i\Delta K'(L_{j}-L_{k})} \right].$$
(1)

This equation follows from equation (7) in Appendix II.

We break down this equation to see separately the contributions from the j = k and the j + k terms

$$P_{3} \propto N + \sum_{j=1}^{N-1} \sum_{k=j+1}^{N} (-1)^{j+k} \left(e^{i\Delta K'(L_{j} - L_{k})} + e^{-i\Delta K'(L_{j} - L_{k})} \right)$$

= N + 2 $\sum_{j=1}^{N-1} \sum_{k=j+1}^{N} (-1)^{j+k} \cos[\Delta K'(L_{j} - L_{k})]$ (2)

A simplest model of the twin spacing would evoke a function $g_1(x-x_0)$ which is defined as the probability of finding the next twin at position x, given a twin at position x_0 . We assume here that a twin's positional probability can be written as a function of the previous twin without explicit dependence on the position of the twin before that one, and also that knowledge of the positions of all previous twins will provide no further information. This is a very powerful assumption and probably is not generally the case. Given that assumption we can proceed to find $g_n(x-x_0)$, the probability of finding at x the nth twin away from the twin at x_0 .

$$g_{2}(x-x_{0}) = \int_{x_{0}}^{x} g_{1}(x'-x_{0}) g_{1}(x-x') dx'$$
 (3)

$$g_{n}(x-x_{o}) = \int_{x_{o}}^{x} g_{n-1}(x'-x_{o}) g_{1}(x-x') dx'$$
 (4)



We return to equation (2) for a moment and rewrite it by twin spacings

$$P_{3} \propto N + \sum_{j=1}^{N-1} \sum_{k=1}^{N-j} (-1)^{k} \cos \Delta K (L_{j} - L_{j+k})$$
(5)

and

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$$P_{3} \propto N+2\sum_{k=1}^{N-1} \sum_{j=1}^{N-k} (-1)^{k} \cos \Delta K (L_{j}-L_{j+k})$$
(6)

Now we average over the probability distributions to get the average power.

$$P_{3} \propto N+2 \qquad (N-k) (-1)^{k} \int_{0}^{\infty} \cos \Delta K g_{k}(x) dx \qquad (7)$$

$$k=1 \qquad 0$$

Consider first the case where the coherence length is very long or $g_k(x)$ has very small values. In this limit

$$\int \cos \Delta K g_k(x) dx + 1$$

and

$$P_{3} = N + 2\sum_{k=1}^{N-1} (N-k) (-1)^{k}$$

$$= \begin{cases} 0 \quad (for \ N \ odd) \\ 1 \quad (for \ N \ even) \end{cases}$$
(8)

Thus very closely spaced twins do not contribute to the radiated power.

If we make the opposite assumption (as in Appendix II) and $\Delta K g_k(x) >> 2\pi$, then the cosine terms average to zero and

$$P_3 \propto N$$
 (9)

We find then that the power radiaced from a group of X twins randomly spaced but with a characteristic spacing ΔL goes roughly



A accurate description of the region between 0 and $2\pi/\Delta K$ would require accurate knowledge of the $g_k(x)$.

APPENDIX IV

DISTRIBUTION OF OUTPUT POWERS OF A RANDOMLY 1WINNED NON ABSORBING CRYSTAL WHERE THE COHERENCE LENGTH IS MUCH SMALLER THAN THE TWIN SPACING

In this model we consider a crystal with N twin planes separated by distances large compared to a coherence length.

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For simplicity we assume N >> 1 so we can ignore the contributions from the ends. We also consider $\alpha L << 1$ so that absorption effects are negligible. In this case the radiation E fields effectively produced at each twin site add up as in a random walk.



The probability distribution of the end point $\omega(\vec{E})$ is determined by this two dimensional random walk.

$$\omega(\vec{E}) = \frac{1}{\pi N} e^{-|\vec{E}|^2/N}$$
(1)

Here we have chosen the normalization so that the field produced for each twin is of unit value.

The distribution is radially symmetric so we can convert from \vec{E} to E magnitude easily

$$\omega(E) = \int_{0}^{2\pi} \omega(\tilde{E}) d\theta = \frac{2}{N} e^{-E^2/N} . \qquad (2)$$

We can check what the average power we can expect is by solving

$$\overline{E^2} = \int_{0}^{\infty} E^2 \omega(E) \ EdE = \frac{2}{N} \int_{0}^{\infty} E^2 e^{-E^2/N} \ EdE .$$
(3)

For clarity we substitute $P = E^2$, dP = 2EdE so

$$\overline{P} = \overline{E^2} = \frac{1}{N} \int_{0}^{\infty} P e^{-P/N} dP = N$$
(4)

which is as we expected.

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We also have found the probability distribution function for P

$$\omega(\mathbf{P}) = \frac{1}{N} e^{-\mathbf{P}/\mathbf{N}} . \tag{5}$$



In many practical experimental situations, a spread of convergence angles, local spatial heating and spreads of input wavelengths will mean that a number of different samples of this distribution will be made for each pulse. Effectively, different parts of the beam will see different sets of spacings of the twins. As has been done in other branches of physics we shall loosely define a term "coherence area" to refer to that part of the beam that sees the same set of twin spacings. For the next section we will consider the case of there being m such coherence areas each sharing the same fraction of the input beam.

To develop the function $\omega(P,m)$ we shall first find $\omega(P,2)$

$$\omega(P,2) = \int_{0}^{P} \omega(P') \ \omega(P-P') \ dP'$$

= $\int_{0}^{P} \frac{1}{N^{2}} e^{-P'/N} e^{-(P-P')/N} \ dP' = \frac{P}{N^{2}} e^{-P/N}$ (6)

Continuing,

$$\omega(P,3) = \int \omega(2P',2) \ \omega(P-P') \ dP'$$

$$= \int \frac{1}{N^3} P' e^{-P'/N} e^{-(P-P')/N} dP' = \frac{1}{2} \left(\frac{P}{N}\right)^2 \frac{e^{-P/N}}{N}$$
(7)

By now the limit is clear

$$\omega(\mathbf{P},\mathbf{m}) = \frac{1}{\mathbf{m}!} \left(\frac{\mathbf{P}}{\mathbf{N}}\right)^{\mathbf{m}} \frac{\mathbf{e}^{-\mathbf{P}/\mathbf{N}}}{\mathbf{N}}$$
(8)

This has the form of a poissonian distribution

$$P = \frac{e^{-b}b^{a}}{a!}$$
(9)

which has, in the limit of large \underline{b} , the form

$$P + \frac{1}{\sqrt{2\pi b}} e^{-(a-b)^2/2b}$$
 (10)

Accordingly we find

$$\omega(\mathbf{P},\mathbf{m}) \rightarrow \frac{1}{N} \frac{1}{\sqrt{\mathbf{P}/N}} e^{-(\mathbf{m}-\mathbf{P}/N)^2/2\mathbf{P}/N}$$
(11)

for large u.

We have now m times as great an average power, as m different systems were added together. In reality each of these systems had 1/m of the input power so we must substitute mP for P.

$$\omega(P,m) = \frac{1}{\sqrt{NPm}} e^{-(m-mP/N^2/2P/N)}$$
 (12)

$$= \frac{1}{\sqrt{NPm}} e^{-(P-N)^2/2PN/m}$$
(13)

For large m (already assumed in (11)) this becomes

$$\omega(\mathbf{P},\mathbf{m}) \cong \frac{1}{\sqrt{NPm}} e^{-(\mathbf{P}/H)^2/2N^2/m}$$
(14)

which has a half width of $\ N/\sqrt{m}$.

To find a r.m.s. fluctuation of a factor of two one would therefore need

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$$.3N = N/\sqrt{m}$$

m ∿

\$0

APPENDIX V

BIBLIOGRAPHY OF PAPERS RELATED TO ENHANCED NONLINEAR

OPTICAL EFFECTS IN ROTATIONALLY TWINNED CRYSTALS

C. F. Dewey, Jr. L. O. Hocker

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APPENDIX VA

Nonlinear Optical Properties of 43m Crystals

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properties of the II-Cds, CdSe, CdTe, ZnS, ZnSe, ZnTe

SEPTEMBER 1975

no, ne 0.		CdS 0.5 to 16	CdSe 0.8 to 23 ⁽¹⁾	1 10 28		0.4 to 14	0.5 to 19	0.5 10 > 20
thickness (microns) Absorption Coefficient et 10. microns (cm ⁻¹) Indices of Refraction ⁽⁶⁾ 0. no, no 0.								
microns (cm ⁻¹) Indices of Refraction ⁽⁶⁾ 0. No. No. 0.		0.01	0.002	0.002			0.005	0.008
Indices of Refraction ⁽⁶⁾ 0.		0.01				2.4207(5)		
no, ne 0.	.50					2.4207	2.655(6)	
	.56	2.566, 2.580			2.356, 2.378(4)	2 369(4)	2.61(3)	3.064(9)
	589	2.501, 2.519			2.350, 2.370	2.3640 ⁽⁵⁾		3.035(9)
crom, 0.	.60	2.404, 2.501				2.333315		2.913(9)
0	.70	2.407, 2.424				2.3336		2.879(9)
0	.75	2.386, 2.403	2.703, 2.710			2.3146(5)		2.853(9)
0	.80	2.371, 2.387	2.640, 2.645	2.84(3)		2.2932(5)	2.48(3)	2.790(9)
	.00	2.330, 2.347	2.546, 2.565	2.64		2.2782.5)		2.741(9)
	.40	2.300, 2.316	2.491, 2.510					
3	1.39		2.4519, 2.4715(8)	2.69(3)			2.392(7)	2.70(8)
1	0.6	2.226, 2.239(2)	2.427, 2.447(1)	42(13)			48(15) . 38(7)	
1/n dn/dT et 10.6 microns (10 ⁻⁶ /°C)				42.00				
Electro-Optic Constants				45(10),88	R)	-1.1 -2 0(11,12)	1 61(6), 2.0(8), 2.2(8 4.51(9) 3.9(10)
r41 ^T (10 ⁻¹² m/V)				45'10', 88"	(3)	104(11)		2.2(10) 7.1(10)
Half-weve Voltage (kV) Wavelength (microns)				10 ,106	5	0 404, 0 546	0 54 75, 0.546, 10.8	0.589, 10.6
r ₄₁ S(10 ⁻¹² m/V) Wavelength (microns)						1.6, 1.4 ⁽⁶⁾ 0.633, 3 39	2.0 ⁽⁸⁾ 0.633	4.3 ⁽⁸⁾ 0.633
-		1.1(8)	1.8 ⁽⁸⁾					
r13 ^S (10 ⁻¹² m/V)		0.633	3.39					
Wavelength (microns)		2.4(8)	4.3(8)					
r33 ^S (10 ⁻¹² m/V) Wevelength (microns)		0.633	3.39					
rc ^T (10 ⁻¹² m/V) Wavelength (microns)		4 ⁽³⁹⁾ , 5.5 ⁽⁸⁾ 0.589, 10.6						
Nonlineer Optical Susception	bilities					31 ± 8	78 ± 29	4 ± 2
(10-12m/V)	d14			-17±6		31 - 0		
(rounded off) et 10.6 microns ⁽⁸⁾	d33	44 ± 13	55 ± 13		37 ± 13	4		
	d31	-26 ± 6	29 ± 6		-19±6			
	d15	29 ± 7	31 ± 8		21 ± 8	25 ± 2	32 = 2	3.0 ± 0.2
et 1.06 microns ⁽⁸⁾	d36					1911	32 - 2	2.6 ± 0.3
	d14							
	433	31 ± 2			15 ± 2			
	431	-16 ± 1			-9 ±2			
	d15	17 ± 1			8 ± 1			
Piezo-Optic Constents								
et 10.6 microns				-5.91 ± 0.2	(14)			
(10-12m2/N)	911			-5.91 ± 0.4 2.22 ± 0.0	n(14)			
	912			2.22 ± 0.0 -2.85 ± 0.3	-(14)			
	944		22	-2.85 ± 0.3	33.14.			
Pulsed Demage Threshold (10 ⁶ w/cm ²)	5		60			6 b a	Cubic	Cubic
Crystal Structure(16)		Hexagonal	Hexagonal	Cubic	Hexagonal	Cubic	Sphaiarite	Sphaierite
		Wurtzite	Wurtzite	Sphalerite	Wurtzite PSmc ^(e)	Sphalerite F43m	F43m	F43m
Space Group (16)		PEmc	P6mc	F43 m		r 4.JM		
Wurtzite Positional Param	neter	0.378	0.377		0.374		0.0244	
u ⁽¹⁷⁾ (ideal = 0.375)	•	4.1367(18)	4.2972(18)	6.4830	3.8218(19		5 668 7	6.1034
Lattice Constants (A)	•0	± .0003	± 0003	± .0004	± 0004	± 0002	1 0001	± 0003
at 25°C		d.7161	7.0065		6.25875			
	°0	±.0005	1.0006		±.0001			

		CdS	CdSe	CdTe	ZnS (Hex.)	ZnS (Cub.)	ZnSe	ZnTe	14
Calculated Density, 25°C (g/cm ³)		4.619	5.670	5.849	4.067	4.086	8.262	5.636	
Cleavage		[1120] [1010]	1120 1010	[110]	[1120] [1010]	[110]	[110]	[110]	\mathcal{I}
Thermal Expension ^(C) (10 ^{-6/G} C) Lc		4.60	4.90	4.5(21)	6.5(22)	5.9	7.1(7)	8.56	
lle		2.6	2.9		4 6(22)				
Temperature (^O C)		250.1000	250.1000	500	250	280.1000	290	250 1000	
Thermal Conductivity, 25 (w/cm/ ⁰ C)		0.27		0.06			0.16	0 18	
Specific Heat, 25°C (cal/g	V [®] K)	0.088(24)		0.053	135	0.116(24)	0.016(24)		
Metting Point (^O C) Vepor Pressure at M.P. (e)		1397±20(18) 2.1	1256±2 ⁰⁽¹⁶⁾ 0.51	1097±2° 1.5	1718±10 ⁽²⁵	1	1526 ± 10 ⁽²⁵⁾	1292±5° 0.6	
Vapor Pressure (atm.): Lo		<u>-11,353</u> T +7.144		- <u>9,969</u> T +6.7		-12,7'.5 +6.830	-12,592	100-00	
IPminimum total vi		T +/.144	-11,101 T +6.948	T +6.7	780	+6.830	<u>-12,592</u> +6.850 T	- <u>11,101</u> T +6.961	
pressure, T inK)									
Flexural Strength (psi) Estimeted Meximum Safe		~4000 > 200°	~ 3000 > 200°	~ 3000 > 200°	~ 10,000 >200 °	> 2000	~ 8500 >200°	~ 3600 > 200°	
Operating Temperatur		~ 200	- 200	- 200	~ 200		~200*	/200-	
Typical Dark Resistivity		> 10 ⁸	> 10 ⁸	10 ⁶		10-1010(11)	t0 ⁸ -10 ⁹⁽²³⁾	108-109	
(ohm-cm)									
Hell Mobilities (cm ² /Vsec				1000 ^(e)					
Highest measured et 3 Highest measured et 8		350(e) 5200	650(e) 5000	1000		100 ^(e)	400 ^(e) 5000	130(h) 2600	
Energy Gap at 300 K (eV		2.42(28)	1 72(29)	1.44(31)			2.7	2.23(32)	
dEgdT (eV/ K)		-5 x 10-4/27)	-4x10-4(30)		3.6			-5.5x10-4(32)	
Effective Mass of Free Ca	rriers								
Electrons		0.205m (33)	0.136me	0.11me	0.27me		0.17me		
Holes Sound Velocities, 25 ⁰ C (r		2.1m ⁽³³⁾	C.7me	0.63m				0.6m	
Longitudinal waves,	m/seci								
Propegation and									
particle motion	lic	4470	3960	3020		5060	4040	3580	1
Propagation and particle motion	ic	4340	3610	3010		3000		3330	\sim
Transverse weves,									
Propegation	[c] []c]	1770	1520	1650		3360	2780	2350	
Particle motion Propagation	[1c]								
Particle motion	lic	1600	1530						
Propagation and particle motion	Le	1700(28)	1590						
Disfectric Constants		10.33	10.65						
25°C(34)	€33 ^T /€0 €11 ^T /€0	9.35	9.70	11(13)		6.3 ₇	9.12	10.10	
	E13 1/C	9.53	10.20					•	
	e11 \$/e0	9.02	9.53			8.32	9.12	10.10	
Presolectric Constants, 25°C(34)	431 433	-5.18 +10.32	-3.92 +7.84						
10-12Coul/Newton)	°33 d ₁₅	-12.98	-10.51						
	d14			~1.54		3.18	1.10	0.91	
(coul/m ²)	*31	-0.244	-0.160						
	*33	+0.440 -0.210	+0.347 0.138						
	*15 *14	-0.210	-0.136	~0.304		+0.147	0.049	0.0284	
Pipeoslectric	k33	0.262	0.194	1.47					
Coupling Fectors(34)	k31	0.1191	0.0836						
	# 15	0.1885	0.1305						
	k, k.	0.154	0.124	~0.023		0.0795	0.026	0.017	
Elastic Constants(34)	¥14 111	2.069	2.338	0.023		1.839	2.26	2.40	
(10-1-1m2/N)	"33 ^E	1.697	1.736				100		
	33 ^E 12 ^E	-0.990	-1.122			-0.707	-0.15	-0.873	
	13E 44	-0.581	-0.572			2.00	2.25		
	44	6.649 6.136	7.595		~3.127(35)	2.168	2.2)	3.21	\sim
	1,0	2.040	2.322		~1.107(35)				_
	"JJ ⁰	1.581	1.870		~0.857(35)				
	*** *110 *330 *120 *120	-1.028	-1.138		~-0.46(35)				
	130 440	-0.523	- 0.539		~-0.21 ⁽³⁵⁾ ~3.51 ⁽³⁵⁾		2.23	3.21	
	44	6.412	7.466		~3.51,001	2 154	2.27	3.21	

A-33

N.

A-	34

ZnTe

		CdS	CdSe	CdTe	ZnS (Hex.)	ZnS (Cub.)	ZnSe
Elestic Constants ⁽³⁴⁾ (Continued)							
(10 ¹⁰ N/m ²)	¢11E	9.07	7.41	5.351(36)		10.46	8.59(37)
	C33E	9.38	8.36				
	c11 c33 c12 c12 c13 c44	5.81	4.52	3.681(36)		6.53	5.06(37)
	C12E	5.10	3.93				
	CAAE	1.504	1.317	1.994(36)		4.613	4.05(37)
		1.630	1.445		~3.2(35)		(27)
	CI D	9.13	7.42		~12.4(35)		8.59(37)
	°33	9.623	6.477		~14.0(35)		(07)
	C12D	5.88	4.53		~6.0(35)		5.06(37)
	617D	4.97	3.86		~4.5(35)		
	66 6110 633 612 613 644	1.560	1.340		~2.85 ⁽⁷⁾	4.643	4.06(37)

We have attempted to be as accurate as possible in gathering data and noting sources, but no guarantees can be made. In general, non-referenced material was internally generated, but it is possible that errors may appear. Apologies are offered to envone whose data are miscredited. Any suggestions for corrections or additions will be incorporated into the mixt revision.

Mixed crystels are available in the systems CcS-CdSe with properties intermediate between the end members. Inquiries are welcomed.

FOOTNOTES

(c.)

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Much of the data in the literature on the "hexegonal" form of ZnS is on polytypes that very only slightly in bulk properties from the cubic form, although such is frequently not disclosed. We have attempted to evaluate the data on the internal evidence and to aliminate those which obviously do not apply to pure wurtzite. The attempt may not have been completally successful. Examples of information on polytypes may be found in the papers by 1. 8. Kobyakov, Soviet Phys. - Cryst, 11,369-71 (1966) and Soviet Phys. - Solid State 9, 1269-71, 1707-11 (1967), and in reference 8. The data on the cubic form of ZnS are usually on material which is free of polytypes. (...)

References 21 and 3 give formulas for calculating indices of refraction versus wavelength (b.)

For CdS		$n_0^2 = 5.235 + \frac{1.817 \times 10^7}{\lambda^2 - 1.651 \times 10^7}$	10 ^{7 ;}	n. ² - 5.2	$\frac{2.076}{\lambda^2}$	1.651 x 10 ⁷
For ZnS	S	$n^2 = 5.164 + \frac{1.208 \times 10^7}{\lambda^2 - 0.732 \times 10^7}$	10 ⁷			
or		$n^2 = A + \frac{B\lambda^2}{(\lambda^2 - C^2)}$, with	A 8 C ²	CeTa 5.68 1.53 0.366	ZnGe 4.00 1.90 0,113	ZnTa 4.27 3.01 0.142
Formula	s for c	siculating thermal expansion versus temp	eratur	.		
Cas	іс с	L = L ₀ (1 + 4.0 x 10 ⁻⁶ T + 11.5 x 10 ⁻¹ L = L ₀ (1 + 2.4 x 10 ⁻⁵ T x 4.5 x 10 ⁻¹	•972_ 972_	- 15 x 10 ⁻ 5 x 10 ⁻¹²	12 ₇ 3 ₁ 7 ³ 1	
CdSe	↓ c c	$L = L_0 (1 + 4.6 \times 10^{-6} T + 3.0 \times 10^{-1} L = L_0 (1 + 2.8 \times 10^{-6} T \times 2.0 \times 10^{-1} L = L_0 (1 + 2.8 \times 10^{-6} T \times 2.0 \times 10^{-1} L = 10^{-1} L$	972) 972)			
ZnTa		L = L ₀ (1 x 8.2 x 10 ⁻⁶ T + 6.5 x 10 ⁻¹ L ₀ = Length at 0°C, T is in ⁰ C				
ZnSe ⁽³⁾	81	$e_t = 5.6681 \times 10^{-8} + 4.16 \times 10^{-13}t$ where e_t is the lattice constant in cm (t 2.13 tt t⁰C.	× 10-16,2	+ 2.79 x	10 ⁻²⁰ r ³

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- 32.33.4.36.38.37.38.39.

1.06µ Doubling

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43 - TA MATERIALS

Figure of Merit	^{D7} ^{L2}	
Nonlinear Coefficient x 10 ¹² Mks	Ð	
Coherence Length 1.06μ Doubling	L _c (µ)	
Refractive Index	a	
Transmission Range	(F)	
Material		

1500	363	286	210	146	123	
4.7	30	25	9.1	ង	32	
17.	2.2	2.4	4.5	2.4	1.5	
1.6	2.3	2.3	2.0	2.1	2.6	
.3+2	.5+23	.4+13	.4+18	.5+21	.5+21	
$N_{A}(CH_{2})_{6}$	Cul -	ZnS	CuC1	CuBr	ZnSe	

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43^m - TA MATERIALS

Figure of Meric $\frac{b^2}{n^3} L_c^2$ 0.38 0.95 0.92 1.6 3.8 2.3 2.1 4.6 130 11.6 10.9 21 Coefficient* x 10¹² Nka 110 (5 40 (8 50 (2 9.5 (7 86 (8 420 (5 630 (5 190 (5 Nonlinear 47 (8 170 (2 11 (7 C H a 10µ Doubling 115**⁽⁶ 170 (7 Coherence 170**(6 8 5 8 9 5 5 C 3 Length Ē 290 450 370 126 46 235 53 104 134 Refractive 1.9 (7 2.7 (3 2.5 (3 3.0 (5 3.3 (6 3.8 (5 3.5 (5 3.5 (6 2.0 (7 3.3 (5 2.7 (2 Index 2.2 E 2 + 20µ ⁽¹ 1.0 + 20 ⁽⁶ 5 5 3 C 9 5 J C S 5 Transmission .6 + 12 1 + 28 .6 + 22 4 + 22 1+17 .5 + 20 .5 + 22 .5 + 17 .6 + 25 .9 + 20 Range E Material ZnSe Alsh CuBr Cucl CdTe CaAs ZnTe CaSb **SANI** CaP InP CuI

Rel to GaAs Ref. 5 except for InP and AlSb.

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** From index values.

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