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A REAL TIME VISIBLE SURFACE ALGORITHM

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June 1970

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by

Gary Scott Watkins

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#### ABSTRACT

With the increasing use of computer graphics, a need is growing for a processor capable of displaying solid objects. Environmental simulation and architectural modeling are only two areas that would benefit from such a display processor.

This dissertation describes an algorithm designed for such a processor, and a program for simulating the hardware processor. The hardware processor would be capable of generating pictures of fairly complicated objects at thirty frames per second. Statistics describing its simulated performance have been extracted and are reported within the dissertation.

#### CHAPTER I

### INTRODUCTION

With the introduction of line-drawing displays, it was soon realized that displaying too much information detracted from the meaning and actually confused the picture. For instance, a single cube can create an optical illusion as shown in Figure 1. However, the optical illusion is removed if lines hidden by surfaces in front of them are not displayed (see Figure 2). A different approach could be taken. Instead of determining the hidden lines, an algorithm could find, color, and shade visible surfaces, thus presenting a more true to life picture. For the past several years, different algorithms have been developed for solving the hidden line or visible surface problem. The various algorithms can be classified into several groups.

## A. Path of Edges Algorithms

Some solutions to the problem have been found by various methods of tracing along the edges of objects and noting which of the edges are wholly or partially visible. The resulting picture is then the display of the visible segments of edges. Algorithms based on this method have been developed by Roberts [1], Loutrel [2], and Appel [3]. This type of approach does not take into account the resolution of the display but solves the hidden line problem to





Cube Presenting Optical Illusion



Figure 2

Cube with Hidden Edges not Drawn

the precision inherent in the object description.

B. Sample Space Algorithms

In 1967 a paper was presented by Wylie, Romney, Evans, and Erdahl [4]. One of the concepts discussed was initiated by Evans and introduced the concept of a sample space. The concept states that given an output device with resolution of  $R_{\mathbf{x}}$  by  $R_{\mathbf{y}}$ , one need only solve the hidden line problem at the discrete resolution points. The sample space can be thought of as taking the original object description in X, Y, Z, and mapping the object on to a two dimensional grid of resolution  $R_x$  by  $R_y$ . Of course, the Z information needs to be preserved in some form. When this is done, the object will exist only at discrete points in X and Y. The reasoning behind this was when a person views a picture he is physically limited by the resolution of the eye and the resolution of the display device. Hence, the hidden line problem need only be solved to the coarser resolution of the two.

In the algorithm, non-intersecting triangles were used as the object description. However, convex polygons could have been used with only small changes in the program. The algorithm used a scan line approach. That is, one Y raster line would be completely solved for visible triangles before the program proceeded to the next scan line. A method of sorting vertices of the triangles was developed by Wylie

and Romney so only triangles concerned with the current scan line were considered. On each scan line, triangle depths were compared only where edges of the triangles crossed the current scan line. Therefore, it was not necessary to do depth computations at all raster points. Later Romney [5] improved the sorting technique and added a "speedy" check to the program to take advantage of scan line-to-scan line coherence. This improved the speed by eliminating depth sorting as long as triangles entering on the scan line were ordered the same as the previous scan line.

Warnock [6] took a new approach but still kept the grid of resolution points. The object description was generalized by allowing polygons (convex or non-convex) which could intersect one another. The first of the scan line approach, Warnock took an area of the picture and tried to "understand" it. If it was simple enough to "understand" he would display it, otherwise he subdivided the area into smaller areas. Eventually, a sub-area could be "understood" and displayed, or a sub-area would reach resolution whereupon it would be displayed without further analysis. This concept of subdividing large problems into smaller (and easier) problems is a "non-deterministic" algorithm.

After Warnock's algorithm was developed, Bouknight [7] took the scan line approach and generalized it to include general polygons which could intersect. Figure 3 shows a classification of the various algorithms.



The new algorithm to be described is of the mapped sample space class, and it allows general polygons which can intersect. Key ideas used in this algorithm are: (1) Scan line-to-scan line coherence of pictures, and (2) an arithmetic unit for Z-depth sorting. Frame-to-frame coherence vas not found valuable (in terms of increasing the speed of the program) for inclusion in this final algorithm.

The program implementing this algorithm is a simulation of hardware to generate visible segments of polygons on each scan line at real time speeds. Thus, the program is a Visible Segment Generator (VSG). The output of the VSG is given to a shader for displaying. The method of shading is very similar to that described by Romney [5] and Warnock [6].

#### CHAPTER II

### PRE-FRAME PROCESSING

Before being accepted by the VSG, the object must be processed so that all translations, rotations, and perspective transformations have been applied. All polygons must be clipped at the boundaries of the viewing sample space. Since the scanning process proceeds from Y=1 to Y=512 (or to the Y-resolution value), the edges must be ordered in a list according to the minimum Y value (Y-min) of each edge. Horizontal edges need not be put in the list since the VSG will reject them. On any scan line the VSG can then immediately find which (if any) edges enter on that particular scan line. For each polygon, three fields are zeroed initially and reserved as sorting fields for the VSG. The formats for the edge block and polygon block are shown in Figure 4. The shading and color information will never be used by the VSG for computations. However, the VSG will pass the information to the shader for displaying if the object is visible.

A user that describes objects as closed polyhedra can double the speed of the processor if edge and polygon blocks are only created for polygons that face the viewer. This process was used on the test objects described in Chapter VII.

### EDGE BLOCK

| POINTER TO NEXT<br>EDGE BLOCK          |
|--|
| POINTER TO POLYGON<br>BLOCK            |
| Y - MAX                                |
| Y - MIN                                |
| X - BEGIN<br>(ASSOCIATED WITH Y - MIN) |
| Δx                                     |
| Z - BEGIN<br>(ASSOCIATED WITH Y - MIN) |
| Δz                                     |

## POLYGON BLOCK

| A REAL PROPERTY AND A REAL |
|--|
| POINTER TO INITIAL<br>SEGMENT ON POLYGON   |
| POINTER TO NEXT<br>CHANGING POLYGON  |
| POLYGON ACTIVE BIT   |
| SHADING AND COLORING<br>INFORMATION  |

# Figure 4

Description of Edge and Polygon Blocks

#### CHAPTER III

## VISIBLE SEGMENT GENERATOR

The VSG can be broken into three separate processors: (1) Segment Generator, (2) Segment Eliminator, and (3) Depth Sorter.

### A. Segment Generator (SG)

The format for a segment block is shown in Figure 5. A segment is defined as the continuous surface of a polygon which exists between two adjacent edges on a scan line. Thus in Figure 6, on scan line 'a' there are two segments, while on scan line 'b' these two segments of the polygon have merged into one segment. A segment block contains a description of the two bounding edges. The two Y-end values specify the Y scan lines when the edges exit from the picture. The X and Z values are stored along with the  $\Delta Z$  and  $\Delta X$  increments for each edge. Thus, when the program proceeds to the next scan line, the X and Z values are updated by adding the increments as in Equation 1.

 $Z+Z+\Delta Z$ ;  $X+X+\Delta X$  (1) The segment blocks are threaded together by four separate list structures:

1. The X-sort list contains all segments on the current scan line sorted with respect to the left edge of each segment. This list has both forward and backward



Figure 5

Segment Block



Segments

pointers.

2. Each polygon segments list contains an ordered set of all segments belonging to a particular polygon on a scan line. They are linked together, with the initial pointer (contained in the polygon block) pointing to the left most segment of the polygon.

3. The active segment list contains only segments of the X-sort list which exist in a specified range of X values. Section F of this chapter will give more detail of it.

4. The sample list is another sorted list that will be explained later.

The SG is checked on each scan line to see if any new edges enter the current scan line from the edge list. If there are no entering edges, control is passed to the segment eliminator. If edges do enter on a scan line, data from the edges is used to create a segment.

The polygon block associated with the incoming edge is checked to see if the active bit is set. Active designates whether or not the polygon is already in the list of changing polygons (polygons that have edges entering or exiting on the current scan line). If the polygon was not previously active, it is tagged as active and put in the list containing all changing polygons on this scan line.

Since an edge has only enough data for one half of a segment, an edge can be inserted into either the right or

left side of an empty segment. Because the program does not know whether an edge bounds the right or left side of a polygon, the algorithm may insert an edge into the wrong half of a segment. However, if this happens, the Segment Eliminator will do the necessary rearranging. The X value of the incoming edge is compared against the X values of segments in the polygon segments list until the appropriate location in the list is found for inserting the edge data.

After finding the correct location in the list, and if there is not an empty half of a segment block, the SG must get a block from free storage and insert it in the list at the correct location. Pointers to the segment block must also be inserted in the X-sort list in the correct location whenever data is stored in the left half of the block.

The preceding process is repeated for all edges that enter on the current scan line. Finally when no more edges enter, control is passed to the Segment Eliminator.

### B. Segment Eliminator (SE)

The SE runs through the list of all changing polygons, and for each of the polygons it disconnects the polygon from the changing polygon list, and resets the active bit. It then proceeds through the list of segments attached to that polygon to determine if any data needs to be shifted from one segment block to another, or if any segment blocks can be returned to free storage. For example, in Figure 6 on scan line 'a' the polygon has two segments. Because the two middle edges exit between scan lines 'a' and 'b,' this polygon will have been inserted into the list of changing polygons. The SE must then take the right edge data from the second segment block and insert that data into the right half of the first segment block. After this, the second segment block will be returned to free storage. Figure 7 gives a step-by-step illustration of what would happen if displaying the polygon in Figure 6. When all active polygons have been checked by the SE, control is passed to the Depth Sorter.

## C. Depth Sorter (DS)

At this point the X-sort list contains all segment blocks on this scan line ordered with respect to the left edge of each scan line. While the SG and SE are concerned only with polygons that change on the current scan line, the DS is concerned with all polygons that exist on the scan line. Therefore, the list handling and memory referencing in this processor are extremely critical to the overall speed of the VSG.

### D. Sampling

A critical factor in the speed of the algorithm is the number of points on the scan line where depths of polygons are sampled. The depth sorter is capable of determining at most a single visible segment for a restricted span of a scan line. Because of this, sampling must at least be done



Scan Line 'a'





POLYGON



Scan Line 'b' after Second Segment Block Has Been Returned to Free Storage

> Figure 7 Packing of Polygon Segment List

at the points of discontinuity (the visible edges). Scan line-to-scan line coherence usually allows the DS to find the visible segment by sampling only at the visible edges contained in the sample list. For the object in Figure 8, one hotices the sampling points actually following the visible edges of the picture. Thus the speed of the algorithm will be more dependent on the visible complexity of the object than on the total object complexity.

The Depth Sorter can be subdivided into three separate processors: (1) The Sample Space Generator, (2) The Depth Comparator, and (3) The Decision Processor.

### E. Sample Space Generator (SSG)

The SSG operates from the sample list. Essentially the list contains the sorted edges (each half of a segment block is an elge) which were visible on the previous scan line. The building of the Sample List was done on the previous scan line by the Decision Processor and will be discussed 'inder that heading.

The left and right sides of the view screen are always implied sample edges. The scan process on a single scan line proceeds from left to right in X. Therefore, the left edge of the view screen becomes the initial left sample point. The X value of the first edge in the sample list then becomes the right sample point. This sample edge is then removed from the sample list. The portion on the scan line which exists between the left and right sample points



Figure 8 Sampling Points is called a span.

Suppose in Figure 9 one found on scan line 'w' that edges B, C, and D were visible, and therefore they were put in the sample list with B at the first of the list. When the program proceeds to scan line 'w+1,' the current X value of edge A is initially set as the left sample point. Edge B then becomes the right sample point. Once a left and right sample point is found, control is passed to the Depth Sorter and Decision Processor. Finally, when the Decision Processor finishes its task, control is passed back to SSG. Now the right sample point 'b' becomes the left sample point. Edge C is read from the sample list, point 'c' becomes the right sample point, and the cycle begins again. The cycling process finally stops when the end of the scan line is reached whereupon control is passed back to the Segment Generator for the next scan line. A flow chart in Figure 10 shows the overall control of the system.

## F. Depth Comparator (DC)

The DC takes all the segments from the X-sort list that exist between the left and right sample points and operates on them in the following manner: (1) The X and Z values are incremented to the values associated with the next scan line and stored back in the segment block. (2) If either of the edges of the segment exit on this scan line, the associated polygon is tagged as active and put in the changing polygon list. (3) The X value of the left edge is compared with the



Figure 9 Sample Edges and Sample Points



Figure 10

VSG Flowchart

last segment stored in the X-sort list being prepared for the next scan line. If the new segment X value is larger, it is inserted at the end of the list. If it is not larger, the backpointers of the X-sort list are used until the correct location in the list is found. The surprising data is that line-to-line coherence of the ten test objects (Chapter VII) causes 97 to 99 percent of all segments to be inserted at the end of the list. This means that the X-sort list can always remain sorted in X with very little time spent for rearranging segments. (4) Along with the sorting just discussed, the DC must compare the incoming segment against the currently visible segment. If the incoming segment is in front, it will become the currently visible segment. Every time a new sample span is generated, the first incoming segment becomes the currently visible segment.

If the right edge of a segment extends to the right of the right sample point, the segment must be saved for future depth comparisons when the sample span is moved along the scan line. For this purpose the active segments list was created. Segments are put in the list from the X-sort list and remain only as long as the right edge of the segment is to the right of the left sample point. Therefore, in addition to segments read from the X-sort list, the DC also compares depths of segments read from the active list.

### G. Segment Clipping

When two segments are being compared, a clipping algorithm is applied to each of the two segments simultaneously. Figure 11 illustrates the procedure. The two lines represent the segment values on the current scan line. As the Z values of a segment decrease, the segment becomes closer to the observer. Two X clipping values must be obtained.  $X_{1clip}$  is defined as the right most left edge in the sample span, and  $X_{rclip}$  as the left most right edge in the sample span. If a left edge does not lie in the sample span, the left sample span value is taken as  $X_{1clip}$ . In Figure 11, the X value of 'e' becomes  $X_{1clip}$  and the X value of 'b' becomes  $X_{rclip}$ . A set of registers is then chosen for the left and right clip points of both lines and loaded as in Figure 12.

Since  $Z_{max}$  and  $Z_{min}$  are stored (not  $Z_{left}$  and  $Z_{right}$ ), an additional bit must be kept which is the sign of  $(Z_{left}-Z_{right})$ . This bit is used to distinguish the relationship of  $Z_{left}$  and  $Z_{right}$  to  $Z_{max}$  and  $Z_{min}$ . Figure 13 shows a more complete gating of the registers contained in dotted box #1 of Figure 12. S of Figure 13 is:

$$S = (XA - X_{lclip} + XB - X_{lclip})/2$$
(2)

or

$$S=(XA+XB)/2-X$$

But (XA+XB)/2 is the midpoint (XM) of the line ab.

$$S=XM-X$$
 lclip (4)



Figure ll Two Segments on a Scan Line











Figure 13 Gating of a Single Quadrant

If S is greater or equal to zero, the midpoint is on X lclip or to the right of X lclip. Then the registers containing X and Z of the previous point to the right of X lclip will be replaced with the midpoint of line ab which is closer to <sup>X</sup>lclip<sup>•</sup> A similar argument applies if S is less than zero. A more complete description of this clipping process used in a line drawing system is described by Sproull [8].

In Figure 14, succeeding clipping cycles are applied to the two segments of Figure 13. Let  $Z_{max1}$  be  $Z_{max}$  of quadrant 1 in Figure 12. Zminl' Zmax2' Zmin2' Zmax3' Zmin3'  $z_{max4}$  and  $z_{min4}$  are similarly defined. If  $(z_{max1} < z_{min3})$ , line ab is in front of line cd at X lclip. However, as in Figure 14 after one clip cycle, then  $(Z_{max3} < Z_{min1})$ . Therefore, line cd is in front of line ab at X lclip Exactly the same argument applies to X rclip, and after two clip cycles line cd is found to be in front of line ab. Since line cd covers line ab everywhere between the sample points 'e' and 'f', it then becomes the currently visible segment.

Many times when lines intersect, or in the case shown in Figure 15, a single currently visible segment cannot be found. In this case a box is made just large enough in X and Z to encompass the two or more lines in question. The amount of data to remember a box description is the same as the amount to remember a line. Also a bit is set declaring a visible box instead of a visible segment. If later a












segment is found to be in front of the box as in Figure 16, then it becomes the current visible segment and replaces the visible box. The processor continues until all segments that exist in the span are checked. When this is completed, control is passed to the Decision Processor.

### H. Decision Processor (DP)

The DP decides whether a visible segment can be put in a display file or if the sample span must be subdivided in some manner and the Depth Comparator started again. If the DP finds there is a visible segment from the DC, it outputs the corresponding segment to the display file. If the DC discovered a visible box, and any of the visible segments in the box have an edge existing within the sample span, the right sample point is set to the X value of that edge (subdivision), and control is passed back to the DP. For instance, the DP would cause the control to subdivide at X=a for segments in Figure 17.

If no edges exist between the left and right sample points, two conditions can exist: (1) For more than two segments existing in the visible box as in Figure 18, the sample span is divided in half. That is, the right sample point is moved half way toward the left sample point. After this subdivision process, control is passed back to the DC again. (2) If only two segments exist in the box, the condition is the intersection case of Figure 19. The



Figure 15 Boxing of Segments









Figure 18 Three Potentially Visible Segments



Intersecting Segments

same clipping hardware used for depth comparisons can also be used for calculating the intersection of these two lines.

# I. Intersecting Segments

The intersection calculation is done in two stages. First, the registers of Figure 12 are loaded exactly in the same manner as for the DC. However, instead of terminating when the  $Z_{max}$  and  $Z_{min}$  tests are satisfied, the adders run until all registers contain either 0 or -1. When the registers reach this state,  $Z_{max1}$  will hold the Z value of line ab at  $X_{1clip}$ ,  $Z_{max2}$  the Z value of line ab at  $X_{rclip}$ ,  $Z_{max3}$  the Z value of line cd at  $X_{1clip}$ , and  $Z_{max4}$  the Z value of line cd at  $X_{rclip}$ . Figure 19 has been reduced to the problem represented in Figure 20.

For the second stage, the problem can be solved by loading the registers in the manner shown in Figure 21. Because of the intersection,  $Z_1$  and  $Z_2$  will have opposite signs. Therefore, after each add cycle the Z sum is stored into the Z register which has the same sign as the sum. The X registers will also be stored in the same direction determined by the Z sum. After  $[log_2(X_{rclip}-X_{lclip})]$  add times,  $X_1$  and  $X_2$  will both contain the X value of the intersect of the two segments.

A block from free storage is obtained at this point and the X intersect value and the pointers to the two segments causing the intersection are stored as data in an implied edge list. When the program proceeds to the next scan line,



Figure 20

Intersecting Segments Clipped to X lclip and X rclip



Figure 21 Registers for Finding Intersection

the intersect will again be calculated. The difference between the intersect on this scan line and the intersect calculated on the previous scan line can be used as the increment of the implied edge. This edge can now be treated as any other visible edge and used for determining sample points. If, on a scan line, an implied edge is found to be no longer visible, the block is returned to free storage.

# J. Building the Sample List

The DP has one other task. That is, to tag the visible edges (determined in the DP), and put them in the sample list. Upon completion of the DP, control is either passed to the SSG if subdivision did not occur, or to the DC if subdivision did occur.

### CHAPTER IV

# FRAME-TO-FRAME COHERENCE

This algorithm can easily take advantage of frame-toframe coherence of pictures. For instance, in a movie if an edge is visible in one frame, it will usually be visible in the next frame. If an edge is found to be visible on the scan line it enters on, the edge block (see Figure 4) is tagged as visible. This means one additional bit must be stored in each edge block. Also two pointers to each edge block must be stored in the segment blocks. Then when the next frame is being processed and an edge was found to be previously visible, the initial X value of the edge is then used as a sample point. The frame-to-frame coherence algorithm was used on some of the earlier versions of the program. However, the scan line-to-scan line coherence was so efficient that the frame-to-frame coherence only decreased the number of memory references by about 0.1 percent. Because of this, it was not implemented in later programs.

### CHAPTER V

# RELATIONSHIP WITH OTHER ALGORITHMS

On the basis of generality of object descriptions, this new algorithm is as good as or better than the others mentioned in the introduction. Convex or non-convex polygons of any number of sides can be used. The algorithm allows polygons to penetrate one another without any pre-processing checks.

Since planar equations are never used for depth sorting, the algorithm can not tell if the points of the polygons lie on a plane. It always assumes a linear interpolation between the edges on a scan line. However, when shading a polygon a discontinuity in shading can be created. For example, if the vertex between scan lines 'a' and 'b' of Figure 6 were not on the plane described by the other three vertices, the linear depth calculations between edges would show a discontinuity in the shading between the two scan lines. Furthermore, the line of discontinuity would always remain horizontal even if the polygon were rotated. Also, since segments are only checked when edges enter or exit, edges of a single polygon should never cross each other. If they do cross, however, a local error will occur in the picture only where that polygon exists and if that polygon is visible. Consequently, points of a polygon

.36

should lie on a plane. (Points not on a plane can introduce edges that cross).

Like Warnock's algorithm, this new algorithm is also non-deterministic, but on a scan line level. For instance, a sample span on a scan line is assumed to have one covering polygon. If it does not, the sample span is made smaller until finally a span is found which is covered by a single polygon.

Romney used an ordering scheme for taking advantage of scan line-to-scan line coherence. He did not allow intersecting triangles. Therefore, as long as the intersection of the edges of triangles on the current scan line were in the same order as on the previous scan line, the same triangles that were visible previously would be visible on this scan line. However, as soon as the order changed, the remainder of the scan line had to be depth sorted. The coherence ordering made a great difference in the speed of his algorithm.

If intersections are allowed, as in the new algorithm, this ordering of edges no longer holds for determining visibility. Therefore, the sampling process described in Chapter III-D was developed. It has the further advantage that even when the order changes, the previously calculated sample points for the remainder of the scan line are still valid.

### CHAPTER VI

# DEVELOPMENT OF THE NEW ALGORITHM

As is usually the case in the development of new algorithms, the process was evolutionary. Successive algorithms were developed, tested, and improved upon. The history of this algorithm can be divided into six distinct steps. These programs are called VSG1, VSG2, etc.

1. The first step used edges on each scan line. The edges were sorted in X separately, and after sorting they were read in order. Every time an even number of edges was found associated with a pclygon, a segment block was created from free storage. Finally, the segments were depth sorted for visibility.

2. VSG2 linked the edges together with pointers after sorting in X. This eliminated the creation of segment blocks on each scan line.

3. VSG3 took the edge data and created segment blocks only when edges entered on a scan line. These segments are described in Chapter III-F. Since there are one half as many segments as edges, the X-sort on each scan line is twice as fast as in VSG2. Also, edges no longer needed to be linked together on every scan line.

4. VSG4 eliminated the X-sort which was done separately before the depth sorting. The X-sort and depth sort were done simultaneously on each scan line.

5. The four previous algorithms used planar equations and a multiplier for calculating depths of the polygons. A divider was also required for finding the intersect of two polygons. VSG5 replaced the arithmetic unit with the midpoint clipping simulation described in Chapter III-E.

6. Up to this point all algorithms used a bucket sort as described by Romney [5] for sorting segments in X. This final algorithm used the assumption that a sorted list will remain sorted by interchanging only a few segments when proceeding from one scan line to the next.

# CHAPTER VII

# TEST DATA

Ten objects were chosen to represent various complexities of pictures. Figures 22-31 contain pictures of the objects. Each object has two pictures. One shows all edges in the picture and the other shows the objects after visible surfaces are found and shaded.

A. Objects

Object 1, Penetration: The object is relatively simple but has many intersecting planes.

Object 2, E-S: Many edges abound in the picture and a great amount of visible complexity exists.

Object 3, Low Area: Although intersections abound, the picture only occupies a small area.

Object 4, Cubel: Twenty-five cubes exist, but only the front cube is visible.

Object 5, Cube2: Object 4 has been rotated so that parts of all twenty-five cubes are visible. An enormous amount of visible complexity exists.

Object 6, Shapel: This object is made up of many long and narrow polygons which are long in the X direction.

Object 7, Shape2: Object 6 has been rotated so the polygons are long in the Y direction. These two objects are to show what effect the object orientation can have on the scanning process.

Object 8, Sheet: This is a wavy object made up of triangles. Everything is at least partly visible.

Object 9, Simplel: This object is made up of a large cube encompassing a sphere and intersecting cubes.

Object 10, Simple2: Object 9 has been changed slightly so the sphere intersects the cube and is partly visible.

### B. Statistics

For each of the VSG algorithms mentioned in Chapter VI, statistics were gathered. These statistics included data about the object (number of polygons, etc.), computation required, memory reference counters, and various other counters. Appendix II contains a list of statistics. At the beginning of each set of statistics for a particular algorithm, there is a table describing the various counters. Figure 32 contains a table of statistics that have been extracted for the Penetration object (Figure 22). The statistics of the six various changes in the algorithm are shown for that object. The table in Figure 33 shows a cross section of statistics for all the objects with the final algorithm.

## C. Analysis

Before any statistics were gathered, arithmetic computation was suspected to be the bottle-neck in solving the hidden line problem. Statistics, however, showed that



Figure 22 Object 1: Penetration



Figure 23 Object 2: E-S



Figure 24 Object 3: Low Area





Figure 26 Object 5: Cube2



Figure 27 Object 6: Shape1

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Figure 28 Object 7: Shape2



Figure 29 Object 8: Sheet



Figure 30 Object 9: Simple1



|   |        |        | T     | · · · · · · · · · · · · · · · · · · · |       |       |
|---|--------|--------|-------|---------------------------------------|-------|-------|
|   | IÐSA   | VSG2   | VSG3  | VSG4                                  | VSG5  | VSG6  |
| 1 | 137607 | 101892 | 37919 | 21730                                 | 21224 | 24291 |
| 2 | 9172   | 112    | 38    | 54                                    | 54    | 56    |
| 3 | 76     | 44     | 25    | 24                                    | 23    | 23    |
| 4 | 7068   | 6975   | 6839  | 9210                                  | _     | -     |
| 5 | 26     | 22     | 22    | 15                                    | _     | -     |
| 6 | -      | -      | -     | -                                     | 35604 | 32925 |

- 1. Number of memory references required
- 2. Number of total memory blocks used
- 3. Maximum number of blocks used at a time
- Number of multiplications for depth test required (If multiplier-divider used)
- 5. Number of divisions for intersections required (If multiplier-divider used)
- Number of addition cycles required for depth comparisons (If multiplier-divider not used)

Figure 32

Statistics of the Penetration Object

for the Six Algorithms

| IMPLE2      | s          |     | 148  | 308   | 1000  | 4000  | 21   | 5263  | Cors | 90  | 22    |       | 14926 | 2.23  | 14000  | 58647 | 4.94  | 1.078  | -    |
|-------------|------------|-----|------|-------|-------|-------|------|-------|------|-----|-------|-------|-------|-------|--------|-------|-------|--------|------|
| IMPLET      | s          |     | 148  | 308   | 6175  | 42162 | 0    | 1652  |      | 66  | 18    | 4444  | 2039  | 1.46  | 30501  | 07094 | 3.74  | 1.128  | 5    |
| TEET        | in         |     | 7.67 | 308   | 12500 |       | a    | 6935  | 200  | 250 | IE    | 26970 | DICON | 2.15  | 14176  |       | 2.07  | 1.17%  | 25   |
| SHAPE2      | (1)<br>(1) | UUL | DOT  | 201   | 25590 |       | 0    | 12023 | 76   | 2   | 50    | 79762 |       | 3.11  | 85941  | 1     | 2.66  | 0.528  | 1600 |
| талунз      |            | 100 |      | 201   | 12424 | 9     |      | 5630  | 50   |     | 24    | 34314 | 1     | 5.16  | 30227  |       | 77.7  | 1.69E  | 10   |
| COBET       |            | 150 | AAC. | 005   | 15410 | 0     | 1000 | 1770  | 121  |     | 0.5   | 80945 | 5 30  | C7.0  | 061601 | 2.05  |       | \$07.4 | 1700 |
|             |            | 150 | 300  |       | BCT/  | 0     | 1228 |       | 25   | 30  |       | 1608  | 1.06  | 10274 | BICAT  | 2.89  | 0 000 |        | 7    |
| LOW AREA    | 100        | DOT | 210  | 9164  | 5     | t's   | 4193 | 001   | 50T  | 31  | VEDAC | TINKT | 2.62  | 25641 |        | 3.23  | 4.06% |        | 2    |
| S-3         |            | 202 | 480  | 15278 |       | 5     | 7052 | 746   | 01.4 | 40  | 47030 |       | 3.07  | 47174 | 2 60   | 4.39  | 3.48% | 30     |      |
| NOITARTENEY |            |     | 105  | 8802  | 14    |       | 3844 | 56    |      | 23  | 24291 | er c  | 61.7  | 32925 | 3 38   | 0000  | 2.96% | 10     |      |
|             | 1          |     | 7    | •     | 4     |       | 2    | 9     | ,    | -   | 8     | a     | •     | 10    | 11     |       | 12    | E      |      |

Statistics of VSG6 for the Ten Test Objects

Figure 33

- Number of polygon blocks used to describe the object Ч.
- 2. Number of edge blocks used to describe the object
- 3. Total number of times that edges cross scan lines
- 4. Number of implied lines
- 5. Number of output segments
- Total number of memory blocks required for storing segment information (300 bits/block) 9
- Maximum number of memory blocks ever used at one time for storing segments 7.
- 8. Total number of references to segment blocks
- 9. Ratio of line 8 over line 3
- (Includes one add Total number of add cycles required (Includes one a cycle per depth test for loading clipping registers) 10.
- (Includes one Average number of add cycles per depth test add cycle for loading clipping registers) Ц.
- ЧO Percent of time when segments are not put on the end X-sort list for the following scan line 12.
- Minimum output segment buffer required for real time display 13.

# Figure 33 Continued

memory bandwidth was the critical factor, with the polygon segment block being the most accessed array! For the hardware processor, a special purpose memory would be used where 300 bits could be accessed at one time. With semiconductor memories it is becoming economical to do this.

From the first five different changes in the algorithm in Figure 32, one can see a steady decrease in the number of memory references. The final algorithm, however, produced an increase in memory references due to the X-sort technique described in Chapter III-F. In spite of this apparent increase in memory references for VSG6, the overall number of memory references in VSG5 would have been greater if accesses to the bucket X-sort memory had been counted. The design and cost for such a bucket X-sort memory also were compelling factors in deleting it even though accesses to the segment memory increased.

When the program proceeds from one scan line to the next, each segment block needs to be accessed for incrementing the X and Z values. At this same time, another X-sort list is being sorted in preparation for the following scan line. Segments are read from the beginning of the X-sort list for the current scan line and are usually inserted at the end of the X-sort list which is being prepared for the next scan line. Figure 33 (line 12) shows the percentage of times that segments cannot be inserted at the end of the list, and when the previous segment pointers

must be used for finding the correct position in the list for inserting the segment block. The percentage varies between 0 to 4 percent for the ten test objects. Thus, the overhead of tracing back through a list to keep it sorted is extremely low. Also, no large, expensive, or possibly time-consuming special sorting hardware needs to be used.

Visual complexity is much more important in determining the speed of the algorithm than is the total object description. Object 4 and Objecc 5 are both sets of twenty-five cubes. However, Object 5 requires over ten times the number of memory references as Object 4. A picture visually identical to Object 4, but containing only one cube, was compared with Object 4. Even though Object 4 contained twenty-five cubes, it only had six times the memory references as the single cube object.

One way of measuring the performance of the algorithm is to create a relationship between the object description and the number of memory references to the segment array. Two memory references (a read from memory followed by a write to memory) are always required to increment the X and Z values of a segment when proceeding from one scan line to the next scan line. From the total number of times edges cross scan lines (line 3 of Figure 33), the minimum number of memory references needed can be calculated from Equation 5.

$$M_{\min} = (S*N)/E$$

(5)

where M<sub>min</sub> is the minimum number of memory references that can be expected. S is the number of memory references required to increment a segment (2). N is the total number of times that edges cross scan lines. E is the number of edges contained in a segment (2). Equation 5 reduces to Equation 6.

$$M_{\min} = N$$
(6)

Equation 7 is the ratio (R) of  $M_{total}$  (the total number of memory references actually used) to  $M_{min}$ .

$$R=M_{total}/M_{min}$$
 (7)

Line 9 of Figure 33 lists the different values of R for the ten test objects.

The clipping of segments for depth sorting is very fast. Line 11 of Figure 33 contains the average number of add cycles required by the clipping registers to satisfy the depth comparison test between two polygon segments (see Chapter III-G). One of the add cycles is for loading the clipping registers. Even counting this, the average number is between two to three add cycles per depth test!

The ten test objects were also used by Stephen McCallister [9] for gathering statistics on different versions of Warnock's algorithm. Comparisons are shown for a particular version which divides an area into four sub-areas using a vertex closest to the center of the large area for the common corner of the four sub-areas. If an area is completely covered by a polygon, is void of all

polygons, or has only one visible edge in the area, it is simple enough to be displayed without further reduction.

Statistics for Object 2, E-S (Figure 23), were gathered. A large data structure was used requiring polygon lists, edge lists, and a vertex and planar equation array. Each polygon block consisted of several words, but only accesses to each polygon block (not word) were counted. The same was also true of the remaining data structure. The following information was gathered:

> Polygon Block Accesses-----336,156 Edge Block Accesses-----427,688 Vertex Array-----220,910 Planar Equation Array-----21,072 Total Accesses-----1,005,826

The number of accesses to memory was far greater than that required by the new scan line algorithm (47,030). Also, Warnock's algorithm requires that the complete object description be stored in fast memory, and not just those objects pertaining to the current scan line.

D. Output Buffering

Whenever a cathode ray tube (CRT) is being continually refreshed, the rate of moving the beam must remain constant if the displayed intensity is to be a function of the analog input intensity. That is, the X and Y deflection circuits must be changed at a constant rate. The output of the VSG

does not generate segments at a rate inversely proportional to the length of the segments. Therefore, a buffer for temporarily storing segments must be inserted between the VSG and the display.

In Figure 26 (Object 5: Cube2), the Y scan goes from the bottom to the top of the picture. The VSG can quickly determine the visibility of the bottom half of the picture but will require a great amount of time for the top half of the picture. The display, however, must spend the same amount of time on each half of the picture. Because of this, almost the entire bottom half of the picture would need to be buffered. On the other hand in Figure 23 (Object 2: E-S), the VSG runs at a fairly constant rate over the whole picture, and only a small amount of buffering would be required.

For the ten test objects, line 13 of Figure 33 shows the smallest number of segments that must be stored at one time in order to have a display running at thirty frames per second with a constant rate for the X and Y deflection of the CRT beam. The VSG was simulated to reference the polygon segment array every 200 nanoseconds. For objects which have a uniform distribution over the area, only a small buffer size was needed. For Cube2, which has a concentration of visible information in the upper right hand corner, a much larger buffer size was required.

### CHAPTER VIII

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### CONCLUSION

The processor described can be built with equipment available today. The segment memory must be in the 200 nanosecond cycle range, and semiconductor memories are available in this range. Also, only a small memory is required since 18 to 50 segment blocks at most are needed at any one time for any of the ten test objects.

The algorithm has been simulated in Fortran IV on a PDP-10 at the Computer Science Department at the University of Utah. Other pictures have been taken to show how coloring and shading adds to the realism of objects. Figures 34-39 show various objects. Total computation time for generating and displaying the pictures is short. Cube. (Object 4) required 30 seconds, and the church of Figure 35 containing 345 blocks (six polygons per block), required only 2.5 minutes. Figure 36 shows the back view of Figure 35 with the blocks randomly colored.



Figure 35 Church



Figure 36 Rear View of Church with Randomly Colored Blocks



Figure 37 Apollo Command and Service Module



Figure 38 Tori



Figure 39 Randomly Colored Surface

3
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#### APPENDIX I

### LISTING OF PROGRAM

The hidden line program is called as a subroutine from a main program. VSG6 contains counters interspersed throughout the program for gathering statistics like those in Appendix II. VSG6 is written in FORTRAN IV.

Several subroutines are called by the program:

- LDRPT(I,J) < loads the right half of J (sign extended) into I.
- LDLPT(I,J) < loads the left half of J (sign extended) into I.

STRPT(I,J) < stores the right half of I into the right half of J. The left half of J remains undisturbed. STLPT(I,J) < stores the right half of I into the left half of J. The right half of J remains undisturbed.

SHOW < displays the segments stored in the VISSEG array. LSTSET(N) < initializes a free list structure with

blocks of N words each.

GETBLK(I) < gets a block from the free list. I is the index of that block and is set by the subroutine. RETBLK(I) < returns a block to the free list. I is the index of the block to be returned.

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SUBROUTINE HIDDEN(PIX, STAT) COMMON/FREE/EDGEST, DUM, POLYST COMMON/FREE1/Q1(4), FRAMEX, FRAMEY COMMON/FREE2/X(1000),Y(1000),Z(1000),CX(700),CY(700), 1CZ(700),CD(700) IMPLICIT INTEGER (A-Z) REAL X,Y,Z,CX,CY,CZ,CD COMMON/SCOPE/VISSEG(512),BUCKY(512) DIMENSION EDGE(1),SEG(1),POLY(1) EQUIVALENCE (EDGEST,EDGE,SEG,POLY) DIMENSION ZS(10),SAM(3,2) DIMENSION PQ(16),Q(10,26),ADDS(20) PQL=16 QL=26 PQ(1)=NUMBER OF TOTAL BLOCKS REQUIRED FOR HIDDEN LINE WORK. PQ(2)=MAXIMUM NUMBER OF TOTAL BLOCKS EVER USED AT ONE TIME. PQ(3)=CURRENT NUMBER OF TOTAL BLOCKS AT A GIVEN TIME. (USED FOR CALCULATING PQ(2).) PQ(4)=TOTAL NUMBER OF EDGE BLOCKS IN FRAME. PQ(5)=NUMBER OF EDGE BLOCKS WITH AT LEAST ONE OF THE CONNECTED POLYGONS DRAWN CLOCKWISE. PQ(6)=NUMBER OF THOSE EDGE BLOCKS OF PQ(5) WHOSE Y VALUE OF THE BEGIN PT IS NOT THE SAME AS THE END PT Y VALUE. PQ(7)=TOTAL NUMBER OF POLYGON BLOCKS IN THE FRAME. PQ(8)=NUMBER OF POLYGON BLOCKS DRAWN CLOCKWISE. PQ(9)=POINT DENSITY. PQ(10)=NUMBER OF INVOLVED SCAN LINES. PQ(11)=MEMORY REFERENCES FOR SEGMENT CREATOR. PQ(12)=NANOSECONDS PER MEMORY REFERENCE FOR SEGMENT CREATOR. PQ(13)=MEMORY REFERENCES FOR DEPTH CALCULATOR. PQ(14)=NANOSECONDS PER MEMORY REFERENCE FOR DEPTH CALCULATOR. PQ(15)=MEMORY REF. TOTAL PQ(11),PQ(13) PQ(16)=NANOSECONDS FOR PQ(15). ADDS(I)=NUMBER OF TIMES THE DEPTH TEST WAS SATISFIED IN.

С

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|   | Q COUNTERS<br>Q(1,X)=TOTAL PER FRAME<br>Q(2,X)=MAXIMUM REQUIRED OF A SCAN LINE<br>Q(3,X)=AVERAGE OF TOTAL SCAN LINES. ALSO SCRATCH FOR Q(2,X)<br>Q(4,X)=REQUIRED FOR PRE-FRAME PROCESSING<br>Q(5,X)=MAXIMUM REQUIRED FOR SCAN PREPARATION PROCESSING<br>Q(6,X)=NANOSECONDS REQUIRED. ALSO SCRATCH FOR Q(5,X)<br>Q(7,X)=MAXIMUM REQUIRED FOR SCAN DEPTH PROCESSING<br>Q(8,X)=AVERAGE OF ACTIVE SCAN LINES. ALSO SCRATCH FOR Q(7,X)<br>Q(8,X)=TOTAL FOR SCAN PREPARATION PROCESSING<br>Q(10,X)=TOTAL FOR SCAN DEPTH PROCESSING   |
|---|--|
| 000000000000000000000000000000000000000 | Q(X,1)=NUMBER OF SLOPE CALCULATIONS.<br>Q(X,2)=NUMBER OF INTERCEPT CALCULATIONS.<br>Q(X,3)=NUMBER OF SAMPLE POINTS STORED FOR NEXT SCAN LINE.<br>Q(X,4)=SUBDIVISIONS (NOT FROM INTERSECTING CASE).<br>Q(X,4)=SUBDIVISIONS (NOT FROM INTERSECTING CASE).<br>Q(X,5)=<br>Q(X,6)=DEPTH SAMPLES REQUIRED.<br>Q(X,7)=<br>Q(X,8)=SAMPLE POINTS DELETED.<br>Q(X,8)=SAMPLE POINTS DELETED.<br>Q(X,10)=OUTPUT SEGMENTS.<br>Q(X,10)=OUTPUT SEGMENTS.<br>Q(X,10)=OUTPUT SEGMENTS.<br>Q(X,10)=OUTPUT SEGMENTS.<br>Q(X,10)=OUTPUT SUBDIVISIONS.<br>Q(X,13)=OVERHEAD PIPELINE TIME.<br>Q(X,13)=OVERHEAD PIPELINE TIME.<br>Q(X,14)=TIME WAITING FOR CLIPPER.<br>Q(X,15)=READS FROM POLY.<br>Q(X,15)=READS FROM SEGE.<br>Q(X,19)=READS FROM SEG<br>Q(X,20)=WRITES TO SEG<br>Q(X,20)=WRITES TO SEG<br>Q(X,22)=<br>Q(X,23)=READS FROM FREE LIST(GETBLK)<br>Q(X,24)=WRITES TO FREE LIST(GETBLK)<br>Q(X,25)=READS FROM BUCKY<br>Q(X,26)=USED FOR SHADER |

| C<br>C   | INITIALIZATION.  |
|----------|--|
|          | D0 8 I=1.QL  |
|          | DO 8 J=1.10  |
| 8        | Q(J,I)=2   |
|          | DO 9 I=1.PQL   |
| 9        | PQ(I)=0  |
|          | DO 12 I=1.20   |
| 12       | ADDS(I)=0  |
|          | DO 10 I=1.FRAMEY   |
| 13       | BUCKY(I)=0   |
|          | CALL LSTSET(14)  |
|          | DEPTH=.TRUE.   |
|          | SAM2S=0  |
|          | SAM2X=FRAMEX   |
|          | SEGS2=0  |
|          | SEGL2=Ø  |
|          | POLYCH=Ø   |
| ~        | IMPLST=0   |
|          | GO THROUGH ALL POLYGONS AND NOTE WHICH WAY EACH POLYGON  |
|          | IS DRAWN (CLOCKWISE OR COUNTER CLOCKWISE) BY CHECKING  |
| C        | CZ OF PLANAR EQUATIONS AND MARK THE POLYGON BLOCK.   |
| <b>.</b> |  |
| 90       | POLYCPOLYPI, EQ. 0) GO TO 99   |
|          | CALL I DED T(INDEX, DOLY(DOLYDE) ON  |
|          |  |
|          | $P(1_{1}) = P(1_{1}) $ |
|          | $0(1, 16) = 0(1, 16) \pm 1$  |
|          | IF(C7(INDEY)   F Q)C0 T0 05  |
|          |  |
|          | POLY(POLYPT+3)-2   |
|          | PQ(R)=PQ(R)+1  |
| 95       | CALL LORPT(POLYPT, POLY(POLYPT))   |
|          | GO TO 90   |
|          |  |

| C   | INITIALIZATION CONTINUED.                        |
|-----|--|
| č   | TAKE EACH EDGE AND PUT IN THE BUCKY GIVEN BY ITS |
| 00  | SPALLEST Y VALUE. THIS IS THE Y-SORT OF EDGES.   |
| 100 | IF(FDCFPT FO GLOD TO OGT                         |
|     |  |
| C   | $I \oplus (4) = F \oplus (4) + I$                |
| č   | FATER FACH FROT IN DUCKN TR LE LE LE             |
| č   | TWO POLYCONE IS DOALN OL CONVERSE                |
| č   | TWO FOLFBUNS IS DRAWN CLOCKWISE.                 |
| •   | CALL I DI PT ( POL VI EDOF (EDOFD THON)          |
|     | CALL LDPPT(POLYL, EDGE(EDGEPT+2))                |
|     | O(1, 17) = O(1, 17) + 1                          |
|     | IF(POLYR FO POLYL) CO TO LLO                     |
|     |  |
|     |  |
| 103 | IF(PO Y(PO YR+1)) IT (B) CO TO 107               |
|     | Q(1,15)=Q(1,15)+1                                |
| 104 | CALL I.DIPTCINDEX, EDGECEDGEPTLIND               |
|     | YBEG=Y(INDEX)                                    |
|     | CALL LDRPT(INDEX, EDGE(EDGEPT+1))                |
|     | YEND=Y(INDEX)                                    |
|     | PQ(5)=PQ(5)+1                                    |
|     | IF (YBEG.EQ.YEND) GO TO 110                      |
|     | PQ(6)=PQ(6)+1                                    |
|     | IF(YBEG.LT.YEND)GO TO 105                        |
|     | I=YEND   |
|     | YEND=YBEG  |
|     | YBEG=I   |
| 105 | YBEG=YBEG+1                                      |
|     | IF(YBEG.LE.Ø)GO TO 115                           |
|     | IF (YEND, GE, FRAMEY) GO TO 115                  |
|     |  |
|     | BUCKY(YBEG)=EDGEPT                               |
|     | $Q(1_{9}18) = Q(1_{9}18) + 1$                    |
| 110 | CALL SILFI(I, EDGE(EDGEPT))                      |
| 110 | CALL LDRPT(EDGEPT,EDGE(EDGEPT))                  |
| 15  |  |
| 12  |  |
| 16  | FORMAT( FRROR OF ICCT NOT IN DOUNDO OF TOTAL     |
|     | TORINITY CHRONALADDECT NOT IN BOUNDS OF FRAME!") |

| с<br>200 | SCAN LINE COMPUTATION.<br>Continue   |
|----------|--|
| 201      | DO 201 I=1,QL<br>Q(4,I)=Q(1,I)   |
| 204      |  |
|          | DO 202 I=1,QL  |
|          | Q(6, I) = Q(1, I)<br>Q(9, I) = Q(9, I) = Q(1, I)                               |
| 202      | Q(3,I)=Q(1,I)  |
| L.       | INITIALIZE ALL POINTERS.   |
|          | SEGLST=SEGL2   |
|          | SEGS2=0<br>SEG12-0   |
|          | SAMIS=SAM2S  |
|          | SAMIL=SAM2L<br>SAM25-0   |
|          | SAMIX=SAM2X  |
|          | SAM2X=FRAMEX   |
|          | SEGCNT=0   |
| C<br>C   | SCAN PREPARATION PROCESSING.   |
| č        | AND BUILD THE SEGMENT LIST (SEC)   |
|          | IF(BUCKY(IY).EQ.0)GO TO 230  |
|          |  |
| 210      | IF(EDGEPT.EQ.0)GO TO 230   |
|          |  |
|          | CALL LDRPT(END, EDGE(EDGEPT+1))  |
|          | YBEG=Y(BEG)  |
|          | DELY=YBEG-YEND   |
|          | $IF(DELF \cdot EQ \cdot 0) GO TO 229$<br>$IF(DELY \cdot LT \cdot 0) GO TO 211$ |
|          |  |
|          | ENDEI  |
| 211      | DELY=-DELY   |
|          | Q(1,1)=Q(1,1)+1  |
|          | XSLOPE=((X(END)-X(BEG))/(Y(END)-Y(BEG)))*262144.0                              |
|          | IX=IX+ZMUL(XSLOPE.DEL)   |
|          | CALL LDLPT(IXE,IX)   |
|          | II=-1  |
| С        | CALL LDRPT(POLYPT, EDGE(EDGEPT+2))   |
| 212      | IF (POLYPT.EQ.0) GO TO 228   |
|          | Q(1,15)=Q(1,15)+1<br>IF(POLY(POLYPT+1) FOLT1)COLTO TO TOT                      |
|          | Q(1,16)=Q(1,16)+1  |
|          | POLY(POLYPT+1)-LT.0)GO TO 213  |
|          | POLYCH=POLYPT  |
| 213      | SEGPT=POLY(POLYPT+1))  |
|          | PREV=0   |
|          | IC NUZPE-1   |

| 214 | IF (SEGPT.EQ.Ø)GO TO 220                   |
|-----|--|
|     | Q(1, 19) = Q(1, 19) + 1                    |
|     | CALL LDRPT(YEND2.SEG(SEGPT+2))             |
|     | CALL LDLPT(YEND1.SEG(SEGPT+2))             |
|     | IF(YENDI, GE, Ø) GO TO 217                 |
|     | TF1 = IX - SFG(SFGPT + 3) + SFG(SFGPT + A) |
|     | IE(TE1 E0 A)TE1-YE1OPE-CECCCECPTAN         |
|     |  |
|     | IF (IEI. LI. 0) 60 10 220                  |
|     | IF (YENDZ.GE.Ø)GU IU 218                   |
|     | TE2=IX-SEG(SEGPT+5)-SEG(SEGPT+6)           |
|     | IF(TE2.EQ.0)TE2=XSLOPE-SEG(SEGPT+6)        |
|     | IF(TE2.LT.0)GO TO 223                      |
|     | GO TO 218                                  |
| 217 | IF(YEND2.GE.Ø)GO TO 218                    |
|     | TE2=IX-SEG(SEGPT+5)-SEG(SEGPT+6)           |
|     | IF (TE2.EQ.Ø)TE2=XSLOPE=SEG(SEGPT+6)       |
|     | IF(TE2.GF.Ø)G0 T0 218                      |
|     | MODE-0                                     |
|     | PDFU-CFCDT                                 |
|     | CO TO COT                                  |
| 010 |  |
| 218 | TENUZFETENUZ                               |
|     | PREVESEGPI                                 |
|     | CALL LDRPT(SEGPT, SEG(SEGPT+1))            |
| •   | GO TO 214                                  |
| 220 | MODE=2                                     |
|     | IF(YEND2P.GE.0)GO TO 227                   |
|     | FROM=Ø                                     |
|     | GO TO 226                                  |

| 223   | FROM=-1   |
|-------|---|
|       | PREV=SEGPT /3   |
|       | CALL LDRPT(SEGPT-SEG(SEGPT+1))  |
|       | GO TO 226   |
| 224   | SEG(1+5)=SEG(PREV+5)  |
|       | SEG(1+6)=SEG(PREV+6)  |
|       | SFG(1+0)-SFG(PPFV+0)  |
|       | SEG(1+10)-SEG(PDEULIA)  |
|       |   |
|       |   |
|       | MODE-2  |
|       | GD TO 227   |
| 226   |   |
|       |   |
|       |   |
|       |   |
|       |   |
|       |   |
|       | TECOTE STATISEGET SEGETTIS  |
|       | IF (I A E V + B E A) (I A B) = O(I A B) =   |
|       |   |
|       |   |
|       |   |
|       |   |
|       |   |
|       | $\sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{i=1}^{n} \sum_{i=1}^{n} \sum_{i=1}^{n} \sum_{i$ |
|       |   |
| 227   |   |
| 2.6.1 |   |
|       |   |
|       |   |
|       | IF (MODE . EQ. (7)CALL SILFI(DELY, SEG(PREV+2))   |
|       | SEGUPEVICENCENTIAL SIRFI(DELY, SEGUREVEZ))  |
|       | SEG(PREVETHODE)=((2(END)-2(HEG))/(Y(END)-Y(REG)))*262144.0  |
|       |   |
|       | SEG(PEEV+7+MODE)=SEG(PREV+7+MODE)+2MUL(SEG(PREV+8+MODE),DEL)  |
| 220   | CALL IN PT(POLYPT EDGE(REV+R+MODE) -SEG(PREV+R+MODE)  |
| 225   | UNLL LULFINFULFFI, LULE(EUGEFI+2))  |
|       |   |
| 220   | [A] = [A]   |
| 664   | CALL LULFI(LUGEFI, EUGE(EUGEPI))  |
|       |   |

| C   | SEGMENT PACKER AND SEGMENT EL THILVATOR   |
|-----|---|
| 230 | IF (POLYCH FR. (1) GO TO 240  |
|     | Q(1.15)=Q(1.15)+1   |
|     | Q(1, 16) = Q(1, 16) + 1   |
|     | CALL STIPT(A. POLY (POLYCULLAN)   |
|     | NEXT=POLY(POLYCHAN)   |
|     | SEGPT=0   |
| 231 | IF (NEXT.FR. 0) GO TO 240   |
|     | PREV:SFGPT  |
|     | SEGPTENERT  |
|     | Q(1, 19) = Q(1, 19) + 1   |
|     | CALL I DRPT(NEXT SECONDENS)   |
|     | IF (SEG(SEGPT+2) NE () CO TO TO   |
|     | IF (PREV. NE 0)0(1 00)-0(1 00)-1  |
|     | IF (PREV NE Q)CALL CTERT (1,20)+1   |
|     | IF (PREV FO G) POLY (POLY (NEXT, SEG(PREV+1))   |
|     | Q(1,24)=Q(1,24)+1   |
|     | PQ(3) = PQ(3) - 1   |
|     | CALL RETRINGERPTY   |
|     | SEGPT=PRFV  |
|     | GO TO 231   |
| 233 | NEXTINEYT   |
|     | CALL LORPT (YEND2 SECRETION)  |
|     | IF (YEND2, GE. Ø) GO TO 017   |
|     | CALL IDIPTIVENDI SECCEPTION   |
|     | IF (YENDI 1 T. 0) GO TO 2305  |
|     | SEG(SEGPT+3)=SEG(SEGPT+5)   |
|     | SEG(SEGPT+4)-SEG(SECPT+C)   |
|     | SEG(SEGPT+7)=SEG(SEGPT+0)   |
|     | SEG(SEGPT+8)=SEG(SEGPT+10)  |
|     | CALL STLPT (YEND2 SEG(SEGPT+2))   |
|     | $\cdot = \cdot \cdot$ |

| 237  | IF(NEXTI.EQ.0)GO TO 241<br>CALL LDLPT(YENDI,SEG(NEXT1+2))<br>Q(1.19)-Q(1.19)+ |
|------|---|
|      | IF (YENDI-GE.Ø) GO TO 238   |
|      | CALL STRPT (YENDI, SEG(SEGPT+2))  |
|      | SEG(SEGPT+5)=SEG(NEXT1+3)   |
|      | SEG(SEGPT+6)=SEG(NEXT1+4)<br>SEG(SEGPT+9)=SEG(NEXT1+4)                        |
|      | SEG(SEGPT+10)=SEG(NEXT1+7)<br>CALL DIST SEG(NEXT1+8)                          |
|      | CALL LDEPT(SI,SEG(NEXTI))<br>CALL LDEPT(S2,SEG(NEXTI))                        |
|      | IF(S1.NE.0)CALL STRPT(S2,SEG(S1))<br>IF(S1.E0.0)SEGYSTES2                     |
|      | IF (NEXTI.NE.SEGLST)CALL STLPT(SI.SEG(S2))                                    |
|      | G(1,20)=Q(1,20)+1   |
|      | SEG(NEXTI)=-1<br>G0 TO 2395   |
| 23F  | CALL LDRPT(YEND2, SEG(NEXT1+2))   |
|      | Q(1,20)=Q(1,20)+2   |
|      | CALL STRPT(YEND2,SEG(SEGPT+2))<br>SEG(NEXT1+2)-0                              |
|      | SEG(SEGPT+5)=SEG(NEXT1+5)   |
|      | SEG(SEGPT+9)=SEG(NEXT1+6)<br>SEG(SEGPT+9)=SEG(NEXT1+9)                        |
|      | SEG(SEGPT+10)=SEG(NEXT1+10)<br>GO TO 2395                                     |
| 239  | CALL LDRPT(NEXTI,SEG(NEXTI+1))  |
| 2395 | IF(SEG(SEGPT).NE1)GO TO 231   |
|      | CALL LDLPT(IXE,SEG(SEGPT+3)+SEG(SEGPT+4))<br>S1=PREV                          |
| 2396 | IF(SI.NE.Ø)CALL LDRPT(S2,SEG(SI))   |
|      | IF (SI .EQ.SEGLST)S2=0  |
|      | Q(1,19)=Q(1,19)+1<br>IF(S2.EQ.0)GO TO 2397                                    |
|      | CALL LDLPT(IX,SEG(S2+3)+SEG(S2+4))  |
|      | S1=52   |
| 2397 | IF (S2.NE.0)SEG (SEGPT) = 52  |
|      | Q(1,20)=Q(1,20)+1<br>CALL STIPT(S1 SEC(SECOTA)                                |
|      | IF(SI.NE.Ø)CALL STRPT(SEGPT,SEG(SI))  |
|      | IF (SI.EQ.0)SEGXST=SEGPT<br>IF (S2.NE.0)CALL STLPT(SEGPT_SEG(SON)             |
|      | IF(S2.EQ.Ø)SEGLST=SEGPT   |
| 240  | POLYCH=POLY(POLYCH+1)   |
| 241  | PAUSE 'UNCLOSED POLYGON'  |
|      | SEG(SEGPT+5)=SEG(SEGPT+3)<br>SEG(SEGPT+6)=SEG(SEGPT+4)                        |
|      | CALL STRPT(0,SEG(SEGPT+2))  |
|      | 10 2342   |

| с   | DEPTH SORTER.                                |
|-----|--|
| 242 | CONTINUE                                     |
|     | DO 276 1=1-0                                 |
|     | $\theta(6, 1) = \theta(1, 1) = \theta(6, 1)$ |
|     | 10(9(5,1)   T 0(6 T))0(6 T)-0(6 T)           |
|     | 0(9,1)=0(9,1)+0(1,1)                         |
|     | P(10,1) - O(10,1) - O(1,1)                   |
| 276 | P(8,1)-0(1,1)                                |
|     | LE(1Y GT ERAMENICO TO AND                    |
|     | SAM(1 2)-1                                   |
|     | SAM(2 2)-4                                   |
|     | CALL IDERT/CCCDT INDERT                      |
| 278 | IF (FECRI FO RECONT AND THE                  |
| 2.0 |  |
|     |  |
|     | PO(1)-PO(1)                                  |
|     | P(1, 24) = O(1, 04) + 1                      |
|     | SECPT-NEVT                                   |
|     | 60 TO 970                                    |
| 279 | INPLST TAPLE THOROUGH                        |
|     | SECART+4                                     |
| с   | SAMPLE CRAN OFURDATION                       |
| 281 | SAMEL SPAN GENERATOR.                        |
|     | SAM(2 1)-SAM(1,2)+1                          |
|     | SAM(1 1)-CAM(1 O)                            |
|     | SAM(2 2)-0                                   |
|     | TE (SAMIN OF SAM(1 1)) OF TA                 |
|     | SAMIN-EDAMEN                                 |
|     | IF (SAMIS ED SAMUELOS TO DES                 |
|     | CALL L DI RT(SAMIN CCOCCUMAN                 |
|     | CALL LOPPT(SAMIC CEO(CAMIS))                 |
| 282 | SAM(1.2)-SAMIY                               |
| 299 | 75(1)-0                                      |
| -•- | FROM-Ø                                       |
|     | SEGPT=SEGACT                                 |
|     | SEGOUTER                                     |
|     | PREV-a                                       |
|     |  |

| С   | CHECK SEGMENTS FROM THE CURRENT ACTIVE LAST        |
|-----|--|
| 301 | IF (SEGPT.EQ.0) GO TO 30A                          |
|     | NUMREF = $-Q(1, 19) - Q(1, 20) - Q(1, 13)$         |
|     | Q(1, 19) = Q(1, 19) + 1                            |
|     | NEXT=SEG(SEGPT+11)                                 |
|     | XLEFT=SEG(SEGPT+3)                                 |
|     | XRIGHT=SEG(SEGPT+5)                                |
|     | ZLEFT=SEG(SEGPT+7)                                 |
|     | ZRIGHT=SEG(SEGPT+9)                                |
|     | CALL LDLPT(IXE XLEFT)                              |
|     | CALL LDLPT(IXX, XRIGHT)                            |
|     | IF(IXX.LE.SAM(1.2))G0 TO 303                       |
|     | PREV=SEGPT   |
|     | IF(IXE.GE.SAM(1,2))G0 TO 335                       |
|     | GO TO 315  |
| 303 | CONTINUE   |
|     | Q(1,20)=Q(1,20)+1                                  |
|     | IF(PREV.NE.Ø)SEG(PREV+11)=NEXT                     |
|     | IF (PREV.EQ.0)SEGACT=NEXT                          |
|     | 1F (1XX.L1.SAM(1,1)) GO TO 335                     |
|     | G(1,20)=G(1,20)+1<br>SEC(SECRT(1))=GECOUP          |
|     | JE (SEGUIT EO () CEOLO-GEODE                       |
|     | SFGOUT-SFCPT                                       |
|     | 60 TO 315  |
| С   | CHECK NEW SEGMENTS FROM THE M CODT LIGHT AND       |
| С   | INCREMENT THE Y Y 7 VALUES AND INCEDIT THE OPPOUND |
| С   | IN THE X-SORT LIST FOR THE NEXT COAN LINE          |
| 304 | SEGPT:SEGXST                                       |
|     | IF (SEGPT.EQ.Ø) GO TO 350                          |
|     | NUMREF== $Q(1, 19) - Q(1, 20) - Q(1, 13)$          |
|     | Q(1,19)=Q(1,19)+1                                  |
|     | CALL LDLPT(IXE, SEG(SEGPT+3)+SEG(SEGPT+4))         |
|     | IF(IXE.GE.SAM(1,2))GO TO 350                       |
|     | FROM=-1  |
|     | CALL LDRPT(SEGXST,SEG(SEGPT))                      |
|     | IF (SEGPT.EQ.SEGLST)SEGXST=0                       |
|     | Q(1,2)=Q(1,2)+1                                    |
|     | SEG(SEGPT+3)=SEG(SEGPT+3)+SEG(SEGPT+4)             |
|     | SEG(SEGPT+7)=SEG(SEGPT+5)+SEG(SEGPT+6)             |
|     | SEG(SEGPT+7)=SEG(SEGPT+7)+SEG(SEGPT+8)             |
|     | XI FET-SEG(SEGPT+T)                                |
|     | XRIGHT-SFG(SEGPTAS)                                |
|     | ZI. EFT=SFG(SFGPT+7)                               |
|     | ZRIGHT=SEG(SEGPT+9)                                |
|     | CALL LDLPT(YENDI SFG(SFGPT+2))                     |
|     | CALL LDRPT(YEND2.SEG(SEGPT+2))                     |
|     | YENDI=YENDI+1                                      |
|     | YEND2=YEND2+1                                      |
|     | CALL STLPT(YENDI.SEG(SEGPT+2))                     |
|     | CALL STRRT (VENDO SEGVEROPTION                     |

|      | IF (SEG(SEGPT+11).GE.Ø) GO TO 309                                   |
|------|---|
|      | IF (IXE+1.NE.SAM(1.1)) = 0 TO 308                                   |
|      | CALL LDLPT(IX,SEG(SEGPT+3)+SEG(SEGPT+A))                            |
|      | IF (IX.LE.Ø.OR.IX.GT.FRAMEX) GO TO 308                              |
|      | SAM(3, 1) = SE GPT + 12<br>SAM(2, 1) = TY                           |
|      | FM=-1   |
|      | GO TO 3091  |
| 308  | CALL RETBLK(SEGPT)  |
|      | PQ(3)=PQ(3)-1   |
|      | (1,24)=Q(1,24)+1<br>(0, T, 0, 335)                                  |
| 309  | MODE=Ø  |
|      | SEG(SEGPT)=-1   |
|      | IF (YENDI.GE.Ø) GO TO 310   |
|      | MUDE=-1   |
|      | IF $(IX_1F_0, 0F_1X_1, SEG(SEGPT+3)+SEG(SEGPT+4))$                  |
|      | FM=0  |
| 3091 | S2=0  |
| 3002 | SI=SEGL2  |
| 0032 | $\begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 $  |
|      | IF(IX, GE, IX1)GO, TO, 3004   |
|      | S2=S1   |
|      | CALL LDLPT(SI,SEG(SI))  |
|      | 0(1,19)=0(1,19)+1<br>0(1,19)=0(1,19)+1                              |
| 3994 | IF(S2.NE.0)SFG(SFGPT)-S2  |
|      | Q(1,20)=Q(1,20)+1   |
|      | CALL STLPT(S1, SEG(SEGPT))  |
|      | IF (S2.NE.0)CALL STLPT (SEGPT, SEG(S2))                             |
|      | IF (S2.EQ.0)SEGL2:SEGPT<br>IF (S1.NF.0)CALL STRET(SCOPT GROUP)      |
|      | IF(SI.EQ.0)SEGS2=SFGPT  |
|      | IF(S2.NE.0)Q(1,20)=Q(1,20)+1  |
| 310  | IF(FM)335,310,364   |
| 510  | IF (YEND2 GE A) CO TO ZOO   |
|      | MODE = - MODE   |
|      | CALL LDLPT(IX,SEG(SEGPT+5)+SEG(SEGPT+6))                            |
| 311  | IF (IX.LE.Ø.OR.IX.GT.FRAMEX) GO TO 115                              |
| C    | IF FITHER OF THE EDOLG OF THE                                       |
| C    | SCAN LINE (MODE), PUT THE COURSEPANT EXIT ON THIS                   |
| С    | THE POLYGON CHANGING LIST.  |
|      | CALL LDLPT(POLYPT, SEG(SEGPT+1))                                    |
|      | V(1, 12) = V(1, 15) + 1<br>TF (POLV(POLVPT11) 1 T (2) on The second |
|      | Q(1,16)=Q(1,16)+1   |
|      | POLY(POLYPT+1) POLYCH   |
|      | POLYCH=POLYPT   |
| 312  | CALL STLPT(-1, POLY(POLYPT+1))                                      |
| 01/2 | IF (IXE.GE.IXX) GO TO TA  |
|      | IF (IXX.GT.SAM(1.2)) GO TO 314                                      |
|      | SEG(SEGPT+11)=SEGOUT  |
|      | IF (SEGOUT.EQ.0) SEGLO=SEGPT  |
|      | GO TO 315   |
| 314  | SEG(SEGPT+11)=SEGACT  |
|      | SEGACT=SEGPT  |
|      |   |

| 315  | CONTINUE  |
|------|---|
|      | $\Theta(1, 6) = \Theta(1, 6) + 1$                         |
|      | IXI FFT-IXF   |
|      | IFCINE IT SAMEL CONTINUES                                 |
|      | CALL IDIPT/VENDI OF///EFTEIXX                             |
|      | IF(YENDL GE G)CO TO THE                                   |
|      | IF(IXE+) NF SAM(1 1))CO TO 316                            |
|      | SAM(3,1)=SEGPT+12   |
|      | CALL LDIPTISANCE IN STOCODER                              |
| 316  | CALL LDRPT(YEND2 SEG(SEGPT+3)+SEG(SEGPT+4))               |
|      | IF (YEND2, GE, B) GO TO 317                               |
|      | 1F(1XX.NE.SAM(1.2))00 TO 112                              |
|      | SAM(3,2)=SE(PT+13   |
| •    | CALL LULPT (SAM (2,2), SEGISEONTIEN GERMAN                |
|      | SIMULATION OF LOADING AND BUNNING THE STATES              |
| C    | UNIT FOR DEPTH COMPARISONS                                |
| 21.7 | ADDITION TIME ONE.  |
| 317  | XL TEST=XLEFT, AND, ( .NOT 262145)                        |
|      | XRIEST=XRIGHT.AND.(.NOT.262143)                           |
|      | NUMADDE1  |
|      | IF (FROM, WE, D) NUMA DD=NUMA DD+1                        |
|      | DELNEW=(XHTEST-XLTEST)/262144                             |
|      | IF(()) TEET ()) DELNEW=DELNEW=1024                        |
|      | TE((XPTECT CAN(1,1)+262144).LT.Ø)XLIEST-SAM(1,1)+262144   |
|      | AD.INFU- FALCE FALCE AD.INFUEST=SAM(1.2)+262144           |
|      | IF(7)FFT 17 707 OUTDAD (UDD)                              |
|      | IF(ZS(1) FO C) CO TO TO TO                                |
|      | ABLLE: FAISE  |
|      | ABLGE= FALSE  |
|      | ABRLE: FALSE.   |
|      | ABRGE= FALSE  |
|      | IF (XI TEST LE ZS(G) ABI IF- THIS                         |
|      | IF (XLTEST, GE, ZS(G))ABLGET, TRUE                        |
|      | IF (XR TEST.LE, ZS(7))ABRLE: TRUE                         |
|      | IF (XRTEST. GE.ZS(7))ABR GE = TRUE                        |
|      | IF ((( NOT ABLGE) AND. ( NOT ABRGE)) OF (( NOT ABLIES AND |
|      | I(.NOT.ABRLE)))GO TO 329                                  |
|      | ALGLIP = XL TEST  |
|      | TP (ABLLE)XLCLIP=ZS(6)                                    |
|      | TECODE CENTRES I  |
|      | DEL-DELAEU  |
|      | IF(DELNEW IT ZODELADEL DELE                               |
|      | ** COLOREW.CI.CODELIDEL=ZSDEL                             |

|      | XAMXL=XLEFT-XICLIP        |
|------|---------------------------|
|      | XBMXL -XRIGHT-XICITE      |
|      | XAMXR=XLEFT=XRCLIP        |
|      | XBMXR=XRIGHT-YPCLID       |
|      | ZAL=ZLEFT                 |
|      | ZBL=7RIGHT                |
|      | ZAR=71 FFT                |
|      | ZBR=ZRIGHT                |
|      | IF (AD INFW) GO TO TOG    |
|      | ZBI = 71 FFT              |
|      | ZAL=ZRIGHT                |
|      | ZBR=ZIFFT                 |
|      | ZARTZRIGUT                |
| 320  | XCMX1 =7S(2) -XLCLTD      |
|      | XDMX1 =7S(1)-YLOLID       |
|      | XCMXR-75(2)-XPOLID        |
|      | XDMXR=7S(X)=XPCLIP        |
|      | 1F(75(1)-2 GF @) CO TO TO |
|      | 7CI =2S(A)                |
|      | ZDL=75(5)                 |
|      | ZCR=75(4)                 |
|      | ZDR=75(5)                 |
|      | ADJOLD=7SADJ              |
|      | GO TO 323                 |
| 321  | ADJOLDE NOT AD HIEU       |
|      | IF (ADJNEW) GO TO 322     |
|      | ZCL=7S(4)                 |
|      | ZDL = 7 S (4)             |
|      | ZCP=75(5)                 |
|      | ZDR=ZS(5)                 |
|      | GO TO 323                 |
| 32.2 | ZCL=7S(5)                 |
|      | Z.DL=ZS(5)                |
|      | ZCR=25(4)                 |
|      | ZDP=ZS(4)                 |

C 

|     | CITP STATE AND OUT AND THE STATE                                    |
|-----|---|
|     | ADDOUL THE ATT ONE ADD TIME EACH PASS.                              |
|     | ADDURL= PALSE   |
|     | ABBCKR=.FALSE.  |
|     | CDBCKI - FALSE  |
|     |   |
|     | CDBCKR= "PALSE"   |
|     | DELZ=_FALSE_  |
|     | HIMOD - HIMADDA   |
|     |   |
|     | ANOLDL=(XAMXL+XBMXL)/2  |
|     | ZHOLDL=(ZA1+7B1)/2  |
|     |   |
|     | ANOLDR - (AAMAR+ABMXR)/2  |
|     | ZHOLDR=(ZAR+ZBR)/2  |
|     | XTERPL = (XCMXI + YDMXI ) /2  |
|     | 7 TEADL - COME TADIACITZ  |
|     |   |
|     | XIEMPR=(XCMXR+XDMXR)/2  |
|     | ZIENPR= (7CR+7DP)/2   |
|     |   |
|     |   |
|     | IF (ZAL-ZDL.GE.Ø)ABBCKI = TRHF.                                     |
|     | IF(7CI -7BL GF A)CODCKL - TOUC                                      |
|     | TECTAD TOD CONTROL STRUE,   |
|     | TEVENNEZDR.GE.GOABBCKR=.TRUE  |
|     | IF(ZCR-ZBR GE 0)CDBCKB= TRUE  |
|     | IF(DEL FO A)DELZ- TRUE  |
|     |   |
|     | LOGE((.NUI.ABLGE.CRNOT.ABRLE) AND. (CDBCKLAND NOT APPOUR            |
|     | I AND NOT CDBCKR) OR ( NOT ABBCKL AND NOT ORDER OF ABBCKR           |
|     | 2.0R. ( NOT ABBCKL AND NOT ADDORL AND ON COBCKL AND COBCKR)         |
|     | LOCHLORO CABBERLAND. NOI COBCRLAND. NOT ABBCKR)))                   |
|     | LUGELUG. OR. ((.NOT.ABLLE. OR . NOT. ABR GF) AND ((APPONE AND       |
|     | IABBCKR . AND . NOT COBCURY OF ( NOT ADDOUT OF CABBCKL . AND . NOT. |
|     | ZABBCKE) OF ( NOT ADDALL ON CONCLAND. NOT COBCKLAND.                |
|     | LOGIL CONCERNIT ABBERL AND NOT CDBCKL AND NOT CDBCKR)               |
|     | LUGELUG. OR. (C.NOT. (ABBCKL AND ABBCKR) AND NOT (COPCY) AND        |
|     | ICDBCKR)) AND (ABI GF, AND ABRI F, AND ADD AND AND CODECKLAND.      |
|     | JCI IP =1 OG AND HOT DELT   |
|     |   |
|     | LUGE((ABLGE, AND, ABRLE), AND, ((ABBCKL, AND, ABRCKD), OP (APPOV.   |
|     | I.NOT.CDBCKR AND.DELZ) OR (ABBCKP AND NOT CORD OR (ABBCKL AND       |
|     | 2.0R. ( NOT COBCKI AND NOT CODORA AND . HOI COBCKL AND DELZ)        |
|     | INBOY TI DO OD (DE TAND THOT CUBCKR AND DELZ)))                     |
|     | DOUAL OG ON CDELZ AND NOT ABBCKL AND NOT CDBCK                      |
|     | I AND NOT ABBCKR AND NOT COBCKR AND ABL CE AND ADDI TO              |
|     | LOG=(ABLLE AND ABRGE) AND HOT (ADLOG ADD CE AND ABRLE)              |
|     | IAND ABBCKR) OP (ABBCKL   |
|     | AND BORN OR CABBURL AND NOT COBCKR) OR (ABBCKR                      |
|     | Z • HRD • • NOI "CDBCKL)))  |
|     | LOG=LOG.AND. ((CDBCK) AND. CDBCKP) OP (CDDCK) AND                   |
|     | 1.NOT. ABBCKD AND DELTA DD CODARD OR CODBCKL AND.                   |
|     | ILDOY BOC OR AND DELZY OR COHCKR AND NOT ABBCKI AND DELZY           |
|     | JIBOX = LOG. UR. (DELZ, AND. NOT ABBCKL AND. NOT CDBCKL             |
|     | I.AND. NOT. ABBCKR AND. NOT COBCKR AND ((AD))                       |
|     | 2 AND NOT ABRIES OF CNOT ADJOR AND CABLLE                           |
|     | (OG=(DELZ AND (CONTACT ABLGE AND ABRGE)))                           |
|     | COLCELL AND CABBCKL AND NOT COBCKL AND NOT ABBCKD AND               |
|     | TCDBCKR) OR. ( NOT ABBCKL ABD CDBCKL AND ABBCKL                     |
|     | 2.AND. NOT CDBCKRYYY  |
|     |   |
|     | LOGILOG. UN. (C.NOI.ABLGE.OR. NOT.ABRLE) AND. (CABBCK)              |
|     | I AND . NOT COBCKL) OR . (ABBCKR AND NOT CORCERNAN                  |
|     | LOG = LOG OR (C. NOT APLIE OR HOT ADDOD CODERRY))                   |
|     | AND NOT APPCKINGE OR NOI ABRGE ) AND. ((CDBCKL                      |
|     | AND AND ABBCKE / OR (CDBCKR AND AND ABBCKR)))                       |
| 1   | JBOXES=LOG.OR. (DELZ.AND. NOT ABBCKI AND NOT CODOW                  |
|     | AND NOT ABBCKR AND NOT COUCED AND AND AUTICOBERE                    |
|     | AND NOT APPLEN OF CODERR AND CONTABLLE                              |
|     | HUNDER ADT CADR LED. UK. ( NOI ABLGE.AND. NOT ABRGE)))              |
|     | Uncuita   |
|     | FCJCLIP) NUMCNT=NUMCNT+)  |
|     | FCIIBOX > NUMENT - NUMENT -   |
|     |   |
| 4   |   |
| 2   | F(JØBOX) NUHCNT=NUHCNT+1  |
| 1   | F(NUMCHT_DF, 1)PAUSE  |
|     |   |
|     | r WULLF / 60 10 325   |
| 1   | F(JIBOX)60 TO 331   |
| 1   | F(JB0XFS) 60 70 320   |
| - 7 |   |
| 1   | - CORDOVICO 10 222  |
|     |   |
|     |   |



| С       | EXPAND BOX TO INCLUDE OLD DOX AND WELL SHE                            |
|---------|---|
| 329     | TS(1)-75(1) INCLUDE OLD BOX AND NEW LINE CLIPPED.                     |
|         |   |
|         | IF (•NOT•DEPTH)GO TO 326  |
|         | IF (ABRLE AND ABRGE AND ABLLE AND ABL GEN OD TO TOOL                  |
|         | IF (7) FFT-7S(A) IT ( AND AD      |
|         | TECTOL TO AND ADJNEWJZS(4)=ZLEFT                                      |
|         | 1 (2R1GH1-25(4).LT.Ø.AND.(.NOT.ADJNEW))75(4)=7R1GHT                   |
|         | IF (ZLEFT-ZS (5) . GE . Ø . AND . ( . NOT . AD INFW) )7C (5) - 71 FET |
|         | IF (ZRIGHT-75(5), GF, G AND AD INFUSTOR (C) 25(5)=2LEF1               |
|         | GO TO 330   |
| 3205    |   |
| 0297    | IF (ADJNEW AND ADJOLD AND CDBCKL)75(A) =741                           |
|         | IF (ADJNEW AND ADJOLD AND ABBCKL) 75 (A) -701                         |
|         | IF (AD.INFW. AND. NOT AD 101 DAND COLOR 4)=201.                       |
|         | IF (AD INEW AND NOT ADJULD AND ZAL LI ZCR)ZS (4) = ZAL                |
|         | TECHDONE (* AND * NOI ADJOLD AND ZAL GE ZCR)ZS(4)=7CR                 |
|         | IFCONDIOADJNEWOANDOADJOLDOANDOZAROLTOZCI )ZSCA)-ZAR                   |
|         | IF (.NOT.ADJNEW.AND.AD.IOI D.AND.ZAR GE ZCL) ZC(A) ZCL                |
|         | IF ( NOT AD INFW AND NOT AD INC DAN DE LOL J25(4)=20L                 |
|         | IF ( NOT AD INEW AND NOT ADJOLD AND CDBCKR)ZS (4) = ZAR               |
|         | (ADJNEW AND NOI ADJOLD AND ABBCKR) ZS (4) = 7CR                       |
|         | IF (ADJNEW AND ADJOLD AND CDBCKR) 75(5) =7DR                          |
|         | IF (ADJNEW AND ADJOID AND ABBCKRIZE(5)-200                            |
|         | IF (AD.INFW. AND. NOT AD IOLD AND ADD TO THE ADD                      |
|         | TECADINEW AND WOI ROJOLD AND ZBR LI ZDL)ZS(5)=ZDL                     |
|         | TP (HOJNEW-AND. NOI ADJOLD AND ZBR GE ZDL)ZS(5)=7BR                   |
|         | IF ( NOT ADJNEW AND ADJOLD AND 7BL IT 7DB 75 (5) -7DB                 |
|         | IF(.NOT.ADJNEW, AND. AD. 101 D. AND ZBL CF ZDD/20(3) - 2DR            |
|         | IF (NOT AD INFW AND NOT AD NOT AD NOT COLOR (5) = ZBL                 |
|         | TEC NOT ADDINES AND NOT ADJULD AND CDBCKL)ZS(5)=ZDL                   |
| 330     | Tread and and and and and and and and and a                           |
| 330     | IF (ABLLE)ZS(6)=XL TEST   |
|         | IF (ABRGE)ZS(7)=XRTFST  |
|         | IF (IXI FFT-75(9) IT A)78(A)-THISET                                   |
|         | 75DFL-9   |
|         |   |
|         | 2S(TB)=SEGPT  |
|         | IF (ABBCKL) GO TO 335   |
|         | ZS(10)=7S(9)  |
|         | 75 (9)-55 CPT   |
|         |   |
| <u></u> | 00 10 335   |
| 6       | MAKE A ONE ELEMENT BOX.   |
| 331     | ZS(1)=1   |
|         | 7S(2)=XIFFT   |
|         |   |
|         |   |
|         | I CADJNEW)ZS(4)=ZLEFT   |
|         | IF(.NOT.ADJNEW)7S(A)-7BIGUT   |
|         | IF (AD.INFW)7S(5)-7DIGUT  |
|         |   |
|         | Tr( WOI WDJNEW)ZS(5)=ZLEFT  |
|         | 2S(6)=XLTEST  |
|         | ZS(7)=XRTEST  |
|         | ZS(8)=IXIFFT  |
|         |   |
|         |   |
|         | ZSADJ=ADJNEW  |
|         | ZSDEL=DELNEW  |
| 135     | CONTINIF  |
|         |   |
|         | VDMRE = (NDMADD+1)/2 - Q(1,13) - Q(1,19) - Q(1,20) - NIMPEE           |
|         | 1F(NUMREF GT 0)Q(1 14) = Q(1 14) + NUMREF                             |
|         | IF(NUMADD.GT.20) NUMADD-20  |
|         | IF CNIIMADD IF GANGIMADD I  |
|         |   |
|         | HOUS (NOWADD) = ADDS (NUMADD) + 1                                     |
|         | IT ( NUI DEPTH) GO TO 402   |
|         | SEGPT=NEXT  |
|         | IF(FROM.FQ. 0) GO TO BOL  |
|         | CO TO 304   |
|         | 00 10 384   |
|         |   |

| C<br>350 | INTEREGATE THE ZS BOX<br>Continue  |
|----------|--|
|          | Q(1,13)=Q(1,13)+1  |
|          | IF(25(1)-2.LT.0)GO TO 355<br>IF(SAM(1,1)-SAM(1.2).EQ.0)PAUSE 'STARTET    |
| С        | IF(ZS(1).EQ.2.AND.(ZS(8).GE.SAM(1,2)))GO TO 400<br>SUBDIVISION NECESSARY |
|          | Q(1,4)=Q(1,4)+1  |
|          | SEG(SEGLO+11)=SEGACT   |
|          | SEGACT=SEGOUT<br>Q(1,20)=Q(1,20)+1                                       |
| 351      | Q(1,19)=Q(1,19)+1  |
| C        | SUBDIVIDE IN THE MIDDLE.   |
|          | Q(1, 12) = Q(1, 12) + 1<br>SAM(1, 2) = (SAM(1, 1) + SAM(1, 2)) (0)       |
| C        | GO TO 299  |
| 353      | SAM(1,2)= $ZS(8)$  |
|          | GO TO 299  |

| C    | OUTPUT SEGMENTS   |
|------|---|
| 355  | IF(ZS(1),GT,0)60 TO 359   |
|      | SAM(2.1)=0  |
| 78.0 | Q(1,8)=Q(1,8)+1   |
| 376  | XEND=SAM(1,2)   |
|      | POLYPT=Ø  |
|      | NEX TGO=1   |
| 350  | GO TO 368   |
| 378  | CALL LDLPT(XEND,ZS(6))  |
|      | IF(XEND.EQ.SAM(1,1))G0 TO 360   |
|      | PULYPTEO  |
|      | NEXIGUE2  |
| 360  | G0 10 363   |
|      | POLVET-7C(A)  |
|      | CALL + DIDM(DALLE) =  |
|      | CALL LDLPI(POLYPT,SEG(POLYPT+1))  |
|      | PA(q) = PO(q) + VEND |
|      | NEXTCO-3  |
|      | GO TO 369   |
| 362  | IF (XEND FO SAM(1 ON) OF TO TO  |
|      | GO TO 356   |
| 364  | POLYPT=75(9)  |
|      | CALL LDIPT (POLVPT SEC(POLVPT)  |
|      | PQ(9)=PQ(9)+SAM(1,2)-SAM(1,1)   |
|      | NEXTGO=4  |
|      | GO TO 368   |
| 365  | XEND=SAM(1.2)   |
|      | POLYPT=ZS(10)   |
|      | CALL LDLPT (POLYPT SEG(POLYPTIC)  |
|      | NEXTGO=1  |
|      | IF (FM.EQ.Ø) GO TO 368  |
|      | SAM(2,1)=IX   |
| 0    | SAM(3,1) = SEGPT + 12   |
| 1.00 | OUTPUT A SPECIFIC SEGMENT.  |
| 208  | IF(SEGCNT.EQ.0)GO TO 372  |
|      | IF (POLYPT.NE.PRESEG) GO TO 372   |
|      | SAM(2,1)=0  |
|      | (1,8)=(1,8)=(1,8)+1   |
| 372  | SEGENT-SECONT.  |
| 012  | $P(1   \alpha) = O(1   \alpha)$   |
|      | PRESEG-POLVPT   |
| 374  | VISSEG(SEGENT)-YEND   |
|      | CALL STIPT(POLVPT VICEDOCEDONIC)  |
|      | IF (SAM(2,1), FO (A) CO TO 7755   |
| С    | STORE A SAMPLE POINT  |
|      | Q(1,3)=Q(1,3)+1   |
|      | IF (SAM2S .NE. 0) GO TO 375   |
|      | SAM2S=SAM(3.1)  |
|      | SAM2X=SAM(2.1)  |
|      | SAM2LX=SAM(2.1)   |
|      | SAM2L=SAM(3,1)  |
| 190  | GO TO 3755  |
| 315  | IF (SAM(2, 1) . LE. SAM2LX) GO TO 3755  |
|      | SAMZLX=SAM(2,1)   |
|      | CALL STRPT(SAM(3,1),SEG(SAM2L))   |
|      | SAM21 - SAM(2, 1), SEG(SAM2L))  |
| 3755 | SAM(2 1)-0  |
|      | G0 T0 (176 766 760 -  |
| 376  | IF (SAM(1 2) FO FDA 55), NEXTGO   |
|      | GO TO 281   |
|      |   |

| C    | INTERSECTING PLANES CASE.                  |  |
|------|--|--|
| 400  | DEPIH: FALSE .                             |  |
|      | 75(1)-0                                    |  |
|      | Q(1,11) = Q(1,11) + 1                      |  |
|      | SEGPT=75(9)                                |  |
|      | NEXT=-1                                    |  |
| 401  | XLEFT=SEG(SEGPT+3)                         |  |
|      | XRIGHT=SEG(SEGPT+5)                        |  |
|      | ZLEFT=SEG(SEGPT+7)                         |  |
|      | ZRIGHT=SEG(SEGPT+9)                        |  |
|      | NUMREF = $-Q(1, 13) - Q(1, 19) - Q(1, 20)$ |  |
|      | G(1,19)=Q(1,19)+1                          |  |
| 402  | NEX T=NEX T+1                              |  |
|      | SEGPT=7S(10)                               |  |
|      | IF (NEXT.EQ.0) GO TO ANI                   |  |
|      | DEP TH= .TRUE .                            |  |
|      | XX TES T=XAMXL                             |  |
|      | UALL LDLPT(XEND,XXTEST)                    |  |
|      | W(1, 19) = W(1, 19) + 2                    |  |
|      | SEGSAM=75(10)                              |  |
|      | CALL STLPT (75(9) SFGGAM)                  |  |
|      | CALL LDLPT (SEGPT. IMPIST)                 |  |
|      | PREV=Ø                                     |  |
| 4010 | IF (SEGPT.EQ.0) GO TO 4030                 |  |
|      | Q(1,19) = Q(1,19) + 1                      |  |
|      | TECSEGSEM NE GEOGRAPHICA                   |  |
|      | IF (BEUSAND NE SEG(SEGPT+1)) GO TO 4020    |  |
|      | IF (PREV. NE. Ø)SEG(PREV) - NEVT           |  |
|      | SEG(SEGPT+4)=XXTEST-SEG(SEGPT+3)           |  |
|      | SEG(SEGPT+3)=XXTEST                        |  |
|      | CALL LDLPT(IX,SEG(SEGPT+3)+SEG(SEGPT+4))   |  |
|      | IF (IX.LE.Ø.OR.IX.GT.FRAMEX) GO TO 4040    |  |
|      | GO TO 3001                                 |  |
| 4020 | PREV=SEGPT                                 |  |
|      | SEGPTENEXT                                 |  |
|      | GO TO 4010                                 |  |
| 4030 | IF(IY.EQ.FRAMEY-1)GO TO 364                |  |
|      | CALL GETBLK(SEGPT)                         |  |
|      | w(1,23)=w(1,23)+1                          |  |
|      |  |  |
|      | IF (PQ(3), GT_PQ(2))PQ(2)-PQ(7)            |  |
|      | SEG(SEGPT+1)=SEGSAM                        |  |
|      | SEG(SEGPT+2)=IY-FRAMEY+1                   |  |
|      | SEG(SEGPT+11)=-1                           |  |
|      | SEG(SEGPT+3)=XXTEST                        |  |
|      | CALL LDRPT(SEG(SEGPT), IMPLST)             |  |
|      | GO TO SCA                                  |  |
| 4040 | CALL RETRIK(SECRT)                         |  |
|      | PQ(3)=PQ(3)=1                              |  |
|      | Q(1,24)=Q(1,24)+1                          |  |
|      | GO TO 364                                  |  |
|      |  |  |

| 498  | CONTINUE  |
|------|---|
|      | DO 499 I=1.01                                       |
|      | Q(10, 1) = Q(10, 1) + Q(1, 1)                       |
|      | Q(3,T) = Q(1,T) = Q(7,T)                            |
|      | $IF(Q(2, T) \mid T \mid Q(3, T))$                   |
|      | P(B, I) = O(1, I) = Q(3, I) = Q(3, I)               |
| 499  | TF(0(7, T) + T, 0(8, I))                            |
|      | IF(IV, GT, FDAMG(8, I))Q(7, I)=Q(8, I)              |
|      | TE (PTY NE GAMEY) GO TO 500                         |
|      | LE CE CONT WE ADUALL SHOW                           |
|      | PQ(10) = PQ(10) + 1                                 |
| 500  |   |
| 200  |   |
|      |   |
|      | Q(3,1)=Q(1,1)/FRAMEY                                |
| 501  | Q(6,1)=10***9/(30**Q(1,1))                          |
| 201  | Q(8,1)=Q(1,1)/YQ(17)                                |
|      | DU 502 I=13,QL                                      |
| 5.00 | PQ(11) = PQ(11) + Q(9.1)                            |
| 202  | PQ(13)=PQ(13)+Q(10,1)                               |
|      | PQ(12)=10.**9/(30.*PQ(11))                          |
|      | PQ(14)=10.**9/(30.*PQ(13))                          |
|      | PQ(15)=PQ(11)+PQ(13)                                |
|      | PQ(16)=10.**9/(30.*PQ(15))                          |
|      | IF (STAT.EQ.Ø) RETURN                               |
|      | TYPE 5002. (J. ADDS (.1) 1-1 20)                    |
|      | TYPE 5001. (J. PQ(J) J=1. POL)                      |
|      | TYPE 5000 (J. (Q(1,1), 1-1, 10) 1-1 01)             |
|      | RETURN  |
| 5001 | FORMAT(' PQ(',12,')=',16 ()                         |
| 5000 | FORMAT( Q(X, T2, T) - TC ATA IN TO TA               |
| 5002 | FORMAT( ADDS / 5( - , 10, 414, 1X, 19, 214, 216, /) |
|      | FND (,12, )= ,16)./)                                |

## APPENDIX II

88.

# STATISTICS OF OBJECTS AND ALGORITHMS

At the beginning of each set of statistics for a particular program there is a description of each of the counters. Following each description, a set of statistics for each of the ten test objects is compiled.

For a copy of the complete listing write to:

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