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# ENGINEERING DESIGN HANDBOOK

# DESIGN OF AERODYNAMICALLY

STABILIZED FREE ROCKETS

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**JULY 1968** 

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### PREFACE

The Engineering Design Handbook Series of the Army Materiel Command is a coordinated series of handbooks containing basic information and fundamental data useful in the design and development of Army materiel and systems. The handbooks are authoritative reference books of practical information and quantitative facts helpful in the design and development of Army materiel so that it will meet the tactical and technical needs of the Armed Forces.

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This handbook provides extremely useful data for the engineer primarily interested in the preliminary design of aerodynamically stabilized free rockets. The data are arranged in a convenient format—tables, graphs, and solution guides—which permits ready access and easy application in order to make possible the rapid response required of preliminary design activities. As a bonus, the chapter arrangement provides each technical area having responsibilities in the preliminary design phase with an appreciation for the data requirements and applications of the supporting technical areas.

The preparation of this handbook was initially an in-house effort of the U. S. Army Missile Command. The organization of the text, data, and much of the written material originated with that agency The Chrysler Corporation Space Division, Huntsville, Alabama, under subcontract to the Engineering Handbook Office of Duke University, prime contractor to the Army Research Office-Durham for the Engineering Design Handbook Series—with the continues<sup>1</sup> assistance of the U. S. Army Missile Command—completed the handbook.

The Handbooks are readily available to all elements of AMC including personnel and contractors having a need and or requirement. The Army Materiel Command policy is to release these Engineering Design Handbooks to other DOD activities and their contractors, and other Government agencies in accordance with urrent Army Regulation 70-31, dated 9 September 1966. Procedures for acquiring these Handbooks follow

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Comments and suggestions on this handbook are welcome and should be addressed to Army Research Office-Durham, Box CM, Duke Station, North Carolina 27706.

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# CHAPTER 1

This handbook, written for the engineer interested in the preliminary design of aerodynamically stabilized free rockets, has a twofold purpose:

a. To provide the preliminary design engineer with specific, "best available" design information and data devised to allow the rapid response rcquired of preliminary design activities, and

b. To provide each technical area having responsibilities in the preliminary design phase an appreciation or "feel" for the data requirements and data applications of other specific technical areas.

The term free-flight rocket implies the absence of an active guidance system. Such a rocket is guided or aimed by a launching rail or tube and can be classified into one of two categories.

a. Spin-stabilized

b. Aerodynamically stabilized

The spin-stabilized rocket, as the name implies, depends upon a high rate of spin and resulting gyroscopic moments to oppose disturbing moments and forces. Conversely, the aerodynamically stabilized rocket depends upon the moments generated by a flare or fins placed aft of the center of gravity to oppose disturbing moments and forces. The aerodynamically stabilized rocket generally employs some spin history to minimize dispersion due to nonstandard conditions (body malalignment, fin malalignment, etc.). The data and concepts presented by this handbook are limited to aerodynamically stabilized free-flight rockets.

The rocket is assumed to be a rigid body, i.e., the elastic properties of the structure have been neglected. However, for some configurations (primarily long, slender bodies) the dynamic modes of oscillation may be of sufficient amplitude to warrant detailed investigations. Finally, there are three major propulsion systems that could be applicable:

a. liquid propellants

b. solid propellants

c. hybrid propellants (combination of liquid and solid)

The applications of this handbook are limited to solid-propellant motors, used almost exclusively in free-flight aerodynamically stabilized rockets.

The basic handbook is organized into chapters, each self-contained and applicable to a particular technical area with which preliminary design is concerned. These areas are: Atmospheric Data, Systems Design, Parametric Performance, Propulsion, Structures, Accuracy, and Aerodynamics.

Chapter 2, Atmospheric Data, presents climatological data pertinent to free rocket design. Chapter 3, Systems Design, discusses the factors affecting design, considering each technical area from preliminary design to actual hardware. Chapter 4. Parametric Performance, presents data describing the performance of various design concepts, with variations that permit consideration of trade-offs to maximize range for given mass or mass for given range. Chapter 5, Propulsion, presents concepts and data necessary to predict propulsion system performance, as well as important aspects to consider in conceptual and preliminary design. Chapter 6, Structures, presents data and methods pertinent to structural design. Chapter 7, Accuracy, considers both burning-phase and ballisticphase errors, the effect of these errors on rocket accuracy, and techniques necessary to estimate accuracy. Finally, Chapter 8, Aerodynamics, presents design curves and formulas that will permit the prediction of stability (force and moment) and drag characteristics for practically any conceivable aerodynamic body or combinations of bodies.

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# CHÀPTER 2 Atmospheric data

### 2-1 INTRODUCTION

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Atmospheric information is a very important consideration in the preliminary design of rockets, particularly those that are free-flight or uncontrolled after launch. Since atmospheric data are time- and space-dependent, and therefore widely variable, statistical processes are normally used for their presentation, analysis, and utilization.

Because some types of statistical data are subject to considerable controversy, one can hardly hope to develop standardized actual climatological data profiles, and perturbations to them, that will receive universal acceptance. Instead, meteorologists have developed synthetic standard profiles, independent of physical location. Means and extremes of these profiles were then developed, dependent upon rather general geographic location. Finally, models of microclimatological (localized) conditions can be accomplished to meet specific conditions.

In rocket design, the preluminary design phase is concerned primarily with macroclunatology (large-scale conditions). Density, temperature, and pressure profiles (variation of these factors with altitude) must be presented to the trajectory analyst so that configuration performance can be determined. Wind profiles and wind shear information are necessary for structural design as well as for accuracy studies. Finally, consideration of extreme conditions is necessary to ensure complete system integration and operation.

### 2-2 ATMOSPHERIC PROPERTIES

# 2-2.1 ATMOSPHERIC DENSITY, TEMPERATURE AND PRESSURE

The U. S. Standard Atmosphere (USSA) is based upon the International Civil Aviation Organization (ICAO) Standard Atmosphere to 20 km altitude, and upon the proposed ICAO extension from 20 km to 32 km. Data for the first 20 km are in agreement with the Air Research and Development Command (ARDC) 1959 Standard Atmosphere The major reason for revising standard atmospheres in recent years has been the observed orbit perturbations of artificial satchlites due to atmospheric drag. This subject is beyond the present scope of interest. See Reference 2 for complete tables.

Table 2-1 presents a useful summary of atmospheric properties taken from Reference 2.

### 2-2.2 WINDS, UPPER LEVEL

The problem of selecting wind profile information for use as design criteria led to development of an estimated synthetic profile which presented the 1 percent probable wind speed and associated shear at the must critical altitude, and speeds of other altitudes typical for such wind fields. Subsequent investigation revealed that, if accuracy in the calculated risk is desired, the use of synthetic wind profiles is hazardous. However, logically developed synthetic profiles are useful in preliminary design. Fig. 2.1 is a synthetic wind profile that was developed in 1954 to determine vehicle responses that would be exceeded during only 1 percent of the windiest season of the year in that area of the U.S. where tropospheric wind streams were considered the strongest. It is rea sonable to shift the curve upward or downward by as much as 5000 ft to make the peak wind speed coincide with the altitude of maximum wind influence.

Ideally, in missile design and accuracy studies. the designer must know mean wind velocity and standard deviation for both hemispheres. Table 2-2 gives the resultant wind direction, vector mean wind velocity and the standard vector deviation for the Northern hemisphere between 20°N and 80°N at altitudes from 10,000 to 100,000 ft for winter and summer.

See Reference 4, the Handbool. of Grophysics and Space Environments, 1965, Chapter 4, for the mean wind speed, standard deviation, and corre lation between levels for a series of altitudes for each vector component at specific stations during the winter season.

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	TADLE 2-1	. U. S. STANDA	RD ATMOSPI	HERE, 1802	
Geometric Altitude, km	Density, kg/m <sup>8</sup>	Temperature, °K	Pressure. N 'm <sup>s</sup>	Accel. of Gravity, m/sec <sup>2</sup>	Speed of Sound, mosec
0	1.2250	288 150	10325	9.8066	340.294
1	<u>i.1117</u>	281.651	89376. <b>2</b>	9.8036	336.435
â	1.0056	275.154	79501 4	9.3055	332.532
3	0.00025	268.059	70121.1	9.7974	328.583
4	0.81935	262.165	61630.4	9.7943	324.589
5	0.73643	255.676	54048.2	9.7912	320.545
6	0.65011	249.187	47217.6	9.7882	316.452
7	0.50002	242.700	41105.2	9 7851	312.306
8	0.52579	236.215	35651.6	9.7820	308.105
9	0.45705	229.733	30300 7	9 7789	303.848
10	0.41351	223.252	26499.9	9.7759	299.532
11	0.30450	21 <sup>R</sup> 774	22699.9	9.7728	295.154
12	0.31194	216.650	19399 4	9.7697	295.069
13	0.20000	216.650	16479.6	9.7667	295.059
14	0.22788	216.650	14170.4	9.7636	235.069
15	0.19475	216.650	12111.8	9.7605	295.069
. ن	0.16647	216.650	10352.8	9.7575	295.069
17	0.14230	216.650	8849.71	9.7544	295.069
18	0.12165	216.650	7565.22	9.7513	295.069
19	0.10400	216.650	6467.48	9.7483	295.069
20	0.038910	216.650	5529.30	9.7452	295.069
21	0.075715	217.531	4728.93	9.7422	295.703
22	0.064510	218.574	4047.49	9.7391	296.377
23	0.055006	219.557	3466.86	9.7361	297.049
24	0.010933	220.500	2971.74	9.7330	297.720
25	0.040034	221.552	2549.22	9.7300	298.389

### 2-2.3 WINDS, LOWER LEVEL

Chapter 4, Section 4.1 of Reference 4 contains information concerning mean wind as a function of height. This section gives approximate equations to compute the mean wind speed. It also gives information and tabulated data concerning wind-direction shifts and directional variation, and low-level jet streams.

Table 2-3 gives the number of years of record, mean, and standard deviation of the extreme wind speed at 50 ft above the ground for various stations in the northern hemisphere.

Fig. 2-2 shows the strongest wind for temperature range observed during a five-year period. Wind speeds are, in general, for 40 to 100 ft above the surface. Speeds at 10 feet are approximetely 80 percent of the values given, except for the coldest temperatures, where winds are 50 percent of the indicated values.

### 2-2.4 REGIONAL ANNUAL AND SEASONAL DENSITY MODELS

Evaluation of flight performance and rocket design necessarily includes the consideration of vertical distribution of atmospheric environment parameters. Our knowledge in this field has rapidly expanded beyond the status of a "Standard Atmospheric Model", which can only describe the atmospheric environment as a first approximation, under limited circumstances. In recognition of these limitations, the Committee on the Extension of the Standard Atmosphere (COESA) has recently adopted supplementary atmospheres (Reference 2).

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Maximum speed (300 ft sec <sup>2</sup>) and associated maximum chear (45 ft sec <sup>-1</sup> per 1000 ft) are likely to be exceeded only 1% of the wintertime over the northesstern USA. Wind speeds and shears at levels al. we and below the levels of maximum speed and shear are t, piral of those likely to be encountered for this 1% probability condition.

### Figure 2-1. Maximum Speed and Associated Shear

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These supplements to the standard atmosphere, although welcomed by the Jesign engineer, still cannot fully describe the status of the atmosphere and are not intended to do so. Besides having reference models of mean conditions, the designer needs information to describe the deviations from these preset models, usually in the form of some error function or standard deviations.

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It has been customary to assume a certain deviation, e.g., the plus-one-sign a threshold, at every height level, and then to connect these points from one level to the next. The resulting synthetic altitude relationship will be called here the plus-one signa envelope (to be disarguished from profiles). A.sc. constants, such a. a 3 percent deviation for density, have been utilized. Such an approach is very attractive because it compresses a large amount of statistical informauon into a few altitude curves. However, it completely ignores the artifude relationship of meteorological elements, which is admittedly complex and cannot be expressed in simple terms. Although it is logical to establish any probability threshold separately at any altitude level, the curves that result when these threshold values are combined to form a single vortical profile deviate totally from realistic profiles, particularly for density. Fig. 2-3 illustrates this point. Improper design of the rocket system may result as a consequence of this negligence

Although the introduction of more realistic profiles may increase some of the engineers' computational work by adding a few profiles or by making his computations more complex, hopefully the engineer will thereby realize a gain for his system by avoiding improper design. Ideally, investigations would employ sample profiles. The disadvantage of this approach is the tremendous amount of calculations that result if individual atmospheric conditions are used as inputs from random data selections. Some of the advantages of realistic data can be retained, with a reasonable amount of computation, by using carefully selected, small but representative samples.

One such selection has been prepared by Dr. O. M. Essenwanger, Chief, Aerophysics Branch, Physical Science Laboratory, Army Missile Comvand, Redstone Arsenal. His collection consists of 800 representative individual profiles, a.ranged in eigl., sets of 100 profiles; two sets for each of four stations represent summer and winter conditions. Fig. 2-3 is a selection from this collection. The entire collection, on punched cards. may be obtained from Dr. Essenwanger.

The next best, and also simpler, approach would be to use a representative profile. Their use will keep computational effort relatively simple, but will provide realistic estimates of actual atmospheric conditions. Data obtained timough use of these profiles will provide information on missile behavior adequate for preliminary design.

Such a set of representative profiles is the 20 sets of air density and associated temperatures presented in Table 2-4 and Fig. 2-4. These profiles may be used to represent mean and onesigma conditions for four zones, by summer, winter, and annual reference periods. The proper profile for each condition is presented on the first page of Table 2-4, where the numbers refer

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to the subscripts in subsequent column headings and the various curves of Fig. 2-4.

Mr. H. P. Dudel of the Aerophysics Branch, Physical Sciences Lab, R&DD, U.S. Army Missile Command, has published a report (Reference 7) giving the mean, minus-one signa, and plus-one sigma density profiles for the midseason months of January and July at latitudes of 15°N, 30°N, 45°N, 30°N and 75°N. The associated temperatures are not yet available, but will be included in a forthcoming report. In the meantime, the Committee on Extension of the Standard Atmosphere (COESA) has announced adoption and proposed republication of the Air Force Interim Supplemental Atmospheres as published by Cole and Kantar (Reference 3). These supplementary atmospheres to the U.S. Standard Atmosphere, 1962, approximate mean conditions at the same geographic latitudes and months as does H. P. Dudel's report, Ref. 7.

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- 2. U. S. Standard Atmosphere, 1962 COESA, NASA, USAF, U. S. Weather Bureau, U. S. Government Printing Office, Dec 1962.
- 3 Air Force Interim Supplemental Atmosphere to 30 Kilometers, Air Force Surveys in Geophysics No. 153, 1963.
- Handbook of Geophysics and Space Environments, AFCRL, McGraw-Hill, April 65.
- 5. AR 705-15, Change 1. Operation of Material Under Extreme Conditions of Environment.
- 6. MIL-STD-210A, Climatic Extremes in Military Equipment.
- 7. H. P. Dudel, Regiona'-Seasoral One-Sigma Density Profiles, Aerophysics Branch, Physical Sciences Lab. R&DD, USAMICOM.

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# TABLE 2.2. RESULTANT WIND CONDITIONS IN THE NORTHERN HEMISPHERE

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Resultant wind direction (d in degrees), vector mean wind velocity (5 in knots), and
standard vector deviation (8 in knots) at various altitudes (H) for various latitudes and longitudes
in the Northern Hemisphere, summer and winter seasons.

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### TABLE 2-2. RESULTANT WIND CONDITIONS IN THE NORTHERN HEMISPHERE (cont)

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Resultant wind direction (d in degrees), vector mean wind velocity ( $\bar{v}$  in knots), and standard vector deviation (8 in knots) at various altitudes (H) for various latitudes and longitudes in the Northern Hemisphere, summer and winter seasons. (Continued)

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### TABLE 2-2. RESULTANT WIND CONDITIONS IN THE NORTHERN HEMISPHERE (cont)

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Resultant wind direction (d in degrees), vector mean wind velocity ( $\overline{v}$  in knots), and standard vector deviation (8 in knots) at various altitudes (H) for various latitudes and longitude? in the Northern Hemisphere, summer and winter sessons. (Continued)

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# TABLE 2-2. RESULTANT WIND CONDITIONS IN THE NORTHERN HEMISPHERE (cont)

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10 20 30 40 50 50 70 80 90 100	260 260 260 265 250 210 240 270 270	30 47 65 74 53 50 10 05 10 25	25 37 45 45 40	260 265 265 275 265 275 260 240 270 270	24 37 53 60 40 20 10 10 25	28 39 45 40 20 10	270 275 275 285 290 270 270 270 270 270	21 32 43 47 35 20 15 10 10 20	29 39 50 45 20 20 15	280 260 285 285 280 290 300 330 330 310	15 29 42 47 35 25 15 10 10 15	23 37 48 43 20 20 20 25 30	285 275 270 270 270 200 290 .00 300 300	20 37 53 60 45 30 20 15 20	23 37 45 35 20 25 30 35	270 270 270 270 270 270 270 270 270 270	35 53 75 80 60 35 25 25 30	25 37 47 40 30 25 25 30 30 35	275 265 265 265 270 270 270 270 270	28 47 57 55 50 35 30 25 30 25 30	27 37 46 48 35 25 25 30 35	260 260 260 265 270 260 260 270 270	15 30 35 40 35 35 30 20 20	28 38 45 43 35	275 282 280 280 270 270 270 270 270 270	12 15 22 25 25 30 25 20 25	24 32 38 38 30
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10 20 30 40 50 60 70 50 100	240 240 240 245 230 230 230 250 270	20 26 35 42 30 25 15 10 15 30	23 24 25 25	260 255 255 260 255 270 260 270 270 270 270	20 32 40 40 30 25 20 15 15 25	30 40 45 40 35 30 25 25	260 270 280 290 290 300 290 290 290	21 32 42 30 20 15 20 20 25	31 43 50 40 35 25 25 30 35	255 280 285 285 285 285 290 300 300 300	18 31 38 30 25 20 25 30	20 35 45 30 35 30 30 30 30 30 30 30 30 30 30 30 30 30	295 290 285 285 285 290 290 290 300 295 295	20 33 42 42 35 30 30 25 30	20 32 33 35 30 30 30 35 40	275 275 270 270 270 280 280 280 280 280	22 37 50 45 50 30 30 30 30 30 30 30 30 30 30 30 30 30	25 35 40 35 30 30 30 30 35 40	265 260 255 255 255 270 270 270 270 270 270	23 40 48 52 45 49 40 40 40 45	27 38 45 40 35 30 30 35 35	250 245 250 250 250 250 250 250 260 270 270	28 43 55 50 35 40 40 35 40 40	33 43 55 45 35	260 265 265 270 275 270 270 270 260 270 270	24 34 40 30 35 35 40 35 35	32 44 50 45 35
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Resultant wind direction (d in degrees), vector mean wind velocity ( $\overline{v}$  in knots), and standard vector deviation ( $\overline{\sigma}$  in knots) at various altitudes (H) for various latitudes and longitudes in the Northern Hemisphere, summer and winter seasons. (Continued)

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# TABLE 2-2. RESULTANT WIND CONDITIONS IN THE NORTHERN HEMISPHERE (cont)

Resultant wind direction (d in degrees), vector mean wind velocity ( $\bar{\mathbf{v}}$  in knots), and standard vector deviation ( $\delta$  in knots) at various altitudes (H) for various latitudes and longitudes in the Northern Hemisphere, summer and winter seasons. (Continued)

													W	inte	r												
ч. -	1	80°	₩	1	160*	W	1	÷0°	Ŵ	1	20•	W	1	.00•	W	1	7 *03	V		60• 1	W		40• 1	W		20• \	W
10 <sup>3</sup> 4	d	V	ð	d	7	8	d	۷	8	d	V	8	đ	v	8	d	Ÿ	8	d	Ø	8	d	Ÿ	8	d	Ÿ	8
											I	.ATI	TUDI	E 70	۰N												
10 20 30 40 50 60 70	300 280 265 240 240 250 250 250	03 06 13 17 25 35 40	26 30 34 30 25	300 280 275 265 260 270 270 270	04 09 17 23 25 35 35	24 30 35 28 25 35 35 35	285 290 285 290 285 290 290 290	07 15 19 20 25 35 35	20 27 33 28 25 30 35 35	310 310 310 315 305 300 310 290	08 14 17 18 25 5 40	20 24 27 25 25 30 35 35	330 325 325 320 310 310 310 290	08 13 17 17 20 30 35 35	18 24 20 25 25	110 190 250 260 275 310 320 300	02 03 05 15 15 20 30	18 27 29 25 25	195 195 200 205 225 270 280 270	07 13 15 15 15 20 25 30	21 33 35 30 25	165 215 225 225 230 250 250 270	08 13 15 20 25 30 35 35	24 36 40 30 30	270 245 250 255 260 260 260 270	09 17 23 25 25 30 35 40	25 56 46 32 30
80 90 100	270 270 270	40 40 40		270 270 270	40 40 45	33 40 45	275 275 275	40 40 45	30 40 45	290 290 290	40	33 40 40	280 270	40 45		280 270	40 45		270 270	30 40		270 270	40 45		270 270	45 50	
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10	<b>∠40</b>	06	16	265	08	15	290	13	15	250	69	15	270	12	15	290	08	15	200	12	14	210	11	17	210	07	r
20	265	27	21	245	15	25	260	22	22	285	23	23	285	22	20	265	24	20	230	20	17	225	25	20	285	17	2
30	265	55	32	260	35	27	275	40	30	270	45	28	260	40	25	250	45	25	255	40	22	245	32	25	295	30	2
40	265	62	35	260	50	30	275	50	30	255	65	33	250	65	30	250	52	25	250	45	25	240	30	28	260	35	30
50	265	50	25	260	45	30	270	45	25	260	55	30	250	55	32	250	45	25	240	40	25	230	25	25	220	30	2
60	270	40		270	35		270	35		270	35		270	40		270	35		260	30		260	20		150	20	
70	250	10		250	15		210	15		210	25		2 <u>2</u> 0	25		230	30		25Û	iû		220	10		90	ίũ	
90	100	03		160	05		30	05		30	05		30	05		30	05		230	05		110	05		70	10	
90	90	05		90	05		90	05											90	10		96	10		90	10	
100	90	10																	90	10		90	15		90	10	
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10	290	14	20	280	16	20	265	20	19	250	18	15							285	28	17	275	30	20	270	30	2
20	280	36	30	270	32	33	255	38	28	265	35	25	270	35	25				270	55	25	270	65	30	265	60	3
30	280	50	45	270	60	45	270	65	40	270	55	35	275	58	35	270	70	35	270	65	35	265	90	35	270	80	Ă
40	280	55	45	270	65	40	270	75	40	255	75	40	260	80	40	270	63	35	270	90	35	270	10	40	270	95	i
50	280	50	35	270	55	30	270	65	30	265	70	35	260	75	35	265	60	35	265	85	35	265	85	35	275	70	3
60	280	30		280	35		260	35		270	35		270	40		270	50		270	55		200	50		260	35	
70	290	20		200	20		260	25		27ú	30		270	30		280	30		260	25		240	20		200	15	
80	290	15		220	20		270	20		260	20		260	20		270	15		240	20		220	15		250	05	
90	270	15		270	25		<b>Z</b> 70	20											250	20		260	20		270	08	
100	270	y.		270	30														270	25		270	25		270	15	

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# TABLE 2-2. RESULTANT WIND CONDITIONS IN THE NORTHERN HEMISPHERE (cont)

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Resultant wind direction (d in degrees), vector mean wind velocity ( $\overline{v}$  in knots), and standard vector deviation (3 in knots) at various altitudes (H) for various latitudes and longitudes in the Northern Hemisphere, summer and winter seasons. (Continued)

_												_	Ħ	linte	r					_							
ч-		0*		<u> </u>	20 • 1	E		40° )	E		<b>60•</b> :	E		80°	E	1	100*	E		120*	E		140•	E		160*	E
10 <sup>8</sup> ft	<u>d</u>	¥	•	d	V	*	d	7	8	d	₹	8	d	Ÿ	8	4	¥	8	d	4	ş	4	¥	8	đ	v	8
											I	лті	TUD	E 40	• N											_	
10 20 30 40 50 60 70 80 90 109	290 305 305 290 290 290 290 270 270	12 18 23 23 25 25 25 25 25 25 25 25 25 25 25 25 25	23 32 40 40 30	200 200 200 200 200 200 200 200 200 200	14 20 33 40 55 35 30 30 30 40	24 32 45 40 35	260 265 255 270 275 270 270 270 270	16 27 40 55 45 35 30 30 35	21 29 37 33 35	260 265 270 265 270 270 270 270	09 16 33 43 45 35 30 35	15 22 35 37 30	270 270 270 270 270 280 270 270	09 27 44 55 50 45 35 35	11 25 35 35 35	295 285 285 280 270 290 230 270	23 40 55 65 60 50 40 40	17 27 36 40 35	300 290 285 280 270 260 250 250 270 270	28 44 60 70 65 55 40 35 35	18 32 37 40 40	285 270 270 260 250 230 210 260 270	34 54 80 90 60 50 40 25 30 35	23 35 50 40 40	265 260 260 250 255 250 220 140 240 270	33 52 75 80 70 40 25 15 20 30	24 34 45 45 45 40
••			••			••				•••		-511 	TUD	E 50	• N												
10 20 30 40 50 60 70 80 90	200 305 305 305 280 280 270 270	15 23 20 30 25 30 30 35 40 50	25 36 50 40 30	220 290 290 290 290 290 290 290 290 290	12 16 20 25 30 35 40 50	20 34 45 35 35	260 270 275 275 275 290 270 270 270 270	11 17 20 25 25 35 35 40 40	25 30 34 32 30	250 270 275 270 275 270 270 270	08 14 18 25 30 40 40 50	21 28 35 35 25	275 285 290 280 280 280 280 280 270	11 20 30 30 40 40 50	20 30 33 33 30	295 300 300 295 275 290 280 270	18 26 35 35 40 45	20 27 33 37 35	315 310 305 300 280 260 250 240 270 270	22 25 25 45 40 40 40 45 40 40 40 40 40 45	18 30 35 35 35	290 275 270 255 230 230 220 270 270	15 x 26 35 40 45 40 40 40	24 35 35 35 35	250 240 240 245 230 230 230 230 230 230 270	12 18 27 40 35 35 25 30 40	27 35 40 40 35
											I	ITA.	TUD	E 60	• N												
16 20 30 40 50 00 70 80 90 100	270 230 235 285 290 270 270 270 270 270	16 25 32 35 30 35 49 40 45 50	26 38 50 40 35	290 290 290 27, 27, 260 270 270 270 270	34222335459	25 33 45 40 35	270 285 290 290 290 290 290 290 270 270	07 10 15 20 30 35 35 40	26 32 33 35 30	260 230 235 290 285 270 270	08 12 17 20 15 25 35	24 34 35 35 25	265 290 295 295 290 280 280	12 16 20 15 25 40	24 33 38 35 30	205 310 315 315 290 280 280	13 15 20 20 25 40	21 28 32 33 30	320 320 330 290 260 250 270 270 270 270	09 09 15 15 20 35 35 40	17 25 30 30 30	300 290 240 245 220 220 230 270 270	04 05 08 15 30 40 40 45	22 28 31 28 30	255 225 210 210 220 230 230 230 270 270	03 05 10 15 20 30 35 35 45	25 35 35 35 30
10	~~~			~				05	02	940	ر عہ	-41 J J	10D	с /U л/	02 02	960	04	200	210	02	17	200	03		200	0.2	~~
10 20 39 40 50 60 70 50 90 100	200 255 260 270 275 270 270 270 270 270 270	11 13 23 25 25 30 30 35 40 50	23 23 24 23 24 23 25 25 25 25 25 25 25 25 25 25 25 25 25	200 270 280 285 290 270 270 270 270	11 13 18 20 20 35 40 55 40 50	22 26 33 30 30	230 230 285 290 250 290 270 270	07 10 15 15 35 40 二 3 、	425 30 30 30 30 30 25	280 250 290 290 290 200 250	5 60 12 10 10 30 35	23 26 30 30 25	245 290 300 300 230 230 TUD	06 10 10 05 30 35 E 80	26 23 30 25	200 310 320 290 270 260	06 03 05 05 25 30	20 24 25 28 25	330 50 300 220 220 270 270	03 03 03 03 03 03 03 03 03 03 03 03 03 0	22 25 25 25	300 210 220 240 240 270 270 270	03 02 05 10 30 35 35 40	25 25 25 25 25	285 250 220 230 230 230 270 270 270	03 04 05 10 15 40 40 40 45	23 27 28 25 25
10	<b>245</b>	07	21	250	06	21	240	06	20	230	05	20	230	03	20	250	03	20	300	02	17	215	03	20	330	03	20
28843332888	240 240 250 250 270 270 270 270 270	12 18 15 15 15 15 20 40	- 23 36 23 25	250 250 270 270 270 270 250 270 270 270 270	10 16 13 10 15 20 20 20 20 20 40	123222	250 250 275 270 270 270 270 270 270	07 10 10 10 10 20 10 15 35	22222	275 270 290 275 200 260	05 10 07 05 10 15	22 22 22 22	290 220 300 250 250 230	04 07 05 05 10 15	22 25 25 25 25	305 300 295 260 230 230	04 04 05 05 10 20	23 23 23 20	320 370 270 260 210 210 270 270	03 03 05 08 15 20 25	22 25 25 25	300 245 250 245 220 220 270 270 270	03 03 07 10 15 25 30 40	25 25 20 20	310 280 260 250 230 230 270 270 270	03 05 10 15 25 30 30 30 35	25 25 25 25 20

### TABLE 2-3. EXTREME ANNUAL WIND SPEEDS

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Extreme annual wind speed (fastest mile) at 50 ft above ground at the given stations; (A) denotes airport station.

	Years			1% Risk
	of	Mean	S.D.	in 10 yr
Station	Kecord	(mile h - 1)	(mile h - 1)	(mile h-1)
Temps, Fle. (A)	1941-56	52	8.8	95
Miani, Fla.	1943-58	54	18.0	143
Wiimington, N. C. (A)	1951-53	67	15.9	146
Hatteras, N. C.	1912-57	62	13.4	129
Dallas, Tex. (A)	1941.58	52	6.5	84
Washington, D. C. (A)	1949-58	50	8.5	92
Dayton, Uhic (A)	1944-58	60	8.6	103
Atlanta, Ga. (A)	1953-58	50	7.4	87
Applene, Iez. (A)	1945-58	83	13.6	131
Columbia, Mo. (A)	1999-58	50	6.2	87
Refisio N V (A)	1939-30	00 60	1.0	90
Albert N $\nabla$ (A)	1020 20		8.3	<b>9</b> 9
Restor Mass (A)	1936-30	50	0.9	29
Chicago III (A)	1930-30	57	14.1	119
Claveland Obio (A)	10(1.59	50	5.0	(9
Detroit Mich (A)	1034.58	40	57	37 77
Minnespolie Minn (A)	1938.58	52	11 1	107
Omaha Nebraska (A)	1936.58	59	13.1	124
El Paso, Ter. (A)	1943-58	58	45	90
Albuquerque, N. M. (A)	1933-58	61	10.2	112
Tucson, Ariz.	1948-58	50	7.1	85
San Diego, Calif.	1940-58	36	6.0	66
Chevenne, Wyo.	1935-58	63	6.9	97
Rapid City, S. D.	1942-58	66	6.7	99
Bismarck, N. D.	1940-58	66	5.2	92
Great Fall, Mont.	1944-54	65	3.5	82
Portland, Ore.	1950-58	57	6.2	<u>91</u>
New York, N. Y.	1949-58	56	4.8	82
Pittsburgh, Pa.	1935-52	52	6.2	83
	Number			
	of Years			
	of Data			
Fairbanks, Alaska	9	37	8.3	78
Nome, Alaska	11	61	9.1	106
Elmendorf AFB, Alaska	14	45	7.1	81
Shemya Island, Alaska	10	70	6.2	101
Hickam AFB, Hawaii	17	45	8.4	86
Clark AB, Philippines	13	39	12.2	100
Lajes Field, Amores	13	62	16.9	146
Albrook Arb, Canal Zone	18	20	7.1 15 7	47
San Pablo, Spain Wheeles A.P. Libes	11	11	13.3	100
Wheelus AD, Lidys	14 21	97 40	11.0	100
Kafanik lasland	10	40	7.0	129
Thule Greenland	14	80	194	155
Tainan Formore	30	53	21.2	159
Tainei Formosa	30	59	21.9	367
Itanika AR. Janan	19	43	10.0	93
Misawa AB. Japan	ii	47	7.2	83
Tokyo Intl. Aircost. Japan	15	52	12.2	103
Kimpo AB, Korea	8	43	8.0	82
Bombay, India	Ū.	50	14.2	120
Calcutta, India	6	57	7.4	93
Gaya, India	6	52	6.8	85
Madras, India	6	45	7.5	82
New Deihi, India	6	52	3.8	70
Poona, India	6	39	6.1	69
Central AB, Iwo Jima	17	78	37.9	266
Kadros AB. Okinawa	14	82	25.3	208

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Strongest wind (five-min average) for temperature range observed during a hve-yr period. Wind speeds are, in general, for 40 to 100 ft above the surface. Speeds at 10 ft are approximately 80% of the values given, except for the coldest temperatures, where winds are 50% of the indicated values. Stations used for this study are:

Caribou, Me. Burlington, Vt. Boston, Mass. New York, N. Y. Washington, D. C. Hatteras, N. C. Jacksonville, Fla. Miami, Fla. Galveston, Tex. Oklahoma City, Okla. Phoenix, Ariz. Los Angeles, Calif. San Francisco, Calif. Tatoosh I., Wash. Great Falls, Mont. Salt Lake City, Utah Wichita, Kansas Minneapolis, Minn. Chicago, Ill. Buffalo, N. Y. Pittsburgh, Pa. Columbus, Ohio

Figure 2-2. Strongest Wind for Temperature Range

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Figure 2-3. Density Deviation Versus Altitude - Worldwide, Annual

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### TABLE 2-4. DENSITY AND TEMPERATURE PROFILES

A. Key to Code Numbers of Density and Temperature Profiles (Figs. 2-4 (A) through (F))

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Zone	Season	Mean Proîle	"+0" Profile	"+0" Profile
	· · · · · · · · · · · · · · · · · · ·	Annual Models		1
Tropics Subtropics Temperate Z. Polas Z.	Annual Annual Annual Annual	が1 ズ3 挙10 券17	(a) #2 #3 #15	(a) #5 #12 #19
	•	Seasonal Models		1
Tropics Tropics Subtropics Subtropics Temperate Z. Temperate Z. Polar Z. Polar Z.	Summer Winter Summer Winter Summer Summer Winter	#1 #1 #2 #5 #3 #12 #15 #7.	(b) (b) ☆4 #7 #11 #14 #18	(b) (b) (b) #6 #9 #13 #16 #20

(a) Annual variation negligible(b) Variation negligible

# B. Density Profiles for Tropics and Subtropics (Unit: kg/m<sup>3</sup>)

Altitude			Profile N	lumber		
()km)	D <sub>1</sub>	Dz	Dj	D4	D <sub>5</sub>	D6
0	1.16375	1.17579	1.19053	1.21632	1.22022	1.24352
1	1.05105	1.06335	ULS76	1.10178	1.11493	1.12318
2	.96623	.26387	.00923	.99730	1.00910	1.02090
3	.57470	.87702	£3321	.8:-313	.90849	.91785
Å.	.72203	.7\$707	£0783	.81057	.81786	.82515
5	.71130	.72232	.72353	.73067	.73636	.74205
6	.64183	.65227	.65750	.65360	.66223	.66586
7	.57822	.23716	.50127	.59320	.59433	.59556
8	.51963	.52747	.50045	.53326	.53195	.53064
9	.43705	.47241	.47604	.47792	47376	.46360
10	.41547	.42143	.42116	.42428	.41862	.41296
11	37976	37450		37249	.30307	.35885
12	Serie .	.30950	.32443	.32262	.31662	.30962
13	.20059	.23084	.23100	.27810	.27142	.26474
14	23317	.25403	.24250	.23355	.23317	.22779
15	.22001	.22043	.20000	.20403	.20054	.19639
16	.19310	.15903	.17903	.17545	.17209	.16373
17	.10005	.16175	.15253	14953	.14656	.14419
18	.15442	.13633	.12923	12634	13480	.12275
19	.11100	.11409	.10000	.10716	.10565	.10614
20	.02335	.023553	.00201	.00057	06944	03931
21	.07912	00057	.07765	.07683	.07576	07459
22	.00177	.00325	000000.	06496	.06424	.)6752
23	.05463	.05795	.05203	.05514	05456	.05396
24	.64792	.0(22)	.04770	.04633	.04637	.04585
ద	.04063	.062290	.04002	.03991	.03046	.03201

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# TABLE 2-4. DENSITY AND TEMPERATURE PROFILES (cont)

Altitude				Profile Number			
(km)	D7	D <sub>8</sub>	D <sub>9</sub>	D <sub>10</sub>	D <sub>11</sub>	D <b>12</b>	D13
U.	1.21521	1.22279	1.23037	1.26119	1.27528	1.29368	1.3120
1	1 '9610	1.10530	1.11550	1.13046	1.12557	1.15177	1.16797
2	. 145	.99965	1.00784	1 01610	1.01591	1.03061	1.04531
3	.84356	.89990	.90624	.91249	.91174	.92344	93514
4	£0425	.80927	.81429	.81934	.81871	.82801	.83731
5	.72371	.72775	.73179	.73584	.73496	.74233	.7497(
6	.65067	.65396	.65725	.66013	65911	.66430	.66349
7	.58444	58715	.58926	.59141	.53954	59356	.59758
3	.52624	.52824	.52624	.52201	.52781	52751	52781
9	.47157	47652	46947	.46942	.46906	46634	.4636
10	.42211	.41769	.41327	41294	41652	40692	.39732
11	.37284	.36522	.35760	.35820	36140	45030	.3392(
12	32160	.31327	30494	.30643	30877	29837	.23737
13	2/348	.26730	.26112	.26110	26132	.25376	.2462
14	23382	22913	22444	22327	22219	.21650	.21031
15	20024	19633	.19302	19129	.18972	.18533	.18094
16	1 36	.16865	.13594	.16385	16232	15872	.1551
17	14667	.14458	.14249	.14020	.13359	.13563	.1326
18	.12547	.12391	.12235	.11995	.11850	.11605	.1136
19	10730	.10612	.10494	10256	.10138	.09932	.0972
20	.091C1	.09091	.03001	.08775	.08673	.03504	.0333
21	.07850	.07750	.07720	.07511	.07405	.07257	.0710
22	.06736	.06680	.06524	.06425	.06330	.06199	0606
23	.05770	.05725	05680	.05495	.05410	.05297	.0518
24	.04940	.04904	.04863	.04701	.04628	.04527	.0442
25	04221	00100	0/167	0:020	02062	02072	0278

# C. Density Profiles for Temperate Zone (Unit: $\frac{1}{2}\frac{1}{2}r_1^8$ )

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### D. Density Profiles for Polar Zone (Unit: kg/m²)

Altitude				Profile Number			
(km)	D <sub>14</sub>	D <sub>15</sub>	D <sub>16</sub>	0 <sub>17</sub>	.) <sub>18</sub>	D <sub>19</sub>	D 26
0	1.22769	1.24200	1.25631	1.33520	1.41360	.43400	1.45440
1	1.09663	1.11235	1.12207	1.17170	1.20340	1.22460	1.24580
2	.99077	1.00261		1.03904	1.05278	1,06968	1.03858
3	.89396	.90223	.91050	.92697	.93477	.94697	.95917
4	.£0508	.81134	.81760	.82868	.83384	.84194	.85004
5	.72466	.72526	.73366	.74063	.74410	.74850	.75310
6	.65195	.65493	.65791	.66121	.66332	.65424	.6/1516
7	.58807	.58742	.58877	.58870	.59061 、	.58701	.58341
8	.52836	.52527	.52418	.52123	.52244	.51479	.50714
9	.47079	.48740	.46401	.45739	.45635	.44617	.43549
10	.41753	.41043	.40333	.39630	.39425	.38265	.37105
11	.36349	.35478	.34607	.33928	332544	32564	.31624
12	91945	.30375	.29505	.29019	.28573	.27831	.27039
13	.28804	.28000	.25396	.24366	.24422	.23950	.23278
14	.22818	.22364	.21910	.21364	.20938	.20468	.19294
15	19328	.19253	.18393	.18360	.17972	.17570	.17168
16	.10354	.16563	.16272	.15780	.15436	.15095	.14754
17	.14480	.14231	.14002	.13560	.13288	.12979	.12690
18	.12404	.12224	.12044	.11640	.11381	.11139	.10697
19	.10623	.10487	.10351	10000	.09773	.09563	.093.63
20	.03106	.02003	.03883	.03530	.03385	.03216	.03045
21	.07818	07733	.07653	.07404	.07193	.07049	.06905
22	.05702	.05011	.06579	.06357	06178	.06045	.05912
23	.65/30	.05700		.05441	.05297	.05183	.05079
24	.01935	.04594	.04853	.04658	.04542	.04442	.04342
25	.04233	.04201	.04109	.03996	-03599	.03203	.03717
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### TABLE 2-4. DENSITY AND TEMPERATURE PROFILES (cont)

					•					
Altiturie	Profile Number									
(km)	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D4	D <sub>5</sub>	D <sub>6</sub>				
0 1 2 3 4 5 6 7 8 9 10 11 2 13 13 13 15 15 15 15	$\begin{array}{c} -5.0 \\ -4.5 \\ -4.0 \\ -3.8 \\ -3.7 \\ -3.4 \\ -2.8 \\ -2.0 \\ -1.2 \\ 0.0 \\ 1.2 \\ 4.1 \\ 8.0 \\ 12.0 \\ 15.5 \\ 18.0 \\ 19.0 \\ 15.0 \\ 19.0 \\ 15.0 \\ 10.5 \\$	-4.0 -4.0 -4.3 -3.5 -2.7 -1.9 -1.2 -5 3 1.1 1.9 2.3 6.0 9.1 11.5 13.2 13.9 13.7 12.1	-2.1 -2.2 -2.0 -1.8 -1.4 9 4 4 4 9 1.5 1.8 1.7 4.0 5.4 6.4 7.3 7.6 7.2 6.2	- 7 -9 -9 -11 -11 -8 .2 .5 14 23 26 21 3.7 4.3 26 21 3.7 4.3 4.7 5.1 5.4 5.1 5.4 5.1 4.3	4 3 2 1 2 .0 3 7 12 1.4 1.2 .2 1.5 1.8 2.3 3.0 3.4 3.2 2.6	1.5 1.5 1.4 .9 .7 .8 .9 .9 .9 .9 .9 .9 .9 .9 .5 1 16 7 7 .0 .8 1.3 1.3 .9				
20 21 22 23 24 22 23	5.0 4.2 3.5 3.0	5.7 7.5 6.1 5.8 5.3	3.5 2.5 2.3 1.9	1.0 1.9 .7 .2	2 4 8	-7 -13 -15 -19				
24	15	3.0	1.0	1	-1.2	-2.5				

E. Density Profiles for Tropics and Subtropics (Unit: Percent Deviations from U. S. Standard Atmosphere, 1962)

F. Density Profiles for Temperate Zone (Unit: Percent Deviations from U. S. Standard Atmosphere, 1962)

Altitude	Profile Number								
(km)	D <sub>7</sub>	D,	D,	D <sub>10</sub>	D <sub>11</sub>	D <sub>12</sub>	D <sub>13</sub>		
0 1 2 3 4 5 6 7 3 9 10 11 12 13 14 15 18 19 20 21 22 21 22 21	8 -14 -1.5 -1.7 -1.8 -1.7 -1.4 9 .1 1.0 2.1 2.2 3.1 2.6 2.8 2.9 3.1 3.1 3.2 3.3 3.5 4.4 4.9	-2 -5 -7 -10 -12 -12 -9 -5 7 10 13 16 18 20 26 35 41		$\begin{array}{c} 2.9\\ 1.7\\ .9\\ .3\\0\\1\\ .0\\ 2\\ .4\\ .5\\1\\ -1.8\\ -2.1\\ -2.0\\ -1.8\\ -2.1\\ -2.0\\ -1.8\\ -1.6\\ -1.5\\ .1.4\\ -1.4\\ -1.3\\ -1.1\\4\\1\\4\\1\\ \end{array}$	4.1 2.1 .9 3 1 2 1 1 1 1 1 1 1 1 1 1	5.6 3.6 2.4 1.6 1.0 8 6 .4 -1 -1.6 -4.0 -4.2 -4.8 -5.0 -4.8 -4.6 -4.5 -4.6 -4.5 -4.5 -4.5 -4.4 -3.7 -3.7	$\begin{array}{c} 7.1 \\ 5.1 \\ 3.8 \\ 2.8 \\ 2.2 \\ 1.8 \\ 1.4 \\ 1.3 \\ .4 \\7 \\ -3.9 \\ -7.0 \\ -7.7 \\ -7.6 \\ -7.5 \\ -7.1 \\ -6.8 \\ -6.6 \\ -6.5 \\ -6.5 \\ -6.2 \\ -6.4 \\ -5.9 \\ -5.8 \end{array}$		
25	5.6	4.9	4.0	.1 .3	-1.4 -1.1	-3.5 -3.4	-5.7 -5.6		

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### **Profile Number** Altitude D<sub>16</sub> D<sub>19</sub> D<sub>15</sub> D<sub>17</sub> D20 (km) D<sub>14</sub> D<sub>18</sub> $\begin{array}{c} 1.4 \\ .0 \\ -.4 \\ -.8 \\ -.10 \\ -.10 \\ -.10 \\ -.10 \\ -.25 \\$ 18.7 12.1 7.9 5.5 3.7 2.3 8 -11 -3.5 -6.7 -10.5 -13.3 -13.1 -12.7 -12.2 -11.8 -11.4 -10.8 -10.4 0 1 2 3 4 5 6 7 8 9 10 11 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 $\begin{array}{c} 2\\ -1.3\\ -1.6\\ -1.7\\ -1.6\\ -1.2\\ -.7\\ 1.\\ 1\\ 8\\ 1.2\\ 1.6\\ 2.0\\ 1\\ 2.4\\ 3.0\\ 3.9\\ 4.5\\ 1\\ 5.6\end{array}$ 9.0 5.4 3.2 19 1.6 2.2 -9 -2.1 -4.2 0 -7.0 -6.7 2-5.7 2-5.7 2-4.3 8 4.5 -2.4 -3.8 4.5 -2.4 -3.8 4.5 -2.1 -4.2 0 -6.7 2-5.7 2-5.7 2-4.2 -5.7 2-5.7 15.4 8.2 4.6 2.8 1.8 1.0 .5 .1 -.6 -2.2 -4.6 -8.0 -8.4 -8.4 -8.1 -7.7 -7.3 -6.8 -6.4 -6.0 -5.7 -5.2 -4.2 -3.7 -3.2 -2.7 -8.4 -8.0 -7.6 -7.1 -6.3 -5.7 -5.4 -5.0 -10.<sup>7</sup> -10.0 -9.5 -9.0 -8.3 -7.7 -7.5 -7.3

### TABLE 2-4. DENSITY AND TEMPERATURE PROFILES (cont)

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### G. Density Profiles for Polar Zone (Unit: Percent Deviations from U. S. Standard Atmosphere, 1982)

H.	Temperature Profiles for Tropics and	I Subtropics
	(Unit: Degrees Kelvin)	-

Altitude	Frofile Number								
(km)	T <sub>1</sub>	T <sub>2</sub>	T <sub>3</sub>	T <sub>4</sub>	T <sub>5</sub>	T <sub>6</sub>			
0	299.5	298.2	293.1	290.5	237.3	284.1			
ĩ	293.2	295.4	239.0	285.1	281.6	278.			
2	288.5	290.8	283.0	279.6	275.6	271.1.			
3	282 8	283.9	276.8	274.0	270.3	284.8			
Ă	278.5	276.9	270.3	268.1	264.5	28.1.9			
5	272.9	269.9	263.6	261.6	257.9	254.4			
6	287.1	282.1	256.6	254.6	250.8	247.2			
ž	260.9	258.4	249.4	247.2	243.5	:239.3			
8	254.3	249.5	242.0	239.6	236.1	232.5			
ŝ	247.2	242.6	234.6	232.2	120.0	200.0			
10	239.5	235.9	223.1	225.0	222.8	222.8			
11	231.6	229.5	222.6	218.4	218.7	222.0			
12	223.4	223.4	213.2	213.0	213.1	221.1			
13	215.4	217.9	215.4	209.8	215.3	219.6			
14	207.7	213.1	213.0	203,4	213.9	217.8			
15	200.9	209.0	210.7	207.2	212.0	215.9			
10	196.0	206.3	209.0	206.2	210.4	214.2			
17	194.6	205.2	203.5	205.6	209.7	213.0			
18	ieu z	206.4	203.2	207.3	209.9	213.0			
19	201.7	253.6	211.1	209.0	211.)	213.5			
20	206.5	\$12.9	213.0	219.7	212.4	214.3			
21	210.2	215.6	21.4.9	212.0	213.9	215.5			
22	213.1	217.7	216.7	213.7	215.4	217.0			
23	215.6	219.6	218.2	215.1	216.9	213.6			
24	218.0	221.4	į 219.8	216.3	218.4	220.3			
25	220.4	223.2	221,4	217.8	219.9	222.1			

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Altituzie	Profile Number								
(km)	ʻr,	T <sub>8</sub>	Т <sub>9</sub>	T <sub>10</sub>	T <sub>11</sub>	T <sub>12</sub>	Т <sub>13</sub>		
0	290.0	203.7	237.4	280.3	276.6	272.8	269.0		
i	205.8	233.6	281.4	276.9	273.8	270.6	267.4		
2	279.7	277.7	275.7	272.0	269.2	268.3	263.4		
3	214.5	272.5	270.5	258.8	263.8	261.0	258.2		
4	233.9	203.9	284.9	261.0	257.8	255.0	252.2		
5	252.6	200.8	259.0	254.5	251.1	248.3	245 5		
6	215.9	254.2	252.5	247.6	244.1	241.3	238.5		
7	263.7	247.1	245.5	240.3	236.7	234.0	231.3		
8	240.1	239.5	237.9	232.9	229.3	226.8	224.3		
9	232.4	231.9	230.6	225.9	222.0	220.5	219.0		
10	225.9	224.9	224.2	220.4	214.9	216.2	216.3		
11	218.8	220.9	222.7	217.5	211.7	214.5	216.6		
12	217.5	220.8	224.3	217.5	211.5	214.9	217.0		
13	219.3	221.8	224.7	218.2	212.5	215.6	217.7		
14	219.5	221.8	224.3	218.3	212.9	215.2	217.5		
15	219.7	221.7	223.7	218.1	212.5	214.9	217.1		
16	220.2	221.7	223.2	217.0	212.1	214.5	216.8		
17	220.8	221.8	222.8	217.6	211.8	214.0	216.3		
18	221.4	222.2	223.0	217.5	211.4	213.6	215.8		
19	221.8	222.6	223.4	217.4	211.1	213.3	215.6		
20	222.3	223.1	223.9	217.5	210.7	213.1	215.4		
21	222.8	223.6	224.4	217.8	210.3	212.9	215.3		
22	223.1	224.1	225.1	217.9	209,9	212.7	215.4		
23	223.7	224.7	225.7	218.2	209.6	212.5	215.4		
24	224.5	225.6	228.7	218.6	209.2	212.3	215.4		
25	225.5	228.7	1 227.9	219.1	203.8	212.1	215.3		

### TABLE 2-4. DENSITY AND TEMPERATURE PROFILES (cont)

I. Temperature Profiles for Temperate Zone (Unit: Degrees Kelvin)

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### J. Temperature Prcfiles for Polar Zone (Unit: Degrees Kelvin)

Altitude	Profile Number								
(km)	T <sub>14</sub>	T <sub>15</sub>	T <sub>16</sub>	т <sub>17</sub>	T 18	T 19	T 20		
0	229.1	282.9	276.7	265.2	254.8	247.8	240.8		
í	203.3	280,3	274.3	268.0	261.0	253.8	246.6		
2	200.3	275.1	269.9	263.4	260.6	253.6	246.6		
3	274.5	269.7	284.9	258.9	256.6	249.8	243.0		
4	203.8	264.0	259.2	253.4	251.0	244.5	238.0		
5	202.7	257.8	252.9	248.1	244.3	238,3	232.3		
6	253.0	251.0	246.0	240.8	237.2	232.0	226.8		
Ť	243.8	243.8	238.8	234.2	229.7	228.0	222.3		
ġ	241.1	233.5	231.9	228.1	223.2	221.3	218.6		
ğ	233.5	239.5	227.4	223.5	217.3	218.5	219.7		
10	223.3	225.1	224.0	221.3	215.1	218.0	221.3		
11	220.2	224.0	227.0	221.6	216.5	219.2	223.1		
12	219.9	224.5	223.5	222.3	217.1	220.0	223.6		
13	221.8	225.5	223.3	222.7	216.7	220.0	223.8		
14	222.4	225.3	227.8	222.5	216.2	219.5	222 4		
18	222.2	224 0	661.3	222.1	215.6	219.2	223.4		
YR	222.1	224.5	228.9	221.8	215.0	218.8	223.2		
17	222.3	224.5	223.7	221.6	214.4	218.5	223.0		
18	222.7	224.8	223.7	221.3	213.8	218.2	222.8		
19	223.1	225.0	223.9	221.2	213.2	217.9	222.6		
	223.6	225.5	227.4	221.2	212.6	217.6	222.4		
21	224.1	223.0	227.9	221.1	212.0	217.4	222.2		
22	224.6	223.5	223.4	220.9	211.4	217.0	222.0		
2	225.1	227.0	223.9	220.7	210.8	216.6	221.8		
24	225.9	227.8	229.7	220.9	210.2	216.2	221.6		
25	223.7	223.6	230.5	221.1	209.6	215.8	221.4		
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Figure 2-4(C). Polar Zone - Annual Density Model

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Figure 2-4(E). Tropics - Seasonal Density Models

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Figure 2-4(G). Polar Zone - Seasonal Density Mcdels

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# CHAPTER 3 System design

### 3-1 GENERAL

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The first point to be considered in the design of a rocket system is the purpose of the system We shall attempt to answer the first questions usually asked: To what use will the system be put; who will use it, and how will it be used? Next will be a more precise and detailed examination of the requirements to provide a basis for developing, first, the conceptual approach and, then, the detailed design. Rocket system requirements can be documented in various forms, as will be explained in more detail later, or they can be orally expressed statements in anticipation of later, formally documented statements Regardless of form, requirements based on real or anticipated needs should precede any system dusign in order for the design to be meaningful. With the requirements as a basis, an orderly and systematic procedure leading to a successful conclusion can then be established.

Before discussing the systematic procedure for the design of a rocket system, however, a brief survey of classes of rockets, operational modes, and launching methods will give us a common background and terminology for the discussion

#### 3-2 CLASSES OF ROCKETS

#### 3-2.1 MILITARY ROCKET SYSTEMS

In general, rocket systems used by the several branches of the armed forces are classed as military systems. They are used, except in several instances which will be noted later, to deliver some form of destructive warhead on an enemy target Th. types used most frequently by the Army are briefly described in the paragraphs which follow.

#### 3-2.1.1 Artillery

Artillery rocket systems are used in the same manner as artillery gun systems--to support porsonnel in contact with the enemy in forward areas They have long range capability and vary in size from small, man-handled rockets to very large rockets requiring heavy equipment for handling and loading. The primary function of an artillery rocket system is support by indirect fire, but most systems have some capability for direct fire. System accuracy is probably the most important consideration in artillery rocket systems.

#### 3-2.1.2 Infantry

Infantry rocket systems are used by cersonnel in forward areas, in direct contact with the opposing forces. Infantry systems are generally direct-fire-type weapons, usually smaller than artillery systems, and, frequently, man-carried and -fired. The most notable type of infantry system is the antitank weapon, carried by the individual soldies and designed to be fired from the shoulder Many special factors must be considered in such systems since the rocket and man are in such close contact. The weapon must be effective, yet safe to be handled and fired without endangering the user. Infantry systems as light. easily transported by men, and simple to facilitate fast reaction to changing battlefield conditions.

#### 3-2.1.3 Air Defense

Air defense rocket systems are used to protect the ground soldier from enemy aircraft. They range in size from small, individually carried and fired systems to large, complicated systems capable of attaining very high altitudes. Many of these employ some type of guidance system to enable the rocket to maneuver and counteract the aircraft evasive tactics. The free rocket systems are generally fired in number into an area where the aircraft is or is expected to be. This results in a pattern in the target area similar to a pattern of shotgun pellets fired at a tlying bird. The rockets in these systems are usually small and simple in design to permit large numbers to be used economically

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#### 3-2.1.4 Armor

Rocket systems used by the armored forces are, in many instances, the same as those used by the infantry and artillery. The tank, armed with a direct-firing gun or rocket system, is the primary weapon of the armored forces. The primary target of tanks is enemy tanks; consequently, the antitank type of rocket is generally employed. However, tank weapons are also used against many types of ground tanjets. For this reason, they carry ammunition mixes suitable to the more prevalent targets expected.

### 3-2.1.5 Aviation

Rocket systems to be mounted on, and fired from, Army fixed and rotary wing aircraft have been of invreasing interest. The need for these small aircraft to have some type of defense, and to be able to perform an attack function in close support of the ground soldier, has been shown to be of considerable importance, as evident in brush-fire activity in several parts of the world When this need for aerial rocket weapons first become urgent, attention was turned to adapting an appropriate rocket system originally developed to fill other requirements. Since aircraft are used by the individual branches of the Army ground forces, rocket systems are used to accomplish the missions assigned the using branch. In addition, airborne rockets are used for the defense against aircraft of the or,posing forces. The notable difference in these systems is that they are fired from an elevated platform that is unstable and in many instances rapidly moving. Rotary wing aircraft can stop and hover but, unlike a tank, they have no firm ground base as a steady firing point. Many additional factors must be considered in the design of aircraft systems to permit attainment of the tactical performance desired without endangering the aircraft or its eress.

#### 3-2.1.6 Logictic

Although no significant development of logistic rocket sys<sup>+</sup> ms has occurred up to this time .r. this class of rocket, it will undoubtedly play an important role in future large scale warfare. The logistic rocket is proposed as an extremely fast direct method of delivering to ground forces all types of supplies needed on the battlefield. In this concept the payload, in tead of being a destructive mechanism, is composed of food, clothing, ammunition, medical items, or any other items of supply needed by personnel, and can be any single item or any desired mixture of items. At the destination, the payload is separated and parachuted to the ground. Rapid movement of men to forward areas and distant points by means of rocket transport has been proposed; however, much more elaborate techniques must be developed and utilized before this method of transport becomes practical.

#### 3-2.1.7 Support

Rocket systems can also be used to support other operations. Examples of such systems are flare rockets for night operations in the battle area, tactical meteorological rockets for obtaining data necessary in artillery fire operations, rockets for delivery of some type of electronic equipment to a specified point for place-marking or transmittal of intelligence, and rockets that will produce smoke or other visual means of spotting on a target. The uses to which rocket systems can be put in their support role seem to have no particular limit. The same design approach is used for support rocket systems as for any other rocket system; the designer is limited only by the particular dictates of the specific requirement.

#### 3-2.2 RESEARCH ROCKET SYSTEMS

#### 3-2.2.1 Goneral

Research rocket systems have, in common with nullitary rockets systems, the general characteristic of delivering a payload to some designated point. Research rockets are also made up of the same general group of components. Their prime function, however, is different. They are designed to accomplish a mission from which useful technological data will be obtained to further a scientific understanding of a specific discipline. In this role, the payload becomes a device to gather data for later evaluation. Su h a payload obviously necessitates a means for payload recovery and a means to prevent payload damage or de-

struction that would negate mission completion. In a sense, many military rockets serve as research rockets during their developmental phase. In this phase, the payload is a ballast weight or data gathering device; equipment exterior to the system also is used to gather information on the rocket flight. The knowlcdge obtained is used to further the understanding of rockets and their behavior as powered airborne vehicles.

#### 3-2.2.2 Meteorological

Rocket systems have been used to place sensing devices at various altitudes in and out of the earth's atmosphere. These have the purpose of providing information about the earth's air, the winds, temperature, radiation, moisture, and other phenomena. Because these systems utilize a vertical or near-vertical trajectory, the objective is the attainment of altitude.

#### 3-2.2.3 High Altitude Sounding

Rocket systems for sounding at high altitudas are used for obtaining some specific bit of information at altitudes ranging to several hundred miles above the earth's surface. These, like the meterological rockets, utilize a vertical or nearvertical trajectory.

#### 3-2.2.4 Satellites

Unguided, aerodynamically stabilized rocket systems can be used to place a payload into earth orbit. The payloads of these systems are usually small sensing devices for gathering information and transmitting it back to earth. These systems are usually multistage, with the first, and perhaps a second, stage operating in the unguided or freeflight mode. In later stages, it is necessary to provide some type of guidance to permit maneuvering into an attitude to attain the desired orbital path. In these stages, the purpose of the unguided phase is to place the vehicle at some appropriate altitude from which the orbital phase can be initiated. For small payloads, this system approach results in considerable saving in guidance hardware, particularly where precise orbital mechanics are not required.

#### 3-2.2.5 Dispensing

Dispensing rocket systems can be either research or military The purpose of such a rocket system is to dispense a material, or materials, at some point in the rocket's trajectory. Examples are chaff-dispensing rockets, leaflet-dispensing rockets, smoke screen rockets, and lockets to disseminate crystals of various substances for cloud seeding to induce rain. The chaff dispensers are used to put large quantities of very small metallic wires into an area at some height above the ground. These wires, or dipoles, are then tracked by ground radar to determine the nature of wind currents at various altitudes. Leaflet rockets are used to deliver propaganda leaflets over areas not accessible from the ground. The poyload is released at a specific altitude and the leaflets flutter, spread, and are carried over large ground areas by the wind. Although not in general use, cloudseeding mckets have been proposed, e.g., a rocket to dispense small pellets of dry ice into fog banks for fog removal over airports and similar areas. It appears practical to use rocket delivery metheds for dispensing materials such as those described above, particularly where other means requiring human presence are not practical or are denied. The rocket's presence is almost unknown until after it has accomplished its mission.

### 3-3 OPERATIONAL MODES

#### 3-3.1 General

Rockets may be designed and used in an almost unlimited number of ways. They have been used not only to serve military and research purposes, as discussed in the foregoing paragraphs, but also to propel aircraft and land-based vehicles, and for other similar purposes. It is not the purpose of this handbook to discuss the many facets of rocket uses, but only t. present the uses most commonly employed in military systems The paragraphs which follow will briefly describe the modes normally used for military rocket systems.

### 3-3.2 GROUND-TO-GROUND

In the ground-to-ground mode the rocket is launched from a point on the ground to a target 1,1

on the ground. Most artillery, infantry, and armor systems are used in this mode.

#### 3-3,3 GROUND-TO-AIR

In the ground-to-air mode the rocket is launched from the ground against an airborne target. The target may be a manned airplane, an unmanned drone, another rocket or missile, or simply a point in space. The air defense, meteorological, high altitude sounding, and dispensing rocket systems operate in this mode.

#### 3-3.4 AIR-TO-AIR

The air-to-air rocket systems are used in defensive and offensive operations from aircraft against other airborne targets. Some of the aviation rocket systems for use on fixed and rotary wing aircraft are in this category.

#### 3-3.5 AIR-TO-GROUND

-Air-to-ground rocket systems are used in suppressive fire over areas of ground, for point targets on the ground, and to deny an enemy a ground position. They are fired from fixed wing and rotary wing aircraft, usually at relatively low altitudes. It is extremely difficult, except in unusual circumstances, to recognize and identify ground targets from an aircraft, and the higher the viewing position, the more difficult this becomes. For this reason most air-to-ground rockcts do not need extremely long range capability; however, they do need to be as accurate as possible to permit effective fire from the unstable aircraft firing platform.

#### 3-3.6 UNDERWATER-TO-AIR

Rocket systems have been designed and built to be fired from under the surface of a body of water and to continue flight after emerging into the atmosphere. At present, the submarinelaunched POLARIS missile system is the most notable example. Although the POLARIS is a guided missile of considerable complexity, there is nothing inherent in rocket technology to prevent any rocket system, guided or un ided, from functioning in this mode. The critical factor is accuracy since the purpose of firing this type of rocket is to hit a target.

### 3-3.7 SURFACE/AIR-TO-UNDERWATER

These systems are the reverse of those described in the preceding paragraph. I., these systems, the rocket is fired from a surface or air launching point, enters a body of water, and continues its trajectory in that medium. One current example is the SUBROC, or submarine rocket, used by the Navy to attack underwater targets from surface ships.

### **3-4 LAUNCHING METHODS**

#### 3-4.1 GENERAL

A rocket is primarily a powered, airborne vehicle. As such, it must have some point of departure, cr launching point. Rocket launchers have assumed many varied shapes and sizes, depending on system requirements and intended uses. The launcher supports the rocket and points it in the desired direction before launching. During the launch operation, the launcher guides the rocket in its first motion and prevents small disturbances from diverting it from the desired path. The launcher can also be used for other purposes, such as a packaging and shipping case, as a transporter, and for imparting other desired motions (such as spin) to the rocket during the launch phase. The paragraphs which follow describe the more common launchers and launching systems.

#### 3-4.2 RAIL LAUNCHERS

Rail launchers derive their name from their similarity to the rail of a railroad track. The rocket is supported on the rail with shoes which slide along the rail as the rocket moves forward. The launching shoes are usually a part of the. rocket and can be fixed, retractable, or jettisoned after leaving the launcher. Since the sliding motion occurs only over a few feet of travel, friction is usually not of critical concern. Rail launchers may have a number of variations, the most common of which are described below.

### 3-4.2.1 Single

Single-rail launchers have one rail along which the rocket moves. The rail must have sufficient width, and the launching shoes must be so designed that lateral, or rocking, motion is prevented or held to a minimum as the rocket moves over the rail.

#### 3-4.2.2 Multiple

Multiple-rail launchers may be interpreted in two ways. One concept is a launcher having two or more rails, each of which serves as the launch guidance for a rocket. The barrage-type rocket systems, which launch a number of rockets simultaneously, often use this launching scheme. On the other hand, a launcher with two or more rails can be used to launch one rocket. Such schemes are used to provide a more rigid launching support and, in some instances, to dispense with launching shoes. The rocket slides through the rail structure the same as it would through a tube.

#### 3-4.2.3 Helical

For this launcher concept, the rail is twisted through a helical angle in order to impart spin to the rocket. Generally, the helical rail launcher has two or more rails to provide a torsional couple to the rocket because it is impractical to impart a torsional couple with one rail. The technique is analogous to the rifling grooves in the bore of a gun or rifle. Unlike the gun, however, helicalrail launchers are not used for spin rates of sufficient magnitude to provide spin, or gyroscopic, stabilization. The spin produced is low in magnitude for the purpose of reducing errors resulting from some of the rocket imperfections. This is discussed more fully in Chapter 7.

### 3-4.3 TUBE LAUNCHERS

Rockets may be launched from tubes in much the same way as gun projectiles. The length of the tube can vary from about one rocket length to several rocket lengths, depending on the characteristics of the rocket, its intended use, the environment in which it will be used, and accuracy considerations. This tube can have a smooth

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bore or may be grooved in some manner to provide or prevent rotational motion during the launching. No launching shoes are required on a tube-launched rocket, although devices known as bore-riders may be used to support a portion of the rocket that is smaller than the tube. The bore-riders prevent the rocket from wobbling, or balloting, as it moves through the tube, and assure its continuing in the desired direction. Tube launchers may be designed to be reusable or may be designed to be disposable after the firing of one rocket. The latter is found quite often as a part of small rocket systems, particularly the small infantry antitank systems. This allows the individual soldier to discard unnecessary encumbrances on the battlefield. For similar reasons, disposable launchers are also incorporated in aviation rocket systems to permit the launcher to be jettisoned after use. The most common types of tube launcher are briefly discussed in the paragraphs which follow.

#### 3-4.3.1 Single

Single-tube launchers are generally used in hand-held or single-man-operated rocket systems and in some systems with automatic feed mechanisms. As with any rocket system, the choice of a single tube results from considerations of the system requirements and rocket characteristics.

#### 3-4.3.2 Multiple

Multiple-tube launchers are used to provide a fast firing rate where the complexity of automatic feed mechanisms in conjunction with a single tube is either undesirable or is prohibitive. With the employment of a multiple-tube launcher, the rockets can be fired all at once, in salvo, or in fast ripples. The ability to fire one rocket at a time is also inherent and can save considerable time by not requiring reloading after cach firing. Multiple-tube launchers are frequently employed as barrage weapons, replacing a number of guns concentrated in a small area.

#### 3-4.3.3 Open Breech

An open-breeck launcher is one where the rear end of the tube is completely open and is the

full diameter of the tube. This is the most common form of tube launcher. The gases exiting from the rocket are unrestricted in passing through and out the rear of the tube, and the tube experiences little if any reaction force.

#### 3-4.3.4 Closed Breech

A closed-breech launcher is one in which the rear end of the tube is completely closed. The gases from the rocket cannot escape, and pressure builds up between the closed tube-end and the rocket. This type of tube launcher experiences a reaction force, or recoil, similar to that of a gun. Tubes of this type are generally used in places where the rocket exhaust gases would be undesirable or dangerous if allowed to exhaust rearward. The tube launcher of a tank-mounted system is an example of the closed-breech launcher. In this instance, the rocket is loaded into the tube from within the tank but the racket exhaust gases, for obvicus reasons, cannot be tolerated inside the tank.

#### 3-4,3.5 Restricted Breech

A restricted-breech tube launcher is one in which the rear end of the launcher has been reduced to some diameter less than the bore diameter, but not sealed off completely. This form of tube launcher is used only in instances where some particular effect is desired. If the restriction is made in the form of a rocket nozzle, some useful forward thrust may be obtained that will counteract to some degree the recoil resulting from the restriction. The higher pressures resulting in the tube may be utilized to afford a higher muzzle velocity to the rocket without changing the rocket or increasing its size.

#### 3-4.3.8 Galling

As this name implies, the gatling launcher is derived from the old Gatling gun concept. It is a form of automatic feeding launcher since, as one or several rockets are firing, one or several are being fed into empty tubes. The tube cluster rotates so that those tubes firing are always at a fixed position, as are those being loaded. Several rocket systems have been designed around this type of launcher, using the closed-breech type of tube mentioned above.

#### **3-4.4 OTHER LAUNCHER TYPES**

In many instances the simple approach to a launcher design is not adequate. It then becomes necessary to examine techniques and designs that will provide a necessary function, a particular motion or effect, or will impari to the rocket some required characteristic. The result may be a modification of one of the types described in the preceding paragraphs, a combination of several types, or a completely new approach. It may be necessary to add varying degrees of sophistication, or to provide additional equipment or devices for a particular effect or function. One of the more notable to be is the zero-length launcher.

This launcher is, as its name implies, one that supports the rocket but releases it from constraints immediately, cr with zero guidance upon first rocket motion. It is not too practical in most instances to achieve a true zero-length guidance; however, guidance lengths of a fraction of an inch have been achieved for small rocket systems and several inches for large systems. The rocket must be adequately supported on the launcher and must maintain its aim alignment until it is launched. Mechanical considerations generally will dictate the size and length of the attaching devices and, consequently, the guidance length in zero-length launchers.

#### 3-4.5 VARIATIONS

#### 3-4.5.1 Autospin

As has already been stated, it is sometimes desirable to impart a slow spin to rockets in order to reduce or eliminate some types of error during the flight phase. One method of imparting spin that has been analyzed and tested uses in the rocket a device that spins the rocket warhead in one direction; the reaction spins the propulsion motor in the opposite direction. Spinning during the flight phase, or even before rocket motion occurs is desirable. Since simplicity is also important, the rocket is made to spin after it has traveled approximately one inch. In this case, the zerolength launcher is necessary, because the rocket

must be free of launcher constraints at the time spinning begins. It must be borne in mind that the thrust and acceleration characteristics of the rocket motor must be suitable to maintain the rocket in an acceptable flight attitude at this time, otherwise, the rocket may drop or deviate in such a manner as to make its flight meaningless.

# 3-4.5.2 Prespin, Automatic Dynamic-Alignment (PADA)

One effect of spinning a rocket is to cause the accrual of errors from dynamic unbalance. No rocket is perfectly balanced, and the center of mass will not lie exactly on the longitudinal axis. Even the longitudinal axis cannot be expected to be perfectly aligned since the rocket is usually made of components joined together. Consequently, the rocket will not spin these components around the longitudinal axis of symmetry, but will seek to spin about some other axis which is the dynamic axis. The rocket, if spun on a rigid launcher and attached to the launcher by rigid mounts. will be constrained to rotate around the longitudinal axis of symmetry purely from mechanical aspects. Once released from the launcher constraints, however, the rocket will seek immediately to spin around its dynamic axis, which results in errors along the flight path. The dynamics and errors resulting from this phenomenon are discussed in more detail in Chapter 7. The zero-length launcher with flexible arms supporting the rocket is one approach to gaining the beneficial effects of spinning the rocket before launching without the undesirable effects of jump at release of launcher constraints. This is more practical than attempting to design flexible shoes for the rocket. Zero length is the logical launch approach since it would be very difficult to provide flexible rails that would function in the desired manner during the guidance phase. The flexible launcher arms permit the rocket to find and align itself along its dynamic axis as it spins, and when launched, to maintain the attitude attained during the spin-up period. The critical consideration in this scheme is to make sure that the spin rate of the rocke, does not couple with the resonant frequency of the launcher arms. This can cause violent perturbations of the rocket and possible failure of the launcher structure. It

is desirable to stay below the critical rate or, if it is necessary to go above, to provide a spin acceleration sufficient to carry through the resonant point as rapidly as possible. The name ascribed to this launcher concept is prespin, automatic dynamic alignment launcher, or PADA (pronounced "Payday").

### 3-4.5.3 Spin-On-Straight-Rail (SOSR)

Although the effects of shifting axes produce undesirable results, prespinning a rocket before launch on a rigid launcher is nevertheless sometimes beneficial. The benefits derived overshadow the ill effects of dynamic unbalance sufficiently to justify the inflexible launcher. The rocket is thus provided with bearing systems in which it can rotate while on the launcher and then be launched along a rail in the usual manner. This technique has been termed spin-on-straight-rail, or SOSR. Although helical rails could be used, they may be undesirable because of length. weight, or other factors. Also, the spin rate desired may not be attainable with any reasonable rail length and helix angle. In the SOSR system almost any desired spin rate can be obtained. The method of spinning can be an integral part of either the rocket or launcher. The spin mechanism, if it is a part of the rocket, is usually a system of small rocket motors exhausting tangentially to the longitudinal axis. If the spin mechanism is a part of the launcher, it may be electrical, hydraulic, mechanical, or it may use whatever power source is most applicable. Power transmission to the rocket may be by belt, gears, or other appropriate means. The dynamic treatment of this technique is also covered in Chapter 7.

#### 3-4.6 METHODS OF TRANSPORT

Rocket launchers can be transported in many different ways, with or without rocket loads. The small infantry launchers designed for the individual soldier are usually hand-carried and strapsuspended, much the same as a rifle. Larger types may still be man-transportable by dividing the system into man-load components, although the assembled launcher when it is fired may have to be supported on a tripod or other appropriate

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base. The larger, heavier, artillery rocket launchers are mounted on wheels and towed behind a vehicle as a trailer, or are mounted on a vehicle that is then an integral part of the launcher system. The largest of these systems are frequently mounted on self-propelled, tracked vehicles to provide a maximum cross-country capability. The mobility characteristics of the rocket-and-launcher system are dictated by the system requirements and the rocket characteristics. Many of the mediurn and large rocket systems are required to be air transportable. Here the designer must be conscious of both weight and size if he is to achieve a system small enough to fit into modern transport aircraft and light enough to be carried. The aviation rocket systems are mounted on, and are an integral part of, the aircraft. Size, weight, and aerodynamic characteristics of the configuration are paramount. A high-drag design can slow an aircraft to the point where its vulnerability to enemy air and ground fire becomes acute. Rocket armament for a tank is also an integral part of its transporter. The factors for serious consideration with these systems are that of space in the tank and that of the burned gases from the rocket. 'The launcher designer must provide means of exhausting the gases, must provide adequate room for the tank crew to operate, and must provide means for handling and loading the rockets from within the tank. Considerable ingenuity is required to achieve an acceptable balance of space, weight, and safety for systems that are to be operated in such closely confined spaces.

### 3-5 SYSTEM ELEMENTS

### 3-5.1 GENERAL

A rocket system is made up of a number of elements, or subsystems, each of which performs a function necessary to the successful performance of the system. In general the system is composed of three main elements: (a) the rocket, (b) the launcher, and (c) the fire control device. Each of these in turn is composed of subelements, or components, each of which has a necessary function to permit successful operation of the whole.

In keeping with the intent and purpose of this handbook, only the rocket will be discussed in

detail. This is not to imply that the other elements are any less important, but they are more properly considered in other handbooks dealing with their particular disciplines. The launcher and fire control elements will be described sufficiently to permit an evaluation and appreciation of the particular problems attendant upon these elements. This approach is also taken with the payload, or warhead, of the rocket, which is covered in considerable detail in other handbooks. ţ

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#### 3-5.2 ROCKET

The rocket is composed of a payload, or warhead, a propulsion motor, and an airframe to provide structural rigidity. In the smaller, simpler rockets the warhead and propulsion motor serve also as the airframe, and no additional structure is required other than the fins or other device to provide aerodynamic stabilization.

#### 3-5.2.1 Warhead

The rocket warhead has a shell, or casing, which is hollow, and which may be aerodynamically shaped to serve as the nose of the rocket. An appropriate high explosive is loaded into the casing. Actuation of the explosive is performed by the fuze. The fuze may be located in a number of positions in the warhead structure, depending on its type and method of operatioon, and on the type of detonation desired. For high explosive warheads, the fuze may be placed at the forward tip of the warhead and may be actuated by striking the ground or another object. The shape of the warhead may take a number of forms, the selection usually being determined by the type of warhead, the aerodynamic characteristics and requirements for the rocket, the fuze type, and structural considerations. The warhead has two general parts, the shaped nose portion, or ogive. and a body, usually a cylindrical portion. The cylindrical portion may or may not be present, depending on the design requirements, but the nose or ogival portion is always used. The ogive may have a number of shapes. It may be conical; it may have curvature and be termed a tangent or secant ogive, or it may be hemispherical. Ogival shapes and their gerodynamic characteristics are covered in more detail in Chapter 8.

The material for the warhead casing is also selected according to requirements. It may be cast iron, steel, aluminum, or a combination of these or other materials. The material, in combination with the high explosive, is the destructive mechanism, and thus must have characteristics that will produce the maximum desired effect on the target.

Fuzes, as mentioned above, can be of several types. The point-detonating fuze initiates the explosive charge immediately upon striking an object. The delay fuze initiates a powder train that delays the actual explosion for a period of time ranging from several seconds to minutes, and in some cases to hours and days. The air-burst fuze is timed to actuate at some desired point in the air above or in the proximity of the target. Fuzes may also be located at the aft end of the explosive charge with an actuating device in the nose. On impact with an object, the actuating device generates an electrical impulse to initiate action of the fuze. For some aircraft rockets the warhead should penetrate and enter the aircraft structure before detonation. These warheads may use a coil-type actuator, located behind the warhead, which will generate an electrical impulse on passing through the metal structure. Fuzes for actuating the explosive charge may be simple, or may be intricate devices requiring the technical competence of a watchmaker to design, build, and assemble. These mechanisms, though precise, must be rugged and must perform well under the most trying conditions.

A necessary aspect of fuze design and functioning is that of safing and arming. The rocker warhead must be kept safe to handle, even to drop, without endangering personnel to accidental explosion. For this reason fuzes have built-in safety devices that must be actuated in some manner before the fuze can function. These safety devices range from simple pull wires, which are removed by hand just prior to firing the rocket, to intricate mechanical and electrical mechanisms that are actuated by the forward acceleration of the rock-In many instances, for safety reasons, the et. fuze should not be fully armed until the rocket has moved for some distance away from its launch point. For these cases the safing and arming device may be a small escapement mechanism (similar to that of a watch) that is actuated by the forward acceleration of the rocket, removing a blocking device between the fuze detonator and the high explosive.

For a full and comprehensive treatment of explosives, warhead design, and fuze types and design, the reader is referred to other handbooks in this series.

#### 3-5.2.2 Motor

The rocket motor is the engine that propels the rocket from the launch point to the target. For present purposes a general description of its components will suffice A more detailed coverage of its design is presented in Chapter 5.

The motor is an internal combustion engine with a combustion chamber, an orifice through which the burning gases are expelled at high velocity, and the propellant charge that produces the high-temperature high-pressure gases as products of the combustion process. Also included is the igniter which starts the combustion process in the chamber.

The propellant charge, or grain, is a mixture of a suitable fucl and an oxidizer. Thus, unlike most air-breathing internal combustion engines, a rocket motor does not utilize or need the surrounding air to operate. In fact, it can and does function equally as well in a vacuum or in outer space When the propellant charge is ignited, the heat generated causes a decomposition of the chemical compounds in its structure to produce combustible gases on the grain surface. The gases are burned, and the process proceeds in an orderly and predictable fashion. The products of the combustion process are high temperature gases and, in some cases, solids in suspension in the gases.

Propellant grains may be obtained in a large variety of compositions and shapes. Each is designed to operate in a specified manner and environment, the particular manner of operation is selected to fit the performance requirements. The grains may be cast directly into the motor combustion chamber, or may be molded or cast into a separate container that is loaded into the chamber as a cartridge. A grain may be end-burning, as a cigarette burns, or it may have perforations in which the burning occurs. Some motors, called multi-grain motors, may be loaded with a number of small grains. Generally the end-burning grains operate at low pressure over relatively long

periods of time, whereas the perforated grains operate at medium and high pressures for relatively short periods of time. Multi-grain motors are usually employed to provide extremely short burning periods at very high temperatures.

Grain compositions vary in operational characteristics. The more general types of fuel mixtures are single base, double base, triple base, and composite propellants. To the fuel is added the chemical oxidizer. Other chemical agents are added to the mixture to obtain desired performance characteristics. These agents act to inhibit or slow down the burning, to speed up burning, to stabilize the burning, to counteract or minimize temperature and pressure effects on the burning, and to produce other desirable effects.

Propellant compositions are in many instances developed to provide desirable physical characteristics. The propellant strength should be fairly uniform over wide temperature ranges, and its density and specific volume remain as constant as possible despite temperature change. Powdered metals are added to some propellants to raise the combustion temperature and the usable energy. The designer is concerned with obtaining the propellant with the highest possible density and energy per unit weight since these factors will provide the least weight and size of motor to do the required job.

The motor combustion chamber is a pressure vessel to contain the propellant and the high-temperature, high-pressure gases during burning. An opening is provided at one end through which the gases are expelled. The size of the orifice relative to the physical dimensions and burning characteristics of the propellant grain is governed by precise mathematical relationships and differs with types of propellant and operating conditions. The motor case may be constructed of any material capable of withstanding the prescure genera ed, but it is of primary interest to keep the weight to a minimum. For this reason, the very high-strength steels, high-strength aluminum, and the glass-reinforced plastics are most often used. Other metals, such as titanium and magnesium, have been used, usually to obtain some particular characteristic not afforded by the more common materials.

The motor exit-orifice, or nozzle, is designed to have precise geometric and mathematical relationships, both with the propellant grain and with the properties of the exhaust gases. The design usually is in the form of the De Laval nozzle with converging-diverging sections. The converging section, located before the throat orifice, is commonly called the expansion cone. Materials used in nozzle construction are generally the same as those used for the motor chamber. However, it is not unusual to employ a reinforced plastic nozzle with a steel or aluminum motor case. Sometimes the nozzle throat is lined with graphite. This material resists the erosive characteristics of the exhaust gases much better than most materials and it changes dimensions very little with changes of temperature. Because it is brittle and has little physical strength, this material must be adequately supported in the nozzle throat to prevent disintegration. Protective coatings of other types also are used to cover the entire inside surface. Particularly applicable to nozzles made of aluminum, the coatings provide a very hard, erosion-resistant surface. These coatings, too, are very brittle in nature and must be adequately supported to prevent disintegration.

Variations of the De Laval nozzle have been employed on rockets. They are designed to provide a particular effect on, or enhancement of, the motor thrust characteristics. The production costs for some of these variations may be appreciably higher than for the simple conical-section De Laval nozzle. Therefore, the effect to be gained must be weighed carefully against the added cost. One variation that has been of considerable interest and study is the plug nozzle. This is essentially an inside-out De Laval nozzle which has the characteristic of providing optimum or nearoptimum expansion characteristics for the exhaust gases at all altitudes, or, more properly stated, at all ambient pressures. Thus, this nozzle has the potential of performing equally as well at sea level as it does in the vacuum of outer space. It is not too difficult to build and should compare favorably with the conventional nozzle in cost and weight.

A necessary consideration for some types of rocket motors is that of insulating the case wall For the long-time, end-burner type of propellant grains, and for cartridge-type grains where the gases may impinge directly on the case wall, the loss of strength in the material can cause rupture and failure of the system. To prevent this occurence, an insulating lining that will prevent over-

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heating and loss of strength should be applied to the wall The material selected for insulation may be applied directly to the wall by painting, casting and curing it in place, or by other suitable Insulation may also be fabricated and means inserted into the motor case. The liner must be bonded to the wall with an adhesive since it will not function properly if the hot gases flew between the insulation liner and the wall. Insulating materials may be of several types. Some are charring in nature, others ablative. No one type is superior, some work best in one type of environment, others best in another environment. The best guide to selection is past experience and experiment The primary consideration is maximum effect for minimum thickness and weight since insulation reduces space available in a given chamber for propellant.

Some device is necessary to initiate propellant combustion in the chamber. The device that performs this function is called the igniter. Although It may take a number of forms, they all have the same general characteristics. The squib, a levice that receives the firing signal, may be electrical or mechanical, the latter usually being of the percussion type The electrical squib is in essence an electric match. The current passes through a resistance wire that becomes very hot, much as the cooking element of an electric stove. The hot wire ignites a small powder charge that generates hot gases. The hot igniter gases are directed against the propellant grain surface that is in turn ignited. The small container in which the igniter is housed is usually of a brittle or very flexible material, plastic in most cases, so that it may be easily ejected through the nozzle after propellant ignition. The igniter cup must not be permitted to block the nozzle throat as this would cause an extremely fast pressure rise in the motor chamber, resulting in chamber rupture.

Most propellants exhibit better ignition characteristics under pressures considerably higher than atmc.pheric. The surface of the grain igrites faster, and the flame front covers the entire burning surface much faster under elevated pressure. To provide this pressure condition a closure, called the nozzle closure, is placed in the nozzle throat. It is designed so that the igniter gases are not permitted to escape, but build up pressure in the combustion chamber. It is also designed to blow out of the nozzle at some predetermined pressure, usually lower than the operating pressure of the motor. The igniter cup may function also as the nozzle closure, or a separate closure may be provided. The closure may be of any suitable material, usually plastic or metal. It must exit at the desired pressure level and must be constructed in such a manner that .he nozzle or expansion cone will be undamaged as it leaves. For some aircraft rockets, the nozzle closure may be ejected at a fairly high velocity. If it were to strike a vital part of the aircraft, it could endanger both aircraft and crew. In such instances the nozzle closure should be made of a material that is very light and that preferably will disintegrate into a powder when ejection occurs. Other problems and environmental requirements may dictate that different materials and techniques be used in designing the nozzle closure.

#### 3-5.2,3 Structure

The rocket must have a frame of some sort to tie the parts together and to provide the desired aerodynamic shape. For the smaller and simpler rockets, the components themselves frequently constitute the airframe, being joined together by threaded sections, by bolts or screws, or by a simple crimping process. The components, warhead and motor, are shaped so that the desired aerodynamic configuration is obtained when they are joined. As size and or complexity increase, it may be desirable or necessary to provide a properly configured frame that will enclose the functional co.nponents. The warhead need be shaped only from a maximum effectiveness standpoint. and the motor for maximum performance. One or both may be enclosed in the airframe, depending on the particular system requirements.

The skin of the airframe is made of a lightweight material, usually aluminum or reinforced plastic. It may be shaped by drawing, hot or cold, by rolling and welding, by stretch forming, or by any other appropriate process. The particular forming process used is the result of considerations of raquirements, materials, and economics. The skin is supported on a framework consisting of bulkheads and, in some cases, stringers. The store elaborate the structure becomes, the more stringent become the requirements for close tolerances, alignments, positioning, and shaping. For a fully enclosed system, the components are tied to sev-

eral key bulkheads; where only part of the components are enclosed, they may be attached to bulkheads and/or the nonenclosed member.

For some types of rockets, several propulsion motors are used in a cluster. This arrangement provides the capability for obtaining different thrust levels by firing varying numbers of the motors to meet varying operational conditions. The clustered motor configuration is one that is usualiy fully enclosed within the airframe.

The rockets of immediate concern in this handbook are the free-flight aerodynamically stabilized rockets. The component that provides the aerodynamic stabilization is most often a set of fins located at the aft end of the airframe. Other means of aerodynamically stabilizing a rocket have been used and a number of proposed methods have been studied. The functional action of fins and other aerodynamic stabilization methods are covered in considerable detail in Chapters 7 and 8.

In order to stabilize a rocket along the flight path, a minimum of three fins, equally spaced circumferentially around the body, is required. The more usual configuration has four fins; however, as many as six and eight have been used to satisfy a particular set of environmental requiremen 3. Generally the fins are either rectangular or triangular, with any number of variations of these. They may be mounted normal to the rocket centerline, or tangential to the airframe. They may be fixed or, if necessary, folded, in which case they open after the rocket is launched. They may open due to rocket acceleration or may be opened by some mechanical device such as springs, pistons and cylinders, or other appropriate means. Folding may be radial or longitudinal; for the latter, they are either forward folding or rearward folding. For some rockets it may be necessary to curve the fins to the same curvature as the airframe to provide a smooth contour prior to launch. This is especially true for some tube-launched rockets where restrictions of size and weight are imposed and where there is insufficient space to mount other types of fins.

The size and configuration of the fin are determined from a comprehensive study by the aerodynamicist of the flight path environment, the performance characteristics, and the configuration of the body of the rocket. As mentioned, the available space, launching technique, and weight restrictions also play important roles in designing the fin planform.

The method of attaching the fins to the airframe is again determined from physical and mechanical considerations of the particular system. They may be welded, riveted, boited, screwed, or cemented on. It is often desirable to mount them with a small cant angle to the rocket centerline so that the aerodynamic reactions on the canted fins will produce a roll in the rocket.

The rocket must he attached to the launcher, except in the tube launcher, where the rocket merely slides through the tube and no special attachment devices are required. Other types of launchers such as rail launchers use a connecting device, or launching shoe, to constrain the rocket to move in a precise and predetermined manner during the launch operation. The number of shoes required is determined 1, the size of the rocket and the degree of completty of launching motion imparted y the launchei to the rocket. For most rocket a minimum of two shoes is usually adequate, particularly where the motion is simply a straight, nonrotating movement along the rail. The shoes may be fixed permanently to the rocket, may be folding or retractable, or may be of an ejection type.

Other devices are at times included in a free rocket system to provide some desirable or necessary function. One frequently employed is a mechanism to produce slow spin is the rocket prior to or immediately after launching. This mechanism ranges from the small canted vanes in the exhaust nuzzzle of the rocket that react to the exhaust gases, to complex devices such as gear trains, drive shafts, pistons operated pneumatically through helixes, and other similar .ystems. Other devices for providing spin may be a component that (a) must be tied into the locket system by the airframe, (b) may be a part of the airframe, or (c) may be a simple attachment-whatever the device, it must have proper consideration and emphasis in the overall structural assembly. In addition, the effect of the spin produced must be considered along with the aerodynamic and acceleration forces when analyzing the structural integrity of the airframe and component assembly.

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### 3-5.3 LAUNCHER

The launcher, like the rocket, consists of several components each of which performs a function to provide the total required performance (see par. 3-4 above). Many of the terms used for launcher components have been carried over from artillery practice since much of the design and development work has been done by gun designers. The similarity between a rocket launcher and an artillery field piece is in many instances quite evident, the gun tube being replaced by the launcher rail. Only a brief description of the three basic launcher components will be given since this subject is more properly covered in other texts and handbooks.

The *launcher rail* is the component on which the rocket rests and which guides it in its first motion of travel. The rail may take any number of forms and may also be a tube through which the rocket slides. It must have sufficient strength to support the rocket and must be sufficiently rigid to prevent successive deflections and oscillations that could cause mallaunch of the rocket.

The launcher rail is supported on an upper carriage through a trunnion connection. This is the joint that provides for the angular elevation and depression of the rail, or change in quadrant elevation, nece sary to achieve varying ranges for the rocket. If the rocket system is large, a means of assisting the elevation change—through gear trains, hydraulic pistons, or other suitable means —may be necessary. The assist mechanism may be manually operated or may be mechanized for remote control, faster operation, or for lessening the burden on the launcher crew.

The launcher rail and upper carriage assembly is mounted on a *lower carriage* through a vertical pin connection around which it can rotate. This provides the change in azimuth, or direction of fire. Manual operations or mechanized means of assisting the motion may be provided. The lower carriage also torms the base of the launcher. It may have wheels mounted to it for towing behind a vehicle; it may be mounted on a wheeled or tracked vehicle as a self-propelled unit; or it may, for small rocket systems, have legs or a base to stand directly on the ground.

Other equipment that may be a part of the launcher to provide a specific function or capability includes devices for imparting spin to the

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rocket; the firing mechanism, either electrical or mechanical; and cranes or hoists to assist loading the rocket on the bil for the larger systems.

Launchers may consist of less than the three basic components-rail, upper carriage, and lower carriage-but, of course, must always have the rail or other device for supporting or guiding the rocket. For the antitank rocket systems of the bazooka type, where the launcher is a tube supported on the man's shoulder, the other components do not exist; the flexibility of the man provides the necessary motion capability for changing azimuth and quadrant elevation. In other systems the carriages may not exist as such being reduced to nothing more than pinned joints or very simple support members. When the system is self-propelled, the vehicle on which it is mounted may constitute the lower carriage; however, it would not be identifiable as such if the launcher were removed. The particular system and the dictates of the system requirements will determine how the launcher rail is to be supported and how the required motions are to be provided.

#### 3-5.4 ANCILLARY EQUIPMENT

Many rocket systems require items of specialized equipment necessary to effect total operation. Military systems are required to have the capability of functioning in all types of weather and terrain conditions anywhere in the world. Some rocket components, such as propellant grains, may be limited in their operational characteristics by temperature or some other factor. In order to provide total capability, it is at times necessary to provide some piece of equipment to aid, facilitate, or accomplish some function to offset the restrictions. In the case of the propellant grains that arc temperature-limited, a heating blanket is provided that can be wrapped around the outside of the motor case. This blanket has electric resistance heating elements very similar to those found in commercial electric blankets for home use.

### **3-6 CONCEPT SELECTION**

#### 3-6-1 REQUIREMENTS

The need for a new weapo, system becomes established when a situation that cannot be

handled by existing weapons is encountered either in actual battle or by projection of what is expected to occur in future conflicts. When the need for a weapon becomes apparent, a set of general requirements can be established that will satisfy the needs. The requirements might be in the form of the amount of explosive force required to destroy the objectives as well as the mobility of the weapon and any adverse condition that might hinder its use. For instance, a requirement might exist for a weapon system that could destroy a 'arget of defined size and hardness in a mountainous environment.

These general requirements for weapon sysiems are usually dorumented and made available to various groups for conceptual studies. At this point parametric studies are made of a wide range of concepts that might meet the requirements. The purpose of these studies is to determine whether the weapon should be a gun, mortar, rocket, etc., and whether the concept lies in the present or foreseeable state-of-the-art.

The end results of the conceptual studies are: the definition of the weapon system; specification of acceptable limits in range, weight, accuracy, etc.; and establishment of problem areas. These requirements are documented and used as the basis for the preliminary design of the weapon system.

#### 3-5:2 CONSTRAINTS

It is not usually possible to proceed directly into the selection of the weapon concept. Circumstances beyond the control of the designer always exist that prevent him from achieving the weapon performance he desires. Inevitably, there are components of each system concept whose performance is limited by the state-of-the-art to something less than required. Therefore, constraints are imposed within which the analyst must work.

There are two alternatives. The time allowable for the development of the weapon may permit components to be included that are outside the present capability of these components but are considered feasible within the development time of the weapon. Thus, a prediction of future component availability is made that is based on present research and expected results. In this case, the analyst is taking the chance of having to extend the time required to put the weapon in the field should unforeseen problems appear in developing the component. In fact, it is possible that the required performance cannot be achieved, and the weapon system may suffer more than it would have if existing components had been specified at the beginning.

The second alternative is to restrict the selection of components to those that are unmediately available. In this situation the analyst is attempting to reduce development time at the cost of system performance. Naturally, considerable thought must be given to either approach so that the best possible weapon can be obtained in the time available.

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#### 3-6.3 PARAMETRICS

The requirements and components having been specified, a range of weapon concepts is considered that will satisfy them. The performance of each system is studied in terms of parametric variations of the important system variables. In this way it is possible further to identify problem areas and to understand the sensitivity of the overall system performance to changes in the performance of critical items. These studies pave the wa, for detailed trade-offs and the selection of the concept that best meets the requirements.

#### 3-6.4 SYSTEM SELECTION

The results of the parametric studies allow cach weapon concept to be compared to all others. Weighting factors can be applied to the advantages and disadvantages of each concept. Finally, a concept is selected; the system is then defined as a rocket, gun, etc.; and its acceptable performance is specified. These specifications are documented and released for the preliminary design of the weapon system.

#### **3-7 PRELIMINARY DESIGN**

The preliminary design phase, like all the other stages of the development of a weapon system, is simply a more detailed refinement of the work that preceded it. The overall process consists of

a continuous review and rework of the design. The depth of the refinements increases, until the final phase when the requirements for each rivet have been established.

We will assume for the remainder of the chapter that the weapon system is a free rocket.

#### 3-7.1 PAYLOAD

The conceptual design phase establishes the function of the payload and the limits of its size and weight. During the preliminary phase, more detailed questions are studied such as the nature of the device to accomplish the objective (antipersonnel, hardened site doutruction, armor penetration, etc.) as well as more exact determination of the size, shape, and weight.

### **3-7.2 PROPULSION**

In the preliminary design of the propulsion system, parametric studies are made to determine the required thrust of the rocket motor, its specific impulse, total impulse, burning rate, etc. Studies are made of zvailable propellants and grain cross sections. In this process problem areas may be uncovered that require further study.

Detailed accounts of the methods used to determine the required motor performance and the design of the motor elements are presented in Chapters 4 and  $\frac{15}{5}$ .

#### 3-7.3 AERODYNAMICS

Acrodynamic shapes must be developed that will contain the payload and motor while keeping drag to a minimum. In addition, the amount of aerodynamic stability required by the mode of operation of the weapon must in established. The amount of stability required is affected by any dispersion reduction techniques that may be employed. These subjects are discussed in Chapters 7 and 8.

In addition to drag and stability considerations, the preliminary aerodynamic analysis must consider the aerodynamic heating tunt is encountered in high speed flight. The results of these studies determine the requirements for insulation and ablative materials.

#### 3-7.4 DYNAMICS

Estimates of the accuracy must be made. Parametric studies are made of the accuracy available with different launcher lengths and levels of stability, as well as spin or other dispersion reduction techniques. Problems associated with launcher requirements and spin methods are identified. In addition, manufacturing tolerances on static and dynamic balances are established.

Computations are made of the dynamic loads under all conditions to which the rocket is expected to be subjected.

#### **3-7.5 STRUCTURES**

A tabulation of the weight and balance characteristics of all the preliminary design configurations under consideration must be constantly kept up to date. In addition, the information from the dynamics analysis must be used to define the proper sizing of all the structural ele ments.

The preliminary aerodynamics analysis will place requirements on any insulation material that must be considered in the structural analysis. Problems in weight and balance must be identified as early as possible so that a wide range of structural materials may be considered.

#### 3-7.6 PERFORMANCE ESTIMATES

Each preliminary design configuration must be evaluated for performance. Comparisons are made between the systems, and changes are defined. The preliminary performance estimates are the basis for important design modifications.

#### 3-7.7 AUXILIARY DEVICES

The preliminary design phase defines the requirements for devices that are not considered a part of the primary rocket system but are necessary for its operation. Such devices are: heating blankets for propellant temperature control, anemometers for field wind measurements, and firing equipment and other devices that might be required to perform functions unique to a given system.

### 3-8 DESIGN OPTIMIZATION

It was mentioned above that the design process is repetitive. The conceptual and preliminary design phases involve similar computation, the only difference is the amount of detail that is included. However, the consideration of some of these details may invalidate or at least modify some of the preceding recults. These detailed considerations are possible because the gross factors have previously been identified. This allows individual areas to be studied in depth. The optimization process is the consideration of the design details and the combination of these details in such a way that cost, performance, and reliability are optimum.

### 3-9 SYSTEM INTEGRATION

System integration is first accomplished during the concept phase design. Estimates of the design and performance characteristics of various elements of a total system are integrated to make up a hypothetical design. An infinite number of design options are available. Components or elements in a range of sizes may be assembled in combinations to make up various configurations. The design and performance characteristics of each selected component or element affect the design and performance characteristics of each of the components or elements of the overall rocket. The selection and integration of these elements, therefore, involve the resolution of numerous design compromises and the formulation of numerous design decisions. The objective is to select and integrate those elements that provide the best promise of achieving system performance requirements, with high reliability and minimum cost by some specified availability date.\*

As design and development progress, the design of each subsystem becomes more specific.

Throughout this period, coordination must be accomplished among the design groups to assure compatibility and to resolve design compromises. A propulsion design group may desire a high chamber pressure to provide higher engine performance. The structural design group may desire lower pressure to save structural weight. These are the obvious considerations of the problem and do not represent all considerations that must be made. The total range of possible chamber pressure must be investigated with respect to effects on all systems and total rocket performance. The objective is to determine the pressure that results in maximum overall rocket performance within cost and schedule limitations. Similar compromises must be resolved in all areas of rocket design. Each must be made on the basis of performance of all elements and the total rocket, and must include considerations of cost, schedule, performance, and reliability.

As the design becomes more refined, the design and performance estimates must be altered. Mission requirements, and the design and performance characteristics of various elements change. Payload weight may increase; mission profiles may change. A problem may occur during the development of an engine, resulting in lower than anticipated thrust. Structural weight, rigidity, etc. may vary from that originally planned. Product improvement proposals may be presented that alter the design and performance characteristics of various systems. Since the design and performance characteristics of each element affect or interact with the design and performance characteristics of each of the other elements, each alteration of original estimates requires reintegration of the locket system. As in the problem of integrating the original rocket design, numerous solutions to each integration problem are possible. Any of several approaches can be employed to meet increased mission requirements. Numerous redesigns can be initiated to regain a performance loss due to failure of a system to meet expectations. Evaluation of a produced improvement proposal may present several design alternatives. Once again, the objective is to select that approach that best meets project objectives of performance, cost, reliability, and schedules.

Any of numerous design changes may be employed to meet increased mission requirements.

<sup>•</sup>The manufacturing, operations, maintenance, and logistics problems and costs associated with each candidate design must also be considered, and can easily be controlling factors in the selection of design options. Fixed and variable costs for anticipated launch rates etc. must be considered. However, this handbook is concerned primarily with the integration of the rocket system, particularly with respect to design and performance characteristics and design and avelopment costs and schedules of rocket systems. Therefore no extensive discussion of manufacturing, operations, maintenance, and logistics factors is included.

Upon development of a design problem, such as an engine that will not produce desired thrust, several redesign alternatives must be considered The alternative that offers the best promise of restoring the original performance with minimum cost and schedule impact must be established. Each proposed product improvement change must be evaluated on the basis of effect on all rocket systems, overall vehicle performance, cost and schedule impact of the change, etc. System integration, therefore, must be accomplished constantly throughout design and development.

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In summary, system integration is first accomplished during conceptual design. Throughout the remainder of design and development, design compromises must be resolved and design options must be selected. Mission requirements change, and design and performance characteristics of various elements of the rocket change. Each of these changes may require reintegration of the total design. For each reintegration problem, there are numerous alternate solutions or approaches to reintegrating the system. The objective is to ensure that the selected approach best meets performance and reliability requirements with a minimum cost by a delivery date.

### 3-10 TESTING METHODS

Before a rocket system can be released for use in the field, it must undergo a series of rigorous tests that verify its performance and integrity. Testing, therefore, is also a part of the development process. Aerodynamic testing of scale models, as well as characteristics, structures, and materials, help to establish the rocket configuration by supplementing theoretical analyses.

This paragraph discusses the role of testing in the development of the rocket system. More detailed coverages of testing methods are available in other parts of this handbook and in the cited reference material.

#### 3-10.1 STATIC TESTING

Static testing is primarily a check of the rocket motor performance that is accomplished by tying down the rocket so that it cannot move. The test rocket may be actual flight hardware or a boilerplate model that has a structure designed to permit firing the rocket motors without the danger of damage.

Static testing permits the use of extensive instrumentation. The testing can be carried out under closely controlled conditions. For these reasons static testing reveals much about the detail characteristics of many of the rocket system components. However, many of the conditions . countered in flight, such as aerodynamic and dynamic loads, are not present.

#### 3-10.2 FLIGHT TESTING

Final evaluation of the rocket system performance, as well as some phases of development, can only be accomplished by actual flight.

Development flight testing consists of making final adjustments of the aerodynamic configuration to provide the required stability. Study of the rocket on the launcher determines if the releasing mechanism and rocket clearances provide satisfactory initial conditions for the flight. Spin systems require extensive development testing, especially those whose ignition timing is critical, such as the Spin-Buck concept.

The final phase of testing is the performance testing where range and accuracy are compared against the expected values. Range testing is straightforward and consists of firing rounds at various quadrant elevations and propellant grain temperatures. However, a precise knowledge of atmospheric conditions is required. Extensive meteorological data are collected over the entire flight trajectory. Measurements of winds, temperature, and density are made on the ground and at altitudes along the path of the rocket.

Accuracy testing requires many rockets to be fired so that the impac points can be combined statistically to determine operational accuracy. Atmospheric effects are eliminated by firing the rockets in pairs.

#### 3-10.3 STRUCTURAL TESTING

The complexity of rocket structures makes it difficult to predict the structural strength of a design with sufficient confidence. The available analytical methods are inadequate to consider

the effects of stress concentrations, fasteners, bonding materials, etc. The heavy loss in performance caused by excess structural weight makes it important to keep the structure as light as possible. Therefore, the design process for rocket structures is a combination of predictions, based on results of theory and past experience with similar structures, and of verification by testing.

Chapter 6 presents a more complete discussion of structural testing methods.

### 3-10.4 AERODYNAMIC TESTING

The design of the aerodynamic configuration requires the development of a shape that will provide adequate volume for the payload while obtaining minimum drag. In addition, the accuracy requirements determine a specific level of aerodynamic stability. Aerodynamic testing, like structural testing, is a process of theoretical prediction and verification. Aerodynamic testing is thus an integral part of the development process.

A more complete discussion of aerodynamic testing methods is presented in Chapter 6.

#### 3-10.5 ENVIRONMENTAL TESTING

Military rockets must be able to operate under a wide range of climatic conditions. Investigation of the effects of temperature, humidity, and other environmental influences, such as sand and rain, on the deployment and firing of the rocket system plays a very important role in determining its value as a field weapon. Some propellants smoke excessively under humid conditions. Most solid propellants must be heated by special blankets in cold climates. Factors such as these must be identified before a weapon is ready for use in any given area of the world.

#### **3-11 COST EFFECTIVENESS**

Cost effectiveness might be thought of as getting the most performance for the money spent on a rocket system. However, the concept is much more complex. There are many factors that must be considered before a value can be attached to performance. The cost of developing higher levels of performance must be considered in relation to time and money. Often performance becomes all-important. For example, the need for a rocket of a given capability might be so great that any cost is justified. Other situations may justify sacrificing performance potential to meet an urgent time requirement. Another possibility is that the highest level of performance possible is not needed to satisfy the existing requirement. The framework within which these cost-performance trade-offs are made is called the design economy. Under war conditions, time and performance are of utmost importance; cost plays a relatively minor role.

It should be emphasized that cost effectiveness is not so much a design method as an awareness of the relationship between cost, performance, and reliability. Cost effectiveness is the conscious evaluation of the trade-offs between these items according to a set of established ground rules throughout the design of a rocket system.

Increased performance capability does not necessarily indicate greater probability of destroying a target. The reliability of weapon systems usually decreases with increased performance since performance is usually gained at the cost of complexity.

Another consideration is the evaluation of the importance to be given the accuracy of the system. From a cost effectiveness standpoint it may be more desirable to fire several rounds of a less accurate weapon than to pay the increased cost of developing a more accurate weapon that may require only one round.

The cost and reliability of a weapon system can be significantly affected by the concentrated effort of the people involved in the design and manufacturing process to avoid mistakes and waste. The Army has called attention to this fact in its Zero Defects program. The time and money saved by avoiding the repetition of work because of errors reflect directly in the cost of the weapon and its availability for use against an enemy.

# **CHAPTER 4** PERFORMANCE PARAMETRICS

### LIST OF SYMBOLS

Symbol

Symbol

Meaning Ballistic coefficient parameter  $(\overline{id^2})$ , psi

- С C' Modified form of ballistic coefficient  $\frac{W_{PL}}{W_{PL}}$ psi
- $C_D$ Drag coefficient of projectile, nondimensional
- CDSTD Drag coefficient of a standard projectile, nondimensional
  - Maximum diameter of projectile, in. d
- $\frac{\pi}{4}$  $d^2$ Reference area for aerodynamic coefficients, in.<sup>2</sup>
  - Thrust of booster motor, lb
- $F_{\mathcal{B}}$  $F_{\mathcal{S}}$ Thrust of sustainer motor, lb
- Gravitational acceleration constant, ft/sec<sup>2</sup> g
- Drag form factor  $(\underline{C_D})$ , nondimensional

- Total impulse of booster motor, lb-sec  $I_{B}$
- Ĩs Total impulse of sustainer motor, lb-sec
- $I_{sp}$ Specific impulse delivered by rocket motor, sec
- in; In Natural logarithm

**P**WF Propellant weight fraction, the ratio of propellant weight to loaded motor weight  $\left(\frac{W_P}{W_{O-W_{PL}}}\right)$ , nondimensional

- Keoning
- Growth factor, the ratio of gross weight to Q payload weight  $(\underline{W_0})$ , nondimensional W<sub>PL</sub>
- QE Quadrant elevation, or launch angle measured from horizontal, deg

$$\begin{array}{l} Booster \ mass \ ratio, \ the \ ratio \ of \ gross \ rocket \ weight \ to \ total \ weight \ without \ propellant \ \left( \frac{W_0}{W_0 \ - \ W_p} \right), \ nondimensional \end{array}$$

- R Range, km
- Range to target, km R<sub>T</sub>
- Booster burning time, sec t<sub>B</sub>
- Time to target, sec  $t_t$
- Velocity increment imparted by booster,  $V_B$ (burnout velocity) fps
- Velocity increment by booster in absence V<sub>IDEAL</sub> of drag and gravity, fps
  - ł Weight, lb
  - H<sub>B</sub> Weight of rocket at burnout, lb
  - Initial or gross weight of rocket, lb No
  - Propellant, weight, lb ₿<sub>₽</sub>
- ₩<sub>PL</sub> Payload weight, lb
- Summit altitude, ft Y<sub>MAX</sub>

No. of Lot

### **4-1 INTRODUCTION**

In the design of any rocket system, the determination of performance parametrics is a necessary first stop since these define the relationship between the performance requirement and physical characteristics. Performance parametrics not only serve as the basis for trade-off considerations among competing requirements and characteristics, but they also serve to show the sensitivity of the rocket's physical characteristics to variations in performance requirement, propulsion system efficiency, aerodynamic characteristics (primarily drag), and energy management technique.

It is not possible, in a handbook of this scope, to present parametric performance dat which will cover every conceivable situation. The purposes of this discussion, therefore, will be to call attention to those parameters which affect the performance of a rocket; to illustrate various approximation techniques; and to present a limited amount of parametric performance information.

The discussion will be limited to items necessary to define the relationships between performance and physical characteristics for the following types of rocket:

a. Indirect-fire, or surface-to-surface artillery rockets

b. Direct-fire rockets of the type normally employed in antitank or similar roles

c. Sounding rockets which are launched vertically for the purpose of reaching extreme altitudes

d. Surface-to-air rockets for an interceptor role

### **4-2 PERFORMANCE PARAMETERS**

The parameters, or variables, that are considered in the evaluation of the rocket's performance can be divided into three major categories:

a. Those factors associated with performance such is payload, velocity, range, altitude, time of flight, and launch angle

b. Factors associated with the propulsion system such as energy management technique, specific impulse, thrust, burning tirue, and propellant-weight fraction c. Aerodynamic considerations such as shape, means of stabilization, drag characteristics, and diameter

### 4-2.1 PERFORMANCE FACTORS

Generally speaking, those factors associated with performance will be specified as fixed conditions for the solution of a given problem, with the possible exception of launch angle (an the case of indirect-fire artillery rockets) and time of flight.

#### **4-2.2 PROPULSION SYSTEM FACTORS**

With regard to the propulsion-system variables, it is necessary to examine the effects of variations in the following:

- a.  $I_{sp}$ : specific impulse delivered by the rocket motor
- b.  $F_R/W_0$ : ratio of booster thrust to rocket takeoff weight (a measure of boost phase acceleration)
- c.  $F_S/F_B$ : ratio of sustainer thrust to booster thrust
- d.  $I_S/I_B$ : ratio of sustainer total impulse to booster total impulse
- e. PWF: propellant weight fraction (ratio of uzable propellant weight to loaded motor weight)
- f. Time and duration of propulsive force application

Determination or selection of optimum values of the propulsion-system variables for a rocket system is called energy-management. Energymanagement determines the magnitude of the boost and sustainer thrusts. and their duration. It also considers the duration of coast periods. The objective of energy-management is to deposit the payload at the target with a minimum expenditure of propulsive energy while meeting performance, ccst, and reliability requirements.

#### 4-2.3 AERODYNAMIC CONSIDERATIONS

With regard to the aerodynamic considerations, it is generally assumed that, for the types of rockets being discussed, drag is of paramount concern. Discussions of the effects of drag on projectile trajectories are given in Reference 1. It shall suffice here to say that the effects of drag

on the trajectory are the functions of the drag coefficient *i*, the mass of the projectile *W*, and the diameter of the projectile *d*. The ballistic coefficient parameter given in Reference 1 is  $C = W/id^2$  and is useful in describing the effects of drag on the rocket during the post-burnout flight phase.

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Although the ballistic coefficient is a useful parameter for the determination of drag effects for the post-burnout trajectory phase, it is not useful for the propulsive phase of the trajectory because of the effects of thrust and weight changes. In the compilation of parametric performance data, it is more convenient to work with a modified form of the ballistic coefficient C, defined as  $C' = W_{PL}/id^2$ , where  $W_{PL}$  is the payload weight in pounds. This form of the ballistic-coefficient parameter is more convenient to use because the rocket payload is usually specified as an initial condition, as opposed to the situation for artillery projectiles where the weight of the complete projectile is specified.

Performance parametrics provide data relating performance to physical characteristics. Weight is the principal physical characteristic with which the rocket designer is usually concerned. This discussion will therefore be limited to the weight consideration. although other physical characteristics-such as length, diameter, or volume-may sometimes also be limiting factors. The weight parameter for a rocket design may be stated in a nondimensional form, as the ratio of rocket gross weight to payload weight. This rails is designated the growth factor Q because it indicates to the designer how much his rocket must weigh in relation to the payload, or how much the overall weight must "grow" to account for unit increases in payload. The growth factor is useful, not only as a nondimensional measure of the weight of the rocket, but also as an indicator of the efficiency of the chosen method of delivery; a low growth factor indicates high efficiency.

## 4-3 APPROXIMATION TECHNIQUES AND APPLICABLE EQUATIONS

#### 4-3.1 ESTIMATION OF VELOCITY REQUIREMENT

Where the effects of drag can be estimated accurately or neglected without undue effect,

It is possible to estimate the velocity increment that the propulsion system must impart to the payload. It is then a simple matter to calculate the size of the propulsion system required. There are various methods for estimating the velocity requirement, depending upon the application, and the degree of accuracy desired. These are discussed in the paragraphs which follow.

#### 4-3.1.1 Indirect-Fire Systems

A crude approximation of the velocity requirement for the indirect-fire rocket is given by the drag-free range equation

$$R = \frac{V_B^2 S cn (2QE)}{g}$$
 (4-1)

which, for the optimum launch angle of 45<sup>°</sup>, yields the required velocity increment

$$V_B = \sqrt{Rg} \qquad (4-2)$$

In the above equations, R is the range;  $V_B$  is the velocity increment imparted by the booster; QE is the quadrant elevation, or launch angle, measured from the horizontal, in degrees; and g is the gravitational acceleration constant. Any consistent set of units may be used.

While the drag-free approximations are adequate for preliminary work on most rocket systems, the relatively greater effect of drag on the indirect-fire system often requires a more accurate calculation. This can be obtained through use of ballistic range tables (Reference 1), which introduce the effect of drag in the form of the ballistic coefficient  $\#/id^2$ . Fig. 4-1 presents the relationship between range, burnout velocity and ballistic coefficient, taken from Reference 1. Since the ballistic coefficient is not independent of burnout velocity, the use of Fig. 4-1 requires an iterative procedure for any given payload and diameter. Flowever, these data are extremely useful for rapid, accurate estimation of performance parametrics for high acceleration, surfaceto-surface rockets.

#### 4-3.1.2 Direct-Fire Rockets

If we asume that the effects of drag can be accounted for, it is usually a simple matter to determine the velocity requirement for a direct-



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fire rocket, based on the range to the target  $R_T$ , the desired time of flight  $t_i$ , and the desired burning distance or time  $t_3$ . In the absence of drag, the velocity requirement for a constant-acceleration boost phase is

$$W_{\rm B} = \frac{R_{\rm T}}{t_{\rm t} - \frac{1}{2} t_{\rm B}}$$
(4-3)

Although this equation neglects the effects of drag and gravity, it is useful for approximation.

#### 4-3.1.3 Sounding Rockets

In the absence of drag, the summit altitude  $Y_{MAX}$  reached by a vertically launched projectile is given as

$$Y_{NAX} = \frac{V_B^2}{2g} \tag{4-4}$$

Therefore, an approximation of the required velocity would be

$$V_B = \sqrt{2g} Y_{WAX} \tag{4-5}$$

### 4-3.2 ESTIMATION OF ROCKET MOTOR REQUIREMENTS

If we can assume that a sufficiently accurate estimate of the velocity requirement is achieved by use of any of the methods described above, we can calculate the weight of the rocket using the relationships defined below.

#### 4-3.2.1 Specific Impulse and Booster-Mass Ratio

The relationship between rocket weight, specific impulse, and propellant weight is given by the "ideal" velocity equation

$$V_{IDEAL} = gI_{sp} \ln \left(\frac{W_0}{W_0 - W_p}\right) = gI_{sp} \ln (r_B)$$
(4-6)

where  $I_{sp}$  is the specific impulse delivered by the rocket motor in seconds,  $W_0$  is the initial or gross weight of the rocket in pounds,  $W_p$  is the propellant weight in pounds, and ln is the natural logarithm. The ratio  $W_0 / (W_0 - W_p)$  is commonly referred to as the booster-mass ratio  $r_B$ . This relationship is illus rated graphically in Figure 4-2.

#### 4-3.2.2 Propellant-Weight Fraction

If we consider the rocket to consist of two major components-the paylcad and the rocket motor-we can define the gross weight as

$$W_0 = W_{PL} + \frac{W_P}{PWF} \qquad (4-7)$$

where PWF is the propellant weight fraction  $W_P/(W_O-W_{PL})$ , nondimensional, and the burnout weight as

$$W_B = \dot{W}_L + \frac{W_P}{PWF} - W_P \qquad (4-8)$$

The booster-mass ratio can then be expressed as

$$r_{B} = \frac{W_{O}}{W_{O} - W_{P}} \cdot \frac{W_{O}}{W_{B}} = \frac{W_{PL} + \left(\frac{W_{P}}{PWF}\right)}{W_{PL} + \left(\frac{W_{P}}{PWF}\right) - W_{P}}$$
(4-9)

#### 4-3.2.3 Growth Factor

Eq. 4-9 can be reduced to a form which expresses the weight of the rocket in a nondimensional form (growti factor Q) as follows:

$$Q = \frac{W_0}{W_{PL}} = \frac{r_B (PWF)}{1 - r_B (1 - PWF)}$$
(4-10)

### 4-3.3 SUMMARY

The relationship among growth factor, propellant-weight fraction specific impulse, and velocity requirement is illustrated in Figure 4-3. Information of this type is useful since it illustrates the sensitivity of the rocket weight (for any given performance level) to variations in specific impulse and propellant-weight fraction.

It should be remembered that the equations developed in paragraph 4-3 are only crude approximations of the representations of rocket performance described in the paragraphs which



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follow. Nevertheless, they are extremely valuable in the preliminary design of any rocket. As demonstrated in the example problem at the cad of this chapter, these relationships are used in the early phases of design to establish the approximate values of the important rocket variables such as  $I_{sp}$  and growth factor. These values will determine if the design requirements are inconsistent with the state of the art. In addition, the approximate numbers will establish the region of interest for the more detailed analysis of the variables.

# 4-4 PARAMETRIC PERFORMANCE DATA Für Indirect-Fire Systems

#### 4-4.1 DELIVERY TECHNIQUES

#### 4-4.1.1 Trajectory Profile

The trajectory profile for an unguided surfaceto-surface rocket (ballistic rocket) is shaped generally like a parabola, with an initial departure angle of between  $45^{\circ}$  and  $60^{\circ}$  for maximum range. Some large ballistic rockets are launched vertically; however, these require a maneuver to tilt the rocket onto a ballistic path. The discussion that follows will be limited to the nonmaneuvering type of rocket.

### 4-4.1.2 Energy-Management Techniques

Among the methods that have been used to impart propulsive energy to indirect-fire rocket systems are:

- a. Boost
- b. Boost/sustain
- .c. Staged boost

In the boost method, the booster motor fires continuously throughout the flight of the rocket, or until fuel is depleted. This approach is by far the least complex of the above and has found use generally in the field of simple, unguided, ballistic rockets.

The boost/sustain approach consists of an initial thrust of the booster motor, followed by a constant gustaining thrust of lesser magnitude. While this approach offers performance advantages over the *boost* approach for some applications, it requires a more complex and costly motor construction.

In the *staged boost* approach, the total thrust is delivered by a series of booster motors, each jettisoned upon burnout. This is the most efficient means of energy-management but its use is limited to those cases where weight considerations override the cost and reliability penalties of staging, and where the hazards of falling motor cases can be permitted. Since very few rockets within the scope of this handbook meet these limitations, this discussion will not include the staged boost approach.

#### **4-4.2 PARAMETRIC PERFORMANCE DATA**

The relationship between growth factor (ratio of gross rocket weight to payload weight) and range for an indirect-fire rocket system is a function of the following items:

- a. QE: launch elevation angle
- b.  $I_{sp}$ : propellant specific impulse
- c. PWF: motor propellant weight fraction
- d.  $W_{PL}/d^2$ : ratio of payload weight to diameter squared
- e. i: drag-form factor, ratio of drag coefficient of rocket under consideration to drag coefficient of standard rocket shape for which range tables have been computed
- f.  $F_B/W_0$ : initial-thrust-to-weight ratio (boost acceleration)
- g.  $F_S/F_{\tilde{B}}$ : ratio of sustain thrust to boost thrust h. $|I_S/I_B$ : ratio of sustain impulse to boost impulse

The angle at which the rocket must be launched in order to achieve maximum range is of initial interest to the designer. Fig. 4-4 presents the effect of boost acceleration  $F_B/W_0$  and growth factor Q on the optimum launch angle for an all-boost system, with fixed values of  $I_{sp}$ , PWF, and  $W_{PL}/id^2$ . Although the data would be different if these parameters  $(I_{sp}, PWF, W_{PL}/id^2)$ were varied, the trends of the curve are worth noting. Low accelerations require the highest launch angles, with the dependence of launch angle on acceleration being "ongest at low accelerations. Higher growth fax or sindicate higher launch

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Figure 4-4. Indirect Fire – All-Boost; Effect of Thrust-to-Weight Ratio on Optimum Launch Quadrant Elevation

angles because they are equivalent to longer boost burning times at any given level of acceleration.

For a boost/sustain system, the optimum launch angle will be a little greater than for an all-boost system, ar shown in Fig. 4-5. As the ratio of sustainer thrust to booster thrust is decreased and/or the ratio of sustainer impulse to booster impulse is increased, an increase in optimum launch angle is indicated.

Fig. 4-6 presents the relationship between growth factor and range for an all-boost system, with QE optimized and PWF,  $I_{sp}$ , and  $W_{PL}/id^2$ held constant. It is seen that the lower accelerations permit more officient energy-management schemes since they yield a lower growth factor for any specified range. Although this curve is constructed for only one value each of  $I_{sp}$ , PKF, and  $W_{PL}/id^2$ , it is indicative of trends; we may therefore say that the growth factor (for a given range) will be inversely proportional to  $I_{sp}$ , PWF, and  $W_{p_L}/id^2$ . The designer would, of course, examine trade-offs between these parameters, as discussed later on in this chapter. Before leaving Fig. 4-6, however, we should note another trend of significance to the designer or to the requirements originator. Examination of the curve shows that significant range increases can be obtained for relatively minor rocket-weight increases. For example, whereas a growth factor

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#### Figure 4-5. Indirect Fire --- Boost/Sustain; Effect of Impulse Ratio on Optimum Launch Quadrant Elevation

of about 2 is required for a range of 30 kilometers, a 25 percent increase in missile weight (an increase of Q from 2.0 to 2.5) doubles the range (to 60 km).

The relationship between growth factor and range for a boost/sustain system will be dependent upon the choice of sustainer parameters in addition to the parameters discussed above for the all-boost system. There is no unique method for determining optimum sustainer parameters since the choice will depend upon which chaiacteristics of the rocket the designer is attempting to optimize; for example, weight or accuracy. The designer has a choice of methods for providing the systainer impulse. This can be done with separate booster and sustainer motors, or by one motor with two thrust levels. In the case of separate motors, it is possible to achieve high specific impulse with each motor, but the propellant weight fraction of the combination is usually lower than for a single motor. In the case of a single motor with two thrust levels, the specific impulse of the sustainer will be less than for the booster (due to decreased chamber pressure during the sustainer phase) if a constant-





Figure 4-6. Indirect Fire - All-Boost; Effect of Range on Growth Factor

geometry nozzle is used. For this discussion it will be assumed that c single motor with two thrust levels and fixed nozzle geometry is used. The relationship between the ratio of sustainer thrust to booster thrust and the resulting ratio of specific impulse is presented in Fig. 4-7.

Fig. 4-8 indicates the type of parametric data which should be generated for optimization of sustainer parameters in situations where minimizing weight is the primary concern.

Fig. 4-9 presents the relationship between growth factor and range for a boost-sustain system, where the sustainer parameters are assumed to have been fixed by considerations other than minimum weight. A comparizon of these data with the data for the all-boost system will show that there are conditions for which the <u>boost/sustain system</u> is heavier than an all-boost system. This results from the reduction in sustainer specific impulse as discussed earlier.

The data above have been presented for only one value each of  $I_{sp}$ , PWF, and  $W_{PL}/id^2$ The designer will be interested in knowing the sensitivity of the missile weight to variations in these parameters also. Fig. 4-10 presents the effects of  $I_{sp}$  and PWF on the growth factor for a specific range, acceleration level, and ballistic coefficient. Fig. 4-11 presents a similar trade-4-10



Figure 4-7. Boost/Srstain Engine; Variation of Specific Impulse With Thrust



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off with acceleration and ballistic coefficient as variables.

The data presented above have not been intended to cover every situation. They are an indication of trends and serve to illustrate the various trade-offs which the designer must consider.

# 4-5 PARAMETRIC PERFORMANCE DATA FOR DIRECT-FIRE SYSTEMS

#### 4-5.1 DELIVERY TECHNIQUES

#### 4-5.1.1 Trajectory Profiles

Both bellistic and maneuvering types of trajectories have been used for direct-fire systems Either of these is essentially flat, however, and the degree of maneuver, if used, is generally limited. Therefore, for purposes of parameterization, no distinction is made between the two types. Generally speaking, it is sufficient for performance calculations to assume a constantaltitude, line-of-sight trajectory.

#### 4-5.1.2 Energy-Management Techniques

Among the commonly employed energy-management techniques for direct fire rockets are:

- a. Boost
- b. Boost/sustain
- c. Boost/coast/sustain

The choice here will depend to some extent on the level of performance required and on the intended method of use. Considering the method of use, we must determine whether burning outside the launch tube can be permitted. In the case of direct-fire infantry weapons, this cannot usually be permitted; whereas for weapons to be employed on armored vehicles, there is no problem (aside from accuracy considerations) involved in burning outside the launch tube. If burning outside the launch tube is permitted, either the boost or the boost/sustain approaches will apply. Where burning outside the tube is not permitted, the choice is between the boost and the boost/coast/sustain approaches, with the boost approach generally limited to low performance systems by the maximum velocity

which can be attained within the limitations of the tube length and the rocket acceleration.

#### 4-5.2 PARAMETRIC PERFORMANCE DATA

In defining the relationship between performance and physical characteristics for direct-fire rockets, it is not necessary to separate those rockets which must have a coast phase from those that do not. The reason for this is that, in the usual case, the additional time of flight will be negligible, on the order of 1/10 sec.

The relationships between growth factor (ratio of rocket weight to payload weight), range, and tines of flight are determined by:

- a.  $I_{sp}$ : propellant specific impulse
- b. PWF: motor propellant weight fraction
- c.  $H_{PL}/d^2$ : ratio of payload weight to diameter squared
- d. i: drag-form factor
- e.  $F_B/W_0$ : ratio of initial thrust to weight f.  $F_S/F_B$ : ratio of sustain thrust to boost
- thrust
- g.  $I_S/I_B$ : ratio of sustain impulse to boost impulse

For initial considerations, the first four of these parameters  $(I_{rp}, PWF, W_{PL}/d^2, i)$  can usually be estimated with adequate accuracy; however, it is desirable also to examine variations of these parameters if the situation permits.

Fig. 4-12 presents the relationship between target range, time of flight, and energy-management scheme for a given set of missile characteristics. The best energy-management scheme is seen to be the boost (no sustainer) in cases where a minimum time of flight is desired. This is usually the core for systems in which the gunrer has no control over the projectile after launch. However, in cases where command guidance is used, time of flight is a secondary consideration, with the velocity of the projectile being limited by considerations of gunner capabilities, command data rates, type of command link, etc. Since the considerations involved in the determination of time of flight (or average velocity) for the command-guided case are many and varied, it is desirable to concentrate for the remainder of this discussion on the system which



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Figure 4-12. Direct Fire - Boost/Sustain; Effect of Impulse Ratio on Time to Target

yields minimum time of flight, namely, the boost system.

Fig. 4-13 presents trade-offs with respect to growth factor, time of flight, range, and boost acceleration. A performance limit appears to be reached at a growth factor of about 3.0 because increases beyond this point reduce the time of flight an insignificant amount. Increasing the boost acceleration reduces the time of flight, but decreases the percentage of powered flight. For example, at a growth factor of 1.7 and  $F_B/W_0 = 20$ the burning distance is about 3 km, and we reach 4 km in 9.7 sec. If we increase  $F_B/W_0$  to 80, the burning distance is reduced to about 1 km and we reach 4 km in 8.5 sec. This illustration points out another of the choices facing the designer, namely, the trade-off between time to target and percentage of powered flight.

Once the designer has examined the trade-offs between range and time of flight, he may wish to



Figure 4-13. Direct Fire – All-Boost; Etfect of Growth Factor on Minimum Time to Target

determine the effects of various design parameters on the missile weight (or growth factor) for a specified performance level. For example, Fig. 4-14 shows the trade-cif between  $W_{PL}/id^2$ ,  $F_{B}/W_{O}$ , and growth factor for a specified performance level of 2 km in 3 sec. Fig. 4-15 illustrates the trade-off between PWF,  $I_{sp}$  and growth factor for the same performance level.

In the preceding paragraphs an attempt has been made merely to illustrate the types of tradeoffs with which the designer of direct-fire rockets must be concerned. From this discussion, the following conclusions can be drawn:

a. For minimum time to target, the boost system is superior to the boost/sustain system. b. The choice of boost acceleration must result from a consideration of the trade-off between time to target and percentage of powered flight desired.



Figure 4-14. Direct Fire - All-Boost; Effect of **Ballistic Coefficient on Growth Factor** 



Figure 4-15. Direct Fire – All-Boost; Effect of Propellant Weight Frection on Growth Factor

c. Increasing PWF,  $I_{sp}$ ,  $W_{PL}/id^2$ . or  $F_B/W_0$ results in decreased missile weight for a given payload weight and specified performance (time to target).

d. Increasing the growth factor beyond about 3.0 results in negligible performance increase for the range of parameters studied.

# 4-6 PARAMETRIC PERFORMANCE DATA FOR SOUNDING ROCKETS

#### 4-6.1 DELIVERY TECHNIQUES

#### 4-5.1.1 Trajectory Frofile

The only trajectory profile to be considered here for the sounding rocket is the vertical ascent. In some cases it may be desirable to launch a sounding rocket away from the vertical to insure impact within a given area, but for purposes of performance parameterization, the vertical ascent is sufficient.

#### 4-6.1.2 Energy-Management Techniques

The energy-management techniques which are used with sounding rockets are the same types as listed for the indirect fire rocket systems, namely:

- a. Boost
- b. Boost/sustain
- c. Staged boost

As stated earlier, the choice between these approaches must be the result of a trade-off, considering the *boost* system to be the simplest, cheapest, most reliable, and least efficient; whereas the *staged boost* would be the most efficient, most expensive, and least reliable. The *boost*/ *sustain* approach would be intermediate in all of the above considerations.

#### 4-6.2 PARAMETRIC PERFORMANCE DATA

The relationship between growth factor and peak altitude for a sounding rocket is determined by the following parameters: \_

- a.  $I_{sp}$ : specific impulse
- b. PWF: propellant weight fraction
- c.  $W_{PL}/id^2$ : ballistic parameter
- d. i: drag form factor
- e.  $F_B/W_0$ : ratio of bcost thrust to take off weight
- f.  $F_S/F_B$ : ratio of sustain thrust to boost thrust
- g.  $I_S/I_B$ : ratio of sustain impulse to boost impulse

In Fig. 4-16 the relationship between growth factor, energy-management scheme, boost acceleration, and peak altitude is presented. It can be seen here that the boost/sustain approach would provide the lowest missile weight for a given altitude. This relationship is abown for only one value each of  $I_{sp}$ , PWF, and  $W_{PL}/id^2$ , some shifting of data would occur if these parameters were changed.

For any given maximum altitude, the growth factor will be inversely proportional to PWF,  $I_{sp}$ ,



Figure 4-16, Sounding Rocket - All-Boost and Boost/Sustain; Effect of Growth Factor on Summit Altitude

and  $W_{PL}/id^2$ . This is shown in Figs. 4-17 and 4-18 for summit altitudes of 150,000 ft and 250,000 ft. These curves are for the all-boost case; bowever, the boost/sustain curves would be similar. From these curves, we see that the lightest missile results from a high performance motor (high PWF and  $I_{sp}$ ) and a large payload-to-diameter ratio.

# 4-7 PARAMETRIC PERFORMANCE DATA FOR SURFACE-TO-AIR ROCKETS

#### 4-7.1 DELIVERY TECHNIQUES

#### 4-7.1.1 Trajectory Profile

The unguided surface-to-air-rocket flies a ballistic trajectory and may be launched at any quadrant-elevation angle recessary for intercept of the target. Usually, the rocket will be designed to reach a given altitude in a given time and, therefore, the vertical ascent is of primary concern. For this reason the vertical trajectory is normally used to size the rocket, although it must be kept in mind that the distance traveled in a given time will be slightly less for trajectories other than the vertical.

#### 4-7.1.2 Energy-Management Techniques

Energy-management techniques applicable to surface-to-air rockets are:

- a. Boost
- b. Boost/sustain
- c. Staged boost

If we consider that minimum time to target will be desired for the surface-to-air rocket, and that



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Figure 4-17, Sounding Rockst - All-Boost; Effect of Propellant Weight Fraction on Growth Factor



Figure 4-18. Sounding Rocket - All-Boost; Effect of Ballistic Coefficient on Growth Factor

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achievable accuracy will limit this type of rocket to low altitude application (under 30,000 ft), the *boost* approach will usually be found to be the most attractive. For this reason, the discussion will be limited to the *boost* approach.

#### 4-7.2 PARAMETRIC PERFORMANCE DATA

The relationship between growth factor and performance requirement (specified as time to a given altitude) is determined by the following parameters:

a.  $I_{sp}$ : specific impulse

b. PMF: propellant weight fraction

c.  $W_{PL}/id^2$ : ballistic parameter

d. i: drag-form factor

e.  $F_B/W_0$ ; ratio of boost thrust to takeoff weight

Fig. 4-19 presents the relationship between growth factor, boost acceleration, and time to al-





titude for target altitude of 20,000 ft. As seen in these curves, an increase in boost acceleration reduces the time to altitude. An increase in growth factor above 5 would decrease time to altitude very little.

The trade-off between  $I_{sp}$ , *PWF*, and growth factor for a specified performance level of 20,000 ft in 5 sec is given in Fig. 4-20. Fig. 4-21 illustrates the trade-off between *PWF*  $_{c}$   $I_{sp}$ , and growth factor for the same performance level.

From the previous discussion, the following conclusions may be drawn:

a. Increasing growth factor above 5 results in negligible performance increase for the range of parameters studied.

b. Increasing PWF,  $I_{sp}$ , and  $W_{PL}/id^2$  results in decreased missile weight for a given payload weight.





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Figure 4-21. Sufface-to-Air - All-Boost; Effect of Ballistic Coefficient on Growth Factor

#### 4-8 NUMERICAL EXAMPLE

An indirect fire surface-to-surface missile design problem is presented here to illustrate the steps to be followed in designing a missile when the required performance is specified. The problem is to determine the propulsion system characteristics, the weight breakdown, and the dimensions of the vehicle that will transfer a given payload over a desired range.

The graphs presented in the preceding paragraphs of this chapter indicate the complexity of the relationships between the performance parameters. Because of these complex relationships, there is no easy way to arr ve at a rocket configuration which will satisfy all the required relationships and still meet the performance requiroments. The only alternative is to assume some of the important rocket or motor parameters, such as body diameter and specific impulse, and calculate the performance for these assumed conditions. The calculated performance data are compared with the desired values; then the original assumptions are modified and the procedure is repeated until the desired results are obtained. It is easily seen that the accuracy of the original assumptions determine the

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amount of work required to reach the final solution. This is the reason that experience with the design of rocket systems is so important <sup>s</sup>uring the preliminary design stage.

Fig. 4-22 is a flow diagram illustrating the steps of the design procedure. Block 1 indicates the design performance specification. In this case the rocket range and payload are specified. Blocks 2 and 3 show the parameters whose values are being assumed - - that is, the first guess at the design configuration. The next sequence of blocks (4 through 8) illustrates the iterative procedure which must be followed until the initial assumptions are verified. After the iterative process is complete, enough is known about the system to define its performance parameters. This is done in the final Block 11, headed CAL-CULATE.

A ballistic coefficient is assumed in the first block of the iterative loop (Block 3). This fixes the burnout velocity, the booster-mass ratio, the burnout-to-payload-weight ratio, and the payload ballistic coefficient. Notice that the value of the payload ballistic coefficient was assumed in Block 3 and it is necessary that this value be duplicated. If this has been satisfied, there are no contradictions and the example can proceed to the defining of values.

If the payload ballistic coefficient value cannot be duplicated and/or the resulting values are not realistic, it will be necessary to make a trade-off study of the parameters in the second block until all criteria are satisfied.

The numerical example which follows utilizes the logic shown in the flow diagram.

- 1. We shall start with a specified range R of 30.0 km and a payload weight of 890.0 lb.
- 2. From a knowledge of similar rockets, assume a propellant weight fraction PWF of 0.77, a specific impulse  $I_{sp}$  of 250 sec and a payload ballistic coefficient  $W_{pL}/id^2$  of 4.0 lb/in.
- 3. For the required range, assume a ballistic coefficient  $W_B/id^2$  of 4.5 lb/in . Therefore, a burnout velocity  $V_B$  of 2700 ft/sec is necessary as shown in Fig. 4-1.
- 4. For an  $I_{sp}$  of 250 sec, the booster mass ratio  $r_B$  is determined from Fig. 4-2 to be 1.4.

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5. For a given  $P \parallel F$  of 0.77, calculate the ratio of burnout weight to payload weight:

$$\frac{m_B}{W_{PL}} = \frac{PhF}{1 - r_B(1 - PWF)}$$
$$= \frac{0.77}{1.0 - 1.4(0.23)} = 1.138.$$

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6. Calculate the ballistic coefficient:

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$$\frac{W_B}{id^2} = \frac{W_B}{W_{PL}} \left( \frac{W_{PL}}{id^2} \right) = 1.138 \quad (4)$$
  
= 4.552 lb/in<sup>2</sup>

- 7. A value of  $W_B/id^2$  was assumed in Step 3. Match this value with the value calculated in Step 6. They are the same. If they were not the same, then another value of  $W_B/id^2$  should be selected and Steps 3 through 7 repeated until they agree.
- 8. After satisfying Step 7, either calculate the growth factor Q or read it from Fig 4-3.

$$Q = r_B \left( \frac{H_B}{H_{PL}} \right) = 1.4(1.138) = 1.59$$

9. The burnout weight  $W_B$  is calculated

$$W_B = \left( \frac{W_B}{W_{PL}} \right) W_{PL} = 1.138(890) = 1014 \ lb$$

10. The rocket diameter d can be calculated

$$d = \left(\frac{W_{PL}}{W_{PL}/id^2}\right)^{1/2} = \left(\frac{890}{4}\right)^{1/2} = 15 \text{ in.}$$

11. Propellant weight  $W_p$  is found by

$$\mathcal{W}_p = PWF(W_{PL})(Q-1)$$

12. Motor weight ∦ is

$$W_{m} = \frac{W_{p}(1 - PWF)}{PWF}$$

$$= \frac{890(0.23)}{0.77} = 120 \ lb$$

13. Total weight  $W_T$  is

$$W_T = W_{BC} + W_P = 1014 + 405$$
  
= 1419 lb

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# CHAPTER 5 PROPULSION

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## LIST OF SYMBOLS

Symbol Symbol Meaning Meaning Velocity, ft/sec Constant (see Eq. 5-19a) v a<sub>1</sub> W Weight, lb Constant (see Eq. 5-19b) a, Area, ft<sup>2</sup> A Erosion factor (see Eq. 5-21) € Ь Constant (see Eq. 5-19b) Ratio of specific heats  $(C_p/C_v)$ Y Effective exhaust velocity, ft/sec; speed of ζd Discharge correction factor С ζ<sub>f</sub> ζ Thrust correction factor sound, ft/sec Cr Thrust coefficient Velocity correction factor Specific heat at constant pressure, BTU/lb θ Propellant burning time, sec C<sub>p</sub> ٩R ρ Density, slug/ft<sup>a</sup> Specific heat at constant volume, BTU/lb Σ Summation С, ٩R Subscripts: Scale factor F Rocket thrust, lb atmosphere Ambient (or atmospheric) Gravitational acceleration, ft/sec<sup>2</sup> conditions g Itotal Total motor impulse, lb-sec Burn-out condition; burning Ь Motor specific impulse, sec I<sub>sp</sub> surface (see Eq. 5-20) Ŕ Erosion burning constant (see Eq. 5-21); basic Basic (or original) configratio of grain burning surface area to uration nozzle throat area В **Back** pressure Mass of propellant, slug Combustion or stagnation m С Mass flow rate, slug/sec conditions 'n. *m*\* Mass flow rate that will produce a velocity Erosion condition; exit cone equal to the speed of sound, slug/sec ditions m Molecular weight of gas,  $R_{\mu}/R$ exhaus t Exhaust (or exit) condition M Mach number Propellant grain g Exponent (see Eq. 5-19a); number of moles n Inlet (or entrance) condition i Combustion chamber pressure parameter р Molal value (see Eq. 5-25) m (see Eq. 5-23b) Conditions for optimum exmax Р Pressure, lb/ft<sup>2</sup> pansion (see Erg. 5-9) Heat of reaction at reference temperature, Q<sub>R</sub> motor Motor condition, BTU/lb scaled Scaled (from basic) config-Grain burning rate, in./sec uration Universal gas constant, 1545 ft-lb/lb-mole R<sub>n</sub> ŝ Throat (or minimum area) જર conditions R Gas constant,  $R_{\mu}/\bar{m}$ Axial distance (along the x T Temperature, °R nozzle centerline)

#### 5-1 GENERAL

A rocket is propelled by an internal combustion engine that burns either liquid or solid fuel. The primary function of rocket propulsion is to move the warhead and airframe from the launcher to the target with prescribed accuracy. Since the oxidizer is carried internally, rocket engines can operate in the atmosphere, above the atmosphere, or under water. As previously indicated, this handbook will discuss only solid propellant rocket engines.

Unlike other combustion engines, a rocket motor does not contain cylinders, pistons, or turbine blades, nor does it need a supply of air to mix with the fuel. Because its oxygen supply is carried within the propellant, a rocket engine has a number of advantages over other types of power plants:

a. Thrust is practically independent of its environment and flight speed.

b. There is no altitude ceiling.

c. It functions in a vacuum.

d. Thrust per unit of frontal area is the largest of any known propulsion engine.

The basic rocket motor consists of an igniter, a propellant charge, and a chamber that is strong enough to withstand the combustion of the propellant and the pressures thus generated. The chamber has a nozzle through which the propellant gases escape in the form of a jet. Igniter types, propellant composition, and chamber materials vary from system to system, depending on the individual requirements. A schematic of a typical rocket motor is shown in Fig. 5-1.

Rocket propulsion involves the study of the burning rate of propellant in the motor chamber and the discharge rate of gas through the nozzle. The pressure in the motor is the result of a delicate balance between the burning of the propellant and the escape of gases through the nozzle.

For the operation of a solid propellant motor, the chamber is loaded with a propellant charge and an igniter. Motor operation is initiated when the igniter ignites the propellant. The burning propellant furnishes at high pressure a continuous supply of gas that expands and is ejected from the chamber nozzle at high velocity.

The thrust of the rocket motor is produced by the change in momentum of the combustion gas expelled through the nozzle and the pressure forces acting on the rocket body, so that

$$F = \overline{m}V_{exhaust} + (P_{exhaust} - P_{atmosphere}) A_{exhaust}$$
(5-1)

where F is the rocket thrust,  $\dot{m}$  is the flow rate of the combustion gas,  $V_{exhaust}$  is the velocity of the exhaust gas,  $P_{exhaust}$  is the pressure of the exhaust gas,  $P_{atmosphere}$  is the atmospheric pressure, and  $A_{exhaust}$  is the exhaust gas flow area. If the flow is ideally expanded in the nozzle



Figure 5-1. Schematic of a Case-Bonded, Unrestricted-Burning Solid-Propellant Rocket Mator

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and

$$F = mV_{ezhaust}$$
 (5-2)

For convenience, an effective exhaust velocity c is defined as

$$c = V_{exhaust} + \frac{(P_{exhaust} - P_{atmosphere}) A_{exhaust}}{\mathring{m}}$$
(5-3)

thus

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$$F_{-}$$
 if  $P_{exhaust} = P_{atmosphere}$  (5-4)

Two useful performance indicators are the specific and total impulses. The specific impulse  $I_{sp}$  is the thrust per unit weight rate of consumption of the propellant; thus

$$I_{sp} = \frac{F}{mg} = \frac{c}{g}$$
(5-5)

where g is local gravitational acceleration (32.2 ft per sec<sup>2</sup>), and all other symbols are as defined previously. The total impulse  $I_{total}$  is the integral of the thrust over the time that the propellant burns. Thus,

$$I_{total} = \int_{0}^{\theta_{b}} Fd\theta = \int_{0}^{\theta_{b}} I_{sp} \ mg \ d\theta \qquad (5-6)$$

or for constant thrust,

$$I_{total} = F\theta_b = I_{ep} mg \tag{5-7}$$

where  $\theta_b$  is the time during which the propellant burns, *m* is the total mass of propellant consumed, and all other symbols are as defined previously.

For additional information on rocket motors see Ref. 9.

#### **5-2. NOZZLE**

The rocket nozzle expands the combustion chamber gas from the chamber pressure to atmospheric pressure. The gas is accelerated by converting internal energy into kinetic energy. Subsonic gas flow (i.e., velocity less than the speed of sound) is expanded and accelerated by decreasing the flow area (e.g., a convergent nozzle). Supersonic gas flow (i.e., velocity greater than the speed of sound) is expanded and accelerated by increasing the flow area (e.g., a divergent nozzle).

The velocity of a gas exhausting from a convergent nozzle increases as the ratio of upstream to downstream pressure increases but will not exceed the speed of sound. To illustrate, let us consider a convergent nozzle with a constant upstream pressure and a variable downstream pressure, such as that shown in Fig. 5-2. When the upstream and downstream pressures are equal, there will be no flow. As the downstream pressure is reduced, the gas will begin to flow and the velocity and mass flow exhausting from the nozzle will increase until the exhaust velocity is equal to the speed of sound. Further reduction in the downstream pressure will have no effect on the velocity or mass flow. The minimum pressure ratio across the nozzle that will yield a sonic velocity is termed the critical pressure ratio, and is a function of the flow conditions and gas properties. At pressure ratios greater than the critical, the velocity will remain sonic and the mass flow can only be increased by increasing the upstream pressure. The sonic velocity will always occur (if it occurs) at the minimum area section. The ratio of velocity to the speed of sound is termed the Mach number M.

The above discussion indicates that a subsonic gas may be accelerated to the speed of sound in a convergent section. It may then be further accelerated to supersonic velocities in a divergent



Figure 5-2. Subsonic Flow Through a Converging Nozzle

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section. Such a nozzle with convergent and divergent sections is called a supersonic or De Laval nozzle. The velocity at the section of minimum area (throat) will always be less than or equal to the speed of sound, depending upon the pressure ratio across the nozzle. To illustrate the flow phenomena, let us consider a supersonic nozzle with a constant upstream pressure and a variable downstream pressure as shown in Fig. 5-3. When the upstream and downstream pressures are equal, there will be no flow. As the downstream pressure is xeduced, the gas will begin to flow, and the exhaust velocity and mass flow will increase until the velocity at the throat is equal to the speed of sound. As the downstream pressure is furthe reduced, the mass flow will remain constant and the velocity at the throat will remain at the speed of sound. A downstream pressure will be reached at which the gas is completely expanded ideally within the nozzle and the exhaust velocity is supersonic. At downstream pressures lower than this, the exhaust flow remains supersonic but the gas is underexpanded within the nozzle; therefore, additional expansion takes place outside the nozzle. At higher downstream pressures the gas is overexpanded in the divergent section of the nozzle, resulting in pressure shock waves and in flow separation from the nozzle wall. Pressure shock waves are distinguished by abrupt pressure rises and a velocity change from supersonic to subsonic.

As internal energy is converted to kinetic energy throughout the nozzle, the gas temperature decreases. The gas pressure and density also decrease as the gas expands through the nozzle.

The above discussion presents a qualitative description of nozzle flow phenomena. The discussion which follows will present methods of defining the flow phenomena quantitatively.

#### 5-2.1 THERMODYNAMIC RELATIONS

To design and evaluate the performance of a rocket, it is necessary to define the thermodynamic relations of the gas flow through the nozzle. The normal approach is to evaluate the thermodynamic relations based on the ideal flow of an ideal gas and then modify these relations for the real flow of the real gas. Generally, the actual rocket motor performance is within 10 percent of the performance calculated for ideal conditions. Flow through nozzles is considered to be ideal when: (a) there is no friction, (b) there is no heat transfer (adiabatic), (c) flow is steady, (d) flow is uniform across sections normal to the nozzle longitudinal axis, (e) flow exhausting to the atmosphere .s parallel to the nozzle longitudinal axis, (f) the gas (products of propellant combustion) is homogeneous, (g) the gas is in chemical equilibrium and does not shift, and (h) the gas obeys the perfect gas laws. The above assumptions allow the definition of flow through the nozzle to be based on the isentropic thermodynamic relations and the perfect gas laws. Flow across pressure shocks cannot be considered as ideal.

If we apply the principle of the conservation of energy and consider the isentropic flow of a perfect gas, the nozzle exhaust velocity is

$$V_{exhaust} = \sqrt{\frac{2g\gamma}{\gamma - 1}} \overline{R}T_{c} \left[1 - \frac{P_{exhaust}}{P_{c}}\right]$$
(5-8)

where g is gravitational acceleration (32.2 ft/sec<sup>2</sup>), y is the ratio of the gas constant pressure specific heat to constant volume specific heat,  $\overline{R}$  is the gas constant  $(R_u/\bar{m})$ ,  $T_c$  is the temperature of the gas in the combustion chamber,  $P_e$  is the pressure of the gas in the combustion chamber, and  $P_{exhaust}$ is the pressure of the exhaust gas. For optimum expansion, the pressure of the exhaust gas will be equal to the atmospheric pressure. If the exhaust gas pressure is greater than atmospheric, the gas will be underexpanded (because the exhaust flow area is too small) and expansion will continue to take place outside the nozzle. The relationship between the area ratio (exhaust to throat) and pressure ratio (chamber to exhaust) for ideal expansion in the divergent section of a supersonic nozzle is shown in Fig. 5-4. If, for a given area ratio, the exhaust pressure (determined from Fig. 5-4) is less than atmospheric, the gas will be overexpanded (as the exhaust flow area is too large) resulting in shock waves and flow separation within the divergent section of the nozzle. When the gas is overexpanded, a portion of the divergent section of the nozzle is unused and, therefore, is unnecessary weight. The decrease of atmospheric pressure with altitude

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Figure 5-4. Superscnic Nozzle Area Expansion Ratios

makes impossible the design of a nozzle that will always operate at optimum expansion. Consequently, the nozzle is generally designed to operate at optimum expansion at sea-level (or at a relatively low altitude) and thus to operate overexpanded at higher altitudes. A maximum exhaust velocity exists for a given combustion gas and combustion temperature. When the ratio of  $P_{extense} / P_c$  is zero ( $P_{exhaust} = 0$ ), as would be the case for optimum expansion in a vacuum, the velocity is:

$$(V_{exhaust})_{max} = \sqrt{\frac{2gy}{\gamma - i}} \tilde{RT}_{e}$$
 (5-9)

Nozzle pressure ratios, for rockets of the class discussed in this handbook, are sufficient to produce a sonic velocity in the threat. The sonic velocity is equal to

$$V_t = \sqrt{\frac{2g\gamma}{\gamma+1}} \overline{R}T_c$$
 (5-10)

If we use the continuity equation, then, for steady flow, the mass flow rate through the nozzle is

$$h = \frac{A_t P_c \gamma \sqrt{\frac{2}{\gamma+1}} (\gamma+1)/(\gamma-1)}{\sqrt{g \gamma \overline{R} T_c}}$$
(5-11)

where  $A_t$  is the throat area and all other symbols are as defined previously.

Under the conditions of adiabatic isentropic flow, the temperature at any axial location x in the nozzle is

$$T_x = T_c - \frac{V_x^2}{1556gC_p}$$
 (5-12)

where  $V_x$  is the velocity at location x, and  $C_p$  is the constant-pressure specific heat of the gas. The relationships between the pressure, temperature, and density in the combustion chamber and location x are

$$\frac{T_c}{T_x} = \left(\frac{p_c}{P_z}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{\rho_c}{\rho_x}\right)^{\gamma-1}$$
(5-13)

The pressure, temperature, and density at any location x are related according to the perfect gas law as

$$P_x = \rho_x \ \overline{R}T_x \tag{5-14}$$

Substituting Eqs. 5-8 and 5-11 into Eq. 5-1 yields the following expression for rocket thrust:

$$F = A_{e} P_{c} \sqrt{\frac{2\gamma^{2}}{\gamma - 1}} \left(\frac{2}{\gamma + 1}\right)^{(\gamma - 1)/(\gamma - 1)} \left[1 - \left(\frac{P_{exhaust}}{P_{c}}\right)^{(\gamma - 1)/\gamma}\right] + (P_{exhaust} - P_{atmosphere}) A_{exhaust} (5-15)$$

The thrust coefficient  $C_F$  is defined as:

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$$\sqrt{\frac{2y^2}{\gamma-1}\left(\frac{2}{\gamma+1}\right)^{(\gamma+1)/(\gamma-1)} \left[1 - \left(\frac{P_{exhaust}}{P_c}\right)^{(\gamma-1)/\gamma}\right]} + \frac{\left(\frac{P_{exhaust}}{P_c} - \frac{P_{atmos\,phere}}{P_c}\right) \frac{A_{exhaust}}{A_t} (5-16)$$

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Thus,

$$F = C_F A_t P_c \tag{5-17}$$

The thrust coefficient is shown graphically in Fig. 5-5 (A) and (B).

#### 5-2.1.2 Real Flow

In real nozzies, friction is present, heat is transferred; flow may be unsteady; flow and gas properties across sections of the nozzle are nonuniform; flow is nonaxial, equilibrium shifts in the nozzle; and the gas is nonhomogeneous and imperfect. An empirically derived correction factor is generally used to account for all deviations from the ideal flow performance.

Reference 1 presents indications of the magnitude of the deviations from ideal conditions. The velocity, discharge, and thrust correction factors account for friction effects, heat transfer, imperfect gases, nonaxial flow, nonuniformity of the gases, and nonuniformity of the flow distribution. The velocity correction factor  $\zeta_{y}$  is the ratio of actual exhaust velocity to ideal exhaust velo-ity, and ranges between 0.85 and 0.98, with an average of 0.92. The discharge correction factor  $\zeta_d$  is the ratio of the actual mass flow rate to the ideal mass flow rate, s.id ranges between 0.98 and 1.15, with an average of 1.04. The thrust correction factor  $\zeta_{L}$  is the ratio of actual thrust to ideal thrust, and ranges between 0.92 and 1.0, with an average of 0.96. The correction factors are related as follows:

$$\zeta_f = \zeta_y \,\,\zeta_d \tag{5-18}$$

The average values of the correction factors indicated above are recommended for preliminary design. In advanced design, it will be necessary to consider chemical equilibrium shifts through the nozzle, gas property variations across sections of the nozzle, and other effects treated only as averages in this handbook.

For a more detailed study of flow in nozzles, consult References 1 and 2.

#### 5-2.2 HOZZLE CONTOURS

The design of the optimum nozzle contour requires complex analyses utilizing high-speed digital computers as cutlined in Reference 3. In general, the contour of the divergent section is critical. The primary requirement on the convergent and throat sections is that they be well rounded to avoid disturbances in the flow.

For ease of manufacture and design, the use of a conical divergent section is often desirable. The cone half angle of such a section, according to Reference 4, should be approximately 9 deg to obtain maximum thrust. Since the nozzle should be as short as possible to reduce weight, a cone half angle as large as 18 deg can be used with only a 2 percent reduction in thrust. To prevent flow separation, angles greater than 18 deg should be avoided. The nozzle exit should be manufactured with a sharp edge to prevent overexpansion and flow separation.

The thrust may be increased by roughly 1 percent by using a parabolic instead of a conical divergent section. A method of approximating the optimum parabolic contour is presented in Reference 4.

#### 5-2.3 NOZZLE EROSION

The high-velocity gases passing through the nozzle contain solid particles that erode the inner surfaces of the nozzle. Erosion at the nozzle throat is particularly serious since the flow area is increased, which alters the combustion chamber pressure, mass flow rate, velocities, and, consequently, the rocket performance. Erosion may be controlled for short durations through use of protective coatings such as chrome plating, or for longer durations by using ceramic or graphite inserts.

#### 5-3 PROPELLANTS

#### 5-2.1 GRAIN

The body or mass of the solid propellant, which is formed by casting, molding, or extrusion, is called the grain. It is a specific chemical composition that sustains combustion. The grain, when it is properly designed, burns at a uniform rate in a direction normal to the burning surface. Burning may be prevented on surfaces by employing inhibitors that are chemically inert substances.



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The burning is termed restricted or unrestricted, depending upon whather inhibitors are used or not. The geometric configuration of the grain determines the burning area and, thus, the chamber pressure and thrust for a given chamber and nozzle design. The burning characteristics are termed progressive, neutral, or regressive, depending upon whether the burning area increases, remains constant, or decreases with time, respectively.

#### **5-3.1.1 Chemical Compositions**

Solid propellants are classified as composite when mede up of an oxidizer and fuel, or as double-base when made up of unstable chemical compounds, each a self-sufficient combustible. The term double-base refers to the common approach of combining two of the unstable compounds in a colloid. Additional ingredients may be added to the grain for strength, heat transfer characteristics, catalysis, chemical stability, reduction in temperature sensitivity, and ease of processing.

The oxidizers generally employed in composite propellants are the perchlorates and inorganic nitrates. Sodium, potassium, magnesium, and ammonium perchlorates, and sodium, potassium, and ammonium nitrates are the most common. The reaction of the perchlorates with the fuel produces chlorine products that are toxic and corrosive, such as hydrogen chloride. Ammonium and potassium perchlorate are useful in situations where the propellant is exposed to moisture since these perchlorates are only slightly soluble in water. Potassium and sodium nitrates produce smoke, where is ammonium nitrate is smokeless and nontoxic but has a low oxidizing potential.

The organic fuels generally employed in composite propellants are asphalts, synthetic rubbers, and plastics. Oil must be added to asphalt fuels to make them less brittle. The addition of oil, however, makes the asphalt soft and subject to deformations at higher storage temperatures. The plastics used are thermosetting (such as phenol formaldehyde) or non-thermosetting (such as styrene). The rubber fuels are especially useful where the propellant is subjected to an environtoent with a wide temperature range.

The compounds generally employed in doublebase propellants are the organic nitrates and aromatic nitro compounds. The most common nitrates are glycerol trinitrate (nitroglycerin), diethyleneglycol dinitrate (DEGN), and cellulose nitrate (nitrocellulose). The most common nitro compounds are ammonium picrate and trinitrotoluene (TNT).

The preceding discussion is only a cursory review of some of the propellants employed in solid rockets and some of their salient characteristics. For a more detailed discussion of solid propellants, see References 4, 5, 9, 10, and 11.

#### **5-3.1.2 Configuration Geometry**

The design of the grain configuration must be based primarily on the required thrust history but must also consider strength, heat transfer, erosion, and missile size requirements. An infinite series of thrust histories can be attained by variations in propellant compositions, grain geometries, inhibitor locations, and grain combinations (when using more than one grain). Complex thrust histories require solution on digital computers. Examples of some typical grain cross sections are shown in Fig. 5-6.

For simple cylindrical grain configurations, the burning will be progressive, if restricted to internal cylindrical surfaces (i.e.; longitudinal ports or port); neutral, if restricted to the cylinder end or allowed on both internal and external cylindrical surfaces; and regressive, if restricted to external cylindrical surfaces. Other sim, le geometries are the cruciform which burns regressively, and the rod and tube (burning on inside of tube and outside of rod) which burn neutrally. Burning will also be neutral if restricted to a starshaped port with a periphery equal to the circumference of the outside of the cylindrical grain. Examples of the installations of some typical grains are shown in Fig. 5-7.

For some configurations, especially the internal star design mentioned above, not all of the grain will be burned. That portion remaining is known as "slivers" and represents added weight to the rocket.

It is desirable to bond the grain to the combustion chamber case; this acts as thermal insulation, allowing thinner and lighter cas. walls Burning on external surfaces subjects the case walls to severe heating, requiring use of insulation or heavier walls.

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Figure 5-6. Examples of Grain Cross-Sections

Combustion gases formed at the forward sections of perforated grains must pass across the aft grain surfaces to reach the nozzle. It is desirable to keep passages through the grain large enough so that gas velocities will be low and erosion effects on the grain surface will be reduced. Erosion will be discussed further in Par. 5-3.1.4. For a more complete discussion of grain configuration design, see References 6, 7, 9, 10, and 11.

#### 5-3.1.3 Burning Rate

The burning rate is the velocity at which the grain is consumed in the direction normal to the burning surface. The burning rate is generally determined empirically and presented in literature supplied by the rocket motor manufacturer.

The following two equations approximate the burning rate:

or

$$r = a_i P_c^n \qquad (5-19a)$$

$$r = a_2 + bP_c$$
 (5.19b)

where r is the burning rate;  $P_c$  is the combustion chamber pressure; and  $a_1, a_2, b$ , and n are empirically determined constants whose values depend on the propellant composition and initial temperature. The burning rate increases with increasing chamber pressure and grain initial temperature. Typical burning rates for the most common propellants vary between approximately 0.025 and 2.5 inches/second. The flow of high velocity gases across the grain burning surfaces increases the burning rate. This phenomenon is defined as erosion and is discussed in Par. 5-3.1.4.

The mass flow rate of propellant is related to the burning rate as follows:

$$\check{m} = A_b \rho_s r \tag{5-20}$$

where  $\dot{m}$  is the mass flow rate,  $A_b$  is the grain burning surface area at the particular time in question, and  $\rho_g$  is the grain density.





#### 5-3.1.4 Eresion

Although only the effects, and not the nature, of erosion are understood, erosion seems to be a result of the increased convection heat transfer rate from the combustion chamber gas to the grain surfaces.

Erosion must be determined experimentally. The effects on the burning rate can be evaluated from the following equation:

$$\epsilon = \frac{r_e}{r} = 1 \Rightarrow K \frac{\dot{m}}{\dot{m}^*}$$
(5.21)

where  $\epsilon$  is the erosion factor, r is the burning rate without erosion,  $r_e$  is the burning rate with erosion, K is the erosion burning constant (determined experimentally),  $\dot{\pi}$  is the mass flow rate through the grain, and  $\dot{\pi}^*$  is the mass flow rate that will produce a velocity through the grain equal to the speed of sound (Mach number  $\approx 1.0$ ).

The erosion effects may be eliminated by designing flow passages large enough to maintain low gas velocities. The effects will be greatest in the early phases of rocket engine operation and will decrease as the grain burns away and the flow passages become larger. Erosion is greater in slow burning propellants than in faster burning grains.

For a further study of erosion, see References 1 and 8.

#### 5-3.2 IGNITION

The ignition of the solid propellant is effected by heating the propellant to its ignition temperature while maintaining the chamber pressure at a sufficient level to sustain combustion. The propellant is usually heated by hot gases produced by a pyrotechnic igniter containing a solid charge that is detonated electrically. A schematic of a typical igniter is shown in Figure 5-8. To build up the pressure in the chamber during ignition, it is sometimes necessary to install a nozzle closure that will rupture when the desired pressure is reached.

The igniter should be positioned to expose the maximum amount of grain surface to the direct impingement of the ignition gases. The most common locations for the igniter are in the forward end of the chamber, in the nozzle, or embedded in the propellants.

The exact nature of ignition is not understood and no adequate ignition theory exists. Therefore, design of ignition systems for solid propellants is based primarily on empirical data and experience.

Propellants employing ammonium nitrate are the most difficult to ignite while double-base propellants and propellants employing ammonium perchlorate as the oxidizer are the easiest to ignite. Propellant manufacturer's specifications are the best source of information for ignition data.



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## 5-3.3 HANDLING

Because they are susceptible to cracking, solid propellant grains must be handled carefully. Cracks increase the burning surface area, altering the rocket performance. Chapter 6 discusses handling procedures that can be applied to the grains.

#### **5-4 INTERNAL BALLISTICS**

The combustion chamber pressure, for a given propellant composition, is a function of the ratio of the grain burning area to the nozzle throat area. Equating the mass generation rate for steady flow (Eq. 5-20) with the nozzle mass flow rate (Eq. 5-11), utilizing the burning rate equation (Eq. 5-19), and rearranging the terms, yields

$$P_{c} = \left(\frac{A_{b}}{A_{t}}\right)^{\frac{1}{1-n}} \left(\frac{\rho_{g}a_{1}\sqrt{g\overline{RT}_{c}}}{\sqrt{\sqrt{\left(\frac{2}{\gamma+1}\right)^{-(\gamma+1)/(\gamma-1)}}}}\right)^{\frac{1}{1-n}}$$
(5-22)

 $k=\frac{A_b}{A_b}$ 

when

and

$$p = \left(\frac{\rho_{\varepsilon} a_{1} \sqrt{g \ \overline{R}T_{c}}}{\sqrt{\gamma \left(\frac{2}{\gamma+1}\right)^{-(\gamma+1)/(\gamma-1)}}}\right)^{\frac{1}{1-n}}$$
(5-23b)

then

$$P_c = p k^{\frac{1}{1-n}}$$
 (5-24)

(5-23a)

where  $P_c$  is the combustion chamber pressure,  $A_b$  is the grain burning area,  $A_t$  is the nozzle throat area,  $P_c$  is the density of the grain,  $a_t$  and n are constants from the burning rate equation (Eq. 5-19),  $\overline{R}$  is the gas constant,  $T_c$  is the temperature of the gas in the combustion chamber, g is the gravitational constant, and  $\gamma$  is the ratio of the constant-pressure specific heat of the gas to its constant-volume specific heat. The evaluation of the combustion chamber gas temperature requires a detailed analysis of the chemical reaction, product composition, and product quantities. Equating the heat of reaction and the summation of the change of each of the combustion chamber products yields

$$Q_{R} = \sum \left[ n \int_{T_{o}}^{T} (C_{p})_{n} dT \right]$$
(5-25)

where  $Q_R$  is the heat of reaction at reference temperature  $T_o$ , n is the number of moles of each product formed,  $(C_p)_{\pm}$  is the constant-pressure molal specific heat of each product formed, and  $\int_{T_o}^T (C_p)_{\mathbf{a}} dT$ is the enthalpy change of the product formed associated with the enthalpy change from reference temperature  $T_o$  to combustion chamber gas temperature T. The heat of reaction is the algebraic difference between the heat of formation of the products and the heat of formation of the reactants. The heat of formation and the constant-pressure molal specific heat of the various compounds are available in standard chemical handbooks. A more detailed discussion of the evaluation of chamber gas temperatures is presented in Reference 1. Rocket motor manufacturer's specifications and performance reports should be consulted to estimate gas temperatures.

Other factors associated with internal ballistics (such as burning rate, erosion, grain configuration, and ignition) were discussed under Paragraph 5-3. Consult Reference 8 for a further discussion of internal ballistics.

# 5-5 SCALING OF SOLID PROPELLANT MOTORS

The performance characteristics of solid propellant rocket motors may be scaled within certain limitations. This means that performance data available for a basic motor may be modified and applied to a similar motor that differs from the basic in size, thrust level, total impulse, and propellant composition.

When all dimensions are varied from the basic motor dimensions by the same scale factor

$$F_{scaled} = f^2 F_{basic}$$
 (5-26)

$$\left(\frac{F}{W_{motor}}\right)_{scaled} = \frac{1}{f} \left(\frac{F}{W_{motor}}\right)_{basic}$$
(5-27)

(I<sub>total</sub>)<sub>scaled</sub> = f<sup>3</sup> (I<sub>total</sub>)<sub>basic</sub>

and

$$(\theta_b)_{scaled} = f(\theta_b)_{basic}$$
 (5-29)

(5-28)

where F is the thrust,  $W_{molor}$  is the weight of the rocket motor,  $I_{totel}$  is the total impulse, f is a scale factor, and  $\theta_b$  is the time required for the propellant to be consumed. In evaluating the rocket motor weight, it is assumed that the same materials and structural criteria are applied to the basic and scaled motors.

When only the length of the grain (with ends restricted) is varied from the basic by the scale factor f, and when the nozzle flow areas are adjusted to maintain the same chamber pressure as in the basic motor,

$$F_{scaled} = fF_{basic} \qquad (5-30)$$

$$(A_t)_{scaled} = f(A_t)_{basic} \qquad (5-31)$$

$$(A_{exhaust})_{scaled} = f(A_{exhaust})_{basic}$$
 (5-32)

and

$$(W_{notor})_{scaled} = f(W_{notor})_{basic}$$
 (5-33)

where  $A_{t}$  is the nozzle throat area,  $A_{exhaust}$  is the nozzle exhaust flow area, and all other symhols are as defined previously. If it is desirable to change the nozzle throat area by utilizing inserts while maintaining the same exhaust area as the basic nozzle,

$$F_{scaled} = f \frac{(C_F)_{scaled}}{(C_F)_{basic}} F_{basic}$$
(5-34)

$$(I_{sp})_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{basic}} (I_{sp})_{basic}$$
 (5-35)

and

$$(I_{total})_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{besic}} (I_{total})_{besic}$$
(5-36)

where  $C_F$  is the thrust coefficient,  $J_{sp}$  is specific impulse, and all other symbols are as defined previously. The above technique is not applicable if the grain erosion effects are altered significantly.

The motor thrust level may be changed by scaling the nozzle throat area by the factor f so that

$$F_{scaled} = f \frac{1}{f} \frac{(C_F)_{scaled}}{(C_F)_{basic}} F_{basic}$$
(5-37)  
$$(P_F)_{total} = f \frac{1}{f} \frac{1}{f} (P_F)_{total}$$
(5-28)

$$(P_c)$$
 scaled =  $J$   $(P_c)$  basic (5-38)  
 $-\frac{n}{4}$ 

$$r_{scaled} = f^{1-n} r_{basic} \qquad (5-39)$$

$$(\theta_b)_{scaled} = f^{f-n} (\theta_b)_{basic}$$
 (5-40)

$$(I_{total})_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{basic}} (I_{total})_{basic}$$
(5-41)

and

$$(I_{sp})_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{basic}} (I_{sp})_{basic} (5-42)$$

where  $P_c$  is the combustion chamber pressure, r is the grain burning rate, n is the exponent in the burning rate equation (Eq. 5-19), and all other symbols are as defined previously. If the grain erosion effects are significantly altered, or if the cham<sup>1</sup> — pressure during burning is not constant, this technique is not applicable. The above technique requires an iterative solution because the thrust coefficient is a function of the nozzle thrust area and combustion chamber pressure.

The total impulse may be changed by scaling the nozzle exhaust flow area, thus changing the expansion ratio so that

$$F_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{basic}} F_{basic}$$
(5-43)

$$(I_{sp})_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{basic}} (I_{sp})_{basic}$$
(5-44)

and

$$(I_{total})_{scaled} = \frac{(C_F)_{scaled}}{(C_F)_{basic}} \quad (I_{total})_{basic}$$

where all symbols are as defined previously.

When the propellant composition is changed, and when it is desirable to maintain the same chamber pressure as the basic motor by changing the nozzle configuration

$$(A_t)_{scaled} =$$

$$\left[\frac{P_{scaled}}{P_{c}}\right]^{1-n_{scaled}} \left[\frac{P_{c}}{P_{basic}}\right]^{(A_{t})_{basic}} (A_{t})_{basic}$$
(5-46)

$$(A_{exhaust})_{scaled} = \frac{(A_t)_{scaled}}{(A_t)_{basic}} \quad (A_{exhaust})_{basic}$$

$$(5-47)$$

$$F_{scaled} = \frac{(A_t)_{scaled}}{(A_t)_{basic}} F_{basic}$$
(5-48)

$$\begin{bmatrix} (a_1)_{basic} \\ (a_1)_{scaled} \end{bmatrix} \begin{bmatrix} p_c & (a_1)_{basic} \\ p_c & (b_2)_{basic} \\ (5-49) & (b_2)_{basic} \end{bmatrix}$$

 $(\theta_{b})_{scaled} =$ 

where p is the constant (combustion chamber pressure parameter) in Eq. 5-23,  $a_1$  is the constant in Eq. 5-19,  $n_{scaled}$  is the new propellant exponent in Eq. 5-19,  $n_{basic}$  is the old propellant exponent in Eq. 5-19, and all other symbols are as defined previously. The above technique is only applicable if the erosion characteristics are not altered significantly and the chamber pressure does not vary significantly during burning.

When changes in the basic motor require more than one of the techniques described above, the scaling should be performed in steps. One scaling technique should be completed and all scaled characteristics computed. This new information is used to complete the next scaling technique, and so on. Care must be exercised in scaling motors in which erosion is significant. Erosion characteristics may not scale well even when the ratio of grain internal flow area to nozzle throat area is preserved in the scaling.

#### 5-6 TESTING

Tests must be conducted on rocket propulsion systems during the periods of development, manufacture, and qualification. These tests are usually of the following types, although additional tests may be required depending on the peculiarities of the particular system:

a. Pressure proof and leak checks

b. Component functional and operational checks

c. Static firings

d. Flight performance

In some cases it may be desirable and necessary to test only statistical samples, while in other cases every item produced must be tested. Often it is possible to test scale models—utilizing scaling techniques discussed in Par. 5-5—thus reducing the cost, the size of the test item, and the size of the test facility. Rather than formulate rigid rules for designing test programs, the test designer should exercise freedom in establishing test criterie, basing his parameters upon the information required from the test and utilizing the most economical and expeditious testing methods.

Propulsion testing will be discussed in the paragraphs which follow. For a more complete presentation and an excellent bibliography, see Reference 1.

Instrumentation is required to measure forces, flows, temperatures, pressures, structural stresses, time sequences, and all other parameters-such as acceleration and vibrations-that are of interest. Instrumentation consists basically of a pickup, a sensing element, and an indicator. Auxiliary equipment, such as electronic amplifiers or telemetering devices to transmit flight measurements to ground stations, may also be needed. The pickup is installed at the location where the value of a particular parameter is to be measured and transmits the magnitude of the parameter to the sensing elements. The sensing element, which often is integral part of the pickup, gauges the magnitude of the parameter under consideration by mechanical, electrical, or other means. The

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indicator then displays the measurements of the sensing element. The American Society of Mechanical Engineers' Power Test Codes describe various forms of instrumentation and present recommendations for their use.

Extensive and elaborate safety precautions are required, especially during the rocket development period. Although solid propellants do not present the explosive hazard exhibited by liquid propellants, personnel must be located remotely when the rocket is launched, in case of explosion or an uncontrolled flight. The ignition must be initiated from a remote location, and the instruments must be capable of remote indication, to allow personnel to monitor and control the test in *i* dety. Photography and television are employed extensively to observe the rocket closely during the test. For flight tests, a range must be constructed that is instrumented and is located away from inhabited areas. For long-range flight tests, it is n ressary to build into the rocket a destruction present that can be activated from the ground if the trajectory should present a hazard to personnel or property.

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# **CHAPTER 6** STRUCTURES

## LIST OF SYMBOLS

Symbol

Symbol

- a Linear acceleration, ft/sec<sup>2</sup>
- A Area, ft<sup>2</sup>
- A, Cross sectional area of fin at exposed root chord (Table 6-1), ft<sup>2</sup>

Megnika

- ò Fin span, ft
- c Airfoil chord length, ft
- c Perpendicular distance from beam neutral surface, ft
- $\mathcal{L}_p$  Aerodynamic drag coefficient, dimensionless
- $C_f$  Skin friction coefficient (see Chapter 8), dimensionless
- C<sub>N</sub> Aerouy ent, per degree Aerodynamic normal force coefficient gradi-
- $C_p$  Constant pressure specific heat, BTU/lb °R
- cg Center of gravity
- cp Center of pressure
- d Diameter, ft
- D Aerodynamic drag force, lb
- E Modulus of elasticity (Young's Modulus), lb/ft<sup>z</sup>
- F Rocket thrust, lb
- $F_{12}$  Radiation combined emissivity, absorptivity, and orientation factor, dimensionless
- $h_{is}$  Inside surface heat transfer coefficient, BTU/ (sec) (ft<sup>2</sup>) (°R)
- hos Outside surface heat transfer coefficient, BTU/ (sec) (ft<sup>2</sup>) (°R)
- I Mass moment of inertia, slug-ft<sup>z</sup>; area moment of inertia, ft<sup>4</sup>
- k Thermal conductivity, BTU/(sec) (ft<sup>2</sup>) (°R/ft)
- K Coefficient of plate stress, dimensionless
- l, & Length or distance, ft
- In Natural logarithm
- m Mass, slug
- M Mach number, dimensionless; bending moment in structure, ft-lb

- $n_{\infty}$  Free stream Mach number, dimensionless

Meaning

- M.S. Margin of Safety, dimensionless
  - n Number of rivets
  - N Aerodynamic normal force, lb
- $N_{Nu}$  Nusselt number, dimensionless
- $N_{p_r}$  Prandtl number, dimensionless
- $N_{Re}$  Reynolds number, dimensionless
- p Pressure, lb/ft<sup>2</sup>
- P Structural load (force), lb
- Dynamic pressure, lb/ft<sup>z</sup>; heat transfer rate, q BTU/sec
- r Recovery factor, dimensionless; radius, ft
- Sref Rocket reference area, ft<sup>2</sup>
  - t Thickness, ft
  - T Temperature,  $^{\circ}\mathbf{R}$
  - **'**11 Overall heat transfer coefficient, ETU/(sec) (ft²) (°R)
  - V Velocity, fps
  - w Width, ft
  - ¥ Weight, lb
  - y Height, ft
  - Thermal radiation absorptivity, dimensionless; angle of attack, deg
  - $\beta$  Angle between the rocket longitudinal axis and the vertical, deg
  - y Ratio of specific heat at constant pressure to specific heat at constant volume, dimensionless
  - $\epsilon$  Thermal radiation emissivity, dimensionless
  - Time, sec θ
  - $\mu$  Dynamic viscosity, slug/ft-sec
  - ρ Density, slug/ft<sup>\*</sup>; internal gage pressure
  - Stress, lb/ft<sup>2</sup>; Stephan-Boltzmann radiation σ constant, BTU/(sec) (ft<sup>2</sup>) (°R<sup>4</sup>)
  - r Shearing stress, lb/ft<sup>2</sup>

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### 6-1 GENERAL

The rocket structure provides a specific external shape, a protective envelope, and a platform for the delivery of a payload to a target. This chapter will present methods of designing a structure with minimum weight and sufficient strength to withstand ground handling and flight loads.

The strength of a structure depends on the physical and mechanical properties of the materials, and the geometric configurations of the structural members. The proportional limit, elastic limit, yield point, ultimate strength, modulus of elasticity, ductility, and hardness are the significant properties of materials for preliminary design. These properties are defined as follows:

a. Proportional limit is the maximum stress that a material can resist without deviating from the law of proportionality of stress to strain (Hooke's law).

b. Elastic limit is the maximum stress that a material can resist without permanent deformation. The proportional limit and elastic limit are often taken as the same value.

c. Yield point is the minimum stress at which the material will deform without an increase in load, and also often will deform with an abrupt decrease in load.

d. Ultimate strength is the maximum stress in a material before fracture.

e. Modulus of elasticity is the ratio of stress to strain, at stresses below the proportional limit.

f. Ductility of a material is the percent of elongation at the time of fracture in tension.

g. Hardwess of a material is a measure of the resistance to scratching, abrasion, and indentation.

The physical dimensions, moment of inertia, and cross-sectional area are the significant geometric factors of the structural members.

#### **8-2 WEIGHT AND BALANCE**

#### 6-2.1 MASS AND CENTER OF GRAVITY ESTIMATION

The mass of much of the rocket structure and many of the rocket components will not be known and must be estimated. For analysis, the rocket should be divided into sections made up of homogeneous materials and volumes that are easily defined. 'The mass of the sections may be estimated by multiplying the section volume by the material density. The volume of thin-skin sections is easily approximated by multiplying the surface area by the skin thickness.

The equations for evaluating the volumes of some typical rocket sections are presented in Tab...s 6-1. The volume of an ogive nose cannot be so easily determined. A method of approximating the volume of an ogive was developed in Reference 1, based on the relationship between the ogive volume and volume of a cone with the same length and diameter. The equivalent cone volume can be evaluated from the nomograph in Fig. 6-1, and the ratio of ogive volume to cone volume can be obtained from Fig. 6-2. The equivalent cone surface area can be evaluated from the nomograph in Fig. 6-3, and the ratio of ogive surface area to cone surface area can be obtained from Fig. 6-4.

The location of the center of gravity of some typical rocket sections is presented in Table 6-1. For convenience these locations should be identified as rocket station numbers, i.e., distances from the nose tip. The location of the center of gravity of the complete configuration can be estimated by summing moments of the section masses about the nose tip and dividing by the total rocket mass, making sure that consistent units are used.

#### 6-2.2 PITCH INERTIA

The rocket pitch inertia is the mass moment of inertia of the complete configuration with respect to the pitch axis, which passes through the center of gravity and is perpendicular to the longitudinal axis of symmetry. For analysis the rocket should be divided, as '. fore, into sections marke up of homogeneous materials and easily defined geometrics. Then the pitch inertia of the complete configuration is the algebraic sum of the individual section moments of inertia with respect to the pitch axis. For convenience, the section moments of inertia may be evaluated with respect to an axis through the section center of gravity and transferred to the parallel pitch axis by the following formula:

 $I_{CC} = \overline{I} + m l^2 \qquad (6-1)$ 

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TABLE 6-1. GEOMETRICAL PROPERTIES OF TYPICAL ROCKET SECTIONS

						<u></u>					AMCP	705-28
MOYENT OF INZRIIA	$I_{g} = \frac{3\pi}{20} (r_{b}^{2} + \frac{t^{2}}{4})$	$I_c = \frac{3\pi r_b^2}{10}$	$\mathbf{I}_{\boldsymbol{\beta}'}$ . Treat as the difference between two cross	$I_{c} = \frac{3\pi (rB^{5} - rB_{1}^{5})}{10 (rB^{3} - rB_{1}^{3})}$	$I_{g} = \frac{\pi}{18} (3r^{2} + t^{2})$	2c ⊭ <u>≊r2</u> 	$\mathbf{I}_{\mathbf{B}}^{i}$ : Treat as the difference between two paraboloids	$I_{c} = \frac{m}{3} \left( \frac{r_{1}^{4} + r_{1}^{2} r_{2}^{2} + r_{2}^{2}}{r_{1}^{2} + r_{2}^{2}} \right)$	$I_{g} = \frac{m}{12} (3r_{1}^{2} + 3r_{2}^{2} + t^{2})$	$r_{c} = \frac{n}{2} (r_{1}^{2} + r_{2}^{2})$	I <sub>a</sub> <sup>3</sup> () (when compared to fin pitch fnertia)	$1_{\mathbf{v}} = \frac{1}{4} \begin{bmatrix} \mathbf{b}^2 & \left(\frac{1}{1} + \frac{3}{2} \frac{\mathbf{c}_{\mathbf{f}}}{1 + \frac{\mathbf{c}_{\mathbf{f}}}{2}}\right) + c_{\mathbf{c}}^2 \end{bmatrix}$
CENTER OF GRAVITY		± 1 2 2 2 3		$\chi_{CC} = \frac{4(r_{B}^{2} + 2r_{B}r_{B1} + 3r_{B1}^{2})}{4(r_{B}^{2} + r_{B}r_{B1} + r_{B1}^{2})}$		8	$x = \frac{1}{2} \left( \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2^{4}} \right) - \frac{2}{3} \left( \frac{1}{2} - \frac{1}{2^{6}} \right) \right]$	$cc (r_1^2 - r_2^2) (r_1^4 - r_2^4)$	X <sub>cs</sub> = <u>/</u>		$r_{CC} = \frac{1}{6} \frac{\left(1 + 2\frac{\frac{1}{2}}{c_T}\right)}{\left(1 + \frac{1}{c_T}\right)} + \frac{1}{2}$	At Centrold of Sectional Area
VOLUNE & SUPPACE AREA	SURFACE AREA = $x \pm B \sqrt{x_B^2 + t^2}$	volues = <sup>x x b<sup>2</sup> / 3</sup>	SUFFACE AREA = $\pi(r_B + r_{B_1}) \sqrt{s^2 + (r_B - r_{B_1})^2}$	volume = $\frac{\pi_{L}^{2}}{3}$ ( $r_{B}^{2} + r_{B_{1}}^{2} + r_{B}r_{B_{1}}$ )	SUTAGE AREA = $\frac{\Delta \pi \epsilon}{3t^2} \left[ \left( \frac{\epsilon^2}{4} + t^2 \right)^3 / 2 - \left( \frac{\epsilon}{2} \right)^3 \right]$	V9).Dræ = <u>#4r<sup>2</sup> 2</u>	SUURACE ANEA: Treat as the difference between two paraboloids	$volume = \frac{\pi t}{2} \left(r_{B}^{2} + r_{B_{1}}^{2}\right),$	1 TILL - SULADE) - STELL	VO:UNE = (rr1 <sup>2</sup> - rr2 <sup>2</sup> ) /	SUUACE AREA = Function of fin cross section	VOLDE = $\frac{\Lambda_{\rm r} b}{4} \left( 1 + \frac{c_{\rm h}}{c_{\rm r}} \right)$ constant thickness
FIGURE	CONE		COME FRUSTUM C		PARABOLODD OF R REVOLUTION CC		FRUSTAN OF E PARABOCOID OF PAR					
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Figure 6-2(C). Ratio of Volume of Tangent Ogive to Cone With Identical Q/d

where  $I_{CG}$  is the section moment of inertia with respect to the pitch axis,  $\overline{I}$  is the section moment of inertia with respect to the local axis that is parallel to the pitch axis, m is the mass of the section, and l is the distance between axes.

The moments of inertia of typical rocket sections can be determined from Table 6-1. The pitch moments of inertia of fins and ring tails may be approximated for preliminary design by considering the fin mass to be concentrated at the rocket base. Then,

$$\tilde{I}_{CG} = m l^2 \tag{6-2}$$

where m is the mass of the fins and l is the distance between the rocket center of gravity and the base. The error due to this approximation will be less than 4 percent if the fin root chord is less than one-third, and the span less than two-thirds, of the distance between the rocket base and the rocket center of gravity.

The moments of inertia are not explicitly defined in Table 6-1 for rocket sections that are partially hollow and/or made up of composite materials. The moments of inertia of these sections can be evaluated by employing the principle that, with respect to a common axis, the total moment of inertia is equal to the algebraic sum of the moments of inertia of the parts. For example, the total moment of inertia of a cone with a hollow cylindrical center is equal to the moment of inertia of the solid cone less the moment of inertia of the cylindrical portion.

#### 6-2.3 ROLL INERTIA

The rocket roll inertia is the mass moment of inertia of the complete rocket configuration with respect to the longitudinal axis of symmetry. For analysis, the rocket should be divided, as before, into sections made up of homogeneous materials and easily defined geometries. Then the roll inertia of the complete configuration is the algebraic sum of the individual section mements of inertia with respect to the longitudinal axis.




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The moments of inertia of typical rocket sections can be determined from Fig. 6-1. The moments of inertia are not explicitly defined in Table 6-1 for rocket sections that are partially hollow and/or made up of a composite of materials but may be evaluated as outlined in Par. 6-2.2 by algebraic summation of the moments of inertia of the parts.

# 6-3 LOADS

6-18

# **6-3.1 TRANSFORT AND HANDLING LOADS**

The preliminary design phase must consider flight loads in conjunction with transportation loads to insure that one does not predominate the other. However, flight loads are generally the most severe since adequate containers containing shock mounts can be designed to account for expected or unexpected transportation loads.

During transportation the rocket package will be subjected to vibrations, shocks, variable temperature environments, and moisture. Reference

2 presents packaging techniques for shipment. The loads during shipment by truck, ship, railway, or airplane are specified in References 3, 4, 5, 6, 7, 8, and 17. Truck transportation subjects the rocket to the most severe vibration and shock loads, and airplane transportation to the least severe, under normal conditions.

The human factor involved in handling makes the problem of specifying loads very lifficult. In general, realistic field conditions are simulated by drop tests. Heights used for these tests vary, from three and one-half feet for twenty pound articles, to one foot for articles weighing more than one hundred pounds.

Rockets launched from air vehicles may be subjected to severe vibrations. 'These loads should be determined from manufacturer's performance reports for the particular vehicle involved.

In general, military specifications are available to desine the design environmental conditions for a particular class of rockets. These specifications should be consulted in avaluating design loads.

### 6-3.2 FLIGHT LOADS

1.1

During flight the rocket will be subjected to loads from engine thrust, aerodynamic lift, aerodynamic drag, inertia of rocket mass, structural weight, and internal pressures. For structural stress analysis, the loads may be divided into axial components acting along the body longitudinal axis, bending components acting perpendicular to the body axis, and internal pressure forces acting circumferentially.

The axial load component is made up of forces from the engine thrust, aerodynamic drag, inertia of the rocket mass in the axial direction, structural weight component acting along the body axis, and internal pressures. Fig. 6-5 shows a free-body diagram of the axial forces acting on a rocket in flight. The sum of these forces is zero. Therefore,

$$-am + F - D - W \cos\beta = 0 \quad (6-3)$$

where a is the rocket acceleration along the longitudinal axis, m is the rocket mass, F is the engine thrust, D is the total drag, W is the rocket weight, and  $\beta$  is the angle between the body longitudinal axis and the vertical. Likewise, the axial load  $(P_{xx})$  at any plane x-x is found by the formula

$$P_{xx} = am_x + D_x + W_x \cos\beta - \rho A \quad (6-4)$$

where  $m_x$  is the rocket mass forward of plane x-x,  $D_x$  is the total drag on the rocket forward of plane x-x,  $W_x$  is the weight of the rocket forward of plane x-x,  $\rho$  is the internal gage pressure, and A is the area of the plane perpendicular to the longitudinal axis on which the internal pressure acts.

The drag coefficient on the rocket sections can be evaluated as indicated in par. 8-3. The drag force D can then be determined as follows:

$$D = C_{\rm D} q S_{\rm ref} \tag{6-5}$$





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where  $C_D$  is the drag coefficient, q is the dynamic pressure, and  $S_{ref}$  is the rocket reference area.

The bending load components are made up of forces from aerodynamic lift and inertia of the rocket mass in the direction purpendicular to the body axis. Manufacturing techniques permit thrust alignment to within approximately 10 sec of longitudinal axis, resulting in negligible bending loads. For preliminary design, the rocket section masses can be considered concentrated at the section centers of gravity, and the section lift forces concentrated at the section centers of pressure.

Fig. 6-6 shows the bending loads acting on a rocket in flight. The inertia loads are equal to

the mass m of the section, multiplied by acceleration a, acting in a direction perpendicular to the longitudinal axis, and

where N is the total lift on the rocket, W is the total weight, and  $\beta$  is the angle between the body longitudinal axis and the vertical.

The normal-force coefficient gradients on the rocket sections can be evaluated as indicated in par. 8-2. The normal force N can be determined as follows:

$$N = C_{N_{\alpha}} \alpha q S_{ref}$$
(6-7)



where q is the dynamic pressure,  $S_{ref}$  is the rocket reference area,  $\alpha$  is the angle of attack, and  $C_{N\alpha}$  is the normal force coefficient gradient. The bending moment at any section of the rocket is equal to the algebraic sum of the moments of the forces acting on either side of the section.

The circumferential load in the combustion chamber cylinder walls, as shown in Fig. 6-7, is caused by the internal pressure acting radially along the cylinder length. The circumferential load at plane A-A ( $P_{A-A}$ ) is

$$P_{A-A} = pA_{A-A} \tag{6-8}$$

where p is the combustion chamber internal gage pressure, and  $A_{A-A}$  is the area on which the pressure acts, projected on plane A-A.



# Combustion Chamber

# **6-4 STRESS**

### 6-4.1 BEAMS

A beam is defined as a structural member subjected principally to transverse loads that tend to bend it. The convex side of a loaded beam is in tension and the concave side is in compression. Between the convex and concave surfaces, there exists a plane called the neutral surface, where the tensile and compressive stresses are zero. The stress distributions across the section of a typical beam are shown in Fig. 6-8. The stress, due to bending loads only, on any element, is

$$\sigma = \frac{Mc}{I} \tag{6-9}$$

where  $\sigma$  is the tensile or compressive stress, Mis the bending moment, c is the distance (positive in the direction of the concave surface and negative in the direction of the convex surface) from the neutral surface to the element in which the stress is to be computed, and I is the section area moment of inertia with respect to an axis through the area centroid and perpendicular to the plane of the loads. When a beam is subjected to axial loads in addition to the transverse bending loads, the total stress on any element across a section of a beam is the algebraic sum of the loads acting independently. Therefore,

$$\sigma = \frac{Mc}{I} + \frac{P}{A}$$
 (6-10)

where P is the axial load, positive if compressive and negative if tensile; A is the area of the beam section; and all other symbols are as defined above. This equation is only true if the beam deflection is negligible and the beam is subjected principally to transverse loads. If the principal loads are axial, the structure must be treated as a column (see par. 6-4.2).

The body and fins of a rocket may act as beams. For preliminary design, the rocket body may be considered as a simple hollow cylinder. Then the maximum stress (positive at the concave surface and negative at the convex surface) at any section due to bending is

$$=\frac{4M}{\pi d_c^2 t}$$
(6-11)

where  $d_c$  is the cylinder diameter, t is the wall thickness, and all other symbols are as defined above. If the cylinder is also subjected to an axial load, the maximum stress is

0

$$\sigma = \frac{4M}{\pi d_c^2 t} + \frac{P}{\pi d_c t}$$
(6-12)



1

where P is the axial load (positive if compressive and negative if tensile), and other symbols are as shown above. The rocket fins act as cantilever beams (one end fixed), with the maximum bending moment occuring at the point of attachment to the rocket body. The maximum stress due to bending at any section of the fin is

$$\sigma = \frac{Mt}{2I} \tag{6-13}$$

where t is the airfoil thickness. The methods of calculating the area moments of inertia of various airfoil sections are presented in Table 6-2.

### **6-4.2 COLUMNS**

A column is defined as a structural member principally loaded axially in compression and of sufficient length that failure tends to occur by buckling at compressive stresses below the elastic limit. The classical formula for buckling is that developed by Euler as

$$P = \frac{\pi^2 E I}{l^2}$$
(6-14)

where P is the buckling load, E is the material modulus of elasticity (Young's Modulus), I is the minimum centroidal moment of inervia of the cross section, and l is the column length. Euler's formula is only applicable to very long columns. Generally, columns must be designed on the basis of empirically-derived relationships.

The rocket body may be a column susceptible to buckling. A method of evaluating the critical buckling stress in thin-walled cylindrical columns, such as rocket bodies, was developed in Reference 9 as

$$\sigma_{cr} = 9\bar{c} \left(\frac{2t}{d_c}\right)^{1.6}$$
(6-15)

where  $\sigma_{cr}$  is the unit compressive stress in the cylinder wall at which buckling will commence, *E* is the material modulus of elasticity, *t* is the cylinder wall thickness, and  $d_c$  is the cylinder diameter. If the cylinder is also subjected to transverse loads, the critical buckling stress due to the axial load is

$$\sigma_{cr} = \Re\left(\frac{2t}{d_c}\right)^{1.6} - \frac{4M}{\pi d_c^2 t} \qquad (6-16)$$

where M is the bending moment due to transverse loads.

### 6-4.3 PRESSURE VESSELS

For the classes of solid propellant rockets discussed in this handbook, the combustion chamber structure is the primary pressure vessel. This structure is generally cylindrical and is subject to circumferential tensile (or hoop) stresses in the walls due to the loads discussed in par. 6-3.2 and shown in Fig. 6-7. This tensile stress is

$$\sigma = \frac{pr}{t} \tag{6-17}$$

where  $\sigma$  is the unit tonsile stress, p is the internal pressure, r is the cylinder inside radius, and t is the wall thickness.

The internal pressure, acting on the ends of the cylindrical vessel, applies in the walls a longitudinal tensile stress that helps support the weight, drag, and inertia compressive stresses.

### 6-4.4 PLATES

Some of the rocket structure—such as access doors or fin panels—may be considered as flat plates, uniformly loaded and fixed around the edges. For such a rectangular plate, the unit stress is

$$\sigma = 6K \frac{Pw}{lt^2}$$
(6-18)

where  $\sigma$  is the unit stress, w is the plate width, *l* is the plate length, *P* is the total load on the plate, *t* is the plate thickness, and *K* is a function of the width-to-length ratio, as shown in Fig. 6-9. Reference 20 presents methods of calculating the unit stress in plates of other geometries and edge conditions.

### 6-4.5 JOINTS

Riveted, welded, and bolted joints are used in rockets of the class discussed in this handbook.

ANTA OF CROSS SECTION	A = <del>6</del>	A = c <sub>2</sub> (l - s)	$A = \frac{(\epsilon^2 - \epsilon^2)^2}{8\epsilon^2} \left(\frac{\pi}{2} - 8\tan^{-1}\frac{\epsilon^2}{\epsilon^2} + \frac{\epsilon^2}{\epsilon^2}\right)^{-\frac{1}{2}} \frac{\epsilon^2}{4\epsilon} \left(\epsilon^2 - \epsilon^2\right)^{-\frac{1}{2}}$	$A = \frac{(t^2 + c^2)^2}{8t^2} \left(\frac{\pi}{2} - 5tn^{-1} \frac{c^2 - t^2}{c^2 + t^2}\right) - \frac{c}{4t} (c^2 - t^2)$ - $\frac{(t_1^2 + c_1^2)^2}{8t_1^2} \left(\frac{\pi}{2} - \xitn^{-1} \frac{c_1^2 - t_1^2}{c_1^2 + t_1^2}\right) - \frac{c_1}{4t_1} (c_1^2 - t_1^2)$	$\Lambda = \frac{1}{2} (cc - c_1 c_1)$	A = ct (l - a) - cjti ( l - aj)
ATTANK NO TRACC	1 <b>ء</b> 148	I <sub>B</sub> = <sup>ct3</sup> (2 - 3a)	I <sub>2</sub> = 4ct <sup>3</sup> 26	I <sub>g</sub> = <sup>4ct<sup>3</sup></sup> · <sup>4c<sub>1</sub> t<sub>1</sub><sup>3</sup> 26</sup>	r <sub>2</sub> = <sup>cr3</sup> - <sup>cr4,3</sup> /48	$I_{5} = \frac{et^{3}}{24} (2 - 5a) - \frac{c_{1}t_{1}^{2}}{24} (2 - 3a_{1})$
TAUX A		W23.FIED 20USN.E WEDGE	BH-CONVEX	RQULOW BLCAWVEX	KOLON DOUBLE FEDGE	HOLLOR SOOIFIED DJUBLE WEDGE

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### Figure 6-9. Flat Plate Stress Width-to-Length Ratio Parameter

Riveted joints are classified as butt plates and butt straps, and are shown in Fig. 6-10. The stresses in these joints are of three kinds:

a. Tension in the connected members

b. Shearing in the rivets

c. Bearing stresses in riv. ts and connected members ai the surface of contact

Each rivet in a joint will carry an equal shearing stress for rivets of constant cross-sectional area. Therefore, the load across any section of the connected members is equal to the total load on the joint multiplied by the number of rivets between the section being analyzed and the applied load, and divided by the total number of rivets in the joint. The stress in the section then is

$$\sigma = \frac{\binom{n'}{n_1}P}{(w-nd)t}$$
(6-19)

where  $\sigma$  is the stress in the connected member, n'is the number of rivets between the applied load and the section under consideration,  $n_{t}$  is the total number of rivets in the joint, P is the applied load, w is the width of the section, n is the number of rivet holes that may be present across AMCP 706-280



Figure 6-10. Riveted and Bolted Saints

the section under consideration, d is the diameter of the rivets, and t is the thickness of the connected member. Where rivet patterns are repeating, it is only necessary to evaluate the stress in a single repeating section since the stress in all other sections will be equal. For example, the stress in the connecting member shown in Fig. 6-12 across the section A-A will be

$$\sigma = \frac{1/4 P}{(w - 2d)t}$$
(6-20)

The shearing rices s in the rivets is equal to the load on rice rivet divided by the cross sectional area of the rivet. Therefore, the unit shearing stress r is

$$r = \frac{4P}{n_{z}\pi d^{2}}$$
 (6-21)



# **FILLET TYPE**



where all symbols are as defined previously. - The bearing stress in the rivets or connected members at each rivet location is equal to the load on the rivet divided by the bearing area. Therefore, the bearing stress  $\sigma_b$  is

$$\sigma_b = \frac{P}{ndt} \tag{6-22}$$

where all symbols are as defined previously.

Welded joints may be used in conjunction with or as a replacement for riveted and bolted joints. Although there exists many types of welds, in many combinations and configurations, only the vec-type and fillet-type shown in Fig. 6-11 will be discussed as the most general and cominon. Welded joints are subjected to shearing, tensile, and compression stresses. The compression or tensile stress in a vee-type joint is equal to the applied load divided by the cross sectional area, at the weld, ot the thinnest member connected. Shearing is the significant stress in a fillet-type weld and is equal to the load, divided by the length of all welds in the joint, multiplied by the weld throat thickness.

Bolts may be subjected to the stresses discussed above for rivets and/or a tensile load along the longitudinal axis as shown in Fig. G-12. Each bolt may be considered to carry an equal portion of the tensile load. Then the unit tensile stress in each bolt is:

$$=\frac{1^{2}}{nA}$$
 (6-23)

where P is the tensile load, n is the total number of bolts in the joint, and A is the cross sectional area of the bolt.

σ

For a more extensive treatment of joints, see Reference 11.



Figure 6-12. Bolted Joints

# **6-5 SAFETY FACTORS**

The factor of safety is defined as the ratio of ultimate strength or yield strength of the material to the allowable stress. The ultimate strength is used for brittle materials and the yield strength for ductile materials. The factor of safety is employed to account for differences between design and actual load conditions, and for statistical variations in the structure. Large factors of safety are desirable for reliability but must be balanced against the associated increase in structural weight.

When possible, it is advisable to base the allowable stress on test results and eliminate the use of the factor of safety. When test data are not available, a factor of safety of 1.15 should be used for the structure in general. For pressure vessels and other structures that may be a hazard to personnel, a factor of safety of 2.0 should be used.

The margin of safety is defined as the ratio of excess strength to the required strength or:

$$M.S. = \left(\frac{\sigma_{allowable}}{\sigma}\right) - 1 \tag{6-24}$$

where M.S. is the margin of safety,  $\sigma_{allowable}$  is the allowable stress, and  $\sigma$  is the actual maximum stress. The margin of safety gives an indication of permissible load increases or structural strength decreases in design modification.

# 6-6 HEATING

### 6-6.1 GENERAL

Heat is transferred by the processes of conduction, radiation, and convection. In general, heat is conducted through a medium by the transport of the kinetic energy of both free electrons and molecules: heat is radiated by the transport of electromagnetic energy, requiring no transport medium; heat is convected by a combination of conduction, radiation, and the motion of a fluid mass. The heat transfer is considered to be transient if heat is being stored or released within the media involved and the temperatures of the media are varying with time The heat transfer is considered to be steady-state if the temperatures of the media do not vary with time. During steady-state conditions the one-dimensional heat transfer across any one section of a medium is equal to the heat transferred across any other parallel section.

### 6-6.1.1 Conduction Heat Transfer

The one-dimensional, steady-state conduction heat transfer through a homogeneous medium with a constant themal conductivity is

$$q = \frac{k}{t} A(T_{1} - T_{2})$$
 (6-25)

where q is the heat transfer rate, k is the thermal conductivity of the medium (obtained from material property data), A is the section area of the medium through which the heat is transferred,  $(T_f - T_g)$  is the temperature difference across the medium, and t is the medium thickness. For a composite of plane media such as shown in Fig. 6-13, the one-dimensional steady-state conduction heat transfer is equal to

$$A_{4-2} = \frac{yw(T_4 - T_2)}{\frac{t_1}{k_1} + \frac{t_2}{k_2} + \frac{t_3}{k_3} + \dots + \frac{t_n}{k_n}}$$
(6-26)





Figure 6-14. Cylindrical Conduction of Heat Transfer Medium

### FACE ORIENTATION

### Figure 6-13. Plane Conduction Heat Transfer <u>Hedium</u>

or in another direction is equal to

$$q_{5-6} = .$$

$$\frac{(k_1 t_1 + k_2 t_2 + k_3 t_3 + \dots + k_n t_n) y (T_5 - T_6)}{w}$$
(6-27)

where  $q_{4-2}$  and  $q_{5-6}$  are the one-dimensional conduction heat transfer rates from face 4 to 2 and face 5 to 6, respectively, with the other four faces insulated;  $T_4$ ,  $T_2$ ,  $T_5$ , and  $T_6$  are the uniform surface temperatures on faces 4, 2, 5, and 6, respectively; and all other symbols are as shown in Fig. 6-13. For a composite of cylindrical mediums such as shown in Fig. 6-14, the steady-state conduction heat transfer is equal to

$$q = \frac{l(T_{1z} - T_{oz})}{\frac{\ln(r_2/r_1)}{2\pi k_1} + \frac{\ln(r_3/r_2)}{2\pi k_2} + \frac{\ln(r_n/r_{n-1})}{2\pi k_n}}$$
(6-28)

where q is the conduction heat transfer rate,  $T_{is}$ and  $T_{os}$  are the uniform surface temperatures on the inside and outside of the cylinder, respectively, and all other symbols are as shown in Fig. 6-14.

### 6-6.1.2 Radiation Heat Transfer

All substances above the temperature of absolute zero emit thermal electromagnetic energy. A body that emits and absorbs the maximum amount of heat is defined as a black body and the heat it emits is equal to

$$q = oAT^4 \tag{6-29}$$

where q is the heat transfer rate;  $\sigma$  is the Stephan-Boltzmann constant, which in the English system of units is 0.48 × 10<sup>-12</sup> BTU/(sec) (ft<sup>2</sup>) (<sup>o</sup>R)<sup>4</sup>; A is the surface area of the body; and T is the absolute temperature of the body surface. Actual bodies radiate and absorb less heat than the black body. The ratio of heat emitted by a black body at the same temperature is called the emissivity  $\epsilon$  and is a function of the body material, temperature, and surface conditions. The heat radiated by an actual body is equal to

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$$q = \epsilon \sigma A T^4 \tag{6-30}$$

The ratio of heat absorbed by an actual body to the total amount of heat incident on the body (that which would be absorbed by a black body) is called the absorptivity  $\alpha$  and is a function of body material, temperature, surface condition, and heat source temperature. Emissivity and absorptivity values may be obtained from standard material handbooks.

The net radiation heat transfer between two bodies is a function of the bodies' emissivities, absorptivities, geometries, temperatures and orientations. This transfer is equal to

$$q_{1} = F_{12} A_{1} \sigma (T_{1}^{4} - T_{2}^{4})$$
 (6-31)

where  $q_1$  is the radiation heat transfer rate of body 1;  $F_{12}$  is the combined emissivity, absorptivity, and orientation factor, which may be obtained from such sources as Reference 12;  $A_1$  is the surface area of body 1; and  $T_1$  and  $T_2$  are the surface temperatures of bodies 1 and 2, respectively. Methods of obtaining the heat transfer between three or more bodies are described in Reference 13.

Following Reference 13, we may define a radiation heat transfer coefficient as

$$h_{Rad} = \frac{\sigma F_{12} (T_1^4 - T_2^4)}{(T_1 - T_2)}$$
(6-32)

By transposition and substitution in Eq. 6-31,

$$q_1 = h_{Rad} A_1 (T_1 - T_2)$$
 (6-33)

### 6-6.1.3 Convection Heat Transfer

The convection heat transfer between a fluid in motion and a solid is equal to

$$q = hA(T_f - T_s)$$
 (6-34)

where q is the convection heat transfer rate, h is the convection heat transfer coefficient, A is the area across which the heat is transferred, and  $T_f$  and  $T_s$  are the temperatures of the fluid and solid, respectively. The convection coefficient; is a function of the temperatures, fluid properties, solid geometry, and solid surface conditions.

The methods of evaluating convection coefficients for a variety of conditions are presented in Reference 14.

### 6-6.1.4 Combined Heat Transfer

Often the heat transfer under consideration takes place by the modes of conduction, radiation, and convection acting simultaneously. Therefore, it is convenient to define an overall heat transfer coefficient U which will include all modes of heat transfer present. For illustration, consider the cylinder in Fig. 6-14 with a hot fluid at temperature  $T_H$  flowing on the inside and a cold fluid at temperature  $T_c$  flowing on the outside. Then the steady-state heat transfer from the inside fluid to the outside fluid is

$$q = UA(T_{H} - T_{c})$$
 (6-35)

where

$$U = \frac{l}{A} \left( \frac{1}{2\pi r_1 h_{is}} + \frac{\ln (r_2/r_1)}{2\pi k_1} + \frac{\ln (r_3/r_2)}{2\pi k_2} + \dots + \frac{\ln (r_n/r_{n-1})}{2\pi k_n} + \frac{1}{2\pi r_n h_{os}} \right)^{-1}$$
(6-36)

 $h_{is}$  and  $h_{os}$  are the inside and outside heat transfer coefficients, respectively, for convection pluz radiation.

### 6-6.1.5 Transient Heat Transfer

When the heat transfer is transient, the rate at which heat is stored in a medium with a constant specific heat is equal to

$$q = mC_p \frac{dT}{d\theta}$$
 (6-37)

where q is the rate at which heat is stored, m is the mass of the medium in which the heat is stored,  $C_p$  is the constant pressure specific heat of the medium,  $dT/d\theta$  is the time rate of temperature change in the medium.

The solutions of three-dimensional transient heat transfer problems are more difficult than

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the above solutions and generally must be solved on high-speed digital computers.

# 64.2 COMBUSTION CHAMBER HEATING

The combustion process produces gas temperatures of 4000° to 7000°R depending on the propellant employed. Heat is transferred from the combustion chamber gases through the structure to the environment by conduction, convection, and radiation. The structure may be protected from overheating by employing insulating materials, a high heat capacity mass, or by transferring heat away to the environment.

The convection heat transfer coefficient on the inside of a cylindrical combustion chamber may be evaluated by the following relationship obtained from Reference 14:

$$N_{Nu} = \frac{hD}{k} = 0.023 \ (N_{Re})^{0.8} \ (N_{Pr})^{0.3}$$
(6-38)

$$N_{Re} = \frac{\rho VD}{\mu} \tag{6-39}$$

$$N_{Pr} = \frac{C_{pll}}{k} \tag{6-40}$$

where  $N_{Ne}$ ,  $N_{Pe}$ , and  $N_{Pr}$  are the dimensionless Nusselt, Reynolds, and Frandtl numbers, respectively; h is the convection coefficient; D is the inside diameter of the chamber; k is the thermal conductivity;  $\rho$  is the density; V is the velocity;  $\mu$  is the viscosity; and  $C_{\gamma}$  the constant pressure specific heat of the chamber gas.

The convection heat transfer coefficient on the outside surface of the combustion chamber is a function of the airflow properties at the particular location under consideration. If the outside surface is exposed to the airstream, the heat transfer may be evaluated as indicated in par. 6-6.3. For other locations, the convection heat transfer coefficients may be evaluated from references cited previously.

If the combustion is over a short period of time, steady-state conditions may not be reached. In this case, for preliminary design, it is recommended that the net heat transfer to the structure at the initial temperature be evaluated over

1×1

an increment of time. The temperature rise in the structure due to heat storage can then be evaluated. Then the net heat transfer to the structure at the new temperature for the next increment of time is evaluated, and so on. The accuracy of this method can be increased by taking smaller time increments.

The methods outlined above can also be used on the rocket nozzle with sufficient accuracy for preliminary design.

# 6-3.3 EXHAUST PLUME HEATING

The rocket exhaust plume transfers heat by radiation to the rocket structure, and by convection to the launcher and surrounding equipment. The heat transferred is a function of the geometry, temperature, flow properties, and radiation properties of the plume; it is also a function of the orientation, temperature, radiation properties, and configuration of the rocket structure, launcher, and surrounding equipment.

The plume geometry is dependent on the exhaust gas pressure and atmospheric pressure as shown generally in Fig. 6-15. The plume geometry, temperature, and flow properties can be defined specifically, as outlined in Chapter 5, par. 5-2.1. The convection heat transfer coefficients on the launcher and surrounding equipment may be determined from references cited previously. The radiation properties of the plume depend on the operating characteristics of the rocket engine. Since this information is generally not available for preliminary design, the conservative approach should be taken and the emissivity and absorptivity assumed to be equal to 0.9.

### 8-3.4 AERODYNAMIC FRICTION HEATING

The heating due to aerodynamic friction on rockets of the class discussed in this handbook generally will not be significant enough for consideration in preliminary design. Therefore, only a cursory discussion of aerodynamic heating will be presented. For a more detailed presentation, consult such sources as Reference 15.

Kinetic energy is imparted by friction to the air surrounding a rocket in flight. Therefore, in the rocket boundary layer there is a kinetic tem-

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Figure 6-15. General Geometry of Rocket Exhaust Plumes

perature zise above the temprature of the atmospheric air. At stagnation points, such as the rocket nose and leading edge of the fins, the air temperature is equal to the atmospheric air temgerature plus the complete kinetic temperature rise or

$$T_s = T_s + \left(\frac{\gamma - 1}{2}\right) M_{\infty}^2 T_o \qquad (6-41)$$

where  $T_s$  is the stagnation air temperature in absolute units,  $T_o$  is the atmospheric air temperature in absolute units,  $\gamma$  is the ratio of the specific heat of air at constant pressure to the specific heat at constant volume, and  $M_{\infty}$  is the free stream Mach number. In regions other than stagnation points, the temperature in the boundary layer will be less than the stagnation temperature calculated above, due to the heat transfer within the boundary layer. This temperature, called the recovery temperature, is evaluated as follows:

$$\underline{T}_{R} = T_{\sigma} + r \left(\frac{\gamma - 1}{2}\right) M_{\omega}^{2} T_{\sigma} \qquad (5-42)$$

where  $T_R$  is the recovery temperature in absolute units, and r is the recovery factor. The recovery factor for laminar and turbulent boundary layers is equal to the Prandtl number (Eq. 6-39) raised to the one-half and one-third powers, respectively. For a smooth flat plate, the boundary layer may be considered as laminar at Reynolds numbers less than 10<sup>5</sup> and turbulent at Reynolds numbers greater than 10<sup>5</sup>.

The heat transfer to the locket surface is evaluated as follows:

$$\frac{q}{A} = h(T_R - T_w) \tag{6-43}$$

where  $\frac{q}{A}$  is the heat transfer rate to the surface per unit area, h is the heat transfer coefficient, and T<sub>\*</sub> is the rocket surface temperature in degrees Rankine. The heat transfer coefficient for laminar and turbulent flow on a flat plate may be evaluated as follows:

$$(C_{H_{\infty}})_{laminar} = \frac{h}{C_{p}\rho_{\infty}V_{\infty}} = \frac{1}{(N_{pr})^{2/3}} \left(\frac{C_{f_{\infty}}}{2}\right)$$
(6-44)

and

$$(C_{H_{\infty}})_{turbulent} = \frac{h}{C_{p}\rho_{\infty}V_{\infty}} = \frac{C_{f_{\infty}}}{2}$$
 (6-45)

where  $C_{H_{\infty}}$  is the dimensionless Stanton number, h is the heat transfer coefficient,  $\rho_{\infty}$  is the

6-23

density of the free stream air,  $V_{\infty}$  is the free stream velocity,  $C_{f\infty}$  is the free stream skin friction coefficient, which is obtained as outlined in Chapter 8, par. 8-32. The heat transfer coefficient on cones is approximately 73 percent and 15 percent higher than flat plate values for laminar and turbulent boundary layers, respectively. Fins and cylindrical bodies may be considered as flat plates for purposes of preliminary design.

# 6-7 TESTING

A test program is often required to supplement the structural analyses outlined above since these analyses do not consider such factors as sizess concentrations, statistical variations, fabrication variations, and imperfections in structural materials and members. Although structural testing generally will not be performed during the preliminary phases of rocket design, a cursory discussion is presented here to indicate the types of tests usually conducted and the testing methods usually employed. Tests are classified as destructive if the test item is permanently deformed or fractured, and as nondestructive if the test item is structurally useful after the test.

The actual mechanical properties of materials may vary statistically from the generally published values. These variations may significantly affect the structural strength since factors of safety must be low to minimize weight. Therefore, samples of materials are prepared and tested, conforming to standards set by organizations such as ASME and ASTM. A detailed discussion of the testing of insterials is presented in Reference 16.

When evaluating structural members, it is generally desirable to employ nondestructive tests so as not to impair the usefulness of the tested item. Deep-seated irregularities such as cracks and voids in the structure can be identified by X-ray. Surface or near-surface irregularities can be identified by Magnaflux or Zyglo inspections. In the Magnaflux inspection the test item is covered by small magnetic particles which are attracted to local magnetic leakage fields around imperfections in the magnetized test item. In the Zyglo inspection, used on nonmagnetic materials, the test item is immersed in a fluorescent fluid that ponetrates and thus reveals cracks, voids, and other imperfections. Observation of the properties of sound waves passed through the structure will also reveal imperfections.

When using small factors of safety and when uncertainties exist concerning the structural strength, it is usually desirable to verify the structure by subjecting it to a proof test. This is especially true for pressure vessels. In general, proof tests are designed to subject the structure to a logd that will permanently deform it 0.01 percent or less.

For a more thorough discussion of structural testing—including vibration, creep, and impact—see Reference 16.

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# CHAPTER 7 ACCURACY

# LIST OF SYMBOLS

Symbol

C<sub>D</sub> Aerodynamic drag coefficient, nondimensional

Neoning

- C<sub>Rq</sub> Aerodynamic damping moment coefficient, nondimensional
- C<sub>Na</sub> rad Aerodynamic, , , rmal force coefficient, per
- CPE Circular probable error
- d Reference diameter of projectile or rocket, ft
- G Rocket acceleration due to thrust, ft/sec<sup>2</sup>
- Gravitational acceleration, ft/sec<sup>2</sup>
- Ι Moment of inertia, slug-ft<sup>2</sup>
- I<sub>sp</sub> Specific impulse, sec
- Radius of gyration, ft k
- L Thrust moment arm due to malalignment, ft
- Aerodynamic static margin, cal l., l.
- $l_t, l_t$  Distance from center of gravity to point of thrust application, ft
- In Natural logarithm
- Projectile mass, slug m
- Number of sample values taken from a uni-N verse of statistical values
- Number of revolutions made by rocket n<sub>a</sub> during first wavelength of yaw
- р Nondimensional launcher length (actual  $auncher length / \sigma$  )
- PE Probable error
- p Rocket spin rate, rad/sec
- Component of projectile angular velocity in q the direction of projectile y axis, rad/sec
- R Standard range, km
- Computed standard deviation s
- Aerodynamic reference area, ft<sup>2</sup> S
- S Nondimensional burning distance (actual burning distance  $/\sigma$ )
- Time of flight, sec; Student's t value t
- u, w Components of projectile velocity in the direction of x and z axes, ft/sec

- Symbol
- Meaning
- V Estimate of population variance
- v Projectile velocity, it/sec
- V. Wind velocity, ft/sec
- Wind velocity in flight-path plane, ft/sec
- Wind velocity normal to flight path, ft/sec w7
- $\vec{X}, \vec{Y}, \vec{Z}$  Earth-fixed launch coordinate system
- x, y Specific sample value taken from a universe of statistical values
- $\overline{x}$ ,  $\overline{y}$  Estimate of  $\mu$  based on available sample values
  - Angle of attack, degrees or rad α
  - β Dispersion reduction parameter ( $\beta$  = dispersion with reduction technique/dispersion with no reduction technique)
- $\gamma_{TS}$  Steady state flight path angle with no disturbances, mils
- ٨ Incremental change in the variable following the symbol
- Thrust malalignment angle, mils δ
- Aerodynamic malalignment angle, mils δŗ
- Angle between rocket longitudinal axis and principal axis, mils
- Projectile pitch attitude angle, measured θ from horizontal, rad
- Mean of a universe of statistical values ĸ
- Atmospheric density, slug/ft<sup>3</sup> ρ
- Yaw oscillation distance or wavelength, ft; σ standard deviation of a sample of size N
- Initial oscillation distance, ft σ
- Standard deviation of a system containing  $\sigma_{sys}$ n statistical variables
- $\sigma_{r}(\sigma_{y})$  Standard deviation of the x(y) values
  - Projectile roll angle, rad +
  - Projectile yaw attitude angle, measured ılı from vertical launch plane, rad
  - Partial derivative д

7.1

3

# 7-1 INTRODUCTION

Accuracy is the measure of the ability of the rocket system to position the payload at a given point at warhead event. Various error sources inherent in the rocket system, together with external conditions such as winds, cause a dispersion of the payload from its intended path. To determine the accuracy of a rocket system, a series of rockets are launabed under carefully controlled conditions. The a tual flight paths of the rockets are compared to an idealized trajectory in order to calculate the discersion. As in the study of the accuracy of any mechanical instrument or system, the error sources are first identified and then categorized as to whether they are predictable (allowing a compensation to be made) or random. The most significant factors influencing the accuracy of free rockets have been identified by extensive comparisons between experimental tests and theory. This chapter is a detailed discussion of the error sources. The main objective is to describe how the designer must compensate for the errors in order to achieve the level of accuracy required by the mission specifications.

# **7-2 DEFINITIONS OF ERROR SOURCES**

The flight of a rocket is divided into three phases:::(1) the launch phase, (2) the propulsive or burning phase, and (3) the ballistic phase. Error sources are labeled according to the phase of flight during which the error causes the rocket to deviate from the idealized trajectory. For example, a burning phase error will cause a deviation to occur between launch and burnout. If no additional errors are encountered during the ballistic phase, the burning phase error will still result in a dispersion of the warhead event. The total error, including prelaunch errors not associated with flight, is the net dispersion due to all errors.

a. Prelaunch Errors. All errors, including aiming errors and prelaunch corrections, that are accrued before rocket ignition.

b. Launch Phase Errors. Those errors that are associated with and result from the launch phase, including the initial conditions transmitted to the rocket by the launcher and dynamic unbalance effects of the rocket. c. Propulsive Phase Errors. The dispersions that result from such errors as thrust malalignment, nonstandard meteorological conditions, aerodynamic assymmetries, and propulsion variations.

d Ballistic Phase Errors. Those dispersives that occur during the period from propulsion cutoff to the end of flight.

The following paragraphs will be concerned with the individual error sources and methods for computing approximate dispersions.

# 7-3 DESIGN CONSIDERATIONS INFLUENCING ACCURACY

The effect of design variables on accuracy and the delicate trade-off process involved in dispersion reduction can be more easily understood by dividing all errors into two groups: (1) speed change errors, and (2) angular errors.

### 7-3.1 DESIGN CONSIDERATIONS ASSOCIATED WITH SPEED CHANGE ERRORS

The speed change errors are characterized by a change from the nominal velocity attained at propellant burnout. These errors, which result in an error in the plane of the trajectory, are due primarily to the variability present in the propulsion system. Any variation in a parameter that influences the delivered total impulse will obviously result in a different burnout velocity of the rocket. These include variations in:

a. Total loaded propellant

b. Propellant specific impulse due to chemical composition

c. Specific impulse due to physical quantities (e.g., nozzle throat diameter)

d. Inert parts weight

In addition to propulsion system variability effects, the burning time and thrust of solid propellant rockets are effected by propellant temperature. Even though the temperature has a negligible effect on total impulse, it does affect the burnout velocity because the rocket is subjected to a different drag history.

Speed change errors are a function of mechanical design manufacturing control, and propellant selection. These items are discussed in more de-

tail in Chapters 5 and 6. The remainder of this chapter will deal exclusively with the angular errors.

# 7-3.2 DESIGN CONSIDERATIONS ASSOCIATED WITH ANGULAR ERRORS

The angular errors are characterized by a change from the degired direction of the velocity vector at propellant burnout. The errors have components both in the plane of the nominal trajectory and normal to that plane, and are caused by:

a. Wind normal to the velocity vector

b. Thrust malalignment or the failure of the thrust vector to pass through the center of gravity

c. Dynamic unbalance

d. Aerodynamic assymmetries

Since the effect of the last two errors can be shown to be equivalent to thrust malalignment, in the paragraphs which follow we shall discuss only wind and thrust malalignment effects.

### 7-3.2.1 The Effect of Aerodynamic Stability

The aerodynamic stability of a rocket is the measure of the tendency of the rocket to align itself with the relative wind. If an aerodynamically stable rocket in steady flight with no aerodynamic moments should be given a disturbance such as a sudden increase in angle of attack, the aerodynamic forces caused by the disturbance direct the rocket back to its original state. The motion of the rocket immediately following the disturbance is generally a rotational osc llation about a lateral axis. One of the most important parameters in the study of the behavior of free rockets is the distance the rocket travels during one oscillation. The yaw oscillation distance  $\sigma$ is related to the aerodynamic stability of the rocket by the static margin (the moment arm of the corrective aerodynamic forces):

$$\sigma = 2\pi \sqrt{\frac{2I}{\rho Sl_s d C_{N_{\alpha}}}}$$
(7-1)

where

 $\sigma$  = yaw oscillation distance or wavelength of yaw, ft

- I = moment of inertia of the rocket about a lateral axis, slug/ft<sup>2</sup>
- $\rho$  = atmospheric density, slug/ft<sup>\*</sup>
- S = aerodynamic reference area, ft<sup>2</sup>
- $l_s =$ rocket static margin, cal
- d = rocket reference diameter, ft
- $C_{N_{\alpha}} =$ rocket normal force coefficient gradient, rad-1

Since  $\sigma$  depends on the aerodynamic coefficients of the rocket, it is subject to a large change during flight as the velocity and/or altitude of the rocket change. Fig. 7-1 shows the variation of  $\sigma$ and the building of angular dispersion for a typical flight.

From the figure, it is seen that most of the dispersion takes place during the first yaw oscillation. During this time  $\sigma$  does not change appreciably (this has been found to be generally true). Therefore, the dependence of dispersion on  $\sigma$  is mainly determined by the initial wavelength of yaw. This initial value will be used to describe the wavelength of a flight.

### 7-3.2.2 The Effect of Wind

Fig. 7-2 illustrates the effect of a wind on a stable rocket.

It can be seen that the rotation of the rocket into the relative wind causes the thrust to drive the rocket from the intended path. Fig. 7-3 shows the effect of  $\sigma$  on the dispersion due to wind. As the rocket becomes less statically stable (thereby increasing  $\sigma$ ), the sensitivity to wind reduces. This suggests that the designer should adjust parameters so as to maximize  $\sigma$ . However, as will be shown in the next paragraph, consideration of the dispersion due to thrust malalignment imposes a conflicting requirement on  $\sigma$ .

### 7-3.2.3 The Effect of Thrust Malalignment \*

Fig. 7-4 shows the effect of a malalignment of the rocket thrust with the vehicle axis. An angular malalignment is indicated. However, the same moment can also be caused by the vehicle. center of gravity lying off the centerline of the vehicle. In fact, a displaced center of gravity has been shown to produce larger angular error than does an angular malalignment.





Figure 7-4. Effect of a Thrust Malalignment on an Aerodynamically Stable Rocket

'The figure indicates that a thrust malalignment causes an aerodynamically stable rocket to rotate until the aerodynamic corrective moments are equal to the moment caused by the malaligned thrust.

Fig. 7.5 shows the effect of  $\sigma$  on the angular dispersion due to thrust malalignment.

For minimum thrust malalignment effects, the designer should select the smallest possible value of  $\sigma$  (maximum aerodynamic stability).

Combining the two error sources produces Fig. 7-6 which suggests an optimum value of  $\sigma$  for minimum total dispersion during burning. The designer may adjust the rocket parameters to obtain this value of  $\sigma$ .

Thé conflicting requirements on the wavelength of yaw result because an attempt was made to decrease two different types of errors by the same method, changing aerodynamic stability. We shall now consider a different method by which the dispersion caused by a body-fixed error, such as thrust or fin malalignment, can be reduced.

### 7-3.2.4 The Effect of a Slow Spin

Fig. 7-7 describes the build-up of the dispersion of a nonrotating rocket with a thrust malalignment. Because the thrust is applied in an unchanging direction, the dispersion grows steadily with time. Fig. 7-8 shows the effect of giving the rocket a slow spin about its longitudinal axis. In this case the direction of the thrust changes as the body rotates. The result is a reduction in the total angular dispersion.



Figure 7-5. Effect of Wavelength of Yaw on Angular Dispersion Due to Thrust Malalignment











Figure 7-8. Growth of Angular Dispersion for a Rocket With a Thrust Malalignment and a Slow Spin



Figure 7-9. Effect of Spin on the Build-Up of Angular Dispersion Due to Thrust Malalignment

Fig. 7-9 describes the variation of the angular dispersion with distance for a typical rocket with and without a slow spin.

From the above discussion, it follows that spin of any kind will have some effect on the angular dispersion of a rocket. The significant factor that determines the effect of a spin technique is the relation between the rotational motion of the body-fixed error and the rotational motion of the rocket about a lateral axis. The rotational motion of the rocket has been shown to be characterized by the wavelength of yaw; therefore, it is expected that this parameter will have a strong influence on the effectiveness of any spin program.

As was shown in Fig. 7-1, most of the angular dispersion takes place during the first yaw oscillation. The spin motion during this period will have the most influence on the angular dispersion. If the spin is constant or increasing in the same direction, the error will tend to accumulate because the acceleration of the rocket causes the influence of the malalignment to decrease as the rocket momentum increases. Therefore, the dispersion caused by the first half of the spin cycle is not completely compensated for by the second half. A uniform spin program will always result in some finite error.

The above considerations have led investigators to study nonuniform spin programs with the intention of developing techniques that would result in zero angular dispersion. The simplest program to visualize is the instantaneous, 180 deg rotation of the v hicle at some point in the trajectory. The point is chosen so that the accumulation of angular dispersion to that point is completely eliminated by reversing the direction of the wror. This concept has been incor-

porated into the Spin-Buck Program which is discussed in par. 7-7.2.4.

Par. 7-7.2 discusses several spin programs which have been of interest to designers of free rockets.

### 7-3.2.5 The Effect of Dispersion Reduction on the Optimum o

The amount of dispersion reduction obtained from any given spin program is measured by the parameter  $\beta$  which is the ratio of the dispersion with no spin to the dispersion with the spin program. Other paragraphs in this chapter indicate values of  $\beta$  for several spin programs. Once estimates of  $\beta$  are known, one can find the optimum value of  $\sigma$  which accounts for the combined effects of the spin-program on thrust malalignment and of the effect of winds. For short launcher lengths:

$$\sigma_{OPT} = \left[\frac{4\pi k^2 V_{\star}}{\sqrt{G} L \beta}\right]^{2/3}$$
(7-2)

where

= rocket radius of gyration, ft

 $V_{*} =$  wind velocity, ft/sec

 $G = \text{rocket acceleration, ft/sec}^{z}$ 

L = thrust malalignment distance, ft

 $\beta$  = dispersion reduction factor, dimensionless

The dispersion for this value of g is given by

$$\gamma_{TS} = \sqrt{\frac{3}{8}} \left[ \frac{(4 \pi)^2 L \beta V_v^2}{G k^2} \right]^{1/3}$$
(7-3)

It is shown in the following paragraphs that the optimum design depends on yaw oscillation wavelength, launching technique, and error source magnitude. In order that these items may be evaluated, these paragraphs present more detailed discussion of the errors and the means of computing dispersion under varying conditions.

# 7-4 PRELAUNCH ERRORS

When preparing to launch a rocket at a specified target, we must first establish the launch angle in the vertical plane (QE) and the azimuth angle under standard conditions. The term standard here applies to the flight that exists under arbitrarily chosen meteorological, positional, and material conditions. Corrections must then be made to this standard aiming for variations of the conditions existing for a given flight from the standard. Both the standard aiming and the corrections are generally obtained from a firing table which is a catalog of standard trajectories and corrections for nonstandard conditions. For example, the usual rocket firing table includes the following:

a. Pertinent data for the standard trajectories of the rocket.

b. Corrections to the standard aiming to compensate for rotation of the earth.

c. Corrections to the standard launch elevation (QE) to compensate for variation in propellant temperature, uninhibited propellant weight, atmospheric pressure, density and temperature, inert weight, and wind.

d. Corrections to the standard azimuth aiming for wind.

### 7-4.1 AIMING ERRORS

Aiming errors may exist due to any combination of the following:

a. Incorrect determination of the standard aiming from the firing table.

b. Error in positioning of the launcher.

c. Incorrect determination of the corrections to be applied for the nonstandard flight.

These errors, while due to different causes, all result in a physical displacement of the launcher from that position required for the rocket to acquire the target. The errors at payload disposition resulting from aiming errors of the launcher are:

$$\Delta Y = \Delta \psi_o R \tag{7-4}$$

$$\Delta X = \Delta \theta_{o} \frac{\partial R}{\partial \theta} \bigg|_{Y = \text{const}}$$
(7-5)

$$\Delta t = \Delta \theta_o \quad \frac{\partial t}{\partial \theta} \mid R = const \quad (7-6)$$
7-7

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$$\Delta Z = \Delta \theta_{o} \left. \frac{\partial Z}{\partial \theta} \right|_{t = const}$$
(7-7)

 $\Delta \psi_o = \psi_{oSTD} - \psi_o \tag{7-8}$ 

$$\Delta \theta_{0} \theta_{0} = \theta_{0}$$
 (7.9)

where

- $\Delta Y =$  deflection error, m
- $\Delta X = range error, m$
- $\Delta t = time of filght error, sec$
- $\Delta Z =$  altitude error, m

 $R = \pi$  standard range, km

- $\Delta \psi_{o} =$  azimuth aiming error, mils
- $\Delta \theta_o = \pm i evation \ a iming \ error, \ mils$

The errors are determined by calculating the difference between a flight with an error and a standard trajectory. Fig. 7-10 illustrates these quantities.

The derivatives— $\partial R/\partial \theta$ ,  $\partial t/\partial \theta$ , and  $\partial Z/\partial \theta$  — will be discussed in more detail in par. 7-8.

# 7-5 CALCULATIONS OF ANGULAR ERRORE

The angular error of a rocket is obtained by solving the differential equations of motion throughout the flight. The equations can be solved with as much generality as desired on an automatic computer. Values are chosen for the error sources and a number of parametric runs are made. The results can then be combined statistically as outlined in par. 7-10.



# Figure 7-11. Definitions of Sign Conventions for the Rocket Equations of Motion

If we assume missile symmetry about the longitudinal axis (Fig. 7-11)—so that normal small angle approximations are valid--and if we omit gyro effects due to missile roll, then the six-degree-of-freedom equations of motion become decoupled in the vertical and horizontal planes. Furthermore, the motion in the two planes is identical except for the gravity terms in the vertical plane. (The effect of gravity is equivalent to a bias error and will not be considered in these equations.) We can then determine the solution

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Figure 7-10. Aiming Errors

# 7-4.2 ERRORS DUE TO VARIATIONS IN METEOROLOGICAL CONDITIONS

In making corrections for nonstandard conditions, one assumes a knowledge of the existing nonstandard conditions. Any variation in conditions from the assumed values introduces an error at the point of warhead disposition. These errors may be treated in the same manner as those described below for the launch, propulsive, and ballistic phases.

in only one plane, thus simplifying the problem considerably. The equations to be solved then become

$$\dot{u} = [G] - \frac{\rho u^2}{2} \left[ \frac{C_D S}{m} \right]$$
 (7-10)

$$\dot{w} = qu - \frac{\rho u}{2} \left[ \frac{C_N S}{m} \right] (w + w_Z) + [G] \delta cos \phi$$
(7-11)

$$\dot{q} = -u \left[ \frac{4\pi^2}{\sigma^2} \right] \left\{ w + w_Z \right\}$$

$$-\left[\frac{C_{nq}d}{2C_{N_{\alpha}}l_{s}}\right]q + \delta_{F}cos\phi + \left[\frac{Gl_{t}}{k^{2}}\right]\delta cos\phi$$
(7-12)

 $\dot{X} = u$  (7-13)

$$\dot{Z} = w - u \theta \qquad (7-14)$$

$$\dot{\theta} = q$$
 (7-15)

$$\phi = f(t)$$
 (This is specified by the spin  
program.) (7-16)

where

θ

m

- u, w = components of the rocket velocity in the directions of the  $X_b$  and  $Z_b$  body axes, ft/sec
- $q, \phi =$  components of the rocket angular velocity in the directions about the  $Y_b$  and  $X_b$  body axes, rad/sec
  - = rocket pitch angle, rad
- $\phi$  = rocket roll angle, rad
- $\dot{X}$  = component of the rocket velocity in the slant range direction, ft/sec
- z = component of the rocket velocity normal to the slant range direction, ft/sec
- G = rocket acceleration due to the thrust, ft/sec<sup>2</sup>
- C<sub>p</sub> = aerodynamic drag coefficient, nondimensional
  - = rocket mass, slug
- S = aerodynamic reference area, ft<sup>2</sup>

- $C_{n_{\alpha}} = aerodynamic pormal force gradient, rad<sup>-1</sup>$
- C<sub>aq</sub> aerodynamic damping moment coefficient, dimensionless
  - 😑 = aerodynamic static margin, cal
  - Listance from center of gravity to point of thrust application, it
  - = reference body diameter, ft

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- = rocket radius of gyration, ft
- = thrust malalignment angle, rad
- $\delta_{\rm F}$  = aerodynamic malalignment angle, rad
  - = component of wind in direction of the  $Z_b$  body axis, ft/sec
- $\sigma$  = wavelength of yaw, ft
- = atmospheric density, slug/ft<sup>\*</sup>
- $X_b$ ,  $Y_b$ ,  $Z_b$  = body-fixed axes with origin at the center of gravity and  $X_b$  along the missile axis

The six expressions in brackets completely specify all the rocket characteristics needed to calculate its motion. Therefore, if the rocket motion is tabulated for variations in each of the six expressions, the results will be applicable to any configuration for which these parameters are known.

Examination of the solutions of the above equations for typical rocket systems indicates that only a relatively few parameters have first-order effects on the angular dispersion. These are the rocket acceleration G, the wavelength of yaw  $\sigma$ , the nondimensional launcher length P, and the burning distance S.

For the equations above, the launcher affects the motion of the rocket through the initial conditions. For convenience, we shall use a nondimensional expression for the launcher length:

$$P = \frac{launcher \ length}{\sigma}$$

The effect of launcher length, then, is represented by an initial value of velocity;

$$u_p = \sqrt{2PG\sigma} \qquad (7-17)$$

where  $u_p =$  velocity in ft/sec at the end of the launcher.

These equations can now be solved on an analog or digital computer and the dispersion at the end of flight determined for any given error source.

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A more informative approach for the designer is to consider each phase separately and identify the major contributors to the latent error.\* In each flight phase different forces predominate; therefore, the important parameters change. In the following subparagraphs the important parameters for each phase will be discussed.

Considering the errors in each flight phase separately has two advantages: (1) the equations can be simplified by including only the forces that predominate during the phase, and (2) the simplified equations can be manipulated to provide analytical solutions. The availability of analytical solutions is of great benefit to the designer because the important variables or gombinations of variables that determine the angular error can be easily identified. These results can then be combined with computer calculations that provide the required accuracy.

Analytical results have been prepared wherever possible and have been plotted with computer issults in illustrate their accuracy.

The criterion chosen for determining the accuracy of a rocket system during the launch and propulsive phases is the dispersion at warhead event. The effects of various errors and the effectiveness of several dispersion reduction techniques will be considered in terms of the steadystate flight path angular error. This representation alkiws rapid evaluation of the accuracy of the rocket without resorting to the complex methods of amounting for ballistic phase errors presented in par. 7-9.

The rocket equations were solved, using an automatic computer, for the burning phase of flight. The angular dispersion at the end of the boost phase is approximated by the following expression:

$$\gamma_{TS} = \theta - \frac{w}{u} + \frac{qk^2}{ul_s} - \frac{\rho SdC_{nq}}{4mul_s} (w + w_Z)$$
(7-18)

where the values of  $\theta$ , w, u, q and the aerodynamic parameters are those at burnout.  $y_{TS}$  is determined by computing  $\lim_{t\to\infty} \frac{2}{u}$  which is the  $t\to\infty$  steady state, post-boost angular dispersion of the direction of the velocity. Thus, for calculating the effect of the boost phase on dispersion at warhead event,  $\gamma_{TC}$  may be treated as an aiming error. The missile is assumed to be launched with the initial conditions taken from booster burnout.

# 7-6 LAUNCH PHASE ERRORS

During the launching process the rocket is deflected from its intended path by motion of the launcher and motion caused by the release of the launcher constraints. The results are conditions undesirable at the beginning of the propulsion phase. These conditions are separated into three modes of motion: (1) initial angular velocity about a lateral axis, (2) initial translational velocity normal to the launcher axis, and (3) angular velocity resulting from rocket dynamic unbalance when some form of spin on the launcher is used. Subparagraphs 7-6.1 through 7-6.3 present the angular dispersion at flight termination caused by these initial conditions.

### 7-6.1 ANGULAR VELOCITY

Figs. 7-12 (A), (B), (C) show the angular dispersion caused by an initial angular velocity of 100 mils per sec. The launcher length, the wavelength of yaw, and acceleration have substantial effects on the dispersion. The dispersion is minimized by increasing the launcher length and the rocket acceleration while keeping the aerodynamic stability as high as possible, i.e., a small value of  $\sigma$ .

### 7-6.2 TRANSLATIONAL VELOCITY

Figs. 7-13 (A), (B), (C) show the effect of an initial translational velocity of 1 ft per sec, normal to the launcher line, on the angular dispersion. The launcher length does not significantly affect the dispersion. An increase in the wavelength of yaw has a beneficial effect that is significant for rockets with high aerodynamic stability. Increasing the rocket acceleration causes a decrease in the dispersion for all cases considered.

<sup>&</sup>quot;The latent sigular error is the error at the end of a given phase. The idealized trajectory must then be used to determine the error at the end of flight.







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The angular dispersion due to initial translational velocity is minimized by making the rocket acceleration as high as possible and the aerodynamic stability low.

### 7-6.3 DYNAMIC UNBALANCE

Dynamic unbalance is caused by spinning the rocket about its geometric longitudinal axis rather than its principal axis of inertia. When the rocket is spun on the launcher, release of the launcher constraints will result in a motion, characteristic of the force-free procession of a rigid body unless the rocket is spinning about its principal axis of inertia (i.e., its dynamic axis). The dynamic unbalance effect limits the spin rate that can be used to reduce thrust malalignment effects.

The precession motion is, for all practical purposes, an angular velocity at launch. The magnitude of this initial angular velocity is:

q<sub>equiv</sub> = pe

where:

p = rocket spin rate, rad/sec

q<sub>equiv</sub> = equivalent initial angular rate due to dynamic unbalance, rad/sec

= angle between the rocket longitudinal and principal axes, rad

After determining the equivalent angular velocity, Figs. 7-12, 7-13, and 7-14 can be used to determine the angular dispersion.

The dispersion due to dynamic unbalance is minimized by increasing the launcher length and the rocket acceleration while maintaining a high level of aerodynamic stability. In addition, the dynamic unbalance angle  $\epsilon$  should be kept as small as possible by careful design and care in manufacturing. The spin rate should be kept as low as possible after considering the requirement for reducing the dispersion due to thrust malalignment.

Par. 7-7.2.6 describes how the effect of dynamic unbalance at launch can be reduced by a unique Tauncher design.

# 7-7 PROPULSION PHASE ERRORS

Angular errors which originate during the propulsion phase of flight are primarily caused by wind normal to the direction of flight, and thrust malalignment. A qualitative description of the effect of wind and thrust malalignment was given in par. 7-3. This paragraph presents some quantitative results which describe the effects of the important rocket parameters on the angular dispersion caused by the same two error sources, wind and thrust malalignment. These results can be used for preliminary accuracy estimates.

Par. 7-3 showed how spinning the rocket about its longitudinal axis will reduce dispersion caused by body-fixed error sources such as thrust malalignment. The major portion of this paragraph is devoted to describing the effectiveness of several spin programs developed to minimize the angular error due to body-fixed error sources In most applications, the choice of a spin technique is heavily influenced by the difficulty of mechanically implementing it. Therefore, while several of the methods presented here result in near-zero dispersion, complexity of the devices needed to carry out the spin program limit its use to systems where high accuracy requirements justify extreme measures.

### 7-7.1 NONROTATING ROCKET

Figs. 7-14 (A), (B), (C) and 7-15 (A), (B), (C) show the angular error caused by a 10 ft per sec wind normal to the flight path of the rocket and by a 0.5-mil thrust malalignment on a nonrotating rocket.

Since the wind force on a symmetric rocket does not depend on the roll crientation, spin does not affect the dispersion due to wind. Therefore, Figs. 7-14 (A), (B), (C) are applicable to any rocket system.

As was pointed out in par. 7-3, the angular dispersion due to wind is minimized by keeping the aerodynamic stability as low as possible. The figures indicate that is uncher length has very little effect on the wind dispersion. The rocket acceleration should be large.

The dispersion due to thrust malalignment is minimized by keeping the aerodynamic stability as high as possible. The effect of acceleration is most significant for rockets with low stability. The angular dispersion increases with increasing acceleration. The effect of launcher length is significant under all conditions—a long launcher is desirable.





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# 7-7.2 DISPERSION REDUCTION TECHNIQUES

Par. 7-3 pointed out that the conflicting requirements on aerodynamic stability caused by wind and thrust malalignment could be overcome by reducing the effects of the malalignment with a separate technique. The most common methods used to reduce the malalignment error employ spin; however, there are other possibilities, such as the variable acceleration program described in par. 7-7.2.6.

The effectiveness of a given method in reducing angular dispersion is represented by the dispersion reduction factor  $\beta$ .  $\beta$  is the ratio of the value of an mular dispersion associated with the dispersion reduction scheme being considered to the value of dispersion for a nonrotated rocket.

### 7-7.2.1 Constant Spin Rate

Fig. 7-9 indicates that, with constant spin, thrust malalignment has its greatest effect during the first wavelength of yaw, but is almost negligible during the remainder of the flight. This observation leads to be use of the number of revolutions made by the rocket during this initial period as one of the most important coin parameters.  $n_{\sigma}$ is the number of revolutions the rocket makes during the first wavelength. Fig. 7-16 shows the dependence of the dispersion reduction factor  $\beta$ on  $n_{\sigma}$ .

Various techniques can be used to achieve spin. Any method used must be capable of spinning the rocket without imparti g unwanted motion to the rocket. The importance of spin during the early portion of flight eliminates aerodynamic fins as a means of obtaining it since fins are least effective during this time. The most common method of providing spin is through auxiliary rockets fired in a circumferential direction.

The importance of early spin has led to the development of systems where the spin is accomplished while the rocket is still on the launcher. These systems involve many mechanical problems because of the difficulties involved in clearing the rocket fins and in releasing the launcher constraints without introducing translational or angular motion to the rocket.



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Fig. 7-16 shows that the angular dispersion decreases as the number of revolutions in the first wavelength increases. On the other hand, the dispersion due to dynamic unbalance increases with spin. These two effects result in an optimum spin rate, beyond which the dispersion reduction associated with thrust malalignment is lost to the dynamic unbalance effect. The spin rates used for the constant-spin results are the optimum values for a dynamic axis malalignment  $\epsilon$  of 0.5 mil.

Figs. 7-17(A), (B), (C)—for the case of constant spin—present the effects of rocket acceleration G, nondimensional launcher length P, and wavelength of yaw  $\sigma$ , on the dispersion reduction factor  $\beta$ . The wavelength of yaw can be seen to have the greatest influence on the dispersion reduction.

In practice, constant spin is not achieved. The programs that are called constant spin are actually composed of a period of high angular acceleration when the spin rockets are fired, followed by a slow deceleration caused by aerodyramic forces on the fins.






Figure 7-17(C). Constant Spin

#### 7-7.2.2 Constant Spin Acceleration

The dispersion reduction technique which is probably the easiest to implement is the constant spin acceleration. This can be achieved by canting the nozzles of the rocket motors (if more than one metor is used) or by placing fins in the rocket exhaust. Unfortunately, due to the slow initial spin, the technique is not as effective as the constant spin.

Figs. 7-18 (A), (B), (C) present the effects of the rocket variables on the dispersion reduction factor for constant spin acceleration. The most significant variable is the wavelength of yaw. The wavelength should be long to minimize the dispersion.

#### 7-7.2.3 Slowly Uniformly Decreasing Spin (SUDS)

The preceding spin programs always result in some finite dispersion. According to the mathematical theory of rocket flight (see Reference 6), it is possible to devise spin programs which result in zero angular dispersion. One such program is that of a Slowly Uniformly Decreasing Spin (SUDS); another is the Spin-Buck program.

The SUDS program begins with a constant spin which is followed by a constant deceleration. The initial spin rate and the value of the deceleration are functions of the rocket parameters. The angular error is very sensitive to changes in the spin rate or the deceleration. For this reason it is not possible to achieve zero dispersion in practice. Also, the limitations of the rocket theory make the zero dispersion result invalid. Figs. 7-19 (A), (B), (C) present the dispersion reduction for SUDS when the assumptions of the rocket theory are removed.

## 7-7.2.4 Spin-Buck

The Spin-Buck program is an attempt to eliminate the angular dispersion caused by thrust malalignment by reversing the spin direction of the rocket. By this reversal, the error accumulated prior to the reversal should be cancelled by the



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subsequent error The motivation behind this concept can be better understood if we consider the case of a nonrotating rocket with a thrust malalignment. We know from Fig. 7-1 that the dispersion builds up rapidly during the first wavelength. If at some instant during this build-up the rocket were rotated 180 degrees, the thrust malalignment would cause the dispersion to go to the negative direction. With the proper choice of the rotation point, the resultant dispersion will be zero.

Since most of the angular dispersion occurs in a very small portion of the flight, it might be expected that the point at which the rotation occurs is very near the launch point. Fig. 7-20 shows how the distance for the instantaneous rotation veries with rocket acceleration and wavelength of yaw.



Figure 7-20. Effect of Wavelength of Yaw on Buck Distance for Zero Angular Dispersion

From a practical standpoint, one shortcoming of this concept is the high sensitivity of the dispersion reduction factor to errors in the rotation distance. Fig. 7-21 indicates that, for a rocket acceleration of 40 g's, an error in rotation or buck distance of 7 percent produces a 40-percent change in the dispersion reduction factor.

The Spin-Buck program is accomplished by firing two banks of spin rockets, one following the other and in opposing directions. The net result is similar to the idealized case discussed above. A small residual spin is allowed, to reduce the effect of any error related to maccuracies in the system.

Field tests of the Spin-Buck program indicate that a dispersion reduction factor of 0.1 is possible

### 7-7.2.5 Prespin Automatic Dynamic Aligament (PADA)

The PADA concept for dispersion reduction differs from those discussed above in that it is not simply a method of spinning the rocket to reduce the effect of thrust malalignment, but incorporates a novel launcher design to reduce errors due to mallaunch, thrust malalignment, and dynamic unbalance. Par. 7-3.2.2 pointed out that control of these errors allows the aerodynamic stability requirement to be reduced. This control also results in a decrease in the rocket's wind sensitivity.

Development of the PADA launcher evolved from the desire to launch a rocket with an initial spin rate. The problem of bulky launchers, which developed in past attempts at launching spinning rockets, was eliminated by mounting the launching shoes on rings attached to the rocket by bearings. The dynamic unbalance effect-which normally limits the maximum spin rate (par. 7-7. 2.1)-has been overcome by a spring suspension system, designed so that natural frequency of transverse angular motion of the rocket on the launcher is considerably less than the rocket spin frequency. The result is that the recket dynamic axis aligns itself with the spin axis. Theoretically (Reference 8), PADA launchers can be constructed that will reduce the effect of dynamic unbalance by more than 90 percent, and possibly even by as much as 99 percent.

## 7-7.2.6 Variable Acceleration

The final dispersion reduction technique is unusual in that it does not utilize spin of any kind. Instead, the dispersion reduction is accomplished by changing the acceleration history of the rocket. This can be done with a throttleable rocket motor or with a combination of rocket motors. The example we shall consider here is a rocket with two levels of acceleration. The thrust level is assumed to vary instantaneously at the same point in the flight (Reference 9).





Figure 7-21. Effect of Buck Distance on Dispersion Reduction

How the rocket translational acceleration affects the angular dispersion is not immediately obvious. Reference 9 indicates that the dispersion due to various error sources, such as mallaunch and thrust malalignment, is affected differently by the change of acceleration. However, the description below, taken from Reference 9, describes the phenomenon.

The dispersion y is found by integrating  $\dot{y}$  with flight time. It can be shown that  $\dot{y}$  is an oscillating function whose magnitude varies as  $1/V^2$ . Therefore, the first half-cycle (when  $\dot{y}$  has one sign) has greater amplitude than the second halfcycle (when  $\dot{y}$  has the opposite sign). The result obtained when  $\dot{y}$  is integrated over the entire cycle is that the first half-cycle dominates the second. If the acceleration is decreased at some time before  $\ldots$  second cycle begins, the contribution of the second half-cycle can be increased and made to offset the first half.

The variable acceleration technique is presented here to show that there is a possibility for dispersion reduction without spin. However, the technique requires more research before its usefulness can be evaluated.

## 7-8 BALLISTIC PHASE ERRORS

## 7-8.1 FORCES ACTING ON THE PROJECTILE

The only forces acting during the ballistic phase are aerodynamic and gravitational. The aerodynamic forces can be separated into drag and those forces acting normal to the flight path.

The aerodynamic forces acting normal to the flight path are due to lift and cross spin. The aerodynamic lift force is well known; the cross spin force is a result of the air flow being disturbed by rotation of the projectile about a lateral axis. The rotation causes a variation of the angle of attack along the body, resulting in an unsymmetric force.

#### 7-8.2 SOURCES OF ERROR

From the definition of dispersion, any force which causes the projectile to deviate from the idealized trajectory will be included as a source of error. Since only drag is considered in calculating the idealized trajectory, normal forces as well as changes in drag will introduce dispersion





Figure 7-22. Action of Winds on a Free Rocket

In addition to dispersion of the flight path, errors associated with fuzing the warhead must also be considered.

#### 7-8.2.1 Errors Due to Winds

The action of winds on a free rocket in its ballistic phase (Figure 7-22) generates three perturbing forces that affect the missile trajectory:

a. Change in Drag Magnitude. Bellistic wind will cause a change in air speed and, consequently, in dynamic pressure and drag force magnitude. This effect will usually be negligible.

b. Lift Forces. A change in wind velocity normal to the ballistic flight path will cause an angle of attack, and consequently, the development of a lift force. Since this is a transient effect, it is usually very small.

c. Change in Drag Direction. In its steady state response to a normal wind, a stable missile will be oriented at some angle with respect to its zero-wind flight path Since the total drag force vector still lies along the missile axis, it will cause an acceleration in the downwind direction until the missile dispersion velocity reaches the wind velocity. This is the predominant force causing ballistic wind error. Since high-altitude winds can reach high velocity—e.g., the jet stream—an attempt is frequently mede to compensate for the winds in the aiming process. This can be accomplished by use of data from firing tables, weather balloons, etc.

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### 7-8.2.2 Change in Drag

A projectile will seldom have an actual drag history exactly the same as the one used in the calculation of the idealized trajectory. Inaccuracies inherent in the methods of determining drag—as well as inaccuracies resulting from manufacturing errors and damage in handling—are typical causes of these drag deviations. Therefore, the effect of changes in the ballistic coefficient C must be considered as a source of dispersion.

#### 7-8.2.3 Nonstandard Conditions

A departure from nonstandard atmospheric conditions will also be considered. This effect is equivalent to a change in drag.

#### 7-8.2.4 Malalignment of Fins

Projectiles with fins that have become malaligned or bent due to careless handling or manufacturing error will cause aerodynamic forces resulting in dispersion. However, fin malalignment will also cause a slow spin which tends to reduce the effect of the error (Reference 1, p. 60).

#### 7-8.2.5 Static Unbalance

Manufacturing tolerances usually result in the projectile center of gravity being located off the longitudinal axis. The aerodynamic forces will then produce a moment resulting in an angle of attack. The dispersion due to static unbalance can be reduced by a slow spin.

#### 7-8.2.6 Dynamic Unbalance

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Manufacturing tolerances plus the unavoidable unsymmetric placement of small components or uneven propellant-burning will result in the inertial spin axis being displaced from the projectile centerline. Therefore, if spin is used to reduce other sources of dispersion, error will be introduced due to dynamic unbalance. Fortunately this effect can usually be kept small by careful design and manufacturing control so that the conflicting requirements can be satisfied without introducing a significant amount of dispersion.

## 7-8.2.7 Curvature of the Trajectory

The trajectory of the projectile during the ballistic phase will approximate a parabolic arc An aerodynamically stable vehicle will attempt to keep its axis aligned with the flight path. However, the inherent resistance of the body to rotation (aerodynamic damping) will cause the projectile axis to lag behind the changing flight path direction. This phenomenon is called the yaw of repose (Reference 1, p. 58), which causes a small dispersion unaffected by spin.

#### 7-8.2.8 Fuzing Errors

a. Impact Fuzing: With impact fuzing (a special case of altitude fuzing), the errors are those associated with the dispersion of the trajectory. There are no errors introduced by the fuzing technique itself.

b. Time Fuzing: With tune fuzing, variation in fuze action time introduces errors in addition to those associated with the dispersion of the trajectory. The result will be additional range and altitude dispersions of the warhead at the time of detonation.

### 7-8.3 CALCULATION OF DISPERSION

The preceding paragraphs have presented methods that can be used to determine the condition of the rocket at motor burnout. The dispersion at burnout associated with the launch and propulsion phases has been given. With the burrout conditions as inputs, the graphs in this paragraph determine the dispersion of the rocket at warhead event. In addition to the launch and propulsion errors, the errors associated with the ballistic phase are introduced. The final results are the dispersions of the rocket at warhead event, caused by the error sources throughout the flight. For the purpose of this handbook only those ballistic phase errors which have the greatest influence on the accuracy have been included. These errors have been taken to be (1) change in atmospheric density, (2) change in the ballistic coefficient, and (3) ballistic wind.

The graphs in this paragraph give the changes in range and deflection for unit changes in the several rocket variables. The plotted data are -----

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# TABLE 7-1. ERROR BUDGET FOR INDIRECT FIRE ROCKET WITH IMPACT FUZE

	Source	One Sigma Magnitude	$\Delta Y$ , meters	.∖R, meters	ΔY, mils	$\Delta l$ , mils
I.	Launch Errors					
	A. Malaim	0.5 mil	14.2	0	0.5	0
	B. Mallaunch					
	a. Translation	1.0 ft sec	-71.0	0	-2.50	0
	b. Rotation	$q = 10.0  \mathrm{ft}  \mathrm{sec}$	55.6	0	1.95	0
	c. Dynamic Unbalance	1.0 mil	55.6	0	1.95	Û
II.	Propulsive Errors					
	A. Wind	3.9 ft/sec	222.0	0	7.80	0
	B. Thrust Malalignment	1.0 mil	182.0	0	6.40	0
	C. Impulse	2.0%	0	76.0	0	2.67
III.	Ballistic Errors					
	A. Density	1.0%	0	222.0	0	7.80
	B. Ballistic Wind	8.1 ft, sec	117.0	148.0	4.11	5.20
	C. Ballistic Coefficient	1.0%	0	222.0	0	7.80

## LAUNCH QUADRANT ELEVATION 45 DEGREES

the results of numerous digital computer calculations. The graphs are used by determining the nominal quadrant elevation and range, which in turn are used to establish the unit effects. The example calculations in pars. 7-8.3.1 through 7-8.3.4 illustrate how the dispersion at warhead event is calculated and tabulated into an error budget, used in the further calculation of probable error components (see par. 7-19). impulse  $I_{sp} = 250$  sec; mass ratio  $r_B = 1.4$ ; G = 48.0 g; quadrant elevation QE = 45 deg; nondimensional launcher length P = 0.0. Typical one-sigma values assumed for the errors are as listed in Table 7-1.

Find: The dispersions at warhead event. Solution: See calculations which follow.

7-8.3.1 Launch Errors

7-8.3.1.1 Malaim

Given: Indirect fire rocket with impact fuze and constant spin; ballistic coefficient C =

 $\frac{W_{BO}}{id^2}$  = 4.0; range at quadrant eleva-

tion for maximum range = 28.5 km; wavelength of yaw  $\sigma = 510$  ft; specific Malaim errors will result in the impact point being deflected off to the side of the desired im-

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Figure 7-23. Initial Velocity Versus Maximum Range

pact. If the malaim error  $\Delta \psi$  is 0.5 mil, the error will be

$$\Delta Y = (\Delta \psi) R$$
$$\Delta Y = 0.5 \ \text{mil} \ \left(\frac{r \ ad}{1000 \ \text{mils}}\right) 28,500 \ \text{m}$$
$$\Delta Y = 14,23 \ \text{m}$$

With a ballistic coefficient C of 4.0, a maximum range R of 28,500 m and with the use of Fig. 7-23, the initial velocity is determined to be 3000 fps. By use of Fig. 7-24(B) in conjunction with the above information, the ratio of a percent change in range per change in departure angle is determined. In this example, the range we are interested in is the maximum value. Thus, the ratio of range desired to maximum range is unity. As seen in Fig. 7-24(B), the partial derivative  $-\frac{\partial R}{\partial \theta}$ is zero; thus, an error in malaim results in a negligible error in range for maximum range.

### 7-8.3.1.2 Mallaunch

A translational error of 1.0 fps will result in an angular dispersion,  $y_{7S}$ , of -2.5 mils as obtained from Fig. 7-13(A). If the same formula is used as in par. 7-8.3.1.1 above, the error in deflection becomes

$$\Delta Y = \left(\frac{-2.5}{1000}\right) 28,500$$
$$\Delta Y = -71, m$$

The shange in range as the result of a mallaunch is zero for the same reason as presented above. A rotation error q of 10 mil/sec will result in an angular dispersion, as found in Fig. 7-12(A), of

$$\gamma_{TS} = 19.5 \text{ mils} \left(\frac{10 \text{ mil/sec}}{100 \text{ mil/sec}}\right)$$
$$\gamma_{TS} = 1.95 \text{ mils}$$

This assumes that the angular dispersion, as a function of G and  $\sigma$ , is affected linearly by rotation rate q.

$$\Delta Y = \left(\frac{1.95}{1000}\right) 28,500$$
$$\Delta Y = 55.6 m$$
$$\Delta R = 0$$

For a dynamic unbalance error of 1.0 mil with a spin rate of 10 rad/sec

$$q = P\epsilon = 10(1) = 10 \text{ mil/sec}$$

From Fig. 7-12

$$Y_{TS} = 1.95 \text{ mils}$$
  
 $\Delta Y = \left(\frac{1.95}{1000}\right) 28,500$   
 $\Delta Y = 55.6 \text{ m}$   
 $\Delta H = 0$ 

## 7-8.3.2 Propulsion Errors

### 7-8.3.2.1 Wind

With a wind error of 3.9 fps, and the use of Fig. 7-14(A), the angular dispersion is

$$y_{TS} = 20 \quad \left(\frac{3.9}{10}\right) = 7.8 \text{ mil}$$
$$\Delta Y = \left(\frac{7.8}{1000}\right) 28,500$$
$$\Delta Y = 222 \text{ m}$$
$$\Delta R = 0$$

### 7-9.3.2.2 Thrust Maialignment

The spinning of the vehicle is an attempt to minimize the thrust malalignment error. Fig. 7-17(A) gives a dispersion reduction factor  $\beta$ :

$$\beta = 0.16 \left(\frac{1}{0.5}\right) = 0.32$$

 $Y_{TS} = 20 \text{ mils}$   $\Delta Y = \beta_{YTS} R$   $\Delta Y = 0.32 \left(\frac{20}{1000}\right) 28,500$  $\Delta Y = 182 \text{ m}$ 

Fig. 7-15(A) gives the angular dispersion

$$\Delta R = 0$$

## 7-8.3.2.3 Impulse Variation

From Fig. 4-8, if we generate a plot of  $I_{sp}$  versus burnout velocity for a constant boostermass-ratio and calculate

$$\frac{\Delta V_B}{\Delta I_{sp}} = 9.1$$

For an impulse error of 2 percent

$$\Delta V_{B} = 9.1 \ \Delta I_{sp}$$
  

$$\Delta I_{sp} = 0.02 \ I_{sp}$$
  

$$\Delta V_{B} = 9.1 \ (0.02 \ I_{sp})$$
  

$$= 0.182 \ (250) \ ft/sec$$
  

$$\Delta V_{p} = 45.5 \ ft/sec$$

From Fig. 7-25(B)

$$\frac{\partial R}{\partial V} = 1.67$$

$$\Delta R = (1.57)(45.5)$$

$$\Delta R = 76 m$$

$$\Delta Y = 0$$

## 7-8.3.3 Bailistic Errors

## 7-8.3.3.1 Dansity

The density error is 1.0 percent. From Fig. 7-2i(B)

$$\frac{\partial R}{\partial p} = 0.78$$

$$\%\Delta R = 1\%(0.78) = 0.0078$$
  
 $\Delta R = 0.0078 (28,500)$   
 $\Delta R = 222 m$   
 $\Delta Y = 0$ 

#### 7-8.3.3.2 Ballistic Wind

The ballistic wind error is 3.1 fps. From Fig. 7-27(B)

$$\frac{\partial R}{\partial V_{\mu}} = 0.064 \frac{\%}{fps}$$
  
%\Delta R = 0.064 (9.1)  
= 0.519% \approx 0.0052  
\Delta R = 0.0052 (28,500)  
\Delta R = 148 m

From Fig. 7-28(B)

$$\frac{\partial Y}{\partial V_{w}} = 0.05 \frac{\%}{f \, ps}$$
  
% $\Delta Y = 0.05 (8.1)$   
= 0.405% \approx 0.0041  
 $\Delta Y = 0.0041 (28,500)$   
 $\Delta Y = 117 \, m$ 

#### 7-8.3.3.3 Ballistic Coefficient

The ballistic coefficient error is 1.0 percent. This error is estimated as if it were an error in density. Thus, from Fig.  $\overline{7}$ - $\overline{26}(B)$ 

$$\frac{\partial R}{\partial C} = 0.78$$
  

$$\% \Delta R = 1\% (0.78) = 0.78\% = 0.0078$$
  

$$\Delta R = 0.0078 (23,500)$$
  

$$\Delta R = 222 \text{ m}$$
  

$$\Delta Y = 0$$

### 7-8.3.4 Tabulation of Results

The results of the above calculations are tabulated in Table 7-1.

### 7-8.3.5 Additional Reference Graphs

The sample calculations above have all dealt with a rocket armed with an impact fuze. Figs. 7-29 and 7-30 give additional reference data for this type of rocket, and Figs. 7-31 through 7-41 give similar reference data for a rocket with a time fuze.

## 7-9 STATISTICAL METHODS

Up to this point, this chapter has been concerned with identifying the sources of error in a rocket system and determining the effect of each error source on the dispersion of the rocket at warhead event. We shall now consider how to use this information to determine the probability of hitting a given target with a rocket system subject to known error sources. More precisely, the problem is find the radius of the circle within which one-half of all the rockets will impact.

Since the error sources are statistical in nature, we can only speak in terms of expected values and probabilities, and it will be necessary to separate the error sources according to their statistical nature. Let us first summarize the basic concepts of statistical analysis used to determine the accuracy of rocket systems. We shall then apply these concepts to determine the curcular probable error *CPE* for the example problem of par. 7-8.3. The following definitions are useful:

a. Fixed Bias Errors. Let us assume that, because of a manufacturing error, the sight for a particular rocket launcher is malaligned with the launcher rail. This will result in a center of impact that is not in line with the intended direction as established by the sight. This type of error is called a fixed bias error. We shall not consider fixed bias errors further because we may assume that they can always be discovered, and compensated for, by systematic tests.

b. Random Bias Errors. Errors which exist for a specific set of shots fixed at the same ele-

vation and deflection setting—such as the misreading of an unchanging wind or the missetting of the quadrant elevation angle—are called random bias errors. Methods will be described for computation of these errors; however, in the description of dispersion, the errors will not be considered since, when prior knowledge of these disturbances exists, correction can be made through such methods as prelaunch computation and aiming.

c. Random Errors. The computation of these errors is the main topic of pars. 7-4 through 7-8. These errors are due to thrust malalignment, weight variations, malaim, incomplete compensation for random bias errors, and many other causes.

The remainder of this chapter is concerned with determining the *CPE* from a knowledge of the random errors.

## 7-9.1 MEASURES OF DISPERSION FOR ONE ERROR SOURCE

In reducing sample dispersion data to determine the accuracy of a missile system, we must show how the values are distributed about their center of impact. This discussion will include procedures used to compute these measures of dispersion in one- and two-dimensional distributions.

The most common measures of dispersion for one-dimensional distribution are the variance, standard deviation, and probable error.

### 7-9.1.1 Variance

The variance  $\sigma^2$  of a population (the whole class about which conclusions are to be made) is defined as the average of the squares of the distances from the universe mean. If a sample of N values is drawn from a population, with mean  $\mu$ , the variance of the population is estimated by the equation

$$V = \sum_{i=1}^{N} \frac{(x_i - \mu)^2}{N}$$
 (7-19)

where  $x_1$  are the sample values.

Generally,  $\mu$  is not known, and an estimated mean  $\bar{x}$  of the sample values must be used. If  $\bar{x}$  is substituted for  $\mu$ , V becomes a biased estimator of the variance. (Reference 17, pp. 31-32) This bias can be corrected by using (N-1) instead of N. The unbiased estimator  $s^2$  of the population variance then becomes

$$\sum_{i=1}^{N} (x_{i} - \overline{x})^{2}$$

$$\sum_{i=1}^{N-1} (7-20)$$

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## 7-9.1.2 Standard Deviation

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The standard deviation  $\sigma$  is the most important measure of dispersion. The standard deviation is the deviation from the mean value  $\mu$  of a set of random values such that approximately 68 percent of the values are between  $\mu$  minus  $\sigma$  and  $\mu$  plus  $\sigma$ . It is a more understandable measure of dispersion than the variance, because the standard deviation is the square root of the variance and, therefore, has the same dimensions as the variable. The standard deviation is estimated from a sample of size N by the equation

$$s = \left[\frac{1}{N-1} \sum_{i=1}^{N} (x_i - \overline{x})^2\right]^{1/2}$$
(7-21)

where s is the estimator of  $\sigma$ . Computation can be simplified by the algebraically equivalent form

$$s = \frac{1}{N(N-1)} \left[ N \sum_{i=1}^{N} x_i^2 - \left( \sum_{i=1}^{N} x_i \right)^2 \right]^{1/2}$$
(7-22)

### 7-9.1.3 Probable Error

The probable error PE is the deviation from the mean  $\mu$  such that 50 percent of the observations are expected to lie between  $\mu$  minus the probable error and  $\mu$  plus the probable error It can be found from a percentage of the normal distribution table (Reference 29, p. 230), that the

probable error for a normal distribution is equal to 0.674 times the standard deviation.

$$PE = 0.674\sigma$$
 (7-23)

To convert probable error to the standard deviation, multiply by 1.48:

$$\sigma = 1.48 PE$$
 (7-24)

The standard deviation is also a very important measure of dispersion for two-dimensional distributions. Considering a sample size of less than 30 items, for a two-dimensional distribution (x and y), the standard deviation can be estimated by using the formula

$$s = \left[\sum_{i=1}^{N} \frac{(x_i - \bar{x})^2 + (y_i - \bar{y})^2}{2(N-1)}\right]^{1/2}$$
(7-25)

It is often desirable to establish an interval about the sample standard deviation or mean in which we can state, with a specified confidence, that the true standard deviation or true mean lies. This is the confidence interval. The confidence interval for the standard deviation can be computed from the formula

$$\left[\frac{(N-1)}{x_2^2}\right]^{1/2} \le \sigma \le \left[\frac{(N-1)}{x_1^2}\right]^{1/2}$$
(7-26)

where

$$X_{2}^{2} = X_{1}^{2} \cdot \frac{\alpha}{2}$$

and

$$X_1^2 = \frac{\chi_{\alpha}^2}{2}$$
, with N-1 .1. grees of freedom

and s is the computed standard deviation. The value of  $\alpha$  is found by subtracting the desired confidence interval from 1:

$$\alpha = 1 - (\text{confidence interval})$$
 (7-27)

The values for  $X_{\frac{\alpha}{2}}^2$  and  $X_{1-\frac{\alpha}{2}}^2$  are obtained from

a chi-squared distribution table.

The confidence interval about the mean is computed by the formula

$$\left[\overline{x} - \frac{t_1 s}{N}\right] \le \mu \le \left[\overline{x} + \frac{t_2 s}{N}\right]$$

where

 $t_1$  = Student's t value for (N-1) degrees of freedom at the  $\frac{\alpha}{2}$  point and  $t_2$  is the same for the  $\left(1-\frac{\alpha}{2}\right)$ -point.

The most widely used measure of dispersion for determining missile accuracy for a two-dimensional distribution is the Circular Probable Error CPE The CPE is defined as the radius of a circle within which one-half of the values are expected to fall. The center of the circle is the mean of the values. The nost popular formula used to compute the CPE is

$$CPE = 1.1774 \sigma$$
 (7-28)

which can be estimated by

$$CPE = K \left[ \sum \frac{(x_{1} - \overline{x})^{2} + (y_{1} - \overline{y})^{2}}{2(N-1)} \right]^{1/2}$$
(7-29)

where

$$K = 1.1774$$

This formula is true only when the horizontal positions x and vertical positions y are independent. normally distributed, and have a common standard deviation  $\sigma$ , where  $\sigma_y = \sigma_x = \sigma$ .

For distributions where there is no common standard deviation, the distribution becomes elliptical instead of circular. An approximation of the *CPE* for an elliptical distribution can be determined by the equation

$$CPE = 1.1774 \left(\frac{\sigma_y + \sigma_x}{2}\right)$$
 (7-30)

where  $\sigma_x$  and  $\sigma_y$  are the standard deviations in the x and y positions. This approximation is correct to within 2.5 percent if the ratios of the standard deviations are less than 7:1. (Reference 22.)

If a more accurate estimation of the CPE for an elliptical distribution  $(\sigma_x + \sigma_x)$  is desired,

Figs. 7-42 and 7-43 can be used. Their use will be described in par. 7-9.3.

## 7-9.2 MEASURES OF DISPERSION FOR SEVERAL ERROR SOURCES

The measures of dispersion previously discussed are used when the errors are from one source. For the total error resulting from several independent error sources, the root-sumsquare (vector sum) method is used. The total error is determined by squaring the errors from each source and then summing them. The square root of this summation is the total error. (Reference 15, p. 201.) In equation form

$$\sigma_{\text{tot}} = \sqrt{\sigma_1^2 + \sigma_2^2 + \ldots + \sigma_N^2} .$$
(7-31)

For a two-dimensional distribution, the total error in each dimension must be found and the average of the two taken to obtain the total error for the system

$$(\sigma_{y})_{tot} = \sqrt{\sigma_{x1}^{2} + \sigma_{x2}^{2} + \ldots + \sigma_{xN}^{2}}$$

$$(7-32)$$

$$(\sigma_{y})_{tot} = \sqrt{\sigma_{y1}^{2} + \sigma_{y2}^{2} + \ldots + \sigma_{yN}^{2}}$$

$$(7-33)$$

$$(7-33)$$

$$(7-34)$$

The CPE is then found by the equation

$$CPE = 1.1774\sigma_{sys}$$
 (7-35)

This method is used extensively in the research and development phase of a missile system. The *CPE* required in order for the missile system to meet its overall accuracy requirement is found. The average (one-sigma) errors of each of the independent error sources are found by testing each of these components. By simulation, the effects of these one-sigma values on the range and deflection of the missile at the impact point are found. These errors in range and deflection are then combined by the root-sum-square method to get the total error for the system. The *CPE* is computed and compared with the required *CPE*. If this computed *CPE* does not meet the **7-34**  requirements, some or all of the components that contribute to the total error must be improved. In this manner, the best design of the missile components can be determined.

Figs. 7-42 and 1-43 can be used to estimate the CPE of an elliptical distribution.

### 7-9.3 USE OF FIGS. 7-42 AND 7-43

Figs. 7-42 and 7-43 provide a more accurate estimate of the circular proable error for an elliptical distribution. The value of K in the equation

$$CPE = (K) \times (Standard Deviation)$$
  
(7-36)

can be more accurately determined. The value 1 1774 is the standard value used for K, but this value is correct only when the horizontal and vertical standard deviations are equal:

 $\sigma_x = \sigma_y$ .

The major difference between Figs. 7-42 and 7-43 is that Fig 7-42 uses the average of the standard deviation in the horizontal and vertical position for the computation of the *CPE* while Fig. 7-43 uses the larger of 'the two standard deviations, i.e.:

$$CPE = K\left(\frac{\sigma_x + \sigma_y}{2}\right) \text{ (Fig. 7-42)}$$

$$CPE = K\sigma_{xax} \text{ (Fig. 7-43)}$$

$$(7-38)$$

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For Fig. 7-42, the smaller of the two standard deviations is divided by the larger. The ratio is then read on the horizontal axis and extended to the curve. The vertical value of this point on the curve is the value of K in Eq. 7-37.

For Fig. 7-43, the minimum value of the two standard deviations is divided by the maximum and the ratio is the vertical value on the curve. This point on the curve is the value of k in Eq. 7-38.

### 7-10 COMPUTATION OF ACCURACY

Using the results of the example dispersion calculation which are presented in Table 7-1, one can determine the probable errors in range and

deflection as well as the CPE. The example calculation considers only one quadrant elevation. The change in the accuracy of a rocket system with range is very important since a variation in target range is to be expected.

## 7-10.1 RANGE PROBABLE ERROR (RPE)

The values given in Table 7-1 are one-sigma dispersions. Therefore, using the formula from par. 7-9.2

 $\sigma_{RANCE} = \sigma_{R}_{TOTAL}$ 

$$= \sqrt{(2.67)^2 + (7.80)^2 + (5.5)^2 + (7.80)^2}$$
  
= 12.5 mils

From par. 7-9.1.3, range probable error

 $RPE = 0.674 (\sigma_{RANCE})$ 

= 0.674 (12.5) = 8.42 mils

Fig. 7-44 indicates the variation of *RPE* with range for a typical free rocket with an import fuze.

### 7-10.2 DEFLECTION PROBABLE ERROR (DPE)

Again from Table 7-1

 $\sigma_{DEFLECTION} = \sigma_{D_{TOTAL}}$ 

$$= \left[ (0.5)^2 + (2.50)^2 + (1.95)^2 + (1.95)^2 + (1.95)^2 + (7.80)^2 + (6.40)^2 + (4.11)^2 \right]^{1/2}$$

AMCP 705-280

= 11.5 mils

Deflection probable error

Fig. 7-45 indicates the variation of DPE with range for a typical free rocket with impact fuze.

#### 7-10.3 CIRCULAR PROBABLE ERROR (CPE)

From the results presented in par. 7-9.2

$$\sigma_{sys} = \frac{\sigma_{RTOTAL} + \sigma_{PTOTAL}}{2}$$
$$= \frac{12.5 + 11.5}{2}$$
$$= 12.0$$
$$CPE = 1.1774 \sigma_{sys}$$
$$= 1.1774(12.0)$$
$$= 14.1 \text{ mils}$$

Fig. 7-46 indicates the variation of *CPE* with range for a typical free rocket with impact fuze.

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Figure 7-38(A). Unit Effect, Alitude/Density Versus  $R/R_{max}$  – Time Fuze

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Figure 7-38(C). Unit Effect, Altitude/Density Versus R/R<sub>max</sub> - Time Fuze







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# CHAPTER 8 AERODYNAMICS

# LIST OF STMBOLS

Symbol	Meaning	Symbol
a *	Sonic velocity, ft sec	P
u	Fin cut cut factor (see Fig. 8-23)	q
α,	Fin geometry-flow parameter (see Fig.	r
·	8-21)	R, RN
A	Area, ft <sup>z</sup> (general reference area)	rte
$A_T$	Jet throat area, ft <sup>2</sup>	
AR	Fin aspect ratio (fin span squared/fin	
	area)	S
Ь	Fin span, ft	Seff
ç	Fin chord, ft	ΤÊ
$\overline{c}$	Fin mean chord (see Fig. 8-23), ft	t
cl	Cord length	V
$C_{D}$	Drag coefficient	X; x
$\mathcal{C}_{f}$	Total skin friction coefficient	Y
$C_{F}$	Thrust coefficient	α
ĊM	Pitching moment coefficient	в
CHa	Pitching moment coefficient gradient	
$C_N$	Normal force coefficient	Ŷ
$C_{N_{\alpha}}$	Normal force coefficient gradient, per rad	0
-	or per deg	
Cp	Pressure coefficient	Δ.
CĠ	Center of gravity location (axially from	
	no <b>se)</b>	Ξ
d	Diameter ft; lifferential	Ч
D	Drag force, lb	A
f	Fineness ratio $(l/d)$	2
h	Fin base thickness (see Fig. 8-46)	л Л
Ι	Correlation parameter for fin-fin interfer-	7
	enc	"
$k_2 - k_1$	Mass factor (see Eq. 8-1)	P C
Кј(б)	Interference factor	~
$K_{t(f)}$	Interference factor	Subscript
£,l	Length measure, ft	
led	Leading edge diameter, ft	a,ab
in	Natural logarithm	Ь
m	Fin geometry-flow parameter (see Fig.	В
	8-21); factor for 1 ig. 8-35	bo
М	Mach number; pitching moment, ft-lb	bt
n	Number of fins; exponent for power law	C
•.	nose	c/2
N	Normal force, lb	cyl
Р	Static pressure lb/ft <sup>2</sup>	сp

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rmbol	Meaning
P	Motor chamber pressure, 16/ft <sup>2</sup>
q	Dynamic pressure, lb/ft²
r	Radius, ft
, RN	Reynolds number
rte	Ring trailing edge (the location of ring
	trailing edge with respect to base of body;
	values aft of body base are positive.)
S	Area, ft <sup>‡</sup> (particular reference area)
Seff	Effective area (see par. 8-2.4.3), ft <sup>2</sup>
ΤÊ	Trailing edge
t	Fin thickness, ít
V	Rocket velocity, ft sec
(; x	Axial distance, ft
Y	Lateral distance, ft
α	Angle of attack, rad or deg
β	$\sqrt{M_{\infty}^2 - 1}$
y	Ratio of specific heats
δ	Boattail half angle, degrees; factor for fin
	correction (see Fig. 8-15)
Δ	Increment
•	Included angle of fin leading edge (see Fig.
	8-23), deg
$\overline{\eta}$	Spanwise location of fin mean chord (see
	Fig. 8-23)
θ	Cone or flare half angle, deg
λ	Fin taper ratio
Λ	Fin leading edge sweep angle, deg
π	3.1416
ρ	Atmospheric density, slug/ft <sup>3</sup>
ω	Fin angle (see Fig. 8-21), deg
bscrip	18:
. ab	Afterbody
<i>b</i>	Body
B	Base
bo	Rocket motor burnout conditions
b:	Boattail
с	Cylinder; cone
c/2	Fin mid-chord
cyl	Cylinder
сp	Center of pressure

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## LIST OF SYMBOLS (Cont)

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hscripis	1		Meaning
e	Exposed	value	

- Flare; fin; friction £
- ĵЬ Forebody
- Exposed fin fe
- Flare fl
- Rocket launch condition
- g IF Interference tree
- Jet (or nozzle exit plane) conditions J
- le Leading edge
- Nose n
- Free stream or stagnation conditions 0,∞
  - Planform р

Subscrip	taz	Meaning
r	Root chord	
re	Exposed root	chord

- **Reference** condition ref
- Ring tail r t
- Т Total

Tip chord ŧ

Trailing edge te

- Theoretical prediction theory
  - Wave drag; "wetted" condition w
  - 2D Two dimensional consideration
  - T Perpendicolar measure

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## 8-1 GENERAL DESIGN CONSIDERATIONS

This chapter will discuss the aerodynamic aspects of free rocket design and will indicate means of predicting the significant aerodynamic coefficients. Simply stated, the usual aerodynamic design goal is to select an external configuration which provides stable flight with minimum drag through the desired altitude-velocity range.

For a rocket to possess flight stability, a restoring moment must be produced when its longitudinal axis is rotated from the flight direction, i.e., when an angle of attack exists. This flight stability is achieved in the case of aerodynamically stabilized rockets by selecting the external configuration such that the center of pressure of aerodynamic forces normal to the longitudinal axis is located farther aft of the rocket's nose tip than the center of gravity. Since the aerodynamic forces are proportional to angleof-attack (the angle between the flight direction or velocity vector and the longitudinal axis of the rocket), any deviation will produce a moment to restore the axis to its aligned condition. When the center of pressure is aft of the center of gravity, the rocket is said to be statically stable.

The degree of aerodynamic stability, or the static margin requirement, varies with the desured accuracy of each rocket and its design approach. For example, a rocket designed for minimum dispersion during powered free flight requires a specific tailoring of the static margin over its Mach number regime, while a high-acceleration rocket which achieves most of its velocity prior to release from the launcher requires only that the stability margin remain with certain upper and lower bounds. The width of this stability band is governed primarily by the requirement to maintain a significant spread between the roll and pitch-yaw frequencies.

Although the static margin is of paramount interest to the accuracy of a free rocket during the powered, high-ac leration phase, the aerodynamic drag or axial force is a prime factor affecting the accuracy and performance during the sustain and ballistic flight phases. For an anguided rocket, the angle of attack is nominally zero; therefore, the axial and drag forces are equal. The general goal is to keep the axial force coefficient as low as possible, consistent with other design considerations such as body length, weight, and structural rigidity. Reduction of the axial force coefficient is more important generally for incirect-fire, artillery-type rockets where the sustain and ballistic flight times are much greater than that of the boost phase. Axial force reduction in this case can result in either a lighter and smaller rocket for a specified maximum range, or increased range for a fixed rocket size and weight. In addition, improved accuracy is achieved by reduced rensitivity to atmospheric variations during the ballistic flight because it is primarily through the aerodynamic axial force that non-gravitational accelerations are transmitted to the rocket.

The external configuration of a free rocket can vary significantly depending on the trade-off between aevodynamic requirements imposed by performance and accuracy considerations, and other system requirements. Some generalization can be made, however, based on past designs. Typically, the rocket's external configuration consists of a pointed body-of-revolution housing payload and propulsion unit. with a stabilizing device attached to the aft section. A circular crosssection is preferred because its symmetry about the longitudinal axis makes for simplicity, both in manufacturing and in determining aerodynamic coefficients and mass-inertia properties. To the rocket body, which normally is aerodynamically unstable, various normal-force-producing devices are attached at its aft end to provide the necessary restoring moment for stability. Thin-profile planar fins, spaced evenly around the circumference of the body, are used in many rocket designs as stabilizing devices. This type of fin usually will produce the maximum stabilizing moment with minimum weight and axial force penalties. When minimum overall diameter is a dominant design consideration, the ring-tail and conical ilare become of greater interest. A ring-tail will produce, at both subsonic and supersonic velocities, approximately twice the restoring moment of a cruciform planar fin with equal total span and chord. The conical flare is of interest for restricted-diameter rockets with maximum velocities above approximately 5000 ft/sec. On the basic of projected planform area, a conical flare will produce better than twice the normal force of cruciform fins at hypervelocity speeds. However, the axial force of a flare greatly exceeds that of fins providing equal restoring moment.

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It should be clear from the preceding discussion that a "best" aerodynamic configuration does not exist. The great multitude of parameters affecting the configuration selection usually results in its choice being based on past design experience and aesthetic values rather than an optimization study.

In order to estimate the aerodynamic stability characteristics for complete rocket configurations and to provide design guidance, it is necessary to know the aerodynamic coefficients of each major rocket component and interference between components. The paragraphs which follow will discuss first the stability parameters for various rocket forebody shapes, fins, ring-tails, conical flares, and boattails; and then will discuss how these component aerodynamic coefficients are combined to arrive at values for the complete configuration. Wherever possible, simple analytical or semi-empirical equations will be presented along with charts to make aerodynamic estimates. No effort will be made to provide the theoretical basis or experimental substantiation for the data presented since numerous textbooks and reports exist which discuss these topics in great detail. Finally, a detailed computational chart will summarize sources and methods of obtaining design data, and will provide a format and check list for design computation.

## 8-2 STABILITY CHARACTERISTICS **OF ROCKETS**

#### 8-2.1 BODIES OF REVOLUTION

## 8-2.1.1 Nese Cylinder

The forebody of a rocket normally consists of a pointed cone, an ogive, or a power series curve, followed by a cylindrical section. The slenderbody theory provides a simple means of expressing the stability characteristics of these bodies in terms of the geometric parameters only, as follows:

$$\left(\frac{dC_N}{dx}\right)_b = \frac{(k_2 - k_1)}{S_{rej}} \quad \left(\frac{dS}{dx}\right) \sin 2\alpha \tag{8-1}$$

which, when integrated from x = 0 to x = l, gives

$$\begin{pmatrix} C_{N_{\alpha}} \end{pmatrix}_{b} = 2(k_{2} - k_{1}) \frac{S_{B}}{S_{ref}}$$
 (8-2)

In the above expressions

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- $C_N$ = normal force coefficient
- C<sub>N</sub>a normal force coefficient gradient, per rad or per deg (see par. 8-2.4.1) = body
  - = angle of attack, the angle between the longitudinal axis of the rocket and the velocity vector, in rad or deg

 $k_2 - k_1 =$  apparent mass factor

- = body length, ft
- dS = incremental cross-sectional area,  $ft^z$
- dx= incremental axial distance, ft = body base area, ft<sup>2</sup>
- S,
- = reference area,  $ft^2$ S<sub>ref</sub>

The factor  $(k_2 - k_1)$  is the apparent mass factor as derived by Munk (Reference 1). The values for ellipsoids of revolution presented in Fig. 8-1 represent a reasonable approximation for any axisymmetrical body of comparable fineness ratio. The center of pressure may be assumed to act at the centroid of the nose projected area for  $M_{m} < 1$ .

The fundamental assumptions of the theory are that all second order partial derivatives of velocity can be neglected, and that velocity perturbations along the body axis are small compared to the transverse values. The solution inaplies that adding cylinder length to the nose ius no effect, and that there is no compressibility effect due to varying Mach number. However, experimental data and more refined theoretical solutions, too complex to discuss here, show these effects to be significant. The reader is referred to References 2, 3, and 4 for further details of





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these solutions. In the absence of more precise solutions, the slender body theory should be used in the subsonic-through-sonic Mach number rrage.

At supersonic Mach numbers, the normal-force coefficient gradient and center-of-pressure estimates should be obtained, respectively. from Figs. 8-2 and 3-3 for tangent-ogive-cylinder bodies, and from Figs. 8-4 and 8-5 for cone-cylinder bodies. These curves were extracted from Reference 5 and were constructed from empirical data covering a Mach-number range from 1.4 to 7.0 and a nose-fineness ratio range from 3.0 to 7.0. Stated accuracies are  $\pm 10$  percent for normal-force coefficient and 0.5 calibers for center of pressure.

A fairly extensive experimental study of the effects of particular nose shapes and cylindrical lengths is presented in Reference 6. Aerodynamic-stability parameters were determined at Mach numbers from 0.8 to 4.5 for tangent-ogive, conical, and power-series noses, all with a fineness ratio of four, combined with cylinder lengths of from 4 to 11 calibers. The effect of changing the nose-fineness ratio from 3 to 5 for conical and tangent-ogive shapes was determined for a cylindrical afterbody length of 6 calibers. Since the overall study covers body configurations of general interest to free rocket design, the pertinent results are presented in Figs. 8-6(A), (B), (C) and 8-7(A), (B), (C). These results should give normal-force coefficient gradients within ±5 percent and center of pressure within  $\pm .1$  caliber for the range of test variables. Whenever the body of interest falls within the range of test variables, it is recommended that the stability parameters be established from these data.

#### 8-2.1.2 Boattail

Where the rocket propulsive nozzle is smaller in diameter than the body cylinder, the rocket afterbody may be tapered to form a boattail, which reduces base drag. The normal loading over this boattail is negative, thus reducing the total normal-force coefficient and shifting the center of pressure forward. The slender-body theory predicts the normal-force coefficient gradient to be:

$$\left(\Delta C_{N_{\alpha}}\right) \approx -2 \frac{S_{bt}}{S_{ref}} \left[1 - \left(\frac{d_{bt}}{d_{c}}\right)^{2}\right]$$
(8-3)

where

S <sub>bt</sub>	=	cross-sectional area of boattail at its
•••		smallest diameter, A <sup>2</sup>
d	=	diameter, ft

bt = boattail

c = cylinder

 $\Delta =$  increment

It is recommended that slender-body theory predictions be used for the subsonic-to-sonic Machnumber range since systematic empirical investigations are not available.

At supersonic Mach numbers, Fig. 8-8 (Reference 5) will provide normal-force coefficient gradients for conical boattails located behind a semiinfinite cylinder; i.e., the local flow conditions upstream of the boattail are equal to the free stream conditions. These data, derived from linearized theory calculations and slender-body theory predictions, have not been verified by a detailed comparison with experimental data. Therefore, no statement can be made concerning the expected accuracy.

The center-of-pressure for the boattail normal force is located approximately  $0.6 l_{bt}$  from the cylinder-boattail juncture at subsonic Mach numbers. The center of pressure at supersonic Mach numbers may be evaluated from Fig. 8-9, taken from Reference 5.

It is recommended that the data in this section be used for boattail angles of less than 10 deg and ratios of  $\frac{d_{bt}}{d_c}$  greater than 0.8 to avoid flow separation from the boattail.

### 8-2.1.3 Conical-Flare Afterbody

A conical-flare afterbody can be added to nose cylinder configurations to provide aerodynamic stability. The slender-body prediction for the incremental normal force coefficient gradient of a flared afterbody is

$$\left(\Delta C_{N}\right)_{\alpha_{f} \ f \ lare} = 2 \frac{S_{f}}{S_{ref}} \left[1 - \left(\frac{\alpha_{e}}{d_{f}}\right)^{2}\right] \qquad (8-4)$$









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Figure 8-8. Normal Force Coefficient Gradient for a Boettail

and center of pressure of the normal-force-increment is

$$\left(\frac{\chi_{ep}}{l_f}\right)_f = \frac{\frac{d_e}{d_f}\left(\frac{d_e}{d_f} + 1\right) - 2}{3\left[1 - \left(\frac{d_e}{d_f}\right)^2\right]}$$
(8-5)

where

Ă.,	<b>a</b>	axial distance from cylinder-flare
		juncture to the flare center of
		pressure, ft
4	38	total flare length, ft
f	=	flare
de	*	cone diameter, It

# flare diameter it

**6-**38

d,

NOTE: Values of  $\frac{X_{cp}}{l_f}$  measured rearward from the cylinder-flare juncture are negative.

The important geometric parameter is seen to be the ratio of forebody cylinder diameter to base diameter. Flare angle and Mach number do not influence the flare normal-force within the limitations of the slender-body assumptions. To a limited degree, the experimental data of Reference 7 verify this trend at transonic Mach numbers and for flare angles of less than 8 degrees.

The actual normal-force contribution of flared afterbodies is shown by other theories (References 8 and 9) and by experimental results to be influenced by flow conditions forward of the flare, as well as by flare angle and length. Also, large flare angles (greater than about 10 deg) are known to cause flow separation at the cylinder-frustum juncture, which alters considerably the local normal-force loading in this region. Precise estimates of the flared-afterbody stability contribution must consider the complete upstream flow field, including boundary-layer characteristics.

For preliminary design estimates, however, the incremental normal-force coefficient gradients presented in Figs. 8-10(A) through (E) are considered adequate. These data were computed from slender-body theory and correlate fairly well with the experimental data presented in Reference 10.

For values of  $d_f/d_c$  greater than 1.5, location of the center of pressure of the incremental normal force — as predicted by slender-body theory varies from approximately 50 percent to 66 percent of the flare length aft of the flare leading edge. The use of 80 percent, for flare geometric variations within the parameters of the investigations described in References 7 and 10, is therefore consistent with the overall experimental accuracy. The combination of data in Figs. 8-10 with cone-cylinder or ogive-cylinder forebody data derived from par. 8-2.1.1 should provide overall normal-force coefficient gradients within  $\pm$  10 percent and center-of-pressure locations within  $\pm$  0.5 caliber.

#### 8-2.1.4 Oversize Head Configurations

Occasionally the nose section is required to have a larger diameter than that of the cylindricel



Figure 8-9. Center of Pressure for a Boattail

afterbody because of warhead considerations. Slender-body theory can be used to estimate normal force and center of pressure through the subsonic-transonic Mach number region. At supersonic Mach numbers, methods provided in the previous paragraphs can be used to calculate the nose-cylinder and boattail characteristics, neglecting the aft-cylinder normal-force contribution. If a tapered boattail is not used to provide a transition section between the nose and cylinder, ir if the boattail angle exceeds 12 deg, then the normal-force and center of pressure characteristics should be calculated assuming an effective 12-deg boattail angle.

## 8-2.2 FINS

The geometric and flow parameters affecting the normal force and conter of pressure of two isolated coplanar fins (2 fins in the same plane) will be discussed initially, followed by a discussion of fin-body and fin-fin interference effects



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Figure 8-11. Subsonic Fin Normal-Force Coefficient Gradient

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(par. 8-2.4). Throughout this discussion, thickness will be considered small relative to fin chord since the general practice is to minimize profile thickness for reduction of drag and weight.

Theoretical studies have shown the aspect ratio to be the dominant geometric factor governing the lifting characteristics of unswept wings or fins. The normal-force coefficient slope varies from  $\frac{\pi(AR)}{2}$ , for a very low aspect ratio (approaching zero), to  $2\pi$  for an aspect ratio approaching infinity. A simple correlation based on liftingline theory (Reference 11) gives

$$\frac{G_{H_{R}}}{AR} = \frac{2\pi}{2 + \left[ (AR)^2 (\beta^2 + \tan^2 \Lambda_{\frac{c}{2}}) + 4 \right]^{1/2}}$$
(8-0)

assuming that the section lift coefficient equals  $2\pi$  and where

$$AR = fin aspect ratio (fin span squared/fin area)
$$\beta = \sqrt{M_{\infty}^2 - 1}$$$$

**M**<sub>00</sub> = free stream Mach number Ā fin sweep angle, degrees fin mid-chord position

This equation, plotted in Fig. 8-11, is valid for thin unswept or swept fins of any aspect ratio and for Mach numbers to 0.6. However, for lowaspect-ratio fins which are of primary interest to rocket designers, valid results can be expected up to Mach numbers approaching one. Subsonically, the fin center of pressure may be assumed at 25 percent of the mean aerodynamic chord  $\overline{c}$ . measured rearward from the leading edge.

The complex nature of transonic flow has precluded reasonably simple mathematical solutions for the flow field about fins, except in the case of thin fins with very low aspect ratios. The linearized slender-wing theory predicts that

$$C_{N_{\alpha}} = \frac{\pi}{2} (AR)$$
(8.7)

Utilizing transonic-similarity laws, McDevitt (Reference 12) obtained from experimental data the correlation shown in Figs. 8-12(A) and (B) for rectangular planform fins. At Mach number

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1, linearized-wing-theory prediction matches the experimental data where  $(AR)(t/c)^{1/3}$  is less than one. Therefore, it is suggested that linearized-wing theory be used as a guide for planforms other than rectangular in the sonic region.

Linearized flow theory has been found to be an accurate means of predicting supersonic stability characteristics of thin-profile fins. Thickness effects are important, primarily when the Mach line emanating from the leading edge rootsection lies close to the leading edge. Reference 13 presents charts, based on linearized theory, to estimate normal-force coefficient gradient and center of pressure for swept leading-edge fins of nearly arbitrary planform.

Figs. 8-13(A), (B), (C) and 8-14(A), (B), (C), respectively, are duplications of the generalized charts for normal-force coefficient gradient and center of pressure. Fig. 8-14 prevides reasonable estimates of center of pressure for the subsonic transonic, and supersonic regions for all fin plantorms other than rectangular. A correction to the theoretical  $C_{N\alpha}$  for thickness effects is given in Fig. 8-15 for swept fins with wedge leading edges. Use of this figure is explained in the computational sheets, par. 8-2.4.4. Thickness has only a minor effect on center-of-pressure, and no correction to the theoretical estimates is considered necessary.

The supersonic normal-force coefficient slope and center-of-pressure of rectangular-planform fins as derived by linearized theory (Reference 14) are presented in Fig. 8-16. These data are valid for  $\beta(AR) \ge 0.5$ .

A general presentation of linearized-supersonicwing theory and serodynamic estimation warts can be found in Reference 15; the reader is referred to this work for fin planform not covered by the charts herein.

#### 8-2.3 RING TAIL

The normal-force coefficient gradients for ring fins installed in a cylindrical afterbody are presented in Figs. 8-17(A) through (F), taken from Reference 16, for Mach numbers from 0.8 to 3.0. The figure shows the normal-force coefficient gradient for various chord lengths and ring diameters plotted in a "carpet plot". Three different positions of the ring trailing-edge relative to the body base are indicated by the solid, chaindashed, and dashed lines.

As ring tails are often used in conjunction with oversized heads, it should be noted that the reference an a of the lift curve is the cross-sectional area of the cylindrical afterbody or which the ring is installed. The data used in Fig 8-17 were obtained from wind tunnel tests on rings having a 4° double-wedge section, with the inside surface of the ring diverging at 4° from the body centerline. (See sketch on Fig. 8-17.) Included are the effects of interference between the body, support strut, and ring on the normal-force coefficient gradient.

It should be noted that the test data are for rings whose trailing-edge diameter is larger than the leading-edge diameter. However, the charts should provide reasonably accurate lift estimates for other ring configurations, provided that the minimum and maximum diameters of the ring are within, the limits of minimum and maximum diameters of the 4° ring case.

The center-of-pressure is assumed to be at the ring mid-chord point.

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## 8-2.4 STABILITY OF COMPLETE CONFIGURATION

#### 8-2.4.1 Ganaral

In the previous paragraphs, consideration has been given to the prediction of force and moment characteristics of individual free flight rocket components. When the force and moment charscteristics of the complete configuration are computed, two major factors must be considered:

a. The data for the individual components may be summed for the total endy if a consistent set of data is used.

b. Certain interference effects must be accounted for when the components are joined to form the complete configuration.

The first factor concerns equatibility between the force and moment coefficients; i.e., the force coefficients must be reduced on a common reference area and the moment coefficients must be reduced on a common reference area and length as well as a common reference point.

To explain further, the normal force coefficient gradient is defined as

$$C_{N_{\alpha}} = \frac{N}{q \alpha A_{r \leq f}} \quad \text{for small values of } \alpha \tag{8-8}$$

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## Figure 8-13(B). Fin Normal Force Coefficient Gradient at Supersonic Mach Numbers

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Figure 8-13(C). Fin Normal Force Coefficient Gradient at Supersonic Mach Numbers

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Figure 8-15. Fin Normal Force Coefficient Gradient Correction Factor for Sonic Leading Edge Region



Figure 8-16. Normal Force Coefficient Gradient and Center of Pressute for Rectangular Fins

## where N

= normal force, lb

q = dynamic pressure  $(1/2 \rho V^2)$ ,  $\ln/ft^2$   $\alpha =$  angle of attack, rad or deg, and  $A_{ref} =$  reference area,  $ft^2$ 

Thus the unit c: measure for  $C_{N\alpha}$  simplifies to units per radian for a measured in radians (representing a slope).  $C_{N\alpha}$  is also sometimes presented as units per degree, which can be converted to radian-measure by the formula:

$$C_{N_{\alpha}}$$
 (per degree) x 57.3  
=  $C_{N_{\alpha}}$  (per radian). (8-9)

Either radian- or degree-measure may be used; however, all coefficients must be consistent.

To illustrate, assume we have obtained the following data:

$$C_{N_{\alpha \ body}} = 2.0/rad$$
 with  $S_{ref}$ 

and

$$C_N = .060/deg with S_{ref}$$
  
= fin planform arec =  $A_p$ 

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Figure 8-17(A). Incremental Normal Force Coefficient Gradient for a Ring Tail Mounted on a Cylludrical Afterbody





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Figure 8-17(E). Incremental Normal Porce Coufficient Gradient for a Ring Tail Mounted on a Cylindrical Afterbody

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Figure 8-17(F). Incremental Normal Force Coefficient Gradient for a Ring Tail Mounted on a Cylindcical Afterbody

First, convert  $C_{\mu}$  to radian measure  $\alpha$  (in

Next select a common reference area (usually the body cylindrical cross-sectional area is selected) as  $A_{ref} = A_{cyl}$ .

Then,

 $C_N = 2.0; rad$ (based on body cross-sectional area)

$$C_{s_{\alpha \text{ body}}} = 2.0/rad \left(\frac{A_{cyl}}{A_{ref}}\right)$$

(based on common area  $A_{ref}$ )

C<sub>Na fin</sub> = 3.43/rad

(based on fin planform area  $A_p$ )

$$C_{N_{\alpha} fin} = 3.43 \left(\frac{A_{p}}{A_{ref}}\right)$$

(based on common area A<sub>ref</sub>)

The total (sum of body and fin) normal-force coefficient gradient is, then, expressed as

$$C_{N_{\alpha} T} = C_{N_{\alpha} body} + C_{h_{\alpha} fin}$$
  
= 2.0/rad + 3.43  $\left(\frac{A_{p}}{A_{ref}}\right)$  /rad (9.10)

and the reference area for the total coefficient  $C_{N_{\alpha}}$  t is  $A_{ref}$ .

The moment coefficient gradient is defined as follows for small values of a:

$$C_{N_{\alpha}} = C_{N_{\alpha}} \left( \frac{X_{cp}}{l_{ref}} \right) = \frac{M}{qA_{ref} l_{ref} \alpha}$$
(8-11)

where M =

X =

As previously explained, radian or degree measures may be used. A comparison of the expressions for  $C_{\#\alpha}$  and  $C_{\chi\alpha}$  indicates that, in addition to a common area reference, the moment coefficient must be reduced on a common reference length and a common reference point.

To illustrate, assume we have obtained the following data concerning the configurations shown in the sketch below:



First, a reference length and point must be selected (usually the body diameter and nose of the body, respectively, are selected). Then, when

> $\dot{A}_{ref} = \frac{\pi d_c^2}{4}, \ \dot{i}_{ref} = \dot{a}_c \quad and$ Reference point = nose tip

$$C_{\mathcal{H}_{\alpha \ body}} = \left( C_{\mathcal{H}_{\alpha \ body}} \right) \left( \frac{2}{3} \cdot \frac{I_n}{d_c} \right) \quad (8-12)$$

$$C_{\boldsymbol{y}} = 2. \, \boldsymbol{\theta} \left( \frac{2}{3} \cdot \frac{l_n}{d_c} \right)$$
 (3-13)

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When

$$A_{rej} = \frac{\pi C_e^2}{4} \cdot l_{rej} = c_r \quad \text{and}$$

Reference point = junction of fin root chord and body surface

$$C_{N_{\alpha} fin} = C_{N_{\alpha} fin} \left( \frac{\chi_{cp}}{r} \right)_{fin} \quad (8-14)$$

Changing reference, when

$$A_{ref} = \frac{\pi d_c^2}{4}, \ l_{ref} = d_c \quad and$$

$$Reference \ point = nose \ tip$$

$$C_{N_{a \ fin}} = (3.0) \left[ \frac{l_n + l_{eb} + \left( \frac{X'_{cp \ fin}}{c_r} \right)}{c_c} \right] c_r$$

$$(8-15)$$

Now, since both moment coefficients have a common reference area, reference length, and reference point, we can write

$$C_{N_{\alpha}T} = C_{N_{\alpha} body} + C_{N_{\alpha} fin}$$
 (8-16)

or

$$C_{W_{cc} T} = 2.0 \left(\frac{2}{3} \cdot \frac{i_n}{d_c}\right)$$

$$+ 3.0 \left[\frac{l_n + l_{ab} + \left(\frac{X'c_p f_{th}}{c_r}\right)}{d_c}\right]c_r$$
(8-17)

where

$$A_{ref} = \frac{\pi d_e^2}{4}, \ l_{\pi i f} = d_e \quad and$$
  
Reference point = nose tip

The total center-of-pressure may be found as

$$\begin{pmatrix} X_{cp} \end{pmatrix}_{Total} = \begin{pmatrix} C_{a} \\ C_{N_{cr}} \end{pmatrix}_{Total} (d_{c})$$
  
(8-18)

measured rearward from the cose up, or the total center-of-pressure expressed in body diameters (or calibers) is

$$\left(\frac{\lambda_{sp}}{d_s}\right)_{Total} \cdot \left(\frac{C_{K_{\alpha}}}{C_{N_{\alpha}}}\right)_{freed}$$
(8-19)

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measured rearward from the nose tip.

The second major factor to be considered concerns the fin-body and fin-fin interference effects. These are covered in greater detail in the paragraphs which follow.

#### 8-2.4.2 Fin-Body Interference

When fins are attached to a bordy-of-revolution, interference effects increase the normal force over that for the isolated fins. This interference effect is particularly important for low-aspectratio fins where the fin span is approximately equal to the body diameter.

The presence of a cylindrical afterbody induces an increased local angle-of-attack along the fin span. If we neglect the nose effects a reasonably accurate prediction of the upwash distribution in the horizontal plane is given by Easkin (Reference 17) to be

$$\frac{\alpha}{\alpha_o} = \left[ 1 + \left(\frac{r}{y}\right)^2 \right]$$
(8-20)

where  $a_0$  is the body angle of attack, r is the body radius in feet, and y is the lateral distance from the body centerline in feet. If we utilize the approach of Reference 18 slender-body theory, the ratio of fin normal force in the presence of a body to the normal force of the isolated fin (interference factor) is

$$K_{f(b)} = \frac{C_{x_{\alpha} - f(b)}}{C_{x_{\alpha} - f(b)}}$$

$$= \frac{\frac{2}{\pi}}{\left(1 - \frac{r}{b}\right)^{-\frac{1}{2}}} \left\{ \left(1 + \frac{r^{4}}{b^{-\frac{4}{2}}}\right) \left[\frac{1}{2} Tan^{-1} \frac{1}{2} \left(\frac{5}{r} - \frac{r}{b}\right) + \frac{\pi}{4}\right] - \frac{r^{2}}{b^{-\frac{1}{2}}} \left[\left(\frac{b}{r} - \frac{r}{b}\right) + \frac{2}{2} Tan^{-\frac{1}{2}} \frac{r}{b}\right] \right\}$$
(8-21)

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Figure 8-18. Values of Lift Ratios Based on Slender-Body Theory

The primary parameter is seen to be the ratio of fin span b to body radius r. Although a more precise analysis would show dependence on Mach number, fin plenform, and location of the fin on the body, the slender-body result will give adequate preliminary design estimates of the ratio  $K_{f(b)}$ . Fig. 8-18 presents  $K_{f(b)}$  as a function of d/b.

Additional normal force is produced on the cylindrical body adjacent to the fins by carryover to the body of lifting pressure distribution on the fins. Subsonically, the method for determining this carryover by slender-body theory is

$$h_{b(f)} = \frac{C_{v_{\alpha}}}{C_{s_{\alpha}}} - \left(1 + \frac{r}{b}\right)^{2} - k_{f(b)}$$
(8-22)

for values of  $H \leq 1$ . Fig. 8-18 presents  $K_{b(f)}$  as a function of 7b.

Contrary to the  $c_{n^{-p}}$  for subconic Mach numbers, fin planform and Mach number are important parameters in determining the supersonic fin carryover normal force to the body. The ratio of carryover normal force to the isolated-fin normal force  $K_{b(j)}$  is determined adequately by the method of Reference 18. This method, based on slender-body theory, integrates the carryover pressure distribution over the region defined by the Mach cones emanating from the root-chord leading edge and trailing edge as shown in Fig. 8-19 taken from Reference 18.

If the fin trailing edge is located flush with the body base, as is the case in many rocket designs, the body area influenced by fin carryover pressures is restricted to that defined by the Mach cone from the rout-chord leading edge and the body base. Values of the ratio  $K_{b(f)}$  are presented in Fig. 8-20 for configurations with no



(A) NONPLAMAR MODEL (B) PLANAR MODEL Figure 8-19. Interference Effects of Firm an Justy

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afterbody and with an afterbody. These represent more refined estimates than those presented in Fig. 8-18.

A second method of estimating total fin-body interference for all Mach numbers and unswept planforms  $(0 < \beta(AP) < \infty)$  was developed by Morikawa (References 19 and 20). This method gives the total interference,  $K = K_{f(b)} + K_{b(f)}$ , only when the trailing edge of the fin is unswept and flush with the base. Figs. 8-21(A)-(F) pre-

and flush with the base.  $\kappa_{\alpha} = \frac{C_{N_{\alpha}}}{C_{N_{\alpha}}}$  (ratio of  $C_{N_{\alpha}}$  f

fin  $C_{N\alpha}$  with interference to basic "isolated" fin), as a function of fin to body geometry, Mach number, and taper ratios from 0.0 to 1.0. This method is generally easier to use when compared to that previously presented and gives preferred data if the configuration being analyzed meets the stated restrictions.

#### 8-2.4.3 Fin-Fin Interference

Cruciform fins-4 fins equally spaced around the body circumference-are the most common means of stabilizing free-flight rockets. In most cases, this type of fin provides the highest ratio of restoring moment to axial force. The data previousl: presented will permit the prediction of force and moment characteristics of this type of configuration. However, some designs might require more than four fins to obtain the necessary restoring moment. This could be particularly true for a configuration that was spanlimited, with a center of gravity located farther aft than normal. The information below will permit reasonably accurate estimates for certain multi-finned configurations or planforms, and also serve as a guide in estimating the force and moincat characteristics of other planforms.

The slender-body theory predicts that, at subsonic speeds, the ratios of the normal-force coefficient gradients for eight and six fin—equally spaced around the body circumference—to the gradient for twin fins—4 fins, 2 equally loaded are 1.52 and 1.37, respectively. Thus for speeds from subsonic up to sonic, the following relations are expected to apply:

$$\frac{C_{N_{\alpha}}}{C_{N_{\alpha}}} = 1.37$$

and

$$\frac{C_{N_{\alpha}}}{C_{N_{\alpha}}} = 1.62$$

where  $C_{N_{\alpha}}$  can be determined from methods

previously presented, and the center of pressure may be assumed at 25 percent of the mean aerodynamic chord  $\overline{c}$ , measured from the fin leading edge.

At supersonic speeds, shock waves from the leading edge can be expected to impinge on adjacent surfaces, causing considerable interference. Wind tunnel tests (Reference 21) on a series of clipped-delta planforms were conducted, and a correlation parameter determined. This correlation parameter is defined as follows:

$$= \frac{c_{re}}{\beta d_c \sin \frac{\pi}{n}}$$
(8-23)

where

$$c_{re} = exposed root chord$$

I

 $\beta = \sqrt{M^2 - 1}$ d<sub>c</sub> = body diameter

n = number of fins

This parameter is shown as the abcissa in Fig. 8-22 The ordinate represents the value of  $C_{N_{\alpha}}$ , based on an effective area  $S_{eff}$ , which is a function of the number of fins *n*, in accordance with the table below:

No. of fins
 
$$\frac{f}{S_{f}}$$

 4
 1.63

 6
 2.43

 8
 3.24

 $S_f$  is the exposed area of a single fin.

Thus, data for a multi-finned configuration may be obtained by computing the parameter I, entering Fig. 8-22 at this value of I and reading

1.37



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or

 $C_{N_{\alpha \ fin}}$  for the appropriate Mach number. Then, multiplying the value of  $C_{N_{\alpha \ fin}}$  by the appropriate value of  $S_{eff}/S_f$  (dependent on number of fins) yields the total fin contribution, based on a reference area equal to the exposed planform area of one fin. It should be emphasized that the data in Fig. 8-22 were developed for, and are directly applicable only to, the particular planforms indicated. However, the data may be used as a guide for predicting the characteristics of other planforms.

When the value of I is less than one, the Mach cone emanating from the leading edge of one fin does not impinge on adjacent fins. Therefore, the ratio of the multi-fin normal-force coefficient gradient to the twin-fin gradient (4 fins, 2 equally loaded) is a function of the number of fins only, and can be written as

$$\frac{C_{N_{\alpha} \ 6 \ fins}}{C_{N_{\alpha} \ 4 \ fins}} = 1.50$$
for I <

$$\frac{C_{N_{\alpha} \ 8} \ fins}{C_{N_{\alpha} \ 4} \ fins} = 2.00$$

and the four-fin data may be computed by methods previously presented.

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$$c = (2/3)c_0 \quad (I-a)\left(1 + \frac{\lambda^2}{1+\lambda}\right) = 4/3 \quad \sqrt{\frac{S_f}{AR}} \quad \left(\frac{1}{1+\lambda}\right) \quad \left(1 + \frac{\lambda^2}{1+\lambda}\right)$$
$$\overline{\eta} = 1/3 \quad \left(\frac{1+2\lambda}{1+\lambda}\right) \quad ; |\overline{x} = \overline{\eta} \left(\frac{b}{2}\right) \text{ TAN Aye}$$

#### Figure 8-23. Fin Geometry

Supersonically, the center of pressure may be assumed in the mid-point of the mean aerodynamic chord  $\overline{c}$ , n.casured rearward from the leading edge of the fin.

#### -9-2.4.4 Sample Calculation Sheet

 Table 8-1 was constructed to summarize the principles and formulas presented in par. 8-2
 Stability Characteristics of Rockets. The table also illustrates in numerical examples the use of the formulas and data curves presented in par. 8-2. Fig. 8-23 gives the geometric relationships for computation of fin geometry. Fig. 8-24 defines lengths and diameters associated with boattail, flare, and finned configurations. Finally, Fig. 8-25 presents an example configuration, with pertinent design data, as a basis for computation of force and moment characteristics. Entries shown in Table 8-1 were developed for this configuration. The superscript circled numbers appearing in Table 8-1 indicate that values for the expressions so annotated come from the column number corresponding to the superscript.

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## 8-3 DRAG

Estimation of drag for free reckets can be restricted to zero-lift since the rocket follows a ballistic path. The total drag on the rocket is the sum of the wave drag produced by pressure forces normal to all surfaces except the base, plus the skin friction drag produced by forces tangential to the surfaces, plus the base drag produced by pressure forces acting normal to the base. The drag coefficient  $C_p$  is equal to the drag force D in pounds divided by  $1/2\rho V^2 S_{ref}$ , where  $\rho$  is the atmospheric density in slugg per ft<sup>\*</sup>, V is the recket velocity in ft per sec, and  $S_{ref}$  is the reference area, in square feet, on which  $C_p$  is based.

## 8-3.1 WAVE DRAG

Wave drag is present on the rocket nose, the afterbody (Loattail or flare), and the fins or other stabilizing surfaces. Since wave drag is produced by pressures normal to the surface, no wavedrag component is present on the cylindrical section.

## 8-3.1.1 Nose Wave Drag

The nose shapes of free rockess are usually slunder since there are no large volume requirements to enclose guidance systems or related components. Blurting the nose with a radius equal 0.1 times the maximum body diameter avoids a sharp point for manufacturing and safety reasons, yet causes only a negligible increase in drag and has no appreciable effect on aerodynamic estimates.

Nose wave drag is influenced primarily by fineness ratio, nose shape, and Mach number. The general trend of nose wave-drag characteristics is shown in Figs. 8-26(A) and (B). For most slender nose shapes, the coefficient is zero below a Mach number of about 0.8 to 0.9; rises sharply through the transonic region; and decreases with increasing supersonic Mach number. The coefficient decreases with increasing nose fineness ratio. However, in practical design, nose fineness ratios are limited by rocket total-length requirements, weight requirements, and increasing friction drag.

For preliminary design estimates, the family of nose shapes-of-interest for free rockets is bounded

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Figure 8-27. Wave Drag Coefficient of Optimum Secont Ogive Cylinder at Transonic Speed

by cones and ogives. A secant ogive, formed by a circular aic with twice the radius of a tangent ogive, yields minimum wave drag for low supersonic Mach numbers (Reference 22); drag characteristics of this nose shape are presented in Fig. 8-27. For higher Mach numbers, a secant ogive with 2.5 to 3 times the radius of a tangent ogive is optimum. However, when optimizing overallconfiguration nose shape, factors other than drag, must be considered.

The transonic wave-drag coefficient of general ogives is presented in Fig. 8-28. Unfortunately, there is no apparent, reliable correlation of transonic wave-drag for cones. It is suggested that estimates be guided by Fig. 8-26 and other experimental data, such as References 23 and 24. Values of supersonic wave drag for cones and general ogives are presented in Fig. 8-29 as a more detailed extension of values presented in Fig. 8-26.

## 8-3.1.2 Boattail Wave Drag

When the exit diameter of the rocket pozzle is smaller than the body-cylinder diameter, the afterbody of the rocket may be tapered to form a boattail and reduce the base drag. This technique, however, increases the wave drag on the configuration. An optimum boattail configuration, therefore, results from balancing the increase in wave drag with the reduction of base drag.









The supersonic wave drag of conical and parabolic boattails is presented in Figs. 8-30 and 8-31. No analytical method or suitable parametric experimental data exist for accurate prediction of boattail wave drag at subsonic and transonic speeds. If experimental data for a particular configuration cannot be found, it is suggested that supersonic data be extrapolated to peak value at a Macl. number of 1.0 to 1.2, with a sharp reduction to a lower value at subsonic speeds. A curve of boattail wave drag, to act as a guide, is shown in Fig. 8-32.

## 8-3.1.3 Flare Wave Drag

Flared afterbodies are useful for rocket sta bilization where precise stability margin control is required. The drag on flares, however, is higher than the drag on fins giving equivalent stabilization. Parametric experimental data and several theoretical methods, which agree well with experimental results, are available for estimating flare wave drag. Cure should be exercised in the use of experimental data for large flare-angles since flow separation at the cylinderflare juncture may be more pronounced in some

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Figure 8-30. Wave Drag Coefficient of Conical Boattails at Supersonic Speeds





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Figure 8-32. Wave Drag Coefficient of a Boattail at Transonic Speeds

tests where the Reynolds numbers are lower than would be expected in actual flight. The wavedrag coefficient determined experimentally (Reference 27) for a series of flares is presented in Figs. 8-33(A)-(I).

#### 8-3.1.4 Fin Wave Drag

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The wave drag on fins is small (on the order of 10 percent) compared to the total rocket drag. The drag is influenced strongly by thickness-tochord ratio and sectional shape. Figs. 8-34(A)-(H) present the theoretical wave drag coefficient, based on planform area, at zero-lift for various sectional shapes and planforms. The discontinuities in the curves will not exist in practice, and values at transonic speeds are not precise. The wave drag for sectional shapes not shown in Fig. 8-34 may be evaluated as follows: in Fig. 8-34, find the wave drag coefficient for a double-wedge section having the same thickness and planform geometry as the sectional shape-of-interest; multiply the value so obtained by the factor for the particular shape from Fig. 8-35. The product will be the desired wave drag coefficient.

The transonic wave drag coefficient of rectangular and delta planform fins is shown in Figs. 8-36 and 8-37. The wave drag for other planforms will be between the values on these two curves for fins with the same sectional shape, thickness-to-chord ratio, and aspect ratio.

#### 8-3.1.5 Ring Tail Wave Drag

The ring tail wave drag coefficient, based on an arbitrary reference area  $S_{ref}$ , may be evaluated by multiplying the two-dimensional drag coefficient by the product of ring-tail circumference times chord length (or "rolled out" planform area):

$$C_{D_{y}} = \frac{\pi d_{r}(c) (C_{D_{y}})}{\frac{S_{ref}}{S_{ref}}}$$
(8-24)

At supersonic speeds, the two-dimensional drag coefficients for particular sectional shapes may be obtained from Fig. 8-35. At transonic speeds. the two dimensional drag coefficient for a symmetrical double-wedge may be obtained from Fig. 8-38. For other sections, the double-wedge value should be multiplied by the appropriate modifying factor in Fig. 8-35.

The drag evaluated above will be slightly higher than the actual flight data due to the interfer-

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Figure 8-33(G) & (H), Wave Drag Coefficient of Conical Flare

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Figure 8-33(1), Wave Drag Coefficient of Conjcal Flare

ence effects of the struts attaching the ring tail to the rocket body. However, since these effects are small compared to the total rocket-drag and the computation of the effects is complex, interference may be neglected for preliminary design.

For further discussion of interference, see Reference 25.

## 8-3.2 FRICTION DRAG

The friction drag depends primarily on conditions of heat transfer, position of transition from laminar to turbulent boundary layer, Reynolds number, and Mach number. The method presented in this paragraph for evaluating the friction-drag coefficient is a rapid approximate method. More precise solutions are presented in References 26 and 27.

The average skin-friction coefficient (frictiondrag coefficient) for flat plates, based on the

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wetted area, is presented in Fig. 8-39 as a function of Mach number and Reynolds number. Reynolds number per foot of length, as a function of Mach number and altitude, may be obtained from Fig. 8-40. The flat-plate coefficient should be used for fin and ring tail surfaces. Correlation of experimental data has shown that the skinfriction coefficient for bodies of revolution is approximately 15 percent higher than the flat-plate values (Reference 28). Therefore, for preliminary design purposes, the values obtained from Fig. 8-39 should be multiplied by 1.15 when the  $\Sigma_{A}$  face is a body of revolution.

#### 8-3.3 BASE DRAG

Base drag is the result of pressure forces due to airflow separation from rearward-facing steps such as body bases and fin trailing edges. The drag is affected by the geometry of the rearwardfacing step and by the properties of the airstream approaching the step, including boundary-layer conditions. A rocket exhaust complicates the base flow phenomenon by adding a second stream with different properties, boundary layer conditions, and approach geometry. The mixing of and interaction between the air and rocket exhaust streams produce a complex fluid mechanics problem.

General curves and empirical relations will be presented to allow a rapid estimation of base drag of a quality suitable for preliminary estimates. No attempt will be made to discuss in detail the effects of various parameters on base drag. Insufficient experimental data exist, throughout the range of parameters, to allow use of design charts.

## 8-3.3.1 Body-of-Revolution Base Drag, Rockat Jet Off

The boundary layer approaching the body base of free rockets is generally turbulent. For cylindrical afterbodies, the variation of base-pressure coefficient (negative of base-drag coefficient, based on the area seen by base pressure) with Mach number is well defined. For boattailed and flared afterbodies, several methods of estimating base pressures are presented in References 22 and 29. These methods, however, have







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Figure 8-34(D). Wave Drag Coefficient of Fins at Supersonic Speeds

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ТҮРЕ	PROFILE	TWO DIMENSIONAL DRAG COEFFICIENT BASED ON PLANFORM AREA	FACTOR
SYMMETRICAL Double Wedge		$\frac{4}{M} \left(\frac{t}{c}\right)^2$	1
DOUBLE WEDGE		$\frac{1}{M} \cdot \left(\frac{t}{c}\right)^2 \cdot \frac{1}{m(1-m)}$	<u>1</u> 4m (1 – m)
SINGLE WEDGE		$\frac{1}{M} \cdot \left(\frac{t}{c}\right)^2$	<u>1</u> 4
CROPPED DOUBLE WEDGE	$\frac{1}{mc} + (1-m)c \rightarrow \frac{1}{mc}$	$\frac{1}{M}\left[\left(\frac{t}{c}\right)^2, \frac{1}{m} + \frac{\left(t-h\right)^2}{c^2\left(1-m\right)}\right]$	$\frac{1}{4} \left[ \frac{1}{m} + \frac{\left(1 - \frac{h}{t}\right)^2}{1 - m} \right]$
SYMMETRICAL PARALLEL DOUBLE WEDGE		$\frac{2}{M} \left(\frac{t}{c}\right)^2 \cdot \frac{1}{m}$	<u>1</u> 2m
PARALLEL DÕUBLE WEDGE	m <sub>1</sub> c <sup>-</sup> (1-m <sub>1</sub> -m <sub>2</sub> )c <sup>-</sup> m <sub>2</sub> c <sup>-</sup>	$\frac{1}{M} \cdot \left(\frac{t}{c}\right)^2 \left[\frac{1}{m_1} + \frac{1}{m_2}\right]$	$\frac{1}{4} \left[ \frac{1}{m_1} + \frac{1}{m_2} \right]$
SYMMETRICAL BICONVEX (CIRCULAR OR PARABOLIC ARCS)		$\frac{4}{M}\cdot\frac{4}{3}\cdot\left(\frac{1}{c}\right)^2$	<u>4</u> 3

Figure 8-35. Wave Drag Coefficient of Fins of Various Sectional Shapes

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Figure 8-40. Reynolds Number as a Function of Flight Mach Number and Altitude

not been confirmed by experiment throughout the Mach-number range or through a sufficient range of afterbody geometric parameters.

The variation of base pressure with Mach number for a cylindrical body (based on experimental correlations) and boattailed or flared afterbodies is presented in Fig. 8-41. Although it is uncertain that afterbody angle is the major parameter affecting base pressure, it is presented in this manner for convenience. If nominal-length boattails and flares are considered. the data presented will be adequate for preliminary design purposes.

## 8-3.3.2 Body-of-Revolution Base Drag, **Rocket Jet On**

A typical example of the base pressure, with the effects of the rocket jet considered, is shown in Fig. 8-42. Examination of the figure reveals several important facts concerning free rocket design. During boost, when the jet exit diameter usually approaches the base diameter, base drug is relatively unimportant. The combination of high chamber pressure, high base pressure, and small base-annulus area results in a low base drag or even a base thrust. For sustainer operation, the jet-exit-to-base-diameter ratio and jetto-free-stream pressure ratio are usually low. resulting in high values of base drag, mounting to as much as 50 to 70 percent of the total drag. After burnout, the effect of residual burning must be considered. Mass added to the base region as a result of residual burning serves to increase the pressure ratio in the base region, re-

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sulting in base pressures considerably higher than would be predicted for the jet-off case. This phenomenon is shown by the peak in base pressure at low jet-to-free-stream pressure ratios. This decrease in base drag due to residual burning effects may lead to errors in range prediction if not considered.

Previous design charts for engineering estimates of jet-on base pressure have been based on a limited amount of unrelated experimental data from various sources, which give reasonable estimates only if the configuration closely matches that on which the data were obtained. A theoretical method for predicting base pressure is presented in Reference 30. This method predicts trends of various parameters independently and can handle several parameters not easily simulated in wind turnel tests. The method, however, is very complex and requires the use of high-storage-capacity computers.

A method, based on the thrust coefficient, has been developed (Reference 31) which allows rapid prediction of base pressures suitable for engineering estimates. For a cylindrical afterbody, the base pressure is given by

$$\frac{P_B}{P_{ab}} = \frac{\frac{3}{5} (C_F)^{\frac{1}{5}}}{\frac{V}{a^{\frac{1}{5}}}}$$
(8-25)

where

$$C_F = \frac{Thrus t}{P_c A_T}$$
(8-26)

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and

$$\frac{1}{a^{*}} = \sqrt{\left(\frac{y-1}{2}\right) M^{2} \left(1 - \frac{y-1}{2} M^{2}\right)^{-1}}$$
(8-27)

and the base pressure coefficient is defined as

$$C_{P_{B}} = \frac{P_{\infty} - P_{B}}{\frac{1}{2} \rho_{\infty} V_{\infty}^{2}} = \frac{1 - \frac{T_{B}}{P_{\infty}}}{\frac{Y}{2} M_{\infty}^{2}}$$
(8-28)

In the above equations,

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base pressure, 1b/ft<sup>2</sup> Р, , motor chamber pressure, lb/ft<sup>2</sup>

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Figure 8-41. Base Pressure Coefficient of Cylinders, Bootyails, and Flares With Rocket Jet Off



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- free stream pressure, lb/ft<sup>2</sup> velocity, fps 12
- free stream velocity. fps

sonic velocity, fps

- thrust coefficient
- jet throat area, ft<sup>2</sup>
- base pressure coefficient
- ρ<sub>∞</sub> atmospheric density. slug ft<sup>3</sup>
- ratio of specific heats Y
- M Mach number

For bodies with flared or boattailed afterbodies,  $P_{B}/P_{\infty}$  is corrected by use of Fig. 8-43. The stated correlation agrees well with most of the available experimental data. It is applicable at jet-to-free-stream pressure ratios above the value where base pressure is minimum (represented by the nearly linear portion of the curves in Fig. 8-42).

To give an indication of the characteristics of buse pressure through a more complete Mach number and jet-pressure range, Fig. 8-44 has been prepared. This figure represents a cylindrical body and a nozzle having a jet Mach number of about 3.0. The solid curves represent either experimental data or the correlation curve. The dashed curves are extrapolated values.

#### 8-3.3.3 Fin Base Drag

The boundary layer approaching the base of fins and other stabilizing urfaces is generally turbulent. The effects of profile shape on the base-pressure coefficient at supersonic speeds with a turbulent boundary layer is small. Fig. 8-45 provides a good estimate of tin base-pressure coefficient at supersonic speeds. At transonic and subsonic speeds, the ratio of trailing edge thickness to chord length is significant, and Fig. 8-46 should be used as a guide for estimating the base pressures.

## 8-3.4 DRAG CHARACTERISTICS OF COMPLETE CONFIGURATIONS

#### 8-3.4.1 Interterence Effects-Fin on Base

The presence of fins on rockets affects the external flow characteristics and usually results in increased base drag. The most important paraineters appear to be fin thickness, fin longitudinal position, number of fins, and free-stream Mach number. Experimental data on the effects of fins are sparse if all important parameters



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Figure 8-44. Base Pressure on Cylindrical Bodies





are considered. It is suggested that the empirical relation developed in Reference 29 be used in estimating fin effects on base dirag:

$$\Delta C_{\rho_b} = \frac{t}{c} \left( \frac{0.825}{M^2} - \frac{0.05}{M} \right) n$$
 (8-29)

where

t c = thickness-to-chord ratio of fins and n = number of fins

This relation is limited to the case where the fin trailing edge is flush with the base. Predicted values using this relation appear to be high at Mach numbers below about 2; with reasonable agreement for Mach numbers greater than 2.

#### 8-3.4.2 Computational Table

The drag characteristics of the complete configuration are computed by summing the individual component drag coefficients, based on a common reference area. Table 8-2, Drag Force Calculation Sheets, which follow, indicate the method of obtaining the drag coefficients of the





Figure 8-46. Base Pressure Coefficient of Fins at Transonic Speeds

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individual components and of the complete configuration based on the configuration presented in Fig. 8-25.

# 8-4 AERODYNAMIC TESTING

The aerodynamic performance of rockets may be evaluated by theoretical estimates, flight testing, or wind tunnel testing. Theoretical estimates, due to lack of refinement, often fail to provide adequate quantitative aerodynamic data. Flight testing provides a slow rate of data collection; does not allow adequate control of the test article; and is expensive because the test article is usually expended. Wind tunnel testing, however, allows precise control of the parameters influencing flight characteristics. A wide scope of the problems associated with placing a rocket in a selected trajectory—such as stability, drag, and propulsion system influence—may be investigated in a complete wind tunnel program.

An indication of the wind tunnels available in the United States is given in References 32 and 36. While this list is not current and therefore incomplete, the uniqueness of the available tunnels dictates the necessity for matching particular

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tunnel characteristics to the particular test requirements. Tunnel operating capabilities and size are foremost among the considerations in selecting a test facility. However, consideration of availability, accessory equipment, and cost of test time cannot be ignored.

Wind tunnels are normally classified according to their operating speed range as follows:

Tunnel Class if ication	Mach Number Range	
Subsonic	Less than 0.7	
Transonic	0.7 to 1.2	
Supersonic	1.2 to 5.0	
Hypersonic	Greater than 5.0	

Due to inherent problems associated with operating at different speed (or Mach number) ranges. wind tunnel facilities usually elect to operate only within the range of their classification Mach numbers. Since a large portion of the rockets considered in this handbook operate over a wide range of the Mach number spectrum, complete testing will require more than one facility. The upper limit for supersonic tunnels, M = 5.0, has been set from considerations of operating procedures and not abrupt changes in flight characteristics. When air is expanded to a Mach number of approximately five and above, the attendant large change in the temperature results in liquefaction of the air. To prevent this, heaters of large capacity, or a medium other than air, may be used to maintain temperatures above the liquefaction point.

The Reynolds-number capability of a wind tunnel is an important consideration. Matching the full-size-rocket Mach number and Reynolds number on the scale model insures that flow patterns are similar and that the measured forces and moments may be scaled up to the full-size rocket Reynolds-number a a function of Mach number and altitude is presented in Fig. 8-40. The flow patterns become fully established at a Reynolds number of approximately two million, and therefore the requirement for matching Reynolds number above this value may be zejaxed.

The capability for matching flight environment temperature in a wind tunnel is only important in the study of high velocities, such as may be produced by reentry trajectories. Flight environment temperatures are not significant on the classes of rocket considered in this handbook.

The investigation of the influence of a propulsion system on the aerodynamic characteristics of a rocket requires a facility with the capability of propulsion testing or propulsion jet simulation. Operation of a propulsion system in a tunnel requires a means for removing the combustion products from the tunnel airstream, and creates fire and explosion hazards. Propulsion jet simulation is much simpler. Jets of compressed gases such as air or nitrogen will closely simulate exhaust flow patterns. The hazards connected with this technique are only those normal to high pressure storage and transmission. Jet exhaust conditions may be more closely simulated by the decomposition of hydrogen peroxide, but personnel hazards require special storage and handling procedures.

It is desirable to test the full-size rocket in order to have the maximum degree of confidence in the data. Generally, however, this is not practical, and a scaled-down test model must be fabricated. Model-size decisions must be based on (1) characteristics to be investigated, (2) instrumentation located in the model interior, (3) model support capabilities, and (4) size of available test facilities.

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The model scale must be large enough so that the component parts which are normally exposed to free stream flow on the full-size article will not be submerged in the boundary layer of the test model. It is desirable that the selected scale provide a boundary layer of the same character that will exist on the full-size article. To maintain a desirable scale and duplicate boundarylayer conditions, the boundary layer often must be controlled by artificial means. There are practical limits to the duplication of small details of the full-size rocket. Duplicated details such as surface condition, small protuberances, screw heads, and small gaps in the scale model usually serve only to increase the fabrication cost, and affect the data to such a small extent that measuring accuracies do not reveal their presence. The tolerances used in manufacturing the fullsize rocket should be considered in development of the test model. The data presented in Fig. 8-47 show a comparison of the test results obtained from a full-size model and an eight-percent scale

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model of a typical artillery rocket, it can be seen that the agreement is excellent.

The amount of instrumentation that must be located inside the model often determines the minimum scale that can be used. Also, the scale of the model is often determined by the ability of the support to withstand the loads imposed on it.

The dimensions of the wind tunnel test section must be large enough so that the model does not significantly alter the velocity of the airstream and so that disturbances imparted to the airstream do not reflect from the tunnel boundaries to the model. It is not possible to quote maximum allowable model dimensions which will avoid these difficulties since they are dependent on overall configuration. position in tunnel. operating conditions. efforts made to attenuate these effects in each tunnel, and the precision of test measurements. Theoretical means of defining the relationship between model maximum size and test section size are not precise. Design decisions must be based on experimental investigations and an intimate knowledge of the testing facility. Fig. 8-48, from Reference 33, gives an indication of the relationship between the geometry of a typical body-of-revolution model and the allowable test-section size for a range of supersonic Mach numbers. However, this information was obtained experimentally, in part, and cannot be applied directly to other test facilities.

A survey of the descriptive literature on several transonic tunnels indicates that the model maximum cross-sectional area should be less than two percent of the test cross-sectional area. This ratio may be slightly increased if the model is not to be tested at large angles of attack. The allowable model cross-sectional area in subsonic tunnels is less restrictive and may be as high as 10 percent of the test cross-sectional area. The maximum model length in subsonic tunnels is determined by the length of the test section containing the desired flow properties.

The necessity of supporting the model in the airstream prevents exact duplication of flow patterns over the base of the model. The normal means of supporting the model is a horizontal sting which extends from the interior of the model through the base and is cantilevered from a vertical support member downstrear... Unlike flight conditions, the sting promotes wake stabilization and creates disturbances that might propagate into the base region. To reduce these effects, the sting should be as small as structural considerations will allow, and abrupt increases in the lateral dimensions should be avoided to provide a relatively straight member over a considerable length. A rule of thumb often applied is that the flow disturbances created by abrupt changes in the support system may be propagated upstream through the support boundary layer and model wake for a distance five times greater than the lateral dimensions of the disrupting portion.

Design decisions on the materials and fabrication of a model must be based on the anticipated loads, severity of vibrations, and structural temperature gradients. The majority of test facilities require that model construction provide a factor of safety of at least four, based on maximum anticipated loads which, in supersonic tunnels, often occur during the establishment of flow in the test section. At Mach numbers of 5.0, the stagnation temperature at some points on the model is approximately six times greater than the static temperature at other points.

The high cost of tunnel test time requires that model changes. necessary during the test. be made in a minimum of time. The expense of designing and fabricating quick-change capability in a model can usually be justified by savings realized through increased utilization of tunnel time.

Balances, fitted in the interior of the test model. resolve the net aerodynamic forces acting on the model into the components shown in Fig. 8-49. The measuring elements of these balances are electrical strain gages, with an accuracy of approximately 1 2 to 1 percent of the maximum ŝ
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	[			MACH	NUMBER	{		
$\theta_{\rm C}$ , deg	x/d	1.5	2	2.5	3	4	5	6
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20	10 2 4 6 8 10	2.30 4.45 6.50 8.60 10.70	6.10 1.60 3.20 4.65 5.95 7.20	4.70 1.35 2.60 3.65 4.65 5.60	4.15 1.20 2.30 3.10 4.00 4.90	3.30 1.00 1.90 2.55 3.25 3.95	2.90 1.00 1.70 2.30 2.85 3.40	2.63 0.95 1.55 2.15 2.65 3.10
HEMI	2 4 6 -8 10	3.75 5.95 8.00 10.05	2.65 4.10 5.37 6.70 7.95	2.20 3.35 4.45 5.40 6.35	2.00 3.00 3.90 4.70 5.60	1.70 2.75 3.20 3.90 4.65	1.65 2.30 2.95 3.60 4.20	1.60 2.23 2.80 3.40 3.90
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Figure 8-49. Aerodynamic Force Components

rated load. To obtain the greatest accuracy, a balance should be selected with a maximum load rating corresponding closely to the predicted test loads, especially if small changes in the total loads are to be measured.

Balances are compensated to operate in temperature environments as high as 180°F. At higher temperatures, a means of cooling must be provided.

Detailed knowledge of the effect of the flow over a model may be obtained by measuring surface pressure with manometers or transducers. Transducers are preferred for greater accuracy and faster response time. Measuring devices should be located near the test model, and the orifices and connecting lines should be large enough to prevent unnecessary time delays in sensing pressure changes.

Temperature measurements are made by thermocouples which are selected for the expected temperature range and compatibility with tunnel read-out instrumentation. Reference 34 presents information on the performance of various types of thermocouples.

Flow visualization techniques are useful in making qualitative evaluations of the flow over a model. Subsonic flow patterns may be determined by observing tufts attached to the surface of the model. Areas where the flow exhibits unusual turbulance or separates from the model surface may be identified by coating the surface with a volatile substance and observing evaporation rates. At supersonic velocities, the compression and expansion waves emanating from the model surfaces are characterized by marked changes in density which may be identified by shadowgraphs, schlierens, or interferometers.

A recommended source of information in planning wind tunnel tests is the descriptive literature issued by each test facility. This literature provides detailed information for all problem areas covered in the foregoing discussion. The Ballistic Research Laboratories at Aberdeen Proving Ground, Maryland, described in Reference 35, provide the most readily available facilities for Army-sponsored wind tunnel tests.

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l Mach No.	2 ß	3 refarea (Å <sub>ref</sub> ) Ft <sup>2</sup>	$\begin{array}{c} & & \\ & & \\ & ref length \\ & & \\ & & \\ & & \\ & & \\ & & Ft \end{array}$	· 5 ref point (body sta)
0 .5 1.0 1.5 2.0 2.5 3.5 4.5	1 .866 0 1.12 1.73 2.29 3.36 4.39	1.225 1.225 1.225 1.225 1.225 1.225 1.225 1.225 1.225 1.225	1.25 1.25 1.25 1.25 1.25 1.25 1.25 1.25	0 0 0 0 0 0 0 0
arbitrarily selected	$\beta = \sqrt{w^2 - 1}$	arbitrarily selected (usually cross sectional area of body cylindrical section or $\frac{\pi d^2_{cyl}}{4}$ )	arbitrarily selected (usually diameter of body cylindrical section, $d_{cyl}^{-1}$ )	arbitrarily selected (usually nose tip)

### TABLE 8-1. COMPUTATIONAL TABLE

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		TABLE 8-1.	COMP	UTATIONAL	TABL	E (cont)		
		Sul	sonic	and Sonia	П.ПШ с Сотр	utation		
Data X		Body -	111111 Force	and Mament	Char	niinnin acteristic:	s	
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1	6 7	7 8	9	10	11	12	13	14
Mach No.	$k_2 - k_1 = \frac{A_1}{A_r}$	$\frac{S_B}{ef} = C_{N_{\alpha} fb}$	S <sub>bt</sub>	ΔC <sub>N</sub> <sub>αbt</sub>	S <sub>f1</sub>	ΔC <sub>N</sub> α. fl	C <sub>N</sub> a body	X <sub>cp</sub>
0 .5 <sup></sup> 1.0	$ \begin{array}{c} .95 \\ .95 \\ .95 \\ .95 \\ 1. \end{array} $	0 1.90 0 1.90 0 1.90		• 0 • 0 0	•	0 0 0	1.90 1.90 1.90	te tip)
2.0 2.5 3.5 4.5	from Fig. 8-1	$C_{N_{\alpha} f_{b}} = 2(k_{2} - k_{1}) \frac{S_{3}}{A_{ref}}$ see alno Figs. 8-6 & 8-7 for specific	Boattail cross-sectional area at minimum diameter section	$\Delta C_{N_{\alpha}bt} = 2 \frac{S_{bt}}{S_{ref}} \left[ 1 - \left(\frac{d_{bt}}{d_c}\right)^2 \right] \text{ per rad; ref are} = A_{ref}$	Flare cross-sectional area at maximum diameter section	$\Delta G_{N_{\alpha fl}} = -2 \frac{S_{fl}}{A_{ref}} \left[ I - \left(\frac{d_e}{d_{fl}}\right)^2 \right] \text{ from Fig. 8-10(A); per rad;}$	$C_{N_{\alpha}} = C_{N_{\alpha}} \bigoplus_{j} \text{ per rad; ref area} = A_{ref};$ add $\Delta C_{N_{\alpha}} \bigoplus_{i} \text{ or } \Delta C_{N_{\alpha}} \bigoplus_{i} \text{ or } \Delta C_{N_{\alpha}} \bigoplus_{j} \text{ if applicable}$	Centroid of projected nose area (measured rearward from n

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Ref Data			Subso	nic and S	onic Comput	tation		
			Fin - For	ce and Mo	ment Charac	cteristic		·
1 .Mach	21 6	22 S <sub>f</sub>	23 AR	24 β²	25 tun²A <sub>c/2</sub>	26 F <sub>1</sub>	27 C <sub>Nac</sub> f	28 <sup>C</sup> Na 5
No. 0 .5 1.0 1.5 2.0 2.5	2.08 2.08 2.08	1.882 1.882 1.882	2.31 2.31 2.31	1.0 .75 0	0.75 0.75 0.75	3.06 2.83 2.00	AR 1.11 1.15 1.30	2.56 2.66 3.00
3.5 4.5	span (see Fig. 8-23)	fin planform area (see. Fig. 8-23)	$AR = \frac{b^2}{S_f}$	$\beta^2 = 1 - M^2$	(tangent of mid-chord sweep angle) <sup>2</sup>	$R_I = AR(\beta^2 + \tan^2 \Lambda_{c/2})^{1/2}$ abscissa entry for Fig. 8-11	from Fig. 8-11	$C_{\mu} = \frac{C_{\mu} \sigma_{\mu}}{2} (m)$ per rad; ref area = $S_{f}$

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1 / Mach	29 67	30 .\	31 Cy	32 <u>1</u>	33	34 <u>N<sup>2</sup> • 1</u>	35
to,	ά		"α γ	ē	(c)	$\left(\frac{t}{c}\right)^{2/3}$	$\left(\overline{c}\right)^{n}\alpha f$
0 .5 1.0 1.5	3.93 4.09 4.61	165.5 165.5 165.5	43.4 45.1 50.9				
2.0 2.5 3.5 4.5	$G_{\alpha}^{\prime} = G_{\alpha} = \left(\frac{N_{f}}{A_{ref}}\right)$ per rad; ref area $A_{ref}$	$V_{rr_{I_{1}}}$ $l_{mr}$ $l_{m}$ , $[l_{n}]$ $n$ $7.5$ measured from nose tip (see Fig. 8-23 for $\overline{c}$ ); assumes fin trailing edge flush with base. [] indicates term could or could not be in the equation, depending upon configuration being analyzed.	$G_{\mathbf{W}} = \int_{\mathbf{A}} G_{\mathbf{A}} = \begin{pmatrix} X_{r,l} \\ I_{r,l} \end{pmatrix}$ per rad; ref area $A_{r,l}$ ; ref $G_{\mathbf{W}}$ ; $M_{r,l}$ ; with respect to nose tip	ratio of Gn maximum thickness to maximum chard length	cutry for horizontal variable, Eig. 8-12(A)	ontry for vertical variable, Fig. 8-12(A)	from Fig. 8-12(A)

AMCP 706-280 Ì TABLE 8-1. COMPUTATIONAL TABLE (cont) Subsonic and Sonic Computation Subsonic and Sonic Computation Ref Data Rectangular Fins - Force and Moment Characteristics 40 1 36 37 38 39  $\left(\frac{\Lambda_{rp}}{c}\right)_f$ C<sub>v</sub>a f C<sub>V</sub><sub>a</sub>, C<sub>V</sub><sub>a f</sub>  $\Lambda_{ep}$ Mach No. 0 .5 1.0 measured from ose tip; assumes 1.5 2.0 2.5 3.5 4.5 per rad; ref area  $A_{rrf}$ ; ref length  $I_{rrf}$ ; with respect to nose tip lindicates depending from Fig. 8-12(B), measured from fin leading edge term could or could not be in the equation, Ś fin trailing edge is flush with body base. per rad; ref area Arel upon configuration heing analyzed. per rad; ref area  $X_{cp_{f}} \leftarrow l_{n} + l_{ab} + \left[l_{bs}\right] - \left[1 - \left(\frac{X_{cp}}{c}\right)\right]c$  $C_{N_{\alpha}} \int \left\{ \left( \frac{1}{c} \right)^{1/3} C_{N_{\alpha}} \int \left( \sqrt{\frac{1}{c}} \right)^{1/3} \right\}$  $\left(\frac{\Lambda_{cp}}{f}\right)$  $C_{\hat{N}_{\alpha}} \int C_{N_{\alpha}} \int C_{N_{\alpha}} \int \left( \frac{S_{f}}{A_{ref}} \right)$  $C_{\mathbf{w}} = C_{\mathbf{w}}$ 8-79

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$\underset{Ref}{\bigotimes}$			Suòson	ic and S	onic Compu	tation	
		R i	ng Tail – I	Force and	Moment Cho	aracteristics 💥	
l Mach No.	41 leading edge diameter (led)	42 chord length (cl)	43 ring te location	44 ^C <sub>Na</sub> , t	45 AC <sub>N</sub> art	46 X <sub>cprt</sub>	47 ΛC <sub>Mα τι</sub>
.5 1.0 1.5 2.0 2.5 3.5 4.5	led $\frac{d_{\rm fr}}{d_{\rm r}}$ , entry for Fig. 8-17	cl $\frac{c}{M_r}$ , entry for Fig. 8-17	location of ring trailing edge with respect to base of body	from Fig. 8-17, (assume constant below Mach No = 0.8); per deg; ref area $A_{rrf}$	$V_{v_{\alpha}}$ , 573 ( $V_{v_{\alpha}}$ ) per rad; refarea $A_{rrf}$	$X_{r_{P_{1}}}$ , $l_{n,r_{r_{r_{1}}}}$ , $l_{n,r_{r_{1}}}$ , $[l_{h_{1}}]$ 0.75 c measured from nose tip; assumes fin trailing edge is flush with body base. [] indicates term could or could not be in the equation, depending upon configuration being analyzed.	$V_{x_{q}}$ , $V_{1_{q}}$ , $V_{1_{q}}$ , $V_{1_{q}}$ , per rad; ref area $A_{ref}$ ; ref length = $l_{ref}$ ; with respect to node tip

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)			TABL	.E 8-1. C	OMPUTATIO	NAL TABLE (con	t)	
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								•
	1	48	49	50	51	52	53	54
	Mach No.	К <sub>f (b)</sub>	K <sub>b(f)</sub>	K,	C <sub>Na bady</sub>	$\begin{pmatrix} C_{N_{\alpha}} \\ f \end{pmatrix}$ IF*	C <sub>Na</sub>	C. <sub>Va total</sub>
	0 .5 1.0 1.5 2.0	1.32 1.32 1.32	.58 .58 .58	1.90 1.90 1.90	1.90 <sup>°</sup> 1.90 1.90	3.93 4.09 4.61	7.44 7.76 8.75	9.34 9.66 10.65
	2.5 3.5 4.5	from Fig. 8-18, invariant with Mach No.	from Fig. 8-18, invariant with Mach No.	k, Kj.h1- Kil),	from column 13 with incremental terms as applicable, per rad; ref area $\lambda_{r,f}$	interference-free fin from applicable column (29 or 37) (Note: Interference effects included in ring tail data) per rad; ref area A <sub>ref</sub>	$C_{N_{\alpha}} = \begin{pmatrix} \mathbf{s} & \mathbf{s} \\ K_{i} & C_{N_{\alpha}} & f \end{pmatrix}_{iF^{*}}$ per rad; ref area = $A_{ref}$	$C_{N_{\alpha}} = C_{N_{\alpha}} = C_{N_{\alpha}} + C_{N_{\alpha}} = per rad; ref area A_{r,f}$
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-	٦	TABLE 8-1. COMPU	TATIONAL TABLE	(cont)		
i i i i i i i i i i i i i i i i i i i		Subson	c and Sonic Comp	utation		
	E Comp	lete Configuratio	on - Force and Mo	oment Cheracter	istics	
1	55	56	57	58	59	
Much No.	C. <sub>Vα</sub> /.	$\begin{pmatrix} C_{y_{\alpha}} \end{pmatrix} = K$	C <sub>Ma</sub>	Cyja total	$\left(\frac{\dot{\lambda}_{e_{\mu}}}{l_{ref}}\right)_{total}$	
C .5 1.0 . 1.5	5.06 5.06 5.06	43.4 45.1 50.9	82.5 85.6 96.5	87.56 90.66 101.56	9.38 9.38 9.52	
2.5 3.5 4.5	ith incremental terms as applicable, Ard; ref length lrd; with respect	fin from applicable column (31 or rence effects included in ring : ref area $\lambda_{ref}$ ; ref length $l_{ref}$ ; se tip	per rad; ref <i>erea</i> <sup>1</sup> <sub>rr/</sub> ; ref length <i>l</i> <sub>rrf</sub> ; with respect to nose tip	(f) per rad; ref area $A_{r,f}$ ; $\alpha^{f}$ ref length $l_{r,f}$ ; with respect to nose tip	; measured from nose tip	
*Intonform	from column 20 wi from to una 20 wi per rad: ref arca to nose tip	interference-free 40) (Note: Interfer tail data); per rad; with respect to nos	$C_{\mu_{\alpha_{f}}} \stackrel{(s)}{=} h_{i} \stackrel{(s)}{\left( C_{\mu_{\alpha_{f}}} \right)_{IF}}.$	C <sub>K</sub> total = C <sub>K</sub>	$\left(\frac{X_{cp}}{l^{ref}}\right)_{total} \qquad \frac{C_{M_{\alpha} total}}{C_{N_{\alpha} totat}}$	
I-12	ince free		<u> </u>	1	<u> </u>	1
8-82	15.256-150 <sub>0-1</sub> 000-10-00-00-00-00-00-00-00-00-00-00-00-				nist vanamining visionaa	

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				in Su	person ic	uuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuuu	s ///		
S Data S				111111111 odv. z. For	IIIIIIII ce. and M	IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII	TIIIIII aristics		
*****		<b></b>	<u>   ī</u>				шищ	111	
			:						
1	60	61	62.	63	64	65	66	67	68
Mach	ß	$l_n$	$l_{ab}$	βd	l <sub>ab</sub>	C <sub>N</sub>	$\left(X_{ep}\right)$	X <sub>cP (b</sub>	C,
No.		त	d	in	$\overline{\beta d}$	CC jb	$\left(\frac{1}{l_n}\right)_{l_n}$		°α fb
0							,,		
.5	•								
1.5	1.12	4.0	7.76	0.280	6.94	2.6	.53	31.8	5.51
2.0	2.29	4.0	7.76	0.434	4.49 3.39	3.0 3.15	.68 .72	41.1 43.2	8.22 9.07
3.5	3.36	4.0	7.76	0.841	2.31	3.25	.83	49.8	10.78
	1.57		1.10	1.10	****	5.65	.00	52.9	11.40
								2	
								Sr Sr	: .
							~	tip. -7 fé	A.,
						der alsc fig-	der	ose d 8- ttion	e tij
	-		4		-	ylin iee con '''f	ylin	n no o an gura	far  'j nose
			engt	~ ~	2	e c fic	c c	froi 8-( nfiș	; re th
		ıgth	ly le	- 20 - 50	00 50	ogiv der) peci are	ogiv der)	red gs. c cc	rad leng oect
		leı	1200	Fi	н Ц	ent- rline rsl	ent-	asuı o Fi cifi	per ref resl
		osou	ufter	v in	y in	angc e-cy 7 fo 1; r(	ange e-cy	me; als spe	
	. 2	al 1	al a	entr	entr	2 (ta cone 1 8- rae	3 (t; cone	r	X cr / 1 rr
	um .	sion	sior	or	0 L	8-8-4 ( -4 ( and Per	-8-	1 11	) 'il x
	colu	nen	nen	le f	le f	Fig. 1. 8. 8-6 n.	Fig.	$\left(\frac{X_{rp}}{l_n}\right)$	لى خ
	uo	ndir	ndir	riab	riab	5m ] Fig gs. atio	bm ] Fig	÷	£
	fre	ou	ou	va	¢ a	frc or Fig urá	frc or	X.p	۳ رو
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Ref Data			i Bo	attail	Supersonic	Computation	acteri	stics /	
1 Mach	69	70 d.	71 d	72	73 C		75 X	76 J	77
No.	.91	- ot	~c	$\frac{d_c}{d_c}\beta$	$\frac{d_{bt}}{1 - \left(\frac{d_{bt}}{d_c}\right)^2}$	ar br	l <sub>bt</sub>		
1.0 1.5 2.0 2.5 3.5 4.5						,, ,  			   
	<b>X</b> <b>X</b> <b>X</b> <b>X</b> <b>X</b> <b>X</b>		er of boattail)			r rad; ref are rea A <sub>ref</sub>		ured from tip	ef
		boattail	large diamet	Fig. 8-8		$1 - \left(\frac{d_{b_i}}{d_c}\right)^2 \right], pe^{\frac{1}{a_i}}$		$\left(\frac{p}{t}\right) l_{bt}$ , meas	$\frac{b_{t}}{f} \begin{array}{c} \text{per rad; } r\\ \text{area} = A_{ref}\\ \text{length} - l_{r}\\ \text{spect to n} \end{array}$
	sngth of boattail	mall diameter of l	ylinder diametèr (	bscissa entry for	-om Fig. 8-8	$\begin{bmatrix} C_{N_{\alpha}} & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ &$	om Fig. 8-9	$cp_{bc} = l_n + l_{ab} + \left(\frac{l_c}{l_b}\right)$	$u_{\alpha} = (NC_{N_{\alpha}}) u_{\alpha} \left( \frac{\lambda_{ep}}{l_{rc}} \right)$

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AMCP 706-280 COMPUTATIONAL TABLE (cont) TABLE 8-1. ainanna tanitatiin meetta ta Supersonic Computations Ref Data Allaalaa Geestees - Force and Moment Characteristics Flare 79 81 82 83 84 78 80 1  $\Delta C'_{N_{\alpha fl}}$ ∆C<sub>µ<sub>α fl</sub></sub> ∆C<sub>N<sub>cc</sub> fl</sub> X<sub>cp<sub>fl</sub></sub> Mach No. dfl θ d<sub>c</sub> 0 . 5 1.0 1.5 2.0 2.5 3.5 4.5  $\chi_{cp_{fl}} = l_{n} + l_{ab} + 0.6 l_{fl}$ , measured from nose tip per rad; ref area =  $h_{ref}$ ; per rad; ref area =  $A_{ref}$ ;  $S_{fl} = \frac{\pi d_{fl}^2}{4}$ from column 71 (minimum diameter of flare) ref length =  $l_{ref}$ ; with from Fig. 8-10 at appropriate Mach number flare diameter (maximum diameter of flare) respect to nose tip 8-24 Fig.  $\Delta G_{\mathbf{X}_{\mathbf{\alpha}}} \int_{I} = (\Delta G_{\mathbf{N}_{\mathbf{\alpha}}}) \int_{I} \left( \frac{A_{cp} f_{I}}{I} \right)$ seč  $\Delta C'_{N_{\alpha} fl} = (\Delta C_{N_{\alpha}})_{fl} \left( \frac{S_{fl}}{A_{ref}} \right)$ flare half angle,

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	Ref &		Super	rsonic Co	mputations }		
		Total	Body	Fin -	Force and M	oment Chara	cteristics
 .,	r K	85	86	87	88	89	90
,	Nach No.	C <sub>Nacb</sub>	C <sub>Nacb</sub>	λ	tan A <sub>le</sub>	$\frac{\beta}{\tan \Lambda_{\rm b}}$	$\frac{\tan \Lambda_{le}}{Q}$
•	0 .5 1.0 1.5 2.0 2.5 3.5 4.5	2.6 3.0 3.15 3.25 3.25	5.51 8.22 9.07 10.78 11.45	0 0 0 0 0	1.732 1.732 1.732 1.732 1.732 1.732	. 646 1. 00	B 1.00 .756 .516 .395
		$C_{N_{\alpha} \cdot l_{r}} = C_{N_{\alpha} - l_{r}} \left( \begin{array}{c} (\mathbf{x}) \\ \mathbf{x}_{\alpha} & \mathbf{y}_{r} \\ \mathbf{x}_{\alpha} & \mathbf{y}_{r} \\ \mathbf{y}_{\alpha} & \mathbf{y}_{r} \\ \mathbf{y}_{\alpha} & \mathbf{y}_{r} \\ \mathbf{y}_{\alpha} & \mathbf{y}_{r} \\ \mathbf{y}_{r \neq f} \\ \mathbf{y}$	$C_{\mathbf{M}_{\mathbf{\alpha}}}$ $L_{\mathbf{M}_{\mathbf{\alpha}}}$ $L_{\mathbf{M}_{\mathbf$	taper ratio (from fin geometry (see Fig. 8-23)	tangent of leading edge sweep angle	abscissa entry for Fig. 8-13	abscissa entry for Fig. 8-13

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#### TABLE 8-1. COMPUTATIONAL TABLE (cont) Supersonic Computations Ref Data Fin - Force and Moment Characceristics 98 91 92 o'r 93 94 95 96 97 1 βC<sub>Nα</sub> $\tan \Lambda_{le} C_{N_{\alpha}}$ C<sub>Na f</sub> AR tan $\Lambda_{le}$ ß ΔΥ $\Delta Y_{\perp}$ δ<sub>⊥</sub> Mach No. $tan \Lambda_{le}$ 0 .5 1.0 1.5 2.0 2.74 . 797 .112 ≈0 .646 4.0 4.75 2.31 . 097 .112 1.0 4.0 4.0 ≈0 4.0 2.5 3.5 4.5 1.75 4.0 .112 4.0 .097 ≈0 .112 1.19 .097 4.0 4.0 ≈0 .097 4.0 0.913 .112 4.0 ≈0 surface coordinates at 15 and $\Delta Y = Y_{.15c} - Y_{0.06c}$ , difference between upper fin per rad; ref area = planform area, S 6 percent chord stations $C_{N_{\alpha} f} = (t \text{ an } \Lambda_{te} C_{N_{\alpha}}) \left(\frac{1}{t \text{ an } \Lambda_{te}}\right) \text{ or } = \beta C_{N_{\alpha}} \left(\frac{1}{\beta}\right)$ in deg; for wedge leading edge only. from Fig. 8-13, for tan $\Lambda_{le}/\beta$ entry, at appropriate taper ratio ( $\lambda$ ) from Fig. 8-13, for $\beta/tcn \Lambda_{le}$ entry, at variable for entry, Fig. 8-13 appropriate taper ratio ( $\lambda$ ) Note: 8-15 abscissa for Fig. $\delta_{\perp} = Tan^{-t} \frac{\Delta Y_{\perp}}{5.85}$ $\Delta Y$ cos $\Lambda_{le}$ T∕∆

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Ref		IABLE +1, GUMPUTATIONAL JABLE (CONT)       Supersonic Computations       Fin - Force and Moment Characteristics								
1 Mach No.	99 tan Λ <sub>le</sub> β	100 C <sub>N</sub> ac f ( <sup>C</sup> Nac f) theory	101 <sup>C</sup> Na f	$\frac{102}{\frac{X_{cp}}{C_{r_f}}}$	103 X <sub>cp f</sub>	104 <sup>C</sup> M <sub>a f</sub>				
.5 1.0 1.5 2.0 2.5 3.5 4.5	1.0 .756 .716 .395	1.0 1.0 1.0 1.0 1.0	4.21 3.55 2.69 1.83 1.402	0.68 0.68 0.68 0.68 0.68 0.68	169.4 169.4 169.4 169.4 169.4 169.4	47.5 40.1 30.4 20.6 15.85				
	abscissa for Fig. 8-15	from Fig. 8-15	$C_{N_{\alpha} fin} = \left(\frac{C_{N_{\alpha} f}}{C_{N_{\alpha}} \text{ theory}}\right) (C_{N_{\alpha}} \text{ theory}) (S_{f}/A_{ref})$ NOTE: $C_{N_{\alpha}} \text{ theory}$ from column 94; per rad; ref area = $A_{ref}$	from Fig. 8-14, at appropriate taper ratio (λ)	$X_{cp_{f}} = l_{n} + l_{sb} + [l_{bt}] - \left[ I - \left( \frac{X_{cp}}{C_{r}} \right)_{f} \right]$ measured from nose tip; assume fin trailing edge is flush with body base. [] indicates term could or could not be in the equation, depending upon configura- tion being analyzed.	$C_{\mathbf{y}_{\alpha}\ f} = C_{\mathbf{y}_{\alpha}\ f} \left( \frac{\lambda_{cp_f}}{l_{ref}} \right)$ per rad; ref area = $A_{ref}$ ; ref length = $i_{ref}$ ; with respect to nose tip				

	TAB	LE 8-1. COMP	UTATIONAL T	NBLE (cont)	
		Super	sonic Comput	ations )))	
Data	Recta	ngular Fin - 1	Force and Mo	ment Charac	teristics
××××××××					
1	105 106	107	108	109	110
Mach No.	$\frac{1}{\beta AR}$ $\beta C_{N_{\alpha}}$	C <sub>Naf</sub>	C' <sub>Naf</sub>	$\frac{X_{cp}}{c}$	X <sub>cp</sub> f
.5 1.0 1.5 2.0 2.5 3.5 4.5	variable for abscissa entry, Fig. 8-16 (Note: β4R≥ 0.5 for data to apply) from Fig. 8-16	$C_{N_{\alpha} f} = (\beta C_{N_{\alpha}}) \frac{1}{\beta}$ , per rad; ref area = $S_{f}$	$C'_{\mathbf{x}_{\mathbf{x}_{f}}} = \left(C_{\mathbf{x}_{\mathbf{x}_{f}}}\right) \left(\frac{S_{f}}{A_{ref}}\right)$ per rad; ref area = $A_{ref}$	from Fig. 8-16, (Note: c = chord length)	$X_{cp_f} = l_n + l_{sb} + \left[ l_{bt} \right] - \left( 1 - \frac{l_{cp}}{c} \right) c$ measured from nose tip; assumes fin trailing edge is flush with body base. [] indicates term could or could not be in the equation, depending upon configuration being analyzed

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TABLE S-1. COMPUTATIONAL TABLE (cont)

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TABLE 8-1. COMPUTATIONAL TABLE (cont)

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TABLE 8-1. COMPUTATIONAL TABLE (cont)

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TABLE 8-1. COMPUTATIONAL TABLE (cont)

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Ref Data				Supersonic Supersonic IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII	Computations		
l Mach No.	119 d/b	120	121 βcot Λ <sub>le</sub>	122 <u>Bd*</u> <sup>C</sup> re	123 H <sub>1</sub> *	124 K <sub>b(f)</sub>	125 K,
.5 1.0 1.5 2.0 2.5 3.5 4.5	tio of body diameter to fin span	cm Fig. 8-18	rametric variable for Fig. 8-20	scissa variable for Fig. 8-20	= $K_{b(f)} \beta \left( C_{\mathbf{w}} \int_{\mathbf{z}} (\lambda_{\mathbf{z}} + 1) \left( \frac{b}{d} - 1 \right) \right)$ Note: If afterbody extends beyond fin <i>te</i> use Fig. 8-20(A). If body base plane and fin <i>te</i> are flush use Fig. 8-20(B).	$D = H_{1}\left[\frac{1}{\beta\left(C_{N_{\alpha}}\right)}\left(\Lambda_{c} + 1\right)\left(\frac{1}{d} - 1\right)\right]$	$= K_{f(b)} + K_{b(f)}$

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Supersonic Computations Ref Data Interference Effects (Method 2) = . 129 1 126 127 128 K<sub>t</sub> Mach d/b a<sub>t</sub>/m  $a_t$ No. 0 .5 1.0 1.5 .646 .375 1.0 1.82 2.0 1.74 1.000 1.0 .375 . 375 2.5 1.322 1.0 1.68 3.5 4.5 .375 1.940 2.530 1.0 1.59 1.55 1.0 .375 variable describing fin geometry (governs choice of Figs. 8-21(A) through 8-21(F),  $a_t = \beta tan\omega$ ; parametric variable for Fig. 8-21 abscissa entry for Fig. 8-21 where  $\mathbf{m} = \beta tanc$ from Fig. 8-21.

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TABLE 8-1. COMPUTATIONAL TABLE (cont)

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Ref &			personic Compute	itions	
	Com	plete Configurati	ion - Force and	Moment Characte	ristics
			1		
1	130	131	132	133	134
Mach No.	C <sub>N</sub> ac <sup>°</sup> body	$\left(C_{N_{\alpha}}\right)_{IF}$ .	C <sub>Naf</sub>	C <sub>N</sub> a total	C <sub>Mab</sub>
۳ ۲0				×	
1.0					
1.5	2.6	4.21	7.66	10.26	5.51
2.0	3.0	3.55	6,18	9.18	8.22
2.5 3.5	3.25	1,83	2, 91	6,16	10.78
4.5	3.25	1.402	2.18	5.43	11.45
	om column d5 with incremental terms s applicable; per rad; ref area =A <sub>ref</sub>	iterference-free fin from applicable column 01 or 108 or 116) (Note: interference effec icluded in ring tail data.) Per rad; ref rea = $A_{ref}$	$\alpha_{f} = K_{t} \begin{pmatrix} (\mathbf{j}) \\ C_{N} \\ \alpha_{f} \end{pmatrix}_{JF}$ . Note: $K_{t}$ from column 12! or 129 as applicab per rad; ref area = $A_{ref}$	$o_{\text{total}} = C_{N_{\alpha}} \frac{(1)}{b_{\alpha j}} + C_{N_{\alpha}} \frac{(1)}{b_{\alpha j}} \text{ per rad;}$	om column 86 with incremental terms as pplicable; per rad; ref area = $A_{ref}$ ; ref ngth = $l_{ref}$ ; with respect to nose tip
			5	0	

COMPUTATIONAL TADLE **\*** 2 . 2'

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### Ì **COMPUTATIONAL TABLE (cont)** TABLE 8-1. Supersonic Computations Ref Data Complete Configuration 1 135 138 136 137 C<sub>Maf</sub> $\begin{pmatrix} C_{\mathcal{M}_{\alpha}} \\ \end{pmatrix}_{IF}$ . Cy a total $\left(\frac{X_{cp}}{l_{ref}}\right)_{total}$ Mach No. 0 , 5 1.0 1.5 47.5 86.5 92.01 8.97 40.1 69.8 78.02 8.50 2.0 2.5 30.4 51.1 60.17 7.85 3.5 20.6 32.8 43.58 7.07 15.9 4.5 24.6 36.05 6.65 tip (104, 111 or 118) (Note: interference effects interference free fin from applicable column measured from nose tip with respect to nose tip area = $A_{ref}$ ; ref lergth = $l_{ref}$ ; with respect to nose tip with respect to nose included in ring tail data); per rad; ref ref length = l<sub>ref</sub>; $= C_{w} + C_{v} + C_{v} + C_{ref}$ ref length = l<sub>ref</sub>; ref area = A<sub>ref</sub>; per rad; per rad; ۲ (Cwa) total (<sup>U</sup>Na) rotal $= K_t \left( C_{M_{\alpha}} \int_{J} J_{J} F \cdot \right)$ 8 6 3 3 total C⊮ Ar total $\frac{X_{cp}}{l_{rej}}$ \* Interference Free 8-95

*		TABLE 5-2.			UN SHEE		
-	>		General	Data			
	, , , , , , , , , , , , , , , , , , ,						
	- -						
1	2	3	4 ·	5	6	7	8
Mech No. M.	β	Altitude, Ft	Reference Area (A <sub>ref</sub> ), Ft <sup>2</sup>	Reynolds No. Per Ft × 10 <sup>-6</sup> of Length	V∞ Ft/Sec		$\frac{P_{\star} \times 10^{-3}}{Lb/Ft^2}$
0	1.0	, 0	1.225	0	0	2.378	2.116
.49	.871	75 171	1.225	3.46	546 834	2.372	2.110
.88	. 474	234	1.225	6.21	982	2.362	2.098
1.02	. 200	308	1,225	7.16	1134	2.357	2.093
1.30	. 835	487	1.225	9.08	1445	2.344	2.020
1.59	1.24	711	1.225	11.06	1769	2.329	2.062
1.90	1.61	981	1.225	13.12	2285	2.310	2.042
eđ		corresponding	ed (usually cross sectional adrical section, $\frac{\pi d_c^2}{4}$ )	iunction of column	-	ity (0.002378 sług/ft <sup>3</sup> )	pressure level, std.)
arbitrarily select	$B = \sqrt{\frac{3}{2}} + \frac{1}{6} H_{\infty} > 0$ $B = \sqrt{1 - H_{\infty}^2} H_{\infty} < 0$	flight altitude at Mach number	arbitrarily select area of body cylii	from Fig. 8-40 ( () and ())	rocket velocity	atmospheric dens at sea level, std.	free stream total (2116 lb/ft <sup>2</sup> at sea
arbit	8 8 8 8 8	flight Mach	arbit area	from Gan	rocke	atmo.	free (2116

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TABLE 8-2. DRAG FORCE CALCULATION SHEET (cont)

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	Mech No. M <sub>∞</sub> 0 .75 .88 1.02 1.15 1.30 1.59 1.90 2.05	Data X
nose fineness ratio = $f_n = \frac{l_n}{d_r}$	$f_n$ 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0 4.0	9
ratio of body surface wetted area to reference area	$ \frac{S_{a}}{A_{ref}} $ 39.0 39.0 39.0 39.0 39.0 39.0 39.0 39.0	10
ratio of body cylinder diameter to base diameter (flares or boattails)	$\frac{d_{c}}{d_{B}}$ 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0	11
$(V/a^*)_j = \sqrt{\frac{\gamma_j + 1}{2}} M_j^2 \left[ 1 + \left(\frac{\gamma_j - 1}{2}\right) M_j^2 \right]^{-1}$ (subscript j refers to rocket je	$\left(\frac{V}{a^*}\right)_j$ 2.36 2.36 2.36 2.36 2.36 2.36 2.36 2.36	12
thrust coefficient = $C_F = \frac{Roc}{Rocket jet chamber}$	et thrust rr pressure x jet throat area	13
ratio of boattail length to cylinder diameter	$\frac{l_{bt}}{d_c}$ 0 0 0 0 0 0 0 0 0 0 0	14
ratio of base area less jet area to reference area	$\frac{S_B - S_j}{A_{rej}}$ . 359 . 359	15

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Ref Data			Fin Geometr		
1 Mach No. M <sub>∞</sub> 0 .49 .75 .88 1.02 1.15 1.30 1.59 1.90 2.05	16 <i>b</i> <i>Ft</i> 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08 2.08	17 $S_f Ft^2$ 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882 1.882	18 <i>AR</i> 2. 31 2. 31	19 tan $\Lambda_{1/2}$ . 866 . 866	20 t Ft .18 .18 .18 .18 .18 .18 .18 .18
	fin span (see Fig. 8-23)	fin area (see Fig. 8-23)	Aspect Ratio $AR = b^{2/S_f}$	tangent of fin mid-chord sweep angle	fin thickness (see Fig. 8-23)

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Ref Data			Fin Geo	ometry		[
1 Mach No. M <sub>∞</sub> 0 .49 .75 .88 1.02 1.15 1.30 1.59 1.90 2.05	21 c Ft 1.8 1.8 1.8 1.8 1.8 1.8 1.8 1.8	22 t/c .1 .1 .1 .1 .1 .1 .1 .1 .1	$   \begin{array}{r}     23 \\     \underline{h_{fin \ base}} \\     \hline     c \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\     .1 \\ $	$ \begin{array}{c} 24 \\ S_{\bullet} \\ \overline{A_{ref}} \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.14 \\ 6.1$	$25 \frac{S_{fin \ base}}{A_{ref}}$ . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306 . 306	26 d <sub>rt</sub> Ft 0 0 0 0 0 0 0 0 0 0 0
	fin chord length	fin thickness to chord ratio	fin base thickness to chord ratio	ratio of fin wetted area to reference area	ratio of fin base area to reference area	diameter of ring tail

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1 Mach No. M. 0 .49 .75 .88 1.02 1.15	$27 \\ \frac{l_n}{d_c} \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0 \\ 4.0$	28 $\left(\frac{\beta}{J_n}\right)^2$ . 063 . 048 . 027 . 014 . 003	29 (Bf <sub>n</sub> ) <sup>2</sup> 16 12.2 7.04 3.62 .64	30 C <sub>D nose</sub> 0 0 0 . 0025 . 0469	31 C <sub>D<sub>2</sub> br 0 0 0 0 0</sub>	32 Reynolds Number × 10 <sup>.6</sup> 0 50.9 77.6 91.2 105.2	33 S. Ft <sup>2</sup> 39.0 39.0 39.0 39.0 39.0 39.0	34 <i>C<sub>f</sub></i> . 0022 . 00204 . 00195 . 00186
1.30 1.59 1.90 2.05	from column (), abscissa entry for Fig. 8-26	column () / column () <sup>2</sup> , abscissa entry for Fig. 8-27	abscissa entry for Fig. 8-28	from Fig. 8-26 (general nose shapes); Fig. 8-27 (optimum secant ogive), Fig. 8-28 (slender ogives), ref area $A_{r,f}$	extrapolate supersonic data using Fig. 8-32 as a guide; rcf arca - A <sub>ref</sub>	Reynolds number based on total rocket length (column (5) $\times l_T$ ) (abscissa entry for Fig. 8-39)	ratio of wetted area of rocket surface to reference area i.e., cylindrical section would be $nd_c l_c$ , column (1)	from Fig. 8-39, refarea S <sub>wr</sub>

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Ref		Subsonic	Computations	
Data		Body I	Drag Force	
1	35	36	37	38
Mach No. M <sub>∞</sub>	C <sub>Df</sub>	C <sub>DB cyl</sub> (Jet Off)	C <sub>DB cyl</sub> (Jet Un)	P <sub>B</sub> /P
0 .49	.0986	. 131	. 128	. 94
.75	.0915	. 135	.100	. 89
.88 1.02	.0874	.145	.099	.85
1.30 1.59 1.90 2.05		ea Arcf	ig. 8-44 (as 1 of column area - A <sub>ref</sub>	
	= Aref	i ref aı	rom F unction 3) ref	
	farea	8-41;		
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### TABLE 8-2. DRAG FORCE CALCULATION SHEET (cont) Subsonic Computations Ref Data Fin Drag Force 46 43 44 45 1 $\frac{C_{F_{a}}}{(t/c)^{5/3}}$ C<sub>D</sub>, $AR\left(\frac{t}{c}\right)^{1/3}$ Mach M2 - 1 No. $\frac{1}{(t/c)^{2/3}}$ M<sub>c</sub> -4.63 0 1.08 0 0 0 1.08 -3.51 .49 .75 1.08 -2.02 0 0 .88 1.08 -1.04 .55 .023 .0949 1,08 .185 2.35 1.02 1.15 1.30 1.59 1.90 2.05 from Fig. 8-36 (rectangular fin) from Fig. 8-37 (delta fin) (fcr other planforms interpolate between above) variable for Fig. 8-36 or 8-37 = (1) $\times \left[ (2) \right]^{1/3}$ **(1)** 2/3 M2 - 1 8-36 or 8-37, $\left| \begin{pmatrix} t \\ - c \end{pmatrix}^{5/3} \quad \left\langle \frac{2S_f}{A_{ref}} \right\rangle$ Arry variable for Fig. [(1/c)<sub>2/1</sub>] ref area = $S_f$ rcf area أحى ئى ئى 8-103

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TABLE 8-2. DRAG FORCE CALCULATION SHEET (cont)

Ref Data X	Supersonic Computations Body Drag Force							
.75 .88 1.02 1.15 1.30 1.59 1.90 2.05	.0669 .0705 .0590 .0581 .0546			.216 .206 .179 .154 .142	.271 .212- .142 .099 .085			
	from Fig. 8-25 or 8-29	from Fig. 8-30 (conical) or 8-31 (parabolic). Note that ordinate is $\& C_{p_{e}} (l_{bt}/dc)^{2}$ so that $C_{p_{e}} = (ord tnate value) / [i (l_{bt}/d_{c})^{2}];$ ref area = $A_{ref}$	from Fig. 8-33 at appropriate Mach number, ref area = A <sub>ref</sub>	$C_{b_B} = -C_{p_B}$ , $C_{p_B}$ from Fig. 8-41 ref area = $A_{ref}$	$C_{B_{B}} = \frac{1 - P_{B}/P_{\infty}}{(\gamma/2) M_{\infty}^{2}} \left( \frac{S_{B} - S_{j}}{A_{rej}} \right); \frac{P_{B}}{P_{\infty}} - \frac{\frac{3}{5} C_{r}^{1/3}}{(\gamma/a^{*})_{j}}$ or Fig. 8-42; ref area = $A_{rej}$ (2)			

AMCP 706-260 Ŀ TABLE 8-2. DRAG FORCE GALCULATION SHEET (cont) Supersonic Computations Ref Data Body Drag Force 63 64 60 61 62 1  $\begin{pmatrix} C_{B_{body}} \end{pmatrix}_{total}$ Jet Off/Jet On C<sub>D<sub>f</sub> b</sub> C<sub>DB fl or bt</sub> (Jet Off) C<sub>D</sub> B fl or be (Jet On) Mach  $C_{f_b}$ No. M<sub>∞</sub> 0 .49 . 75 . 88 1.02 1.15 .00182 .0815 .3644/.4194 .0770 1.30 .00172 .3535/.3595 1.59 .0739 .00165 .3119/.2749 1.90 .00150 .0672 .2793/.2243 8-43 .0654 .00146 2.05 .2620/.2050 rom Fig. indicates term could or could not be in the equation, depending upon configuration being ç  $P_{B_{cyl}}$ í P<sub>Bbr</sub> from Fig. 8-39 with Reynolds Number A ref  $\frac{3}{5} C_F^{-1/3}$ 6  $C_B$  from Fig 8-41; ref area =  $A_{ref}$ C<sub>D</sub> be or fi  $(V/a^{*})$ S or  $C_{D_f} = 1.15 (C_f) \left(\frac{\partial_x}{A_{ref}}\right)$ ; refarea = (i) or (i) or (i) or (i)  $C_{D_B}$  refarea  $-A_{re}$ . based on body length or  $(5) \times l_T$ م. ا م × Cof + | 5. A ref If or Abr = C<sub>D</sub> nose S ref area = A<sub>rej</sub> Aref  $(1 - P_B/P_\infty)$ 8  $(y/2 M_{\infty}^{2})$ ы С  $c_{D_B} = - c_{P_B}$ ref area analyzeá. 11 رم<sup>ھ</sup> YAR JI 8-107

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	Supersonic Computations								
Data 💥	W Fin Dray Force W								
1	65	66	67	68	69				
. Mach No.	BAR	AR tan A <sub>1/2</sub>		C <sub>D</sub>	C <sub>D</sub> w rt				
<i>M</i> ∞			$AR\left(\frac{t}{c}\right)^{2}$						
.49	i								
.75									
1.02									
1.15	1.305 1.93	2.00	1.61	. 1205					
1.59	2.87	2.00	1.50	. 1122					
1.90 2.05	3.72 4.14	2.00	1.25	. 0935					
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TABLE #2. DRAG FORGE CALCULATION SHEE

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