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OPERATIONS EVALUATION GROUP

COMPUTER CALCULATION OF DISCRETE FOURIER TRANSFORMS USING THE FAST FOURIER TRANSFORM

By J.C. Wilson

OEG Research Contribution No. 81

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CENTER FOR NAVAL ANALYSES

COMPUTER CALCULATION OF DISCRETE FOURIER TRANSFORMS USING THE FAST FOURIER TRANSFORM

By J. C. Wilson

James C Mallon

5 June 1968

Work conducted under contract N00014-68-A-0091

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Enclosure (1) to OEG ltr (OEG)463-68 Dated 14 August 1968

ABSTRACT

This research contribution describes a computer program (CNA Number 76-67) which determines the Discrete Fourier Transform of a set of data, using a recently developed technique known as the Fast Fourier Transform. The relation between Discrete Fourier Transforms and Fourier Series when the data is periodic is also shown.

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COMPUTE A ALCENATION OF DISCRETE FORKIER TRANSFERMENT AND FUE FAST FOURTER TRANSFORM

The Fast domain the soform (FFT) is a technology recently developed to complete the Debrate allocation (FFT) is a technology recently developed to Fourier Transform is a featomistion (DFT) of a set of data. The Discrete Fourier Transform is a featomistic of a good approximation to the Fourier Series coefficient, of a curle series (for periodic photomena) or () the isotrier lategral (for aperiodic photomena) where ver the or all or ries is known only at discrete point in three the addition, the DFT as a use of transform in its own right and is discrete of in some detail in the refer meet. Interest in the Fast thariter Transform vas a perared at CNV by some problems in its soft of message and involves to review it, and also involved investigating re-still periodicities at the curve prodests.

Computing the DFT of a time series is very similar to computing Fourier Series coefficients and, until recently -s taken an amount of time approximately propertional to N², where N is the number of data points used. Computing the Fast Fourier Transform, however, uses time proportional to N log₂N, which

can result in a substantial saying of computer time if the number of data points is large. An additional advintage is that the roundoff error is reduced because tower calculations have to be performed.

Because of the speed of the FFT and the consequent greater utility of the OFT, a program (CNA 70-67) was written to compute the DFT of a set of data us in the East Fourier Transform. This program can provide a method of detecting periodicities in data by using the DFT as an approximation to Fourier Series. In addition, the user who is more familiar with transform techniques can use z to dot, many relations between several sets of data (least squares fits, time lags, cross-correlation, etc.).

A complete description of the Fast Fourier Transform is too tayolyed to be given here, but is presented quite clearly in references (a) through (c). Basically, the technique consists of successively dividing the data into groups of N/2, N/4, N(8, ..., N, N) points, then accombining these groups with appropriate weighting tactors.

Three many potentials in the issue the program to should be mentioned. First, the procent overks only for sets of N40^K data point to the nok issue there is the number of period devices may have to solve a some of his data to the number of period devices the next lower power of 2, we that data is a ty 2, 4, 5, ..., 2^K will be possible. Second, when the Directed to over the advances does an approximation to the Fourier series of a set of data only the first Y, 2 DFU coefficients, instead of all Y, stoud be considered. The mean term has be does used an appendic 2. Not hardly, because of a treatment of the does sed an appendic 2. Not hardly, because of a treatment of the CDC 5400 FORTRAN system on mays of data points and cot actuals and term from 1 to N instead of from 0 to N-1 Coursed in the equations

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in the derivations), which will usually entail some extra input and output operations to keep the format in line with the format in the derivations.

Appendix A contains the definition of the Discrete Fourier Transform and its relation to the Fourier Series. Appendix B is a description of the computer program, which uses the FFT technique, along with its limitations and some possible uses. Also included is a listing of the program itself, which is written in FORTRAN II for the CDC 3400 computer. Appendix C gives an example of how the program can be used and some numerical results.

「「「「「「「「「「」」」」」 そのできる あいたりません あ APPENDIX A ÷ ۰.

APPENDIX A

DEFINITIONS

Given a time series $x(k\Delta)$, k=0, ..., N-1, the Discrete Fourier Transform (DPT) and its inverse are defined as follows:

$$B(n) = \frac{1}{N} \sum_{k=0}^{N-1} x(k) \exp\left(\frac{-2\pi i k n}{N}\right), \quad n=0, 1, \dots, N-1$$
 (1.1)

and
$$\mathbf{x}(\mathbf{k}) = \sum_{n=0}^{N-1} B(n) \exp\left(\frac{\pm 2\pi i n \mathbf{k}}{N}\right), \quad \mathbf{k} = 0, 1, \dots, N-1$$
 (1b)

where $i = \sqrt{-1}$

B(n) will in general be complex when x is real. The similarity between the DFT and the Fourier Series is evident when we consider the exponential form of the Fourier Series:

$$C(n) = \frac{1}{T} \int_{0}^{T} x(t) \exp\left(\frac{-2\pi int}{T}\right) dt, \quad \text{all integer n,}$$
(2a)
$$x(t) = \sum_{n=\infty}^{n=\infty} C(n) \exp\left(\frac{+2\pi int}{T}\right), \quad \text{where } x(t) \text{ is piecewise continuous and}$$
(2b)

periodic with period T.

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Now if the above integral is approximated by its Riemann sum, C(n) becomes approximately

$$C(n) = \frac{1}{N} \sum_{k=0}^{N-1} x(k \Delta t) \exp\left(\frac{-2\pi i n k}{N}\right), \text{ where } T=N\Delta t, \text{ In other words we use } N \text{ samples in the semi-open interval } \begin{bmatrix} 0, T \end{bmatrix},$$

But the sum on the right is just B(n), so we have

$$C(\mathbf{n}) \stackrel{\scriptscriptstyle \leftarrow}{=} B(\mathbf{n}) \tag{3}$$

This then is the relation between Fourier Series and Discrete Fourier Transforms when x(t) is periodic. The C(n) tell us how much of x(t) can be attributed to sinusoids of "frequency"

$$f = \frac{n}{T} = \frac{n}{N} \left(\frac{1}{st}\right).$$

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 $n = -\alpha$

and can be approximated by the DFT coefficients B(n). This becomes clearer when we realize that in fact (reference (b))

$$B(n) = \sum_{j=-\infty}^{\infty} C(n+jN) , \qquad n=0, 1, ..., N-1.$$
 (4)

That is, B(n) is the sum of overlapped segments of C(n). Figure A-1 shows this relationship between B(n) and C(n). In order to make B(n) a better approximation to C(n) we must increase the number of samples in the period T.

Now if x(k) is real, C(n) will be an even function of n; that is, C(n)=C(-n). Equation (4) then gives us some further information about B(n):

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Thus B(n) is symmetrical about n=N/2 (see figure A-1). Care must be taken, therefore, not to use B(n) as an approximation to C(n) when $h \ge N/2$.



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APPENDIX B

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APPENDIX B

DESCRIPTION OF THE PROGRAM

The core of the program to compute the DFT of a c_{mer} series is really quite compact, and can be expressed as a set of 4 nested do loops:

 $\begin{array}{l} 1 \ge 100 \ j = 1, \ s \\ DO(100 \ k = 0, \ 2^{j-1} - 1) \\ DO(100 \ n = 0, \ 2^{j-1} - 1) \\ DO(100 \ n = 0, \ 1 \\ \end{array} \\ B(n \pm k + 2^{j} \pm n + 2^{j-1}) = B(n \pm k + 2^{j}) \pm (-1)^{m} B(n \pm k + 2^{j} \pm 2^{j-1}) \exp\left[\frac{-2\pi \ i}{2^{s}} \ n(s \pm 1 - j)\right]$

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where $N=2^{S}$ data points are used. *

An advantage of the program not mentioned in the body of the text is that the coefficients can use the same storage as the original data, since the program exchanges pairs of values (m=0, 1 in the above formulation) after appropriately weighting them. An important programming consideration, however, is that all arrays must be in complex notations to effect this space-saving, so real time series must be converted to a complex format before being used.

The program allows up to $1024\approx 2^{10}$ data points. To store up to 2^{15} points, the user need only redimension the arrays to set aside that much storage. If still more data is used, then complicated changes must be made to the subroutine written in COMPASS.

The user may also call for the inverse transform to get back a time series from a set of coefficients by calling the subroutine INVERSE. At any time after calling the subroutines for the transform or inverse transform, the results are stored (in complex form) in the original data locations, available to the user for printout or manipulation.

As a final feature, the user may call subroutines to smooth the coefficients. The reason for wanting to smooth the DFT coefficients is that our data extends only over a finite time interval; this however, usually only represents the portion of the process we have chosen to record, and in fact, the process will often be infinite in duration. Using only that data we have recorded is equivalent to clipping the actual process at arbitrary end points in time. In the frequency domain this distorts the frequency components (DFT coefficients) from what they would be if we were to consider the process as having infinite duration in time. To reduce this distortion, the data points can be smoothed so that the clipping is not so pronounced. The drawback, however, is that some of the statistical value of the data is lost, since smoothing distorts the data in the time domain. Thus, it is wise to look at both the unsmoothed coefficients as well as the smoothed coefficients in any practical problem. In the program described in this paper, the smoothed results may either be simply printed out (CALL SMOOTHI) or placed in the data cells (CALL SMOOTH).

The program is available in the form of subroutines assembled in a binary deck. It is the option of the user to plot the data and to make his own printouts.

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A limitation of the CDC 3400 computer is that the index on the array B must run from 1 to N instead of from 0 to N=1. Therefore, in the actual program, B(j) is the DFT coefficient of C_{2} (j=1), N Δ t instead of j/N Δ t.

SUMMARY OF AVAILABLE SUBROUTINES

- B(n). $n=1, \ldots, N$ is assumed to be a complex array with $N=2^{M}$ elements.
- XFORM(M. B) computes the 2^M DFT coefficients of the series B(1), B(2), ..., B(N) and stores these coefficients in the array B, replacing the original series.
- INVERSE(M. B) computes the 2^M inverse DFT coefficients of the series B(1), B(2), ..., B(N) and stores these coefficients in the array B, replacing the original series.
- SMOOTH(M, B) smooths the 2^{M} DFT coefficients located in the array B. replacing the elements of B with these smoothed coefficients.

SMOOTH1(M. B) smooths the 2^M DFT coefficients located in the array B and prints the smoothed coefficients. The original coefficients are left undisturbed.

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SUNHOUTINE SMOUTH (K+B)
TYPE COMPLEX 8+ BEG+ XONE+ XTWO
 DIMENSION H(1024)
  KPUw=2**K
  HEGEB(1)
  XTW0=.25+(-B(2)+2.+B(')-B(KPOW))
  KPOWM=KPUW-2
  DO 5 JEL+KPOWM
  XONESTWO
  XTW0=,25*(=B(J)+2,*B(J+1)=B(J+2))
  A (J) #XUNE
5 CONTINUE
  KONE=XTWO
  XTW0=.25*(-R(KPUW-1)+2.*B(KPOW)-HEG)
  H (KPOH-1) =XONE
  H (KPO#) =XTWO
  HETURN
  END
```

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```
SUBHOUTINE SMOOTHL(K+H)
       TYPE COMPLEX B. BS
DIMENSION B(1024)
       PRINT 199
PRINT 200
        KPOW#2**K
        H5=+25*(-H(2)+2++B(1)-B(KPOW))
        ARL=CABS(BS)
        JL=0
        AFL=1.
        PRINT 201. JL. AFL. ARL. BS
        KPOWMEKPOW-1
        00 30 J#2. KPOWH
        JL=J-1
        HS=+25*(-H(JL)+2+8(J)-R(J+1))
        AEL=CABS(BS)
        AFL=AEL/ARL
        PRINT 201+ JL+ AFL+ AFL+ 85
  30 CONTINUE
        HS# _25*(-8(KPU#M)+2,*8(KPOW)-8(1))
AEL#CAHS(HS)
        AFL=AEL/AHL
AFL=AEL/AHL

PHINT 201, KPOMM, AFL, AEL, BS

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2* AHS VALUE = AHS VALUE OF COEF*,/* ADJ COEF = ARS VALUE *

3*DIVIDED BY ABS VALUF OF COEF AT ZERO*,//)

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1 *HEAL COEF*,3X,*IMAG COEF*,)

201 FOHMAT (1X,*FREU*,3X,*IMAG COEF*,2,2X,*(FR-2*F12-2))
201 FORMAT (1X.14.34.F8.5.3X.E9.3.3X.C(E9.2.E12.2))
        HETURN
        END
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APPENDIX C

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APPENDIX C

$\Lambda N \to X \Lambda MPLE$

In order to show how the program works, we shall compute the Discrete Fourier Transform of x()=sin(2π ft)=sin(2π t(4).

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N=64 data points T=64 so $\Delta t = -1$

a Fourier Series representation of this function is a pair of spikes at n=+16 and n=-16, corresponding to a sine wave of frequency $f = \frac{n}{T} + \frac{16}{64} = \frac{1}{4}$. Sampling x every $\Delta t=1$ seconds gives

$x(n) = sin(2\pi n/4)$.

The modulus of each of the DFT coefficients of x(n) is plotted in the accompanying graph. Note that there is indeed a peak at n=16, but as warned in appendix A, there is also a peak at n=64-16-48. This shows that we can only use the first N/2 coefficients when trying to detect periodicities. When using the DFT as a transform in its own right, this restriction does not necessarily hold.

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PROGRAM TEST
       TYPE COMPLEX A. CMPLK
       DIMENSION A(100), 8(100), X(100)
C.
       ANHAY A MUST BE IN COMPLEX FORM FOR USE IN SUMROUTINE XFORM
٩
       70 53 J=1. 64
       x(J)=(J=1)+1.
   50 A( )+CMP_X(SINF(2,+3,14159265+(J+1)/4,),+,)
C
С
       N=n; SINCE 2++6=64
       CALL XFG4M(64A)
A4RAV A NOW CONTAINS THE DET CONFETCIENTS
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С
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   AN COMPLIE AND PLUT THE AUSULUTE VALUE OF THE DET CONFEIGIENTS
NO 51 JE1:64
60 H(J):CARS(A(J))
      TALL PLOTTERIX, 0, 64, -16, 5HINDEX, 5, 12HCOEFFICIENTS, 12.
     1 274-70JHILH COEFFICIENTS, 20,0)
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References: (a) Cochrim et al., "What is the Fast Fourier Transform?" <u>IEEE Proceedings</u>, pp. 1664-1674, Oct 1967

- (b) Cooley, Lewis, and Welch, "Application of the Fast Fourier Transform to Computation of Fourier Integrals, Fourier Series, and Convolution Integrals," <u>IEEE Transactions on Audio and Electroacoustics</u>, pp. 79-84, Jun 1967
- (c) Brighan and Morrow, "The Fast Fourier Transform," <u>IEEE Spectrum</u>, pp. 63-70, Doi: 196

Note: The June 1967 is the OEEE Transaction on Audio and Electroacoustics is devoted to applications of the East Fourier Transform and Discrete Fourier Transform.

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