

AFRL-AFOSR-VA-TR-2016-0106

Scalable High-order Methods for Multi-Scale Problems Analysis, Algorithms, and Applications

Mark Ainsworth BROWN UNIVERSITY IN PROVIDENCE IN STATE OF RI AND PROVIDENCE PLANTATIONS

02/26/2016 Final Report

DISTRIBUTION A: Distribution approved for public release.

Air Force Research Laboratory AF Office Of Scientific Research (AFOSR)/ RTA2 Arlington, Virginia 22203 Air Force Materiel Command

REPORT DOCUMENTATION PAGE				Form Approved OMB No. 0704-0188				
The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing the burden, to the Department of Defense, Executive Service Directorate (0704-0188). Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.								
1. REPORT DA	TE (DD-MM-YY)	YY) 2. REPO	RT TYPE			3. DATES COVERED (From - To)		
	Final Report				9/30/12-11/29/16			
4. TITLE AND S	TITLE AND SUBTITLE 5a. Co			5a. CON	ITRACT NUMBER			
Application	order wiethous to	i Multi-scale i lot	Jenis. Analysis, Algorit	nins and				
rippiloution					5b. GRANT NUMBER			
						FA9550-12-1-0463		
					5c. PRO	GRAM ELEMENT NUMBER		
6. AUTHOR(S) George Karniad	akis				5d. PRO	DJECT NUMBER		
0001901100					5e. TAS	KNUMBER		
l								
l					5f. WOR	5f. WORK UNIT NUMBER		
7. PERFORMIN	IG ORGANIZATI	ON NAME(S) AN	D ADDRESS(ES)			8. PERFORMING ORGANIZATION		
Brown Universit	ity					REFORT NOMBER		
Applied Mather	natics							
Providence RI	02912							
9. SPONSORIN		GAGENCY NAME	E(S) AND ADDRESS(ES	5)		10. SPONSOR/MONITOR'S ACRONYM(S)		
AFOSR				,		+ FOSD		
801 N. Randolp	h Street					AFOSR		
Arlington, VA	22203					11. SPONSOR/MONITOR'S REPORT		
						NUMBER(S)		
12. DISTRIBUTI	ON/AVAILABILI	TYSTATEMENT						
Approved for P	ublic Release, Di	istribution Unlimi	ted					
13. SUPPLEME	NTARY NOTES							
14. ABSIRACI	that in future go	norations of mass	ively perallel computer	systems a signif	Ficant norti	on of processors may suffer from hardware or		
software faults	rendering large-s	scale computation	s useless. In this project	t the PI and his	students ac	ddress this problem from the algorithmic side		
proposing resilient frameworks that can recover and continue the solution with gappy fields from such faults irrespective of their fault origin. In								
addition to its r	obustness and re	silience, the new	framework generalizes p	previous multisc	ale and mu	ultifidelity approaches in a unified parallel		
computational f	framework.							
15. SUBJECT T	ERMS							
Fault-resilient r	nethod, multifide	enty simulation, d	omain accomposition, C	лер, gappy data	i, estimatio	on theory, and gap-tooth algorithm.		
16. SECURITY	6. SECURITY CLASSIFICATION OF: 2. BEPORT IN ARSTRACT OF 17. LIMITATION OF 18. NUMBER ABSTRACT OF		19a. NAME OF RESPONSIBLE PERSON George Karniadakis					
	S. ABOTINACT	S. THIST AGE	PAG	PAGES	19h TEL			
UU	UU	UU	UU			401-863-1217		
	-				•	Standard Form 298 (Rev. 8/98)		
		DIS	TRIBUTION A: Distributi	on approved for	public rele	Prescribed by ANSI Std. Z39.18 Adobe Professional 7.0		

INSTRUCTIONS FOR COMPLETING SF 298

1. REPORT DATE. Full publication date, including day, month, if available. Must cite at least the year and be Year 2000 compliant, e.g. 30-06-1998; xx-06-1998; xx-xx-1998.

2. REPORT TYPE. State the type of report, such as final, technical, interim, memorandum, master's thesis, progress, quarterly, research, special, group study, etc.

3. DATES COVERED. Indicate the time during which the work was performed and the report was written, e.g., Jun 1997 - Jun 1998; 1-10 Jun 1996; May - Nov 1998; Nov 1998.

4. TITLE. Enter title and subtitle with volume number and part number, if applicable. On classified documents, enter the title classification in parentheses.

5a. CONTRACT NUMBER. Enter all contract numbers as they appear in the report, e.g. F33615-86-C-5169.

5b. GRANT NUMBER. Enter all grant numbers as they appear in the report, e.g. AFOSR-82-1234.

5c. PROGRAM ELEMENT NUMBER. Enter all program element numbers as they appear in the report, e.g. 61101A.

5d. PROJECT NUMBER. Enter all project numbers as they appear in the report, e.g. 1F665702D1257; ILIR.

5e. TASK NUMBER. Enter all task numbers as they appear in the report, e.g. 05; RF0330201; T4112.

5f. WORK UNIT NUMBER. Enter all work unit numbers as they appear in the report, e.g. 001; AFAPL30480105.

6. AUTHOR(S). Enter name(s) of person(s) responsible for writing the report, performing the research, or credited with the content of the report. The form of entry is the last name, first name, middle initial, and additional qualifiers separated by commas, e.g. Smith, Richard, J, Jr.

7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES). Self-explanatory.

8. PERFORMING ORGANIZATION REPORT NUMBER. Enter all unique alphanumeric report numbers assigned by the performing organization, e.g. BRL-1234; AFWL-TR-85-4017-Vol-21-PT-2.

9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES). Enter the name and address of the organization(s) financially responsible for and monitoring the work.

10. SPONSOR/MONITOR'S ACRONYM(S). Enter, if available, e.g. BRL, ARDEC, NADC.

11. SPONSOR/MONITOR'S REPORT NUMBER(S). Enter report number as assigned by the sponsoring/ monitoring agency, if available, e.g. BRL-TR-829; -215.

12. DISTRIBUTION/AVAILABILITY STATEMENT. Use agency-mandated availability statements to indicate the public availability or distribution limitations of the report. If additional limitations/ restrictions or special markings are indicated, follow agency authorization procedures, e.g. RD/FRD, PROPIN, ITAR, etc. Include copyright information.

13. SUPPLEMENTARY NOTES. Enter information not included elsewhere such as: prepared in cooperation with; translation of; report supersedes; old edition number, etc.

14. ABSTRACT. A brief (approximately 200 words) factual summary of the most significant information.

15. SUBJECT TERMS. Key words or phrases identifying major concepts in the report.

16. SECURITY CLASSIFICATION. Enter security classification in accordance with security classification regulations, e.g. U, C, S, etc. If this form contains classified information, stamp classification level on the top and bottom of this page.

17. LIMITATION OF ABSTRACT. This block must be completed to assign a distribution limitation to the abstract. Enter UU (Unclassified Unlimited) or SAR (Same as Report). An entry in this block is necessary if the abstract is to be limited.

FINAL REPORT: Scalable High-order Methods for Multi-scale Problems: Analysis, Algorithms and Applications AFOSR Grant Number:FA9550-12-1-0463

George Em Karniadakis

Division of Applied Mathematics Brown University

Abstract

It is anticipated that in future generations of massively parallel computer systems a significant portion of processors may suffer from hardware or software faults rendering large-scale computations useless. In this project, the PI and his students address this problem from the algorithmic side, proposing resilient frameworks that can recover and continue the solution with gappy fields from such faults irrespective of their fault origin. In addition to its robustness and resilience, the new framework generalizes previous multiscale and multifidelity approaches in a unified parallel computational framework.

Objectives

The general objective of this project was to develop a general CFD framework for multifidelity simulations to target multiscale problems but also resilience in exascale simulations. The specific objective was to develop a fault-recovery and fault-resilient algorithm using approximation theory, domain decomposition, and machine learning based information-fusion together.

Approach

Fault-recovery algorithm

We employ three different types of recovery algorithms, namely (1) projective integration (temporal estimation), (2) coKriging (spatial estimation), and (3) resimulation (spatio-temporal estimation). We introduce the concepts of the three approaches briefly next, for detail see (S. Lee et al. 2015).

First, if numerical solutions are sufficiently smooth in time, the temporal estimation based on previous saved data can give a highly accurate result on a missing part of the solution. To accomplish this, we employ an equation-free/Galerkin-free projective integration. The projective integration is based on the proper orthogonal decomposition (POD) for a dimension reduction. The basic algorithm of the projective integration consists of three stages: the restriction (a dimension reduction by POD), estimation (of the coefficient for the POD basis), and lifting (a reconstruction of the gappy field).

While for the temporal estimation we use the previous flow field data and smoothness in time, in the spatial estimation we need to use geometrically neighboring data points at the current time to exploit smoothness in space. In this project, a "multi-fidelity coKriging interpolation method", the unbiased linear interpolation, is introduced for estimating the missing part.

The "resimulation" method is employed to solve the Navier-Stokes equations again on the missing part only with estimated initial condition (by the coKriging) and estimated field variables at the boundary (by the projective integration), see Figure 1.

Preprint submitted to AFOSR FINAL REPORT

February 15, 2016



Figure 1: "Re-simulation" with estimated boundary condition: First, we estimate the initial condition for the missing part (blue) with two sample sets: refined (orange) and coarse (red). Subsequently, we use the projective integration to update the boundary using the refined sample set. Finally, we solve the Navier-Stokes equation in the missing part only.

Fault-resilient algorithm – Gappy simulation

In the gappy simulation framework, we compute explicitly the solution to a PDE not on the entire domain but only partially on some sub-domains with some auxiliary data that span the entire domain and obtained independently. The main idea is to combine the global coarse information with some finely resolved sub-domains and appropriately combine the two solutions to obtain a more accurate solution on the entire domain. This set up admits two different interpretations. From the multiscale perspective, the global coarse solution represents the large scales whereas the fine-resolution sub-domains represent regions of finer scales. The gappy regions may also be regions of finer scales but with spatial correlations determined by the resolved regions. From the parallel computing perspective, the gappy sub-domains may be regions corrupted by random software or hardware faults whereas the global coarse solution is obtained on an independent small set of processors, which is assumed to be immune to such faults that the big computer system may suffer from.

A flow chart of the gappy simulation is shown in Figure 2. First, upon notification of a fault detection (not discussed here), we check which domains are affected by errors, and define computational subdomains and gaps, respectively. Next, we choose a proper buffer size, and the gappy simulation estimates the fields at the local boundaries of each subdomain by the information fusion method using also the independent auxiliary data. After setting-up all the parameters and variables, the gappy simulation solves each subdomains on independent nodes during non-interaction time steps τ . After time τ , all subdomains are re-joined together and the buffer region of each subdomain is cut-off. Finally, using the auxiliary data, the new field variables at the boundaries can be updated via coKriging. The gappy simulation repeats again this procedure until the main simulation ends or all faults are fixed.

Main Results

The first main algorithmic result of this project is the reconstruction of missing data using three different approaches according to three fault scenarios. These lead to a robust and effective recovered solution in various fault scenarios. We have also developed the fault-resilient CFD algorithm in a unified parallel computational framework. Combining approximation theory and domain decomposition together with machine learning techniques, this results in robustness and resilience with low-resolution auxiliary data. We highlight some of the simulation results next.



Figure 2: A flow chart for a gappy simulation (start from left-top): We first check where the gappy domains are located. Next, we choose a buffer size and estimate field variables at local boundaries. Each sub-domain is solved in parallel and independently during non-interaction time τ . After τ , all gappy domains are re-joined together after cutting-off the buffer region. Finally, using information fusion method with auxiliary data, all field variables are updated at the local boundaries of the subdomains. This is one complete cycle of the gappy simulation algorithm.

Fault-recovery Simulations

We present results for two benchmark problems – a lid-driven cavity flow (quasi-steady) and a flow past a cylinder (quasi-periodic), for details see (Lee et al, 2015). To this end, we consider three types of available fault scenarios: (1) a gappy region but with no previous gaps and no contamination of surrounding simulation data, (2) a space-time gappy region but with full spatiotemporal information and no contamination, and (3) previous gaps with contamination of surrounding data. To recover from such faults, we employ different reconstruction and simulation methods, namely the projective integration, the co-Kriging interpolation, and the resimulation method. The results with respect to RMS error and capability are shown in Tables 1 and 2. We summarize here the main findings of our study:

- For sufficiently small time gaps, the projective integration method is the best while for longer time gaps the co-Kriging method is better.
- Overall, the "resimulation" method seems to be the most robust method, performing well in all three fault scenarios.
- Estimating the boundary condition using projective integration leads to accurate results for the "resimulation" method in scenario 3 where the other two methods fail.

Fault-resilient Simulations

We apply our fault-resilient framework to the heat equation and the Navier-Stokes equations, and obtain important first results via a parametric study. Specifically, we employ the finite difference method to perform

Velocity	Time gaps (ΔT_g)	Scenario	P.I.	CoKriging	Resimulation
streamwise	0.5	1	0.0044	0.0136	0.0075
		2		0.0136	0.0074
		3			0.0078
	1.0	1	0.0156	0.0150	0.0124
		2		0.0150	0.0122
		3			0.0158
crossflow	0.5	1	0.0007	0.0177	0.0060
		2		0.0177	0.0059
		3			0.0088
	1.0	1	0.0116	0.0192	0.0108
		2		0.0192	0.0106
		3			0.0105

 Table 1: Comparison of RMS error for three different methods in lid-driven cavity flow. "-" represent inability for corresponding scenario.

Table 2: Comparison of RMS error for three different methods in flow past a circular cylinder. "-" represent inability for corresponding scenario.

Velocity	Time gaps (ΔT_g)	Scenario	P.I.	CoKriging	Resimulation
streamwise	0.27	1	0.0039	0.0219	0.0060
		2		0.0219	0.0172
		3			0.0175
	0.47	1	0.0193	0.0251	0.0144
		2		0.0251	0.0235
		3			0.0291
crossflow	0.27	1	0.0046	0.0178	0.0065
		2		0.0178	0.0168
		3			0.0189
	0.47	1	0.0231	0.0159	0.0149
		2		0.0159	0.0241
		3			0.0374



Figure 3: Time history of the RMS error in the heat equation with different parameters. In (a), a fixed parameters is τ =1. In (b), fixed parameters are the buffer=30% and the auxiliary data=6 × 6 grid.

a gappy simulation in both benchmark problems. The gappy domains looks like a checker board, see Figure 2. We observe that the RMS error of all test simulations are converging to zero at steady-state. Moreover, we investigate the key parameters of this framework: 1) type of correlation kernel, 2) size of buffer, 3) accuracy of auxiliary data, and 4) non-interaction time, τ . The results of our parametric study are shown in Figure 3 and 4. We summarize here the main findings of our study below:

- *Kernel*: the Matérn kernel is found to be the best kernel with respect to RMS error and stability in both problems.
- *Buffer*: the bigger buffer can guarantee the smaller RMS error in both problems because the error at the local boundary can be diffused in a buffer region. Moreover, as the auxiliary data is inaccurate or auxiliary data may not be available, the size of buffer enhances the effectiveness in this framework.
- *Auxiliary data*: the finer resolution auxiliary data gives the smaller RMS error in both problems because of increasing accuracy of results by information fusion. As shown in Figure 3 and 4, the accuracy of auxiliary data is found to be the most important parameter to reduce the RMS error effectively.
- *Non-interaction time* (τ): In the heat equation (only diffusion), near the *allowable* τ , calculated by the estimation of a penetration length for a diffusion, we can guarantee the smaller RMS error. However, in the Navier-Stokes equations (combined diffusion and advection), the smaller τ (update boundary values more frequently) gives the smallest RMS error.

Acknowledgement/Disclaimer

This work was sponsored by the Air Force Office of Scientific Research, under grant/contract number FA9550-12-1-0463. The views and conclusions contained herein are those of the author and should not be interpreted as necessarily representing the official policies or endorsements, either expressed or implied, of the Air Force Office of Scientific Research or the U.S. Government.



Figure 4: Time history of the RMS error in a Naiver-Stokes equation with different parameters. In (a), fixed parameters are τ =5 and auxiliary data=8×8 grid. In (b), fixed parameters are the buffer = 25% and the τ =5. In (c) fixed parameters are the buffer=25% and the auxiliary data= 8×8 grid.

Personnel Supported During Duration of Grant

- Faculty: G. E. Karniadakis, The Charles Pitts Robinson and John Palmer Barstow Professor of Applied Mathematics, Brown University.
- PhD Student: Seungjoon Lee, Paris Perdikaris, Yu-Hang Tang, Brown University

Honors & Award

- Society for Industrial and Applied Mathematics, 2015, Ralph E Kleinman Award.
- US Association of Computational Mechanics, 2013, Tinsley Oden medal (inaugural)
- US Association of Computational Mechanics, 2007, Computational Fluid Dynamics award.
- Fellow of SIAM, 2011-.
- Fellow of the American Physical Society, 2004.
- Fellow of the American Society of Mechanical Engineers, 2003.
- Associate Editor of Journal of Computational Physics, 2005.

Publications

- 1. S. Lee, I.G. Kevrekidis and G.E. Karniadakis, "Resilient algorithms for reconstructing and simulating gappy flow fields in CFD", Fluid Dynamic Research, vol. 47, 051402, 2015.
- Y. Yu, H. Yan, Y. Constantinidis, O. Oakley and G.E. Karniadakis, "Suppression of vortex-induced vibrations by fairings: A numerical study", Journal of Fluid Structures, vol. 54, 679-700, 2015.
- Y. Yu, M. Bittencourt and G.E. Karniadakis, "A semi-local spectral/hp element solver for linear elasticity problems", International Journal for Numerical Methods in Engineering, vol. 10, 347-373, 2014.

Interactions/Transitions

The PI and his group had interaction with Prof. I.G. Kevrekidis (Princeton University) on issues related to the gappy simulations for the fault resilient algorithm and the projective integration method for the fault recovery approach.

1.

1. Report Type

Final Report

Primary Contact E-mail

Contact email if there is a problem with the report.

George_Karniadakis@brown.edu

Primary Contact Phone Number

Contact phone number if there is a problem with the report

4018631217

Organization / Institution name

Brown University/Division of Applie

Grant/Contract Title

The full title of the funded effort.

Scalable High-Order Methods for Multi-scale Problems: Analysis, Algorithms and Applications

Grant/Contract Number

AFOSR assigned control number. It must begin with "FA9550" or "F49620" or "FA2386".

FA9550-12-1-0463

Principal Investigator Name

The full name of the principal investigator on the grant or contract.

George Karniadakis

Program Manager

The AFOSR Program Manager currently assigned to the award

Jean-Luc Cambier

Reporting Period Start Date

09/30/2012

Reporting Period End Date

11/29/2016

Abstract

The first main algorithmic result of this project is the reconstruction of missing data using three different approaches according to three fault scenarios. These lead to a robust and effective recovered solution in various fault scenarios. We have also developed the fault-resilient CFD algorithm in a unified parallel computational framework. Combining approximation theory and domain decomposition together with machine

learning techniques, this results in robustness and resilience with low-resolution auxiliary data. We highlight some of the simulation results next.

Distribution Statement

This is block 12 on the SF298 form.

Distribution A - Approved for Public Release

Explanation for Distribution Statement

If this is not approved for public release, please provide a short explanation. E.g., contains proprietary information.

SF298 Form

Please attach your SF298 form. A blank SF298 can be found here. Please do not password protect or secure the PDF The maximum file size for an SF298 is 50MB. DISTRIBUTION A: Distribution approved for public release.

FA9550-12-2-0463_SF298.pdf

Upload the Report Document. File must be a PDF. Please do not password protect or secure the PDF. The maximum file size for the Report Document is 50MB.

FA9550_12_1_0463_FinalReport_GK.pdf

Upload a Report Document, if any. The maximum file size for the Report Document is 50MB.

Archival Publications (published) during reporting period:

Changes in research objectives (if any):

Change in AFOSR Program Manager, if any:

Extensions granted or milestones slipped, if any:

AFOSR LRIR Number

LRIR Title

Reporting Period

Laboratory Task Manager

Program Officer

Research Objectives

Technical Summary

Funding Summary by Cost Category (by FY, \$K)

	Starting FY	FY+1	FY+2
Salary			
Equipment/Facilities			
Supplies			
Total			

Report Document

Report Document - Text Analysis

Report Document - Text Analysis

Appendix Documents

2. Thank You

E-mail user

Feb 15, 2016 15:18:20 Success: Email Sent to: George_Karniadakis@brown.edu