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HELICOPTER NOISE SYMPOSIUM

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SEPTEMBER 28-30, 1971

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DURHAM'S HOTEL AND MOTEL DURHAM NORTH CAROLINA

Sponsored by:

U. S. Army Research Office-Durham

American Helicopter Society, Incorporated

HELICOPTER NOISE SYMPOSIUM

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Sponsored by: U. S. Army Research Office—Durham American Helicopter Society, Incorporated SEPTEMBER, 1971

FOREWORD

In these days much of the interest and activity of scientists, engineers and even laymen is directed toward the elimination of those by-products of an exploding population and burgeoning technology that are detrimental to the health and well being of the populace. One hears much of the man-made perturbations of the ecology and the environment. One hears even more about those elements contributing to those perturbations; elements such as air, water and solid pollutants.

Among trees problems is another which has received less attention but in terms of its insidious effects may approach the others in importance. This is the ever present intrusion upon the conscicus and maybe upon the subconscious human mind of sound. Not the sound of the mountain brook or symphony but the random and raucous cacophony produced by much of our technology in action. Except when such sound evidences itself in abnormal frequencies and amplitudes, one is not conscious that we live with it continuously. What effect it has on our serenity and our ability to concentrate is probably not too well known. Nevertheless, if we are to have a well-balanced and tranquil life, it is necessary that we understand how such undesirable vibrations are initiated, how they influence our lives and what we can do to suppress or eliminate them.

This meeting devoted to the source and suppression of sounds associated with a single type of aerial vehicle is not directed toward the more general subject but it is hoped that the information evolving from these efforts will be applied to the specific case of the vehicle in question and will at the same time make a worthwhile contribution to the recolution of the larger, more comprehensive problem.

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INTRODUCTION

In 1968, scientists of the United States Army Research Office, Durham, North Carolina (ARO-D), and members and staff of the National Academy of Sciences and National Academy of Engineering, identified an urgent need for renewed effort toward suppression of helicopter and V/STOL noise in military operations. Academy studies also noted that short-haul commercial aviation was expected to grow rapidly over the next few years with increasing noise abatement problems.

Subsequently, a conference on the subject of helicopter and V/STOL noise generation and suppression was jointly sponsored on July 30-31, 1968 by ARO-D and the National Academy of Sciences and National Academy of Engineering. An NAS-NAE report entitled, "Helicopter and V/STOL Noise Generation and Suppression", November 1968, summarized the findings of this conference and identified important areas of research.

In response to the findings of the July 1968 assessment meeting, ARO-D initiated in July 1969, a Helicopter Noise Investigation Program with six new projects. At the inception of this program, a coordination meeting was held at ARO-D to encourage the free exchange of information between participants and to integrate the efforts of various researchers. An ARO-D report entitled, "Army Helicopter Noise Investigation Program", September 1969, gave summaries of the work to be performed on the ARO-D projects, three AVLABS projects, two other relevant ARO-D projects, and the in-house research efforts of the Army Aeronautical Research Laboratory.

Since the Helicopter Noise Program has been in operation approximately two years, it was felt that a good professional look at the whole program

was required at this time. Thus, a symposium in which recognized experts in the helicovter noise field would participate has been organized. Primary researchers from ten ARO-D-sponsored contracts and five other groups presented papers on the subject of helicopter noise. In addition, helicopter noise research at two U. S. Army Air Nobility R & D Laboratories (AAMRDL), at NASA Langley Research Center, and at the Office of the Chief of Research and Development (OCRD) was discussed.

This report includes all formal papers presented at the Helicopter Noise Symposium held in Durham, North Carolina, on September 29-30, 1971. Although much cross correlation and discussion between helicopter noise researchers was encouraged, this report was handed to each symposium attendee as the official proceedings and no discussion could be included herein.

ROTARY WING ACOUNTIC RESEARCH AT THE AMES DIRECTORATE OF THE U.S. ARMY AIR MOBILITY RESEARCH & DEVELOPMENT LABORATORY

The research is air-raft noise which is being conducted by the U. S. Army Air Nubility Research & Development Laboratory is almost exclusively related to rotary ving vehicle noise. Although some effort is going into lift-fan noise reduction, the majority of the work addresses serodynamically generated rotary ving noise. The Army's primary objective (Slide 1) to be obtained through this noise reduction research program is to minimize aircraft detection time and distance on present and future V/STOL aircraft. The minimization of crew station cabin noise and the minimization of the annoyance of Army aircraft operations to the aurrounding commuties are two additional goals. These objectives are being achieved through efforts which are fundamental in nature and are directed primerily at understanding and reducing the noise sources.

ROTARY W'NG ACOUSTIC RESEARCH

PROGRAM GOAL

 UNDERSTANDING AND ELIMINATION / REDUCTION OF ROTARY WING NOISE MECHANISMS

ARMY'S DIRECT INTERESTS

- . DEFINE AND MINIMIZE DETECTABILITY
- . MINIMIZE CABIN NOISE
- MINIMIZE THE ANNOYANCE OF ARMY AIRCRAFT TO THE SURROUNDING COMMUNITY

Slide 1

The Ames Birectorate of AMBDL is Jocated at SASA's Ames Research Conter, (Slide 2) Hoffett Field, California, Under an agreement for Joint participation between SASA and the Army, the staffs of both organizations perform jointly in accomplishing research of motual interest. Enchange of monumer and fiscal resources is included.



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The Ames Directorate has concentrated its efforts on four basic areas of acoustic research which are listed in Slide 3. They are basic acoustic cheory, helicopter and V/STOL moise reduction, systems studies of noise-performance tradeoffs, and acoustic wind tunnel investigations. A quick review of each subject area will now be presented in order to outline the extent of the Amos Directorate's research effort.

ACOUSTIC RESEARCH

- . BASIC ACOUSTIC THEORY
- . HELICOPTER AND WISTOL NOISE REDUCTION
- . SYSTEMS STUDES OF NOISE-PERFORMANCE TRADEOFFS
- . ACOUSTIC WIND TUNNEL INVESTIGATIONS

Slide J

Th. first area of research, entitled "Basic Acoustic Theory," address.s the fundamentals of the generation and massurement of aerodynamic sound. Under a stady contract with Staaford University, the sound produced by a vortex interacting with a rigid flat plate airfoil is being explored. A simple two-dimensional analysis of the vortex-wing interaction has been developed to absess the importance of the induced vortex's motion on the generation of noise (Slide 4).



Slide 4

As the vortex passes the rigid airfoll, it is allowed to follow its own trajectory as determined by the wing-vortex interaction. In previous investigations, the motion of this cortex has been restricted to move parallel to the sizisil. Proliminary results indicate that the additional sound produced by allowing the cortex to move along its own trajectory is significant.

The second major area of retary wing acoustic research is belicopter and V/STOL noise prediction and reduction. Here of the programs in this area are being performed in-house.

One particularly annoying feature of helicopter flight is the occurance of inpulsive noise in certain flight regimes. Theoretical and experimental programs are being pursued in an effort to try to understand the parameters which are important in the generation of this type of moise. At high advancing tip Nach numbers, significant increases in level and haraonic content of rotor moise have been noticed. Data which was gathered in the MASA-Ames 40200 Feet Wind Tunnel in which moise was measured on a full-scale helicopter rotor showed a rapid increase is sound pressure level with increasing tip Mach number when operating in the transonic cange (Slide 5). Poor correlation between theory and experiment was noted when operating in this range.

EFFECTS OF ADVANCING TIP MACH NUMBER



Including the noise due to compressibility drag, however.

cignificantly improved the correlation between theory and experiment. (Slide 0).

CALCULATED AND MEASURED SOUND PRESSURED LEVEL



AVES SHEEFORATE USERLITY HESEARCH & HEVELOPHERT LABORATORY

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Blade misp (impulsive moles) is also thought to occur what the blade of a rotor interacts with the tip vortex of the preceding blade. It was noted in data collected from provious full-occile wind tunnel investigations of helicopter noise that distinct opikes in the sound pressure level data were occurring at locations which corresponded to potential blade vortex interactions. Tests have now been conducted in the AMBDL-Amous 7X10 Foot Wind Tunnel using a 50-inch dismeter madel rotor. Stop-action photographs showing top and side views of several stages of vortex intermetion are shown in Silds 7. The

TIP VORTEX TRAJECTORY OF A TWO-BLADED HINGELESS ROTOR



Slide 7

objectives of this test were to correlate the hypothesized blade vortex interactions with the sound pressure level recordings. Results of this investigation have not been completely satisfying. The primary problem which was encountered was correlating the sound pressure lever recordings and the film data. Work is currently being conducted on obtaining better data arquisition and analysis equipment and developing more sophistic tex techniques for providing this correlation.

As in-house concard, effort to correlate the latest available retical predict* echniques with experimental amise data is being pursual. .. program related to this effort is one in which an attempt in being made to verify and extend loading laws which have been stulated previously for use in the prediction of retary wing rotational unioe. Under a provision Army supported effort, a theoretical method was developed by Louise and Olivrhead for the surgeous of studictics mically generated union. A drawback to the developed theory the requirement for very detailed acrodynamic loading information and this remained detail is not available for retary wise webicles y. Recognizing this, the investigators analyzed integrated percentation ere data which was available and hypothemized a loading law to be used in lies of the required detailed servicesmanic insur. Veder nt program, detailed blade loading data and far fleid accountic data have been similantemaly recorded. This data was obtained from wind tunnel experiments over a wide range of operating parameters. Becuits from this program are just becoming qualiship. It is unficipated that this data will yield part of the information which is required to extablish blads loading low wer a wide range of operating parameters

RUTARY HING ACOUSTIC RESEARCH AT THE AMES DIRECTORATE OF THE U. S. ADNY AIR MOBILITY RESEARCH & DEVELOPMENT LABORATORY

and that this loading law information can then be used to provide more accurate predictions-for the rotational component of rotary wing serodynamically generated noise. Data from this program will be augmented with data being taken under a present MSA-Army program at the Langley Research Center. Simultaneous blode pressure data and acoustic measurements are being taken on full-acale belicopter blades operating on the MSA-Langley Whirl Tower Facility.

In cooperation with NASA, a limited affort also exists to understand and prodict lift-fan noise. Some concepts actively being investigated include-the use of a serrated-Jeeding edge to reduce fluctuating lift moise and stator lean to reduce rotor-strter interaction noise.

The last area of reversch which can be classified under the heading of helicopter and V/STOL thise prediction and reduction is entitled rotor acoustic synthesis. This program is just beginning. Its primary objective is to develop a method of synthesizing audible sound is order to a) verify analytical noise analysis by comparison of analytically produced synthetic noise and actual measured noise, and b) predict noise characteristics of future africtaft or of medifications to existing africaft. The significance of this effort lies in the immediate elimination of existing subjective miss judgements. The ass will be given the opportunity to judge the characteristics of the apalytically generated noise. Such a technique will enable .quantitative evaluation of rotary wing operational and design traiseoffs to accertain the more important acoustical characteristics of proposed designs prior to experimental cesting.

Systems studies <u>of</u>.V/STOL noise is the third area of active research. As implied previously, the most direct and effective way of alleviating the rotary wing noise problem is to eliminate the source. This, however, may not be feasible. Therefore, ways and means of reducing aircraft noise through system design and/or a judicious selection of flight paths are being investigated. The current in-house effort; which was initiated under an Army-NASA contractivith Boeing-Verto; consists of the optimization of the trajectory of a tilt-rotor aircraft

TRAJECTORY OPTIMIZATION OF A TILT- ROTOR AIRCRAFT WITH NOISE CONSTRAINTS

TASK OBJECTIVES

- EXPLORE, THEORETICALLY, MINIMUM TIME AND FUEL TRAJECTORES OF A TRIT-ROTOR AIRCRAFT DURING TAKEOFF AND LANDING WITH STRUCTURAL, AERODYNAMIC, TRAJECTORY, AND HOISE CONSTRAINTS
- BETTER DEFINE THE AREAS WHERE THEORETICAL AND / OR EXPERIMENTAL RESEARCH NEEDS TO BE CONCENTRATED
- EAPENINE HIAL HESEANCH NEEDS TO BE CONCENTRATED
- TRY TO ESTABLISH AND MINIMIZE MEANINGFUL SUBJECTIVE NOISE CRITERIA WHICH EVALUATE TOTAL ARCRAFT. DERATIONAL NOISE

Slide 8

with moles constraints.-(Slide 8). The objectives of the initial gragina were to explore on a theoretical basis the minious time and the -fugletrajectories of a tilt-rotor alrecaft during the takeoff and landing phines of flight with structural, aerodynamic, and moles constraints. Secondary objectives were to define areas of research where theoretical and esperimental effort needs to be concentrated as well as establish and minimize meaningful subjective noise criteria which evaluate total alrecaft operational noise. Gurrently, the emphagin is being placedupon using this theoretical study to assess methods of reducing tiltrotor defectability through flight-jath control.

This program has involved the development of both a theoretical performance and far-field acoustic model of a tilt-rotor stretst



ROTATIONAL NOISE PREDICTION OF A TILTING ROTOR IN NON-AXIAL FLIGHT MODIFICATION OF OLLERHEAD & LOWSON HELICOPTER ROTATIONAL NOISE PREDICTION TECHNIQUE (NERON II). BLADE LOADING LAWS WILL BE CORRELATED WITH PERFORMANCE PARAMETERS (I.C., INFLOW) VORTEX NOISE: EMPIRICALLY FITTED DATA ENGINE NOISE: EMPIRICALLY FITTED DATA

511de 9-

(Slide 9). Înithe acoustic model, rotational noise and voitez-noise were considered and found to be dominant over engine and transmission noise. The rotational noise was predicted from a modified version of Lowson and Ollerhead's method for predicting helicopter rotational noise. The program previously mentioned regarding the generation of blade loading-law-information is being incorporated into this model. The blade loading laws postulated by the previous investigators are not suitable for the wide range of operating conditions experienced by a tilt-rotor-aircfaft. In this model, -vortex noise is predicted using empirically fitted data.

A typical-moise abacement takeoff=profile that might berfiom by EFFECTIVE: PERCEIVED NOISE LEVEL VERSUS DISTANCE ALONG THE-FLIGHT PATH-



a commercial tijt-rotor aircraft is illugitated in Slide 10. Apurely vertical takeoff=trajectory is flown-to an altitude of 3000 feet to reduce the noise exposure near a hypothetical takeoff site. Anobserver located at the three locations, for G, and E, which correspond to distances of 200, B00, and 3200 feet; from the takeoff point=yould hear the maximum movid pressure level-curve illustrated in Slide 11. Rotational and yortex noise components are discernible in each case. The effects of atmospheric absorption included in the model are moticable at the higher Sarmonics where they drop off rapidly as distance in increased. SOUND PRESSURE LEVEL VERSUS FREQUENCY

10 1000



Although the first phase of this effort is complete, a similar in-house theoretical study of other rotary wing V/STOL configurations is planned. Emphasis will be placed upon understanding the operational tradeoffs which are possible with V/STOL aircraft through flight trajectory management.

The 'ast area of research to be reviewed is acoustic wind tunnel investigations. The Army has embarked upon several in-house programs to determine the feasibility of using the wind tunnel to gather acoustic data. This effort is toquired to help develop an adequate supply of accurate V/STOL acoustic data which has been taken under carefully controlled test corditions.

Unfortunately, taking acoustic data in the confines of a wind tunnel is not an easy task. In some tunnels it may not be possible to accurately re-produce the acoustic characteristics of free-field moles. Reverberation effects, tunnel (an noise, and boundary layer noise may make it difficult, if not impossible, to distinguish model generated moles from tunnel background noise.

An in-house program to survey the acoustic properties of the Ames Directorate's own 7X10 Foot Wind Turnel (Slide 12) is nearing





Sitde 12

completion. Preliminary results indicate that the amplification factor of the tunnel is both a strong function of frequency and microphone location in the tunnel. Thus it will be necessary to acoustically treat the tunnel "o make quantitative rotary wing noise measurements that can be co.rected to free field conditions. At the present time, the Amon wirectorate is supporting a research contract with Penn State University to explore various alternative means to improve the acoustical characteristics of the 7X10 boot Subsonic Wind Tunnel.

The 40X80 Foot Wind Tunnel (Slide 13) is also being used to take



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acoustic data on full scale aircraft. One third octave band amplification factors have been established for the tunnel and the performed there have a policy of taking noise measurements for all tests. Leaningful quantitative accustic data has been taken in the confines of the tunnel illustrating both broad accustic trends and the effects of incremental design and operational changes on the accustical characteristics of several V/STOL aircraft. Acoustic measurements will be taken by WASA on both the OV-10 (Slide 14) and XV-5 (Slide 15) aircraft in the



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ROTARY WING ACOUSTIC RESEARCH AT THE AMES DIPECTOPATE OF THE U. S. ARMY AIR MOBILITY RESEARCH & DEVELOPMENT LABORATORY

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NASA +0180 Foot wind Tunnel Infortunately, because of the amplification factor's apparent dependence upon sound source and microphone position, some uncertainty as to the validity of data which has been corrected to free-field co-ditions still exists Jummary of Helicopter Noise Research at Eustis Directorate, U.S. Army Air Mobility BAD Laboratory

by:

John E. Yeates, Chief, Aeromechanics Division William E. Nettles, Aerospace Engineer William T. Alexander, Aerospace Engineer

Helicopter noise research has been underway at Eustis Directorate since about 1960 and numerous reports reporting the results have been published.

The present report treats only those research efforts that are just being completed or are now in progress.

Summary of the following research studies will cover five general areas.

- a. Tip vortex mise
- b. Shed vortex and rotational noise
- c. Internal noise (transmission, engine, etc.)
- d. Tail totor noise
- e. Measurement & detection of noise

1. INVESTIGATION OF THE REDUCTION OF BLADE TIP VORTICES AND HOISE DUE TO ROTOR WALE/BLADE INTERACTION, BY AIR INJECTION AT THE BLADE TIP

Summary: Subject effort is being performed by RASA under Contract DAAJ02-71-C-0036. The program is essentially an experimental investigation to determine the practicality of introducing a mass of air into the tip vortex core of a rotating rotor blade, as a means of modifying or dissipating the vortex. Essential to the conduct of this study will be the measurement of influential parameters, and both visual and optical (photographic) recording of-blade tip-and vortex flow patterns in the University of Yaryland 8'X 11' Wind-Tunnel. Improved discernment of flow patterns is expected by application of new hydrogen bubble techniques. The test model will be a-full scale helicopter blade tip with the span properly sized to fit the wind tunnel test section. A few of the parameters that will be studied are angle of attack, mass-injection rate, location and size of mass injection, lift, drag, vorticity distribution, etc. Their effects on the coupling characteristics of-the trailed vortices and the aerodynamic flow of-the model will be investigated.

Finally, all data will: be analyzed: to determine if tip injection is a practical menns-for eliminating the vortex without compromising rotor performence,

NOTE: Completion date: January 1972,

2. <u>INVESTIGATION OF THE VORTEX HOISE PRODUCED by A HELICOPTPR BUTOR</u> <u>Summary</u>: The objective of this program was twofold. The first part was to dovelop an advanced capability to accurately analyze the more suble components of helicopter noise, in particular, the broad band or writex noise. The second part consisted of the development of an explicit analyses to predict rotor vortex noise based on a correlation of the vortex noise components with a shed vortex analysis. That is, instead of being satisfied with empirical curves fit to what is nominally called vortex noise as had been done in the past, an attempt was made to predict vortex noise based on a specific aerodynamic source.

The effectiveness of this research-required the development of a digital band pass filter for analyzing noise records. This computer program,

based on Fourier transform techniques, provided a marrow digital filter which accurately calculated both amplitude and phase of the noise compoments. This digital technique also allowed close central of the specific sample of the noise signature selected for analysis, an item of particular importance where the noise has a transfert quality.

In the second_phase of this program, this filter was used to extract-the vortex noise from selected signatures. The noise was examined and correlated with shed vortex calculations. The correlation results were used with existing noise analysis theory, and an analytical technique was developed for predicting the helicopter vortex noise signature.

The resulting analyses were used to study the basic character of vortex noise produced by the helicopter rotor. One point of particular interest was the ability to reproduce on magnetic tape a vortex noise pattern which could readily be identified as a helicopter noise signature although rotational noise was not present. While the results of this work have not yet been fully reported or evaluated, it is anticipated that these findings will produce a significant new capability to analyze and understand the quality of helicopter noise.

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NOTE: This work has just been completed under Contract DAAJ02-70-C-0023 with Rochester Applied Sciences Associates (RASA). Final report to be distributed about December 1971.

3. DEVELOPMENT OF A TECHNIQUE FOR REALISTIC PREDICTION AND ELECTROVIC SYNTHESIS OF HELICOPTER ROTOR NOISE

Objective: Extend current analytical prediction technique=for rotor broadband noise to include rotational noise and develop a method of simulating the noise signature of a-helicopter from the predicted noise force constants.

Approach:

a. Develop an acoustical data bank (controlled data, I.e., whirl tower, flight test,-etc.)

 Extract rotational noise from the broad-band noise (vaing method developed under Contract-DAAJ02-70-C-0023)

c. Extend RASA analytical prediction technique to include rotational noise.

d. Develop technique for converting predicted noise into analog acoustic tapes.

 e. Evaluate effectiveness of noise prediction and simulation methods by comparing predicted results with experimental data.

Summary: RASA, under Contract DAJ02-70-C-0026, developed an analytical technique for predicting the acoustical signature of a helicopter rotor. This method, however, only accounted for the broad band (boundary layer) oscillatory moles. The current study is designed to expand this tool to include derivation of the force constants for rotational moles. The technique will be designed to predict noise of a rotor using auch parameters as: number of blades, blade chord, blade thickness, blade twist, rotations: speed, forward velocity, aircraft weight, and aircraft attitude.

In attacking this problem, the Contractor will research and catalog all noise data considered accurate and applicable to the task. Selected data will then be converted from analog to digital form to permit separation of the rotational from the broad band (vortex) noise using the extraction method developed under the above contract. The force constants derived for both noise sources (broad band & rotational) are then converted into

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SUMMARY OF HELICOPTER NOISE RESEARCH AT EUSTIS DIRECTORATE, U.S. ANNY AIR MOBILITY RAD LABORATORY

parametric form as functions of the above-listed control parameters to form a data bask.

In addition to the above, the Contractor is to investigate a means of electronically simulating rotor noise by converting the predicted digital noise signatures into analog acoustic tape. Such tapes then can be used as a design tool in subjective evaluation of a new design or planned rotor midification.

Finally, the Contractor is to test the accuracy of this design tool by correlating the predicted results with experimental data from the UH-IB and Vertol Model 347. Data will be compared as: (a) pressure time history plots, (b) noise spectrum plots, and (c)-subjective evaluation of audio tapes. Further, for the NLN configuration currently under development, the Contractor will predict and provide simulated noise tapes in the same format as for above alteraft.

Upon completion of the above, the Contractor will demonstrate and instruct Army personnel-in the capabilities and practical use of the design tool.

NOTE: This study is being performed under Control DAAJ02-71-C-0064, (A 12-month effort with a completion date of June 1972)

INTERNAL NOISE REDUCTION (Gearbox Noise and Vibration Reduction for Rotary-Wing Algorith

Summary: Approximately four years ago, this Directorate initiated a program with Mechanical Technology, Inc. (MTI) of New York to analytically investigate means of reducing the internal noise levels of helicopters by improved design of transmission gearing. Also, this effort was-further enhanced by the possibility of schieving an extended Time Between Overhaul (TBO) as a result of reducing the dynamic force levels between drive train components. One of the achievements to result from this initial effort has been the development of-analytical tools and methods of predicting noise levels of various gear trains. This Directorate now has a computer program that provides means of evaluating new transmission designs as well as proposed modifications for noise reduction.

Although some of the recommendations derived from the MII programs have proved impractical (such as machining complicated tooth profiles) others. such as operating too near critical vibratory frequencies and having too stiff or too soft bearing supports, are proving to have merit. Hany of the MTI findings are being experimentally verified through a research program now being conducted at Boeing/Vertal *(Investigation of Helicopter Transmission Noise Reduction by Vibration Absorbers).

A survey of the major airframe manufacturers and Government agencies is currently being mode in-house to determine the overall status of noise reduction efforts and whet is required to assure quiet helicopters of the future.

It is becoming increasingly clear and essential that a key to any successful noise reduction program is cooperative effort between the designer and Acoustician during initial design and in the application of the tools now eveliable.

"NOTE: Final Report due September 1971.

5. ADVANCED RESEARCH PROJECTS AGENCY (ARPA)-JULET HELICOPTER PROCRAM Summary: It is well known-that the tactical use of the helicopter-in Southeast Asis has been somewhat compromised by its high noise levels. That is, the element of surprise is negated by early sural detection.

In an effort to sectify this condition, APRA recommended that three "crash" programs be initiated to prove the feasibility of quietening three operational type helicopters (the Kaman HH-438, Sikorsky SH-3A, and Hughes OH-6A) using current technology. The Hustis Directorate, was directed to manage the technical and contractual aspects of each program. The necessity for

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- I REDUCED BOTH MAIN & TAIL BOTOR OPM
- ? INSTALLED LOWER SPEED TAIL ROTOR GEAR BOX 3 TWO DIFFERENT TAIL ROTORS USED (2 & 4 BLADE)

NH-438

- I ROTOR SPIID RIDUCID
- 2 TIP CAPS WITH SWEPT LEADING EDGES ADDED TO THE ROTOR BLADIS
- 3 MODIFIED ENGINE TAIL PIPE
- S ADDED ACOUSTICAL BLANKETING TO REAR CABIN
- S THICKER TRANSMISSION OIL

SH-3A

- I REDUCED BOTH MAIN & TAIL ROTOR APM
- ? INCREASED MAIN ROTOR FROM 5 TO 6 BLADES
- 3 ADDED TRAPEZOIDAL CAPS 10 MAIN ROTOR BLADE TIPS
- 4 INSTALLED LOWER SPEED TAIL BOTOR GEAR BAX S INCREASED NO. OF TAIL NOTON BLADES FROM 5 TO 10
- & TAIL PYLON WAS CAMBINED
- I LINED THE DUCTS OF ENGINE INLETS & EXHAUSTS

Figure:1

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separate contracts is apparent from the responsibility given each Contractor in performing Phase I: The design, fabrication, and installation of those modifications that the Contractor felt would aid in reducing the external noise of his particular helicopter. Phase-II: the evaluation whase, was the_responsibility of the Government which:conducted noise messagements at the Wallops Island test station "before and after" the modifications for each aircraft to determine the noise reduction achieved.

The modifications performed on each vehicle are identified in Figure 1.

Although the quantitative results of the three programs are classified, some of the conclusions that may be revealed are:

A. In tip speed of the main rater has the most programmed effect on the helicopter's noise signature. However, helicopter performance is compromised (forward sp. d, pay_load, range)_ as a result of reducing rotor speed.

b. Mechanical sources of sound such as gearbones, transmission, etc. are not board until the aircroft is relatively close. Noise attenuating efforts should be directed, therefore, towards the main and tall rotors.

NOTE: A listing of papers which report on the results of the program is shown in the Appendix.

6. BASELD/E HOISE HEASINGHENTS OF ANNY HELICOPTERS

Summary: The principle aims of this program are the development of a data bank of helicopter acoustic signatures and a draft specification that may be used as a standard in the test and measurement of helicopter acoustic

SUMMARY OF HELICOPTER NOISE RESEARCH AT EUSTIS DIRECTORATE, U.S. ANNY AIR MOCILITY RED LABORATORY

signatures. Initially, effort will be directed to: (1) researching current techniques employed in the measurement and analysis of acoustical data and (2) defining a total field measurement program (instrumentation, flight patterns, pertinent parameters, calibration, etc.).

The acoustic signatures were measured at Camp Pickett, Virginia for five Army belicopters, the OH-6A, UH-1B, AH-1G, CH-67B and CH-56A, during hover and flyover modes of operation. This phase is critical to the success of any reasurement program because of the mecessity of having reliable equipment, knowing precise position of aircraft relative to recording media, documenting att environment, instrument, aircraft descriptive data, and the re-ording of the aircraft noise in a manner that will assure validity and easy retrieval of the recorded data.

The data from these tests were quantitatively evaluated through narrow band analysis to define frequency distribution, harmonics, random noise, acoustic energy, etc., and identify the contributors or sources of the total alcotate noise.

Finally, the Contractor recommended procedures, equipment specs, calibrations, flight conditions, signal and recording particulars, etc., essential to the development of standardized noise data banks. The moise data, recorded on magnetic-tape, will be retained in a data bank at the Eustis Directorate.

NOTE: The above effort was conducted under Contract DAAJ02-70-C-0025, with Vyle Labs. It is now complete and reported in 2 Vols, USAAMBDL TH 071-36A and 71-36B, 71-36B is classified because noise levels for the aircraft are specified.

7. HELICOPTER AURAL DETECTION

Summary: This is an analytical study designed to:

a. Determine the survivability of current tactical helicopters on the basis of their noise signatures.

5. Develop nesse signature criteria for optimum helicopter survivability,

Fundamental to the analysis is that only <u>aural</u> detection of the helicopter will be considered as it is "flown" against hostile forces.

The program is divided into three (3) phases: Phase I, Study Definition; Phase II, Survivability Determination: and Phase III, Analysis and Results. In Phase I, those parameters that describe the-tactical use of the five classes of aircraft (observation, attack, cargo, utility and heavy lift) will be defined. From this appropriate scenarin/program material will be arranged to support the basic analysis. Consideration of enemy threat will be limited-to gural and visual perception of the approaching helicopter by the enemy (i.e., PADAR, optical/acoustical aids are not considered in the detection).

Phase II will be devoted to the development of aural detectability contours as dictated by the helicopter noise spectra and environments. Determination of survivability will be based upon:

- a. Single ground wapon vs single aircraft
- b. Alteraft penetrating forward battle line

The final phase will be devoted to analyzing the helicopter areal detection patterns (costours) to determine the probability of kill-from energy fire. Perommendations will then be made as to what kill probability for each aircraft would represent an optimized survivability/mission effectiveness level. As a consequence, new optimized acoustic detectability distance contrass will also be developed for each class of aircraft.

NOTE: This study is being conducted by Boeing/Vertol under Contract DAAJ02-71-C-0065. (Estimated completion date is June 1972)

Repetulity, the moles research brief presented above gives some indication of the new importance given to this area of work.

The results from the acoustics work presented Above show that significant gains have been male in experimentally resulting and analyzing data, the capabilities and limitations of existing instrumentation are before understood, and in many cases whole new systems and techniques have evolved

In the area of theoretical analysis, major improvements have been made in defining the mechanics of the noise source. This has led to the development of aero-acoustic teams which have attacked the problem at the rource and, in many cases, have demonstrated that this approach can produce significant reductions in the noise signature of a helicopter. As a result, the helicopter noise problem is no longer a secondary consideration, but is being treated by the preliminary designer in his initial conceptual layouts.

In:effect, the-subject of rotary wing acoustics-is becoming-increasingly important and is no longer simply an art, but a well defined science

APPENDIX 1

Reports on the ARPA Culet Helicopter Program

NASA-JANGLEY WORKING PAPERS:

1, #755 - Description of the Noise Measurement Program on a Standard and a Modified Kaman Hild/38 Helicopter-with Some Initial Results. June 6, 1969,

2 4838 - Description of the Noise Peasurement Program on a Standard and Two-Multied Hughes 08-04 indicopters with Some Initial Results. Dec 23, 1969.

1 9963 - Description of the Noise Heasurement Program on a Standard and the Nudified Phase 11 Jughes Off-AA Heilcopter - Nay 26, 1971

 PB03 - Description of the Soise Brasurement Program on a Standard and a Medified Sikersky SH-DA Helicopter with Some Initial Results – Sep 30, 1969.

REPORTS

 MASA Technical Newsrandum #X-2226 - Ground Solise Sessurements During Flywer, Hover, Landing and Takeoff Operations of a Standard and a Bodified HM-638 Helicopter - February 1971

2 Sikorsky Final Report 4528+611678 prepared under C-stract DAJ02-69-C-0020, title - HUSH Final Report - Quiet Helic-ster Program (S-61)

3 Hughes Final Report, HTG-AD 70-26, Contract DAJ02-69-C-0078, Lifte-Procease to Reduce the Sulse Signature of the OlioA Holicopter

4 Kabin Final Report 48-188 of April 21, 1969, Contract INAJ02-69-0-00019, Litle, Softe Reduction Program HH-638 Helicopter

NOTE: All of the above reports are classified CONFIDENTIAL,

RECENT ASPECTS OF THE ANNI'S INTEREST IN THE REDUCTION OF MELICOPTER MOISE

Richard L. Ballard Office, Chief of Research and Development Department of the Army

The problem of the noise signature of a helicopter is an inportant aspect in the consideration of the survivability of the helicopter on the battlefield. During the 1960's, the U. S. Army was involved in a war that was classified as low intensity and therefore in the area of survivability the main emphasis was placed on providing protection to the aircrews from 7.62mm (30 cal) projectiles. No real attempt was made to reduce the noise-signature of the belicopter or any of the other signatures (radar, infrared, or optical). The real desire was to-produce helicopters that would operate effectively against the enery. Any changes to the design of the helicopter that reduced_its ability to accomplish its main mission were not accepted. In the case of noise, no changes to reduce noise were allowed because it meant penalties in that the aircraft gross weight was increased with accompanying reduction in payload or the rotor efficiency was decreased or expensive modification to an existing fleet would be required. The Army has learned a lot about fighting with helicopters and is changing its attitudes toward survivability. The Army is now designing its aircraft (HLM, UTTAS) to operate in mid-intensity. The aircraft must be capable of withstanding hits frue 12.7mm (50 cal) projectiles, and must have reduced signatures. Therefore, - phasis at the present time is to reduce noise, infrared, and raisr signatures of Army sircraft.

The Army has produced a short film on the noise reduction program conducted by APPA with the Army on the OH-6A. The research effort on the bh-6A employed a different design philosophy than previous noise reduction programs in that the design of the helicopter was for minimum noise level, regardless of the reduction in performance except that it must be able to fly.

This film showed some very remarkable results. These results are going to be used in a program for a scout helicopter. This effort brought out one very important aspect of designing helicopters for low noise signature. -- "It is possible to give the pilot the option of selecting his noise signature." For example, at home base the pilot loads the helicopter to the normal gross weight and takes off. Prior to approaching the target area, the pilot reduces the speed to that requiring the minimum horsepower and reduces the rotor MPM to about 67 percent. The noise signature is greatly reduced as well as the performance. The helicopter can continue to fly straight and level but is very limited in maneuverability. The performance has been reduced, but not the payload. When the pilot arrives in the target area and determines that he must have the performance to land or maneuver, and/or the noise signature is no longer important, the pilot can increase the rotor PfM to 100 percent. The modern Army helicopter will be using a broader definition of survivability than has previously been used, and the noise signature will be carefully considered. I am sure that in such aircraft as the NIM and UTTAS, only minor reductions in performance will be allowed for design features that will reduce the noise signature. However, in special purpose helicopters such as the serial scout, other major changes in design may be appropriate and justified that result in significant reductions in noise signature.

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VTOL HOISE RESEARCH AT THE LANGLEY RESEARCH CENTER

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Robert J. Pegg -Langley Research Center

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Robert N. Hosier - Langley Directorate U. S. Army Air Mobility Research and Development Laboratory

SUMMARY AND ADSTRACT

A brief overview of the SASA langley programs in VTUL noise reduction research is presented. Incluied are descriptions of specialized facilities relating to VTUL nulty, and programs designed to explore basic theoretical concepts and to develop noise control technology for quiet vehicle designs. Introduction

INTERPORTICA

The joint SAIA-WAANDL acoustics research program at Langley, is broadly based and diverse in nature. Included are several specific research areas relating directly to VTOL noise control, and these are outlined in figure 1. The purpose of this paper is to present brief discussions of the activities in each of these areas and in the order listed in the figure.

Epecific areas of VTOL noise research include rotor blade noise reduction; the development of techniques for measuring flyower noise reduction; reciprocating engine eshaust muffling technology; human factors studies which deal-primarily with the effects of noise on uncommute and task-performance; and special facility developments. In this work, see is made of facilities and equipment which will be described triefly along with discussions of the associated research profects. Reference, are made also to future facility modifications and developments now moder consideration.

ROTOR BLADE NOICE REDUCT. -

The sound of a retor wraft is complex in nature since it is probable by reveral individual sources which say generate acoustic energy by various meanisms. The primary emphasis in Lengley V50 noise research 1. reverse of abtaining a nore complete universation of these generation methanisms. An example of inchouse fundamental research 1. the study of the effects of fluctuating table pressures on the far field radiated methanisms. The primary emphasis in this figure predicted noise tered, due to steady rater loads show a rapid drop off with intrees ing harmonic number, whereas experimental data indicate a wery slow reduction. Recent theories such as that of reference 1, which are established and have a steady rater loads show a rapid moder levels are stabilished a steady rater loads show a rapid drop off with intrees ing harmonic number, whereas experimental data indicate a wery slow reduction. Recent theories such as that of reference 1, which are established to the experimental data. This result suggests that a prediction method based on fluctuating black loads may be useful, particularly for the higher harmonics which are of concern for retemility annotations.

The nature of the fluctuating loads theory is indicated by the formula of figure 3. The measure hermonics. In, are expressed as a function of the thrust, T_{μ} , and targue, Q_{μ} , black loading harmonics. The Beasel function $J_{\mu,\mu-\nu}$ (and sine) and the ross term define the directivity pattern associated with rotor noise wherear the term e^{-160} represents, in complex form, the Fourier series expansion of the black

loading. The objective of one research program is the simultaneous mensurement of the fluctuating loads quantities ($T_{\rm fl}$ and $Q_{\rm sl}$) and the residute house (in), to validate the quantum constants

The name work will be carried out on the landley which tower blast in figure 4. For field noise data will be time correlated with simultaneous blasts pressure measurements at several spansize and chordsize locations. An attempt will be made to correlate the above rotary data with civiliar tota from a two dimensional wing in a wind tunnel test at comparable Reynolds numbers. Special instrumentation of the type inveloped by 36M (see reference 5) will be used to new are surface pressures in the frequency range up to 1 sHg and to telestor theory data from the black to showed based recorders. In addition to the dowe programs, confidential being given to research that will evaluate the viscous discipation of the black new two and pacified beneficial noise effects by means of tip air mate injection. These statises will be traced on initial work performed by RAM, and George Wathington University (See reference 4).

FLYOVER HOLSE MEASUREMENTS

Several holicopter flight test programs have been conducted at the SKMA Wallops Justion noise measurement range which is shown in figure b. The range consists of an operational airstrip, located in relatively open and flat terrain. Because there is little air traffic and sparse population is the arch, the amble — also levels are generally low. All measurement protectors used at this range to pressure external air traffic noise conform at clusely as possible to the standards set forth in reference b. In stilling to provisions for themble time correlated microphone army. involving additible mobile two reventing station: (see inset post), there is a precision-tracking rotar for obtaining aircraft post ion, ad completermeterological facilities.

A an example of the set of this test range a flight investigation we performed to establish information we the noise rediction characteristics of a heliciptic information in the effects of characteristic operating permeters on the noise characteristics. A typical institution relies redict a pattern is shown in figure . In order to prove such results, at it measures to the correlate at a singulater channel, with the beliespter perities information. The beliespter estimates of the tests we the Gleek ingle rotor, " at its powered sincraft". The results of the tests, show that the institute roles redictions patternance strongly directional, the main a noise rediction being in the direction of flight. The primery personner that affected institute noise was not a speed, only and terreficiel effects on redicted noise was ender a product with reduced forward open and reduced ends of the state (see reference b).

A belinopter noise measurement program speakened by ARPA way old accompliabed at the above noise measurement range. At a part of the above program the two vehicles of figure (were to-ted. The standard configuration is shown in the top photo and the modified wer see is shown in the bottom photo. The objective was to response a structure helicipter with one especially modified for low-external below. It was concluded from the results of the tests that the noise reflections were substantial.

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VTOL HOLSE RESEARCH AT THE LANGLEY RESEARCH CENTER

RECIPROCATING ENGINE EXHAUST MUTPLING

Piston engines have been replaced in the majority of military helicopters by less noisy gas turbine engines, but they are still used to power many small civil helicopters. Operations over congested areas by users such as police departments may require engine noise reduction.

Langiery Research Tenter Las had a sustained program to develop reciprotating engine exhaust muffler technology. The development of a muffler to a point where it can provide large noise reductions and still have acceptable weight and performance, has in the past required a lengthy "cut and try" approach. This approach has been supplemented by a newly developed, more exact, computerized suffler attenuation, evaluation, and design procedure. This program allows for such constraints as rolume and size to be placed on the suffler design. The program then performs the required numerical iterations to define an expansion chamber muffler whose aboutic performance is maximized within the initial size and volume constraints.

Using the above technique, two muffler configurations shown in figure 8 have teen designed and evaluated on the MASA H-13M helicopter. Typical marrow band-moles spectrum results of these tests are presented in figure 9, for the hovering flight condition. The upper curve is for the basic engine, and the lower curve is representative of muffler configuration I for comparable operating conditions. A large number of noise peaks observed for the basic engine are essentially eliminated by the muffler, with an associated substantial reduction in the overall moles levels. The acoustic results for configuration II were the same as those for configuration I but the weight and back pressure were less. The results of this study alw show that for the H-1) helicopter, the mufflers can be designed within acceptable size and back pressure limits, (less thun 5 ln. Hg).

HOMAN FACTORS

The Langley Research Center has active contractor studies in the area of homan response to VIOL noise. As an example of some of this work, figure 10 illustrates the test configuration for a Sikorsky Aircraft Company study to determine the effects of rembined noise and vibration stimuli in VIOL plict performance. As is illustrated, pilots placed in a cockpit simulator are exposed to pre-recorded helicopter noise and wibrations. While being this exposed, the pilots fly a simulated commercial air route, performing IFE marightics tasks. Filot performance ratings are and during efficient and post-filight questionaires are also animistered. This program is still is progress and the final results are not yet available.

Another example of Langley supported psychosconstits work is illustrated in figure 11. Shown is the test environment for a Boeing/ Vertol study to determine the absolute acceptability of VIOL aircraft noise during simulated termined area operations. Subjects are placed in the test trailer, which simulates a work and leisure environment, and asked to pursue a number of activities such as job related work, playing turds, or whiching television. While the subjects are performing these activities, recorded VIOL terminal area noise records are played to them through the speaker systems for evaluation purposes. The results of this work are awaiting publication as a NACA Contractor Report. The Longley Low Frequency Hoise Pacility (LFNF), shown in figure 12, provides an in-house capability to study human and structural response to VROL noise in the frequency range below 50 Hi. Room-size structures can be placed in the noise field generated by the facility in order to evaluate the effects of low frequency noise exposure of people both inside and outside of structures.

SPECIAL SECTIONED DEVELOPMENTS

Two of the Laugley subscrip wind tunnels which are ideally suited for VIOL serodynamics research are being acoustically calibrated. Measurements are being made to determine the sound absorpting treatment moded to increase the utility of the tunnels for evaluating the effects of forward velocity on rotor noise characteristics. An example of the results of this calibration work accomplished to date are shown in figures 13 and 14. Typical experimental data obtained in the evaluation of the Full Scale tunnel are shown in figure 13 where the noise levels from a calibrated accustic source are shown as a function of distance in the nnel test section. At the large distances, the measured noise levels approach those in the reverberant field. For the example shows, the measured values exceed those of the inverse distance las by 3 dB at a distance of about 17 feet. This is defined as the hall radius which in the limiting distance at which useable acoustic data can be obtained. A plan view shetch of the test area of this wind tunnel is shown in figure 14 and the current useable acoustics test area is shown cross batched. Consideration is being given to the inclusion of acoustic wall treatment so that the acoustics test area can be considerably increased as indicated by the dashed lines.

Of special interest is the Aircraft Moise Reduction Laboratory now under construction at Langley and which is shown as an artists conception in figure 15. This laboratory will specifically:support VTOL noise reduction research by providing for rutor noise studies at forward welocities up to 150 ft/sec. Of particular significance is the capability for testing rotor models up to 3 feetin diameter is an anechoic environment and where the tunnel soise and turbulence levels are a minimum. In addition, the laboratory will provide improved capability to quantitatively determine the effects of noise on people and for engine and anhoust noise control studies:

CONCLUDING REMARCIN

The MASA/USANDEL research programs uploting VTOL noise from the source (rotors and engines) to the receiver (human and atructural response) have been outlined. The various research facilities at which the above verk is being conducted were also described. Proposed future programs were shows to provide increased emphasis on helicopter noise reduction and prediction techniques, and to include considerations of improved facility capabilities.

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- ROTOR BLADE NOISE REDUCTION
- FLYOVER NOISE MEASUREMENTS
- RECIPROCATING ENGINE EXHAUST MUFFLING
- HUMAN FACTORS
- SPECIAL FACILITY: DEVELOPMENTS .

Figure I. - Langley VTOL acoustics research.



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VTOL NUISE RESEARCH AT THE LANGLEY RESEARCH CENTER



HUGHES OH-6A STANDARD



HUGHES OH-6A MODIFIED

Figure 7. - Quiet helicopter program.



Figure 8. - H-13 multier test configurations.



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Figure 9. - Helicopter hovering noise measurements.



Figure 10. - Combined noise and vibration test configuration.



Figure II. - Test environment for subjective reaction to VTOL aircraft noise.

VTOL NOISE RESEARCH AT THE LANGLEY RESEARCH CENTER

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NOISE ANALYSIS OF THE EXTERNAL ARROWNAMEC DIFFUSER APPLIED TO SUBOUDED PROPELLERS

> E. E. Longhouse and J. R. Builey

CENTER FOR ACOUSTICAL STUDIES MECHANICAL AND AEROSPACE ENGINEEDING DEPARTMENT NORTH CAROLINA STATE UNIVERSITY BALEICH, NORTH CAROLINA

Abettact

It is well known that propeller performance can be improved by proper addition of a shroud. Provious investigators have shown that, attendant with the improved performance, the shroud significantly reduces the system noise, provided inlet flow separation does not occur.

External aerodynamic diffusion (EAD) of the enhoust flow provides an evitasion of the shrouded propeller concept. This concept, which is useful for V/STOL aircraft during hover operation, significantly improves the system thrust/power ratio compared to the conventional shrouded propeller with no diffusion. Attendant with the performance increase is A reduction in the system noise. The noise reduction is a result of a decrease in the fam blade aerody amic loading and final exhaust velocity. EAD, therefore, provides a method of decreasing the system noise while improving system performance. Durrent techniques of reducing the noise of V/STOL propulsive units tend to degenerate system performance.

Introduction

Per-V/STOL aircraft incorporating shreaded propellers or fan-in-wing units, the system noise and thrust to power ratio can be significantly improved by using external acrodynamic diffusion during hover operation. External acrodynamic diffusion (EAD) is a process that produces acrodynamic expansion of the fan exhaust flow. EAD can be accomplished by providing a short expansion area—in the exit section of r shroud and by preventing flow separation on the diffuser wall for high divergence angles.-Figure 1. The effect of EAD is to increase the effective exhaust to fan disc area ratio which, in turn,-reduces the final exit flow velocity, fan back pressure, and fan biade acrodynamic loading for a gimen thrust condition.

The noise produced by the propulsion unit is related to the magnitude of steady and fluctuating blade loading components and to the exhaust velocity. Reduced blade loading, as given by EAD, would therefore tend to reduce the intensity of sound produced. Furthermore, since-jet with depends on the 8th power of the exhaust velocity and the 2nd power of the exhaust diameter (1), lowering the exhaust velocity would exterially reduce jet noise (2).

Early studies of shrouded two-blade propellors by Nublard (1) indicated that the presence of the shroud, which decreases hlade loading, reduced the sound pressure level by 6 dB at the fundamental frequency and by as much as 20 dB for the higher harmonics for smooth flow conditions. Plow separation at the inlet of the shroud caused the noise level to increase to the unshrouded values and greater with more acoustic energy concentrated at the higher frequencies. It was also noted that flow separation is an attendant problem with shrouded propeller systeme. Expansion of the exhaust flow will tend to aggravate this situation since the mass flow through the system is increased. Therefore, considerable attention must be given to the inlet wall contour. Inlet boundary control matheds (suction, etc.) may be required.

Since fuel requirements are about ten times greater in the hover modes compared to level flight, the increase in the thrust to power ratio that can be provided by EAD is most attractive. An operational aircraft with lift fams equipped with EAD would have increased range and paylead capability and would decrease the probability of human annoyance response since less moise would be produced in the hover modes where the potential of moise annoyance is greatest. EAD, therefore, has the potential of providing a built-in noise reduction mechanism that enhances rather than degrades system performance. Corrent precedures under investigation (4, 5) degenerate system performance.

While early experimental investigations at Princeton (6, 7) did not establish positive banefits with EAD, more recent experimental results (8, 9, 10) indicate considerable system performance improvement can be acheived. An increase in anhoust area of 502 can be expected. The effect of this increase in enhaust area is to reduce the fam blode loading by 342 and the exhaust velocity by 502 at constant thrust.

Receptizing that the noise produced by a propulsive unit is related to the magnitudes of the steady and fluctuating blade loading forces and the enhaust velocity, the intent of this paper is to examine the potential offered by RAD for simultaneous improvement of system noise and performance.

Moise Reduction Analysis

- The noise is considerably reduced by using EAD due to three effects:
 - (a) Reduction in steady loads
 - (b) Reduction in fluctuating forces on the blades
 - (c) Reduction in final exhaust velocity

It is important to understand that large area increases are possible. Increases of 50% in area are realizable. The following example will illustrate how this affects blade loading for the simple case of ideal, uniform flow. For a propeller (shrowled or unshrowled).

 $\begin{array}{c} \frac{T_{B}}{T_{T}} = \frac{1}{2} \ , \ \text{where } T_{T} = \text{propeller thrust} \\ (i.e., \ blade \ loading) \\ T_{T} = \text{system total thrust} \end{array}$

Consider the cashs that follow:



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NOISE ANALYSIS OF THE EXTERNAL AERODYNAMIC DIFFUSER APPLIED TO SHROUDED PROPELLERS



In the preceding example, it is shown that a shrouded propeller with 502 diffution will cause a decrease in blade loading of 67% in comparison to an unshrouded propeller for the same total thrust. It appears that a significant reduction in noise would therefore be expected. As demonstrated by Hubbard (3), shrouding the free propeller (doubling exhaust area) reduced the fundamental frequency noise of the system by 6 dB. This reduction is the order of magnitude that yould be expected since T_p , and assuming a proportionate change in torque, was reduced by a factor of 2.0. The pressure would be reduced by the same order of magnitude. The external aerodynamic diffuser provides an extension of the use of propeller thrust relief as a means of pure tone noise reduction.

A similar comparison of a standard shrould proveller with no diffusion to a shroud with # = 1.5 can be made. The latter has 34% less loading on the blades. This represents approximately a 3.5 dB fundamental frequency. noise reduction. Only the noise reduction due to the steady lift has been considered. The unstatdy pure-tone noise is also reduced by the Jecreased blade loading via a decrease in the potential field interaction. This can be illustrated as follows. Since the thrust increase at constant pressure ratio is proportional to area, the system with g =1.50 has -50% more thrust than the system with $\Lambda = 1.0$. Thus to return to comparable thrust levels, the pressure ratio of the diffuser system must be significantly reduced, i.e., the propeller must be throttled back. If the propeller was originally operating at $P_{T}/P_{T} = 1.40$, this means the pressure ratio must be reduced to P_{μ}/P_{μ} = 1.255_to make a noise comparison at constant thrust. The affect of pressure ratio on noise for a typical system (7), considered here to be the General Electric lift fan LP475, is shown in Figure 2. The applicable reduction in pressure ratio indicates a 5.5 dB reduction in the fundamental frequency noise. The difference in this value and the steady lift noise is attributed to unstaady loading noise reduction and reduced enhaust velocity.

It is espected that the noise reduction achelyed for a given σ will: depend significantly on the characteristics of the particular propulsive unit. The numbers presented here are for the purpose of showing the order of magnitude to be espected. From a free propeller to a shrouded propeller with $\sigma = 1.5$, the order of magnitude of fundamental frequency noise reduction is 10 dB for constant thrust.

Diffuent System Parformance

Use of an external aerodynamic diffuser significantly increases the system thrust to power ratio. Considering the case of the constant thrust for ideal, uniform total pressure flow, it can be shown that the performance improvement ratio is

diffusion . (Thrust) no diffusion

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ALC: NO

at constant thrust. Thus, for $\sigma = 1.50$, the performance improvement factor is 1.225, so that the performance improvement is 22.5% at constant thrust.

Thus, not only has the system noise been reduced, but the hover performance has been significantly improved.

The overall performance of the EAD will be dependent on the efficiency of the means incorporated for diffuser boundary layer control. Several methods may be applied, e.g., blowing from slots, trapped vortex, suction, etc. Also the weight of the shroud must be considered. Too large of a shroud would tend to megate the performance gains.

Use of EAD for performance improvement is not without problems. Experimentation to date has indicated that the high divergence angle diffuser system tends to be unstable when subjected to disturbances (side winds, etc.). Thrust variations of 10% or more can be expected. Also, the flow will tend to separate at the inlet unless proper design is followed. Current experimentation indicates that the inherent instability of the system is the major obstacle that must be overcome before system integrity can be acheived.

Conclusions and Recommendations

Corrent experimental investigations substantiate theoretical claims that the system thrust to power ratio can be significantly-improved. A comparable decrease in system noise is also predicted, but it remains to be shown experimentally.

EAD is not a panasas. The problems with the inherent-instability Tomains a major obstacle in its application. Attendant with the instability would be aggrevation of the noise problem.

It is believed the potential merits of EAD variant further experimental and theoretical-investigations to eliminate the instability problem and to delineate the absolute level of noise reduction.





Figure 1. Competison of Conventional and RAB Fee Configurations

NOISE ANALYSIS OF THE EXTERNAL AERODYNAMIC DIFFUSER APPLIED TO SHROUDED PROPELLERS

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Fan Pressure Ratio Figure 2. Power Lavels at the Fundamental of Blade Passing Prequency vs.-Fressure Ratio

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THEORETICAL AND EXPERIMENTAL STUDIES OF HELICOPTER HOISE DUE TO BLADE-WORTEX INTERACTION Sheils Widsall, Sing Chu and Albert Lee Department of Aeronautics and Astronautics Massachusetts Institute of Technology ABSTRACT

The generation of impulsive sound, commonly called blade slap, due te blade-vortex interaction for helicopter rotors is discussed. Two cases are considered: first, blads-vertex interactions for which the angle between the blade and vortex is loss than a critical value such that the ostire longth of the blade patticipates in efficient sound generation--likely to occur for tandes rotors only; second, blade-vortex interaction in which the unsteady interaction of the vortex with the tip of the blade in the primary cause of noise--important for the single rotor belicopter. For the first type of blade vortex interaction, the unsteady lift on the blades is calculated using an existing linear unsteady aerodynamic theory for oblique blade-vortex interactions. For the tip dominated blade-vortex interaction, unsteady slender-body theory is used to calculate the unsteady force on the blade as it oncounters the vortex. A theoretical model for radiated sound due to the transient lift fluctuations is presented. Predictions of the directivity, frequency spectrum and transient acoustic signal are presented. Calculations of the transient-signal are presented in comparison with recent experimental results. The agreement is good, particularly for the small angle blade-vortex interactions.

Introduction

The generation of lift by a helicopter rotor in forward flight is accompanied by the creation of an aerodynamic flow field of great complexity in both space and time. The characteristic noise signature is-largely determined by the fluctuating loads on the blades due to operation in this nonuniform flow field. In many cases, the operation of the helicopter rotor produces an impulsive sound. One source of this is due to transonic flow effects at the tip on the advancing bladeside. A recent paper by Lyon (1) has demonstrated that when an airfoll changes its forward speed relative to the fluid in an unsteady momer, as does a rotating blade in forward flight, sound is generated even though the flow speed is less than sonic everywhere. Another source of blade slop is the unsteady lift fluctuation on a blade due to interaction with the vortex-from another blade.

Even when the helicopter operates in a condition which subjectively is described as non-banging, it is likely that blade-vortex interaction prevides much of the higher harmonic content in the rotational noise spectrum. As has been noted by many authors, the boundary between blade-slap noise and rotational noise is not sharp. Below speeds for which compressible blade slap can occur, both are due to fluctuating forces acting on the blade which although very complex are none-the-less deterministic. The distinction between blade slap and rotational noise is made for convenience, upually on basis of subjective response.

In this paper, we discuss two potential-flow m-lets for the flowawting life due to blode-vortex interaction and the resulting impulsive noise signature. Some recent experimental results are also presented.

If we consider the roter flow fields shotch in Fig. 1 we see that the possible blade-vortex interactions are quite different for the single roter as compared with the tondem roter. As is well known, for the tandem roter, blade-vortex interactions can take place in which the angle between the blade and vortes is small (say less than 30°) and for which a good portion of the blade will esperience a "fluctuating lift forceThis of course gives rise to tandom-rotor blade slap which on the nover helicopters was substantially reduced by raising the aft rotor well above the forward rotor. For the single rotor helicopter it is likely that the blade tip on the advancing side in the most likely area of blade-vortex interaction although a possible interaction could occur between blade 3 and the vortex from blade 4. (See Fig. 1). Since the rotor wake in not well modeled by assuming no distortion of the vortex filaments (the rigid-wake assumption) a great deal more must be learned from flow visualization to accurately locate the vortices relative to the blades. Two potential-flow models which are appropriate for tandom-rotor blade interaction and single-rotor tip interaction will now be discussed.

If we consider the tandom-rotor flow field interaction sketched in Fig. 1 and we see that the essence of the blade-vortex interaction problem is that of a long blade passing obliquely over a vortex. Except-near the blade tip, the aerodynamics of this interaction can be modeled as a two-dimensional airfoll in an oblique gust. Two recent aerodynamic theories have been developed to predict the unsteady life fluctuations on a blade due to an oblique sinusoidal gust. Filotas (2) has considered the oblique gust interaction for incompressible flow. Johnson (3) has considered the oblique gust interaction for subsonic compressible flow. Johnson has also applied this theory to the calculation of helicopter airloads for bladevortex interactions.

In a recent-paper, Widnall (4) presented a model for sound radiation dow to this type of blade-vortex interaction. The results of this analysis will be discussed and compared with experiments.

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Multe the analytic model of blade-vortex interaction present in (6) is very suitable for the-tandem-rotor interactions, it would not correctly predict the radiated noise due to blade-vortex-interaction near the tip on the advancing blade side of a single-rotor holicopter. This is because the wasteady aerodynamics assumes an infinite two-dimensional blade with no tip. This aerodynamic model is not able to account-for the unsteadimess as the tip of the blade rotates and moves over the vortex.

A preliminary treatmant of this aspect of blade-vortex interaction, based on sleader-body theory, will be discussed.



GINE IMPORTANT BLADE-VORTEX INTERACTION



FIG.1 SKETCH OF TIP VORTEX CONFIGURATION FOR SINGLE AND TANDEM HELICOPTER ROTORS.

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THEORETICAL AND EXPERIMENTAL STUDIES OF HELICOPTER NOISE DUE TO BLADE-VORTEX INTERACTION

INPULSIVE HOISE DUE TO SCADE-VORTER INTERACTION --- HODEL I

The most straight forward calculation of the impulsive noise due to blade-vortex interaction is to use the model sketched in Figure 2. In this model the observer is located in the fluid at a distance r from the location of a vortex, which is taken at root in the still fluid. The blade moves in the positive y direction at to be nd U a distance h above the vertex, which is oblique to the leading edge by an angle λ . The vortex height h is taken as constant along the span. The sound sensrated by repeated accuracion of this transiant. Is occur for helicopter eneration. is built up in a simple vey from the fourier transform of the transient signal. This simplified model contains the essential features of the blade-vortex interactions which occur for tandem rotors but does not include the complexities of blade rotation, muniform free stream at each blade element due to rotation, the curvature of the se the vortex filement and changes in distance between the blade and vortex along the length of the blade. In the calculation of the unsteady lift on the blade a twodimensional theory is used, thus ignoring three-dimensional effects at the tip. The finite longth of the blade is considered only in the acoustic calculation.

A. The Unsteady Acrodynamics Of Blade-Vertex Interaction

The unstandy lift on the blade due to blade-wortex interaction is calculated using linear unsteady seredynamics in a manner analogous to the theory of Sears (3) developed for parallel interactions. The unsteady lift on the blade is primarily due to the interaction between the vertical velocity field of the disturbance and the solid airfoil surface. Linear theory treats this vertical velocity input as an imposed unstandy upush field which creates the unsteady lift distribution on the sinfoil surface mecassary to satisfy the condition of no flow through the airfoil, Figure 3 shows the geometry of the interaction. As is standard in







FIG. 3 GEOMETRY OF BLADE/VORTEX INTERACTIONS.

unstandy moredynamics, the blade samicherd b_g , and the blade velocity U are used as reference quantities. The mondimensional frequency is then $S=b_g/U$, the Strouhal frequency.

The velocity field of a vortex of strength I located a distance h from the blade may be modeled as a distribution of oblique sinusoidal gusts. Using Fourier transforms, travertical velocity field at the airfeil location due to the vortex may be written

$$u(s) \varphi \sim \frac{\Gamma}{2\pi} \frac{s}{s^2 + h^2} = \int_{-\pi}^{\pi} U(s) e^{+i\sigma s} ds, \qquad (1)$$

where

$$W(\sigma) = \frac{\delta T}{4\pi \cdot |\sigma|^{\alpha}} - |\sigma|^{h}$$
(2)

is the Poweler transform of W(s). For a real vertex, with a viscous core, a reasonable fit to the velocity distribution is obtained if h is replaced by $(h^2 + h_{\sigma}^2)^{1/2}$, where h_{σ} is the radius of the vertex core, to the point of maximum tangential velocity.

A sinusodial gust with this orientation will cause an unstandy lift on a blade section of frequency

S = d cook	(3)
ed sinuspidel veriation along the open	

$$L(x, S) = L_{a}(S, \lambda) \exp\{i\sigma x \ oin \lambda - iSt\}, \qquad (4a)$$

or alternately,

 $L(\pi, S) = L_{\mu}(S, \lambda) \exp\{i \sigma \sin \lambda \{\pi - (\cosh/\sin \lambda)c\}\}$ (4b)

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 (\mathfrak{h})

This can be interpreted as a sinusoidal pattern of lift visit's is convected along the blade with convection speed

For the simplest acoustic model, a criterion for very efficient sound radiation would be $U_g > \sigma$, the speed of sound. This would correspond to radiation from a disturbance moving at a supersonic spied with respect to the fluid.

The unsteady lift for such an oblique sinusoical gust interaction is available from the incompressible flow theory of Filetas (2) or the more general subsonic theory of Johnson (3) in the form

 $L(x,S,\Lambda) = \{2\tau_0 \cup_{k=0}^2 (\sigma_{k-1} + c X + \pi_2) \} \{ (k_g x - St) \},$

where

To obtain the spectrum of the 1113 due to biade-vortex intraction, $L(\bar{x}, S, z)$ from Eq. 6 is multiplied by the fourier transform of the vortex velocity, Eq. 2, expressed as a function of S. A factor 1/cosA appears in the transformation do to dS. Expressing the unsteady lift as a function of frequency and A only, we obtain

$$L(x, S, \Lambda) = (2\tau_{21}t^{2}b_{0})C_{L2D}(S/\cos\lambda, \Lambda, H)e^{i(k_{x}x - St)}$$

$$\int \int \frac{1}{4\left(\frac{1}{2}t\right)^{2}} \frac{e^{-\frac{1}{2}S/\cos\lambda\frac{1}{2}\lambda}}{\cos\lambda}$$
(7)

Filotas has developed a simple analytic expression for \mathcal{C}_{L2D} (\mathcal{C}_{L2D} is a complex quantity with both magnitude and phase dependent upon frequency)

C_{L2D}(S/cos4,A; H = 0)

$$= \left[\frac{1}{\sqrt{1 + \frac{1}{\cos \lambda}} + \frac{1}{(1 + \cos^2 \lambda + x - 5 \tan^2)}} \right]_0^{-10}$$
 (8a)

where the a-rodynamic phase shift between the gust input and the unsteady lift is

$$\frac{4(S, \Lambda; H = 0)}{S \cdot [1 - \frac{Y \cdot [\frac{Y}{2} - \lambda]}{\cos^{1} + 2tS \cdot [1 + \frac{1}{2} \sin \Lambda]}}$$
(8b)
(8b)

This expression was used in the numerical predictions of the acoustic transfert signal due to blide-vortex interaction. A more complete account of these aerodynamic theories can be found in (2) to (3).

8. Acoustic Rediation From Blade-Vortex Interaction

In developing the expression for sound generated by blade-vortex interaction, we consider the blade translating normal to its leading edge to pass over the vortex which is at rest in the still fluid, as sketched in Fig. 2. For a helicepter in forward flight, there is a flow siong the blade which could be represented by saveping back one blade. This additional coeplication has not been included, since the convective Hach number of flow along the blade never exceeds the forward flight speed of the helicopter. In addition, on the advancing blade side where the Hach number is the highest, the most critical condition for noise generation, the flow component along the blade is identically zero.

In (b), a detailed analysis of the acoustic field due to a single-frequency considered unstably life-way presented assuming their the blade cherd-is smaller then a wavelength so that the unsteady lift may be modeled as a line of acoustic dipoles, distributed along the span, moving with velocity U in the y-direction.

Under these conditions the far field growatic pressure due to a single frequency component of unstandy lift caused by the oblique sinusoidal gust was shown to be

where L_0 is the amplitude of the functuaring lift, y and ϕ are the elevation and azimuth angles of Fig. 2, h is the angle between the blade and the vortex H is the blade Mach number, k is the u-oustic wave number u/c. (Equation 9 differs from eq. 30 of ref (4) in that an error was made previously in poing from acoustic power to acoustic pressure for a moving aroustic source). Equation 9 didicates that the angle h between the blade and vortex has a major effect on the acoustic field. This is because the angle between the vortex and blade determines the trace velocity of the interaction along the blade. If this trace velocity is subsonic, very little acoustic power is generated for the fluctuating force level which exists at the various spanwise stations along the blade. In fact, if the bladz were infinitely long, exactly no sound usuid be generated by these fluctuating forces, (This is discussed in more detail in (4)).

Figure 4 shows the maximum amplitude of the directivity function defined as

$$D(0,\psi) = \frac{\sin[\pi_{0}\kappa[\tan 1/N - \cos \theta \sin \pi//L - N \cos \theta \cos 2)]}{\pi_{0}(1 - N \cos \theta \cos \theta)}$$
(10)

$$D(0,\psi) = \frac{\sin[\pi_{0}\kappa[\tan 1/N - \cos \theta \sin \theta/(L - N \cos \theta \sin \theta)]}{\pi_{0}(1 - N \cos \theta \sin \theta)}$$
(10)

$$v_{\theta} = \frac{\sin[\pi_{0}\kappa[\tan 1/N - \cos \theta \sin \theta/(L - N \cos \theta \sin \theta)]}{\pi_{0}(1 - N \cos \theta \sin \theta)}$$
(10)

for various combinations of Λ and Mach number M. The most important feature of these curves is the dependence on Λ . As the angle between the blade-and vortex increases, the acoustic efficiency is greatly reduced. The results of ref.(4)also indicated a strong beaming of the signal in a direction normal to the blode (say within 20°).



FIG. 4 MAXIMUM AMPLITUDE OF THE DIRECTIVITY FUNCTION AS A FUNCTION OF 8:20 bg D (θ, ψ_{DT1}) FOR hs_>>1.

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Since the directivity function does not centain the magnitude of the unsteady lift, a further reduction in the signal is obtained as A increases due to a decrease in the fluctuating lift. Fig (5) taken from (4) indicates the effect on the acoustic spectrum of the reduction in unsteady lift due to increasing blade vortex angle A and blade vortex spacing h. Recalling that an increase in vortex core size is equivalent to an effective increase in h, we can see a reduction in level and high frequency content would accompany an increase in vortex core size.

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As A approaches 90° the acoustic and aerodynamic theories in this model predict no unsteady lift and no sound radiation. This is one reason why this model does not characterize blade-vortex interaction which occur near the tip for a single rotor since these interactions occur at angles very close at 90°. The complexities of the real flow which have been left out of the simplified model must then be re-examined.



FIG. 5 NORMALIZED SPECTRA OF THE TRANSIENT BLADE/VORTEX INTERACTION AS A FUNCTION OF S; A = BLADE/VORTEX ANGLE, h=BLADE/ VORTEX SEPARATION.

EXPERIMENTAL STUDY

Some of the earliest experimental data we had accres to on the acoustic signature due to blade-wortes interaction was obtained by Boring Vertol (6) using the model rotor of McCormick (7). The comparison between the peak to peak pressure in the transient acoustic signal as obtained from the experiment and as predicted form the theoretical model are shown in Fig. 6 and 7, then from (4). Also shown is a aketch of the transient acoustic pulse from both the theoretical prediction and the experiment. We felt that the double pulse obtained in the experiment was the result of reflection of some marky surface. This was later confirmed when we obtained our one shortmental results. Also shown in Fig.-6-is the theoretical prediction of the effect of a charge in core size on the signal. As would be expected the care size affects the level significantly for very close interactions but is unimportant if the blade passes only through the potential-flow region of the vector,

We have now begun to obtain experimental data on radiated noise due to bladevortex interaction in our open jet wind tunnel. Figure 8 shows a skonstic of the experiment (the tunnel with the model helicopter rotor and the upstream vortex generator) as well as the transient accustic signal due to blade-vortex interaction at an angle A+40°. The accustic signature is processed on a "Moveferm Educator" which extracts the repeated transient signal from the uncerrelated background noise. The lower trace shows the row data (at a reduced scale), the upper trace the extracted blade-vertex transient signal. The left-hand curves shows the acoustic signal obtained from the model rotor without flow in the tunnel. This signal is just the rotational noise of the model rotor in hover. The right-hand curves show the acoustic signal due to blade-vortex interaction -- the vortex being generated upstreem in the tunnel by a fixed vortex generator. The processing of the signal by the wave analyser improves the clarity of the transient signal in comparison with the raw



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data. The typical shape of the blade-vortex interaction transient-is clearly visible in the processed signal. One can also see the reflected pulse from the concrete ceiling (the ceiling will eventually be covered with an anechoic treatment). This reflected pulse is much clearer in some of the acoustic data which will be presented later in this paper.

In order to predict the transient acoustic pulse one must know the tangential velocity distribution in the vortex. This was obtained by measuring the vorticity distribution in the vortex (near the point of intersection) with the vorticity meter developed by McCormick (8). The experimentally determined vorticity distribution and the calculated tangential velocity distributions are shown in Fig. 9. In applying the analytical prediction method for intersection through the vortex cere, the vortex is modeled as a potential vortex with the effective distance and circulation chosen so as to match both the location and magnitude of the maximum normal velocity at the blade.

The experimental results for the peak-to-peak pressure in the transient acoustic signal, present in the form 20 log Δp re $\Delta 002$ µb vs. the blade-vortex separation h in inches, are presented in Figs. 10, 11, 12 and 13 for values of blade-vortex interaction angle Δ of 0°, 11°, 38.5° and 63°. The results indicate a rapid decrease in SPL as Λ and h increase. The agreement-between theory and experiment is certainly acceptable considering the simplicity of the model. In replacing a rotating blade interacting with a vortex with a finite length blade translating over a vortex, one does not krow precisely how to choose the affective translational velocity and the offective blade interaction length. The agreement between theory and experiment is poor for very large interaction angles, (λ +65°). This is to be expected since many of the assumptions in the simple model are not valid as the blade-vortex interactions occurs near the tip region. The present analytic model seems to underpredict the radiated noise although we consider the experimental results to h_{ν} somewhat preliminary



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6. S'EXPERIMENT TO MEASURE TRANSIENT ACOUSTIC SIGNAL DUE TO BLADE - VORTEX INTERACTION .

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FIG. 13 THE EFFECT OF SPACING BETWEEN VORTEX AN ROTOR ON SPL OF TRANSIENT SIGNAL; & +63.5".

since the amechoic treatment has not yet been applied to the walls of the test area.

Figures 14 and 15 show the shape of the transient pulse for $\Lambda = 11^{40}$ and $\Lambda = 63^{40}$ obtained from the experiment as well as from analytic predictions. The experimental results show many reflections from the wells of the enclosure which make the interpretation of just what constitutes the blade-slap signature a bit difficult. The second pulse has been identified as a reflection from the celling with later returns coming from the wells and the floor. The analytic predictions do agree with the shape of the "first-arrival" of the transient signal.

The effect of rotor angular velocity on Δp is shown in Fig. 16. In this emperiment, the circulation of the vortex was held constant. The theoretical curve predicts an increase in SPL proportional to U^4 , the experiment suggests U^5 with some scatter. The U^4 dependence ocurrs because the induced angle of attack for a given circulation is inversely proportional to velocity.

In an actual helicopter (holding the lift constant) the circulation would be roughly inverse to the velocity so that the blade-slap signature SPL would increase as U^2 . This however ignores the effect of this change in operating condition on both the vortex core size and the blade-vortex separation--both very important parameters in determining the blade-slap signatury.

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FIG. 14 EXPERIMENTAL RESULTS AND THEORETICAL PREDICTIONS OF THE ACOUSTIC PULSE DUE TO BLADE - VORTEX INTERACTION; A = 11*.





FIG. 15. EXPERIMENTAL RESULTS AND THEORETICAL PREDICTIONS OF THE ACOUSTIC PULSE DUE TO BLADE - VORTEX INTERACTION ; A = 63*.



FIG. 16 EFFECT OF ROTOR ANGULAR VELOCITY ON SPL OF TRANSIENT SIGNAL.



While the analytic model of blade-vortex interaction is very suitable for the tandem rotor interactions, it does not correctly predict-the radiated noise due to blade-vortex interaction near the tip on the advancing blade side of a single rotor helicopter. This is because the unsteady aerodynamics assumes an infinite (two-dimensional) blade with no tip. This arrodynamic model is not able to account for the unsteadiness as the tip of the blade rotates and moves over the vortex.

Qualitatively, we expect the force on the blade due-to blade-vortex interaction to behave as shown (fig. 17). When the blade is in position (i) the net force due to the presence of the vortex is small, in position (4) it is also small because the positive and negative forces along the spon will nearly cancel. However, as the blade moves from (1) to (4) a negative force will be feir as the tip interacts with the negative downwash of the vortex; the net unsteady force, F(t), should behave as sketched. The radiated noise is determined by the rate-of-change of this force $\frac{dF}{dt}$ (t).

We will argue that since the rate of change of angle of attack at the tip due to the presence of the vortex, especially in the situation where the vortex is very close to the surface of the wing the unsteady flow field may be analyzed by applying alender body theory to the tip region. This of course is not valid in from the tip. Although analytic difficultier present a rigorous matching to a two-dimensional or lifting-line theory for the rest of the blade, we feel that come insight into possible optimum tip pin form shapes might be goined by applying the misple ideas of slenderbody theory rather than attempt a complete numerical treatment of the full threedimensional unsteady are dynamics of the tip. Signeder-body theory does however have a number of pscullar fustures even in steady flow which are difficult to accept for helicopter-blade tips--As will be seen.

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FIG. 17 BLADE-VORTEX INTERACTION IN THE ROTOR TIP REGION.

Figure 18 shows the geometry of blade-vortex interaction at the tip in which the coordinate system is so chosen that ξ and η axes are on the blade with the ξ satis parallel to the vortex while the η axis is normal and passes through the intersection of leading edge and trailing edge (in the case shown in figure 18, the tip edge is also treated as a trailing edge). Since the vortex-filament is static with respect to the fluid (under the rigid wake assumption) in this coordinate system, the free stream velocity V_{g} is in the ξ axis direction and the blade is moving in η direction with velocity V_{g} . Both V_{f} and V_{g} are functions of flight speed and advance ratio. They are also functions of time but for the short period of interaction, they are assumed to be uniform for simplicity.

From many experimental works such as Simons, Pacifico and Jones (9) and Piercy (10) it is found that the corp diameter of the tip vortices are of the order of one tenth of the blade chord. This fact allows the use of slender-body theory to calculate the unsteady force acted on the blade and thus its time derivative. By using the alender-body theory, three-dimensional unsteady compressible flow problem can be reduced to two-limensional steady incompressible flows in the crossflow plane with the third space coordinate and time as parameters no the governing equation is

$$\frac{3^2}{34^4} + \frac{3^2}{34^4} = 0 \tag{11}$$

and the preseure is given by

$$p = -p \left[\frac{2\phi}{2\phi} + \nabla_{\mu} \frac{2\phi}{2\phi} \right]$$
(12)

From Fig 18 the crossflow has a semi-infinite plate and a vertex, the potential f the flow can be found through Schwarz - Christoffel transformation



FIG.18 BLADE ~ VORTEX INTERACTION NEAR THE TIP AND THE TWO-DIMENSIONAL FLOW IN THE CROSS-FLOW PLANE.

$$\phi = \frac{\Gamma}{2\pi} \left[\tan^{-1} - \frac{\sqrt{r} \sin\left(\frac{\phi}{2}\right) - \sqrt{A_{r}} \sin\left(\frac{\phi}{r}\right)^{2}}{\sqrt{r} \cos\left(\frac{\phi}{2}\right) - \sqrt{A_{r}} \cos\left(\frac{\phi}{r}\right)^{2}} \right]$$
(13)

$$= \tan^{-1} \frac{\sqrt{\overline{r}} \sin \left(\frac{\overline{\theta}/2}{2}\right) - \sqrt{\overline{A_{r}}} \sin \left(\frac{\theta_{r}/2}{2}\right)}{\sqrt{\overline{r}} \cos \left(\frac{\overline{\theta}/2}{2}\right) + \sqrt{\overline{A_{r}}} \cos \left(\frac{\theta_{r}/2}{2}\right)}$$

where

$$= \{(n - t)^2 + c^2\}^{1/2}$$
(14)

$$\tilde{\Psi} = \tan^{-1} \left(\frac{\zeta}{\eta - \tau} \right)$$
(15)

$$A_{g} = [\tau^{2} + h^{2}]$$
 (16)

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$$\Phi_{\mu} = \tan^{-1} \left(\frac{h}{m}\right) \tag{17}$$

C and t exist as parameters in t, for straight leading edge

$$t (t, t) = V_c t + t \cot \delta_L$$
(18)

where $\delta_{\underline{L}}$ is the interaction angle with looding edge. So the pressure can be written as

$$\mathbf{y} = -\mathbf{y} \frac{\partial \delta}{\partial T} \left(\frac{\partial \tau}{\partial L} + V_g \frac{\partial \tau}{\partial L} \right) = -\mathbf{p} V_g \left(1 + \frac{\partial \tau/\partial L}{V_g \left(2 \tau/\partial L} \right) \right) \frac{\partial \delta}{\partial L}$$
(19)

with t(L,t) given by (10)

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(20)

(22)

(26)

$$p = -p V_f \left(1 + \frac{V_c}{V_f} \tan \delta_L\right) \frac{\partial \phi}{\partial c}$$

In this process, the unsteady part of the pressure is written in terms of the steady part; this will simplify the space integration process to get the force. From the slender-body theory, the portion of the blade after the intersection of leading edge and trailing edge will make no contribution to the lifting force so the sorce per unit length along the blade is given by

$$f(t_{n}; t) = \int_{LE}^{C=0} \Delta p \rangle_{C=0} \frac{dC}{dt}$$
(21)
$$= \rho - V_{f} - (1 + \frac{V_{C}}{V_{f}} \tan \delta_{L}) \Delta \phi \rangle_{C=0} \frac{1}{LE} \int_{LE}^{C=0} \delta_{L} dt$$

where

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since a is continuous at the leading edge so

 $t_n = x(t_n, t) = n$

$$f(t_n; t) = o V_f \left(1 + \frac{V_c}{V_f} t_{n-\delta_c} \right) \delta + I_{c} = 0$$

$$\zeta = 0 +$$
(23)

with (13) substitute into (23)

$$(t_{\eta}; t) = -\frac{p_{\tau}}{s} v_{f} (1 + \frac{v_{c}}{v_{f}} \tan \beta_{L}) [t_{\eta}]^{-1} \frac{2\sqrt{t_{\eta}} \sqrt{\lambda_{f}} \cos (\theta_{\tau}/2)}{\lambda_{f} - t_{\eta}}]_{f} = 0$$
(24)

The section lift coefficient can be obtained as

$$C_{f}(f_{\gamma}; t) = \frac{f(f_{\gamma}; t)}{1/2 \rho V_{f}^{2}(2b_{\rho})}$$
(25)
= $-\frac{1}{\tau} \left(\frac{f}{b_{\rho} V_{f}} \right) \left(1 + \frac{V_{c}}{V_{f}} \tan \delta_{L} \right) \left[\tan^{-1} \frac{2/f_{\gamma}}{A_{f}} \frac{\sqrt{A_{p}}}{\Delta_{f}} \cos \left(\frac{\sigma_{J}}{2} \right) \right]_{L} = 0$

But it should be noted that this result is applicable only to the tip region of the blade while away from it, two dimensional lifting line theory should be used to calculate the section lift coefficient. This gives

$$C_{f2D}(r:t) - 2\pi \frac{\forall}{\forall f}$$

= $(\frac{\Gamma}{b_{\alpha} \forall f}) \frac{b_{\alpha}(t-f_{\alpha})}{(t-f_{\alpha})^{2} + h^{2}}$

(To correctly match these two regions an intermediate three-dimensional region should be used. This may be investigated in the future.)

In Fig. 19 C_ℓ $(f_{\gamma};t)$ and $C_{\ell 20}$ $(f_{\gamma}^*;t)$ for given $\forall_c,~\delta_L$ and h are plotted for various times.

There should be a region on the blade, say $(t_n)_{c=0} = r_n$, where the theory used to calculate the force should be changed from the tip elender-body theory to the two-dimensional lifting line theory. Then the total force on the blade will be

 $F(t) = \{1/2 > V_{\xi}^2 (2b_0)\} \times$

$$\left(\int_{0}^{r_{\rm B}} C_{f}\left(e_{n};-\epsilon\right) \cdot d_{-}t_{n} + \int_{r_{\rm B}}^{r_{\rm B}} C_{f2D}\left(e_{n};\epsilon\right) d_{-}t_{n}^{2}t_{f} = 0$$



FIG. 19 THE SECTION LIFT COEFFICIENTS FROM SLENDER-BODY THEORY AND LIFTING LINE THEORY AT THE TIP REGION.

Before we evaluate the force and its time derivative, we first examine the characteristic of the "unsteadiness" of the two parts of the force due to the tip region and due to the rest of the blade.

The second part of the force, which can be obtained from two-dimensional-theory, has a definite lift distribution which depends only on the angle of attack. Hence, its "unsteadiness" comes just-from its uniform translation along the blade. From early consideration for the tip-interaction of single rotor, this translation_speed is very low and the acoustic radiation from this translating force is negligible.

So the effective force that contributes to the acoustic radiation is only that due to the tip region

$$\mathbf{F}_{eff}(\mathbf{c}) = [1/2 \circ V_f^{-2} (2b_0)] \{ \int_0^{V_m} \mathbf{C}_{f-}(t_{\gamma}; \mathbf{c}) d t_{\gamma} \}_{f=0}^{J_{f=0}}$$
(28)

With (25) substituted into (28),=this becomes

$$F_{eff}(t) = -\frac{p \Gamma V_f}{\pi} \left(1 - \frac{V_c}{V_f} \tan \delta_L\right) x$$

$$\left((r_m - t) \tan^{-1} \frac{2\sqrt{r_m} \sqrt{A_f} \cos \left(\frac{\theta_f}{2}\right)}{A_f - r_m} - 2\sqrt{A_f} \cdot \overline{r_m} \cos \left(\frac{\theta_f}{2}\right)$$

$$- \frac{h}{2} \log \left(\frac{r_m + A_f}{r_m + A_f} - 2\sqrt{r_m} \sqrt{A_f} \sin \left(\frac{\theta_f}{2}\right)\right) I_{f_e} = 0$$
(29)

the time derivative or the force-is given by

$$\frac{\mathrm{i}\mathbf{F}_{off}}{\mathrm{d}\mathbf{t}}(t) = \frac{\mathrm{i}\mathbf{F}_{off}}{\mathrm{i}\mathbf{t}} \frac{\mathrm{i}\mathbf{t}}{\mathrm{i}\mathbf{t}} = \frac{\mathrm{i}\mathbf{t}^{\mathrm{T}}\mathbf{V}_{\mathrm{F}}\mathbf{V}_{\mathrm{F}}}{\mathrm{v}_{\mathrm{F}}} (\mathbf{1} + \frac{\mathrm{v}_{\mathrm{F}}}{\mathrm{v}_{\mathrm{F}}} \tan \delta_{\mathrm{L}}) \times \qquad (30)$$

$$(\tan^{-1}(\frac{2\sqrt{r_{\mathrm{m}}}/\Lambda_{\mathrm{F}}}{\Lambda_{\mathrm{m}}} \cos (\varepsilon_{\mathrm{F}}/2)) = 2\sqrt{(r_{\mathrm{m}}/\Lambda_{\mathrm{F}})} \cos (\theta_{\mathrm{F}}/2))$$

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THEORETICAL AND EXPERIMENTAL STUDIES OF HELICOPTER NOISE DUE TO BLADE-VORTEX INTERACTION

This is the strength of the acoustic dipole and the acoustic pressure field can easily be calculated.

The value of r_m remains an open question. It may depend on the unsteadiness i.e. V_c . Results from (30) are plotted in Fig. 20 by choosing a cutoff of one chord leight; this shows the shape of the impulse qualitatively.

From (30) we can see that the magnitude of the time derivative of force increases with V_c and δ_L . This suggest that it can be reduced by modifying the rotor and blade design.

First consider V_c, for a given flight speed. V_c can be reduced by reducing the advance ratio with the extreme limit V_c = 0 at hovering.

The leading edge interaction angle δ_L depends on both the interaction angle Λ and the evept angle of leading edge (Fig. 21). δ_L is decreasing as Λ increases, this can be accomplished by two ways -- reduce the advance ratio and increase the number of blades. To increase the number of blades has another benefit that the loading on each blade is reduced and thus the strength of the tip vortices can be reduced. δ_L can also be reduced by having a swept forward leading edge near the tip; this is described geometrically in Fig. 21.

To summarize, the blade slap noise of a single rotor can be reduced by having a smaller advance ratio, more blades on the rotor and a swept forward leading edge near the tip of the blade. Of course, the noise could be further reduced by-reducing the flight speed and gross weight.

CONCLUSIONS

We have presented the mesults of our ongoing theoretical and experimental studies of signature due to blade-vortex interaction. The experimental and theoretical results obtained to date clearly demonstrate the ability of simple unsteady potential flow models to predict the blade-slap signature. The analysis of the tip region using signeder body theory is still in the very preliminary stages. We would hope-to obtain some-insight into possible optimum tip shapes to reduce blade slap noise and to test these concepts in the wind tunnel.





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FIG. 21 MODIFIED BLADE TIP WITH SWEPT-FORWARD LEADING EDGE.

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SYNTHESIS OF HELICOPTER ROTOR TIPS FOR LESS NOISE

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Richard H.-Lyon®, William D. Mark, and Robert W. Pyle, Jr.

Bolt Beranek and Newman Inc. Cambridge, Massachusetts 02138

ABSTRACT

Theoretical and computational studies of rotor tip sound radiation have been conducted for the purpose of designing rotor tips that radiate less sound in specified frequency bands. Consideration is given to radiation due to lift and thickness effects. Effects of unsteady vortex shedding on lift radiation are examined. It is shown that lift radiation is generally negligible in comparison with thickness radiation. A computational algorithm is developed for the synthesis of tip shapes that couse minimum thickness radiation in specified frequency bands. Numerical results are obtained for tip shapes that minimize highfrequency radiation, and a substantial reduction of radiation in comparison with existing shapes is shown. The uncertainty principle is used to establish a fundamental relationship between the tip section chord length and the minimum possible cutoff frecuency for effective suppression of high-frequency sound. Factors that affect trade-offs between choices of airfoil section and planform are discussed.

1. INTRODUCTION

In this paper, we present the results of theoretical and computational studies of rotor-tip sound radiation. The purpose of the research is the design of rotor tips that radiate less sound in particular frequency bands. By design, we mean the selection of a combination of planform and airfoll section shapes based on a constical and aerodynamic considerations. The sound radiation that we consider is that due to compressibility effects that are important as the Mach-number of the advancing rotor tip approaches unity.

The theory of found radiation from accelerating airfoils has been presented in another paper (J). Sound radiation is due both to the lift distribution on the tip and to the longitudinal section area. Since a functional-relation was developed between the radiated sound spectrum and these functions, it is implicit that we should be-ably to derive tip shapes that will radiate less sound, at least in some frequency bands.

As we seek other shapes however, it will be necessary to impose constraints on the area and lift distributions. The area function must be positive. We can keep the tip volume constant by fixing the-integral of the-area function, and the center of gravity is fixed if the first-moment of area is fixed. In two case of the lift distribution, we might like to keep the total lift, the pitching moment (first chordwise moment of lift), and the center of pressure fixed. The actual constraints employed are discussed below.

4

It is not necessary to point out that designing airfoils by acoustical considerations is unusual. To aeredynamicists such an approach may seem naive and presumptive. But we do not minimize the aerodynamic problems. The design suggestions offered here are only partial. Sufficient freedom will be available after the acoustical design is complete to allow for aerodynamic performance optimization, which must include both acoustical and aerodynamic experimentation. We do feel, however, that our approach - the definition of thickness and lift distributions through acoustical considerations = is a viable and desirable procedure.

11. RADIATION BY LIFT AND THICKNESS EFFECTS

In Kef. 1, a particular model is used for the calculation of the sound radiation. The rotor tip is modeled as a "torpedo", an axially symmetric shape with lift and longitudinal section area (LSA) identical to that of the tip section. Further, the lift and area effects are replaced by body force and volume velocity distributions along the axis of the torpedo. Thus, we replace a boundary value problem on an airfoil that has dimensions in feet with an inhemogeneous wave equation problem where the source terms are concentrated along a single line. It is worthwhile dircussing the limitations that may result from this approximation.

The area effect alone can be treated as a distribution of simple sources over the tip planform. Generally, these sources produce no normal velocity in the plane in which they are breated. Thus, the rigid boundary condition is automatically satisfied for thin airfoils. In addition, as we showed in Ref. 1, the direction of sound radiation from the area effect in very strongly forward. thus, in the spanwise direction, the trace wavelength for radiating wavenumbers is quite large compared to the tip spanlength. This means that the radiated sound is insensitive to the distribution of volume velocity in this dimension. The volume velocity may therefore be concentrated . to a-line in the chordwise direction.

The 'satification for the lift-body force replacement is more difficult. In part it is, as we shall see, that the lift radiation is to much weaker than the area radiation that it 'ocsn't much matter what we assume as long as we get a "ball park" calimate. We can, however, do better than that.

The dipole-distribution over-the planform representing the lift stress would produce nonzero velocitier in the plane of the airfoil; therefore, the rigid surface of the airfoil will affect the radiation from these sources. We need to estimate the size of this effect that we are not accounting for. We can do this by noting that Pfowes Williams has shown that supersonic multipoirs radiate independently of each other (2).

Presently, Indieson of Mechanical Engineering, Hossachuretts Institute of Technology, Gasbridge, Masachusetts 02139.

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Thus, at least for the supersonic wavenumbers describing the source distribution, the effect of an infinite rigid plane passed through the plane between the positive and negative monopoles making up the elementary dipoles is to increase the sound radiation by 6 dB (3 dB for each side of the plane). Since the actual rigid plane is the size of the tip planform, the radiation augmentation will be less than 6 dB. With the infinite rigid plane inserted, the justification for collapsing the dipoles into a chordwise line is the same as above, since the radiation from the lift distribution is also very strongly forward [2].

In Ref. 1, the lift force per unit length in the chordwise direction is given by

$$L(x) = P_{e}V_{r}^{2} a(t) \{BC_{n}(x)\}$$
 (1)

The product BC_p is proportional to the incremental lift force per radian increase in angle of attack, and is expressed in Ref. 3 by the product

$$\frac{1}{2} BC_{p}(x) = \frac{v}{v_{t}} \frac{\Delta v_{a}}{v_{t}}, \qquad (2)$$

where the two factors on the rhs of Eq. 2 are tabulated for various airfoils.

Applying the formulation of Ref. 1, we have calculated the sound-power radiated by an airfoil of the following specifications:

Section Shape	NACA 0012	Rotor Disk Diameter	48 52
Chord Length	18 in.	RPM	300 (5 Hz)
Number of Blades	2		
Tip Span	46 in.	Forward Speed	333 ft/sec
Average Angle of Attack	8°	Advancing Tip Hach No.	0.96

The radiated sound power is expressed as the m.s. pressure at 50 ft-averaged over all directions. The results of the calculations are shown in Fig. 1. The difference in level in nearly all bands is at least 40 dB and in the higher bands it approaches 70 dB. Thus, even with a 6 dB augmentation of lift radiation due to blade baffling effects, our conclusion that lift radiation is unimportant would not be affected.



Fig. 1. One-third octave band spectra for thickness and lift radiation. (Sectext for parameters.)



Fig. 2. One-third octave band spectra for thickness and lift radiation including high-frequency vortex shedding. (See text for parameters.)

We can include the effects of unsteady vorticity shedding from the rotor tip by postulating a "high frequency" component in the angle of attack. As an example, we have assumed the same conditions as those for Fig. 1, but have added a fluctuating angle of attack of 1 degree amplitude at the 50sh harmonic of the rotor rotation rate (frequency of vortex shedding = 250 Hz). The results of this calculation are shown in Fig. 2. Note that the augmentation in radiation is quite broad band, and does not show up in the 250 Hz band at will. This example does show, however, that excessive fluctuation in the shed vorticity during the forward sweep of the blade may cause lift radiation that could compete with thickness radiation in the higher bands.

The principal lesson from the foregoing, insofar as design is concerned, is that we can concentrate on minimizing thickness radiation. This circumstance is fortunate since the relation between tip shape and thickness radiation is very direct, while the lift distribution depends on shape in a rather complicated fashion [3]. Thus, our approach is to synthesize tip shapes for minimal noise, under certain constraints. We can then-look at the pressure distributions on these derived "optimal" shapes from the viewpoint of flow separation and lift radiation. If they appear to be acceptable, they will become candidates for a new tip design, to be studied experimentally.

III. MATHEMATICAL FORMULATION AND NUMERICAL RESULTS

In Ref. 1, the LSA function A(x) was expanded in an exponential Fourier series,

$$A(x) = x^{-1} \prod_{m=m}^{m} A_{m} e^{\frac{1k_{m}x}{m}}, \quad 0 \le x \le 1$$
 (3)

where $k_{g} = 2\pi r/t$. The period 1 is the spacing between rotor tips in the rotor model used in Ref. 1; each interval 1 contains one rotor tip. It was shown in Ref. 1 that, for practicel purposes, there is a one-to-one correspondence between the frequency spectrum of thickness radiation and the squared magnitudes $|A_{m}|^2$ of the expansion coefficients of n(x). The radiatud angular frequency corresponding to a spatial wavenumber k_{m} is ck_{m} , c being the speed of sound. We can therefore find optimal LSA functions
by minimizing the values of $|A_m|^2$ over chosen wavenumber bands, where the minimization is subject to an appropriate set of constraints applied to the function A(x).

The expansion coefficients in Eq. 3 are

$$A_{m} = \int_{0}^{t} A(x) e^{-ik_{m}x} dx , \qquad (4)$$

which is also-the-Fourier transform of A(x) evaluated at wavenumber k_m . We can therefore formulate the optimization problem in terms of the Fourier integrals,

$$A(x) = \frac{1}{c\pi} \int_{-\infty}^{\infty} \tilde{\lambda}(k) e^{ikx} dk , \quad -\infty < x < \infty$$
 (5)

$$\tilde{A}(k) = \int_{-\infty}^{\infty} A(x) e^{-ikx} dx , \qquad (6)$$

instead of Fourier series. The optimization problem is thus reduced to minimizing the integral

$$L \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} V(k) [\vec{\lambda}(k)]^2 dk , \qquad (7)$$

where V(k) is a-nonnegative real spectrum weighting function that is chosen to be-large over the range of k-where we wish to minimize $\|\tilde{A}(k)\|^2_{p-and}$ where the admissible A(x) are required to satisfy an appropriate set of constraints.

A. Choice of Constraints

The LSA function A(x) must be constrained in the minimization process so that it_will be possible to design_an aerodynamically acceptable tip from the minimizing A(x) function by choosing an appropriate tip planform. (Factors affecting this choice are discussed in Sec. IV.) To help insure that the minimizing form of A(x) is "reasonable", we shall constrain the admissible class of A(x) to those-functions lying between appropriately specified upper and lower bounds which are functions of x. That is, the admissible A(x)-shall be constrained to satisfy

where a(x) and b(x) are these bounds, and where L is the maximum chorm of the tip section under consideration. At the very least, it is clear that A(x) must be constrained to be positive and finite; that is, a(x)>0 and b(x)<=.

If $|\tilde{A}(k)|^2$ were to be minimized over a certain interval of k subject only to the constraint of Eq. 8, it is clear that the minimizing A(x) function would tend to fall on the lower bounding function a(x), since the requirement that $|\tilde{A}(k)|^2$ be small favors small values of A(x). Such behavior unnecessarily restricts the shape of A(x) and can be avoided by also constraining the area of A(x) = 1.e., by requiring that the admissible A(x) also satisfy

$$\int_{a}^{b} A(\mathbf{x}) \, \mathrm{d}\mathbf{x} = \mathbf{H}_{a} \,, \tag{9}$$

where X_{ij} is a specified number.

We shall require A(x) to satisfy one additional constraint. It is shown in Appendix A that, insofar as the constraint of Eq. 8 permits, the minimization of $|\tilde{A}(x)|^2$ over given bands, subject only to the constraint of Eq. 9, would lead to minimizing functions A(x) that tend to be symmetric about the midchord point x = L/2. This aerodynamically undesirable result can be controlled by additionally constraining the first moment of A(x):

$$\int_{0}^{L} xA(x) dx = M_{1}, \qquad (10)$$

where M_i is specified. Equations 9 and 10, taken together, are equivalent to constraining the area and center of gravity of A(x). It is clear that intelligent choices for M_0 and M_1 will not be independent of the choices for the bounding functions a(x) and b(x).

8. Formulation-of Problem in Terms of Sampled Area Functions

For numerical solution of the minimization problem, the limit constraint described by Eq. 8 is, in large measure, the determining factor in-our choice of method of representing the LSA function. This is because it must be possible to conveniently transform this constraint to whatever representation of the LSA function we decide upon. This transformation is most easily carried out if we base our representation of A(x) on an appropriate set of the sample values $A_j = A(x_j)$. It-will be convenient to use equally spaced samples; that is, $x_j = j\Delta$, $j = 0,1,\ldots, 11$, where Δ is the sampling interval, and where N = L/L. For values of $x \neq x_j$, A(x)-is defined from the set of samples A_j , $j = 0,1,\ldots, 11$ by interpotation. Our representation of A(x) can thus be expressed as

$$A(\mathbf{x}) = \sum_{j=0}^{N} A_j \mathbf{w}_j(\mathbf{x}) , \quad A_j = A(j\Delta) , \quad (11)$$

where

$$w_{i}(x) = w(x-j\Lambda) , \qquad (12)$$

where $w(\xi)$ is an appropriate interpolating function with the properties

 $\kappa(n\Delta) = 0, m = \pm 1, \pm 2, \dots$ (14)

In most of our numerical work we have used for the interpolating function $% \left({{{\left[{{{{{\bf{n}}}_{{{\rm{s}}}}} \right]}_{{{\rm{s}}}}}} \right)$

$$w(\xi) = \frac{\sin(\pi\xi/\Delta)}{\theta^{-1}\sinh(\theta\pi\xi/\Delta)}, \qquad (15)$$

which is a generalization of an interpolating function suggested by Lerner [4]. The decay of the tails of Eq. 15 is controlled by the parameter=0. For large 0, the tails-have strong decay, whereas, as 6=0, the rhs of Eq. 15 approaches the familiar [$sin(s\xi/\delta)$]/($s\xi/\delta$]. For most of our numerical work, we have used 0 = 0.40.

To minimize the integral of Eq. 7 subject to the constraints of Eqs. 8-10, it is first necessary to express $\left|\tilde{A}(k)\right|^2$ in terms of A(x) as represented by Eq. 11. After carrying out the integration in Eq. 7, we can then express the integral I as an exこうちょう いいのないないないないないないないないないないないない しょうちょう

(8)

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plicit function of A_{i} , A_{i} ,..., A_{N} .

Defining

$$\hat{w}_{j}(k) = \int_{-\infty}^{\infty} w_{j}(x) e^{-ikx} dz$$
, (16)

we obtain, by substituting Eq. 11 into Eq. 6,

$$\bar{A}(k) = \int_{j=0}^{N} A_{j} \bar{w}_{j}(k) .$$
 (17)

Multiplying Eq. 17 by its complex conjugate yields

$$\begin{split} |\widetilde{A}(\mathbf{k})|^{2} &= \sum_{j=0}^{N} \sum_{m=0}^{N} \Lambda_{j} A_{m} \widetilde{\Psi}_{j}(\mathbf{k}) \widetilde{\Psi}_{m}^{0}(\mathbf{k}) \\ &= \sum_{j=0}^{H} \Lambda_{j}^{2} \widetilde{\Psi}_{j}(\mathbf{k}) \widetilde{\Psi}_{j}^{1}(\mathbf{k}) + \sum_{j< m} \sum_{k=0}^{N} \Lambda_{k} \widetilde{\Psi}_{j}(\mathbf{k}) \widetilde{\Psi}_{m}^{0}(\mathbf{k}) \\ &= \sum_{j=0}^{N} \Lambda_{j}^{2} |\widetilde{\Psi}_{j}(\mathbf{k})|^{2} + 2 \sum_{j< m} \sum_{k=0}^{N} \Lambda_{k} Re[\widetilde{\Psi}_{j}(\mathbf{k}) \widetilde{\Psi}_{m}^{0}(\mathbf{k})] , \quad (18) \end{split}$$

where the asterisk denotes the complex conjugate, and where Re[...] denotes the real part of the quantity within the brackets. We now substitute Eq. 12 into Eq. 16 and then_introduce the change of variable $\xi \neq x-j\Delta$:

$$\tilde{w}_{j}(k) = \int_{-\infty}^{\infty} w(x-j\Delta) e^{-ikx} dx$$

$$= e^{-ikj\Delta} \tilde{w}(k) , \qquad (19)$$

where we have used the definition

$$\widetilde{\mathbf{w}}(\mathbf{k}) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} \mathbf{w}(\xi) \, e^{-\mathbf{i}\mathbf{k}\xi} \, \mathrm{d}\xi_{-} \, . \tag{20}$$

Combining Eqs. 18 and 19 yields

$$\begin{split} & [\hat{A}(k)]^{2} = [\hat{A}(k)]^{2} \left(\sum_{j=0}^{N} A_{j}^{2} + 2 \sum_{j \leq n}^{N} A_{j}^{j} + 2 \sum_{j < n}^{N} A_{j}^{$$

One can show that as $\Delta * 0$, Eq. 21-becomes in the limit

$$[\tilde{\lambda}(x)]^{2} = 2 \int_{\xi=0}^{L} \int_{x=0}^{L-\xi} \Lambda(x) \lambda(x+\xi) dx \cos(k\xi) d\xi_{-}, \qquad (22)$$

which is the Wiener-Khintchine theorem for deterministic waveforms A(x) that are defined over a finite interval 0 < x < L. We can therefore interpret-Eq. 21 as the Wiener-Khintchine theorem for sampled_deterministic waveforms.

To express I explicitly in terms of $A_0,A_1,\ldots,A_N,$ we must now substitute Eq. 21-into Eq. 7. Defining

$$G_{n} \stackrel{\Delta}{=} \int_{0}^{\infty} V(k) [\tilde{w}(k)]^{2} \cos(kn\Delta) dk , n=0,1,...,N , (23)$$

we obtain

$$I(A_{s},A_{1},\ldots,A_{H}) = G_{s}\left(\sum_{n=0}^{H} A_{n}^{2}\right) + 2\sum_{n=1}^{N} \left[G_{n}\left(\sum_{j=0}^{H-n} A_{j}A_{j+n}\right)\right].$$
(24)

Equation-24 is the desired explicit expression for the weighted integral-of Eq. 7 insterms of the samples $A_j \in A(j\Delta)$. The coefficients G_n are defined by Eq. 23.

Next, we must express the constraints in Eqs. 8-10 in terms of the LSA function samples A_1, A_2, \ldots, A_N . From Eqs. 11-13, we immediately have for the limit constraint

where

and

$$b_{j} \triangleq b(j\Delta) , j=0,1,...,N ,$$
 (27)

are specified sets of numbers. From Eqs. 6, 17, and 19, we have for the volume constraint

$$\sum_{j=0}^{N} A_j = \frac{\dot{R}_0}{w(0)}$$
 Constraint 3, (28)

where, from Eq. 20_{μ} it follows that

$$\tilde{w}(0) = \int_{-\infty}^{\infty} w(\xi) d\xi , \qquad (29)$$

is the area under the interpolating function. Turning to the first moment constraint, we have by differentiating Eqs. 6 and 17, and then combining the results:with Eq. 10

$$x_{1} = \sum_{j=0}^{N} \lambda_{j} \tilde{w}_{j}^{j}(0) , \qquad (30)$$

where the prime denotes differentiation. Next, we differentiate Eq. 19-and combine-the result with Eq. 30-which gives, after some rearrangement,

$$\sum_{j=0}^{N} (j\Delta + \gamma)\lambda_j = \frac{M_1}{\widetilde{w}(0)} , \quad Constraint C , \quad (31)$$

where

$$\gamma \stackrel{\text{d}}{=} 1 \frac{\overline{u}^{*}(0)}{\overline{u}(0)} = \frac{\int_{-\infty}^{\infty} \xi u(\xi) d\xi}{\int_{-\infty}^{\infty} u(\xi) d\xi} , \qquad (32)$$

according to Eq. 20. Notice that γ is the center of gravity of the interpolating function $w(\xi)$; thus γ is zero for symmetric interpolating functions such as Eq. 15. Equation 31 is the desired expression for the first-moment constraint in-terms of the LSA: function samples A_1, A_2, \dots, A_N .

Equations 24, 25, 28, and 31 collectively define the optimization problex under consideration. The problem is to minimize $I(A_0, A_1, \ldots, A_N)$, as given by Eq. 24, where the admissible vectors $\{A_0, A_1, \ldots, A_N\}$ are subject to the constraints given by Eqs. 25, 28, and 31. Our method of solution, which is based on the Gradient Kethod, is described in Appendix B.

C. Solutions for Particular Cases

For several combinations of parameters, we have used the technique described in Appendix B to find-optimum LSA functions. In all-of our numerical work, the initial vector $\{A_{\mu}^{(0)}, A_{\mu}^{(0)}, \ldots, A_{N}^{(0)}\}$ was taken to be a sampled version of an NACA 0012 airfeli. The upper and lower bounding vectors that constitute Constraint λ were both taken proportional to the initial vector.

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In most cases, $\{a_0, a_1, \ldots, a_N\}$ and $\{b_0, b_1, \ldots, b_N\}$ were taken to be 0.5 and 1.5 times $\{A_0^{(G)}, A_1^{(O)}, \ldots, A_N^{(O)}\}$ respectively. The moments H_0 and H_1 , used in Constraints B and C, were evaluated from the initial vector using Eqs. 28 and 31. This insured that, at every stage of the iterative procedure described in Appendix B, $\{A_1^{(1)}, A_1^{(1)}, \ldots, A_N^{(1)}\}$ had the same area and center of gravity as the NACA-0012 starting vector.

Figure 3 shows the optimum LSA functions and their corresponding spectra for chord lengths L ranging, in 7.5-ft increments, from 1.5 ft to 4.0 ft. For all of the results_presented in Fig. 3, the spectrum weighting function V(k)-was chosen to minimize the sound radiated over the entire frequency band above 700 Hz. This was accomplished by taking $V(k)_s k = 2\pi f/c$, to be unity in-the band from 700 Hz to 11,300 Hz and zero outside this band. However, the value of 11,300 Hz can be regarded as being effectively-infinite since the sampled LSA function representation used in computing the results of Fig. 3 has an inherent cutoff frequency of about 5500 Hz as we shall now show.

Using tabulated integrals, we find the Fourier transform, Eq. 20, 00 the interpolating function, Eq. 15, to be

$$\tilde{v}(k) = \frac{\Delta \sin(\pi/\Phi)}{\cosh(\pi/\Phi) + \cosh(k\Delta/\Phi)}$$
(33)

In all of the cases shown in Fig. 3, we have taken 0 = 0.40. For this value of 0, Eq. 33 is very close to a rectangular function with cutoff wavenumber $k_c = (\pi/\Delta)$. Hence, the cutoff frequency- f_c , in Hz, is $f_c = [ck_c/(2\pi)] = [c/(2\Delta)]$. For all cases shown in Fig. 3, we have taken $\Delta = (L/N) = 0.10$ ft; hence, $f_c = 5c = 5500$ Hz, the number cited above. The fact that the cutoff wavenumber of w(k)-coincides with the inherent cutoff wavenumber of cur sampled LSA function representation follows directly from Eq. 21.

The radiated spectra were computed using the formula

$$\int_{\kappa_{1}}^{r_{2}} |\tilde{A}(\kappa)|^{2} d\kappa = \Psi_{\bullet}(\kappa_{1},\kappa_{2}) \Big[-\sum_{n=0}^{N} A_{n}^{2} \Big] + 2 \sum_{n=1}^{N} \Psi_{n}(\kappa_{1},\kappa_{2}) \Big[\sum_{j=0}^{N \geq n} A_{j+n} \Big] ,$$

where

 $\mathbf{v}_{\mathbf{n}}(\mathbf{x}_{1},\mathbf{x}_{2}) \stackrel{\text{d}}{=} \int_{-\mathbf{k}_{1}}^{\mathbf{k}_{2}} |\bar{\mathbf{x}}(\mathbf{x})|^{2} \cos(\mathbf{k}\mathbf{n}\delta) d\mathbf{k}_{2}, \qquad (35)$

where k_1 and k_2 are the lower and upper wavenumbers ($k = 2\pi f/c$) corresponding to the standard one-third octave bands. Equation 34 was-obtained by integrating Eq. 21 between the limits k_1 and k_2 . The spectra of both the initial sampled version of the NAGA-0012 airfoil and the final optimized LSA function is shown for each of the-cases studied.

Referring now to the spectra shown in Fig. 3, we see that virtually no improvement in the spectrum of the LGA function with a:1.5-ft chord was possible. However, as the chord was increased from 1.5 ft to 3.0 ft, considerable improvement was achieved. Increasing the chord beyond 3.0 ft produced no further significant improvement relative "o the NACA 0012 shapes.





Fig. 3. Optimum-LSA functions and their radiated one-third octave band spectra (solid curves) for chord lengths L-ranging from 1.5 to %.0 ft. Radiation is animized above 700 Hz. Upper and lower bounds (dashed curves) on-allowable LSA functions are 0.5 and 1.5 times_NACA 0012 sirfolf-of uniform spanwise thickness. Dashed spectra are these of NACA 0012 airfols of same chord length, sectional area, and center of gravity as optimum LSA functions.





Fig. 5. Optimum L3A functions and their radiated one-third octave band spectra (solid curves) for 3.0 ft chord lengths. Padiation is minimized above 700 Hz. Lower bound on allowable LSA functions: 0.75, 0.5 and 0.25 times NACA 0012 airfoll or uniform spanwise thickness. Upper bound is 1.5 times NACA 0012 airfol for all-cases. Dashed curves have same meaning as in Fig. 3.

(34)

Turning now to the optimize LSA functions shown in Fig. 3, we see that the result in the 1.5-ft chord case has a very blunt leading edge. As the chord is increased to 3.0 ft, both the leading and the trailing edges drop onto the lower-bound constraint. Then, as the chord=is further increased, the trailing edge rises and takes on a more complex shape.

Table 1 lists the ordinates of the optimum LSA functions shown in Fig. 3. Since the termination of the optimization technique was chosen to given answers accurate to one part in one thousand, three significant figures are tabulated in Table 1.

TABLE 1. ORDINATES OF OPTIMUM LSA FUNCTIONS SHOWN IN FIG. 3. ONGINATES ARE GIVEN AS FRACTIONS OF CHORD-LENGTH L.

x, ft	L=1.5	L=2.0	L=2.5	L=3.0	L=3.5	L=4.0
0.00.000001111111111220002222223333345673904 012345678901234567890123456789012345678901234567390	.030 .084 .089 .107 .114 .122 .120 .120 .120 .120 .028 .030 .013 .001	.000 .056 .067 .083 .102 .118 .129 .137 .131 .139 .137 .131 .106 .072 .037 .024 .037 .024 .031	.000 .018 .049 .068 .103 .118 .122 .150 .150 .150 .150 .150 .150 .087 .027 .027 .027 .027 .017 .001	.000 .0040 .0040 .0050 .119 .1253 .159 .1511 .1511 .150 .057 .057 .057 .057 .057 .057 .057 .0	.000 .038 .058 .058 .056 .118 .133 .155 .155 .155 .149 .1431 .155 .155 .149 .1431 .155 .067 .067 .067 .064 .0328 .0328 .0328 .0328 .0328 .056 .057 .044 .0328 .056 .057 .056 .056 .055 .055 .055 .055 .055 .055	.000 .026 .036 .0567 .084 .115 .129 .129 .129 .129 .129 .129 .129 .129

In Fig. 4 we show the effects of varying the height of the lower bound constraint for the case of a 3.0-ft chord. Going from top to bottom in Fig. 4, the lower bound was taken to be 0.75, 0.50, and 0.25 times the NACA 0012 starting shape. The spectrum weighting function V(k) and interpolating function $w(\xi)$ were the same as those used in obtaining the results of Fig. 3. Thus, the middle result shown in Fig. 4 is a repeat of the 3.0-ft chord result shown in Fig. 3. The general behavior of the spectra shown in Fig. 4 is as expected.

In Fig. 5 we show the LSA function that was obtained by taking V(k), k = 2zf/c, to be unity in the two octave band from 700 Hz to 2800 Hz and zero outside this band. For the interpolating function, we used Eq. 15 with $\theta = 0.50$. The chord L-was taken to be 3.0 ft, and the number of samples N to be 50. This gives $\ell = (L/N)^{-1} = 0.06$ ft; hence, $r_{e} = (c/(24))^{-1} = 9200$ Hz is the inherent-cutoff frequency of the sampled LSA: function representation.





Fig. 5. Optimum LSA function and its radiated spectrum (solid curves) where radiation was minimized between 700 and 2800 Hz. Chord length is 3.0 ft. Dashed-curves have same meaning as in Fig. 3.

It is clear from the spectrum shown in Fig. 5 that the frequencies between 2800 Hz and 9200 Hz were not suppressed in the optimization process. It is this high-frequency content that causes the erratic behavior of the LSA function shown in Fig. 5. However, in comparing the spectrum shown in Fig. 5 with the spectrum for the L = 3.0 ft case shown in Fig. 3, we see that virtually the same reduction of radiated sound in the two octave band from 700 Hz to 2800 Hz was obtained for the two cases.

To test the dependence of the above results on the particular interpolating function chosen, the 3.0 ft-chord case shown in Fig. 3 was also run with a triangular interpolating function that decreased linearly from unity at any given sample to zero at its two nearest neighbors. The maximum fractional difference between the two LSA functions obtained was 2.35. The optimum LSA function obtained with the interpolating function of Eq. 15 would seem to be somewhat preferable, however, since the continuous function defined between the sample points by-Eq. 11 is smooth when Eq. 15-is used for-interpolation.

The general behavior of the spectra shown in Fig. 3 can be partially explained with the aid of the uncertainty principle for Fourier transforms, which can be expressed (5) hs

$$2k_{\text{H}} L_{e} \geq 2\pi$$
, (36)

or, in our application, as

$$2f_{m}L_{e} \ge c , \qquad (37)$$

where $k_{\rm m}$ is the maximum-angular wavenumber in the spectrum-of the LSA function; hence, $r_{\rm m} = ck_{\rm m}/(2\pi)$ is the maximum frequency in the radiated spectrum in Hz, and where $L_{\rm e}$ is the nominal (3) effective LSA function chord, and crist the speed of sound.

Since we are considering rather sharp cutoffs in the frequency domain, we might first take $L_e = 1/2$, where L is the actual chord. The "uncertainty principle", Eq. 37 in this case becomes $f_{\rm m}L \ge c$. Solving the equality in this relation for L, using c = 1100 ft/sec and $f_{\rm m} = 700$ Hz, gives L = 1.57 ft. For the situation studied in Fig. 3 we could not, therefore, have expected sharp reductions in the radiated spectrum for chord lengths less-than about 1.5-ft. In-fact, we saw little reduction for the 1.5 ft chord, but began to see strong reductions for the larger chords. However, we must recall that the center of gravity of the LSA functions of Fig. 3 has also been constrained to be off center. As far as the uncertainty principle is concerned, this has the effect of reducing the effective chord length somewhat further. The sharp reduction in the sound

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radiation at frequencies beyond 700 Hz that occurs as the chord is increased from 1.5 ft to 3.0 ft is therefore completely consistent with the "uncertainty principle", as described by Eq. 37. The results of Fig. 3 therefore can be regarded as verification of Eq. 37, which is an expression of the fundamental limitation on the reduction of high-frequency sound radiation due to thickness effects.

IV. IMPLICATIONS FOR ROTOR TIP DESIGN

The synthesis results presented in Sec. III determine an LSA function only. The relation teteren the LSA function and the airfoil section and planform functions is shown graphically in Fig. 5, which is reproduced from Ref. 1. It is clear that having determined a new LSA function, we have the option of using a standard airfoil section and modifying the planform or the reverse, or modifying both planform and airfoil section. The purpose of this section is to discuss the factors that affect our choices in doing this.



Fig. 6. Diagram of rotor blade tip showing how area function $A(\mathbf{x})$ is derived.

If we sary the airfoil-section shape, then two-dimensional airfoil theory can be used to compute the new pressure distribution as a function of chord for both surfaces [3]. Of course we wish the lift to remain constant, but we will also have to examine the pitching moment, and center of pressure. Certain aerodynamic derivatives, such as the changes of pitching moment and lift with angle of attack should also be evaluated so that the aerod-lastic stability of the rotor is maintained.

A major difficulty with tip design of current rotors is the rather bluff end of the rotor. This is thought to cause-separation of flow when the tip is forward of its maximum relative speed point, so-that the inflow vector has a component inward along the blade-span. When the inflow has this component, then the bluff end of the rotor is heading into the flow, and irregular or separated flow is likely to result. To avoid this problem, a combination of planform and airfoil section that presents an aerodynamic section to the flow as the inflow vector changes would be desirable. From an acoustical viewpoint, this means that the 534 function should also be relatively invariant to the direction of inflow, at least-for variations in inflow direction of-20 degrees or so from the normal to the span. The LSA function must now be defined along the direction of the inflow vector, not along the chord (normal to the span).

The-forces and moments on the outer regions of the rotor also affect the airfoil section/planform-tradeoff. The lift on the rotor increases as one proceeds outward toward the-tip, falling off rapidly at the tip. The distribution of lift-along the span must be compatible with the spanwise bending rigidity. This would not seem to be a serious factor, however, in-choosing the planform-or airfoil section shapes.

If the lift varies along the span, vorticity will be shed along the span and the tip vortex will be spread out in a sheet. The amount of this spreading may have some effect on the shape (core size) of the trailing vortex from the tip and on the interaction of this vortex with a trailing rotor blade. Such interaction is known to produce acoustical impulses, termed "blade slap".

Clearly, the research presented in this paper-does not allow us to draw-detailed designs of rotor-tips that not-only produce less sound, but are also aerodynamically well behaved, etc. There is still enough flexibility in the choice of in airfoil to allow considerable-latitude in designing for proper aerodynamics, since the allowable set of planform-airfoil-section combinations that meet the required LSA shape is still-quite large. We believe that more theoretical research should-be carried out on the simultaneous optimization-for both acoustical and aerodynamic performance. We also believe-that supporting experimental studies = both acoustical and aerodynamic - should be carried-out to clarify actual benefits of the new designs and-how sensitive the gains are to minor molifications in-the airfoil and flow parameters.

Quite apart from the improved design of rot, - tips for less noise radiation, we believe that the optimization method presented in Sec. III and the Appendices has a much broeder application potential to minimizing the noise from rotors and propellors. Since analytical formulations for the sound radiated from rotating airfolls have been developed, it should be possible to minimize the rotational noise from propellors, for example, by procedures very similar to those presented in this paper. and the second second

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V. ACKNOWLEDGEMENT

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APPENDIX A. MATHEMATICAL MOTIVATION FOR THE FIRST NOMENT CONSTRAINT

We show here that minimization of $|\tilde{A}(k)|^2$ over given bands of k, subject only to the constraint of Eq. 9, would lead to minimizing functions A(x) that are even functions about the midchord point x = L/2. After changing the origin of the abscissa to the midchord point x = L/2 by defining the new coordinate y = x-(L/2), we express the translated longitudinal section area function $A^{\dagger}(y)$ as the sum of its even and odd parts $\bar{A}_{\phi}^{\dagger}(y)$ and $\bar{A}_{\phi}^{\dagger}(y)$ respectively:

$$= \Lambda_e^{\mathsf{T}}(\mathbf{y}) + \Lambda_{\phi}^{\mathsf{T}}(\mathbf{y}). \tag{A.1}$$

For the Fourier transform $\tilde{A}^{\dagger}(k)$ of $A^{\dagger}(y)$ we have

$$\tilde{\lambda}^{\dagger}(k) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} \lambda^{\dagger}(y) e^{-iky} dy \qquad (A.2)$$

where

$$\hat{s}_{c}^{\dagger}(h) = \int_{-\infty}^{\infty} A_{c}^{\dagger}(y) - \cos(ky) dy$$

$$\hat{s}_{s}^{\dagger}(k) = \int_{-\infty}^{\infty} A_{c}^{\dagger}(y) \sin(ky) dy . \qquad (A.3)$$

From Eqs. A.1 and A.2 it follows that

$$\bar{A}(k)]^2 = [\bar{A}^{\dagger}(k)]^2$$

= $[\bar{A}^{\dagger}_{c}(k)]^2 + [\bar{A}^{\dagger}_{s}(k)]^2$. (A.4)

Now, since $A_{4}^{\dagger}(y)$ is an odd function, it contributes nothing to the area-of $A^{\dagger}(y)$ which is the same as the area of A(x); however, the contribution of $A_{4}^{\dagger}(y)$ to $[\tilde{A}(k)]^2$, according to Eqs. A.3 and A, 4, is: $[\tilde{A}_{3}^{\dagger}(k)]^2$. It follows that the minimization of $|\tilde{A}(k)|^2$ over given bands; subject only to the area constraint of Eq. 9, would yield minimizing functions $A^{\dagger}(y)$ that have no odd part; that is, minimizing functions A(x) that are-symmetric-about the midthori-point x-a L/2.

APPENDIX 3. NETHOD OF OPTIMIZATION

The problem-is to minimize I(A, ,A, ,..., A,,), as given by Eq. 13, where the admissible vectors $(A_{a}, A_{b}, \dots, A_{d})$ are subject to the constraints given by Eqs. 25, 28, and 31. Before discussing our approach to this problem, it is instructive to consider the problem with constraint A, Eq. 25 removed. The resulting problem is a classical minimization problem-that, in principle, is easily solved using Lagrange sultipliers. The solution involves matrix-inversion and the solution of linear algebraic equations only. We world generally expect the solution to be unique; that is, we would expect only one vector $\{A_n, A_1, \dots, A_N\}$ to yield a stationary value of $\{A_n, A_1, \dots, A_N\}$ subject is the constraints of Eqs. 28 and 31. However, we would not generally expect this solution vector to-setisfy the constraint given by Eq. 25. In fact, some elements of this solution vector may have negative values. A-similar situation=exists with the "aristional problem that is formulated by findingian extremum of the integral in Eq. 7, where in this care $|\bar{A}(k)|^2$ is given by Eq. 22, and where the admissible A(x) functions are subject to the constraints of Eqs. 9 and 10. In this case we would not generally expect the minimizing function to satisfy Eq. 8.

Our approach to the minimization problem defined by Eqs. 24, 25, 28 and 31 has been-based on an intuitively appealing technique generally called either the method of gradients or the method of steepest descent. In discussing our approach, it is convenient to consider any set $\{A_0, A_1, \cdots, A_N\}$ of LSA function samples as a point in a space of N+1 dimensions. Constraint A defines a rectangular region of this space. The collection of points that satisfies *both* constraint 3 and constraint C defines a N-1 dimensional hyperplane within this space. Thus, the admissible points are points on this hyperplane that lie within the closed rectangular region defined by constraint A. Associated with each of these admissible points is a value of $I(A_0, A_1, \cdots, A_N)$. The problem is to find the admissible point $\{A_0, A_1, \cdots, A_N\}$ where $I(A_0, A_1, \cdots, A_N)$ takes on its minimum value.

Our numerical solutions were obtained using an iteration procedure. The procedure we used was chosen instead of one of the rather sophisticated gradient methods such as Davidson's method or the method of conjugate gradients because of the restriction imposed on the admissible domain of $I(A_0, A_1, \cdots, A_n)$ by constraint A. The approach described below is conceptually simple and allows the straightforward imposition of all of the constraints.

Our numerical procedure is begun with an initial choice $\{A_{i}^{(0)}, A_{1}^{(0)}, \cdots, A_{N}^{(0)}\}$ of LSA function samples that satisfies constraints A, R-and C. Hence, this starting point in our N+1 dimensional space lies on the hyperplane defined by constraints B and C, and it lies in the interior of the region defined by constraint A. The computation begins with the evaluation and storing of the N+1 values of G_{n} defined by Eq. 23. $1^{(0)}\{A_{i}^{(0)}, A_{i}^{(0)}, \cdots, A_{N}^{(0)}\}$, the initial value of I, is then evaluated using Eq. 24. An increment δA_{j} in each of $A_{i}, A_{i}, \cdots, A_{N}$ is then computed such that the new point

 $\{A_{g}^{(1)}, A_{1}^{(1)}, \cdots, A_{N}^{(1)}\} = \{A_{g}^{(0)} + \delta A_{g}, A_{1}^{(0)} + \delta A_{g}, \cdots, A_{N}^{(0)} + \delta A_{N}\}$ (B.1)

also-satisfies=constraints A, B and C.

The increments $4A_{j,k}j=0,1,\cdots,N$ are chosen to maximize the rate of decrease of $I(A_0,A_1,\cdots,A_N)$ by taking the vector $\{4A_0,4A_j,\cdots,4A_N\}$ parallel to the negative of the gradient of $I(A_0,A_1,\cdots,A_N)$. Since we want to constrain the argument of $I^{(1)}(A_0^{(1)},A_1^{(1)},\cdots,A_N^{(1)})$, where $I^{(1)}$ is the new value of $I_{j,k}$ to lie on the hyperplane defined by constraints R and C, $I(A_0,A_1,\cdots,A_N)$ must be regarded as a function of only K-1 independent A_j , the two-remaining A_j also-reing regarded as functions of the N-1 independent A_j , where this latter functional-dependence is determined by constraints B and C, Eqs. 28 and 31. We must adhere to this rule in forming the gradient of $I(A_0,A_1,\cdots,A_N)$. Let us designate the two dependent A_j by A_m and A_n . Then A_m and A_n can be explicitly expressed as functions of the N-1 independent A_j by solving Eqs. 28 and 31 for A_m and A_n . Then A_m where the explicitly expressed as functions of the N-1 independent A_j by solving Eqs. 28 and 31 for A_m and A_n . Then A_m and A_n the explicitly expressed as functions of the N-1 independent A_j by solving Eqs. 28 and 31 for A_m and A_n .

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$$A_{m} = \frac{1}{(n-m)} \left[\frac{(n\Delta + \gamma)N_{a} - N_{a}}{\Delta \tilde{w}(0)} - \sum_{j \neq m, n} (n-j)A_{j} \right]$$
(B.2)
$$A_{n} = \frac{1}{(m-n)} \left[\frac{(m\Delta + \gamma)N_{a} - N_{a}}{\Delta \tilde{w}(0)} - \sum_{j \neq m, n} (m-j)A_{j} \right] ,$$
(B.3)

where $j\neq_{2,n}$ designates the set of all integers $0\leq j\leq N$ except j=mand j=n. Continuing to consider A_m and A_n as functions of the N-1 independent A_j , we can now find $\exists I/\exists A_k$ by differentiating Eq. 24:

$$\frac{31}{3A_{k}} = 2 G_{\bullet}(A_{k} - \frac{n-k}{n-m} A_{m} - \frac{m-k}{m-n} A_{n})$$

$$+ 2 \int_{J=1}^{11} G_{J} \begin{bmatrix} J_{-J} \\ J_{0} \\ I = 0 \end{bmatrix} A_{1}(\delta_{1+J,k} - \frac{n-k}{n-m} \delta_{1+J,m} - \frac{m-k}{m-n} \delta_{1+J,m})$$

$$+ A_{1+J}(\delta_{1,k} - \frac{n-k}{n-m} \delta_{1,m} - \frac{m-k}{n-n} \delta_{1,n}) \end{bmatrix} , k \neq m,n$$
(B.4)

where 61, j denotes Kronecker's delta, and where in carrying out the above differentiation, we required the partial derivatives

$$\frac{\partial A_{n}}{\partial A_{k}} = -\frac{(n-k)}{(n-n)} , \qquad \frac{\partial A_{n}}{\partial A_{k}} = -\frac{(n-k)}{(n-n)} , \quad k \neq n, n \qquad (B.5)$$

which were obtained by differentiating Eqs. B.2 and B.3. From the definition of the gradient, the increments δA_j ($j \neq n, n$) are thus given by

$$\delta A_j = -h \frac{2I}{2A_j}$$
, $J \neq n, n$ (B=6)

where h is a constant independent of j that determines the step cize, and where $\partial I/\partial A_j$ is determined for all $\partial \leq j \leq 0$ except J = 0 - m, nby evaluating-the right-hand side of Eq. B.4 using the initial ret $\{A_{ij}^{(3)}, A_{ij}^{(3)}, \dots, A_{ij}^{(3)}\}$ of A_{ij} 's.

From the increments δA_j determined by Eq. .(, the new set of A_j 's is then evaluated for all $0 \le j \le N$ except $j < m_j$ at

$$\lambda_1^{(1)} = \lambda_1^{(0)} + \delta \lambda_1, J \neq m, n$$
 (U.7)

It is possible that one or more of these values of $A_j^{(1)}$ will fall subside the intervals defined-by constraint A. Hence, at this functure, each of these values of $A_j^{(1)}$, $j \neq m,n$ is tested to insure that is satisfier constraint A. Any value that crossed either of the bundaries, a_j or b_j , is set equal to the value of the bundary that was crossed.

Using Eqr. 8.2 and 8.3, $A_{\rm m}^{(1)}$ and $A_{\rm m}^{(1)}$ are then evaluated From the K-1 values of $A_{\rm j}^{(1)}$ determined by Eq. 8.7. These values of $A_{\rm m}^{(1)}$ and $A_{\rm m}^{(1)}$ are then tested to insure that they do not violate constraint A. If either violates constraint A, a smaller value of h in Eq. 8.6 is chosen, and the procedure from Eq. 8.6 on is repeated. The method explained in Appendix 6 for choosing the values of a and n insures that the computed values of $A_{\rm m}$ and $A_{\rm m}$ will select violate constraint A when-reasonable values of h are used. The above procedure for determining $\{A_{\rm e}^{(1)}, A_{\rm i}^{(1)}, \cdots, A_{\rm m}^{(1)}\}$ Governments that this new-point will satisfy constraints A, h and C.

At this stage, the value of $I^{(1)}(\lambda_1^{(1)}, \lambda_1^{(1)}, \cdots, \lambda_N^{(1)})$ is computed using Eq. 24. It is then somepared with the value of

 $I^{(0)}(A_{6}^{(0)},A_{1}^{(0)},...,A_{N}^{(0)})$. Unless h was taken too large, $I^{(1)}$ will be less than $I^{(0)}$. If $I^{(1)}$ is greater than $I^{(0,1)}$ a smaller value for h is chosen, and the operations beginning with Eq. B.6 are repeated. If $I^{(1)}$ is less than $I^{(0)}, \{A_{6}^{(1)},A_{1}^{(1)},...,A_{N}^{(1)}\}$ becomes the new starting point, and the operations beginning with the evaluation of Eq. B.4 ar repeated.

Eventually, for some value of 1, $(1+1)(A_0^{(1+1)}, A_1^{(1+1)}, \dots, A_n^{(1+1)})$ $A_N^{(1+1)}$ will be greater than $I^{(1)}(A_0^{(1)}, e_1^{(1)}, \dots, A_N^{(1)})$. When this occurs, the admissible point (A_1, A_1, \cdots, A_N) , where $I(A_{a},A_{1},\cdots,A_{N})$ takes on its minimum-value, has been overshot. Hence; at this stage, h is given a smaller value and the computation is returned to the operations beginning with Eq. 8.6. Using this smaller value of h, we again continue to march toward the admissible point where I takes on its minimum value, always going in the most downhill direction on the admissible hyperplane defined by constraints B and C, and always staying within the admissible region defined by constraint A. When it is observed that, for some larger 1, I(1+1) again exceeds I(1), then the value for h is further reduced, and computation is again returned to the operations beginning with Eq. B.G. This process is terminated when negligibly small step sizes lead to an increase in I(A, A, ..., An). In our numerical calculations, we automatically terminated the above process when changes in At, with magnitudes no larger than (1/1000) of the largest value of A_1 , led to an increase in the value of $I(A_1, A_1, \cdots, A_N)$.

Because evaluation of the function I and its gradient involves only computation of quadratic forms in the A_{j} 's, each "downhill step" took-relatively little computer time. Thus the comparatively slow convergence (typically, on the order of 100 steps were required) was not costly. In fact, more processor time was required for the evaluation of the coefficients a_{j} through the integrals of Eq. 23 than was needed for the entire gradient descent.

APPENDIX C. METHOD-USED FOR DETERMINING # AND n

At any given stage of the iteration procedure described in Appendix:B, the use of Eqr. B.2 and B.3-to evaluate $A_{\rm m}^{(1)}$ and $A_{0}^{(1)}$ from the remaining $A_{j}^{(1)}$'s guaranteed that the set of $A_{j}^{(1)}$'s. j = 0,1,...,N would satisfy constraints B and G. At each stage of iteration, n and n-were chosen so that the values of $A_{\rm m}$ and An, computed from Eqs. B.2 and B.3, were very unlikely to violate constraint A when reasonably small values for a were used. This was accomplished by-choosing m to be the index J of the LNA function cample of the prior iteration-that had the sargest minimum distance from the bounds aj and bj in the first one-third of the interval digit, and by choosing a in a similar fachien from the indices J in the last one-third of the Interval U<j<N. That is, to determine m at n-given stage of the iteration, we found the maximum over) of the scaller of $(A_j^{(i-1)}-a_j)$ or $(b_j-A_j^{(i-1)})$ as j was varied over the integers Osis[(8-2)/3]. The resulting value of Jewas chosen for m. The came determination over the integers

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 $[(2\bar{N}+2)/3] \le j \le N$ yielded the value j = n. We chose m from the first one-third and n from the last one-third of $0 \le j \le N$ to insure that the magnitudes of the derivaliators n-m and m-n in Eqs. 8.2 and 8.3 were reasonably large. By choosing m and n in the above many, it was assured that the magnitudes of the increments $\delta A_m = (A_m^{(1)} - A_m^{(1-1)})$ and $\delta A_n = (A_n^{(1)} - A_n^{(1-1)})$ could be relatively large without the new values $A_m^{(1)}$ and $A_n^{(1)}$ violating constraint A.

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LIST-OF FIGURE CAPTIONS

- Figure 1. One-third octave band:spectra for thickness and lift radiation. (See text for parameters.)
 - One-third octave band_spectra for thickness and lift radiation including high-frequency vortex-shedding. (See text for parameters.)

- 3. Optimum LSA functions and their radiated one-third octave band-spectra (solid curves) for chord lengths L ranging from 1.5-to 4.0 ft. Radiation is minimized above 700 Hz. Upper and lower bounds (dashed curves) on allowable LSA functions are 0.5 and 1.5 times NACA 0012 mirfoil of uniform spanwise thickness. Dashed spectra are those of NACA 0012 airfoils of same chord length, sectional area, and center of gravity as optimum LSA functions.
- 4. Optimum LSA functions and their radiated one-third octave band spectra (solid curves) for 3.0 ft chord lengths. Radiation is minimized above 706 Hz. Lower bound on allowable LSA functions is 0.75, 0.5 and 0.25 times NACA 0012 airfoll of uniform spanwise thickness. Upper bound is 1.5-times NACA 0012 airfoll for all cases. Dashed curves have same meaning as in Fig. 3.
- Optimum LSA-function: and its radiated spectrum (solid curves) where radiation was minimized between 700 and 2800 Hz. Chord length is 3.0°ft. Dashed curves have same meaning as in Fig. 3.
- 6. Diagram of rotor blade-tip showing how-area function A(x) is derived.

Part 1 Moustic Radiation from a Plane Surface with Application to Rotyrs" by Gregory F. Homics

Abstract

A formalian is developed for predicting acoustic radiation from a plane surface that exerts a fluctuating load upon the surrounding fluid. The development assumes the pressure field on the surface to be random and stochastic; it may be both non-stationary and inhomogeneous. The result is an expression for the acoustic powr spectrum in terms of an integral over the disturbance region of the generalized four-dimensional Fourier spectrum of the forces. It is capable of predicting discrete-frequency as well as broad-band spectra. A feu illustrative examples pertaining to rotors are presented; the results agree with those cases that have been freated previously. The treatment is being extended to the broad-band noise enameting from a rotor in turbulent air.

I. Introduction

The classic problem in rotor noise theory was analyzed by Gutin (1) in-1936. He modeled the blades as B point forces rotating at constant angular velocity with no variation in their magnitudes and obtained a discrete spectrum at multiples of the blade-passage frequency B.A. Lowson and (1,3) Cllorhand , as well as Wright , have extended this to the case where the force varies-simusoically in the azimuth angle. The spectrum is still discrete, though Louson et al. (4) briefly discuss the extension to random leads, and hence brond-band acoustic spectra. Sharland (S) gives evidence that free-stream turbulence can be a simificant factor in such loadings. He estimates the total radiated accustic energy from & fan rotor under such-circurstances; however, his result leans rather heavily on empirical estimates of the correlation areas and is useful primarily in estimating orders of magnitude or in interpreting data. Flowes Williams and Haukings culculate the radiation from a rotating point force with random loading in terms of the load spectrum as measured moving with the dipole. : brar and Tanna⁽⁷⁾ consider the same problem and obtain the acoustic spectrum as a power series in Ω/f . Both leave open the question of how the load spectrum might be related to the turbulence characteristics. iprice (a) and Davik (a) handle this by modeling the blades as an infinite cascade and then using two-dimensional incompressible airfoil-theory; this is a better opproximation for compressors and fans than for helicopter rotors. Both also assume the blade chords to be acoustically compact, i.e., a blade becomes a line of dipoles. In many practical applications, particularly at-higher frequencies, and higher subsonic back numbers, the above assumptions are difficult to justify a priori.

It is hoped that the present treatment will point the way toward relaxing some of these approximations. A groundwork is presented for the prediction of broad-band as well as discrete-frequency noise radiated free a surface distribution of dipoles in an otherwise unbounded fluid; it is directly applicable to calculation of the acoustic signatures of rotors

 This research was supported under contract \$14,120-70 C 0057; it was carried out under the supervision of Professor A.-R. George, whose invaluable guidance is gratefully acknowledged. encountering atmospheric turbulence. The acoustics equations themselves are linear, and linearized acrodynamic theory will be used to obtain the lift response. Hence the overall problem can be viewed as that of determining the statistical response characteristics of a linear system subjected to a random input.

The system may be conveniently divided into two sub-systems: The first determines the lift response of a fixed point in the rotor to a given pattern of turbulence, and the second determines the radiated sound from the lift remonse. The lift response is characterized by an impulseresponse function, or equivalently by an aerodynamic transfer function. We will neglect the effects of drag and centrifugal forces, as well as those of turbulent velocity components in the rotor plane. Assuming the appropriate transfer functions are known, these could be easily included. The second sub-system, using the above response as input, transforms it into the resultant noise spectrum at the observer's polition. This is achieved through the far-field solution of the inhomogeneous acoustic wave equation as formulated by Lighthill . The present discussion concerns prisarily the latter analysis, and # s results are generally applicable to a much broader class of problems than that of rotating-forces: it is easily extended to surface distributions of other acoustic singularities, such as monopoles or quadrupoles. A few elementary examples pertinent to lifting rotors are presented; the results agree_with those of other authors_in those cases previously investigated. A preliminary discussion of the analysis of the lift response is then given.

II. Solution of Acoustic Have Equation

The equation describing the guarantion of traveling waves by a distribution of acoustic dipoles is $^{(n)}$

$$\frac{i}{\alpha_{1}} \frac{\partial^{2} \rho}{\partial x_{1}} - \nabla^{2} \rho = \frac{\partial F_{1}}{\partial x_{1}}$$
(1)

where \vec{F} represents force/volume. The far-field solution can be expressed

$$\rho = \frac{1}{\#\pi a_i^3} \frac{\chi_i}{\hbar^4} \int \left[\frac{\partial F_i}{\partial t}\right] d^3 y$$

Equation: (2) is valid under the following conditions:

$$k\pi \gg -1 \qquad (A)$$

$$\hbar \gg |\vec{g}|_{max} \qquad (E)$$

(2)

(3)

(4)

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Assumption (B) is a statement that the disturbance region appears geometrically compact to the observer. Using the identropic relation, $-\rho = a_{\mu}^{\lambda}\rho$,

and our supposition that $\vec{F} = L \hat{n}_{g}$ (see Fig. 1), we get

$$\mathcal{P} = \frac{1}{4\pi a_{1}} \frac{X_{1}}{\Lambda^{1}} \int \left[\frac{\partial L}{\partial t}\right] d^{2}y$$

In our case, not only does (B)-hold, but to lowest order the forces -all lingin the plane $y_1 = 0$. Hence we can substitute $L = \int \delta(y_1)$, -resulting in the surface integral form

$$\rho = \frac{1}{4\pi a_{e}} \frac{\sin \phi}{\Lambda} \int \left[\frac{3f}{3t}\right] d^{4}y$$

-where it is understood that \vec{y} now lies in the horizontal plane.



Fig. 1. Rotor geometry and coordinate systems.

Since our problem is random, we example an expression for $\mathcal{P}(\bar{x},t)$ as a deterministic function, but we can work with an acoustic intensity averaged over a hypothetical ensemble of realizations. Consider the quantity

$$p^{(\bar{x},t-\bar{\gamma}_{2};j)}p^{(\bar{x},t+\bar{\gamma}_{2};j)}$$

where the argument j is an ensemble parameter whose different integer. values 1, 2,... N refer to different realizations of the same experiment. Performing a statistical-average over all realizations, we obtain-

$$R_{rf}(\vec{x},t,\tau) = \overline{\rho(\vec{x},t-\tau/2)} \cdot \rho(\vec{x},t+\tau/2)$$
(5)

and hence the ensemble-averaged instantaneous intensity as

$$\overline{J}(\overline{x},t) = \frac{\overline{\rho^{*}(\overline{x},t)}}{\overline{\rho_{*} a_{*}}} = \frac{R_{H}(\overline{x},\overline{t},0)}{\rho_{*} a_{*}}$$

(6)

(75)

Now consider the Fourier transform of $R_{pp}(\vec{x}, \vec{t}, \tau)/\rho_0 a_0$, with respect to τ , and its inverse:

$$S(\vec{x},t;f) = \int_{-\infty}^{\frac{\pi}{P_{e}}} \frac{(\vec{x},t;\gamma)}{p_{e}a_{e}} e^{-i\lambda\pi f\gamma} d\tau$$
(7a)

$$\frac{\bar{R}_{P}(\bar{x},t,\tau)}{P_{e}a_{e}} = \int_{-\infty}^{\infty} S(\bar{x},t,f) e^{-i2\pi f\tau} df$$

Substituting from (7b) into (6) we find:

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$$\overline{J}(\overline{x},t) = \int_{-\infty}^{-\infty} S(\overline{x},t,f) df$$
(0)

and hence S is the spectral decomposition of \overline{J} ; it represents the acoustic energy radiated within the frequency interval f to f + df.

substituting for $p(\vec{x}, t; j)$ from (4) into (5) yields

$$\frac{R_{p}(l,t,\gamma)}{f^{0,0}} = \frac{\sin^{1}\phi}{16\pi^{1}f^{0,0}\lambda^{1}} \chi$$

$$\iint_{\substack{\frac{\partial}{\partial t} (\overline{y}_1, t - \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{x} - \frac{g}{g})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z}_1, t + \frac{\gamma_2}{2} - i\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z})/q_0; \quad \frac{\partial}{\partial t} (\overline{z})/q_0; \quad \frac{\partial}{\partial$$

It is convenient to denote the geometric coefficient preceding the integral by the symbol G_{i} . We also introduce the average and relative position vectors, \mathcal{T} and \mathcal{E} , defined by (see Fig. 2)





Fig. 2. Coordinate transformations.

It is easily verified that the Jacobian of this transformation is 1, and hence $d^{b}y d^{b}z \xrightarrow{} d^{b}y d^{b}z$ directly.

Now consider the term $i\vec{x} - \vec{y}i/a$, first retarded time. From Fig. 2 we see that

$$\overline{x} - \overline{y} = \overline{x} - \overline{\eta} + \overline{z}/2$$

$$\overline{x} - \overline{y} = \frac{1}{2} \overline{x} - \overline{\eta}^{+} + \overline{z} \cdot (\overline{x} - \overline{\eta}) + 1\overline{z} \overline{z}^{+}/4$$

$$|\vec{x} - \vec{y}| \simeq |\vec{x} - \vec{\gamma}| \left\{ 1 + \frac{\vec{\varepsilon} \cdot (\vec{x} - \vec{\gamma})}{2 |\vec{x} - \vec{\gamma}|^{\lambda}} + O\left(\frac{|\vec{\gamma}|_{A^{-1}}}{\lambda}\right)^{\lambda} \right\}$$

-(10a)

(106)

(11)

occurring in the

(9)

 \hat{H} being the unit vector along $\vec{X} = \vec{T}$. Similarly

$$|\overline{x}-\overline{z}| \simeq |\overline{x}-\overline{\eta}| - \overline{\varepsilon} \cdot \overline{\eta}/z + O\left(\frac{|\eta|}{\lambda}\right)$$

Thus (9) becomes

$$\frac{R_{qq}(s,t,\gamma)}{p_{s}a_{s}} = G \iint_{-\infty}^{\infty} \frac{\partial f(q-t_{l_{1}},t-\gamma_{2}-\frac{\partial t-q_{1}+\xi\cdot A_{l_{2}}}{a_{s}})}{\int_{-\infty}^{\infty} \frac{\partial f(q-t_{l_{1}},t-\gamma_{2}-\frac{\partial t-q_{1}+\xi\cdot A_{l_{2}}}{a_{s}})}{\partial t} \times \frac{\partial f(q+t_{l_{1}},t+\gamma_{l_{2}}-\frac{\partial t-q_{1}}{a_{s}})}{\partial t} d^{s} \eta d^{s} \xi$$

Form the Pourier transform with respect to \mathcal{T} :

$$S(R,t,f) = G \int_{-\infty}^{\infty} e^{-i\lambda\pi f \tau} d\tau \iint \frac{\partial f(\tau-\tau)}{\partial t} \frac{\partial f(\tau-\tau)}{\partial t} d^{2} \tau d^{2} t$$

and define

being the average retarded time between $\vec{\mathcal{Y}}$ and $\vec{\Xi}$. Then

$$(t,f) = G \int_{a}^{a} e^{-i a \pi f s} ds \iint_{a} e^{+i a \pi f \frac{g}{a}} x$$

$$\frac{\partial f}{\partial t} \left(\frac{\eta}{\eta} \cdot \frac{\delta / a}{a}, t_{mn} - \frac{\delta / a}{2} \right) \frac{\partial f}{\partial t} \left(\frac{\eta}{\eta} + \frac{\delta / a}{a}, t_{mn} + \frac{\delta / a}{2} \right) d^a \eta d^a \varepsilon$$

(12)

(14)

The arguments appearing in the correlation now appear-in symmetric form, allowing us to write

$$S(\vec{x}, t, f) = G \int_{a}^{b} d^{2} \gamma \int_{a}^{b} ds e^{-i\lambda\pi fs} \int_{a}^{b} e^{-i\lambda^{2}f} e^{-i\lambda^{2}f} \frac{f}{s} A_{s} \cdot \varepsilon_{X}$$

$$R_{jj}(\vec{\gamma}, \xi, t_{mas}s) \qquad (13)$$

It is easily shown that replacement of A by \hat{R}_{0} in the exponent requires $\|\hat{g}\|_{Max}^{2}/A \ll \alpha_{0}/f$, or

$$\frac{k \ln n}{2} \ll 1 \quad (c)$$

which is called the Praimhofer or diffraction parameter. Carrying out the last two integrations,

$$S(\vec{x}, t, f) = G \int_{-\infty}^{\infty} d^{*} \eta \cdot P_{jj} (\vec{\eta}_{j} - \frac{f}{a_{j}} \vec{n}_{s}, t_{m_{N_{j}}} f_{s})$$

where $P_{jj} (\vec{\eta}_{j}, \vec{k}_{j} = t_{m_{N_{j}}}, f)$ is the generalized-four-dimensional

Fourier transform of R_{jj} with respect to $\tilde{\epsilon}$ and \tilde{s} , but evaluated at $\tilde{k} = -\frac{s}{a_0} \tilde{a}_{s}$. Note that the appearance of the spatial transform with this argument is a result of having retained differences in retarded times in (11); the decomposition of the lift distribution into its Pourier components in space would be unnecessary had we assured an acoustically compact source region. There is a simple physical interpretation of why the two-dimensional wave vector. It is easily seen that the spatial transform of a fingle-wavelength two-dimensional sinusoid (see Fig. 3) is simply $\frac{1}{4} [f(k_1 - k_0)] + f(k_1 + k_0] f(k_1) f(k_1)$. We have cincled



Fig. 3. Constructive interference at frequency f .

out a magnitude, f/α_{o} , and direction, \hat{R}_{o} , for \vec{K} , and hence $K_{i} = -\frac{f}{\alpha_{i}}$ cos ϕ . So the above requires that

$$k_s = \pm \frac{1}{a_s} \cos \phi$$
 or $\lambda_s = \pm \lambda / \cos \phi$

i.e., just as in a diffraction grating, the intensity at frequency at an elevation angle \emptyset depends only on those sources oscillating with frequency f and distributed spatially with the wavelength λ_s given above. Only then do the signals constructively interfere, as is easily seen from the geometry of Fig. 3.

While (14) provides more detailed information than (11), we would like to get the integral in terms of P_{II} , since I is more componing available than I. To this end we quote a useful result from stochasticprocess theory, which expresses R_{II} in terms of R_{II} .

$$R_{jj}(t_{i}, t_{i}) = \frac{3^{k}R_{jj}(t_{i}, t_{i})}{\delta t_{i} \delta t_{i}}$$

where here t_{i} and t_{j} are both absolute values of time. In our notation,

$$t=\frac{t_{\star}+t_{\star}}{2} \qquad \gamma=t_{\star}-t_{\star}$$

and the chain rule for differentiation easily transforms the above to

$$R_{jj}(t, r) = \frac{1}{\tau} \frac{\partial^2 R_{jl}}{\partial t^2} - \frac{\partial^2 R_{jl}}{\partial r^2}$$

which we use in

$$P_{jj} = \iint_{R_{jj}} R_{jj} e^{-i\lambda\pi(fr+\vec{k}\cdot\vec{\epsilon})} dr d^{*}\epsilon$$

$$= \iint_{R_{jj}} \{\psi_{ij}^{*} = \frac{j^{*}}{j\tau}\} R_{jj} e^{-i\lambda\pi(fr+\vec{k}\cdot\vec{\epsilon})} dr d^{*}\epsilon$$

In the first term, $\frac{3^4}{3E_1}$ may be brought outside the integrals, and the second term may be integrated by parts twice to yield

(16)

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(15)

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$$P_{jj} = \left\{ \frac{1}{4}, \frac{2^{1}}{2t}, + (a\pi f)^{1} \right\} P_{jj}$$

so that (14) becomes

$$S(\vec{x}, t_i f) = G\left(\frac{1}{7} \frac{2^{k}}{2t} + 4\pi^{k} f^{k}\right) \times \int_{-\infty}^{\infty} P_{II}\left(\vec{\eta}, -\frac{f}{a_{*}}\hat{n}_{*}, t - \frac{1}{12}\frac{1}{7}\frac{1}{a_{*}}, f\right) d^{k}\eta$$

(18)

(17)

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If the integrand was only weakly non-stationary, the $\frac{1}{2}$ term could be negligible in comparison with the $\int_{-\infty}^{\infty}$ term in a particular application. In any case, in most acoustical applications and measurements, the physical quantity of interest is the time-averaged power spectral density ⁽¹²⁾:

$$\langle S(\vec{x},f) \rangle = \lim_{T \to \infty} \frac{1}{T} \int_{-\pi/2}^{\pi/2} S(\vec{x},t,f) dt$$

Under such an averaging process, the first term in (18) contributes nothing, as

$$\left\langle \frac{3^{1}P}{3t^{4}} \right\rangle = \lim_{T \to \infty} \frac{1}{T} \int_{-\frac{1}{2}t^{4}}^{\frac{1}{2}P} dt$$

$$\left\langle \frac{3^{1}P}{3t^{4}} \right\rangle = \lim_{T \to \infty} \frac{1}{T} \frac{3P}{3t^{4}} = 0$$

provided only that $\frac{\partial P_{ii}}{\partial t}$ is finite at $\pm \infty$. Thus the acoustic analysis reduces to its final form in terms of

time-averaged quantities:

$$\mathcal{I} = \langle \mathcal{J}(\vec{x}) \rangle = \int_{-\infty}^{\infty} \langle S(\vec{x}, F) \rangle df \qquad (19)$$

where

$$\langle S(\hat{x},f) \rangle = \frac{d \hat{x} + \hat{x} + \hat{y} + \hat$$

- (20)

Equation (20) is thy main result of this section. It assumes only that the disturbance region is planar and that

Either broad-band or discrete-frequency spectra can be handled, and no simplification for the case of rotors has yet been made. Since the manipulativas involved are concerned primarily with the arguments of the disturbance functions, rather than their physical significance, results analogous to (20) for acoustic monopoles and quadrupples are easily derived.

We note that the calculations in (20) are all performed in spacefixed coordinates; this can be a big advantage in calculating noise fromrotors in turbulence, since it is in such a coordinate frame that turbulent velocity correlations and spectra are most easily specified. Host investigations have assumed that the spectrum of lift fluctuations as seen by the moving blade is known, which is usually true only if such measurements have been made.

Section IV will give a brief introduction as to how

$$\langle P_{II}(\overline{\eta}, -\frac{f}{4}, A, f) \rangle$$
 can be determined theoretically.
The next section gives a few elementary examples in which P_{II}
is prescribed a priori, to desynstrate the application of (20).

III. Emeples of Acoustic Analysis

In this section three examples of the application of (20) to lifting rotors are given. The first two involve discrete spectra; the last is broad-band. They all involve a point dipole rotating in a circle and experiencing fluctuations of the forms

Case A: cos X (cf. Outin⁽⁾, Lowson and Ollerhead⁽³⁾, Wright^(f)) Oase B: may gX, new

Case C: "white noise" (cf. Pforcs Williams and Hawkings ⁽⁶⁾) • In Case C, the result has been extended to any planar motion,

<u>Case A:</u> Consider B point lift forces rotating at angular frequency Ω about the origin, with their magnitude varying as $C = V \otimes V \otimes V \otimes V$ being a positive integer or zero (see Fig. 1). By inspection,

$$J(R, 0, t) = L_{s} \cos Y \Theta \, \delta(\bar{R} - R_{s}) \sum_{f=0}^{\frac{R}{2}} \frac{\delta(R_{s} \Theta - \frac{2\pi R_{s}^{-1}}{B} - 2\pi R_{s} n t)}{f \Theta}$$

$$= \frac{L_{s}}{R_{s}} \cos Y \Theta \, \delta(R - \bar{R}_{s}) \sum_{f=0}^{\frac{R}{2}} \delta(\Theta - \frac{2\pi f}{B} - 2\pi n t)$$

(21)

where we have used

$$\int f(x) - \delta \left\{ a \left(x - x_{s} \right) \right\} dx = \int \frac{f(x)}{a} \delta \left(x - x_{s} \right) dx$$

Even though this is a deterministic problem, it is still-valid to speak in terms of correlations and spectra, if one keeps in mind that $\overbrace{i}^{n} = ($) and hence all realizations by definition coincide with the mean value, ife form-

$$R_{II} = \frac{L_{A}^{2}}{R_{A}^{2}} \delta(R-R_{a}) \delta(\epsilon_{R}) \cos Y (\theta - \epsilon_{A/2}) \cos Y (\theta + \epsilon_{A/2}) \times$$

$$\sum_{A=0}^{0} \sum_{m=0}^{1} \delta(\theta - \epsilon_{A/2} - \frac{2\pi I}{R} - 2\pi I (t - \pi/2)) \delta(\theta + \epsilon_{A/2} - \frac{2\pi I I}{R} - 2\pi I (t + \pi/2))$$

$$=\frac{L_{k}^{k}}{R_{0}^{k}}\delta\left(R-R_{0}\right)\delta\left(\epsilon_{k}\right)\frac{1}{2}\left(\cos^{2}\lambda\epsilon_{0}+\cos^{2}\lambda\gamma_{0}\right)\int_{A=0}^{\Phi_{1}}\delta\left(0-\frac{2\pi L}{\Phi}-2\pi L\right)$$

$$\int_{A=0}^{\Phi_{1}}\delta\left(\epsilon_{0}-\frac{4\pi L}{\Phi}-2\pi L\gamma\right)$$

$$\cdot$$

$$(22)$$

We can perform the time average ismediately. Since dependence on \hat{L} is periodic with a fundamental frequency of $\hat{B}_{12}^{(n)}$, we average over the interval O to \hat{B}_{212} , which picks up one "pulse" from the sum over \hat{L} . The result is

$$\langle R_{JJ} \rangle = \frac{BL_{a}^{b}}{4\pi R_{a}^{b}} \left[\cos \vartheta \epsilon_{a} + \cos \hat{\chi} \vartheta \right] \delta(R-R_{a}) \delta(\hat{\epsilon}_{R}) \times \\ \sum_{m=0}^{b-1} \delta(\epsilon_{a} - \frac{2\pi m}{B} - 2\pi m T)$$
(23)

Prom (20),

$$\langle S \rangle = 4\pi^{2}f^{2}G \int_{R}^{\infty} R dR \int_{d\Theta}^{d\pi} \int_{dT}^{\pi} e^{-i\lambda\pi fr} \times \int_{R} d\epsilon_{0} \int_{0}^{\pi} d\epsilon_{R} e^{+i\lambda\pi \frac{f}{q_{0}}\hat{n}_{0} \cdot \vec{\epsilon}} \langle R_{M} \rangle$$
(24)

The integrations over \mathcal{K} and $\mathcal{E}_{\mathcal{K}}$ are easily performed due to the presence of the δ functions. Taking use of the geometry in Figs. 1 and 4 and 6 little manipulation in the exponent gives

$$\langle 5 \rangle = \frac{\beta L^{\lambda}}{4\pi} (4\pi^{\lambda} f^{\lambda}) G \int_{0}^{0} d\tau e^{-i2\pi f\tau} \int_{0}^{2\pi} d\theta \int dt_{\theta} (\cos \theta t_{\theta}) dt_{\theta} dt_{\theta} (\cos \theta t_{\theta}) dt_{\theta} dt_{\theta}$$

$$\langle S \rangle \equiv \frac{BL^{3}}{\sqrt{\pi}} (\sqrt{\pi^{2}} f^{3}) G \int_{-\infty}^{\frac{\pi}{2}} e^{-i\lambda\pi^{\frac{2}{7}}T} \int_{0}^{2\pi} \int_{0}^{2\pi} \int_{0}^{2\pi} \left\{ \cos \left(\frac{2\pi\pi}{B} + 2\pi\Omega T\right) + \cos \left($$

Integration over Θ of the first term yields a zeroth-order Bessel function; the change of variable $\chi = \Theta - \beta + \pi/2$ is useful in the second term, which gives, after some manipulation, another Bessel function:



Fig. 4. Polar coordinates for rotating point forces.

$$\langle S \rangle = \frac{gL_{0}^{2}(4\pi^{4}f^{4})G}{2} \int d\tau e^{-i2\pi f\tau} \times \frac{gL_{0}^{2}(4\pi^{4}f^{4})G}{2} \int d\tau e^{-i2\pi f\tau} \times \frac{gL_{0}^{2}(4\pi^{4}f^{4})G}{2} \int \frac{gL_{0}^{2}(4\pi^{4}f^{$$

The argument of the Bessel functions is

 $4\pi R_0 \frac{f}{d_0}$ in ϕ ain $(\pi R_0 T^* + \pi m/B)$: The factor-in curly brackets is periodic; hence we expect a discrete spectrum, i.e., δ - functions. To this end, after such algebra, we can manipulate both terms into integrals of the form

$$\int_{-\infty}^{\infty} J_{au}(zz, int) e^{iz,\mu t} dt = \pi \left\{ J_{u}^{A}(z), \delta(\mu) + \sum_{k=0}^{\infty} (-1)^{k} J_{u-k}(z) J_{u+k}(z) \left[\delta(\mu+k) + \delta(\mu-k) \right] \right\}$$

Also needed are

(28)

$$J_{\mu}(z) = (-1)^{\mu} J_{\mu}(z)$$
(2)
(7)

$$\sum_{m=0}^{d-1} e^{i 2\pi m \mu} = \begin{cases} \beta & \text{if } \mu = 0, \pm 1, \pm 2, \dots, \\ 0 & \text{otherwise} \end{cases}$$
(30)

The final result is

$$\langle S(\bar{x},f) \rangle = \frac{B^2 L_{n,\alpha}^2 \omega^2 \phi}{\tilde{s} f_0 a_0^2 A^2} \sum_{n=1}^{\infty} f^2 \left(J_{nB-Y}^2 + J_{nB+Y}^2 + 2(-1)^{\gamma} \omega^2 a^{\gamma} A^{\gamma} - J_{nB+Y}^2 - f^2 \left(J_{nB-Y}^2 + J_{nB+Y}^2 - f^2 \right) \right)$$

$$+ 2(-1)^{\gamma} \omega^2 a^{\gamma} \beta J_{nB-Y} J_{nB+Y} - f^2 \left(f_{nB-R} - f^2 \right)$$

$$(31)$$

The argument of all the Bersel functions is

 $2\pi R_{0} \frac{f}{a} \cos \phi = 2\pi R_{0} k \cos \phi = n\beta M \cos \phi$ The above result is in agreement with those obtained by lowson and Otherhead ^(a) and by Wright.⁽⁴⁾ The former have defined $-\theta = 0$ as the observer's azimuth; hence our results differ by the phase angle β . For Y = 0, (31) reduces to

$$\langle S(\vec{x}, \vec{t}) \rangle = \frac{B^2 L_{p,a}^2 m^2}{R_{p,a}^2 \Lambda^4} \sum_{n=1}^{\infty} \int_{n=1}^{2} J_{nB}^2 \delta(\vec{t} - nB\Omega)$$

(27)

which agrees with Gutin's analysis (') of a constant-point force-rotating in a circle.

A computer program was used to evaluate (31) for rotational mathematical members of 0.5 and 0.9, for $\chi' = 1$ and 10. The observer's position was taken as $\phi' = 30^{\circ}$ and $\phi' = 45^{\circ}$. Fecults are presented in Fig. 5a and 5b in the form of the dimensionless power, $\frac{(A_{ab})}{L_{ab}} = \frac{R_{ab}}{R_{ab}} \frac{R_{ab}$

49



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tend to peak near the lower harmonics with the peak broadening as M increases. Increasing Y -tends to shift the spectrum to the right, as one would expect due to the faster fluctuations of the dipoles. <u>Case B:</u> Any spatially fixed two-dimensional upwash pattern that is frozen in time can be represented as a Fourier superposition of waves of the form $\min_{n \in M} q {X_n \atop M_n}$ and $\max_{n \in M} q {X_n \atop M_n}$. In principle, the resultantilift response can then be modeled in the same manner. Thus, the accounting response to such a fundamental mode would be useful as a building block in situations in which a decomposition into asimuthal modes as discussed in tase A is inconvenient.

Consider: B point lift forces rotating at angular frequency Ω , about the origin, with their magnitudes varying as $A_{in} \in X_{i}$, where Q_{i} is any real number (see Fig.-6). Hence, rather than each dipole oscillating at constant frequency, as in the previous example, at any instant its variation non-depends on whether it is moving along or perpendicular to the X, direction. By inspection,

$$\int (R_1 \Theta, t) = \frac{L_0}{R_0} \min_{q \in X_1} \delta(R - R_0) \sum_{j=0}^{\Phi'} \delta(\Theta - \frac{3\pi f}{\Phi} - 3\pi \Lambda t)$$
(33)
orming R_{in} , and setting $X_1 = R_1 \cos \Theta$ yields



ł

$$R_{AB} = \frac{L_{a}}{R_{a}} \delta(R-R_{a}) \delta(\epsilon_{R}) \min\left\{qR_{a}\cos\left(\phi-\frac{\epsilon_{a}}{2}\right)\right\} \min\left\{qR_{a}\cos\left(\phi+\frac{\epsilon_{a}}{2}\right)\right\} \times$$

$$\sum_{l=0}^{\infty}\sum_{m=0}^{\infty}\delta(0-\frac{e_{m}}{2}-\frac{2\pi\pi}{8}-2\pi\pi(t-\frac{\pi}{2}))\delta(0+\frac{e_{m}}{2}-\frac{2\pi\pi}{8}-2\pi\pi(t+\frac{\pi}{2}))$$



b. Side View

Fig. 6. Potating point dipole fluctuating simusoidally in X_{ij} .

The dependence on $-\Theta$ and E_{A} can be separated using standard trigonometric-identities, and the time average yields a factor \tilde{B}'_{27} just as in Case A. Mence,

$$\langle R_{JJ} \rangle = \frac{BL_{a}^{b}}{\sqrt{\pi}R_{a}^{b}} \delta(R-R_{a}) \delta(\epsilon_{R}) \left\{ \cos\left(2qR_{a}\min\theta\min\frac{\epsilon_{R}}{2}\right) - \cos\left(2qR_{a}\cos\theta\cos\theta\cos\frac{\epsilon_{R}}{2}\right) \right\}_{m=0}^{\frac{d}{2}} \delta\left(\epsilon_{a} - \frac{2\pi\pi}{8} - 2\pi\overline{L}T\right)$$
(35)

$$\langle S(\bar{\mathbf{x}};f) \rangle = G(\Psi \pi^{2}f^{2}) \int_{R}^{\infty} R dR \int_{A}^{2\pi} d\Phi \int_{-\infty}^{\pi} d\tau e^{-i2\pi f \cdot \tau} x$$
$$\int R d\epsilon_{0} \int_{A}^{\infty} d\epsilon_{R} e^{+i2\pi \frac{f}{a_{0}}\cdot \hat{n}_{0} \cdot \hat{\epsilon}} \langle R_{JJ} \rangle$$
(36)

The transformation of $\frac{f}{a_{a}} = \hat{n}_{a} + \hat{\epsilon}$ to polar coordinates is the same as used in Case A, and so the integration over $\hat{\epsilon}_{a}$ yields

$$\langle \hat{S} \rangle = \frac{g i \hat{a} (4 \pi^{1} f^{1}) G}{4 \pi} \int_{-\infty}^{\infty} d\tau \, e^{-i 2 \pi f \tau} \int_{0}^{\lambda \pi} d\theta \sum_{m=0}^{\alpha, i} X$$

$$\left\{ \cos\left(2 q R_{\bullet} - i n \theta \sin\left(\frac{\pi m}{8} + \pi n \tau\right)\right) - \cos\left(2 q R_{\bullet} \cos \theta \cos\left(\frac{\pi m}{8} + \pi n \tau\right)\right) \right\}$$

$$e^{\pm i 4 \pi^{2}} \hat{R}_{\bullet} \frac{f}{a_{\bullet}} \cos \phi \sin\left(\beta - \theta\right) \sin\left(\pi n \tau + \frac{\pi m}{8}\right)$$

(37)

By writing the cosines as complex exponentials and several charges of variable, one can show that the integral over \oplus results in four terms; all involve J_{\bullet} , but each with a different argument. Two of these-terms can be integrated with respect to \mathcal{T} using (28). The other two can be manipulated into a form in which the following expansion by Sonine⁽³⁾ is useful:

$$J_{\bullet}^{\bullet}\left[\sqrt{A^{2}+C^{2}-2AC\cos X}\right] = J_{\bullet}^{\bullet}(A) J_{\bullet}^{\bullet}(C) + 2\sum_{J=1}^{2} J_{J}^{\bullet}(A) J_{J}^{\bullet}(C) \cos J_{X}$$
(35)

Identities (27) and (30) are also required, and the final result is

$$\left\langle \tilde{S}(\tilde{x},f) \right\rangle = \frac{B^{4}L^{4}_{A,c} \sin^{4}\phi}{Bp_{a}a^{4}_{a}A^{2}} \sum_{n=1}^{\infty} f^{2} \left\{ J^{2}_{nB}(A) + J^{4}_{nB}(C) - 2 \cos nB^{4} \psi J_{nB}(A) J_{nB}(C) \right\} \left\{ \left(f - nB \Omega \right) \right\}$$

$$(33)$$

vhere

$$A = R_{o} \left[\frac{q^{\lambda}}{a} + 4\pi q \frac{f}{a_{o}} \cos \phi \cos \beta + 4\pi^{2} \left(\frac{f}{a_{o}} \right)^{\lambda} \cos^{2} \phi \right]^{\frac{\gamma_{\lambda}}{2}}$$

$$C = R_{o} \left[\frac{q^{2}}{q^{2}} - 4\pi q \frac{f}{a_{o}} \cos \phi \cos \beta + 4\pi^{2} \left(\frac{f}{a_{o}} \right)^{\lambda} \cos^{2} \phi \right]^{\frac{\gamma_{\lambda}}{2}}$$

$$\frac{\gamma}{2} = t_{om}^{-1} - \frac{4\pi^{2} q}{q^{2} - 4\pi^{2} \left(\frac{f}{a_{o}} \right)^{2} \cos^{2} \phi}$$

Their poise to $c \rightarrow q X$, is the above with a (+) sign preceding the last-term. It is easily seen that this reduces to Gutin's result for

last term. It is easily seen that this reduces to usual structure in q = 0. For a $\begin{cases} \sin \beta \\ \cos \beta \end{cases} q X_{A}$ variation, the response is that for $\begin{cases} \sin \beta \\ \cos \beta \end{cases} q X_{i}$ but with $\sin \beta$ replaced by $\cos \beta$ and vice versa.

The asymptotic behavior of (39' as $q \rightarrow 0$ is

$$\left\langle S(\mathfrak{K},\mathfrak{f})\right\rangle \sim \frac{(\mathfrak{q}_{\mathcal{K}})^3 B^3 L^3_{n \dim 1^3} d\sigma}{8 \, \rho_* \, a_{\sigma}^{3-n} L^2} \sum_{n \cong 1}^{\infty} \, \mathfrak{f}^3 \left\{ J_{n \oplus 1}^3 + J_{n \oplus 1}^{\lambda} \right\} \\ - 2 \, \cos 2 \left\{ \beta \, J_{n \oplus -1} \, J_{n \oplus +1}^* \right\} \, \left\{ \left(f - n B \, \Omega \right) \right\}$$

where the argument of the Persel-Functions is $2\pi R_{0} + \frac{f}{a_{0}} \cos \phi$.

(40)

and the second

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Since

$$in q^{X_1} = nin (qR_1 \cos \theta);$$
$$= 2 \sum_{\substack{i=1\\ Y \equiv i}}^{i} (-1)^{\frac{Y \equiv i}{2}} J_{y'}(qR_1) \cos \theta$$

~ qR. coe 0 + 0 (qR.)3

۷e

the above should agree with a calculation using (31) with $\gamma = 1$ and multiplied by the factor $(qR_s)^4$. This is easily seen to be the case,

The computer was again used to evaluate (39) for M = 0.5 and 0.9 and values of $(qR_o) = 10^{-3}$, 1, and 10 for ϕ = 30° and

 $\beta = 45^{\circ}$. Results are plotted in Figs. 7a and 7b. Again, raising M broadens the spectrum while increasing $-(qR_{\bullet})$ shifts it to the right. For all practical purposes, the curves for Y = 1 of Case A and

 $qR_{\bullet} = 1$ of Case B essentially collicide; however, the difference between the X = 10 curve and that: for $qR_{\bullet} = 10$ is significant, and here the Mach number plays a strong role. Most likely, directionality is also important. The case $-qR_{\bullet} = 10^{-3}$ was run to verify numerically that the asymptotic behavior of (39) as $qR_{\bullet} \longrightarrow 0$ agreed with (31) for X = 1, as discussed above. Accounting for the factor $(qR_{\bullet})^{3} = 10^{-6}$, they essentially lie atop one another at M = 0.5, at M = 0.9 the difference is discernible, though still negligible. Figs. 5 and 7 display nearly constant slopes for all the curves at the higher harmonics, evidently independent of X or qR_{\bullet} . Apparently

M does have a strong effect on this exponential decay rate. Unfortunately, results for very large values of X or qR, are unavailable at this writing due to numerical difficulties with the Bessel functions.

Case C: Consider point forces rotating at angular speed Ω about the origin, but with their magnitudes varying randoaly in such a way that no correlation exists from one instant to the next, or equivalently from one point to another. This is commonly referred to as white noise, and results in a flat load spectrum independent of frequency. The correlation function for such a system is easily seen to be

$$R_{JJ} = \frac{\overline{L^{3}}}{R_{\bullet}^{1}} \delta(R-R_{\bullet}) \delta(\epsilon_{R}) \delta(\underline{\epsilon}_{\bullet}) \overline{\delta(r)} \sum_{m=0}^{\delta-1} \delta(\theta - \frac{2\pi m}{\delta} - 2\pi n t)$$
(41)

where $\overline{L^{4}}$ is the mean-square_lift-exerted by one of the dipoles. Even though we know that the accustic spectrum will be broad-band and hence have no "fundamental" frequency, the non-stationarity in time exhibited by (%1) is still periodic. Hence a time average over the interval O to Van is still meaningful and results in a factor $\frac{2}{4\pi}$. Prom (20)

$$\langle S \rangle = G (4\pi^{4}f^{4}) \int_{0}^{\infty} R dR \int_{0}^{2\pi} d\Phi \int_{0}^{\infty} d\tau e^{-i2\pi f\tau} \int R dE_{0}$$

$$\int_{0}^{\infty} dE_{R} e^{+i2\pi \frac{f}{40}\hat{n}_{0} \cdot \vec{e}} \frac{B\overline{L^{3}}}{2\pi} \cdot \vec{S} (R-R_{0}) \vec{S} (E_{R}) \vec{S} (E_{0}) \vec{S} (\tau) \qquad (47)$$



(43)

$$\langle S(\vec{x},f) \rangle = 4\pi^2 f^2 B \overline{L^4} G = \frac{B \overline{L^4} dim^2 \phi}{4f_0^4 \sigma_0^4 A^2}$$

which is independent of the dipoles' motion. This result was noted for the case 8 = / by Fronce Williams and Hawkings (6) . Note that we only gain a factor of B in power as contrasted to B² in Cases A and B. This is "ecause successive dipoles no longer reinforce each other's signals, as their phases are random; hence the intensities add rather than the pressure amplitudes.

The case with which this result was arrived at due to the delta functions in $\mathcal T$ and $\vec{\mathcal E}$ suggests that it may hold for any planar motion, not circular or even periodic. A single point force whose path is prescribed as $\tilde{y}_{\tilde{e}}(t)$ and which fluctuates in the above manner is described by

$$R_{M}(\hat{\gamma}, \vec{\epsilon}, t, \gamma) \stackrel{=}{=} L^{\lambda} \delta(\vec{\gamma} - \vec{\gamma}_{0}(t)) \delta(\vec{\epsilon}) \delta(\tau)$$

$$(44)$$

$$S(\vec{x}, t, f) = \tilde{G}(\frac{-1}{4} \frac{2^{\lambda}}{2t^{\lambda}} + \sqrt{\pi^{\lambda}} f^{\lambda}) \int_{-\infty}^{\infty} d^{\lambda} \eta \int_{-\infty}^{\infty} d^{\lambda} \tau^{-i\lambda\pi} f^{\tau} x$$

$$\int_{-\infty}^{\infty} d^{\lambda} \epsilon e^{\frac{1}{2}i\lambda\pi} \frac{f}{q} \hat{n}_{0} \cdot \vec{\epsilon} \frac{1}{L^{\lambda}} \delta(\vec{\gamma} - \vec{\gamma}_{0}(t)) \delta(\vec{\epsilon}) \delta(\tau)$$

$$= \overline{L^{2}} G \left(\frac{1}{7} \frac{2^{1}}{2t} + 4\pi^{2} f^{2} \right) \int_{-\infty}^{\infty} \delta \left(\frac{1}{7} - \frac{1}{7} (t) \right) d^{2} \eta$$

$$= 4\pi^{2} f^{2} \overline{L^{2}} - G = \frac{\overline{L^{2}} \sin^{2} \phi f^{2}}{4\rho_{0} G_{0}^{2} \pi^{2}}$$
(45)

Hence, as long as the dipole remains in a plane, its accustic radiation is the same as if it were innobile. The result for 8 dipoles is **B** times the above, by linear superposition, even-if each executes a different motion. This is because the assumption that trajectories are geometrically compact precludes amplitude variations in the spectrum, and the Doppler shifts are indiscernible in a flat spectrum.

IV. Lift Response of Potor to Turbulent Unach Pattern

As mentioned above, our acoustic analysis requires the space-time lord spectrum, P_{II} , expressed in fixed coordinates as seen by the observer. To obtain this quantity, we begin with the following approximations:

- i) linearized aerodynamic theory is applicable hence, we can superroce solutions.
- 2) the turbulence is homogeneous in space.

The need for 1) is obvious; .) is not absolutely necessary, but it considerably simplifies the analysis.

The variations-in w (J, t; j) give rise to fluctuations in the angle of attack $\alpha = \omega r/v$, U being the local mean horizontal velocity, which varies linearly with distance from the hub. He presume that we have $\mathcal{J}_{\mathcal{J}}(\mathcal{J}, t, \mathcal{I})$, the lift loading at a

fixed point $\overline{\mathcal{T}}$ at time t due to a simusoidal upwash distribution of wave-vector y . This function, generally complex, is referred to as the aerodynamic transfer function. Then the response at $\overline{\mathcal{A}}$ at time $\overline{\mathcal{T}}$ to a turbulent openach pattern is, by linear superposition

$$\mathcal{L}(\vec{g},t;j) = \int \mathcal{L}_{\sigma}(\vec{g},t,\vec{v}) F_{\sigma}(\vec{v};j) d^{3} d^{$$

$$F_{j,j}(\vec{x};j) = \int_{-\infty}^{\infty} (\vec{x};j) e^{-i\lambda\pi \vec{y}\cdot\vec{y}} d^{3}\vec{y} \qquad (47)$$

where where and $F_{\mu \mu}$ are taken as generalized random functions. Now we form the correlation of the lift loading.

$$R_{JI}(\vec{\gamma}, t_{1}, \vec{z}_{1}, t_{n}) \equiv R_{JI}(\vec{\gamma}, \vec{\varepsilon}, t, \tau)$$

$$= \iint_{\mathbf{z}} J_{j}(\vec{\gamma}, \vec{\varepsilon}_{n}, t, \tau) J_{j}^{\mathbf{z}}(\vec{\eta}, \vec{z}_{n}, t, \tau) \overline{f_{j}}(\vec{\tau}) \overline{f_{j}}(\vec{\tau}) d^{2} d^{2} d^{2} J_{j}$$

(48)-

Homogeneous turbulence has the property that oscillations of any given wavelength must-be uncorrelated with those of any other: i.e.,

$$(\overline{x}) \sim \overline{F}_{ac}(\overline{x}) \cong -\overline{P}_{ac}(\overline{x}) \sim \overline{F}_{ac}(\overline{x})$$

(49)

Parar being the power spectral density of the turbulence. Ferforing the integration over \mathbf{J}^{*} gives

$$R_{JI}(\vec{\tau},\vec{\epsilon},t,\tau) = \int_{-\infty}^{\infty} \int_{0}^{\infty} (\vec{\tau}-\vec{t}_{2},t\cdot\vec{\tau}_{2},\vec{\tau}) \int_{0}^{\pi} (\vec{\tau}-\vec{t}_{2},t\cdot\vec{\tau}_{2},\vec{\tau}) \times \int_{0}^{\infty} (\vec{\tau}) d^{2}v$$
(50)

Consequently,

$$P_{II}(q, -\frac{1}{4}, \hat{\pi}_{a}, t, f) = \int_{0}^{\infty} d^{4}\epsilon \ e^{+i2\pi \frac{f}{4}} \hat{\pi}_{a} \hat{\pi}_{a} \hat{\epsilon} \int_{0}^{\infty} d^{4}r \ e^{-i2\pi f \tau} \times \int_{0}^{\infty} d^{4}y \ \hat{J}_{y}(\bar{q}, \bar{\tau}_{A}, t + \bar{\tau}_{A}, \bar{v}) \ \hat{J}_{y}^{n}(\bar{q}, \bar{\tau}_{A}, t + \bar{\tau}_{A}, \bar{v}) \ P_{max}(\bar{y})$$
(51)

Unfortunately, (51) in conjunction with (20) implies a total of eight scalar integrations, well beyond the capability of even the fastest ecoputers. It is hoped that some may be deme-analytically; but even with the Proper, by is usually complicated enough simplest forme for to prohibit this.

One simplification would be to neglectiretarded-time differences across turbulent eddies: i.e., to assume that they are much smaller than the acoustic wavelength. Mofortunately, integral-scales in the atmosphere typically run-to-several feet, so such an approximation breaks down at high frequencies. A more reasonable approach is to consider the chord as acoustically COMPACE: L

$$c \propto \frac{V}{ca}c = M < < 1$$

where we have taken U/c as typical of the highest frequency. Hence this effectively-limits the results to incompressible flow. Another approach

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would be to model the chordwise loading as rectangular. However, this and the provious assumption both imply that alist , as seen by a fixed point in the disk, is zero except at the discontinuities. The form of (13) suggests that this would tend to oversuphasize the higher frequency components; indeed, this may explain why Gutin's calculation overestimates the higher harmonics as the transonic regime is approached.

We plan to apply the present analysis to a point dipole rotating at constant angular velocity in a homogeneous and isotropic turbulent field, with an ad hoc application of quasi-steady aerodynamics or the Sears function to obtain I_J . We then plan to consider the effects of finite chord and sporluding the different orientations of the spatial Fourier components of turbulence relative to the blades.

V. Survey and Conclusions

in acoustic analysis of a surface distribution of dipoles has been made with a minimum of assumptions; both discrete and broad-band spectra can be accommodated, and extension to acoustic monopoles and quadrupoles is straight-forward. The formulation has been applied here to several examples and shown to agree with previous approaches where applicable.

In particular, it is expected to be of value in treating the problem of a lifting rotor in atmospheric turbulence, as it assumes knowledge of the space-time loading spectrum in fixed coordinates, P_{II} . This is a frame in which the turbulence characteristics are nost easily specified. However, a number of integrations are involved in the determination of P_{II} , and further approximations will probably be required before practical results will be obtained.

VI. - Monenclature

- R position vector of observer
- 7, Z position vectors of disturbances within the rotor
 - average position vector of disturbances
 - ĩ relative displacement vector between disturbances
 - λ. = 111
 - A. unit vector along X
- R. o polar coordinates in plane
 - azimuth angle of observer
 - angular elevation of observer
 - t time
 - nean retarded time t
 - separation in time r
 - P pressure
 - ۴ density
 - a speed of sound
 - J. angular rotation frequency, Hz;
 - С blade chord
 - f acoustic frequency, Hz.
 - acoustic wavelength, a./f 2
- -K acoustic_wave vestor, n./2
- $y_{1} = q$ wave number of lift fluctuations
- upwash_component of turbulence
- turbulence wave vector
- J instantaneous acoustic intensity
- I thre averaged acoustic intensity

- S acoustic spectrum
- R correlation function
- P___ power spectral density
- M Mach number
- 1 lift loading (force/area)
- lift force
- -monthle parameter
- 5-1 i
- G geometrical factor, defined in Eq. (9)
- 2 delts function
- R blade number

- () deviation from ()
- [] to be evaluated at retarded time
- I absolute value
- () ensemble averaged quantity
- < > -time averaged quantity
- ()[#] -complex conjugate

VII. Maferences

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- n harmonic number
- () undisturbed value

SOME ASPECTS OF MELICOPTER MOISE THEORY Fart II Recent Results Relating to Engine Noise* by M. R.-Sears Cornell University

The second s

Abstract

An investigation of blade forces arising from rotor-stator interactions in subsonic flow is reports:. One conclusion is that the Komp-Sears type of approximation can be extended to include compressibility effects by means of the technique suggested recently by Aviet and Sears.

In the course of this investigation, some apparent discrepancies in the results of Johnson on gust loads in subsonic two-dimensional flow were encountered. These are reported here, without explanation, especially in view of the importance of Johnson's three-dimensional results in helicopternoise research.

T. Aerodynamic Interference between Hoving Blade Rova

Under contract with the Mechanics Branch of AFOGR we have continued our studies, begun in the 1950's, of unsteady effects in axial-flow familiand compressors. Although there exist, in principle, methods for solution of these problems, within the two-dimensional and small-perturbation approximations but without further simplifications, the practical situation is that these are generally not in forms suitable for practical situation the therefore, still of interest to investigate possibilities of extending the Kemp-Sears type of approximations to subsonic compressible flows. Mr. C. Osborne has carried out such an investigation.

The Kemp-Searc-theory⁷ treats inter-row interference as a perturbation of steady flow through a stage consisting of an upstream stationary row of blades and a downstream moving row - stator and rotor, say. It is clear, first of all, how to account for compressibility in the steady flow fields attached to the respective rows; namely, by the Prandtl-Glauert rule. A possible approximation (\emptyset 1) is to make only this correction for compressibility and to use, as Kemp and Sears did, incompressible unsteadyairfoil results to estimate the unsteady forces that result from the motion of the up- or downstream blades through this periodic flow field. Proposal \emptyset 2 might be to invoke Prindtl-Glauert theory again, in a straightforward quasisteady fashion, to estimate the unsteady forces; i.e., to transform the flow field encountered by the moving blade by Prandtl-Glauert stretching with respect to its relative flow direction, before employing incompressible unsteady-airfoil results, and an forth,

But in a recent paper². Anlet and Sears pointed out that a consistent first-order theory for unsteady flow, analogous to the Frandtl-Glauert, involves an additional effect: there is the Frandtl-Glauert stretching, but there is also a first-order <u>distortion</u> of any time-varying boundary condition. (Fir want of a better mane, I suggest calling this the "GASP" approximation, although unfortunately this acronym puts Frandtl last(). This yields a related incompressible unsteady flow if terms of order 4^d are neglected compared to 1 and terms of order 6 are retained, where 6 denotes the ratio of body length 4 to wave length of sound:

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where f is the frequency and a the speed of sound. Thus f is also equal to $1/2\pi$ times the product of the such number and the conventional "reduced frequency" of unstaady-airfoil theory based on the half-chord.

It is only when terms of order & are also neglected that the approximation of #2 above - "straightforward quasi-steady Prandtl-Glauert" is obtained. Thus, our third proposition (#3, say) is to proceed, once again, as in #1-and #2, but to transform the flow field (which is unsteady in the frame of reference involved here) as per the GASP approximation.

Of course, one would employ, instead, <u>compressible-flow</u> insteadyairfoil results to estimate fluctuating forces if such were available. To a limited extent they are available: some years ago Drischler et al.³ of HACA obtained the gust-response functions for three Mach numbers, by a series of ingenious numerical approximations.⁴ Two parts of the inter-row interaction are gust-like, viz. viscous-wake and vortex-wake interference, i.e., the passage of downstream blades through these two kinds of values. (Incidentally, viscous-wake interference is said to be the most important part of inter-row interaction in present-day engines.) Consequently we have calculated these two phenomena by use of Drigchler's results, especially for comparison with approximations $\#1_1, \#2_2$ and $\#3_3$, above; we call this $\#4_2$.

Our numerical results are admittedly limited. They all pertain to the 45°-45° stage treated by Kemp and Sears, with varying Much number, gap/chord, and axial row-spacing. Two different assumptions were made regarding the unperturbed rotor-blade-loading distribution. Hore cases could easily be calculated, since the results appear in closed-form formulas for direct-evaluation for all four approximations. The conclusions are simple: Taking #4 as our standard of comparison,

1. Approximation \mathcal{J} 1 (incompressible unsteady-mirfoil theory) shows the right trends with lach number, but seems to underestimate the effects of compressibility.

 Approximation \$2 (quasi-steady grandtl-glauert) is completely without merit, predicting_compressibility_effects that even have the wrongtrends with varying then number.

3. Approximation β 3 ("GASP") is relatively satisfactory, even up to $\mathcal{M}\simeq$ 0.7, and even for relatively large 6.

4. The principal effect of compressibility, in general, is to reduce the magnitude of inter-row interaction (lift fluctuations). This is recognized as a general phenomenon in unsteady-airfoil flows, and can be explained easily in the framework of the GAUP transformation. It also becomes clear, in this framework, why the predictions of our 62 are so wrong.

Having thus succinctly stated our conclusions, we shall not present any of Qaborne's graphs here. They appear in his thesis ⁶, which we propose to abstract in the form of one or more published papers as soon as possible. <u>II. The Response of Thin Airfoliz to Sinusoidal Guets at Subsonic Flow Sprove</u>

Calculations of the pressures and forces on eirfoils of infinite span is convected sinusoital gust fields have been carried out, for compressible flow, in references 4 and 5.

foth investigations involve solving integral equations for the singularity distributions in the presence of vortex wakes. Johnson⁴ transforms to a coordinate system in which the flow becomes steady (three-dimensional) - an ingenious device which, of course, cannot be used to produce the two-dimensional case. Nevertheless, both withors do present

(1)

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data for the two-dimensional case; Johnson's are in the form of exponential formulas obtained from his numerical solutions by curve-fitting, while Graham's are presented (to date) only in a single vector diagram whose scale is not adequate to provide accurate values for computations. It is, therefore, impossible to make meaningful comparisons of Johnson's and Graham's results at this meeting.

On the other hand, it is possible to compare Johnson's values (a) with the corresponding incompressible-flow function 7 , (b) with the results of applying the GASP transformation to this function, and (c) with frischler's approximate results 3 . These comparisons are presented in Figs. 1-3, where the absolute value of the ratio of lift to quasi-steady lift is plotted against reducti frequency ω -and Mach number of flight M. It should be recalled that the validity of the GASP approximation is limited by M and the frequency parameter \in j=viz.,

B* = 1-M2 ≪1

and
$$e^{e} = \left(\frac{M\omega}{2\pi}\right)^{e} <<1$$

The curves of Figs. 1-3 therefore leave us with some concern for the accuracy of Johnson's results for the two-dimensional case. It is hard to believe that the effect of compressibility is gollarge at very small M^1 . As indicated, the value of G^2 for M = 0.3 and $\omega = 4$ is only .04, so that we effect the accuracy of the GAST approximation to be very good.

We have, therefore, foregoine the application of Johnson's results. That is more important, especially to those interested in broad-band noise prediction, is whether Johnson's yesults for other angles of inclination of the situsoidal gists to the wing are dependable. Pending the publication of detailed results by Graham, or the equivalent, sit seems impossible to answer this important question.

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Figure 1. Batio of lift magnitude to quasi-steady lift as function of reduced frequency, for sinusoidal guist at various tach manters of flight, according to "GASP" approximation $\frac{2}{3}$. Cross-plotted curves show values of $C = M \omega / 2\pi$. (From Reference 6)

ibre recently, papers by Graham and Johnson have appeared, which also include the compressible-flow gust-response function in principle. Our reasons for using irischler's approximation instead of these will be "Mentioned below.



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Figure 2. Intio of lift magnitude to quasi-steady "ift as function of reduced frequency, for sinusoidal gust at various lach numbers of flight, according to Johnson $\frac{4}{3}$. (From Performe 6)



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Figure 3. Ratio of lift magnitude to quasi-steady lift, for sinusoidal guists, according to "GASP" 3 , Johnson 4 , and Weischler et al. 3 , as functions of Each number M for two values of reduced frequency <3. (From Reference 6)

DETERMINATION OF THE ARRODYNAMIC CHARACTERISTICS OF VORTEX SHEDDING FROM LIFTING AIRPOILS FOR APPLICATION TO THE ANALYSIS OF HELICOPTER NOISE*

By

S. G. Sadler ROCHESTER APPLIED SCIENCE ASSOCIATES, INC. 140 Allens Creek Road Rochester, New York

ABSTRACT

The purpose of this project is to determine whether or not vortex-shedding noise from helicopter rotors exists, and if it exists, to determine the associated aerodynamic characteristics. The first year's effort was directed toward an evaluation of the feasibility of an experiment-to attempt to measure vortex shedding noise on an airfuil. It was notermined that the state-of-the-art experimental techniques and equipment would be adequate to measure vortex shedding if it had cortain-assumed fraquency characteristics and if some specific model, instrumentation, and wind-tunnel requirements were met. The second year's effort was directed toward_coordinating design of the airfoil model and instrumentation and conducting experiments on two-dimensional and three-dimensional airfoil models. Surface pressure measurements on the airfoil, hot-wire measurements in the wake, sound measurements, and accelerometer measurements were made. Those measurements indicate that vortex shedding at a discrete frequency exists but that its frequency may be higher than has been used in helicopter-hoise prediction techniques. Details of this and other noise characteristics as observed from the experimental data will be presented and discussed. A brief discussion of the upcoming year's effort will be presented.

Introduction

Helicopter rotors are an important helicopter_noise source. Reductions in helicopter rotor noise are desirable from various considerations, including detection, annoyance, and hearin, damage. An improved understanding of the mechanisms involved in holicopter noise generation-are important in the obtainment of reduced helicopter=rotor noise. Vortex shedding noise-has heen suggested as one source of high frequency=noise, and under some-flight conditions it has been suggested as a source of high-amplitude=high frequency noise.

The primary_purpose of this work is to establish whether or not yorkex street-shedding from heliconter rotors is a significant noise source. The bulk of studies of vortex shedding-have involved blunt bodies. Considerable work in the great of vortex shedding from airfoits has been done-recently, and is presently-being conducted. Of particular interest is work done at UARL by Patterson,

This study is supported by the Department of the Army, U.S. Army mesearch Office-Eurham, Durham, North Carolina, under Contract DANC04-69-C-0090. et al.¹ Hanson² has done extensive experimental work on notched and bluff airfoils. An extensive survey of literature concerned with the singing propeller problem (primarily for hydrodynamic "application) by Ross³ contains interesting papers which are pertinent to the current work on-airfoils.

The first year's efforts were directed toward determining, insofar as was available from existing literature and simple theory, important vortex shedding characteristics, orders of magnitude of frequencies and amplitudes which might be expected, and important aerodynamic parameters and their effects on vortax shedding characteristics. The feasibility of an experimental investigation to attempt to determine vortex shedding characteristics of an airfoil was evaluated. It was determined that such an experiment was feasible, subject to certain restrictions and requirements on experimental facilities and instrumentation. The second year's effort was to perform the experiment and to analyze the experimental data. The third year's effort is to be directed toward the use of the experimental results in modeling helicopter noise.

The effort has been completed through the obtainment of experimental data. Data analysis has not been completed, so the results presented here are of a preliminary nature. The experimental effort was delayed approximately nine months from the schedule originally planned, and completion of the data analysis had been delayed accordingly. The delay in the experimental phase of the effort was due to problems associated with experimental facility construction, instrumentation, and shakedown.

Summary of Expected Vortex Characteristics and Test Feasibility Studies

Expected vortex shedding characteristics which were determined early in the investigation included the following:

 The-oscillatory lift force, L(t), duc-to-vortex shedding at frequency, w,=from an airfoil with chord, c, length, t, and lift curve slope, a,, in a-fluid with density, s, and relative velocity. V, with angle of-attack magnitude duc-to vortex shedding of a_v, is given by

 $L(L) = (\frac{1}{2} + V^2 + C + a_*) + a_{\mu} + e^{i\mu L}$

 Similarly, the first harmonic drag (orce, D(t), -ix-given by

$$E(t) = \left(\frac{1}{2} - e^{-\frac{1}{2}t} + \frac{1}{2} - e^{-\frac{1}{2}t} + \frac{1}{2} + \frac{1$$

where no is the steady airfoil angle of attack.

 The Portex shedding angle of attack magnitude, a_g, is expected to have a range as given by?

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where cd is the airfoll dray coefficient, and is a

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function of airfoll shape and surface-condition, angle of attack, and Mach number.

4. The second harmonic drag force is negligible with respect to the first harmonic drag force except at very small angles of attack, is of the order of a, times the first harmonic lift, and is expected to be negligible for essentially all practical flight conditions for helicopter rotors.

The feasibility study for the experimental tests indicated that tests were desirable if certain test facility, model, and instrumentation requirements could be achieved.

Test facility requirements included the following:

- 1. Wind tunnel turbulence, $\frac{1}{10^2} \frac{1}{0} \leq .0004$
- Known wind tunnel speed and angularity-distributions; speed range to-600 ft/sec.
- Sound field measurements outside the open jet test section, with tunnel empty and with a known sound source in the Test section (both with tunnel running).
- Capability to achieve full-scale helicopter Reynolds number range.

Nodel and instrumentation requirements included the following:

- Size large enough to achieve full-scale helicopter Reynolds number-range.
- 2. Standard airfoil shape, preferably NACA-0012.
- 3. Two- and three-dimensional-models.
- Hodels and mounts as rigid-as possible to reduce model motion.
- 5. Known model natural frequencies in flap-and torsion.
- 5. Accelerometer measurements to determine model motion.
- Surface pressure measurements to determine pressure magnitudes, correlation lengths, and frequencies;

Tests were performed at the United Aircraft Research Acoustic wind tunnel, which was designed for a turbulence level $(\sqrt{u^2}/U_1)$ of 0.0004. An SPL of the turbulence has not yet-been made by-RASA, but the overall level was reported to be approximately 0.001, somewhat higher than the design level. The tunnel test section can be operated as on open jet, in an acechnic chamber. The chamber is anechoic above 270 Az. Microphones were positioned within the anechoic chamber so as to be in the far field of the sound radiated from the model in the test section. The test section used during these tests had an open top and bottom with approximate dimensions of 21 inches (spanwise) by 30 inches=(streamwise). Steel side walls provided model-and instrumentation support, and some flow containment. Various-arrangements of flow control devices were used to reduce noise levels associated with the open jet nozzle and collector. Alternate downstream open-jet lengths were evallable, and offered advantages and disadvantages. The 30 linch length was chosen Lecause it represented, in our view, the most "well known" and reliable operating configuration of a new tunnel facility. The general arrangement of the test section is shown in Figure 1. The tunnel fan-undewent some modifications between the times that the 2-D

and 3-D model tests were conducted. Detailed analyses of tunnel noise have not been made for the two fan configurations, but preliminary investigations indicate that changes in the test section conditions were small. (A more detailed analysis may be available by the date this paper is presented).

Two wing models were used in these tests. Plan views are shown in Figure 2. Both were MACA 0012 airfoils, made of steel, with spanwise internal holes for surface pressure microphone and accelerometer cables, and with a surface pressure microphone mounted in a spanwise slider mechanism to permit the 30% surface pressure microphone to be traversed along the airfoil span. The two-dimensional model: (21 inch span) was clamped at each end, and the slider microphone could be moved to any desired spanwise position. The slider mechanism was observed to have a slight-gap along its leading edge and to be a few thousandths of an inch above the airfoil sufface. The three-dimensional model (# 11 inch span) was clamped at one end, and the slider microphone could be moved incremental amounts, Gepending upon available inserts to fill the slider gap. The slider=mechanism fit was better on the three-dimensional model than on the twodimensional model. A chordwise array of surface microphones was located seven inches from one end, for both wing models, with microphones at 15%, 30%-(slider), 38%, 50% and 70% chord. An accelerometer was located at midchord; at midspan of the 2-D model, and near the tip of the 3-D model. The acceleroweters were internal to=the surface. The surface pressure Microphones were mounted so assto have a very small-gap around the exposed diaphrage, and with the diaphrage wounted as nearly flush with the airfoil surface as possible. During some of the 3-D tests, not all of the surface pressure microphones were operational, and in any event only five of the surface pressure microphones, the accelerometer, and the two sound pressure microphones could be-recorded at:one time due to the limited numbers of powers supply units which were available for various amplifiers.

Two hot-wire-anemometers were mounted downstream of the wire. as shown in Figure 1. One was on a traverse mechanizm which permitted spanwise and vertical (normal to airfoil middle surface) motions, and is referred to as the "movable" hot-wire. The other could be adjusted manually only, and is referred to as the "fixed" hot-wire. It could be located at any spanwise position and at one inch vertical increments. The movable hot-wire required a vertical slot in one side wall to allow vertical motions. Holes were drilled in the side to permit vertical adjustment of the fixed hot-wire. Only positions below the O* angle of attack plane were attainable. Originally, it had been intended to make wake surveys at approximately 0.5 and 3.0 chord lengths downstream of the trailing edge of the airfoll. The use of a 30-Inch test section opening together with rather severe buffeting near the collector precluded making surveys at 3.0 chord lengths downstream, and the surveys at 0.5 were shifted to 1.0 due to interference with other instrumentation.

Two sound pressure microphones were located in the anechoic chamber, as shown in Figure 4. One was located directly above the

model centerline, midway between the tunnel walls, had an easily adjusted height, and is referred to as the overhead microphone. Another was located at a lower, more downstream location, but not so as to be in the direct "shadow" of the collector nozzle, was normally kept at a somewhat smaller radius from the model centerline as the cverhead microphone, and is referred to as the "downstream" microphone.

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Appropriate amplification of transducer signals was provided when necessary. An oscilloscope was available for some on-line monitoring and investigation, and an oscillograph and a magnetic tape recorder were used to record transducer output. The oscillograph had 7 mirror-type_galvanometers which were flat within \pm 5% to about 1K Hz and had a gradual drop off above-that. (The response is down about 25% at 2K Hz, and about 75% at 3K Hz.) The tape recorder was a one inch, 14 channel, FM recorder with a 27K Hz carrier signal, and had a flat frequency response up to 5K-Hz.

Test Procedures and Results-

Instrumentation-was tested and calibrated before each set of "ests. Individual components were monitored with the oscilloscope and replaced, repaired, or removed when found to be defective. System check-out included runs-made with the tunnel empty and with a one inch diameter strel cylinder placed at the airfoil midchord position. Some of these tests indicated significant characteristics of the system. They provide a base of reference for other measurements, as well.

It was noted during calibration of other instrumentation that the accelerometer seemd to have a residual output of 0.053g at about 60 Hz and 0.0204g at about 180 Hz. This was probably line noise, and could be a significant part of some of the accelerometer time histories. The overhead-microphone also had a residual signal with 30 Hz and higher frequency: noise contained in it.

The oscillograph-records are the source of most of the results presented in this paper. The primary function of the oscillograph was to serve as an on-line multi-channel monitoring device. Thus, all channels were used for primary transducer-output, and for most runs no reference signal for frequency (or paper speed) was recorded on the oscillograph. The maximum nominal paper speed was 80 ips, and there were occasionally variations by as much as a factor oftwo or more. Frequency values based on an assumed paper speed of the-oscillograph are-known to be inaccurate.

Tunnel-empty tests and cylinder tests indicated that noise from-objects-within the tunnel snould be of sufficient amplitude to be measurable, and rot be masked by tunnel background noise. A beating pattern, which was observed during the cylinder tests in the overhead and downstream sound microphone records, could be from flight spanwise nonuniformities in the tunnel-velocity or angularity. (Regular shedding from the cylinder was observed at all-velocities through peak velocities of about 670 ft/sec, or Reynolds numbers of about 2.4 x 10^5 .)

Spanwise correlation lengths in the wake and on the airfoil surface were investigated. Preliminary estimates of the length over which wake velocities were in phase-were made by observing whether or not-Lissajous figures-were generated on the oscilloscope when one hot-wire anemometer was used as the horizontal input and the other was used as the vertical input. In-phase velocity variations for the two-dimensional model were indicated for only a 4* angle of attack. at low velocities. At 4* and 100 ft/sec this length was approximately 1.5 inches; at 200 ft/mec-the length fell to approximately 1 inch. The correlation was not found, however, except on the vertical "edge" of the most turbulent region as indicated in Figure 5, and at the spanwise coordinate position of the chordwise array of surface pressure microphones. This indicates that either (1) the surface pressure microphones caused the correlation in the wake, or (2) the wake was warped vertically and surveys at other spanwise locations missed the region of correlation. It was observed that the maximum amplitude disturbance for 4* and 100 ft/sec occurred from-approximately 0.2 inch to 0.4 inch below the 0° plane. The observed dominant frequencies, together with this size of peak amplitude region indicates-that thu-wake thickness is approximately one-tenth the airfoil's projected dimension on the free-stream. It is possible that-helicopter rotors have lower frequencies and larger wake thicknesses than those observed during these tests. Different turbulent levels, airfoil surface conditions, and other differences in operating conditions could result in different frequencies, and it is expected that most-of these-differences would tend to lower the shedding frequency.

For those-configurations where pure-tones were observed, the surface pressure microphone measurements:indicate that the surface pressures were-correlated over the entire length of the airfoil. As shown in Figure 6, at 4° and 100 ft/sec the 151 surface pressure microphone, the overhead and downstream sound pressure microphones, the accelerometer, and to a degree, the 701 surface pressure microphone and the hot-wire anemometers all appeared to be correlated and have a dominant frequency of about 1160 Hz. A traverse with the JOA surface pressure microphone indicate, no-variation of magnitude,-phase, or frequency with span, and-appeared to have the same amplitude as the 151 microphone.

One result of the spanwise surface pressure midrophone traverse was the observation that the 15t microphone (and probably all "upstream" microphones) had a significant effect on the 30t microphone (and probably other downstream microphones), as shown in Figure 7. A high frequency disturbance of significant magnitude was introduced by placement of the 30t microphone downer and of the 15t microphone used Figure 7.4) and was eliminated whether 30t microphone was removed from the downstream position by approximately 0.5 inch (see Figure 7.b). The 30t-microphone output shown on Figure 7: is as free from this-high frequency disturbance as any-downstream microphone signal recorded during most of the runs. Other conditions of angle of attack and velocity showed similar effects of moving the

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30% microphone out of the "downstream" position. All downstream surface_microphones had output containing significant amounts of high frequency output: as compared with the 15% microphone butput for cases where-it had a-relatively clean signal. (That is, output was similar to the 30% microphone when it was downstream of the 15% microphone). Thus, it must be assumed that most, if not all, of such-output is due to the upstream surface microphone. The oscillograph records_of-the chordwise surface pressure microphones are of doubtful value, but analysis of the magnetic tape records may yelld more information.

Wake correlation was also investigated during the threedimensional model tests. Correlation lengths of approximately 0.5 inch were observed for the wing at 4° angle of attack and at tunnel-velocities of 100 ft/sec and 200 ft/sec, downstream of the surface pressure microphone array-during the three-dimensional model tests. Again, J wake-region of peak disturbances and observed frequencies indicated a wake thickness on the order of one tenth the airfoil's projected dimension on the free stream. There did=not appear to be increased spanwise-correlation lengths in the wake near the tip of the three-dimensional model. Surface pressure microphone traverses indicated-that the 15%-and 30% (movable) microphones had the same amplitude, frequency, and phase along the entire span, for those cases investigated.

The models could be expected to respond most-rusdily near their natural-frequencies. An attempt was made to determine natural frequencies of the three-dimensional model by tapping the model mear the typ. Resulting accelerometer output indicated that the two lowest bending natural frequencies of the three-dimensional model were at approximately 135 Hz and 527 Hz. Higher frequency modes exist, but mode types and frequencies were not clearly indicated by these simple tests. Model-physical properties and support conditions are not felt to be known sufficiently well to permit a theoretical estimate of the model matural frequencies.

The accelerometer output indicated that there was model=motion at the same frequency as surface and far field signatione pressure variations for many-angle of attack and flow conditions. At other conditions the accelerometer either had no significant output with the same frequency as the microphones, or that frequency component was not clearly distinguishable from the oscill graph record. The possibility of model motion exists, and either torsional pr-flatwise=motions would_have a corresponding angle-of-attack, lift-variations, and possibly wake velocity and sound pressure variations, Model-motion, as measured by the accelerometer, was valculated for the two-dimensional model for y = 4* and v = 100 ft/sec. This condition resulted in very nearly pure tone (single frequency) output from all instrumentation. It also had one of the largest ratios of model velocity-to sound pressure ratios, indicating that if model sotion-were ever-important, it should be for this condition. Calmilations for this-case-indicate_that (1) the-airfoil potion-as a flat place would not be large enough-to cause the observed sound-pressures at the overhead microphone, and (2) lift variations due to the angle of attack caused by flapping velocities would not be large enough to cause the observed sound pressures at the overhead microphone. The measured surface pressures, however, would be sufficient to cause the observed sound pressure. Therefore, model motion does not appear to be the primary source of sound even when it is at a relatively large level-compared to the sound. It is entirely-possible that model motion, though small, does contribute to the mechanism(s) involved in vortex shedding and turbulence, and thus plays an important roll in sound-generation for some model configurations. The observed surface-pressures for-these conditions was approximately 1/2 the maximum pressure predicted in the preliminary study mentioned earlier, so is the correct order of magnitude for vortex shedding pressure disturbances. Analysis of other test conditions is dependent upon frequency analysis of the magnetic tape records, which was not completed at the time of the printing of this-maper. It-is expected that further analysis of the experimental data will be-done, including spectral analysis of some of the recorded pressure time histories. The results of this and other available work will be:used to develop methods for predicting wortex shedding-parameters as a function of airfoil and operating characteristics. These methods will be-used in conjunction with existing rotor-blade loads programs and rotor noise prediction programs to predict helicopter main rotor vortex noise for helicopters in various flight regimes.

Conclusions

The expected magnitude of surface pressures was observed for cases where "pure tone" signals were observed, but frequencies were an order of magnitude higher than predicted on the basis of airfoli dimension perpendicular to the free stream. Model motion did not appear to be of sufficient magnitude to account for the observed sound levels, but may be an important part of the mechanismis) involved in vortex shedding noise, particularly where pure tones are exitted. Shedding frequencies may be different on operational helisopter rotors than those observed during these controlled tests.

Nost angle of attack and velocity conditions did not result in pure tone calssion, but was characterized by sound emission over a range of frequencies. None of the observed frequencies:were in the range which would be predicted using a Stroubal number of approximately 0.7 and the airfoll's dimension perpendicular to the free stream; the observed frequencies were approximately an order of cagnitude higher than those-predicted on that banks.

For conditions where pute tones were observed the surface prossure variations were in phase over the entire airfoil, wake velocities were in phase for lengths on the order of the sirfoil thickness, and accelerometer, surface and sound pressure microphones, and hot-wire enemometers all had the same design that frequency.

No increase was observed in the spanwise length within which wake velocities were correlated in the tip segion of the three-

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dimensional model, as compared with two-dimensional model results. Three-dimensional effects do not appear to have a significant effect on surface pressure or sound pressure frequencies or magnitudes.

further analysis of the data-is anticipated, and may modify these-conclusions and indicate other important facts related to the generation of sound by airfoils.

21 ACCELEROMETER (midchord) 11 MICROPHONES MICROPHONES Ì 7 MODEL SUPPORT SLIDER AT JON CHORD TWO-DIMENSIONAL MODEL THREE-DIMENSIONAL MODEL

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Figure 1. Test-section arrangement



Figure 3. Hor-wire anemoneter arrangement

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OVERHEAD MICROPHONE DOWNSTREAM MICROPHONE (20", 0, 41")

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Typical sound pressure microphone arrangement Figure 4.

15% SURFACE PRESSURE MICROPHONE

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OVERHEAD SOUND PRESSURE PICROPHONE Martin Martin Martin Martin Martin

DOWNSTREAM SOUND PRESSURE MICROPHONE

Typical-transducer signals-for "pure tone" conditions Figure_6.



Figure-5. Wake correlation region



A. JOB downstream of 15%

B. 30% not:downstream of 15%

Figure 7. Effect of vostream surface pressure microphone on downstream surface pressure microphone DETERMINATION OF THE AERODYNAMIC-CHARACTERISTICS OF VORTEX SHEDDING FROM LIFTING AIRFOILS FOR APPLICATION TO THE AMALYSIS OF HELICOPTER NOISE

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Figure 8. Model motion - sound pressure comparison

ROTATING BLADE VORTEX HOISE WITH AND WITHOUT AXIAL VELOCITY

James Scheiman and David A. Hilton MASA Langley Research Center Hampton, Virginia

SUMMARY

An experimental investigation has been made in the Langley full-icale tunnel and outdoors to investigate some of the characteristics of vortex noise generated on a rotating blade system. Acoustic measurements were made for two different blade sections with several tip shapes when the blades were rotating in their own shed wake and when the shed wake was blown downstream. The blades were operated only at zero-lift at each radial section. The results indicate that the tip shape changes had very little effect on the overall sound pressure level. Introducing atlativelocity to blow away the blade shed wake for the rotating circular blade:section resulted in an increase in the noise level, while, for the airfoil section, the overall noise level decreased.

INTRODUCTION

"ctor noise is a major operating problem of helicopter and propeller driven aircraft. The development of satisfactory methods for predicting so-called "vortex roise" has been an objective of the helicopter and propeller industry, but a lack of experimental data has retarded this goal. For example, in reference 1, Yulin encountered difficulties in the experimental separation of rotational and vortex noise. Also, Deming, reference 2, states that gusts of wind may cause the sound pressure to vary considerably.

The origin of "vertex noise" is controversial. In reference 3, Stevell and Seming designed special rods in an attempt to isolate peaks in the specterm corresponding to the Stroubal frequency; however, they found that such attempts were unsuccessful. More recently, the origin of vortex noise has been attributed by some to Yon Kirzán vortex rheiding and by others to turbulence abevi of the blais. For example, reference 4 assumes that the oscillating blade surface pressures are associated with the sheiding of eddles resulting free vortex street effects; whereas reference 5 initiates that the vortex noise is associated with the random turbulence aheat of the blaie, which in turn exuses surface pressure oscillations.

A shortage of experimental information on vortex noise had seemed the major imperiment to devising and correlating theory with test results. To help overcome this obstacle, the NAGA-Langley Mesearch Center has recently completed a test program within the Langley full-scale tunnel and outdoors. The test program consisted of noise measurements for a rotor specaring at zero lift for two minfoll sections. The tests included rotor operation with the blades rotating in their complete which and with the blade wake blown downstream. The two blade sections were a circular pipe and an SAGA CO12 minfoll section. Noth blades had the same roin diameter and blade thickness, namely, $f_{\rm c}O_{\rm S}$ and $5_{\rm c}O_{\rm c}$, respectively. For the wind-on conditions, the SAGA CO12 section blade was provided with a helical twist so the airfoll operated at zero lift all along its-span. Various blade-tip configurations were tested.

SYNCAR

D rotor disactory M-

f frequency, Hz-

f rotor rotational speed, rpm

hall radius (see text for definition), m

velocity along the axis of rotor rotation, m/sec

n rotor angular speed, rad/sec

TESTS

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Test.Setup

The indoor tests were conducted in the Langley $9.15 \times 18.5 \pm$ full-scale wind tunnel. A schematic sketch of the test setup drawn to scale is shown in figure 1 and a photograph of the setup is shown in figure 2. The rotor rotational axis was in the center of the tunnel and approximately 3.96 m above the ground board. The pertinent microphone locations are indicated by the solid dots in figure 1. The microphones shown are aligned with or at 45° to the rotor rotational axis. The zero-wind indoor tests were duplicated in the catdoors. For the outdoor tests the rotor axis was aligned parallel to and approximately 2.44 m above the ground-level. The recording microphones were located at every 22.5° azimuth angle end at a 2-diameter distance. The outdoor tests were conducted to obtain a reverberation evaluation of the fullscale tunnel.

Pull-Scale-Tunnel-Reverberation Effects

The question of the reverberation effects arises whenever acoustic measurements are made in a closed-chamber. Two separate test programs were conducted in order to answer-this question. The first program consisted of identical tests conducted with the rotors inside the tunnel and outdoors under zero-wind coulitions. The second program was conducted inside the testchamber only and was directed-specifically toward obtaining directivity_and reverteration times within-the test.chamber.

Comparisons of indoor and outdoor noise-frequency spectra for two differort models are shown in figure 3. One of the models is the blade with the circular cross section and the other is the blade with the NACL CO12 airfoll section. The comparison is for zero axial velocity and for one microphone position, namely, at a distance of two rotor diameters and alined along the retor rotational axis. The comparison of the amplitude and spectrum distribution for the circular blade section is quite good. For the NACL CO12 blade section, is also quite good, but not so good as for the circular blade section.

With indoor-state only, an evaluation was made on the basis of moise decay rate with distance (inverse-square law). The measured data indicated a 5- to bodd difference as compared with a theoretical free-field value of 9.6 dB. This difference of about 5-dB is the magnitude of the reverteration effect.

In addition to the index-outleer noise comparison, reverteration tests were conducted in the test chamber. The results of this program are presented in reference 6. These-results, for zero-wind velocity, have been extrapolatedfor the models tested herein, and samples of the conclusions are presented in figures 5 and 5 for the two different rotor blate sections. The 0^9 aximpth positive on these figures is aligned with the rotor rotational axis vector (using the right-hand rule). These plots are in terzs of the hall radius divided by the rotor diameter. The hall-radius is defined as the distance from the source where the sound pressure from the direct field equals the space average sound pressure of the reverberant field. In other words, accustic measurements at one hall radius will be 5 dB above the corresponding

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free-field measurements. Further, at a distance of one-half the hall radius, this difference would be 1 dB. Im general, the original test-chember accustical evaluation (ref. 6) indicated that a 1000-Km frequency band resulted in the smallest hall radius. Further, for octave-band center frequencies outside of the range plotted, the hall radius is greater than that for a frequency of 250 Hz. Figures 4 and 5 indicate that microphone positions alianed with and at h_5° to the rotor rotational axis at the 2D distance are inside of or near a distance of one hall radius, with the asception of the 1000-Km frequency band. Therefore, except for the 1000-Km band the indoor data presented herein chould be between 1 and 3 dB too high. Comparison of the two methods of evaluating the test-chember reverberation than the comparison of the indoor and outdoor measurements.

NEBULTS AND DISCUSSIONS

A plot of the radiation pattern is presented in figure 6 for the two rotor blaic sections. This is based on outdoor measurements and presents the overall sound pressure level at a two-rotor-diameter distance with zero axial velocity and for variations in rotor rotational speeds. The zero angle is aligned with the rotor rotational axis (using the right-hand rule). The data indicate that the indication is nearly symmetrical about the 90° azimuth angle, as would be expected for zero-wind conditions.

For the circular bladed rotor, figure 6(a), the radiation pattern indicates algost equal-radiation in all-directions. Since rotor torque will produce dipole radiation in the plane of the rotor whereas wortex shedding will produce dipole radiation along the axis of the rotor, figure 6(a) indicates that the radiation pattern of both noise sources are nearly equal. Further, it appears that the radiation pattern increases equally in all directions as the rotor rotational speed is increased.

The radiation pattern=for the mirfoll bladed rotor is shown in figure6(b). At low rotational=speeds the vortex=shedding seems to be the predominant noise source, whereas at the high speed the torque radiation is dominant. This behavior is certainly different for the two blade sections. The reason for this difference will be explored further in=figures 7 and 8.

Figure 7 is a plot of the 1/5 cutave frequency spectra for the airfoll bladed rotor. One plot is for a microphone alined with the rotor rotational -axis (fig. 7(a)) and the other plot is for a microphone in the blade rotational plane (fig. 7(b)). From figure 7(b), it is seen that for the higher-rotational speeds, the high-amplytude noise levels originate in the low-frequency spectrum, namely, 50-to-125 Mg center-Sand frequencies. This result is indicative of rotor-torque-or-blade thickness noise radiation.

These same data are shown scaled in figure 8. The amplitudes were scaled according to the sixth power of the rotational tip speed and the frequencies are shown divided by the tip speed. This figure shows that the data aligned with the rotor rotational axis (fig. 8(a)) scale well, whereas the data in the blade rotational plane (fig. 8(b)) do not. This observation is another manifestation of the results from figure 6(b). Figure 8(b) shows not only that amplitude does not scale but also that the scaled frequencies are mixed. A search of the literature shows no amplanation; therefore, it is concluded that this strong phenomenon is not understood.

Effect of Tip Shapes

Vortes noise radiation has been shown to be proportional to the velocity to the 3.5 power (e.g., ref. 3). By far the largest portion of the noise level, therefore, originates from the extreme outer part of the blade. Thus, it might be reasoned that changes in the blade-tip fluid flow conditions might produce large changes in the noise level. Further wind-tunnel tests of loads on stationary circular cylinders: (refs. 7 and 8) with various tips had show i a significant effect of tip shape. In order to confirm this influence on ro-sting blades, various geometric tip shapes were tested. The results of a portion of these tests are shown in figure 9 for a microphone position aligned with the rotor-rotational axis and at a distance of two rotor dismeters from the source. From figure 9 it is evident that the various blade tip shapes tested did not produce any significant difference in the overall-sound pressure level. Similar results were obtained for other microphone positions.

For the MACA 0012 bladed rotor a squared-off blade tip and a blade tip body of revolution were tested. The body of revolution blade tip had a radius equal to one-half the blade thickness at that chord station. A comparison of the noise radiation for these two blade tips (fig. 9) shows the same result as tests with the circular bladed rotor, that is, no noticeable difference in the overall noise level.

On the basis of the results of references 7 and 8 the blade-tip flow conditions are certainly changing. However, the results herein indicate that sound pressure radiated from the remainder of the blade dominates, and therefore the effects of tip changes are unnoticed.

Effect of Plade Airfoil Section

Figure 10 presents a comparison of the sound pressure level for the two difforent blade cross sections (circular and MACA 0012) with and without axial velocity. The results indicate that the blade with the circular section makes a significantly larger noise level both with and without axial fluid flow when the blade frontal areas are equal. This conclusion is in agreement with the conclusions in reference 1, where it is stated that the intensity of vortex sound increases in proportion to the form dreg. Powever, Yudin in reference L'encountered difficulties separating "rotational" and "vortes" noise with the compencement of axial flow. This difficulty is not believed present in this investigation because the blades did not produce lift. Acoustically, it is concluded that the same frontal area, rod, and airfoll blade acctions behave differently and this difference exists when the rotor operates with or without axial velocity.

Effect of Turbulence

An attempt was made to determine more explicitly the origin of vortex noise. Figure 11 depicts the effect, for two different microphone positions, of imposing a small axial velocity on the rotating blades to blow their sheiwake away-before the passage of the following blade. One microphone is aligned with the rotor rotational axis and the other-is at 45° to the rotor rotational axis. Both microphones are at a distance of two rotor diameters. Recall that the rotor with the airfoll section had a helical twist and that keeping zero lift on the entire blade span requires precise combinations of rotational and axial velocity. Therefore, the axial velocity for this model varied contimuously with each change in rotational speed. The results in figure 11 indicate that the introduction of axial velocity on the circular blade section

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increases the overall sound pressure level by about 3 dB; whereas, the introduction of axial velocity on the NACA 0012 bladed rotor resulted in a decrease of about 6 dB in the overall sound pressure level.

Part of the reason for the foregoing results might be explained as follows: The mirfoll rotating in its own wake contains some "rotational noise" due to lift which is caused by velocity fluctuations in the shed wake. These fluctuations in lift do not occur when the shed wake is blown downstrawn, thus resulting in a decreased noise level. Small axial-velocity fluctuations (present when the blade rotates in its own shed wake) will produce relatively large lift fluctuations on the mirfoll section because of its high-lift-curve slope but would produce zero lift on the symmetrical circular blade section.

On the other hand, the fact that the circular airfoil section produced more noise then its shed wake was blown away by axial velocity cannot be explained. This section is a poor actodynamic section, so that blowing the wake away would not some to affect the section either aerodynamically or acoustically. Introducing axial velocity certainly increases the dynamic pressure on the blade; however, the vectorial addition of the axial velocity and tangential velocity vectors will not produce a sufficient increase in totalhead to explain the 2 to 3 dB increase in sound level.

CONCLUDING REMARKS

An experimental investigation was conducted to define further the characteristics of vortex noise generated from a rotating blade system. The analysis of the data indicates the following results:

1. A comparison of the amplitude and spectrum distribution for two models tested in the wind tunnel and outdoors is good. Evaluation of the wind-tunnel ,verberation from the inverse-square law of the overall sound pressure levels. , also relatively good. Purther, the test chamber "hall radius" has beendetermired for the two different blade sections operating in the wind-off condition.

2. The sound-pressure radiation pattern indicates that for the circular bladed rotor, the noise level increases equally in all directions with increase in rotor rotational speed, whereas the radiation pattern for the airfoll-bladed-rotor increases more rapidly in the plane of the rotor than along the aris of the rotor with increasing rotor rotational speed. The reason for this is presently not understood.

The blade tip shapes tested did not show any appreciable "ffection.
 overall sound pressure level.

4. The circular section is much the noisier of the two sections even though the frontal areas of both blades were the same. This result confirms previously found results indicating a direct relationship between increased noise level and increased form drag.

5. The introduction of axial velocity to blow us-y the turbulent shed wake of one blade before the passing of the following blade caused a decrease of approximately 6 dB in the noise level of the airfoil section as compared to the case for zero axial velocity. Part of the explanation of this resultwould seem to be that small axial-velocity fluctuations (present when the blade rotates in its whet wake) would produce relatively large lift fluctuations on the airfoil section because of its high lift-curve slope, but would produce zero lift on the symmetrical circular blade section.

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Figure 1.- Test setup.



Figure 2.- Test setup.

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Figure 11.- Noise level versus rotational tip speed.

Vortex Shedding Hoise of an Isolated Airfoil

Robert W. Paterson, Paul G. Vogt, Roy K. Amiet, and Martin R. Fink United Aircraft Corporation Research Laboratories East Martford, Connecticut 06108

ABGTRACT

Vertex noise produced by an isolated nonrotating airfoll in low-turbulence flow is being investigated analytically and experimentally. This paper serves as a progress report on the not yet completed investigation. Surface and far-field acoustic spectra and cross-correlations were obtained with full-span and semispan NACA 0012 airfoll models of 7-in. (23 cm) chord. These were tested in a semi-open jet with solid sidewalls 21-in. (53 cm) apers A= open jet boundaries above and below the test section. Airspeeds ranged from about 100 to 670 fps (30 to 200 m/sec), providing a range of Reynolds number from 0.5 x 10^6 to 2.7 x 10^6 .

At low Reynolds numbers, the observed far-field spectra were dominated by a discretistione. The intensity of this tone increases to a maximum and then decreases with increasing velocity. The airfoll noise could not be detected above the far-field tackground noise for high Reynolds numbers and low angles of attack. The measured surface pressure spectra then were typical of those expected for turbulent boundary layer pressure fluctuations.

An approximate analytical methol for describing and predicting the surface and far-field tone noise phenomena is being developed.

INTRODUCTION

A-ne.Respirer rotor generates three major types of noise: periodic, interference, and vortex. The periodic noise is caused by the pressure pattern of the rotor blaie's thickness and life distribution. That pattern varies once per revolution relative to the links etc. is pared past on observer as the blaie rotates. Interference noise 1. caused by relative motion between the blaie and an adjacent physical or serolynamic obstruction (a fuselage or another blaie's tip vortex). The remaining type of noise, vortex noise, is caused by interaction of a blaie with its own boundary layer and near wake. Vortex noise imposes a floor on the noise generated when rotor lowling and interactions have been minimized. Thus the study of vortex noise is important since it represents a practical minimum limit on helicopter rotor noise and forms an interesting problem in basic fluid dynemics.

Prior to studying the vortex noise of rotating blaids, it would be useful to understand the simpler problem of the vortex noise produced-by a nonrotating airfoll. This vortex noise will be accompanied by broadband noise from lift fluctuations induced by upstream turbulence and from pressure fluctuations within the airfoll's turbulent boundary layer. The only analytical description of vortex noise is that of Sharland (Pef. 1), which does not permit calculation of surface pressure fluctuations. Few experimental studies are available. Nost of these were conducted with low arperi ratio models supported through the shear layer and tested at relatively low beynoid numbers and might not be representative of high aspect ratio blaides at full-scale conditions. Also, the contribution of free stream turbulence to previously measured vertex noise characteristics is not known. Finally, in morter noise experiments only far-figit gound pressure neasurements have been made with no-determination of ourface pressure fluctuations and correlation areas. Availability of such data would be useful for separate evaluation of different assumptions within various portions of analytical methods for calculating vortex noise.

Recently, an acoustic wind tunnel was constructed at United Aircraft Research Jaboratories. This tunnel is capable of testin- mirfoll models at full-scale Reynolds numbers and Much numbers for the rotor bludes of small belicopters. ...uch models are large enough to contain commercially available mircophone instrumentation for measurement of very weak surface pressure fluctuations. Provisions have also been made to ensure a very low turbulence level in the mirflow in an attempt to minimize its effect on vortex noise. The objectives of the investigation described herein were (1) to obtain mirfoil surface and far-field acoustic data in that wind tunnel for variations of velocity and incidence, (2) to utilize these data in evaluating analytical assumptions concerning details of the process that generates vortex noise, and (3) to combine the velidated assumptions into a new analytical method for predicting mirfoil-vortex noise.

The experimental effort is being funded by Army Research Office - Durham under Contract No. NAHOOA-69-0-0089. The analytical effort is being conductal as part of the United Aircraft Persearch Laboratories Corporate-funde resourch: progress. Both portions of this investigation are in progress ar of the dat of this report; completion and preparation of a final report are scheduled for the end of this year. This paper therefore should be regarded as a progress report sather than a description of completed effort a

DESCRIPTION OF EXIFRIMENTAL FOULTMENT

Acoustic Percarch Tunnel

The Artistic Berearch Tunnel, shown schematically in Fig. 1, is a controlled turbulence level, open circuit, open-jet wind tunnel designed specifically for actrolynamic noise research. Intensitivity of test section flow to external wind condition. I. achieved by the use of a high length to diameter ratio (72) honeycomb at the tunnel inlet. For the present experiment, five 25 mesh turbulence suppression creative reprovided in the inlet. Here of the screens in conjunction with a contraction ratio of 1° preduced both a low turbulence level and a spatial mean relacity distribution in the test section messured to be uniform to within f0.25 percent. The ratio of the rm testical furbulent velocity fluctuation to mean belocity was measured to be less than to percent for frequencies above 206 Hz. The open jet is contained within a 10 ft high. 18 ft long (axial direction), and 22 ft wide realed reinforced concrete chalter line with one foot fiberglass wedges. Hensurements of the chamber acoustic properior have demonstrated that the chamber is amended (6 4B decrease in the production of the two demonstrated that the chamber is amended (6 4B decrease in the production of the chamber for frequencies at an above 206 Hz.

Figure , hows the tell section arrangement employed in the present study. A rentangular feet section of in, high by 21-in, wide with 5 in, couniet corners was on on the provide two-dimensional films. To provide a uniform spanwise variation of ionizing on Fact-open wirfold models, the vertical sides of the jet were closed with asdeplate estending from the contraction outlet into the jet collector inlet. The une of ideplate also eliminated the need to estend the wirfold or airfold support through the thick, highly turbulent jet shear region which would normally exist in

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their absence. With sideplates installed, variations in spanwise velocity distribution occur only in the sideplate boundary layers. The sideplates were constructed of aluminum with a smooth finish and were not acoustically treated.

To isolate the mirfoil models from vibrations of the tunnel structure, the mirfoils were directly supported from the anechoic chamber floor. A 1/2-in. annular clearance, filled with sponge rubber, provided isolation between the sideplates and the mirfoil's circular end supports.

The semi-open jet was collected at the diffuser entrance by a jet collector. The interior edge of the collector was located on the constant mass flux streamline which divides the mean jet flow from the chamber recirculation pattern. This positioning helped to minimize streamline distortion in the test section. Based upon model tests, a 4-in. radius collector lip was provided which minimized the background noise due to shear layer -- collector lip interaction. In addition to this broadband model, an acoustic coupling between the contraction outlet and the collector lip produced strong discrete-frequency background noise (edge tones) at certain tunnel speed-. To suppress this noise source mechanism, an array of 20 small triangular tabs projecting 1/2 in. into the jet were installed at the contraction outlet. Based on the measured variation of tunnel background noise with open jet length, a test section length of 30 in. was chosen for the present experiments.

The three-stage diffuser located downstream of the jet collector operates unstalled and is therefore not a major source of background noise. To attenuate tunnel fan noise, an absorptive Z-shaped muffling section consisting of parallel fiberglass baffles and lined bends is located between the diffuser and fan inlet. For frequencies above which the chamber is anechoic (250 Hz), the fan muffling is sufficiently high that the background noise level in the chamber is set by noise radiated from the jet shear layer and from the shear layer -- collector interaction. Padial vanes located at the inlet of the 1800 rps centrifugel fan provide continuously varible test section velocities from 60 to 670 ft/sec. Tunnel speed is determined from total pressure at the contraction inlet and-static pressure from a ring of taps at the contraction outlet. Fluctuations in tunnel speed with time were measured to be less than ²0.5 percent.

Models and Instrumentation

Three mirfoil models of 9-in, chord were fabricated for this program. Two have MACA 0012 sections and the third has an MACA 0018 section. One of the MACA 0012 mirfoil models and the MACA 0018 mirfoil model completely span the 21-in, wide UARL Accustic Research Tunnel test rection. The other model spans only half of the test section and has a tip fairing to simulate a wing tip. The models were fabricated from stainless steel with a surface finish of approximately 32 micro-inches. A tolerance of $\frac{1}{2}$ -0.010 in, was obtained with 0.005 to 0.015 in, discontinuity on the instrumented aide and less than 0.005 in, on the other side. Drawings of the three mirfoil models are presented in Figs. 3 and $\frac{1}{2}$. The models were mounted as shown in Fig. 2 with the leading edge 9.5 in. downstream of the inlet contraction lip. The mounting was designed to prmait variations in mirfoil angle of ettack.

The microphons installation sketche: in Fig. 4 require: a minimum of 0.95-in. mirfoli thickness. In order to obtain microphone positions between 15 and 50 percent chord of an NACA CO12 mirfoll, a 9-in. mirfoll chord was required. Druel 2 Kjøer (DMK) condenser microphones were used because of their high sensitivity to pressure fluctuation and low sensitivity to vibration and temperature changes. From the results of small-scale tests conducted with microphones flush and cavity-mounted. it was decided to flush-mount the microphones to avoid cavity resonance. It was also decided to test without the microphone grid to avoid highfrequency noise caused by the grid. The microphones-in the airfoil were optically aligned to within 0.004 in. of the sirfoil surface. An annular gap of 0.008 in. existed around the installed micronhones. The micronhones were installed in a manner similar to that described in Ref. 2. In order for the microphones to be flush mounted in the airfoll surface, BAK right-angle adapters had-to be used. The 1/4-in. microphones were the smallest for which such adapters are made. As shown in Fig. 3. five 1/4-in. Bik microphones were located on the NACA 0012 airfoil models. Four were fixed at one-third span and 15, 38, 50, and 70 sercent chord. The right-angle adaptor was rebuilt in order to fit within the airfoil section at 70 percent chord. The fifth microphone was mounted at 30 percent chord in a slider which allowed spanwise travel (Fig. 3). For the half-span model, inserts were used to close the gap caused by movement of the slider. To obtain far-field pressure measurements, a 1/2-in. microphone was mounted on a boom 7 ft above the tunnel centerline.

Data were sequired on line with swept one-third octave and 10 Hz filters and reel-time correlations. A BMK Audio Frequency Spectrometer (Type 2113) coupled with a DMK Lavel Recordsr (Type 2305) produced the one-third octave spectra. All sound pressure levels in decibels were determined for 2 x 10⁻⁶ dynes/cm² reference pressure. A Quan-Tech Wave Analyzer (Hodel 305-R) produced the 10 Hz spectra and a Salcor Correlation and Probability Analyzer (SAI-42) the correlograms.

The microphones were calibrates with a BAK Mistonphone at 250 Hz and with a General Radio Calibrator at 125, 250, 500, 1000, and 2000 Hz. An acoustic coupler fabricated at-UAR was used during calibration of the surface microphones. The signals were filtered (with IICA type 550 25 filters) when using the correlator in order-to remove low-frequency noise associated with the tunnel drive fam.

A NAK Accelerometer (Type 4336) was installed in the mirfolls as shown in Figs. 3 and 4. This accelerometer operated in conjunction with a MAE Vibration Pick-'P Preamplifier (Type 1606) and Microphone Amplifier (Type 2603). The accelerometer was calibrated at 60 Hz with the Vibration Pick-Up Preamplifier.

DESCRIPTION OF ANALYTICAL METHOD

A general framework for studying the acoustic radiation caused by vortex noise is provided by the relationship between surface pressure and the far-field radiated sound field. Within this framework, measured or analytically predicted surface pressure fluctuations can be used to predict the radiated acoustic field of an airfold undergoing vortex shedding. In addition, such a framework can be used to help interpret aerodynamic and acoustic data and to evaluate assumptions within various analyses of vortex noise.

The theoretical foundations for relating surface pressures on a body in a field to the sound produced by this body were originally developed in Ref. 3 and later generalized in Refs. 4 and 5. These analyses permit the sound produced by the body to be expressed in terms of a distribution of monopoles and dipoles on the surface of

VORTEX SHEDDING NOISE OF AN ISOLATED AIRFOIL

the body. Since the monopole distribution is proportional to the normal velocity of the surface, and since the mirfoil for the present experiment is stationary relative to the free stream velocity, the monopole term is zero. Thus, only the dipole distribution over the surface contributes to the noise. If the surface loading (or pressure) at each point on the mirfoil is known as a function of time, the farfield sound pressure produced by the mirfoil can be calculated by integration of Eq. (2.18) of Ref. 4 over the mirfoil curface, i.e., by

$$P = \frac{d\omega_{\ell}}{4\pi a_{\ell}} e^{\omega(t - \frac{1}{2})} \int_{A} G(\omega, \underline{a_{\ell}}) e^{\frac{d\omega}{dt} (\frac{d\pi}{dt} \cdot - \frac{1}{2})} \frac{da_{\ell}}{da_{\ell}}$$
(1)

where the \times axis is in the flow direction, the y axis is in the span direction, and z normal to the span. In general, however, for a random or nondeterministic process, the detailed distributions of airfoil loading as a function of time and position required for evaluation of Eq. (1) is not known. This equation must then be cast in terms of functions characteristic of random processes such as the loading power spectrum and correlation length.

The Power Spectral Density (PSD) in the far field is obtained by Bultiplying the Fourier transfer of Eq. (1) by its complex conjugate. When this is done, Eq. (2) is obtained.

This equation relates the FDD in the far field to the cross-correlation of surface pressure fluctuations on the mirfoil and is valid for any loading distribution. Significant simplification of this equation is possible for random processes whose dominant wavelengths are much larger than the linear dimensions of the regions on the mirfoil-over which pressure fluctuations are correlated or in phase. These regions are considered correlation meas. It is important to note that the phasing between correlation areas is random for a random process. This permits the mirfoil FDD to be computed by summing up the separate FDD contributions of each meas. If the process is deterministic (i.e., not random) then even though regions on the mirfoil can be found over which pressure fluctuations are in phase, the contributions from each area cannot be misci separately since the phasing between meass is not random. In this case, the contibution of all the "meass" to the pressure must be computed first and then the FDD obtained. Thus, for deterministic processes, the concept of correlation area loads some of its physical appent.

The assumption that-the wavelength is large compared to a correlation area is equivalent to a compact source assumption. This assumption allows the exponential phase in the integral of Eq. (2) to be neglected, significantly simplifying the integral. Use of the compactness assumption is valid if the difference in distance from the chaerver to any two points within a correlated area is small compared to an acoustic wavelength. This assumption will be met if, as discussed above, the correlation length is small compared to a wavelength. The assumption can also be met if the far field observer is directly above the airfoil since all points of the airfoil will then be equidistant from the observer (for an airfoil with small camber and angle of attack). This is an important point since the *i* axis is also where most of the far field acoustie measurements are being maie. The neglect of the exponential factor in Eq. (2) for either of these two reasons then allows a correlation area to be introduced as

$$S_{c}(\underline{\alpha}, \omega) = \frac{1}{S_{qq}(\omega, \underline{\alpha}, \omega)} \int_{A} S_{q, q_{1}}(\omega, \underline{\alpha}, \underline{\alpha}, \underline{\alpha}, \omega) \underline{\alpha}, \qquad (3)$$

:

For a rendom process, this area takes on the physical significance discussed earlier. The far field PSD can now be written as:

$$S_{pp}(\omega, z) = \frac{\omega^2 z^4}{(\omega \pi^2 a^2 x^2)} \int_{\Delta} S_{c}(\underline{x}, \omega) S_{\underline{x}, \underline{x}}(\omega \underline{x}, \underline{y}) dz \qquad (4)$$

Equation (4) is now in a form which can be easily interpreted and in which Sc and S_{QQ} can be obtained from surface pressure measurements and correlations. As can be seen, Eq. (4) essentially sums the contributions of each correlation area over the whole airfoil as discussed above. It is generally valid for all field point locations if the wavelength is large compared to the correlation length and, in particular, is exact, independent of wavelength for field point locations directly above the airfoil.

If eirfoll vortex noise is essumed to be a broadband raniom process, as in Ref. 1, the far field PSD given by Eq. (4) can be integrated over all frequencies and over a spherical area surrounding the sirfoll to obtain the total radiated energy. This procedure yields Eq. (3) of Ref.-1. It was assumed in that analysis that broadband noise was caused by fluctuating loadings generated by fluctuations of near-wate flow direction. The center frequency of this broadband noise was taken as that for a Stroubal number of 0.2 referencei to airfoll maximum thickness. The correlation area was taken equal to the maximum eddy size, which was assumed to have a linear dimension equal to the airfoll half-thickness.

An alternate approach is obtained by assuming that vortex noise occurs as a discrete tone, as was observed in this experimental program. The aerolynamic behavior of the near-wake fluctuations and surface pressure fluctuations that radiate noise to the far field could then be examined.

An approach to calculation of near-wake fluctuations had been developed by Krzywoblocki (Ref. 6) to predict the buffeting of sircraft tail surfaces caused by the wing wake. In that analysis, it was recognized that the wing produces a steady boundary layer that becomes unstable as it flows into the wake. For sufficiently low Reynolds numbers, the near wake then develops into a periodic Karman vortex street. Some fraction of the vorticity generated by the boundary layer-during one period of the vortex street then would be concentrated to comprise each vortex. The wing pressure distribution must fluctuate in response to formation and downstream movement of vortices in the near wake. The change in airfoll lift force, and hence the radiated acoustic energy, could then be calculated from the circulation of each vortex. This circulation would depend on the frequency, which should be that for a constant Stroubal number referenced to the near-wake thickness. It was incorrectly assumed in Ref. 6 that the relevant thickness was the projected maximum thickness of the mirfoil. For this mirfoils having smooth pressure distributions, it is assumed herein that the thickness of a inminar boundary layer at the airfoll trailing edge should be used. The lift force would be caused by vortices in the near wake rather than by airfoll incidence. As can be seen from Fig. 3 of Pef. 7, the chordwise distribution of loading due to a vortex in the
near wake would be relatively constant along most of the chord and peaked mear the leading and trailing edges. In contrast, the loading caused by fluctuating incidence was shown in Ref. 7 to rescable that for steady incidence (sharply peaked near the leading edge and decaying smoothly to zero at the trailing edge).

If the pressure fluctuations on the similar caused by vortices located in the near wake, relatively little variation of β_{QQ} slong the chord would be expected except near the leasing and trailing edges. Also, the surface pressure fluctuations measured at low Reynolds numbers and described in a following portion of this report had relatively little variation along the instruments' whordwise region. The dominant portion of the measured FSD's was a discrete tone. Therefore the power spectral density of the surface pressure fluctuation at each symmise position was assumed to occur at only one frequency $f = \frac{\omega^2}{2^{-1}}$ and to be independent of chordwise position. Then, with

for a discrete tone and Z equal to r, Eq. (4) becomes

For a two-dimensional airfoll of span b, the correlation area and the surface pressure fluctuation (and its frequency) should be independent of spanwise position. Then

$$= \frac{1}{2} \left(\frac{2}{2} \right) \left(\frac{1}{2\omega} \right) \left(\frac{1}{2\omega} \right) \left(\frac{1}{2\omega} \right)$$
(7)

so the ratio of correlation area to planform area could be determined experimentally from the measured frequency and the measured pressure fluctuations on the surface and in the far field. Also, the correlation area for each surface microphone location could be measured by cross-correlation with the other surface microphones.

As shown in the next section, it is observer that vertex tone noise occurs when a laminar boundary layer is expected along most of one or both surfaces of an effoil. The thickness of a laminar boundary layer at the trailing edge would be approximately

where R is the Peynolds number based on airfoil chord. If the Strouhel number $f\delta/U$ is assumed constant when referenced to the laminar boundary layer thickness at the trailing edge.

where K_1 would be 1/60 if the Stroubal number were equal to 0.2 referenced to twice that thickness. The tone frequency therefore is predicted to vary with velocity to the 3/2 nover and to be inversely proportional to the square root of sirfoil chord.

The rate at which vorticity is convected within an attached boundary layer was shown in Vol. I, Section 22 of Ref. 8 to be $(1/2)^{1/2}$. It has been found for bluff bodies that approximately helf of the vorticity (Ref. 8, Vol. II, Section 244) is transported into the initividual eights that comprise the vortex strest endths remainder cancels itself or breaks down into turbulence. This rate at which vorticity is transformed

into vortex-street circulation, multiplied by the period of the fluctuation, must equal the circulation of each vortex.

$$\Gamma \cdot \left(\frac{\partial \Gamma}{\partial t}\right) \left(\frac{1}{t}\right) = \frac{K_{L} O'}{t}$$
(10)

The fluctuation of sirfoil lift force would be proportional to the circulation and sloo to the product of sirfoil chord and the chordwise-sverage surface pressure fluctuation. Therefore,

$$\mathcal{L} \Delta f_{RMS} = K_S \hat{f} \cup f' \tag{11}$$

Combining Eqs. (9), (10), and (11).

$$4T_{PPS} = 2K_{L}K_{S} \left(\frac{1}{2}\rho u^{S}\right) \left(\frac{fc}{u}\right)^{2}$$
(12)

or, in terms of Reynolds number,

$$a \cdot p_{Am_{3}} = \left(2 K_{L} K_{3} / K_{1}\right) \left(\frac{1}{2} \rho U^{2}\right) \tilde{\kappa}^{2}$$
(13)

The product of the two constants K_2 and K_3 can then be evaluated experimentally from measured surface pressure fluctuations and tone frequency. From Eq. (13), the ratio of average surface pressure fluctuation to free-stream dynamic pressure is expected to vary inversely with the square root of Mymolds number. In contrast, the surface pressure fluctuations caused by velocity fluctuations within a turbulent boundary layer, divided by dynamic pressure, are approximately constant (Ref. 1). The root mean-square pressure fluctuation at the surface is predicted to vary with velocity to the 1.5 power, while the method of Ref. 1 predicts e variation with velocity to the j.6 power. A variation with velocity squared would be expected for a bluff-body dipole process.

This prediction of surface pressure fluctuation from Eq. (12) can then be combined with Eq. (7) to determine the functional dependence of the far-field acoustic pressure fluctuation above a two-dimensional airfoil.

$$\overline{P}^{*} = \left[\left(\mathbb{I} < \mathbb{I}$$

Thus the far-field mean equate of the acoustic pressure is predicted to vary with velocity to the sixth power multiplied by the as yet unknown velocity dependence of the correlation area.

In summary, the pumerical constants for predicting the tone frequency and the surface pressure fluctuation can be determined from narrow-band surface pressure measurements. These can then be used for predicting surface spectra for other mirfolls.. Ratios of correlation area to planform area can be determined from the measured surface and far-field pressure coefficients. These ratios, whose values are difficult to anticipate for a deterministic process, should be approximately equal to those determine by the lengthler technique of cross-correlating the surface microphones. If the experimentally evaluated ratios can be generalized in terms of the ratio of near-wake laminar boundary layer thickness to airfoll chord, the far-field sound pressure level generated by an arbitrary mirfoll could then be predicted. The oversimplified analysis - would be verified if the assumed constants as determined from the data actually prore to be approximately independent of the experimental variables. A simple method for

predicting surface and fur-field spectra of arbitrary airfoils and three-dimensional rotating blades would then exist.

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DISCUSSION OF EXPERIMENTAL RESULTS

General Regimes of Noise Concration

One major result of this investigation was the finding that eirfoll vortex noise reaches a maximum intensity and then decreases with increasing velocity. As judged from acoustic spectra measured in the fas field at different velocities and angle of attack, three different regimes of noise behavior occurred. Approximate boundaries of these regimes are shown in Fig. 5 for the full-span NACA 0012 airfoll. At sufficiently low velocities and moderate angles of attack, the far-field acoustic spectra were dominated by a strong discrete tone. Vortex tone noise also was reported in Ref. 4 for small airfoll models at Reynolds numbers up to 0.75 x 10⁶. Broadband vortex noise with an intensity and center frequency predicted by the method of Ref. 1 was not observed.

At sufficiently large velocities and all but large angles of attack, the airfoil did not raise the far-field noise spectrum above-its background level. For this region, designated in Fig. 5 as "no tone", airfoil vortex noise appears to have decreased below that produced by the pressure fluctuations within the airfois turbulent boundary layer. In the intermediate regime, the intensity of the vortex tone noise decreased with increasing velocity at constant incidence.

The boundary between the regime of increasing tone strength and that for tone decay resembles another type of aerodynamic boundary. Judging from the data shown in Fig. 8 of Pef. 9, this curve also gives the minimum angle of attack for which the pressure-surface boundary layer on an NACA 0012 airfold remains laminar over the entire blade chord. Agreement between these aerodynamic and acoustic boundaries tends to confirm the physical mechanism described earlier for vortex tone noise. Every of tone Intensity with increasing velocity could then be associated with a rapid decrease in the chordwise extent of laminar flow.

The measured range of these three regions was not symmetrical about zero angle of attack for this nominally symmetrical NACA CO12 wirfoil model. Tones were observed for a considerably smaller range of Peynolds number when the model was tested at negative angles of attack. The model contained a slider that produced surface discontinuities at approximately 28 and 32 percent chord scrots the model span on one surface. At negative angles of attack relative to the wind tunnel, these discontinuities caused premature transition of the pressure-surface houndary layer. The model then was inverted in the wind tunnel so that the Slider was on the surface at negative angles of attack. For those tests, the boundaries shown in Fig. 5-for positive angles of attack were approximately reprediced at regative angles of attack. This result helps to describe that the measured vortex tone noise was caused by the attachil itself rather than by some unusual interaction between the airfoil, the wind tunnel, and the anechoic chamber.

The semisjon NACA OD12 wirfoil model has a smaller regime in which the tone increases with increasing velocity. The boundaries between the three regimes resembled those shown in Fig. 5 but were located at Reynolds maskers roughly 0.5 x 10^6 smaller at constant angle of attack. The presence of the wing tip vortex may cause earlier transition of the boundary layer. Only a small fraction of this model's span would have been unaffected by either the tip vortex or the sidewall turbulent boundary layer.

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High Neynolds Number

The test conditions that had seemed of greatest applicability to noise generation by helicopter rotor blades were those corresponding to outboard portions of full-scale blades. A convenient reference condition for calculation of rotor performance has been the 75 percent radius location. For typical light observation helicopters, the corresponding Reymolds numbers are near 2×10^5 and the relative Mach numbers near 0.40. Therefore, tests were conducted at a velocity of 450 fps which produced a Reymolds number of about 2.0 $\times 10^5$ and a Mach number of 7.41. At these conditions and small angles of attack, neither the full-span nor the semispan µACA 0012 model produced far-field noise greater than the tunnel background noine. They did produce measurable high-frequency broadband noise in the far field at large angles of attack. For the full-span model, this increased noise was observed at 8-deg angle of attack which is well below the 11-deg angle of attack expected for stall at this Mach number and Reymolds number.

Surface pressure spectra at different chordwise locations on the suction surface of the full-span model are shown in Fig. 6 for 0 and 8 deg angles of attack at 450 fps velocity. The spectra were assentially identical up to 1030 Hz. A broad-peak, not shown in Fig. 6, was produced by tunnel edge tones between 200 and 400 Hz. The surface pressure spectra shown in Fig. 6 have the general appearance expected for static pressure fluctuations associated with the velocity fluctuations of a turbulent boundary layer. This is most noticeable in the spectra measured 5 0 and 70 percent chord. Center frequencies of the measured broad peaks decreased with increasing streamwise distance (increasing boundary layer thickness), but the maximum asplitutes were approximately constant. Spectra measured further forward on the airfoil wolf be expected to have their peaks at frequencies, larger than the 20,00 Hz limit of the one-third-octave recorder.

The overall round pressure-level of the high-frequency portions of the spectra for zero angle of attack at 50 and 70 percent chord corresponded to a root mean square pressure fluctuation about 3.00% times the free-stream dynamic pressure. As can be shown from Pefs. 1. 3. 10, and 11, this value is close to but stashing telew that expected for tarbalent boundary layers in pill pressure gradients. The pressurements have not been corrected for the effect of a nonzero microphone diameter relative-to the expected correlation length of turbulent eidles in the boundary layer. This effect would probably raise the measurements to the expected level. As would be expected from Ref. 11, the chordwise correlation between prefiltered signals from the two ciorest surface microphones (10 and 18 percent chord) was small. A 1000-Hz highpess filter was utilized to remove the highly correlated signals at the tunnel fan and eige tone frequencies. Increasing the angle of attack increased the pressure fluctuations on the mirfois suction surface (Fig. 6). This result would be expected because of the increasing miverse pressure gradient. Surface pressure spectra measured on the scalepan model at small angles of attack were essentially identical to those for the full-span motel. Their amplitude increased less_rapidly_with increasing geometric angle of attack, probably because the effective angle of attack at the instrumented spanwike position would be about half the geometric angle of attack. Apparently the

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accountic radiation from mirfolls with evtensive turbulent boundary layers on both surfaces is approximately that caused by velocity fluctuations within the turbulent boundary layer. This radiation can be calculated by the method of Ref. 10. Its far-field intensity is small, not because the surface pressure fluctuations are small but-because the correlation lengths are of the oundary layer thickness, which is very small relative to the mirfoll chord and span. This result that the "inface pressure fluctuation spectra for an mirfoll at full-scale Reynolds numbers are "hose for a turbulent boundary layer and therefore-produce very small far-field mediation radiation was also determined in the smilplane flight texts reported in Pef. 12.

Low Reynolds Numbers

One-third-octave spectra taken in the far field generally contained one band that was much stronger than the background, along with the first harmonic of that band at 10 to 16 dB ameller amplitule. Shen analyzed at 10 Hz bantwidth, the apparent fuplamental tone usually appeared as one strong sharp tone and one or more weak nonbarmonic tones at nearby frequencies. The amount by which the weak tone protrules above the broadband noise usually was at least 5 dB below that of the strong tone. Typical 10 Hz spectra are shown in Fig. 7 for the full-span MACA 0012 airfoll over · small range of velocity of 6 deg angle of attack. The measured variation of farfield tone frequency with velocity for the full-spen SiCA 0012 sirfoil at 6 deg angle of attack is shown in Fig. 8. For small changes of velocity, the frequency of the strong tone and usually those of the very weak tones shown in the upper portion of Fig. 7 sociel approximately with velocity to the 0.8 power. With sufficient increase of velicity, one of the very weak tones at a larger frequency that the strongest true became considerably stronger than the others. At is shown in Figs. 7 and 8, this fore then became dominant, and the formerly strongert tone became vesker. The resulting restance of points, with quantum jumps of frequency in narrow ranges of velocity. julistively receptes the behavior of eige tone . However, there was no hypteresis of frequency with velocity for these tones. The same relative strength of toner was fruit whether a test condition was approached by increasing or decreasing the velocity. Decrive of these jumps of frequency, the general trend, as shown in Fig. C. was that of a variation with velocity to the 3/2 power. The comerical values of frequency at each velocity are predicted reasonably well by use of Eq. (9) with Ky arbitrarily taken equal to 1/90, as would occur if the trailing-edge boundary layer was 50 percent. thicker than that for a flat plate. These frequencies are in order of magnitude larger than those calculated for a Stroubal number of 9.2 referenced to the airfall maximum thickness (Fig. 8).

The jumps of frequency seemed to occur when an integer number of acoustic wavelengths was approximately equal to the chord. Delow about 190 fps, the wavelength was greater than the airfoll chord. Lets for this model at other angles of attack had roughly the same behavior. Tests of these closely spaced velocities were not conducted with the semispan RACA 0017 airfoll model, but its merrow-band tone frequencies generally matched those for the full-span model.

At the time this written paper was preparel, only limited surface pressure data had been obtained, a typical comparison of one-third-enter spectra in the far field and on the suction and pressure surfaces of the scalapan model is given in Fig. γ . On the pressure surface, where the boundary layer was laminar despite the pressure of

the slider as a surface discontinuity, the one-third-octave bands that contained the tone and its first harmonic were provinent. On the suction surface, the tone tend was only a week disturbance as compared with the broadband level of the transitional boundary layer at 30 and 50 percent chord. At 15 percent chord, upstream of the slider, the spectrum resembled that for the pressure surface. Sound pressure levels at the tone frequency, as determined from marrow-band spectra or these one-thirdoctave spectra, were approximately equal on both surfaces. They were approximately independent of chordwise position from 15 to 50 percent chord and generally were largest at 70 percent chord. In contrast, loslings gauged by fluctuations of incidence angle would have caused the sound pressure level at 15 percent chord to be about 3.5 dB stronger than that for 50 percent chord. Curface pressure fluctuations at velocities near 100 fps were about half as large for the semispen as for the full-span MACA 0012 airfoil. If the far-field tone was strong, these levels were roughly intependent of angle of attack. The effect of velocity on surface pressure fluctuations at the strong tone frequency for the full-span NACA 0012 mirfoll is shown in Fig. 10. The general level of these data is given by Eq. (12) with K, and Ny taken equal to 0.02 and Ny taken as 1/90. It is possible that improved agreement could be obtained at higher velocities if either by or Ky were not actually constant but variet with Reynolds number.

Grors-correlations at these low velocities led to the interesting result that the disturbance on the mirfoil appears to be propagating from the trailing edge toward the leading edge. A sample plot of the cross-correlation and auto-correlations of the 30 and 70 percent chord microphones is shown in Fig. 11. The cross-correlation function and the two auto-correlations are seen to vary nearly clausoidally with the delay time because of the discrete, deterministic character of the tone. The normalized erostcorrelation coefficient for this particular case had a magnitude of 1.3 chowing that there is mignificant correlation between the 30 and 70 percent microphone pre-same measurements.

The indication that a wave was moving from the trailing edge toward the leading odge becomes evident on examining the phase of the cross-correlation. It is observed that its first peak occurred at a time delay of about 2.5° milliseronic. The distance between the centers of the two microphones was 3.6 in, so that the predicted value of time delay based on the assumption of a count wave moving toward the leading edge and a sound spect of 1130 fps is 0.5° . milliseronic. The cross-correlation between the 3D and 5, percent chord microphones and shows, had a measured time delay of 0.10 milliceronics compared to a calculated value of 0.14 milliseronic. Civilar agreement between measured and calculated values of time delay was obtained from cross-correlations between the other microphones on the airfoil corface.

The time felay between arrival of a signal at an aft microphone and at the shirer microphone varied with spanwise position of the slifer. The corresponding spanwise correlation leasts have not yet been datermined. Correlation areas also can be formally computed from the measured narrow-band frequencies and the surface and farfield sound pressure levels by use of Eq. (12). When this was fore, the calculated correlation areas were a significant fraction of the planform area. It is possible that the pressure fluctuations actually are not relatively constant along the chord bot are highly pesked near the uninstrumented trailing else. If this were the care,

the correlation areas determined in this manner for those larger surface pressure areas would be much smaller. Tests with NACA COLS full-span airfoll model (Fig. 5), which has surface microphones from 5 to 80 percent chord, should be useful in determining the actual chordwise variation of fluctuating loading. They may also provide a better indication of whether the concept of correlation area is meaningful for this apparently deterministic measuric process.

COMPARISON WITH OTHER DATA

Not-wire investigations of the vortex shedding frequency of flat plates at low Erymolds rumbers were reported in Ref. 13. For thin plates relative to the boundary layer, the Strouhal number referenced to the effective displacement thickness of the mear wake was constant. The Strouhel number for an NACA 0012 sirfoil at zero angle of attack, referenced to the airfoil maximum thickness, also is given in Fig. 1 of Ref. 13. This quantity was found to be proportional to the square root of Reymoldsnumber, as is predicted by use of Eq. (6) berein. The frequencies reported for those hot-wire data measured on the wake centerline should be twice the acoustic frequency. As expicted, those frequencies were closely predicted by Eq. (9) with a numerical constant K₁ taken equal to twice the value of 1/90 used in calculating the solid line shown in Fig. 8.

Far-field acoustic spectra were given in Ref. 14 for an uncambered and a cambered-RACA 65 series mirfoil of 10 percent thickness ratio and 2-in, thord. Prequencies at which the peak intensities occurred were plotted in Figs. 14 and 15 of Ref. 14 for velocities from 200 to 500 fps (Reynolds numbers from roughly 0.2 x 10⁵ to 0.5 x 10⁶) and several angles of attack. These values are compared in Fig. 12 harein with the frequencies calculated from Eq. (9) with K_1 taken equal to 1/90. The predicted variation with velocity to the 3/2 power is in good agreement with the data. It is more easily justified then the linear variations taken from Ref. 14 and shown as wolid innes in Fig. 12, which would pass through zero frequency at about 100 fps velocity.

Far-field acoustic spectra and overall sound pressure levels for high aspect ratio wings of larger chord and span are given in Nef. 15. These data were obtained from low-altitude flybys of several saliplanes. A one-third-octave spectrum for the Libelle sailplane, taken from Fig. 66 of Net. 15, in reproduced in Fig. 13. The ametrum contains a broad tone centered in the 1000 Hz band caused by the satinlane wing and a tone in the 5000 Hz band described as background noise caused by crickets. It should be noted that the presence of a wing-generated tone at these large heynolds numbers (up to 3×10^5) is attributed to the airfoll sciulons used on the saliplanes. They are of types that wehleve low drag at their design conditions by maintaining a ling chordwise extent of laminar flow on the pressure surface. Tone frequencies calculated for the root and tip chords of this topered wing planform also were shown in this figure. The observed dominant frequency is about half a one-third-octave band higher than that calculated for the wing tip chord. In contrast, the frequency that corresponds to a Stroubal number of 0.2 referenced to wing maximum thickness is below 100 Hz, an order of magnil de smaller. By use of Eq. (9), the observed frequency of 1000 Hz for 10% fps velocity and 25 in. meen chord would scale to roughly 9000 Hz for 1% for velocity and 2 in, chord. This scaled frequency is in good agreement with the data of Fer. 15 for sinfails with 2 in. chord as shown in Fig. 12 herein. Thus the predicted variation of frequency with the inverse square root of chord is verified for an order of magnitude change in chord.

DESCRIPTICA OF REMAINING EFFORT

During the remainder of this investigation, we plan to (1) conduct additional measurements of surface pressure spectra and cross-correlations for the full-span NAC4 0012 airfoil to determine the acoustic phenomena at wavelengths less than the chord length, (2) conduct limited tests with the full-span NAC4 0018 airfoil to determine the qualitative effect of airfoil thickness ratio and obtain surface pressure data over a larger percentage of the chord, and (3) compare sound pressure levels calculated by any prediction method developed from these tests with data-for smallscale (Ref. 1%) and full-scale (Ref. 15) configurations.

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LIST OF SWEELS

- Speed of sound, ft/see
- b Span, ft
- e Cherd, ft
- f Frequency, hz
- K1,K2,K3 Empirical constants
- P Acoustic pressure in far field above airfoil, 1b/ft²
- Q Pressure jump across airfoil surface, 15/ft2
- r Distance above airfoil in far fiell, ft
- roir1 Position on airfoil surface A, ft
- R Reynolds number, equal to Uc/~
- Sc Correlation area, ft²
- Spp Power spectral density of far-field pressure fluctuation, 1b2/ft4sec
- S_{QQ} . Power spectral density of surface loading fluctuation, $1b^2/rc^4 zec$
- $S_{Q_0}Q_1$ Cross power spectral density of losiing fluctuations at two points on the airfoil surface, $1b^2/fz^4$ sec
- t Time, sec
- U Free stream velocity, ft/ser
- x,y,z Cartesian coordinates in the streamwise, spanwise, and normal directions, ft
- I' Circulation:of an individual vortex, ft²/sec
- b Boundary layer thickness of trailing eige, ft
- $\Delta f_{\rm RMS}^{\prime}$. Root mean square pressure fluctuation on airfoil surface, 1b/ft²
- V Kinematic viscosity, ft²/sec
- P Density, slugs/ft3
- W Frequency, rat/sec

Superipts

- 0,1 Coordinate on airfoil surface
- _____ Vector quantity

Superscripts

- Mean value
- Complex conjugate



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ACOUSTIC TUNNEL TEST SECTION

FIG. 2

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REGIMES IN WHICH DISCRETE TONE VORTEX NOISE OCCURS

FULL-SPAN HACA 0012 AIRPOIL SLIDER ON SUCTION SURFACE SYMBOLS REPRESENT TEST POINTS



FIG. 6

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FIG. 5

SURFACE PRESSURE SPECTRA AT REYNOLDS NUMBER - 2X304

MACA 6612 FULL-SPAM AIRFON, SUCTION SURFACE VELOCITY - 450 PPS





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FAR-FIELD AND SURFACE ONE-THIRD-OCTAVE SPECTRA IN STRONG TONE-REGIME





FREQUENCY, He

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FIG. 10

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FIG. 11 TYPICAL CROSSCORRELATION AND AUTOCORRELATIONS IN STRONG TONE REGIME

INCROPHONES AT 30% AND 74% CHORD OF NACA 0012 FULL-SPAN WODEL





FIG.12

COMPARISON OF MEASURED AND CALCULATED FREQUENCIES FOR AIRFOILS WITH 2-W- CHORD

DATA AND SOLID LINE FAIRINGS FROM REF. 14







ONE-THIRD-OCTAVE SPECTRUM OF LIBELLE SAILPLANE FLYBY

10 FT ALTITUDE AT 304 FT/SEC VELOCITY

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H. Kevin Johnson and Walter M. Katz

ROCHESTER APPLIED SCIENCE ASSOCIATES, INC. 140 Allens Creek Road Rochester, New York

ABSTRACT

Karmán-street type vortex shedding #rom a lifting surface was analyzed as .. source of noise from a helicopter rotor in hover. The theoretical program that was conducted used acoustic pressure-time histories measured by NASA at the Wallops Island Test Station for a UH-1B helicopter in hover and forward flight.

The experimental pressure-time histories were analyzed and high resolution spectra were developed over a frequency range of 0 to 5000 Hz using a 0.7 Hz filter. On the basis of these spectra the main and tail rotor rotational moise as well as discrete noise sources were identified and then removed from the measured pressuretime histories leaving pressure-time histories representing only the broadband noise radiated from the rotor system. This broadband noise was then related to-the noise induced by Kármán-vortex street shedding on the rotor blade.

The theoretical analysis-that was developed-related the acoustic radiation of the vortex shedding forces on the blade to the pressure-time histories measured by the sicrophones located in the far field. This analysis was then used to solve for the oscillatory forces on the blade that would duplicate the proadband noise characteristics of measured pressure-time histories of the helicopter in various flight regimes.

The results of the investigation indicated that "vortex noise" is the major source of accustic radiation from a helicopter rotor in hover or low-speed flight and that it is concentrated in the frequency range of 200 to 500 Hz. Because of the excellent correlation obtained between measured and predicted acoustic signatures using the averaged nondimensional force constants for vortex shedding extracted from the data-analysis, it is believed that the basis of a realistic pathod of predicting the total acoustic signature of any helicopter rotor in various flight regimes has been developed and demonstrated.

INTRODUCTION

The primary contributor to the external sound of modern graturbine powered helicopters in the aerodynamically induced noise from the rotor system. Noise measurements have shown that the Acoustic pressure time-history at an observer's location is due Almost entirely to the noise output of main and tail rotor systems.

This study was supported by the Eustis Directorate, U. S. Army Air Mobility Research & Development Laboratory, Fort Eustis, Virginia, under Contract DAJJ02-70-C-0023. This means that the helicopter's detectability and to a large extent its effectiveness as a weapons system is determined by the noise signature of its rotor system. In addition, because of the strong emphasis today in noise pollution control there has been interest in rotor noise with regard to commercial helicopter operations. For these reasons, aerodynamically induced sound from rotor systems has been extensively investigated, particularly in the last five years. (See References 1, 2, 3, 4, and 5.)

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Rotor noise consists of two basic types of sound signatures: one is repetitive in frequency, the other is broadband or nonrepetitive. The repetitive noise is typically called "rotaticnal" noise in which the frequencies are integral multiples of the rotorblade passage frequency. The broadband or non-repetitive-type noise can be generally classified as "vortex" noise. In addition, there are other-helicopter noise classifications such as "blade slap", and sources such as engine and transmission noise. These other noises and sources are not treated explicitly in thiz report. (See Reference 5 for a discussion of rotor noise sources.)

Rotational noise is typically regarded as a dominant sotor noise source (see Lowson, Reference 5). For this reason it is not surprising that many-investigators have concentrated in this area of acoustic research. Results have shown that whereas rotational noise is dominant in all cases for frequencies below 100 Hz, above 100 Hz, rotational noise may dominate but in most cases broadhand noise will mask out the rotational noise. It has been found, however, that the noise source that is predominant is dependent upon the location of the noise source relative to the observer.

Since in general broadband noise will be nonperiodic with respect to blade passage frequency, such noise is often classified as nonrotational. The broadband noise that is associated with helicopter rotor blades is usually related to vortex shedding that occurs along the blade. Since vortex-generated noise is believed to occur in the frequency range closer to that of maxinum human ear sensitivity, the subjective loudness of such noise can be greater than that of low frequency rotor rotational noise. even though the latter may be of higher absolute magnitude.

Little is known about vortex street shedding .ron lifting surfaces. Vortex shedding noise from rotating cylindrical bodies was first measured by Stowell and Deminy (6). Later Yudin (7) and Blokhintsev (8) developed theories medicting such noise. Hubbard (9) has reported overall noise levels due to all sources on propeller blades, and has given an estimate of noise due to vortex shedding. He found for propellers that the rotational and vortex components can be of the same order of magnitude. He noted that the vortex component has a higher frequency content than the entational component and increases in intensity with increasing tip speed. Schlegel, et al (3) have made further refinements in Hubbard's vortex noise magnitude formula. Krzywoblocki (10) has measured the vortex shedding frequency for airfolls at low Reynolds numbers: however, the data for angles of attack below stall had wide scatter. Poshko (11) reasured the frequency of shedding from circular cylinders in high Reynolds number flow,

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ANALYSIS OF KANNAN-STREET-VORTEX SHEDDING USING MEASURED HELICOPTER SOUND PRESSURE DATA

but not for airfoil-type sections.

To summarize the experimental work to date, it is noted that measurements have been made of the frequency of vortex shedding, but not within the range of flow conditions encountered by helicopter rotor blades. Nowever, to date no measurements have been made within any range of flow conditions of the magnitude of the oscillating lift and drag forces due to vortex shedding. It is, therefore, necessary that the basic characteristics of vortex shedding from airfoils should be documented in order to develop a better understanding of their effects on rotor noise. Empirical or semi-empirical constants will, therefore, have to be used to investigate the relative importance of vortex shedding on the noise characteristics of helicopter rotors until the time that suitable measurements are obtained.

Sadier and Loewy (2) have determined, by semi-empirical means, overall constants for the lift and drag forces associated with discrete vortex shedding. In this case the constants were assumed to be independent of Mach number, angle of attack, blade radius, and azimuth. It is, however, believed that these force constants are not entirely independent of the aforementioned parameters.

The program reported on hereir was set up so that the lift and drag force constants might be developed from experimental data. For the mathematical model the helicopter rotor blade was represented acoustically by a series of dipoles whose strength and frequency varied radially in the case of hover, or both radially and azimuthally in the case of hover, or both radially and azimuthally in the case of forward flight. If the local angle of attack and Mach number are known at a blade element, then based upon Strouhal number the frequency of vortex shedding could be precalculated. Since there is a known relationship between dipole strength at a given point in space and acoustic pressure at another point, it was possible in this program to use experimental pressure-time histories measured at a fixed observer's location to determine the Vortex constants that produced the nonharmonic (broadband) characteristics of the measured signature.

The purpose of the program discussed herein was, therefore, to determine the characteristics of the vortex shedding forces on a helicopter rotor blade in hover-and forward flight. A more complete bresentation is contained in Reference 12.

ANALYSIS OF EXPERIMENTAL DATA

TEST PROGRAM

No. St

The data used in the analysis was generated during controlled acoustic tests of an UH-1B helicopter conducted during November 1969 at Wallops Island, Virginia (13). This data has been discussed by Evans and Nettles (13).

The noise tests were conducted by the Army at the Wallops Island Air Station with cooperation of the Dynamic Loads Division of the NASA/Langley Research Center. The test area consisted of an array of microphones in the form of a cross. This is shown in Figure 1. As shown, the positive X-axis is in the direction of flight and microphones 1, 2, 3 are at X = 200, 500 and 700 feet; microphones 7, 8, and 9 are at X = 200, - 500, and - 700 feet; microphones 4, 5, 6 are to the right of the flight path at Y = -200, - 500, - 700 feet; microphones 10, 11, 12 are to the left of the flight path at Y = 200, 500, 700 feet; and microphone 13 is at X = Y = 0. A local coordinate system centered at the main rotor hub moves with the helicopter and is shown in Figure 2. A variety of test conditions were covered during the test program including low, medium and high-speed forward flight and two hover flight conditions (6 feet and 100 feet).

GROUND REFLECTION EFFECT

The importance of ground reflection in the data is revealed by comparing spectra for different microphone-helicopter orientations, see Figures 8 and 3, which represent extended spectra at positions 4 and 6 for the 100 ft hover condition. Observe that the general characteristic of each spectrum in the broadband region reveals a series of maxima and minima separated throughout the second by equal frequency inservals. However, it is seen that this frequency interval is not the same for both recording positions. The frequency interval between successive maxime or minime on the records is seen to change as the orientation between source and observer changes. It should be noted that for a given microphone height above the ground, the microphone receives one signal directly from the sound source and another that is reflected-from the ground and then received. It can be shown that the frequency interval referred to between successive peaks or valleys on the SPL records is related to this time senaration between original and reflected signal. Thus the frequency spectrum received by an observer is distorted from that of the source, some frequencies will be amplified by reflection while others are suppressed.

The reflected signal time lag at position 6 is less than that of position 4 because the increase in distance travelled by a reflected wave received at position 6 is less than the increase in distance travelled by a reflected wave received at position 4. That is, the increase in distance travelled by a reflected wave at position 6 is 1.48 ft while the increase in distance travelled by a reflected wave at position 4 is 4.65 ft. Therefore, the time lay for a sound-wave at position 6 is 1.34×10^{-3} sec (745 Hz) while the time lag for position 4 is 4.22×10^{-3} sec (237 Hz). The maxima or reinforced frequencies would, therefore, correspond to integral multiples of this frequency and the minima or cancelled frequencies correspond to (n + 1/2)f. The first minimum frequency at position 5-is 373 Hz and the first and second minima at position 4 is 118 Hz and 356 Hz, respectively (see Figures 8, 3). These frequencies are consistent with the predicted minima (372.5 Hz for position 6 and 118.5 Hz-and 355.5 Hz-for position 4). DIGITIZATION

In order to perform computer analysis of the acoustic data the pressure-time history had to be converted into digital form so as to be compatible with computer input format. This process is called digitization. The original FN recordings were digitized using a high-resolution electronic conversion technique specially developed by RASA for carrying out this work. By coupling a mini-computer with special circuitry, a 1.45-second record could be digitized at an 11.3 KMS rate providing approximately 16000 data points. The resulting frequency response of the digitized

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data extended from about 0.7 Hz to 5650 Hz, which exceeded the range of the recording system of 20 Hz to 5000 Hz. The signalto-noise ratio of the developed system was noted to be excellent, at better than 45 db.

To demonstrate the accuracy of this digitization the digitized data was plotted and compared with the corresponding oscillograph records, see Figure 4. The digitized data-is seen to be in excellent agreement with the oscillograph trace. In fact, if differences do exist, the electronically digitized results should be considered the more reliable for two reasons. First, the conversion was done directly off the FM carrier of the recorded signal. This technique bypasses the FM demodulator unit, which in itself introduces some distortion to the output. In addition, the electronically digitized data bypasses the frequency response of the oscillograph galvanometers, which were flat to only about 3KC.

EVALUATION OF VORTEX GENERATED HOISE

Since the shedding of Kármán-type vortices off an airfoil causes variation of lift and drag on the airfoil surfaces, the resulting oscillatory force on the airfoil will create noise. A variety of empirical t chniques exist for estimating the magnitude of noise caused by shed vortices from rotating wings. (See References 2, 3 and 9.) The analysis carried out under this program determined the magnitude of these oscillatory forces from the measured pressure-time history of the recorded sound.

The RASA electronically digitized pressure-time histories were separated-into '-sadband and discrete components using *pectral analysis techniques. The broadband pressure-time history was then used in a computer program which determined the oscillatory force on the sirfoil that created the peasured signal. Because of the importance of the value of the Strouhal number used in the calculations and because the Strouhal number has not been accurately measured, particularly for airfoil sections, the fitting technique used to determine the oscillatory forces was also used to determine the "best" Strouhal number.

The data used in this program was only sufficient to determine the contribution of each-airfoil-section to the prossure-time history. The data was not sufficient to evaluate the relative contribution of both lift and drag. Since it has been estimated that the oscillatory drag forces are very small compared to the oscillatory lift forces as regards the acoustic signal, the contribution from each station was assumed to result only from the oscillatory lift.

THE VORTEX SHEDDING MODEL

The vortex-streat phenomenon requires a upparated waku caused by the viscous offects in the boundary layer. While airfoil design minimized this separation effect, it did not eliminate it. On a physical basis, the wake formed from a separated boundary layer will be influenced by its width at the separation point and the flow conditions. The Stroubal number correlates the frequency of shedding for various bodies. For cylinders, the Eliminal number changes with Reynolds number and is not known for airfoils or cylinders at large Reynolds number. The Strouhal number is not a universal constant but is dependent on body geometry as well as Reynolds number. The results of References 3, 10, 14, 15 are consistent with a Strouhal number in the range of 0.11 to 0.2 for streamlined bodies. This renge is only approximate, but will be used as a guide until tests can determine the existence of Strouhal-type shedding from airfoils and the proper range and dependencies of the Strouhal number on the controlling parameters.

In the present analysis, the Stroubal number for airfoil vortex shedding will be allowed to vary within the range $0.1 \stackrel{<}{=} S_{\rm t}$ = 0.3, which exceeds the limits defined previously. The Stroubal number will be considered constant, however, along the blade for each calculation, that is, the Stroubal number will not be allowed to vary with blade velocity and/or angle of attack. It is anticipated that the Stroubal number is dependent on these parameters, but in lieu of this knowledge, the approach used is believed to be reasonable. Thus, the vortex street shedding frequency is assumed to be:

where us vortex shedding frequency (Hz)

- U-= resultant velocity (ft/sec)
 - d = projected dimension of the body perpendicular to the resultant velocity (ft)

and $S_{\pm} =$ Strouhal number: $0.1 \stackrel{<}{=} S_{\pm} \stackrel{<}{=} 0.3$

Effects of vortex shedding on the two-dimensional lift and drag forces acting on the airfoll can be investigated by considering the circulation around the appropriate airfoll section. Assuming regular shedding of vortices of alternating sign, an oscillatory circulation may be considered to be superimposed upon the stordy circulation. The corresponding lift and drag forces acting c...the airfoll section will then orgillate about a mean value of lift and drag. The oscillatory lift and drag due to vortex shedding can, therefore, be formulated as

$$(L_{\nu})_{ij}(t) = (K_{L\nu})_{ij} \{ [1/2 \circ U_{ij}^{2}] C_{1} \pi i \} \sin (u_{ij}t + z_{ij})$$

$$(D_{\nu})_{ij}(t) = (K_{D\nu})_{ij} \{ [1/2 \circ U_{ij}^{2}] C_{1} \pi i \} \sin (u_{ij}t + u_{ij})$$

$$(2)$$

where $(K_{LV})_{ij}$ = nondimensional force constant associated with oscillatory lift

- # -- density of air
- U₁₁ = relative velocity of the airfoll
- C_i = chordleanth
- /r, = station width
- "is " frequency of vortex shedding
- "ii = phrse of the vortex forces

The noise source treated are those generated aerodynamically from heliropter rotors. It is assumed that helicopter rotor-noise is produced by variable forces on the rotor blades, not finid mass displacement by the blades nor flow turbulence. It is, therefore, reasonable to use dipoles so represent these blade forces (see References 5 and 16). The pressure received at an observer's location from an array of moving dipoles can be cast in the following form (see Reference 5):

$$\hat{x}_{0,t} = \sum_{i,j} \left[\frac{1}{4\pi c R_{ij}^{2} \left[1 - H_{R_{ij}} \right]^{2}} \left\{ \hat{r}_{ij} \cdot \hat{v}_{ij} - (\hat{x}_{0} - \hat{x}_{ij}) \cdot \left[\hat{r}_{ij} + \frac{\hat{r}_{ij}}{\left(1 - H_{R_{ij}} \right)} \left[\hat{H}_{R_{ij}} + \frac{c}{R_{ij}} \left[1 - H_{ij}^{2} \right] \right] \right] \right]_{t}$$

where $[1]_{t}$ = graduation of those quantities inside the brackets

are at-a "rotarded time" t' corresponding to a real -time t

c = speed of sound

 \hat{X}_0 = location of the observer

$$R_{ij} = \left[(\vec{x}_0 - \vec{x}_{ij}) \cdot (\vec{x}_0 - \vec{x}_{ij}) \right]^{1/2}$$

$$R_{ij} = \frac{(\vec{x}_0 - \vec{x}_{ij}) \cdot \vec{n}_{ij}}{R_{ij}}$$

$$R_{ij} = \frac{(\vec{x}_0 - \vec{x}_{ij}) \cdot \vec{n}_{ij}}{R_{ij}}$$

$$\vec{n}_{ij} = \frac{v_{ij}}{c}$$

Fij = force on the blade at blade element

With terms comprising Equation (3) formulated, the pressure at an observer's location may be specified once the appropriate sources have been located in retarded time. The acoustic signature of the rotor is assumed to imanato from a series of dipoles located at blade stations. The sound reaching a microphone at some instant in time, t, originates from each of these stations at some earlier time, t'. The time that the sound originated from each station (retarded time) is a function of the position of each station and its motion and is in general different for each station. A retarded time calculation procedure has been programmed for computer use. The program developed locates for an observer's location at time t, the contributing retarded time position of each radial blade station. The results of a typical retarded time calculation is shown in graphical form in Figure 5. As can be seen, the rotor disk has been broken up into 40 azimuthal Sections and 10 radial sections and that the azimuthal spacing in retarded time is not equal as it would be in true time. The difference in the spacing between the advancing blade (observer on the negative y-axis) and the retreating blade is very upvious in this graphical presentation.

HOVER ANALYSIS

For this analysis, the UH-1B helicopter was in the hover configuration 100 ft over the microphone data cross with helicopter orientation along the flight path. The data received was recorded at microphone 4 which was 200 ft to the right of the flight path. DETERMINATION OF ANGLES OF ATTACK, RESULTANT VELOCITIES, SHEDDING PARQUENCIES

The Strouhal shedding frequency of the UH-ID mirfoil (NACA 0012) was assumed to be proportional to the flow velocity and inversely proportioned to the separation thickness of the flow. This flow separation has been assumed to be equal to the projected dimension, d, of the airfoil perpendicular to the resultant velocity U. The dependence of the projected dimension as function of angle of attack for the NACA_0012 blade is shown in Figure 6. NUMBERICAL TECHNIQUE

Measured pressures can now be related to the oscillatory force constants. The objective is to solve for the unknown oscillatory force constants in terms of the measured pressure-time history. For the hover configuration, the values of the oscillatory forces are assumed constant about the rotor disk, since angle of attack and velocity are similarly assumed to be constant. The geometric parameters, however, change considerably with respect to an observer so it is desirable to segment the time for each blade passage into smaller time intervals. If the time intervals are small enough, the geometric parameters are essentially constant during the interval.

If the geometric parameters can be assumed constant in a small interval of time then the predictive equations can be linearized. When possible such a linearization of a set of equations greatly reduces the numerical difficulties of their solution. The time interval chosen constrains the frequency range and number of oscillatory stations such in the same way that length of record is related to bandwidth. The largest time interval that was felt consistent with constant geometric parameters was 1/200 sec. For example, if the time for one blade passage is divided into 20 equal time intervals (the blade passage frequency is 10.8 Hz), cach time interval is approximately 1/200 sec. Thus, phenomena which change with frequency less than 200 Hz cannot be considered. This cutoff is a judicious compromise between frequency range and blade element-station size. That is, if a smaller time interval were chosen, the area swept by the blade (the station size) would be smaller but the lower frequency cutoff would increase Conversely, if a larger time interval were chosen the lower frequency cutoff would decrease, but the area swept by the blade would increase tending to invalidate this discrete element analysis.

The time intervals when one blade advances toward the observer while the other blade retreats-is particularly advantageous.

The Strouhal frequency formulation is such that the shedding frequency increases with radius. Recause of the Doppler effect the observed frequencies are increased further on the advancing blade while decreased on the retreating blade. This is coupled to the Nach number effect in Equation (3) which increases the pressure amplitude of the advancing blade stations through the terms $1/1-H_R$ and decreases the pressure amplitude of the retreating blade stations (H_R is negative for a retreating blade, positive for an advancing blade).

The larger frequency spread on the advancing blade allows a larger number of blade elements with observer frequency separations above >200 Hz. On the retreating blade the Doppler effect works in reverse and decreases the observed frequencies. The net-result is that for the observer frequencies above 500 Hz the section of the sirfoil from midspan to the tip of the advancing UN-1B blade contributes while below 500 Hz the inboard half of ANALYSIS OF KANNAN-STREET VORTEX SHEDDING USING MEASURED HELICOPTER SOUND PRESSURE DATA

the advancing blade and the whole retreating blade contribute. SOLUTION TECHNIQUE

A REAL PROPERTY AND A REAL

In order to solve for the magnitude of the oscillatory forces on the helicopter blade several assumptions have been made. The following list is a review of the assumptions used in this analysis.

- The oscillatory forces on an airfoil occur at the frequancies associated with Strouhal shedding.
- The Strouhal number is assumed to be independent of Reynolds number.
- The oscillatory forces are sinusoidal and have components only in the lift and drag direction.
- The oscillatory forces on the blade can be represented by oscillatory dipoles acting at the center of ten spanwise stations.
- For each small increment of time (%0.005 seconds) the aerodynamic and geometric parameters at each of the ten spanwise regions remains essentially constant.
- 6. In the time intervals when one blade advances toward the observer while the opposite blade retreats the noise at the observer for frequencies above 500 Hz is assumed to originate from the advancing blade above.

Using these assumptions the pressure-time history at an observer for A blade in the advarcing region is:

$$P(t) = \int_{1-2}^{1-2} \left\{ (K_{Lv})_i [(\lambda_L)_i \sin (\omega_i \tau_i + \sigma_i) + (B_L)_i \cos (\omega_i \tau_i + \sigma_i) \right\}$$

+
$$(K_{DV})_{i}[(\lambda_{D})_{i} \sin (\omega_{i}\tau_{i} + s_{i}) + (B_{D})_{i} \cos (\omega_{i}\tau_{i} + s_{i})]$$

(4)

where ri is the retarded time

 $\omega_{\rm f}$ is the Stroubal shedding frequency

 v_1 is the phase of the shedding

 $(A_L)_i$, $(B_L)_i$, $(A_D)_i$ and $(B_D)_i$ are the geometric coefficients predicted by the moving, oscillatory dipole theory.

The assumption that the aerodynamic and geometric parameters remain constant in a 0.005 second time slice is now applied. The term $\omega_i \tau_i$ is replaced by w't where w'_i is the Doppler shifted frequency at the observer's location. Equation (4) then becomes for each blade

$$P(t) = \sum_{i=1}^{10} (K_{5})_{i} \sin (\omega_{i}^{2} t + v_{i}) + (K_{c})_{i} \cos (\omega_{i}^{2} t + v_{i})$$
(5)

where
$$(\pi_{g})_{i} = (\kappa_{L})_{i} (\lambda_{L})_{i} + (\kappa_{D})_{i} (\lambda_{D})_{i}$$

 $(\kappa_{C})_{i} = (\kappa_{L})_{i} (B_{L})_{i} + (\kappa_{D})_{i} (B_{D})_{j}$

The exact time-interval chosen to solve for the excitiatory forces was 0.0046 seconds. The rate at which the data was electronically digitized was 11.3 KHz. Therefore, there are 52 measured values of the recorded pressure in each 0.0046-second time interval. Linearizing Equation (5) by removing the arbitrary phase gives

$$P(t_{i}) = \int_{1}^{10} \left[(K_{j}^{*})_{j} \sin (w_{1}^{*}t_{j}) + (K_{c}^{*})_{j} \cos (w_{1}^{*}t_{i}) \right]$$

$$t = 1, \dots, 52$$

where $f(K_{\pm}^{i})_{\pm}^{2} + (K_{c}^{i})_{\pm}^{2} = f(K_{\pm}^{2})_{\pm} + (K_{c})_{\pm}^{2} = K_{\pm}$

and K_{i} is the total magnitude of the oscillatory force constants. Since there are 20 unknowns in Equation (6) ten $(K_{g})_{i}$ and ten $(K_{c})_{i}$ and 52 equations the problem is overdetermined. The solution was determined using the standard least squares techniques for a set 0 linear equations.

OBTAINING EXPERIMENTAL MAIN ROTOR VORTEX NOISE

The acoustical pressure-time history recorded-at the microphone position is assumed to be a linear supposition of many sources of noise. Among these sources are:

- 1. engine noise
- 2. engine exhaust noise
- 3. main and tail rotor year box noise
- 4. tail rotor rotational noise
- 5. main rotor rotational noise
- 6. Main rotor vortex noise
- 7. tail rotor vortex noise

Since the analyses that were performed herein are associated with only main rotor vortex noise, item (6), all the other sources of noise in the measured pressure-time historics had to be removed in order to obtain the desired pressure-time history.

In the model developed in this contract, the noise associated with rotor blade vortex shedding is assumed to be generated at discrete frequencies defined by a Stroubal formulation. Those shedding frequencies are determined by the airfoils-chord, thickness, angle of attack and velocity. Shedding frequencies, while in part determined by rotor rotational speed are not integral harmonics of the rotor rotational frequency. In addition, since the blade is moving and continually changing direction, the Doppler shift on these frequencies also continually changes. This differs from items 1. 2. 3. 4. and 5 of the listed sources of noise which are observed at discrete frequencies. This is clearly illustrated in Figure 8, the spectrum of measured helicopter rotor noise for the hover flight condition. It can be seen that the rotor rotational noise appears at discrete multiples of the blade-passage-frequency (10.8-Hz) and the full rotational noise occurs at multiples of its blade passage frequency (55.1 Hz). The peaks at 1922 Hz and 2100 Hz are identified with the tailrotor gear clash frequencies of the 42-degree and 90-degree (second harmonic) gears.

In the data shown in Figure 8 the rotational and distrete noise peaks are sufficiently-narrow so that-they can be removed without-significantly-changing the content of the underlying broadband noise. Once the discrete noise perts are-identified their corresponding Fourier coefficients as determined from the Fast Fourier Transform of the digitized data, are set equal to zero. The broadband pressure-time history is then gonerated by using the inverse Fourier transform.

In order to correlate the measured providentiate history with the theory, the azimuthal blade position must be known. The Wallops Island test did not record this important piece of information. The azimuthal location of the rotor was determined ANALYSIS OF KARMAN-STREET VORTEX SHEDDING USING MEASURED HELICOPTER SOUND PRESSURE DATA

by matching the measured rotation noise signature with a theoretically predicted rotational noise pressure-time history. <u>RESULTS OF THE THEORETICAL ANALYSIS</u>

A total of four hover cases were analyzed. Three of these cases were from position 4 (200 feet to the right of the helicopter) and one from position 6 (700 feet to the right of the helicopter). The radial stations selected were:

 r_{i} = 7, 9, 11, 13, 15, 17, 18.5, 19.5. 20.5 and 21.5 ft. for i=1 to 10 respectively. The electronically digitized records are ~1.5 seconds long. Therefore, 15 blade passages were analyzed for each of the cases.

The set of equations solved had more equations (52) than unknowns (20). By using the method of least squares the resulting deviation is a measure of the equality of the solution. Since the Strouhal number is not accurately known for airfoils at these Reynolds numbers, a search was performed to determine the Strouhal number which gave the most satisfactory solutions. The optional Strouhal number was determined to be 0.235:.02 which is within the range for which results have been obtained by previous investigations.

One of the recordings obtained 200 ft to the right was used to evaluate the method of removing discrete rotational noise sources. The portion of the recording used was 35 seconds into the recorded signal. For the first of the four cases (to be referred to as Case A) all-noise below 140 Hz, the tail rotor peaks at 165 Hz and 220 Hz; and all noise above 1860 Hz was removed. In Case B all noise above 2820 %z was removed (instead of above 1960 Hz as in Case Al together with the gear clash spikes at around 1930 Hz and 2140 Hz. In order to determine how much the results were dependent on when in time the data was analyzed, another portion of the data taken 200 ft to the right and 26 seconds into the recording was analyzed. This condition is referred to as-Case C. The electronically digitized pressuretime history and spectrum for this case are shown in Figures.7 and 5 respectively. The rotational and discrate noise was recoved by setting the following coefficients of the Fourier representation of the digitized record equal to zero: «140 Hz, 165 Hz, 220 Hz, 1930 Hz, 2140 Hz, and >2820-Hz. Figure 9 presents the spectrum of the noise that was removed and Figure 10 presents the spectrum of the vortex noise that was analyzed for this case. The pressure-time history of the rotational noise is shown in Figure 11 and of the vortex noise in Figure 12. The fourth case that was analyzed (Case D) was data peasured 700 feet to the right of the helicopter. A portion of the recording 26 seconds into the record was analyzed. In this position the gear clash frequencies occur at 1930 Hz and 1990 Hz. The frequency components removed were «140 Hz, 165 Hz, 220 Hz, 276 Hz, 330 Hz, 385 Hz, 1930 Hz, -1990 Hz, and >2820 Hz.

The analyses that were carried out used 15 blade passages of digitized date. Because of the previously noted inability to separate the lift and drag components and because it has been shown elsewhere that the drag contribution is insignificant compared to the lift distribution, the $(K_D)_{i,S}$ were assumed zero in

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all of the analyses that were conducted. Therefore, only $(K_{\underline{L}})_{\underline{i}}$'s were calculated for the 15 blade passages in each case. For each radial station, the distribution of these $(R_{\underline{i}})_{\underline{i}}$ values multiplied by that station's dynamic pressure is shown in Figure 13. The $(K_{f_i})_i (1/2_0 U_i^2)$ for the ten radial stations for each of the four cases are tabulated (Table I) and plotted in Figure 14. Although there is some scatter in each of the distributions the mean results are remarkably similar for all four cases. The comparison of Case A and Case B shows that the results are fairly insensitive to variations in the high frequency cutoff in the data, although the magnitudes of station 10 for Case A are somewhat suppressed from Case B. Going to a different position of the record also does not significantly alter the distributions (see distributions for Case C). Some of the distributions for position 6. (Case D) however, do differ from the first three cases. This is due, in part, to the differences in ground reflection. The magnitudes of the oscillatory pressures are ~ 1 to 2 $1b/ft^2$ for the tip 1/3 of the blade (14-22 ft). On the inboard stations (6-14 ft) the magnitude of the oscillatory pressure ranges from 4 to-30 lb/ft². It must be remembered, however, that these stations include significant contributions from the retreating blade whereas the outboard blade sections do not. For each of the four cases that were analyzed, the calculated oscillatory forces were used in a theoretical program to determine if the essential noise characteristics had been retained. For each of the cases, therefore, a pressure-time history and a corresponding spectral analysis were predicted for comparison with the experimental data. The predicted pressuretime history and the corresponding spectrum for Case C are shown in Figures 15 and 16 respectively. When these prodicted results are compared with the measured results in Figures 12 and 10, it

TABLE I. MACHITURES OF THE OSCILLATORT LIFT FORTES AS A FUNCTION OF PARALL POSITION FOR EACH OF THE FOR CASE									
Station Padius	Angle of Attack	Not's Kather	Shelding Frequency	Oscillatory Pressate []b/ft2]					
_((1)	[6+1]		[V1]	CALO A	Case 3	Case C.	Ca20 D		
7.3	5.7	0.22	217	29.25	19.24	19.53	30.60		
9.C	5.6	0.20	284	20.03	23.60	29,03	23.10		
11.9	5.2	0.34	354	8.25	1.95	13.9:	18.53		
13.9	4.7	5.43	43.	4.93	4.45	4,45	11.39		
15.5	4.2	0.46	\$12	2.15	2.10	2.19	2.35		
12,0	3.6	9.52	598	1.39	1.05	1.05	1.97		
14.5	3.1	0.57	558	1.20	\$,38	1.40	1.54		
19.3	2,0	5.60	752	9.43	¢.91	0.47	2.35		
_ 23,5	2.5	0.43	* 745	3.41	0.50	0.63	1.05		
21.5	2.2	9.66	787	2.39	¥.55	0.43	6.03		

is seen that the colculated oscillatory forces have retained all of the assential characteristics of the measured pressure-time history. Similar comparisons were made for Cases A, B, and D.

GENERAL DISCUSSION OF PESULTS

The technique that was developed in this contract effort, of electronically digitizing and analyzing measured sound pressuretime histories to create high resolution spectra, such as shown in Figure 8, has permitted the detailed shalysis of various rotor sources. For example, the fine frequency resolution that can be obtained by these techniques, allows separation of the

ANALYSIS OF KANNAN-STREET VORTEX SHEDDING USING MEASURED HELICOPTER SOUND PRESSURE DATA

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individual peaks associated with main rotor and tail rotor rotational noise and discrete sources such as oil pumps, gear boxes, etc., from the broadband noise. Since these types of noise sources can now be adequately separated, the characteristics of the various noise sources can be studied independently. The study that was reported on herein stressed the analysis of the broadband noise rather than the rotational noise although the rotational and discrete noise sources were separated from the total noise signature and studied as regards the characturistics of their pressuretime history.

The vortex pressure-time histories (Figure 12, for example) that were generated from the total experimental pressure-time histories by removing the rotational and other discrete noise have the same general characteristics. The signals are essentially random with a modulation in amplitude occurring every blade passage. The high amplitude region has higher frequency than the low applitude regions. This feature is consistent with the Doppler effect discussed previously, i.e. the advancing blade towards the observer raises the frequency and magnitude of any oscillatory pressure amplitudes recorded at an observer's location. It is noted that each blade passage, however, is distinctly different in its:structure. In order to evaluate the effect of this difference on the sound signature of vortex noise each blade passage of the digitized vortex signal was converted to an analog signal and then repeated so that a 5-second analog record of each particular blade passage could be constructed on tape. When a series of each of these 5-second records were played on a tape recorder, it was obvious that each blade passage sounds distinctly different. Qualitatively, this difference from blade passage to blade passing may be described as a modulated signal of varying frequency or "tone". That is, when listening-to a series of blade passage recordings a different frequency content may be discerned in each of the blade passaves.

The vortex shedding model allowed a finite frequency range to be "fit" to the experimental pressure-time history. The relative magnitudes of each of the radial station's oscillatory forces reflected the frequency content of the signal received at the observer for that blade passage. Thus, since the signal varies from blade passage to blade passage both in frequency and magnitude, the oscillatory pressures calculated at the helicopter blade had a corresponding variation. Since each blade passage is different. each calculation-performed results in slightly different radial array of oscillatory forces. This effect is shown in the histograms (see Figure 13), which illustrates how these oscillatory pressures varied:at each radial station over=the 15 blade passages for each of the four cases that were analyzed. Histograms plot the frequency of occurrences of a giver event. In this case, the histograms record the frequency of occurrence of the calculated oscillatory-lift forces in a given range. Reference to Figure 13 shows that the scatter of results increases as the radial station decreases which relates to the previous discussion of the gradual degeneracy of the solution technique as the fraquency of shedding on t * blade decreases. The amount of scatter

of a station corresponds to the variability of the frequency appropriate to that station contained in the experimental record. Thus, for Case C, the frequency appropriate to station 2 was changing significantly from blade passage to blade passage while the frequency appropriate to station 6 changed little from blade passage to blade passage.

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The mean values for each of these distributions were determined. The mean values are listed in Table I and plotted in Figure 14. The shelding frequencies appropriate to the helicopter rotor reference system are listed as well as the Mach number and angle of attack.

The advancing blade, as previously noted, has its shedding frequencies raised and spread apart while the retreating blade has its shedding frequencies lowered and pushed together. The Doppler shifted frequencies on the advancing blade range from about 275 Hz at 7 ft radius to 2100 Hz at 21.5 ft radius. The exact amount of the shift depends on the observer's location relative to the velocity of that blade station. The Doppler shifted frequencies on the retreating blade range from 180 Hz at 7 ft radius to about 500 Hz at 21.5 ft radius. ...ence the outboard section of the advancing blade is associated with high frequency noise and the inboard section of the advancing blade together with the retreating-blads are associated with low frequency noise. For the observer, the radial stations at 7 ft and 9 ft on the advancing blade are in the same frequency range as the retreating blade because of the Doppler effect and hence these stations also reflect the noise energy of the retreating blade. This contribution partially leads to higher values of oscillatory pressure calculated at those radial stations. The noise energy of the entire retreating blade has been-lumped into these two stations.

As shown in Figure 14, the decreasing oscillatory pressure magnitudes at larger blade radius reflect the gradual fall off with frequency of the noise energy shown in the spectra (see Figure * for example). The spectra generated in this analysis comparewell with the findings of Cox and Lynn, Reference 17, in that the major source of audible vortex noise is concentrated in the frequency range of 200 Hz to 500 Hz. The maxima and minima in these spectra caused by ground reflection also affect the calculated oscillatory pressures as the model does not include this reflection effect.

The mean oscillatory pressures have been used to create a pressure-time history at an observer's station. As discussed previously, these created pressure-time histories and these spectra compare very well with the experimental pressure-time histories and spectra. See Figures 15, 16, 12 and 10 for example. Audio tapes created from the calculated pressuretime history sound like the experimental tapes except for the frequency variation from blade passage to blade passage eliminated by using the mean values.

Since the essential characteristics of the experimental acoustic signal can be duplicated with these mean oscillatory forces in a rotating blade frame of reference, it is possible with proper parameterization of the force constants to effectively

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simulate the noise produced by helicopter rotors for a variety of operating conditions. Because of the advanced data analysis proc.dures that have been developed, the rotational and broadband vortex noise can be separated and studied independently. It is, therefore, possible to parameterize the vortex noise and the rotational noise as functions of the rotor geometric and operating conditions such as number of blades, rotational speed, thrust, chord, twist, etc. The parameterization of the vortex noise and rotational noise can be carried out by analyzing various rotor data from whirl tower tests, as was done in this program for a hovering helicopter. Once the parameterization has been accomplished, for a number of different rotor sistems, it should be possible to predict the acoustic signature of any rotor system given only the geometric and operating conditions of the helicopter.

CONCLUSIONS

On the basis of the analyses carried out in this investigation, it was shown that random or "vortex" noise is a major yource of noise from a helicopter in the hover condition. For the cases analyzed, cain rotor rotational noise was not significant above 100 Hz and the major cudible cources of vortex noise were concentrated in the frequency-range of 200 to 500 Hz. In their respective frequency-ranges the main rotor rotational noise was about 30 db above the threshold of hearing while the vortex noise was about 45 db above a normal background noise.

In addition to the above general conclusions the following specific conclusions were drawn:

- Ground reflection effects can significantly distort the radiated acoustic pressure-time history.
- The broadband noise created by a helicopter rotor can be represented by Karman-street vortex induced noise.
- The "vortex" noise correlated for a Stroubal number of 0.235.
- The vortex noise can be simulated by an array of poving, oscillating dipoles with frequencies corresponding to the Karman-vortex street phenomenu.
- The basis of a technique by which the acoustic signature of any rotor system can be predicted in hover or forward flight has been developed and demonstrated.
- A new technique has been developed whereby significantly improved high resolution acoustic spectra can be generated.

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Figure 1. Polative Positions of Microphenes at Wallops Island Air Station.

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DISCRETE NOISE FROM HIGH AND LOW SOLIDITY- NOTORS

S. E. Wright

Institute of Sound and Vibration Research, University of Southampton, Southampton, S09 5 NH, England

Introduction

A single unified theory is described to account for the discrete radiation generally from the whole family of heavily run axial flow rotors, including helicopter rotors, propellers and gas turbine compressors.

The approach used, is to Fourier analyse the periodic blade loading variation (aximuth profile) into blade loading harmonics, and then sum the total radiation from each BLM. In this way, the radiation from any arbitrary blade loading variation, and thus the rotor noise can be determined. To indicate trends, the effect of blade loading profile, load excursion width and number of excursions is considered. The blade of course can sweep out some very complicated source distributions, and again to be in a position to assess the radiation, approximations have to be made.

With this in mind, the basic differences between high and low solidity rotor spectrums are considered, emphasizing the difference between subsonic and supersonic rotor noise. The special effect of helicopter blade slap and compressor rotorstator interaction is discussed, and measured rotor spectrums have been included to help illustrate the theory. The paper is an extract (Section 6) from the publication Discrete radiation from periodic sources in circular motion (1) and is a continuation of the work reported earlier in reference (2). 1. Blade loading spectra

Consider the aerodynamic load on a blade: if the total arithmetic loading varies as the blade rotates, so that is is reproducible for each blade revolution, then the arimuth blade loading profile, see Fig. 1, can be Fourier analysed into blade loading harmonics, such that

$$L(z) = L_{0} + \sum_{g=1}^{m} (A_{g} \cos s_{F} + D_{g} \sin s_{F})$$
(1)

(2)

$$L_{g} = (A_{g}^{2} + B_{g}^{2})^{\frac{1}{4}} + L_{g} = \tan^{-1} (\frac{B_{g}}{A_{g}})$$
 (3)

Any arbitrary periodic azimuth B.L. function can be analysed in this way, and again for convenience the B.L. harmonic amplitude can be represented by a constant times a spectrum function, Viz.

Here the blade loading spectrum level is given by the average value term, Avg, which is equal to the pulse or excursion area divided by the excursion period. The blade loading spectrum

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shape is determined by the blade loading spectrum function χ_g , which is a function of the load excursion profile, width and number per blade revolution.

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Some simple pulses with their spectra are shown in Fig. 14,(1). The representative rectangular pulse is an even function and has cosine terms only, ΔL is the pulse height or load change from the mean value.

$$\chi_{g} = \frac{\sin \pi f t_{o}}{\pi f t_{o}} , Avg = \Delta L \frac{t_{o}}{T}$$
 (5)

The smoothly varying half cosine pulse is also an even function and has cosine terms only,

$$x_{s} = \frac{\cos sft_{0}}{1 - (2ft_{0})^{2}}, \quad \lambda vg = \frac{23L}{2} \cdot \frac{t_{0}}{2}$$
(6)

and the zero lift full sine pulse is an odd function having only sine terms

$$\chi_{s} = \frac{\sin \pi (ft_{0}^{-1})}{4(ft_{0}^{-1})} + \frac{\sin \pi (ft_{0}^{+1})}{4(ft_{0}^{+1})} , \ \lambda vg = \frac{2\Delta L}{\pi} , \ \frac{t_{0}}{T} (7)$$

In terms of rotor parameters, if W is the pulse or azimuth excursion width and E is the number of excursions per blade revolution, then the excursion time t_0 and periodic time T between excursions is

$$f_{T}^{s} = \frac{W}{V_{e}} = \frac{W}{2\pi M r_{e}}, T = \frac{1}{EN}$$
 (8)

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$$\frac{t_o}{T} = E \rho_w \text{ and } f t_o = s E \rho_w \qquad (9)$$

Where $\rho_{\rm c}$ is the load solidity, which is the fraction of the effective annulus that the loading region occupies. viz.

$$P_{W} = \frac{W}{2\pi r_{e}}$$
(10)

The first sE zero is given by

$$(sE)_{z} = \frac{(t_{0})_{z}}{\rho_{w}}$$
(11)

where $(ft_0)_z$ for simple pulses can be read from figure 14 ,(1) e.g. rectangular $(ft_0)_z = 1$, half cosine $(ft_0)_z = 1.5$, triangular $(ft_0)_z = 2$ etc.

As an example, let the blade experience a short stall or an impulsive load change of height LL from the mean load L_0 . If we represent the load encursion by a rectangular distribution then the blade loading spectrum is

where

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(12)

Avg =
$$\Delta L.E.\rho_{u}$$
. and $\chi_{s} = \frac{\sin \pi s E \rho_{u}}{\pi s E \rho_{u}}$

This and other χ_g for more realistic load excursions are shown in Fig. 2, the average value term for the half cosine and sine excursion is

$$\operatorname{Avg}_{\frac{1}{2}\cos} = \operatorname{Avg}_{\operatorname{sine}} = \frac{2}{\pi} \Delta L \cdot E \cdot o_{\operatorname{w}}.$$
 (13)

It is shown that the blade loading spectrum level when expressed in dB, is little different for a variety of simple loading functions, providing the pulse height, width and number per blade revolution is the same. Further, for a given function, the spectrum level is independent of how the average value is arrived at, i.e. it does not matter how high, how wide or how many pulses there are per blade revolution, providing the multiple value is the same.

The spectrum shape is similar for simple all positive or all-negatively going pulses. Pulses with equal positive and negative areas (zero lift functions) similar to the full sine function, have zero value blade loading harmonics at zero order. Blade loading functions that have more than one excursion per blade revolution have blade loading harmonics only at multiples of the excursion number E. The parameter that has the largest effect on the B.L. spectrum is the pulse width or load solidity ρ . Figure 3 shows that the spectrum level falls off rapidly with increasing ρ_{μ} or excursion width W.

2. Blade loading radiation

Having considered the blade-loading spectrum generated by representative blade loadings, we are now in a position to predict the resulting radiation. From equation 70,(1) the sound pressure from a single blade loading harmonic, s is

$$(S\hat{P}_{CB})_{single s} = \frac{a_s}{\delta} K \cdot \gamma_q \cdot \chi_a \cdot \chi_b \cdot \chi_I$$
 (14)

The distributive functions χ_a , χ_b , y_1 account for the linear interference along the chord and span, and between source and image (ground reflection) respectively. For free-field radiation and point-loading or at low frequencies, the three functions are unity. The directivity function γ_{cj} accounts for the circular interference around the rotor disk, and the blade loading spectrum amplitude α_s together with the operating constant K determines the acoustic spectrum level. If the rotor disk is uniformly loaded, then the disk radiates as a whole and s=0 in equation 14 gives the discrete radiation.

If there is a complete spectrum of blade loading harmonics contributing to the sound pressure, then equation 83, (1) together with the relative phase information has to be summed for all values of s, equation 103, (1) will now give the acoustic radiation thus

$$(SP_{mB})_{cont. s} = \frac{a_s}{2} \cdot K_{T} \cdot mB \cdot \chi_a \cdot \chi_b \cdot \chi_f$$
 (15)

Here all the passbands radiated from each B.L.H. sum-to a smooth radiation spectrum, and each mode-radiation at a particular mB number constructs a smooth polar directivity. For a flat B.L.H. spectrum (a_g is constant for all s values), equation 15 is an exact result. Here there is no circular interference operating as in the case of a uniformly radiating disk and therefore γ_q collapses exactly to mB and K to K_m .

Physically the B.L. spectrum assembles to a B.L. impulse and therefore the acoustic spectrum is dominated by radiation from a local loading region within the rotor disk. It is not suprising then, that the polar directivity term K_T is now that of a dipole inclined at the blade force angle. For general B.L. spectrums including random phasing between blade loading harmonics, equation 15 will basically hold, except K_q increasingly contributes to the radiation normal to the dipole axis for progressively less inpulsive loadings.

The blade loading spectrum amplitude a_g can either be measured directly-from the blade, or if the blade loading variations can be roughly estimated in terms of the maximum load change LL and width of load excursion W, then from section 1, where impulsive blade loadings are our main interest

$$\alpha_{g} = \frac{L_{g}}{L_{\alpha_{s}}}, L_{g} = 2 \lambda v_{g} \chi_{g} \qquad (16)$$

and for the simple load excursion considered

Avg =
$$\Delta L.E\rho_{\rm sc}$$
 and $\rho_{\rm sc} = \frac{W}{2\pi r_{\rm sc}}$ (17)

giving

$$\frac{\alpha_g}{2} = \frac{\Delta L \cdot E \cdot \rho_{gg}}{-L_0} - \chi_g$$
(18)

Three pertinent blade loading spectrums and their resulting radiation are illustrated in figure 4, s-has now been replaced by sE to accommodate for multiple-blade loading excursions. For a single blade loading harmonic, a passband of discrete freguencies is radiated, (figure 4(a)) whose radiation magnitude in terms of load solidity p_{ij} , number of load excursions E, and excursion height: 6L. is from equation 14 and 18

$$\hat{sP}_{mB} = \frac{\Delta LE \rho_{\varphi}}{L_{\varphi}} \cdot K \cdot Y_{q} \cdot X_{sE} \cdot X_{a} \cdot X_{b} \cdot X_{I}$$
(19)

The first two terms are basically constants for a particular blade loading function, and therefore set the spectrum level. The directivity function γ_{q} determines the width of the radiation passband, and the four distributive functions $\chi_{gE}\chi_{a}\chi_{b}\chi_{I}$ are unity for point-disk, chord and span loading radiating in free field.

Figure 4(b) shows the effect of multiple blade loading excursions per blade revolution. Here blade loading harmonics only exist at multiples of E. (the concept is analaguous to sound pressure harmonics existing at multiples of B in the \square B spectrum.) Each B.L.H. radiates a passband of discrete frequencies situated about sE where s = 1,2,3 etc.

Here the sound pressure spectrum is given by equation 19. For low E numbers or high H_e , the passbands will overlap and simple B.L.H. radiation addition discussed in section 5.1,(1) will have to be considered. Physically multiple blade loading excursions correspond to E equispaced fixed radiated regions within the rotor disk. Therefore the overlapping passbands now reconstruct new interference patterns, which correspond to the interference between an array of E equispaced inclined dipoles.

Figure 4(c) typifies the radiation from a single load excursion per blade revolution (E=1). A single excursion gives rise to a continuous blade loading spectrum, continuous in the sense that the blade loading harmonics exist at every SE number. Therefore equations 15 and 18 now give the acoustic radiation as

$$(SP_{mB})_{cont.s} = \frac{\Delta L.E.\rho_{o}}{L_{o}} \cdot K_{T} \cdot mB \cdot \chi_{sE} \cdot \chi_{s} \cdot \chi_{b} \cdot \chi_{I}$$
(20)

The sound pressure harmonic falloff is now the resultant of the four distributive spectrum functions $x_{gE} x_a x_b x_1$, whose onset of effectiveness (departure from unity) is measured by the reciprocal of their individual solidities p. For free field radiation $x_1^{=1}$ and point chord and span loading $(o_a^{=}o_b^{=}o, y_a^{=}x_b^{=})$, the relation between the acoustic spectrum and the blade loading spectrum is 6dB per uctave within the limitations of equation 103.(1)

The fact that a relationship between the blade loading spectrum and its acoustic spectrum has been established has fascinating possibilities. It means that aerodynamic data can now be accessed from the acoustic spectrum. To obtain the blade loading coefficient for a single load excursion, we combine equations_15 and 14

$$\frac{(sp)_{cont.s}}{(sp)_{sro}} = \frac{\sigma_s \kappa_{a} m s_{a} v_b v_I}{2 \kappa_{p} m s_{a} v_b v_I}$$
(22)

then

$$a_{s=nB} = \frac{(SP)_{cont.s}}{(SP)_{s=0}} \xrightarrow{K} \frac{K}{\kappa_T} \cdot \frac{2\gamma_{mB}}{mB}$$
(23)

The blade loading coefficient at the crossover point, i.e. the point where the fluctuating load radiation starts to dominate the steady load radiation is

$$a_{g=\pi B} = \frac{K}{K_T} + \frac{2r_{\pi B}}{\pi \delta} = \frac{2K}{K_T} + J_{\pi B}(x)$$
 (24)

Assuming K_{η} , K_{η} , $A_{s=0}$, $B_{s\neq0}$, and for the observer mituated along the maximum directivity K_{η} , K_{η} liste $B_{s=0}$ is not necessarily

equal to $\beta_{g\neq 0}$). The blade loading coefficient in dB is then

20 log
$$u_s = 20 \log (SP)_{cont.s} - 20 \log (SP)_{s=0} + 20 \log \frac{2Y_{mB}}{mB}$$
 (25)

where from equation 12,(1)

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$$20 \log \frac{2\gamma_{mB}}{mB} = - (20 \log \frac{mB}{2} + 7 + mB 20 \log \frac{0.7}{H_e})$$
(26)

The fractional change in load $\frac{\delta L}{L_O}$ can then be calculated from equation 16 thus

$$\frac{\Delta L}{L_0} = \frac{\alpha_g}{2 \cdot E \cdot \rho_W x_g}$$
(27)

Similarly, to obtain the blade-loading coefficient for a large multiple-excursion spectrum we-can write down equation 14 twice for $s = -\pi E$ and $s = -\sigma$ thus

$$\frac{(SP)_{gE}}{(SP)_{g=0}} = \frac{gE^{K_{p}}qX_{a}X_{b}X_{I}}{2K_{p}}$$
(28)

then

$$\alpha_{sE} = \frac{(SP)_{sE}}{(SP)_{seo}} + \frac{2\gamma_{mB}}{\gamma_{g}}$$
(29)

where q=mB-sE, or simply at low frequencies

$$a_{sE} = \frac{2(SP)_{sE}}{K_{Y_{q}}} \quad \text{and} \quad \frac{\Delta L}{L_{o}} = \frac{(SP)_{sE}}{K_{Y_{q}} L_{o}} \chi_{sE} \qquad (30)$$

Y is preferred to y_q , as its zeroes in practice are never clearly resolved. From equation 63,(1)

$$\hat{M}_{q} = mBJ_{q}(x) = (\frac{2}{2})^{\frac{1}{2}} \cdot \left\{ \frac{mR}{M_{c} \cos \delta} \right\}^{\frac{1}{2}}$$
 (31)

i.e. Y rises at the rate of 3 dB per octave in mB.

The load solidity o_{μ} , the blade loading spectrum x_{g} and the static and dynamic loads on the blade can therefore be estimated from a knowledge of the acoustic spectrum. In genetal for subsonic rotors, if there are large discretes high in the acoustic spectrum, then p_{μ} is low and the blade is experiencing impulsive loading. If the discretes fall off quickly, then p_{μ} is high and the loading is varying slowly. If the harmonics fall off very rapidly-according to equation (1) then p_{μ} = 100% and the blades are sustaining static loading only. For supersonic rotors, the stead; lift dominates the acoustic spectrum.

3. General rotor spectrums

From a noise point of view, rotors can be conveniently divided into two classes; high and low solidity-rotors. Low solidity rotors are those with a few narrow blades such as helicopter and propeller rotors. As a result of having few concentrated rotating forces (B small), the steady lift or thrust (seo) on this type of rotor in clean flow, dominates the low frequency rotor spectrum in accordance with equation 11.(1). In the case of

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higher raving rotor (propeller), the steady lift radiates well into the audible part of the acoustic spectrum and therefore gives a reasonably indication of the rotor noise. However for the lower r.p.m. rotor (helicopter rotor), the steady lift radiation from the higher order B.L.H. is all that is heard. In order to predict propeller noise accurately and account for the subjective noise from helicopter rotors, fluctuating lift radiation (sfo) must be taken into account.

Fluctuating lift is generated by varying persistence in the rotors disc loading asymmetry. The causes are numerous, some obvious effects are fuselage, wings and forward speed, examples of transient effects are crosswind, atmospheric turbulence and aircraft maneuvers. Some readers may remember the abrupt change in pitch of the Spitfire's maneuver in the last war. To produce strong periodic-tones well into the rotor spectrum, the loading asymmetries must be "spike like", produced by impulsive type blade loading functions. Such a source of current interest, is the banging noise heard in certain situations on helicopter rotors, sometimes referred to as blade clap. Here rotor blades are thought to cut or pass near to tip vortices shed by proceeding blade producing a sudden load excursion. It can be argued that strong blade-tip vortex interaction can occur particularly in high Jorward speed, and in-hover in the case of a tandem-rotor machine. In either case the radiated spectrum from the impulsive loading will be given by equation 20, and the polar directivity will be dipole like, inclined in the direction of the effective blade force angle. If more than one bladetip vortex interaction occurs per blade revolution, the multiple load excursion theory has to be considered.

For moderate tip speeds, high solidity rotors such As fans and gas turbine compressors (B large), produce negligible steady lift radiation. This is immediately evident from equations 11 ,(1) and-12,(1). For high values of B, γ_{mB} is very small even for the first harmonic (m=1) and therefore no matter how big K and α_{g} are within roason, the sound pressure will be very small. However for tip speeds approaching Mach one, the mB falloff is negligible and the steady-lift dominates the acoustic spectrum. For tip speeds greater than Mach one, the harmonics actually increase with order for point loading as shock waves propagate from the blades, and a loud objectionable noise known in the fan-industry as buzz saw noise is heard. It is clear than, that to remove steady lift-radiation, a rotor must have a large number of blades and operate at low tip speeds.

Unfortunately, fluctuating lift radiation is not-reduced by increasing a rotors solidity, and any disc loading asymmetryproduced in high solidity rotors again produces large discrete radiation. Further examples of asymmetry are motor support struts on high speed fans and stator blades on gas turbine compressors. Hence the blades experience impulsive blade loading fluctuations as the blades pass over the obstructions in the "flow. Essentially there is little difference between rotorstator interaction and blade-tip vortex interaction previously mentioned. Basically-only the number of load excursions and rotor frequency are different, the blade-tip vortex radiation is therefore heard as a banging noise and rotor-stator radiation, because of the more frequent load excursions, is heard as a high pitch whime.

Large number of load excursions produce fascinating rotor spectrums. Figure 5 is an example of such a spectrum. Here the emphasis is on the radiation addition of a few B.L.H. passbands situated at sultiples of E, rather than the summation of a complete spectrum of blade loading harmonics s for E=1. In the figure, the passbands are represented by flat plateaus of length given by equation 9,(1) situated about q=o where s+sE for E>1, their level of course would be given by the blade loading function x_{g} . The sound pressure harmonics are represented by the dotted lines and occur at multiples of B. Any rotor spectrum can be constructed in this way. In the illustration, the rotor spectrum represents a free field compressor with 23 rotor blades and 36 stator blades. It can be seen that the first yound pressure harmonic does not radiate, it is below cut off, only the first B.L.H. contributes to the second sound pressure harmonic and s=1 and 2=to the third, the radiation addition here is discussed in Section 5.1,(1). By rearranging equation 9,(1) for the lower cut off all number

$$\frac{sE}{RB}_{c} = 1 + H_{e} \cos \sigma \qquad (32)$$

it can be seen that for particular combinations of sE and mB, certain sound pressure harmonics do not radiate. For example it can be said that for the fundamental blade loading harmonic (s=1), the fundamental blade passage frequency (m=1) will not radiate if

$$\frac{z}{B} < 1 + H_{e} \cos \sigma$$
 (33)

Alwo, by choosing a convenient blade number B and excursion number: E combination, the q-o mode radiation can be seen to be avoided. In terms of frequency f=m2N, our compressor example running at say N=100Hz, the spectrum above mB=140 (f=14,000Hz) is of no further interest.

4. Meacured rotor spectrums

To help illustrate the theory, several measured rotor spectrums from rotors of widely different solidity and operating conditions are analyzed. Figure 6(a) is one of many acoustic spectrums of a OH4 Bell helicopter measured by Pegg reference 3. Here the main rotor has B=2 blades, a tip radius r_e =16.65 ft. and a shaft frequency of N=6.6 Hz, giving a tip Mach number of M_e =0.62. The rotor was lifting L_y =2750 lbs. at a forward speed of 61 knots, its altitude was 500 ft. and 1200-ft. head of the microphone, making an elevation angle of σ =23°. The microphone height was 5 ft. above a grass coverud terrain and the analysis made on a 2Hz constant bandwidth analyser.

In the figure, the steady lift radiation is seen dominating the low frequencies in accordance with equation 1,(1) for s=o

DISCRETE NO. 5 FROM HIGH AND LOW SOLIDITY ROTORS

(assuming $\beta=6^{\circ}$). The first harmonic m=1 is muted through the low frequency response of the recorder (20 Hz), but the harwonic falloff is 1.5db per mB, and is given by equation 11,(1) using a value of $r_{e}=0.9r_{e}$. The remainder of the spectrum is contributed by fluctuating lift, here discrete frequencies stretch well into the acoustic spectrum at multiple of the blade passage frequency. The rotor is therefore experiencing impulsive loading, the radiation from which is given by equation 20. It is difficult to assess the exact contributions of each of the functions in equation:20 without blade loading information, but by making a few first order assumptions progress can be tady. Firstly, the spectrum is noticeably modulated by the image spectrum function χ_1 , caused through ground reflection (equations 67,(1) and 68,(1)). In this particular measuring set up, the helicopter height is less than its range and therefore the first and second spectrum zeroes f_x are 130Hz and 390Hz and are adequately given by-equation 69(b),(1) where n=1 and 3. Other simultaneous acoustic spectrums taken at different observation positions, show that the f_ move around in the spectrum according to the above equations.

Taking account of χ_1 and neglecting the harmonics of the tail rotor particularly $m_{\mu}=1$ and $m_{\mu}=4$, the spectrum falloff will be given by $K^{}_{\rm T},\;mB,\chi^{}_{\rm g}\chi^{}_{\rm a}\chi^{}_{\rm b}.$ In all probability the spectrum is generated from a single load excursion per blade revolution E=1. and therefore the polar directivity will be highly directional (that of a dipole inclined at-the effective blade force angle). The directivity information is contained in the K_m term and is defined for the observer at-0" azimuth. If the observer lies along the axis of the dipole-then cost sins is effectively unity in K_r and the impulsive spectrum will have its maximum value. If the load excursion occurs-on-the starboard side of the helicopter rotor, then the lower lobe of the dipole will be tilted towards the ground in the direction of forward notion. Listening to the sraid pressure time-histories of advancing 'blade slapping' helicopters supports-this-description, i.e. the banging is heard when approaching and then stops overhead.

Before we can estimate the blade loading spectrum function x_g , we must assess the effectiveness of the chord and span distributive functions. The chord solidity and first $(mB)_g$ would be $c_A \approx 13$ and $(mb)_g \approx 100$ assuming a rectangular chord distribution of a=1 ft. If a tip vortex blade interaction is the cause of the inpulsive loading, it is unlikely that the whole span length would be affected. Therefore assuming an effective span length of say b=2 ft. and a rectangular distribution, the corresponding span solidity and first $(mB)_g$ is 1% and 100 respectively. For more realistic distributions, say the half cosine function, a solidity of 1% w 'f give $(mB)_g \approx 150$. In either case the departure from unity of $\frac{1}{2}$ and $\frac{1}{2}$ functions, would not be appreciable at mB=30.

With the above assumptions, the spectrum hump situated around mB=30 must be that of the blade loading spectrum function x_g along. Peferring to figure 2, something similar to the full sine x_g function with a load solidity $c_g = 34$ would best account for the acoustic spectrum. This is most encouraging as the full sine type blade loading function is consistent with what is thought to occur when a blade cuts or passes near to a tip vortex, reference 4. Also in-flight blade loading measurements reference 5 on a XH-51A compount helicopter show blade loading functions cimilar to the zero lift full sine function but with load solidities of the order of 50%. In this case the spectrum hump would occur at mB=2, giving little high order discrete radiation. Assuming a χ_g function of the full sine type (of ρ_g =3% and E=1), then from equations 25 and 26, the maximum blade loading coefficient $\hat{\alpha}_g$ =30 is -50dB or 1/300th, and corresponds to a fractional load change (equation 27) of $\frac{L_1}{L} = 5$ %.

Figure 6(b) is an acoustic spectrum from a low solidity high reving rotor (OVIO propeller). The salient operating conditions are B=3, r_e =4.25 ft, N=26.6 Hz, M_e = 0.64 torque 1000 ft. lbs. (T_e =1200 lbs.) ==0.6 ft., σ =0° R=50 ft., analyser bandwidth=2Hz. Because of few blades, the steady lift radiation can be seen dominating the low frequency spectrum according to equation 1,(1) and the harmonic falloff (2.7dB per mB) is given by equation 11,(1) using a value of r_e =0.8 r_e . The spectrum is typical of many spectrums-investigated by Crigler reference 6, and shows the so called vortex shedding hump resolved into an almost flat spectrum of discretes. Subharmonics can also be seen in between the main harmonics, and occur because the blade forces are unequal, i.e. each blade force is unique and therefore gen= erate harmonics at multiples of mB where B=1.

The spectrum is probably generated by a single load excurtion E=1 and the harmonic falloff will therefore be given by $mB_{2} = y_{A} x_{b} x_{1}$. Again it is difficult to access the effectiveness of each of the spectrum functions without blade loading data. However χ_r appears ineffective, and assuming a chord and span solidity of less than 1%, $x_a x_b$ will have little effect on the spectrum shown. The spectrum envelope will then be $mB_{K_{act}}$, i.e. x_{g} is falling off at=6dR per octave in mB. Referring to fig. 14,(1) a triangular type blade loading function would then best fit this blade loading spectrum. The same result could be obtained using say a half-cosine type function together with lower chord or span solidities. The truth is probably a combination of both. In either case the rotor is experiencing impulsive loading, and the blade loading coefficient of at the crossover point (mB+12)-from equation 24 and 26 (assuming the observer is along the maximum directivity) is -60dB or $\frac{1}{1000}$. Nothing can be said about the fractional change in load without a knowledge of the load solidity.

Figure 6(c) is a spectrum from a high speed high solidity rotor (3 stage axial-flow compressor) investigated by Chestnutt and Clark reference 7. The operating parameters are D=2),-E=36. r_e =0.5 ft. H=290Hz, M_e =0.8, horsepower=800 (T_p =200 lbs. first stage) ==60° R=100 ft. from bellmouth. Measurements were made in the anechold chamber and the analysis performed on a SoHz analyser. Due to a large blade number, the steady loading s=0 is not contributing to the rotor noise at this particular operating speed (X_p =0.8) and observation angle (=660°1. If for example the rotor had only one blade (all other things being equal) then the steady load radiation would have been 140dB at the first harmonic. Or at supersonic speeds the steady load line s=0 would become horizontal at $\sigma=0^{4}$ (see fig. 10,(1)) and the steady load radiation then dominates the spectrum irrespective of blade number.

However in this particular-situation the steady load contribution to the first harmonic is only 28dB and the harmonic falloff given by γ_{q} is 4.6dB per mB. The spectrum is therefore generated by impulsive loading caused through rotor-stator interaction. Here because of the large number of load excursions E, the acoustic spectrum will be given by equation 19. The first and second sound pressure harmonics $m_1=1$. $m_1=2$ of the first stage compressor can be seen dominating the spectrum at mB=23 and 46. The first harmonic $m_2=1$ of the second stage is at mB=31 and the first harmonic $m_3=1$ of the third stage is at mB=46. The subharmonics at multiples of mB where B=1, is caused through unequal blade forces as explained previously.

Because of the high shaft speed and large blade number, the separation between the first and second sound pressure harmonic of the first stage is almost 7 KHz and practically the entire audible acoustic spectrum 0-14kFz=1s covered by these first two harmonics. (It is interesting to compare this spectrum with the equivalent first two harmonics of the helicopter rotor spectrum which covers only 24Hz). The passbands for the first and second blade loading harmonic s=1, s=2 for the first stage are shown in-dotted outline. It can be seen that only the s=1-blade loading harmonic-contributes to the first sound pressure harmonic and s=1 and s=2 to the second. The first harmonic is right at the end of its payshand and by reducing the rotor tip speed a little, the passbands will shrink accordingly thus cutting off the first harmonic. From equation 30 the blade-loading coefficient at the first narmonic mB=23-is $n_{23} = -47$ dB or $\frac{1}{300}$ th approximate/y.

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DISCRETE NOISE FROM HIGH AND LOW SOLIDITY ROTORS

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An Investigation of Noise Generation

on a Hovering Rotor H. Sternfeld and

R. H. Spencer

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Deductive Development of Aerodynamic Criteria for Hovering-Single Kotor Impulsive Noise Generation

C. J. Bobo

and R. F. Child

The Boeing Company Vertol Division

INTRODUCTION

This paper presents the results of a program of helicopter rotor noise measurement. The program was carried out using a 3 bladed +0-foot-diameter CH-47B rotor on the Boeing-Vertol-engineeringrotor whirl tower. The preserve objectives of the program were:

- We obtain -acoustical data over a frequency range wide enough to define all elements:of rotor noise under well-documentedambient conditions.
- Y0 measure the tip vortex position with respect to a trailing blade using-high=speed_cameras and smoke to visualize the tip vortex, and to relate blade=vortex separation distance to noise level.
- 3. To determine the propagation enaracteristics of retor noise.
- To evaluate two current analytical-procedures for predicting rotor noise (Ref. 1, 2) against the measured data.

The testing on-the GO-foot-diameter rotor encompassed a range of tipspeeds from 600 to 900 fps and thrusts from 6,300 lb to 32,000 lb (disk loadings-of 2.2 to 11.) psf). Where have been several programs aimed at measurement of pressures on the surface of a-rotor blade, 3, 4, 5 but these studies have been concerned with rotor performance and have not recorded data with sufficient frequency response to be useful in noise research. For the most part this was due to the general unavailability of adequate instrumentation. Several programs have also been performed 6, 7 to collect noise data in the near and far field of the rotor and at-several positions of rotor azimuth. Much of this data has been obtained un flight aircraft and therefore includes all other noise-sources inherent in such a vehicle. In at least one other program, smoke has been released at-the tip of a blade to study the blade wake in terms of the position of the tip vortex.¹⁰ However, no data in terms of a complete noise-measurement-program has_been published for adequate study of the generation and propagation of the noise of helicopter lifting rotors.

The-concept of the program-described in this paper was (a) to clarify the-situation (at least inspart) by dealing with the simplest case, namely a single hovering rotor, (b) providing instrumentation adequate to the task of defining the complete acoustical signature, (c) devising a-test technique which would, insofar as possible, permit separate identification of the noise sources, and then to (d) compare these results with current "state-of-the-art" analytical predictions in order to more accurately assess current capabilities and to identify the more serious shortcomings. 7

The rotor system, tested in this program is that designed for the Army CH-47B "Chinook" helicopter and is a three-bladed, fully articulated rotor of 30 feet radius and 25.25 inch chord.

The individual rotor blades are fabricated from a steel "D" spar with fiburglass laminate covered trailing edge boxes. The airfoil is a 23010-1.58 section as shown in Figure 1 and the blade is ...tapered in either planform or thickness. The tip of the blade siminates in a simple plate closing the outboard box, a "square tip". For the purpose of this investigation the blade was modified by the addition of smoke generators. The smoke generator canisters had been developed previously for a flight test program on a CH-464 helicopter ¹⁰.

The subject program was conducted on the beging-Vertol Engineering Rotor Test Facility (Figure 2). The rotor on this-tower is 50=ft. above he ground and is powered by a 10,000 hp electric motor which drives through a water-cooled clutch. The electric drive, along with suitable gear reduction system, is housed in the concrete-base of=the structure. This base serves to minimize the drive System noise radiated outside to a level which is negligible when making



Figure 1 Test Airfoil



Figure 2 -Rotor Test Tower

rotor noise measurements. The fundamental control-modes available are rotor speed, and thrust-which is achieved through collective pitch. No cyclic pitch, or smaft angle variation was utilized. Rotor rpm readout is available to the towar operator and rotor Append can be maintained to an occuracy limited by variations in achient wind, generally to Within 1 pps.

The microphones used were of the condenser type and were located as-illustrated in Figure 2. The microphones designated 0.2R, IR, ID, JD, 50 were used to acquire the primary data. As shown, they were

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supported by cables and arranged along a single path from a point just below the blade hub to the ground. The direction chosen permitted a large radial distance without proximity to other buildings or structures. In general, the microphone array was upwind of the rotor. These microphones were selected for this program because of their high sensitivity at low frequencies as well as flat frequency response characteristics. This is especially important for the study of rotational noise, where fundamental blade passage frequencies may be below 10 Hz. In specific, the microphones employed were Photocon 747 transducers with Dynaga;e DG-605D signal conditioners.

Ideally, it would have been desirable to have several radial arrays of these low frequency microphones, each along a different azimuth direction. Since program limitations and equipment availability precluded such an extensive system, it was decided to provide four monitor microphones .ocated around the tower base as noted in Figure 2. These were Brunl and Kjaer Type 4131 condenser microphones of more conventional frequency range. In this program it was not intended that this information be made available, but rather that if the primary data should appear inconsistent, they would permit the possibility of determining whether a change in directivity of the radiated sound might be responsible for the inconsistencies.

The acoustical and atmospheric information was recorded on an Ampex FR-1300 wide band FN system operating at a tape speed of 30 ips. The acoustical inputs were continuously monitored on

individual-oscilloscopes to determine the required attenuation, or amplification in order to ensure-optimum quality data witha high signal-to noise ratio. The use-of-monitoring oscilloscopes also permitted the engineer to observe noteworthy changes in noise characteristics as the test progresses. The Bo ing-Vertol Nobile Acoustical-Laboratory was used as a test control center for dataacquisition. Figure 3 shows several views of the instrumentation employed. Prior to the test program each complete data system was calibrated. A system was defined as a combination of microphonetransducer, cathode follower, cables, signal conditioner, and recording track. Once calibrated, the elements remained as a moninterchangeable system for the remainder of the program.

Since the program was essentially a hover program, small changes in ambient wind conditions could become important. To monitor ambient conditions, an anemometer and wind vane were erected on a 50 foot high mast approximately 150 ft. from the rotor tower. This tower located the instrumentation at the same height above the groundas the rotor, but kept it far enough away to be relatively unaffected by the rotor downwash. The output of the velocity indicator was recorded directly on the magnetic tape along with the sound pressure level data. Ambient temperature and barometric pressure were measured at ground level but not recorded on tape. These data were used both for correlation with the acoustical information and for the tower torque/thrust calibration. Prior to the tust program, an evaluation was made to determine the influence, if any, of the tower structure, nearby-buildings, and the terrain itself on the acoustical signals sensed by the microphones by



MOBILE LABORATORY AND TAPE VAN



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WEATHER INSTRUMENTS IN MOBILE LAB



SMOKE INSTRUMENTATION



WHIRL TOWER INSTRUMENTATION

Figure 3 Test:Instrumentation.

reverberations tests conducted with 38 caliber blank revolver cartridges. The results of this are discussed later.

Smoke generators were ignited in the blade tips to mark the vortex. High speed motion pictures were taken of the smoke utilizing two cameras which were placed on the tower, one-aimed toward the blade tip from just under the rotor at about 0.2R, and one-aimed upward from the ground at the tower base. These two cameras provided vortex position measurements at one-azimuth. Two additional cameras were mounted in the rotating system to measure the separation between a trailed vortex, and the blade which followed the vortex generating blade. In order to measure the films for vortex position, two-cable grids with ping-ping balls securely attached for targets were used. Measuring the images of the targets and combining those measurements with knowledge of the camers positions and the target positions produced the desired blade and vortex positions.

DATA REDUCTION

The primary analysis used for the reduction of the acoustical data employed techniques and equipment referred to as Real Time Digital Analysis. Application of this relatively new technique to the study of rotor noise is one of the major innovations of this program.

Before-discussing the detailed application of the processing to rotor=noise data, it will be=helpful to characterize some-aspects of rotor noise and to agree on convensent terminology. First-of all,_it=is_important to recognize=that any real data, even=low wind=hover, will display many transient changes due to uncontrollab:

AN INVESTIGATION OF NOISE GENERATION ON A HOVERING ROTOR

variables. These may be minor in nature, or may be so large that they completely dominate the scoustical signature. For many purposes, especially when comparing data with analytical predictions, it is important to know whether the data under discussion is invarient with time or contains the afovementioned transients. In this paper, all data will be defined either as "steady state", implying that it is valid at any time, or as "transient", implying that it is only-valid at a particular instant in time.

A second sot of definitions which apply to the frequency (rather than the time) domain are the terms 'discrete' ard'broadband' which describe the amplitude-frequency distribution. There is no rigorous definition of discrete but it can be easily understood that it implies a concentration of acoustical energy in a rather narrow range such that the levels at adjacent higher and lower frequencies are significantly less. It should be kept in mind that these discrete frequencies may be harmonically related to the rotor passage, (and to each other) or may be independent if produced by a non-harmonic source.

In this program, steady state harmonic analyses were used for comparison with analytical predictions, while transient analysis was used to study tip vortex noise phenomena. In order to compare the broadband vortex noise with analytical prediction, conventional octave band analyses were performed:using analog equipment (BsK 2112 Spectrum Analyzer and BsK-2305-Level Recorder). This method was used because the prediction method is essentially a statistical matching of data with blade operating parameters.

RUN . 54 TIP SPEED 750 FT/SEC THRUST 19000 LB







Figure 4







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Figure 4

DISCUSSION OF RESULTS

A fundamental purpose of the program was to document $t_{\rm b}$ moise of a rotor over a broad range of test variables and under conditions which were closely monitored. This was accomplished with a recording system which, as previously described, had a frequency response which had no sensitivity variation over a frequency range of 2 - 5000 Hz and was within 2 db of the nominal value over the range 5000-10,000 Hz.

The basis data was analyzed for the range 0-500-P* a.d averaged over 32 rotor cycles to preserve definition of individual harmonics of blade passage for a broad frequency range. A representative matrix of data was also analyzed over the frequency range 0-10,000.

Figure 4 presents a typical set of data.

REVERBLEATION

The influence of reflective surfaces, including the ground plane, was investigated and it was shown that data from excreptiones at 0.2R, IR and ID were not generally degraded-from accustical reflection. However, data observed at the 3D and 3D locations were not free field. Agreement between the prediction and

AVG 27X

measurement is evidence that only the ground reflected wave was the major source of interference. Destructive interference of the ground_reflected_ray with the unreflected incident-wave occurs in the range of signal frequencies which correspond to

one-half the wavelength of the period associated with the time delay between incident and reflected wavefronts. The pressure amplitude at a microphone resulting from the incident and time delayed reflected wave is,

- $P_{3D} = P_0 \sin t + aP_0 \sin \{\omega(t + \Delta t)\}$
 - Po = Pressure amplitude of original wave
 - a = attenuation coefficient
 - At = time delay of reflected wave (sec)
 - w = sound frequency (rad/sec)

expandiny,

- $P_{3D} = P_0 \sin \omega t + aP_0 \sin \omega t \cos \omega at + \cos \omega t \sin \omega at$
 - = P_{2} min wit (1 + a-cos w.at) + (aPo sin wat) (cos wt)

$$P_{0} a^{2} \sin \left(\omega + 1 \right)$$
where $a^{2} = \left\{ \left(1 + a \cos \omega \cdot at\right)^{2} + a^{2} \sin^{2} \left(\omega \cdot \Delta t\right) \right\}^{1/2}$
and $\eta = \tan^{-1} \left[\frac{a \sin \left(\omega \cdot \Delta t\right)}{1 + a \cos \omega \cdot \Delta t} \right]$

In the form of the identity,

$$a^{1} = [1 + 2 a \cos u. \delta t + a^{2} \cos^{2} u. \delta t + a^{2} \sin^{2} u. \delta t]^{1/2}$$

or $a^{4} = \left[1 + 2 a \cos u \cdot \delta t + a^{2}\right]^{1/2}$

The measured sound level at 3 diameters is

SPL30 = SPLo += 20 log a'

where SPLo is the level from the incident wave only.



Figure-5 Signal Amplification Due:to Reflection,

Evaluation of the attenuation coefficient, a', then permits a correction to be made to obtain free field data. 20 log a' is plotted as a function of frequency in Figure 5.

HARMONIC

Predicted levels for the test rotor have been compared with measurements-(e.g. Figure 6) for those frequencies which are identifiable as harmonics of blade passage. The theory of Reference 1 has been corrected for the specific test site conditions for reflection, by the method developed, and the reflected wave amplitude has been corrected for source directivity. The underprediction, as noted by Lowson, is thought to result from the lack of adequate high harmonic sensitivity of the instrumentation which measured airloads utilized by him in developing the theory. This difference between predicted and measured levels is also illustrated in Figure 7, the zero reference being the data value.



Figure 6 Comparison of-Harmonic Data with Theory of Ref. 1



Comparisons of the data with predictions in terms of tip Mach number and thrust coefficient were-also made. Good agreement was also displayed at-harmonic numbers of blade passage below five. Mecause of this agreement, at low harmonic numbers, the fundamental_blade passage frequency was used in investigating data trends with tip-speed, illustrated in Figure 8. The data shown for the lowest thrust, displays a 5.3 power law trend. This slope decreases with increasing thrust to n = 3.4. Straight lines were fit to the data by the method of dats to gate. Powerlaw trends at the low-thrust values are in conformance with other published data.

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Figure-8 Tipspeed Trends.

It-can be generally concluded that the low harmonics of blade passage are predictable in that they can be estimated to within 5-db of the measurement value, at loast-over the range of operating condition. investigated in this program. Further, it is not surprising that the best agreement between theory and data is in he-same range-of tip speeds-and thrusts-as the airload data which Scheiman reported and which Lowson utilized for development-of-his Reference-1 theory. Airloading data with improved high harmonic content appears to be the solution to increased accuracy of noise-prediction of lifting-rotors.

BROADBAND NOISE

Table I presents a comparision of methods for broadband noise prediction developed by other researchers working in helicopter noise. The constants in the expressions presented account for the field point where comparison data was obtained. Predictions have been made for-only one data point.

TRANSIENT IMPULATVE NOISE

In previous investigations of the noise-generated from a hovering rotor as reported in Reference 9, a transient, impulsive noise was observed above the relatively constant rotational noise. This noise dominates the signature and becomes greater-in magnitude with increasing tip speed and thrust. It had been previously

TABLE III							
COMPARISON	14	VOPTEX	NOISE	PRIDICTION	NETHODS		
WITH PLASURED DATA							

AUTHOR	FORM	E MAX	FREDICTION	DJ TA
NUBRARD	$SPL_{100} = 10 lwy \left(\frac{KSV_{07}}{10^{16}}\right) \cdot 4.6$			LOUIVALINT TO OVERALL VORTED
SCHLEGEL NING & MULL	$SPL_{100} = 20 \log V_{0.7} + 20 \log T$ = 10 log A _D = 31,3	0.20 V0.7	\$6.3	102
DAVIDSON & HARGEST	$\frac{100}{100} + 23 \log V_{1} + 20 \log T$ - 10 log 5 = 16.5		104.0	102
STUCKEY & GOUDARD	$SPL_{180} = 26.8 \text{ log V}_{1} + 16.6 \text{ log T}$ = 20 log SEC t = 49.2	0.18 1 0.40	98.6	102
LEVERTON	SPL 180 = 40 log V + 10 log 5 - 91		104.1	102

V + MLANE VELOCITY NOTOR THRUST

S + A_L + BLADE APEA 187.5 102 180 71

- DISTANCE TO HICPOPIENE

F . ANGLE DETWEEN THE LOCATED LIPOLE AXIS AND RECEIPHINE

750 PT/SMC

19,000 LB.

hypothesized that this impulsive signature was due to blade-vortex intersections and, therefore, smoke visualization of the vortex was used to measure vortex position in order to correlate blade-vortex separation with recorded noise level. Figure 9 illustrates typical-results from the vortex position analysis. These measurements-and extrapolations indicate that intersections occur for all the conditions observed. Of special interest is the fact that-intersections were observed for a low thrust condition (Figure 9b) for which no transient impulsive noise was observed, and=for a higher-thrust condition, Figure-9a, which did display a transient impulsive noise_in-its signature. Thus any correlation between separation and the occurrence of this impulsive noise is not meaninuful.

Since the existence of absence of transient impulses in an acoustical signature cannot be determined by the existence or absence of blade-vortex intersections alone, one of the following conclusions can be-drawn: (a) the vortex-does not enter into the requirement for impulsive noise generation, or (b) the presence of the vorte: is-not the total determinant of impulsive noise generation. Discussion of this is continued in the following section along with a possible-mechanism of-generation of single rotor transient-noise.

AN INVESTIGATION OF NOISE GENERATION ON A HOVERING ROTOR



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STUDIES RELATING TO STEADY AND UNSTEADY AERODYNAMICS

OF MELICOPTER BOTORS

by

Barnes W. McCornick Department of Aerospace Engineering The Pennsylvania State University

Abstract

This paper describes the results of research projects which ary presently being undertaken by the Department of Aerospace Engineering, The-Pennsylvania State University, relating to-the steady and unsteady serodynamics of helicopter rotors. Emphasis is placed in particular on the ANO-D sponsored-project which is concerned primarily with blade motion and air loads for large helicopters. In addition, however, results of a roter-vortex interaction study, including a short sound movie are presented. In the ARO-D project means are being explored for reducing the excessive flaming to be expected with large rotors. Using-a Lagrangian approach, equations of motion have been Jeveloped for coupled flapping. lead-lag and torsional motion. A modified Bernoulli-Euler=(slender beas) theory considers the effects of rotary inertia and shear deformation. The numerical solution is designed to handle an arbitrary elastic restraint at the hub as well as a general spanwise and chordwise distribution of mass and structural stiffness. Instantaneous airloads=are calculated. knowing the blade's motion, by starting the rotor at rest and calculating the position of the free wake which is generated as the steady operating condition is approached.

The analytical problem of the servine constants forces caused by a partial span, oscillating jet flap on a helicopter rotor blade is being investigated as a means of reducing the flapping. An asymptotic estantion technique-used to solve the steady-state problem of a full-span jet on a three-dimensional wing, is being applied to the unsteady problem of a jet-flapped wing. The boundary conditions for the wing and jet have been altered to include the unsteady effects and the empansions for velocity potential are being written with the reciprocal of aspect ratio as the small parameter.

A study is underway to design a device capable of controlling the jet flap position. The device would in some manner sense the rotor blade displacement and accelerations to control the jet flap to a position related to the motion. Of particular interest are fluidic control devices because of their mechanical simplicity and available power from the jet flap pressure chamber. A two-dimensional model of the device will be built and investigated in a wind tunnel.

Introduction

The Department of Aerospace Engineering at The Pennsylmania State University has been undertaking studies⁽¹⁾ relating to helicopter moise for approximately three years. Hore recently studies have begun⁽²⁾ on unsteady serodynamic-problems specifically related to very large helicopters. This paper, in a sense, is a progress report on all of these studies and presents future plans as well as some of the results obtained to date.

The NASA supported studies have been concerned with the rotor-blade, vortex-interaction problem. Both experimental and analytical studies are being conducted. Presently, a modification to our subsonic wind tunnel is being concluted which will allow more beaningful noise measurements to be made. \rightarrow some sacrifice in velocity, the-test section has been increased in size from 2' x 3' to 4' x 5'. In addition an unechoic chamber has been purchased which will surround the open-jet configuration of the new-test section. Once back in operation, the interior of the tunnel will be systed acoustically in incremental steps to study the effects of such treatment on-the ambient-noise and test-section flow.

The results which have been obtained to date include unsteady pressure measurements on a single-bladed rotor which sweeps through a vortex trailing from a wing mounted in the tunnel shead of the rotor. Most of these results have already been recorded inreferences 1 and 2. Some analytical results, which have not received wide disimination, are to be found in reference 3. Here, numerical colculations of the unsteady flow about a two-dimensional airfoil are presented. A free, point vortex placed in the flow far shead of the airfoil is carried past the airfoil generating an unsteady pressure distribution on the airfoil. The predicted form of the time-dependent pressure distribution is shown to be similar to the experimental peasurements obtained with the rotor in the wind tunnel. Related to the vortex-interaction problem are the results of a brief mulysis which the author performed while a consultant to the U.S. Army Acronautical Research Laboratory at NASA Ames. A recent extension of this work has shown that a simple two-dimensional approximation to the rotor blade slap problem predicts-reasonably well-the nulse spectrum for such a rotor.

The ARO-D studies are concerned primarily with the dynamics of large felicopter rotors and possible means of reducing excessive flapping associated with such rotors. Using a Lagrangian approach, equations of motion are being formulated for coupled flap, lead-lag, and torsional motion of an arbitrarily restrained elastic tlade. Hopefully it is planned to calculate the instantaneous air loads for the rotor blade using a free wake analysis beginning with the rotor blade at rest. Initially, however, the usual-strip method will be used for determining the air loads in order to proof the numerical problem for calculating the rotor dynamics.

The possibility of reducing the blade flapping by means of an oscillating jet flap is being investigated. The position of this flap will be controlled by sensing in some manner the rotor

⁽¹⁾ Spaceted by NASA Langley under contract WGR-39-009-111

⁽²⁾ Sponsored by ANO-Durham under contract=DA-ANO-D-31+124-71-613

blade displacement and acceleration. The analytical formulation of the problem is presently underway and an asymptotic expansion technique, which has been applied to the steady-state problem, is being extended to the unsteady jet-flapped wing. Presently a fluidic control system is being considered for control of the position of the jet flap. It is plauned to construct and test a two-dimensional model of such-a device.

Vortex Interaction Studies

The experimental apparatus pictured in figure 1 is described in detail in reference 1. This single-bladed, counter-balanced rotor blade as a 1 foot radius, 2 inch chord, a 0015 airfoil section and is equipped with 5 ministure absolute-pressure transdurers. Measurements have been made to date of the unsteady chord-wise pressure distributions at the .75, .85, .9 and .95 radius stations for various vortex strengths, rotor advance ratios and sotor positions relative to the vortex center. Typical results are present ... In figures 2, 3, and 4.* These measurements were obtained by recording photographically the outputs from the pressure transducer on an oscillos.ope. The photographs were then transferred to-IBM cards using a trace reader and the results measured on one side of the blade matched with the corresponding results from the other side and processed through a digital computer. From measurements such as these the following tentative conclusions have been drawn.

 The maximum lift coefficient difference, 201, and their time variations, as defined in figure 2, are a maximum when the rotor intersects the center of the vortex.

2. Values of LC_1 at high as 1.15 at 0.75k and 0.75 x 10^3 /sec for $\frac{LC_1}{\Delta t}$ at 0.9k were measured in the present experiments.

3. $LG_1 = and \frac{LG_1}{dL}$ increase approximately linearly with vortex strength with the slopes being different for different rotor plane









Fig. 6. Farlation of 20g with Spin

4. δC_{j} at each open station increases as the shaft axis is moved away from the vertex axis (lie. as the intersection angle decreases).

5. At a particular Z/R, $\Delta C_{\rm L}$ at the inheard span stations are higher then these at the outboard span stations. However, no definite trend exists in the case of the time variation of maximum lift. difference; i.e., $\frac{\Delta C_{\rm L}}{\Delta t}$.

STUDIES RELATING TO STEADY AND UNSTEADY AERODYNAMICS OF HELICOPTER ROTORS

A two-dimensional formulation of this problem was performed in reference 3. The procedure is illustrated in figure 5. More a thin airfoil-is divided into increments with a discrete vortex placed at the "quarter-chord" point of each segment with the boundary condition being satisfied at the "three quarter-chord" point of each segment. The vortex, at zero time, is placed in the flow far shead of the airfoil. The ensuing unstrady problem is then calculated as the vortex is allowed to move with the flow past the airfoil. At each succeeding time increment induced velocities-are calculated at the position of the free vortex and each control point along the airfoil. The strength of the discrete vortices are then found which will-satisfy the boundary-conditions.

Naving determined these the unsteady pressure distribution on the sirfoil is then predicted using the unsteady Bernoulli equation which leads to the following expression for the instantaneous lift.



Figure 5 Simulation of Two-Dimensional Aitfoll by Point Vortices

A typical-result from reference 3 is presented in-figure 6. In this-instance the experimental results have been normalized in terms-of the maximum peak lift coefficient to illustrate that the_prediction of the form of-the time-wise variation of the sectional lift coefficient agrees with the experimental result. The magnitude of the experimental results were considerably below those-predicted by the two-dimensional analysis but as pointed out in_reference 3 this_discrepancy could easily be attributed to tip_losses associated with the three-dimensional-flow of the rotor. A typical comparison, corrected for such-losses is presented in figure 7. For h/c values or -25 and -5 the_predicted ΔC_1 agrees fairly-well with the measured results. However for h/c of 0.1 the two-dimensional predictions are high, probably due to the reduction in the tangential velocity in the vortex core which is neglected in the calculations.

Nore recently Johrson, as reported in reference 4, has developeda-lifting-surface theory which is applicable to th, rotar bladcvortex interaction probles. Although not shown on figures 2, 3 and 4, his results agree closely with the experimental measurements presented in those figures. A sound movie accompanys this paper. This movie was taken as the plane of rotation of the rotor was gradually moved through the vortex generated by the wing shead of the rotor. As this is done one can observe on an oscilloscope the output of a pressure transducer on the blade as it develops a sharp spike. Simultaneously the noise produced by the vortex interaction is distinctly heard.







An Approximate Relationship Baturan Blade Loading and Far-Fisid Major for the Condition of Blade Slap

By comparison with the noise spectrum for a rator without blade slop, the noise levels for the slopping rotor exhibits much higher harmonics than the ordinary rotor. If the assumption is made that the noise produced by blade slop predominates the rotor noise and is generated by a discrete disple source resulting from a timevarying concentrated force, F(c), then it is possible to relate

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F(t) to the noise spectrum. The time, through the rotor angular velocity, can be related to the azimuth angle ψ , hence $F(\psi)$ can be obtained from F(t).

The nonhomogeneous wave equation governing the radiation from a stationary dipole source is

$$\nabla^2 \cdot \mathbf{p} - \frac{1}{c^2} \frac{\partial^2 \mathbf{p}}{\partial t^2} = \nabla \cdot \overline{\mathbf{p}}$$
(1)

 \overline{P} being the external force per unit volume acting on the fluid. c is the acoustic velocity and p the pressure. The solution to this equation for a concentrated force P(t) can be found in several

(2)

references and is given by $p(x,y,z,z) = -\frac{1}{4\pi} \text{ div } \left[\frac{\hat{F}(\hat{z} - \frac{S}{2})}{S} \right]$

 $\overline{F}(t - \frac{S}{C})$ means that $\overline{F}(t)$ is to be evaluated at the "retarded time," $(t - \frac{S}{C})$ with S being the distance from the source to the observer. To simplify the algebra, let us place the origin of the coordinate system at the concentrated force with the observer located in the x-z place. The distance S then can be written as

S-= V2+ 2

Also, to further simplify matters, let the direction of \tilde{F} be along the 2-axis. Equation (3) then becomes

$$p(x,z,t) = \frac{1}{4x} \left[\frac{Fz}{s^3} + \frac{z}{s^2} F'(t - \frac{s}{c}) \right]$$
(4)

F' is the derivative of \vec{F} with respect to time and, again, is. evaluated at the tetarded time. For the for field, the first term on the right side of Equation (4) will be small and is neglected leading to

 $\tilde{p}(x,z,t) = \frac{z}{4\pi s^2 e} F'(t-\frac{\tilde{s}}{c})$ (5)

The above equation suggests_the interesting possibility of integrating the output from-s pressure microphone to obtain F(t) directly.

The curve labelled "with slap" in Figure (8), taken from reference (5), is a 10 cycle band width noise spectrum for a two-bladed rotor operating at 314 rpm and a tip Mach number of 0.9 on the advancing blade. The rotor diameter is 48" and the chord is 1.72". The fundamental-blade passage frequency is 10.5 hz.

Consider now the following closed-form solution which is a two-dimensional equivalent of the solution to the rotor obtained in reference (6).

-Consider a row of blades-spaced a distance D apart having a uniform chordwise loading as pictured in figure 9. The-loading on each blade is zero except as a blade passes through a pulse F(x). Then the total chordwise load is F(x). The problem is to calculate



the noise level at a point x_1 , x_1 as a function of the cho.d, a; spacing, D; velocity, V; and F(x).

Assuming a concentrated force P(t) at x which radiates only when covered by the blade, F(t) will appear as shown in figure (10). P(t) is periodic with a period of \tilde{D}/V . Let

$\theta = -2\pi \frac{k}{T} = 2\pi \frac{\pi}{D}$

Then F(t) can be expressed as

$$F(t) = F_0 + \tilde{L} F_B e^{\ln \theta}$$
(6)

If we arbitrarily let $\theta = 0$ in the center of the pulse, then

$$F_n = \frac{F(x) \, dx}{n^2 a} \sin \frac{n^2 a}{D} \tag{7}$$

$$-F_{0} = \frac{F(x)}{2\pi a} dx \qquad \int d\theta = \frac{F(x)}{D^{-}} dx \qquad (8)$$
$$= \frac{TA}{D^{-}}$$

Hence F(t) becomes

$$F(t)^{-} = \left[\begin{array}{c} F(x) \\ D \end{array} \right] + \begin{array}{c} T \\ T \\ \pi^{-} \end{array} \left[\begin{array}{c} F(x) \\ T \\ \pi^{-} \end{array} \right] \sin \left[\begin{array}{c} \pi \tau_{a} \\ D \end{array} \right] \cos \pi \theta \right] dx \qquad (9)$$

Now 0 was chosen to be zero for a time t = (x + a/2)/V. Hence,

$$\theta = \frac{2\pi}{2} \left[t = \frac{2\pi + a}{2V} \right]$$
 (10)

F(t) then become

$$F(t) = \left[\frac{F(y)}{D} + \int_{n=1}^{\infty} \frac{F(x)}{7ne} \sin \frac{n\pi e}{D} \cos \left(\frac{27nVT}{D} \right) = \frac{27nx}{D} - \frac{n\pi e}{-D} \right] dx$$
(11)



Spatial Variation of Force on Blade Row
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Time-Variation of Force at X

In order to calculate the acoustic pressure p(x,z,t), from equation (5), the above is differentiated with respect to time. Hence for the far field,

$$p = \frac{V_z}{2\tau_a Ds^2 c} \sum_{n=1}^{\infty} \sin \frac{n\tau_a}{D} F(x) \sin \left(\frac{2\pi_0 VT}{D} - \frac{2\tau_0 x}{D} - \frac{n\tau_a}{D}\right) dx$$

Now let us expand F(x) as follows

$$F(x) = A_{0} + \sum_{k=1}^{\infty} A_{k} \cos \frac{2\pi kx}{\lambda}$$
(13)

Substituting the above into the expression for p, the nth hermonic of the mean pressure over one cycle becomes,

$$\tilde{p}_{n} = \frac{V_{\mathcal{E}}}{2\pi a D S^{2} c} \frac{1}{\pi/2} \sin \frac{n\pi a}{D} \sin \frac{n\pi 1}{D} \left\{ \frac{2A_{D}}{\frac{n\lambda}{D}} + \sum_{k=1}^{\infty} \frac{(-1)^{k}}{(\frac{n\lambda}{D})^{2} - k^{2}} \right\}$$
(14)

To examine the behavior of the above consider the case where $A_{\rm g}=0$, i.e., F(x) is a pulse. In this case

$$\tilde{p}_{n} = \left[\frac{\Psi_{RAO}}{\pi^{2}/2} \frac{1}{4S^{2}c}\right] \frac{1}{n} \sin \frac{n\pi_{B}}{D} \sin \frac{n\pi_{A}}{D}$$
(15)

The above shows that \tilde{p}_n decreases as $\frac{1}{n}$ and further, if $\frac{na}{D}$ or $\frac{n1}{D}$ should be close to an integer, $= \tilde{p}_n$ for these particular n values will be low.

The predicted noise spectrum, in db, will be given by 20 log P.,

or

$$db = C_n + 20 \log \frac{1}{n} + 20 \log \sin \frac{n\pi a}{D} + 20 \log \sin \frac{n\pi \lambda}{D}$$

(16)

(12)

In the above C_n is a constant of proportionality corresponding to the constant terms in the squate brackets of equation (13).

Referring to figure 8 it appears-likely that, for the slapping case, the sharp decrease in the levels at about 60 and 150 hz result-from the width of the region of impulsive loading. A d/λ of 6.7 appears to fit the shape of the spectrum best corresponding to a ψ of 27°. D/a for this=rotor is approximately 40, hencr-this term would not be expected-to have much-affect except near a frequency of approximately 400 hz.

Figure (11) presents again the spectra with blade slap of figure (8), together.with equation:(16) with and without the sin terms. The simple two-dimensional approximation to the slapping-rotor appears to characterize the spectrum surprisingly well. The decrease of the maximum envolope above:10 hz. is predicted-fairly closely as well as the shapes of the valleys and peaks. Formulation of the Structural Dynamics of Elastic Rotor Blades

Presently rather complete equations defining the response of fully articulated elastic rotors to arbitrary aerodynamic forces are buing formulated. Three degrees of freedux are being considered; finpping, lead-lag, and torsional. Generally these three motions are coupled, not only because of the structural properties of the blade, but also because of the nature of the seredynamic forcing functions. The three unknown displacements which are functions of time and spanwise position will be obtained from three simultaneous equations derived using a Lagrangian approach. For a non-conservative system the Lagrangian form of the equations of motion are well known and cam be written as



 $\frac{d}{dt} \left(\frac{\partial L}{\partial q_i} \right) = \left(\frac{\partial L}{\partial q_i} \right) = Q_i \qquad (i = 1, 2, 3) \qquad (17)$

where L, the Lagrangian, is the difference between the totalkidetic energy. T, of the blade and its potential energy. V. Q_i is a non-conservative force and q_i a generalized coordinate. The contribution to the total kinetic energy of the blade results from its linear and angular motions due to flapping, its in-plane linear and angular motions and the torsional deflections of the blade about its elastic axis. In writing the kinetic energy terms due to angular-displacements of a modified Bernoulli-Fuler beam theory is being used where both the angle of rotation of the beam cross section and the angle of shear deformation are considered. Nence the following two relationships are obtained by considering the flapping and lead-lag actions:

 $\frac{2}{2\pi}$ {W(x,z)} = $\xi(x,z) + \gamma(x,z) = 8$

(18)

$$\frac{3}{3x}$$
 (h(x,t)) = n(x,t) + t(x,t) = 2

where:

- w linear displacement of section in flapping from reference (Fig. 13)
- a linear displacement of section in lead-lag from reference (Fig. 1))
- 8 flapping angle of elastic blade
- c = lead-lag angle of elastic blade
- 4 cross-section angle-of-rotation in flapping

n = cross section angle-of-rotation in lead-lag

 γ = angle of shear deformation-in flapping

t = angle of shear deformation in lead-*ag

The total potential energy of the blade is the sum of that due to gravity and the strain energy due to blade deflactions. This latter energy must include the strains due to flapping, lead-lag, and toreional deflections as well as the strain due to stresses resulting from centrifugal forces. The gravity potential energy is written relative to the initial vertical displacement of the blade in its drooped position. With the Legrangian being calculated as just described, the next step in deriving the three dynamical equations for a blade is to examine the dynamic equilibrium of a differential element of a blade. Such an element with the forces acting on it is shown in Figure-13. Here for simplicity only, flapping motion is-considered. Notice that the rotary inertia term, J_B-dx, is considered in the equilibrium of the element and is an additional modification to the classical Bernoulli-Euler beam theory. If we take as a generalized coordinate, w, the displacement of the blade from a reference position of a pseudo-rigid rotor weithen obtain,

$$\frac{d}{dt} \left(\frac{\partial L}{\partial u}\right) = \frac{\partial L}{\partial u} = F_{u}$$
(19)

where F_{ij} is the sum of the non-conservative forces atting on the element. Summing moments about the center of mass results in $\frac{\lambda^2}{r_1} \frac{\lambda^2}{r_2^2} (\phi_e + \mu) = -\frac{\partial H_i}{\partial x} + S_i + F_c \sin(\theta_e + \theta)$ (20)

where σ_1 is the blade-mass per unit-length and \mathbb{I}_2 is the moment of inertia about the z axis. These-equations,-(19) and (20), are related by the following equations

$$EI_{z} \frac{1}{3x^{2}} + N_{u}(x)$$

$$\frac{3}{3x} \left[EI_{z} \frac{x^{2}u}{3x^{2}}\right] = -\frac{3N_{u}}{3x}$$

$$\frac{1}{3x^{2}} \left[EI_{z} \frac{3^{2}u}{3x^{2}}\right] = -\frac{3^{2}N_{u}}{3x}$$
(21)

After considering algebraic reduction the preceding equations reduce to the following_equation governing the flapping motion of the blade.

$$\frac{\partial}{\partial x} \left[\varepsilon_1 t_x \frac{\partial^2}{\partial t^2} (\theta_e + \beta) \right] = \left[\left(-\frac{1}{\cos^2 dx} \left[\frac{\partial}{\partial t} \left(\frac{\partial L}{\partial v} \right) - \frac{\partial L}{\partial v} \right] \right] + q_L - \frac{\partial F_e}{\partial x} \frac{\sin^2 \theta_e}{\cos^2 \theta} \right] + \frac{\partial^2}{\partial x^2} \left[\left[E t_x \frac{\partial^2 v}{\partial x^2} \right] + \frac{\partial}{\partial x} F_e^{\sin^2 \theta} \left(\frac{\theta_e}{\theta} + \theta \right) \right]$$
(22)

Sinttarial for the lead-lap pottor.

$$\frac{\partial}{\partial \pi} \left[\left(\sum_{i=1}^{2} \frac{\lambda^{2}}{2e^{2}} \left(\left(\sum_{i=1}^{2} + p \right) \right) \right] - \left(\frac{1}{\cos p} \frac{1}{d\pi} \left(\frac{\lambda}{dt} \left(\frac{\lambda I}{\lambda h^{2}} \right) - \frac{\lambda I}{\partial h} \right) \right]$$

$$= q_{D} + \frac{\partial F_{c}}{\partial \pi} \frac{\sin n}{\cos \sigma} \frac{\Gamma}{c} - \frac{\lambda^{2}}{2\pi^{2}} \left[\tan \frac{\lambda^{2} I}{2e^{2}} + \frac{\lambda}{2\pi} \left[F_{c} \sin (0 - \Gamma) \right] \right]$$
(23)

and for torsional motion,

$$\frac{d}{dt}\left(\frac{3\sigma_{T}}{2}\right) = \frac{3\sigma_{T}}{2} = \frac{3}{2}\sigma_{T} = \frac{3}{2}\sigma_{T} = \frac{3\sigma_{T}}{2} = \frac{3\sigma_{T$$

These then are the simultaneous equations which are to be solved for the two linear displacements, w and h, and the angular displacement, $-\theta_{\rm g}$. The cross section of a typical blade is shown in Figure 14. Generally the three motions of the blade will be coupled since the center of gravity of each section, its elastic ames, and the center of pressure are not coincident. If the



Figure 14. Typical Blade Section

elastic axis is-displaced upward an amount w and the section is twisted through an angle of $\theta_{\rm t}$ than the displacement of the CG from Figure 14 will be

u =:v − eθ,

This coupling between the linear and angular displacement must be considered when writing the kinetic energy for the linear flapping motion. For example,

$$T_{BL} = \frac{1}{2} \int_{e}^{R} n V_{B}^{2} dx$$

wherei

$$\nabla_{\mathbf{g}} = \left[\left(\mathbf{r} - \mathbf{e} \right) \frac{\mathbf{\hat{g}}}{\mathbf{e}} + \frac{\mathbf{\hat{u}}}{\mathbf{u}} \right]$$
$$= \left(\mathbf{r} - \mathbf{e} \right) \frac{\mathbf{\hat{g}}}{\mathbf{e}} + \frac{\mathbf{\hat{u}}}{\mathbf{u}} = \mathbf{e} \frac{\mathbf{\hat{u}} + \mathbf{\hat{u}}}{\mathbf{u}}$$

Fortunately Jt-has been shown by others that for a slender beam, the three dynamic:equations (22), (2)), and (24) can be unroupled before solving for w, h, and $\theta_{\rm g}$. In order to obtain the kinetic energies associated with the blade motions the blade will be divided into lumped massee-and then a normal mode approach assumed of the form

$$w(\mathbf{x}, \mathbf{t}) = \frac{\overline{\mathbf{z}}}{\mathbf{z}} + \frac{1}{\mathbf{z}} \mathbf{x} \cdot \mathbf{q}_{\mathbf{1}}(\mathbf{z})$$
$$h(\mathbf{x}, \mathbf{t}) = \frac{n}{\mathbf{z}} + \frac{1}{\mathbf{z}} \mathbf{x} \cdot \mathbf{q}_{\mathbf{1}}(\mathbf{z})$$

$$e_0 \theta_{T}(x,t) = \sum_{\substack{i=n+1\\t}}^{n} d_i(x) q_i(t)$$

where e is an arbitrary-length defined so as to maintain consistent dimensions for the ϕ_i terms. $\phi_i(x)$ is the spanwise dependent function and q_t(t) is the time dependent generalized coordinate. These functions which must-satisfy the boundary conditions for the three types of displacements can be obtained from the uncoupled natural modes of the beam. Thus the equations are reduced to an Eigen-value problem which can be solved by the usual matrix method to obtain the natural frequencies and-Eigenvectors-for the generalized coordinates e, (t). In order to calculate the blade motion from these equations the blade will be started initially from rest at-the static droop position. The instantaneous actudynamic forces and moments acting on each blade section will be determined from a consideration of the local instantaneous velocities acting at the blade section. Ultimately:it is hoped that this program can be combined with a free wake analyses of the rotor blade. It is realized however that such a program will be very-time consuming and it may therefore take a considerable effort to evolve one which is economically feasible. In the interim some sort of a strim method, probably using a uniform downwash assumption, will be utilized to calculate the aerodynamic = loads. In any event it is planned to account for reverse flow effects, blade dynamic stall and Nach number.

Studies of a Jet Flap for Rotor Control

In order to reduce the excessive:flapping and coming associated with large helicopter rotors both analytical and experimental studien are underway to investigate the practicability of applying a controllable:jet flap to such a rotor. It is not planned, at least at this time, to actually drive the rotor with the jet:flap but rather to provide only enough jet blowing for the required control forces. The position of such a jet flap would be controlled automatically by sensing both the blade acceleration and its local angle-of-attack. These signals would be fed back to the jet.flap in order to provide aerodynamic forces which would oppose the motion of the blade.

As the present time, because of sts potential simplicity, the possibility of using a fluidic control system is being invectigated. The same pressure sources which supply the flow for the jet flap could be used to power the fluidic device. One such possible scheme is pictured in Figure 15. Here the jet flap is basically a digital or bistable fluid amplifier. When a control flow, q., is applied through the lower control port the jet flap will separate from the bottom surface emiting through the top channel thus producing an upward deflection of the jet. A similar jet flap design considered by Eastman (Reference 12) was shown to require a control flow equal to approximately 11% of the primary flow at the jet flap. The stagnation pressure required in the control flow-is also approximately the same fraction of the stagnation pressure in the mean jet; thus, there should be no difficulty in obtaining the required control power from the main plenum chamber.

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There are two possible ways that a signal reluted to an angleof-attack of a blade suction can be obtained. First consideration is being given to measuring the difference in pressures between

> Figure 13 JET FLAP DE'/ICE



corresponding points on the upper and lower surfaces of the alsfoll. Secondly, since-the acceleration will-be needed anyway, she might integrate this signal in order to obtain an output proportional to the vertical velocity of the blade. One difficulty here, however, might be the fact that this velocity=is only one factor which determines the angle-of-attack. The-acceleration schenris-envisioned as a jet of air which deflects under acceleration. The deflected let thas enters one of two receivers and is then amplified to control the jet flap. The final control scheme which is devised will be tested in our-4-x 3 foot; wind tunnel: at a velocity of approximately 100 ft/sec. using a two-dimensional, jet-flapped sitfoil model. From some preliminary considerations on the size of large helicopters it_appears as if a range of reduced frequencies_of from we/V = .06 up-to approximately .5 should be investigated. Cr values as high as .6 should probably be studied corresponding_to conditions on a retreating blase,

In addition to the experimental studies an analytical investigation to predict the performance of an oscillating 3-dimensional jet flap is being undertaken. Using a matched asymptotic expansion approach, the work of Tokuda (heference 14) for the steady threedimensional jet-flapped wing is being extended to the unsteady case. Figure 16 illustrates the geometry of the problem.

The inner region is-close to the wing, i.e. $X = \{l_A^{\pm}\}$ assuming a large aspect ratio wing whereas the outer region implies $X = \{l_A^{\pm}\}$ any from the wing. The approach in this case-is to expand the uniterally velocity potential and deviation in the regions using the reciprocal of mapect ratio as the small parameter. The so called

STUDIES RELATING TO STEADY AND UNSTEADY AERODYNOMICS OF HELICOPTER NOTORS

Figure 16

JET-FLAPPED WING

SIDE VIEW





inner and outer expansions are matched in the intermediate region along the X main. Since the flow is assumed incompressible, Laplace's equation governs the problem.

 $\varphi_{XX} + \varphi_{XX} + \varphi_{XX} = 0 \tag{25}$

The downwash boundary conditions_are given as:

on the ving
$$u_y(x,y,0,z) = 0 - \frac{c(y)}{2} < x < \frac{c(y)}{2}$$
 (26)

at the trailing edge
$$\Theta_t(x,y,0,t) = U_t e^{i\Psi t} X = C$$
 (27)

sesuring small To

$$m \text{ the } [\text{tet.} U_j(x,y,0,x)] = \frac{\partial h_j}{\partial x} + \frac{U_m}{\partial x} \frac{\partial h_j}{\partial x}$$
(274)

$$= h_0(x,y) \log^{1+t} + U_{\mu} \frac{\partial h_1}{\partial x} \quad (27b)$$

The third boundary condition is arrived at from the assumption of small transverse momentum in the jet sheet"(momentum in the y direction). The contention is that the edge of the jet does not begin to roll up until it is far enough domnatream that it nas a small effect=upon the induced_downwash in the near wake. Mashell and Spence-(Ref. 15) give the=pressure difference across the_three dimensional=jet sheet as,

$$p_1 = p_u + k_z - J(y)$$

kg - curvature in etreamvise direction

J(y) - jet memonium flux per unit-open

The y co-ordinate enters only as a parameter. The singularity due to flow discontinuity at the trailing edge has a small effect. Also, far from the wing and jet_the flow must-be uniform.

$$x^{2} + y^{2} + z^{2} + z \neq 0$$

Outer flow:

To an observer in the outer region the large aspect ratio wing appears as a lifting like with a trailing jet sheet. The boundary condition on the jet sheet is satisfied directly whereas that on the wing must be satisfied through matching with the inner solution. The outer expansion is witten as

 $\phi^{\circ}(x,y,z,z, 1/A) = \phi_{1}^{\circ} + \frac{1}{A} \phi_{2}^{\circ} + \frac{1}{A} 2 \phi_{3}^{\circ} + ...$

$$(29)^{0}(x,y,z,t, 1/A) = \omega_{1}^{0} + \frac{1}{-A} \omega_{2}^{0} + \frac{1}{A^{2}} \omega_{3}^{0} + \dots$$

At a fixed field point in the outer region there is no disturbance from the wing in the limit of wery large aspect ratio so,

(30)-

(31)-

(28)

u° = ti<u>a</u>a

Inner flow:

In the inner region the velocity potential and the x and z axes are stretched as follows,

X - AX, Z - AZ,

$$A\phi_{-} = \Phi(x,y,x,t, 1/A)$$

 $\Phi(x,y,x,t, 1/A) = \phi_1 + \frac{2}{A} + \phi_2 +$

 $\omega(x,y,x,t, 1/A) = \omega_1 + \frac{1}{A} \omega_2 +$

Laplace's equation becomes

$$\Phi_{-\pi\pi}^{+} + \Phi_{\pi\pi}^{-} + \frac{1}{A^2} + \frac{1}{yy} = 0$$
(32)-

To obtain the first order inner solution, fix a field point
 x, y, x and=let A + =. From equation (32) the velocity
 potential is seen to satisfy the two-dimensional problem.
 Sponce (Reference 16) has solved this problem and gives the jet height above the mean line as a function of x, in this

jet height above the mean line as a function of x, in this case the inner variable, $h_{j}(X) = u \frac{c}{2} \tau_{0} (x/c/2)^{-1/2} h(\bar{X}) e^{iwc}$ (33)

where
$$\bar{x} = \frac{x-c/2}{\mu c/2}$$

$$u = \frac{1}{4}c_{j} = \frac{1}{4} \frac{1}{\frac{1}{2} + U_{2}^{2}}c_{j}$$

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$$u \ll 1$$
 realistic:assumption Hade:for convenience
h(\bar{x}):= $[\bar{x} + \frac{1}{2}, (\frac{\pi^2}{2}), 1:\bar{x} + \theta(\bar{x}^2),]$ (34)

(34)

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Using the following equation,

the first order inner downwash on the x axis is found as,

$$w_1 = \mu \frac{c}{2} \tau_0 \left(\frac{d}{cT^2}\right)^{-1/2} \left(\bar{x} + \frac{1}{2} \left(\frac{\bar{x}^2}{c}\right) \ln \bar{x} + \dots \right)$$
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ر بیش**ی با میرونی ا ک**امه بوده، به رویه گرور در در

$$= \frac{1}{2} \left(\frac{x}{c/2} \right)^{-3/2} u \tau_0 \left[\bar{x} + \frac{1}{2} \left(\frac{\bar{x}^2}{x} \right) \ln \bar{x} + \theta(\bar{x}^2) \right] e^{i\psi t}$$

$$+\tau_{0} \left(\frac{x}{c/2}\right)^{-1/2} \left[1 + \frac{\bar{x}}{3} - \ln \bar{x} + \right] e^{-i\omega t}$$
 (35)

Equations (37) and (35) satisfy the boundary conditions at the trailing edge. This first order inner downwash will influence the second order outer downwash, w_2 , through the matching process. This is presently being pursued. Only the first three orders should be necessary for accurate results from which the unsteady lift and drag can be determined. Effects of thickness and camber can also be included by appropriately altering the boundary conditions.

This work will be extended to include a partial span jet flap and further a transverse (y direction) shear flow will be. Introduced to better represent the environment of the helicopter rotor.

Acknowledgment

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AS EXPERIMENTAL STUDY OF MELICOPTER ROTOR INFULSIVE MOISE

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WILLIAM E. BAUSCH & ROMALD G. SCHLEGEL

Sikorsky Aircraft Division of United Aircraft Corporation Stratford, Connecticut, U. S. A.

INTRODUCTION

The helicopter generates noise of both mechanical and aerodynamic origin. Mechanical noise, such as that due to the gearboxes, bearings, hydraulic systems, etc., is in most cases important only at locations near the helicopter. Of the scrodynamic sources, such as the main and tail rotors and the engine compressors. sain rotor generated impulsive noise (when it occurs) can be by far the most aredominant noise, exceeding even piston engine exhaust noise (as has been shown recently by Cox and Lynn, Reference 1). While the other serodynamic sources of belicopter poise (notor rotational noise, rotor vortex poise, turbing engine compressor noise, etc.) have been studied in quite some detail during the past fer years, rotor impulsive noise (RIN) has been generally referred to as a unique and separate phenomenon and has been largely isnored until very recently. The present reper-gives results of a study of RIS, sponsored by the U. S. Army AMRDL, that sought to identify the mechanisms causing RIN, to determine if RIN is primarily rotational or broadband, and to check the ability of an existing accusic analysis to calculate characteristics of RIM. Reference (2) contains more detailed descriptions of the experimental program, the acoustic analysis, and the correlation study.

Noise and rotor airloads were measured simultaneously rop-flight conditions of hover, 120 kt., 150 kt, and 170 kt. The flight test vehicle was a CN-534 helicopter configured for a neutral center of gravity and nominal gross weight of 35.000 pounds. One main rotor blade varied flush-mounted pressure transducers at 5 chordwise stations for each of 5 spanwise stations. Figure 1 shows the configuration of the aircraft and of the instrumented rotor blade. The frequency response of the aircraft and of the instrumented 30 harmonics of airload to be extracted from the data with an accuracy of 125 of full scale on vibratory measurements and 135 of full scale on steady measurements.

During the flight test, RIN was observed only during hover and 170 knotflight. Principal conclusions are 1) that RIN is a form of rotational noise, 2) that hover RIN is essentially an aerodynamic process involving the interaction of the main rotor with its own and/or tail rotor vortices, 3) that high-speed RIN is caused by the combination of a moving source accustic process and an aerodynamic process associated with blade drag, and b) that an existing acoustic analysis predicts qualitative differences between flight-conditions with and without RIN, but that quantitative correlation of RIN is deficient due to (1) the lack of profile drag and moving source terms in the malysis and (2) the current-inability to predict the higher harmonics of airload necessary to predict the higher acoustic harmonics.

CENERAL DISCUSSION

Several investigators (References 1, 3, and 4) have postulated that the observed character of impulsive noise from rotors is due to severe amplitude modulation of broadband noise. While this phenomenon can be observed during RIN conditions, it is highly unlikely that it is the sole cause of the impulsive acoustic waveforms which are perceived by an observer as impulsive noise. RIN occurs at-the rotor blade passage frequency and is primarily a harmonic phenomenon whose origin appears to be ordered rotational noise rather than random broadband noise. A Fourier analysis of periodic impulsive thise produces a frequency spectrum with very high harmonic content and relatively little amplitude decay with frequency. This has recently been demonstrated analytically by Lowson and Ollerbood (Reference 5) and Leverton (Reference 6), and experimentally by King and Schlagel (Reference 7). King and Schlagel found that during nonimpulsive noise conditions, blade airloading harmonics decay with harmonic order, λ , approximately as $1/\lambda^{1.4}$ to $1/\lambda^{1.6}$ while during impulsive noise conditions the airloads decay about as $1/\lambda^{0.6}$. The increased high frequency airloading harmonic levels for the impulsive noise case result in increased high frequency sound harmonic levels. yielding the observel "slap". Furthermore, the phasing of the sound harmonics is important in determining the impulsive nature of the observed sound; for_example, a harmonic apactrum with harmonics phase shifted by 90 degrees with respect to the fundamental may be more inpulsive than one with all harmonics in phase. In a recent paper, Sadler and Lory (Reference 8) indicate that the high frequency content of RIN may be primarily associated with worter (broadband) noise. This, too, appears to be highly unlikely since vortex noise is random in amplitude. frequency, and phase. Consequently, it does not contain the necessary harmonic content and phase coherence necessary to define an inpulsive sound.

The effect on acoustic waveform of harmonic amplitude and phase is shown in Figures (2) and (3). Figure (2)-compares waveforms for noise harmonic_falloffs of 3 db/ octave and 10 db/octave, from which we conclude that RIN requires a rotational noise spectrum that is fich in harmonics. Figure (3) shows the radical change in waveform that is caused by shifting the phase of all harmonics-90 degrees from those of Figure (2).

HOVER RIN

The statement that ispulsive noise during hover-involves strong blade/vake interactions is supported by the flight data. Comparison of airload amplitude-refrequency spectra_shows that many more harmonics are present for the RIN case than for the RIN-free case. This increase in high frequency-loading raises the higher harmonics of noise, thereby satisfying one requirement for RIN. The location of the main rotor blades at the instant of impulse generation corresponds to the stimuthal region of maximum airload_fluctuation during hover. This was determined by relating acoustic-impulses recorded at 3 locations inside the helicopter to the locations of the rotor blades at the instant that the noise was generated.

Interactions of rotor blades with acrodynamic wakes cause the rapid airload fluctuations that produce RIW during hover. Clark and Leiper (Reference 9) Semonätrated analytically that a vortex_frequently will rise above the rotor disc_plane before starting down during ideal hover of a 6-bladed main rotor, but this behavior does not guarantee blade/vortex intersections. Intersections frequently occur in a real hover because the wake respondator reflections from the ground plane and small wind disturbances which induce blade flapping and further changes in the wake structure. Figure (4) shows how blade/wake intersections affect the asimuthal variation of airloads during hover. In this case, the impinging vortices came from the tail rotor during hover OGG with the tail rotor upwind of the main rotor in a 10 knot ambient wind. Intersections of main rotor blades with main rotor tip vortices were not indicated from the data of this particular fright test.

HIGH-SPLED NIN

The impulsive noise observed during 170-knot flight appears to be primarily an acoustic event, rather than an accodynamic event as was the case during hover. The airload amplitude - frequency spectra for cruise with and without RIX phoved no strong differences, and acoustic impulses were not detected inside the helicopter.

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Stationary observers on the ground heard RIM only at large distances in front of the helicopter. These observations lead to the conclusion that motion of the noise source toward an observer is a major source of high-speed JIM.

This form of RIN was originally thought to be due to the formation of weak local shock waves on the advancing blady. As mentioned by Ollerhead and Lowson (Reference 10) and discussed by Leverton (Reference 6), an observer can hear such a shock wave only if the blade speed is supersonic. If the blade speed is subsonic. the shock wave can not propagate to an observer's ear. However, the formation of local shocks can affect rotor noise levels by influencing the local airloading acting on the blade. High-speed RIN as discussed in Reference 10 is basically an accustic effect resulting from the confescence of the harmonic wave fronts at high source translational speeds and can be explained by the Lowson/Ollerhead theory. The predicted increase in levels of higher-order noise barmonics with increasing tip speed is independent of the loading spectrum and satisfies one of the requirements for RIN. The highly directional characteristic of high-speed RIH noted by observers on the ground track is an acoustic effect which results from the forward speed correction where the distance term, r. is modified to reflect the rotor's Mach number toward an observer by substituting r(1-M_) in the argument of the Bessel functions, thus influencing the directivity characteristics. This effect can be seen in Figure 5, taken from Reference 5. As forth ' speed increases, the radiated sound becomes highly_directional in the forward direction, particularly for the higher harmonics. This means that the RIN experienced by a helicopter at high speeds will be radiated perferentially forward with the maximum at about 15-20 degrees below the plane of the rotor. This effect was shown experimentally by Cox (Reference 11) in full-scale wind tunnel tests. Thus, the acoustic effect of a high-tim Mach number is at least partially responsible for the generation of the inculsive noise and the mircraft forward speed accounts for the highly directional character of this type of RIS.

The serodynamic forces used in current acoustic theory to predict-rotational noise are the in-plane (induced drag) and out-of-plane (thrust) components of the blade section lift. The profile drag is ignored, since it is generally small conpared to the other terms. When advancing tip speeds exceed a critical Mach number. however, the drag increases rapidly due to drag divergence. This increased drag say be a significant contributor to the radiated noisy. In a recent paper, Arnit and Borgman (Reference 12) examined the effect of drag divergence on the radiated noise. The effect of this drag term is to increase the levels of the higher have monicy of noise, a necessary condition for impulsive noise. While Arndt and Borgman indicate that the addition of this term-to the Lowson/Ollerhead poise equation enhances correlation, they unfortunately do not show to what degree. For small angles of attack (such as near the tip), the lift term may be quite small and the drag terms will dominate the poise radiation. In this case, the directivity will be that of a dipole with its maximum radiation in the plane of rotation, thus further contributing to the observed directivity of high-speed RIN. An additional factor which may contribute to the observed directivity and character of RIN is thickness poist. While it is not significant for highly loaded rotors at low forward speeds. thickness noise can become significant at high forward speeds. Arndt and Borgman accounted for thickness noise by applying a forward speed correction to the theory developed by Diprose (Reference 13) for a static propeller. No attempt was made to correct for the normalform velocity field over the rotor disk, but the results show that the levels of the higher harmonics of rotational noise increase rapidly As tip speed increases. This effect, coupled with the in-plane directivity pattern of thickness polse will tend to enhance the severity of the observed RIN.

CONSCILATION AND AMALYSIS

Measured and calculated rotor noise data were compared to determine how well an existing acoustic analysis could predict waveform and rotational noise harmonic levels for flight conditions with and without RIN. Waveforms correlated well as can be seen in Figures 6 and 7. RIN was not heard by ground observers during the 140-knot flight that resulted in Figure 6, and the waveforms reflect the absence of impulsiveness. Waveforms for 170-knots and helicopter/observer placement comparable to Figure 6 definitely appear impulsive in Figure 7, which agrees with observers reporting RIN for this flight condition.

Despite the good qualitative agreement between measured and calculated waveforms for the 175-knot case, the unsteady behavior of the calculated waveform between pulses suggests that the acoustic analysis underestimates the h. ther harmonics Figure 8 gives a general indication of the correlation between measured and calculated rotational noise harmonic levels. Measured harmonic levels are consistently greater than calculated ones at distances over 1500 to 2000 feet in front of the helicopter during high-speed forward flight. Consequently, although the calculated waveforms accurately reflect the trends of measured variations with airspeed, these waveforms do not have esough higher-harmonics content to produce the measured steadiness of pressure between pulses. The inability of the analysis to predict the higher-order harmonic levels far in front of the rotor is attributed to the following factors.

- Hotion of the rotor system in the direction of an observer-isnot included.
- Drag divergence aerodynamic forces are not included in determining source strength and directionality.

The acoustic analysis that was used represents the rotor system as a conical surface of dipole radiators inclined at an angle to the ground plane. At any point on this surface, the dipole radiates continuously at integer multiples of the blade passage frequency to produce the pressure field experienced by that point as a blair passes over it. Lamb's nonhomogeneous wave equation is used to transfer the acoustic pressure at the source to the pressure reaching an observer, and the total acoustic pressure field is obtained by integrating the contributions of all source dipoler on the rotor surface for all noise harmonics.

SUMMARY

In summary, a number of important conclusions have resulted from this study. The first of these is-that Rotor Impulsive Holse (RIH) is characterized by an increase in sound pressure level of the higher harmonics of rotational noise, rather than increases in broadband noise amplitude and modulation, with up to 23 harmonics (425 Merts) being measured during RIM.

The second conclusion is that cruise RIM and hover RIM of single rotor helicopiers appear to be generated by different acroacoustic mechanisms. Criise RIM is highly directional with maximum severity occurring directly shead of the helicopter at-small angles below the plane of the main rotor, and appears to result from the combination of acoustic effects of source motion towards an observer at high subsonic tip Mach numbers and of the merodynamic effects of drag divergence. Acrodynamic shock does not repear to be a primary contributor in cruise RIM. Hover ".IN results from high frequency oscillations in airloads commonly caused by blade/wake (main and/or tail) interactions.

The acoustic analysis developed by Sikorsky Africraft under sponsorphip of the Bustin Directorate of U. S. Army AMOU appears this adequate to predict the humonics and time histories of rotor noise fairly well in OGE hover and at moderate distances from the helicopter (up to 1,000-1,500 feet) during cruise

AN EXPERIMENTAL STUDY OF HELICOPTER ROTOR IMPULSIVE NOISE

providing that high frequency harmonic blade airload data are available. The major problem here, however, is that normal data acquisition/processing techniques used in studies of helicopter airloads have not-provided information in the frequency range required for good acoustic correlation. Also, currently available theoretical airloads prediction programs are incapable of predicting the higherharmonic amplitude and phase data that are needed for predicting the higher harmonics of noise. Correlation at large distances from the helicopter (beyond 1,000-1,500 feet) tends to be poor during high speed cruise, presumably due to the analytical omission of source motion and drag divergence effects, and possible atmospheric scattering effects on the highly directional, higher frequency radiating patterns.

FUTURE RESEARCH RECOMPRIMATIONS

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Limited ability of theoretical minibad analyses to predict higher harmonic amplitude and phose suggests that new empirical approaches are required to provide minibad data for acoustic predictions. Such minibad data can probably be most economically developed through the use of acoustic wind tunnel facilities, such as the one recently developed by the United Aircraft Pesearch Laboratories and the one-planned at-SASA Langley.

In addition to the development of such high frequency_mirload prediction schemes, current analyses should be modified to include the effects of source translation as well as profile drag and drag divergence.

A final point which should be made is that although the primary emphasis currently in the military and industrial research and development programs is on the development of hardware for reduced-noise, experience has shown that-only a thorough understanding of the aeroacoustic mechanisms can guarantee a high probability of success. As there are a great many areas of ignorance in rotor noise generation still to be explored, continued support must be given to basic research, such as those programs supported by AROD, if we are sver to achieve quiet vehicles which are economically feasible.







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AS EXPERIMENTAL STUDY OF HELICOPTER ROTOR IMPULSIVE NOISE



18.45

CALCULATED

140 KT, NO RIN, HELICOPTER APPROXIMATELY 500

FT AWAY

NEASURED AND CALCULATED WAVEPOINTS

Figure 6

MEASURED

CALCULATED

Figure 3

170 KT, MAXIMUM RIN, HELICOPTER 500 TO 1000 FT AWAY

MEASURED AND CALCULATED WAVEFORMS Figure T



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A SYSTEMS STUDY- OF MOISE REQUIREMENTS ON THE DESIGN OF V/STOL AIRCRAFT

> Robert W. Simpson Henry B. Faulkner Anthony P. Hays

PLIGHT TRANSPORTATION LABORATORY Massachusetts Institute of Technology

1.0 Introduction

The reduction of helicopter noise in military operations has two main purposes:

- 1) Avoidance of detection, or delay of detection to increase the surprise element of an operation
- Minimization of noise levels in the region of friendly forces to reduce communication loss-due to operations.

The chief elements of heligopter noise are due to vortex and rotational noise from the main rotor and tail rotor, and engine noise. One method of reducing the effect of helicopter noise is to reduce the noise at the source, using techniques such as slowing down the rotors, adding more blades, and using engine and gearbox noise suppression techniques. The first section-of this paper will show the penalties in performance and payload (as measured by operating cost) which result from using this approach.

An alternative method-of reducing the effect of-aircraft noise is to modify the flight profiles-in position and speed. The ability of-the aircraft-to fly the modified profiles may be constrained-by its available thrust, acceleration limits, etc., and some-small penalty may be incurred in fuel or time of flight. The second section of this paper describes a method for finding noise optimal trajectories for a-helicopter takeoff-and climbout.

2.0 Helicopter Design for Minimum Noise Generation

The process for preliminary design of air vehicles can be computerized such that fast, parametric variations can be obtained. These computer programs are now a design tool used to find optimal configurations for required vehicle performance in terms of payload, range, speed, etc. At the Plight transportation Laboratory, we are extending our design programs to include the noise generation of a given vehicle (as best we can estimate it) as one of the performance measures of the vehicle. We then can meet other design objectives at varying levels of noise, or can search for optimal denigns for a specified noise level. The following section briefly describes one such computer program, for helicopters, and shows some of the noise tradeoffs one can study using the program.

2.1 Description of the Helicopter Design Program

a) The Design Logic

The helicopter computer design program is fully described in PTL Technical Memo 71-3 (Reference 1). Briefly, the purpose of this program is to provide a rapid means of investigating tradeoffs between design parameters and various figures of merit, such as direct operating cost and noise-generation. This program considers only conventional pure helicopters.

6.15

The program begins by reading input data such as design payload, range, speed, etc. and generating constants, including atmospheric data, for later use. Calculations regarding hover performance are dong for a hot day, all other calculations assume a standard day.

Then the program goes into a design procedure which is an iteration on gross weight. Initially a gross weight is estimated based on the design-payload; on succeeding iterations the previous gross weight is used. The rotor is then designed considering both cruise and hover. Mext the fuselage is sized and parasite drag is calculated. Then the power plant and drive system is sized to the maximum of cruise and hover requirements. If hover rpm is less than cruise rpm then the installed power required for cruise is increased accordingly. This completes the selection of design parameters.

The vehicle is then flown through the design mission to find the fuel consumed. Ten phases in the mission profile are considered: hover, vertical climb, accelerationto advance ratio .325, unaccelerated climb, acceleration to cruise, cruise, undecelerated descent, deceleration to advance ratio .325, deceleration to hover, and vertical descentthe time, distance and fuel consumed in each phase is calculated. A table of rotor lift to drag ratio vs. advance ratio and thrust coefficient to solidity ratio is used to estimate performance above advance ratio .325. This table was derived from Ref. 2.

Then the component weights are calculated, resulting in a new gross weight. If the difference between new and old gross weights is greater than 10 lbs., the design procodure goes through another cycle. When the iteration is complete the parameters describing the final design are output.

b) Vehicle Operating Cost

Then the vehicle is flown-through various mission lengths-that are less than the design range, with appropriate:cruise altitudes and speeds. The time, distance, and fuel consumed for each phase of each mission is calculated, output, and stored for use in the calculation of direct operating cost (DOC).

Then the program-calculates_DOC's, broker down by categories, for each stage length and prints this out. The DOC is now calculated according to the Lockheed VTOL formula (Mefs. 3, 4).

c) Vehicle Noise Generation

Finally, the program makes calculations regarding the noise generated by the vehicle. Vortex noise: is calculated using the well established formula taken from-reference 5 for an observer at 300 feet distance:

$$L_{p} = 10 \log_{10} \frac{7.62 \times 10^{-10} T^2 (V_{\rm Lip})^2}{2 \lambda_{\rm b}}$$

=L $p \neq \text{oversl}$ sound pressure level, db where $T \neq \text{thrust}, =1b$.

mere $T = Chrust_{i=1}^{i}$

V_{tip} = xotoritip speed, ft/sec = air density, slugs/ft³

 A_{B}^{-} = total rotor blade area, ft²

Simple inverse square law attenuation is assumed for observers at other distances. Directivity effects are not

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considered. This formula is applied to all flight conditions. In cruise the advancing blade tip speed is used.

Contrary to most trajectory optimization problems using dynamic programming, controls are applied at a given state and stage to find the optimum path from the initial conditions to that state, rather than applying controls forward in time and finding the optimal path to the terminal conditions. The main reason for this is that the initial conditions are more precisely defined than the terminal conditions.

3.1.2 Dynamic Hodel of the Aircraft

A dynamic model of the aircraft is shown in Figure 9. \hat{b} and T (and hence the noise generated) are calculated in terms of the state variables, \hat{x} and \hat{h} , and control variables $\Delta \hat{x}$ and $\Delta \hat{h}$.

The system constraints with this program are

```
0 \le x \le 250 \text{ ft/sec}

0 \le h \le 90 \text{ -ft/sec}

-10 \text{ ft/sec}^2 \le x \le 10 \text{ ft/sec}^2

-10 \text{ ft/sec}^2 \le h \le 10 \text{ ft/sec}^2

Power limitation P \le P_{max}
```

Other constraints, such as maximum height, could easily be added-but have not been-implemented at this stage. Initial conditions are

at congretons are		
x = 0	ż	Ō
h = 0	'n	Ō-

Terminal conditions are

ĸ	=	×term
h	-	hterm
	_	

t = t_{term}

Rotational noise was hand-calculated for a sample case using the method of Ollerhead and Lowson, Ref. 6, and another method developed in the Plight-Transportation Laboratory (Ref. 7). Both results indicated that rotational noise was not significant for helicopters with low tip speeds, and thus it has not been included in the program.

The standard takeoff profile assumed throughout the helicopter design procram is shown in Fig. 1. The landing-profile is just the reverse. During the acceleration phase the vehicle tries to accelerate horizontally at the allowable acceleration, and if it has more than enough power to do this, it uses the excess power to climb. Mence the profile varies depending on how much power is available and the maximum acceleration allowed. During the climb phase the vehicle climbs at constant forward speed. The observers are always in the place of the takeoff profile. Varying the height of vertical climb has the effect of shifting the noise profile up or down. Reducing the maximum acceleration chuses greater excess power to be available for climb and hence has the effect of tilting the path upward during acceleration.

As the vehicle accelerates from rest to its verticalrate of climb, thrust is greater than weight and hence extra noise is genorated. The noise resulting from maximum thrust is calculated and assumed to represent the noise in the first few seconds of the takeoff profile.

The noise is calculated at 15 points during the takeoff_profile and output along with the time, altitude and hor-





repeated for observers at different distances from the takeoff point. Noise on the ground due to the vehicle-cruising at:cruise altitude directly overhead is also calculated.

2.2 Typical Results

2.2.1 Melicopter Moise Tradeoffs

A study of the tradeoff between noise generated and DOC, using the helicopter computer design program, has been started. The initial results are shown in Pigures 2, 3 and 4. DOC is plotted vs. perceived noise level in hover for an 16,000 lb. payload tandem helicopter. The DOC is for a multiple hop trip with hope of 5, 20 and 100 miles for a total of 125 miles.

Other symbols on the graphs are as

follows:

 C_{T} = rotor thrust coefficient

σ = rotor solidity

M_{at} = advancing-tip Mach number in cruise

- V_{cr} = cruise speed, mph
- DR = design range,-miles
- \bar{v}_{th} = blade tip speed in hover, ft/sec

V_{ter} = blade tip speed in cruise, ft/sec

DL = disc loading, lbs/ft²

The formula for the calculation of rotor vortex:noise at:300 ft from Ref: 5 may be written as follows for the hover condition:

$$L_p = 10 \log (3.04 \times 10^{-9} (V_{th})^6 A_B C_L^2)$$

where

M_{gr} = vehicles-gross weight

 C_{χ} = average blade lift coefficient

CL = 6(C,/e)

In order to reduce vortex noise in hover it is clear that we must reduce hover tip speed. Nowever, since the same rotor develops very nearly the same thrust in hover and cruise, the following relation applies:

 $1/2 \rho_{\text{hover}} V_{\text{th}}^2 (C_{\pi}/r)_{\text{hover}} = 1/2 \rho_{\text{cruise}} V_{\text{tcr}}^2 (C_{\pi}/r)_{\text{cruise}}$

A safe maximum for (C_{T}/r^{2}) is 0.100. V_{ter} is given by

$$\Psi_{tcr} = \frac{a_{cr}^{H}at}{1+\mu}$$

where

advance ratio a_{cr} = speed of sound at cruise altitude.

Thus we keep μ at a practical maximum of 0.50 and V_{tcr} is proportional to M_{at} . Hence, in order to xeduce noise we must reduce $(C_{\rm T}/\sigma^{-})_{\rm cruise}$ or $M_{\rm st}$. These are the variations shown in Figures 2 and 3, respectively, for different values of DL. These two sets of curves assume that $V_{\rm th}$ and $V_{\rm tcr}$ are independent. This requires either: that there is no variation in engine power or specific fuel consumption with engine rpm over the appropriate range: or, that there is a transmission ratio change between cruise and hover. This assumption is optimistic. The variation in Figure 4 is equivalent to Figure 3 only with $V_{\rm th} = V_{\rm tcr}$, eliminating this Assumption.

The propagation conditions assumed account for geometric spreading only from a nominal distance of 300 ft. There is no correction for ground reflection, effects of air absorption.

Figures 2 and 3 show about 25% increase in DOC for a 6 dB reduction in Sound Pressure Level. In general, reduction of ($C_{\rm m}(r)$) in cruise appears to be a slightly less expensive way of reducing noise than reducing $M_{\rm at}$, except for very low disc loadings. This is because DOC is quite sensitive to cruise speed, which depends directly on $M_{\rm at}$. Also the optimum disc loading is shown to be about 5 for this vehicle. This is somewhat lower than current practice. However, the reduction in hover power-required, and hence in engine and rotor weight, and the cost of maintaining these components, justifies a movement toward lower disc loading. The curves of Figure 4 are similar to those of Figure 3 except they are displaced upward for a given hover tip speed. This is because putting $V_{\rm th} = :V_{\rm ter}$ has reduced $V_{\rm ter}$ and consequently cruise speed.

Unfortunately, there are no presently operating helicopters which are equivalent to the vehicles studied here. The right hand ends of the various curves indicate vehicles which are close to optimal (minimum DOC) without regard to noise. Presently operating helicopters were also designed without regard to noise, and hence, should make roughly the











FIGURE 4 DOC VS LP FOR VARIATIONS IN MAN WITH (CT/+)- (CT/+ HOVER - AND OR CONSTANT

same noise for a given vehicle size. The helicopters under study here are assumed to incorporate 1975 technology. This is reflected in various aerodynamic and structural parameters which are input to the program. Thus present day helicopters would fall above the right-hand ends of the curves. Since they have $V_{\rm th} = V_{\rm ter}$, they would be plotted in Figure 4.

2:2.2 Nelicopter Noise Mistories

Another study has examined the noise perceived by a listener under-the takeoff path of three distinct helicopter designs; one representing a current helicopter, one representing a minimum operating cost vehicle designed using present state of the art technology, and the last representing a quiet vehicle designed using present state of art-technology.

The three vehicles are all tandem helicopters, carrying 10,000 lbs.-payload and a crew of three. They all fly takeoff and landing profiles similar to those previously described, and cruise at 5000 feet. The vehicles are compared in Table I.

The first, called R70, represents what is existing and available now. It is an approximation of the Boeing/ Vertol 347, a helicopter_prototype which first flew in

1

May 1970, except that it has less parasite drag. It has slightly more range than the other two, but does not have the ability to hover after engine failure.

The second vehicle, called MC75, is a minimum DOC vehicle_designed without regard for noisw. It represents what could be flying in prototype form in 1975 using the latest technology. It is an optimal vehicle given the size and flight profile. The single rotor configuration was considered for this and the third vehicle but the comparable single rotor ship was always blightly more expensive to operate and slightly noisier.

Table-1: - Vehicle Comparison

Table It Venicle Comparison	270	HC75	075
Payload, 1b	10,000	10,000	10,000
Cruise Speed, mph	217	252	210
Cruise Altitude, ft.	5000	5000	5000
Range with reserve, mi.	600	400	400
Gross-Weight, Lb	46,140	33,813-	43,003
Engine-out Hover Capability	No	Yes	Yes
Installed Power, hp	7257	5448	6913
Disc Loading, 1b/ft ²	7.0	5.0	5.0
Solidity	.088	.083	. 205
Number= of blades	8	6	Ĝ.
Tip Speed, Hover, ft/ sec	707	640	720
Tip Speed, Cruise. ft/sec	707	672	514
C_/_ Hover	.067	.062	.100
C_/s Cruise	.078	.065	.045
Advance-Ratio in Cruise	.45	.55	.55
Idvancing Tip Mach No.	.935	.950	-750
Lift/drag Cruise	4.86	5.52	5.36
DOC @-100 mi ¢/seat mile	3.87	3.07	4.02
L_ Takeoff @ 500 ft, dB	82	79	70
L_ Cruise @ 5000 ft, dB	64	61	56
-			

The two configurations, however, differ by less than the accuracy of our techniques and hence no definite choice can-be-made.

. The third vehicle, called Q75, is a minimum DOC vehicle designed to have a peak Sound Pressure Level at takeoff or landing of 70 dB at 500 feet_and a peak Sound Pressure Level in cruise flyover of 56 dB at 5000 feet. The 5000 feet cruise altitude was chosen to make the vehicle comparable to the first and second vehicles, but this vehicle couldEcruise at 10,000 feet, making an L_p of 50:dB, with only assmall penalty in DOC. This vehicle also uses 1975 technology and is optimal within the size, flight profile and noise constraints given.

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The direct operating cost (DOC) of the three vehicles is shown in Fig. 5. DOC is shown in dollars per-seat trip which makes a clearer presentation than cents_per seat mile. Each-vehicle could have 50 seats. It can be readily seen that at very short ranges the DOC is about the same for all three while at longer ranges E70 and Q75 cost about the some while MC75 is significantly cheaper.

Figures 5, 6 and 7 show the Sound Pressure -Level versus time duying the takeoff of the three helicopters as heard by three_observers at 500, 1000 and 1500 feet distances from the takeoff point.

Various conclusions can be drawn from these curves. It is clear that Q75 is dramatically quieter, not-only because it generates less noise but because it moves out of the take-



200 NISSICN LENGTH, MI FIGURE 5 DIRECT OPERATING COSTS FOR 3 HELICOPTERS

100

one at lift off (vertical acceleration) and one approximately

off area more rapidly. All of the curves show two peaks,



FIGURE & TAKEOFF NOISE VS. TIME FOR OBSERVER AT 500 FT



FIGURE 7 TAKEOFF NOISE VS. TIME FOR OBSERVER-AT 1000 FT

A SYSTEMS STUDY OF NOISE REQUIREMENTS ON THE DESIGN OF V/STOL AIRCRAFT



FIGURE & TAKEOFF NOISE VS. TIME FOR OBSERVER A 1500 FT

overhead in flyover. Which peak is greater depends_on-the takeoff trajectory and the observer location. The effects of increasing the height of vertical climb and of tilting the flight path upward after vertical climb are similar. This raises the question of the optimal flight trajectory to minimize either annoyance or detection resulting from the noise, and the design of the aircraft capable of flying this trajectory.

3.0 Optimal Noise Takeoff Profiles for a Helicopter

For a given-helicopter with its performance constraints, and noise generation-characteristics, the question-still remains of how to operate that helicopter such as to minimize the noise exposure (by-some criteria) of a given-set of listeners. If an optimal trajectory can be found, then the effects of constraints arising from vehicle performance can be investigated, and a feedback established to the vehicle design process. The following section describes the use of dynamic programming to minimize the annoyance due to noise of a helicopter in the takeoff and climbout:phases of flight on a listener directly under the flight path. A more complete description may be found in References 8, 9.

3.1 The Mathematical Model

3.1.1 Use of Dynamic Programming

A detailed description of dynamic programming may be found in Reference 10; in this example the state variables have been chosen to be horizontal and vertical components of velocity, \dot{x} and \dot{h} . Control variables are discrete differences in the values of the state variables, $\Delta \dot{x}$ and $\Delta \dot{h}$. This affords some simplification of the problem since application of controls takes the aircraft directly from one set of quantized values of state variables to another. This avoids the necessity for interpolation. As it is usually the case the stage variable is taken to be time, t, which is also quantized into discrete values of interval Δt .

Height and ground track at the terminal conditions are unconstrained.

3.1.3 Noise Generation Model and Annovance Criteria



IL AND IC ARE COMPONENTS OF INERTIAL REACTION PARALLEL AND PERPENDICULAR TO THE FLIGHT PATH

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FIGURE 9-DYNAMIC-MODEL OF AIRCRAFT

A noise generation model is required which predicts the sound pressure level in octave bandwidths at any point on a sphere of given radius centered on the aircraft. From a knowledge of attenuation due to spherical spreading, ground effect and atmospheric attenuation, the sound pressure level in octave bandwidths as heard by a listener could be determined, and the perceived noise level in PMOB calculated. This figure could then be substituted into some function relating perceived noise level and annoyance so as to find the annoyance over the given time interval.

Unfortunately such a noise model does not yet exist in analytic form so some simplifying assumptions must be made. Rotor rotational noise is a low frequency phenomenon, and although the SPL may be higher than for vortex noise, its contribution to annoyance is small. Assuming that continued use of noise suppression techniques can reduce engine, transmission and tail rotor noise to acceptable levels, main rotor vortex noise remains as the most important parameter.

This is somewhat of an oversimplification but it-does mean that an easily manageable noise model can be created. Using Schlegel's equation for overall vortex noise from Appendix C of Reference=l1,-the sound pressure level-at a radius x from a helicopter is given by

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SPL = 10 [2 log V_{0.7} + 2 log T - log A_b ~ 2 log (r/300) -3.57] where V_{0.7} is the linear blade velocity of the 0.7-rad. section.

A_b is the total blade area (blade plunform area.x number of blades)

T is thrust.

R,

Directivity effects:have-not been included at this_stage. From a knowledge of the vortex noise frequency distribution, the perceived noise level may be calculated in terms of the overall SPL.

3.1.4 The Criterion of Annovance

In a study by Erzburger and Lee (Ref. 12) on optimal trajectories with respect to noise for conventional-aircraft, the unit of annywance called the noy was used. This is related to PMC by

$$= 10 \frac{(902-40)/33.2}{(2)}$$

where $M_{\rm p}$ is total noisiness in noys. For noise in the urban environment there are two factors that make the noy unsuitable. The first is that noise level below 80 PMB appears to be acceptable to the majority of the population (according to results in Ref. 13). The second is that if the background urban noise level is 80 PMB, then any additional noise below 80 PMBB does not have much effect.

A possible alternative is to use a modified noy definition in the form

Annoyance =
$$\left[10^{(PNL-80)'33.2}\right]_{PNL380} = \left[\frac{MT}{16}\right]_{PNL380}$$
 (3)

In this work the following relationship was used

Annoyance =
$$\left[\frac{\left(\frac{1}{10}-\frac{1}{50}\right)^2}{10}\right]$$
 (4)

This expression agrees with equation (3) to within 1 unit over the range 85 to 123 PNdB (see P:g-te 10).

The other effect that must be considered is the duration of the noise on annoyance. In this work the performance function to be minimized was chosen to be

$$J = \sum_{i=1}^{L} \left[\frac{\left(\text{PNL} \left(\dot{x}_{i}, \dot{n}_{i} \right) - 80 \right)}{10}^{2} \right] \cdot \frac{\Delta \tilde{\varepsilon}_{i}}{\Delta \tilde{\varepsilon}_{i}}$$
(5)

where J is the function=to be minimized, and given the unit S-numbers

L is the number of time intervals

 \dot{x}_i is the horizontal velocity

h, is the vertical-velocity.

 $\Delta t_i \text{ is the time interval over. which PML is measured} \\ \Delta t_{rat} \text{ is some reference time interval.}$

i) the S-number sums annoyance ($\sim 10^{33-2}$) whereas the EPNL sums energy ($\sim 10^{-10}$).

so that the duration effect is given more relative importance in the 5-number formulation.



FIGURE TO NOISE LEVEL VS. ANNOYANCE

 the BHE, has no explicit background noise level cutoff, whereas the S-number does.

iii) the EPHC takes the logarithm of the sum, whereas the S-number does not.

3.2 Beaults

3.2.1 Values of Parameters in Example

Figures 11 to 17 show the graphical output from onecomputer run. It is only intended to show how the programoperates;-it is not possible to draw any conclusions about improvement; to the aircraft design from these figures. Mevertheles; they do show what the program is capable of and, more importantly, how it meeds to be improved. The Day meters used in this supple amount of filework.

	THE CHINE AVERNTE	ILA HE LOTTOMES
Grocs weight	:	58,000-1b.
Blade chord		4.18 ft.
Blade thick		.50 ft.
Rotor radius	1	36.4 £t.
Rotor angula	r velocity	14.3 rad/sec
Notor blade	angle of attack	0.07 red.
Number-of b]	ades_per rotor	3
Number:of ro	tors	2
Puselage equ plate area	ivalent flat	39.5 ft ²
Distance of take-off	observer from	500 ft.
Maximum allo	wable PML	Unlimited
Terminal hor	izontal velocity	150 ft/sec.
Terminal ver	tical velocity	0 ft/sec.
Time to reac conditions	h terminal	29 sec.
Total:shaft	horsepower	22,000-hp.

3:2:2 Discussion of Results

<u>Figure 11: Flight Path Profile:</u> This figure shows the shape of the flight path profile. Program constraintsprevent negative values of \hat{x} or \hat{n} . As might be expected the sircraft takes off vertically and gradually translates to horizontal flight.

<u>Piqure 12: Meight and Ground Track plotted equinat time:</u> This figure serves only to reference the subsequent figures, which are plotted originst time, against the flight path profile. In which time is not expressed explicitly.

<u>Figure 13: Values of v. π and h_1 </u> The figure shows that the microsoft initially clubs vertically until a rate of climb of 40 ft/sec. is reached; it then starts to accelerate horizontally and the rate of climb remains constant at 50 ft/sec. The reason for this can be seen from Pigure 15, which shows that at t w-5 seconds increase of rate of climb is restricted by power limitation. When the horizontal velocity has reached 60 ft/sec, the induced power has decrossed sufficiently for the microsoft to increase its rate of climb to 60 ft/sec., whereafter the rate of climb remains constant for 2 seconds and then gradually decreases.

The decrease in horizontal velocity at t = 21 seconds serves to decrease the thrust, and hence noise level, while the aircreft is in audible range. From Figure 16 it can be seen that for t P < 25 seconds the aircraft is out-of audible range and is able to accelerate to terminal conditions without.causing further annoyance. The overall reduction, in annoyance gained by this manosurer is very small and in

A SYSTEMS STUDY OF NOISE REQUIREMENTS ON THE DESIGN OF=V/STOL AIRCRAFT



FIGURE II FLIGHT PATH PROFILE



FIGURE 12 HEIGHT AND GROUND THACK-VS, TIME



FIGURE 13. V. BLAND & VS. TIME

practice would hardly be worth performing.

<u>Figures 14 and 15; Thrust and Power Required:</u> The plot of power requirement against time shows up one of the major limitations of the program as configured at present; sircraft performance is limited primarily by-the number of control options that are available, and only secondarily by the maximum power constraint. For example, it would probably be advantageous to apply full power immediately after take-off, but the rate-of-climb control available does not use full power at the take-off conditions. The solution to this problem would be to have a greater range of controls available, so that controls utilizing maximum power could be used under all flight conditions.

Figure 16: Annoyance Produced: The curve shows the cumulative annoyance, so that the gradient of the curve indicates the level of annoyance at any given time. The curve is steep for the first 6 seconds when the highest lavel of thrust is applied, and less steep when thrust is reduced. The rate of cumulative annoyance finally decreases to zero as the aircraft recedes out of audible range.

3.3 Program Limitations and Extensions

3.3.1 Use of More Controls

In this dynamic programming example the control variables were numerically equal to the quantized increments in state variables. This avoided the need for interpolation procedures.



FIGURE 14 THRUST VS, TIME

العاليات فللمعا فيقاعه والراقي أكرليه أحماره والالبان فكسابه ومقاماته فالمراجع والروا

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FIGURE 15-POWER VS. TIME



FIGURE 16 ANNOYANCE PRODUCED VS. TIME

If more controls were used the aircraft could fly at states that were not quantized increments in state variables. E.g., at present it can fly at either 20 ft/sec or 30 ft/sec but not intervening speeds.

Use of more controls would require a considerable increase in computing time but only a small increase in additional computer storage.

3:3.2 More Refined Noise Model

Reference 6 gives a directivity correction to equation

(1) as

$$-\pi_{D} \approx 10 \log \left[\frac{-\cos^{2} \phi + 0.1}{\cos^{2} 70 + 0.1} \right]$$
 (6)

where K_{D} is the correction to be applied to (1).

is the anglebatween listener and shaft axis. This correction can be applied without difficulty.

1.1.3 Use of More Listeners

Another useful modification to the program would be in the addition of more listeners, who could be positioned out of the plane of the flight path. Work is presently continuing on all these aspects of improvement. <u>4.0</u> <u>Conclusions</u>

- 4.1 By including noise as a measure of vehicle performance, it appears possible to design future helicopters which are significantly quieter (10-20 db) than current versions. The penalties for this quietness as measured by operating costs are in the range of 20-30%.
- 4.2 The optimal noise annoyance profile for a helicopter takeoff involves a vertical climb for 100 feet or more, and a substantial reduction in power as the listener is overflown.

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Sound Attenuation Over Simuleted Ground Cever * 5. P. Pro and L. B. Evens Wyle Laboratories, 7800 Governors Drive, Huntsville, Alabama 35807

ABSTRACT

In dealing with wave propagation over land below 1000 Hz, ground attenuation is on important consideration. Very often, the actual ground surface is covered with a thick layer of vegetation which has a very high overall void to volume ratio. Such a composite boundary should be represented as layered medie in order to assess the ground attenuation effect correctly. The wave attenuation characteristics under such conditions are studied in this paper. It is found through theoretical analysis that a layered boundary gives rise to strong selective absorption in certain frequency bands. Experimental date has been taken under laboratory conditions over a wide range of normalized parameters, and the results quantitatively confirm many aspects of the predictions. Both theory and experiment indicate that significant attenuation to very low frequencies can be expected for sound propagation over a deep layer of vegetation. Other results include the confirmation of a strong sound presure gradient in the vertical direction near the layered boundary, that the excessive âttenuation can increase at most 6 dB per doubling distance, and that the effectiveness of ground attenuation depends critically on the elevation angle of the sound source.

INTRODUCTION

The precise analytic nature of sound attenuation near a boundary with known acoustic impedance was first made clear in a series of studies by Rudnick ¹, Ingard ², and Lawheed and Rudnick ³. The main application has been the estimation of ground attenuation effects on sound propagation in the atmosphere. Some subsequent analytical studies^{4,3} and experiments ^{6,7,8} have further explored the details of this phenomenon. In these studies, the acoustic media above and below the boundary plane are assumed to be semi-infinite. Constant values are prescribed to either the impedances of the two media or the normal impedance of the boundary itself. However, in many situations with practical importance, the boundary between the upper and the lower semi-infinite acoustic medie is not a simple plane, but a porous layer with finite thickness. It is natural, then, to investigate the wave attenuation characteristics, near such a comparise boundary.

In the analysis of the simple boundary configuration, the only geometrical parameter is the rätio of source height to the wave length. The magnitude of ettenuation depends mainly on the impedance ratio, or the homal impedance, at the boundary. It was pointed out in the previous analytical studies that ground absorption orises because the sound wave propagetes at nearly glancing angres of incidence, and the wave front is spherical. On the boundary, the ground attenuation increases of 6 dB per doubling the separation distance between the sound source and the point of observation. A steep sound pressure gradient exists near the boundary such that the ground attenuation effect decreases rapidly as one moves away from the boundary.

In previous experimental studies ^{6,7}, selective absorption of sound due to ground effects has also been observed. The peek obsorption band is usually located between 300-600 Hz. Two probable explanations have been offered: "the interference effect of differential paths

The material in this paper was presented in part at the 80th Meeting of the Acoustical Society of America, November 1970, Houston, Texas. of wave propagation, and the variation of normal impadance of the boundary with respect to frequency. Evidence has been found to support both theories 4,5,4.

Owing to the special nature of wave reflections at near glancing angles of incidence, it is not possible to assign a constant value to the impedance of the entire composite boundary. A layered media representation becomes necessary in this case. It is required to specify both the acoustic impedance and the wave transmission constant of the parous transition layer. A new analysis is therefore required for estimating the magnitude and characteristics of the ground attenuation of such a layered houndary.

In addition to the analysis, an experimental study has also been undertaken to determine the attenuation characteristics of a layered boundary. The results of the experiment are intended for the verification of the theory as well as for obtaining a separate view of the problem from an independent approach. The experiment was performed under laboratory conditions such that the ground attenuation effect can be studied without the uncertainty of other complications such as wind refraction and turbulent scattering. Overall, the present study has found significant departure in several aspects of the attenuation characteristics of a layered media from those of a simple boundary. Thus, one may find the results useful in dealing with a varity of practical problems where a layered representation of the boundary is warranted.

I. FORMULATION AND ANALYSIS

The geometrical configuration for wave propagation over a layered boundary is shown in Figure 1. In this figure, the top sumi-infinite layer is assumed to be air, which has a density af ρ_{0} , speed of sound c_{0} , and acoustic impedance of $\rho_{0}c_{0}^{2}$. The middle layer is assumed to be a porous material. Its density and speed of sound are in general complex quantities. In other words, it has a complex acoustic impedance such that a plane wave transmitted from the air into this layer will be refrected into the layer with a phase shift, and will be attenueted as it propagates through this material. A third medium which represents the ground, occupies the lawer half space. For the simplicity of analysis, a constant normal impedance is prescribed at the interface between the middle layer and the semi-infinite ground. Also shown in Figure 1 is a schematic of wave propagation paths through which the sound from a point source can reach an arbitrary point in the half space above the layered boundary. The interference of the waves through these paths is responsible for the boundary attenuation effect.

As pointed out in previous studies, the simple ray acoustics approach can not account for the abserved ground attenuation phenomenon, and a more rigorous mathematical analysis must be followed. In the present study, the approach of logard ², together with coordinate systems and symbols in thet paper, has been adapted. The coordinate systems are shown in Figure 2.

A spherical wavefront which originates from a point source can be represented as an integral of its plane wave elements

$$\frac{e^{ikr}}{kr} = \left(\frac{i}{2\pi}\right) \int_{0}^{2\pi} d\phi \int_{0}^{-\frac{\pi}{2} + i\omega} e^{i\left[k_1 \times k_2 \cdot k_3 \cdot (h-z)\right]} \sin \theta \, d\theta \qquad (1)$$

In the above integral, the vector $\{k_1, k_2, k_3\}$ identifies the wavenumber of a plane wave element, and h denotes the height of the sound source above the top of the leyered boundary. The reflection of the primary wave at a boundary can evidently be represented as

$$P_{r} = \left(\frac{1}{2\pi}\right) \int_{0}^{2\pi} d\phi \int_{0}^{\frac{\pi}{2} + i\omega^{+} i \left[k_{1}x + k_{2}y + k_{3}(h+2)\right]} R(\phi, \theta) \sin \theta d\theta \qquad (2)$$

where R (ϕ , θ) is the plane-wave reflection coefficient. The reflection coefficient R (ϕ , θ) is a function of ϕ and θ .

It is more convenient for the purpose of integration to write Equation (2) in a new spherical coordinate system v here the principal direction of the reflected ray is chosen as the reference axis ². The new angular variables are defined as ψ and η . Equation (2) can now be represented as

$$\rho_r = \left(\frac{i}{2\pi}\right) \int_0^{2\pi} d\psi \int_0^{\frac{\pi}{2} + i \cos \psi} e^{ikr_2 \cos \eta} R(\psi, \eta) \sin \eta \, d\eta$$
(3)

An integral of this form can be evaluated by using the method of steepest descent⁹ in the acoustic far field where the value of kr_2 is large compared to unity. Along the paths of steepest descent in the complex n-plane, a new variable can be defined such that

where it is mail and positive.

The reflected wave can be then written as

$$P_{f} = \frac{e_{r_{2}}}{kr_{2}} (kr_{2}) \int_{0}^{2\pi} \int_{0}^{\infty} e^{-\frac{kr-t}{2}} R(\psi, t) dt d\psi = \frac{e_{r_{2}}}{kr_{2}} Q$$
(5)

which has the form of a wave originating from an "image source", located at a distance. In below the top of the layered boundary, with a variable strength. O.

For an arbitrarily given function of R ($\dot{\nu}$, θ), Equation (5) can only be integrated approximately. A first asymptotic approximation has been given by Brekhovskikh¹⁰ as

$$P_{r} = \frac{\frac{1}{2} \frac{1}{kr_{2}}}{kr_{2}} \left\{ R(\gamma_{0}) + \frac{1}{1kr_{2}} \left(\frac{1}{2} (1-\gamma_{0}^{2}) R^{*}(\gamma_{0}) - \gamma_{0} R^{*}(\gamma_{0}) \right)^{2} \right\}$$
(6)

where

R⁴ and R^{**} are the first and second derivates of R with respect to $y = \cos \theta$. Equation (6) serves as a starting point for the present analytical investigation into ground attenuation awing to layered media.

γ = cos θ

It remains here to determine the plans-wave infraction coefficient R(8) for a boundary with a layered configuration. The overall reflection coefficient accounts for the wave reflection at the top of the middle layer, as well as the wave which is transmitted into the middle layer, reflected by the ground, and returned into the air, (Figure 3). Hence, the averall reflection coefficient of the Inversed boundary can be given

$$R(\theta) = (\cos \theta - \beta_1 \cos \theta_1) / (\cos \theta + \beta_1 \cos \theta_1) +$$

$$+ 4\beta_1 \cos \theta \cos \theta_1 (\cos \theta_1 - \beta_2) \Phi / \{(\cos \theta + \beta_1 \cos \theta_1)^2 (\cos \theta_1 + \beta_2)\} (7)$$

ith
$$\Phi = \exp \left\{ 2 \operatorname{ih} (n^2 - 1 + \cos^2 \theta)^{\frac{1}{2}} \right\}$$

and $\cos \theta_1 = n^{-1} \left\{ n^2 - 1 + \cos^2 \theta \right\}^{\frac{1}{2}}$,

where
$$\beta_1$$
 is the specific admittance ratio of the middle layer with respect to air, β_2 is
the specific admittance ratio at the interface of the middle layer and the ground, and θ_1
is the refraction angle in the middle layer. The function Φ accounts for the phase difference
between the two reflected wave components. This phase shift is caused by path difference
and the wave transmission characteristics of the middle layer.

The instantaneous value of sound pressure in the far field can now be determined as

$$P = \frac{\frac{ikr_1}{kr_i}}{kr_i} \left\{ 1 \cdot \frac{r_i}{r_2} e^{ik(r_2 - r_i)} X \right\}$$
$$\times \left[R(\gamma_0) \cdot \frac{1}{ikr_2} \left(\frac{1}{2} (1 - \gamma_0^2) R^*(\gamma_0) - \gamma_0 R^*(\gamma_0) \right) \right] \right\}$$
(8)

The derivatives of R(θ) with respect to $\cos \theta$ can be obtained from Equation (7). By substituting the known expressions for R(θ), R', and R^{*} into Equation (6), an explicitexpression can be obtained for the reflected wave. The attenuation of sound near the layered boundary can now be obtained by simply adding the incident and the reflected sound pressure fields.

The algebraic expressions involved in the computation of the sound pressure field in the upper half space is straightforward, but relatively bulky. Therefore, the results have been programmed for calculation using a digital computer. The asymptotic approximate solution is very accurate for computations of sound pressure levels in the far field, i.e., points which are more than a few wavelengths away from the sound source. For the study of groundattenuation effects, this is a practically insignificant restriction. In the computing program, all of the geometrical and acoustical parameters can be varied independently. In particular, the specific admittance ratios β_1 , β_2 and the refraction index n, are assumed to be complex numbers. Some computations have been made for the limiting cases where the thickness of the middle layer opproaches zero and the results agree very well with those given by legard².

II. EXPERIMENTS

The measurements of sound attenuation over a layered boundary were made on a 20 ft by 8 ft plywood plattum. It serves as an idealized hard ground surface with very high acoustic impedance. A layer of porous material of uniform thickness is placed on top of this platform. The construction of the platform, the layout of the porous material, and the set-up of instrumentations, are relatively straightforward. The longest range distance available on this platform is 200 inches, and the thickness of the porous layer varies from 2 to 6 inches in the various cases. The chosen sound source is an acoustic transducer with a 3/4 in.

diameter threat openning. One-half inch Bruel and Kjaer microphones are mounted at six leastions on the top and above the layer of porcus material to measure the sound pressure layers in the far field.

The entire test set-up was placed in a free field environment since a large enachoic chember was not available. However, the free field arrangement was quite satisfactory since the ambient noise level was below 45 dB, and wind and turbulence in the test erea were virtually non-existent. The data was corrected for molecular absorption in air and, in most cases, this correction was very small and negligible.

From experience gained through preliminary tests, it was found that waves propagating at near glancing angles of incidence can penetrate through a parous layer and re-amarge from it only if the layer is extremely parous. Layers composed of other types of acoustic materials with higher densities may behave like sami-infinite layers. Hence, the choice of layer material for this test becomes a particularly interesting tesk. Basicelly, the suitable material should be extremely parous and yet have a stable and uniform structure such that repeatable data can be obtained with accuracy. The materials chosen for this experiment are listed below:

- (1) Rubberized Horsehair Material This is a matrix type of material composed of rubberized synthetic fibers. The density is 1.36 lb/ft³. The estimated void to volume ratio is 97.8%. Average fiber diameters are approximately 0.004 ~ 0.01 inch. The average distance between two nonintersecting fibers is approximately 0.005 ~ 0.15 inch. However, large clear opennings of 1/2 inch in diameter and depth are not uncomman. This material is originally intended for packaging of electronic instrumentation. It is commercially available in sheets of 2-inch thickness.
- (2) Glass Fiber Air Filter This is the material commonly used as air filters in heating and air-conditioning units. It is composed of long, stiff, and unbanded glass fibers. The size of the filers is fairly uniform with a naminal diameter of 0.002 inch. The average distance between parallel fibers is approximately 0.05 inch. The density of this material is 0.52 lb/ft³, and the void to volume ratio is approximately 99.7%. This material is commercially available in rolls of 1-inch thickness and up to 36 inches in width.
- (3) Fiberglas bett A 4-inch thick Fiberglas bett was elso chosen. In spite of its extremely low density of 0.27 lb/ft³, it has an acoustic impedence comparable to the above two materials. Moreover, the chaorption factor for sound propagation in this material is relatively high.

The acoustic impedance of these materials has been measured in an impedance tube ¹¹. Due to the low densities of these materials, the combined normal impedance of the sample and the rigid end plate of the tube has actually been measured. It was found that the acoustic impedance characteristics of the first two materials are approximately equal. The measured impedance values are frequency dependent. For frequencies above 1000 Hz, however, the impedance reaches a constant limiting value. Attempts have been made to determine the acoustic impedance of the sample itself by decoupling the effects due to the solid backing. Some analysis indicates that the specific admittance ratio of the first two meterials with respect to air is between 0.5 to 0.7. In the third material, the demping factor for wave immension through this material is relatively high. Hence, the effect of the solid backing is much less prominant. The measured specific admittance ratio of the fibergles bett is approximately 0.6.

The refrection indices of these materials have not been measured. According to the data given in Beranak¹², materials in a similar density range usually have a refraction index between 1.10 and 1.25 at frequencies above 1000 Hz.

A total of twenty sets of massurements were made for verieus cambinations of materials, layer thickness, and sound source height. In each set, micrephone readings were taken at six locations in the far field over a frequency range of 1 K Hz to 20 K Hz. The scaling factor of this laboratory experimental set-up with respect to verious proctical field conditions ranges approximately from 1/10 to 1/100. Therefore, the texted sound frequencies would correspond to a frequency range of 10 Hz to 2000 Hz in the field. Out of these texts, a significant range of normalized conditions for sound attenuation over layered media has been encompassed. Since the texts are performed in terms of descrete frequencies and the microphone readings are recorded directly on a level recorder, the data reduction procedure was relatively simple.

111. DISCUSSION OF RESULTS

By using Equation (8), a series of case studies have been calculated to investigate the dependence of sound attenuation on various geometrical and acoustical parameters. In this study, the principal geometrical quantities are the wavelength, the middle layer thickness, and the height of sound source above the top of the middle layer. For calculations of sound pressure levels in the fer field, the wävelength is chosen to normalize the coordinates, while in studies of sound absorption spectrum, the layer thickness is chosen as the reference length to normalize the frequencies. Among the three acoustical parameters, β_1 and in are more important; β_2^- is usually much smaller than unity, and it has only secondary influence on the overall results. For a highly porous middle layer, $-\beta_1^-$ is generally in the neighborhood of unity. The refrection index, in , is also close to one for isotropic porous materials with low densities.

Sound attenuation over a layered boundary is found to depend on the layer thickness. A typical case is shown in Figure 4. The sound pressure level contours in the far field for a sound source logated at the top of the boundary have been computed for two different leyer thicknesses. A general redistribution of sound can be seen in this figure. Of particular significance is the attenuation pattern near the boundary. On the boundary itself, the attenuation at any point can differ by about 5 dB from one case to another. The difference in sound pressure level decreases gradually as one moves away from the boundary. At line AA, the difference in sound pressure level at different layer thicknesses prevails even if the sound source is located high above the boundary. However, the point of maximum difference in such cases will be located somewhere between the boundary and the line AA. Figure 4 shows also that the sound pressure gradient near the boundary is very steep.

Calculations have also been made to investigate the dependence of sound attenuation on frequency and individual acoustic parameters. For simplicity, the layer thickness, the source height, and β_{2} , are assumed to be constant. The source height is assumed to be one layer thickness above the boundary. Sound pressure levels in the fer field are computed for given frequencies and various values of β_{1} and n. It was found in these calculations that, for a given pair of values for β_{1} and n. The attenuation of sound at the boundary itself remains more or less constant for all frequencies. However, at a slight distance above the boundary, a significant bend absorption pattern emerges due to the variation of the sound pressure gradient for different frequencies.

At this point, a subtle descrepency between the analysis and practical ground attenuation consideration becomes expanent. In the analysis, the acoustic media in all layers are assumed to be perfectly homogeneous and stationary, and the boundaries are perfectly flat surfaces. A sound pressure gradient can always be maintained even though it may be extremely large. However, in laboratory or field measurements, slight perturbations in the speed of sound or material non-uniformity will exist. Under such conditions, the actual sound pressure level contour will not be as sharp as predicted by the analysis. One can only measure the average sound attenuation value over a portion of this computed steep sound pressure gradient. Hence, in subsequent discussions of attenuation spectrum, the value of sound attenuation due to boundary effect is taken by averaging over a distance of 0.10 of the layer thickness immediately above the boundary. The 0.10 thickness value is set arbitrarily. However, it is portially related to the fact that most of the experiments were made with layers of 4^m to 6^m thick, and the microphones used in these measurements were 1/2-inch diameter, which is approximately 1/10 of the layer thickness. The pressure signal sensed by the microphone is, therefore, an average value.

The dependence of the sound attenuation spectrum on the refraction lindex is shown in Figures 4 and 5. The specific admittance ratios are held constant. in these figures, the wavelengths are normalized with respect to the constant layer thickness. The sound attenüätion due to the boundary effect is shown in decibels for a point 50 layer ilucknesses away from the sound source. In Figure 5, three curves with small values of the refraction index, n, are shown. The attenuation spectrum shows clearly a peak in the low frequency range. The location of this peak depends on the value of the refraction index. For a layer of 20 ft thickness, these absorption peaks will correspond to frequencies between 50 Hz $\,\sim\,$ 200 Hz. The dash vertical line indicates the expected absorption peak location if the middle porous layer were removed such that only the high impedance bare ground were left. For values of a between 1:20 and 2.0, the attenuation peak oscillates in the law frequency more (kh < 40). However, the overall attenuation spectrum shows a definite shift towards lower frequencies as a increases. In some cases, there is more than one peak. In the limiting case of a layer with a very large complex refraction index. i.e., $n \gg 2$, the layered boundary is effectively equivalent to a simple boundary with a normal impedance. The attenuction spectrum, which is an average value over a short distance near the boundary, decreases monotonically with frequency. The computed attenuation spectra for $-n \gg 2$, and for n== 2, are shown in Figure 6. The attenuation spectrum for _ n _>>2-shows a higher level of sound attenuation than all computed spectra at other values of in .

For a fixed value of refraction index near unity, the variation of an attenuation spectrum with respect to B_{μ} is quite simple. A typical set of curves is shown in Figure 7. The magnitude of attenuation increases with the specific admittance ratio while the attenuation peak remains in approximately the same location.

The experimental data obtained in this study have been reduced and normalized. The general characteristics of ground attenuation, such as the existence of a steep sound pressure gradient immediately above the boundary, and that the ground attenuation increases by 6 dB per doubling the distance from the sound source, have been clearly confirmed. The experimental data was found to be repeatable within a band of about 2 d3. The classical law of reciprocity, which implies that the value of sound attenuation remains unchanged if the positions of the sound source and the microphones are exchanged, was found to hold in this experiment. Although it had nothing to do with the objective of this study, it was a convenient reference for the verification of accuracy. A few unique properties of sound attenuation over a layered media are also born out by this experiment. A comparison of the experimental and theoretical attenuation spectra is shown in Figure 8. Three sets of attenuation measurements with similar normalized geometrical configuration, but with different materials and layer thicknesses are shown on this figure. The agreements of the magnitude of sound attenuation and the location of the peak are very close. Although the acoustic parameters used for the theoretical curve is probably not the exact value for the acoustic materials used in the experiment, the prediction, nevertheless, shows the correct trend and order of magnitude.

By comparing the analytical curve with the data, one finds that the data is significantly below the prediction in the high frequency range. It is probably because the wave reflections become randomized such that the ground interference effect becames ineffective. It is interesting to note that the measured absorption peak frequency is significantly below the expected "bare ground" interference peak, which is computed by using ray acaustics and is indicated by the dash line. This is particularly significant since the layered materials used in the experiment have a void to volume ratio of well over 97 percent, and large surface openings. Intuitively, one might think that such materials should have little effect on ground absorption.

Some anormalies of the dependence of sound attenuation versus distance have been measured. In Figure 9, a variation of ground absorption versus distance is shown. The values were obtained from the experiments. For the low density ground materials that were used, and for ground attenuation in distances of less than 50 wavelengths (k x < 300), the ground absorption and rate of increment is smaller than the classical predictions. The 6 d8 per doubling distance rate is observed for distances beyond 50 wavelengths. In some sets of data,

IV. SUMMARY AND CONCLUSIONS

Several important characteristics of sound attenuation, which are unique to a layered -boundary, have been found through this analytical and experimental study:

- Selective sound attenuation in a certain frequency band has been predicted and observed for a layered boundary with constant (frequency independent) occustic properties. Such an effect has not been considered in previous investigations in the literature.
- A layer of extremely porous material can still öffer significant attenuation to sound propagating at near glancing angles of incidence.
- 3. For an extremely porous layer, the sound attenuation in the near field of the sound source is usually very low. Pressure doubling may occur due to the reflected wave from the hard ground surface. However, the attenuation at distances sufficiently far away from the source will be dominated by the acoustic properties of the layered material, and significant attenuation levels are observed.

pressure doubling has also been detected in the near field at the lower frequencies. It was found also in the analysis and the experiment that the magnitude of ground attenuation depends critically on the height of the sound source. Figure 10 shows the dependence of sound attenuation on the apparent elevation angle of the sound source as observed from a point in the fat field. The data points are obtained in the experiment. If the sound source is at many than 8 degrees above the horizontal, the boundary attenuetion drops below 5 d8. In many practical situations where noise control is of primary concern, the ground attenuation at large elevation angles becomes Insignificant. An enalytical computation, showing the effect of source height on the far field sound pressure level pattern, is given in Figure 11.

The analytical results obtained in this study seem to predict the correct trends and magnitude of sound attenuation over a layered media, an ! can probably be used as a basis for the development of practical ground attenuation prediction techniques for situations where a layered boundary description is warranted. Of course, a substantial amount of work has yet to be done.

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Figure 1. Reflection of a Plane Wave from Layered Media at Near-Glancing Incidance Angles



Figure 2. Coordinate Systems Employed by Ingard in his Theoretical Treatment of Ground Attenuation (Reference 2)



Figure 3. Reflections of a Plane Wave from a Layered Boundary



Figure 4. Ground Attenuation Directivity Pattern for two Different Ground Cover Thicknesses. The layer thickness for ______ is 0.,5 wavelen;th, and the layer thickness for _ _ _ is 0.,25 wavelen;th. The sound source is located at one wavelength above the boundary.

3. A BA



Figure 5. Ground Attenuation Spectrum as a Function of the Refraction Index. The sound source height equals the layer thickness, h. Sound attenuation values are computed for a point 50h away from the sound source. The location of absorption peak for hard ground without cover is indicated by a deshed lice.







Figure 7. Ground Attenuation as a Function of the Specific Admittance Ratio of the Layer.



Figure 8, Comparison of Experimental Ground Attenuation Spectrum with a Theoretical Prediction.» Data obtained for three ground cover materials are shown: O horsehoir at 4-in. Michness; A horsehair at 2-in. thickness; and D fiber filter at 6-in. Mickness.



Figure 9. Ground Attenuation as a Function of Distance. Data are obtained for four types of layer materials: ○ fibergiess filter et ó-in. "thickness: △ fibergiess filter at 4-in, thickness: □ horsehair at 4-in, thickness; and ◇ horsehair at 2-in, thickness.



Figure 10, Ground Attenuation as a Function of Evaluation Angle of the Sound Source.





ATMOSPHERIC ABSORPTION OF SOUND: THEORETICAL PREDICTIONS *

L. B. Evens	Wyle Lahoratories, Huntsville, Alabama 35807
H, E. Ins	University of Mississippi, Department of Physics & Astronomy University, Mississippi 38677

L.C. Sutherland Wyle Laboratories, El Segundo, California 90245

ABSTRACT

By assuming äir is composed of four gaset, 1.e., nitrogen, axygen, water vapor, and curban diactide, and applying energy transfer rates for the binary collisions inherent in such a system, absorption of sound in the atmosphere has usen predicted. The colculated curves based upon twenty-four energy transfer mechanisms are compared with experimental date over the humidity range of 0-100 % relative humidity. Agreement between theory and experiment is very good. By including classical absorption and ratetional related on effects the two atmospheric absorption is also predicted at 20° C. Calculations made for verious concentrations of CO_2 indicate that low CO_2 levels (less than 0.1%) do not significantly effect obsorption of audible sound at high humidities. At very low humidities, however, CO_2 is an important factor.

I. INTRODUCTION

A basic characteristic of sound propagation is the attenuation with distance due tovarious irreversible processes which remove energy from an acoustic wave and convert it to 'heat. Prediction of sound propagation in air over long distances has become a metter of 'increasing practicel significance in several areas including:

- Prediction of community noise levels around airports
- Analysis or acoustic detection of tectical aquipment or aircraft
- Evaulation of very low frequency sound in the atmosphere generated by racket engines or from natural sources such as tided motion, -certhewakes, wind stams, etc.
- Investigation of the vertical propagation of sonic disturbances from signaling granules or sonic booms.

Where it is necessary to evaluate sound propagation over a substantial number of wavalengths, the absorption of sound by the atmosphere must be considered. Propagation characteristics are dependent upon (a) atmospheric conditions, (b) the pasition of the source relative to the ground, and (c) the terrain/vegetation features adjecent to the sound path. The above listed factors which effect the intensity of the sound arriving at the observer can be classified as follows:

Spranding Losses

- Uniform spherical spreading (Inverse Square Low) lasses
- Non-uniform spreading
 - reflection by finite bounderies
 - refrection by non-uniform etmosphere
 - difiraction (scattering) by non-stationary atmosphere

* The material in this paper has been presented in part at the Helicopter Noise Symposium, Durham, North Carolina, September 28-30, 1971 and at the 82nd meeting of the Acoustical Society of America, Donver, Colorado, October 1972.

Absorption Lesses

- Absorption by ground and ground cover
 - Absorption by amoughors
 - classical absorption
 - melecular relanction absorption

Of these sound propagation offects, different ones may be the controlling factor for different atmospheric metaerological canditions and far varying source-receiver placement; however, for any type of condition or any type of sound propagation path, the absorption due to classical and melocular effects are fixed for a homogeneous atmosphere and are functions only of the propagation path distance, the humidity content, gas impurities, and the temperature. Before the more variable propagation effects can be accurately assessed, it is necessary, therefore, to establish the proper values for these fixed absorption losses.

Atmospheric Absorption Lasses

Atmospheric absorption lesses have two basic forms: (1) classical losses estociated with the change of acoustical energy (or kinetic energy of molecules) into heat by fundamental ges transport properties, and (2) for polyntamic gases, relevantion losses estociated with the change of kinetic or translational energy of the molecules into internal energy within the molecules themesives.

The classical lasses can be further sub-divided into

- e Viscous Lasses
 - Heat Conduction Losses
- Diffusion Lawes
- e Rediction Loues

Only the Stakes-Kirchhoff Lasses are considered significant for eir under normal atmospheric conditions. Diffusion lasses contribute only about 0,3% more and rediction lasses are significant only at very law frequencies.

Relaxation absorption losses in polyatamic gases are known to have the following forms.

- Thermel relation between translational energy and vibrational energy
 states of the molecules
- Thermal relaxation between a close vibrational resonance of two different melecules:
- Themes relaxation between the vibration of one molecule and the rotation of a different molecule
- Thermal referention between translational energy and rotational energy states of the molecules
- Electromagnetic relaxation between translational energy and allowable electronic energy states of the molecule.

As fer as is known, electromagnetic relevation is significant for only one common gas, nitric axide, NO, and then, only at very high ultrasonic frequencies?.

In the helence of this paper, a basic theoretical technique for predicting the total etmospheric absorption fosces is presented along with supporting experimental data.

II. THEORETICAL METHOD

Investigations of sound obserption mechanisms in air have been certied out by many different laboratories since the pioneering experimental work of Pielemeier² in 1929 problems culminated recently in the work of Herris³, Herris and Tempest⁴, Mank³, and Evens and Sutherland⁶. The mearetical treatment of the problem has lagged somewhat behind the experimental results. Knowers' 1933 theoretical treatment has largely been used to replain the experimental date?. However, it has always been recognized that this theory does not give an adequate description of the antire problem. Sutherland⁶ and Plercy⁹ have shown that at frequencies well below the maximum absorption there is a distinct systematic deviation from single releasetion theory. It is this area that this paper attempts to clarify.

In this paper, air is considered as a four-gar mixture, i.e., nitregen, anygen, carbon diaxide and water vapor. By applying the energy transfer rates for the binary collisions inherent in such a system, absorption of sound in the atmosphere is predicted. The colculated curves are based upon twenty-four energy transfer mechanisms as shown in Tables I and II.

The theoretical prediction of total sound absorption also requires calculation of the losses due to classical effects and molecular relaxistion. The classical absorption can be written as

$$i_{c1} = \frac{2\pi^2 f^2}{\gamma^{P}_{0} V_{0}} \left[\frac{4}{3} \eta + \frac{\gamma - 1}{C_{p}} \kappa + \gamma a_{d} D_{12} \rho \right]$$
(1)

where

are total classical absorption

- # ges pressure
- sound frequency
- affective specific heat ratio of the gas
- = sound velocity at low frequencies
- viscosity of the Jos
- # effective specific heat of the ges at constant pressure
- a_ = a molecular diffusion constant
- D 12 # diffusion coefficient for O2 and N2 mixture

s ≝ gas denvity

thermal conductivity

For frequencies less than that at which rotational relaxation occurs this expression can be evaluated in terms of the viscosity based on measured values for the above constants 10

$$a_{c1} = \frac{2\pi^2 f_{c}^2}{\gamma F_{0}} \left[1.900 \right] n$$
 (2)

For frequencies greater than that at which rotational releasation occurs the general expression must be used and the effective values of the frequency dependent terms utilized¹¹. Equation (2) was utilized to calculate classical losses in this study with y taken as its low frequency value.

The absorption due to thermal relaxation between translational and rotational energy states of the molecules was calculated assuming that the rotational relaxation of each molecule was the same in air as in the pure gas. This assumes that during a collision with unlike moleccules, the probability of transferring rotational energy for each molecule is independent of the collision perture. This assumption, of course, would be very poor for high frequencies. For the frequencies of interest, however, a change by a factor of 2 or 3 in the rotational relexation time for any constituent molecule would lead to very little change in the total absorption. The effects of relational relexation were included by writing the effective specific heat as the sum of the centributions from the translational, (3/2R), vibrational, and rotational modes.

$$(C_{v})_{\text{effective}} = \frac{3}{2} R^{\frac{1}{2}} (C_{v})_{\text{vibration}} * R \sum_{j=1}^{n} \pi_{j} \frac{(r_{j}-3)}{2} \frac{1}{1+i\omega\tau_{j}}$$
(3)

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where j represents the constituent molecules of eir, i.e., CO3, H3O, O3 and N3; and

- e, = cóncentration èf molecule .}
- = number of degrees of freedom of molecule j
- $u = 2\pi$ times the sound frequency
- r, = rotational relaxation time of molecule j
- = number of types of melecules considered.

For purposes of this study, only CO₂, N₂, O₂ and H₂⁻O were considered; however, the method is quite general provided the above assumption regarding the effects of ünlike collisions on the rotational relevation times is valid.

The final term to be considered includes the sound loss due to the thermal relexiation between translational energy and vibrational energy states (V-T), between vibration of one melocule and the vibration of enother (V-V), and between the vibration of one molecule and the relation of the same or different molecule (V-R). The difference between (V-T) and (V-R) processes is only important when calculating energy transfer rates; so, for these calculations both processes will be considered as being (V-T). These vibrational relaxation processes are the deminent causes of loss at low occustic frequencies.

The sound absorption due to vibrational relaxation was calculated using the method first advanced by Tanczos¹² which was expanded to a two component system by Shields¹² and later expanded by Shields and Bass¹⁴ to allow for three-for-one (V-V) exchange between colliding molecules. The only information required to perform such calculations are the binary rate constants and the concentration of each gas present.

Shields' equations for expressing the ecourtic absorption and dispersion as a function of the various energy transfer rates of importance were used as a starting point for these calculations. The only modifications required to expand the method to a four component system was a change in Equation (6) of Reference 13. The modified equations become

where the terms have been defined in Reference 13. These two expressions allow the effective vibrational specific heet to be calculated which in turn can be used to determine the obsorption and velocity of sound using Reference 13.

A total of 24 energy transfer processes were considered. The rates for these processes are given in Table 1. Rates are laboled as $MAP_{b}^{0}(I,J,A)$. The letter A^{-} indicates the type molecules involved in the collision. An index to the numbering system used is given in Table 11. MA is the number of collisions of type A occurring each second in air at one atmosphere of pressure. $P_{b}^{0}(I,J,A)$ is the probability that, during a collision between the molecules involved in type A collisions, made 1 of one molecule will lose "a" quanto of vibrational energy while made J of the same malecule or the collision pertner geins "b" quanta of energy. The medes are numbered as follows:

Node 0 = translational mode of any molecula

Made 1 = symmetric stretching mode of CO₂ ($v_1 = 1300$ cm⁻¹):

Made 2 = bending made of CO₂ ($V_1 = 667 \text{ cm}^{-1}$) (doubly degenerate)

Mode 3 = asymmetric stratching mode of CO₂ ($v_{1} = 2349 \text{ cm}^{-1}$)

Mode 4 = vibrational mode of N₂ ($v_a = 2331 \text{ cm}^{-1}$)

Mode 5 + vibrational mode of O_2 (V = 1580 cm⁻¹)

Made 6 = banding made of $H_2O(v_s = 1595 \text{ cm}^{-1})$

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For example $M2P_1^1$ (4,0,2) is the rate for the (V-T) process N

and M4P1 (4,5,4) is the rate for the (V-V) process

$$O_2 + N_2^* \rightarrow O_2^* + N_2^*$$

where * indicates a vibrationally excited made. The symmetric and and the stretching modes of H₂O were not considered since their contributions to the total spucific heat is very small.

A rother large number of rates have been considered since at different humidity and frequency combinations different rates are the centrolling mechanisms for the sound absorption. For example, at high humidities the effect of CO₂ is insignificent in concentrations below 1000 parts per million. However, in relatively dry air the CO₂ content connets the relatation frequency of the mixture as shown in Figure 1. The mest important rates for the study are the (V-T) and (V-V) rates for $O_{3}/H_{3}O$ collisions; the (V-T) rate for $H_{3}Q/H_{3}O$ collisions; the (V-T) and (V-V) rates for Ng/HgO collisions; and at law humidities the (V-T) cud (V-V) rates for On/COn interactions. It should be recognized that any of the allove (V-1) rates could very well be the result of a (V-R) process followed by a rapid (R-T) process.

Although only the absorption has been discussed, the velocity could also be calculated by the same method. The velocity, however, is less sensitive to the preferre of relevation.

The same of the theoretical method used is its versatility. The same theoretical method and computer program could be used for any combination of gases. The effect of pollutents on the frequency dependence of sound absorption and the absorption of sound in alien atmospheres could readily be calculated provided the binary collision rates were known. In many cases, these rates can be found in the literature. These not available in the literature can be measured In controlled laboratory conditions without being concerned with all the variables inherent in field measurements. The temperature dependence of the relaxation absorption can also be calculated if the temperature dependence of the individual transition rates are known. Additional laboratory measurements of the tem; stature dependence of the rates important in sound absorption must be made before more accure theoretical predictions will be possible. A great deal of progress has been made towards developing theoretical expression: for energy transfer rates. Once such expressions are developed, calculations of sound absorption from molecular constants will be possible. This area clearly deserves additional attention. III. RESULTS

The gradicted curves are shown in Figures 2 through 5 plane with available experimental date. Of the three vety of date. Herris and Tennest's is thought to be the most occurate. Agreement between theory and experiment is very good. The curves and data have been presented in the form, m/m venus V/f where m is the intensity attenuation coefficient and m max is its value at the relexation frequency f_{\max} . By normalizing both exes, data for the various different humidities can be plotted on the same graph. In each case the experimental data has been normelized by f_____ predicted by Monk's expression and the value of m_____ has been computed using the Planck-Einstein relationship for the specific heat of the oxygen content, -An error in f_{max} will move a data point along a 45° line; on error in m_{max} will change the vertical position of the data point on the $m/m_{\rm max}$ scale and hence both parameters effect the agreement between theory and experiment.

Figure 6 depicts the predicted curves of μ/μ_{max} versus (/p where μ is the absorption per wavelength. It is readily abview from these curves that sound absorption in air is a multiple

releastion process. The curves have been normalized by the major peak which is due to the vibrational specific heat of anygen, hence, as a result of the nitrogen relaxation μ/μ_{max} does not necessarily equal one. The minor peak is not as easily explained. It is primatily due to the nitregen centent of eir; hewever, its position in frequency is primarily a function of the water valuer centent¹³

Comparison between farmer and theory as a function of humidity is shown in Figure 7 along with Mark's curve⁵. It is not surprising that Mark's results and 'the present work are identical at high humidities since we have taken the rates which are important at high humidities from Monk's paper. However, there is considerable difference at lower humidities (Figure 1). This work approaches a value of approximately 30 Hz for the relexation frequency at zero huminity. This agrees very well with the values reported by Piercy ¹⁶ which were extracted from very law temperature air data. There is some uncertainty in this 30 Hz prediction since the rate for O_{3}/CO_{3} (V_) (V-V) coupling is not well known. As shown in Figure 1 a difference of one order of magnitude in this particular rate makes approximately the same difference in f_{\max} at zero humidity. For this work, MOP (5, 2, 0) was chosen to be $3.0 \times 10^{5} \text{ sec}^{-1}$ atm⁻¹ to agree with Piercy's ¹⁶ results. Taylor and Bitterman $\frac{V}{2}$ suggest a value of 3.0 x 10⁶ sec⁼¹ atm⁻¹. The third curve in Figure 1 emphasizes the importance of including the trace emounts (300 ppm) of CO2. Without CO2 the zero humidity relaxation frequency is approximately 6 Hz.

The acoustician is often faced with making corrections for atmospheric absorption and for these purposes Figure 8 is included. These curves show the total absorption (i.e., classical, vibrational, and retational absorption) in d8/1000 friversus 6/p at 20° C. It is fait that the accuracy of these predicted curves will be well within any experimental error in field measurements and can be used without hesitytian,

IV. SUMMARY

The theoretical method developed allows the acoustic absorption to be calculated to an accuracy comparable to that of present experiments. If the need for more accurate predictions of sound absorption orises, then the transition rates required in the theory must be determined more accurately, especially these involving water vapor. Further, if the theoretical method is to be expended to elien atmospheres, the necessary binary vibrational energy transfer rates must be determined apportmentally or colculated. The ability of the theoretical technique to predict the temperature dependence of the sound absorption depends upon the temperature dependence of the various vibrational rates. Again these rates involving water vapor need additional study. In order to make calculations of the absorption of sound in air, or any other calculation which requires transition rates, without "a priori" knowledge of the various transition rates, theoretical exercisions for these rates must be developed. To date there has been morginal success with (V-T) calculations and with (V-R) calculations but none with (V-V) theory. These calculations also deserve additional study.

Some error may be introduced into the present calculations by exclusion of the trace nts of H₂ and Ar which are present in the atmosphere. These constituents, particularly H₂ , may have some importance at extremely low humidities. The uncertainty introduced by neglecting these two trace elements, however, is certainly no greater then that elready present awing to the uncertainty in the transition rates,

These calculations were expedited by most of the needed transition rates being available In Taylor and Bitterman's ¹⁷ excellent review article on the transition rates important for CO₂ lesers. Other reviews of this nature, where the various data sets are not only recorded but their accuracy assessed, are certainly needed.

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It is felt by these authors that the method and curves presented can be used to predict atmospheric sound propagation reliably at 20° C and probably safely over a 5° spread around 20° C. Not until better information is available on the temperature adpendence of many of the transition rates will accurate calculations as a function of remperature be passible.

V. ACKNOWLEDGMENTS

This work was spansared by the Army Research Office - Durham. One of us (HEB) wishes to express his gratitude to the Committee on Faculty Research of the University of Mississippi and the Office of Navel Research for support. We all express our gratitude to Dr. F. D. Shields of the University of Mississippi for making available a copy of his computer program for a binary gas mixture.

fate	Value in sec ^{*1} etm ⁻¹	Reference
MOPI (3,2,0)	6,0 x 10 ⁴	•
M0P ¹ (2,0,0)	3.0 × 104	•
MOPI (5,2,0)	3.0 x 10 ⁵	•
M0P1 (1,2,0)	4,5 x 10 ⁴	n
ж М1Р <mark>1</mark> (2,0,1)	1,8 x 10 ⁵	•
M1P ¹ (3,2,1)	1.5 x 10 ⁵	•
M1P ¹ (1,2,1)	4.5 x 10 ⁴	- 8
M2P ¹ (2,0,2)	3.4×10^4	•
M2P1 (4,0,2)	1.0	•
M2P1 (3,4,2)	• 1,8 x 10 ⁷	•
M2P1 (3,2,2)	6.0x 104	•
M2PI (1,2,2)	4,5 x 10 ⁸	a
M3P1 (2,0,3)	4.2 × 10 ⁴	ь
M4P ¹ (4,5,4)	1,5 x 10 ²	•
MIP1 (5,0,4)-	40	•
M4P1 (4,0,4)	1.0	•
MSP1 (5,0,5)	63	c
M6P1 (6,5,6)	4.6 x 107	c
M4P1 (5,0,6)	1.1×10^4	¢
M6P1 (6,0,6)	6.0 x 104	c
M7P1 (4,0,7)	1.0	·
MBP ¹ (4,0,8)	1,13 x 10 ⁵	d
M8P1- (6,0,8)	1.4 x 10 ⁴	c
M92 ¹ (6,0,9)	1.0 x 10 [*]	c

TABLE 1

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- c. See Reference 5.
- d. See Reference 15.
- e. Reference 17 gives an estimated value of $\sim 3 \times 10^{4}$ sec⁻¹ etm⁻¹. However, for this work we have chosen a value of 3×10^{5} -sec⁻¹ etm⁻¹ which agrees with results of Reference 16.

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TABLE II

Molecules Colliding - A		Molecules Colliding – A	
c02/02	0	02/02	5
co₂/co₂	1	0 ₂ /H ₂ O	6
CO2/N2	2	N2/N2	7
с0 ₂ /н ₂ 0	3	= N ₂ /H ₂ O -	8
02/N2	4	H20/H20	•

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10.11





Figure 3. - Hermalized Intensity Absorption as a Function of Normalized Frequency for 0.3% to 1.2% H₂O Molecules. The solid curve has been calculated for 23° C and represents an average value of the calculated curves in this humidity range. The difference in 1% calculated values over this range is about twice the line michness.





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Figure 8. -Total Absorption of Saund in Air as a Function of Frequency. The curves range from 0 to 100% relative humidity and are for 20 9 C.

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Addendum to Proceedings

Helicopter Noise Symposium 28-30 September 1971

SUMMARY SESSION

Mr. Richard Ballard:

I think a summary session is very important for a couple of reasons. One is that it gives us an opportunity to sum up the papers that we have had during the last day and a half of meetings. The other thing is that it gives us a good opportunity to take a look and to assess where we have been and where we might be going. I would suggest that you give a little thought to where we are going in some of our programs and if we are really effective in solving the problem of the helicopter in the military environment. As I mentioned to you yesterday, operators are going to be reluctant to sacrifice performance to reduce noise. They are going to be reluctant to pay more for quieter helicopters with the exception of special purpose vehicles. These special purpose vehicles have a grouping of their own, so I don't think we're going to orient our efforts in that direction. Also, if we're going to reduce the noise of helicopters, we cannot do it at the expense of performance. I think we should keep these points in mind as we proceed.

We have five sessions, and I propose to let the chairman of each one o. these sessions approach it as he wishes. He may summarize the session or make his own remarks. The first session yesterday morning was chaired by Mr. Meade Mitchell and addressed the Government programs, so I will ask Mr. Mitchell to start off.

Mr. Meade Mitchell:

We have given considerable thought to trying to summarize the session we had yesterday. Generally it was a summary of the programs being sponsored by AMRDL (the Army Air Mobility Research and Development Laboratories) in conjunction with NASA. Out of that, a couple of remarks would be appropriate now from the AMRDL standpoint. It is evident that we are going to continue to invest a considerable amount of our limited resources, that is, funds, manpower and, in the case of NASA, facilities. We are going to depend pretty heavily on NASA for support as far as the Government facilities are concerned, and also on industry and universities for support of our noise program. However, it is evident that we must concentrate now on coming to an agreement amongst ourselves about defining the causes and possible solutions, and then acceptable ways of predicting noise and noise reduction methods. There are questions of how we put this in specifications from the Government's standpoint in our new systems work, how we specify what we want, and then, after we've specified it all, how we measure it.

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I think there is some work to be done on coming up with an acceptable, understandable, common system of measuring noise reduction techniques. We have made some starts on this, such as under what conditions do we measure, what type of instrumentation do we use, what are the atmospheric conditions under which we are going to grade the contractor for his efforts, what kind of terrain is to be considered and things like that. It's about time we try to bring some of these aspects into focus. As we said yesterday, we are going ahead to develop systems whether or not we reduce the noise.

I am excited about some of the work that has been reported here, sponsored by ARO-D, some of the independently sponsored work, and some of the work we're trying to sponsor through the Army labs. I think we are on the verge of coming up with some techniques of predicting and eliminating noise. Now that we are beginning to understand some of the fundamental mechanisms that cause it, I think there are some design techniques that we can use. That has been evident in some of the papers presented today by Vertol. So, in summary, I think we've got to bring into focus some of these things that we are all discussing - the techniques, the measurements, and more important, the way to specify what we want without compromising performance. After we have specified, how do we grade the contractor and how do we make him stick to his contract of producing what we say we want?

I think that generally summarizes our session of yesterday. Again, I am encouraged by the things I've heard here today. It seems as though we are well on the road to a better understanding of the causes of noise and how to use them to make design improvements to reduce noise.

Aerodynamic Theory

Dr. Robert W. Truitt:

Thank you, Dick. As most of you know, I have worked with ARO-D closely over the past six or more years. And in raticular, I saw the planning of Dr. Kumar in what we now see as the beginning of fruitful work in helicopter noise.

First of all, I want to say that I am impressed with the quality of papers that we had in this session. I think it's clear, and Meade Mitchell mentioned this, that there have been some important things reported here. I do think that the mission we set out to accomplish in this noise program can be realized, and I emphasize "can be" because I think it's clear to all of us that we still are a long way from answering some of the real, fundamental questions.

First of all, I want to mention the papers that were presented during this session. The first paper was a preliminary "Noise Analysis of the External Aerodynamic Diffuser Applied to Shrouded Propellers", presented by Dr. Ron Bailey and Mr. Richard Longhouse. It was brought out during the discussion of this paper that the instability of the flow due primarily to any forward motion would be caused by flow separation, that is, separation off of the shroud itself. This points to the important fact that viscosity effects are of great importance not only in the aerodynamic considerations but to noise problems as well.

The second paper was concerned with "Theoretical and Experimental Studies of Helicopter Noise Due to Blade-Vortex Interactions" and was presented by Drs. Widnall. Chu and Lee. The first type of bladevortex interaction discussed was for the tandem rotor, where the unsteady lift on a blade is calculated using an existing linear unsteady aerodynamic theory for blade-vortex interaction. For the tip-dominated blade-vortex interaction, unsteady slender body theory is used to calculate the unsteady forces on the blade as it encounters the vortex. The theoretical model for radiated sound due to transient lift fluctuations was presented along with the predictions of the directivity, frequency scectrum, and transient acoustic signals. Agreement was found to be good compared with the experiment for small angle blade-vortex interactions. It occurred to me that perhaps one of the places where we need to consider an improvement in the approach to a problem as complicated as this is to hope that sometime we can get into the nonlinear theory, particularly as you approach larger angles of attack. The inviscid slender body theory is, of course, an old standby that we always lean upon, but there are many new theories that are concerned with the viscous-transonic slender body flow which I hope we can incorporate soon.

As we move along, hopefully we can improve our theories and our ability to predict by putting in more realistic inputs from the aerodynamics point of view. Right now, transonic aerodynamics is a very popular subject. ARO-D is supporting some very interesting work in viscous transonic flow, and we are hopeful that important findings will develop from these studies. I think it would behoove us as helicopter people to keep abreast of all of this new research activity.

The third paper, given by Drs. Lyon, Mark and Pyle, was entitled "Synthesis of Helicopter Rotor Tips for Less Noise". Dr. Lyon gave a presentation of studies of rotor tip sound radiation for purposes of designing rotor tips that radiate less sound in specified frequency bands. Consideration, as you may recall, was given to radiation due to lift and thickness effects. Dr. Lyon showed that lift radiation is generally negligible in comparison with thickness radiation in specified frequency bands. Factors that affect trade-offs between choices of airfoil section and planform were discussed. Now, here again, I believe that the non-linear viscous aerodynamics that we might have as an input might be an improvement in the approach to this problem. In other words,

both the second and third papers seemed to me to require a better input than linear inviscid slender-body theory. I do not mean to imply that we won't be needing to use the wind tunnel to get a lot of answers, because theory is not going to be completely sufficient. But, some very important theoretical findings are available concerning optimum or shockless transonic airfoils. The work of Nicuwland and others may lead to optimum airfoils, bodies and wing-body combinations that will be efficient in the transonic range. They are not going to be as efficient at lower speeds, but it looks like we can hope to have some better and more efficient means to operate very near the speed of sound or certainly in the super critical range. It seems clear to me that an optimum aerodynamic body shape (meaning optimum with respect to, say, drag rise) is compatible with an optimum shape for less noise. I don't think we are going to eliminate noise but I would certainly be surprised if when you get a good aerodynamic configuration in the transonic range, you're going to have a good noise configuration too. I would like to hear what someone else in the audience has to say about that.

The fourth paper, as you recall, was given in two parts, one by Professor Sears and the other by Mr. Homicz. The first part of this presentation was related to engine noise and involved an investigation of blade forces arising from rotor-stator interaction in subsonic flow. One important conclusion was that the Kemp-Sears type of approximation can be extended to include compressibility effects by means of techniques suggested by Amiet and Sears. He also mentioned some apparent discrepancies in the results of Johnson on gust loads in subsonic twodimensional flow. But, in particular, the extension of the Kemp-Sears theory in the compressible range involved a first-order theory for unsteady flow that was analogous to the Prandtl-Glauert correction, but it had an additional effect, that is, a first order distortion of any time-varying boundary condition, which was referred to as the gasp approximation. It is very clear that this work cannot be applied to the transonic range or even to the super critical range, because the Prandtl--Glauert theory simply breaks down. This, again, points to the fact that a better viscous-transonic approach is needed. The noise problem is most acute in this aerodynamic regime. Finally, you recall, Greg Homicz gave the second part of the presentation: "Acoustic Radiation from a Plane Surface with Application to Rotors". He developed a general approach for predicting acoustic radiation from a plane surface that exerts a fluctuating load upon the surrounding fluid. But again, if your recall, nis analysis called for a linearized aerodynamic theory input. The same remarks that I made before pertain here, too.

It would now seem appropriate to have questions or comments from the audience.

Dr. Sheila Widnall:

I certainly agree with much of what you say. And when you and I talk about transonic flow, we know what that extension requires. I think many of the other people here may not realize how difficult transonic flow has always been for the aerodynamicist. It's one of those fields like turbulence, which everybody knows is very important. There have been very few strides made in transonic flow and these have always been won at great expense and great complexity. The reason that we use tools like linear aerodynamics analysis is that they allow us to predict an enounous number of phenomena with fairly good accuracy at a fairly low cost. The transonic flow is not that kind of a problem, although I certainly agree it is a very important problem. I would also make the remark that it is known that in the case of unsteady transonic flow, the linear theory is often much better than it has any right to be. I'm sure you are familiar with the work of Martin Landahl, who did a lot of work in unsteady transonic flow. In the unsteady flow regime, you may be much better off using linear theory than you would be in the corresponding steady flow case. This has an application to what Dick Lyon is doing. He is looking at an unsteady transonic flow problem, using linear theory. Because it is unsteady, it is very likely that his results are more accurate than they would ever hope to be in a steady flow problem. So, what I am suggesting is that I do agree that transonic flow, if we could do it, is very important. One has to realize how much that is going to cost. And I put quotations around the word "cost", because I don't mean just money. I mean our ability to understand our results and our ability to obtain results, including the fact that we would have to do separate calculations for every single set of parameters, every single case would have to be investigated as a separate topic, possibly numerically. So, that is a cost in our ability to understand the results.

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Dr. Robert Truitt:

I would like you to comment also on the compatibility of the best aerodynamics we can do. How do you feel about that as far as the noise is concerned?

Dr. Sheila Widnall:

Certainly the work that Harry Sternfeld and Boeing are doing shows that if you want to fly that tip at Mach numbers close to one, you might as well design it from Mach numbers close to one. Now nobody would ever design jet transport aircraft with straight wings to fly at Mach .92. There is technology in that field. Certainly supersonic or swept wings utilize planform shaping, and certainly the helicopters ought to take advantage of it. That's going to be rather slow in coming because it has to be done very carefully, but it's a direction in which to go. I do agree with you that if you do have an efficient tip shape from

the point of view of drag and performance, then I intuitively feel, as you do, that it will be more efficient from the noise point of view. Boeing correlations with critical Mach number of the airfoil section and the onset of very high impulsive loading and high impulsive noise certainly bear that out.

Dr. Fred Schmitz:

We, at Ames, have a group now doing transonic aerodynamics quite actively and the unsteady problem in particular. We are doing both theoretical and theoretical-numerical computations; that is, doing the full-blown problem. We hope to run some experiments within the next year in the wind tunnel on various operating conditions. I'm not an expert in the area, but I do know the unsteady problem is being attacked right now. And it's not just the Army; it's the Army and NASA -- a group of about six people who are attacking it. All of a sudden it's a very popular problem.

Mr. Meade Mitchell:

Bob, you triggered a thought that had been playing on my mind through the whole session -- your best shape aerodynamics would probably give you your best noise condition. There's an old adage, you know; "Where there's moke, there's fire". I've been thinking about this, where there's noise, there's vibration. If we can reduce the noise, I think it will have a great effect on reducing the over-all vibration of the helicopter, and that's of serious concern to us right now from the standpoint of the reliability and maintainability of the machine. So, I think we can relate noise to that aspect. We have active contracts right now trying to isolate vibration or study vibration in relationship to what has been done to the reliability of parts and maintenance on the machine. I know Sikorsky has realized some improvements in their maintenance of the machine using a damper on the rotor. Of course, we can isolate vibrations, but if we can reduce them, the reduction in noise, I think, will have a great payoff too. That is a point I wanted but forgot to make.

Dr. Paul Pao:

I have a comment to make which is not related to transonic flow, but to the question of how you get noise out from a sound source in a transonic flow? In some recent analysis that I have done, I found that in transonic flow conditions with a sound source embedded in it, the local condition due to the flow gives a very serious distortion to the acoustic properties near the sound source. So the correspondence between the sound source and the far field noise are quite different from what we can see from a simple wave equation as was used in the theory. I don't know how much this property will affect the intensity of the noise but certainly it has something to do with the directivity. Transonic flow is, of course,
an extremely difficult thing, but transonic wave equations are easier to handle. So as the first step, probably we can do something in that direction.

Mr. Ronald Schlegel:

Bob, just to reiterate something I have said earlier, but in support of something you and Meade had mentioned. We find that the work we are doing right now and which is in very active progress at Sikorsky to develop quieter and more efficient rotor blades is in exactly the direction in which you're talking. We are using transonic airfoils. We do find that we can achieve very significant improvements in performance with reductions in noise level which are on the order of five to ten pndb in the range in which we're looking. We find from the vibration point of view that, in fact, as you would intuitively guess, when you reduce this separation mechanism and improve your drag characteristics on the blade the vibration levels do improve. Also, we find, in the high speed flight regimes, very significant reductions in control loads. I think that a lot of this work we are doing now is really helping us finally if not to fully understand the problem, at least to probe in some of the correct directions. I'm not sure we really understand many of the mechanisms which are going on, but I think the indications from the research which we're doing are at least heading us in the right direction.

Dr. Robert Truitt:

Would you comment a little more on the optimum type shape that you're using or is that a trade secret.

Mr. Ronald Schlegel:

Well, I think the latter is probably true at this stage. I don't want to talk in detail, and frankly, I'm not qualified to talk in detail about some of the shapes which you're looking at.

Mr. William Nettles:

In the same vein in which Ron is speaking, I would like to point out that there is one thing you must keep in mind. Now, Dr. Whitcomb is doing some airfoil work, and the tendency is to use his airfoil. The helicopter blade section must operate over a very wide range of angles of attack, over a very wide range of Reynolds numbers, and over a very wide range of Mach numbers. Now, when you do that very frequently you find that if you design a blade section that will do one thing for you, make one point better, it makes the other point worse. Some recent work which Boeing is doing produced an airfoil that gives them an increase at low Mach numbers, but with the high Mach number range they have a problem. I don't mean to make a negative statement about what you're saying because I think this is perhaps the best point being made in this conference. But in considering the comments that have been made, I think it's necessary that you keep this practical problem in mind.

Dr. Robert Truitt:

Do you speculate that you might, if you were smart enough, change the airfoil shape under different operating conditions?

Mr. William Nettles:

You mean actually change the airfoil shape as you fly?

Dr. Robert Truitt:

Yes, perhaps changing the configuration with flaps. You might be able to do that.

Mr. William Nettles:

I would not want to be negative and say no. This is something we don't want to close our minds to. Command is working on what they call a controllable twist rotor, which I find fascinating because it does all kinds of good things like this. And I know you people don't like to hear about that. But we do, in particular with the heavy lift work -and this work is fascinating because we are trying to do something new, and we do run into this Mach number variation problem and Reynolds number problem. If you could, perhaps, come up with an airfoil change, perhaps it's worth looking at. Let me make one more point. Maybe I shouldn't say this. Dr. Truitt's comments to Sheila Widnall were very good, but then if Sheila Widnall had not done the work she has done, Dr. Truitt could not have asked the questions he asked. Now that's the problem that existed two years ago. Some of these questions couldn't be asked then, because nobody had done enough work at that point to ask it.

Mr. Richard P. White:

We have come a long way over the last three years in terms of vortex noise. I don't know if we've gone so far that we are sophisticated enough in vortex noise and understand it well enough that we've had the privilege of using it for systems studies. I thought that it was pretty good that people are really considering vortex noise. They're concerned with it in terms of flight paths, like Bob Simpson this morning. It wasn't too many years ago that if somebody said vortex noise, they would lock at you and say you were out of your mind. It did start receiving some recognition as a serious area that should be understood. If you understand it, you may be able to do something

about it. There are some handy formulas. Ron Schlegel had one that worked pretty well. And Martin Lowson had one. I think the first person I can remember that used it discretely in an analysis to determine what effect it might have on the correlation between measured and predicted was based primarily on how large the rotor loading was. Dr. Lowy and Gene Sadler indicated that even with the simplified analysis they could do at this time, it gives tremendously better correlation at a high frequency in a spectrum. Also, what they determined for one helicopter seemed to apply very well to another helicopter. This led to some things, and I think it was one of the forces that led to the two programs that were sponsored by ARO-D. We heard the preliminary results of those programs yesterday. All the data have not been analyzed yet. I think the session that I had the privilege of chairing was fortunate in that it covered a wide spectrum, with some very basic research being reported in which conditions were painstakingly controlled. One controlled experiment not truly representative of all aspects of a rotor in its natural environment was work recorded by Jim Scheiman. Then we went through the full gamut of looking at the importance of vortex noise as determined from the machine we call a hclicopter, working in its own environment. I think that the spectrum we have covered in this session pointed out something very interesting and something that shows a need for detailed analysis. I think the basic programs that were conducted under ARO-D sponsorship had a primary objective of doing controlled tests to demonstrate and show, hopefully conclusively, that from an airfoil type lifting section, discrete vortex shedding of the Karman vortex street type did exist and also to determine some of its basic characteristics. I think generally that those programs, within the analysis of the data that has been accomplished to date, have indicated that it does. At the same time these programs are going on, there are other investigators who have been doing some work making some measurements that have also indicated a discrete shedding on an airfoil does exist. There has been work at M.I.T. and by Dave Smith from the Air Force on the sail plane work.

It was very impressive to hear those tapes. When you come to that discrete tone, they can pick up a sail plane a quarter of a mile away. Robin Gray's very recent report with Allen Pierce indicated the extent of the noise that might be obtained by an airfoil shedding vorticity. The results of the two programs sponsored by ARO-D are somewhat preliminary because the investigators have not had the opportunity to analyze all the data they obtained. As for UARL, they are still obtaining some data. But I think some of the conclusions that were drawn or indicated yesterday are interesting to note again. There is an indication that there is a pure tone. But the frequencies associated with these tones are not what we expected. They are much higher, and they seem to be associated with the weight thickness rather than airfoil thickness. Dr. Sadler reported that in the work

he had been looking at there is some indication that the pressure fluctuation at these pure tone frequencies were correlated across the entire span of both the two-dimensional and the three-dimensional models, but they were not in the wake. That's puzzling. He also indicated in the figures he showed us that the models seemed to be vibrating at the same frequency as the pure tone, but the force output from the model through that vibration was not nearly sufficient to be the noise that was measured. Just possibly, then, that small oscillatory pressure might have correlated all the somewhat random effects we might have gotten from the shedding. It also indicated that the primary dipole associated with this is in the lift direction, not in the drag direction. We have had an indication that the laminar boundary layer associated with the pressure side of the airfoil might be one of the controlling aspects of the vortex shedding. As I've said, these are somewhat preliminary results the two investigators reported, and I think that when they look at the data in more detail and more extensively, we'll probably find other and more interesting things. I think the comparison of some of the data in results that were obtained from the basic controlled experiment to the controlled experiments of the rotor system to the somewhat uncontrolled experiments associated with a real life vehicle might shed an interesting light, and may be where we don't understand things.

I'd like to refer to the slides presented by Jim Scheiman. I thought what he showed here was very interesting. The indication from both the circular rotor and the lifting rotor with a microphone on the axis of rotation was that a peak output of the acoustic pressure occurred at roughly the same frequency. The db level from both of these is approximately the same. This is interesting because most Karman vortex-street shedding investigations have been associated with rods. I commend Jim for giving us this base point to work from. The characteristic dimension of the rod in its shedding is its diameter. If that be the case, and it seems to correlate very well, then I get the same frequency with the lifting surface. You can get strong indication that the frequency that was measured here was associated with the thickness of the airfoil and not the weight. That is different from what we got from the basic experiment with the fixed wing or models in the wind tunnel.

Another slide that Jim presented showed a lifting rirfoil. The measurements made on the axis of rotation and measurements made in the rotor point showed tremendous correlation in the lifting point in the axis of rotation. This is associated with measurements of vortex shedding in the lift dipole. He didn't quite show that in the rotor point. But it did show one thing: there is about 20 db difference in the peak levels, which indicates that the drag dipole is much weaker than the lift dipole. This apparently compares with the observations and conclusions reached for the isolated airfoil in the non-rotating flow field. Then Jim threw us a hooker. It was pointed out yesterday that this might be affected by the doppler effect.

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The oscillatory signal seems to peak in magnitude at the frequency that has been associated with vortex shedding. I think there are a couple of reasons for this. Even a circular rod can generate lift if it is in a sheared flow. If you have an oscillatory sheared flow created by the vortex shedding and quite possibly the lifting surface, that is why the lifting surface could develop an oscillatory lift. The circular rod could not, possibly because of the characteristic dimension of the airfoil versus the rod in the sheared flow. The wavelengths are about right to be magnified by the airfoil section. Also, in the picture of the experiment that he showed, the flow was over the motor, over the strut and into the rotor. The induced flow that I might have had with the turbulences that Sevin Wright showed yesterday could cause a pressure to be developed. This might be coming from the oscillatory pressures that are developed by working the shear flow or possibly slight interactive turbulence over the strut that excites one of the natural modes of the model. Due to the doppler shift as it goes around in the rotor plane, we see a spectrum like this. There might be a reason for it. I suggest that he ought to take a look at his data to get some information on this. I don't think it is a problem of concern in terms of vortex shedding and lift. He also noted in his paper that tip shapes did not seem to have much effect. Does this indicate to you the possibility that maybe the maximum output of the noise is not associated with the high Q area? This is something that you intuitively don't expect.

There is indication in the measured data when you get all the other types of noise sources out, that the basis of vortex shedding as an important noise source is there. The papers that were presented in this session and the data that was given to us to review and analyze raise a very serious question. Generally you first do a basic, well-controlled experiment. You are given the results and analyze and understand everything that's going on. I think from the differences that we have seen between static-type rotor tests and free rotor tests, compared to real basic experiments, there seems to be too many areas of disagreement to get the meaning that we need to support ourselves in analyzing vortex noise associated with real life systems. I thought this was a very good session. We have learned a lot. From what Kevin Johnson presented, there is a strong indication that a semi-empirical method can be devised which encompasses all different types of noise and which can be used for prediction of helicopter noise of a given configuration, given the basic parameters. That's not the first time that a semi-empirical analysis that's related to basics has been able to do a very good job. But I think we have a long way to go yet before really understanding vortex noise, and I'd appreciate getting your comments along these lines.

Mr. Harry Sternfeld:

The comment I wanted to make, hoping maybe it will trigger somebody else's thinking, is that one of the things that's vexed me involves blade slap. I'm using the very general term, but I'll say specifically tandem, although the frequencies aren't very different when we get it on our single rotor tower. We get harmonic spikes. They have an envelope and they peak right up at around the same frequency that we usually associate with vortex noise. There was no lift so there shouldn't have been a vortex. In addition, that frequency doesn't seem to move around very much if we make an airfoil change or something like that. So, my comment is that the characteristic that was shown by Schieman is very similar to the characteristic we see when we get through harmonic analysis.

Mr. Richard White:

As most of you know, I'm a proponent of vortex noise. I'm glad Harry made the initial input here, and I think the work of Robin Gray is pertiment to what he is saying. What is wrong with saying, or assuming, that a Landau shock on the blade causes separation? Can I not possibly feed in that characteristic? If I get near stall, can I not get the same thing? Robin Gray indicates that maybe you can. I'll explain any noise in terms of vortex shedding, so let's keep an open mind.

Mr. Ronald Schlegel:

What I'm going to say is an open question relative to shock formation. We concluded that the formation of a local shock on the blade itself, in relating the phenomena of the acoustic dissipation to the impulsive noise in the far field, was not an important factor. However, our impulsive noise study did conclude that blade drag and drag divergence formation was very important. The work we are doing on the full scale model tends to show that for a transonic airfoil as you move the shock formation on the suction side of the blade back, you stabilize the shock. Then, in fact, the noise does go down. I wonder if anyone here has given much thought to the acoustics of the oscillating shock. In other words, what are the acoustic characteristics of the oscillating shock? What does this do to the subsequent turbulence and loading on the rest of the blade, and is the stability of the shock formation important acoustically?

Mr. Chris Bobo:

That is exactly the mechanism we are using to define impulsive noise. The vortex interaction is the trigger for moving that shock wave, and if you think of it as an impulsive change in Mach number or angle

you get, therefore, a pulse in that shock wave position. And that pulse radiates to the acoustic signal.

Mr. William Nettles:,

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I'm not speaking on this particular topic, but on an earlier topic that Harry made. Perhaps what I'm going to say isn't too terribly pertinent but in preparation for some of the testing we did to get you the data for your vortex noise work, we went over to West Point, Virginia, which is a very quiet area. It is a deserted air field. We did some preliminary noise measurement and when we evaluated what we got, we found that there was an unusual spike in the spectral analysis data. After further evaluation we found that it was a dog barking in the distance. Now, if I find anything in the future that comes at that particular frequency, I think I'll say maybe it's dogs barking in the distance. I have some reservation in drawing conclusions too quickly based upon that one experience. I disagree with some of what Jim said. I disagreed also with some of what Harry showed yesterday. He showed some work relative to bladevortex intersection which was particularly interesting and was left unanswered. I recommend that we try to leave these questions unanswered until such time that we have a thorough review of what we have and a rigorous explanation.

Mr. Peter Arcidiacano:

It seems to me that it's possible that one path of speculation might indicate that there is no vortex noise: that a well streamlined body operating in turbulent free air may not, indeed, generate any vortex noise, particularly if one includes such things as surface roughness on the airfoil to perhaps eliminate the pure tone that we did observe under very specialized conditions. Certainly in the high Reynolds number ranges and even up into stall, the pure tone did disappear in this turbulent free environment. I wonder, and I'd like to suggest that perhaps a lot of what people have been calling vortex noise may in fact be turbulence generated noise.

Mr. Richard White:

I refer to the data that Dr. Sadler was analyzing which we obtained in your tunnel. We talked about this high frequency, and I had them try to generate some turbulence. They put a tripper on it. It didn't do anything. I think I have to take exception to some of what you say. However, we hope that the data that we are getting and that we, as well as you people, are analyzing will give us information to better understand what I am calling vortex noise in a rotor blade. We get very strong indications on controlled rotor tests that this is in fact there. But it does not correlate with what we are getting with our fixed wing tests.

Mr. William Nettles:

I refer to Jim Scheiman's work. With air flow, it appeared that the spectral character of the rotor was definitely changed. Instead of having that hump associated with vortex noise, we had almost a concave signature except for that one little peak, which Jim says he doesn't believe. So, I can view that as saying that turning the air on removes the wakes from the other blades, reduces the turbulence encountered by the blades and there is no vortex noise.

Dr. Sevin Wright:

One shouldn't say they believe or don't believe in vortex noise. I think first of all we should discuss what we mean by vortex noise. The sound that radiates in the upper frequencies is usually referred to as vortex noise. I think we should remove that word vortex and talk about the noise in the high frequencies. Both mechanisms exist. what you call vortex noise, I would prefer to call blade self noise noise generated by the blade operating in clean flow conditions that minimum noise you would get from an airfoil. The purpose of the demonstration yesterday was to show how you can increase that minimum self noise. We run the rotor in free air, no obstructions upstream, no crosswind, no blowing, and the rotor noise was minimal. As soon as we made any external disturbance on the blade, the rotor noise went up. If you look in a propeller spectrum, or a helicopter spectrum, in the high frequencies, you will find a proportion of broadband noise which I think most people credit to the shedding mechanism. It would tend to be random and would give a random output, and therefore the spectrum would be continuous. But any kind of asymmetry in the loading will produce rotational noise and a discrete spectrum. If it is periodic, then it will be discrete, or as the last speaker indicated, if the inflow in wrong, if it's incoming turbulence, then that will give rise to an increase in the broadband noise. So, it's not an argument about whether it exists or not - both forms of radiation exist. The argument really is how much of which dominates. In the absence of obvious external influences, then I think your self noise is the dominant feature.

lir. James Scheiman:

I agree with the comments of Dr. Wright, and I think the problem is more of terminology. For example, von Karman described airfoil drag with vortex streets. If you associate vortices with airfoil drag, then fine. Also, in case of lifting on the airfoil, if you take the starting and stopping shed vortices and say that they rediate noise, and then put fluctuating lift on the airfoil, and then put fluctuating starting and stopping vortices, and if you believe Prandtl's theory, then I think it's hard to separate. You are describing the same phenomena by two different mathematical techniques. What you mean by

vortex noise is what it amounts to, I think. The other comment I have is that in addition to the testing that we did, we put some transition strips on the airfoil and we definitely had separation. These transition strips were directed towards changing the airfoil characteristics. I think it was published in a NASA-TN, which came out just a few weeks ago. But the strips caused an increase in the airfoil noise and there still is a peak in the radiation pattern. One of the problems that is bothering me right now is in the 2-dimensional testing. Why is it this has the discrete radiation whereas in 3-dimensional testing where the Strouhal shedding frequency is different along the full span, we always get one predominant frequency shedding? Why isn't it more broad? What radius dominates the other radii in determining the frequency center? Why is it that with a transition strip in it, definitely creating turbulent flow, we had a center band frequency, whereas from the 2dimensional tests that were performed, evidently with transition or turbulence on the airfoil, there is no discrete frequency. I think these are all questions that will require further investigation.

Mr. Richard White:

I would like to take this opportunity to thank all the authors in my session for their work in preparing these papers, and in presenting them.

Aerodynamic Test

Professor Rene Miller:

Well, we'll try to sum up. I think maybe I'd like to go back to our meeting of 1968 and remind you of a curve that I showed at that time, which I think emphasizes the importance of test in the evaluation of helicopter rotor noise. This slide shows the penalty that is paid for producing noise based purely on test results. It's based on Sheila Widnall's data. It tells you that as you reduce the tip Mach number you're going to get a penalty in performance and that the main reduction in noise is going to come from reducing rotor tip speed. I think we have to bear in mind this basic problem which we have is just to cut down rotor noise. I think Colonel Buchan made the point very clear last night that we can't wait for very refined theories: we have to do something about rotor noise. There is a limit to how far you can go in reducing rotor noise by reducing rpm. This limit is actually a limit due to the geometry of the rotor. Only a certain number of blades can be put into the rotor before the weights go up asymptotically. So far we really have nothing in the past two days which indicates that we have a real means of reducing rotor noise

other than reducing tip speed and increasing the number of blades, and, of course, playing around with the separation of the rotor to reduce the impulsive noise. We should not be concerned with trying to differentiate between vortex noise and periodic noise, but should try to concentrate specifically on the problem of how to cut down the noise. So far, the only tools we have are from test results. Consequently, I think that the papers that were presented in this. session on the aerodynamic test are of particular significance. I would like to draw your attention to one item which you can also see by looking at the data. The test data for rotational noise presented by Boeing and Sikorsky both show about a 10 db error between the calculated and the experimental data. The problem that we are up against is that we really have no techniques at the present time for predicting rotational noise. This is primarily because of our lack of knowledge of the high frequency content of the rotor. The paper by Sevin Wright contained the interesting statement that, as I interpret it, given the periodic forces, you can predict the noise. However, we all realize that these forces are not yet given. The paper by Harry Sternfeld showed a fascinating problem which is associated with the lack of bang at vortex interaction. A follow-on paper by Bobo on the effect of drag rise on triggering this slap was an interesting and original contribution. It would be interesting if Harry would expand his paper and play us a tape showing how, by these straightforward things that I mentioned, he has succeeded in achieving an appreciable noise reduction.

Mr. Harry Sternfeld:

I am sure you will all recognize that this is extremely spontaneous. Professor Miller and I had discussed this and we thought the two things which this tape illustrates are: (1) we've got to produce now, and (2) we know that better can be done, but we can't wait. You've heard a lot of reference to the 347, a Chinook derivative, throughout the meeting by other speakers. There will be three steps in each of these sound tape sequences. The first is the original Chinook, the A model, which had absolutely no concession for noise reduction in its design. The performance and production costs were the driving parameters. Then we came to the C model and found out that if we adjust the rotor tilt we can make improvements, particularly at high forward speed. So, the C model has different blade vortex separation. The 347 was made from the Chinook, but reduced rotor noise and elimination of rotor bang were primary program objectives. We made the aft pylon 30 inches longer and we made the fuselage 110 inches longer. That got us blade vortex separation. we put a 4-bladed rotor on it and slowed the tip speed down from about 720 to 650 feet per second. The first set of tapes is in the sequence of first the A, then the C, and then the 347. We will hover, fly at 50 knots, 120 knots and 167 knots on the 347. One of the places where the problem is not solved is in hover. The

microphone on the fly-bys is 200 feet on the right side of each aircraft. The microphone in the hover is at a 200 feet radius at the azmuth of the worst impulse noise. This azimuth changes and we can relate it to the position of the blades in the vortices. (The tapes were played and noise reductions were evident.)

Professor Rene Miller:

I think these tapes are very interesting. The need for these test data is extremely evident - we need tests badly. However, this doesn't downgrade in any way the need for theory, for unless we have the theory and analyses we really don't know what we are testing.

I had to cut the discussion off yesterday at several places. In the paper by Sevin Wright we were in the midst of discussing the classical topic of "Can the rotor noise be entirely described by periodic forces?" In the second paper, I think there was sufficient discussion unless you want to comment on the tapes we heard this morning. The third paper was an interesting survey by Barney McCormick on his work. He showed a comparison between the simplified theory and the test. These simplified theories are always attractive as a means of understanding the phenomena with which we are dealing. The discussion ended on a question as to how important the angle of a dissection was. The fourth paper that came up was by Mr. Schlegel. Now, let's continue yesterday's discussion.

Mr. William Nettles:

With regard to the data that Harry just showed us, and I'd like to address this to Sevin Wright in particular, there are two ways that Mach number can get to us. They are perhaps dependent, but they could be called quasi-independent, whatever that means. One is in the compressive effect on the aerodynamic noise source. The other is the compressibility effect on the propagation of the noise. I believe these two are essentially independent. If my contention is correct, does Dr. Wright think the increased tendency toward popping as Mach number was increased was the result of the propagation effect or compressibility effect over the airfoil itself?

Dr. Sevin Wright:

I think there were three Mach number effects there. One is the source strength or the effect of aerodynamics. Then, the effective Mach number affects the radiation cancellation mechanism. Thirdly, the effective Mach number affects the directivity and also the sound power radiated through the doppler effect. So, there are three points there.

Mr. William Nettles:

Mr. Sternfeld's tape seems to show an increasing popping characteristic when you increase the Mach number. My question concerns the cause for this.

Dr. Sevin Wright:

I think it's basically the source, the fact that it increases the intensity of the magnitude of the fluctuating lift on the blade. This increases the radiation, therefore, increasing the popping sound.

Dr. Richard Lyon:

I have to take issue with that, at least in terms of our calculations. Our studies of the effective radiation of the tip due to thickness and lift effects simultaneously have in them, explicitly in the analyses, the effect of the changing speed on the source strength and the effect of the changing speed on the radiation efficiency, which is what Sevin meant when he said the cancellation effect. Now, it's very clear in our calculations for acceleration of the blade near Mach 1 that the radiation efficiency effect far outweighs the effect of fluctuating lift or the fluctuating sources due to volume displacement on the blade. These come out as explicit terms in our analysis. We can compare one against the other and there is no question that for accelerations near Mach 1, the radiation effect is far stronger than the source strength effect. You have to evaluate the source strength at the point of maximum radiation, it has that effect, but the fact that it fluctuates in strength near that point of maximum speed does not have an effect. It's merely the acceleration and deceleration of the blade.

Dr. Sevin Wright:

I agree with you if it's a point source and you're talking about steady forces. Near Mach 1 these things tend to dominate. But I think blade slap is a particular case where it's a very local region in the disc that radiates. You can almost treat it as a stationary problem, because the blade slap impulse is not to be regarded as in motion. The point at which it occurs is a particular point in the flight path and it's not as though you're treating the problem as a constant source in motion. It only occurs a few milliseconds for each blade revolution and so the stationary approach would give you this effect without any cancellation.

Dr. Richard Lyon:

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The directivity, itself, denies that assumption, because you cannot have directivity from a point source that is strongly leaning forward. It takes, in fact, a convection effect which means that the wavelength

nust preserve itself over several of its own lengths in order to get sufficient coherence along the flight of the source in order to radiate directively. So, the fact that you get for the thickness effect a solid cone of only 10 degrees and for the lift effect this double cone, but still within a beam width of about 15 degrees, itself means that the source must be important over about 3 or 4 wavelengths at the frequencies you are considering. You cannot have directivity unless you have a source that is extended in phase. Now, it looks like a point source when you take a picture of it but it must preserve itself over some distance in order to have that directive effect.

Dr. Sevin Wright:

Have you measured these directivities for impulsive noise, such as blade slap? Have you shown that the dipole is in fact pushed forward? We are familiar with this idea that in forward flight, the directivities move forward. I'd like to ask Harry Sternfeld about the directivity of the recordings we heard this morning. I have not heard many tandem rotors banging but on single rotors the directivity is always pointed forward. In other words, you hear the banging on approach and it ceases overhead. And that was the point where Jim Scheiman cried "vortex noise". We heard the banging and as soon as the helicopter passed overhead the banging ceased and, in Dick White's terminology, the vortex noise was audible. The way I see that is, if you think of a simplified model of a dipole produced by this very localized loading in the disk, this dipole will be tilted, depending upon the angle of attack, and so on. You can explain this very nicely if you assume that the dipole, particularly on a single rotor, is tilted forward as a function of the blade angle of attack. The lower lobe of the dipole will be pointing forward and the upper lobe will be pointing up in the air, so, you will only hear sound in the forward direction.

Dr. Richard Lyon:

A dipole that is tilted forward has a directivity index of 6 db and I think the directivity is stronger than that.

Dr. Sevin Wright:

Along a line normal to the dipole, the radiation is 0, so you have an infinite number of db's from right angles to along the axis of the dipole.

Mr. Harry Sternfeld:

I have two pieces of information to impart. First of all with respect to directivity, if you listen carefully or if you look at a stripout of the tape as the aircraft approaches in the distance you would see

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that with a tandem rotor the number of pulses is twice the blade passage period of one rotor. As the aircraft gets close to overhead but is still on the approach, you will hear that period halved. Then you can hear the squish which may be vortex noise or modulated engine noise. The length of time that the single rotor noise exists correlates quite closely with the time it takes the aircraft to travel the distance between its two rotors. So the noise is very strongly radiated forward and in the distance we're seeing it coming from the two rotors, then we have a period when we see it coming only from the one rotor and then it goes away. The other point of information I wanted to supply was that if we plot the sound pressure level against Mach number, look for a knee in the curve, and then we plot those, the shape just about follows the drag divergence curve for the airfoil and seems to be in the vicinity of Mach 0.5 to 0.6 or higher. The shape appears to be very strongly associated with the divergence curve.

Mr. James Scheiman:

I'm not sure the distinction between vortex noise and rotational noise is really clear. For example, I think Loewy and Sadler, in their theory in which they try to describe a vortex noise, show there is fluctuating lift force at the rate at which von Karman vortex streets are shed, and there is a fluctuating drag force which is twice the frequency of the fluctuating lift force. Prandtl described the whole lift on the airfoil with his lifting line theory. Now, if we say we're going to use lifting line theory to describe the lift forces on a blade or the fluctuating lift forces on a blade, then the problem is one of using the vortices to describe the fluctuating pressures on the blade or is one of using the fluctuating pressures on the blade to calculate its noise. I think we're both trying to solve the same problem, looking from different directions. I think it's wrong to say it's all vortex noise or it's all rotational noise. I don't think we understand enough about it and I think vortex noise terminology is a poor choice.

Dr. B. W. McCormick:

You mentioned that in order to predict the impulsive noise we would need to know the shape of the pulse which is producing this. I think here is an area where we need some further testing. Nobody really knows the shape of a vortex coming off a rotating blade at high Mach numbers. There haven't been any measurements. Somebody should give some thought as to how to obtain a velocity field through a vortex coming off a rotating blade at fairly high Mach numbers. Also, let me mention the effect of the intersection angle where Dr. Widnall and I seem to have a disagreement. She said at the lower values of intersection angle she obtained a higher noise level. I said that at the lower angle the pressure differences across the section tended to decrease. In the lower angle intersection case, the entire blade

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is being influenced at once by the vortex and even though you may have smaller differential pressures, the noise level could certainly be higher in that case. So I'm not sure there is really a disagreement.

Mr. Ronald Schlegel:

I think in our rush yesterday we missed a few points in the study which we had conducted. I'd like to take a few minutes to hit some of its highlights. This study has just been released by AVLABS as Technical Report 70-72 of June 1971. It's a rather comprehensive study and I think it has some good data in it. As a matter of fact, it asks a lot of questions and doesn't necessarily answer as many as it asks. We were looking at rotor impulsive noise (RIN) as an impulsive noise. I want to point out the purpose and intent of the program. We had a program which was being conducted on the CH-53A to measure rotor loads. A blade that was very well instrumented with surface pressure transducers both chord-wise and radially was used. Since this is one of the few aircraft that we built that we have been able to experience rotor impulsive noise on, it offered to us an opportunity to study this phenomena. We contracted with AVLABS under the direction of John Yeates to conduct this study along with the loads study. It was really a 3-phase study. It included measuring noise concurrently with measuring the loads on the helicopter and also at the same time conducting some inside measurements of the noise generated. The second phase was a data analysis phase in which we looked at the data with greater detail than we had before. All of the data was reduced using real time analyses. we saw some things which we had never seen before, such as the fact that has been brought out today by many people that rotor impulsive noise is a manifestation of rotational noise. In other words, it is periodic noise. By doing real time analysis we are able to see that it was very ordered noise, extending well out into the 400 - 500 Hz regions. We were also able to determine that the types of impulsive noise which we got, at least on the CH-53A type of helicopter, were different for hover and cruise conditions. The hover rotor impulsive noise is more associated with blade loading vortex interaction and the cruise noise was extremely directional in the forward plane of the rotor, indicating the probability of blade Mach effects as well as profile drag. We did some modifications to our acoustic analyses which included blade motion terms. One of the things which we also tried to show was whether with this acoustic analysis we could even approach the prediction of rotor impulsive noise. We got some sualitative agreement. We found that without the inclusion of the arag and the source translational terms for the forward flight case, where we started getting into rotor impulsive noise, that we were not capable of predicting the highly directional characteristic of the sound nor were we able to predict the level to any extent. In other words, the analysis failed for high speed rotor impulsive noise.

We were not able to predict above the 4th or 5th harmonic for even normal inflow conditions such as hover very well either. As Dr. Truitt mentioned earlier, there is an awful lot of work to be done to gain a better understanding of the higher harmonics of load. Another conclusion was that when we modified the analysis to include blade slapping and coning as steady and first harmonic effects, we did not significantly improve the correlation of measured and predicted noise level.

I would like to recommend as one final thought that we make a concerted effort, possibly through some central committee which may be the AHS or another organization like ASSP, to standardize some of the terminology which we use.

Professor Rene Miller:

I don't think we want to lose sight of the fact that right now the only way to reduce rotor noise is by slowing down the rotor and increasing the number of blades. From the chart I showed, we see that 10 db reduction is going to cost 20% - 30% increase in gross weight. You can tolerate that on a commercial vehicle because direct operating cost doesn't change much with gross weight for many reasons. We obviously can't tolerate it for military aircraft. The important thought I would like to leave on this session is that what we need right now more than anything else is not so much a better definition of the terms, but more tests which give us other tools than cutting down the rotor speed, such as blade tips and revised loading distribution on the blade, to reduce noise. Much of the work that is going on now on non-rigid weights will give some indication on how to do this. We need more tests and more theory on how to interpret these tests, but we have to find one other way of reducing noise than just reducing tip speed. I think it is important to recognize, too, that we have other vehicles than the helicopter coming along, which have entirely different noise characteristics. I'm thinking of the tilt rotor and the tilt wing. We do have to get test data to try and get a better handle on how to reduce the noise.

Environmental and System Studies

Dr. Franklin Hart:

Let's briefly look at the section on environment and systems studies. One item early in the program was identified as detectability and annoyance. There were three main sections under that heading. One was ground and environmental attenuation in masking, utilizing existing theories. The types of recommended tests involved were field tests to be made under different environmental conditions involving troops and aircraft. Another area was strictly subjective response and a third was criteria. Under the heading of systems analysis, the

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topics were vulnerability vs. noise reduction, management of effectiveness of noise reduction and development of Army criteria and the penalties involved. I think you can see, based on what we had in this combined session, that this area is perhaps lagging in terms of total effort being given to all of the areas that have been identified as being prominent. Particularly, we are talking about annoyance and detection, and these things are not the same. Which should you give priority to? I am not sure we have gotten to the point here where we can really ask all the right questions.

The first of the three papers presented was given by Bob Simpson. Here he was talking about direct operating costs vs. noise and procedures for achieving operational reductions. He utilized the term vortex noise. He did have an analytical term there that he could put into his program, and I think we should keep in mind that that was the essential point. Also, I believe he indicated that on the data he used the annoyance, the PNL, was something like 10 plus the sound pressure level. This is a very restricted look at the total noise of the aircraft. This is certainly no criticism because all of these things can be built into the model when he has the right analytical predictions techniques.

In the second paper, Pao covered sound attenuation over simulated ground cover. He showed that there were selective frequency bands where you get more attenuation. The discussion following the paper started on the fact that he used a simple source and how these predictions change if you use a more realistic sound source, as for example a helicopter.

The last paper, by Dr. Evans, was on atmospheric absorption of sound. Mitrogen was identified as a more important part of the absorption than previously reported. It was also pointed out that some of the people working in the field would like to have the data cover at least one additional octave band beyond what he had in the paper. Also, he discussed how he is going to bring temperature into the atmospheric absorption picture. The problem of human factors, which we like to think about in systems has received little attention here. This area of environmental considerations and systems analysis is not receiving the effort that some of the other areas are. Now, I think it would be well to ask for points of discussion on Bob Simpson's paper.

Dr. Richard Lyon:

You pointed out that there are loudness criteria and there are detection criteria. If we do achieve V/STOL aircraft at perceived noise levels of 95 db at 500 feet, that means that at a quarter of a mile away they are in an urban background noise. Perhaps the proper question then is one for criteria. That is, maybe you can

detect it but can you classify it. I bring that up because there is a very interesting set of tapes by Hamilton Standard on the DHC-7 flying past at a distance of, I think, a quarter of a mile in the presence of urban background. There is a freeway nearby, and when the DHC-7 goes by, it is clearly audible but it sounds like a truck. That is, if you don't know it's there you cannot tell that it's an airplane. When we begin to get these aircraft quieter, from a commercial point of view the criteria may include classification.

Mr. William Nettles:

The fact of the matter is that detection is a problem. But as far as the Army is concerned, I think they are beginning to realize that the man working around a helicopter, the man flying in a helicopter, whether he is crew or passenger, must be thought of as well. I believe the Army is beginning to recognize this as more of a problem, particularly when they are working on something like the heavy-lifthelicopter where men will be working on the ground below the helicopter. One of the interesting points is that anything that you do to quiet in the detection end will probably help you in the other end as well. So I think the Army is giving consideration to this other problem.

Mr. Richard White:

I'm going to use this last session and Simpson's paper as an excuse to say something else. What we have been working on is getting rid of the problem area of the tip vortex. We have been notably successful is small model experiments and have obtained almost negligible degradation of performance. We are going to test a large tip section of the HU-1-D blade. If we are successful with the full scale blade section, we hope this can be followed by a whirl tower test, running under conditions of rotor blade slap to demonstrate that we did get rid of the high induced effect because we have gotten rid of the vorticity.

Mr. Harry Sternfeld:

I just want to read into the record that Langley is doing quite a bit of work in the Human Factors area. They are sponsoring Sikorsky's program on vibration and noise on pilots. We have been involved in programs on subjective response to V/STOL noise and so have other people. So there is an agency which is working on this in conjunction with the Army and independently. This should be at least recognized.

Mr. Richard Lewis:

We, at the Aviation Systems Test Activity, are conducting a very comprehensive series of tests in conjunction with the people at AVLABS,

in which we are going to be measuring in-flight vibrations on all of the fleet aircraft. We have also done some work of great importance to the Army on the effect on crew environment during weapons firing. I think you know that most of the aircraft are flown with doors off. We have measured sound levels on the OH6 during firing of very small weapons (the 5.56 and 7.62) in excess of 150 db in the cockpit. This is another area that may be of great interest in the future.

(Call for discussion on Ground Attenuation and Atmospheric Absorption)

Dr. L. B. Evans:

I would like to comment that when you try to correct your data and use our curves, be aware that these absorption coefficients are plotted as a function of frequency over pressure. For an extreme case, a half atmosphere pressure of 1000 Hz signal gets absorbed like it's 2000 Hz. If it's low humidity, this can make as much as 5 or 6 db per 1000 feet. If I am going to put out this interim report and set of tables, I would like to be sure that I have the coefficients and type of units engineers would like to use. So, let me know if anybody wants anything different from db per thousand feet. Another question. We've heard a lot about helicopter noise, but nothing about the infrasonic spectrum. Is it important? Does a helicopter put out 1 Hz signals? The reason I ask this is that Harry mentioned you could hear this one helicopter five miles away. If it puts out an infrasonic signal, you might be able to hear it 20 miles away. Does anybody have any information on this? Is the Army even interested in this type of detection? Does anybody know what the spectrum might look like?

Mr. Harry Sternfeld:

We certainly have the blade passage period, which is, if you like, infrasonic, depending on the aircraft it could be 10 Hz. So there's certainly that fundamental which falls off on the audio range. I can't speak below that - I don't know if anyone can. But certainly fundamental blade passage periods of the order of 10 - 15 are very common, so it's not unimportant.

Dr. L. B. Evans:

Very recently I have seen data from White Sands Missile Range detecting a cannon shot 47 miles upwind, and to me this is rather remarkable. They are looking at 1 Hz signals. Also, at Ft. Monmouth they detect the Saturn V first stage when it reenters the atmosphere about 1500 miles away. Again, it's 1 Hz type signals. So, perhaps there is a long range detectability factor here that we could look at.

Mr. Richard Ballard:

I would like to thank the session chairmen and others for their participation.

Mr. James Murray:

I want to thank you all for participating. There has been some suggestion that there be a follow up meeting of this nature. Any suggestion of this within the next year or two year's time is entirely dependent upon the productivity of you people, and the efficiency with which you do the work in question - whether you think it would be satisfactory to have a meeting two years from now or three years from now, ten years from now or six months from now. Any suggestions as to where it should be, how it should be or when it should be?

Dr. Sheila Widnall:

What is the relationship between this meeting and the Theme reviews that you have?

Mr. James Murray:

This is more specialized. We have over 30 projects in the helicopter area, of which this is a component part representing about 8 or 9. We'd rather break it up because it gets a little too specialized. After all, you've had four sessions here. I'm afraid the other twothirds of the investigators in the program might not find it attractive. We would be running double sessions and I don't think we are in a position to do that at this time. My suggestion is that the next meeting should be hosted by the Ames people if they are so inclined. In that way, their people out there could participate a little bit more directly.