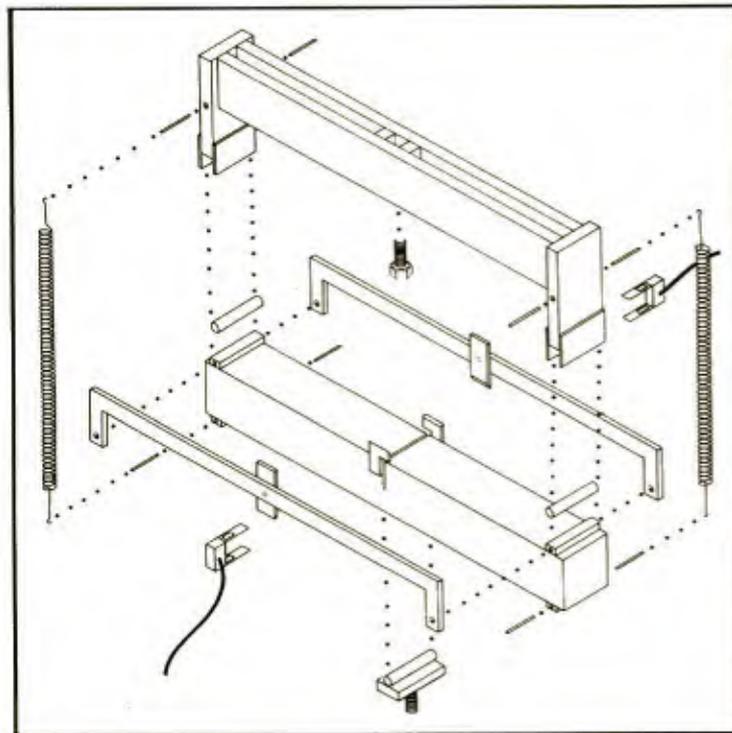


# NCEL

Technical Report

## Fracture Energy for Three-Point Bend Tests on Single-Edge Notched Beams

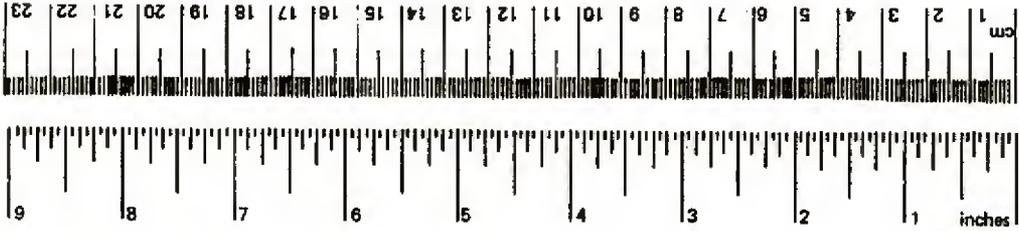


**ABSTRACT** Three test series of single-edge notched beams in three-point bending were conducted to evaluate the fracture energy of concrete. The fracture energy was determined from the area under the complete load versus load-point deflection diagram. The nonlinear Fictitious Crack Model was implemented in a finite element analysis, showing good agreement with the experimental data.

By varying the notch depth and the beam depth it was shown that the fracture energy, traditionally presented as a material property, depends upon the specimen size and configuration. This is attributed to the energy dissipation in the process zone which is not accounted for in the analytical model.

METRIC CONVERSION FACTORS

Approximate Conversions to Metric Measures				Approximate Conversions from Metric Measures			
Symbol	When You Know	Multiply by	To Find	Symbol	When You Know	Multiply by	To Find
		<b>LENGTH</b>				<b>LENGTH</b>	
in	inches	*2.5	centimeters	mm	millimeters	0.04	inches
ft	feet	30	centimeters	cm	centimeters	0.4	inches
yd	yards	0.9	meters	m	meters	3.3	feet
mi	miles	1.6	kilometers	km	kilometers	1.1	yards
		<b>AREA</b>				0.6	miles
in <sup>2</sup>	square inches	6.5	square centimeters	cm <sup>2</sup>	square centimeters	0.16	square inches
ft <sup>2</sup>	square feet	0.09	square meters	m <sup>2</sup>	square meters	1.2	square yards
yd <sup>2</sup>	square yards	0.8	square meters	km <sup>2</sup>	square kilometers	0.4	square miles
mi <sup>2</sup>	square miles	2.6	square kilometers	ha	hectares (10,000 m <sup>2</sup> )	2.5	acres
		<b>MASS (weight)</b>					
oz	ounces	28	grams	g	grams	0.035	ounces
lb	pounds	0.45	kilograms	kg	kilograms	2.2	pounds
	short tons	0.9	tonnes	t	tonnes (1,000 kg)	1.1	short tons
	(2,000 lb)						
		<b>VOLUME</b>					
tsp	teaspoons	5	milliliters	ml	milliliters	0.03	fluid ounces
Tbsp	tablespoons	15	milliliters	l	liters	2.1	pints
fl oz	fluid ounces	30	milliliters	l	liters	1.06	quarts
c	cups	0.24	liters	l	liters	0.26	gallons
pt	pints	0.47	liters	m <sup>3</sup>	cubic meters	36	cubic feet
qt	quarts	0.96	liters	m <sup>3</sup>	cubic meters	1.3	cubic yards
gal	gallons	3.8	liters	°C	Celsius	9/5 (then	Fahrenheit
ft <sup>3</sup>	cubic feet	0.03	cubic meters	°C	temperature	add 32)	temperature
yd <sup>3</sup>	cubic yards	0.76	cubic meters				
		<b>TEMPERATURE (exact)</b>					
°F	Fahrenheit	5/9 (after	Celsius	°C	Celsius		°F
	temperature	subtracting	temperature				
		32)					



\*1 in = 2.54 (exactly). For other exact conversions and more detailed tables, see NBS Misc. Publ. 286, Units of Weights and Measures, Price \$2.25, SD Catalog No. C13.10-286.

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## INTRODUCTION

Classical linear elastic fracture mechanics (LEFM), which has been successfully applied to metallic and brittle materials, is limited when applied to concrete. LEFM cannot model the behavior of small specimens of the size typically used in laboratories. As a consequence, several nonlinear models have been developed which approximate LEFM for large sizes. The two best known models are the fictitious crack model (FCM) introduced by Hillerborg et al. (Ref 1), and the smeared or crack band model (CBM) introduced by Rashid and developed by Bazant et al. (Ref 2, 3, 4, 5). Among others, the two-parameter model by Jenq and Shah (Ref 6) is more recent and is supported by only limited data.

In finite element applications, CBM approach shows a dependency on the element size used in the mesh. Results do not converge in successive analyses where the element size is continuously reduced. This problem can be circumvented by linking the softening stiffness of the cracked elements to the fracture energy  $G_f$ . However,  $G_f$  determined from the load-deflection diagram is suspected to depend on specimen geometry and size (Ref 5). The FCM is also based on  $G_f$ , which is assumed to be a material property.

The existing approaches for determination of the fracture energy are evaluated in this report and a new test method proposed. Three series of tests and a finite element analysis using FCM were conducted. The objectives were:

- Calculate the fracture energy following RILEM Technical Committee 50-FMC guidelines (Ref 7) and compare it to the fracture energy,  $G_f^*$ , according to a method presented in this report.

- Conduct a finite element analysis with different strain softening relations based on the experimental value of  $G_f$ .
- Determine the effect of notch-to-depth ratio and specimen size on  $G_f$ .

## EVALUATION OF THE FRACTURE ENERGY $G_f$

For a beam in three-point bending (Figure 1a), the load typically varies with load-point deflection (LLPD) as shown in Figure 1b.

The LLPD plot comprises three stages of behavior. The deflection increases linearly with the load in the first stage and the crack is opened but does not extend. A fracture process zone develops during the second stage where microcracks form and slow crack growth is apparent. In the third stage, known as the strain softening zone, rapid crack growth is evident. During strain softening most of the damage to the specimen is concentrated in a narrow zone. This concentration is higher as the load carrying capacity decreases and energy dissipation eventually occurs through a single major crack. Strain softening has been considered a material characteristic.

The area,  $U_0$ , under the LLPD curve (Figure 2a) represents the energy required to break the specimen. For a single-edge notched beam in three-point bending, RILEM TC 50-FMC defined the fracture energy,  $G_f$ , as:

$$G_f = (U_0 + mgd_0)/A$$

where  $A = \text{ligament area} = B(W - a_0)$

$B = \text{width}$

$W = \text{specimen depth}$

$a_0 = \text{notch depth}$

$mg = \text{weight of the specimen}$

$d_0 = \text{load-point deflection at fracture}$

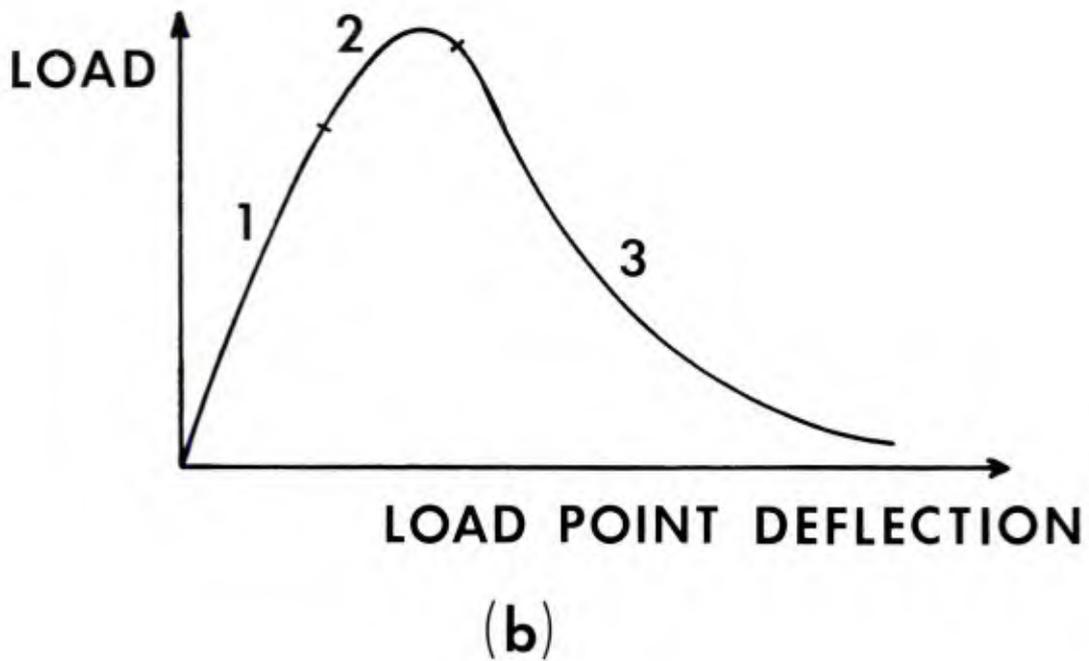
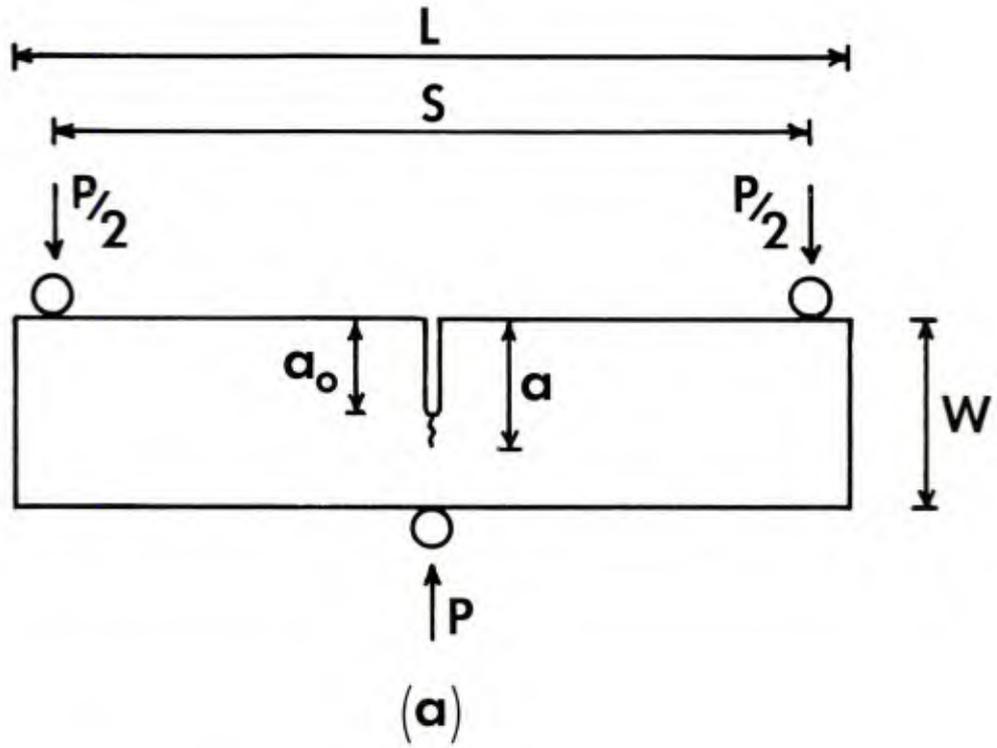


Figure 1. Specimen schematic and load versus load-point deflection plot.

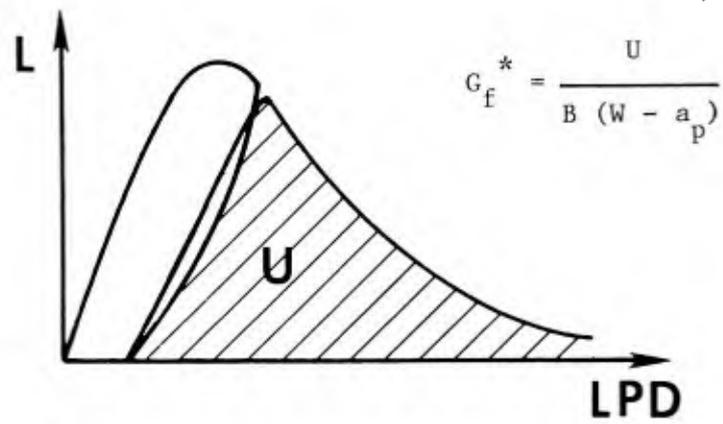
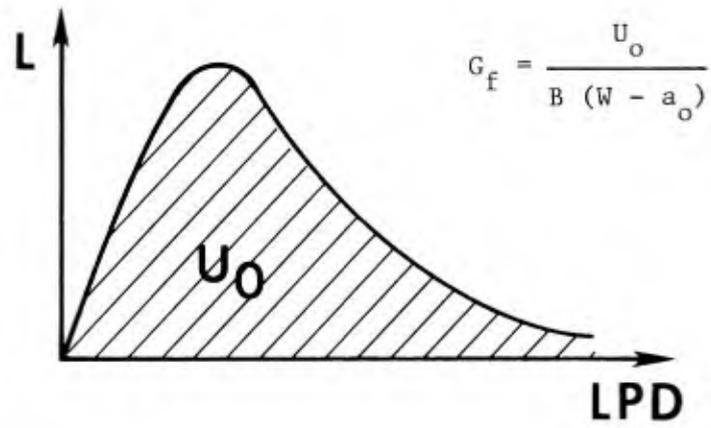


Figure 2. Evaluation of the fracture energy.

This definition relies on the assumption that all the energy required to break the specimen is transformed into surface energy by extension of a single macrocrack. However, energy dissipation outside of the fracture zone is included in the determination of  $G_f$  and should not be overlooked. This energy depends on the specimen size and notch depth. It is dissipated in creating and extending a process zone by debonding aggregates and opening microcracks. Most of this energy consumption is believed to occur during slow crack growth. Consequently, using the whole area under the curve leads to an overestimate of  $G_f$ .

## TEST METHOD

From the preceding observations it was concluded that an improved measure of the toughness of concrete would be obtained with a three-point bend beam specimen and the following procedure:

1. Set up the beam with the notch on the top surface. This will help in applying dye into the cracked surface for determining crack growth.
2. Load the specimen up to the point of instability defined as the point past peak load where the load drops off to 95 percent of its maximum value, then remove the load completely. The area enclosed in this load-unload loop includes the energy spent on formation of a process zone, slow crack growth, and the inelastic energy spent outside of the crack zone.
3. Insert dye through the notch and allow it to flow into the crack to highlight the crack length,  $a_p$ , at the point of instability.
4. Reapply the load and obtain the strain softening zone. A one-time unloading and reloading will not significantly affect the LLPD curve.

5. Define  $U$  as the total area under the LLPD curve minus the area in the load-unload loop indicated in the second step (see Figure 2b).

6. Define  $G_f^*$  as the energy spent on developing one major crack divided by the ligament area existing at that moment:

$$G_f^* = U/B(W-a_p)$$

## DETAILS OF EXPERIMENTAL METHODOLOGY

### Fracture Area

During the strain softening process a crack will actually follow a surface which is not flat but governed by the aggregate size and relative hardness compared to the mortar matrix. An invariant  $G_f$  will be obtained using the ligament area,  $B(W-a_0)$ , if the total energy spent in the formation of a unit projected area is constant (as assumed in the RILEM approach), or if the energy spent other than in formation of the macrocrack is discarded (as attempted here).

### Precracking

Precracking of the specimen (or fatigue cracking) is not necessary in the proposed method. Measurement of the energy takes place only after a sharp crack has been formed, and does not depend on the initial condition, whether it is precracked, form notched, or saw notched.

### Rate of Loading

RILEM recommends reaching peak load after 30 to 60 seconds which corresponds to a rate on the order of  $5 \times 10^{-6}$  m/sec ( $2 \times 10^{-4}$  in./sec). The work of fracture and the strain energy release rate increase slightly (about 15 percent) for cross-head deflection rates from  $5 \times 10^{-7}$  to  $5 \times 10^{-5}$  m/sec ( $2 \times 10^{-5}$  to  $2 \times 10^{-3}$  in./sec) (Ref 8).

## Beam Weight

By supporting half of the beam weight at the ends, a complete LLPD curve is obtained. The LLPD curve actually begins after the applied load equals half of the specimen weight. In the LLPD plot the effect of beam weight is easily identified and discarded from the total area under the curve (Figure 6). This discarded area ( $1/2$  weight  $\times$  midspan deflection at total fracture) corresponds to work being transformed into potential energy as the center of gravity of the beam is forced up.

## Displacement and Support Indentation

According to RILEM, the midspan deflection can be measured with reference to the loading apparatus as long as the inelastic indentations at the load points do not exceed 0.01 mm (0.0004 in.) (Ref 7). For nonstandard specimens with small span/depth ratios (e.g.,  $S/W = 4$ ) the inelastic indentations at the loading points are not negligible. They have to be considered or else the deflection due to load indentations has to be measured.

The error caused by inelastic indentation is estimated for a  $27.65 \text{ MN/m}^2$  (4,000 psi) concrete specimen with dimensions 102 by 7 by 76 by 406 mm (4 by 3 by 16 in.) (depth by width by span), with an initial notch depth  $a_0 = 25 \text{ mm}$  (1 in.) and bearing directly on 51-mm (2-in.) diameter rollers. A maximum load of approximately 3.12 kN (700 lb) should be expected. The minimum bearing area at the center roller is  $3.12/0.02765 = 113 \text{ mm}^2$  (0.175 in.<sup>2</sup>) and the minimum bearing width is  $113/76 = 1.5 \text{ mm}$  (0.058 in.). This implies an indentation of the flat surface at the center roller only of  $0.75 \times 0.75/25.5 = 0.022 \text{ mm}$  (about 0.001 in.). In this case the indentation represents about 25 percent of the midspan deflection at peak load.

The clip gage described by ASTM E399 seemed most appropriate for accurate displacement measurements. Clip gages were manufactured out of high strength aluminum (7075-T6) which was more readily available and easier to machine than a titanium alloy as recommended by ASTM. High strength aluminum presents a ratio of yield strength to modulus of

elasticity as high as 0.0069. High strength aluminum ensures a large range of measurement without permanent deformation of the gage. Two clip gages were employed, one on each side of the specimen, to mitigate errors due to asymmetry.

### **Point of Instability**

The point of instability was chosen as the point after maximum load where the load decreases to 95 percent of its peak value as recommended by Swartz and Yap (Ref 9). A small variation of load near peak value is accompanied by a small displacement on the LLPD curve; however, this small amount of external work causes a significant crack advance. This is apparent on typical load versus crack mouth opening displacement (LCMOD) plots (Ref 9) where the CMOD increases significantly for almost constant maximum load. This instability is attributed to a redistribution of the elastic energy to surface energy inside the specimen. Thus, it is necessary to measure crack length past peak load to yield reliable and stable values.

### **TEST SETUP**

The test setup is shown in Figures 3 and 4. Figure 5 is a photograph of an example specimen. Figure 3 shows the beams were tested with the notch on the top surface. The beam weight was supported by four springs aligned with reaction rollers. The rollers were located on bearing pads to minimize energy dissipation at the bearing points.

The load was applied through a closed-loop, servo-controlled, 20 kip, MTS testing machine. The tests were displacement controlled with a cross-head displacement rate of approximately  $5 \cdot 10^{-6}$  m/sec ( $2 \cdot 10^{-4}$  in./sec).

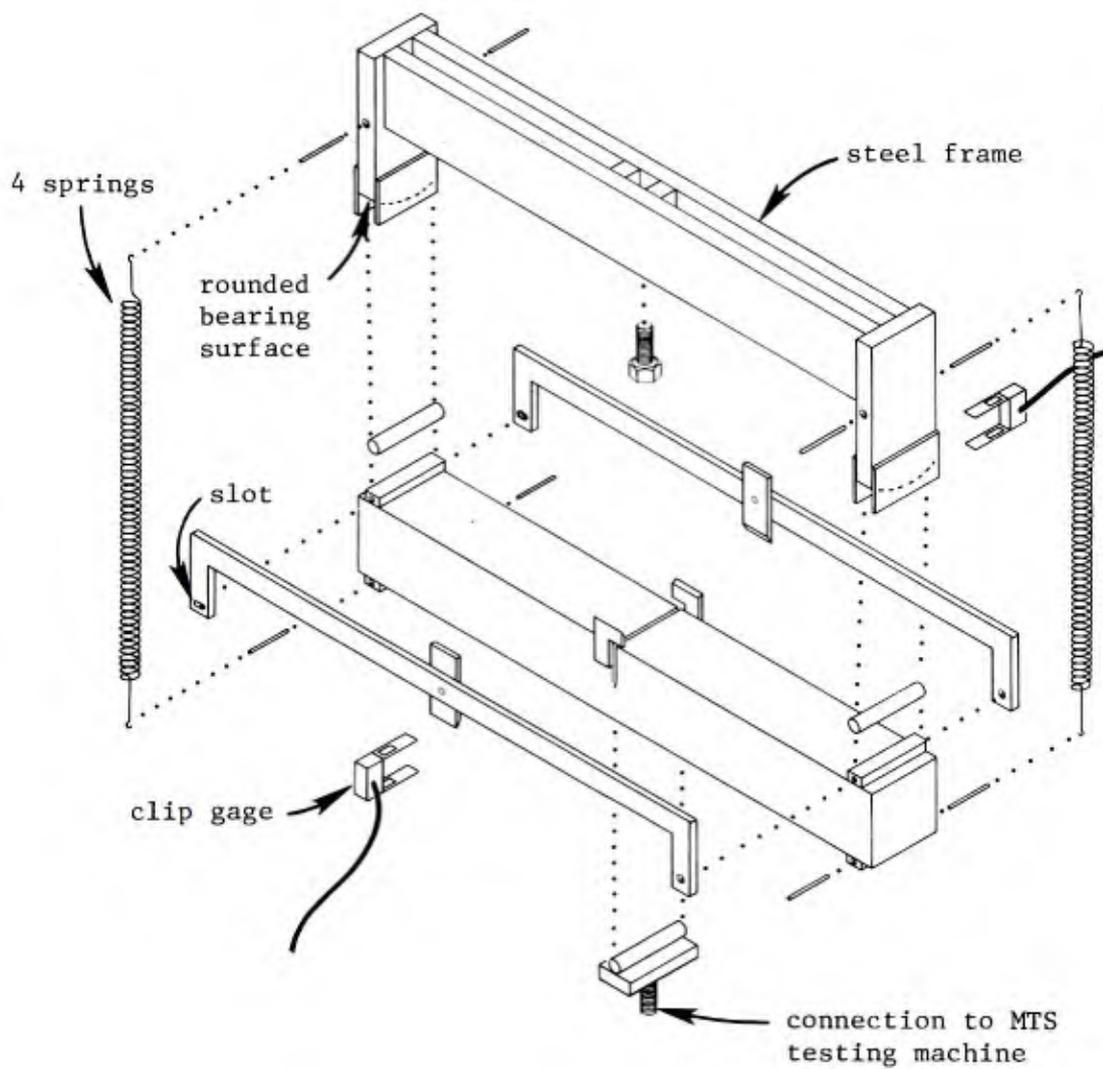


Figure 3. Set up schematic.

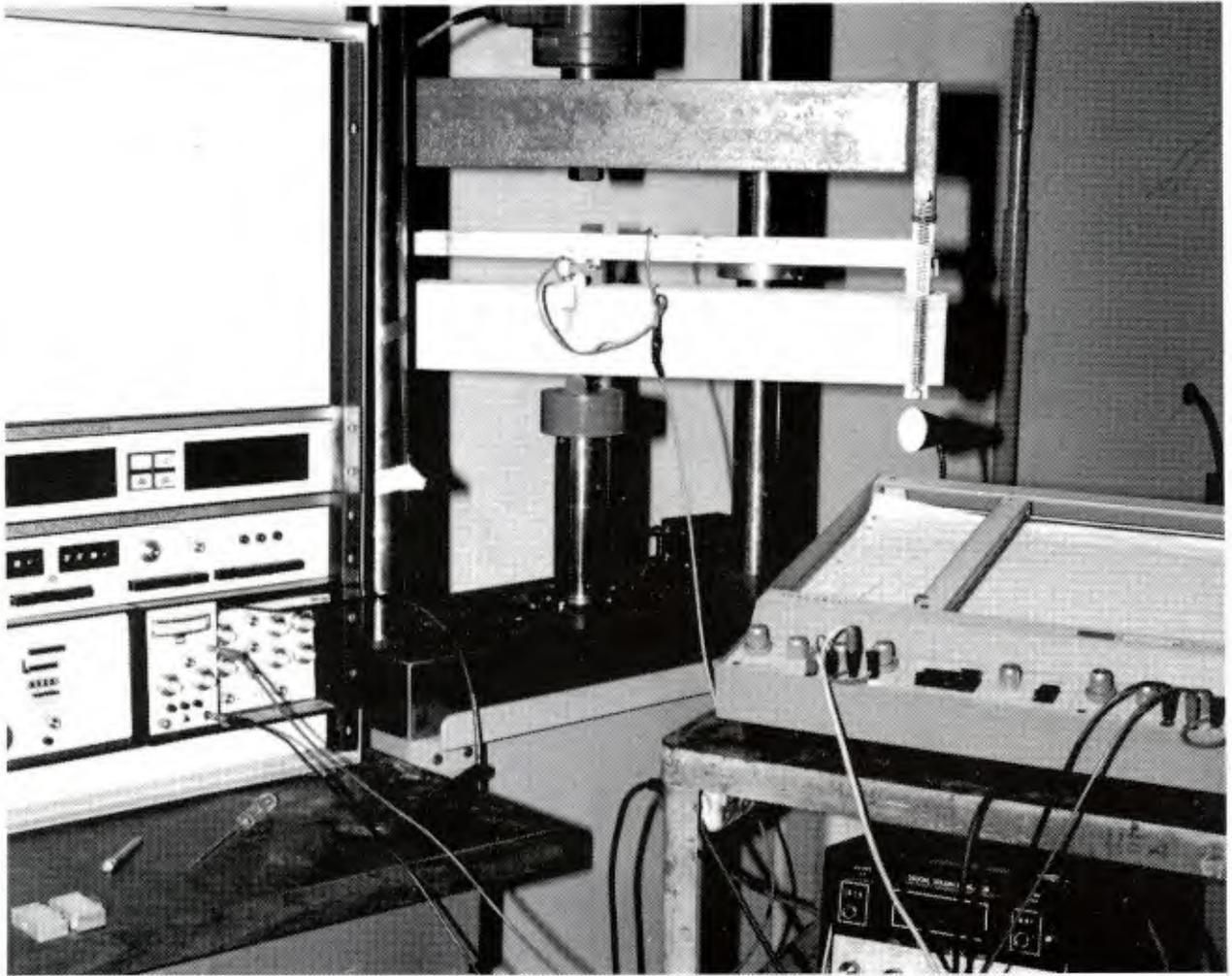


Figure 4. Test setup.

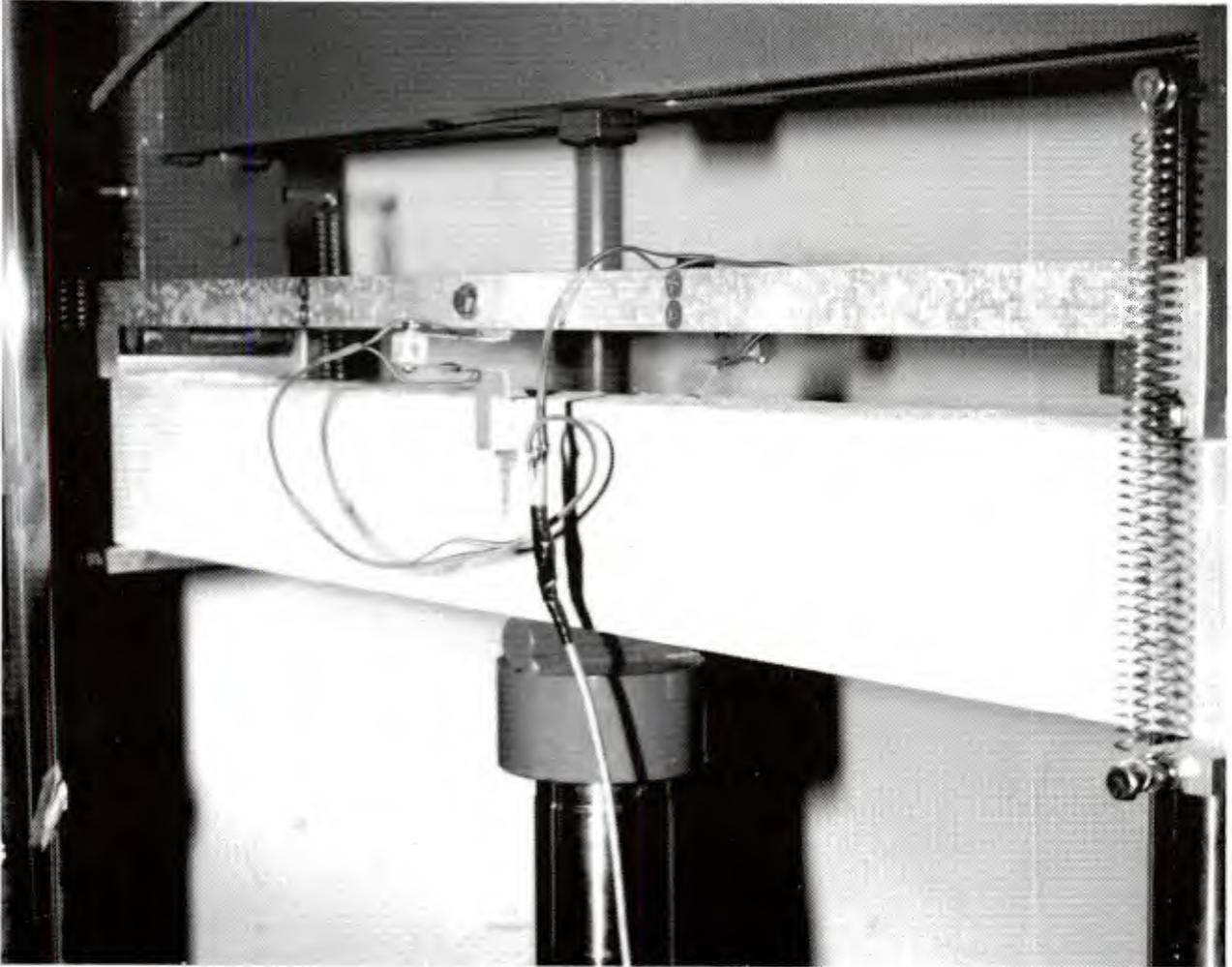


Figure 5. Clip gages and loading frame.

Two clip gages with a sensitivity of 0.0025 mm (0.0001 in.) were installed across from the load point. The clip gages bore against two aluminum beams which span across the reaction points (Figure 5). Tight fitting slots and holes machined in the frame allowed for rotation and horizontal displacement without vertical movement and negligible friction.

In order for the forces on the beam to be statically determinate, the two reaction rollers bore on a cylindrical surface whose axis was perpendicular to the rollers' axis. Thus, obtaining a single point of contact equivalent to spherical bearing.

An important advantage of the setup lies in obtaining the long tail of the LLPD plot (Figure 6), representing not only the beam weight but also other similar effects (such as clip gages weight and reaction) as well as possible constant friction. If some variable effects are present during the test, these can be evaluated by observing the linearity of the plot after the load carrying capacity of the beam has been spent.

## TEST SERIES

Three series of tests were conducted. RILEM guidelines were followed in all tests for maximum aggregate size, conditions of storage, support and loading arrangement, accuracy of measurement, and rate of loading.

The concrete mixes with their mechanical properties are given in Table 1. The maximum aggregate size was 10 mm (3/8 in.) in all cases. The initial modulus of elasticity in compression,  $E$ , is also tabulated.

### Series I

Twelve baseline beams (similar to RILEM's smallest specimen) were cast with dimensions of 102 by 102 by 788 by 838 mm (4 by 4 by 31 by 33 in.) (width by depth by span by length) (Figures 1 and 3). The notch-to-depth ratio,  $a_0/W$ , was 0.5. During the tests, the beams were

**Table 1. Material Properties**

Series	Cement (kg/m <sup>3</sup> )	Water (kg/m <sup>3</sup> )	M/C (%)	10 mm Gravel (kg/m <sup>3</sup> )	Sand (kg/m <sup>3</sup> )	$f_c'$ (MPa)	$f_t$ (MPa)	E (GPa)
I	279	167	0.60	1062	907	29.0	3.1	21.7
II	613	245	0.40	1034	443	58.9	4.2	24.5
III	400	220	0.55	1044	540	33.1	3.5	19.7

**Notes:**

The compressive strength,  $f_c'$ , was obtained at 28, 35, and 30 days, respectively for each series. In every case, three 152- by 305-mm (6- by 12-in.) cylinders were tested.

The tensile strength,  $f_t$ , was obtained at 28, 32, and 29 days, respectively, using the same type of cylinders. Six splitting tensile tests were performed for Series I, then only three each for the other series due to the uniformity of the values.

The modulus of elasticity was calculated by measuring the cylinders strain at the beginning of the compression tests.

unloaded past peak load and both  $G_f$  and  $G_f^*$  obtained. The beams were tested in four groups of three after curing for 27, 28, 29, and 32 days in a fog room.

**Series II**

Twelve additional specimens with the same overall dimensions as Series I were prepared. They were divided into three groups of four beams with the same  $a_o/W$ . The initial notch-to-depth ratio was 0.3, 0.5, and 0.7 for groups 1, 2 and 3, respectively. In order to isolate the effect of notch depth from the effect of curing time one specimen of the four from each group was tested on the same day after curing for 28, 29, 32, and 33 days.

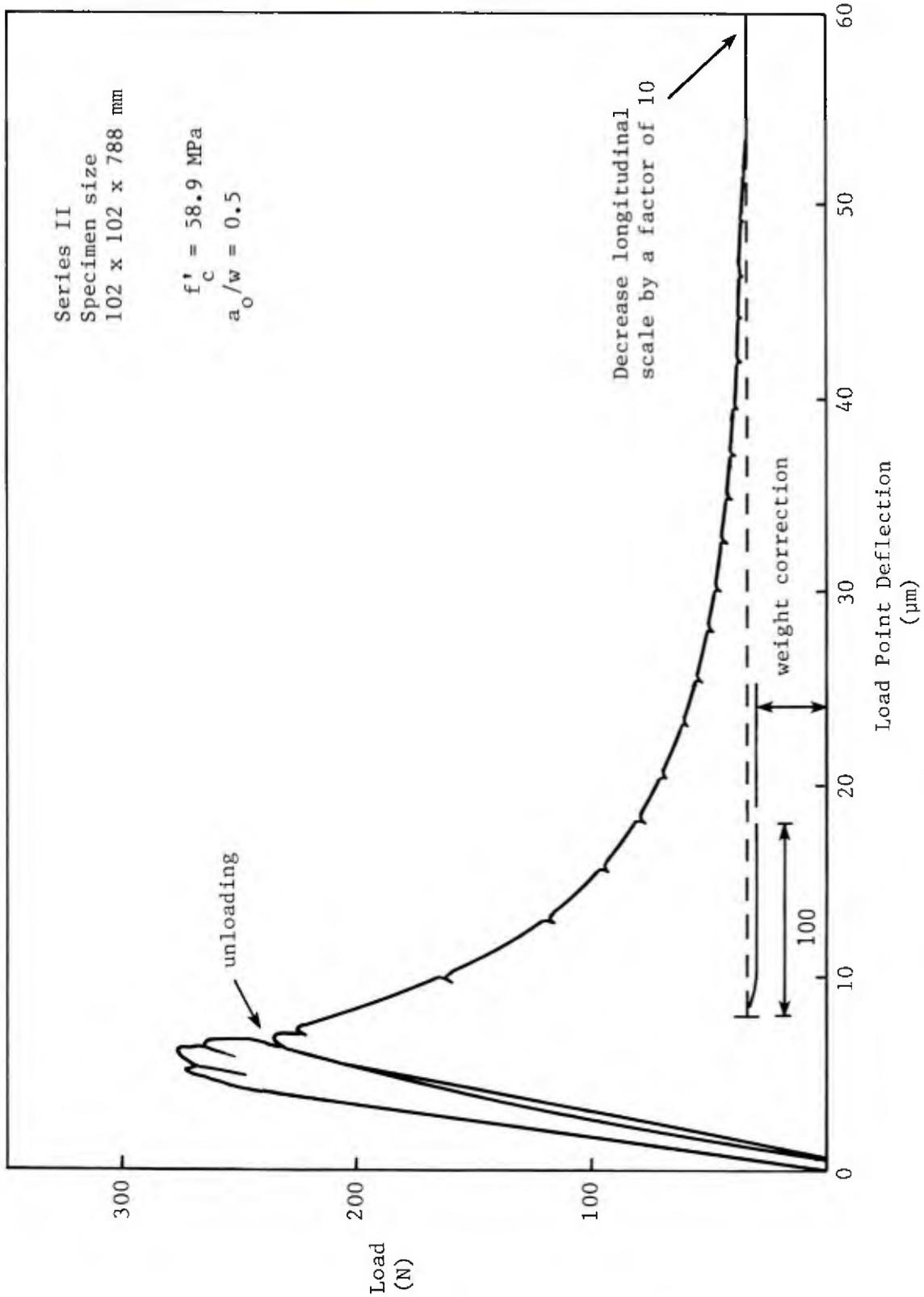


Figure 6. Load versus load-point deflection.

### Series III

The third series consisted of four additional baseline specimens (same dimensions as series I with  $a_o/W = 0.5$ ) plus four specimens with depths of 216 mm (8.5 in.) but with the same width, span, length, and  $a_o/W$ . While not geometrically similar to the standard RILEM specimen, the increase in ligament area (unbroken area at the notch) demonstrated the size effect on  $G_f$ .

One baseline specimen and one deeper beam were tested each day after curing for 28, 29, 30, and 32 days.

### ANALYTICAL REPRESENTATION WITH FINITE ELEMENTS

The finite element program, ADINA (Ref 10) features user-supplied loading which can be expressed as an arbitrary function of nodal displacements. This allowed the implementation of an FCM approach. The element mesh was derived from Reference 11 and is shown in Figure 7. Due to symmetry, only half of a beam needed to be discretized. The notch-to-depth ratio,  $a_o/W$ , was chosen as 0.5. The beam was loaded in displacement control (both in the program and in the actual tests) and whenever the tensile strength,  $f_t$ , was reached at a node, the node was released and the midspan displacement was step increased until another  $f_t$  was exceeded at another node. This iterative process was continued until the crack progressed across the beam cross section.

The modulus of elasticity,  $E$ , used in the finite element analyses was measured as the initiation slope of the stress strain diagram of a compression test on a 152 - by 305-mm ( 6- by 12-in.) cylinder. Others, including Peterson (Ref 12), have used the dynamic modulus of elasticity,  $E_d$ , for analysis. The difference between dynamic and static is small ( $E_d$  is about 10 to 20 percent higher than  $E$ ) and the loading rates between the cylinder tests and the three-point bend (3PB) tests is within one order of magnitude. Small differences have also been reported between tests carried out in tension compared to compression (around 10 percent lower according to Reference 13). Hence,  $E$  was chosen as the modulus of elasticity of the equivalent homogeneous elastic material.

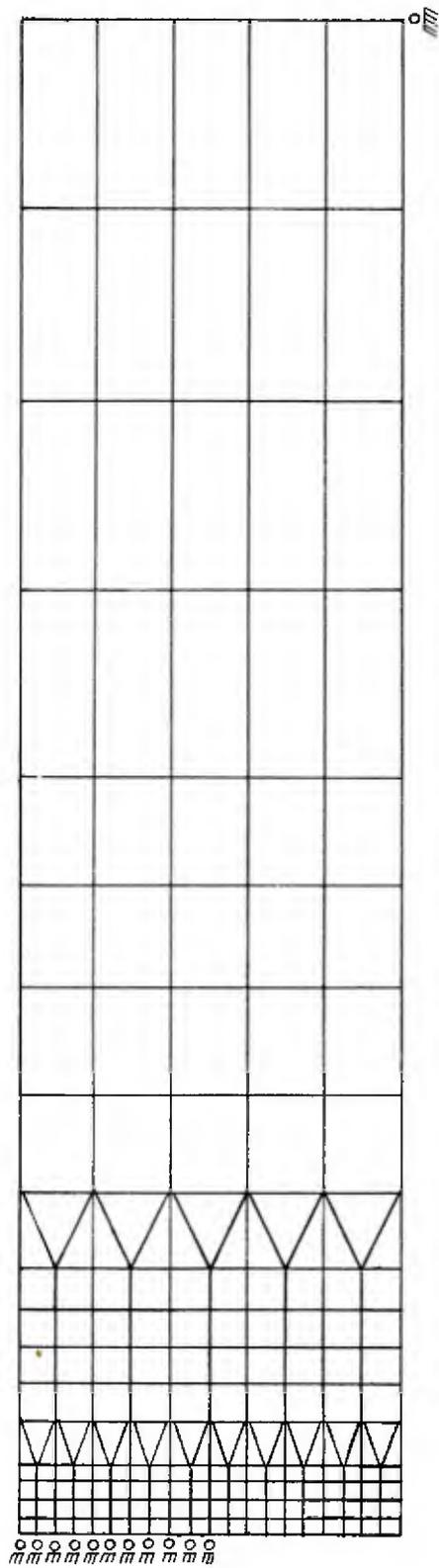


Figure 7. Finite element model.

Four stress versus crack width ( $\sigma$  versus  $w$ ) relations were analyzed and are described in Figure 8. The straight line (SL) and bilinear or concrete (C) relations were proposed by Peterson (Ref 9), the exponential (E) relation is proposed by the authors (from curve fitting relationships derived in Ref 11 and 14), and the power function (P) by Reinhardt (Ref 15). In all cases, the relations conform to:

$$G_f = \int_0^{\infty} \sigma dw$$

as recommended by Hillerborg et al. (Ref 1).

## RESULTS

### Test Series I

Values of  $G_f^*$ , peak load, deflection at peak load ( $d_p$ ), and deflection when the load carrying capacity of the beam vanishes ( $d_o$ ), are reported in Table 2. The increase in crack length,  $\Delta a$  (measured by dye insertion) is also indicated. In some cases the closed loop servo control on the testing machine did not allow the unloading to take place immediately after the maximum load (when it decreases to about 95 percent of its peak value), so experimental values were not reported.

The LLPD plots were drawn until a long horizontal trace was obtained (Figure 6), indicating that the beam was not carrying any load. The noise and random friction then measured showed an effect of about  $\pm 4$  N ( $\pm 1$  lb).

Dye insertion highlighted a crack front which appeared fairly straight. Typically the dye was inserted from the top, but in a couple of cases excess dye was allowed to run along the sides of the beam. In those cases the crack front appeared curved due to dye absorption on the sides.

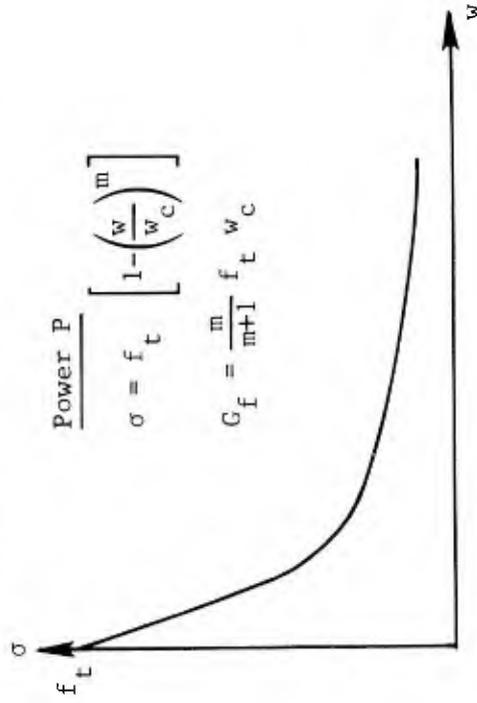
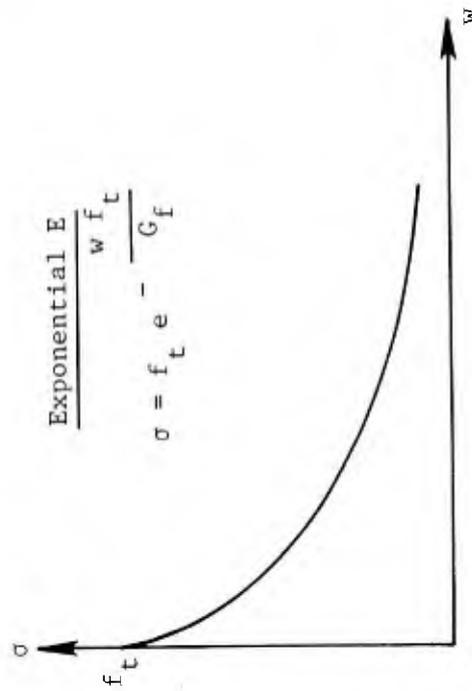
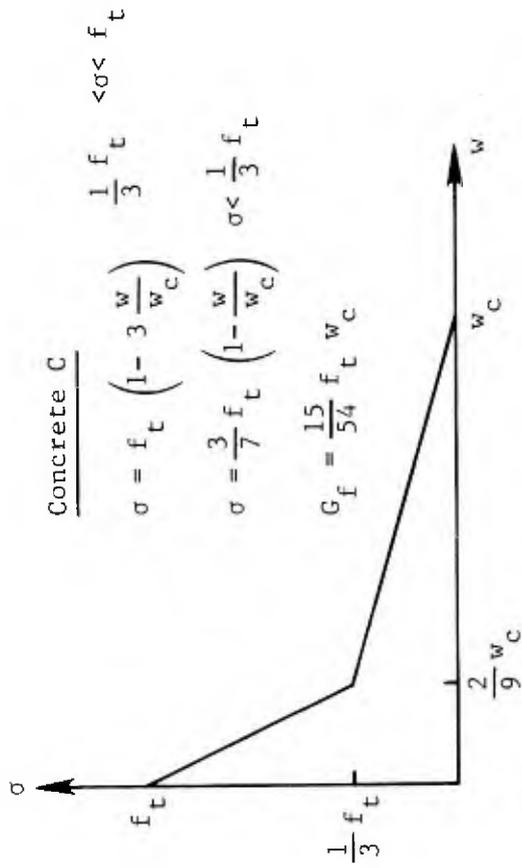
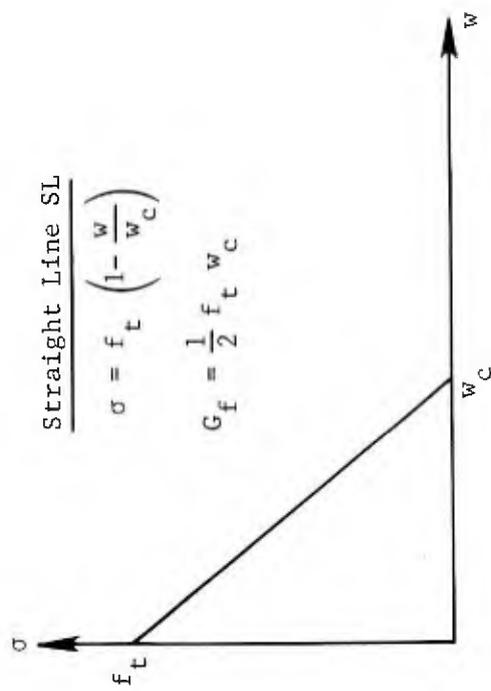


Figure 8. Stress versus crack width relations.

Table 2. Results - Series I

Specimen	$G_f$ (M/m)	$G_f^{\#}$ (M/m)	Peak load (N)	Unloading at (% of peak load)	$d_p$ (mm)	$d_o$ (mm)	$\Delta a$ (mm)
1	72.3	68.9	853	86	0.17	2.8	6.5
2	79.7	79.5	999	88	0.18	2.4	9.3
3	85.6	80.5	945	96	0.19	2.8	5.3
4	70.5	69.0	820	95	0.17	2.2	4.7
5	75.7	-	910	-	0.15	3.1	-
6	72.4	-	921	-	0.15	2.2	-
7	83.4	72.8	1011	91	0.16	2.5	3.0
8	75.3	69.6	950	88	0.17	2.9	5.9
9	68.1	63.6	883	87	0.13	2.4	5.7
10	68.6	-	950	-	0.16	2.6	-
11	84.1	-	950	-	0.16	2.7	-
12	79.8	76.4	997	94	0.15	2.0	3.6
Mean	76.3	72.5	932	90	0.16	2.6	5.5
Std Deviation	6.1	4.8					

## Test Series II

Series II results are detailed in Table 3. A strong dependency of  $G_f$  on  $a_o/W$  is apparent with variations of about 25 percent (from its value at  $a_o/W = 0.5$ ).  $G_f$  decreases as  $a_o/W$  increases. It should also be noted that  $G_f^*$  follows  $G_f$  closely.

## Test Series III

Series III results are reported in Table 4. An increase in  $G_f$  of about 24 percent is observed when the depth is increased from 102 to 216 mm (4 to 8.5 in.).

## Finite Element Analysis

Figure 9 shows the average LLPD plot from the 12 tests of Series I (solid trace) and the approximations from finite element analyses carried out using the four different  $\sigma$  versus  $w$  relations.

## DISCUSSION

### Effects on $G_f$

The variation of  $G_f$  with notch depth and beam depth indicates that the fracture energy is not a material property and is dependent on the specimen configuration. When modelling concrete as an equivalent homogeneous linear elastic material, all the energy supplied is assumed to be converted into surface energy by propagation of a single macrocrack. The microcracking in the process zone also dissipates energy that the model cannot take into account. The process zone depends upon the stress field which is dependent on the geometry (Ref 16). The process zone depends upon the aggregate-to-specimen size ratio which is a size parameter (Ref 4). This dependency raises a question about the reliability of using a specimen in three-point bending instead of in direct tension to determine the stress versus crack width relation.

Table 3. Results - Series II

Group	a/W	Specimen	$G_f$ (N/m)	$G_f^{\#}$ (N/m)	Peak load (N)	Unloading at (% of peak load)	$d_p$ (mm)	$d_o$ (mm)	$\Delta a$ (mm)
1	0.3	1	80.8	71.9	1683	88	0.13	3.3	4.2
		4	85.3	74.3	2133	93	0.16	2.1	7.6
		7	69.0	-	1951	-	0.15	2.3	-
		10	74.2	-	2200	-	0.15	1.9	-
		Mean	77.3	73.1	1992	90	0.15	2.4	5.9
2	0.5	2	58.9	-	1024	-	0.14	2.5	-
		5	76.9	68.9	1078	88	0.14	2.5	5.8
		8	60.8	54.8	1127	87	0.13	2.1	6.1
		11	62.7	54.6	1140	97	0.15	2.0	0.7
		Mean	64.8	59.4	1092	91	0.14	2.3	4.2
3	0.7	3	44.9	44.4	410	96	0.16	1.8	5.5
		6	43.8	-	432	-	0.16	1.5	-
		9	62.5	-	468	-	0.15	2.7	-
		12	43.6	40.8	330	93	0.15	1.9	3.6
		Mean	48.7	42.6	410	94	0.15	2.0	4.5

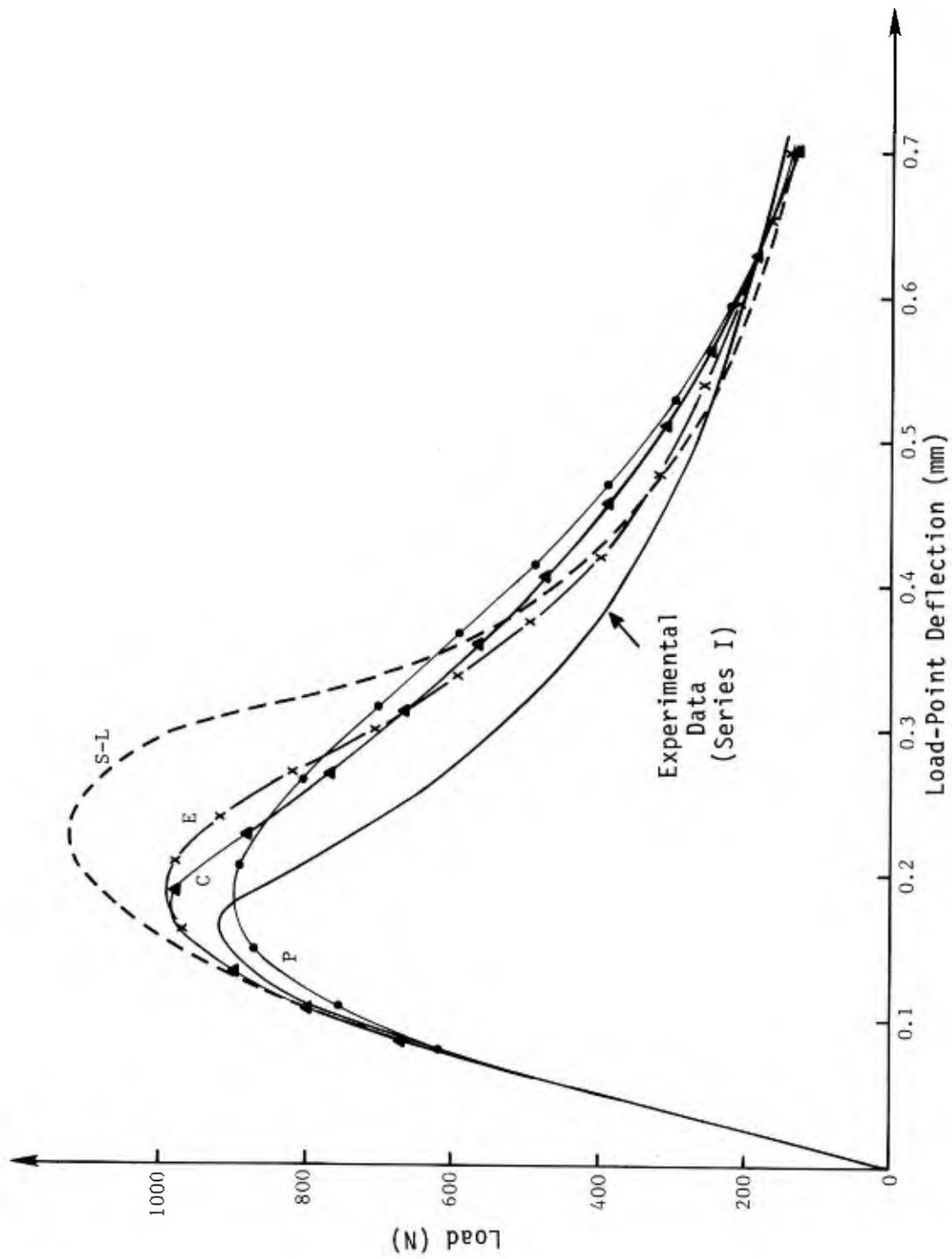


Figure 9. Analytical representations.

Table 4. Results - Series III

N (mm)	Specimen	$G_f$ (N/m)	$G_f^{\#}$ (N/m)	Peak load (N)	Unloading at (% of peak load)	$d_p$ (mm)	$d_o$ (mm)	$\Delta a$ (mm)
102	1	76.6	76.8	909	90	0.14	2.9	7.9
	3	81.9	-	958	-	0.16	2.9	-
	5	71.6	70.6	908	89	0.15	2.9	7.9
	7	59.2	58.2	793	92	0.12	3.0	3.2
	Mean	72.3	68.5	892	90	0.14	2.9	6.3
216	2	84.7	-	3795	-	0.09	1.9	-
	5	89.5	-	3900	-	0.10	2.2	-
	8	90.7	-	3875	-	0.11	1.9	-
	11	92.2	85.7	3580	89	0.10	2.0	7.2
	Mean	89.3	85.7	3788	89	0.10	2.0	7.2

Sensitivity analyses (Ref 17) and further analyses by the authors have shown that the model is typically not as sensitive to variations in  $G_f$  as it is to variations of the other parameters. Most of the energy does appear to dissipate through crack surface formation ensuring the validity of the model.

#### $G_f$ versus $G_f^*$

$G_f^*$  was defined in an attempt to quantify and eliminate the energy dissipated outside of the crack zone. The strong variation of  $G_f$  with  $a_o/W$  seems to indicate a dependency on the stress field, i.e., an energy dissipation through microcracking in the process zone which is greater than indicated by  $G_f^*$ . For standard specimen sizes, the difference between  $G_f^*$  and  $G_f$  is about 5 percent while the fracture energy shows variations in the order of 25 percent. Furthermore, both values vary in the same manner and show size and geometry dependency. The proposed

approach does not seem to discard all the energy spent in the process zone. Further research is needed to refine the model. Given the additional steps involved in its evaluation,  $G_f^*$  does not appear to present any practical advantage over  $G_f$ .

### **Crack Front**

The crack front appearance seems to be linked to the dye impregnation procedure. When the dye was inserted only from the top, the crack front appeared straight. In a few cases the dye was inserted from the sides and the top, and then the front appeared curved (Ref 16). The latter crack front appearance seemed to indicate an anisotropy of the process zone where the microcracks would tend to merge laterally before joining the macrocrack. In the determination of  $G_f^*$  a straight front was assumed.

### **Analytical Model**

The good agreement between the ascending part of the LLPD curve of the average experimental plot and the model results supports the acceptability of using  $E$  from standard cylinder tests. This is an advantage since  $E$  is more readily available than  $E_d$ .

Among the different  $\sigma$  versus  $w$  relations, the SL is the coarsest, followed by the E and the P models. The bilinear relation, C, gives only a slight overestimation of the peak load and reasonably approaches the descending branch. Keeping  $f_t$  and  $G_f$  constant, the bilinear relationship could be improved to yield a better match, as done by Roelfstra and Wittmann (Ref 18) and Carpinteri et al. (Ref 19).

### **CONCLUSIONS AND RECOMMENDATIONS**

The fracture for notched beams in three-point bending was experimentally determined. Three series of tests were conducted on a total of 32 beams and a finite element analysis carried out using a nonlinear model. The following conclusions were derived:

- The experimental setup led to more reliable and consistent values of concrete fracture energy and measured crack length.
- $G_f^*$  (calculated by current crack size and ligament area) did not present any substantial advantage over  $G_f$  (determined by RILEM guidelines).
- Finite element analysis yielded accurate representations of the fracture behavior when coupled with a bilinear stress versus crack width relation.
- $G_f$  is dependent upon size and geometry. The fracture energy increases with increasing size.

The inconsistency that arises from applying the FCM approach seems to be linked to its inability to represent the nonlinearity of the material and the energy dissipation outside the fracture zone. The model assumes all the energy to transform into surface energy through formation of a single major crack and only introduces nonlinearity in the stress-crack width relation.

The fracture model for plain concrete should be extended to three-dimensional applications and to bar-reinforced concrete. To add reinforcement, the mechanism for transferring shear from concrete to steel will need to be modeled, but the technological risk is low.

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