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THE ABSORPTION BY H<sub>2</sub>O BETWEEN 1630 AND 2245/cm  
(6.13 - 4.44 MICROMETER)

Darrell E. Burch, et al

Philco-Ford Corporation

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by

Darrell E. Burch  
David A. Gryvnak  
John D. Pembroke

Philco-Ford Corporation  
Aeronutronic Division  
Ford Road  
Newport Beach, California 92663

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Principal Investigator and Phone No.  
Dr. Darrell E. Burch/714 640-1500

AFCRL Project Scientist and Phone No.  
Dr. Robert A. McClatchey/617 861-3224

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13. ABSTRACT The absorption by samples of H <sub>2</sub> O and H <sub>2</sub> O + N <sub>2</sub> has been studied between 1630 and 2245 cm <sup>-1</sup> . Spectral curves of transmittance have been obtained for samples covering a wide range of pressures with temperatures between 308 K and 428 K. The emphasis has been on continuum absorption in approximately 30 narrow windows where most of the absorption results from lines centered more than 1 cm <sup>-1</sup> from the point of absorption. Comparison of the results with calculated values based on published line parameters indicates that the extreme wings of H <sub>2</sub> O lines absorb more than Lorentz-shaped lines of the same intensity and half-width. The continuum absorption decreases with increasing temperature at a faster rate than is predicted by simple theory on line shapes.			

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KEY WORDS

H<sub>2</sub>O

Atmospheric Transmission

Absorption

Continuum Absorption

LINK A		LINK B		LINK C	
ROLE	WT	ROLE	WT	ROLE	WT

*ia*

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## SECTION I

### INTRODUCTION

#### Background

The parameters of nearly all of the  $\text{H}_2\text{O}$  lines of significance in the spectral region  $1630 - 2245 \text{ cm}^{-1}$  covered by this report have been tabulated by Benedict and Calfee.<sup>1</sup> The tabulated parameters for each line are: line center  $\nu_0$ , intensity  $S$ , half-width  $\alpha_0$  normalized for air at 1 atm pressure, and the value  $E''$  of the lower energy level involved in the transition. The latter parameter is required in order to calculate the intensity at a temperature different from the standard temperature for which the parameters apply. A combined experimental-theoretical approach was used to determine the parameters. Detailed comparisons with experimental results have not yet been made for all of the individual lines, but there is generally good agreement over intervals several  $\text{cm}^{-1}$  wide.

Many very strong  $\text{H}_2\text{O}$  lines occur throughout this region, particularly from 1630 to approximately  $2000 \text{ cm}^{-1}$ , so that the average transmittance is quite low over lower atmospheric paths of a few hundred meters. Although the average transmittance is low, the transmittance may be appreciable in a few "gaps" or narrow "windows" separated by a few  $\text{cm}^{-1}$  from any very strong lines. The invention of the CO laser has created new interest in these small windows because they coincide with many of the laser lines. Obviously, the performance of the CO laser for communications depends strongly on the atmospheric attenuation. Long et al.<sup>2</sup> have recently used a CO laser as a radiant energy source to study the transmission of synthetic atmospheres of  $\text{H}_2\text{O} - \text{N}_2$  contained in a multiple-pass absorption cell. The emphasis was on several of the narrow windows between approximately  $1840$  and  $1990 \text{ cm}^{-1}$ . Long et al have compared many of their experimental results with calculated results based on the Lorentz line

shape and the line parameters published by Benedict et al. In nearly every case, the observed absorptance was greater than the calculated value, sometimes by as much as a factor of 3. Rice,<sup>3</sup> using a different method of measuring the attenuation of CO-laser radiant energy by H<sub>2</sub>O, has also found poor agreement with calculated results.

The present laboratory investigation was undertaken to check the experimental results of Long et al and to provide additional data from which the continuum absorption could be determined and compared to the calculated results. The discrepancy between the observed and calculated values cannot be explained. It also seems unlikely that errors in the intensities or half-widths are large enough to cause such large errors in the calculated absorptance. Furthermore, it is not probable that the "extra" absorption in this spectral region is due to an H<sub>2</sub>O:H<sub>2</sub>O dimer as has been suggested as the primary cause of H<sub>2</sub>O continuum absorption between 8 and 12  $\mu$ m. The most probable explanation involves a deviation from the Lorentz line shape in the extreme wings ( $\nu - \nu_0$  greater than approximately 10  $\text{cm}^{-1}$ ) of the lines. Preliminary analysis of our data indicate that the lack of knowledge about the shapes of the wings of the lines accounts largely for the inability to calculate the absorption reliably. Further analysis of the data, many of which are shown in Sections 2 and 3, will provide additional information on the accuracy of the published values of  $S$  and  $\alpha^0$ . It is also anticipated that these data along with other data<sup>4,5,6,7</sup> on H<sub>2</sub>O absorption in windows will provide better insight into the behavior of the wings of lines.

#### Symbols, Units, and Definitions

At the pressures involved in the present study, the H<sub>2</sub>O vapor density is proportional to its partial pressure  $p$  so that the absorber thickness  $u$  of a sample is given by

$$\begin{aligned} u(\text{molecules/cm}^2) &= 2.69 \times 10^{19} p(\text{atm}) L(\text{cm}) (273/\theta) \\ &= 7.34 \times 10^{21} pL/\theta. \end{aligned} \quad (1-1)$$

The true transmittance that would be observed with infinite resolving power is given by

$$T' = \exp(-u\kappa), \quad \text{or} \quad (-1/u) \ln T' = \kappa, \quad (1-2)$$

where  $\kappa$  is the absorption coefficient. Because of the finite slitwidth of a spectrometer and possible variations in  $\kappa$  with wavenumber due to line structure, the observed transmittance  $T$  may differ from  $T'$  at the same wavenumber. The quantity  $T$  represents a weighted average of  $T'$  over the interval passed by the spectrometer.

The intrinsic absorption coefficient due to a single collision-broadened absorption line at a point within a few  $\text{cm}^{-1}$  of the line center,  $\nu_0$ , is probably given adequately by the Lorentz shape:

$$k = \frac{S}{\pi} \frac{\alpha}{(\nu - \nu_0)^2 + \alpha^2} \quad (1-3)$$

The line intensity  $S = \int k d\nu$  is essentially independent of pressure for the conditions of the present study. It has been shown<sup>8,9,10</sup> that for  $|\nu - \nu_0|$  greater than a few  $\text{cm}^{-1}$ , the Lorentz equation may require modification. One method is to employ a factor  $\lambda$ , which is a function of  $(\nu - \nu_0)$ , so that Eq. (1-3) becomes

$$k = k_L \lambda = \frac{S}{\pi} \frac{\alpha \lambda}{(\nu - \nu_0)^2 + \alpha^2} \quad (1-4)$$

where  $k_L$  denotes the value given by the Lorentz coefficient. The value of  $\lambda$  is approximately equal to unity for small  $|\nu - \nu_0|$ , but may be quite different for large  $|\nu - \nu_0|$ . For example,  $\lambda \ll 1$  for the extreme wings of  $\text{CO}_2$  lines, but the data presented below indicates  $\lambda > 1$  for  $\text{H}_2\text{O}$  lines.

The half-width  $\alpha$  is proportional to pressure so that  $k$  is, in turn, proportional to pressure in the extreme wings where  $|\nu - \nu_0| \gg \alpha$ . It follows from Eq. (1-4) that the wing-absorption coefficient  $C$  due to the extreme wings of several lines is equal to the sum of all the  $k$ 's due to the individual lines and is proportional to pressure, ( $C = C^0 p$ ). Since wing absorption changes slowly with wavenumber, it is frequently called continuum absorption.

Continuum absorption may also arise from dimers,<sup>11</sup> such as  $\text{H}_2\text{O}:\text{H}_2\text{O}$ , or from pressure-induced bands. These two types of continuum have the same pressure dependence as absorption by line wings; therefore, it is not necessary to determine which is the source of the absorption being measured. In the following discussions, we refer to it as wing absorption, although it is possible that some dimer absorption or pressure-induced absorption also occurs. The absorption coefficient due to local lines whose centers occur within a few  $\text{cm}^{-1}$  of the point of observation is denoted by  $\kappa(\text{local})$ . This quantity may vary rapidly with wavenumber and depends on pressure as indicated by Eq. (1-3) because of collision-broadening of the absorption lines. At a given wavenumber, there may be absorption by local lines as well as by continuum. Therefore, for a pure  $\text{H}_2\text{O}$  sample, the total absorption coefficient  $\kappa$  in Eq. (1-2) is given by

$$\kappa = \kappa(\text{local}) + C_s = \kappa(\text{local}) + C_s^0 p \quad (1-5)$$

The normalized continuum coefficient  $C_s^0$  is the value of  $C_s$  when  $p = 1$  atm. The subscript  $s$  denotes self-broadening of the lines. Since  $u$  is proportional to  $pL$ ,  $(-L_n T)$  due to continuum is proportional to  $p^2 L$ .

For a mixture of  $H_2O + N_2$ , such as several of those used in the present study, Eq. (1-5) must be modified to account for the broadening of the  $H_2O$  lines by  $N_2$ .

$$\kappa = \kappa(\text{local}) + C_s^0 p + C_{N_2}^0 p_{N_2}, \quad (1-6)$$

where  $p_{N_2}$  is the partial pressure of  $N_2$ .

The equivalent pressure  $P_e$  given by the following equation is a convenient parameter when dealing with  $H_2O$  absorption by mixtures of  $H_2O$  in  $N_2$  or in air, which is approximately 80%  $N_2$ :

$$P_e = Ep + p_{N_2} = (B-1)p + P, \quad (1-7)$$

where  $P$  is the total pressure.  $B$  is the ratio of the self-broadening ability to the broadening ability of  $N_2$ , i.e.,  $C_s^0/C_{N_2}^0$ . We note that  $P_e$  approximates  $P$  for dilute mixtures of  $H_2O$  in  $N_2$  ( $p \ll p_{N_2}$ ). Values of  $C_s^0$  and  $C_{N_2}^0$  and  $B$  are given in Table 3-1 for selected wavenumbers  $^2$  at different sample temperatures,

## SECTION 2

### SPECTRAL TRANSMITTANCE FROM 1860 TO 2230 $\text{cm}^{-1}$

Figures 2-1 through 2-4 show spectral curves of transmittance from 1860 to 2243  $\text{cm}^{-1}$  for two pure samples of  $\text{H}_2\text{O}$  at a temperature of 322 K. The spectral slitwidth varied from 0.45 to 0.6  $\text{cm}^{-1}$ . The two samples were contained in a multiple-pass absorption cell adjusted to 32 passes for a path length of 948.7 meters. After the spectrum of each sample was scanned, a background curve was obtained with the cell evacuated. It was difficult to determine accurately the position of the background curve (corresponding to 100% transmittance) relative to the sample spectrum because of drift during the scanning time of 2-3 hours. In order to position the background curves the following procedure was followed.

Spectral curves were scanned over 8 selected narrow windows for a variety of pure  $\text{H}_2\text{O}$  samples at different pressures. The time required to obtain these data was short enough that the drift in detector signal could be accounted for. The quantity  $(-1/u) \ln T$  was plotted against  $p$  for the point of maximum transmittance in each window (See Fig. 3-1). These curves were used to modify the background curves relative to the curves for Samples 25 and 18. For wavenumber calibration, more than 55  $\text{H}_2\text{O}$  absorption lines were identified from a paper by Benedict, Claassen, and Shaw<sup>12</sup> and their positions were determined from a listing by Benedict and Calfee.<sup>1</sup>

Figures 2-5 through 2-9 show transmittance spectra for 4 pure  $\text{H}_2\text{O}$  samples at 428 K contained in a multiple-pass cell adjusted for 4 and 32 passes. Background curves were fitted to the sample curves by the method described in the previous paragraph. Table 2-1 lists values of the integrated absorptance  $\int A(\nu) d\nu$  for the samples represented in Figs. 2-1 through 2-9, ( $A(\nu) = 1 - T(\nu)$ ).

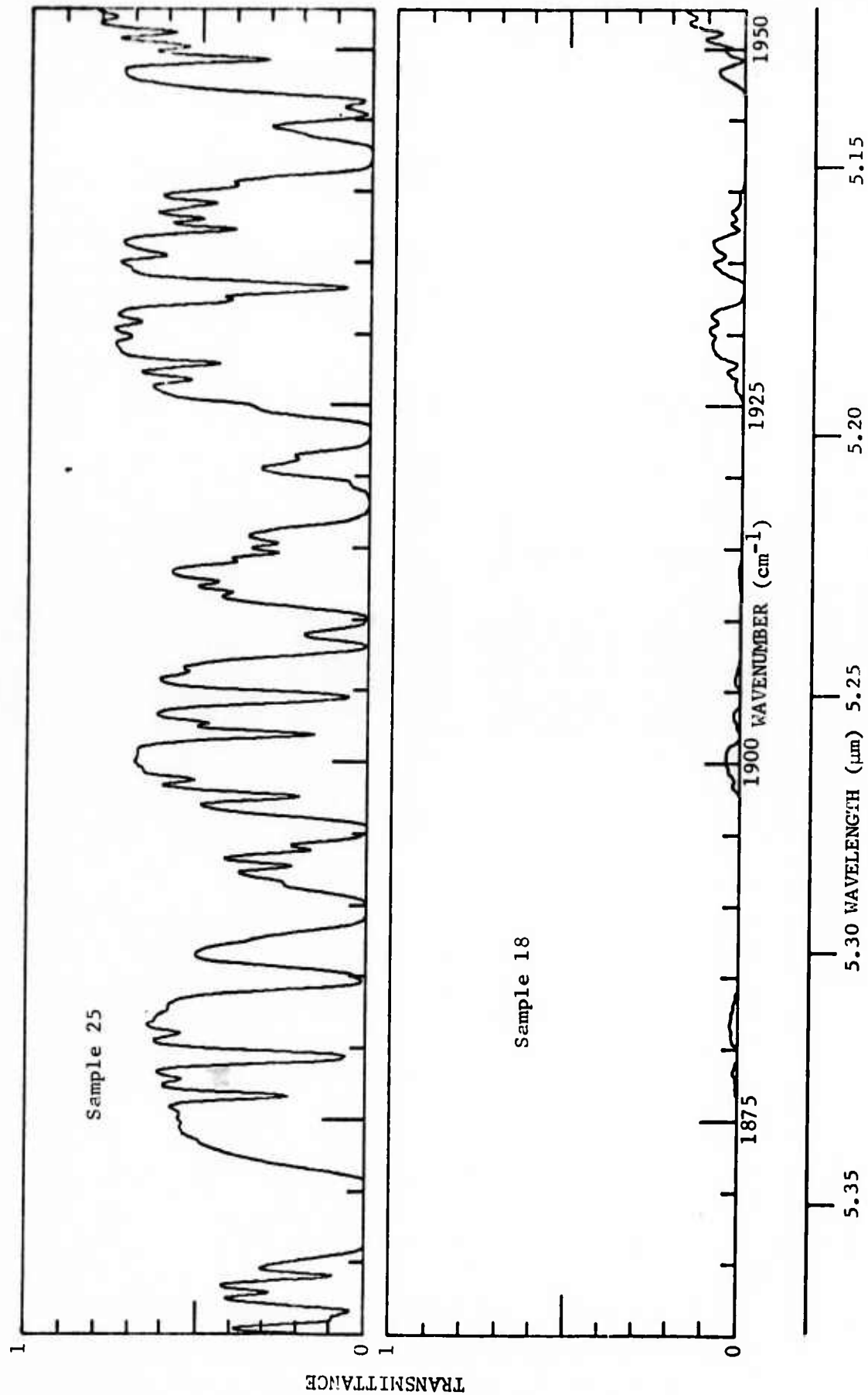


FIG. 2-1. Spectral curves of transmittance from 1860 to 1953  $\text{cm}^{-1}$  for 2 pure samples of  $\text{H}_2\text{O}$ . Spectral slitwidth  $\approx 0.45 \text{ cm}^{-1}$ .

Sample #	P (atm)	L (cm)	$\bar{e}$ (K)	$u$ molecules/ $\text{cm}^2$
25	0.0167	94870	322	360 E20
18	0.0526	94870	322	1140 E20

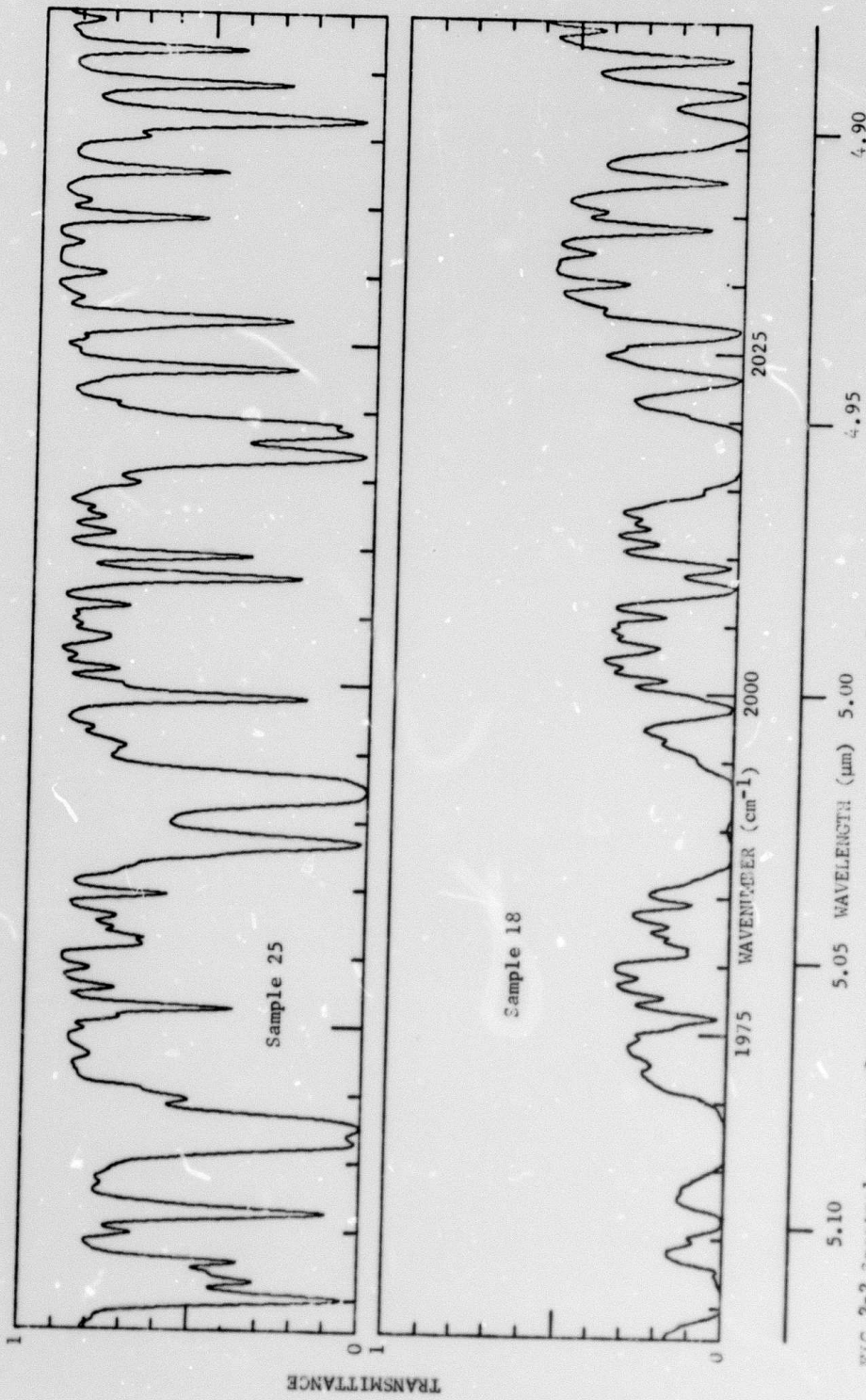


FIG. 2-2. Spectral curves of transmittance from 1953 to 2049  $\text{cm}^{-1}$  for 2 pure  $\text{H}_2\text{O}$  samples. Spectral slitwidth  $\approx 0.47 \text{ cm}^{-1}$ . Sample parameters are given in Fig. 2-1.

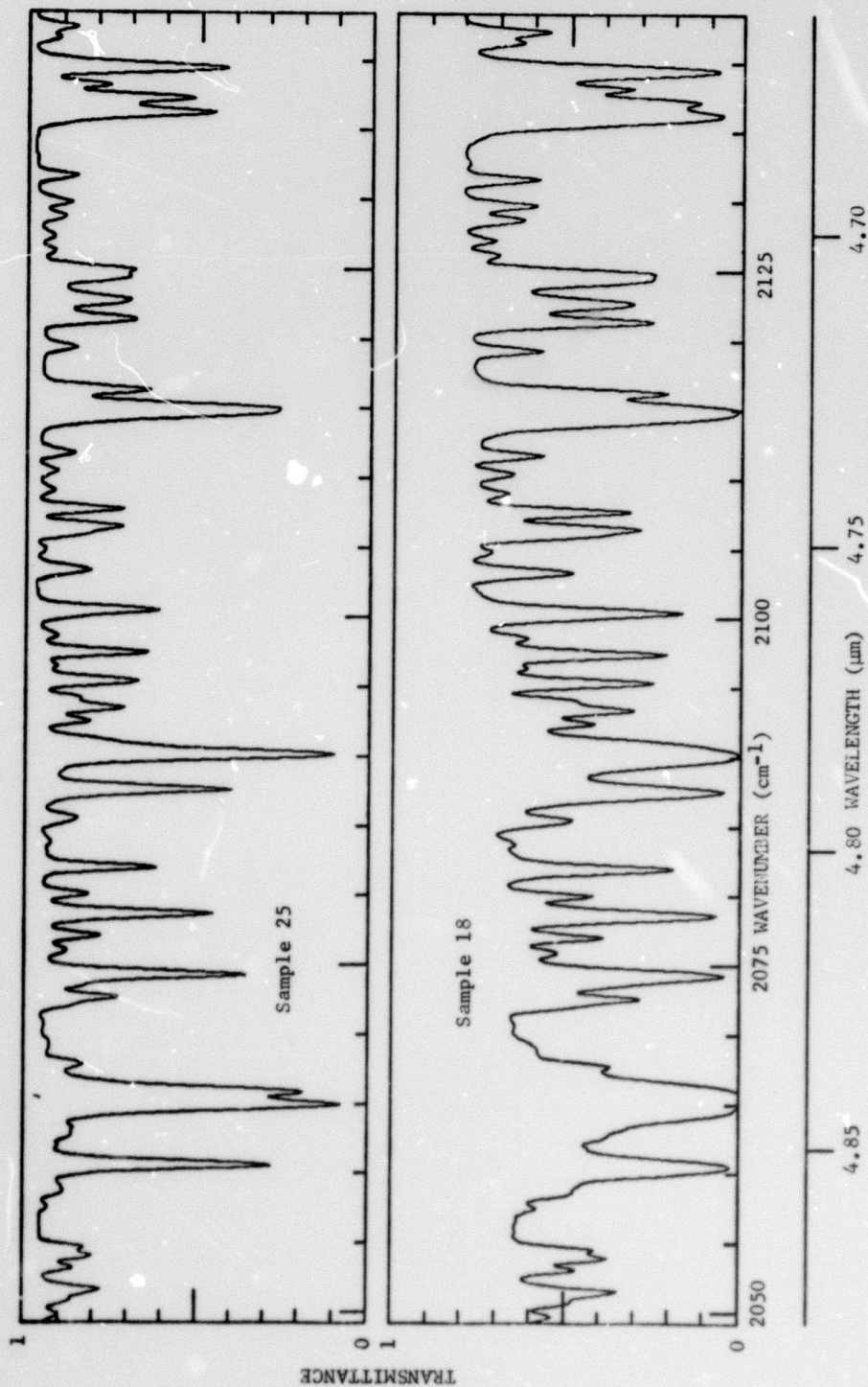


FIG. 2-3. Spectral curves of transmittance from 2049 to 2143  $\text{cm}^{-1}$  for 2 pure  $\text{H}_2\text{O}$  samples. Spectral slitwidth  $\approx 0.52 \text{ cm}^{-1}$ . Sample parameters are given in Fig. 2-1.



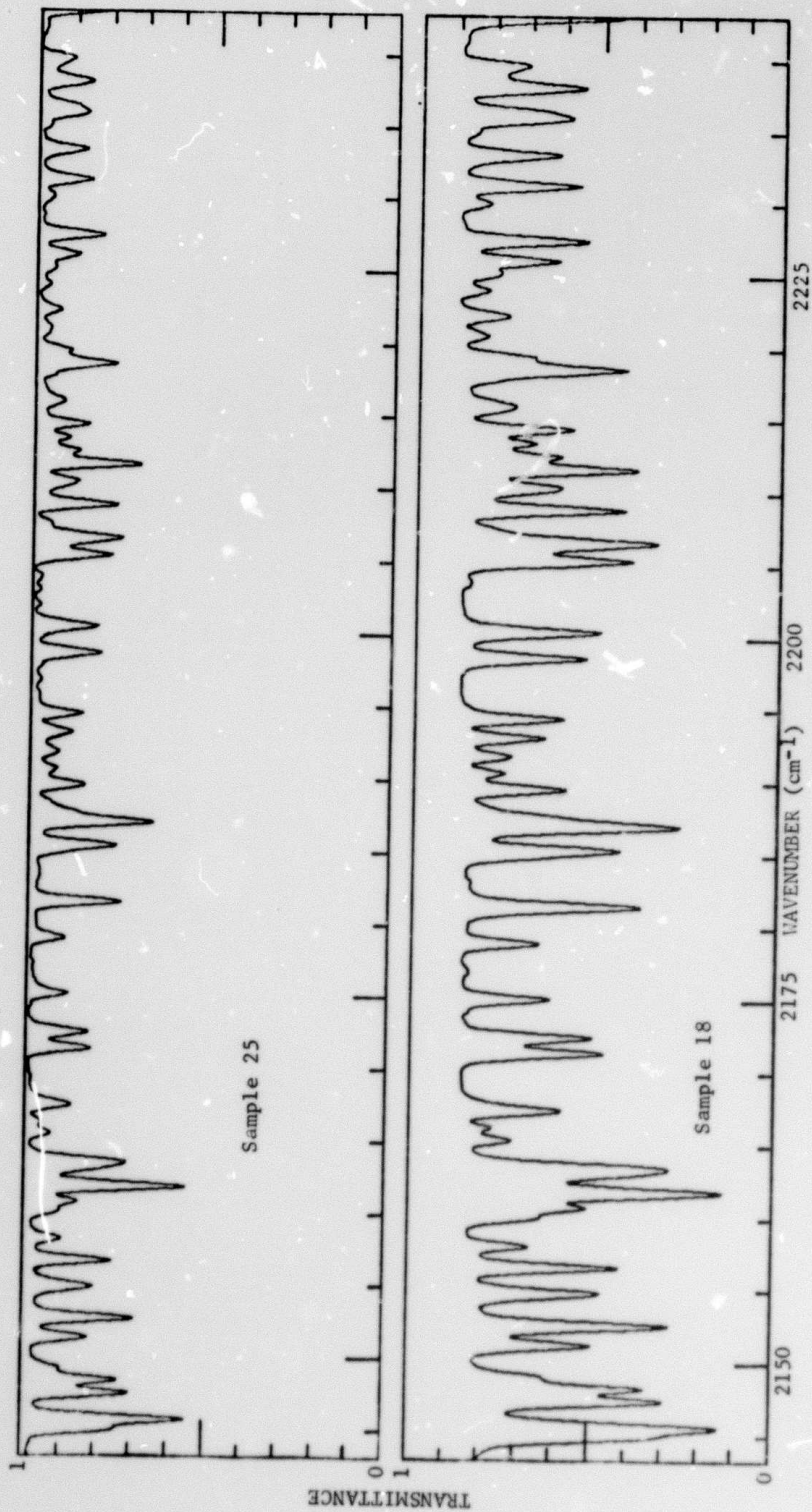


FIG. 2-4. Spectral curves of transmittance from 2143 to 2243 cm<sup>-1</sup> for 2 pure H<sub>2</sub>O samples. Spectral slitwidth ≈ 0.6 cm<sup>-1</sup>. Sample parameters are given in Fig. 2-1.

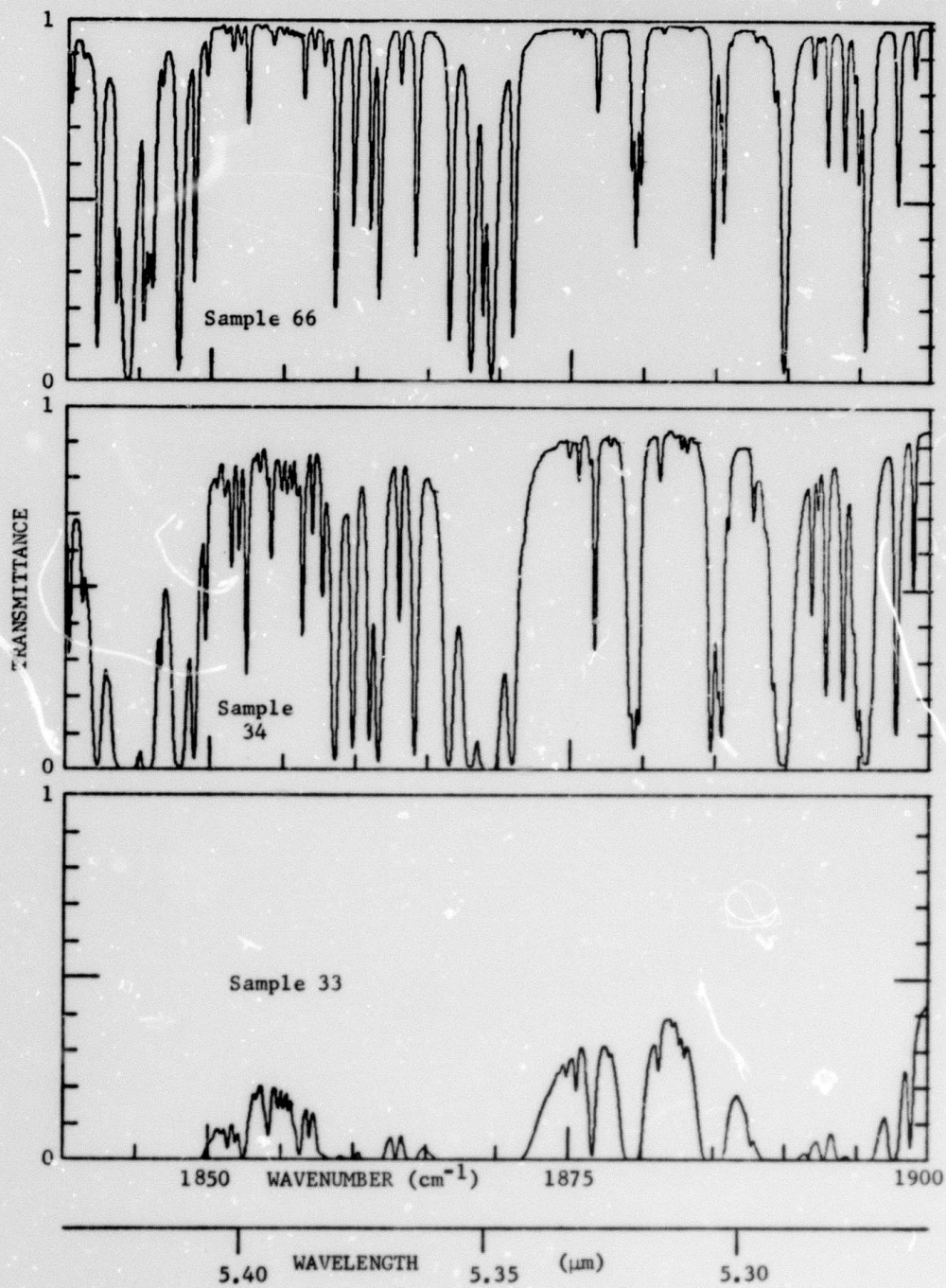


FIG.2-5. Spectral curves of transmittance from 1840 to 1900  $\text{cm}^{-1}$  for 3 pure  $\text{H}_2\text{O}$  samples. Spectral slitwidth  $\approx 0.18 \text{ cm}^{-1}$ .

Sample #	P atm	L cm	$\theta$ K	$u$ molecules/ $\text{cm}^2$
66	0.05	416	428	3.58 E20
34	0.05	3291	428	28.2 E20
33	0.2	3291	428	113 E20

2-6

10

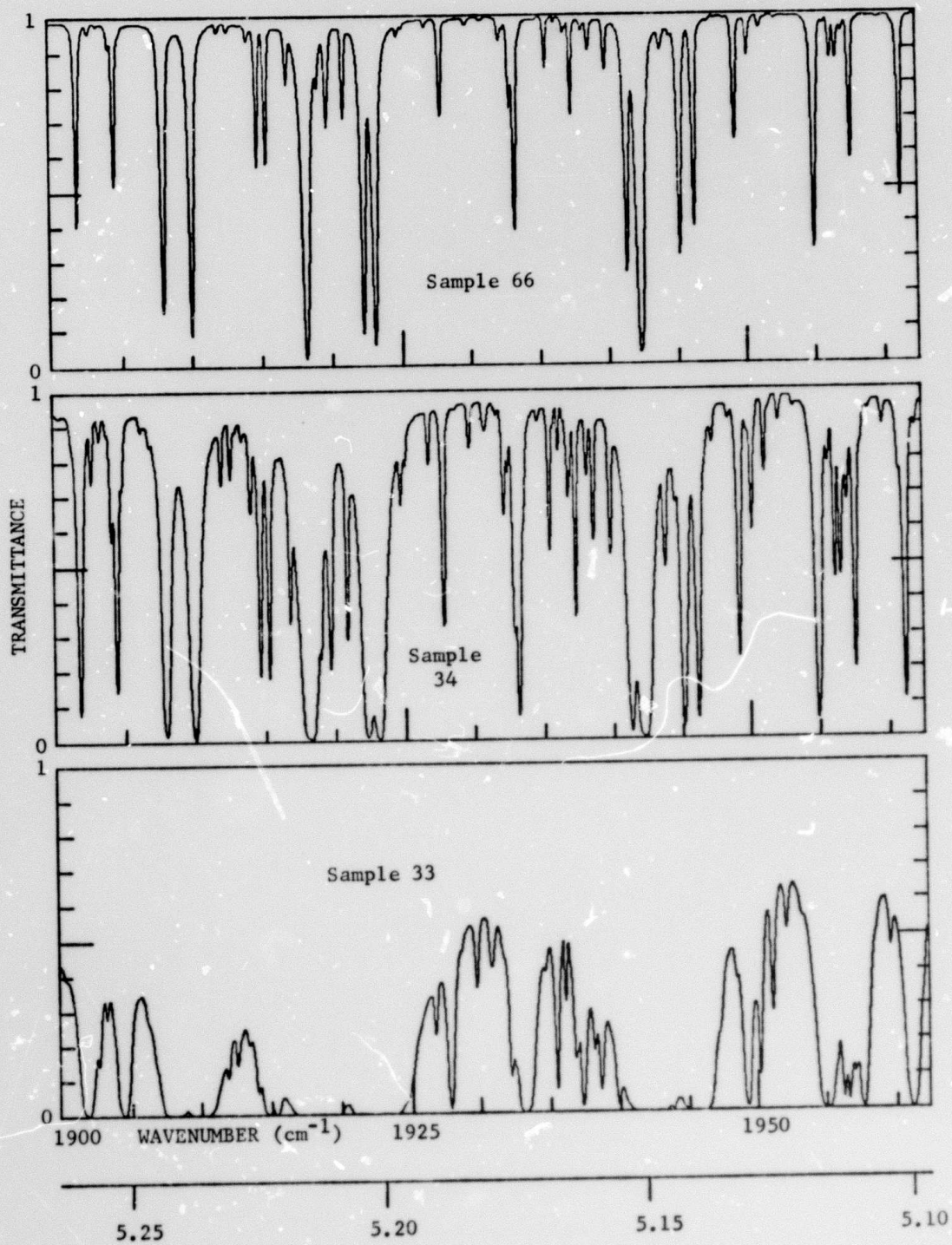


FIG. 2-6. Spectral curve of transmittance from 1900 to 1963 for 3 pure samples of H<sub>2</sub>O. Spectral slitwidth  $\approx 0.19$  cm<sup>-1</sup>. Sample parameters are given in Fig. 2-5.

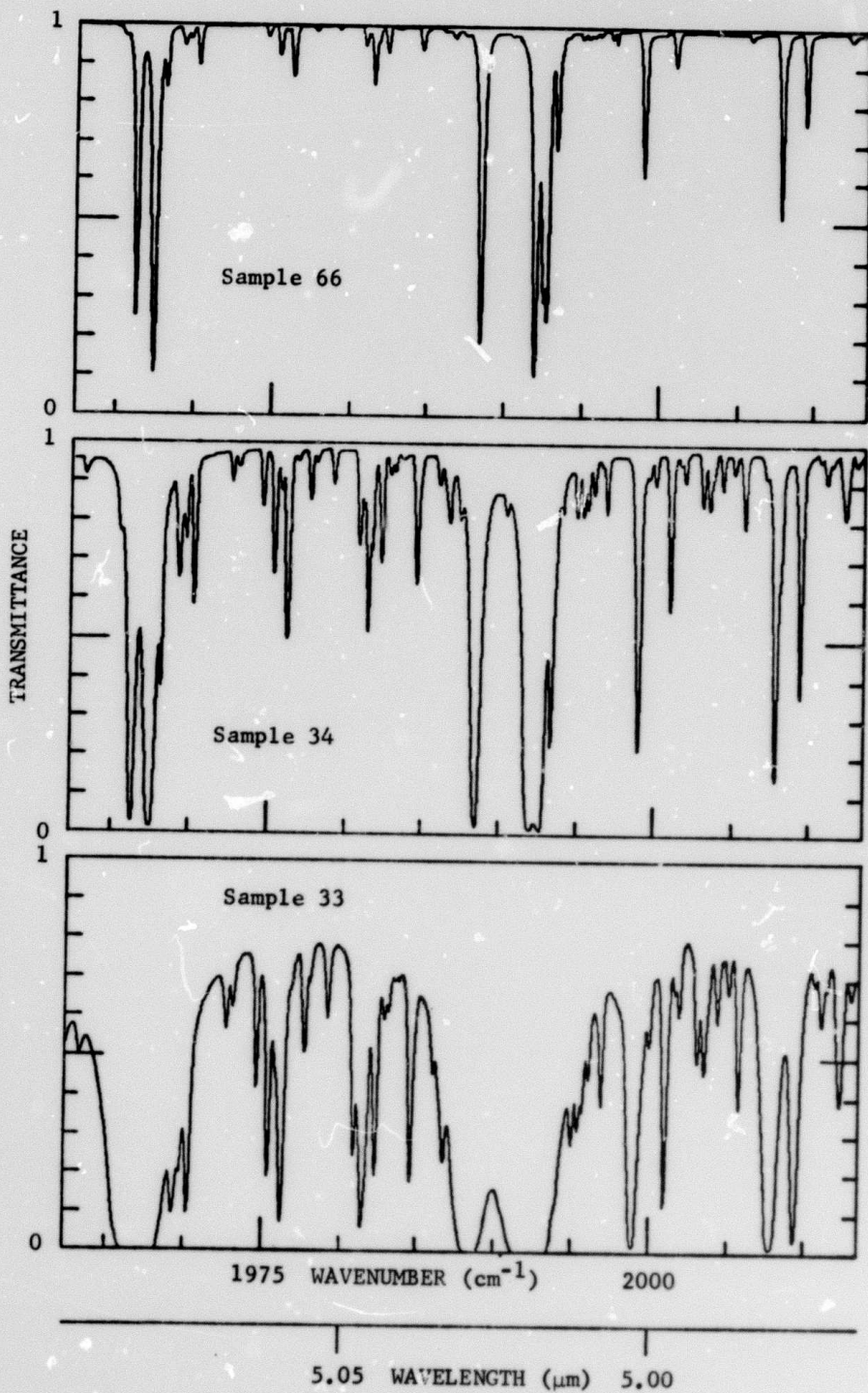


FIG.2-7. Spectral curve of transmittance from 1963 to 2015  $\text{cm}^{-1}$  for 3 pure  $\text{H}_2\text{O}$  samples. Spectral slitwidth  $\approx 0.19 \text{ cm}^{-1}$ . Sample parameters are given in Fig. 2-5.

2-8

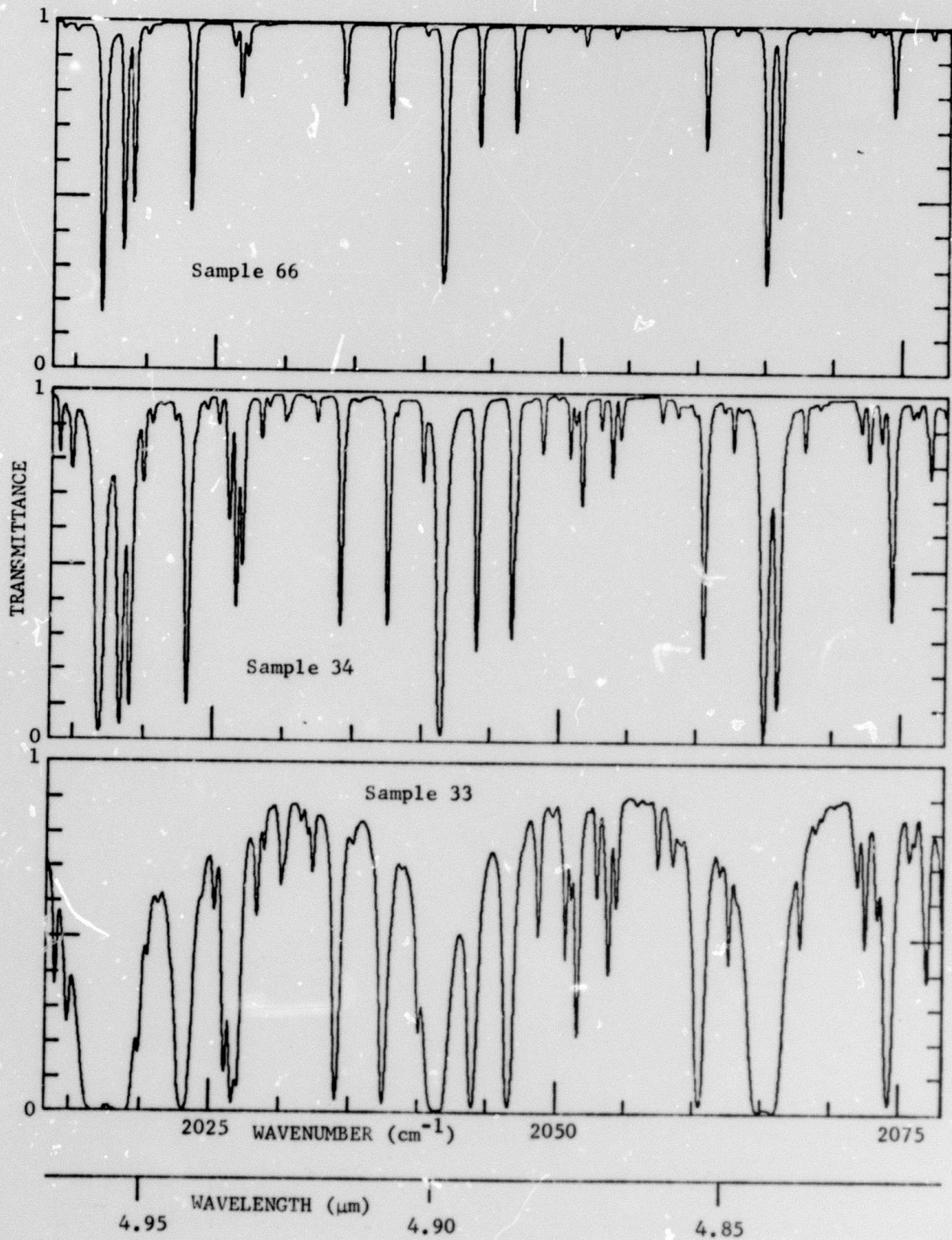


FIG. 2-8. Spectral curves of transmittance from 2015 to 2080  $\text{cm}^{-1}$  for 3 pure  $\text{H}_2\text{O}$  samples. Spectral slitwidth  $\cong 0.20 \text{ cm}^{-1}$ . Sample parameters are given in Fig. 2-5.

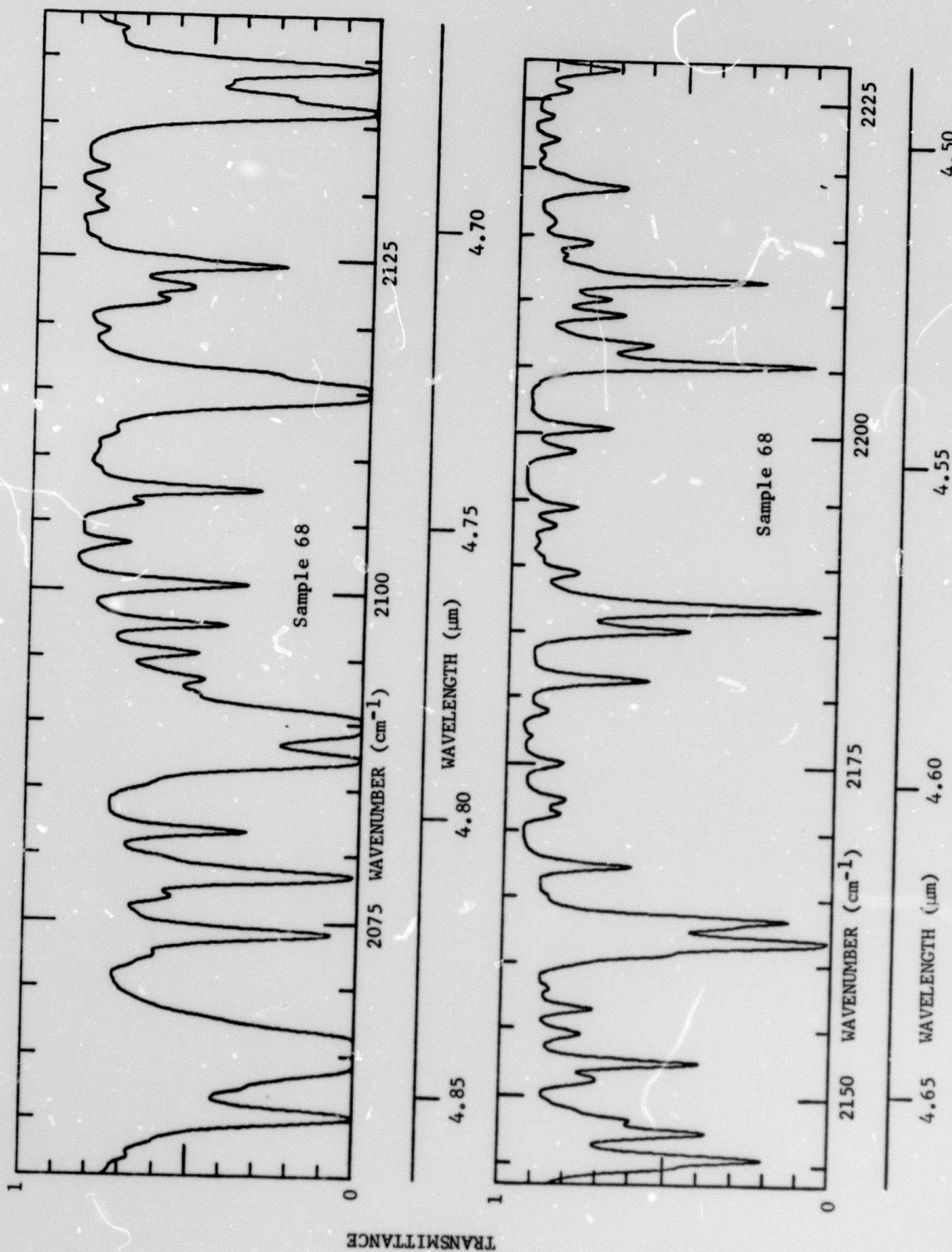


FIG.2-9. Spectral curve of transmittance between 2055 and 2230  $\text{cm}^{-1}$ . Spectral slitwidth  $\approx 0.3 \text{ cm}^{-1}$ . Sample parameters are: 1 atm pure  $\text{H}_2\text{O}$  sample at 428K, 416 cm path length and  $u = 71.4 \text{ E20 molecules/cm}^2$ .

TABLE 2-1  
INTEGRATED ABSORBANCE FOR PURE H<sub>2</sub>O  
 $\int_{\nu_1}^{\nu_2} \mu(\nu) d\nu$  (cm<sup>-1</sup>)

Sample # @ (K)	v <sup>1</sup> (cm <sup>-1</sup> )		v <sup>2</sup> (cm <sup>-1</sup> )		v <sup>1</sup> (cm <sup>-1</sup> )		v <sup>2</sup> (cm <sup>-1</sup> )		v <sup>1</sup> (cm <sup>-1</sup> )	v <sup>2</sup> (cm <sup>-1</sup> )	v <sup>1</sup> (cm <sup>-1</sup> )	v <sup>2</sup> (cm <sup>-1</sup> )
	1840	1845	1840	1845	1840	1860	2056	1860				
1840	0	0	0	0	0	0	0	0	0	0	0	0
1845	5,000	3,866	0	2,124	0	0	0	0	0	0	0	0
1850	9,993	7,708	3,915	3,915	3,915	3,915	3,915	3,915	11,308	185,471	185,471	98,691
1855	14,494	8,899	4,142	3,915	8,899	8,899	8,899	8,899	13,962	188,222	188,222	99,864
1860	19,216	10,927	4,831	3,915	10,927	10,927	10,927	10,927	15,681	190,367	190,367	100,114
1865	24,143	13,235	5,649	3,915	13,235	13,235	13,235	13,235	19,457	193,673	193,673	101,291
1870	29,132	17,184	7,808	3,915	17,184	17,184	17,184	17,184	22,397	196,777	196,777	102,506
1875	33,650	18,921	8,399	3,915	18,921	18,921	18,921	18,921	24,050	199,138	199,138	103,209
1880	37,807	20,453	8,957	3,915	20,453	20,453	20,453	20,453	25,290	201,042	201,042	103,745
1885	41,639	21,452	9,261	3,915	21,452	21,452	21,452	21,452	26,726	203,153	203,153	104,339
1890	46,385	23,734	10,199	3,915	23,734	23,734	23,734	23,734	28,894	205,419	205,419	105,256
1895	51,301	25,947	10,852	3,915	25,947	25,947	25,947	25,947	31,116	207,611	207,611	106,064
1900	55,643	27,766	11,597	3,915	27,766	27,766	27,766	27,766	33,015	210,306	210,306	107,062
1905	59,723	29,046	11,990	3,915	29,046	29,046	29,046	29,046	33,909	211,820	211,820	107,468
1910	64,192	30,933	12,736	3,915	30,933	30,933	30,933	30,933	34,789	213,036	213,036	107,662
1915	68,674	32,359	13,137	3,915	32,359	32,359	32,359	32,359	38,640	216,710	216,710	109,210
1920	73,637	35,334	14,307	3,915	35,334	35,334	35,334	35,334	40,050	218,330	218,330	109,570
1925	78,591	38,111	15,470	3,915	38,111	38,111	38,111	38,111	42,065	220,810	220,810	110,467
1930	81,984	38,708	15,600	3,915	38,708	38,708	38,708	38,708	43,336	222,662	222,662	111,023
1935	85,467	39,739	15,907	3,915	39,739	39,739	39,739	39,739	44,141	224,081	224,081	111,422
1940	89,349	40,709	16,119	3,915	40,709	40,709	40,709	40,709	46,925	226,559	226,559	112,247
1945	94,293	43,572	17,382	3,915	43,572	43,572	43,572	43,572	47,626	227,649	227,649	112,463
1950	98,411	45,176	17,971	3,915	45,176	45,176	45,176	45,176	48,199	229,037	229,037	112,791
1955	101,280	45,915	18,199	3,915	45,915	45,915	45,915	45,915	48,639	230,001	230,001	112,990
1960	105,054	47,164	18,540	3,915	47,164	47,164	47,164	47,164	49,491	231,276	231,276	113,315
1965	108,188	47,882	18,722	3,915	47,882	47,882	47,882	47,882	51,305	233,184	233,184	113,987
1970	112,821	50,150	19,534	3,915	50,150	50,150	50,150	50,150	51,851	234,400	234,400	114,343
1975	114,759	50,470	19,572	3,915	50,470	50,470	50,470	50,470	52,283	235,367	235,367	114,601
1980	116,736	50,927	19,644	3,915	50,927	50,927	50,927	50,927	52,948	236,375	236,375	114,821
1985	119,222	51,538	19,744	3,915	51,538	51,538	51,538	51,538	54,556	238,310	238,310	115,419
1990	123,065	52,801	20,141	3,915	52,801	52,801	52,801	52,801	55,899	240,076	240,076	115,989
1995	127,637	55,122	21,163	3,915	55,122	55,122	55,122	55,122	56,603	241,397	241,397	116,375
2000	130,411	55,783	21,325	3,915	55,783	55,783	55,783	55,783	56,991	242,213	242,213	116,541
2005	132,262	56,166	21,382	3,915	56,166	56,166	56,166	56,166	243,328	243,328	243,328	116,847
2010	135,225	57,006	21,630	3,915	57,006	57,006	57,006	57,006	244,404	244,404	244,404	117,126
2015	137,267	57,351	21,686	3,915	57,351	57,351	57,351	57,351	245,811	245,811	245,811	117,530
2020	141,876	59,518	22,516	3,915	59,518	59,518	59,518	59,518	246,369	246,369	246,369	117,633
2025	144,722	60,184	22,729	3,915	60,184	60,184	60,184	60,184	246,369	246,369	246,369	117,633
2030	146,900	60,808	22,875	3,915	60,808	60,808	60,808	60,808	246,369	246,369	246,369	117,633
2035	148,382	61,161	22,959	3,915	61,161	61,161	61,161	61,161	246,369	246,369	246,369	117,633
2040	150,355	61,551	23,066	3,915	61,551	61,551	61,551	61,551	246,369	246,369	246,369	117,633
2045	154,103	62,837	23,595	3,915	62,837	62,837	62,837	62,837	246,369	246,369	246,369	117,633
2050	155,888	62,264	23,724	3,915	62,264	62,264	62,264	62,264	246,369	246,369	246,369	117,633
2055	157,413	63,602	23,778	3,915	63,602	63,602	63,602	63,602	246,369	246,369	246,369	117,633
2060	158,344	63,718	23,811	3,915	63,718	63,718	63,718	63,718	246,369	246,369	246,369	117,633
2065	161,290	64,581	24,115	3,915	64,581	64,581	64,581	64,581	246,369	246,369	246,369	117,633
2070	163,801	65,591	24,495	3,915	65,591	65,591	65,591	65,591	246,369	246,369	246,369	117,633

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### SECTION 3

#### CONTINUUM ABSORPTION

Two different methods were used to obtain data on the continuum for self-broadening in the narrow windows. In the first method, a sample of H<sub>2</sub>O vapor was placed in the cell and several narrow spectral intervals containing a window were scanned. Additional H<sub>2</sub>O was added and the narrow intervals were re-scanned. The process was repeated for 3 to 5 pressures, requiring approximately four hours for a series of measurements. In the second method a single narrow interval was studied at a time. The sample was added to its maximum pressure as quickly as possible and the transmittance was measured. Transmittance was measured at four or five pressures as the pressure was decreased, with about 20 minutes required to make the series of measurements over a single interval. Data obtained by the second method were more self-consistent than the others. The results obtained by the two methods did not agree as well as expected, although the discrepancies were smaller than those observed in a previous study of the 2400-2900 cm<sup>-1</sup> region.

Only the first method was practical for samples contained in the large absorption cell. The cell is so large that it takes a lot of H<sub>2</sub>O and a long time to introduce a sample. The large vacuum pump used with the long cell vibrates the cell so that the mirrors must be readjusted each time the pump is operated. It is difficult to exactly duplicate the previous alignment, so it is impractical to use the same background curve for different samples obtained by removing a portion of the previous sample. Therefore, samples were changed by adding H<sub>2</sub>O to the previous one. Only 7 short spectral intervals were scanned by this method when using the long cell. The scans were repeated a few times for each sample to allow averaging. Several of the measurements were repeated by evacuating the cell and introducing a new H<sub>2</sub>O sample.



The second method was used for samples contained in the small multiple-pass cell. The cell is small enough that only a few minutes are required to fill the cell. The pump used to evacuate the cell is connected to it by rubber tubing and does not cause vibrations that affect the optical alignment.

Determining the continuum coefficients for pure H<sub>2</sub>O involved the application of Eqs. (1-2) and (1-5) to transmittance values observed at the points of maximum transmittance in the short spectral interval scans. We plotted values of  $(-1/u) \ln T$  at a given wavenumber versus  $p$  for a fixed temperature and path length. In accordance with the discussion of Eq. (1-5), we expect the plotted points to fall on a straight line that intersects the  $p = 0$  line at  $\kappa(\text{local})$  and has a slope equal to  $C_g^0$ . Two typical plots are shown in Fig. 3-1 for 1978.6 cm<sup>-1</sup>. This wavenumber is very close to one of the CO laser lines studied by Long et al.<sup>2</sup> The straight line fits the points well and passes near the origin. This result is expected for continuum absorption with little contribution due to local lines. Similar results were obtained at other wavenumbers and for samples at other temperatures.

Values of the continuum coefficient,  $C_g^0$ , for self-broadening are listed in Table 3-1 for four different temperatures and several wavenumbers. The symbol L adjacent to some of the wavenumber listings indicates that some local-line absorption had to be accounted for in order to determine the continuum coefficient at that position. The 322 K samples were contained in the long absorption cell; the others were in the short cell. A long path length was needed at 322 K in order to produce a measurable absorptance because the maximum H<sub>2</sub>O pressure was limited to approximately 0.07 atm by the H<sub>2</sub>O vapor pressure.

Several factors contribute to the errors in the results. One of the most important is the error in the assumed 100% transmittance curves (background). This error is obviously most serious when the absorptance is small. Noise, or short term fluctuations, also contribute. Additional uncertainty arises from errors in accounting for the local line absorption and the influence of the finite slitwidth of the spectrometer. The estimated errors are  $\pm 5\%$  for the majority of the values listed in Table 3-1. These results were obtained from plots of  $(-1/u) \ln T$  vs  $p$  that contain several points. Values of  $C_g^0$  in the table with an estimated error of  $\pm 10\%$  result from either of two types of data. Some result from plots of  $(-1/u) \ln T$  vs  $p$  with considerable scatter, or with only two or three points. Other values are based on the transmittance curves shown in Section 2. The majority of the values listed for 322 K were obtained from the transmittance curves of Samples 25 and 18.

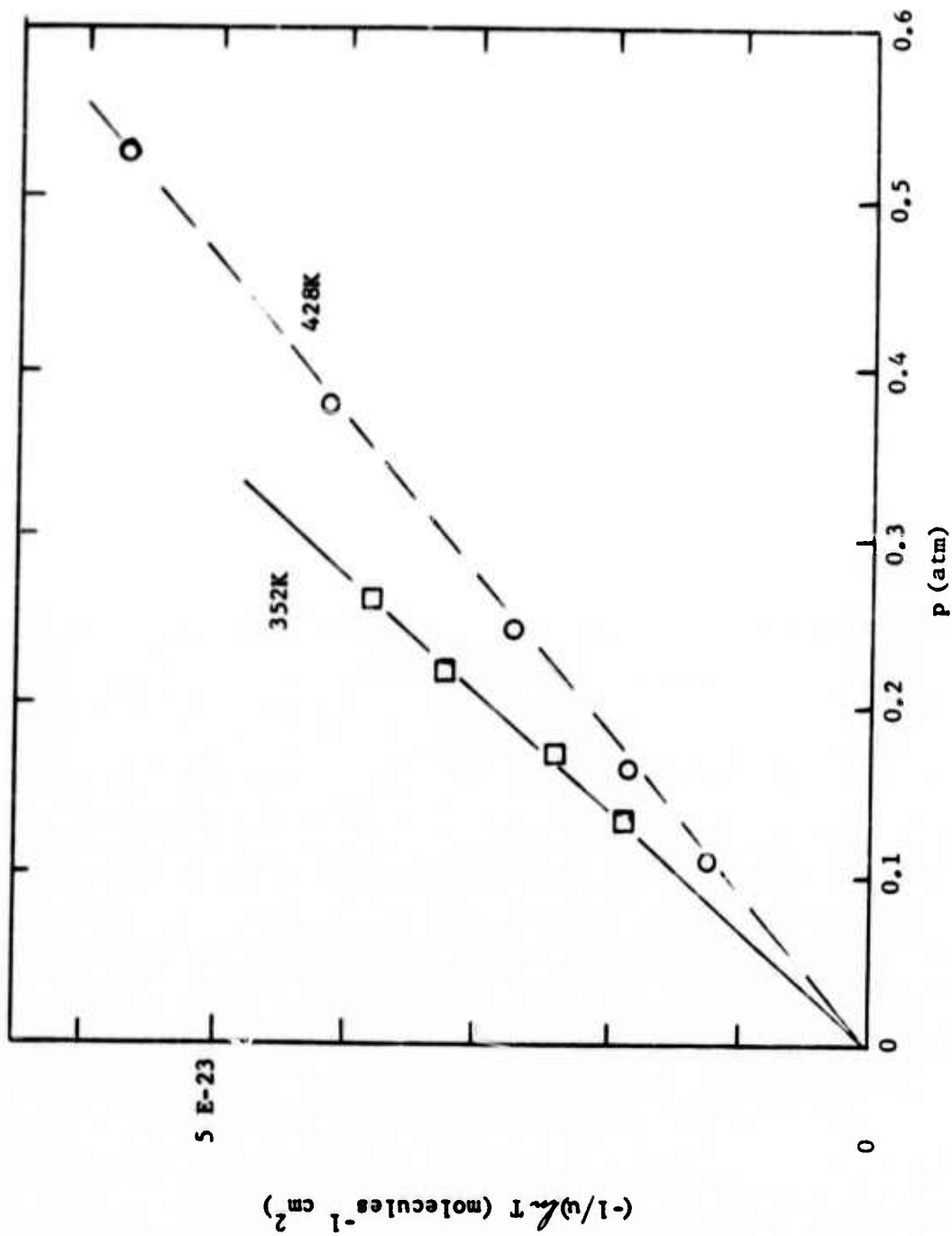


FIG. 3-1. Plots of  $(-1/u) \cdot T$  vs  $p$  at  $1978.6 \text{ cm}^{-1}$  for  $\text{H}_2\text{O}$  at 352 K and 428 K.

TABLE 3-1

SELF-BROADENING AND N<sub>2</sub> BROADENING COEFFICIENTS FOR DIFFERENT TEMPERATURES

ν cm <sup>-1</sup>	Multiply all values by 10 <sup>-24</sup> molecules <sup>-1</sup> cm <sup>2</sup> atm <sup>-1</sup>						B = C <sub>B</sub> <sup>o</sup> /C <sub>N<sub>2</sub></sub> <sup>o</sup>			
	C <sub>B</sub> <sup>o</sup>			C <sub>N<sub>2</sub></sub> <sup>o</sup>			428 K	353 K	308K	
	428 K	353 K	322 K	308 K	428 K	353 K	308 K			
1630.5		5040		8640		871	1040		5.8	8.3
1665.5		6120		10000		1100	1360		5.6	7.4
1691.5		8410		11900		1500	1820		5.6	6.5
1725.2		4250		6770		696	723		6.1	9.4
1765.0		4570		5350		695	688		6.6	7.8
1786.5		2810		3420		419	425		6.7	
1814.5		1490		1890		195	190 *		7.7	8.1
1839.8		1780		2160		283	297 *		6.3	9.9
1854.6 L	583	845			83.1	90		7.0	9.3	6.9
1882.0 L	419	560	724 *		57.0	58		7.3	9.6	
1900.0	371		619 *					6.5		
1905.6	488	600	808 *		84.5	91.5		5.8	6.6	
1920.5	1640		1900 *		296			5.5		
1927.1	433		654 *							
1929.2	281	342	478 *		42.9	41.0		6.6	8.4	
1931.3	285	372	488 *							
1948.2	344		514 *		46.4	37.7 *		6.2	9.9	
1952.6 L	199	247	284		29.7	26.3 *		6.7	9.4	
1959.0	222		342 *							
1962.8	238	283	392 *			39.5 *			7.2	
1974.0	118		204		16.7			7.1		
1978.5	108	144	190 *		13.7	12.5 *		7.9	11.5	
1983.8 L	139		218 *							
1990.0 L	766		905 *		159			4.8		
1997.4	164		222 *		27.5			6.0		
2002.3 L	93.1		157 *							
2006.4 L	139		172 *							
2008.8 L	272		330 *							
2011.8 L	122		172 *							
2029.3	61.8	77.7	105 *			6.2 *			12.5	
2036.1	80.7		110 *		12.2			6.6		
2045.3	125		137 *							
2055.5	40.4		72.5 *		5.55 *			7.3		
2056.0	39.1		74.8							
2071.1	43.1	52	70.5 *		6.65 *	4.5 *		6.5	11.5	
2083.6 L	37.8	42.5	59.3 *							
2102.4 L	20.2		35.0			3.8 *			11.2	
2109.6 L	22.6		47.9 *		3.0 *			7.5		
2130.7 L	18	20	37.1 *		1.9 *	1.7 *		9.5	11.8	
2133.0	21.1		38.2							
2169.8	8.8		25.1 *		1.2 *			7.3		
2196.7	7.0	11.8 *	23.2 *		.86 **	0.58 **		8.1	20	
2223.3 L	7.9		20							
2290.0			17.9							

Estimated errors for C<sub>B</sub><sup>o</sup> and C<sub>N<sub>2</sub></sub><sup>o</sup> are ± 5% except for values marked \* and \*\* which indicate ± 10% and ± 20%, respectively. Errors in B depend on the associated values of C<sub>B</sub><sup>o</sup> and C<sub>N<sub>2</sub></sub><sup>o</sup>.

## Influence of Nitrogen-Broadening on the Continuum

The earth's atmosphere contains much more  $N_2$  and  $O_2$  than  $H_2O$  so that the broadening of  $H_2O$  lines by  $N_2$  and  $O_2$  is generally more important than the self-broadening. Furthermore, the  $N_2$  concentration is approximately 4 times that of  $O_2$  and the continuum coefficient  $C_{O_2}^0$  is not expected to be greatly different from  $C_{N_2}^0$ . Therefore,  $C_{N_2}^0$  can probably be used for air in the place of a more accurate weighted average of  $C_{N_2}^0$  and  $C_{O_2}^0$ . No data were obtained with  $O_2$ .

In a typical measurement of  $C_{N_2}^0$  the spectrometer was adjusted to one of the narrow windows where the  $N_2$  continuum absorption dominates over the local-line absorption. A sample of  $H_2O$  was added to the cell until the transmittance dropped to about 80%. A spectrum was scanned over the window, and  $N_2$  was added in steps to produce transmittance of about 60, 45, 30, and 20%. The transmittance was measured at each pressure after the sample had mixed for several minutes. The total operation for all the pressures required between 20 and 30 minutes for a single window. We plotted  $(-1/u) (\ln T - \ln T')$  versus  $p_{N_2}$ , where  $T'$  is the transmittance of the pure  $H_2O$  sample. In accordance with Eq. (1-6) the points fell on a straight line drawn through the origin with a slope of  $C_{N_2}^0$ . The values obtained for three different temperatures are given in Table 3-1. The estimated errors for  $C_{N_2}^0$  are as high as 20% at some wavenumbers because the increase in  $N_2$  absorption resulting from the  $N_2$  was very small. The large errors were assigned to the values that were determined from  $(\ln T' - \ln T) < 0.05$ . The three right-hand columns in Table 3-1 list values of  $B = C_s^0 / C_{N_2}^0$  for three different temperatures.

In previous studies<sup>6,13</sup> we have found  $B$  to occur between 4 and 6 at wavenumbers where most of the absorption is due to lines centered within 5 or 10  $cm^{-1}$ . As can be seen in Table 3-1, values of  $B$  for the continuum may extend to higher values. The wider variation can probably be attributed to differences in the distances from the centers of the lines producing most of the absorption. At 1920.5  $cm^{-1}$ , for example, where the strong nearby lines are responsible for most of the absorption,  $B$  has a relatively low value of 5.5. In contrast, no strong lines occur within several  $cm^{-1}$  of 1978.5  $cm^{-1}$ ; therefore, a large fraction of the continuum at this point is probably due to lines centered more than 10  $cm^{-1}$  away. The corresponding value of  $B$  is much larger, 7.9 at 428 K and 11.5 at 353 K.

Variations in  $B$  are shown graphically by the curves of transmittance in Fig. 3-2. Sample 42 consists of pure  $H_2O$  in the small multiple-pass cell adjusted for a path length of 8.26 meters. For Sample 45 the cell was adjusted to 32.9 meters, and 0.0486 atm of  $H_2O$  was introduced to match the absorber thickness of Sample 42; then  $N_2$  was added to 0.5 atmospheres. To produce Sample 45,  $N_2$  was added to Sample 45 to a total pressure of 1 atm. Portions of two of the curves have been omitted where

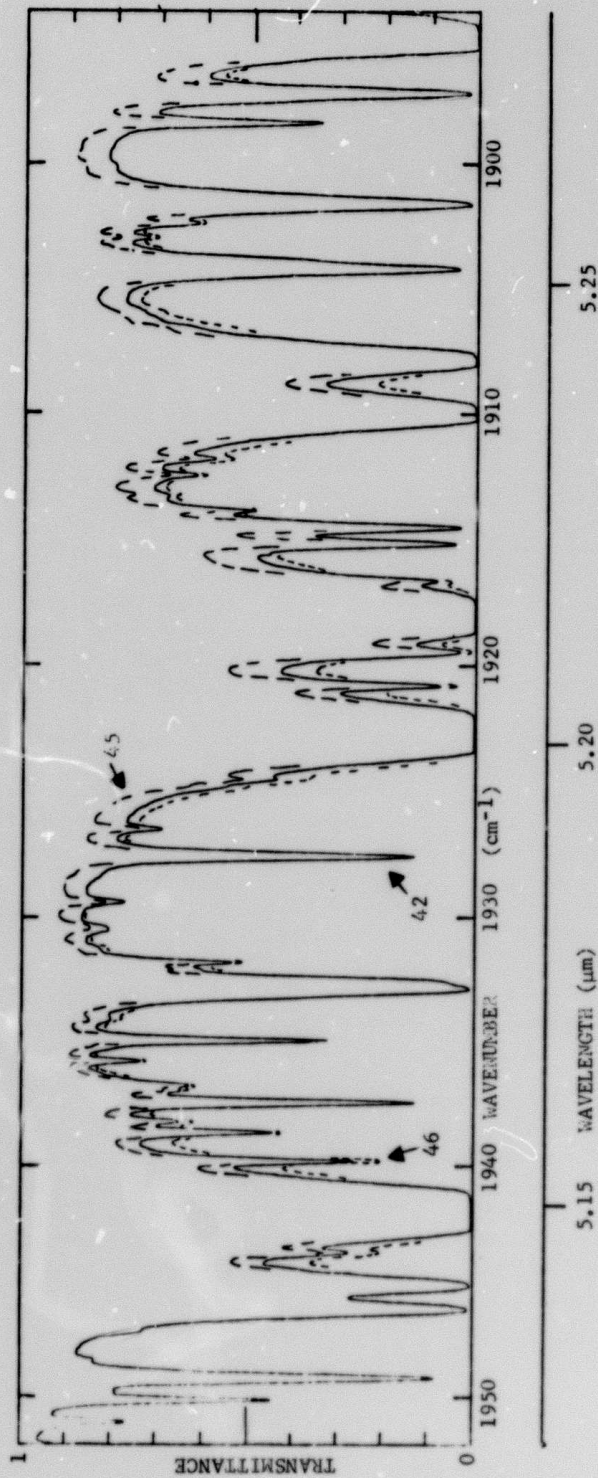


FIG. 3-2. Spectral curves showing a comparison of self-broadened and  $N_2$ -broadened  $H_2O$  lines. Spectral Slitwidth =  $0.19 \text{ cm}^{-1}$ .

Sample #	P :tm	P :tm	$\bar{v}$ K	$\bar{v}$ K	u molecules/cm <sup>2</sup>
42	0.195	0.195	428	428	27.6 E20
45	0.0486	0.5	428	428	27.6 E20
46	0.0486	1.0	428	428	27.6 E20

they are nearly coincident with the curve for Sample 42. All three samples have the same absorber thickness; therefore, any differences in the curves are due to differences in line width or shape. In the case of Sample 42 the lines are entirely self broadened, whereas the lines in Sample 45 and 46 are partially self broadened and partially  $N_2$  broadened. If the  $N_2$ -broadened lines had exactly the same shape as the self-broadened lines, we would be able to adjust the  $N_2$  pressure in a sample such as Samples 45 or 46 so that its spectral curve was coincident with that of Sample 42. Inspection of Fig. 3-2 shows that this is not possible. For example, near 1900 and 1930  $cm^{-1}$ , Sample 46 nearly matches Sample 42. By substituting the corresponding pressures in Eq. (1-7), we can show that this corresponds to  $B = 6.5$ . At the transmittance maxima near 1909 and 1919  $cm^{-1}$ , the value of  $B$  found by interpolation is very close to 5. At other points within the spectral interval shown where the curves are not too steep to measure accurately, the corresponding values of  $B$  lie between about 5.0 and 6.5.

Data similar to those shown in Fig. 3-2 were obtained in other portions of the spectra. As indicated in Table 3-1, larger values of  $B$  were observed in some of the windows at higher wavenumbers. Generally  $B \approx 5$  at places where most of the absorption can be attributed to lines centered within 5-10  $cm^{-1}$ . The value of  $B$  is consistently greater than 5 at points where a large fraction of the continuum results from lines centered more than 10  $cm^{-1}$  away. This result is consistent with previous work by Palmer<sup>14</sup> in the 250-500  $cm^{-1}$  region and with other work<sup>4,5,7,15</sup> in the 8-12  $\mu m$  window and the 4  $\mu m$  window.

The variation in  $B$  can be explained on the basis of a difference in the shapes of the extreme wings of  $N_2$ -broadened and self-broadened  $H_2O$  lines. Within about 5 or 10  $cm^{-1}$  of the centers, both types of lines apparently have similar shapes with the normalized half-width  $\alpha^0$  about 5 times as great for self-broadened lines as for  $N_2$ -broadened ones. However, beyond 5 or 10  $cm^{-1}$  from the centers, the absorption by self-broadened lines relative to  $N_2$ -broadened ones is apparently greater than it is near the centers. This corresponds to a larger value of  $\chi$  (in Eq.(1-4)) for the wings of self-broadened  $H_2O$  lines than for  $N_2$ -broadened lines.

Values of  $C_s^0$  at a given wavenumber are seen from Table 3-1 to decrease with increasing temperature. The temperature dependence generally cannot be explained by changes in the intensities and widths of the lines. Line widths decrease with increasing temperature, but not at sufficiently fast rate to account for the changes in  $C_s^0$ . Throughout most of the spectral region studied, the intensities of the lines increase with increasing temperature, an effect opposite to that required to explain the temperature dependence of  $C_s^0$ . The most probable explanation is a change in the shapes of the wings of the lines that can be represented by a decrease in  $\chi$  with increasing temperature. The largest

relative changes in  $C_s^0$  occur at wavenumbers where a significant portion of the absorption is due to distant lines. Thus, we conclude that the relative temperature dependence of  $\chi$  increases with increasing  $|\nu - \nu_0|$ .

At most of the wavenumbers investigated,  $C_{N_2}^0$  also decreases with increasing temperature. At those places where  $N_2$  this does not occur, the dependence can probably be explained by the increased intensities of the lines producing the absorption. The results generally indicate that  $\chi$  for  $N_2$ -broadened lines also decreases with increasing temperature, but at a slower rate than self-broadened lines. This accounts for the decrease in  $B$  with increasing temperature.

Long et al.<sup>2</sup> have measured the absorption coefficients at several wavenumbers for relatively dilute samples of  $H_2O$  in  $N_2$  at 1 atm total pressure. Their experimental values are from about 1.2 to 3 times as great as values calculated by using the line parameters of Benedict and Calfee<sup>1</sup> and the Lorentz line shape. The ratio of the experimental to the calculated values is generally less at points where the nearby lines ( $|\nu - \nu_0| < 10 \text{ cm}^{-1}$ ) contribute most of the absorption than it is at points where the absorption is due primarily to distant lines. At wavenumbers where direct comparisons can be made with room temperature data, we find good agreement between our values and the results of Long et al. At other wavenumbers where we have data only at elevated temperatures, we extrapolated curves of  $C_s^0$  and  $C_{N_2}^0$  to room temperature and, again, found good agreement with Long et al.<sup>2</sup> These results imply that the wings of  $N_2$ -broadened  $H_2O$  lines are "super-Lorentzian"; i.e., they absorb more than Lorentz lines having the same intensities and widths. ( $\chi > 1$  in Eq. (1-4).)

In summary, the results indicate that  $\chi$  is greater for the wings of self-broadened  $H_2O$  lines than for  $N_2$ -broadened ones, and that it is greater than unity for both types at the temperatures studied. Furthermore, the ratio of  $\chi$  for self-broadened lines to that for  $N_2$ -broadened ones increase with increasing distance from the line centers and with decreasing temperature.

## SECTION 4

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