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RELIABILITY OF STEP-LAP BONDED JOINTS

E. B. Birchfield, et al

McDonnell Aircraft Company

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20.

elastic-plastic analysis procedure. The static strength, residual strength and lifetime data were assumed to be from Weibull distributions. The shape and scale parameters for each of these distributions were calculated using the best linear unbiased (BLU) estimation procedure. Using these procedures wearout models were calibrated and checked, and conclusions concerning scaling, and translation of parameters were drawn.

Tests were also conducted to determine the effect upon lifetime of load truncation, load frequency, relaxation time between missions, and temperature.

FOREWORD

This report was prepared by McDonnell Aircraft Company, St. Louis, Missouri, 63166 under USAF Contract Number F33615-74-C-3015, Project Number 4364, and Task Number 13680126. The objective of the program was to improve the technology base of data and methods applicable to the rational and efficient design of graphite-epoxy-to-titanium- step-lap bonded airframe joints that are optimized for reliability under military flight loading. The program was administered under the direction of the Air Force Flight Dynamics Laboratory by Mr. R. T. Achard, Project Engineer (AFFDL/FBS).

The program was conducted by the Structural Research Department at MCAIR, and was managed by A. J. Breining, with E. B. Birchfield as principal investigator. Major contributors to the program were Mr. L. F. Impellizzeri, Dr. R. T. Cole, and Dr. J. Hart-Smith (Douglas Aircraft Company).

This report covers the entire program contract period from January 1974 to April 1975. This report was released by the authors in April 1975.

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LIST OF SYMBOLS

A	- Area (in^2)
A_2	- $\beta_s^{2(r-1)} / (r-1) \beta_f$
$A(N,M,I)$	- Weight for estimating scale parameters
a	- $[1 - (N_o/N_p)^2]$
b	- $a/(N_o/N_p)$
$C(N,M,I)$	- Weight for estimating shape parameters
E	- Elastic modulus (psi)
E_c	- Effective tensile modulus of adhesive (psi)
$E(\text{CP})$	- Expected cross product
$E(\text{LB})$	- Expected loss for estimate of shape parameter
F	- Strength (lbs) or (lbs/in)
F^{ty}	- Tensile yield stress (psi)
F_R	- Residual strength (lbs/in)
F_S	- Static strength (lbs) or (lbs/in)
f	- Frequency (cycles)
G	- Elastic shear modulus of adhesive (psi)
$G(f)$	- Power Spectral Density
L	- Length (in)
l	- Bond Length (in)
N_o	- Total number of zero crossings per unit time with positive slope
N_p	- Total number of peaks per unit time
N_X	- Cumulative peak exceedance
N_z	- Maneuver load factor
P	- Axial load (lbs)
$P(x/a\sigma)$	- Probability of exceeding $x/a\sigma$ determined from a standard Gaussian or normal probability table

LIST OF SYMBOLS (CONTD)

$R(\tau)$	- Autocorrelation function
r	- $\alpha_s/2\alpha_f + 1$
T	- Temperature ($^{\circ}F$); lifetimes
t	- Thickness (in)
W	- Width (in)
$X(t)$	- Load at time, T (lbs) or (lbs/in)
α	- Thermal coefficient of expansion ($^{\circ}F^{-1}$)
α_f	- Weibull shape parameter for fatigue life distribution
$\alpha_R(T)$	- Weibull shape parameter for residual strength distribution at time, T
α_s	- Weibull shape parameter for static strength distribution
β_f	- Weibull scale parameter for fatigue life distribution (lifetimes)
β_s	- Weibull scale parameter for static strength distribution (lbs/in)
$\beta_R(T)$	- Weibull scale parameter for residual strength distribution at time, T (lbs/in)
γ	- Variance of a population
γ_e	- Elastic shear strain (in/in)
γ_p	- Plastic shear strain (in/in)
λ	- $\sqrt{2G/Et\eta}$ (in^{-1})
η	- Bondline thickness (in)
σ	- Root mean square (RMS) of $X(t)$
σ_p	- Peel stress (psi)
τ_p	- Plastic shear stress (psi)
$()_o$	- Designates outer adherend
$()_i$	- Designates inner adherend

SECTION 1

INTRODUCTION

Joining of composite structural elements to metals or other composites is one of the most troublesome aspects of advanced composite airframe design. In theory, adhesive bonding is a most efficient approach. Although adhesive bonding eliminates many of the problems associated with stress concentrations at point attachments (such as found in conventional mechanical joints), this type of joint is subject to stress concentrations near the edge of the bond. Furthermore, a variety of failure modes are possible in the bond and adherend areas of a laminated joint. The problem of adhesive joint design is compounded for fatigue-critical applications, especially for primary-load-carrying structures where heavy overdesigned composite concepts may be employed, or where the application of composites may be rejected altogether for lack of confidence in bonded joint behavior. The ultimate goal for the technology generated under this program was practical application to improvements in the structural integrity and cost effectiveness of Air Force aircraft.

1.1 Objectives

The general objective of this program was an improved technology base of data and methods applicable to the rational and efficient design of graphite-epoxy-to-titanium step-lap-bonded airframe joints that are optimized for reliability under military flight loading. Specific objectives of the program were:

- o Development of a controlled, statistically significant base of empirical data on strength and fatigue life of graphite-epoxy composite to titanium step-lap bonded joints.
- o Demonstration of analytical methodology for designing step-lap bonded joints.
- o Development of an analytical wearout model for step-lap bonded joints (statistical distribution of static and residual strengths, and time to failure) subjected to flight-by-flight random stress history.
- o Correlation of the effects of scale-up on joint design, and definition of the non-dimensional parameters affecting scale-up.
- o Determination of the effects of test variables on time to failure (test load frequencies, relaxation times, load truncation, and temperature effects).

1.2 Scope

This program was built around a conceptual structural application representative of a highly loaded aircraft structural joint. The specific application is the kick splice plate from the F-15 low cost production composite wing (Figures 1 and 2). This joint introduces loads from the lower wing skin to fuselage frame attachments. The purpose of the conceptual application was to realistically define an end item towards which this study is directed, and to provide a point of departure from which load intensities, loading spectra, environment, and scale designs for specimens could be derived.

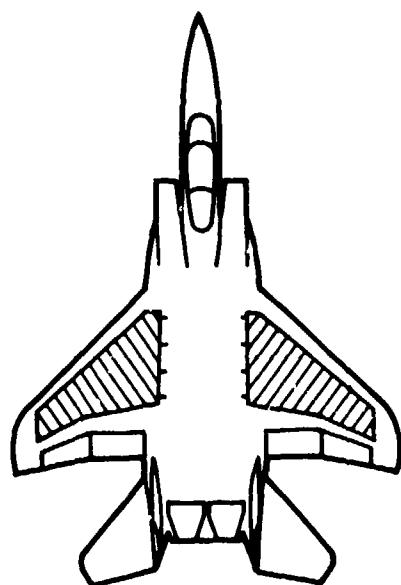
The program was conducted in two phases. Early in Phase I a specimen verification task was conducted to select the most cost effective specimen design to establish the data base and to demonstrate that the specimens would give the desired data. This task was run using the F-15 wing root bending moment semi-random spectrum. After evaluating eleven different specimen configurations, designs for 25% scale simple double lap, 70% scale step-lap, and full scale step-lap joints were selected to establish the reliability data base. Simultaneously, a random spectrum for the F-15 wing root bending moment was developed. This spectrum was subsequently used in all repeated load tests to establish the data base for defining lifetime and residual strength characteristics. The static strengths of the tested specimens were compared with the predictions of the elastic-plastic analysis. The static strength, residual strength and lifetime data were assumed to be from Weibull distributions. The shape and scale parameters for each of these distributions were calculated using the best linear unbiased (BLU) estimation procedure. Using these parameters, the wearout models were calibrated and checked, and conclusions concerning scaling, and translation of parameters were drawn.

In Phase II, tests were conducted to determine the effect upon lifetime of load truncation, load frequency, relaxation time between missions, and temperature.

In this program, a total of 278 specimens in addition to those required for specimen design verification were fabricated. Of these, one hundred and eighty-eight were tested to provide the empirical data base. Ninety specimens were delivered for testing by the Air Force. Specimens evaluated in this program to establish the reliability data base are shown in Table 1.



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FIGURE 1 F-15 HIGH PERFORMANCE FIGHTER

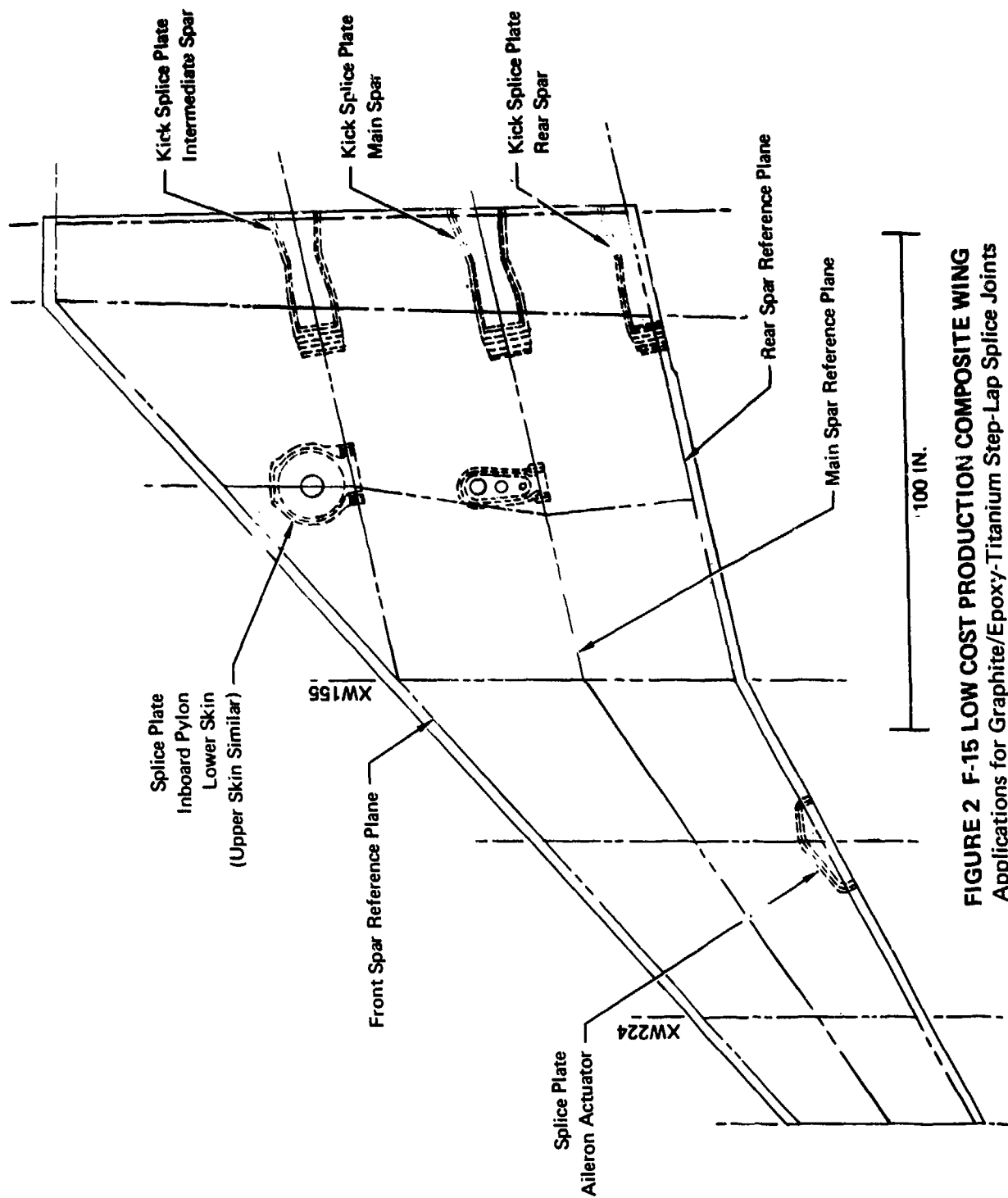


FIGURE 2 F-15 LOW COST PRODUCTION COMPOSITE WING
Applications for Graphite/Epoxy-Titanium Step-Lap Splice Joints

TABLE 1 SPECIMEN PLAN FOR THE RELIABILITY DATA BASE

Description of Testing		No. of Simple Joints	No. of Small Step-Lap Joints	No. of Full Scale Step-Lap Joints	Random Spectrum Identification No.
P H A S E I	Static	8	10	10	
	Residual (2 Life Times)	—	10	10	1
	Residual (3 Life Times)	10	10	10	1
	Fatigue (Run-Out) or 6 Life Times	10	40	30	1
	USAF Testing	60	30		
Total Phase I Specimens		88	100	60	
Total Phase I Tests		28	70	60	
P H A S E II	Frequency Effects	—	—	6	3
	Relaxation	—	—	6	4
	Truncation	—	—	6	2
	Temperature	—	—	12	1
	Total Phase II	—	—	30	
TOTAL PROGRAM Specimens		88	100	90	
TOTAL PROGRAM Tests		28	70	90	

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SECTION 2

SPECIMEN SELECTION, DESIGN AND ANALYSIS

Three specimen types were selected for testing in this program in order to provide an improved technology data base and methodology applicable to the efficient design of graphite-epoxy-to-titanium step-lap bonded joints. The kick splice plate for the F-15 low cost production composite wing (Figure 3) was selected as the basic conceptual structural application around which the program is built. One of the principal reasons for this selection was that the joint is representative of a USAF high performance aircraft primary load carrying joint and its basic design characteristics and requirements are well-defined. Specimen designs selected for testing in this program are: (1) simple double lap joints, (2) small scale step-lap joints, and (3) full scale step-lap joints. The requirements placed on the specimens are derived from the conceptual structural application and are discussed in paragraph 2.1. The methodology used in the design and analysis of these specimens is detailed in paragraph 2.2. At the start of the program a specimen verification task was conducted to verify that the specimens would yield representative data. The specimen verification task and the selection of the specimen design to establish the data base for the remainder of the program are discussed in paragraph 2.3 and the analysis of these specimens is presented in paragraph 2.4.

2.1 Requirements

The requirements placed on the specimens are derived from the F-15 low cost production wing kick splice, the conceptual structural application. This structural application is an internal MCAIR conceptual study. An additional objective was to achieve bondline failures rather than laminate failures. The layup of the graphite-epoxy in the splice through a section along the spar is a balanced laminate (36.4% $\pm 45^\circ$, 54.5% 0° , 9.1% 90°). The ultimate static strength of the splice must be greater than or equal to 15,000 lb/in. Design limit load (DLL) for the splice is 10,000 lb/in. The endurance must be greater than or equal to 4 lifetimes (16,000 flight hours). With the above considerations in mind, the specimens were designed to meet the following objectives:

Simple Double-Lap Joints

- o Must fail in bondline
- o Must be stiffness balanced with adherends scaled from full scale step-laps

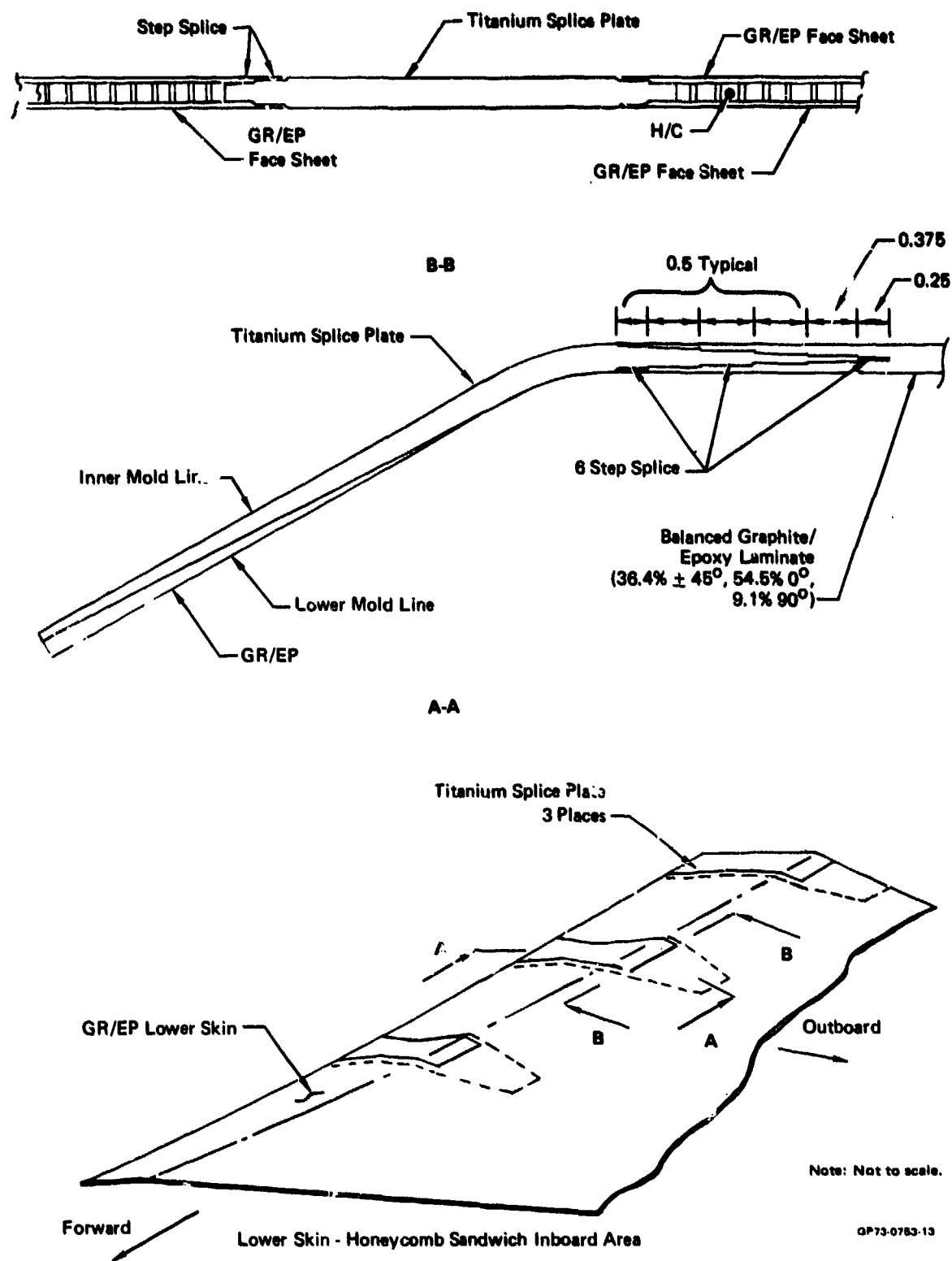


FIGURE 3
F-15 LOW COST PRODUCTION COMPOSITE WING CONCEPTUAL JOINT APPLICATION

- o Must have full scale bondline

Small Scale Step-Lap Joints

- o Must have the same number of steps as the full scale step-lap joints
- o Must have the same laminate layup percentagewise on each step as the full scale step-lap joints (limited by need to have integral numbers of plies).
- o Must have scaled thickness on each step (limited by need to have integral numbers of plies).
- o Must have scaled lap length.
- o Must have scaled adhesive system.

Full Scale Step-Lap Joints

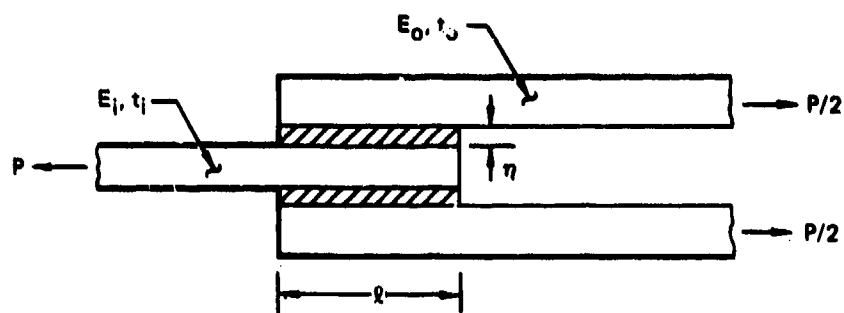
- o Must have same layup (36.4% $\pm 45^\circ$, 54.5% 0° , 9.1% 90°) as F-15 lower skin at splice
- o Must fail in bondline
- o Must have a static strength greater than : equal to 15,000 lbs/in
- o Must have an endurance greater than or equal to 4 lifetimes under the F-15 wing root bending moment random spectrum (developed in this program) with DLL greater than or equal to 10,000 lbs/in.

2.2 Analytical Methods

Two analytical methods guided design of the test specimens. The analysis approach for static strength design is described in paragraph 2.2.1 below. The analyses to assure that joint designs meet lifetime requirements is described in paragraph 2.2.2.

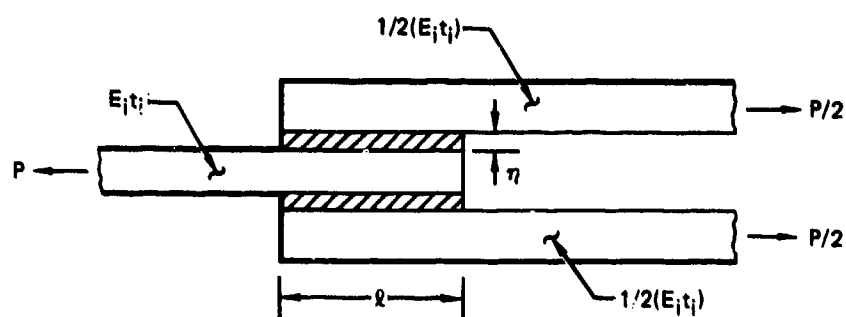
2.2.1 Static Strength Design - The procedure used to design joints for static strength is based on the elastic-plastic analysis of Reference 1-6. This procedure, as it applies first to double lap joints and then to step-lap joints, is described in the paragraphs which follow. The impact of this analysis on scaling adhesive bonded joints is discussed.

2.2.1.1 Double Lap Joint - A typical double lap joint is illustrated in Figure 4. To analyze this joint, it is first stiffness balanced with $E_1 t_1$ held constant (see Figure 5). The strength of the balanced joint is then determined from Figure 6, where λ is given by equation (1)



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FIGURE 4 TYPICAL DOUBLE LAP JOINT



GP74-1037-17

FIGURE 5 STIFFNESS BALANCED ($E_i t_i$ CONSTANT) DOUBLE LAP JOINT

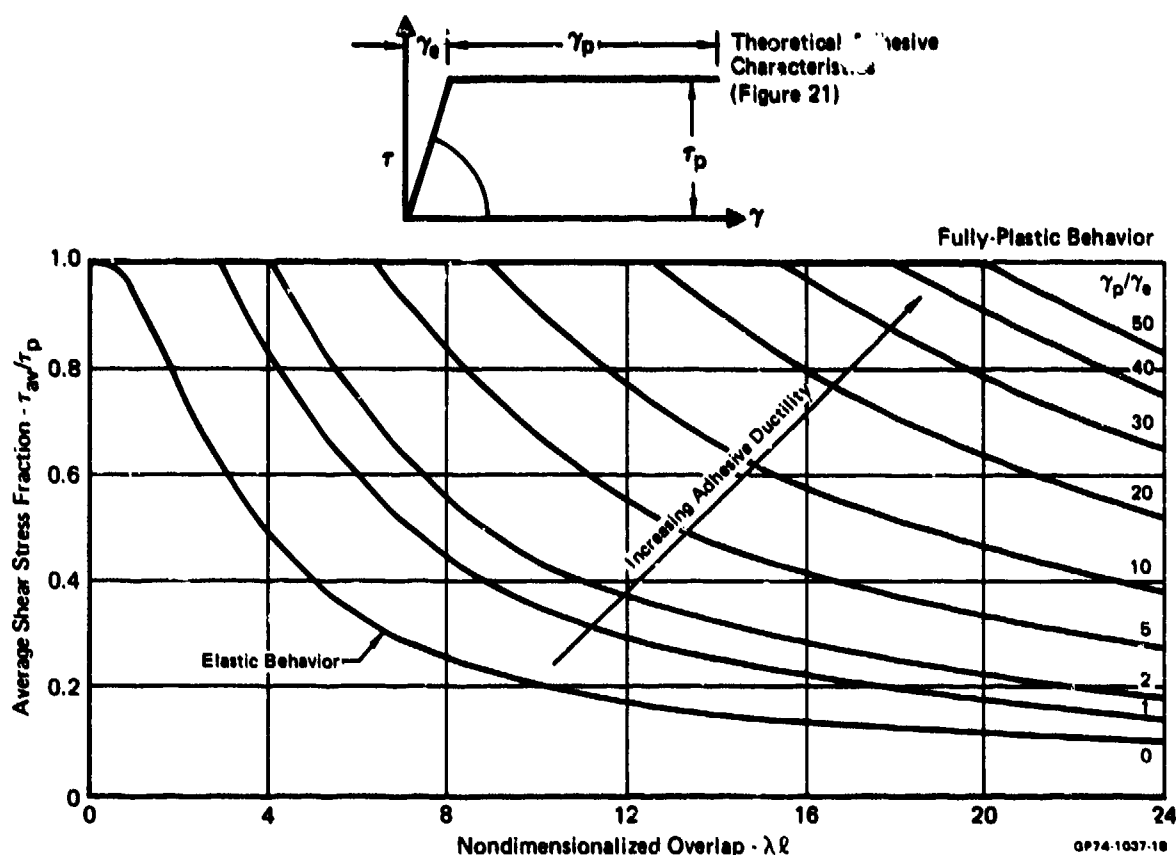


FIGURE 6 AVERAGE SHEAR STRESSES IN DOUBLE-LAP ADHESIVE BONDS

$$\lambda = \sqrt{2G/Et\eta} \quad (1)$$

where G is the adhesive shear modulus and η is the bondline thickness. Figure 7 is used to correct for the stiffness imbalance. Figure 8 is used to correct for thermal imbalance. The maximum peel stress in the adhesive is given by equation (2).

$$\sigma_p = \tau_p \frac{3E'_c(1 - \mu^2)t_o}{E_o\eta}^{1/4} \quad (2)$$

where E'_c is the "effective" tensile modulus of the adhesive

$$\frac{1}{E'_c} = \frac{1}{E_c} + \frac{k_1}{E_{in}} + \frac{k_2}{E_{on}}$$

E_{in} and E_{on} are the transverse tensile moduli of the inner and outer adherends respectively. The constants k_1 and k_2 refer to the number (or fraction) of adhesive layer thicknesses for which the adherends are affected by the peel stresses. These equations are derived in Reference 2.

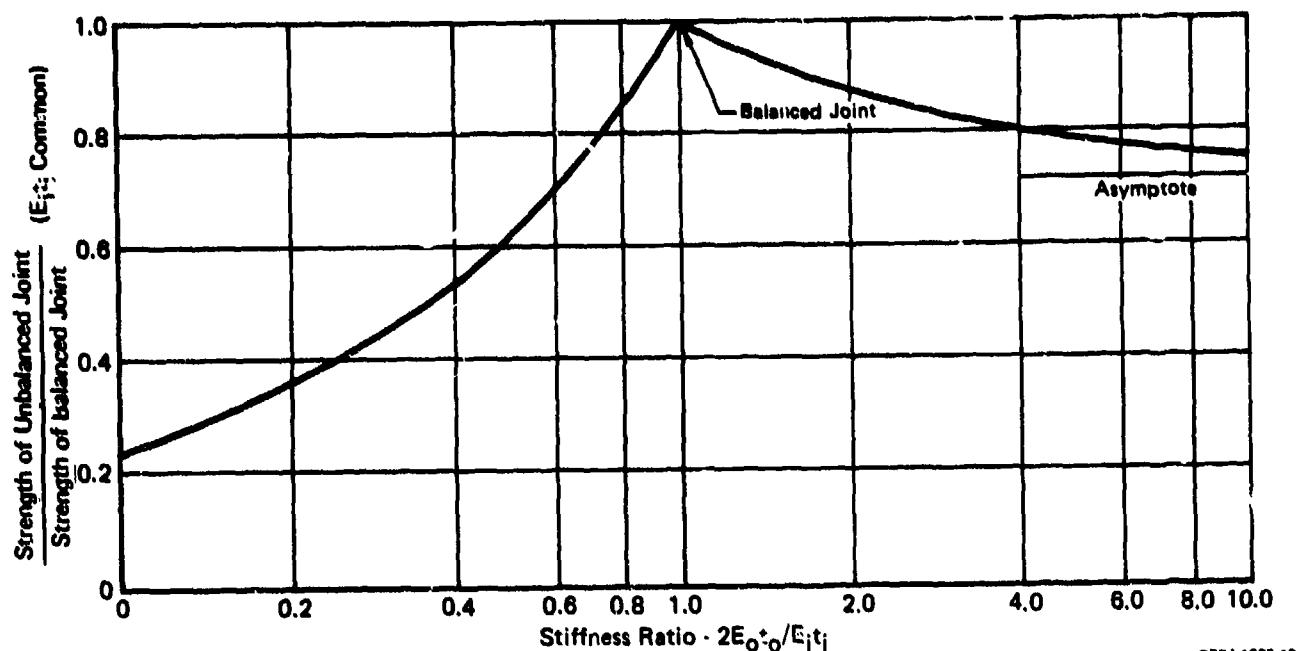


FIGURE 7 STRENGTH REDUCTION IN BONDED JOINTS DUE TO ADHEREND STIFFNESS IMBALANCE

2.2.1.2 Step-Lap Joints - The procedure used to design step-lap joints is outlined below:

- o Adherends - the adherend thickness and the laminate layup are determined from strength requirements
- o Number of Steps - initially determined by dividing the total number of plies by 8 and rounding off to next highest whole number
- o Stacking Sequence - a zero degree ply is placed on the face of each step; the plies are interspersed to avoid adverse stacking effects
- o Length of Bondline - assume that the joint is scarfed; the length of a scarfed joint required to carry a load P is given by equation (3)

$$l = P/\tau_p [E_2t_2/E_1t_1] \quad (3)$$

where

$$E_2t_2 > E_1t_1$$

- o Length of Each Step - select the length of the tang (the thinnest titanium step) so that it would not yield if the adhesive on it was totally plastic, thus its length is given by equation (4)

$$l = tF^{ty}/2\tau_p \quad (4)$$

(machining tolerances require that the thickness of the tang exceed 0.021 inch).

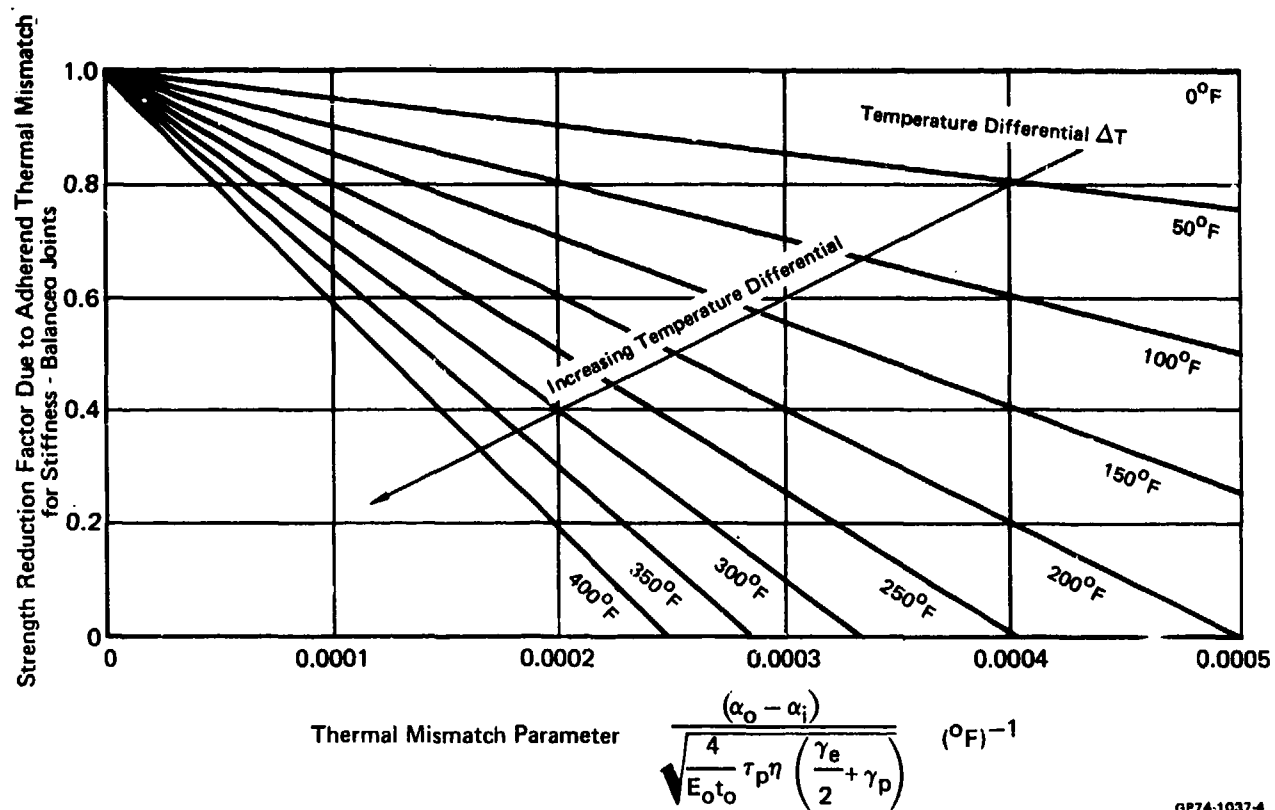


FIGURE 8 STRENGTH REDUCTION FACTOR IN DOUBLE-LAP BONDED JOINTS, DUE TO ADHEREND THERMAL MISMATCH

- o Optimization - iterative changes to joint dimensions to maximize joint strength) - (computer program A4EGX described in Appendix A may be used to perform required computations).

2.2.1.3 Scaling Joints - To scale a structural element it is first necessary to recognize the nondimensional parameters which control the stresses in the element. If these parameters are held constant while the characteristic physical dimensions are scaled the failure load will also be scaled. In Reference 14 the nondimensional parameters which control the bondline shear and normal stresses and the adherend axial stresses are shown to be:

$$E_o t_o / E_i t_i, \quad \gamma_p / \gamma_e, \quad \text{and} \quad l \sqrt{G / \eta E_o t_o}$$

and $\Delta \alpha \Delta T E_o t_o / \tau_p \eta, \quad E'_c (1 - \nu^2) t_o / E_o \eta$

(on each step).

Upon examination of these parameters it can be seen that the proper scaling parameters for step-lap joints are l , t_i , t_o and η . The same materials and the same percentage layups must also be used. In practice, such scaling cannot be exact because: (a) tolerances make it difficult to produce actually scaled bond lengths; (b) materials usually have a fixed per-ply thickness; (c) actual values of bondline thickness are hard to determine and control because of adhesive migration into the composite resin. Bondline thickness is probably a direct function of the adhesive carrier thickness which is normally made with minimum thickness material. An additional uncertainty is associated with the requirement that all adhesive properties remain constant when the bondline thickness is varied.

2.2.2 Lifetime Analysis - The Air Force anticipates incorporating into the Advanced Structural Integrity Program a definite approach for verifying the damage tolerance of safety of flight structure fabricated from advanced composite materials. An analytical as well as an experimental qualification for lifetime will be required. Previous analysis methods for metal structures included the use of Miner's rule in conjunction with a massive amount of data, including smooth S-N curves over a range of stress ratios, stable cyclic stress strain curves, and a notch analysis.

Aircraft which are now in the conceptual stage are showing a considerable usage of advanced composite materials and adhesive bonded jointing. The problem of providing the analytical qualification for these aircraft will be complicated primarily because the required data base is not available and because the cost of generating such a base would be astronomical especially considering the tailorability of composite materials.

To provide an adequate data base at minimum cost, a wearout model (probability statement for residual strength as a function of lifetimes under a fixed spectrum and load level) presented in equation (5), derived in Reference 8, and summarized in Appendix B was used:

$$P[F(t) > F] = \exp - \left[\frac{F^{2(r-1)} + A_4(r-1)t}{\beta_s^{2(r-1)}} \right]^{\alpha_f} \quad (5)$$

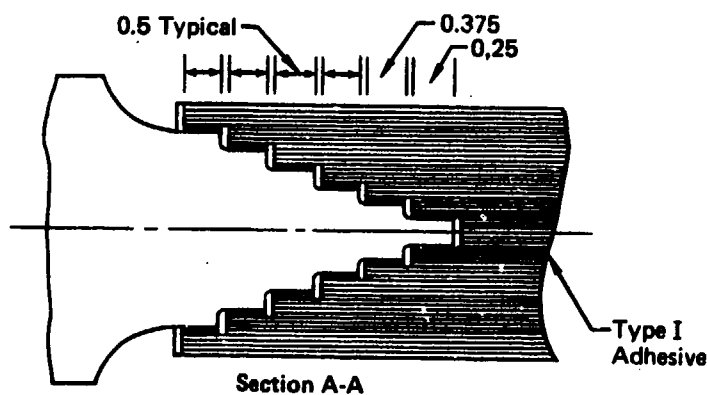
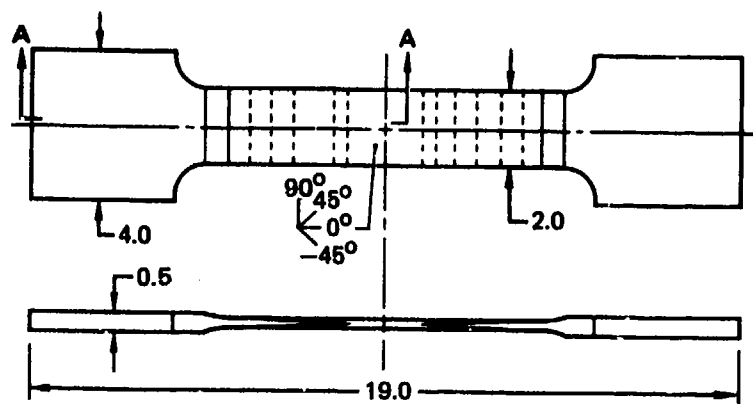
where

- α_s = static shape parameter
- β_s = static scale parameter
- α_f = fatigue shape parameter
- β_f = fatigue scale parameter
- $\alpha_f = \alpha_s / 2(r-1)$
- $\beta_f = \beta_s^{2(r-1)} / A_4(r-1)$

To calibrate this model, it was necessary to perform static strength and lifetime tests under a spectrum loading, to assume a Weibull distribution for these variables, and to estimate the parameters of the distributions for the element of interest.

2.3 Verification and Selection of Specimen Design for Reliability Data Base

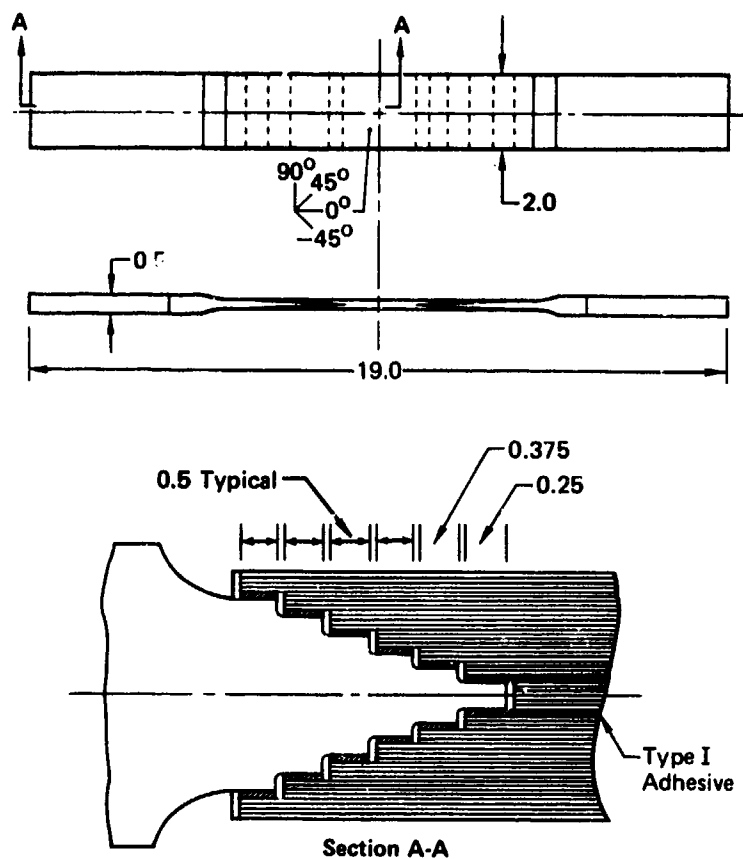
At the start of the program a specimen verification task was conducted to assure specimens would yield representative data. In this task, eleven different specimens (Figure 9 thru Figure 20) were designed. All but the specimens of Figures 12 and 20 were fabricated, and tested. The test results are listed in Tables 2 and 3. For the lifetime tests for the verification task the F-15 wing root bending moment semi-random spectrum was used, since it was the most representative spectrum available at the time. A random spectrum was developed and used for the remaining tasks. Based on



Ply No.	Oreinta-tion	Ply No.	Orienta-tion
1	45°	26	45°
2	0°	27	-45°
3	-45°	28	45°
4	0°	29	0°
5	45°	30	-45°
6	0°	31	0°
7	-45°	32	0°
8	0°	33	45°
9	90°	34	0°
10	0°	35	0°
11	45°	36	-45°
12	0°	37	0°
13	90°	38	90°
14	0°	39	0°
15	-45°	40	45°
16	0°	41	0°
17	0°	42	90°
18	45°	43	0°
19	0°	44	-45°
20	0°	45	0°
21	-45°	46	45°
22	0°	47	0°
23	45°	48	-45°
24	-45°	49	0°
25	45°	50	45°

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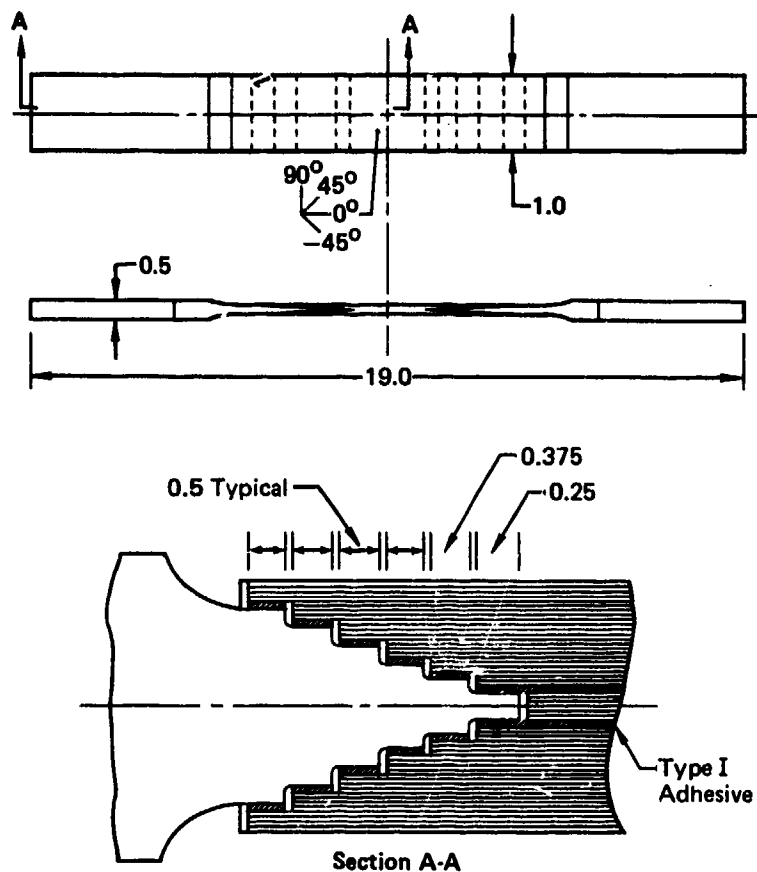
FIGURE 9 FULL SCALE, STEP-LAP SPECIMEN TWO INCHES WIDE, DOG BONED GRIPS



Ply No.	Orien-tation	Ply No.	Orien-tation
1	45°	26	45°
2	0°	27	-45°
3	-45°	28	45°
4	0°	29	0°
5	45°	30	-45°
6	0°	31	0°
7	-45°	32	0°
8	0°	33	45°
9	90°	34	0°
10	0°	35	0°
11	45°	36	-45°
12	0°	37	0°
13	90°	38	90°
14	0°	39	0°
15	-45°	40	45°
16	0°	41	0°
17	0°	42	90°
18	45°	43	0°
19	0°	44	-45°
20	0°	45	0°
21	-45°	46	45°
22	0°	47	0°
23	45°	48	-45°
24	-45°	49	0°
25	45°	50	45°

**FIGURE 10 FULL SCALE, STEP LAP SPECIMEN
TWO INCHES WIDE, CONSTANT WIDTH**

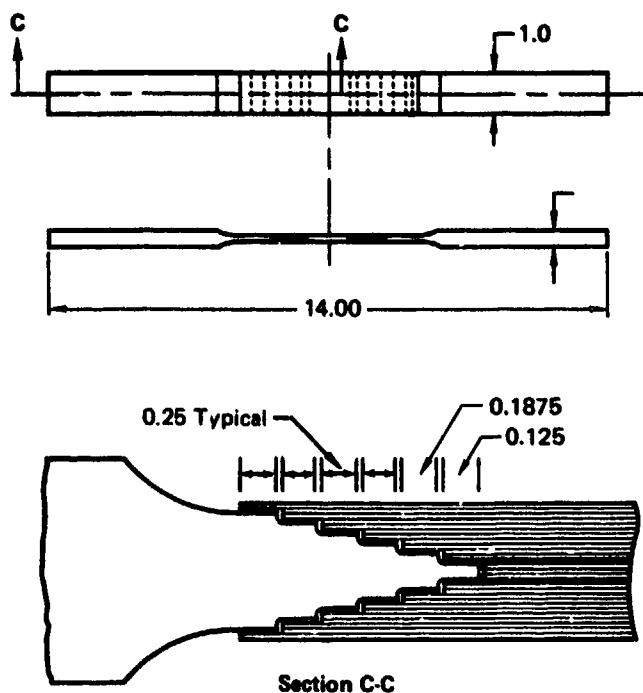
GP74-1037-6



Ply No.	Orienta- tion	Ply No.	Orienta- tion
	45°	26	45°
2	0°	27	-45°
3	-45°	28	45°
4	0°	29	0°
5	45°	30	-45°
6	0°	31	0°
7	-45°	32	0°
8	0°	33	45°
9	90°	34	0°
10	0°	35	0°
11	45°	36	-45°
12	0°	37	0°
13	90°	38	90°
14	0°	39	0°
15	-45°	40	45°
16	0°	41	0°
17	0°	42	90°
18	45°	43	0°
19	0°	44	-45°
20	0°	45	0°
21	-45°	46	45°
22	0°	47	0°
23	45°	48	-45°
24	-45°	49	0°
25	45°	50	45°

FIGURE 11 FULL SCALE STEP-LAP SPECIMEN; CONSTANT WIDTH

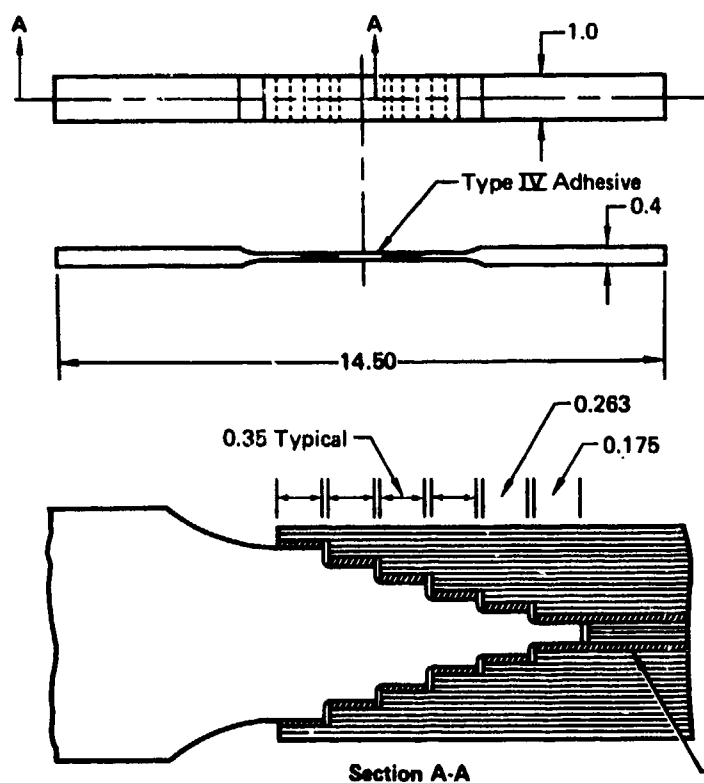
GP74-1037-7



Ply No.	Orien-tation	Ply No.	Orien-tation
1	0°	14	-45°
2	45°	15	0°
3	0°	16	-45°
4	-45°	17	0°
5	0°	18	45°
6	90°	19	0°
7	0°	20	90°
8	45°	21	0°
9	0°	22	-45°
10	-45°	23	0°
11	0°	24	45°
12	45°	25	0°
13	90°		

GP74-1037-8

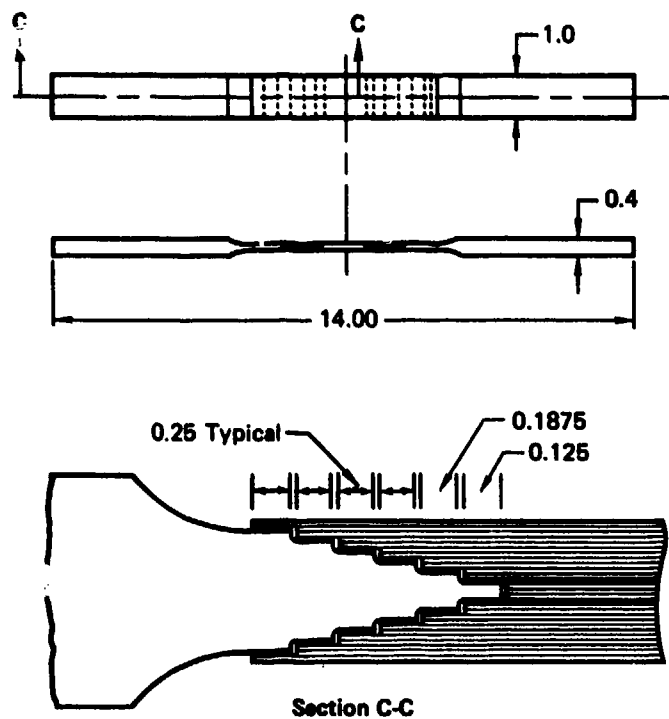
FIGURE 12 50% SCALE, STEP-LAP SPECIMEN, 50% SCALE ADHESIVE



Ply No.	Orien-tation	Ply No.	Orien-tation
1	45°	18	-45°
2	0°	19	45°
3	-45°	20	0°
4	0°	21	-45°
5	0°	22	0°
6	45°	23	45°
7	90°	24	0°
8	0°	25	0°
9	-45°	26	-45°
10	0°	27	0°
11	0°	28	90°
12	45°	29	45°
13	0°	30	0°
14	-45°	31	0°
15	0°	32	-45°
16	45°	33	0°
17	-45°	34	45°

GP74-1037-8

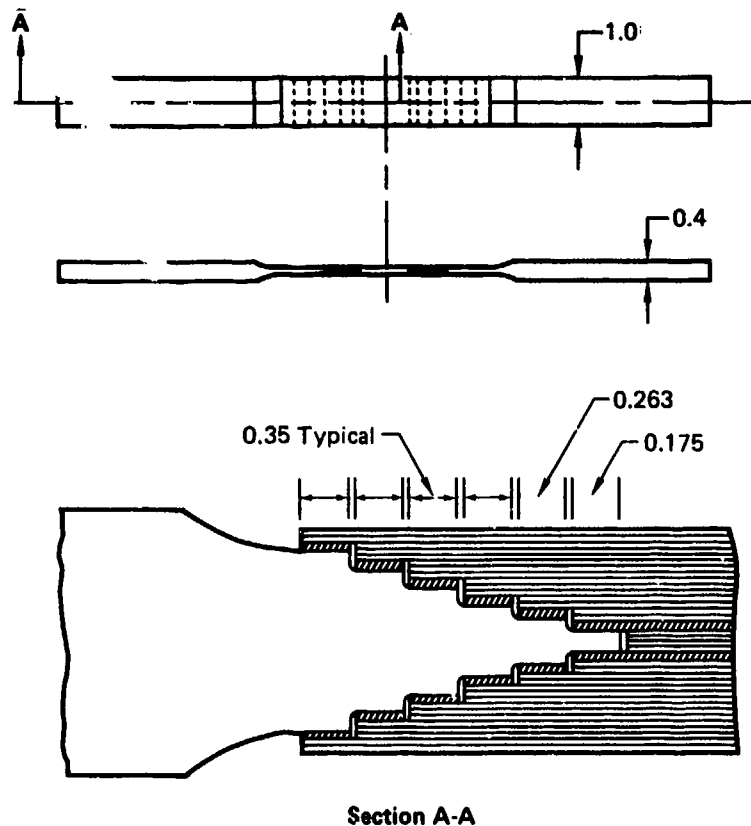
FIGURE 13 70% SCALE STEP-LAP SPECIMEN, 70% ADHESIVE



Ply No.	Orien-tation	Ply No.	Orien-tation
1	0°	14	-45°
2	45°	15	0°
3	0°	16	-45°
4	-45°	17	0°
5	0°	18	45°
6	90°	19	0°
7	0°	20	90°
8	45°	21	0°
9	0°	22	-45°
10	-45°	23	0°
11	0°	24	45°
12	45°	25	0°
13	90°		

GP74-1037-10

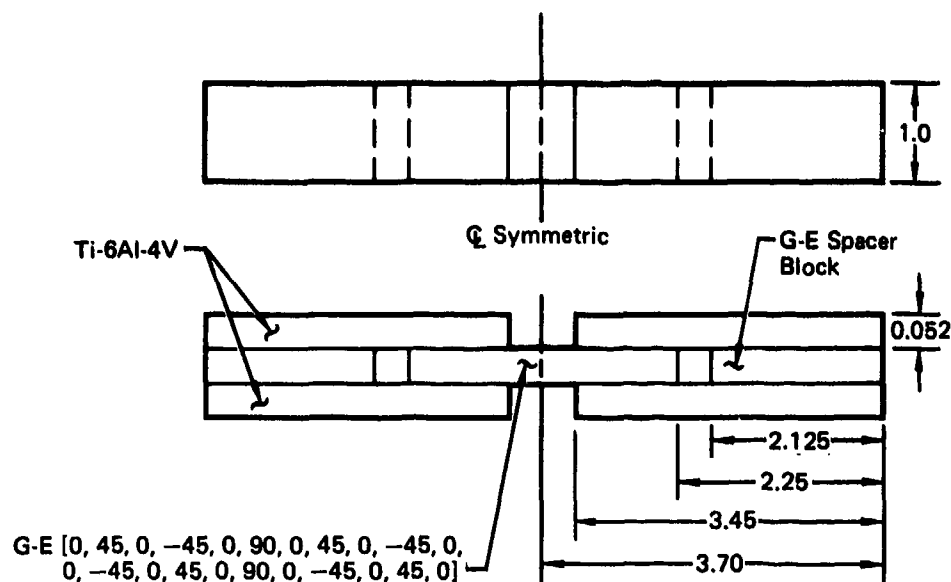
FIGURE 14 50% SCALE, STEP-LAP SPECIMEN, FULL SCALE ADHESIVE



Ply No.	Orien-tation	Ply No.	Orien-tation
1	45°	18	-45°
2	0°	19	45°
3	-45°	20	0°
4	0°	21	-45°
5	0°	22	0°
6	45°	23	45°
7	90°	24	0°
8	0°	25	0°
9	-45°	26	-45°
10	0°	27	0°
11	0°	28	90°
12	45°	29	45°
13	0°	30	0°
14	-45°	31	0°
15	0°	32	-45°
16	45°	33	0°
17	-45°	34	45°

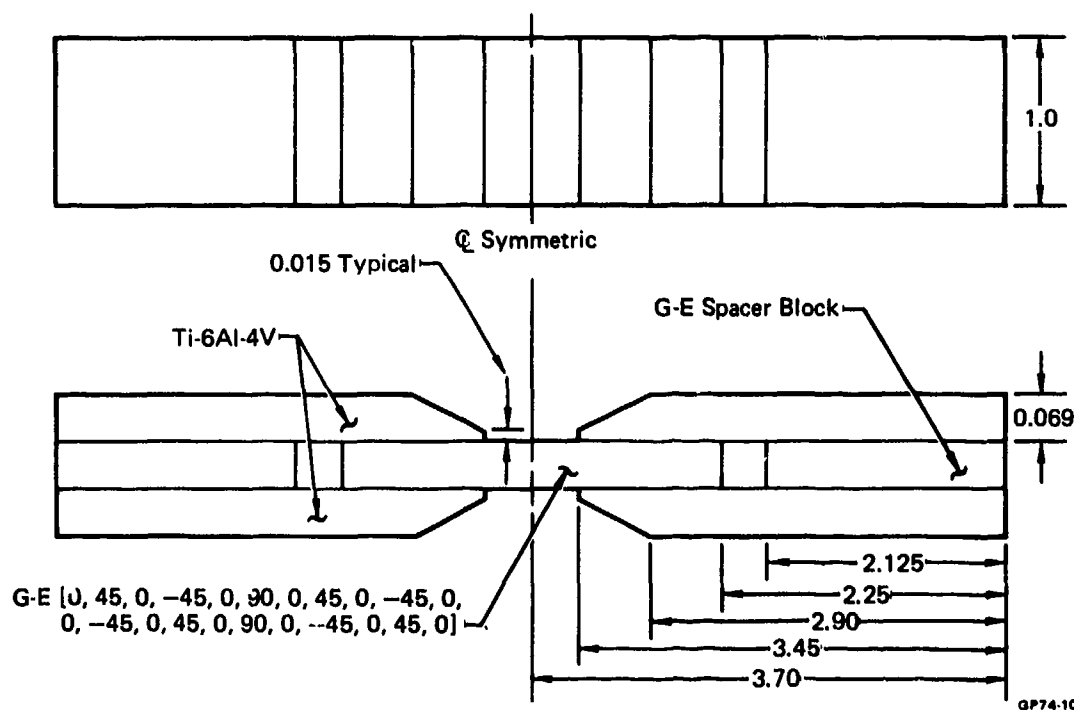
GP74-1037-11

FIGURE 15 70% SCALE, STEP-LAP SPECIMEN, FULL SCALE ADHESIVE



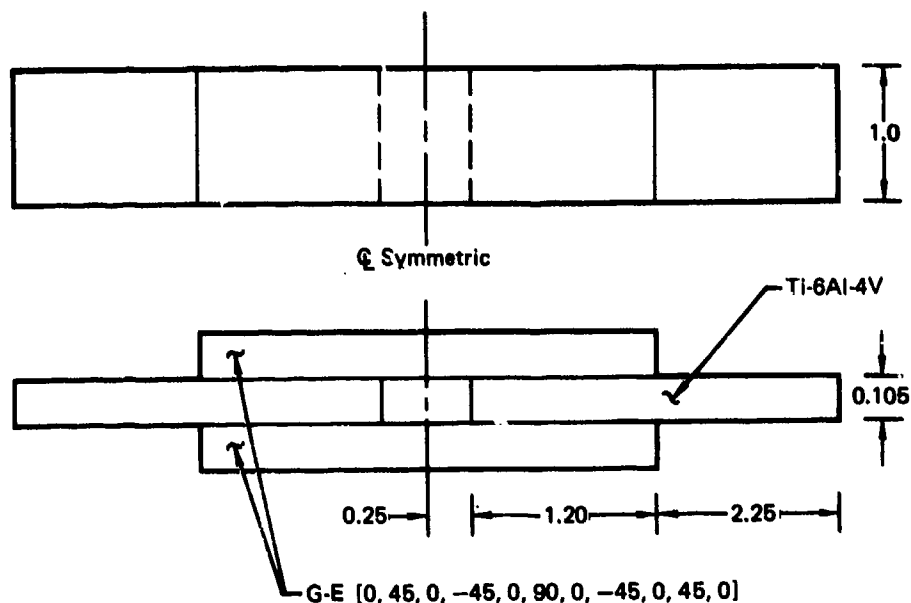
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FIGURE 16 50% SCALE, DOUBLE LAP SPECIMEN, FULL SCALE ADHESIVE



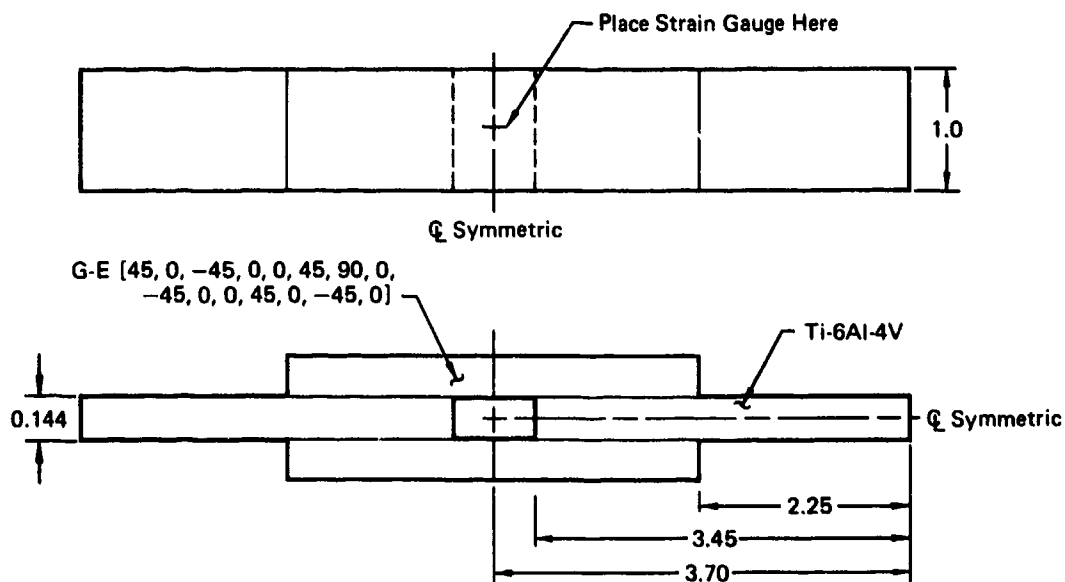
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FIGURE 17 50% SCALE, TAPERED LAP SPECIMEN, FULL SCALE ADHESIVE



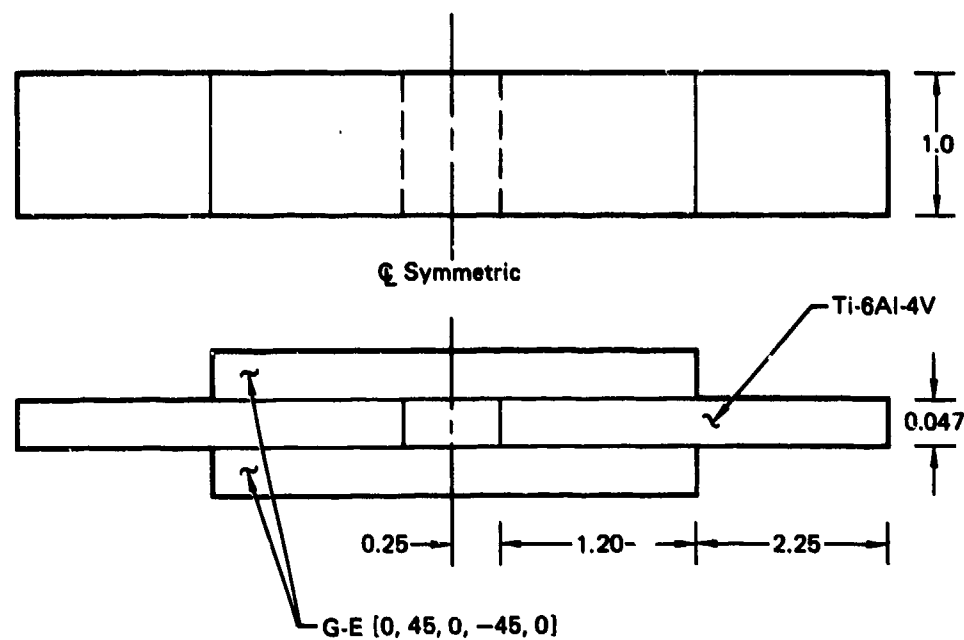
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FIGURE 18 50% SCALE, DOUBLE LAP SPECIMEN, FULL SCALE ADHESIVE



GP74-1037-15

FIGURE 19 70% SCALE, DOUBLE LAP SPECIMEN 70% SCALE ADHESIVE



GP74-1037-16

**FIGURE 20 SIMPLE SPECIMEN (25% SCALE DOUBLE LAP)
FULL SCALE ADHESIVE**

**TABLE 2 STATIC STRENGTH TESTS CONDUCTED UNDER
VERIFICATION TASK**

Specimen Description (Figure)	Reference No.	Predicted Strength (lb/in.)	Failure Load (lb)	Width (in.)	Running Load at Failure (lb/in.)
9	1	17,629	37,750	2.012	18,760
	2	17,629	31,500	1.965	16,030
10	1	17,629	34,300	1.954	17,550
11	1	17,629	19,125	0.995	19,220
	2	17,629	20,850	1.002	20,810
	3	17,629	18,750	0.994	18,960
13	1	12,341	14,750	0.988	14,930
	2	12,341	15,300	0.993	15,410
	3	12,341	14,825	0.975	15,210
14	1	9,376	11,400	0.994	11,470
	2	9,376	11,328	0.987	11,480
	3	9,376	11,000	0.996	11,040
15	1	13,340	15,800	1.001	15,780
	2	13,340	16,200	0.998	13,230
	3	13,340	13,400	1.001	13,390
16	1	8,600	4,050	1.057	3,830
	2	8,600	4,175	1.040	4,010
	3	8,600	3,690	1.061	3,480
17	1	4780	3,880	1.044	3,720
	2	4780	3,735	1.051	3,550
	3	4780	3,415	1.061	3,220
18	1	8,600	9,550	1.010	9,460
	2	8,600	10,750	1.001	10,740
	3	8,600	11,475	1.003	11,440
19	1	8,200	11,450	1.004	11,400
	2	8,200	10,850	1.004	10,810
	3	8,200	10,700	1.003	10,670

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**TABLE 3 FATIGUE LIFE TESTS CONDUCTED
UNDER VERIFICATION TASK**

Specimen Description (Figure)	Reference No.	Test Limit Load (lb)	Width (in.)	Life Times	Last Load (% TLL ²)	Residual Strength (lb)
9	1	22,900	2.001	4.0000		25,175
	2	24,000	1.998	2.0000	125	
10	1	19,800	1.999	4.0000		37,000
	2	22,900	2.001	4.0000		28,500
11	1	13,050	0.993	4.0000		14,850
	2	13,700	0.998	2.4200	87	
	3	13,700	1.001	3.3000	81	
	4	13,700	0.999	2.0000	125	
13	1	9,280	0.987	3.5000	109	
	2	9,280	0.978	3.5000	101	
	3	9,280	0.988	3.0300	91	
14	1	5,295	1.005	4.0000		11,925
	2	7,150	1.003	2.1900	80	
	3	7,150	1.003	1.1700	74	
15	1	9,500	1.001	3.3050		
	2	9,300	1.000	2.0000	113	
	3	9,000	0.998	3.1790	75	
16	1	1,994	0.993	4.0000		(1)
	2	2,850	1.003	4.0000		(1)
	3	3,000	1.001	0.0325	87	
17	1	1,840	1.001	4.0000		(1)
	2	2,452	1.005	4.0000		(1)
	3	2,900	1.003	4.0000		(1)
18	1	5,295	1.005	4.0000		(1)
	2	7,150	1.003	2.1900	82	
	3	7,150	1.003	1.1700	74	
19	1	5,500	1.005	4.0000		10,675
	2	7,150	1.004	2.9200	89	
	3	7,150	1.001	4.0000		11,600

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- (1) No residual tests were run since the data would not help in specimen selection
(2) Test limit load (TLL)

the results of these tests, three specimen types (Figures 11, 13 and 20) were selected for testing to establish the program data base. Simultaneously the random spectrum for the F-15 wing root bending moment was developed for use in lifetime and residual strength tests. The three specimen configurations selected to establish the reliability data base are discussed in the following paragraphs.

2.3.1 Full Scale Step-Lap Specimen Development - Several specimen configurations were evaluated during the specimen verification task. One of the first configurations evaluated is shown in Figure 9. The grips of this specimen were thicker and wider than the test area to avoid possible grip failures caused by the unknown stress concentration factor associated with the serrated grips on the fatigue test machine. Also early in the program several specimens were fabricated without the additional grip width, Figure 10. These specimens were tested and no grip failures occurred (Tables 2 and 3). These specimens (Figures 9 and 10) were two inches wide to minimize edge effects. One inch wide specimens were tested statically and compared with the results of the two inch wide specimens. The comparison is presented in Table 2. From this table it can be seen that the average running load is nearly the same for each specimen. This implies that the edge effects for the one inch wide specimen are minimal. Thus, the one inch wide full scale step-lap specimen (Figure 11) was selected to establish the data base.

2.3.2 Small Scale Step-Lap Specimen Development - Originally, the small scale step-lap specimen was selected to be 50% of full scale (Figure 12). This scale was judged to be the minimum practical in which to simulate realistic ply distributions. At this time, it was assumed that the bondline thickness (and thus adhesive scale) could be controlled with the bonding pressure. Upon further investigation, it was found that the adhesive thickness was controlled by the thickness of the adhesive carrier (FM-400 is an epoxy adhesive with an aluminum filler and a nylon carrier). Only two FM-400 adhesive systems were available; these were type I and type IV. The physical characteristics of these systems (as provided by American Cyanamid, the adhesive manufacturer) are presented in Table 4. Type IV adhesive is 70% as thick as Type I adhesive. Consequently, the small scale joints were designed to be 70% of full scale in order to use scaled adhesives. The 70% scale step-lap specimen (Figure 13) was selected to establish the required data base.

TABLE 4 PHYSICAL CHARACTERISTICS OF FM-400 SYSTEMS

Scale	Type	Weight (lb/ft ²)	Nylon Carrier Specification	Carrier Thickness (in.)	Nominal Bondline Thickness (in.)
1.0	I	0.10	EP-15	0.0063	0.007
0.7	IV	0.07	TC-15	0.0045	0.005

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2.3.3 Simple Specimen Development - The simple specimen configuration was originally selected to represent 50% scale design (Figures 16 and 17) for investigation of scale and complexity effects by comparison with the 50% step-lap joints. At the same time the transferrability of the Weibull parameters could be investigated which is the primary function of these specimens. It had been postulated (Reference 11) that the Weibull static shape parameter would be the same for simple specimens and full scale specimens as long as the failure modes (cohesion) are the same. The tapered double-lap specimens were selected to account for the possibility that the double lap specimens might fail in peel. Graphite-epoxy was used as the central adherend for tapered lap specimens because the specimens could not be fabricated otherwise. Graphite-epoxy was used as the central adherend in the double-lap specimen for consistency with the tapered lap specimens. Several specimens were fabricated to these configurations and tested. The results are also presented in Tables 2 and 3. As can be seen by comparison of the predicted and experimental strength values, the specimens did not behave as expected. It was concluded that the laminates were resin rich due to the inadequate bleed caused by the central location of the graphite-epoxy. Additional (non-tapered) specimens were made with the composite as the outer adherend (Figures 18 and 19). The specimens with 70% scale laminates were

to reveal size and complexity effects and the 50% scale double lap specimens would be used to demonstrate similarity of shape parameters for simple and step-lap joints. The results are presented in Tables 2 and 3. Experimental strength compares well with the predicted value; however, partial peel failures were observed. To avoid this failure mode the laminates were reduced to 25% scale (Figure 20). This configuration was used to establish the data base for the simple specimen design for the remainder of the program.

2.4 Specimen Analysis

The methods used in the strength analyses are outlined in paragraphs 2.2.1 and 2.2.2. Adhesive properties are taken from Table 4 and Figure 21. Mechanical properties used for graphite-epoxy are presented in Table 5. Modulae of the layups on each step of these specimens were determined using computer program ABDMATM listed in Appendix C. Strength allowables for each of the specimens were determined by multiplying the corresponding modulae by the longitudinal strain allowable from Table 5. Properties used for titanium were taken from MIL-HDBK-5B.

$A_1 = A_2 = \text{Area Between Curves}$

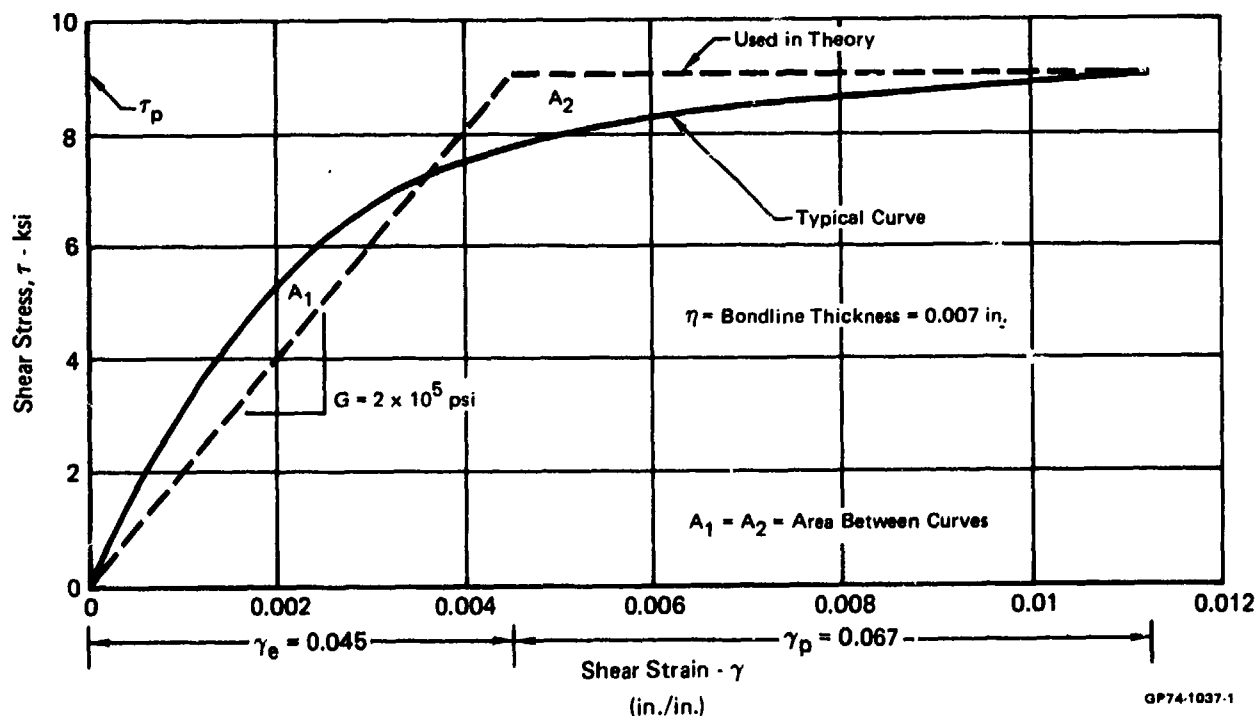


FIGURE 21 SHEAR STRESS STRAIN CURVE FOR ADHESIVE

**TABLE 6 MECHANICAL PROPERTIES OF UNIDIRECTIONAL
NARMCO 5208/T300 GRAPHITE-EPOXY**

Type Loading	Stress ksi	Modulus msi	Strain μ in./in.
0° Tension	200.7	22.3	9,000
90° Tension	7.8	1.95	4,000
0° Compression	267.8	20.6	13,000
90° Compression	48.7	3.6	13,500
0° - 90° Shear	10.6	1.0	23,000

$U_{12} = 0.21$

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Per ply thickness = 0.0054 in.

2.4.1 Step-Lap Specimen - Strength analysis of these specimens were accomplished with the aid of computer program A4EGX discussed and listed in Appendix A. The predicted strength of the full scale step-lap specimens is 17,629 (lb/in) with a cohesive failure in the adhesive initiating on the tang. The predicted strength of the 70% scale step-lap specimen is 12,341 (lb/in) with a cohesive failure initiating on the tang.

2.4.2 Simple Specimen (25% Double Lap) - The strength analysis of this specimen was accomplished using the procedure of paragraph 2.2.1. Figure 6 is entered with a value of λl equal to 14.75 and a γ_p/γ_e equal to 1.5. This gives a τ_{av}/τ_p equal to .25 and a strength of 5400 (lb/in). Thermal stresses were not considered. Experience indicates that for both ductile and brittle adhesives thermal stresses are usually relieved on double lap specimens by creep.

SECTION 3

SPECIMEN FABRICATION

The test specimens for this program were fabricated utilizing MCAIR process specifications and materials bought to MCAIR material specifications. The materials, fabrication procedures, and non-destructive testing (NDT) procedures are discussed in this section.

3.1 Materials

Three materials were used in specimen fabrication: graphite-epoxy, FM-400 adhesive, and titanium 6Al-4V.

3.1.1 Graphite-Epoxy - The graphite-epoxy was supplied as Rigidite 5208/T300 by Narmco Whittaker Materials Division, Costa Mesa, California to meet MCAIR material specification MMS 548. The 50% scale double lap and the 50% scale tapered lap specimens (Figures 16 and 17) were made from Batch 174. The remainder of the specimens were made from Batch 149. Certified properties and/or MCAIR qualification test results for these batches are given in Table 6 together with the requirements of MMS-548.

3.1.2 FM-400 Adhesive - The adhesive film was supplied as FM-400 by American Cyanamid Havre De Grace, Maryland to meet MCAIR material specification MMS-307 Type I and Type IV. Qualification data for the batches of adhesive used in the program and a comparison with specification properties are given in Table 7.

3.1.3 Titanium - The titanium details were fabricated from Ti-6Al-4V annealed sheet purchased to meet the requirement of MIL-T-9046 Type III Composition C.

3.2 Fabrication Procedures

Two procedures were used in the fabrication of these specimens: (1) initial procedure which was used early in the program and (2) a final procedure which was used to fabricate all the specimens for the reliability data base.

3.2.1 Initial Procedure - The first step in this procedure is the fabrication of titanium finger panels such as those illustrated in Figure 22. This concept was used to avoid machining of the titanium at the graphite-epoxy-to-titanium bond because burrs might be created on the titanium during machining, which could lead to a premature fatigue failure in the titanium. These finger panels were laid up with graphite-epoxy prepreg

TABLE 6 RESULTS OF GRAPHITE-EPOXY QUALIFICATION TESTS

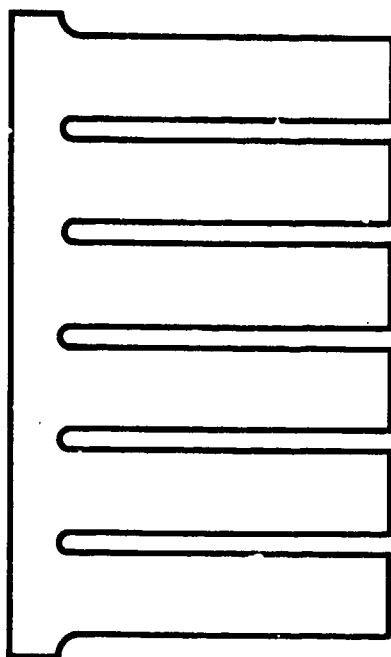
Measured Property		MMS-548 Requirement	Batch 149	Batch 174
0°	Tensile Stress (ksi)	180	227	230
0°	Tensile Strain at Failure (micro in./in.)	—	10463	11092
0°	Tensile Modulus (msi)	—	21.1	22.1
90°	Tensile Stress (ksi)	8.0	8.0	10.2
90°	Tensile Strain at Failure (micro in./in.)	4000	5800	5667
90°	Tensile Modulus (msi)	—	2.3	2.0
Prepreg Resin Content (%)		39-44	37-43	38
Cured Resin Content (%)		—	30.4	—
Volatiles (%)		1.5	0.4	0.4
Resin Flow (%)		—	15.3	17

QP74-1037-188

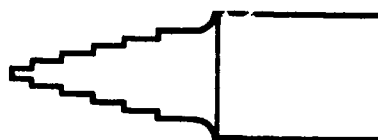
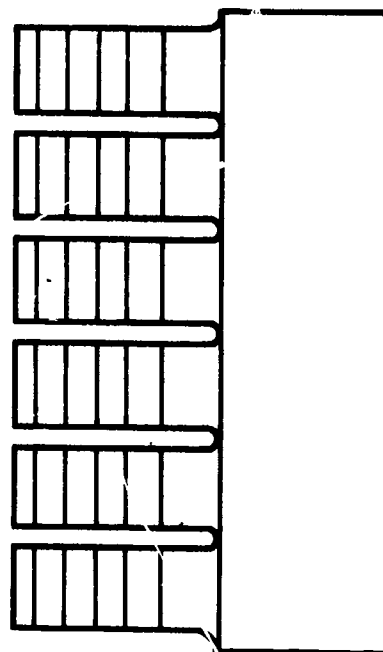
TABLE 7 RESULTS OF FM-400 QUALIFICATION TESTS

Test Temperature (°F)	Lap Shear Strength		
	MMS-307 Requirement (psi)	Batch 162 Roll 579 (psi)	Batch 150 Roll 510 (psi)
RT	3000	3820	3547
365	2400	2540	2593
420	1500	2063	2210

QP74-1037-188



Double Lap



Step Lap

GP74-1037-203

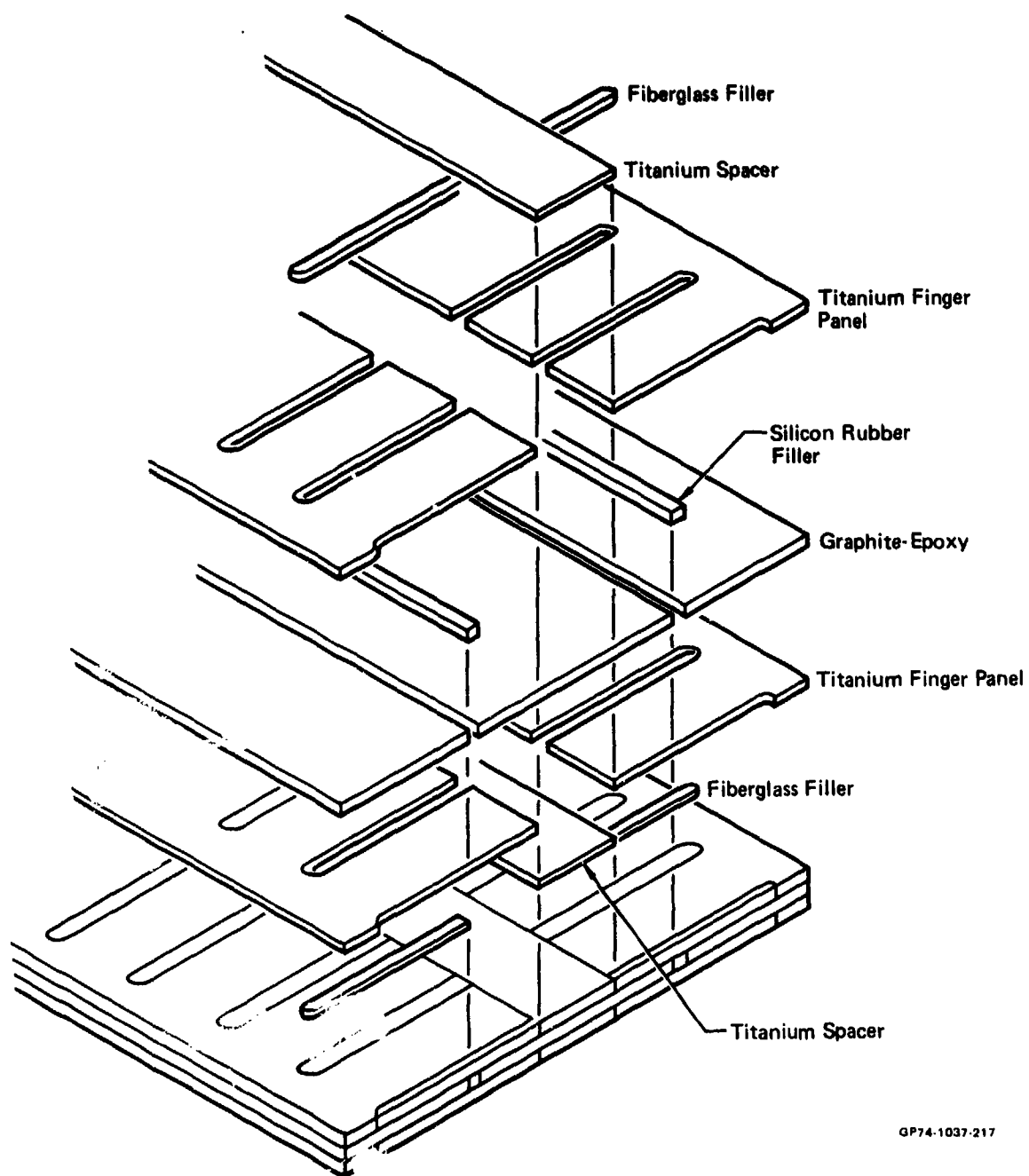
FIGURE 22 TITANIUM FINGER PANELS

and other details as shown in Figure 23. Step lap specimens were laid-up in the conventional manner shown in Figure 24. Both types of lap specimens were laid up on a tooling plate, using shims to support the specimens, and then bagged. After curing, the individual specimens were cut out of the panels. This fabrication procedure proved to be expensive and a better way was found to fabricate the specimens as discussed below.

3.2.2 Final Procedure - Layup procedures were modified to eliminate the tooling plate and associated shimming by utilizing a double bag and picture frame holder. Pressure plates were used to maintain flatness. The finger panel concept was discarded in favor of machining the graphite-epoxy-to-titanium interface using diamond wheel slicing followed by grinding. The grinding operation removed any burrs on the titanium. These procedures are detailed as follows:

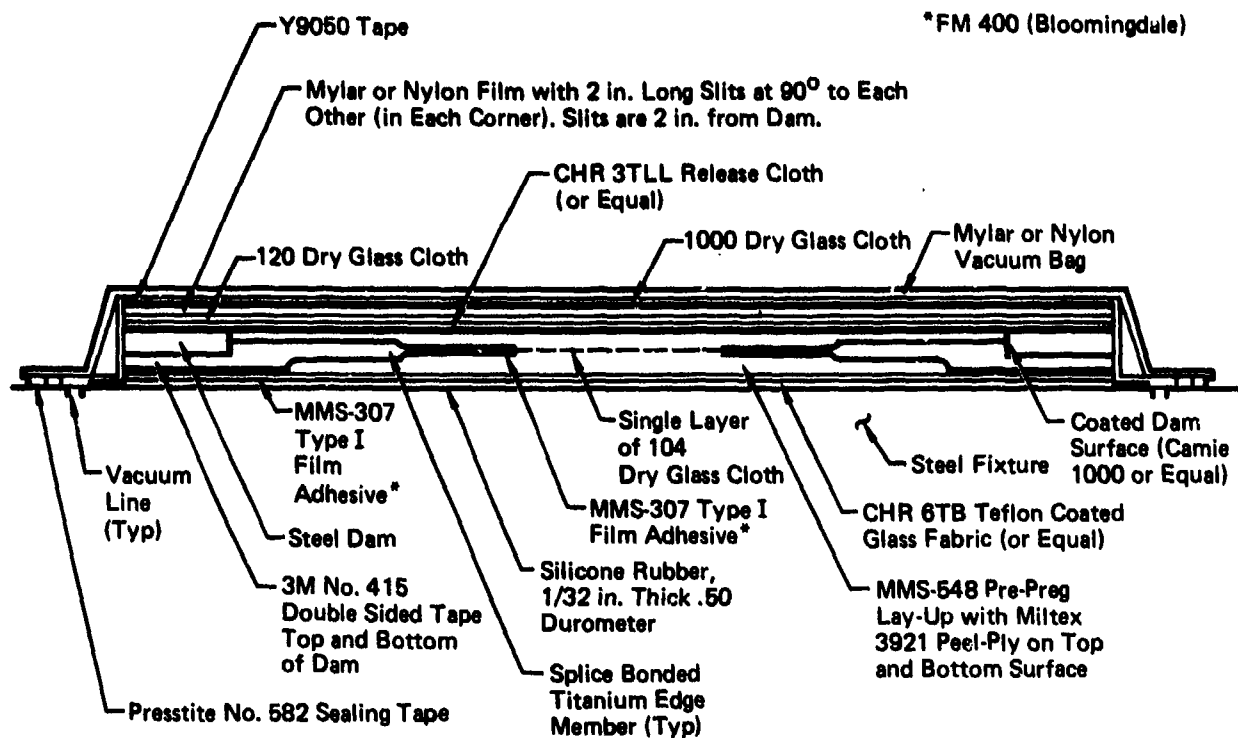
Simple specimens were fabricated to the specification of Figure 25 according to the procedures listed below:

- (1) Panel assemblies, designed to provide ten simple specimens per assembly were assembled according to the requirements shown and noted in Figure 26.
- (2) Each assembly was then placed in the layup configuration shown and noted in Figure 27.
- (3) The vacuum bag was placed in an autoclave and connected to the autoclave vacuum system.
- (4) Pressure in the vacuum bag was reduced to less than 0.1 inches of mercury.
- (5) Autoclave was pressurized to 50 psig.
- (6) Vacuum bag was checked for leaks.
- (7) Autoclave pressure was reduced to 10 psig.
- (8) Pressure in the vacuum bag was increased to 18-19 inches of mercury.
- (9) Assemblies were heated to 270°F at a rate of 3-5°F per minute.
- (10) Assemblies were maintained at 270°F for 30 minutes (the 30 minutes hold was started when assemblies reached 275°F).
- (11) Autoclave was pressurized to 85 psig.



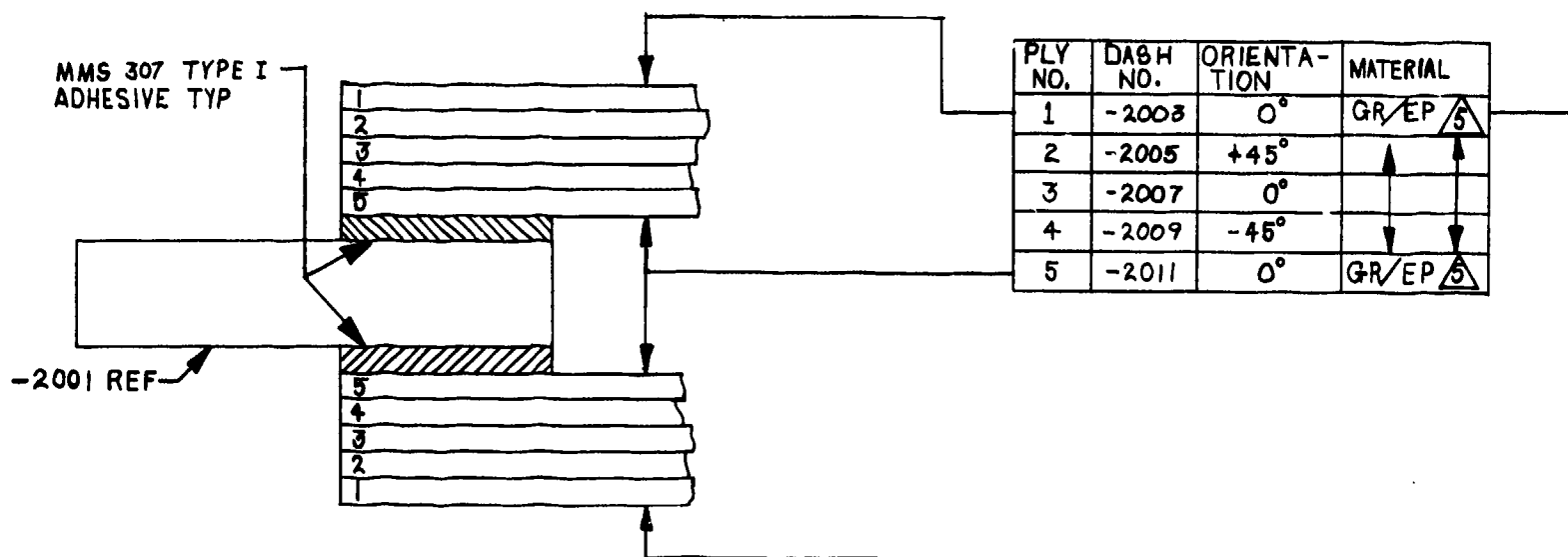
GP74-1037-217

FIGURE 23 LAY-UP SEQUENCE FOR DOUBLE AND TAPERED LAP SPECIMENS



GP74-1037-216

FIGURE 24 INITIAL LAY-UP FOR STEP LAP SPECIMENS



SECTION A-A



SCALE : NONE

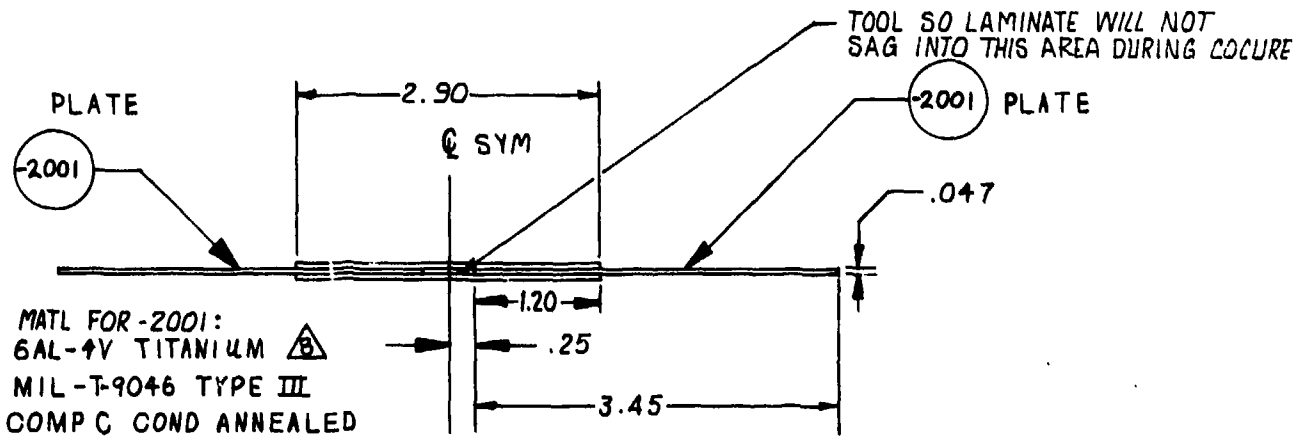
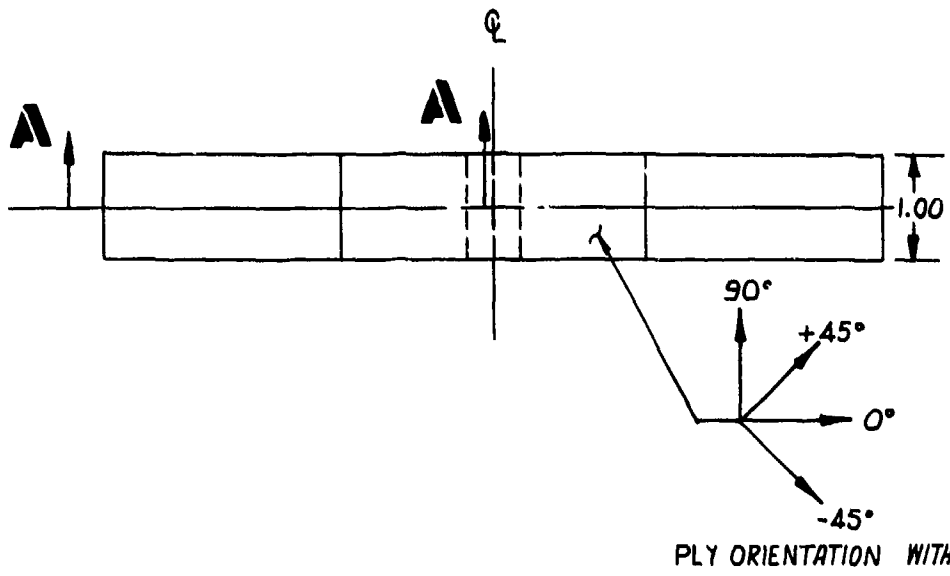
9. Penetrant inspect -2001 per PS 21202
- Material shall be free of Alpha case; shall be cleaned per PS 12037 and primed per PS 14130
- 7 Break sharp edges per PS 23041 on -2001
6. Surface roughness 125 RHR or better for -2001
- Graphite/epoxy material per MMS 548 Rev A Amend I (NARMCO 5208/THORNEL 300)
4. Fabricate and bond per PS 14240 PB 4-258 (COCURE).
3. Graphite/epoxy cured ply thickness: 0.0054 ± 0.0003
2. Last section better used: A
1. Marking per PS 16001

Notes:

QP74-1037-26

FIGURE 25. SIMPLE SPECIMEN DRAWING

MATERIAL
GR/EP 
↑
↓
GR/EP 



-1001
 SCALE-1/1

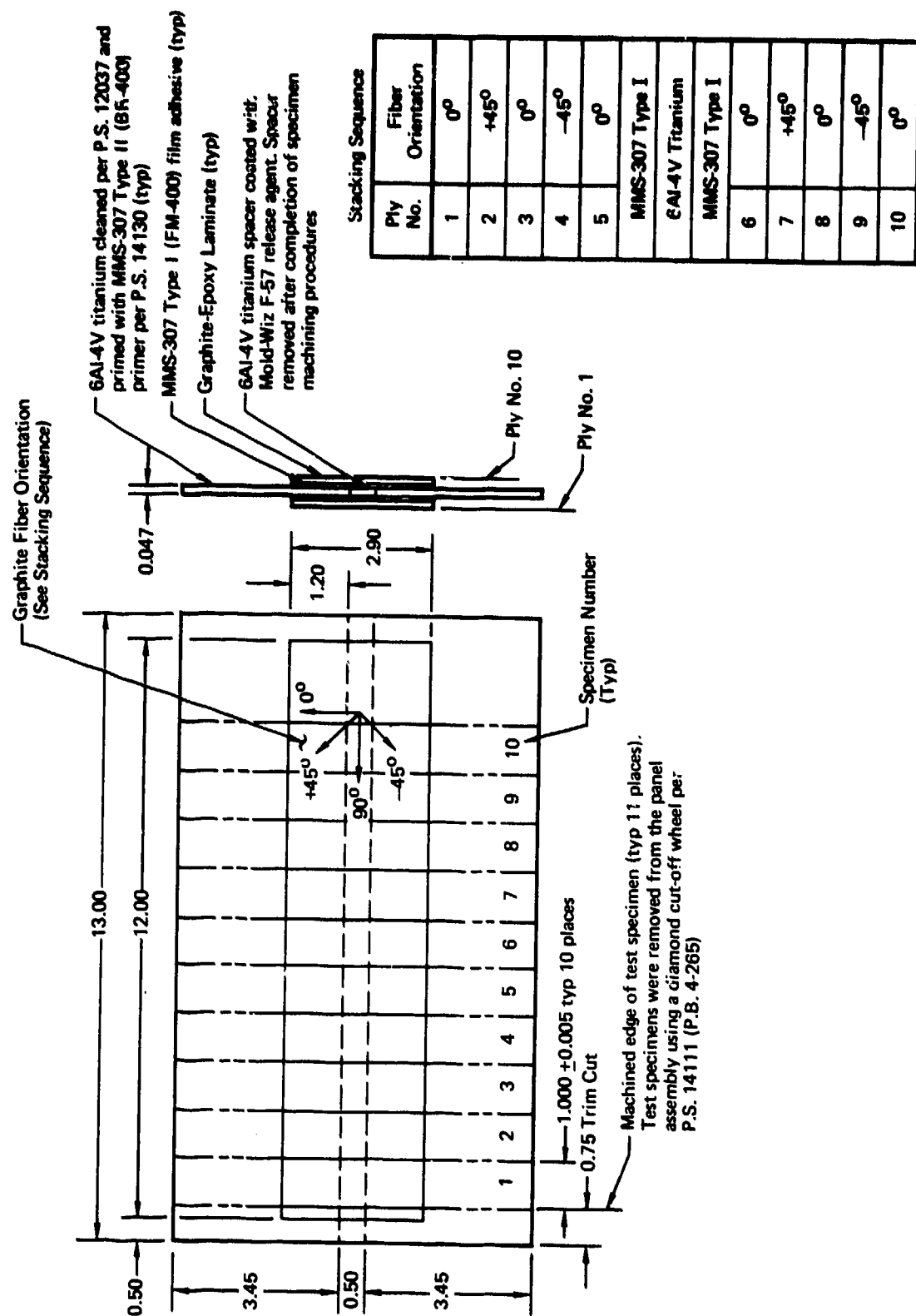


FIGURE 26 SIMPLE JOINT PANEL ASSEMBLY AND SPECIMEN MACHINING REQUIREMENTS

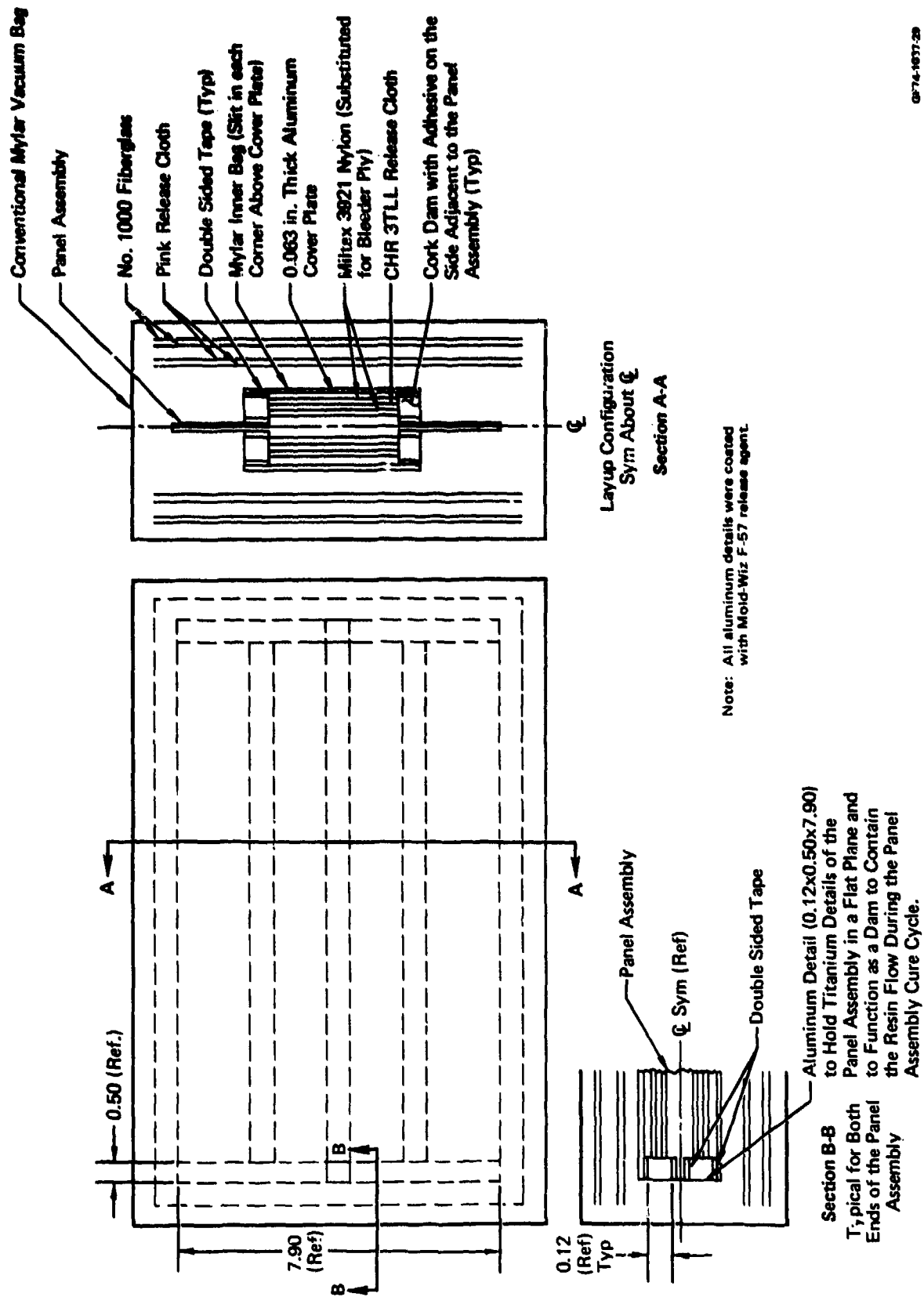


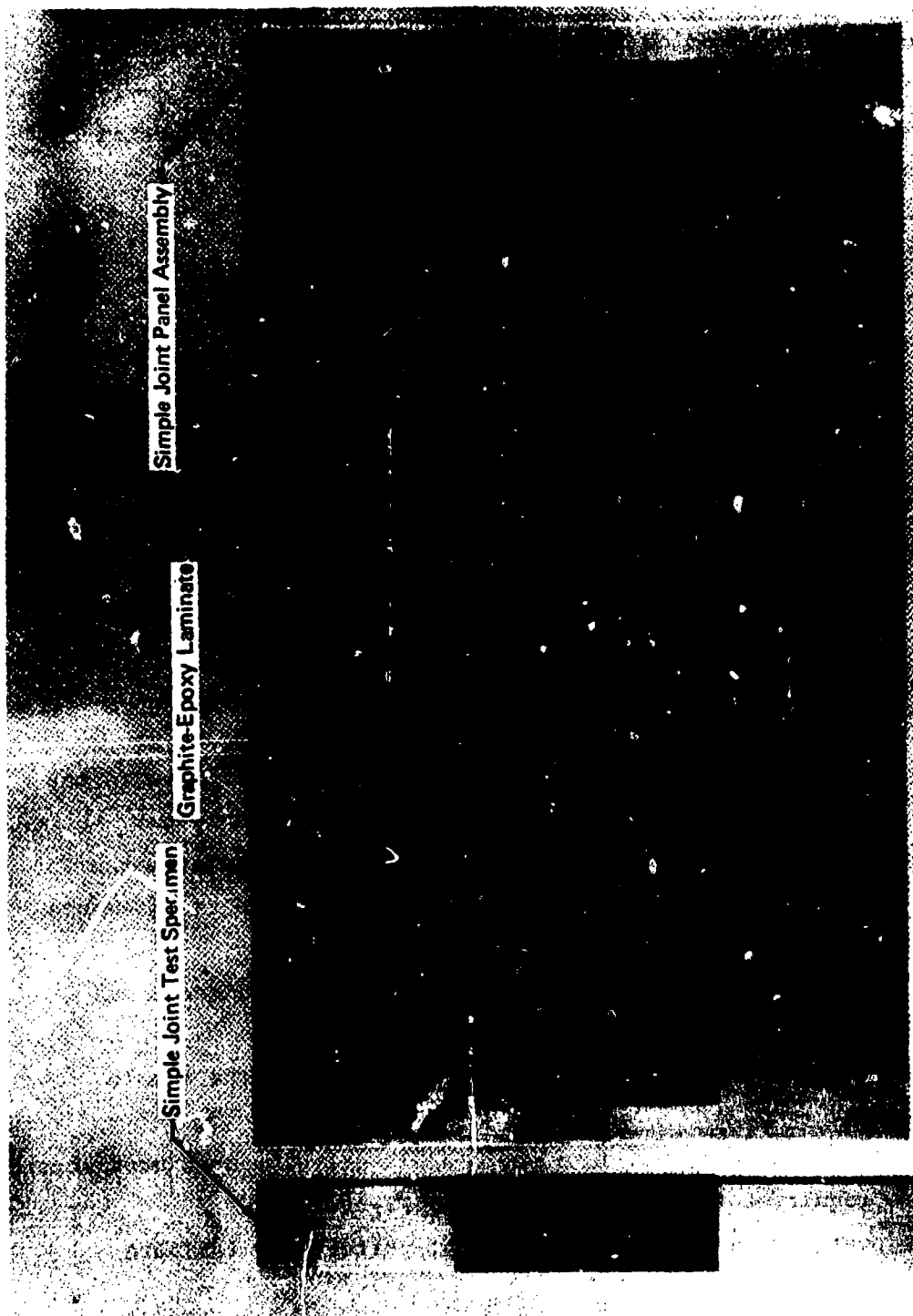
FIGURE 27 SIMPLE JOINT PANEL ASSEMBLY LAYOUT CONFIGURATION

- (12) Vacuum bag was vented to atmospheric pressure when autoclave pressure reached 25 psig. Vacuum bag was not back filled.
- (13) Assemblies were heated to 350°F at a rate of 3-5°F per minute.
- (14) Assemblies were maintained at 350°F for 120 minutes.
- (15) Assemblies were cooled to 150°F, or less, while maintaining full autoclave pressure.
- (16) Vacuum bag was disconnected from the autoclave vacuum system and vacuum bag was removed from the autoclave.
- (17) Assemblies were removed from vacuum bag.
- (18) Assemblies were removed from layup configuration.
- (19) Assemblies were placed in a cool air circulating oven.
- (20) Assemblies were heated to 350°F at a rate of 3-6°F per minute.
- (21) Assemblies were maintained at 350°F for 8 hours.
- (22) Assemblies were cooled to 150°F.
- (23) Assemblies were removed from the oven.
- (24) Assemblies were machined into simple specimens in accordance with requirements shown and noted in Figure 26.
- (25) The nylon peel ply was removed from the graphite-epoxy laminate portions of each test specimen.

A completed panel assembly and a completed simple specimen is in the photograph, Figure 28.

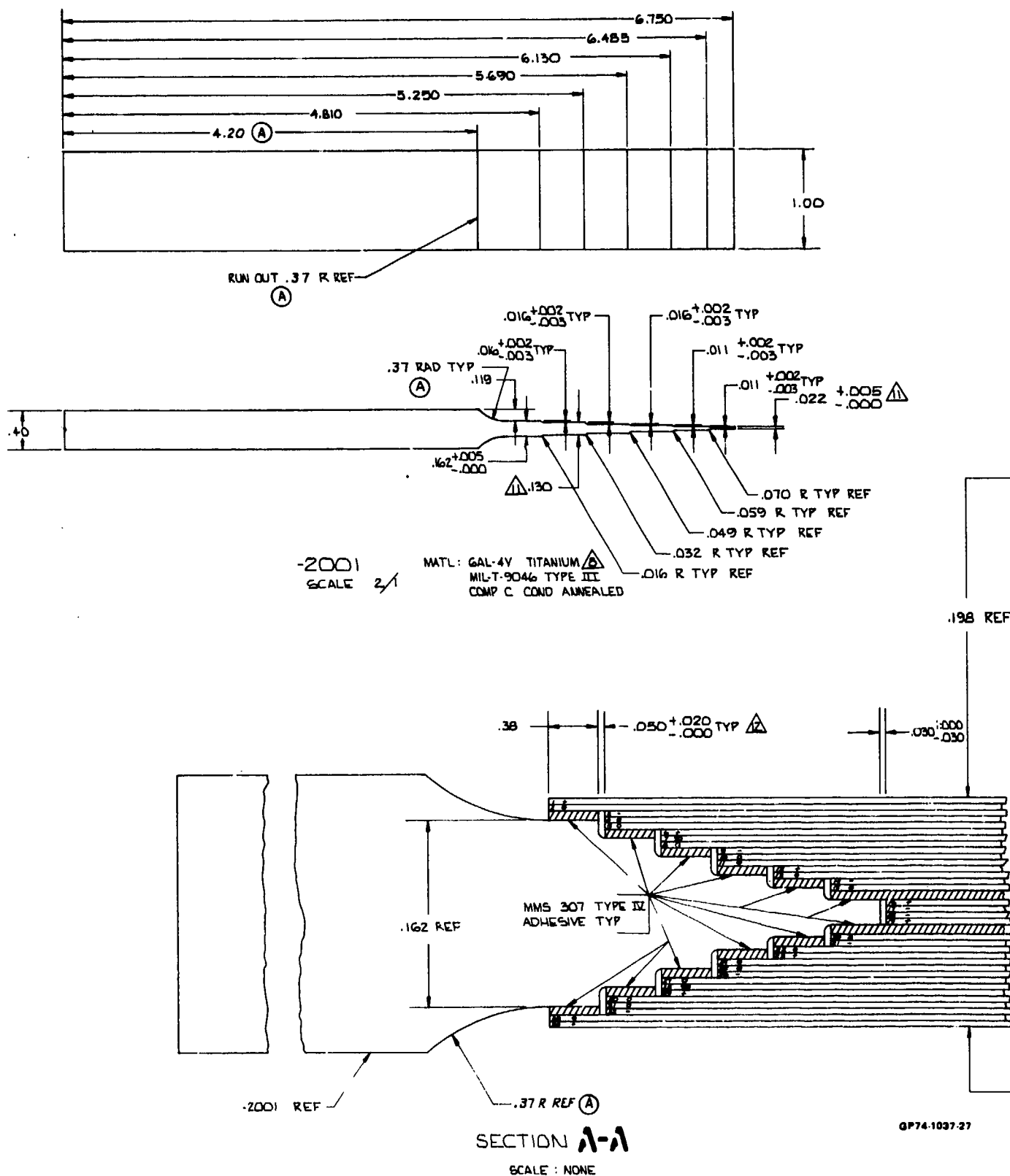
The small scale step-lap specimens (Figure 13) were fabricated to the specifications of Figure 29 according to the procedure listed below:

- (1) Panel assemblies, designed to provide 10 small scale step-lap specimens per assembly, were assembled according to requirements shown and noted in Figure 30.
- (2) Each assembly was placed in the layup configuration shown and noted in Figure 31.
- (3) thru (23) Same as procedures (3) through (23) for the simple specimens.
- (24) Assemblies were machined into small scale step-lap specimens according to requirements shown and noted in Figure 32.
- (25) Nylon peel ply was removed from the graphite-epoxy laminate portions of each test specimen.



OP74-1037-36

FIGURE 28 COMPLETED SIMPLE JOINT PANEL ASSEMBLY AND TEST SPECIMEN

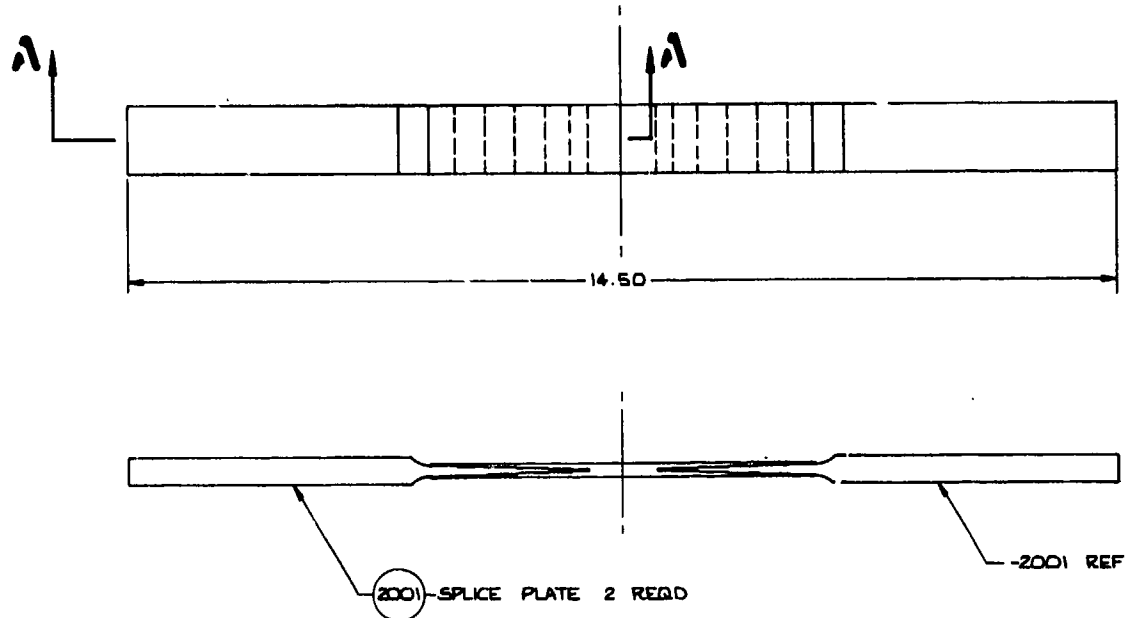


PLY NO	DASH NO	ORIENT
1	-2003	+45
2	-2005	0
3	-2007	-45
4	-2009	0
5	-2011	0
6	-2013	+45
7	-2015	90
8	-2017	0
9	-2019	-45
10	-2021	0
11	-2023	0
12	-2025	+45
13	-2027	0
14	-2029	-45
15	-2031	0
16	-2033	+45
17	-2035	-45
18	-2037	-45
19	-2039	+45
20	-2041	0
21	-2043	-45
22	-2045	0
23	-2047	+45
24	-2049	0
25	-2051	0
26	-2053	-45
27	-2055	0
28	-2057	90
29	-2059	+45
30	-2061	0
31	-2063	0
32	-2065	-45
33	-2067	0
34	-2069	+45

QP74-1037-27

FIGURE 29. SMALL SCALE STEP-LAP SPECIMEN DRAWING

REVISIONS			
SYMBOL	DESCRIPTION	DATE	APPROVED
A	.37R TYP WAS 1.00R TYP, 4.20 WAS 4.00	8/27/74	J. S. HUTTON



PLY NO	DASH NO	ORIENTATION	MATERIAL
1	-2003	+45°	GR/EP Δ
2	-2005	0°	
3	-2007	-45°	
4	-2009	0°	
5	-2011	0°	
6	-2013	+45°	
7	-2015	90°	
8	-2017	0°	
9	-2019	-45°	
10	-2021	0°	
11	-2023	0°	
12	-2025	+45°	
13	-2027	0°	
14	-2029	-45°	
15	-2031	0°	
16	-2033	+45°	
17	-2035	-45°	
18	-2037	+45°	
19	-2039	+45°	
20	-2041	0°	
21	-2043	-45°	
22	-2045	0°	
23	-2047	+45°	
24	-2049	0°	
25	-2051	0°	
26	-2053	-45°	
27	-2055	0°	
28	-2057	90°	
29	-2059	+45°	
30	-2061	0°	
31	-2063	0°	
32	-2065	-45°	
33	-2067	0°	
34	-2069	+45°	GR/EP Δ

-10001

- Δ 12 Tolerance applies to first ply on step, tolerance for remaining plies is +0.000 - 0.030
- Δ 11 Accumulation of tolerances by step height dimensions to be controlled by end dimensions
- Δ 10 Graphite/epoxy material per MMS 548 rev A Amend I (NARMCO 5208/THORNEL 300)
9. Penetrant inspect -2001 per PS 21202, Class A in step areas; all other areas Class C
- Δ 8 Material shall be free of Alpha case; shall be cleaned per PS 12037 and primed per PS 14130
7. Break sharp edges per PS 23041 on -2001
6. Surface roughness 125 RHR or better for -2001
5. Chem mill per PS 20022
4. Fabricate and bond per PS 14240 PB 4-258
3. Graphite/epoxy cured ply thickness: 0.0054 ± 0.0003
2. Last section letter used: A
1. Marking per PS 16001

Notes:

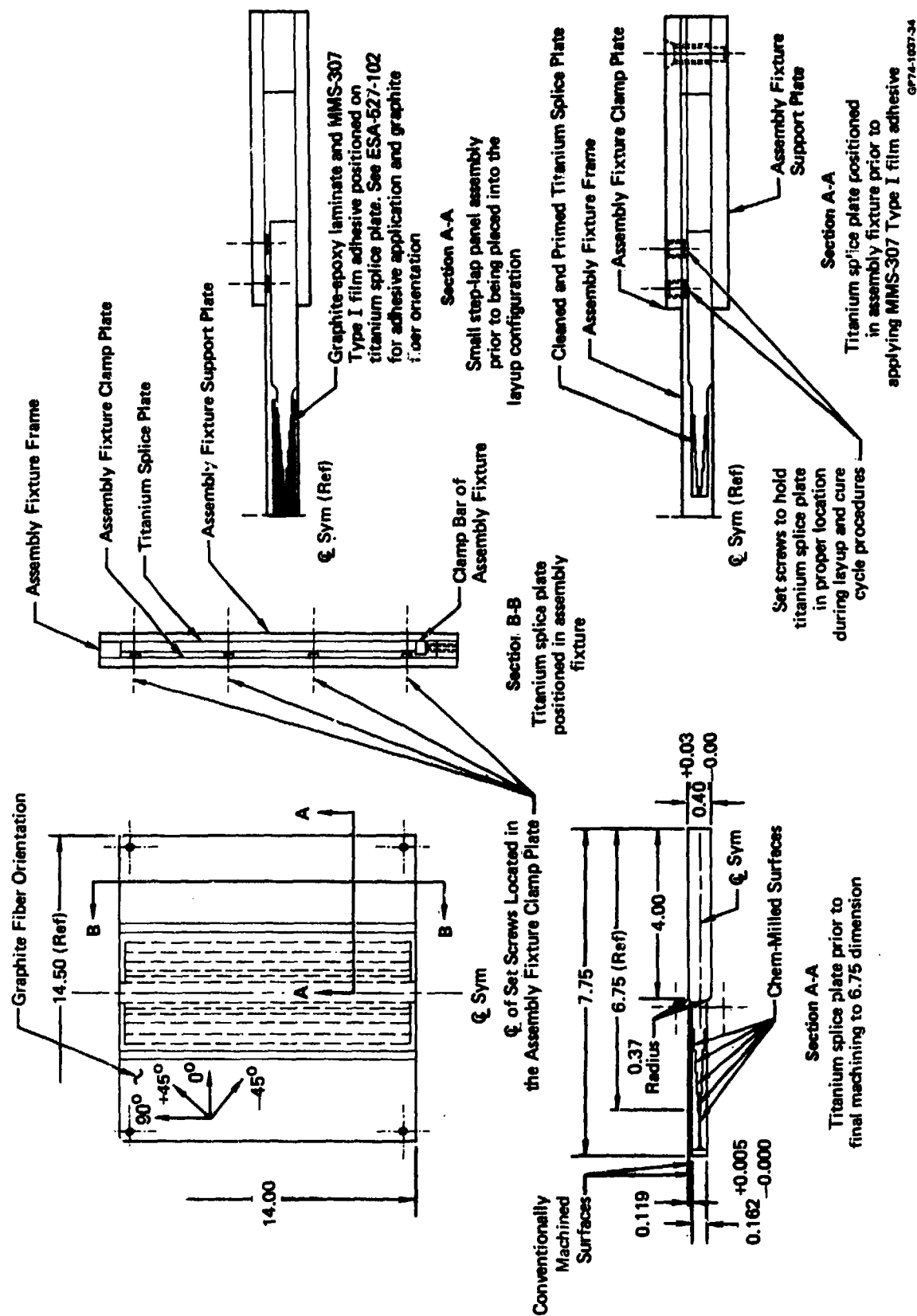


FIGURE 30 SMALL SCALE STEP-LAP PANEL ASSEMBLY

GP74-1037-34

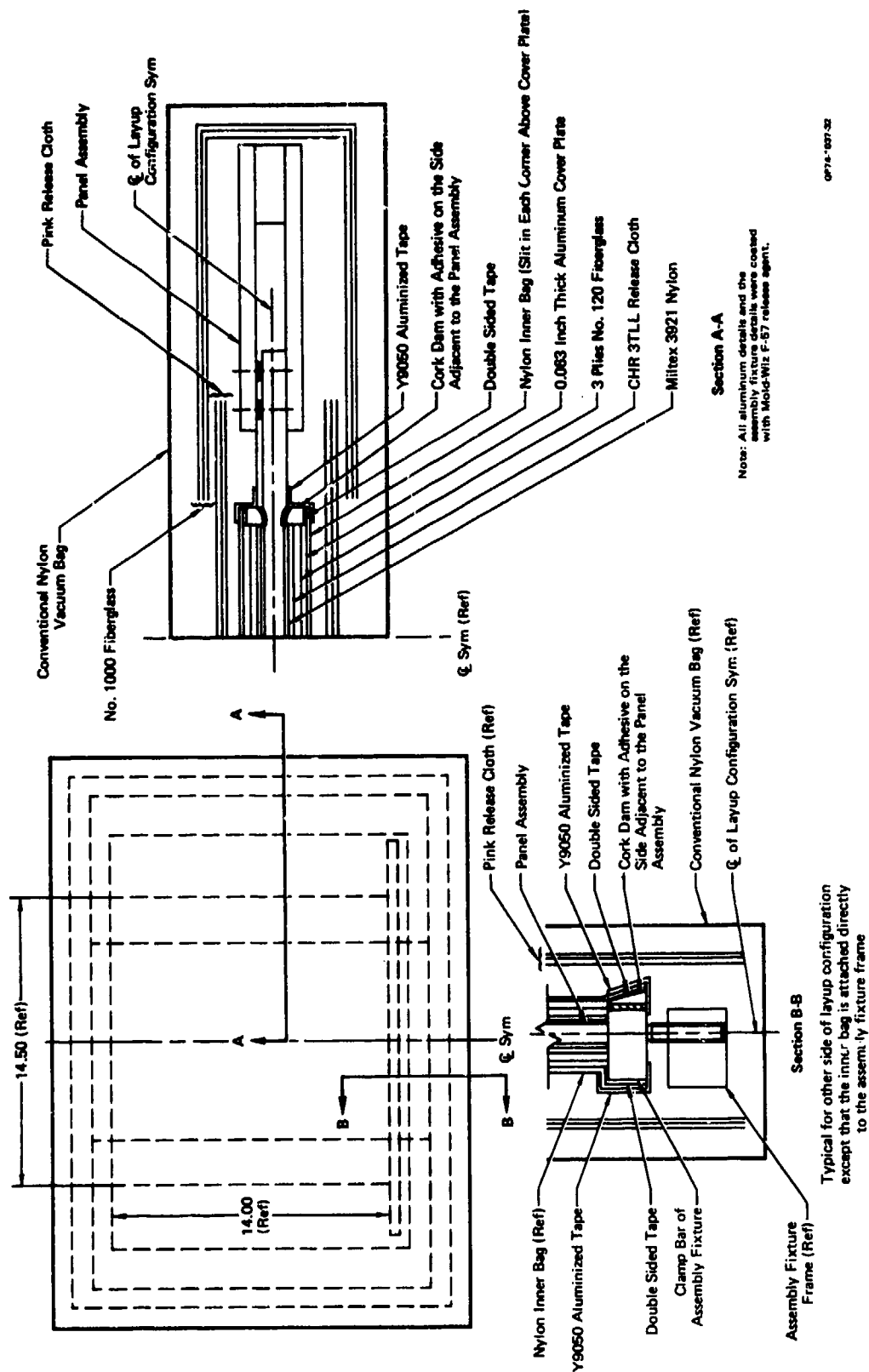
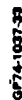


FIGURE 31 SMALL SCALE STEP-LAP LAYUP CONFIGURATION



45

A completed panel assembly and a completed small scale step-lap specimen is shown in Figure 33. A completed panel assembly which has been bandsawed prior to being machined with a diamond cut-off wheel is shown in Figure 34.

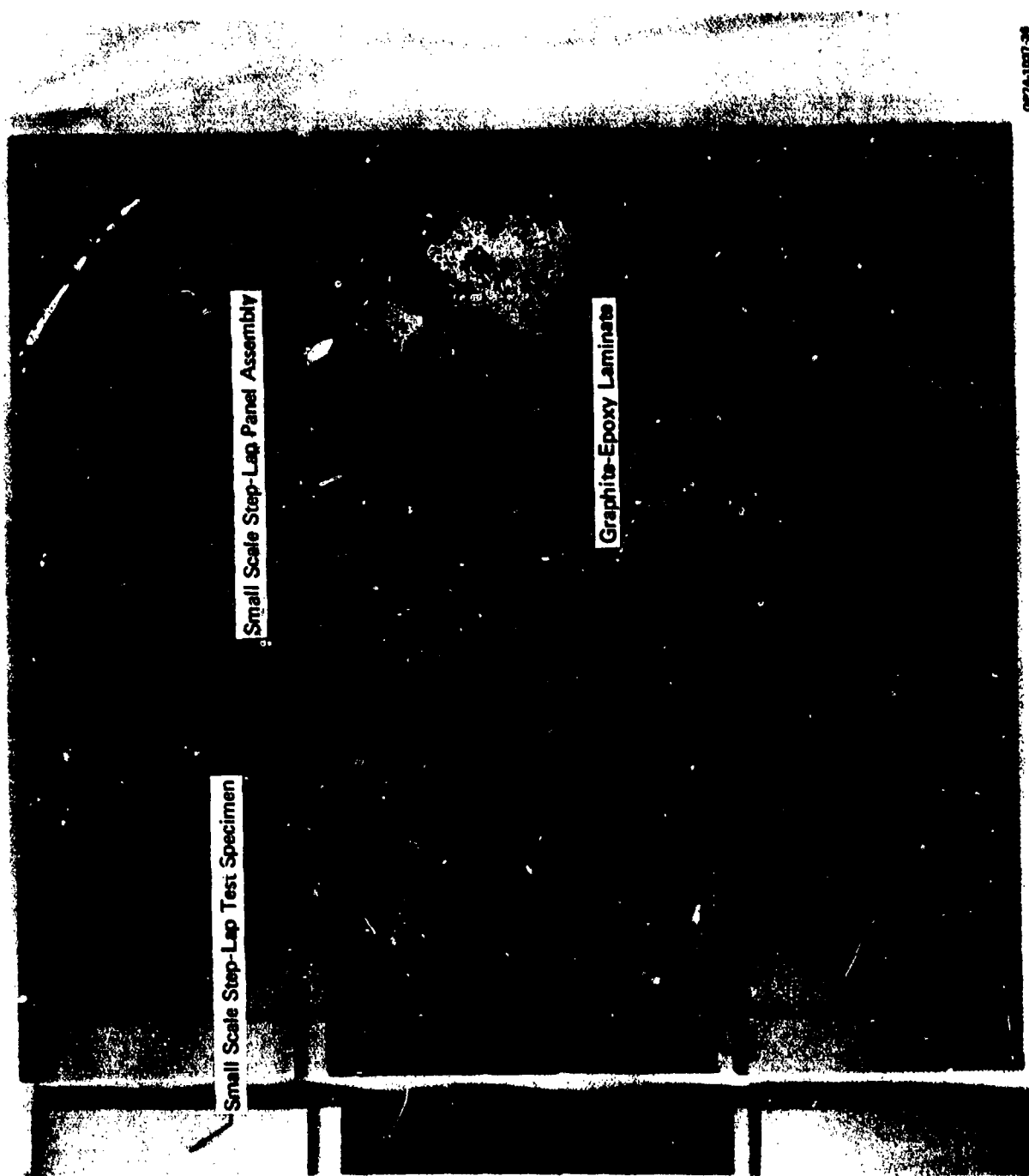
The full scale step-lap specimens (Figure 11) were fabricated to the specifications of Figure 35 according to the procedures listed below:

- (1) Panel assemblies, designed to provide 10 intermediate scale step-lap specimens per assembly, were assembled according to requirements shown and noted in Figure 36.
- (2) Each assembly then was placed in the layup configuration shown and noted in Figure 37.
- (3) thru (23) Same as procedures (3) through (23) for the simple specimens.
- (24) Assemblies were machined into step-lap specimens according to requirements shown and noted in Figure 38.
- (25) Nylon peel ply was removed from the graphite-epoxy laminate portions of each specimen.

A series of photographs showing a full scale step-lap assembly in various stages of assembly are shown in Figures 39 through 45.

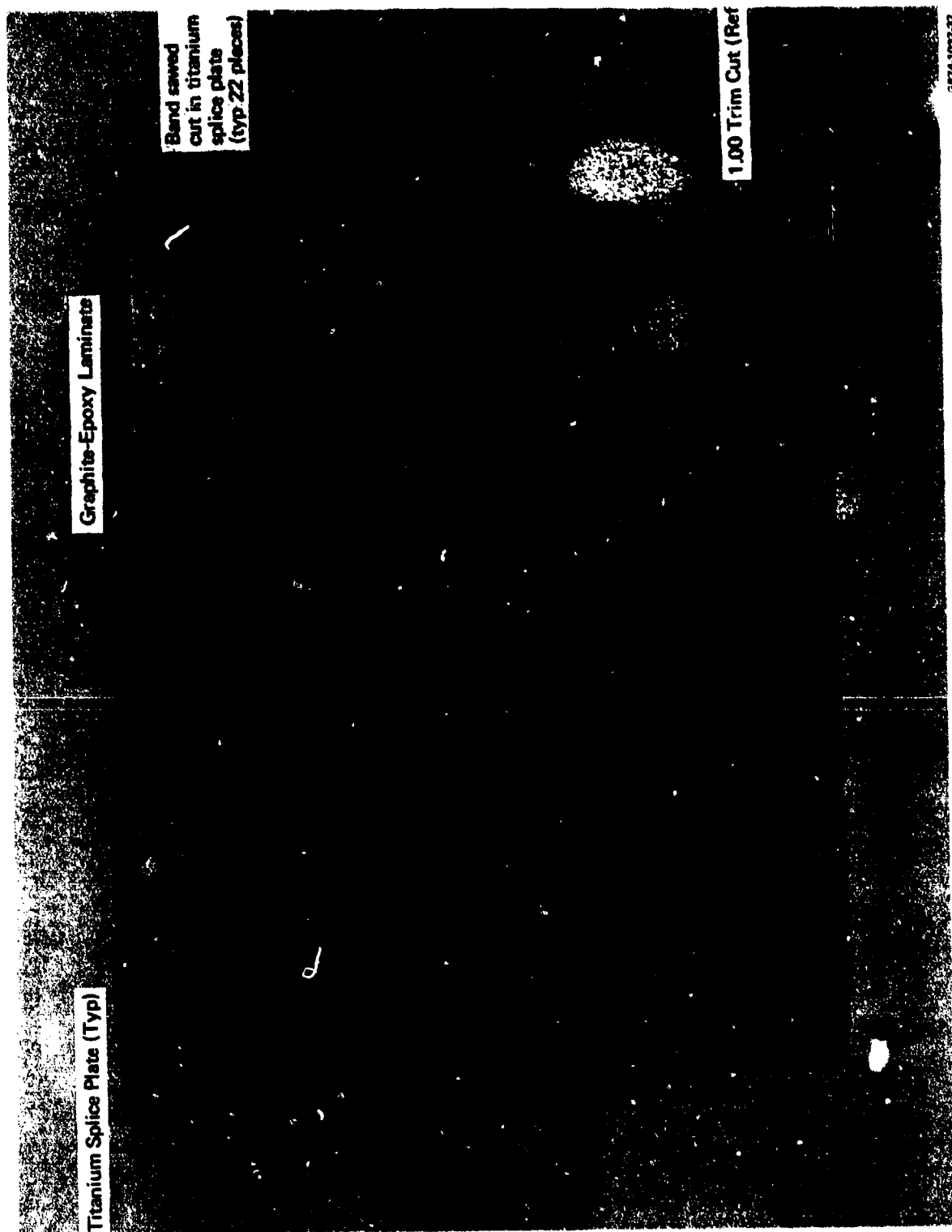
Thickness and width measurements of each test specimen fabricated for this test program were determined according to requirements shown and noted in Figure 46.

Test specimens designated for static testing at room temperature were instrumented according to requirements shown and noted in Figure 47. Table 8 identifies in which autoclave runs the specimens were cured.



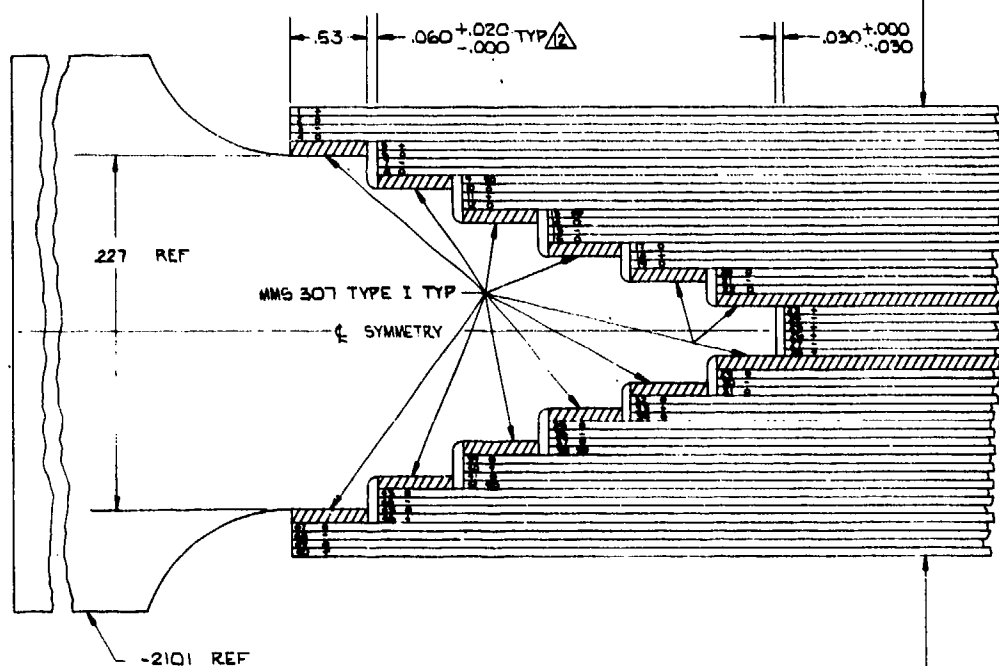
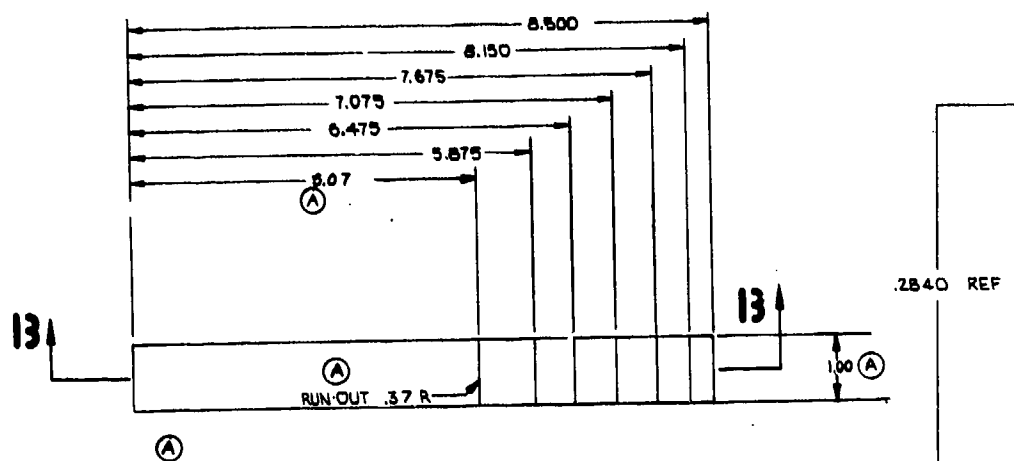
OP74-1057-36

FIGURE 33 COMPLETED SMALL SCALE STEP-LAP PANEL ASSEMBLY AND TEST SPECIMEN



GP74-1037-37

FIGURE 34 COMPLETED SMALL SCALE STEP-LAP PANEL ASSEMBLY PRIOR TO
BEING MACHINED WITH A DIAMOND CUT-OFF WHEEL



SECTION A-A

SCALE : NONE
(TYP EACH END)

TABLE I

PLY NO	DASH NO	ORIENTATION	MATERIAL
1	-2001	+45°	GR/EP
2	-2003	0°	
3	-2005	-45°	
4	-2007	0°	
5	-2009	+45°	
6	-2011	0°	
7	-2013	-45°	
8	-2015	0°	
9	-2017	90°	
10	-2019	0°	
11	-2021	+45°	
12	-2023	0°	
13	-2025	90°	
14	-2027	0°	
15	-2029	-45°	
16	-2031	0°	
17	-2033	0°	
18	-2035	+45°	
19	-2037	0°	
20	-2039	0°	
21	-2041	-45°	
22	-2043	0°	
23	-2045	+45°	
24	-2047	-45°	
25	-2049	+45°	
26	-2051	+45°	
27	-2053	-45°	
28	-2055	+45°	
29	-2057	0°	
30	-2059	-45°	
31	-2061	0°	
32	-2063	0°	
33	-2065	+45°	
34	-2067	0°	
35	-2069	0°	
36	-2071	-45°	
37	-2073	0°	
38	-2075	90°	
39	-2077	0°	
40	-2079	+45°	
41	-2081	0°	
42	-2083	90°	
43	-2085	0°	
44	-2087	-45°	
45	-2089	0°	
46	-2091	+45°	
47	-2093	0°	
48	-2095	-45°	
49	-2097	0°	
50	-2099	+45°	GR/EP

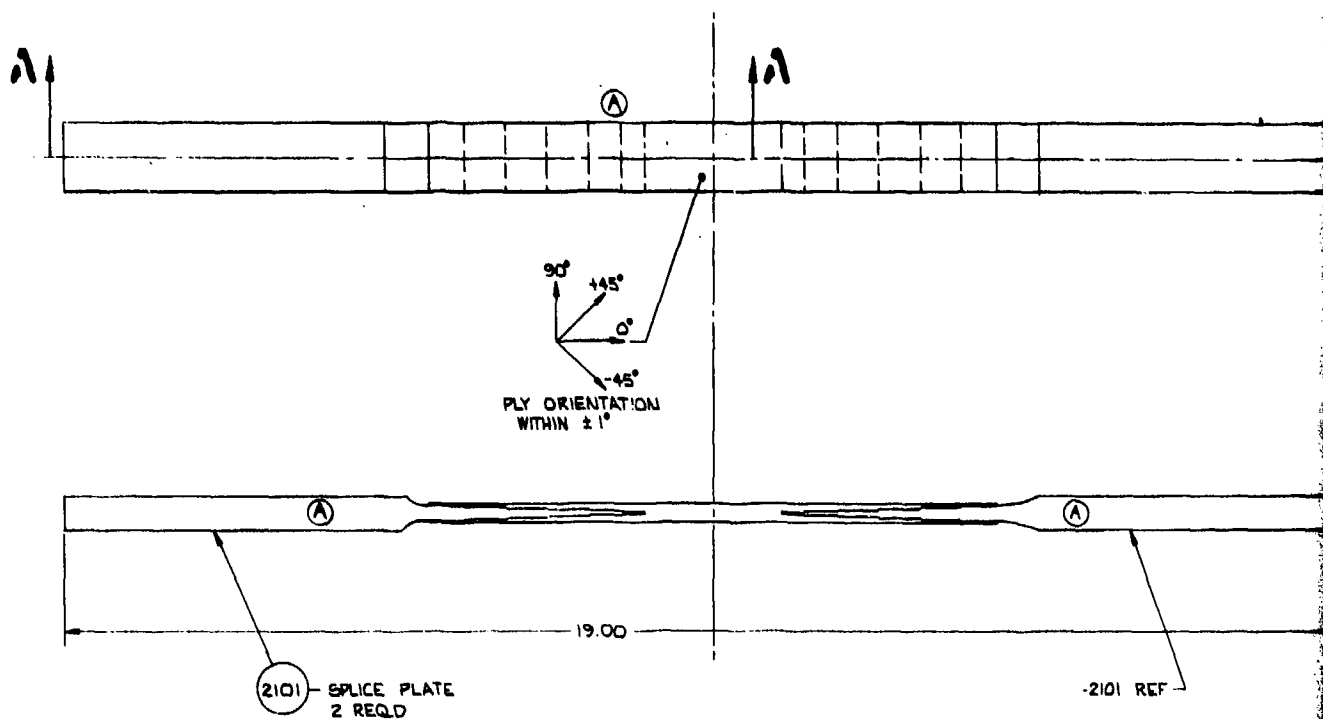
GP74-1037-28

FIGURE 35. FULL SCALE STEP-LAP SPECIMEN DRAWING

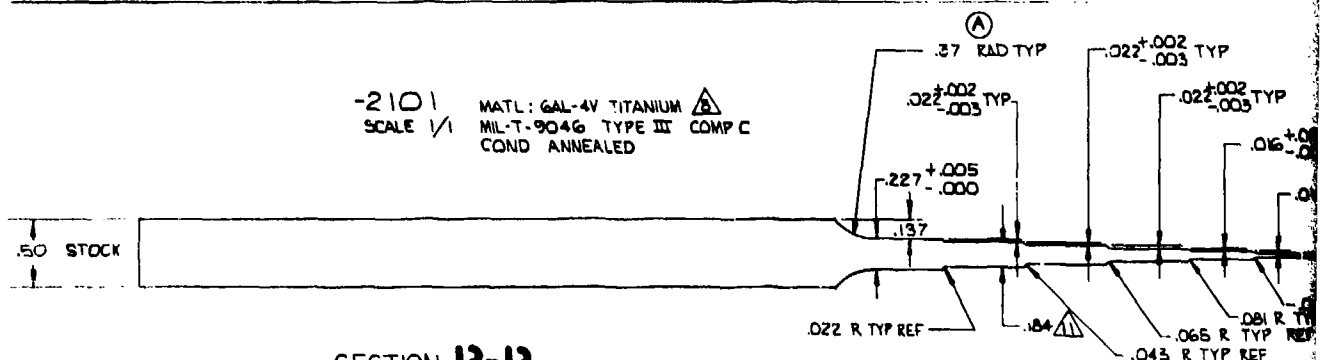
TABLE I

PLY NO	DASH NO	ORIENTATION	MATERIAL
1	-2001	+45°	GR/EP
2	-2003	0°	
3	-2005	-45°	
4	-2007	0°	
5	-2009	+45°	
6	-2011	0°	
7	-2013	-45°	
8	-2015	0°	
9	-2017	90°	
10	-2019	0°	
11	-2021	+45°	
12	-2023	0°	
13	-2025	90°	
14	-2027	0°	
15	-2029	-45°	
16	-2031	0°	
17	-2033	0°	
18	-2035	+45°	
19	-2037	0°	
20	-2039	0°	
21	-2041	-45°	
22	-2043	0°	
23	-2045	+45°	
24	-2047	-45°	
25	-2049	+45°	
26	-2051	+45°	
27	-2053	-45°	
28	-2055	+45°	
29	-2057	0°	
30	-2059	-45°	
31	-2061	0°	
32	-2063	0°	
33	-2065	+45°	
34	-2067	0°	
35	-2069	0°	
36	-2071	-45°	
37	-2073	0°	
38	-2075	90°	
39	-2077	0°	
40	-2079	+45°	
41	-2081	0°	
42	-2083	90°	
43	-2085	0°	
44	-2087	-45°	
45	-2089	0°	
46	-2091	+45°	
47	-2093	0°	
48	-2095	-45°	
49	-2097	0°	
50	-2099	+45°	GR/EP

GP74-1037-28



-10001

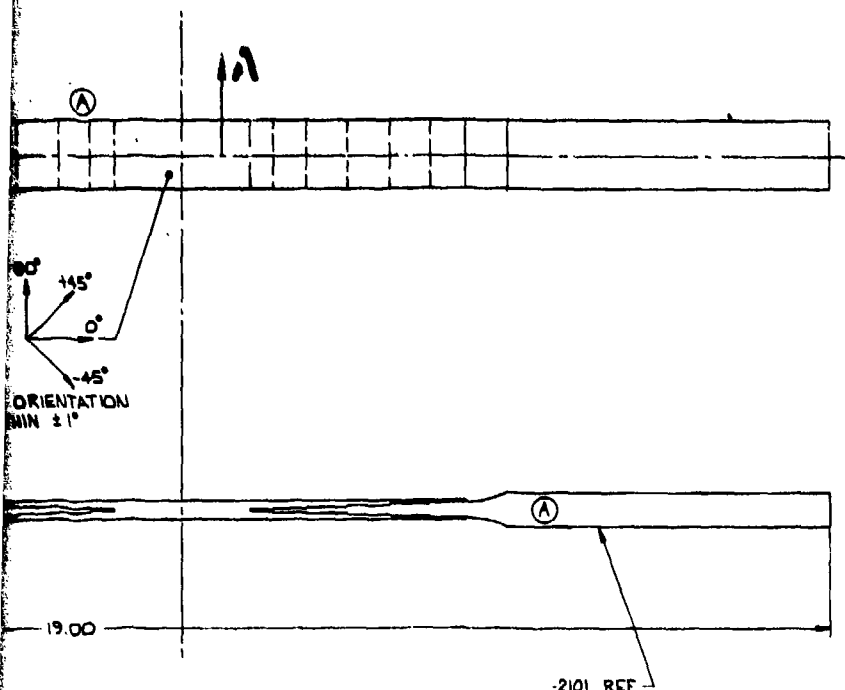


SECTION 13-13

SCALE 2/1

- (A) 13 Tolerance applies to first ply on step, tolerance
- (A) 12 Accumulation of tolerances by step height
- (A) 11 Graphite/epoxy material per MMS 548 Rev
- (A) 10 9. Penetrant inspect -2101 per PS 21202, Class
- (A) 9 Material shall be free of Alpha case; shall be
- (A) 8 7. Break sharp edges per PS 23041 on -2101
- (A) 7 6. Surface roughness 125 RHR or better for -2
- (A) 6 5. Chem mill -2101 per PS 20022
- (A) 5 4. Fabricate and bond per PS 14240 PB 4-250
- (A) 4 3. Graphite/epoxy cured ply thickness: 0.005
- (A) 3 2. Last section letter used: B
- (A) 2 1. Marking per PS 16001

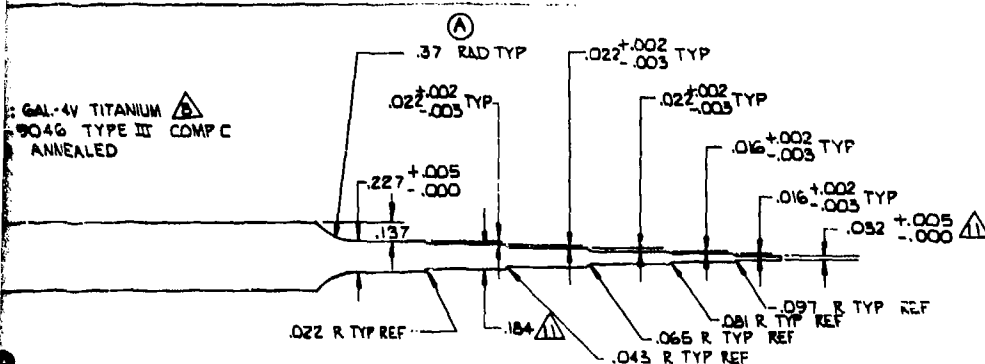
Notes:



REVISIONS		
SYMBOL	DESCRIPTION	DATE/APP/REV
A	.37 R TYP WAS 1.50 R TYP 5.07 WAS 4.72; NOTE 13 DELETED ON -2101 GRIPS WERE 4.00, NOW 1.00 ON -2101 WIDTH IS 1.00, WAS 2.00 FOLLOWING DASH NOS. ARE OBSOLETE: -1008, -2105, -2106, -2107, -2109, -2111, -2112, -2115, -2117, -2119, -2121, -2123, -2125, -2127, -2129, -2131, -2133, -2135, -2137, -2139, -2141, -2143, -2145, -2147, -2149, -2151, -2153.	8-77 J.E. COLLINS

DISOLETE -1003 (A)

-1001



- (A) 13
12 Tolerance applies to first ply on step, tolerance for remaining plies is +0.000 - 0.030
11 Accumulation of tolerances by step height dimensions to be controlled by end dimensions
10 Graphite/epoxy material per MMS 548 Rev A Amend I (NARMCO 5208/THORNEIL 300)
- (A) 9. Penetrant inspect -2101 per PS 21202, Class A in step areas; all other areas Class C
(B) 8. Material shall be free of Alpha case; shall be cleaned per PS 12037 and primed per PS 14130
(A) 7. Break sharp edges per PS 23041 on -2101
(A) 6. Surface roughness 125 RHR or better for -2101
5. Chem mill -2101 per PS 20022
4. Fabricate and bond per PS 14240 PB 4-258
3. Graphite/epoxy cured ply thickness: 0.0054 ± 0.0003
2. Last section letter used: B
1. Marking per PS 16001

Notes:

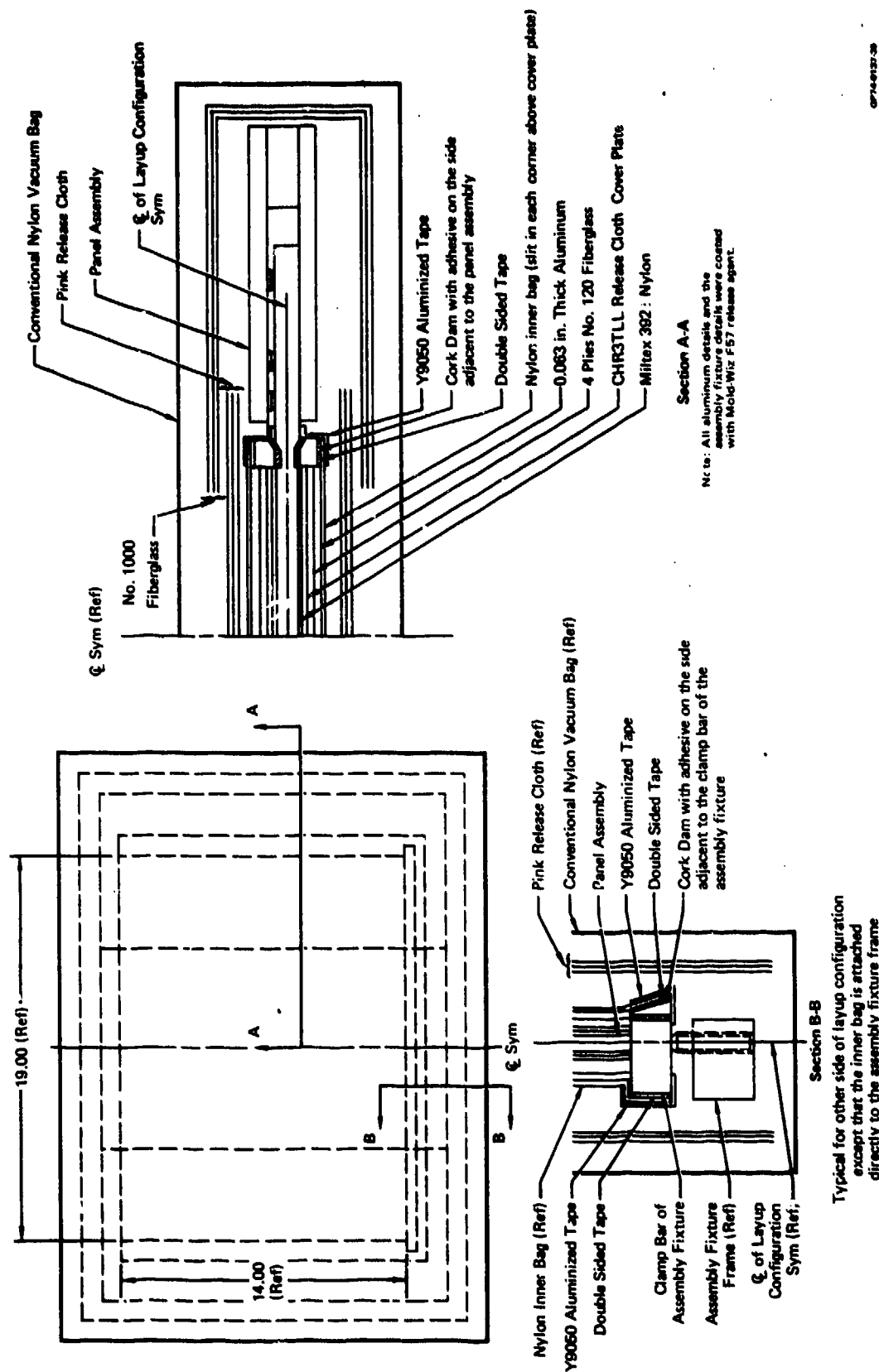
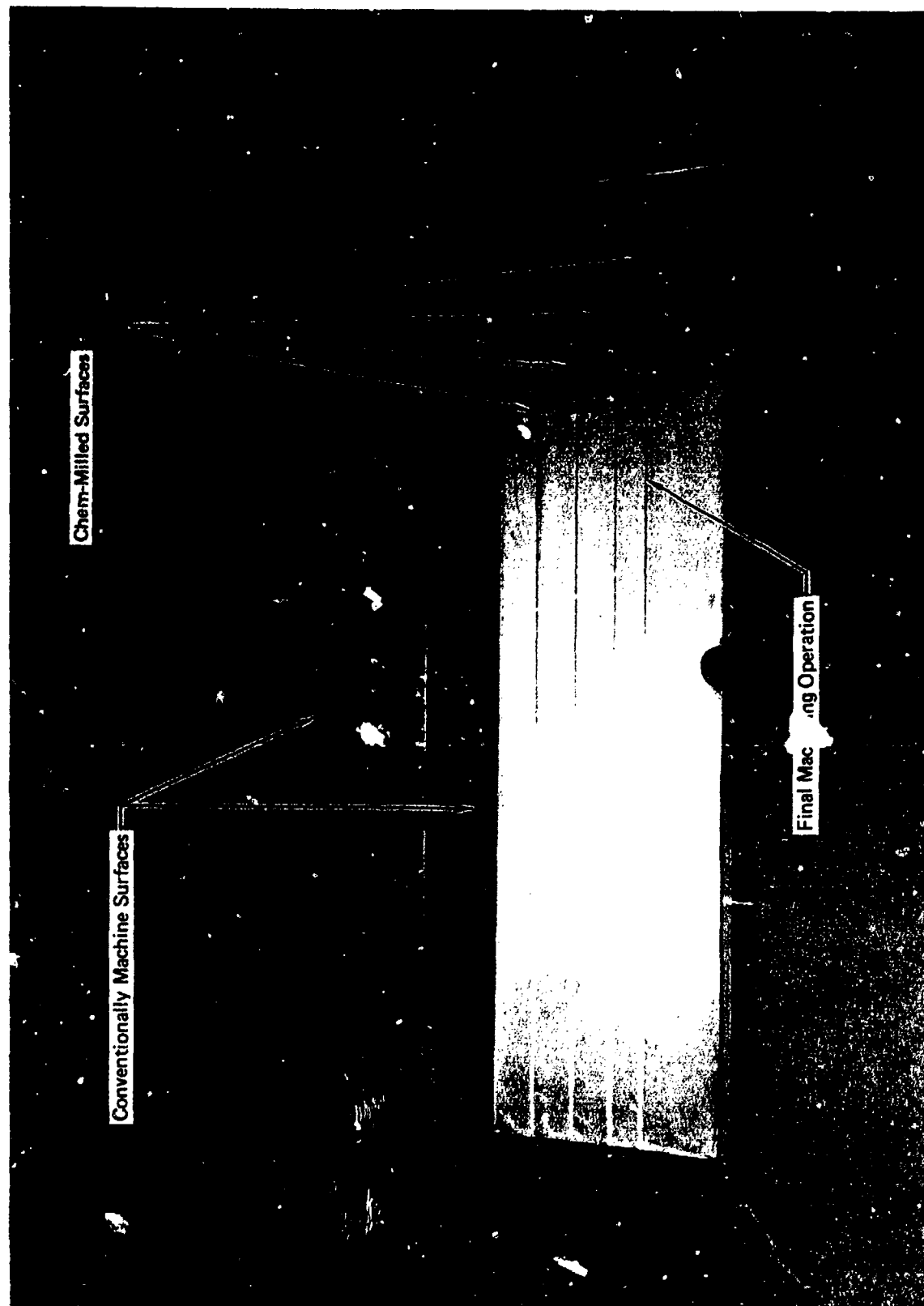


FIGURE 37 FULL SCALE STEP-LAP LAYUP CONFIGURATION



GP74-1337-40

FIGURE 38 TITANIUM SPLICE PLATE PRIOR TO FINAL MACHINING OPERATION

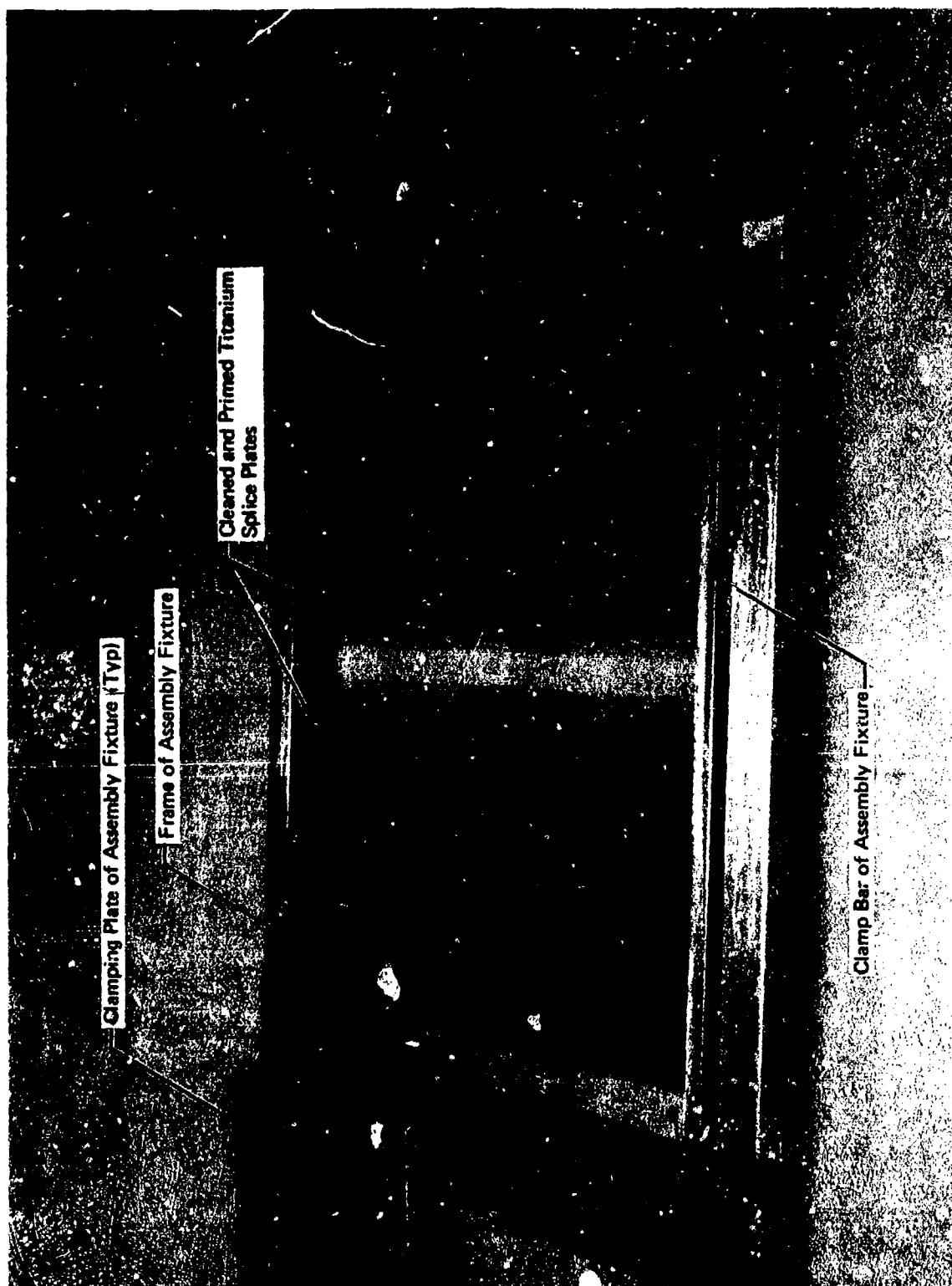
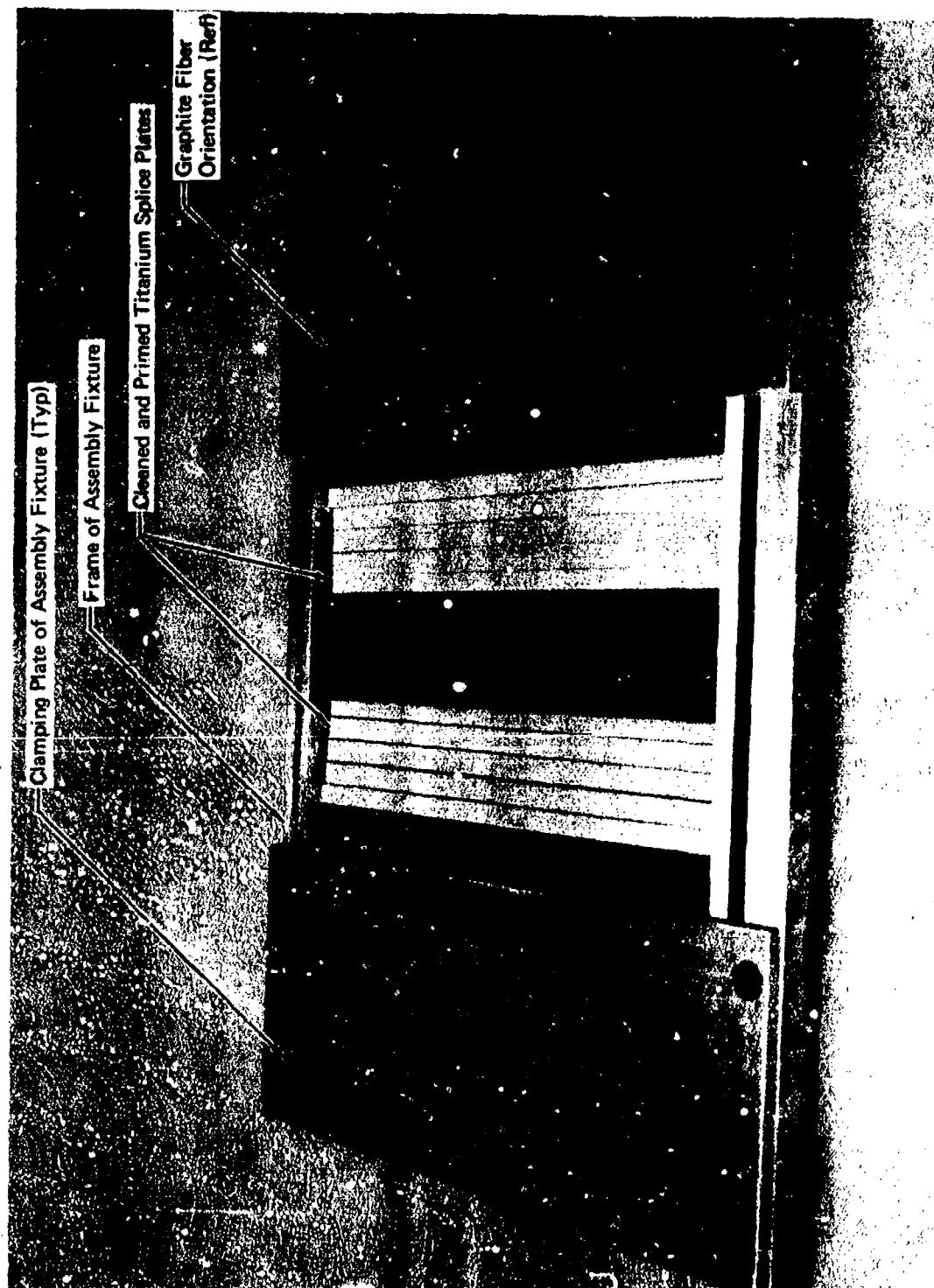


FIGURE 39 TITANIUM SPLICE PLATES POSITIONED IN ASSEMBLY FIXTURE



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**FIGURE 40 TITANIUM SPLICE PLATES AND ASSEMBLY FIXTURE CONFIGURATION
BEFORE APPLYING THE MMS-307 TYPE I FILM ADHESIVE**

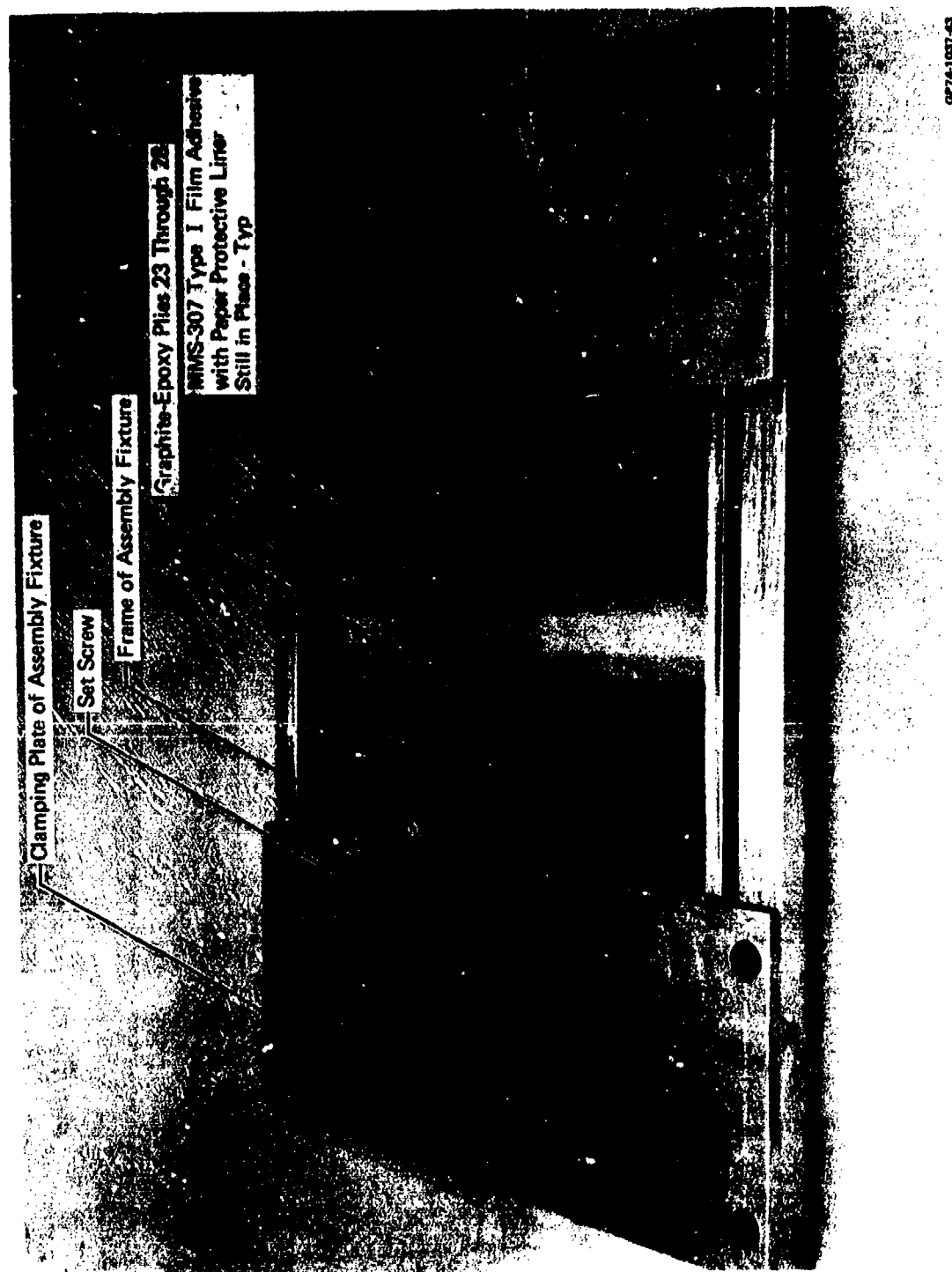
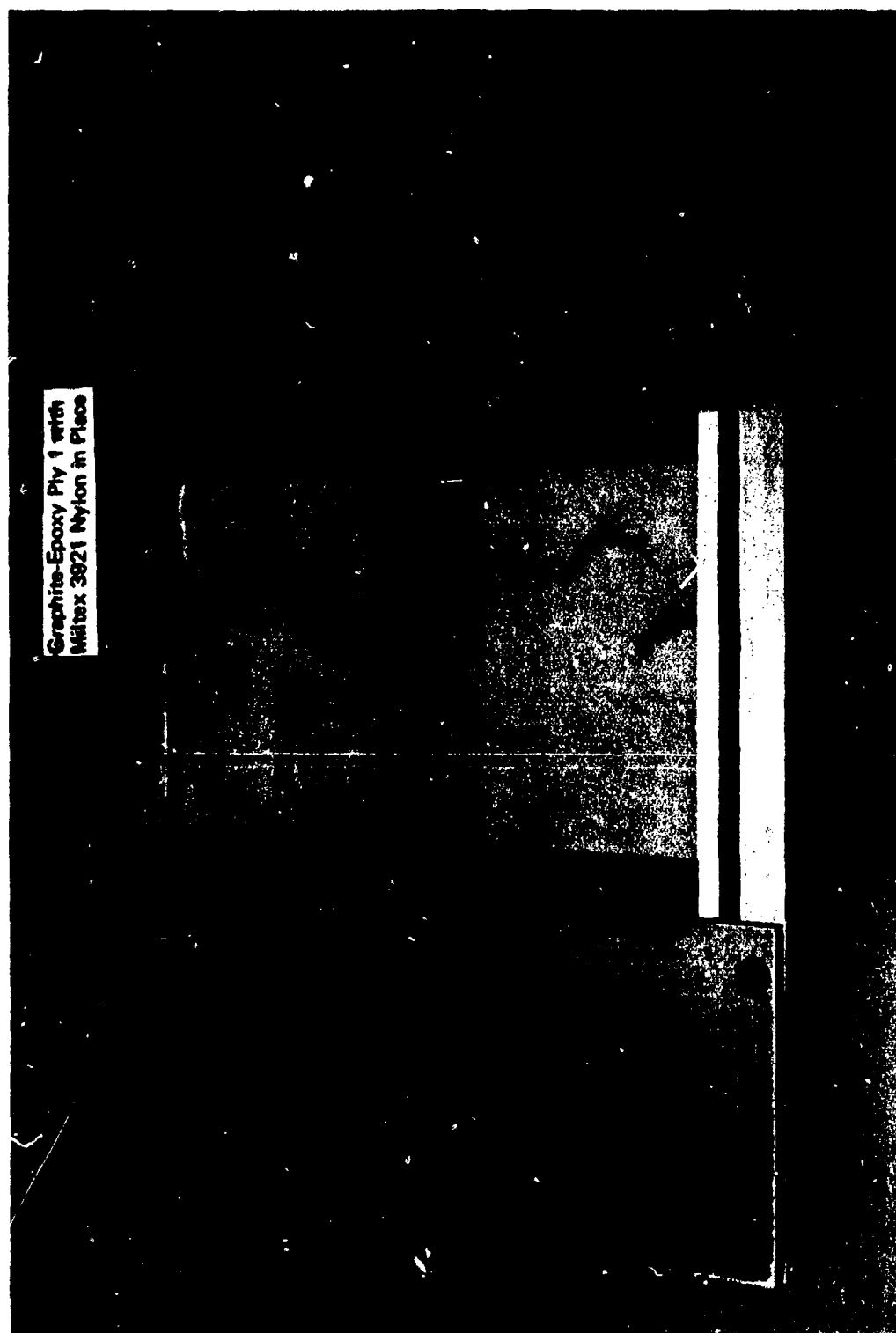


FIGURE 41 PANEL ASSEMBLY WITH GRAPHITE-EPOXY PLYS 23 THROUGH 28
AND MMS-307 TYPE I FILM ADHESIVE IN PLACE



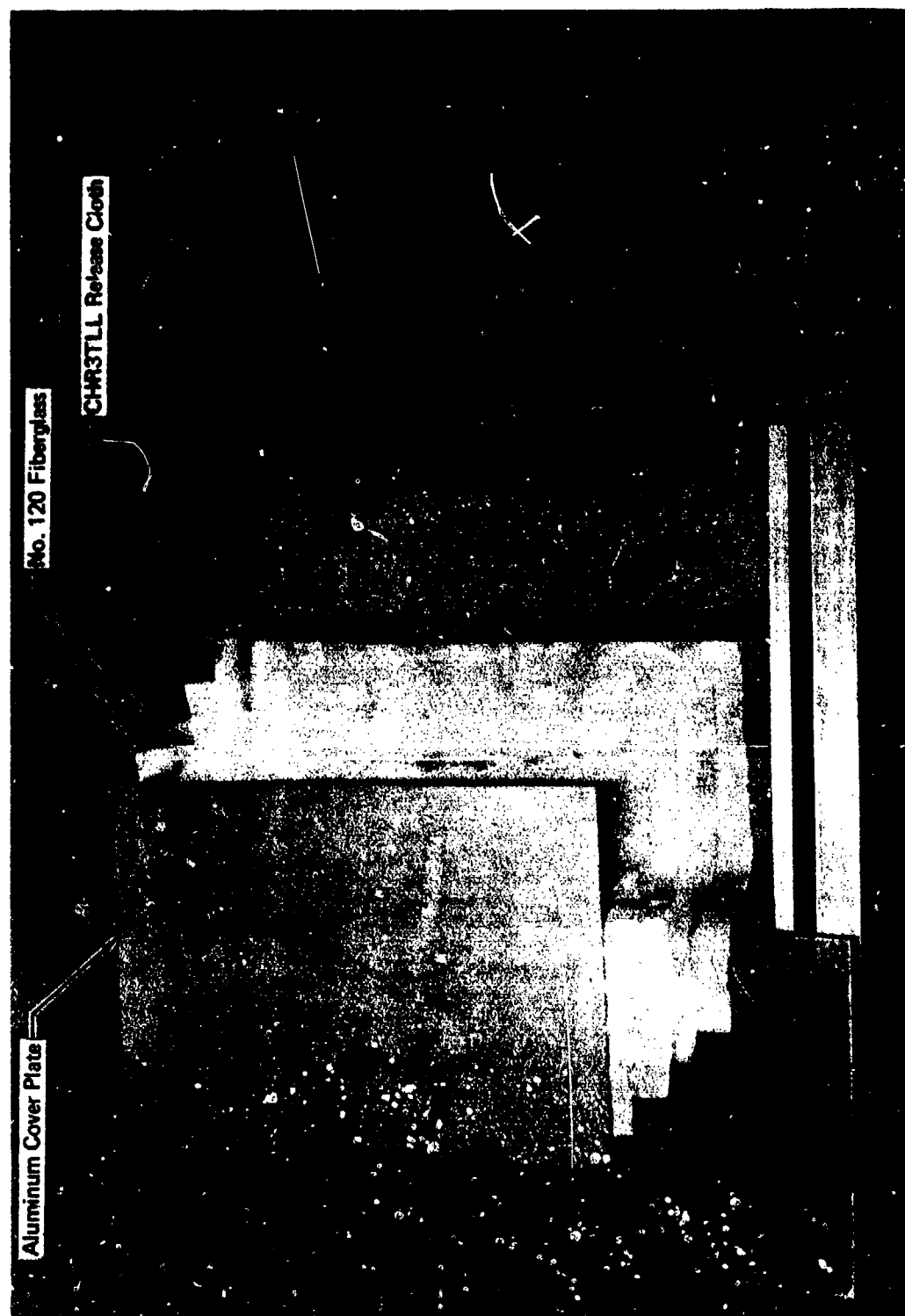
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FIGURE 42 PANEL ASSEMBLY SHOWING PARTIALLY LAID UP GRAPHITE-EPOXY LAMINATE



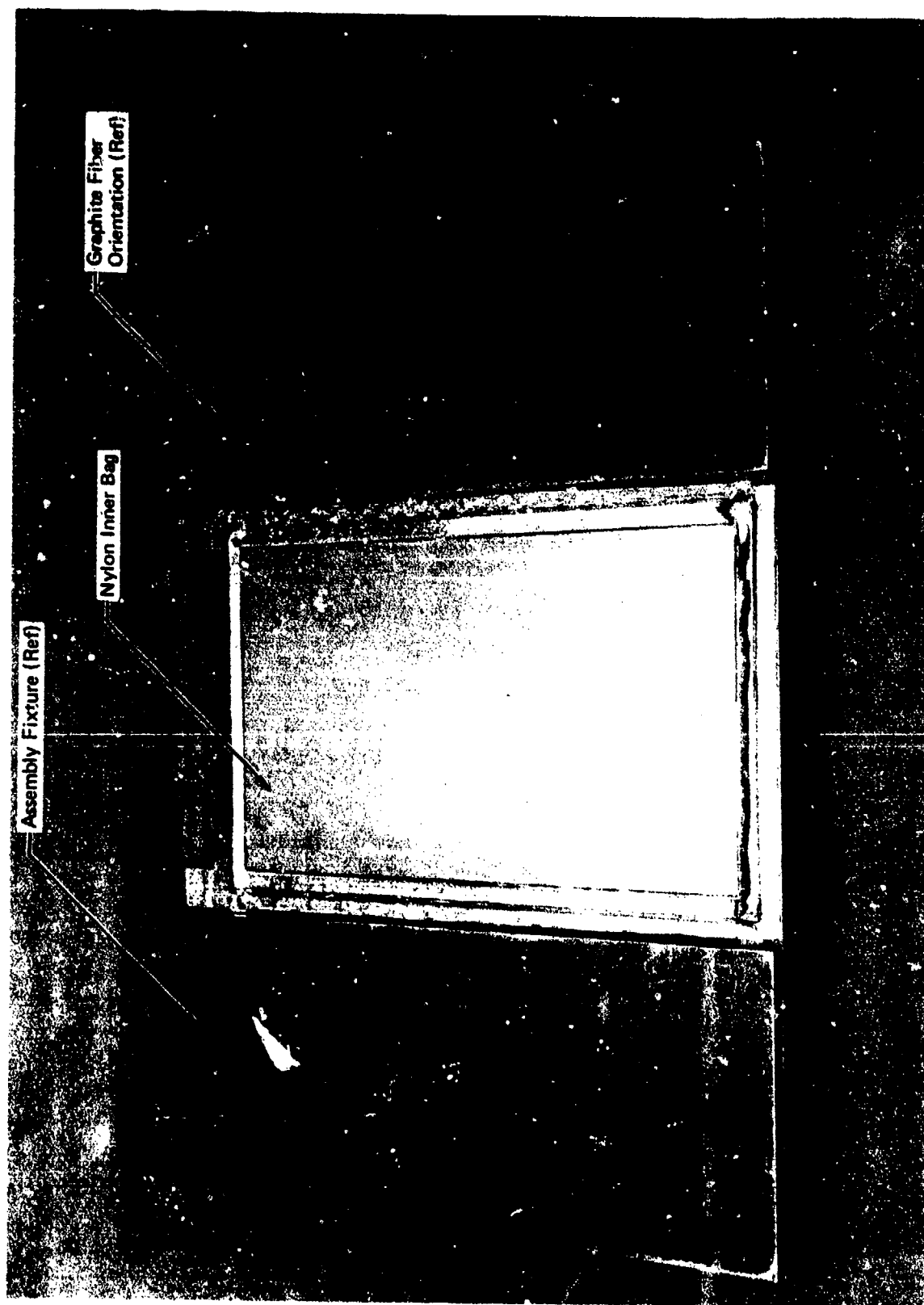
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FIGURE 43 PANEL ASSEMBLY COMPLETELY LAID UP



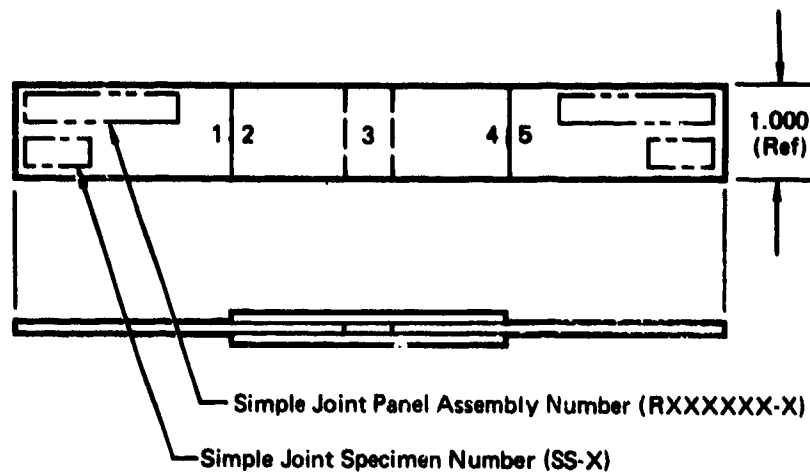
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FIGURE 44 PANEL ASSEMBLY SHOWING LAY-UP CONFIGURATION DETAILS
PRIOR TO FINAL POSITIONING

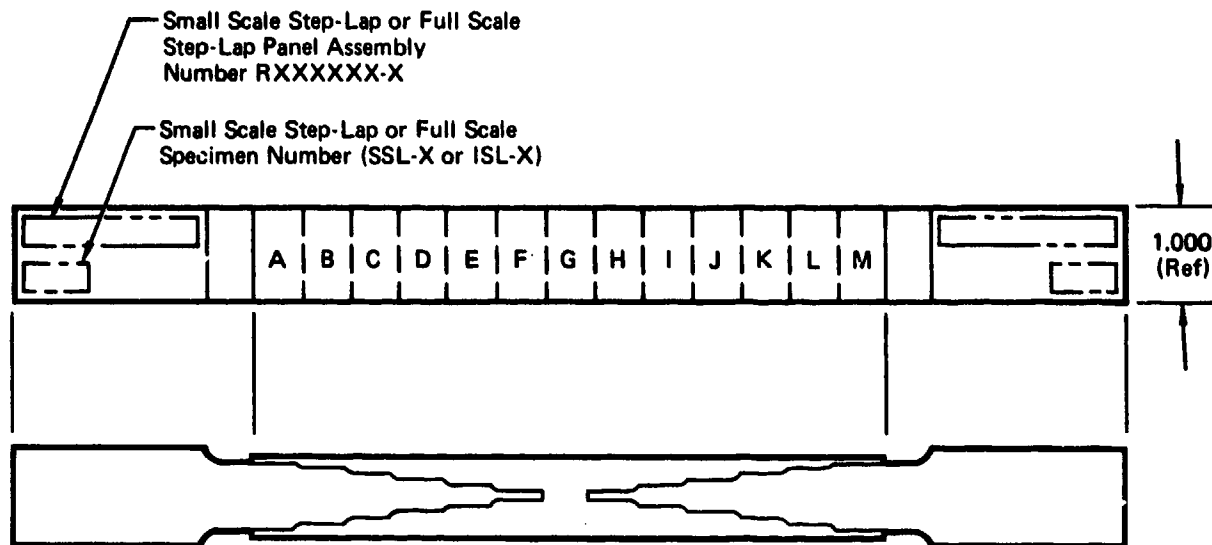


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FIGURE 45 LAY-UP CONFIGURATION PRIOR TO BEING WRAPPED IN PINK
RELEASE CLOTH AND NO. 1000 FIBERGLASS



Thickness measurements were taken at points 1 through 5 and width measurements were taken at Points 2, 3 and 4.



Thickness measurements were taken at Points A through M and width measurements were taken at Points A, G and M

1037-30

FIGURE 46 THICKNESS AND WIDTH MEASUREMENT LOCATIONS

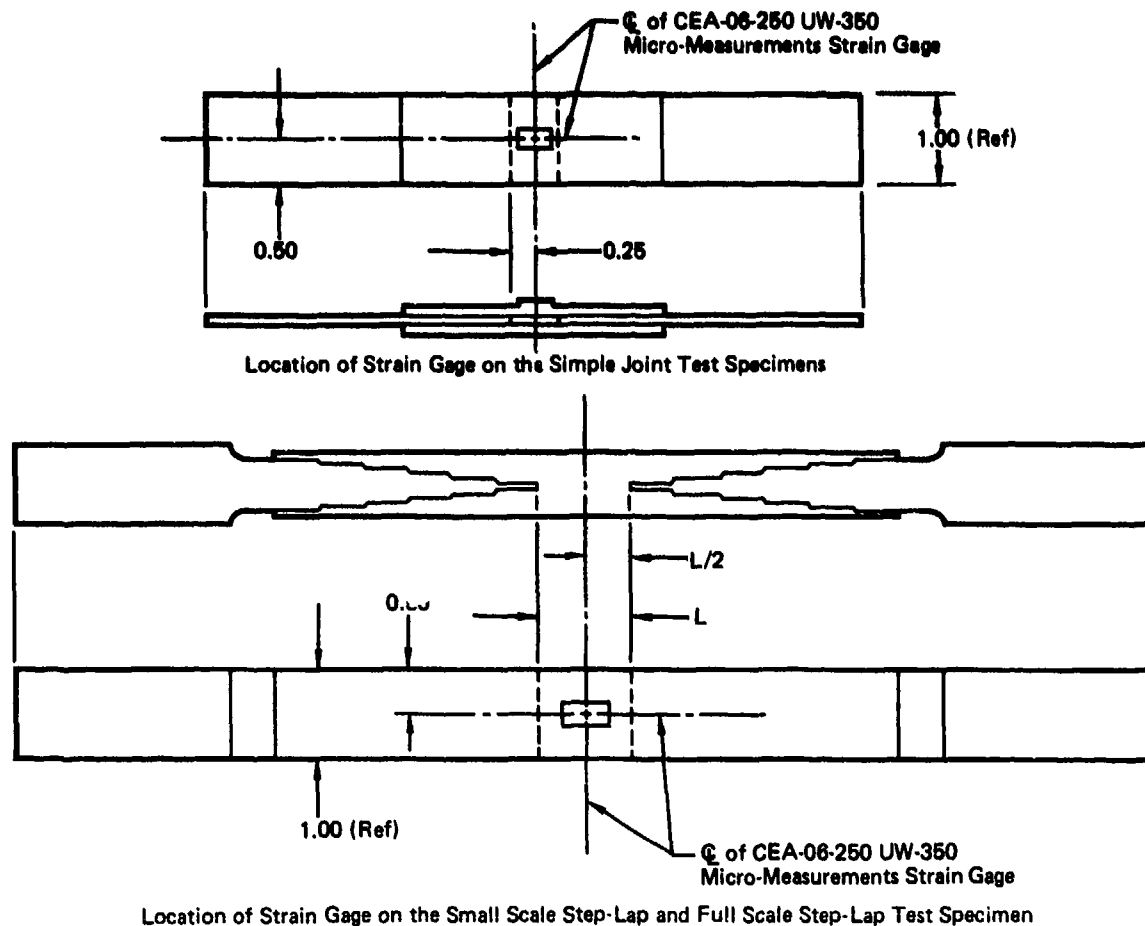


FIGURE 47 STRAIN GAGE REQUIREMENTS

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TABLE 8 AUTOCLAVE RUNS IN WHICH THE SPECIMENS WERE CURED

Run No.	Run Date	*Specimen Nos.
1	24 July 1974	SS 1-50
2	25 July 1974	SS 61-90
3	8 Oct 1974	SSL 1-20
4	11 Oct 1974	SSL 21-40
5	15 Oct 1974	SSL 41-60
6	17 Oct 1974	SSL 61-80 and 36A
7	22 Oct 1974	SSL 81-100
8	25 Oct 1974	FSL 1-20
9	5 Nov 1974	FSL 21-40
10	12 Nov 1974	FSL 41-60
11	15 Nov 1974	FSL 61-80
12	20 Nov 1974	FSL 81-90

SS - Simple Specimen
 SSL - Small Scale Step-Lap Specimen
 FSL - Full Scale Step-Lap Specimen

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3.3 Non-Destructive Testing (NDT)

Each specimen evaluated under this program was radiographically, ultrasonically and visually inspected to insure acceptable quality.

The procedures used in the conduct of these inspections are discussed in paragraph 3.3.1. The inspection standard passed by the specimens is summarized in Paragraph 3.3.2.

3.3.1 Inspection Procedures - The procedures used in the conduct of the radiographic and ultrasonic inspections are discussed below:

Radiographic - Low Kilovoltage/high contrast techniques were used in accordance with MCAIR P.S. 21206.3 "Radiographic Inspection of Honeycomb Assemblies and Composite Structures". The test parameters were as follows:

- o Kilovoltage - The kilovoltage used in each test was determined from Figure 48. The graphite-epoxy thickness was not considered in determining the kilovoltage over the titanium steps.
- o Milliamperes/Minute - These are adjusted to obtain a film density in the area of interest of 2.5 to 3.5 H and D density units.
- o Cassettes - Blackened film with 0.01 inch thick lead back screen was used.
- o Backing - 1/8 inch thick lead lying behind the cassette.
- o Processing - Automatic.
- o Focal Spot to Film Distance - 58 inches.
- o X-ray Machine Type - Constant potential, beryllium window with 0.4 and 3.0 millimeter focal spots (some radiographs were made with each size focal spot).
- o Interpretation - All interpreters are qualified to at least SNT-TC-1A level II.

Ultrasonic - The ultrasonic inspections were conducted in accordance with MCAIR P.S. 21211.4 "Ultrasonic Inspection of Honeycomb Assemblies and Composite Structures." The reflector plate technique illustrated in Figure 49 was used. The test parameters were as follows:

- o Ultrasonic Scope - Automatic Industries UM 721 (or UM 771B) with 100 pulser-receiver.
- o Search Unit - A 5 MHz, 3/4 inch diameter, 3 inch focal length, ceramic search unit was used on all the double lap specimens and small

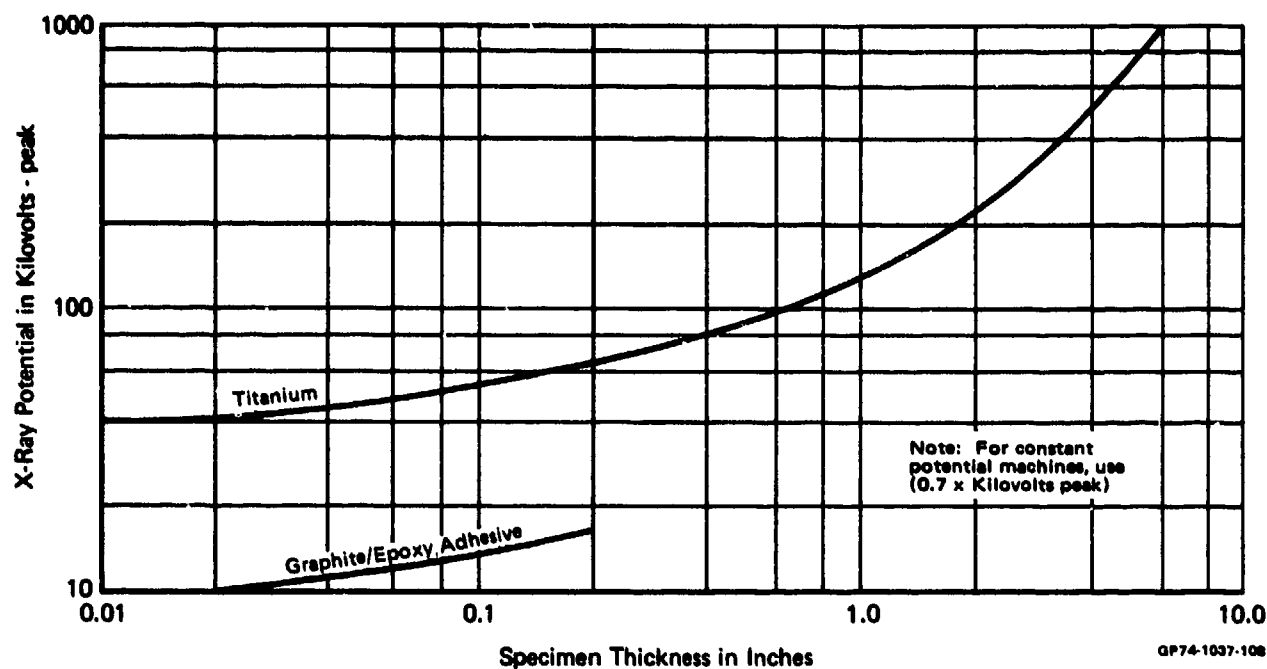


FIGURE 48 X-RAY POTENTIAL

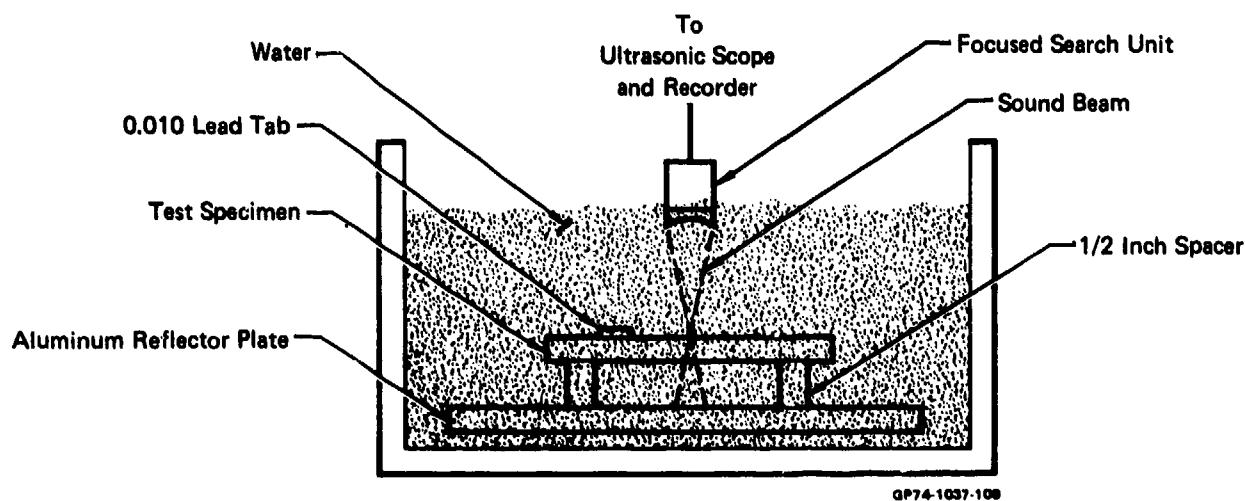


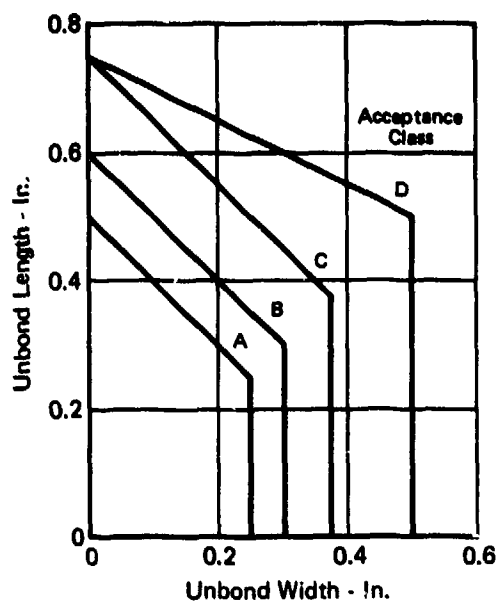
FIGURE 49 THE ULTRASONIC INSPECTION TECHNIQUE USED

scale step-lap specimens 1 through 40. In subsequent tests a 2.25 MHz, 3/4 inch diameter, 3 inch focal length, ceramic search unit was used.

- o Lead Tab - 1/4 inch diameter lead tabs, consisting of two .005 inch thick plies with adhesive backing, were used (one per step on each specimen) for calibration of the C-scan system.
- o Focusing - The search unit-to-test specimen distance was adjusted to focus round beam at sound entry surface.
- o Sensitivity - The instrument/recorder was adjusted until the print of the lead tab was actual size. Experience on other programs indicates that the minimum detectable void/unbond is about 1/8 inch in the minor direction.

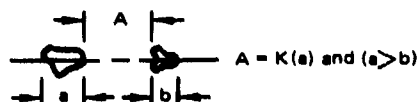
3.3.2 Specimen NDT Results - For this program a specimen was accepted if it passed the A acceptance class criteria identified in Figure 50. Ten of the full scale step-lap specimens (Numbers 44, 45, 46, 47, 51, 52, 53, 54, 58 and 59), which were laid up and cured with a total of twenty specimens on 12 November 1974, see Table 8, did not pass this criteria. These specimens had total disbond indications on the tang of one end. They would not have slipped by in a production NDT, since these specimens were being inspected by production NDT personnel and equipment. Tests were run on these specimens to verify NDT indications. As expected the strength of these specimens was inferior. This data was not used in the development of the wearout model.

These specimens are relatively narrow (one inch). For wide splice plates in representative aircraft structure a more liberal acceptance could undoubtedly be used. More effort needs to be expended in this area.



Notes:

1. W is the maximum projected unbonded width, measured across the void in the "narrow" direction. L is the projected unbonded length measured perpendicular to W.
2. The Engineering drawings, process specifications, or procurement specifications or documents shall specify the ratio (K) of the separation distance of any two voids to the dimension of the largest adjacent void where the dimension is measured along the line joining the two voids. This requirement is applicable to voids whose dimensions are smaller than the maximum allowable void for the particular class of acceptance but have minor dimensions in excess of 0.060 inches. For this program, K shall equal 4 for unbonds in the graphite to titanium joints and 8 for delaminations in the graphite/epoxy laminates.



3. Parts with any voids having a minor dimension in excess of 0.060 inch and exceeding the maximum dimensions illustrated in the figure above for the applicable class are rejectable.

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FIGURE 50 DEFINITION OF ACCEPTANCE CLASSES FOR UNBONDS

SECTION 4

RANDOM SPECTRUM DEVELOPMENT

4.1 Mission Segment Cumulative Peak Load Factor Exceedance Curves

The F-15 air superiority fighter was designed for a 4000 hour lifetime with a scatter factor of four. The planned operational usage included a specific set of missions each with its own requirements. In particular, there were four different air-to-air missions, two different air-to-ground missions, and one instrumentation and navigation training type of flight. Each of these missions was further divided into mission segments, viz. ascent, cruise, combat, descent, and loiter. The speed, altitude, and gross weight were determined for each of these segments based on optimizing the airplane performance, mission range, fuel consumption, etc. Varying external loading distributions were used for each flight condition (defined by speed, altitude, gross weight and airplane configuration) where both symmetric and asymmetric maneuvers were executed based on the mission analysis. These external loading distributions were used in combination with the cumulative peak load factor exceedance curves to determine internal structure repeated loads for critical components. Ground loads were included as specified to apply the loads on a flight by flight basis.

A schematic of the cumulative peak load factor exceedance curves for the various F-15 mission segments is shown in Figure 51. These are given in terms of peak exceedances per hour of time spent in a given segment. For each of the seven basic F-15 missions, the time spent in each mission segment is determined by the mission analysis. These time lengths are multiplied times the appropriate curve in Figure 51 to obtain the total number of peaks for the mission segments of each mission. It is apparent from Figure 51 that combat maneuvering is considerably more severe than any of the others as would be expected. In fact, when the actual number of peaks are compared for the F-15 lifetime, 87% of all peaks exceeding 2 g's and 99% of all peaks exceeding 4 g's are recorded in the combat segments.

4.2 Random Test Methodology

Cumulative load exceedance curves for the F-15 wing root bending moment fatigue spectrum have been approximated with random load level applications on a flight by flight basis. The random load wave shapes have been determined from actual aircraft maneuver time histories recorded during combat

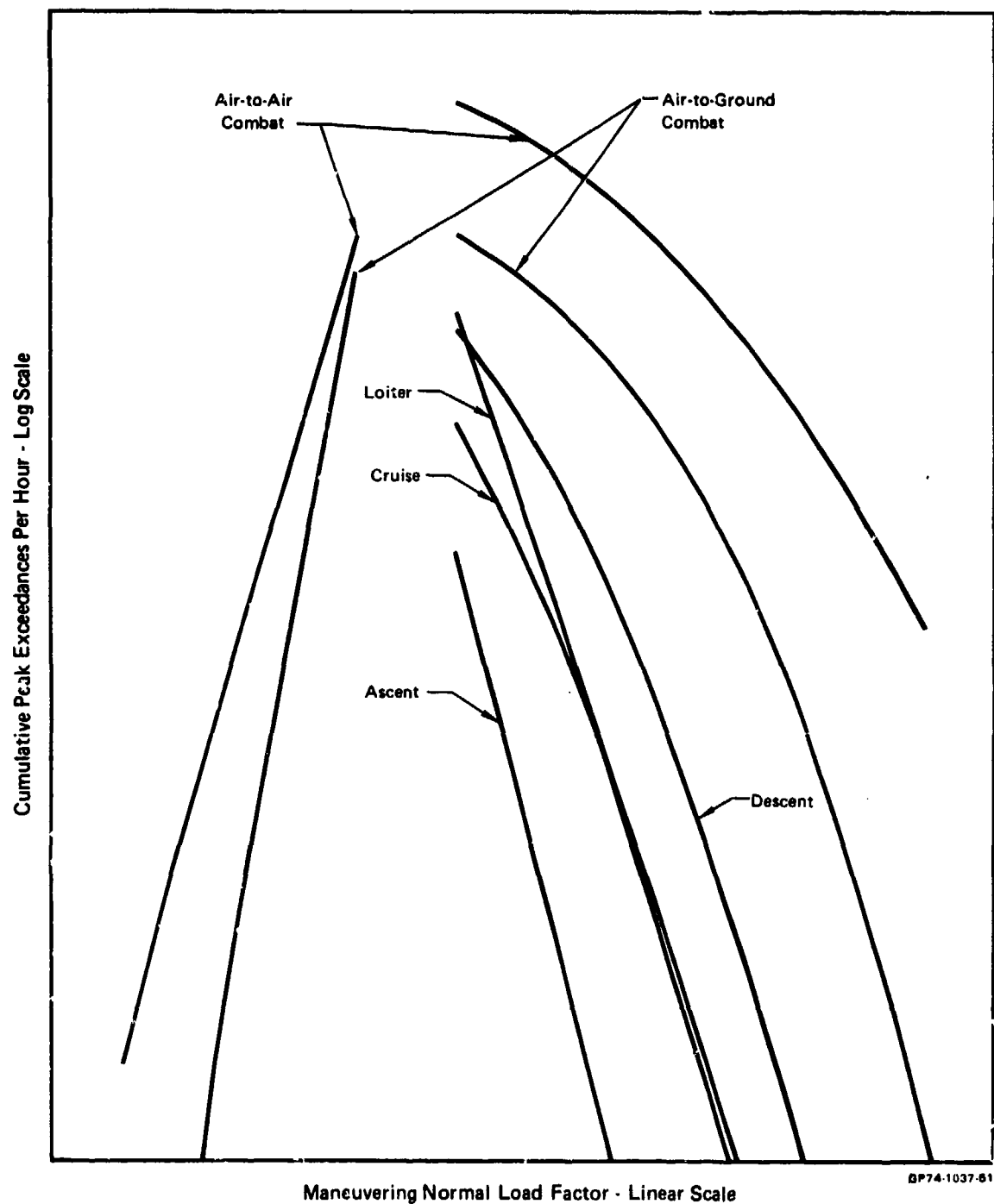


FIGURE 51 F-15 MISSION SEGMENT
Positive and Negative Peak Exceedance Curves - Maneuver Load Factor - N_z

training. The detailed technical approach for matching the cumulative load exceedance curves and aircraft maneuver wave shapes using random noise theory is described in this section. The discussion of random load fatigue test experience in paragraph 4.2.1 and the brief discussion of random noise theory in paragraph 4.2.2 are included here to provide the necessary background for the detailed development of the flight by flight random fatigue spectrum given in paragraphs 4.2.3 through 4.2.5.

4.2.1 Random Load Fatigue Experience - In order to minimize testing complexity, the sequence of load level application for aircraft structural fatigue tests has oftentimes been very ordered, e.g., Lo-Hi or Hi-Lo, and in a specified block size. The effects of sequence, block size, negative loads, etc., have therefore become the subject of many fatigue test programs. References 12, 13, and 14 are but a few examples where the fatigue life was shown to vary by as much as an order of magnitude resulting from a sequence change usually associated with a high positive or high negative load level. MCAIR has conducted literally thousands of spectrum fatigue tests in conjunction with the F-101, F-4, and F-15 structural development programs. The significant effect of load level sequence and positive and negative loads was apparent in many of these tests. Typical results on aluminum and titanium are presented in Tables 9 and 10. Although these particular tests show that the random sequence of load levels gives more life than the Lo-Hi sequence, this trend is spectrum dependent. A variation in the fatigue spectrum shape could result in a random sequence producing the lower life. A method of life prediction developed at MCAIR, which shows favorable comparisons with the test results in Tables 9 and 10, is a cumulative damage analysis technique which accounts for the stress-strain variations at the specimen notch root critical location caused by local plasticity. These inelastic effects, which contribute toward the importance of load sequence, are taken into account using Neuber's rule and the cyclic stress-strain characteristics of the material in question. Development and application of this method is discussed in References 15 and 16.

Test results discussed in the preceding paragraph are all for metal specimens, but it is expected that bonded joints would also be significantly influenced by load level sequence effects. A review of aircraft load usage time histories indicates much more of a random sequence than any kind of an

TABLE 9 COMPARISON OF PREDICTED LIFE TO ALUMINUM FATIGUE TEST RESULTS FOR SPECIMENS WITH OPEN HOLES

Spectrum Definition		Test Life Laboratory Spectrum Hours	Life Predictions	
			Conventional n/N Computations	MCAIR Method
Spectrum A	Random Sequence Without Unloading	4300	4300	4300
	Random Sequence With Unloading	3040	4300	3070
	Random Sequence With Negative Loads	1750	3920	2050
	Lo-Hi Sequence With Unloading	2700	4300	2700
	Lo-Hi Sequence With Unloading Truncated at 85%	1510	4530	1650
Spectrum B	Lo-Hi Sequence With 1G Minimum	1420	1680	1150
	Lo-Hi Sequence With -1G Minimum	680	1500	625
	Lo-Hi Sequence With -3G Minimum	380	1300	450

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TABLE 10 COMPARISON OF PREDICTED LIFE TO TITANIUM FATIGUE TEST RESULTS FOR SPECIMENS WITH OPEN HOLES

Spectrum Definition		Test Life Laboratory Spectrum Hours	Life Predictions	
			Conventional n/N Computations	MCAIR Method
Spectrum C	Random Sequence of peaks 250 hour block size. Highest load = 131.6%	94,750	94,750	94,750
	Random Sequence of Peaks 250 Hour Block Size. Highest Load = 111.8%	65,250	94,750	62,000
	Lo-Hi Sequence of Peaks 250 Hour Block Size. Highest Load = 131.6%	24,250	94,750	18,000

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orderly application. This fact is primarily what has led to random load fatigue testing in the aircraft industry. The initial step in this direction for aircraft maneuver loads was reported by Payne in Reference 17 in 1956. Analysis of aircraft maneuver loading using random noise theory was first reported in the late 1950's by Mayer and Hamer (Reference 18). Analysis of aircraft gust loading using random noise theory was initiated in an earlier time frame. Clementson and Miles, References 19 and 20, respectively, published reports on the subject in the early 1950's. Both of these papers were based on mathematical analyses of random noise developed by Rice in 1945 and presented in Reference 21. Fatigue testing using electromechanical shakers driven by a Gaussian white noise generator was the obvious next step. References 22 through 25 describe typical laboratory studies in this area spanning the time period from 1959 to 1972. These tests simulated aircraft gust loading environment. MCAIR has developed techniques for the F-15 using servohydraulic test equipment to simulate aircraft maneuver loading environment on a flight by flight basis with ground loads applied between each flight. These techniques represent the basis of the fatigue test approach used in this program. The selection of the wave form shape is based on actual fighter aircraft flight time histories of air-to-air combat maneuvering and air-to-ground combat maneuvering.

4.2.2 Random Noise Theory - If it is assumed that the load $x(t)$ on a given structural element is a stationary random function of time, the probability density function of $x(t)$ is independent of time and defined as the probability that $x(t)$ will fall within the range of x to $x + dx$ at any instant in time. If this probability density function takes on the classical Gaussian or normal form, (it should be emphasized that many random processes approach this function by virtue of the powerful central limit theorem) the time history appearance of $x(t)$ would be anywhere between the two wave shapes shown in Figure 52. The wave shape is governed by the frequency distribution of $x(t)$. The wave shape called narrow band in Figure 53 obviously consists of variable amplitude cycles of very nearly the same frequency. The term narrow band refers to the limited frequency bandwidth existing in the time history of $x(t)$. Similarly, the wave shape called wide band in Figure 53 also consists of variable amplitude cycles, but with a significant spread in the cyclic frequency. The term wide band refers to the generally unlimited frequency bandwidth existing in the time history of $x(t)$.

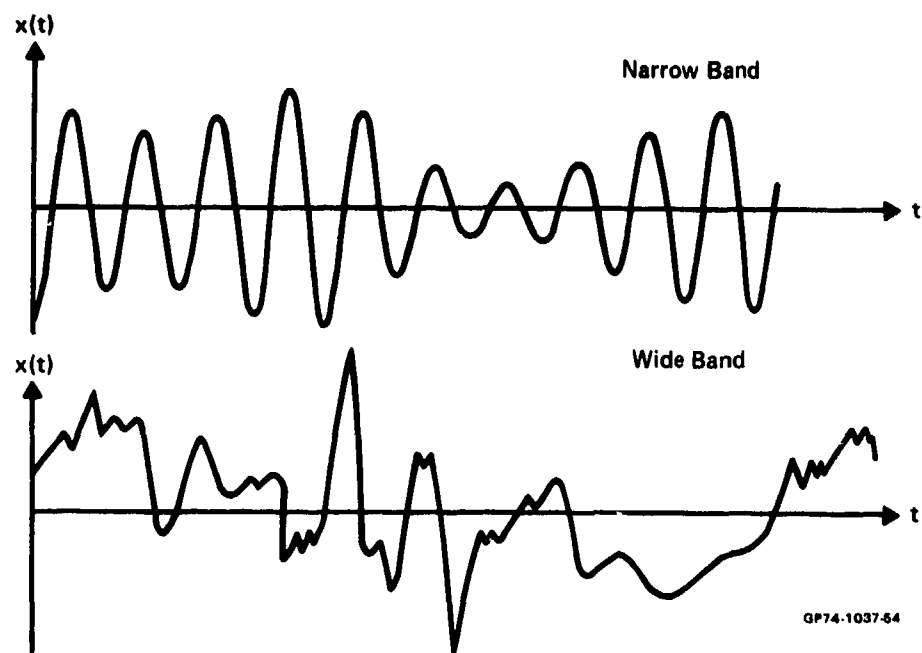


FIGURE 52 TIME HISTORY WAVE SHAPES FOR GAUSSIAN RANDOM NOISE

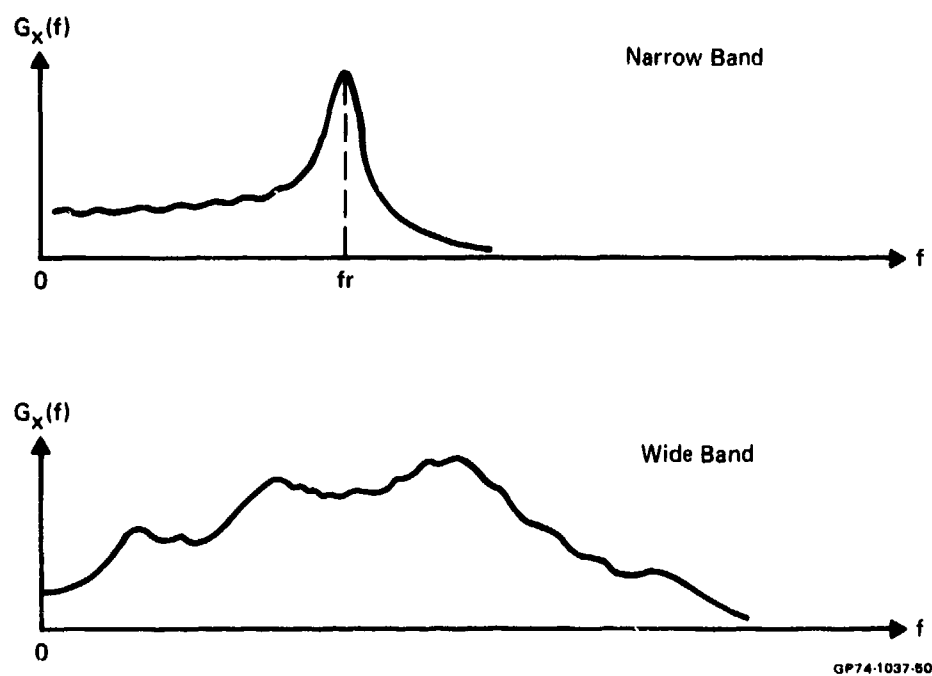


FIGURE 53 POWER SPECTRAL DENSITY vs FREQUENCY

The frequency distribution of $x(t)$ which governs its wave shape is specified by $G(f)$, the power spectral density of $x(t)$. It quantitatively defines the density of the mean square value of $x(t)$ at any given frequency. The integration of this density, therefore, over the entire range of frequencies yields the mean square of $x(t)$. The power spectral densities for the time histories in Figure 52 are presented in Figure 53. The mean square value of $x(t)$ is given by the area under the Figure 53 curve. The square root of this area is the root mean square (RMS) value for $x(t)$. The mean square value of $x(t)$ is specifically called the autocorrelation function $R(\tau)$ at $\tau = 0$. The autocorrelation function is determined from $x(t)$ as follows:

$$R(\tau) = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T x(t) x(t + \tau) dt \quad (6)$$

As indicated earlier the equation above for $R(\tau)$ evaluated at $\tau = 0$ gives the mean square value of $x(t)$. The autocorrelation function and the power spectral density are related by the Fourier inversion formulae:

$$G(f) = 4 \int_0^{\infty} R(\tau) \cos 2\pi f \tau d\tau \quad (7)$$

$$R(\tau) = \int_0^{\infty} G(f) \cos 2\pi f \tau df \quad (8)$$

It is of interest to note that if τ is set equal to zero in the second equation above, it reduces to the integration of the power spectral density over the entire range of frequencies which then equals the autocorrelation function at $\tau = 0$ or the mean square value of $x(t)$ as stated above.

If the probability distribution of $x(t)$ is Gaussian, the probability distribution of the maxima or peaks of $x(t)$ will either be Gaussian, Rayleigh, or somewhere in between depending on the power spectral density of $x(t)$. In particular for a narrow band process, the probability density of the peaks of $x(t)$ is Rayleigh. For a wide band process, the probability density of the peaks is Gaussian. In terms of structural fatigue design criteria, the distribution of peaks is usually defined by cumulative peak exceedance curves. For a frequency distribution between the two extremes of narrow and wide band random noise, the cumulative peak exceedance N_x is given as follows:

$$N_x = N_p P(x/a\sigma) + N_o [1 - P(x/b\sigma)] e^{-x^2/2\sigma^2} \quad (9)$$

where N_p = total number of peaks per unit time
 N_o = total number of zero (or mean level) crossings per unit time with positive slope
 $P(x/a\sigma)$ = probability of exceeding $x/a\sigma$ determined from a standard Gaussian or normal probability table
 σ = root mean square (RMS) of $x(t)$
 $a = \sqrt{1 - (N_o/N_p)^2}$
 $b = a/(N_o/N_p)$

It is of interest to note the variation in N_x with the ratio N_o/N_p sometimes called the irregularity factor. For $N_o/N_p = 1$, $a = b = 0$ and therefore $P(x/a\sigma) = P(x/b\sigma) = 0$ which gives

$$N_x = N_p e^{-x^2/2\sigma^2} \quad (10)$$

which is the Rayleigh distribution. This should represent a narrow band process. Figure 52 demonstrates this fact since it is apparent that the number of peaks equals the number of zero crossings (with positive slope) for the narrow band time history. For $N_o/N_p = 0$, $a = 1$ and $b \rightarrow \infty$ and therefore $P(x/b\sigma) = 1$ which gives

$$N_x = N_p P(x/\sigma) \quad (11)$$

which is the Gaussian distribution. This should represent a broad band process. Figure 52 also demonstrates this fact since it is apparent that the number of peaks is much greater than the number of zero crossings (with positive slope) for the broad band time history. The calculation of N_o/N_p is based on the following equations:

$$N_o^2 = \frac{\int_0^\infty f^2 G(f) df}{\int_0^\infty G(f) df} \quad (12)$$

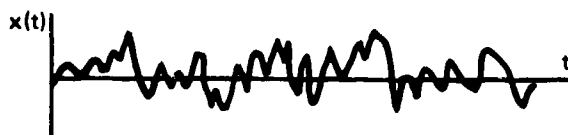
$$N_p^2 = \frac{\int_0^\infty f^4 G(f) df}{\int_0^\infty f^2 G(f) df} \quad (13)$$

4.2.3 Load Time History Wave Shape - The frequency distribution which governs the load time history wave shape is specified by the curve of power spectral density (PSD) versus frequency. In order to determine appropriate PSD versus frequency curves for fighter aircraft, actual load factor time histories from F-4's were analyzed. A total of 5,658 seconds of air combat maneuvering training data and 15,675 seconds of air to ground combat maneuvering training data were included in the calculations. These data were digitized and then numerical techniques used to perform the integration specified in Figure 54 where $x(t)$ represents a typical load factor time history. The resulting PSD versus frequency curves for air to air maneuvering and air to ground maneuvering are shown in Figure 55 and 56, respectively. A side by side comparison of an actual load factor time history during air combat maneuvering and a Gaussian random noise time history with the air to air PSD is presented in Figure 57. The one to one likeness of the two charts is considered to represent the primary justification for utilizing this approach in fatigue testing.

4.2.4 Cumulative Peak Exceedances - Press, et al. in Reference 26 presents a method of fitting measured gust peak distribution curves with combinations of Rayleigh distributions with different RMS values. Their method is based on an approximation of the peak distribution by the level crossing distribution which is always Rayleigh as shown by Rice in Reference 21 for a Gaussian random process. This same approximation is made by Manning, et al, in Reference (8). However, this approximation using the Rayleigh is

Autocorrelation Function

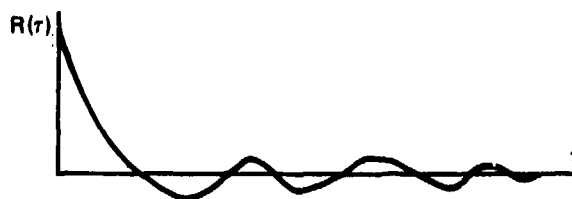
$$R(\tau) = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T x(t) x(t + \tau) dt$$



Note: x is Variation from Mean

Power Spectral Density - PSD - G(f)

$$G(f) = 4 \int_0^{\infty} R(\tau) \cos 2\pi f \tau d\tau$$



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FIGURE 54 COMPUTATIONS FOR PSD

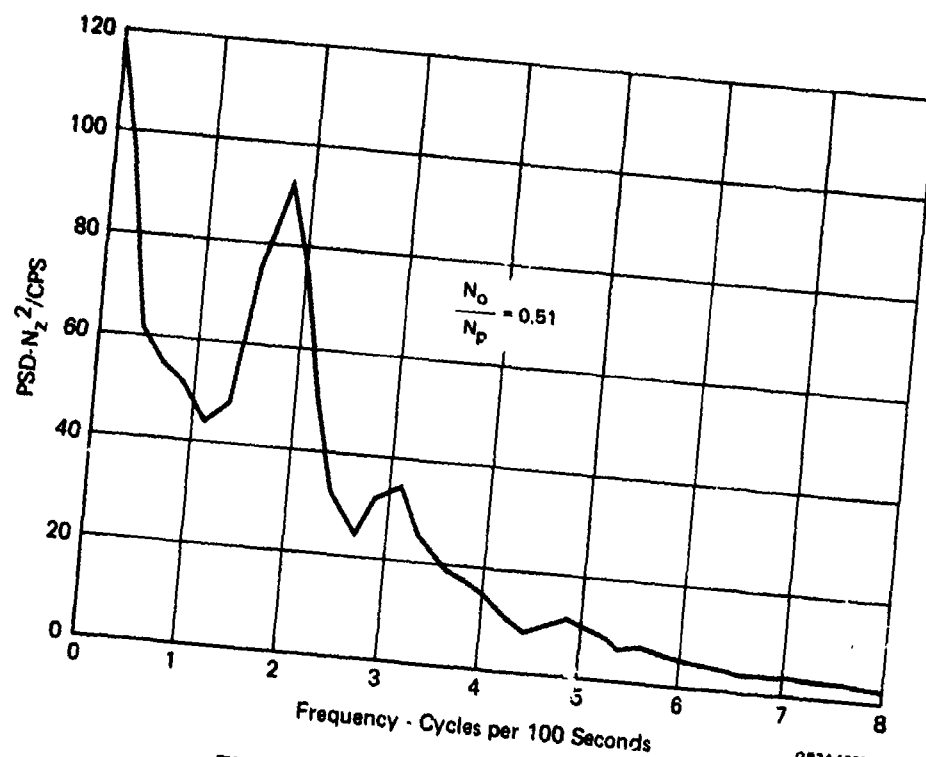


FIGURE 55 PSD vs FREQUENCY
Air-To-Air Training Data - 5658 Seconds

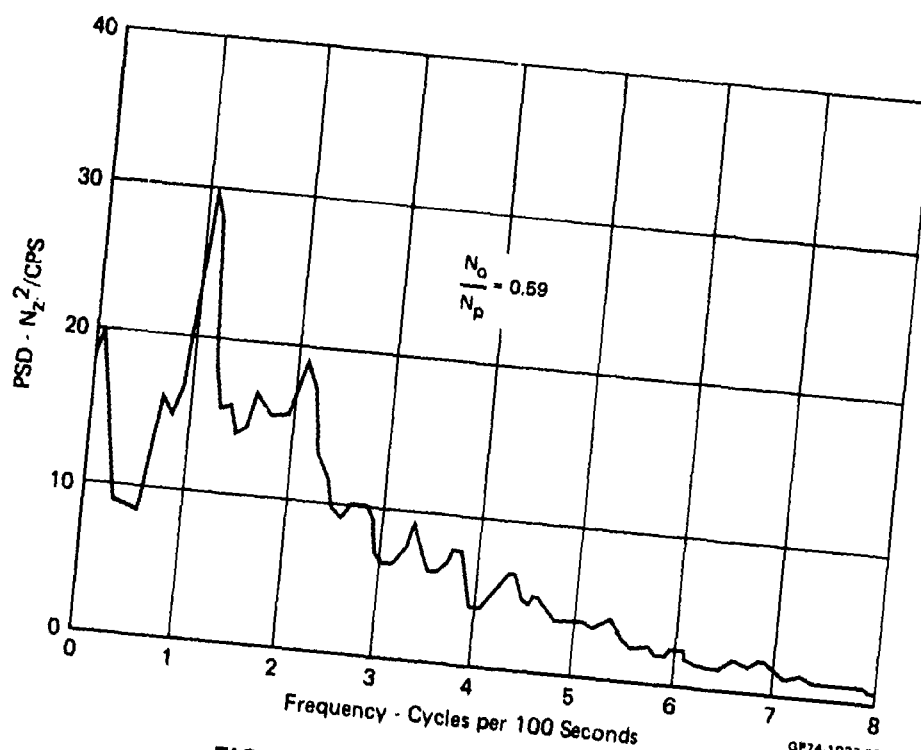


FIGURE 56 PSD vs FREQUENCY
Air-To-Ground Training Data - 15,675 Seconds

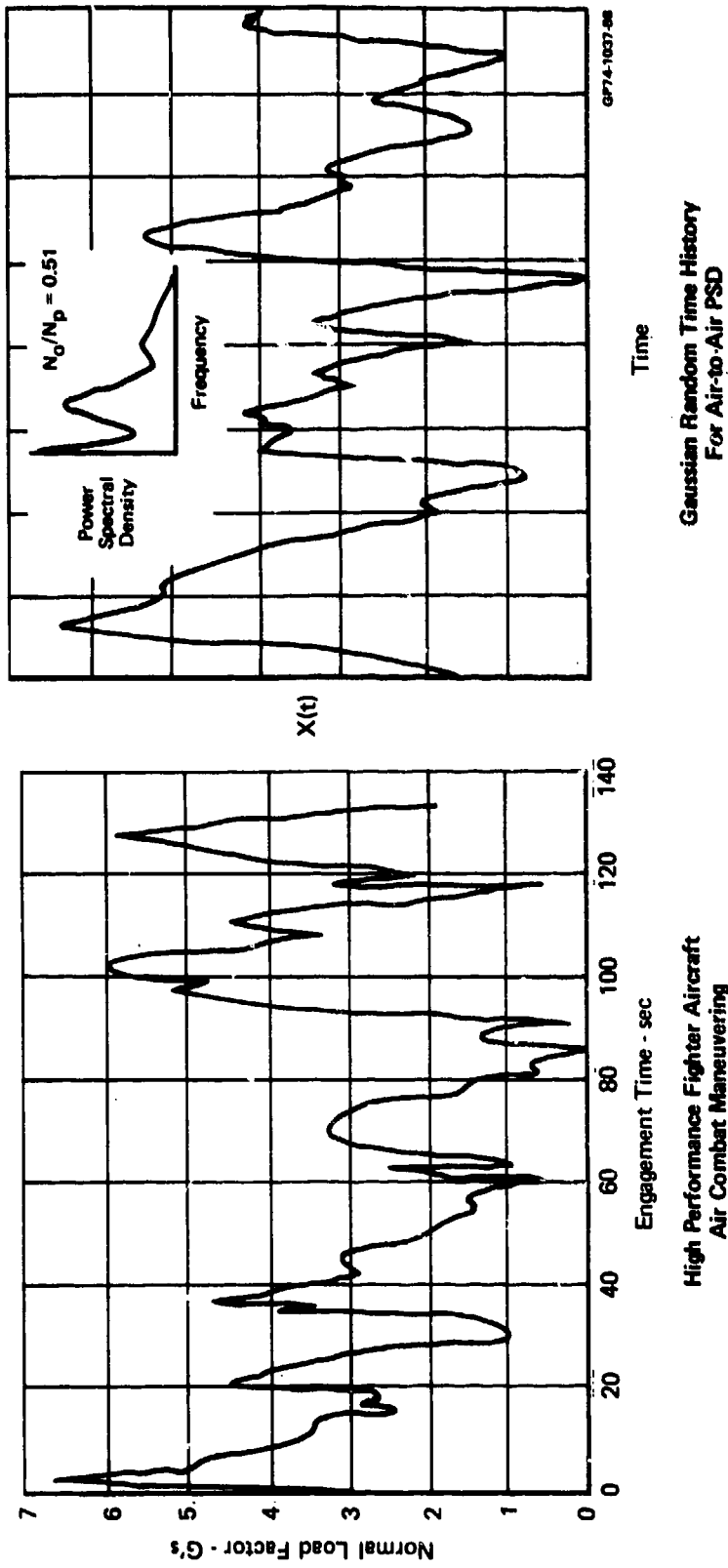


FIGURE 57 COMPARISON OF ACTUAL LOAD FACTOR
TIME HISTORY WITH A GAUSSIAN RANDOM
NOISE TIME HISTORY

considered unnecessary since the exact distribution of peaks is readily determined as discussed in the following paragraphs.

Rice derived the exact probability density function for peaks and presented it as Equation 3.6-5 in Reference 21. The equation appears rather unwieldy but in fact is relatively straightforward. Huston and Skopinski in Reference 27 modified the terms, somewhat simplifying the appearance of the equation, and integrated it to obtain the number of peaks per unit time exceeding any given value of x . The resulting expression is given by Equation 9 in Section 4.2.2. This equation became more widely publicized when it was presented in Reference 28 by Bendat, et.al., in 1961. Then in 1964, Bendat used the equation again in a discussion of peaks, fatigue damage, and catastrophic failures in Reference 29. The equation requires only simple computations utilizing a standard Gaussian probability table. It includes basically four constants, viz., the total number of peaks N_p , the irregularity factor N_0/N_p and the mean and RMS values for $x(t)$. This provides reasonable flexibility to fit most aircraft cumulative peak exceedance curves, especially when the random process can also be clipped at one end or the other or both and added to another random process with different mean and RMS values. A typical theoretical exceedance curve using the equation above is shown in Figure 58. Another exceedance curve using a smaller RMS value is shown in Figure 59 and the sum of the two is shown in Figure 60. The peak exceedance curves in Figures 58 through 60 define the number of times in the random load excursions that the peak of a cycle exceeds a given load level in the positive direction in 1000 spectrum hours. Similarly, the valley exceedance curves define the number of times in the random load excursions the valley or trough of a cycle exceeds a given load level in the negative direction in 1000 spectrum hours.

4.2.5 Flight by Flight Spectrum - The step by step procedures for the flight by flight random spectrum generation are as follows:

- o Continuous Gaussian random noise signal is generated using a specified PSD shape and RMS level.
- o The continuous time history is digitized and transcribed onto computer compatible magnetic tape.
- o A computer program is written to count the peaks and valleys to verify conformance with theoretically derived exceedance curves.
- o Incremental segments of the digitized time history are separated by digitally added ground cycles to form the flight by flight spectrum.

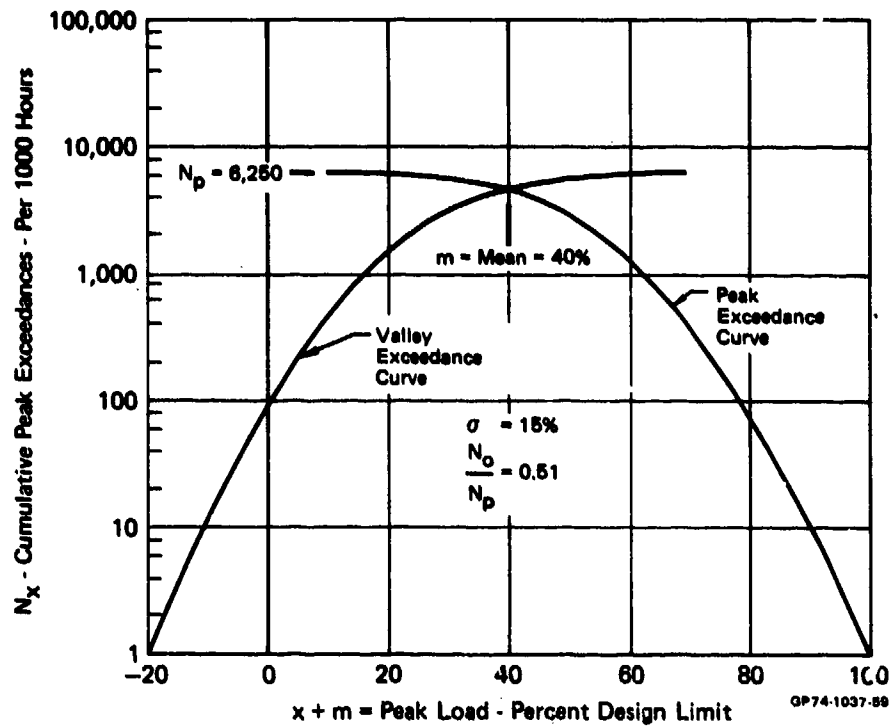


FIGURE 58 TYPICAL EXCEEDANCE CURVES

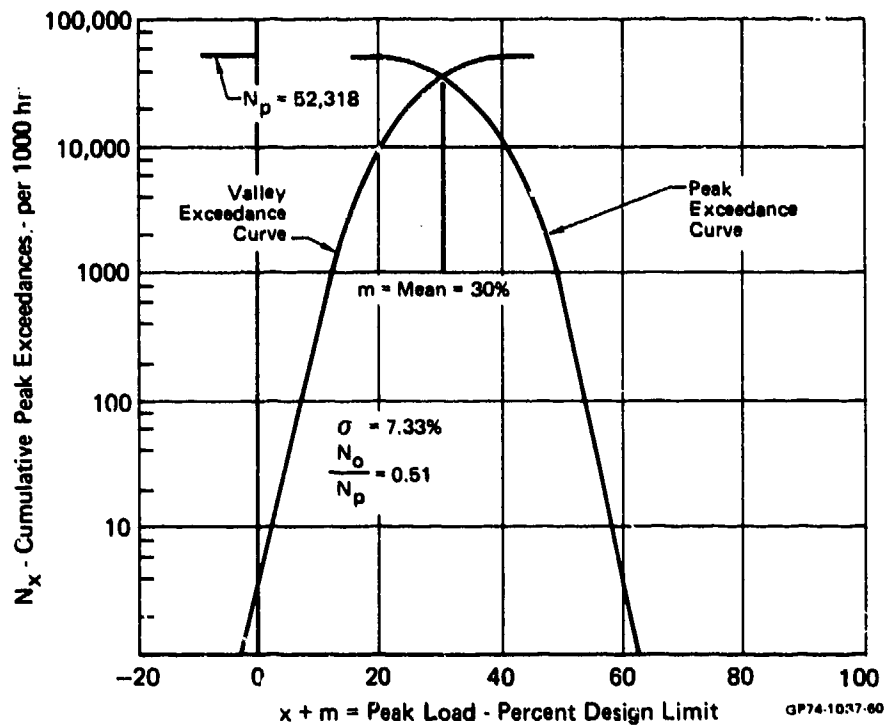


FIGURE 59 TYPICAL EXCEEDANCE CURVES (LOWER RMS)

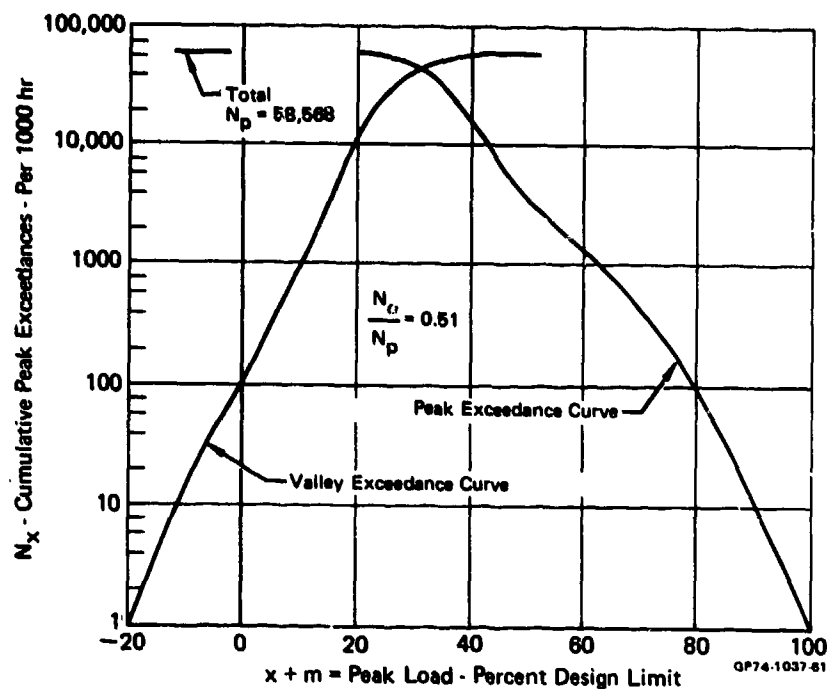


FIGURE 60 SUM OF TWO EXCEEDANCE CURVES

- o A digital to analog subsystem converts the digitized flight by flight spectrum to a corresponding analog signal required for the fatigue test machine.

The spectrum includes a total of 720 flights or missions in 1000 hours. The detailed listing for the test sequence of the various F-15 missions is as follows:

25 missions of A-A1 followed by
 52 missions of A-A2 followed by
 77 missions of A-A3 followed by
 28 missions of A-A4 followed by
 177 missions of A-G followed by
 25 missions of A-A1 followed by
 52 missions of A-A2 followed by
 78 missions of A-A3 followed by
 28 missions of A-A4 followed by
 178 missions of A-G

1000 hours of F-15 usage

It is expected that the F-15 operational usage will include deployment in particular modes of operation for extended periods of time rather than a completely erratic mission mixture. The above sequencing of missions wherein air-to-air missions are grouped together and air-to-ground missions are grouped together was selected on that basis. The four air-to-air missions are different with respect to fatigue loading primarily as a result of different lengths of time in the combat maneuvering segment. The A-A4 (air to air four) mission is more severe than A-A3 on a per mission basis; A-A3 is more severe than the A-A2; A-A2 is more severe than A-A1. The A-G (air-to-ground) mission is about equal in severity to A-A1. Each of the 720 missions in the 1000 hour sequence is in general different since each consists of a different sample of the governing random process. This complete 1000 hour record was analyzed; in particular, peaks and valleys were counted when there was at least an equivalent 1.00 g rise and 0.75 g fall or vice versa which represents the techniques used in developing the F-15 cumulative peak exceedance curves. In addition, the irregularity factor N_o/N_p for the complete 1000 hours was computed as were the power spectral density shapes. These computations provided satisfactory comparisons with the desired cumulative peak exceedance curves and time history wave shapes. The final 1000 hour tape was applied over and over again in the fatigue testing so that all specimens were subjected to exactly the same repeated loading history. Example time histories of the various missions and comparisons to the semi random spectrum used in the F-15 full scale fatigue test are presented in Figures 61, 62 and 63.

Two random spectra were developed to evaluate the effect of adding low load level cycles. The parameters used for these spectra are given in Figure 64. Random spectrum #2 is the same as #1 except an additional time burst of a lower RMS signal is added before and after the Random Spectrum #1 cycles in each mission. A comparison of the time histories of these two spectra is given in Figure 65. It should be emphasized that these added low load cycles would be expected to occur in the combat segments; the non-combat segments such as the cruise segment also have low load level cycles but only an insignificant number compared to combat. A third time history shows another variation to Random Spectrum #1 wherein hold time is added at zero load. A comparison of the peak exceedances per 1000 hours for Random Spectrum #1 and #2 is given in Figure 66. A comparison to the semi-random spectrum is also shown.

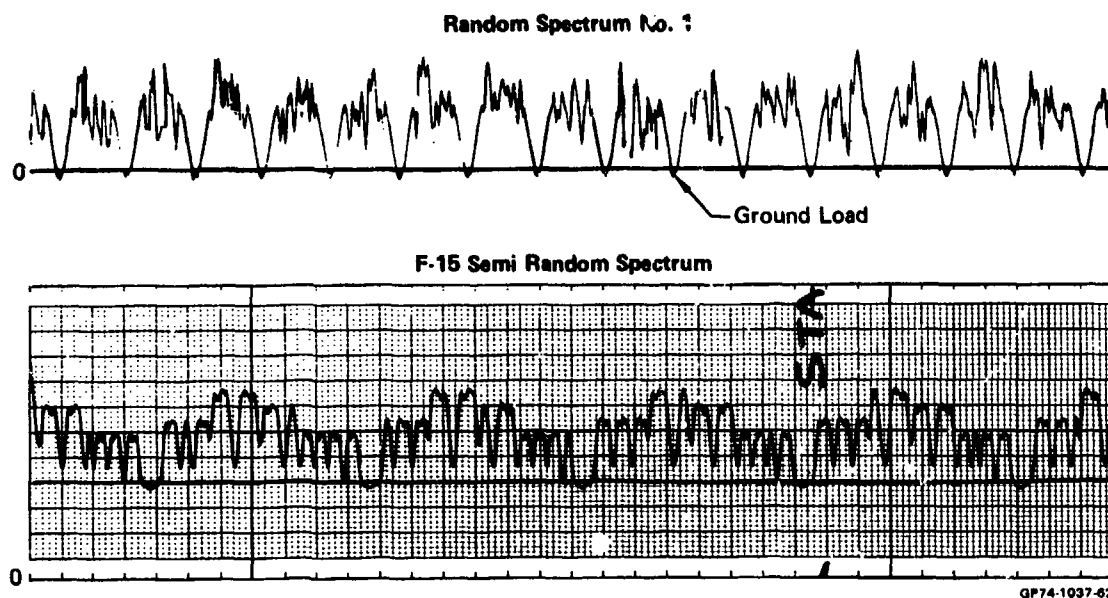


FIGURE 61 EXAMPLE TIME HISTORY OF A-A2 MISSIONS

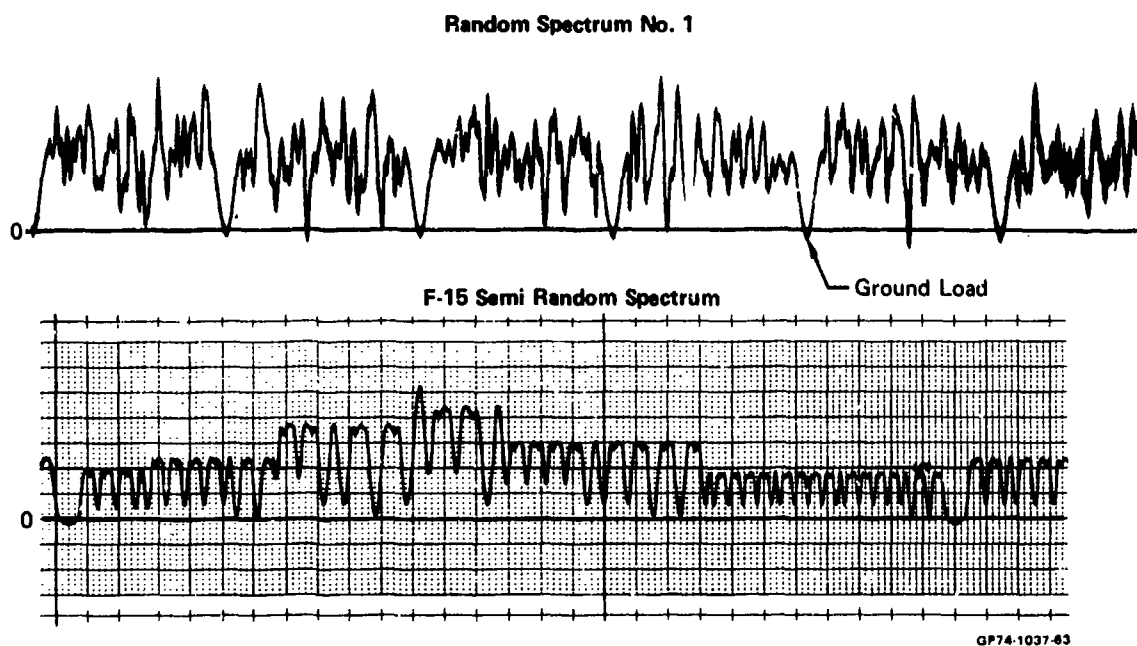


FIGURE 62 EXAMPLE TIME HISTORY OF A-A4 MISSIONS

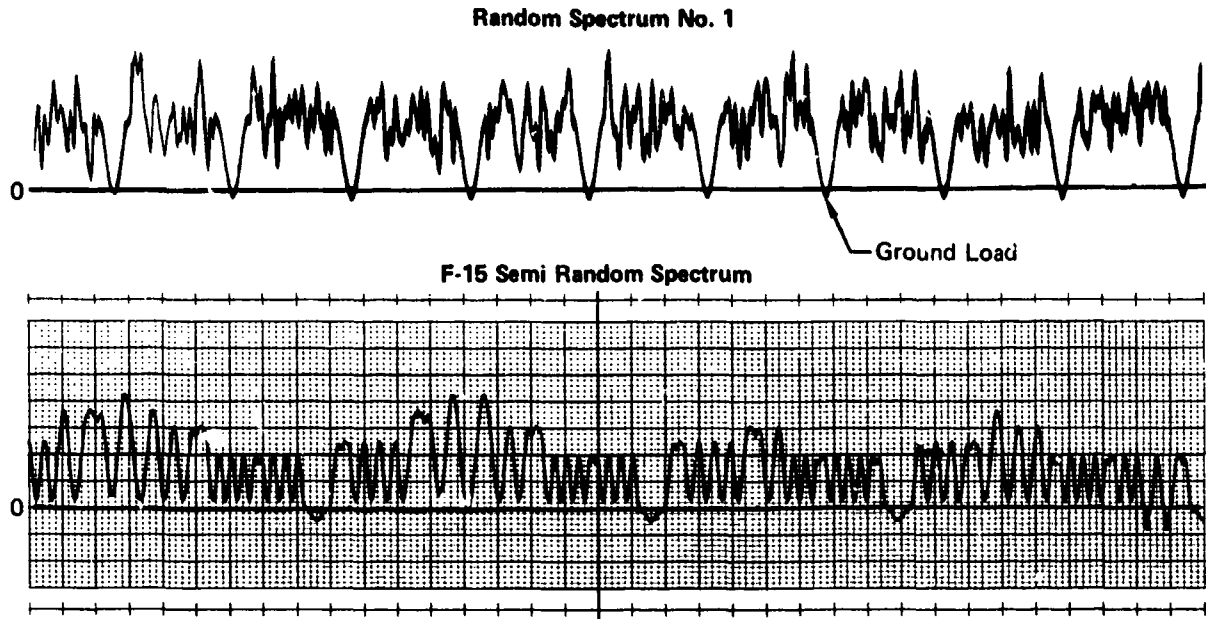


FIGURE 63 EXAMPLE TIME HISTORY OF A-G MISSIONS

GP74-1037-64

Spectrum	Percent Design Limit		N_p	N_o/N_p
	Mean	RMS		
Random Spectrum No. 1				
Air-To-Air	40%	15%	6,250	0.51
Air-To-Ground	31%	12%	4,500	0.59
Random Spectrum No. 2				
Same as No. 1 Plus				
Air-To-Air	30%	7%	52,318	0.51
Air-To-Ground	30%	7%	13,736	0.59

GP74-1037-65

FIGURE 64 PARAMETERS FOR DIFFERENT RANDOM SPECTRA

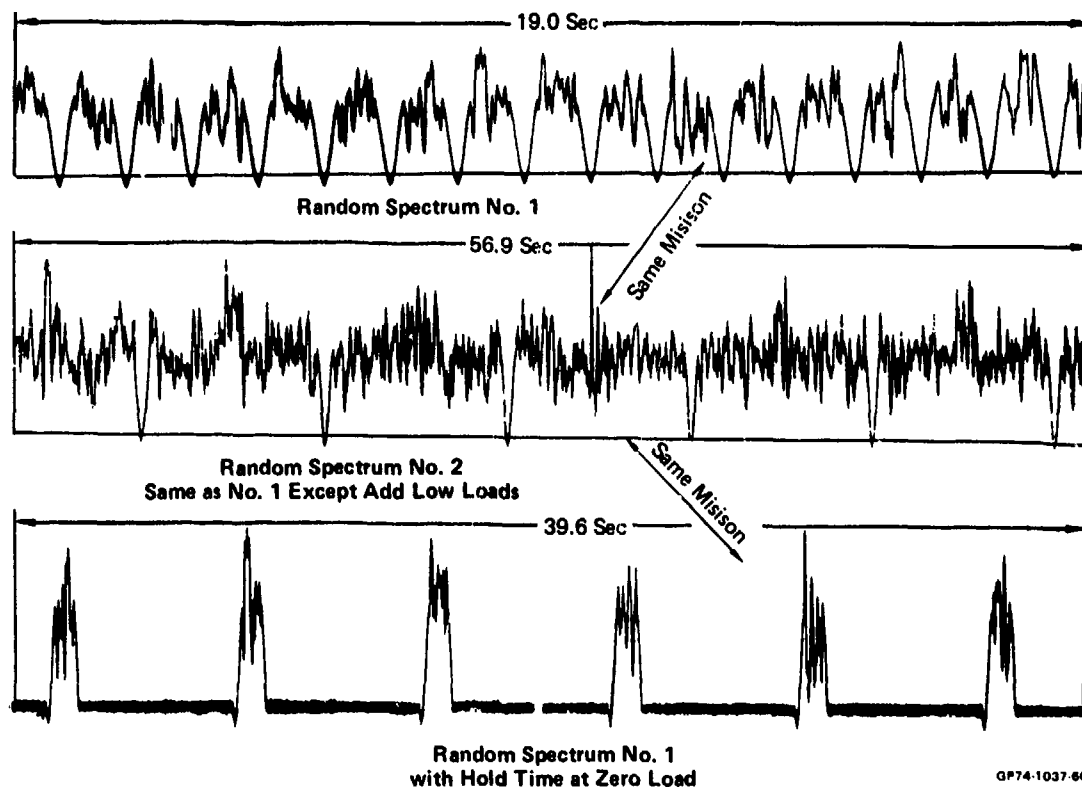


FIGURE 65 COMPARISON OF VARIATIONS IN RANDOM SPECTRUM

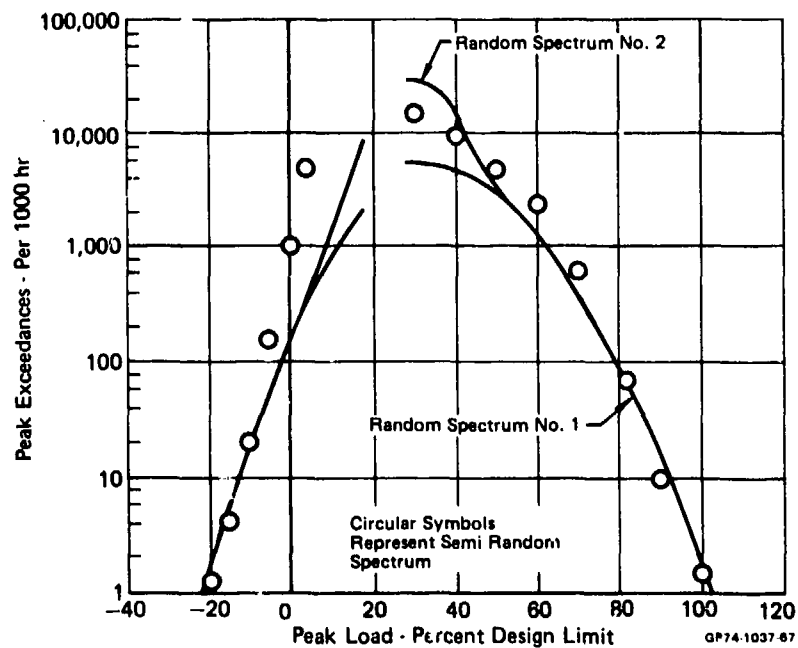


FIGURE 66 FATIGUE SPECTRA COMPARISON

SECTION 5

EXPERIMENTAL PROGRAM

In this program 34 static strength tests, 104 fatigue tests, and 50 residual strength tests were conducted. Test procedures and results are presented in the three paragraphs below. The mean, standard deviation and coefficient of variation for each of the data sets is presented. Standard formulas were used in their determination for the static strength data. Graphical procedures were used for the lifetime and residual strength data to compensate for fatigue life runouts and premature residual strength failures.

5.1 Static Strength Tests

All static strength testing was done on a Baldwin 30,000 pound universal test machine and the test set-up is shown in Figure 67. All specimens were strain gauged and a deflection gauge was placed between the grips of the test machine. Load was applied continuously to failure at a rate of .050 in/min. Before any tests were run, the temperature and humidity in the lab were checked to insure that they were in the approved ranges (~~68-72~~°F and 50-70% relative humidity). Several specimens were tested at 350°F on the same machine and were enclosed in an air circulating oven. Specimens were heated to 350°F, held at this temperature for ten minutes and then loaded as described above. Results of tests of full scale step-lap, small scale step-lap and simple specimens are presented in Tables 11 through 14. Results of 27 static strength tests run under the verification task are presented in Table 2 in Section 2.

5.2 Fatigue Life Tests

Each fatigue test was done in one of three 150,000 pound fatigue machines (see Figure 68). Hydraulic load cylinders were each controlled by a load feedback servo system programmed by a magnetic tape function generator. A strip chart recorder was used to make a continuous record of both the programmed signal and the loading applied during the test. The temperature and humidity of the air around the specimens were controlled so that they were within the required ranges.

Four tapes, numbers 1, 2, 3, 4, were used in the conduct of these tests. Tape 1 is the baseline spectrum called Random Spectrum #1 in Section 4. Tape 2 has a considerable number of low load levels added to Tape 1 and is called Random Spectrum #2 in Section 4. Tape 3 is the same as Tape 1 with frequency of load application reduced by a factor of eight. Tape 4 is the same as Tape 1 with hold time between missions increased by a factor of ten.

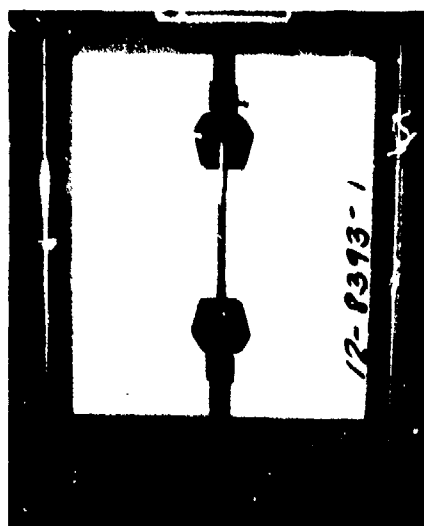


FIGURE 67 STATIC STRENGTH TEST SETUP

TABLE 11 STATIC STRENGTH TESTS OF FULL SCALE STEP-LAP SPECIMENS
AT ROOM TEMPERATURE

Reference No.	Specimen No.	Failure Load (lb)	Width (in.)	Running Load at Failure (lb/in.)	Laminate Strain at Failure (in./in. x 10 ⁻⁶)
1	1	21,775	0.9979	21,821	7,235
2	2	21,250	0.9998	21,254	6,890
3	3	21,300	1.0021	21,255	6,735
4	49	19,000	1.0070	18,868	6,360
5	81	20,925	1.0053	20,815	6,993
6	82	20,300	1.0081	20,137	6,640
7	83	16,640	1.0071	16,523	5,560
8	84	20,900	1.0066	20,763	7,200
9	85	20,550	1.0078	20,391	6,680
10	86	19,300	1.0050	19,204	6,480

Mean	20,103
Standard Deviation	1,556
Coefficient of Variation	0.077

GP74-1037-89

**TABLE 12 STATIC STRENGTH TESTS OF FULL SCALE STEP-LAP SPECIMENS
AT 350°F**

Reference No.	Specimen No.	Failure Load (lb)	Width (in.)	Running Load at Failure (lb/in.)	Laminate Strain at Failure (in./in. x 10 ⁻⁶)
1	61	15,750	1.0014	15,728	5400
2	62	16,275	1.0019	16,244	5610
3	63	16,125	0.9992	16,138	5265
4	64	15,775	0.9992	15,788	5280
5	65	16,490	1.0004	16,433	5397
6	66	16,240	1.0038	16,179	5247
Mean				16,003	QP74-1037-40
Standard Deviation				287	
Coefficient of Variation				0.018	

**TABLE 13 STATIC STRENGTH TESTS OF SMALL SCALE STEP-LAP SPECIMENS
AT ROOM TEMPERATURE**

Reference No.	Specimen No.	Failure Load (lb)	Width (in.)	Running Load at Failure (lb/in.)	Laminate Strain at Failure (in./in. x 10 ⁻⁶)
1	1	15,450	1.0038	15,392	7,745
2	2	17,650	1.0039	17,581	8,960
3	3	16,400	1.0099	16,239	9,520
4	36A	18,300	1.0024	18,256	9,000
5	65	18,750	1.0060	18,638	8,500
6	66	18,575	1.0049	18,484	8,600
7	67	17,325	1.0037	17,261	8,240
8	68	17,100	1.0045	17,023	8,200
9	69	17,050	1.0056	16,955	7,920
10	70	17,800	1.0066	17,683	8,600
Mean				17,351	QP74-1037-61
Standard Deviation				1,015	
Coefficient of Variation				0.058	

TABLE 14 STATIC STRENGTH TESTS OF SIMPLE SPECIMENS AT ROOM TEMPERATURE

Reference No.	Specimen No.	Failure Load (lb)	Width (in.)	Running Load at Failure (lb/in.)	Laminate Strain at Failure (in./in. x 10 ⁻⁶)
1	7	6,025	1.0029	6,008	8,000
2	25	6,450	0.9980	6,463	8,385
3	83	5,325	1.0017	5,316	6,960
4	20	6,425	0.9997	6,427	8,295
5	58	6,525	1.0037	6,501	8,750
6	84	5,475	1.0018	5,465	7,020
7	73	5,275	1.0010	5,270	7,455
8	46	6,475	1.0045	6,446	9,366
Mean				5,987	GP74-1037-P2
Standard Deviation				552	
Coefficient of Variation				0.092	



FIGURE 68 FATIGUE TEST MACHINE

Load levels used were selected with test limit load (TLL) in a 60-70% range of average static strength to produce failures at about four lifetimes using Tape 1. This was done because the F-15 low cost production flight wing, the conceptual structural application, was to be designed for four lifetimes. The TLL selected for the full scale step-lap specimens is 13,500 (lb/in) which is 35% greater than the minimum required design limit load (DLL) of 10,000 (lb/in). If failure did not occur prior to six lifetimes, testing was stopped and the residual strength was determined at that point.

The high temperature tests were conducted on the same machines and were enclosed in an air circulating oven. The specimens were heated to 350°F, held at this temperature for ten minutes, and then tested to failure. Results of lifetime tests of full scale step-lap, small scale step-lap and simple specimens are presented in Tables 15 thru 22. The results of the 29 lifetime tests run under the verification task using the F-15 semi random wing root bending moment spectrum are presented in Table 3 (Section 2).

5.3 Residual Strength

Each residual strength specimen was fatigue tested in one of three 150,000 pound fatigue machines for the required number of lifetimes, then removed and failed statically in a Baldwin 30,000 pound universal test machine.

Results of residual strength tests of full scale step-lap, small scale step-lap and simple specimens are presented in Tables 23 thru 27.

5.4 Failure Analysis

Each specimen tested under this contract was carefully examined and the failure surfaces were analyzed. All the simple specimens failed in a similar mode, partially adhesive and partially interlaminar. Typical failure surfaces are illustrated in Figure 69. The failure surfaces of the step-lap specimens fell into seven general classifications. These are listed below:

- Type A - cohesive failure on tang
- Type B - adhesive failure on tang
- Type C - partial interlaminar failure on tang
- Type D - interlaminar failure on tang
- Type E - adhesive failure on tang and adjoining step
- Type F - cohesive failure on tang and adjoining step
- Type G - titanium failure on tang

Each type failure surface is illustrated in Figure 70. In Figure 71 the failure modes of each step-lap specimen are identified by type.

**TABLE 15 FATIGUE LIFE OF FULL SCALE STEP-LAP SPECIMENS AT ROOM
TEMPERATURE BASELINE SPECTRUM**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	4	13,700	0.9983	2.5000*	115.0	
2	5	13,700	0.9981	3.1425*	95.0	
3	6	13,500	1.0013	3.0325	95.0	
4	7	13,500	1.0016	4.1250	85.0	
5	8	13,500	0.9983	5.5927	85.0	
6	9	13,500	0.9953	4.5000	115.0	
7	14	13,500	1.0112	6.0		18,900
8	15	13,500	1.0089	6.0		19,620
9	16	13,500	1.0020	6.0		13,960
10	17	13,500	0.9993	3.5000	115.0	
11	18	13,500	1.0026	6.0		18,720
12	24	13,500	1.0045	6.0		18,260
13	25	13,500	1.0053	6.0		17,870
14	26	13,500	1.0059	5.6070	95.0	
15	27	13,500	1.0030	5.1510	100.0	
16	28	13,500	1.0016	6.0		14,540
17	29	13,500	1.0043	6.0		19,800
18	30	13,500	1.0038	6.0		18,940
19	31	13,500	1.0063	5.4010	100.0	
20	32	13,500	1.0071	6.0		20,920
21	33	13,500	1.0072	6.0		19,770
22	34	13,500	1.0067	6.0		21,680
23	35	13,500	1.0070	6.0		17,700
24	19	13,500	1.0029	5.5000	95.0	
25	48	13,500	1.0012	3.1123	87.5	
26	50	13,500	1.0064	2.0000	90.0	
27	79	13,500	1.0065	2.0000	125.0	
28	87	13,500	1.0047	1.5000	115.0	
29	88	13,500	1.0048	2.5000	115.0	
30	89	13,500	1.0039	2.0000	125.0	
Mean				5.8100	GP74-1037-97	
Standard Deviation				2.8800		
Coefficient of Variation				0.496		

* Not included in determination of mean since it corresponds to a different TLL.

**TABLE 16 FATIGUE LIFE OF FULL SCALE STEP-LAP SPECIMENS
AT 350°F BASELINE SPECTRUM**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	75	10,100	1.0094	6.0000		18,750 ⁽¹⁾
2	67	10,500	1.0031	6.0000		16,500
3	68	11,000	1.0052	6.0000		12,850
4	69	11,000	1.0042	6.0000		12,800
5	70	12,000	1.0051	2.0000	125	
6	76	11,500	1.0077	3.0315	100	

(1) Specimen was tested at room temperature.

GP74-1037-88

(2) No statistical parameters are presented because there is insufficient data with a common TTL.

**TABLE 17 FATIGUE LIFE OF FULL SCALE STEP-LAP SPECIMENS AT ROOM
TEMPERATURE FREQUENCY OF LOAD APPLICATION SLOWED
TO 1/8 OF BASELINE**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	12	13,500	1.0088	5.1820	95	
2	13	13,500	1.0109	4.1258	90	
3	20	13,500	1.0020	2.0000	125	
4	21	13,500	1.0032	3.2580	95	
5	22	13,500	1.0039	6.0000		18,660
6	23	13,500	1.0043	6.0000		14,840

GP74-1037-99

Mean	4.7200
Standard Deviation	2.5600
Coefficient of Variation	0.542

**TABLE 18 FATIGUE LIFE OF FULL SCALE STEP-LAP SPECIMENS AT ROOM
TEMPERATURE ADDITIONAL LOW LOADS INCLUDED**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)
1	10	13,500	0.9987	1.4060	100
2	11	13,500	1.0082	2.0000	125
3	80	13,500	1.0063	1.6543	100

GP74-1037-101

Mean	1.6868
Standard Deviation	0.2983
Coefficient of Variation	0.177

**TABLE 19 FATIGUE LIFE OF FULL SCALE STEP-LAP SPECIMENS
AT ROOM TEMPERATURE RELAXATION TIME INCREASED
TO TEN TIMES BASELINE**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)
1	56	13,500	1.0086	0.5000	115
2	57	13,500	1.0044	1.5000	115
3	71	13,500	1.0090	3.1108	95
4	72	13,500	1.0094	4.5000	115
5	73	13,500	1.0103	3.5000	115
6	74	13,500	1.0096	2.0000	125
				Mean	2.5185
				Standard Deviation	1.4574
				Coefficient of Variation	0.579

GP74-1037-100

**TABLE 20 FATIGUE LIFE OF FULL SCALE STEP-LAP SPECIMENS
AT ROOM TEMPERATURE WITHOUT 115% AND 125%
TLL LOADS**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)
1	77	13,500	1.0080	4.1510	100
2	78	13,500	1.0073	4.1510	100
3	90	13,500	1.0048	1.1645	100
				Mean	2.5185
				Standard Deviation	1.3930
				Coefficient of Variation	0.752

GP74-1037-102

TABLE 21 FATIGUE LIFE OF SMALL SCALE STEP-LAP SPECIMENS AT ROOM TEMPERATURE BASELINE SPECTRUM

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	4	9,280	0.9996	6.0*		16,550
2	5	9,280	1.0068	6.0*		17,025
3	11	10,500	1.0095	6.0*		15,825
4	12	10,500	1.0003	6.0*		13,975
5	13	11,500	1.0095	4.0550	84.2	
6	6	11,500	1.0055	5.0000	92.1	
7	7	11,500	1.0050	3.5000	115.0	
8	8	11,500	1.0073	2.0000	125.0	
9	9	11,500	1.0059	2.0000	125.0	
10	10	11,500	1.0072	2.0000	125.0	
11	14	11,500	1.0092	5.0303	90.0	
12	15	11,500	1.0007	5.5000	115.0	
13	16	11,500	1.0029	5.2750	92.5	
14	17	11,500	1.0059	4.5000	115.0	
15	18	11,500	1.0079	5.1798	90.0	
16	19	11,500	1.0100	6.0		13,375
17	20	11,500	1.0079	5.4010	90.0	
18	21	11,500	1.0051	3.5000	115.0	
19	22	11,500	1.0073	3.8913	80.0	
20	23	11,500	1.0078	2.4050	82.2	
21	24	11,500	1.0054	2.0000	125.0	
22	25	11,500	1.0057	3.4057	87.5	
23	26	11,500	1.0067	2.0000	125.0	
24	27	11,500	1.0071	4.1510	92.5	
25	28	11,500	1.0063	1.8118	92.5	
26	29	11,500	1.0074	2.0000	125.0	
27	30	11,500	1.0056	6.0		13,775
28	31	11,500	1.0076	4.7815	100.0	
29	32	11,500	1.0087	1.9013	95.0	
30	33	11,500	1.0089	2.0000	125.0	
31	34	11,500	1.0093	4.5000	115.0	
32	35	11,500	1.0071	2.5000	115.0	
33	37	11,500	1.0069	2.6483	90.0	
34	38	11,500	1.0041	1.9018	90.0	
35	39	11,500	1.0069	4.1050	115.0	
36	40	11,500	1.0077	4.8025	75.0	
37	41	11,500	1.0004	3.5000	115.0	
38	42	11,500	1.0029	4.3935	80.0	
39	43	11,500	1.0008	1.7698	82.5	
40	64	11,500	1.0051	2.2505	82.5	

Mean	3.5500
Standard Deviation	1.7480
Coefficient of Variation	0.492

GP74-1037-95

* Not included in calculation of the mean since it corresponds to a different TLL.

**TABLE 22 FATIGUE LIFE OF SIMPLE SPECIMENS AT ROOM TEMPERATURE
BASELINE SPECTRUM**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Lifetimes	Last Load (% TLL)
1	71	3,600	1.0013	1.3525*	100
2	16	3,600	0.9994	3.6500*	110
3	88	3,480	1.0011	2.1700	95
4	30	3,600	1.0009	2.3750*	100
5	21	3,480	0.9988	4.4250	95
6	32	3,480	1.0011	4.7700	97.5
7	6	3,480	1.0028	1.6850	95
8	24	3,480	0.9989	4.5625	95
9	66	3,480	1.0040	3.0200	95
10	23	3,480	0.9983	4.5000	95
Mean				3.5904	GP74-1037-93
Standard Deviation				1.2802	
Coefficient of Variation				0.357	

*Not included in calculation of mean because it corresponds to a different TLL.

**TABLE 23
THREE LIFETIME RESIDUAL STRENGTH OF FULL SCALE STEP-LAP SPECIMEN
AT ROOM TEMPERATURE BASELINE SPECTRUM**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Residual Run Load (lb/in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	36	13,500	1.0047	20,086	3.0000		20,180
2	37	13,500	1.0049	18,400	3.0000		18,490
3	38	13,500	1.0067	21,327	3.0000		21,470
4	39	13,500	1.0062	21,258	3.0000		21,390
5	40	13,500	1.0070	18,620	3.0000		18,750
6	41	13,500	1.0038	16,736	3.0000		16,800
7	42	13,500	1.0093	18,458	3.0000		18,630
8	43	13,500	1.0093	16,566	3.0000		16,720
9	92	13,500	1.0073		2.0000	125	
10	99	13,500	0.9988	16,470	3.0000		16,450
11	44 ⁽¹⁾	13,500	1.0081		1.1505	95	
12	45 ⁽¹⁾	13,500	0.9989		1.2500	95	
(1) Rejected by NDT				Mean	18,250	GP75-0332-45	
				Standard Deviation	2,760		
				Coefficient of Variation	0.151		

TABLE 24
TWO LIFETIME RESIDUAL STRENGTH OF FULL SCALE STEP-LAP SPECIMEN
AT ROOM TEMPERATURE BASELINE SPECTRUM

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Residual Running Load (lb/in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	91	13,500	1.0082	18,250	2.0000		18,400
2	93	13,500	1.0086	18,304	2.0000		18,460
3	94	13,500	1.0067		0.5000	115	
4	95	13,500	1.0051		1.5000	115	
5	96	13,500	1.0010	17,023	2.0000		17,040
6	97	13,500	1.0011		1.5000	115	
7	55	13,500	1.0086	16,458	2.0000		16,600
8	98	13,500	1.0006		1.5000	115	
9	100	13,500	0.9991	12,651	2.0000		12,640
10	60	13,500	1.0030	15,479	2.0000		15,525
11	46 ⁽¹⁾	13,500	0.9980		1.0611	95	
12	47 ⁽¹⁾	13,500	1.0048		0.8623	90	
13	51 ⁽¹⁾	13,500	1.0050		0.0005	80	
14	52 ⁽¹⁾	13,500	1.0042		0.4010	90	
15	53 ⁽¹⁾	13,500	1.0089		0.3615	95	
16	54 ⁽¹⁾	13,500	1.0053		0.5000	115	
17	58 ⁽¹⁾	13,500	1.0067		0.9010	95	
18	59 ⁽¹⁾	13,500	1.0086		1.9020	100	
(1) Rejected by NDT				Mean	14,650		
				Standard Deviation	3,808		
				Coefficient of Variation	0.260		

TABLE 25 TWO LIFETIME RESIDUAL STRENGTH OF SMALL SCALE STEP-LAP SPECIMENS
AT ROOM TEMPERATURE BASELINE SPECTRUM

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Residual Running Load (lb/in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	53	11,500	0.9991	16,100	2.0000		16,115
2	54	11,500	0.9997	16,000	2.0000		16,005
3	55	11,500	1.0017		1.4018	105.0	
4	56	11,500	1.0000	15,000	2.0000		15,000
5	57	11,500	0.9976	12,000	2.0000		12,029
6	58	11,500	0.9979		0.5000	115.0	
7	59	11,500	0.9976		1.5000	115.0	
8	60	11,500	0.9956		1.6500	95.0	
9	61	11,500	1.0029		1.0163	87.5	
10	62	11,500	0.9883		1.5000	115.0	
				Mean	11,800		
				Standard Deviation	3,840		
				Coefficient of Variation	0.326		

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**TABLE 26 THREE LIFETIME RESIDUAL STRENGTH OF SMALL SCALE STEP-LAP SPECIMENS
AT ROOM TEMPERATURE BASELINE SPECTRUM**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Residual Running Load (lb/in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)
1	44	11,500	1.0027	13,185	1.0543	95.0	13,250
2	45	11,500	1.0012		2.0000	125.0	
3	46	11,500	1.0030		1.5000	115.0	
4	47	11,500	1.0049		3.0000		
5	48	11,500	1.0032		2.0000	115.0	
6	49	11,500	1.0033	16,245	1.3750	95.0	16,200
7	50	11,500	1.0005		1.1500	92.5	
8	51	11,500	0.9972		3.0000		
9	52	11,500	0.9997		1.1250	90.0	
10	63	11,500	1.0064		1.0313	95.0	
Mean				6,820			
Standard Deviation				7,128			
Coefficient of Variation				1.044			

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GP74-1037-104

**TABLE 27 THREE LIFETIME RESIDUAL STRENGTH OF SIMPLE SPECIMENS
AT ROOM TEMPERATURE BASELINE SPECTRUM**

Reference No.	Specimen No.	Test Limit Load (lb)	Width (in.)	Residual Running Load (lb/in.)	Lifetimes	Last Load (% TLL)	Residual Strength (lb)	
1	87	3,480	1.0023	6,449	2.1100	57.9	6,475	
2	49	3,480	1.0040		2.0000			
3	57	3,480	1.0031		3.0000			
4	79	3,480	1.0015		3.0000			
5	54	3,480	1.0020		3.0000			
6	63	3,480	1.0031	6,272	2.0000	125.0	6,300	
7	72	3,480	1.0013		2.5000	115.0		
8	47	3,480	1.0044		3.0000			
9	90	3,480	1.0029		2.0500	81.5		
10	85	3,480	0.9939		2.2900	92.5		
Mean				4,100	GP74-1037-10			
Standard Deviation				2,212				
Coefficient of Variation				0.540				

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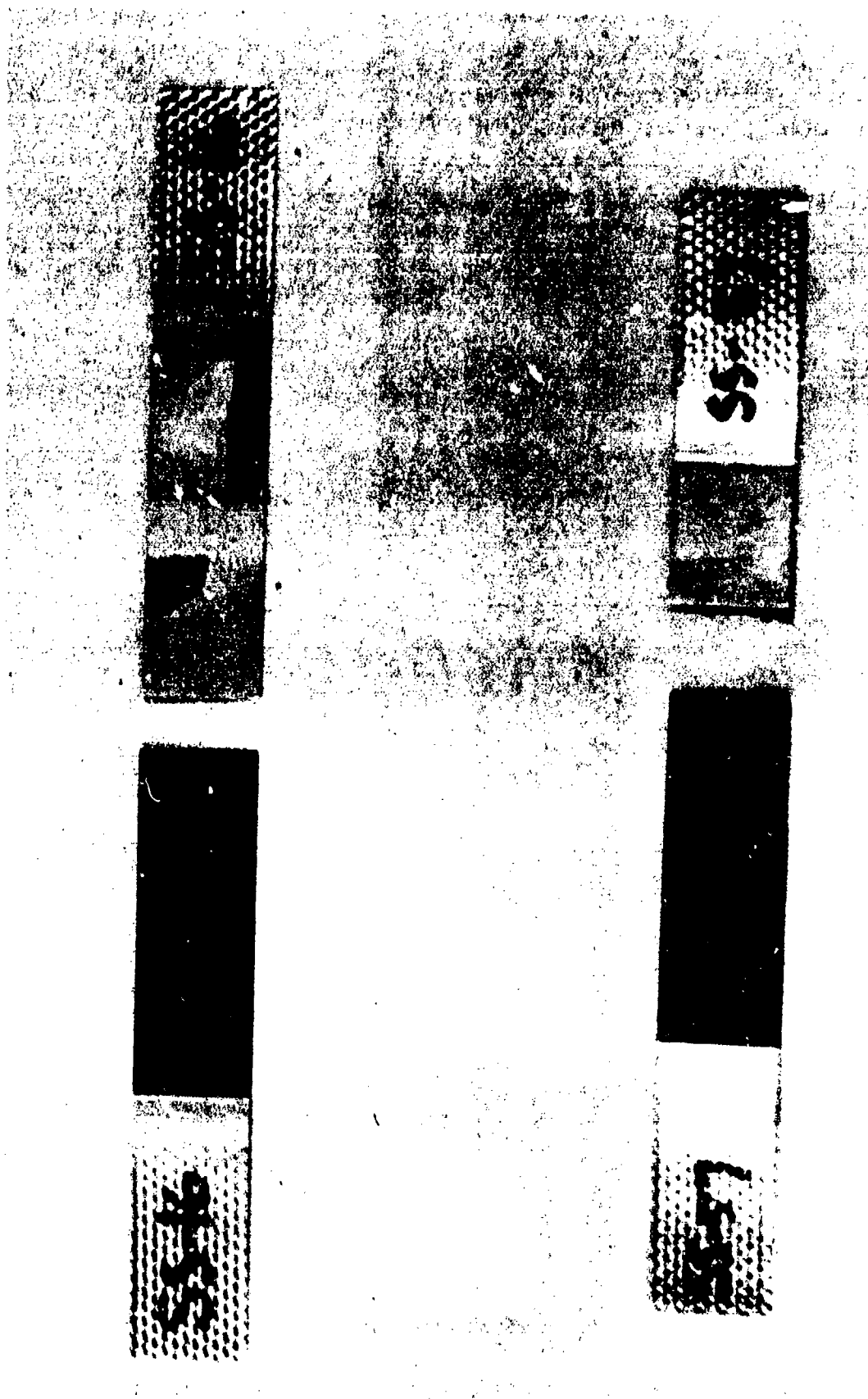
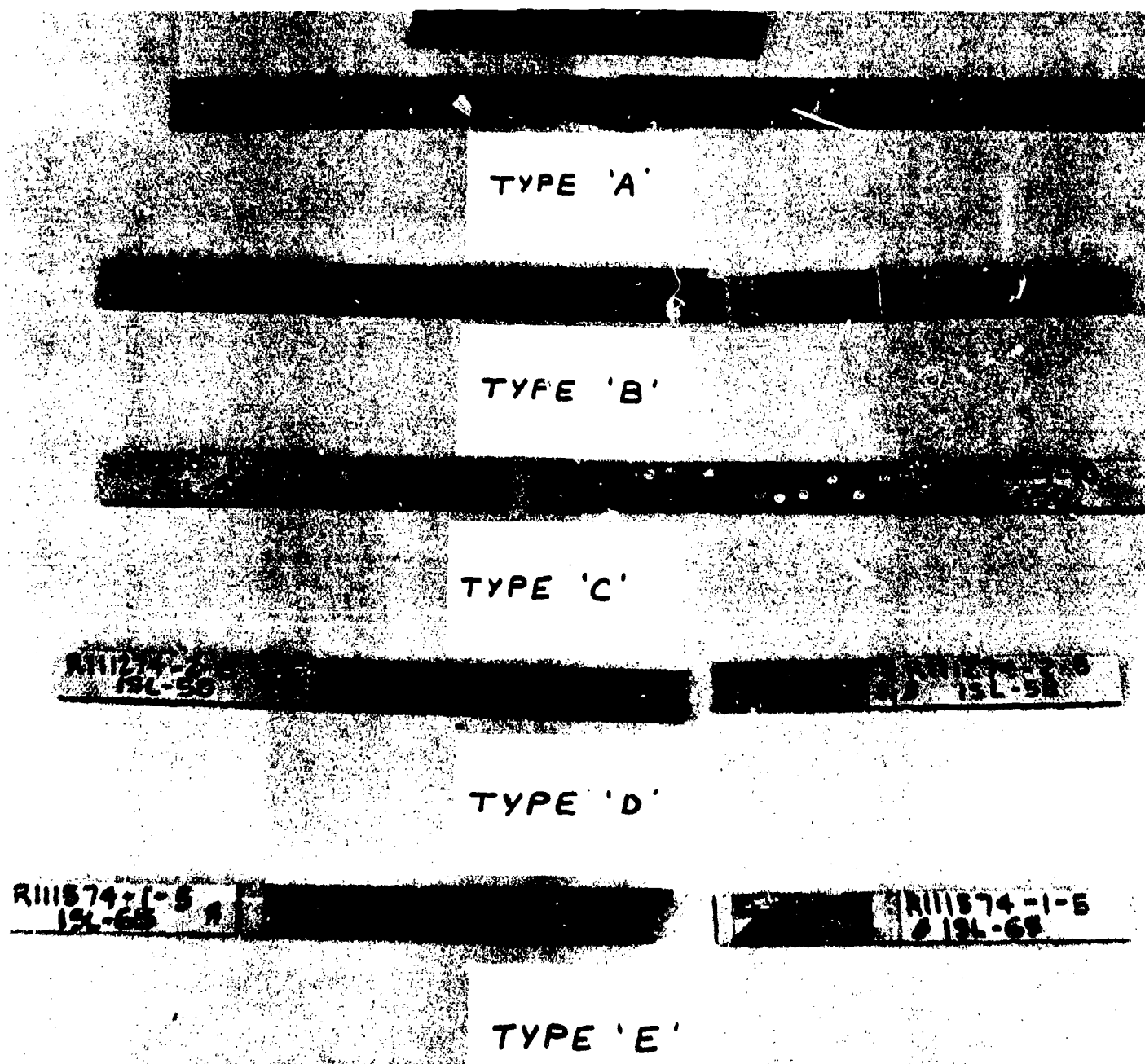


FIGURE 69 TYPICAL FAILURE MODE FOR SIMPLE SPECIMENS



Full Scale Step-Lap Specimens

FIGURE 70 TYPICAL FAILURE MODES FOR STEP-LAP SPECIMENS



TYPE 'A'



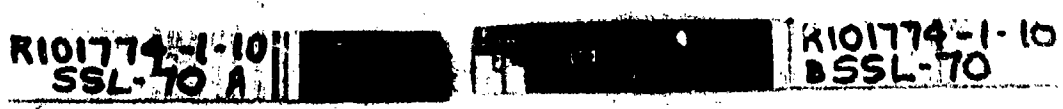
TYPE 'B'



TYPE 'C'



TYPE 'D'



TYPE 'E'

Small Scale Step-Lap Specimens

FIGURE 70 TYPICAL FAILURE MODES FOR STEP-LAP SPECIMENS (Continued)

Full Scale Step-Lap No.	Type	Small Scale Step-Lap No.	Type	Full Scale Step-Lap No.	Type	Small Scale Step-Lap No.	Type	Full Scale Step-Lap No.	Type	Small Scale Step-Lap No.	Type
1	D	1	D	31	B	31	B	61	F	61	A
2	D	2	D	32	D	32	A	62	A	62	B
3	C	3	D	33	C	33	A	63	F	63	B
4	A	4	D	34	D	34	B	64	F	64	B
5	A	5	D	35	D	35	A	65	F	65	D
6	B	6	A	36	D	36A	D	66	F	66	C
7	B	7	A	37	D	37	B	67	F	67	C
8	B	8	B	38	D	38	B	68	A	68	C
9	B	9	B	20	D	39	B	69	F	69	C
10	B	10	A	40	B	40	B	70	F	70	G
11	A	11	C	41	D	41	A	71	F		
12	B	12	B	42	D	42	A	72	B		
13	B	13	A	43	B	43	A	73	B		
14	B	14	B	44	C	44	D	74	C		
15	B	15	B	45	B	45	A	75	C		
16	C	16	B	46	A	46	D	76	F		
17	B	17	C	47	B	47	A	77	B		
18	A	18	B	48	A	48	A	78	B		
19	A	19	B	49	C	49	A	79	C		
20	C	20	A	50	C	50	A	80	C		
21	E	21	A	51	D	51	B	81	D		
22	B	22	A	52	D	52	B	82	D		
23	B	23	B	53	D	53	D	83	D		
24	B	24	B	54	D	54	D	84	C		
25	B	25	B	55	D	55	B	85	D		
26	B	26	B	56	D	56	C	86	D		
27	B	27	A	57	C	57	B	87	D		
28	E	28	B	58	D	58	C	88	D		
29	B	29	A	59	A	59	B	89	D		
30	B	30	A	60	D	60	B	90	C		

Notes:

- (1) 20% failed in mode A
34.35% failed in mode B
13.75% failed in mode C
23.75% failed in mode D
1.25% failed in mode E
6.25% failed in mode F
0.65% failed in mode G
- (2) This data could not be related to batch effects
- (3) Type A - cohesive failure on tang
Type B - adhesive failure on tang
Type C - partial interlaminar failure on tang
Type D - interlaminar failure on tang
Type E - adhesive failure on tang and adjoining step
Type F - cohesive failure on tang and adjoining step
Type G - titanium failure on tang

FIGURE 71 IDENTIFICATION OF FAILURE MODES FOR STEP-LAP SPECIMENS

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SECTION 6

DATA REDUCTION

Static strength, residual strength and fatigue life are each assumed to be statistically distributed according to the Weibull probability function. This assumption is required in the development of the wearout model given in Appendix B. An evaluation of the data generated in this program indicates a favorable comparison with the Weibull distribution.

The probabilities given by the Weibull function are presented in the following equations:

$$P [F_s] = \exp - [F_s/\beta_s]^{\alpha_s} \quad (14)$$

$$P [F_R(T)] = \exp - [F_R(T)/\beta_R(T)]^{\alpha_R(T)} \quad (15)$$

$$P [T] = \exp - [T/\beta_f]^{\alpha_f} \quad (16)$$

Probabilities thus defined are that a given specimen will have a static strength equal to or greater than F_s , a residual strength at time T equal to or greater than $F_R(T)$, and a fatigue life equal to or greater than T . The terms α_s and β_s , $\alpha_R(T)$ and $\beta_R(T)$, and β_f and α_f are shape and scale parameters for static strength, residual strength at time T and fatigue life respectively. Scale and shape parameters for residual strength and fatigue life correspond to a given loading spectrum with specified load levels and environments. The Weibull scale parameter, β , plays a role similar to the mean of the normal distribution. Data scatter is related to $1/\alpha$, i.e., small values of the shape parameter α represent large scatter. Several procedures are available for the estimation of the scale and shape parameters of a Weibull distribution, e.g., Maximum Likelihood Estimation (MLE), Best Linear Unbiased (BLU) estimate and Menon's estimate. No consensus concerning the best procedure is found in the literature and a comparison of the parameters estimated using these procedures showed little difference. Since MCAIR has previously used the BLU procedure, Reference 16, it was used throughout this work.

6.1 BLU Procedure

The Best Linear Unbiased estimate for determination of parameters of the Weibull distribution is developed in Reference 30. Only the essentials required to make the estimates in this report are presented here. The table of weights used to make estimates is given in Reference 31. In this table N corresponds to the number of tests, M corresponds to the number of data points (failures) obtained and I is an ordering index where I = 1 corresponds to the smallest data point, I = 2 the next smallest, etc. For the assumed Weibull distribution given by equation (17)

$$P [F] = \exp - [F/\beta]^\alpha \quad (17)$$

the BLU estimates of the parameters are obtained from equations (18) and (19)

$$\alpha = [1 - E(LB)] / \sum_{I=1}^M C(N,M,I) \ln F_I \quad (18)$$

$$\beta = \exp \left[\sum_{I=1}^M A(N,M,I) \ln F_I + E(CP) \sum_{I=1}^M C(N,M,I) \ln F_I / [1 - E(LB)] \right] \quad (19)$$

The table contains values for $N \leq 25$. For sets in which there are more than 25 data points, the points should be randomly grouped into subsets with 25 or fewer data points. The set estimate is then taken to be the weighted average of the subsets where the weighting factor is the reciprocal of the term, γ , given in equation (20),

$$\gamma = E(LB) / [1 - E(LF)] \quad (20)$$

6.2 Scale and Shape Parameter Estimation

The estimation procedure described in Section 6.1 was used to generate Weibull shape and scale parameters for each of the static strength and fatigue life data sets presented in Section 5. The calculations used to get these estimates are presented in Appendix D. This procedure cannot be used to bias a residual strength distribution downward to account for the fact that some of the specimens may fail prior to the time at which the residual strength was to be measured. Each of the groups of specimens which were selected for residual strength tests at some predetermined time had premature failures of this type. The Weibull parameters for the residual strength data sets presented in Section 5 were thus determined graphically (see Appendix E). The measured residual strengths were ranked from highest to lowest and the probability of survival, P_S , was determined from equation (21)

$$P_S = \frac{n}{N+1} \quad (21)$$

where n is the rank of the data and N is the total number of specimens tested including the ones which failed prematurely. The resulting data was plotted as $\ln \ln \frac{1}{P_S}$ vs $\ln F_r$. A best fit straight line is then drawn through these points. The scale parameter is the value of F_r at which the resulting line intersects the $\ln \ln \frac{1}{P_S} = 0$ line. The shape parameter is the slope of this line. A summary of the parameters determined is presented in Table 28.

6.3 Transformation of Parameters to Single Variate

The specimens used in this program are double ended to facilitate load introduction. The weakest of the joints at each end will fail first. The Weibull parameters developed directly from the data may thus be considered as representing a least of two (L02) strength or fatigue life distribution. These were transformed to represent a single variate (SV) distribution by using equation (22)

$$\begin{aligned} \alpha_{SV} &= \alpha_{L02} \\ \beta_{SV} &= \beta_{L02} \exp \frac{1}{\alpha} \ln 2 \end{aligned} \quad (22)$$

as shown in Reference 8.

TABLE 28
SUMMARY OF WEIBULL PARAMETERS

Spec Type	Type Test	Spectrum Identification	Test Limit Load (lb/in.)	Data Source		α	Weibull Parameters		Table of Calculations
				Table	No. of Spec		β (lb/in.) or Least of Two Variate	Lifetimes Single Variate	
Simple	Static Strength	N/A	N/A	14	8	14.66530	6,224	9,525	D1
	3.0 Life R.S.	Baseline	3,480	27	9	4.05000	4,890	5,803	-
	Lifetime	Baseline	3,480	22	7	3.53845	4.0360	4.9094	D2
Small Scale	Static Strength	N/A	N/A	13	10	20.33760	17,831	18,449	D3
	2.0 Life R.S.	Baseline	11,500	25	10	2.85710	12,772	16,279	-
Step-Lap	3.0 Life R.S.	Baseline	11,500	26	10	1.60000	9,414	14,518	-
	Lifetime	Baseline	11,500	21	36	2.52659	4.12828	5.4314	D4
Full Scale	RT Static Str	N/A	N/A	11	10	17.96945	20,762	21,579	D5
	350°F Static Str	N/A	N/A	12	6	59.55926	16,240	16,430	D6
Step-Lap	2.0 Life R.S.	Baseline	13,500	24	10	4.42300	15,329	17,930	-
	3.0 Life R.S.	Baseline	13,500	23	10	7.00000	19,341	21,354	-
	Lifetime	Baseline	13,500	15	28	2.19849	6.86920	9.4153	D7
	Lifetime	1/3 Base Load Freq	13,500	17	6	2.28462	5.61701	7.6080	D8
	Lifetime	Low Loads Incl	13,500	18	3	5.55864	1.84710	2.0924	D9
	Lifetime	10 x Base Freq	13,500	19	6	1.65186	2.97119	4.5203	D10
	Lifetime	High Loads Exclud	13,500	20	3	1.87371	3.70800	5.3678	D11

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6.4 Comparison of the Cumulative Frequencies with The Weibull Distributions

Comparison of the cumulative frequencies obtained from tests with the corresponding Weibull distributions for which there was a statistically significant data base is presented in Figures 72 through 75. The cumulative frequencies are represented by the circles on these figures. The comparison is favorable.

6.5 Development of the Wearout Models

The parameters of the wearout models, r and A_4 , are determined from the Weibull parameters with the aid of equations (23).

$$r = \frac{\alpha_s}{2\alpha_F} + 1$$

$$A_4 = \frac{\beta_s^{2(r-1)}}{(r-1) \beta_F}$$

(23)

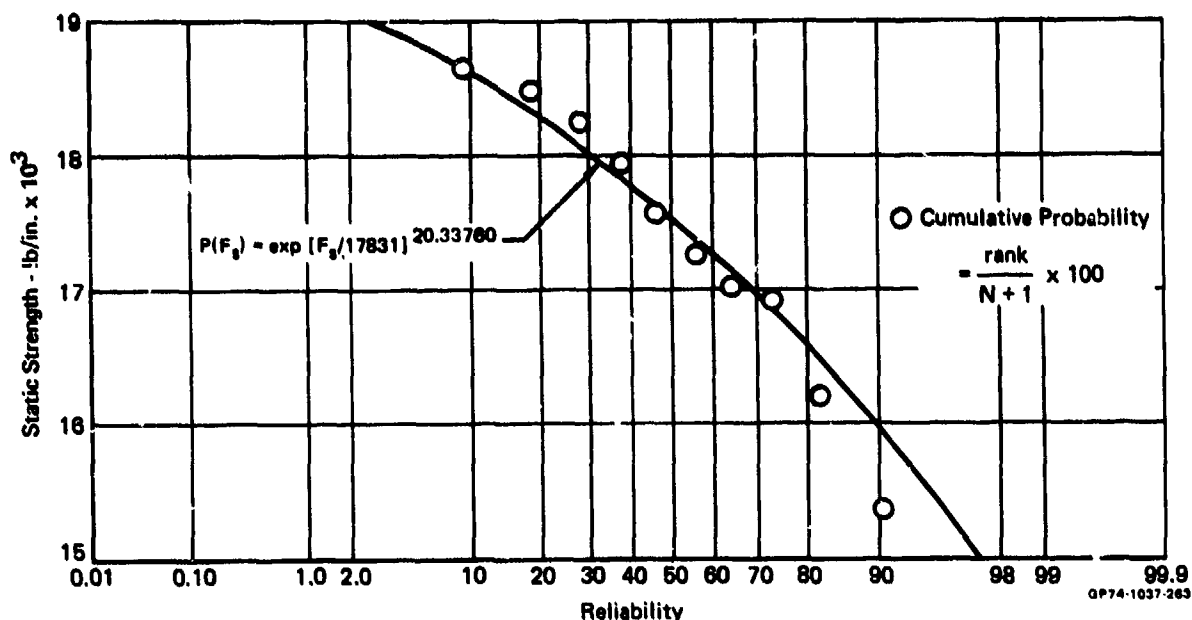


FIGURE 72 COMPARISON OF STATIC STRENGTH DATA FOR THE SMALL SCALE STEP-LAP SPECIMENS WITH CORRESPONDING WEIBULL DISTRIBUTION

These parameters along with the corresponding wearout models are summarized for each type specimen and each load condition in Table 29.

6.5 Evaluation of Wearout Models

The residual strength tests conducted under this contract were to provide data to evaluate the accuracy of the wearout models. The comparison of these data with the predictions of the wearout models is presented in Figures 76 thru 80. The solid lines in these figures represents the predictions of the wearout models. The circles represent the cumulative frequencies associated with each test point and the dashed lines correspond to Weibull distributions developed from the residual strength test data.

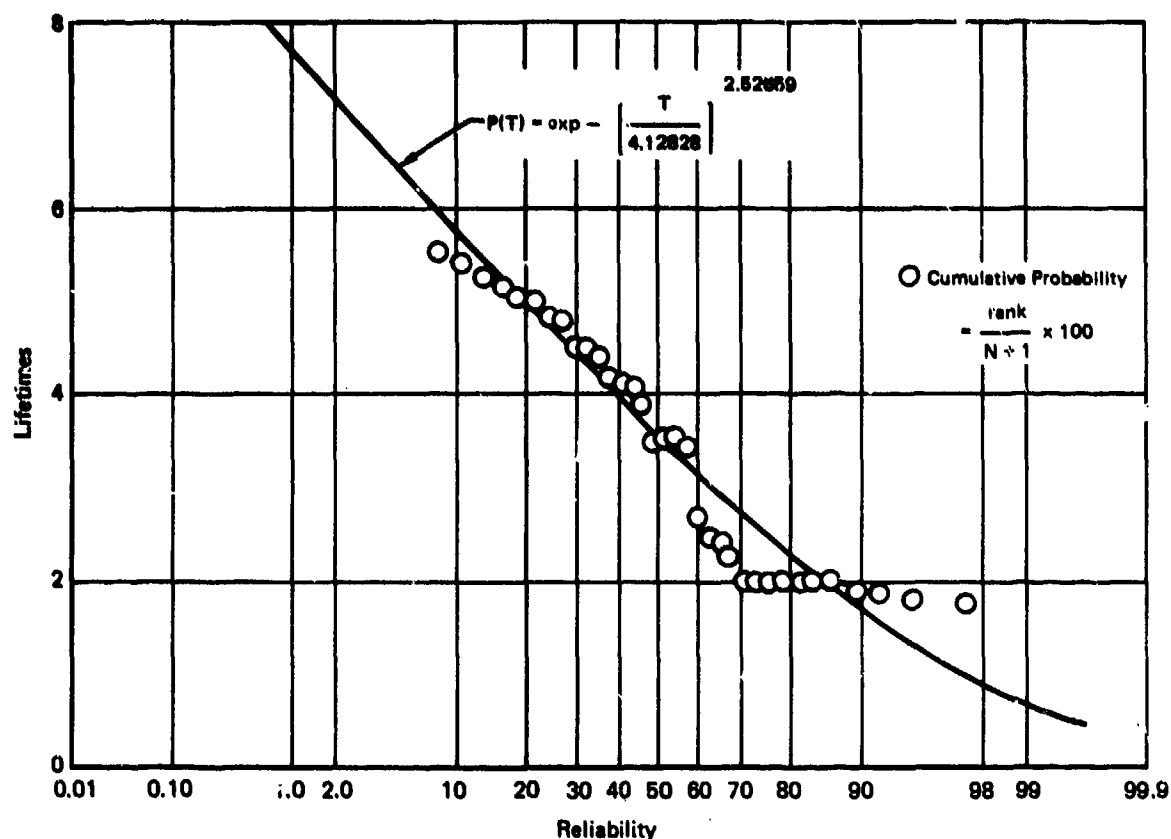


FIGURE 73 COMPARISON OF LIFETIME DATA FOR THE SMALL SCALE STEP-LAP SPECIMENS WITH CORRESPONDING WEIBULL DISTRIBUTION

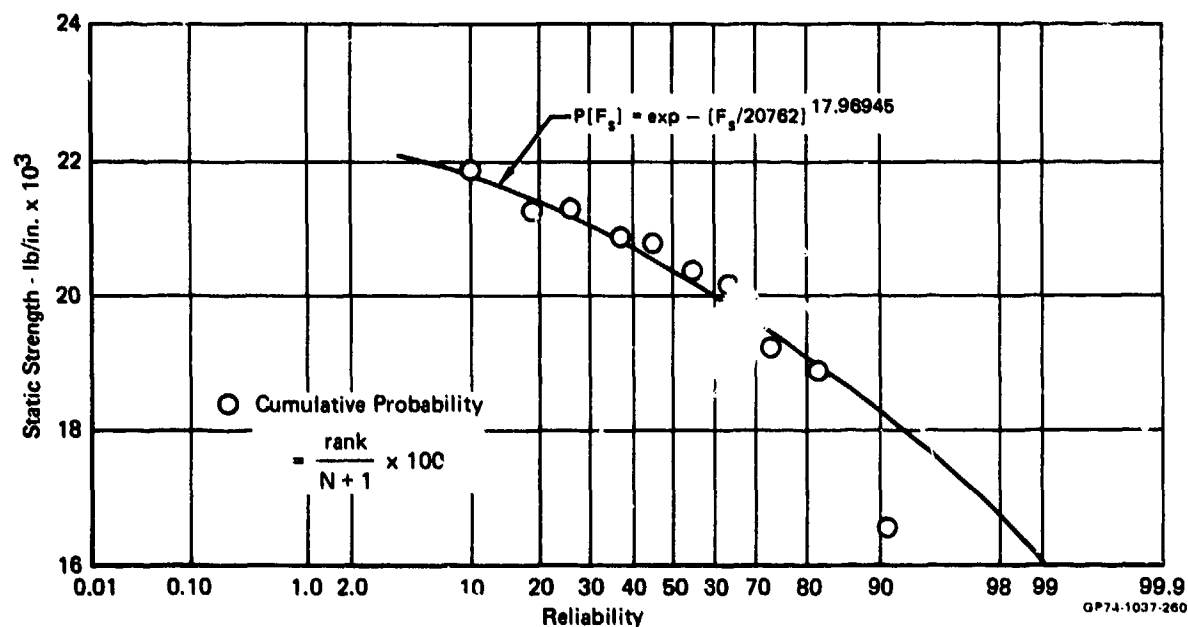


FIGURE 74 COMPARISON OF STATIC STRENGTH DATA FOR THE FULL SCALE STEP-LAP SPECIMENS WITH CORRESPONDING WEIBULL DISTRIBUTION

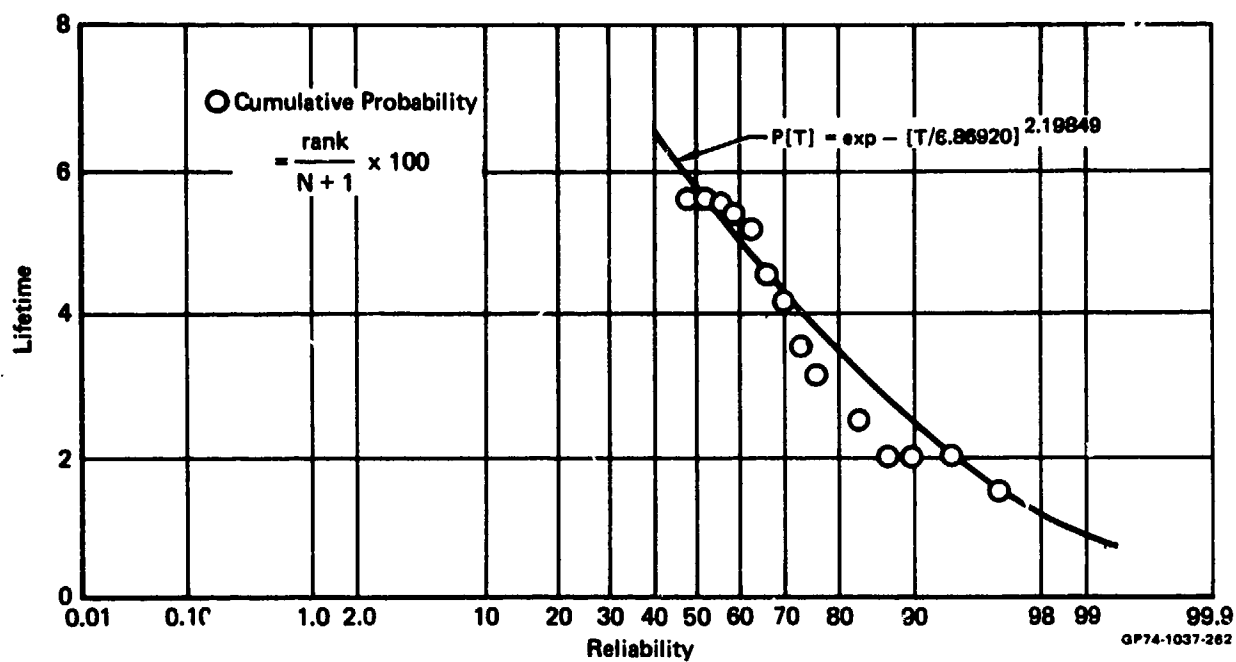


FIGURE 75 COMPARISON OF LIFETIME DATA FOR THE FULL SCALE STEP-LAP SPECIMENS WITH CORRESPONDING WEIBULL DISTRIBUTION

TABLE 29 SUMMARY OF THE WEAROUT MODELS AND THEIR PARAMETERS

Specimen Type	Spectrum/Ident	Test Limit Load (lb/in.)	Parameters		Wearout Models
			r	A ₄ (lb/in. x 10 ⁴) Lifetimes	
Simple Spec	Baseline	3,480	3.07228	0.01675	$P[F] = \exp - \left[\frac{F^{4.14456} + 0.03471 t}{0.14012} \right]$ 3.53845
Small Scale Step-Lap	Baseline	11,500	5.02471	6.32871	$P[F] = \exp - \left[\frac{F^{9.04942} + 25.47122 t}{105.15228} \right]$ 2.52659
Full Scale Step-Lap	Baseline	13,500	5.08677	13.96131	$P[F] = \exp - \left[\frac{F^{8.17354} + 57.05666 t}{391.93350} \right]$ 2.19849
Full Scale Step-Lap	Freq 1/8 of Baseline	13,500	2.59956	1.15206	$P[F] = \exp - \left[\frac{F^{3.19912} + 1.84279 t}{10.3510} \right]$ 2.28462
Full Scale Step-Lap	Additional Low Loads	13,500	2.61635	3.55312	$P[F] = \exp - \left[\frac{F^{3.23270} + 5.74309 t}{10.60806} \right]$ 5.55864
Full Scale Step-Lap	High Loads Excluded	13,500	5.79515	62.05327	$P[F] = \exp - \left[\frac{F^{9.55030} + 297.55474 t}{1103.33319} \right]$ 1.87371
Full Scale Step-Lap	Relax. 10 x Baseline	13,500	6.43916	174.94173	$P[F] = \exp - \left[\frac{F^{10.87832} + 951.53606 t}{2827.19484} \right]$ 1.65186

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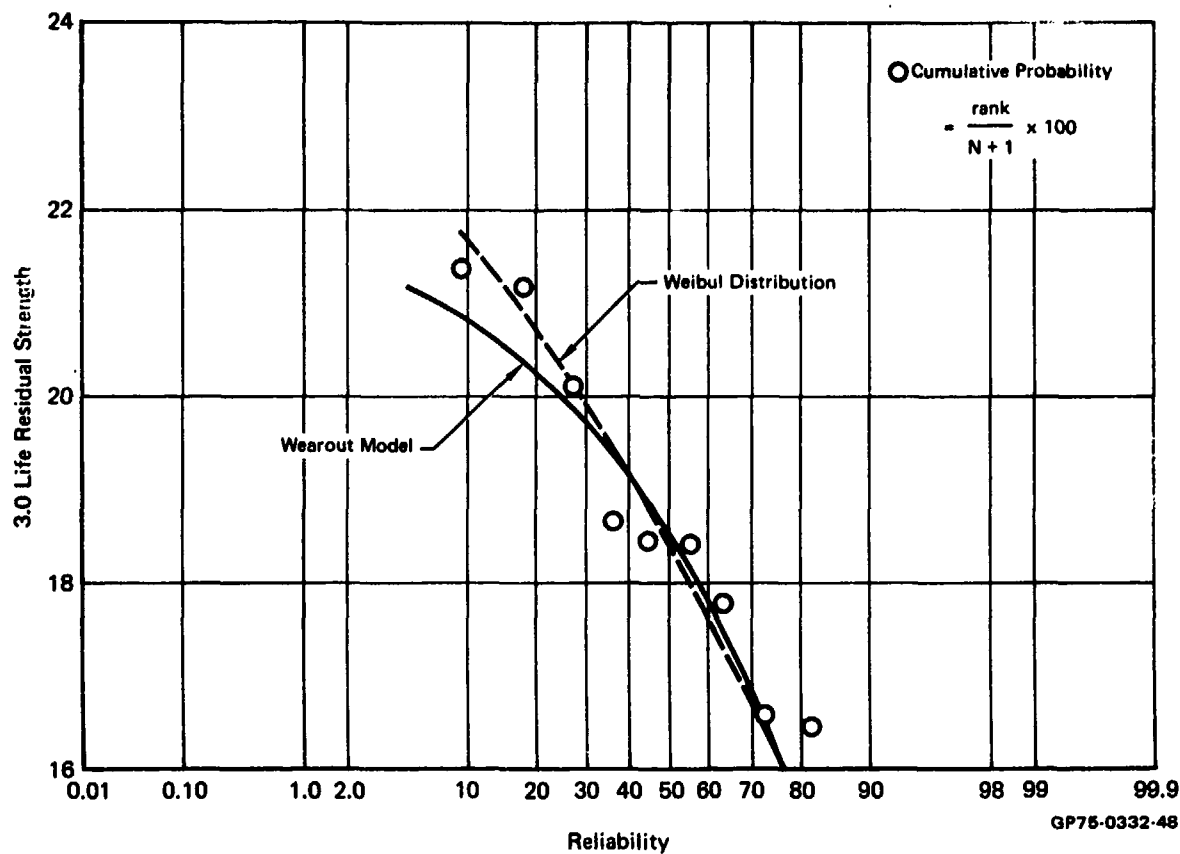


FIGURE 76 COMPARISON OF WEAROUT MODEL FOR FULL SCALE STEP-LAP SPECIMEN AT 3.0 LIFETIMES WITH WEIBULL DISTRIBUTIONS

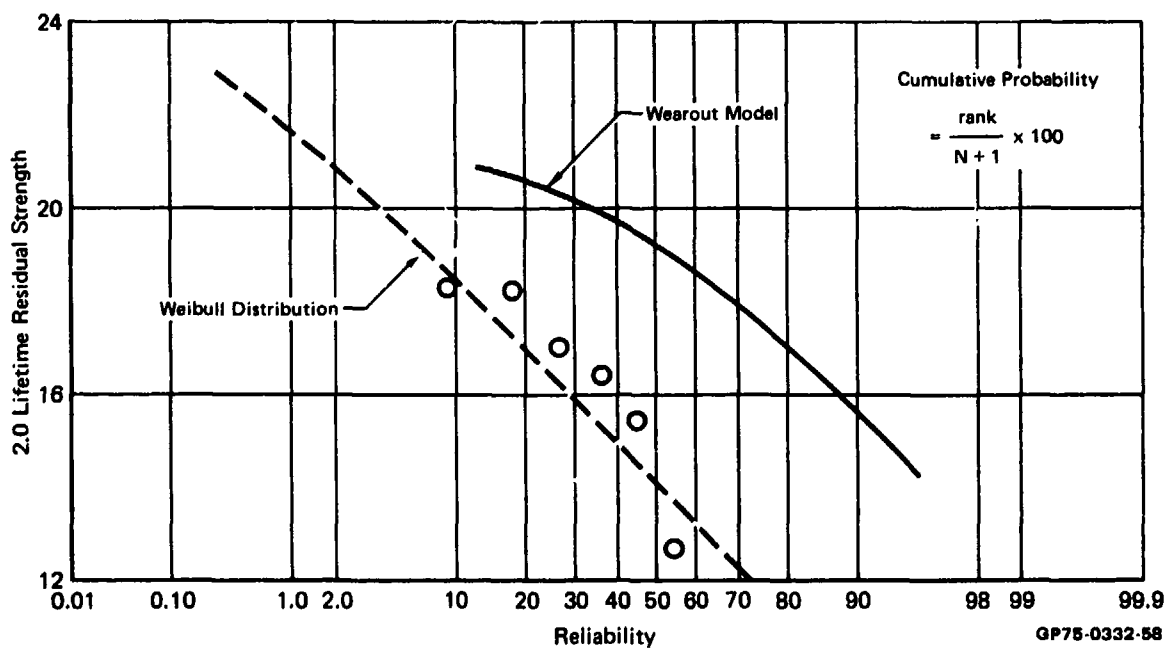


FIGURE 77 COMPARISON OF WEAROUT MODEL FOR FULL SCALE STEP-LAP SPECIMENS AT 2.0 LIFETIMES WITH WEIBULL DISTRIBUTION

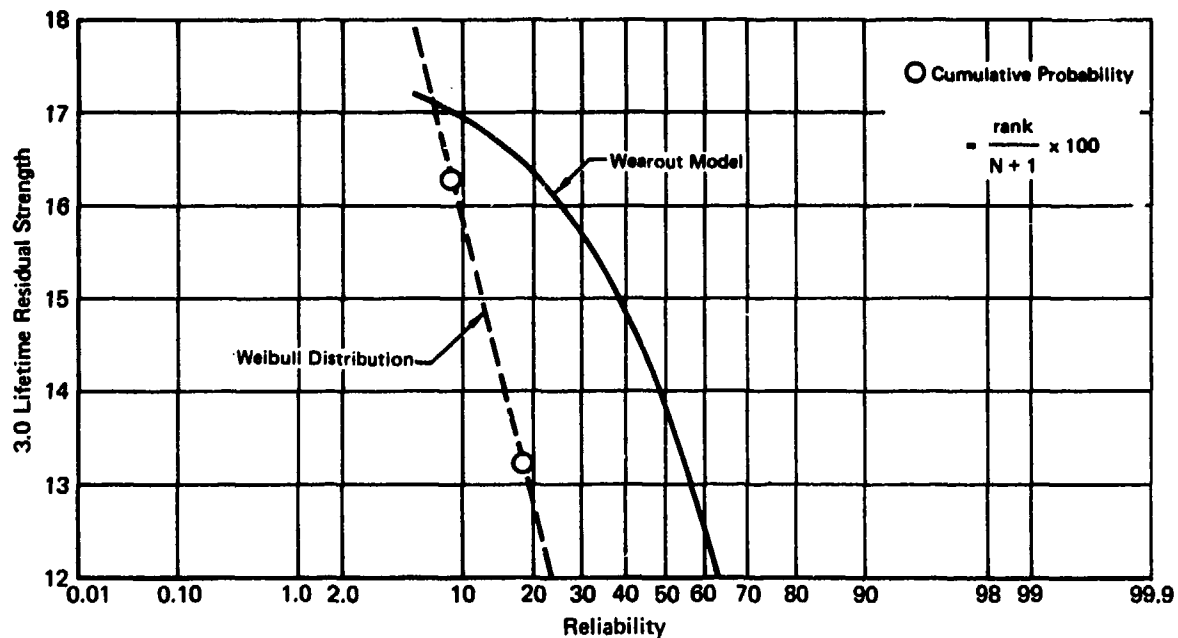


FIGURE 78 COMPARISON OF WEAROUT MODEL FOR SMALL SCALE STEP-LAP SPECIMEN AT 3.0 LIFETIMES WITH WEIBULL DISTRIBUTION

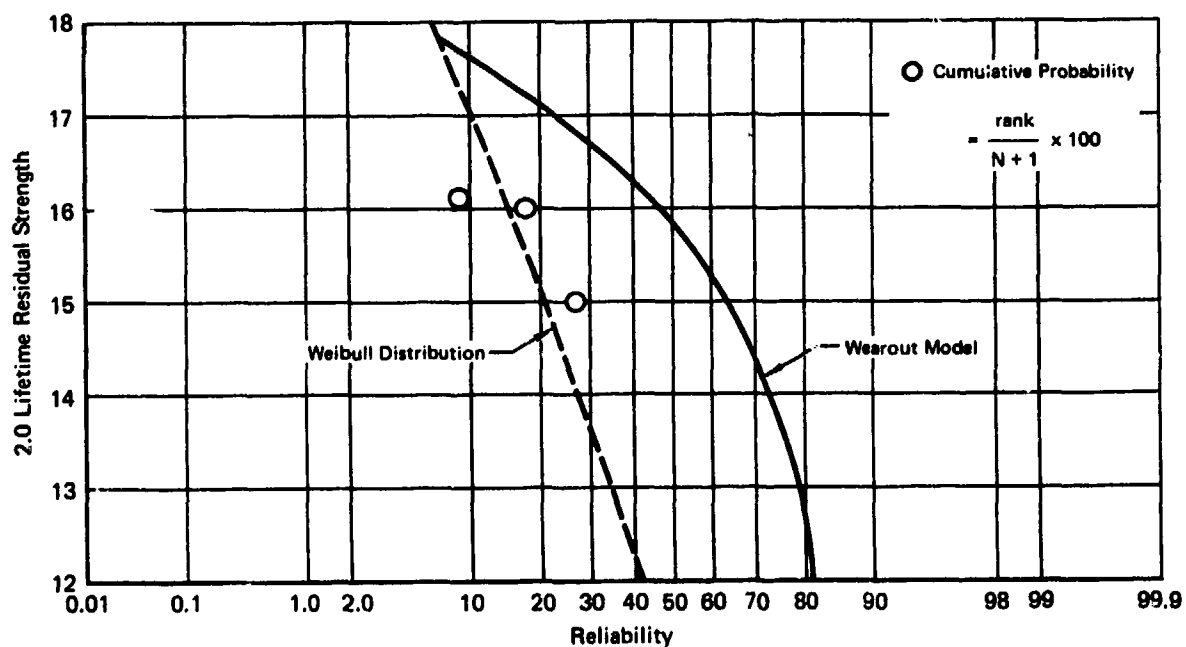


FIGURE 79 COMPARISON OF WEAROUT MODEL FOR SMALL SCALE STEP-LAP SPECIMENS AT 2.0 LIFETIMES WITH WEIBULL DISTRIBUTION

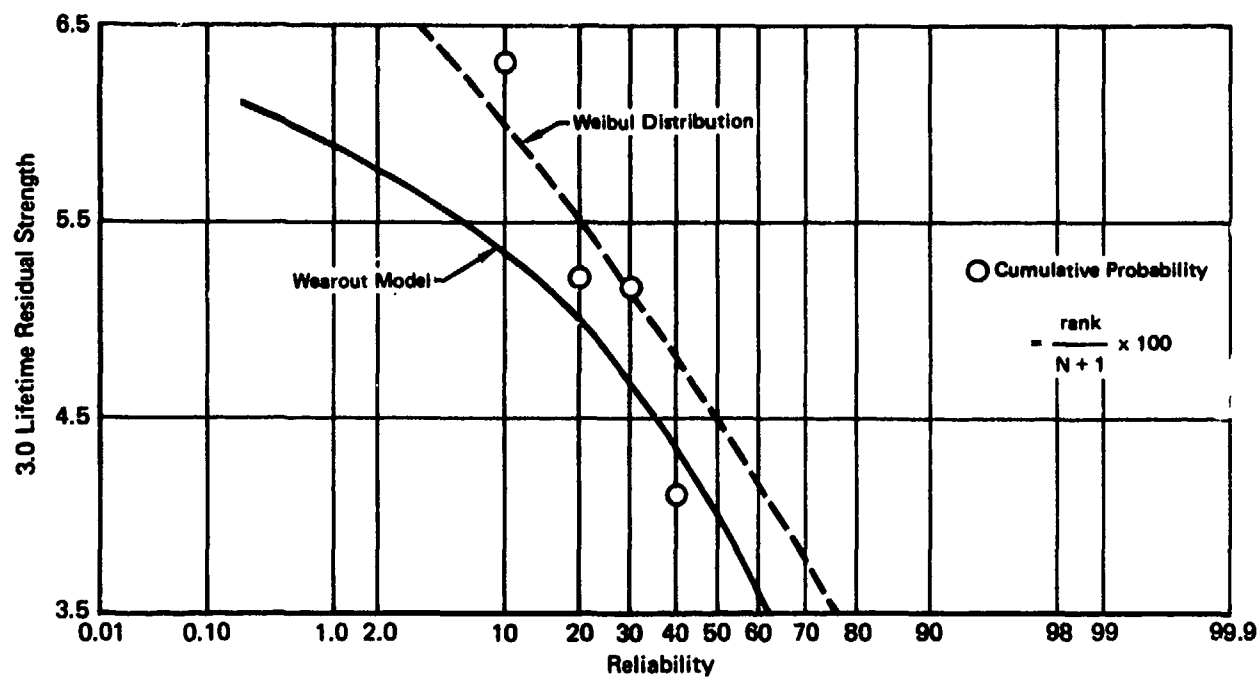


FIGURE 80 COMPARISON OF WEAROUT MODEL FOR SIMPLE SPECIMENS AT 3.0 LIFETIMES WITH WEIBULL DISTRIBUTION

SECTION 7

APPLICATION OF WEAROUT MODEL

In this section the wearout model derived in Section 6 is applied to address the subjects of effects of scale, dependence of Weibull parameters to specimen configuration, the effects of variations in spectrum and environment, proof testing and the inference that can be drawn from the analysis of test results from this program to the design of the F-15 kick splice plate joints.

7.1 Scaling

An evaluation of the scalability of bonded joints was made by comparing the results of the 70% scale step-lap specimen tests with those of the full scale step-lap specimen. It is surmised, based upon this evaluation, that bonded joints are scalable, but that because of practical considerations such as influence of tolerances and determination and control of adhesive thickness, scalability has not been conclusively proven.

It could be concluded that this joint was scaled if the following relations were identically satisfied:

- o The shape parameter, α , for 70% scale joint static strength should equal α for the full scale joint: $\alpha_s^{.7} = \alpha_s^{1.0}$.
- o The scale parameter, β , for the 70% scale joint static strength should be 70% of the corresponding β for full scale joint:
 $\beta_s^{.70} = .70 \beta_s^{1.0}$.
- o And similarly, the shape parameters for fatigue life should be equal:
 $\alpha_f^{.70} = \alpha_f^{1.0}$, and the scale parameters for fatigue life should scale:
 $\beta_f^{.70} = .70 \beta_f^{1.0}$ ($TLL^{.70} = .7 TLL^{1.0}$).

The actual parameter relations from Table 28 are as follows:

$$\begin{aligned}
 \alpha_s^{.70} &= 1.14 \alpha_s^{1.0} \\
 \beta_s^{.70} &= .856 \beta_s^{1.0} \\
 \alpha_f^{.70} &= .878 \alpha_f^{1.0} \\
 \beta_f^{.70} &= .505 \beta_f^{1.0} \quad (TLL^{.70} = .851 TLL^{1.0})
 \end{aligned}
 \tag{24}$$

The actual relationship between $TLL^{.70}$ and $TLL^{1.0}$ is not scaled because the test limit loads were not analytically determined based on an assumption of scalability but that the TLL for each specimen was selected by trial and error to give fatigue failures in the neighborhood of 4.0 lifetimes.

None of the experimental relations are identical to the expected relations. It is thus evident that it cannot be conclusively demonstrated that this joint scales. However, the relations do agree reasonably well considering the effects of tolerances and control of bondline thickness due to adhesive migration into the graphite-epoxy. It is felt that the approximation is close enough to indicate that theoretically joints can be scaled.

7.2 Translation of Parameters

The interest in determining which, if any, of the Weibull parameters of static strength, lifetime and residual strength distributions, translate unchanged from simple adhesive bonded joints to actual joints has been generated by the potential for cost savings (it would be much cheaper to develop shape parameters from simple joints than to use full scale specimens). This program was planned to illustrate if any of the shape parameters from simple specimens would translate unchanged to the full scale step lap specimen. By comparing the shape parameters in Table 28, it can be seen that static and lifetime shape parameters agree reasonably well.

7.3 Effect of Spectrum and Environmental Variations

To determine the effect of spectrum and environmental variations on fatigue life, several full scale step-lap specimens were tested to failure with the baseline spectrum modified in the following ways: 1) added low loads, 2) deleted high loads, 3) frequency of load application reduced to 1/8 of the baseline, and 4) relaxation time between missions increased to ten times the baseline. In addition, several specimens were tested at 350°F to evaluate sensitivity of Weibull parameters to temperature. A comparison of the BLU estimates of the Weibull parameters for baseline spectrum and environment with those for modified spectra and environment is presented in Table 28. The large increase in static shape parameter indicates that less scatter is observed at 350°F. The fatigue shape parameters are affected significantly only by the addition of low load levels and the reduction of the baseline frequency of load applications. In each case, less scatter is indicated. The fatigue scale parameter is reduced for added low load cycles, indicating that the baseline spectrum is unconservative in that

the observed lifetimes under any of the modified spectra would be shorter than indicated by the baseline data, for each modified spectrum. The addition of low loads is the most detrimental. It reduces the fatigue scale parameter to approximately 27 percent of the baseline value. The significant changes in the shape and scale parameters can probably be attributed to the limited number of specimens (3-6 specimens). More data are needed in this area before any definite conclusion can be reached. Indications are that more low load levels should be included in the spectrum when testing adhesive bonded joints than when testing metals. More effort is needed in this area.

7.4 Proof Testing of Bonded Joints

Proof testing has been proposed as a method of improving the reliability of a structure. In this method, each article is preloaded to a level which would reveal unacceptably weak members. For example, if a specific load level is selected for the proof test and the static strength probability distribution at zero time indicates that one percent of the population would fail below that load level, weak members would be eliminated by an initial proof test. Similarly, if the probability distribution at one-half lifetime indicates that ten percent of the population would fail below the proof load level, weak members would be eliminated by a proof test at one-half lifetime. The weak members eliminated by the proof testing would have been among the first articles to fail in fatigue, and therefore the time to first failure would be extended by their elimination.

The full scale step-lap specimen used in this program is representative of a conceptual application designed for an ultimate load of 15000 pounds per inch. Design limit load is 10000 pounds per inch. The conceptual application would experience maximum fatigue loads of 12,500 pounds per inch (125% DLL). A likely proof load for such a design would be 12,500 pounds. Proof testing at this level would have detected no weak elements. In fact, only five specimens of all those passing NDT failed at less than 12,500 pounds, and these, after fatigue testing, at 135% of DLL for from 2 to 5.5 lifetimes.

7.5 Implications of Wearout Model on Conceptual Structural Application

To determine what the wearout model implies about the capability of the conceptual structural application it must be recalibrated to reflect a residual strength at a given number of lifetimes equal to the maximum load in the fatigue spectrum (12500 pounds/inch) which is 125 percent of design limit load. The wearout model calibrated in Section 6 applies to a test limit load

(TLL) of 13500 pounds/in. This (TLL) was selected in order to obtain failure in about 4 lifetimes.

To recalibrate the model, values of α_f and β_f are needed for TLL = 10,000 (lbs/in.). To get these values, it is assumed that α_f is independent of load value as indicated in Reference 11. To obtain β_f , a plot of β_f vs TLL is required. In the absence of this data, it is impossible to determine what the probability is for the conceptual application having a certain residual strength at a lower test limit load than the 13500 pounds/inch used for fatigue lift testing.

The wearout model (Figure 76) indicates that the full scale joint has a 75 percent probability of having a residual strength of 16000 lbs/in. after 3 lifetimes of cycling at 135 percent of the design load spectrum. The design limit load (DLL) requirement for the conceptual application is 10,000 pounds/inch. There would be a high probability of having a residual strength of 10,000 pounds/inch after 3 lifetimes.

SECTION 8
COST SUMMARY

In this section a summary of the manhours required to fabricate the specimens, to Non-Destructive Test (NDT) the specimens and to perform the required strength and fatigue life testing is presented. This summary will be useful in estimating cost of fabricating and testing specimens and actual airframe bonded joints similar to those used in this program.

8.1 Specimen Cost

The total time required to fabricate and NDT the simple, small scale step-lap and full scale step-lap specimen is summarized in Table 30. The fabrication cost of each of these specimens is broken down in Tables 31, 32, and 33.

8.2 Test Cost

The estimated cost of running the tests conducted in this program is presented in Table 34.

TABLE 30
SUMMARY OF SPECIMEN COSTS

Specimen Identification	Materials ⁽¹⁾ Costs	NDT Costs (mhrr)	Fabrication ⁽²⁾ Costs (mhrr)
Simple Specimen	\$1.30	0.80	1.39
Small Scale Step-Lap	\$7.75	1.40	5.46
Full Scale Step-Lap	\$22.10	1.40	5.60

(1) Allowing 20% for scrappage

(2) Spreading set-up costs over total number of specimen fabricated

TABLE 31 SIMPLE SPECIMEN FABRICATION COST BREAKDOWN

Operation Number	Operation	Cost in Hrs. for First 10	Cost in Hrs. for Additional 10
1	Engineering liaison, and engineering effort required to establish design, fabrication and machining procedures for making a simple joint panel assembly to provide 10 simple joint test specimens.	5.0	0.0
2	Chem-Mill titanium sheet stock to required thickness.	4.0	0.0
3	Conventionally machine titanium into details required to fabricate a simple joint panel assembly.	4.0	1.0 (2)
4	Fabricate aluminum dams and cover plates required to fabricate the simple joint panel assembly.	0.5	0.5
5	Lay-up the graphite/epoxy and MMS-307 Type I film adhesive assemblies required to fabricate the simple joint panel assemblies.	2.0	0.5
6	Clean and prime titanium details from Operation No. 3.	2.0	0.5
7	Assemble the simple joint panel assembly and the required layup configuration.	2.0	1.0
8	Cure the simple joint panel assembly.	4.0	0.0
9	Remove the simple joint panel assembly from the layup configuration.	1.0	0.5
10	Post-cure the simple joint panel assembly.	0.5	0.0
11	Machine the simple joint panel assembly into simple joint test specimens using a diamond cut-off wheel.	6.0	6.0
12	Remove titanium spacer details from the simple joint test specimens and clean up and identify the test specimens.	1.5	1.5
Totals		32.5	11.5

Notes:

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1. Cost breakdown is based upon fabricating a simple joint panel assembly which provides 10 simple joint test specimens.
2. Cost breakdown is based upon stacking two pieces of titanium sheet stock and machining both pieces to the required lengths and widths simultaneously.
3. The cost in hours for additional test specimens (in 10 specimen increments) is generally applicable up to a total quantity of approximately 50 test specimens. For quantities of specimens greater than 50, e.g., 100, the cost in hours noted for the first 10 specimens should be multiplied by 2 and the cost in hours noted for additional 10 specimens should be multiplied by 8. If the quantity of specimens are to be fabricated at various times to simulate production runs the cost in hours noted for the first 10 specimens for Operation Nos 5 through 10 should be included as many times as the required number of simulated production runs.

**TABLE 32 SMALL SCALE STEP-LAP SPECIMEN FABRICATION COST
BREAKDOWN**

Operation Number	Operation	Cost in Hrs. for First 10	Cost in Hrs. for Additional 10
1	Engineering liason, and engineering effort required to establish design, fabrication and machining procedures for making a small step-lap panel assembly which provides 10 small step-lap test specimens.	24.0	0.0
2	Rough saw two pieces of titanium from 1/4 inch thick stock.	3.0	3.0
3	Machine two pieces of titanium to required thickness holding required flatness and parallelism.	4.0	4.0
4	Machine two pieces of titanium to required width and length.	4.0	1.0 (3)
5	Machine initial step into each side of each piece of titanium.	3.0	3.0
6	Drill tooling holes in one titanium detail.	0.5	0.0
7	Fabricate one Chem-Mill template using titanium detail from Operation No. 6.	8.0	8.0
8	Drill tooling holes in remaining titanium detail using template from Operation No. 7.	0.3	0.3
9	Chem-Mill remaining steps into each side of each piece of titanium using template from Operation No. 7.	8.0	8.0
10	Machine Chem-Milled titanium to required length.	1.0	1.0
11	Fabricate aluminum cover plates required to fabricate the panel assembly.	0.2	0.2
12	Layup 13 graphite/epoxy laminates (1 configuration for each step on each side and 1 configuration for the land area between the titanium) required to fabricate the panel assembly.	6.0	1.5
13	Clean and prime the titanium details from Operation No. 10.	2.0	0.5
14	Install titanium details in assembly fixture.	0.3	0.3
15	Cut MMS-307 Type I film adhesive strips and apply to both sides of each titanium detail. Install graphite/Epoxy laminate in the land area between the titanium and cover the strips of MMS-307 Type I film adhesive	1.5	1.5
16	Assemble the 12 remaining graphite/epoxy laminates from Operation No. 12 into the required panel assembly configuration.	2.0	2.0
17	Place the completed panel assembly into the required layup configuration.	2.0	2.0
18	Cure the panel assembly.	4.0	4.0
19	Remove the panel assembly from the layup configuration.	1.5	0.5
20	Post-cure the panel assembly.	0.5	0.0
21	Machine the panel assembly into test specimens	16.0	16.0
22	Cleanup and identify test specimens.	1.5	1.5
	Total	93.3	50.3

Notes:

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1. Cost breakdown is based upon fabricating a small step-lap panel assembly which provides 10 small test specimens
2. Cost breakdown does not include 12 hours required to design the required assembly fixture nor does it include the 48 hours required to fabricate two such fixtures. The fixture was designed to accommodate both the small and intermediate step-lap panel assemblies so that the cost could be spread out over the entire step-lap panel assembly fabrication
3. Cost breakdown is based upon stacking 4 pieces of titanium and machining all pieces simultaneously
4. The cost breakdown is generally applicable up to a total quantity of 20 specimens in that only two assembly fixtures were fabricated. However, in estimating for quantities of specimens greater than 20, the cost in hours noted for the first 10 specimens for Operation Nos. 1, 6, 7 and 11 should be deleted and the cost in hours noted for additional 10 specimens for Operation No. 11 should be deleted
5. Operation Nos. 6, 7, 8, 9 and 10 may be deleted and replaced by an operation involving the conventional machining of the required number of steps into the titanium details especially when only a limited number of test specimens are to be fabricated

TABLE 33 FULL SCALE STEP-LAP SPECIMEN FABRICATION COST BREAKDOWN

Operation Number	Operation	Cost in Hrs for First 10	Cost in Hrs for Additional 10
1	Engineering liaison, and engineering effort required to establish design, fabrication and machining procedures for making an intermediate step-lap panel assembly which provides 10 intermediate step-lap test specimens.	24.0	0.0
2	Rough saw two pieces of titanium from 1/2 inch thick stock.	3.5	3.5
3	Machine two pieces of titanium to required thickness holding required flatness and parallelism.	5.0	5.0
4	Machine two pieces of titanium to required width and length.	4.5	1.5 (1)
5	Machine initial step into each side of each piece of titanium.	3.5	3.5
6	Drill tooling holes in one titanium detail.	0.5	0.0
7	Fabricate one chem-mill template using titanium detail from Operation Number 6.	8.0	8.0
8	Drill Tooling Holes in Remaining Titanium Detail Using Template From Operation Number 7	0.3	0.3
9	Chem-Mill Remaining Steps Into Each Side of Each Piece of Titanium Using Template from Operation Number 7	4.0	2.0
10	Machine chem-milled titanium to required length.	1.0	1.0
11	Fabricate aluminum cover plates required to fabricate the panel assembly.	0.2	0.2
12	Layup 13 graphite/epoxy laminates (1 configuration for each step on each step on each side and 1 configuration for the land area between the titanium) required to fabricate the panel assembly.	6.0	1.5
13	Clean and prime the titanium details from Operation Number 10.	2.0	0.5
14	Install titanium details in assembly fixture.	0.3	0.3
15	Cut MMS-307 Type I film adhesive strips and apply to both sides of each titanium detail. Install graphite/epoxy laminate in the land area between the titanium and cover with strips of MMS-307 Type I film adhesive.	1.5	1.5
16	Assemble the 12 Remaining Graphite/Epoxy Laminates from Operation Number 12 into the Required Panel Assembly Configuration	2.0	2.0
17	Place the completed panel assembly into the required layup configuration.	2.0	2.0
18	Cure the Panel Assembly	4.0	0.0
19	Remove the panel assembly from the layup configuration.	1.5	0.5
20	Post-cure the panel assembly	0.5	0.0
21	Machine the panel assembly into test specimens	18.0	18.0
22	Cleanup and identify test specimens.	1.5	1.5
Totals		97.8	50.8

Notes:

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1. Cost breakdown is based upon fabricating an intermediate step-lap panel assembly which provides 10 intermediate step-lap test specimens
2. See note 2 for small step-lap cost breakdown
3. See note 3 for small step-lap cost breakdown
4. See notes 4 and 5 for small step-lap cost breakdown

TABLE 34 ESTIMATED COST TO CONDUCT TESTS

Type Test	Spectrum Description	Temperature	Set Up Time (Manhours)	Test Time per 1000 Spectrum Hrs (Manhours)	Test Time (Manhours)
Static	N/A	R.T.	1	0	0.50
Static	N/A	350°F	1	0	0.75
Fatigue	Baseline	R.T.	0	0.42	0
Fatigue	Baseline	350°F	0	0.42	0
Fatigue	Low Loads Included	R.T.	0	3.32	0
Fatigue	High Loads Excluded	R.T.	0	0.42	0
Fatigue	1/8 Baseline Frequency	R.T.	0	3.36	0
Fatigue	10 Times Baseline Relaxation	R.T.	0	2.22	0

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SECTION 9

CONCLUSIONS AND RECOMMENDATIONS

The "Reliability of Step-Lap Bonded Joints" program has demonstrated that the wearout model derived in Appendix B can be successfully used to predict the residual strength characteristics of adhesive bonded joints under a given spectrum and environment. The fatigue spectrum utilized represented fighter aircraft flight by flight loading and was developed using random noise theory and actual fighter and attack training data to establish appropriate PSD shapes for fighter aircraft maneuvering time histories. Indications are that the exclusion of low load levels from the spectrum and the use of short relaxation times between missions may lead to unconservative estimates of fatigue life. However, this observation is based on very few data points and additional testing is required to verify these trends. The program has shown that certain Weibull parameters used in the development of a wearout model of a full scale adhesive bonded joint, namely α_g , can be reasonably approximated by the same parameter developed for simple specimens which fail in similar modes. It was shown that the design procedures used for the conceptual structural application, produced a highly reliable structure. Finally, it was illustrated that although bonded joints can be theoretically scaled the problem of obtaining scaled adhesives, and controlling tolerances, makes scaling impractical and not economically justified in most cases.

Based upon the results of the "Reliability of Step-Lap Bonded Joints" program the following recommendations are made:

- (1) Further work should be done to study the effect of spectrum variations, especially the exclusion of low load levels and the use of short relaxation times, on the fatigue life of adhesive bonded joints and that the wearout model be used in the study.
- (2) A study should be conducted to determine what uncontrolled variables lead to the batch effects in the fabrication of graphite-epoxy-to-titanium bonded joints.
- (3) The elastic-plastic analysis procedure for adhesive bonded joints along with available adhesive shear stress strain curves should be included in the "Structural Design Guide for Advanced Composite Application."
- (4) Further work should be conducted to determine moisture effects on graphite-epoxy-to-titanium bonded joints.

- (5) Further work should be conducted to establish NDT acceptance criteria for wide graphite-epoxy to titanium splice-plates such as those found in representative aircraft structure.

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APPENDIX A COMPUTER PROGRAM A4EGX

A.1 A4EGX Input Data Required

The computer program A4EGX computes the elastic and elastic-plastic joint strength of any step-lap bonded joint. The program prints out the most critical adherend and adhesive stresses for each step of the joint. The input data is printed out to supplement the solution output. The program accounts for arbitrary combinations of adherend stiffnesses, thermal imbalances, non-uniform step thickness increments, and non-uniform step lengths.

The input data required is read in by three card sets.

CARD SET 1: (Format I2 - One Card)

Number of joint configurations user desires to solve
(card sets 2 & 3 must be input for each configuration)

CARD SET 2: (Format 8F10.3 - 2 Cards)

TAUMAX	~	Peak Adhesive Shear Stress (τ_p)
G	~	Elastic Adhesive Shear Modulus
GAMMAX	~	Maximum Adhesive Shear Strain ($\gamma_e + \gamma_p$)
GAMMAE	~	Elastic Adhesive Shear Strain (must exactly equal τ_p/G)
ETA	~	Bond Line Thickness (η)
ALPHAO	~	Outer Adherend Coefficient of Thermal Expansion (α_o)
ALPHA1	~	Inner Adherend Coefficient of Thermal Expansion (α_1)
DELTEMP	~	Temperature Differential ($T_{\text{operating}} - T_{\text{stress free}}$)
SGNLD	~	+1. For Tension Joint Loading -1. For Compression Joint Loading
ANSTEP	~	Number of Steps in the Joint (controls number of cards required in card set 3)

CARD SET 3: (Format 7F10.3 - Number of Cards Required is *N = ANSTEP + 1)

THICKO (N)	~	Sum of Outer Adherend Thicknesses (In)
THICK1 (N)	~	Thickness of Inner Adherend (In)
STEPL (N)	~	Length of Nth Step (In)
ETOTR (N)	~	Net Extensional Stiffness of Outer Adherend ($E_o t_o$) at Nth Step
ETINR (N)	~	Extensional Stiffness of Inner Adherend ($E_1 t_1$) at Nth Step

STROTR (N) ~ Net Strength of Outer Adherends (Lb/In) at Nth Step

STRINR (N) ~ Strength of Inner Adherend (Lb/In) at Nth Step

- * The last step required is actually the portion of the joint just after the final step terminates. (Ref. Figure A-1)

Thus at the last step:

THICKO (N) = 0.

THICKI (N) = THICKI (N-1)

STEPL (N) = 0.

ETINR (N) = ETINR (N-1)

ETOTR (N) = 0.

STRINR (N) = STRINR (N-1)

STROTR (N) = 0.

The card set formats listed above are for use on the IBM 370/195.

The data given on card set 2 needs further elaboration. The data needed to typify the adhesive system is obtained by modeling the actual adhesive stress-strain curve, obtained from torsion ring or thick adherend testing if available, into an elastic-plastic curve.

Consider the following ductile adhesive stress-strain curve, Figure A-2, at room temperature and the idealized elastic-plastic equivalent. The variables needed for card set 2 are defined by this figure.

A.2 Stepped-Lap Joint Parametric Trends

Using the A4EGX analytic procedure certain parametric trends become evident with respect to adhesive bonded step-lap joints. The following characteristics should be acknowledged and accounted for in both the design and analysis of an optimized step-lap joint configuration.

- a. Each step is loaded via a lightly loaded elastic trough with high elastic spikes developing at the step-to-step interfaces. At the final step(s) of the joining plastic "plateaus" may develop instead of the elastic spikes.
- b. The ductility of the adhesive system plays the dominate role in suppressing the elastic spikes, increasing the average adhesive shear stress per step, and promoting formation of the plastic "plateau" regions.
- c. On any one step, beyond a certain overlap length, no additional gains in load carrying capacity are achieved. To acquire more load capacity more steps of reduced step thickness are required.

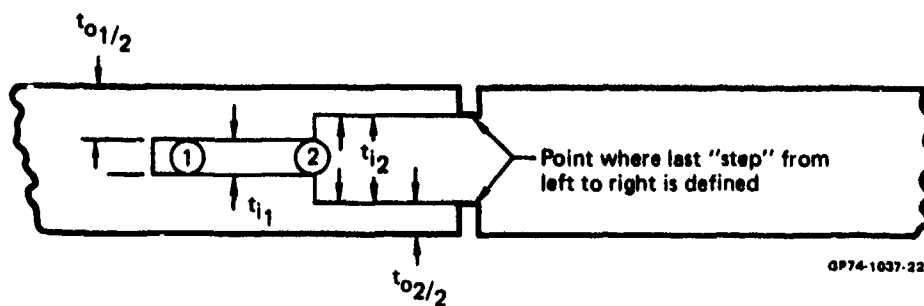


FIGURE A-1 TWO STEP JOINT

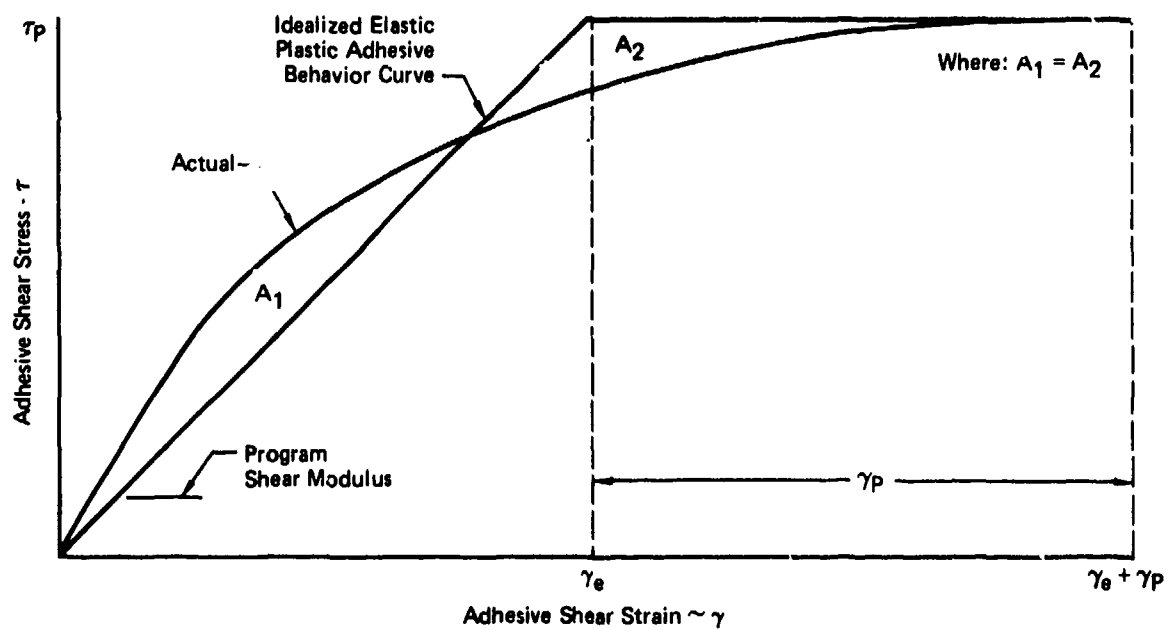


FIGURE A-2 TYPICAL ADHESIVE STRESS-STRAIN CURVE

- d. Adherend stiffness imbalance always effects a reduction in joint efficiency. The end of the joint from which the less stiff adherend extends will have intensified shear strains, thus the imbalance reduces strength by unloading the less critical end.
- e. Adherend thermal mismatch may cause the critical end of a step lap joint to change ends when the load is reversed. This step-lap joint characteristic requires analyses to be performed with the maximum tensile and maximum compression loads to determine the limiting joint strength capability.
- f. In a reasonably well designed step-lap joint, the joint load capacity is basically determined by the end three steps of the more critical end of the joint. In fact, once a joint is fairly well optimized major changes to steps other than the first three will cause very little change in overall joint capability. The reality of this type of internal stress distribution in step lap joints dictates that the average adhesive shear stress, in the critical end's first three steps, will in reality be considerably higher than the average adhesive shear stress of the overall joint or of any remaining joint step.

A.3 Program Listing

The program listing follows:

0674-9027-908

GP74-1037-109

APPENDIX B
DERIVATION OF WEAROUT MODEL

Derivation of the Wearout Model

Two assumptions are made. First assume that the damage rate accumulation may be approximate by a power-law growth equation (B-1)

$$\frac{\partial C}{\partial t} = A_0 F^{2r} C^r \quad (B-1)$$

where C is the dimension of the critical damage zone and F is the critical load.

Second, assume that the critical load is related to an apparent toughness parameter, K, by

$$F \sqrt{C} = K \quad (B-2)$$

These assumptions appeal to intuition because of their similarity to relations often used in classical work (for instance Reference B-1). Namely,

$$\frac{F}{A} = \frac{K}{\sqrt{\pi C}} \quad (B-3)$$

$$\frac{\partial C}{\partial t} = A_1 K^{2r} \quad (B-4)$$

From equation (B-3)

$$K^{2r} = \frac{\pi^r}{A^{2r}} F^{2r} C^r \quad (B-5)$$

Putting (B-5) into (B-4) gives

$$\frac{\partial C}{\partial t} = A_2 F^{2r} C^r \quad (B-6)$$

which is the classical relation which furnishes the intuitive appeal of the first assumption. Equation (B-3) is the classical relation which provides the intuitive appeal of the second assumption.

Integrating (B-1) gives equation (B-7)

$$\int_{C_0}^C \frac{\partial C}{C^r} = \int_{t_0}^t A_0 F^{2r} dt \quad (B-7)$$

Since the spectrum was developed as a random process that preserved the expected cumulative statistics for the F-15, $F(t)$ is a stationary random process and the right hand side of (B-7) becomes

$$A_3 (t - t_0) \quad (B-8)$$

Thus (B-7) becomes

$$\frac{1}{C_0^{r-1}} + \frac{1}{C^{r-1}} = A_3 (r - 1) (t - t_0) \quad (B-9)$$

From (B-2)

$$C^{r-1} = \frac{K^{2(r-1)}}{F^{2(r-1)}} \quad (B-10)$$

Putting (B-10) into (B-9) gives

$$F(t_0)^{2(r-1)} - F(t)^{2(r-1)} = A_4 (r - 1) (t - t_0) \quad (B-11)$$

Assume the initial strength distribution is Weibull

$$P [F(t_0) > F] = \exp - [F/\beta_s]^{\alpha_s} \quad (B-12)$$

To produce the time dependent residual strength function use (B-11) as shown below,

$$\begin{aligned}
 P [F(t) > F] &= P \{ [F(t_0)^{2(r-1)} - A_4 (r-1)(t-t_0)]^{\frac{1}{2(r-1)}} > F \} \quad (B-13) \\
 &= P \{ [F(t_0)^{2(r-1)} - A_4 (r-1)(t-t_0)] > F^{2(r-1)} \} \\
 &= P \{ F(t_0) > [F^{2(r-1)} + A_4 (r-1)(t-t_0)]^{\frac{1}{2(r-1)}} \}
 \end{aligned}$$

But the probability statement in (B-13) can be expressed by direct substitution into (B-12) as,

$$P [F(t) > F] = \exp - \left[\frac{F^{2(r-1)} + A_4 (r-1)(t-t_0)}{\beta_s^{2(r-1)}} \right]^{\alpha_f} \quad (B-14)$$

where

$$\alpha_f = \frac{\alpha_s}{2(r-1)}$$

Another relation is needed to allow the determination of A_4 . This relation is provided by showing that (B-14) is approximately equal to a Weibull distribution for fatigue lifetime if fatigue failures are obtained at a load level $F_{TRU} \leq \beta_s/2$, which is the case for joints used in this program. First take $t_0 = 0$ and rewrite (B-14) as,

$$\begin{aligned}
P [F(t) > F_{TRU}] &= \exp - \left\{ \frac{t}{\left[\frac{\beta_s}{A_4 (r-1)} \right]} + \frac{F_{TRU}}{\beta_s} \right\}^{2(r-1) \alpha_f} \\
&= \exp - \left\{ \frac{t}{\left[\frac{\beta_s}{A_4 (r-1)} \right]} + \text{error} \right\}^{\alpha_f} \\
&\approx \exp - \left\{ \frac{t}{\beta_f} \right\}^{\alpha_f} = P (T > t)
\end{aligned}
\tag{B-15}$$

where

$$\beta_f = \frac{\beta_s}{A_4} \frac{2(r-1)}{(r-1)}
\tag{B-16}$$

Equation (B-16) is the needed relation.

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APPENDIX C

COMPUTER PROGRAM ABDMATM - COMPOSITE LAMINATE PROPERTY CHARACTERIZATION

C.1 Program Description

Procedure ABDMATM calculates the initial laminate elastic moduli, stiffness matrix [A], bending extensional matrix [B], and flexural stiffness matrix [D]. The above output is valid for any laminate stacking sequence or multi-material system.

A note of caution is directed toward the application of the laminate elastic properties (E_x , E_y , G_{xy} , ν_{xy}); in design it must be realized that the four elastic constants are sufficient in number to adequately characterize only an orthotropic laminate. All laminates of higher anisotropy (which is the case if a laminate does not possess a balanced and symmetric stacking) require a number of elastic constants greater than four to adequately characterize their bending-shear-extensional behavior.

C.2 Input Instructions:

- o The data required are the material characteristics of the individual unidirectional material systems involved.

E_{11} , E_{22} , ν_1 , and G

where:

E_{11} = 0° ply longitudinal (fiber) modulus

E_{22} = 0° ply transverse (matrix) modulus

ν_1 = major Poisson's ratio

G = shear modulus

- o The program is conversational in nature and generates its own input data instructions.

C.3 Program Listing

The program listing follows:


```

105AD
20 DIMENSION AH(40),TH(40),QBAR(40,3,3),Q11(40),Q22(40),Q12(40)
30 DIMENSION AT(40),AZ(3,3),U1(40),G(40),AZZ(3,3),AZZZ(3,3)
40&,A(3,3),B(3,3),D(3,3),A0T(3,3),Q66(40),ANT(8),E1(40),E2(40)
50&,AT3(3,3),AI(3,3),AL(3,3)
60 OUTPUT, 'HOW MANY PROBLEMS DO YOU WISH TO RUN'
70 READ, KPR
80 DO 190 I1K = 1, KPR
90 OUTPUT, 'HOW MANY PLIES IN YOUR LAMINATE?'
100 READ, MA
110 IF(I1K.GT.1) GO TO 1412
120 OUTPUT, 'AFTER EACH QUESTION MARK(?) INPUT'
130 OUTPUT, 'THICKNESS, PLY ORIENTATION, AND THE'
140 OUTPUT, 'NUMBER 0 OR 1.....'
150 OUTPUT, 'INPUT 1 FOR THE FIRST PLY AND FOR'
160 OUTPUT, 'EACH PLY WHICH HAS DIFFERENT MATL'
170 OUTPUT, 'PROPERTIES FROM THE PREVIOUS PLY.'
180 OUTPUT, 'AFTER INPUTTING A 1 THE MATL'
190 OUTPUT, 'PROPERTIES ARE DESIRED'
200 OUTPUT, 'INPUT E1,E2,U1,G.....AFTER ?'
210 OUTPUT, 'FOR ALL PLIES AFTER THE 1ST'
220 OUTPUT, 'IF THE MATL PROPERTIES ARE'
230 OUTPUT, 'THE SAME INPUT A 0(ZERO)'
240 OUTPUT, 'THEN INPUT A NEW PLY THICKNESS,'
250 OUTPUT, 'ORIENTATION AND A 0 OR 1 AGAIN.'
260 1412 CONTINUE
270 DO 149 I1K=1, MA
280 READ, AT(I1K), TH(I1K), JK
290 IF(I1K.EQ.1) GO TO 148
300 IF(JK.EQ.1) GO TO 148
310 E1(I1K)=E1(I1K-1)
320 E2(I1K)=E2(I1K-1)
330 U1(I1K)=U1(I1K-1)
340 G(I1K)=G(I1K-1)
350 GO TO 149
360 148 READ, E1(I1K), E2(I1K), U1(I1K), G(I1K)
370 149 CONTINUE
380 MB=MA+1
390 DO 50 I2 = 1, MB
400 AH(I2) = 0.0
410 50 CONTINUE
420 DO 60 I3 = 2, MB
430 AH(I3) = AT(I3-1) + AH(I3-1)
440 60 CONTINUE
450 AHK = AH(MB)/2.0
460 DO 70 I4 = 1, MB
470 AH(I4) = AH(I4) - AHK

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480 A7T = 2.0*AHK
490 70 CONTINUE
500 D0 80 I5 = 1,MA
510 U2 = E2(I5)/E1(I5)*U1(I5)
520 DEL = 1.0 - U1(I5)*U2
530 Q11(I5) = E1(I5)/DEL
540 Q22(I5) = E2(I5)/DEL
550 Q12(I5) = Q11(I5)*U2
560 Q66(I5) = G(I5)
570 C0N = TH(I5) * (3.1415926536D0/180.0D0)
580 C0 = DC0S(C0N)
590 C02 = C0**2
600 C03 = C0**3
610 C04 = C02**2
620 SI = DSIN(C0N)
630 SI2 = SI**2
640 SI3 = SI**3
650 SI4 = SI2**2
660 SIC0 = SI2 * C02
670 QBAR(I5,1,1) = Q11(I5)*C04+2.0*(Q12(I5)+2.0*Q66(I5))*SIC0+
680&Q22(I5)*SI4
690 QBAR(I5,1,2) = (Q11(I5)+Q22(I5)-4.0*Q66(I5))*SIC0+
700&Q12(I5)*(SI4+C04)
710 QBAR(I5,1,3) = (Q11(I5) - Q12(I5) - 2.0*Q66(I5))*C03*SI +
720&(Q12(I5) - Q22(I5) + 2.0*Q66(I5))*SI3*C0
730 QBAR(I5,2,1) = QBAR(I5,1,2)
740 QBAR(I5,2,2) = Q11(I5)*SI4+2.0*(Q12(I5)+2.0*Q66(I5))*SIC0+
750&Q22(I5)*C04
760 QBAR(I5,2,3) = (Q11(I5) - Q12(I5) - 2.0*Q66(I5))*SI3*C0 +
770&(Q12(I5) - Q22(I5) + 2.0*Q66(I5))*C03*SI
780 QBAR(I5,3,1) = QBAR(I5,1,3)
790 QBAR(I5,3,2) = QBAR(I5,2,3)
800 QBAR(I5,3,3) = (Q11(I5) + Q22(I5) - 2.0*Q12(I5) - 2.0*Q66(I5))*
810&SIC0 + Q66(I5)*(SI4+C04)
820 80 CONTINUE
830 D0 100 I6 = 1,3
840 D0 90 J6 = 1,3
850 A(I6,J6) = 0.
860 B(I6,J6) = 0.0
870 D(I6,J6) = 0.
880 A0T(I6,J6) = 0.
890 90 CONTINUE
900 100 CONTINUE
910 D0 130 I6 = 1,3
920 D0 120 J6 = 1,3
930 D0 110 NN = 1,MA
940 AZ(I6,J6) = AH(NN+1) - AH(NN)
950 AZZ(I6,J6) = (AH(NN+1)**2 - AH(NN)**2)/2.
960 AZZZ(I6,J6) = (AH(NN+1)**3 - AH(NN)**3)/3.
970 A(I6,J6) = A(I6,J6) + QBAR(NN,I6,J6)*AZ(I6,J6)
980 B(I6,J6) = B(I6,J6) + QBAR(NN,I6,J6)*AZZ(I6,J6)

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990 D(I6,J6)=D(I6,J6)+QBAR(NN,I6,J6)*AZZZ(I6,J6)
1000 110 CONTINUE
1010 AT3(I6,J6)=A(I6,J6)/ATT
1020 120 CONTINUE
1030 130 CONTINUE
1040C
1050C *****COMPUTE THE A/T INVERSE MATRIX
1060C
1070 DET=(AT3(1,1)*AT3(2,2)*AT3(3,3))+(AT3(1,2)*AT3(2,3)*AT3(3,1))
1080& +(AT3(1,3)*AT3(2,1)*AT3(3,2))-(AT3(1,3)*AT3(2,2)*AT3(3,1))
1090& -(AT3(1,1)*AT3(2,3)*AT3(3,2))-(AT3(1,2)*AT3(2,1)*AT3(3,3))
1100 AL(1,1)=(AT3(2,2)*AT3(3,3)-AT3(2,3)*AT3(3,2))/DET
1110 AL(1,2)=(AT3(2,3)*AT3(3,1)-AT3(2,1)*AT3(3,3))/DET
1120 AL(1,3)=(AT3(2,1)*AT3(3,2)-AT3(2,2)*AT3(3,1))/DET
1130 AL(2,2)=(AT3(1,1)*AT3(3,3)-AT3(1,3)*AT3(3,1))/DET
1140 AL(2,3)=(AT3(1,2)*AT3(3,1)-AT3(1,1)*AT3(3,2))/DET
1150 AL(3,3)=(AT3(1,1)*AT3(2,2)-AT3(1,2)*AT3(2,1))/DET
1160 AL(2,1)=AL(1,2)
1170 AL(3,1)=AL(1,3)
1180 AL(3,2)=AL(2,3)
1190 D0 270 I=1,3
1200 D0 270 J=1,3
1210 AI(I,J)=AL(I,J)/ATT
1220 270 CONTINUE
1230 FE1=1.0/AL(1,1)
1240 FUI=-FE1*AL(1,2)
1250 FE2=1.0/AL(2,2)
1260 FG=1.0/AL(3,3)
1270 PRINT2
1280 2 FORMAT(///,16H      A MATRIX ,//)
1290 PRINT1,((A(M,N),N=1,3),M=1,3)
1300 PRINT3
1310 3 FORMAT(///,16H      B MATRIX ,//)
1320 PRINT1,((B(M,N),N=1,3),M=1,3)
1330 PRINT4
1340 4 FORMAT(///,16H      D MATRIX ,//)
1350 PRINT1,((D(M,N),N=1,3),M=1,3)
1360 PRINT5
1370 5 FORMAT(///,18H      A/T MATRIX ,//)
1380 PRINT1,((AT3(M,N),N=1,3),M=1,3)
1390 1 FORMAT(E10.3,5X,E10.3,5X,E10.3,/)
1400 OUTPUT,
1410 OUTPUT,"FOLLOWING ARE THE AVERAGE LAMINATE PROPERTIES"
1420 OUTPUT,
1430 PRINT20,FE1,FE2,FG,FUI
1440 20 FORMAT('E11= ',E10.2,5X,'F22= ',E10.2,5X,'G= ',E10.2,5X,
1450& 'NUI2= ',F4.2)
1460 OUTPUT,
1470 190 CONTINUE
1480 END

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APPENDIX D
CALCULATION OF WEIBULL PARAMETERS

D.1 Calculation of Weibull Parameters

The calculation of the Weibull parameters are presented in the tables which follow:

TABLE D-1 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR THE STATIC STRENGTH OF SIMPLE SPECIMENS

Specimen No.	i	F_{Si} (lb/in.)	$C(8, 8, i)$	$A(8, 8, i)$	$\ln F_{Si}$	$C(8, 8, i)$ $\ln F_{Si}$	$A(8, 8, i)$ $\ln F_{Si}$
73	1	5270	-0.093270	0.034052	8.56979	-0.799304	0.29182
83	2	5316	-0.098886	0.053552	8.57848	-0.848291	0.45939
84	3	5465	-0.093994	0.073452	8.60612	-0.808924	0.63214
7	4	6008	-0.079752	0.095062	8.70085	-0.693910	0.82712
20	5	6427	-0.053918	0.119768	8.76826	-0.472767	1.05016
46	6	6446	-0.010179	0.149934	8.77122	-0.089282	1.31510
25	7	6463	0.069325	0.191236	8.77385	0.608247	1.67788
58	8	6501	0.360675	0.282943	8.77971	3.166622	2.48416

Avg 5987

$\Sigma = 0.062391 \quad \Sigma = 8.73777$

$E(LB) = 0.08501680; E(CP) = -0.02386561$

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$\alpha_s = 14.6653 \quad \beta_s = 6223.8253$

TABLE D-2 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR LIFETIME OF SIMPLE SPECIMENS

Specimen No.	I	T_I (Lifetimes)	C (7, 7, I)	A (7, 7, I)	$\ln T_I$	C (7, 7, I) $\ln T_I$	A (7, 7, I) $\ln T_I$
6	1	1.6850	-0.108323	0.038743	0.52177	-0.05652	0.02021
88	2	2.1700	-0.113479	0.064086	0.77473	-0.08792	0.04965
66	3	3.0200	-0.103569	0.090785	1.10526	-0.11447	0.10034
21	4	4.4250	-0.078748	0.120971	1.48727	-0.11712	0.17992
23	5	4.5000	-0.032632	0.157657	1.50408	-0.04908	0.23713
24	6	4.5625	0.054727	0.207825	1.51787	0.08307	0.31545
32	7	4.7700	0.382022	0.319934	1.56235	0.59685	0.49985
Avg 3.5904						$\epsilon = 0.25481$	$\epsilon = 1.40255$

$$E (lb) = 0.09836496 \quad E (CP) = -0.02578937$$

$$\alpha_f = 3.53845 \quad \beta_f = 4.0360$$

TABLE D-3 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR THE STATIC STRENGTH OF SMALL SCALE STEP-LAP SPECIMENS

Specimen No.	I	FS_I (lb/in.)	C (10, 10, I)	A (10, 10, I)	$\ln FS_I$	C (10, 10, I) $\ln FS_I$	A (10, 10, I) $\ln FS_I$
1	1	15,392	-0.072734	0.027331	9.64160	-0.70127	0.26351
3	2	16,239	-0.077971	0.040034	9.69517	-0.75594	0.38814
69	3	16,955	-0.077242	0.052496	9.73832	-0.75221	0.51122
68	4	17,023	-0.071876	0.065408	9.74232	-0.70024	0.63723
67	5	17,261	-0.061852	0.079262	9.75620	-0.60149	0.77331
2	6	17,581	-0.045420	0.094638	9.77457	-0.44396	0.92505
70	7	17,683	-0.020698	0.112414	9.78036	-0.20243	1.09945
36A	8	18,256	0.017927	0.134239	9.81225	+0.17590	1.31719
66	9	18,484	0.085070	0.164178	9.82466	+0.83578	1.61299
65	10	18,638	0.324597	0.230001	9.83296	+3.19175	2.26159

$$\text{Avg} = 17,351$$

$$\Sigma = 0.04589 \quad \Sigma = 9.78968$$

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$$E (LB) = 0.06679250; E (CP) = -0.02050852$$

$$\alpha_s = 20.33760 \quad \beta_s = 17,830.57572$$

**TABLE D-4 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS
FOR LIFETIME OF SMALL SCALE STEP-LAP SPECIMENS**

Subgroup I

1 Specimen (19) Went 6.0 Lifetimes With No Failures

$$E(Ib) = 0.15690540 \quad E(CP) = 0.00888019 \quad \alpha_{fI} = 2.47115 \quad \beta_{fI} = 4.32114 \quad \gamma_I = 0.18611$$

Specimen No.	I	T_I	C (6, 5, I)	A (6, 5, I)	$\ln T_I$	C (6, 5, I) $\ln T_I$	A (6, 5, I) $\ln T_I$
26	1	2.0000	-0.16992	0.007521	0.69315	-0.11778	0.00521
9	2	2.0000	-0.166319	0.048328	0.69315	-0.11528	0.03350
7	3	3.5000	-0.129510	0.101608	1.25276	-0.16225	0.12729
27	4	4.1510	-0.054453	0.172859	1.42335	-0.07751	0.24604
31	5	4.7815	0.520201	0.669685	1.56475	0.81399	1.04789
						$\Sigma = 0.34117$	$\Sigma = 1.45993$

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Subgroup II

1 Specimen (30) Went 6.0 Lifetimes With No Failures

$$E(Ib) = 0.12760617 \quad E(CP) = 0.00130057 \quad \alpha_{fII} = 2.30340 \quad \beta_{fII} = 4.10855 \quad \gamma_{II} = 0.14627$$

Specimen No.	I	T_I	C (7, 6, I)	A (7, 6, I)	$\ln T_I$	C (7, 6, I) $\ln T_I$	A (7, 6, I) $\ln T_I$
28	1	1.8118	-0.138436	0.013524	0.59432	-0.08228	0.00804
32	2	1.9013	-0.140342	0.041588	0.64254	-0.09018	0.02672
23	3	2.4050	-0.121821	0.075499	0.87755	-0.10690	0.06625
25	4	3.4057	-0.082938	0.117461	1.22545	-0.10164	0.14394
17	5	4.5000	-0.015394	0.172092	1.50408	-0.02315	0.25884
40	6	4.8025	0.498931	0.579835	1.56914	0.78289	0.90984
						$\Sigma = 0.37874$	$\Sigma = 1.41363$

GP75-0332-73

**TABLE D-4 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS
FOR LIFETIME OF SMALL SCALE STEP-LAP SPECIMENS (Continued)**

Subgroup III

$$E(lb) = 0.08501680 \quad E(CP) = -0.02386561 \quad \alpha_{fIII} = 2.40593 \quad \beta_{fIII} = 3.93645 \quad \gamma_{III} = 0.09292$$

Specimen No.	I	T_I	$C(8, 8, I)$	$A(8, 8, I)$	$\ln T_I$	$C(8, 8, I) \ln T_I$	$A(8, 8, I) \ln T_I$
43	1	1.7698	-0.093270	0.034052	0.57087	-0.05324	0.01944
8	2	2.0000	-0.098886	0.053552	0.69315	-0.06854	0.03712
24	3	2.0000	-0.093994	0.073452	0.69315	-0.06515	0.05091
35	4	2.5000	-0.079752	0.095062	0.91629	-0.07308	0.08710
22	5	3.8913	-0.053918	0.119768	1.35874	-0.07326	0.16273
34	6	4.5000	-0.010179	0.149934	1.50408	-0.01531	0.22551
18	7	5.1798	0.069325	0.191236	1.64477	0.11402	0.31454
15	8	5.5000	0.360675	0.282943	1.70475	0.61486	0.48235
						$\Sigma = 0.38030$	$\Sigma = 1.38020$

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Subgroup IV

$$E(lb) = 0.09836496 \quad E(CP) = -0.02578937 \quad \alpha_{fIV} = 2.67860, \beta_{fIV} = 4.08920 \quad \gamma_{IV} = 0.10910$$

Specimen No.	I	T_I	$C(7, 7, I)$	$A(7, 7, I)$	$\ln T_I$	$C(7, 7, I) \ln T_I$	$A(7, 7, I) \ln T_I$
38	1	1.9018	-0.108323	0.038743	0.64280	-0.06963	0.02490
29	2	2.0000	-0.113479	0.064086	0.69315	-0.07866	0.04442
37	3	2.6483	-0.103569	0.090785	0.97392	-0.10087	0.08842
41	4	3.5000	-0.078748	0.120971	1.25276	-0.09865	0.15155
42	5	4.3935	-0.032632	0.157657	1.48013	-0.04830	0.23335
14	6	5.0303	0.054727	0.207825	1.61548	0.08841	0.33574
20	7	5.4010	0.382022	0.319934	1.68658	0.64431	0.53960
						$\Sigma = 0.33661$	$\Sigma = 1.41798$

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TABLE D-4 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR LIFETIME OF SMALL SCALE STEP-LAP SPECIMENS (Concluded)

Subgroup V

$$E(lb) = 0.08501680 \quad E(CP) = 0.02386561 \quad \alpha_{fV} = 2.93100 \quad \beta_{fV} = 4.01072$$

$$\gamma_V = 0.09292$$

Specimen No.	I	T_I	C (8, 8, I)	A (8, 8, I)	$\ln T_I$	C (8, 8, I) $\ln T_I$	A (8, 8, I) $\ln T_I$
33	1	2.0000	-0.093270	0.034052	0.69315	-0.06465	0.02360
10	2	2.0000	-0.098886	0.053552	0.69315	-0.06854	0.03712
64	3	2.2505	-0.093994	0.073452	0.81115	-0.07624	0.05958
21	4	3.5000	-0.079752	0.095062	1.25276	-0.09991	0.11909
13	5	4.0550	-0.053918	0.119768	1.39995	-0.07548	0.16767
39	6	4.1050	-0.010179	0.149934	1.41221	-0.01437	0.21174
6	7	5.0000	0.069325	0.191236	1.60944	0.11157	0.30778
18	8	5.2750	0.360675	0.282943	1.66298	0.59979	0.47053
						$\Sigma = 0.31217$	$\Sigma = 1.39711$

THE PARAMETERS FOR THE GROUP ARE

$$\alpha_f = 2.52659 \quad \beta_f = 4.12828$$

TABLE D-5 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR THE STATIC STRENGTH OF FULL SCALE STEP-LAP SPECIMENS AT ROOM TEMPERATURE, BASELINE SPECTRUM

Specimen No.	i	F_{Si} (lb/in.)	$C(10, 10, i)$	$A(10, 10, i)$	$\ln F_{Si}$	$C(10, 10, i) \ln F_{Si}$	$A(10, 10, i) \ln F_{Si}$
83	1	16,523	-0.072734	0.027331	9.71251	-0.70643	0.26545
49	2	18,868	-0.077971	0.040034	9.84522	-0.76764	0.39414
86	3	19,204	-0.077242	0.052496	9.86287	-0.76183	0.51776
82	4	20,137	-0.071876	0.065408	9.91031	-0.71231	0.64821
85	5	20,391	-0.061652	0.079263	9.92285	-0.61176	0.78651
84	6	20,763	-0.045420	0.094638	9.94093	-0.45152	0.94079
81	7	20,815	-0.020698	0.112414	9.94343	-0.20581	1.11778
2	8	21,254	0.017927	0.134239	9.96430	0.17863	1.33760
3	9	21,255	0.085070	0.164178	9.96435	0.84767	1.63593
1	10	21,821	0.324597	0.230001	9.99063	3.24293	2.29785

Avg = 20,103

$\Sigma = 0.05193$ $\Sigma = 9.94202$

GP74-1037-225

$E(LB) = 0.06679250$; $E(CP) = -0.02050852$

$\alpha_s = 17.96945$ $\beta_s = 20,762$

TABLE D-6 CALCULATION FOR THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR THE STATIC STRENGTH OF FULL SCALE STEP-LAP SPECIMENS AT 350°F

Specimen No.	i	F_{Si} (lb/in.)	$C(6, 6, i)$	$A(6, 6, i)$	$\ln F_{Si}$	$C(6, 6, i) \ln F_{Si}$	$A(6, 6, i) \ln F_{Si}$
61	1	15,728	-0.128810	0.044826	9.66320	-1.24472	0.43316
64	2	15,788	-0.132102	0.079377	9.66701	-1.27703	0.76734
63	3	16,138	-0.111951	0.117541	9.68893	-1.08469	1.13885
66	4	16,179	-0.064666	0.163591	9.69147	-0.62671	1.58544
62	5	16,244	0.031796	0.226486	9.69548	0.30828	2.19589
65	6	16,483	0.405733	0.368179	9.71008	3.93970	3.57505

Avg = 16,093.

$\Sigma = 0.01483$ $\Sigma = 9.69573$

GP74-1037-226

$E(LB) = 0.11657671$; $E(CP) = -0.02771574$

$\alpha_s = 59.55926$ $\beta_s = 16,240$

**TABLE D-7 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS
FOR LIFETIME OF FULL SCALE STEP-LAP SPECIMENS AT ROOM
TEMPERATURE, BASELINE SPECTRUM**

Subgroup I

7 Specimens (14, 16, 24, 28, 30, 33, 35) went 6.0 Lifetimes with no Failures

Specimen No.	i	T_i (Lifetimes)	C (14, 7, i)	A (14, 7, i)	$\ln T_i$	C (14, 7, i) $\ln T_i$	A (14, 7, i) $\ln T_i$
87	1	1.5000	-0.130915	-0.078656	0.40547	-0.05308	-0.03189
50	2	2.0000	-0.132521	-0.068666	0.69315	-0.09186	-0.04760
89	3	2.0000	-0.126123	-0.052554	0.69315	-0.08742	-0.03643
6	4	3.0325	-0.114051	-0.031776	1.10939	-0.12653	-0.03525
17	5	3.5000	-0.096788	-0.006522	1.25276	-0.12125	-0.00817
27	6	5.1510	-0.074184	0.023467	1.63919	-0.12160	0.03847
8	7	5.5927	0.674581	1.214708	1.72146	1.16127	2.09107

Avg = 3.2537

$\Sigma = 0.55953$ $\Sigma = 1.97020$

GP74-1037-211

E (LB) = 0.12547311; E (CP) = 0.08030259

$\alpha_f = 1.56296$

$\beta_f = 7.5502$

Subgroup II

6 Specimens (15, 18, 25, 29, 32, 34) went 6.0 Lifetimes with no Failures

Specimen No.	i	T_i (Lifetimes)	C (14, 8, i)	A (14, 8, i)	$\ln T_i$	C (14, 8, i) $\ln T_i$	A (14, 8, i) $\ln T_i$
79	1	2.0000	-0.112041	-0.048365	0.69315	-0.07766	-0.03352
88	2	2.5000	-0.114637	-0.039964	0.91629	-0.10504	-0.03662
48	3	3.1123	-0.110509	-0.027495	1.13536	-0.12547	-0.03122
7	4	4.1250	-0.101635	-0.011849	1.41707	-0.14402	-0.01679
9	5	4.5000	-0.088422	0.006905	1.50408	-0.13299	0.01039
31	6	5.4010	-0.070735	0.029002	1.68658	-0.11930	0.04891
19	7	5.5000	-0.048074	0.054897	1.70475	-0.08195	0.09359
26	8	5.6070	0.646052	1.036868	1.72402	1.11380	1.78758

Avg = 4.0932

$\Sigma = 0.32737$ $\Sigma = 1.82232$

GP74-1037-212

E (LB) = 0.10683049; E (CP) = 0.05038249

$\alpha_f = 2.72829$

$\beta_f = 6.30149$

GROUP ESTIMATES ARE

$\alpha_F = 2.19849$

$\beta_F = 6.8692$

TABLE D-8 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR LIFETIME, OF FULL SCALE STEP-LAP SPECIMENS AT ROOM TEMPERATURE WITH LOADING FREQUENCY SLOWED TO 1/8 OF BASELINE

Two Specimens (22 and 23) Went 6.0 Lifetimes with no Failure

Specimen No.	i	T_i (Lifetimes)	$C(6, 4, i)$	$A(6, 4, i)$	$\ln T_i$	$C(6, 4, i)$ $\ln T_i$	$A(6, 4, i)$ $\ln T_i$
20	1	2.0000	-0.225141	-0.063569	0.69315	-0.15806	-0.04408
21	2	3.2580	-0.209083	-0.006726	1.18111	-0.24695	-0.00794
13	3	4.1258	-0.146386	0.079882	1.41726	-0.20747	0.11321
12	4	5.1820	0.580610	0.990412	1.64519	0.95521	1.62942

$$\Sigma = 0.34473 \quad \Sigma = 1.69063$$

$$E(LB) = 0.21242254 \quad E(CP) = 0.0803562$$

GP74-1037-210

$$\alpha_f = 2.28462 \quad \beta_f = 5.61701$$

TABLE D-9 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR LIFETIME, OF FULL SCALE STEP-LAP SPECIMENS AT ROOM TEMPERATURE WITH ADDITIONAL LOW LOAD LEVELS INCLUDED

Specimen No.	i	T_i (Lifetimes)	$C(3, 3, i)$	$A(3, 3, i)$	$\ln T_i$	$C(3, 3, i)$ $\ln T_i$	$A(3, 3, i)$ $\ln T_i$
10	1	1.4060	-0.278666	0.081063	0.34075	-0.09496	0.02762
80	2	1.6543	-0.190239	0.251001	0.50338	-0.09576	0.12635
11	3	2.0000	0.468904	0.667936	0.69315	0.32502	0.46298

$$\text{Avg} = 1.6867$$

$$\Sigma = 0.13430 \quad \Sigma = 0.61695$$

GP74-1037-213

$$E(LB) = 0.25634620; E(CP) = -0.01842169$$

$$\alpha_f = 5.55864 \quad \beta_f = 1.8471$$

TABLE D-10 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR LIFETIME OF FULL SCALE STEP-LAP SPECIMENS AT ROOM TEMPERATURE WITH 10 TIMES BASELINE RELAXATION

Specimen No.	i	T _i (Lifetimes)	C (6, 6, i)	A (6, 6, i)	lnT _i	C (6, 6, i) lnT _i	A (6, 6, i) lnT _i
56	1	0.5000	-0.128810	0.044826	-0.69315	+0.08928	-0.03107
57	2	1.5000	-0.132102	0.079377	0.40547	-0.05356	0.03218
74	3	2.0000	-0.111951	0.117541	0.69315	-0.07760	0.08147
71	4	3.1108	-0.064666	0.163591	1.13488	-0.07339	0.18566
73	5	3.5000	0.031796	0.226486	1.25276	0.03983	0.28373
72	6	4.5000	0.405733	0.368179	1.50408	0.61025	0.55377

Avg = 2.5185

Σ = 0.53481 Σ = 1.10574

E (LB) = 0.11657671; E (CP) = -0.02771574

GP74-1037-214

α_f = 1.65186

β_f = 2.97119

TABLE D-11 CALCULATION OF THE BLU ESTIMATES OF THE WEIBULL PARAMETERS FOR LIFETIME, OF FULL SCALE STEP-LAP SPECIMENS AT ROOM TEMPERATURE WITH HIGH LOADS EXCLUDED

Specimen No.	i	T _i (Lifetimes)	C (6, 6, i)	A (6, 6, i)	lnT _i	C (6, 6, i) lnT _i	A (6, 6, i) lnT _i
90	1	1.1645	-0.278666	0.081063	0.15229	-0.04244	0.01235
78	2	4.1510	-0.190239	0.251001	1.42335	-0.27078	0.35726
77	3	4.1510	0.468904	0.667936	1.42335	0.71011	0.95071

Avg = 3.1556

Σ = 0.39689 Σ = 1.32032

E (LB) = 0.25634620; E (CP) = -0.01842169

GP74-1037-215

α_f = 1.87371

β_f = 3.7080

APPENDIX E

GRAPHICAL DETERMINATION OF WEIBULL PARAMETERS

If the strength, F , of a particular type of specimen has a Weibull distribution equation (F-1) holds

$$P_S (F > f) = \exp - (f/\beta)^\alpha \quad (F-1)$$

where P_S is the probability that a given specimen will have a strength greater f and α and β are the shape and scale parameter respectively.

Equation (F-1) can alternately be written as equation (F-2).

$$\ln \ln \frac{1}{P_S} = \alpha (\ln f - \ln \beta) \quad (F-2)$$

In this form it is seen that a plot of $\ln \ln \frac{1}{P_S}$ vs $\ln f$ is linear. The slope of that line is α and at the point where $\ln \ln \frac{1}{P_S} = 0$ (ie $P_S = 1/e$) $\ln f = \ln \beta$.