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OFFICE OF NAVAL RESEARCH

SONAR ARRAY STUDIES Final Report Under Contract N00014-70-A-0166 Task 0091, Item 9, Exhibit I

> Contract N00014-70-A-0156 NR 240-014



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ARL-TR-71-51 29 March 1972

SONAR ARRAY STUDIES

Final Report Under Contract N00014-70-A-0166 Task 0001, Item 9, Exhibit I

Jon M. Cooper, Louis H. Fowler

THIS RESEARCH WAS SPONSORED BY OFFICE OF NAVAL RESEARCH Contract NO0014-70-A-0166 NR 240-014

# APPLIED RESEARCH LABORATORIES THE UNIVERSITY OF TEXAS AT AUSTIN AUTOR, TEXAS 78712

#### ABSTRACT

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This report summarizes work performed under Contract NOOOl4-70-A-O166, Task OOOl, Item 9, Exhibit I, Sonar Array Studies. The study described was aimed at developing design guidelines for sonar projecting arrays to be used for high source level, wide sector applications. The effort began with a literature survey described in the first two sections: "General Power Limits of Sonar Transducerz," and "Piezoelectric Properties of Ceramics." The piezoelectric equations of state are presented, along with a discussion of and results from two computer programs written to predict the performance of some different ceramics under various environmental and operational conditions. An analysis of beam patterns and directivity index of curved face arrays is presented in Section V. The final section contains conclusions and recommendations.

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# TABLE OF CONTENTS

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			Page
ABST	RACT		iii
I.	INT	RODUCTION	1
п.	GEN	ERAL POWER LIMITS OF SONAR TRANSDUCERS	3
III.	PIE	ZOELECTRIC PROPERTIES OF CERAMICS	7
IV.	TRA OF	NSBUCER ANALYSIS BASED ON PIEZOELECTRIC EQUATIONS STATE	19
	Α.	5-Port Equations for Thickness Mode Piezoelectric Plate with Losses Included	19
	в.	Equivalent Circuit of Ideal (Lossless) Piezoelectric Plate	23
	c.	Optimum Design Considerations Based on Equivalent Circuits	26
	D.	Transducer Performance Predictions Based on Computer Solutions of 5-Port Equations	32
۷.	CUR	VED FACE SONAR ARRAY ANALYSIS	53
	A.	Wide Sectors	53
	в.	Directivity Index	59
	c.	Source Level	65
VI.	CON	CLUSIONS AND RECOMMENDATIONS	69
	A.	Summary	69
	в.	Recommended Future Work	71
REFE	RENCI	S	73

#### I. INTRODUCTION

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This reput curvarizes the work performed under Contract NOOO14-70-A-0166, Task 0001, Item 9, Exhibit I, Sonur Array Studies. The purpose of this work was to investigate curved face array configurations to provide guidelines for designing high acoustic power, high search rate sonar transmitting arrays capable of large angular sector coverage. High search rate zonars, operating at high power levels, increase the probability of ceramic element failure resulting from overheating and/or overstressing. Such instances have occurred with some prototype and experimental projectors built at Applied Research Laboratories (ARL). If, as proposed.<sup>1,2</sup> future generation transmitting arrays are to be operated at even higher search rates and with an order of magnitude increase over present operating power levels, it seems imperative to know the effects of these future requirements on sonar performance, so that adequate design guidelines may be formulated. This report documents the results of a one year effort directed toward prediction of projector performance.

To limit the problem to a manageable scope, the present effort was concerned only with piezoelectric ceramic arrays. The dismissal of magnetostrictive sources is at least partially justified in an effort to obtain maximum acoustic output power:

For low Q transducers, heavily loaded by radiation (low Q) the presently available nickel-cobalt alloys are capable of far less power/pound than are the lead zirconate titanate ceramics. On the other hand, the strength of the magnetostrictive metals is an important advantage, especially for large structures such as low frequency ring transducers .... Breakthroughs in fundamental research would probably be required, however, to put magnetostrictive materials in a position of general supremacy.<sup>3</sup>

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Although hydroacoustic sources of sound are suited for low frequency applications,<sup>4</sup> the hydroacoustic projector was not considered since the primary interest in this study was the ultrasonic frequency range.

The study was conducted as parallel efforts in two areas: array configuration, and properties and limitations of the piezoelectric ceramic materials.

The remainder of this report is divided into five major sections. Section II deals with general power limitations of sonar transducers. Section III briefly reviews the important piezoelectric properties of ceramics and discusses some important factors which affect the various properties.

In Section IV, a theoretical analysis of transducer performance based on the piezoelectric equations of state is presented. A mathematical model is developed for a lossless, thickness-mode piezoelectric plate, and the equivalent circuit technique is demonstrated. The analysis is extended to include both mechanical and electrical losses in the ceramic. Details of two computer programs based on this analysis are discussed.

An analysis of curved face sonar arrays is given in Section V. Beamwidth and directivity index calculations are considered as a function of array configuration, element size and type, and amplitude shading techniques. A relationship between directivity, source level, and acoustic power is also given. The final section (VI) contains conclusions and recommendations.

#### II. CENERAL POWER LIMITS OF SONAR TRANSDUCERS

The power output of a sonar transducer may be considered to have an electrical, a mechanical, an acoustical, and a thermal limit. Woollett<sup>5</sup> discusses the electrical and mechanical limits for both an electric field transducer and a magnetic field transducer. The electrical limit is proportional to storable electric and elastic energies, mechanical Q. mechanoacoustical efficiency, and electromechanical coupling coefficient. Woollett's analysis was done for linear electroacoustic transducers. The limits on stored energy are imposed by such factors as insulation breakdown, depolarization of materials, distortion resulting from dielectric (and ferromagnetic) nonlinearities, and deterioration of efficiency resulting from a rise in the dissipation factor at high fields. Thus, it would seem that a dynamic approach to power limits would be required in considering the high power (and therefore high driving field) operating conditions. The mechanical limit depends on the transducer's capacity to store elastic energy and is primarily determined by the elasticity of ceramic or crystal transducers.

Urick<sup>6</sup> discusses the cavitation limitation of acoustic power. The expression relating cavitation threshold and sound pressure level is

 $I_{c} = \frac{\left(0.707\right) 10^{6} P_{c}\right)^{2}}{\rho c} \times 10^{-7} = 0.3 P_{c}^{2} W/cm^{2}$ ,

where

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 $I_{c} = \text{cavitation threshold, }:/cm^{2},$   $P_{c} = \text{peak pressure of sound wave causing cavitation, atm,}$   $\rho = \text{density of water, g/cm}^{3},$  c = sound speed in water. m/sec.

The cavitation limit for a given projector can be obtained by multiplying  $I_c$  by the surface area of the transducer and using  $P_c$  adjusted for operating depth. The cavitation threshold

$$I_c = 0.3 P_c^2 A$$

,

where A is the surface area of the projector  $(cm^2)$ , represents the maximum working value for the power output (W) of the projector. At the limiting power level several phenomena begin to occur which degrade the projector performance. These include erosion of the projector surface, loss of acoustic power in absorption and scattering by the cavitation bubble cloud, a deterioration in the beam pattern of the projector must operate. The cavitation threshold is inversely proportional to pulselength and directly proportional to frequency. An approximation to measured values is shown in Dwg. AS-71-668.

The sound pressure at the cavitation threshold is a function of depth (hydrostatic pressure),

$$P_{c}(h) = P_{c}(0) + \frac{h}{33}$$
 atm

where h is in feet (33 ft of water is equivalent to 1 atm of pressure).

Sherman<sup>7</sup> introduced a factor y to account for the nearfield effect on the cavitation threshold,

$$I_{e} = 0.3 \gamma \left( P_{e}(0) + \frac{h}{33} \right)^{2}$$



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Experimental values for  $\gamma$  are between 0.3 and 0.6 for a circular piston, with an average of about 0.5. Therefore, the cavitation threshold of a transducer can be expressed as

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$$I_{c}(f,h,\tau,A) = 0.15 \left( P_{c}(0) + \frac{h}{33} \right)^{2} \cdot g(f) \cdot e(\tau)$$

where g(f) is frequency dependence and  $e(\tau)$  is the pulselength factor, as described in Dwg. AS-71-668.

The thermal limit of acoustic power is exceeded, for a transducer composed of piezoelectric ceramic, when the power dissipated within the element is sufficient to raise the temperature of the material to the Curie temperature. At the Curie temperature, the piezoelectric property is destroyed and is not restored when the ceramic cools.

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The temperature behavior of a piece of piezoelectric ceramic is a function of time, of the thermal conductivity of the surrounding media, of ceramic volume, of ambient temperature signatures, and of the dissipation factor of the ceramic. The dissipation factor  $(\tan \delta)$  is the ratio of energy dissipated within the ceramic in the form of heat to the energy converted into mechanical metion. It varies with planar stress (hydrostatic pressure), driving field, and type of ceramic.

Only a limited amount of experimental or theoretical work has been published on the thermal behavior of electroacoustic projectors. Smith and Burbage<sup>®</sup> performed some experiments in connection with a comparative study of piezoelectric ceramics. They found that specimens of commercially available ceramics very similar in low field properties can show extreme variation in high field loss behavior. One anomaly observed at high operating fields was the occurrence of "hot spots," uneven heating of the ceramic.

# III. PIEZOELECTRIC PROPERTIES OF CERAMICS

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The power level capability of a projector is dependent upon properties of the piezoelectric ceramic. The values of these parameters are available from data sheets published by various suppliers. Typical values for piezoelectric ceramics commonly used in projectors are given in Table 7.

Several studies of ceramic behavior under various operational and environmental conditions have been published in the literature. Drawings AS-71-669 through AS-71-674 are adaptations of experimental data. The ceramics are referred to by brand name, and only the behavior of projector materials is reported here.

Brown<sup>9</sup> tested the variations of several properties of PZT4 and NRE4 ceramics as a function of planar stress and electric field. Drawings AS-71-669, AS-71-670, and AS-71-671 are adaptations of his results, using one-dimensional static pressure for conventional mass loaded stacks. Martin<sup>10</sup> reported on the variation of coupling factor with pressure and his results are shown with Brown's in Dwg. AS-71-672.

Berlincourt<sup>11</sup> reported the behavior of dissidation factor as a function of electric field and temperature for the three Clevite projector materials, FZT4, FZT8, and Ceramic B. These results have been summarized in Dwg. AS-71-673.

Gerson<sup>12</sup> observed variations of mechanical Q and Young's Modulus as a function of stress (Dwg. AS-71-674). His work was done with two cersmic compositions with characteristics different from the so-called

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# TABLE I

# SUMMARY OF PROJECTOR CERAMIC PROPERTIES

Property (Symbol)	Definition	Principal Punctional Dependence	Desired Features	Typical Value
Dielectric Dieskipsticm Pactor (tem d <sub>E</sub> )	Measure of the distantic loses in in the material-resided to heet generated within the ceramic	Klectric field rtrength; planar stress	ş	0.01 - 0.03
Curie Temperature	The temperature at which the crystal structure will permanently loos its piercelectric activity	Electric field strength; time	19 E	300°>0°C
Electromechanical Complian Commeteer (k, j) <sup>3</sup>	A measure of the ceramic's sollity to convert energy from one form to mother k = alectricel output	Cermaic's characteristic resconst frequency: strength of pleaselactric effect of cermaic	High	0.50 - 0.55
Planar coupling confficient (b)	Combines the plescelectric elastic and dielectric properties in a timple parameter	Matural mechanical resonance of ceranic	fi i gh	0.50 - 0.55
Birtis content (s <sub>1</sub> )e	Am indication of pinsonlectric emailtrity of cermaic. Plactric field. Meanues un-alacial strain to applied alactric field. Preasures the actract certage produced produced by a given voltage across the matrial. a supplied field	Electric force field applied	<b>4</b>	d <sub>31</sub> 95 - 10 <sup>-12</sup> d <sub>33</sub> - 220 - 15 <sup>-12</sup> K
Voltage constant (s <sub>13</sub> )e	Meleks open ciruit voltage aud actimical stress. 1 <u>voltage</u> stress 6 open circuit field 6 open circuit field	Stress applied	Ki đi	6 <sub>33</sub> + 25 + 10 <sup>-3</sup> Na

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TABLE I (Cont'd)

Presenterie ecupaneus are generally written as tensor components; k<sub>31</sub> ar k<sub>15</sub>. These 13 subscripts are related to orthogonal area z, y, a represented as 1, 2, 3, respectively. The first subscript, 1, is the electrical direction; the second, J. is the motionical direction. The numbers  $\lambda_1$  5, 6 refer to abser in the ys, m, and m planes (around the m, y, and n anes).

respectively: i.e.,  $d_{\rm M}$  is a measure of the definetion miony the s-axis is response to a voltage applied parallel to the s-axis.  $^{10}$ 



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VARIATION OF DIELECTRIC AND PIEZOELECTRIC CONSTANTS WITH PRESSURE (One-Dimensional Static Pressure for Conventional Mass-Loaded Stacks)

> ARL - UT AS -71 -661 JHC - DR 5 - 26 - 71





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VARIATION OF COUPLING FACTOR WITH PRESSURE FOR NRE4 AND PZT4 AS MEASURED BY BROWN (9) AND MARTIN (10)

> ARL - UT AS-71-672 JMC - DR S - 26 - 71

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projector materials. No such data have been found on this particular type of ceramic used in projectors. Gerson's results are reproduced here only as an example of what may happen under certain conditions.

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#### IV. TRANSDUCER ANALYSIS BASED ON PIEZOELECTRIC EQUATIONS OF STATE

In this section, the piezoelectric equations of state will be used to develop a mathematical model of a thickness wode piezoelectric plate in which both electrical and mechanical losses are taken into account. Once the equations have been developed for the general case, an equivalent circuit will be developed for the idealized case of a thickness mode ceramic with no internal losses. Several examples are cited from the literature in which equivalent circuit techniques were used to obtain design guides for transducer performance (resonance frequency, power input, power output, dissipated power, impedance). In the remainder of this section. two computer programs written to predict transducer performance are discussed. The programs involve an exact solution to the piezoelectric equations developed at the beginning of this section. The first program, CERAMIC, predicts transducer performance as a function of frequency and drive level. The second program, CALTEMP, predicts the temperature rise and associated effects on ceramic performance resulting from the calculated power dissipated in the ceramic.

#### A. <u>3-Port Equations for Thickness Mode Piezoelectric Plate with</u> Losses Included

A common mode for driving sonar projectors is that in which the applied electric field is parallel to the direction of elastic wave propagation, and the crystal is expanded in the thickness direction as shown in Dwg. AS-71-1101.

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# BROAD PLATE RESONATOR GEOMETRY

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If mechanical losses proportional to the strain rate are assumed, then the equation for the generated stress may be written

$$T = c^{D}(1+j \tan \delta)S-hD$$

where

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c<sup>D</sup> is the stiffness constant, S is the strain, h is a piezoelectric constant, D is the electric displacement, j is √-1, and tan ∂ is the mechanical "loss tangent" of the ceramic.

By definition, the loss tangent is the ratio of the elastic chergy dissipated to the elastic energy stored per radian. For one-dimensional motion in the 3 direction, the stress equation is

$$T_3 = c_{33}^D (1+j \tan \delta_c) S_3 - h_{33} D_3$$

The time-independent electric field equation of state is given by

$$E_{3} = -h_{33}S_{3} + \frac{1}{\epsilon_{33}^{B}}D_{3}$$
$$= -h_{33}\frac{\partial u(z)}{\partial z} + \frac{1}{\epsilon_{33}^{B}}D_{3}$$

where  $\epsilon_{33}^*$  is the complex dielectric permittivity defined as

$$e_{33}^{*} = e_{33}^{*} (1-j \tan \delta_{E})$$

The quantity  $\epsilon_{33}^3$  is the real permittivity measured at constant strain and tan  $\delta_{\rm g}$  is the electrical loss tangent for the ceramic. The (peak) applied voltage is given by

$$\Phi_{12} = -\int_{z=0}^{z=l} \vec{E} \cdot \vec{d}z$$

The face velocities and the input current obtained for the 3-port equations are (time dependence is suppressed):

$$\begin{aligned} \mathbf{v}_{2} &= -\frac{\Phi_{12}^{Z}_{13}\left(\mathbf{z}_{12}-\mathbf{z}_{11}\right)}{\mathbf{z}_{35}\left(\mathbf{z}_{11}\mathbf{z}_{22}-\mathbf{z}_{12}^{2}\right) + \mathbf{z}_{13}^{2}\left(\mathbf{z}_{12}-\mathbf{z}_{11}-\mathbf{z}_{22}\right)} \\ \mathbf{v}_{1} &= \frac{\Phi_{12}^{Z}_{13}\left(\mathbf{z}_{12}-\mathbf{z}_{22}\right)}{\mathbf{z}_{33}\left(\mathbf{z}_{11}\mathbf{z}_{22}-\mathbf{z}_{12}^{2}\right) + \mathbf{z}_{13}^{2}\left(\mathbf{z}_{12}-\mathbf{A}_{11}-\mathbf{z}_{22}\right)} \\ \mathbf{I} &= \frac{\Phi_{12}\left(\mathbf{z}_{11}\mathbf{z}_{22}-\mathbf{z}_{12}^{2}\right) + \mathbf{z}_{13}^{2}\left(\mathbf{z}_{12}-\mathbf{A}_{11}-\mathbf{z}_{22}\right)}{\mathbf{z}_{33}\left(\mathbf{z}_{11}\mathbf{z}_{22}-\mathbf{z}_{12}^{2}\right) + \mathbf{z}_{13}^{2}\left(\mathbf{z}_{21}\mathbf{z}-\mathbf{A}_{11}-\mathbf{z}_{22}\right)} \\ \end{aligned}$$

with the impedance parameters Z<sub>ij</sub> defined as follows:

$$Z_{11} = ZJ_{1} - jZ_{0} \cot \gamma i ,$$
  

$$Z_{22} = ZL^{2} - jZ_{0} \cot \gamma i ,$$
  

$$Z_{10} = jZ_{0} \csc \gamma i ,$$

$$Z_{13} = -j \frac{h_{33}}{\omega} ,$$
  
 $Z_{33} = -j \frac{l}{\omega \epsilon_{33}^* A} .$ 

Detailed derivations of these equations appear in contract status reports for 1 December 1970 - 30 May  $1971^{14}$  and 1 June 1971 - 31 August 1971.<sup>15</sup>

The 3-port equations are, within the limits of the assumptions made, an exact description of the kinetic energy, the potential energy, and the motion in the mechanical vibrating system as a function of frequency. Because most engineers are more familiar with electrical systems than with mechanical systems, mechanical systems are often analyzed in terms of an equivalent electrical circuit. An electrical circuit is analogous to a mechanical system if the differential equation of the circuit is the same type as the differential equation which describes the mechanical system and if the two systems exhibit identical energy characteristics at each frequency.

#### B. Equivalent Circuit of Ideal (Lossless) Piezoelectric Plate

To illustrate the application of equivalent circuit techniques and the way in which such analyses can yield useful design information, the equivalent circuit for a thickness mode plate with no losses is developed. Also, some results obtained through equivalent circuit analysis by various authors are reproduced in this section.

The equivalent electrical circuit is obtained by assuming that voltage is analogous to force, current to velocity, mass to inductance, capacitance to mechanical compliance, and resistance to mechanical resistance (the sc-called "impedance" or "classical" analogy). Under these assumptions, the equivalent circuit for the lossless, thickness mode plate can be shown to be the circuit given in Dwg. AS-71-1248, where

$$C_0 = \frac{Ae^0}{1}$$

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# EXACT EQUIVALENT CIRCUIT FOR THICKNESS MODE PIEZOELECTRIC PLATE

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The circuit shown in Dwg. AS-71-1248 is an exact representation of the piezoelectric ceramic operating in the thickness mode and it is valid for any frequency. In using this circuit to describe a general situation in which the ceramic faces drawa mechanical loads, it is necessary to connect to the mechanical terminals of the circuit the appropriate mechanical load impedances presented by the loads. The final form for the distributed circuit with loads attached is shown in Dwg. AS-71-1025.



# FINAL FORM FOR DISTRIBUTED EQUIVALENT CIRCUIT FOR THICKNESS MODE PIEZOELECTRIC PLATE AS-71-1025

If the resonator is operated near the mechanical resonance frequency  $f_0 = V_0/2l$ , then the distributed impedances may be approximated by lumped impedances. It can be shown<sup>16</sup> that the term  $j2Z_0 \cot \beta l/2$  is approximated by a series-resonant circuit with a compliance  $C_m$  given by

$$C_m = \frac{1}{\pi^2 f_o Z_o}$$

and an inductance given by

100

$$L_{m} = \frac{1}{\frac{4\pi^2 f_0^2 C_{m}}{2}}$$

Salar Carlo Carlo

The j2Z tan  $\beta i/2$  is approximated by a shunt-resonant circuit for which

and

The equivalent circuit near resonance is shown in Dwg. AS-71-1026.

 $L_{g} = \frac{1}{\frac{1}{4\pi^{2}f_{o}^{2}C_{g}}}$ 

 $c_{s} = \frac{\pi^{2}}{18} c_{m}$ 



## LUMPED ELEMENT EQUIVALENT CIRCUIT FOR THICKNESS MODE PIEZOELECTRIC NEAR RESONANCE

AS-71-1026

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## C. Optimum Design Considerations Based on Equivalent Circuits

The application of electrical circuit theory as an aid in analyzing electro-mechano-accustical vibrating systems has been well documented in the literature. The representation of a piezoelectric crystal as an equivalent electrical circuit element was originally given by Van Dyke.<sup>16</sup> The analysis of the piezoelectric transducer driving a mechanical and/or accustical load has been discussed by Mason, <sup>17,18</sup> Olson, <sup>19</sup> and Katz,<sup>20</sup> as well as others. Work of a more specific nature was conducted by Roth,<sup>21</sup> in which the equivalent circuit of a thickness mode piezoelectric transducer was used to determine the electrical driving point impedance as a function of loading and frequency. Thurston<sup>22</sup> has performed an analysis of the transducer loss and bandwidth as a function of mechanical and electrical loading based on the equivalent circuit for a piezoelectric transducer. Kossoff<sup>23</sup> has made use of equivalent circuit techniques in analyzing the effects of backing and matching on the performance of PZT7A transducer. Further references<sup>24, 25, 26, 27</sup> of a more general nature are listed in the bibliography.

The effects of electrical and mechanical resistances on transducer loss and bandwidth have been analyzed by Thurston<sup>22</sup> for a transducer operating near resonance. Three cases are considered: (1) a transducer electrically tuned by a shunt coil, (2) a transducer tuned by a series coil, and (3) an untuned transducer. Some results of his analysis, given below, are valid for the case of a transducer free on one end or a transducer driving a symmetrical load on each end.

The transducer loss at resonance for a shunt-tuned transducer, as determined by Thurston, is shown in Dwg. AS-71-681 as a function of load and source resistance. Transducer loss is defined by

$$TL = 10 \log \frac{P_{max}}{P_{a}}$$

where

P = power actually absorbed in load R,

max = power which would be absorbed if load and generator were matched.

The source impedance is the quantity  $R_g$ . The transducer loss as a function of frequency is shown in Dwg. AS-71-684.





For the case of the series-coil-tuned transducer, the results are essentially the same as the shunt-coil case, as long as the fractional bandwidth of the transducer is small. The fractional bandwidth (FEW) is given by

$$FBW = \frac{f_2 - f_1}{\sqrt{f_2 f_1}}$$

where  $f_2$  and  $f_1$  are the high and the low cutoff frequencies respectively.

A 53, 540

For the case of an untuned transducer, the transducer loss and the approximate FBW are given in Dwg. AS-71-683 as a function of the parameter  $\alpha$  defined by

$$\alpha = \alpha_R C_o R_L$$

The effects of backing and matching on the performance of piezoelectric transducers have been analyzed in a paper by Kossoff.<sup>23</sup> The analysis is valid for a thickness mode transducer for which the loading and backing media are large enough in extent so that no energy is reflected to the transducer. For the nommatched cases, the transducer is assumed to drive directly into the loading and backing media.

Computer calculations were carried out by Kossoff for a FZT7A transducer, 2.5 cm diam, with a series-resonance frequency at 2 MHz. The transmitting sensitivity curves for several conditions of backing and matching are presented in Dwg. AS-71-682. The transducer is assumed to be driving into a water load. For those curves in which the transducer was matched either to the backing, the load, or both, the matching layer was assumed to be a quarter-wavelength thick at the transmitting resonance frequency,

$$f_{o}' = f_{o}\sqrt{1 - \frac{\mu_{c_{m}}}{|c_{E}|}}$$




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( $f_o$  is the series resonance of the  $L_m$  and the  $C_m$  circuit elements of Dwg. AS-71-1026 (see p. 26).)

The "z" and "k" quantities in the figures are defined by Kossoff as follows:

- z<sub>h</sub> = characteristic mechanical impedance of backing medium,
- $k_{\rm h} = z_{\rm h}/z_{\rm mh}$
- z = characteristic mechanical impedance of quarter-wave section used to match transducer to backing medium,

From these analyses it is apparent that optimum power transfer occurs near the resonance frequency of the transducer with the load and source impedance matched. The bandwidth of the transducer is increased by matching either to the backing or to the load, but only at the expense of reduced output power. However, matching both to load and to backing produces a wide bandwidth as well as a satisfactory transmitting response. 

### D. Transducer Performance Predictions Based on Computer Solutions of 3-Port Equations

Two FORTRAN computer programs which were written to obtain theoretical performance data are discussed in this section.

#### 1. Progress CEPAMIC

Program CERAMIC was written to obtain a solution to the 3-port equations as a function of frequency for the piezoelectric plate. The elastic, dielectric, and piezoelectric constants of the ceramic(s) (Section III) provide the necessary input data. The computer solutions are obtained for ceramics operated at field levels for which input data are available. The individual ceramic parameters must be specified for each applied field level. In this study, three ceramics commonly used and commercially available as projector materials, PZT6, Channelite 5400, and Channelite 5800, were examined.

The complex expressions for the (time-independent) face velocities and the input current are reprinted for convenience:

 $v_{2} = -\frac{\Phi_{12}Z_{13}(Z_{12}-Z_{11})}{Z_{33}(Z_{11}Z_{22}-Z_{12}^{2}) + Z_{13}^{2}(Z_{12}-Z_{11}-Z_{22})}$   $v_{1} = \frac{\Phi_{12}Z_{13}(Z_{12}-Z_{22})}{Z_{33}(Z_{11}Z_{22}-Z_{12}^{2}) + Z_{13}^{2}(Z_{12}-Z_{11}-Z_{22})}$   $(z_{1}, z_{1}, z_{2}^{2})$ 

$$I = \frac{\Phi_{12}(z_{11}z_{22}-z_{12}^2)}{z_{33}(z_{11}z_{22}-z_{12}^2) + z_{13}^2(z_{12}-z_{11}-z_{22})}$$

The equations for  $V_1$ ,  $V_2$ , and I are solved by CERAMIC as functions of frequency and field level and the values are used to calculate the rms input and output powers and the rms dissipated electrical and mechanical powers as functions and frequency for each field level. The rms electrical input power for steady state current and voltage is given by

$$P = \frac{1}{2} \phi_{12} |I| \cos \theta$$

where  $\theta$  is the phase angle between  $\Phi_{12}$  and I. The input power per volume of ceramic per kilohertz is given by

$$P = \frac{\Phi_{12}^2 \operatorname{Re}(Y_{1n})}{2A \cdot I \cdot f} \frac{W}{cm^3 \cdot kHz}$$

where

# $Re(Y_{i_n})$ is the total input conductance, and

 $\Phi^{}_{12}$  is expressed in volts, A.1 in cubic meters, and f in kilohertz. The dielectric dissipated power (P^{}\_{UE}), determined from the rms loss current, is

$$P_{DE} = 10^7 \pi \epsilon_{33}^2 \tan \ell_E \left(\frac{\Phi_{12}}{\ell}\right)^2 \frac{W}{cm^3 + kHz}$$

where  $(\Phi_{1,2}/l)$  is the electric field magnitude expressed in kV/cm.

The ceramic plate was arbitrarily assumed to have a radiating area of 0.01 m<sup>2</sup> and a thickness of 0.015 m. The values of the density and sound velocity for the acoustic medium (water) are, respectively,  $10^{3}$  kg/m<sup>3</sup> and 1500 m/sec. The remaining ceramic parameters necessary for the computer calculations are given in Table II. The velocity of sound in the ceramic was calculated from the given values of  $\rho$  and  $s_{\pi\pi}^{D}$ .

$$v_{o} = \sqrt{\frac{c_{33}}{\rho}}$$

based on the assumption that the stiffness constant is the inverse of the elastic compliance. The piezoelectric constant,  $h_{33}$ , is the product of the voltage constant and stiffness constant.

The input power, output power, and dissipated powers were calculated for each teramic as a function of frequency for various drive levels. For PZT8, the applied electric field assumed integral values of 1, 2, ..., 7 kV/cm. The applied field values ranged from 1 to 4 kV/cm for Channelite 540C, and from 1 to 6 kV/cm for Channelite 5800.

TABLE II

	+	++	<b>*</b> 1	Applied Field
Quantity	, 8TZY	Champelite 5400	Channelite 5800	(kV/cm) (peak)
o (density),10 <sup>3</sup> kg/m <sup>3</sup>	7.6	7.6	7.6	I
ψ <sub>c</sub> ,(1/tan δ <sub>c</sub> )	1000	500	1050	ł
g <sub>33</sub> ,10 <sup>-3</sup> Vm/N	24.5	25.3	25.1	I
kıı	ı	0.65	0.62	•
γ <sup>E</sup> 33, 10 <sup>10</sup> N/m <sup>2</sup>	ı	6.75	7.30	3
s <sup>D</sup> , 10 <sup>-12 m2</sup> /N	8.5	8.587 +++	8.434 +++	1
r <sub>13</sub>	1000	1300	980	0
۵۴ <sup>۲</sup> 33, ۲	0.01	1.0 6.3 6 6 6 6	0.3 1.1 1.1	- 0 6 ×
	0.4 9 9 7 9 9 7 9	n 1 1 n	5.0	****
tan <sup>6</sup> k	0.0048 0.006 0.0069	0.009 0.015 0.02125 0.02765	0.00375 0.004 0.005 0.005	<- <- <- <- <- <- <- <- <- <- <- <- <
	0.010		0.00755	r 10 10 10
Proc. IEEE 53, p. 1	1376.			

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CERAMIC PROPERTIES USED IN CALCULATIONS

Proc. IEEE  $\sum_{i=1}^{D}$ , p. 1370. Channel Industries Data Sheet. Calculated from values of  $k_{23}$  and  $Y_{33}^{E} = 1/s_{33}^{D}$ ;  $s_{33}^{D} = s_{33}^{E}$   $(1-k_{33}^{2})$ ‡‡

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As indicated in Table II, the values of the electrical loss tangent, tau  $\delta_{\rm E}$ , and the values of the electric permittivity were specified as a function of the applied field. The table lists the percent increase (from the no-field condition) in the relative dielectric constant,  $k_{33}^{\rm T}$ , as a function of applied field. The permittivity at some field strength E at constant strain is calculated from  $k_{33}^{\rm T}(0)$ ,  $\Delta k_{33}^{\rm T}$ , and the coupling factor,  $k_{33}$ , by

$$\epsilon_{33}^{s}(E) = \kappa_{33}^{T} \epsilon_{0} \left( \frac{\Delta \kappa^{T}}{100} + 1 \right) \left( 1 - \kappa_{33}^{2} \right)$$

The reasonance frequency of a broad plate resonator is defined for the purposes of this report as the frequency of maximum input current. For thickness mode vibrating plate projectors that have a constant D f boundary condition, it is pertinent to note that the resonance quency defined above does not occur at the frequency for which the plate thickness is equal to  $\lambda/2$ , where  $\lambda$  is the wavelength of the elastic disturbance in the ceramic. The deviation of the actual resonance frequency from the half-wave frequency is given by Kossoff<sup>23</sup> on the basis of equivalent circuit analysis.

$$f_{o}' = f_{o} \sqrt{1 - \frac{4C_{M}}{|C_{E}|}}$$

where  $C_M$  is the motional compliance of the near-resonance equivalent circuit and 3 is the negative compliance

where  $\phi = h_{55}C_{0}$  is the electromechanical transformer-turns ratio.

The capacitance  $C_0$  is proportional to the permittivity, and the actual resonance frequency  $f'_0$  will be reduced as  $\epsilon^S_{33}$  increases with increasing field strength. This is illustrated in Dwg. AS-71-990, in which the ratio of the actual resonance frequency to the half-wave frequency,  $f'_0/f_0$ , is plotted as a function of applied field. These results were obtained from computer calculations for PZT8, Channelite 5400, and Channelite 5800. As can be seen from the graph, the reduction in resonance frequency is greatest for Channelite 5400 at all field levels.

The calculated dielectric loss power is shown as a function of applied field in Dwg. AS-71-991. The electric loss tangent was assumed constant with frequency and the results shown are independent of any frequency considerations. The mechanical power losses are plotted as a function of applied field in Dwg. AS-71-992. These plots were made from data calculated at the respective resonance frequency for each ceramic at each value of applied field strength and, therefore, represent the maximum loss as a function of applied field. The last set of curves shown in Dwg. AS-71-993 gives the calculated electro-acoustical efficiency  $\eta_{ea}$  as a function of applied field for each of the three ceramics. The plotted values correspond to the values of  $\eta_{ea}$  at the calculated resonance frequency of each respective ceramic at each value of applied field.

2. Program CALTEMP

The results from program CERAMIC were obtained on the assumption that all of the energy dissipated in the cernaic was transmitted into the surroundings so that no change occurred in the caramic temperature. To obtain a more realistic picture of transducer performance, it ...as essential to include a phenomenological description of a temperature rise in the ceramic resulting from the dissipated internal energy. This seemed especially necessary because future sowars will probably operate at higher search rates and at greater power levels than do present systems.



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Time was insufficient for detailed development of a temperature model; hence, what is presented here may appear somewhat oversimplified; however, this analysis is a beginning from which a more sophisticated description can evolve.

If Q represents the total power dissipated in the ceramic (in units of W/cm<sup>3</sup>/kHz), then at a frequency  $f_0$  (kHz), the power/cm<sup>3</sup> dissipated in the ceramic is

The dissipated power per kilogram of mass is then

1000 Qf /p (W/kg) ,

where p is the density in  $g/cm^3$ . The specific heat,  $C_p$ , (J/kg/deg) can then be used to obtain the rate of temperature rise in the ceramic

$$\frac{\Delta \mathbf{T}}{\Delta \mathbf{t}} = 1000 \frac{Q \mathbf{f}_{0}}{\rho C_{p}} \left(\frac{\mathrm{deg}}{\mathrm{sec}}\right)$$

To simplify the analysis, it is assumed that no heat transfer occurs from the ceramic to the surroundings. After a time  $\tau$  the heat rise is

$$\Delta T = 1000 \frac{Q_0^*}{\rho C_p} \tau$$

and

$$T_f = T_o + \Delta T$$

where  $T_{f}$  and  $T_{o}$  are the final and initial temperatures, respectively.

1) the ceramic operates under steady state conditions during the time interval  $\tau$ , and

 no temperature change occurs during the period between the end of one time interval and the beginning of the next,

Because of these restrictions, the model can be interpreted as a cw system with a parameter update time  $\tau$  or as a pulse mode system with a pulselength  $\tau$ .

In program CALTEMP this temperature model was used to predict transducer performance, taking into account an associated ceramic temperature rise. The ceramic dimensions were assumed to be the same as in CERAMIC:

Area = 0.01  $m^2$ Thickness = 0.015 m

The load impedance on ceramic face 1 was assumed to be zero, and calculations were obtained for the case of an air load on face 2 as well as for the case of a water load.

The only ceramic for which parameter temperature data were available was PZT4.<sup>24</sup> The published data consist of the measured value of the dielectric constant at constant stress,  $X_{33}^{T}$ , and the electric dissipation factor, tan  $\delta_{\rm E}$ . Both parameters were measured at several temperatures for field levels of 1, 2, and 3 kV/cm. Using the published data, each parameter, at each field level, was estimated for each of 36 temperatures (the set  $[T_g]$ ), and the results were read into the program as a 3 × 36 array for each parameter. A 1 × 36 array of the basic corresponding temperature set  $[T_g]$  used in the calculation was also read in and will be referred to as the array  $T_g$ .

The relative dielectric constant at constant stress was converted to the value at constant strain from the relationship

$$\kappa_{33}^{s} = \kappa_{33}^{T} \left(1 - k_{33}^{2}\right)$$

where  $k_{33}$  is the coupling factor. The initial ceramic temperature,  $T_0$ , was taken to be 25°C for each field level. The resonance frequency at that temperature was determined for each field level from program CERAMIC. These frequencies were used in CALTEMF as the operating frequency  $f_0(L)$  for the appropriate field level L.

In CALTEMP, the expressions for  $V_1$ ,  $V_2$ , and 1 are evaluated at the frequency  $f_0(L)$  for each pulse and the input, output, and dissipated powers are calculated. The temperature  $T_f$  at the end of each pulse is determined and compared with the temperature values in the array  $T_s$ . The parameter values used for the next pulse are those corresponding to the temperature in the array  $T_s$  nearest the calculated ceramic temperature  $T_e$ .

The results obtained from CALTEMP for each sequence of 500 pulses (updates) are presented in Dwgs. AS-71-1315 through AS-71-1320. The first three sets of curves were obtained for bilateral radiation into a zero impedance load with pulselength (parameter updates) of 100, 300, and 700 msec. The temperature versus pulse number, input resistance versus temperature, input conductance versus temperature, and input power versus temperature are plotted for each value of pulselength. A second set of similar graphs is shown for the case of air backing, with the ceramic radiating into a water load. In each set an additional curve is shown depicting the output power as a function of temperature.

The temperature effects become more dramatic the longer the drive time and the greater the field strength. As indicated from



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PERFORMANCE MEASURES FOR WATER LOAD, TAU-700 FOR FIELD LEVELS OF 1, 2 AND 4-kV/cm

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PERFORMANCE MEASURES FOR AIR LOAD, TAU = 100 FOR FIELD LEVELS OF 1, 2 AND 4-kV/cm

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PERFORMANCE MEASURES FOR AIR LOAD, TAU = 300 FOR FIELD LEVELS CF 1, 2 AND 4-kV/cm

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120 100 50 TEMPERATURE - °C 40 80 2 RESISTANCE - N 60 1 40 к 20 2 ĩ 0 L 25 0 50 75 100 TEMPERATURE - °C 125 200 300 PULSE NUMBER 500 400 0 100 150 125 +100-+75 REACTANCE +50 +25 25 1 50 75 100 TEMPERATURE - •C 125 0 L 25 -25 125 100 50 75 TEMPERATURE - +C

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PERFORMANCE MEASURES FOR AIR LOAD, TAU = 700 FOR FIELD LEVELS OF 1, 2 AND 4-kV/cm the resistance versus temperature curves, there is a reduction in the input resistance as the temperature increases. The increase in reactance with temperature indicates a shift in resonance to a lower frequency as the temperature increases. The severity of these effects on the input power level is seen from the reduction of input power as the ceramic temperature rises.

Experimental results of a similar nature have been obtained by Kerdig and Clarke.<sup>28</sup> They report a reduction of resonance frequency with increasing temperature and an increase in input resistance with increasing field strength. These results are consistent with those presented here.

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However, Kendig end Clarke also measured an increase in input resistance with increasing temperature whereas CALITEMP calculations would indicate just the opposite. In their measurements, Kendig and Clarke adjusted their operating frequency with temperature so that their ceramic element was driven at resonance for all measurements. In CALITEMP, the driving frequency was maintained constant at all temperatures. No valid comparison of the results for resistance versus temperature can, therefore, be made.

## V. CURVED FACE SONAR ARRAY ANALYSIS

This section will cover the beam patterns of various curved face arrays, directivity index of arrays, and source level, as related to the array configuration.

A. Wide Sectors

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Any beamwidth can be achieved with a planar array if power levels inversely proportional to array length (and, therefore, amount of ceramic in the projector) are acceptable. One technique for increasing the amount of ceramic in a transducer without reducing the beamwidth is to use a curved face array configuration. This can be done by either using a section of a piezoelectric ceramic cylinder or by arranging thickness mode staves vertically as though on the surface of a cylinder. The former is the limiting case of the latter. As the staves become more densely packed, the farfield beam pattern calculations become the same.

The farfield pressure beam pattern of any array of discrete radiators can be expressed as

$$P(\theta) = \frac{1}{N} \left| \sum_{k=1}^{N} E(\theta, k) \cdot A_{k} \cdot e^{i\psi(\theta, k)} \right|$$

where

- $E(\theta, k)$  is the response of the kth element in the  $\theta$  direction,
  - A<sub>k</sub> is the relative amplitude of the kth element and is proportional to driving voltage, mode coupling coefficient. and ceramic area of the kth element.

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 $\psi(\theta, \mathbf{k})$  is the phase of the contribution from the kth element in the  $\theta$  direction. This may be due to electronic phasing and/or geometry of the array.

For the curved face array of identical, discrete, equally spaced line sources driven in phase, the contribution of the kth element in the  $\theta$  direction is

$$E(\theta, k) = \frac{\sin\left(\frac{\pi s}{\lambda} \sin \gamma_k\right)}{\frac{\pi s}{\lambda} \sin \gamma_k}$$

where

s is the length of each element, in inches,

 $\lambda$  is the wavelength, in inches,

and

$$\gamma_{\mathbf{k}} = \theta - \left(\frac{N+1}{2} - \mathbf{k}\right) \alpha \quad \mathbf{k} = 1, 2, ..., n,$$
  
=  $\theta - \frac{\Phi}{2} + (\mathbf{k}-1) \alpha ,$ 

with

N = the number of radiators in the array,
 α = angular spacing between element centers

 (2 • sin<sup>-1</sup> d/2R as shown in Dwg. AS-72-483),
 Φ = angular width of the array (see Dwg. AS-72-483).

Each element is driven in exactly the same manner so that  $A_{i_{k}} = 1, k = 1, 2, ..., N$ .



AS-72-483

For an array of identical elements driven electrically in parallel under the same coupling mode conditions, the function  $\psi$  is given by

$$\psi(\theta,\mathbf{k}) = \frac{2\pi\mathbf{R}}{\lambda}\cos\gamma_{\mathbf{k}}$$
,

where

 $\lambda$  and  $\gamma_k$  are as defined above, and

R is the radius of curvature of the array, in inches.

There are several parameters which affect the behavior of  $F(\theta)$ . In order to isolate the effects of some of them, the following simplifications were made:

 To eliminate the frequency (wavelength) dependence, the distance measures are expressed in units of wavelengths:

$$s = \frac{s}{\lambda} ,$$
  

$$R' = \frac{R}{\lambda} , \text{ and}$$
  

$$d' = \frac{d}{\lambda} .$$

(2) If the element size is allowed to approach zero, the  $\frac{\sin x}{x}$  term in the summation is almost constant. In the limiting case,

$$\lim_{s'\to 0} \frac{\sin(\pi s' \sin \gamma_k)}{\pi s' \sin \gamma_k} = \lim_{s'\to 0} \frac{\left[\pi \sin \gamma_k [\cos(\pi s' \sin \gamma_k)]\right]}{\pi \sin \gamma_k} = 1$$

for all 7.

In the past, curved face projectors built at ARL have been required to insonify a maximum sector of about 70°. As a general rule, ARL curved face projectors have been constructed with an arc of angular width approximately 15% to 20% larger than the desired beamwidth; for example, to achieve a 60° beamwidth, an arc of approximately 70° was used. This general rule is also valid for wider beamwidths. A series of patterns was calculated for different angular width arrays and radii of curvature of  $5\lambda$ ,  $10\lambda$ ,  $20\lambda$ , and  $50\lambda$ . The elements were assumed candidirectional to eliminate the effect of the individual element patterns in the calculation. The relationship between the array parameters R and  $\hat{\mathbf{v}}$  and the beamwidth is shown in Dwg. AS-71-701.

With linear arrays, a zonal shading technique will broaden the beam as well as lower the side lobe levels, so that a wider sector can be covered without much loss in directivity index. Patterns utilizing several zonal schemes with curved face arrays were calculated. Four patterns are shown in Dwg. AS-71-1086 which illustrate the effects of shading. All patterns are for an array of 65 point sources, equally spaced around a 130° arc with radius of curvature of 10 wavelengths. The directivity is increased by these zonal shading techniques, but this increase is due to a severe narrowing of the main beam rather than side lobe suppression.



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In order to determine the influence, if any, of the type of element used, the same array geometry and amplitude shading were used to calculate beam patterns using the following individual radiators:

- (1) Point
- (2) Line
- (3) Piston
- (4) Circular Ring.

It was noted that for the parameters used (center-to-center spacing  $\approx 0.35\lambda$ ) the beam patterns do not vary significantly from the patterns calculated with point sources. However, for larger center-to-center spacing, the point source approximation is less accurate.

In summary, then, any sector width can be achieved using curved face arrays. The limitations on the source level are those associated with the ceramic itself, available power, cavitation limits, and any limits on the physical size of the array. The amount of ceramic used to convert electrical to acoustic power can be increased by using a larger radius of curvature and/or using a longer vertical stave (or array), with a correspondingly narrower beam.

A wider sector can be covered in both the horizontal and vertical planes by curving the face of the transducer in both directions. Beam patterns were calculated for such a configuration, and, as one might expect, the response in the respective planes was equivalent to those for the cylindrical configuration with the same radius of curvature.

### B. Directivity Index

In order to relate the beam pattern of a curved face array configuration to the source levels which can be achieved, the relationship between the beamwidth (or sector covered) and the directivity

must be established. The directivity index for any transducer can be calculated from its three-dimensional beam pattern. This involves, however, a numeric or analytic volume integral of the beam pattern. The numeric form is quite time consuming and a general analytic expression for the beam pattern of a curved face array is not readily attainable. Two approximations to the directivity index are outlined below. Results are calculated over a wide range of parameter values.

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For wide angle curved face projectors, there are several possible configurations, depending on the nature of the desired pattern and the amount of ceramic needed to handle the required electroacoustical power conversion. The two which will be considered here are the sector of a cylinder (curved in one direction, planar in the perpendicular direction) and the sector of a torus (i.e., two radii of curvature).

C. T. Molloy<sup>29</sup> has derived the directivity index for the first configuration, using the following simplifying assumptions:

1) The intensity of radiation is different from zero only in the region  $-\Phi/2505\Phi/2$ ,  $-\pi/25\xi \le \pi/2$ .

2) Inside the above defined region, the farfield, the intensity is assumed independent of  $\theta$ .

3) The dependence of the intensity on  $\gamma$  is assumed to be given by the following expression:

$$I(\theta,\zeta) = \left[\frac{\sin(\pi s \sin(\zeta)/\lambda)}{\pi s \sin(\zeta)/\lambda}\right]^2$$

where the geometry is assumed to be as shown in Dwg. AS-71-1253.

The approximation can be improved by using the actual angular beauwidth instead of the sectoral width  $(\Phi)$  as the boundary of the region of insonification.



AS-71-1253

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The functional form for directivity index (DI) is given by

$$DI = -10 \log_{10} (W(z) \cdot \alpha)$$

where

$$W(z) = \frac{1}{2\pi} \left[ 2 \frac{\mathrm{Si}(z)}{z} - \frac{\mathrm{sin}^2(z)}{z^2} \right]$$

z = 0.46393 × (vertical height of staves, in inches) × f (frequency, in kilohertz),

Si is the integral sine function,

and

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α is the angular half-power beamwidth, in radians, in the plane of curvature of the horn or cylindrical sector.

The values for which the curves were calculated by Molloy were for the application of loudspeakers in air. The curves have been calculated for values of general interest in sonar, and are presented in Dwg. AS-71-1250.

The second configuration projector would be more useful for high power applications in which a relatively large angular sector is desired in both the horizontal and vertical planes.

Assume the intensity is uniform and maximum within a solid augle defined by the angles  $\alpha$  and  $\beta$  (as shown in Dwg.AS-71-1251), and is zero elsewhere.

The directivity ratio  $(R_p)$  is defined by Nolloy as "... the ratio of the total acoustic power output of a radiator to the acoustic power output of a point source producing the same pressure at the same point on the axis.<sup>n29</sup> The directivity index is given by

 $DI = -10 \log_{10} R_{p}$ 



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The total accustic power is the intensity integrated over the entire range of angles  $\alpha$  and  $\beta$ , or the volume enclosed by the beam pattern function. The ratio of acoustic power outputs can then be computed from the volume of the directional and candidirectional patterns. The ratic is

$$R_{p} = \frac{Volume}{Volume} \operatorname{direccional}_{\operatorname{mid} \operatorname{reccional}} = \frac{(20\beta1^{3})/\pi}{(4/3)\pi 1^{3}} = \frac{0\beta}{2\pi^{2}}$$

and

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$$DI = -10 \log_{10}\left(\frac{O\beta}{2\pi^2}\right) = 10 \log_{10}\left(\frac{2\pi^2}{O\beta}\right)$$

This formula gives directivity index as a function of the product of the beamwidths in the two perpendicular planes of the acoustic axis of the transducer. The approximation is as good as is the assumption that the volume of the figure shown in Dag. AS-71-1251 is the volume within the real beam pattern. The "volume" of an actual beam pattern is probably less than the approximation bec-use maximum source level is soldom, if ever, achieved throughout the entire sector.

Directivity in lex as a function of the product OB is shown in Dwg. AS-71-7252. The angles must be in radians for use with this figure.

### C. Source 1 vel

The source level of a projector can be calculated from the total acoustic power cutput and the directivity index:

Source Level =  $71.6 + 10 \log P + DI (dB)$ 



where

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P = total radiated acoustic power, in watts, DI = transmitting directivity index of the transducer, and 71.6 is a factor (in decibels) to convert radiated power in watts to intensity, reference the intensity with P=1 dyne/cm<sup>2</sup>.30 Section and sugar

Drawing AS-71-1094 shows the relationship between sound pressure level and total ecoustic power generated by the transdyper, with directivity index as a parameter.


## VI. CONCLUSIONS AND RECOMMENDATIONS

## A. Summary

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The acoustic projection requirements for high power, high search rate, wide sector sonar systems can be met using curved face transmitter arrays. If additional ceramic is needed to handle the conversion of electrical to acoustic power, a larger radius of curvature can be used to achieve comparable sector coverage if the arc length is increased accordingly. This method of designing projectors is acceptable only as long as the physical size of the transducer remains reascable for the specific application.

A direct application of planar array zonal amplitude shading is not particularly fruitful because the beamwidth is severely narrowed and because only the highest amplitude elements can be driven at full power. If the beamwidth of a shaded array is acceptable, more of the energy is concentrated in the main beam and the array is therefore more directive.

In order to achieve the sector coverage and source levels at which this study is aimed (40° to 60° in either direction), significantly more electrical power will be required than is used by present sonars. If, for example, a 30° by 60° beam is to be achieved with a uniform source level of 120 dB, approximately 10 kW of <u>accustic</u> output power is required. Assuming 50% energy conversion efficiency (a typical value for present systems), 20 kW of electrical power would be required. State of the art power amplifiers can deliver such levels of power

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for duty cycles up to about 0.5%.\* A 0.5% duty cycle would provide a system range of 800 yd and range resolution of 25 ft if achieved with a 5 msec pulse and pulse repetition rate of one per second. Better resolution would lead to lower duty cycle and even more readily fulfilled demands for electrical power. Higher repetition rates or cw operation could greatly increase electrical power requirements, but the limitations of the ceramics examined here would be encountered before all available electrical power would be used.

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The adverse effects on ceramic performance resulting from high drive levels are documented in Section IV. In summary, calculations predict that:

1) The resonance frequency of thickness mode ceramics shifts to lower frequencies as field level increased.

2) The electroacoustical efficiency drops with increasing field levels.

3) The ceramic temperature increases with increasing field level.

4) The increase in ceramic temperature produces adverse effects such as reduction of resonance frequency and loss of acoustic power output.

The assumptions made in analyzing the problem of electroacoustic energy conversion and associated source levels are necessary as well as instructive in a study such as the one described here. Its results aid in understanding the relevant parameters and serve as guidelines for future work.

Present work at ARL.

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## B. Recommended Future Work

(1; Develop a computer model for transmitting arrays. Such a model would provide a prediction capability, not only for the failure of the ceramic, but also for other aspects of array performance quality. A computer model becomes especially attractive when its cost is compared to the cost of "trial and error" construction and testing.

(2) Conduct a theoretical and experimental study of heat transfer properties of transducer arrays. This study should include the ceramic backing material, the geometry of the ceramic, the acoustic window, and the surrounding medium. Whatever energy is not radiated as acoustic power will be dissipated within the ceramic as generated heat or given up to mounting losses. In general, a rise in temperature has two undesirable effects: (c) it adversely affects ceramic performance, and (b) if transmitted to the surrounding medium, it tends to lower the cavitation threshold. No guidelines are known to exist on the thermal design of transducers. An initial effort in this area would in 'ude a literature search for thermal data on the materials used in various components of transducer systems.

(3) Consider the effects of cavitation on transducer performance. This item is important because the onset of cavitation is the ultimate limit of sonar source level. Also, if the cavitation threshold is exceeded, the load into which the coramic operates is reverely decreased. Such a decrease causes an increase in electrical power dissipated within the cerawic, resulting in a rapid and possibly fatal rise in teme-erature. A simple model could be developed, using a curve fitted to published data. Such a model would be of limited scope and would in no way be a complete formulation of the cavitation process, but would be useful as a general guideline in a study of sonar performance.

The onset of cavitation could most readily be modeled as discrete and complete at a predetermined pressure at the face of the transducer. That pressure would be dependent on frequency, temperature, depth (ambient pressure), and pulselength. This approach ignores many factors such as particulate matter and dissolved gases in the water.

(4) Experimentally verify the model for the transducer array. The credibility and usefulness of any computer model is dependent upon comparison with experimental results. Two sources of experimental data are available: (a) parameters of the acoustic projection phenomenon measured in the laboratory where strict control of conditions can be elurcised, and/or (b) published experimental results.

(5) Evaluate the usefulness of newly developed ceramics with a computer model. Two developments reported recently are the whisker-reinforced ceramics<sup>31</sup> and the ferroelectrics containing traces of lauthanum and manganese.<sup>32</sup> The improvement in system performance to be realized by utilizing such materials could be critically examined with a computer model of a projecting array.

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