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FRACTURE MECHANICS ANALYSIS OF AN ATTACHMENT LUG

AEROELASTIC AND STRUCTURES RESEARCH LABORATORY DEPARTMENT OF AERONAUTICS AND ASTRONAUTICS MASSACHUSETTS INSTITUTE OF TECHNOLOGY CAMBRIDGE, MASSACHUSETTS 02139

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Project Engineer

FOR THE COMMANDER

ROBERT M. BADER, Chief Structural Integrity Branch Structures Division

Gerald G. Leigh, Lt Col, USAF Chief, Structures Division

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lug analysis procedure covers the physical problem, modeling, program flow and options, input/output conventions, execution times and limitations which must be observed. Results from example analyses of some attachment lugs are presented.

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FOREWORD

The developments documented in this report were carried out at the Aeroelastic and Structures Research Laboratory (ASRL), Department of Aeronautics and Astronautics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, under Contract No. F33615-74-C-3063 (Project 1367, Task 136703) from the U.S. Air Force Flight Dynamics Laboratory. Mr. James L. Rudd (AFFDL/FBE) served as technical monitor. The contractor's report number is ASRL TR 177-1.

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Section 1

INTRODUCTION

The application of linear elastic fracture mechanics analysis to structural details in new aircraft designs has received growing emphasis from the Air Force and from aircraft manufacturers during the past few years. Not only have fracture mechanics data become more readily available in recent years [1,2], but also, there has been a trend toward treatment of the problem of fracture in its own right, distinct from fatique. Within the past year, this trend has culminated in the establishment of structural design criteria by the Air Force which require an aircraft designer to take specific design-analysis actions to protect structures against fracture [3]. Required design calculations now include, generally, comparison of load-induced stress intensity factors to material fracture toughness and assessment of crack growth rates, based on assumptions concerning the size and location of possible cracks in the structure. Both types of calculation require prior estimation of the load-induced stress intensity factor. Hence, there has also been considerable emphasis on adding to the body of available fracture mechanics solutions.

Because so few geometrical configurations are amenable to a purely analytical solution of the equations of elastic fracture mechanics, the finding of new solutions depends upon development of numerical analysis techniques. Extensive contributions have been made by Bowie and his colleagues [4,5,6] using the complex variable formulation of elasticity in combination with conformal mapping, analytic continuation and boundary collocation methods. Tada, et al. [7] have recently collected and classified a comprehensive body of solutions based on the semi-analytical methods (complex variables, boundary collocation, Fourier transforms, etc.) among which appear many new solutions by Tada. However, the semianalytical methods have not as yet proved capable of application to the irregular geometrical configurations which are found so often

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in real airframe structural details. Stress analysis of irregular structure has been the province of the finite-element methods for the past decade. Within the last six years, numerous contributors have extended the finite-element technique to fracture mechanics analysis.

Work on finite-element fracture mechanics analysis at MIT has followed the path of assumed-stress hybrid elements, first proposed by Pian [8] for ordinary continuum elements. The hybrid method was subsequently extended by Tong, Pian, Luk, and Lasry [9,10,11,12] to formulation of rectangular elements which incorporate an elastic crack-tip singularity, but which also have an assumed linear or quadratic variation of displacements along the element edges and are thus compatible with ordinary elements (Figure 1). Numerical experiments have demonstrated that the hybrid crack-containing elements are capable of producing estimates of K_{τ} and $K_{\tau\tau}$ with less than 1 percent error, using 20 to 50 total degrees of freedom in the analysis, for simple geometrical configurations. Hence, it becomes possible to create economically practical analysis procedures for structural details by refining the mesh or ordinary elements to pick up the stress gradients caused by nonuniform loading and complicated boundary geometry, leaving to the special hybrid element the task of picking up the local gradients caused by the crack-tip singularity.

This report summarizes recent developments at the MIT Aeroelastic and Structures Research Laboratory (ASRL) in which the crackcontaining hybrid element has been applied for the first time to some typical structural details, found in current production aircraft, with geometries too complicated for economical solution by other techniques. The "PCRK59" crack element used in these analyses is a generalized version of the original Lasry element [12] which was formulated and programmed by Tong and subsequently modified for greater utility by the ASRL computing staff.

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Section 2

BASIC ELEMENTS AND METHODS

2.1 Element QUAD4

The ASRL QUAD4 four-node quadrilateral element (Figure 2) is used as the basic building block in the analysis procedure. QUAD4 is the well-known bilinear isoparametric assumed-displacement element which has been used for continuum stress analysis for many years [13]. The ASRL version has been programmed as an independent subroutine which includes the options of individual rotation transformations at each node and calculation of a "B" matrix for stress analysis.

The nodal coordinates X_1 , Y_1 , X_2 ,..., Y_4 , element thickness T and the elastic constants matrix:

$$\begin{split} & \underset{\sim}{\mathcal{C}} = \begin{pmatrix} c_{11} & c_{12} & c_{13} \\ c_{12} & c_{22} & c_{23} \\ c_{13} & c_{23} & c_{33} \end{pmatrix} , \qquad \begin{cases} \sigma_{XX}' \\ \sigma_{YY}' \\ \sigma_{XY}' \end{pmatrix} = & \underset{\sim}{\mathcal{C}} \begin{pmatrix} \varepsilon_{XX} \\ \varepsilon_{YY} \\ \varepsilon_{XY} \end{pmatrix} \end{split}$$
 (1)

comprise the required basic input information. For isotropic materials

$$\begin{split} & \sum_{n=1}^{C} = \frac{E}{1-y^2} \begin{pmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & \frac{1-\nu}{2} \end{pmatrix} & or \quad \frac{E}{(1+\nu)(l-2\nu)} \begin{pmatrix} 1-\nu & \nu & 0 \\ \nu & 1-\nu & 0 \\ 0 & 0 & \frac{1-2\nu}{2} \end{pmatrix} \quad (2) \\ & (plane \\ stress) & strain) \end{split}$$

Subroutine QUAD4 allows for general plane orthotropic behavior, a capability which is included in the attachment lug program. Plane stress is assumed in the analysis. The lug program does not use the rotation transformation option.

The element stiffness matrix k is calculated by numerical area integration, using 3x3-point Gaussian quadrature [14] for

-3-

ELEMENT

$$\dot{\mathbf{k}} = \mathbf{T} \iint_{\mathbf{AREA}} \mathbf{D}^{\mathsf{T}} \mathbf{C} \quad \mathbf{D} \quad \mathsf{d} \mathbf{X} \, \mathsf{d} \mathbf{Y} \tag{3}$$

where D contains the interior strain-nodal displacement relations:

$$\{\varepsilon_{XX} \ \varepsilon_{YY} \ \varepsilon_{XY}\} = \mathcal{D}(X, Y) \{q_1 \ q_2 \cdots \} \}$$
(4)

The stiffnesses are returned in Lower Triangle Vector (LTV) form:

$$k = \lfloor k_{11} \ k_{21} \ k_{22} \ k_{31} \ k_{32} \ \cdots \ k_{88} \rfloor$$
(5)

For the purpose of stress analysis, Eqs. 1 and 4 may be combined to give:

$$\underbrace{\mathcal{O}}_{\mathcal{O}}(\mathbf{X},\mathbf{Y}) = \underbrace{\mathcal{C}}_{\mathcal{O}}\underbrace{\mathcal{D}}_{\mathcal{O}}(\mathbf{X},\mathbf{Y})\underbrace{\mathcal{F}}_{\mathcal{F}} = \underbrace{\mathcal{B}}_{\mathcal{O}}(\mathbf{X},\mathbf{Y})\underbrace{\mathcal{F}}_{\mathcal{F}}$$
(6)

QUAD4 also returns the matrix $B(X_C, Y_C)$, formed at the fifth Gaussian station, for later calculation of stresses at the element "centroid", defined in terms of the nodal coordinates:

$$X_{c} = \frac{1}{4} \sum_{i=1}^{4} X_{i} \qquad Y_{c} = \frac{1}{4} \sum_{i=1}^{4} Y_{i}$$
(7)

The behavior of QUAD4 has been studied extensively on other projects and is well understood. Uniform or nearly uniform stress fields can be picked up to within the roundoff accuracy of the digital computer being used for the analysis. The inability of the bilinear assumed displacement fields to follow the quadratic deflection of the neutral axis of a cantilever beam loaded by an end moment has been well documented elsewhere [15] and constitutes a limitation on the QUAD4. In practical terms, this requires that the element aspect ratio (Figure 2) be held close to unity for models of structures which are expected to have quadratic or higher-order displacement behavior. In some cases, even an aspect ratio of unity is not sufficient to insure convergence of the solution. For example, the

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QUAD4 element was used recently to model a thick-walled cylinder subjected to centrifugal loading from its own mass, due to rotation [16]. The analytical solution of this axisymmetric problem includes an r^3 term in the radial displacement field which the bilinear element is unable to pick up; errors of 25% were found for a cylinder with a 2:1 ratio of outside-to-inside radius, using four unit-aspectratio QUAD4 elements through the wall thickness.

The misbehavior of the bilinear element in the presence of higher-order gradients requires the use of many elements to model complicated geometries. Also, "calibration" of the finite-element model is a good idea, where possible, by comparing the numerical results with independent solutions. Calibrations for this project have included comparisons with the classical elasticity solution for stresses and displacements near a circular hole in a semiinfinite strip under tension [17] and with finite-element analyses using higher-order assumed-displacement elements.

2.2 Element PCRK59

Formulation of the assumed-stress hybrid finite-element method begins with the Principle of Minimum Complementary Energy:

$$\mathcal{T}_{c} = \sum_{n} \left[\int_{S_{u}} \hat{u}^{\mathsf{T}} \mathcal{T}_{d} dS - \int_{V} \frac{1}{2} \mathcal{G}^{\mathsf{T}} \mathcal{S} \mathcal{G} dV \right]$$
(8)

where

 Σ indicates summation over the element set. $S_u = part of the element boundary over which displace$ ments are prescribed.

V = element volume.

 \hat{u} = vector of prescribed displacements on S_{u} .

 σ = stress vector.

S = compliance constants = C^{-1} ($\varepsilon = S\sigma$).

T = vector of surface tractions = Ng, where N is a matrix of surface normal direction cosines.

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If Π_{c} is used directly, only the stress field is assumed, subject to admissibility criteria requiring that the assumed stresses satisfy:

- (i) Interior equilibrium $\partial \sigma_{ij} / \partial x_j + \hat{F}_i = 0$, in V, where \hat{F}_i are prescribed body forces.
- (ii) Mechanical boundary conditions $N\sigma = T$ on S_{σ} , that part of the element boundary over which the surface tractions \hat{T} are prescribed.
- (iii) Equilibrium of surface tractions $N\sigma$ across the interelement boundaries S, which are distinct from S_u and S_{σ}.

Formal application of the variational calculus to Eq. 8 leads to two sets of Euler equations:

- (iv) Interior compatibility, $S\sigma = \varepsilon$ in V, where $\varepsilon_{ij} = 1/2 (\partial u_i / \partial x_j + \partial u_j / \partial x_i)$.
- (v) Displacement boundary conditions, u = u on S_{u} .

If assumed stress functions are substituted and Eq. 8 is integrated before $\Pi_{\rm C}$ is varied, there results a linear equation system in which the generalized coordinates to be solved for are forces. This approach leads to a Matrix Force Method analysis which brings with it the programming problem of systematic identification and elimination of redundant quantities.

The assumed-stress hybrid approach avoids the complications of force redundancy by modifying I_c so that the primary unknowns in a finite-element application become displacements once again. The Principle of Minimum Complementary Energy is modified by addition of Lagrange multiplier terms [8,18] which change admissibility criteria. Specifically, conditions (ii) and (iii) above are relaxed and confition (v) is enforced. Under the new principle, stress functions satisfying only the interior equilibrium conditions (i) may be assumed, and displacement functions which satisfy interelement compatibility and conditions (v) must now be assumed as well. The modified energy principle which replaces Eq. 8 is:

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$$\mathcal{T}_{i} = \sum_{n} \left[\int_{\partial V} \mathcal{I}^{\mathsf{T}} \mathcal{I} \mathcal{A} \mathsf{S} - \int_{V}^{\frac{1}{2}} \mathcal{G}^{\mathsf{T}} \mathcal{S} \mathcal{I} \mathcal{A} \mathsf{V} - \int_{\mathcal{S}_{\mathcal{T}}} \mathcal{I}^{\mathsf{T}} \mathcal{I} \mathcal{A} \mathsf{S} \right] \qquad (9)$$

where " ∂V " represents the entire element boundary, $S + S_u + S_\sigma$. To convert Π_1 into a finite-element formulation, the stress vector σ is assumed within each element and the displacement vector \overline{u} is assumed on the boundary, ∂V , of each element:

 $\sigma = \Pr(\mathbf{x}, \mathbf{y}, \mathbf{z}) \boldsymbol{\beta} \qquad \overline{\mathbf{u}} = \operatorname{L}(\mathbf{x}, \mathbf{y}, \mathbf{z}) q \qquad (10)$

where P and L are matrices of interpolation functions. Vector β contains generalized stress coordinates, while g is a vector of nodal displacements. Matrices P and L are assumed independently, with L defined only along the element boundary ∂V . Substitution of Eq. 10 into Eq. 9 then leads to:

$$\mathcal{T}_{1} = \sum_{n} \left[\mathcal{A}^{\mathsf{T}} \mathcal{G} \mathcal{G} - \frac{1}{2} \mathcal{A}^{\mathsf{T}} \mathcal{H} \mathcal{A} - \mathcal{J}^{\mathsf{T}} \mathcal{Q} \right] \tag{11}$$

where

$$\hat{\mathcal{G}} = \int_{\partial V} (NP)^{\mathsf{T}} \mathcal{L} \, dS \qquad \mathcal{H} = \int_{V} P^{\mathsf{T}} SP \, dV$$

$$\hat{\mathcal{Q}} = \int_{S_{\mathsf{T}}} \mathcal{L}^{\mathsf{T}} \hat{\mathcal{T}} \, dS = \text{Consistent nodal force vector} \qquad (12)$$

and where $N\sigma = NP\beta$ has been substituted for the surface traction vector T in the expression for G.

Direct assembly and solution of the equation system represented by Π_1 is possible, but results in a mixed matrix method, with both force and displacement unknowns. A more versatile formulation is obtained by recognizing that, since the stresses are assumed independently within each element, $P\beta$ for one element is not coupled with any other elements. Therefore, the unknowns β may be formally eliminated by applying the variational calculus to Π_1 :

 $\delta \Pi_{1}(\beta \text{ for only one element varied}) = \delta \beta^{T} \{\partial \Pi_{1}/\partial \beta\} =$

$$\delta_{\beta}^{\beta} (\operatorname{Gq} - \operatorname{H}_{\beta}^{\beta}) = 0$$

which leads to

$$\mathcal{A} = \mathcal{H}^{-1} \mathcal{G} \mathcal{G} \mathcal{G}$$
(13)

Substitution of Eq. 13 back into Eq. 11 then yields *:

$$\Pi_{I} = \sum_{n} \left[\frac{1}{2} \underbrace{g}^{\mathsf{T}} \underbrace{g}^{\mathsf{T}} \underbrace{H}^{\mathsf{L}} \underbrace{g}^{\mathsf{T}} \underbrace{$$

The alternate expression for Π_1 given by Eq. 14 represents a pure Matrix Displacement Method. The quantity $G^T H^{-1}G$ can be recognized as an element stiffness matrix. The Σ notation may now be identified as a conventional Matrix Displacement Method structure model assembly procedure. Hence, structure models can be created by assembling conventional and hybrid elements, provided only that compatibility across the interelement boundaries is maintained by proper choices for the assemed displacement fields. The versatility of the hybrid method lies in its ability to provide special-purpose elements, for restricted regions, which may be coupled into a model containing conventional elements in the remaining regions which are free of singularities or other unusual behavior.

The original hybrid crack elements [9,10] were derived from ${\rm II}_1$ by assuming a stress field containing ${\rm r}^{-1/2}$ terms, where ${\rm r}$ measures radial distance from the crack tip and, by assuming displacement fields which vary linearly from one node to the next, along the element boundary. However, subsequent analysis of error sources [19] has indicated that the area integration required for computation of H (see Eqs. 12) gives poor results for the $r^{-1/2}$ terms since some of the Gaussian stations are close to the crack This situation may be remedied by increasing the number of tip. Gaussian stations, but the computation of k then becomes too costly. A better approach, used for the second-generation crack elements [11,12] has been followed in the present work. The energy principle Π_1 may be further modified by introducing two displacement fields: \overline{u} assumed on ∂V and u assumed in V. There now arises another compatibility condition, $u = \overline{u}$ on ∂V , which is relaxed by the Lagrange

^{*}Note that H and H^{-1} are symmetric matrices.

multiplier method. At the same time, the condition that \underline{u} must satisfy the interior equilibrium equations, as well as the straindisplacement relations, is enforced. As a result, the area integration is converted to a boundary integral and $\underline{\Pi}_1$ is modified to the form:

$$\mathcal{T}_{z} = \sum_{n} \left[\int_{\partial V} \mathcal{I}^{\mathsf{T}}_{\mathcal{U}} dS - \frac{1}{2} \int_{\partial V} \frac{1}{2} (\mathcal{I}^{\mathsf{T}}_{\mathcal{U}} + \mathcal{U}^{\mathsf{T}}_{\mathcal{I}}) dS - \int_{\mathcal{S}_{\mathsf{P}}} \mathcal{I}^{\mathsf{T}}_{\mathcal{I}} dS \right]$$
(15)

The same boundary displacement field \overline{u} can be used for both Π_1 and Π_2 . However, the interior assumed fields in Π_2 must be a complete elasticity solution: stresses σ and displacements u which satisfy all of the equations of elasticity, with $\underline{T} = N\sigma$ a derived quantity. The distributions for σ and u are obtained from a complex variable solution of the equations of elasticity near a crack tip or equivalently, by solving the biharmonic equation for an Airy stress function. Computation of the element stiffness matrix is the same as for Π_1 , except that H is now computed by a boundary integral:

$$H = \frac{1}{2} \int_{\partial V} \left[\left(N P \right)^{T} A + A^{T} N P \right] dS$$
(16)

where A is a matrix of shape functions corresponding to the interior assumed displacement field, u = Aq.

The principle I_2 also possesses the advantage of convenience for treatment of arbitrary shapes, since only boundary integration is required. Figure 3 illustrates the PCRK59 element based on I_2 . Input information required by this element is similar to the information required by QUAD4:

- (i) Geometry: global coordinates of the crack tip X_+, Y_+ ; global coordinates of each node $X_1, Y_1, X_2, \dots, Y_9$.
- (ii) Material properties: the shear modulus $G = E/2(1+\nu)$ and a second constant $\eta = (3-\nu)/(1+\nu)$ for plane stress (3-4 ν for plane strain)

PCRK59 is programmed only for isotropic material and does not incorporate the rotation transformations available in QUAD4. In fact, rotation transformations cannot be applied once the PCRK59

stiffness matrix has been formed. This limitation is caused by the appearance of the crack tip coordinates in the numerical integration scheme, but the restriction does not affect many practical fracture mechanics problems. The numerical integration is by five-point Gaussian quadrature [14] between each pair of nodes, except that the crack surfaces are skipped. Omission of the crack surfaces is justified because they constitute S_{σ} , over which $\hat{T} = 0$, and because the derived tractions T satisfy this stress-free condition at least in an average sense.

The PCRK59 element has two other important features. First, unit thickness is assumed. Second, a symmetric "half-element" option is available, under which nodes 1,5 and the crack tip are assumed to lie on a line parallel to the global X-axis, while the element and applied loading are assumed to be symmetric about this line. Under these conditions, a half-model of a structure may be analyzed to obtain Mode I stress intensity solutions only; e.g., for the coupon in uniform tension with edge cracks, shown in Figure 4. The "half-element" consists of nodes 1,2,...5, only, with node l requiring a roller restraint to maintain the assumed symmetry. Another input parameter determines which option is executed:

KEY = 1 for "half-element"

2 for full element

The "half-element" option is used mainly for illustrative examples and performance testing. The full element option has been used exclusively in the present work.

Element PCRK59 computes and returns a stiffness matrix in LTV form (see Eq. 5) for either the 10 degree-of-freedom "half-element" or the 18 degree-of-freedom full element. In addition, a special B matrix for calculation of stress intensities is returned. Eq. 13, \tilde{u} used in the derivation of the stiffness matrix, can also be used to compute the generalized stress coordinates β after the element nodal displacements q have been obtained. For the PCRK59,

 $\beta = \{ k_1 \ \beta_2 \ \beta_3 \ \cdots \ \beta_g \ k_2 \ \beta_{11} \ \cdots \ \beta_{18} \}$ (17)

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where k_1, k_2 , are the Mode I, Mode II stress intensity factors, defined by:

$$\sigma_{XX} = \frac{k_1}{\sqrt{2r}} f_1(\theta) + \frac{k_2}{\sqrt{2r}} f_2(\theta) + (terms in \beta_2, \beta_3, \cdots)$$

$$\sigma_{YY} = etc. \cdots$$
(18)

The functions f_1, f_2 , are from the classical crack tip solution, and the other generalized coordinates $\beta_2, \beta_3, \ldots, \beta_{18}$ represent far-field behavior. Thus, B is formed by extracting the first and tenth rows of $H^{-1}G$, so that the stress intensities may be calculated from:

$$\{k_1, k_2\} = B_{(2\times 18)} \{q_1, q_2, \cdots, q_{18}\}$$
 (19)

for the full element. Only the first row of $H^{-1}G$ is extracted if the "half-element" option is in effect:

$$k_1 = \mathcal{B}_{(1\times 10)} \{ \xi_1 \ \xi_2 \ \cdots \ \xi_{10} \}$$
 (20)

NASA/ASTM standard stress intensity factors may be computed after Eq. 19 or Eq. 20 by:

$$K_{I} = k_{1} \sqrt{\pi} \qquad K_{II} = k_{2} \sqrt{\pi} \qquad (21)$$

If a structure model with thickness $T \neq 1$ is to be analyzed, this may be done simply by scaling the PCRK59 stiffness to:

$$\mathbf{k}' = \mathbf{T} \mathbf{k} \tag{22}$$

Performance of the PCRK59 element has been tested extensively by comparison with classical and boundary collocation solutions [19]. Solutions for K_I accurate to better than 1 percent have been obtained with a rectangular crack element surrounded by only a few QUAD4 elements. Other tests have shown that solution accuracy within 3 percent is maintained when the crack element shape is distorted by relocating some nodes as much as 0.3 x (length of crack within element) away from the positions they occupy for a rectangle. Also, the 3 percent accuracy limit can be maintained with the crack tip located anywhere from 20 to 70 percent across a line between

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nodes 5 and 1, with the element shape kept rectangular. The distortions of element shape and crack tip location required for the structure models analyzed in the present work are well within these limits.

The PCRK59 element possesses one unavoidable quirk which arises from its linearity. If the element is placed in a region with compressive stress normal to the crack, a negative value of K_I is obtained. In a real structure, the crack would close and cease to be a problem in this situation. Therefore, negative K_I values should be interpreted as signaling the absence of Mode I stress intensity. On the other hand, the solution for K_{II} will be positive (negative) according to whether the crack is being subjected to positive (negative) shear stress, as defined by the standard conventions of elasticity. In this case, the correct interpretation is to take the absolute value of K_{II} .

In summary, the PCRK59 element permits efficient computation of stress intensity factors by well established procedures of the Matrix Displacement Method. The unusual features of the element are internal to its subroutine. The element subroutine requires familiar input information and returns k and B matrices like a conventional element. The structure model is assembled and a global displacement solution is computed by standard techniques. Computation of either the centroid stresses in the conventional elements or the stress intensity factors in the crack element is then merely a matter of extracting the element displacements g from the global solution and performing a straightforward matrix multiplication.

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Section 3

ATTACHMENT LUG PROGRAM

Program LUG has been developed for analysis of stresses or stress intensity factors in an attachment lug typical of many structural details found in current aircraft. This section describes the lug structure model and explains how the program is used. Results obtained from some example analyses are presented in Section 4.

3.1 Lug Structure Model

Figure 5 illustrates the structure which Program LUG models. The detail consists of a straight shank, built in at the foot and a rounded ear whose outer edge is concentric with a bearing pinhole. Provision is made to treat the lug as a two-material system composed of an isotropic bushing ring surrounding the bearing pinhole, and the lug proper, which may be treated as either isotropic or plane orthotropic. A perfect mechanical bond between the bushing and lug is assumed. A monolithic single-material lug is obtained if identical isotropic material properties are specified for the bushing and the lug proper.

Bearing loads are assumed to be applied to the structure at the bearing pinhole surface. Tension, compression, positive shear or negative shear may be applied. These loads are defined in Figure 5. Each load component is represented as a radial bearing pressure over one-half the circumference of the bearing pinhole, with the pressure distribution centered on and symmetric about the line of action of the load. Options for a cosine pressure distribution or a uniform pressure distribution are available.

The attachment lug is assumed to be under plane stress, with two analysis options allowed. Under option 1, a model of an uncracked lug is assembled, using only QUAD4 elements, and a conventional stress analysis is executed. Under option 2, a small radial crack is assumed to emanate from the bearing pinhole surface,

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with the crack tip located in the bushing. The length of the crack is specified by the program user (Figure 6). Program LUG automatically executes a sequence of solutions in which the crack location is varied step-wise around the entire bearing hole circumference.

3.2 Input Conventions

The input data conventions for Program LUG are summarized in Figure 7. Formats for all numerical data have been standardized to I5 fields for integers and El0.0 fields for floating point numbers. Integer data and floating point data supplied in E format should be right-justified in the field. However, floating point data may also be given in F format, if desired, without changing the program code. F format data need not be right-justified. Also, the implied decimal point location for floating point data may be overridden. A maximum of 3 decimal figures may be input under E format and up to 7 decimal figures may be input under F format.

A series of independent cases may be analyzed in one run. The first input data card specifies the total number of cases which follow. The remainder of the input deck consists of six cards per case which give the program a complete description of the case. The conventions for these cards are as follows:

- <u>Card 2</u> may contain any alphanumeric information which identifies the case. This information is printed as a heading title.
- <u>Card 3</u> specifies the options selected by the user for four control parameters:
 - IANL = 1 (Conventional stress analysis without crack).
 - 2 (Stress intensity analysis).
 - LOAD = 1 (Cosine pressure distribution).
 - 2 (Uniform pressure distribution).
 - MODE = 1 (Lug treated as isotropic).
 - 2 (Lug treated as orthotropic).
 - NT = Total number of QUAD4 elements wanted per 45° arc around the bearing pinhole. A minimum value of 3 is recommended.

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Card 4 - specifies the lug dimensions and crack size.

| DI = | Inside | diameter | of | bearing | pinhole. |
|------|--------|----------|----|---------|----------|
|------|--------|----------|----|---------|----------|

- DB = Outside diameter of bushing.
- W = Lug width.
- H = Total (root to tip) length of lug.
- T = Lug thickness (lug and bushing assumed to have equal thickness).

CSIZE = Length of crack.

<u>Card 5</u> - specifies the material properties of the bushing, which is always assumed to be isotropic:

- E = Young's modulus.
- v = Poisson's ratio.
- <u>Card 6</u> specifies the lug material properties. If MODE = 1 on card 3, the convention is:
 - E = Young's modulus.
 - v = Poisson's ratio.
 - If MODE = 2 on card 3, the convention is:
 - E_T = Longitudinal modulus.
 - E_{I.T} = Cross-coupling modulus.
 - E_m = Transverse modulus.

 $G_{T,TT}$ = Shear modulus.

θ = Angle between lug XY axes and material LT axes (degree measure, positive CCW from X to L).

Card 7 - specifies the bearing force value:

TENSN = Tension or compression bearing force. SHEAR = Positive or negative shear bearing force.

The lug dimensions and crack size were defined in Figures 5 and 6. Any value of thickness may be specified. Program LUG rescales the model internally to unit thickness. Figure 8 illustrates a finite element mesh which might result when NT = 3 elements per 45° arc is specified on card 3. The positive convention for the relationship between the lug XY axes and material LT axes is also shown. The quantities E_L , E_{LT} , E_T , G_{LT} are the conventional plane-orthotropic moduli for; e.g., a fiber composite laminate. The stress-strain relations take the form:

$$\begin{cases} \sigma_{\mathrm{L}} \\ \sigma_{\mathrm{T}} \\ \sigma_{\mathrm{LT}} \end{cases} = \begin{cases} E_{\mathrm{L}} & E_{\mathrm{LT}} & 0 \\ E_{\mathrm{LT}} & E_{\mathrm{T}} & 0 \\ 0 & 0 & G_{\mathrm{LT}} \end{cases} \begin{cases} \varepsilon_{\mathrm{L}} \\ \varepsilon_{\mathrm{T}} \\ \varepsilon_{\mathrm{LT}} \end{cases}$$
(23)

in the LT axis system. For $\theta \neq 0^{\circ}$ the stress-strain relations in the XY axis system take a more complicated form:

$$\begin{cases} \sigma_{XX} \\ \sigma_{YY} \\ \sigma_{XY} \end{cases} = \begin{cases} C_{11} & C_{12} & C_{13} \\ C_{12} & C_{22} & C_{23} \\ C_{13} & C_{23} & C_{33} \end{cases} \begin{cases} \varepsilon_{XX} \\ \varepsilon_{YY} \\ \varepsilon_{XY} \end{cases} = \begin{array}{c} C & \varepsilon \\ \tilde{c} & \tilde{c} \\ \varepsilon_{XY} \end{cases}$$
(24)

where, in general, C_{13} , $C_{23} \neq 0$. The matrix <u>C</u> in Eq. 24 is computed from E_{T} , $E_{T,T}$,..., θ by ASRL subroutine CTFORM.

The bearing load conventions were indicated in Figure 5. The value of TENSN or SHEAR supplied on card 7 refers to total bearing force; the corresponding pressure distributions are computed internally. A positive (negative) value TENSN has the effect of applying a tension (compression) bearing load to the structure. A positive (negative) value for SHEAR similarly applies a positive (negative) shear bearing load.

Figure 9 illustrates a portion of the actual finite element mesh generated for a hypothetical large all-aluminum wing root attachment lug. Since the "bushing" diameter does not have any physical significance in this single-material case, it is used to control the mesh so that the tip of a 0.5-inch long crack lies at the middle of the PCRK59 element. The crack is shown with a finite opening for clarity. However, nodes 5 and 6 of the crack element (Figure 3) actually overlap to provide the correct model of a sharp crack. The PCRK59 element has replaced a group of four adjacent

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QUAD4 elements in the mesh. When analysis option 2 is in effect, a series of structure models are generated and analyzed one after the other, with the PCRK59 shifted circumferentially by one pair of QUAD4's after each analysis. Thus, for the case shown in Figure 9 (NT = 3), 24 stress intensity solutions are obtained with the crack located successively at $\theta = 0^{\circ}$, 15°, 30°,...,345°. Figure 10 summarizes the input data deck required to run a stress analysis (case 1) and a stress intensity analysis (case 2) for the hypothetical lug detail.

3.3 Required Subprograms and Other Features

Program LUG requires the following FORTRAN-IV subroutines to form an executable load module:

- (i) ASRL FEABL-2 subroutines ASMLTV, BCON, FACT, ORK, SETUP, SIMULQ, and XTRACT [20,21].
- (ii) ASRL element and utility library subroutines QUAD4, PCRK59, and CTFORM.
- (iii) IBM Scientific Subroutine Package routines MFSD and SINV which are required by the PCRK59 element subroutine.

The entire source deck is supplied in IBM 029-punch format. The following features of Program LUG may cause machinedependence problems on non-IBM hardware:

- (i) The 20A4 format for input of case title information may be incompatible with some systems. This may be remedied by changing FORMAT statement 502 to 80A1 and redimensioning vector TITLE to 80.
- (ii) FORTRAN unit numbers 5 and 6 are assumed for the card reader and line printer respectively. Program LUG may be converted to other hardware standards simply by reprogramming the two lines of code:

KR = 5KW = 6

which appear shortly after the FORMAT statements near the beginning of the program.

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- (iii) Program LUG requires a sequential-access scratch dataset, designated as FORTRAN file 20, when analysis option 1 (uncracked structure stresses) is in effect. The file must consist of (30 singleprecision words per record) x (records = maximum number of QUAD4 elements expected). A total of 600 records should be adequate for most analyses. A job control instruction, specific to the installation where the program is being executed, is required to create this file on a system disk. However, Program LUG may be executed without creating this file if only stress intensity solutions are sought.
 - (iv) IBM/SSP subroutines MFSD and SINV may not be compatible with other systems. If this problem arises, reprogramming or substitution will be required.

3.4 Model Generation and Program Flow

Program LUG automatically generates the geometrical information, element interconnections, etc., which are required to compute and assemble the element stiffnesses, restrain the structure properly, apply the bearing load and execute a stress or stress intensity analysis. The program flow is summarized in Figure 11. Parenthesized numbers in the figure refer to FORTRAN statement numbers in the program listing (Appendix A).

After the input data has been read for a case and some auxiliary values have been calculated, the case title and input data are printed for checking. A sample output from this section of the program is shown in Figure 12. The number of QUAD4 elements required radially in the bushing and lug and the number required axially in the lug shank are then computed by rounding off to the nearest whole number which gives an average element aspect ratio closest to unity for each region. The total number of elements, total degrees of freedom and some additional parameters are then calculated, and the vectors which will contain the K-solutions are erased.

The major section of the code, a loop over the crack locations, then follows. The location loop is executed 8*NT times for a stress intensity analysis, but only once for a conventional uncracked structure stress analysis. Previous results are erased and the interconnections for an uncracked structure are generated. Figure 13

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illustrates the node and element numbering conventions, using the example mesh from Figure 8. The numbering patterns are as follows:

- (i) Nodes are numbered, globally, radially outward from the bearing pinhole on each ray. The rays are taken in counterclockwise order, beginning at $\theta = 0^{\circ}$. Vertical lines of nodes in the lug shank are numbered afterward, from the top down and from right to left. The last line of nodes is restrained.
- (ii) Degrees of freedom are numbered 2n-1 (displacement parallel to X) and 2n (displacement parallel to Y) at each node n.
- (iii) Elements in the bushing are numbered radially outward and counterclockwise, partially following the node numbering pattern.
 - (iv) Elements in the lug ear are numbered radially outward and counterclockwise after the bushing elements.
 - (v) Elements in the lug shank are numbered last, from the top down and from right to left.

If a stress intensity analysis is being executed, the location of the PCRK59 element is now computed from the crack location loop index and connections for this element are generated. As shown in Figure 14, the PCRK59 element overlays four QUAD4 elements. The central node of this group of elements is transferred to the bearing pinhole to accommodate the PCRK59. The element numbers of the four overlaid QUAD4 elements are also flagged.

The global XY coordinates for each node in the model are now computed, assuming an uncracked structure. If a stress intensity analysis is being executed, the transferred node coordinates are adjusted and global coordinates are computed for the crack tip. The area corresponding to the global force vector \hat{Q}_{G} in the FEABL-2 storage system is used as temporary storage for the node coordinate data.

After auxiliary storage for element-level data has been prepared, a loop over all QUAD4 elements is executed. The node coordinates for each element are extracted from the global data, other required input is provided from auxiliary storage and k and B are

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computed for the element. Also, centroid coordinates X_{c} , Y_{c} are computed for the element; B, X_{c} , Y_{c} are stored in FORTRAN file 20 (stress analysis option only) and k is assembled into the global stiffness matrix. If a stress intensity analysis is being executed, these procedures are skipped for the four flagged elements, while k and B are computed and k is assembled for the PCRK59.

After assembly, Q_{G} is erased and replaced by prescribed nodal forces which are statically equivalent to the specified bearing load and the assumed (cosine or uniform) pressure distribution. For stress intensity analysis, the two nodes at the crack opening each receive one-half the nodal force which would have been applied to a single node at that location in an uncracked structure.

The final section of the code executes a solution of the global equation system and either a stress or a stress intensity analysis. In the latter case, the stress intensity factors are saved and a complete table is printed after the crack location loop has been completed.

3.5 Output Conventions and Error Messages

If a stress analysis has been executed, nodal forces, nodal displacements and element stresses are printed. The table of forces and displacements appears immediately below the problem input data and merely lists the force or displacement value for each degree of freedom ("ROW" in the table heading). The stress table contains one line of information for each element:

Element No., X_c , Y_c , σ_{xx} , σ_{yy} , σ_{xy} , σ_{rr} , $\sigma_{\theta\theta}$, $\sigma_{r\theta}$ The stress values are computed for the element's centroid location X_c , Y_c . Figures 15 and 16 present samples of these output tables.

If a stress intensity analysis has been executed, only a table of K-solutions is printed. Each line of the table corresponds to one crack location, containing:

Angle to crack opening, K_{I} , K_{II} A sample is shown in Figure 17.

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If abnormal conditions occur during execution, certain error messages may be printed by Program LUG. The messages and actions required are as follows:

(i) Insufficient core memory available for storage of the problem data causes the message:
 THE LENGTH OF THE "DATA" VECTOR FOR THIS CASE IS XXXX WHICH EXCEEDS YYYYY = THE MAXIMUM ALLOWED IN THE DIMENSION STATEMENT.

The entire run will be terminated if this condition occurs. The dimensions of vectors RE and IN (line 2 of the program code) are yyyyy. Redimension these vectors to 1.15 (xxxxx).

(ii) Ill-conditioning of the structure model causes the message:

INDEFINITE MATRIX; THIS CASE CANCELLED.

Execution continues with the next case. The most likely cause is misplacement of the crack tip, relative to the bushing O.D. Recheck the input data to make sure that the crack tip does not extend beyond the bushing, even if a singlematerial lug is being analyzed. Material property errors are another probable source. Illconditioning may result if the bushing is too stiff, compared to the lug, or vice versa. Errors may also results from incorrect specification of orthotropic material properties.

3.6 Visual Interpretation of Output

Level contour plots are recommended as the best means of visually interpreting the output from a stress analysis case. For this purpose, a scale plan of the lug outline should be prepared and the element centroid positions marked on the plan. The stress values may then be transferred and a contour plot prepared. Plots of σ_{rr} , $\sigma_{\theta\theta}$, $\sigma_{r\theta}$ in the region around the bearing pinhole and of σ_{xx} , σ_{yy} , σ_{xy} in the shank region are recommended. The nodal displacement solution table may be used to provide a plot of the deformed structure, if desired. The output from a stress intensity analysis is best treated by means of polar plots for K_I and K_{II}. These plots are discussed in detail with examples in Section 4.

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3.7 Program Status

At the date of this report, the following program options have been exercised successfully:

- (i) Stress and stress intensity analysis.
- (ii) Bearing load: tension, compression, positive shear, and negative shear.
- (iii) Cosine and uniform pressure distribution.
 - (iv) Isotropic, single-material lug.
 - (v) NT = 3, 4, and 6.

The following options have not been exercised to date:

- (vi) Isotropic, two-material lug.
- (vii) Isotropic bushing with orthotropic lug.
- (viii) NT > 6.

Section 4

RESULTS OF EXAMPLE ANALYSES

Two example analyses were run to demonstrate the program. The first was limited to stress and stress intensity analysis of the hypothetical wing root attachment lug shown in Figure 9. Second, a detail similar to the aft engine support pylon truss lug in the C-5A was subjected to a more extensive analysis. Experience with the program to date, on IBM S-370/165 and S-370/168 computers, indicates that approximately 1.8 to 3.6 CPU seconds per K_{I} , K_{II} solution pair are required, depending upon the amount of detail in the model.

4.1 Analysis of Wing Root Attachment Lug

Figure 18 summarizes the stress distribution in the hypothetical wing lug. Stress contours for σ_{rr} , $\sigma_{\theta\theta}$, and $\sigma_{r\theta}$ are shown. A survey of the numerical data confirmed that σ_{rr} , $\sigma_{\theta\theta}$ were symmetric about the lug centerline. Hence, only half-plots are shown for those contours. The survey also indicated that $\sigma_{r\theta}$ behaved antisymmetrically, as shown in the second part of Figure 18.

Figure 19 presents polar "butterfly" plots for K_I and K_{II} as functions of angle to the crack opening. The crack was 0.5 inches long and oriented radially. Again, the data behave symmetrically about the lug centerline (crack at 0° and 180° locations). The interpretation of these polar plots is explained in Figure 20. If the origin of the plot is identified with the center of the bearing pinhole, a radius vector through the assumed crack location may be constructed. The length of the vector between the origin and the K-plot then gives the corresponding stress intensity value.

If the crack size is small compared with the lug dimensions, there follows an intuitive hypothesis that the stress intensities ought to behave in the same manner as the uncracked structure stresses. This hypothesis can be confirmed, for the present case, by comparison of Figures 18 and 19. For a radially-oriented crack,

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 K_I should be influenced primarily by $\sigma_{\theta\theta}$, while K_{II} should be influenced primarily by $\sigma_{r\theta}$. Maxima of $\sigma_{\theta\theta}$ and K_I are observed to occur near $\theta = 90^{\circ}$, 270°. Maxima of $\sigma_{r\theta}$ occur approximately at $\theta = 45^{\circ}$, 135°, 225°, and 315°, while K_{II} maxima occur approximately at 60°, 120°, 240°, and 300°. The apparent discrepancy between K_{II} and $\sigma_{r\theta}$ can be explained by recognizing that the crack tip actually lies near the 1.5 and 2.0 ksi stress contours. Local maxima for $\sigma_{r\theta}$ in those regions are less sharply defined.

4.2 Analysis of Engine Pylon Truss Lug

Figure 21 is a scale plot of the structure model used to analyze a detail similar to the C-5A engine pylon aft truss lug. The actual lug has two tongues to place the bearing pin in double shear. It can be reasonably assumed that the load transferred into the engine pylon at this point is borne equally by both tongues. Hence, the lug program has been used to analyze one tongue. The model is 0.19 inch thick, with:

| D _I | = | 1.75 | inches | D_{B} | = | 2.35 | inches |
|----------------|---|------|--------|---------|---|------|--------|
| Н | = | 10.5 | inches | W | = | 3.5 | inches |

A 0.15-inch long crack was assumed, with radial orientation. Material properties for high-strength steel alloys were used:

 $E = 30 \times 10^6 \text{ psi}$ v = 0.295

The "bushing" O.D. was chosen merely to locate the crack tip at the middle of the bushing region. Models were run with 24 elements (NT = 3, "coarse mesh") and 32 elements (NT = 4, "fine mesh") around the bearing pinhole. The fine mesh model is shown in Figure 21. All runs were made with a 1,000-pound bearing load, as a standard for plotting the results.

Figure 22 summarizes the stress distribution near the hole, as obtained from a fine mesh model of the uncracked structure, with a cosine bearing pressure distribution. The symmetries discussed in Subsection 4.1 were observed again. Three additional checks were made to assure that the model accurately reflects the stress

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gradients caused by the lug geometry. First, in a typical section through the shank, the tension stress $\sigma_{_{\mathbf{X}\mathbf{X}}}$ was found to be uniform and statically equivalent to the bearing load, to better than one percent accuracy, for both models. Second, a section was taken through the bearing pinhole center (0 = 90°, 270°) and σ_{AA} was plotted. The radial variation of $\sigma_{A\,A}$ was found to agree generally with Timoshenko's classical solution for an eye bolt under tension bearing [17]. Also, numerical evaluation of $T \int \sigma_{AA} dr$ gave the bearing load, with 1.7 percent error for the coarse mesh and 1.4 percent error for the fine mesh. Finally, the solution for σ_{rr} was compared with the bearing pressure distribution. The peak value of the bearing pressure is given by $p_o = P/\pi D_T T$, where P is the bearing load. For the present case, $p_o = 3.83$ ksi and acts at $\theta = 0^{\circ}$. The two elements with centroid locations nearest to $r = D_{\tau}/2$, $\theta = 0^{\circ}$ were found to have $\sigma_{rr} = 3.5$ ksi, and the radial stress could be extrapolated to a value close to p. at the peak point. Based on these results and the measured performance of the PCRK59 element (Subsection 2.2), the fine mesh model was accepted as giving a converged solution for K_{τ} , having a cumulative error of 5 percent.

Butterfly plots for K_I and K_{II} are shown in Figure 23. Again, the stress intensities behave symmetrically to better than 1 percent accuracy for both models, and K_I follows $\sigma_{\theta\theta}$, while K_{II} follows $\sigma_{r\theta}$. The data for K_I , shown in the upper half of the figure, demonstrate that convergence has been obtained. The data for K_{II} , in the lower half of the figure, indicate that additional refinement of the mesh might be required to demonstrate Mode II stress intensity convergence. However, since the K_{II} values are generally smaller than K_I , and since they tend to decrease as the solution converges, no further refinements were made. The coarse model contained 408 degrees of freedom and took 48 CPU seconds to compute a complete set of 24 pairs of K_I and K_{II} solutions. The fine model contained 608 degrees of freedom and took 102 CPU seconds to compute 32 solutions.

The length of the lug detail was reduced from 10.5 inches to 7.0 inches for the remaining analyses, to eliminate superfluous elements in the shank and thus reduce computation costs. Fine

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mesh models (and a few "very fine" models) were analyzed in the remaining series. The shortened lug fine mesh model is illustrated by Figure 24.

The stress intensity analysis for cosine tension bearing was repeated to assess the influence of the change in shank length. Figure 25 compares the K_I and K_{II} butterfly plots from Figure 23 with corresponding plots for the shortened lug. A slight increase in stress intensities with decrease in shank length can be observed. Figure 26 compares butterfly plots for the 7-inch lug under cosine and uniform bearing. Three significant differences can be observed:

- (i) The increased ability of a uniform bearing pressure to spread the part outward changes the hoop stress from compression to tension at $\theta = 0^{\circ}$. Compare the uncracked structure stress contours for cosine bearing (Figure 22) with the contours for uniform bearing, shown in Figure 27.
- (ii) The maximum K_I value changes from 5 ksi $\sqrt{\text{in.}}$ at θ = 85° (cosine bearing) to about 4.7 ksi $\sqrt{\text{in.}}$ at θ = 107° (uniform bearing).
- (iii) Mode II stress intensities are lower for uniform bearing.

The third series of runs analyzed the case of positive shear bearing. Figure 28 illustrates the stress contours obtained for shear bearing with a cosine distribution. The behavior of $\sigma_{\rm rr}$ near the bearing pressure peak (now at $\theta = 90^{\circ}$) is similar to the tension bearing case (compare with Figure 22). The Cartesian stress components in the shank region were surveyed to provide additional equilibrium checks. Figure 29 compares the finite element stress distributions for $\sigma_{\rm XX}$, $\sigma_{\rm XY}$ through a typical shank section and for $\sigma_{\rm XX}$ axially, with engineering beam theory calculations:

$$\sigma_{XX} = -\frac{M(X)Y}{I} \qquad \sigma_{XY} = \frac{3V(X)}{2A} \left[1 - \left(\frac{2Y}{W}\right)^{2}\right]$$
(25)

where

M(X) = Section bending moment at X

V(X) = Section shear at X

I = Section moment of inertia = $TW^3/12$

A = Section area = TW

It is evident from the figure that the finite element results are within 1 or 2 percent of engineering beam theory. The only exception is the axial behavior of $\sigma_{\rm XX}$ which exhibits some stress concentration effects:

- (i) Due to the cantilever restraints, as the left end of the shank is approached.
- (ii) Due to the influence of the hole, as the shank/ ear interface is approached.

Based on these results, the fine mesh model was judged to be capable of giving stress intensities for shear bearing which are comparable to the tension bearing results (5 percent error).

Figures 30 and 31 present K_{T} and K_{TT} butterfly plots for cosine and uniform pressure distributions, respectively. Data for a "very fine" model (NT = 6, 48 elements around the hole) as well as for the fine mesh model, are shown in Figure 31. The refined model was run to improve the fairing of the curves, after plots of the fine mesh model were seen to have large gaps between ${\tt K}_{\tau}$ data points. The refined model data indicate that the fine mesh has not quite converged the K_{τ} solutions. Two interesting features are illustrated by these plots. First, the stress intensity maxima and minima no longer coincide with the stress distribution. Apparently, even a small crack is sufficient to change the stress distribution significantly when the bearing load is shear. Second, the significant difference between cosine and uniform pressure now occurs at the K_T maxima, which are about 10 percent larger for uniform pressure. This arises from the fact that the K_{T} maxima are located near and nearly opposite to the bearing load line of action.

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A fourth series of analyses treated the case of compression bearing, using only the fine mesh model. Both the stresses and stress intensities were found to behave symmetrically, similar to the case of tension bearing. Equilibrium checks and stress contour plots have been omitted, in view of the results already presented. Figures 32 and 33 show K_I and K_{II} butterfly plots for compression bearing with cosine and uniform distribution, respectively. The most interesting feature is the extreme sensitivity to load distribution when the crack is at or opposite to the load center. The Mode I stress intensity for uniform bearing increases by factors of 2 at the first location and 4 at the second. This extreme sensitivity results from the high hoop stresses which are present in these regions.

4.3 Example Application

To provide an example of how the butterfly plots may be applied to structural integrity verification analysis, the following data have been abstracted from load calculations for the original C-5A engine pylon truss design [22]:

| Load Condition | Tension (Compression) | Shear |
|----------------------------|------------------------|----------|
| "Maximum Compression" (MC) | -221×10^3 lb. | -340 lb. |
| "Maximum Tension" (MT) | 148×10^3 lb. | 220 lb. |

The values in the above table represent total load transferred through the attachment lug, and must be divided by 2 to obtain the loads per tongue. Since shear bearing can obviously be ignored for the above conditions, there results:

> Condition MC: 110.5×10^3 lb. Compression Bearing Condition MT: 74 x 10³ lb. Tension Bearing

Assuming that a cosine pressure distribution is representative, the following calculations can be made for 0.15-inch cracks assumed to be located at 0°, 45°, 90°, and 180°:

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| P | | · · · · · · · · · · · · · · · · · · · |
|----------|---|---|
| Crack | Condition MC | Condition MT |
| Location | (K values in ksi√in.) | (K values in ksi \sqrt{in}) |
| 0° | $K_{I} \approx 0.4 \times 110.5 = 44.2$ $K_{II} = 0$ | $K_{I} = K_{II} \cong 0$ |
| 45° | $K_{I} \approx 0.3 \times 110.5 = 33.2$ $K_{II} \approx 0$ | $K_{I} \approx 2.6 \times 74 = 192.4$ $K_{II} \approx 1.25 \times 74 = 92.5$ |
| 90° | $K^{I} = K^{II} = 0$ | $K_{I} \approx 5 \times 74 = 370$ $K_{II} \approx 0.2 \times 74 = 14.8$ |
| 180° | K _I = 1.63 x 110.5 = 180.1 K _{II} = 0 | $K_{I} = K_{II} \cong 0$ |

"Unit" K values are read from Figure 26 for Condition MT and from Figure 32 for Condition MC. The actual values are then computed by using the actual load to scale the unit values.

Potential fracture sites may be assessed by comparing K_I with K_{IC} for a proposed lug material. Since high strength steel alloys have fracture toughness generally below 100 ksi $\sqrt{in.}$, the above data indicate that a 0.15-inch crack is longer than critical size if the crack is located at 45°, 90°, or 180°. If a criterion that 0.15-inch cracks be less than critical is to be met, the designer might do this by increasing the lug thickness. Since the numerical data result from a linear analysis, the design can be scaled. For example, a revised thickness

$$T' = \frac{370}{K_{IC}} \times T = \frac{370}{50} \times 0.19 \approx 1.41 \text{ in.}$$
 (26)

can be calculated, assuming that protection against a 0.15-inch crack at 90°, in a material with $K_{IC} = 50$ ksi $\sqrt{in.}$, is required. At other points; e.g., $\theta = 45^{\circ}$ (Condition MT), K_{I} and K_{II} are comparable, and interaction formulas such as:

$$\left(\frac{K_{I}}{K_{IC}}\right)^{2} + \left(\frac{K_{II}}{K_{IIC}}\right)^{2} \leq 1$$
(27)

may be used to assess structural integrity.

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Section 5

CONCLUSIONS

A finite-element analysis program for computation of Mode I and Mode II stress intensity factors in attachment lug details has been presented. Since the program is based on an assumed-stress hybrid crack element, relatively crude structure models can be used. Performance tests of the crack element and the lug program have indicated that K_I and K_{II} solutions can be obtained to \pm 5 percent accuracy, for 1.8 to 3.6 CPU seconds per solution pair on currentgeneration large computers.

A series of demonstration examples, involving a lug detail similar to the C-5A engine pylon aft truss attachment lug, served to illustrate a number of important features of the K solutions. With the crack size held at 0.15 inch and the crack orientation kept radial, parametric analyses were conducted for K_I and K_{II} with the lug subjected to tension, shear and compression bearing forces. In each case, data were obtained for both a cosine and a uniform pressure distribution, to represent possible extremes of load transfer across the bearing surface. The parametric capability of the program was used to compute for each case a number of K_I and K_{II} values corresponding to location of the crack at various positions around the bearing pinhole. Polar plots of K_I and K_{II} versus angle to the crack location were presented to provide a concise picture of the parametric behavior.

The following specific conclusions can be drawn from the results of the analysis. First, uniform bearing pressure has more tendency than cosine pressure to spread the lug apart, and this is reflected by increased K_I values. This effect interacts with the relation between the crack location and the line of action of the bearing load. The most significant sensitivity to pressure distribution occurs when a K_I maxima coincides with or is close to the line of action of the load, or when a maximum lies opposite to the

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load line. Second, the most critical locations for a given crack often lie in unexpected places or correspond to unexpected load conditions. For example, cracks at +90° to the lug axis appear to be most critical in tension bearing. However, cracks at +45° may actually be the most critical if the luq material happens to have a low Mode II fracture toughness. A significant Mode I stress intensity value for a crack at 180°, under compression bearing, is another unexpected result. Finally, the maxima and minima of K_{T} and K_{TT} sometimes tend to follow local maxima and minima of the stress distribution in an equivalent uncracked structure, if the crack is small compared to the structure detail dimensions. However, the coincidence of maxima and minima occurs only for some load conditions, while significant discrepancies occur under other load conditions. One is, therefore, led to conclude that a stress analysis of an uncracked structure does not always provide a good map of where to expect the most critical stress intensities, even for small cracks.

REFERENCES

- Campbell, J. E., et al., "Damage Tolerant Design Handbook", Metals and Ceramics Information Center, Battelle Columbus Laboratories, 505 King Avenue, Columbus, Ohio, 1972.
- Matthews, W. T., "Plane Strain Fracture Toughness (K_{IC}) Data Handbook for Metals", Army Materials and Mechanics Research Center, Watertown, Massachusetts 02172, AMMRC MS 73-6, December 1973.
- 3. Anon., "Airplane Damage Tolerance Design Requirements", MIL-A-83444, U.S. Air Force Aeronautical Systems Division, Wright-Patterson AFB, Ohio 45433, June 1974.
- 4. Bowie, O. L., J. Appl. Mech., Vol. 31, pp. 208-212 (1964).
- 5. Bowie, O. L. and Neal, D. M., Int. J. Fracture Mech., Vol. 6, pp. 199-206 (1970).
- Bowie, O. L., Freese, C. E. and Neal, D. M., "Solution of Plane Problems of Elasticity Utilizing Partitioning Concepts", ASME Paper No. 73-APM-C, 1973.
- 7. Tada, H., Paris, P. C., and Irwin, G. R., <u>The Stress Analysis</u> of Cracks Handbook, DEL Research Corporation, Hellertown, Pennsylvania, 1973.
- 8. Pian, T. H. H., AIAA J., Vol. 2, pp. 1333-1336 (1964).
- 9. Tong, P. and Pian, T. H. H., Int. J. Solids Struc., Vol. 9, pp. 313-321 (1973).
- Luk, C. H., "Assumed Stress Hybrid Finite Element Methodology for Fracture Mechanics and Elastic-Plastic Analysis", Aeroelastic and Structures Research Laboratory, MIT, ASRL TR 170-1, December 1972.
- 11. Tong, P., Pian, T. H. H. and Lasry, S. J., Int. J. Num. Meth. Eng., Vol. 7, pp. 297-308 (1973).
- 12. Lasry, S. J., "Derivation of Crack Element Stiffness Matrix by the Complex Variable Approach", Aeroelastic and Structures Research Laboratory, MIT, ASRL TR 170-2, AFOSR-TR-73-1602, February 1973.
- 13. Zienkiewicz, O. C. and Cheung, Y. K., <u>The Finite Element Method</u> in Structural and Continuum Mechanics, McGraw-Hill, 1967.

- 14. Abramowitz, M. and Stegun, I. A. (ed.), <u>Handbook of Mathematical</u> <u>Functions</u>, National Bureau of Standards, U.S. Department of <u>Commerce</u>, Ninth Ed., November 1970.
- 15. Desai, C. S. and Abel, J. F., Introduction to the Finite Element Method, Van Nostrand Reinhold Company, 1970.
- 16. Orringer, O., "FEABL (Finite Element Analysis Basic Library) Documentation of Sample Program for Export Version", Aeroelastic and Structures Research Laboratory, MIT, ASRL TM 162-3-4, February 1974.
- 17. Timoshenko, S. and Goodier, J. N., <u>Theory of Elasticity</u>, McGraw-Hill, 1961.
- Washizu, K., <u>Variational Methods in Elasticity and Plasticity</u>, Pergamon Press, 1968.
- 19. Lin, K. Y., Tong, P. and Orringer, O., "Effect of Shape and Size on Hybrid Crack-Containing Finite Elements", submitted for presentation at ASME Pressure Vessels and Piping Conference, San Francisco, California, June 1975.
- 20. Orringer, O. and French, S. E., "FEABL (Finite Element Analysis Basic Library) User's Guide", Aeroelastic and Structures Research Laboratory, MIT, ASRL TR 162-3, AFOSR-TR-72-2228, August 1972.
- 21. Orringer, O. and French, S. E., "FEABL (Finite Element Analysis Basic Library) Version 2/Release 2", Aeroelastic and Structures Research Laboratory, MIT, ASRL TM 162-3-3, February 1974.
- 22. Neilson, J. A., Shockley, E. J. and Dallas, C. H., "C-5A Pylon Evaluation and Redesign Recommendations", Lockheed-Georgia Aircraft Company, Marietta, Georgia, Report No. SRD 72-21-775, p. 29.

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FIG. 1 COMBINATION OF ASSUMED-DISPLACEMENT ELEMENTS WITH HYBRID CRACK-CONTAINING ELEMENT



FIG. 2 CONVENTIONS FOR ASRL QUAD4 ASSUMED-DISPLACEMENT ELEMENT







APPLICATION OF PCRK59 ELEMENT TO SYMMETRIC ANALYSES FIG. 4

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FIG. 5 ATTACHMENT LUG DETAIL



FIG. 6 CRACK PARAMETERS

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FIG. 11 PROGRAM LUG FLOW CHART



FIG. 11 (CONTINUED)



FIG. 11 (CONCLUDED)

CASE 36: LUG PROGRAM STRESS INTENSITY ANALYSIS

ANALYSIS OPTION= 2; LCAD OPTION= 2

MODE= 1 (1=ISOTROPIC, 2=CATHCTECTIC LUG) TOTAL OF 32 ELEMENTS AROUND PIN HOLE BOLE I.D.= 0.2002+01 BUSHING 0.E.= 0.300E+07

CRACK LENGTH= 0.200E+00; DIRECTION= 0.0

BUSHING MATERIAL: B= 0.100E+08 ND= 0.300E+00

ISOTROPIC LUG: E= 0.100E+08 NU= 0.300E+00

APPLIED TERSION= 0.100E+04 LB. AND SHEAE= 0.0

LB.

LUG WIDTH= 0.400E+01 LUG LENGTH= 0.700E+01 THICKNESS= 0.100E+01

FIG. 12 PRINTOUT OF INPUT DATA





(a) Node Numbering Diagram



FIG. 13 (CONCLUDED)

(b) Element Numbering Diagram







CASE 1: CASE 1 11 DECEMBER 1974 ANALYSIS OFFICN- 11 LOAD OFFICN- 2 -OPTHOTROPEC LUGE ISOTAOPIC. APJUND TOTAL OF 32 ELEMENTS HOLE I.D.= 0.175E+01 UND PIN HOLE BUSHING J.D.+ 0.235E+01____ LUG WIDTH+ 0.350E+01_ LUG_LENGTH+ 0.700E+01_ THICKNESS+_0.190E+00 _ ISOTROPIC LUGT E= 0.300E+08 NU= 0.295E+30 APPLIED TENSION- 0.100E+04 LB. AND SHEAR+ 0.0 PRESCRIBED FORCE/DISPLACEMENT VECTORS ROM 1 2 VALUE 0.987E+02 -0.124E-03 0.0 0.0 0.0 0.0 NON _______ 11 _____ 12 _____ VALUE 0.963E+02 0.192E+02 0.0 -13_ 14 ..נג 0.0 A 3 NOW 21 22 . VALUE 0.907E+02 0.376E+02 0.0 _0.0 0.0 0.0 0.0 34 0.0 0.0 0.0 0.0 0.0 ROW 41 42 VALUE 0.494E+02 0.694E+02 0.0 0.0_ 53 NOW 51 52 52 VALUE 0.545E+02 0.816E+02 0.0 0.0 ROW 61 62 VALUE 0.376E+02 0.907E+02 0.0 0.0 0.0 ROW _____71 ___72 ____ VALUE 0.192E+02 0.963E+02 0.0 .75 0.0 82 4918+02 809 41 HELVE 0.0 447 AOW 0.0 0.0 VALUE . 0.0 0.0 .0.0 0.0. . 0.0 .. . 0.0. 451 AON VALUE 453 424. 455 556 457 158 .0.0 0.0 0.0 0.0 0.0 0.0 461 ° ROW 462 .__0.0. 0.0 DISPLACEMENT SOLUTION VECTOR: ROW VALUE L 2 3 4 5 5 6 7 6 9 10 0.572E-03 0.654E-06 0.556E-03 0.861E-06 0.543E-03 0.875E-06 0.527E-03 0.907E-06 0.516E-03 0.929E-06 ROW LI 12 LI 14 L5 L6 17 L8 19 20 VALUE 0.567E-03 0.213E-04 0.550E-03 0.225E-04 0.537E-03 0.239E-04 0.519E-03 0.279E-04 0.508E-03 0.339E-04
 NOW
 21
 22
 23
 24
 25
 26
 27
 28
 29
 30

 VALUE
 0.553E-03
 0.396E-04
 0.534E-03
 0.412E-04
 0.520E-03
 0.434E-04
 0.499E-03
 0.503E-04
 0.484E-03
 0.409E-04
 ROW 31 32 33 34 35 36 36 37 38 39 40 WALUE 0.530E-03 0.536E-04 0,509E-03 0.772E-04 ROW 41 42 43 44 45 46 47 40 50 0.500E-03 0.618E-04 0.477E-03 0.602E-04 0.459E-03 0.605E-04 0.430E-03 0.666E-04 0.405E-03 0.795E-04 ADW 51 52 53 54 55 56 57 58 57 58 59 60 VALUE_0_465E=03__0.635E=04__0.661E=03__0.550E=04__0.390E=03__0.576E=04__0.361E=03__0.674E=04 ADM 61 62 63 64 65 66 67 68 69 70 WALUE 0.427E-03 0.403E-03 0.403E-03 0.403E-04 0.3344E-03 0.418E-04 0.3535E-03 0.3383E-04 0.322E-03 0.429E-04 ROW 71 72 73 74 75 76 76 77 78 79 RO VALUE 0.388E-03 0.454E-04 0.365E-03 0.303E-04 0.349E-03 0.210E-04 0.322E-03 0.127E-04 0.294E-03 0.116E-04 ROW 91 92 93 94 95 96 97 98 99 100 0.311E-03 -0.822E-05 0.303E-03 -0.163E-06 0.295E-03 -0.216E-06 0.295E-03 -0.296E-06 0.295E-03 -0.356E-06

FIG. 15 FORCE AND DISPLACEMENT TABLES FROM STRESS ANALYSIS

WING LUG PGM TEST CASE #4a: ALUMINUM LUG FOR STRESSES ONLY ~ STRESS ANALYSIS FOR CASE

-0.427E+03 0.286E+03 -0.448E+03 -0.124E+04 -0.974E+03 -0.105E+04 -0.875E+03 -0.145E+04 -0.495E+03 0.790E+03 0.117E+04 0.115E+04 0.216E+04 0.126E+04 0.242E+04 0.113E+04 0.217E+04 0.796E+03 0.152E+04 -0.285E+03 -0.547E+03 -0.796E+03 -0.246E+03 -0.683E+03 -0.175E+04 -0.184E+04 0.548E+03 -0.152E+04 -0.113E+04 ----RT----POLAR STRESSES ----11-----0.185E+04 0.244E+04 0.319E+04 0.331E+04 0.556E+04 C.483E+04 0.841E+04 0.662E+04 C.110E+05 0.818E+04 0.126E+05 C. 887E+04 0.120E+05 0.839E+04 0.920E+04 C.674E+04 0.553E+04 0.429E+04 0.186E+04 -0.109E+04 -0.150E+03 -0.275E+04 -0.127E+04 -0.275E+04 -0.127E+04 -0.109E+04 0.180E+04 -0.150E+03 0.186E+04 -0.106E+05 -0.153E+03 ----RR-----0.115E+05 -0.931E+04 -0.846E+04 -0.89CE+04 -0.687E+04 -0.649E+04 -0.469E+04 -C.365E+04 -0.212E+04 -C.360E+03 0.391E+03 0.113E+04 0.162E+04 0.732E+03 0.150E+04 0.487E+03 C.107E+04 0.195E+03 0.617E+03 -C.302E+02 0.254E+03 C.701E+02 - C. 153E+03 0.701E+02 0.254E+03 0.194E+03 C.616E+03 -C.301E+02 ----X -----0.197E+0.4 -0.195E+04 -0.536E+04 -0.685E+03 0.643E+03 -0.253E+03 0.218E+04 0.329E+03 0.211E+04 C.926E+03 0.110E+04 0.932E+03 0.355E+03 0.598E+02 -0.354E+03 -0.110E+04 -0.504E+04 -C.723E+04 -0.610E+04 -0.693E+04 -0.459E+04 -0.457E+04 -0.262E+04 -C.120E+04 0.113E+04 C.188E+03 -0.594E+02 -C.188E+03 -0.93.1E+03 CARTESIAN STRESSES ---- \ \ ----C.213E+04 C.708E+03 -0.74CE+03 -0.212E+04 -0.267E+C3 0.425E+03 0.143E+04 0.116E+04 0.743E+03 C.733E+02 0.1505+03 -0.727E+03 -0.150E+04 -0.116E+04 -0.278E+04 -0.135E+04 -0.278E+04 -C.15CE+04 0.148E+03 -0.727E+03 0.156E+04 0.685E+03 -0.198E+04 -C.228E+04 -0.163F+04 0.111F+04 0.113E+04 -0.139E+04 -0.117E+04 -0.120E+04 ----X X -----0.127E+04 -0.112E+05 -0-895E+04 -0.586E+04 -0.260E+04 0.421E+04 0.770E+04 0.544E+Ò4 0.315E+04 0.378E+03 -0.124E+03 0.378E+03 0.315E+04 -0.842E+03 0.390E+04 0.949E+04 0.125E+05 0.884E+04 0.120E+05 0.857E+04 0.878E+04 0.750E+04 0.488E+04 0.190E+04 0.189E+03 -0.124E+03 0.189E+03 0.127E+04 0.190E+04 -0.811E+04 ---- XC----0.421E+0C 0.485E+00 0.421E+00 0.485E+00 0.142E+01 0.196E+01 0.226E+01 0.196E+01 0.142E+01 -0.421E+00 -0.485E+00 -0.123E+01 0.123E+01 0.298E+01 0.369E+01 0.226E+01 -0.196E+01 -0.226E+01 0.256E+01 0.295E+01 0.343E+01 0.319E+01 0.343E+01 0.256E+01 0.295E+01 -0.142E+01 0.319E+01 0.369E+01 0.298E+01 0.123E+01 CENTROID LOCATION, 0.319E+01 0.369E+01 C.298E+01 0.343E+01 C.256E+01 C.295E+01 C.196E+01 0.226E+01 C.123E+01 C.142E+01 0.421E+00 C.485E+00 -C.421E+00 -0.485E+00 -0.196E+01 -0.226E+01 -C.256E+01 -0.319E+01 -C.319E+01 -0-369E+01 -0.123E+01 -C.142E+01 -C.295E+01 -0.298E+01 -C.343E+01 -0.369E+01 -0.298E+01 -0.343E+01 -0.295E+01 ----XC-----C.256E+01 A: BUSHING PART 5 T 22 23 24 26 28 52 30 4 S 90 ω J 201 12 5 14 ŝ 16 8 20 27 LNUP 17 21

PART OF STRESS TABLE FIG. 16

-0.217E+04

0.180E+04

553F+0/

¢

^.211E+04

....0

0.488E+04

c 1

-C.196E+01

• • •

-0.113E+04

LUG PROGRAM STRESS INTENSITY ANALYSIS 36 STRESS INTENSITIES FOP CASE

| K2 | 0.869E-01 | 0.207E+02 | C.5C9E+01 | C.370E+02 | C.172E+02 | 0.390E+02 | 0.720E+02 | C.579E+02 | 0.679E+01 | 0.233E+03 | 0.409E+03 | 0.403E+03 | C.267E+C3 | 0.152E+03 | C.998E+02 | C.582E+02 | 0.208E-01 | 0.582E+02 | C.998E+02 | 0.151E+03 | C.267E+03 | C.403E+03 | C.4C9E+03 | C.233E+03 | C.675E+01 | C.580E+02 | C.723E+02 | 0.393E+02 | C.168±+02 | C.366E+02 | C.529E+01 | 0.2052+02 |
|---------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|------------|-----------|-----------|------------|------------|------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|------------|-----------|-----------|-----------|-----------|-----------|-----------|
| ********** | 0.382E+03 | 0.4218+03 | 0.488E+03 | 0.5068+03 | 0.489E+03 | 0.495E+03 | 0.532E+03 | 0.594E+03 | 0.713E+03 | 0.876E+03 | 0.927E+03 | 0.773E+03 | 0.5288+03 | 0.298E+03 | 0.106E+03 | -0.313E+02 | -0.813E+02 | -0.312E+02 | 0.106E+03 | 0.2985+03 | 0.5283+03 | C.773E+03 | 0.9273+03 | 0.876E+03 | 0.714E+03 | 0.595 2+03 | 0.533E+03 | 0.496E+03 | 0.4902+03 | 0.506E+03 | 0.487E+03 | 0.421E+03 |
| SI CI ES | 0.0 | 0.112E+02 | 0.225E+02 | 0.337E+02 | 0.4503+02 | 0.562E+02 | 0.675E+02 | 0.787E+02 | 0.900E+02 | 0.101E+03 | 0.112E+03 | 0.124E+03 | 0.135E+03 | 0.146E+03 | 0.157E+03 | 0.169E+03 | 0.180E+03 | 0.191E+03 | 0.202E+03 | 0.214E+03 | 0.225E+03 | 0.2365+03 | 0.2478+03 | 0.259E+03 | 0.270E+03 | 0.281E+C3 | 0.292E+03 | 0.304E+03 | 0.3152+03 | 0.326E+03 | 0.337E+03 | 0.349E+03 |
| ₽OS ****** | - | 2 | m | Ţ | ŝ | 9 | ٢ | œ | 6 | 0, | 11 | 12 | 1 3 | 14 | 15 | 16 | 17 | 8 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 1 | 32 |

4 ļĮ STRESS INTENSITY FACTOR TABLE FROM ANALYSIS WITH NT FIG. 17



FIG. 18 STRESS CONTOURS FOR WING ROOT LUG



FIG. 18 (CONCLUDED)







FIG. 20 INTERPRETATION OF BUTTERFLY PLOTS





.



STRESS CONTOURS FOR ENGINE PYLON TRUSS LUG (TENSION BEARING, COSINE PRESSURE) FIG. 22



FIG. 23 BUTTERFLY PLOT FOR ENGINE PYLON TRUSS LUG (TENSION BEARING, COSINE PRESSURE)







FIG. 25 EFFECT OF SHANK LENGTH ON STRESS INTENSITY (TENSION BEARING, COSINE PRESSURE)



FIG. 26 COMPARISON OF COSINE AND UNIFORM PRESSURE DISTRIBUTIONS (TENSION BEARING)





FIG. 27 STRESS CONTOURS FOR 7-INCH ENGINE PYLON TRUSS LUG (TENSION BEARING, UNIFORM PRESSURE)







FIG. 28 STRESS CONTOURS FOR 7-INCH ENGINE PYLON TRUSS LUG (POSITIVE SHEAR BEARING, COSINE PRESSURE)







Note: See Fig. 24 for location of x'y' axes

FIG. 29 COMPARISON OF FINITE ELEMENT RESULTS WITH ENGINEERING BEAM THEORY (POSITIVE SHEAR BEARING, COSINE PRESSURE)


BUTTERELY PLOTS FOR 7-INCH ENGINE PYLON TRUSS LUG (POSITIVE SHEAR BEARING, COSINE PRESSURE)



PROCEDURE LUG IS A FINITE-ELEMENT ANALYSIS PROGRAM FOR STRESS ANALYSIS AND/OR* CALCULATION OF NASA/ASTM STANDARD STRESS INTENSITY FACTORS IN A ONE- OR TWO- * PROCEDURE LUG AUTC-GENERATES A STRUCTURE MCDEL REPRESENTING AN ATTACHMENT LUG* RESULTANT BEARING FORCE. THE BEARING FORCE IS INPUT AS A TENSION COMPONENT #1) IS CONCENTRIC WITH THE SEMI-CIRCLE. THE LUG (MATL #2) MAY BE ISOTROPIC 6E10.0) 2E10.0) (5E10.0) (2E10.0) 2E10.0) CIRCULAR SHAPE ON THE RIGHT. AN INTEGRALLY BONDED ISOTROPIC BUSHING (MATL OF ORTHOTROPIC WITH MATERIAL AXES INCLINED AT AN ARBITRARY ANGLE TO THE XY A COSINE OR UNIFORM PRESSURE BEARING LOAD IS APPLIED TO THE LEFT (VERTICAL) EDGE OF THE LUG IS BUILT IN. 20 A4) (FARALLEL TO X, POSITIVE TO RIGHT) AND A SHEAR COMPONENT (PARALLEL TO Y, (112) THE LUG BEGINS WITH CCNSTANT WIDTH (Y-DIRECTION) AND FAIRS INTO A SEMI-15) MULTIPLE CASES MAY BE RUN BY INNER SURFACE OF THE BUSHING, CENTERED ON THE LINE OF ACTION OF THE **1** = STRESS ANALYSIS AND FULL PRINT THE INPUT DATA CARD STACK. TITLE = ANY DESCRIPTIVE INFORMATICN FOR THIS CASE MATERIAL LUG SUBJECTED TO A BEARING LOAD. PLANE STRESS IS ASSUMED. NCASES = TOTAL NO. OF CASES TO BE RUN ELT2, ET2, G2, THETA ATTACHMENT LUG PROCEDURE (LUG) CSIZE PARALLEL TO THE X-AXIS. THE REPEATING CARDS 2 THRU 7 OF E N MCDE, Н, Т, IANL = ANALYSIS CFTICN: STACK: TENSN, SHEAF IANL, LCAD, DATA CARD DI, DB, POSITIVE UP). Δ **V**2 NCASES AXIS SYSTEM. TITLE EXPLANATION: EL2, ы, E2, 08 TUPUT 1. 4. **ں** 9 υ υ υ υ υυ υυ $\upsilon \upsilon$ \mathbf{U} 0 د ۲ 000 U

APPENDIX A

x ÷¥ X * * ×. ¥. ×. X ¥ TOTAL NO. OF DIVISIONS IN 45-DEGREE INTERVAL AROUND BUSHING; 8*NT DIVS ANGULAR INTERVALS FROM 0 TO 360 DEGREES AROUND THE CDIR = ANGLE (DEGREES) FROM RADIAL DIRECTION TO CRACK DIRECTION, POSITIVE WILL OCCUR ARCUND ENTIRE EUSHING. (MESH IS AUTO-GENERATED FROM NT.) 2 = STRESS INTENSITY ANALYSIS; PLACE CRACK AT BUSHING; PRINT ONLY K1 AND K2 VERSUS ANGLE. EI2, ELT2, ET2, G2 = LUG ELASTIC MODULI THETA = ANGLE PROM X-AXIS TO L-AXIS, POSITIVE CCW (DEGREES) PROCEDURE LUG REQUIRES THE FOLLOWING SUBROUTINES: = ORTHOTRCPIC LUG ASHLTV, ECON, FACT, ORK, SETUP, SIMULQ, XTRACT E1, V1 = BUSHING YCUNGS MODULUS, EOISSCN RATIO 1 = ISCIROPIC LUGCSIZE = CRACK LENGTH (USED ONLY IF IANL = 2) NT VALUES FRCM 2 TO 4 CAN BE CHOSEN. $E2_{\sigma} V2 = SAME FOR LUG (ONLY IF MODE = 1)$ TENSN, SHEAR = BEARING FORCE COMPONENTS = UNIFORM EEARING COSINE BEARING CCW (USED CNLY IF IANL = 2) 2 = MATERIAL MCLE OPTION: = LUG LENGTH, RCCT TO TIP CTFORM, QUAD4, PCRK59 Ħ • ASRL FEABL/V2: 3 LOAD OPTION: = LUG THICKNESS DI = BUSHING I.D. DB = BUSHING O.D.ASRL EGL: FOR MODE = 2: W = LUG HIDTHH 11 LCAD **.**-5 MODE НN EH ш 000000000000000000 υυ \mathcal{O} 0000 000000000 υυ υ υυ

| ¥ | ¥ | ¥ | * 1 | € ¥ | × | * | ¥ | * | ¥ | ¥ | ¥ | ¥ | ¥ | ¥ | × | ¥ | ¥ | ¥ | ¥ | ¥ | ¥ | ¥ | Ξ | 2 | ŋ |),t | ທ | 9 | 5 | 8 | 6 | 0 | 4 | 2 |
|------------|-------|---|--------------------|--|------------|---------------|--------------|----------|-----------|--------|---|-------|----------|-----|---|------------------|----------|--------|---|--------|---|-------------|-----|----------|------------|--------|------------|----------|------------------|--------|--------|---------------------|----------|--------|
| | | | ¢ | د | • [# | $\frac{1}{2}$ | } | | | | | | | | | | | | | | | *** | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 001 | 001 | 60 |
| | | | 4 | | | 0 B | ;) | | | | | | | | | | | | | | | *** | ŋ | Ð | ũ | ŋ | ŋ | ŋ | Ð | ŋ | B | ŋ | ŋ | ŋ |
| | | | NA | - 7 - 7 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 | | | | RAN | ΡY | • | | | | | | | | | | | | *** | 3 | Ц | H | L L | Ц | 1 | Г | H | Ξ | 1 | h | H |
| | | | ATR. | C M M | 20 K | | III. | DB T | IDC | | | | | | | | | | | | | *** | | | | | | | | | | | | |
| | | | E O E | ם בי ש ש | | 50 | 5 | , E4 | ž | | | | | | | | | | | | | ** | | | | | | | | | | | | |
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| | | | DAE | រជ ភ្ល ភ្ល | | | 1 1 20 | រ ដ ខ | : | • | | | | | | RΥ | | | | | | *** | | | | | | | | | | 0D | 18) | |
| | | | AN | | i S | i sa Fa | DQ | E | E E | | | | | | | 1 0 L | | | | | | ** | | | | | | | | | | Ň | 2 | |
| | | | E S C | 2 12 2 12 2 12 | | | U O | RO . | s su | | | Х | 4 33 | | | ORA | | | | 061 | | *** | | | | | | | | | | Э) | C B | |
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| | | | ZÂ | ŏ | H | S | 5 | | 10 | B | | S | _ | F | | P. | _ | E E | _ | ບັ | | ** | | | | | | | • | i | E. | | | |
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0028 0013 0014 0015 0016 0017 00 18 0019 0022 0023 0024 0025 0026 0029 0032 0033 0034 0035 0036 0037 0038 0039 0042 0043 0045 0046 0020 0027 00 30 01100 0044 00 47 00 48 0021 0031 0041 LUG DIUG LUG DUL IUG LUG LUG LUG LUG LUG LUG LUG LUG LUG **TUG** LUG LUG LUG 601 FORMAT(5H1CASE,I4,1H:,1X,2CA4)
602 FORMAT(6HCMODE=,I2,33H (1=ISOTROPIC, 2=ORTHOTROPIC LUG),/,1X,8HTOTLUG I.D.=, E10.3,5X,LUG LUG SHEAR=, E10.3, 4H LB.) LUG CASE CANCELLEDLUG 4--,2X,10H----XY----,2X,10H----RR----,2X,10H----TT---,2X,10H----RTLUG LUG LUG LUG LUG FOLUG 3 7X, 10H----XC----, 2X, 10H----YC----, 2X, 10H----XX----, 2X, 10H----YY--LUG LUG LUG LUG 607 FORMAT (25H1STRESS ANALYSIS FOR CASE, 14, 1X, 20A4, /, 5H0LNUM, 4X, 18HCENLUG 610 FORMAT (28H1STRESS INTENSITIES FOR CASE, I4, 1X, 20A4, //,4H POS,7X,10HLUG 2TPOID LOCATION, 12X, 18HCARTESIAN STRESSES, 20X, 14HPOLAR STRESSES, /, 6042 FORMAT (44H0ORTHOTROPIC LUG WITH MATERIAL AXES INCLINED, E10.3,18H 313HBUSHING 0.D.=,E10.3,5X,10HLUG WIDIH=,E10.3,2X,11HLUG LENGTH=, ATTACH LUG PROGRAM 2-- ANGLES--, 2X, 10H----K1----, 2X, 10H----K2----, /, 1X, 46 (1H*) 613 FORMAT (14H0CRACK LENGTH=, E10.3, 12H; DIRECTION=, E10.3) 606 FORMAT (1HC, 10 (4H****), /, 39HJINDEFINITE MATRIX; THIS 612 FORMAT (17 HCANALYSIS OPTION=, I2, 14H; LCAE OPTION=, I2) 2AL OF, I3, 25H ELEMENTS ARCUND FIN HCLE, /, 1X, 10HHOLE 603 FCRMAT (21HOBUSHING MATERIAL: E=, E10.3,4H NU=, E10.3) E=, E10.3, 4H NU=, E10.3) DATA TEMP/4*9./, NOD/4*0/, CB/9*J./, PI/3.141593/ 605 FORMAT (17HUAPPLIED TENSION=, E10.3, 15H LE. AND 2EG AND C MATFIX=,3X,3E15.3,/,2(75X,3E15.3,/) **DNIM** 5----,/,1X,25(4H****),/,1X,15HPART A: BUSHING) 611 FCRMAT (1X, I3, 7X, E10.3, 2X, E10.3, 2X, E10.3) 600 FORMAT (4 (1X,30 (4H****) ./) ./.36H0FEABL-2 DIMENSION ONE (48), TWO (48), ANGLE (48) 2R,I4,6H CASES,/,4(1X,3C(4H****),/)) STORAGE FOR SIRESS INTENSITY RESULTS 4 E10.3,2X,10HIHICKNESS=,E10.3) (E(1,1), C(1,1)) 6041 FORMAT (21H0ISCIRCPIC LUG: 608 FORMAT (1X, 11HPART B: LUG) 609 FORMAT (1X, 14, 8 (2X, E10.3)) 2,/,1X,1C(4H****)) SQPI = SQRT(PI)READ/PRINT CONTROL 501 FORMAT (8E10.3) 500 FORMAT (1615) EQUIVALENCE 502 FORMAT (20A4) DEVICE CODES υ υ υ

0050 0055 0059 0063 00.64 0053 0056 0058 0060 0061 0062 0066 0068 00 69 0049 0051 0052 0054 0067 06.70 0076 0078 0057 0073 0074 0075 0079 0080 0082 0083 0084 0071 0072 0077 0081 LUG LUG LUG LUG LUG LUG LUG LUG LUG DUL LUG **DUG** LUG (STRESS ANALYSIS: NO CRACK) OR 2 (STRESS INTENSITY ANALYSIS ARC OVER 180-DEG (COSINE BEARING) OR 2 (CCNSTANT BEARING) = THOPI* (SIN (AAA3+AAA4) -SIN (AAA3-AAA4)) (ISOTROPIC LUG) OR 2 (ORTHOTROPIC LUG) CDIR WITH CRACK SEQUENCED AFOUND PIN HOLE) = DIVISIONS PER 45 DEG AROUND PIN HCLE T, CSIZE, IANL , LOAD, MODE, NT IF (IANL .EQ. 2) MAXLOC = NT8H. ICASE, TITLE . **1, NCASES** (KR, 501) DI, DB, WRITE (KW, 600) NCASES NCASES TITLE DO 100 I = 3, NT8, 2= 0.25*PI/NT = AAA2+AINC = AAA3+AINC (KW, 601) COS (AAA2) H 3*NT+1 = AINC/2. L+LN*t:= = 5*NT+1+ I = 6 * N + .(KR, 50C) READ (KR,502) = NT2+1= 2./PI (KR, 500) = -PI/2ICASE Z*NT $TR = 8 \pm NT$ • • = I+1 MAXLOC = КŅ 11 ſ DO 32 KT1 =WRITE I •--NT2 =NT6P1 CASE LOOP THOPI KW = NT 2P1 NT 3P1 NT 4P1 NT5P1 READ AAA3 READ AINC READ AAA2 AAA2 AAA4 11 A A A 3 AAA1 CA2 LP 1 It KR Ħ 11 LOAD MODE IANL ΤN υ 00000

0109 0113 0115 0116 0118 0119 0085 0086 0087 0089 0092 0093 00.94 0095 0096 1600 0098 6600 0100 0101 0102 0103 0104 0105 0106 0107 0108 0110 0111 0112 0114 0117 0120 0088 0600 0091 LUG LUG LUG LUG LUG LUG LUG DUL LUG LUG LUG LUG DOT LUG LUG LUG LUG LUG LUG LUG LUG LUG LUG LUG LUG LUG TUG ЧO TO LINE SURFACE OUTWARD NORMAL 24 CDI E۰ CSIZE, æ DB, ISOTROPIC) WRITE (KW, 613) MCDE, NT8, DI, -0.5*AAA4 = CCW ANGLE FRCM BEARING WRITE (KW, 612) IANL, LOAD CRACK (DEGREE MEASURE) = AAA1*SA2 = AAA4*SA2 (Δ+• AAA4*CA2 = AAA1*CA2 0.5*AAA4 (ALWAYS . 0 11 ċ PIN HOLE DIAMETER H ŧI 5 • CB (2, 0.5¥E. 0 V*CB (CB (1, = SIN (AAA2) = PART THICKNESS CSIZE = CRACK SIZE(KW, 602) (KW, 603) エート IF (IANL . EQ. SCALE (NT8+1, 1) SCALE (NT8+1,2] SCALE (NT8+2,2 SCALE (NT8+2,1) = BUSHING 0.D. (KR, 501) Ħ BUSHING MATERIAL Ņ IP1,1) [IP1,2) = 0.5 * DI0.5*03 (I,2) SCALE(I,1) = 0.5*H = LUG LENGTH SCALE (1, 1) SCALE (2,2) ţ SCALE (2,1) SCALE (1,2) HIGIN SOT = W <u>H-H</u> = (3,3) CB (1, 1] CB (2,2) CB (1,2' WRITE FRITE CB (2,1 SCALE SCALE (SCALE (READ łł SA2 RL CB RB RI CDIR IJ 100 DВ HQ E FI 000 υ 00000

0129 0131 0132 0135 0136 0139 0143 0144 0145 0146 0147 0148 0149 0150 0154 0156 0122 0123 0124 0125 0126 0127 0128 0130 0133 0134 0137 0138 0140 0141 0142 0151 0152 0153 0155 0121 LUG LUG LUG LUG LUG LUG E UG LUG LUG LUG LUG LUG LUG LUG LUG LUG CL (2,2), CL (3,3), THETA THETA = MATERIAL AXIS INCLINATION (DEGREES) ,1), CL(1,2), TENSN, SHEAR GO TO 4000 READ (KR, 501) TENSN, SHEAR WRITE (KW, 6042) THETA, CL FOR CL GO TO CALL CTFORM (THETA, C, CL) (Λ+• 四/(1.-7*1 ETA = (3. - V) / (1. + V)(•0 SFECIAL TRANSFCRMATICN GO TO (1,2), MCDE (6,4), MODE CL(2,1) = CL(1,2)**/ヨ*ら・** 114 V*CL (C(I,J) = CL(I,J)T_NSNET SHEAR/T IF (THETA .EQ. WRITE (KW, 6041 = -THETA CT (1 WRITE (KW, 605) IF (IANL . EQ. READ (KR, 501) 2 READ (KR, 501) ~ **~** ~ • • • 0 || 0 # 0 || G = CB(3,3)n 11 Ŋ APPLIED LOADS MATERIAL DO 5 I = DO 5 J = TENSN = H ORTHOTROPIC T = 1.0CL (3,2) CL (2,2) CI (3,3) GO TO 3 CL (1, 3) CL (2,3) CL (1, 2) CL (3,1) CL (1, 1) THETA GO TO SHEAR ISOTROPIC m LUG - 4 ഹ Q υ C υ C υ C

0158 0159 0162 0163 0165 0157 0160 0161 0164 0166 0167 0168 0169 0170 0171 0172 0173 0174 0175 0176 C177 0178 0179 0180 0181 0182 0183 0184 0185 0186 0188 0189 0187 0190 0192 0191 L UG LUG DUL LUG LUG LUG LUG LUG LUG T UG LUG LUG LUG LUG LUG 10 L **H**SEE THE BY SIZING C TOFOLOGY PARAMETERS AND HOUSEKEEPING; BEGIN KEEP ELEMENT ASPECT RATIOS CLOSE TO UNITY CALL SETUP (LDATA, NDW, LIST, RE, IN) LIST = LIST+19GO TO 2002 (THREE STAGES) = NM 1+1 = 2* (NT8*NNR+NA*NT2P1) \sim GO TO 2002 D0 2011 LOC = 1, MAXLOC 1, MAXLOC 11 H ΤΞN NM1 = NT8 + NR + 2 + NT + NANRB NRL = (RB-RI) /E+0.5 = (RL-RB) /E+0.5 H E = PI*(RI+RB)/NT8E = PI * (RB + RL) / NT8NA IF (IANL .EQ. 2) 3 ELEMENT CONNECTIONS 7 7 C CFACK LOCATION LOOP NETBP1 = NETB+16 NETB = NT8 + NRBIF (NA .LE. 0) DC 2001 LOC = ò • NRB+2 IF (IANL . EQ. IF (IANL . EQ. (NRB .LE. NEBP1 = NRE+1IF (NRL .LE. E = 0.5 * 4 / NTNA = A/E+0.5NR = NRB+NRL $NDW = 4 \pm NT \pm 2$ STAGE 1: BUSHING $LIST = 9 \neq NM1$ $= 2 \pm NNR$ IMASTR IJ Ħ = NR+1= NM1 4 COO CONTINUE NREP2 = ONE (LOC) 2001 TWC (LOC) H NNR LUN NRL NRB NDR NET Ъ LP C υυ

0193 0194 0195 0196 0198 0199 0203 0205 0206 0208 0209 0226 0197 0200 0201 0202 02.04 0207 0210 0211 0212 0213 0214 0215 0216 0217 0218 0219 0220 0221 0222 0223 0224 0225 0227 0228 LUG LUG LUG LUG LUG LUG LUG LUG DUL DUL LUG LUG LUG LUG TUG LUG WHICH (TRACK NUMBERING IN A LATA VECTOR OVERLAY, WITH CCNSTRAINED DOF #S IN CORRECT BLOCK) 2*I - 1STAGE 2: SURROUNDING LUG AREA 2*I-1 NT8*NDF+1-NDM Ħ It $K = NDR^{\pm}(J-1) + 2 \pm I - 3$ = NDR* (J-1) +2*I-NR3P1, NR E 20 = K + N - 1+(1-[])+ = K + N =**1,NT8** = 2,ND9 . EQ. NT8) .EQ. NT8) 1,NT8 I, NRB I, NA = IMASTR+NET 3: LUG FCOT M+2 € # 8+2 M+3 3 + •) NI ⊷ ⊪ بر ۱۱ DO 10 J = 11 H K+NDR = I D + 1K+NDR = IP+1Ħ 11 H I -N+T) NI 1 11 10 H ŋ $\mathbf{I} = \mathbf{I} + \mathbf{8}$ = **L+8** 5 IN (L+5) IN (I+6) (1+5)(1+6)(++1) NI z [++] 2 IN (I+1) IN (L+7) 8 8 IN (LP) IN (LP) + C 5 D0 15 (C) NI œ WILL END (L) NI D0 1 11 IJ IN (0 D D а. Н LP IN NI NI 00 ЦP g 00 Ъ oq SIAGE E Ч 1 5 ω 2 -2 δ υυ υ

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| IN(L+3) = K+5+NDF | LUG | 0265 |
|---|-------------|-------|
| IN(L+4) = K+2+NDF | DUL | 0266 |
| IN(L+5) = K+3+NDF | LUG | 0267 |
| IN(L+6) = K+NDF | LUG | 0268 |
| IN(L+7) = K+1+NDR | T0 | 0269 |
| IF (LOC .NE. MAXLOC) GO TO 30CO | LUG | 0270 |
| C READJUST TOP EDGE DOF IF THE PCRK59 RECONNECTS WITH THE NUMBERING | LUG | 0271 |
| C START LINE | LUG | 0272 |
| IN(L+2) = 5 | LUG | 0273 |
| IN(L+3) = 6 | LUG | 0274 |
| IN(L+4) = 3 | LUG | 0275 |
| IN(L+5) = 4 | LUG | 0276 |
| IN(L+6) = 1 | LUG | 0277 |
| IN(L+7) = 2 | LUG | 0278 |
| 3000 CONTINUE | LUG | 0279 |
| C LAPPED NODE | LUG | 02.80 |
| IN(L+8) = K | LUG | 0281 |
| IN(L+9) = K+1 | LUG | 0282 |
| LAPX = IQ+K-1 | LUG | 0283 |
| LPPY = IQ+K | LUG | 02.84 |
| C MCVED NODE | LUG | 0285 |
| IN(L+1C) = K+2 | LUG | 0286 |
| IN(L+11) = K+3 | LUG | 0287 |
| MOVX = IQ+K+1 | LUG | 0285 |
| MOVY = IQ+R+2 | DU J | 0289 |
| $DO \ 2003 \ N = 1,6$ | T 00 | 0290 |
| 2003 IN (L+11+N) = K-1+N-NDR | LUG | 029 |
| IF (LOC .NE. 1) GO TO 2005 | DUL | 0292 |
| C SPECIAL CASE WHEN FCRK59 OVERLAYS NUMBERING START LINE | LUG | 0293 |
| LDUMY(1) = 2*NT8-1 | LUG | 029(|
| LDUMY(3) = 2*NT8 | LUG | 0295 |
| M = NDR*(NT8-1) + 1 | D0 T | 0296 |
| $DO \ 2004 \ N = 1,6$ | DUL | 0297 |
| 2004 IN(L+11+N) = M-1+N | LUG | 0298 |
| 2005 CONTINUE | DOT | 0295 |
| CALL ORK (LDATA, RE, IN) | DUL | 030(|

0313 0305 0309 0302 0303 0304 0306 0307 0308 0312 0314 0315 0316 0319 0320 0323 0326 0328 0329 0333 0301 0310 0311 0317 0318 0321 0322 0324 0325 0327 0330 0331 0332 0334 0335 0336 LUG LUG LUG LUG LUG DUL LUG DUL LUG DUT LUG LUG LUG LUG TUG LUG L UG DOT IUG LUG 1 UG FORCE/DISPLACEMENT VECTOR FOR + INTERPOLATION (THREE STAGES SIMILAR TO CCNNECTIONS) 17 СI О 00 .LT. NT6P1) (CIRCULAR ABC) ALGORITHM: OVERIAY IN OUTER EDGE -RL*TAN(THETA-0.5*PI) -RL*TAN (1.5*PI-THETA) = -RL*TAN (THETA-PI) = RL*TAN (PI-THETA) 18 6 GO TO 20 = RL*SIN (THETA) STAGE 2: SURROUNDING LUG, BY IF (J.GT. NT2F1 .AND. J = R*SIN (THETA) 60 TO RE (IQ+K) = RL * COS (THETA)(J .GT. NT4P1) GO TO FIRST AND FOURTH QUADRANTS = R*CCS (THETA) = NDR*(J-1)+2*(I-1) THETA = (J-1) * AINC(J-1) *AINC (LdEIN NT5E1) DO 16 I = 1, NRBP1 = -BLDC 16 J = 1, NT8DO 22 J = 1, NTE(RE-RI)/NRB RI = RI + (I - 1) * E-RL - B L COORDINATE CONVENIENCE 11 1: BUSHING K = J * NDR - 2QUADRANT (J . GT. RE (IQ+1+K) (J .GT. RE (IQ+K) =II RE (IQ+1+K) 11 RE (IQ+K) =THIRD QUADRANT RE (IQ+1+K) RE (IQ+1+K) RE (IQ+1+K) RE (IQ+1+K) RE (IQ+K) GO TO 21 TO 21 T0 21 GO TO 21 RE (IQ+K) RE (IQ+K) 0 THETA بط ۱۱ GLOBAL SECOND 09 ЧF 09 면 면 너 LATER SIAGE ₩ щ 16 17 61 20 18 υυ υ υ υ υ υ

0338 0339 0340 0343 0345 0337 0342 0344 0346 8460 0349 0355 0356 0358 0362 0363 0368 0341 0347 0350 0351 0352 0353 0354 0357 0359 0360 0361 0365 0366 0367 0369 0370 0371 0372 0364 L UG DUG LUG DUG LUG LUG LUG LUG LUG TUG TUG T UG LUG LUG LUG LUG LUG LUG LUG LUG IF (L . EQ. LDUMY (1) .OR. L . EQ. LDUMY (2) .OR. L . EQ. LDUMY (3) TO LAPPED NODE = RE (LAPX) +CSIZE*COS (CDIR+E) YTIP = RE(LAPY) +CSIZE*SIN (CDIE+E) SKIP DUMMY QUAD4 ELEMENTS IN OVERLAY (RE (IQ+1+K)-RE (IQ+1+L))/NRL IF (IANL .EC. 1) GO TO 2006 C CHANGE COORDINATES OF MOVED NCDE (RE (IQ+K) -RE (IQ+L))/NRL ANGLE TO CRACK; TIF COORDINATES GO TO 2007 REWIND 20 22 RE (IQ+1+L) = RE (IQ-1+L) + VRE (IQ+L) = RE (IQ+L-2) + E= RL - (I - 1) * VANGLE (LOC) = 180.*E/PICDIR = PI*CDIR/180.= - (RL+J*E) = NDR* (J-1) + 2*NRB RE (MOVX) = RE (IAFX) = RE(IAPY)DO 22 I = NRBP2, NR 1,NT2P1 IF (IANL . EQ. 1) $\mathbf{Z} = (\mathbf{LOC-1}) * \mathbf{AINC}$ IF (IANL . EQ. 1) 1, NM1 C GENERATION/ASSEMBLY T,NA DO 24 K = 1,183: LUG FOCT = NT8*NDF RE (IQ+K) = RE (IQ+1+K) DO 26 L = D0 23 J = Ħ INTERPOLATION = W/NT2• • = A/NA RE (MOVY) CONTINUE DO 23 I K = K+2L = L+2AITX H Q (K) 11 21 L STAGE × μ ⊳ ស្រា 23 2006 2# υ υ υ Q

0406 0407 0408 0405 0388 0389 0390 0392 0393 0394 0395 0396 0397 0398 0399 04 00 0401 0402 0403 0404 0385 0386 0382 0383 0384 0387 0391 0378 0380 0375 0376 0377 0379 0381 0373 0374 LUG LUG L UG LUG LUG LUG LUG LUG L UG DUL LUG LUG T UG LUG LUG LUG LUG LUG LUG 10G LUG LUG LUG LUG LUG LUG LUG C UG LUG LUG LUG LUG LUG LUG LUG CALL QUAD4 (EXY, T, TEMP, CL, U, NOD, ANG, Q, SM, B, L, KW) CALL QUAD4 (EXY, T, TEMP, CB, 0, NOD, ANG, Q, SM, B, L, KW) 288 (CLEVER!!) 0 E 0 U CALL PCRK59 (2,6, FTA, XTIP, YTIP, EXY, SM, BCR) COORDINATES . EQ. B, Ed 26 CALL ASMLTV (NET, 18, SM, Q, RE, IN) XTRACT (NET, 18, EXY, RE, IN) .AND. TENSN G GO TO 282 GO TO 2008 HRITE (20) CALL ASMLTV (L, 8, SN, Q, RE, IN) CALL XTRACT(L, 8, EXY, RE, IN) THUS RETRIEVING THE FROPER <u>6</u> RID OF NODAL CCORDINATES 2 . OR. L . EQ. LDUMY (4)) = E+0.25*EXY (2*N-1) $V = V + 0.25 \times EXY(2 \times N)$. • IF (IANL .EQ. 1) .LE. NETE) (IANL .EQ. 1) EXY(11) = EXY(8)= EXY(7).GT. NETE) DC 27 K = IQ, IQASSEMBLE THE PCRK59 = EXY(6)= EXY(5)EXY (4) $= \Xi X Y (3)$. EQ. . EQ. = 1,4 SHEAR -0 -H IF (SHEAR CONTINUE IF (SHEAR CONTINUE CONTINUE SHEAR IFLAG = DO 25 N 11 0 EXY (10) . 0 1 IJ 5 • • RE (K) EXY (8) EXY(7) EX I (4) EXY (5) CàLL **J**3 = J4 = A A A 1 F4 F-1 년 년 ΗL APPLY ы 5 ជា 2008 C GET 27 2007 26 25 • υ υ C

LUG LUG LUG LUG 288 GO TO IF (SHEAR) 280,282,281 IF (TENSN). 283,288,284 ••• 282 IF (TENSN .EQ. J3 = 0 AAA4 = -TENSN= SHEAR PCSITIVE TENSION AAA2 = TENSN NEGATIVE TENSICN NT4P1 POSITIVE SHEAR NEGATIVE SHEAR = NT4P1 J1 = NT2P1NT6P1 •0• = NT6P1 • GC TO 285 GO TO 285 APPLY TENSION IFLAG = 0் GO TO 285 2 = NT8 ۲ ا AAA3= 0. NT8 283 NSEG = 1 li Ħ IJ J4 = 0 11 AAA3 11 - LC AAA4 H J1 = NSEG . 1 = L AAA2 280 NSEG AAA1 281 NSEG IJ H **1**3 Jt 32 32 **J**2 **J**2 33 284 υ υ υ υ C

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0445 0446 0447 0448 0449 0450 0452 0453 0454 0455 0456 0458 0459 0462 0463 0464 0465 0456 0468 0469 0470 9472 0451 0457 0460 0461 0467 0473 0475 0476 0478 0471 0474 0477 0479 0480 LUG LUG LUG LUG LUG DU T LUG LUG LUG LUG LUG LUG LUG DU J LUG LUG L UG LUG **DUL** L UG LUG = RE (KX+1) +AAA3*SCALE (IP1, LCAD) +AA44*SCALE (I, LOAD) RE (KX) + AAA 1* SCALE (I, LOAD) + AAA2* SCALE (IP1, LOAD) CRACK OPENING ΤV (POSITIVE-DEFINITE MATRIX) APPLY HALF OF LCAD AT EACH NODE 2009 (KW,607) ICASE, TITLE GO IO 282 IF (IANL .EQ. 1) GO TO 289 29 \circ = C.5*RE(LAPY)0 H = 0.5 * RE (LAPX)GO TO Ħ = IQ + NDR* (ILINE-1)CALL FACT (ISGN, RE, IN) 1, NSEG KT1 = JI, JU 000 CALL SIMULQ (E, RE, IN) = RE (MOVX) = RE (MOVY) F 5 IF (ISGN . EQ. 1) 289 CALL BCCN (RE, IN) LOADING IS COMPLETE 1,NET H (IANL .EQ. WRITE (KW, 606) . EQ. IF (IANL . EQ. 286 ILINE 287 ISEG STRESS SOLUTION = NT2P1 1) 1 IP1 = I+1REWIND 20 IF (IFLAG GC TO 32. RE (KX) = င ၂၂ RE (MOVX) CONTINUE RE (KX+1) RE (MOVY) = J4 RE (LAPX) RE (LAPY) = 1 = J2 = I+2 = J3 1 HRITE D0 31 SCLUTION ISGN od XX JL ŋŋ 머머 0 G 1 U T JL UU н н 288 285 286 287 29 υ υ C υ

0482 0483 0489 0493 0508 0481 0484 0485 0486 0487 0488 06 10 0492 0494 0495 0496 0498 0499 0503 0504 0505 0506 0509 0491 0497 0500 0502 0507 0510 0501 0511 0512 0513 0514 LUG L UG LUG DUL LUG (LOC, ANGLE (LOC), JNE (LCC), TWO (LOC) C CCNVERT TO NASA/ASTM STANDARD STRESS INTENSITIES = SC* (SXY (2) -SXY (1)) + (CSQ-SSQ) *SXY (3) = SXY (1) *CSQ+SXY (2) *SSQ+2, *SXY (3) *SC SXY (1) *SSQ+SXY (2) *CSQ-2.*SXY (3) *SC IF (L . EQ. NETEF1) WRITE (KW. 608) = TRO(LOC) + BCR(2, J) + Q(J)= CNE (LOC) +BCR (1, J) *Q (J) (KW,609) L, E, V, SXY, SRT = ABS (SQPI*TWO (LOC)) WRITE (KW, 610) ICASE, TITLE = SXY(I)+B(I,J)*Q(J) CALL XTRACT (NET, 18, Q, RE, IN) IF (IANL .EQ. 1) GO TO 32 = SQPI*GNE (LOC) CALL XTRACT (L,8, Q, RE, IN) C SIRESS INTENSITY SCLUTICN DO 2010 J = 1,18 OF LOCATICN LOCP 2 LOC = 1, MAXLCC(20) E, E, WRITE (KW,611) 8 H = E + 2 + 2 + 2 + 2CSQ = E * E/HH/v*v = 022DO 30 J = 1SC = E * V/Hłį GO TO 2011 IJ H CONTINUE ONE (TOC) TWO (LOC) ONE (LOC) TWO (LOC) CONTINUE END OF CASE DO 30 I SXY(I) SRT (2) SRT (3) WRITE SXY (I) SRT (1) READ STCP END 2010 2009 000 1 25 C END 2011 υ

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