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Giant spin Hall effect in two-dimensional monochalcogenides

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Abstract

One of the most exciting properties of two dimensional materials is their sensitivity to external tuning of the electronic properties, for example via electric field or strain. Recently discovered analogues of phosphorene, group-IV monochalcogenides (MX with M = Ge, Sn and X = S, Se, Te), display several interesting phenomena intimately related to the in-plane strain, such as giant piezoelectricity and multiferroicity, which combine ferroelastic and ferroelectric properties. Here, using calculations from first principles, we reveal for the first time giant intrinsic spin Hall conductivities (SHC) in these materials. In particular, we show that the SHC resonances can be easily tuned by combination of strain and doping and, in some cases, strain can be used to induce semiconductor to metal transition that makes a giant spin Hall effect possible even in absence of doping. Our results indicate a new route for the design of highly tunable spintronics devices based on two-dimensional materials.

1. Introduction

The spin Hall effect (SHE) is a phenomenon emerging from spin-orbit coupling (SOC) in which an electric current or external electric field can induce a transverse spin current resulting in spin accumulation at opposite sample boundaries [1-4]. The charge/spin conversion without the need of applied magnetic fields makes the SHE an essential tool for spin manipulation in any spintronics devices [5, 6] and the subject of intensive theoretical and experimental research. The intrinsic SHE in crystals was predicted and observed experimentally in a variety of materials, ranging from doped semiconductors (GaAs) [2] to elemental metals with strong SOC, such as platinum, tantalum, palladium and tungsten [7-13]. It has been also investigated in metallic and semimetallic thin films [14] where SHE can be enhanced with respect to the corresponding bulk phase. Studies related to SHE in two dimensional (2D) materials are limited to only few works focused on transition metal dichalcogenides [15] and simple material models [16].

In this paper, a giant intrinsic SHE tunable by combination of strain and doping is predicted for the first time in monolayer group-IV monochalcogenides MX with M = Ge, Sn and X = S, Se, Te, often referred to as analogues of phosphorene due to their structural similarity [17–19]. The bulk parent compound has the orthorhombic crystal structure of black phosphorus (Pnma) and consists of weakly bonded van der Waals layers, making an exfoliation process a viable route to produce atomically thin films or single layer crystals; indeed, some materials from this family have been already synthesized experimentally [20-24]. As most 2D materials, group-IV monochalcogenides exhibit several extraordinary mechanical, electronic and optical properties. These include high flexibility, large thermal conductivity, giant piezoelectricity [25], multiferroicity [26, 27], superior optical absorbance [28–30], and even valley Hall effect [31], making them promising candidates to use in multifunctional devices. Finally, the strong SOC suggests their high potential for spintronics.

The group-IV monochalcogenides possess wide band gaps, which precludes existence of non-negligi-





ble spin Hall conductivity (SHC) at intrinsic chemical potential, similarly to conventional bulk semiconductors where significant electron or hole doping is needed in order to achieve a measurable spin Hall effect. Although our calculations show that a giant SHC could be reached with p- or n-type doping of $n_{h/e} = 1 \times 10^{14} \ e \ cm^{-2}$, which is an order of magnitude lower than in case of transition metal dichalcogenides [15], such values may still be difficult to reach experimentally. Here, we propose an alternative route to realize SHE in these materials. We demonstrate that compressive or tensile strain along any axis not only can tune the position of the SHC resonances, but can also induce semiconductor to metal transitions that make a giant spin Hall effect possible even in absence of doping. As such, different phases of SHE can be switched externally via strain allowing direct engineering of spintronics functionalities in these materials.

2. Methods

Our noncollinear DFT calculations were performed using the QUANTUM ESPRESSO code [32, 33] interfaced with the AFLOW π and PAOFLOW computational infrastructures [34, 35]. We used the generalized gradient approximation (GGA) in the parametrization of Perdew, Burke, and Ernzerhof (PBE) [36] and, to further improve the description of the electronic properties, a novel pseudo-hybrid Hubbard selfconsistent approach ACBN0 [37]. The ion-electron interaction was treated with the projector augmentedwave fully-relativistic pseudopotentials [38] from the pslibrary database [39] while the wavefunctions were expanded in a plane-wave basis of 50 Ry (500 Ry for the charge density). The Brillouin zone sampling at DFT level was performed following the Monkhorst-Pack scheme using a $24 \times 24 \times 1$ k-points grid, further increased to $140 \times 140 \times 1$ with PAOFLOW's Fourier interpolation method to accurately integrate spin Berry curvatures.

The intrinsic spin Hall conductivities were calculated using the PAOFLOW code [35] following the linearresponse Kubo-like formula [40–42]:

$$\sigma_{ij}^{s} = \frac{e^{2}}{\hbar} \sum_{\vec{k}} \sum_{n} f_{n}(\vec{k}) \Omega_{n,ij}^{s}(\vec{k})$$
$$\Omega_{n,ij}^{s}(\vec{k}) = \sum_{m \neq n} \frac{2 \mathrm{Im} \langle \psi_{n,\vec{k}} | f_{i}^{s} | \psi_{m,\vec{k}} \rangle \langle \psi_{m,\vec{k}} | v_{j} | \psi_{n,\vec{k}} \rangle}{(E_{n} - E_{m})^{2}}$$

where $\vec{j} = \{s, \vec{v}\}$ is the spin current operator with $s = \frac{\hbar}{2}\beta\Sigma(\beta, \Sigma: 4 \times 4 \text{ Dirac matrices})$ and $f_n(\vec{k})$ is the Fermi distribution function for the band *n* at \vec{k} . We note that, in contrast to most of reported calculations of SHC based on the above formula [8, 15, 42], we do not add any infinitesimal term δ in the denominator to avoid singularities if the bands are degenerate. We have evidence (see figure S1 in supplementary material (SM) (stacks.iop.org/TDM/6/025012/mmedia)) that using a finite δ in Kubo's formula leads to the unphysical behavior of non-zero values of SHC within the semiconductor's gap whose origin was unclear so far. Using perturbation theory for degenerate states to avoid numerical singularities ensures that σ_{ij}^{s} always vanishes at the Fermi level.

Figure 1 shows the 2D non-centrosymmetric unit cell of the phosphorene-like phase used in the calculations for all six compounds. It contains four atoms arranged in two buckled layers resembling a monolayer of black phosphorus with a mirror symmetry axis along x, representing one of the four ground states of the system [26, 27, 43]. The lattice constants and ionic positions were fully relaxed without including SOC whose influence on forces is known to be negligible. The electronic structure was then recalculated with SOC self-consistently. The vacuum region of 20 Å was set to prevent any interaction between spurious replicas of the slab. The configurations with the relaxed lattice constants were used as a starting point for the simulations of strained structures; we considered **IOP** Publishing

strains varying between -10% to 10% along *x* and *y* axis simultaneously, in each case relaxing the positions of the atoms. We analyzed, in total, 726 different structures. Further details of the calculations as well as additional results, including lattice constants, values of band gaps and convergence tests for SHC are reported in the SM (table S1, figure S1).

3. Spin Hall effect in unstrained monolayers

Let us first consider unstrained structures. Figures 2(a)and (b) summarize the relativistic band structures of sulfides, selenides and tellurides (green, blue and red lines, respectively), while panels (c) and (d) display their corresponding spin Hall conductivity as a function of chemical potential. Due to the reduced symmetry of two-dimensional structures, the only non-vanishing independent component is $\sigma_{xy}^{z} = -\sigma_{yx}^{z}$. Our band structures and the values of the band gaps calculated with the ACBN0 functional are in good agreement with existing simulations that use hybrid functionals and with available experimental data (see SM, table S1). Comparison of the scalarrelativistic band structures (plotted as black lines in panels (a) and (b)) with the fully relativistic ones, clearly indicates a strong impact of SOC, which induces several anti-crossings and splittings of the bands. These effects are moderate in selenides and most pronounced in tellurides given the heaviness of Te atoms. Although it is quite difficult to attribute particular features of the relativistic band structures to the specific peaks (resonances) in $\sigma_{xy}^{z}(E)$, one can easily observe that severe SOC-induced modifications in the electronic structure of GeTe and SnTe result in giant values of spin Hall conductivity, \sim 300 and 500 $(\hbar/e)(\Omega \times cm)^{-1}$, respectively, for higher binding energies. We note that even the resonances closest to the Fermi level (E_F) still achieve values as large as 200 $(\hbar/e)(\Omega \times cm)^{-1}$. The selenides exhibit slightly lower (~ 100) magnitudes of SHC and the sulfides do not seem to display any spin Hall effect at all.

As we have mentioned above, similarly to other semiconductors, either *p*-type or *n*-type doping is needed to reach the SHC resonances. In table 1, we list the values of the SHC peaks and the corresponding doping levels expressed as a Fermi level shift and number of electrons per surface unit, for six compounds reported in figure 2. In general, the doping concentrations are of the order of $n_{h/e} = 10^{14} e \text{ cm}^{-2}$, an order of magnitude lower than in the case of recently studied transition metal dichalcogenides [15] but still beyond the typical values achieved in experiments $(\sim 10^{12} - 10^{13} \text{ e cm}^{-2})$. However, for the compounds with highest SHC peaks, the spin Hall effect could be very large even at lower doping: for instance, in SnTe the SHC reaches 100 $(\hbar/e)(\Omega \times \text{cm})^{-1}$ for doping of $\sim 10^{13}$ e cm⁻². We also note that the estimated values of doping listed in table 1 are simply derived

from the density of states following similar analysis in previous theoretical works dealing with SHE in semiconductors [15] and the carrier concentrations in real samples might be different. Therefore, we believe that the intrinsic spin Hall effect could be achieved experimentally even in the unstrained structures.

4. Spin Hall effect in strained monochalcogenides

As a next step, we have explored the possibility of tuning the electronic properties and spin Hall conductivity via external strain. The band gap (E_g) manipulation in group-IV sulfides and selenides was previously reported in [19], where compressive strains along either x or y axis were found to strongly reduce the band gap, and for larger strains could induce a semiconductor to semimetal transition. In the present study, we consider all possible strain configurations varying between -10% to +10% with the step of 2%, thus 121 different configurations for each compound. Below, we will discuss only the results for SnTe which displays the highest potential for spintronics; the complete set of results for all considered group-IV monochalcogenides is reported in the SM (figures S3–S7).

4.1. SHE in the metallic phase

Figure 3 summarizes the electronic properties and spin Hall conductivity in SnTe for each considered strain configuration. The band gap landscape displayed in panel (a) shows several interesting features: (i) compressive (tensile) strain always leads to decrease (increase) in E_g , (ii) the lowest values of E_g are achieved when a compressive strain along only one of two axis is applied, (iii) the combinations of tensile and compressive strain can also lead to a decrease in E_{g} , larger than in case of compressive strains applied along both axes. We have observed similar behavior in all compounds; in selenides the band gaps are in general wider, thus larger strains are required to enable the semiconductor to semimetal transition. In sulfides, in contrast, a metallic phase cannot be achieved, in agreement with conclusions of [19].

The corresponding spin Hall conductivities calculated at intrinsic chemical potential plotted in panel (b) clearly reflect the profile in (a), that is, as long as the material is semiconducting, it cannot exhibit any spin Hall effect. Within the regions of $E_g = 0$, the values of σ_{xy}^z vary because each of these strain configurations induces different modifications in the electronic structure. However, we are still able to draw general conclusions regarding the impact of the strain based on the analysis of few selected configurations A, B, C displayed in figure 3(c) which embody rather huge modifications of both electronic and spin properties. First of all, it is clear that the same strain applied along axis x and y (configurations A and B) affect the dispersion of the bands in an asymmetric way. The strain



Figure 2. Relativistic electronic structures of group IV monochalcogenides GeX (a) and SnX (b), X = S, Se, Te represented as green, blue and red lines, respectively. The corresponding scalar-relativistic band structures are superimposed (black lines). ((c) and (d)) Spin Hall conductivities σ_{xy}^z calculated as a function of chemical potential for compounds in panels ((a) and (b)) employing the same color scheme.

along *x* (panel A), in general, brings upwards the occupied bands along the $S - Y - \Gamma$ paths and downwards the unoccupied spectrum along $\Gamma - X - S$ resulting in *p*-type pockets near Y and *n*-type pockets near X, while *y*-strain (panel B) is found to cause opposite shifts. The band structure of configuration C confirms that such tendency is more general; this lower strain configuration is structurally similar to B and indeed its electronic properties are very similar to the latter.

The spin Hall conductivities of structures A, B, C shown in figure 3(d) significantly differ from those of the unstrained structure in figure 2(d), which is not surprising, given the substantial modification of electronic structure at the Fermi level. In order to facilitate a systematic analysis, we have introduced the labels E_1 and E_2 corresponding to the two SHC resonances below and above E_F and we followed their behavior due to the electronic structure changes induced by the strain (the positions of E_1 and E_2 without strains are reported in table 1).

It is evident that the σ_{xy}^z can be giant without any doping (structures A, B), which we attribute to the presence of resonance E_2 much closer to the Fermi level than in the unstrained monolayer (E_F is located on the slope in both A and B configurations). Statistical analysis of these two parameters for all calculated structures confirms that indeed the change in the band gap is mainly correlated with the resonance E_2 (calculated Pearson's correlation between E_g and E_2 is around 80%), while the position of E_1 hardly depends on the band gap. This means that strain is more likely to shift/ modify unoccupied bands which will also determine the SHC. Finally, the σ_{xy}^z in the moderately strained

Table 1. Resonance values of spin Hall conductivity and the corresponding values of doping expressed as Fermi level shift ΔE and hole/electron concentrations per surface unit $n_{h/e}$. Spin Hall conductivity σ_{xy}^z is expressed in $(\hbar/e)(\Omega \times \text{cm})^{-1}$, ΔE in eV, and $n_{h/e}$ in $10^{14} e \text{ cm}^{-2}$.

	GeS	GeSe	GeTe	SnS	SnSe	SnTe
σ_{xy}^z	43	98	103	148	128	215
E_1	-1.18	-1.86	-1.00	-0.93	-1.09	-0.79
n_h	7.12	5.61	6.24	7.34	4.70	4.78
σ_{xy}^{z}	_	92	45	61	110	245
E_2	_	0.62	0.79	1.45	0.86	1.09
n _e	_	4.25	0.74	1.70	0.74	2.56

configuration C also exhibits a finite value at the Fermi level, but since the peak E_2 is not so close to E_F the spin Hall effect is weaker.

4.2. Tuning of SHC via strain and doping

The experimental realization of SHC, its tuning and switching on/off, is likely to require a combination of doping and strain. In order to quantitatively estimate the effect of both we have calculated the values of σ_{xy}^z averaged over the range of chemical potential that correspond to a given electron/hole concentration for every configuration of strain. The results for SnTe are shown in figure 4. In accordance with table 1, *n*-type doping of ~10¹⁴ e cm⁻² (a) guarantees giant values of SHC for unstrained and weakly strained structures. Surprisingly, a compressive strain (a) leads to the reduction of SHC rather than to its increase, which is related to the oscillating character of the intrinsic spin Hall conductivity as a function of chemical potential. In this case, the combination of doping and



Figure 3. Electronic properties and spin Hall conductivities of SnTe as a function of strains. (a) Band gap E_g versus strains of a (along x axis) and b (along y axis) displayed as a 3D surface in lattice constants space. The corresponding legend is shown in the upper left corner. (b) Heat-map of spin Hall conductivities calculated at zero chemical potential for each strain configuration. The legend is displayed in the bottom left corner. The reversed contrast of maps (a) and (b) clearly reflects their physical meaning and the fact that σ_{xy}^z can have a finite value only for $E_g = 0$. Since uniaxial strain is often considered in experimental realizations, we have also introduced complementary plots summarizing the influence of uniaxial strains along x and y on the band gap and the SHC (see SM, figure S2). (c) Band structures of SnTe calculated for selected points in strain space marked in ((a) and (b)), A: $a = 0.9a_0$, $b = 1.0b_{0}$, B: $a = 1.0a_0$, $b = 0.9b_0$, C: $a = 1.04a_0$, $b = 0.94b_0$, where a_0 and b_0 denote original (unstrained) lattice constants. (d) Corresponding σ_{xy}^z calculated as a function of chemical potential. Labels E_1 and E_2 at each curve denote resonances of SHC closest to the Fermi level.





compressive strain shifts the Fermi level excessively, well beyond the resonance peak of SHC. Moreover, it is clear that a biaxial strain could be used to switch on/ off the SHC. We can observe similar behavior also for *n*-type doping of $\sim 10^{13} e \text{ cm}^{-2}$ (b), in such case the values of SHC are lower, but can still be considered large even for unstrained/weakly strained structures. For $n_e \sim 10^{12} \ e \ cm^{-2}$ (c) the finite but small values of SHC can be increased by uniaxial compressive strain; this low doping configuration resembles the properties of the undoped structures (d) and weakly p-type doped configuration (e). Further increase in *p*-type doping to $n_h \sim 10^{13} \ e \ cm^{-2}$ (f) offers a possibility of even broader modulation of SHC by strain; while biaxial compressive strain can result in switching off the SHC, unaxial strain leads to its increase. Overall, however, the values of SHC are lower here than in case of electron doping. Thus, as anticipated in the previous section, the manipulation of SHE seems to be more feasible in *n*-type doped systems. Finally, among the other monochalcogenides, GeTe reveals interesting properties for spintronics, while the sulfides and selenides either do not possess large SHC at all or it does not exhibit sufficiently high tunability (see SM, figures S4–S7).

5. Summary and conclusions

In summary, we have reported for the first time the emergence of a giant spin Hall effect in group IV monochalcogenides, which can be switched on/ off and modulated either by doping or uniaxial compressive strain. The most interesting candidate for spintronics is SnTe. We have predicted that the SHE in this compound can be very strong. Moreover, the monolayer and multilayer samples have been recently synthesized and they reveal high potential for technology [23, 24, 44]. While our work is limited to monolayers structurally similar to black phosphorus, it is worthwhile to mention that the multilayer stacks can exhibit more intriguing spin-orbit related properties and with even broader possibilities of tuning. Finally, SHE has been achieved in bulk β -SnTe which suggests that its successful realization in 2D phase is very probable [45]. Despite the values of doping/strain required to reach/tune the giant SHC might seem large, the actual 2D character of these compounds can greatly help to overcome these difficulties. For example, different stacking order or thickness of the multilayer might reduce the required doping or the Fermi level could be additionally shifted by any charge originating from a substrate [46], or any additional strain could result from lattice constant matching at the interface.

Finally, we emphasize that 2D spintronics is not just a hypothesis; the recent discovery of 2D ferromagnetism [47, 48] brings it much closer to realization and new candidate materials will be needed. The giant SHC of monochalcogenides combined with low charge conductivity even in metallic phase suggest they might be useful in versatile spintronics applications, such as spin detectors [6], and even more likely in novel multifunctional devices. We believe that the properties unveiled in this paper clearly show the high potential of 2D phosphorene analogues for spintronics, and will trigger the interest in the experimental realization of spin Hall effect in these materials.

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