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STRESS AND STRAIN DISTRIBUTION IN THE VICINITY OF INTERFERENCE FIT FASTENERS

MERLE ALLEN J. A. ELLIS

GENERAL DYNAMICS/CONVAIR AEROSPACE DIVISION

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FOREWORD

This report was prepared by General Dynamics, Convair Aerospace Division, Fort Worth Operation, Post Office Box 748, Fort Worth, Texas 76101, under United States Air Force contract F33615-73-C-3026. The contract was initiated under Project No. 1467, "Structural Analysis Methods," Task. No. 146702, "Thermal Elastic Analysis Methods." The program was administered by the Air Force Flight Dynamics Laboratory (AFFDL). Mr. Gene E. Maddux, AFFDL/FBR, was the Froject Engineer. The analysis reported was performed during the period 29 August 1972 to 20 October 1972 under the direction of Mr. Merle G. Allen of the Structural Dynamics Group, Structures and Materials Technology Section, Structures and Design Department. The manuscript was released by the authors in November 1972 for publication as an AFFDL Technical Report.

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This technical report has been reviewed and is approved.

FRANCIS J. JANIK, JR Chief, Solid Mechanics Branch Structures Division

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ABSTRACT

A body of detailed stress and strain distributions in the vicinity of interference fit fasteners has been analytically obtained and is presented. These data, obtained on simple installations, present trends which may be used by designers in determining how or whether to use interference fit fasteners.

The analysis was performed with a finite element digital procedure which has the nonlinear constitutive behavior programmed and interrelates internal loading and deformations. Preparations for the analysis of thirty six conditions included analyzing a test article for which good correlations are shown.

Stress and strain distributions are presented for conditions which include two fastener hole sizes, two levels of interference fit, three plate materials (steel, titanium and aluminum) and three levels of uniaxial loading.

The results indicate that the radial strains in that part of the plate which is strained beyond the yield point are sensitive to the value of plastic modulus of the material. Also, the fastener diameters may be any size provided that the insertion is adjusted accordingly.

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SECTION I

INTRODUCTION

The use of interference fit fasteners in airplane construction extends back prior to World War II days when tapered pins were used in push-pull tubes. In the early 1960 time frame, their use was incorporated into numerous types of joints on several aircraft types. As in-service experience was accumulated and the benefits to be gained were experimentally verified, their usage rate grew until the present where virtually all large aircraft manufactured in this country and abroad incorporate interference fit fasteners. As an example, the F-111 uses approximately 8500 per ship in sizes up to one-half inch diameter and the C-5A uses approximately 700,000 in sizes up to seven sixteenths inch diameter. Available documentation indicates the Concorde uses in excess of 100,000 in sizes up to one-half inch.

The benefits for ductile joint materials is primarily extension of fatigue life. Emphasis is placed on ductile because if the material is brittle, the prestress due to the interference fit can cause failure. Other benefits include a more uniform distribution of stress throughout the joint and elimination of fastener free play. The disadvantages include increased costs of hole preparation and quality control.

The increase in use of interference fit fasteners is due nearly entirely to confidence in the application generated by empirical evidence and not to any appreciable extent to analytical considerations. The lag of analytical treatment behind experimental data is due to the complexity of the basic load deflection interactions and to the fact that effective interference fits strain the joint material into the inelastic range.

The purpose of this report is to help fill the analysis void by presenting a body of data for interference fit fasteners analytically obtained. The data consists of stress and strain distributions in a plate in the vicinity of a fastener. In the analysis, no load is reacted through the joint and the plate is large enough (five by eight inches, 0.10 inch thick with the hole centered) that it may be considered infinite for all practical purposes.

Thirty-six conditions have been analyzed. These consist of using three materials for the plate (while holding the fastener material constant), two hole sizes, two levels of interference and three static loads on the plate. The plate materials were aluminum (2024-T851), titanium (annealed 6A1-4V) and steel (D6ac heat treated to 220-240 psi). The fastener material was 5 Cr-Mo-V steel. Hole sizes were one-fourth (1/4) and three-eights (3/8) inch diameters. The load conditions were interference fit only, interference fit plus an applied uniaxial load resulting in a gross area stress of thirty-five percent of yield and interference fit plus an applied uniaxial load resulting in a gross area stress of seventy percent of yield. (An exception occurred with the titanium plate with the lower level of interference because the plate separated from the bolt when the seventy percent uniaxial load was applied. Hence, the load was reduced to fifty percent to avoid separation.) The two levels of interference were such that if the bolt did not deform and all the deformation occurred in the plate. the tangential strains at the hole interface would have been 0.010 and 0.020 inch per inch. Because the bolt does deform, the plate strains were somewhat less. However, it will be shown by the data that most of the total deformation occurs in the plate.

The analysis methods used are briefly discussed in Section II. These methods have been applied to a test specimen on which test results were available and the analyses/test results are compared in Section III. Section IV contains details of the production conditions and Section V contains conclusions and recommendations. The body of analysis results is presented in the Appendices I, II and III for the aluminum, titanium and steel plates, respectively. Each appendix contains 176 figures. Because of this large quantity, they are not included in the list of figures. Instead, figure indexes are supplied on foldouts following the appendices. It is believed these indices will be more convenient for the reader interested in details, since otherwise approximately 50 pages would have been required just to list the figures.

SECTION II

ANALYSIS METHOD

An automated finite element digital procedure has been used to perform the analysis reported herein. This section only summarizes the method since it is presented in reterence 1. However, a finite element has been added to those available so it is discussed and the technique used to obtain the interference using finite elements is presented.

The nonlinear constitutive behavior, a dominant feature of the interference fit fastener systems, is a basic part of the input data. This nonlinear behavior is programmed into each element so that the element stiffness is a function of the state of strain and the load-deflection relationship is nonlinear and interdependent. Proportional loading is used in the subject method, consistent with its contemporaries, and the accuracy of the results is controllable by using more load increments at the expense of more computations.

The primary difference in this procedure and its contemporaries is that the latter usually solve linear equations for each load increment (piecewise linear approach), modifying the element stiffnesses after each step. The subject procedure casts the equations in differential form and integrates numerically for each load increment. The equations are of first order and are nonlinear and ordinary. The fourth order Range-Kutta scheme with Simpson rule coefficients is used for integration to obtain deflections.

For the biaxially stressed element, the concept of isotropic hardening and a generalized stress are used to evaluate an effective modulus and Poisson's ratio, which vary continuously from their initial values during elastic straining action to their asymptotic values during intense plastic straining action. The surface of plasticity for the element closely approximates the von Mises surface when the generalized stress is set equal to the von Mises stress and the strain distribution is essentially identical to that obtained by the Prandtl-Reuss incremental flow theory.

The principle finite element used for the analysis reported herein was a quadrilateral membrane composed of four constant stress (linear deformation) type triangular elements. The four triangles are assembled as indicated in Figure II-1 to form the quadrilateral. The displacement degrees of freedom for the



The element stress of each of the four constant stress triangles is calculated and then averaged to obtain the quad plate element stress.

Figure II-1 Quadrilateral Membrane Finite Element from an Assembly of Four Triangular Elements center grid are automatically eliminated from the stiffness matrix for the quadrilateral element before it is added to the structure matrix.

After calculating deflections for each load increment, the element strains are easily obtained. Secant properties are then used to calculate element stresses. Quadrilateral element stresses are obtained by averaging the four triangular element stresses.

In applying finite elements to the analysis of interference fit fastener systems, a problem arises in appropriately representing the interference. Prestress or predeformations cannot be used. The former cannot be used because the distribution of interference between the plate and bolt is unknown before the analysis is performed. The latter cannot be used because the bolt and plate must be allowed to deform as the plate is loaded uniaxially.

This problem has been overcome by replacing the bolt with an internally pressurized ring. The elastic stiffness of the ring was adjusted to be the same as the bolt which it replaced. Under the action of uniaxial load the plate hole tends to become oval but the bolt inside the hole tends to keep it round. Replacing the bolt with the ring allows the bolt effects on the plate to be retained while also allowing the ring to be pressurized internally to produce the desired interference. This analysis predicts the effects of the bolt on the plate (not the plate on the bolt). Hence, this approximation is considered satisfactory.

The relationship used for the cylinder modulus was

$$\overline{E} = \frac{E}{(1-2\nu)(1+\nu)} \quad \left(\frac{a^2 + r^2}{r^2 - a^2} - \nu\right)$$
(II-1)

where E is the bolt modulus

- v is Poisson's ratio
- a is the inner cylinder radius
- r is the hole radius

Equation II-1 was derived by considering the bolt as being approximated by a solid disk in plain strain. The elastic stiffness of this disk is presented in reference 2, page 282. The stiffness of a ring in plain stress is presented in reference 3, page 57. The solid disk stiffness and ring stiffness were set equal to produce the results in equation II-1 above. The pressure inside the ring, required to produce the desired interference, is

$$P = \frac{r^2 - a^2}{2a^2r} \quad \overline{E} \quad \overline{U} \tag{II-2}$$

where \overline{U} is the desired radial interference. This expression was also obtained from reference 3, page 56.

SECTION III

ANALYSIS CREDIBILITY

At the initiation of the analysis task, a test program had made available a small amount of data consisting of strains in a round plate with an interference fit fastener in the center. Therefore, this test specimen became the subject of a finite element analysis as a first step in determining the required grid density and value of other parameters necessary to yield engineering accuracy.

The test specimen consisted of a round plate eight inches in diameter with a three-eighth inch hole in the center. The plate was 0.25 inch thick and fabricated from D6ac steel heat treated to 220/240 ksi. Two finite element patterns (Figures III-1 and III-2) were used for analysis. Advantage was taken of the symmetry conditions and only one quadrant was represented; hence, the tangential deformations along each radial edge were constrained. Note that in both idealizations (one element per 15 degrees, Figure III-1 and one element per 10 degrees, Figure III-2) there are two bands of finite elements inside the hole. These two bands represent the ring replacing the steel fastener as discussed in Section II. Pressure was applied as mechanical loads at the inside grid ring inside the bolt and caused the bolt to expand which stressed the plate.

For a trial condition, an interference fit consisting of 0.35 inch bolt insertion was used for both idealizations and analysis was performed. For the integration, four load increments (50, 75, 90 and 100 percent) were used in order to insure accuracy. The value of plastic modulus was very small, being 30,000 psi. The resulting bolt hole radial deformation was the same for both idealizations, being 0.00320 inch. Since the total radial interference was 0.00365 inch, approximately 88 percent of the total was absorbed by the plate. This corresponds to 67 percent for the elastic case which may be obtained analytically from the expressions on pages 57 and 58 of reference 3.

The results of using both element patterns are presented in Table III-1. Any differences in the two are insignificant.



Figure III-1 Idealization of Test Specimen with Finite Elements at 15 Degrees



Figure III-2 Idealization of Test Specimen with Finite Elements at 10 Degrees

Finite Element Analysis Results for Idealizations Using Elements 10 and 15 Degrees Wide Table III-1

1 Stresses h2x10-3)	15 Degrees	-45	92	55	33	20	12	
Tangentia (Lbs/inc)	10 Degrees	-45	16	55	33	20	12	
Stresses ch ² x10 ⁻³)	15 Degrees	-242	-88	-53	-32	-19	-11	
Radial (Lbs/in	10 Degrees	-242	-88	-53	-32	-19	-11	
1 Strains 10 ³	15 Degrees	10.7	4.08	2.45	1.48	0.891	0.539	
Tangentia x	10 Degrees	10.7	4.07	2.45	1.47	0.889	0.538	
Strains 3	15 Degrees	-35.7	-4.00	-2.39	-1.43	0.857	-0.511	
Radial Sul	10 Degrees	-35.5	-4.00	-2.39	-1.43	-0.855	-0.510	
Radius	1n Inches	0.21475	0.27715	0.35765	0.46150	0.59555	0.76855	
lement	15 Degrees	13-18	19-24	25-30	31-36	37-42	43-48	
Finite E Numb	10 Degrees	19-27	28-36	37-45	46-54	55-63	64-72	

Next. the two inside bands of elements in the plate. adjacent to the hole, were replaced with four bands in both the 10 and 15 degree grid patterns. This refined the grid pattern in and adjacent to the plastic zone. The same four load increments and plastic modulus were used as before. Again, the results were the same for both the 10 and 15 degree simulations and the radial deformation was insignificantly lower. being 0.00319 inches. The radial and tangential strains resulting from the coarse and refined grids are plotted for comparison in Figure III-3. It will be noted that the plate strains in the plastic zone resulting from the refined grid are slightly lower than those from the coarse grid. Using the radius and radial deformation the tangential strain at the edge of the hole may be calculated as 0.0171 inch per inch. This point may be added to Figure III-3 and either set of finite element calculated tangential strains extrapolated to it. (This has not been done in the subject illustration.)

Since the 15 degree grid pattern was as accurate as the 10 degree pattern and yet was more economical to compute, the 10 degree pattern was discarded at this point.

Two parameters were then explored consisting of the number of load increments and the non-linear stress-strain curve relationship as defined analytically. In addition to the four load increments, previously defined, six increments (60, 75, 85, 90, 95 and 100 percent) were used. The use of six increments did not change the results. This implied that perhaps one increment (100 percent) would also produce accurate answers and be computationally more economical. One load increment was then used and the same results were obtained as for the cases using four and six. Hence, one load increment was used for all subsequent conditions including the production conditions.

The non-linear stress-strain curve is defined analytically through use of a parameter n (Reference 1). Its effect, and correlation with the material characteristics, is illustrated in Figure III-4. As may be seen from the figure, the higher values of n correlate more closely with the material characteristics. However, it was discovered that using values above five would cause some slight unbalances to occur across those finite elements which occupy the plastic zone surrounding the hole. Using a value of ten caused an unbalance in the radial direction of approximately three percent of the applied load. (Equilibrium was satisfied in the tangential direction.)



Figure III-3 Finite Element Calculated Strains for Coarse and Refined Grids



Figure III-4 Effect of Parameter n on Stress -Strain Curve for D-6ac Steel at Room Temperature

Since computation was being performed in single precision on an IBM system, a temporary change to double precision was made. The same unbalances were obtained in double precision for the higher values of n. (These unbalances are now attributed to the sharpness of the "corner" of the stress-strain curve.)

Because equilibrium was satisfied when a value of five was used and no strains were expected in the vicinity of the "corner", the value of five for n was selected and used for all subsequent analysis. Double precision was used for a small number of production conditions until the change could be made to single precision in which most of the production analyses were performed.

Two test conditions were then selected for analysis; a bolt insertion of 0.45 and 0.30 inches, because these corresponded rather closely with the parameters to be used in the production cases. The testing, on the eight inch diameter plate previously discussed, had been performed using strain gages and also using grid lines. The strain gages had been installed along 90 degree radial lines, with two rows for tangential strains 90 degrees apart and two rows for radial strains also 90 degrees apart. In the grid line method, a copper strip was plated on the disc and scribed. Only radial deformations are measured using grid lines and tangential strains are then calculated by dividing by the radial distance.

The experimental tangential strains resulting from a bolt insertion of 0.45 inch are shown in Figure III-5. Three finite element analysis results are superimposed for comparison. The first analysis results were obtained by analytically calculating the pressure as indicated in Section II. This resulted in a plate radial deformation of 0.00414 inches or about 88 percent of the total. The grid line test had indicated that the radial deformation was only 0.00350 inches. Because of this, the bolt pressure was linearly reduced with the results that the calculated radial deformation was 0.00367 inches. For both these analyses conditions, 3×10^6 was used for the value of plastic modulus. In order to determine the effects of the plastic modulus and also because no good definition of plastic modulus could be found for D6ac steel, a third computation was made using 6 x 10^6 . This resulted in a calculated plate hole radial deformation of 0.00356 inches. These three analyses results are shown in Figure III-5.





Test results obtained from strain gages for both tangential and radial strains resulting from a bolt insertion of 0.45 inches are shown in Figure III-6. These are compared with calculated results from the latter two conditions described above. Note that the level of plastic strain has a pronounced effect on the calculated radial deformations in the plastic zone with the higher value correlating more closely with test. It should be indicated that the hole radial deformation from this test was 0.00333 inch. This deformation was obtained by extrapolating to the hole edge the tangential strains obtained from strain gages and multiplying by the hole radius. This consideration makes the analysis/test comparison even more favorable.

Test results from both strain gages and grid lines for a 0.30 bolt insertion are shown in Figure III-7. Analysis results are superimposed for comparison. The calculated hole deformation was 0.00214 inch; in comparison to 0.00202 inch obtained by extrapolating both the grid line and strain gage data as in the case for 0.45 insertion.

After performing the above described analyses and viewing the analyses/test comparisons, the analytical approach was deemed qualified to predict trends which was the objective of the production conditions.



Figure III-6 Analysis/Test Comparison of Radial and Tangential Strains for 0.45-Inch Bolt Insertion



Figure III-7 Analysis/Test Comparison of Radial and Tangential Strains for 0.30 Inch Bolt Insertion

SECTION IV

DISCUSSION OF PRODUCTION CONDITIONS

The analysis subject for the production conditions was a rectangular plate measuring five by eight inches of 0.10 inch gage. Two finite element representations were used because of the two bolt hole sizes. Figure IV-1 shows the representation used for the plate with the 3/8 inch diameter hole and Figure IV-2 shows the representation used for the plate with the 1/4 inch diameter hole. One fourth of the plate is included in the representations which takes advantage of the double symmetry condition. The plate was constrained against longitudinal translation by fixing those longitudinal coordinates along the centerline which forms the bottom edge of the quadrant in Figures IV-1 and IV-2. Lateral translation was constrained along the centerline forming the left edge of the quadrant in the subject figures.

The one element per 15 degree arrangement which proved satisfactory in Section III was reused in this representation. Also, the aspect ratio of the quadrilateral elements surrounding the hole are essentially unchanged. These dimensions were selected because the resulting stresses and strains are nearly the same as in an infinite plate, yet the plate lends itself to modeling with finite elements. Also, the dimensions will allow economical testing by any interested individual.

Because of the voluminous nature of the analyses results, they are presented in the appendices. The presented data consists of stresses and strains in numerical and contour form, both prepared by the Stromberg-Carlson 4020 plotter. The numerical form consists of printing the numerical level of the stress or strain on each finite element in the representation. The contours consist of isolines which represent constant levels of stress or strain. Because the highest stress and strain levels and gradients occur in the vicinity of the fastener only that region adjacent to the fastener is included in the plots. For the plate with the 3/8 inch hole, a region extending from the hole edge to a radial distance of 1.442 inches from the hole center is included for the plots. This region is illustrated in Figures IV-1 and IV-3, the latter of which identifies the finite elements by number. The region of the plate surrounding the 1/4 inch hole measures 0.866 inch radially from the hole center and is illustrated in Figures IV-2 and IV-4.



Figure IV-1 Finite Element Representation Used for the Plate with 3/8 Inch Diameter Hole



Figure IV-2 Finite Element Representation Used for the Plate with 1/4 Inch Diameter Hole



Figure IV-3 Region of Plate Surrounding the 3/8 Inch Hole Used to Present Stresses and Strains



Figure IV-4

Region of Plate Surrounding the 1/4 Inch Hole Used to Present Stresses and Strains

A total of thirty-six conditions have been analyzed, twelve each for aluminum, titanium and steel. For all cases a steel bolt was used. The conditions are defined and numbered for the aluminum plate in Table IV-1. In the table, the diametral interference is total, being the sum of change in diameter of the bolt and plate due to the interference.

The condition numbers for titanium and steel are the same as aluminum except that the letter designation is changed to "T" and "S", respectively. Also, a uniaxial load of 50 percent of gross area yield was used for the titanium plate at the lower levels of interference fit in lieu of the 70 percent because the latter was sufficient to cause separation of the bolt and plate.

The applied uniaxial load was measured as a percent of that gross area stress which would cause yielding to occur in a plate without a hole. The yield point was defined as 50,000 psi stress for aluminum, 210,000 psi stress for steel and 130,000 psi stress for titanium. For all plates, the uniaxial load was applied in a direction parallel to the longitudinal axis and distributed evenly as an edge force along the width.

The uniaxial stress-strain curves used for aluminum and steel are shown in Figures IV-5 and IV-6, respectively. The uniaxial stress-strain curve used for titanium was taken from Reference 4, page 5-85. The value of Poisson's ratio used for each of the three materials was 0.33 for aluminum, 0.31 for titanium, and 0.32 for steel. These values were all obtained from Reference 4, pages 3-44, 5-75, and 2-12, respectively.

The plate hole deformations as a result of the interference fit and applied uniaxial load are computed as a part of the analysis. These deformations are shown in Tables IV-2, IV-3 and IV-4 for the aluminum, titanium and steel conditions, respectively. The grid points at which the deformations were calculated are illustrated in Figure IV-7.

Appendices I, II and III present the results for the aluminum, titanium and steel plates, respectively. Following the appendices is an index of figures for the appendix contents.

Condition Number*	Hole Diameter	Diametral Interference	Uniaxial Load
	(Inches)	(Inches)	(Percent of Yield)
Al	3/8	0.00375	0
A2	3/8	0.00375	35
A3	3/8	0.00375	70**
A4	3/8	0.00750	0
A5	3/8	0.00750	35
A6	3/8	0.00750	70
A7	1/4	0.00250	0
A8	1/4	0.00250	35
A9	1/4	0.00250	70**
A10	1/4	0.00500	0
A11	1/4	0.00500	35
A12	1/4	0.00500	70

Table IV-1Definition of Analysis Conditionsfor Aluminum Plate

* The numerical part of the condition number is the same for all materials; the letter part is "A" for aluminum, "S" for steel and "T" for titanium.

** A uniaxial load of 50 percent was used for this condition for the titanium plate because at the 70 percent level the plate separated from the bolt.



Figure IV-5 Typical Compression Stress-Strain Curve at Room Temperature for 2024-T851 Aluminum Alloy Plate



Figure IV-6 Typical Compression Stress-Strain Curve at Room Temperature for D-6ac Steel Forgings (Longitudinal)
	Node 7	0 .00172	0 •00185	0 .00201	0 • 00357	0 • 00366	0 •00376	0 .00107	0.00115	0 .00124	0 .00221	0 • 00226	0 •00232
	Node 6	.00044	.00045	.00046	.00092	.00093	.00093 .00363	.00028	.00028	.00029	.00058 .00214	.00058 .00218	.00059
ctions	Node 5	.00087	.00087	.00088 .00169	.00180	.00181	.00182	.00054 .00092	.00054 .00097	.00055	.00190	.00112	.00112
ole Defle	Node 4	.00122	.00121	.00120 .00133	.00254 .00254	.00253	.00253	.00075	.00074 .00078	•00074 00082	.00156	.00155	.00155
um Plate H	Node 3	.00149	.00145 .00089	.00140	.00311	.00308	.00305 .00183	.00092 .00054	.00089 .00055	。00087 。00056	.00191	.00189	.00188
Aluminu	Node 2	.00167 .00044	.00159	.00151 .00045	.00346	.00341 .00092	.00337	.00103 .00028	00099 00028	.00094 .00028	.00214	.00058	.00209
ble IV-2	Node 1	.00172 0	. 00164 0	.00154 0	•00357 0	.00352 0	• 00347 0	.00107 0	.00102 0	0 0	.00221 0	.00218 0	.00215 0
Ta	DIRECTION	×	х У	× v	X Y	× Y	х У	×	x y	х	х	х У	хv
	COND. NO.	Al	A2	A3	A4	A5	A6	A7	A8	A9	A10	A11	A12

lectio
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IV-2
le

	Node 7	0 .00163	0 .00197	0 .00213	0 • 00345	0 • 00360	0 • 00400	0 .00101	0 。00122	0 .00131	0 •00213	0 •00223	0 .00248
	Node 6	.00042	.00044 .00189	.00045 .00203	.00089 .00334	.00088 .00348	.00091 .00385	.00027 .00098	.00028	.00028	.00056	.00056 .00216	.00057
	Node 5	.00082	.00084	.00085	.00174	.00173	.00176	.00051	.00052	.00053	.00107 .00183	.00107 .00192	.00109
	Node 4	.00116	.00112	.00111	.00245 .00245	.00243	.00241	.00071	.00070	00069 00083	.00150	.00148	.00148
	Node 3	.00142	.00131	.00126	.00300	.00296	.00284	.00088	.00081	.00079	.00183	.00180	.00174
	Node 2	.00158	.00140	.00132	.00334	.00328	.00307	.00098	.00088	.00083	.00206	.00201	.00189
	Node 1	.00163 0	.00143 0	.00133 0	.00345 0	.00337 0	.00312 0	.00101 0	• 00089 0	• 00084 0	.00231 0	.00207 0	.00194 0
•	DIRECTION	x Y	x Y	х	у	x y	х У	X Y	X Y	х У	хх	x Y	××
	COND. NO.	71	T 2	T 3	74	T5	Т6	Т7	T8	T9	T10	TII	T12

Table IV-3 Titanium Plate Hole Deflections

IRECTION	Table IV-4 Node 1 Nod	Steel de 2	Node 3	Node 4	Node 5	Node 6	Node 7
x .00148 .001 y 0 .000	10	43	.00129	.00105	.00075	.00038	0 .00148
x .00125 .001 y 0 .000	20	124	.00116	.00101	.00075	.00040	0.00191
x .00099 .00 y 0	0	101 044	.00103	.00098	.00078 .00194	.00043	0 .00241
x .00315 .00 y 00 .00	C -	305 081	.00274 .00159	.00223	.00159	.00081	0 .00314
x .00296 .00 y 00 .00		1289 1084	.00264	.00220	.00160	.00083	0.00352
x .00271 .00 y 00 .00	0-	268 086	.00253	.00219	.00163 .00336	.00085	0 • 00401
x .00093 .00 y 00 .00	0	090 024	.00080	.00065	.00046	.00024	0 • 00092
ж .00079 .00 у 00 .00	0	078 026	.00072	.00063	.00047	.00025	0.00119
ж .00063 .00 у 00 .00	0	064 028	.00065	.00061	.00049	.00027	0 • 00149
x .00196 .00 y 0 .00	01	189 051	.00169	.00138	.00098	.00051	0 .00195
x .00184 .00 y 00 .00	0-	180	.00163	.00136 .00148	.00099	.00052	0 •00218
ж .00170 .00 у 00 .00	5	168	.00156	.00135	.00101	.00053 .00238	0 • 00248

Daflactione (---F 1



Figure IV-7



SECTION V

CONCLUSIONS AND RECOMMENDATIONS

A body of data has been generated and is presented. The data consists of stress and strain distributions in the vicinity of interference fit fasteners with and without uniaxial load applied. The resulting trends may be used as guide line information for designers in deciding whether or how to use interference fit fasteners on new aircraft structural systems. Analysis and test strains have been favorably compared in Section III for the case of interference fit without uniaxial load. These Section III results should increase the confidence level of the designer in using both the trends and levels predicted in the body of data.

The Section III results indicate that varying the numerical level of the plastic modulus of the material has a pronounced effect on the radial strains in that region of the material stressed beyond the yield point. (The terminology "plastic modulus" is used here to indicate the slope of that part of the uniaxial stress-strain curve which is beyond the yield zone.) Increasing the plate plastic modulus has the effect of stiffening that part of the plate which is strained beyond the elastic range. For a prescribed level of interference, the stiffened plate will be deformed less (than the unstiffened plate) and the bolt more with the changes in each being negligibly small. The radial deformations (u) and tangential strains (u/r) in the plate are thus essentially unchanged at the hole edge. Because the "plastic" portion of the structure is stiffened, the radial strains in that area are reduced which, in turn, increases the radial and tangential strains in the elastic portion. The values of plastic modulus used to produce the results presented in this report are representative of the specified materials; however, plastic modulus values can vary widely for different members of the same family of materials.

For all analysis conditions, two fastener hole sizes were used; 1/4 and 3/8 inch diameter. However, the bolt insertion length was adjusted so that if the bolt had been rigid and all the work due to insertion had deformed the plate, the plate tangential strains at the hole edge would have been 0.010 and 0.020 inch per inch for the two interference levels used regardless of the hole size. The resulting stresses and strains in the plates for the same conditions, except differing hole sizes, are essentially the same. These results show that the hole diameter may be varied within any practical range for the joint without changing the stresses or strains if the insertion is adjusted accordingly.

For all the analysis reported herein, the bolt was replaced with a ring which had equivalent elastic spring stiffness. The ring was then pressurized to produce the interference effect. For interference fit only, the pressure inside the plate hole would have been sufficient since this is what the plate "feels" from the bolt. However, under the effects of uniaxial load, the ring stiffness is required inside the hole because the pressure exerted by the bolt varies around the circumference as the hole changes to an elliptical shape.

To calculate the equivalent ring stiffness, the bolt was assumed to be in plain strain. This produced a ring which was slightly too stiff. A plain stress assumption could have been made for the bolt but this would have produced a ring too flexible because the bolt is in a three dimensional state of stress which is neither plain strain nor plain stress but is in between. In using the slightly too stiff ring, the plate always absorbed a slightly larger percentage of the total interference than the test results indicated (documented in Section III). This means that the analysis used more "effective" insertion and is the primary reason for including the hole deflections in this report (Tables IV-2, IV-3 and IV-4). It also means that for the plate under uniaxial load, the analysis should predict a plate hole slightly more "rounded" than tests would predict.

Three recommendations are made. For any future analyses, the ring stiffness should be adjusted slightly downward by tempering with test results and/or first performing a three dimensional analysis of the bolt to determine its radial stiffness under pressure. Two dimensional analyses of interference fit fasteners should be performed to determine edge effects and effects of transferring load through the fastener. This latter is actually a three dimensional problem but a large number of three dimensional conditions would be prohibitively expensive. The two dimensional analysis is relatively cost effective and would produce good approximations for thin gage materials.

APPENDIX I

ALUMINUM PLATE RESULTS

This appendix presents the results of the finite element analysis for the aluminum plate with the steel bolt inserted. The results consist of stresses and strains in the vicinity of interference fit fasteners. The analysis conditions are discussed in Section IV and Figures IV-3 and IV-4 illustrate the regions of the plates for which results are presented.

The figures are presented in pairs. The first consists of a numerical level of stress or strain superimposed on each finite element. The second consists of isolines or contours representing constant levels of stress or strain. Results are presented in the same sequence as the analysis conditions Al through Al2, defined in Table IV-1. Radial and tangential stresses and strains are presented for each condition. For those cases where no uniaxial load is applied, these stresses are the principal stresses, hence, no other data is presented. For those cases where uniaxial load is applied, radial-tangential shear strains are presented plus other stresses consisting of radial-tangential shear stress, and the three principal stresses; first, second and shear. The figures are otherwise selfexplanatory.

Note: The numbers printed for stress and strain have been truncated back (as opposed to rounded off). The printed stresses are in units of 1000 pounds/inch squared; the printed strains are in units of 0.001 inches/inch. The numbers should be interpreted as being representative of the level at the element center. Negative stresses and strains are compressive, positive stresses and strains are tensile.



Figure AI-1 Radial Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AI-2 Radial Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AI-3 Tangential Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AI-4 Tangential Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AI-5 Radial Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Figure AI-6 Radial Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Figure AI-7 Tangential Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Figure AI-8

Tangential Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Figure AI-9 Radial Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-10 Radial Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference, 35% Uniaxial Load



Figure AI-11 Tangential Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-12 Tangential Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-13 Radial-Tangential Shear Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-14 Radial-Tangential Shear Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-15 Radial Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-16

Radial Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-17 Tangential Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-18 Tangential Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-19 Radial-Tangential Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-20 Radial-Tangential Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-21 First Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-22 First Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-23 Second Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-24 Second Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-25 Principal Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-26 Principal Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AI-27 Radial Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-28 Radial Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-29 Tangential Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load


Figure AI-30 Tangential Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-31 Radial-Tangential Shear Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-32 Radial-Tangential Shear Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-33 Radial Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-34 Radial Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-35 Tangential Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-36 Tangential Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-37 Radial-Tangential Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-38 Radial-Tangential Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-39 First Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-40 First Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-41 Second Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-42 Second Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-43 Principal Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-44 Principal Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AI-45 Radial Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-46 Radial Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-47 Tangential Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-48 Tangential Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-49 Radial Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-50 Radial Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-51 Tangential Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-52 Tangential Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AI-53 Radial Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-54 Radial Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-55 Tangential Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-56

Tangential Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-57 Radial-Tangential Shear Strain Values for Alumimum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-58 Radial-Tangential Shear Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-59 Radial Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-60

Radial Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-61 Tangential Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-62 Tangential Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-63 Radial-Tangential Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-64 Radial-Tangential Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-65 First Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load


Figure AI-66 First Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-67 Second Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-68 Second Principal Stress Context for Aluminum Plate with 3/16 Inch Hole Radius; 0. . 75 Inch Radial Interference; 35% Uniaxie Load



Figure AI-69 Principal Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-70 Principal Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AI-71 Radial Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-72 Radial Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-73 Tangential Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-74 Tangential Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-75 Radial-Tangential Shear Strain Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-76 Radial-Tangential Shear Strain Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-77 Radial Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-78

Radial Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-79 Tangential Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-80 Tangential Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-81 Radial-Tangential Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-82 Radial-Tangential Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-83 First Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-84 First Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-85 Second Principal Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-86 Second Principal Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-87 Principal Shear Stress Values for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-88 Principal Shear Stress Contours for Aluminum Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AI-89 Radial Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-90 Radial Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-91 Tangential Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-92 Tangential Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-93 Radial Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-94 Radial Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-95 Tangential Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-96 Tangential Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AI-97 Radial Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-98

Radial Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-99 Tangential Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-100

Tangential Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-101 Radial-Tangential Shear Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load


Figure AI-102 Radial-Tangential Shear Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-103

Radial Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-104 Radial Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-105 Tangential Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-106 Tangential Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-107 Radial-Tangential Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-108 Radial-Tangential Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-109 First Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-110 First Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-111 Second Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-112 Second Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-113 Principal Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-114 Principal Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AI-115 Radial Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-116 Radial Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-117 Tangential Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-118 Tangential Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-119 Radial-Tangential Shear Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-120 Radial-Tangential Shear Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-121 Radial Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-122 Radial Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-123 Tangential Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-124 Tangential Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-125 Radial-Tangential Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-126 Radial Tangential Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-127 First Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-128 First Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-129 Second Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-130 Second Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-131 Principal Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-132 Principal Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AI-133 Radial Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-134 Radial Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-135 Tangential Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-136 Tangential Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-137 Radial Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load


Figure AI-138 Radial Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-139 Tangential Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-140 Tangential Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AI-141 Radial Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-142 Radial Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-143 Tangential Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-144 Tangential Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-145 Radial-Tangential Shear Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-146 Radial-Tangential Shear Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-147 Radial Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-148 Radial Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-149 Tangential Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-150 Tangential Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-151 Radial-Tangential Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-152 Radial Tangential Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-153 First Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-154 First Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-155 Second Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-156 Second Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-157 Principal Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-158 Principal Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AI-159 Radial Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-160

Radial Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-161 Tangential Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-162 Tangential Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-163 Radial-Tangential Shear Strain Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-164 Radial-Tangential Shear Strain Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-165 Radial Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-166 Radial Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-167 Tangential Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-168

Tangential Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-169 Radial-Tangential Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-170 Radial-Tangential Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-171 First Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-172 First Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-173 Second Principal Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load


Figure AI-174 Second Principal Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-175 Principal Shear Stress Values for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AI-176

Principal Shear Stress Contours for Aluminum Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load

APPENDIX II

TITANIUM PLATE RESULTS

This appendix presents the results of the finite element analysis for the titanium plate with the steel bolt inserted. The results consist of stresses and strains in the vicinity of interference fit fasteners. The analysis conditions are discussed in Section IV and Figures IV-3 and IV-4 illustrate the regions of the plates for which results are presented.

The figures are presented in pairs. The first consists of a numerical level of stress or strain superimposed on each finite element. The second consists of isolines or contours representing constant levels of stress or strain. Results are presented in the same sequence as the analysis conditions T1 through T12, defined in Table IV-1. Radial and tangential stresses and strains are presented for each condition. For those cases where no uniaxial load is applied, these stresses are the principal stresses. Hence, no other data is presented. For those cases where uniaxial load is applied, radial-tangential shear strains are presented plus other stresses consisting of radial-tangential shear stress, and the three principal stresses; first, second and shear. The figures are otherwise selfexplanatory.

Note: The numbers printed for stress and strain have been truncated back (as opposed to rounded off). Also, the stresses printed are in units of 1000 pounds/inch squared; the strains printed are in units of 0.001 inches/inch. The numbers should be interpreted as being representative of the level at the element center. Negative stresses and strains are compressive, positive stresses and strains are tensile.

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Figure AII-1 Radial Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-2 Radial Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-3 Tangential Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-4 Tangential Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-5 Radial Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-6

Radial Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-7 Tangential Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-8 Tangential Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AII-9 Radial Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-10 Radial Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-11 Tangential Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-12 Tangential Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-13 Radial-Tangential Shear Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-14 Radial-Tangential Shear Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-15 Radial Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-16 Radial Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-17 Tangential Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-18 Tangential Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-19 Radial-Tangential Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-20 Radial-Tangential Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-21 First Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-22 First Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-23 Second Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-24 Second Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-25 Principal Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-26 Principal Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AII-27 Radial Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-28 Radial Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-29 Tangential Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-30 Tangential Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-31 Radial-Tangential Shear Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-32 Radial-Tangential Shear Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load


Figure AII-33 Radial Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-34 Radial Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-35 Tangential Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-36 Tangential Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-37 Radial-Tangential Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-38 Radial-Tangential Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-39 First Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-40 First Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-41 Second Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-42 Second Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-43 Principal Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-44 Principal Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 50% Uniaxial Load



Figure AII-45 Radial Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-46 Radial Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-47 Tangential Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-48 Tangential Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-49 Radial Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-50 Radial Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-51 Tangential Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load

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Figure AII-52 Tangential Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AII-53 Radial Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-54 Radial Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-55 Tangential Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-56 Tangential Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-57 Radial-Tangential Shear Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-58 Radial-Tangential Shear Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-59 Radial Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-60 Radial Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-61 Tangential Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-62 Tangential Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-63 Radial-Tangential Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-64 Radial-Tangential Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-65 First Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-66 First Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-67 Second Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-68 Second Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load


Figure AII-69 Principal Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-70 Principal Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AII-71 Radial Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-72 Radial Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-73 Tangential Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-74 Tangential Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-75 Radial-Tangential Shear Strain Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



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Figure AII-76 Radial-Tangential Shear Strain Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-77 Radial Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-78 Radial Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-79 Tangential Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-80 Tangential Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-81 Radial-Tangential Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-82 Radial-Tangential Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-83 First Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-84 First Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-85 Second Principal Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-86 Second Principal Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-87 Principal Shear Stress Values for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-88 Principal Shear Stress Contours for Titanium Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AII-89 Radial Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AII-90 Radial Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AII-91 Tangential Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference: No Uniaxial Load



Figure AII-92 Tangential Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AII-93 Radial Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AII-94 Radial Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference: No Uniaxial Load



Figure AII-95 Tangential Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AII-96 Tangential Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AII-97 Radial Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-98 Radial Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-99 Tangential Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-100 Tangential Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-101 Radial-Tangential Shear Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-102 Radial-Tangential Shear Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-103 Radial Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-104 Radial Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load


Figure AII-105 Tangential Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-106 Tangential Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-107 Radial-Tangential Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-108 Radial-Tangential Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-109 First Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-110 First Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-111 Second Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-112 Second Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-113 Principal Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-114 Principal Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AII-115 Radial Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-116 Radial Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-117 Tangential Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-118 Tangential Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-119 Radial-Tangential Shear Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-120 Radial-Tangential Shear Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-121 Radial Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-122 Radial Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-123 Tangential Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-124 Tangential Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-125 Radial-Tangential Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-126 Radial Tangential Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-127 First Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-128 First Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-129 Second Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-130 Second Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-131 Principal Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-132 Principal Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 50% Uniaxial Load



Figure AII-133 Radial Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-134 Radial Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-135 Tangential Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-136 Tangential Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-137 Radial Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-138 Radial Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-139 Tangential Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AII-140 Tangential Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load


Figure AII-141 Radial Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-142 Radial Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-143 Tangential Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-144

Tangential Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-145 Radial-Tangential Shear Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-146 Radial-Tangential Shear Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-147 Radial Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-148 Radial Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0,0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-149 Tangential Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-150 Tangential Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-151 Radial-Tangential Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-152 Radial-Tangential Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-153 First Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-154 First Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-155 Second Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-156 Second Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-157 Principal Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-158 Principal Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AII-159 Radial Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-160 Radial Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-161 Tangential Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-162 Tangential Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-163 Radial-Tangential Shear Strain Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-164 Radial-Tangential Shear Strain Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-165 Radial Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-166 Radial Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-167

Tangential Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-168 Tangential Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-169 Radial-Tangential Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-170 Radial-Tangential Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-171 First Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-172 First Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-173 Second Principal Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-174 Second Principal Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-175 Principal Shear Stress Values for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AII-176 Principal Shear Stress Contours for Titanium Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load
APPENDIX III

STEEL PLATE RESULTS

This appendix presents the results of the finite element analysis for the steel plate with the steel bolt inserted. The results consist of stresses and strains in the vicinity of interference fit fasteners. The analysis conditions are discussed in Section IV and Figures IV-3 and IV-4 illustrate the regions of the plates for which results are presented.

The figures are presented in pairs. The first consists of a numerical level of stress or strain superimposed on each finite element. The second consists of isolines or contours representing constant levels of stress or strain. Results are presented in the same sequence as the analysis conditions S1 through S12, defined in Table IV-1. Radial and tangential stresses and strains are presented for each condition. For those cases where no uniaxial load is applied, these stresses are the principal stresses. Hence, no other data is presented. For those cases where uniaxial load is applied, radial-tangential shear strains are presented plus other stresses consisting of radial-tangential shear stress, and the three principal stresses; first, second and shear. The figures are otherwise self-explanatory.

Note: The numbers printed for stress and strain have been truncated back (as opposed to rounded off). Also, the stresses printed are in units of 1000 pounds/inch squared; the strains printed are in units of 0.001 inches/inch. The numbers should be interpreted as being representative of the level at the element center. Negative stresses and strains are compressive, positive stress and strains are tensile.

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Figure AIII-1 Radial Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AIII-2 Radial Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AIII-3 Tangential Strain Values For Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Tangential Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Radial Stress Values for Steel Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Radial Stress Contours for Steel Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Figure AIII-7 Tangential Stress Values for Steel Plate with 3/16 Inch Hole Radius; .001875 Inch Radial Interference; No Uniaxial Load



Figure AIII-8 Tangential Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; No Uniaxial Load



Figure AIII-9 Radial Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial Strain Contours for Steel Plate with 3/16 Inch Hole Radius 0.001875 Inch Radial Interference, 35% Uniaxial Load



Tangential Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-12 Tangential Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial-Tangential Shear Strain Values for Steel Plate with 3/16 Inch Hole Radious; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial-Tangential Shear Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-15 Radial Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Tangential Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Tangential Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial-Tangential Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial-Tangential Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-21 First Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



First Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Second Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference 35% Uniaxial Load



Second Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-25 Principal Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Principal Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 35% Uniaxial Load



Radial Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load

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Radial Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Tangential Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Tangential Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Radial-Tangential Shear Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load

Figure AIII-31



Radial-Tangential Shear Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-33 Radial Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-34 Radial Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Tangential Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load


Figure AIII-36 Tangential Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Radial-Tangential Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-38 Radial-Tangential Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference: 70% Uniaxial Load



First Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



First Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Second Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Second Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Principal Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-44 Principal Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.001875 Inch Radial Interference; 70% Uniaxial Load



Radial Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Radial Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Tangential Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Figure AIII-48 Tangential Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Radial Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Radial Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Tangential Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Tangential Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; No Uniaxial Load



Radial Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference 35% Uniaxial Load



Radial Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Tangential Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Tangential Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Radial-Tangential Shear Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Radial-Tangential Shear Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Radial Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Radial Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Tangential Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-62 Tangential Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-63 Radial-Tangential Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-64 Radial-Tangential Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-65 First Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-66 First Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-67 Second Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Second Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-69 Principal Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-70 Principal Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-71 Radial Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load


Figure AIII-72 Radial Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-73 Tangential Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-74 Tangential Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-75 Radial-Tangential Shear Strain Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-76 Radial-Tangential Shear Strain Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-77

Radial Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-78 Radial Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-79 Tangential Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-80 Tangential Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-81 Radial-Tangential Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-82 Radial-Tangential Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-83 First Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-84 First Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-85 Second Principal Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-86 Second Principal Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-87 Principal Shear Stress Values for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-88 Principal Shear Stress Contours for Steel Plate with 3/16 Inch Hole Radius; 0.00375 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-89 Radial Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-90 Radial Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-91 Tangential Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-92 Tangential Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-93 Radial Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-94 Radial Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-95 Tangential Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-96 Tangential Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; No Uniaxial Load



Figure AIII-97 Radial Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-98 Radial Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-99 Tangential Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-100

Tangential Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-101 Radial-Tangential Shear Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-102 Radial-Tangential Shear Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-103 Radial Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-104 Radial Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-105 Tangential Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-106 Tangential Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-107 Radial-Tangential Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load


Figure AIII-108 Radial-Tangential Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



First Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Intereference; 35% Uniaxial Load



Figure AIII-110 First Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-111 Second Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-112 Second Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-113 Principal Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Principal Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-115 Radial Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-116 Radial Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Tangential Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-118 Tangential Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-119 Radial-Tangential Shear Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-120 Radial-Tangential Shear Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Radial Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-122 Radial Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-123 Tangential Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-124 Tangential Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Radial-Tangential Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-126 Radial Tangential Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-127 First Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-128 First Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Second Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-130 Second Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-131 Principal Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-132 Principal Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.00125 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-133 Radial Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AIII-134 Radial Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Tangential Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AIII-136 Tangential Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AIII-137 Radial Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AIII-138 Radial Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AIII-139 Tangential Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Tangential Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; No Uniaxial Load



Figure AIII-141 Radial Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Radial Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-143 Tangential Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load


Figure AIII-144 Tangential Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-145

Radial-Tangential Shear Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-146 Radial-Tangential Shear Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-147 Radial Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-148 Radial Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-149 Tangential Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-150

Tangential Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-151 Radial-Tangential Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-152 Radial Tangential Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-153 First Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-154 First Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-155 Second Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



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Figure AIII-156 Second Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-157 Principal Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-158 Principal Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 35% Uniaxial Load



Figure AIII-159 Radial Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-160 Radial Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-161

Tangential Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-162 Tangential Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-163 Radial-Tangential Shear Strain Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-164

Radial-Tangential Shear Strain Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-165 Radial Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-166 Radial Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-167 Tangential Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-168

Tangential Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-169 Radial-Tangential Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-170 Radial-Tangential Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-171 First Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-172 First Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-173 Second Principal Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-174

Second Principal Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-175 Principal Shear Stress Values for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load



Figure AIII-176 Principal Shear Stress Contours for Steel Plate with 1/8 Inch Hole Radius; 0.0025 Inch Radial Interference; 70% Uniaxial Load APPENDIX I INDEX OF FIGURES

ALUMINUM PLATE RESULTS

(NOTE: Because of the large number of figures (176) included to present the aluminum plate results, this index is included in lieu of a list of figures. The data presents the figure and the page numbers in 2 rows. Figure numbers are in the first row; page numbers are immediately below in the second row).

					The second se							
2 T12		26 61	44		70 105	88 123		114 149	132 167		158 193	176 211
		25	43 78		69 104	87 122		113 148	131 166		157 192	175 210
		24 59	42		68 103	86 121		112 147	130 165		156 191	174 209
$\mathcal{J}_{\mathrm{RT}}$ \mathcal{O}_{R} \mathcal{O}_{T} \mathcal{O}_{T} $\mathcal{J}_{\mathrm{RT}}$ \mathcal{O}_{I} \mathcal{O}_{I}		23 58	41 76		67 102	85 120		111 146	129 164		155 190	173 208
		22 57	40		66 101	84 119		110	128 163		154 189	172 207
		21 56	39 74		65 100	83 118		109 144	127 162		153 188	171 206
		20 55	38 73		64 99	82 117		108 143	126 161		152 187	170 205
		19 54	37 72		63 98	81 116		107 142	125 160		151 186	169 204
	8 43	18 53	36 71	52 87	62 97	80 115	96 131	106 141	124 159	140 175	150 185	168 203
	7 42	17 52	35 70	51 86	61 96	79 114	95 130	105 140	123 158	139 174	149 184	167 202
	6 41	16 51	34 69	50 85	60	78 113	94 129	104 139	122 157	138 173	148 183	166 201
	5 40	15 50	33 68	49 84	59 94	77 112	93 128	103 138	121 156	137 172	147 182	165 200
		14 49	32 67		58 93	76 111		102 137	120 155		146 181	164 199
		13 48	31 66		57 92	75 110		101 136	119 154		145 180	163 198
£τ	4 39	12 47	30 65	48 83	56 91	74 109	92 127	100 135	118 153	136 171	144 179	162 197
	38.3	11 46	29 64	47 82	55 90	73 108	91 126	99 134	117 152	135 170	143 178	161 196
R	2 37	10	28 63	46 81	54 89	72 107	90 125	98 133	116 151	134 169	142 177	160 195
w	1 36	6 44	27 62	45 80	53 88	71 106	89 124	97 132	115 150	133 168	141 176	159 194
Interference (Inches)	0.001875	0.001875	0.001875	0.00375	0.00375	0.00375	0.00125	0.00125	0.00125	0.00250	0.00250	0.00250
Load (Percent)	0	35	70	0	35	70	0	35	70	0	35	70
Size (Inches)	3/8	3/8	3/8	3/8	3/8	3/8	1/4	1/4	1/4	1/4	1/4	1/4
	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{J}_{RT} \mathcal{O}_{R} \mathcal{O}_{T} \mathcal{T}_{RT} \mathcal{O}_{1} \mathcal{O}_{2} \mathcal{T}_{12}	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{J}_{RT} \mathcal{J}_{RT} \mathcal{J}_{R} \mathcal{J}_{T}	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} $\tilde{\mathcal{O}}_{RT}$ $\tilde{\mathcal{O}}_{T}$ $\tilde{\mathcal{C}}_{RT}$ $\tilde{\mathcal{O}}_{1}$ $\tilde{\mathcal{C}}_{2}$ $\tilde{\mathcal{T}}_{12}$ (inches) (percent) (inches) (nches) 1 2 3 4 $\sqrt{40}$ 41 42 43 3 3 3 3 3 3 3 3 4	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{J}_{RT} \mathcal{G}_{T} \mathcal{G}_{T} \mathcal{G}_{T} \mathcal{T}_{12} (inches) (percent) (inches) 1 2 3 4 \mathcal{I}_{T} \mathcal{G}_{R} \mathcal{G}_{T} \mathcal{G}_{T} \mathcal{G}_{T} \mathcal{T}_{T2} 3/8 0 0.001875 1 2 3 4	Size (Inches)LoadInterference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{J}_{RT} \mathcal{O}_{T} \mathcal{T}_{T} \mathcal{O}_{I} \mathcal{T}_{Z} \mathcal{T}_{I2} 3/800.001875123440414243555657585960613/8350.001875910111213141516171819202122232425263/8350.001875444546474849505152535657585960613/8700.0018752728293031326869707172737443443/800.0018754546474869505152535657767778793/800.001875272829303132686970717273744445443/8000.001875454647486950717273747573747374 <td< td=""><td>Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{T}_{RT} \mathcal{T}_{T} \mathcal{T}_{T}</td><td>Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{O}_{RT} \mathcal{O}_{T} \mathcal{O}_{T}</td><td>Size Load Increase \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{T}_{RT} \mathcal{T}_{R} \mathcal{T}_{R} \mathcal{T}_{T} \mathcal{T}_{T2} 3/8 0 0.001875 $\frac{1}{6}$ $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{4}$</td><td>Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{T}_{RT} \mathcal{T}_{RT} \mathcal{T}_{RT} \mathcal{T}_{T} \mathcal{T}_{T}<td>Load Transference \mathcal{E}_{R} \mathcal{E}_{T} $\mathcal{T}_{\mathrm{RT}}$ \mathcal{T}_{T} \mathcal{T}_{T}<td>Size Far \mathbf{C}r C</td><td>Titution Err ∇rr ∇r ∇r ∇r ∇r Γ Γ</td></td></td></td<>	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{T}_{RT} \mathcal{T}_{T}	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{O}_{RT} \mathcal{O}_{T}	Size Load Increase \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{T}_{RT} \mathcal{T}_{R} \mathcal{T}_{R} \mathcal{T}_{T} \mathcal{T}_{T2} 3/8 0 0.001875 $\frac{1}{6}$ $\frac{1}{3}$ $\frac{1}{4}$	Size Load Interference \mathcal{E}_{R} \mathcal{E}_{T} \mathcal{T}_{RT} \mathcal{T}_{RT} \mathcal{T}_{RT} \mathcal{T}_{T} <td>Load Transference \mathcal{E}_{R} \mathcal{E}_{T} $\mathcal{T}_{\mathrm{RT}}$ \mathcal{T}_{T} \mathcal{T}_{T}<td>Size Far \mathbf{C}r C</td><td>Titution Err ∇rr ∇r ∇r ∇r ∇r Γ Γ</td></td>	Load Transference \mathcal{E}_{R} \mathcal{E}_{T} $\mathcal{T}_{\mathrm{RT}}$ \mathcal{T}_{T} <td>Size Far \mathbf{C}r C</td> <td>Titution Err ∇rr ∇r ∇r ∇r ∇r Γ Γ</td>	Size Far \mathbf{C} r C	Titution Err ∇rr ∇r ∇r ∇r ∇r Γ

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APPENDIX II INDEX OF FIGURES

TITANIUM PLATE RESULTS

Because of the large number of figures (176) included to present the titanium plate results, this index is included in lieu of a list of figures. The data presents the figure number and the page numbers in 2 rows. Figure numbers are in the first row; page numbers are immediately below in the second row). (NOTE:

		-											
	\mathcal{C}_{12}		26 238	44 256		70 282	88 300		114 326	132 344		158 370	176 388
Principal Stress			25 237	43 255		69 281	87 299		113 325	131 343		157 369	175 387
	02		24 236	42 254		68 280	86 298		112 324	130 342		156 368	174 386
			23 235	41 253		67 279	85 297		111 323	129 341		155	173 385
			22 234	40 252		66 278	84 296		110 322	128 340		154 366	172 384
	Z _{RT} D		21 233	39 251		65 277	83 295		109 321	127 339		153 365	171 383
SS			20 232	38 250		64 276	82 294		108 320	126 338		152 364	170 382
1 Stre			19 231	37 249		63 275	81 293		107 319	125 337		151 363	169 381
Radial-Tangentia	9,1	8 220	18 230	36 248	52 264	62 274	80 292	96 308	106 318	124 336	140 352	150 362	168 380
		7 219	17 229	35 247	51 263	61 273	79 291	95 307	105317	123 335	139 351	149 361	167 379
	$q_{\rm R}$	6 218	16 228	34 246	50 262	60 272	78 290	94 306	104 316	122 334	138 350	148 360	166 378
		5 217	15 227	33 245	49 261	59 271	77 289	93 305	103 315	121 333	137 349	147 359	165 377
su	$\mathcal{X}_{\mathrm{RT}}$		14 226	32 244		58 270	76 288		102 314	120 332		146 358	164 376
L Strai			13 225	31 243		57 269	75 287		101 313	119 331		145 357	163 375
gentia]	έ _T	4 216	12 224	30 242	48 260	56 268	74 286	92 304	100312	118 330	136 348	144 356	162 374
al-Tang		3 215	11 223	29 241	47 259	55 267	73 285	91 303	99 311	117 329	135 347	143 355	161 373
Radia	~	2 214	10 222	28 240	46 258	54 266	72 284	90 302	98 310	116 328	134 346	142 354	160 372
	~	1 213	9 221	د 27 239	45 257	53 265	71 283	89 301	97 309	115 327	133 345	141 353	159 371
Radial	Interference (Inches)	0.001875	0.001875	0.001875	0.00375	0.00375	0.00375	0.00125	0.00125	0.00125	0.00250	0.00250	0.00250
Uniaxial	Load (Percent)	0	35	50	0	35	70	0	35	50	0	35	70
Bolt Hole	Size (Inches)	3/8	5/8	3/8	3/8	3/8	3/8	1/4	1/4	1/4	1/4	1/4	1/4

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APPENDIX III INDEX OF FIGURES

STEEL PLATE RESULTS

Because of the large number of figures (176) included to present the steel plate results, this index is included in lieu of a list of figures. The data presents the figure numbers and the page numbers in 2 rows. Figure numbers are in the first row; page numbers are immediately below in the second row). (NOTE:

	-												
Principal Stress	2		26 415	44 433		70	88 477		114 503	132 521		158 547	176 565
	₹ <u>1</u>		25 414	43 432		69 458	87 476		113 502	131 520		157 546	17 5 564
			24 413	42 431		68 457	86 475		112 501	130 519		156 545	17 4 563
	6		23 412	41 430		67 456	85 474		111 500	129 518		155 544	173 562
			22 411	40 429		66 455	84 473		110	128 517		154 543	172 561
	$\widetilde{c}_{\mathrm{RT}}$ G_1		21 410	39 428		65 454	83 472		109 498	127 516		153 542	171 560
			20 409	38 427		64 453	82 471		108	126 515		152 541	170 559
Stress			19 408	37 426		63 452	81 470		107	125 514		151 540	169 558
tial 3		8 397	18 407	36 425	52 441	62 451	80 469	96 485	106 495	124 513	140 529	150 539	168 557
-Tanger	6 ¹	7 396	17 406	35 424	51 440	61 450	79 468	95 484	105 494	123 512	139 528	149 538	167 556
Radial-		6 395	16 405	34 423	50 439	60 449	78	94 483	104 493	122 511	138 527	148 537	166 555
	RT GF	5 394	15 404	33 422	49 438	59 448	77 466	93 482	103 492	121 510	137 526	147 536	165 554
50			14 403	32 421		58 447	76 465		102 491	120 509		146 535	164 553
Strain	Ø		13 402	31 420		57 446	75 464		101 490	119 508		145 534	163 552
ntial	н	4 393	12 401	30 419	48 437	56 445	74 463	92 481	100 489	118 507	136 525	144 533	162 551
-Tangel	R E	3 392	11 400	29 418	47 436	55 444	73 462	91 480	99 488	117 506	135 524	143 532	161 550
Radial		2 391	10 399	28 417	46 435	54 443	72 461	90 479	98 487	116 505	134 523	142 531	160 549
	W	1 390	9 398	27 416	45 434	53 442	71 460	89 478	97 486	11 5 504	133 522	141 530	159 548
Radial	Interference (Inches)	0.001875	0.001875	0.001875	0.00375	0.00375	0.00375	0.00125	0.00125	0.00125	0.00250	0.00250	0.00250
Uniaxial	Load (Percent)	0	35	70	0	35	70	0	35	70	0	35	70
Bolt Hole	Size (Inches)	3/8	3/8	3/8	3/8	3/8	3/8	1/4	1/4	1/4	1/4	1/4	1/4

571,572
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A body of detailed stress and strain distributions in the vicinity								
of interference fit fasteners has been analytically obtained and is presented. These data, obtained on simple installations, present trends which may be used by designers in determining how or whether to use interference fit fasteners.								
The analysis was performed with a finite element digital procedure which has the nonlinear constitutive behavior programmed and interre- lates internal loading and deformations. Preparations for the analysis of thirty six conditions included analyzing a test article for which good correlations are shown.								
Stress and strain distributions include two fastener hole sizes, two plate materials (steel, titanium and iaxial loading.	are presen levels of aluminum)	interfer and three	condi rence : ee leve	tions which fit, three els of un-				

The results indicate that the radial strains in that part of the plate which is strained beyond the yield point are sensitive to the value of plastic modulus of the material. Also, the fastener diameters may be any size provided that the insertion is adjusted accordingly.

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14.	KEY WORDS	ROLE	wт	ROLE	wт	ROLE	wт
	Interference Fit Fasteners						
	Observed and Observed						
	Stresses and Strains						
	Plasticity						
	Nonlinear Materials						
							1
						1	