



AFRL-RI-RS-TR-2016-172

## **NON-PARAMETRIC MODEL DRIFT DETECTION**

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USC INFORMATION SCIENCES INSTITUTE

*JULY 2016*

FINAL TECHNICAL REPORT

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## Summary

In this project, we developed and validated a novel methods for detecting and correcting model drift in unsupervised settings. The proposed approach has two components: drift detection, and drift correction. For the first sub-problem, we have utilized our recently developed method, Correlation Explanation, or CorEx, for detecting distributional changes in high dimensional data. For the second sub-problem, we have developed a decision-theoretic approach that provides a computational framework for trading off cost versus expected performance gain. We have validated the above framework on two tasks in NLP domain, topic modeling, and machine translation. Our main findings are summarized as follows:

- We can measure important distributional changes with CorEx using the notion of *surprise*. We also find that a decrease in classification accuracy is accompanied by increase in surprise, although the opposite is not always true: there are some distributional changes that result in increasing surprise, but not necessarily affecting the algorithmic performance.
- While an alternative measure of model drift (empirical KL distance) can sometime produce similar results, its behavior is less reproducible across the datasets. Also, there are scenarios where this measure will fail detect important distributional changes.
- The proposed drift-correction framework performed as expected, with some small variations across the datasets. We found that the optimal frequency of retraining depends on the cost of retraining, e.g., the higher the cost, the less frequent retraining. The main advantage of the proposed approach is its ability to adapt to different cost/benefit ratio for a given scenario.

Below we report on our main findings in more details.

## Introduction

Most machine learning methods operate under the assumption that the training and the test data are sampled from the same distribution. Unfortunately, in most cases, this assumption does not hold. For instance, in the case of machine translation, a model learned using a large corpus of parallel-annotated data in one source domain (e.g., newswire) is employed to translate documents in a different domain (e.g., scientific literature) because of the difficulty in retraining the model for the target domain in a timely or cost-efficient manner. Furthermore, in most real-world situations the data generation process is itself time varying (e.g., even the news domain shifts over time and new words/phrases enter the vocabulary). Thus, it is important to have efficient and accurate methods for detecting, quantifying, and mitigating the negative consequences of model drift.

The goal of this effort was to develop and validate a computational framework for model drift detection and correction in unsupervised settings. In particular, the project was addressing the following two broad questions:

1. Given a reference dataset, and a model trained on that dataset, to what extent can we apply the learned model directly to a new dataset without retraining?
2. When a drift is detected, what is the optimal strategy of retraining the model, depending on the cost of retraining, expected performance deterioration if not retrained, and so on.

For the first sub-problem, we have utilized our recently developed method, Correlation Explanation, or CorEx, for detecting distributional changes in high dimensional data. For the second sub-problem, we have developed a decision-theoretic approach that provides a computational framework for trading off cost versus expected performance gain.

To validate our approach, we have focused on topic modeling and monitoring problem, with a particular emphasis on understanding and characterizing model drift in scientific literature. Our experiments were geared toward demonstrating the two central aspects of our approach: In the first set of experiments, we evaluated the ability of the proposed approach to detect and quantify model drift. And in the second set of experiments, we have performed a quantitative evaluation of the proposed decision-theoretic framework for drift correction, based on cost-sensitive model retraining paradigm. In addition to topic modeling, we have also conducted experiments in another domain, machine translation.

## Methods, Assumptions, and Procedures

The proposed approach consists of two main components, *Measuring Drift* and *Decision Framework*, as schematically illustrated by the colored boxes in Fig.1. We now describe each individual component in more detail.

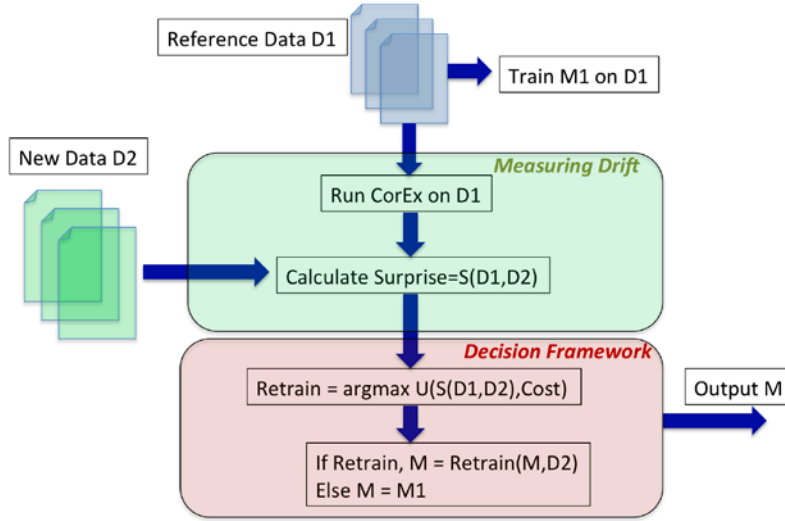


Figure 1 Schematic illustration of the proposed Model Drift detection & Correction Framework

## Measuring Model Drift via Surprise

Consider a setting where we are given two datasets, and would like to know whether the model learned for the first dataset can be applied to the second dataset. In the absence of labeled data, one alternative for measuring model drift is to characterize the distance between distributions from which those datasets originate. For instance, one could compare the various moments of those distributions (e.g., skewness or kurtosis). A more general approach pursued here is to characterize the change in the distribution themselves, using information theory. Intuitively, distributional differences can be described using the metaphor/language of “surprise.” The surprise of an observation,  $x$ , is defined as its negative log likelihood,  $S(x) = -\log p(x)$  (according to the “true” distribution,  $p(x)$ ).

Imagine we are given one or several samples from a new, unknown distribution,  $q(x)$ . Are these samples different enough from the original distribution that we should re-train our model? Here we suggest a model-free approach for calculating the surprise. Estimating information-theoretic quantities from samples is difficult because they depend on the unknown probability,  $p(x)$ . If  $x$  is actually an  $n$ -dimensional variable, then the number of samples needed to estimate  $p(x)$  is exponential in  $n$ . Instead of estimating  $p(x)$ , we define an information-theoretic optimization whose output produces a function  $f(x)$  that is an upper bound for the true surprise. Greater computational effort in the optimization leads to successively tighter bounds eventually converging to the true bound. This approach relies on the recently introduced method of Correlation Explanation (CorEx) that defines an information-theoretic coarse-graining for high-dimensional data [1,2]. CorEx is a fully non-parametric method that grounded in information theory, works as follows: Given a set of high-dimensional sample points, it learns a hierarchical generative model that explains the observed correlations in the covariates. Specifically, given



the observed covariates, CorEx introduces a layer of hidden variables, so that, when conditioned on those variables, the covariates become uncorrelated (or less correlated). Mathematically, this is done by minimizing an information-theoretic entity called *Total (conditional) Correlation*; see [1,2] for more details.

## Drift Correction Methods

Once we have detected a distributional shift, the next step is to decide whether to retrain the model or not. Our proposed drift correction framework is based on a utility-maximization approach. Namely, our decision process is formulated via the following optimization problem:

$$R = \underset{r \in \{1,0\}}{\operatorname{argmax}} U(r)$$

$$U(r) = -Cr - \gamma \operatorname{Err}(r)$$

Here  $C$  denotes the cost of retraining;  $\gamma$  is a parameter controlling the relative tradeoff between cost and error, and  $r$  is a binary variable indicating whether there is retraining or not: when  $r = 1$ , we retrain the model, otherwise we do not; and finally,  $\operatorname{Err}(r)$  is the expected error for the particular choice of  $r$ . Since we do not have a way of estimating the error (in the absence of labeled data), we will use empirically measured relationship between surprise and error. As detailed in previous reports, this relationship can be approximated by piecewise linear function.

In our experiments reported below, we used  $\gamma = 1$ , and will tried 5 different values for the cost  $C$ , to ensure that we capture various realistic scenarios.

For comparison, below we have considered the following baselines:

- B1: No retraining
- B2: Always retraining;
- B3: Retraining when the change in surprise is more than 10%.

In our experiments, we have compared those approaches across two different performance metrics: *utility*, as defined above, and *classification accuracy*; and *utility* as defined above.

## Results and Discussions

We now describe the datasets used in our validation studies, and the main findings from our experiments.

### Datasets

#### Topic Modeling Task

The experiments were conducted on three datasets, arxiv, PubMed, and NIPS.

The arxiv data contains paper abstract from different disciplines and sub-disciplines, including Computer Science, Math, Physics, covering the period 1995-2013. Here we will focus on CS papers, which itself is comprised of different subcategories, CS.AI, CS. Logic, etc. The PubMed dataset contains papers from four journals, *BMC Bioinformatics*, *BMC Developmental Biology*, *BMC Genomics*, and *BMC Cancer*. These papers span from 2001 to 2015. Finally, the NIPS dataset contains papers from NIPS (Advances in Neural Information Processing Systems) conference series from 1988-2003.

For all datasets, we set up a binary classification task, by dividing the papers into two classes, A and B. For the *arxiv* data, we considered papers in CS.AI as class A, and the rest of the CS papers as class B. For PubMed data, we considered *BMC Cancer* to be class A, and all the other papers as class B. For NIPS, we set up class A to contain all the papers on neural network and neuroscience, while the other papers constitute the class B. Note that we had to manually label NIPS papers for setting up this classification task. Additionally, for NIPS we also planned a different classification task, where class A contained papers written by a selected group of authors, and class B included all the other papers. Unfortunately, as indicated below, the classifier did not achieve a reasonable accuracy even for the reference dataset, so those experiments turned out to be not that valuable.

The statistics of the datasets are listed in the tables below.

#### NIPS data

Number of documents	2709
Dictionary size	4005
Number of authors	2484

#### PubMed data

Number of documents	19369
Dictionary size	23222
Number of journals	4

#### arxiv data

Number of documents	184015
Dictionary size	9989

## Machine Translation Task

One of the main required resources for current state of the art MT systems is parallel data. The main idea behind our experiments is thus as follows: We assume we have a parallel data in one domain, but not in the second domain. Thus, when we train an MT engine in one domain, we should decide whether to apply it to a second domain, or to get additional parallel data from that domain and retrain. Since building MT engines is a time and resource consuming exercise, we have designed a careful plan for experimentation.

- **Data:** French-English parallel data from <http://opus.lingfil.uu.se/>
  - D1: OpenSubtitles2015 (66k/51M/338.5M docs/sentences/words)
  - D2: MultiUN (87k/13.2M/320M docs/sentences/words)
- **MT engines development**
  - Select training data: 20M words of training data per domain
  - 2,500 sentences for tuning per domain
  - Train 3 MT engines: D1, D2, D1+D2
- **Test data setup**
  - Select 5,000 documents for each domain (D1, D2)
  - Construct a test dataset  $D_{\text{test}}$  by taking a weighted combination of D1 and D2 (for different weights of each component).
  - Translate each document in  $D_{\text{test}}$  with each of the three engines.

The quality of the MT engine is measured by the Bleu score.

## Drift Detection for Topic Modeling Task

### Experiments with gradual shift

First, we look at the experiments with gradual drift. In this settings, we use papers published in  $\{Y_1, Y_2, \dots, Y_t\}$  for training, and then use each of the years  $\{Y_{t+1}, Y_{t+2}, \dots, Y_T\}$  as training sets.

Her we focus on PubMed and NIPS datasets.

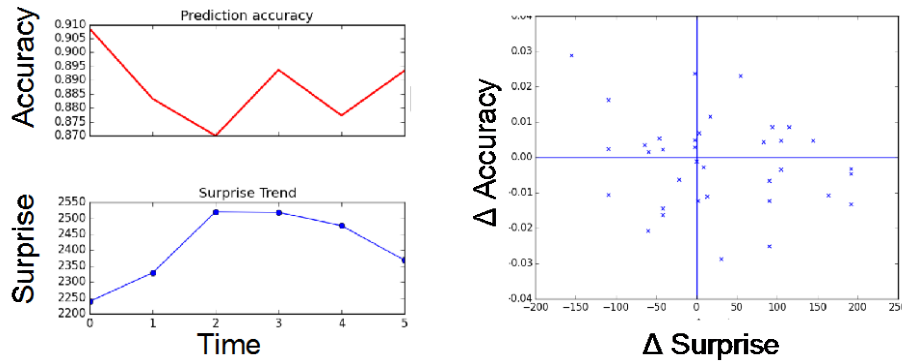


Figure 2 Temporal drift results for PubMed dataset

Fig. 2 shows results from a representative run for the PubMed data. We used all the papers published in the range 2001-2009 as the training set. Correspondingly, the papers published during 2010-2015 are the test set. The number of topics for this experiment is set to 50. After learning an LDA model on the training, or reference, set  $D_R$ , we use an SVM classifier that separates the classes A and B. We then apply this classifier to each publication year in the test set  $D_T$ , and track the prediction accuracy. We also calculate the surprise  $S(D_R, D_T)$  for each of the testing dataset  $D_T$ .

In the left panel, we plot the prediction accuracy and surprise against time. We observe that the dip in accuracy is match by an increase in surprise. After the decrease, the accuracy fluctuates, while the surprise becomes almost constant, and then even decreases. On the right, we show a scatter plot of the change in accuracy vs change in surprise. Note that we have performed multiple runs for generating the scatter plot.

Next, we discuss results from the NIPS data, shown in Fig. 3, which shows a typical run with a number of topics set to 100. The papers from the first 8 conferences comprise the training set, and each subsequent conference is treated as a test set.

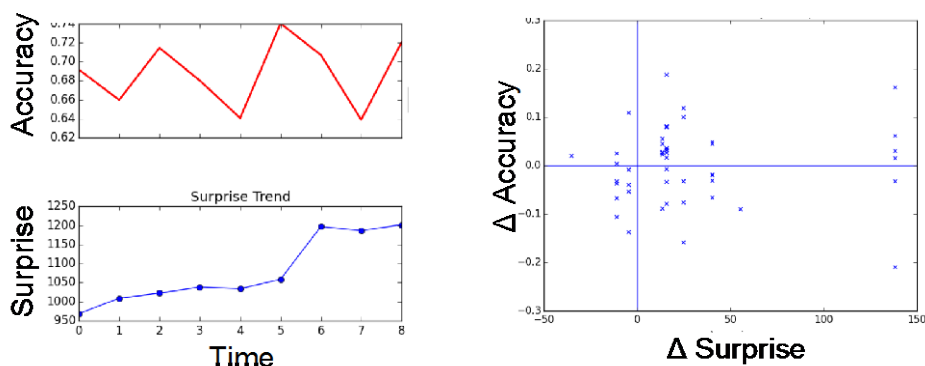


Figure 3 Temporal drift results for the NIPS dataset

We note that the classification accuracy does not show a clear temporal tendency to decline. Instead, it rather fluctuates around the value  $Acc \approx 0.68$ . The surprise, on the other hand, increases, except for the 5<sup>th</sup> and 8<sup>th</sup> test sets. This is somewhat counterintuitive, although we note that most of the increase in surprise is very moderate, except for the 7<sup>th</sup> test set, which also accompanies relatively big drop in accuracy. Also, the scatter plot on the right does not show any significant correlation between change in accuracy and change in surprise.

Finally, we consider the second classification task with NIPS dataset, where the goal is to classify the papers according to their authors. Namely, class A contains all the papers written by a selected list of  $K$  authors, whereas class B contain all the other papers. As we already mentioned, the results for this classification task were poor even for the reference dataset, as shown in Fig. 3. Thus, this particular problem is not very useful from the perspective of detecting model drift.

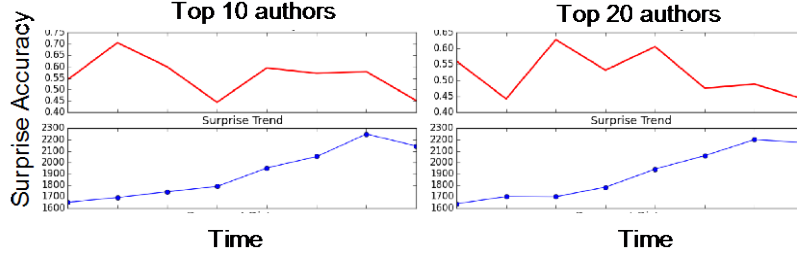


Figure 4 Author classification results for NIPS dataset

### Experiments with abrupt shift

Now we focus on experiments when the model drift is abrupt. The abrupt shift was implemented as follows.

Let  $D_A = \{a_1, a_2, \dots, a_N\}$  and  $D_B = \{b_1, b_2, \dots, b_N\}$  be two corpora of documents for our binary classification task. For instance, in the case of NIPS data,  $D_A$  is the set of papers in the category NN (Neural Networks), whereas  $D_B$  is the set of papers in the other category NotNN (not Neural Networks). Furthermore, let  $D_C = \{c_1, c_2, \dots, c_M\}$  be yet another set of papers. For instance, this can be a subset of the NotNN category papers. Or, it can be from a totally different collection.

We divide the sets  $D_A$  and  $D_B$  **randomly** into a Reference and Test sets,  $D_A = D_A(Ref) + D_A(Test)$ ,  $D_B = D_B(Ref) + D_B(Test)$ . So now we have a Reference and Test datasets,  $\mathbf{D}_{Ref} = D_A(Ref) \cup D_B(Ref)$  and  $\mathbf{D}_{Test} = D_A(Test) \cup D_B(Test)$ . The LDA model, the corresponding SVM classifier, and CorEx, will be trained on this set  $D_{Ref}$ . Note that according to the above construction,  $\mathbf{D}_{Ref}$  and  $\mathbf{D}_{Test}$  come from the same distribution. Thus, an SVM classifier trained on  $\mathbf{D}_{Ref}$  should produce accurate results for  $\mathbf{D}_{Test}$  as well.

We now introduce a parameterized abrupt drift as follows:

1. Let  $\alpha$  be a number between 0 and 1.
2. For each document  $\mathbf{d}$  in  $\mathbf{D}_{Test}$  do the following:
  - a. Select a random document  $\mathbf{c}$  from set  $D_C$
  - b. For each word in document  $\mathbf{d}$ , with probability  $\alpha$ , replace it with a random word from document  $\mathbf{c}$
3. Repeat the above for  $\alpha = \{0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0\}$

For each value of  $\alpha$ , the above procedure will result in a new, **drifted** test set  $\mathbf{D}_{Test}(\alpha)$ . For each of those dataset, we will test for model drift and calculate the relationship between accuracy and surprise.

In addition to surprise a calculated via CorEx, we will also consider another measure of distributional distance for measuring the drift. The KL distance between the Reference and Test datasets,  $\mathbf{D}_{Ref}$  and  $\mathbf{D}_{Test}$  is defines as follows,

$$KL(\mathbf{D}_{Ref} || \mathbf{D}_{Test}) = \sum_d p_{Ref}(d) \log \frac{p_{Ref}(d)}{p_{Test}(d)}$$

where the summation is over all the possible documents (in bag of words representation), and  $p_{Ref}, p_{Test}$  are the distributions generating the reference and test sets, respectively.

Direct evaluation of KL distance is impossible due to the enormous state space. Thus, we replace the distributions  $p_{Ref}, p_{Test}$  by their empirical approximations as follows. We first combine all the documents in the Reference (Test) set into a single document, and corresponding bag of work representation, e.g.,  $\mathbf{BOW}_{Ref} = \{w_1, w_2, \dots, w_K\}$ , where  $K$  is the dictionary size, and  $w_k$  is the number of times the  $k$ -th word appears in the corpus. Let  $N = \sum_{k=1}^K w_k$  be the total number of words in the corpus, and let  $x_k = \frac{w_k}{N}$ . We then approximate  $p_{Ref}$  by multinomial distribution  $Mult(x_1, x_2, \dots, x_K)$ . The approximation for the test set is defined similarly. With this approximation, the KL distance can be calculated easily.

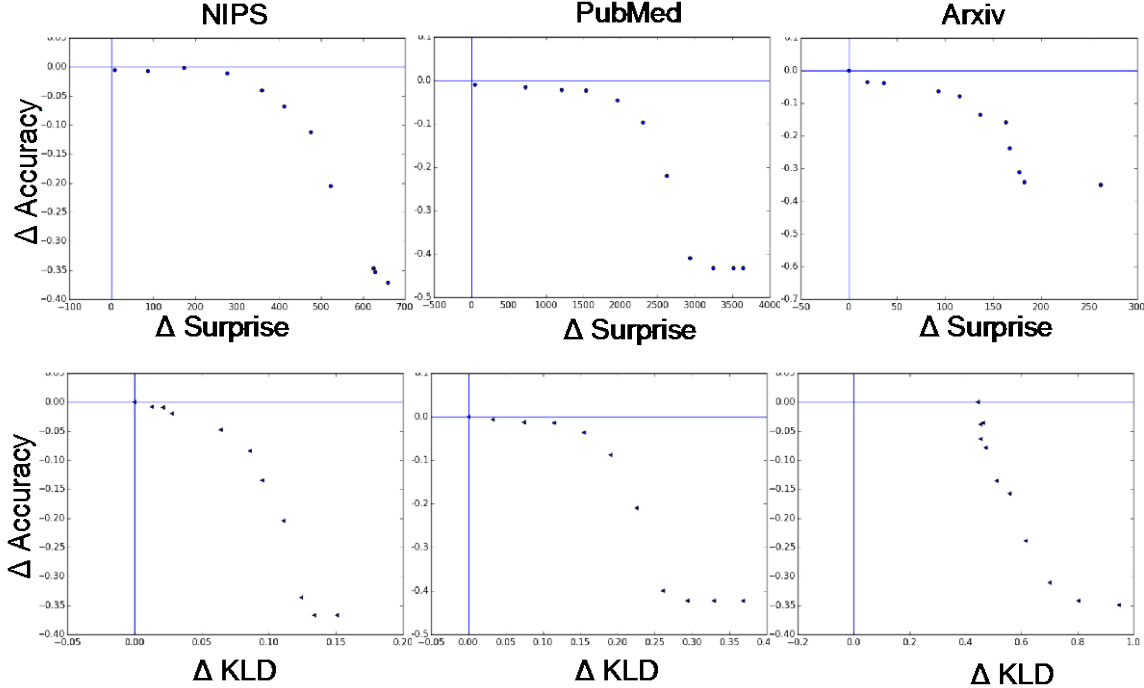


Figure 5 Relationship between change in accuracy and surprise/empirical KL distance

The results from the experiments are shown in Fig. 5, where we show a scatter plot of the change in accuracy  $\Delta Accuracy$  vs change in surprise  $\Delta Surprise$  (upper panel) and the empirical KL distance  $\Delta KLD$  (lower panel). Each point corresponds to a specific value of  $\alpha$ .

First, we observe that for the abrupt drift scenario, the relationship between the change in accuracy and surprise is less noisy, and more well-defined. Namely, if the change in surprise is larger than some threshold value, then there is also a noticeable drop in accuracy. The threshold value varies from dataset to dataset, which is expected. More importantly, the relationships are qualitatively similar for three datasets (despite quantitative differences).

We observe a similar picture with the empirical KL distance, especially for the NIPS and PubMed dataset. However, for the arxiv dataset (which has shorter documents), the behavior is more abrupt, which suggests that the empirical KL distance is not a universally good measure of distributional change.

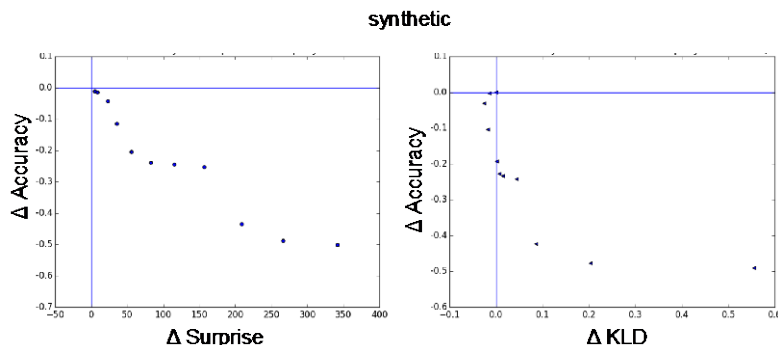


Figure 6 Relationship between change in accuracy and surprise/empirical KL distance for synthetic data

Indeed, our experiments with synthetic data confirm this point. For instance, Fig 5 shows results from experiments with synthetically generated data, which shows that the empirical KL distance is not detecting any change, even though the accuracy has dropped significantly. In fact, it is possible to construct example where the empirical KL distance fails to recognize distributional changes. For instance, let  $x_k^A$  and  $x_k^B$  be the probabilities of seeing the  $k$ -th word in class A and B, respectively. Since the empirical KL distance depends only on the aggregate probability  $x_k^A + x_k^B$ , any transformation of those probabilities that does not change the aggregate probability will not change  $p_{Ref}$  (or  $p_{Test}$ ) either. The surprise, on the other hand, is calculated by first estimating the correlation structure of the data, and will detect any relevant distributional drift.

## Drift Correction for Topic Modeling Task

For drift correction, we used NIPS, PubMed, and arxiv datasets for our experiments, and focused on abrupt drift scenario as described above. Recall that in this scenario, we have a **drifted** test set  $\mathbf{D}_{Test}(\alpha)$  for each value of the mixing parameter  $\alpha$ . We will conduct our drift correction experiments for each of those datasets.

We start our discussion of results with the NIPS data.

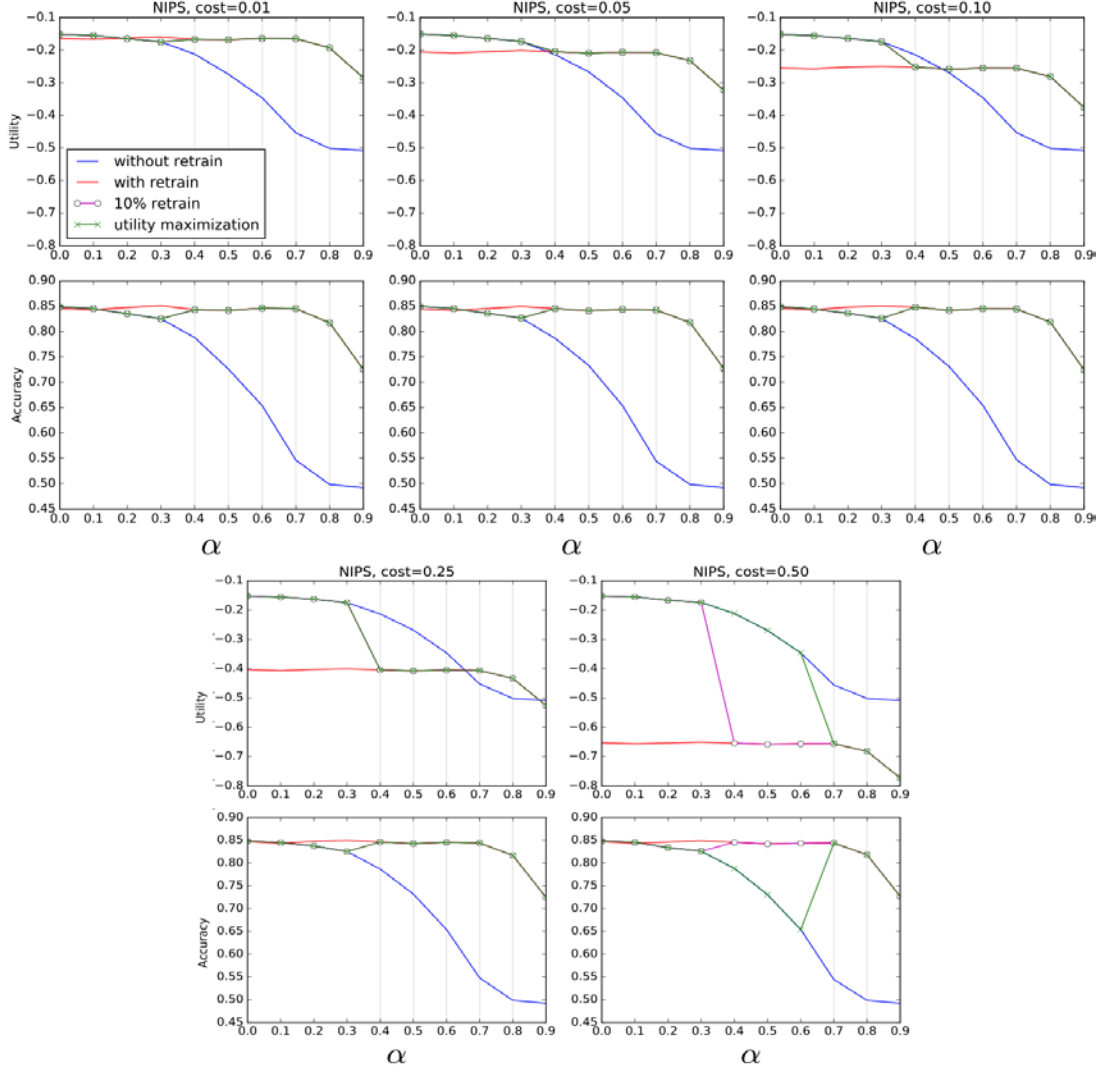
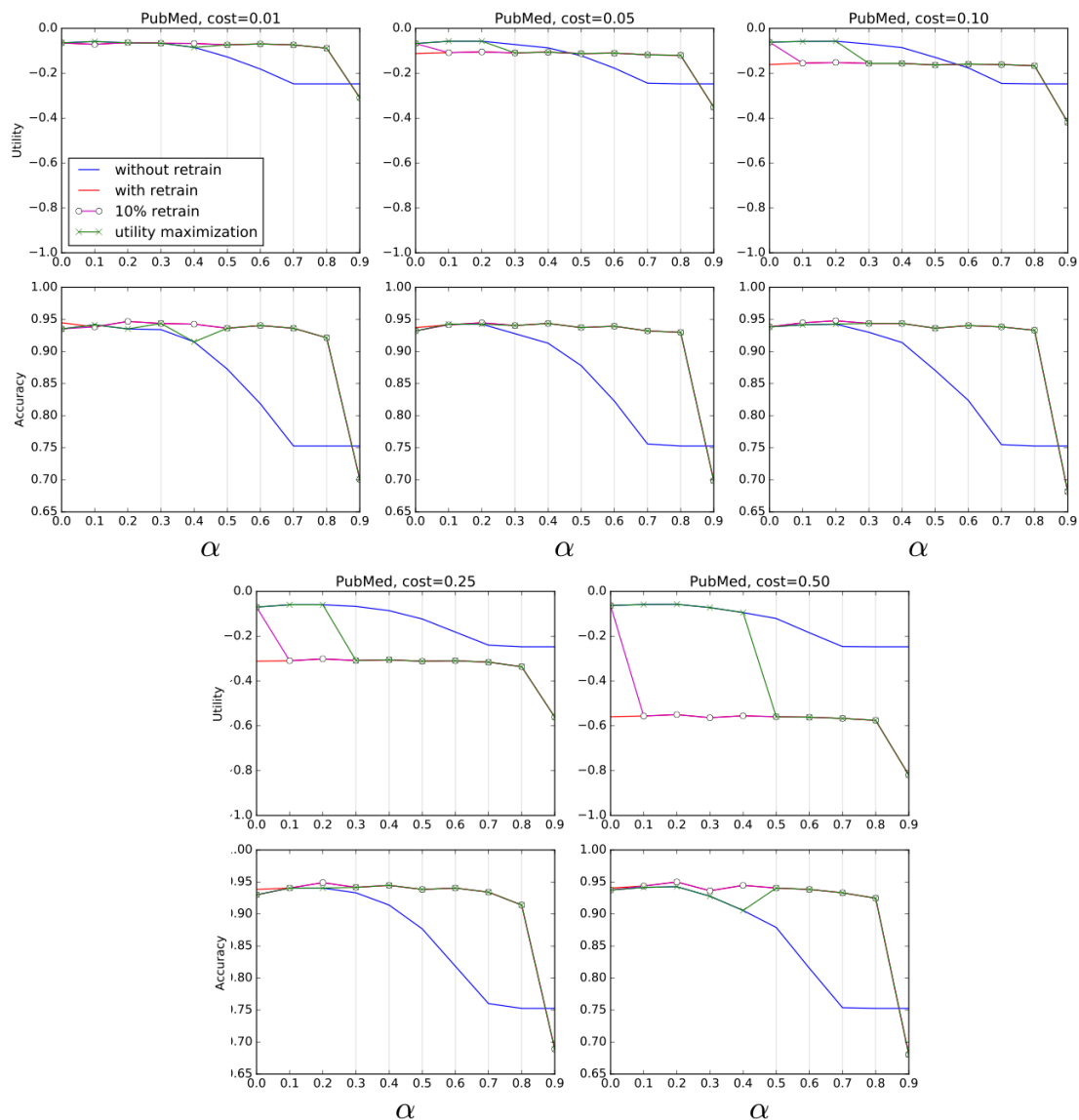


Figure 7 Results for the NIPS dataset. The vertical grey lines indicate “retraining” for our decision-theoretic method

Fig. 7 shows the utility and accuracy as a function of  $\alpha$  under the four strategies, and five different values for the cost parameter,  $C = \{0.01, 0.05, 0.1, 0.25, 0.5\}$ .

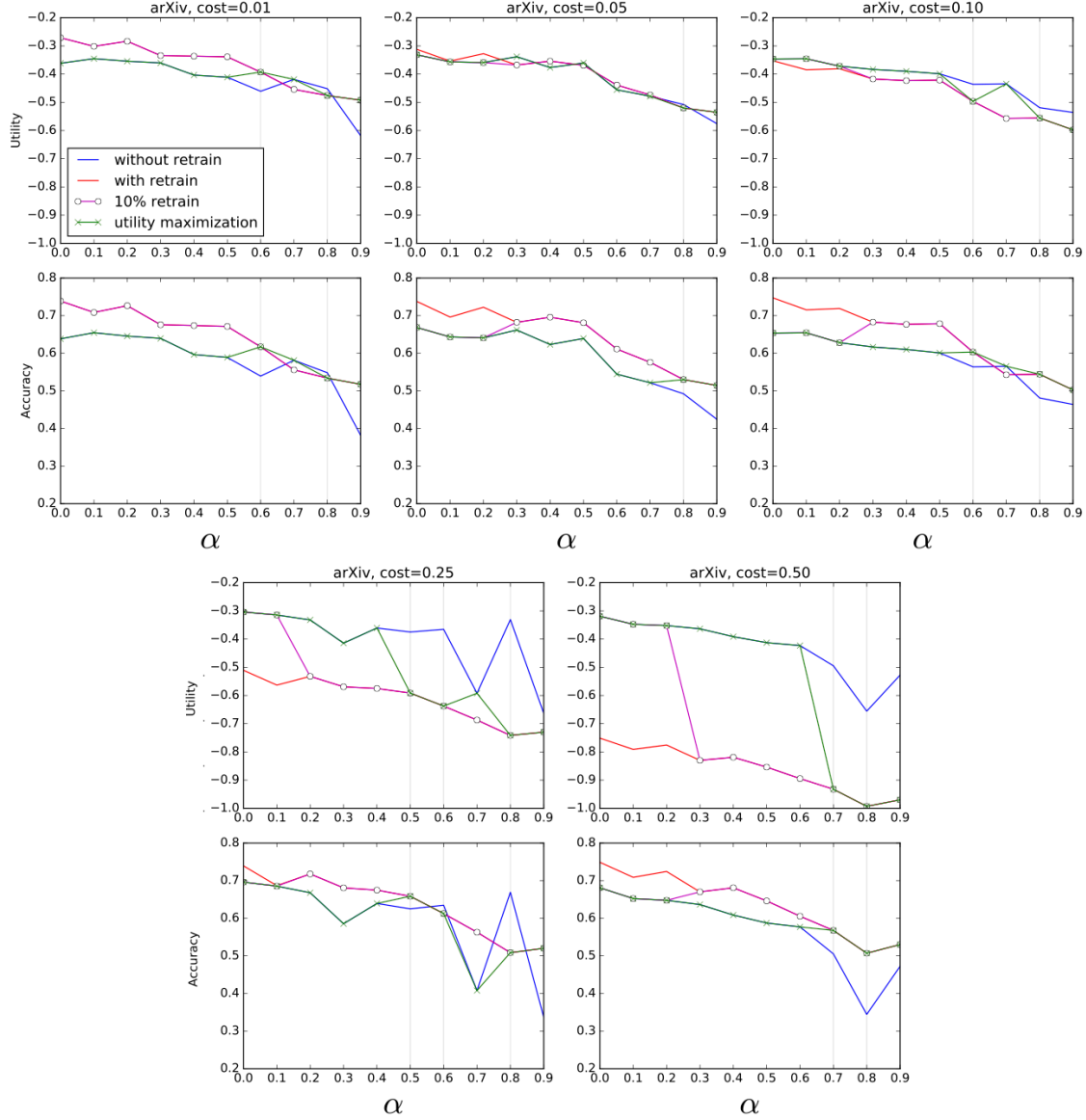


The results are exactly what we expect: we consistently get a high accuracy of 0.85 if we always retrain, and our accuracy tapers down to 0.5 if we never retrain. The always-retrain strategy achieves high utility when the cost of retraining is low, and the never-retrain strategy achieves high utility when the cost of retraining is high. Both the +10%-surprise and utility-maximization perform about equally well in the low- to mid- retraining cost scenarios, but the +10%-surprise strategy suffers when the cost of retraining is high. Note that by suffering we mean that the utility of the strategy is lower: the accuracy under this strategy is of course better. However, the gains in accuracy are erased by high cost of retraining. Thus, overall, the utility-maximization approach produces better results.



**Figure 8 Results for the PubMed dataset. The vertical grey lines indicate “retraining” for our decision-theoretic method.**

The results for the PubMed (see Fig. 8) demonstrate the same general behavior. Here, always retraining gets us an accuracy score of about 0.95, and our accuracy dips to 0.75 when we never retrain. The always-retrain strategy edges out the never-retrain strategy when cost is low, but suffers greatly when the cost of retraining is high. The +10%-surprise strategy performs almost no better than the always-retrain strategy; the surprise for this dataset grew rapidly with  $\alpha$ , so the +10%-surprise strategy decided to retrain except for very small alpha. We expect this to be the case for at least some datasets, since '+10%' is not a learned constant. The utility-maximization strategy almost always outperforms the +10%-surprise strategy for this dataset. For this dataset especially, the utility-maximization function performs worse than the never-retrain strategy for high values of  $\alpha$ . This means a better surprise-to-accuracy estimation function than ours would be less optimistic about retraining when  $\alpha$  is large.



**Figure 9 Results for the arxiv dataset. The vertical grey lines indicate “retraining” for our decision-theoretic method**

Finally, we focus on the arxiv dataset (Fig. 9). Note that one of the main differences of this dataset from the other two is that the documents are significantly shorter (abstracts instead of full text), thus there are significant fluctuations. For this dataset, retraining does not give a significant improvement in accuracy, so the cost of retraining is the most significant factor in the utility model (although, note that increasing cost does not necessarily mean fewer number of retrains, due to above mentioned fluctuations). As with the PubMed dataset, the +10%-surprise strategy decides to retrain for all except very small  $\alpha$ . The performance of the utility-maximization strategy is more mixed here, although, overall, it still yields the most balanced approach to retraining. It sometime performs the best except for when  $\alpha$  and the retraining cost are high, in which case the never-retrain strategy

performs better. As with the PubMed dataset, our surprise-to-accuracy estimation function should show less affinity to retrain when  $\alpha$  is large.

## Drift Detection for the Machine Translation Task

### Training Machine Translation Engines

Our experiments in the machine translation domain will focus on English-French parallel corpora-based translations. We focused on two main datasets, D1=OpenSubtitles2015 (*os*), which contains subtitles from movies, and D2= MultiUN (*mun*), which is a multilingual corpus from the United Nations documents.

Based on those two corpora, we trained three MT engines, M1, M2, and M3. The first two engines have been trained on D1 and D2, respectively, whereas M3 has been trained on the union of two corpora D1+D2.

We evaluate the quality of the given MT engine (when applied to a given dataset) by the so-called BLEU Score (see <https://en.wikipedia.org/wiki/BLEU>), which is the adopted metric in the MT research community.

File Name	BLEU(M1)	BLEU(M2)	BLEU(M3)
en/2005/UNEP_POPS_COP1_12.xml.gz	33.9	10.9	33.6
en/2005/A_C5_60_L22.xml.gz	76.8	8.4	76.7
en/2005/CD_PV971.xml.gz	46.2	11.9	44.6
en/2005/FCCC_KP_CMP_2005_6.xml.gz	32.5	13.1	32.5
en/2005/A_C1_60_L33_REV1.xml.gz	69.7	13.9	68.4
en/2005/S_AC45_2005_27.xml.gz	34.8	12.4	32
en/2005/E_CN4_2005_L63.xml.gz	73.6	16.1	73.8
en/2005/TRANS_WP29_2005_82.xml.gz	76.2	10.9	77.7
en/2005/CCPR_C_83_D_823_1998.xml.gz	37.9	12.7	36.5
en/2005/E_2005_L51.xml.gz	55.5	13.3	53.7
en/2005/A_60_PV17.xml.gz	57.5	14.8	55.1
en/2005/HBP_WP7_2005_8.xml.gz	23.6	9.88	22.9
en/2005/S_PV5277.xml.gz	52.2	12.5	50.8
en/2005/E_CN4_SUB2_2005_L40.xml.gz	69.8	21	71.7
en/2005/FCCC_KP_CMP_2005_3.xml.gz	41.2	15.1	41.7
en/2005/S_2005_494.xml.gz	50.2	20.7	52.5
en/2005/NPT_CONF2005_MCIWP2.xml.gz	67.0	15.9	70.2

Partial output of the trained MT engines on dataset D1 is shown in the table above. The first column shows the name of the documents (5000 in the test dataset). The second, third and fourth columns show the BLEU scores of models M1, M2, and M3, respectively, for the corresponding document. Note that the BLEU score of M2 (column 2) are considerably smaller than BLEU(M1). This is of course due to the fact that the M2 is trained on a different dataset (D2), and the relatively poor performance is due to domain mismatch between D1 and D2.

### Surprise vs Drift

We have examined this phenomenon in a more fine-grained manner, by constructing a test set that was a tunable mixture of  $D_1$  and  $D_2$ ,  $D_{Test} = (1 - \alpha)D_1 + \alpha D_2$ . Thus,  $\alpha = 0$  and  $\alpha = 1$  corresponds to no drift and maximum drift, respectively.

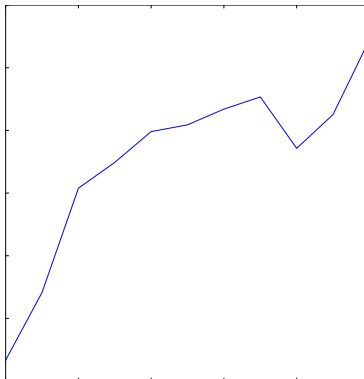


Figure 10 Surprise as a function of mixing parameter alpha

The results are shown in Figure 10. The relationship is mostly what we expect, with surprise increasing with  $\alpha$ . One exception is for  $\alpha = 0.7$  where the surprise had a slight decrease, but then it starts increasing again. We believe this counterintuitive decrease will disappear if we average the results for many random trials.

### Domain Drift and Translation Accuracy

Next, we study the relationship between the amount of domain drift (as measured by surprise) and the translation accuracy as measured by BLEU scores.

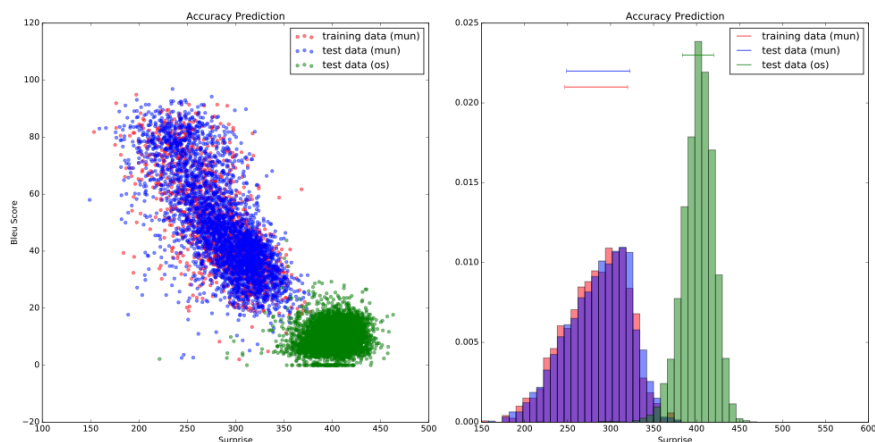


Figure 11 (Left) Scatter plot of BLEU vs Surprise, where each point is a document; training and test sets are as indicated in the legend. (Right) Histogram of Surprise for training and test sets

Figure 11 shows the scatter plot of the BLEU scores vs surprise, when the *mun* is the reference dataset and *os* is the test dataset. There are several worthwhile observations we can make. First, we see that there are two well-separated clusters

of documents corresponding to either datasets. Second, when the test set is also chosen from *mun*, there is no discernable differences between the train and test sets; see the figure on the right where we show the histogram of the Surprise for all three datasets. Finally, document level BLEU score is ***decreasing with surprise***, so that more surprising documents are translated less accurately.

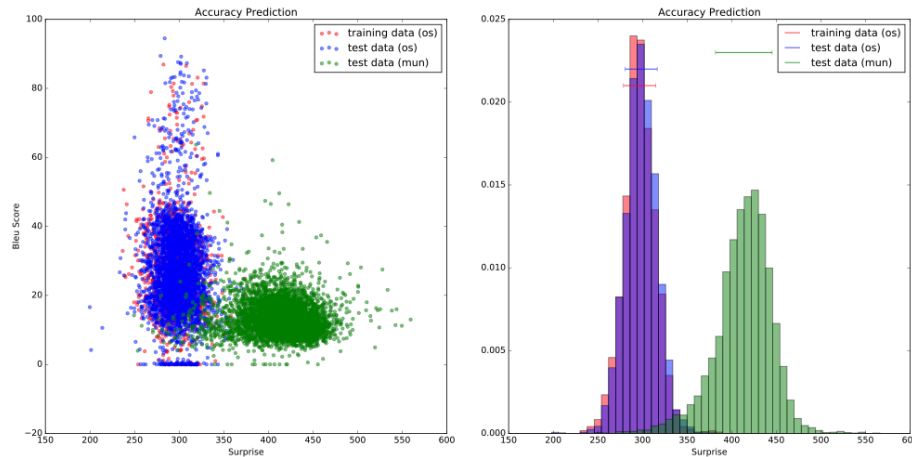


Figure 12 Same as in Figure 2 but for different train and test split; see the legend

Similar picture albeit with some differences is observed when we train on *os* and then test on *mun*. Namely, there are still two well-separated clusters. However, in this case, the relationship between the BLEU scores and Surprise in the training dataset is much more random. Namely, two documents might have the same surprise, but their BLEU scores can differ by significant amount. Note also that there are some documents in the test set (*mun*) that have higher BLEU score than some of the documents in the training set, even if those documents have higher values of surprise. We are planning to analyze this phenomenon in more details in coming weeks.

### Toward Active Drift Correction Methods

We have also conducted experiments with more elaborate retraining cost models compared to what we had considered for the topic modeling problem. Remarkably, this type of cost models are omnipresent in MT domain. Namely, given two domains such as *mun* and *os*, and the distributional mismatch as measured by Surprise, we can ask the following questions:

1. If we are getting higher surprise in the test dataset, how much we will gain if we spend some budget on annotating additional data (for MT, annotating means manually building a parallel corpus)?
2. For a given budget, which of the documents one should translate for building that parallel corpus?

For the second question, the baseline approach would be to select documents at random. However, another intuitive approach would be selecting the documents based on their Surprise, e.g., documents that have higher surprise should get higher priority for annotation.

A full analysis of the above strategy would correspond to training more MT engines with different sets of parallel corpora, which is a very costly exercise, and given the limited time we have for the program, might not be feasible. Instead, we conducted an alternative set of experiments, where, instead of evaluating the data selection approach on translation accuracy, we evaluate it based on how much it reduces surprise.

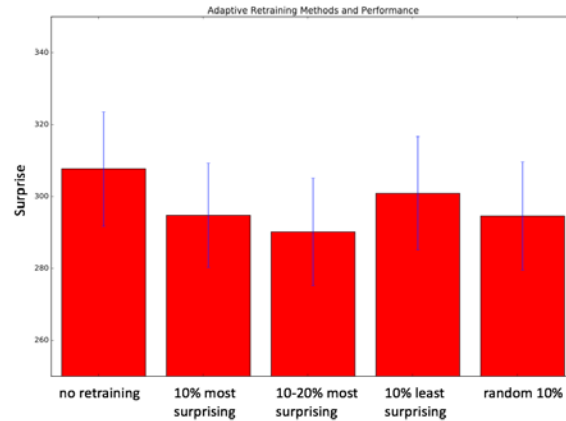


Figure 13 Surprise under different data selection strategies

The results are shown in Figure 13. First, we rank all the documents in the test set according to the Surprise, e.g., top 10%, 10-20%, ..., bottom 10%. In addition to the baseline method with no retraining, we consider 4 different data selection strategies: (1) Select from the top 10%; (2) Select from 10%-20%; (3) Select from the bottom 10%; (4) Select randomly. Under all four strategies we observe decrease in surprise, which is intuitive. Furthermore, the decrease is the weakest under strategy (3), which is also understandable, since the documents that are not so surprising were already well-represented in the original training set, and including them again will not change much. Perhaps the more interesting findings are that selecting the top 10% results in the same decrease in surprise as selecting randomly, and that selecting from 10%-20% yields the best reduction in surprise. This is probably because this range of surprise includes documents that are typical, and not just outliers in the test set. However, this point needs further examination.

## Conclusions

To conclude, we have proposed a novel computational framework for detecting and quantifying model drift, and correcting drift based on decision-theoretic framework. We have also performed exhaustive experiments for validating and evaluating the proposed framework. In our first evaluation, the experiments for drift detection and quantification confirmed that surprise as measured by CorEx is indeed able to capture important distributional changes. Furthermore, our experiments also helped with understanding the relationship between drift and performance deterioration. While our results for temporal/gradual drift are not very conclusive, for the abrupt drift scenario we find that there is significant statistical relationship between increase in surprise and performance deterioration. Importantly, the relationship seems to be qualitatively similar for different datasets (albeit with quantitative difference that are expected).

In the second evaluation, we found that our proposed decision-theoretic drift-correction framework performed as expected. Specifically, the advantage of the proposed approach is its ability to adapt to different cost/benefit ratio of a given scenario. Indeed, for low cost of retraining, the behavior produced by the utility-maximization approach is similar to “always retrain” and “10% retrain” strategies, while for larger  $C$ , it starts to become more similar to “never retrain” strategy. This adaptive nature of the proposed method makes it the best overall choice among the baselines, when the performance is measured via the utility function.

## Recommendations

Based on the findings of our project, we believe there are several important directions where further explorations are needed. First of all, one of the central problems we encountered within our seedling project was the performance prediction, e.g., ability to predict the performance of an algorithm trained on one dataset, when that algorithm is used on a previously unseen dataset. While this is an active research area for domains such as machine translation, we believe that efficient solutions to this problem can be relevant and valuable for diverse set of machine learning applications. On a more general note, while our project has addressed specific aspects of model drift phenomenon, we believe there is a need for a more general and broader research agenda for machine learning in time-varying and non-stationary environments.

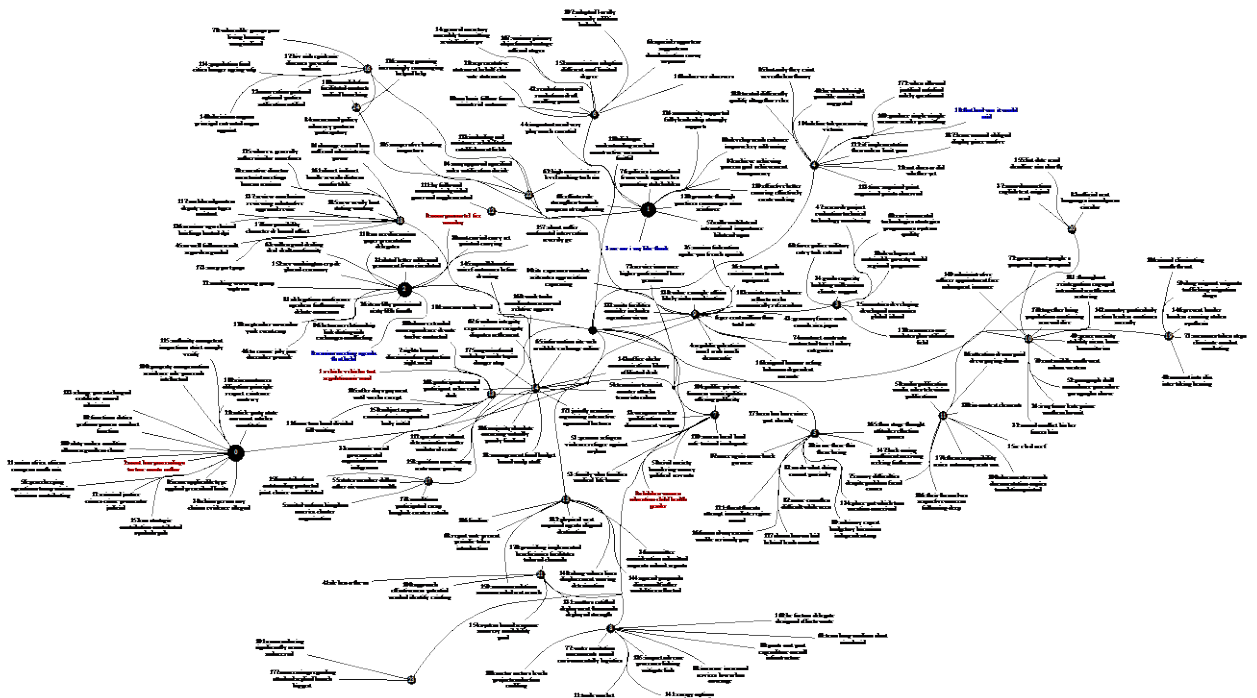


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- [1] Greg Ver Steeg and Aram Galstyan. Discovering structure in high-dimensional data through correlation explanation. In Proc. of NIPS'14, 2014.
- [2] Greg Ver Steeg and Aram Galstyan. Maximally Informative Hierarchical Representations of High-Dimensional Data. In Proc. of AISTATS'15, 2015.

## Appendix

### A. Hierarchical structure learned by Corex on mun dataset



## B. Topics learned by Corex on mun dataset

Below we provide the list of topics discovered by CorEx for the MultiUN dataset. There are two line for each topic: The first line shows the Group number corresponding to a latent variable, and the total correlation  $TC(X;Y_j)$  between that latent variable and words in that topic. The second line shows the top words that are most relevant to that topic.

When running CorEx, the number of latent variables (and hence # of topics) was set to 200.

Group num: 0,  $TC(X;Y_j)$ : 0.690  
0:children,women,education,child,health,gender,school,care,age,men  
Group num: 1,  $TC(X;Y_j)$ : 0.546  
1:vehicle,vehicles,test,regulation,air,used,mm,manufacturer,amend,temperature  
Group num: 2,  $TC(X;Y_j)$ : 0.489  
2:court,law,proceedings,torture,courts,author,act,detention,cases,offence  
Group num: 3,  $TC(X;Y_j)$ : 0.432  
3:we,our,i,my,like,thank,us,me,hope,today  
Group num: 4,  $TC(X;Y_j)$ : 0.407  
4:republic,palestinian,israel,arab,israeli,democratic,congo,mr,president,occupied  
Group num: 5,  $TC(X;Y_j)$ : 0.383  
5:united,nations,kingdom,america,charter,organization,bretton,woods,summits,according  
Group num: 6,  $TC(X;Y_j)$ : 0.344  
6:per,cent,million,than,total,rate,estimated,average,years,less  
Group num: 7,  $TC(X;Y_j)$ : 0.340  
7:rights,human,discrimination,protection,right,racial,cultural,freedoms,fundamental,promotion  
Group num: 8,  $TC(X;Y_j)$ : 0.327  
8:room,pm,am,tel,fax,monday,mail,wednesday,thursday,friday  
Group num: 9,  $TC(X;Y_j)$ : 0.272  
9:session,meeting,agenda,th,at,held,hoc,ad,seventh,twenty  
Group num: 10,  $TC(X;Y_j)$ : 0.257  
10:that,had,was,it,would,said,were,noted,could,stated  
Group num: 11,  $TC(X;Y_j)$ : 0.257  
11:trade,market,investment,markets,growth,production,economy,agricultural,products,business  
Group num: 12,  $TC(X;Y_j)$ : 0.246  
12:criminal,justice,crimes,crime,prosecutor,judicial,judges,prison,acts,prosecution  
Group num: 13,  $TC(X;Y_j)$ : 0.233  
13:weapons,nuclear,proliferation,arms,disarmament,weapon,destruction,treaty,iaea,npt  
Group num: 14,  $TC(X;Y_j)$ : 0.227

14:general,secretary,assembly,transmitting,revitalization,pv,heads,moon,fullest,personalities  
Group num: 15, TC(X;Y\_j): 0.222  
15:c,e,b,d,see,f,ii,annex,cn,para  
Group num: 16, TC(X;Y\_j): 0.194  
16:transport,goods,emissions,assets,costs,equipment,carriage,transactions,creditor,creditors  
Group num: 17, TC(X;Y\_j): 0.175  
17:hiv,aids,epidemic,diseases,prevention,malaria,infection,disease,unaids,tuberculosis  
Group num: 18, TC(X;Y\_j): 0.175  
18:management,fund,budget,board,undp,staff,financial,funds,activities,funding  
Group num: 19, TC(X;Y\_j): 0.167  
19:development,sustainable,poverty,world,regional,programme,environment,summary,cooperation,eradication  
Group num: 20, TC(X;Y\_j): 0.153  
20:article,party,state,covenant,articles,constitution,provisions,code,under,art  
Group num: 21, TC(X;Y\_j): 0.151  
21:union,africa,african,european,south,asia,caribbean,latin,pacific,region  
Group num: 22, TC(X;Y\_j): 0.147  
22:working,www,org,group,wp,trans,http,informal,htm,ended  
Group num: 23, TC(X;Y\_j): 0.145  
23:convention,protocol,optional,parties,ratification,ratified,conventions,protocols,treaties,instruments  
Group num: 24, TC(X;Y\_j): 0.140  
24:iraq,timor,leste,prime,northern,kuwait,iraqi,kosovo,minister,sri  
Group num: 25, TC(X;Y\_j): 0.127  
25:countries,developing,developed,economies,global,island,small,least,transition,landlocked  
Group num: 26, TC(X;Y\_j): 0.121  
26:item,fifty,provisional,sixty,fifth,fourth,second,ninth,third,forty  
Group num: 27, TC(X;Y\_j): 0.117  
27:been,has,have,since,past,already,several,begun,completed,gone  
Group num: 28, TC(X;Y\_j): 0.116  
28:not,does,or,did,whether,yet,nor,either,neither,necessarily  
Group num: 29, TC(X;Y\_j): 0.111  
29:representative,statement,behalf,chairman,vote,statements,representatives,vice,election,elected  
Group num: 30, TC(X;Y\_j): 0.100  
30:out,carried,carry,set,pointed,carrying,sets,carries,pointing,setting  
Group num: 31, TC(X;Y\_j): 0.100  
31:dated,letter,addressed,permanent,from,circulated,letters,verbale,herewith,identical  
Group num: 32, TC(X;Y\_j): 0.100  
32:armed,conflict,his,her,forces,him,displaced,civilians,conflicts,war  
Group num: 33, TC(X;Y\_j): 0.098

33:economic,social,governmental,organizations,non,indigenous,socio,peoples,institutions,participation  
Group num: 34, TC(X;Y\_j): 0.097  
34:goals,capacity,building,millennium,climate,support,change,lessons,partnerships,learned  
Group num: 35, TC(X;Y\_j): 0.094  
35:russian,federation,spoke,you,french,spanish,arabic,your,chinese,sir  
Group num: 36, TC(X;Y\_j): 0.094  
36:committee,consideration,submitted,requests,submit,reports,recommends,notes,observations,requested  
Group num: 37, TC(X;Y\_j): 0.093  
37:record,corrections,english,text,original,read,copy,insert,verbatim,rose  
Group num: 38, TC(X;Y\_j): 0.089  
38:claim,person,any,claims,evidence,alleged,claimant,facts,finds,panel  
Group num: 39, TC(X;Y\_j): 0.088  
39:is,are,there,this,these,being,however,still,even,most  
Group num: 40, TC(X;Y\_j): 0.087  
40:peace,security,stability,sierra,leone,humanitarian,sudan,darfur,afghanistan,lasting  
Group num: 41, TC(X;Y\_j): 0.087  
41:de,la,n,o,the,m,facto,et,des,of  
Group num: 42, TC(X;Y\_j): 0.083  
42:resolution,council,resolutions,draft,recalling,pursuant,reaffirming,sponsors,declaration,res  
Group num: 43, TC(X;Y\_j): 0.081  
43:germany,france,costa,canada,rica,japan,italy,netherlands,australia,norway  
Group num: 44, TC(X;Y\_j): 0.074  
44:important,need,very,play,much,essential,success,strong,crucial,good  
Group num: 45, TC(X;Y\_j): 0.072  
45:as,well,follows,result,regards,regarded,serve,whole,insofar,viewed  
Group num: 46, TC(X;Y\_j): 0.071  
46:to,ensure,july,june,december,provide,march,necessary,october,april  
Group num: 47, TC(X;Y\_j): 0.071  
47:research,project,evaluation,technical,technology,monitoring,institute,science,studied,analysis  
Group num: 48, TC(X;Y\_j): 0.069  
48:account,into,alia,inter,taking,bearing,mind,take,incorporation,chase  
Group num: 49, TC(X;Y\_j): 0.065  
49:be,should,might,possible,considered,suggested,given,soon,desirable,acceptable  
Group num: 50, TC(X;Y\_j): 0.063  
50:drug,migrant,migrants,trafficking,migration,drugs,workers,narcotic,smuggling,undcp  
Group num: 51, TC(X;Y\_j): 0.062  
51:persons,refugees,violence,refugee,against,asylum,disabilities,victims,unhcr,camps  
Group num: 52, TC(X;Y\_j): 0.061

52:paragraph,shall,accordance,procedure,paragraphs,above,rule,referred,described, subparagraph  
Group num: 53, TC(X;Y\_j): 0.060  
53:family,who,families,medical,life,home,woman,hospital,psychological,live  
Group num: 54, TC(X;Y\_j): 0.058  
54:terrorism,terrorist,counter,attacks,terrorists,cuban,suppression,cuba,taliban,qaida  
Group num: 55, TC(X;Y\_j): 0.056  
55:states,member,dollars,other,oic,commonwealth,sovereign,mutual,bush,participating  
Group num: 56, TC(X;Y\_j): 0.053  
56:peacekeeping,operations,troop,mission,missions,contributing,contributors,monument,unamsil,stabilization  
Group num: 57, TC(X;Y\_j): 0.052  
57:calls,multilateral,international,importance,bilateral,upon,agreements,commitment,reaffirms,continue  
Group num: 58, TC(X;Y\_j): 0.052  
58:radio,publication,media,sales,television,publications,published,broadcasting,print,broadcast  
Group num: 59, TC(X;Y\_j): 0.050  
59:civil,society,laundering,money,political,servants,aviation,servant,makeup,fortune  
Group num: 60, TC(X;Y\_j): 0.049  
60:force,police,military,entry,task,entered,civilian,officers,personnel,enter  
Group num: 61, TC(X;Y\_j): 0.048  
61:term,long,medium,short,sized,mid,beginning,remainder,haul,nigger  
Group num: 62, TC(X;Y\_j): 0.046  
62:high,commissioner,level,ranking,tech,sin,leonard,wan,bump,jam  
Group num: 63, TC(X;Y\_j): 0.045  
63:with,regard,dealing,deal,dealt,conformity,connection,line,associated,conjunction  
Group num: 64, TC(X;Y\_j): 0.043  
64:special,rapporteur,rapporteurs,decolonization,envoy,myanmar,visit,colonialism,visits,visiting  
Group num: 65, TC(X;Y\_j): 0.039  
65:information,site,web,available,exchange,online,sites,readily,accessible,disseminate  
Group num: 66, TC(X;Y\_j): 0.037  
66:efforts,role,strengthen,towards,progress,strengthening,played,comprehensive,reform,implement  
Group num: 67, TC(X;Y\_j): 0.036  
67:freedom,integrity,expression,sovereignty,disputes,settlement,territorial,dispute,independence,belief  
Group num: 68, TC(X;Y\_j): 0.033  
68:report,note,present,periodic,takes,introduction,questions,detailed,hrc,endorses  
Group num: 69, TC(X;Y\_j): 0.032  
69:environmental,technologies,strategies,programmes,systems,quality,knowledge,indicators,tools,frameworks

Group num: 70, TC(X;Y<sub>j</sub>): 0.031  
 70: east, middle, north, west, sahara, western, near, atlantic, hills, lawn  
 Group num: 71, TC(X;Y<sub>j</sub>): 0.029  
 71: measures, taken, steps, eliminate, combat, combating, preventive, corruption, preven  
 ting, anti  
 Group num: 72, TC(X;Y<sub>j</sub>): 0.026  
 72: government, people, s, proposed, space, proposal, outer, additional, foreign, uses  
 Group num: 73, TC(X;Y<sub>j</sub>): 0.026  
 73: service, insurance, higher, professional, lower, pension, employees, providers, fees, ca  
 reer  
 Group num: 74, TC(X;Y<sub>j</sub>): 0.025  
 74: contract, contracts, contractual, travel, salary, categories, allowance, salaries, categor  
 y, temporary  
 Group num: 75, TC(X;Y<sub>j</sub>): 0.024  
 75: many, difficulties, despite, problem, faced, causes, face, remains, recent, decades  
 Group num: 76, TC(X;Y<sub>j</sub>): 0.024  
 76: policies, institutional, framework, approaches, promoting, stakeholders, issues, initia  
 tives, improving, mechanisms  
 Group num: 77, TC(X;Y<sub>j</sub>): 0.022  
 77: water, sanitation, assessments, sound, environmentally, logistics, base, electricity, dri  
 nking, assessment  
 Group num: 78, TC(X;Y<sub>j</sub>): 0.022  
 78: executive, director, secretariat, meetings, bureau, sessions, administrator, consultati  
 on, preparation, steering  
 Group num: 79, TC(X;Y<sub>j</sub>): 0.019  
 79: vulnerable, groups, poor, living, housing, marginalized, affected, increasing, socially, u  
 nemployment  
 Group num: 80, TC(X;Y<sub>j</sub>): 0.019  
 80: posts, cost, post, expenditure, overall, infrastructure, expected, operational, external,  
 savings  
 Group num: 81, TC(X;Y<sub>j</sub>): 0.018  
 81: delegations, conference, speakers, forthcoming, debate, consensus, convening, discus  
 sions, advance, intend  
 Group num: 82, TC(X;Y<sub>j</sub>): 0.017  
 82: so, do, what, doing, cannot, precisely, lose, afford, sight, reason  
 Group num: 83, TC(X;Y<sub>j</sub>): 0.017  
 83: official, sent, languages, issued, press, circular, interpreters, gazette, written, received  
 Group num: 84, TC(X;Y<sub>j</sub>): 0.016  
 84: areas, rural, policy, advocacy, partners, participatory, capacities, makers, decentraliza  
 tion, integration  
 Group num: 85, TC(X;Y<sub>j</sub>): 0.016  
 85: but, only, they, exist, nevertheless, theory, properly, confined, reversed, picking  
 Group num: 86, TC(X;Y<sub>j</sub>): 0.015  
 86: attention, drawn, paid, drew, paying, draws, amazing  
 Group num: 87, TC(X;Y<sub>j</sub>): 0.015  
 87: some, can, often, difficult, while, seen, way, both, become, far

Group num: 88, TC(X;Y\_j): 0.015  
88:on,basis,follow,forum,ministerial,outcome,conferences,intergovernmental,thematic,concentrate  
Group num: 89, TC(X;Y\_j): 0.015  
89:advisory,expert,budgetary,biennium,independent,cop,experts,cp,biennial,unfccc  
Group num: 90, TC(X;Y\_j): 0.014  
90:its,expresses,mandate,reiterates,appreciation,expressing,endorsed,reiterated,expeditiously,literature  
Group num: 91, TC(X;Y\_j): 0.014  
91:damage,caused,loss,suffered,administering,power,causing,cause,lost,compensate  
Group num: 92, TC(X;Y\_j): 0.014  
92:functions,duties,perform,powers,conduct,function,responsible,statutory,performing,confidentiality  
Group num: 93, TC(X;Y\_j): 0.014  
93:achieve,achieving,process,goal,achievement,transparency,accountability,contribute,transparent,achieved  
Group num: 94, TC(X;Y\_j): 0.013  
94:may,approval,specified,rules,notification,decide,prior,reference,listed,receipt  
Group num: 95, TC(X;Y\_j): 0.011  
95:case,applicable,type,applied,prescribed,limits,applies,defined,specify,partial  
Group num: 96, TC(X;Y\_j): 0.011  
96:between,relationship,link,distinguish,exchanges,conflicting,devil,derek,tooth,crying  
Group num: 97, TC(X;Y\_j): 0.011  
97:once,again,come,back,go,mere,never,thing,tell,says  
Group num: 98, TC(X;Y\_j): 0.010  
98:increase,increased,services,low,urban,coverage,skills,remote,volunteers,generating  
Group num: 99, TC(X;Y\_j): 0.010  
99:develop,needs,enhance,improve,key,addressing,assist,objectives,facilitate,strengthened  
Group num: 100, TC(X;Y\_j): 0.010  
100:documents,records,documentation,copies,translation,printed,page,pages,certified,versions  
Group num: 101, TC(X;Y\_j): 0.010  
101:cross,reducing,significantly,across,reduce,red,gap,cutting,greater,pace  
Group num: 102, TC(X;Y\_j): 0.009  
102:circumstances,obligation,principle,respect,existence,contrary,considers,distinction,constitute,accept  
Group num: 103, TC(X;Y\_j): 0.009  
103:sector,sectors,levels,projects,reduction,enabling,structural,grants,incentives,learning  
Group num: 104, TC(X;Y\_j): 0.009  
104:public,private,finances,municipalities,offering,publicity,branches,besides,treasure  
Group num: 105, TC(X;Y\_j): 0.008



105:after,days,payment,until,weeks,except,exceeding,exceed,termination,suspended  
Group num: 106, TC(X;Y\_j): 0.008  
106:their,themselves,respective,concern,following,deep,especially,approved,others,  
recognized  
Group num: 107, TC(X;Y\_j): 0.008  
107:adopted,l,orally,unanimously,addition,barbados,frank  
Group num: 108, TC(X;Y\_j): 0.008  
108:property,compensation,residence,sale,proceeds,intellectual,permits,ownership,  
restitution,deed  
Group num: 109, TC(X;Y\_j): 0.008  
109:approach,effectiveness,potential,needed,identify,existing,priority,identified,ass  
ess,identifying  
Group num: 110, TC(X;Y\_j): 0.008  
110:dialogue,understanding,reached,constructive,memorandum,fruitful,participate,  
restricted,tripartite,unknown  
Group num: 111, TC(X;Y\_j): 0.006  
111:by,followed,accompanied,guided,governed,supplemented,backed,thereafter,env  
elope  
Group num: 112, TC(X;Y\_j): 0.006  
112:question,without,determination,matter,unilateral,centre,prejudice,proceed,ans  
wer,resolved  
Group num: 113, TC(X;Y\_j): 0.006  
113:time,required,point,organized,points,observed,delays,frame,terms,uncertainty  
Group num: 114, TC(X;Y\_j): 0.006  
114:population,food,cities,hunger,ageing,wfp,madrid,launched,bridge,repercussions  
Group num: 115, TC(X;Y\_j): 0.006  
115:authority,competent,inspections,strict,comply,verify,complying,purposes,seabe  
d,discovery  
Group num: 116, TC(X;Y\_j): 0.006  
116:one,two,hand,divided,fall,waiting,expense,rob,writes,fame  
Group num: 117, TC(X;Y\_j): 0.006  
117:such,headquarters,deputy,means,types,assistant,adviser,coordinator,nature,liai  
son  
Group num: 118, TC(X;Y\_j): 0.005  
118:un,ece,discussion,paper,presentation,delegates,subsidiary,cefact,ensuing,doc  
Group num: 119, TC(X;Y\_j): 0.005  
119:effective,better,ensuring,effectively,create,making,best,creating,objective,encou  
rage  
Group num: 120, TC(X;Y\_j): 0.005  
120:access,local,land,safe,trained,inadequate,provinces,districts,aid,councils  
Group num: 121, TC(X;Y\_j): 0.005  
121:threat,threats,attempt,immediate,regime,annual,commit,threatened,pose,refrai  
n  
Group num: 122, TC(X;Y\_j): 0.005  
122:if,implementation,then,unless,limit,pass,escape,exact,discovered,sit  
Group num: 123, TC(X;Y\_j): 0.005

123:including,and,assistance,rehabilitation,establishment,fields,withdrawn  
Group num: 124, TC(X;Y\_j): 0.004  
124:community,supported,fully,leadership,strongly,supports,called,renewed,urgent  
ly,pillar  
Group num: 125, TC(X;Y\_j): 0.004  
125:where,a,generally,rather,similar,sometimes,longer,difference,consequence,beco  
mes  
Group num: 126, TC(X;Y\_j): 0.004  
126:among,growing,increasingly,encouraging,helped,help,helping,active,things,frien  
dly  
Group num: 127, TC(X;Y\_j): 0.004  
127:down,known,laid,behind,leads,constant,run,exit,allowing,fairly  
Group num: 128, TC(X;Y\_j): 0.003  
128:resources,core,mandates,plan,utilization,field,enhancement,utilize,genetic,unde  
rtaken  
Group num: 129, TC(X;Y\_j): 0.003  
129:september,november,york,event,cmp  
Group num: 130, TC(X;Y\_j): 0.003  
130:promote,through,practices,encourages,aims,reinforce,met,complemented  
Group num: 131, TC(X;Y\_j): 0.003  
131:matters,entitled,deployment,thousands,deployed,strength,status,start,direction,  
driven  
Group num: 132, TC(X;Y\_j): 0.003  
132:units,facilities,consider,includes,operation,views,made,activity,formed,owned  
Group num: 133, TC(X;Y\_j): 0.003  
133:charge,parent,charged,certificate,award,admission,german,admitted,awarded,a  
wards  
Group num: 134, TC(X;Y\_j): 0.003  
134:place,put,which,turn,mention,conceived,assumed  
Group num: 135, TC(X;Y\_j): 0.003  
135:impact,adverse,processes,fishing,mitigate,fish,migratory,capabilities,catch,com  
plement  
Group num: 136, TC(X;Y\_j): 0.002  
136:seminar,ngo,chaired,briefings,hosted,dpi,symposium,ababa,addis,fellowship  
Group num: 137, TC(X;Y\_j): 0.002  
137:review,conclusions,reviewing,substantive,appraisal,revise,thorough,severe,isol  
ated,fabric  
Group num: 138, TC(X;Y\_j): 0.002  
138:in,context,elements  
Group num: 139, TC(X;Y\_j): 0.002  
139:value,example,affairs,likely,risks,combination,depends,easily,flexible,real  
Group num: 140, TC(X;Y\_j): 0.002  
140:administrative,officer,appointment,free,subsequent,issuance,appointments,prel  
iminary,branch,zones  
Group num: 141, TC(X;Y\_j): 0.002

141:energy,options,current,input,stocks,renewable,meet,reply,mentioned,geographical  
Group num: 142, TC(X;Y\_j): 0.002  
142:country,particularly,section,leaders,continues,recently,bringing,notably,pursued,ties  
Group num: 143, TC(X;Y\_j): 0.002  
143:office,ohchr,communications,library,affiliated,desk,center,advisor,fresh  
Group num: 144, TC(X;Y\_j): 0.002  
144:agreed,proposals,discussed,further,modalities,reflected,implications,outlined,registered,immigration  
Group num: 145, TC(X;Y\_j): 0.002  
145:up,collaboration,unicef,outcomes,before,drawing,exception,foundation,explanation,clusters  
Group num: 146, TC(X;Y\_j): 0.002  
146:prevent,border,borders,crossing,stolen,synthesis,recovering,pep  
Group num: 147, TC(X;Y\_j): 0.002  
147:lack,owing,insufficient,receiving,seeking,furthermore,lacking,formal,sought,problematic  
Group num: 148, TC(X;Y\_j): 0.002  
148:along,values,lines,displacement,moving,deterioration,governing,steady,shape,pressures  
Group num: 149, TC(X;Y\_j): 0.002  
149:decisions,organs,principal,entrusted,organ,appoint,demonstration,tend,chain,coupled  
Group num: 150, TC(X;Y\_j): 0.002  
150:subject,separate,examination,incorporated,body,initial,covered,examined,settlements,mentioned  
Group num: 151, TC(X;Y\_j): 0.002  
151:commission,adoption,different,conf,limited,degree,operate,multiple,routine,beneficiary  
Group num: 152, TC(X;Y\_j): 0.002  
152:rev,washington,crp,dc,placed,ceremony,requires,ensured,forming,tom  
Group num: 153, TC(X;Y\_j): 0.001  
153:no,strategic,contribution,contributed,symbols,pub,ya  
Group num: 154, TC(X;Y\_j): 0.001  
154:system,based,response,recovery,availability,pool,observing  
Group num: 155, TC(X;Y\_j): 0.001  
155:list,date,send,deadline,aim,shortly,advised,nominated,postponed,sphere  
Group num: 156, TC(X;Y\_j): 0.001  
156:contributions,outstanding,protected,choice,consolidated,exclusive,acquire,abandoned,belong  
Group num: 157, TC(X;Y\_j): 0.001  
157:about,suffer,continental,intervention,severely,gc,kinds,shelf,every,disproportionate  
Group num: 158, TC(X;Y\_j): 0.001  
158:position,same,voting,seats,none,passing,reserved,having,yes,discharged

Group num: 159, TC(X;Y\_j): 0.001  
 159:recommendations,recommended,rest,search  
 Group num: 160, TC(X;Y\_j): 0.001  
 160:work,tasks,coordinators,removed,relative,appears,upcoming,settled,noticed  
 Group num: 161, TC(X;Y\_j): 0.001  
 161:direct,indirect,handle,reveals,distress,comfortable,turns  
 Group num: 162, TC(X;Y\_j): 0.001  
 162:he,factors,delegate,designed,effects,wrote,suited,adapted,samuel,incorporating  
 Group num: 163, TC(X;Y\_j): 0.001  
 163:observer,observers  
 Group num: 164, TC(X;Y\_j): 0.001  
 164:signed,honour,acting,bahamas,dependent,accurate,sensitivity,anthony,deficiencies,phillip  
 Group num: 165, TC(X;Y\_j): 0.001  
 165:thus,stage,thought,attitude,reflection,proves,anywhere,mistaken  
 Group num: 166, TC(X;Y\_j): 0.001  
 166:own,always,remain,unable,seriously,pay,equally,assume,giving,trying  
 Group num: 167, TC(X;Y\_j): 0.001  
 167:various,primary,objection,advantage,offered,stages,created,sensitive,linked,relationships  
 Group num: 168, TC(X;Y\_j): 0.001  
 168:participants,round,participant,eclac,ends,dark  
 Group num: 169, TC(X;Y\_j): 0.001  
 169:produce,single,simple,measure,render,permitting,typical,replacing,leaves,instant  
 Group num: 170, TC(X;Y\_j): 0.001  
 170:together,bring,populations,continuing,renewal,dire,willingness,goose  
 Group num: 171, TC(X;Y\_j): 0.001  
 171:jointly,seminars,organizing,interactive,sponsored,lectures,intact  
 Group num: 172, TC(X;Y\_j): 0.001  
 172:when,allowed,justified,satisfied,solely,questioned,exactly,aside,thoroughly,entirely  
 Group num: 173, TC(X;Y\_j): 0.001  
 173:unep,part,pops  
 Group num: 174, TC(X;Y\_j): 0.001  
 174:them,responsibility,series,autonomy,rests,usa,summarized,realm,cos  
 Group num: 175, TC(X;Y\_j): 0.000  
 175:organizational,workshop,unido,topics,danger,stop,consultant,idb,committees,disturbed  
 Group num: 176, TC(X;Y\_j): 0.000  
 176:co,possibility,character,dr,bound,affect,bear,advisers,explicit,proper  
 Group num: 177, TC(X;Y\_j): 0.000  
 177:concerning,regarding,attached,replied,launch,biggest  
 Group num: 178, TC(X;Y\_j): 0.000  
 178:conditions,participated,escap,bangkok,creates,entails,star  
 Group num: 179, TC(X;Y\_j): 0.000

179:providing,implemented,beneficiaries,facilitates,tailored,channels  
 Group num: 180, TC(X;Y\_j): 0.000  
 180:duty,makes,condition,allows,regardless,choose,irrespective,chosen,govern,weekend  
 Group num: 181, TC(X;Y\_j): 0.000  
 181:throughout,reintegration,engaged,intensified,resettlement,restoring,demonstrating,tactics  
 Group num: 182, TC(X;Y\_j): 0.000  
 182:physical,next,acquired,agents,aligned,destination,documented,timetable,occurrence,recognise  
 Group num: 183, TC(X;Y\_j): 0.000  
 183:maintenance,balance,reflects,seeks,economically,referendum,reliance,saving,sophisticated,assumptions  
 Group num: 184, TC(X;Y\_j): 0.000  
 184:aimed,eliminating,month,thrust  
 Group num: 185, TC(X;Y\_j): 0.000  
 185:new,newly,host,stating,wasting  
 Group num: 186, TC(X;Y\_j): 0.000  
 186:majority,absolute,occurring,virtually,poorly,finalized,tough,string  
 Group num: 187, TC(X;Y\_j): 0.000  
 187:leave,normal,obliged,display,piece,motive  
 Group num: 188, TC(X;Y\_j): 0.000  
 188:treated,differently,qualify,altogether,relax  
 Group num: 189, TC(X;Y\_j): 0.000  
 189:draw,extended,correspondence,devote,twelve,contacted,photographs,sixteen,photograph,courtesy  
 Group num: 190, TC(X;Y\_j): 0.000  
 190:consolidation,facilitated,contacts,unified,launching  
 Group num: 191, TC(X;Y\_j): 0.000  
 191:unesco,unodc,usual  
 Group num: 192, TC(X;Y\_j): 0.000  
 192:notwithstanding,instances  
 Group num: 193, TC(X;Y\_j): 0.000  
 193:times,falling,pressed  
 Group num: 194, TC(X;Y\_j): 0.000  
 194:define,tokyo,removing,victoria  
 Group num: 195, TC(X;Y\_j): 0.000  
 195:cooperative,hosting,inspectors  
 Group num: 196, TC(X;Y\_j): -0.000  
 196:finalize  
 Group num: 197, TC(X;Y\_j): -0.000  
 197:  
 Group num: 198, TC(X;Y\_j): -0.000  
 198:  
 Group num: 199, TC(X;Y\_j): -0.000  
 199:inspectors,falls,sunset,hosting

# Symbols, Abbreviations, and Acronyms

S – Surprise

TC – Total Correlation

$D_{Ref}$  - Reference dataset

$D_{Test}$  - Test dataset

$\alpha$  - mixing parameter

*CorEx* – Correlation Explanation

OS - OpenSubtitles2015 dataset

Mun - MultiUN dataset

MT - Machine Translation