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Submitted by

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I. Rudnick, Project Director

Hypersonic Attenuation in the Vicinity of the Superfluid Transition of Liquid Helium

by

Daniel E. Commins

Details of illustrations in this document may be better studied on microfiche

Office of Naval Research Contract: N00014-69-A-0200-4014 NR No. 384-302 Department of Physics University of California Los Angeles, Calif. 90024 いたいにおいたいとうないないに、

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3 ABSTRACT The relative ultrasonic attenuat	ion in liquid	helium at	1 GHz has been
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FIRST SOUND						
ATTENUATION						
CRITICAL PHENOMENA						
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# LIST OF SYMBOLS

<b>A</b> :	Signal Amplitude
C <sub>p</sub>	Specific Heat for Constant Pressure
cs	Specific Heat Under Saturated Vapor Pressure ;
C <sub>v</sub>	Specific Heat for Constant Volume
Не	Helium
He I	Helium Above the Lambda Transition
He II	Helium Below the Lambda Transition
He <sup>3</sup> , He <sup>4</sup>	Helium Isotopes
к <sub>т</sub>	Isothermal Compressibility
k	Boltzmann Constant
<b>k</b> , ,	Wave Vector
k,	Light Scattering Wave Vector
k n	Neutron Scattering Wave Vector
k i	Ultrasonic Wave Vector
<m></m>	Magnetization
'	Order Parameter
P'	Pressure
S	Entropy per Unit Mass
S <sub>s</sub> :	Entropy of the Superfluid per Unit Mass
s	Ising Spin
t	Time
T	Temperature
T <sub>λ</sub> ;	Lambda Temperature for He <sup>4</sup>
T <sub>c</sub>	Critical Temperature
TP	Temperature of the Attenuation Peak
u <sub>1</sub>	Velocity of First Sound
u	Velocity of Second Sound
u_4	Velocity of Fourth Sound
u <sub>o</sub>	Zero Frequency Limit of u
u <sub>co</sub>	Infinite Frequency Limit of u
V <sub>A</sub>	Acoustical Signal Amplitude

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v <sub>E</sub>	Electrical Signal Amplitude
vn	Normal Fluid Velocity
vs	Superfluid Velocity
α	Attenuation of First Sound
α <sub>abs</sub>	Absolute Attenuation
α <sub>c</sub>	Classical Attenuation
α <sub>KC</sub>	Khalatnikov-Chernikova Attenuation
$\alpha_{LK}$	Landau-Khalatnikov Attenuation
α <sub>total</sub>	Total Attenuation
α <sub>κ</sub>	Attenuation Due to Thermal Losses
α <sub>n</sub>	Attenuation Due to Viscous Losses
β <sub>p</sub>	Isobaric Coefficient of Thermal Expansion
β <sub>sat</sub>	Coefficient of Thermal Expansion Under Saturated
	Vapor Pressure
β <sub>T</sub>	Isothermal Compressibility Coefficient
Ŷ	Ratio of C <sub>p</sub> and C <sub>v</sub>
δ	Acoustical Path
Δ	Complex Gap Parameter
ε	$(T-T_{\lambda})/T_{\lambda}$ , Normalized Temperature
ζ	Volume Viscosity
η	Shear Viscosity
n <sub>n</sub>	Shear Viscosity for the Normal Fluid
η <sub>s</sub>	Shear Viscosity for the Superfluid
κ	Heat Conductivity
λ	Lambda (Transition)
ν	Frequency
ν <sub>A</sub>	Interatomic Collision Frequency
ξ	Correlation Length
ρ	Mass Density
ρ <sub>c</sub>	Critical Density
ρ <sub>n</sub>	Normal Fluid Density
ρ <sub>s</sub>	Superfluid Density
τ	Relaxation Time
τ <sub>eff</sub>	Effective Cut-off Relaxation Time

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τ<sub>1</sub> ξ/u<sub>1</sub>τ<sub>2</sub> ξ/u<sub>2</sub>τ<sub>pr</sub> Phonon-Roton Relaxation Timeτ<sub>3+2</sub> Five-Phonon Process Relaxation Timeψ Wave Functionω Angular Frequency

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I wish to thank Professor Isadore Kudnick for his guidance and for his support and friendship.

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Merci!

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# ABSTRACT OF THE DISSERTATION Hypersonic Attenuation in the Vicinity of the

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Superfluid Transition of Liquid Helium

Daniel Edwin Commins Doctor of Philosophy in Physics University of California, Los Angeles, 1972 Professor Isadore Rudnick, Chairman

The attenuation of first sound waves has been measured in liquid belium at a frequency of 1 GHz. Absolute measurements were performed with a variable path interferometer for temperatures extending from 1.1°K to 4.2°K. The results confirm those obtained earlier by the same method and those obtained from the Brillouin spectrum of scattered light. They can be described in terms of three regions: a) the normal fluid region above 2.3°K where the attenuation is attributed to the classical losses associated with viscosity and thermal conduction; b) the critical region between 2.0°K and 2.3°K, where the attenuation has a sharp peak occurring near  $T_{\lambda}$ ; c) the superfluid region where the attenuation shows a broad maximum centered at 1.5°K and which is in agreement with the Khalatnikov-Chernikova theory. When the 1 GHz results are compared with the Brillouin stattering results, which vary in frequency from 556 MHz to 768 MHz, it is found that the attenuation scales as  $\omega^2$  over the whole temperature range with the possible exception of the data below 1.5°K and in the immediate vicinity of  $T_{\lambda}$ .

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In the critical region, extending from 2.0°K to 2.3°K, more accurate attenuation measurements were performed with a fixed path interferometer. The helium sample was isolated from the helium bath and its temperature was allowed to drift as slowly as  $3 \times 10^{-6}$  °K sec<sup>-1</sup>.

The attenuation exhibits a sharp maximum in the region of the lambda transition; the largest value is about 2500 cm<sup>-1</sup> and occurs at a temperature  $T_{\lambda}$ -  $T_p$  = 3.26 ± 0.20 millidegrees, which was found to be independent of the power of the input signal.

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After subtracting the classical attenuation due to viscous and thermal losses, the temperature dependence has been determined on both sides of the peak by fitting a power law of the form

$$\alpha = a / |T_{p} - T|^{n}$$

if the immediate vicinity of the maximum is excluded. For  $T > T_{\lambda}$ ,  $\tilde{n} = 0.49 \pm 0.06$  and  $\tilde{a} = 232 (°K)^{n}/cm$ . For  $T < T_{\lambda}$ ,  $\tilde{n} = 0.51 \pm 0.05$  and  $\tilde{a} = 152 (°K)^{n}/cm$ .

The contribution of the Landau-Khalatnikov relaxation mechanism at a frequency of 1 GHz is a peak, centered 94 m°K below  $T_{\lambda}$ , of only about 180 cm<sup>-1</sup>; therefore the present results cannot be explained by such a process. The other existing theories have been surveyed and no satisfactory explanation of the sharp attenuation peak has been found.

#### I. INTRODUCTION

The aim of this investigation is to study the behavior of hypersonic waves in liquid helium in the vicinity of its lambda transition. To introduce the subject, the general properties of liquid helium will be reviewed and different types of wave propagation will be described. To familiarize the reader with the quantities used throughout this work, the two fluid model of helium and the lambda transition will be discussed. Finally, the relevant experimental results concerning the absorption of ordinary sound in liquid helium will be reviewed. 1.1 Thermal Properties of Liquid He<sup>4</sup>

Two stable isotopes of helium can be found: He<sup>3</sup> and He<sup>4</sup>; in the present work only the latter will be considered. The phase diagram in the P-T plane for He<sup>4</sup> is shown in Fig. 1. It exhibits many interesting features of this extraordinary liquid.

In contrast with the phase designam of an ordinary liquid, it does not show a triple point where the substance can be present at equilibrium in three states: solid, liquid and vapor. Another interesting feature is that helium can exist in the liquid state down to 0°K and no other substance can: the pressure which is required at absolute zero to solidify the liquid is approximately 25 atm., which indicates that the interatomic forces are very weak and the zero-point energy very large. Another manifestation of the same characteristics is the low critical point.

The so-called lambda line suparates the two liquid phases of helium. On the high temperature side, where it is named "liquid He I, helium be-



haves as an ordinary liquid, except close to the transition, while on the low side, that of liquid He II, helium exhibits its superfluid behavior; it is the region where quantum effects become macroscopic.

The lambda transition is not accompanied by a latent heat and the quantities which are first derivatives of the Gibbs free energy, the entropy and density, <sup>(1)</sup> (Fig. 2), are continuous across the transition. Higher order derivatives are affected by the transition. For instance, the specific heat, along the vapor pressure curve, becomes large in the vicinity of the lambda transition on both sides (Fig. 3). <sup>(2)</sup> Being shaped like the Greek letter lambda, it suggested the name of the transition. A semi-logarithmic plot<sup>(3)</sup> (Fig. 4) shows that the specific heat, at the saturated vapor pressure, has a logarithmic singularity at  $T_{\lambda}$ .

## 1.2 Wave Propagation in Liquid He<sup>4</sup>

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这些这些事件是不可能不可能不可能的。这些是这些事件是不是是不是是不是是不是不是不是不是不是不是的。 第二章 Above the superfluid transition, the only propagating mode is the ordinary pressure-density sound wave. Below the transition, several types of wave motion can propagate: they are called "sound," even though they are not all acoustic waves, and they are numbered from one to four.

Ordinary sound, the adiabatic propagation of a pressure density excursion: is called "first sound" and its velocity is given classically by

$$u_i^2 = \left(\frac{\partial P}{\partial f}\right)_{\varsigma} = \frac{\varsigma}{f \beta_{\tau}}$$
(1)

where  $\gamma = C_p/C_V$  is the ratio of the specific heats at constant pressure and at constant volume,  $\rho$  is the density, and  $\beta_r$  is the





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SPECIFIC HEAT OF He<sup>4</sup>



isothermal compressibility coefficient.

As shown in Fig. 5, the velocity of first sound is almost constant as a function of temperature except for a curp around the transition.

"Second sound"<sup>(4,5)</sup> is a temperature wave, that is, an entropytemperature disturbance; a temperature pulse, generated by a heater at one point, can be detected undistorted at another. The temperature dependence of the second sound velocity  $u_2$  is complex, as can be seen in Fig. 5.

In restricted geometries, other types of waves may exist. "Third sound"  $^{(6,7)}$  is the propagation of surface waves on a helium film. "Fourth sound"  $^{(6,8,9)}$  is a thermal wave propagating in a narrow channel, and its velocity is given by a combination of  $u_1$  and  $u_2$ . Figure 5 shows the temperature dependence of  $u_4$ , the velocity of fourth sound.

## 1.3 The Two-Fluid Me lel of He II

To explain the behavior of He<sup>4</sup> below the lambda transition, Tisza<sup>(10)</sup> proposed to study the liquid as if it were composed of two interpenetrating fluids: the normal fluid which exhibits the features of an ordinary liquid with density  $\rho_n$  and velocity  $\vec{v}_n$ , and the superfluid with density  $\rho_s$  and velocity  $\vec{v}_s$ . The total density is the sum of the particle densities

$$f' = f_m + f_s \tag{2}$$

The temperature dependence of  $\rho_n/\rho$  and  $\rho_s/\rho$  under saturated vapor pressure is shown in Fig. 6.

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experimental determinations of the viscosity. When measuring the flow of He<sup>4</sup> below T<sub> $\lambda$ </sub> through narrow capillaries,<sup>(11,12)</sup> it was found that the viscosity became immeasurably small. When measured by the rotating disk method,<sup>(13)</sup> the viscosity, even though decreasing with temperature, is found to be of the same order as the viscosity of He I. The two fluid model clarifies this paradox: in the capillary method, only the "non-viscous" superfluid flows through, while in the rotating disk method part of the normal fluid gets dragged by the rotating disk, causing viscous losses.

In addition to being assumed non-viscous, the superfluid does not carry entropy:

The superfluid equation for low velocities in the absence of external forces is<sup>(15)</sup>

$$f_{s} \frac{\partial \vec{v}_{s}}{\partial t} = -\frac{f_{s}}{f} \vec{\nabla}P + f_{s} \vec{\nabla}\vec{\tau}$$
(4)

and the normal fluid equation is, under the same conditions,

$$\int_{m} \frac{j\vec{v}_{m}}{jt} = -\frac{f_{m}}{f} \vec{\nabla}P - \int_{s} \vec{S} \vec{\nabla}T + \eta \vec{\nabla} \cdot \vec{\nabla} \cdot \vec{v}_{m} \quad (5)$$

where S is the entropy per unit mass,  $\eta_n$  is the coefficient of shear viscosity of the normal fluid, P is the pressure, and T is the temperature. The last two equations show the duality between the influence of a thermal gradient and a pressure gradient on the fluid.

To complete the set of equations, one expresses the laws of conser-

vation of mass and entropy:

$$\frac{\partial p}{\partial t} = - \vec{\nabla} \cdot \left( \int_{S} \vec{v}_{s} + \int_{m} \vec{v}_{m} \right)$$
(6)

$$\frac{\partial (f^{S})}{\partial t} = - \vec{\nabla} \cdot (f^{S} \vec{v}_{m})$$
(7)

From Eqs. (2) - (7), the modes of propagation which are of interest in this study can be derived. First sound, in which the normal fluid and the superfluid move in phase

$$\vec{v}_{\rm m} = \vec{v}_{\rm g} \tag{8}$$

propagates with a velocity

$$u_{1} = \left(\frac{\partial P}{\partial f}\right)^{1/2}$$
(9)

First sound, present below and above the transition, remains finite and continuous through the lambda point. The zero frequency limit of its velocity, at its minimum which occurs at  $T_{\lambda}$ , is  $u_0 = 217$  m/sec.

Second sound, present only in the He II phase, is a real propagating mode and not a simple diffusion wave. The normal fluid and the superfluid move out of phase, with

$$\int_{S} \vec{v}_{s} + \int_{m} \vec{v}_{n} = 0 \qquad (10)$$

Its velocity is given by

$$u_{z} = \left(\frac{f_{s}}{f_{m}} \frac{S^{2}T}{C_{p}}\right)^{\prime / z}$$
(11)

and is plotted in Fig. 5.  $u_2$  continuously goes to zero as the transition is approached since  $\rho_S$  goes to zero and  $C_p$  has a singularity at  $T_{\lambda}$ .

1.4 The Lambda Transition

The lambda transition of liquid helium is only one example of the phase transitions which can be described in terms of an order parameter that is a measure of the symmetry of the system in the vicinity of the transition temperature. (16)

Table I lists some transitions of order higher than one and the order parameter  $\langle p \rangle$  associated with each of them. <sup>(17)</sup> The order parameter may have a zero average value in the disordered phase, that is, above the transition, and must be non-zero in the ordered phase below the transition.

In the vicinity of the lambda transition, the singular behavior of thermodynamic quantities is attributed to long-range fluctuations of the order parameter. The characteristic length  $\xi$  of these fluctuations is assumed to vary as some power of

$$\varepsilon^{-\prime} = \left| \cdot - \frac{T}{T_1} \right|^{-1}$$
(12)

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and diverges as T approaches  $T_1$  .

Landau studied the thermodynamics of second order phase transitions by expressing the chemical potential as a function of three variables: the pressure P, the temperature T, and the order parameter. In the neighborhood of the transition, he expands the chemical potential as a power series of the order parameter; by studying the derivatives of this function with respect to temperature it is possible to determine the temperature dependence of the order parameter and the discontinuity of the specific heat  $C_p$ . In the particular case of liquid helium, this

TABLE I:

Partial List of Phase Transitions and Their

Order Parameter . (17)

Transition

Liquid - Gas Ferromagnetic

Heisenberg Model Ferromagnet

Antiferromagnet

Ising Model

Superconductors

Superfluid

Ferroelectric

Phase Separation

Meaning of  $\langle p \rangle$   $0 - \rho_c$ Magnetization  $\langle M \rangle$ Magnetization  $\langle M \rangle$ Sublattice Magnetization Ising Spin s Complex Gap Parameter  $\Delta$ Condensate Wave Function  $\langle \psi \rangle$ Lattice Polarization

Concentration

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theory seems to fail because it does not take into account the effect of fluctuations which, near  $T_{\lambda}$ , may be large and lead to the singular behavior of  $C_p$ . Static scaling laws (17,18) assume that the consequences of fluctuations can be attributed to the characteristic length  $\xi$  and that, within a critical region, singular thermodynamic quantities can be found to vary as some power of  $\varepsilon$ . The relations between these exponents as determined by the scaling laws have in many cases been corroborated by experimental results. However, some unexplained contradictions leave questionable the validity of the static scaling laws.

By assuming, in addition to a characteristic length, a characteristic reciprocal time or frequency, static scaling theory can be extended to phenomena exhibiting non-zero wave vectors  $\vec{k}$  thereby becoming the dynamic scaling theory. (19,20)

At a given temperature, the characteristic length  $\xi$  defines several regions (Fig. 7): (I) the hydrodynamic region below  $T_{\lambda}$  (T >  $T_{1\lambda}$ ,  $k\xi << 1$ ), (II) the critical region near  $T_{\lambda}$  ( $k\xi >> 1$ ), (III) the hydrodynamic region above  $T_{\lambda}$  (T >  $T_{1\lambda}$ ,  $k\xi << 1$ ).

The separation between critical and hydrodynamic behavior is indicated by the lines  $k\xi = 1$ .

This figure shows that while neutron scattering experiments deal with large wave-numbers  $k_n$  and hydrodynamics does not apply, for light scattering experiments characterized by very small wave numbers  $k_1$  hydrodynamics applies at almost all temperatures. For ultrasonic absorption experiments the relative width of the critical region can be adjusted by the choice of the frequency.



The present study is an attempt to investigate the region for which  $k\xi$  is not small; it must be pointed out, however, that, since little is known about  $\xi$ , the quantity  $k\xi$  cannot be evaluated with certainty. It is nevertheless of incerest to evaluate the attenuation of first sound at high frequencies, since some absorption processes might be enhanced while some others become insignificant.

### 1.5 History of First Sound Attenuation Near T

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The absorption of sound waves has been used extensively to investigate the properties of solids and fluids. Ultrasonic measurements, in particular, provide a rather complete tool for the study of phase transitions<sup>(21)</sup> since their static and dynamic properties can be probed. In a superfluid, moreover, due to the extraordinary thermal nature of the fluid, it is possible to approach the critical region more easily than in other substances. The "anomalous" or "critical" attenuation in liquid helium near the lambda transition was first observed by Pellam and Squire<sup>(22)</sup> in 1947 at a frequency of 15 MHz. Several other experiments were performed to increase the temperature and frequency range and to determine the absorption and the velocity of sound more accurately. In 1958, Chase<sup>(23)</sup> realized for the first time that the maximum in attenuation occurred below the transition but, since these measurements were conducted in an open bath, the submillidegree resolution which would have been necessary to assert this fact could not be reached. Higher temperature resolution techniques were used by Barmatz and Rudnick,<sup>(24)</sup> who were able to pinpoint the temperature of the shifted maximum and more recently, Williams

and Rudnick<sup>(25)</sup> evaluated quantitatively the temperature of the peak for frequencies between 600 KHz and 3 MHz.

At higher frequencies, the work of Imai and Rudnick<sup>(26)</sup> at 1 GHz showed a very sharp peak in the region of the transition and indicated that the maximum occurred at  $3 \times 10^{-3}$  °K below  $T_{\lambda}$ . This result was somehow uncertain for the same reasons invoked above in the case of Chase's experiment. The purpose of the present investigation was to develop a technique to determine with a high temperature resolution the behavior of the attenuation in the vicinity of  $T_{\lambda}$  and the position of the maximum. Other high frequency measurements have been performed<sup>(27-29)</sup> using the Brillouin scattering technique, but no conclusion can be reached regarding the temperature of the attenuation peak.

An important aspect of measurements such as those reported here lies in the fact that the phenomena observed in liquid helium might be generalized to other order-disorder transitions. In fact the similarity between the behavior of first sound near the lambda point of liquid helium and near the critical temperature of another substance has already been observed<sup>(30)</sup>; in nickel the attenuation maximum is located below the magnetic critical point and is temperature dependent. 

# II. ATTENUATION OF FIRST SOUND NEAR T, , THEORY

Many theories have attempted to explain the anomalous attenuation of first sound in the vicinity of a phase transition or critical point. In spite of the fact that experiments have shown for some time that there exists a shift of the attenuation maximum, no attempt has been made so far to devise a unified theory which would predict the experimental observations. Also, most of the existing theories are restricted to low frequencies such that the product  $\omega \tau << 1$ , where  $\tau$  is a relaxation time. Therefore, it is not clear whether any of the existing theories can be used to explain the measurements performed at high frequencies.

At a given temperature, the total attenuation is due to several causes, besides the well known losses due to the shear viscosity and thermal conductivity. A recent study of ultrasonic propagation at low frequencies in liquid helium near the lambda point (25) has been interpreted by such a combination of attenuation processes; the attenuation maximum could be attributed to a) a symmetric attenuation maximum due to fluctuations of the order parameter and b) a relaxation peak which is present only below the lambda transition. A similar interpretation will be attempted here and a brief account will be given of the absorptions due to fluctuations and to relaxation processes.

#### 2.1 Attenuation Due to Fluctuations

Spontaneous internal fluctuations of a system in thermal equilibrium in the vicinity of a phase transition, or critical point, can be a cause

for the anomalous attenuation of ultrasonic waves. The first sound waves interact with the fluctuations and give rise to an absorption which is symmetrical with respect to the lambda point, since fluctuations occur below and above the transition. The magnitude of the effect depends on the coupling of the sound wave, that is, of the pressure or density, to the mean square value of the order-parameter. This mechanism was first studied by Ginzburg.<sup>(31)</sup> Levanyuk,<sup>(32)</sup> using a timedependent Ginzburg-Landau theory of second order phase transitions, performed the first detailed calculation of the interaction between a sound wave and intrinsic time-dependent fluctuations. The results show that an increase in the fluctuations of the characteristic transition parameter is responsible for an increase in the attenuation both above and below the transition. However, the temperature and frequency dependences do not match all the experimental data. Stauffer and Wong<sup>(33)</sup> reconciled the classical time dependent Landau<sup>(16)</sup> theory of second order phase transitions and the scaling laws<sup>(17,18,34)</sup>; they conclude that parafluidity, i.e., the enhancement of fluidity due to order-parameter fluctuations, is manifested in the divergence of the first sound attenuation, which is found to vary as  $\varepsilon^{-1}$  above  $T_{\lambda}$  if a relaxation time  $\tau_{A}$  proportional to  $\epsilon^{-1}$  is used. Below  $T_{\lambda}$ , they conclude that the main contribution of the attenuation is a Landau-Khalatnikov relaxation peak, which will be explained in the next section.

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Wong<sup>(35)</sup> studied the hypersonic attenuation and derived from a theory of relaxation of the order parameter in the critical regime  $(k\xi >> 1)$  that the attenuation has a broad symmetric maximum centered at  $T_{\lambda}$ . Its temperature dependence is asymmetric:  $\epsilon^{-1}$  for  $T < T_{\lambda}$  and

 $\varepsilon^{-1/2}$  for T > T<sub> $\lambda$ </sub>; and its frequency dependence is  $\omega^2$  both below and above the transition. In a supercritical region for which nonlinear fluctuations become important and which is estimated to have its threshold at a frequency of 10 GHz the attenuation should be symmetrical. It was not possible to determine whether the experimental data of Imai and Rudnick<sup>(26)</sup> obtained at 1 GHz were exhibiting this supercritical phenomenon.

Kawasaki<sup>(36,37)</sup> has investigated high-frequency first sound attenuation using the mode-mode coupling theory and the static and dynamic scaling theories. The region of frequencies where this theory is valid has the characteristic frequency of order-parameter dynamics as a lower limit. The higher limit is the frequency of a sound wave whose wavelength is equal to the correlation range of local order-parameter fluctuations. When the frequency  $\omega$  is larger than the average relaxation frequency  $\tau_{-1}^{-1} = u_2/\xi$  where  $u_2$  is the velocity of second sound and  $\xi$  the correlation length, the various wavevectors k characteristic of the spontaneous fluctuations correspond to frequencies larger and smaller than  $\omega$ ; only those which have a relaxation time smaller than  $\omega_{-1}^{-1}$  will contribute to the attenuation. This corresponds to an effective cutoff relaxation time  $\tau_{eff}$  which is frequency dependent. The attenuation can be written

$$\alpha(\omega) = \frac{\Delta u}{u_o^2} \left[ \frac{\omega^2 z_{eff}}{\iota + \omega^2 z_{eff}^2} \right]$$
(13)

Assuming a linear dependence  $\tau_{eff} \propto \omega$  for  $\omega \tau >> 1$ 

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$$\alpha(\omega) = \frac{\Delta u}{u_a^2} \omega \qquad (14)$$

 $\Delta u = u_{\infty} - u_{0}$  is the difference between the high frequency and low frequency limits of the first sound velocity. The interesting consequence of this theory is that

$$\alpha' \propto \omega \varepsilon' \qquad \omega \tau \gg l$$
 (15)

This attenuation maximum is roughly symmetric about the transition.

A recent calculation of high frequency hydrodynamics  $(^{38})$  confirmed this result.

#### 2.2 Attenuation Due to Relaxation Processes

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Considering the relaxation mechanism associated with the orderparameter, Landau and Khalatnikov<sup>(39)</sup> were able to predict the presence of an attenuation peak in the vicinity of a second-order phase transition. Since they used the Landau<sup>(16)</sup> theory of second order phase transitions which does not apply to the lambd<sup>2</sup> transition of liquid helium, the same results were rederived by Pokrovskii and Khalatnikov<sup>(40)</sup> using the modified hydrodynamic equations of Pitaevskii. The superfluid density  $\rho_s$  plays the role of the independent variable instead of the order parameter. The time characteristic of the relaxation of the superfluid density when it is disturbed from equilibrium is

$$\tau = \frac{\xi}{u_1}$$
(16)

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where  $\xi$  is the order parameter correlation length and  $u_2$  is the velocity of second sound.

The relaxation time of the normal density is shorter;  $\tau_1$  is  $v_A^{-1}$ where  $v_A^{-1}$  is the interatomic collision time. For low frequency sound waves, this relaxation process may be considered instantaneous; for the
high frequency waves used in this experiment,  $\tau_1$  might scale as  $\omega^{-1}$ . It must be noted, however, that the Pokrovskii-Khalatnikov theory is valid only for low frequencies, and its range of validity should be extended to cover the present results.

The absorption of acoustic energy is attributed to the generation of second sound by the first sound waves. The first sound attributed associated to a relaxation process<sup>(41)</sup> can be written

$$\alpha(\omega) = \frac{\Delta u}{u_{\star}^{2}} \frac{\omega^{2} z}{1 + \omega^{2} z^{2}} \qquad (17)$$

It is maximum at

$$\omega z = 1$$
 (18)

Since the correlation length  $\xi$  is inversely proportional to the superfluid density  $\rho_{s}$  and since the velocity of second sound  $u_{2}$  goes as the square root of  $\rho_{c}$ ,

$$\xi \propto f_s^{-\prime}$$
,  $\mu_s \propto f_s^{\prime/L}$  (19)

$$\mathcal{Z} = \frac{\xi}{u_{2}} \propto \frac{f_{s}}{f_{s}^{\prime/2}} \propto f_{s}^{-3/2}$$
(20)

Since  $\rho_s \propto \varepsilon^{2/3}$ , then  $\tau \propto \varepsilon^{-1}$ . The maximum in attenuation therefore occurs at  $\omega \varepsilon^{-1} = \text{constant}$ . This determines the temperature of the attenuation maximum for a given frequency. Except for the fact that it is a simple assumption, there exists no theoretical justification for the presence of a single relaxation time. In a detailed microscopic analysis, Pokyakov<sup>(51)</sup> showed that the collective excitation spectrum is defined by several scaling lengths. He concluded that the anomalous

attenuation of sound is induced by two mechanisms: a one-particle relaxation mode and a thermal relaxation mode. This implies that at least two correlation lengths, or two relaxation times, play a role in the absorption mechanisms of sound waves in the vicinity of an orderdisorder transition.

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### **III. EXPERIMENTAL APPARATUS**

In its first stage, this experiment consisted in carefully reproducing the data obtained by Imai, <sup>(42,26)</sup> using the variable path interferometer that he described. The system, schematically shown in Fig. 8, consists of a pulsed oscillator which feeds two signal paths: the acoustical path yielding a signal of amplitude  $V_A$ , which can be varied by adjusting the distance between the transducers, and an electrical path yielding a signal amplitude  $V_E$ . The sum of these signals, depending on their relative phase, has a value which lies between a maximum  $|V_A + V_E|$  and a minimum  $|V_A - V_E|$  as shown in Fig. 9. As the acoustical path is increased, the amplitude oscillates between these limits over an acoustic wavelength, and the exponential decrease of  $V_A$  is reflected by the exponentially decreasing envelope as shown in Fig. 10. This method leads to an absolute value of the attenuation. der sterskierdigter her stersterskieden her sterster beskender som offenskier (s. – kontreker stersterse som

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In its second stage, a sealed interferometric system was conceived. It is isolated from the helium bath by a vacuum jacket to permit control of its temperature within a fraction of a millidegree. Since the acoustical path is fixed, it gives a relative measurement of the attenuation. This system will be described here in detail.

#### 3.1 Cryogenic System

The low temperatures needed to conduct this experiment were obtained in a standard silvered glass double dewar system (Fig. 11). The inner dewar had a working inner diameter of three inches and held about five liters of liquid helium. The outer dewar was filled with liquid nitrogen to precool the cryostat and the acoustic probe. The two dewars were



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FIGURE 11. CRYOGENIC SYSTEM

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isolated from each other by a vacuum jacket which, during the precooling phase, was filled with about 1 mm of nitrogen gas.

The temperature of the liquid belium was lowered by pumping the helium vapor by means of a 140 cu-ft/min pump (Stokes Model 212); temperatures as low as 1°K could be obtained. The temperature of the helium bath was controlled by the manostat described by Imai<sup>(42)</sup> and could be regulated to within  $\pm$  0.001°K. The bath temperature was monitored by two dial manometers (Wallace and Tiernan models FA-160 and FA-145) and, when necessary, by a Texas Instrument model 145 precision pressure gauge.

A helium gas reference tank was available, so that it was possible to collect helium gas of extremely high purity directly from the helium bath and to condense it later in the sample chamber. A dial manometer (Wallace and Tiernan FA-145) could be used to monitor the pressure of the helium gas tank and therefore determine the amount of gas condensed in the sample chamber. A DESCRIPTION OF A DESCRIPTION OF

The system was also equipped with a He<sup>3</sup> refrigerator  $^{(43)}$  consisting of a He<sup>3</sup> tank, a sealed pump (Welch 5 cu-ft/min) and a diffusion pump (CVC 21 liter/sec). He<sup>3</sup> gas could be condensed in the He<sup>3</sup> chamber of the experimental probe and by isolating the probe from the He<sup>4</sup> bath and pumping on the He<sup>3</sup> chamber, temperatures below 1°K could be reached, if needed.

The liquid air level in the outer jacket was maintained above a preset level by a level controller consisting of a thermistor activating a Schmidt trigger.<sup>(44)</sup> A timer, in series with the level controller, protected the installation against a prolonged malfunction.

#### 3.2 Acoustic Probe and Transducers

The acoustic probe is shown on Fig. 12. It consists of three independent chambers: the sample chamber, which holds the two cadmium sulphide transducers and several temperature sensors; the He<sup>3</sup> chamber where He<sup>3</sup> gas can be condensed and evaporated to cool the sample below 1°K; and an exchange gas chamber, used to isolate the sample chamber from the helium bath or, during the cooling phase, to put the sample chamber in intimate thermal contact with the bath.

## 3.2.1 Sample Chamber

The sample chamber (Figs. 13, 14) was a cylindrical cavity 2" long and about 4/3" I.D. It was supported by the 1/4" thin walled He<sup>3</sup> line. To minimize the heat leak between the helium bath and the sample chamber, this tube was made out of stainless steel which at helium temperatures has a small heat conductivity. The He<sup>4</sup> gas was fed to the sample chamber, after having been collected from the bath, through a 0.025" 0.D. stainless steel tube. This capillary was terminated by a flange which was screwed to the sample chamber and sealed by a 0.026" diameter indium "O" ring. A 1500 ohm heater was wound into a groove around the chamber using Manganin resistive wire (30.7  $\Omega/ft$ ) and was covered with GLYPTAL. Six electrical feedthroughs were built into the wall of the chamber so that several thermometers could be installed in the sample: they were composed of a copper core, which was epoxied to the wall (Stycast 2850 GT and Catalyst 24 LV); two monel prongs were soldered to the core of each feedthrough, so that the connecting wires could be soldered and unsoldered without overheating the epoxy.

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FIGURE 12. ACOUSTIC PROBE





FIGURE 14. SAMPLE CHAMBER

The bottom flange was sealed to the body of the chamber by a 0.032" indium "O" ring and served as a coaxial connector to the bottom transducer; for this purpose a MICRODOT 051-0315 plug was soldered in its center. The top flange was similarly used as a seal and as a connector, since it had an indium "O" ring and a MICRODOT 051-0049 connector but it was also the reservoir of the helium-three evaporative cooling system. The reservoir was given an annular shape so that the center of the plate was made available for the coaxial connector. The purpose of the grooves was to provide an intimate thermal contact between the heliumthree condensate and the sample chamber.

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The sample chamber was contained in the exchange gas chamber and all the leads and coaxial lines were pinned thermally to the helium bath since they were soft-soldered or epoxied (STYCAST 2850 GT) to the copper flange of the exchange gas chamber. 

#### 3.2.2 Connection Box

The connection box (Fig. 15), at the top of the probe, was given a cylindrical shape and its axis was horizontal. The front flange could be screwed onto the body of the box and a rubber "O" ring was used to seal the system. Two connectors (AMPHENOL type N) were provided and connected to the transducers by coaxial cables (MICROCOAX UT-141-SS) which introduced an attenuation of 25 db/100 ft. Two tuning stubs (MICROLAB SL-03 N) could be mounted directly on the connectors. The various electrical leads were connected to a multi-prong glass-to-metal feedthrough. A 1/2" "Quikonnect" (from Goddard Valve Corp.) was connected to the He<sup>4</sup> exchange gas pump line. Three 1/4" Quikonnect fittings were installed



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FIGURE 15. CONNECTION BOX

so that a mechanical system could be used if necessary. A relief valve was also mounted on the box for safety purposes.

The filling line of the sample chamber went clear through the top of the connection box and was linked to the cryogenic system through a needle valve. A relief valve, a thermocouple gauge, and a discharge vacuum gauge were provided.

#### 3.2.3 Transducers

The purpose of this investigation was to study the propagatior of sound waves at a frequency of 1 GHz. The transducers used were sulphide films deposited on quartz substrates.

Moreover, such transducers are unaffected by thermal shock and magnetic field and can be used at their fundamental resonant frequency or at an odd harmonic in the gigacycle range.

The quartz substrates were 12 mm in diameter and 2 mm thick, ' optically flat to 1/20 wave of green light and parallel to 3 sec of arc. The edges were beveled at 45° angle. A rather complicated, but mandatory, cleaning procedure was used; the films have a tendency not to adhere to the substrates if they are not perfectly clean. Moreover, 'epitaxial growth might not occur. The plates were washed first in concentrated nitric acid, then in concentrated sodium hydroxide. They were then rinsed in distilled water and boiled for several minutes in ethyl

alcohol. The ethyl alcohol vapor was then used to dry the samples. They were immediately transferred to a vacuum chamber and submitted to an intense ion bombardment (70) V to 1000 A.C. volts under 100 to 200 microns pressure) for 10 to 20 minutes. A coating of gold, with an underlay of chrome for adhesion, was vacuum evaporated on one side of the sample. Since both sides of the quartz plate had to be coated with gold to minimize the radio-frequency cross-talk between the transducers, the vacuum was briefly broken and the plates turned over; then the coating process was repeated. The plates were cooled and kept under a pressure of  $10^{-6}$  to  $10^{-7}$  mm Hg.

The cadmium sulphide must be evaporated onto the back we quartz substrate with its c-axis normal to the substrate in order to generate efficiently longitudinal waves. A rotation of the c-axis leads to the unwanted generation of shear waves in the substrate, thereby decreasing the efficiency of the system.

The simplest evaporation technique, (42,47) making use of CdS powder only, does not always result in a good stochiometry because the partial pressure of the sulphur is too low. This situation can be remedied by simultaneously vaporizing CdS and S or, better, Cd and S in two independently monitored crucibles. (48) A schematic diagram of the vapor-deposition chamber is given in Fig. 16. To increase the probability of obtaining an identical pair of transducers, the piezoelectric substance was deposited in one operation on two quartz plates. The substrates could be heated and held at a temperature T such that  $180^{\circ}C < T < 200^{\circ}C$ . This temperature range was chosen to insure that neither pure cadmium nor pure sulphur would deposit



FIGURE 16. CADMIUM SULPHIDE VAPOR-DEPOSITION CHAMBER

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from the vapor. Two separate crucibles were used, one for cadmium and the other for sulphur. Each crucible had its own heater and thermocouple.

During the preheating phase, necessary to bring the cadmium and sulphur to their boiling point and to adjust the vapor emission, a shutter was placed directly below the substrates to isolate them from the vapor. During the actual deposition, the shutter could be either completely removed or simply lowered to play the role of a baffle. Though the two methods gave positive results, the second was used since it gave more reproducible films. Without a baffle the operation lasted only a few minutes. The baffle, which protected the substrate from the direct molecular beams, slowed down the deposition rate and one or two hours were necessary to obtain the expected result. The deposition rate on the observation window gave an excellent idea of the amount of CdS deposited on the quartz.

At the end of the operation the shutter was used to stop the deposition. The transducers were then mounted in holders made out of gold-plated brass and teflon (Fig. 17). Only a small central region with a diameter of 1 mm was excited to help reduce the critical alignment problem.

The transducers could then be mounted in the sample chamber. An aligning sleeve made sure that they were centered properly.

Since it was known from previous results<sup>(26)</sup> that the attenuation could be of the order of 2500 cm<sup>-1</sup> near the lambda point and therefore that the amplitude of the emitted sound wave could be reduced to 1/e of its value over approximately 40,000 Å or 20 wavelengths, the distance





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FIGURE 17. TRANSDUCER ASSEMBLY between the transducers was set at about  $2 \times 10^5$  Å or 100 wavelengths. Two narrow strips were cut from a mica sheet 0.7 to 0.8 mils thick and were pressed between the two quartz plates. The separation between the mica strips was approximately 5 mm. The spacers also made sure that the quartz plates were sufficiently parallel. Since the active portion of the transducers was 1 mm in diameter, phase cancellation occurred if the non-parallelism exceeded or equaled an angle of  $10^{-4}$  radians.

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## IV: MEASUREMENT TECHNIQUES

## 4.1 Transfer Procedures

The dewar and the acoustic probe were cooled down to about 77°K and maintained at that temperature by keeping the liquid nitrogen jacket of the double dewar full and filling the vacuum jacket with about 1 mm of nitrogen gas.

Liquid helium was transferred into the dewar and helium gas was collected directly from the vapor of the bath and stored in the helium gas tank at room temperature. This 20 liter volume was filled to one atmosphere and sealed off. CULLAGE CONTRACTION

A small amount of helium gas, 20  $\mu$  Hg, was introduced in the exchange gas chamber and in the sample chamber to put them in good thermal contact with the helium bath, which could then be cooled to approximately 1.5°K by pumping on its vapor.

Through a needle valve, helium gas was slowly transferred from the helium gas reference tank in the sample chamber. The warm helium gas heated the sample chamber and the condensation rate was adjusted so that the chamber was always kept under the lambda temperature. The mass of gas transferred could be determined by monitoring the initial and final pressures of the helium gas tank. It was also possible to know that the chamber had been filled above the transducer level by observing the transmission of sound through the sample.

The chamber was then sealed off and was ready for the experiment. To keep the system operational for a long period of time, one half-day or more, it was only necessary to replenish the supply of liquid helium

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## 4.2 <u>Temperature Measurements</u>

The sample chamber contained two thermometers: one was an Allen-Bradley 1/10W, 82  $\Omega$  carbon resistor and the other was a Cryoresistor CR 50-VC from Cryocal, Inc., which could be used for measurements below 1°K. The carbon resistor was placed at the level of the gap and as close as possible to the acoustic field, namely 7 mm from the center of the transducers.

The change in resistance was measured on a Wheatstone bridge of high precision (Fig. 18) and the deviation from equilibrium could be measured on a D.C. null voltmeter. A direct recording of this deviation could be obtained simultaneously with a recording of the amplitude of the acoustic signal. The power dissipated in the resistor was limited to a few microwatts to prevent self-heating effects from disturbing the measurements.

To calibrate the resistor, helium gas was condensed in the exchange gas chamber and all the chambers were connected through the external lines. The pressure above the helium bath was measured by a Wallace and Tiernan model FA 160 absolute pressure gauge and a high precision Texas Instrument Model 145 pressure gauge. At each point, the system was given several minutes to reach equilibrium and the value of the resistor was read only when the stability was satisfactory. For comparison purposes, another Allen-Bradley 1/10 W, 22  $\Omega$  carbon resistor was hung in the helium bath and measured at each point. It should be noted that, even though the sample chamber was thermally in contact with the helium are on the second structure of the second second structure and a second second second second second second second



bath, the stability of the liquid contained in the sample chamber was much greater than that of the bath.

The location of the lambda point was determined by the characteristic step in resistance due to the change in self-heating as the lambda point is crossed.

#### 4.3 Attenuation Measurements

4.3.1 <u>Electronics</u>

Each transducer was tested individually using the circuit shown in Fig. 19. The best self-resonance frequency of the transducer was found by varying the frequencies of both the pulsed oscillator and the local oscillator. The intermediate frequency was 30 MHz. The tuning stub was adjusted so that a maximum power would be delivered to the load and the strongest self-resonance could be observed. A typical result is shown in Fig. 20. It should be pointed out that the performance of the transducers was greater at helium temperature than at room temperature since the internal losses in the quartz are less in a cold system. Each transducer and stub combination had to be individually adjusted at the same frequency, in order to obtain a matched pair, which is a mandatory requirement if the transducers are operated at resonance.

To measure the attenuation, the configuration of Fig. 21 was used. As explained in Chapter II, if this circuit was used with the variable path interferometer, the absolute attenuation could be measured at a given temperature. The gate width and delay could be set to sample the portion of the signal in the shaded area of Fig. 22. By varying the spacing between the transducers, the amplitude oscillated between  $|V_A+V_F|$ 



## FIGURE 19.

BLOCK-DIAGRAM FOR TESTING RESONANCE OF INDIVIDUAL TRANSDUCERS

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FIGURE 20. OSCILLOSCOPE DISPLAY ILLUSTRATING RESONANT RESPONSE OF AN INDIVIDUAL TRANSDUCER.THE TRAILING SIGNAL IS DUE TO RINGING AND INDICATES EXCITATION AT A CHARACTERISTIC MODE. THE RINGING MAY PERSIST FOR AS LONG AS 100 MICROSECONDS AT





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FIGURE 21. BLOCK-DIAGRAM OF INTERFEROMETER SYSTEM

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## FIGURE 22.

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A SCHEMATIC REPRESENTATION OF THE DEMODULATED RECEIVED SIGNAL. THE DASHED LINE INDICATES THE AREA WHICH CHANGES WHEN THE SIGNAL VARIES BETWEEN  $|V_A + V_E|$  AND  $|V_A - V_E|$ . THE SHADED AREA IS THAT SAMPLED FOR AN ABSOLUTE ATTENUATION MEASUREMENT. THE CROSS-HATCHED AREA IS THAT SAMPLED FOR A RELATIVE ATTENUATION MEASUREMENT.

and  $|V_A - V_E|$  and a signal such as the one shown in Fig. 10, could be obtained after proper processing through the box-car integrator.

The configuration of Fig. 21 could be used with the fixed path interferometer, in which case the amplitude of the signal in the crosshatched area (Fig. 22) was sampled by the gate and the temperature of the helium was varied. This procedure gave a relative attenuation measurement, that is, a plot of the amplitude of the transmitted signal versus temperature (Fig. 23). This same result could be obtained also by using only the transmitted acoustical signal, that is, by setting the attenuator of the electrical reference path to infinity. Then the signal has no electrical component  $V_{\rm E}$  and one deals only with  $V_{\rm A}$  (Fig. 24).

It should be noted that by sampling the trailing portion of the received signal, the measurements were actually performed during the "off" portion of the duty cycle of the pulsed oscillator, thereby eliminating the interferences caused by electromagnetic crosstalk. 

#### 4.3.2 Temperature Drift

When the preliminary operations described above were completed, the exchange gas chamber could be pumped out to minimize the heat leak between sample chamber and helium bath. The bath was always maintained at a temperature slightly lower than the range under investigation. For the runs limited to the lambda region, 2.0°K to 2.3°K, the bath was kept at 1.95°K, typically. Heat was then provided to the sample by the heater wound around the sample chamber and the sample started to warm up. By regulating the current in the heater, one could choose the drift rate or reverse the direction of the drift. Drift rates as low as 10 m°K per



# FIGURE 23.

RECEIVED SIGNAL AMPLITUDE VERSUS TEMPERATURE DURING A RELATIVE ATTENUATION MEASUREMENT. THE ABRUPT CHANGE IN SIGNAL AMPLITUDE OCCURS WHEN THE HELIUM IN THE BATH CROSSES THE LAMBDA POINT.



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## FIGURE 24. ACOUSTICAL SIGNAL V<sub>A</sub>.

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hour, or  $3 \times 10^{-6}$  °K sec<sup>-1</sup> could thus be obtained.

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#### V. RESULTS AND ANALYSIS

## 5.1 Absolute Attenuation Measurements

The method used for absolute measurements of the attenuation is identical to the one used previously by Imai. (26,42) At each point, the temperature of the system is stabilized and a plot, such as shown in Fig. 10, is generated. The amplitude of the signal decreases exponentially with the distance between the transducers. A semilogarithmic plot of the amplitude versus the number of wavelengths of displacement (Fig. 25) can be translated into an absolute attenuation by measuring its slope. The results of these measurements are shown in Fig. 26, and confirm the previous results. Three regions can be distinguished.

## 5.1.1 The Normal Fluid Region (T > 2.3°K)

In this region, the attenuation is due principally to classical shear viscosity losses and to classical thermal conductivity losses. The continuous curves labeled  $\alpha_{\eta}$  and  $\alpha_{\kappa}$  represent the attenuation due to these two processes, computed from the Stokes-Kirchhoff equation (Appendix A) using known values for the quantities involved. <sup>(49)</sup> As the  $\alpha_{total}$  curve shows, the Stokes-Kirchhoff attenuation fits well the experimental points above 3°K. Below 3°K, the discrepancy can be attributed to the fact that the critical attenuation extends into the normal fluid region.

## 5.1.2 The Critical Region $(2^{\circ}K < T < 2.3^{\circ}K)$

The sharp peak in attenuation occurring in the vicinity of the

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FIGURE 25.

SEMI-LOGARITHMIC PLOT OF THE RECEIVED SIGNAL AMPLITUDE VERSUS DISTANCE. ONLY EVERY FIFTH WAVELENGTH IS SHOWN FOR CLARITY. THE FIT OF THE POINTS TO A STRAIGHT LINE INDICATES THE PARALLELISM OF THE SYSTEM.



lambda transition will be investigated in more detail in section 5.2 using a temperature drift and the fixed path interferometer. The continuous curve labeled  $\alpha_{LK}$  is the attenuation due to the order parameter relaxation as derived in the Landau-Khalatnikov theory,  $(^{39,40})$  for a 1 GHz sound wave. It can be seen that this peak, which has a maximum value of 180 cm<sup>-1</sup>, 94 m°K below the lambda point, represents only a small amount of the total attenuation. . Reinsserrenninghvärkköreitikan serrasion son ser

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## 5.1.3 The Superfluid Region $(T < 2^{2}K)$

In this region, the attenuation goes through a maximum of 1200 cm<sup>-1</sup> at 1.5°K, approximately. The total attenuation can be attributed to two processes:

a) The Landau-Khalatnikov  $\alpha_{LK}$  attenuation mentioned earlier.

b) The peak in attenuation,  $\alpha_{KL}$ , described y Khalatnikov and Chernikova,<sup>(50)</sup> which is associated with the relaxation times for equilibrium of the elementary excitations. This includes

the attenuation due to classical viscosity losses (Appendix B).

As can be seen in Fig. 26, the agreement with the experimental points is good.

The location of the Khalatnikov-Chernikova peak and its shape show good agreement, except for the low temperature slope, when compared to some results obtained by Brillouin scattering by Woolf, et al., <sup>(27)</sup> and by Heinicke, et al. <sup>(28)</sup> (Fig. 27). Compared to the results of St. Peters, et al., <sup>(29)</sup> obtained also by Brillouin scattering, the agreement is good even for the low temperature slope. Since all those measurements were obtained at different frequencies, ranging from 556 MHz to


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768.1 MHz, the experimental data shown in Fig. 27 has been normalized to a frequency of 1 Giv, the scaling factor being proportional to  $\omega^2$ . The good agreement between most of the data points over the whole temperature range indicates that the attenuation actually scales as  $\omega^2$  with the possible exception of the lambda point region, where few points are available, and of the region below 1.5°K, where  $\alpha$  might scale differently. It should be noted, however, that, even if it is the case, a disagreement still exists between the low temperature slope exhibited by the data of Woolf, et al., and Heinicke, et al., and the data of St. Peters, et al., and the present data.

### 5.2 Relative Attenuation Measurements in the Critical Region

In the critical region  $(2^{\circ}K < T < 2.3^{\circ}K)$  the fixed path interferometer described in Chapters III and IV was used. While the temperature of the sample was allowed to drift slowly, a simultaneous recording of the received signal amplitude and of the temperature was made (Fig. 28).

The amplitude and the attenuation are related through the equation

$$A = A_{\rho} e^{-\alpha \dot{\delta}}$$
(21)

which expresses the spatial attenuation over an acoustical path  $\delta$ , which is here the fixed gap between the transducers. The quantity A<sub>0</sub> is also a constant of the system for each run. Equation (21) can be rewritten

$$\ln A = \ln A_0 - \alpha c \qquad (22)$$

To calibrate the relative attenuation, the absolute values obtained earlier (Fig. 26) were used; for each T, ln A is plotted against the



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SIMULTANEOUS RECORDING OF THE RECEIVED AMPLITUDE SIGNAL (THICK LINE) AND OF THE TEMPERATURE (THIN LINE) Alexis Arrent Arran Stand Arros CATARS A Arrange Arrange Arrange and a standard and a standard and a standard a

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absolute value of  $\alpha$ , taking into account the experimental scattering. This procedure is shown in Fig. 29. The best straight line fitting through these points gives the scaling factor. The best value of  $\delta$  for twenty runs, was found to be 1.86 x 10<sup>-3</sup> cm which is compatible with the thickness of the spacers which was 0.75 ± 0.05 mil (1.91 x 10<sup>-3</sup> ± 0.13 x 10<sup>-3</sup> cm). The separation between the crystals is expected to be slightly greater than the actual thickness of the spacers.

For each run, the value of  $A_0$ , which depends on the input power, can be determined by extending the plot ln A versus  $\alpha_{abs}$ ; the intercept with the  $\alpha_{abs} = 0$  axis gives ln  $A_0$ .

The temperature measured is that of the sample itself, the thermometer being located 7 mm from the center of the transducers and at the level of the gap. 

## 5.2.1 Experimental Results

The outcome of these measurements is displayed in Fig. 30; typical data points are shown and the continuous line is the best fit curve for ten experimental runs. There is no singularity near the lambda transition and the absorption maximum is shifted to a temperature  $T_p$  lower than  $T_{\lambda}$ . The average of the maximum value of the attenuation is 2470 cm<sup>-1</sup>. To separate that part of the attenuation which involves directly critical phenomena, and which will be called critical attenuation, the contribution of classical losses associated with the shear viscosity and thermal conductivity had to be subtracted from the total attenuation. <sup>(49)</sup> The result is shown in Fig. 31. For  $T > T_{\lambda}$  both the shear viscosity and thermal conductivity losses have been taken 'nco account;







for  $T < T_{\lambda}$  only the viscosity is available. The critical attenuation has a maximum value of about 2000 cm<sup>i-1</sup>.

To determine accurately the temperature  $T_p$  at which the attenuation reaches its peak value, a large number of very slow temperature drifts across the transition were performed. Drift rates as slow as  $3 \times 10^{-6}$  °K sec<sup>-1</sup>, upward as well as downward, were reached. The amplitude of the input signal was changed from run to run and the pulse repetition frequency was varied between 1 and 300 pulses per second. No significant shift in  $T_p$  could be observed. A semi-logarithmic plot of the total attenuation versus  $|T-T_1|$  is shown in Fig. 32.

Eleven runs were used for the determination of the peak temperature  $T_p$ ; its average value was found to be 3.26 ± 0.20 millidegrees below the lambda point.

The temperature dependence of the critical attenuation can now be investigated. Since the variations of the critical attenuation are large compared to those of the classical attenuation, subtracting the classical attenuation does not change significantly the temperature  $T_p$ of the maximum. The temperature dependence can be approximated by a power law of the form

$$\alpha = \frac{a}{\left|T - T_p\right|^n}$$
(23)

In order for the fitted curve not to diverge, only the data points lying in a region  $|T_p-0.02| < T < |T_p-0.125|$ °K were considered. The average values for the exponent n and the coefficient a were found to be

$$T > T_{\lambda}$$
  $\bar{n} = 0.49 \pm 0.06$   $\bar{a} = 232(^{\circ}K) n/cm$   
 $T < T_{\lambda}$   $\bar{n} = 0.51 \pm 0.05$   $\bar{a} = 152(^{\circ}K) n/cm$ 



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The values of  $\bar{n}$  given by Imai<sup>(26)</sup> are  $\bar{n} = 0.46$  for  $T > T_{\lambda}$  and  $\bar{n} = 0.48$  for  $T < T_{\lambda}$  and were computed by a function identical to (23) where  $T_p$  was  $T_{\lambda}$ -0.003 °K.

### 5.2.2 Analysis and Interpretation

The present results confirm those obtained earlier in this laboratory. <sup>(26)</sup> The conditions under which the experiments were conducted at the time, namely, the fact that a submillidegree accuracy could not be achieved, made it impossible to pinpoint the temperature of the maximum in attenuation; it could only be located between 3 and 4 m°K from the transition. The present results therefore add accuracy to this result by indicating that  $T_p$  is 3.26  $\pm$  0.20 m°K below  $T_{\lambda}$ .

First sound attenuation measurements in liquid helium at frequencies from 0.6 to 3.17 MHz<sup>(25)</sup> have also shown that the temperature at which the maximum occurs is below  $T_{\lambda}$  and the absorption has been interpreted as being due to two phenomena: (1) a relaxation process occurring only below  $T_{\lambda}$ , <sup>(40)</sup> and having a relaxation time  $T_2 = \xi/u_2$  where  $u_2$  is the velocity of second sound and  $\xi$  a coherence length of magnitude 1.36 ×  $10^{-8} (T_{\lambda}-T)^{-2/3}$  cm; (2) a critical attenuation which is symmetric about  $T_{\lambda}$ , non-singular and due to fluctuations of the order parameter. The sharp attenuation maximum occurring at about 3.3 millidegrees below  $T_{\lambda}$  cannot be explained by those two mechanisms. A relaxation peak due to a relaxation time  $\tau_2 = \xi/u_2$  as above would reach a maximum of about 180 cm<sup>-1</sup>, 94 millidegrees below  $T_{\lambda}$ , as shown in Fig. 26, and therefore is not a significant contribution at 1000 MHz.

On the other hand, the symmetrical attenuation peak centered at  $T_{\lambda}$ 

is worthy of consideration. As shown in Fig. 33, the low frequency values of  $\alpha_{\lambda}$ , that is, the attenuation at the lambda transition, when extrapolated to a frequency of 1 GHz, is in satisfactory agreement with the experimental results. The value of the attenuation at the transition is found to vary as  $\omega^{1.22}$  from 16.8 KHz to 1 GHz as reported earlier by Williers.<sup>(25)</sup> This result agrees reasonably with those obtained by Kawasaki<sup>(36)</sup> using the mode-mode coupling theory and those of Khalatnikov, et al., resulting from a study of dynamic phenomena in a weakly interacting Bose gase, which in both cases find that the attenuation is proportional to  $\omega \varepsilon^{0}$  in the region  $\omega \tau >> 1$ . If the presence of a highly symmetrical peak, centered at  $T_{\lambda}$ , is confirmed by the theory, for the high-frequency sound waves considered here, the excess attenuation which shifts the attenuation maximum to 3.3 millid@grees below the lambda point suggests that a relaxation time, other than  $\tau_2$ , manifests itself at 1 GHz.

This might indicate that, since for this very high frequency the quantity  $k\xi$  does not remain small, the decay of the first sound wave in o ther first sound modes becomes significant, as suggested by Hoherterg.<sup>(37)</sup>



FIGURE 33. ATTENUATION AT T =  $T_{\lambda}$  vs. FREQUENCY.

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## VI. CONCLUSIONS

The first part of this experiment, consisting in measuring the attenuation of 1 GHz sound waves with a variable path interferometer, from 1°K to 4°K, confirms the results obtained before by the same method and those obtained by the Brillouin scattering method. It is found that the attenuation scales as the square of the frequency over the whole temperature range, with the possible excoption of data below 1.5°K and in the immediate vicinity of  $T_1$ .

In a second part, the attenuation at 1 GHz has been measured with a fixed path interferometer in the region of the lambda transition between 2°K and 2.3°K. The sharp attenuation peak, in the critical region, is fc\_n? to occur at 3.26  $\pm$  0.20 m°K below'T<sub> $\lambda$ </sub>. The maximum value of the attenuation is close to 2500 cm<sup>-1</sup>.

After the contribution of viscous and thermal losses to the attenuation has been subtracted, the temperature dependence of the critical attenuation is found to be approximately  $|T_p-T|^{-1/2}$  on both sides of  $T_p$ , the temperature of the peak, excluding the immediate neighborhood of  $T_p$ .

Since the contribution of the Landau-Khalatnikov mechanism to the attenuation at a frequency of 1 GHz is only about 180 cm<sup>-1</sup> at its maximum, which occurs 94 millidegr 's below  $T_{\lambda}$ , the large absorption is due to other processes. The exist. ; theories of first sound attenuation in liquid helium have been surveyed and no satisfactory explanation of the sharp attenuation peak in the vicinity of  $T_{\lambda}$  has been found.

## VII. SUGGESTED EXPERIMENTS

In order to reach a better understanding of attenuation phenomena in the lambda transition region, the following experiments would be of interest:

1) The gap existing between the present results and those obtained at low frequencies should be narrowed. Measurements between 4 MHz and 1000 MHz would be useful. A good knowledge of the relaxation times involved will come from frequency dependent data.

2) Measurements of the attenuation under different pressures (including high pressure) would provide an interesting evaluation of the Pokrovskii-Khalatnikov theory.<sup>(40)</sup>

3) Finally, measurements over the whole frequency range, in mixtures of He<sup>4</sup> and He<sup>3</sup> and in other substances undergoing an orderdisorder lambda transition, will lead to interesting comparisons and generalizations.

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## APPENDIX A

### THE STOKES-KIRCHHOFF EQUATION

The classical attenuation of sound in an ordinary liquid is given by the Stokes-Kirchhoff equation

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$$\alpha = \frac{\omega^2}{2f u_i^3} \left(\frac{4}{3}\eta + \zeta + \frac{\delta - 1}{\delta} \frac{\kappa}{C_v}\right)$$
(24)

where  $\omega$  is the angular frequency,  $\rho$  the density,  $u_1$  the velocity of (first) sound,  $\eta$  the shear viscosity,  $\zeta$  the volume viscosity,  $\gamma$  the ratio of the specific heats,  $\kappa$  the heat conductivity, and  $C_v$ the specific heat at constant volume.

To compute the last term of this equation, which represents the absorption due to thermal losses, it must be expressed in terms of quantities measured  $^{(49)}$  at the saturated vapor pressure:

$$\pi_{k} = \frac{\omega^{2}}{2\rho u_{i}^{3}} \frac{x^{-1}}{y} \frac{k}{c_{v}}$$
Using the following relations:  
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best available copy.
(25)

$$\vec{x} = \frac{T \vec{v} \cdot \vec{3}_{p}}{\kappa_{T} C_{v}}$$
(26)

$$j_{P}^{3} = - \frac{T v}{c_{s}} \left(\frac{\partial P}{\partial T}\right)_{sat} \left[j_{sat}^{3} + \frac{1}{f^{u_{i}^{2}}}\right]$$
(27)

$$C_{p} = \frac{C_{s}}{1 - \frac{TV}{C_{s}} \left(\frac{\partial P}{\partial T}\right)_{sat} \left[\mathcal{A}_{sat} + \left(\frac{\partial P}{\partial T}\right)_{sat} \frac{1}{\rho u_{s}^{2}}\right]}$$
(28)

this term reduces to:

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 $X_{K} = \frac{\omega^{2} \kappa \tau V}{2 u_{f} c_{s}^{2}} \left[ \int_{-sat}^{s} + \left( \frac{er}{c} \int_{sat}^{1} \frac{1}{r^{u_{f}}} \right)^{2} \right]$ (29)

where  $\beta_p$  is the isobaric coefficient of thermal expansion,  $C_p$  is the specific heat at constant pressure,  $K_T$  is the isothermal compressibility. The subscript "sat." indicates that a quantity is evaluated at the saturated vapor pressure.

#### APPENDIX B

## THE KHALATNIKOV-CHERNIKOVA THEORY

The Khalatnikov-Chernikova theory of the absorption of sound in superfluid helium states that the interactions of elementary excitations (phonons and rotons) cause many mechanisms of energy dissipation. To each of those mechanisms is associated a relaxation time  $\tau$  characteristic of the amount of time required for the distributions of elementary excitations to adjust to the disturbance created by the sound wave. Some processes do not contribute significantly to the attenuation because their relaxation time is very short; such is the case for the elastic scattering of phonons by phonons and for the roton-roton scattering processes. Some other processes, by their relatively long relaxation times, contribute to the attenuation; such are the interactions which involve the conversion of a phonon into a roton, to which is associated a relaxation time  $\tau_{pr}$ , or the conversion of three phonons into two, the five-phonon process to which is associated a relaxation time  $\tau_{3+2}$ .

The expression for the attenuation of first sound can be simplified in the high temperature region, above 1.2°K, for which the only case of interest is  $\omega \tau_{\rm pr} << 1$ . In the notation of Whitney<sup>(52)</sup>

$$\alpha(\omega, \tau) = \frac{\omega^2 \tilde{\tau}_{pr}}{\mu_1} \left( \frac{f_1}{f} \right) \left[ \frac{2}{15} + \frac{1}{\sqrt{5}} \left( 3u + 1 \right)^2 \right]$$
(30)

with

$$\widetilde{z}_{pr} = \overline{z}_{pr} \left[ 1 + \frac{.376}{.451 \frac{\overline{z}_{pr}}{.6_{3 \rightarrow 2}} + .0036} \right]$$
(31)

$$\frac{1}{3} = \left[\frac{1.453}{T} + \frac{z_{3\to 2}}{z_{pz}} \times .166\right] \frac{z_{pz}}{z_{3\to 7}}$$
(32)

where

$$C_{3 \to 2} = 1.288 \times 10^{-8} T^{-4}$$
(33)  

$$U = \frac{f}{u_{1}} \left(\frac{\partial u_{1}}{\partial \rho}\right) = 2.642$$

$$\frac{f_{m}}{f} = 1.218 \times 10^{-4} T^{-4}$$
(34)  

$$\frac{f_{m}}{f} = 1.28 \times 10^{-4} T^{-4}$$
(35)  

$$\frac{1}{z_{pz}} = 1.28 \times 10^{-2} T^{-4} e^{-\frac{M}{kT}}$$
(36)

where k is the Boltzmann constant and  $\Delta = 3.4 \times 10^{43}$ .

The five-phonon collision time is the adjustable parameter of this:

At high temperatures the relaxation times involved in the scattering processes are short compared to the period of the acoustic wave; the system is in a hydrodynamic regime. At low temperatures, on the contrary, the relaxation times are long and the system is in a collisionless regime. The two regimes are separated by an attenuation maximum. At 1 GHz this maximum occurs at  $1.48^{\circ}$ K and has an amplitude of 1012 cm<sup>-1</sup>.