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Foreign Technology Division Wright-Patterson Air Force Base, Ohio

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## FOREIGN TECHNOLOGY DIVISION



WEAK HARMONIC-SIGNAL DETECTION IN GAUSSIAN NARROW-BAND NOISE USING THE STATISTICS OF INTERVALS BETWEEN ZEROES

by

I. N. Yerimichoy and V. M. Koshevoy





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By: I. N. Verimichoy and V. M. Koshevoy

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\* ye initially, after vowels, and after T, E; e elsewhere. When written as ë in Russian, transliterate as y or ë. The use of diacritical marks is preferred, but such marks may be omitted when expediency dictates. ত হয় প্ৰথম জান দিবলৈ, প্ৰথম কি য় যে, বন্ধা প্ৰথম আৰু প্ৰথম বিশ্ব বিশ্ব বিশ্ব বিশ্ব বিশ্ব বিশ্ব বিশ্ব বিশ্ব বি

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### DESIGNATIONS OF THE TRIGONOMETRIC FUNCTIONS

Russian	English
sin	sin
COS	<b>≎08</b>
tg	ten
ctg	cot
50C	Sec
COSOC	CSC
sh	sinh
ch	cosh
th	tanh
cth	coth
sch	sech
cach	cach
arc sin	sin <sup>-1</sup>
arc cos	cos-1
arc tg	tan-1
arc ctg	cot <sup>-1</sup>
ATC SOC	sec-1
arc cosec	csc <sup>-1</sup>
arc sh	sinh-l
arc ch	ccsh-1
arc th	tanh-1
arc cth	coth-l
arc sch	sach-l
arc cach	cach-l
rot	curl
lg	log

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WEAK HARMONIC-SIGNAL DETECTION IN GAUSSIAN NARROW-BAND NOISE USING THE STATISTICS OF INTERVALS BETWEEN ZERJES

I. N. Yerimichoy and V. M. Kcshevoy Engineers

Recently there have appeared many works devoted to receivers in which a rigid limitation at the input is used. Systems for detecting a harmonic signal, which use optimum phase treatment of the input process [6], the numbers of passages through "zero" in a given time interval [1, 5], and moments of passage through "zero," were examined. <u>ilder Seiter and Seiter and Seiter and Seiter and Seiter and Seiter and Seiter and Seiter and Seiter and Seiter</u>

Let us examine the question of the optimum detection of a weak harmonic signal in narrow-band gaussian noise using the statistics of intervals between "zerdes." The problem is solved based on the theory of checking statistical hypotheses.

Beginning with the proposition of the nondependence of the access elements  $y = (y_1, y_2, ..., y_n)$ , let us write the probability ratio

 $l(y) = \frac{\prod_{i=1}^{n} \mathbf{w}_1(y_i/a)}{\prod_{i=1}^{n} \mathbf{w}_1(y_i)}.$ 

Let us determine the density of the probability of intervals between zeroes for the case of the presence of the useful signal. Let  $\xi(t)$  be the normal random process which is the sum of harmonic signal  $A_m \cos \omega_c t$  and narrow-band noi:: n(t) with a zero average and dispersion

$$E(t) = A_{a} \cos \omega_{c} t + n(t) = E(t) \cos [\omega_{c} t + \varphi(t)], \qquad (1)$$

The interval between adjacent zeroes involves a derivative from the phase of the random process by the following expression [7]:

$$=\frac{\pm z}{\Delta t}$$
 (2)

where

 $\Phi'=\bullet_c+\phi'.$ 

Since the probability of negative values  $\phi$ ' is very slight  $P(\phi < 0) \gtrsim 0$  [2], then

$$\tau = \frac{\pi}{\phi'} = \frac{\pi}{u_c + \varphi'}.$$
 (3)

Instead of  $\tau$  it is more convenient to examine the random magnitude  $y = \tau \frac{\omega_0}{\pi}$ , where  $\omega_0$  is the central frequency of the noise power spectrum.

$$y = \frac{w_0}{\pi} \frac{\pi}{w_c + v} = \frac{1}{1 - q\sqrt{k} + z\sqrt{k}},$$
 (3')

where  $x = \frac{\varphi'}{\omega_0}$ ;  $\omega_0 = \frac{1}{\sigma} \left[ \int_{\sigma}^{\sigma} (\omega - \omega_0) F(\omega) d\omega \right]^2$  - is the average square width of the noise spectrum, and  $k = \frac{\sigma_0^2}{c_0^2}$ ;  $q = \frac{\omega_0 - \omega_c}{\omega_0}$  - is the standardized detuning of the signal frequency from the central frequency of the noise spectrum.

Using equation (3') we can express the density of the probability of a random value of y in terms of the density of

random value x

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$$\Psi_1(y) = \phi_1(x) \left| \frac{dx}{dy} \right|. \tag{4}$$

The expression of the probability closeness  $\omega_1(x)$  for random process (1) is shown in the equation [4]:

$$\mathbf{e}_{1}(x/a) = \mathbf{e}_{0}(x) \left[ (1 + c^{\gamma}) I_{0} \left( \frac{a(1-\gamma)}{2} \right) + a_{1}I_{1} \left( \frac{a(1-\gamma)}{2} \right) I^{-\frac{a(1-\gamma)}{2}}, \quad (5)$$

where  $u_{\epsilon}(x) = \frac{1}{2} [1 + (q - x)^{\frac{3}{2}}]; v = \frac{x^{3}}{1 + (q - x)^{2}}; v = \frac{(1 + q^{3} - qx)^{3}}{1 + (q - x)^{2}}; a = \frac{x^{3}}{2a^{3}}$  is the ratio of signal power and noise power.

For low signal-to-noise ratios (a << 1), using the expansion of the Bessel and exponential functions, equation (5) can be rewritten as follows:

$$\mathbf{w}_{1}(x/a)_{\gamma} \simeq \mathbf{w}_{0}(\lambda) \left[ 1 - a \left( \frac{1}{2} + \frac{1}{2} \nu - \gamma \right) \right].$$
 (6)

Using formulas (3'), (4), and (6), we can write the probability density of the random magnitude y:

$$\Psi_{1}(y|a) = \Psi_{1}(y) \left\{ 1 - a \left[ 1 - q^{2} - \left( \frac{3}{2} + \frac{3q}{\sqrt{k}} - \frac{3}{2} q^{2} \right) v^{-1} + \frac{3q}{\sqrt{k}} (yv)^{-1} \right] \right\}, \quad (7)$$

where

$$W_1(y) = \frac{1}{2\sqrt{ky^2}} v^{-\frac{3}{2}}.$$
 (8)

The probability density of standardized intervals between zeroes in the absence of useful signal

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$$v = 1 + \frac{1}{k} \left( 1 - \frac{1}{y} \right)^3.$$
 (9)

The obtained probability density coincides with Byaliy's results [2], while for low signal-to-noise ratios it coincides with the result obtained in work [7].

Using equations (7) and (8), let us write the logarithm of the probability ratio

$$\ln l(y) = \sum_{i=1}^{n} \ln \left\{ 1 - \alpha \left[ 1 - q^3 - \left( \frac{3}{2} + \frac{3q}{\sqrt{k}} - \frac{3}{2} q^3 \right) v^{-1} + \frac{3q}{\sqrt{k}} (y_i v_i)^{-1} \right] \right\} > C, \qquad (10)$$

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where C is the threshold selected in accordance with the accepted criterion,  $n = 2T\Delta F$ , where n is the volume of independent selections of the instantaneous values of the process, T is observation time, and  $\Delta F$  is the width of the output-process energy spectrum.

If we limit curselves to the first terms of the expansion  $\ln l(y)$  (which is admissible for low values of a), expression (10) is rewritten in the following form:

$$\sum_{i=1}^{nb} \left[ \left( \frac{3}{2} + \frac{3q}{\sqrt{k}} - \frac{3}{2} q^2 \right) v_i^{-1} - \frac{3q}{\sqrt{k}} (y_i v_i)^{-1} \right] >$$

$$> bn (1-q)^2 + \frac{1}{q} C = C_1.$$
(11)

where b is the ratio of the interval of the nondependence of scattering durations to the magnitude  $\frac{1}{2\Lambda F}$ .

Let us designate the expression under the sum sign in formula (11) by  $f(y_i)$ . Then the optimum procedure of the treatment is written

$$\sum_{i}^{r} f(y_{i}) > C_{i}. \tag{12}$$

4

If the access volume is large (bn >> 1), the distribution of the sum of independent random magnitudes  $\sum_{j=1}^{\infty} f(y_j)$  is close to the normal value with the average

if there is no useful signal, and with the average value  $\lim_{i \in \mathcal{I}_{4}} \{14\}$ 

when there is a useful signal, where

$$m_1\{\eta\} = \int_0^{\infty} f(y) \Psi_1(y) \, dy; \qquad (15)$$

$$m_{1} \{\tau_{z}\} = \int_{0}^{\infty} f(y) \Psi_{1}(y/a) dy = m_{1} \{\tau_{i}\} - \frac{1}{2} - \frac{1}{2} (1 - q^{2}) m_{1} \{\tau_{i}\} + am_{1} \{\tau_{i}^{2}\}, \qquad (16)$$

and with dispersion if there is no useful signal

$$bn (m_1 \{\eta^2\} - m_1^2 \{\eta\})$$
(17)

Since a << 1, dispersion (17) as assumed to be identical for the cases of the absence and presence of a signal.

Using formulas (13), (14), and (17), we can write the probability of a false alarm  $p_{r,r}$  and correct observation  $p_{n,s}$ :

where  $F(z) = \frac{1}{2\pi} \int_{-\infty}^{z} t^{-\frac{t^{2}}{2}} dt$ .

From equations (18) and (19) we can find n<sub>0.0</sub> (the access volume necessary to observe a signal with probability p<sub>1.0</sub> with a given value of  $p_{n,T}$  and  $\frac{p_c}{p_m} = a;$ 

$$n_{\mu,0} = \frac{1}{b} \frac{m_1 \{\tau^2\} - m_1^2 \{\tau_i\}}{[m_1 \{\tau_i^2\} - (1 - q^2) m_1 \{\tau_i\}]^2} \times \frac{1}{a^2} [\arg F(1 - p_{\mu,\tau}) - \arg F(1 - p_{\mu,0})]^2, \qquad (20)$$

where arg F(z) = t, if F(t) = z.

For the optimum amplitude (square) detector the access volume is written in the following form [6]:

$$n_{e,0} = \frac{2}{a^2} \left[ \arg F(1 - p_{a,T}) - \arg F(1 - p_{a,Q}) \right]^2, \qquad (21)$$

The relative asymptotic effectiveness [3] of the interval optimum detector relative to the amplitude optimum is written as:

$$l_{n,0,2,0} = \lim_{\substack{n_{n,0} \\ n_{n,0}}} \frac{\pi_{n,0}}{\pi_{n,0}} = \frac{2b[m_1\{\tau^3\} - (1 - c^{2})m_1\{\tau\}]^2}{m_1\{\tau^3\} - m_1^3\{\tau\}}$$
(22)

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The results of calculating the standardized relative asymptotic effectiveness  $\frac{l_{10}, ..., ..., ...}{b}$  and  $m_1(y^2)$  for various values of q and k = 0.01 (for 0.01 and 0.001 the results practically coincide) are shown in the table.

The graph shows the dependence of the standardized relative asymptotic effectiveness on detuning the signal frequency relative to the central frequency of the noise energy spectrum.

The dimensionless quantity q is plotted along the horizontal axis from -1.8 to +1.8, while the dimensionless quantity  $i_{n.0.2.0}$  is plotted on the vertical axis from 0 to 11. The figures 3, 6, and 9 are to values of the corresponding points of the vertical axis.

From the above graph it can be seen that with an increase in the absolute detuning value, the noiseproof quality of the interval optimum detector increases. To quantitatively evaluate the noiseproof ruality of the interval detector it is necessary to know the value of b.

To calculate b it is necessary to find the correlation function of the intervals between zeroes.

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It we assume that the interval of independence for intervals between zeroes and the phases of the random processes coincide (b = 2), for the signal coinciding with the edge of the square frequency characteristic curve of the filter (q =  $\pm 1.76$ ), ላይችው በዚህ በዚህ የስት አስት የሰላ በዚህ በዚህ የሚያስት በዚህ የስት የስት የስት የስት በዚህ የስት በዚህ የስት በዚህ የስት በት የስት በት የስት በት በት እስ በት እ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እስ በት እ

Thus, under this assumption the noiseproof quality of the optimum Graph of the dependence of the standardized relative

asymptotic effectiveness on detuning the signal frequency.



Interval detector is substantially higher than the noiseproof quality of the amplitude detector.

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