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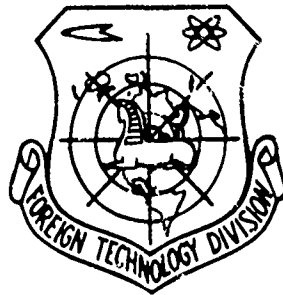
FOREIGN TECHNOLOGY DIVISION



APPROXIMATION METHOD FOR THE CALCULATION OF
TEMPERATURE IN A MICROCIRCUIT

by

F. A. Gur'yanova and S. A. Nikitin



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13. ABSTRACT <p>An approximation method is given for calculating the temperature distribution on the support for an integral microcircuit when there is a large number of heat-releasing sources on the support and the knowledge of the average surface temperature of the support is insufficient. Formulas and graphs are given and on the basis of their explanation a sequence is given for the approximate computation of temperatures in a microcircuit. The results are compared with data obtained on a computer and from an experiment.</p>			

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Block	Italic	Transliteration	Block	Italic	Transliteration
А а	<i>А а</i>	A, a	Р р	<i>Р р</i>	R, r
Б б	<i>Б б</i>	B, b	С с	<i>С с</i>	S, s
В в	<i>В в</i>	V, v	Т т	<i>Т т</i>	T, t
Г г	<i>Г г</i>	G, g	У у	<i>У у</i>	U, u
Д д	<i>Д д</i>	D, d	Ф ф	<i>Ф ф</i>	F, f
Е е	<i>Е е</i>	Ye, ye; E, e*	Х х	<i>Х х</i>	Kh, kh
Ж ж	<i>Ж ж</i>	Zh, zh	Ц ц	<i>Ц ц</i>	Ts, ts
З з	<i>З з</i>	Z, z	Ч ч	<i>Ч ч</i>	Ch, ch
И и	<i>И и</i>	I, i	Ш ш	<i>Ш ш</i>	Sh, sh
Й й	<i>Й й</i>	Y, y	Щ щ	<i>Щ щ</i>	Shch, shch
К к	<i>К к</i>	K, k	Ъ ъ	<i>Ъ ъ</i>	"
Л л	<i>Л л</i>	L, l	Ы ы	<i>Ы ы</i>	Y, y
М м	<i>М м</i>	M, m	Ь ь	<i>Ь ь</i>	'
Н н	<i>Н н</i>	N, n	Э э	<i>Э э</i>	E, e
О о	<i>О о</i>	O, o	Ю ю	<i>Ю ю</i>	Yu, yu
П п	<i>П п</i>	P, p	Я я	<i>Я я</i>	Ya, ya

* ye initially, after vowels, and after ъ, ь; e elsewhere.
 When written as ѐ in Russian, transliterate as э or ѐ.
 The use of diacritical marks is preferred, but such marks
 may be omitted when expediency dictates.

APPROXIMATION METHOD FOR THE CALCULATION OF TEMPERATURE IN A MICROCIRCUIT

F. A. Gur'yanova and S. A. Nikitin

During the designing of integral microcircuits in a number of cases the knowledge of the average surface temperature of the support on which the components are arranged proves to be insufficient and knowledge of temperature at isolated points of its surface is necessary.

The computation of the temperature distribution on support, when on it large number of heat-releasing sources are arranged, represents a sufficiently complex and laborious problem which is usually solved with the use of a computer. However, a simple engineering procedure which makes it possible, rapidly and with satisfactory accuracy, to obtain information about the temperature at various points of a microcircuit is of definite interest.

A fine support (isotropic plate) is examined and the temperature differences in depth can be disregarded. This assumption is correct when the minimum size of the heat-releasing source is greater than the thickness of the support. The disregard of the temperature distribution in the depth of support for sources, one of dimensions of which is less than the thickness of the support,

gives rise to errors in determining the temperature on source, which apparently explains to some degree the divergence of results of calculation according to the proposed procedure and from experiment.

The support is found under conditions of free convection and in the range of temperatures in which microcircuits usually work it is possible to consider the heat-transfer coefficient independent of temperature. Its magnitude is calculated as the mean value of the heat-transfer coefficients from both sides of the support. The coefficient of thermal conductivity is taken independent from temperature. As a result of the thinness of support the convective heat removal from the ends can be disregarded.

For the indicated assumptions the stationary temperature distribution on the support can be described by the equation [2]

$$\frac{\partial^2 U(x, y)}{\partial x^2} + \frac{\partial^2 U(x, y)}{\partial y^2} - \kappa^2 U(x, y) = 0 \quad (1)$$

with the following boundary conditions:

$$\begin{aligned} \frac{\partial U(x, y)}{\partial n} \Big|_z &= 0, \\ -\lambda \frac{\partial U}{\partial n} 2(l_x + l_y) &= Q, \end{aligned} \quad (2)$$

$$Q = \oint_S \alpha U(S) dS,$$

where $U(x, y)$ - temperature gradient at a point with coordinates x, y with respect to the surroundings;

α - coefficient of heat transfer from the surface of the support;

λ - coefficient of thermal conductivity;

δ - thickness of support;

$2(l_x + l_y)$ - the perimeter of the heat source;

Q - heat flux of the source;

Σ - ends of support;

S - area of support;

$$x^2 = \frac{a}{\lambda \delta}.$$

Using numerical methods on an M-20 computer S. A. Volkov obtained the solution of equation (1) with boundary conditions (2). The dimensions and coordinates of heat-releasing sources were arbitrary and were considered assigned, the thermal conductivity from the surface of source as a result of the smallness of the latter was not considered, and it was assumed that all the heat is drawn into the support. The approximate temperature distribution in a rectangular plate is given in work [1]. Specifically, if in the center of the support with sides L_x and L_y there is a heat-releasing source of a rectangular form, the sides of which are parallel to sides L_x and L_y and are equal respectively to l_x and l_y , then for temperature on the boundary of source the following expression is given

$$\Delta t = \frac{Q}{2\pi\lambda} \varphi(p, \gamma),$$

where Q - power of the source;

$$\varphi(p, \gamma) = \frac{1}{\pi p} \frac{I_1(\gamma) K_0(\gamma p) + K_1(\gamma) I_0(\gamma p)}{I_1(\gamma) K_1(\gamma p) - K_1(\gamma) I_1(\gamma p)}; \quad (3)$$

$$p = \frac{2l_n}{\sqrt{L_x^2 + L_y^2}}; \quad (4)$$

$$\gamma = \sqrt{\frac{\pi L_x L_y}{\pi \lambda \delta}} \sqrt{\frac{1 - \frac{l_x l_y}{L_x L_y}}{1 - p^2}}; \quad (5)$$

$l_n = \min\{l_x, l_y\}.$

Using the same principle - replacement of the real support of rectangular form by the equivalent plate of a circular form, as in G. N. Dul'nev's work [1], S. A. Volkov and Yu. A. Sher obtained the following expressions:

$$p = \frac{l_n}{\sqrt{L_x^2 + L_y^2}}, \quad (6)$$

$$\gamma = \sqrt{\frac{\pi L_x L_y}{\pi \lambda \delta}} \sqrt{\frac{\sqrt{\pi l_x l_y}}{l_x + l_y} \frac{1}{1-p^2}}. \quad (7)$$

In the derivation of these relationships instead of the requirements for the equality of thermal conductivities λ , thickness δ , and the perimeters of the heat-releasing sources of real and equivalent bodies the requirement was advanced for the equality of the areas of heat-releasing sources $l_x l_y = \pi r_0^2$ and the average heat fluxes from the center of the source to the edges of the support

$$\lambda \frac{\theta_{\text{max}} - \theta_{\text{min}}}{\sqrt{(L_x/2)^2 + (L_y/2)^2}} = \lambda_0 \frac{\theta_{\text{max}} - \theta_{\text{min}}}{R},$$

where r_0 - radius of the source of an equivalent plate;
 R - a radius of equivalent plate.

Under the condition of numerical agreement of average temperature indices of real and equivalent bodies, i.e., when

$$\theta_{\text{max}} - \theta_{\text{min}} = \theta_{\text{max}} - \theta_{\text{min}}$$

we obtain the expression

$$\frac{2\lambda}{\sqrt{L_x^2 + L_y^2}} = \frac{\lambda_0}{R}.$$

Table 1.

Values being calculated	Dimensions of support, cm.												$\frac{1}{\lambda} \cdot \frac{1}{c\pi}$			
	$L_x = 4.8; L_y = 5.0$			$L_x = 2.4; L_y = 3.0$			$L_x = 2.0; L_y = 4.8$									
	a	b	c	a	b	c	a	b	c	a	b	c				
f		0.045	0.023			0.031			0.015			0.025			0.012	
γ	1.37	1.68	1.59	1.82	0.84	0.75	1.71		0.75			0.97			0.89	
Error, %		32	14		4	22			22			6			13	0.0154
γ	1.24	2.3	2.18	1.56	1.15	1.02	1.46		1.02			1.33			1.22	
Error, %		35	15		16	9			9			12			9	0.0288
γ	1.12	3.25	3.41	1.36	1.63	1.45	1.26		1.37			1.87			1.72	
Error, %		39	22		30	7			7			17			6	0.0575
γ	1.0	4.59	4.37	1.22	2.31	2.05	1.12		1.18			2.65			2.43	
Error, %		41	22		26	3			3			19			5	0.115

*The errors of computation were determined relative to data obtained on a computer.

Table 1 gives the dimensionless temperatures

$$\phi = \frac{\Delta t \lambda s}{Q},$$

where Δt - temperature gradient on the boundary of source relative to the surrounding medium.

The values of dimensionless temperature ϕ are obtained from the solution of a problem of calculating the temperature on the boundary of a source arranged in the center of rectangular support by the following:

a) by means of solving on a computer the equation (1) with boundary conditions (2) for a source of rectangular form;

b) by means of computation of dimensionless temperature using formula (3) with parameters computed using formulas (4) and (5);

c) by means of computation of dimensionless temperature using formula (3) with parameters computed using formulas (6) and (7).

The mean value of the error of calculations for the variants, which are presented in Table 1, is 23% for method b and 12% for method c. Therefore in the subsequent calculations of $\phi(\gamma, p)$ the computation of p and γ is made using formulas (6) and (7).

When on a support the source occupies any intermediate position between angular, lateral and central its temperature can be calculated with the help of dimensionless criterion N , determined by formulas [1]:

$$N = N_1 \operatorname{ch} \left(\frac{d_1}{d_{12}} \operatorname{Arch} \frac{N_1}{N_2} \right) \text{ when } N_2 > N_1, \quad (8)$$

$$N = N_2 \operatorname{ch} \left(\frac{d_2}{d_{12}} \operatorname{Arch} \frac{N_1}{N_2} \right) \text{ when } N_1 > N_2.$$

where d_1 - the distance between sources with criteria N_1 and N ;
 d_2 - the distance between the sources with criteria N_2 and
 N ;
 d_{12} - the distance between the sources with criteria N_1 and
 N_2 .

If the source is located in the center of the support, then
 N is connected with φ by the expression

$$N = \frac{1}{2} \varphi(\rho, \gamma). \quad (9)$$

Sources with criteria N_1 , N_2 , N should be arranged in such
a way that their centers lie on one straight line. The criteria
of sources located in the center, on the side, and in the corner,
are connected by the relationship [1]

$$N_x : N_y : N_z = 1 : 2 : 4.$$

Substituting in (8) instead of criteria N_1 and N_2 the criterion
for the central, lateral, and angular positions of a source, it
is possible to calculate the family of curves which represents
the location of sources which have an identical dimensionless
criterion N (Fig. 1). An analogous problem was also solved on
a computer, for which the source was placed in various places
on the support (Fig. 2). It is evident from Fig. 1 that there is
considerable difference in the results obtained using the
approximation formulas (8) and from the exact solution of the
problem on a computer. Therefore in the subsequent calculations
the criteria N obtained on a computer will be used.

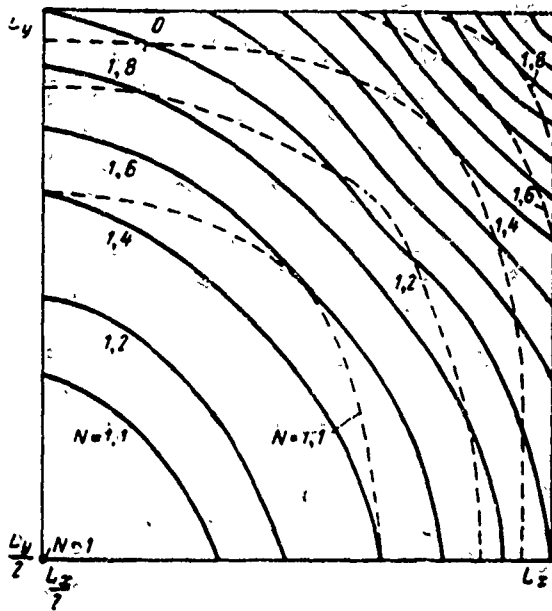


Fig. 1. Comparison of the results of the calculations of dimensionless criteria, N obtained using formula (8) (—) and on a computer (---).

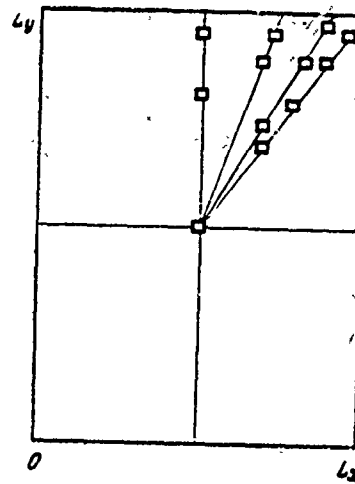


Fig. 2. The location of sources on a support during calculations on a computer.

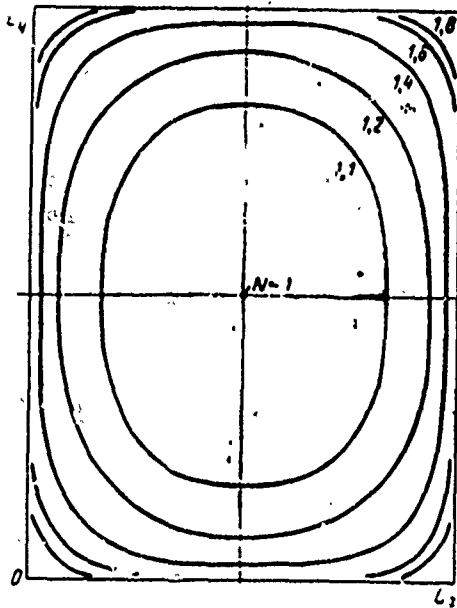


Fig. 3. The dependence of dimensionless criterion N on the location of the source on a support with the dimensions 4.8×6.0 cm (M 1.25: 1).

Figure 3 gives the curves which characterize the dependence of dimensionless criterion N on the location of the source on the support. The calculations for the determination of this dependence were performed for three dimensions of the support 4.8×6.0 cm, 2.4×3.0 cm and 2.0×4.8 cm, and showed that dependences $N(x, y)$, constructed in relative coordinates, i.e., $N\left(\frac{x}{L_x}, \frac{y}{L_y}\right)$, coincide for these dimensions of supports.

The graphs depicted in Fig. 3 make it possible to determine the temperature gradient on a source arranged in an arbitrary point with coordinates x and y on a support with dimensions L_x and L_y , referred to the temperature gradient on a source arranged in the center of a support. For this in Fig. 3 new coordinates are given for the heat-releasing source x' , y' which are connected with the following assigned relationships:

$$x' = 1,25 \frac{4,8}{L_x} x, \quad y' = 1,25 \frac{6,0}{L_y} y. \quad (10)$$

where x , y , L_x , L_y are expressed in centimeters and the value of dimensionless criterion N is determined. If necessary linear interpolation is conducted.

Computer calculations of the temperature field of a single source located in various places of a rectangular support showed that the isotherms represent ellipses which are distorted only in the vicinity of the source and at the edges of the support. The axes of the ellipses are parallel to the edges of the support and are related to each other approximately as the square of the corresponding sides of the support. Such a nature of isotherms in practice does not depend on the location of the source on the support. Consequently the simple scale conversion of support converts ellipse-isotherms into circumference-isotherms. This conversion makes it possible to present the temperature field of a single source in the form of the function of one coordinate Δr - the distance of the source on the converted support.

Figures 4 and 5 depict the dependence of the standardized temperature of support m in the function of distance from the source Δr for three directions - horizontal, vertical and diagonal, and for three positions of sources - central, lateral, and angular. Temperatures are standardized to temperature on the source.

Coordinates y in these figures are multiplied by the value $(L_x/L_y)^2$. From an examination of Figs. 4 and 5 it may be concluded that the form of the isotherms is close to circumferences.

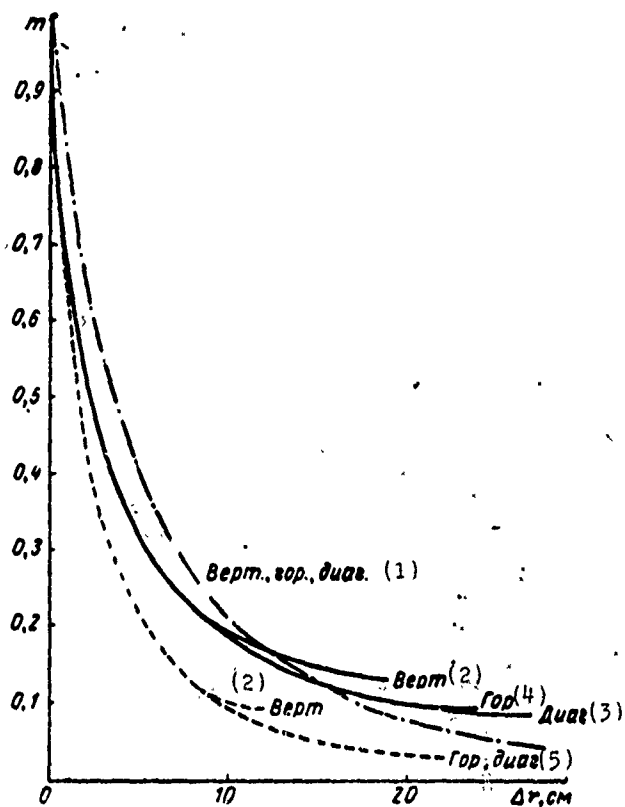


Fig. 4. The dependence of standardized temperature of supports on the distance Δr in a horizontal, vertical, and diagonal directions. The dimensions of the supports are 4.8×6.0 cm and 2.4×3.0 cm: — central; --- lateral; - - - angular location of source. KEY: (1) Vert., hor., diag.; (2) Vert.; (3) Diag.; (4) Hor.; (5) Hor., diag.

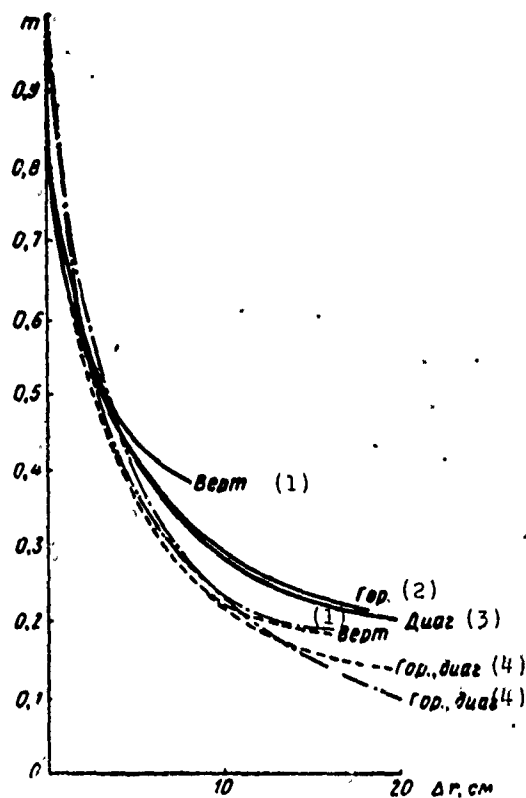


Fig. 5. The dependence of the standardized temperature of the support 2.0×4.8 cm on the distance Δr in horizontal, vertical, and diagonal directions: — central; --- lateral; - - - angular location of source. KEY: (1) Vert.; (2) Hor.; (3) Diag.; (4) Hor., diag.

Figure 6 depicts the dependences of standardized temperature m on the distance Δr on a converted support with the dimensions 4.8×6.0 cm at different values of the coefficient $\kappa = \alpha/\lambda\delta$.

Also written down in this figure are the temperature values calculated for other dimensions of supports and coefficients κ^2 . It is easy to see that agreement of temperatures is observed when there is agreement of values $\kappa^2(L_x^2 + L_y^2)$, i.e., agreement of Biot's criteria.

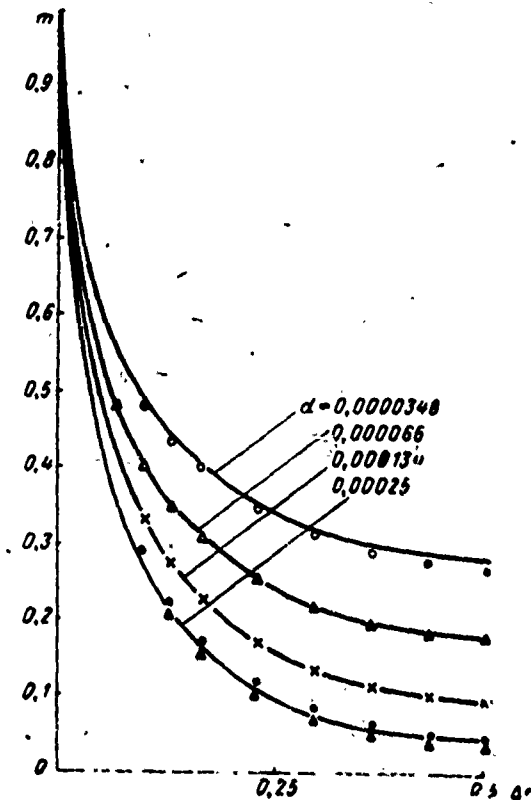


Fig. 6. The dependence of standardized temperature m on the distance Δr for a support with the dimensions of 4.8×6.0 cm: \circ - dimensions of support 2.4×3.0 cm, $\alpha = 0.000134$; Δ - dimensions of support 2.4×3.0 cm, $\alpha = 0.00025$; \bullet - dimensions of support 1.6×6.0 cm, $\alpha = 0.000382$; \blacktriangle - dimensions of support 4.8×4.8 cm, $\alpha = 0.000322$; here α [cal/cm²·deg].

Figure 7 shows the family of dependences of standardized temperature on the distance from the source in a converted support for the various values of Biot's criterion. From Fig. 7 it is

possible to determine temperature at distance Δr from the source if the temperature on the source itself and the value of Biot's criterion $\alpha/\lambda\delta(L_x^2 + L_y^2)$ are known.

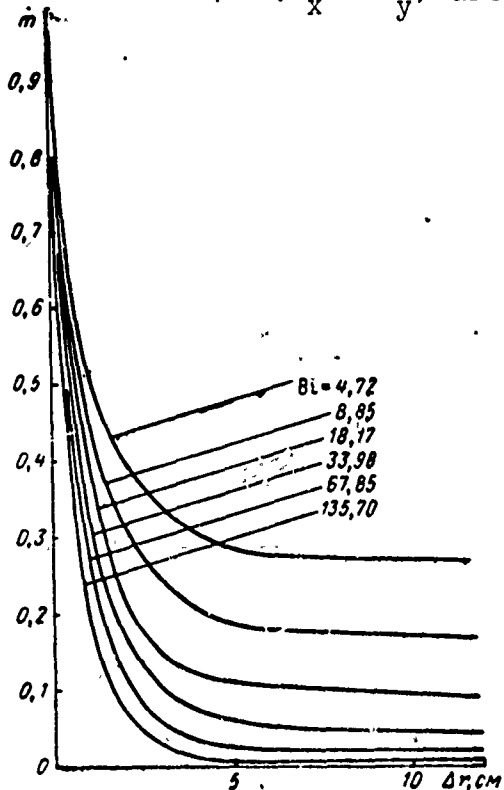


Fig. 7. The family of dependences of standardized temperature on the distance Δr .

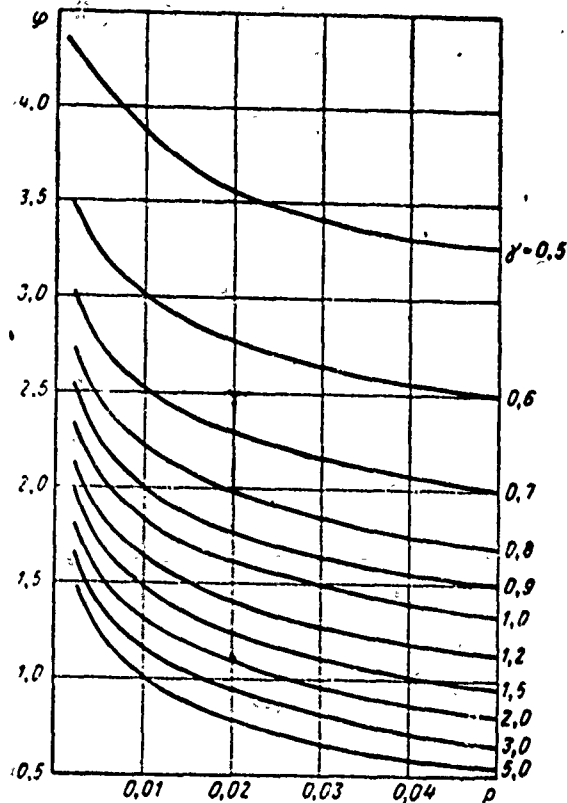


Fig. 8. Dependence of φ on p at different values of γ .

On the basis of what was expounded above it is possible to compile the following sequence for the approximate computation of temperatures in a microcircuit.

1. Using formulas (6) and (7) for every source γ_i and p_i (i - the number of source) are determined and using formula (3) or from the graph in Fig. 8 the values of dimensionless temperatures φ_i are found.

Using the formula

$$\Delta t_i = \frac{Q_i \varphi_i}{2\lambda\delta}$$

the value of temperature on every source is determined.

2. On tracing paper a rectangle is traced with sides 6 cm along the axis Ox and 7.5 cm along the axis Oy, in which the coordinates of heat-releasing sources are written as calculated using the formulas

$$x'_i = 6 \frac{x_i}{L_x} \text{ [cm]},$$

$$y'_i = 7.5 \frac{y_i}{L_y} \text{ [cm]},$$

where x_i, y_i - the true coordinates of heat-releasing sources;

L_x, L_y - the actual sizes of the support. The figure obtained on tracing paper is superimposed on Fig. 3 and for every source the value N_i is found (if necessary linear interpolation is conducted).

For every source the value of $\Delta t_i N_i$ is determined.

3. On a drawing grid a rectangle is constructed with the dimensions of 12 cm along the axis Ox and $12 \frac{L_x}{L_y}$ cm along the axis Oy. In this rectangle the coordinates of sources are calculated using the formulas:

$$x''_i = 12 \frac{x_i}{L_x} \text{ [cm]},$$

$$y''_i = 12 \frac{y_i}{L_y} \left(\frac{L_x}{L_y} \right)^2 \text{ [cm]}$$

and on this figure the distances between the point at which the temperature is calculated (let us assume the point with coordinates x_j, y_j) and the heat-releasing sources Δr_{ji} (in cm) are found.

We compute the value of Blot's criterion $\alpha/\lambda\delta(L_x^2 + L_y^2)$, we find from the graph (Fig. 7) that curve on which the dependence of the temperature on distance will be calculated, and we determine value $m_{ji}(\Delta r_{ji})$.

We compute the value of $\Delta t_i N_i m_{ji} (\Delta r_{ij})$.

4. The temperature difference in the point which interests us is found by using the formula

$$\Delta t_j = \sum_{i=1}^k \Delta t_i N_i m_{ji} (\Delta r_{ji})$$

where k - the number of heat-releasing sources.

The value of the temperature is defined as

$$t_j = t_c + \Delta t_j$$

where t_c - the temperature of the surrounding medium.

Table 2 gives the results of the calculation of temperature at the points of location of 14 sources by the expounded procedure and a comparison is made with the results of calculation on a computer.

Table 2.

t_i in solution on computer, °C	50	52	54	56	56	56	58	57	57	57	54	48.5	49.5
t_i in approximate solution, °C	52	52	54	57	56	56	56	56	58	57	60	50	51

Table 3 gives the results of the calculations of temperature of a microcircuit with six heat-releasing sources which were obtained on a computer and by an approximate procedure, and their comparison with the results of an experiment (temperatures were calculated at the points of the location of the sources).

Table 3

t_i in solution on a computer, °C	32	30	29	29	29	29
t_i in an approximate solution °C	35.0	30.0	26.8	23.5	23.1	23.6
Experimental value t_i , °C	29.3	27.8	27.4	27.2	27.2	27.2
Error of solution on a computer, %	9	8	6	7	7	7
Error of approximate solution, %	19	8	2	14	15	13

The calculations conducted show that the approximate procedure has an accuracy which is acceptable for engineer calculations and is distinguished by a high degree of simplicity and it can be recommended for calculations of the temperature fields of hybrid integral microcircuits with film resistors as heat-releasing sources.

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