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NAVAL CIVIL ENGINEERING LABORATORY Port Hueneme, California

Sponsored by NAVAL FACILITIES ENGINEERING COMMAND

DYNAMIC TESTING OF LOAD HANDLING WIRE ROPE AND SYNTHETIC ROPE (U)

January 1970

An Investigation Conducted by

Preformed Line Products Company 5318 St. Clair Avenue Cleveland, Ohio 44103 Project No. M7009-T

N62399-69-C-0013



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### TEST REPORT

### DYNAMIC TESTING OF LOAD HANDLING WIRE ROPE AND SYNTHETIC ROPE (U) NAVAL CIVIL ENGINEERING LABORATORY N62397-69-C-0013 PROJECT NO. M9009-T

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### ABSTRACT

A testing program was initiated by U.S. Naval Civil Engineering Laboratory to conduct dynamic tests on torque balanced wire and synthetic rope. The tests were conducted at the laboratories of Preformed Line Products Company, Cieveland, Chio.

The scope of the work was to provide date so that a basis can be established to select the best type of line for load-handling purposes in the deep ocean environment. The tests consisted of tension vs elongation, rotation and kink formation, and longitudinal dynamic response.

The tension elongation tests yielded data typical to stranded line construction.

The rotation-kink tests revealed that negligible ratations resulted in the test cables when under load and that no kinks were formed when the load was suddenly released.

The dynamic response tests showed that the measured dynamic stresses were dependent upon the exciting frequency. The natural frequency for the synthetic rope sample was 0.3 cps and 0.6 cps for the wire rope.

The tests indicated that the highest values of combined static and dynamic stresses occur at resonance which could cause failure of the cable at points of high stress concentration.

It is recommended that some hydraulic parameters and random excitation be introduced in the future testing of this type. Stress relieving fittings should be investigated for use on load handling lines in the ocean environment. January 1970

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### TEST REPORT

### DYNAMIC TESTING OF LOAD HANDLING WIRE ROPE AND SYNTHETIC ROPE (U) NAVAL CIVIL ENGINEERING LABORATORY N62399-69-C-0013 FROJECT NO. M9009-T

### Introduction

The testing program described have in was conducted for the Naval Civil Engineering Laboratory, Contract No. N62399-69-C-0013, on government furnished steel wire rape and synthetic rope. The tests were conducted at the laboratories of Preformed Line Products Company, Cleveland, Ohic.

The objective of this work was to provide test data to be analyzed and evaluated as a basis for the selection of the best type of rope for load-handling purposes in the deep ocean environment. The types of tests conducted consisted of tension vs elongation, rotation and kink formation, and longitudinal dynamic response.

### TENSION VS ELONGATION TEST

### **Description of Test Equipment**

The equipment used to conduct the tension elongction tests was a horizontal testing machine with a loading capacity of 50,000 pounds and a spon length of 60 feet. Fig. 1 is a schematic of the equipment.

The test machine has nonrotating clavis ends, one attached to a hydroulic ranand the other to an adjustable dead-cod. The hydroulic system has a constant pressure pump with a flow control to vory the loading range. The load synsing system is composed of commercial load cells installed in series with electronic components and a 24-inch dial readout with varying load ranges up to 50,000 pounds. Because of the substantial differences in the physical properties of the wire rope and the synchetic rope, the test setup was modified to suit the respective test samples. Since the strength of the wire rope exceeded the test machine loading capacity, a force-doubling pulley arrangement was applied between the machine ram and its frame and one end of the test sample. A 200,000-pound load cell was installed in series with the test sample to sense the load and a Baldwin SR-4 Strain Analyzer was employed to measure the tensile load in the test sample as shown in Fig. 2. Optical cathometers were used to measure the elongation. Fig. 3 shows the setup used.

The double patter arrangement was not used for testing the synthetic rope, however, because of the stretch characteristics of the rope. The calculated elongation of the rope revealed that the machine ram travel was insufficient. Therefore, turnbuckles were used in line with the test sample to take up the initial stretch. Fig. 4 shows the test setup used. Elongation was measured with  $\oplus$  steel tape to the nearest 1/8 inch.

### Test Samples

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> All tests were performed using government furnished steel wire rope and synthetic rope. The wire rope was new. However, there was evidence that the synthetic rope had been in service prior to testing. The contractor was responsible for test sample terminations. The loops in the synthetic rope samples were formed by Samson Cordage, Boston, Massuchusetts and the wire rope was terminated with spelter socket fittings. Specifications of the respective ropes are listed in Figs. 5 and 6.

### Test Proceedure

Each test sample was placed in the test machine and pulled taut to an initial tension of 1,000 pounds. A 60-inch gage length was then marked with an accuracy of  $\pm 1/16$  inch.

Additional tensile load was then applied at the rate of 0.619 inches per minute in 5,000-pound increments. These incremental loads were held for one minute. During the load-holding periods, the corresponding elongations of the gage length were measured at the beginning and again at the end of the holding periods. The duplicate measurements were made in anticipation of possible hunde errors and for possible creep in the line material. Measurements were taken up to 60 per cent of the rated breaking strength of the material. The test samples were then pulled to centruction noting the approximate breaking load.

### Test Results

Test results for the wire rope are tabulated in Tables 1 and 11 and shown in curve form in Fig. 7.

Test results for the synthesic rope are tabulated in Table 111 and shown in curve form in Fig. 8.

The ultimate fracture occurred at or near the terminaling device for both types of material. Fig. 9 reveals that the wire rope failed at the edge of the zinc socket and Fig. 10 clearly shows the failure of the synthetic rope at the junction of the loop and the long end of the rope.

### Discussion

The following problems were encountered during this series of tests.

The breaking strength of the wire rope exceeded the test machine capa ity. A method to obtain higher loading was devised to utilize the existing test equipment.

The ram travel of the test machine was limited. A system and technique to take up the extensive stretch of synthetic rope had to be devised and employed.

Failures of the test samples below the rated breaking strength was a serious problem. In the case of the synthetic rope, the required elongation reading prior to failure was nor measured because of the premature failure. This also caused concern for the satety of the laboratory personnel who were taking elongation readings. Nonrepeatability and deviation in measured data was evident.

In order to obtain confident elongation readings on the wire rope, several samples were tested. In the first samples, problems developed with the hydraulic system and the sample was cycled several times before it failed. The test sample was loaded to the capacity of the test machine and then the load was released and a pulley arrangement was installed. This technique resulted in a discontinuity and a hysteresis curve as shown in Fig. 13.

A second sample was tested. There was a strong deviation of data in this test and upon inspection of the test sample it was noted that at one socket fitting a strand had slipped our prematurely which could have caused the erratic readings. This data was discarded.

The most dependable data was obtained from the third sample tested and the data is presented in Fig. 7.

Additional samples of the synthetic rope were not tested because it was decided that the one test clearly indicated the weakness of the synthetic rope termination. To conduct further testing would have required additional time and expenditure to design, develop and manufacture a special end fitting to hold the full-rated strength of the synthetic rope.

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For multistranded cable such as used in these tests, the attainment of full rated breaking strength depends a great deal upon the uniform loading of the individual strands. This is not a simple task when using most commercial fittings.

Due to intrinsic variations in the tensile and physical properties of a terminated cable, several test samples should be tested in order to yield enough data to determine an effective holding strength and a representative cable modulus of elasticity Unfortunately, extra test samples were not available because of the limited amount of material on hand and for the economic reasons mentioned earlier.

### ROTATION AND KINK FORMATION TESTS

### Test Equipment and Setup

The laboratory was faced with the problem of testing relatively long lengths at various high loads in a vertical configuration. Existing laboratory equipment did not have the required amount of weight, the lifting capacity nor the needed heights. Therefore, it was decided to conduct the rotation and kink tests outdoors at a local scrap yard where the weights and a crane with lifting and height capacity were available.

Each test sample was vertically suspended from a boom having a locked clevis attachment at the top. The bottom end of the suspended test sample was loaded with attached weights and was free to rotate.

Four groups of preweighed weights were used for each test sample. Weights of 2,250, 4,500, 6,900, 9,000 pounds were used to test the synthetic rope samples, and 4,100, 7,800, 11,800, 15,400 pounds were used to test the wire rope samples.

A 36-inch machinist scale was suspended from an upper gage mark of each test sample to measure elongation.

Visual observations of the associated rotations were made by means of stationary and rotating markers, one on the ground and one on the attached weight assembly, respectively.

Test Somples

Eight test samples were prepared as follows:

Test Sample Flo. 1	19 feet 2 inches	Synthetic
Test Sample No. 2	10 feet 11 5/8 inches	Wire
Test Sample No. 3	19 feet 5/8 inch	Synthetic
Test Sample No. 4	10 feet 11 1/8 inches	Wire
Test Sample No. 5	18 feet 9 5/8 inches	Synthetic
Test Sample No. 6	10 feet 11 5/8 inches	Wire
Test Sample No. 7	17 feet 11 1/8 inches	Synthetic
Test Sociale No. 8	Il feet i inch	Wire

The lengths is the wire rope were measured from mouth-to-mouth of the socket filting. The lengths for the synthetic rope were measured from pin-to-pin.

### Tes? Procedure

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At the baginning of each test, the test scaples were preloaded with a tare load of 200 pounds. At this time the initial naminal length was measured, the 120-inch gOgo length was marked, visual alignment of the end fittings was ascertained and a beach mark, or zero reading, for subsequent rotation was obtained.

The sample was thus forward and the required weights were attached to the test sample. Such loaded test sample was then raised off the ground. During the raising process, the weighted end was monually held by a technician in the zero preition. The manual rotational restraint was then released and the assembly was cllowed to rotate and oscillate freely. Observations of the direction and magnitude of the maximum rotations were made and recorded. When the oscillations stopped, the elongation position of the lower gage mark was measured and recorded. (Fig. 12)

The weighted azembly was then dropped to the ground by rapidly lowering the boom. The test sample was allowed to collapse several feet. Observations for kink formation were then made. Figs. 13 and 14 show the collapsed cable with no kinks.

### Test Rasults

The results are tabulated in Tables IV and V. Graphs were not constructed because the observed angular rotations were comparatively small and inconsistent. An example of this inconsistency can be seen in Table V. During the autdoor testing of the synthetic rope, the sample rotated 225 degrees at a load of 4,500 pounds. At a load of 6,900 pounds, the sample rotated 45 degrees, and at 9,000 pounds, 135 degrees.

### Discussion

Prior to testing, it was assumed that the constructionally tarque-balanced test samples would tend to twist when loaded axially and that they would form characteristic kinks upon sudden release of the tensile load. The test results indicate otherwise, and all the tests showed comparatively little or no rotation and no kinks were formed. Because of the unexpected results, several repetitious tests were run. Also, a suries of rechecks in the laboratory on the horizontal testing machine were conducted to compare with data obtained outdoors. In the laboratory the test samples were attached to a rotating clevis of the subt-bearing nonstruction on one end to allow the sample freedom of rotation during boading. Despite some frictional resistance of the rotating clevis, these laboratory rechecks substantially corresponded with the cutdoor results regarding the order of magnitude for the expected angular rotation. Again, these angular movements were were small in comparison with what might be expected from multistrand cable not harding; torque-balance design features.

These test results indicate that the manufacturer's claims to a targue-balanced line were vistually substanticted, at least for the lengths of the test samples employed. This does not imply that the test samples were free of targue conditions. The test results brought attention to the need for finite rotational measurements, when this does is required to extrapolate sample lengths to substantially longer lengths of targuebalanced cable.

The results of no kink formation indicated that the targue developed under lond was negligible for these cable constructions, resulting in no rotation. Therefore, there was no cable distortion which would cause kinks in the cable, should a slack condition suddenly develop.

### DYNAMIC RESPONSE

### Considerctions Prior the Testing

The luboratory was faced with numerous test-engineering problems prior to testing. These problems and their respective solutions are described as follows.

Interpretation of realistic sec-state periods corresponded to relatively low frequencies in tensile excitation which were coupled with relatively small cyclic specimer: displacements.

In order to determine the modifications required to match our existing equipment capabilities with the test performance requirements as outlined, the basic dynamics of the test program were further analyzed. The N.C.E.L. Technical Report No. 433 (AD 631 267) was reviewed and the mathematical model was converted to a laboratory test model. Such efforts revealed the following:

- 1. Fundamental resonance can occur at relatively low frequencies for both rope materials, particularly when design parameters were scaled down to those of a laboratory test model. Calculations are included at the end of the text.
- 2. The magnitude of the cyclic axial displacements did not enter into the dynamic response of the taut-rope mass system.
- 3. The installation of another weight at the driving end of the test span, for the purpose of maintaining a notional rope tension during the cyclic excitation, did not essentially affect the dynamic response, porticularly at resonance.

Practical test equipment modifications, and a test procedure and setup were devised and employed. Such Aquipment was believed to provide calld simulation of the dynamics involved in a vertical ocean-lift system.

The equipment erray, as shown in Figs. 15 and 16, was designed, fobricated and assembled for conducting this series of tests.

After some preliminary tests using the wire rope test sample (squipment and technique shake-down period), the dynamic forces at resonance indicated the need for substantial rope terminating fittings. This requirement became acute for the synthetic rope material, in light of the termination deficiency experienced with the loop termination during the previous tension elongation tests.

Because of this necessity, an encapsulated tensination of the synthesic rape was developed and was cycled between 10,000 and 20,000 pounds (expected region under the dynamic test equipment) in the tensile testing machine without any slippage.

### Test Samples

Both types of rope material ware furnished by N.C.E.L. thuy ware out to length and equipped with termineting fittings. The length of the wire rope test sample was 126 feat 7 inches. The length of the synthetic rope test sample was 117 fest 3 inches. Both lengths were measured under a cominal tension of 10,000 pounds tension while resting in the test spon.

The tanning fittings for the wire rope were identical to those described and shown in Fig. 9.

The terminating fittings for the synthetic repe ware constructed as follows:

- The core and the acter layer strands were untwined and thuroughly wetted with Scatch-Cast No. 9 resin (3-14 product).
- b. The objectation strongs were circumferentially placed and wedged by a metallic cone piece against the inside well of the alevis-type socket fitting.

- c. The core strands were fed through the large center hole of the wedging cone piece. The extended core strands were radially mushroomed outward.
- d. The entire assembly was than potted with Scotch-Cast No. 9 resin, making particularly certain that sufficient resin was present in the necked cavity of the fitting.

### Test Equipment, Setup and Instrumentation

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The test equipment, setup and instrumentation were common to both test samples of wire and of synthetic rope. The overall arrangement is shown schematically in Fig. 17. The constituents were as follows:

Abutments provided the supporting structure for the spanned test assembly.

- <u>Guides</u> offered horizontal guidance at three different locations along the span to minimize vibration to the test span.
- <u>Turnbuckles</u> provided a means of fine adjustment in tensioning the test samples to the desired nominal 10,000-pound line tension. One clevis stud of each turnbuckle was instrumented with strain gages to measure axial tensile load.
- Pillow Blocks provided the longitudinal guidance for the actuating linkages. These pillow blocks were constructed of Thomson linear ball bearings, thus offering minimal sliding friction.
- Loading Beams & Dead Weights provided load multipliers and the maintenance of line tension. The driving beam end transmitted ine sinusoidal excitation. The pivoting beams were constructed with antifriction ball bearings.
- Load Cells were used to sense the tension variations at the input and output ends. The safe working load for both load cells was 18,000 pounds.
- Linear Variable Differential Transformers were used to measure the longitudinal displacements.
- Drive Mechanism provided the cyclic longitudinal displacements at variable frequencies and amplitudes. The mechanism consisted of a variable gear motor, sprocket-chain, jack-shaft reduction stage, driving a variable crank-arm, four-slide mechanism. The slider was attached to the pivoted beam through a pin-slot.

### Instrumentation Seconder was a Honeywell No. 1020 multichannel oscillograph. It was complemented with a Heiland oscillator and carrier amplifiers. The recording galvos were of 1,600 cps response.

### Test Procedure

The test samples were installed between the abutments of one of the 125-foor vibration beds. In order to arrive at the correct final installed test sample lengths between the end abutments required a predetermination of the load-free length of the test sample.

For the wire rope, theoretical calculations of the required length were rather straightforward. However, for the synthetic rope, predetermination of the length was not so easily accomplished. The theoretical calculations of the stretch only provided a regional length. The exact length dimension was difficult to determine because of the various inaccuracies of the physical data used to calculate the stretch length when under load. One of these factors was looseness of the external layer of the synthetic rope. Therefore, a trial and error method was used. That is, a length of rope was installed and the length under load was noted. The sample was then removed and shortened and then reterminated. The final load-free length resulted in a much shorter length than the calculations indicated. The test samples were pulled into position by using ratchet type line hoists. The test samples were then secured in the test span when the inline load reached 10,000 pounds for the wire rope and 13,000 pounds for the synthetic rope. When the pulling end device was removed, the span line tension dropped to somewhat below the required test load.

The final nominal tensioning to test load was accomplished by adjusting the ture uckles which were installed in series with the test samples. After acquiring the desired test tension, the guides were attached to eliminate transverse vibration of the test samples.

The required instrumentation used to sense the predetermined test parameters was then installed and calibrated. This instrumentation consisted of two LVDT's to measure the displacement at either end and two load cells to measure the force variations at the input and output end. During the cunning of the test all the force and displacement signals were simultaneously recorded on the oscillograph.

To reach the low natural frequency of the tested taut-rope mass system, the driver mechanism was started at a speed above resonance, then incrementally swept upward about 5 cps and swept downward until the resonant frequency was reached. At resonance, the driven end of the wire rope displayed significantly large amplitudes of displacement.

In the case of the synthetic rope, resonance was not obtainable from the machine drive because its lowest geared downspeed was not low enough to approach the natural frequency of the system. The method used to obtain the natural frequency was to rap the driven beam at the rate of about two or three times a second until an apparent and sustaining resonance resulted.

In each test, simultaneous oscillographic recordings of the four sensors were taken at incremental excited frequencies with two or three different longitudinal displacement amplitudes. After completing the dynamic test, the setups were disassembled and the individual moving parts were weighed. A list of these weights is presented in Table XVII, so that correlations with the associated analytics can be accomplished.

### Test Results

Tesr results for the wire rope are tabulated in Tables VI through X and shown in curve form in Fig. 18.

Test results for the synthetic rope are tabulated in Tables XI through XVI and shown in curve form in Fig. 19.

A typical recording of the dynamic response data is presented in Fig. 20.

These tests clearly indicated that the dynamic amplitudes and stress in the rope were dependent upon the exciting input frequency. This dependence can be more specifically related to the ratio of the exciting frequency and the natural frequency for a given taut-rope mass system. Although maximum dynamic amplitudes were always obtained at resonance, maintaining resonance was observed to be very difficult because the resonance frequencies peaked over sharply and the delineation between resonant and nonresonant states was quite abrupt. Consequently, most of the test results were obtained under nonresonant conditions. At these conditions, the driven end was virtually at a standstill. This indicated that the input-exciting displacements caused elastic elongations in the test samples.

Since the synthetic rope has a lower spring constant and associated dampening, it had to be excited with larger longitudinal displacements than the wire rope in order to yield readable data.

### Discussion

### Selection of the frequency spectrum

The taut rope-mass arrangement of this experimentation could be compared to a spring-mass system with the support being sinusoidally excited. The natural frequency of such a simplified system is dependent upon the effective spring constant and the suspended mass.

In relating laboratory testing to a specific oceanographic application, the k/m expression can vary widely. Such large variations can be caused by the rope material, its length and the "virtual" mass of the submerged constituents. The laboratory experiments indicated the rope material and length appeared to be the most effective parameters. Since the effective spring constant, k, varies inversely with the length of a line, relatively low natural frequencies would be expected. In this regard, the experimental setup simulated a considerably longer rope length than the test sample due to the modifying dynamic effect of the lever arm ratio, a/l, for the pivoting beam.

The employment of relatively low test frequencies can be further supported by laboratory test efforts in attempting to obtain and observe maximum dynamic stresses in the cable. Maximum dynamic stresses are most easily obtained at fundamental resonance; that is when the frequency of the exciting source equals the fundamental frequency of the taut rope system. In reference to sea applications, the heaving movement of a ship is characterized by low frequencies.

Therefore, when the above aspects are combined, the selection of the reported test frequency spectrum (0.3 to 5.0 cps) appears to be in order with realistic line parameters and with the expected excitations at sea.

### Maximum stress

Measurements of the dynamic stresses indicated they can be of significant magnitude occurring almost simultaneously and of equal magnitude at both ends in the relat" rely short laboratory test samples. Consequently, fatigue may become a serious concern for an actual sea application.

The most likely occurrence of incipient fatigue may be at or near the ship end, because at that location the state of combined stresses is the most severe. In contrast, the magnitude of the combined stresses decreases with increasing depth along a nonbuoyant line due to diminishing line weight. However, high local stress concentration can result from attaching to the cable some fittings and appendages which do not have stress-relieving design features. These conditions can cause an early failure of the cable. In such cases, failure usually occurs where these fittings are located along the submerged line.

### Combined stress

A load-handling rope in the ocean can be and usually is, subjected to a combination of staric and dynamic stresses which can exceed the critical stress of the rope material and cause failure. These stresses are usually axial, torsional, flexural and radial compressive and are generally identifiable. Howaver, radial compressive stresses are not easily defined and do not lend themselves to analytical solutions. For example, in the case where two layers of individual wires are stranded in opposite lay direction, as in double-armored cable, there is point-to-point contact between the two layers and any radial compressive stresses, such as passage over a sheave or the attachment of any bolted hardware to the line, will contribute to the high levels of localized st. ss concentration.\*

The need for endurance information under combined stresses and wet conditions have become apparent. Such data would provide an ultimate meaning to field and laboratory determinations.

### Elongations

During the past it was observed that at resonance the elastic elongations of the rope were toward the driven or output end. During nonresonance the elongation took place in the opposite direction, toward the input or simulated ship end. This can be observed from Fig. 19, and by noting the dynamic response Tables VI through XVI. Referring to Fig. 19, at resonant frequencies the output-input ratio is relatively high compared to the nonfrequency ratios.

For example, from Fig. 19 and Table VII, at a frequency of .60 cps the input displacement is 90 mils and the autput displacement is 700 mils. The ratio is 7.78. However, at a nonresonant frequency of 1.5 cps and higher, the ratio tends to become flat but at a much lower value of .040 at 3.00 cps.

Relating these observations to a combined construction of wire and synthetic ropes, then substantially all the dynamic elongations would occur in the synthetic rope whether at resonance or at norresonance.

### Problems encountered

Some experimental problem areas may be outlined as:

- 1. A comprehensive test engineering analysis was necessitated prior to the design of the experimental equipment.
- 2. The appropriateness, limitations and modifications of the existing facilities had to be thoroughly explored.
- 3. The need for a suitable, dynamic terminating fitting for the synthetic rope was required and had to be constructed so as to insure successful completion of the test program.
- \* J. C. Poffenberger, E. A. Capadona, and R. B. Siter, "Dynamic testing of cables," Transactions, 2nd Annual Marine Technology Society Conference, Washington, D. C., <u>Exploiting the ocean</u>, pp 485–523. June 27 – 29, 1966.

### Summary

The laboratory experiments indicated the rope material and length appeared to be the parameters which most affected the k/m expression. The tests also confirmed the relatively low natural frequencies which were expected in the considerable longer rope lengths used in the ocean.

The laboratory tests also indicated that the maximum dynamic stresses usually occur at fundamental resonant frequencies of the rope system. Measurements of these dynamic stresses showed that they can be of significant magnitude occurring simultaneously at both ends of the relatively short laboratory samples. A study of Fig. 20 and the dynamic response tables indicate this situation and also reveal that at resonance the elastic elongations of the rope are toward the driven or output end. During nonresonance, the elongation takes place in the opposite direction, toward the simulated ship end.

### RECOMMENDATIONS

- 1. Closer simulation of the sea opplication may be obtained by introducing some of the hydraulic parameters, viz., drag, buoyancy.
- 2. Random loading of test samples should be investigated. Under random loading conditions, low frequency resonance becomes difficult to sustain because the resonant frequencies peaked very sharply and the dolineation between resonant and nonvesonant state was abrupt.
- 3. Endurance data for various rape material is needed and is of great importance in the sea environment. The needed endurance data could be categorized as a high state of stress combined with a low cycle life, and a low state of stress combined with high cycle life.
- 4. Terminating fittings should be carefully selected in conjunction with the associated dynamics since the weakest link in some systems is at or near the termination.
- 5. A reliable terminating device should be designed and employed, in order to establish an adequate basis for comparison and selection of the best type of line for load-handling purposes. Then, a relatively large number of samples should be tested. Testing of several samples is desirable for any material. This desirability becomes especially acute for stranded line materials which are inherently characterized by nonuniformity of loading along the individual strands and/or among their groupings.
- 6. More sophisticated instrumentation should be developed to obtain vernier rotation measurements which could become useful, so that the amount of rotation from relatively short length laboratory samples could be extrapolated to longer field lengths. If loops had been formed and kinks developed on short lengths in the laboratory, then it could be safely assumed that loops and kinks will form on very long lengths.

7. It is recommended that the rotation kink formation phase of testing be further investigated from the standpoint of determining how much rotation is actually needed to form a loop and a kink.

### ACKNOWLEDGEMENTS

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Gratitude is expressed to Mr. R. A. Komenda and the Research and Engineering Laboratory personnel for their planning and performance of laboratory tests, and to Mr. S. Grosshandler for his consulting assistance and coordination between the Marine Systems Division and the Laboratory. Also, greatly appreciated is the assistance of several other personnel who helped complete the final test report.

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### TABLE 1

### TENSION ELONGATION DATA FOR WIRE ROPE SAMPLE NO. 1 \*

Gage Length - 60 inches

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lst Load	ing Cycle	Unloadir	ng Cycle	2nd Load	ling Cycle**
Load	Elongation	Load	Elongation	Load	Elongation
(ibs)	(ins)	(ibs)	(ins)	(lbs)	(ins)
1,000	.000	50,000	.306	10,000	.000
5,000	.047	45,000	.341	20,000	.056
20,000	.084	40,000	.298	30,000	.100
15,090	- 123	35,000	.254	40,000	.146
20,000	.132	30,000	.228	50,000	.236
25,000	.170	25,000	. 190	55,000	.242
30,000	.202	20,000	.152	60,000	.307
35,000	.204	15,000	. 142	000,زە	.329
40,000	.232	10,000	. 105	•	
45,000	.263	5,000	.055		
50,000	.306	1,000	.029		

\* See Hysteresis Curve Fig. 11.

\*\* Force multiplying pulley arrangement was installed to obtain higher loadings.

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### TABLF II

### TENSION ELONGATION DATA FOR WIRE ROPE SAMPLE NO. 3

### Gage Length - 60 inches

Load	Elongation
(ibs)	(ins)
1,000	.000
5,000	. 103
10,000	.152
15,000	. 184
20,000	.224
25,000	.260
30,000	.296
35,000	.335
40,000	.366
45,000	.410
50,000	.433
55,000	.494
60,000	.528

Wire rope failed at 66,500 pounds.

### TABLE III

### TENSION ELONGATION DATA FOR SYNTHETIC ROPE SAMPLE NO. 1

### Gage Length - 60 inches

Load	Elongation
(ibs)	(ins)
1,000	0,00
2,009	0.50
5,000	2.00
10,000	4.31
15,000	6.50
20,000	8.44
25,000	10.63

Synthetic rope failed at 29,200 pounds.

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### TABLE IV

### ROTATION AND ELONGATION DATA FOR WIRE ROPE

### (Outdoor Measurements)

Lead	Specimen No.	Elongation	Rotation
(ibs)		(ins)	(degrees)
200		Ċ	0
4,100	2	6/64	Ĉ
7,800	4	7/64	45
11,800	6	14/64	90
15,400	8	12/64	135

### (Laboratory Measurements)

1.ood	Specimen No.	Elongation	Rotation
(lbs)		(ins)	(degrees)
200		0	0
4,100	2	5/64	20
7,800	4	10/64	5
11,800	6	13/64	9
15,400	8	17/64	4

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### TABLE V

### ROTATION AND ELONGATION DATA FOR SYNTHETIC ROPE (Cuilibor Measurements)

Load	Specimen No.	Elongation	Solation
(lbs)		(ins)	(degrees)
290		0	C
2,250	1	4 11/64	C
4,500	3	7 32/64	225
6,900	7	9 43/64	45
9,000	5	30 55/64	135

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Remorts	Line Terretons 10,250 the	Attn. Used		7. 110.1 DOOT				-0															
240		3.09	3.8	ຊ	8	.25	8	8	.25		8	8	8 <u>,</u>	8	8	8	8	8	8	8	8 <sub>.</sub>	8	
ri AT		1,335	1.335	55.	.637	.667	8 8 8	.363	.583	8		585.	805.	538		55.	8 <u>.</u> 5.	83		<u>.</u>	.585	<b>S</b> .	
Displacement Output (Do)	(mil)	185	180	5	15	5	0	23	ŝ	ŝ	0	0	0	0	a	0	0	0	0	o	0	0	
Displacement Input (A1)	(114)	Ş	8	3	23	3	\$	Ş	3	3	3	3	3	3	Ş	3	\$\$	65	8	Ş	3	3	
Force Output (Fo)	(Ibe)	89	250	30	800	800	330	300	800	250	230	200	8	30	800	8	8	80	250	800	8	800	
Force Input (Fi)	(14)	850	006	350	35	8	300	350	350	85	200	38	350	350	336	350	350	350	330	350	350	350	
Frequency	(cps)	0.55	0.55	8.	8.	1.10	1,40	- Cr5	<b>49</b> . (	1.46	<b>8</b> .7	8.2	2.25	2.25	3.33	2.50	2.50	2.5	2.66	2.66	3.00	3,0	

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### TÀBLE VI

## STEEL WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 60 Mil Peak-to-Peak

TABLE VI (continued)

## STEEL WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 60 Mil Peak-to-Peak

		۵٬۰۰۰ ۲۰۰۰ ۲۰۰۰ ۲۰۰۰ ۲۰۰۰ ۲۰۰۰ ۲۰۰۰ ۲۰۰۰
Remarks		
<u>00</u>		88888
₽i Pi		.538 .572 .572 .572 .572
Displacement Output (∆o)	(mil)	00000
Displacement Input (∆i)	(mil)	\$ R R R R R
Force Output (Fc)	(lbs)	8 8 8 8 8 8 8 8 8 8
Force Input (Fi)	(lbs)	350 350 000 000 000 000 000 000 000 000
Frequency	(cps)	6 6 6 8 6 7 7 7 8 8 6 7 8 8 8 9 7 9 9 9 9

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### WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 120 Mil Peak-to-Peak

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									:	Cell No.	68087	466 # /Div	233 # /Div	94 #/Div	47 #/Div							
	00 lbs	tion	£	1				ر ما اد ت ما اد		Cell No.	9009 M	348 # /D:	184 #/Div	74 # /Div	37 #/Div							
	nsion: 10,6	Calibro	ומאז			20	10	, hav 1			µ <td>Q</td> <td><u>ج</u> ک</td> <td>ς α</td> <td><b>)</b> ~</td> <td></td> <td><b>lse</b>d</td> <td>0.1</td> <td>ells 0.1</td> <td></td> <td></td> <td></td>	Q	<u>ج</u> ک	ς α	<b>)</b> ~		<b>lse</b> d	0.1	ells 0.1			
Remark	Line Te			A 44 m		0.1	0.2				Attn.			4 ¥		2.	Attn. U	LVDT	Load C			
\ \ \ \ \ \ \		3 0300	6.6000	7.7200	7.7800	6.8700	1.1300	.3590	.5830	.3200	. 1600	.1600	.1600	. 1200	.1200	.1200	. 1200	.1250	.0400	.0768	0220	.0400
ш!<	i	1 070	3.130	3.070	3.610	3.720	1.250	.800	.833	.800	.638	<b>00</b> 9.	.640	.638	.625	.625	.625	.625	.583	.615	.538	.560
Displacement Output (Ao)	(mil)	550	86	925	200	1,030	135	45	20	40	20	20	20	15	15	15	15	15	ŝ	01	01	ŝ
Displacement	(mil)	07	150	145	8	140	120	125	120	125	125	125	125	125	125	125	125	120	120	130	130	125
Force	(lbs)	, <b>6</b> ,00	4.400	1,050	3,900	4,700	1,300	800	<u>%</u>	800	700	700	200	700	600	600	600	650	600	700	603	550
Force	(1bs)	003	4.700	4.450	3,250	5,200	1,500	1,000	000,1	1,000	800	750	300	800	750	750	750	750	700	800	200	700
	(cps)	- L - L - C	00 85.0	0,60	0.60	0.66	0.85	00.1	00.1	1.10	1.40	1.40	1.50	1.55	1.55	1.65	1.75	1.75	2.00	2.00	2.00	2.30

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### WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 120 Mil Peak-to-Peak

	Remarks																				
<u>ک</u> ہ	Δi		.0400	040	. 0370	.0400	.0357	. 0400	.0400	.0400	.0537	.0400	0000.	000.	000.	0000.	0000.	0000.	 ą. <u></u>	 	
Ē	۵i		.560	.638	.518	.638	.500	<u>8</u>	.616	8%.	.50	.538	<b>00</b> 9.	.483	.556	.593	.536	.483			
Displacement	Output (∆o)	(mil)	ۍ	5	5	5	5	ŝ	ŝ	5	S	5	0	0	0	0	0	0			
Displacement	Input (∆i)	(mil)	125	125	135	125	140	125	130	125	140	130	125	145	135	135	140	145			
Force	Output (Fo)	(lbs)	600	200	650	750	600	600	200	200	650	200	200	200	800	200	200	200			
Force	Input (Fi)	(Ibs)	200	800	200	800	200	750	800	750	200	8,	750	200	750	800	750	092			
	Frequency	(cps)	2.50	2.50	2,60	2.70	2.85	3.00	3.00	3.20	3.30	3.50	3.50	3,80	3.90	4.00	4.00	4.00	 		

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### WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 120 Mil Peak-to-Peak

Remarks	Line Tension: 10,000 ths	Atta. Used																
<u>Δ0</u> Δĭ		.3660	.4000	1590	. 1200	.0547	.0540	.0540	.0540	.0150	.0150	.0070	.0070	0000 0000		. <u>17-14-1</u> -14-14		 
Fi Di		.994	. 913	.746	.746	.697	.697	.680	.662	-644	.657	.632	<u>4</u> 9.	.620				
Displacement Output (۵0)	(mil)	45	50	<b>5</b> 0.	15	7	7	4	5	2	2	g.m.	<b>C</b> ~~	0				
Displacement Irput (∆i)	(mil)	123	125	126	125	128	127	128	135	135	136	136	139	14				
Force Output (Fc)	(lbs)	980	980	802	814	11	11	750	77.	795	795	810	795	832	 		 	
Force Input (Fi)	(lbs)	1,100	1,128	940	940	893	893	870	833	870	893	870	833	893				
Frequency	(cps)	.00	00.1	1.50	1.50	2.00	2.00	2.50	2.50	3.00	3.00	3.50	3.50	4.00				

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### WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 130 Mil Peck-to-Peak

Remarks	Line Tension: 10,000 lbs	Attn. Used	LVUI		At .59 cps South LVDT Attn. changed	to .1,	Ali others remained the same.										
∆1 ∆1		1.965	1.550	5.000	5.530	5.660	1.060	.520	.640	.440	.320	.360		 			
Fi ∆i		.212	.488	3.650	2.930	3.070	1.230	1.240	1.015	.884	.827	.865					
Displacement Output (△0)	(mil)	155	210	725	830	850	130	65	80	55	۶0	45					
Displacement Input (∆i)	(mil)	133	135	145	150	150	125	125	125	125	125	125			 	 	
Force Output (Fo)	(lbs)	259	592	3,406	3,922	4,070	1,387	1,387	1,110	980	888	543		 	 		
Force Input (Fi)	(lbs)	282	638	3,854	4,394	4,606	1,540	1,551	1,269	1,104	1,034	1,081					
Frequency	(c.jse)	0.40	0.50	0.55	0.59	0.62	0.82	0.83	0.90	1.00	1.10	1.10	C 2000,000,000,000,000		 		

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Remarks	Line Tension: 10,000 lbs	Attn. Used														
∆i ∆i		1.280	2.190	5.140	5.560	6.230	2.880	1.12	.457	.417	.375	 				
<b>₽</b>		.263	.830	2.690	2.950	3.470	2.330	1.350	.940	.860	.860					
Displacentent Output (△o)	(mil)	160	285	720	805	860	360	140	55	Û <sup>©</sup>	45					
Displacement Input (Ai)	(mil)	125	130	140	145	i38	125	120	120	120	120					
Force Output (Fo)	(કવા)	277	962	3,330	3,737	4,292	2,590	1,443	980	925	\$0%				 	
Force Input (Fi)	(lbs)	329	1,081	3,760	4,277	4,794	5,514	1,622	1,128	1,034	1,034				 	
Frequency	(cps)	.425	.526	.570	009.	069.	.833	.833	000.1	1.050	1.080					

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TABLE X

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### WIRE ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 130 Mil Peak-to-Peak

TABLE XI

## SYNTHETIC ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 120 Mil Peuk-io-Peak

		الانكافات انوباد مردي اكرم كريم كيونا في بعد فكريم (عدار المحدود في المحدود).
Remarks	Line Tension: 11,300 lbs	Attn. Used LVDT .1 Load Cells .1
<u>Δ0</u>		
Fi ∆i		
Uisplacement Output (∆a)*	(ini i)	00000000
Dicplacement Input (∆i)	(mi!)	120 130 130 130 130 130 130 130 130 130 13
Force Output (Fo)*	(sql)	0000000
Force Input (Fi)*	(lbs)	0000000
Frequency	(cps)	۰. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵. ۵

\* The force and displacement r≈adings were below the resolution of the instrumentation. Therefore, these rendings were tabulated as zero.

	Remarks	Line Tension: 11,000 lbs	Attn. Used	1 VDT 2		road Cells																			
00	۵i		1	8	8	8	8	8	8.	8.	8	8	8	8.	8.	8.	8	8	8	8	8			فعيينا	
iE	Δi			.0495	.0495	.0495	.0483	.0483	.0483	.0483	.0483	.0483	.0483	.0483	.0483	.0483	.0477	.0477	.0477	.0470	.0477	-			
Displacement	Output (∆a)	(mil)		0	0	0	0	0	0	0	0	o	0	0	Q	0	0	0	0	0	0				
Displacement	Input (Ai)	(mil)		8	8	190	195	195	195	195	195	195	195	195	195	195	197	197	397	200	197				
Force	Output (Fo)	(lbs)		8	74	74	74	74	74	74	74	74	74	74	74	74	74	74	74	74	74				
Force	Input (Fi)	(sdl)		3	94	54	54	74	94	24	54	94	94	54 24	94 24	94	94 24	94	94 94	94	94				
	Frequency	(cps)		.40	.50	.55	09	.63	.63	.63	.63	.63	Ċ.B.	66	1.00	1.50	2.00	2.50	3.60	3.50	3.70		_		

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TABLE XIÎ

# SYNTHETIC ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 200 Mit Peak-ta-Peak

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# SYNTHETIC ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 200 Mii Peak-to-Peak

Remarks	Line Tension: 11,000 lbs	Attn. Used		Load Cell															
<u><u><u></u> <u> </u> <u> </u></u></u>		8	8.	8	8	8.	8	8	8	8	8	8	8	8.	8	8		 	 
Fi <u> </u>		.0477	.0477	.0477	047	.0477	.0477	.0477	.0477	.0477	.0470	.0457	.0457	.0447	.0447	.0437	 		 
Displacement Output (△↩)	(mil)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		 	
Displacement Input (∆i)	(mil)	197	197	197	197	197	197	197	197	167	200	205	205	210	210	215			
Force Output (Fn)	(lbs)	74	74	74	74	74	24	7	74	74	74	74	74	74	74	74			
Force Input (Fi)	(14-2)	94	76	94	54	94	94	54	54	84	64	54	64	94	8	94	 		
Frequency	(cps)	.40	.45	.50	.55	09.	.67	-69	.97	8.	1.50	2.00	2.50	3.00	3.50	3.80			

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Remarks	Line Tensian: 11,000 lbs	Attn. Used		Loog Lelis																
0 1 1 1 1		.217	.166	.123	8	ર્શ્ર	.050	090.	.050	050	.015	.015	.010	8.	8.	8	ŝ		 	
E I		.0470	.0470	.0470	0710.	.0470	.0463	.0463	.0463	.0463	.0463	S48.	.0463	1510.	.0444	1610.	.0427			
Displacement Output (20)	(mil)	65	50	37	20	20	15	15	15	15	S	ŝ	n	7	, <b>_</b>	0	0			
Displacement Input (∆i)	(mil)	300	300	300	300	80	305	305	305	305	305	305	305	310	317	325	330			
Force Output (Fo)	(jht)	111		111		111	111	111	111		115		111	111	111	1)1	111			
Force Input (Fi)	(ક્વા)	14]	141	141	343	141	14 2	141	141	141	141	141	141	141	141	141	143			
Frequency	(cps)	40	.43	.47	.56	.60	.62	.62	.63	.63	.94	1.00	1.50	2.00	2.50	3.00	3.50			~

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TABLE XIV

# SYN" IETIC ROPE DYNAMIC RESPONSE DATA

Excitation Displacement: 300 Mil Peak-to-Peak

	RESPONSE DATA
TABLE XV	DYNAMIC
	ROPE
	SYNTHETIC

Excitation Displacement: 300 Mil Peak-to-Peak

Remarks	Line Tension: 11,000 lbs	Altn. Used														
<u>40</u>		8	8	8	8	8.	8	8	8.	8.	8.	 				
Fi ∆1		0390	83.	.0470	.0470	23	.0455	.0447	1610.	.0427	.0422			 		
Displacement Output (Ao)	(mil)	0	ç	0	0	0	0	0	0	S	0					
Displacement Input (Ai)	(mit)	300	300	305	305	305	310	315	325	330	335					
Force Output (Fo)	(164)	2	6:	22	8	8	8	8	92	8	8		 	 		
Force Input (Fi)	(165)	112	141	14:		~	141	141		141	141	 		 		
Frequency	(cps)	08.	.54	0,	8	00.1	1.50	2.00	2.50	3.00	3.50		 			

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# SYNTHETIC ROPE DYNAMK, RESPONSE DATA

Excitution Displacement: 480 Mil Feakstu-Peuk

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Remarks	Line Tension: 11,000 lbs	Attn. Used	LVDT { South .2									 				
215		.3630	.2090	.1700	8 ?	88	0110	.0327	.0218	.0218	.0153		 		 	
নাত		.0620	7670	.0494	1610.	.0494	640.	.0488	,0488	0488	.0488					
Displacement Cutput (20)	(I))	165	55	7	45	27	20	15	0	0	~					
Displacement Input (AI)	(mil)	454	455	455	435	455	455	460	460	460	460		 	 		
Force Output (Fo)	(101)	284	2	148	.48	148	148	148	146	871	148				 	
Force Input (F1)	(Ibs)	696	235	233	235	235	235	235	235	235	235					
Frequency	(cps)	υ τ τ τ	0.44	0.46	0.55	0.64	0.73	0.85	0.93	0.93	1.00					

### TABLE XVII

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### WEIGHTS OF INDIVIDUAL MOVING COMPONENTS USED IN DYNAMIC RESPONSE TESTS

### Driving End

Weight and Basket	670 lbs	6 oz
Beam and Clevis	73 lbs	7 oz
Pillow Block Shaft	71 lbs	15 oz
LVDT Actuator Core	2 !bs	0 oz
Turnbuckle Assembly	21 lbs	3 oz

### Driven End

Weight and Basket	1,127 lbs	5 oz
Beam & Clevis	76 lbs	3 oz
Pillow Block Shaft	11 lbs	11 oz
LVDT Actuator Core	3 lbs	14 oz
Turnbuckle Assembly	21 lbs	12 oz
Wire Rope Test Sample with Fittings	171 lbs	7 oz
Synthetic Rope Test Sample Fittings	69 lbs	8 oz



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Fig. 3 Typical use of Cathometers to Measure Elongation. The Actual Test Setup is Shown in Fig. 2.







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LOAD-POUNDS

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Fig. 9 Ultimate Fracture for the Wire Rope Test Sample No. 3 Occurred at the Edge of Fitting.



Fig. 10 Ultimate Fracture of the Synthetic Rope Test Sumple No. 1 Occurred at the Junction of the Loop and the Long Length of Rope.



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Fig 13 Typical Result Showing the Absence of Kink Formations when the Load was Suddenly Released in the Rotation-Kink Test of the Wire Rope Samples.



Fig. 14 Typical Result Showing the Absence of Kink Formation when the Loads were Suddenly Released in the Rotation-Kink Test of the Synthetic Rope Samples.

*....* 



Fig. 15 Schematic of Driver End Test Setup



Fig. 16 Schematic of Driven End Test Setup



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![](_page_52_Figure_0.jpeg)

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### **APPENDIX A**

### DYNAMIC EFFECTS OF LEVER ARM RATIO

### Consideration :

In the ocean: a rope of undetermined length. The dampening effects of sea water were not considered.

The frequency is

$$\omega = \sqrt{\frac{K}{M}}$$
where  $K = \frac{T}{\delta}$  and  $\delta = \frac{TL_1}{AE}$ 
hence  $K = \frac{AE}{L_1}$ 
 $\therefore \omega = \sqrt{\frac{AE}{L_1M}}$ 
Let  $C = \sqrt{\frac{AE}{M}}$ 
then

$$\circ C \left[\frac{1}{L_1}\right]^{\frac{1}{2}}$$

Consideration II

In the laboratory. (Refer to Fig. 16.)

$$\omega = \frac{\alpha}{1} \sqrt{\frac{k}{m}}$$
  
where  $k = \frac{AE}{L_2}$ ;  $\frac{\alpha}{T} = \frac{1}{\frac{1}{\alpha}}$ ;  $\alpha < 1$ 

hence

تن

$$\omega = \frac{1}{\frac{1}{\sigma}} \sqrt{\frac{AE}{L_2m}}$$
$$= \sqrt{\frac{AE}{\left(\frac{1}{\sigma} L_2\right)\left(\frac{1}{\sigma} m\right)}}$$

To obtain the same loading in the laboratory as expected on the ocean rope, a pivoting beam was used with a force multiplier of 1.

a

 $M = \frac{i}{\sigma} m$ and  $C = \sqrt{\frac{AE}{M}}$ then

$$\omega = C \left[ \frac{1}{\frac{1}{2} L_2} \right]^{\frac{1}{2}}$$

It can be seen that the equivalent length of ocean rope to give the same frequencies as in the laboratory test, rope is  $\frac{1}{\sigma} \times L_2$ . This is equal to 15  $L_2$  so

that 115 feet of laboratory test rope simulated an ocean rope length of 1,725 feet.

A list of symbols.

- a = Beam lever arm length, short length.
- A = Cross sectional area of rope.
- $C = Constant \sqrt{\frac{AE}{M}}$
- E = Modulus of elasticity of rope.
- K = Spring constant of ocean rope.
- k = Spring constant of laboratory rope.
- I = Beam lever one length, long length.
- $L_1 = \text{Length of account rope}$ .
- $L_2 = \text{Length of laboratory rope.}$
- $M = Mass in ocean. = \frac{1}{n} (m)$
- m = Mass in laboratory.
- T = Rope tension.
- $\omega$  = Angular frequencies in radians per second.
- & = Elegation.

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Synthetic Rope						
Rotation						
Torque						
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