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BURIED ANTENNA PERFORMANCE: DEVELOPMENT OF SMALL RESONANT BURIED ANTENNAS

Howard E. Bussey, et al

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Small resonant dipole antennas at 145 MHz were developed suitable to be buried for concealment. Theory of the pattern and the loss of buried dipoles is summarized. Experiments are described that confirm the theory. The circuit representation of a resonator is utilized in measuring and analyzing the Q, bandwidth, and impedance of the antennas. The field strength performance of buried candidate antennas was measured and agreed with expected losses due to burial and inefficiency. Theoretically a resonant horizontal magnetic

20. ABSTRACT (continued)

dipole has the lowest burial loss for the fully buried condition. A resonant horizontal electric dipole may have equally low loss in practice because its efficiency is better (for the size allowed). Low (ten centimeter) profile vertical electric dipoles, not fully buried, exhibit even smaller losses and would be useful. The performance of these buried antennas could be improved by allowing a larger encapsulation.

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FOREWORD

This Final Report is by the National Bureau of Standards, Electromagnetics Division, Boulder, Colorado, for Rome Air Development Center, Griffiss Air Force Base, New York, under Contract F30602-72-F-0332, Job Order 692B0304. NBS Project Number is 2727438. Mr. Russell A. King (DCCN) was the RADC Project Engineer.

The report describes a study performed from May 1972 to August 1973.

This report has been reviewed by the RADC Information Office (CI) and is releasable to the National Technical Information Service (NTIS).

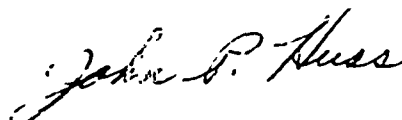This technical report has been reviewed and is approved.

APPROVED:

RUSSELL A. KING
Project Engineer

APPROVED:

FRED I. DIAMOND, Technical Director
Communications and Navigation Division

FOR THE COMMANDER:

JOHN P. HUSS
Acting Chief, Plans Office

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Evaluation

This effort was a study to investigate, theoretically and experimentally, the possibility of Burst Communication by radio transmission from an antenna buried for concealment. Low transmitter power, 1 watt, maximum antenna width of 5 inches and VHF frequency were major parameters. The emphasis was on antenna design and not communications system design. The results of the study indicate theoretically useful ground to airborne communications.

In view of the theoretical and experimental feasibility indicated, an expansion of the effort is recommended. It should include further experimentation and flight testing to explore the more practical aspects of adapting the experimental antennas to existing buried transmit devices. An experimental buried antenna/transmit combination unit should be constructed for this purpose.

Laurel a King

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1. INTRODUCTION

The objective of this effort is to provide engineering
services to study the feasibility and practicality of low power
radio frequency transmissions from antennas that are buried
just below the surface of the earth. Burial is for concealment
only.

The main purpose is to predict the communications range
to an assumed receiver from a buried transmitting antenna. In
doing this the theory of buried antennas, which is available in
the literature. is outlined; experiments were performed to con-
firm the theory; and small resonant antennas for burial were
developed and tested. Construction details are given for some
candidate antennas.

Compromises and trade-offs are described for various types
of antennas, e.g., vertical and horizontal dipoles. The main
factor in the research is the requirement of a small antenna to
allow convenient burial deployment. This requirement was ac-
complished by the use of resonant antennas at the assigned fre-
quency, 145 MHz.

The theory of emission from a buried source to the air space
is discussed in section 2. The general properties of resonant
antennas are described in section 3. The effects of burial on
impedance, bandwidth, efficiency, and pattern are described in
section 4, and a series of candidate antennas is described.
Experimental results for the candidates are given in section 5.
The maximum communication range is predicted in section 6.

2. THEORETICAL FIELD CALCULATIONS

A. INTRODUCTION

A theoretical discussion of the effect of burial in the ground on antenna performance consists of three main aspects: one aspect is the change of the efficiency of the antenna; the second aspect is the exact field pattern calculation; and the third aspect is the change in impedance, and especially the change in the resonant frequency of resonant antennas. The determination of efficiency of buried antennas by theoretical methods has been done only for certain antennas, e.g., for a spherical dipole [1]. Theoretical work on efficiency was not done in the present contract. Experimental determinations of efficiency are discussed in a later section.

The field at a receiving point in the air may be compared to that from a monopole set on the ground at the place where the radiation emerges from the buried antenna. This method makes it clear how much loss arises from the burial. A more rigorous method is to state the loss relative to an isotropic source. This method shows the total effect of the burial and the propagation. Both presentations will be used.

B. GAIN PATTERN IN AIR OF A BURIED DIPOLE

The field in the air space is greatly influenced by the burial. The notation TM and TE waves will be used to denote* the wave components with horizontal magnetic vector and horizontal electric vector respectively. Table 1 indicates some characteristics of the waves from buried dipoles and from a reference quarter wavelength monopole set on the earth. The latter is a useful basis for comparison. It has approximately -3 dB gain with respect to isotropic at 10° elevation angle.

---

*Another notation for TM and TE is vertically and horizontally polarized respectively.

Dipole antennas, including a small loop which is a magnetic dipole, are considered almost exclusively. The following notation will be used:

> VED, vertical electric dipole;
> VMD, vertical magnetic dipole;
> HED, horizontal electric dipole;
> HMD, horizontal magnetic dipole.

A buried vertical dipole gives a weaker field throughout the air space than does a buried horizontal dipole, other things being equal, and the dielectric constant, ε', of the ground being greater than 2, which is almost always the case. This is due to the cone of emission from the ground into the air space (fig. 1). For $\varepsilon' = 6$ the cone angular radius is 24°. The vertical dipoles give no emission straight up and at 24° the underground pattern factor of the dipole is 8 dB weaker than the maximum, which occurs in the broadside direction.

The buried horizontal dipole sends maximum energy straight up. The horizontally traveling surface wave is emitted at 24° from maximum of the dipole, for both the TE and TM polarizations, causing at most 0.7 dB loss due to the underground pattern factor of the dipole at 24° from broadside, ε being 6.

For any antenna system the field strength decreases at low elevation angles, as indicated in table 1. At low angles the buried antenna exhibits an approximately constant loss compared to an antenna on the surface, see last line of table 1. This extra loss due to burial is explained in sections C and D below. The loss is about 30 dB for TM wave and 40 dB for TE waves at 1° elevation angle, ε' being 6. The TM wave is almost always stronger than the TE wave and is therefore more useful. Also it gives a ground wave, useful for nearby on-the-ground reception.

Power gain is defined in the footnote of table 1.

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Table 1. Fields of a monopole, and various dipoles buried in
earth, with dielectric constant = 6 and conductivity = 0.003 S/m,
stated relative to an isotropic emitter. Depth is assumed zero.
The eighth line shows the depth attenuation per meter.

Antenna	TM/TE Character	Power Gain[a]		
		10° Elevation	1° Elevation	2° Elevation
λ/4 monopole with λ/2 radius metal ground plane	TM	∿ -3 dB	∿ -18 dB	∿ -14 dB
Buried VED	TM	-21.8 dB	-38.7 dB	-33.0 dB
Buried VMD	TE	-25.9 dB	-46.1 dB	-40.2 dB
Buried HED	TM	-14.6 dB	-31.7 dB	-26.1 dB
	TE	-19.0 dB	-38.3 dB	∿ -32.6 dB
Buried HMD	TM	-13.8 dB	-30.9 dB	-25.4 dB
	TE	-19.8 dB	-39.1 dB	-33.3 dB
1 meter depth absorption	TE,TM	-2.19 dB	-2.20 dB	- 2.20 dB
Buried HED relative to surface monopole	TM	-11.6 dB	-13.7 dB	-12.1 dB

(a) The power gain of an antenna at any angle is the ratio of
     the power density observed to the theoretical power density
     that would have been furnished by an isotropic emitter in
     free space at the same distance.
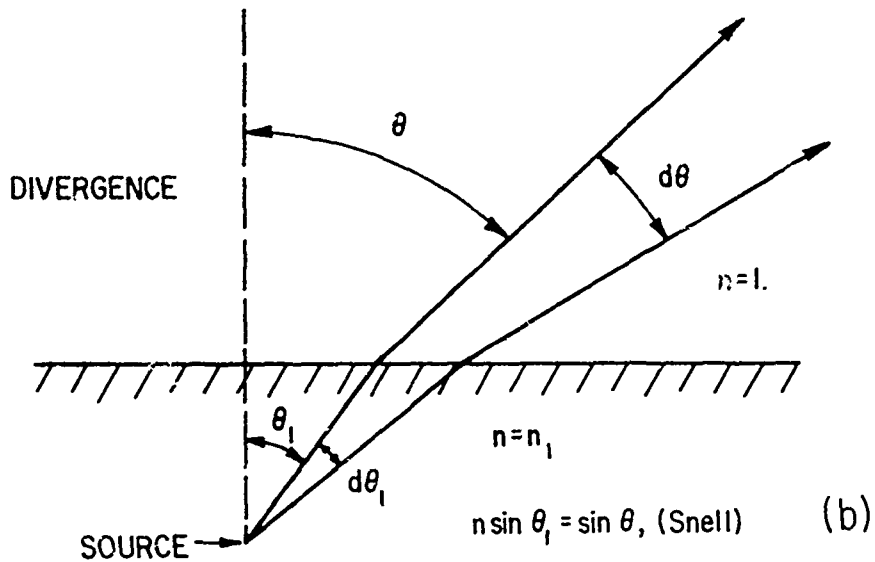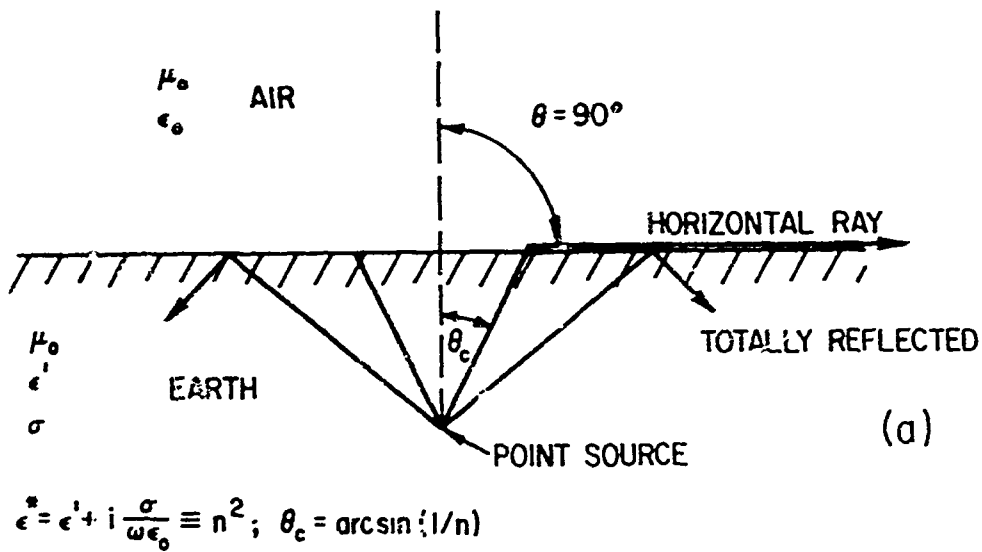
Figure 1, a. Rays at critical angle; b. divergence.*

*Long captions for all figures are given in the "List of Figures". The caption accompanying each figure will usually be abbreviated.

C. THEORETICAL DERIVATION OF THE PATTERN GAIN

A convenient summary of buried antenna theory is that of Hufford [1]. Earlier results include [2], [3], [4]. The Sommerfeld method for a dipole in a half space is used. The final results are given below. The notation is as follows:

ε_0, μ_0 are the constitutive parameters of free space.

In the ground $\mu_1 = \mu_0$, and the complex refractive index, n, is given by

$$n^2 = \varepsilon_1/\varepsilon_0 = \varepsilon' + i\,\sigma/(\omega\varepsilon_0); \text{ also } \varepsilon^* = \varepsilon_1/\varepsilon_0.$$

σ = conductivity, S/m.

$$k_0 = \omega(\mu_0\varepsilon_0)^{\frac{1}{2}}, \quad Z_0 = \sqrt{\mu_0/\varepsilon_0},$$
$$k_1 = nk_0, \quad Z_1 = Z_0/n,$$
$$\sin\theta_1 = \sin\theta/n \quad \text{(complex Snell's law)},$$
$$\cos\theta_1 = (n^2-\sin^2\theta)^{\frac{1}{2}}/n,$$

loss tangent = $\varepsilon''/\varepsilon' = \sigma/(\varepsilon'\varepsilon_0\omega)$, $\omega = 2\pi f$.

A ray at the critical angle of incidence in the ground, θ_c, emerges horizontally with $\sin\theta = 1$ in the air, figure 1a, thus

$$\sin\theta_c = 1/n, \quad \cos\theta_c = (n^2-1)^{\frac{1}{2}}/n.$$

The equations for the far fields in the air at a height greater than a few wavelengths, due to dipoles buried in a flat earth (half space), for TE and TM waves respectively, are stated relative to the field of an isotropic emitter in free space as follows [1]:

$$E_e/E_f = L\,C_e\,D\,A_e$$
$$E_m/E_f = L\,C_m\,D\,A_m$$
$$L = 2/(\operatorname{Re}\,n)^{\frac{1}{2}}$$
$$D = \exp\,(i\,k_0\,h(n\cos\theta_1-\cos\theta))$$
$$C_e = \cos\theta/(n\cos\theta_1+\cos\theta)$$
$$C_m = \cos\theta/(\cos\theta_1+n\cos\theta), \tag{1}$$

where

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$$A_e = 0, \qquad \text{VED}$$

$$A_m = -i(3/2)^{\frac{1}{2}} \sin \theta_1, \quad \text{VED} \tag{2}$$

$$A_e = i(3/2)^{\frac{1}{2}} \cos \phi, \quad \text{HED}$$

$$A_m = i(3/2)^{\frac{1}{2}} \cos \theta_1 \sin \phi, \quad \text{HED} \tag{3}$$

$$A_e = i \, n/|n| \times (3/2)^{\frac{1}{2}} \sin \theta_1, \quad \text{VMD}$$

$$A_m = 0, \qquad \text{VMD} \tag{4}$$

$$A_e = -i \, n/|n| \times (3/2)^{\frac{1}{2}} \cos \theta_1 \sin \phi, \quad \text{HMD}$$

$$A_m = i \, n/|n| \times (3/2)^{\frac{1}{2}} \cos \phi, \quad \text{HMD} \tag{5}$$

ϕ = the azimuth angle measured from an axis that is perpendicular to the horizontal dipoles.

Equations (2) to (5) are equations (7.18), (7.19), (7.23), and (7.24) of [1]. The p.oduct LCD of equation (1) would be used for a buried isotropic point source. The factor A represents the effects of coupling the dipole pattern to the angular cone of emission. The field E_f of an isotropic emitter of power W watts in free space is

$$E_f = (W \, Z_0/4\pi R^2)^{\frac{1}{2}} \quad \text{V/m, rms}$$

$$= (30 \, W)^{\frac{1}{2}}/R. \tag{6}$$

The range R is measured in meters.

The simplicity and utility of Hufford's normalization (to an isotropic source) should be noted. Many of the theoretical formulations give the field pattern for a dipole with a specified current or a specified dipole moment, which leaves the reader with some work to do, to find the current or moment from the power. By the present method [1] from W and R, the E field of an isotropic source is found from equation (6), assuming 100 percent efficiency. Then one applies the gain pattern of the buried source, equations (1)-(5), and gets the predicted field in the air.

The predicted ground wave is found in the same way using equations (18)-(20), section E, below.

D.   PHY. iCAL OPTICS OF BURIED ANTENNAS, [9]

It is instructive to try to obtain the transmitted far field based on physical optics. There are three main steps: one step is to find the power transmission factor of the interface using plane wave concepts; a second step is to obtain the change in the spherical wave divergence factor at the interface, considering the point source aspects; and the third step is to calculate the absorption in the ground.

The interface transmission coefficient may be found from Fresnel's equations and conservation of energy. The refractive index is temporarily assumed to be real, and losses are added later. The power transmission coefficients for a plane wave in the dense medium refracted into the vacuum (air) are:

$$T_e^2 = \frac{4n \cos \theta_1 \cos \theta}{(n \cos \theta_1 + \cos \theta)^2},$$
(7)

$$T_m^2 = \frac{4n \cos \theta_1 \cos \theta}{(\cos \theta_1 + n \cos \theta)^2},$$
(8)

where e and m denote TE and TM waves respectively. These are obtained from Fresnel's field equation, section 9.5 of [5], taking into account changes of the impedance and the area of a beam at an interface.

Considering the spherical wave from an elementary doublet as a bundle of rays we find the change in the solid angle due to refraction into the air space, figure 1. The spherical angles are

$$d\Omega_1 = \sin \theta_1 d\theta_1 d\phi_1, \text{ in the earth}$$
$$d\Omega = \sin \theta d\theta d\phi, \text{ in the air.}$$
(9)

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It is true that

$$d\phi_1 = d\phi. \tag{10}$$

From Snell's law

$$\sin \theta = n \sin \theta_1, \tag{11}$$

and by differentials

$$\cos \theta d\theta = n \cos \theta_1 d\theta_1. \tag{12}$$

Using equation (10) and equation (12) in equation (9) we have

$$d\Omega = \sin \theta d\phi_1 \, n \cos \theta_1 d\theta_1 / \cos \theta. \tag{13}$$

The power per solid angle in the air relative to the power per solid angle in medium 1 is the power gain of the interface transmitting into the air. Denoting this as $p_{12,e}$ for a TE mode wave

$$p_{12,e} = \frac{p_0 \, 4n \cos \theta_1 \cos \theta}{(n \cos \theta_1 + \cos \theta)^2 \sin \theta d\phi_1 \, n \cos \theta_1 d\theta_1 / \cos \theta}$$

$$\div \frac{p_0}{\sin \theta_1 d\theta_1 d\phi_1}$$

$$p_{12,e} = \frac{4 \cos^2 \theta}{(n \cos \theta_1 + \cos \theta)^2 \, n} \tag{14}$$

Likewise for the TM case

$$p_{12,m} = \frac{4 \cos^2 \theta}{(\cos \theta_1 + n \cos \theta)^2 \, n} \tag{15}$$

Equations (14) and (15) are identical to $(L \, C_e)^2$ and $(L \, C_m)^2$ of equations (1) using a real refractive index. The inclusion of complex n and θ_1 requires that the squares be replaced by absolute values squared.

The pattern factor A of a dipole in the ground includes $\sqrt{3/2}$, and $\sin \theta_1$ for vertical dipoles, $\cos \theta_1$ for horizontal dipoles, end fire, and a sine or cosine of ϕ appears, see equations (2) to (5).

Finally the attenuation in the ground may be obtained approximately from the propagation factor in the ground and the ray optical distance,

$$D' = e^{ik_1 d/\cos \theta_1'}, \tag{16}$$

where $k_1 = k_0 n$ is the complex wave number and θ_1' is a real angle defined as the direction of a plane wave refracted by the ground using the velocity in the ground, c/n'. An approximate Snell's law with this assumption is

$$\sin \theta_1' = n'^{-1} \sin \theta, \tag{17}$$

where n' is the real part of the complex refractive index of the ground. The attenuations given by D of equations (1) and by D' of equation (16) are nearly the same in spite of the different forms. The attenuation exponent in equation (16) becomes 1 percent greater than in equations (1) when the loss* tangent is 0.6. A correct electromagnetic treatment of equation (16) is given in section 9.8 of reference [5] as well as in [1].

E. GROUND WAVE

The ground wave ($\theta = 90°$) is obtained from a Sommerfeld type of theory. Equations (1) are replaced by [1],

$$E_e/E_f = S_e U_e \, DA_e/(-ik_0 R)$$
$$E_m/E_f = S_m U_m \, DA_m/(-ik_0 R), \tag{18}$$

where R is the horizontal distance to the field point, and

$$S_e = 2/\left((Re \; n)^{\frac{1}{2}} \times (n^2-1)\right),$$
$$S_m = 2 \, n^3/\left((Re \; n)^{\frac{1}{2}} \times (n^2-1)\right), \tag{19}$$

*Provided also $\varepsilon' > 5$.

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$$U_e = 1 - i \, k_0 \, z \, Z_0 \cos \theta_c / Z_1,$$
$$U_m = 1 - i \, k_0 \, z \, Z_1 \cos \theta_c / Z_0, \tag{20}$$

where z is the height of the field point above the interface; z is restricted to a few wavelengths. At greater heights the space wave approximation, equations (1), are used. Equations (18) state that the ground wave field decays at 1/R relative to the reference field E_f which already decays as 1/R, equation (6). The ground wave is not important when the receiving station is an aircraft. There is evidence of the ground wave in the field trials described below. The receiving tower was 30.5 m horizontally from the point of burial. The theoretical loss at low angles is greater than that observed at low angles. For example, the gain at 2° elevation angle should be approximately 12 dB less than the gain at 10° elevation angle. The experiments show approximately a 6 dB difference. We therefore usually discuss results at 10° elevation angle. Another evidence of the ground wave occurs in figure 11. With no ground wave the results for the two reference monopoles would nearly coincide, as in figure 9. The ground wave, stronger at lower frequencies, shows clearly as a difference in the fields at low angles.

F. CALCULATION OF THE FIELD FROM EQUATIONS (1)

A computer program was written to evaluate the field in the air of a buried dipole, from equations (1). The important factor from these equations for low-angle reception is LC which, as we have seen in section 2D, arises from divergence and from the Fresnel transmission. The power gain due to LC combined with the broadside power gain of a dipole, 1.5, will be denoted as the interface gain, I. However, the term interface loss will also be used for I. Figure 2 shows the TM wave interface loss in dB, at certain angles, versus ε' of the earth. Specifically the curves give the value in dB of

$$I = 1.5|LC|^2 = 6 \cos^2 \theta / (n'|\cos \theta_1 + n \cos \theta|^2).$$

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The transformation from the buried dipole to the air space is often adequately represented by I, since depth attenuation and underground pattern factors may be taken as zero dB.

The next factor considered is depth attenuation computed from $|D|^2$ in equations (1). Figure 3 shows the depth attenuation in dB/m for a range of ground conditions.

There are some simple factors remaining to obtain a complete evaluation of equations (1):

1. The azimuthal variation of a horizontal dipole is either $\sin \phi$ or $\cos \phi$ as indicated in equations (2)-(5).

2. The vertical dipole has an important factor $|\sin \theta_1|^2$, see figure 4. (This factor is sufficient to remove the fully buried vertical dipole from consideration for high ε'; however, partial burial will be discussed.)

3. The horizontal dipole has a factor $|\cos^2 \theta_1|$ for the end fire component. This is of interest for the TM wave from the HED. It is a small factor under usual conditions (fig. 4).

In summary, figures 2, 3, 4 can be used to determine the loss (neglecting inefficiency) of the TM wave from a buried horizontal elementary dipole, or a buried VED.

The graphs, which concentrate on low elevation angles, are based entirely on equations (1). For the TE wave emitted end fire from a HMD use figures 3, 4, and 5. The TE and TM waves emitted broadside from the horizontal electric and magnetic dipoles do not suffer the underground pattern factor, figure 4.

An example of using the curves may be useful. Consider the TM wave of a horizontal electric dipole buried 0.1 m deep in ground with $\varepsilon' = 10$ and $\sigma = 0.01$ S/m. The receiving point is at 2° elevation angle. We sum the following losses

Interface loss (fig. 2)------------27.0 dB
Depth attenuation (fig. 3)--------- 0.55 dB
Underground pattern (fig. 4)------- 0.45 dB
Total loss   28.0 dB

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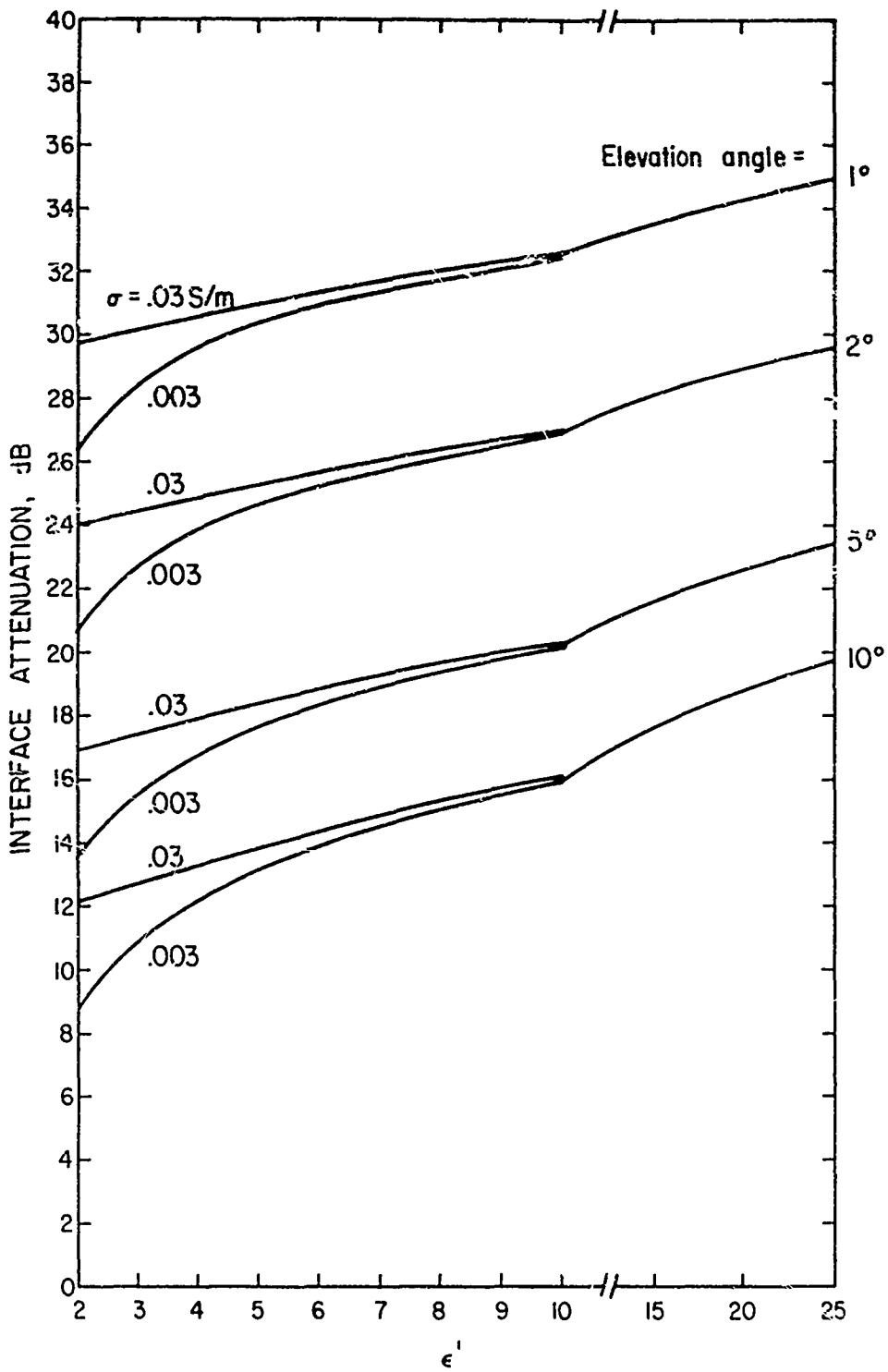
Figure 2. Interface-divergence loss of TM wave.

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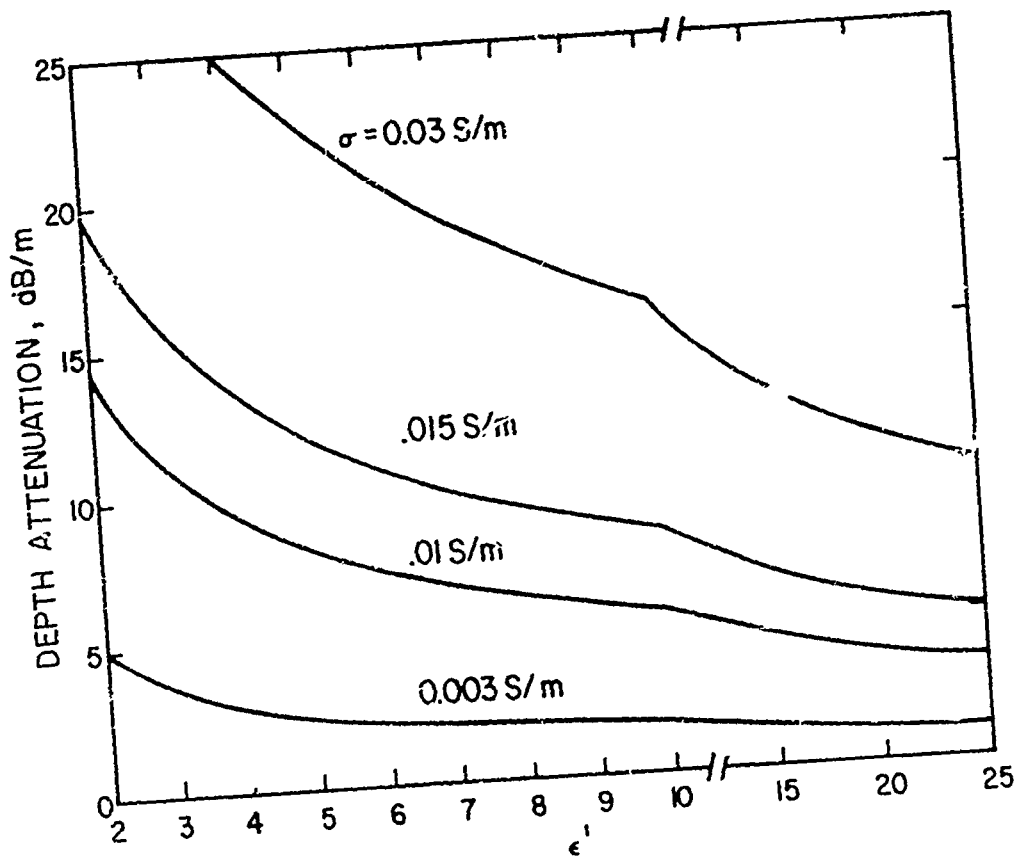
Figure 3. Depth Attenuation.

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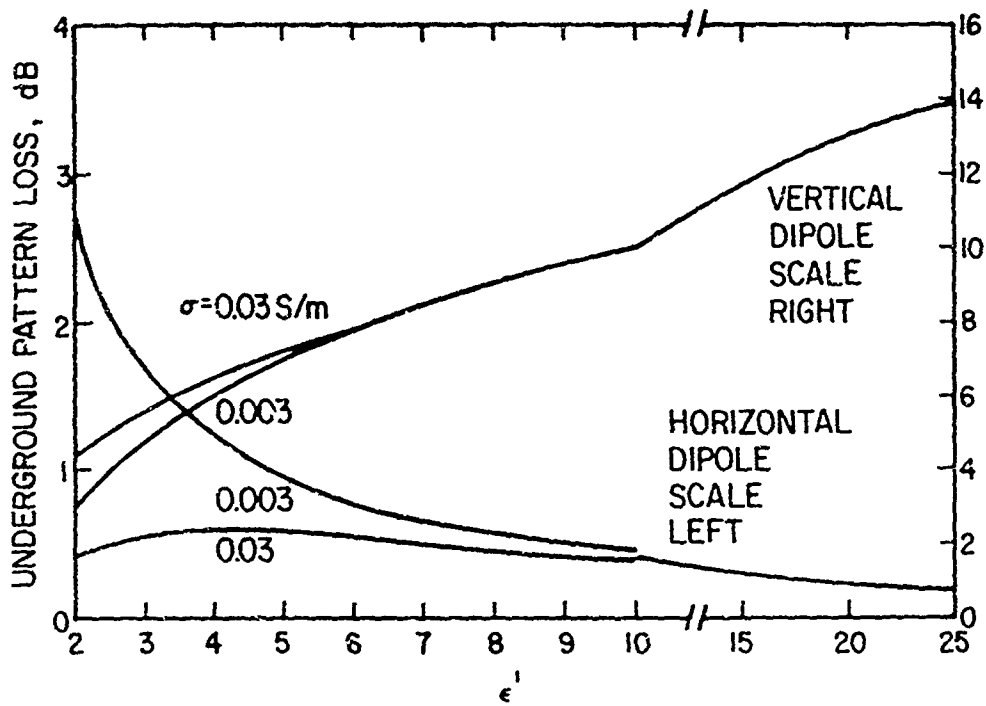
Figure 4. Underground pattern loss.

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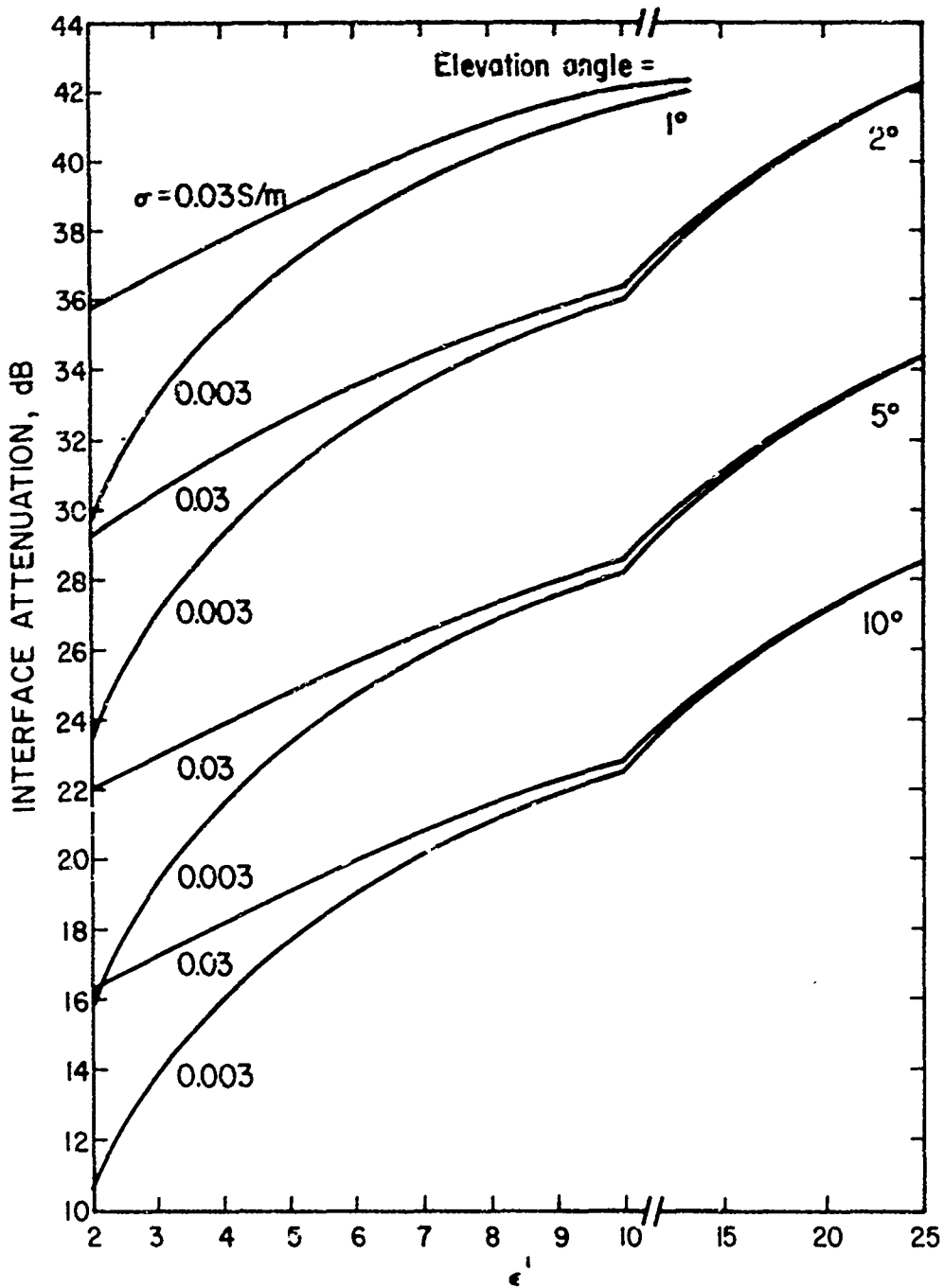
Figure 5. Interface-divergence loss of TE wave.

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At an elevation angle of 10°.

Interface loss (fig. 2)------------16.0 dB

Depth Attenuation (computer)------- 0.54 dB

Underground pattern (computer)----- 0.44 dB

Total loss   16.98 dB

The main factor during shallow burial will be the interface loss, and it depends strongly on the elevation angle.

The TM wave from a horizontal magnetic dipole (HMD) has a small advantage over that from the HED in that the underground pattern factor is zero dB.

Figure 4 shows that the vertical dipoles have more loss than the horizontal dipoles. This is because the vertical dipole is working mainly end fire in exciting the interface within the critical angle θ_c.

G.   EFFICIENCY

The received field strength also depends on the efficiency of the antenna, which is influenced by burial. Efficiency will be treated experimentally, below.

3. EXPERIMENTS COMPARED TO EQUATIONS (1)

A. INTRODUCTION

Experiments were carried out initially mainly to verify the theory contained in equations (1). Later, the main purpose was to develop resonant antennas where the focus is on efficiency, impedance, Q factor, and ground effects on these. The comparison with theory was quite satisfactory, thus allowing the main emphasis to be on the resonant antenna development in the later work which is described in sections 4 and 5.

The agreement of the experiments with the theory contained in equations (1) occurs mainly in two areas:

(1) The predicted absolute value of the fields relative to an isotropic source are approximately correct, including the fact that the TE waves are weaker than TM waves.

(2) The gain pattern as a function of elevation angle is approximately correct.

The remainder of this section describes the experimental measurement method and illustrates results that yield the above conclusions.

Figure 6 shows the main elements of an experimental system for measuring [8] field strength and antenna gain.

B. TRANSMITTED POWER

Direction couplers measure the forward and reverse power, denoted as P_1 and P_2 respectively. The attenuation (fig. 7) of the RG-9 cable of length u was measured at 72° and 32°F using a network analyzer. The curve shown for 50°F was interpolated.

Assuming that the directivity of the two couplers is infinite, the power delivered to the antenna is

$$P_a = P_1 \, 10^{-dB_c/10} - P_2 \, 10^{+dB_c/10}, \qquad (21)$$

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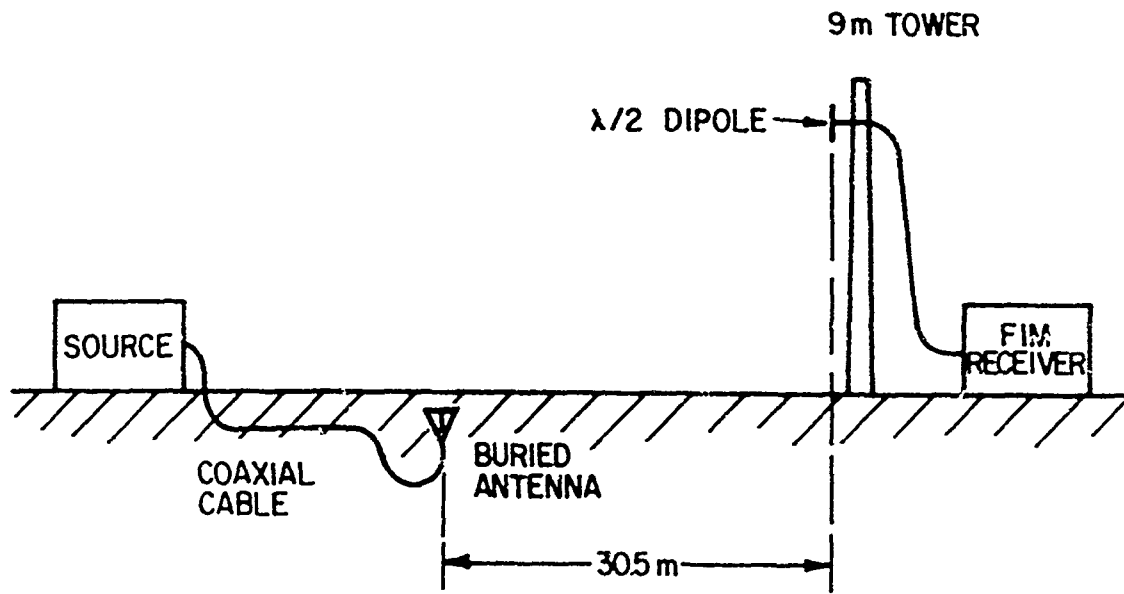
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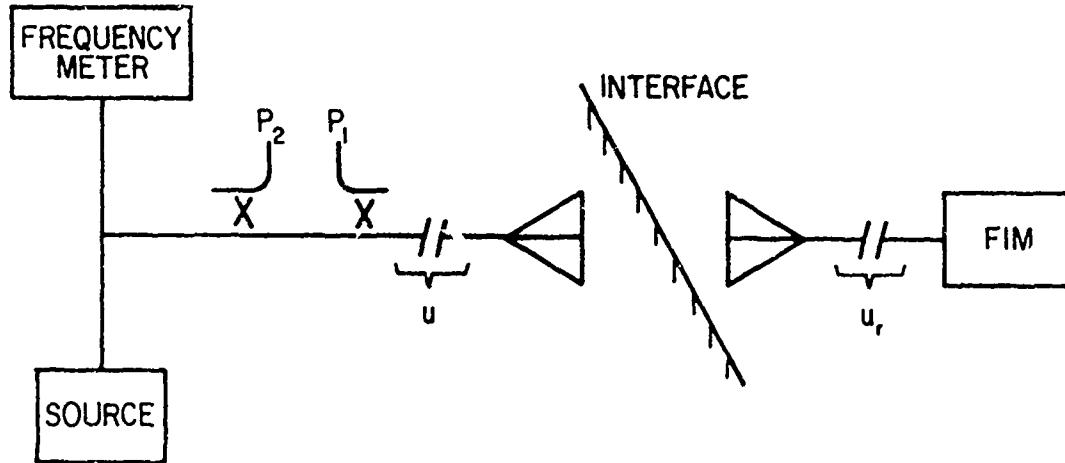
(b)

Figure 6. Experimental system for field measurements.

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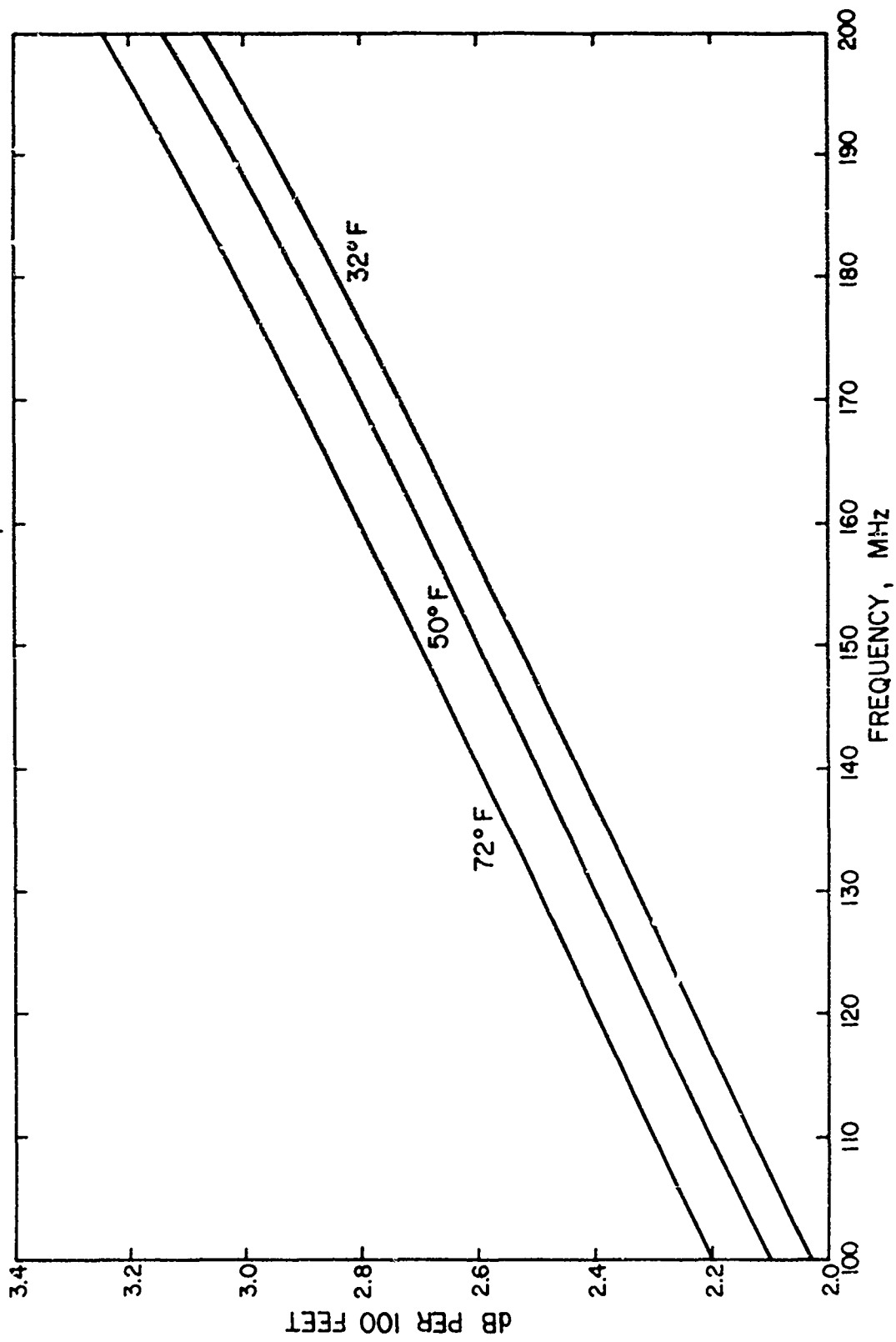
Figure 7. Measured one-way attenuation of cable.

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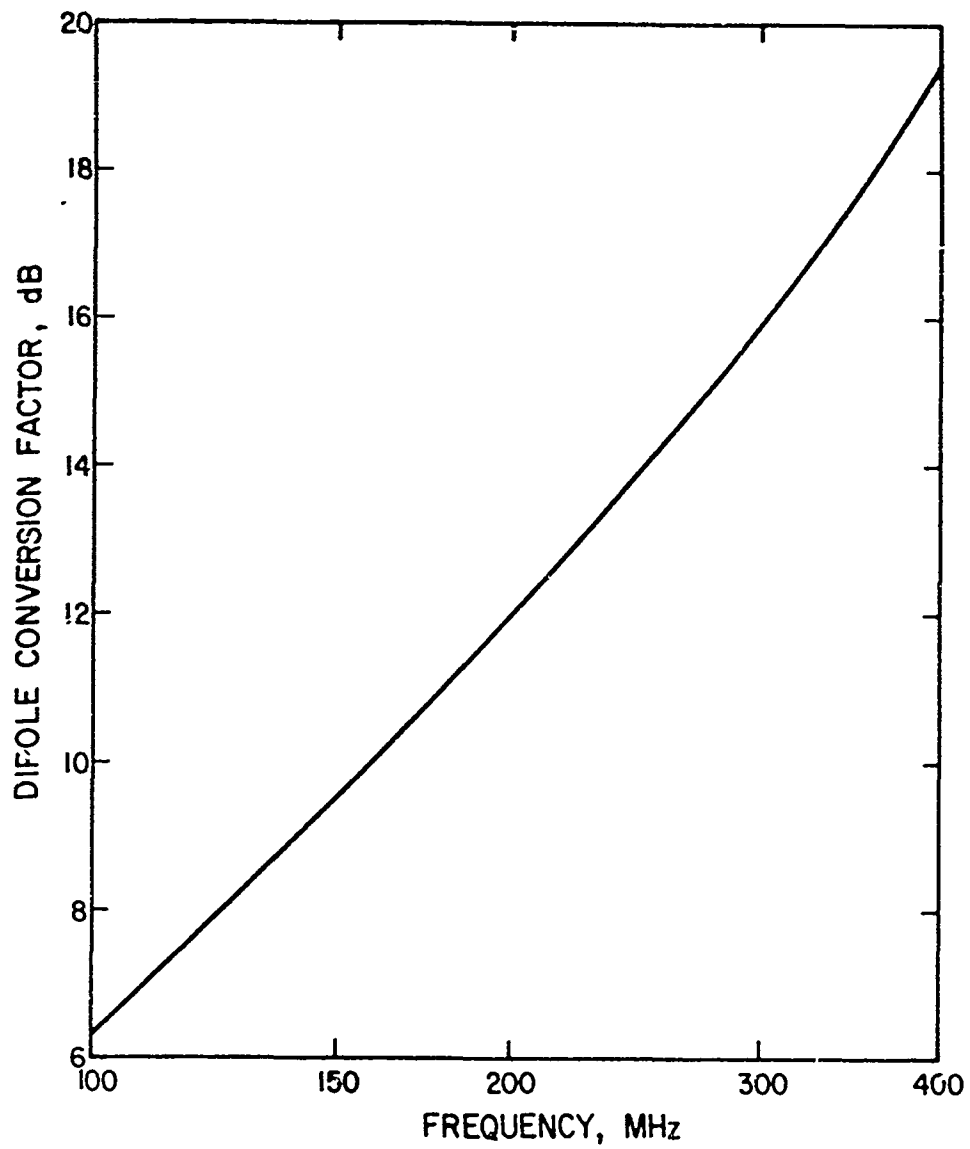
Figure 8. Field strength conversion factor of receiver.

where dB_c is the one way attenuation of the cable with reflectionless terminations.

The radiated power, P_r, is P_a multiplied by the efficiency, J, of the antenna

$$P_r = J P_a. \tag{22}$$

The efficiency of an antenna is the ratio of radiated power to the total input power, which consists of ohmic heating power plus radiated power

$$J = P_r/P_t = P_r/(P_r+P_{cu}), \tag{23}$$

where P_{cu} denotes ohmic heating power.

The efficiency of the antennas was measured and estimated, as will be discussed in section 4E.

C. FIELD STRENGTH CALIBRATION

The field intensity meter (FIM) at the receiving terminal consists of a calibrated rf voltmeter and its associated antenna and cable of known characteristics and calibration factors. The rf voltmeter had an internal calibration system. This was recalibrated and corrected where necessary.* The antenna and impedance factors were measured by the NBS standard field method [6], with results as shown in figure 8. At 145 MHz the factor is 9.3 dB, which can be approximately explained as follows:

1. The effective length conversion factor, from the field in V/m to the voltage across an open circuited half wave dipole is λ/π, or -3.63 dB at 145 MHz.
2. The conversion from an open circuited generator to a matched load, the receiver, is 0.5 in voltage or -6 dB.
3. A conversion factor, arising from the mismatch of the antenna and receiver to the cable, and consequent interactions, is unknown.

---

*This calibration includes the loss of the cable.

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The sum of factors 1 and 2 nearly equals the measured conversion factor, -9.3 dB, which implies that the third factor was small.

D. COMPARISON OF THEORY AND EXPERIMENT FOR A "REFERENCE" MONOPOLE

A quantitative comparison using the rather predictable field of a "reference" monopole adds considerable confidence to the evaluation of unknown HF and VHF antennas. (The term reference is in quotes. The gain pattern of this type of antenna has shown good agreement between theory and experiment.) The so-called reference monopole is a quarter wavelength slim wire antenna on a ground plane one wavelength in diameter set on the earth. Available well-developed theory [7] is then applied to predict the space wave over an earth with dielectric parameters ϵ' and σ. The use of a reference monopole in compact range experiments, as in the present work, thus provides a check on the transmitted power calibration and the FIM calibration described above. Figure 9 exhibits the theoretical far-field power gain pattern of the reference monopoles at two frequencies, for certain ground constants.

Measurements to be compared with theory were made at a rented alfalfa field site, 5 miles east of Boulder, Colorado. The horizontal distance from the monopole antenna to the receiver tower (fig. 6) was 100 feet (30.5 m).

Table 2 gives the steps in comparing the theoretically calculated field and the measured field of reference monopole antennas at 145 and 300 MHz. The comparison is made at an elevation angle of 10° where the field is less dependent on surface imperfections and surface waves than at low angles.

The predicted and measured voltmeter readings with all conversion factors taken into account are seen to agree to within 1 dB.

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Table 2. Theoretical and measured field strengths of the reference monopole antennas at 145 and 300 MHz. The ground was dry, $\epsilon' = 5.0 \pm 1.0$ at the surface. Elevation angle of receiving point is 10°.

Frequency	145 MHz	300 MHz
Theoretical field[a] at 30.5 m of 1 W isotropic source, dB > 1 µV/m	105.1	105.1
Resonant dipole field strength conversion factor (fig. 8)	-9.3 dB	-16.0 dB
Theoretical[b] gain pattern factor at 10°, $\epsilon' = 5$, $\sigma = 0.05$ S/m	-3.1 dB	-3.0 dB
Predicted voltage of receiver, dB > 1 uV (theoretical).	92.7 dB	86.1 dB
Measured voltage at 10° elevation	101.5 dB	90.7 dB
Conversion to 1 W source[c]	-11.0 dB	-7.0 dB
Transmitter cable and VSWR factor,	+1.5 dB	+2.1 dB
Experimental 10° reading converted to 1 W radiated	92.0 dB	85.8 dB

(a) From equation (6).

(b) Reference [7].

(c) At 145 MHz P_1 is 12.56 W; 5 W were indicated but the directional coupler was -4 dB from the rated value at 145 Mc. At 300 Mc P_1 is 5 W. Values of P_2 are 0.32 W and 0.19 W at 145 and 300 MHz respectively.

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From this close agreement we conclude that the transmitted power, the FIM voltage, and the cable attenuations have been accurately determined. It is estimated that the power delivered to the antenna and the field strength at the receiving antenna are being measured with an accuracy of ± 1.0 dB.

E.   FAR FIELD PATTERN VERSUS ELEVATION ANGLE

The height dependence of the field pattern is quite similar for a buried source and for the monopole set on the interface. As shown in table 3, the theoretical patterns differ by nearly a constant ratio (constant number of dB), and the difference is due to interface loss plus depth attenuation. We may say that the buried antenna becomes, to a good approximation, a weakened virtual monopole on the surface.

The presentation in table 3 makes it clear that loss due to burial at low angles is mainly an interface loss, plus depth attenuation if present, and not a change in shape of the space wave pattern compared to the pattern of a monopole at the interface.

F.   MEASURED LOSS OF RATHER IDEAL BURIED DIPOLES

Experiments were done to check the loss of a buried horizontal dipole against the theory [1].

A sleeved dipole was constructed using handbook values of length and diameter to attain resonance at 145 MHz and an impedance of 50 ohms. The dipole diameter was 2.5 cm and the length was 98 cm. The dipole was contained in a 10 cm diameter lucite tube to reduce the effect on the resonant frequency of the surrounding ground.

The dipole was buried as a HED 15 cm below the surface. The TM wave was received in the end fire direction.
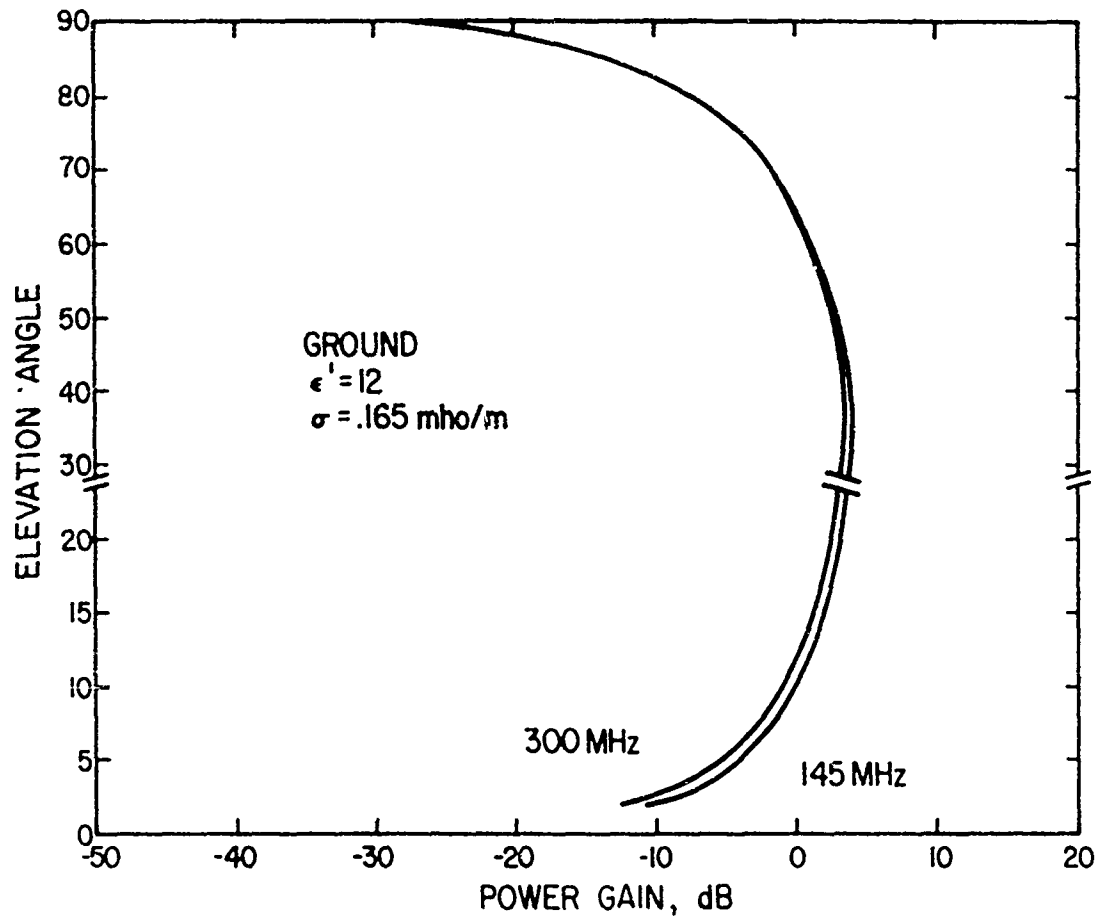
Figure 9. Theoretical far-field pattern of monopole.

Table 3. TM-wave gain pattern of a "reference" monopole set on the interface and of a buried horizontal magnetic dipole (interface gain only, depth loss is zero). Ground constants are $\epsilon' = 10$, $\sigma = 0.03$ S/m; frequency = 145 MHz.

Elevation Angle	dB Gain, Reference Monopole [a]	Interface dB Gain of HMD [b]	dB Difference
2	-12.28	-27.01	14.73
4	-7.16	-21.86	14.70
6	-4.46	-19.14	14.68
8	-2.75	-17.38	14.63
10	-1.53	-16.13	14.60

(a) Reference [7], by an approximate calculation.

(b) Only the interface gain is given. Depth attenuation would be nearly constant versus angle, see figure 3.
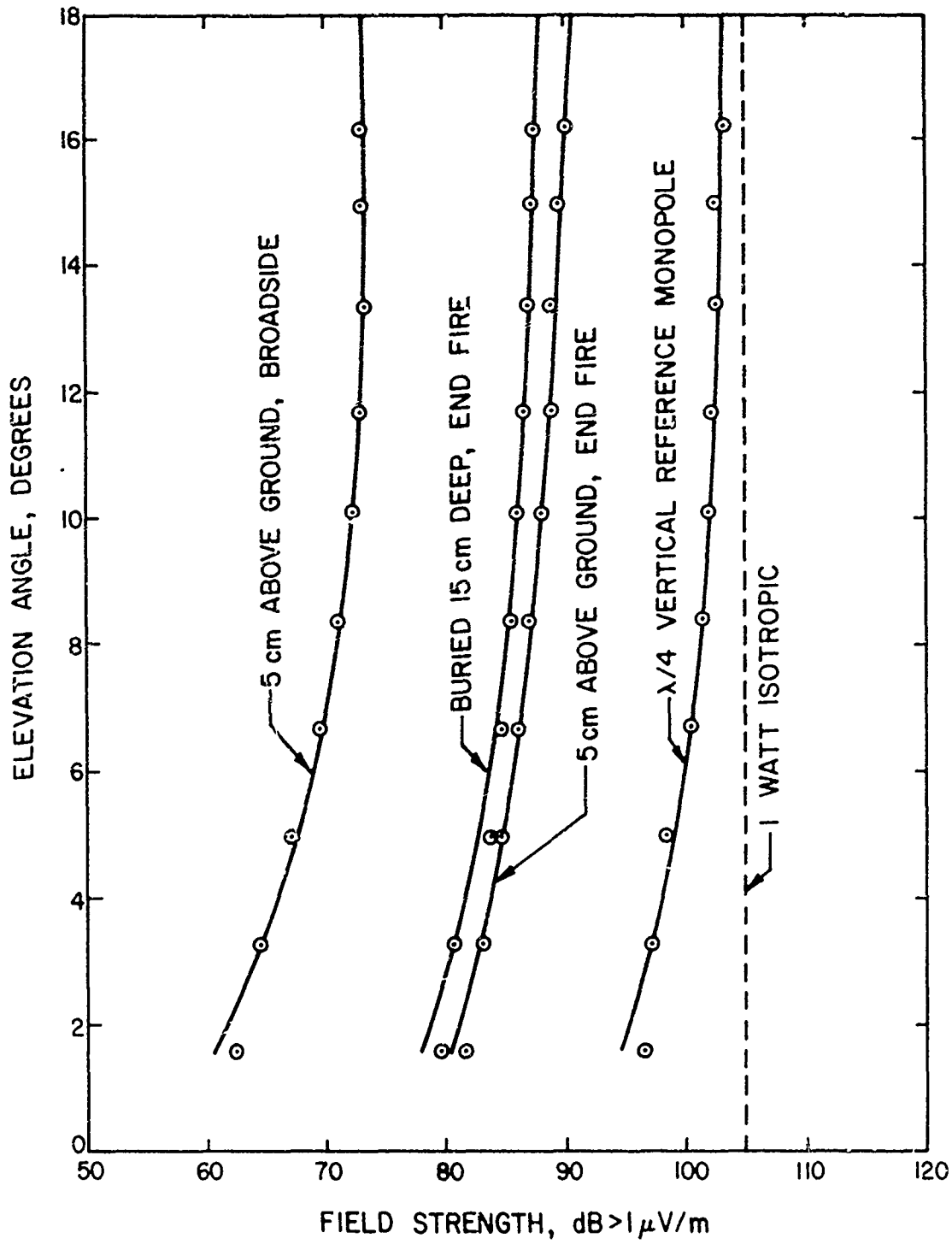
Figure 10. Measured field of monopole and buried dipole.
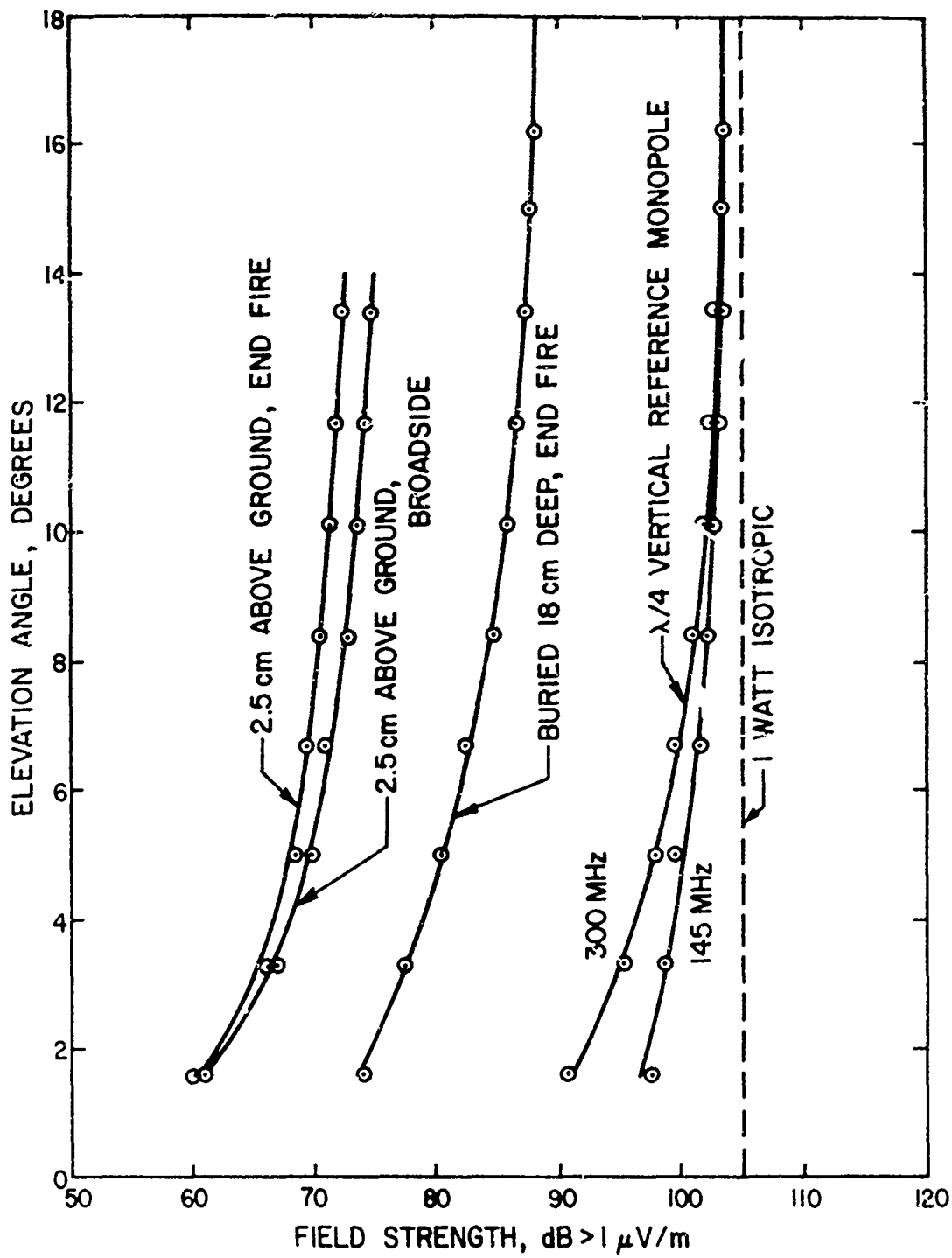
Figure 11. Measured field of monopole and buried dipole.

The dielectric constant of the undisturbed ground (quite wet), based on a core sample, was approximately 13. The disturbed dielectric constant of the dug-up ground is estimated as 10.

The estimated theoretical end-fire loss of a
buried horizontal electric dipole, $\varepsilon' = 10$,
$\sigma = 0.068$ S/m, at 10° elevation, relative
to an isotropic emitter, from figures 2, 3,
and 4 is--19 dB.

The measured loss in the same condition was--------19 dB.

Figure 10 shows curves for the sleeved dipole. The field strength of the end fire above-ground test is questionable.

Figure 11 gives results for a folded dipole at 300 MHz. The above-ground end fire results are quite weak, and thus do not agree with the sleeved dipole end fire above ground. For this buried dipole the loss at 10° elevation angle relative to an isotropic radiator is again 19 dB. The agreement with theory is very good, but does depend heavily on having assumed that ε' of the repacked dirt is 10.

G.   EFFECT OF SHALLOW BURIAL

This section is concerned with the interface loss and the underground pattern loss, see figures 2, 4, and 5, as functions of the burial depth. (For simplicity, the depth loss is assumed to be negligible.) When an elementary dipole is raised above the interface, the field strength at low angles in the far field increases. The Sommerfeld height-gain function for this effect is [1]

$$E(z) \sim 1 - i \, k_0 \, \delta \, z, \quad z \geq 0 \qquad (24)$$

where z is the height, $\delta = Z_1 \cos \theta_c / Z_0$ for TM waves, and other symbols are defined above equations (1).

30
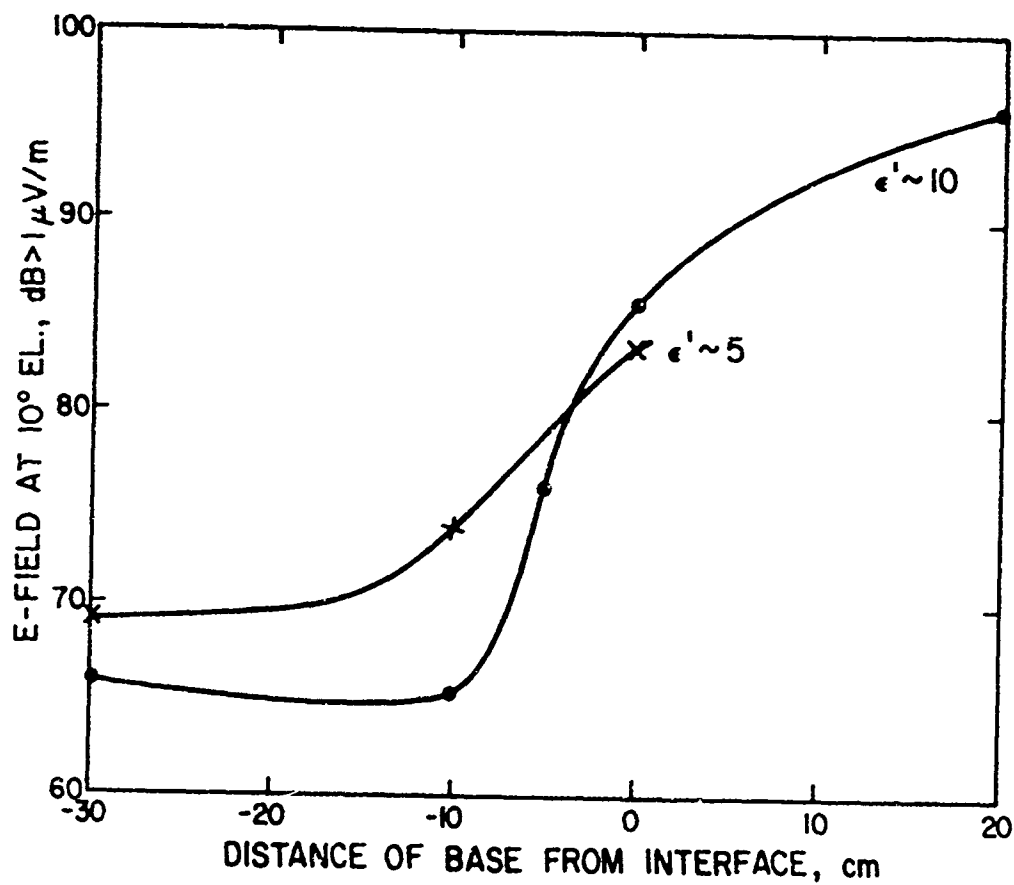
Figure 12. Field versus height of a VED.

31

When an encapsulated miniature dipole penetrates the earth the interface loss is initially less than would occur for a bare dipole because the encapsulant initially prevents the antenna from being covered. Figure 12 shows measured height (and depth) gain results for the A3 antenna (furnished by Frank Reggia, Harry Diamond Laboratories), a 2.54 cm length vertical monopole* on a 10 cm diameter ground plane. A polyfoam encapsulant 10 cm in diameter extends 2.54 cm above the top of the antenna.

The experimental curve shows that such a vertical monopole loses approximately 10 dB when the base is 5 cm below the interface, and approximately 20 dB when the base is well below the interface.

Equation (23) is not quantitatively obeyed above the interface in figure 12, probably due to the RG-9 cable feeding the bottom of the antenna. As the antenna is raised its effective length may increase due to the exposed cable.

The results in figure 12 suggest that a good candidate antenna is the low profile miniature vertical monopole on a small base plate, set in the ground with its top near the interface. The diameter of the base plate and encapsulant must be 4 or 5 times the height of the antenna, so that fairly low angle radiation can be emitted without intercepting the earth.

H. SUMMARY

Experiments using the "reference" monopole, see table 2, indicate that the experimental field measurements are quite accurate. Therefore, confidence can be placed in the characteristics of the buried antennas measured with the same system.

The experiments with rather ideal buried dipoles, as discussed in section F, indicate reasonable agreement with the theory of such buried antennas.

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*The design is rather similar to that of antenna A8, figure 13. This type of antenna, a so-called monopole, is of course mainly a dipole because the ground plane is small compared to a wavelength.

It is therefore assumed that both the theory and the experimental measurements of the characteristics of buried antennas are well in hand. The remaining effort concentrates on practical construction and testing of miniature resonant antenna for burial.

Theory and experiment agree that buried dipoles exhibit considerable loss, except when ε' is small, as in dry sand. The low silhouette vertical monopole at the surface as described in section G has advantages of being simple and less lossy than fully buried designs. The monopole is further examined below.

4. DEVELOPMENT OF MINIATURE RESONANT ANTENNAS

A. INTRODUCTION

This section describes useful miniature antennas for
burial, including principles of design and practical construc-
tion. The assigned frequency is 145 MHz and the allowed dimen-
sions are a circular cylindrical form approximately 5 inches
(12.7 cm) in diameter and of the order of 1 foot (30 cm) in
length.

As concluded from the theory and theoretical comparisons,
an ideally buried antenna has an unavoidable interface loss, I,
as well as the smaller depth loss, and in some cases a small
underground pattern loss (figs. 2, 3, 4, 5). The possibility
of employing directive gain to counteract these losses was of
course considered. Rather thorough reports on aperture antennas
and traveling wave antennas with gain when buried [8], and arrays
with gain [9], are available, but such methods are not suitable
for the present purpose because of size and complicated burial
requirements. Therefore the remaining task is to develop
convenient miniaturized antennas for burial. The main concerns
in designing the miniature antennas are as follows:

1. Impedance matching, coupling to the generator.
2. Efficiency.
3. Bandwidth.
4. Changes in the above as the capacitive stray field of the
   resonant antenna interacts with the burial medium.
5. Practicality and convenience.

B. CONSTRUCTION DETAILS

Figure 13 to 19 are schematic mechanical layouts for seven
of the candidate antennas. In each case the antenna is built
above an inverted copper cup, 12.7 cm in diameter and 12.7 cm

34

Grid Dips,
145 MHz

7.6 Diam Upper Plate

Nylon
Screws

13 Diam Base Plate

Plastic Cyl.

$3\frac{1}{2}$ Turn Coil of
0.5 Wide Brass Strip

5.4

Input Link, 1 Turn,
Diam = 2.

3.8

Type N
Connector

13 Diam x 13 High
Copper Base,
Inverted Cup.

´Dimen. cm`
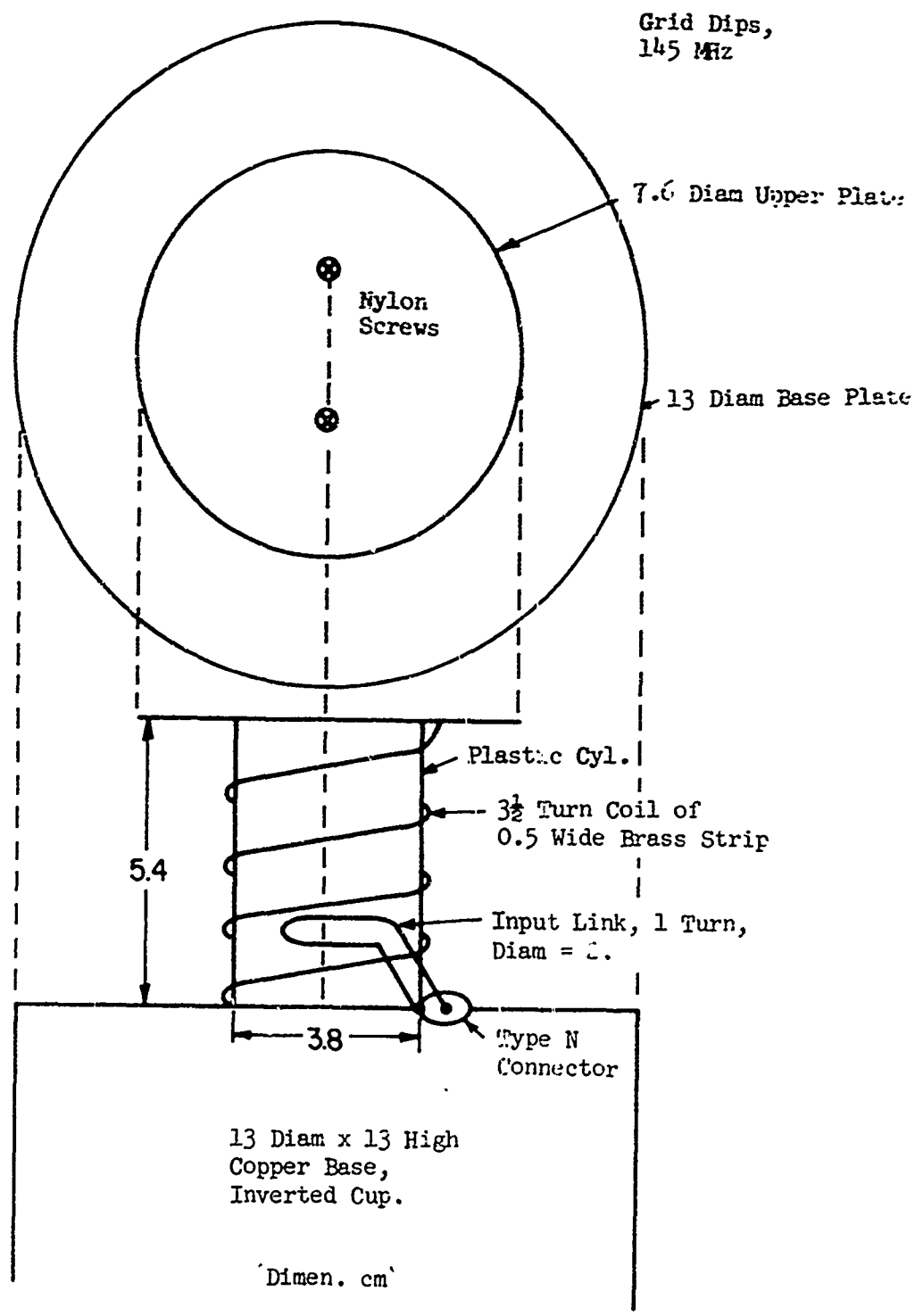
Figure 13. Vertical electric dipole, VED, A8.

35

Grid Dips, 150 MHz

Plastic Cylinders

2.87 Turns of
0.6 Copper Tubing

8.9

Tapped 3/4 Turn
From Bottom

7.6

Copper Base, 13 Diam
13 High.

Dimen. cm
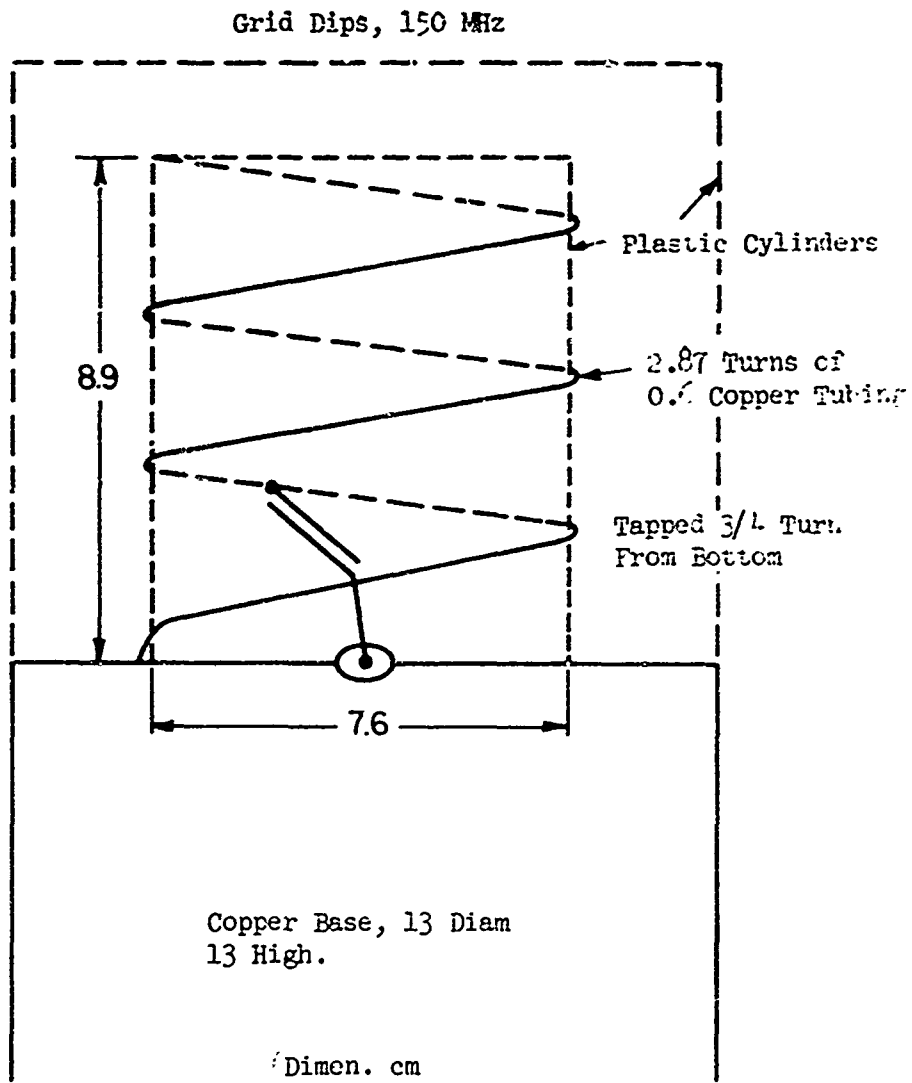
Figure 14. Antenna C4, a VED.

36

119 Ferrotron
Slug 3.5 Diam,
7.6 Long, in Plastic
Cyl.

Capacitor
Plates, Cu.

12.7

10

Ferrotron

3.5

3.8

N Connector

Link, 1 Turn
2.5 Diam

Base 13 x 13
(cm)

Figure 15. B3, a HED.

Grid Dips, 140 MHz

Base Plate

Plastic Cyl.
10 Diam, 7.6 High

5 Turn Coil of No. 10
Wire, 3.2 Diam

Coil Form

Capac Plate
5 x 10

5

2.5

Link, 1 Turn,
1.9 Diam

N Connector

Base, 13 x 13
(cm)

Figure 16. B4, a HED.

38

Plastic Cover

Capacitor, Circular
Plates, 5 Diam,
0.3 Spacing

Strap, 1.3 Wide

1 Turn Loop,
Cu Strap
2.5 Wide

$d=5$

0.7

Plastic Cyl.

N Connector

Base 13 x 13
(cm)

Figure 17. D3, a HMD.
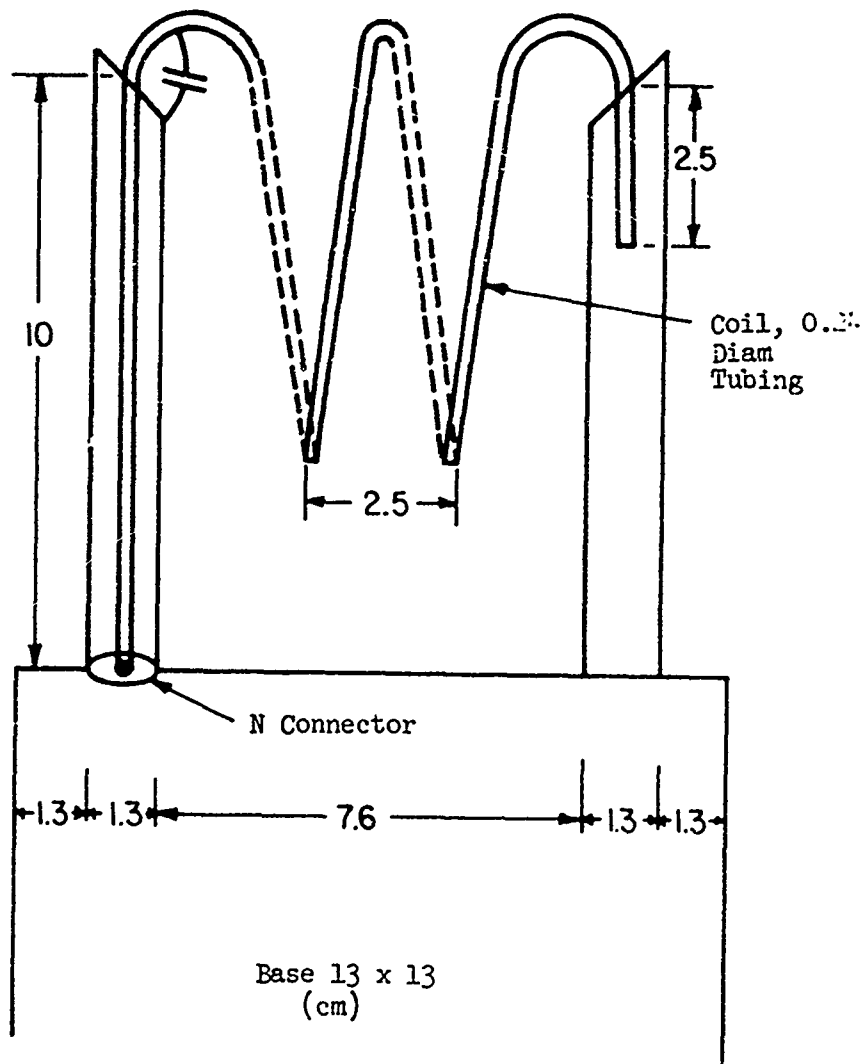
Figure 18. D4 (Pi-match antenna), HED-HMD.

40
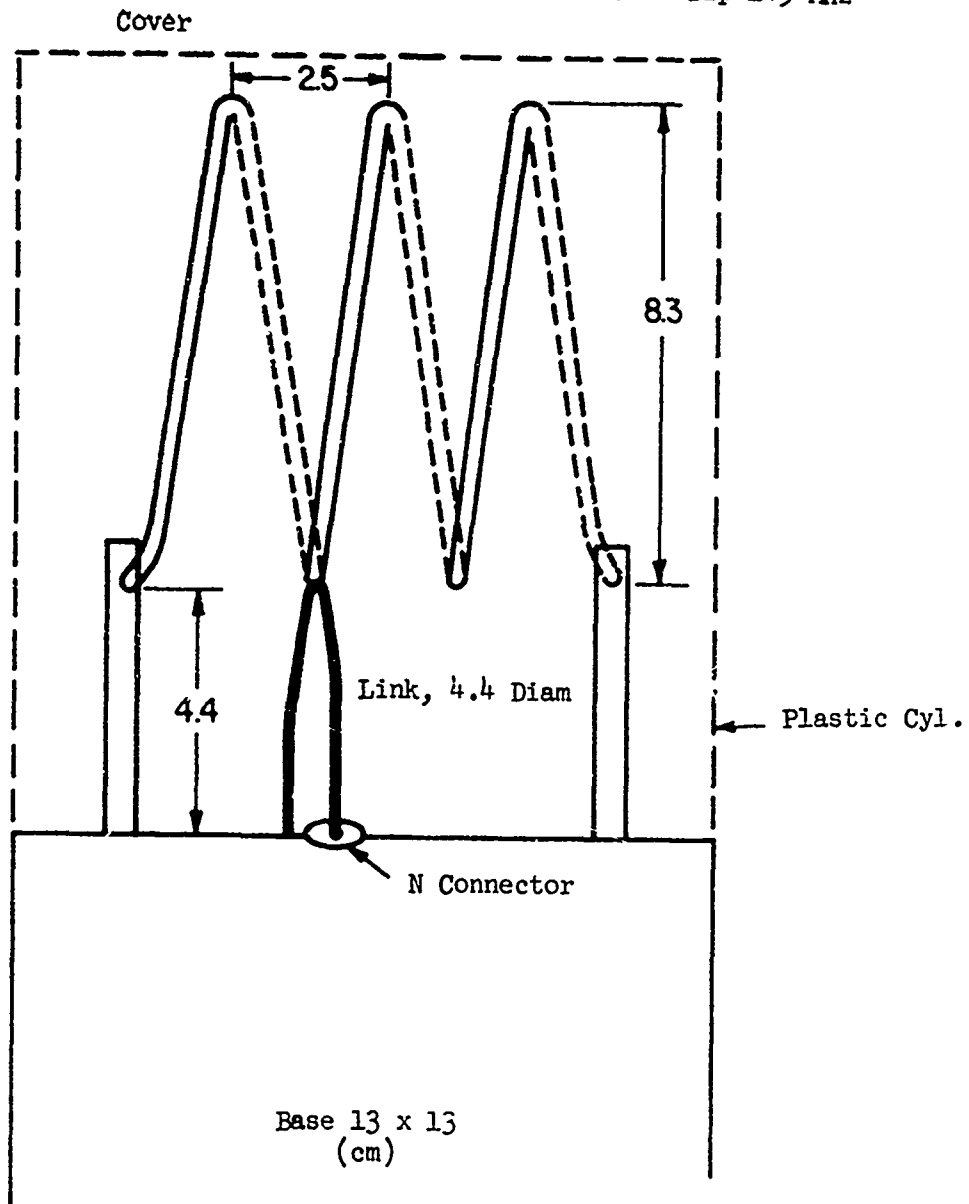
Figure 19. D5, HED and HMD.

in length (5" x 5") as a base. In each case the coupling consists of either a link which couples to the magnetic field of the antenna coil, or a tap on the coil. In each case a type N connector is mounted in the base near the feed point of the antenna. In our experiments the feed cable comes to the connector from below. In each case the antenna is "encapsulated" by setting a 12.7 cm diameter plastic cylinder over it with a top cover approximately 3 cm above the top of the antenna.

One requirement in design is to obtain a resonant frequency, near 145 MHz. This was obtained empirically. The size of the coil and the size of the capacitor plates at the ends of the coil were thus determined experimentally. Measurements of resonant frequency were made initially with a grid dip meter, and finally with the network analyzer; the latter tests will be described later.

Another requirement is to adjust the coupling coefficient of the antenna system for approximately 100% absorption of the energy from the transmission line. This adjustment requires that the antenna be critically coupled (which will be explained), which requires that the impedance be equal to that of the transmission line. The automatic network analyzer was the main instrument for studying the coupling.

C. IMPEDANCE MEASUREMENTS WITH THE NETWORK ANALYZER

Measurements of impedance versus frequency in the neighborhood of resonance may be analyzed to obtain the coupling coefficient, resonant frequency, and Q of a resonator. The antenna is a 1-port resonator insofar as the impedance measuring system is concerned. (Strictly it is a multiport resonator because it is coupled by radiation to the surrounding space.)

Impedances were measured with the antenna radiating into a small anechoic chamber near the automatic network analyzer. Calibration of the analyzer was obtained in the usual way by an

open circuit, short circuit, and pad successively connected to the end of the cable in the anechoic room. Then the antenna was connected to the cable and the complex impedance R + jX was measured at the plane of the connector. These results were plotted on the impedance circle charts for analysis. Figure 23 shows an example of the plots. The bandwidth, reflection coefficient and coupling coefficient, and frequency of resonance may be analyzed from the impedance plot. The main requirements are that the impedance curve pass near R = 50 ohm at the desired frequency and that the bandwidth be sufficient. The bandwidth is defined as the frequency separation of two points on the impedance curve at which the VSWR is 6:1, i.e. at which half of the power is reflected from the antenna (and half is accepted). Having exhibited the results qualitatively, we now go to a circuit analysis and a more quantitative analysis of the impedance data.

D. CIRCUIT REPRESENTATION AND Q ANALYSIS

Circuit analysis is useful in finding the antenna efficiency. Figure 20 shows two possible circuit representations of a resonator (the antenna) terminating a transmission line [10]. Part a. represents a series resonant circuit and part b. transforms to the parallel resonator circuit shown in c. The experimental data agreed with the parallel resonance, parts b. and c.

The measured impedance at the input to the primary inductor L_1 in figure 20b is given by the formula

$$Z = j\omega L_1 + (\omega M)^2 / (R(1+j2Q_0\delta)) \tag{25}$$

where $\delta = (\omega-\omega_0)/\omega$, and the Q of the resonance is

$$Q_0 = R/\omega L. \tag{26}$$

The (angular) frequency of resonance is $\omega_0 = 2\pi f_0$, and ω is the test frequency. The first term in equation (25) is a shift

43
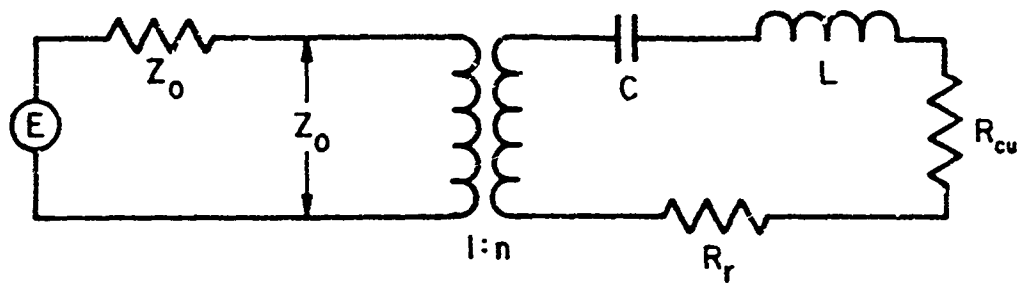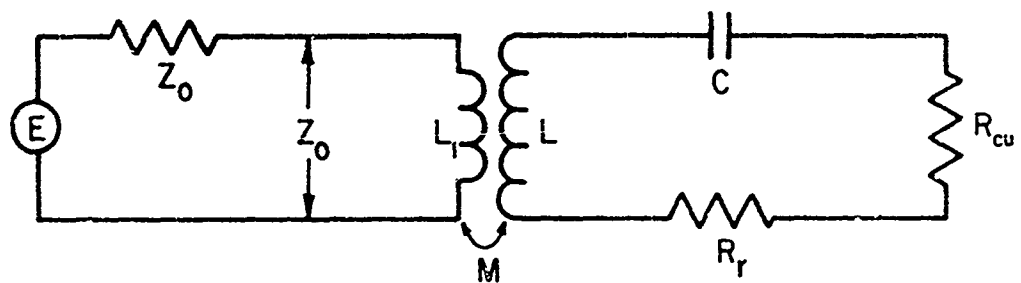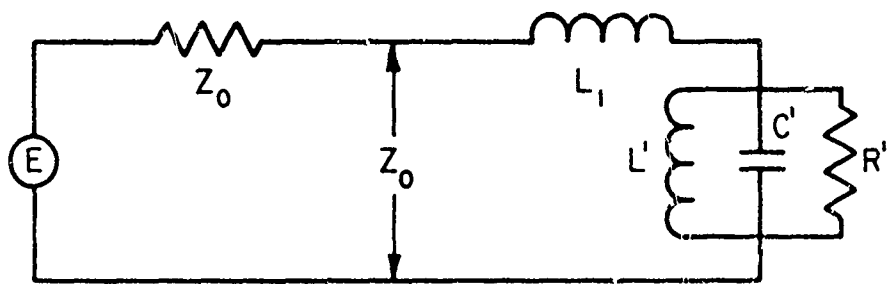
Figure 20. Circuit representations of a resonator
coupled to a transmission line.

44

along the imaginary axis of an impedance plot. The second term
is a circle in the complex plane. Normalizing to the charac-
teristic impedance of the input transmission line, Z_0 (50 ohms
in all of the present work), and separating the second term into
real and imaginary parts gives

$$\frac{Z - jX_1}{Z_0} = \frac{R' + jX'}{Z_0} = (\omega^2 M^2/RZ_0)(1-j2Q_0\delta)/(1+4Q_0^2\delta^2) \qquad (27)$$

where $X_1 = \omega L_1$, and $R' + jX'$ is the impedance of the transformed
parallel resonator shown in figure 20c.

The ratio X'/R' is $-2Q_0\delta$ from equation (27) and is the
tangent of the angle θ_i of the ith impedance point of the
impedance circle plotted in the rectangular impedance plane
(fig. 21). θ_i is measured from the real axis to the radius
vector from $R = 0$ to the ith point. From this we find

$$X'/R' = \tan \theta_i = 2Q_0(\omega_i-\omega_0)/\omega_i, \qquad (28)$$

which shows that frequency displacements from the point of
maximum R on the real axis are proportional to $\pm \tan \theta_i$, assuming
high Q. This fact from equation (28) permits accurate nonlinear
interpolation of frequency around the circle. In figure 21 for
example, from θ_1 and θ_2 and the corresponding frequencies, we
find that a difference of tan θ of 1 between two impedance
points corresponds to a frequency shift of 0.186 MHz. Then the
frequencies at $R' = \pm X'$, $\theta_i = \pm 45°$, may be found and from
equation (28)

$$Q_0 = 0.5 \ \omega_0/(\omega_0-\omega_{45°}), \qquad (29)$$

which gives a Q for this case of 392.

The Q may be found from any two points on the circle plot
using a difference formula from equation (23)

$$Q_0 = 0.5 \ (\omega_1 \tan \theta_1-\omega_2 \tan \theta_2)/(\omega_1-\omega_2), \qquad (30)$$

where points 1 and 2 would usually be chosen near the $\pm$ 45°
points.

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Having fitted the circle to the measured data, the resistance R_0' at $X = 0$ may be found, and Q_0 is proportional to this R_0', from equation (26).

E.   ANTENNA EFFICIENCY

Antenna efficiency is defined as the ratio of power radiated to the total power delivered to the antenna, equations (22) and (23). Two ways to measure efficiency are as follows:

1.   Measure the power to the antenna, the antenna gain pattern, and the resulting field strength in the air, and attribute any discrepancy to inefficiency, i.e., ohmic losses [20].

2.   Measure the resistance of the antenna, or its Q, when the antenna is radiating in the open and when it is enclosed in a small metallic enclosure which prevents all radiation [11]. Efficiency is obtained from the equation,

$$J = 1 - R_{open}/R_{enclosed},$$ (31)

where the representation is a parallel resonant circuit. From equation (26) one finds

$$J = 1 - Q_{open}/Q_{enclosed}.$$ (32)

The resistances in equation (31) are each evaluated at resonance.

Efficiency was measured by the second method. The network analyzer was used to measure the impedance of the antennas near resonance, first when the antenna was radiating into the anechoic chamber, and second when the antenna was enclosed in Wheeler's so-called radiansphere [11], which for this work was a closed circular cylinder of copper, 0.6 m in diameter and 0.6 m long. These dimensions, for f = 145 MHz, satisfy the criterion that the spherical enclosure radius shall be less than the wavelength divided by 2π.

46
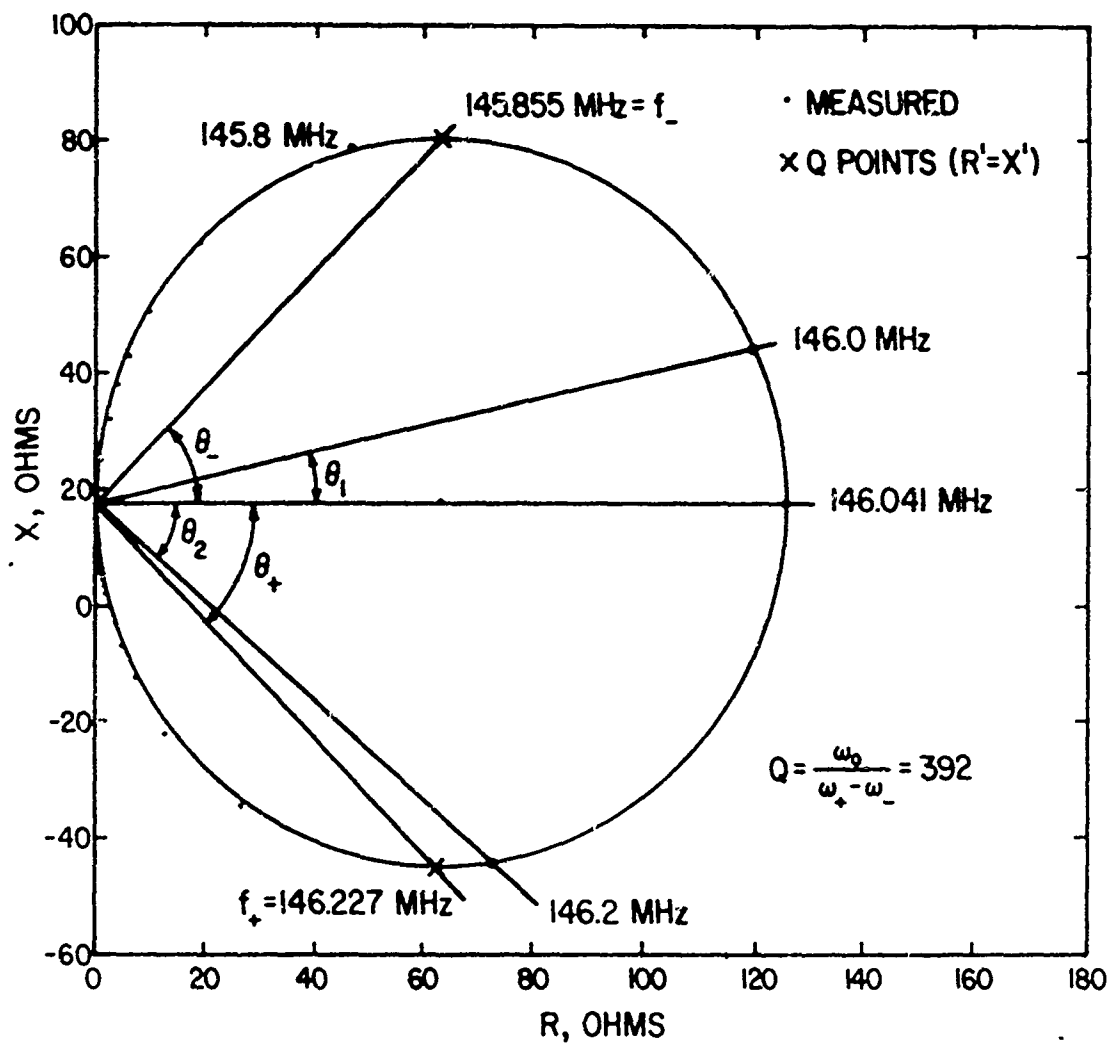
Figure 21. Q analysis, antenna enclosed in a box.

47
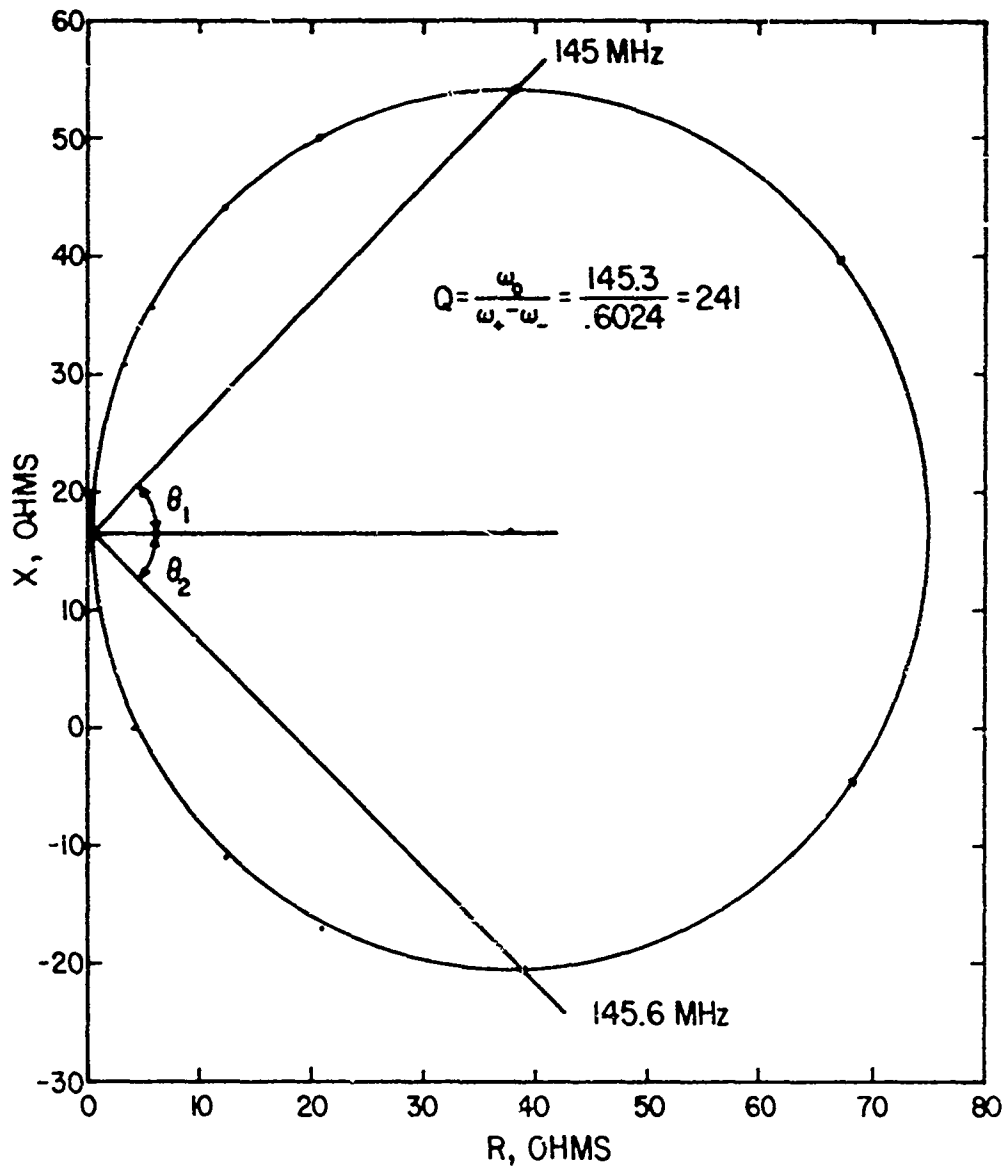
Figure 22. Same as Figure 21 but antenna radiating.

Figures 21 and 22 show the circular plots of X versus R in the rectangular impedance plane, for the enclosed and radiating conditions respectively. The Q is 392 enclosed and 235 when radiating, from which in equation (31), E = 0.4, The resistances, $R_0^!$ in the plots, are 125 and 75 respectively from which in equation (32), E = 0.4. A similar analysis was made of impedance data for five of the resonant antennas. The results are given in table 4.

The efficiencies obtained by this method are quite high. The accuracy of the method was not investigated; however, the results appear to be reasonable, and the network analyzer data certainly indicates a very definite increase in the Q when the antenna is enclosed.

Theoretical estimation of the efficiencies is of interest, and may be based on the estimated radiation and ohmic resistances of the antennas. The radiation resistances of antennas that are small compared to the wavelength may be obtained from straightforward analysis [12]. The equations are

$$R = 20 \ (\pi \ell / \lambda)^2, \text{ dipole in free space}$$

$$R = 40 \ (\pi \ell / \lambda)^2, \text{ monopole on a ground plane}$$

$$R = 20 \ \pi^6 N^2 (D/\lambda)^4, \text{ loop in free space}$$

where ℓ is the length of the dipole or monopole, D is the diameter of the loop, λ is the wavelength, and N is the number of turns. For example at 145 MHz, for a 10 cm dipole and a 10 cm diameter one-turn loop we find

$$R = 0.5 \text{ ohm, dipole}$$

$$R = 0.11 \text{ ohm, loop.}$$

Ohmic loss must be kept small in order to obtain useful efficiencies.

Table 4. Q and maximum R', and the efficiencies calculated from the Q's and R's.

Antenna Designation	Q_{open}	$Q_{in\ cav.}$	R'_{open}	$R'_{in\ cav.}$	J(R)	J(Q)
A8	78.9	337	145	615	0.77	0.76
C4	40.6	734	631	12120	0.948	0.945
B3	70	81	2780	3350	0.17	0.14
D3	234	392	75	125	0.4	0.4
D5	37.6	2279	96	7600	0.987	0.983

Theoretical estimates of the efficiency will be given for comparison with the measurements in table 4. Consider the antenna D5, which, for purposes described later, has a coil diameter and spacing calculated to give approximately the same radiation resistance from its electric dipole moment and from its magnetic dipole moment. Using the skin depth of copper at 145 MHz, 0.0055 mm, and the dimensions in figure 19, the ohmic resistance of the full length coil is 0.16 ohms. Using sine squared current dependence on length only half of this, or 0.08 ohms, is effective. From equations (33) radiation resistances are 0.44 ohms for the magnetic dipole component and 0.32 ohms for the electric dipole component. The predicted efficiency is then

$$J = 1 - 0.08/(0.08+0.44+0.32) = 0.90,$$

which is less than the value for D5 by the radiansphere method, table 4. There is, however, at least qualitative agreement on the high efficiency.

This sort of estimate of the resistances was made for six of the antennas. The results are given in table 5, and compared with the measured values. It would appear that efficiencies can be estimated to within approximately 3 dB.

F. COUPLING COEFFICIENTS, THEORY, AND EXPERIMENTS FOR ONE ANTENNA

The coupling coefficient of a one-port resonator to a transmission line has been defined [10] as

$$\beta = (\omega M)^2/Z_0 R \qquad (34)$$

which is the first term in the numerator of equation (27). β is the ratio of coupled in resistance from the line $(\omega M)^2/Z_0$

Table 5. Estimated ohmic resistance, R_{cu}, and radiation resist-
ances, R_r and consequent estimated efficiency.

Antenna	R_r	R_{cu}	J, Estim.	J, Meas.
A8	1.5	0.27	0.85	0.76
C4	1.5	0.13	0.92	0.95
B3	0.5	1.5[a]	0.25	0.14
B4	0.27	0.21	0.56	
D3	0.11	0.03	0.78	0.4
D5	0.76	0.08	0.90	0.98

(a) The magnetic loss tangent of the ferrite was 0.011; the
     electric was 0.014.

to the resonator resistance R, and R is composed of two resistances in series

$$R = R_r + R_{cu}, \tag{35}$$

where R_r is radiation resistance and R_{cu} is ohmic resistance. R_{cu} includes ohmic losses in conductors, magnetic losses in magnetic cores, and dielectric losses in the dielectrics including encapsulation, and in the earth when buried, due to near field interaction (see section 6 and figure 11 of reference [1]). The coupled-in resistanc· is proportional to the mutual inductance squared represented in figure 20b. In the present antennas the larger the link or the higher the tap point from the base, the larger the mutual M. The resonator is overcoupled, critically coupled, undercoupled accordingly as β is greater than, equal to, less than 1. The mismatch reflection of the resonator (antenna) is a function of $R' + jX'$. If ωL_1 is suitably annulled, usually by a series capacitor for link coupling, then the reflection coefficient at resonance ($\delta = 0$ in equation (27)) is

$$|\Gamma_{res}| = (1-\beta)/(1+\beta), \tag{36}$$

which is zero when $\beta = 1$. This means that the antenna accepts maximum power from the line when it is critically coupled, provided $j\omega L_1$ has been annulled.

In general the expected qualitative relationship between input impedance and the size of the coupling link occurs. Figures 23 to 33 are Smith chart impedance plots of the type of network analyzer impedance measurements previously discussed.

The results of adjusting the coupling coefficient are illustrated by figures 23 to 25, and a change due to burial is shown by figure 27. In figure 23 the height, d, of the tap (shown in fig. 17) is 6.7 cm and the input resistance near resonance is some 210 ohms. When d = 4.5 cm the input resistance is 72 ohms (fig. 24), and when d = 2.5 cm (fig. 25) the resistance near resonance is approximately 30 ohms. In figure 26 the

53
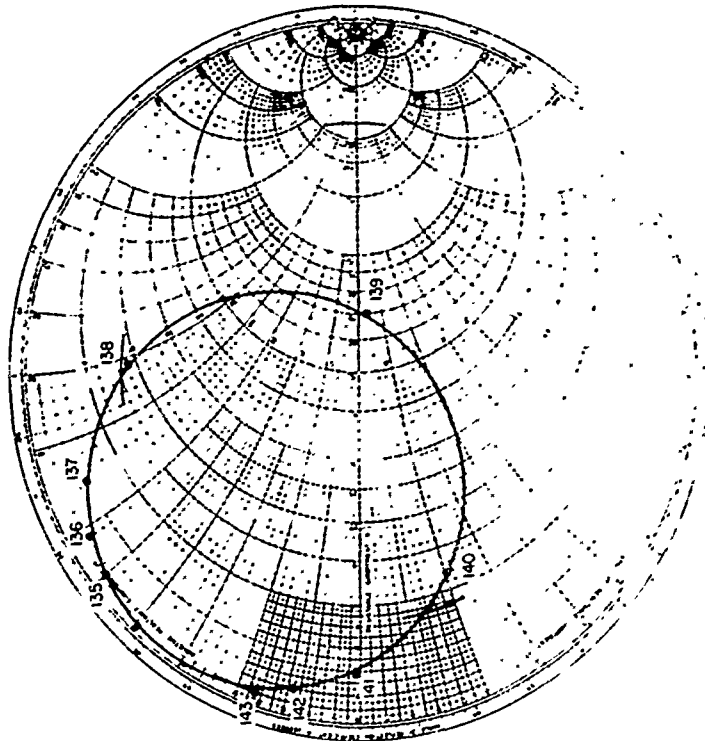
Figure 24. D3-4, d = 4.5 cm.
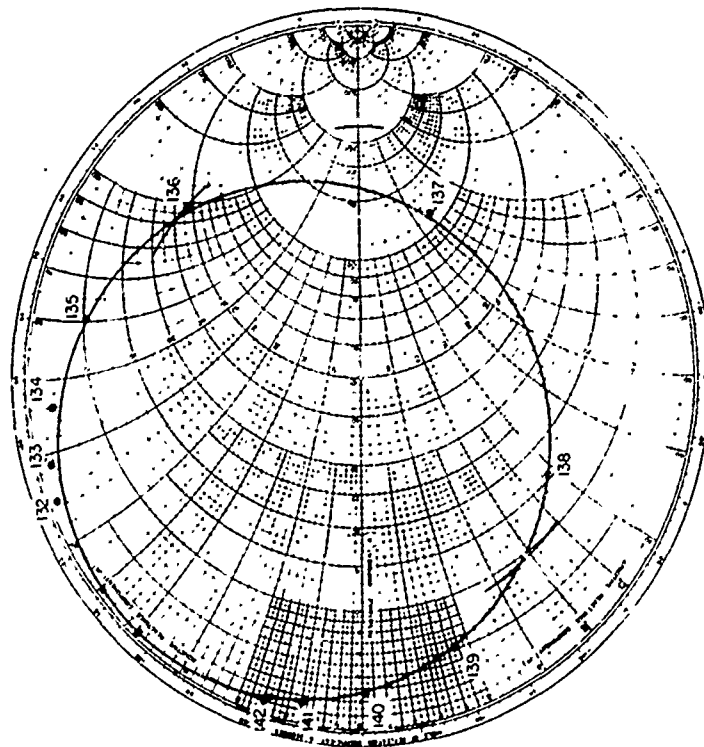
Figure 23. Impedance circle, D3-2 with d = 6.7 cm.

54
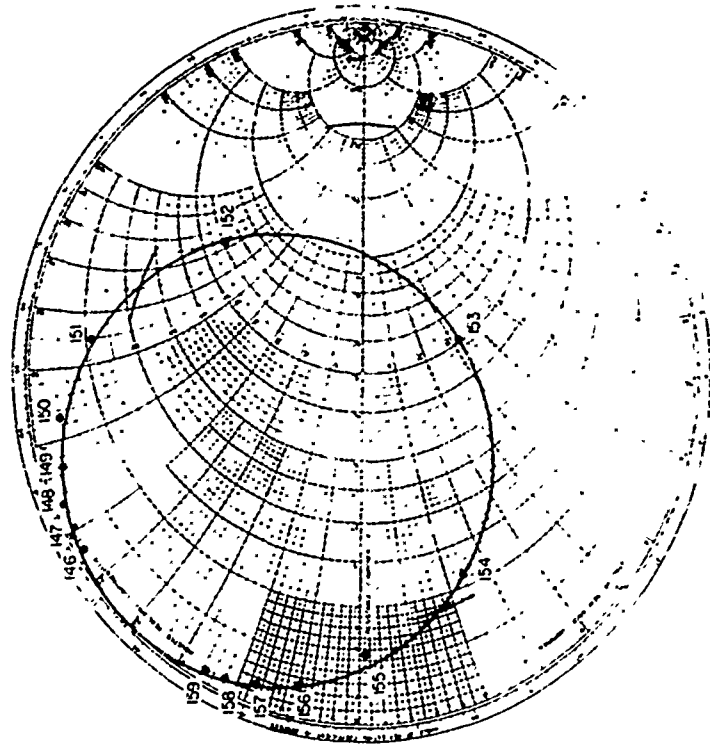
Figure 26. D3-6, d = 4.5 cm and soldered.

Figure 25. D3-6, d = 2.5 cm.

55
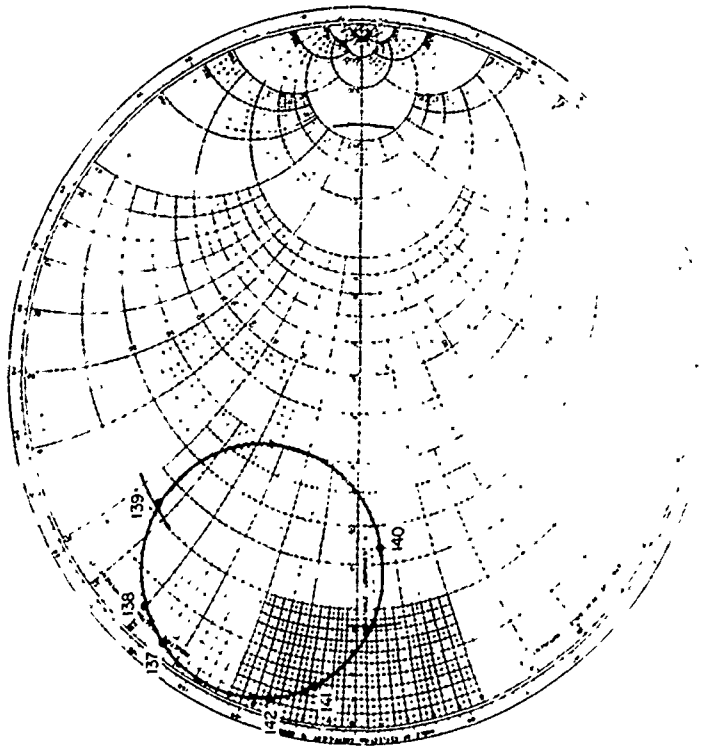
link was returned to approximately 4.5 cm and R was 200 ohms. The antenna was then "buried" by putting it in a hole in a concrete cylinder in the anechoic room, which adds to R through the dielectric losses in R_{cu} of equations (35), which brings the antenna nearer to critical coupling as shown in figure 27. If the concrete were more lossy the antenna would probably become undercoupled.

This work indicates that the coupling and impedance dependence on the geometry of the link and the dependence on near field dielectric losses behave qualitatively as would be expected from the theory, equation (34).

G. COUPLING, AND RADIATION RESISTANCE DISCUSSION OF ALL ANTENNAS

The impedance measurements of six of the antennas detailed in figures 13 to 19 are shown in figures 28 to 33. These measurements were made prior to making field tests discussed in figure 35 below. The impedances will be individually discussed.

The impedance plot (fig. 28) versus frequency for antenna A8 shows undercoupling, $R' \sim 30$ ohms, and lack of capacitance. The diameter of the input link should be approximately 1.2" (3 cm). Also a small capacitor such as that in figure 14 should be in series with the link.

This antenna probably acts as an asymmetrically fed dipole, length 18 cm, radiation resistance 1.5 ohms.

The impedance of C4 (fig. 29) is too capacitive. The input capacitor should be slightly reduced. The tap at 7/8 turn gives approximately critical coupling. The radiation resistance is similar to that of A8.

The impedance of B3 is nearly 50 ohms at 146 MHz (fig. 30). The dipole length, 10 cm, gives 0.5 ohms for R_r.
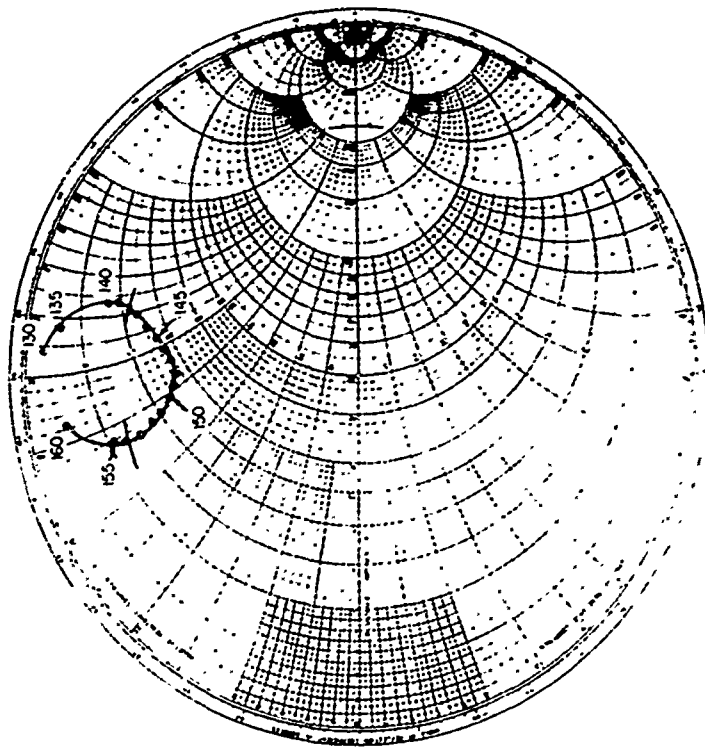
Figure 28. Impedance of AN in anechoic room.
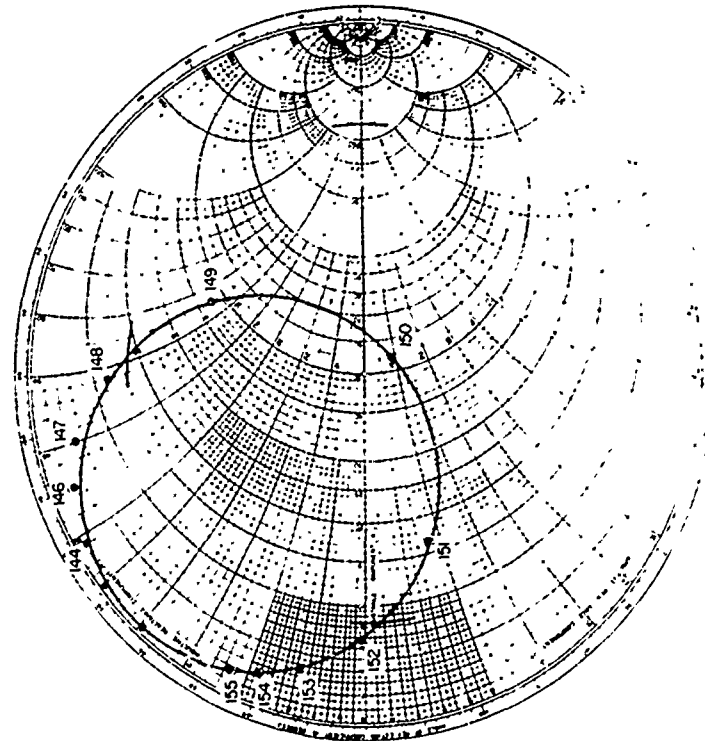
Figure 27. D3-8 buried in concrete with loss tan = 0.01.

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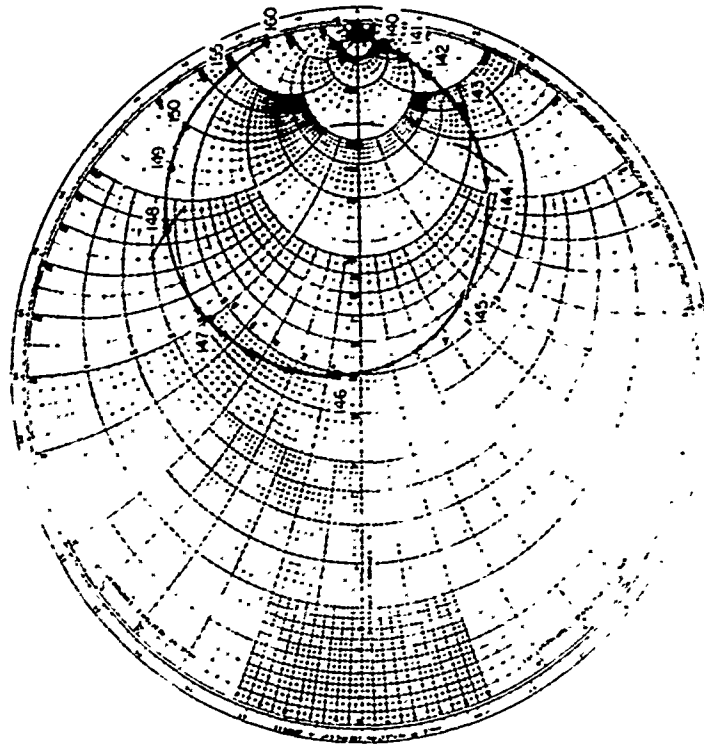
Figure 30. B3 in anechoic room.
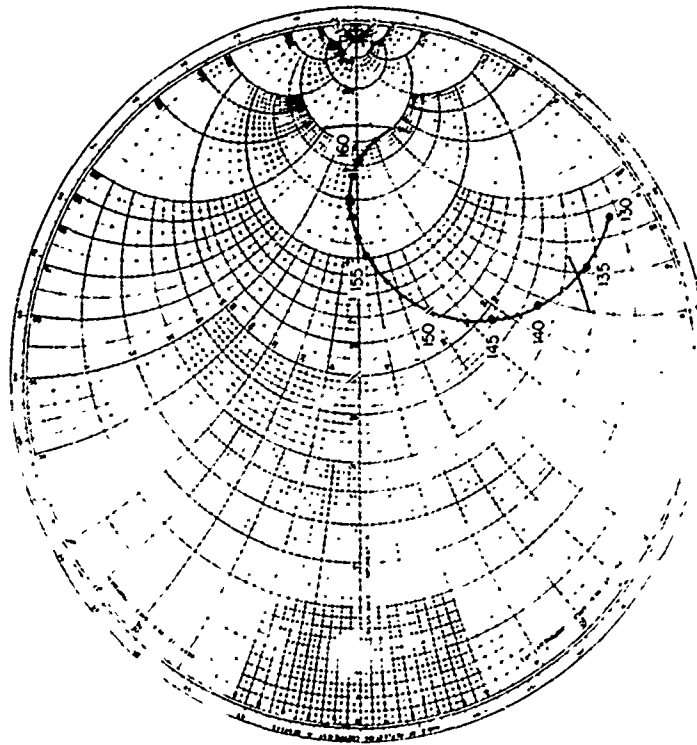
Figure 29. C4 in anechoic room.

58
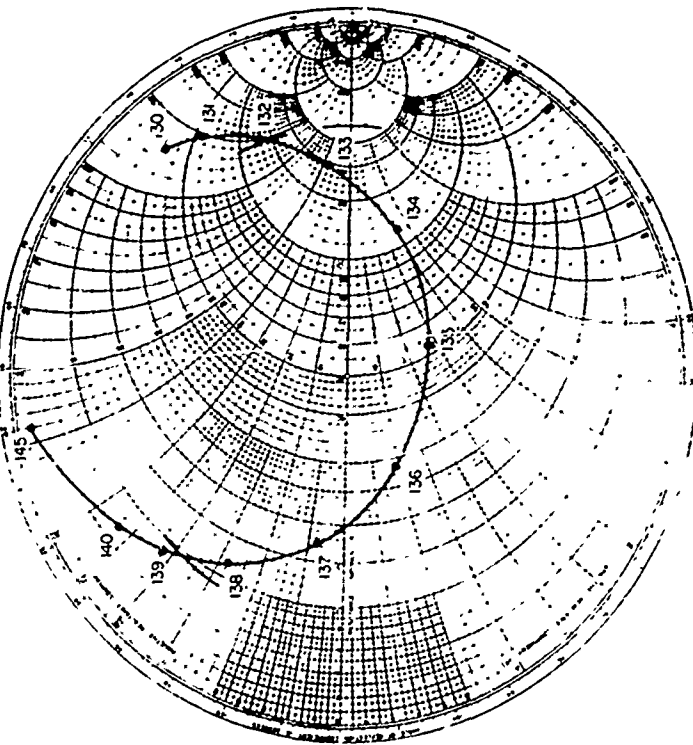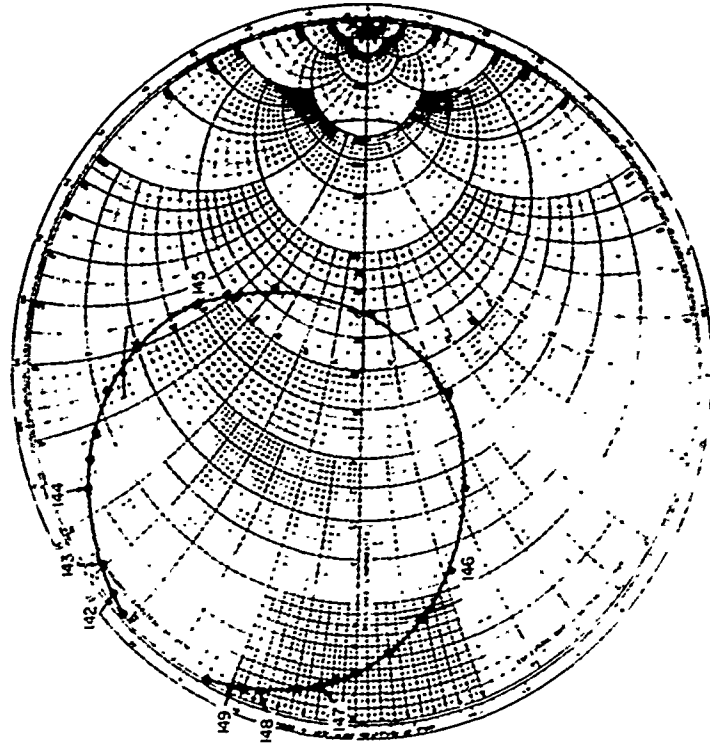
Figure 32. D3 in anechoic room.

Figure 31. B4 in anechoic room.

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Figure 31. Circuit for analyzing interaction with burial medium.

Figure 33. D5 in anechoic room.

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The impedance plot of B4 (fig. 31) attains its bandwidth by leaving the input link inductive so that the curve is rather parallel to the real axis. R_r is of the order of 0.3 ohms for the 7.6 cm length coil.

The impedance plot for D3 is shown in figure 32. The coupling is correct for burial in low loss ground. The radiation resistance R_r of this loop is very low 0.11 ohms; however, the resistance R_{cu} is also low. Furthermore, a small loop has much smaller interaction with the burial medium than does an electric dipole. Therefore, the small loop probably maintains its efficiency after burial better than electric dipoles do.

The impedance of antenna D5 (fig. 33) is inductive; some input series capacitance is needed, which would improve the bandwidth as well as the impedance match. The two radiation resistances of D5 are discussed in section 4E.

The coupling development may be summarized by stating that automatic network analyzer data plotted on a Smith chart is extremely valuable in adjusting the coupling. Funds did not permit optimization of all the antennas, but the methods are rather straightforward and desirable modifications have been pointed out.

H. INTERACTION WITH THE BURIAL MEDIUM

The near electric field of the antenna interacts with the complex permittivity of the surrounding medium. As a result, the resonant frequency is lowered; the apparent ohmic loss of the antenna increases; and the radiation resistance decreases, which lowers the efficiency.

Figure 34 shows a circuit that we have used for analysis of the above-mentioned dielectric effects. It is assumed, a) that C_1 arises from the electric field that does not fringe into the burial medium; b) that C_3 arises from the electric

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field in the burial medium; and c) that C_2 arises from electric field lines within the encapsulation that, in their continuations, fringe out into the burial medium and contribute to C_3.

The equation for the frequency of resonance ω_i in terms of the circuit elements and the permittivity of the burial medium, ε'_i, where i denotes the <u>ith</u> experiment, is

$$\omega_i^{-2} = LC_1(1+C_2C_3\varepsilon'_i/(C_1(C_2+2C_3\varepsilon'_i))). \qquad (37)$$

Of the four unknowns in equation (37), three combinations, viz., LC_1, C_2/C_1, and C_3/C_1, were evaluated from the measured frequencies of resonance in three burial media, namely, air, dry sand, and concrete, with relative permittivities of 1, 2.85, and 6.5 respectively. Three antennas were so measured (table 6). The unknowns were evaluated for two of the antennas, in the third case the iterative solution employed did not converge. From the results the resonant frequencies are predicted for permittivities of 8 and 15.

The minimal encapsulation used (12.7 cm diameter plastic cover) does not provide sufficient isolation of the electric dipole antennas from the burial medium. The isolation is marginal even for the loop, D3. It will be necessary to allow a larger encapsulation; the required size was not determined; more research is needed.

I.   BANDWIDTH IMPROVEMENT

Attaining required bandwidth in a resonant antenna is a research problem. Bandwidth may be increased by making longer dipoles, thus increasing the radiation resistance, and perhaps by so-called active antenna techniques [13,14]. (These two references refer to many papers on miniature and active antennas.)

Table 6. Measured frequencies of antennas buried in air, sand, and concrete; evaluation of C_2/C_1 and C_3/C_1 and prediction of resonant frequency for $\epsilon' = 8$ and 15. Frequencies are in MHz.

Antenna	Meas. Freq. in the three Media	C_2/C_1	C_3/C_1	Calculated Freq.	
				$\epsilon' = 8$	$\epsilon' = 15$
B4	150.9 133.5 128.5				
D3	167.35 165.49 163.35	0.29	0.02	162.8	161.2
D5	150.8 138.14 133.16	3.53	2.39	132.4	130.7

Small antennas have very low resistances, see table 5.
Resonating them provided a way of raising the impedance for more
convenient matching to a generator. Active antenna techniques
provide another method of impedance matching, and at the same
time usually a broadband characteristic can be obtained. Ap-
plication of active antenna techniques was not made in the
present research. Attention was confined to resonant techniques.

The bandwidths were measured by means of the impedance
plots on Smith charts. Circular arcs representing a VSWR of
6:1 are drawn on the chart. The portion of the measured antenna
impedance curve that has less than 6:1 VSWR is useful and repre-
sents the bandwidth (see figs. 28 to 33). The measured band-
widths of the antennas before modification are given in table 7.

Section 4H showed that the small loop, D3, exhibits the
least interaction with the medium, which was a useful develop-
ment. However, table 7 shows that D3 has a narrow bandwidth,
which has some obvious disadvantages:

1. The bandwidth may be insufficient for the communications
   system; a spread spectrum system with 10 MHz bandwidth is
   a possibility.

2. The frequency shift due to burial, although small, is
   larger than the bandwidth, for a permittivity of the
   burial medium greater than approximately 2. This problem
   may be overcome by a larger encapsulation.

J. ADDITIONAL MODIFICATION OF ANTENNAS; RESULTING BANDWIDTH
    AND INTERACTION WITH MEDIA

Last-minute modifications of the antennas were performed
with the purpose of making the frequency when buried nearer
to 145 MHz, or improving the coupling, e.g., by the experiments
on D3 described in part F. The changes were not always benefi-
cial but are of interest especially for bandwidth and frequency
shift purposes. The changes and measured characteristics are
listed in table 8.

Table 7. Measured bandwidths of the antenna in the anechoic chamber, defined as the frequency region where more than half of the power is accepted from the transmission line, i.e., VSWR less than 6:1.

Antenna	Bandwidth, MHz
A8	11.6
C4	27
B3	4.4
B4	6.7
D3	1.5
D5	5.9

Table 8. Characteristics of the changed antennas

Antenna	Frequency (MHz)		Bandwidth[b] (MHz)		Changes Made
	in air	in concrete	in air	in concrete	
A8-2	164	149[a]	20	8	Coil=3.25 turns. Coupling tap at ½ turn.
C4-2	147	135[a]	47	13	Coil=2.5 turns, 9.4 cm high. Coupling tap at 3/4 turn.
B3-2	150	139	2.8	2.6	Capac plate now circular. Coupling link, approximately as in D5.
B4-2	152	129	5.5	4.9	Coil stretched out=6.3 cm. Coupling, no change.
D3-8	153	150	2.9	3.5	Capacitor spaced 0.25 cm. Input link 0.94 cm gap and 4.6 cm to the short.
D5-2	153	148	1.4	0.8	Coil=2.8 turns with 1.6 cm turn spacing. Coupling link centered on coil, coil rotated 90° around its axis.
D6	149	138	0.8	1.1	Similar to D5, but with 8.9 cm diameter capacitor plates on the ends. Coupling link similar to that of D5.

(a) Frequency when set at interface, not buried, A8-2 = 163 MHz, and C4-2 = 146 MHz.

(b) Bandwidth is obtained from Smith chart impedance plots, and is defined as the frequency region in which the VSWR is less than 6:1.

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Usually the bandwidth decreased on burial in concrete, in
the anechoic room. From the impedance plots (not shown) it
appears that only antenna D3-8 is suitably coupled. The others
are too inductive, and overcoupled or undercoupled. Antenna
C4-2 is incorrectly coupled but does have very large bandwidth.
The results indicate that trial and error experiments on impedance
and coupling are usually required in order to approach an
optimum.

K. CONCLUSIONS FOR SECTION 4

Section 4 contains construction details for six resonant
antennas, and a detailed account of using impedance data to
study Q, coupling, efficiency, bandwidth, and interaction with
the burial medium. Theoretical circuit analysis of resonant
antennas has been described and applied to the mentioned charac-
tersitics.

An outstanding conclusion from this work arises from a
synthesis of the findings. From theory and by inspection of
the results in tables 6, 7 and 8, we make the hypothesis that
the frequency shift due to burial is approximately proportional
to the bandwidth. For example a long dipole has more stray
field, giving more C_3 in the circuit representation (fig. 34),
and because of its length, more radiation resistance. Thus
the Q will decrease and the bandwidth will increase, which is
very desirable; but the frequency shift due to more stray field
is larger, which is undesirable. Table 8 shows that in most
cases the shift in the resonant frequency due to burial in
concrete, $\epsilon' = 6.5$, is greater than half the bandwidth, which
means that the oscillator and antennas must be tuned beforehand
in anticipation of the burial. According to equation (37) and
the predictions in table 6 the frequency decrease saturates

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as ε' increases. This fact might be useful in offsetting the frequency of the generator and the antenna in air in anticipation of the shift of resonance upon burial.

Footnote (a) of table 8 shows that the so-called monopole antennas, A8 and C4, shift frequency only by 1 MHz when the top of the copper base is flush with the interface. Unfortunately, the frequency shift for partial burial (antenna top flush with the surface) was not obtained. In view of the suggestion in section 3G, to partially bury the monopoles, flush with the surface, it would be important to obtain a curve of frequency shift as a function of the penetration through the interface.

Active antenna techniques versus resonance techniques should also be investigated.

5. FIELD TESTS OF BURIED ANTENNAS

A. INTRODUCTION

Some field test results have been presented already in section 3. The important remaining field tests indicate performances of candidate antennas, which for reasons stated are small antennas.

If the theory is obeyed, as was concluded in section 3, and if the efficiency is known from the various methods in section 4, then comparison measurements as presented here are unnecessary; however, measurements were made and are believed to be worthwhile for verification. Also, the theory of a partially buried finite dipole was not treated; therefore, experiments are necessary for low-profile vertical dipoles.

B. THEORETICAL AND PRACTICAL CONSIDERATIONS

The space wave field depends on theoretical factors which are understood. The field after burial is predicted to be

$$E = E_f \ I \ D \ P \ J^{\frac{1}{2}}, \tag{38}$$

where E_f is the free space inverse distance field of equation (6), I is the interface loss of figures 2 and 5; D is the depth loss of equations (1) and figure 3; P is the underground pattern factor of figure 4 including in addition $\cos \phi$ or $\sin \phi$ for angles other than broadside and end fire, and J is the efficiency from equation (23).

The TM wave of the vertical electric dipole suffers considerable pattern loss P unless the dipole is "low profile," not fully buried.

The TM wave broadside from the horizontal magnetic dipole is theoretically the strongest possible wave. The pattern factor P is 1. The efficiency is least degraded by burial because a small loop has small near electric fields to interact with the losses of the burial medium. However, as seen in table 4 the ohmic efficiency of the 10 cm diameter loop (D3) is somewhat low; a 13 cm diameter would probably reduce the ohmic inefficiency loss to less than 1 dB loss.

The small loop is also attractive as a low-profile antenna, not fully buried. It does not, however, furnish the convenient 360° azimuthal coverage of the low-profile vertical dipole; crossed loops for circular polarization on the vertical axis would be required, and there is a loss of 3 dB compared to the vertical dipole because approximately half the energy of a horizontal dipole goes into TE waves.

The antenna D5 was designed with a diameter and pitch to give equal radiations from the electric and magnetic dipole moments [15]; furthermore, the theory shows that these two radiations are 90° out of phase, giving circular polarization. Thus, considering the broadside and end fire TM waves, there is 360° azimuthal coverage with TM waves from the buried horizontal electric and magnetic dipoles.

C. FIELD SITE PERFORMANCE OF SMALL ANTENNAS

The measuring arrangement is that indicated in figure 6. The field site is on the NBS grounds and is not as smooth as the previously mentioned alfalfa field. Burial is accomplished by placing concrete rings in the ground with outer diameter 30.5 cm and inner diameter 13 cm to accept each 12.7 cm diameter candidate antenna. Concrete disks are put on top of the antenna after it is set down in the hole. By this method, to a good approximation, all antennas are buried under the same medium of known dielectric constant.

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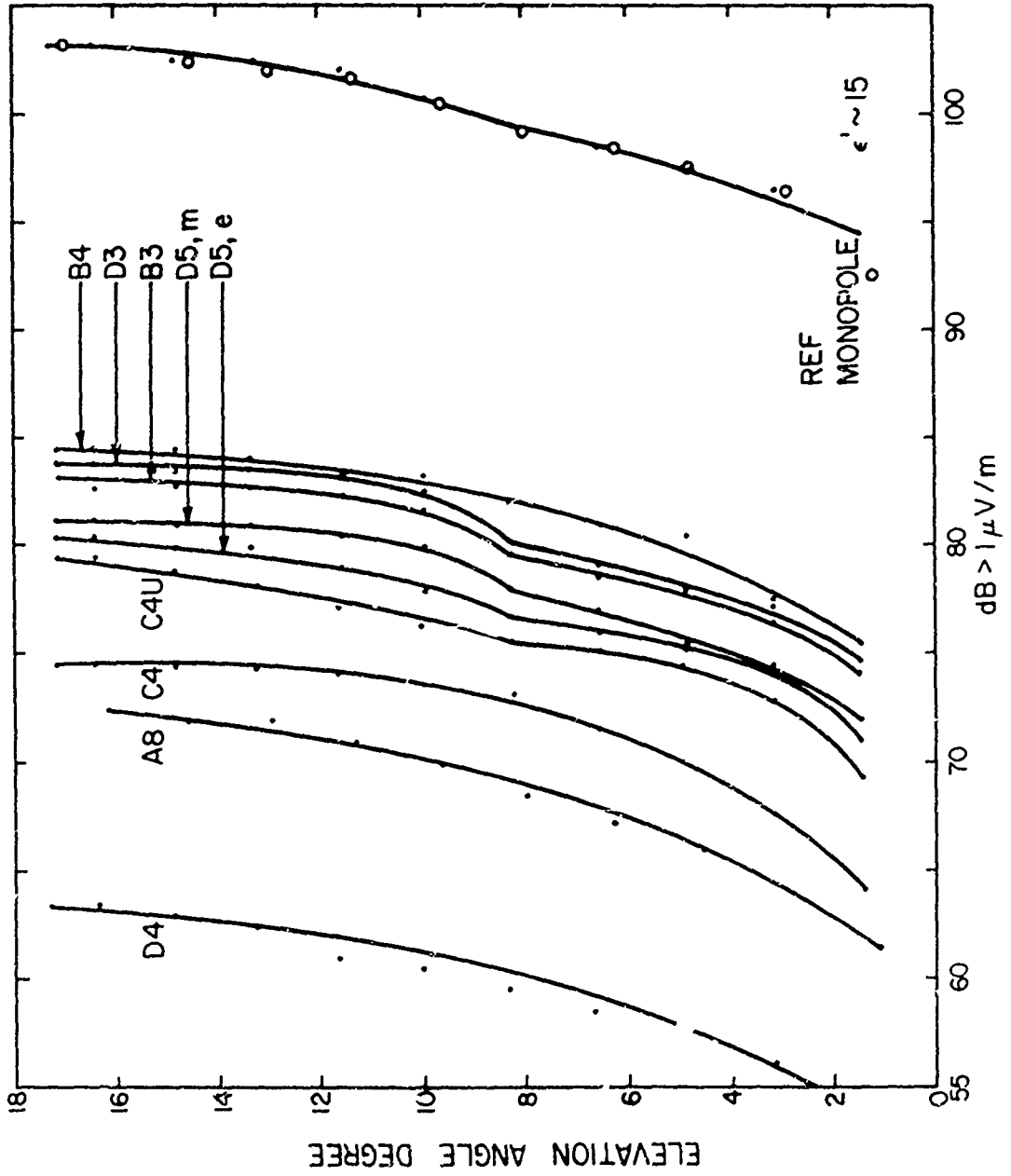
Figure 35. Field measured at R = 30.5 m; P_a = 1 w to the buried antenna.

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The concrete was made from a 94% aluminum oxide cement. It was assumed to have a relative dielectric constant of 6.5 and a loss tangent of approximately 0.008, since it was cured at elevated temperature, 125°C, as recommended in [8].

Figure 35 shows the received field strength in dB greater than 1 microvolt per meter at 30.5 m horizontal distance, normalized to 1 W power input into the antenna, for several antennas. The field strengths were obtained from the received voltage, taking into account transmitted power and receiving conversion factors as outlined in section 3D and 3E. The length, u, of the transmitter cable was 10.7 m. In addition, a small correction was estimated to allow for the change in efficiency of the antenna due to the lower resonant frequency (below 145 MHz) when buried. Table 9 lists the test frequency and the conversion factors just mentioned. Bends in many curves of figure 35 are similar to bends observed in reference [8], which were due to a mismatch between the concrete and the earth.

The results show that antenna B4, a HED, furnishes the strongest signal, by a small margin. The loop D3 is slightly weaker, presumably due to inefficiency, because its radiation resistance is only 0.11 ohm. The loop needs to be larger.

The circularly polarized design D5 is a very good antenna. For performance comparisons 3 dB should be added to both measured fields in order to compare on the same power basis with B3, B4, and D3. This is true because D5 consists in effect of two crossed dipoles. B3, B4 and D3 would have to be fabricated as crossed dipoles fed 90° out of phase to give the same field coverage as D5, and would lose 3 dB in the process.

It will be noted that this group of horizontal dipoles, all of similar performances, (converting to 360° coverage) is about 20 dB weaker than the reference monopole. This loss is unavoidable for a horizontal electric dipole. The theoretical losses relative to isotropic may be itemized as follows,

Table 9. Conversion factors to obtain field strength normalized to 1 W power into the antenna, and correction for the lower efficiency due to the frequency being less than 145 MHz.

Antenna	Test Freq. MHz	Conversion to Field and 1 W Normaliz., dB	Correction[c] for Freq. Effect on Efficiency, +dB
A8	130.3	-1.37	0.06
C4	111.6	-2.05	0.34
C4,u[a]	116.5	-2.2	0.34
B3	128.1	-1.2	0.9
B4	113.1	-2.1	1.0
D3	142.9	+1.0	0.14
D4	146.5	+1.1	--
D5,e[b]	117.1	-2.2	0.05
D5,m[b]	116.7	-2.2	0.11
Monopole	145	+0.1	--

(a) Antenna buried about 5 cm; other burials were 10 to 20 cm.

(b) The letters e and m signify the electric and magnetic dipole radiations of the coil, respectively.

(c) Efficiency $J = R_r/(R_r+R_{cu})$; R_r is proportional to f^2 for electric dipoles and f^4 for magnetic dipoles.
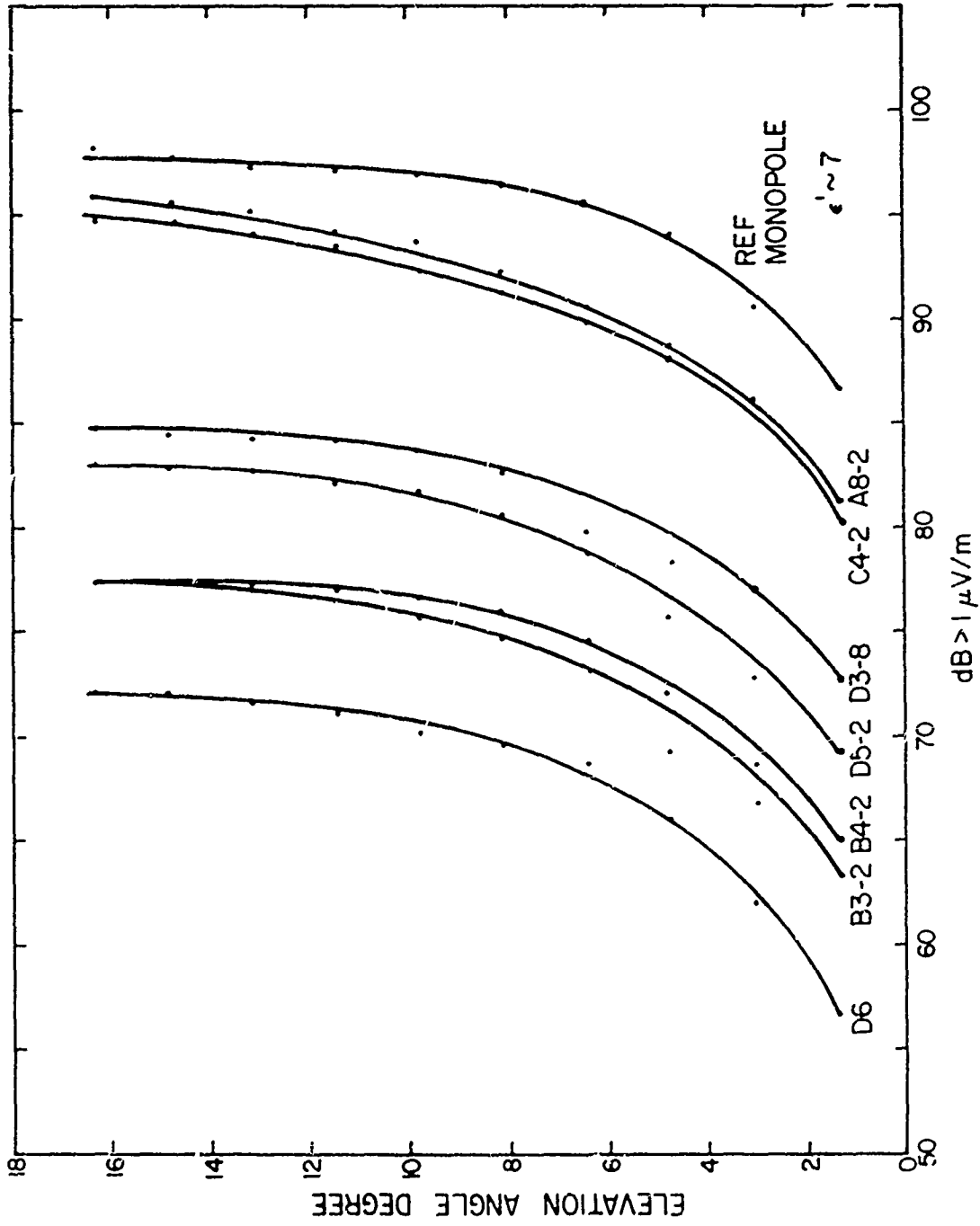
Figure 36. Same as Figure 35 but antennas modified.

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at 10° elevation, and dielectric constant of the burial
medium = 6.5:

    a.   Interface loss, I,   14 dB

    b.   Depth loss, D,   0.2 dB

    c.   Pattern factor, P   0.3 dB

    d.   Circular polarization   3 dB
            power loss

    e.   Efficiency, J, $\sim$ 1 to 3 dB

    Total Loss, Relative to Isotropic, 18.5 to 20.5 dB.
Some of this loss might be avoidable with D3 as a low-profile
partially buried antenna.

The reference antenna has approximately 0 dB gain with
respect to an isotropic emitter at 10° elevation. The HED
system with 360° azimuthal coverage is approximately 20 dB
weaker than the monopole experimentally; thus the experiment
is in good agreement with the above theoretical estimate.

Figure 36 shows electric field strength patterns, measured
in the same way as in figure 35, but after the candidate antennas
were modified as indicated in table 8.

The D3 antenna, with nearly optimum coupling and the fre-
quency increased by 5 percent, now gives more signal than B3
and B4. Surprisingly D3 is only 13 dB weaker than the reference
monopole (16 dB weaker, if circular polarization coverage is
added). However, the reference monopole is approximately 4 dB
weaker than in figure 35, presumably because the ground was dry
for figure 36 and wet for figure 35. D3 on an absolute basis
(relative to isotropic) is approximately 1 dB better than in
figure 35. At any rate D3 is doing as well as can be expected
for an antenna buried in a medium with $\varepsilon' \sim 6.5$.

Antenna D5-2 was modified incorrectly and consequently it
lost much of its electric dipole strength, but the magnetic
dipole component is still very good.

Antennas B3-2 and B4-2, as modified, and D6 are in need of
further development.

The vertical dipoles A8-2 and C4-2 were not buried; the top
of the base was at the interface. The resonant frequencies
were only lowered 1 MHz by this partial "burial." These antennas
furnish 360° azimuthal coverage. If the low profiles (7 and
10 cm) are acceptable for concealment, then these are certainly
convenient and useful antennas. They are easy to fabricate,
can have a bandwidth of 10 MHz or more, and give fields about
4 dB weaker than does the reference monopole.

Figure 12 has indicated the variation of loss as a function
of burial depth. However, more work of this type is desirable
in order to know the effect of various parameters, such as
dielectric constant and conductivity, on the curves shown in
figure 12.

D. SUMMARY OF RESONANT ANTENNAS

The low-profile vertical electric dipole, VED, at the
earth's surface conveniently furnishes the desired TM wave (wave
with horizontal magnetic vector) in space without serious in-
efficiency loss or burial loss.

The profile can be flush with the interface by accepting
some additional loss. The amount of this loss (fig. 12) can be
reduced by a larger encapsulation diameter than the 13 cm
diameter used here.

A low profile situated or a "flush" buried HMD, i.e., an-
tenna D3, figure 17, has approximately 3 dB less gain than the
VED because half of its energy goes into TE waves. It will be
less convenient because crossed dipoles for circular polariza-
tion are required.

The HED either on the surface or buried will suffer the
apparently unavoidable interface loss, furnishing a gain of
-18 to -20 dB below that of a reference monopole on the inter-
face, assuming a dielectric constant of 6.5.

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6. PREDICTED DISTANCE OF COMMUNICATION

A. INTRODUCTION

The gain of a fully buried antenna appears to be that pre-
dicted by Sommerfeld theory [1] as given by equations (1) above.
The gain of a low profile vertical dipole is approximately -4 dB
relative to a high efficiency quarter wavelength monopole on a
one wavelength diameter metal disk, and the latter has well
known gain properties [7]. Using these facts, predictions may
be made of the distance over which communications can be re-
ceived from buried and low-profile antennas.

B. ASSUMED TRANSMITTER POWER AND RECEIVER CHARACTERISTICS

It will be assumed that 1 W is accepted by the buried or
partially buried antenna, of which the fraction J is radiated,
where J is the antenna efficiency.

The criterion for reception depends on the bandwidth, noise
level, and modulation scheme. At 145 MHz the equivalent median
value field strengths due to various noise sources are estimated
as follows, per kHz receiver bandwidth [16]:

Urban Man-Made Noise	∿ -120 dBV/m/kHz
Cosmic Noise	∿ -129 dBV/m/kHz
Internal Receiver Noise	∿ -138 dBV/m/kHz

The field specified for equaling internal receiver noise
may be interpreted as follows: The room temperature Johnson
noise of a 50 ohm resistor, approximately -151 dBV/kHz,* has
been converted to equivalent field strength using the dipole
conversion factor of 9.3 dB, section 3C, and a noise figure of
3.7 dB has been included, yielding -138 dBV/m/kHz. A rural
environment without urban noise will be assumed.

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*dBV/kHz denotes dB relative to 1 volt, per kHz bandwidth.
 dBV/m/kHz denotes an equivalent field in volts per meter
 per kHz [16].

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The bandwidth of a modern receiver may reasonably be of the order of 10 to 100 kHz. Using the cosmic noise level of -129 dBV/m/kHz as a criterion for reception, the required signal electric field in the air is

-119 dBV/m, at 10 kHz bandwidth

-109 dBV/m, at 100 kHz bandwidth,

for a 1:1 signal to noise ratio, S/N.

C.   GAIN PATTERN OVER A SPHERICAL EARTH

All preceding discussions of the gain pattern in the air space have been for a flat earth. Fortunately, at the angles considered, elevation angles of 1° or more, the flat earth results also apply to spherical earth propagation at UHF frequencies, provided that the elevation angle of the field pattern is measured with respect to a plane tangent to the sphere at the point where the antenna is buried [17]. Reference [17] shows that at elevation angles of 1° or more the field of a monopole or dipole located on or near the earth is nearly the same for a flat earth and for a spherical earth. The tangent plane would be somewhat spherical to allow for the earth's atmosphere, but instead we use the usual 4/3 earth's radius approximation [18]. Then the height h in feet of the new flat tangent plane is h = $R^2/2$ where R is the horizontal distance in miles from the point of tangency. The elevation angle is obtained from the height above this tangent plane.

D.   FIELD STRENGTH VERSUS DISTANCE

The chosen communications model is a 1 W source driving a buried or a low-profile antenna and a receiver 50,000 feet above the spherical earth. Figure 37 shows the predicted fields versus the horizontal distance for various conditions. Only a TM wave is considered.

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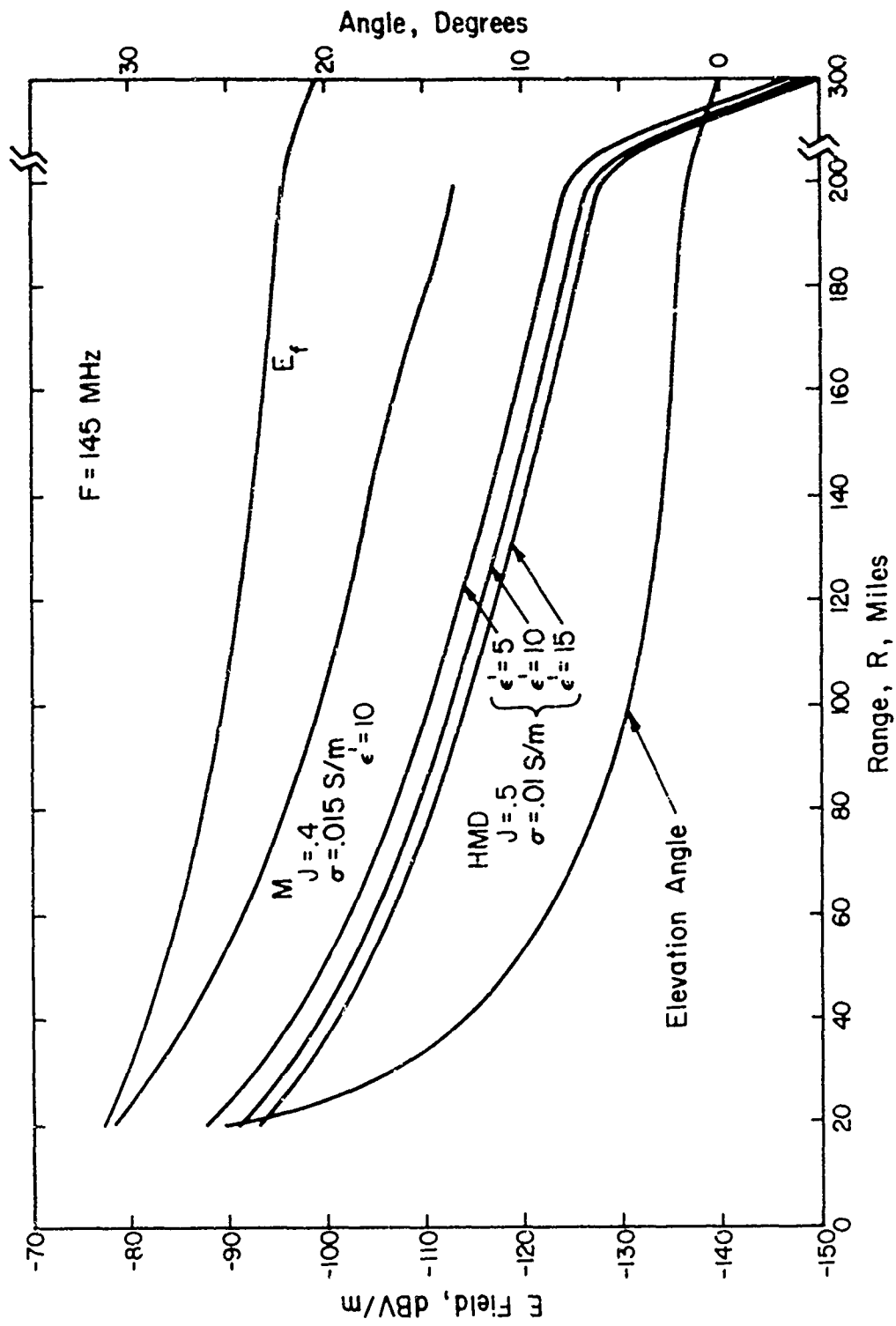
Figure 37. Field strength at 50,000 feet versus range; 1 watt source.

The curve E_f for free space is evaluated from equation (6).
The elevation angle, measured as previously discussed, is indi-
cated by another curve. The curve marked M (monopole) is
evaluated from

$$E = E_f \, M \, J^{\frac{1}{2}} \qquad\qquad (39)$$

where M is the vertical monopole pattern factor [7] of figure 9,
and J = 0.4 to represent the 4 dB loss of the low-profile verti-
cal dipole (fig. 36) compared to the "reference" monopole.

The group of curves with parameters ϵ' = 5, 10, and 15
is evaluated for a buried loop (HMD) using equation (38)

$$E = E_f \, I \, D \, P \, J^{\frac{1}{2}}.$$

It is assumed that P = 1 for the HMD, that D = 1 (shallow burial),
and that J = 0.5. The computer routine used for figure 2 was
modified to include the proper angle and range.

A field strength of -109 dBV/m, as suggested above for
equaling cosmic noise in a 100 kHz bandwidth receiver, will be
used as a criterion for reception. (Reference [19] in a study
of spread spectrum techniques uses an ultimate receiver sensi-
tivity of -107 dBm corresponding to -120 dBV at the receiver and
-110 dBV/m field strength in the air. We have, however, used
-109 dBV/m as a criterion.)

The results for the buried HMD antenna show that a field of
-109 dBV/m occurs at 92 miles for ϵ' = 5, at 79 miles for ϵ' = 10,
and at 72 miles for ϵ' = 15. The conductivity was 0.01 S/m
throughout. The curve M for the low profile VED falls to
-109 dBV/m at a range of 172 miles.

The communications range may be found for other source
powers by a shift of scale of 10 dB per factor 10 in power.
Also other criteria may be used for the required field strength
for reception; e.g., the assumed dipole receiving antenna may
be replaced by a higher gain antenna to increase R.

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7. DISCUSSION AND CONCLUSIONS

Electrically small resonant dipole antennas were developed
to be buried in the earth for concealment. For a buried dipole,
the gain and the pattern in the upper half space are well pre-
dicted by Sommerfeld theory and also in general by physical
optics methods which were developed. Experiments confirm the
theoretical factors, in particular the interface loss and the
pattern in space. A "reference" monopole on the surface con-
firmed the accuracy, ± 1 dB, of the overall measuring system,
i.e., of the transmitted power and received field strength
measurements.

In contrast with above-ground antenna experience, the
required TM wave is not best obtained from a buried vertical
dipole. Buried horizontal dipoles, either the HMD or the HED,
provide stronger TM waves, but there is a sine or cosine
azimuthal dependence. Coverage over 360° is provided by crossed
horizontal dipole with circular polarization.

The interface loss due to burial will often be in the range
of 15 to 25 dB; it increases with the dielectric constant of
the ground. An additional difficulty is the shift of the
resonant frequency and consequent mismatch of the antenna to
the generator, resulting from burial. The resonant electric
dipoles may remain matched to the generator after burial, either
by adjusting for the frequency shift ahead of time, or by using
a larger encapsulation to prevent interaction with the ground.
The preceding statement probably also applies to resonant loops.
The roughly 10 cm diameter loop investigated had a comparatively
small frequency shift, table 6, but still it exceeded the band-
width of the resonance, table 7.

In view of the above problems, methods of avoiding fully
buried antenna are desirable. Convenient vertical dipoles,
figures 13 and 14, may be partially buried, rising 7.5 and 10 cm

8.

above the earth's surface respectively. The loss due to burial
is then approximately 4 to 5 dB (fig. 36), and TM waves are
obtained over 360° in azimuth. The frequency shift due to
burial in $\varepsilon' = 6.5$ was small, 1 MHz. Theoretically, crossed
HMD loops with circular polarization would also function well
as a low-profile antenna. Finally, this antenna and the VED
could be set flush with the surface of the ground for conceal-
ment, and with a slightly larger, 15 to 18 cm, diameter plastic
cover, the loss due to burial is estimated to be only 5 to 10
dB more than for low-profile above-ground antennas.

Active antenna techniques, section 41, remain to be invest-
igated. These techniques have been used [13] instead of resonance
to match an antenna to generator. The advantage would be that
the impedance match would not be lost if the system were buried.

Section 4 gives a detailed account of impedance measure-
ments for analysis of the efficiency, bandwidth, coupling, and
interaction with the burial medium.

The predicted maximum range of communication with 1 W power
and a receiver at 50,000 feet altitude is 170 miles using a
low-profile VED. The predicted range when the antenna is a
fully buried HMD (resonant loop) is 70 to 90 miles.

According to reciprocity theory the antennas developed
here for transmitting purposes will have the same burial loss
and efficiency when used as receiving antennas.

It is recommended that the present research be extended to
include a study of the bandwidth, frequency shift, and inter-
face attenuation as functions of shallow burial depth (near
the interface) and as functions of the size of the encapsulation.
Also, the allowed dimensions for convenient tactical deployment
should be redetermined with the idea of obtaining increased
bandwidth by a larger structure.

The active antenna alternative should be investigated
and might obviate the frequency shift and bandwidth problems
encountered,

The buried HED and HMD antennas are useful assuming that
the frequency shift due to burial is engineered into the
design, or reduced by allowing more encapsulation. The VED
antennas A8 and C4, figures 13 and 14, may be used as
convenient low profile partially buried antennas.

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by

The NBS Electromagnetics Division Staff

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