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DEVELOPMENT AND APPLICATIONS OF THEORETICAL METHODS FOR EVALUATING STABILITY OF OPENINGS IN ROCK

WOODWARD-LUNDGREN AND ASSOCIATES

PREPARED FOR BUREAU OF MINES Advanced Research Projects Agency

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FINAL REPORT

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March 14, 1972 - December 14, 1973

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Principal Investigators: K. Nair and C-Y Chang Telephone Number: (415)444-1256

Name of Contractor: Woodward-Lundgren & Associates

Effective Date of Contrac*: March 14, 1972 Project Scientist or Engineer: C-Y Chang, K. Nair and R. D. Singh Telephone Number (415)444-1256

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Development and Applications of Theoretical Methods for Evaluating Stability of Openings in Rock

Contract Expiration Date: December 14, 1973

Amount of Contract: \$78,920

This research was supported by the Advanced Research Projects Agency of the Department of Defense and was monitored by the Bureau of Mines under Contract Number HO220038.

TECHNICAL REPORT SUMMARY

CONTRACT OBJECTIVES

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The objectives of this contract are:

(1) To incorporate into the finite element computer program for plane strain analysis, with capabilities to perform joint perturbation, no tension and elasto-plastic analyses developed under Contract No. H0210046, the capability to model and analyze: (a) structural support schemes used in the construction and design of tunnels, and (b) typical excavation sequences utilized in underground construction, and

(2) To evaluate the analytical method (computer program) developed in (1) by a study of case histories.

GENERAL APPROACH AND TECHNICAL RESULTS

The approach to this study can be divided into two phases:

I. On the basis of available information on excavation techniques, construction and excavation sequence, mechanisms of ground support and current design techniques for support systems, formulate computational models and modify the existing computer program to incorporate these computational models, and

II. Analyze case histories and compare predicted and measured performance.

(I) <u>Formulation of Computational Models and Modifications</u> of Existing Computer Program

On the basis of the review of the available information, the following modelling concepts were developed:

(1) Excavation Techniques - It is known that excavation of an opening creates some disturbance in a rock mass surrounding the opening. Depending upon the excavation technique, e.g., drilling and blasting, smooth wall blasting or boring machine, rock conditions and time of installation of support systems, the zones of loosening and fracturing and the depths of overbreak around the opening will be different. Zones of disturbance may be estimated on the basis of experience at locations with similar geologic conditions and excavation methods or determined by seismic refraction surveys in the field.

The essential features that have to be modelled in simulating the effects of excavation techniques are the following:

- (i) The stress-free excavation face. It has been shown that excavation may be simulated in the finite element method by applying stresses to the boundary exposed by excavation so that there is no resultant stress on the excavation face. A similar technique was used in this study.
- (ii) The disturbed zone in the vicinity of the excavation. This zone can be modelled by assuming a lower modulus for the material in the zone or by assuming that the material is incapable of carrying any tensile stress. Both these techniques were utilized in this study.

(2) Construction and Excavation Sequence - The essential features to be modelled and the basic concepts in modelling them are described below:

- (i) The time sequence of construction, including installation of supports. Because of the limitations that only time-independent material properties can be included in the program, the time sequence of construction will be modelled in accordance with the following two-stage analyses:
 - (a) An initial analysis prior to any support installation will be conducted.
 - (b) A subsequent analysis will be conducted with the support system installation treating the results of the analysis in (a) as the initial condition. In a practical problem, it will be necessary to bracket possible initial conditions.
- (ii) The excavation sequence. The opening goes through many shapes before reaching the final shape. If the problem could be treated as linear elastic, the final stress distribution would be independent of the excavation sequence; for non-linear problems, it is necessary to consider the sequence. Excavation sequence will be simulated by removing those elements that will be excavated and ensuring that the excavation face is stress free.

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(3) Support Systems - This development is based on considering the interaction of the support and the surrounding rock mass. The three basic support systems considered in this study, (i) steel sets, (ii) rock bolts, and (iii) shotcrete liners, are discussed separately.



- (ii) Rock Bolts Because of difficulties associated with analysis of a rock bolt system i.e., the threedimensional aspect, the interaction of each rock bolt with the rock cannot be modelled in this study. The following approximations are proposed to idealize the rock bolt support system:
 - (a) To increase the stiffness of the rock mass in the immediate vicinity of rock bolts to account for the presence of rock bolts and grouted rock bolts.
 - (b) To approximate the effects of tensioned bolts on the rock mass by applying a set of opposite concentrated loads at the anchor and bearing plate. Each concentrated load is considered to be an equivalent line load along the tunnel axis to represent a row of rock bolts. The

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magnitude of the line load is determined by the bolt tension and the spacing of bolts.

- (c) Untensioned grouted rock bolts may be idealized as one-dimensional bar elements with material properties similar to those of rock bolts.
- (iii) Shotcrete or Concrete Linings Shotcrete or concrete linings may be idealized as a plane strain structure. Grouting or back packing behind the lining may be modelled in the analysis with materials of different stiffness.

Before modifications were made for the present contract, two improvements were incorporated into the program. These were (i) utilization of elasto-plastic stress-strain relationship to compute the axial strain, and (ii) updating the element stiffness at each load increment to improve convergence.

Several example problems were solved using the modified computer program, and the results compared when possible with results published by other investigators.

(II) <u>Evaluation of Analytical Method (Computer Program)</u> -Case History Studies

To illustrate the use and evaluate the capabilities of the computer program model developed in (I) well documented case histories on the performance of underground openings were analyzed. These covered a range of conditions to illustrate the wide applicability of the program. Computed performance was compared with observed performance.

The cases analyzed are described below.

Model Tests - (a) Lined and (b) Unlined Openings The model tests conducted by Hendron et al. (1972) on lined openings in jointed rock were analyzed. The model has a colled opening of 4 inches in diameter and a 0.035-inchthick aluminum liner and was constructed with a 2-inch joint spacing in two mutually perpendicular directions at 45° to the principal loading directions. The model was tested at a principal stress ratio, $\sigma_{\rm H}/\sigma_{\rm V}$ = 2/3 to a maximum vertical model pressure of 1300 psi under plane strain conditions and was instrumented with eight pairs of buried extensometers and six diametrical extensometers in the tunnel liner to measure the deformability of the jointed model as well as the movements around the opening. Both the joints and the liner were modelled in the analysis.

The Tumut I Underground Power Station

The power station is situated under the lower part of the very steep eastern wall of the Tumut Valley in the Snowy Mountains of Southeast Australia. It is located about 1100 feet vertically below the ground surface, 1200 feet in from the river, and 150 feet below the level of the river bed. The machine hall is 306 feet in length, 44 feet in maximum width, and 104 feet in maximum height. The machine hall excavation was made in several stages. After the pilot tunnel was driven, the roof section of the machine hall was excavated to full width, systematical rock bolts and permanent concrete ribs installed. Following this, the main body of the machine hall was excavated by quarrying methods. The vertical walls and roof were systematically rock-bolted as soon as they were exposed. The behavior of the rock mass around the machine hall was observed during construction by strain measurements in many of the reinforced concrete arch ribs and measurements of the horizontal movements of points at the ends of the concrete ribs and on the rock walls, and angular rotation of points on the reinforced concrete abutment

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beams and on the rock walls. A simplified excavation sequence and the influence of rock bolts and concrete ribs were included in the analysis. Two 'faults' which intersect the machine hall were also modelled in the analysis.

Rock Tunnel Washington D.C. METRO

The rock tunnel analyzed was driven through a foliated rockschistose gneiss of quartz-mica composition. Average rock quality, defined as the RQD of the rock cores, ranges between fair to good, except in the shear zones where rock quality is poor to very poor. The geologic features present at the tunnel consist of four highly continuous, smooth, planar joint sets and eight major shear zones. The major shear zones and two of the joint sets are subparallel to rock foliation and strike within 10° of the axis of the The tunnel was excavated in several stages together tunnel. with installation of shotcrete, grouted rock bolts and steel ribs. Rock movements were monitored by a series of multiple position extensometer during excavation. Rock reinforcement, joints and a simplified excavation sequence were utilized in the analysis.

Results

Verification of the program in the strictest sense was not possible because in all the cases analyzed there was insufficient direct information to model all significant aspects of the problem. The major lack of information was found to be with respect to geologic discontinuities. It is believed that this will be true in most practical problems. Analysis of the case histories has shown that it is possible by means of a parametric study to select appropriate properties of geologic discontinuities which are both reasonable according to published information and if used in further analysis will result in predictions of reasonable accuracy. A collection of case history studies categorized by geologic conditions would provide a means of selecting appropriate properties to predict the performance of excavations. Furthermore, in a continuing excavation (e.g. a subway) information obtained during its early stages can be used to calibrate the program in terms of appropriate properties to predict future performance. The results indicate that the program developed can be an extremely useful aid in **designing** excavations in rock.

DOD IMPLICATIONS

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The evaluation of the structural stability of underground openings, ground support structures, and other facilities is an essential step both in the design and in the survivability/vulnerability assessment of underground structures and weapon systems.

A computer program has been developed to analyze the influence of excavation techniques, construction, and excavation sequence and structural support schemes on the stability of excavations in rock masses where the rock mass behavior is dominated by block slippage along discrete joint planes, or a global inability of the rock mass to resist tensile stress, or elastic-plastic behavior of the rock mass, or any combination of the three rock mass physical characteristics. This computer program should be considered as a tool to assist in the evaluation of supported and unsupported underground openings.

CONSIDERATIONS FOR FURTHER RESEARCH

Studies of a limited number of the case histories have indicated that the analytical models developed under this contract could predict the behavior of underground openings with reasonable accuracy. As indicated, the major problem in utilizing the computer code is the lack of information on the properties of geologic discontinuities. 1.17

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By studying additional well documented case histories and using an iterative procedure appropriate material properties for different geologic conditions can be determined. Such information would be extremely valuable for future work and should be developed.

ACKNOWLEDGMENTS

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The research was supported by the Advanced Research Projects Agency of the Department of Defense and was monitored by the Bureau of Mines. Dr. R. D. Singh and Mr. A. M. Abdullah contributed significantly to the research reported herein. The Project Officer of the Bureau of Mines was Mr. Grant Anderson; his assistance and cooperation in conducting this study is acknowledged.

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A combined Computer Program Using Finite Element Techniques for Elasto-Plastic, Joint Perturbation and No Tension Analysis of Sequential Excavation and Construction of Underground Openings in Rock

APPENDIX B

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Computer Program Listing

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INTRODUCTION

In the previous contract (HO210046), a general plane strain finite element computer program was developed for the analysis of underground openings in rock. Under the present contract, it is proposed to add to the capabilities of this computer program by including techniques to analyze the influence of excavation techniques, construction and excavation sequence, and structural support schemes on the stability of excavations in rock.

Because of the development of increased analytical capabilities, it is considered appropriate to consider these capabilities in the context of the total problem of evaluating the stability of openings in rock. Whereas the results of analytical studies can be of great assistance in the evaluation of stability, there are several other factors that enter into the evaluation, and it is necessary that one not be lulled into a sense of false security because of elaborate computational techniques.

METHODOLOGY FOR EVALUATING THE STABILITY OF OPENINGS IN ROCK Analysis of openings in rock is a complex problem because of the numerous factors influencing the behavior and stability of the opening. These include (i) rock properties, (ii) the location, geometry and size of the opening, (iii) geologic conditions such as joints, foliation surfaces, bedding planes, shear zones and fault zones, (iv) in-situ stress conditions, (v) excavation and construction methods, and (vi) support systems. Because of the complexity of the nroblen, it is appropriate to develop a general framework for evaluating the stability of openings in rock. Such an approach is summarized in Figure 1. This approach consists of the following major steps:

1. Establishment of Objectives and Performance Criteria. In any design process, it is necessary to establish the objectives of the design and to translate these objectives into performance criteria. In general, the objective of the design

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is that the opening remains stable and usable during its design life. The performance criteria, for example, may be in terms of limiting the stress, strain and/or displacement induced in the rock mass and support system surrounding the opening.

2. Definition of Input and Output (Response) Variables. The major inputs can be considered in terms of loads, external and internal, e.g., in-situ stress, the effects of construction methods and excavation techniques including environmental (temperature and moisture) factors. The output variables may be stress, strain and displacement in the rock mass and support system. In defining the output variables, it should be recognized that they should be in terms of the performance criteria in order that a comparison can be made.

3. <u>Physical Description of the System</u>. The description of the system consists of the following: (a) the size and geometry of the opening, (b) its location below the ground surface, (c) distribution of geologic discontinuities (e.g., joints, foliation, bedding planes, faults, shear zones) of the rock mass, (d) mechanical properties of the rock mass, and (e) support systems used to maintain stability.

4. Determination of the Response of the System. This requires (i) the development of a model or idealization for the system, and (ii) the use of analytical and experimental techniques to determine the response of the model to the prescribed inputs. There are two general approaches for determining the response of the system.

(a) Experimental Approach - Laboratory models using photoelastic techniques or blocks of rock-like materials tested under simulated field conditions or a full scale test conducted in the field may provide data which can be useful in understanding the behavior of the real structure and developing an empirical design procedure for openings constructed under similar geologic conditions. However, WOODWARD-LUNDGREN & ASSOCIATES it is often difficult to extrapolate an empirical design procedure to conditions different from those under which the procedure was developed.

(b) Macroanalytical Approach - This approach involves the development of a mathematical model for the system and the solution of an appropriate boundary value problem. The development of such a model should be based on a physical understanding of the problem and an evaluation of past performance. The objective of such an approach is to develop a general, theoretically sound method of analysis on the basis of which the output of the system can be determined if the input is prescribed and the system adequately described. It is the macroanalytical approach that forms the basis for the majority of the existing design methods in engineering practice. It is within the context of this approach that the analytical techniques under development in this contract have to be viewed.

5. <u>Decision on Acceptability of Design</u>. The predicted output of the system should be compared with performance criteria to see if stress, strain and displacement in the surrounding rock mass and support system are within allowable limits to prevent failure of the support system and the opening.

6. <u>The Feed Back Loop - Optimization</u>. In the idealization of a physical system as complex as an underground excavation in a rock mass, it is necessary to make many simplifying assumptions. In order to establish the validity of these assumptions, it is necessary to compare the performance of the actual system with the predictions. This comparison is essential to establishing the reliability of the techniques developed for evaluating stability. The results of monitoring the performance of the actual system should then be fed back into the methodology for evaluating stability to improve the assumptions and idealizations. In this manner the methods for evaluating stability

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will improve. In this context the development of a theoretically sound method for evaluating the stability of openings in rock is an iterative process as indicated in Figure 2.

The work performed under this and the previous contract are indicated in the context of the total system in Figures 1 and 2. As more information is obtained from observed performance and better analytical techniques are developed, there will undoubtedly be further improvements in the methods of evaluating stability.

OBJECTIVES

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The objectives of this study are:

(1) To incorporate into the finite element computer program for plane strain analysis, with capabilities to perform joint perturbation, no tension and elasto-plastic analyses developed under Contract No. H0210046, the capability to model and analyze:

- (a) structural support schemes used in the construction and design of tunnels, and
- (b) excavation techniques and construction and excavation sequence in underground construction;

and

(2) To evaluate the analytical method developed in (1) by a study of case histories.

It is not proposed to make any basic modifications in the previously developed program but rather to add to its capabilities. Therefore, the additional capabilities have to be incorporated into the program within the context of the limitations of the previous program; the major limitations being (i) plane strain

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- *1. As a first iteration linear elastic analyses were utilized.
- 2. Comparison with observed performance indicated that the linear elastic analysis was not satisfactory.
- 3. We are now in the second iteration having improved our analytical methods.

FIGURE 2 - DEVELOPMENT AND VERIFICATION OF ANALYTICAL METHODS FOR ANALYSIS OF UNDERGROUND OPENINGS

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conditions have to be assumed, and (ii) time dependent material properties cannot be included. The emphasis of the computational models is to the design and construction of tunnels.

RESEARCH APPROACH

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In order to meet the objective of the contract, the following general research approach was adopted:

- (i) Review, for the purpose of developing computational models, the available information on excavation techniques, construction and excavation sequences, the mechanisms of ground support and the current design techniques for support systems.
- (ii) Formulate the computational models on the basis of the review in (i).
- (iii) Modify the computer program to incorporate the computational models.
 - (iv) Select case histories for analysis.
 - (v) Idealize the case history problems for analysis and conduct analysis.
- (vi) Compare actual performance with predicted performance.
- (vii) Formulate conclusions on the adequacy of the computational method based on (vi) and recommend improvements.

The report is organized in accordance with this approach.

EXCAVATION TECHNIQUES, CONSTRUCTION AND EXCAVATION SEQUENCE AND SUPPORT SYSTEMS

In order to develop models to include excavation methods, construction sequence and support systems, it is first necessary to review existing information in these areas so that the essential elements that should be modelled can be identified.

EXCAVATION TECHNIQUES

The drill and blast method and the boring machine are two methods commonly used in rock excavation. Excavation by blasting causes loosening and fracturing of the rock beyond the excavated boundary. The depth of the disturbance depends on the blasting technique and rock conditions, and may be estimated by empirical methods based on experience or by seismic refraction surveys in the field. Seismic refraction surveys along the tunnel walls (Deere, et al. 1969) have shown a 2- to 10-ft-thick low velocity zone which is considered to be disturbed by blasting. The thickness of this zone is a function of the rock quality. The loosening and the thickness of the zone of disturbed low velocity rock increases as the rock quality decreases.

Compared to the fracturing and loosening of the rock by blasting, the boring machine causes little or no disturbance. The rock immediately adjacent to the opening can be assumed to have essentially the same properties as that of the undisturbed rock.

It appears, therefore, that the essential capability that should be developed in modelling the excavation technique is the ability to model loose and fractured rock in the vicinity of the opening.

CONSTRUCTION AND EXCAVATION SEQUENCE

The construction sequence is the sequence in which the excavation is conducted and the support system installed. The effect of the time scale of these operations depends to a large degree on the time-dependent response of the rock.

Tunneling causes changes in stress and gradual loosening in the vicinity of the opening. The gradual loosening depends not only on the quality, bedding, jointing and foliation of rock, as well as the width of the excavation, but also on the distance between the last support and the rock face. For a certain period prior to breakdown, the loosened rock itself is capable of overbridging the unsupported cavity. This is referred to as the bridge-action period (t_h) . The sequence and method of excavation should be selected to enable the installation of the necessary new support before the bridgeaction period has expired. The typical position of the bridgeaction period in relation to the sequence of operations during the construction of a tunnel excavated by blasting in certain rocks is shown in Figure 3. Figures 4 through 6 show the relation between time, overbreak and rock load for various rock types and support systems. The degree of overbreak, depending on the length of the unsupported section in a horizontally stratified rock, is illustrated in Figure 4. Figure 5 shows the progressive loosening in the supported section with time and the effect of backpacking on the rock load in blocky and seamy rocks. The relation between time, overbreak and rock load is presented in Figure 6.

The following techniques are commonly used in excavation of underground openings:

<u>Full Face Method</u> - In a full face operation, the tunnel is blasted out full size at each round. Small size tunnels always are driven full face.

<u>Heading and Bench Method</u> - In this method, illustrated in Figure 7, a top heading is carried ahead of the bench about 1-1/2 times the length of one round, usually about 6 to 16 feet. The heading

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has the full width of the tunnel and is carried down to the spring line. Both bench and heading are shot out at each round, the bench charges being fired first.

<u>Top Heading Method</u> - Instead of taking out the bench along with the heading, the top heading may be driven clear through as one operation, followed later by removal of the bench.

<u>Side Drift Method</u> - The side drift method, as shown in Figure 8, is sometimes employed in a large size tunnel through bad rock which requires support before mucking out.

<u>Multiple Drift Method</u> - This method is usually a combination of side drifts and top drift. It is employed to get through crushed rock in fault zones which may behave like soil. A typical case is shown in Figure 9.

Excavation of a large-size tunnel or underground powerplant sometimes may follow a complicated sequence. Some typical excavation sequences commonly used are illustrated in Figure 10.

In simulating the actual excavation sequence by plane strain conditions, considerable engineering judgment is required. Because of the discontinuities that exist in rock masses and their nonlinear behavior, the construction sequence can have a significant influence on the stresses and deformations in the rock mass.

SUPPORT SYSTEMS

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In order to consider various support systems and their mechanisms, it is first appropriate to review the general concept of the function of a support system. When a support system is installed, the stability problem becomes complex and involves rock-support interaction. The stress redistribution and the rock-support interaction will depend on the flexibility of the support system. Deere, et al. (1969) have presented a schematic relationship shown in

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Figure 11 between the deformation in the rock, the time of installation, and stiffness of the support system. This relationship has been called the ground reaction curve. Certain basic concepts in the functioning of a support system can be explained on the basis of this curve. (i) If a support system is installed in time before the loosening of the rock occurs and it is so stiff that no yielding will occur in the support, the support system will be subjected to the initial stresses in the rock existing before the excavation is made. In reality, this case seldom occurs, because after the excavation and before a support system can be installed, the surrounding rock would have undergone some movements and redistribution of stresses. (ii) For a support installed at point a and with a stiffness represented by a-b, the opening will stabilize when the load on the support system and the radial deformation are represented by point b. (iii) A support with the same stiffness but insufficient load carrying capacity will yield and follow the path a-c-d without stabilizing the opening. (iv) A support that is too flexible will follow the path a-e without stabilizing the opening. (v) A support with a stiffness between a-b and a-e would stabilize the opening but might undergo an intolerable deformation. The true shape of the ground reaction curve is a function of the in-situ properties of the rock, the rocksupport interaction, and the construction procedure.

Mechanisms of Ground Support

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Excavation of an underground opening causes loosening of the rock and a redistribution of stresses in the vicinity of the opening. If the opening is unsupported and the rock in the immediate vicinity of the opening is in an unconfined state, it may be incapable of resisting the increased stresses. If this is the case, gradual loosening of the rock will occur leading to a consequent redistribution of stresses. The loosening zone shifts further inward until the magnitude of the increased stress decreases to a value lower than the strength of the rock. This process of the development of stress-relieved zone around the opening is schematically shown in Figure 12.





The purpose of the ground support is to supply the load-carrying capacity that the rock cannot provide and, thus, help the rock support itself. Because of interlocking and arching, a discontinuous rock mass in which an opening is excavated has a certain strength. Beyond a certain time limit (bridge-action period) and movement, the rock mass may become unstable. For a hard rock, the bridge-action period may be very short and the movement small when the maximum strength develops. The rocksupport system is installed to provide sufficient load-carrying capacity before the bridge-action period expires or excessive movement has occurred. Because each type of support system requires different construction techniques and has different load-deformation characteristics, the ground-support interaction and, thus, the mechanisms of supporting the opening are different. The mechanisms of the ground support for steel sets, rock bolts, shotcrete and concrete liners are briefly described in the following paragraphs.

Steel Sets

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Steel sets are commonly designed on the basis of Terzaghi's rock load concepts and are installed to support the weight of a rock mass that would fall out if unsupported.

A comprehensive discussion of the types, applications, design and construction of steel sets is contained in Proctor and White (1946). The following types of steel support systems have been developed and used for tunnels in rock, Figure 13.

- (a) continuous rib types (leg and rib in one piece)
- (b) rib and post type (arches on posts)
- (c) rib and post wall type (arches on wall plates)
- (d) rib wall plate and post type (arches on wall plates and posts)
- (e) full-circle rib type



Every one of the steel supports listed above consists of two or more different elements. These elements include the ribs, posts, wall plates, bracing and lagging, crown bars and truss panels. The functions of these elements are briefly described in the following paragraphs.

The rib, rib and post or rib, post and invert strut form a frame placed at right angles to the axis of the tunnel. The frames serve to receive the load and to transmit it to footings or to carry it by ring action as in full-circle ribs.

The wall plates serve as sills for the ribs. They transmit the load from the ribs through blocks or posts onto the rock. The lagging bridges the space between the ribs and is in direct contact with the rock. Thus, it transmits rock load to the ribs. The bracing is required to prevent buckling or shifting of ribs or posts.

The crown bars are located in the crown of the tunnel, parallel to the tunnel axis. After blasting and ventilating, they can rapidly be slipped forward, to support the newly exposed roof by cantilever action beyond the ribs. They may also be used to support the roof temporarily while the bench is being taken out.

The truss panels serve a function similar to the latter function of the crown bars. They are located at the spring line and constitute a temporary support for the ribs while taking out the bench, and are to be replaced by posts in the final stage of erection.

The steel sets are generally installed several feet behind the face of a tunnel and are spaced from two to eight feet on centers depending on the type of ribs and rock conditions. Because of construction techniques and structural flexibility, a steel support, in general, involves more rock loosening than rock bolting

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and shotcreting. However, most supports are installed before the rock in the roof loosens all the way back to a stable arch i.e., before the bridge-action period expires. The load actually carried by the supports depends on the time the supports are installed and the amount of additional loosening that takes place after installation of the supports. This additional loosening depends on the type and quality of the support. Figure 14 shows that a typical support load varies with the rigidity of the support itself. Determination of support loads and, thus, the stability of the rock support system are very complicated because of the difficulty of modelling rock-support interaction.

Rock Bolts

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Unlike steel sets, rock bolts and shotcrete are installed to help the rock support itself. Rock bolts can be installed at the working face directly after blasting and within a short time can exert a stabilizing pressure on the loosened rock surface. This early installation prevents the gradual relaxation or loosening of the decompression zone behind the new rock face.

The essential components of a rock bolt are the shank, the anchorage and the bearing plate assembly. Rock bolts are generally classified according to the type of anchor as sliding wedge and expansion shell. The process of rock bolting is to insert a shank in a hole drilled in rock and anchor the bolt in the bottom of the hole. The bolt is placed in tension between the anchor and the plate, thereby exerting a compressive force on the rock. The rock bolt is different from anchor bars which are grouted into holes in rock, but which are not prestressed.

The possible mechanisms of a rock bolt system in maintaining stability of an opening can be represented by the following two concepts.



(a) Rock Support Concept - Rock bolts are used to secure loose joint blocks to solid ground to prevent the blocks from falling from the roof of the tunnel or spalling along the sidewall. Rock bolts may be placed in a horizontally stratified rock and spaced so that their combined strength is equal to the dead weight of the strata that would tend to fall. This concept of rock supporting may be called suspension. This type of support may be achieved by ungrouted, untensioned rock anchors or continuously grouted, untensioned reinforcing rods.

(b) Rock Reinforcement Concept - In this case, the purpose of the rock bolt is to confine the rock so that it will become a part of the total structure supporting the opening. This concept has been used to install the bolts in stratified rocks to bind the various strata together to act as a single beam capable of supporting itself and the overlying rock across the opening. In this case, the rock bolts are assumed to increase the friction and, thereby, prevent slippage between the beds, hence, forcing them to act as a beam. Extensive research has been done by Panek (1956a, 1956b, 1964) for design of bolting for a stratified roof. A typical bolting system is illustrated in Figure 15.

In the case of a fractured, jointed rock, when used in appropriate patterns, the bolts create a principal compressive stress normal to the free surface of the opening; and this, in turn, creates a zone of rock which acts as a structural membrane capable of providing its own support (Lang 1961). A schematic diagram illustrating the action of rock bolts on the rock around an excavation is shown in Figure 16. Figure 17 shows a typical pattern for rock bolts and its effect on the zone of the stressed membrane surrounding an opening.







Shotcrete may be defined as follows (Lorman 1968):

Mortar or concrete that has been conveyed (by regulated air pressure or by positive displacement pump or screw) through a hose and discharged through a nozzle (usually hand held) at high velocity into a suitably prepared inflexible surface; the product, which has been premixed either dry (water added at the nozzle) or wet (water added prior to entry into the hose), is sufficiently stiff at impaction to support itself without sagging from an overhead surface or sloughing from a vertical surface.

Basically, fine shotcrete is mortar, and coarse aggregate shotcrete is concrete. Engineering properties of coarse aggregate shotcrete at age 28 days are similar to concrete (Lorman 1968).

The purpose of using shotcrete for ground support is to maintain the equilibrium and self-supporting capabilities of the rock surrounding the opening. Deere, et al. (1969) present a comprehensive discussion on the use of shotcrete for ground support. A layer of shotcrete is usually applied to a tunnel wall shortly after blasting. It provides continuous resistance to tunnel wall deformations. Several qualitative hypotheses for the mechanism of shotcreting support in a rock excavation have been suggested e.g., Alberta (1963, 1965):

- (a) Shotcrete is forced into open joints, fissures, and seams and, in this way, serves the same binding function as mortar in a stone wall.
- (b) Shotcrete hinders water seepage from joints and seams in the rock and, thereby, prevents piping of joint filling materials and air and water deterioration of the rock.

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- (c) Shotcrete's adhesion to the rock surface and its own shear strength provide a considerable resistance to the fall of loose rock blocks from the roof of a tunnel.
- (d) A thicker shotcrete layer (15 to 25 centimeters) provides structural support, either as a closed ring or a fixed arch-type member.

The loads on a shotcrete liner are a function of the type and condition of the rock, the time of installation, rigidity of the support, and the interaction between the rock and the support.

Concrete Lining

Precast-concrete segments are commonly used for the support tunnels in soft ground. Except in a pressure tunnel, a concrete lining is used as a second or permanent liner of a tunnel in hard rock either to protect the first or temporary liner e.g., steel sets, rock bolts or shotcrete or to meet a secondary requirement such as improving the aesthetics, the acoustics or the aerodynamic flow properties of the tunnel. In this case, only the first liner is designed to support the total expected load. If a concrete lining is expected to carry some rock loads, its idealization is similar to that of shotcrete linings.

Current Design Techniques for Ground Support Systems

The purpose of reviewing the current design techniques is to establish how ground support systems are currently being modelled. Szechy (1967) and Deere, et al. (1969) discuss current design techniques for ground support systems. The current design techniques may be summarized as follows:

(1) Analysis of Unlined Openings - In this approach, the rock is considered as a continuum and the stresses and deformation around an unlined opening are investigated on the basis of an elastic or elastic-plastic analysis. Based on these analyses, the rock pressure on the support system is estimated.

(2) Rock Load Concept - The rock mass that is considered likely to fall if the opening is unsupported is determined. The weight of this rock mass is assumed to be the load that is to be carried by the support system. Basically, this is an empirical approach and does not consider rock support interaction. A typical example of this is Terzaghi's rock load theory.

(3) Support-Rock Interaction - Methods of analysis to account for effects of support-rock interaction on tunnel linings have been reported by Szechy (1967). Recently, Dixon (1971) has presented a similar technique to consider supportrock interaction in the analysis of tunnel support systems. This approach idealizes the rock mass with the Winkler-type foundation. Because of the limitations of the Winkler-type foundation in modelling the behavior of rock masses, this model is not considered to be realistic.

Current methods of tunnel lining and other support systems design tend to consider the estimate of rock load and the design of the structural lining as an independent process. The current design methods for steel sets, rock bolts and shotcrete lining are briefly described in the following paragraphs.

Steel Sets

Selection of the steel set support system depends on the following factors: (1) method of excavation, (2) rock behavior, and (3) size and shape of the tunnel cross-section. Design of steel sets is generally based on Terzaghi's rock load theory. Terzaghi (1946) defines rock load as the height of the mass of rock which tends to drop out of the roof of a tunnel. The magnitude of the rock load depends on the rock quality. Based on his experience on wood-blocked steel sets in tunnels excavated by conventional drilling and blasting techniques, Terzaghi (1946) established certain recommended design load ranges on the lining structure depending on certain rock classes. These are summarized in Table 1.

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ROCK LOAD H_p in feet of rock on roof of support in tunnel

WITH WIDTH B (FT) AND HEIGHT H_t (FT) AT DEPTH OF MORE THAN 1.5 (B + H_t)

(AFTER TERZAGHI, 1946)

Remarks	Light lining, required only if spalling or popping occurs.	Light support. Load may change erratically from point to point.		No side pressure.	Little or no side pressure.	Considerable side pressure. Softening effect of seepage towards bottom of tunnel requires either continuous support for lower ends of ribs or circular ribs.	Heavy side pressure, invert struts required. Circular	ribs are recommended.	Circular ribs required. In extreme cases use yielding support.
Rock Load H _p in feet	zero	0 to 0.5 B	0 to 0.25 B	0.25 B to 0.35 (B + H _t)	(0.35 to 1.10) (B + H _t)	1.10 (B + H _t)	(1.10 to 2.10) (B + H _t)	(2.10 to 4.50) (B + H _t)	Up to 250 ft irrespec- tive of value of (B + H _t)
Rock Condition	1. Hard and intact	 Hard stratified or schistose 	3. Massive, moder- ately jointed	 Moderately blocky and seamy 	5. Very blocky and seamy	<pre>6. Completely crushed but chemically intact</pre>	7. Squeezing rock, moder- ate depth	8. Squeezing rock, great depth	9. Swelling rock

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Rock Bolts

A rock bolt support system is generally selected based on a consideration of the possible modes or mechanisms of failure of the rock around the opening. At present, there is no generally accepted design method.

Panek (1955, 1956a, 1956b, 1956c, 1962a, 1962b, 1964) has conducted an extensive study on design of bolting systems to reinforce laminated roofs. Figure 18 shows a design chart developed by Panek (1956b) for the reinforcement of a laminated horizontal roof on the basis of the development of friction between the layers resulting from the clamping action of tensioned rock bolts. The following factors are considered in the development of this design chart: (a) average bed thickness of mined roof, t_m ; (b) length of bolts, h; (c) bolt tension and anchorage capacity, P; (d) number of bolts per set across the opening, N; (e) spacing of sets, b; (f) width of opening, L; (g) reinforcement factor, RF_t , or percent decrease in strata bending, $\frac{\Delta \varepsilon}{\varepsilon_n fs}$; and (h) coefficient of friction along planes of stratification, F.

Recently, McNiven and Ewoldsen (1969), Ewoldsen and McNiven (1969) and Goodman and Ewoldsen (1970) have attempted to analyze and design a rock bolt support system on a sound theoretical basis. This approach first computes the stress distribution in a rock mass surrounding an opening due to an installation of rock bolt reinforcement. In the stress computation, it is assumed that the rock mass is a linear elastic continuum. Stability along certain prevalent joint sets is examined by comparing shear strength and shear stress along the joint planes. Thus, an optimal design of the rock bolt system is achieved by an iterative process.

Shotcrete

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At the present time, there is no rational design procedure for a shotcrete lining. Selection of the shotcrete support is largely based on experience and is a trial and error process. From the



accumulated experience with the use of shotcrete for underground support, some empirical design guides have been established for support selection. An example of these design guides is presented by Linden (1963), Figure 19. The design should be modified by local experience and geologic conditions. Deere et al. (1969) present a design approach based on structural consideration. This approach assumes that the liner is subjected to a uniform rock load. The desired lining thickness is adjusted to bring the combined thrust and bending stresses below the allowable values. Similar to the other rock support design, this approach does not directly consider the support-rock interaction.

SUMMARY - ESSENTIAL FEATURES TO BE MODELLED

The purpose of this review was to establish the essential features in the excavation techniques, the construction and excavation sequence and the support system that have to be modelled. It is, therefore, appropriate that this summary identifies these essential features.

Excavation Techniques

Excavation of an opening creates some disturbance in a rock mass surrounding the opening. Depending upon the type of excavation methods, e.g., drilling and blasting, smooth wall blasting or boring machine, rock conditions and time of installation of support systems, zones of loosening and fracturing and depths of overbreak around the opening will be different. Generally, the drilling and blasting method causes more disturbance than other types of excavation. It is, therefore, necessary to be able to model the loosened and fractured rock in the vicinity of the opening.

Construction and Excavation Sequence

The time lag that occurs in installing any supports after the rock face has been exposed should be considered. The excavation sequence in which the excavation has many intermediate shapes

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Jneupported Width of Span



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- (A) No support is required (Sound rock).
- (B) Alternatively rock boits on 1.5 2m spacing with wire net, occasionally reinforcement needed only in arch. (Sound, stratified or schistose rock, unstable after long time).
- (C) Aiternatively rock bolts 1 1.5m spacing with wire net, occasionally reinforcement needed only in arch. (Sound, s*ratified or schistose rock, unstable after short time).
- (D) Shotcrete with wire net; alternatively rock bolts on 0.7 im spacing with wire net and 3 cm shotcrete. (Strongly fissured rock, broken).
- (E) Shotcrete with wire net; rock boits on 0.5 1.2m spacing with 3 - 5 cm shotcrete sometimes suitable; alternatively steel arches with lagging. (Fully mechanically disturbed rock, very broken; gravel and sand).
- (F) Shotcrete with wire net and steel arches; alternatively strutted steel arches with lagging and subsequent shotcrete. (Pseudo-sound rock, properties change with time; squeezing).
- (G) Shotcrete and strutted steel arches with lagging. (Heavy squeezing, swelling rock, silt, clay).

FIGURE 19 - ROCK REINFORCEMENT WITH SHOTCRETE (AFTER LINDER, 1963)

before reaching the final shape should be considered. An intermediate shape may be more critical from a stability standpoint, and the stability of the final excavation may depend on the excavation sequence.

Structural Support Schemes

I. Geometry and Rigidity of a Support System

- (a) Steel sets are generally installed as required by local rock conditions at specific spacings which may vary along the length of a tunnel. The spatial distribution and rigidity of steel sets along the length of the tunnel should be approximated in the computational model.
- (b) A tensioned rock bolt exerts some localized threedimensional effects on the stress-deformation of the rock mass in the vicinity of the rock bolt. Effects of bolt tension on the stress-deformation of the rock mass should be modelled. The presence of rock bolts and grouted rock bolts may increase the stiffness of the rock mass after support installation.
- (c) Shotcrete or concrete linings are generally continuous along the tunnel axis. Their geometry and the structural support they provide must be modelled.

IL Support-Rock Connection (Interaction Effects)

(a) Steel Sets - Blockings which transfer loads between the rock and the support are placed at certain convenient discrete points on the steel set. The spatial distribution of blockings may affect the distribution of the bending and axial stresses in the steel set. It is necessary to model the blockings in the analysis.

- (b) Rock Bolts Bearing plates, anchorages and grouting along the rock bolt are the support-rock connections which may require consideration in the idealization of rock bolt systems. Goodman (1966) made a detailed study and concluded that effects of bearing plates are of little importance with respect to stresses more than two feet away from the free surface. This indicates that no appreciable error will result if the loading through bearing plates is approximated by point loads. This conclusion may also apply to anchorages. The grouting may affect the stiffness of the rock mass in the vicinity of the rock bolt.
- (c) Shotcrete or Concrete Linings Grouting or back packing behind a concrete lining should be modelled in analysis.

DEVELOPMENT OF COMPUTATIONAL MODELS

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The computational models have to be formulated within the context of the finite element program developed under Contract No. H0210046. It is, therefore, appropriate to first describe briefly the existing program and its limitations in terms of modelling the excavation technique, the construction and excavation sequence, and the support systems.

BRIEF DESCRIPTION OF EXISTING FINITE ELEMENT PROGRAM The existing finite element computer program which was developed

under Contract No. H0210046 and which will be modified for the present project has capabilities to perform the following analyses under <u>plane strain</u> conditions in addition to a linear elastic analysis.

1. No Tension Analysis - The program is capable of performing a no tension analysis similar to that developed by Zienkiewicz, et al. (1968) and modified by Chang and Nair (1972). A rock may be assumed to be capable of sustaining a limited amount or no tensile stress. This condition may occur due to the presence of numerous cracks and fissures.

2. Joint Perturbation Analysis - A one-dimensional joint formulation similar to that developed by Goodman, Taylor, and Brekke (1968) was used in the program. The joint is assumed incapable of resisting tensile normal stress and has a certain shear strength under a compressive normal stress. The shear strength of a joint is expressed by:

 $\tau_f = C + \sigma_N \tan \phi_e$

where:

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C = cohesion along the joint.

- σ_n = compressive normal stress across the joint.
- 3. Elasto-Plastic Analysis In the elasto-plastic analysis, the rock is assumed to be an elastic perfectly plastic material. The yield function utilized is a generalization of the Mohr-Coulomb hypothesis suggested by Drucker and Prager (1952) and is represented by the following equation:

 $f = \alpha I_1 + \sqrt{J_2} = k$

where:

α and k = material constants, I₁ = first stress invariant, J₂ = second invariant of stress deviation.

The above-mentioned analyses may be performed concurrently depending on the idealization of the actual structure.

LIMITATIONS OF EXISTING PROGRAM

The limitations of the program in modelling excavation techniques, construction and excavation sequence and support systems can be divided into two broad categories: (i) geometry, and (ii) material properties.

Geometry

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The existing program is limited to plane strain problems; therefore, any computational model has to develop idealizations which are compatible with the plane strain assumption. The following paragraphs discuss briefly how this assumption influences the development of computational models for excavation techniques, construction and excavation sequence and support systems.

Excavation Techniques

The modelling of the effects of excavation techniques is not influenced by the geometrical limitations except that the modelling is only valid at a sufficient distance from the actual excavation face. Therefore, the immediate effects of the utilization of a particular excavation technique cannot be modelled.

Construction and Excavation Sequence

The construction and excavation sequence refers to the shape of the openings at various times and the installation of the support systems at various times. Again, the major limitation is that the sequence near the face of the excavation cannot be modelled.

Support Systems

In addition to the limitation of modelling the system at a sufficient distance from the excavation face, there is the additional problem that support systems are in general not continuous. Rock supports using shotcrete or concrete lining may be modelled as continuous supports along the axis of the opening. However, support systems utilizing rock bolts or steel sets would have to be modelled on the basis of various idealizations to fit them within the framework of a plane strain analysis.

Material Properties

The existing program is limited to materials with time-independent properties. The influence of this limitation on the development of a computational model arises from the fact that the excavation, construction sequence and support system installation occurs over a finite time interval. Any time-dependent material response that would occur over this period cannot be directly accounted for.

GENERAL MODELLING CONCEPTS Excavation Techniques

It has been discussed in the previous sections that excavation of an opening creates some disturbance in a rock mass surrounding the opening. Depending upon the excavation technique, e.g., drilling and blasting, smooth wall blasting or boring machine, rock conditions and time of installation of support systems, the zones of loosening and fracturing and depths of overbreak around the opening will be different. Zones of disturbance may be estimated on the basis of experience at locations with similar geologic conditions and excavation methods or determined by seismic refraction surveys in the field.

The essential features that have to be modelled in simulating the effects of excavation techniques are the following:

(i) The stress free excavation face.

Dunlop, Duncan and Seed (1968), Chang and Duncan (1970), Clough and Duncan (1969), and Chang and Nair (1972) have shown that excavation may be simulated in the finite element method by applying stresses to the boundary exposed by excavation so that there is no resultant stress on the excavation face. A similar technique will be used in this study. (ii) The disturbed zone in the vicinity of the excavation. This zone can be modelled by assuming a lower modulus for the material in the zone or by assuming that the material is incapable of carrying any tensile stress. Both these techniques will be utilized in this study.

Construction and Excavation Sequences

The essential features to be modelled and the basic concepts in modelling them are described below:

- (i) The time sequence of construction, including installation of supports.
 Because of the limitation that only time-independent material properties can be included in the program, the time sequence of construction will be modelled in accordance with the following two stage analyses.
 - (a) An initial analysis prior to any support installation will be conducted.
 - (b) A subsequent analysis will be conducted with the support system installation treating the results of the analysis in (a) as the initial condition. In a practical problem, it will be necessary to bracket possible initial conditions.
- (ii) The excavation sequence.

The opening goes through many shapes before reaching the final shape. If the problem could be treated as linear elastic, the final stress distribution would be independent of the excavation sequence; for nonlinear problems, it is necessary to consider the sequence. Excavation sequence will be simulated by removing those elements that will be excavated and ensuring that the excavation face is stress free.

Support Systems

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This development is based on considering the interaction of the support and the surrounding rock mass. The three basic support systems considered in this study, (i) steel sets, (ii) rock bolts, and (iii) concrete and shotcrete liners, are discussed separately.

- Steel Sets A scries of beam elements which are (i) capable of carrying both bending and axial stresses may be used to idealize a steel set. The supportrock connections, i.e., blockings, may be idealized by a one-dimensional or a regular element if the connections are to transfer axial forces or both axial and shear forces. As described previously, this study is confined to analysis of plane problems; and, thus, both the opening and its support system are to be idealized as plane strain problems. It is proposed that the sets along some length of the tunnel be idealized by a continuous support with a section modulus equivalent to the average section modulus of the sets. The blockings are assumed to be continuous along the length of the tunnel. The idealization of the steel sets is illustrated in Figure 20.
- (ii) Rock Bolts Because of the difficulties associated with analysis of a rock bolt system, i.e., the three-dimensional aspect, the interaction of each rock bolt with the rock will not be modelled in this study. The following approximations are proposed to idealize the rock bolt support system:
 - (a) To increase the stiffness of the rock mass in the immediate vicinity of rock bolts to account for the presence of rock bolts and grouted rock bolts.

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- (b) To approximate the effects of tensioned bolts on the rock mass by applying a set of opposite concentrated loads at the anchor and bearing plate. Each concentrated load is considered to be an equivalent line load along the tunnel axis to represent a row of rock bolts. The magnitude of the line load is determined by the bolt tension and the spacing of bolts. This idealization is illustrated in Figure 21.
- (c) Untensioned grouted rock bolts may be idealized as one-dimensional bar elements with material properties similar to those of rock bolts.
- (iii) Shotcrete or Concrete Linings Shotcrete or concrete linings may be idealized as a plane strain structure as shown in Figure 22. Grouting or back packing behind the lining may be modelled in the analysis with materials with different stiffness.

MODIFICATIONS OF THE EXISTING FINITE ELEMENT COMPUTER PROGRAM It has been indicated that the computer program developed under Contract No. H0210048 is to be modified for the present contract to include the capability for modelling and analyzing structural support schemes used in the construction and design of tunnels, and excavation techniques and construction sequences used in underground construction. Before modifications were made for the present contract, two improvements were incorporated into the program. These were (i) utilization of elasto-plastic stress-strain relationship to compute the axial stress, and (ii) updating the element stiffness at each load increment to improve convergence.

Computation of Axial Stress

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Pariseau (1972), in discussing the paper by Chang, Nair and Karwoski (1972), indicates that the equation employed to compute the axial stress for an elasto-plastic analysis is only valid for a rigid, perfectly plastic material. Re-examination of the formulation





of the analysis appears to indicate that the results of an elastoplastic analysis would be correct only if loading is applied in small increments. For each small load increment, each element is checked to determine if the element behaves elastically or plastically. Under the plane strain conditions for which $\varepsilon_{zz} = 0$, the increment of the axial stress $\Delta \sigma_{zz}$ is computed depending on the condition whether the element behaves elastically or plastically. When an element goes from an elastic to a plastic state in an increment, an intermediate stress, when yielding commences, is found by interpolation. In this manner, either the material is acting elastically or plastically at any one time, and the axial stress is computed accordingly. Therefore, the axial stress σ_{zz} is correctly calculated at every step of the analysis according to the assumptions made in the analysis. A modification which is described in the following section has been made in the program to compute the axial stress σ_{zz} correctly without any restriction on the magnitude of load increments. The modification is described in the subsequent section.

Incremental Stress-Strain Relations

In the elastic range, the strains are related to the stresses by the generalized Hooke's law under plane strain conditions as

$$\begin{cases} \sigma_{x} \\ \sigma_{y} \\ \sigma_{z} \\ \tau_{xy} \end{cases} = [D] \begin{cases} \varepsilon_{x} \\ \varepsilon_{y} \\ \varepsilon_{z} \\ \gamma_{xy} \end{cases}$$
(1)

where the strain-stress matrix is

$$[D] = \frac{E}{(1+\nu)(1-2\nu)} \begin{bmatrix} (1-\nu) & \nu & \nu & 0 \\ \nu & (1-\nu) & \nu & 0 \\ \nu & \nu & (1-\nu) & 0 \\ 0 & 0 & 0 & \frac{(1-2\nu)}{2} \end{bmatrix}$$
(2)

and E is the elastic modulus and v the Poisson's ratio for the linear isotropic elastic material.

In the plastic range, it is assumed that the material behaves perfectly plastically with the yield criteria represented by

$$f = \alpha I_1 + \sqrt{J_2} = k$$
(3)
$$\dot{f} = 0$$
(4)

where: α , k = material constants I_1 = first stress invariant J_2 = second invariant of stress deviation

The total strain rate ε_{ij} may be expressed by

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$$\dot{\epsilon}_{ij} = \dot{\epsilon}_{ij}^{(e)} + \dot{\epsilon}_{ij}^{(p)}$$
(5)

where the elastic strain rate may be computed from the generalized Hooke's law as:

$$\dot{\epsilon}_{ij}^{(e)} = \frac{1+\nu}{E} \dot{\sigma}_{ij} - \frac{\nu}{E} I_1 \delta_{ij} \qquad (6)$$

and the plastic strain rate may be computed from the associated flow rule as:

$$\dot{\epsilon}_{ij}^{(p)} = \dot{\lambda} \frac{\partial f}{\partial \sigma_{ij}} = \dot{\lambda} \left[\alpha \delta_{ij} + \frac{S_{ij}}{2J_2^{\frac{1}{2}}} \right]$$
(7)

where: $\dot{\lambda} = a$ scalar positive function of σ_{ij} and ε_{ij} $\delta_{ij} = Kronecker's delta$ $S_{ij} = stress deviator tensor$
Utilizing the preceding relations, Reyes (1966) developed incremental stress-strain relations for an elastic, perfectly plastic material. These relations can be expressed by:

$$\dot{\sigma}_{ij} = 2G \left[\dot{\epsilon}_{ij} - \frac{\dot{w}}{kp} \left[h_0 \delta_{ij} + \frac{\sigma_{ij}}{2J_2^{l_2}} \right] - \dot{\epsilon}_{kk} \left[h_2 \delta_{ij} + h_1 \sigma_{ij} \right] \right\}$$
(8)

where:
$$p = \frac{J_2^{\frac{1}{2}}}{k} \begin{bmatrix} 1 + 9\alpha^2 \frac{K}{G} \end{bmatrix}$$

 $\dot{w} = \sigma_{ij} \dot{\varepsilon}_{ij}$

for plane strain cases:

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 $\dot{w} = \sigma_{x}\dot{e}_{x} + \sigma_{y}\dot{e}_{y} + \tau_{xy}\dot{\gamma}_{xy}$ K = bulk modulus G = shear modulus $h_{o} = \frac{3K\alpha}{2G} - \frac{I_{1}}{6J_{2}^{\frac{1}{2}}}$ $h_{1} = h_{o} / \left[J_{2}^{\frac{1}{2}} \left(1 + 9\alpha^{2}\frac{K}{G} \right) \right]$ $h_{2} = \frac{2h_{o} \left[\alpha - \frac{I_{1}}{6J_{2}^{\frac{1}{2}}} \right]}{\left(1 + 9\alpha^{2}\frac{K}{G} \right)} - \frac{3\nu Kk}{EJ_{2}^{\frac{1}{2}} \left(1 + 9\alpha^{2}\frac{K}{G} \right)}$

Equation (8) may be expressed in a matrix form as:

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$$\begin{cases} \ddot{\sigma}_{x} \\ \dot{\sigma}_{y} \\ \dot{\sigma}_{z} \\ \dot{\tau}_{xy} \end{cases} = [D]_{e.p.} \begin{cases} \ddot{\epsilon}_{x} \\ \dot{\epsilon}_{y} \\ \dot{\epsilon}_{z} = 0 \\ \dot{\tau}_{xy} \end{cases}$$
where: $[D]_{e.p.} = \begin{bmatrix} D_{11} & D_{12} & D_{13} & D_{14} \\ D_{21} & D_{22} & D_{23} & D_{24} \\ D_{31} & D_{32} & D_{33} & D_{34} \\ D_{41} & D_{42} & D_{43} & D_{44} \end{bmatrix}$

$$D_{11} = 2G \left(1 - h_{2} - 2h_{1}\sigma_{x} - h_{3}\sigma_{x}^{2} \right)$$

$$D_{22} = 2G \left(1 - h_{2} - 2h_{1}\sigma_{y} - h_{3}\sigma_{y}^{2} \right)$$

$$D_{33} = 0$$

$$D_{44} = 2G \left(k_{1} - h_{3}\tau_{xy}^{2} \right)$$

$$D_{12} = D_{21} = -2G \left[h_{2} + h_{1} \left(\sigma_{x} + \sigma_{y} \right) + h_{3}\sigma_{x}\sigma_{y} \right]$$

$$D_{13} = D_{31} = -2G \left[h_{2} + h_{1} \left(\sigma_{x} + \sigma_{z} \right) + h_{3}\sigma_{x}\sigma_{z} \right]$$

$$D_{14} = D_{41} = -2G \left[h_{1}\tau_{xy} + h_{3}\sigma_{x}\tau_{xy} \right]$$

$$D_{23} = D_{32} = -2G \left[h_{2} + h_{1} \left(\sigma_{y} + \sigma_{z} \right) + h_{3}\sigma_{y}\sigma_{z} \right]$$

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(9)

$$D_{24} = D_{42} = -2G \left[h_1 \tau_{xy} + h_3 \sigma_y \tau_{xy} \right]$$
$$D_{34} = D_{43} = -2G \left[h_1 \tau_{xy} + h_3 \sigma_z \tau_{xy} \right]$$
and
$$h_3 = \frac{1}{2J_2 \left(1 + 9\alpha^2 \frac{K}{G} \right)}$$

The strain-stress relation described by equations (1) or (9) has been used in the program to compute the axial stress and to form the stiffness depending whether the element is in the elastic or plastic range.

Updating the Element Stiffnesses

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It has been experienced that in an elasto-plastic analyses, if a constant initial stiffness is used in the initial stress approach, the computing time is greatly reduced for each iteration. However, it has been shown that in this case, the solution convergence is very slow. The program has been modified to improve the rate of the solution convergence. An additional option has been added to the program so that the stiffness of the system may be updated at each new increment of load. It has been found that by doing this, generally 2 to 4 iterations are sufficient at each load increment to ensure that the equilibrium conditions are satisfied.

The technique for performing nonlinear analysis with the above modification is illustrated in Figure 23. This technique may be summarized as follows:

(1) For each increment of load, an initial elastic stiffness is used and the elastic solution is obtained. Using the elastic stiffness for each increment of load may ensure that a correct solution is obtained if the structure is unloaded.

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(2) If the elastic solution indicates that some elements are in yield, excess stresses are computed and redistributed by iterative processes. During the redistribution of excess stresses, a new stiffness updated after the first iteration is used in subsequent iterations.

(3) Step (2) is repeated until the equilibrium conditions are satisfied.

(4) Repeat Steps (1) to (3) for all increments of load.

A flow diagram illustrating the algorithm for the modified elastoplastic analysis is shown in Figure 24. It may be noted that the incremental stress-strain relations described in the previous section have been incorporated in the formulation of the method of analysis.

<u>Modifications of the Computer Program for Modelling Excavation</u> <u>Techniques, Structural Support Schemes and Construction Sequences</u> The general concepts in developing computational models for simulating excavation techniques, structural support schemes, and excavation and construction sequences have been described in the previous sections. The detailed procedure can be summarized as follows:

(1) For illustrative purposes, an underground opening is shown in Figure 25 to be excavated in several stages. The first step in the analysis is to assign values of initial stresses, σ_i , to each element. The initial state of stress may be estimated or determined in the field.

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(2) Read in data describing the current stage of construction, i.e., elements to be excavated, elements situated within disturbed zones, nodal forces for simulating rock bolts installation, and/or elements as a structural support or lining, if any;



FIGURE 24 - MODIFIED STRESS TRANSFER TECHNIQUE FOR ELASTO-PLASTIC ANALYSIS





nodal points along the excavated face which describe the geometry of the current stage of excavation. The elements to be excavated are assigned a small modulus to simulate the existence of a cavity. The elements in the disturbed zones are assigned with a lower modulus or no tensile strength. The elements for structural supports are assigned with appropriate properties corresponding to the material used for the structural supports.

(3) Initial stresses, σ_i , on the boundary exposed by excavation are computed from stresses in the surrounding elements using a technique similar to that used by Clough and Duncan (1969). The detailed procedure has been described in the final report under Contract No. HO210046. To simulate excavation, changes in stress, $\Delta\sigma$, which are equal in magnitude and opposite in sign to the initial stresses, σ_i , are applied to the boundary exposed by excavation.

(4) An initial elastic analysis is conducted. Increments of elastic stresses and strains are computed.

(5) Unbalanced excess stresses are determined and redistributed by iterative processes until the equilibrium conditions are satisfied.

(6) Repeat Steps (2) to (5) for all construction stages.

A flow diagram showing the proposed procedure to simulate excavation techniques, structural support schemes, and excavation and construction sequences is illustrated in Figure 26. The proposed procedure has been used to modify the existing computer program. To verify and illustrate the use of the modified computer program, several example problems were analyzed. The results of the analyses are described in the following section.

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ILLUSTRATIVE PROBLEMS

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Definition of Problems

The following four example problems were analyzed using the modified computer program:

I. Elasto-plastic analysis of a thick-walled circular tube with the Von Mises yield criterion. A closed form solution is available for this case for verification.

II. Elasto-plastic analysis of a circular opening with the generalized Mohr-Coulomb yield criterion. The results are compared with those obtained by Reyes (1966).

III. Elastic analysis of a circular opening by two stages of excavation and gravity turn-on procedures.

IV. Analysis of a circular opening reinforced by rock bolts and a concrete lining.

Problems (I) and (II) were analyzed to show the improved accuracy and rate of the solution convergence as compared with those reported in the final report under Contract No. H0210046. Problem (III) was analyzed to indicate the ability of the computational technique used to simulate excavation sequences. Problem (IV) was analyzed to illustrate capabilities of the modified computer program for simulation of excavation techniques, support installation and construction sequences.

Results

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I. Elasto-plastic Analysis of a Thick-walled Circular Tube Subject to Internal Pressure

The dimensions of the rube, the material properties and the finite element idealization of the problem are shown in Figure 27. The results of the analysis, together with the closed form solution



obtained by Prager and Hodge (1951) are shown in Figures 28 through 31. Comparison between the results obtained from the finite element analysis and those from the closed form solution indicates good agreement.

II. Elasto-plastic Analysis of a Circular Opening with the Generlized Mohr-Coulomb Yield Criterion

The finite element idealization together with the definitions of the problem is shown on Figure 32. The analysis was conducted by applying pressures on the cavity face. The boundary pressures were applied in five increments. It should be noted that only two to four iterations were required for each increment of load for solution convergence, indicating improved rates of solution convergence obtained by updating the stiffness, the additional option added to the existing program. The results of the analysis together with those obtained by Reyes (1966) are shown in Figures 33 and 34.

III. Elastic Analysis of a Circular Opening by Two-Stage Excavation and Gravity Turn-on Procedures

The finite element idealization of a circular opening 20 feet in diameter is shown on Figure 35. The elastic stress distribution was obtained by a two-stage excavation procedure. The initial state of stress was obtained by the gravity turn-on procedure. The first-stage excavation of a 10-foot-diameter cavity was conducted using the proposed technique for simulating excavation. After the elastic stress distribution for the firststage excavation was obtained, the remaining rock was removed by the second-stage excavation. The elastic stress distribution obtained by the two-stage excavation procedure is compared with the one-step gravity turn-on procedure as shown in Figure 36. It may be noted that the virtually identical stress distribution was obtained by both procedures indicating that the proposed technique for simulating excavation is accurate enough for engineering purposes.

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IV. Analysis of a Circular Opening Reinforced by Rock Bolts and a Concrete Lining

The assumed construction sequences of the opening analyzed is shown in Figure 37. It is assumed that the opening is to be excavated full face, followed by installation of a set of rock bolts. At the final stage of construction, a concrete liner, 1 foot thick, is installed. The opening, 10 feet in diameter. is assumed to be situated in a rock mass under an initial stress field which consists of a vertical stress of 1000 psi and a horizontal stress of 400 psi. The finite element idealization of the problem is shown in Figure 38. Sixteen sets of rock bolts are installed. Each set is tensioned to 28,300 pounds per linear foot along the tunnel axis equivalent to 100 psi compressive stress applied to the cavity face. The analysis was conducted in accordance with the following procedure: (1) an elastic analysis of the structure subjected to boundary pressures simulating excavation and installation of rock bolts was first performed; (2) a concrete liner was then "installed." The results of analysis obtained from Step (1) was considered as an initial condition in the subsequent analyses in which excess stresses were redistributed. The results of the analysis, as shown in terms of the stress distribution in both the concrete liner and the rock surrounding the opening, is illustrated in Figure 39. For the purpose of comparison, the results of the analysis on the unsupported opening obtained in Problem (II) are also shown in Figure 39. The difference in the stress distribution obtained in Problems (II) and (IV) is due to the installation of the rock bolts and the concrete liner.





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EVALUATION OF ANALYTICAL METHOD (COMPUTER PROGRAM) - CASE HISTORY STUDIES

To evaluate the capabilities and reliability and illustrate the use of the computer code developed, studies were made on a number of well-documented model tests and case histories of underground openings. These include the analysis of model tests on lined and unlined openings in jointed rock, the analysis of Tumut I Underground Power Station, and a rock tunnel of Washington D.C. Metro. Analyses of these case history studies are described in the following sections.

ANALYSIS OF LABORATORY MODEL OF LINED AND UNLINED OPENINGS IN JOINTED ROCK

Description of Model Study

Hendron, et al. (1972) conducted a series of model tests on lined openings in jointed rock fabricated by a rock-like material. One of these models analyzed in this study is shown in Fig. 40. The joint blocks used to construct the model were made by sawing them out of larger compacted blocks. The material used was a water/plastic/sand mixture and was the same as that used by Heuer and Hendron (1969) in model tests of unlined openings in solid blocks. The model analyzed in this study was constructed with a 2-inch joint spacing in two mutually perpendicular directions at 45° to the principal loading directions. A 4-inch-diameter opening was cored after the model was constructed in the testing machine and a seating load of about 25 psi was applied in both the vertical and horizontal directions. The 0.035-inch-thick aluminum liner was then installed in the opening and grouted in place using a liquid grout consisting of one part water to one part sulfaset rock bolt cement by weight. The model was tested at a principal stress ratio $\sigma_{\rm H}/\sigma_{\rm V}$ = 2/3 to a maximum vertical model pressure of 1300 psi under plane strain conditions. The model was instrumented with eight pairs of buried extensometers and six diametrical extensometers in the tunnel liner as shown in Fig 41.





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Fig. 41 Locations of Extensometers in Jointed Test Blocks (After Hendron et al., 1972)

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Behavior of Model

The average stress-strain curves of the model obtained from the buried extensometers are shown in Fig. 42. The average strains represent the strains of the total model block. Both the vertical and horizontal strains are compressive. The vertacal strain is approximately three times larger than the horizontal strain. The liner buckled at a vertical pressure of about 1100 psi. The buckling of the liner is reflected in the average stress-strain curves of the block as a sharp deviation from linearity at a pressure of about 1100 psi.

The diametrical strains measured by the six diametrical extensometers are plotted in Fig. 43 as a function of the vertical model pressure. Buckling of the liner is clearly shown at a vertical pressure of about 1100 psi at which the diametrical strains increased at greater rates. A photograph of the jointed block after test is shown in Fig. 44. It may be seen that the actual buckling occurred as a pair of buckles located along the 45° diametrical plane which coincided with the intersection of a joint plane with the tunnel liner.

Analysis of Model Study

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Idealization of the Model - The finite element idealization of the jointed model with a lined opening is shown in Fig. 45. The joints were idealized by one-dimensional joint elements, and the rock blocks were idealized by one or several twodimensional elements. Because of the variation in the size of blocks and the difficulty involved in the assemblage of the model, the joint blocks of the actual model were not separated by continuous straight joints. For the idealization necessary for the analysis, the joints had to be assumed as straight and continuous.



Measured and Computed Average Stress-Strain Curves of Model Test on Joint Block with Lined Opening Fig. 42

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Measured and Computed Diametrical Strains of Liner as a Function of Vertical Applied Pressure - Case B Fig. 43

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(a) View of whole model after test



(b) Closeup of tunnel liner after test (photograph taken from the other side)

Fig. 44 Photographs of Jointed Block After Test (After Hendron et al., 1972)

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Thickness of liner not in scale.

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Fig. 45 Finite Element Idealization of Jointed Model

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Material Properties Used in the Analysis - The material properties of the intact block used in the model were selected on the basis of results obtained from a series of triaxial tests conducted by Heuer and Hendron (1971), and Hendron et al. (1972). The Mohr envelope of the rock-like material used is shown in Fig. 46. The strength parameters were determined to be c = 170psi, $\phi = 32.5$ degrees, and the tensile strength of 33 psi. The average value of the modulus was determined to be 833,000 psi and the Poisson's ratio to be 0.14.

The aluminum liner was assigned the modulus of 10^7 psi and the Poisson's ratio of 0.33. The aluminum was assumed to follow the Von Mises yield criterion with the tensile and compressive strength of 40,000 psi.

As described previously, the joint blocks were sawed from larger compacted blocks. The deformability of the joints which consists of the normal and shear stiffnesses depends on the roughness of the sawed surface. No test data were available for evaluation of the deformability of the joints. The angle of shearing resistance on the joint surfaces was obtained by Hendron, et al. (1972) from a series of direct shear tests. The results of these tests are shown in Fig. 47. The effective angle of shearing resistance decreases from 33° to 29° with increasing normal pressures. The effective angle of shearing resistance of the joint surfaces used in the analysis was selected to be 29°.

Table 2 summarizes the material properties except the deformability of the joints used in the analysis of the model test.

Selection of Joint Deformation Characteristics - A parametric study was conducted assuming various combinations of both normal



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Summary of Material Properties Used in the Analyses Table 2.

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of Model Test on Joint Block

Material	Modulus psi	Poisson's Ratio	C psi	¢ deg.	Tensile Strength psi
Intact Block	833,000	0.14	170	32.5	33
Aluminum Liner	10,000,000	0.33	20,000	0	40,000
Joint	:	-	0	29.0	0

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and shear stiffnesses in order to select a reasonable set of the joint deformability characteristics for the detailed analysis. A total of 13 cases were analyzed. The normal stiffness was varied from 2.0×10^4 pci to 4.17×10^7 pci and the shear stiffness was varied from 4.0×10^3 pci to 1.5×10^4 pci. The results of the parametric study in terms of the average model strains and the diametrical strains of the liner at the vertical model pressure of 1000 psi are summarized in Table 3.

From the results of the parametric study, the deformability of the joints which would provide magnitudes of both vertical and horizontal strains similar to those observed at the applied vertical pressure of 1000 psi was selected for the detailed analysis. The normal and shear stiffnesses of the joints selected were 3.5×10^4 pci and 1.5×10^4 pci, respectively. The magnitudes of these joint stiffnesses were later found to be reasonable and compatible with the deformability of various rock joints compiled by Goodman (1969).

Results of Analysis - The following three cases were analyzed: Case A assumed that the liner continued to remain intact with the joint block at a vertical pressure greater than 1100 psi; Case B assumed that the liner buckled at the vertical pressure of 1100 psi and would not take any load at greater pressures; Case C analyzed the unlined cavity.

The results of these analyses are presented in Figs. 42, 43, 48, 49, 50 and 51. Fig. 42 shows the computed and measured average and horizontal strains as a function of the applied vertical pressure. For both Cases A and B, the computed and measured strains are in good agreement up to a vertical pressure of about 1200 psi at which point the cavity elongated in the horizontal direction due to buckling of the liner. Fig. 43

			**Averas	ge Strains in/in	**Dia	netrical Si µ in	trains of I /in	iner	× ×
Case	K _N PCI	KS PCI	Vertical	Horizontal	θ = 15°	$\theta = 45^{\circ}$	θ = 75°	$\theta = -45^{\circ}$	
1	4.17x10 ⁷	4.0x10 ³	19,700	-18,200	9,700	-2,100	- 5,600	3,200	Ď
2	4.17×10 ⁷	8.0x10 ³	10,700	- 9,200	7,400	- 760	- 3,300	2,900	
S	4.17×10 ⁶	4.0x10 ³	19,900	-18,300	10,100	-2,160	- 5,700	3,380	
4	4.17x10 ⁵	4.0x10 ³	22,000	-19,000	16,300	-4,800	-10,200	4,900	
S	4.17x10 ⁵	5.0x10 ³	18,100	-15,000	14,000	-3,050	- 8,100	4,400	
9	8.0x10 ⁴	5.0x10 ³	22,800	-10,800	13,800	570	- 7,600	3,600	$\sigma_{\rm v}$ = 1,000 psi
7	4.17x10 ⁴	5.0x10 ³	27,900	- 6,600	19,800	3,700	- 9,500	2,700	
80	3.0x10 ⁴	1.0×10 ⁴	22,900	4,900	17,700	4,400	- 5,900	2,200	$\sigma_{h} = \frac{2}{3} \sigma_{v}$
6	3.0x10 ⁴	1.3×10 ⁴	20,900	5,200	16,400	4,600	- 4,600	2,250	
10	2.5x10 ⁴	1.3x10 ⁴	23,500	9,200	17,700	5,300	- 5,000	1,900	
11	2.0x10 ⁴	1.2x10 ⁴	28,000	12,400	19,900	6,300	- 5,900	1,300	
12	3.0x10 ⁴	1.5x10 ⁴	20,100	7,550	15,800	4,650	- 4,000	2,290	
***13	3.5x10 ⁴	1.5x10 ⁴	18,200	5,810	14,800	4,090	- 3,750	2,540	
*Measur	ed Strains	= 2 2	17,880	5,940	θ = 0° 22,000	0 = 45° 11,000	θ = 70° 0	0 = -45° 5,000	
~ ^	h	n 3 ^v			$\theta = 20^{\circ}$ 18,000		θ = 90° -10,000		

Table 3. Summary of Parametric Study of Model Test on Jointed Block

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*After Hendron, et al. 1972
**Compression = +
Extension = ***Joint stiffness used in the detailed analysis

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Fig. 48 Development of Yielded Zones in Liner



Fig. 49 Relative Tangential Displacements Across Joints in the Vicinity of Opening at Vertical Stress of 1100 psi

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Computed Average Stress-Strain Curves of a Jointed Model With an Unlined Opening 50 Fig.

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Computed Diametrical Strains of an Unlined Opening of a Jointed Model 51 Fig.

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shows the computed diametrical strains obtained from the analysis of Case B together with the measured strains at various locations along the liner. Generally, the magnitudes of the computed strains are in reasonable agreement with those measured at their respective locations along the liner. However, the rate of increase in the measured diametrical strain is greater than those computed at vertical pressures greater than 1100 psi.

Fig. 48 illustrates the propagation of computed plastic zones in the model as well as the liner with an increase in the applied pressure. The plastic zones are confined to the liner and the immediate vicinity of the opening. It is interesting to note that at the vertical pressure of 1100 psi, the plastic zones appear to propagate over the entire liner, a result consistent with the observed buckling of the liner at the same applied pressure.

To examine the cause of buckling of the liner which occurred along the 45° diametrical plane (MN) as shown in Fig. 44, relative tangential displacements across the joints in the vicinity of the opening at the applied vertical pressure of 1100 psi are plotted in Fig. 49. It may be noted that the relative tangential displacements across the joint along the 45° diametrical plane AA' increased from 0.01 inch at the locations away from the opening to 0.02 inch at the intersection of the joint and the liner, indicating that the joint plane was penetrating the liner at the location where the buckling of the liner occurred.

The results of the analysis on the unlined opening (Case C) are shown in Figs. 50 and 51. The comparison between the average model strains of the lined and unlined openings indicates that the liner has an insignificant effect on the average strains of the models. However, the comparison between the diametrical strains computed for the unlined opening shown in Fig. 51 and those for the lined opening shown in Fig. 43, indicates that

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the liner has a large effect in restraining the inward movements of the opening. Also shown in Fig. 51 are the diametrical strains measured after the liner buckled in the model test described in the previous section. It may be noted that at the vertical pressure of 1300 psi, the computed diametrical strains are on the same order of magnitude as those measured after the liner buckled, indicating that the behavior of the opening after. the liner failed could be predicted by analyzing the opening with no liner.

Summary

The results of the analyses of the laboratory model of the lined opening in jointed rock conducted by Hendron et al. (1972) indicate that the behavior of the model is greatly affected by the deformability of the joints expressed in terms of the normal and shear stiffnesses. Although no data were available to determine the deformability of the joints, it was possible through an iterative process to determine joint stiffnesses which would provide a reasonable agreement between the computed and measured deformabilities of the model. Using these joint stiffnesses, the behavior of the lined opening up to the buckling of the liner could be predicted with reasonable accuracy. The discrepancy between the computed and measured diametrical strains may be attributed to the approximations involved in the idealization of the actual jointed model and the interaction of the liner and the jointed blocks in the vicinity of the opening.

A comparison of the results of the analyses of the lined and unlined openings showed that the liner had a significant influence in restraining the inward movement of the opening. It was also found that the behavior of the lined opening after the failure of the liner could be predicted from an analysis of the unlined opening. ANALYSIS OF TUMUT I UNDERGROUND POWER STATION, SNOWY MOUNTAINS, AUSTRALIA

Description and Geological Structure of the Site The Tumut I underground power station (Moye, 1964) is situated under the lower part of the very steep eastern wall of the Tumut Valley in the Snowy Mountains of southeast Australia, about 1100 feet vertically below the ground surface, 1200 feet in from the river, and 150 feet below the level of the river bed. The plan of the power station is shown in Fig. 52. The machine hall is 306 feet in length, 44 feet in maximum width, and 104 feet in maximum height.

The Tumut I power station is located in a complex mass of granitic parogneiss and granulite intruded by sheets of granites. The group of metamorphic rocks is referred to as Boomerang Creek granitic gneiss, and the granites as Happy Valley granite. The granite sheets strike N65°E to N100°E and dip 40°-50° SE. Their distribution at power station level is shown in Fig. 52.

At Tumut I power station site, two small but persistent minor faults intersect the machine hall. One is over the full length of the roof (Fig. 52, A). It strikes N40°E to N60°E and dips approximately 35°SE. In the granite, it is seen as one or a group of several persistent fracture planes with 1/2 to 1 inch of crushed granite containing a little clay along the planes, or as a zone of close jointing. In the gneiss, it is represented by a zone of close jointing 5-10 feet wide, with joints spaced 2-6 inches apart. These joints are usually smooth, coated with chlorite but not clay, slickensided, and tightly closed. The second small fault has a strike of N30°E and dips It cuts across the tailrace surge chamber, draft 60°-70°W. tubes, and the western end of the machine hall (Fig. 52, B). In the granite it usually consists of one or two fracture planes with 1/4 to 1 inch of clay and crushed granite along the planes. As the contact with the gneiss is approached, it



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Fig. 52 Plan and Sections of the Tumut I Power Station

becomes less distinct and splits into several parallel <u>clay</u>-<u>coated joints</u>, many without crushed rock, and continues in the gneiss as a group of clay-coated joints.

In addition to these minor faults, there is a very persistent zone of close fracturing a few inches in width, which occurs in the lower part of the power station walls, and in the walls of the transformer hall (Fig. 52, D). This zone has been found only in the granite. It has a roughly north-south strike and a gentle dip to the east.

In addition to these well-defined localized structures the rock mass is extensively jointed. The joint pattern is similar in both rock types, but the spacing of the joints is usually much closer in the gneiss than in the granite. Most joints can be grouped into the following three principal sets (Fig. 52, a, b, c):

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Set a: Strike N40°-60°E and dip 35°SE. These are parallel to fault A.

Set b: Strike N30°E and dip 65°W to 80°E. The strike of these joints makes a small acute angle with the long walls of the machine hall.

Set c: Strike N130°E and dip 80°W. These joints are spaced 40-80 feet apart but are very persistent. A single joint may split into two or more closely spaced joints. The joint surfaces are rough and irregular. The strike of these joints is nearly at right angles to the long walls of the machine hall.

In the gneiss the spacing of the joints of sets a and b is generally 6 inches to 2 feet with some areas of narrower and some of wider spacing. The joint surfaces are usually smooth and slickensided. Most joints are tightly closed. In the granite, the spacing of the joints of sets a and b is variable but generally in the range of 1 to 5 feet.

Construction Sequences and Behavior of the Excavations

The machine hall was excavated in several stages. The detail of excavation sequences is shown in Fig. 53. After the pilot tunnel was driven, the roof section of the machine hall was excavated to full width, rock bolts and permanent concrete ribs installed. Following this, the main body of the machine hall was excavated by quarrying methods. The vertical walls and roof were systematically rock-bolted as soon as they were exposed (Moye, 1964; Lang, 1958). The rock bolts used consisted of mild steel bars 1 inch in diameter, mostly 10 or 15 feet long, with a slot-and-wedge-type anchor and furnished with 6-inch- or 8-inch-square steel plates for bearing against the rock surface. They were spaced 4 or 5 feet apart. During installation, they were stressed to a nominal load of 20,000 pounds tension. The concrete ribs were of 4 feet x 4 feet cross-section, with a spacing between ribs of 8 feet over onehalf of the hall and a spacing of 4 feet over the other half, where the rock was more jointed. During excavation, overbreak to the extent of 1 to 3 feet was common under the effects of blasting. On the upstream wall rather extensive loosening of the granite joint blocks occurred. This loosening apparently was influenced by the zone of close jointing along fault A in the middle of the wall being intersected by joints of set b dipping steeply toward the excavation.

The behavior of the rock mass around the machine hall excavation was observed during construction by the following quantitative instrumental measurements:

 (a) The strain in many of the reinforced concrete arch ribs was measured by means of electric resistance-type



strain meters embedded in the concrete, and by observation of Huggenberger deformeter points fixed on the surface of some ribs.

- (b) The horizontal movement of points at the ends of the concrete ribs and on the rock walls was measured by precise survey methods.
- (c) The angular rotation of points on the reinforced concrete abutment beams and on the walls was measured by means of sensitive clinometers.

The data obtained from the instrumental measurements were summarized by Alexander, et al. (1963) and shown in Fig. 54. At Rib No. 15, the strains developed in the roof rib one year after the excavation was complete were 800 μ in./in. at the downstream side. The abutment deflections at RL 2746 developed in the 5-month period after the excavation was completed were 0.3 inch at the downstream side and 0.07 inch at the upstream side. Both sides of the abutment moved towards the center of the hall. It may be noted that the initial measurements of the reference points were made after the excavation was complete. Therefore, the movements which occurred during excavation were not recorded. While the instrumental data presented in Fig. 54 were not sufficient to give a complete picture of the behavior of the excavation, certain trends are recognizable. Significant features of the behavior of the excavation are summarized below:

(1) The movements due to excavation were much larger on the downstream side of the machine hall. This behavior was manifested by large strains and deflections measured on the downstream side of the concrete ribs and the rock walls as compared with small movements observed on the upstream side. The asymmetrical behavior of the



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Fig. 54 Tumut I Power Stations--Observations on Ribs and Abutments (After Alexander et al. 1963)

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machine hall may be attributed to topographic effects and the existance of the two intersecting minor faults and joints near the downstream end.

(2) Severe cracking was observed in the concrete abutment beams on which the roof ribs were supported and spalling noted in a number of ribs in locations adjacent to both upstream and downstream abutments, the spalling being more severe at the downstream end. It is interesting to note that the cracking was first noticed when the excavation was nearing completion and grew progressively worse until the excavation was complete, after which no further worsening was noticed. This appears to indicate that the construction sequence had definite effects on the behavior of the support and excavation.

Idealization of the Power Station Excavation

Finite Element Idealization - For the purpose of analysis, a cross-section through the roof Rib Nc. 15 shown in Fig. 54 was selected. A finite element idealization of the section is shown in Fig. 55. Because the power station is situated at a depth greater than 1100 feet below the ground surface, it can be assumed that the presence of the ground surface has a negligible effect on the behavior of the excavation. For this reason, the boundaries of the finite element mesh were assumed fixed against any movements. The essential feature in the idealization is the presence of two faults, A and B. These faults are sub-parallel to the axis of the excavation. Therefore, the plane strain assumption of these geologic features should not incur serious errors in the analysis. The faults were idealized with Goodman's one-dimensional joints. To simulate actual excavation sequences (shown in Fig. 53) a simplified 4-stage excavation as shown in Fig. 56 was employed in the analysis. The concrete rib of 4 feet x 4 feet cross-section with spacing between ribs of 8 feet was idealized as a 2.8-footthick continuous concrete arch with the same section modulus. The effect of patterned rock-bolting in the roof and vertical walls was simulated by applying an equivalent pressure of 7 psi to the excavated face and the interior of the rock mass along rock anchors. The pressure was applied when the excavation was made.

Initial State of Stress - Stress measurements were made at one of the machine halls of Tumut I when the power station excavation was well advanced (Alexander, et al. 1963). The measured stresses were corrected by the stress-concentration factors estimated at the test sites. The initial state of stress at the springline of Tumut I was computed to be:

vertical stress σ_v = 1800 psi horizontal stress σ_h = 1500 psi shear stress τ_{vh} = 250 psi

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Because Tumut I is situated below a steeply sloping wall of the Tumut Valley, it was considered reasonable to assume that shear stresses and high horizontal stress would exist at the site.

In the analysis of Tumut I power station, the initial state of stress in the rock mass was computed in accordance with the following procedure: (1) the vertical stress in the rock mass was calculated by applying correction due to gravity to the assumed vertical stress of 1800 psi at the springline; (2) the horizontal stress was computed by multiplying the vertical stress by 0.83, the ratio of the horizontal to vertical stress at the springline; and (3) the shear stress was assumed constant throughout the rock mass.

Material Properties - The rock present at the section of interest is predominantly Happy Valley Granite. The strength and elastic properties of the rock were measured from a series of triaxial tests on pieces of drill cores free from visible joints or other defects and are summarized in Table 4. In general, because of the presence of joints and fractures, the moduli of a rock mass are much less than those determined on small intact rock specimens. For the purpose of analysis, a lower value of modulus, as summarized in Table 4, was used.

Both faults A and B were idealized by one-dimensional joint elements. The properties of these faults were approximated by the normal and shear joint stiffnesses (Goodman, 1969) which are functions of normal and tangential deformability of the faults and the thickness of the fractured zones. No data was available for evaluation of the normal and shear stiffnesses. However, fault "B" appears to be more deformable than "A" because of the presence of clay and clay-coated joints in "B". A number of sets of joint stiffness was utilized to parametrically study the influence of the deformability of the faults on the behavior of the excavation. The values which provided a good agreement between the observed and computed strains in the concrete rib are summarized in Table 4.

Analysis Procedures

To study the behavior of the machine hall excavation, a fourstage construction and excavation sequence as shown in Fig. 56 was simulated in the analysis. The initial state of stress before excavation was first calculated for each element. Nodal forces to simulate excavation and rock-bolting, if any, were computed, and a linear elastic analysis was conduced at each excavation stage. Additional iterative analyses were performed to redistribute any excess stresses if two-dimensional elements yielded or failed in tension, or joint elements failed in shear or tension. The stress, strain, and deformation components due to each stage of excavation were cumulated in accordance

Table 4 Rock Properties at Tumut 1 Underground Power Station

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A. Happy Valley Granite (Moye, 1964)

	Values Obtained from Tests	Values Used in Analysis
Young's Modulus, psi	6 to 10 x 10 ⁶	3 x 10 ⁶
Poisson's Ratio	0.16 to 0.21	0.18
C ^{**} , psi	4,000	4,000
¢**, deg.	44	44
Tensile Strength, psi	500 to 1,500	500
y pcf	165	165

B. Faults "A" and "B" (Assumed)

Fault	Normal Stiffness pcf	Shear Stiffness pcf	C psi	¢ degree
A	1×10^{7}	5 x 10 ⁶	0	35
B	1 x 10 ⁶	5 x 10 ⁵	0	27

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with the appropriate sequences. In this case study, the concrete ribs were installed after roof excavation, and only the subsequent excavations caused stresses and strains to develop in the roof ribs. Following the actual construction sequence, the sequential stress and strain developed in the rock mass and supports could automatically be accounted for.

Presentation and Discussion of Results

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The results of the analysis presented in Fig. 57 show the distribution of maximum compressive strain computed in the concrete rib. It may be noted that considerably larger strains developed at the downstream side as compared to the strains at the upstream side. Also shown in Fig. 57 are the measured strains at the crown, downstream and upstream sides. The analysis also indicated that a tensile "cracked" zone developed at the upstream edge of the concrete rib. The comparison indicates that the observed and computed strains in the concrete rib are in fairly good agreement.

Also shown in Fig. 57 are the computed lateral wall deflections. A maximum deflection of 1.7 inches was calculated near the upper portion of the downstream wall, and 0.5 inches on the upstream wall. No data of observed wall deflections were available for comparison. However, the observed wall deflections developed after the excavation was essentially completed indicate that movements on the downstream wall were greater than those on the upstream wall, a result similar to that obtained from the computations. The larger strains in the concrete rib and the larger wall deflection at the downstream side than those at the upstream side indicate that the presence of the fault "B" had a significant effect on the behavior of the excavation.

Evaluation of the stress distribution in the rock mass surrounding the excavation showed that the stress levels were well

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Fig. 57 Comparison of Observed and Predicted Behavior of Tumut I Underground Power Station

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below the yield strength computed by the strength parameters prescribed, and the overall stability of the rock mass was maintained throughout the excavation. The results of the analysis indicated that a 50-foot section of the fault "A" at the upstream side immediately above the roof of the excavation failed in shear after the first stage of excavation (see Fig. 53). However, subsequent stress redistribution and installation of the concrete ribs prevented any further failure along the fault "A".

In summary, the analysis of the Tumut I underground machine hall indicated that the observed behavior of the excavation following a complicated excavation sequence could be predicted with a reasonable accuracy using the general computer program that has been developed. The major difficulty in analysis, however, lies in the determination of the distribution of major geologic discontinuities and their stress deformation characteristics.

ANALYSIS OF A ROCK TUNNEL, WASHINGTON D.C. METRO Construction of rock tunnels for the Washington D.C. Subway (METRO) has been described by Mahar, Gau and Cording (1972), and Bawa and Bumanis (1972). Due to the detailed documentation of the geologic conditions and the performance data of the tunnel excavations, it is believed that the tunnel excavations of METRO would provide excellent case histories for this study to verify the reliability of the general computer program developed for evaluation of stability of underground excavations. General geologic, excavation and support conditions, and the results of instrumentation on rock movements during excavations of a rock tunnel were provided to us by Dr. E. J. Cording (1973) and J. W. Mahar (1973) of University of Illinois, Urbana. The general geologic, excavation and support conditions are briefly described in the following section.

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General Geologic Conditions

The rock tunnel analyzed was driven through a foliated rockschistose gneiss of quartz-mica composition. Average rock quality, defined as the RQD of the rock core, ranges between fair to good, except in the shear zones where rock quality is poor to very poor. The significant features of the rock are: (1) the continuous, smooth joint planes which form large rock blocks, and (2) highly continuous shear zones which parallel the rock foliation.

The major features of the rock structure observed at the rock tunnel consist of foliation, eight major shear zones, joints in seven principal orientations designated as Set Nos. 1, 2L, 2H, 3L, 3H, 4L, and 4H. The orientation of the joints is shown in Fig. 58. Rock foliation is moderate to well developed and strikes sub-parallel to the long axis of the tunnel (N15°W) and dips 60° to 70° west.

The major shear zones, all of which are oriented sub-parallel to rock foliation or Joint Set 1, strike 10° to 20° right of tunnel axis and dip 50° to 60° west. These zones are generally 1 to 5 feet in width and spaced 10 to 50 feet apart. The most prominent features within the shear zones are layers of gouge and/or broken rock. The layers are generally 1 to 6 inches wide, highly continuous and are planar to slightly wavy. The gouge consists of a sandy, clayey material and is generally 1 to 2 inches thick. Rock fragments are generally less than 2 inches in size. Slickensides occur throughout the gouge and along the boundaries of the rock fragments. The distribution of the shear zones as shown on the cross-section analyzed is given in Fig. 59.

Joints and slickensided joints designated as Joint Set 1 having the same altitude as the major shear zones are prominent throughout the tunnel. These joints are highly continuous,

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smooth and planar. The slickensided joints generally contain a talc and chlorite filling 1/8 to 1/2 inch thick. The average spacing of Joint Set 1 is 1 to 3 feet.

Joints in six other principal orientations are generally tight, planar, and continuous. These joints are not as commonly sheared or filled with gouge as the joints of Set No. 1. However, these joints may contain up to 1/4 inch of talc and chlorite and may be wet, particularly when the joints are located in the vicinity of foliation shear zones.

General Excavation and Support Conditions

The crown of the rock tunnel analyzed in this study is approximately 60 feet below the ground surface. The ground cover consists of a 30-foot-thick layer of soil immediately below the ground surface and a 30-foot-thick rock separated by 1 to 2 feet of weathered rock. The tunnel was driven in several stages: the pilot tunnel and Stages 1, 2a, and 2b.

The pilot tunnel was driven as a 6 foot by 8 foot exploratory drift through the full length of the station. After completion of the pilot tunnel, three rock bolts (24 feet long and 1-1/8 inches in diameter) were installed every 5 feet in the crown of the tunnel. Prior to driving Stage 1, bearing plates of most of the bolts were tightened and the first 6 feet of these bolts were grouted with cement.

The Stage 1 drift was driven as a box-shaped opening. The drift at the cross-section analyzed was a 18-foot-wide-by-24-foot-high opening. The drift was supported with shotcrete, rock bolts, and steel ribs. The heading of the Stage 1 excavation was initially supported with a layer of shotcrete having an average thickness of 2 inches. Steel ribs consisting of 14 WF posts which did not provide lateral support to side walls and 8 WF beams were placed every 5 feet. After the steel ribs had been installed, four rock bolts were installed in the crown of the Stage 1 drift, two on either side of the pilot tunnel. These bolts spaced 5 feet of center and installed within 4 feet of the face were fully grouted with resin.

The 2a and 2b drifts were driven in approximately 10 feet by 10 feet openings in 5 feet advances. The thickness of the rock pillar between the Stage 1 drift and the side drifts at the cross-section analyzed was approximately 13 feet.

Idealization of Tunnel Excavation

Finite Element Idealization - The finite element idealization of the tunnel excavation is shown in Fig. 59. The idealization of the geologic profile includes a number of shear zones and Joint Sets 1, 3L, and 3H as projected from the geologic map on to the cross-section analyzed. Joint Sets 2L, 2H, 4L, and 4H were not present on the cross-section because the strikes of these joints are approximately perpendicular to the axis of the tunnel. The excavation was idealized as a 3-stage excavation: Stages 1, 2a, 2b. The pilot drift was considered to be a part of Stage 1 excavation. During excavation of the pilot drift and Stage 1 drift, installation of seven rock bolts at the crown was simulated by application of equivalent nodal point forces of 4000 lbs/ft at the bearing plate and the anchor of each rock bolt. Idealization of the grouted rock bolts may be improved by considering the rock bolts as one-dimensional bar elements with the same material properties as those of the rock bolts. The 2-inch-thick layer of shotcrete and the steel ribs were not simulated in the analysis. As noted in Fig. 59, the upper 30-feet-thick layer of soils immediately below the ground surface was replaced by applying a uniform pressure equivalent to the overburden pressure of 3600 psf on the upper boundary of the rock cover in order to minimize the number of

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elements and nodes required in the idealization. The total number of elements and nodes used were 863 and 986, respectively.

Initial State of Stress - No stress measurements were made at the site. However, Cording (1973) expressed the opinion that there is no high horizontal stress existing at the site and the vertical stress is approximately equal to the overburden pressure. In the parametric study to be described later, two initial states of stress were assumed. The vertical stress was assumed equal to the overburden pressure and the ratios of horizontal to vertical stress were 0.6 and 0.8 for two initial stress conditions.

Material Properties - No test data were available for determination of material properties for intact rocks, shear zones and joints present in the geologic profile. However, reasonable values were assumed for deformation moduli and strength parameters for the intact rock and shear zones, and for deformability and shear strength of the joints, and a parametric study conducted to select the properties for more detailed analysis. The assumed material properties used in the parametric study (Cases A, B and C) are summarized in Table 5. The deformation modulus of the intact rock was assumed to be 1,000,000 psi for all three cases, and 1,000,000 psf for the shear zones. The values of the Poisson's ratio were assumed to be 0.15 and 0.3 for the intact rock and the shear zones, respectively. For Cases A and B, the normal stiffness of the joints were assumed to be 1×10^7 pci and the shear stiffness to be 5×10^6 pci, and the angle of shearing resistance equal to 25 degrees with no cohesion. The normal and shear stiffnesses for the joints for Case C were 100% higher than those for Cases A and B and the angle of shearing resistance was reduced to 20 degrees.

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Joinčs	K _s pcf	5.x10 ⁶	5.x10 ⁶	1.x10 ⁷	srtical S σ _V = Hor rerburder
. Kn pcf	K _n pcf	1.x10 ⁷	1.×10 ⁷	2x10 ⁷	α ^α ν = Κ
	φ deg.	35	35	35	
nes	C psf	.0	.0		
ar 201	2	0.3	0.3	0.3	
She	E psf	1.x10 ⁶	1.x10 ⁶	1.×10 ⁶	ments
	φ deg.	45	45	45	it Ele
t Rock	C psf	7.2x10 ⁵	7.2x10 ⁵	7.2x10 ⁵	for Join
Intac	2	0.15	0.15	0.15	Ratic Iffness
	E psf	1.44x10 ⁸	1.44x10 ⁸	1.44x10 ⁸	Modulus Poisson's Normal Sti
Case		A	B	U	н н н н > Ж

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C = Cohesion

K_s= Shear for Joint Elements

\$ = Angle of Friction

Presentation and Discussion of Results

Three cases were analyzed in the parametric study to examine the effect of the initial stress conditions and the deformability and strength properties of the joints on the computed movements surrounding the tunnel due to Stage 1 excavation. The results of the parametric study are summarized in Table 6. Comparing Cases A and B for the elastic solution, when the ratio of the horizontal to vertical stress decreases from 0.8 (Case A) to 0.6 (Case B), the movement at the crown increases 15% while the movement on the side walls decrease 20% to 25%. In the non-linear solution in which effects of joint and shear zone failure were considered, the movements at the crown and the east wall for Case B were 10% higher than those for Case A, indicating that more elements would fail under low horizontal stress conditions. Comparing Cases A and C, it may be noted that while the joint stiffnesses increased 100%, the movements decreased 10 to 20% indicating the presence of the shear zones might have significant effects on the behavior of the excavation. It is interesting to note that for all three cases, the movement on the west wall remained about the same for both elastic and non-linear solutions.

The detailed analysis was conducted using the material properties and the initial stress conditions assumed for Case A. The results of the detailed analysis of the 3-stage excavation are summarized in Table 7 and Figs. 60 and 61. Table 7 and Fig. 60 summarize the computed movements at the crown and side walls of the Stage 1 drift due to each stage of excavation. The computed movement at the crown increased from 0.27 inches due to the Stage 1 excavation to 0.41 inches at the end of the Stage 2b excavation. The total movement observed at the crown was 0.42 inches. The computed movement on the east wall increased from 0.52 inches due to the Stage 1 excavation to 0.61 inches at the end of Stage 2b excavation. The total movement Table 6. Summary of Results of Parametric Study on

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a Rock Tunnel, Washington, D. C. Metro

ions	ıtion	DX 21 West Wall	0.24 in.	0.18 in.	0.20 in.
Excavation ometer Direct	onlinear Solu	DX 20 East Wall	0.52 in.	0.57 in.	0.49 in.
to Stage 1 the Extense	Ň	DX 3,4 Crown	0.27 in.	0.31 in.	0.21 in.
vements Due Surface in	uo	DX 21 West Wall	0.24 in.	0.17 in.	0.19 in.
Computed Mo on the Excavated	lastic Soluti	DX 20 East Wall	0.48 in.	0.37 in.	0.43 in.
	EJ	DX 3,4 Crown	0.20 in.	0.23 in.	0.15 in.
		Case	Α	B	U

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Table 7. Summary of Results of Analysis of a Rock Tunnel, Washington D. C. Metro.
-Computed and Observed Movements on the Excavated Surface in the Extensometer Directions

(Case A)

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One-Step	Elastic Solution	0.26 in.	0.51 in.	0.19 in.
Observed	(final)	0.42 in.	0.67 in.	*0.85 in.
Side Drift	2b	0.41 in.	0.61 in.	0.22 in.
Side Drift	2a	0.34 in.	0.55 in.	0.21 in.
ixcavation	Nonlinear Solution	0.27 in.	0.52 in.	0.24 in.
Stage 1 E	Elastic Solution	0.20 in.	0.48 in.	0.24 in.
Location		DX 3,4 Crown	DX 20 East Wall	DX 21 West Wall

*Due to loosening of a rock block, large movement was only observed near the excavated surface.




observed on the east wall was 0.67 inches. The computed movement on the west wall was 0.24 inches due to the Stage 1 excavation and decreased slightly at the end of the Stage 2b excavation. Also shown on Table 7 are the movements computed from the elastic solution of the 3-stage excavation. The crown movement computed was 0.26 inches as compared to 0.41 inches computed from the nonlinear solution. The east wall movement computed was 0.51 inches as compared to 0.61 inches computed from nonlinear solution. The west wall movement computed was slightly less than that computed from the nonlinear solution.

Figure 61 illustrates the comparison between the computed and observed movements due to the excavation of the rock tunnel analyzed. The computed total move ants at the excavated surface are generally in close agreement with those observed, except the one on the west wall for which the larger movement was measured near the surface due to loosening of near-surface rock blocks. However, a significant portion of movements was computed at the anchor points of the extensometers, indicating that the computed movements within the instrumented rock zones are less than those measured. It is expected that the results of the analysis could be improved and would tend to indicate failure and loosening of larger portions of shear zones and joint blocks, similar to the behavior observed in the field, if lower values of the friction angles for shear zones and joints, and higher values of modulus for shear zones are used in the analysis.

The results of the analysis of the rock tunnel of the Washington D.C. METRO indicate that the behavior of the rock mass formed by various continuous joint sets and shear zones due to underground excavations could be predicted with a reasonable degree of accuracy. Although the properties of significant geologic features; e.g., joints and shear zones, present in the rock mass were not available for the analysis, it was possible to determine reasonable material properties from a parametric

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study and the observed performance of the underground excavation. The analysis was considered to be useful in understanding the behavior of the excavation in that particular rock mass. The material properties utilized can be employed to predict the response of the rock mass around further tunnel excavations in similar geologic conditions.

CONCLUSIONS AND RECOMMENDATIONS

For the purpose of evaluating the capabilities and illustrating the use of the computer code developed, studies on a number of well documented model tests and case histories of underground openings were analyzed. These included the analysis of model tests on lined and unlined openings in jointed rock, and the analysis of Tumut I underground power station and a rock tunnel of Washington, D.C. (METRO) Subway.

The conclusions drawn from this evaluation are as follows:

- 1. The major problem in utilizing the computer code developed to the analysis of practical problems is the lack of information on the properties of the rock mass especially with respect to the location and deformation characteristics of geological discontinuities.
- The properties of geological discontinuities can be determined through a parametric study using various combinations of material properties and comparing the results with limited aspects of observed performance.
- 3. Utilizing the properties selected in (2) additional aspects of the behavior of excavation in rock can be predicted with reasonable accuracy.

- 4. The program can be calibrated in terms of material properties in the initial phases of an excavation and then utilized to predict future performance.
- 5. The results of this study indicate that if the location and properties of geologic discontinuities can be defined then the computer code developed can be a valuable aid to the design of excavations in rock.

Recommendations for Future Research

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Although studies of a limited number of the case histories indicated that the analytical models developed under this contract could predict the behavior of underground openings with a reasonable accuracy, more case history studies are required to fully evaluate the capabilities and the improvements required for the computer code developed.

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APPENDIX A

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A COMBINED COMPUTER PROGRAM USING FINITE ELEMENT TECHNIQUES FOR ELASTO-PLASTIC, JOINT PERTURBATION AND NO TENSION ANALYSIS OF SEQUENTIAL EXCAVATION AND CONSTRUCTION OF UNDERGROUND OPENINGS IN ROCK

A COMBINED COMPUTER PROGRAM USING FINITE ELEMENT TECHNIQUES FOR ELASTO-PLASTIC JOINT PERTURBATION AND NO TENSION ANALYSIS OF SEQUENTIAL EXCAVATION AND CONSTRUCTION OF UNDERGROUND OPENINGS IN ROCK

Identification

The program which consists of a main program and 15 subroutines (NPSTRS, STIFF, MODIFY, QUAD, TRISTF, JTSTIF, BANSOL, STRESS, INITST, PRINST, LOAD, JTSTR, EPLAST, STRSTR, NPFORC) is a modification of the computer program developed and documented in the report, "A Theoretical Method for Evaluating Stability of Openings in Rock," by C. Y. Chang and K. Nair, U.S. Bureau of Mines Contract No. HO210046 (April 1972). The major improvements and modifications have already been discussed elsewhere in this report.

Purpose

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The combined program has been developed to take into account the actual construction and excavation sequences which are important factors to be considered, especially in non-linear materials. The rock mass may consist of joints, faults, bedding planes and other geologic discontinuities. The intact rock may be incapable of sustaining any tensile load and exhibit elastic-perfectly plastic behavior.

Sequence of Operation

- (a) The main program handles the initial input and monitors the calling of the subroutines in a specified order as shown in Fig. Al. If specified for the last iteration of the last step in analysis stresses, excess stresses to be redistributed, nodal point displacements and yield functions are punched onto cards to be used for restarting computation. This allows one to monitor the results as analysis proceeds, without loss of computer time.
- (b) Subroutine NPSTRS computes stresses at nodes on the excavated boundary from stresses in surrounding elements.
- (c) Subroutine STIFF assembles the general stiffness matrix for the entire structure, adds the concentrated loads at the nodal points, and modifies the stiffness matrix for the boundary conditions.
- (d) In Subroutine QUAD the stiffness of a two-dimensional element is formulated.
- (e) Subroutine JTSTIF forms the stiffness matrix for each joint element.

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- (f) Subroutine TRISTF forms the stiffness matrix for triangular sub-elements and, if specified, element loads due to gravity are calculated.
- (g) Subroutine MODIFY modifies the stiffness matrix for the boundary conditions.
- (h) Subroutine LOAD calculates equilibrating nodal point forces due to gravity, if specified, and for excess stresses computed in Subroutine EPLAST for elasto-plastic and/or no tension materials.
- (i) Subroutine BANSOL solves the simultaneous equations representing the structural stiffness matrix and the structural load vector for nodal point displacements.
- (j) Subroutine STRESS calculates incremental stresses and strains, cumulates stresses, and prints stresses and strains for two-dimensional elements.
- (k) Subroutine JTSTRS calculates and prints normal and tangential displacements (cumulative and incremental) and excess normal and tangential stresses to be redistributed by comparing stress with strength for joint elements. The equilibrating nodal point forces are also computed from the excess stresses and stored for the next iteration.
- (1) Subroutine EPLAST calculates yield functions and elastoplastic stress-strain relation for those two-dimensional elements in yield. The excess stresses to be redistributed are computed as a difference between changes in stress calculated from the elastic stress-strain relation and those calculated from the elasto-plastic stress-strain relation.
- (m) Subroutine INITST generates initial stresses under freefield conditions.
- (n) Subroutine PRINST calculates magnitudes and directions of the principal stresses and strains.
- () In Subroutine STRSTR the constitutive law for the material is formulated.
- (P) In Subroutine NPFORC the nodal point forces due to boundary pressures are calculated.

Output

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The data describing the finite element configuration, the material properties and pressures applied to the excavated face to simulate excavation for the opening are printed after being read. Nodal point displacements (incremental and cumulative), stresses, strains and yield functions for two-dimensional elements; normal and tangential stresses, normal and tangential displacements (incremental and cumulative) for joint elements, are printed after each increment or iteration. If specified, for the last iteration of the last increment in the last construction step specified in an analysis, stresses, strains and excess stresses to be redistributed for two-dimensional elements, normal and tangential stresses for joint elements, nodal point displacements and yield functions for two-dimensional elements are punched onto cards to be used for restarting computation.

Input Data Procedure

1st CARD TYPE: FORMAT (8A10) (One Card) Cols 2-80 Identifying information to be printed with results. 2nd CARD TYPE: FORMAT (315, 2FI0.2, 15, 2FI0.5, 415) (One Card) Cols. 1-5 NUMNP - Number of nodal points (maximum 999) 6 - 10NUMEL - Number of element (maximum 900) 11-15 - Number of different materials NUMMAT (maximum 12) 16 - 25ACELX - Acceleration in X-direction 26 - 35ACELY - Acceleration in Y-direction 36-40 NRES* - = -1, Residual stresses generated from which residual load is calculated. = 0, Residual stresses generated, but residual load is zero. = 1, Residual stresses read as input, from which residual load is generated. = 2, Residual stresses read as input, but residual load is zero. = 3, Residual stresses will be computed for the purpose of calculating nodal forces along excavated boundary. REFPR 41-50 - Vertical stress at the reference point.

*If NREAD = 1, NRES should not be greater than zero. If NRES = -1 or 1, gravity turn-on analysis is performed.

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	51-00	DEPIN -	1. ordinate at the reference point.
	61-65	NANALY -	= 0, Analysis using stress transfer techniques with constant initial stiffness.
		NANALY -	= 1, Analysis using stress transfer techniques with updating ele- ment stiffness at each incre- ment of load.
	66-70	NCONST -	Total number of construction steps simulated in analysis.
	71-75	NPUNCH -	= 0, Data will not be punched out at the last iteration.
			= 1, Data will be punched out at the last iteration of the last increment at the last construc- tion step.
	76-80	NREAD -	= 0, No data from previous compu- tation will be read as input.
			= 1, Data from last increment are read as input.
3rd CA	RD TYPE	FORMAT	(215) (One Card)
Cols.	1-5	MJØINT -	Total number of material types for joints (maximum 12)
	6-10	MTENS -	Total number of material types tha t can sustain tension.
4th CA	RD TYPE	FORMAT	(16I5) (Omit this card if MJOINT = 0 on 3rd Card Type)
Cols.	1-5	MJNT(I)	- Material type number for joint elements.
	6-10	Same	
	11-15		
<u>5th CA</u>	RD TYPE	FORMAT	(1615) (Omit this card if MTENS = 0 on 3rd Card Type)
Cols.	1-5	MNTEN(I)	- Material type number which can sustain tension.
	6-10	Same	
	11-15		

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6th CA	ARD TYPE:	FORMAT (I	5,	2F10.5) (One Card)
Cols.	1-5	MTYPE	-	Material type number.
	6-15	RO(MTYPE)	-	Mass density of this material type.
	16-20	AKO(MTYPE)	-	Ratio of horizontal to vertical stress under initial stress conditions.
7th C/	ARD TYPE:	FORMAT (8	FI	.0.5, I5)
Cols.	1-10 E	(1, MTYPE)	•	Tensile strength for normal materials or normal stiffness for joint materials.
	11-20 E	(2, MTYPE)	•	Modulus in compression for normal materials or shear stiffness for joint materials.
	21-30 E	(3, MTYPE)	-	Poisson's ratio for normal materials or cohesion for joint materials.
	31-40 E	(4, MTYPE)	-	Modulus in tension for normal materials or angle of friction for joint materials (degrees)
	41-50 E	(5, MTYPE)	-	Cohesion for normal materials or maximum allowable closure (input as negative) for joint materials.
	51-60 E	(6, MTYPE)	-	Angle of friction for normal materials (degrees)
	61-65 N	TEST	-	Type of Test = 0, if c and Ø obtained from triaxial test
				= 1, if c and β obtained from plane strain test.
	66-75 C	RAC (MTYPE)	-	Fraction of tensile strength which the material is allowed to take after tension failure.
Repea	t 6th and	7th card t	y	pes for all material types.
8th C	ARD TYPE:	FORMAT (I each noda	5	, F5.0, 4F10.0) (One card for point)
Cols.	1-5 N		-	Nodal point number.

6-10 CODE (N) - Number which indicates if displacements or forces are to be specified.

- = 0 UR is the specified X-load and UZ is the specified Y-load
- I UR is the specified X-displacement and UZ is the specified Y-load
- = 2 UR is the specified X-load and UZ is the specified Y-displacement
- = 3 UR is the specified X-displacement and UZ is the specified Y-displacement

Cols.	11-20	R(N)	- X-ordinate	
	21-30	Z (N)	- Y-ordinate	
	31-40	UR(N)	- X-load or displacemen	it
	41-50	UZ(N)	- Y-load or displacemen	nt

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Nodal points must be numbered in sequence. If nodal point numbers are omitted, those omitted are generated automatically at equal spacings, between those specified and CODE(N) is assigned zero. The first and last nodal points must be specified.

9th C	ARD TYPE	FORMAT	(615) (One card for each element)
Cols.	1-5	М	- Element number
	6-10	IX(M,1)	- Nodal point I
	11-15	IX(M,2)	- Nodal point J
	16-20	IX(M,3)	- Nodal point K
	21-25	IX(M,4)	- Nodal point L
	26-30	IX(M,5)	- Material number

The nodal point numbers must be numbered consecutively proceeding counterclockwise around the elements. The nodal point numbers for any element must not differ by more than 44. If element numbers are omitted, those missing will be generated by incrementing the element number and each nodal point number (I, J, K and L) by one, and assigning the same material number as the last element specified. The first and last elements must be specified. Triangular elements are also permissible, and are identified by repeating the last nodal point number (i.e., I, J, K, K). For joint elements, nodal points must be numbered I, J, K, L counterclockwise proceeding along length of joint from I to J and along length from K to L. Nodal points I and L (J and K) have different numbers but identical coordinates.

One-dimensional elements are also permissible and are identified by the node number sequence (I, J, J, I).

<u>10th</u>	CARD TYPI	E: FORMAT (element)	IS	5, 4E15.	5) (One	card	for	each
Cols.	1 - 5	N	E	Element	number			
	6-20	STRS(N,1)	-	Initial	stress	σ _x		
	21-35	STRS(N,2)	-	Initial	stress	σy		
	36-50	STRS(N,3)	-	Initial	stress	^τ xy		
	51-65	STRS(N,4)	-	Initial	stress	σ,		

This card type is neglected if NRES ≤ 0 or NRES=3 on the 2nd card type.

11th CARD TYPE: FORMAT (I5)

Cols. 1-5NJT- Total number of joint elements.12th CARD TYPE:FORMAT (2F20.5, I5)Cols. 1-20FN(I)- Normal stress across joint element
NEJT(I)21-40FT(I)- Tangential stress across joint

41-45 NEJT(I) - Element number for joint element Repeat 12th card type for all joint elements.

element NEJT(I)

11th and 12th card types are neglected in MJOINT = 0 on the 3rd card type or NRES \leq 0 or NRES = 3 on the 2nd card type. 13th CARD TYPE: (315)

Cols. 1-5 NCPSNT 6-10 NPRSNT 11-15 ITPSNT 14th CARD TYPE: (8A10)	 Present construction sequence number Present load increment number Present iteration number
Cols. 2-80 TITLE	- The information regarding this construction sequence number to be printed out.

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15th (CARD TY	PE: (8	I5)	
Cols.	1-5	NERSP	-	Number of elements to be excavated and/or for structural support.
	6-10	NUMPC	-	Number of pressure cards.
	11-15	NPF	-	Number of nodal points at which forces are applied.
	16-20	NPCAV	-	Number of nodal points along current excavated face.
	21-25	NP		Number of load increments by which <u>boundary</u> <u>pressures</u> and <u>pressures</u> computed for <u>excavation</u> simulation will be divided into small load increments. The magnitude of increment is to be specified on the card type.
	26-30	NGLD	-	= 0 Not a gravity turn-on analysis step.
				= 1 Present step is gravity turn-on to obtain initial stresses.
	31-35	MTRM	-	Material type for excavated elements.
	36-40*	NSPT	-	Index indicating if there is any element to be converted to liner for current construction step.
				= 0 if there is no element to be converted to liner
				<pre>= 1 if there are some elements to be converted to liner</pre>
<u>16th (</u>	CARD TY	<u>PE</u> : (1 ca	615 rd) (Neglected if NERSP = 0 on the 15th type)
This or add as are	card typ led and e requi	pe carr their red to	ies cha be	the numbers of all elements removed anged material type. As many cards provided.
Cols.	1-5	NE(I)	-	Element number.
	6-10 1	MT(I)	-	New material type for this element.
	11-15 !	MSP(I)	-	Material type of liner if the element is to be "excavated" first and then converted to the liner. MSP(I)=MT(I) if NSPT=0 on the 15th card type or the element not to be "converted" to the liner.
	16-20 21-25 26-30		-	Same as above.
17th (CARD TY	<u>PE</u> : FO	RMA	AT (16I5)
Cols.	1-5	IJBC(L,	1)	- Nodal point number I along the boundary IJ where the boundary pressure is applied.

*See Table A-1 for significance of the index.

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6-10 IJBC (L,2)	-	Nodal point J along the boundary IJ.
11-15	_	Same as above; two nodal point
16-20		the boundary pressure is applied.
21-25	-	
26-30		

As shown in Fig. A2, nodal points I and J must be ordered in counterclockwise order about centroid of element on which the pressure is applied.

18th CARD TYPE: FORMAT (15)

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1-5 NPBCP - Number of nodal points along the boundary Cols. where the stresses are applied.

19th CARD TYPE: FORMAT (I5, 3F10.0)

Cols. 1-5 NPBC(M) - Nodal point number where the boundary pressure is applied.

6-15 PSCA(M,1) - σ_x at nodal point.

16-25 PSCA(M,2) - σ_v at nodal point.

26-35 PSCA(M,3) - T_{XY} at nodal point.

Stresses (σ_x , σ_y and τ_{xy}) are shown positive in Fig. A2. To simulate excavation, these stresses are equal in magni-tude and opposite in direction to the initial stresses at the nodal point. As shown in Fig. A2, stresses (σ_x , σ_y and T_{XY}) at the nodal points are converted to normal and shear stresses on the boundary. Then the nodal point forces are calculated from the normal and shear stresses along the boundary assuming linear stress distribution along the boundary. The normal and shear stresses are shown positive in Fig. A2. These cards are provided to take into account externally applied stresses.

17th, 18th and 19th card types are neglected if NUMPC = 0 on the 15th card type.

20th CARD TYPE: FORMAT (15, F5.0, 2F10.0)

These cards read the information regarding the change in the boundary conditions for all the nodal points involved.





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Cols. 1-5 N

- Number of nodal point.

6-10 CODE(N) - Type of nodal point.

11-20 UR(N) - Load or displacement in X-direction.

21-30 UZ(N) - Load or displacement in Y-direction.

These cards are omitted if NPF = 0 on the 15th card type.

21st CARD TYPE: FORMAT (515)

Cols. 1-5 NS(I) - Nodal point number at which nodal stresses are to be computed.

6-10 NSEL(I,1) - First interpolation element number.
11-15 NSEL(I,2) - Second interpolation element number.
16-20 NSEL(I,3) - Third interpolation element number.

21-25 NSEL(I,4) - Fourth interpolation element number.

Repeat for all nodal points at which nodal stresses are to be computed. These are provided to simulate excavation.

The mid-points of no three of the four interpolation elements may lie on a horizontal or vertical line. These elements should be read in a criss-crossed fashion as shown in Fig. A3. The centroids of the first and second elements should not lie on a vertical line.

These cards are omitted if NPCAV is zero on the 15th card type.

22nd CARD TYPE: FORMAT (15)

Cols. 1-5 NCAVPC - Number of pressure cards on the cavity face to simulate excavation.

23rd CARD TYPE: FORMAT (1615)

Cols.	1-5	IJBCA	(L,1)	Ξ	Nodal point I along boundary IJ where pressure is applied.
	6-10	IJBCA	(L,2)	÷	Nodal point J along boundary IJ.
	11-15				Same as above. Two nodal point
	16-20			•	the boundary pressure applied.

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21-25 ----26 - 3022nd and 23rd card types are neglected if NPCAV = 0 on the 15th card type. 24th CARD TYPE: FORMAT (15, F10.5) - Number of iteration for Nth increment. Cols. 1-5 ITN(N) 6-1." PRATIO(N) - Fraction of total pressure applied for Nth increment. The sum of PRATIO (N) for all increments should be equal to 1. Repeat for each loading increment. Binary data cards for all elements which are 25th CARD TYPE: punched out at the end of the previous computer run. STRS(N,1) - σ_x STRS(N,2) - σ_v $STRS(N,3) - \tau_{xy}$ SEP(N,1) - Excess stress σ_x' SEP(N,2) - Excess stress σ_y' - Excess stress τ_{xy} SEP(N,3) $STRS(N,4) - \sigma_z$ - An index indicating if the element has failed in MTAG(N) tension or yielded under compressive stress field. If MTAG(N) = 1, the element has not failed in tension or compressive stress field MTAG(N) = 2, the element has failed in tension in one direction only. MTAG(N) = 3, the element has failed in tension in two orthogonal directions. MTAG(N) = 4, the element has not failed in tension but yielded under compressive stress field. MTAG(N) = 5, the element has failed in tension in one principal stress direction, and subsequently yielded under compressive stress field. MTAG(N) = 6, the element has failed in tension in two orthogonal directions, and subsequently yielded under compressive stress field.

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<u>26th CARD TYPE</u>: Binary data cards for all joint elements, neglected if MJOINT = 0.

NJT - Total number of joint elements FN(N) - Normal stress across joint element FT(N) - Tangential stress across joint element

25th and 26th card types are neglected if NREAD = 0 on the 2nd card type, i.e., these cards are only needed to restart the computation.

<u>27th CARD TYPE</u>: Binary data cards for all nodal point displacements, yield function, and all strain components for all elements.

DISP(N,1) - X-displacement for node N DISP(N,2) - Y-displacement for node N FY(N) - Yield function for element N STRN(N,1) - Strain component, ε_x , for element N.

STRN(N,2) - Strain component, c_y , for element N.

STRN(N,3) - Strain component, γ_{xy} , for element N.

27th card type is neglected if NREAD = 0 on the 2nd card type, i.e., these cards are only needed to restart the computation.

Repeat 14th through 24th card types for all subsequent construction stages.

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TABLE A-1 Manipulation of Scratch Tapes for Storing Stiffness and Element Strain-Displacement Transformation Matrix

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NOTE:	NCT = Construction stage	number	NNN = Load increment number	NIT = Iteration number NANALY = 0 Use constant elastic	stiffness NANALY = 1 Use both initial and	tangent stiffness during computation	NSPT = 0 No element to be	CORVETTED TO LINET NSPT = 1 Some elements converted	to liner WVN - WW-HAR of closents withdad	NID - NUMBEL OL ELEMENTS FIELDED NCALC = 1, Compute elastic	stiffness and store on tapes 80 § 90	NCALC = 2, Compute elastic	stilfness with elements converted to liner and	score on tapes so a ou NCALC = 3, Compute tangunt	stiffness and store on tapes 30 §40	NCALC = 4, Use elastic stiff-	ness on tapes ou q gu NCALC = 5. Use elastic stiff-	ness with liner on tapes 50 ६ 60	NCALC = 6, Use tangent stiff-	icas on rapes of 4 to			
	[=]	NYD>	0	NCALC= 1	2	3	9	4	5	3	6	4	5	3	9	1	2	3	9	4	5	3	9
ſ=1	NSP	NYD=	0	NCALC=	2	S	S	4	5	5	5	4	5	5	s	1	2	S	S	4	5	2	S
NANAL	0=	NYD>	0	NCALC=	3	9	9	4	3	6	9	4	3	6	6	1	3	6	9	4	3	9	9
	NSPT	-dyn	0	NCALC= 1	4	4	4	4	4	T ?	4	4	4	4	4	1	4	4	4	4	4	4	4
Тλ=0	NSPT	 		NCALC=	2	s	s	4	υ,	2	S	4	S	S	2	1	2	S	s	4	2	S	S
NANA	NSPT	0=		NCALC= 1	4	4	4	4	4	4	4	4	4	·4	4	1	4	4	4	4	4	4	4
	LIN			1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4
	NNN				-	-			~	J			۲	ŋ				4			۰ ۲	1	
	NCT								F							7							

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APPENDIX B

COMPUTER PROGRAM LISTING

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B-1-A
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	PROGRAM NTJTEP2(INPUT, OUTPUT, TAPE9, TAPE90, TAPE91, TAPE3,	NTJT	10
	1 PUNCHB, TAPEBO, TAPE30, TAPE40, TAPE50, TAPE50, TAPE53, NPUT,	NTIT	20
	2 TAPE1=DUNCHB, DUNCH)		70
		NIJI	30
	C TENSION, JUINT PERIORBATION, AND ELASTIC PLASTIC ANALYSIS OF	NTJT	40
	C PLANE STRAIN STRUCTURES WITH INCREMENTAL CONSTRUCTION.	NTJT	50
_	C**** THIS PROGRAM DEVELOPED BY C-Y CHANG OF WOODWARD-LUNDGREN SEPT. 73	NTJT	60
I	COMMON / / NUMNP, NUMEL, NUMMAT, NUMPC, ACELX, ACELY, HED (8), NNN, NP,	NTJT	70
	1 NPCAV, REFPRS, DEPTH, NRES, N. VOL, NCALC, IBACK, MJUINT, MTENS, NTT.	NTJT	AC
	2 ITN (20) . PRATIO (20) . NISTOP . NREAD . NSTSPT . NANALY	NT TT	00
	3.NET.NEGNET.NPREP.NEAVPE		40
I		NTJI	100
	LUMMUN /MATP/ MITPE, RU(12), E(8,12), AKU(12), MNTEN(12), MJNT(12)	NTJT	110
	1 , CHAC(12)	NTJT	120
	CUMMON /ELUATA/IX(900,5),MTAG(900),EPS(900),STRS(900,4),SEP(90,3)NTJT	130
E	COMMUN /NPDATA/ R(999),Z(999),CODE(999),UR(999),UZ(999)	NTJT	14C
	COMMON /PSLD/ IJBC(50,2), PSCA(75,3), NPRC(75)	NTJT	150
	COMMON /BANARG/ B(180) . A(90, 180) . MBAND . ND2 . NUMBI K. MBMAY . NB	NTTT	140
	1.MTAD1.MTAD3		100
L	FUNDAL (ADD/E) 777/EN B/1A (AN D/(AN DAVDA/AN DAVDA/AN ADAD AMAKA	NIJI	170
•	CUMBUM /ARG/ RRA(5)/222(5)/S(10/10)/P(10)/RS(RS(4)/LBAD/LM(4)/	NTJT	180
	1 ANGLE(4), XI, HH(6, 10), C(4, 4), EE(4), H(6, 10), D(6, 6),	NTJT	190
ĩ	<pre></pre>	NTJT	200
ŧ.	COMMUN /JNT/ FN(450),FT(450),NJT	NTJT	215
	COMMON /NPS/ PSCAV(75,3),IJBCA(50,2),NS(75)	NTJT	225
	DIMENSION DISP(999,2), FY(900), NEJT(450)	NTIT	230
T	DIMENSION STRN (900,3)	NT.TT	240
L	DIMENSION NE(150) MI(150) NSEL (4.50) TITLE (8) MODILEON	NTTT	350
		NIJI	236
		NTJT	59C
E	ENVIVALENCE (NEUTALOUDD))	NTJT	270
Ł	EQUIVALENCE (STRN, A (6500))	NTJT	280
	DATA MEMAX/90/, ND2/180/, END/3HEND/, NB/45/	NTJT	290
	C READ AND PRINT OF CONTROL INFORMATION AND MATERIAL PROPERTIES	NTJT	300
Ł	LBAD = 0	NT.TT	310
	50 READ 1000. HED	NT IT	320
	TE (HED(1) . ED. END) GD TO BODO		JEL
	C+++++ETNAL CARD TN DECK MILLY DEAD+ END +	NIJI	336
	DEAD LAAD MUMME WUNEL MUMAE AREA METER WERE DEFENSION	NIJT	34C
Ŧ	READ 1009, NUMNP, NUMEL, NUMMAT, ACELX, ACELY, NRES, REFPRS, DEPTH,	NTJT	35C
	INANALY, NCONST, NPUNCH, NREAD	NTJT	36C
T	PRINT 2000, HED, NUMNP, NUMEL, NUMMAT, ACELX, ACELY	NTJT	37C
	PPINT 2070, REFPRS, DEPTH, NRES, NANALY, NCONST	NTJT	380
	IF (NANALY .EG. 0) PRINT 3800	NTJT	390
-	IF (NANALY ,EQ. 1) PRINT 3900	NTIT	400
ľ	C **** NANALYSO INITIAL STRESS METHOD WITH CONSTANT STRESSES	NTTT	1100
	C **** NANAL VET INTITAL STOFRE METHOD WITH CHANCING ATTERNED AT FAAN	NTUT	410
	P +++++TNPPENENT OF LOID	NIJI	420
-		NTJT	43C
	DI IN UNKEAU CO IJ PRINI 3510	NTJT	44C
	IF (NPUNCH .EQ. 1) PRINT 3520	NTJT	45C
	READ 1005, MJDINT, MTENS	NTJT	46C
-	IF (MJOINT .EQ. 0) GO TO 52	TLTN	470
	READ 1005, (MJNT(I), I=1, MJDINT)	NTIT	LAC
	PRINT 3200, (MJNT(I), 1=1, MJDINT)	NTTT	100
	52 TE (MTENS . FQ. 0) 60 TO 52	NIJI	446
	DEAD TARE (MNTEN/TY THE MERIAN	NIJT	500
	TLAU IVVDA LANDENARY THA NETRONAL	NTJT	510
	TRINT SSUDJEMNIENCESJENTENS)	NTJT	52C
	55 CUNTINUE	NTJT	53C
	DO 59 ME1, NUMMAT	NTJT	540
	READ 1001, MTYPE, RU(MTYPE), AKD(MTYPE)	NTIT	550
	C *** CRAC IS DECIMAL FRACTION OF TENSILE STRENGTH ADDITED TO PHERE NO	NT 101	556
	The second interview of the other of AFFLIED ID CHECK NU	NIJI	200

	c		
	し、大会	TENSION CONVERGENCE	NT.IT STC
-		READ 1030, (E(J,MTYPE), J=1,6), NTEST, CRAC(MTYPE)	NTJT SAC
		IF (MJUINT EQ. 0) GO TO 55	NT.IT SOC
	5/	VU 34 I=1,MJUINT	NTJT 60C
	54	PPTNE 2011 MANDE DECEMBER 10 58	NTJT 61C
11		FRINT 2011, MTTPE, HOLMTYPE), AKO(MTYPE), (E(J, MTYPE), J=1,6), NTEST	NTJT 620
R	C * * *	NTESTED TE C AND DUE DECEMBER	NTJT 63C
	C ± ± +	NTESTED IF C AND PHI OBTAINED FROM TRIAXIAL TEST	NTJT 64C
π.	•	ANGERIA HTYPEN OF DOCT	NTJT 65C
		F(6. MTVDE1+AND	NTJT 66C
8		TEINTEST ED AN CO TO EL	NTJT 67C
-		TANGETAN(ANG)	NTJT 68C
		FDESORT(9 +12 +TANC++3)	NTJT 69C
16		F(7. MTVPF) ETANC/FD	NTJT 70C
		E(8. MTYPE) 38 +E(5. MTYDE) (ED	NTJT 71C
1		GD TO 59	NTJT 72C
	56	SINAESTNIANGY	NTJT 73C
		CPSA=COS(ANG)	NTJT 74C
11		F0=1.732+(3.0-STNA)	NTJT 75C
		E(7, MTYPE)=2.0+STNA/FD	NTJT 76C
		E(8, MTYPE)=6.0*E(5. MTYPE)+COSA/EC	NTJT 77C
11		GN T() 59	NTJT 78C
11	58	PRINT 2017, MTYPE, (FLI, MTYPE), 1-1 EN	NTJT 79C
њ.,	59	CONTINUE	NTJT BOC
C	;	READ AND PRINT OF NODAL POINT DATA	NTJT B1C
		PRINT 2004	NTJT 82C
•		L = 1	NTJT 83C
	60	READ 1002. N,CODE(N),R(N),Z(N),UR(N),UZ(N)	NTJT 84C
11		IF (N = L) 100, 90, 70	NTJT 85C
Ц.	70	ZX=N=L+1	NTJT 86C
		DR = (R(N) - R(L-1)) / ZX	NTJT 87C
1		DZ = (Z(N) - Z(L-1)) / ZX	NIJT BEC
Ŀ.	80	CODE(L)=0.0	NIJI 89C
		R(L) = R(L-1) + DR	NIJI YUL
-		Z(L)=Z(L-1)+DZ	NIJI VIL
			NTIT 920
85	9.0		NT.IT QUC
	70	PRINT 2002, L, CUDE(L), R(L), Z(L), UR(L), UZ(L)	NT.TT OFC
I		IF (L. E.G. NUMNP) GO TO 110	NT.IT 960
1			NTJT 97C
	100	$\frac{1}{1} (N - L) = 00, 00, 00$	NTJT GAC
1	100		NTJT 99C
1			NTJT100C
	110	CONTINUE	NTJT101C
		NCAL F=1	NTJT102C
С		READ AND PRINT OF FLENENT DRODE STARS	NTJT103C
C		DETERMINE RAND WIDTH	NTJT104C
		PRINT 2001	NTJT105C
		MBAND = 0	NTJT106C
		N = 1	NTJT107C
	130	PEAD 1005, M. (IX(M.I). TE1.5)	NTJT108C
		DO 131 I=1,3	NTJT109C
		I1 = I + 1	NTJT110C
		DO 131 L = 11,4	NTJT111C
-			NT.TT1120

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1			
		KK = IAHS(IY(M, I) = IX(M, L))	NTJT113C
86	1 7 1	IF (KK .GE. NB) GU TA 179	NTJT114C
-	1 3 1	IF (KK e151 e MHAND) MHAND 3 KK TE (M - N) 180 170 150	NTJT115C
8	150	$\frac{1}{1} \left(\frac{1}{1} + \frac{1}{1} \right) = \frac{1}{1} \left(\frac{1}{1} + \frac{1}{1} \right)$	NTJT116C
64 -31	100		NTJT117C
		TY(N Z)=TY(N_4 Z)+4	NTJT118C
			NTJT119C
		TY(N-5)=TY(N-1-5)	NTJTIZOC
	170	PRINT 2003. N. (TY(N.T). T=1.5)	NTJTIZIC
П	•••	IF (N FR. NUMFL) OD TO 190	NTJ11220
		NEN+1	NTJ11230
		IF (M - N) 130, 170, 150	NTUT1240
i i	179	N = N + 1	NT 171340
н	180	PRINT 2018, M. KK. N	NTITIZOL
6.5		LBAD = LBAD + 1	NT.TT128C
		GO TO 130	NT.TT120C
н	190	CONTINUE	NT.ITI 30C
4 r		MBAND = 2 * MBAND + 2	NTJT131C
		PRINT 2012, MBAND	NTJT132C
11	C****	***************************************	***NTJT133C
	C	READ INITIAL STRESSES FOR THE PROBLEM, PRINT AS PART OF FIRST S	TEPNTJT134C
	C ***	************	***NTJT135C
T1		DO 32 N=1, NUMEL	NTJT136C
		STRS(N, 4)=0.0	NTJT137C
		00 32 I=1,3	NTJT138C
63	72	$\frac{\partial \mathbf{L} \mathbf{F}(\mathbf{N}_{f} \mathbf{I}) = 0_{0} 0}{\mathbf{O}_{f}(\mathbf{N}_{f} \mathbf{I}) = 0_{0} 0}$	NTJT139C
11	36	TE (NPER LE AN CO TO 44	NTJT140C
			NTJT141C
1			NTJT142C
Ш		SENT RESTRUCT STRESS ARE GENERATED FROM WHICH RESTRUCT TOAD ON A	NTJT143C
u -	C+NRES	BEO RESTOUAL STRESS APE GENERATED BUT DESTDUAL LUAD LALL	ULANTJT144C
	C+NRES	SEL RESTOUAL STRESS ARE INPUT AS DAYA FROM WHICH DESTOUAL LOAD	CENNETTER CENNE
H	C+NRES	SE2 RESIDUAL STRESS ARE INPUT AS DATA BUT RESIDUAL LOAD TO TED	GENNIJI140L
4.1	C*NPE!	SE3 COMPUTE RESIDUAL STRESSES REFORE ANALYSIS FOR COMPUTING FOR	FR NT "T1//00
	C****	*** UN EXCAVATED FACE*******	NT.TTIMOC
* .	47	READ 1007, N. (STRS(N.I), I=1,4)	NTITISAC
		IF(N-L) 40,41,42	NT.1T151C
	42	DO 46 I=1,4	NTJT152C
1	46	STRS(L,I)=STRS(L=1,I)	NTJT153C
١.	41	IF (L .EQ. NUMEL) GO TO 45	NTJT154C
		L=L+1	NTJT155C
		IF(N - L) 47, 41, 42	NTJT156C
H.	40	LBAD=LBAD+1	NTJT157C
£ 6		PRINT 1008, N, LBAD, L	NTJT158C
		GD TO 47	NTJT159C
1	45		NTJT160C
49		PRINT LAAT IN CATROLY IN THE AND A CONTRACT	NTJT161C
		TE (MIOINT ED AN CO TO ""	NTJT162C
		TE CHOUINT SEUS UT GU T() 44 DEAD AIAAA NIT (EN(T) ET/T) NETBATY DEA MATH	NTJT163C
ala		PRINT HOUPHULFFULTS AFTER FLANDING	NTJT164C
		CO TO 44	NTJT165C
1	48	DO 210 N = 1. NUMEL	NTJT166C
		MTYPE=IX(N.5)	NTJT167C
			NTJT168C

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 $I = I \times (N_{1} + 1)$ NTJT169C J=IX(N,2)NTJT170C K=IX(N,3) NTJT171C L=IX(N,4) NTJT172C IF (K .EQ. L) GO TO 204 NTJT173C ZZZ(5) = (Z(I) + Z(J) + Z(K) + Z(L)) + 0.25NTJT174C GO TO 205 NTJT175C 204 ZZZ(5)=(Z(I)+Z(J)+Z(K))/3. NTJT176C 205 IF(RD(MTYPE).FQ.0. . AND. E(2.MTYPE) .LE. 1.)GU TU 210 NTJT177C CALL INITST NTJT178C 210 CONTINUE NTJT179C NRES=0 NTJT180C 44 CONTINUE SOLVE NON-LINEAR STRUCTURE BY SUCCESSIVE APPROXIMATIONS NTJT181C C NTJT182C DO 350 N=1, NUMEL NTJT183C EPS(N)=0.0 NTJT184C MTAG(N)=1 NTJT185C 350 CONTINUE NTJT186C READ 1005, NCPSNT, NPRSNT, ITPSNT NTJT187C PRINT 6000, NCPSNT, NPRSNT, ITPSNT NTJT188C IT1=ITPSNT NTJT189C NPRS1=NPRSNT NTJT190C NELPNCH=0 NTJT191C DO 900 NETENCESNT, NEONST NTJT192C IF(NCT.GT.1) NRES=0 NTJT193C IF (NCT. GT. NCPSNT) NPRSNT=1 NTJT194C READ 1000, TITLE NTJT195C READ 1005, NEPSP, NUMPC, NPF, NPCAV, NP, NGLD, MTRM, NSPT NTJT196C IF (NCT.EQ.NCPSNT) NP1=NP NTJT197C PRINT 6001, TITLE, NERSP, NUMPC, NPF, NPCAV, NP, MTRM, NSPT NTJT198C C** NSPT = 1 IF THERE IS LINER FOR THIS CONSTRUCTION STEP C** NSPT = 0 IF THERE IS NO LINER FOR THIS CONSTRUCTION STEP NTJT199C NTJT200C IF (NGLD .EQ. 1) PRINT 6200 NTJT201C IF(NCT.GT.NCPSNT) GO TO 610 NTJT202C IF (NPRSNT.LE.NP) GO TO 610 NTJT203C PRINT 3600 NTJT204C GO TO 9000 NTJT205C 610 CONTINUE NTJT206C IF(NERSP.LE.0) GO TO 810 NTJT207C NELPNCH=NELPNCH+1 NTJT208C NCALC=1 NTJT209C PEAD 1005, (NE(I), MT(I), MSP(I), I=1, NERSP) NTJT210C PRINT 6002 NTJT211C PRINT6007, (NE(I), MT(I), MSP(I), I=1, NERSP) * MT(I) = MATERIAL NO. ASSIGNED FOR NIT = 1 NTJT212C C * MSP(I) = MATERIAL NO. ASSIGNED FOR NIT GREATER THAN 1 NTJT213C NTJT214C 810 IF (NUMPC.EQ.0) GO TO 820 NTJT215C PRINT 2005 NTJT216C READ 1005, ((IJBC(L, I), I=1,2), L=1, NUMPC) NTJT217C PRINT 2007, ((IJBC(L,I), I=1,2), L=1, NUMPC) NTJT218C READ 1005, NPBCP NTJT219C PRINT 2050 NTJT220C DO 815 ME1, NPBCP NTJT221C READ 1020, NPBC(M), (PSCA(M, I), I=1, 3) NTJT222C PRINT 1020 , NPBC(M), (PSCA(M, I), I=1, 3) NTJT223C 815 CONTINUE NTJT224C

820 CUNTINUE NTJT225C IF(NPF.EQ.0) GO TO 840 NTJT226C PRINT 6005 NTJT227C DU 830 I=1,NPF NTJT228C READ 1002 , N, CODE(N), UR(N), UZ(N) NTJT229C PRINT 6008, N, CODE(N), UR(N), UZ(N) NTJT230C 830 CONTINUE NTJT231C 840 CONTINUE NTJT232C IF (NPCAV.EQ.0) GO TO 850 NTJT233C PRINT 6006 NTJT234C READ 1010, (NS(I), (NSEL(J,I), J=1,4), I=1, NPCAV) NTJT235C PRINT 4000. (NS(I), (NSEL(J,I), J=1,4), I=1, NPCAV) NTJT236C READ 1005, NCAVPC NTJ1237C READ 1005 , ((IJBCA(L,I),I=1,2),L=1,NCAVPC) NTJT238C PRINT 2005 NTJT239C PRINT 2007 , ((IJBCA(L,I),I=1,2),L=1,NCAVPC) NTJT240C 850 CUNTINUE NTJT241C IF THE PRESENT CONSTRUCTION STAGE IS NOT THE FIRST ANALYSIS OF C*** NTJT242C THIS RUN NPRSNT=1 С NTJT243C READ 1040 , (ITN(N), PRATID(N), N=NPRSNT, NP) NTJT244C C** ITN .GE.2IF NSP = 1 NTJT245C PRINT 3400, ((N, ITN(N), PRATIO(N)), NENPRSNT, NP) NTJT246C IF (NCT .GT. NCPSNT .OR. NREAD .NE. 1) GO TO 860 NTJT247C READ (5) ((STRS(N,I),SEP(N,I),I=1,3),STRS(N,4),MTAG(N),N=1,NUMEL) NTJT248C IF (MJDINT ,EQ. 0) GD TO 860 NTJT249C READ (5) NJT, (FN(N), FT(N), N=1, NJT) NTJT250C 860 IF (NPCAV .EQ. 0) GO TU 861 NTJT251C CALL NPSTRS(NSEL, NPCAV) NTJT252C 861 CONTINUE NTJT253C IF(NERSP LE. 0) GO TO 870 NTJT254C DO 865 I=1, NERSP NTJT255C N=NE(I) NTJT256C MTAG(N)=1 NTJT257C IF (MTRM .EQ. MT(I)) GO TO 863 NTJT258C GO TO 865 NTJT259C 863 MTAG(N)=0 NTJT260C DO 864 J=1,4 NTJT261C STRS(N,J)=0.0 NTJT262C 864 CONTINUE NTJT263C 865 CONTINUE NTJT264C 870 CONTINUE NTJT265C NTJT266C DO 500 NNNENPRSNT, NP ITAPE=0 NTJT NISTOP=0 NTJT267C ITNP=ITN(NNN) NTJT268C -IF (NNN.GT.NPRSNT.OR.NCT.GT.NCPSNT) ITPSNT=1 NTJT269C . DO 450 NITEITPSNT, ITNP NTJT270C NYD = NTJT271C Ĩ DD 872 N = 1, NUMEL NTJT272C IF (MTAG(N) , GE, 4) NYD = NYD + 1 NTJT273C 872 CUNTINUE NTJT274C IF(NIT .GE. 3) GO TO 890 NTJT275C 1 IF (NERSP .EQ. 0) GO TO 890 NTJT276C IF (NSPT .EQ. 0) GO TO 875 NTJT277C IF (NIT .EQ. 1) GO TO 875 NTJT278C IF (NIT .EQ. 2) GO TO 880 NTJT279C GO TO 890 NTJT280C

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875 DU 877 I=1, NERSP B-6 N = NE(I)877 IX(N,5) = MT(I) GO TO 890 880 DU 881 I=1, NERSP N = NE(I) IF(MSP(I) .NE. MTRM) MTAG(N) = 1 BB1 IX(N,5) = MSP(I)890 CONTINUE IF (NNN .EQ. 1 .AND. NIT .EQ. 1) NCALC = 1 TF (NANALY .ER. O .AND. NSPT .ER. 0) GU TO 200 IF (NANALY .EQ. 0 .AND. NSPT .EQ. 1) GO TO 220 IF (NANALY .EQ. 1 .AND. NSPT .EQ. 0) GO TO 240 IF (NANALY .EQ. 1 .AND. NSPT .EQ. 1) GO TO 260 CALL EXIT 200 IF (NNN .EQ. NPRSNT .AND. NIT .EQ. ITPSNT) NCALC = 1 IF (NNN .NE. NPRSNT . UR. NIT .NE. ITPSNT) NCALC = 4 GO TO 270 220 IF (NNN .ER. 1 .AND. NIT .ER. 2) NCALC = 2 IF (NNN .ER. 1 .AND. NIT .GT. 2) NCALC = 5 IF (NNN .GT. 1 .AND. NIT .EQ. 1) NCALC = 4 IF (NNN .GT. 1 .AND. NIT .GT. 1) NCALC = 5 GO TO 270 240 IF (NIT .GE. 2) NCALC=3 IF (NIT .GT. 2 .AND. ITAPE .EQ. 1) NCALC=6 IF(NYD .EQ. O .AND. NIT .GE. 2) NCALC = 4 IF (NNN .GT. 1 .AND. NIT .EQ. 1) NCALC = 4 GC TO 270 260 IF (NNN .EQ. 1 .AND. NIT .EQ. 2) NCALC = 2 IF (NIT .GE. 3) NCALCES IF (NIT .GT. 3 .AND. ITAPE .EG.1) NCALCES IF(NIT .GE. 3 .AND. NYD .EQ. 0) NCALC = 5 IF (NNN .GT. 1 .AND. NIT .EQ. 1) NCALC = 4 1 IF (NNN .GT. 1 .AND. NIT .EQ. 2) NALC = 5 270 CONTINUE MTAP1 = 80 MTAP2 = 90 IF (NCALC .ER. 2 .OR. NCALC .ER. 5) GO TO 280 IF (NCALC .EQ. 3 .DR. NCALC .ER. 6) GD TO 285 GD TD 290 280 MTAP1 = 50 MTAP2 = 60GO TO 290 285 MTAP1 = 30 MTAP2 = 40 ITAPE=1 290 CONTINUE PRINT 3100, NNN, NIT CALL SECOND(T1) IF (NIT .EQ. 1 .OR. NCALC .EQ. 1) GO TO 357 IF (NCT. GT. NCPSNT) GU TO 760 IF (NNN.EQ.NPRSNT.AND.NIT.EQ.IT1) GO TU 357 760 IF (NPF.GT.0) GO TO 770 IF (NNN .EQ. NPRSNT .AND. NIT .EQ. IT1) GO TO 357 IF (MJOINT .EQ. 0) GO TO 355 770 DU 354 N=1, NUMNP IF (ABS(UR(N)) .LE. 1.) GO TO 354 ÷ · ·

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NTJT281C

NTJT282C

NTJT283C

NTJT284C

NTJT285C

NTJT286C

NTJT287C

NTJT288C

NTJT289C

NTJT290C

NTJT291C NTJT292C NTJT293C NTJT294C

NTJT295C NTJT296C

NTJT297C

NTJ7298C NTJT299C NTJT300C

NTJT301C

NTJT302C

NTJT303C

NTJT304C NTJT306C

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NTJT330C

NTJT331C

NTJT332C

NTJT333C NTJT334C

NTJT335C

NTJT336C

NTJT

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JF (ARS(HZ(N)) .LE. 1.) GO TO 354
                                                                                NTJT337C
         NISTOP=NISTOP+1
                                                                                NTJT338C
  C****
                                                                                N/JT339C
  C*****
                                                                                NTJT340C
     354 CONTINUE
                                                                                NTJT341C
     355 CONTINUE
                                                                                NTJT342C
         IF (NNN.E9.1.AND.NSPT.EQ.1.AND.NIT.EQ.2.AND.NISTOP.GT.0) GO TO 357NTJT343C
         IF (NISTOP .ER. 0) GO TO 460
                                                                                NTJT344C
     357 CONTINUE
                                                                                NTJT345C
  Ĉ
         FORM STIFFNESS MATRIX
                                                                                NTJT346C
         CALL STIFF
                                                                                NTJT347C
         CALL SECOND(T2)
                                                                                NTJT348C
         IF (LBAD .NE. 0)
                            GO TO 8950
                                                                                NTJT349C
  C
         SOLVE FOR DISPLACEMENTS
                                                                                NTJT350C
         CALL BANSOL (NNN, NIT, NCALC)
                                                                                NTJT351C
44
  C
                                                                                NTJT352C
         CALL SECOND(T3)
                                                                                NTJT353C
         PRINT 2016
                                                                                NTJT354C
         DO 360 NE1, NUMNP
                                                                                NTJT354C
         DO 360 I=1,2
                                                                                NTJT356C
    360 DISP(N,I)=0.0
                                                                                NTJT357C
         DO 361 NE1, NUMEL
                                                                                NTJT357C
         DO 362 I=1.3
                                                                                NTJT359C
    362 STRN(N, I)=0.0
                                                                                NTJT360C
         FY(N)=-1000.
                                                                                NTJT361C
    361 CONTINUE
                                                                                NTJT362C
         IF (NNN .EQ. 1 .AND. NIT .EG. 1.AND.NCT.EQ.1) GO TO 380
                                                                                NTJT363C
         IF (NREAD, EG. 1. AND, NNN, EQ. NPRSNT, AND, NIT, EQ. IT1) GO TO 370
                                                                                NTJT364C
         REWIND 3
                                                                                NTJT365C
        READ (3) ((DISP(N,I),I=1,2),N=1,NUMNP),(FY(N),(STRN(N,I),I=1,3),
                                                                                NTJT366C
       1N=1, NUMEL)
                                                                                NTJT367C
        GD TD 380
                                                                                NTJT368C
    370 READ (5) ((DISP(N,I),I=1,?),N=1,NUMNP),(FY(N),(STRN(N,I),I=1,3),
                                                                                NTJT369C
       1N21, NUMEL)
                                                                                NTJT370C
    380 00 400 N=1, NUMNP
                                                                                NTJT371C
        N2=N+2
                                                                                NTJT372C
        DISP(N, 1)=DISP(N, 1)+B(N2=1)
                                                                                NTJT373C
        DISP(N,2)=DISP(N,2)+B(N2)
                                                                                NTJT374C
        PRINT 2006, N.B(N2-1), B(N2), CODE(N), DISP(N, 1), DISP(N, 2)
                                                                                NTJT375C
    400 CONTINUE
                                                                                NTJT376C
        IF (NGLD.NE.1) GO TO 410
                                                                                NTJT377C
        DO 405 N=1, NUMNP
                                                                               NTJT378C
        DISP(N,1)=0.0
                                                                                NTJT379C
        DISP(N,2)=0.0
                                                                                NTJT380C
    405 CONTINUE
                                                                               NTJT381C
    410 CONTINUE
                                                                               NTJT382C
  C
        COMPUTE STRESSES
                                                                               NTJT383C
        NISTOP=0
                                                                               NTJT384C
        CALL STRESS
                                                                               NTJT385C
 C
        RESET UP AND UZ EQUAL TO ZERO
                                                                               NTJT386C
        IF( NIT .GE. 2) GO TO 415
                                                                               NTJT387C
        IF(NERSP.EQ. 0) GD TO 415
                                                                               NTJT388C
        00 414 I = 1, NERSP
                                                                               NTJT389C
        IF ( MTRM
                   .NE.
                         MT(I)) GO TO 414
                                                                               NTJT390C
        N = NE(I)
                                                                               NTJT391C
        0^{1} 413 J = 1,3
                                                                               NTJT392C
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1			
	413	CONTINUE	NTJT3930
	414	CANTINUE	NTJT3940
	415	CONTINUE	NTJT3950
			NT.IT3940
1			NT.173070
			NT : TTOPO
-			NT 177000
	480	CONTINUE	N101344C
2		IF(HJUINT,EQ.0) GO TO 409	NTJT400C
		CALL JTSTR	NTJT401C
1	409	CONTINUE	NTJT402C
J		REWIND 3	NTJT403C
		WRITE(3) ((DISP(N.T), TEL 2) NEL NUMBER (EVAN)	NTJT404C
		1N=1, NUMEL)	NTJT405C
1		CALL SECONDETAN	NTJT406C
		TTET4-TI	NTJT407C
		T1=T2=T1	NT.IT408C
17			NT.IT409C
-1			NTITHIAC
			NT.TT#11C
	1150	NREAUE()	NTITULDE
	450	CUNTINUE	NIJ1412L
19	400	LUNTINUF	NIJT413C
	500	CONTINUE	NTJT414C
11	400	CONTINUE	NTJT415C
	C****	PUNCH OUT INITIAL STRESSES FROM GRAVITY TURN-ON ANALYSTS	NTJT416C
46		IF (NGLD NE. 1 OR. NRES NE. 1) CO TO 510	NTJT417C
		PUNCH 1000, HED	NTJT418C
11		PRINT 1007, (N. (STRS(N. T), TEL (), NET WINELS	NTJT419C
		PUNCH 4300 . (N. (STRSIN, T), THE AN WEAK HELD	NTJT420C
	510	CONTINUE (CONTINUE)	NTJT421C
		IF (NPUNCH NE. 1) GO TO 400	NTJT422C
н		PUNCH 1000, HED	NTJT423C
4.		PINCH 3700 NEGURA UD	NTJT424C
		TEINEL BACH LE AN OR TO THE	NT.TT425C
T		DUNCH ALLAN NEL DUAL	NT.IT426C
Ш			NT 17/1270
	534	PUNCH 1015, ((M, (IX(M, I), I=1, 5)), M=1, NUMEL)	NT 17/1200
-	260	WRITE(1) ((STRS(N, I), SEP(N, I), I=1, 3), STRS(N, 4), MTAG(N), NEL, NUMELS	NTJ1420C
н		IF (MJUINT .EQ. 0) GO TO 550	N1J1429C
44		WRITE (1) NJT, (FN(N), FT(N), N=1, NJT)	NIJI450C
	220	CONTINUE	NTJT451C
-		WRITE(1) ((DISP(N,I), I=1,2), N=1, NUMNP), (FY(N), (RTPN/N, T), TAT	NTJT432C
а.	1	N=1, NUMEL)	NTJT433C
10	600	CONTINUE	NTJT434C
~		GO TO 50	NTJT435C
	1000	FORMAT (BA10)	NTJT436C
5.	1001	FORMAT (15.2F10.5)	NTJT437C
	1002	FORMAT (15.F5.0.5F10 A)	NTJT438C
7	1004	FURMAT (215-FIG A)	NTJT439C
1	1005	FORMAT (1ATS)	NTJT440C
	1006		NTJT441C
	1	TPESSAY, THYATDERATY ANY TAL STRESSE S/SHOELEMENT3Y. THYS	INTJT442C
1	1007	ENDERT THE WEAR IN THE STRESS)	NT.174420
1	1007	CONTAL (10,4215.5)	NT 17/14436
	1008	UNMAIL RESIDUAL STRESS INPUT ERROR, Nat, 110. +LBADat, TIA. +L - TIA.	NT 17444C
	1004	URMAT (SI5,2F10.2,15,2F10.5,4I5)	1014450
	1010	11RMAT (515)	NTJT446C
•	1015	URMAT(615)	NTJT447C
			NTJT44AC

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	e u	1	1	11	JR	M	A T	(40	10	X	, 1	5	НМ	A '	TE	FI	AL		101	MB	ER	15	51	1 H	06	X	.2	HK	N1	3X	. 2	HK	T 1	4 X	. 1	нс	11	XY	- 31	NT.	17	47	60
			1	H	PH	11	3 X	.1	21	HM	AX		C	1	03	UF	RE	15	E1	5.	4)									-		-		•		• •			2			++		
	20	1	8	FI	DR	MA	T	(11	5 H	F	L	FM	F	NT	(- 4	RD	N	in	6	. 5	٧.	4		-	- 1		=	~	.	NE			1200	• .	ĭ					41.	110	47	12
	20	1	9	FI	h	M	T	Ì	2	Z H		11.13			0	0		ED	ne	in a			~ *	-			• 1	. 4 (12	4.	eΠ	NE	XT	N	-	16)				- 1	NT.	JT/	471	8C
	21	5	6				-			2 11					-	Or			RL	182		-0	UN	101	4)															1	NT.	JT (47	90
	20	5		-	JR			5	1.	2	01	1	M I	NI	•	31	I	FF	F		5.	5 X	. 6	HE		NS	αL	Fl	8.	3,	5 X	,9	HI	TE	RA	TI	ON	Fa		3)	1	NT.	TT	44	oc.
	20	5	Q	Ft	JR	M	AT.	(1	•0	PL	A (NE		S T	R/	11	N	AN	AL	. YS	SI	9	OF	۰.	JO	IN	TE	ED	S	TR	UC	TU	RE		1			•••			NT.	14		10
	SC	5	0	F()R	MA	T	(2	5 H	1	N	ĪT	1	AL		31	RE	95	ES	3 /	AT	N	n	F	R	11	5	4	N.I	D				10	í.								# C)	
			1	Y				S I	G	YY)				-			_		-							/ -			•••	•			9	10	AA				211	a T I	41.	111	40	20
	20	7	0	FI	P	м /	T	1	5		11 .				t •	•	4		* *	E e			-	-								_									1	NT.	JT	48	3C
		'		-	, n			- L	21	11			¥ C.		11	6.4	L.	3	IN	ES	55	•	T	RŁ	P	ER	EN	CE		PQ:	IN	T	(P;	3F)=	F	20	.2	!/		1	VT.	JT/	48	4C
			1	2	1	54	114	EL	. E 1	A	11	CH	N	A	T	RE		ER	EN	CE		P0	IN	T	(FŤ)=	-	:5	0.1	21	5X	, 51	IN	RE.	5=		Ī1	0		1	NT.	TTI		50
			C		.7	HI	Y	PE	. (JF	A	N		Y	5 I	3=	8	, I	5/	5)	11	27	HN	0.	(T	C	ON	13	TRI	JC	TI	N N	3	TE	PQ		. 1	5.	11	1 1	T	17/		50
4	30	0	2	Fr	R	MA	T	(1(DF	7.	4)											-					-					v	1.61			. 7			, ,	414		101	
	31	0	0	FC	R	MA	T	1	1	11	AH	0	NO		0	F	1	NC	DF	ME	-	-		16		e v		7.		-		-				• -					r	4Th	114	18	70
	22	•	ñ	Fr	סו		-	2	20	3.4	M		•	۰.	0		-						-!	13		7 ×		1		1.	U	۳	ITI	R R	AT.	10	ŊE		15	5/:))	VT.	114	480	30
	77	-		E.	-			Ľ	5	1	14		•	Г	VU V	•	- 1	J.K	J	01	NI		E L	EM	E	NT	9 3		11	516	5)										1	VT.	JT (18	26
4	23	0	0	PL	IR	M A	T	(56	H	M	A '	T a	P	VD		W	HI	СH	C	AN	1	SU	ST	4	IN	T	EN	VS:	10	NE		12	16)							TT.	TT	191	hr
	34	0	0	FC)R	MA	T	(21	\mathbb{R}	L	01	D	IN	NG	1	N	CR	EM	EN	T	N		.1	5.	.5	Υ.	31	H	Nn		nF	T	FFI			DNI	•		70	-		++ /		
			1	HI	18	1	N	CR	EN	E	NT	1		. 1	15	. 5	Y.	. 3	1 H	PF	Rr	F	NT	AC	F	n	E	00	55	0.01	ini	61 E	1 11				UN4	3	r L	JE.	1 7	414	114	• •	
	35	0	0	FC	IR	MA	T	1	1	12	14			6		ALT		0	-	7 1	-	-			1.4.0				E	331	JR	E _ (API		121		•	r 1	0.	12		4T.	114	192	2C
		•	•					-						5.4		N I		-0	AU	10	0	1	NC	RE	M	N	T_	NC]•1	••]	15	, 5	X	. 41	4Ι,	TE	RA.	1I	ON	N M	101	IT.	174	193	5 C
			1	• 1		12	1				RE	A)=		15	/	8	•	N3	τ.	RŢ		, I	5,	5)	(,)	63	HN	13.	t SF	11	. NI	E. (811	RES	531	ES	1	IN	RH	UT.	11/	191	10
			2	•]		0 I	R	EC	11	0	NS		N I	LL		AL	.80	5	BE	P	RI	IN'	TE	D	OL	JT.	1	3					-			_								105	-
	35	1	0	FC	R	MA	T	(1	51	•	**	**		42	2H	DA	T	1	FR	OM	1		ST.	T	Nr	P	FM	EN	17		36	DI	-				10								
7 5	35	2	0	FC	R	MA	T	(1	51		**	* *		64	H	DA	T		WT	11		F	0	4 1 A 2	CL	1E		0	-				- AL		-3	11		11		1	N	111	174	146	36
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	20	U I		PC	R	MA	T	(7	4⊦	. 1	R	E S	SE	NT		LC	140	1(NG	1	NC	R	EM	EN	T	N	D.	I	3	GF	RE I	ATE	R	TH	-	1 1	4	57	1	N	DA	IT	+	100	20
			1	EN	E	NT		NO		*1	15	TC	P(**	ł)																									1 11				
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			1			15		z	HA	10				5 1						U M	1.4			C	r 1	, N 1	•	A	I'N L	1 6		LE	33	31	RE	: 33	501	AC.	OV	131	TEN	IT J	115	01	. C
1	20		•		-		-	3	111	11.			1	3)										-																	N	ITJ	TE	102	25
	30	(1)				A P	-	(Ħ	U	11	NG		IN	II.	II	AL		ST	RE	55	1	٩E	TH	OC) i	N T	TH	C	ON	18	TAN	T	S1	TF	FFN	NES	2.5	+)		N	17.		107	C
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																							-													141	- 00		- 1	C	, # N	114	12	996	

B-9

1CH INCREMENT OF LOAD BUT CHANGING STIFFNESS IN SUBSEQUENT ITERATIONTJT505C 2NS+) NTJT506C 4000 FORMAT(//* N.P. ALONG EXCAVATED FACE SURROUNDING ELEMENTS * / NTJT507C * (I20,10X,415)) NTJT508C 4100 FORMAT(15/(2F20.5,15)) NTJT509C 4200 FORMAT (///* INITIAL NORMAL AND TANGENTIAL STRESSES FOR JOINTS*// NTJT510C 1 * JOINT NO. NORMAL STRESS TANGENTAL STRESS EL. NO. */(NTJT511C 2 I10,2E15.5,I10)) NTJT512C 4300 FORMAT (* INITIAL STRESSES*/(15,4E15,5)) NTJT513C 6000 FORMATC NTJT514C 1 50HO NUMBER OF PRESENT CONST. STEP-----15/ NTJT515C 2 50HO NUMBER OF PRESENT LOAD INCREMENT------15/ NTJT516C 3 50HO NUMBER OF PRESENT ITERATION -----15/) NTJT517C 6001 FORMAT(1H1,8A10// NTJT518C 1 5X,* FOLLOWING DATA ARE REQUIRED FOR PRESENT CONSTRUCTION STAGE* NTJT519C 2 //5X, +NUMBER OF ELEMENTS TO BE EXCAVATED AND OR FOR STRUCTURAL NTJT520C 3SUPPORT = +, I10,/5X, + NUMBER OF PRESSURE CARDS = +, I10,/5X, + NTJT521C ANUMBER OF NODAL POINTS AT WHICH FORCES ARE APPLIED +, 110, / 5x, NTJT522C 5*NUMBER OF NODAL POINTS ALONG CURRENT EXCAVATED FACE REGIRED FOR NTJT523C 6 EXCAVATION SIMULATION = *, I10, /5X, * NUMBER OF LOAD INCREMENTS = *NTJT524C 7, I10/ 5X, * MATERIAL TYPE FOR EXCAVATED ELEMENTS= *, I10/ NTJT525C A 5X,* INDEX(=1 IF THERE IS LINER) FOR LINER = +, I10//) NTJT526C 6002 FORMAT(// 5X, * MATERIAL TYPE FOR FOLLOWING ELEMENTS ARE CHANGED NTJT527C 1 AS INDICATED #//5X, * ELEMENT NO. *, 5X, NTJT528C 2 *MAT. TYPE(NIT=1)*, 2X, *MAT. TYPE(NIT GT 1)*) NTJT529C 6005 FORMATE //5X, *FULLOWING BOUNDARY CONDITIONS ARE CHANGED FOR CURRENNTJT530C IT CONST. STAGE *,//1X,* NODAL POINT*,2X,* TYPE*,2X,* X LOAD OR DISNTJT531C 2PLACEMENT +, 2X, + Y LOAD OR DISPLACEMENT +) NTJT532C 6006 FORMAT(// 5%, * PRESSURE BOUNDARY CONDITIONS TO SIMULATE EXCAVATIONNTJT533C 1 -) NTJT534C 6007 FORMAT (2112,120) NTJT535C 6008 FORMAT(18, F9.2, 2E30.5) NTJT536C 6100 FORMATE * ELEMENT PROPERTY HAS BEEN CHANGED *, 15, 2X, * TIMES*; NTJT537C 6200 FORMAT(// 5X, + THE PRESENT STEP IS GRAVITY TURN ON TO OBTAIN NTJT538C * INITIAL STRESSES * //) NTJT539C C NTJT540C 8950 PRINT 2019, LBAD NTJT541C 9000 CONTINUE NTJT542C END NTJT543C

B-10
1		SUBROUTINE NPSTRS(NSEL, NPST)	NPST	10
		COMMUN /ELDATA/IX(900,5),MTAG(900),EPS(900),STRS(900,4),SEP(90	0.31NPST	20
		COMMON /NPDATA/ R(999),7(999),CODF(999),UR(999),U7(999)	NDST	20
		COMMON INPS/ PSCAV(75.3) TIBCA(50.2) NO(75)	NDOT	50
T			NPSI	46
		01 MENAION L(4,4), F(3,4), NSEL(4,50)	NPST	50
		PHINT 1005	NPST	60
		DD 500 I=1, NPST	NPST	70
		NC=NS(I)	NPST	AC
44		DO 200 Jai.4	NDCT	00
		MMENSFL(J.T)	NPOT	
			NPSI	100
			NPST	110
14			NPST	120
		KNEIX(MM,3)	NPST	13C
		LN#IX(MM,4)	NPST	140
		XX = (R(IN) + R(JN) + R(KN) + R(LN)) + 0.25	NPST	150
2.1		YY=(Z(IN)+7(JN)+7(KN)+7(LN))+0.25	NDET	140
			NPOT	100
111			NPST	170
			NPST	180
2.1	200		NPST	190
	500		NPST	202
		DO 380 NE1,4	NPST	215
		D=C(N,N)	NPST	220
4.4		DO 330 J=1,4	NDET	370
	330	C(N, I) = C(N, I) / D	NFOT	230
			NPSI	240
11			NPST	250
			NPST	292
		111 300 J=1,4	NPST	27C
		IF (N .EQ. J) GO TU 360	NPST	28C
de la	_	C(K,J)=C(K,J)+C(K,N)+C(N,J)	NPST	290
	360	CONTINUE	NPST	300
	370	C(K,N)=C(K,N)/D	NPST	310
		C(N,N)=1-/D	NDOT	320
1.1	380	CONTINUE	NEST	320
		DD 300 K=1.3	NPST	330
			TPST	34C
			NPST	35C
2.2	240	r(x,L)=0.0	NPST	36C
		UN 450 K=1,3	NPST	37C
E.		DO 450 L=1,4	NPST	380
1.		DO 450 Ma1,4	NPST	200
		MMENSEL (M.I)	NDOT	100
		F(K,L)=F(K,L)+C(L,M)+STPS(MM,K)	NPSI	400
11	450		NPST	410
11			NPST	420
		NO HOU NEIJS	NPST	43C
-	460	$P_3CAV(1,K) = F(K,1) + F(K,2) + R(NC) + F(K,3) + 2(NC) + F(K,4) + R(NC) + 2(NC)$	NPST	44C
		PRINT 1007, NC, (PSCAV(1,K), K=1,3)	NPST	45C
-	500	CONTINUE	NPST	460
		RETURN	NPST	470
-	1005	FORMAT (1H1, /* N.P. SIGXY STOVY STOVY	NDET	HAC
	1007	FORMAT (15, 3E15.5)	NDOT	400
90		FND	NFSI	446

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B-12

1			
I care	SUCKULINE STIFF	STIF	10
C T T T	A CALCULATION OF STIFFNESS MATRIX FOR FIRST STEP ONLYIFNANALYRO	STIF	20
C#**	* CALCULATION OF B ARRAY FOR EACH TIME STEP	CTTE	20
	COMMON / / NUMNP, NUMEL, NUMMAT, NUMPC, ACELY, ACELY, HEDRAS MININ NO	ETTE	36
11.	1 NPCAV, REFPRS, DEPTH, NRES, N. VOL, NCALC, TRACK, MIDTHE MEDICOL, NON, NP,	9116	40
	2 ITN(20), PRATIO(20), NIGTOR, NEED NOTOR NAME NOT NAME NOT	STIF	50
	3. NET. NEANST. NEARED, NEAVER	STIF	60
	COMMON /HATR/ MTYPE DO/125 CAR ADD HUDIEL	STIF	70
-	COMMON /MATE/ MITPE, RU(12), E(8, 12), AKD(12), MNTEN(12), MJNT(12)	STIF	80
	J (RAC(12)	STIF	90
11	CIMMUN /ELDATA/IX(900,5), MTAG(900), EPS(900), STRS(900,4), SEP(900,7)	USTIF	100
	CUMMON /NPDATA/ R(999), Z(999), CODE (999), UR(999), UZ(999)	CTTE	1100
0	COMMUN /PSLD/ IJBC(50,2), PSCA(75,3), NPBC(75)	OTTE	110
	COMMON /NPS/ PSCAV(75,3), IJBCA(50,2), NS(75)	9111	120
1	COMMUN /BANARG/ B(90) . B2(90) . A(90. 90) . A2(90. 90) MBAND NOD ANIMENT	3114	130
6	1 MBMAX, NR, MTAP1, MTAP2	STIF	140
	COMMON /ARG/ REP(5) 777(5) 8(10 10) D(10) DOPDOTAL LOUD	STIF	15C
	ANGLESS VILLESS VILLES	STIF	16C
	E(4,4),EE(4),H(6,10),D(6,6),	STIF	170
6.0	CONHON (1) (510(6), SIG(6), DSIG(6), RR(4), HSEL(31,4), DSIGZ	STIF	180
	$V_{JN1} = V_{JN1} + V_{450}, F_{1450}, N_{J}$	STIF	190
	NDEMBMAX	STIF	200
L	INITIALIZATION	STIF	210
- F	NISTOPEO	RTIE	220
	PPINT 2010	ATTE	220
	REWIND 9	3111	230
	IF (MTAP1 .EQ. 90) PRINT 3000. NEALE	3115	240
	IF (MTAP1 .ER. 30) PRINT 3010, NOALC	STIF	22C
	IF (MTAP1 FR. 50) PRINT 3020, NEALC	STIF	26C
300	O FORMATC// 10% + THIS TTERATION HORE FLIGTE CONTRACTOR	STIF	270
	18 + 5Y + NCALCHA IS THERATION USES ELASTIC STIFFNESS WITHOUT LIN	ESTIF	280
301	$ = \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum$	STIF	290
201	A NCALCE TELLS ITERATION USES TANGENT STIFFNESS *, 5X,	STIF	300
202	1 + N(AL(EW, 1)//)	STIF	310
205	FURMAT(7/ 10X, * THIS ITERATION USES ELASTIC STIFFNESS WITH LINER	+STIF	320
	1 , 5%, + NCALC=+, 15//)	STIF	320
	REWIND MTAP1	RTTE	330
	REWIND MTAP2	OTTE	340
	NUMBLKED	9111	336
	NJTEO	STIP	300
	00 49 N=1,ND	STIF	370
40	9 B2(N)=0.0	STIF	380
	TE INCALE ST. 31 GD TD AN	STIF	390
	ASSIGN 170 TO NEYT	STIF	400
	DO SO NEL NOS	STIF	41C
		STIF	42C
5/		STIF	430
50	$J = (H_0 N) = U_0 0$	STIF	44C
L	FIRM STIFFNESS MATRIX IN BLOCKS	STIF	450
0(D NUMBLK=NUMBLK+1	STIF	146
	NHENB+(NUMBLK+1)	OTTE	400
	NMENHENB	0111	476
8	NLENM-NB+1	9111	480
	KSHIFT=2+NL-2	STIF	490
C	ADD CONCENTRATED FORCES WITHIN BLOCK	STIF	500
	00 250 NENLANM	STIF	51C
	TE(N GT NUMARE CO TO SEA	STIF	520
	KEDAN-KENTET	STIF	53C
		STIF	54C
		STIF	550
	DC(KJAU,O	STIF	560
		ALTL	100

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	BIK-INTHRINARDIK-IN	STIE ETC
		OTTE EAR
35.4	DC(R=1)=0.0	STLP SHC
250		STIF SAL
201	CUNTINUE AN DOTHE STAA	STIP BOC
	IF LLDAU .NE. 03 PHINT 2500	STIP 61C
2300	PURMAT (* PRESSURE B. C. NOT CALCULATED SINCE LBAD .NE. 0*)	STIF 62C
	IT LLMAD .NE. 03 GU TO 350	STIF 63C
	IF (NIT .GT. 1) GO TO 350	STIF 64C
	IF (NUMPC .E.9. 0) GD TO 310	STIF 65C
	CALL NPFORC(NUMPC, IJBC, NPBCP, PSCA, NL, NM, KSHIFT, NNN, PRATIO, R,	STIF 66C
1	1 Z, B, NPBC, CODE)	STIF 67C
510	LUNTINUE	STIF 68C
	1 (NPCAV, EQ, 0) GO TO 350	STIF 69C
	UALL NPEORC (NCAVPC, IJBCA, NPCAV, PSCAV, NL, NM, KSHIFT, NNN, PRATIO, R,	STIF 70C
1	1 Z, H, NS, CODE)	STIF 71C
350		STIF 72C
	UU ZIO NEI,NUMEL	STIF 73C
-		STIF 74C
	1r (1X(N,5)) 210,210,65	STIF 750
65	UU OU 14174	STIF 76C
-	IF (IX(")I)=NL) 80,70,70	STIF 77C
70	17 (1X(N)1)=NM) 90,90,80	STIF 78C
80	CONTRACTOR CONTRACTOR	STIP 79C
		3111 800
40	TE (MUUTNI (CU) UJ (0) 10 43	3115 610
	MITELLX(N/D) DD 94 I-4 MIDINT	STIP 820
0.1	TE ANTARS EN MINICANN ON TO AN	311P 83C
91	TE (MITEE "EM" MONICIT POLIC AS	311F 84C
		311F 85C
45	TE (NEALE ET 2) CO TO 340	STIF BOD
	AF LIVERLE 9018 33 00 10 204	0117 87C
	TE (VOL GT A A) CO TO 145	STIF BOD
	LANDELBADA1	OTTE DAC
		STIF OLD
0.7	TE (NCALC	STIF VIL
42		STIF OTC
		STIF DEC
	TE (VAL LE. 0.0) GO TO 200	STIF OFF
OF		STTE DAC
77	CALL LOAD(1-MTAP1)	STIF OTC
1/1/1	TECTY(N. 3) = TY(N. 4)) 145.145.146	STIF DAP
144	AN NANNYAJITANNAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAA	STIF ODE
142		STIFLOOP
	P(II)=P(II)=CC+P(10)	STIFIALC
	DO 150 JJ=1-9	STIFICIC
154	S(II_J)=S(II_J)=CC+S(10_J)	STIFIATE
150	CONTINUE	STIFICUE
191	DO 161 II=1.8	STIFIASC
	CC#S(II,9)/S(9.9)	STIFIALC
	P(II)=P(II)=CC+P(9)	STIFIATC
	IF (NCALC .GT. 3) GO TO 161	STIFICAC
	DD 160 JJ=1.8	STIFIAGE
160	S(II.JJ)=S(II.JJ)=CC+S(9.JJ)	STIFLIAC
141	CONTINUE	STIFILLE
145	DO 166 I=1.4	STIFILD
103		VI 41 1120

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106 LM(I)=2*IX(N,I)=2 DO 200 1=1,4 DO 200 K=1,2 II=LM(I)+K=KSHIFT KX=2+I-2+K B(II)=B(II)+P(KK)GD TO NEXT, (199,170) 170 DO 196 J=1,4 DO 196 L=1,2 JJ=LM(J)+L=II+1=KSH1FT LL=2+J=2+L IF(JJ .LE. 0) GO TO 196 A(JJ,II) = A(JJ,II) + S(KK,LL)196 CONTINUE 199 CONTINUE 200 CONTINUE 209 IX(N,5) = -IX(N,5)210 CONTINUE IF (LBAD .NE. 0) GO TO 405 IF (NCALC .LE. 3) WRITE (MTAP2) A,A2 IF (NCALC .GT. 3) READ (MTAP2) A, 42 2. DISPLACEMENT B.C. C DO 400 MENL, NH IF (M .GT. NUMNP) GO TO 401 N=2+M-1-KSHIFT IF (CODE(M) .LE. 0.0) GD TU 400 316 IF (CODE(M) .ER. 2.0) GD TD 390 CALL MODIFY (A, B, ND2, MBAND, N, UR(M)) IF (CODE(M) .EQ. 1.0) GO TO 400 390 N = N + 1 CALL MODIFY (A, B, ND2, MBAND, N, UZ(M)) 400 CONTINUE 401 CONTINUE WRITE BLOCK OF EQUATIONS ON TAPE AND SHIFT UP LOWER BLOCK C WRITE (9) B IF (NCALC .LE. 3) WRITE (9) A 405 IF (NM .GE. NUMNP) GO TO 480 IF (LBAD .NE. 3) GO TO 60 11 IF (NCALC .GT. 3) GO TO 60 DO 420 N#1,ND DO 420 M=1,ND A(M,N)=A2(M,N) 420 A2(M,N)=0.0 GO TO 60 C 480 CONTINUE ASSIGN 199 TU NEXT 500 RETURN 2010 FORMAT(1H1) END

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STIF113C STIF114C STIF115C STIF116C STIF117C STIF118C STIF119C STIF120C STIF121C STIF122C STIF123C STIF124C STIF1250 STIF126C STIF127C STIF128C STIF129C STIF130C STIF131C STIF132C STIF133C STIF134C STIF135C STIF136C STIF137C STIF138C STIF139C STIF140C STIF141C STIF142C STIF143C STIF144C STIF145C STIF146C STIF147C STIF148C STIF149C STIF150C STIF151C STIF152C **STIF153C** STIF154C STIF155C **STIF156C** STIF157C STIF158C STIF159C STIF160C STIF161C STIF162C

		SI.	JB	R	ึกเ	11	I	N	E	Q	U	D	(11		P1)																														Q	UA	0	10
		03	M	M	01	N	1			1		U	MI	VP		NL	M	EL		NI	JM	M	A 1		NI	JM	P	с.		CE		X	. A	CI	EL	Y	. 1	IE	D	(8)	. N	NN		NP		Q	UA	D	20
	1	Ņ	VP	C		٧.	R	E	FP	R	S	D	EI	PT	H	. 1	R	ES		N	. v	0	1.	N	CI	AL.	C	. 1	8	AC	K		4.	in	IN	T	. 1	11	E	NS	. 1	T	τ.				Q	UA	0	30
	2				I'	TN	10	2	0)	,	PF	AS	T	I Ü	C	20	1	. 1	II	5	rc	P	. 1	NR	E	AD		NS	IT	SF	T		NA	N	AL	Y											G	UA	0	40
	3	. 1	NC	T	. 1	NC	n	N	91		NF	PR	CI	۶,	NI	CA	V	PC							_																						Q	UAI	2	50
		ĊC	MC	M	U	V	1	M.	AT	P	1	M	T	YP	E	. 8	0	(1	2	1	E	1	8	. 1	2	١.		KC)(12	2)	.!	4 N	T	EN	10	12	21		M.J	N1	rc	12	1			()	UA	2	60
	1							C	RA	C	(1	12	1	• •	-									-	-											•••		1				•	• •				0	UA	2	70
	1	CC	DM	M	10	N	1	E		A	TI	1	I)	(9	0 0		5)		м'	TA	G	(0	0	۱.	E	PS	11	90	00	1	. 5	TF	2.5	11	9 (0 0		4 1		SE	P(91	0.0	.3	הו	UA	>	80
		CC	M	M	01	V	1	NI	PC	A	TV	1	-	21	9	99	5	. 2	ć	9	99	1)	. (:0	DI	E (9	99	1		JR	0	99	9) .	U	Z	(9	9	9)					••		Q	UA	2	90
		CC	ĴМ	M	01	V	1	A	RG	1	5	R	R	(5)	, Z	Ż	Z	5)	. 5	1	1 ().	10	0)		P	1	0)		R	3 1	R	5 (4	5	L	B	AD	.1	M	(4	1			Q	UA	2	100
	1										1	N	GL	E	0	4)		XI		H	10	6		0	5	. C	1	4.	4)	E	E	(4	1	. +	11	6	. 1	0	١.	D	16	. 6	1			G	UA	5	110
	2										F	- (6	.1	0) .	3	IG	. (6),	D	SI	I G	C	6)		RF	11	4 1		H	SE	L	(3	11	. (41		DS	Ī	SZ					G	UA	2	120
																																		-						-							Q	UA)	130
		1:	= 1	X	()	N,	1)																																							Q	UA	5	140
		J	= 1	X	(1	N,	2)																																							G	UA	5	150
		K :	= 1	X	(1	Ν,	3)																																							Q	UAI	5	160
			EI	X	(1	N,	4)																																							0	UAI	5	170
		MI	TY	P	E	E]	X	(N,	5)																																				Q	UAI	D	180
		vŗ	DL.		0																																										Q	UA	D	190
																																															Q	UA	D	200
FO	R	M	S	T	RĮ	ES	19		S 1	R	A 1	[N	1	RE	L	A 1	I	10	S	H	I P)	F (R	1	PL		NE		31	R	A	IN	ł													Q	UA	0	215
																																															G	UA	D	220
		NE	EP	8	0																																										Q	UAI	D	230
		Ç/	AL	L	:	51	R	3	T F) (31	ľJ	1	. 3	T	Ja	.,	\$1	G	Z	Τ,	N	EI	۹,	N	. 1	C	AL	.C)																	Q	UA	D	245
***	*	* 1	* *	*	* 1	* *	*	×	**	* *	* 1	* *	*	* *	*	* *	r #	* 1	* *	*	k 1	* *	*1	* *	*	* *	*	*1	**	* 1	* *	*	* *	*	* 1	**	* 1	* *	*	**	*1	* *	**	1			Q	UA	2	250
			F	0	RI	ч	Q	U	AC	R	IL	A	TI	ER	A	L	S	T 1	F	FI	VE	S	S	M	A	TF	1	X																			Q	UAI)	250
***	*	* 1	k #	*	* 1	* *	*	*	* *	*	*1	* *	*	* *	*	* *	*	*1	* *	*	k 1	* *	* 1	* *	*	* 1	*	* *	*	* 1	k #	*	* *	*	* 1	* *	* 1	* *	*	* *	*						Q	UA	5	278
			ו	9	4	P	8	1	. 4	1																																					Q	UA)	200
		MN	4 =	1	X	(N	,	M)																																						G	UA)	290
93		86	29	(M) =	R	(MM	1)																																					G	UAI	2	300
94		Ζ Ζ	ZZ	(M) =	Z	(hh	1)																																					Q	UA	2	310
																																															Q	UA	0	320
		Dr	<u>,</u>	1	0(D	I	I	= 1		10)																																			Q	UAI)	330
		P (Ī	I):	= ()	•	0																																							Q	UA	0	34C
		DC		9	5	5	J		1,	6																																					Q	UAI	5	350
95		HH	4 (J	J	• 1	I)		•	0																																				Q	UA.	0	360
		DI:) 	1	00	0	J	J	=]		10	כ																																			Q	UA	D	370
100		5 (Ĩ	I		JJ	2	-	0.	, Q																																					Q	UA	D	300
				1	1	9	1	I	=]		4																																				Q	UA	D	300
		D		1	14	8	1	J	=]		5	1																																			Q	UA	D	400
118		H S	5E	5	U.	IJ		I			0	0																																			G	UA.	D	410
			JE	1	X	(]	1	I								-		-																													Q	UA	P	420
114		A •	16	-	2	(1	1)	# ()	,0	D	: (J	1)	/	51	•	5																													Q	UA	p	430
		e /	-	м								-																																			Q	UA	P	440
		r (JH			51	R		31	1	r 1	N		33																																	Q	UA	D	450
		T P	-	,				, i						7		•	-	E /		•			21																								Q	UA	D	440
3/16		11	5	l n	1	* (N	1	<)		1)	K L	N	, 3	1	J	C	5	,	2	• (¢ :) (G	UA	D	470
240			₹ #			1 J		* *	11																																						G	UA		800
				2	1	, , ,		2		1	2		7	• •		•																															G	UA	U	490
		~	. 1	3	14	41	(P	1	* *	21	-0	4	R R	2	1															•																Q	UA		500

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XL=SQRT(DR++2+DZ++2)
RRR(5)=(R(I)+R(J))/2.=2.*EE(4)*DZ/XL
                                                                                                   QUAD 510
ZZZ(5)=(Z(I)+Z(J))/2.+2.*EE(4)*DR/XL
                                                                                                   QUAD 520
IF (NCALC .NE. 1 .UR. NRES .GT. 0) GO TO 242
IF (NREAD .EQ. 1.DR.NNN.GT.1.OR.NCT.GT.1) GO TO 242
IF (RO(MTYPE) .EQ. 0. .AND. E(2,MTYPE) .LE. 1.) GO TO 242
                                                                                                   QUAD 530
                                                                                                   QUAD 54C
                                                                                                   QUAD 550
CALL INITST
                                                                                                   QUAD 56C
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242 CONTINUE QUAD 57C CALL TRISTF(1,2,5) QUAD 58C GO TO 130 QUAD 59C 250 CONTINUE 1 QUAD 60C 1 IF (K .NE. L) GO TO 125 QUAD 61C RRR(5)=(RRR(1)+RRR(2)+RRR(3))/3.0 WUAD 62C Z7Z(5)=(ZZZ(1)+ZZZ(2)+ZZZ(3))/3.0 QUAD 63C IF (NNN .GT. 1 .OR. NCT .GT. 1) GO TO 121 QUAD 64C 2. IF (NCALC .NE. 1 .OR. NRES .GT. 0) GO TO 121 QUAD 65C IF (NREAD .EQ. 1) GO TO 121 JUAD 66C IF (RO(MTYPE) .ER. 0. .AND. E(2,MTYPE) .LE. 1.) GO TO 121 QUAD 67C CALL INITST NUAD 68C 121 CONTINUE QUAD 69C CALL TRISTF(1,2,3) RUAD 70C VOL = XI QUAD 71C IF (VOL .GT. 0.0) GO TO 130 QUAD 72C С ERROR RETURN QUAD 73C 122 LPAD = LBAD + 1 QUAD 74C GO TU 135 QUAD 75C 125 VOL=0.0 DUAD 76C RRR(5)=(R(I)+R(J)+R(K)+R(L))/4.0 QUAD 77C ZZZ(5)=(Z(1)+Z(J)+Z(K)+Z(L))/4.0 GUAD 78C IF (NRES .GT. 0) GO TO 126 QUAD 79C IF (NREAD .E9. 1) GO TO 126 GUAD BOC IF (NCALC .NE. 1 .OR. NNN .GT. 1 .OR. NCT .GT. 1) GO TO 126 GUAD 81C IF (RD(MTYPE) .EQ. 0. .AND. E(2, MTYPE) .LE. 1.) GO TO 126 QUAD 82C CALL INITST QUAD 83C 126 CONTINUE QUAD 84C CALL TRISTF(4,1,5) QUAD ASC CALL TRISTF(1,2,5) RUAD B6C CALL TRISTF(2,3,5) QUAD 87C CALL TRISTF(3,4,5) QUAD 88C IF (VOL .LE. 0.0) GO TO 122 QUAD 89C 145 DO 140 II=1,6 QUAD 90C DO 140 JJ=1,10 QUAD 91C 140 HH(II,JJ)=HH(II,JJ)/4.0 QUAD 92C 130 CONTINUE QUAD 93C WRITE(MTAP1) N, S, HH, RRR(5), ZZZ(5), C, P, HSEL QUAD 94C 135 RETURN QUAD 95C END QUAD 96C SUBROUTINE PRINST (SIG) PRIN 10 DIMENSION SIG(6) PRIN 5C CC = (SIG(1) + SIG(2)) + 0.5PRIN 30 BB = (SIG(1) - SIG(2)) + 0.5PRIN 4C $CR=SQRT(BB \pm 2 + SIG(3) \pm 2)$ PRIN 50 SIG(4)=CC+CR PRIN 60 SIG(5)=CC-CR PRIN 70 C****SIG(6) IS AN ANGLE MEASURED FROM RWAXIS TO THE PLANE ON WHICH PRIN 80 C**** MINOR PRINCIPAL STRESS ACTS. POSITIVE IF COUNTERCLOCKWISE

SIG(6)=45. IF (BB .NE. 0.) SIG(6)=23.64785*ATAN2(SIG(3),BB) RETURN END PRIN 10C PRIN 10C PRIN 10C PRIN 12C PRIN 12C PRIN 13C

	Carl and the second		
1	SUBROUTINE TRISTF(II,JJ,KK)	TRIS	10
	COMMON / / NUMPANUMEL NUMMATANUMPCACELY ACELY HED (A) NNN NP.	TRIS	20
		1010	20
1	I NPCAVAREPROJUEPTHANREDANAVULANCALLAIBACKAMJUINTAMTENSANITA	IKT2	36
	R ITN(20), PRATIO(20), NISTOP, NREAD, NSTSRT, NANALY	TRIS	4C
	3.NCT.NCONST.NPRCP.NCAVPC	TDIS	50
		1010	10
	CUMMUN /MATP/ MITPE, RU(12), E(8,12), AKU(12), MNTEN(12), MJNT(12)	TRIS	90
	1 ,CRAC(12)	TRIS	70
	COMMON JARG/ REP(5),777(5), 9(10,10), P(10), PETP((4), LRAD, 14(4),	TOTE	80
		1419	n.
	ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6),	TRIS	90
17. I	F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIG7	TRIS	100
	DIMENSION 77(4), DD(3, 3), HEAVE(3, 10), HO(31)	TOTO	110
24		1419	110
	EQUIVALENCE (F(1,1),HS(1),HSAVE(1,1))	TRIS	120
1000	IBACK#IBACK+1	TRIS	130
C		TOTO	140
		1413	THE
		TRIS	150
	LM(2)=JJ	TRIS	120
100	I MIJIEKK	TDIE	1 7 2
		1419	1/5
1.1	KK(I)=KKK(III)	TRIS	165
	RR(2)=RRR(JJ)	TRIS	170
100	RR(3) BRRD(KK)	TOTE	200
		TRAD	
12	PR(4)=RRR(II)	TRIS	210
7.5	ZZ(1)=ZZZ(II)	TRIS	220
	Z7(2)=Z77(JJ)	TOTH	380
	77/3/#777/44)	TOTO	240
		1813	Eat
6.1		TRIS	25C
85	DO 100 I=1,6	TRIS	260
21	DD 90 JE1-10	TOTO	270
		1419	210
10 Con 10		TRIS	28 C
90	H(I,J)=0.0	TRIS	290
	DD 100 JE1-6	TOTE	305
100		1810	300
100		THIS	310
C	FORM INTEGRAL(G)T+(C)+(G)	TRIS	320
	COMM=RR(2)*(ZZ(3)=ZZ(1))+RR(1)*(77(2)=77(3))+RR(3)*(77(1)=77(2))	TRIS	330
11	YI = COMM / 3.0	TOTO	740
		INTS	340
R4	IF (XI GT 0 0) GO TO 102	TRIS	350
	PRINT 1000, II,JJ,KK, N	TRIS	360
	I BADEL BAD+1	TOTE	170
1000		1419	370
1000	FURMAL (SEN ZERO OR NEGALIVE AREA, IRLANGLESIO, 5%, MELEMENTIS)	TRIS	380
	RETURN	TRIS	390
102	VOL=VOL+XI	TRIS	400
	0(2,2)=Xt +((1,1)	TOTA	1100
		IKT2	410
	D(2,6) = XI + C(1,2)	TRIS	42C
	D(3,3)=X1 + C(4,4)	TRIS	43C
	D(3.5)#XT +C(4.4)	TOTE	110
		1419	440
100	U(J,J)EXI #L(4,4)	TRIS	45C
	D(6,6)=XI +C(2,2)	TRIS	460
	D(2,3)= X1+C(1,4)	TOTO	170
1		1410	910
1		TRIS	430
	U(5,6)= XI*C(4,2)	TRIS	49C
	D(5.6)=D(3.6)	TRIS	500
1 104		TOTO	840
1 100		INT2	210
		TRIS	52C
	$D_{0} 110 J = K_{1}6$	TRIS	530
. 110	D(J.T)=D(T.J)	TOTA	EAA
1.10		1412	346
l C	FUHH CUEFFICIENIOUISPLACEMENT TRANSFORMATION MATRIX	TRIS	55C
	DD(1,1)=(RR(2)+ZZ(3)=RR(3)+ZZ(2))/COMM	TRIS	560

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1	DD(1,2)=(RP(3)*ZZ(1)=RR(1)*ZZ(3))/COMM	TRIS 57C
	DD(1,3)=(PP(1)+77(2)-PP(2)+77(1))/(OMM	TRIS SAC
	101133-(NR(1)-22(2)-RR(2)-22(1))/0000	TDIE EOF
		1813 340
4	DD(2,2)=(ZZ(3)=ZZ(1))/CUMM	TRIS BOC
	DD(2,3)=(ZZ(1)-ZZ(2))/CDMM	TRIS 61C
100	DD(3,1)=(RR(3)-RP(2))/COMM	TRIS 62C
	DD(3.2)=(BP(1)=PP(3))/(OMM	TRIS 63C
	50(5,5)=(RR(2)=RR(1))/COMP	1R13 040
0	DN 120 I=1,3	TRIS 650
	J=2*LM(I)=1	TRIS 66C
	H(1,J)=OD(1,T)	TPIS 67C
	H(2.1)=DD(2.1)	TRIS 68C
		TOTS AOC
	$H(4, J+1) \equiv DU(1, 1)$	IRIS TUC
	H(5,J+1)=DD(2,I)	TRIS 71C
120	H(6,J+1)=DD(3,I)	TRIS 72C
C	ROTATE UNKNOWNS IF REQUIRED	TRIS 73C
	DO 125 Ja1-2	TRIS 74C
		TOTE 750
(h-c)		
	IF (ANGLE(I)) 122,123,123	1K12 /00
122	SINA=SIN(ANGLE(I))	TRIS 77C
	COSA=COS(ANGLE(I))	TRIS 78C
	IJ=2*I	TRIS 79C
	DO 124 Kate6	TRIS BOC
0.		1413 010
· · · · · · · · · · · · · · · · · · ·	H(K, IJ=1)=TEM+CUSA+H(K, IJ)+SINA	TRIS 52C
124	H(K,IJ)= -TEM*SINA+H(K,IJ)*COSA	TRIS 83C
i 25	CONTINUE	TRIS 84C
c	FORM FLEMENT STIFFNERS MATRIX (H)Y+(D)+(H)	TRTS ASC
		TRIE SAC
	DU 150 K=1+0	TRIS DIL
	IF(H(K,J) .ER. 0.0) GD TO 130	TRIS BBC
128	DO 129 I=1,6	TRIS 89C
129	F(I,J)=F(I,J)+D(I,K)+H(K,J)	TRIS 90C
130	CONTINUE	TRIS 91C
		TRTE OOP
		1810 720
	00 140 K=1,6	1413 420
	IF (H(K,I) .EQ. 0.0) GO TO 140	TRIS 94C
138	DD 139 J=1,10	TRIS 95C
139	S(I,J)=S(I,J)+H(K,I)+F(K,J)	TRIS 96C
140	CONTINUE	TRIS 970
r	FORM DESTDUAL LOAD MATRY	TOTE OAP
		TO10 002
C****	FORM RESIDUAL LUAD MATRIX	INTS AAC
150	DD 160 I=1,10	TRIS100C
	HSAVE(1,I)=H(2,I)	TRISIOIC
9	HSAVE(2,I)=H(6,I)	TRIS1020
160	HSAVE(3, T)=H(3, T)+H(5, T)	TRISIOSC
		TRICLOUC
L	TE ANEALE NE 4 OD NAT AT AN TO ATA	18101040
5.)	IF INLALL ONE O LOUMONCTOGIOID GU TU 171	TM15105C
	IF (NREAD, EQ. 1. DR. NNN. GT. 1) GO TO 171	TRIS106C
43	IF (ACELX.EQ. 0.0 .AND. ACELY.EQ. 0.0) GO TO 171	TRIS107C
	COMM = RO(MTYPE) + XI / 3.0	TRISIOBC
1411	DO 170 TE1.3	TRISIAOF
		TOTOLIAP
19		18131100
1	PLJJ = PLJJAALELXACUMM	THISIIIC
1 170	P(J+1) = P(J+1) = ACELY COMM	TRIS112C

	171 400 410 420	CONTINUE FORM STRAIN TRANSFORMATION MATRIX DO 410 I=1,6 DD 410 J=1,10 HH(I,J)=HH(I,J)+H(I,J) HS(31)=XI DO 420 I=1,31 HSEL(I,IBACK)=HS(I) RETURN END	TRIS113C TRIS114C TRIS115C TRIS116C TRIS116C TRIS116C TRIS118C TRIS120C TRIS121C TRIS122C
c	235	SUBROUTINE MODIFY(A, B, NEQ, MBAND, N, U) DIMENSION A(90, 180), B(180) DO 250 M=2, MBAND K=N=M+1 IF (K .LE. 0) GO TO 235 IF (A(M,K) .EQ. 0.0) GO TO 235 B(K) = B(K) = A(M,K) \pm U A(M,K) = 0.0 K=N+M-1 IF (K .GT. NEQ) GO TO 250 IF (A(M,N) .EQ. 0.0) GO TO 250 B(K) = B(K) = A(M,N) \pm U A(M,N) = 0.0 CONTINUE A(1,N) = 1.0 B(N)=U RETURN END	MODI 1C MODI 2C MODI 3C MODI 4C MODI 4C MODI 5C MODI 6C MODI 7C MODI 6C MODI 9C MODI 10C MODI 10C MODI 11C MODI 12C MODI 12C MODI 12C MODI 15C MODI 15C MODI 15C MODI 16C MODI 16C MODI 16C MODI 16C

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SUBRIUTINE JISTIF	JTS	T 1C
COMMON / / NUMNP, NUMEL, NUMMAT, NUMPC, ACELX, ACELY, HE	D(8) NNN NP. JTS	1 20
1 NPCAV, REFPRS, DEPTH, NRES, N. VOL, NCALC, TRACK, MICINT, MT	FNG NTT.	1 10
	LASINITI JIS	1 30
THE THE OFFET TO LEGISTISTOP, NEE AD, NSTSRI, NANALY	JTS	T 4C
S NCT, NCUNST, NPBCP, NCAVPC	JTS	T 5C
COMMON /MATP/ MTYPE,RO(12),E(8,12),AKO(12),MNTEN(12)	MUNT(12) ITS	74 7
- 1 (CRAC(12)		
COMMON (EL DATA (TY/DAD EL MELO/DAD) FROM COM	JIS	1 / L
COMMON /ELUATA/IX(900,5),MTAG(900),EPS(900),STR5(900),4),SEP(900.3)JTS'	T 8C
CIMMON /MPDATA/ R(999),Z(999),CODE(999),UR(999),UZ(9	199) JTS'	T 9C
COMMON /ARG/ PPR(5),ZZZ(5),S(10,10),P(10),RSTRS(4),I	HAD .I MCHT. ITS	1 100
1 ANGLE (4) - YT - HH (6 - 10) - C (4 - 4) - EE (4) - H (6 -		1 100
	J, J, J (0,0), J13	1110
= c (0,10),316(0),D316(0),RR(4),H3EL(31,4)	,DSIGZ JTS	1 1 2 C
CUMMUN /JNT/ FN(450),FT(450),NJT	JTS	130
DIMENSION ESTIF(10,10), PPP(8), TR(2,2), Y(4,4)	.178	1 140
EQUIVALENCE (L.VOL) (S(1.1) ESTTE(1.1))	170	1 150
REAL KS.KN.I	515	1 150
	JTS	T 16C
· · · · · · · · · · · · · · · · · · ·	,-1.,1.,2./ JTS	T 17C
II=IX(N,1)	175	180
s, n) XI = LL (S, n) XI = LL	179	7 102
DR#R(JJ)-R(TT)	513	1 196
	JTST	1 500
	JTSI	515
	JTST	226
IF(L_EQ.0.) GO TO 201	1755	580 5
MTYPE=IX(N,5)		010
TET NEES GT AN CO TO HA	3131	246
	JYST	1250
IF (NCALC.NE.1) GU TU 40	J737	246
IF(NNN.GT.1.OR.NCT.GT.1) GO TO 40	17.91	2 240
IF (NREAD .ER. 1) GO TO 40	1705	2 13.0
RRR(5)=0 5+(P(11)+P(TT))	0131	600
	JTSI	1 8 h
	JTS7	210
CALL INITST	JIST	340
40 CONTINUE	.1799	850
C** MATERIAL PROPERTIES	1101	مية يتواقي در (ماره م
KNEF (1, MTYDE)	3131	0.7 0
	JTSI	340
NJECC, MITPEJ	JIST	350
- 50 COMS#KS*L/6.	.17.89	350
COMN=KN+L/6.	ITCT	194
	5151	3/5
	JIST	38C
	JTST	390
r(TI)=0°0	JTS?	400
PPP(II)=0.0	1151	412
00 100 JJ=1,8	1464	120
100 FSTTF(IT.JJ)=0.0	5131	426
	JIST	430
L DEVELOP RESIDUAL STRESS CONTRIBUTIONS TO THE LOAD V	ECTOR JTST	246
C THE FOLLOWING SIGN CONVENTION IS ADOPTED. THE NORMAL STRE	SS IS POSITIVEJTST	85C
C DIRECTED OUTWARDS THE ELEMENT ON THE FACE (II, JJ) THE SH	FAR STRESS TO ITOT	1162
C WHEN DIRECTED FROM JJ TO IT AND LL TO KK ON THE ELEN	FNT PAR	1999
TP/1.13=00/1	ENI. JISI	11/2
	J731	264
	JTSY	490
IF (NCALC.NE.1) GO TO 162	1797	582
IF (NNN, GT. 1, OR, NCT. GT. 1) GD TO 162	1767	512
IF (NRES .ER. O .OR. NRES FO 21 CO TO 142	0131	336
0" - TD/1.13 - TD/1.34	JTSY	250
$\mathbf{U} = [\mathbf{U}_{1}] \times [\mathbf{U}_{2}]$	JTST	530
3C # [H(1,2) ## 2	JTST	540
C2 = TR(1,1) ** 2		550
111 RSTRS(1)=STRS(N,1)+S2+STRS(N,2)+r2=2 +etDe(N, 1)+0r	0101	
	JTST	20C

		RSTRS(2)=(STRS(N,2)-STRS(N,1))+SC-(STRS(N,3)+(S2-C2))	JTST 57C
		EL2 = L / 2.0	JTST 58C
		DO 160 I=1,4	JTST 59C
į.		J=2+I=1	JTST 60C
		PPP(J) = RSTRS(1) + EL2	JTST 61C
9		J#2#1	JTST 62C
	160	PPP(J) = RSTRS(2) + EL2	JTST 63C
		DO 161 TE1.4	JTST 64C
	161	PPP(I)=-PPP(I)	JTST 65C
	162	CONTINUE	JTST 66C
ł.			JTST 67C
		13=2+11-1	JTST 68C
		TNE2+TT	JTST 69C
			JTST 70C
		JS g 2+J.j=1	JTST 71C
١.		.IN = 2+1.1	JIST 72C
		FETTELTS, IS' ACOMS+V(IT.I.I)	JTST 73C
1	200	FRTTF/TN.IN)=COMN+V(TT.II)	JTST 74C
-	200	POTATE TO GLOBAL COOPDINATES	JIST 75C
-		TP(2.1) • TP(1.2)	JTST 760
÷		TP(2,2) = TP(1,1)	JTST 77C
		TE(TP(1, 1), E0, 1, 1) CO, TO, 405	JITST 78C
٢.			JTST 790
			JITST BOC
		11= 2+NN=1	JTST ALC
i.		TEMP - FETTE(TT. 1.1)	JTST 82C
		ICAL - COLLECTION	JIST ASC
		CETTE(TT, 11)+TEMP+TD(1,KK)+FETTE(TT, 2+NN)+TD(2,KK)	JIST 84C
	4.10		JTST ASC
٢.	410	DO 426 TTE1.8	JTST 86C
		11-2+NN-1	JTST ATC
		TEMD SERTE(11.TT)	ITST AAC
ł,		10 436 KKe1.3	ITST ADE
		CETTE(II, TI)=TD(I, KK)=TEMD=TD(2, KK)=FETTE(2=NN, TI)	ITST 90C
1	1120		ITST 91C
l	420		JIST 920
	400		ITST 03C
	403	TE INDER ED A OR NREG ED 21 CO TO 402	ITSY QUE
		TO HAT THE H	JTST 95C
h			ITST 96C
			1759 977
4		11=K×1 D/11=_0DD/11+TD/1 31+DDD/111+TD/3.31	IST GAC
ł.		P(J) = PPP(J) = (R(J) = (R(J) = (R(J) = (R(Z) = (R(Z	1797 996
	401		11811000
•	402		.17871012
	244	DOTAT DADA N	11871026
	201	PETIDA PETIDA	TRTIAT
	2000	EDDMAT/1/14 BAD TOTAT No 12/3	TRTIANP
	2040	END END	TRTIASE
			01011000

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T		SUBROUTINE BANSOL (NNN.NIT.NCALC)	HANS	10
1		COMMON /BANARG/ 8(90), 82(90), 4(90,90), 42(90,90), MBAND, ND2, NUMBLY,	BANG	20
		1 MAMAY.NRR .MTAP1.MTAP2	DANE	10
~		SOUTVALENCE (MM. MBAND)	DANO	36
1		NNSMRMAY	DANO	46
4.1		N'TADE WMTADO	BANS	50
			BANS	6C
Ē.		TERING OF	BANS	70
	0.0	REWIND 41	BANS	80
	44	RENIND 9	BANS	90
		NB#0	BANS	100
1	2	GO TO 150	BANS	110
0	C	REDUCE EQUATIONS BY BLOCKS	BANS	120
	C	1. SHIFT BLOCK OF EQUATIONS	BANS	130
	100	NAENB+1	BANS	14C
		00 125 N=1, NN	BANS	150
		B(N) = B2(N)	BANS	160
		82(N) = 0.0	BANS	170
		DC 125 M=1, MM	BANS	180
5.4		A(M,N) = A2(M,N)	BANS	190
	125	A2(M.N) = 0.0	BANG	200
	C	2. READ NEXT BLOCK OF FOUATTONS INTO CORF	BANO	210
		IF (NUMBLK-NB) 150.200.150	BANG	220
	150	READ (9) B2	DANG	220
		READ (NTAPE) A2	DANO	230
		TE (NB .ER. 0) GO TO 100	DANS	240
L.	C	3 PEDUCE BLOCK DE EDUATIONE	BANS	250
	200	TE (NEALE ET 3) ER TE SAAA	BANS	260
r.	200	NO 300 NET NN	BANS	272
			BANS	280
		1° (A(1)N) $_{\circ}$ EG ($_{\circ}$ O) G(1 TO 500	BANS	590
			BANS	300
		IF (A(L,N) .EU. 0.0) GU TU 275	BANS	310
L		C = A(L,N) / A(1,N)	BANS	350
		I=N+L=1	BANS	330
		JEO	BANS	34C
		DO 250 K=L,MM	BANS	35C
		J=J+1	BANS	360
	250	$A(J_{j}I) = A(J_{j}I) = C + A(K_{j}N)$	BANS	370
4		A(L,N) = C	BANS	380
	275	CONTINUE	BANS	390
	300	CONTINUE	BANS	400
		WRITE(MTAP2) A	SANS	410
L.	2000	DO 2300 NE1, NN	RANG	1120
÷		IF (A(1.N) .EQ. 0.0) GO TO 2300	BANC	420
		DO 2275 L=2, MBAND	BANC	430
		IF (A(L.N) .FQ. 0.0) GD TO 2275	DANO	440
		T=N+L=1	DANG	436
		B(T)=B(T)=A(L_N)+B(N)	DANO	400
-	2275	CONTINUE	BANS	470
		BINTEBINT /AIT.NY	BANS	480
9	2200		BANS	490
	2300		BANS	50C
1	LANA	TEAMARK FOR MON OF FOR THE STATE STA	BANS	510
1	225	17 (NUMDER .EWA ND) 6U TU 599	BANS	52C
	315	MATIC (AI) R	BANS	53C
		GC TU 100	BANS	54C
-	2	BACK-SUBSTITUTION	BANS	55C
	399	BACKSPACE MTAP2	BANS	56C

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		NTAPERMTAP2
	400	DD 450 M#1, NN
		NINN+1-M
		D0 425 K=2, MM
-		L=N+K+1
	425	$B(N) = B(N) - A(K_{s}N) + B(L)$
T		$B_2(N) = B(N)$
1	400	A2(NB,N) = B(N)
		NB=NB=1
T		IF (NB .EQ. 0) GO TO 500
1	475	BACKSPACE MTAP2
3		BACKSFACE 91
		READ (MTAP2) A
Τ.		READ (91) B
1		BACKSPACE MTAP2
		BACKSPACE 91
1		GO TU 400
C		ORDER UNKNOWNS IN B ARRAY
	500	K=0
,		DO 600 NB=1.NUMBLK
		DO 600 NE1, NN
1		K=K+1
	600	B(K) = A2(NR,N)
- 1		RETURN
1		END

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BANS 57C BANS 58C BANS 59C BANS 60C BANS 61C BANS 62C BANS 63C BANS 64C BANS 65C BANS 66C

BANS 67C BANS 68C BANS 69C BANS 70C BANS 71C BANS 72C

BANS 73C

BANS 74C BANS 75C BANS 76C BANS 77C BANS 78C BANS 79C BANS BOC

BANS 81C

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		SUBROUTINE STRESS	STRE	10
		COMMON / / NUMNP, NUMEL, NUMMAT, NUMPC, ACELX, ACELY, HED(8), NNN, NP,	STRE	20
		1 NPCAV, REFPRS, DEPTH, NRES, N. VOL, NCALC, IBACK, MJOINT, MTENS, NTT.	STRE	30
		2 ITN(20), PRATID(20), NISTOP, NREAD, NSTSRT, NANALY	STRE	40
		3.NCT.NCONST.NPBCP.NCAVPC	STRE	50
		COMMON (MATR/ MTYPE, PO(12), F(8 12), AKO(12) MATEN(12) MINT(13)	OTOE	50
			SIRE	
			STRE	70
		COMMON /ELUATA/IX(900,5), MTAG(900), EPS(900), STRS(900,4), SEP(900,5)STRE	80
		CUMMUN /BANANG/ B(180), A(90, 180), MBAND, ND2, NUMBLK, MBMAX, NB	STRE	90
		1. MTAP1. MTAP2	STRE	100
		COMMON /ARG/ RRP(5),ZZZ(5),S(10,10),P(10),RSTRS(4),LBAD,LM(4),	STRE	110
		1 ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6),	STRE	120
		2 F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIGZ	STRE	130
		COMMUN / NT/ FN(450), FT(450), NJT	STRE	140
		DIMENSION TP(6), FY(900)	STRE	150
		DIMENSION STRN (900,3)	STRE	160
		EQUIVALENCE (STRN.A(6500))	OTDE	170
		FRUTVALENCE (EV. ACHOROD)	OTOE	100
C		COMPLITE ELEMENT STOFREE	SIRE	100
Ŭ		REWIND MTADA	SIRE	190
		TENMAY#O O	STRE	205
			STRE	210
			STRE	220
			STRE	23C
			STRE	240
		DI IOD NEINUMEL	STRE	25C
	100	$I \times (N, 5) = I \Delta B S (I \times (N, 5))$	STRE	26C
		NELMJENUMFLENJT	STRE	27C
		DD 300 MN=1, NELMJ	STRE	28C
		CALL LOAD(9, MTAP1)	STRE	290
		DO 120 I=1,4	STRE	300
		II=2+I	STRE	31C
		JJ=2*IX(N,I)	STRE	320
		P(II=1)=8(JJ=1)	STRE	330
	120	P(II)=B(JJ)	STRE	340
		DO 150 I=1.2	STOF	350
		RR(T)=P(T+8)	OTDE	336
		DO 150 K=1.8	OTOE	370
	150	RR(T)=RR(T)=S(T+8.K)+P(K)	OT DE	700
		Γ $MM = S(9, 9) + S(10, 10) - S(9, 10) + S(10, 0)$	SIRE	300
		TE (COMM) (55.140.155	STRE	390
	155		STRE	400
	100	P((A)=(-S(10, 0)+PP(1)+8(0, 0)+PP(3))/COMM	SIRE	410
	140	- (10) + (- 3(10) +) + KH(1) + 3(4) +) + KH(2)) / LUMM	STRE	42C
	100		STRE	43C
			STRE	44C
		UU 1/0 K = 1, 10	STRE	45C
	170) TP(I)=TP(I)+HH(I,K)+P(K)	STRE	46C
		RR(1)=TP(2)	STRE	47C
		RP(2)=TP(6)	STRE	48C
		RP(3)=0.0	STRE	490
		RP(4) = TP(3) + TP(5)	STRE	500
		IF (NCALC .NE. 1 .OP. NREAD .EQ. 1) GO TO 175	STRF	510
		IF (NNN, GT. 1, DR. NCT. GT. 1) GD TO 175	STRE	520
		IF (NRES. GT. 0) GO TO 173	STOF	510
		STRS(N, 4) = STRS(N, 1)	STOP	500
	173	CONTINUE	STOP	SHU
		IF (ABS(STRS(N.1)), LT. 0.001 AND ARG(GTDG(AL 355 LT A AA4 AND	OTOF	336
		- CONTRACTOR CONT	SIRE	200

B-	2	5
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	ABS(STRS(N,3)) .LT.0.001) GD TO 175	STRE 57C
	STJ1=STR3(N,1)+STRS(N,2)+STRS(N,4)	STRE SAC
	ST.12=((STRS(N,1)=STRS(N,2))++2+(STRS(N,2)=STRS(N,4))++2+	STRE EOC
	(STRS(N, 4)=STRS(N, 1))++2)/6 +STRS(N, 3)++2	OTHE STO
	FY(N)=F(7,MTVPF)+ST.1(+SOPT(ST 10)_F(8,MTVPF)	STRE BUC
175		ATRE DIL
		STRE BZL
		STRE 63C
4.0.4	UJ 180 K=1,4	STRE 64C
100	DSIG(I) = DSIG(I) + C(I,K) + RP(K)	STRE 650
	USIGZ=DSIG(3)	STRE 66C
	DSIG(3)=DSIG(4)	STRE 67C
	DO 181 I=1,3	STRE 68C
181	SIG(I)=RSTRS(I)+DSIG(I)	STRE 69C
	DU 400 J=1,3	STRE 70C
	STRS(N, J) = STRS(N, J) + SIG(J)	STRE 71C
	SIG(J)=STRS(N,J)	STRE 72C
400	CONTINUE	STRE 7%C
	STRN(N, 1) = RR(1) + STRN(N, 1)	STOF THE
	STRN(N, 2)=RR(2)+STRN(N, 2)	STDE 750
	STRN(N.3)=RR(4)+STRN(N.3)	STOF 740
	DO 450 I=1.2	6705 770
	TP(T)ESTRN(N.T)	6T65 782
450	CONTINUE	STRE TOU
	TP(3)=0 5+STRN(N-3)	STRE 790
	CALL PRINST(TP)	SIRE OUL
	TP(T)=QTRN(N,T)	SIRE BIL
r	OUTDUT CTDECEEC	SIRE BEL
r	CALCHLATE DOTNETDAL GTOREGE	STRE BOC
C	CALLOLAIL FRINCIPAL SIRESSES	STRE 84C
	$\frac{1}{1}$	STRE 85C
	15/5/3 HTHES IT 3 100 FC 3/3	STRE B6C
		STRE 87C
	1F (MIENS .E.W. 0) 60 10 570	STRE 88C
ELA	DU SOU JEL,MIENS	STRE 89C
500	IP (MITPE .EQ. MNTEN(J)) GO TO 263	STRE 90C
510		STRE 91C
	IF (SIG(4) LE. TENMAX) GO TO 200	STRE 920
	TENMAX=SIG(4)	STRE 93C
	NTEN#N	STRE 94C
200	CONTINUE	STRE 95C
	TMAXEE(1, MTYPE)	STRE 96C
	IF (MTAG(N) .GE. 2) GD TD 250	STRE 970
	IF (SIG(4) .LE. TMAX) GO TO 263	STRE 980
	MTAG(N)=2	STRE 99C
250	IF (MTAG(N) .EQ. 3) GO TO 263	STRE100C
	IF (SIG(5) .LE. TMAX) GO TO 263	STRE101C
	MTAG(N)#3	STRE102C
263	CONTINUE	STRE103C
C****		STRF1040
	IF (MPRINT .NE. 0) GO TO 110	STRF1050
105	PRINT 2000	STRF10AC
	PRINT 2400	STRF1070
	PRINT 2300	STDFIARC
	MPRINT=25	9705100C
110	MPRINT=MPRINT=1	QTDE11AP
	MPRINTEMPRINT+1	STDE114P
	PRINT 2001, N, RRR(5), ZZZ(5), (SIG(1), T=1.6). TP	CTDE112
		JIRCLIEU

STRE113C
NISTRE114C
STDE115C
STREIISC
SIREIIOL
STRE117C
STRE118C
STRE119C
STRE120C
X STRE121C
STREIZZE
TRETRETOR
INSINCIESU
STRE124C
STRE125C
STRE126C
STRE127C
STRE128C
STRE1200
eTDELIAC
STREISUL
Y=STRE151C
RESTRE132C
STRE133C
NTSTRE134C
STRE135C
STRE136C

COMMON / / NUMNP, NUMEL, NUMMAT, NUMPC, ACELX, ACELY, HED(8), NNN, NP, INIT 20 1 NPCAV, REFPRS, DEPTH, NRLS, N, VOL, I CALC, IBACK, MJDINT, MTENS, NIT, INIT 30 2 ITN(20), PRATIO(20), NISTOP, NEAD, NSTSRT, NANALY INIT 40 3, NCT, NCONST, NPBCP, NCAVPC INIT 50 COMMON /MATP/ MTYPE, RO(12), E(8, 12), AKD(12), MNTEN(12), MJNT(12) INIT 60 3 , CRAC(12) INIT 70 COMMON /ELDATA/IX(900,5), MTAG(900), EPS(900), STRS(900,4), SEP(900,3) INIT 80 COMMON /ARG/ RRR(5), ZZZ(5), S(10,10), P(10), RSTRS(4), LBAD, LM(4), INIT 90 1 ANGLE(4), XI, HH(6,10), C(4,4), EE(4), H(6,10), D(6,6), INIT 100 2 F(6,10), SIG(6), DSIG(6), RR(4), HSEL(31,4), DSIGZ INIT 100 3 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)=DEPTH) INIT 120 IF (NRES .EQ. =1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STR3(N,2) INIT 140 RETURN INIT 150 END INIT 160	1	SU	BR	01	UT	I	NE		I	N :	I T	5	T																																			IN	TIN		10
1 NPCAV, REFPRS, DEPTH, NRES, N, VOL, I CALC, IBACK, MJDINT, MTENS, NIT, INIT 30 2 ITN(20), PRATIO(20), NISTOP, NEAD, NSTSRT, NANALY INIT 40 3, NCT, NCONST, NPBCP, NCAVPC INIT 50 COMMON /MATP/ MTYPE, RO(12), E(8,12), AKD(12), MNTEN(12), MJNT(12) INIT 60 3 , CRAC(12) INIT 60 4 , CRAC(12) INIT 60 5 , CRAC(12) INIT 60 6 , CRAC(12) INIT 60 7 COMMON /ELDATA/IX(900,5), MTAG(900), EPS(900), STRS(900,4), SEP(900,3) INIT 80 6 , COMMON /ARG/ RRR(5), ZZZ(5), S(10,10), P(10), RSTRS(4), LBAD, LM(4), INIT 90 1 ANGLE(4), XI, HH(6,10), C(4,4), EE(4), H(6,10), D(6,6), INIT 100 2 F(6,10), SIG(6), DSIG(6), RR(4), HSEL(31,4), DSIGZ INIT 100 3 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)-DEPTH) INIT 120 IF (NRES_EQ1) STRS(N,1)=AKO(MTYPE)*STRS(N,2) INIT 140 RETURN INIT INIT INIT 150 END INIT INIT 160 <	1	CO	MM	0	N	1			1	1	٧U	MI	NF	۶,	N	IJ١	E	2	, N	U	MM	4	i	, 1	U	M	PC		A	CE	L	X	, A	C	EL	. Y	. 1	IE	D	(8)	, N	N	٩,	NP	,		IM	TIN		20
2 ITN(20), PRATIO(20), NISTOP, NEAD, NSTSRT, NANALY INIT 40 3, NCT, NCONST, NPBCP, NCAVPC INIT 50 COMMON /MATP/ MTYPE, RO(12), E(8,12), AKO(12), MNTEN(12), MJNT(12) INIT 60 3 , CRAC(12) INIT 60 4 , CRAC(12) INIT 70 5 , CRAC(12) INIT 70 5 , CRAC(12) INIT 70 6 , CMMON /ELDATA/IX(900,5), MTAG(900), EPS(900), STRS(900,4), SEP(900,3) INIT 80 6 , COMMON /ELDATA/IX(900,5), MTAG(900), EPS(900), STRS(4), LBAD, LM(4), INIT 90 1 ANGLE(4), XI, HH(6,10), C(4,4), EE(4), H(6,10), D(6,6), INIT 100 2 F(6,10), SIG(6), DSIG(6), RR(4), HSEL(31,4), DSIGZ INIT 2 F(6,10), SIG(6), DSIG(6), RR(4), HSEL(31,4), DSIGZ INIT 3 TRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)-DEPTH) INIT 1 INIT 100 3 STRS(N,1)=AKO(MTYPE)*STR3(N,2) INIT RETURN INIT INIT END INIT INIT	1	N	PC	4	۷,	R	EF	P	R	S	, 0	EI	P1	ſΗ		NR	1E	S	, N		V	JL		1	24	L	C,	I	B	AC	K	, 1	мJ	0	IN	IT	۰,	11	E	NS	, 1	NI	1,	,				IN	TIV		3C
3,NCT,NCONST,NPBCP,NCAVPC INIT SCOMMON /MATP/ MTYPE,RO(12),E(8,12),AKO(12),MNTEN(12),MJNT(12) INIT SCOMMON /MATP/ MTYPE,RO(12),E(8,12),AKO(12),MNTEN(12),MJNT(12) INIT SCOMMON /ATP/ MTYPE,RO(12),FC(8,12),MJNTEN(12),MJNT(12) INIT SCOMMON /ATP/ MTYPE,RO(12),FC(8,12),MJNTEN(12),MJNT(12) INIT SCOMMON /ATP/ MTYPE,RO(12),FC(8,12),MJNTEN(12),MJNT(12) INIT SCOMMON /ATP/ MTYPE,RO(12),FC(8,12),FC(900),STRS(900,4),SEP(900,3)INIT SCOMMON /ATP/ MTYPE,RO(12),FC(900,5),FTRS(900,4),SEP(900,3)INIT SCOMMON /ATP/ MTYPE,RO(12),FC(900,3)INIT SCOMMON /ATP/ MTYPE,RO(12),FC(10),FC(10),FTRS(4),LBAD,LM(4),INIT INIT SCOMMON /ATP/ MTYPE,RO(12),FC(10),FTRS(4),LBAD,LM(4),INIT INIT SCOMMON /ATP/ MTYPE,RO(12),FTRS(10,10),FC(10),FTRS(4),LBAD,LM(4),INIT INIT I	2			1	TN	10	5())		PI	RA	T;	IC) (2	0)	,	N;	19	T	OF	Ρ,	N	•	EA	D	, h	15	T	S A	T	, 1	NA	N	AL	. Y												11	TIV		4C
COMMON /MATP/ MTYPE,RO(12),E(8,12),AKD(12),MNTEN(12),MJNT(12) INIT 60 SCRAC(12) INIT 70 COMMON /ELDATA/IX(900,5),MTAG(900),EPS(900),STRS(900,4),SEP(900,3)INIT 80 COMMON /ARG/ RRR(5),ZZZ(5),S(10,10),P(10),RSTRS(4),LBAD,LM(4), INIT 90 COMMON /ARG/ RRR(5),ZZZ(5),S(10,10),P(10),RSTRS(4),LBAD,LM(4), INIT 100 PECON // ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6), INIT 100 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)=DEPTH) INIT 100 IF (NRES .EQ. =1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STR5(N,2) INIT 140 INIT 140 RETURN INIT INIT INIT 160	3	, N	CT	, 1	NC	0	N S	3 T		N	98	CI	P	, N	C	4 V	P	C																														11	TIV	9	5C
i ,CRAC(12) INIT 70 COMMON /ELDATA/IX(900,5),MTAG(900),EPS(900),STRS(900,4),SEP(900,3)INIT 80 COMMON /ARG/ RRR(5),ZZZ(5),S(10,10),P(10),RSTRS(4),LBAD,LM(4), INIT 90 I ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6), INIT 100 P F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIGZ INIT 100 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)-DEPTH) INIT 100 INIT 100 STRS(N,1)=AKD(MTYPE)*STR5(N,2) INIT 100 INIT 100 RETURN INIT INIT 100 END INIT 100 INIT 100	1	00	MM	0	N	1	M	T	P	1	M	T	YF	PE	,	RC)(1 8	2)	,	E	(8		17	2)		AH	()	0	12)	, 1	MN	IT	E١	J (12	2)	,	MJ	N'	T (11	2)				IM	TIN		6C
COMMON /ELDATA/IX(900,5),MTAG(900),EPS(900),STRS(900,4),SEP(900,3)INIT 80 COMMON /ARG/ RRR(5),ZZZ(5),S(10,10),P(10),RSTRS(4),LBAD,LM(4), INIT 90 1 ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6), INIT 100 2 F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIGZ INIT 100 3 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)=DEPTH) INIT 120 IF (NRES .EQ. =1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STR5(N,2) INIT 140 INIT 140 RETURN INIT 150 INIT 160 END INIT 160 INIT 160	5						CF	1	C	0	15)																																				I	TIV	1	7 C
COMMON /ARG/ RRR(5),ZZZ(5),S(10,10),P(10),RSTRS(4),LBAD,LM(4), INIT 90 ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6), INIT 100 P F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIGZ INIT 110 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)=DEPTH) INIT 120 IF (NRES .ER1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STR3(N,2) INIT 150 RETURN INIT 150 END INIT 160	1	CO	MM	0	N	1	EL	.D		T/	4/	I	X ((9	0	0,	5) (, M	T	A (G (9	0 ())		EP	.5	0	90	0) (, 5	IT.	RS	3 (9(0 0		4)		BE	PI	(9	00	1	3)	IN	TIN	ł	8C
ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6), INIT 10C P F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIGZ INIT 11C STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)=DEPTH) INIT 12C IF (NRES .EQ. =1) STRS(N,2)=0.0 INIT 13C STRS(N,1)=AKD(MTYPE)*STR3(N,2) INIT 15C RETURN INIT 15C END INIT 16C	1	CD	MM	01	N	1	AF	۹G	1	1	R	R	(5	5)		Z 2	Z	(5)	,	S (()	0	. 1	0)	, F) (1 (0)	,	R	5 T	R	5 (4) ,	. L	B	AD	1	M	(4	4)	1			It	TIV		90
P F(6,10),SIG(6),DSIG(6),RR(4),HSEL(31,4),DSIGZ INIT 110 STRS(N,2)=REFPRS+R0(MTYPE)*(ZZZ(5)-DEPTH) INIT 120 IF (NRES .EQ1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STR5(N,2) INIT 140 RETURN INIT 150 END INIT 160	1									1	A N	GI	. 6	E (4),	X	I,	, н	H	((5,	1	0 ;	•	C	(4	1,	4),	E	E	(4	1)	.+	10	6	, 1	0),	D	(6	, (5)	,			I	TIV	1	0 C
STRS(N,2)=REFPRS+RO(MTYPE)*(ZZZ(5)=DEPTH) INIT 120 IF (NRES .EQ. =1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STR5(N,2) INIT 140 RETURN INIT 150 END INIT 160	2									_	F (6	, 1	0)	, 5	I	G ((6)	, [)9	I	G	(6)	, F	R	(4)		H	SE	Ľ	(]	51	,1	4)		DS	11	GΖ						IN	TIV	1	10
IF (NRES .EQ1) STRS(N,2)=0.0 INIT 130 STRS(N,1)=AKD(MTYPE)*STRS(N,2) INIT 140 RETURN INIT 150 END INIT 160		5 T	RS	0	N,	2)=	R	E	FI	PR	8	+ F	10	(M 1	Y	PE	E)	×	(7	ZZ	Z	(5	5)	-	DE	P	TI	H)																		IN	TIV	1	2C
STRS(N,1)=AKD(MTYPE)+STRS(N,2)INIT 140RETURNINIT 150ENDINIT 160		IF	_(N	RE	9	•	,Ε	Q	•	-	1)	5	T	RS	10	N,	, 2)	= ().	0																									I١	TIN	1	30
RETURN INIT 150 END INIT 160	1	ST	RS	(1	Ν,	1) =	I A	K	0	(M	T	YF	PE)	+ 5	T	R	3 (N	, i	2)																										It	TIV	1	4 C
END INIT 160	1	RE	TU	RI	N																																											IM	TIN	1	5C
		ΕN	D																																													It	TIV	1	6C

		SUBROUTINE LOAD (JUMP, MTAP1)	LOAD	10
	C****	FROM STIFF JUMPE1	LOAD	20
	C****	FROM STRESS JUMPES - ONLY NEED P(9) AND P(10)	IDAD	30
		COMMON / / NUMNP, NUMEL, NUMMAT, NUMPC, ACELX, ACELY, HEDRAL, NNN, NP.	LOAD	40
		1 NPCAV, REFPRS, DEPTH, NRES, N. VOL, NCALC, TRACK, MIDINT, MTENE ATT	LOAD	HU FC
		2 ITN(20), PRATIC(20), NISTOP, NEFAD, NGTOPT, NAMALY	LOAD	50
1		3. NCT. NCONST. NPBCP. NCAVPC	LUAU	OL.
. 1		COMMON /MATP/ MTYPE, PO(12), F(8, 13), AKO(13), MUTEN(13), MUTEN(13)	LUAD	10
		1	LUAD	80
		COMMON JELDATA ITY (900 E) HTAC (000) FOR (000) ADDRESS AND ADDRESS	LOAD	90
1		COMMON (APC/ PPP/E) 777(E) 0(10 (0), EP3(900), STRS(900, 4), SEP(900, 3)	LOAD	100
		COMMON /ARG/ RER(3),222(5),5(10,10),P(10),RSTRS(4),LBAD,LM(4),	LOAD	110
		ANGLE(4),XI,HH(6,10),C(4,4),EE(4),H(6,10),D(6,6),	LOAD	120
1		<pre></pre>	LOAD	130
		UIMENSIUN HS(31), X(3, 10)	LOAD	140
		EQUIVALENCE (MS(1),X(1,1))	LOAD	150
		IF (NCALC "LE. 3 .AND. JUMP .EQ. 1) GO TO 500	LOAD	160
- 1		READ(MTAP1) NI, S, HH, RRR(5), ZZZ(5), C, P, HSEL	LOAD	170
Ŧ		NENI	LOAD	180
	500	LUNTINUE	LOAD	190
1		MTYPE=IX(N,5)	LOAD	205
1		IF (NCALC .EQ. 1 .AND. NCT .EQ. 1 .AND. NNN .EQ. 1	LOAD	210
		AND. NIT .EQ. 1) GO TO 105	LOAD	225
		IF (NCALC .EQ. 1) GO TO 105	LOAD	230
	C***	DO NOT CLEAR GRAVITY FOR FULL CALCULATION	IDAD	245
		DO 100 I=1,10	LOAD	250
	100	P(I)=0.0	LOAD	240
1	105	DO 110 I=1,4	LOAD	270
1	110	RSTRS(I)=0.0	LOAD	200
		IF (MTAG(N).EQ.0) GO TO 400	LOAD	200
		IF(E(2, MTYPE) .LT. 2.) GO TO 400	LOAD	240
1		IF (NCALC .NE. 1. OF. NNN. GT. 1) GO TO 200	LOAD	300
		IF (NREAD .EQ. 1. DR. NCT. GT. 1) GD TD 200		310
		IF (NRES .ER. 0 .OR. NRES .ER. 2) GD TD 200	LUAU	326
3		DO 120 I=1,3	LOAD	336
1	120	RSTRS(I)=-STRS(V,I)	LUAD	346
		RSTRS(4)=RSTRS(3)	LUAD	350
		IF (JUMP , EQ. 1) GO TO 200	LUAD	300
÷.		DD 270 1=1.3	LUAD	370
		STRS(N,I)=STRS(N,I)+RSTRS(I)	LUAD	380
	270	CONTINUE	LUAD	390
T.	200	CONTINUE	LUAD	400
		DO 310 T=1.3	LUAD	410
	310	RSTRS(I)=RSTRS(I)=SEP(N,I)	LUAD	420
1	C		LUAD	430
1	-	1F (1X(N.2) .FR. TX(N.3)) CD TO 340	LUAD	44C
		IF (IX(N,3) FO IX(N,4)) CO TO 740	LOAD	45C
-		$T_{\pm 4}$	LOAD	46C
T.		GO TO 350	LOAD	47C
۲.	340		LOAD	48C
	350	00 360 JEL TT	LOAD	490
2	000	DO 355 T.I.st. 31	LOAD	50C
1.	155	HS(TJ)=HSEL(TT, T)	LOAD	510
	ررز		GAD	520
-	240	DU JOV 14JUTFILU	LCAD	53C
	300	(1) - (1) - (3) (X(N) (X(1)) + X(1, 1) + RSTRS(2) + X(2, 1)	LOAD	54C
		1 MSTHS(5)*X(3,1))	LOAD	55C
	400		LUAD	56C
			LOAD	570
			LOAD	SAC

L.		SUBROUTINE JISTR	JIST	10
		COMMON / / NUMNP.NUMEL.NUMMAT.NUMPC.ACELX.ACELY.HED(8).NNN.NP.	JTST	25
	1	NPCAV, REFPRS, DEPTH, NRES, N, VOL, NCALC, IBACK, MJOINT, MTENS, NIT.	JTST	30
Ε.		TIN(20), PRATIO(20), NISTOP, NREAD, NSISRI, NANALY	JTST	40
		3.NCT.NCONST.NPBCP.NCAVPC	JIST	50
		CUMMON /ELDATA/IX(900.5), MTAG(900), EPS(900), STRS(900.4), SEP(900.3	JIST	60
8		COMMON /BANARG/ B(180), A(90, 180), MBAND, ND2, NUMBI K, MBMAX, NB	JTST	70
	1	1, MTAP1, MTAP2	JIST	BC
•		COMMON /MATP/ MTYPE, RO(12), E(8, 12), AKO(12), MNTEN(12), MJNT(12)	JIST	90
	1	L (CRAC(12)	JTST	100
E		COMMON /NPDATA/ R(999), Z(999), CODE (999), UR(999), U7(999)	JTST	110
ŧ.		COMMON /ARG/ RRR(5), Z7Z(5), S(10, 10), P(10), RSTRS(4), LBAD, LM(4),	JIST	120
		1 ANGLE(4).XI.HH(6,10).C(4,4).EE(4).H(6,10).D(6,6).	JTST	130
1	č	F(6,10), SIG(6), DSIG(6), RR(4), HSEL(31,4), DSIG7	JIST	140
		COMMON /JNT/ FN(450), FT(450), NJT	JTST	150
		DIMENSION DISP(900,2),V(4),U(4)	JTST	160
1		EQUIVALENCE (DISP, A(2000))	JIST	170
		REAL LAKNAKS	JTST	180
1		PRINT 1001	JTST	190
_ C	ES	TABLISH DISPLACEMENT ALONG AND NORMAL TO JOINT	JTST	200
1		IF (NRES .EQ1) PUNCH 2000, HED, NJT	JTST	210
1	2000	FORMAT (8A10,/* INITIAL STRESSES FOR JOINTS*/15)	JTST	22C
		NJT=0	JTST	230
1		DO 500 NEI,NUMEL	JTST	240
1		MAT = IX(N, 5)	JTST	250
		IF (MJOINT .EQ. 0) GO TO 500	JTST	260
1		DO 50 I=1,MJDINT	JTST	270
	50	IF (MAT .EQ. MJNT(I)) GO TO 60	JTST	280
		GC TC 500	JTST	290
	6 C	CONTINUE	JTST	300
ĩ.		KN=E(1,MAT)	JTST	310
h.		KS=E(2,MAT)	JIST	320
		NJT=NJT+1	JTST	33C
7		IF(MTAG(N).GT.O) GO TO 70	JTST	34C
ŝ.		FN(NJT)=0,	JTST	35C
		FT(NJT)=0.	JTST	360
r		GN TN 500	JTST	37C
	70		JTST	380
7		L#IX(N,1)	JTST	390
		J# IX(N/2)	JTST	400
1		UK#K(J)+R(I)	JTST	410
1			JTST	420
		<pre>HRJ=0,0+(H(J)+K(J)) 77*-0.Extractory</pre>	JTST	430
1			JTST	440
1		1.=39K+(UK#UK+UZ#UZ)	JTST	450
			JIST	460
1			JIST	4/0
k –		LO IVO II-IPA	JISI	450
		N#1A(N#11) N/TT\=_8/3+K_+\\+N7+8/3+K\+N0	1131	440
	100		JIST	500
L,	· • • • •	MONTE FEFETTVE QTDATN	1101	510
	F P C I	N POSTTIVE MEANS JOINT TO OPEN	1131	520
_ /	FDC	T POSTITVE MEANS (KK,11) MOVES ALONG HA MODE THAN (TT. 11)	1121	236
ľ	200	EPSTED.5*(U(4)=U(1)+U(3)=U(2))	1707	546
	94 V V	EPSN=0.5+(V(4)+V(1)+V(3)+V(2))	10101	550
		······································	0101	200

			TPTIL	571
10	COM	PUTE NORMAL AND SHEAR FORCE PER UNIT LENGTH AND CALCULATE STRENGT	TTET	SAC
C	INIT	IAL STRESSES INPUT ARE ALWAYS COMPRESSIVE (NEGATIVE)	1131	200
		FNRH=0_0	JISI	590
		FTRM=0_0	JTST	600
		FPNRMED_0	JIST	61C
		TECNEALE NE 1 OR NNN GT. 11 GU TO 300	JIST	620
		TE (NORE ED 1 OP NORS ED 21 60 TO 300	JIST	63C
		T = (NREAD = RO + OR + OR + OR + OF + OF + OF + OF +	JTST	64C
		[P (NREAD + EW, 1, 0R + 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,	ITST	65C
			ITST	660
		S2=DZ**2	TTST	670
Sec. 1		SC=DR+DZ	1101	680
		FNRES=STRS(N, 1) + S2+STRS(N, 2) + C2=STRS(N + S) + 2 + SC	1707	400
		FTRES=(-STRS(N, 1)+STRS(N, 2))+SC-STRS(N, 3)+(S2-C2)	1767	700
		FN(NJT)=FNRES	3131	700
		FT(NJT)=FTRES	JIST	/10
	300	DO 310 II=1,4	JIST	120
		K=IX(N,II)	JIST	730
		V(TI) = -DISP(K, 1) + DZ + DISP(K, 2) + DR	JTST	74C
	310	U(TT)=DTSP(K,1)+DR+DISP(K,2)+DZ	JTST	75C
		TEPST=0.5*(U(4)-U(1)+U(3)-U(2))	JTST	76C
1		TEPSNE0.5 + (V(4) - V(1) + V(3) - V(2))	JTST	77C
		FN(NIT)SKN+FPSN+FN(NJT)	JTST	78C
		TE (EN(N)TT) = E = 0.3 GO TO 201	JTCT	790
			JTST	800
			JTST	810
	2.0.4		JIST	820
	201	$\frac{1}{1} \left(\left[$	JIST	830
1.		IF LIEPSN . UI. ELDIMATIJ BU TU EVE	JTST	84C
L C		WARA AND DE THOUT AN A NECATIVE ONANTITY	JTST	850
' C	E(5,	MAT) SHOULD BE INPUT AS A NEGATIVE QUANTITY	TTOT	865
C			TTOT	870
ι		FNRH#KN*(TEPSN=E(5,MAT))	1707	880
		EPNRM=TEPSN=E(5, MAT)	1101	900
	505	FT(NJT)=KS*EPST+FT(NJT)	J 131	040
1		STREN = 0.	J151	400
1		IF (FN(NJT) .GE. 0.) GO TO 205	JIST	910
•		IF (TEPST .EQ. 0.) GU TO 210	JIST	920
		STREN = E(3, MAT) + ABS(FN(NJT)) * TAN(E(4, MAT) * 0.01745329)	JIST	930
1		IF (ABS(FT(NJT)) .LT. STREN) GO TO 210	JTST	940
ŧ.,		IF (FT(NJT) .LT. 0.) GO TO 203	JTST	950
		FTRM=FT(NJT)+STREN	JTST	960
		Gr. TO 210	JTST	970
1	201	FTRME FT(NJT)+STREN	JTST	980
F	2 V 3	CO TO 210	JTST	990
	DAE	FTDM+FT/NIT)	JTST	1000
T.	213		JTST	1010
	210	DOTNT 1000 N DOT. 77.1. EN(NIT) . ET(N.TT) . TEPSN. TEPSN. FPSN. FPST. FNRM.	JTST	1020
	220		JTST	1030
		T THE THE STAR STARTS STATES	JTSI	1040
1		THE CARES SENS TO FUNCH 2100 PROCESSION CONTRACTOR	JTST	1050
	5100	FURMAT (Cr20, 7, 17)	.17.91	1040
		IF (EPNRM .EQ. 0.) GU TU 421	1701	1070
2		EPNRM=EPNRM+0.5	170	11070
1		DN 420 II=1,4	113	1000
		K=IX(N,II)	J13	11040
		SIGNT=1.	JIS	11100
		IF (II .GT. 2) SIGNT==1.	JTS'	11110
		IF (CODE(K) .EQ. 3) GO TO 420	JTS'	11150

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		A REAL PROPERTY OF THE RE	
		IF(COPE(K) +EQ, 1) GO TO 415	JTST113C
		DISP(K,1)=DISP(K,1)=SIGNT+EPNRM+DZ	11511140
		1F (CODE(K) .EQ. 2) GO TO 420	17071150
	415	DISP(K, 2) =DISP(K, 2) + SIGNT+FPNPN+DP	JI311150
	420	CONTINUE	JISTILEC
	421	CONTINUE	JTST117C
			JTST118C
		IF (FNRM .CQ. 0. AND. FTRM .EQ. 0.) GO TO 431	JTST119C
		IFLEPNEM .NE. 0.) GC TO 425	JTST120C
		FN(NJT) = FN(NJT) - FNRM	JTST121C
	425	FT(NJT) = FT(NJT) - FTPM	JTST122C
		FNRM#FNRM+0.5	JTST123C
		FTRM#FTRM+0.5	11511240
		DZ=DZ+L	TETIOFC
		DR=DR+L	TETIOLE
		D0 430 II=1,4	JI31120L
		K=IX(N,II)	J151127C
		SIGNTE1.	J131128C
		IF (IT GT. 2) STONTE-1	JIST129C
			JTST130C
		IE (CODE(K) = EG = S) = GO = TO = SO	JTST131C
		$\frac{1}{10} \frac{1}{10} \frac$	JTST132C
		TE (CODE(K) - EO - D - OF FORMADR)	JTST133C
			JTST134C
	420	UZ(K)=UZ(K)=SIGNT+(FNRM+GR+FTRM+DZ)	JTST135C
	430	CUNTINUE	JTST136C
	451	CINTINUE	JTST137C
	500	CONTINUE	JTST138C
		RETURN	JISTISOC
1	1000	FORMAT (15,2F8,2,8E13,5)	11911400
	1001	FORMAT(1H1, 6HEL NO., 4X, 1HX, 5X, 1HY, 3X, 12HNORMAL STRS. 13H TANGTI	ST ITST1/14C
	1	IRS., 14H TOT. NOR. DISP., 14H TOT. TANGDISP., 14H DEL NOP DIED . 14H	FL TTETINGE
	ž	2TANGDISP., 12H REMOVD SIGN, 12H REMOVD SIGT //)	TOTINE
		END	11011436
			J181144C

and the second second second

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			SU	81	10	UT	1	NE	F	PL	_ A	5 T		(N	E.X	I	T)										_				_									EPLA	10
4 C	***	k:	TH	I	5	SU	8	RO	UT	11	NE	C	A	- C	UL	4	TE	S	3	TP	RE	35	5	IN	E		EM	EN	IT.		T i	ΥI	EL	D						EPLA	20
			CU	Mł	1()	N	1		/		٩U	MN	IP,	, N	IN	EI	.,	NI	JM	M	L T	# ħ	U	MP	С,		CE	LX		C	EL	۷,	HE	D (8)	, NI	NN,	, NI P	•	EPLA	30
I -		1	N	P(. A	۷,	R	EF	PQ	5	, D	EP	1	••	NR	E	5,	N,	, v	OL	.,	NC		LC	, 1	8	AC	ĸ,	Μ.	10	IN	۲,	MT	EN:	8,1	NI.	Tir -			EPLA	40
1		2			1	TN	10	20),	PF	R A	ΤI	0	(2)	0)		NI	31	10	P.	, N	RE		D,	NS	17	SR	۳,	N	IN/	AL	Y								EPLA	50
		3	, N	C'	٢,	NC	ŋ	NS	τ,	NF	Þ g	CP	., 1	NC	AV	P	5																							EPLA	60
			Cin	M	٩Ŋ	N	1	MA	TP	1	M	TY	P	E,	RC	10	12	3	E	(8	ι,	12	1	, Α	KC	10	12).	MP	T	EN	(1	2)	, M.	JN'	TC	12)			EPLA	70
		1						CR	AC	0	12)														·									-		• - •			EPLA	BC
100			cr	0	iÒ	N	1	ĒL	DA	T	1	ĪX	1	90	0,	5),	M	T A	G	(9	00	1	. E	PS	0	90	0.1		TI	28	(9	0.0	.4	1.5	SEI	P (9	00	.3	FPLA	90
			Ċņ	M	10	N	1	54	NA	R	3/	8	10	18	01		AC	9		18	30).	MI	RA	NC		ND	2.	NI	IM	3Ľ1	ĸ.	MB	MA	X . I	NB				EPLA	100
		1	, M	1	1P	1.	M	TA	PZ		•									-								-												E PLA	110
		-	cn	MI	10	N	1	AR	G/	1	R	R	5	١.	77	7	15	ά.	. 9	11	0	. 1	0	١.	P	1	0.1	. 6	81	R	1.8	41		BAI	0.1	M	(4)			FPLA	121
		1	• /				1			1	L FJ	CI.	F	14	1.	Y	7.	H	41	À.		0.3		ŕŕ	4	4	γ.	FF	11	1	H	16	1	01		16				E DI A	130
		2									= (6.	1	01		í.	. , . ,	6		D	1	6 /	6	1.	RE	11	41		191	EI.	12	1.	43	. D	ete	67				EDI A	140
			DT	M	E N	s 1	n	N	5 V	1	a n	01		ŝ	10	Ð	15	5		0.0		91	, v				- /						77		0.1.1					EDIA	150
			FO	11	r v	41	F	NC	F	è	FV		1	40	0.0	1	1																							EDIA	140
			DE	=	• •				-		'			- 0			/																							CPLH.	100
			nv	0	/ • / •	•																																		EPLA	170
			TF	1		2	M	Ŧ V	DF	5		. 1	•	2			e c		t n		7 0	0																		EDIA	100
			<u>n</u> n			2		1' 80 1	7		•	5	•	c	• /		a (.	,	10		10	0																		CPLA	140
			De	TI	De	11			12																															CPLA CDLA	200
	3.07	. .		D	1 0 1 N																																			CPLA	210
	1	J	JE	-	4 7	10	1	- V - 1	+ U E	•	•	•	-	n	*		7 0	•																						CPLA	226
			11				•	~ •	. 5		. 0	,	9	1)	10	0																						EPLA	230
	10		00	-		1	1	= 1 + T	13																															EPLA	240
	10	1	21	9	- L	11	3	21	6	4.)																													EPLA	250
			12	N	51	× (•	0																																EPLA	590
			1 E	N	52	= (•	0	0.5																															EPLA	270
			PN	= (5,	199 	11	24)				•																										EPLA	28C
			IF		(M	TE	N	8	• E	0		0)		G()	1	D	1	1	n –																					EPLA	290
			00		0	5	I	3 1	1	T	EN	5								-																				EPLA	300
	10	5	IF		(M	TY	P	E	• E	Q,	•	MN	IT	EN	(1))	G(0	T(2	15	0				_													EPLA	310
C	***	k		L	SU	LA	T	E	TE	N	5 I	LE		5 T	R	5	3	11	N	N(7	TE	N	9 I	01	1	EL	E	'E!	NT	5									EPLA	350
	11	D	CU	IN.	TI	NU	JE				_	-																												EPLA	330
			EP	3	13	31	G	(6)/	5	7.	29	95	77																										EPLA	340
			SZ	8	5 I	N	E	P 9	MJ	*1	+2																													EPLA	350
			C S	=	00	3 (E	P 9	M)	*1	*2																													EPLA	360
			CS	#	3 I	N (E	PS	M)	*(C ()	9 (E	P 5	M)																									EPLA	370
			TM	4	X Z	E (1	, M	T١	P	E)																													EPLA	38C
			IF		(M	T	G	(N)		EQ	•	1)	GC)	TC		15	0																				EPLA	390
			IF		(9	IG	60	4)		G	τ.	C	R	A C	()	T	YF	E:) *	T	MA	X		AN	D,		MT	A () (I	(/		NE		4)	G	0	TD	11	12	EPLA	40C
			IF		(3	IG	;(4)	•	L	Ε.	1	M	A X)	G	D	1(D.	1!	50																			EPLA	41C
	11	2	TE	N	91	= 5	11	G (4)	١.,																														EPLA	420
			IF		(M	TA	G	(1)		EQ	•	3		4	D	•	5	IG	(5)		G	۲.	().)	GC	<u>,</u> ,	t O	1	10								EPLA	43C
			IF		(9	10	; (5)		L	Ε.	1	M	A X)	G	D	T(C	11	2 ()																			EPLA	44C
	11	4	TE	N	<u>S S</u>	= 5	31	G (5)																															EPLA	450
	12	0	CU	IN.	t I	NL	IE																																	EPLA	46C
			T 1	E	TE	NS	11																																	EPLA	47C
			PN	2	1	.1	P	N =	Ph	1																														EPLA	4AC
ι,			TE	N	51	=1	Έ	N S	1+	PI	N2	+1	E	NS	21	P	N #	PI	42																					EPLA	490
			TE	N	52	=1	'E	N S	21	PI	N2	+1	1	*P	N	P	NZ																							EPLA	500
			RS	T	29	(1)	= 1	EN	18	1 *	c 2	+	TE	NS	2	• 5	2																						EPLA	510
6			RS	TI	28	(2	:):	= T	EN	19	1 *	92	+	TE	NS	2	*0	2																						EPLA	520
			RS	T	29	(3	5):	= (TE	N	51	-1	E	NS	2)	*	C S	1																						EPLA	530
			DO		12	5	I	= 1	, 1		-	·																												EPLA	540
			IF		(4	85	10	19	TR	S	(1))		G	۲.		1)		ΝĪ	51	ro	PE	N	15	10	P	+ 1													EPIA	550
	12	5	9 I	G	(1) 1	9	IG	(1	3.	R	ST	R	5 (11					-																				EPLA	540
				201	-	-	-					0.0		- •	~ •																										200

																																							_	
			Г, A	L	Ļ	PF	ł١	N	5 T	15	51	G)																									EPLI		570	1
÷	1	50	IF		(4	85	5 (S	I G	(1	1))	.1	E		1.	E	- 1	0	1	AN	D.	A	850	15	TG	(2)	1)		I.F.	. 1	.F	+10	160	1.10	600	NEPL A		580	
			AN	G	= F			MI	TY	PF	1				•																• •			,			-		Ear	
			AL	0	- 5		, ,	м 1																													LPLE		140	-
			E La	F				_	T																												EPLA		500	,
			PR	31	E (5	, M	T	P	E]																											EPLA		51C	
			CA	LI	L i	PF	٩I	NS	3 T	(0	9.9	IG)																								EPLA	. (520	
			IF		(N	4.1	N A	LN	1	. E	0		0		AN	D.	. (FY	(N	1)		Ť		0.1)	GO	Tr	1	16	0							EPI A		30	•
			TF	1	NC	01	r	Ē.,	= 0		4	•		in.		N 1	Ŧ		61		2		ē.u	Ť	ĥ.,	1.6	•										E DI A		LAC	
			TE	ì														. :	91	-	<u>، د</u>	′ .	90	A	5	TO	0 6 / 1 3		r	•		~					CPLA		546	
			1.0				5 L.	T	٠	1910		1				•	IN .	11			•	1	•	a nu c	•	N .	3		• 5	14 .	0)	6	U I	0 1	00		CPLA		150	
			1 1		()	Ψ.((IN)	•	LI	•	0)	60		rQ.	1	60)																	EPLA	(996	£
			ns	1	GΖ	= ().	51	• (0.5	3 T	G (4) +	DS	IC	50	5)	• (0	SI	G (4)	-05	51	G ('	5)) * (9 I	NC	A NG	;))					EPLA		570	•
	1	01	SI	G	7 T	= 5	ST	25	5 (NI,	4)+	US	51	GΖ	-	N	* (RS	ST	RS	(1)+	RSI	R	SC	2))									EPLA		36	
			56	7	T T	= 5	S I	67	ZT																												F PLA		or	•
			\$6	7	T =		T G	7	1																												C DL A		100	
			eT					-			•	~ /	E 1		0	•																					EFLA		ruc.	1
				1	1 -	3	10		* /	13	э т .	61	2		31	194														_	1.1						EPLA		10	
			51	J	2=	((9	10	9 (4)		51	6	5))	*1	-2	+ (51	G	(5) =	51	GZ1	()	**;	2+1	(3)	ŢĢ	ZT	-SI	G (4))	**5)/6		EPLA	1	150	
			FA	K	= A	LF	*	5.1	IJ	1 -	F	K																									FPLA		130	
			SP	11	2=	SO) R	T	(S	T J	51)																									EPLA		140	ь
			FY	2:	=F		(+)	S	L S	2																											FPLA		150	
C																																					LDIA		160	•
-			TE		15	V 2		0	15		•	0	1	C	n	70	•	• •	5																		EFLA		100	
						10			36	•	.0		1.					10	2																		EPLA	1	110	5
			15		<u> </u>	A) (N	•	P 1		•)		11	AG	C	1	= <u>5</u>																			EPLA		180	
			IF	C	MŢ	A	5 (N	• (EG	•	5)		11	A G	0	()	= 2																			EPLA	1	190	,
			IF	0	MŢ	A (G (N.).	EG	•	4)	۴	1 T	A G	()	1):	= 1																			EPLA	. 8	300	
			ST	R	9 (N	, 4):	S S	TH	25	(N	,4	1)	+P	NI	- (DS	IG	; (4)	+0	SI	GC	5)) = 1	PNI	. (1	RS	TR.	5(1)+	RSI	PS (211		EPLA	1	310	•
			GC	1	T		57	0																							• • •						F PI A		100	•
	1	65	rn	N.	T T	NI	IF	•																													EPLA		14.5	
	•		TE	1				N . 1		5 0	•	• •		4.7				- /1																			EFLA	0	121	
			4.0			AC	9 (- /	14 2	•	E 9	•				е) щ С			- 4																			EPLA	e	4 25 2	
			17	C	4 T		9 (N	•	26	-	2)		1	A (;	()	•):	= 5																			EPLA	8	356	6
			IF	C	MŢ	A (5 (N]	• •	EG	•	3)		4 T -	▲ G	()	1):	= 6																			EPLA			
			IF		(🔺	RS	3 (FI	K)		LT	•	0	. 0	00	1)	GC) '	TO	1	70														EPLA	1	1.	
			FY	21	91	2 -	F	YP	21	FA	K																										FPLA		1.0-	
			GO	1	TO	1	17	5																													E DI A			
	1	70	FY	21	T	= 1	n n	·																													EPLA			
	-	76	-	AL I		1.1	187	•																													EPLA		0-	
	1	15		1.4	11	IN T	JE	-		~ -				-					-				2														EPLA		1 4 -	
			15		(=	Ye		T	٠	GI	•	0	• (2)	N]	5	τņ	141	IN	IS	T()	P +	1													EPLA	1	150	
			Tb		(P	Ye	K	T		GE		0	• 1	5)	CF	Y	- 1	• (EPLA	1		,
			IF		(F	YZ	58	T		L1	•	0	. 1	5			D		FΥ	121	RT		GĿ	. ().	1)	CF	FYI	= ()	. 7	5						EPLA	0	94C	
			IF		(F	YZ	R	T		LI		0	. 1	0)	CF	Y	= 0	. 5	50		-				1	-			÷ .							FPI A	c	1.1	ē.
			IF		(F	Y	N)		GF		0	.1		Gn		n	7	0.0)																	FDIA	e	367	
0	* *	* *	FI	9	TC	01)	11	•	76	P	n	Ri	17	5	10		6.5		F	71	50	0														LPLA		100	4
e	1		. (0.	4 (9			- 1		50		4	J	/ 1	r		11	01	G	Ē	2		.,1														EPLA		11	6
C												• -																									EPLA	9	38	ł.
			DJ	13	= D	51	G	(4	1)	+ D	5	IG	(5))	+0	51	G	L																			FPLA	<	990	
			DJ	2:	E (([)5	IC	;(4)	-	DS	IG	6 (!	5)) +	t th i	2+	(0	S	IG	(5) =	081	IG:	Z):	**2	+									EPLA	1.0	000	
		1	l			([)§	IC	şΖ	• 0	9	IG	(4	1))*	*2	2)	16																			EPLA	10	11.	
			DF	=	L	PI	D	JI	+	36	R	TC	D	12)				-																		FPI A	11	120	
			TF		(]	8	51	D	1	- 4	E.	F	1		ÔF		0	1	6 m	1	TO	5	00														COLA	4 4	120	2 •
			DE			2		Ē	'	•	E I	•		٠	ν C	- 1	0	,	91.	1	10	2	., 0														EPLA	10	126	
			200	-1	ा २ ह	E /		r m f		1																											EPLA	1(140	,
	_				23	U	1	-	1	2																											EPLA	1 (050	
	5	50	SI	G	(I)=	:5	10	;(I)	•	09	IG	6 ()	I)	*F	F																				EPLA	10	050	
			SG	2	t t	2						(1	•	R	F)	*F	N	+ (DS	11	G (4	4)	+D.	SIG	5(5)) - F	N	* (RS	THS	(1)+R	STR	\$ (2))	EPLA	10)7C	
		1	+5	T	R'S	(1	١,	4])													,				20				_							FPI A	10	Ar	•
			ST	G	71	8.5	36	71	T	+ A	F	* 0		*	()	91	G	(4	14	D		G r	51		9 (TG	4	-		TG	151	3+	STA	1 A M	611		FOLA	+ /	10-	
			CT	1	1 -	01	in	2	1			C (21	-		71	-		, ,				11			10	-		00	1.13	())	14	914	LAN	911		CPLA	1.1	40	1
			01		3-	31	19 1 m	11		+0		5 (a Ŧ	e J o A			L	1			~																	EPLA	11	UC	
			51	J	2 8	C	5	16) (1)	•	21	G (2))	* 1	2	• (51	6	(2)) =	5G.	211		**	=+(3(GZ	TT	-51	G (1))	**5	1/6	.+	EPLA	11	110	
		1				5	51	G (3) *	*	2																									EPLA	11	25	6

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300	CONTINUE	EPLA113C
	NEP=1	EPLA114C
	VSTED	EPLA115C
310	CALL STRSTR(STJ1, STJ2, SG7TT, NEP.N, NCALC, NEXTT)	FPLA116C
	00 350 fs1.4	FPLA117C
	STG(I)=0	60141160
75.0		EPLATIAC
326	SIG(I) = SIG(I) + C(I,K) + HH(K)	EPLA1200
	DSIG22=SIG(S)	EPLAIPIC
	SIG(3)=SIG(4)	EPLA122C
360	CONTINUE	EPLA123C
C		EPLA124C
C++++	CALCULATE EXCESS STRESS TO BE SUPPORTED BY BODY FORCES	EPLA125C
С		EPLA126C
	Dr. 370 TE1.3	EPLA127C
370	SEP (N. T)=DSIG(T)=SIG(T)	EPLA12AC
	051673-08167-081677	EDIA1300
r	191923-03102-031022	
500	C (18) Y T 8111 C	
1416		EPLAISIC
		EPLA1320
505		EPLA133C
210	SIG(I)=SEP(N,I)+OVAX	EPLA134C
520	SIGZNE SGZI- DSIGZS+OVRX	EPLA1350
	SGZTTESIGZN	EPLA136C
525	CONTINUE	EPLA137C
	DO 550 I=1,3	EPLA138C
550	SIG(I)=SIGP(I)-SIG(I)	EPLA: 39C
	STJ1=SIG(1)+SIG(2)+SIGZN	EPLA140C
	STJ2=((SIG(1)=SIG(2))**2+(SIG(2)=SIGZN)**2+	EPLA141C
	1 (SIGZN=SIG(1))**2)/6.+SIG(3)**2	EPLA142C
	NSTENST+1	EPLA143C
	IF (DVRX .EQ. 1 .AND. NST .EQ. 1) GO TO 310	EPLA144C
	FYCUR=ALP+STJ1+SQRT(STJ2)=FK	EPLA145C
	IF (E(7. HTYPE) .LT. 0.0001) GO TO 555	FPLA146C
	TE (OVRY . EQ. 1.) GO TO 552	FPLA147C
	TE (EVELIP	EPI A1/JRC
562		
136	TE (EVEND IT EVENDED TO ESE	
	TELNING OF IN CO TO EES	EPLAINUL
	TE LOUDY OF A EX CO TO FEE	EPLAIDIC
		EPLA152C
		EPLA153C
	Gr Tr 505	EPLA154C
555	CONTINUE	EPLA155C
	DC 560 I=1,3	EPLA156C
560	SEP(N,I)=SEP(N,I)+OVRX	EPLA157C
	PRINT 2000, FY(N),FY2,FY2RT,FYCUP,OVRX,SIGZT	EPLA158C
	STRS(N, 4)=SIGZN	EPLA159C
2000	FORMAT (22x,8E12,4)	EPLA160C
570	FY(N)=FY2	EPLA161C
600	CONTINUE	EPLA162C
	DP 650 I=1,3	EPLA163C
650	SFP(N,I)=SEP(N,I)+RSTRS(I)	EPI A164C
700	CONTINUE	FPI A1650
	RETURN	FPLA144P
	FND	EDI 11470
		SELEID/L

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	SUBROUTINE STRETE (STJ1, STJ2, SIG7T, HEP, N, NCALC, NEXIT)	STRS	10
	COMMON /ELDATA/IX(900,5), MTAG(900), EPS(900), STRS(900,4), SEP(900,3)STRS	20
	COMMON /MATP/ MTYPE, PO(12), F(8, 12), AKO(12), MNTEN(12), MJNT(12)	STRS	30
	1 ,CPAC(12)	STRS	40
	COMMON /ARG/ PHR(5),777(5),S(10,10),P(10),KSTRS(4), 1840,18(4),	STHS	50
	1 ANGLE (4) XT. HH(6.10) . C(4.4) . FE(4) . H(6.10) . D(6.6) .	STRS	60
	2 F(6,10), STG(6), USTG(6), HR(4), HSFL(31,4), DSTG7	STRS	70
	DO 100 T=1.4	STDS	Ar
		CTUS	90
		CTOC	100
100		0100	100
7.000		5145	110
		SIRS	120
		STRS	150
	1 F (MIAG(N) 6 T 3) 61 11 200	STRS	140
104	CONTINUE	STRS	150
	111 105 KKZ1,4	STRR	160
105	£E(**)=E(**+1,*T*PE)	STRS	170
C		STRS	180
C++++	MTAGE1 MEANS THAT BOTH PPINCIPAL STRESSES ARE COMPRESSIVE	STRS	190
C****	"TAGE? MEANS THAT ONLY THE MAJOR PRINCIPAL STRESS IS TENSILE	STKS	500
·****	MTAGES MEANS THAT BOTH PRINCIPAL STRESSES ARE TENSILE	STES	212
C****	MTAGE4 MEANS THAT THE ELEMENT FAILS IN COMPRESSION	STRS	SSC
C****	"TAGES MEANS THAT IT FAILS UNDER TENSILE MAJOR PHINCIPAL STRESS A	NSTRS	230
[****	MTAGES MEANS THAT IT FAILS UNDER BUTH TENSILE PRINCIPAL STRESSES	ASTRS	240
C		STRS	250
	IF ("TAG(N)=2) 182,184,183	STRS	292
182	EE(3)=EE(1)	STRS	270
	GN TO 184	STRS	280
183	EE(1) = EE(3)	STES	290
184	EE(1)=EE(1)/(1.0-EE(2)**2)	STRS	300
	EE(3)=EE(3)/(1,-EE(2)++2)	STRS	310
	EE(2)=EE(2)/(1.=EE(2))	STRS	320
	XX = EE(1)/EE(3)	STRS	330
	COMM#EE(1)/(XX-EE(2)++2)	STRS	340
	C(1,1)=C(1MH+XX	STRS	350
	C(1, 2) = CDMM + EE(2)	STRS	365
	C(2,1)=C(1,2)	STES	370
	C(2,2)=C()MM	STRS	JAC
	C(3,1) = C(1,2)	STRS	390
	C(3,2)=C(1,2)	STRE	400
	C(4,4) = .5 + EE(1) / (XX + EF(2))	STPC	410
	GO TO 300	STRE	120
200	00 210 1=1.3	STRC	430
	STG(T) = STRS(N,T) - SER(N,T)	STDE	440
210	CONTINUE	STPC	150
	SIGZT=STPS(N,4)	STPS	450
	ST.J1=SIG(1)+SIG(2)+SIG71	QTUQ	170
	STJ2=((ST)(1)+STG(2))++2+(STG(2)-STG7T)++2+(STG(1)-STG7T)	GTDE	120
	1++2)/6_0+\$10(3)++2	6700	401
250	SRIDE SOUT(STID)	STUP	440
6.10	TF (STJ2	SIKS	SUL
	NEYTTENEYTTAI	SIRS	510
	POTNT 2000. N.STIL STI2	3185	520
2000	FOUNATION ALAGAMAA DV AEL NO AA TE EV ATAAA PAE E ATAAA TAE EN	SIRS	230
000 <u>3</u> ^*¢		STRS	540
¢/0		STRS	550
		PATE	560

		0.110 F.7.5
		STRS 571
	FK=F(H,MTYPF)	STRS 58C
	EC=E(P,MTYPE)	STRS 590
	EG=FC/((1,+PN)*2.)	STRS 60C
	FK=FC/(3,*(1.+2.*PN))	STRS 61C
	HD=1.+9.*(ALP**2)*EK/EG	STRS 62C
	H1=(1,5*EK*ALP/EG=STJ1/(6,*SRJ2))/(SRJ2*HD)	STRS 63C
	H2=((ALP=STJ1/(6.+SRJ2))+(3.+EK+ALP/EG=STJ1/(3.+SRJ2))=	STRS 64C
	3. *PN*EK*FK/(EC*SRJ2))/HD	STRS 650
	H3=0.5/(STJ2+H0)	STRS 460
C		STUS ATC
C++++	CALCHEATE FLAGTO-PLACTIC STRESS-STRATE DELATIONS ATD	
r	CHEGODALE CERCICALERGITE SINEGRASHIER KEENITONSHIE	
	6/1 11-2 AFRA(1 -42-2 ANTARTC/12 ATARTC/12 ATA	
		STRS TUL
	$(1) < j = 2 \cdot \times E_{0} \times (H < H) \times (S_{1} \in (1) + S_{1} \in (2)) + H \le S_{1} \in (1) \times S_{1} \in (2))$	STRS 71C
	L(1,4)==2,*LG*(H1*SIG(5)+H5*SIG(1)*SIG(5))	STRS 72C
	C(2,1)=C(1,2)	STRS 73C
	C(2,2)=?.*EG*(1H2=2.*H1*SIG(2)=H3*SIG(2)**2)	STRS 74C
	C(2,4)=-2,*EG*(H1*SIG(3)+H3*SIG(2)*SIG(3))	STHS 750
	C(3,1) = -2 * EG * (+2++1*(SIG(1)+SIGZT)++3*SIG(1)*SIGZT)	STRS 76C
	C(3,2)==2,*FG*(H2+H1*(SIG(2)*SIGZT)+H3*SIG(2)*SIGZT)	STRS 77C
	C(3,4) = -2, *EG*(H1*SIG(3)+H3*SIG(3)*SIGZT)	STRS 78C
	C(4,1)=C(1,4)	STRS 79C
	C(4,2)=C(2,4)	STRS BOC
	C(4,4)=2.*EG*(0.5-H3*SIG(3)**2)	STRS BIC
C		STPS A2C
300	JF(EPS(N), EQ. 0.0) GO TU 400	STRS 83C
C		STRS 84C
	SS=SIN(EPS(N))	STRS 850
	CC=COS(FP3(N))	STRS BAC
	\$2=\$\$ * \$\$	STRS BTC
	02=00+00	STUS BAC
	SC=SS+CC	STRS POR
	D(1,1)=C2	STPS PAC
	0(1,2)=52	STRE DIC
	0(1,3)=0	
	D(1, 4) = SC	5709 07C
	D(2,1)=02	
		3183 44L
		5148 450
		STR8 460
		STRS 97C
		STR5 98C
		STRS 99C
	((3, 5) =), (0)	STRS100C
	D(3, 4)=0, 1	STRS101C
	0(4,1) = -2.0 + 5C	STRS102C
	D(4,2) = -D(4,1)	STRS103C
	1)(4,3)=0,0	STRS104C
	0(4,4)=C2=82	STRS105C
	DO 350 II=1,4	STRS106C
	00 350 JJ=1,4	STRS107C
	H(II,JJ)=0.0	STRS108C
	DN 350 KK=1,4	STRS109C
350	H(II,JJ)=H(II,JJ) +C(II,KK)+D(kK,JJ)	STRS110C
	DO 360 II=1,4	STRS111C
	00 360 JJ=1,4	STRS112C

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I.	B-36	
360 400	C(II,JJ)=0.0 DD 360 KK=1,4 C(II,JJ)=C(II,JJ)+D(KK,II)+H(KK,JJ) CONTINUE RETURN END	STRS113C STRS114C STRS115C STRS116C 3TRS117C STRS118C
I		
I		
1		
1		
1		
1		
1		
4		
1		
1		
1	5	
1		
1		
		1

	CHRISTING ADDRESS AND A THE ADDRESS BACK ALL AN YOUTET AND ODATED	NDEO	10
	SUBRUITINE NPFORCENUMPE, IJBE, NPCAV, PSCA, NE, NM, KSHIFT, NNN, PRATEU,	NETT	10
1	R,Z,B,NPCA,CODE)	NPEQ	20
	DIMENSION IJBC(50,2), PSCA(75,3), PSBC(6), PRATIO(20), R(999),	NPFO	30
1	Z(999),B(90),NPCA(75),CODE(999)	NPFD	4C
	DIMENSION ID(2)	NPFO	50
	10(1)=2	NPED	60
		NPEO	70
		NPEO	80
	CONDICK CONDITIONS	NDEG	00
	BUUNDARY CUNDITIONS	NEFU	40
		NPFU	100
	1. PRESSURE 3.C.	NPEN	110
		NPFD	120
	DU 300 L=1,NUMPC	NPF()	13C
	I=IJBC(L,1)	NPFO	140
	J=IJBC(L,2)	NPER	150
	NTPE1	NPFO	160
	IF ((I.GE.NL) AND, (I.LE.NM)) NTP=0	NPFO	17C
	IF ((J.GE.NL) AND, (J.LE.NM)) NTP=0	NPEO	180
	TE (NTP	NPEO	190
		NPEO	200
		NPED	210
		NEED	270
	SINAE1.U	NPFU	226
	CUSATO,0	NPPO	230
	$IF(ABS(DR) \downarrow LT, 1 \downarrow E = 1 \cap) GO TU 252$	NPED	240
	AG#ATAN2(DZ,DR)	NPFO	25C
	SINA=SIN(AG)	NPFO	26C
	COSA=COS(AG)	NPFO	270
252	SZISINAXSINA	NPFO	280
	C2=COSA+COSA	NPFO	290
	SC=SINA+COSA	NPFQ	300
	KD=0	NPEO	310
	DO 253 NEEL NPLAN	NPEO	320
	TE (T EO NPEA(NEN) KDM1	NPEO	110
	$\frac{1}{1} = \frac{1}{1} = \frac{1}$	NDEO	330
	IP (U ALUA NEUAINUJJ RUPE.	NEFU	346
		NPFU	350
	KUP2=KU+2	NPru	300
	KDP4=KD+4	NPPO	370
	PSBC(KD)=PSCA(NC,1)	NPFO	38C
	PSBC(KOP2)=PSCA(NC,2)	NPFO	390
	PSBC(KDP4)=PSCA(NC,3)	NPFO	400
253	KD=n	NPFO	41C
	DO 255 M=1,2	NPFO	420
	SIGNN=S2+PSBC(M)+C2+PSBC(M+2)=2.+SC+PSBC(M+4)	NPFO	43C
	STGT==SC+PSBC(M)+SC+PSBC(M+2)+(C2=S2)+PSBC(M+4)	NPFO	44C
	PSBC (M)=STGNN	NPEO	450
	MP2=M+2	NPEO	460
355	DORCIMPONESTCT	NPEO	470
6.33	DD 200 Net 2	NDEO	100
		NDEO	400
	N#1//"J	NEEU	470
	1 = 1 J D U U U U U U U U U U U U U U U U U U	NPPD	200
	JEIJHU(L,N)	NPEN	510
	IF((I.LT.NL) .DR. (I.GT.NM)) GO TO 290	NPFU	52C
	I2=2*I-KSHIFT	NPFD	53C
	I1=I2-1	NPFO	54C
	PI=PSBC(M)	NPFO	550
	PJ=PSBC(N)	NPFO	56C
			-

ľ		SI≠PSRC(M+2) SJ≠PSRC(N+2)	NPFO 570
		PM=(2,*PJ+PJ)/6.	NPFN SOC
		8M=(2,*SI+SJ)/6.	NPEO 600
F.		R1==DZ+PM+DR+SM	NPED 610
		R2= DR+PM+DZ+SM	NPED 620
		R1=R1+PRATIC(NNN)	NPEO 630
3		R2=R2+PRATIO(NNN)	NPEO 64C
Ł		SINA=0.0	NPED 650
		COSAE1.0	NPED 660
1		IF (CUDE(I) .GE. 0.) GO TO 280	NPFO 67C
		AG=CODE(I)/57.29577	NPED 68C
r		SINA=SIN(AG)	NPFO 69C
		COSA=CUS(AG)	NPFD 70C
1	560	R(I1)=R(I1)+R1+COSA+R2+SINA	NPFO 71C
Į.		P(I2)=B(I2)=R1+SINA+R2+COSA	NPFO 720
	290	CONTINUE	NPED 73C
•	500	CONTINUE	NPFO 74C
	510	CONTINUE	NPFO 75C
		RETURN	NPFD 76C
		END	NPEO 770

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