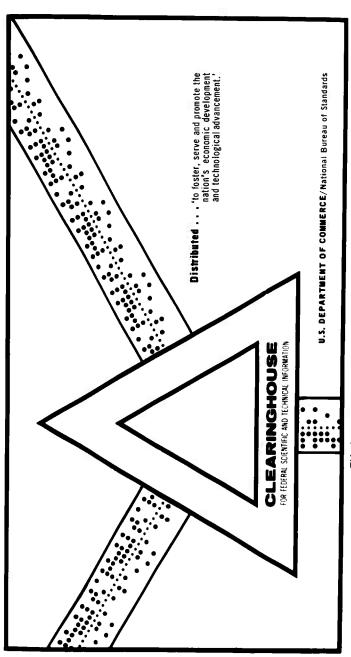
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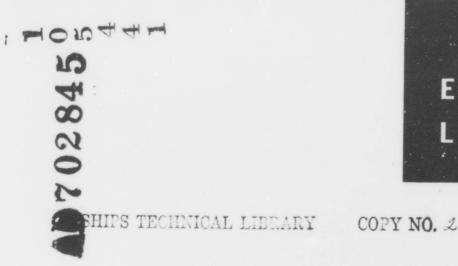
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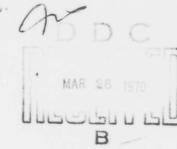
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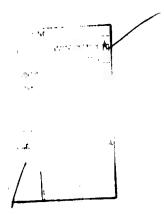
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	Maximum Temperature Vs. Unit Loading
31	39" O. D. x 19-1/2" I. D. Bearing - Hydrodynamic Oil Flow
32	41" O. D. x 20-1/2" I. D. Bearing at 100 RPM -
	Film Thickness Vs. Unit Loading
33	41" O. D. x 20-1/2" I. D. Bearing at 200 RPM -
	Film Thickness Vs. Unit Loading
34	41" O. D. x 20-1/2" I. D. Bearing at 100 RPM -
	Maximum Temperature Vs. Unit Loading
35	41" O.D. x 20-1/2" I.D. Bearing at 200 RPM
	Maximum Temperature Vs. Unit Loading
36	41" O. D. x 20-1/2" I. D. Bearing - Hydrodynamic Oil Flow
37	45" O. D. x 22-1/2" I. D. Bearing at 100 RPM
	Film Thickness Vs. Unit Loading
38	45" O. D. x 22-1/2" I. D. Bearing at \$70 RPM -
	Film Thickness Vs. Unit Loading
39	45" O. D. x 22-1/2" I. D. Bearing at 100 RPM -
	Maximum Temperature Vs. Unit Loading
40	45" O. D. x 22-1/2" I. D. Bearing at 170 RPM-
	Maximum Temperature Vs. Unit Loading
41	45" O. D. x 22-1/2" I. D. Bearing - Hydrodynamic Oil Flow
42	50" O. D. x 25" I. D. Bearing at 100 RPM -
	Film Thickness Vs. Unit Loading
43	50" O. D. x 25" I. D. Bearing at 170 RPM -
	Film Thickness Vs. Unit Loading
44	50" O. D. x 25" I. D. Bearing at 100 RPM -
4.5	Maximum Temperature Vs. Unit Loading
45	50" O. D. x 25" I. D. Bearing at 170 RPM -
44	Maximum Temperature Vs. Unit Loading
46	50" O. D. x 25" I. D. Bearing - Hydrodynamic Oil Flow

Figure	
Number	Caption
47	Groove Mixing Temperature
48	26" O. D. x 17-1/2" I. D. Bearing at 160 RPM -
	Film Thickness Vs. Unit Loading
49	26" O. D. x 17-1/2" I. D. Bearing at 160 RPM -
	Maximum Temperature Vs. Unit Loading
50	26" O. D. x 17-1/2" I. D. Bearing at 160 RPM -
	Hydrodynamic Oil Flow Vs Unit Loading .
51	31" O. D. x 16-1/2" I. D. Bearing at 320 RPM -
	Film Thickness Vs. Unit Loading
52	31" O. D. x 16-1/2" I. D. Bearing at 320 RPM -
	Maximum Temperature Vs Unit Loading
53	31" O. D. x 16-1/2" I. D. Bearing at 320 RPM -
- 4	Hydrodynamic Oil Flow Vs. Unit Loading
54	35" O. D. x 18-1/2" I. D. Bearing at 170 RPM -
55	Film Thickness Vs. Unit Loading
55	35" O. D. x 18-1/2" I. D. Bearing at 170 RPM - Maximum Temperature Vs. Unit Loading
56	35" O. D. x 18-1/2" I. D. Bearing at 170 RPM -
50	Hydrodynamic Oil Flow Vs. Unit Loading
57	$31''$ O, D, x 15-1/2" I, D, Bearing at 180 RPM, $T_{avg}/R = 0.130$
2.	Film Thickness Vs. Unit Loading
58	31" O. D. x 15-1/2" I. D. Bearing at 320 RPM, Tavg/R = 0, 130
-1 -1.	Film Thickness Vs. Unit Loading
59	31" O. D. x 15-1/2" I. D. Bearing at 180 RPM. T/R = 0, 130
	31" O. D. x 15-1/2" I. D. Bearing at 180 RPM, T <sub>avg</sub> /R = 0, 130 Maximum Temperature Vs. Unit Load
<b>ь0</b>	31" O. D. x 15-1/2" I. D. Bearing at 320 RPM, Tavg/R = 0, 130
	Maximum Temperature Vs. Unit Load
61	31" O. D. x 15-1/2" I. D. Bearing at 180 RPM, Tavg/R = 0, 193
	Film Thickness Vs. Unit Loading
62	31" O. D. x 15-1/2" I. D. Bearing at 320 RPM, Tavg/R = 0, 193
	Film Thickness Vs. Unit Loading 🚽
63	31" O. D. x 15-1/2" I. D. Bearing at 180 RPM, Tavg/R= 0, 193
	Maximum Temperature Vs. Unit Loading
64	31" O. D. x 15-1/2" I. D. Bearing at 320 RPM, Tavg/R = 0, 193
45	Maximum Temperature Vs. Unit Loading
65 66	31" O. D. x 15-1/2" I. D. Bearing - Hydrodynamic Oil Flow 31" O. D. x 15-1/2" I. D. Bearing at 180 RPM, r <sub>D</sub> % = 53
00	Sin O. D. x 15-1/2" I. D. Bearing at 160 KPM, r p = 53
67	Film Thickness Vs. Unit Loading 31" O. D. x 15-1/2" I. D. Bearing at 320 RPM, $r_p$ % = 53
01	Film Thickness Vs. Unit Loading
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Figure	
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### Caption

68	31" O. D x 15-1/2" I. D. Bearing at 180 RPM, rp% = 53
	Maximum Temperature Vs. Unit Loading
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	Maximum Temperature Vs. Unit Loading
70	31" O. D. x 15-1/2" I. D. Bearing at 180 RPM, r <sub>p</sub> % = 47
	Tilm Thiskness Vo. Unit I seding
71	Film Thickness Vs. Unit Loading
11	31" O. D. x 15-1/2" J. D. Bearing at 320 RPM, rp%= 47
	Film Thickness Vs. Unit Loading
72	31" O. D. x 15-1/2" I. D. Bearing at 180 RPM, rp% = 47
	Maximum Temperature Vs Unit Loading
73	31" O.D. x 15-1/2" I.D. Bearing at 320 RPM, rp% = 47
	Maximum Temperature Vs. Unit Loading
74	31" O. D. x 15-1/2" 1. D. Bearing - Hydrodynamic Oil Flow
75	31" O. D. x 15-1/2" I. D. Bearing, T <sub>GR</sub> = 130°F
	Minimum Film Thickness Vs. Unit Loading
76	31" O. D. x 15-1/2" I. D. Bearing, T <sub>GR</sub> = 130°F
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77	31" O. D. x 15-1/ I. D. Bearing. $T_{GR} = 130^{\circ}F$
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78	$39^{11} O D = 1/2^{11} I D Beaming T = 1300F$
10	39" O. D. x 19-1/2" I. D. Bearing, T <sub>GR</sub> = 130°F Minimum Film ThicknessVs. Unit Loading
79	39" O. D. x 19-1/2" J. D. Bearing, T <sub>GR</sub> : 130°F
• •	Maximum Temperature Vs. Unit Loading
80	$39''$ O. D. x 19-1/2'' I. D. Bearing, $T_{GR} = 130^{\circ}F$
•	Hydrodynamic Oil Flow Vs. Unit Loading
81	Bearing Size Vs. Unit Loading
82	51-1/2" O. D. x 32" I. D. Bearing at 200 RPM -
92	Si-1/2" O.D. X 52" I.D. Bearing at 200 RPM -
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87	Chart of Maximum and Average Temperatures
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Figure Number	Caption
91	Chart of Load Carrying Capacity, 8 pads, h <sub>min</sub> = 0.001"
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93	Chart of Load Carrying Capacity, 8 pads, hmin = 0,0006"
94	Chart of Load Carrying Capacity, 10 pads, hmin = 0.001"
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97	Chart of Hydrodynamic Oil Flow
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99	Location of point of Minimum Film Thickness
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#### BACKGROUND AND SCOPE

In 1958 the General Engineering Laboratory made a study of propeller shaft thrust bearing operation and reported its findings in Reference 1. Following this study a comprehensive analytical and experimental program was undertaken, for the purpose of extending present understanding of these bearings and in order to provide a body of design information for use in bearing design and selection. This program, like the preceding introductory study, is being performed under a contract awarded by the Bureau of Ships to General Electric Company's Medium Steam Turbine, Generator and Gear Department.

The program is divided into three phases as follows:

- Phase I:
   Investigate analytically the performance of propeller shaft thrust bearings using the existing Reynolds-Energy Method of solution to provide data necessary in design and selection of these bearings.
- Phase II: Extend existing analytical techniques for propeller shaft thrust bearings by including a numerical method of solution of the Elasticity Equation. Review, and where necessary, modify the design data obtained in Phase I, so as to include the effects of pad distortion caused by pressure distribution and thermal gradients.
- **Phase III:** Instrument thrust bearings on two U. S. Navy ships and obtain experimental data on the performance of these bearings. This data is to be obtained in tests carried out at the time of scheduled sea trials. The thrust bearing performance measurements obtained in these sea trials is to be used for correlation with the design data obtained analytically in Phases I and II.

A fourth phase which included the building of a thrust bearing test stand was contemplated but was not included in the present program, since the findings of the program could be used to determine the features of the stand.

The following is our final report on Phase I.

#### I INTRODUCTION

Virtually all ships in this country, both merchant and combat, use Kingsbury type tilting pad bearings to transmit the propeller thrust to the hull of the vessel. The geometry of these bearings and the principles on which they operate are well known and are described in most texts on lubrication as well as in the catalogues of Kingsbury Machine Works.

Generally, the bearing pads are centrally pivoted, i.e., the spherical pivot back of each pad is located mid-way between the leading and the trailing edges. Central pivot location is required for reversibility, i.e., for operation under either direction of shaft rotation.

Conventional bearing calculations in which temperature variations in the oil film are neglected and in which a converging wedge is formed by the tilting of a flat pad, fail to predict the load carrying capacity of centrally pivoted bearings. The reason for this is illustrated in Figure 1 (a) which shows the hydrodynamic pressure profile that is generated between flat surfaces separated by fluid film that converges slightly in the direction of motion. Under these conditions, calculations show that the resultant of the hydrodynamic pressures lies downstream of the radial centerline of the pad. Since the reaction to these pressures must pass through the pivot, a moment exists which tends to eliminate the convergence and hence load carrying capacity. However, when the temperature variations in the oil film and the deformation of the pad under load are considered in the analysis, the somewhat paradoxical result obtained above is eliminated. Calculations then show that there is a value of pad inclination (generally other than zero) for which the resultant of the hydrodynamic pressures passes through the central pivot as shown in Figure 1 (b).

As the oil flows through the bearing gap, its temperature rises due to the shearing of the film. This rise in temperature produces a "thermal wedge" action which accounts for part of the load carrying capacity of the bearing (provided that the viscosity and mass density of the lubricant decrease with temperature rise, which is the case for all known oils). Early in the program, calculations were made to determine the magnitude of the thermal wedge effect in a centrally pivoted finite pad. A sector shaped pad of a 31" 8-shoe bearing was analyzed, first with the pivot in optimum position and then with the pivot centrally located. In both cases, the pad was assumed to remain flat and the other operating conditions were:

> Speed - 320 RPM Minimum Film Thickness - 0.001" Oil - 2190T Oil Temperature at Pad Inlet - 130°F

The results are shown in Figures 2 (a) and 2 (b). It is seen that the thermal wedge effect allows the flat centrally pivoted pad to carry approximately 56% of the load carried by the pad with optimum pivot. At the same time, the maximum temperature reached with the flat centrally pivoted pads is 25°F higher than that reached in the pad with optimum pivot. Experience, however, suggests that the difference in performance between central and optimum pivot locations is not so severe. It was, therefore, decided at that time that, in order to make a more realistic analysis in Phase I, it should be extended to incorporate a simplified elasticity approach which allows pad deformation to be approximated and included in the calculation. Figure 2 (c) shows the load and maximum temperature of the 31" 8-shoe centrally pivoted bearing pad under the same operating conditions but with pad deformation included. Comparison of Figures 2 (a) and 2 (c) now show that the centrally pivoted pad is capable of carrying approximately 92% of the load carried by the flat pad with optimum pivot. Its maximum temperature is 6°F higher than that of the flat pad with optimum pivot. These results are in better agreement with experimental evidence and the method of analysis which includes a simplified elasticity solution has been used in all succeeding calculations.

(To the extent that pad deformation was included in the Phase I calculations the results presented in this report have anticipated those to be obtained in Phase II. In the latter phase, the Elasticity Equation is more rigorously sdved and includes, in addition, thermal deformation of the pad. However, it requires a considerably more elaborate digital computer program. It may be expected that comparison between the two sets of results will suggest modifications of the Phase I approach to yield a simple yet suffic.ently rigorous method of solution.)

The conflict between the isothermal, flat pad method of solution and experience with centrally pivoted pads has been realized, since the time that Albert Kingsbury accomplished his pioneering work on slider bearing performance (Ref. 2). More recently, interest in the effects of thermal wedge and of pad deformation has resulted in analytical studies of infinitely wide bearings, some of which are reported in References 3, 4 and 5. For the case of the finite bearings, the importance of including the effects of temperature variations in the oil film has been studied by one of the authors of this report and it is explained in Reference 6. To the best knowledge of the authors, the present report is the first published study of finite centrally pivoted pad bearings in which the effects of radial and tangential inclinations, temperature variations in the oil film, and pad deformation are all considered. The results obtained have shown good agreement with experience. They have indicated that pad deformations are of the order of the minimum film thicknesses and they have explained such test results as:

1. bearing failures caused by high pad temperatures.

- 2. occurrence of bearing failures in the vicinity of the pivot.
- 3. insensitivity of trailing edge film thicknesses at high loads.

In order to make the Phase I study as complete as possible, approximately 70% more cases were analyzed than were called for in the contract for this phase. In all, 262 operating points were calculated. At each operating point, the values of radial and tangential pad inclination which satisfied equilibrium of moments were obtained using a trial and error procedure. This procedure required an average of 5 solutions of the Reynolds and Energy Equations for each operating point, so that the total number of solutions exceeded 1300.

The studies were conducted as follows:

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- 1. Eight standard bearings were analyzed which scanned the range of present day propeller shaft bearing sizes (19" O. D. to 50" O. D.) and propeller speeds (100 R. P. M. to 320 R. P. M.). Each bearing was analyzed at two speeds and with 6, 8 and 10 pad geometries. Calculations were made at three values of minimum film thicknesses, at each speed and geometry. These calculations have yielded the value and location of the minimum film thickness, the temperature and pressure distributions, the oil flow and horsepower loss as functions of bearing size, number of pads, unit load and speed. In particular, they have shown the optimum number of pads as a function of bearing size, unit load and speed.
- 2. The ahead bearing of DD933 (U.S.S. Barry) was analyzed at the full speed ahead conditions. Its astern bearing was similarly analyzed at full speed astern condition. (The U.S.S. Barry was earlier selected by the Bureau of Ships to be the first ship for sea trial thrust bearing tests under Phase III of the program. The thrust bearings of the starboard shaft of this ship were instrumented and the tests at sea have just been completed.)
- 3. The ahead bearing of DL1 (U.S.S. Norfolk) was analyzed under full speed ahead operation. This bearing was selected for analysis because of the past history of several successive failures.
- 4. A 31" O. D. x 15-1/2" I. D. bearing was extensively analyzed in order to investigate the effects of pad thickness and radial pivot location on bearing performance.
- 5. A 31" O. D. x 15-1/2" I. D. and the 39" O. D. x 19-1/2" I. D. bearing were further analyzed to determine the effect of pad inlet oil temperature on bearing performance. In particular the effect of pad inlet temperature on load carrying capacity and maximum temperature were investigated.

- 6. Additional bearing sizes ranging up to 100" O.D. were analyzed to investigate the relationship between bearing size, pad thickness and unit loading.
- 7. A 51-1/2" O, D. x 32" I. D. bearing with 10 and 12 shoe geometries was analyzed at 200 R. P. M. and at 400 R. P. M. These analyses were made under separate contract with General Electric Company's Medium Steam Turbine, Generator and Gear Department who authorized their inclusion in the present report. They are of interest because the upper speed is quite high and the results illustrate some of the thrust bearing operating characteristics that will be encountered as propeller speeds are raised.

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#### II ANALYSIS AND METHOD OF CALCULATION

The important considerations in thrust bearing analysis are:

- 1. Pressure distribution and hence load carrying capacity
- 2. Temperature distribution
- 3. Location of the center of pressure
- 4. Oil flow
- 5. Horsepower loss

all as functions of the bearing geometry, film shape and speed.

In this section, the equations from which these quantities can be calculated are given. The film shape which includes the effects of pad inclinations and deformation is discussed, as are the groove mixing temperature and the viscositytemperature relation. Before proceeding to these, however, it is necessary to point out here the principal limitations of the analysis.

1. The analysis applies only to steady state conditions. It does not supply any information on the transient conditions that occur during start up and shut down. It also does not apply to dynamic load conditions (such as crash ahead and crash astern) when relative axial motion between the runner and the bearing introduces squeeze film effects.

2. Laminar conditions prevail in the oil film. Actually the Reynolds Number in present day propeller shaft thrust bearings is small enough for this condition to be satisfied under steady state operation. This is illustrated by the following calculation for an extreme case:

> D = 50" N = 320 RPM h = 0.002"  $\mu$  = 1 x 10<sup>-6</sup> lb. -sec /in. <sup>2</sup>  $\odot$  = 0.803 x 10<sup>-4</sup> lb. -sec. <sup>2</sup>/in.<sup>4</sup> U<sub>max</sub> = 840 in. /sec.

Reynolds Number (Maximum) = 
$$\frac{\rho U_{\text{max}} h}{\mu}$$
 = 135

3. Oil inertia effects are negligible. At the relatively low surface speeds of propeller shaft thrust bearings, this assumption too is quite valid.

4. The fluid is incompressible.

5. Variation of the specific heat of the oil with temperature are neglected.

#### A. <u>Reynolds and Energy Equations and Their Boundary Conditions</u>

The Reynolds Equation describes the hydrodynamic pressures generated in the oil film of a bearing. These pressures separate the bearing and runner surfaces when there is a relative motion between them. For a finite pad, the Reynolds Equation in polar coordinates is (Ref. 7):

$$\frac{\partial}{\partial r} \left( \frac{rh^3}{\mu} \frac{\partial p}{\partial r} \right) + \frac{\partial}{\partial r} \left( \frac{h^3}{\mu r} \frac{\partial p}{\partial \theta} \right) = 6 \omega r \frac{\partial h}{\partial \theta}$$
(1)

The boundary conditions that are needed for the solution of this equation arise from the fact that the pressure falls to zero at the pad perimeter.

With the coordinate system shown in Figure 3, the bandary conditions are then:

$$p = p = p = p = p = 0$$
(2)  
(r, 0) (R-L,  $\theta$ ) (r,  $\theta_{rr}$ ) (R,  $\theta$ )

Because the oil film may break down in diverging regions in the bearing, it is necessary to impose an additional condition which states that the pad pressures never fall below atmospheric.

In order to include in the analysis the effects of temperature (and hence viscosity) variations in the oil film, the Energy Equation has to be solved together with the Reynolds Equation. The Energy Equation can be written (Ref. 7):

$$\frac{\mu}{h}(\omega \mathbf{r})^{2} + \frac{\mathbf{h}^{3}}{12\mu} \left[ \frac{\partial \mathbf{p}}{\mathbf{r} \partial \theta}^{2} + \left( \frac{\partial \mathbf{p}}{\partial \mathbf{r}} \right)^{2} \right] - C_{\mathbf{p}} \rho \mathbf{g} \mathbf{J} \left[ \left( \frac{\mathbf{r} \,\omega \mathbf{h}}{2} - \frac{\mathbf{h}^{3}}{12\mu} - \frac{\partial \mathbf{p}}{\mathbf{r} \partial \theta} \right) \frac{\partial \mathbf{T}}{\mathbf{r} \partial \theta} - \frac{\mathbf{h}^{3}}{12\mu} - \frac{\partial \mathbf{p}}{\partial \mathbf{r}} \frac{\partial \mathbf{T}}{\partial \mathbf{r}} \right] = 0 \quad (3)$$

In Equation (3) it is assumed that the oil flow through the clearance space is adiabatic. All the heat generated within the fluid due to fluid shear is considered to be carried away by the mass transfer of the fluid and no heat is gained, or lost through the bearing surfaces. This is a comparatively good assumption, for the heat transfer coefficient at the fluid boundaries is very small. (Reference 8)

The boundary conditions used for the solution of Equation 3 are that

a) the pad inlet oil is at the groove temperature and

b) the radial temperature gradient is zero along the inner and outer circumferences to the pad because of the cooling effect of the surrounding oil. Thus:

$$T_{(\mathbf{r}, \mathbf{o})} = T_{\mathbf{GR}}$$

$$\left(\frac{\partial \mathbf{T}}{\partial \mathbf{r}}\right)_{(\mathbf{R}-\mathbf{L}-\mathbf{\theta})} = \left(\frac{\partial \mathbf{T}}{\partial \mathbf{r}}\right)_{(\mathbf{R}, -\mathbf{\theta})} = 0$$
(4)

With the introduction of the proper film shape, the solutions of Equations (1) and (3) yield the pressure and temperature distributions on the bearing pads.

#### B. Load Carrying Capacity

The total reaction of each bearing pad and hence the load it carries is given by the integral of the hydrodynamic pressures over the pad area. Thus:

$$\mathbf{W} = \int_{\mathbf{R}-\mathbf{L}}^{\mathbf{R}} \int_{0}^{\theta_{\mathrm{T}}} \mathbf{p} \mathbf{r} \, d\mathbf{r} \, d\theta \tag{5}$$

#### C. Oil Flow

Oil is introduced into each pad through the clearance space at its leading edge, by the motion of the runner. Part of this oil leaves the clearance space in the same manner from the trailing edge. The remaining part of the oil is forced out from all edges by the pressure gradients that are built up over the bearing surface. Referring to Figure 3, the oil flow (in G. P. M.) through the four edges is:

Flow into the pad:

$$\frac{231}{60} \quad \mathbf{Q}_{1} = \frac{\mathbf{R}}{\mathbf{R}-1} \left( \frac{\omega \mathbf{r} \mathbf{h}}{2} \right)_{\boldsymbol{\theta}=0} \quad \mathbf{d}\mathbf{r} = \frac{\mathbf{R}}{\mathbf{R}-1} \left( \frac{\mathbf{h}^{3}}{\mathbf{\mu} \mathbf{r}} - \frac{\partial \mathbf{p}}{\partial \theta} \right)_{\boldsymbol{\theta}=0} \quad \mathbf{d}\mathbf{r}$$
(6)

Flow out of the pad:

$$\frac{231}{60} \quad \mathbf{Q}_{2} = \int_{0}^{\mathbf{\theta}_{T}} \left( \begin{array}{c} \mathbf{h}^{3} \mathbf{r} & \underline{\partial} \mathbf{p} \\ \mathbf{\mu}^{\mathbf{\theta}} & \overline{\partial} \mathbf{r} \end{array} \right)_{\mathbf{r} = \mathbf{R} - \mathbf{L}} d\theta$$
(7)

$$\frac{231}{60} Q_{3} = \int_{R-L}^{R} \left(\frac{\omega rh}{2}\right)_{\theta=\theta_{T}} dr + \int_{R-L}^{R} \left(\frac{h^{3}}{\mu r} - \frac{\partial p}{\partial \theta}\right)_{\theta=\theta_{T}} dr$$
(7)  
$$\frac{231}{60} Q_{4} = \int_{0}^{\theta_{T}} \left(\frac{h^{3}r}{\mu} - \frac{\partial p}{\partial r}\right)_{r=R} d\theta$$

It is seen that the flow through the leading and trailing edges is made of two components. The first of these is independent of the pressure gradients and it is referred to as the "Shear Flow". The second component depends on the pressure gradients and it is referred to as the "Pressure Gradient Flow".

Since there is no relative radial motion between the runner and the bearing pads, there is only "Pressure Gradient Flow" out of the inner and outer circum-ferential boundaries of the bearing pads.

#### D. Horsepower Loss

It is assumed that all of the heat generated in the oil film goes into temperature rise of the oil. Thus, the horsepower loss can be computed from the oil flow through the bearing pads and its temperature rise. Thus:

$$HP_{2} = \frac{C_{p} \cap g}{0.707} \int_{0}^{\theta_{T}} \left[ \frac{h^{3}r}{\mu} \frac{\partial p}{\partial r} (T - T_{GR}) \right]_{r} d\theta$$

$$HP_{3} = \frac{C_{p} \cap g}{0.707} \left\{ \int_{R-L}^{R} \left[ \frac{\omega rh}{2} (T - T_{GR}) \right]_{\theta=\theta_{T}}^{\theta_{T}} dr + \int_{R-L}^{R} \frac{h^{3}}{\partial \theta} (T - T_{GR}) \frac{dr}{\theta=\theta_{T}} \right\}$$
(8)

$$HP_{4} = \frac{C_{p} fg}{0.707} \int_{0}^{0} \left[ \frac{h^{3}r}{\mu} \frac{\partial p}{\partial r} (T - T_{GR}) \right]_{r=R} d\theta$$

I the total horsepower loss per pad is

$$HP = HP_2 + HP_3 \quad HP_4 \tag{9}$$

#### E. Center of Pressure

The point on the pad surface through which the resultant of the hydrodynamic pressures acts is called the center of pressure. Its coordinates are given by:

$$\mathbf{r_{cp}} = \frac{\left\{ \begin{bmatrix} \mathbf{R} & \mathbf{\theta}_{\mathrm{T}} \\ \mathbf{R} - \mathbf{L} & \mathbf{0} \end{bmatrix}^{2} + \begin{bmatrix} \mathbf{R} & \mathbf{\theta}_{\mathrm{T}} \\ \mathbf{R} & \mathbf{p} & \mathbf{r}^{2} \sin \theta \, \mathrm{dr} \, \mathrm{d\theta} \end{bmatrix}^{2} \right\}^{1/2}}{\mathbf{W}}$$
  
$$\mathbf{\theta}_{cp} = \tan^{-1} \left\{ \begin{bmatrix} \mathbf{R} & \mathbf{\theta}_{\mathrm{T}} \\ \mathbf{R} & \mathbf{p} & \mathbf{r}^{2} \sin \theta \, \mathrm{dr} \, \mathrm{d\theta} \\ \mathbf{R} & \mathbf{p} & \mathbf{r}^{2} \sin \theta \, \mathrm{dr} \, \mathrm{d\theta} \\ \mathbf{R} & \mathbf{p} & \mathbf{r}^{2} \sin \theta \, \mathrm{dr} \, \mathrm{d\theta} \\ \mathbf{R} & \mathbf{p} & \mathbf{r}^{2} \cos \theta \, \mathrm{dr} \, \mathrm{d\theta} \\ \mathbf{R} & \mathbf{L} & \mathbf{0} \end{bmatrix} \right\}$$
(10)

#### F. Film Shape

Under the hydrodynamic pressures and the pivot reaction, each pad bends so that the bearing surface becomes slightly convex, as shown in Figure 1 (b). The shape that the pad assumes under load can be calculated from a solution of the Elasticity Equation and this is done in Phase II. For the present, however, it is assumed that the bearing surface becomes very slightly spherical. In accordance with plate theory, the bending deflections are taken to be proportional to load and inversely proportional to the pad thickness cubed. Since the pads are ball seated, they also tilt in both radial and tangential directions, till moment equilibrium is satisfied.

The film shape is then (see Appendix):

$$h = h_{a} + m_{\theta} \left[ r_{a} \sin \left( \theta_{a} - \frac{\theta_{T}}{2} \right) - r \sin \left( \theta - \frac{\theta_{T}}{2} \right) \right] - m_{r} \left[ r_{a} \cos \left( \theta_{a} - \frac{\theta_{T}}{2} \right) - r \cos \left( \theta - \frac{\theta_{T}}{2} \right) \right] + \frac{1}{2R_{c}} \left[ r^{2} - r_{a}^{2} - 2r r_{p} \cos \left( \theta - \theta_{p} \right) + 2r_{a} r_{p} \cos \left( \theta_{a} - \theta_{p} \right) \right]$$
(11)

For cases where loads are light and the bending deflections are small, it is convenient to use as reference, the point at the inside radius and trailing edge of the pad. Equation (11) then becomes (for a centrally pivoted pad):

$$h = h_{1} + m_{\theta} \left[ (R-L) \sin \frac{\theta_{T}}{2} - r \sin \left(\theta - \frac{\theta_{T}}{2}\right) - m_{r} \left[ (R-L) \cos \frac{\theta_{T}}{2} - r \cos \left(\theta - \frac{\theta_{T}}{2}\right) \right] + \frac{1}{2R_{c}} \left[ r^{2} - (R-L)^{2} + 2(R-L) r_{p} \cos \frac{\theta_{T}}{2} - 2 r r_{p} \cos \left(\theta - \frac{\theta_{T}}{2}\right) \right]$$
(12)

For cases where the loads are large and the bending deflections are of the same order as the minimum film th.ckness, the point of minimum film thickness may fall within the pad boundary. It is then more convenient to use this point as reference. Its coordinates can be obtained by differentiating Equation (11) and setting:

$$\frac{\partial h}{\partial r} = 0$$
 and  $\frac{\partial h}{\partial \theta} = 0$ 

The coordinates of the point of minimum film thickness are then found to be:

$$r_{m} = R_{c} \left[ m_{\theta}^{2} \left( \frac{r_{p}}{R_{c}} - m_{r} \right)^{2} \right]^{1/2}$$

$$\theta_{m} = \frac{\theta_{T}}{2} + \tan^{-1} \left( \frac{m_{\theta}}{r_{p}} - m_{r} \right)^{2} \right]$$
(13)

Substituting Equation (13) into Equation (11), the film thickness profile becomes (for a centrally pivoted pad):

$$h = h_{\min} + \frac{R_c}{2} \left[ m_{\theta}^2 + \left( \frac{r_p}{R_c} - m_r \right)^2 \right] + r \left[ m_{\theta} \sin \left( \theta - \frac{\theta_T}{2} \right) + \left( \frac{r_p}{R_c} - m_r \right) \cos \left( \theta - \frac{\theta_T}{2} \right) - \frac{r_c}{2R_c} \right]$$
(14)

In Equations 11 through 14 above,  $R_c$  is the radius of curvature of the bent pad. In the present analysis, it is calculated from the load and pad thickness (see Appendix) using the relation:

$$\frac{1}{2R_{c}} = 0.75 \times 10^{-8} \frac{W}{t^{3}avg}$$
(15)

where W is the load per pad

t<sub>avg</sub> is the mean thickness of the pad

#### G. Oil Groove Temperature

The temperature at which the oil enters the clearance space between the runner and the pads has an important effect on the load carrying capacity of the bearing. It is introduced in the analysis as one of the boundary conditions of Equation (3).

In general, the temperature of the oil in the feed grooves between the pads is several degrees higher than at the housing inlet ports. This difference is largely due to the mixing in each groove with hot oil discharged from the trailing edge of the downstream pad. It is, therefore, significantly affected by such factors as:

- a) quantity of oil admitted to the housing (this is generally several times the amount that flows through the clearance spaces.)
- b) extent of the grooves
- c) pad discharge temperature

In the Phase I calculations, the pad groove temperatures are obtained from the experimental data of several investigators. The experimental points are plotted in Figure 4 and a representative curve is drawn through them. This curve shows the feed groove temperature as a function of the unit load carried by the bearing, when the oil temperature at housing inlet is 115 F.

Figure 4 is, of course, an average curve. In the experimental work on which it is based, the oil flow through the bearing housing was four to five times the clearance flow and the total area of the grooves was 15% of the effective runner area.

Different values of these quantities or the location of major heat sources or sinks near the bearing housing would be expected to affect the groove temperature.

#### H. Viscosity-Temperature Relation

The viscosity-temperature relation of the lubricant is required in the simultaneous solution of Equations (1) and (3). In all the Phase I calculations, the lubricant properties used were those of 2190T oil.

The absolute viscosity versus temperature plot for 2190T oil is shown in Figure 5.

#### I. Numerical Solution of the Reynolds and Energy Equations

A finite difference procedure was used to solve the Reynolds and Energy Equations. These, however, were first put in dimensionless form (Equations A-2 and A-5 of the Appendix) in order to facilitate comparison between geometrically similar bearings.

The finite difference form of the dimensionless Reynolds and Energy Equations are given by Equations A-4 and A-7 of the Appendix. These are two sets of algebraic equations that can be solved on a digital computer using an iterative procedure. Their solutions yield the pressure and temperature profiles over the pad surface.

Figure 6 is a typical thrust bearing sector pad, divided into a mesh of  $m \ge n$  sections. Referring to Equation A-4 and Figure 6, it is seen that the dimensionless pressure  $\overline{p_{i,j}}$  at any point is expressed in terms of the corresponding dimensionless pressures, viscosities and film thicknesses. The boundary condition states that the pressure is zero around the periphery of the sector. In order to meet this condition, the pressures at fictitious image points outside the boundary are set equal in magnitude but opposite in sign to the pressures at the corresponding points inside the boundary. By employing a process of iteration the m  $\ge n$  equations represented by Equation A-4 are solved on the computer and the pressures  $\overline{p_{i,j}}$  are determined at each mesh centerpoint. The process of iteration is continued until the difference between successive values of the sum of the pressures converges to within a prescribed error. In this analysis, the error is specified to be less than 0.1%, i.e.

Error = 
$$\frac{\sum_{j=1}^{m} \sum_{i=1}^{n} \left[ \left( \overline{P}_{i, j} \right)_{k} - \left( \overline{P}_{i, j} \right)_{k-1} \right]}{\sum_{j=1}^{m} \sum_{i=1}^{n} \left( \overline{P}_{i, j} \right)_{k}} < 0.001 ... (16)$$

The load carrying capacity of a bearing is greatly influenced by the oil viscosity. The temperature (hence the viscosities) at each mesh point are obtained from the solution of Equation A-7 . The boundary conditions for this equation are introduced by setting: a) the temperature, along the inlet edge equal to the groove temperature and b) the temperatures at fictitious image points outside the inner and outer circumferential boundaries equal in magnitude and sign to those at the corresponding points inside the boundaries.

The steps for the simultaneous solution of the Reynolds and Energy Equation are then performed in the following manner:

- (1)The value of the film thickness at every point is determined.
- $\overline{P}_{i,j}$  is assumed equal to zero and the known value of inlet temperature (2)
- (3)
- (4)
- The values of  $\overline{T}_{i,j}$  are then determined at every point from equation A-7 The values of  $\overline{F}_{i,j}$  are calculated from values of  $\overline{T}_{i,j}$ . The values of  $\overline{P}_{i,j}$  are calculated from values of  $\overline{T}_{i,j}$ . Having the values of  $\overline{P}_{i,j}$ ,  $\overline{h}_{i,j}$ , and  $\overline{p}_{i,j}$ , the first approximation of the pressure field is determined from equation A-4 and improved several (5) times by iteration.
- The value of the pressure field thus obtained is used to recalculate the (6) temperature distribution from which a new set of  $\vec{F}_{i,j}$  values is determined.
- A second approximation of the pressure field is now obtained. This cycle (7) of pressure and temperature iterations is continued until the error, which is the difference between successive values of the pressure field, falls within the limit prescribed in equation 16.
- The final value of the pressure field is then used to compute the final (8) value of the temperature field.
- The total pad load, oil flow, horsepower loss and the coordinates of the (9) center of pressure are calculated by means of Equations A-8, A-10, A-15 and A-16.

#### Trial and Error Procedure for Pivoted Pad Bearings J.

At each operating point, the pad deformation has to be related to the pad load in accordance with Equation 15. The film shape which depends on this deformation and on the inclinations of the pad has to be such that the resulting center of pressure passes through the pivot. Finally, the groove temperature used has to be related to the unit loading in accordance with Figure 4. In order to meet these requirements, the following trial and error procedure was used:

- For the bearing geometry being studied, select a value of minimum film (1) thickness.
- Estimate the corresponding unit load and hence the groove temperature (2)  $(T_{GR})$  and the bending coefficient  $(K = 1/2R_{c})$ .
- Select values of radial and tangential inclinations (m, and m, respectively). (3)
- Introduce the above as input data and obtain the corresponding computer (4) solution.
- From the computer output data determine the coordinates of the center (5) of pressure and the actual unit load (and hence the actual groove temperature and bending coefficient). Check whether these agree with the estimated ones within the following error limits:

a) 
$$|(T_{GR})_{actual} - (T_{GR})_{estimatec}| \le 2^{\circ}F$$
  
b)  $|(K)_{actual} - (K)_{estimated}| \le 2 \times 10^{-6} \text{ in.}^{-1}$   
c)  $|r_{cp}\% - r_{p}\%| \le 0.5\%$   
d)  $|\theta_{cp}\% - \theta_{p}\%| \le 0.5\%$ 

If any of the conditions, a through d of Equation 17, are not satisfied. steps 2 through 5 are repeated until all errors are within the specified limits.

This procedure was found to require an average of 5 trial computer solutions for each operating point obtained.

#### K. Estimate of Errors

A 7 x 7 mesh was used in the numerical solution of the Reynolds and Energy Equations. This was the finest mesh fize that could be accommodated with an IBM 650 computer for the present program. Previous experience of the authors has indicated that satisfactory accuracy can be achieved with the 7 x 7 mesh, provided there are no sharp inflexion points in the film thickness profile. As an additional check, the calculations for one case were repeated on a larger computing machine, using a  $13 \times 13$  mesh. The results agreed with those obtained using the 7 x 7 mesh within 1%.

The error limits defined in Equation 17 were set up in order to limit the number of iterations required for each solution. On the basis of calculations carried out with smaller allowable errors, the effects of the limits set in Equation 17 are estimated to be:

Error in calculated maximum temperature  $\leq 5^{\circ}F$ Error in calculated minimum film thickness  $\leq 0.0001^{\circ\circ}$ 

In the calculation of the hydrodynamic oil flow and the horsepower loss, additional errors are introduced in the numerical calculation of the pressure gradients at the pad edges (see equations A-13 and A-15). Particularly at high loads, where the pad bending deflections are correspondingly large, errors in the calculated values of hydrodynamic oil flow and horsepower loss may be as high as 20%.

#### III RESULTS

 Eight bearings ranging in size from 19" to 50" diameter were analyzed, sach at two speeds in the range 100 to 320 RPM, These were:

BEARING SIZE (O, D, '' x L, D, '')	SPEEDS (RPM)		
<u>,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,</u>			
19 x 9-1/2	160 and 310		
25 x 12-1/2	120 and 240		
31 x 15-1/2	180 and 320		
$37 \times 18 - 1/2$	180 and 320		
39 x 19-1/2	150 and 200		
$41 \times 20 - 1/2$	100 and 200		
45 x 22-1/2	100 and 170		
50 x 25	100 and 170		

These bearings were all geometrically similar, with the following properties:

$\frac{\mathbf{L}}{\mathbf{R}} = \frac{1}{2}$	k = 0.85
$\frac{t_{avg}}{R} = 0.154$	r <sub>p</sub> % = 0 <sub>p</sub> % = 50

In all cases, 6, 8, and 10 pad geometries were analyzed. The results are given in Tables 1 through 8 and plotted in Figures 7 through 46.

 The ahead and astern bearings of the USS Barry (DD933) and the ahead bearing of the USS Norfolk (DL1) were studied at their full speed condition. These are:

	<b>SIZE</b> (O. D. " x L. D. ")	NUMBER OF PADS	SPEED (RPM)
Astern Bearing USS Barry*	26 x 17-1/2	8	160
Ahead Bearing USS Barry	$31 \times 16 - 1/2$	8	320
Ahead Bearing USS Norfolk	$35 \times 18 - 1/2$	8	170

The results are given in Tables 9 through 11 and plotted in Figures 48 through 56.

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\* In the case of the astern bearing of DD933, Figure 47 was used to determine  $T_{GR}$ . This is because the grooves between the pade of the bearing amounted to approximately 35% of the effective runner area, as compared with about 15% in the other bearings. In the absence of data for this size groove, Figure 47 was obtained from Figure 4, considering the groove temperature rise to be inversely proportional to the extent of the grooves 3. In order to estimate the effects of pad thickness, radial pivot location, groove temperature and bearing size, several additional calculations were made varying these parameters one at a time. The calculations were made for the following:

Bearing Size (O. D. x L. D.)	No. of Pads	Speeds (RPM)	tavg R	r <sub>p</sub> %	TGR
31 x 15-1/2	6, 8 and 10	180 and 320	0.130	50	Per Figure 4
$31 \times 15 - 1/2$	6, 8 and 10	180 and 320	0.193	50	Per Figure 4
$31 \times 15 - 1/2$	6, 8 and 10	180 and 320	0.154	53	Per Figure 4
$31 \times 15 - 1/2$	6, 8 and 10	180 and 320	0.154	47	Per Figure 4
$31 \times 15 - 1/2$	8	180 and 320	0.154	50	130°F
39 x 19-1/2	8	150 and 200	0.154	50	130°F
19 x 9-1/2	6, 8 and 10	100	0.154	50	Per Figure 4
75 x 37-1/2	6, 8 and 10	100	0.154	50	Per Figure 4
100 x 50	6, 8 and 10	100	0.154	50	Per Figure 4
19 x 9-1/2	6	100	0.130	50	Per Figure 4
45 x 27-1/2	6	100	0.130	50	Per Figure 4
75 x 37-1/2	6	100	0.130	50	Per Figure 4
100 x 50	. 6	100	0.130	50	Per Figure 4

The results are given in Tables 12 through 21 and plotted in Figures 57 through 81.

4. A 51-1/2" O. D. x 32" L D. bearing that was analyzed under separate contract with M. S. T. G. &G. Dept. has also been included in this report. The geometry and operating conditions were:

Bearing Size (O. D. x L. D. )	No. of Pads	Speeds (RPM)	t <sub>avg</sub> R	r <sub>p</sub> %	TGR
51-1/2 x 32					Per Figure 4

The results are given in Table 22 and plotted in Figures 82 through 86.

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#### IV DESIGN CHARTS

In order to facilitate design and selection of thrust bearings, where the outer diameter is roughly twice the inner diameter, the data in Tables 1 through 8 was used to arrive at a set of design charts. These are given in Figures 87 through 98. Note that in these charts (as in the other figures in this report) solid lines represent data within the range of calculations and dashed lines indicate extrapolated values.

When the oil film temperatures in Tables 1 through 8 are plotted, it is seen that both the maximum and the average temperatures are, with good accuracy, functions only of the unit load, number of shoes and pad inlet temperature. This allows the maximum and average temperature to be represented on a single chart, Figure 87. The accuracy of this chart, up to  $T_{max} = 235^{\circ}F$ , is  $\pm 5^{\circ}F$ . Above  $T_{max} = 235^{\circ}F$ , the accuracy is  $\pm 10^{\circ}F$ .

The minimum film thickness is a function of bearing size and speed as well as unit loading, number of shoes and pad inlet temperature. It is represented here as a function of these variables, in the set of nine charts, Figures 88 through 96. The accuracy of these charts is  $\ddagger 0.0001"$  within the calculated regions. In the extrapolated regions, 'errors may be somewhat larger.

The hydrodynamic oil flow per pad is plotted in Figure 97, as a function of

the dimensionless parameter  $\begin{pmatrix} \mathcal{U}_{avg} & \mathbf{U}_{avg} \\ \mathbf{p}_{avg} & \mathbf{B} \end{pmatrix}$  As was pointed out earlier, the oil

flow calculations are subject to significant error (in some cases as high as 20%), in part because of the numerical approximation of the pressure gradient at the pad edges. It is also necessary to keep in mind that the oil flow given by Figure 97 is only that which flows through the clearance spaces between the runner and the bearing pads. The total flow furnished to the bearing should be several times this quantity.

The friction horsevower loss per bad is plotted in Figure 93, also as a

function of the dimensionless parameter  $\begin{pmatrix} \mu & U \\ avg & avg \\ P & avg & B \end{pmatrix}$  This horsepower loss

is dependent on the calculated oil flow and is thus subject to the same errors. In addition, it should be noted that Figure 98 shows only the horsepower loss due to fluid shear in the oil film. There are additional losses in the bearing, such as those due to turbulence in the oil grooves. The example below illustrates the use of the charts.

Example: Compare the performance of 6 8 and 10 pad geometries for a 35'' O. D. x 17-1/2'' I. D. bearing at a speed of 280 RPM and a unit load of 650 psi. (Oil 2190T, k = 0.85 in all cases)

	6 Pad	8 Pad	10 Pad
p <sub>avg</sub> at h <sub>min</sub> = 0.0010" (Per Figures 88, 91 and 94)	528	520	453
$P_{avg}$ at $h_{min} = 0.0008''$ (Per Figures 89, 92 and 95)	623	663	620
Pavg at hmin = 0.0006" (Per Figures 90, 93 and 96)	745	832	815
$h_{min} at p_{avg} = 650 psi (by interpolation)$		0. 0082"	0. 0077"
T <sub>max</sub> at 650 psi (Per Figure 87) - <sup>0</sup> F	237	215	207
T <sub>avg</sub> at 650 psi (Per Figure 87) - <sup>O</sup> F	185	185	184
Mavg (Per Figure 5)	1.8x10-6	1.8x10-6	1.8x10-6
$U_{avg} = 2\pi (\mathbf{R} - \mathbf{L}/2) \mathbf{N} - in/sec$	385	385	385
B = (R - L/2) $\theta_{T}$ = (R - L/2) $\frac{2k\pi}{n}$ - in.	11.7	8.76	7.01
$\left(\frac{\mathcal{U}_{avg} U_{avg}}{P_{avg} B}\right) \times 10^{6}$	0. 091	Q 122	0.152
$\left(\frac{Q}{B L U_{avg}}\right) \times 10^6$ (Per Figure 97)	24.9	24.7	24.6
Q GPM	0.98	0.73	0, 58
$Q_{tot}$ GPM (= n x Q)	5.9	5.8	5.8
f x 10 <sup>3</sup> (Per Figure 98)	0.97	1.01	1.12
$HP = \frac{f B L p_{avg} U_{avg}}{6600}$	3.77	2. 94	2.61
HP <sub>tot</sub> (= n x HP)	22.6	23.5	26.1

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#### V DISCUSSION AND CONCLUSIONS

1. The two principal criteria of thrust bearing performatice are the minimum film thickness and the maximum temperature. The present analysis, which was limited to 6, 8 and 10 pad bearings, showed that:

a) For each condition of operation (bearing size, load and speed), there is an optimum number of pads, from the standpoint of minimum film thickness. This can be seen by comparing the design charts, Figures 88 through 96.

b) The maximum temperature can be decreased by increasing the number of pads in the bearing. This gain is greatest in the critical high load regions as shown in Figure 87.

Note also from Figure 87 that the maximum temperature is a very sensitive indicator of bearing load. This is in contrast to the oil temperature which is little influenced by load changes.

2. At low loads, the minimum film thickness occurs at the inside radius of the trailing edge. However, as the bearing load (and hence the pad deformation) increases, the point of minimum film thickness moves toward the pivot, as shown in Figure 99. This figure shows that the radial location of the point of minimum film thickness moves quite rapidly towards the center region of the pad. It can be concluded from this that failures which result from small dirt particles in the oil film are most likely to occur near the pivot. This is borne out by experience.

Figure 99 also shows that the location of the point of minimum film thickness is dependent on the pad subtended angle. Thus, it moves inward from the trailing edge most rapidly in the case of the 6 pad bearing.

The marked divergence, at high loads, between the minimum film thickness and the film thickness at the inside radius of the trailing edge is also shown in Figure 100. In fact this figure shows that at high loads, the film thickness at the inside radius of the trailing edge becomes almost insensitive to load changes.

- 3. The effect of pad thickness is illustrated in Figures 101. Note that there is an optimum pad thickness at each specific load, from both the standpoints of minimum film thickness and maximum temperature. At low loads, thinner pads are preferable for the deformation there allows a more favorable film shape. At high loads, on the other hand, deformations become excessive and reduce load carrying capacity.
- 4. Since propeller shaft bearings are required to operate under either direction of rotation, the pivot location can be varied only radially. Figure 102 shows the effect of radial pivot location on minimum film thickness and maximum temperature, for several values of unit loading. Both these sets of curves indicate that there is an optimum pivot location, that varies with unit loading. The optimum locations obtained from the two sets of curves are, however, different. Thus, from the standpoint of minimum film thickness, the optimum pivot location approaches the mean radius from the outer circumference, as the unit loading increases. From the standpoint of maximum temperature on the other hand, the optimum pivot location approaches the mean radius from the inner circumference, also as the unit load increases.
- 5. The groove mixing temperature plays a very important role in bearing performance. Figure 103 shows the reduction in load carrying capacity that accompanies a rise in the groove temperature. This reduction is a major one, as indicated in the following table (obtained from Figure 103):

<sup>h</sup> min "	<sup>T</sup> GR <sup>°F</sup>	P <sub>avg</sub> psi	T oF max
0.0006	130	1030	220
0.0006	158	800	235

Thus, for a constant minimum film thickness, a reduction of  $28^{\circ}$ F in groove temperature achieves an increase of 28% in unit load, together with a reduction of  $15^{\circ}$ F in the maximum temperature.

- 6. For a geometrically similar series of bearings, the unit loading will increase with bearing size (at a given angular speed and minimum film thickness) as shown, for example, in Figure 81. This is of course due to the higher surface speed of the larger bearings. Note however, that the slope of the curve decreases quite rapidly due to the rise in groove mixing temperature and bending deflections. This points up again the importance of these two factors on bearing performance.
- 7. Early in this report, it was pointed out that the inclusion of thermal wedge and pad bending in the analysis explains the load carrying capacity of centrally pivoted pads. The load carrying capacities of a flat pad bearing with optimum pivot location and of a centrally pivoted pad were then compared in Figure 2, for a particular pad geometry. It should be noted, however, that the hydrodynamic pressure profiles differ markedly in the two cases, as shown in Figure 104.
- 8. In the present analysis, heat conduction was neglected. Thus, the calculated maximum film temperatures are somewhat higher than those which occur in practice. (The calculated values are therefore conservative.) Furthermore, whereas the calculated maximum temperatures are at the trailing edge, in practice they will occur at a small distance inward, also because of conduction.

#### V. RECOMMENDATIONS

- 1. The simplified analysis that was used here has shown that several aspects of bearing geometry, such as number of pads, pad thickness and radial pivot location, have a significant effect on load carrying capacity. The effect of number of pads was studied for a large range of bearing cizes. The effects of the other factors were studied for a 31" O. D. x 15-1/2" I. D. bearing. It is desirable to:
  - a) Verify the results using a more rigorous elasticity analysis (as is being done in Phase II).
  - b) Extend the results obtained to bearings with different L/R ratios.
  - Obtain experimental verification (PhaseIII and contemplated thrust bearing test machine.)
- 2. Groove mixing temperature plays a very important role in determining the load carrying capacity of thrust bearings. Gains in load capacity on the order of 25% can be achieved if mixing in the grooves can be inhibited, thus lowering the pad inlet temperature of the oil. This suggests an investigation aimed at developing suitable baffles in the oil grooves which would reduce the carry over of hot oil from the downstream pad. (A reduction in the di temperature at housing inlets also serves to improve performance.)
- 3. The major importance of pad geometry and groove mixing temperature on bearing performance indicate that design modifications can be made to greatly increase the load carrying capacity of tilting pad bearings. In such designs, consideration should be given to multi-point supports and to shaped pad surfaces as well as to the other aspects of bearing geometry studied in this report. Advantage should also be taken of the elasticity of the pads in optimizing the bearing design.
- 4. The present analysis was limited to steady state conditions. Analytical and experimental investigations are necessary in order to arrive at means of predicting bearing performance under transient conditions, such as acceleration, crash maneuvers, start up under load (as in a submerged submarine) and others.
- 5. Metallurgical work is badly needed to-day to set up operating temperature limits of the various babbitts in use as well as to develop alternative materials.

- 6. In future analytical work, the effect of thermal conduction should be studied.
- 7. The extent of misalignment present in thrust bearing installations on board ship needs to be investigated. In parallel with this, the degree of load equalization between pads and the load carrying capacity of the bearings under misalignment should be analyzed.

APPENDIX

#### APPENDIX

#### 1. Finite Difference Equations

The numerical solution of the Reynolds and Energy Equations by means of finite differences is described in Reference 11. Here a brief outline of the procedure is given.

For convenience of comparison between geometrically similar pads, the Reynolds and Energy Equations are first put in dimensionless form.

Let 
$$\mathbf{r} = \mathbf{R} \cdot \mathbf{\bar{r}}$$
  
 $\mathbf{h} = \mathbf{h}_{\mathbf{a}} \cdot \mathbf{\bar{h}}$   $\mathbf{p} = 12 \text{ W} \cdot \mathbf{N}' \mathcal{A}_{\mathbf{GR}} \cdot \mathbf{\bar{p}} \left[ \text{where } \mathbf{N}' = \frac{\mathbf{R}}{\mathbf{h}_{\mathbf{a}}} \cdot \mathbf{N} \right]$   
 $\theta = \overline{\theta}$   
 $\mathcal{A} = \mathcal{A}_{\mathbf{GR}} \cdot \mathbf{W}$   $\mathbf{T} = \frac{12 \text{ W} \cdot \mathbf{N}' \mathcal{A}_{\mathbf{GR}}}{\rho \text{ g} \text{ J} \cdot \mathbf{C}_{\mathbf{p}}} \cdot \mathbf{\bar{T}}$  (A-1)

Introducing Equation (A-1) into Equation (1) of the text, we obtain the Reynolds Equation in dimensionless form:

$$\frac{\partial}{\partial \overline{r}} \left( \frac{\overline{rh^3}}{\overline{\mu}} \frac{\partial \overline{r}}{\partial \overline{r}} \right) + \frac{\partial}{\overline{r} \partial \overline{\theta}} \left( \frac{\overline{h^3}}{\overline{\mu}} \frac{\partial \overline{p}}{\partial \overline{\theta}} \right) - \frac{\overline{r} \partial \overline{h}}{\partial \overline{\theta}} = 0 \qquad (A-2)$$

Referring to Figure 6, we can write

$$\frac{\partial}{\partial \overline{r}} \left( \frac{\overline{rh}^{3}}{\overline{\mu}} \frac{\partial \overline{p}}{\partial \overline{r}} \right) = \frac{\frac{\overline{rh}^{3}}{\overline{\mu}} \Big|_{i+1/2, j} \left( \frac{\overline{p}_{i+1, j} - \overline{p}_{i, j}}{\overline{\Delta \overline{r}}} \right) - \frac{\overline{rh}^{3}}{\overline{\mu}} \Big|_{i-1/2, j} \left( \frac{\overline{p}_{i, j} - \overline{p}_{i-1, j}}{\overline{\Delta \overline{r}}} \right) \\ \frac{\partial}{\partial \overline{r}} \left( \frac{\overline{h}^{3}}{\overline{\rho}} \frac{\partial \overline{p}}{\partial \overline{r}} \right) = \frac{\frac{\overline{h}^{3}}{\overline{\mu}} \Big|_{i, j+1/2} \left( \frac{\overline{p}_{i, j+1} - \overline{p}_{i, j}}{\overline{\Delta \overline{\theta}}} \right) - \frac{\overline{h}^{2}}{\overline{\mu}} \Big|_{i, j-1/2} \left( \frac{\overline{p}_{i, j} - \overline{p}_{i, j-1, j}}{\overline{\Delta \overline{\theta}}} \right)$$

$$(A-3)$$

$$\frac{\overline{\rho}}{\overline{\rho}} = \frac{\overline{r}_{i, j} \left( \overline{h}_{i, j+1/2} - \overline{h}_{i, j-1/2} \right)}{\overline{\Delta \overline{\theta}}}$$

And, introducing Equation (A-3) into Equation (A-2) and solving for  $\overline{P}_{i,j}$  we obtain

$$\overline{P}_{i,j} = \frac{\left(\frac{\overline{rh}^{3}}{\mu}\right)_{i+1/2,j} \left(\frac{\overline{p}_{1+1,j}}{\Delta T^{2}}\right) + \left(\frac{\overline{rh}^{3}}{\mu}\right)_{i-1/2,j} \left(\frac{\overline{p}_{1-1,j}}{\Delta T^{2}}\right) + \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} \left(\frac{\overline{h}^{3}}{\Delta T^{2}}\right) + \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} \left(\frac{\overline{h}^{3}}{\Delta T^{2}}\right) + \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\Delta T^{2}}\right) + \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\Delta T^{2}}\right) + \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i+1/2,j} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i+1/2,j} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i-1/2,j} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j+1/2} + \frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left(\frac{\overline{h}^{3}}{\mu}\right)_{i,j-1/2} \left$$

Similarly, from Equations (A-1) and Equation (2) of the text, we obtain the Energy Equation in dimensionless form:

$$\frac{\overline{\mu r}^{2}}{3\overline{h}} + \frac{\overline{h}^{3}}{\overline{\mu}} \left[ \left( \frac{\overline{c}\overline{\rho}}{r\partial \theta} \right)^{2} + \left( \frac{\partial\overline{p}}{\partial\overline{r}} \right)^{2} \right]^{2} = \left[ \overline{h} - \frac{\overline{h}^{2}}{\overline{\mu r}} \frac{\partial\overline{p}}{\partial\theta} \right] \frac{\partial\overline{T}}{\partial\overline{\theta}} - \left( \frac{\overline{h}^{2}}{\overline{\mu}} \frac{\partial\overline{p}}{\partial\overline{r}} \right) \frac{\partial\overline{T}}{\partial\overline{r}}$$
(A-5)

Referring to Figure 6, the above equation can be reduced to a difference equation:

$$\frac{\mu \overline{r}^{2}}{3\overline{n}}\Big|_{i,j} + \frac{\overline{h}^{3}}{\mu}\Big|_{i,j} \left[ \left( \frac{\overline{P}_{i,j+1} - \overline{P}_{i,j-1}}{2\overline{r}\Delta \theta} \right)^{2} + \left( \frac{\overline{P}_{i+1,j} - \overline{P}_{i-1,j}}{2\Delta \overline{r}} \right)^{2} \right]$$

$$= \left[ \overline{h} \Big|_{i,j} - \frac{\overline{h}^{3}}{\mu \overline{r}}^{2} \Big|_{i,j} \frac{\overline{P}_{i,j+1} - \overline{P}_{i,j-1}}{2\Delta \theta} \right] \frac{\overline{T}_{i,j+1} - \overline{T}_{i,j-1}}{2\Delta \theta}$$

$$- \frac{\overline{h}}{\mu}\Big|_{i,j} \left( \frac{\overline{P}_{i+1,j} - \overline{P}_{i-1,j}}{2\Delta \overline{r}} \right) \left( \frac{\overline{T}_{i+1,j} - \overline{T}_{i-1,j}}{2\Delta \overline{r}} \right)$$
(A-6)

Now solving for  $\widetilde{T}_{i, j+1}$ , we obtain

$$\begin{split} \overline{T}_{1,j+1} &= \frac{2\overline{\Delta\theta} \left[ \frac{\overline{\mu_{1}} z^{2}}{3h} \Big|_{1,1} + \frac{\overline{h}^{2}}{\mu} \Big|_{1,1} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\theta}} \right)^{2} + \left( \frac{\overline{p}_{1+1,1} - \overline{p}_{1-1,1}}{2\overline{\lambda}} \right)^{2} \right)}{\left[ \overline{h} \Big|_{1,j} - \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\theta}} \right) \right]} \quad (A-7) \\ &+ \frac{+ \frac{\overline{h}^{2}}{\mu} \Big|_{1,1} \left( \frac{\overline{p}_{1+1,1} - \overline{p}_{1-1,1}}{2\overline{\lambda\overline{x}}} \right) \left( \frac{\overline{1}_{1+1,1} - \overline{1}_{1-1,1}}{2\overline{\lambda\overline{x}}} \right) + \left\{ \overline{h} \Big|_{1,1} - \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{x}}} \right) \right] \\ &- \frac{- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,1} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1-1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1-1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1-1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1-1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{p}_{1,1+1} - \overline{p}_{1,1-1}}{2\overline{\lambda\overline{y}}} \right) \right] \frac{\overline{1}_{1,1}}{2\overline{\lambda\overline{y}}} \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \right) \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \Big|_{1,j} \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \right) \right) \right] \\ &- \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \right) \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \Big|_{1,j} \left( \frac{\overline{h}^{2}}{\mu \overline{x}} \Big|_{1,j} \right) \right) \right]$$

.

The pressure and temperature profiles are obtained by the numerical solution of the two sets of  $E_1$ uations(A-4) and(A-7) using the iterative procedure described on Page 13.

The load carried by each bearing pad (Equation 5 of the text) is obtained by a numerical integration of the pressure field over the pad surface.

$$\overline{\mathbf{w}} = \Delta \ \overline{\mathbf{\theta}} \ \Delta \ \overline{\mathbf{r}} \quad \sum_{j=i}^{m} \sum_{i=1}^{n} (\overline{\mathbf{p}}_{i,j})_{\mathbf{k}} \ \overline{\mathbf{r}}_{i,j} \qquad (A-8)$$

The oil flow out of each pad is given in Equations 7 of the text. In order to generalize the solutions, a dimensionless factor is used:

$$\overline{\mathbf{Q}} = \frac{231 \, \mathbf{Q}}{60 \, \mathrm{Tr} \, \mathrm{NRL} \, \mathrm{h}_{\mathrm{A}}} \tag{A-9}$$

Equations (A-1) and (A-9) are introduced into Equation 7 and four point approximations are used for the pressure gradients at the pad edges (Reference 12). Noting that the pressure is zero along the edges, the numerical form of the flow equations becomes:

$$\begin{split} \overline{Q}_{2} &= \frac{R}{L} \frac{\bigtriangleup \overline{\theta}}{\bigtriangleup r} \sum_{j=1}^{m} (\frac{\overline{h}^{3}}{\varkappa \overline{r}})_{1/2, j} (3, 000 \ \overline{p}_{1, j} - 1, 500 \ \overline{p}_{1-1/2, j} + 0, 333 \ \overline{p}_{2, j}) \\ \overline{Q}_{3} &= \frac{F}{L} \bigtriangleup \overline{r} - \sum_{i=1}^{n} (\overline{r} \ \overline{h})_{i, m+1/2} \\ &+ \frac{R}{L} - \frac{\bigtriangleup r}{\bigtriangleup \overline{\theta}} - \sum_{i=1}^{n} (\overline{r} \ \overline{h})_{i, m+1/2} (3, 000 \ \overline{p}_{i, m} - 1, 500 \ \overline{p}_{i, m-1/2} + 0, 333 \ \overline{p}_{1, m-1}) \\ &+ \frac{R}{L} - \frac{\bigtriangleup r}{\bigtriangleup \overline{\theta}} - \sum_{i=1}^{n} (\frac{\overline{h}^{3}}{\varkappa \overline{r}})_{i, m+1/2} (3, 000 \ \overline{p}_{i, m} - 1, 500 \ \overline{p}_{i, m-1/2} + 0, 333 \ \overline{p}_{1, m-1}) \\ &\overline{Q}_{4} &= \frac{R}{L} - \frac{\bigtriangleup \theta}{\bigtriangleup \overline{r}} - \sum_{j=1}^{m} (\frac{\overline{h}^{3}}{\varkappa \overline{r}})_{n+1/2, j} (3, 000 \ \overline{p}_{n, j} - 1, 500 \ \overline{p}_{n-1/2} + Q_{133} \ \overline{p}_{n-1, j}) \end{split}$$

The total flow out of the bearing is given by

$$\bar{\mathbf{Q}} = \bar{\mathbf{Q}}_2 + \bar{\mathbf{Q}}_3 + \bar{\mathbf{Q}}_4 \tag{A-11}$$

The horsepower loss by fluid shear in each bearing pad was written in Equation 8 of the text in the form

$$HP = \frac{231}{60} \times \frac{C_p \rho g}{0.707} \times Q \triangle T$$
 (A-12)

In dimensionless form this is:

$$\overline{HP} = \overline{Q} \ \triangle \overline{\Gamma} \tag{A-13}$$

where, from Equations (A-1), (A-9) and (A-12):

$$\overline{HP} = \frac{0.707}{12 \pi^2} \frac{J h_a}{N^2 R^3 \mu_{GR} L}$$
(A-14)

In numerical form the horsepower loss is then given by:

$$\overline{HP}_{2} = \frac{R}{L} \frac{\Delta \overline{\theta}}{\Delta \overline{r}} \sum_{j=1}^{m} (\frac{\overline{h}^{3}}{\mu \overline{r}})_{1/2, j}^{n} (3.000 \, \overline{P}_{i, j} - 1.500 \, \overline{P}_{1-1/2, j}^{n} + 0.333 \, \overline{P}_{2, j}^{n}) (\overline{T}_{1/2, j}^{-T} \, GR)$$

$$\overline{HP}_{3} = \frac{R}{L} \Delta \overline{r} \sum_{i=1}^{n} (\overline{r} \, \overline{h})_{i, m+1/2} (\overline{T}_{i, m+1/2}^{-} \, \overline{T}_{GR}^{n})$$

$$+ \frac{R}{L} \frac{\Delta \overline{r}}{\Delta \overline{\theta}} \sum_{i=1}^{n} (\frac{\overline{h}^{3}}{\mu \overline{r}})_{i, m+1/2} (3.000 \, \overline{p}_{i, m}^{-} - 1.500 \, \overline{p}_{i, m-1/2}^{+0.333 \, \overline{p}}_{i, m-1}) (\overline{T}_{i, m+1/2}^{-} \, \overline{T}_{GR}^{n})$$

$$(A-15)$$

$$\widetilde{HP}_{4} = \frac{R}{L} \frac{\angle \widetilde{\theta}}{\angle \widetilde{r}} \sum_{j=1}^{m} \frac{\widetilde{h}^{3}}{\sqrt{r}} \Big|_{n+1/2, j} (3.000 \widetilde{p}_{n, j} - 1.500 \widetilde{p}_{n-1/2} + 0.333 \widetilde{p}_{n-1, j}) (\widetilde{T}_{n+1/2, j} - \widetilde{T}_{GR})$$

and the total horsepower loss in each bearing pad is:

# $\overline{HP}$ = $\overline{HP}_2$ + $\overline{HP}_3$ + $\overline{HP}_4$

The equations for the center of pressure (Equations 10 of the text) are in numerical form:

$$\frac{\Delta \theta \Delta \overline{r} \sum_{j=1}^{m} \sum_{i=1}^{n} r_{i,j}^{2} \sin \theta_{i,j} (\overline{p}_{i,j})_{k}}{W}$$

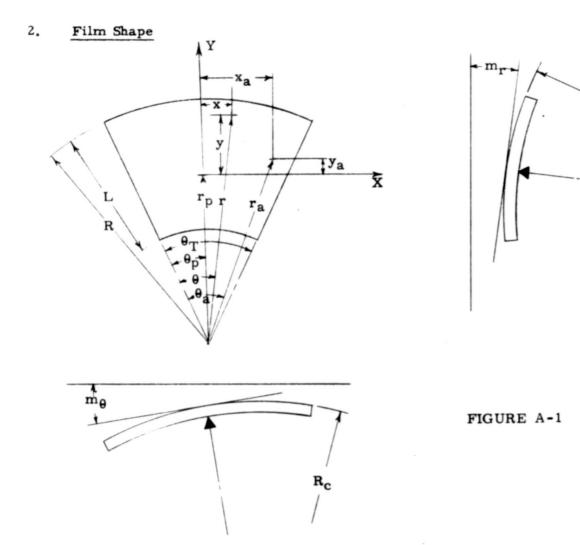
$$W \qquad (A-16)$$

$$W = \frac{\Delta \theta \Delta \overline{r} \sum \overline{r}_{i,j}^{2} \cos \overline{\theta}_{i,j} \overline{p}_{i,j})_{k}}{W}$$

$$V = \frac{W}{W}$$

$$V = r_{p}\% = 10. \left\{ 1 - \frac{R}{L+1} + (\overline{x}^{2} + \overline{y}^{2}) \right]^{\frac{1}{2}}$$

$$H = \frac{100 \tan^{-1} (\overline{x}/\overline{y})}{\theta_{T}} \qquad (A-17)$$



We consider that the convex shape to which the pad bends under load may be represented by part of a spherical surface whose radius of curvature is  $R_c$ , as shown in Figure A-1. In all cases considered here,  $R_c$  is very large, greater than  $10^4$ inches. In addition, the pad inclines, so that its tangent plane directly above the pivot point has slopes  $m_{\theta}$  (circumferentially) and  $m_r$  (radially), with respect to the plane of the runner, as shown in Figure A-1. The pad inclinations are small so that

```
\sin m_{\theta} = \tan m_{\theta} = m_{\theta}
\cos m_{\theta} = 1
\sin m_{r} = \tan m_{r} = m_{r}
\cos m_{r} = 1
(A-18)
```

Rc

Let the film thickness at a reference point  $(x_a, y_a)$  on the pad surface be  $h_a$ . The film thickness at any other point (x, y) can ther be written:

$$h = h_{a} - m_{\theta} (x - x_{a}) + m_{r} (y - y_{a}) + R_{c} \left[ \left( 1 - \frac{x_{a}^{2} + y_{a}^{2}}{R_{c}^{2}} \right)^{\frac{1}{2}} - \left( 1 - \frac{x^{2} + y^{2}}{R_{c}^{2}} \right)^{\frac{1}{2}} \right]$$
(A-19)

Since  $R_c$  is very large, powers of the ratio  $\left(\frac{r^2}{R_c^2}\right)$  are neglected. Equation (A-19) then becomes:

$$h = h_{a} - m_{\theta} (x - x_{a}) + m_{r} (y - y_{a}) + \frac{(x^{2} + y^{2}) - (x_{a}^{2} + y_{a}^{2})}{2 R_{c}}$$
(A-20)

This equation can be converted from the x, y co-ordinate system to the r,  $\theta$  coordinate system of Figure A-1 by means of the relations:

$$x = r \sin \left(\theta - \frac{\theta}{2}\right) - r_{p} \sin \left(\theta_{p} - \frac{\theta}{2}\right)$$

$$y = r \cos \left(\theta - \frac{\theta}{2}\right) - r_{p} \cos \left(\theta_{p} - \frac{\theta}{2}\right)$$
(A-21)

The general equation for the film shape in polar coordinates is then:

$$h = h_{a} + m_{\theta} \left[ r_{a} \sin \left( \theta_{a} - \frac{\theta_{T}}{2} \right) - r \sin \left( \theta_{p} - \frac{\theta_{T}}{2} \right) \right] - m_{r} \left[ r_{a} \cos \left( \theta_{a} - \frac{\theta_{T}}{2} \right) \right]$$

$$- r \cos \left( \theta - \frac{\theta_{T}}{2} \right) \left] + \frac{1}{2 R_{c}} \left[ r^{2} - r_{a}^{2} - 2rr_{p} \cos \left( \theta - \theta_{p} \right) + 2r_{a}r_{p} \cos \left( \theta_{z} - \theta_{p} \right) \right]$$

$$(A-2)$$

(note that Equation A-22 can also be used to describe the film shape for flat pads. In such cases,  $R_c$  is infinite, thus eliminating the fourth term on the right hand side of the equation, )

#### 3. Bending Coefficient

Equation A-20 and Figure A-1 show that (with the simplified elasticity approach used here), the bending deflection along a point on the pad surface is proportional to the square of its distance from the pivot, i.e.

$$\delta = K \left( x^2 + y^2 \right) \tag{A-23}$$

(A-24)

where  $K = 1/(2R_c)$ 

The value of the bending coefficient K was obtained by calculating the deflection at the rim of an equivalent circular plate point supported at the center of its lower face and carrying a conically distributed load on its upper face. A circular plate was used because a closed solution for its bending deflections is available (Reference 11). A conical load distribution was selected because the ratio of peak to average pressure (3:1) is similar to that in an actual bearing pad.

Integrating Equation 57 of Reference 11, for a steel circular plate (radius "a" and thickness " $t_{avg}$ ") under the loading and support described above, the deflection at the rim is found to be:

$$\delta = 0.75 \times 10^{-8} \frac{Wa^2}{_{avg}}$$
(A-25)

From equations A-23 and A-25, the relation between the bending coefficient and the pad load is:

$$K = 0.75 \times 10^{-8} \frac{W}{3}$$
 (A-26)

This relation was used in all the Phase I solutions.

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TABLES

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TABLE NO. 1

19" 0.D. x 9 1/2" I.D. THRUST BEARING  $\left(\frac{1}{R} = 0.5\right)$ 

Sq. In. (k = 0.85)In.  $\begin{pmatrix} k_{avg.} = 0.15k \\ R & 0.15k \end{pmatrix}$ In.  $(r_{p,M} = 90; 0, m_{s} = 50)$ Effective Bearing Area - 181 Average Pad Thickness - 1.462

Pivot Pitch Diameter - 14.25 011 - 2190 T at 115°F Inlet

-		1						
101.9.H		1.34 1.56 1.46	67.7 3.90	1.76	4.7 4.66 4.2	1.76 1.80 1.71	5.09 4.58 4.39	
e ror	Ĕ	0.816 0.575 0.510	1.78 1.25 1.13	0.60 0.48 0.412	1.7	0.769	1.55 1.09 0.94	
PMX 101×10-3	adi	12 64.7 93.3	30.3 93.5 123.0	54.4 95.5 123.0	36.3 86.9 13 <b>4.0</b>	25.3 82.6 120.7	61.6 124.0 169.7	
MX	Ĭ	275 868 1529	370 1372 2099	685 1355 1920	1122	301 1073 1686	747 1672 2448	
PAVG	pei.	353 517	168 518 682	302 528 682	201 744	140 458 670	341 688 533	
Ţ, ĸ	oF	150 184 209	165 207 239	£1828	164 195 226	155 188 211	176 215 242	
TAVG	oF	136 155 171	12 18 18 18	154 175	172	143	159 193 212	
Ľ.	٥F	125 132 142	126	81 15 15	120	126 150	153	
<u>د</u>	in	0.00135 0.00077 0.00065	0.00136 0.00085 0.000732	0.000667 0.000529	0.00102 0.00071 0.00058	07000°0 0°00075	0.00069 0.00051 0.00028	
<b>0</b> <sup>11</sup>		100 95 85.2	100 91.4 83.8	100 96.7 89.7	100 100 94.8	888	100 100 98.2	angen angele Malain-Maleran
ж "		22.22	22 27	35.7 46	14.3 42.8 45	35.7 28.6 42.8	14.3 42.8 44	
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∎ <sub>0</sub> ×10 <sup>6</sup>	in/in	75 143 170	130 190 210	88 Z S S	113 135	69 56 [03	115 128 140	
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No. of	Pads	مەمە	999	ແດຍເພ	ຍະຄະຍ	000	000	
1	Deg.	ជជជ	ជជជ	33.25 33.25 38.25	38.25 38.25 33.25	30.6 30.6 30.6	30.6 30.6	
Gase	No.	<b></b> (2 m)	450	r-wa∿	121	813	12	

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TABLE NC. 2

25" C.D. x 12.5" I.D. THRUST BEARING  $\left(\frac{L}{R} = 0.5\right)$ 

In.  $\frac{1}{2} \frac{1}{R} \frac{1}{R} = 0.154$ In.  $(r_{p} = 50; \theta_{p} = 50)$ Sq. In. (k = 0.25)Average Fad Thickness - 1.025 Effective bearing Area - 312

Pivot Pitch Diameter - 18.75 011 - 2190 J at 115°F Inlet

	н		1						
:	Ю. н		2.16 2.12	20.5	2.39	6.9 6.9	2.53	7.57 7.74	
			1.12 0.525	2.59 1.94	1.14 0.86 0.69	3.04 1.86 1.55	0.94	2.95	
5-UL2 21	ATT LOL. XWW, DAV.	lbs	34-5 127-8 174-1	77.0 175.2	46.8 119.6 187.4	52.3 180.0 250.3	91.3 174.8 235.2	52.8 156.1 250.1	
۵	XW.	psi	1106	563 1622 2410	327 923 1636	79.7	650 1391 2022	363 1150 2040	
6	AVG	psi	110 410 558	382	383 383 600	571	× 7 5	170 504 809	
1	XVM	٥F	155 190 217	173 216 253	155 179 207	160 205 230	160	160 191 227	
I.I.I	AVG	ч	130 159 174	142 176 194	150	201	155 175 196	147 173 201	
Ļ	5	ų.	125 125	12F 14L 153	125 134 146	126 145 158	130	126 140 159	
Ĺ	-	'n	0.00130 12000.0	0-00133 0-00133 0-00033	0*00000*0 0*000002*0	0.00054 0.00069	0.00065 0.00065 0.00042	0.00069 0.00069 0.00069	
ж 0		-	100 50.7 32.5	100 86.5 30.4	001 001 7.16	100 94.2	100	885	
ب ال	5		51 - 8 51 - 8	57.1 52	14.3	21.4 43 46	21.4 35.7 43	0 28-6 42-8	
, e		i	0.00126 0.0006 0.0004	0-00121 0-0006 0-0004	0.00000 0.0006 0.0004	0.00052 0.0006 0.0002	0.0005 1000.0 0.0003	0.00062	
4	۴Ĵ	10-° in-	323¢	71 71 70	5.12	°.20 £	282	2667	
Bx10 <sup>6</sup> Brx10 <sup>6</sup>	-	In/in	888	828	335	892	8.13 8	56.99 76	
<b>*</b> ₀×10 <sup>6</sup>		In/in	22 161 161	126 188 201	00 100 1100	105 134 153	20 12 12	125	
2		Ĭ	120	540	120	ลิลิลิ	120	2222	
No. of	1	Fads	فرمرد	φ <b>φ</b> ψ	<b>α.</b> τι, τι)	化化物	000	200	
	Į	6		555	<b>38.25</b> 38.25 38.25	35.25 38.25 38.25	30.6 9.9 9.9	30.6 30.6	
Gase	2		5 8 2	สมส	282	888	<b>8</b> 88	388	

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TABLE NO.

BEARING  $\left(\frac{1}{2} = 0.5\right)$ 15.5" I.D. THRUST × 0.D 3,

In.  $\left(\frac{\mathbf{t}_{NQ}}{\mathbf{R}} = 0.154\right)$ In.  $\left(\mathbf{r}_{P}\mathbf{x} = 50; \mathbf{0}_{P}\mathbf{x} = 50\right)$ In. (k = 0.85)ġ i. Average Pad Thickness - 2.385 Effective Bearing Area - 480

Pivot Pitch Diameter - 23.25 Oil - 2190 T at 115°F Inlet H.P. TOT 19.6 18.0 20.2 21.5 28.5 20.52 3.18 2.53 Q<sub>TOT</sub> 3.48 6.5 2.94 3.94 2.47 2.6.0 2.43 5.05 5 PMAX | "TOT×10" 154.2 284.5 346.0 213.1 350.4 425.0 99.5 289.0 382.0 324.0 503.0 73-5 269-3 411-3 370.5 546.3 1bs 456 1618 2440 453 1899 779 1802 2520 1046 3492 783 2172 3323 3278 1344 2295 1 345 200 1058 PAVG 213 772 1138 207 619 811 5253 5268 ра Т 2321 T 259 5676 303 181 2222 ų, 156 I AVG 38.8 55016 122 21193 181 220252 ÷ \_® 127 158 243 535 130 152 Ľ۵ -----0.00153 0.00118 0.00114 0.00015 0.00132 0.00076 0.00076 0.000133 0.00104 0.00098 0.00129 0.00838 0.00076 0.00132 0.00094 £ E 97.2 82.7 77.6 100 95.5 86.3 100 100 92.7 100 8.2.7 100 ¥. 0 5.5 6.5 35.7 46 47 12.0 7.73 у<sup>я</sup>. "Е 2222 5222 0.00132 0.000603 0.0004 7000°0 0.00124 0.0006 0.0004 0.0004 0.00061 0.0004 0.00011 0.0006 0.0004 , e e 0.0012 0.0006 0.0004 5 -**l**≋ <sup>'</sup> 10-6 3338 338 385 5122 528 385 ₽, **m<sub>0</sub>x10<sup>6</sup> | m<sub>r</sub>x10<sup>6</sup>** 1n/in 3208 でいる えええ 33.82 3333 858 1n/in 222 107 126.95 848 132.95 ឌភ្ល 888 32033 180 3202 150 2222 ž z No. of Pads 222 222 000 000 00 00 00 00 (0) (0) 38.25 38.25 38.25 38.25 30.6 30.6 30.6 30.6 30.6 • Å 322 ផ្លូន Gase ş. 5 % R 344 424 244 **3**255 362

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TABLE NO. 4

37" 0.D. x 18.5 " 1.D. THRUST BEARING  $\left(\frac{1}{R}$  = 0.5  $\right)$ 

E.	Sq. In. (k = 0.85)	Average Pad Thickness - 2.85 In. $\left(\frac{t_{avg.}}{avg.} = 0.154\right)$	- 27.75 In. (rp# = 50 ; 0 % :
	ż	i	i.
	685	2.85	27.75
1			
	Effective Bearing Area - 685	Thickness	Pivot Pitch Diameter
		ped	te
	iv		Id
	Effect	Averag	Pivot

50	
- *	
-	
5	
a .	
In. $(r_p = 50 + 0 = 50)$	
	*
. 27.75	Inle
•	5
	115
te	+
Ĩ	F
E	8
5	5
H	•
ivot Pitch Diameter	011 - 2190 T at 115°F Inlet

unu "	=	223	347 546 647
MAX	pei	934 2101 3135	1342
PAVG	pei	26 3E	792 862 846
Twax	ч	185 234 275	206 268 317
TAVG	ч	157 184 201	171 201 218
L.	4e	133 149 156	157
ď	În	0.00152 0.0012 0.00116	0.00163
×		94 81.5 77.3	91.5 80 76.8
2° E		282	50.5
hmin	In	0.0012	0.0012
-18 2	10-6 in-	57 TZ	35 35 35
"x10 <sup>6</sup>	in/in	25 25	887
<b>*</b> 0×10 <sup>6</sup>	1n/in	150 185 194	183 220 230
z	RPM	130 180 180	320 320 320
30	*		

TOT. "H.		13.4 13.4 14.6	31.0 33.2 38.6	13.9	35.7	14.7	39.6 32.3 34.2	
Q.TOT	udb	4.92 4.15 4.02	9.5 8.46 8.47	3.22	10.02 7.15 6.77	6.83 3.7 3.11	11.6 7.09 6.13	
PMAX WIOT*10-3	lbs	252.2 439.7 529.8	347.4 546.9 647.8	195.5 485.6 623.2	324.6 628.5 786.5	51.5 474.9 655.4	195.3 627.5 884.5	
YWW	pei	934 2101 3135	1342	636 1995 2980	2634 4115	1748 2709	617 2384 3907	
PAVG	pei	36.25	507 798 946	285 709 910	474 918 1148	75 693 957	285 916 1291	
Twx	ч	185 234 275	206 268 317	172 226 263	191 254 303	153 214 254	175 242 288	
TANG	ч	157 184 201	171 201 218	154 192 210	169 209 227	142 191 215	158 213 234	
L.	4e	133 149 156	157	153	137 161 165	125 152 164	130 163 165	
ŕ	in	0.00152 0.0012 0.00116	0.00163	0.00131 0.00092 0.00092	0.00138 0.00113 0.00113	0.00156 0.00032 0.00079	0.00137 0.000020 150000.0	
***	-	94 81.5 77.3	91.5 80 76.8	100 89	100 88.3 82.5	100 100 90.2	100 97.5 88	
% E		2023	52.5	28.6 47.5 48	35.7 49 49	0 45.8	0 3 3	
hain	ţ	0.0012	0.0012 0.0006 0.0004	0.00126 0.0006	0.00121 0.0006 0.0004	0.00156	7000.0 9000.0	
-1s	10-6 in-	322	30 35	19	13 25 32	55 C	50 <del>6</del> 28	
"x106	1n/in	***	52 52	58 22 58 22	26 27 27	68 97 07	262	
*****	1n/in	150 185 194	183 220 230	95 134 156	135 175	<b>1</b> 26 <b>1</b> 26	90 153	
z	RPM	130 180 180	320 320	180 180	320 320	180 180	320	
No. of	Pade	مەم	000	<b>60 60</b> 60	ຜິຜິຜ	999	1000	
•	Deg.	222	522	<b>38.25</b> 38.25 38.25	38.25 38.25 38.25	30.6 30.6 30.6	30.6 30.6 30.6	
	No.	285	889	<b>69 69</b>	<b>7</b> 999	69 69	825	

TABLE NO. 5

39" 0.D. x 19.5" I.D. THRUST BEARING (H = 0.5

Sq. In. (k = 0.85)In.  $\begin{pmatrix} t & 0.15k \\ R & 0.15k \\ R & 0.15k \end{pmatrix}$ In.  $(r_{p} = 50 \ i \ 0_{p} = 50)$ Effective Bearing Area - 760 Average Fad Thickness - 3.00

Pivot Pitch Diameter - 29.25 011 - 2190 T at 115°F Inlet

			1						
	101 101		11.8 11.7 12.9	18.6 13.2 21.5	14.2	22.0 17.7 13.4	14.9 13.4 12.1	22.9 19.7 19.1	 
	e TOT	udő	4.60 3.88 3.74	6.40 5.47 5.61	<b>4.78</b> 3.37 3.08	6.55 4.69 4.4	2.51	6.3 4.73	
	e-otxiol	lbs	266.7 466.4 568.9	321.7 526.9 595.5	224.0 517.7 650.0	283.4 586.0 722.5	276.4 515.0 697.0	345.8 579.5 816.0	
	PMAX	pe1	<b>894</b> 2037 3063	1081 2340 3434	658 1920 2843	853 2193 3296	809 1711 2662	1027 1965 3146	
	PAVG	pei	351 614 749	1368	<b>294</b> 681 855	575 177 177	364 678 917	455 763 1072	
	Twx	οF	183 230 271	193 246 288	170 220 258	180 234 276	175 210 249	188 224 264	
	TAVG	oF	155 181 197	206 1960 206 1960	152 188 206	159 197 215	159 187 212	169 221	
	Ļ.	۰F	133 148 155	152	126 151 161	131 156	132 150 163	137 157 164	
	P1	in	0.00156 0.00122 0.00117	0.0016 0.0013 0.0013	0.00132 0.00098 0.00094	0.00133 0.00103 0.00102	0.0010 0.00083 0.0008	0.00102 0.00088 0.00085	
	0 1		85.4 81.4 77.9	93.7 81 76.6	100 89.8 84.4	100 39 83	100 100 90.4	100 99 89.5	
1-677 1	ыя. "П		លជន	355	35.7 46 43	35.7 47 48	21.4 42.8 45	28.6 43	_
14hm J-CTT 18 1 0477 -	h min	ţı	0.00012 0.0006	0.0012 0.0006 0.0004	0.00124 0.0006 0.0004	0.00122 0.0006 0.0006	0.0006 0.0006 0.0006	0.0006 0.0006 0.0004	
110	-18 <u>2</u>	10-6 In-	58%	325	7 18 23	<b>5</b> 6 09	547	8 16 22	
	.x10 <sup>6</sup>	in/in	ខ្លួន	និដដ	355	48 31 27	38 31 31	32.32	
	10°6	in/in	120 127 187	160 207	96 133 13	106 148 165	87 110 121	94 116 131	-
	Z	RPM	150	8 8 8 8	150	2 2 2 2 7 2 2 2	150	200 200 200 200	
1	No. of	Pads	രംഗം	مەم	ໜໜໜ	ແຫນ	000	999	
	•	Deg.	ជជុំជ	ជជជ	38.25 38.25 38.25	38.25 38.25 38.25	30.6 30.6	30.6 30.6 30.6	-
-	e S	No.	273	24 24 25 25 26 26 26 26 26 26 26 26 26 26 26 26 26	<b>5</b> 8 5	8688 8	83 87 87 87 87 87 87 87 87 87 87 87 87 87	83 69 60	

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TABLE NO. 6

41" 0.D. x 20.5" I.D. THRUST BEARING  $\left(\frac{1}{R}$  = 0.5

Sq. In. (k = 0.85)In.  $\left(\frac{t}{8}$  o.154 In.  $(x_{p}) = 50 \pm 0 p_{p} = 50$ Pivot Pitch Diameter - 30.75 Average Pad Thickness - 3.16 Effective Bearing Area - 840

011 - 2190 T at 115°F Inlet

	5		ļ							
	H.P. TOT		7.72 7.45 8.15	21.0	8.49	20.4	9.26 8.57 7.81	25.97 22.78 22.18		
	<b>1</b> 01 <b>0</b>	đđ	3.14 2.72 2.60	7.02 6.4 6.37	3.5 2.4 2.15	7.45 5.05	3.35 2.48 2.0	6.89 5.41 4.59		
	PMAX "TOTXIO"	lbs	<b>244.0</b> 458.0 560.0	373.0 583.0 700.0	194.0 496.0 635.0	341.9 661.0 829.4	218.8 480.0 673.7	436.7 675.6 913.9		
ſ	XMM	ž	715 1781 2667	2425 3683	518 1646 2426	954 2285 3500	571 1451 2309	1210 2097 3303		
-	AVG	Ĩ	23 246 546	33.995	232 590 757	407 787 987	260 802 802	520 804 1083	·	
•	NW.	οF	175 216 251	252 252 294	201 202	185 239 283	3985	193 228 272		·····
•	AVG	٥F	149 172 188	163 192 208	146 178 197	163 199 218	150 178 202	5223		
+	G	4	129 143 150	%1 2 2 2 2 2 2	127 146 156	135 158 164	128 145 158	158		-
4	1	ų	0.00147 0.001110 0.0	0.00164 0.00138 0.00133	0.00131 0.00093 0.00088	0.00139 0.00100 0.00106	0.00080 0.00080 0.00074	0.00092 0.00092 0.0009		
	R.		96.4 82.5 78	90.5 89 76.6	100 90.3 84.2	100 88 82.6	888	100 88.5 87.4		
1	е. , П		2228	823	28.6 45 47	42.8 47.5 48	7.1 42.8 44.5	35.7 43		
	ula	ų	0.0012 0.0006 0.0004	0.0012 0.0006 0.0004	0.0004	0.00121 0.0006 0.0004	0.000 <del>0</del> 0.0006	0.00093 0.0006 0.0006		
ÿ	ส	10-6 in-	23 18 <del>0</del>	238	-9 15 16	S 8 5	12 20	888		
■ ×10°	4	1n/1n	202	53 50 IS	38%	385	228	32.52		
• ×10 <sup>6</sup>	Þ	in/in	11 <b>4</b> 150 167	156 196 203	85 119 130	115 152 165	5 <b>2</b> 101	131 205		
z		RPM	100 100	8 8 8 8 8 8	888	8 8 8 8 8 8	888 888	8 8 8 8 8 8		
No. of		Pade	999	مەم	<b>60 63 80</b>	യതേത	000	000		
		Deg.	512	***	38.25 38.25 38.25	38.25 38.25 38.25	30.6 30.6	30.6 30.6 30.6		
e.		No.	91 93	828	66 86	101	105	901 102 103		

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PHASE
-1
ARING PROGRAM
品
THRUST
MARINE

TABLE NO. 7

 $45^{\circ}$  0.D. x 22.5" I.D. THRUST BEARING  $\left(\frac{1}{R}$  = 0.5

Effective Bearing Area - 1012 Sq. In. (t = 0.85)Average Pad Thickness - 3.46 In.  $(\frac{t}{R} = 0.154)$ Pivot Pitch Dismeter - 33.75 In.  $(r_{P}^{*} = 50; 0_{P}^{*} = 50)$ 

Oil - 2190 T at 115°F Inlet

			1							
_	H.P. TOT		11.8 10.0 11.7	21.5 22.7 26.8	11.7 9.96 10.2	25.8 21.2 22.9	12.4 10.9 10.3	26.8 23.3 22.8		 
-	<b>6</b> .101	5	3.52 3.52 3.52	16.9	2.98	7.9 5.76 5.33	4.5 3.09 2.54	7.32 5.73 4.94		
_	"TOT*10"	lbs	337.6 562.1 692.4	455.1 711.6 825.4	238.8 654.4 815.7	430.7 797.1 990.9	232.7 621.8 875.4	539.0 810.9 1082.2		
	YW	Ĩ	842 1911 2895	1205 2494 3774	517 1837 2687	1000 2305 3533	494 1616 2542	1243 2140 3337		
-	AVG	psi	334 555 684	450 703 816	236 638 806	728 778 778	230 614 865	533 801 1069		
-	TWX	οF	1 <b>79</b> 223 260	197 252 295	164 214 250	184 239 284	162 207 2 <b>42</b>	192 226 272		
-	TAVG	oF	152 177 191	162 191 206	147 183 201	161 198 217	148 184 207	172 201 222		 
-	_ <b>6</b>	٥F	130 146 151	136 152 153	126 148 156	134 157 163	126 160	140 158 165		 
-	<u> </u>	în	0.00153 0.00129 0.00124	0.00169 0.00142 0.0014	0.00132 0.000988 0.000948	0.0014 0.0013 0.00113	0.00011 0.00086 0.00079	0.00106 0.00006 0.00106	<u></u>	
-	м. •	_	93.8 80.3 76.9	<b>89.8</b> 79.5	100 38.2 83	100 87.4 81.8	97 97 89.3	100 96.1 87.5		 
-	ы. Н <sup>В</sup>		£ 5 5	577.23 2.5	21.4 46 47	42.8 47 48	42 45	35.7 43 46		 
-	h ain	in	0.00012 0.0004	0.0012 0.0006 0.0006	0.0013 0.0006 0.0004	0.00121 0.0006 0.0004	0.0001 0.0004	0.00093 0.0006 0.0004		
-	-18' #	10-6 in-	9 18 21	855 E	17 18 18	6 <sup>81</sup> 22	15	6 <u>5</u> 20		 
	T ×10°	in/in	170 20 19	53 58 53 FB	<b>2</b> 86 286 27	385	5882	37 31 31		
`	<b>B</b> x10	1n/1n	118 162 168	156 185 200	73 116 130	114 143 155	63 95 102	10 <b>4</b> 1118 1118		 
	z	RPM	100 100 100	170 170 170	800	170 170 170	100 100	170 170 170		
_	No. of	Pads	৫৩৫	७७७	ພະເກ	ເບີດເຫ	000	0000		
	<b>.</b>	Deg.	555		38.25 38.25 38.25	38.25 38.25 38.25	30.6 30.6 30.6	30.6 30.6 30.6		 
	3	No.	801 110 111	112 113 114	115	118 119 120	122 123 123	125		 

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TABLE NO. 8

50" 0.D. x 25" I.D. THRUST BEARING (E = 0.5

Sq.  $I = (1 - ... S_{2})$ In.  $(1 - ... S_{2})$ In.  $(1 - ... S_{2})$ In.  $(1 - ... S_{2})$ Effective Bearing Area - 1250 Average Pad Thickness - 3.85

Pivot Pitch Diameter - 37.5 Dil - 2100 T - 11605 Toler

		1						
H.P. TOT		13.2	29.2 32.1	16.0 13.5 14.1	34.5 29.6 32.4	16.3 15.0 14.0	32.2 32.2	
enor		5.38 4.89	10.01 9.2 9.75	5-57 4-05 3-74	10.0 7.64 7.07	69.4 69.4 7.00	9.21 6.42	
"101×10-3	lbe	467.4 740.9 902.8	611.9 909.9 1043.5	126.9 847.5 1044.3	601.5 1050.1 1316.6	389.6 874.3 1133.2	760.6 1103.2 1468.7	
Pwx XM	De 1	990 2137 3244	1370 2730 4189	787 2036 <b>295</b> 1	1166 2577 3951	1262 1863 2827	3787	
PAVG	De l	374 593 722	490 728 839	342 678 835	481 840 1048	520 699 907	8608 883 1175	
Twx	٥F	184 231 272	262 262 309	588 89 13	500 500 500	190 214 254	500 536 586	
TAVG	4 e	155 180 196	167 196 211	206 1353	168 204 223	172 189 213	2200	
L G	Ч,	51 12 12	139 154 160	151	133	127 151 162	165	
£.	in	0.00166 0.00142 0.00134	0.00151 0.00155 0.00156	0.00136 0.00111 0.00105	0.00124	16000°0 16000°0 36000°0	0.00103	
×.	_	90.6 73.5 76.7	27.7 73 76.2	100 86.6 81.5	100 85.5 81	100 96.5 86.4	93.02 86.2 86.2	
н Ж		53.5 50	50.5 50.5	35.7 47 47	42.8 48 48	35.7 43 46	495.7	
hain	ţ		1000'0 1000'0	10000	000	A SALE		
~ s` Ľ	10-6 in-	0110	នទង	14 14	9 20 20	8 11 15	o. 7 8	
•	tn/in	16 13	20 S 18	8333	32%	385	53.47 58.38	-
•a×10*	1n/in	169 169	164 136 200	91 125 131	114 148 152	87 97 106	115	
z	RPM	100 100 100	222	888	221 221 221	888	170	
No. of	Pads	مەمە	৵৵৵	လဆေးသ	<b>හ</b> හ හ	000	999	
<b>0</b> <sup>1-</sup>	Deg.	ភន <b>ភ</b>	555	38.25 38.25 38.25	33.25 38.25 38.25	30.6 30.6	30.6 30.6 6	
<b>.</b>	No.	127 128 129	51 131 132	132	136 137 138	170	354	

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14	
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-	
<b>m</b>	
-	
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	-
0.327	So. In. (k =0.631)
"	-
-14	5
26" 0.D. x 17 $\sqrt{2}$ " I.D. THRUST BEARING ( $\frac{L}{R}$ = 0.327	S
THRUST	181
.	•
3	
17 1/2"	offective Bearing Area - 18/
×	d
. O.D.	ortive
56	**

		50
In. (k =0.631)	In. $\left(\frac{\mathbf{t}_{avg.}}{\mathbf{b}} = 0.113\right)$	$(r_{p} = 50 + \theta_{p})$
ż	In.	In.
		- 21.75
•	•	•
Effective Bearing Area - 184	werage Pad Thickness - 1.47	vivot Pitch Diameter
ve Be	Ped	itch
ffecti	verage	ivot P

(r. %	
In.	
21.75	Inlet
•	11505
Diameter	-
Pitch D	2100
t bi	- 180
-	- 24

		1	
	H.P. TOT		0.35
	Q_TOT	udb	0.92 0.75
	WTOT ×10-3	lbs	63.8 103.7 157.7
	PWAX	psi	788 2535 2535
	PAVG	psi	350
	TWX	do	243
	TAVG	Чo	194
	, B	do	137
	ų	in	0.00051 0.00055 0.00053
LATUT	%	-	99 85.9
I-CTT 1	r. %		50.2
NATUR J-CTT 18 1 0617 - 110	hain	In	0.00072
110	-18 2	10-6 in-	5 8 2
		1n/in	150
	Bx106 Brx106	1n/in	133
	z	RPM	160 160
	No. of	Pads	00 00 00
	θ <sub>Τ</sub>	Deg.	28.4
	Case	No.	145

						101	21.0 15.2 13.2	
						5	¥28	
					C-01. E	5	11-1-0 361.0 253.0	
							1.72.22	
				~			i reg	
		(68)	_	In. (r. 5 = 51.74 • 5 = 50			238	
			0.12	•	T.		. <u>36</u> %	······································
a		1-0 - 1 8	59. In. (k = 0.85) In. (terre. = 0.122	- <b>-</b>	1		223	
1990 - 1		BEARING (		i.	æ	5	0.00149	
200	9	THRUST	2.20	- 24 F Inlet	*		8.5° 8.5°	
	TANE NO. 10		- 114 -	ter t 11595	بر ار		83.2	
- 1990 - Meddar Dathar Islan andre		31" 0.D. x 16 1/2" I.D. THRUST BEARING (1 = 0.468	Effective Bearing Area - Average Pad Thickness -	Ploot Pitch Diamoter - 24 Oil - 2190 I at 1150F Inlet	u tu	ţ	0.00020 0.00060 0.00060	
		31" 0	Effecti Average	Pivot F	-1e 4	10-4 in-	553	
					∎_×10 <sup>6</sup>	la/in	21 25	
					*10*	ta/in	150 190 210	
					*	KP	320	
					No. of	Pada	ໜ່ໜ່	
					•	Deg.	38.25 38.25 38.25	
					e S	No.	120 150	

								1	
						N.P. 701		199	
						<b>P</b>	1	<b>J</b> <sup>1</sup> <sup>2</sup>	
					• • % )		Part and allors	1	2:54 2:54 2:54
						3	Ĩ	24 1123 1221	
				-		PANS	ja I	78F	
						, M	<u>ا</u>	227 227	
		اع ا	0.25)	61.0		TAWG	ł	<u><u>sus</u></u>	
22		10	۳ ۳		R	, <b>5</b>	÷		
- 1941		THRUST BEARING ( L = 0.471	<b>Sq. In. (k = 0.25)</b> In. /t.	יר י		4	ų	0.0210 20113 2010 2010 2010 2010 2010 2010	
NEXT	=	THINKI	- <del>5</del> 91 - 2.33	5	Inlet	¥.	-	8.82	
1	IABLE NO.	- - -	-		t 115°F	¥. .,#		57.2	
t 1944 - March antan 1944 - 1944		D. x 18 1/2" I.D.	Effective Bearing Area - Average Ped Thickness -	Pivot Pitch Dimeter	011 - 2190 T at 115°F Inlet	e ju	ţ,	0-00120 0-00040 0-00040	
a line		35" O.D.	Effects Average	Pivot P	110	-18	10 <sup>-6</sup> 1n <sup>-</sup>	262	
						•x10*	tn/in	252	
						*10 <sup>4</sup>	1n/in	125 125	
						z	RPM	170	
						No. of	Pads	ũ ( th C	
						•	Deg.	2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5	
						e U	W	151	

THAT MADE BARTHE MADE AND AND

IABLE NO. 12

31" 0.D. x 151/2" 1.D. THRUST DEARING ( $\underline{L} = 0.5$ 

Effective Bearing Area - 400 Sq. In. (k = 0.95)Average Pad Thickness - 2.01 In.  $\frac{1}{k_{WGL}} = 0.130$ 

Plvot Pitch Diameter - 23.25 In.  $(r_p = 50 + p_s = 50)$ Oil - 2190 I at 115eF Inlet

N.P. TOT 21.5 315 £8 5 12.2 4.2.0 101 48.5 6.% 5.2% 222 8.55 8.5.R 8.5.R 6.25 Pmx | "TOT=10" 25.5 317.6 2.00 9.98.0 9.98.0 TRE C 1 1.55 3516 Ĩ ËFŞ 223 £88 8.22 385 PANG 223 Z 382 REZ 385 386 2:5:8 1 ۲ 223 23**2** 585 383 388 ១ខ្លង្គ ANG 322 355 \$ 38 \$62 348 383 -.0 233 \*\*\* 235 232 858 255 ų., 0.00128 0.00173 0.00170 0.00150 0.00119 0.00103 0.000135 10100-0 2-0000-0 £ 5 93.0 1.05 1 5.28°.2 888.8 225 888 ខ្ទ័ងត у**к**. \_ Ш 20.02 35.7 7.35 844 033 0700010 0210000 , i 0,0000.0 0700010 0.00121 0.00060 0.00040 0.000135 0.00060 0.00128 0.00060 0.00020 5 -**180**, -223 242 223 838 23.7 224 •x10 11/in 282 \*5\* 822 22% 885 8:538 av10<sup>6</sup> 1n/in 8.8.8 20238 2222 5325 39 23 25% z R. ខ្លួនខ្ល 3333 8081 8888 868 8888 No. of Pade 222 200 999 000 a) w as 60 60 60 38.25 38.25 38.25 33.25 38.25 38.25 30.6 30.6 30.6 • ġ 323 525 Sase No. 522 153 160 525 163 922E

LAND THEY MADE THEY PORT TOTAL

IANLE NO. 13

 $31^{n}$  0.D. x 151/2" 1.D. THRUST BEARDIG  $\left(\frac{1}{6} = 0.5\right)$ 

Sq. In. (k = 0.85)In.  $\left(\frac{t_{max}}{k} = 0.193\right)$ In.  $(r_{p} = 50 + 0.193\right)$ Average Pad Thickness - 2.99 Effective Bearing Area - 480

Pivot Pitch Dismeter - 23.25

011 - 2190 T at 1150F Inlet

		1						
N.P. TOT		8.00 8.00 8.00	111	8.c2 8.c2	7.51	10.00	222	
<sup>Q</sup> ror	8	2.2 1.97 1.74	3.5.5	2.5 2.5 2.5	1.15 1.15 1.15	2.28	38-8 26-7 26-12	
Pmx   "Tor*10"	Ą	129.8 304.0 414.0	1.221 393.7 521.5	66.2 290.0 118.1	8.111 992.9 996.0	113.5 223.1 414.7	51.5 322.5 599.7	
Ĩ	i	£ 2 3	3222	* 35	838	និន្តីខ្ល	5000 5071	
ANG	Ĩ	853	375	809 SE	222	* 53	161 123	
	5	= X X	85 85 S	210	25.72	120	212 212 212	
TANG	ii.	<u> </u>	288	195	232 205 232	155 172 210	145	
, <b>5</b>	ų.	838	782	233	130	<u>8</u> 69	525	
4	şn	0.00126 0.00072	0.00142 0.00093 0.00054	0.00142 0.00072 0.00058	0.000136 77000.0 77000.0	0.00092 0.00068 0.00068	0-00160 0-00067 0-00056	
	_	100 1.4 85	100 88.8 52.3	888	888	<u>888</u>	888	
R		5.1 23.1	338	0 12.8 16.4	7.1 42.8 46.5	0 21.4 42.8	0 23.6 42.7	
h ein	In	07000°0 09000°0 51100°0	07000-0	0700000	07000°0 09000°0	0.0092 0.00066 0.00041	07000°0 09000°0 09000°0	
-18 2	10-4 1n-	6 14 18	683	707	~ 78	12.730	90 13,9 30	
• rto•	in/in	2229	15	882	825	3582	832	-
*01x8	1n/1n	8 82 9	22 22 29 29 29	288	80 115 120	82 Z 60	388	,
*	N.	180	88 88 88	180	2222	180 180 180	2222	
No. of	Pads	مەم	يەمم	<b>69</b> 60 60	රෙසෙන	992	<b>99</b> 9	
•	Deg.	~~~		38 <b>.25</b> 38 <b>.25</b> 38 <b>.25</b>	38.25 38.25 38.25	30.6 30.6 30.6	30.6 30.6	
3	¥0.	232	175 176 176	52 <u>6</u> 68	181 182 133	134 136 136	139	

L MARA - MARANA PARAMA LENNI - MARAN

IAME NO. 14

31" 0.D. x 151/2" I.D. THRUST BEARING (1 = 0.5)

ł

Sq. In. (k = 0.85)	<b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b>
In.	J
ġ	I.
Effective Bearing Area - 480	Average Pad Thickness
ł	2
Effectiv	Average Pad Th

Pivet Pitch Diameter - 23.72 In.  $(r_{\beta} = 53 + 6) = 50$  ) 011 - 2190 T at 1150F Inlet

l			7.8	<b>9</b> 7	13.7 21.0	0.15 2.01	2	22.5	10.01	. ×.	22.	<b>.</b>					
-	-	_			22	0.60	r 	នឌ្	는 음* 		81	2	ha y.	a			
•	ļ	1	นี้ส์	3.2	កូខ្ល	2.52	8	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3.17	10	6.9	(f)					
10.01	and a	1	148.0	2 2	2.23	116.0	0. 	13.5	2.6.1 2.9.5	417.6	3-262	5-155			 		•
	1	ī	747	2	56	23	4	2165	123	2375	1116	ŝ			 		<b></b>
1		Ĭ	2 2 2	e hi	12	35		200			767				 •••		-
	_		2 X X	8	ŝ	R	5	138	<u>8</u> 3	3	196				 		
1. m	2	•	525			288			155 1		57 32 32				 		
	-		533	22	ធ្ម	238		18:3	136		158				 		
	•	Ę	0.00129 0.00129		0.00136	0.00152 0.00102 0.00102		0.00116	0.00109		0.000000		••••		 	-	
¥			782.5		_	9100 85.6		5.5	88		99.6 9.6				 		
×."			2.58			40.8	_	8.8	52.1		52				 		<b></b>
q		5	0.00000	0,000.0	07000-0	0.00125 0.00060 0.00040	0.00122	0,00060	0.0000		0.0006	_			 		
-1:			288	25	8	° 7 5	12	8%	8 9 C		28:			• =	 		
•r*10*	- 10		9- <u>1</u> -9	<u>ر</u> ئ ا	ŗ.	<b>4</b> 00	Ŷ	<b>0</b> w	825	:	825	:	•		 		
*01×0*	4 m / 4 m		¥#2	<b>18</b> 220	[2]	601 651 551	134	89 161	838		883	ţ			 	-	****
=			8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	<u>8</u> 88	220	81 81 81 81 82 83	320		180						 		
No. of	Pada		مەمە	~~~	0	ຍະຄະ	ໜ		999		222				 		
•			222	555	7	38.25	38.25	38.25	30.6 30.6	7 00	2000 1999 1999				 		
Case	No.	2	161	193 194	61	195 195	199	50	2020	300	50K		-		 		

MART - MARTIN RANDA TANK

# TAME NO. 15

31" 0.D. x 151/2" 1.D. THRUST BEARING (H = 0.5

Average Pad Thickness - 2.80 Sq. In. (k = 0.65)Average Pad Thickness - 2.385 In.  $\left(\frac{1}{k_{R}} = 0.15k}{R}\right)$ Pivot Pitch Disamter - 22.78 In.  $(r_{R} = 47 + 0) = 50$  ) 011 - 2190 T at 115 Finlet 

		ł						
н.Р. <sub>ТОТ</sub>		01.0	19.5	17.5	22.8 12.6 15.3	5. K S	22.5	
<b>P</b>	8	3.5	2:5 7:57	2.5	9-4- 9-9-4-	3.15	20 - 10 - 10 - 10 - 10 - 10 - 10 - 10 -	
C-OFRHUE	Å	136.0 266.0 343.5	123.5 339.0 416.0	122.7 272.6 379.0	0.63.0 0.63.0	147.8 219.0 321.6	123.1 325.6 520.6	
ž	Ĩ	3352	222	576 2371 2371	2030 2030 3107	710		
PAVG	Ĩ	716 258 716	265	×\$\$	52 E	ĕ 38	ផ្តនន្ត្	
Taxa I	*	<u>883</u>	¥38	39 I Q2	28 E	ន្មត្តដ	825 835	
TANG	<u>بر</u>	<u>878</u>	20 20 20 20 20	201 222	152 196 218	158 171 201	2162 223	
<b>_</b> 6	<u>и</u> .	838	223	121	ยั่งวั	138	<u>zzz</u>	
£"	ţ	81100-0 99000-0	0.00100.0 0.00100.0	79000°0 14000°0	0.00120 0.00072	0.00076 0.00064 0.00052	0.00078	
*	_	100 85.7 80	100 124.5 78.6	8.5 8.5 8.5	85%	100 100 95.6	8138	
ыя. "Ш		39.6 23.6	35.7	37.5	0 35 38.7	0 14.3 31.2	0 36.4	
e a	In	0,0000.0	07000°0 09000°0 07000°0	0.00090	0-00120 0-00060 0-00040	0.00076 0.00063 0.00043	07000°0 19000°0 82000°0	
- <b>1</b> 8' <u>"</u>	10-6- In-	7%F	3338	26 19 4. 26	33.55	\$ <u>5</u> 6	9 27 27	<b>**** *****</b>
T x10	in/in	253	888	2992	81 <b>9</b> 3	100 85 62	120 63 83 63	
*10*	1n/in	130 169 180	164 213 218	80 124	72 155 169	8 9 2 2 2 2 2	83 139	
E	RPM	130 180	320	180 180	32.02	180 180	32033	
No. of	Pade	مەمە	৵৵৵	ໜາດໜ	<b>100</b> 100 100	222	000	
e <sub>T</sub>	Deg.	555	888	38.25 38.25 38.25	35.25 39.25 39.25	30.6 30.6 37.6	30.6 30.6	
5	No.	203 209 210	212	214 215 216	217 213 219	220 221 222	57 <b>5</b> 7	

						101 - H	C7-5	0	2.6 2.6 2.6	
						<u>d</u>	3.55	5.2	55R	
						<sup>2</sup> IOI <sup>#</sup> IOI <sup>=</sup>	11 5.5 87.5 82.0	0.605	175.5 195.0 6.50	
						Ĩ	<b>1</b> 8:00	31%	107	
				~			<b>1</b> 37	1047	8 <u>63</u>	
			_	8	-	<b></b>	30 E	230	ริลิฆิ	
		0.5 )	0.85)	20 1 0 <sup>2</sup>	•		- 35	195	198	
-			In. (k = 0.85) (t		-	5	25	130	និតិត្តិ	
Null -		× 151/2" I.D. THRUST BEARING (E =	in. In.	<u>יי</u> לי בי	£	- e	16100.0	15000-0	0.00105	
TROCK	4	THRUST	- 480 - 2.385		1		93.1 93.1	001	90.9 85.9	······································
<b>MUDE</b>	IABLE NO. 16	7 I.D.		ter	1	1	14.3	35.7	£7.8	
- 1944 - ANDRE LEISTER ANDRE	Η	.D. x 151/2	Effective Bearing Area Average Pad Thickness	Pivot Pitch Diamater - Oil - 2190 I at 11505 Inlat			8.85		07000.0	
194		31" O.D.	Effecti Average	Pivot P Oil	4	10-6 In-	r 48	2	n 13	
					•x10*	1n/1n	388	88	9 £	
					*10*	1n/1n	155 92 182	135	236	
					×	RPM	180 180 180	23	N.R.	
					No. of	Pads	າບເບໜ	လေးရ	0.60	
					• 1	Deg.	38.25 38.25 38.25	38.25 38.25	38.25	
					ŝ	No.	55 55 57	622 022	វិនី	

					IOL-4-H		13.7 14.5 15.6	สี่สี่สี่	
					<sup>0</sup> ror	1	4.8 3.69	8.5 8.5 8.5	
					"TOL" IOL	-	266.7 266.7 814.0	298.5 738.0 947.0	
					X	2	552	206 2112 2335	
				~	AVG	Ĩ	8,3 E	2233	
				8	Tan 1	•F	220	82 I 28	
	-	<u>_</u>	0.154 0.154	05 = \$ <sup>d</sup> = 20	JAVG	3. •	133 135 189	191	
-		= 0.5	In. (k = 0.25) ( <sup>t</sup> me. = 0.154		, E	4. •	800 800 800	222	
1	Ì	THRUST BEARING (1 =	ĕ.₽Ţ ġĘ	_ت بة	£	In	0.00133 0.00106 0.00110	0.00137 0.00116 0.00116	
PLOBULE	5	THRUST	- 760 - 3.00	- 29.25 F Inlet	¥.	_	100 89.7 83.4	100 88.5 84.2	
<b>MALON</b>	TABLE NO.	191/2" I.D.		- ñ,	и. М		35.7 47.2 48.5	35.7 47.5 49.1	
A PART - MADE PARTY PARTY - MARK	·	0.D. × 191/2	Effective Bearing Area Average Pad Thickness	Pivot Pitch Diameter - 29.25 Oil - 2190 I at 115°F Inlet	hain	tn 1	0.00124 0.00060 0.00040	0.00023 0.00060 0.00023	
N.C.		34.0	Effectă Average	Pivot P 011	-16 2	10 <sup>-6</sup> 1n <sup>-</sup>	\$ ~ a	332	
					=	1n/in	328	48 35 28	
					*10 <sup>4</sup>	in/in	102 158 186	119 183 204	
						RPM	150	888	
					No. of	Pads	ຍຍ	10 10 10	
					•	Deg.	38.25 38.25 38.25	38.25 38.25 38.25	
					3	No.	232	5252	

						н.Р.	2	5.2 2.22	500 297	0 3 8 8 8 8 8 8									
									6 O	992									
						2-012-112-2	1	57 50 9.7.5 9.7.5	35.2 74.7 101.0	17.4 58.4 94.3									
						ľ	1	35.59	5	88 × 82									
					~	Å.	Ĩ	. 738	£3£										
				$\sim$	8			282	8.888	385									
		19" 0.D. x 9 1/2" 1.D. THRUST BEARDIG ( = 0.5		1 S	ANG	<u>u</u> .	382	42E	385										
a)					- 1.462 In. ( <b>1.464</b> - 1.462 In. ( <b>1.464</b> - 1.462) In. ( <b>1.9</b> 5	_ <b>5</b>	4. •	883 2	583	<b>21</b> 53									
AND THEY BUILD TRANSM INC.			Sq. In	• - 181 \$9. • - 1.462 In. • 14.25 In.  947 Inlet		<b>.</b>	1n	0,0000.0	0.00065	0.000 <del>69</del> 0.000 <u>69</u> 0.00024									
	10		181 -			y. •	_	97.2 87.4 82.2	2.1 2.1 2.1	888									
	IARE NO. 18					1 <sup>4</sup>		53.1 52.1 50.2	28.6 45.2	21.4									
						ate of	5	0,00050	0.00063 0.00020 0.00030	<b>e3000.0</b> <b>52000.0</b> 0F000.0									
			Effecti			-18	10-6 19-0	276	228	498									
																=_x10*	1n/in	8 8 Q	328
						*10t	in/in	3 <b>48</b>	89 20 21	188									
						•	ŝ	888	<u>558</u>	<u>888</u>									
						10. of	2 2 2	مەم	ଣ ୧୯୦୦	999									
						<b>.</b>	Ż	222	38.25 38.25 38.25	30.6 30.6 30.6									
						3	2	ลี่ถึงวิ่ง	สสล	สสส									

75" 0.D. x 371/2" I.D. THRUST BEARING ( $\frac{1}{R}$  = 0.5 TABLE NO. 19 Effective Bearing Area - 2810

Sq. In. (k = 0.85)In.  $\left(\frac{t_{avg.}}{R} = 0.154\right)$ In.  $(r_{p}K = 50 \ i \ \theta_{p}K = 50$ ) Pivot Pitch Diameter - 56.25 Average Pad Thickness - 5.77

011 - 2190 T at 115°F Inlet

H.P. TOT		53.1 61.8 47.3	53.6 47.3 51.4	
9 nor	adb	16.0 16.7 13.1	12.2 11.5 10.9	
"IOT×10"	lbs	1985.0 2200.0 2260.0	2825.0 2544.0 3180.2	
XW	psi	3203 4390 2927	4517 2819 4311	
PAVG	psi	706 783 802	1004 902 1128	
TWX	PF	272 318 263	319 254 306	
TAVG	oF	196 210 206	225 213 232	
۴.	oF	153 157 160	163 162 165	
£	in	0.00205 0.00210 0.00166	0.00161 0.00137 0.00137	
* <b>•</b>		76.3 74.6 81.0	78.3 86.5 82.8	
*		50 50	46.6	
hin	in	09000.0	07000-0	
-18 2	10-6 in-	ពួនផ	12	
•	1n/in	22 52 52 52 53	22 SS 23	
•0×10* •×10*	in/in	170 183 137	136 115	
=	RPM	100	888	
No. of	Pads	666	8 10	
•	Deg.	51 51 38.25	38.25 30.6 30.6	
Case	No.	247 248 249	250 251 252	

1

TABLE NO. 20

50" 1.D. THRUST BEARING  $\left(\frac{L}{R} = 0.5\right)$ 100" 0.D. ×

In.  $(r_{p} = 50 ; \theta_{p} = 50)$ Sq. In. (k = 0.85)In.  $\left(\frac{t_{avg.}}{avg.} = 0.154\right)$ Effective Bearing Area - 5000 Average Pad Thickness - 7.70

011 - 2190 T at 115°F Inlet Pivot Pitch Diameter - 75

	Б				
	н.Р. тот		3122	138 118 132	
	Q_TOT	adb	39.2 47.8 28.2	27.4 26.7 25.7	
	WIOT X10-3	lbs	3730 4380 4890	5280 5151 6493	
	XW	psi	4268 6451 3995	5939 3758 5862	
	AVG	psi	116 875 875	1055 1028 1296	
	TWX	ч	305 352 301	367 289 353	
	TAVG	ч	206 226 221	237 226 248	
	<b>_</b> 5	ч	156 160	165	
	ď	in	0.00284	0.00226 0.00191 0.00191	
	يد م		74.5 72.1 79.4	76.8 83.0 81.1	
	". %		49.8 49 47.8	48.5	
	hmin	In	0.00060	0,000,0	
	- <b>1</b> 8	10-6 in-	11	16 <sup>01</sup>	
	<b>s</b> x10 <sup>6</sup>	1n/in	22 23 23	853	
	•0×10*	1n/1n	179 175 130	146 116 122	
	z	RPM	100	00100	
	No. of	Pads	ଜଦନ	8 10	
	•	Deg.	51 51 38.25	38.25 30.6 30.6	
	Gase	No.	253 254 255	256 257 253	

### MARINE THRUST BEARING - Phase I

## Table No. 21

# 011 - 2190 TEP at 115°F Inlet

R in.	9.5	22.5	37.5	50
L in.	4.75	11.25	18.75	25
t <sub>avg</sub> in.	1.236	2.924	4.88	6.50
θ <sub>T</sub> - degrees	51	51	51	51
n	6	6	6	6
r_ \$	50	50	50	50
rp % 9p %	50	50	50	50
N - RPM	100	100	100	100
$m_{\Theta} \times 10^{-6} in/in$	187	228	215	211
$m_r \times 10^{-6}$ in/in	25	27	25	23
$K \times 10^{-6} in^{-1}$	47	30	21	17
h <sub>min</sub> - in.	0.00040	0.00040	0.00040	0.00040
r %	50.2	46.5	49.2	49.0
e ‴ <b>≴</b>	81.7	75.5	70.7	68.7
T <sub>GR</sub> - °F	134	145	151	154
T <sub>AVG</sub> - °F	155	181	204	220
T <sub>MAX</sub> - °F	188	251	286	300
PAVG - P.S.I.	377	565	666	704
P P.S.I.	1203	3004	4625	5682
$W_{\rm TOT} \times 10^{-3}$ - Lbs.	68.1	572.0	1870	3520

TABLE NO. 22

51 1/2 " 0.D. x 32 " I.D. THRUST BEARING  $\left(\frac{1}{R}$  = 0.379  $\right)$ 

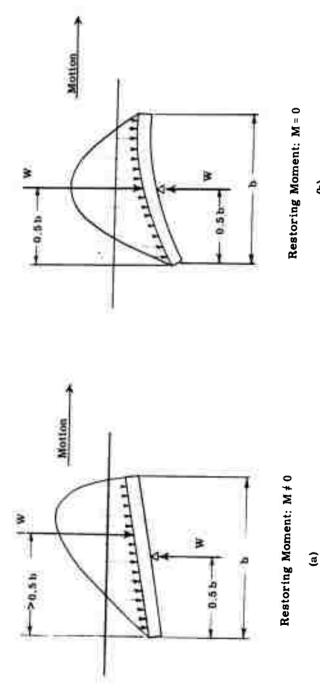
Effective Bearing Area = 1,085 Sq. In. (k = 0.85) Average Pad Thickness = 3.00 In.  $\left(\frac{t}{1844} = 0.117\right)$ Pluot Pitch Diameter = 42.25" In.  $\left(r_p \% = 52.61 \ p \% = 50\right)$ Effective Bearing Area - 1,085

Oil - 2190 T at 115°F Inlet

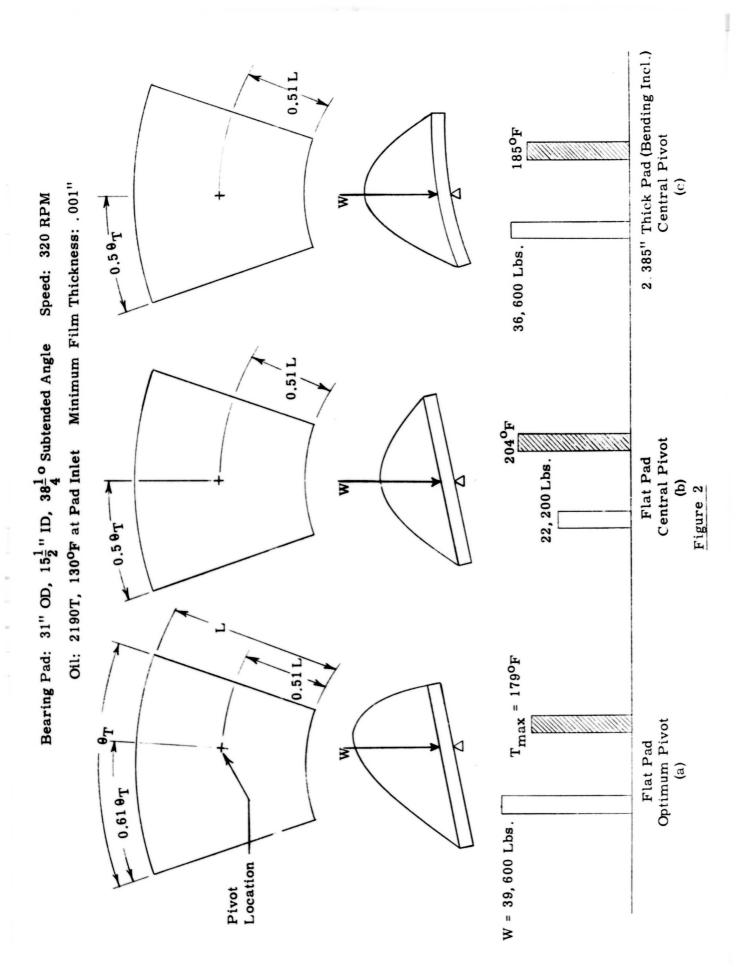
H.P.	2	47.5 48.9	40.8 42.5 47.7	125	152 42.6 52.0	49.2 42.3 47.1	751 171 171	130		
Q <sub>TOT</sub>		19.0 4. 15.3 4/			······					Male o de station canto a no
		1 2 2 2		4 <u>स्</u> री	1222		32.1	23.6		
6-01×101"	ž	296.9 296.1 269.1	916.1 1147.6	779.3 830.5 1264	1475 215.0 346.1	529.8 969.9 1271	287.6 661.0 767.6	1390 1740		
Pwx X	, su	610 1019	2663 4111 777	1841 2011 3939	5935 429 707	1155 2574 4005	566 1425 1713	3873	· · · · · · · · · · · · · · · · · · ·	
PAVG		202	844 1058 134	718 765 1165	1360 198 319	488 894 1172	265 265 708	1281		
TMAX	4º	174 194 202	262 312 182	2200	374 162 176	302 L 196	172 212 223	<b>297</b> 361		
TAVG	Ъ С	150 162 168	204 222 155	190 195 225	245 145 155	230 <b>2</b> 30 <b>2</b> 30 <b>3</b>	150 182 194	231 256		
Ľ,	0 10	8 5 F	166 166	152	165 128 130	141 163 165	128 146 153	165 165		
ĥ	t,									
¥. 0 <sup>6</sup>						·				
уя. 1, <sup>111</sup>					· ' <u>'</u>					
h nin	In	0.00151	0.00060 0.00040 0.00292	0.00120 0.00112 0.00060	0.00040 0.00246 C.00189	0.000131 0.00060 0.00040	0.00297 0.00140 0.00116	0,00060		
-18 2	10-6 in-	9 12 15	33.8	ក្ខន្លក	g,∞∞	248	6 15 18	33		
•0x106 = x106	1n/in	5 <b>8</b> 2		ဂိုလိုမှ	<b>6</b> 555	ů ů ů	-17 -17 -17	0 01		
<b>*</b> 0*10*	1n/in	125	198 208 185	215	266 132 125	145 170 176	175 183 183	212		
Z	RPM	888	888	007 007 007	300 <b>60</b>	8 <b>8 8</b>	800 700 700 700	80 <b>7</b>		
No. of	Pads	999	222	900	122	222	222	12		
•	Deg.	30.6 30.6	30.6 30.6	<b>30.6</b> 30.6 30.6	30.6 25.5 25.5	25.5	25.55	25.5		
đ	No.	\$\$ <b>\$</b> \$ <b>\$</b>	265 265 265 265	<b>\$</b> 22	272 273 274	212 212 212	273 279 280	281 282		

FIGURES

Figure 1 MOMENT EQUILIBRIUM



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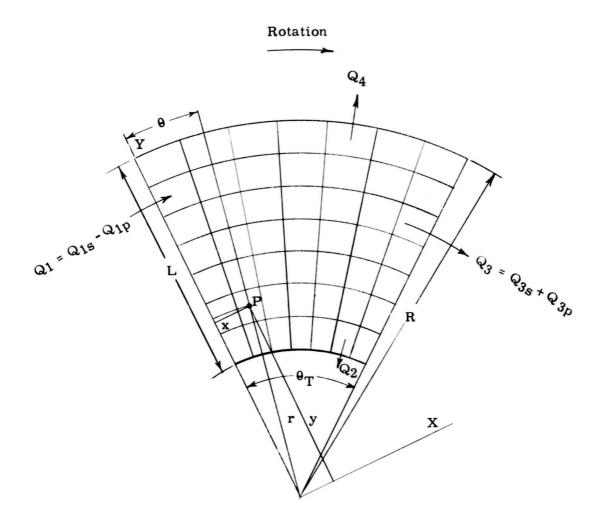
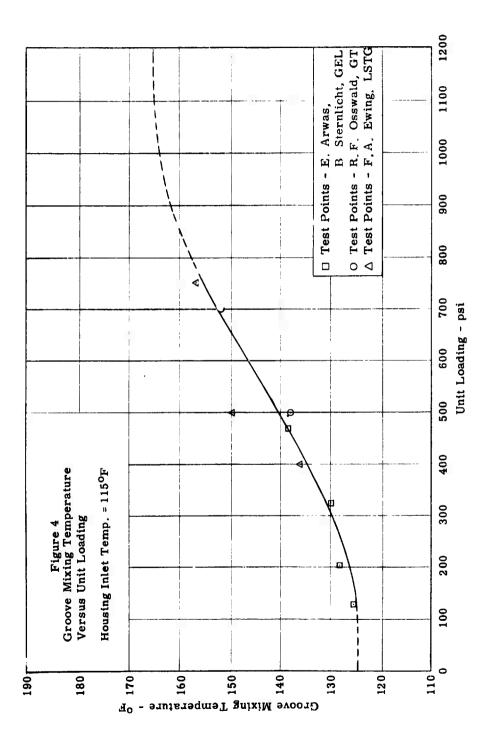


Figure 3 Co-ordinate System

•



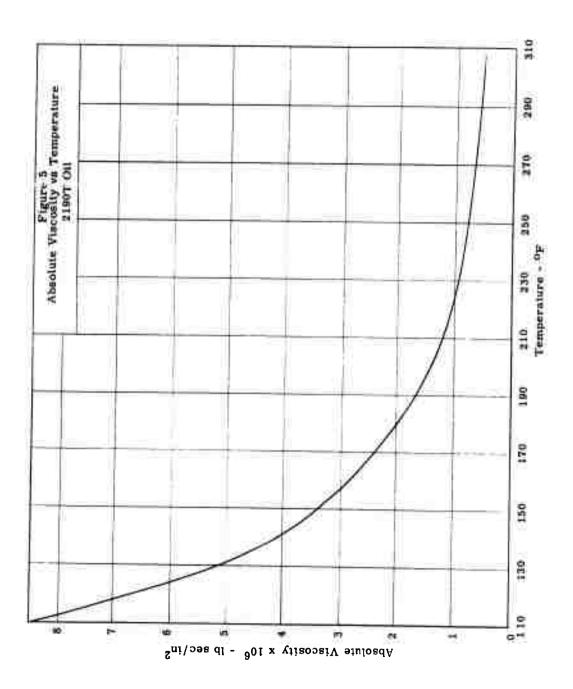


Figure 6 MESH NOTATION

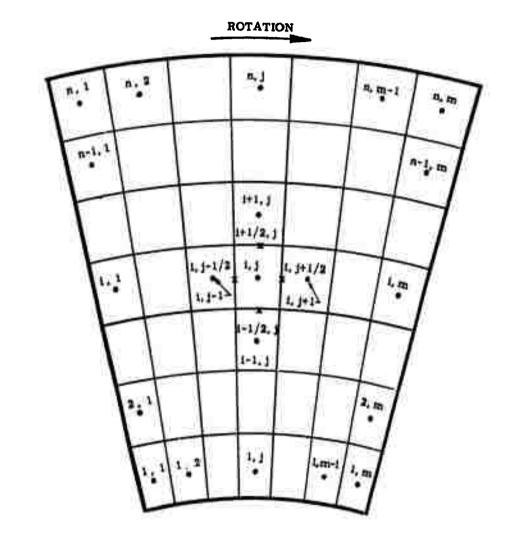
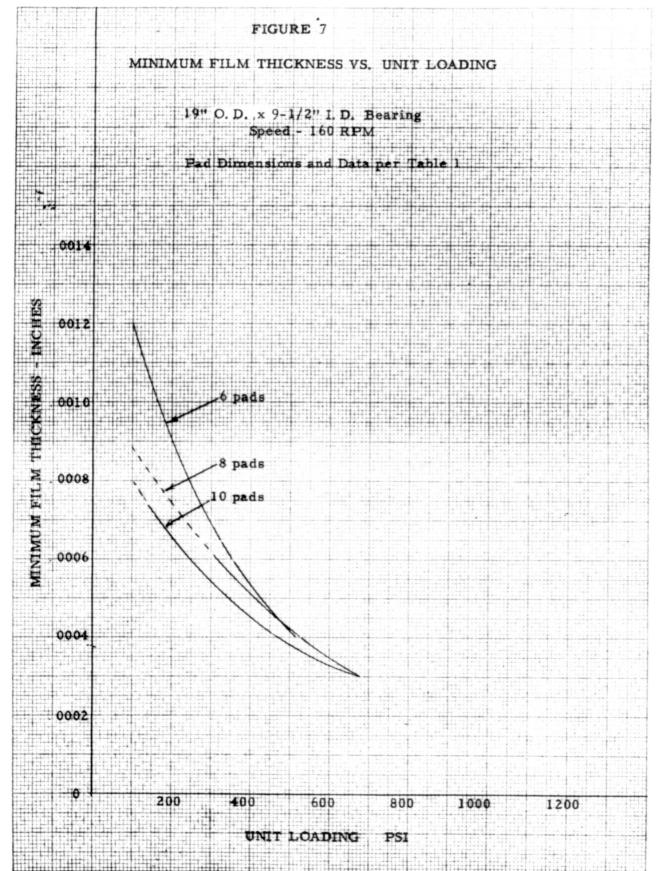
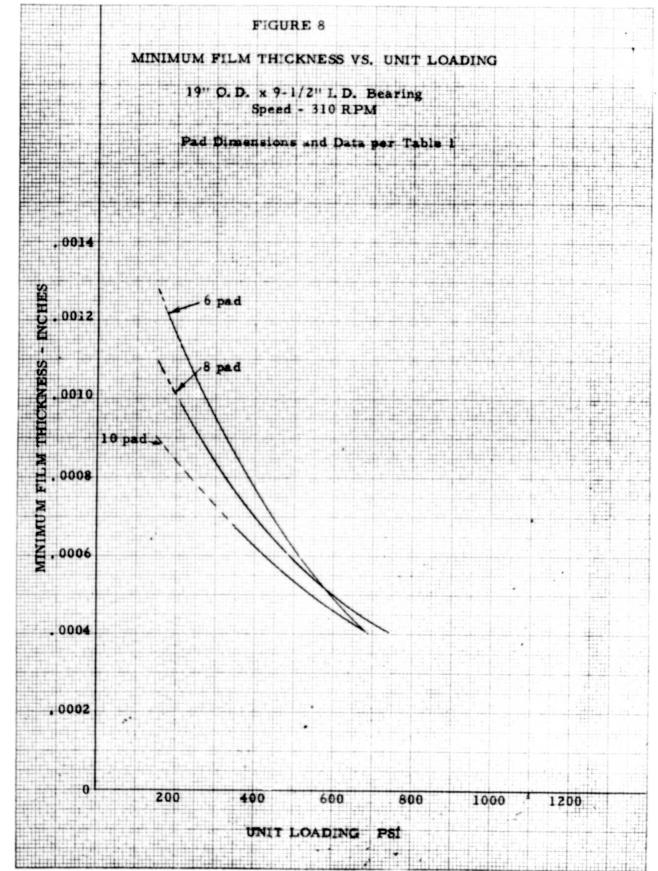


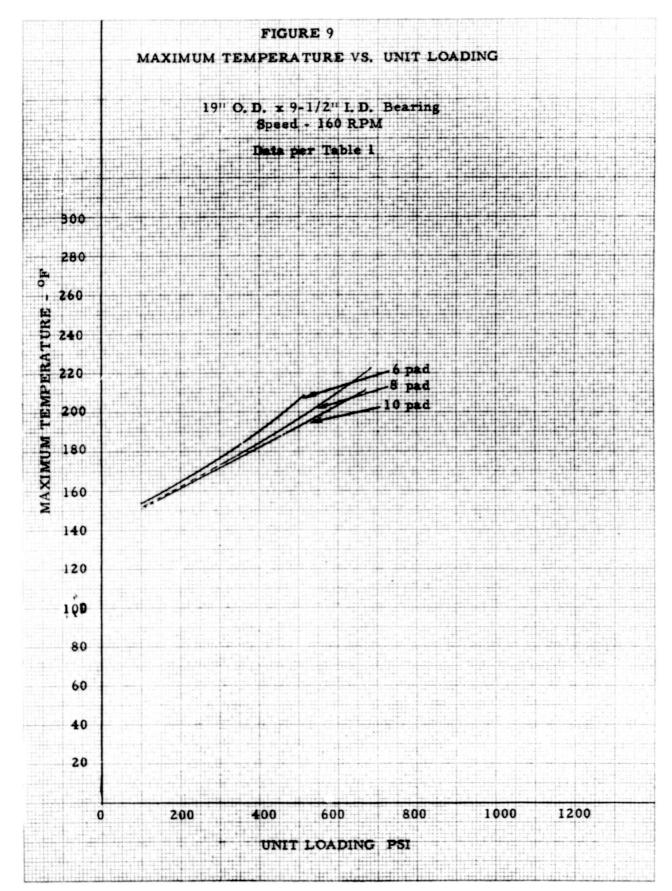
Figure 6

۲.



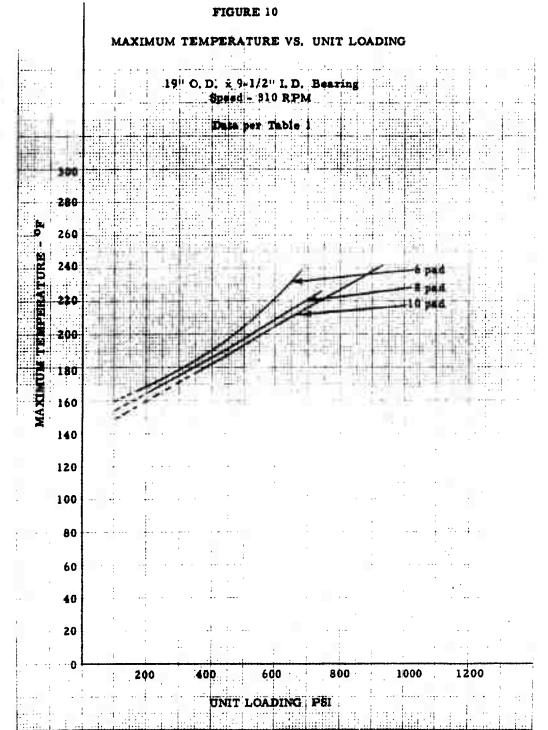


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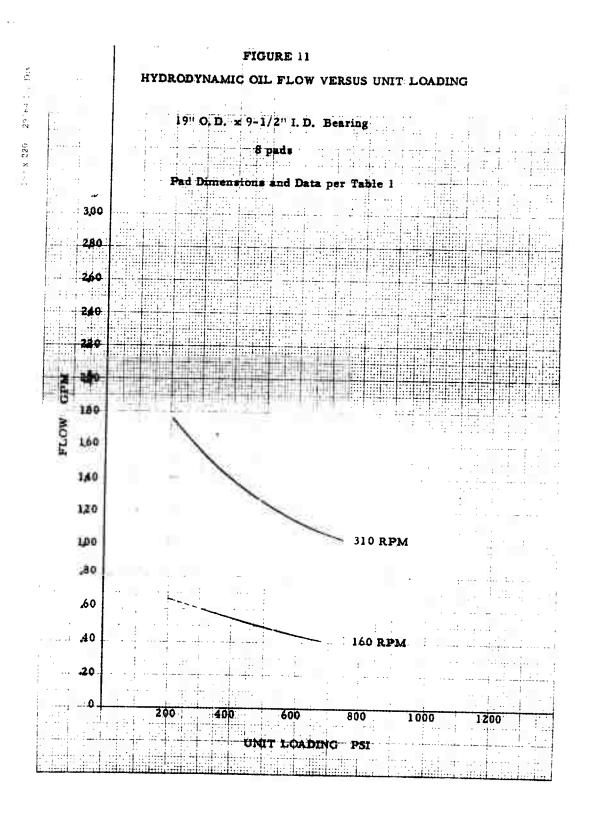


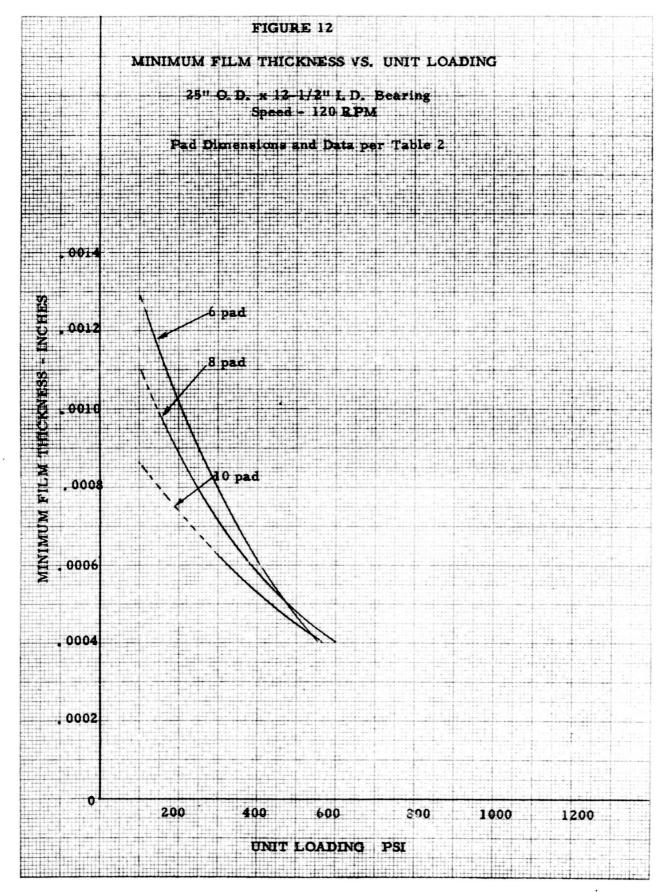
160 x 220 29/64 In.

4 In. Div.

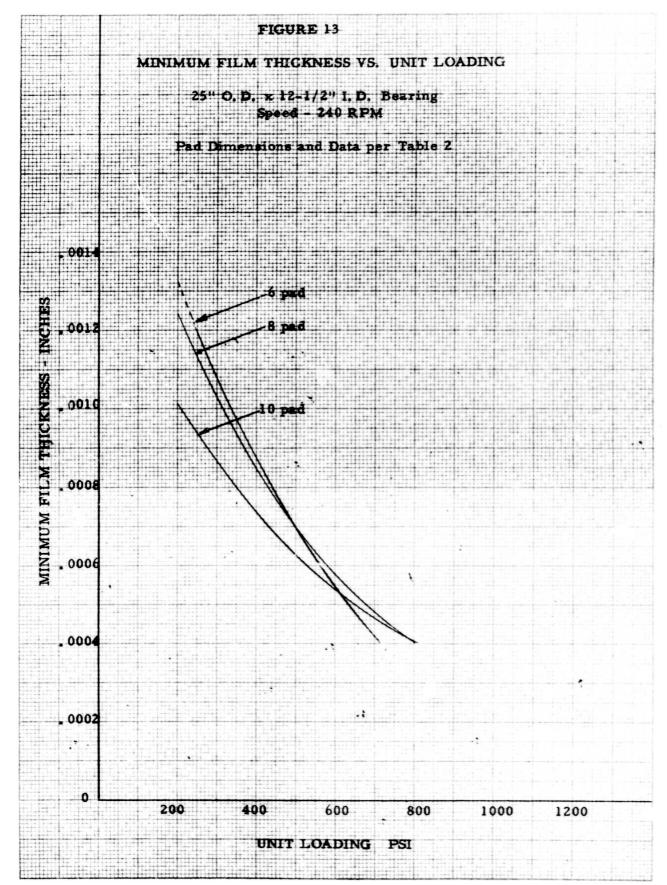


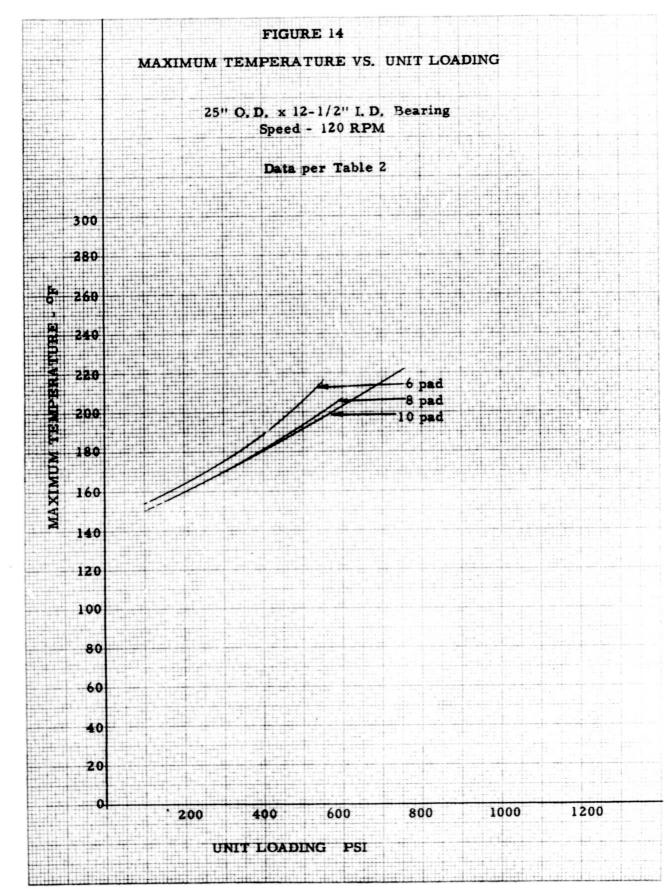
23/64 In 160 x 220



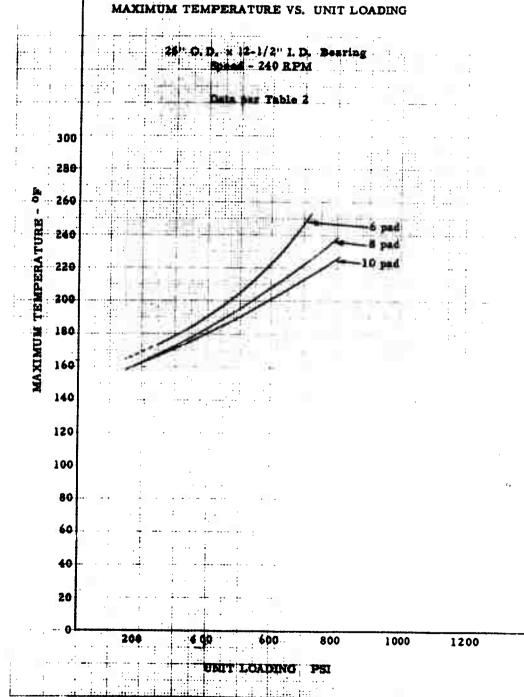


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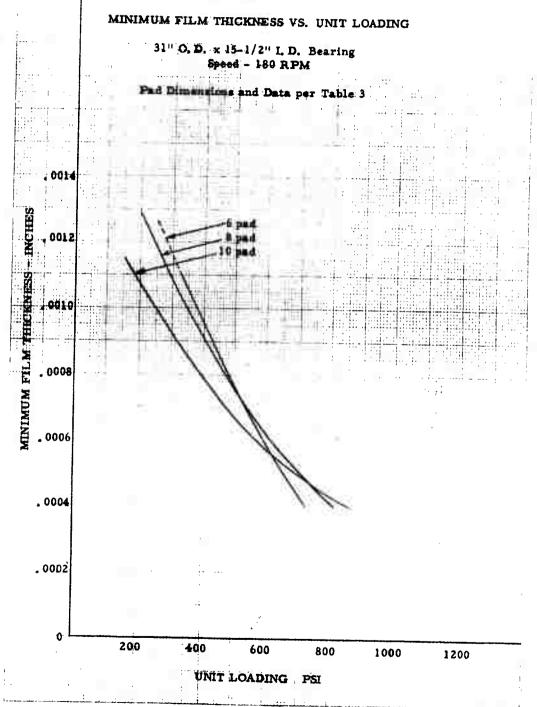


:50 x 220 25, +:

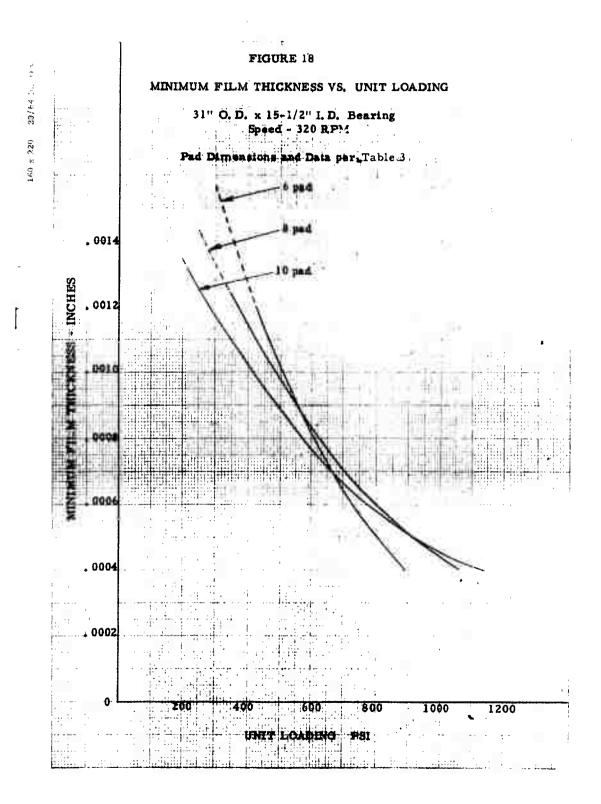
FIGURE 16 HYDRODYNAMIC OLL FLOW VERSUS UNIT LOADING 25" Q.D. x 12+1/2" 1.D. Bearing 8 Pade 3.3 Pad Dimansions and Data per Table 2 8.0 2.8 2.6 2, 4 2.2 2.0 2 d 0 1. % 1.6 240 RPM 1.4 1.2 1.0 . 8 120 RPM .6 . 4 . 2 ...... 1200 2.00 400 600 800 1000

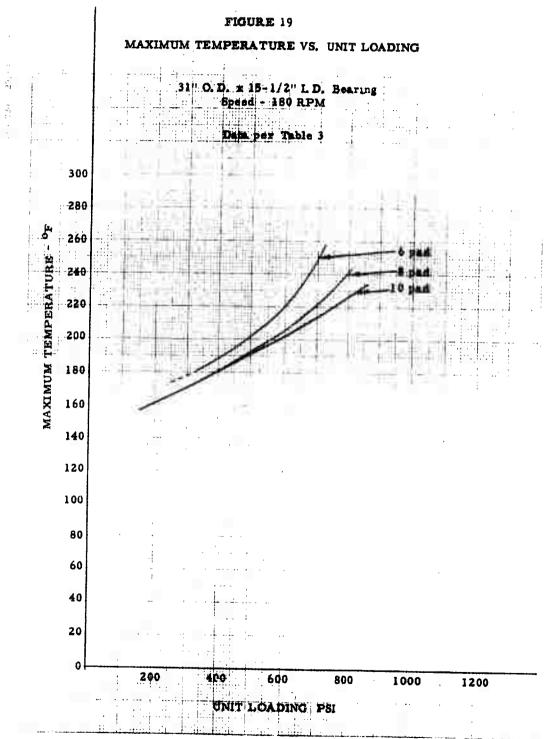
UNIT LOADING PSI

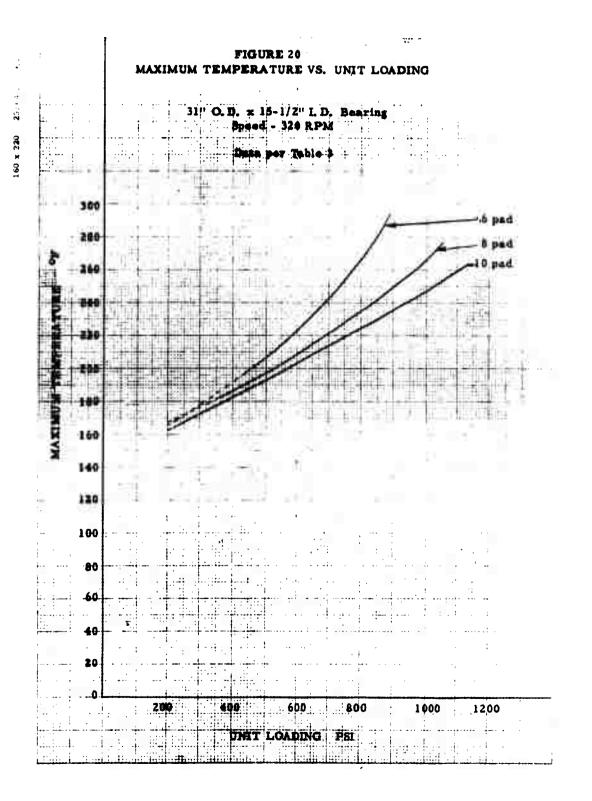


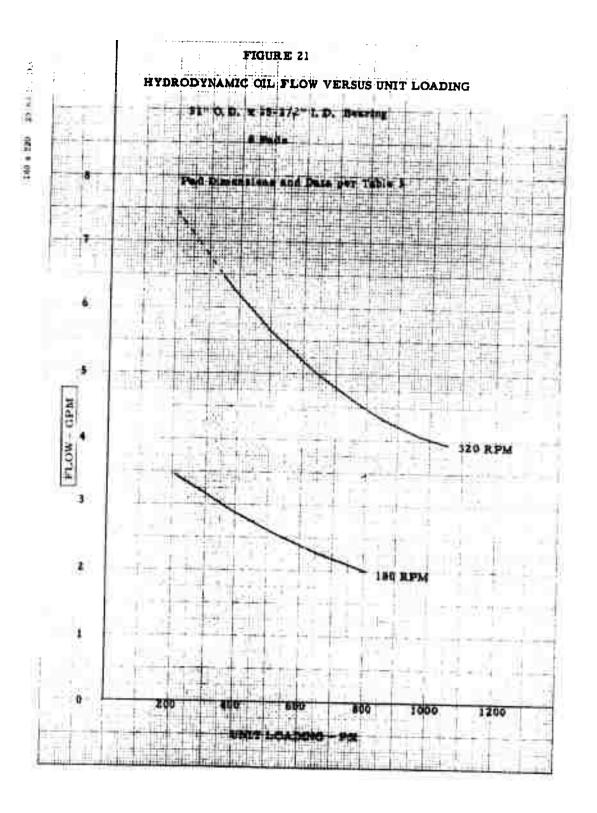


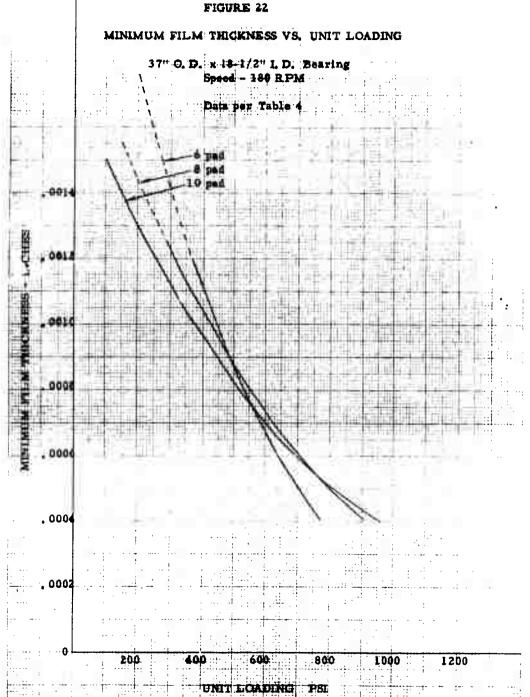
160 x 220 23, 6 + j.





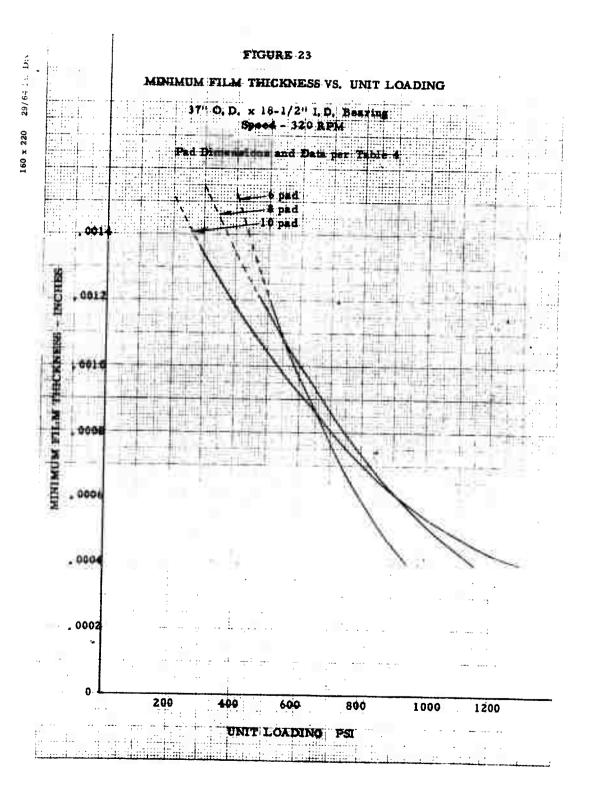


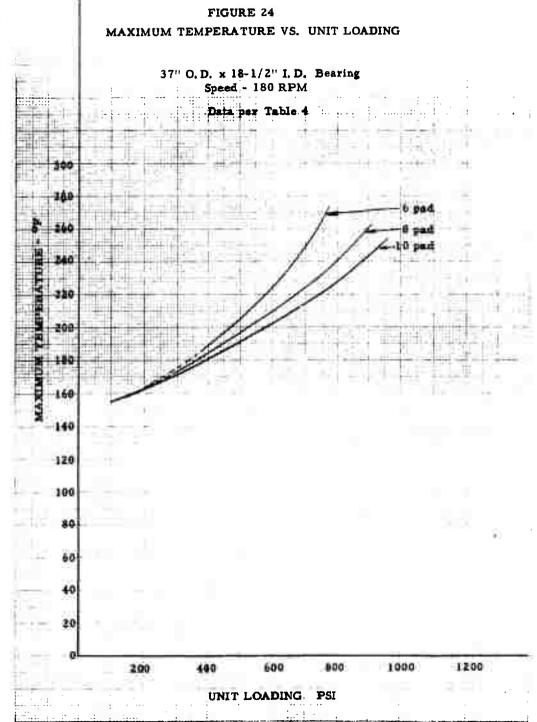




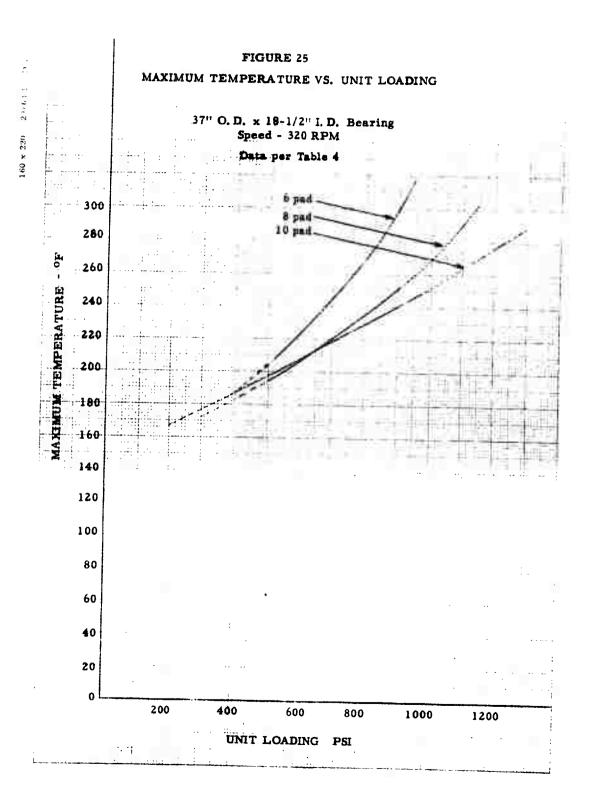
22/64 14 160 x 220

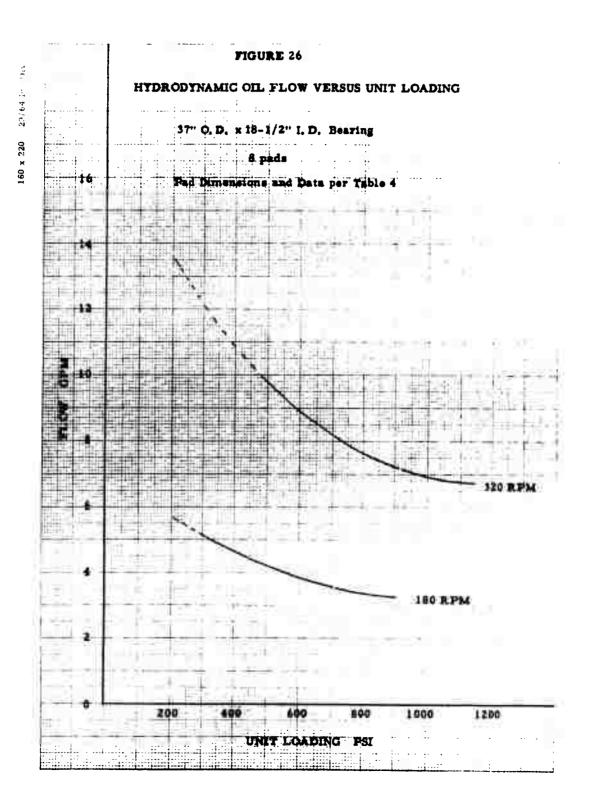
i:Til:

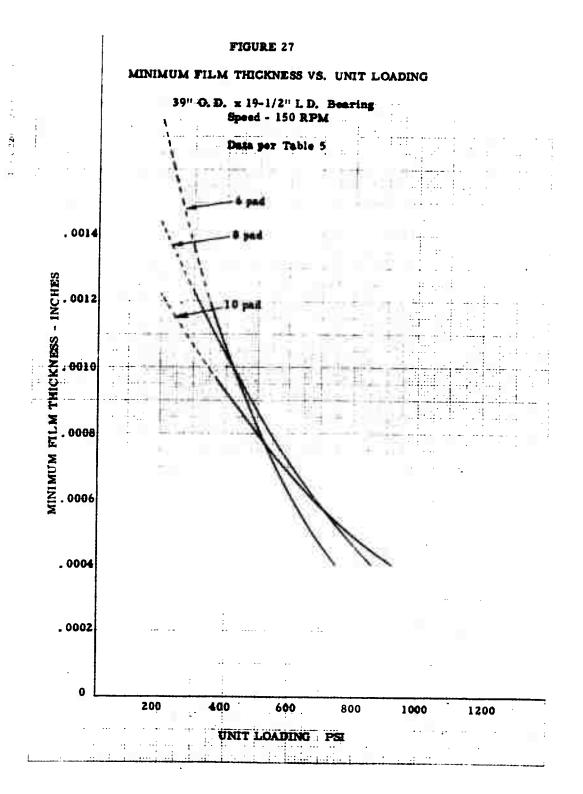


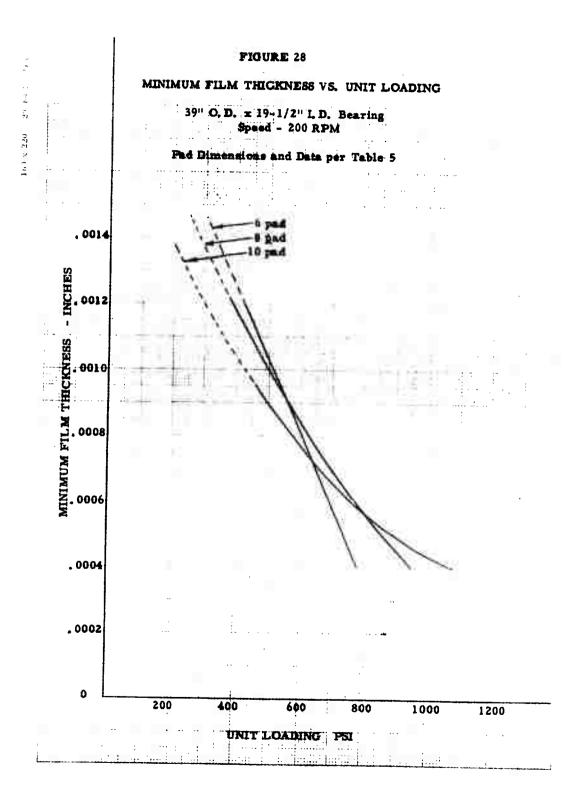


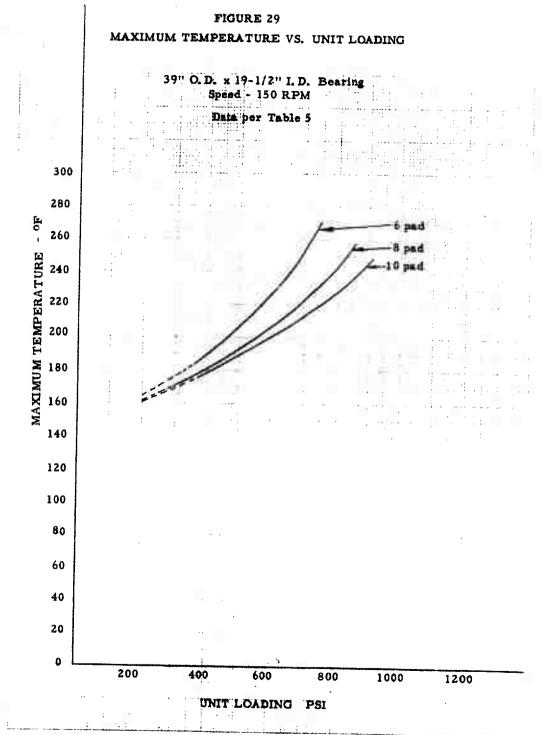
160 x 220 29/64 in Div





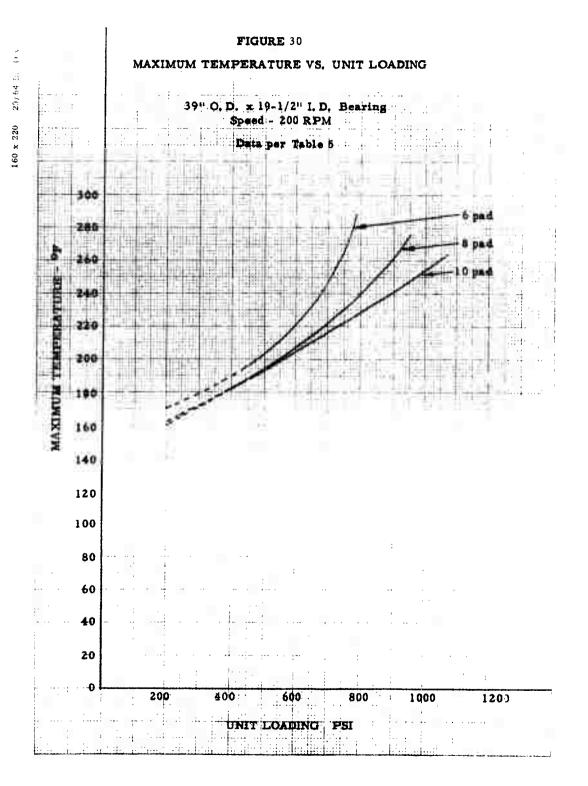


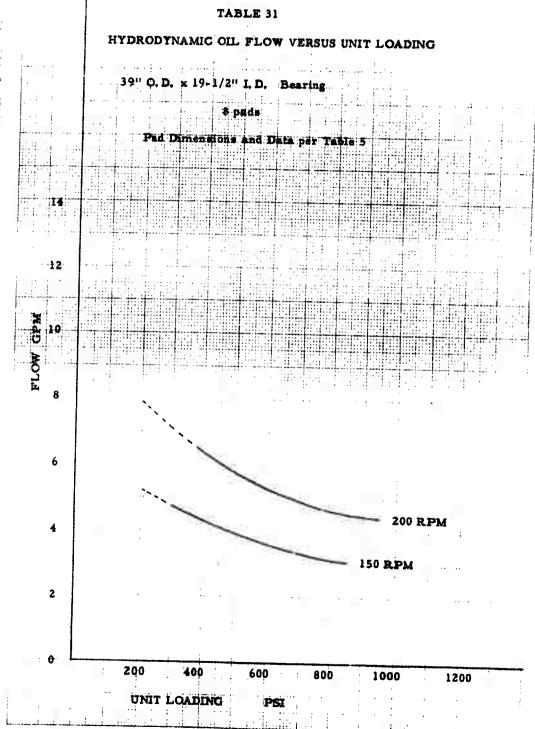




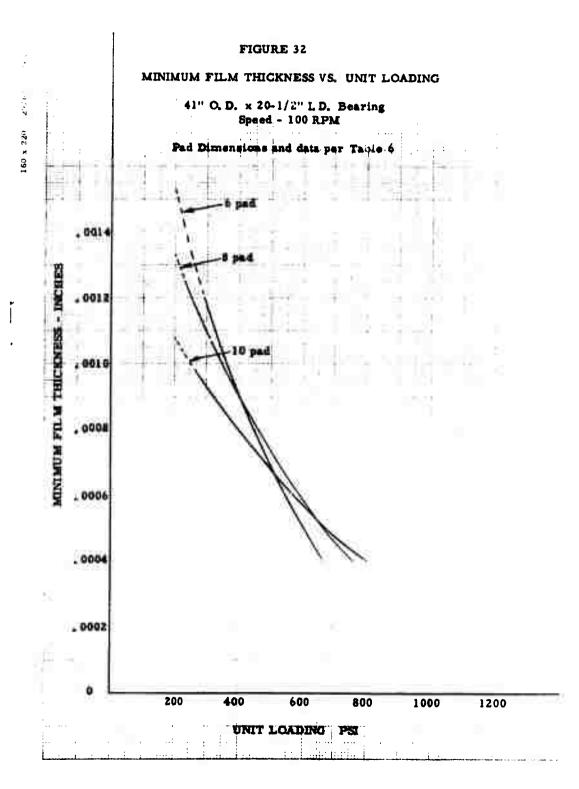
IoJ X 220 2+++

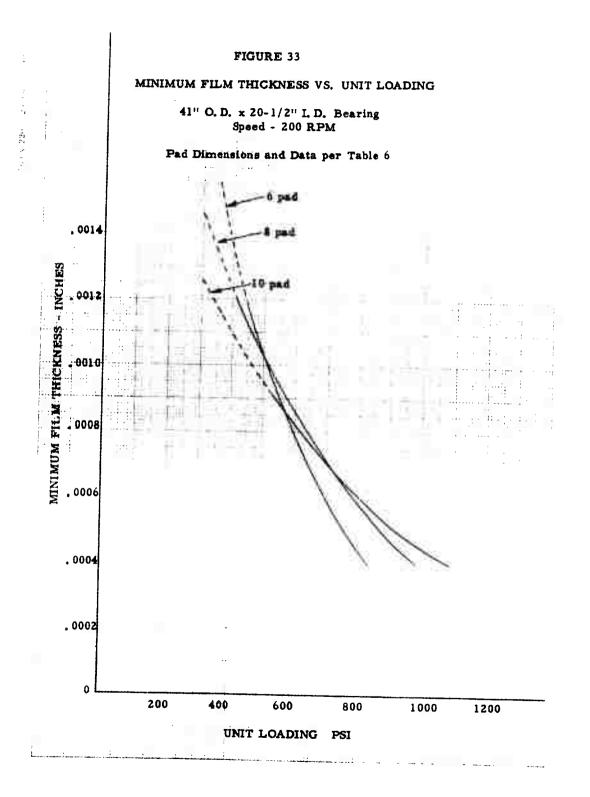
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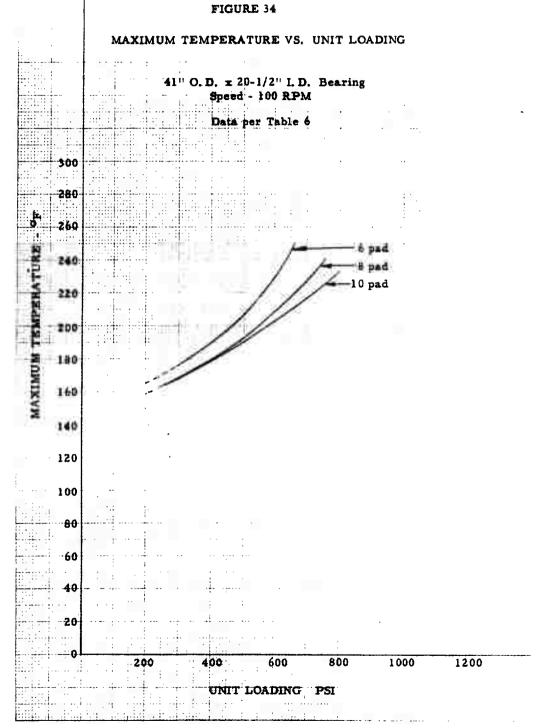




16J x 220 27.144







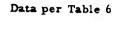
160 x 220 29/64 In

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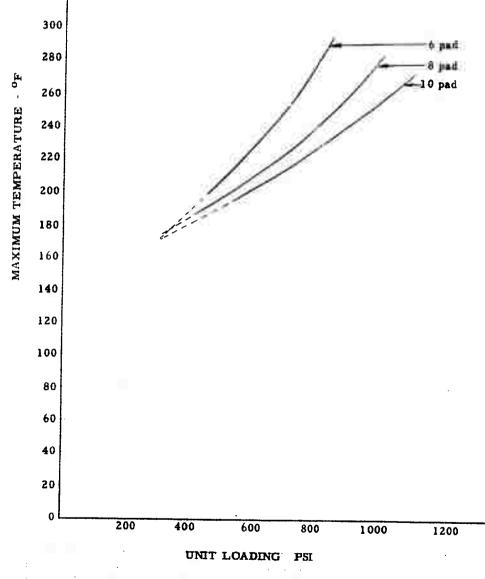


MAXIMUM TEMPERATURE VS. UNIT LOADING

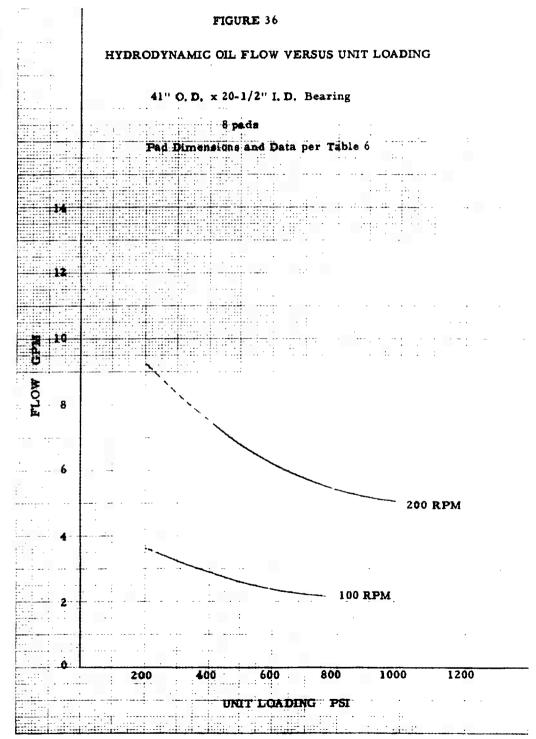
41" O. D. x 20-1/2" I. D. Bearing Speed - 200 RPM



.

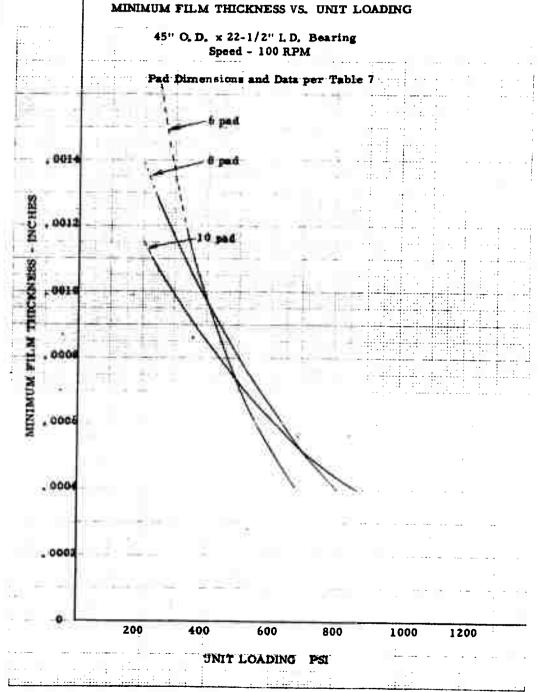


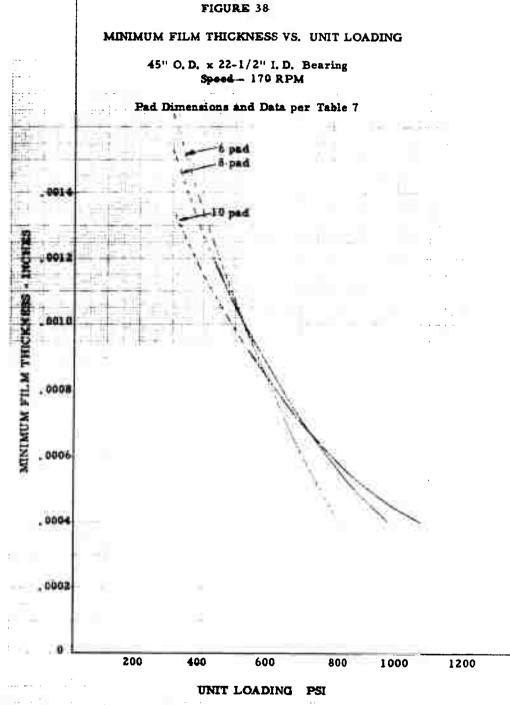
16. 5 2.



23/64 In. 13.V 160 x 220

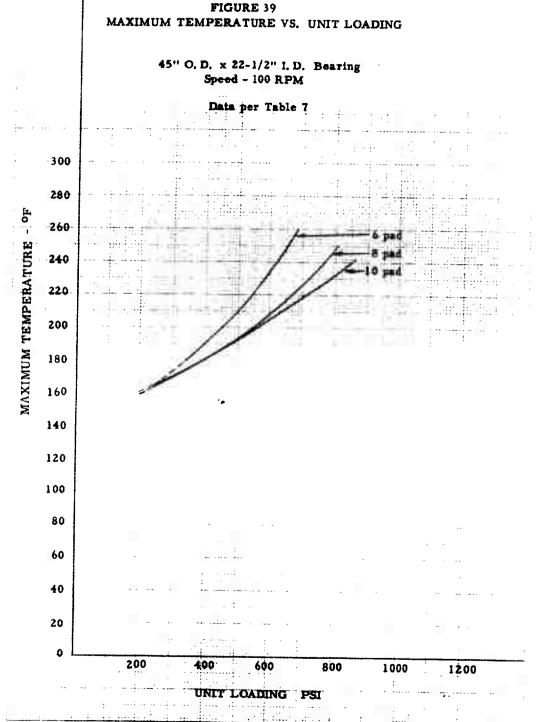




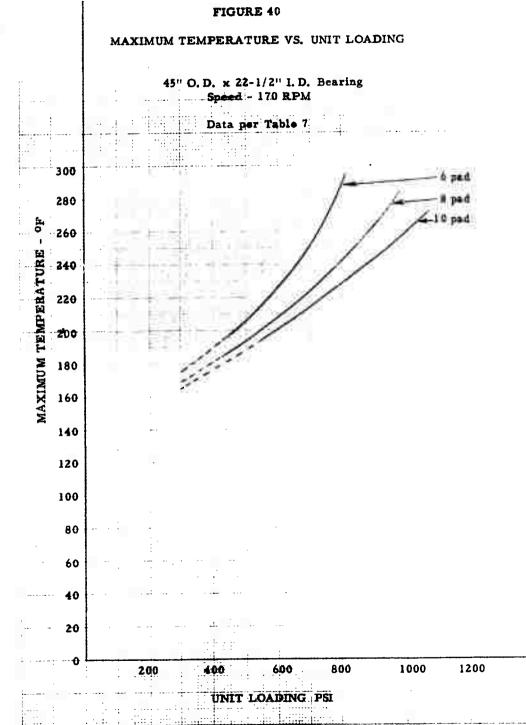


160 x 220 24/1

160

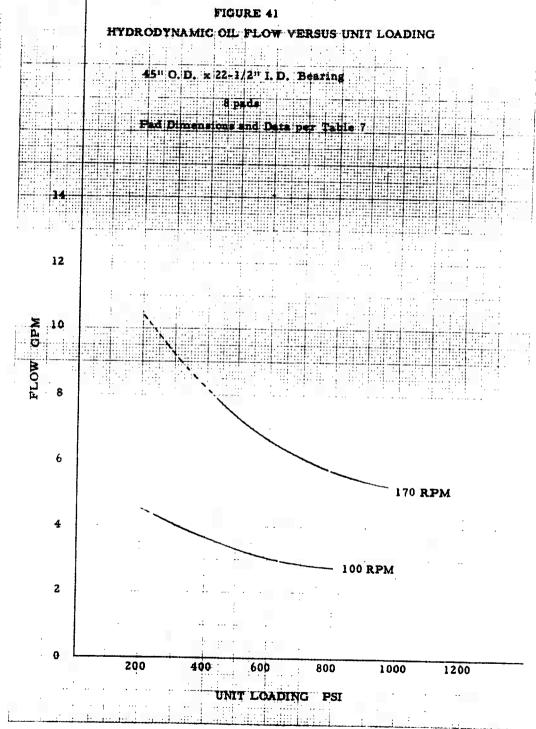


52 × 69

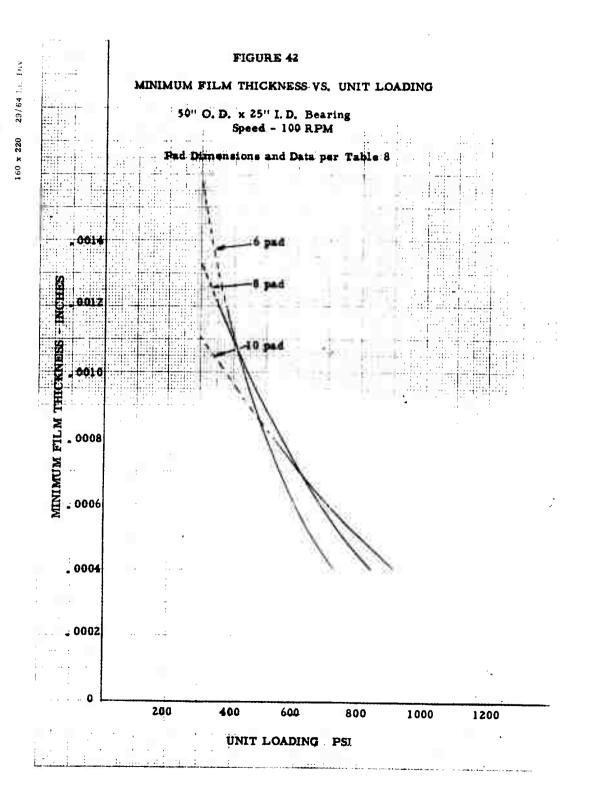


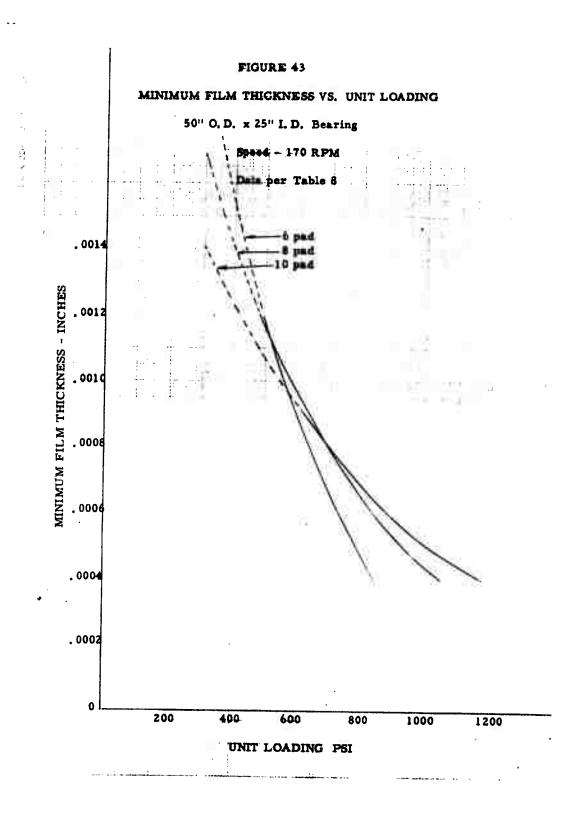
160 x 220

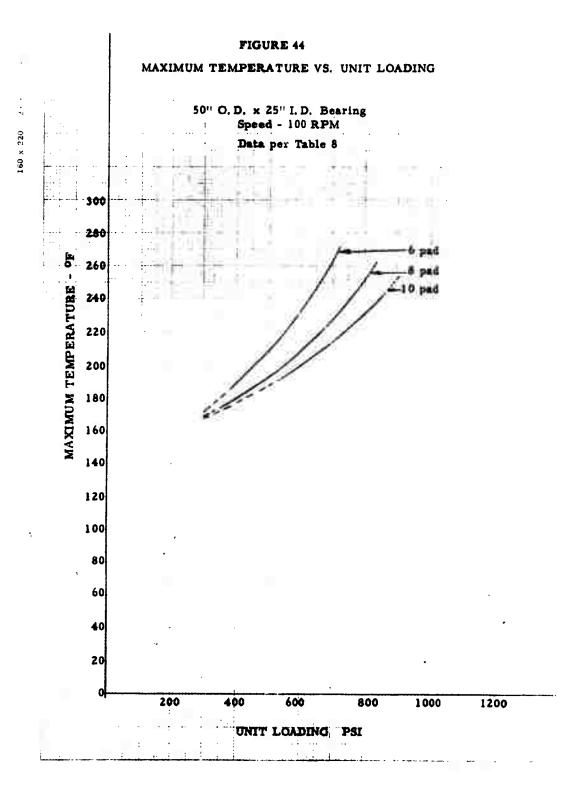
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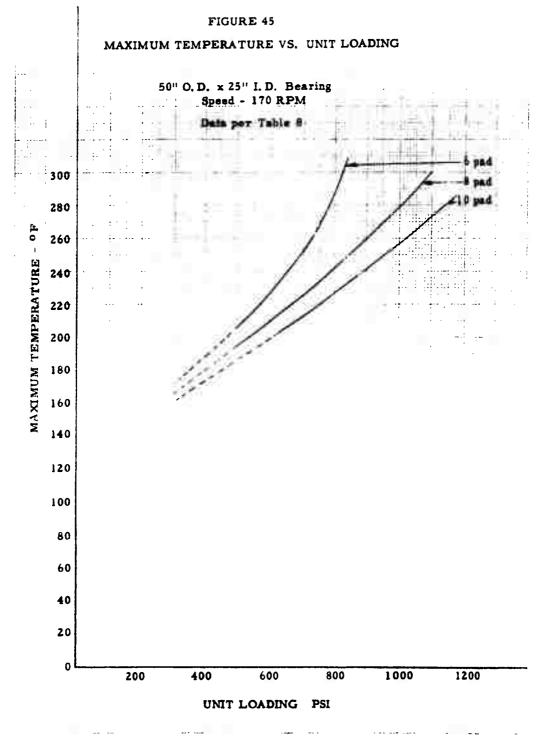


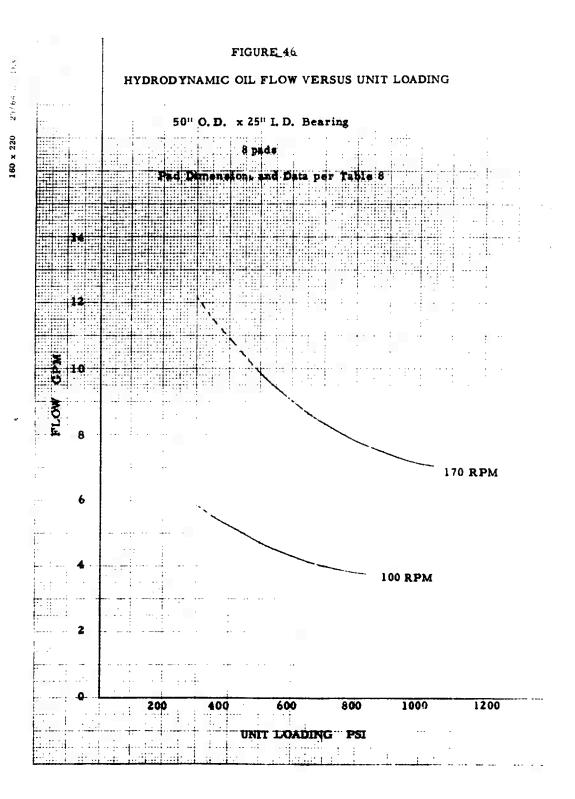
160 x 220 23/64 In. D.V.

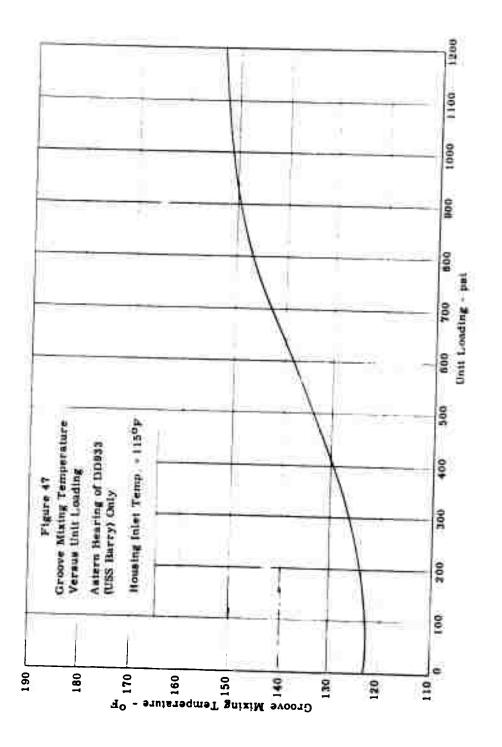




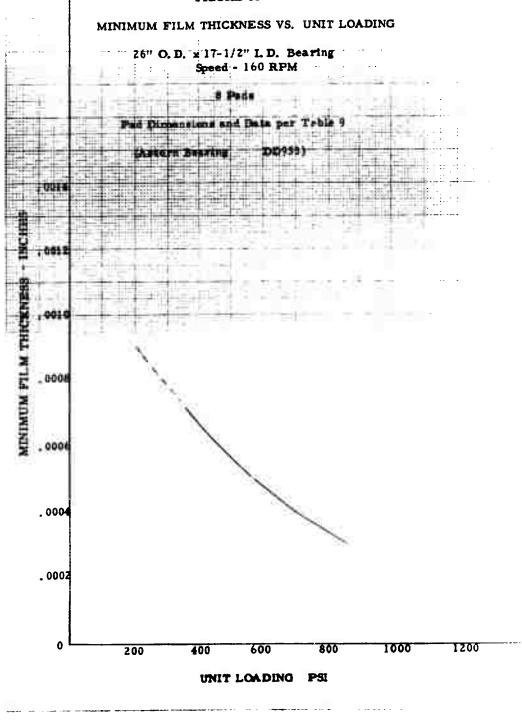


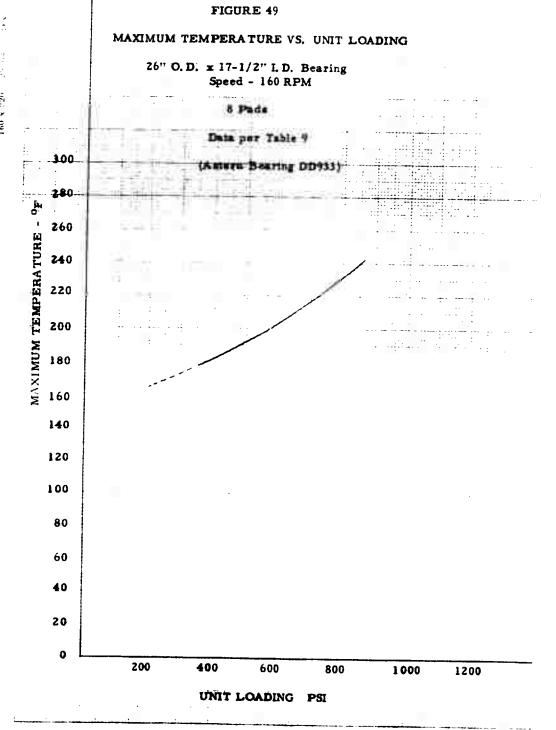


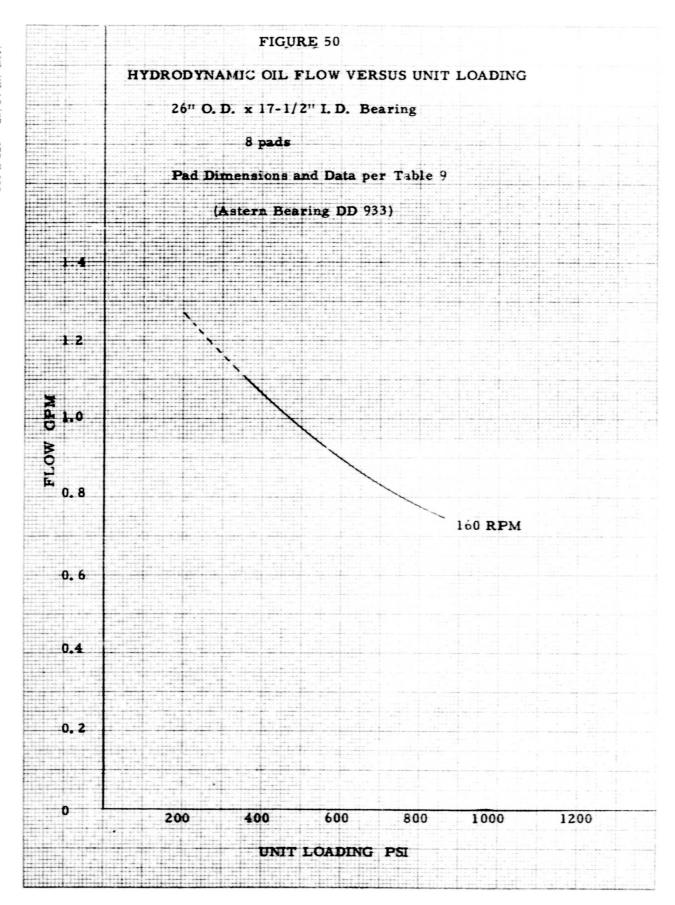






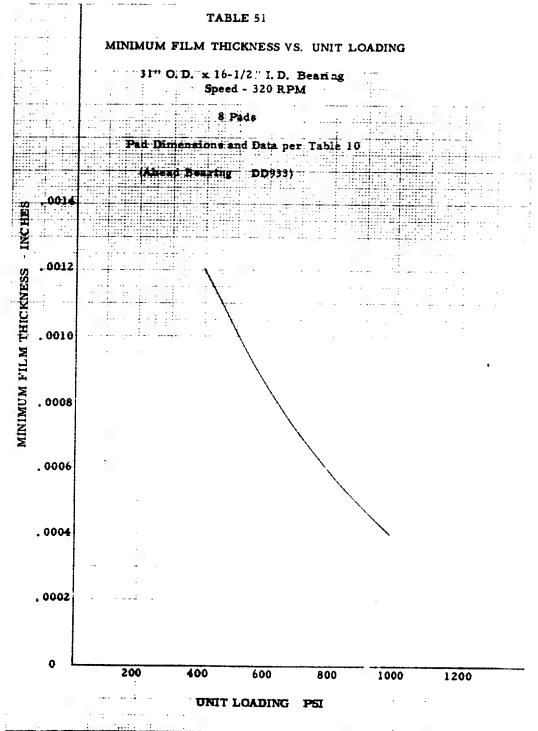






160 x 220 29/64 In. Div.

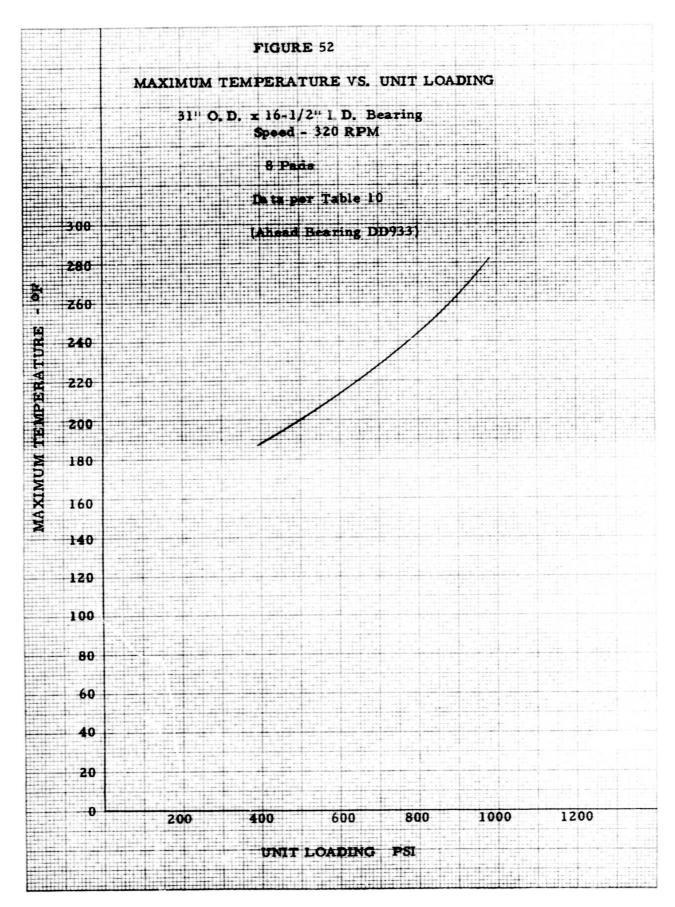
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20 24/44 In

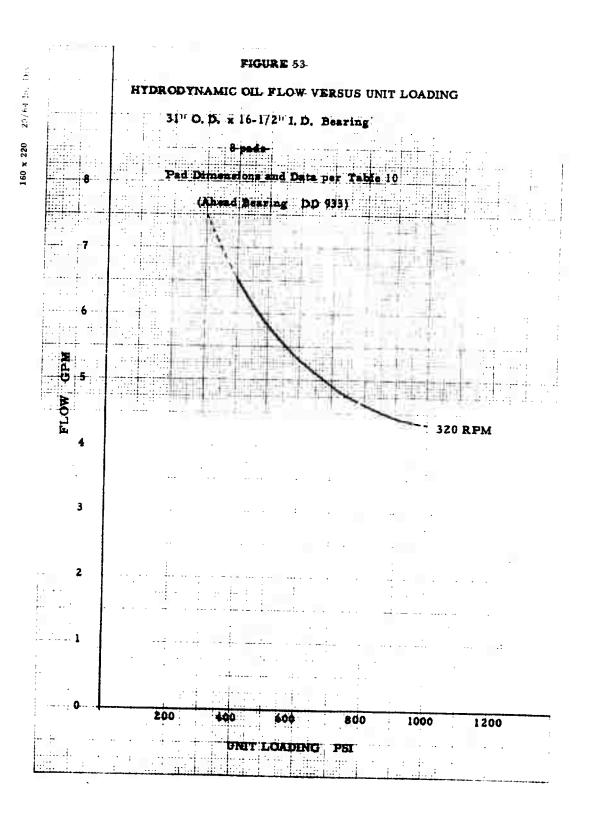
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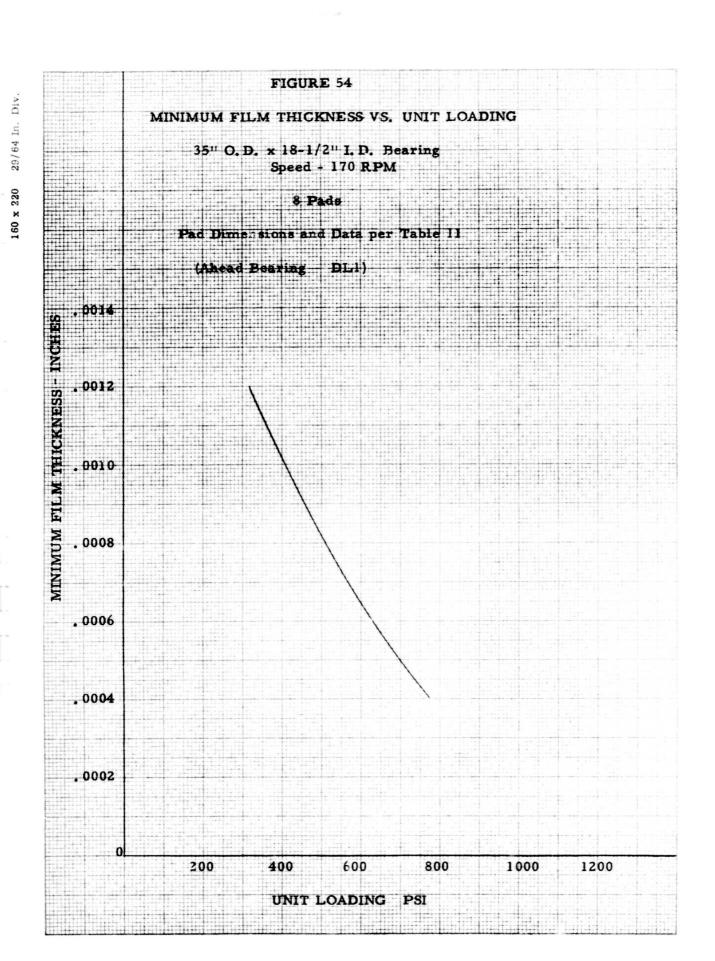
160 x 220

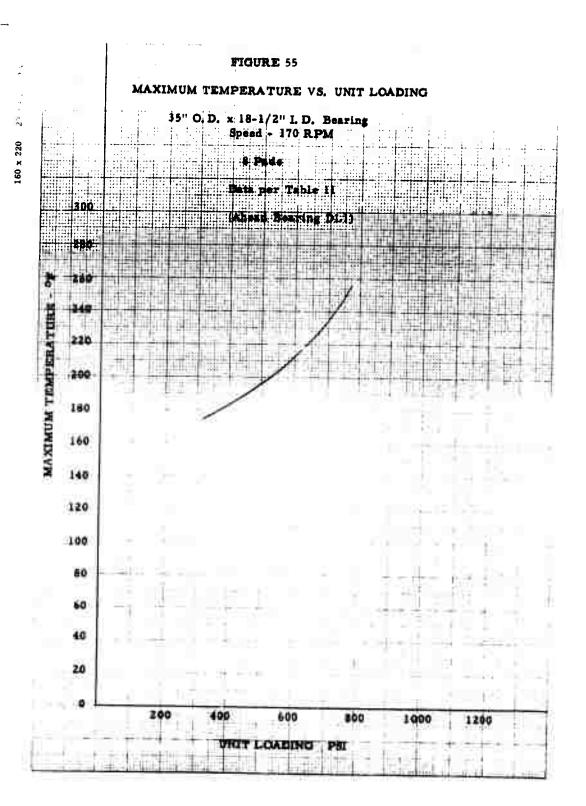


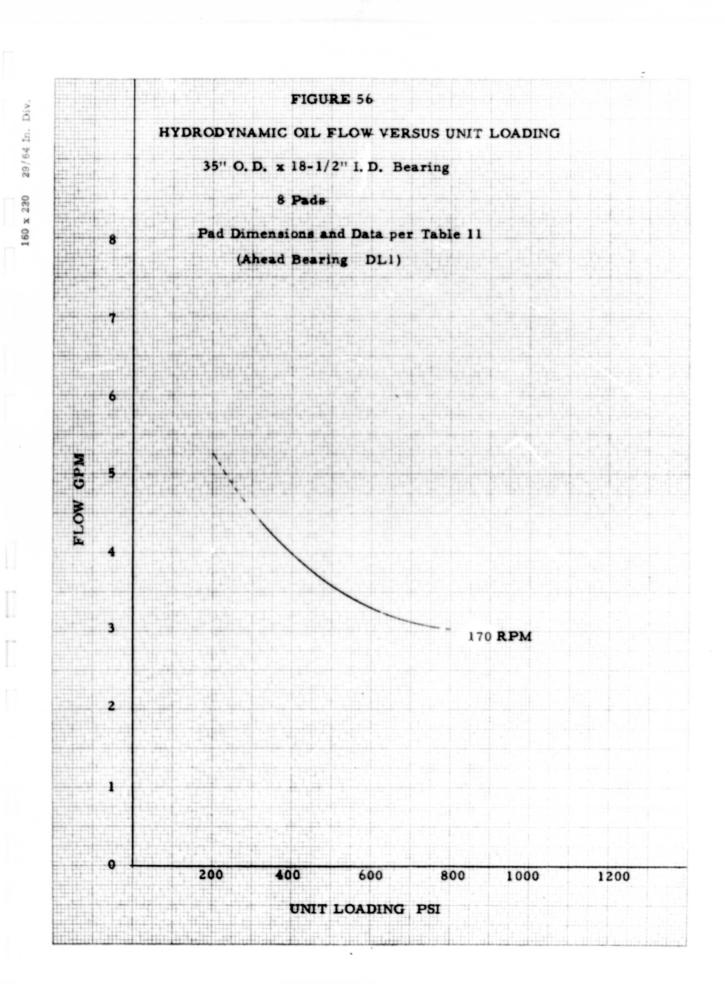
160 x 220 29/64 In. Div.

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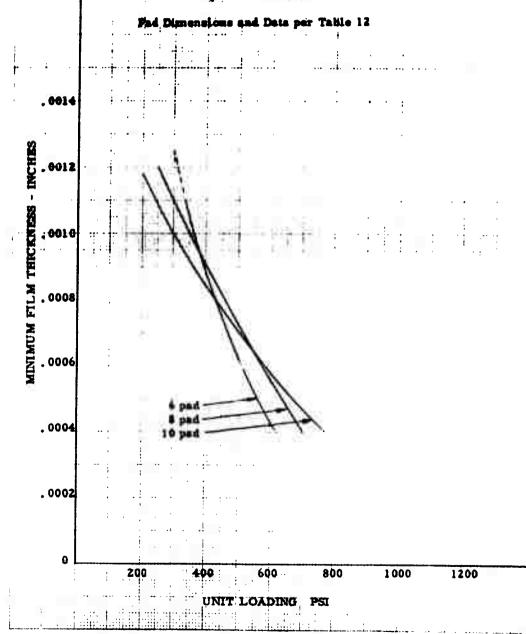


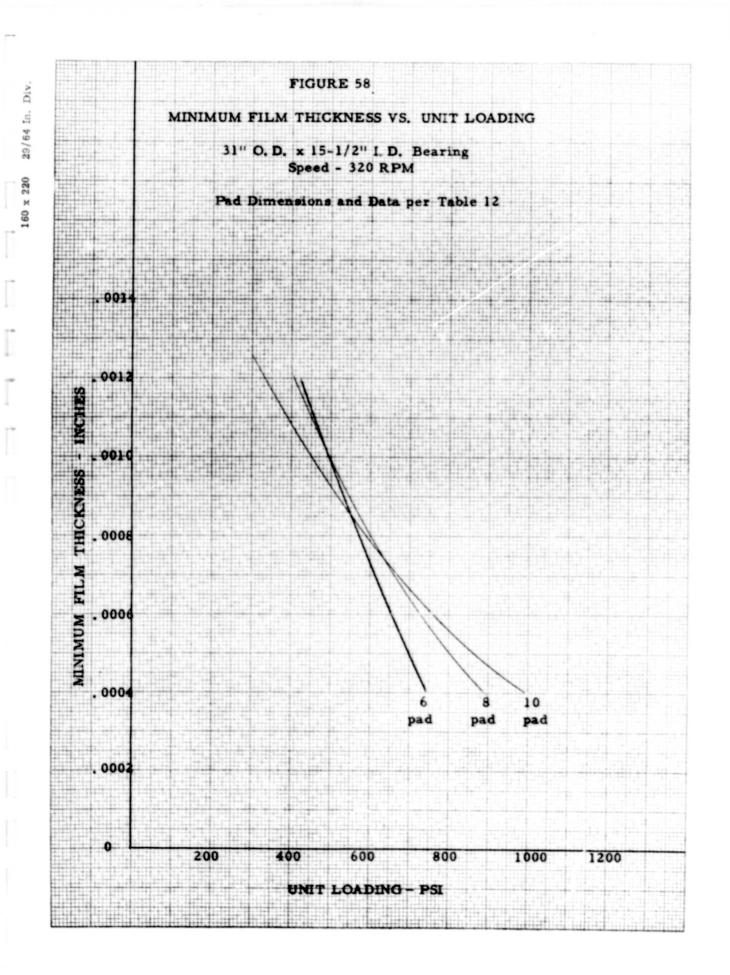
#### FIGURE 57

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MINIMUM FILM THICKNESS VS. UNIT LOADING

31" O.D. x 15-1/2" 1.D. Bearing. Speed - 189 RPM



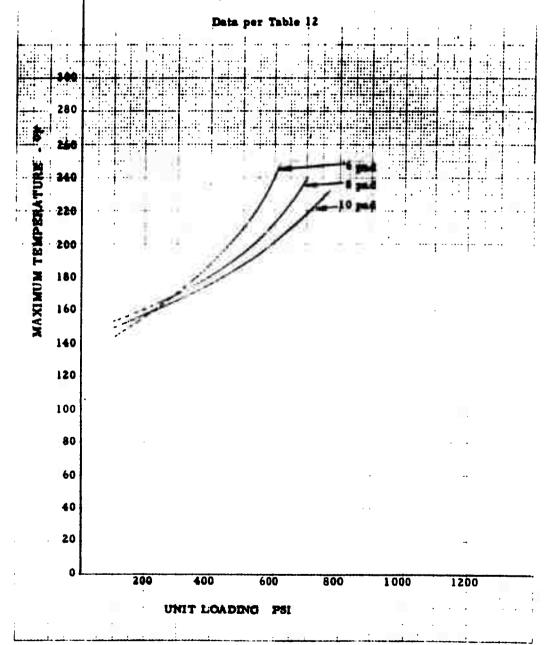


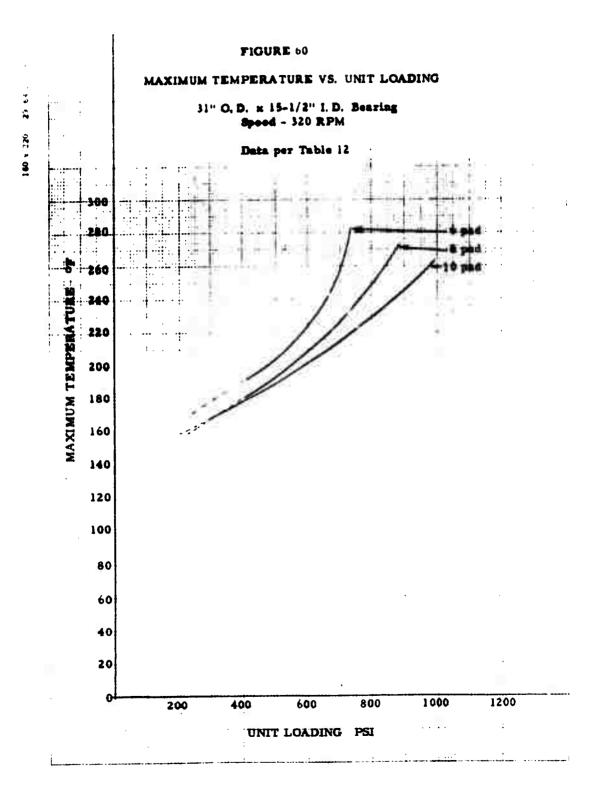


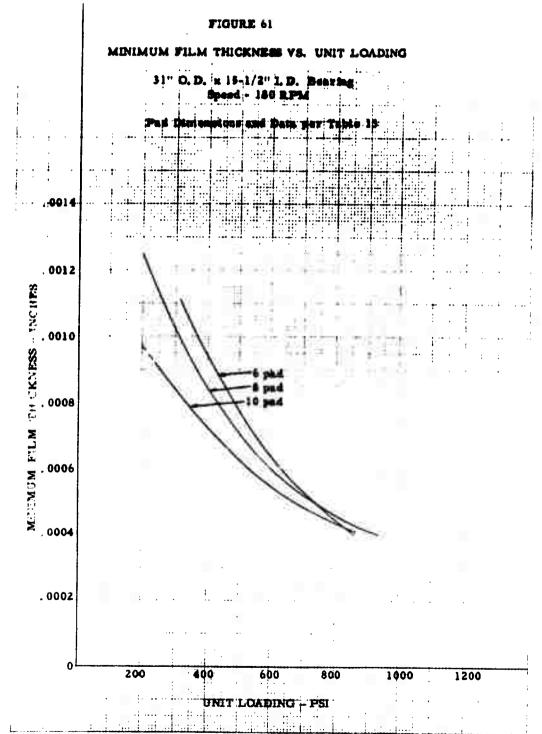
160 + -2-

### MAXIMUM TEMPERATURE VS. UNIT LOADING

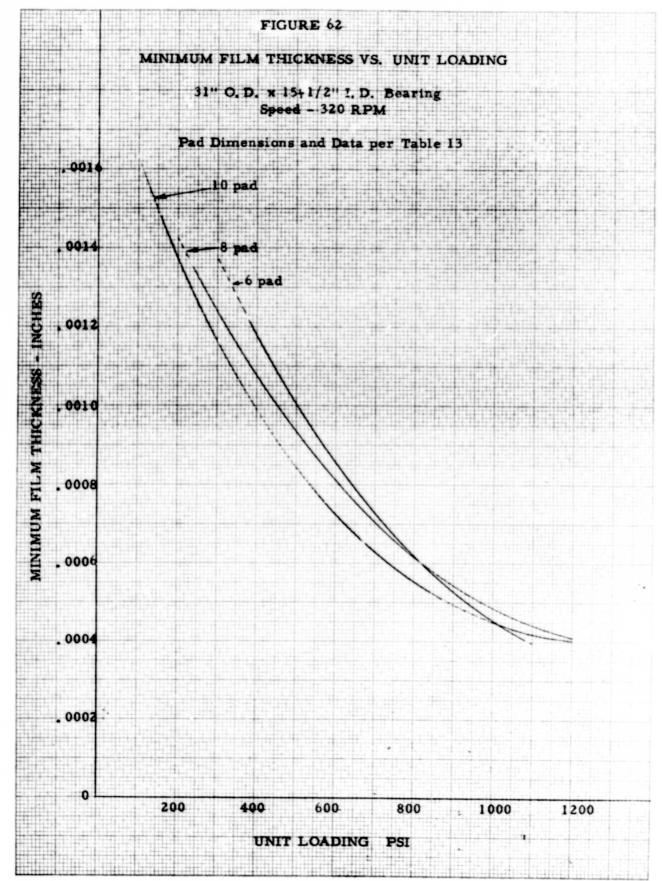
## 31" Ο. D. π 15-1/2" I. D. Bearing Speed - 180 RPM





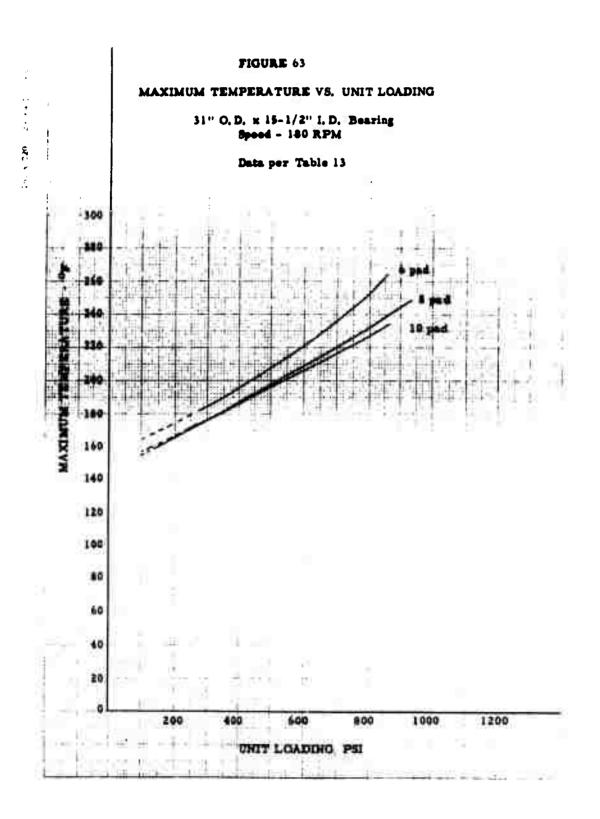


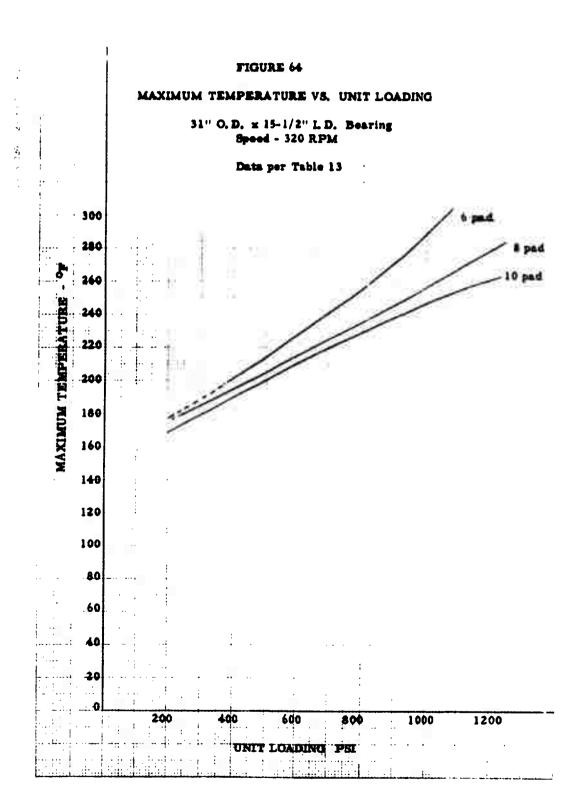
2 P I 9 ]

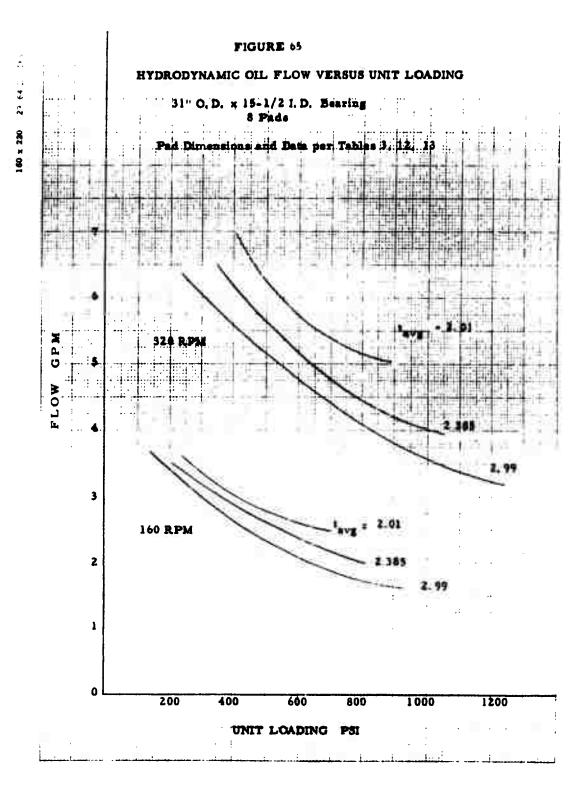


160 x 220 29/64 In. Div.

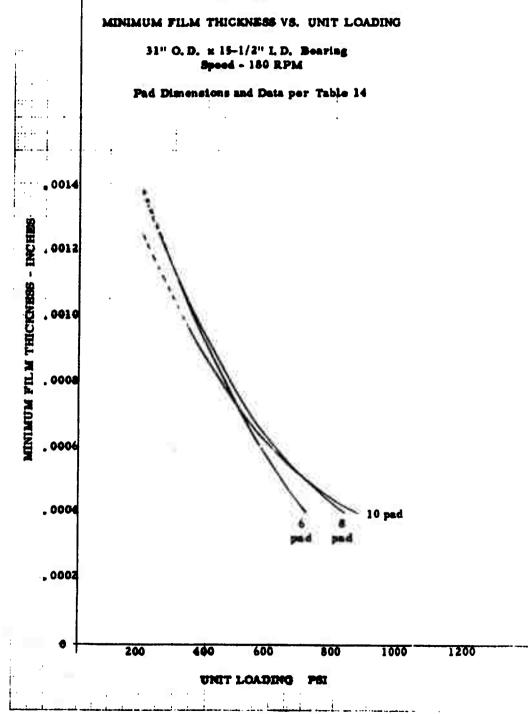
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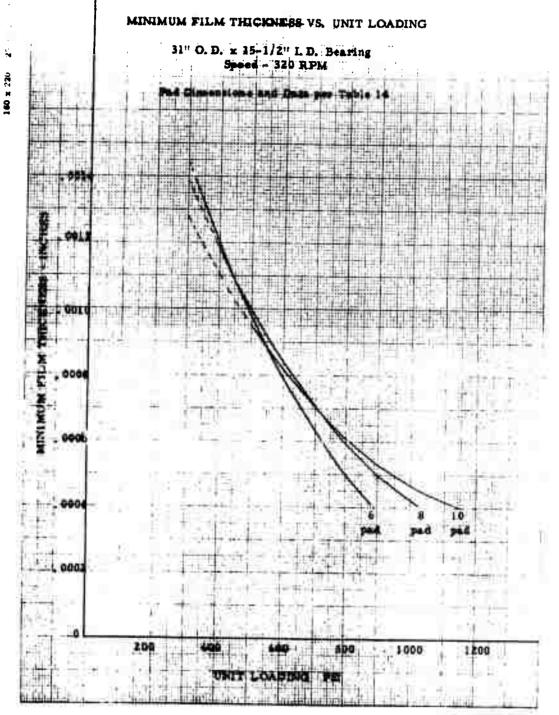


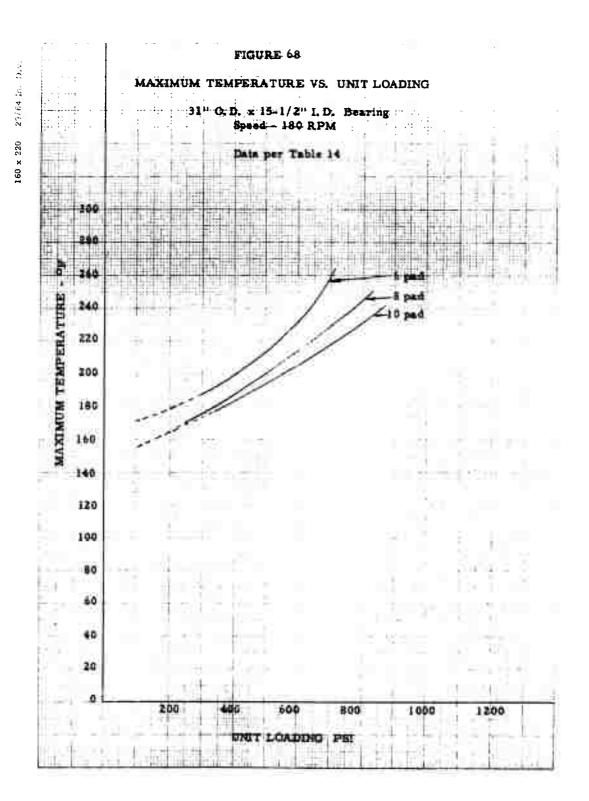


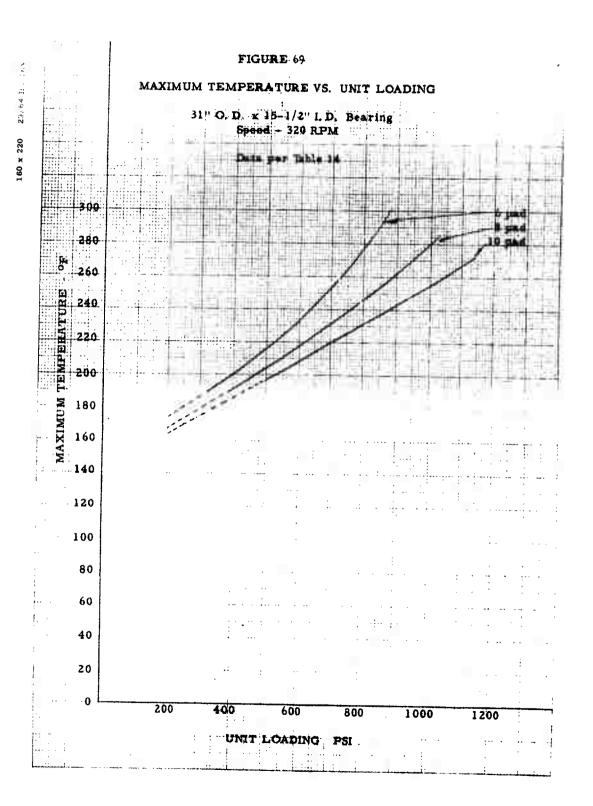


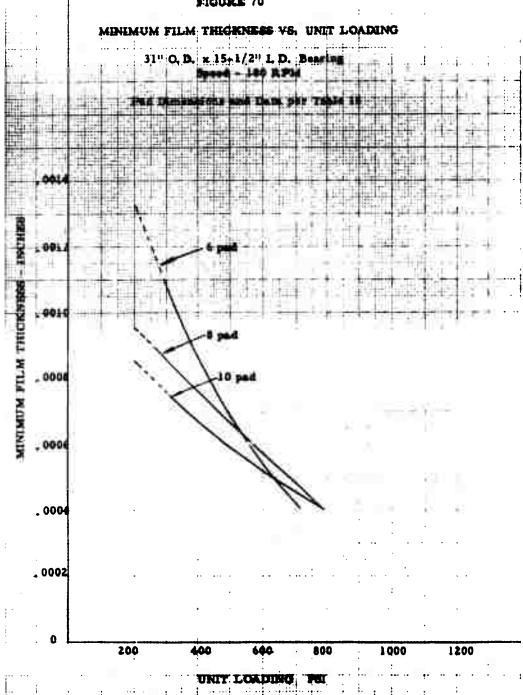
160 x 220 2 . t.











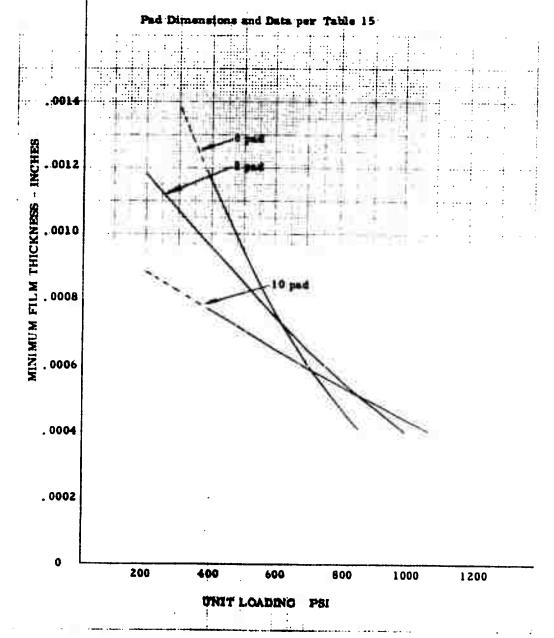
160 x 220 29/64 In. Div

### FIGURE 70

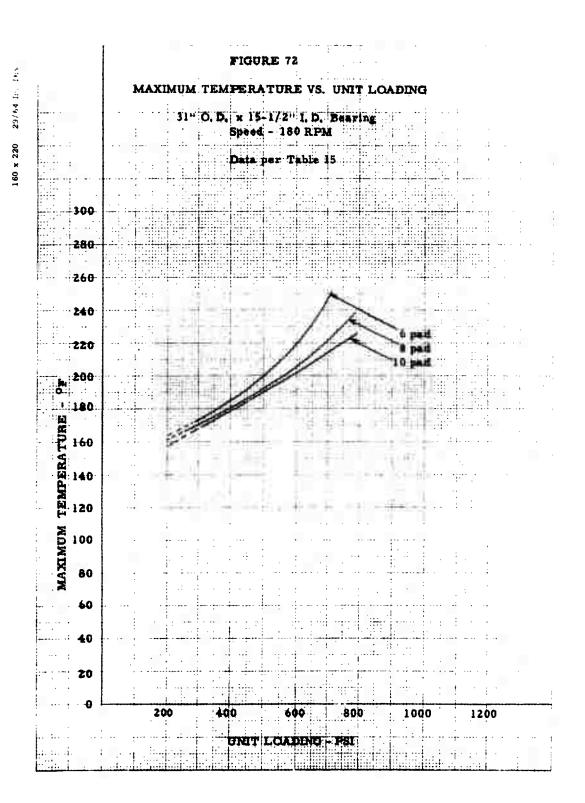
## FIGURE 71

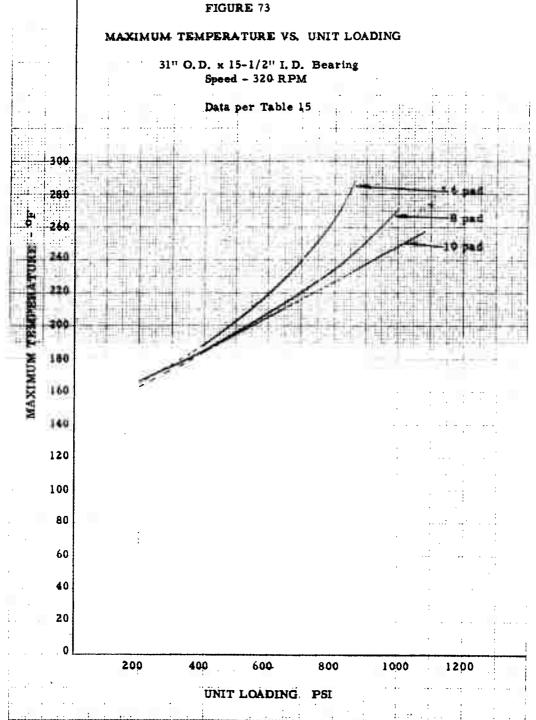
# MINIMUM FILM THICKNESS VS. UNIT LOADING

## 31" O. D. x 15-1/2" I. D. Bearing Speed- 320 RPM

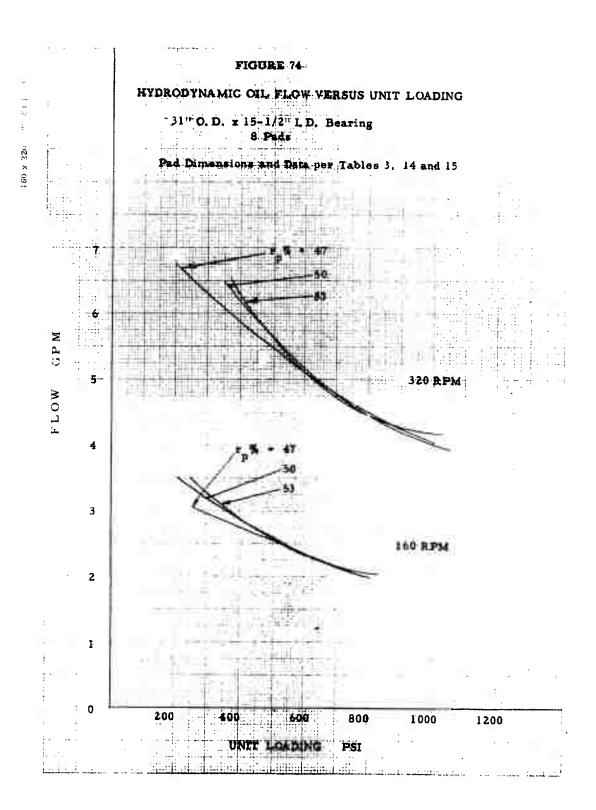


. (y:





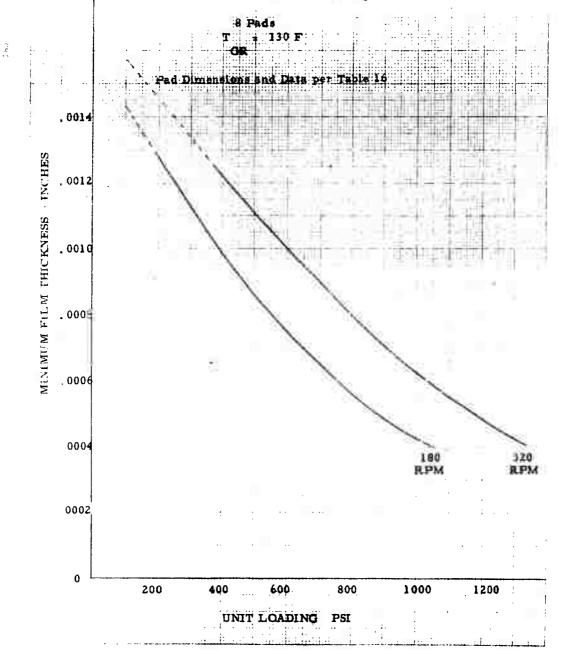
23/64 In. D.V 160 x 220

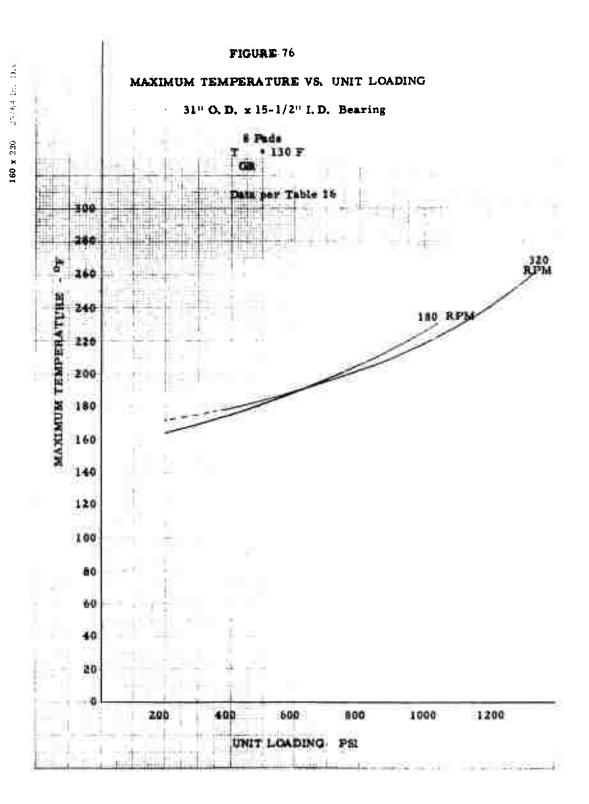


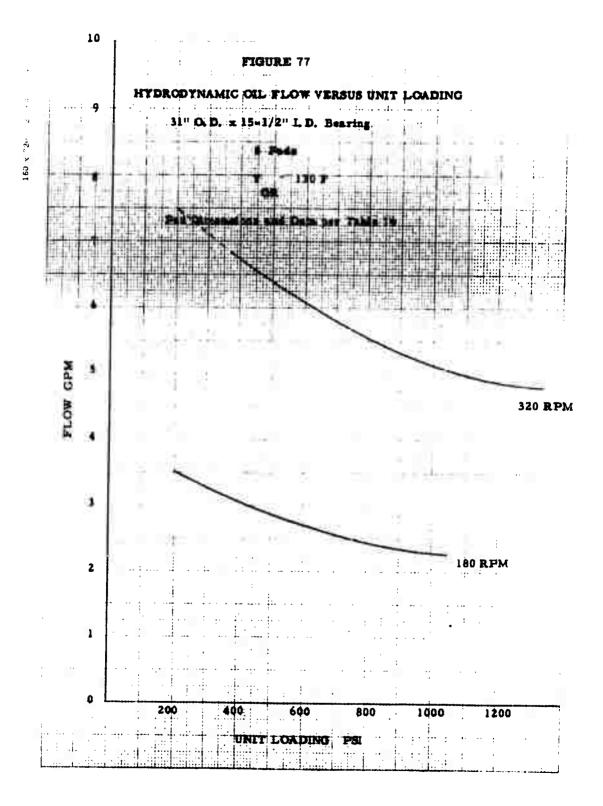
## FIGURE 75

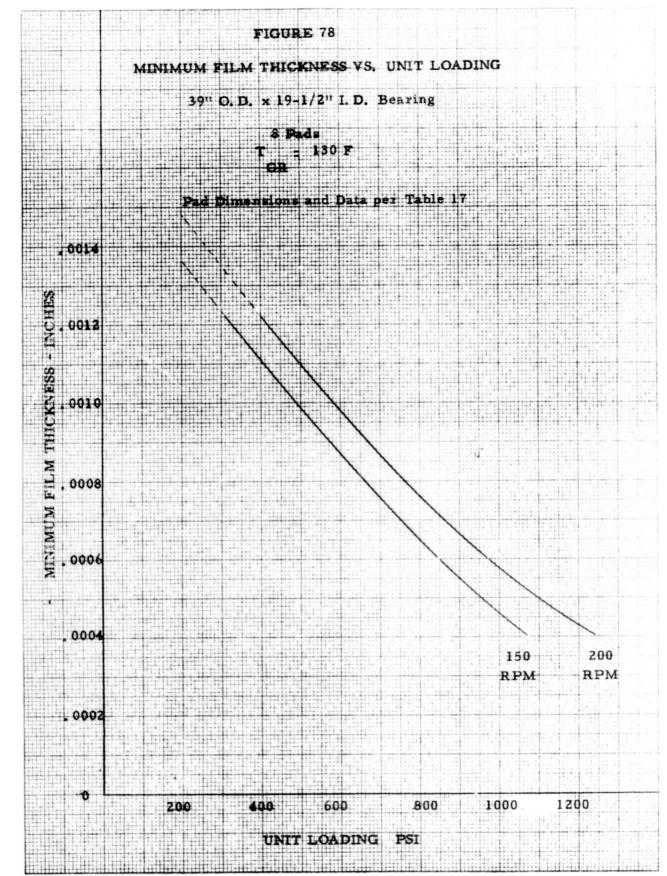
## MINIMUM FILM THICKNESS VS. UNIT LOADING

31" O.D. x 15+1/2" I.D. Bearing

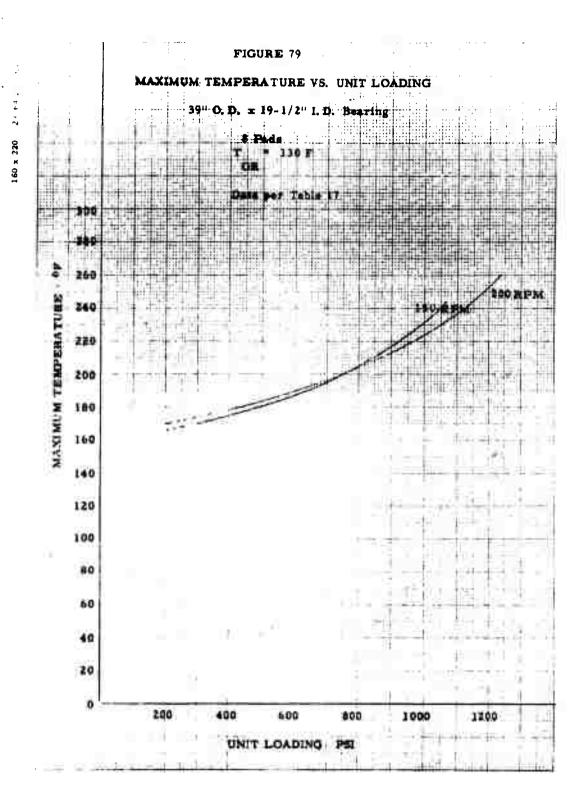


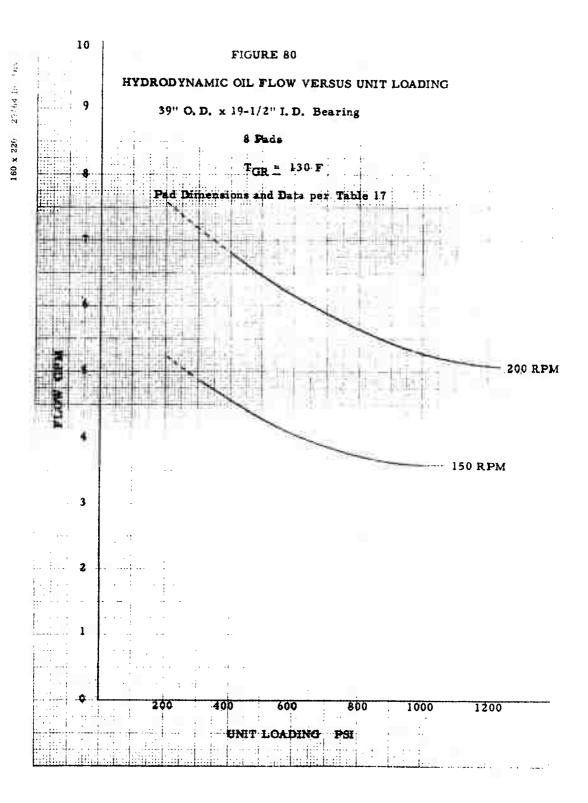




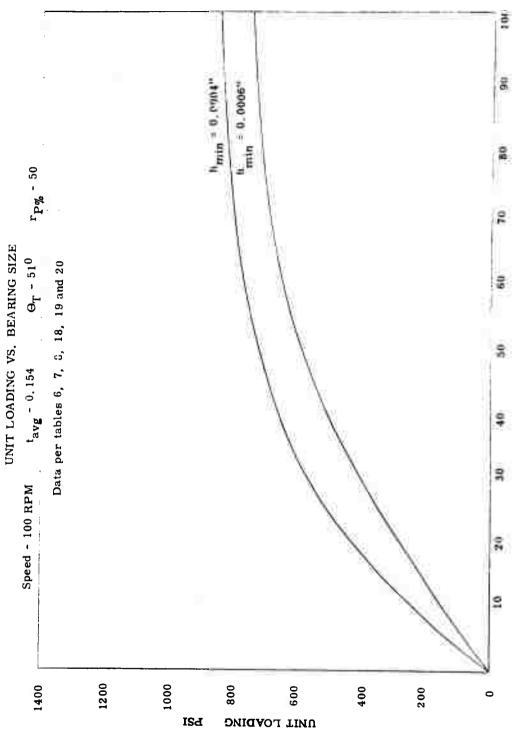


160 x 220 29/64 In. Div.

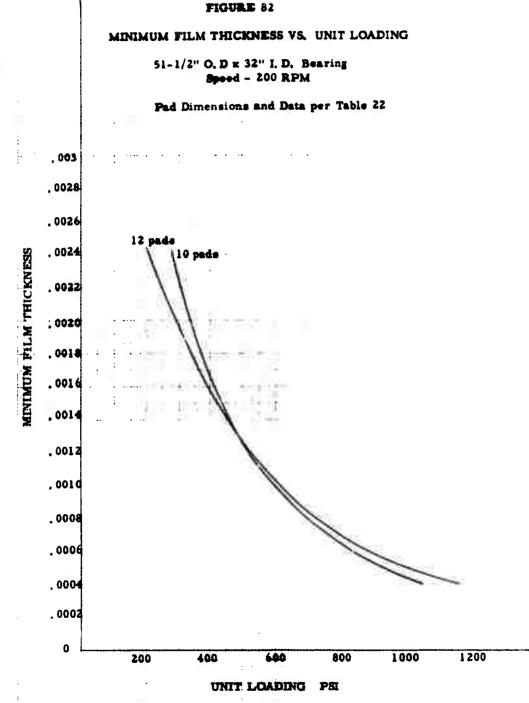




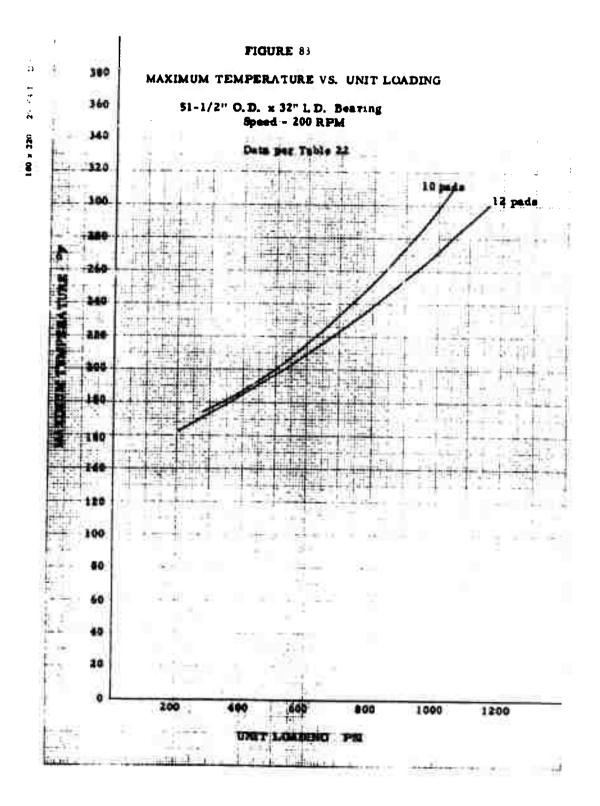


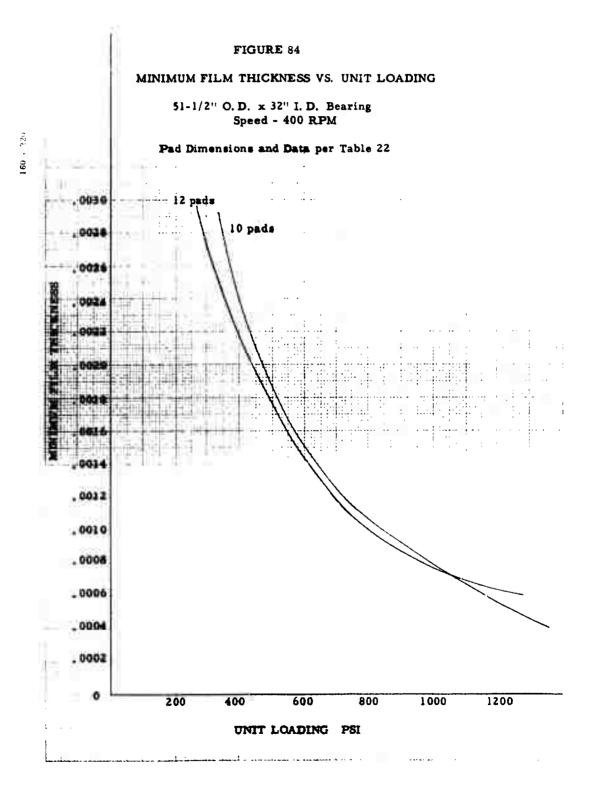


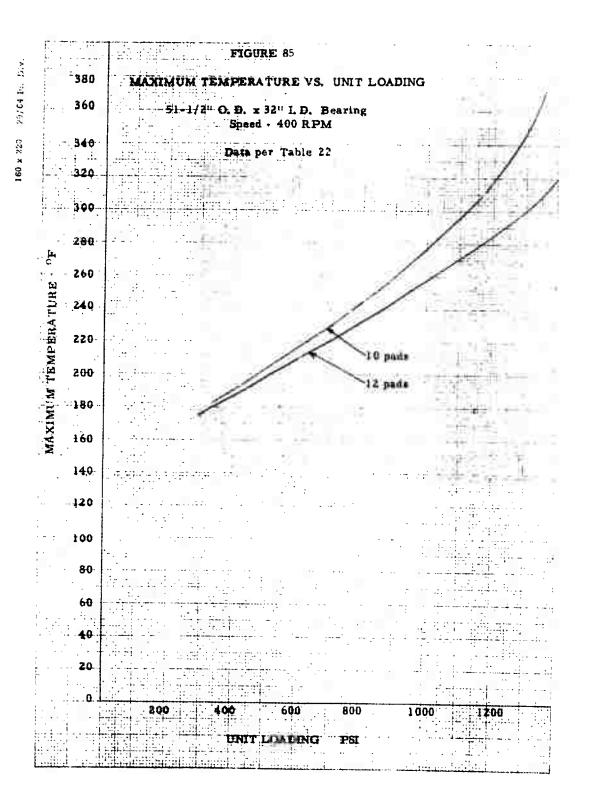
BEARING Q.D. - INCHES

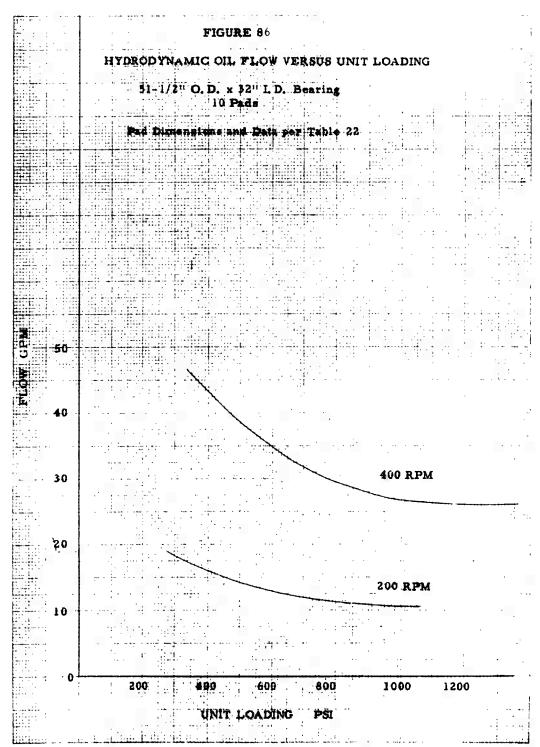


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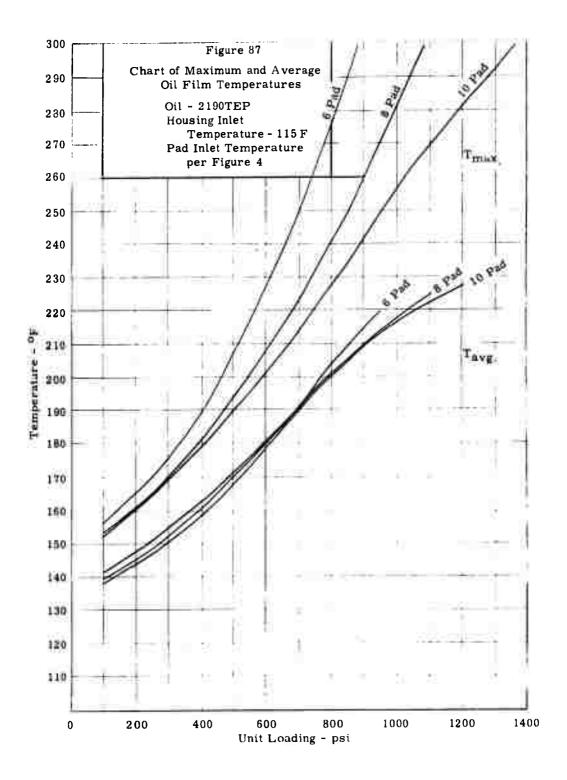


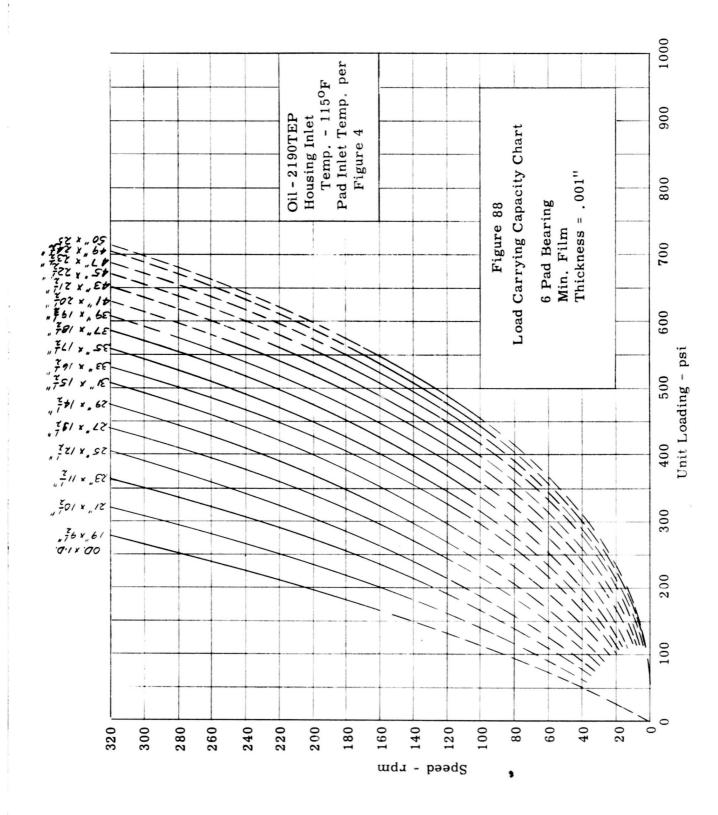


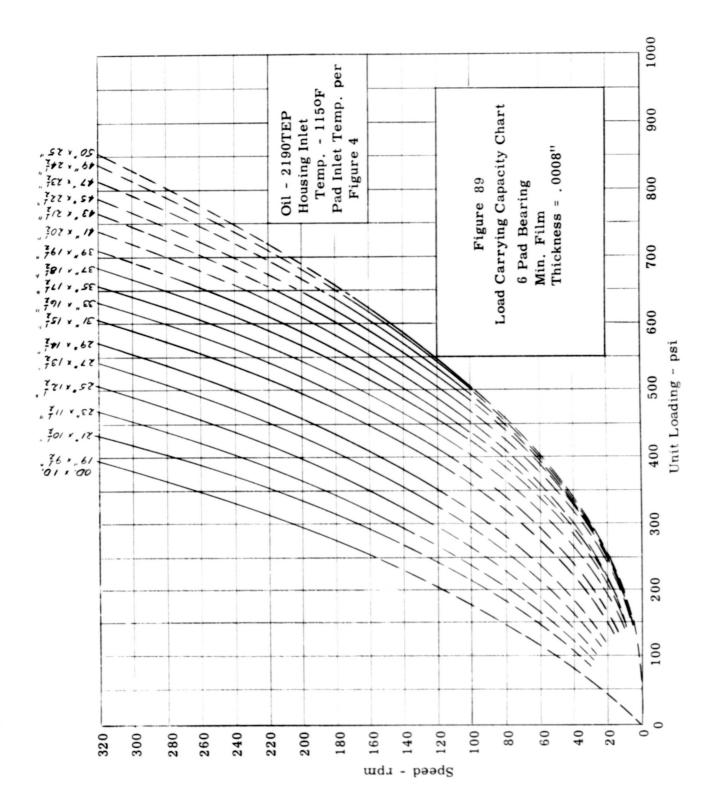


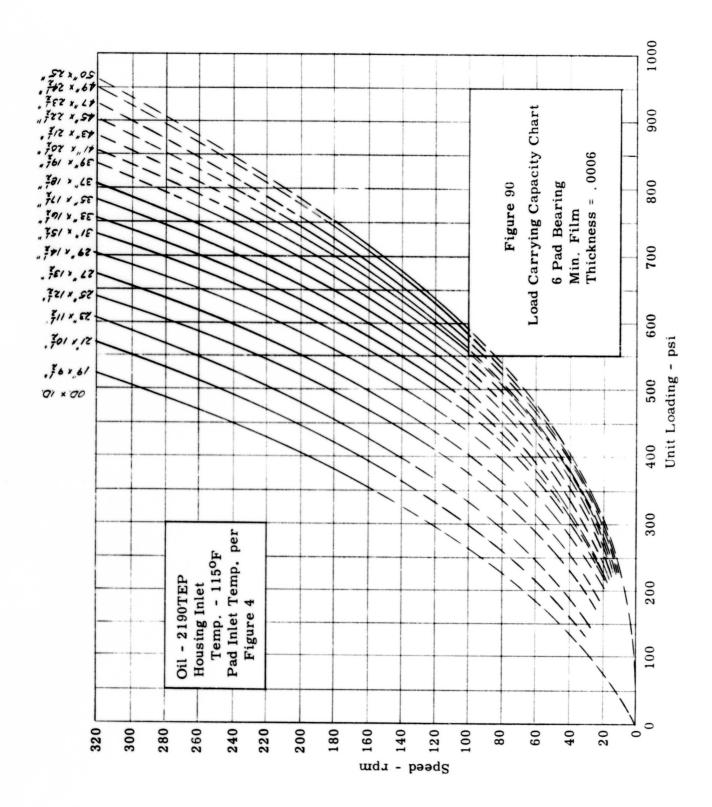


160 x 220 29/64 In. Div.

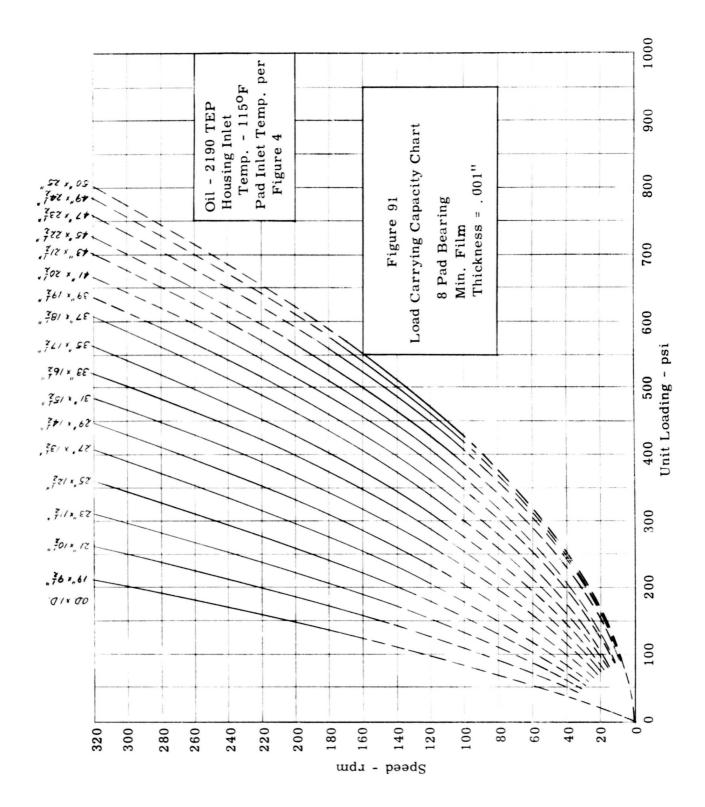


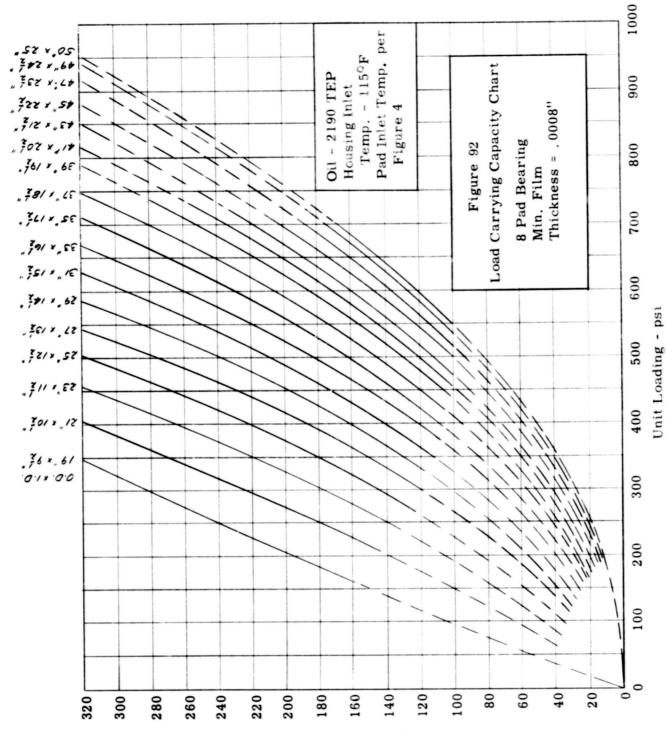






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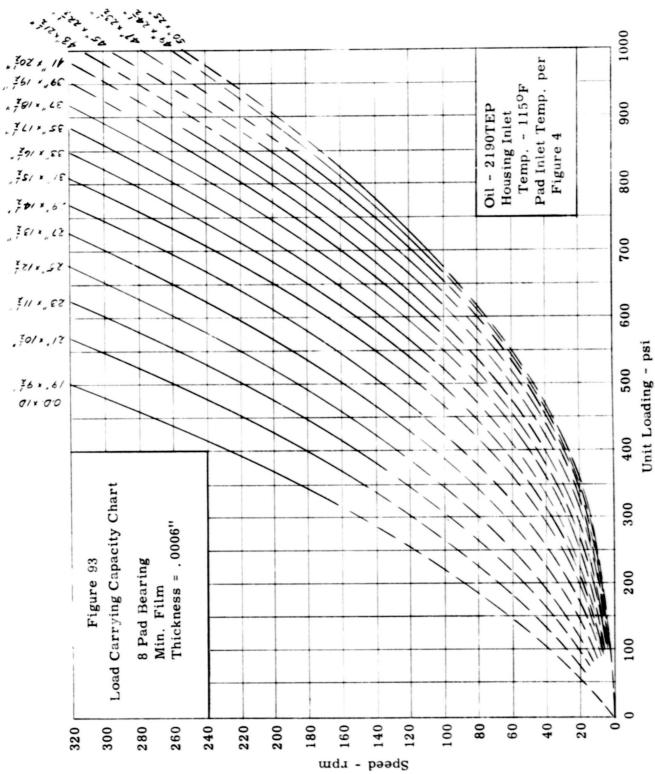


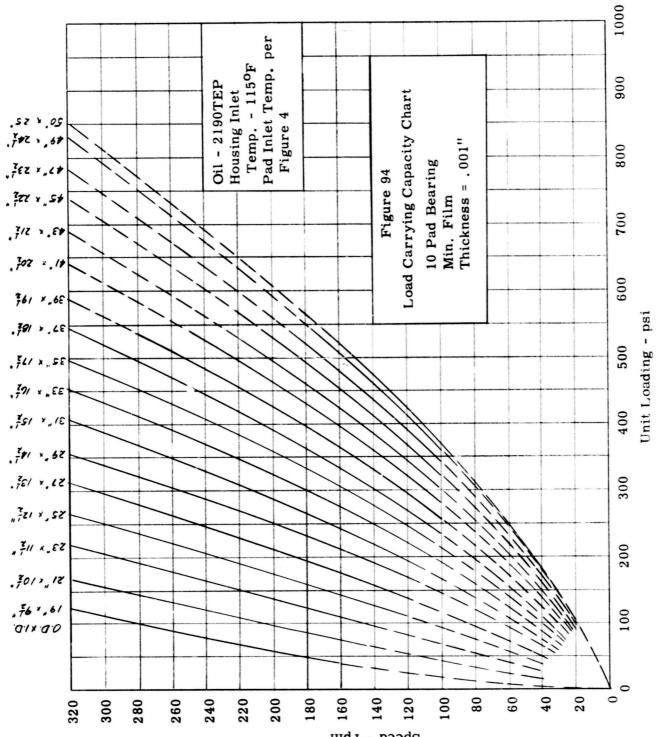


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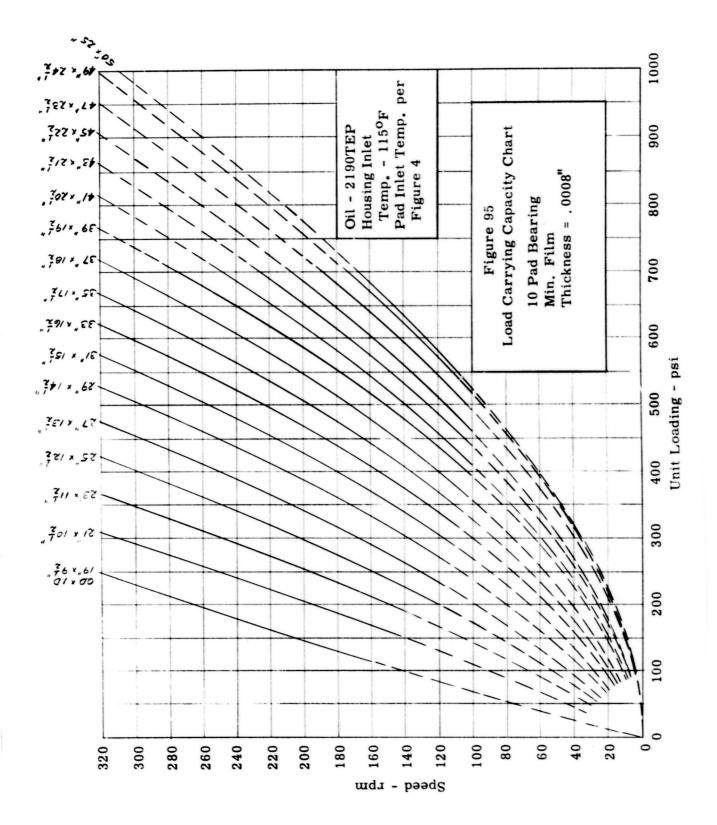
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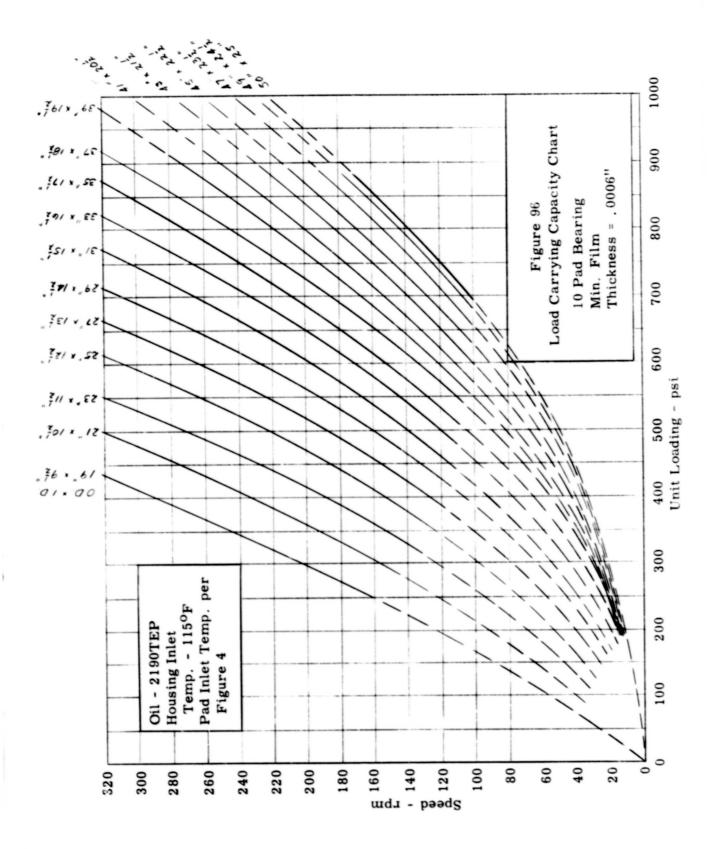
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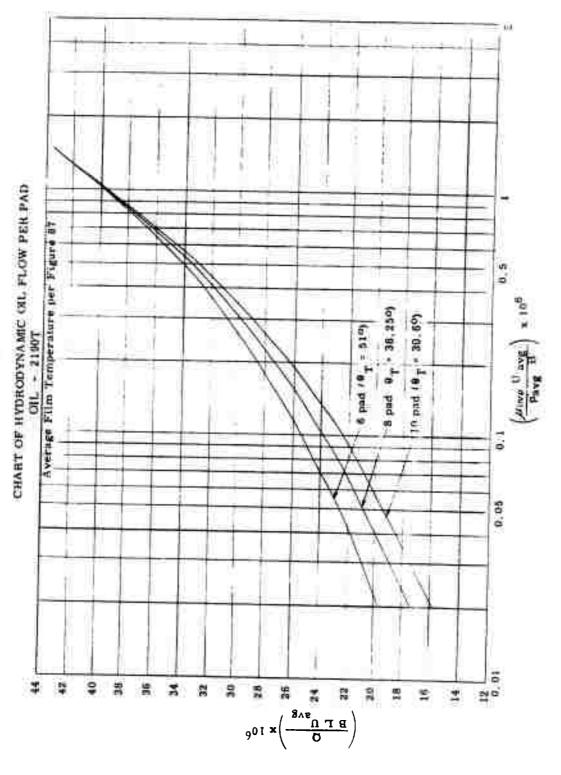


zbeeq - Lbm



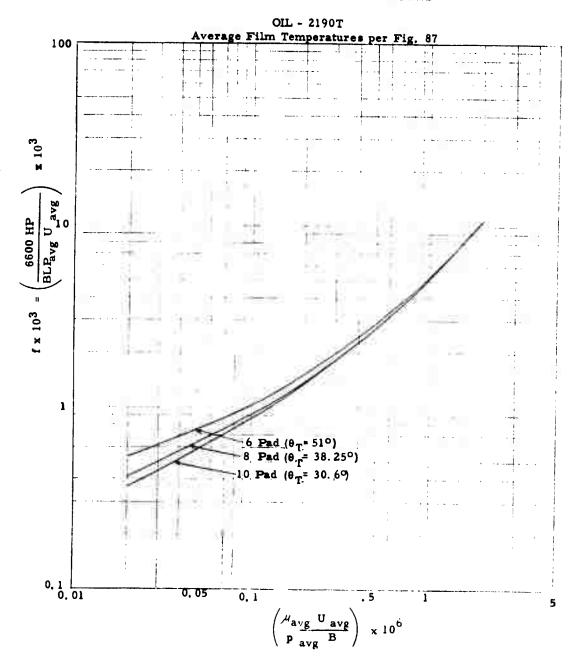


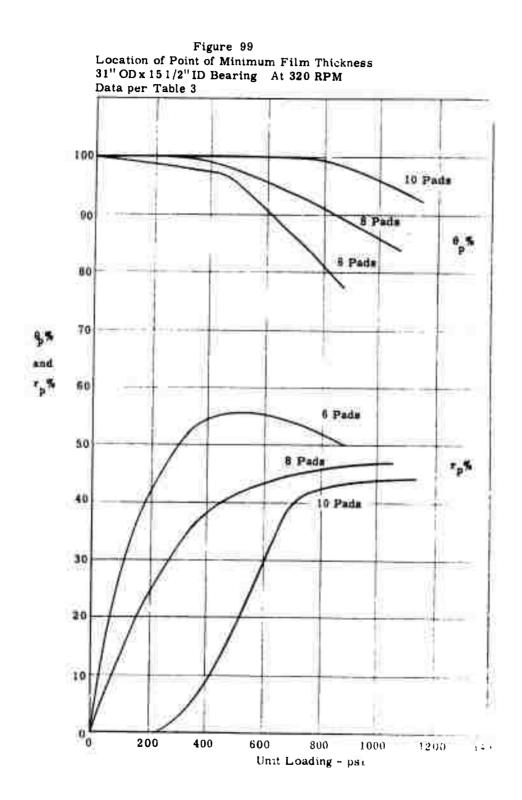




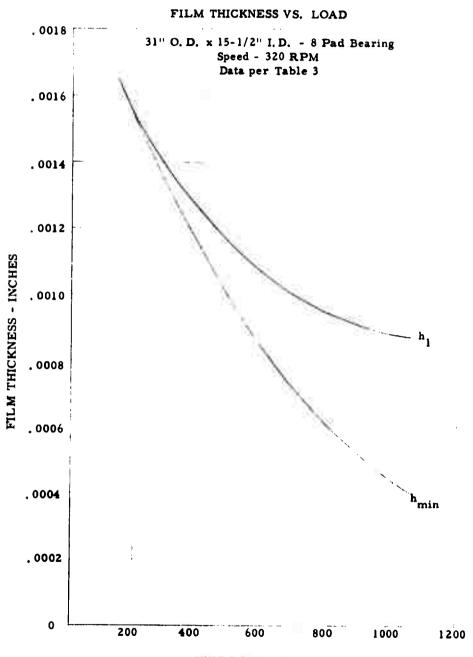


# CHART OF HORSEPOWER LOSS PER PAD

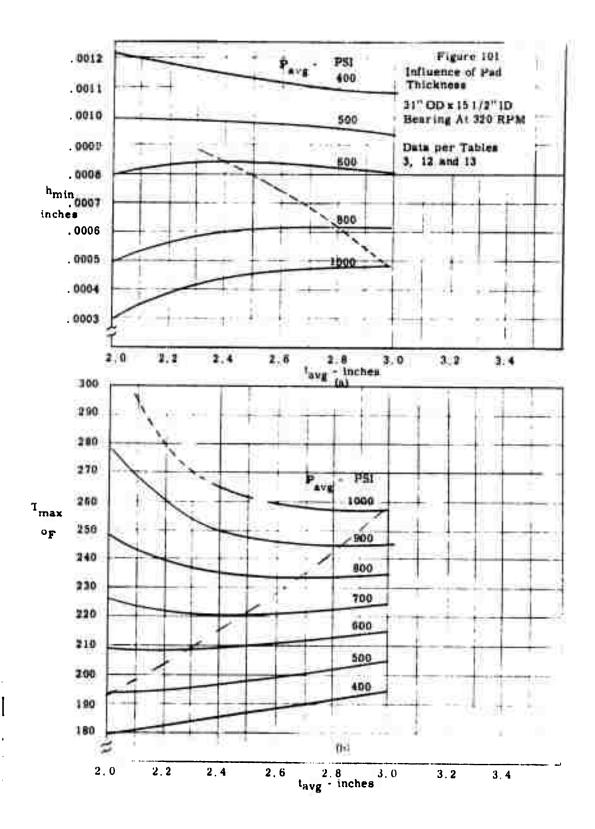


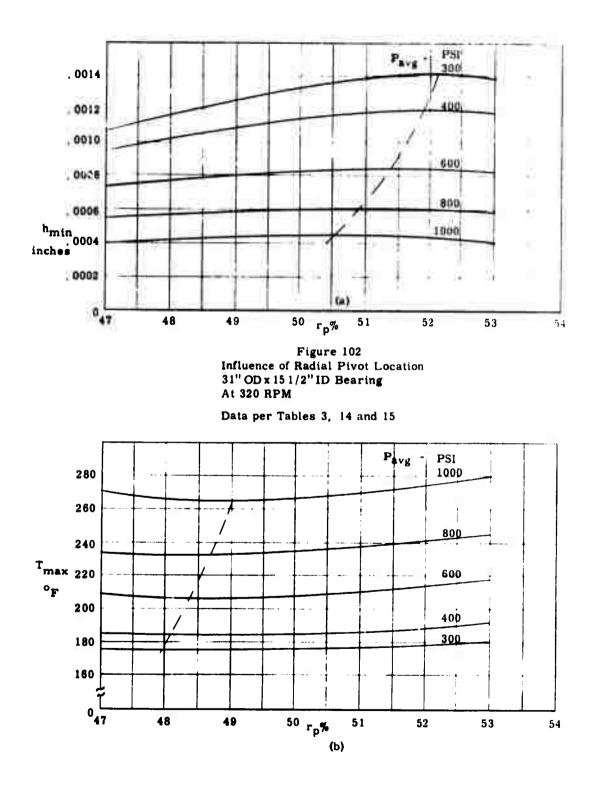


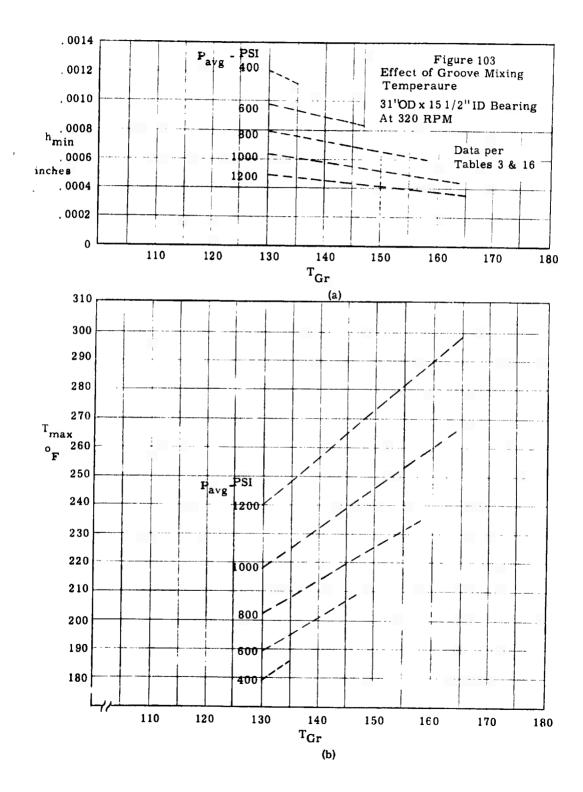




UNIT LOADING PSI

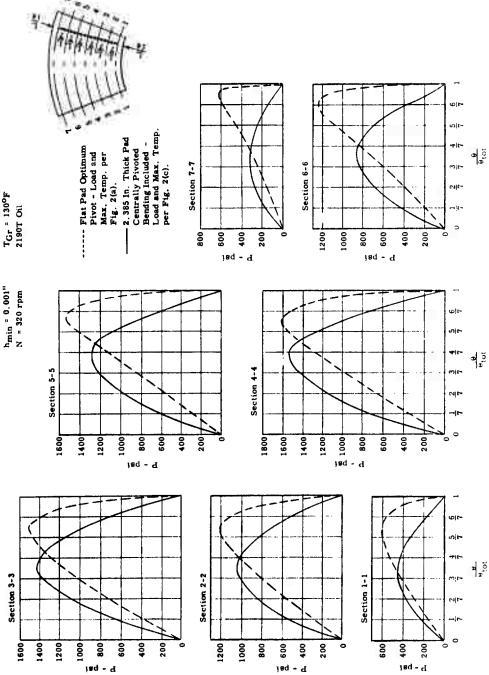








COMPARISON OF PRESSURE PROFILES 31"OD×151/2"ID Bearing (9<sub>tot</sub> = 38.25<sup>0</sup>) h<sub>min</sub> = 0.001" T<sub>G</sub>r = 130<sup>0</sup>F N = 320 rpm 21907 Oil



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SYMBOLS

	Radius of equivalent circular plate	inches
в	Average circumferential pad length [. (R - L/2) 0,	inches
C <sub>p</sub>	Specific heat of oil	BTU/16. x .F
1	Coefficient of friction	
	Film thickness	
h.	Film thickness at inside radius of trailing edge	inches
h.	Film thickness at reference point (ra, 8)	inches
hmin	Minimum film thickness	inches
HP		
HPtot	Horsepower loss per pad Total horsepower loss in bearing	H. P.
HP2. 3.	Components of pad horsepower loss corresponding to Q2. 3. 4	H. P. H. P.
3	Mechanical equivalent d thermal energy (= 9339 in. 1be./BTU)	
	Ratio of effective pad area to total available area ( Area of p	ade )
	Area of pade + Are	a of grooves /
	(Also used as subscript to denote number of iterations.)	
ĸ	Bending coefficient	inches"
L	Radial length of pad	inches
ma	Tangential pad inclination	radiane
m,	Radial pad inclination	radiane
n	Number of pads in the bearing	
	(Also used as subscript to denote outermost mesh in radial direction. )	
N	Angular speed	R. P. S.
1.0		
P	Pressure Average pressure (unit loading)	pei
Pave	Maximum pressure	pei
9		-
	Hydrodynamic flow per pad Edge flow (see Figure 3)	G. P. M. G. P. M.
Q1. 2. 3, 4 Qtot	Hydrodynamic flow per bearing	G. P. M.
:	radial co-ordinate radial co-ordinate of reference point	inches
*	andial an andiante of contas of concerns	inches
	radial co-ordinate of center of pressure { 100 [rep-(R-L)]/L}	inches
cp s cp s		inches
P.S.	radial co-ordinate of pivot	inchee
. p.*	radial co-ordinate of pivot { = 100 [rp - (R-L)]/L }	inches
R	Outer radius of pad	inches
Rc	Radius of curvature of bent pad	inches
	Average pad thickness	inchee
ave		Inches
т	Temperature	4
Tave	Average pad temperature	
GR	Groove mixing temperature Maximum film temperature	9
Tmax		•
Uave	Average surface speed [ : 2 # (R-L/2) N]	inches/sec.
	Load per pad	
Wtot	Total bearing load	ibe.
tot		
(x, y)	co-ordinates	inches
(x. y.)	co-ordinates of reference point	inches
8	Bending deflection	inches
Δ	Increment	
	Angular co-ordinate	rediane
CP.	Angular co-ordinate of center of pressure	radiane
cp *	Angular co-ordinate of center of pressure = $100 (\theta_{cp}/\theta_T)$ Angular co-ordinate of point of minimum film thickness	radians
em	Angular co-ordinate of point of minimum film thickness Angular co-ordinate of pivot	radiane
5%	Angular co-ordinate of pivot = 100 (0, 0, )	radiane
C C R R R R		
	Angular extent of pad	radiane
f	Mass density of cil	1b. sec2/in4
	Absolute viscosity of oil	lbs sec. in.2
AGR	Absolute viscosity of oil at T	lb. sec. /in. 2
Mave	Absolute viscosity of oil at Tavg	1b. sec. /in. 2
ω		
-	Angular velocity	radians/sec.

### SUBSCRIPTS

i Defines value of r in the thrust bearing pad mesh, running from 1 to n

Defines value of 0 in the thrust bearing pad mesh. running from 1 to m

k Iteration number

j

Bar above symbols denotes dimensionless quantity.