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A PROGRAM FOR COMPUTING TRANSMISSION OF PLANE ELECTROMAGNETIC WAVES THROUGH AN INHOMOGENEOUS PLASMA SLAB

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Laboratory Operations AEROSPACE CORPORATION

Prepared for

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FOREWORD

This report is published by the Aerospace Corporation, El Segundo, California, under Air Force Contract No. F04701-68-C-0200.

This report, which documents research carried out from February 1968 through March 1968, was submitted on 8 October 1968 to Lieutenant Gregory Mayforth, SMTTA, for review and approval.

Approved

Director

R. X. Meyer, Director Plasma Research Laboratory

Publication of this report does not constitute Air Force approval of the report's findings or conclusions. It is published only for the exchange and stimulation of ideas.

Gregory S7 Mayforth Lieutenant, United States Air Force Project Officer

ABSTRACT

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A computer program for calculating plane wave transmission through an inhomogeneous cold plasma slab is described. The program accepts arbitrary profiles (including jumps) in number density and collision frequency. It prints out the electric and magnetic field profiles for the angles of incidence, direction of incidence, and polarizations of the wave that are called for. It also gives the reflection and transmission coefficients in each case.

CONTENTS

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FORE	EWORD.	• •	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	٠	ii
ABST	RACT .	•••	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	iii
1.	INTROD	UCTI	ON	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	1
n.	FORMUI	LATIC	ON	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	٠	•	3
ш.	DATA IN	IPUT	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	5
REFERENCES								15														

FIGURES

1.	An Example of Input Data	•	•	•	•	•	•	•	•	•	•	•	•	•	•	8
2.	An Example of Output Data	•	•	•	•	•	•	•	•	•	•	•	•		•	9

I. INTRODUCTION

In estimating the attenuation and reflection of plane electromagnetic waves by a plasma layer it is often adequate to replace the layer by an equivalent one with uniform properties, for which the transmission loss is given by a simple formula (Ref. 1). On the other hand, in cases where the plasma properties vary significantly in the space of a wavelength, the uniform slab approximation is not justified. Furthermore, in studying breakdown under intense electromagnetic fields one is interested in the electric field profile in the vicinity of points where the dielectric constant goes to zero, and then it is clearly necessary to take account of the variation in the dielectric constant. Finally it is useful to have a systematic way for comparing existing programs (Refs. 2 through 4) and for checking estimates based on equivalent homogeneous slabs against exact calculations.

For these reasons it was decided to write a computer program for the inhomogeneous case that would be as flexible and easy to use as possible. The present report describes the program and gives a listing of it in the hope that it may also be of value to others.

The program applies to a cold plasma that is characterized by its electron number density and electron -neutral collision frequency profiles. It is designed to be as flexible as possible in the following respects. The user is free to input any arbitrary profiles of number density and collision frequency (including discontinuities) by listing the values of these quantities over any arbitrary set of corresponding abscissa values. He can call for the calculations to be performed for any number of frequencies and for any uniformly spaced sequence of angles of incidence, and for either or both polarizations of the incident wave. Finally he can have the wave be incident on the slab from either side. The computer output lists the collision frequency and number density profiles that were input. It then tabulates the transverse electric and magnetic field profiles, the dielectric constant profile, and the profile of the absolute value of the total electric field through the slab for

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each case (angle of incidence, frequency, and polarization) that was called for. Finally it gives the reflection and transmission coefficients. -----

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The next section shows some of the details of the formulation. The following one gives the exact format in which the data must be input and shows a sample of the output in an illustrative case. Finally the program itself is listed in the Appendix.

II. FORMULATION

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The plasma slab is considered to be contained in the region $0 \le x \le d$ with the xy plane being the plane of incidence. For a plane wave incident on the slab at an angle θ with respect to the x-axis, Maxwell's equations take the form

$$\frac{\partial \mathbf{E}_{\mathbf{z}}}{\partial \mathbf{x}} = -\mathbf{i}\omega \mathbf{B}_{\mathbf{y}}$$
$$-\mathbf{i}\omega \quad \frac{\partial \mathbf{B}_{\mathbf{y}}}{\partial \mathbf{x}} = \mathbf{k}_{0}^{2}(\beta^{2} - \mathbf{K})\mathbf{E}_{\mathbf{z}}$$
$$\mathbf{B}_{\mathbf{x}} = (\beta/c)\mathbf{E}_{\mathbf{z}}$$

for the TE mode (for which E_x , E_y , and B_z are zero) and

$$\frac{\partial B_z}{\partial x} = \frac{i\omega}{c^2} KF_y$$

$$\frac{i\omega}{c^2} K \frac{\partial E_y}{\partial x} = k_0^2 (\beta^2 - K)B_z$$

$$E_x = -(\beta c/K)B_z$$

for the TM mode (for which B_x , B_y , and E_z are zero). Here $\beta = \sin\theta$ and $k_0 = \omega/c$, where $\omega/2\pi$ is the frequency. The dielectric constant K for a cold plasma is given by

$$K = 1 - \frac{\omega_p^2}{\omega(\omega + i v_c)}$$

-3-

where v_c is the electron-neutral collision frequency and where ω_p^2 , the square of the plasma frequency, is proportional to the electron number density n. If n is measured in electrons/cm³ then

$$\omega_{\rm p}^2 = 3.186 \times 10^9 \,{\rm n}$$

For the TE mode the computer gives the profiles of E_z , B_y , and $|E_z|$. For the TM mode it gives the profiles of E_y , B_z , and $\sqrt{|E|_x^2 + |E|_y^2}$. The electric field components E_z or E_y are always normalized to unity on the incident side. The K profile is given in both cases.

Outside the plasma slab the waves are taken to be of the form

 $(1-R) E = \exp(ik_0 \cos\theta x) - R \exp(-ik_0 \cos\theta x) \qquad \text{for } x \le 0$ $(1-R) E = T \exp(ik_0 \cos\theta x) \qquad \text{for } x \ge d$

where E is any component of the electric field. Solving for R and T we find

$$R = \frac{E_1' - ik_0 \cos\theta E_1}{E_1' + ik_0 \cos\theta E_1}$$

$$T = (1-R)(E_2/E_1) \exp(-ik_0 \cos\theta d)$$

in terms of E_1 and E_2 , which are the values of E at x = 0 and x = d, respectively. (The prime denotes the x derivative.) The computer furnishes these values together with their decibel equivalents (defined as $20 \log_{10} |\mathbf{R}|$ and $20 \log_{10} |\mathbf{T}|$, respectively).

-4-

III. DATA INPUT

The data are input on regular 80-column Fortran cards. At least 7 cards are required for each case. A particular case consists of a plasma slab defined by its thickness and its profiles of number density and collision frequency together with a set of plane waves having 1 to 10 different frequencies and any number of angles of incidence. Any number of cases can be run by stacking the corresponding groups of cards. The cards required to represent one case are as follows:

CARD 1 contains 6 two-digit numbers placed in first 12 columns as follows: (A one-digit number is preceded by 0, e.g., 3 becomes 03.)

Columns 1,2:	Number of stations at which number density is given. (See CARD 2.) Maximum allowed is 30.
Columns 3,4:	Number of stations at which collision frequency is given. (See CARD 3.) Maximum allowed is 30.
Columns 5,6:	Number of frequencies. Maximum allowed is 10.
Columns 7,8:	Number of angles of incidence. (See CARD 6.)
Columns 9, 10:	Mode: 01 for TE, 02 for TM and 00 (or blank) for both. (Only one mode is computed at normal incidence.)
<u>Columns 11, 12:</u>	Direction of x-component of incident wave: 00 (or blank) if to the right (i.e., the direction in which the data on CARDS 2 - 5 is entered), 01 if to the left.

CARD 2 lists stations (values of x/d) at which number densities are to be given. These values must be listed in increasing order starting with 0. (representing the front of the slab) and ending with 1. (representing the back). Each one

-5-

(including the last) requires a decimal point and occupies 5 columns, so the total number of columns is 5 times the first number entered on CARD 1. If more than 80 columns are required, two cards must be used, and the second then counts as the continuation of CARD 2. If at any station two values of the number density are to be given (corresponding to a discontinuity in the profile) then the corresponding station must appear twice. Thus a homogeneous slab requires 4 stations viz., 0., 0., 1., 1.

CARD 3 lists stations at which collision frequencies are to be given. Remarks under CARD 2 apply.

CARD 4 lists number densities in multiples of $10^9/\text{cm}^3$ corresponding to the stations listed on CARD 2. The first and last values correspond to the media carrying the incident and transmitted waves respectively, and will normally be 0 (for vacuum). Each value occupies 5 columns, so the total number of columns used is the same as on CARD 2. The smallest possible number density is $10^5/\text{cm}^3$ (entered as .0001) and the largest is $10^{14}/\text{cm}^3$ (entered as 99999). Values between $10^{13}/\text{cm}^3$ and $10^{14}/\text{cm}^3$ are entered as 5 digit numbers without a decimal point.

CARD 5 lists collision frequencies in multiples of 10^9 sec^{-1} corresponding to the stations listed on CARD 3. Remarks under CARD 4 apply.

CARD 6 contains 3 numbers, each occupying 5 columns, including the decimal point.

Columns 1-5: Slab thickness in centimeters.

<u>Columns 6-10:</u> First angle of incidence to be run; 0 (or blank) corresponds to normal incidence. Thereafter this value is incremented by the number appearing in Columns 11-15 of this card until a total number of angles of incidence has been run equal to the number appearing in Columns 7,8 of CARD 1.

-6-

<u>Columns 11-15</u>: Interval in degrees between successive angles of incidence.

CARD 7 lists wave frequencies in GHz. Each value occupies 5 columns, including the decimal point. The total number of frequencies listed must not be less than the number appearing in Columns 5 and 6 of CARD 1.

As a particular (rather artificial) example we consider a plasma slab 1.50 cm thick and having an electron number density which starts at 10^{12} /cm³ at x/d = 0, falls linearly to 10^{11} /cm³ at x/d = .63, at which point it jumps to 10^{11} / cm³, and then falls off linearly to zero at x/d = 1. We take the collision frequency to follow a triangular distribution, 0 at $x/d = 0, 1 \text{ and } 10^6 \text{ sec}^{-1} \text{ at } x/d = .5.$ We call for one angle of incidence 37.5 deg, and one frequency, 3 GHz. We ask for the wave to be incident from the right and polarized in the TM mode. The input data as it would be entered on the seven cards is shown in Fig. 1. The corresponding output is shown in Fig. 2. The results (in this case the real and imaginary parts of E₁, B₂, and K, and the value of $\sqrt{|E|^2} + |E|^2$ are printed out at intervals of x/d = .1 except at jumps where they are printed out twice, to the left and to the right of the jump. The electric field is always normalized to unity on the incident side. The fact that in the printout it is unity at x/d = 1 serves as a reminder that the wave was required to be incident on this side of the slab. On the transmitted side we have a single plane wave in free space for which $E_v/cB_z = -\cos(37.5^\circ)$.

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TRANSHISSION THROUGH PLASHA SLAD

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NUMBER DENSITY AND COLLISION PREQUENCY PROFILES (SLAB THICKNESS D = 1.500 CH)

υ	0. 1.00£-06 0.	
a/x	0 • 5 0 1 • 9 0	
z	0. 1.006+12 1.006+10 1.006+10 1.006+11	
0/X	600 00 00	E NABUTTE MORE

TRAMSVERSE MAGNETIC MODE (FREQUENCY = 3.006.00 HZ, ANGLE OF INCIDENCE = 37.5 DE0)

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A DS (E)	-5422		1409	1.1002	1.3113		
	•	6.01965-05 1.30495-04	1.5088E-04 1.4136E-04	1.0194E-04 2.1748E-05	3.52055-06 3.52055-05 2.1445-05	2.57165-05 3.44165-11	
×].0000E+00 -7.54755-00	-6.55832.00	-3.7400£+00 -2.3308E+00	-9.2161E-01 4.8757E-01	9.10335-01 1.03255-01 2.79915-01	5.15276-01 7.5764E-01 1.0000E+00	
-	-7 .9308E -10 -7 .9308E -10	-1.71126-09 -2.54376-09	-3 .2616 [-09 -3 .0612 [-09		-4.25815-09 -4.25815-09 -4.22025-09	-4.1108E-09 -3.9279E-09 -3.6602E-09	:
	-1.6241E-09 -1.6241E-09	-1.24216-00	01-36196*4-	-7.6907E-10	-7.7022E-10	-7,73985-10 -7,76545-10 -7,78265-10	
-	1.0076E-01 1.0076E-01	1.1314E-01	5° 95295 - 02	0-30(50-0)	5.1212E-03 2.2244E-02	2。1 652E- 02 1。2657E-02 0。	
	3.8454E-01 3.8454E-01	• - 2+2+2 - 0 • • 992+2 - 0 • • 992+2 - 0	6.92256-01 6.34485-61	9-0445-01 9-02015-01	9.8281C-01 8.8840E-01	8.91576-01 9.38286-01 1.00086480	V COEFFICIENT
X/D				93	321		EFLEX 10

MEFLEXION COEFFICIENT = (=.0954, .0052) # -1.0 DB TRANSMISSION COEFFICIENT = (.4930, .3147) # -4.7 DB

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Figure 2. An Example of Output Data

-9-

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APPENDIX

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THE PROGRAM

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. - AEROSPACE CORPORATION PROGRAM PLASMA(IMPUT.OUTPUT.TAPE]=IMPUT.TAPE2=OUTPUT) COMMON BETA.C(30).EPS.F(10).I.*IMAX.IMC.J.JMAX.KF.KO.M.M(30).XC(30) *XN(30).Y(5).YP(5) DIMENSION E(40).MODE(2).S(3.40).TEMPS(50).X(40) COMPLEX EPS.MASE.R.S.T REL KOYXYM DATA DX.DP.C1.C2.TP1/.01..1.2.0944.E-10.5.071E8.6.20319/ DATA DX.DP.C1.C2.TP1/.01..1.2.0944.E-10.5.071E8.6.20319/ DATA DX.DP.C1.C2.TP1/.01..1.2.0944.E-10.5.01710355/ DATA CL.EU/405.E-44.405.E-4/.MMAX.MMIN/.010..010/ DATA CL.EU/405.E-44.405.E-4/.MMAX.MMIN/.010..010/ Indel. 00012 00012 00012 00012 00012 210000 999012 900012

I READ(1.200) [MAX, JMAX, MMT, MMA, M1, INC II = [MAX + 1 READ(1.201) (XW(I), I=1, II) Ju = JMAX + 1 READ(1.201) (XW(I), sum , Ju) READ(1.202) (W(I), sum , Ju) READ(1.202) (C(J), s •IMTEGATION 3 DO 150 KA = 1,MPA 3 DO 150 KF = 1,MPA 7 META = THETA1 + DTMETA•(KA-1) DO 150 KF = 1,MPF 16 (M1.60.0 M = 1 17 (M1.60.0 M = 1 17 (M1.ME.0) H = M1 00012 000031 000033 000047 000047 0000105 000105 000136 000136 000136 000136 000136 000136 00172

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5 MAD = 7META=.017453 BETA = 51M(MAD) K0 = 6197(KF)=0 KX = K0=C05(RAD) XP = 0.

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Call VERTY 60 Call FAMMK(Y)PDERIY000.EU.EL.MAR.MUIN.TEMPS) 70 [f(Y(1) - (XC(J+1)-.Z=0X1) 80.10010 80 [f(Y(1) - (XP-.Z=0X1) 90.20.30 90 [f(Y(1) - (XP-.Z=0X1) 60.100110 90 [f(Y(1) - (1.-.2=0X1) 60.110.110 100 [f(Y(1) - (1.-.2=0X1) 60.110.110 110 PHSE = CMPLX(YP(Z=M-1)) 00.110.110 8 a (CMPLX(YP(Z=M))YP(Z=M-1)) + KXe(0..1.)*S(1.L1)/(CMPLX(YP(Z=M)). 110 PHSE = CMPLX(COS(KX1.SIM(KX1)) 8 a (CMPLX(YP(Z=M))YP(Z=M-1)) + KXe(0..1.)*S(1.L1)/(CMPLX(YP(Z=M)). 110 PHSE = CMPLX(S=0.1.)*S(1.L1) + KXe(0..1.)*S(1.L1)/(CMPLX(YP(Z=M)). 111 PHSE = CMPLX(S=0.1.)*S(1.L1) + KXe(0..1.)*S(1.L1)/(CMPLX(YP(Z=M)). 112 PHSE = CMPLX(S=0.1.)*S(1.L1) + KXe(0..1.)*S(1.L1)/(CMPLX(YP(Z=M)). 113 PHSE = CMPLX(S=0.1.)*S(1.L1) + KXe(0..1.)*S(1.L1)/(CMPLX(YP(Z=M)). 114 T = (1.-4)*PMSE/S(1.L1)*(1.0.1.)*S(1.L1) + Z=M) 0 70(40+5) H 4 5(1.L) = CMPLK(Y(2),Y(3)) 5(2.L) = CMPLK(Y(4),Y(5)) = (0..1.6-0)/(3.0K0) 4 5(1.L) = CMPLK(Y(4),Y(5)) 5(1.L) = CMPLK(Y(2),Y(3)) = (0..-1.6-0) = K0/3. 5(2.L) = CMPLK(Y(2),Y(3)) = (0..-1.6-0) = K0/3. [= 1+] [f(xM(1).E0.XN(1+1)) 00 70 360 [f(1.61+1)60 70 80 J = J+1 |[[XC(J].E0.XC(J+1]) 00 T0]70 |[[J.61.1] 00 T0 90 FIL.0T.1) 00 TO 100 1.50 . (1.....) 40+04 (1) * (1) ğ TENS •
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KEY WORDS

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Electromagnetic wave transmission Inhomogeneous plasma slab Plane wave transmission

Abstract (Continued)

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