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Nicholas George

California Institute of Technology

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Dr. Nicholas George

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This technical report has been reviewed and is approved.

Ne INGO NA RADC Project Engineer

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## 1. Program Summary

The two main objectives are (1) to develop a theory of photogrammetric measurement for continuously varying contrast distributions and (2) to test our concepts on film of Project Secede Tests supplied via Gerald Meltz of the MITRE Corporation.

For the continuous tone objects, we planned to compare direct parallax measurements made visually on unmodified imagery with those made on imagery which had been artificially contoured using an isodensity recording. The first experiments were done manually, the results being inconclusive largely due to the poor availability of proper stereo-pairs. While at the outset extension of these tests to more precise stereoplotting equipment had been planned, this did not seem advisable after the preliminary parallax measurements had been made, and further effort on the project was terminated. The detailed technical findings are included in the following text.

The figures appearing in this report do not follow in numerical sequence.

## 2. Technical Discussion

#### 2.1 Stereoscopy

Stereoscopy is applicable to the problem of precisely determining the spatial structure of a photographic record. Using the standard photogrammetric methods described in Section 2.2, numerical data is obtained for a selected stereo pair of photographs of a barium release cloud. The resolution limits of these methods are discussed based on the inherent limitations of the photographic system. Problems remaining due to the nature of the photographic image - the cloud itself - are mentioned and a possible path toward their solution is outlined.

The procedure leading up to the actual application of the parallax measurements is as follows. A sequence of seven frames was selected from the 35mm color Spruce footage. A sequence was chosen in which the shape of the cloud was relatively well defined and the striations pronounced. The frames in this sequence were then prepared for use in a stereo viewer. By a stereo visual inspection of various combinations of pairs from the sequence, a single pair was chosen for the work which followed. The frames which made up this stereo pair had been separated by three frames in the original footage, thereby implying a time lapse of 30 seconds. The frame which was chronologically first in the sequence became the right member of the pair and the later frame became the left member. This choice is not arbitrary as becomes apparent in Section 2.2.

The continuously contrast varying transparencies were converted into quantized feature data using a Joyce-Loebl/Technical Operations

Isodensitometer. The resulting left and right isodensity recordings are reproduced in Figures 1a and 1b respectively. The isodensity contours were enlarged by a factor of 20-to-1 over the 35mm transparencies which allowed the recording of the entire cloud on a single sheet; however, recording ratios up to 1000-to-1 are possible. The scanning spot during the recording was a square  $80\mu$  by  $80\mu$ ; considerably higher resolution is possible as is mentioned in Section 2.3.

Besides the quantative measurements of the isodensity recordings, several tracings were made of the recordings and prepared for stereo viewing. This was done in an effort to obtain qualitative visual information from the isodensity recordings. These tracings are shown in figure 2. The first such pair (figure 2a and b) resulted in a confused image when viewed in stereo. The later traced pairs (figures 2c and d and 2e and f) produced a slight three dimensional effect when viewed in stereo but did not yield any real "depth" information about the image.

## 2.2 Photogrammetry of Isodensity Recordings of Barium Ion Clouds

In considering the subject of stereoscopy we will treat both cases in which a stereo pair is produced (a) from multiple camera site photographs and (b) from images recorded by a single camera at different times.

For the case of multiple camera sites we refer to figure 3. The point P is imaged at points  $y_a$  and  $y_b$  on films A and B respectively. By using geometrical optics we obtain the following relationships which form the basic equations of photogrammetry:



(a)



(b)







(d)



(f)

(e)

Figure 2

$$\tan \theta_{a} = \frac{y_{a}}{S_{f}} = \frac{y_{a}}{S'} = \frac{d_{\infty} + y_{b}}{S'}$$
(1)

$$\tan \theta_{b} = \frac{y_{b}}{s_{f}} = \frac{y_{b}}{s'}$$
(2)

An expression for the distance from the lens plane to the point P is

$$\mathbf{S'} = \frac{\mathbf{S_f} \, \mathbf{d_{\infty}}}{\mathbf{p}} \approx \frac{\mathbf{f} \, \mathbf{d_{\infty}}}{\mathbf{p}} \tag{3}$$

where p is the parallax of the point P and is defined by

$$\mathbf{p} = \mathbf{y}_{\mathbf{a}} - \mathbf{y}_{\mathbf{b}}$$

For the case of two point images at distances  $S_1$  and  $S_2$  from the lens plane, it can easily be shown from equations (1) and (2) that

$$s_2' - s_1' = \frac{s_1'(v_1 - v_2)}{v_2}$$
 (4)

where  $p_1$  and  $p_2$  are the parallax of points  $P_1$  and  $P_2$  (not shown in figure 3) respectively.

The same principles apply in the case of a pair of photographs from a single camera when the camera is moved a distance  $d_{\infty}$  in the plane of the lens during the time inverval between the two exposures. Relatively, an equivalent pair of photographs results if the object moves a distance  $-d_{\infty}$  with respect to a stationary camera during the same time interval. We wish to consider an object moving with velocity <u>v</u> with respect to a







stationary camera and for simplicity we assume for the present that

$$\underline{\mathbf{v}} \cdot \underline{\mathbf{n}} = \mathbf{0} \tag{5}$$

where n is the unit normal to the lens.

In figure 4, points  $P_1$  and  $P_2$  are moving to the right and A and B are the positions of the camera (relative to  $P_1$  and  $P_2$ ) at times  $t_2$  and  $t_1$  respectively (where  $t_2 > t_1$ ). The analysis is now the same as in the two camera case of figure 3. We see that equations (1) through (4) still apply but now  $d_{\infty} = v(t_2 - t_1)$ .

Figure 5 illustrates the fact that in the stereo viewing of transparencies produced by the systems of figure 3 or 4, a definite rightto-left relationship exists between the members of the stereo pair. The image produced at point A becomes the left member of the stereo pair while that produced at point B becomes the right member. If the transparencies are interchanged by translation only, the distances  $S_1'$ and  $S_2'$  will appear inverted. The same principle applies in making parallax measurements and must be taken into account when we calculate normal distances from photographs or isodensity recordings made from a stereo pair.

We can determine the corresponding azimuthal coordinate of the object point by first measuring the position of the object point on either view of the stereo pair. Then using equation (1) or (2), whichever is appropriate, we can calculate the corresponding object coordinate using the value of S' calculated from equations (3) or (4).



## Figure 5

Twenty points were used in the photogrammetry; of these, six typical points are shown in Fig. 1a and 1b. The star points are labeled with an S. The points selected for this analysis lie in the striated portion of the cloud and are numbered as follows: points 1 through 5 and 11 through 15 lie along the dark or higher optical density bands which mark the striations; points 6 through 12 and 16 through 20 lie on the lighter or lower optical density bands. The points A,B and C represent stars in the background sky; since these can be considered to lie at an infinite distance from the camera, they have a parallax p = 0 and can be used as reference points in each view.





Figure 1b: isodensity recording of right view

Referring now to figure 6a we see a field of numbered vectors which represent the change in position of each of the points. The tip of each vector is the location of the corresponding point in the left view (figure 1a) and the tail locates the position of the point in the right view (fig. 1b). Unfortunately we see that the vectors are not all parallel as was implicitly assumed in the discussion of section 2.2. We will consider the problem of errors introduced by local variations in velocity in Section. 2.5.2. For now we will consider only the projection of each vector in some average direction which we will call the y-axis. The direction of this axis is taken to be antiparallel to the direction of the cloud velocity which we approximate by the following averaging method. The vector field of figure 6a indicates the direction of the velocity of each point but gives no information regarding the magnitude of the velocity. However our stereoscopic analysis assumes that these magnitudes are equal. As a first-order approximation we sum twenty vectors of equal magnitude (as shown in figure 6b) whose directions are those of the corresponding vectors in figure 6a; we take the direction of the resultant to be an approximation to the direction of cloud travel.

Since the parallax of each point is

 $p = y_a - y_b = y_{left} - y_{right}$ 

We can now determine the value of  $p_n$  for the nth point by measuring the length of the projection of the nth vector onto the y-axis. We see in table I that the parallax of point #8 is near the average for the set.









We can rewrite equation (4) in the following way:

 $S_{n}' - S_{8}' = \frac{S_{8}'(p_{8} - p_{n})}{p_{n}}$  $S_{n}' = \frac{S_{8}'(p_{8} - p_{n})}{p_{n}} + S_{8}'$ (6)

Assuming that point #8 lies at a distance of 100 km from the camera we set  $S_8' = 100$  km and compute the distances of the remaining points using eqn. (6). The results are shown in table I.

### 2.3 Error Analysis

or

Errors in determining the exact location of a point from a stereo pair of images of the plasma cloud are due to the following: (1) Resolution limits of the systems used to record and process the imagery. (2) Variation of the shape of the cloud. (3) Uncertainty in location of corresponding points in the two stereo views. Of these, (1) is independent of the nature of the imagery itself; and (2) and (3) are directly related to the nature of the object, namely the plasma cloud.

# 2.4 Resolution and Diffraction<sup>3</sup>

Because lens diffraction and film resolution eause each image point to be spread out into a spot on the photographic record there is a limit to the precision with which the position of points can be measured on the photographic image. It follows that there will be a corresponding error in the determination of the distance S' from a stereo pair.

n	p <sub>n</sub> (mm)	$S_n'(km)$	
1	-2.4	225	
2	-9.4	57	
3	-8.7	62	Group 1
4	-11.9	45	(dark band)
5	-22.5	24	
6	-2.3	235	
7	-4.7	115	Crain 2
8	-5.4	100	(light band)
9	-9.3	58	
10	-9. <sup>1</sup> +	57	
11	-2.4	225	
12	-6.7	81	
13	-9.0	60	Group 3 (dark band)
14	-7.0	77	
15	-11.6	46	
16	-3.4	159	
17	-1.3	416	Group 4
18	-3.4	159	(light band)
19	-14.0	135	
20	-2.5	216	

 $p_{average} = -5.9$ 

Table I

We can obtain expressions for diffraction errors from eqs. (1), (2) and (3) by differentiation.

For image points inclined at an angle  $\theta$  (shown in figure 3) to the lens optical axis, the spread  $\delta y$  recorded on the film plane due to diffraction is

$$\delta \mathbf{y} = \frac{\mathbf{f} \delta \boldsymbol{\theta}}{\cos^2 \boldsymbol{\theta}} \tag{7}$$

where f is the lens focal length. Thus the maximum possible uncertainty in parallax r for a stereo pair (assuming  $\delta \theta_a = \delta \theta_b$ ) is

$$\delta \mathbf{p} = \delta \mathbf{y}_{\mathbf{a}} + \delta \mathbf{y}_{\mathbf{b}} = \mathbf{f} \delta \theta \left( \frac{\mathbf{l}}{\cos^2 \theta_{\mathbf{a}}} + \frac{\mathbf{l}}{\cos^2 \theta_{\mathbf{b}}} \right)$$
(8)

This uncertainty in parallax then gives a maximum uncertainty  $|\delta S'|$  in the photogrammetrically calculated altitude

$$|\delta S'| = \frac{fd_{\infty} \delta p}{p^2} = \frac{(S')^2 \delta \theta}{d_{\infty}} \left( \frac{1}{\cos^2 \theta_a} + \frac{1}{\cos^2 \theta_b} \right)$$
(9)

The error introduced by diffraction in the azimuthal coordinate becomes, to first order at least,

$$|\delta \mathbf{y}_{\mathbf{a}}'| = |\delta \mathbf{y}_{\mathbf{b}}'| = \frac{\mathbf{S}' \,\delta \theta}{\cos^2 \theta}$$
 (10)

The angular uncertainty  $\delta \theta$  is given by

$$\delta \theta = \frac{1}{wf} + \frac{2\pi}{\pi D}$$
(11)

where w is the film resolution in cycles/mm, f is the lens focal length,  $\lambda$  is the wavelength of the light, and D is the diameter of the camera aperture. If we assume a photographic system in which f = 50 mm, w = 50 cycles/mm, D = f/1.4,  $\delta\theta = 0.4 \times 10^{-3}$  radian.

Table II shows the optimum limits of resolution for the system indicated above, a typical cloud altitude of S' = 100 km, cloud velocity of 70 m/sec, and an interval between exposures of 30 sec. The parameters  $\ell_0$  and  $\ell_1$ , referred to in table II are characteristic lengths which indicate the degree of resolution attainable in altitude and azimuth. Figure 7 shows schematically how these parameters apply to the detail structure of the ion cloud. Note that the values of  $\ell_0$  and  $\ell_1$  calculated in table II refer to a 30 sec time lapse. A longer time interval yields a proportionally higher degree of resolution.







5

Item	resolution, 56 and diffraction)	áe resolution, $\ell_0$	hal resolution, t <sub>l</sub>	variation in cloud iform expansion	lse parallax from fferential shape change	
Algebraic form of error term	$\frac{1}{wT} + \frac{2\lambda}{\pi D}$	$\frac{(5')^2 5\theta}{d_{co}} \left( \frac{1}{\cos^2 \theta} + \frac{1}{\cos^2 \theta_b} \right)$	s' 59 cos <sup>20</sup> min	correctable ± 10%	S <sup>1</sup> 5v	
Resolution for syst described in sectio	0.4 x 10 <sup>-3</sup> radiar	l4 km	H 04			

Factors Influencing Quantitative Stereo-Analysis of Barium Ion Cloud

Table II

#### 2.5 Shape Variation of Cloud

Two difficulties arise in parallax measurements of a stereo pair due to the change in the shape of the cloud. These can be attributed to (1) uniform expansion of the cloud and (2) differential shape change.

## 2.5.1 Uniform Expansion

If the ion cloud expands uniformly there is an inward drift velocity toward the camera and therefore eqn (5) is no longer true. This being the case, one would expect that severe errors might be introduced.

A laboratory experiment was conducted to assess this effect. Using the three-dimensional styroform model with "pencil-rod" features (shown in figure 8) a stereo pair was made corresponding to a base line separation of 15 miles. A series of progressively larger and smaller prints were made of only one photograph of the pair; these were viewed with the fixed-scale left band member. No undue difficulty was observed with scale changes to  $\pm 10\%$ . In our data reduction we can correct for this effect by using a different lens-to-transparency distance for the left and right members of the pair.

## 2.5.2 Differential Shape Change?

This effect appears to contribute a relatively serious error to the photogrammetry from successive time-elapse photographs. To estimate the effect we suppose some element of the ion cloud has a velocity different from the drift velocity by an amount dv. By differentiation



Figure 8

of eqn (3) we find:

$$dS' = \frac{fd_{\infty} dp}{p^2} + \frac{f}{p} (vdt + tdv)$$
(12)

where the first term on the right is the elevation uncertainty of equation (9). The first term in parentheses is equal to zero in the case of a stereo vair since t is constant for all image points. The false parallax due to shape changes therefore reduces to

$$dS' = \frac{ftdv}{p}$$
(13)

$$dS' = \frac{S'dv}{v}$$
(14)

For v = 70 m/sec and a fluctuation locally of dv = 5 m/sec we find an error  $dS' \approx 10$  km. In the case of photographs taken from an aircraft in steady flight, the v in ean. (14) is large and the resultant error varying as the ratio  $\frac{dv}{v}$  is decreased.

## 2.6 Uncertainty in Location of Corresponding Points in the Two Views

For the purpose of calculating the altitude of a point from a stereo vair of images it is of major importance that we be able to identify and locate accurately the corresponding points on both views. Upon viewing the photographs of the plasma cloud it is easy to identify outstanding features such as the striations. One can even estimate visually the center of the striations at a given point but the intensity

of the vhotograph is too smoothly varying to allow a very accurate visual estimation. It is certainly not accurate enough to resolve the change of position with respect to the two views for a point on the cloud. The isodensity traces on the other hand afford a means of associating limiting contours with the features of the object and thus a clue in identifying individual points. For the calculations of section 2.2 the points were located by making the tentative assumption that corresponding points in the photographs map into points of equal density on both isodensity recordings. A point was then located in both views by selecting a point on a contour in one view and then finding its apparent image on the contour representing the same density in the other view. Of course there still remains some uncertainty in the location of a given point but we now have a means of making a much better approximation than was available with the photographic records. The errors due to uncertainty in the location of corresponding points will have the same algebraic form as ean (12):

$$|\delta S'| = \frac{fd_{\infty} \delta p}{p^2}$$

## 2.7 Discussion of Results

In view of the discussions of photogrammetry and error analysis some comments can now be made regarding the calculated data found in table I. Some of the S<sub>n</sub> values in the table can be seen to contain large and obvious errors. Referring to figure 6a we see that vector 17 is very small; since the scale at which the measurements were made is the same as that of figure 6a, it is reasonable to assume that point 17 is an error due to poor precision. This sort of error can be minimized by making the measurements on an enlargement of the original stereo isodensity recordings.

It is possible that points 1, 6, and 11 also suffered from lack of precision since the projections of their vectors along the y-axis (in figure 6a) are small. However, these three vectors also indicate a differential shape change at those points. Each of these vectors has a component perpendicular to the y-axis which is comparable to the ydirected component. This introduces an uncertainty in the magnitude of the corresponding velocity vector which is comparable with the magnitude of the velocity itself, i.e., by is of the same order as v. From eqn. (14) we see that this suggests a possible error of the order of 100% for these points.

Disregarding points 1, 6, 11 and 17 in table I and considering the remaining points it is obvious that the size of the cloud implied by this data is several times larger than the actual dimensions. The values in table I should be clustered more tightly around the 100 km value which implies that the vectors in figure 6a should be more nearly equal in length. This would seem to imply that we have made an error in the attempt to locate corresponding points on the left and right isodensity recordings. This in turn would imply that the assumption mentioned in section 2.6 is not valid. Clearly, if varallax measurements are to yield reliable numerical results, another method of accurately

locating a point in both views of the stereo pair must be tried.

It is now apparent that the image points represented by an isodensity contour in one view are not necessarily represented by a contour of equal density in the other view. This could be due, in part at least, to an overall decrease in optical density resulting from the uniform expansion of the cloud. (Note that this would not apply to stereo pairs obtained from multiple cite cameras.) In this case we might take as a new trial assumption the following: that a set of image points corresponding to an isodensity contour in one view is represented by some isodensity contour on the other. If this is so, then we can attempt to match corresponding pairs of contours on the two density recordings. Once this is done, corresponding points can be located on the appropriate pairs of contours and the photogrammetric process proceeds as usual. The matching of contours could be accomplished by cross-correlating the shapes of various pairs of contours and matching the pair for which the correlation is a maximum. Unfortunately it would be difficult at best to do this visually. However, such a cross-correlation process could be done with a high degree of accuracy using optical processing.

## 2.8 Conclusion

We have seen in sections 2.3, 2.4, 2.5, 2.6 that a reasonable degree of resolution can be attained in locating both altitude and azimuthal coordinates of an object using standard photogrammetry techniques. A major factor in achieving such resolution, however, for the case of the plasma cloud is the accuracy with which an image point can be identified and located in both views of the stereo pair. Visual examination of the photographic records and even of the isodensity recordings failed to give the required accuracy in point location. It appears, however, that the production of a stereo pair of isodensity recordings from the photographic pair is a good initial step in solving the problem. A higher lev?l of sophistication in further processing of the isodensity recordings has been suggested involving cross-correlation of the individual contours in the stereo pair. Unless a solution to the problem of accurate point location is found, the photogrammetric methods outlined herein will not yield satisfactory numerical values for object coordinates.

## REFERENCES

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- 2. N. George et al, Photogrammetry of Barium Clouds, California Institute of Technology, March 1971, pp. 5-6.
- 3. Ibid., pp. 7-9.
- 4. Ibid., p. 12.
- 5. Ibid., pp. 12-13.

3. Research Personnel, References, Acknowledgment

3.1 Personnel Who Participated in this Research Program

Name	Classification
Dr. Nicholas George	Principal Investigator
Dr. R. B. MacAnally	Senior Research Fellow
Christian Juvan	Junior Electrical Engineer
R. E. Gray	Doctoral Scholar
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subject contract)

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Dr. R. P. Porter	Woods Hole Oceanographic Laboratories Woods Hole, Massachusetts		

## 3.3 Acknowledgment and References

Helpful participation by G. Meltz and R. P. Porter is acknowledged. Also some references of particular interest in connection with this work are the following:

- "Holography and Stereoscopy: The Holographic Stereogram," Nicholas Seorge and T.J. McCrickerd, Photographic Sci. and Engin. <u>1</u>, 342 (1969).
- "Photogrammetry of Barium Clouds," Nicholas George, R. P. Porter,
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   MITRE Corp, March 1971.
- 3. "Three-Dimensional Structure of Continuous-Tone Objects by Stereo-Photogrammetric Techniques," R. P. Porter, The MITRE Corp., Unpublished memo.



A-1 Original set of seven frames from the 35 mm spruce footage. Frame 1 and frame 4 were used for the photogrammetric calculations.



FRAME

4



FRAME 3



9 FRAME

FRAME S

Figure A-1 continued



FRAME 7

Figure A-1 continued











A-6 Light contour tracing of left view.







FRAME 2

FRAME 1

A-10 Two More Frame's From the Spruce Footage



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A-12 Right isodensity contour made from right A-10 frame.