

UNCLASSIFIED

AD NUMBER

AD840382

LIMITATION CHANGES

TO:

Approved for public release; distribution is unlimited.

FROM:

Distribution authorized to U.S. Gov't. agencies only; Administrative/Operational Use; 31 JUL 1967. Other requests shall be referred to Defense Atomic Support Agency, Washington, DC 20305.

AUTHORITY

DASA ltr 19 Apr 1971

THIS PAGE IS UNCLASSIFIED

L

AD640382

1964-1965

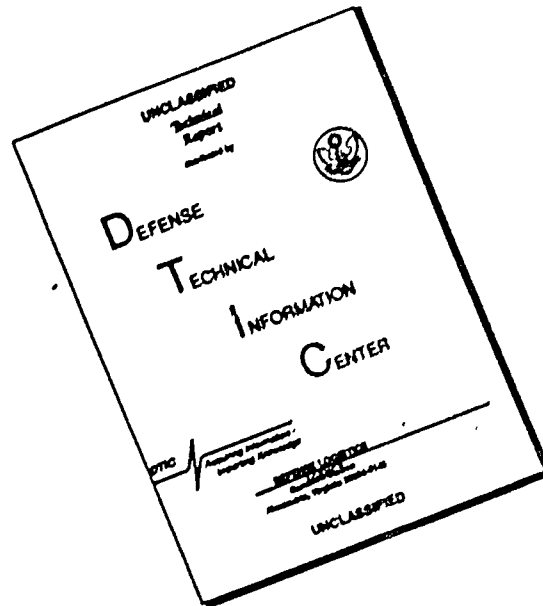
Final Report

THE ENERGY PERFORMANCE OF THE
SPECTRA CALCULATOR

Vol. III: Program Description

UNION CARBIDE CORPORATION

DISCLAIMER NOTICE



THIS DOCUMENT IS BEST QUALITY AVAILABLE. THE COPY FURNISHED TO DTIC CONTAINED A SIGNIFICANT NUMBER OF PAGES WHICH DO NOT REPRODUCE LEGIBLY.

UNION CARBIDE CORPORATION
DEFENSE AND SPACE SYSTEMS DEPARTMENT

UCC/DSSD - 299

Final Report

LOW ENERGY PHOTOELECTRIC CROSS
SECTION CALCULATIONS

Vol. II: Program Description

A. Glick and H. Brysk

July 31, 1967

OCT 8 1968

Work Performed under Contract No. DA-49-146-XZ-511

Each transmittal of this document outside
the agencies of the U.S. Government must
have prior approval of the Director, Defense
Atomic Support Agency, Washington, D.C. 20305.

Space Sciences and Engineering Laboratory
5 New Street
White Plains, New York 10601

107

FOREWORD

This report was prepared by the Union Carbide Corporation, Defense and Space Systems Department, White Plains, New York, under Contract DA-49-146-XZ-511, Project 5710, funded by the Defense Atomic Support Agency (DASA). Inclusive dates of research were 1 June 1966 to 30 June 1967. The report was submitted 31 August 1967 by the AFWL Technical Monitor, Captain Guy Spitale (WLRP).

The report has been divided into two volumes for convenience. Volume I presents the theoretical analysis and the discussion of results. Volume II is a detailed description of the program.

The project was initiated and formulated by Dr. C. D. Zerby. The theoretical derivation was completed by Dr. H. Brysk, who also planned and analyzed the calculations. Programming support was supplied by Mr. A. Glick in writing the program and by Mr. E. C. Imperatore in resolving the systems problems of transcribing the tapes containing the Los Alamos Scientific Laboratory (LASL) self-consistent-field data to the UCC and the AFWL operating systems. The program is written in FORTRAN IV and is operational on the CDC 6600 computer at AFWL. We thank Dr. J. T. Waber (of LASL) who supplied us the output of his self-consistent-field program on tape.

This report has been reviewed and is approved.

ABSTRACT

A computer program was developed for the calculation of photoelectric cross sections, including angular distributions, using as input the results of a relativistic Dirac-Slater self-consistent-field program. The program was used to calculate the aluminum cross sections over the range from 1 to 150 keV and uranium cross sections at four energies within that range, and the results were correlated with pre-existent experimental and theoretical data.

Volume I presents the theoretical analysis and the discussion of results. Volume II is a detailed description of the program.

This page is intentionally left blank.

TABLE OF CONTENTS

	<u>Page No.</u>
I. INTRODUCTION	1
II. OPERATING INSTRUCTIONS	3
III. SAMPLE OUTPUT	7
IV. THE PROGRAM	15
PELEC	21
ANGLE	35
CØEFS	39
DERIV	47
FILL	51
HUM	57
INTERP	63
LEGEND	67
LØGGAM	73
MUSS	77
RADINT	81
RKUT	91
SINDEX	95
SPHBES	99
WNØRM	103
XDERIV	107
XRKUT	111

I. INTRODUCTION

This volume is a self-contained description of a program (PELEC) for the computation of photoelectric cross sections. The companion volume (UCC/DSSD - 299, Volume I) develops the theory used and discusses the results obtained with the program.

Chapter II contains the operating instructions. It describes the input cards and self-consistent-field data tape required. The utilization of a test option to ascertain the optimum input parameters in a series of runs is indicated.

Chapter III presents sample output.

Chapter IV exhibits the program itself. For each routine, its purpose and the method of achieving it are stated. The routines it calls and those it is called by are given, as well as the Common blocks it uses and the calling sequence (if any). The variables are defined. A schematic flow chart is provided. Finally, the routine is listed.

This page is intentionally left blank.

II. OPERATING INSTRUCTIONS

This chapter gives all the operational details needed in order to run the photoelectric program. The input variables and format are listed, along with the program diagnostics. Tape unit assignments are given and the test option is described.

Input Variables

A complete set of data consists of a single data card. The variables described below are read in on a format (9I5, 2E15.8):

5	10	15	20	25	30	35	40	45	60	75
JM	KMAX	LM	NTAPE	NEDGE	IA	IB	IZ	Loop	QV	SAVE

Upon completion of a problem, the program recycles, reading in the next data card. Termination of the program is obtained by setting the flag value NEDGE = -1.

Name	Dimensions	Mode	Meaning
JM		I	Maximum order of Legendre coefficient
KMAX		I	Maximum κ for electron
LM		I	Maximum l for photon
NTAPE		I	The logical tape unit assigned for tape containing the self-consistent-field data
NEDGE		I	= -1: terminates Program = 0: normal run > 0: sets photon energy to NEDGE th binding energy
IA		I	= 0: normal case > 0: calculation commences after IA shells
IB		I	= 0: calculation to include outermost shell > 0: calculation cuts off after IB shells
IZ		I	Atomic number
Loop		I	= 0: normal case = 1: photon angular momentum reduction
QV		R	Photon energy in keV
SAVE		R	Total cross section accumulation from previous run; = 0 ordinarily.

Input Testing

The program sifts the input data to insure that certain criteria are not violated. If any difficulty is observed, a violation signal is printed and the run terminated. Listed below in abbreviated form are the criteria that must be satisfied and that the program tests for:

$$\text{MIN (JM, KMAX, IM, IA, IB)} \geq 0$$

$$2 < \text{IZ} < 102$$

$$\text{QV} > 0$$

$$\text{LOOP} = 0 \text{ or } 1$$

$$\text{NEDGE} \leq \text{JX}$$

$$\text{IA} < \text{JX}$$

$$\text{IB} \leq \text{JX}$$

$$\text{NK, NKP} \leq 200$$

In addition to the above the program examines the following variables and alters them if necessary:

$\text{JM} > 24$, program sets $\text{JM} = 24$, prints this fact and proceeds.

$\text{KMAX} > 12$, program sets $\text{KMAX} = 12$, prints this fact and proceeds.

$\text{LM} > 12$, program sets $\text{LM} = 12$, prints this fact and proceeds.

This is to insure that the dimension size of the variable of the program as written for the IBM 7094 is not exceeded.

Program Options

The program has two option procedures controlled by LOOP and by the combination of values of IA , IB , and SAVE .

By setting $\text{LOOP} = 1$, we can reduce the original angular momentum quantity LM (max l for photon) in unit increments (until a minimum of one is reached). The selection rules may then reduce the range limits KM and JM . The summing process is repeated to recalculate the differential and total cross sections.

By altering the input values IA and IB we can segment a run. The program proceeds through IB electron shells rather than the totality of shells (JX). The total cross section up to that point can be fed back in as part of the input (SAVE) when the user desires to continue the run. With IA greater than zero, the program starts after the first IA electron shells. This process is useful when long computer running time is not available.

System Information

The program as run at the New York Regional Computer Center utilizes the following tapes:

Logical tape unit 5	Read
Logical tape unit 6	Write
Logical tape unit 1	Self-consistent-field data

This page is intentionally left blank.

III. SAMPLE OUTPUT

The output from an actual run is given. The complete output contains the differential cross section for each subshell in succession. Only one subshell is reproduced here, for economy.

INPUT DATA FOR PHOTOELECTRIC CALCULATION

INPUT CARD HEADS

JM	KMAX	LM	NIAPE	NEGE	IA	IB	IZ	LCOP	OV	SAVE
11	0	4	1	0	0	0	13	0	0.10000000E 02	C.

INPUT DATA FOR PHOTOELECTRIC CALCULATION

13 = NUCLEAR CHARGE
10.000 = PHOTON ENERGY
0 = MAX KAPPA FOR ELECTRON
4 = MAX L FOR PHOTO:
11 = MAX J (LEGENDRE COEFF.)

TAPE POSITIONED PROPERLY.

AL = ELEMENT
13 = ATOMIC NUMBER
6 = NUMBER OF ELECTRON SHELLS
0.19449370E 00 = SCREENING FACTOR OF OUTERMOST BOUND ELECTRON
257 = RADIAL GRID UP TO X = 1.0
1281 = RADIAL GRID UP TO X = 65.0
1436 = TOTAL RADIAL GRID
0.82222162E 04 = OUTERMOST RADIAL VALUE

1S1/2 = SHELL
0.27269274e 03 = INTEGRATION CUT-OFF
1327 = NUMBER OF WAVE FUNCTION. GRID POINTS
5 = MAX KAPPA FOR THIS SHELL
25 = NUMBER OF MATRIX ELEMENTS FOR THIS SHELL

LENGTH UNITS ARE HBAR / MC (1 BOHR RADIUS = 137)

INTEGRATION STEP SIZE IS 0.0078125 UP TO 1.000

INTEGRATION STEP SIZE IS 0.1250000 UP TO 65.000

INTEGRATION STEP SIZE IS 1.0000000 UP TO 272.693

11 = MAX J (LEGENDRE COEFF.)
5 = MAX KAPPA FOR ELECTRON
4 = MAX L FOR PHOTON

LEGENDRE COEFFICIENTS OF CROSS SECTION

J	U(J)
0	0.84832748E 02
1	0.34841149E 02
2	-0.76300052E 02
3	-0.33218958E 02
4	-0.82906764E 01
5	-0.15982244E 01
6	-0.22848516E 00
7	-0.24835064E-01
8	-0.2069956E-02
9	-0.11737233E-03

ELEMENT ATOMIC NUMBER SHELL
 AL 13 1S1/2

BINDING ENERGY PHOTON ENERGY ELECTRON KINETIC ENERGY
 1.5499309 KEV 10.000000 KEV 8.4500691 KEV

UNPOLARIZED CROSS SECTION (BARN/STERADIAN)

THETA	COS THETA	CROSS SECTION	ANG. DIST.
0	1.0000000	0.10482765E-01	0.0000778
2	0.9993906	0.31837447E 00	0.0023632
4	0.9975640	0.12387132E 01	0.0091947
6	0.9945219	0.27615944E 01	0.0204966
8	0.9902661	0.48706563E 01	0.0361540
10	0.9848078	0.75433565E 01	0.0559929
12	0.9781476	0.10751303E 02	0.0798049
14	0.9702957	0.14460679E 02	0.1073389
16	0.9612617	0.18632747E 02	0.1383074
18	0.9510565	0.23224424E 02	0.1723906
20	0.9395926	0.28188594E 02	0.2092409
22	0.9271839	0.33476281E 02	0.2484882
24	0.9135455	0.39034332E 02	0.2897446
26	0.8987940	0.44809127E 02	0.3326098
28	0.8829476	0.50745737E 02	0.3766766
30	0.8660254	0.56789170E 02	0.4215355
32	0.8480481	0.62834551E 02	0.4667804
34	0.8290375	0.68978249E 02	0.5120127
36	0.8090170	0.75018242E 02	0.5568465
38	0.7880108	0.80954696E 02	0.6009117
40	0.7660444	0.86740461E 02	0.6438584
42	0.7431448	0.92331495E 02	0.6853596
44	0.7193398	0.97687210E 02	0.7251140
46	0.6946584	0.10277077E 03	0.7628484
48	0.6691306	0.10754931E 03	0.7983186
50	0.6427876	0.11199406E 03	0.8313111
52	0.6156615	0.11608047E 03	0.8616438
54	0.5877853	0.11978819E 03	0.8891655
56	0.5591929	0.12310107E 03	0.9137564
58	0.5299193	0.12600702E 03	0.9353266
60	0.5000000	0.12849794E 03	0.9538164
62	0.4694716	0.13056947E 03	0.9691930
64	0.4383712	0.13222024E 03	0.9814509
66	0.4067366	0.13345459E 03	0.9906087
68	0.3746066	0.13427632E 03	0.9967063
70	0.3420202	0.13469443E 03	0.9998118
72	0.3090170	0.13471978E 03	1.0000000
74	0.2756374	0.13436550E 03	0.9973702
76	0.2419219	0.13364660E 03	0.9920340
78	0.2079117	0.13257975E 03	0.9841149
80	0.1736452	0.13118296E 03	0.9737468
82	0.1391731	0.12947556E 03	0.9610716
84	0.1045285	0.12747693E 03	0.9462376

86	0.0697565	0.12520828E 03	0.9293979
88	0.0348995	0.12269040E 03	0.9107082
90	0.0000000	0.11994453E 03	0.8903260
92	-0.0348995	0.11699190E 03	0.8684091
94	-0.0697564	0.11385362E 03	0.8451144
96	-0.1045284	0.11055058E 03	0.8205965
98	-0.1391731	0.10710323E 03	0.7950075
100	-0.1736482	0.10353156E 03	0.7684956
102	-0.2079117	0.99854979E 02	0.7412050
104	-0.2419219	0.96092227E 02	0.7132748
106	-0.2756373	0.92261351E 02	0.6848389
108	-0.3090170	0.88379639E 02	0.6560257
110	-0.3420201	0.84463592E 02	0.6269576
112	-0.3746066	0.80528891E 02	0.5977510
114	-0.4067366	0.76590405E 02	0.5685164
116	-0.4383711	0.72662151E 02	0.5393577
118	-0.4694715	0.68757333E 02	0.5103729
120	-0.5000000	0.64888321E 02	0.4816540
122	-0.5299192	0.61066679E 02	0.4532866
124	-0.5591929	0.57303176E 02	0.4253509
126	-0.5877852	0.53607805E 02	0.3979208
128	-0.6156615	0.49989820E 02	0.3710652
130	-0.6427876	0.46457748E 02	0.3448472
132	-0.6691306	0.43019425E 02	0.3193252
134	-0.6946593	0.39682028E 02	0.2945523
136	-0.7193398	0.36452100E 02	0.2705772
138	-0.7431448	0.33335594E 02	0.2474439
140	-0.7660444	0.30337900E 02	0.2251926
142	-0.7880107	0.27463871E 02	0.2038592
144	-0.8090170	0.24717871E 02	0.1834762
146	-0.8290376	0.22103603E 02	0.1640724
148	-0.84804E1	0.19625136E 02	0.1456737
150	-0.8660254	0.17284947E 02	0.1283030
152	-0.8829476	0.15085945E 02	0.1119602
154	-0.8987940	0.13030508E 02	0.0967230
156	-0.9135454	0.11120710E 02	0.0825470
158	-0.9271638	0.93583400E 01	0.0694652
160	-0.9396926	0.77449520E 01	0.0574893
162	-0.9510565	0.62818686E 01	0.0466291
164	-0.9612617	0.49702084E 01	0.0368929
166	-0.9702957	0.38109178E 01	0.0282977
168	-0.9781476	0.28047778E 01	0.0208193
170	-0.9848078	0.19524343E 01	0.0144926
172	-0.9902681	0.12544079E 01	0.0093112
174	-0.9945219	0.71109624E 00	0.0052783
176	-0.9975640	0.32280832E 00	0.0023961
178	-0.9993908	0.89753443E-01	0.0006662
180	-1.0000000	0.12053592E-01	0.0000995

INTEGRATED CROSS SECTION = 0.10660397E 04 BARN-S

ELEMENT

ATOMIC NUMBER

AL

13

PHOTON ENERGY = 10.000000 KEV

TOTAL CROSS SECTION = 0.11461591E 04 BARNs

IV. THE PROGRAM

The program is written in FORTRAN IV. The versions used on the IBM 709⁴ and the CDC 6600 are identical except for control cards. The data tapes contain the same information in binary form, but are not compatible between the two machines.

All the Common blocks appear in the main routine (PELEC). The definition of the Common variables is given first. In the subroutines, Common blocks used are quoted. The unlabelled Common is the same wherever it appears.

Definition of Variables in COMMON

Unlabelled Common: Length 107₈

Name	Dimensions	Mode	Meaning
PI		R	π
HALFPI		R	$\pi/2$
FOURPI		R	4π
RAD		R	$\pi/180$
SQ2		R	$2^{-1/2}$
Q		R	Photon energy (in mc^2 units)
ZA		R	Atomic number
ZAZA		R	$ZA * ZA$
EFN		R	Free electron energy -1 (in mc^2 units)
EGN		R	Free electron energy +1 (in mc^2 units)
V		R	Potential; screening factor/radius
CG	30	R	$-\kappa - \gamma$ if radius < 1 ; $-\kappa$ if radius > 1
GAM	30	R	$\sqrt{\kappa^2 - ZAZA}$

/BESSEL/ Common: Length 420₈

Name	Dimensions	Mode	Meaning
FL	15	R	Numerical factors used in the construction of the spherical Bessel function.
PC	15	R	
PF	15 x 15	R	
M1		I	Largest order of Bessel function needed
M2		I	$M1 + 1$
B	15	R	Spherical Bessel function

/DFUNC/ Common: Length 1047₈

Name	Dimensions	Mode	Meaning
F	30	R	"Small" component of free-electron wavefunction
G	30	R	"Large" component of free-electron wavefunction
DF	30	R	Derivative of F
DG	30	R	Derivative of G
DFK	200	R	Integrand for matrix elements $K_{\ell}(\mu\mu')$
DFKP	200	R	Integrand for matrix elements $K_{\ell}(\mu'\mu)$
CF	30	R	$\kappa - \gamma$ if radius < 1; κ if radius > 1
H		R	Integration step size

/FAC/Common: Length 324₈

Name	Dimensions	Mode	Meaning
FACT	67	R	Numerical factors used in the calculation of the Clebsch-Gordan coefficients.
RTFACT	95	R	
R ϕ T	50	R	

/FID ϕ / Common: Length 746₈

Name	Dimensions	Mode	Meaning
FI	30 x 15	R	$\phi(\kappa, \lambda)$
D	30	R	Legendre coefficient of cross section
JMP		I	Max. order of Legendre coefficient + 1
NAME		ALFA	Element
SHELL		ALFA	Electron shell
QV		R	Photon energy (in keV units)
EB		R	Binding energy of shell (in keV units)
IZ		I	Atomic number

/KUT/ Common: Length 24₈

Name	Dimensions	Mode	Meaning
RK1	4	R	Numerical coefficients used for the Runge-Kutta integration (Gill Form)
RK2	4	R	
RK3	4	R	
RK4	4	R	
K4	4	I	

/LIMIT/ Common: Length 13₈

Name	Dimensions	Mode	Meaning
JM		I	Max order of Legendre coefficient
LM		I	Max l for photon
KM		I	Max κ for free electron
K2M		I	2 * KM; number of free electron states
IEND		I	Flag for zero electron kinetic energy state
NEW		I	Flag to save repetition of calculation when radius is not advanced
NK		I	Number of matrix elements $K_l(\kappa\kappa')$
NKP		I	Number of matrix elements $K_l(\kappa'\kappa)$
JKB		I	Twice j_{κ}
LMKB		I	$l_{-\kappa}$
NTAB		I	Radial index in bound state tabulation

/MAT/ Common: Length 1535₈

Name	Dimensions	Mode	Meaning
SF	30	R	Integration storage variable for "small" component of free electron wavefunction
SG	30	R	Integration storage variable for "large" component of free electron wavefunction
FK	200	R	Matrix elements $K_l(\kappa\kappa')$
FKP	200	R	Matrix elements $K_l(\kappa'\kappa)$

Name	Dimensions	Mode	Meaning
SFK	200	R	Integration storage variable for matrix elements $K_l(\kappa\kappa')$
SFLP	200	R	Integration storage variable for matrix elements $K_l(\kappa'\kappa)$
RCUT		R	Cut-off radius for integration

/QUANT/ Common: Length 322₈

Name	Dimensions	Mode	Meaning
LK	30	I	l_κ
LMK	30	I	$l_{-\kappa}$
JK	30	I	Twice j_κ
FKAP	30	R	κ
SN	30	R	Sign of κ
SI	30	R	Sine of phase shift
CR	30	R	Cosine of phase shift

/ONWARD/ Common: Length 4₈

Name	Dimensions	Mode	Meaning
RX		R	Radial variable beyond radial cutoff on uniform grid tabulation
SCX		R	Interpolated value of screening factors
GBX		R	Interpolated value of "large" component of wavefunction
FBX		R	Interpolated value of "small" component of wavefunction

/TAPES/ Common: Length 13562₈

Name	Dimension	Mode	Meaning
X	1500	R	Radial value
SCF	1500	R	Screening factor
FB	1500	R	"Small" component of bound state wavefunction

Name	Dimensions	Mode	Meaning
GB	1500	R	"Large" component of bound state wavefunction
GAMB		R	$\sqrt{\kappa^2 - ZAZA}$ for bound state
SCREEN		R	Normalization factor for least bound electron

/TRANS/ Common: Length 1700₈

Name	Dimensions	Mode	Meaning
HF	30 x 15	R	H (κ, μ') for $\mu' > 0$
HFM	30 x 15	R	H (κ, μ') for $\mu' < 0$
JNG	30	I	$(-\mu')$ max + 1/2
JPS	30	I	(μ') max + 1/2 provided $\mu' > 0$ permitted; -1 otherwise

/VECT/ Common: Length 1441₈

Name	Dimensions	Mode	Meaning
KF	200	I	Index for κ values for $K_l(\kappa' \kappa)$
KG	200	I	Index for κ values for $K_l(\kappa \kappa')$
LBES	200	I	Photon angular momentum + 1 for $K_l(\kappa' \kappa)$
LBS	200	I	Photon angular momentum + 1 for $K_l(\kappa \kappa')$
LKB		I	$l_{\kappa'}$

ROUTINE PELEC

Purpose: This is the main program. It serves as the control section, reading the input cards and the tape containing the self-consistent-field data and setting up the calculations. Nearly all the actual computation is done in subroutines.

Method: Numerical constants are computed and stored, the input read and checked (and diagnostics printed, if needed), then printed with interpretation; the tape is scanned for the element required and the data read from it and interpreted. For each subshell, SINDE \bar{X} is called to set up the matrix elements and their quantum numbers, RADINT to perform the radial integrations. LEGEND is called to perform the angular momentum sums, ANGLE to produce the differential cross section (headings are supplied for the tables printed in the subroutines); if the matrix reduction option is called for, the cutoff values of the quantum numbers are reduced and the program loops back through the angular sums. The total cross section is accumulated in PELEC and printed out. The program recycles to read the next input card and perform the next case, until a flag on the input card signals termination.

Subroutines called: SINDE \bar{X} , RADINT, LEGEND, ANGLE, HUM

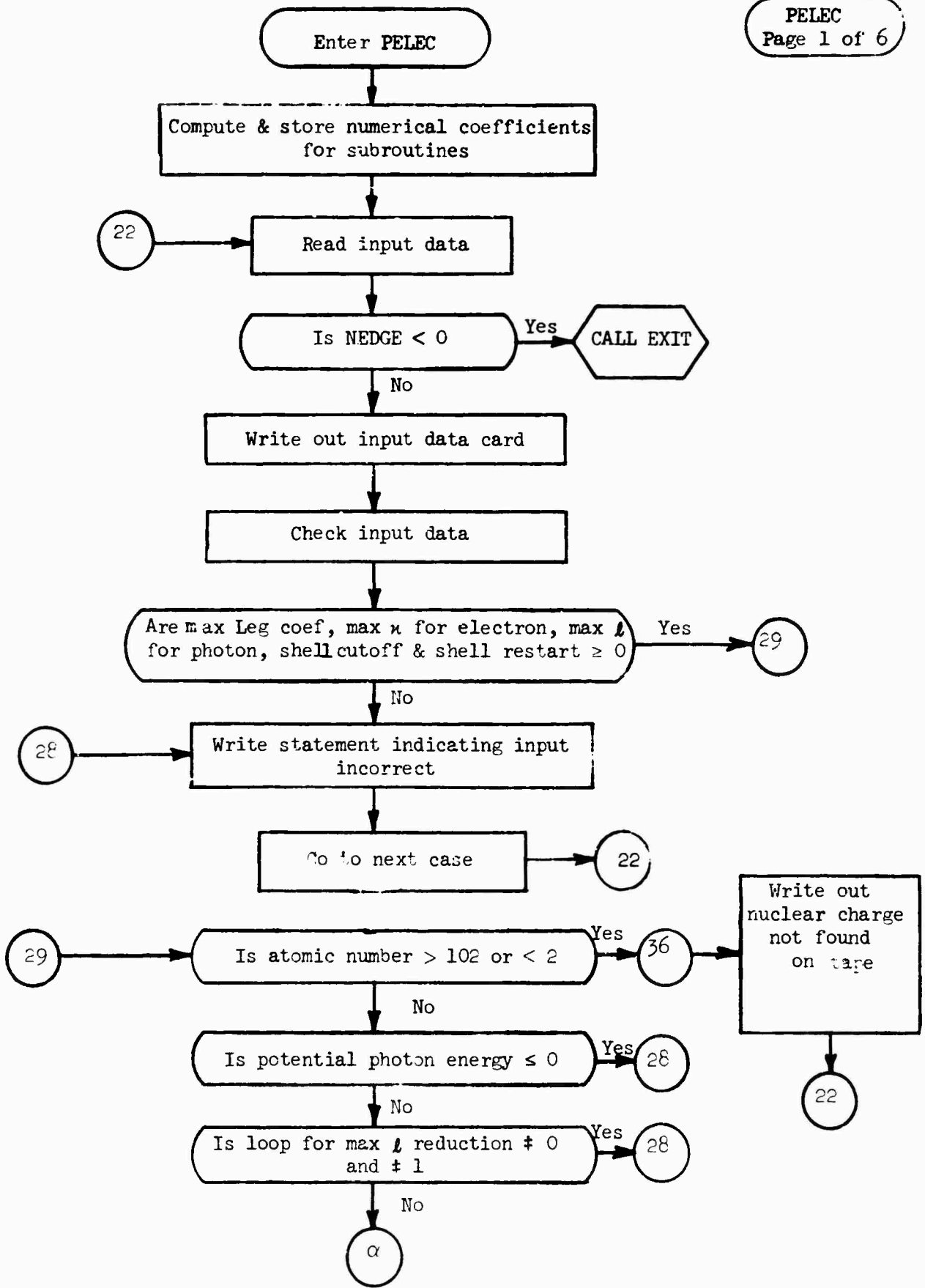
Variables in unlabelled Common: PI, HALFPI, FOURPI, RAD, SQ2, Q, ZA, ZAZA,
EFN, EGN, V, CC, GAM

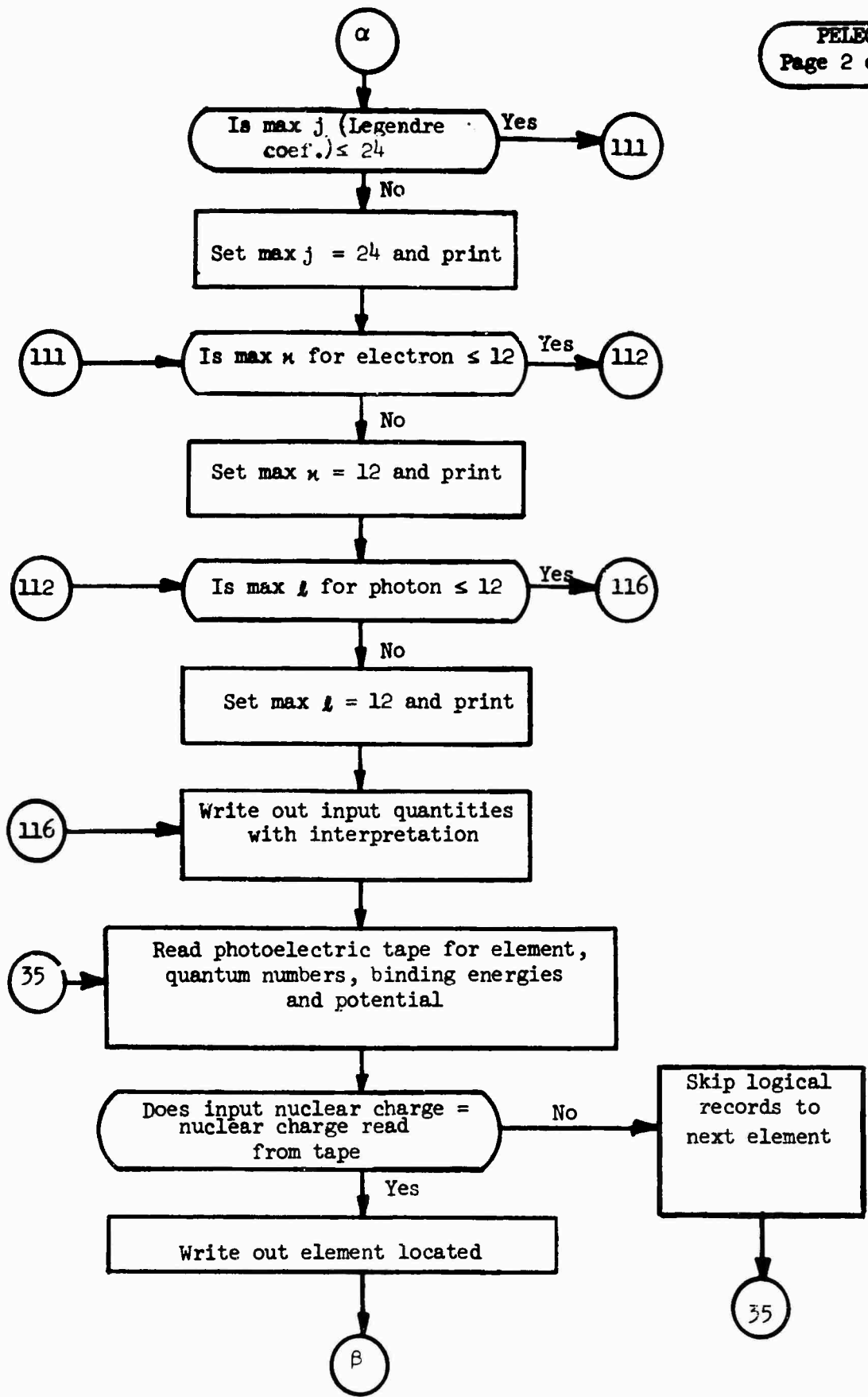
Labelled Common: BESSEL, DFUNC, FAC, FID \bar{A} , KUT, LIMIT, MAT, QUANT, ANWARD,
TAPES, TRANS, VECT

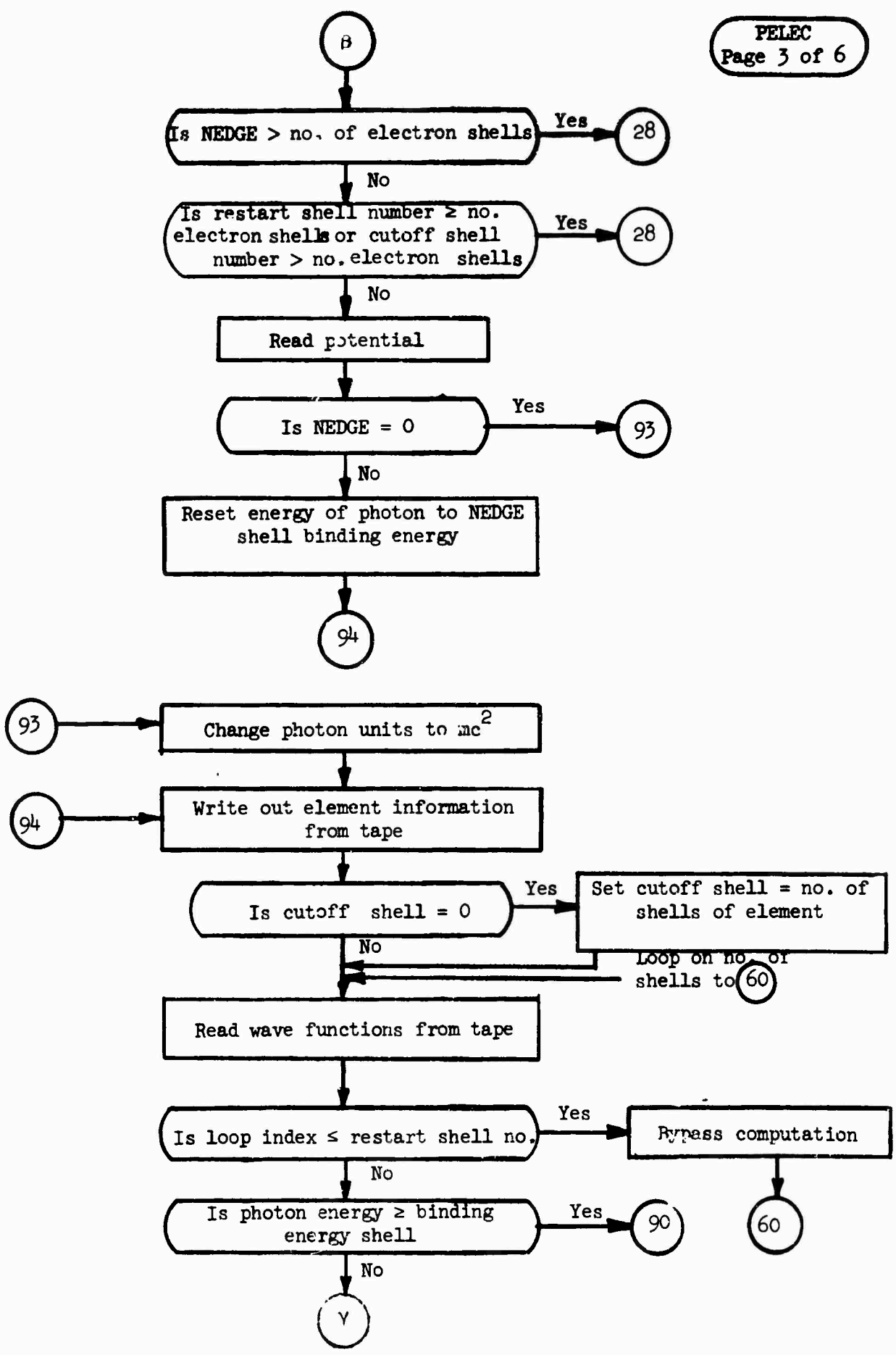
Local Variables:

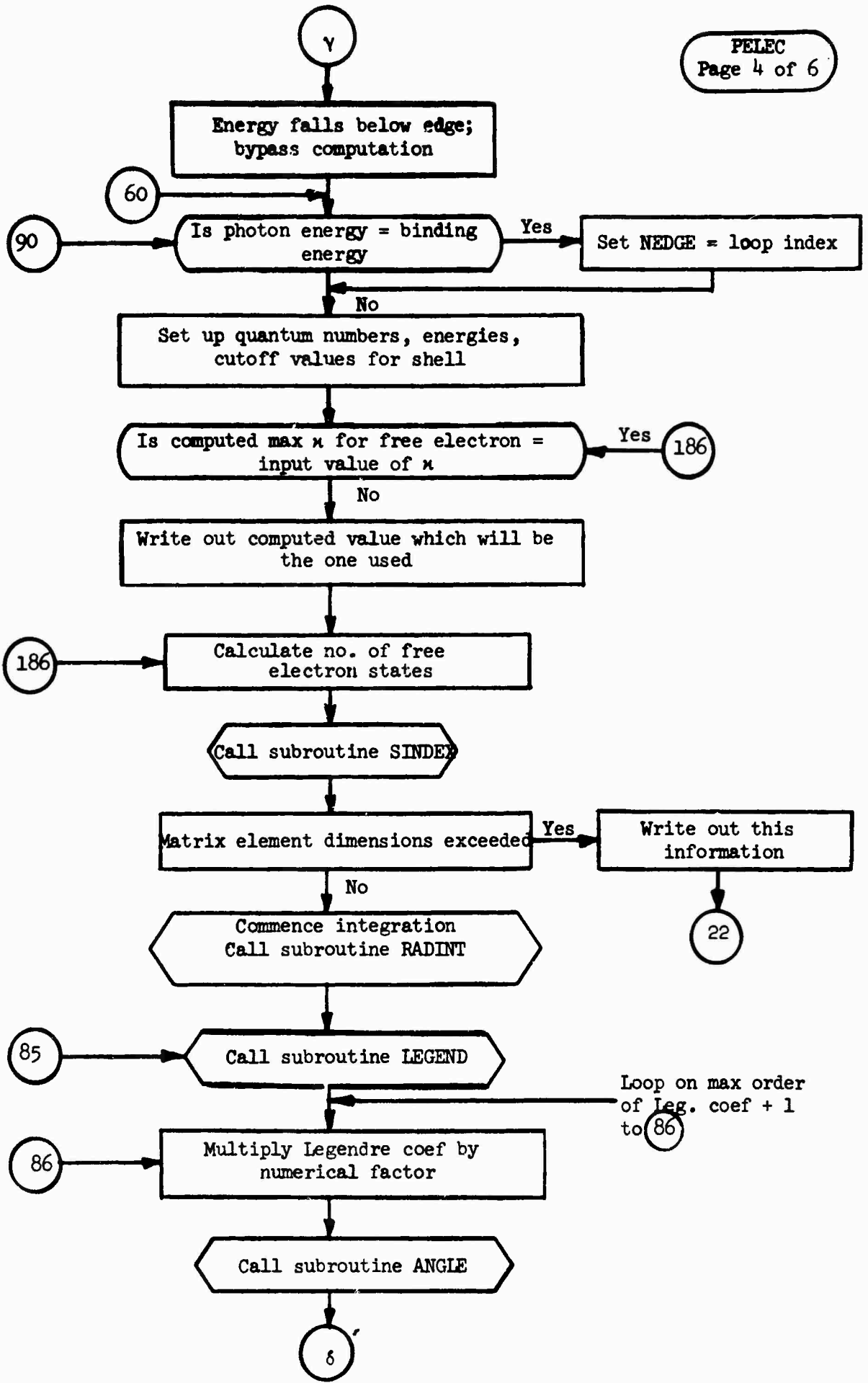
Name	Dimension	Mode	Meaning
KMAX		I	Input max κ for free electron
NTAPE		I	The logical tape unit assigned for tape containing the self-consistent-field data
NEDGE		I	= -1 terminates program. = 0 normal run = integer sets photon energy to NEDGEth binding energy
IA		I	= 0 normal case > 0 calculation commences after IA shells
IB		I	= 0 calculation includes outermost shell > 0 cuts off calculation after IB shells
LOOP		I	= 0 normal case = 1 for photon angular momentum reduction
QV		R	Input photon energy in keV
SAVE		R	Input total cross section; accumulation from previous run; = 0 otherwise
IZ		I	Input atomic number
NGRID		I	Number of grid points in table
ISIXFI		I	Number of grid points for radial value of 65 (1/2 Bohr unit)
IOLE		I	Number of grid points for radial value of one
RSIXFI		R	Radial value of 65, read from tape
ROLE		R	Radial value of one, read from tape
ZTRY		R	Atomic number read from tape
JX		I	Number of electron shells
XN	36	ALFA	Shell identification
XL	36	R	k_{κ}
XJ	36	R	j_{κ}
XZ	36	R	Shell occupancy

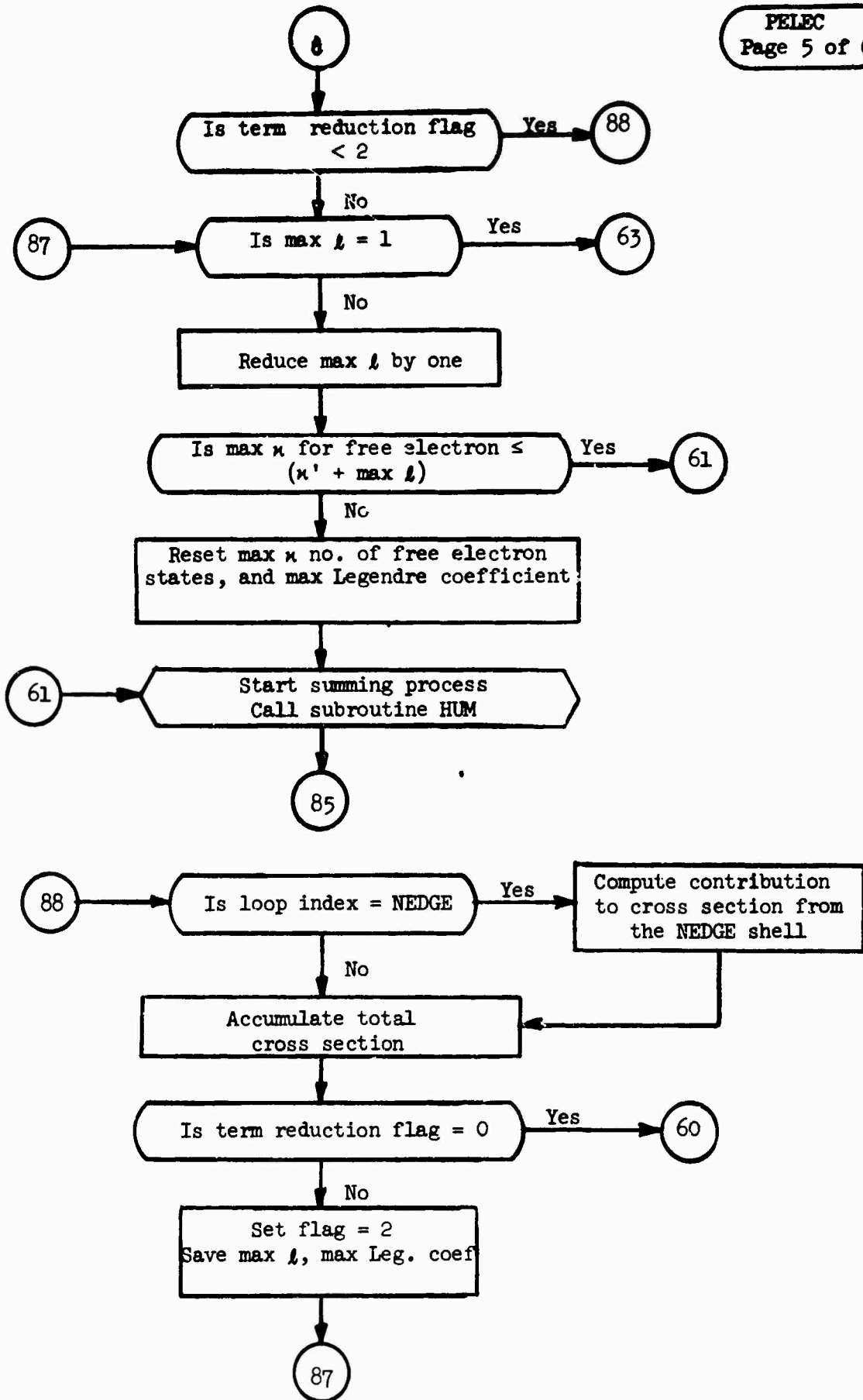
Name	Dimension	Mode	Meaning
ERG	36	R	Binding energy
KJI		I	Number of wavefunction grid points
SECT		R	Total cross section
NTOT		I	Number of matrix elements for shell
SEDGE		R	Cross section jump at edge
LMS		I	Initial max l (in loop reduction)
JMS		I	Initial max order of Legendre coefficient (in loop reduction)
JPS		I	Initial max order of Legendre coefficient + 1 (in loop reduction)
CCM		R	Conversion factor (keV/mc ²)
ALFA		R	Fine structure constant: 1/137.0367
REL		R	Classical electron radius (in cm) x 10 ¹²
KB		I	j_{κ}
FKB		R	j_{κ}

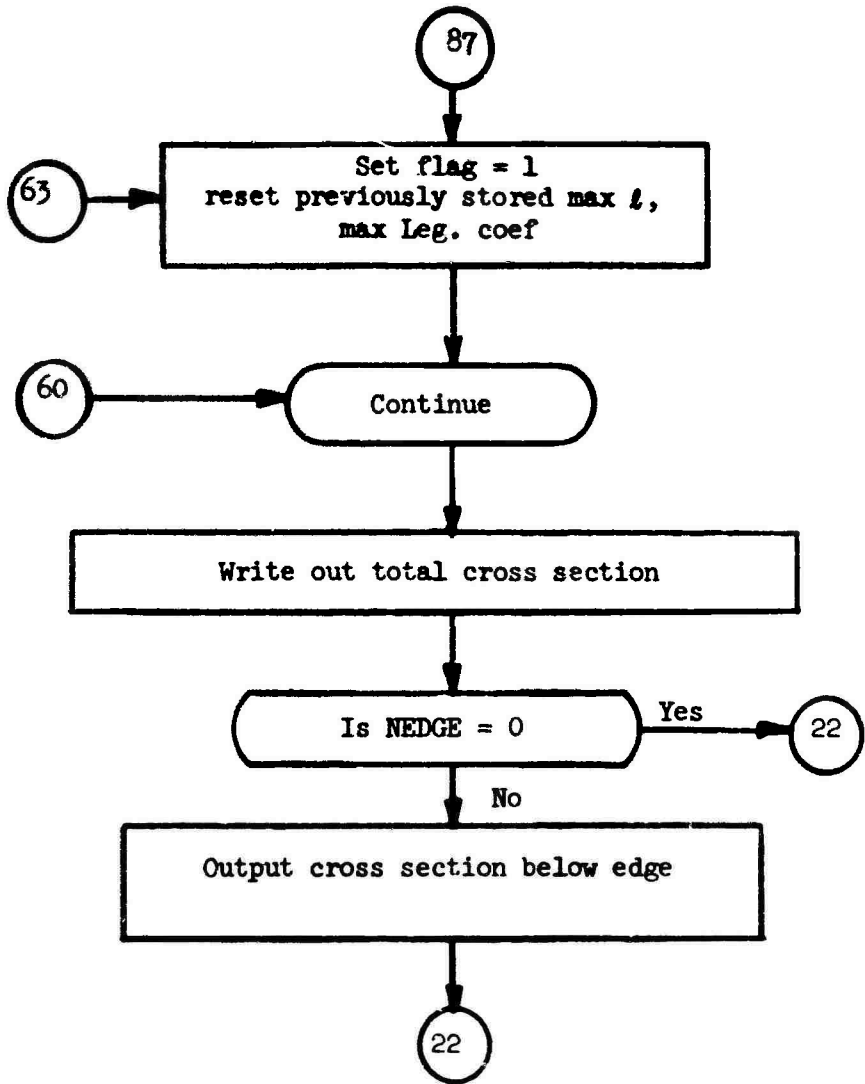












SIMPLIC PELEC

```

C FOR LUC 6600 OPERATION, ADD CARD READING
C PROGRAM PELEC(INPUT,OUTPUT,TAPE1,TAPE5=INPUT,TAPE6=OUTPUT)
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,C6(30),GAM(30) PEL00010
COMMON/BESSL/FL(15),PC(15),OF(15,15),M1,M2,B(15) PEL00020
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),H PEL00030
COMMON /FAC/FACT(67),RTFAC(95),ROOT(50) PEL00040
COMMON/FIDO/FI(30,15),U(30),JMP,NAME,SHELL,QV,EB,IZ PEL00050
COMMON /KUT/RK1(4),RK2(4),RK3(4),RK4(4),K4(4) PEL00060
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LKMB,NTAB PEL00070
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT PEL00080
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30) PEL00090
COMMON /ONWARD/RX,SCX,GBX,FBX PEL00100
COMMON /TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN PEL00110
COMMON/TRANS/HF(30,15),HFM(30,15),JNG(30),JPS(30) PEL00120
COMMON/VECI/KF(200),KG(200),LBES(200),LBS(200),LKB PEL00130
DIMENSION XN(36),XL(36),XJ(36),ERG(36),XZ(36) PEL00140
FL(1) = 1.0 PEL00150
PC(1) = 1.0 PEL00160
DO 5 L=2,15 PEL00170
FL(L) = 2*L-1 PEL00180
PC(L) = PC(L-1)/FL(L) PEL00190
DO 5 J=1,15 PEL00200
FLJ = J*(2*(L+J)-1) PEL00210
5 OF(L,J) = 1.0/FLJ PEL00220
ROOT(1) = 1.0 PEL00230
DO 10 I=2,50 PEL00240
FAT = I PEL00250
10 ROOT(I) = SQRT (FAT) PEL00260
FACI(1) = 1.0 PEL00270
FACI(3) = 1.0 PEL00280
RTFAC(1) = 1.0 PEL00290
RTFAC(3) = 1.0 PEL00300
FAT = 1.0 PEL00310
DO 15 I=2,55 PEL00320
F1 = I PEL00330
FAT = FAT*F1 PEL00340
FACI(2*I+1) = FAT PEL00350
15 RTFAC(2*I+1) = SQRT(FAT) PEL00360
FAT = 1.0 PEL00370
DO 20 I=34,47 PEL00380
F1 = I PEL00390
FAT = FAT*F1 PEL00400
20 RTFAC(2*I+1) = SQRT(FAT)*RTFAC(67) PEL00410
SQ2 = 1.0 / ROOT(2) PEL00420
RK1 (1) = 0.5 PEL00430
RK1 (2) = 1.0-SQ2 PEL00440
RK1 (3) = 1.0+SQ2 PEL00450
RK1 (4) = 1.0/6.0 PEL00460
RK2 (1) = 2.0 PEL00470
RK2 (2) = 1.0 PEL00480
RK2 (3) = 1.0 PEL00490
RK2 (4) = 2.0 PEL00500
RK3 (1) = 0.5 PEL00510
RK3 (2) = 1.0-SQ2 PEL00520
RK3 (3) = 1.0+SQ2 PEL00530
RK3 (4) = 0.5 PEL00540
RK4 (1) = 0.5 PEL00550
RK4 (2) = 0.0 PEL00560
RK4 (3) = 0.5 PEL00570
RK4 (4) = 0.0 PEL00580
K4(1) = 1 PEL00590

```

```

K4(2) = 0
K4(3) = 1
K4(4) = 0
CCM = 511.0062
ALFA = 1.0/157.0367
REL = 0.281777
PI = 3.14159265
FOURPI = 4.0*PI
HALFPI = 0.5 * PI
KAD = PI / 180.0
FIB = 0.250*PI*REL*REL/ALFA
22 READ (5,25) JM,KMAX,LM,NTAPE,NEDGE,IA,IB,IZ,LOOP,QV,SAVE
25 FORMAT (9I5,2E15.8)
C ORDINARILY, IA = 0, IB = 0, SAVE = 0.
C IB .NE. 0 CUTS OFF CALCULATION AFTER IB SHELLS
C IA .GT. 0 RESTARTS AFTER IA SHELLS
C SAVE IS THEN CROSS SECTION OF FIRST IA SHELLS READ BACK IN
C QV ENTERED IN K.E.V., SAVE ENTERED IN BARNS
C LOOP = 0 ORDINARILY, LOOP = 1 FOR LM REDUCTION
C NEDGE NEGATIVE TERMINATES PROGRAM
C IF (NEDGE.LT.0) CALL EXIT
WRITE (6,27)
27 FORMAT (1H1//2X,40HINPUT DATA FOR PHOTOELECTRIC CALCULATION //2X,
116HINPUT CARD READS//2X,38HJM KMAX LM NTAPE NEDGE IA IB IZ,
26H LOOP, /X,2HQV,1UX,4HSAVE //)
C WRITE (6,25) JM,KMAX,LM,NTAPE,NEDGE,IA,IB,IZ,LOOP,QV,SAVE
DATA CHECKING
IF (MIN0(JM,KMAX,LM,IA,IB).GE.0) GO TO 29
28 WRITE (6,102)
102 FORMAT (5X,15HINCORRECT INPUT //)
GO TO 22
29 IF ((IZ.LT.2).OR.(IZ.GT.102)) GO TO 36
IF (QV.LE.0.0) GO TO 28
IF ((LOOP.NE.0).AND.(LOOP.NE.1)) GO TO 28
IF (JM.LE.24) GO TO 111
JM=24
WRITE (6,109) JM
109 FORMAT (/5X56HIN ORDER NOT TO EXCEED DIMENSION JM HAS BEEN REDUCED
1 TO 15/)
111 IF (KMAX.LE.12) GO TO 112
KMAX=12
WRITE (6,113) KMAX
113 FORMAT (/5X58HIN ORDER NOT TO EXCEED DIMENSION KMAX HAS BEEN REDUCED
1ED TO 13/)
112 IF (LM.LE.12) GO TO 116
LM=12
WRITE (6,114) LM
114 FORMAT (/5X56HIN ORDER NOT TO EXCEED DIMENSION LM HAS BEEN REDUCED
1 TO 13/)
116 Z = IZ
ZA = Z*ALFA
ZAZA = ZA*ZA
WRITE (6,50) IZ,QV,KMAX,LM,JM
50 FORMAT (1H1//5X40HINPUT DATA FOR PHOTOELECTRIC CALCULATION //
114X, 14,17H = NUCLEAR CHARGE /9X,F9.3,16H = PHOTON ENERGY //
215X13,25H = MAX KAPPA FOR ELECTRON /15X13,19H = MAX L FOR PHOTON /
315X13,26H = MAX J (LEGENDRE COEFF.) //)
REWIND NTAPE
READ (NTAPE) NGRID,ISIXFI,IONE,RSIXFI,RONE,(X(I),I=1,NGRID)
35 READ (NTAPE) ZTRY,JX,NAME,SCREEN,(XN(I),XL(I),XJ(I),XZ(I),ERG(I),
11=1,JX)
IZI = ZTRY + 0.01

```

```

PEL00600
PEL00610
PEL00620
PEL00630
PEL00640
PEL00650
PEL00660
PEL00670
PEL00680
PEL00690
PEL00700
PEL00710
PEL00720
PEL00730
PEL00740
PEL00750
PEL00760
PEL00770
PEL00780
PEL00790
PEL00800
PEL00810
PEL00820
PEL00830
PEL00840
PEL00850
PEL00860
PEL00870
PEL00880
PEL00890
PEL00900
PEL00910
PEL00920
PEL00930
PEL00940
PEL00950
PEL00960
PEL00970
PEL00980
PEL00990
PEL01000
PEL01010
PEL01020
PEL01030
PEL01040
PEL01050
PEL01060
PEL01070
PEL01080
PEL01090
PEL01100
PEL01110
PEL01120
PEL01130
PEL01140
PEL01150
PEL01160
PEL01170
PEL01180
PEL01190
PEL01200
PEL01210

```

	IF (IZ .EQ. IZT)	GO TO 40	PEL01220
	READ (NTAPE) (SCF(I),I=1,NGRID)		PEL01230
C	SKIPS LOGICAL RECORD CONTAINING POTENTIAL		PEL01240
	DO 99 ISKIP=1,JX		PEL01250
99	READ (NTAPE) KCUT,KJI, (GB(I),I=1,KJI), (FB(I), I=1,KJI)		PEL01260
C	SKIPS UNWANTED LOGICAL RECORDS TO NEXT ELEMENT		PEL01270
	IF (IZT .LE. 102)	GO TO 35	PEL01280
36	WRITE (6,30) IZ		PEL01290
30	FORMAT (//30X19HNUCLEAR CHARGE Z = I3,1X18HNOT FOUND ON TAPE.)		PEL01300
	GO TO 22		PEL01310
40	WRITE (6,45)		PEL01320
45	FORMAT (/////20X,25HTAPE POSITIONED PROPERLY.////)		PEL01330
	IF (NEDGE.GT.JX)	GO TO 28	PEL01340
	IF ((IA.GE.JX).OR.(IB.GT.JX))	GO TO 28	PEL01350
	READ (NTAPE) (SCF(I),I=1,NGRID)		PEL01360
	IF (NEDGE .EQ. 0)	GO TO 93	PEL01370
	Q = ERG(NEDGE)		PEL01380
	QV = Q * CCM		PEL01390
	GO TO 94		PEL01400
93	Q = QV / CCM		PEL01410
94	WRITE (6,175) NAME,IZ,JX,SCREEN,IONE,RONE,ISIXFI,RSIXFI,NGRID,		PEL01420
	IX(NGRID)		PEL01430
175	FORMAT (//25XA6,1X9H= ELEMENT/28X13,1X15H= ATOMIC NUMBER/		PEL01440
	129X12,1X27H= NUMBER OF ELECTRON SHELLS/		PEL01450
	216XE15.8,1X46H= SCREENING FACTOR OF OUTERMOST BOUND ELECTRON/		PEL01460
	328X13,1X24H= RADIAL GRID UP TO X = F4.1/		PEL01470
	427X14,1X24H= RADIAL GRID UP TO X = F5.1/		PEL01480
	527X14,1X19H= TOTAL RADIAL GRID /16XE15.8,1X24H= OUTERMOST RADIAL	VPEL01490	
	VALUE //	PEL01500	
	SECT = SAVE	PEL01510	
	IF (IB .EQ. 0)	IB = JX	PEL01520
	DO 60 I = 1, IB		PEL01530
	READ (NTAPE) KCUT,KJI, (GB(L),L=1,KJI),(FB(L),L=1,KJI)		PEL01540
	IF (I.LE.IA)	GO TO 60	PEL01550
	IF (Q.GE.ERG(I))	GO TO 90	PEL01560
	WRITE (6,95) XN(I)		PEL01570
95	FORMAT (/5X,18HENERGY FALLS BELOW,1XA6,1X4HEDGE//)		PEL01580
	GO TO 60		PEL01590
90	IF (Q .EQ. ERG(I))	NEDGE = I	PEL01600
	WRITE (6,80) XN(I),KJICUT,KJI		PEL01610
80	FORMAT(1H1/25XA6,1X7H= SHELL/16XE15.8,1X21H= INTEGRATION CUT-OFF/		PEL01620
	127X14,1X37H= NUMBER OF WAVE FUNCTION GRID POINTS /)		PEL01630
	FST = FIB*XZ(I)/Q		PEL01640
	LKB = XL(I) + 0.01		PEL01650
	JKB = 2.0*XJ(I) + 0.01		PEL01660
	LMKB = JKB-LKB		PEL01670
	FKB = XJ(I)+0.5		PEL01680
	GAMB = SQRT(FKB**2-ZA*ZA)		PEL01690
	KB = FKB + 0.01		PEL01700
	KM = MAXU (KB+1, KMAX)		PEL01710
	KM = MINU (KM, KB+LM)		PEL01720
	IF (KM.EQ.KMAX)	GO TO 186	PEL01730
	WRITE (6,187) KM		PEL01740
187	FORMAT (28X13,27H = MAX KAPPA FOR THIS SHELL)		PEL01750
186	K2M = 2 * KM		PEL01760
	JMP = MINU (JM+1,K2M)		PEL01770
	EFN=Q-ERG(I)		PEL01780
	EB=ERG(I)*CCM		PEL01790
	SHELL=XN(I)		PEL01800
	CALL SINDEK		PEL01810
	IF ((NK.LE.200).AND.(NKP.LE.200))	GO TO 83	PEL01820
	WRITE (6,100) NK,NKP		PEL01830

100	FORMAT (5X34H MATRIX ELEMENT DIMENSIONS EXCEEDED, 14X5H K = I4,	PEL01840
	16H NKP = I4//30X12H CASE DROPPED //)	PEL01850
	GO TO 22	PEL01860
85	NTOT = NK + NKP	PEL01870
	WRITE (6,1101) NTOT	PEL01880
1101	FORMAT (27X,I4,43H = NUMBER OF MATRIX ELEMENTS FOR THIS SHELL //)	PEL01890
	CALL RADINT	PEL01900
85	CALL LEGEND	PEL01910
	DO 86 J=1,JMP	PEL01920
86	U(J) = FST * U(J)	PEL01930
	WRITE (6,2) JM, KM, LM	PEL01940
2	FORMAT (1H1///15X,I3,26H = MAX J (LEGENORE COEFF.)/ 15X,I3,	PEL01950
1	25H = MAX KAPPA FOR ELECTRON/15X I3,19H = MAX L FOR PHOTON//)	PEL01960
	CALL ANGLE	PEL01970
	IF (LOOP.LT.2) GO TO 88	PEL01980
	WRITE (6,62) LM	PEL01990
62	FORMAT (///50X23H LOOP REDUCTION TO LM = I2)	PEL02000
87	IF (LM.EQ.1) GO TO 65	PEL02010
	LM = LM - 1	PEL02020
	IF (KM.LE.(KB+LM)) GO TO 61	PEL02030
	KM = KB + LM	PEL02040
	K2M = 2 * KM	PEL02050
	JMP = MINU (JMP, K2M)	PEL02060
	JM = JMP - 1	PEL0207C
61	CALL HUM	PEL02080
	GO TO 85	PEL02090
88	IF (1.EQ.NEDGE) SEDGE = FOURPI * D(1)	PEL02100
	SECT = SECT + FOURPI * L(1)	PEL02110
	IF (LOOP.EQ.0) GO TO 60	PEL02120
	LOOP = 2	PEL02130
	LMS = LM	PEL02140
	JMS = JM	PEL02150
	JPS = JMP	PEL02160
	GO TO 87	PEL02170
65	LOOP = 1	PEL02180
	LM = LMS	PEL02190
	JM = JMS	PEL02200
	JMP = JPS	PEL02210
60	CONTINUE	PEL02220
	WRITE (6,200) NAME, IZ, QV, SECT	PEL02230
200	FORMAT (1H1///30X,7HELEMENT,27X,13H ATOMIC NUMBER//32X,A6,31X,I3//	PEL02240
1	30X,17H PHOTON ENERGY = ,F12.7,5H KEV //// 40X,	PEL02250
2	22H TOTAL CROSS SECTION = ,E15.8,7H BARNS ////)	PEL02260
	IF (NEDGE.EQ.0) GO TO 22	PEL02270
C	IF AT EDGE, CROSS SECTION BELOW EDGE	PEL02280
	SECT = SECT - SEDGE	PEL02290
	WRITE (6,75) SECT	PEL02300
75	FORMAT (/40X27H CROSS SECTION BELOW EDGE = E15.8,6H BARNS/)	PEL02310
	GO TO 22	PEL02320
	END	PEL02330

This page is intentionally left blank.

SUBROUTINE ANGLE

Purpose: This routine computes the angular distribution from the Legendre coefficients of the cross section and a calculation of the Legendre polynomials, and outputs the differential cross-section at two degree intervals.

Method: Legendre polynomials are computed at two degree intervals, then multiplied by the Legendre coefficients of the cross section and finally summed.

Subroutine called: None

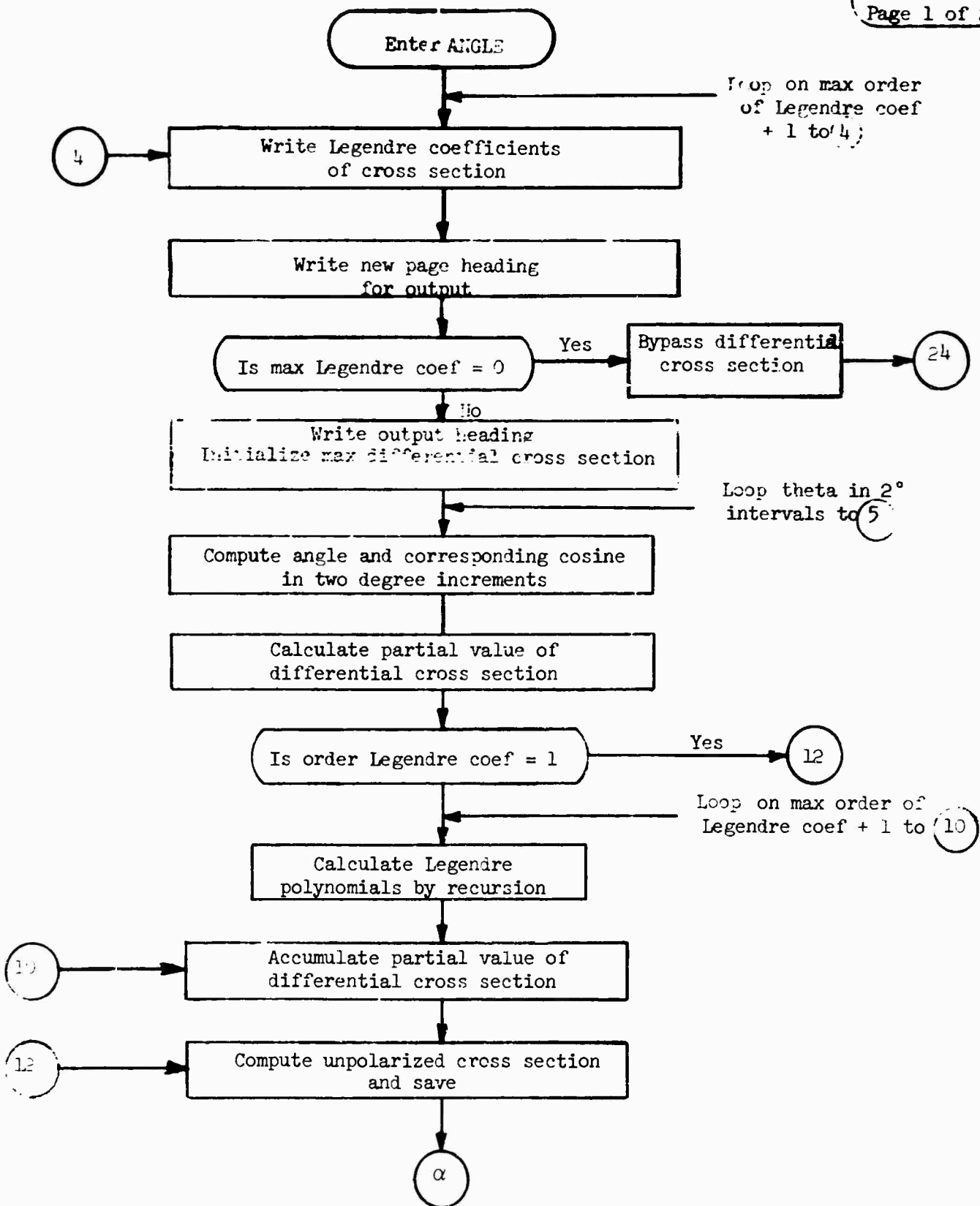
Subroutine called by: PELEC

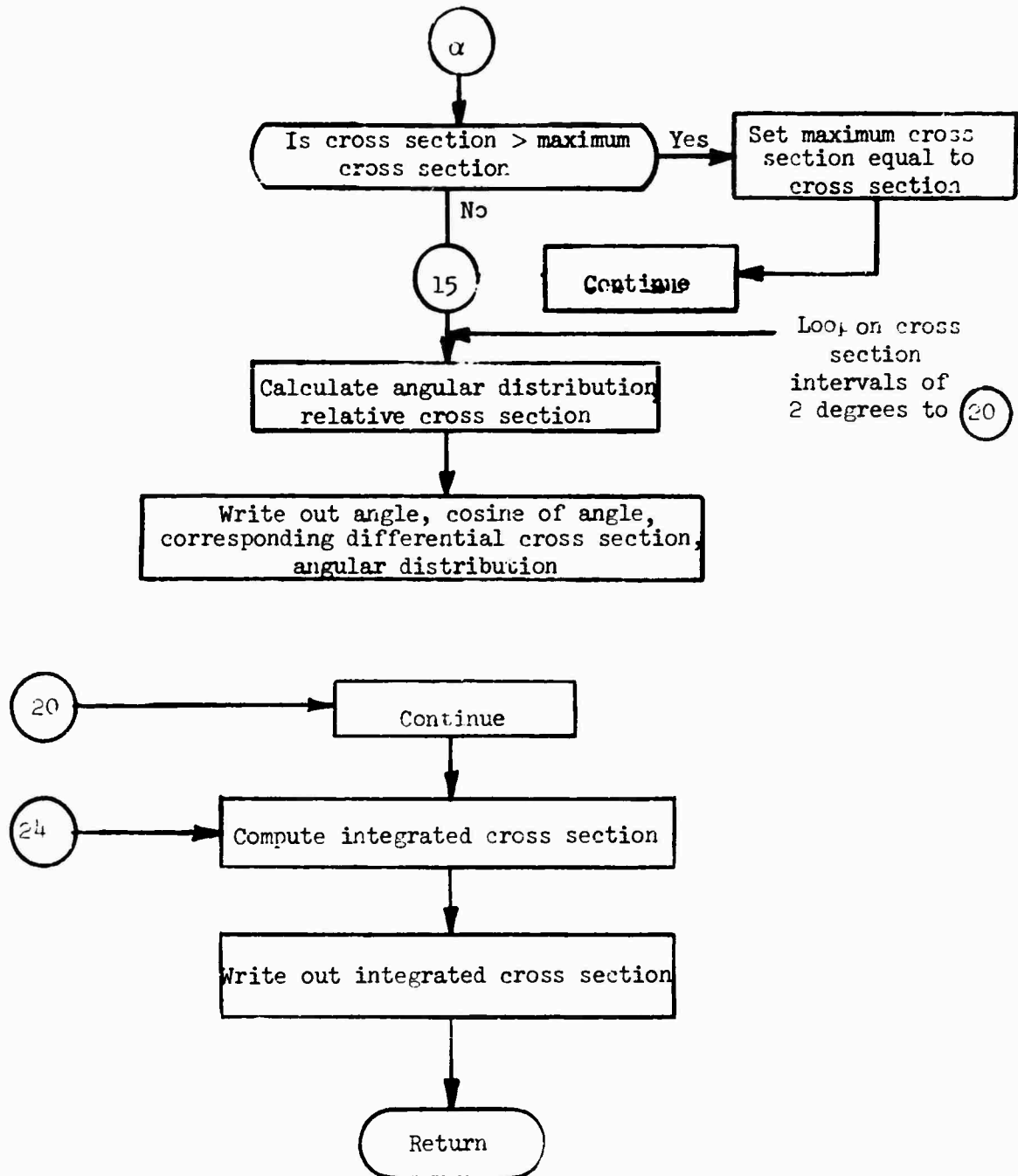
Variables in unlabelled Common: PI, HALFPI, FOURPI, RAD, SQ2, Q, EA, LAZA, EFN, V, CG, GAM

Labelled Common: FID0

Local Variables:

Name	Dimension	Mode	Meaning
JL		I	Order of Legendre coefficient
EL		R	Electron kinetic energy in keV
SMAX		R	Maximum differential cross section
KMUQ		I	Indexing variable
ITHETA		I	Angle (in degrees) between photon and electron
IT	91	I	Stores angle values
FMUQ		R	Cosine of angle
SIP		R	Unpolarized cross section (in barns/steradian)
PPL		R	Legendre polynomial
SP	91	R	Stored values of unpolarized cross section
AD	91	R	Angular distribution
XSEC		R	Integrated cross section (in barns)
QMU	91	R	Stored values of cosine of angle





SIBFIC ANGL

```

SUBROUTINE ANGLE
COMMON PI,HALFPI,FOURPI,RAD,SG2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30)
COMMON/FIDU/FI(30,15),D(30),JMP,NAME,SHELL,QV,EB,IZ
DIMENSION IT(91), QMU(91), SP(91), AD(91)
WRITE (6,2 )
2 FORMAT(///10X,38HLEGGRE COEFFICIENTS OF CROSS SECTION//
1 6X,1HJ,10X,4HD(J) // )
DO 4 J = 1, JMP
JL = J - 1
WRITE (6,3 ) JL, D(J)
3 FORMAT ( 17,5X, E15.8 )
4 CONTINUE
EL = QV - EB
WRITE (6,5) NAME, IZ, SHELL, EB, QV, EL
5 FORMAT (1H1////,33X,7HELEMENT,7X,13HATOMIC NUMBER, 13X,5HSHELL//
1 35X,A6,11X,13,17X,A6///16X,14HBINDING ENERGY,17X,
2 13HPHOTON ENERGY,11X,23HELECTRON KINETIC ENERGY//
3 3(14X,F12.7,4H KEV) /// )
IF ( JMP .EQ. 1 ) GO TO 24
WRITE (6,8)
8 FORMAT(25X,43HUNPOLARIZED CROSS SECTION (BARN/STERADIAN) //
1 16X,5HTHETA,15X,9HCOS THETA,18X,13HCROSS SECTION, 16X,
2 1UHANG. DIST. // )
SMAX = 0.0
DO 15 KMUQ = 1, 91
ITHETA = 2 * ( KMUQ - 1 )
IT(KMUQ) = ITHETA
THE=RAD*FLOAT (ITHETA)
FMUQ=COS (THE)
QMU(KMUQ) = FMUQ
PMI=1.0
PN=FMUQ
SIP = D(1) + FMUQ * D(2)
IF (JMP.EQ.2) GO TO 12
DO 10 J=3,JMP
FN=J-2
PPL = ( PN*FMUQ*(2.0*FN+1.0) - PMI*FN ) / ( FN+1.0 )
PMI=PN
PN=PPL
10 SIP = SIP + PPL * D(J)
12 SP(KMUQ) = SIP
IF ( SP(KMUQ) .GT. SMAX ) SMAX = SP(KMUQ)
15 CONTINUE
DO 20 KMUQ = 1, 91
AD(KMUQ) = SP(KMUQ) / SMAX
WRITE ( 6,18) IT(KMUQ), QMU(KMUQ), SP(KMUQ), AD(KMUQ)
18 FORMAT ( 15X,15,15X,F10.7,17X ,E15.8 , 15X, F10.7 )
20 CONTINUE
24 XSEC = FOURPI * D(1)
WRITE (6,25) XSEC
25 FORMAT (////30X27HINTEGRATED CROSS SECTION = E15.8, 6H BARN //)
RETURN
END

```

SUBROUTINE COEFS

Purpose: Computes Clebsch-Gordan coefficients.

Method: For computer computation economy, the requisite square roots of integers, factorials and square roots of factorials are stored in common. The routine uses explicit algebraic expressions for Clebsch-Gordan coefficients whose smallest angular momentum value is two or less (with appropriate permutation of indices). Otherwise the general formula is used, with a specialization for the parity Clebsch-Gordan coefficients. The input variables are double the angular momenta quantities, in order to use them in integer mode.

Subroutine called: None

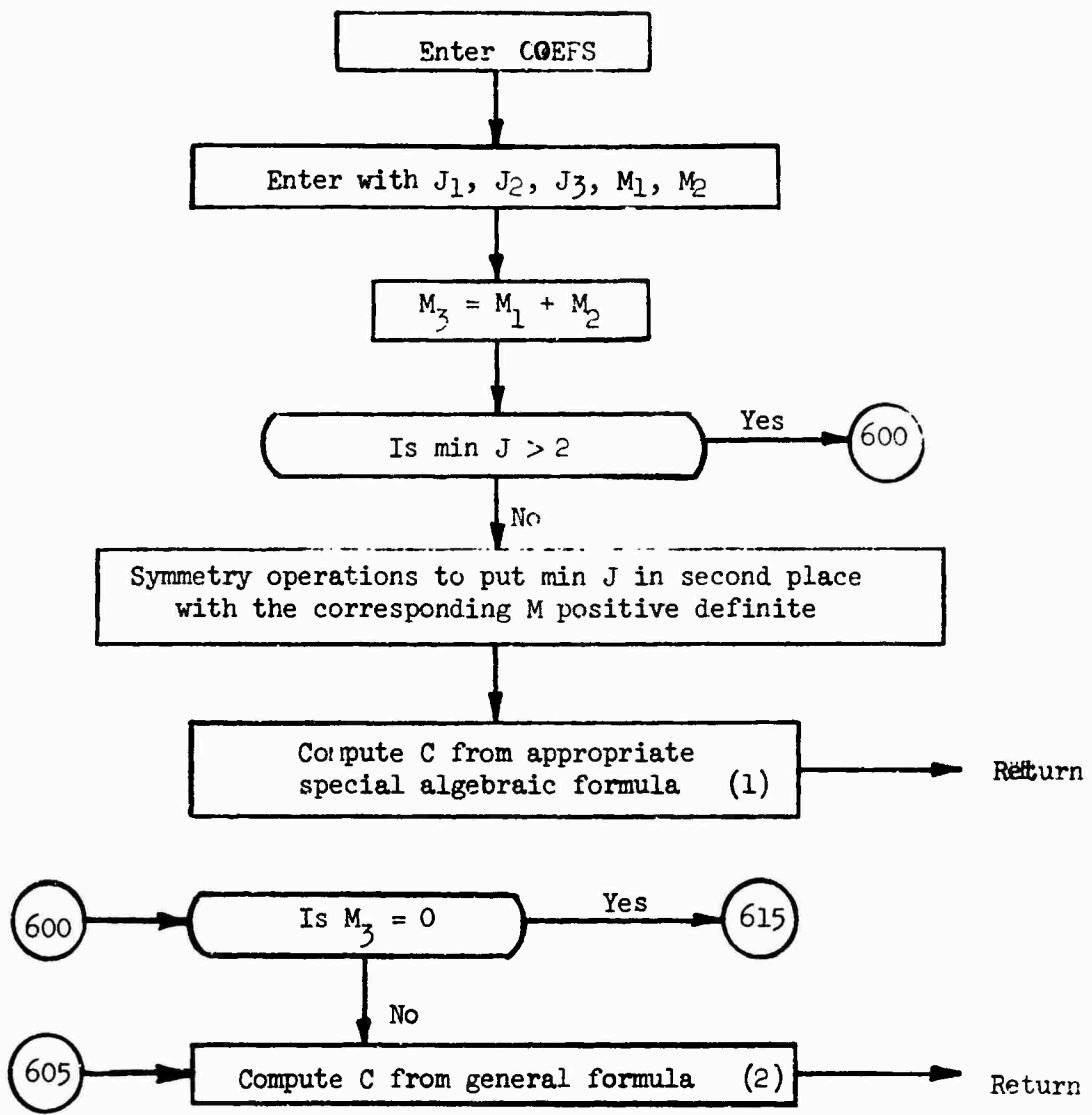
Subroutine called by: FILL, HUM, MUSS

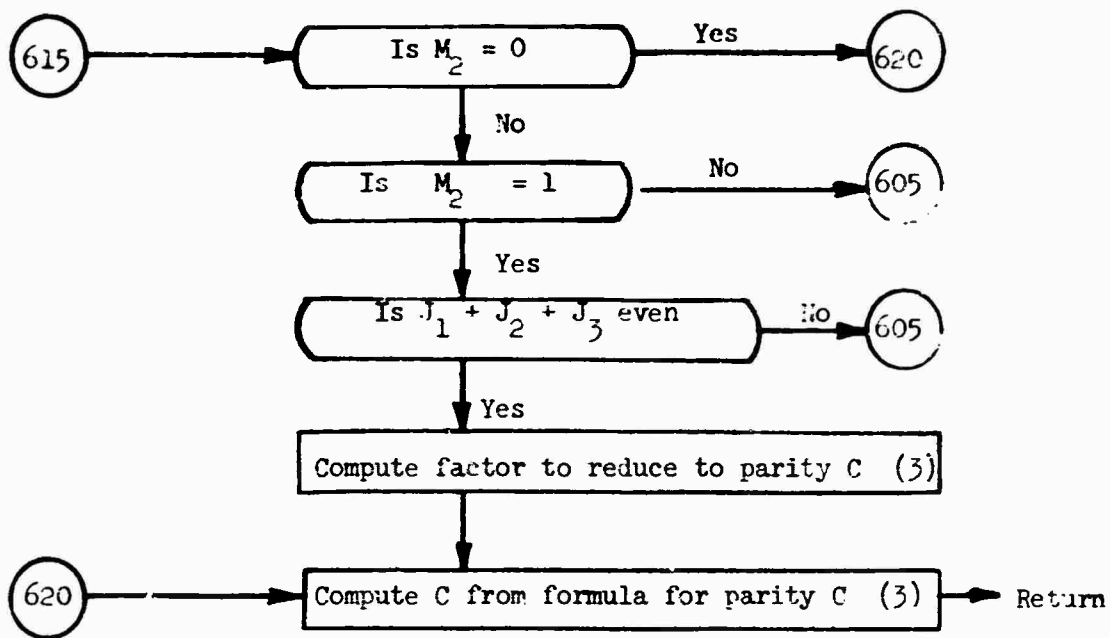
Labelled Common: FAC

Argument sequence: (J1, J2, J3, M1, M2, C)

Argument List:

Name	Dimension	Mode	Meaning
J1, J2, J3		I	Angular momenta
M1, M2		I	Magnetic quantum numbers
C		R	Clebsch-Gordan coefficient





References:

- (1) E. V. Condon and G. H. Shortley, Theory of Atomic Spectra, (Cambridge University Press, 1935).
- (2) G. Racah, Phys. Rev. 62, 438 (1942).
- (3) L. C. Biedenharn and M. E. Rose, Rev. Mod. Phys. 25, 729 (1953).

SUBPIC COEF

SUBROUTINE COEFS (J1,J2,J3,M1,M2,C)	COF00010
COMMON /FAC/F(67),RT(95),R(50)	COF00020
M3 = M1 + M2	COF00030
C = 0.0	COF00040
SIGM = 1.0	COF00050
JMIN = MIN0 (J1,J2,J3)	COF00060
IF (JMIN .GT. 4) GO TO 600	COF00070
IF (JMIN .EQ. J2) GO TO 220	COF00080
IF (JMIN .EQ. J3) GO TO 230	COF00090
210 L1 = J2	COF00100
L2 = J1	COF00110
L3 = J3	COF00120
LM1 = -M2	COF00130
LM2 = -M1	COF00140
LM3 = -M3	COF00150
GO TO 240	COF00160
220 L1 = J1	COF00170
L2 = J2	COF00180
L3 = J3	COF00190
LM1 = M1	COF00200
LM2 = M2	COF00210
LM3 = M3	COF00220
GO TO 240	COF00230
230 L1 = J1	COF00240
L2 = J3	COF00250
L3 = J2	COF00260
LM1 = M1	COF00270
LM2 = -M3	COF00280
LM3 = -M2	COF00290
SIGM = R(L2+1)/R(L3+1)	COF00300
IF (MOD (J1 - M1 , 4) .NE. 0)	SIGM = - SIGM
240 IF (LM2) 245, 250, 250	COF00310
245 LM1 = - LM1	COF00320
LM2 = - LM2	COF00330
LM3 = - LM3	COF00340
IF (MOD (L1 + L2 - L3 , 4) .NE. 0)	SIGM = - SIGM
250 JMIN = JMIN+1	COF00350
K = L1+LM3	COF00360
L = L1-LM3	COF00370
GO TO (255,260,300,700,400), JMIN	COF00380
255 IF (L1-L3) 800,256,800	COF00390
256 IF (LM1-LM3) 800,257,800	COF00400
257 C = SIGM	COF00410
GO TO 800	COF00420
260 IF (L3-L1-LM2) 265,280,270	COF00430
265 SIGM = -SIGM	COF00440
270 K = L	COF00450
280 KP1 = K + 1	COF00460
C = R(KP1)/R(2*L1+2)	COF00470
290 C = SIGM*C	COF00480
GO TO 800	COF00490
300 IF (L3-L1) 305,310,315	COF00500
305 IF (LM2) 800,325,330	COF00510
310 IF (LM2) 800,340,345	COF00520
315 IF (LM2) 800,355,360	COF00530
325 C = -R(L)*R(K)/(R(2*L1)*R(L1+1))	COF00540
GO TO 380	COF00550
330 C = R(L)*R(L+2)/(2.0*R(L1)*R(L1+1))	COF00560
GO TO 380	COF00570
340 C = FLOAT(LM3)/(R(L1)*R(L1+2))	COF00580
GO TO 380	COF00590
	COF00600
	COF00610

345	LOX = L+2				COF0062U
	C = -R(K)*R(LOX)/(R(2*L1)*R(L1+2))				COF00630
	GO TO 380				COF00640
355	LOX = L+2				COF00650
	LAX = K+2				COF00660
	C = R(LOX)*R(LAX)/(R(2*L1+2)*R(L1+2))				COF00670
	GO TO 380				COF00680
360	C = R(K)*R(K+2)/(2.0*R(L1+1)*R(L1+2))				COF00690
380	C = SIGM*C				COF00700
	GO TO 800				COF00710
400	M = LM2/2+1				COF00720
	J = (L3-L1)/2 +3				COF00730
	GO TO (480,510,540), M				COF00740
480	GO TO (485,490,495,500,505), J				COF00750
485	C = R(J)*R(L)*R(L-2)*R(K)*R(K-2)/(R(8)*R(L1-2)*R(L1-1)*R(L1)				COF00760
	1*R(L1+1))				COF00770
	GO TO 575				COF00780
490	C = -0.5*FLOAT(LM3)*R(6)*R(L)*R(K)/(R(L1)*R(L1-2)*R(L1+1)*R(L1+2))				COF00790
	GO TO 575				COF00800
495	C = 0.5 *FLUAT(3*LM3*LM3-L1*(L1+2))				COF00810
	1 / (R(L1)*R(L1-1)*R(L1+2)*R(L1+3))				COF00820
	GO TO 575				COF00830
500	LOX = L+2				COF00840
	LAX = K+2				COF00850
	C = 0.5*FLUAT(LM3)				COF00860
	1 *R(6)*R(LOX)*R(LAX)/(R(L1)*R(L1+1)*R(L1+2)*R(L1+4))				COF00870
	GO TO 575				COF00880
505	LOX = L+4				COF00890
	LAX = L+2				COF00900
	LLX = K+4				COF00910
	LXX = K+2				COF00920
	C = R(J)*R(LOX)*R(LAX)*R(LLX)*R(LXX)/(R(8)*R(L1+1)*R(L1+2)*R(L1+3)				COF00930
	1*R(L1+4))				COF00940
	GO TO 575				COF00950
510	GO TO (515,520,525,530,535), J				COF00960
515	C = -R(L+2)*R(L)*R(L-2)*R(K-2)/(2.0*R(L1-2)*R(L1-1)*R(L1)*R(L1+1))				COF00970
	GO TO 575				COF00980
520	C = 0.5*FLUAT(L1+2*LM3-2)				COF00990
	1 *R(L+2)*R(L)/(R(L1)*R(L1-2)*R(L1+1)*R(L1+2))				COF01000
	GO TO 575				COF01010
525	LOX = L+2				COF01020
	C = (1.0-FLOAT(LM3))*R(J)*R(LOX)*R(K)/(R(2*L1)*R(L1-1)*R(L1+2)				COF01030
	1*R(L1+3))				COF01040
	GO TO 575				COF01050
530	C = 0.5*FLUAT(2*LM3-L1-4)				COF01060
	1 *R(K+2)*R(K)/(R(L1)*R(L1+1)*R(L1+2)*R(L1+4))				COF01070
	GO TO 575				COF01080
535	LOX = L+4				COF01090
	C = R(LOX)*R(K+4)*R(K+2)*R(K)/(2.0*R(L1+1)*R(L1+2)*R(L1+3)*R(L1+4))				COF01100
	GO TO 575				COF01110
540	GO TO (545,550,555,560,565), J				COF01120
545	C = R(L-2)*R(L)*R(L+2)*R(L+4)/(4.0*R(L1)*R(L1-2)*R(L1-1)*R(L1+1))				COF01130
	GO TO 575				COF01140
550	C = -R(K-2)*R(L)*R(L+2)*R(L+4)/(2.0*R(L1)*R(L1-2)*R(L1+2)*R(L1+1))				COF01150
	GO TO 575				COF01160
555	LOX = L+2				COF01170
	LAX = L+4				COF01180
	C = R(J)*R(K-2)*R(K)*R(LOX)*R(LAX)/(R(8)*R(L1)*R(L1-1)*R(L1+2)				COF01190
	1*R(L1+3))				COF01200
	GO TO 575				COF01210
560	LUX = L+4				COF01220
	C = -R(K-2)*R(K)*R(K+2)*R(LOX)/(2.0*R(L1)*R(L1+2)*R(L1+4)*R(L1+1))				COF01230

CO TO 575	COF01240
565 C=R(K-2)*R(K)*R(K+2)*R(K+4)/(4.0*R(L1+1)*R(L1+2)*R(L1+3)*R(L1+4))	COF01250
575 C = SIGM*C	COF01260
GO TO 800	COF01270
700 M = (LM2+1)/2	COF01280
J = (L3-L1+5)/2	COF01290
GO TO (710, 740) , M	COF01300
710 GO TO (720, 725, 730, 735) , J	CGF01310
720 C = R(J)*R(K-1)*R(L-1)*R(L+1)/(R(8)*R(L1)*R(L1-1)*R(L1+1))	COF01320
GO TO 780	COF01330
725 C = -FLOAT((L1+3*LM3-1)/2)*R(L+1)/(R(2)*R(L1-1)*R(L1+1)*R(L1+2))	COF01340
GO TO 780	COF01350
730 KP1 = K + 1	COF01360
C = -FLOAT((J-3*LM3+L1)/2)*R(KP1)/(R(2)*R(L1)*R(L1+1)*R(L1+3))	COF01370
GO TO 780	COF01380
735 LOX = L+3	COF01390
KP1 = K + 1	COF01400
KP3 = K + 3	COF01410
C = R(J)*R(KP1)*R(KP3)*R(LOX)/(R(8)*R(L1+1)*R(L1+2)*R(L1+3))	COF01420
GO TO 780	COF01430
740 GO TO (750, 755, 760, 765) , J	COF01440
750 C = -R(L-1)*R(L+1)*R(L+3)/(R(8)*R(L1)*R(L1-1)*R(L1+1))	COF01450
GO TO 780	COF01460
755 LOX = L+3	COF01470
LAX = L+1	COF01480
C = R(J)*R(K-1)*R(LAX)*R(LOX)/(R(8)*R(L1-1)*R(L1+1)*R(L1+2))	COF01490
GO TO 780	COF01500
760 LOX = L+3	COF01510
C = -R(J)*R(K-1)*R(K+1)*R(LOX)/(R(8)*R(L1)*R(L1+1)*R(L1+3))	COF01520
GO TO 780	COF01530
765 C = R(K-1)*R(K+1)*R(K+3)/(R(8)*R(L1+1)*R(L1+2)*R(L1+3))	COF01540
780 C = C*SIGM	COF01550
GO TO 800	COF01560
C THIS IS THE BEGINNING OF COMPUTATION OF C-COEFFICIENT	COF01570
C USING THE GENERAL EXPRESSION.	COF01580
600 L1 = J1+J2-J3+1	COF01590
L2 = J1-J2+J3+1	COF01600
L3 = -J1+J2+J3+1	COF01610
L10 = J1+J2+J3+3	COF01620
IF (M3 .EQ. 0) GO TO 615	COF01630
605 L4 = J1+M1+1	COF01640
L5 = J1-M1+1	COF01650
L6 = J2+M2+1	COF01660
L7 = J2-M2+1	COF01670
L8 = J3+M3+1	COF01680
L9 = J3-M3+1	COF01690
ST = RT(L10) / (RT(L1)*RT(L4)*RT(L5))	COF01700
ST = ST / (RT(L6) * RT(L7))	COF01710
ST = ST / (R(J3+1)*RT(L2)*RT(L3))	COF01720
ST = ST / (RT(L8) * RT(L9))	COF01730
N7 = L1-L7	COF01740
N4 = L1-L4	COF01750
MIN = MAXU (0,N4,N7)	COF01760
MAX = MINU (L1,L5,L6)	COF01770
IF (MOD(MIN,4).NE.0) SIGM=-1.0	COF01780
MIN = MIN+1	COF01790
N1 = L1+1	COF01800
N5 = L5+1	COF01810
N6 = L6+1	COF01820
SUM = 0.0	COF01830
DO 610 LZ=MIN,MAX,2	COF01840
N1L = N1-LZ	COF01850

N5L = N5-L2		COF01860
N6L = N6-L2		COF01870
N4L = -N4+L2		COF01880
N7L = -N7+L2		COF01890
TERM = ST * F(L2) * F(N1L) * F(N5L) * F(N6L) * F(N4L) * F(N7L)		COF01900
C = C + SIGM / TERM		COF01910
610 SIGM = -SIGM		COF01920
GO TO 800		COF01930
615 IF (M2 .EQ. 0)	GO TO 620	COF01940
IF (IABS(M2) .NE. 2)	GO TO 605	COF01950
JMOD = MOD ((L10 + 1) , 4)		COF01960
IF (JMOD .NE. 0)	GO TO 605	COF01970
ST = J3 * (J3 + 2) - J1 * (J1 + 2) - J2 * (J2 + 2)		COF01980
SIGM = 0.5 * SIGM * ST / (R(J1)*R(J1 + 2)*R(J2)*R(J2 + 2))		COF01990
620 JMOD = MOD ((L1 - 1) , 8)		COF02000
IF (JMOD .NE. 0)	SIGM = - SIGM	COF02010
L4 = (L1 + 1) / 2		COF02020
L5 = (L2 + 1) / 2		COF02030
L6 = (L3 + 1) / 2		COF02040
L7 = (L10 - 1) / 2		COF02050
C = SIGM * R(J3 + 1) * F(L7) / (F(L4)*F(L5)*F(L6))		COF02060
C = C * RT(L1) * RT(L2) * RT(L3) / RT(L10)		COF02070
800 RETURN		COF02080
END		COF02090

This page is intentionally left blank.

SUBROUTINE DERIV

Purpose: Computes for the Runge-Kut a integration the derivatives of the bound state wavefunctions and the integrands of the matrix elements up to one-half Bohr radius.

Method: Calculates the derivative of the radial components from the coupled Dirac radial equations. In evaluating the integrand of the matrix elements the r^Y factor is restored if $r < 1$.

Subroutine called: SPHBES

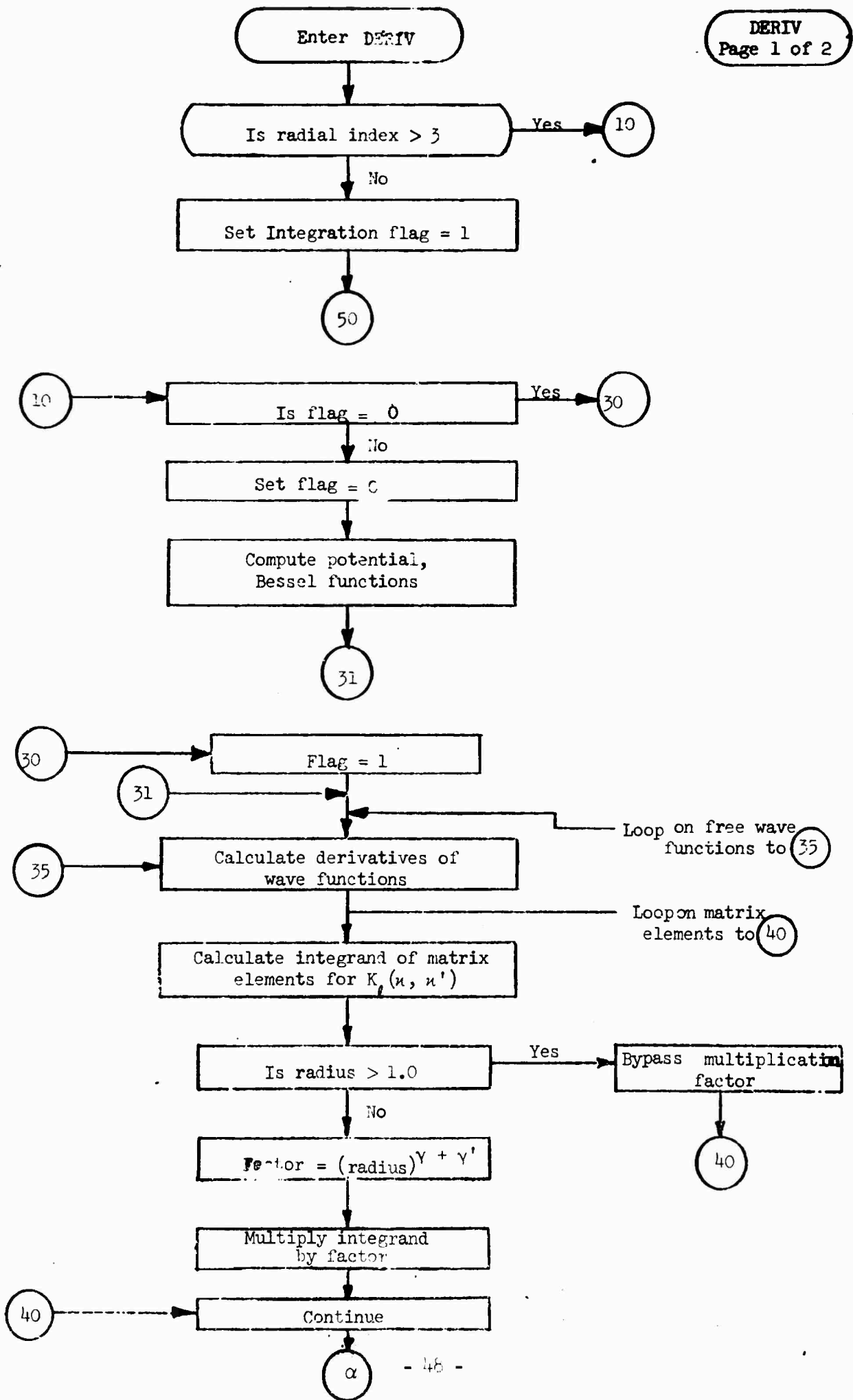
Subroutine called by: RKUT, RADINT

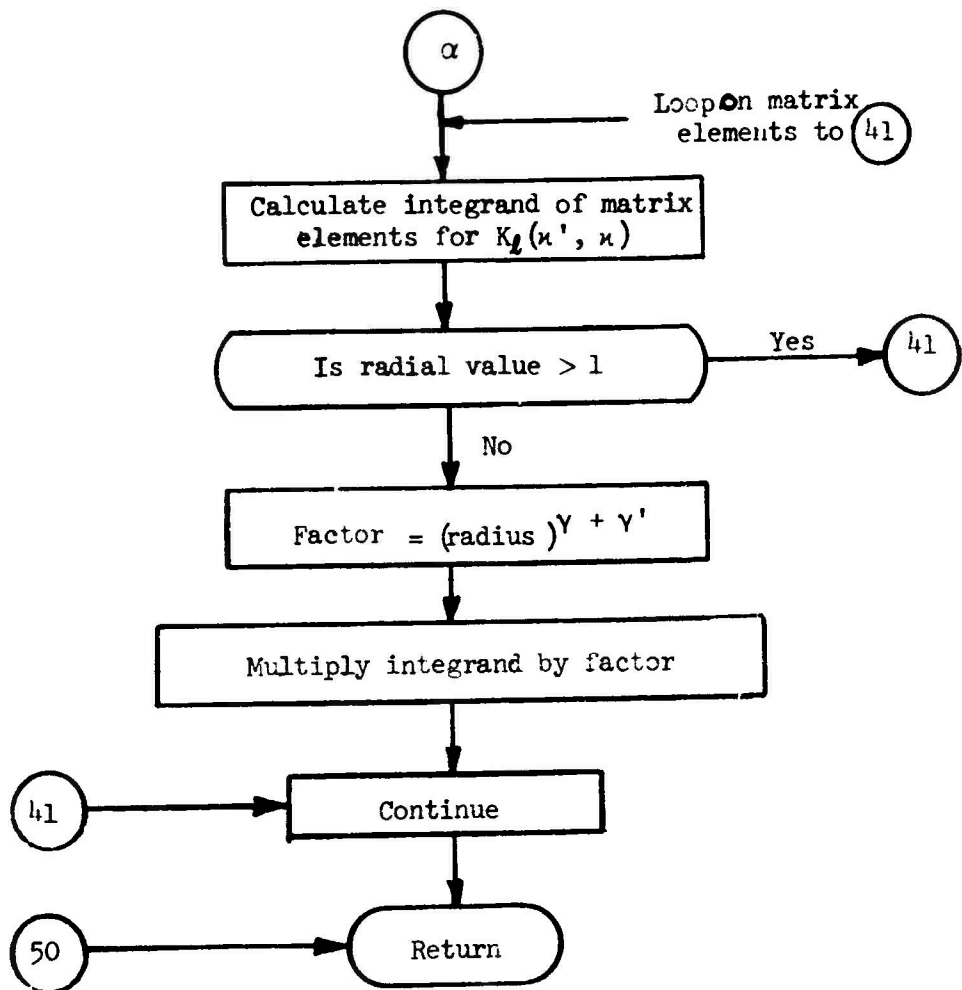
Variables in unlabelled Common: PI, HALFPI, FØURPI, RAD, SQZ, Q, ZA, ZAZA,
EFN, EGN, V, CG, GAM

Labelled Common: BESSEL, DEFUNC, LIMIT, TAPES, VECT

Local Variables:

Name	Dimension	Mode	Meaning
Z		R	Photon momentum * radius
I		I	Indexing variable
A		R	Sum of gammas of bound and free state electron





SIBPIC DER1

SUBROUTINE DER1V

DER00010

C COMPUTES DERIVATIVES

DER00020

COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,C6(30),GAM(30) DER00030

COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15) DER00040

COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HDER00050

COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB DER00060

COMMON /TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN DER00070

COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB DER00080

IF (NTAB.GT.3) GO TO 10 DER00090

NEW = 1 DER00100

GO TO 50 DER00110

10 IF (NEW.EQ.0) GO TO 30 DER00120

NEW = 0 DER00130

V=-SCF(NTAB)/X(NTAB) DER00140

Z = Q*X(NTAB) DER00150

CALL SPHRES (Z) DER00160

GO TO 31 DER00170

30 NEW = 1 DER00180

31 DO 35 N=1,K2M DER00190

DF(N) = CF(N)*F(N)/X(NTAB)-(EFN-V)*G(N) DER00200

35 DG(N) = CG(N)*G(N)/X(NTAB)+(EGN-V)*F(N) DER00210

DO 40 N=1,NK DER00220

I = KG(N) DER00230

L = LBES(N) DER00240

DFK(N)=B(L)*G(I)*FB(NTAB) DER00250

IF (X(NTAB).GT.1.0) GO TO 40 DER00260

A = GAM(I)+GAMB DER00270

DFK(N) = DFK(N)*(X(NTAB)**A) DER00280

40 CONTINUE DER00290

DO 41 N=1,NKP DER00300

I = KF(N) DER00310

L = LBS(N) DER00320

DFKP(N)=B(L)*F(I)*GB(NTAB) DER00330

IF (X(NTAB).GT.1.0) GO TO 41 DER00340

A = GAM(I)+GAMB DER00350

DFKP(N) = DFKP(N)*X(NTAB)**A DER00360

41 CONTINUE DER00370

50 RETURN DER00380

END DER00390

SUBROUTINE FILL

Purpose: Computes $\phi(\kappa, \lambda)$

Method: $\phi(\kappa, \lambda)$ is computed in two passes, one for $K_{\ell}(\kappa \kappa')$ contributions the other for $K_{\ell}(\kappa' \kappa)$ and then the two pieces are added in subroutine HUM to yield ϕ . The selection rules are examined for each matrix element contribution to determine what values of $(\lambda - \ell)$ are allowed. If $\lambda = \ell \pm 1$, f can assume only the one value $f = \lambda \mp 1/2$; if $\lambda = \ell$ both the preceding values of f are possible. In the final run-through the remaining selection rules required for R are checked, R is computed from explicit algebraic expressions for the Racah coefficient with $J_5 = 1/2$, the corresponding Clebsch-Gordan coefficient called and $\phi(\kappa, \lambda)$ formed with appropriate ℓ summation. The indices used for ϕ are λ and K (K is a positive integer uniquely related to κ).

Subroutine called: CØEFS

Subroutine called by: HUM

Labelled Common: FAC, LIMIT, QUANT

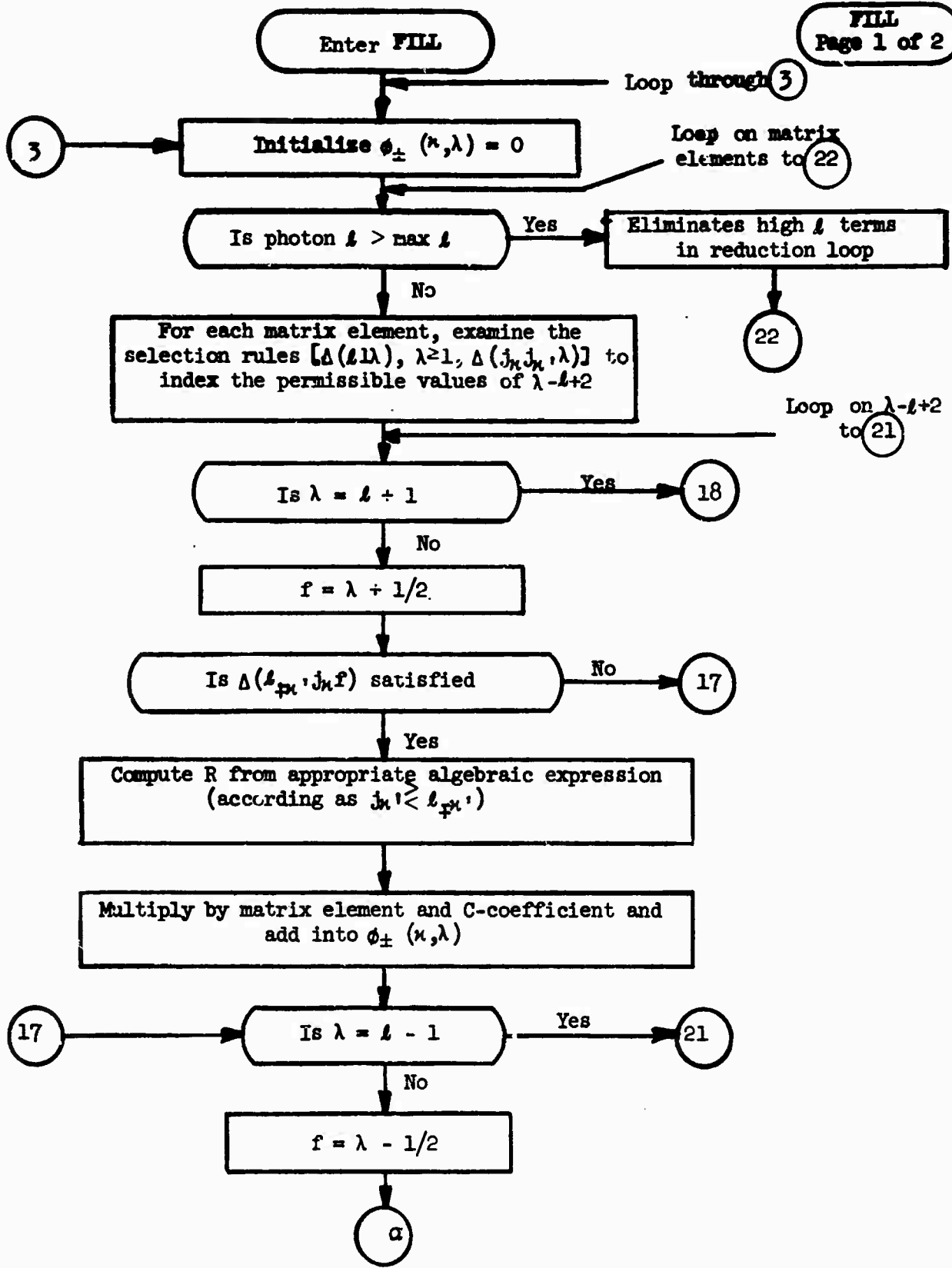
Argument sequence: (TK, KW, LB, NT, LP, FI)

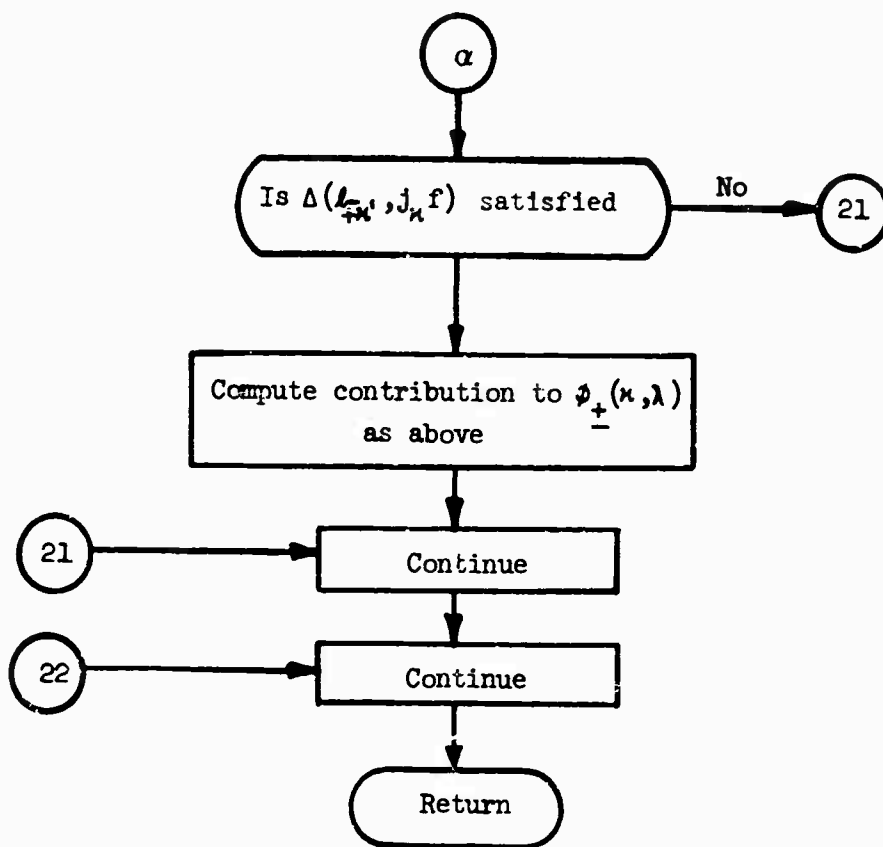
Argument List:

Name	Dimension	Mode	Meaning
TK	200	R	Matrix elements
KW	200	I	Index for κ values in matrix elements
LB	200	I	Photon angular momentum + 1 for matrix elements
NT		I	Number of matrix elements $K_{\ell}(\kappa \kappa')$ or $K_{\ell}(\kappa' \kappa)$
LP		I	$\ell_{-\kappa}$, or ℓ_{κ} ,
FI	30 x 15	R	$\phi_{+}(\kappa, \lambda)$ or $\phi_{-}(\kappa, \lambda)$

Local Variables:

Name	Dimension	Mode	Meaning
LMP		I	Max photon angular momentum + 1
LA		I	λ
K		I	Index of free electron state
LD		I	Twice bound electron l_{+n}
N		I	Index of matrix element
L		I	Photon angular momentum
JC		I	Twice free electron j_{κ}
NA, NB		I	Loop index for the range of $(\lambda - l)$
LAM		I	$2 * \lambda$
LEF		I	$2 * (\lambda \pm 1/2)$
NL		I	$(\lambda - l) + 2$
IR, IS		I	Terms in R
R		R	$R(j_{\kappa}, l_{+n}, \lambda f j_{\kappa})$
C		R	Clebsch-Gordan coefficient
JPL		I	$2 \times j_{\kappa} + 2 \times j_{\kappa} - 2 \times$ photon angular momentum
JML		I	$ 2 \times j_{\kappa} - 2 \times j_{\kappa} - 2 \times$ photon angular momentum





SIBPIC FILE

```

SUBROUTINE FILL (TK,KW,LB,NT,LP,FI)
COMMON /FAC/FACT(67),RTFAC(95),ROOT(50)
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LKKB,NTAB
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)
DIMENSION IK(200),KW(200),LB(200),FI(30,15)
LMP=LM+1
DO 3 LA=1,LMP
DO 3 K=1,K2M
3 FI(K,LA)=0.0
LD=2*LP
DO 22 N = 1, NT
L=LB(N)-1
IF (L.GT.LM) GO TO 22
K=KW(N)
JC=JK(K)
IF (L.EQ.0) GO TO 8
L2=2*L
JPL=JKB+JC-L2
JML=IABS (JKB-JC)-L2
IF (JPL.LT.2) GO TO 9
4 IF (L.EQ.1) GO TO 6
IF (JML.GT.(-2)) GO TO 6
NA=1
NB=3
GO TO 14
6 IF (JML.GT.0) GO TO 8
NA=2
NB=3
GO TO 14
8 NA=3
NB=3
GO TO 14
9 IF (L.EQ.1) GO TO 13
IF (JPL.GE.0) GO TO 11
NA=1
NB=1
GO TO 14
11 IF (JML.GT.(-2)) GO TO 13
NA=1
NB=2
GO TO 14
13 NA=2
NB=2
14 DO 21 NL=NA,NB
LA=L-2+NL
LAM=2*LA
IF (NL.EQ.3) GO TO 18
LEF=LAM+1
IF ((LD+JC).LT.LEF) GO TO 17
IF (IABS(LD-JC).GT.LEF) GO TO 17
IF (JKB.GT.LD) GO TO 15
IK=JKB+JC+LAM+4
IS=JKB-JC+LAM+2
R=-ROOT(IK)*ROOT(IS)*ROOT(LA)
GO TO 16
15 IS=JC+JKB-LAM
IF (IS.EQ.0) GO TO 17
IR=JC-JKB+LAM+2
R=ROOT(IR)*ROOT(IS)*ROOT(LA)
16 CALL COEFS (LEF,LD,JC,1,0,C)
FI(K,LA)=FI(K,LA)+TK(N)*R*C

```

FIL00010
 FIL00020
 FIL00030
 FIL00040
 FIL00050
 FIL00060
 FIL00070
 FIL00080
 FIL00090
 FIL00100
 FIL00110
 FIL00120
 FIL00130
 FIL00140
 FIL00150
 FIL00160
 FIL00170
 FIL00180
 FIL00190
 FIL00200
 FIL00210
 FIL00220
 FIL00230
 FIL00240
 FIL00250
 FIL00260
 FIL00270
 FIL00280
 FIL00290
 FIL00300
 FIL00310
 FIL00320
 FIL00330
 FIL00340
 FIL00350
 FIL00360
 FIL00370
 FIL00380
 FIL00390
 FIL00400
 FIL00410
 FIL00420
 FIL00430
 FIL00440
 FIL00450
 FIL00460
 FIL00470
 FIL00480
 FIL00490
 FIL00500
 FIL00510
 FIL00520
 FIL00530
 FIL00540
 FIL00550
 FIL00560
 FIL00570
 FIL00580
 FIL00590
 FIL00600
 FIL00610

```

17 IF (NL.EQ.1)      GO TO 21
18 LEF=LAM-1
   IF ((LD+JC).LT.LEF)      GO TO 21
   IF ((ABS(LU-JC).GT.LEF)   GO TO 21
   IF (JKB.GT.LD)      GO TO 19
   IS=JC-JKB+LAM
   IF (IS.EQ.0)      GO TO 21
   IR=JC+JKB-LAM+2
   GO TO 20
19 IS=JKB-JC+LAM
   IF (IS.EQ.0)      GO TO 21
   IR=JKB+JC+LAM+2
20 R=ROOT(IR)*ROOT(IS)*ROOT(LA+1)
   CALL COEFS (LEF,LU,JC,1,0,C)
   FI(K,LA)=FI(K,LA)+TK(IN)*R*C
21 CONTINUE
22 CONTINUE
   RETURN
   END

```

```

FIL00620
FIL00630
FIL00640
FIL00650
FIL00660
FIL00670
FIL00680
FIL00690
FIL00700
FIL00710
FIL00720
FIL00730
FIL00740
FIL00750
FIL00760
FIL00770
FIL00780
FIL00790
FIL00800

```


SUBROUTINE HUM

Purpose: Computes $H(\kappa, \mu')$

Method: For every $\kappa > 0$, the selection rules on the Clebsch-Gordan coefficient are examined to determine the allowed range of λ values. The maximum (positive) value of μ' and its minimum (largest negative) value are computed and indexed for subsequent use. Since j_κ depends only on the absolute value of κ , the Clebsch-Gordan coefficient is the same for $(-\kappa)$ as for κ . Over the allowed range of positive μ' , the Clebsch-Gordan coefficients are computed for given λ and κ , multiplied in turn by $\phi(\kappa, \lambda)$ and $\phi(-\kappa, \lambda)$ to obtain corresponding contributions to $H(\kappa, \mu')$ and $H(-\kappa, \mu')$, and the products are summed over λ . The results are denoted by $HF(K, M)$ where K is a positive integer indexing κ , and $M = \mu' + 1/2$. The procedure is then repeated for μ' negative, leading to $HFM(K, M)$, where K is as above and $M = -\mu' + 1/2$. The explicit separation of positive and negative μ' terms is useful later on.

Subroutines called: COEFS, FILL

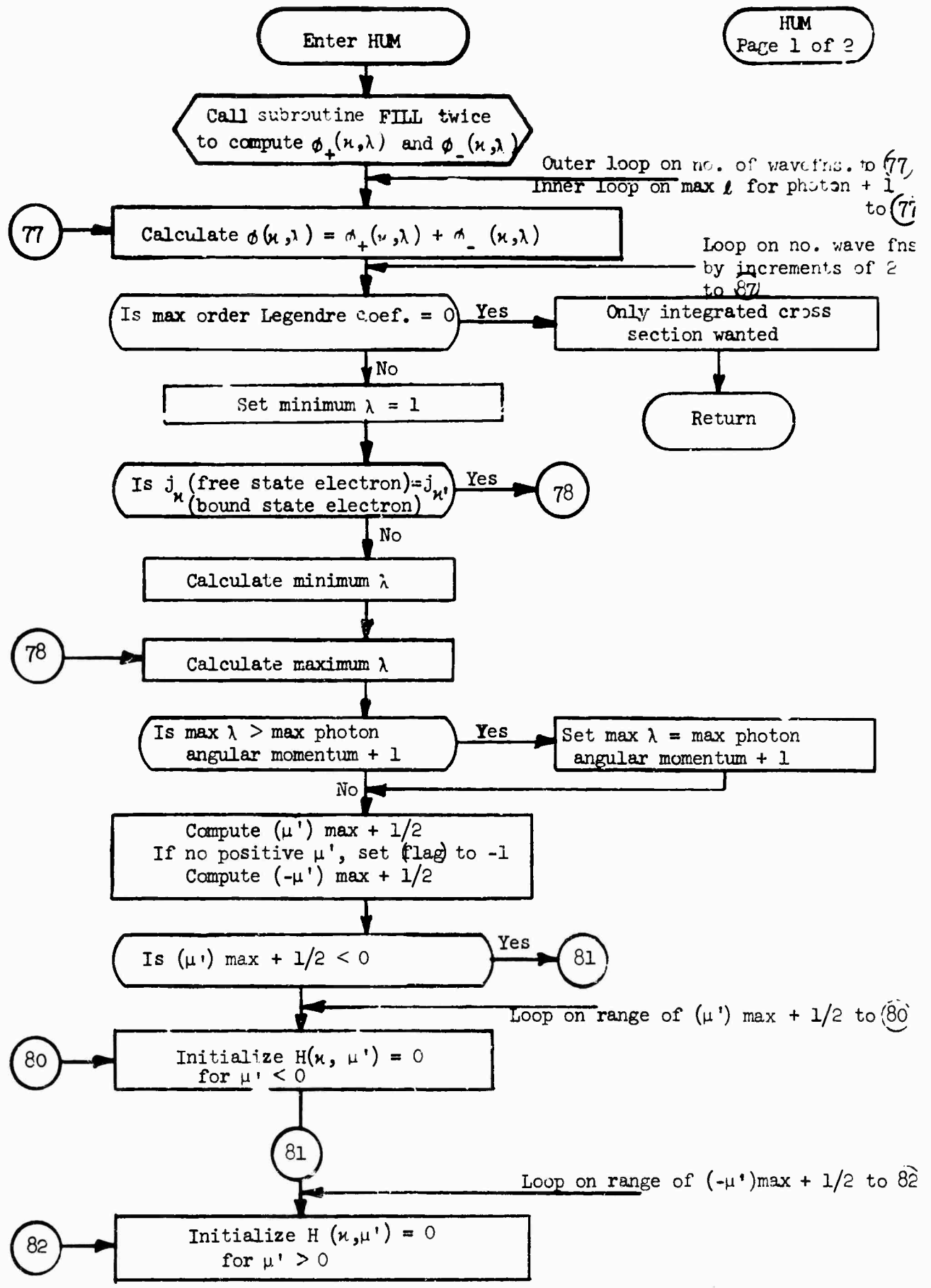
Subroutine called by: RADINT

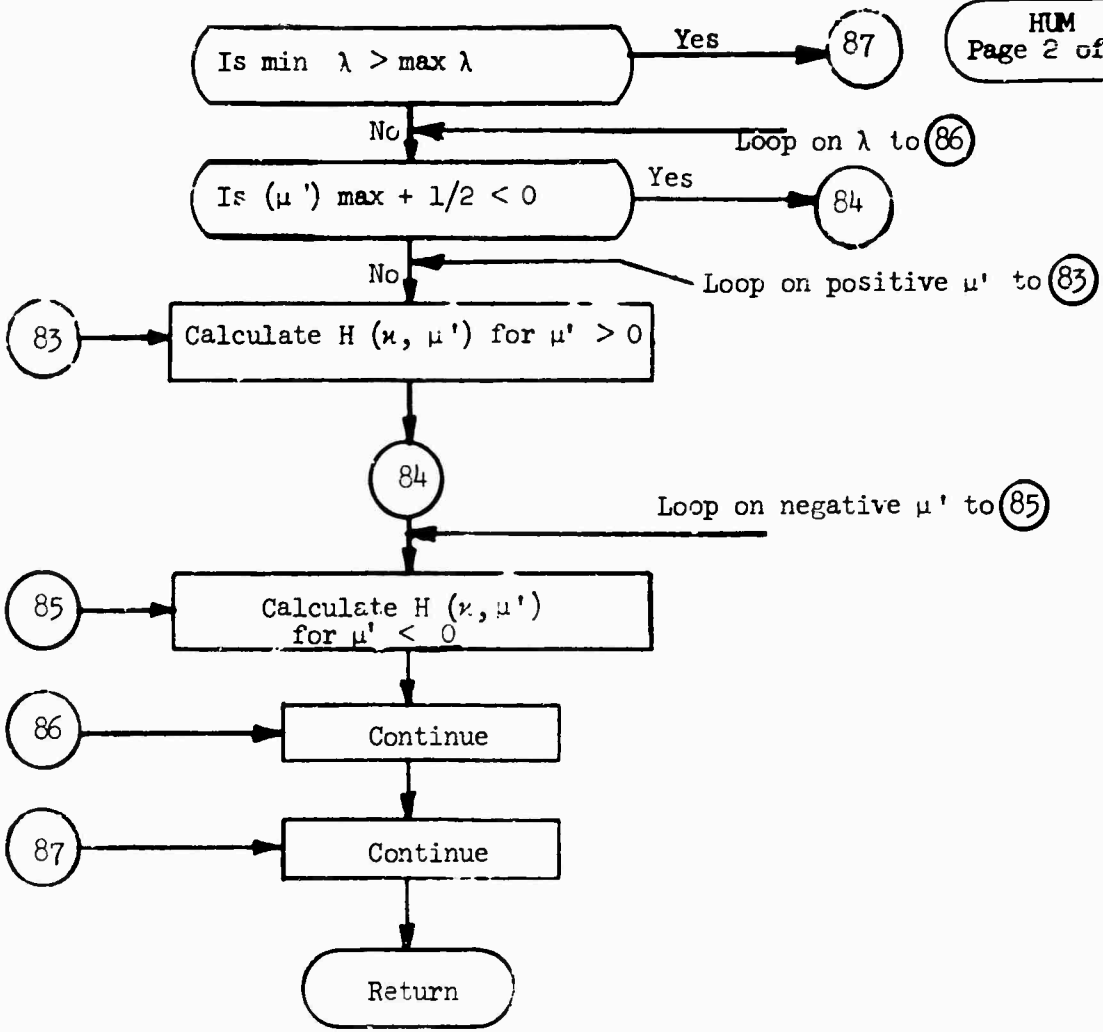
Labelled Common: FIDØ, LIMIT, MAT, QUANT, TRANS, VECT

Local Variables:

Name	Dimension	Mode	Meaning
LMP		I	Maximum photon angular momentum + 1
K		I	Loop index for bound electron state
LA			λ
JC		I	Twice j_κ (free electron state)
LAD		I	Minimum λ from selection rules

Name	Dimension	Mode	Meaning
LAP		I	Maximum λ from selection rules
JP0S		I	$(\mu')_{\max} + 1/2$ provided $\mu' > 0$ permitted, -1 otherwise
JNEG		I	$(-\mu')_{\max} + 1/2$
M		I	Loop index for μ'
LAM		I	Twice λ
MU		I	Twice μ'





SIBFIC HUMM

SUBROUTINE HUM	HUM00010
COMMON/FI00/FI(30,15),D(30),JMP,NAME,SHELL,QV,ES,IZ	HUM00020
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	HUM00030
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT	HUM00040
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)	HUM00050
COMMON/TRANS/HF(30,15),HFM(30,15),JNG(30),JPS(30)	HUM00060
COMMON/VECI/KF(200),KG(200),LBES(200),LBS(200),LKB	HUM00070
DIMENSION FI(30,15),FTP(30,15)	HUM00080
LMP=LM+1	HUM00090
CALL FILL (FK,KG,LBES,NK,LMKB,FT)	HUM00100
CALL FILL (FKP,KF,LBS,NKP,LKB,FTP)	HUM00110
DO 77 K=1,K2M	HUM00120
DO 77 LA=1,LMP	HUM00130
// FI(K,LA)=FI(K,LA)+FTP(K,LA)	HUM00140
IF (JM .EQ. 0)	RETURN
DO 87 K=1,K2M,2	HUM00150
KP = K + 1	HUM00160
JC=JK(K)	HUM00170
LAD=1	HUM00180
IF (JC.EQ.JKB) GO TO 78	HUM00190
LAD=IABS (JC-JKB)/2	HUM00200
78 LAP = (JC+JKB)/2	HUM00210
IF (LAP .GT. LMP)	LAP = LMP
JPOS=JC-2	HUM00230
IF (JC.LT.4) GO TO 79	HUM00240
JPOS=MIN0 (JKB,JPOS)	HUM00250
JPOS=(JPOS+1)/2	HUM00260
79 JNEG=MIN0 (JKB,(JC+2))	HUM00270
JNEG=(JNEG+1)/2	HUM00280
JNG(K)=JNEG	HUM00290
JPS(K)=JPOS	HUM00300
JNG(KP)=JNEG	HUM00310
JPS(KP)=JPOS	HUM00320
IF (JPOS.LT.0) GO TO 81	HUM00330
DO 80 M=1,JPOS	HUM00340
HF(K,M) = 0.0	HUM00350
80 HF(KP,M) = 0.0	HUM00360
81 DO 82 M=1,JNEG	HUM00370
HFM(K,M) = 0.0	HUM00380
82 HFM(KP,M) = 0.0	HUM00390
IF (LAD.GT.LAP) GO TO 87	HUM00400
DO 86 LA=LAD,LAP	HUM00410
LAM=2*LA	HUM00420
IF (JPOS.LI.0) GO TO 84	HUM00430
DO 83 M=1,JPOS	HUM00440
MU=2*M-1	HUM00450
CALL COEFS (LAM,JKB,JC,2,MU,C)	HUM00460
HF(K,M) = HF(K,M) + FI(K,LA) * C	HUM00470
83 HF(KP,M) = HF(KP,M) + FI(KP,LA) * C	HUM00480
84 DO 85 M=1,JNEG	HUM00490
MU=1-2*M	HUM00500
CALL COEFS (LAM,JKB,JC,2,MU,C)	HUM00510
HFM(K,M) = HFM(K,M) + FI(K,LA) * C	HUM00520
85 HFM(KP,M) = HFM(KP,M) + FI(KP,LA) * C	HUM00530
86 CONTINUE	HUM00540
87 CONTINUE	HUM00550
RETURN	HUM00560
END	HUM00570

This page is intentionally left blank.

SUBROUTINE INTERP

Purpose: Interpolates on the bound-state tabulations for radii greater than one-half Bohr unit where the integration grid is much finer than the table, to obtain intermediate values of the bound-state wavefunctions and corresponding potential.

Method: Linear interpolation between successive entries in table.

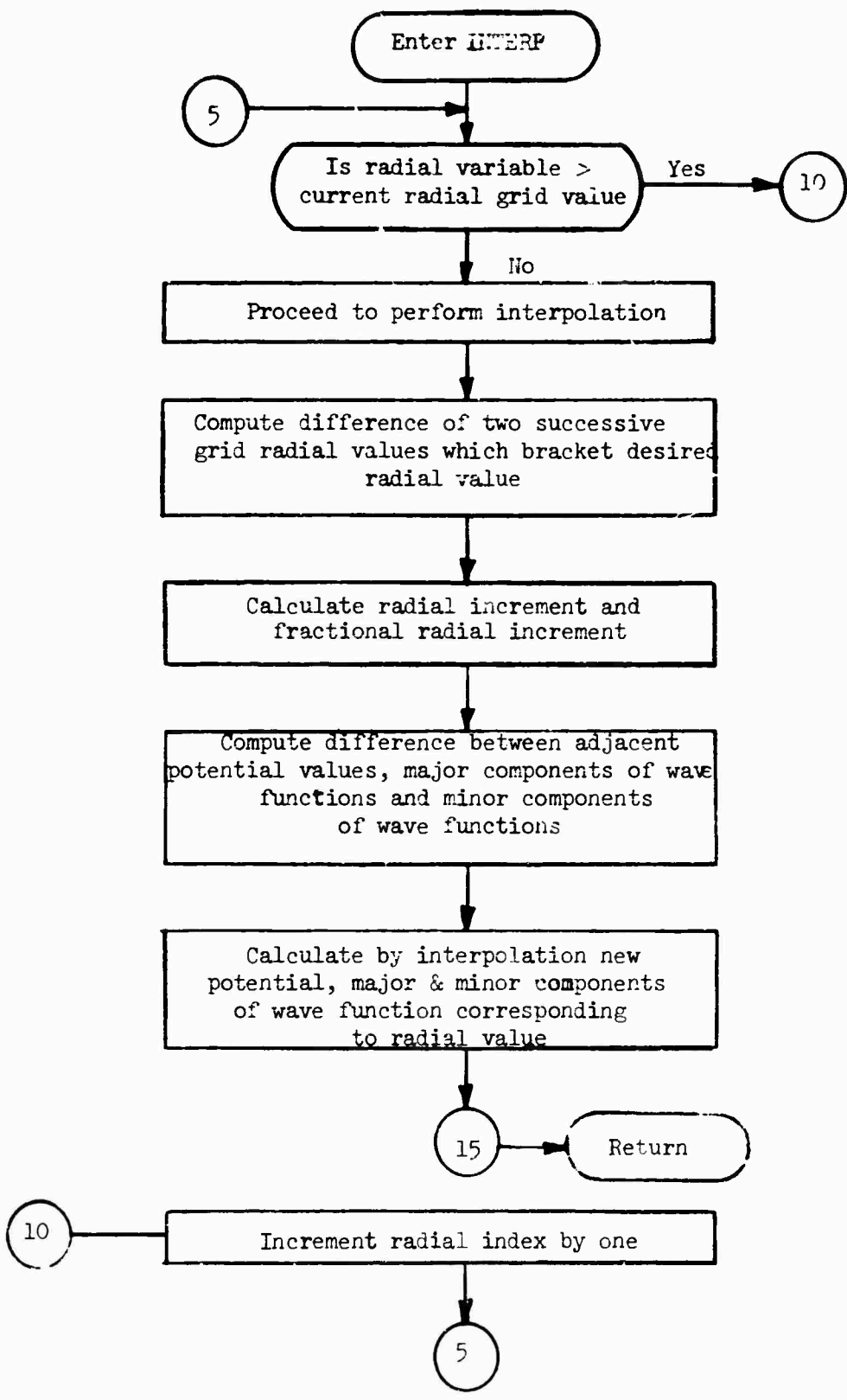
Subroutine called: None

Subroutine called by: XDERIV

Labelled Comm.: LIMIT, ϕ NWARD, TAPES

Local Variables:

Name	Dimension	Mode	Meaning
DX		R	Difference between two successive tabulated radial values
DL		R	Radial increment; difference between integrating radius and lower grid point
QU ϕ T		R	Fractional radial increment
DV		R	Difference between two successive tabulated potential values
DGB		R	Difference between two successive tabulated values of "large" component of wavefunction.
DFB		R	Difference between two successive tabulated values of "small" component of wavefunction.



SUB-10 INTP

```

SUBROUTINE INTERP
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB
COMMON /ONWARD/RX,SCX,GBX,FBX
COMMON/TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN
5 IF (RX.GT.X(NTAB+1)) GO TO 10
UX = X(NTAB+1)-X(NTAB)
DL = RX-X(NTAB)
QUOT = DL/UX
UV = SCF(NTAB+1)-SCF(NTAB)
UGB = GB(NTAB+1)-GB(NTAB)
DFB = FB(NTAB+1)-FB(NTAB)
SCX = SCF(NTAB)+QUOT*UV
GBX = GB(NTAB)+QUOT*UGB
FBX = FB(NTAB)+QUOT*DFB
GO TO 15
10 NTAB = NTAB+1
GO TO 5
15 RETURN
END

```

```

INT00010
INT00020
INT00030
INT00040
INT00050
INT00060
INT00070
INT00080
INT00090
INT00100
INT00110
INT00120
INT00130
INT00140
INT00150
INT00160
INT00170
INT00180
INT00190

```

This page is intentionally left blank.

SUBROUTINE LEGEND

Purpose: Computes the Legendre coefficients of the cross section.

Method: For $j = 0$, this consists of carrying out the sum

$$D_0 = \frac{\pi^2 e^2 w}{2\epsilon} \sum_{\lambda} \frac{1}{2\lambda + 1} \sum_{\kappa} \beta^2(\kappa, \lambda) \text{ over all } \kappa \text{ and } \lambda$$

(The ϕ 's have been initialized.) For $j > 0$, subroutine MUSS

is called where the $T_j(\kappa, \kappa')$ of the sum

$$D_j = \frac{\pi^2 e^2 w}{2\epsilon} (-1)^j \sum_{\kappa \kappa'} \cos(\delta_{\kappa} - \delta_{\kappa'}) T_j(\kappa, \kappa')$$

is performed.

The summation $(-1)^j \sum_{\kappa \kappa'} \cos(\delta_{\kappa} - \delta_{\kappa'}) T_j(\kappa, \kappa')$ is subject to the selection rules $\Delta(j_{\kappa}, j_{\kappa'}, j)$, $\Delta(l_{\kappa}, l_{\kappa'}, j)$ and $l_{\kappa} + l_{\kappa'} + j = \text{even}$ integer. The diagonal terms in the double sum are done first

(with the cosine equal to unity), carried over $j_{\kappa} > 1/2$ and

contributing to even j terms only. Since the off-diagonal terms

are symmetric in κ and κ' , twice the sum with $\kappa' < \kappa$ is taken.

For given κ and κ' , the smallest j for which there can be a

contribution is $|l_{\kappa} - l_{\kappa'}|$ provided $|j_{\kappa} - j_{\kappa'}|$ is not larger;

otherwise $j = |j_{\kappa} - j_{\kappa'}|$ has the wrong parity and the minimum

j value is $|j_{\kappa} - j_{\kappa'}| + 1 = |l_{\kappa} - l_{\kappa'}| + 2$. There may also be

contributions for larger j (going up in steps of two to preserve

parity) up to the lesser of $(l_{\kappa} + l_{\kappa'})$ and $(j_{\kappa} + j_{\kappa'})$, or up to

an assigned maximum j if smaller.

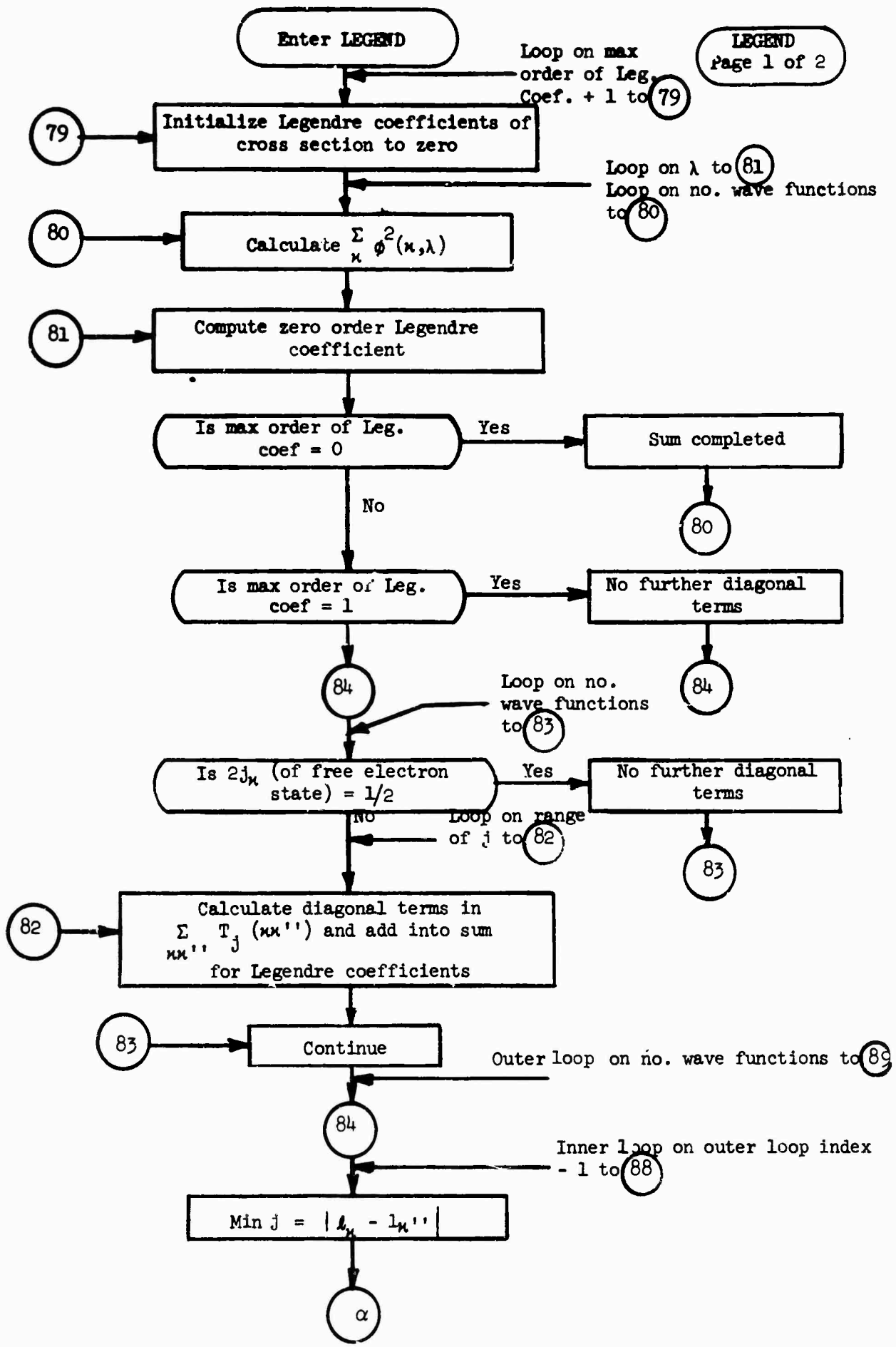
Subroutine called: MUSS

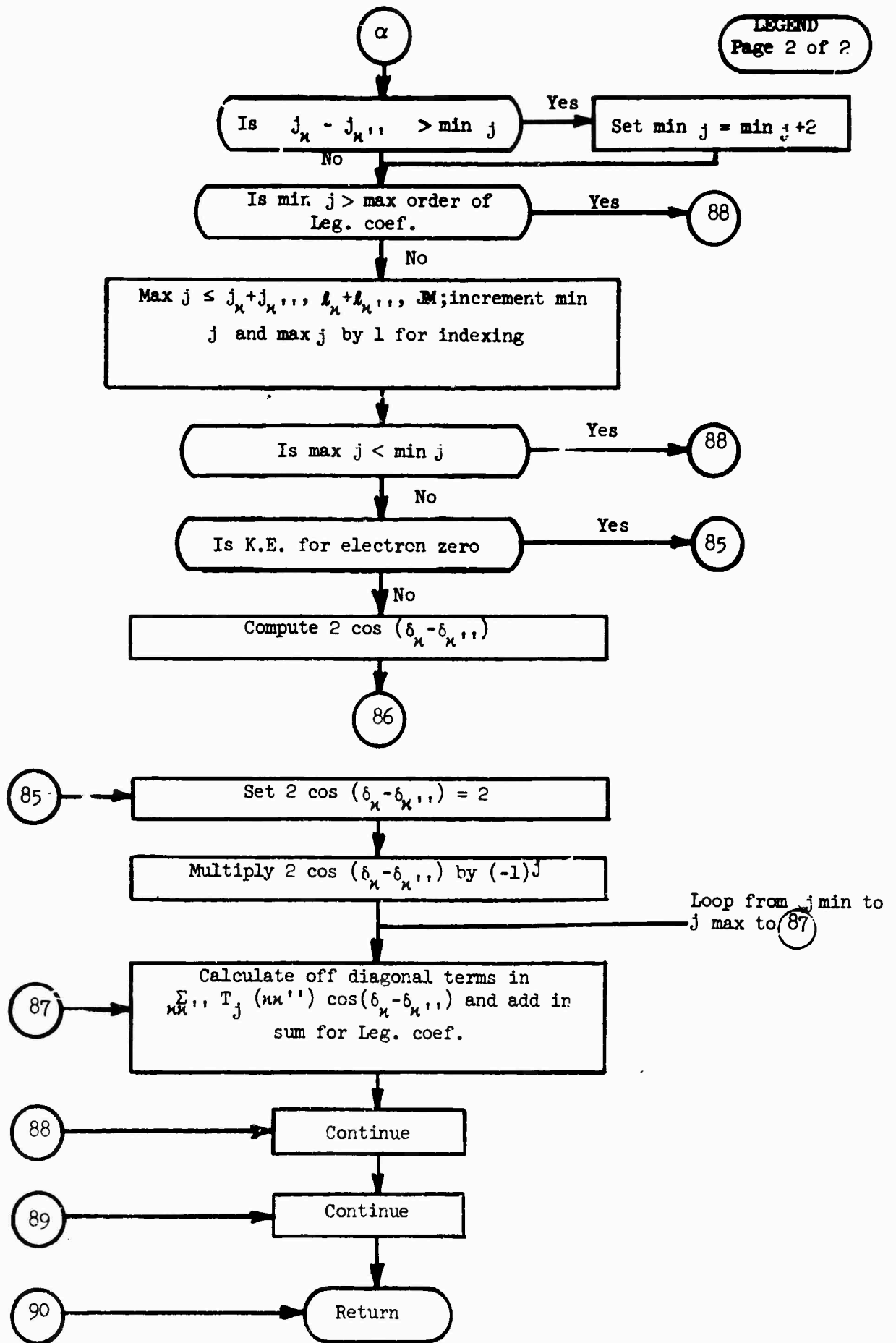
Subroutine called by: FELEC

Labelled Common: FID ϕ , LIMIT, QUANT

Local Variables:

Name	Dimension	Mode	Meaning
LMP		I	Max photon angular momentum + 1
J		I	Order of Legendre coefficient
LA		I	λ
STAT		R	$2\lambda + 1$
SKP		R	$\sum_{\kappa} \phi^2(\kappa, \lambda)$
JMAX		I	Max j contribution for given κ and κ''
JMIN		I	Min j contribution for given κ and κ''
K		I	Loop index for bound electron state
TJ		R	$T_j(\kappa, \kappa'')$
JDIF		I	$ \delta_{\kappa} - \delta_{\kappa''} $
CØD		R	$2 \cos(\delta_{\kappa} - \delta_{\kappa''})$
MINI		I	$(-1)^{j-1}$





SUBROUTINE LEGEND

SUBROUTINE LEGEND	LEG00010
COMMON/FIDU/FI(30,15),D(30),JMP,NAME,SHELL,QV,EB,IZ	LEG00020
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	LEG00030
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)	LEG00040
LMP=LM+1	LEG00050
DO 79 J=1,JMP	LEG00060
79 U(J)=0.0	LEG00070
DO 81 LA=1,LMP	LEG00080
STAT=2*LA+1	LEG00090
SKP=0.0	LEG00100
DO 80 K=1,K2M	LEG00110
80 SKP = SKP+FI(K,LA)*FI(K,LA)	LEG00120
81 U(1)=U(1)+SKP/STAT	LEG00130
IF (JM.EQ.0) GO TO 90	LEG00140
IF (JM.EQ.1) GO TO 84	LEG00150
DO 83 K=1,K2M	LEG00160
IF (JK(K) .EQ. 1) GO TO 83	LEG00170
JMAX=MINU(JK(K),2*LK(K),JM)+1	LEG00180
DO 82 J=3,JMAX,2	LEG00190
CALL MUSS(K,K,J,TJ)	LEG00200
82 U(J)=U(J)+TJ	LEG00210
83 CONTINUE	LEG00220
84 DO 89 K=2,K2M	LEG00230
KLS=K-1	LEG00240
DO 88 KK=1,KLS	LEG00250
JMIN=IABS(LK(K)-LK(KK))	LEG00260
JDIF=IABS(JK(K)-JK(KK))	LEG00270
IF (JDIF.GI.(2*JMIN)) JMIN=JMIN+2	LEG00280
IF (JMIN.GI.JM) GO TO 38	LEG00290
JMIN=JMIN+1	LEG00300
JMAX=MINU((JK(K)+JK(KK))/2),(LK(K)+LK(KK)),JM)+1	LEG00310
IF (JMAX .LT. JMIN) GO TO 88	LEG00320
IF (IEND .EQ. 1) GO TO 85	LEG00330
COD = 2.0 * (CR(K)*CR(KK) + SI(K)*SI(KK))	LEG00340
GO TO 86	LEG00350
85 COD = 2.0	LEG00360
86 MINI=MOD(JMIN,2)	LEG00370
IF (MINI.EQ.0) COD=-COD	LEG00380
DO 87 J=JMIN,JMAX,2	LEG00390
CALL MUSS (K,KK,J,TJ)	LEG00400
87 U(J)=U(J)+TJ*COD	LEG00410
88 CONTINUE	LEG00420
89 CONTINUE	LEG00430
90 RETURN	LEG00440
END	LEG00450

This page is intentionally left blank.

SUBROUTINE LOGGAM

Purpose: Computes the natural logarithm of the gamma function for complex arguments, i.e. $\text{Re } \ln \Gamma(x + iy)$ and $\text{Im } \ln \Gamma(x + iy)$

Method: a) Set $\Gamma(z) = -z + (z - 1/2) \ln z + \ln \sqrt{2\pi} + J(z)$ where $J(z)$ is given as a continued fraction. See Wall, "Analytic Theory of Continued Functions," p. 364, formula 93.9.

b) For $x > 2$, $\ln \Gamma(z)$ is computed from the recursion relation:

$$\ln \Gamma(z) = \ln \Gamma(1 + z) - \ln z$$

c) For negative x , the $\text{Im } \ln \Gamma(z)$ can be thought of as being equal to $V + 2\pi k$ where k is an integer and V is given by this routine.

Restrictions: a) x and y may not both be equal to zero.

b) if $y = 0$, x may not be equal to a negative integer

This routine is taken from M. S. Shapiro and M. Goldstein, "A Collection of Mathematical Computer Routines," NYO-1480-14 (1965).

Subroutine called: None

Subroutine called by: RADINT

Argument sequence: (X, Y, U, V)

Argument List:

Name	Dimension	Mode	Meaning
X		R	Real part of argument
Y		R	Imaginary part of argument
U		R	Real part of result
V		R	Imaginary part of result

SIBFIC LGAM

SUBROUTINE LOGGAM(X,Y,U,V)	LGM00010
C THIS SUBROUTINE COMPUTES THE NATURAL LOG OF THE GAMMA FUNCTION FOR	LGM00020
C COMPLEX ARGUMENTS. THE ROUTINE IS ENTERED BY THE STATEMENT	LGM00030
C CALL LOGGAM(X,Y,U,V)	LGM00040
C WHERE X IS THE REAL PART OF THE ARGUMENT	LGM00050
C Y IS THE IMAGINARY PART OF THE ARGUMENT	LGM00060
C U IS THE REAL PART OF THE RESULT	LGM00070
C V IS THE IMAGINARY PART OF THE RESULT	LGM00080
DIMENSION H(7)	LGM00090
H(1)=2.269488974	LGM00100
H(2)=1.517473649	LGM00110
H(3)=1.011523068	LGM00120
H(4)=.5256064690	LGM00130
H(5)=.2523809524	LGM00140
H(6)=0.0333333333	LGM00150
H(7)=0.0833333333	LGM00160
E2=1.57079632679	LGM00170
E8=3.14159265359	LGM00180
B1=0.0	LGM00190
B2=0.0	LGM00200
J=2	LGM00210
X2=X	LGM00220
4 IF(X)1,2,3	LGM00230
3 B6=ATAN (Y/X)	LGM00240
I=X*X	LGM00250
5 B7=Y*Y+I	LGM00260
C REAL PART OF LOG	LGM00270
T1=0.5*ALOG(B7)	LGM00280
IF(X-2.0)/,7,6	LGM00290
7 B1=B1+B6	LGM00300
B2=B2+T1	LGM00310
X=X+1.0	LGM00320
J=1	LGM00330
GO TO 4	LGM00340
6 T3=-Y*B6+(T1*(X-.5)-X+.9189365332)	LGM00350
T2=B6*(X-.5)+Y*T1-Y	LGM00360
T4=X	LGM00370
T5=-Y	LGM00380
T1=B7	LGM00390
DO 8 I=1,7	LGM00400
T=H(I)/T1	LGM00410
T4=I*T4+X	LGM00420
T5=-(I*T5+Y)	LGM00430
8 T1=I4*I4+T5*T5	LGM00440
I3=I4-X+I3	LGM00450
I2=-I5-Y+I2	LGM00460
GO TO (9,10),J	LGM00470
9 I3=I3-B2	LGM00480
I2=I2-B1	LGM00490
10 IF(X2)11,12,12	LGM00500
12 U=T3	LGM00510
V=T2	LGM00520
X=X2	LGM00530
RETURN	LGM00540
11 U=T3-E4	LGM00550
V=I2-E5	LGM00560
X=X2	LGM00570
RETURN	LGM00580
C X IS ZERO	LGM00590
2 I=0.0	LGM00600
IF(Y)13,14,15	LGM00610

```

13 B6=-E2
GO TO 5
15 B6=E2
GO TO 5
C X IS NEGATIVE
1 E4=0.0
E5=0.0
IE6=0
16 E4=E4+.5*(ALOG(X*X +Y*Y ))
E5=E5+ATAN (Y/X)
IE6=IE6+1
X=X+1.0
IF(X)16,17,17
17 IF( MOD (IE6,2))18,4,18
18 E5=E5+E8
GO TO 4
14 WRITE(6,19) X2,Y
19 FORMAT(29H ATTEMPTED TO TAKE LOGGAM OF 2HX=F6.0,1X2HY=F6.0)
CALL EXIT
RETURN
END

```

```

LGM00620
LGM00630
LGM00640
LGM00650
LGM00660
LGM00670
LGM00680
LGM00690
LGM00700
LGM00710
LGM00720
LGM00730
LGM00740
LGM00750
LGM00760
LGM00770
LGM00780
LGM00790
LGM00800
LGM00810
LGM00820

```

This page is intentionally left blank.

SUBROUTINE MUSS

Purpose: Performs the μ' sum and computes the term $T_j(\kappa, \kappa'') =$

$$C(j_{\kappa''}, j_{\kappa}, j; 1/2, -1/2) \sum_{\mu'} (-1)^{\mu' + 1/2} H(\kappa, \mu') H(\kappa'', \mu')$$

$$C(j_{\kappa''}, j_{\kappa}, j; \mu' + 1, -\mu' - 1)$$
 which is used in computation of D_j (Legendre coefficient).

Method: The sum is carried out first for $(\mu' + 1/2) \geq 0$, computing the C-coefficients and recording them as an indexed variable, the upper limit on μ' being the lesser of the upper limits for κ and κ'' computed in subroutine HUM. The sum for the negative $(\mu' + 1/2)$ is similarly carried up to the lesser of the maximum $|\mu'|$ values for negative μ' , but the C-coefficient is obtained from the previously obtained ones by a symmetry operation (introducing at most a sign change). The C-coefficient in front of the sum is the one computed for $\mu' = -1/2$.

Subroutine called: CØEFS

Subroutine called by: LEGEND

Labelled Common: QUANT, TRANS

Argument sequence: (K, KK, J, TJ)

Argument List:

Name	Dimension	Mode	Meaning
K		I	Index for κ
KK		I	Index for κ''
J		I	Order of Legendre coefficient + 1
TJ		R	$T_j(\kappa, \kappa'')$

Local Variables:

Name	Dimension	Mode	Meaning
JD		I	Twice order of Legendre coefficient
C		R	Clebsch-Gordan coefficient
CL	30	R	Clebsch-Gordan coefficient saved
JP0S		I	Range of positive μ' (-1 means none)
M		I	Loop index for μ'
PM		R	$(-1)^{\mu'} + 1/2$ (times $i^{j_{\mu} + j_{\mu'} + j}$ if μ' negative)
MP		I	$2 \mid \mu' + 1 \mid$
JNEG		I	Range of negative μ'
JM0D		I	$i^{j_{\mu} + j_{\mu'} + j}$

Enter MUSS

MUSS
Page 1 of 1

Calculate $T_j(\kappa\kappa'')$ term for
for $\mu' = -1/2$ and save C-coef.

Calculate $(\mu') \max + 1/2$ as lesser
of values for κ and κ'' obtained
in HUM

Is this value equal to -1

Yes

No positive μ'

No Loop on range of
positive μ' to 30

30

33

30

Compute $T_j(\kappa\kappa'')$ terms for $\mu' > 0$
and add; save C-coefs.

33

Calculate $(-\mu') \max + 1/2$ as lesser
of values for κ and κ''

Is this value equal to 1

Yes

Finished summing

Loop on range of
negative μ' to 31

31

32

31

Compute $T_j(\kappa\kappa'')$ terms for $\mu' \leq -1/2$
and add; use appropriate C-coef.
values from above

32

Final value of sum for $T_j(\kappa\kappa'')$
multiplied by C-coef. value for
 $\mu' = -1/2$

Return

SIBFIC MUSE

SUBROUTINE MUSS (K, KK, J, TJ)	MUS00010
COMMON/QUANT/LK(30), LMK(30), JK(30), FKAP(30), SN(30), SI(30), CR(30)	MUS00020
COMMON/TRANS/HF(30,15), HFM(30,15), JNG(30), JPS(30)	MUS00030
DIMENSION CL(30)	MUS00040
JD=2*(J-1)	MUS00050
CALL COEFS(JK(K), JK(KK), JD, 1, -1, C)	MUS00060
TJ = HFM(K,1) * HFM(KK,1) * C	MUS00070
CL(1)=C	MUS00080
JPOS=MIN0(JPS(K), JPS(KK))	MUS00090
IF (JPOS.EQ.(-1)) GO TO 33	MUS00100
PM=1.0	MUS00110
DO 30 M=1, JPOS	MUS00120
PM=-PM	MUS00130
MP=2*M+1	MUS00140
CALL COEFS(JK(K), JK(KK), JD, MP, -MP, C)	MUS00150
CL(MP)=C	MUS00160
30 TJ = TJ + HF(K, M) * HF(KK, M) * C * PM	MUS00170
35 JNEG=MIN0(JNG(K), JNG(KK))	MUS00180
IF (JNEG.EQ.1) GO TO 32	MUS00190
JMOD=MOD((JK(K)+JK(KK)+JD), 4)	MUS00200
PM=-1.0	MUS00210
IF (JMOD.EQ.0) PM=1.0	MUS00220
DO 31 M=2, JNEG	MUS00230
PM=-PM	MUS00240
MP=2*M-3	MUS00250
31 TJ = TJ + HFM(K, M) * HFM(KK, M) * CL(MP) * PM	MUS00260
32 TJ=J*CL(1)	MUS00270
RETURN	MUS00280
END	MUS00290

SUBROUTINE RADINT

Purpose: This is the control subroutine for the integrations.

Method: The requisite coefficients and the initial values of the free-electron wavefunctions and their derivatives are computed. The radial integrals are performed by calling the Runge-Kutta integration subroutines in DØ loops. Normalization factors are obtained from WNORM and applied to the matrix elements. The phase shifts are obtained by wave-matching. Finally, subroutine HUM is called to start the angular momentum sums.

Subroutines called: LØGGAM, RKUT, DERIV, XDERIV, XRKUT, WNØRM, SPHBES, HUM

Subroutine called by: PELEC

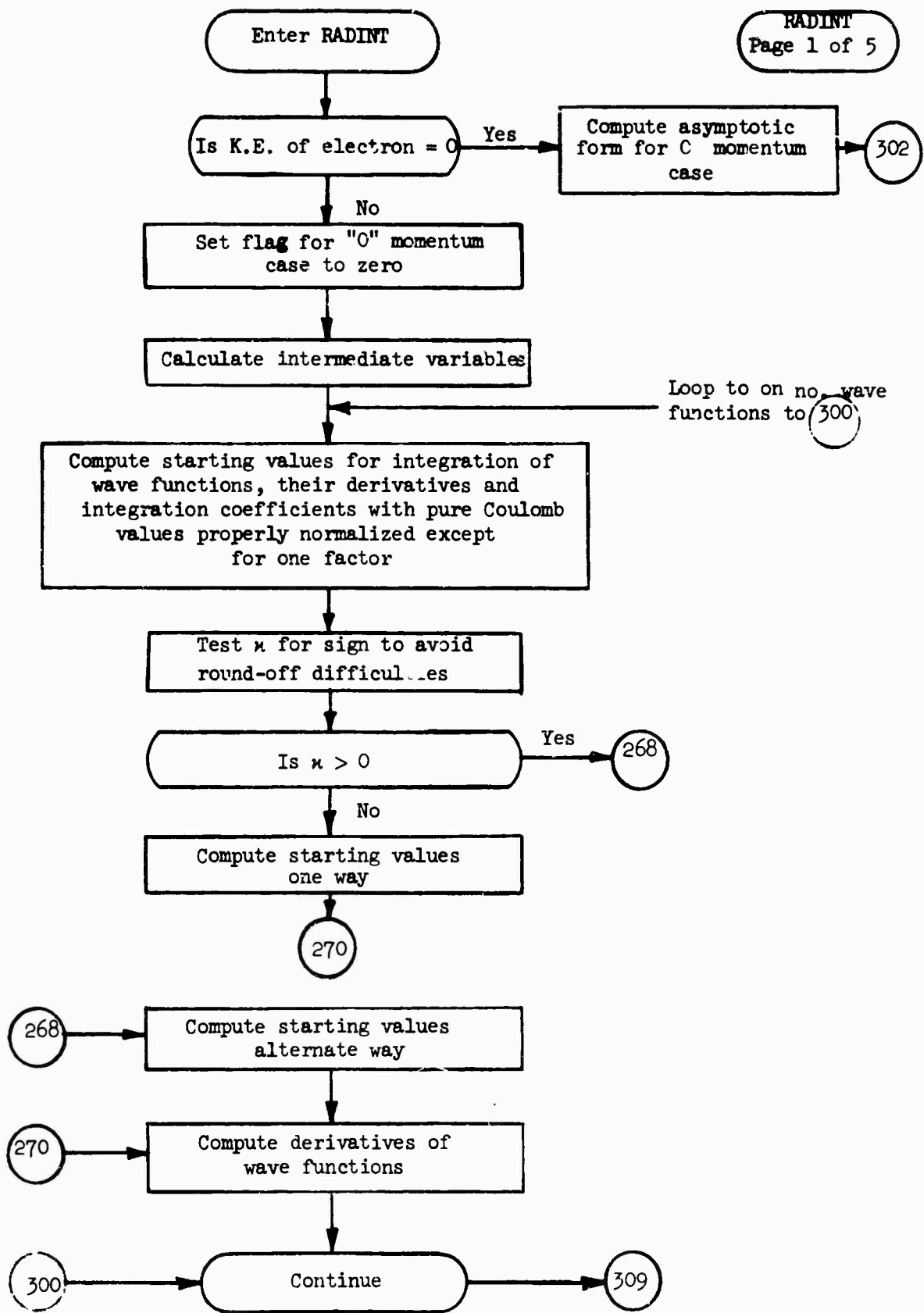
Variables in unlabelled Common: PI, HALFPI, FØURPI, RAD, SQ2, Q, ZA, ZAZA,
EFN, EGN, V, CG, GAM

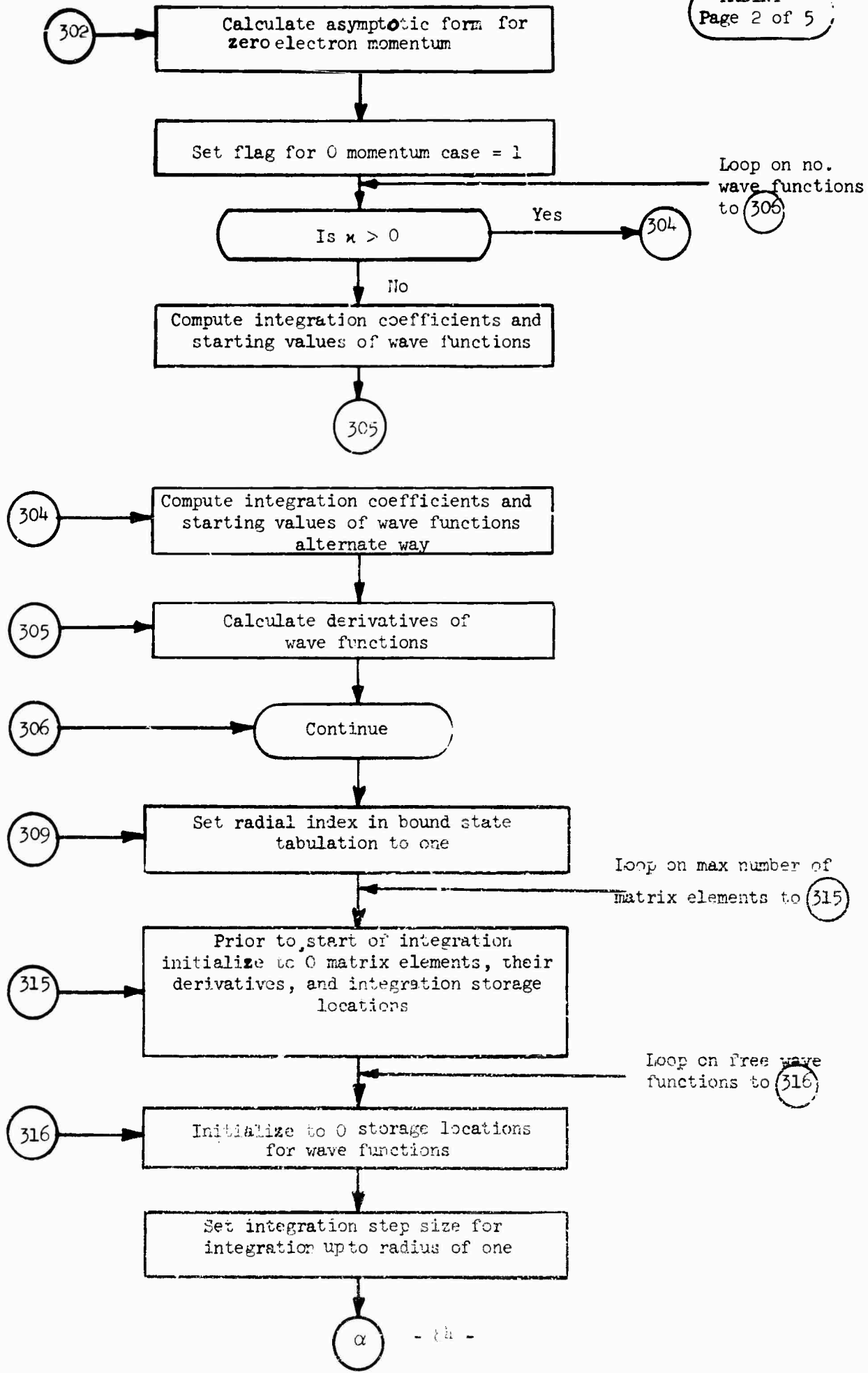
Labelled Common: BESSEL, DFUNC, LIMIT, MAT, QUANT, VECT, ØNWARD

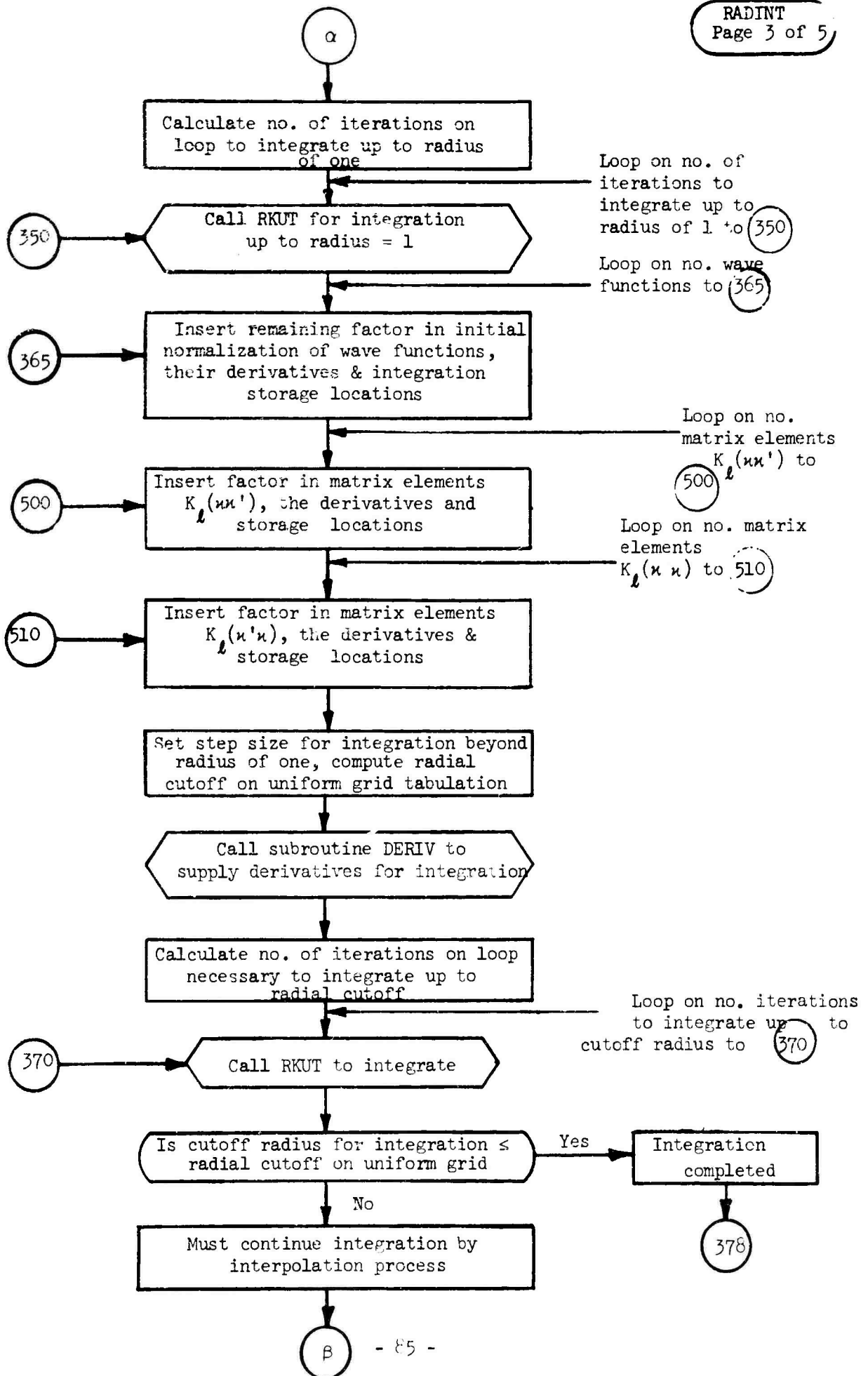
Local Variables:

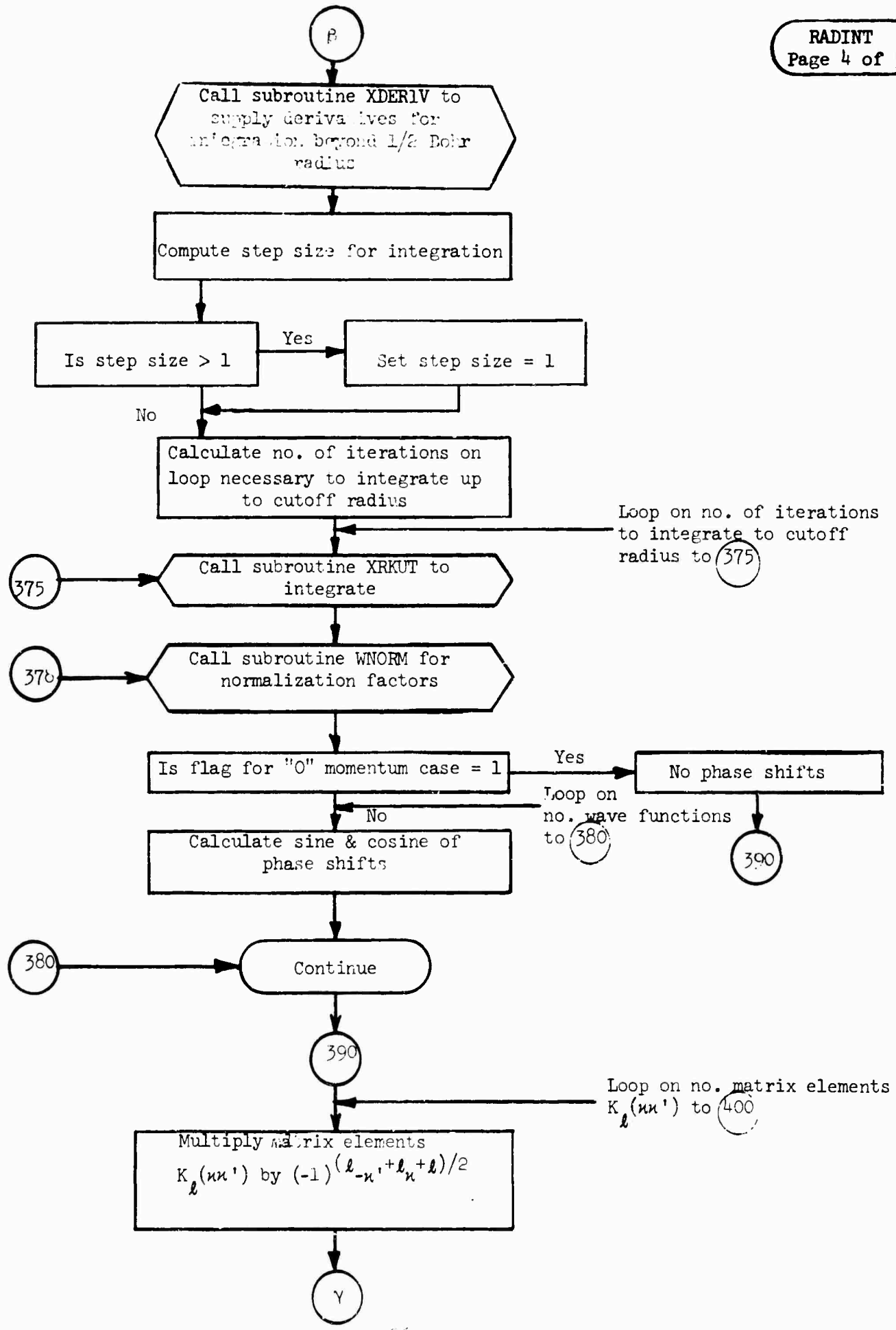
Name	Dimension	Mode	Meaning
E		R	Free electron energy (in mc^2 units)
RK		R	$\sqrt{E^2 - 1}$, free electron momentum
I		I	Loop index of free electron state
TUGAM	30	R	$2\sqrt{k^2 - \left(\frac{Z}{137.0367}\right)^2 + 1}$
IUP		I	Max number of matrix elements
NØ		I	Loop index to initialize to zero components of free electron wavefunction, their derivatives, integrand for matrix elements and their integration storage variables.
N		I	Range on number of iterations for radial integration up to radius of one.
XCUT		R	Radial cutoff on uniform grid in tabulation.
WAVE		R	Max of wave numbers of free electron and photon.

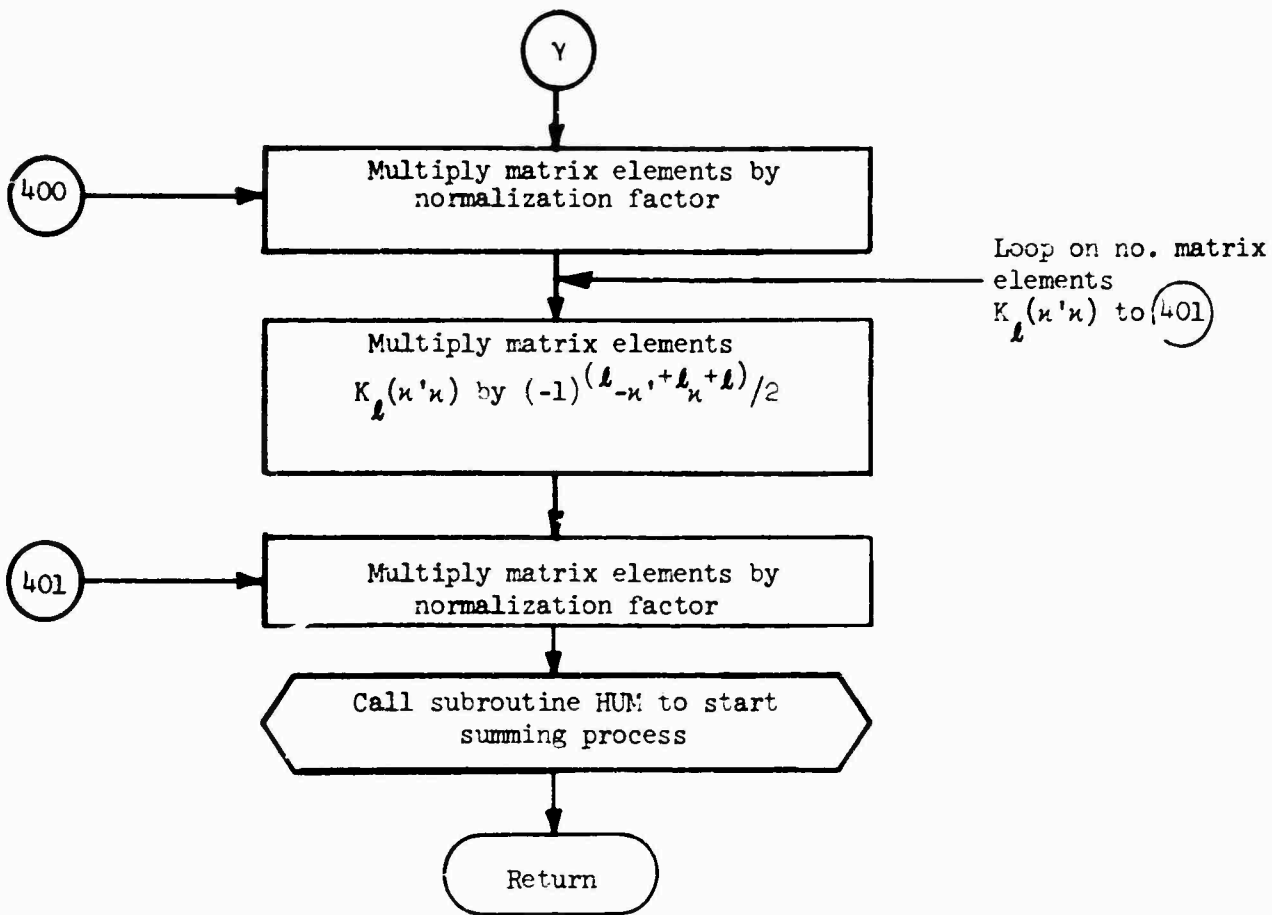
Name	Dimension	Mode	Meaning
LUB		I	Range on number of iterations beyond one-half Bohr radius for radial integration
RX		R	Current radial variable beyond one-half Bohr radius
LTOT		I	$l_{-n} + l_n + l$











SIBFIC RADN

```

SUBROUTINE RADINT
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30)RAD00010
COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15)RAD00020
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HRAD00040
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LKKB,NTABRAD00050
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUTRAD00060
COMMON /ONWARD/RX,SCX,GBX,FBXRAD00100
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)RAD00070
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKBRAD00080
DIMENSION RNOBK(30), TUGAM(30)RAD00090
100 FORMAT(5X,5UHLNGTH UNITS ARE HBAR MC ( 1 BOHR RADIUS = 137 )//)RAD00110
101 FORMAT (5X,24HINTEGRATION STEP SIZE IS,F11.7, 5X,5HUP TO,F9.3//)RAD00120
E = EFN+1.0RAD00130
EGN = E+1.0RAD00140
IF ( EFN .EQ. 0.) GO TO 302RAD00150
RK = SQRT(EFN*EGN)RAD00160
IEND = 0RAD00170
SQEG = SQRT (EGN)RAD00180
SQE = RK/SQEGRAD00190
RKE = RK / EGNRAD00200
GNU = ZA*E/RKRAD00210
TRK = 2.0*RKRAD00220
TWORK = EXP ( GNU * HALFPI ) / SQRT ( TRK * PI )RAD00230
DO 300 I=1,K2MRAD00240
GAM(I) = SQRT (FKAP(I)**2-ZAZA)RAD00250
TUGAM(I) = 2.0*GAM(I)+1.0RAD00260
CALL LOGGAM (GAM(I),GNU,XRE,XIM)RAD00270
ZK = TWORK*(TRK**GAM(I))*EXP(XRE)RAD00280
IF (FKAP(I).GT.0.0) GO TO 268RAD00290
CF(I) = FKAP(I)-GAM(I)RAD00300
CG(I) = -ZAZA/CF(I)RAD00310
HM = ZAZA * EFN / ( CF(I) * ( E * FKAP(I) - GAM(I) ) )RAD00320
HP = 2.0 - HMRAD00330
HM = SQRT ( HM )RAD00340
HP = SQRT ( HP )RAD00350
G(I) = ZK * SQEG * ( GAM(I) * HP + GNU * HM )RAD00360
F(I) = ZA*G(I)/CF(I)RAD00370
GO TO 270RAD00380
268 CG(I) = -FKAP(I)-GAM(I)RAD00390
CF(I) = -ZAZA/CG(I)RAD00400
HP = -ZAZA * EGN * ( E*FKAP(I)+GAM(I) ) / CG(I)RAD00410
HP = HP / ( EFN * EGN * FKAP(I) + ZAZA )RAD00420
HM = 2.0 - HPRAD00430
HM = SQRT ( HM )RAD00440
HP = SQRT ( HP )RAD00450
F(I) = ZK * SQE * ( GAM(I) * HM + GNU * HP )RAD00460
G(I) = -ZA*F(I)/CG(I)RAD00470
270 DG(I) = F(I)*((1.0-CF(I))*EGN-CF(I)*EFN)/TUGAM(I)RAD00480
DF(I) = -G(I)*((1.0-CG(I))*EFN-CG(I)*EGN)/TUGAM(I)RAD00490
300 CONTINUERAD00500
GO TO 309RAD00510
302 HAZ=SQRT (ZA)RAD00520
TUAZ = 2.0*ZARAD00530
IEND = 1RAD00540
DO 306 I=1,K2MRAD00550
GAM(I) = SQRT (FKAP(I)**2-ZAZA)RAD00560
TUGAM(I) = 2.0 * GAM(I) + 1.0RAD00570
F(I) = HAZ*(TUAZ**GAM(I))RAD00580
IF (FKAP(I).GT.0.0) GO TO 304RAD00590
F(I) = -F(I)RAD00600
CF(I) = FKAP(I)-GAM(I)RAD00610

```


CG(I) = -ZAZA/CF(I)	RAD00620
AZKAP = CF(I)/ZA	RAD00630
GO TO 305	RAD00640
304 CG(I) = -FKAP(I)-GAM(I)	RAD00650
CF(I) = -ZAZA/CG(I)	RAD00660
AZKAP = -ZA/CG(I)	RAD00670
305 G(I) = AZKAP*F(I)	RAD00680
UF(I) = -F(I)*TUAZ/TUGAM(I)	RAD00690
DG(I) = 2.0*F(I)*(1.0-CF(I))/TUGAM(I)	RAD00700
306 CONTINUE	RAD00710
309 NTAB = 1	RAD00720
M1 = LM+1	RAD00730
M2 = LM+2	RAD00740
IUP = MAX0 (NK,NKP)	RAD00750
DO 315 NO=1,IUP	RAD00760
FK(NO) = 0.0	RAD00770
FKP(NO) = 0.0	RAD00780
DFK(NO) = 0.0	RAD00790
DFKP(NO) = 0.0	RAD00800
SFK(NO) = 0.0	RAD00810
315 SFKP(NO) = 0.0	RAD00820
DO 316 NO=1,K2M	RAD00830
SF(NO) = 0.0	RAD00840
316 SG(NO) = 0.0	RAD00850
H=0.0078125	RAD00860
N = 1.0/H + .1	RAD00870
RONE=1.0	RAD00880
DO 350 I=1,N	RAD00890
350 CALL RKUT	RAD00900
DO 365 I=1,K2M	RAD00910
CALL LOGGAM (TUGAM(I),0,DUM1,DUM2)	RAD00920
RNORM(I) = EXP (-DUM1)	RAD00930
F(I) = F(I)*RNORM(I)	RAD00940
G(I) = G(I)*RNORM(I)	RAD00950
DF(I) = DF(I)*RNORM(I)	RAD00960
DG(I) = DG(I)*RNORM(I)	RAD00970
SF(I) = SF(I)*RNORM(I)	RAD00980
SG(I) = SG(I)*RNORM(I)	RAD00990
CF(I) = FKAP(I)	RAD01000
365 CG(I) = -FKAP(I)	RAD01010
DO 500 N=1,NK	RAD01020
I = KG(N)	RAD01030
FK(N) = FK(N)*RNORM(I)	RAD01040
DFK(N) = DFK(N)*RNORM(I)	RAD01050
500 SFK(N) = SFK(N)*RNORM(I)	RAD01060
DO 510 N=1,NKP	RAD01070
I = KF(N)	RAD01080
FKP(N) = FKP(N)*RNORM(I)	RAD01090
DFKP(N) = DFKP(N)*RNORM(I)	RAD01100
510 SFKP(N) = SFKP(N)*RNORM(I)	RAD01110
WRITE (6, 100)	RAD01120
WRITE (6,101) H,RONE	RAD01130
H = 0.125	RAD01140
XCUT = AMIN1 (RCUT,65.0)	RAD01150
WRITE (6, 101) H, XCUT	RAD01160
NEW = 1	RAD01170
CALL DERIV	RAD01180
NDON = (XCUT-1.0)/H+0.1	RAD01190
DO 370 NDO=1,NDON	RAD01200
370 CALL RKUT	RAD01210
RX = XCUT	RAD01220
IF (RCUT.LE.XCUT) GO TO 378	RAD01230

NEW=1	RAD01240
CALL XDERIV	RAD01250
WAVE = AMAX1 (RK,Q)	RAD01260
IH=PI/WAVE	RAD01270
H=FLOAT (IH)/8.0	RAD01280
IF (H.GT.1.0) H=1.0	RAD01290
WRITE (6, 101) H, RCUT	RAD01300
LUB = (RCUT-RX)/H+0.1	RAD01310
DO 375 I=1,LUB	RAD01320
375 CALL XHKUT	RAD01330
378 CALL WNORM (RNORM,RX)	RAD01340
IF (IEND .EQ. 1) GO TO 390	RAD01350
M1 = KM + 2	RAD01360
M2 = KM + 3	RAD01370
Y = RK * RCUT	RAD01380
CALL SPHBES(Y)	RAD01390
DO 380 I=1,K2M	RAD01400
J1 = LMK(I) + 1	RAD01410
J2 = LK(I) + 1	RAD01420
SI(I) = HKE * SN(I) * G(I) * B(J1) - F(I) * B(J2)	RAD01430
CR(I) = HKE * G(I) * B(J2) + SN(I) * F(I) * B(J1)	RAD01440
RNM = SQRT (SI(I) * SI(I) + CR(I) * CR(I))	RAD01450
SI(I) = SI(I) / RNM	RAD01460
CR(I) = CR(I) / RNM	RAD01470
380 CONTINUE	RAD01480
390 DO 400 K=1,NK	RAD01490
I = KG(K)	RAD01500
LTOT = LMKB+LK(I)+LBES(K)-1	RAD01510
IF (MOD(LTOT,4).NE.0) FK(K)=-FK(K)	RAD01520
400 FK(K) = FK(K)*RNORM(I)	RAD01530
DO 401 K=1,NKP	RAD01540
I = KF(K)	RAD01570
LTOT = LMKB+LK(I)+LBS(K)-1	RAD01550
IF (MOD(LTOT,4).NE.0) FKP(K)=-FKP(K)	RAD01560
401 FKP(K) = FKP(K)*RNORM(I)	RAD01580
420 CALL HUM	RAD01590
RETURN	RAD01600
END	RAD01610

SUBROUTINE RKUT

Purpose: Performs the Runge-Kutta integration. The routine uses indexed tabulated values of the bound-state wavefunction and the potential obtained previously by interpolation from the Waber output. Radial integration is performed up to a maximum of one-half Bohr radius.

Method: Runge-Kutta Integration (Gill Form). A fourth order integration scheme in which the error in each step is of the order h^5 , where h is the interval size.

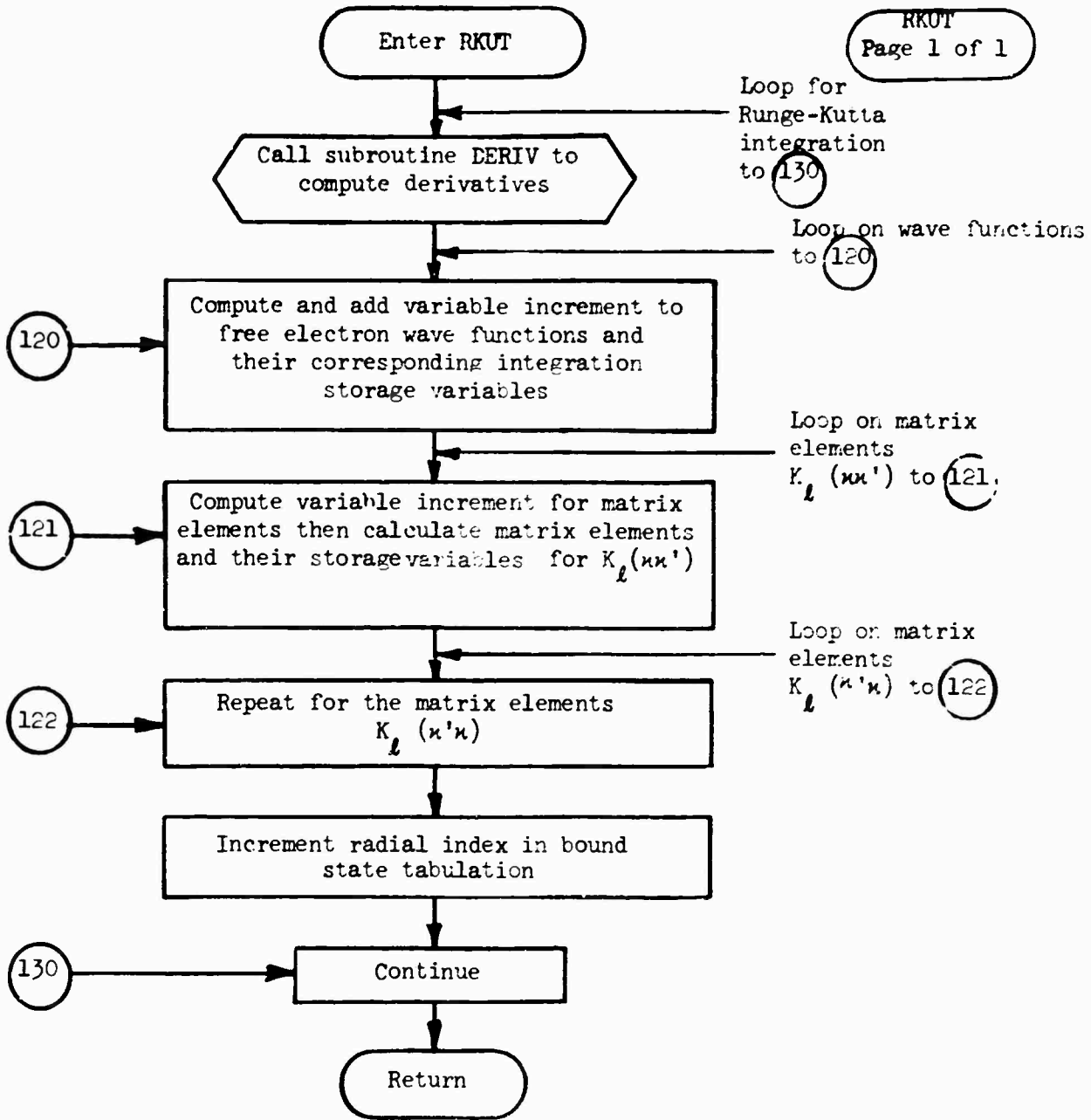
Subroutine called: DERIV

Subroutine called by: RADINT

Labelled Common: DFUNC, KUT, LIMIT, MAT, TAPES

Local Variables:

Name	Dimension	Mode	Meaning
J		I	Loop index on Runge-Kutta integration
I		I	Loop index on; number of free wavefunctions, number of matrix elements $K_l(\kappa\kappa')$ and $K_l(\kappa'\kappa)$
Z		R	Incremental variable for "small" component of free electron wavefunction
ZP		R	Incremental variable for "large" component of free electron wavefunction



SIBFIC RKUG

SUBROUTINE RKUT

RKU00010

C

RUNGE-KUTTA INTEGRATION

RKU00020

COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HRKU00030

COMMON /KUI/RK1(4),RK2(4),RK3(4),RK4(4),K4(4) RKU00040

COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB RKU00050

COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT RKU00060

COMMON /TAPE ,/X(1,00),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN RKU00070

DO 130 J=1,+ RKU00080

CALL DERIV RKU00090

DO 120 I=1,K2,1 RKU00100

Z = RK1(J)*(DF(I)-RK2(J)*SF(I)) RKU00110

ZP = RK1(J)*(DG(I)-RK2(J)*SG(I)) RKU00120

F(I) = F(I)+H*Z RKU00130

G(I) = G(I)+H*ZP RKU00140

SF(I) = SF(I)+3.0*Z-RK3(J)*DF(I) RKU00150

120 SG(I) = SG(I)+3.0*ZP-RK3(J)*DG(I) RKU00160

DO 121 I=1,NK RKU00170

Z = RK1(J)*(DFK(I)-RK2(J)*SFK(I)) RKU00180

FK(I) = FK(I)+H*Z RKU00190

121 SFK(I) = SFK(I)+3.0*Z-RK3(J)*DFK(I) RKU00200

DO 122 I=1,NKP RKU00210

Z = RK1(J)*(DFKP(I)-RK2(J)*SFKP(I)) RKU00220

FKP(I) = FKP(I)+H*Z RKU00230

122 SFKP(I) = SFKP(I)+3.0*Z-RK3(J)*DFKP(I) RKU00240

NTAB=NTAB+K4(J) RKU00250

130 CONTINUE RKU00260

RETURN RKU00270

END RKU00280

This page is intentionally left blank.

SUBROUTINE SINDEK

Purpose: To catalogue and index matrix elements consistent with selection rules.

Method: Routine examines the angular momentum values to find and index all the matrix elements compatible with the selection rules and with the input cutoff values of the quantum numbers and records the free electron κ and the photon l values for each matrix element in reference vectors (separately for the two kinds of matrix elements).

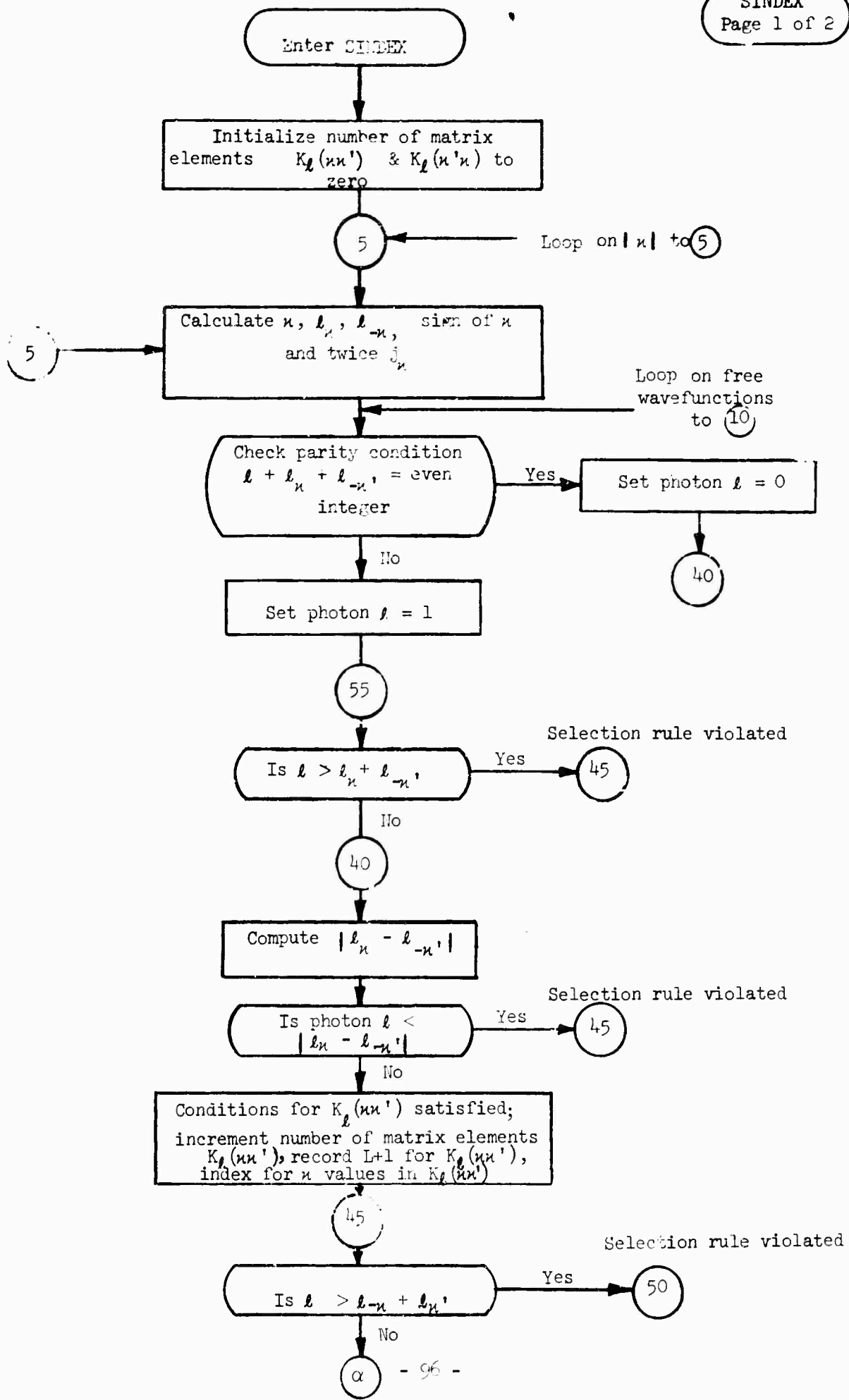
Subroutine called: None

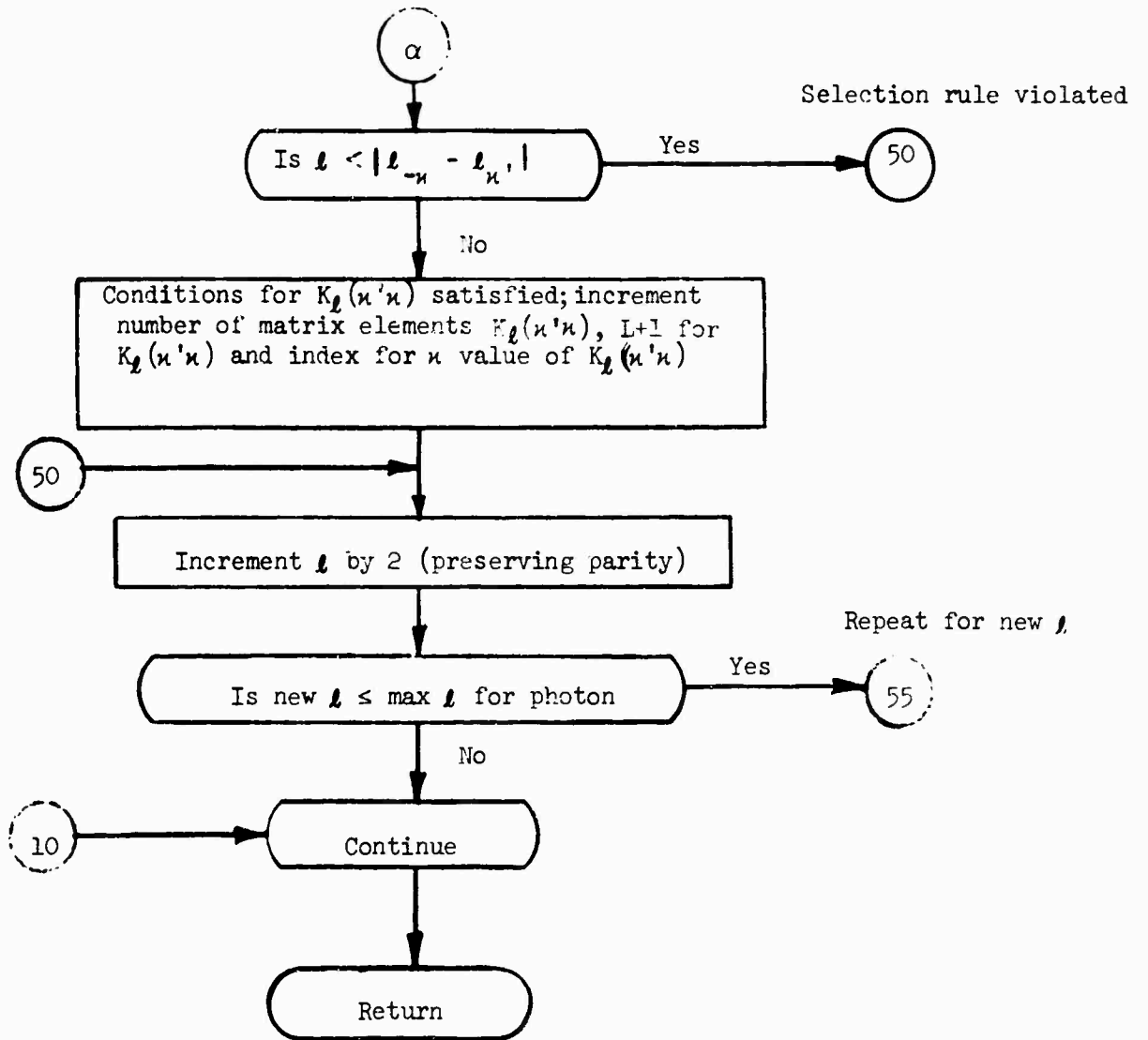
Subroutine called by: PELEC

Labelled parameters: QUANT, VECT, LIMIT

Local Variables:

Name	Dimension	Mode	Meaning
I		I	Loop index on max κ for electron
K		I	Loop index on number of free electron states
LSUM		I	$l_n + l_{-n}$
LDIFF		I	$ l_n - l_{-n} $
L		I	Photon angular momentum





SIBFIC SIND

SUBROUTINE SINDEX	SND00010
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)	SND00020
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB	SND00030
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	SND00040
NK=0	SND00050
NKP=0	SND00060
DO 5 I=1,KM	SND00070
K=2*I-1	SND00080
J=K+1	SND00090
FKAP(K)=-I	SND00100
FKAP(J)=I	SND00110
LK(K)=I-1	SND00120
LK(J)=I	SND00130
LMK(K)=I	SND00140
LMK(J)=I-1	SND00150
SN(K)=-1.0	SND00160
SN(J)=1.0	SND00170
JK(K)=LK(K)+LMK(K)	SND00180
5 JK(J)=JK(K)	SND00190
DO 10 K=1,K2M	SND00200
LSUM = LK(K)+LMKB	SND00210
IF (MOD(LSUM,2)) 35,30,35	SND00220
30 L=0	SND00230
GO TO 40	SND00240
35 L=1	SND00250
55 IF (L.GT.LSUM) GO TO 45	SND00260
40 LDIFF = IABS (LK(K)-LMKB)	SND00270
IF (L.LT.LDIFF) GO TO 45	SND00280
NK=NK+1	SND00290
LBES(NK)=L+1	SND00300
KG(NK)=K	SND00310
45 LT=LMK(K)+LKB	SND00320
IF (L.GT.LT) GO TO 50	SND00330
LD=IABS(LMK(K)-LKB)	SND00340
IF (L.LT.LD) GO TO 50	SND00350
NKP=NKP+1	SND00360
LBS(NKP)=L+1	SND00370
KF(NKP)=K	SND00380
50 L=L+2	SND00390
IF (L.LE.LM) GO TO 55	SND00400
10 CONTINUE	SND00410
RETURN	SND00420
END	SND00430

SUBROUTINE SPHBES

Purpose: Computes the values of the spherical Bessel function.

Method: The zero order function is obtained as $\sin R/R$. For small argument the higher order functions are calculated from the power series expansion. For large argument, the first order function is computed from its explicit sinusoidal representation and the remaining ones obtained by recursion relations. For intermediate arguments, the lower order functions are obtained by recursion, the higher order by power series.

Subroutines called: None

Subroutine called by: DERIV, XDERIV, RADINT

Labelled Common: BESSEL

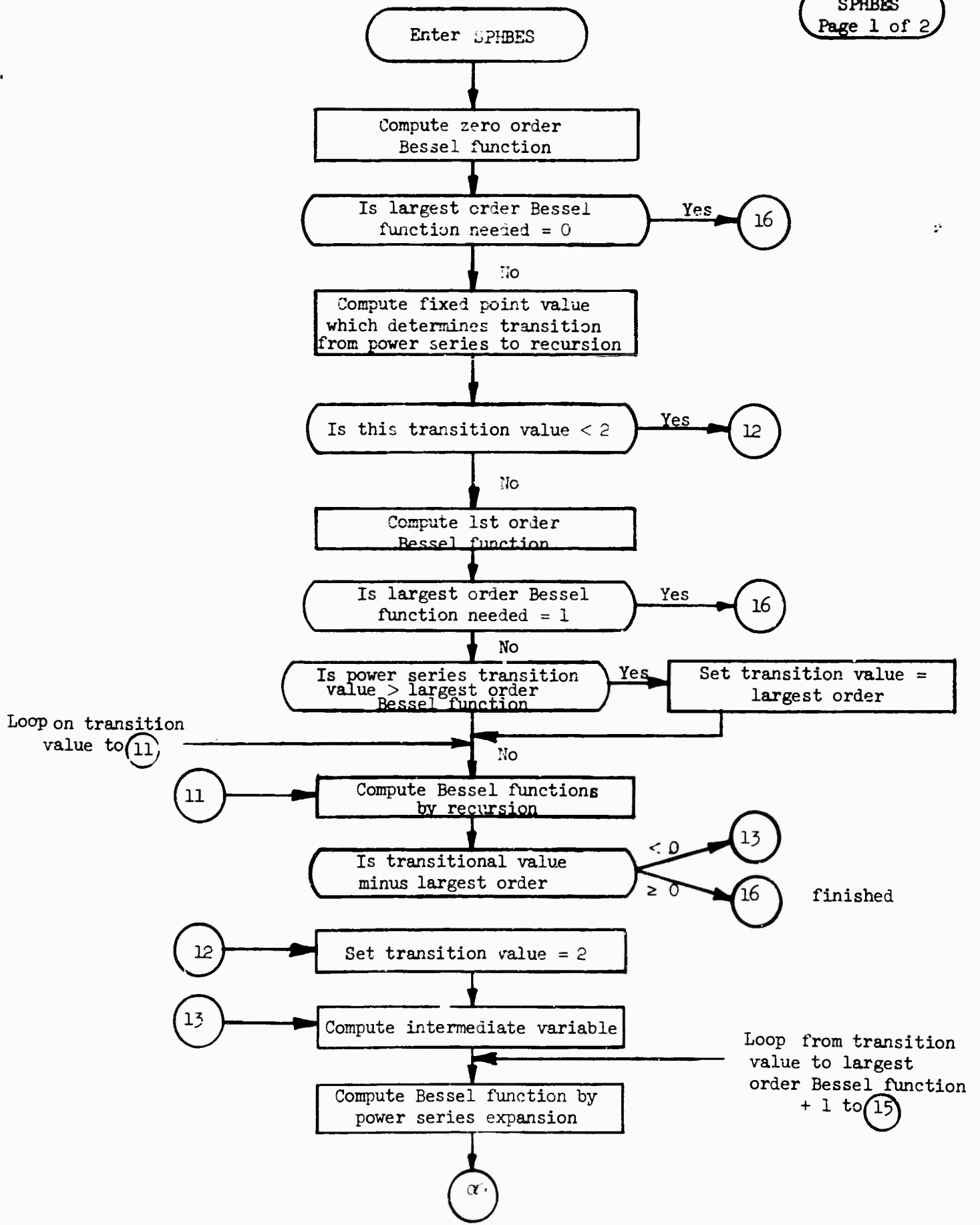
Argument sequence: (R)

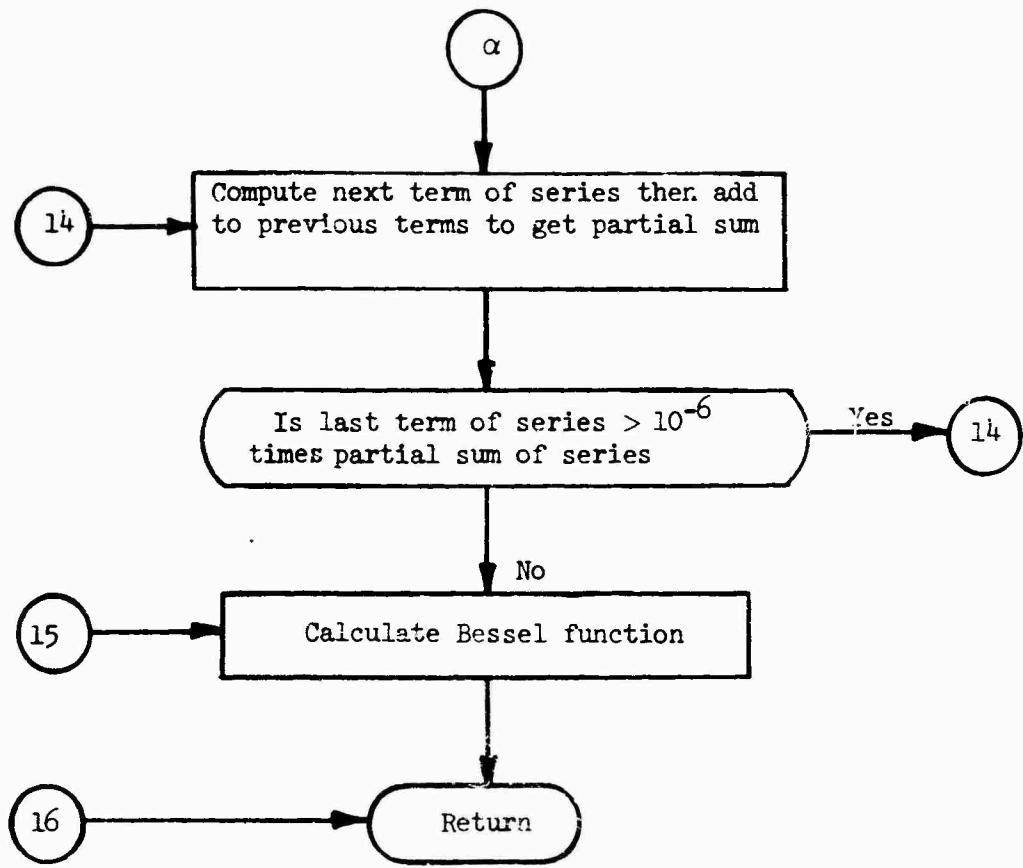
Argument List:

<u>Name</u>	<u>Dimension</u>	<u>Mode</u>	<u>Meaning</u>
R		R	Bessel function argument; photon momentum * radius from DERIV, XDERIV; free electron momentum x radius from RADINT.

Local Variables:

<u>Name</u>	<u>Dimension</u>	<u>Mode</u>	<u>Meaning</u>
NR		I	Defines transition from power series to recursion.
L		I	Loop index on calculating Bessel function.
SER		R	Partial sum of power series expansion.
TER		R	Last term of series expansion.





SPH001C SPHB

```

SUBROUTINE SPHBES (R)
SPHERICAL BESSEL FUNCTION
COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15)
OR = 1.0 / R
B(1) = SIN(R) * OR
IF ( M1 .EQ. 1 )      GO TO 16
NR = R + 2.0
IF ( NR .LT. 2 )     GO TO 12
B(2) = ( B(1) - COS(R) ) * OR
IF ( M1 .EQ. 2 )     GO TO 16
IF ( NR .GT. M1 )    NR=M1
DO 11 L = 2, NR
11 B(L+1) = FL(L) * B(L) * OR - B(L-1)
   IF ( NR - M1 )    13,16,16
12 NR = 2
13 HAS = 0.5 * R * R
   DO 15 L = NR, M2
   J = 0
   SER = 1.0
   TER = 1.0
14 J = J + 1
   TER = - TER * HAS * OF(L,J)
   SER = SER + TER
   IF ( ABS(TER) .GT. ( 0.000001 * ABS(SER) ) )      GO TO 14
15 B(L) = SER * PC(L) * ( R**(L-1) )
16 RETURN
END

```

SPH00010
 SPH00020
 SPH00030
 SPH00040
 SPH00050
 SPH00060
 SPH00070
 SPH00080
 SPH00090
 SPH00100
 SPH00110
 SPH00120
 SPH00130
 SPH00140
 SPH00150
 SPH00160
 SPH00170
 SPH00180
 SPH00190
 SPH00200
 SPH00210
 SPH00220
 SPH00230
 SPH00240
 SPH00250
 SPH00260
 SPH00270

SUBROUTINE WN ϕ RM

Purpose: Computes the normalization factors for the free-electron wavefunction after termination of the numerical integration.

Method: The normalization factors are determined by a matching to the W.K.B. solution. Derivatives of the potential in the W.K.B. expression are obtained from a numerical fit of an exponential to the screening function (ratio of screened to unscreened potential) at the cutoff radius. When the W.K.B. conditions fail (vanishing kinetic energy and high angular momentum), the normalization factor of the previous wavefunctions is used.

Subroutine called: None

Subroutine called by: RADINT

Variables in unlabelled Common: PI, HALFPI, F ϕ URPI, RAD, SQ2, Q, ZA, ZAZA, EFN, EGN, V, CG, GAM

Labelled Common: DFUNC, LIMIT, TAPES

Argument sequence: (RN RM, RX)

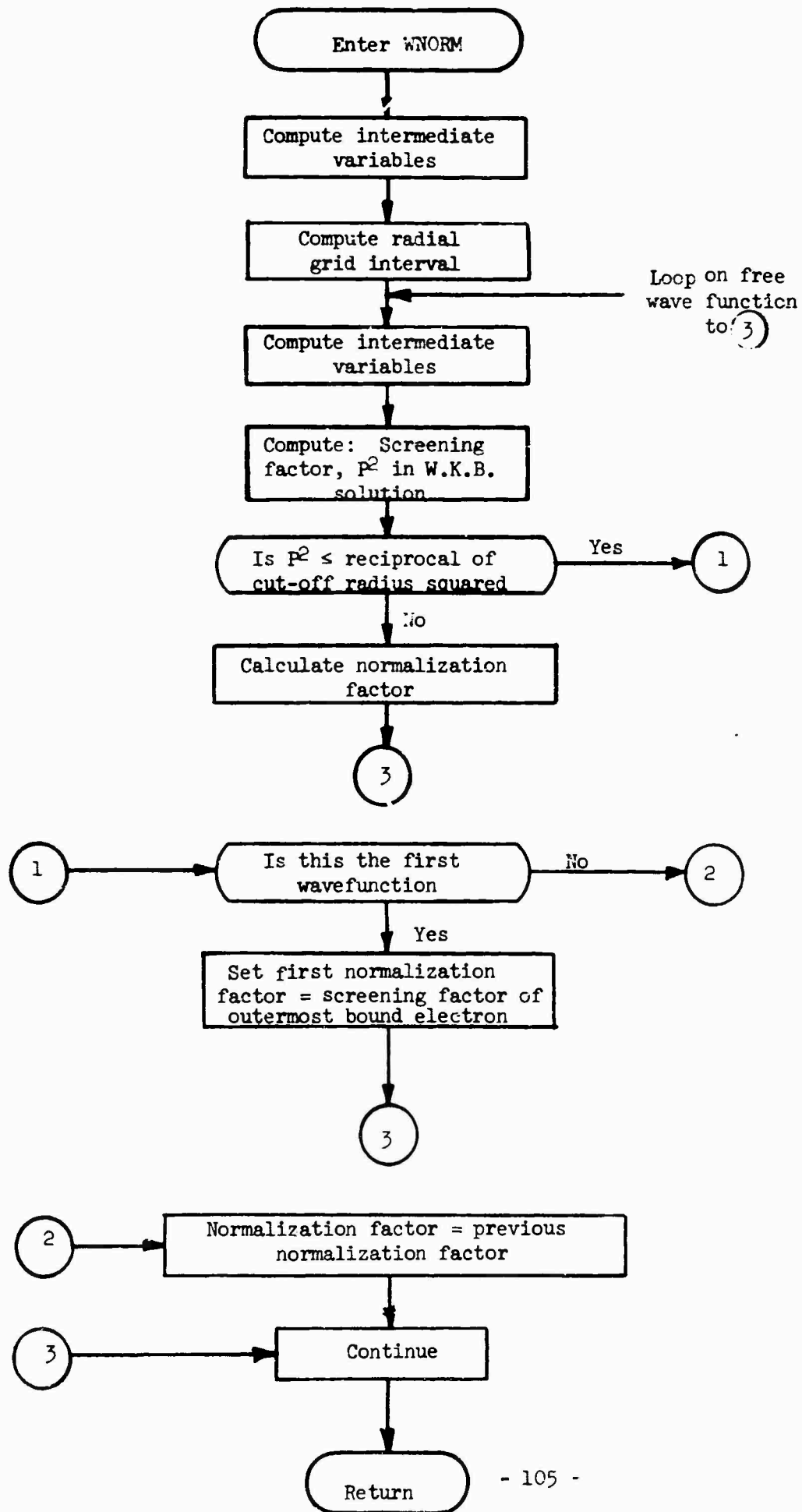
Argument List:

Name	Dimension	Mode	Meaning
RN ϕ RM	30	R	Normalization factors
RX		R	Terminal radius on numerical integration

Local Variables:

Name	Dimension	Mode	Meaning
ϕ VERR		R	Reciprocal of terminal radius
EMVP1		R	Free electron energy - potential energy + 1
EMV		R	Free electron energy - potential energy
ϕ RIGH		R	Radial grid interval
I		I	Loop index on number of free electron states

<u>Name</u>	<u>Dimension</u>	<u>Mode</u>	<u>Meaning</u>
RA, RB		R	Tabulated values of screening factor at grid points bracketing terminal radius
EP		R	Screening attenuation coefficient
P'Q		R	P^2 in W.K.B. solution
PSQP		R	Derivative of P^2



SIB-TC WNR

```

SUBROUTINE WNORM (RNORM,RX)
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30)
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),H
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB
COMMON/TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN
DIMENSION RNORM(30)
OVERR = 1.0 / RX
OVRRSQ = OVERR*OVERR
EMVP1 = EGN-V
EMV = EMVP1-1.0
Y = -V/EMVP1
ORIGH = X(NTAB+1) - X(NTAB)
DO 3 I=1,K2M
PK = CF ( I )
FKSQ = PK*(PK+1.0)
FKR = PK * OVERR
FOR = FKSQ * OVRRSQ
RA = SCF(NTAB)
RB = SCF(NTAB+1)
EP = ALOG(RA/RB)/ORIGH
V1 = EP + OVERR
V2 = V1 * V1 + OVRRSQ
V3 = V1 * V2 + 2.0 * OVRRSQ * (V1 + OVERR)
V1X = V1*Y
V2X = V2*Y
VXSQ = V1X * V1X
FKVR = V1X*FKR
PSQ = EMV * EMV - 1.0 + FKVR - 0.75 * VXSQ + 0.5 * V2X - FOR
IF (PSQ.LE.OVRRSQ) GO TO 1
PSQP = 2.0 * EMV * V * V1 + (FKR - 1.5*V1X) * VXSQ + 2.0* V1X* V2X
1 - 0.5 * V3 * Y - OVERR * (FKVR + PK*V2X - 2.0*FOR)
TERM3 = G(I)*(0.5*V1X-FKR+0.25*(PSQP/PSQ))+F(I)*EMVP1
A = (PI/(SQRT (PSQ)*EMVP1))*(PSQ*G(I) *G(I) +TERM3*TERM3)
RNORM(I) = 1.0/SQRT (A)
GO TO 3
1 IF (1.GT.1) GO TO 2
RNORM(I)=SCREEN
GO TO 3
2 RNORM(I)=RNORM(I-1)
3 CONTINUE
RETURN
END

```

WNR00010
WNR00020
WNR00030
WNR00040
WNR00050
WNR00060
WNR00070
WNR00080
WNR00090
WNR00100
WNR00110
WNR00120
WNR00130
WNR00140
WNR00150
WNR00160
WNR00170
WNR00180
WNR00190
WNR00200
WNR00210
WNR00220
WNR00230
WNR00240
WNR00250
WNR00260
WNR00270
WNR00280
WNR00290
WNR00300
WNR00310
WNR00320
WNR00330
WNR00340
WNR00350
WNR00360
WNR00370
WNR00380
WNR00390
WNR00400
WNR00410
WNR00420

SUBROUTINE XDERIV

Purpose: Supplies the derivatives for the Runge-Kutta integration of the bound-state wavefunctions and the integrands of the matrix elements for numerical integration beyond one-half Bohr radius.

Method: Calculates the derivatives of the radial components from the coupled Dirac radial equations and the integrand of the matrix elements using values obtained by linear interpolation on the Waber grid of bound state wavefunctions.

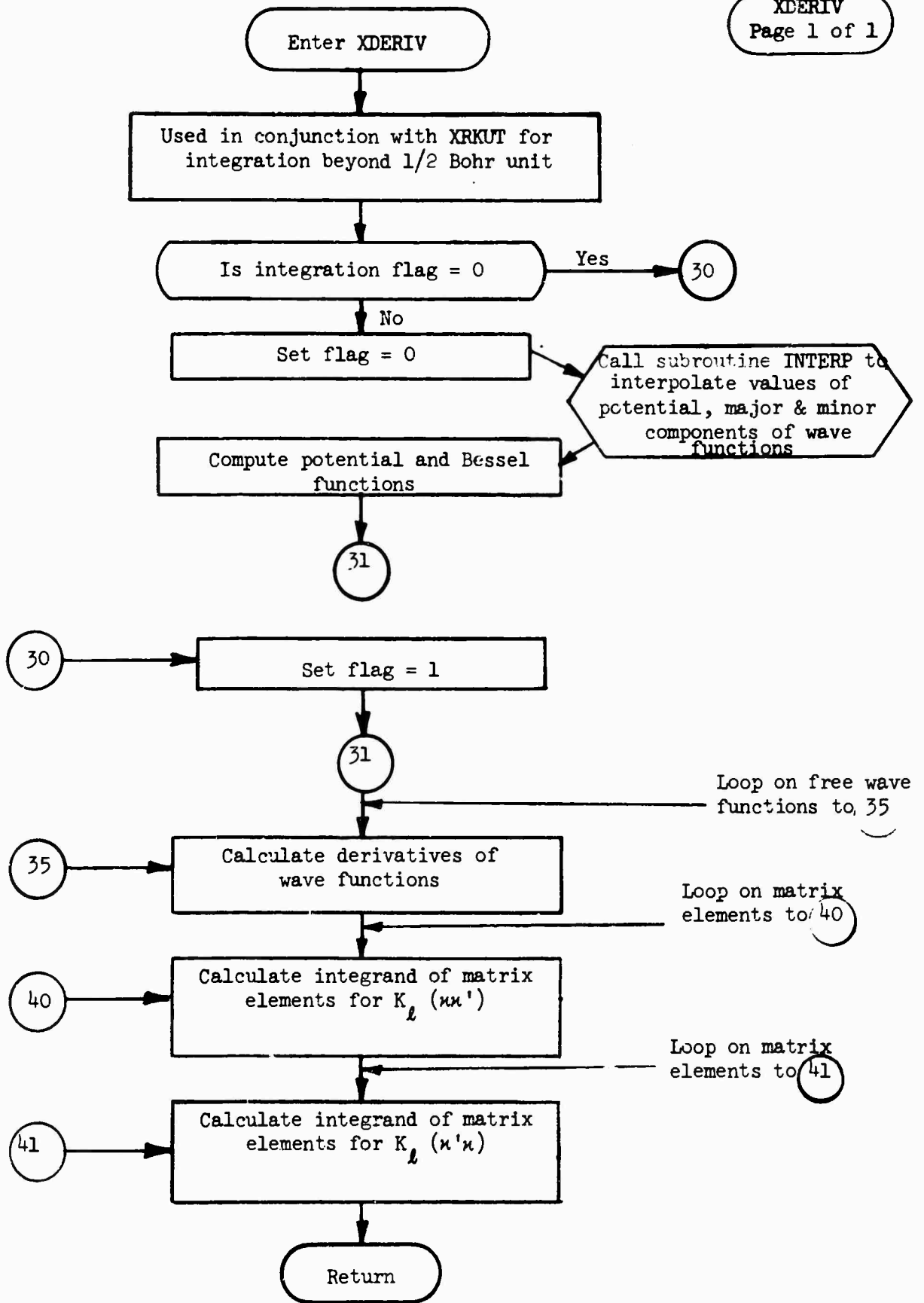
Subroutines called: SPHBES, INTERP

Subroutines called by: XRKUT, RADINT

Labelled Common: BESSEL, DFUNCT, LIMIT, ϕ NWARD, VECT

Local Variables:

Name	Dimension	Mode	Meaning
Z		R	Photon momentum * radius
N		I	Indexing variable



SUBTC XDER

SUBROUTINE XDERIV

COMPUTES DERIVATIVES

	XDR00010
	XDR00020
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30)	XDR00030
COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15)	XDR00040
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),H	XDR00050
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	XDR00060
COMMON /ONWARD/RX,SCX,GBX,FBX	XDR00070
COMMON/VECI/KF(200),KG(200),LBES(200),LBS(200),LKB	XDR00080
IF (NEW.EQ.0) GO TO 30	XDR00090
NEW = 0	XDR00100
CALL INTERP	XDR00110
V = - SCX / RX	XDR00120
Z=0*RX	XDR00130
CALL SPHBES (Z)	XDR00140
GO TO 31	XDR00150
30 NEW = 1	XDR00160
31 DO 35 N=1,K2M	XDR00170
DF(N) = CF(N)*F(N)/RX-(EFN-V)*G(N)	XDR00180
35 DG(N) = CG(N)*G(N)/RX+(EGN-V)*F(N)	XDR00190
DO 40 N=1,NK	XDR00200
I = KG(N)	XDR00210
L = LBES(N)	XDR00220
40 DFK(N) = B(L)*G(I)*FBX	XDR00230
DO 41 N=1,NKP	XDR00240
I = KF(N)	XDR00250
L = LBS(N)	XDR00260
41 DFKP(N) = B(L)*F(I)*GBX	XDR00270
RETURN	XDR00280
END	XDR00290

This page is intentionally left blank.

SUBROUTINE XRKUT

Purpose: Performs the Runge-Kutta integration for radial values beyond one-half Bohr radius. The routine uses linearly interpolated values of the bound-state wavefunctions and the potential.

Method: Runge-Kutta Integration (Gill Form)

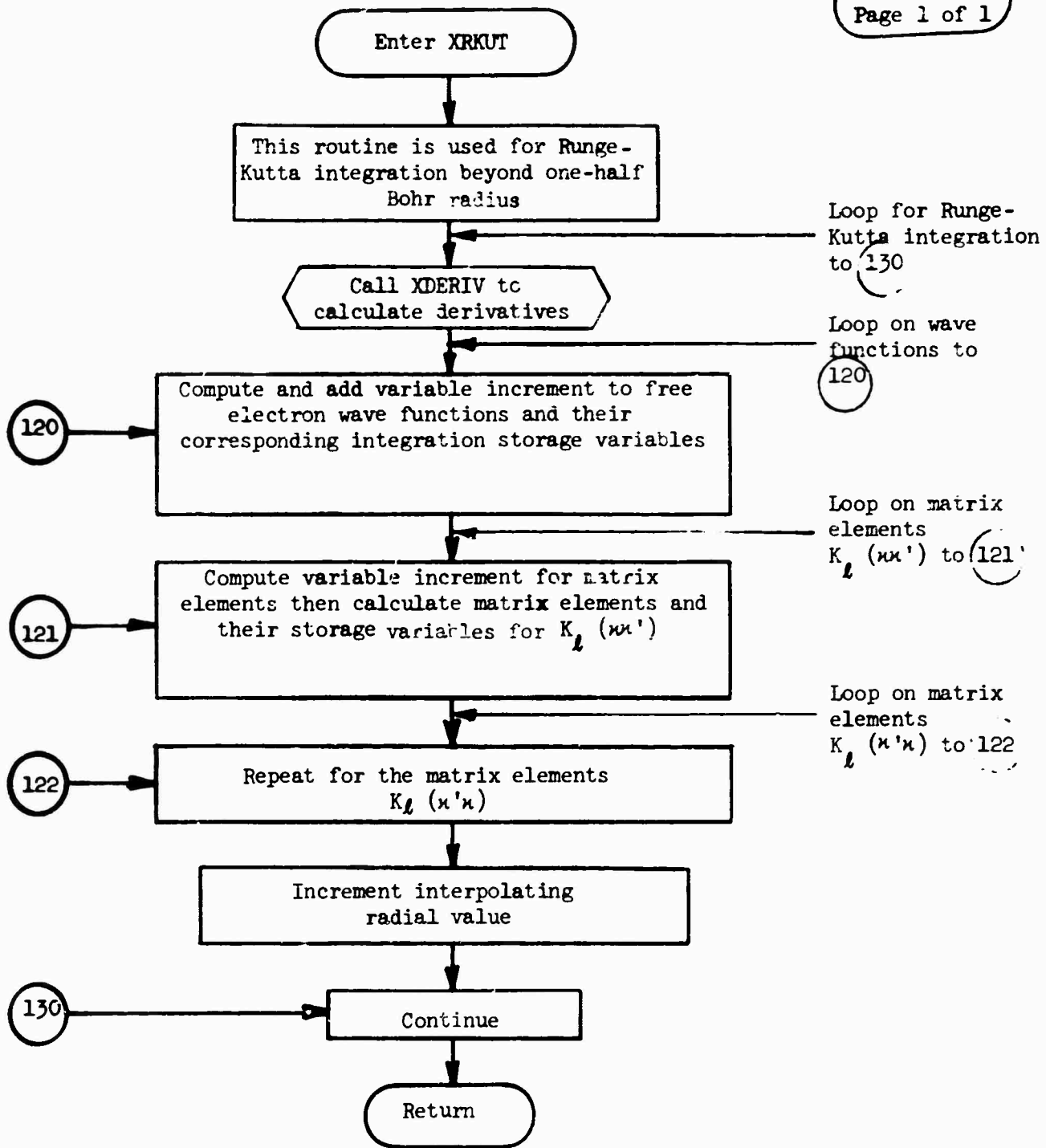
Subroutine called: XDERIV

Subroutine called by: RADINT

Labelled Common: DFUNC, KUT, LIMIT, MAT ϕ WARD

Local Variables:

<u>Name</u>	<u>Dimension</u>	<u>Mode</u>	<u>Meaning</u>
J		I	Loop index on Runge-Kutta integration
I		I	Loop index on; number of free wavefunctions, number of matrix elements $K_l(\mu\mu')$ and $K_l(\mu'\mu)$
Z		R	Incremental variable for "small" component of free electron wavefunction
ZP		R	Incremental variable for "large" component of free electron wavefunction



SUBROUTINE XRRU	
SUBROUTINE XRRUT	XRK00010
RUNGE-KUTTA INTEGRATION	XRK00020
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),H	XRK00030
COMMON /KUT/ RK1(4),RK2(4),RK3(4),RK4(4),K4(4)	XRK00040
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	XRK00050
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT	XRK00060
COMMON /ONWARD/RX,SCX,GBX,FBX	XRK00070
DO 130 J=1,4	XRK00080
CALL XDERIV	XRK00090
DO 120 I=1,K2M	XRK00100
Z = RK1(J)*(DF(I)-RK2(J)*SF(I))	XRK00110
ZP = RK1(J)*(DG(I)-RK2(J)*SG(I))	XRK00120
F(I) = F(I)+H*Z	XRK00130
G(I) = G(I)+H*ZP	XRK00140
SF(I) = SF(I)+3.0*Z-RK3(J)*DF(I)	XRK00150
120 SG(I) = SG(I)+3.0*ZP-RK3(J)*DG(I)	XRK00160
DO 121 I=1,NK	XRK00170
Z = RK1(J)*(DFK(I)-RK2(J)*SFK(I))	XRK00180
FK(I) = FK(I)+H*Z	XRK00190
121 SFK(I) = SFK(I)+3.0*Z-RK3(J)*DFK(I)	XRK00200
DO 122 I=1,NKP	XRK00210
Z = RK1(J)*(DFKP(I)-RK2(J)*SFKP(I))	XRK00220
FKP(I) = FKP(I)+H*Z	XRK00230
122 SFKP(I) = SFKP(I)+3.0*Z-RK3(J)*DFKP(I)	XRK00240
RX = RX+RK4(J)*H	XRK00250
130 CONTINUE	XRK00260
RETURN	XRK00270
END	XRK00280

This page is intentionally left blank.

Unclassified

Security Classification

DOCUMENT CONTROL DATA - R&D		
<i>(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)</i>		
1 ORIGINATING ACTIVITY (Corporate author) Union Carbide Corporation	2a REPORT SECURITY CLASSIFICATION Unclassified	2b GROUP
3 REPORT TITLE Low Energy Photoelectric Cross Section Calculations Vol. I: Theory and Results; Vol. II: Program Description		
4 DESCRIPTIVE NOTES (Type of report and inclusive dates) Final Report - Inclusive dates of research were 1 June 1966 to 30 June 1967		
5 AUTHOR(S) (Last name, first name, initial) Vol. I - Brysk, Henry; Zerby, Clayton D. Vol. II - Brysk, Henry; Glick, Arnold		
6 REPORT DATE 31 July 1967	7a TOTAL NO OF PAGES I - 54; II - 120	7b NO OF REFS I - 18; II - none
8a CONTRACT OR GRANT NO. DA-49-146-XZ-511	9a ORIGINATOR'S REPORT NUMBER(S) UCC/DSSD - 299	
8b PROJECT NO.	9b OTHER REPORT NO(S) (Any other numbers that may be assigned this report) DASA-2023, Volume I and DASA-2023-1, Vol I	
10 AVAILABILITY/LIMITATION NOTICES Not for open publication. Each transmittal of this document outside the agencies of the U.S. Government must have prior approval of the Director, DASA, Washington, D. C. 20305.		
11 SUPPLEMENTARY NOTES	12 SPONSORING MILITARY ACTIVITY Air Force Weapons Laboratory	
13 ABSTRACT		

DD FORM 1473
1 JAN 64

Ans 4