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**COMPARISON OF THEORETICAL AND
EXPERIMENTAL MODEL ROTOR
BLADE VIBRATORY SHEAR FORCES**

By

Lawrence J. Bain

October 1967

**U. S. ARMY AVIATION MATERIEL LABORATORIES
FORT EUSTIS, VIRGINIA**

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COMPARISON OF THEORETICAL AND
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BLADE VIBRATORY SHEAR FORCES

SER-50419

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Lawrence J. Bain

Prepared by

United Aircraft Corporation
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for

U. S. ARMY AVIATION MATERIEL LABORATORIES
FORT EUSTIS, VIRGINIA

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SUMMARY

An investigation was undertaken to obtain quantitative measurements of the vibratory forcing functions from the blades of rotary wing aircraft in the flight speed range encompassing both pure and compound helicopter operation. These measurements were made using dynamically scaled model rotor blades mounted on a specially instrumented rotor head. Testing was accomplished in the United Aircraft Corporation's 18 foot subsonic wind tunnel within a range of equivalent forward speeds from 75 to 300 knots and within a range of full scale rotor lifts from zero to 40,000 pounds. In addition to rotor performance, the final data include ten harmonics of the orthogonal blade root shear forces, rotor blade bending moments, and rotor control loads.

It was concluded from the experimental work that:

- 1) High harmonics of vibratory shear forces can be measured at the blade root over a wide range of speeds and lifts.
- 2) Only the first harmonic of flatwise and edgewise shear force is significantly effected by the flapping trim condition of the rotor.
- 3) Elimination of lag damping may increase or decrease the edgewise shear force, depending on its proximity of the operating condition to a blade natural frequency.
- 4) Increasing forward speed causes an increase in both flatwise and edgewise shear forces, the latter becoming predominant at the highest forward speeds.
- 5) Increasing rotor lift at constant forward speed causes a gradual increase in the magnitude of the flatwise shear force harmonics.
- 6) The radial shear force first harmonic longitudinal component takes on values which can be significant, but the fundamental nature of this force is not well defined.

The experimental results were correlated at seven test points with a fully coupled aeroelastic analysis. The evaluation of this work led to the following conclusions:

- 1) The inclusion of wake-induced velocity effects in the theoretical method shifts the calculated flatwise shear forces in a direction which improves the correlation but has no significant effect on the calculated edgewise shear forces.
- 2) The overall degree of correlation is strongly influenced by the accuracy to which the blade natural frequencies are known, the continuity of the calculated induced velocity distribution, and the predictability of the edgewise rotor blade behavior.

FOREWORD

This program was sponsored by the U. S. Army Aviation Materiel Laboratories (formerly U. S. Army Transportation Research Command) Fort Eustis, Virginia, and was monitored by Mr. Joseph McGarvey.

The experimental and theoretical research program was carried out from May 1964 through November 1965. Assisting in this program was Mr. P. J. Arcidiacono of the United Aircraft Corporation Research Laboratories, who directed the development of the rotor head and the impedance analysis.

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SYMBOLS

<u>Dimensional</u>		<u>Unit</u>
A_{1s}	lateral cyclic pitch	degrees
B_{1s}	longitudinal cyclic pitch	degrees
c	blade chord	feet
D	rotor drag	pounds
L	rotor lift	pounds
Q	rotor torque	foot-pounds
r	radial distance to local blade station	feet
R	rotor radius	feet
V	forward speed	feet per second
V_k	forward speed	knots
α_s	shaft angle of attack	degrees
α	rotor angle of attack, $\alpha_s - B_{1s}$	degrees
θ	collective pitch	degrees
ρ	mass density of air	slugs per cubic foot
ψ	azimuth angle, measured from downwind position in direction of rotation	degrees
Ω	rotor angular velocity	radians per second

SYMBOLS

(continued)

Nondimensional

b	number of blades
C_D/σ	rotor drag coefficient-solidity ratio, $D/\pi R^2 \rho (\Omega R)^2 \sigma$ $= D/R^3 \rho \Omega^2 bc$
C_L/σ	rotor lift coefficient-solidity ratio, $L/\pi R^2 \rho (\Omega R)^2 \sigma$ $= L/R^3 \rho \Omega^2 bc$
C_Q/σ	rotor torque coefficient-solidity ratio, $Q/\pi R^2 \rho (\Omega R)^2 R \sigma$
$M_{(x, \psi)}$	Mach number at radius station x and azimuth position ψ .
x	radius station, r/R
μ	advance ratio, $V/\Omega R$
σ	rotor solidity, $bc/\pi R$

Note: All Fourier series coefficients for shear forces and rotor blade flapping and lagging motions are based on the assumption of a positive series; i. e.,

$$f(t) = A_0 + A_1 \cos \Omega t + A_2 \cos 2\Omega t + \dots + A_N \cos N \Omega t + \dots \\ + B_1 \sin \Omega t + B_2 \sin 2\Omega t + \dots + B_N \sin N \Omega t + \dots$$

where A_N = Nth harmonic cosine coefficient

B_N = Nth harmonic sine coefficient

N = harmonic order

INTRODUCTION

As continual improvements have been made in the performance characteristics of rotary wing aircraft, attention to the problems of vibratory loading and associated structural fatigue has increased. The achievement of low fuselage vibration levels and subsequent improvement in aircraft component life and crew efficiency requires, however, a detailed knowledge of the origin of the forces which excite the fuselage. Prior to the start of this investigation, the cause-effect relationship between vibratory loading and fuselage response was not well defined. Previous studies, such as Reference 1, have presented rotor blade vibratory airloads and stresses, and successful attempts have been made to measure vibratory loads by instrumenting the rotor shaft, as in Reference 2. None of these studies, however, have reached the source of fuselage forced response; that is, the vibratory forces fed into the fuselage from the rotor blades at the blade root.

It was not considered feasible to design and fabricate a rotor head which could be instrumented to measure these vibratory forces until two conflicting objectives were resolved. First, maximum sensitivity had to be achieved so that higher harmonics of the loads could be accurately measured; second, the stress in the structural components of such a rotor head had to be minimized to reduce the probability of failure. The development of the semiconductor strain gage effectively closed the gap between these two objectives, thus making possible a detailed investigation of rotor blade vibratory root shear forces.

The purpose of the present investigation was to obtain quantitative measurements of the vibratory forcing functions from blades of rotary wing aircraft within the flight speed range encompassing both pure and compound helicopter operations. In addition, the degree of correlation between experimental results and theoretical calculations, including the effects of wake-induced velocities, was to be determined. The experimental data were to be obtained from wind tunnel tests of dynamically scaled model rotor blades mounted on a specially designed rotor head instrumented to measure flatwise, edgewise, and radial vibratory root shear forces.

The objective of this report is to present the experimentally obtained data and to place these data into a meaningful context by discussing, with specific examples, the effects of forward speed, rotor loading, lag damping, and flapping trim condition. The experimental results are correlated with a theory developed at Sikorsky Aircraft, described in Reference 3.

DESIGN DATA AND DESCRIPTION OF EQUIPMENT

ROTOR HEAD

The model rotor head was designed to utilize semiconductor strain gages having a gage factor of approximately 100. The structural components of the head, namely, the upper and lower plates, are 7075-T6 aluminum alloy. A fail-safe mechanism with a safety factor of 20 was provided to prevent major damage in the event of failure in the instrumented section. Figure 1 (a) shows the basic rotor head with the installed semiconductor strain gages, and Figure 1 (b) shows the assembly of the head. The pitch control horns are adaptable to pitch-flap coupling ratios of zero and unity, but the present investigation was conducted entirely in the $\delta_3=0$ configuration. Figure 2 is a schematic diagram showing the force and moment conventions and the location of the strain gages.

CALIBRATION

The model rotor head instrumentation was statically calibrated to determine primary slopes, interaction constants, and temperature compensation factors. In the course of this work it was found that to obtain a satisfactory calibration matrix, it was necessary to include measurements of the tangential moment on the instrumented section caused by the lag damper reaction and the edgewise shear force. The resolution of the shear force measurements based on the static calibrations and the noise level of the data acquisition system was determined to be:

Flatwise ± 0.17 pound

Edgewise ± 0.12 pound

Radial ± 0.05 pound

The repeatability of the shear forces determined during the wind tunnel testing and the magnitude of the calibration matrix elements resulted in a final shear force accuracy of ± 0.2 pound in all three directions. The flatwise and edgewise shear force strain gage circuits were each composed of two active and two dummy gages wired to measure the total shear force and to cancel bending in the instrumented section caused by the shear force. The radial shear force circuit was composed of four active gages in the Poisson arrangement. This circuit also measured the total shear force and cancelled bending. The tangential moment circuit was composed

of two active and two dummy gages to measure the bending moment on the upper instrumented section. All of the dummy gages were mounted on the unstressed center section of the upper plate.

ROTOR BLADES

The model rotor blades were untwisted, 9-foot diameter, 2.69-inch chord with an NACA 0012 airfoil section, and were dynamically scaled in flatwise, edgewise, and torsional stiffness properties from the Sikorsky S-56 (CH-37) main rotor blades.* With the specially instrumented, four-bladed rotor head, the rotor solidity is 0.0634. Figure 3 shows the components of a model blade and a fully assembled blade. The model spar was built up of laminations of fiber glass and paper. Trailing edge pockets were composed of balsa wood ribs covered with magnesium and were bonded to the spar. Figure 4 shows the blade spanwise mass and stiffness distributions, and Figure 5 shows the flatwise, edgewise, and torsional natural frequencies of the blade as functions of rotor speed.

The development of the fiber glass model blades evolved from dynamically scaled model rotor blades made of aluminum, used in studies such as Reference 4. These metal blades were designed to operate at full scale tip speeds, but the investigation of rotor behavior at high forward speeds necessitated the development of blades which would retain their dynamic similarity while operating at reduced tip speeds. The reduced speeds resulted from the desire to simulate forward speeds higher than the wind tunnel limit of 175 knots. Reference 5 describes the development of this type of blade using reduced-stiffness spars of fiber glass-paper laminate construction. The various scaling ratios, listed in Table III, are taken from reference 5. The stiffness of the composite spars is scaled in the flatwise, edgewise, and torsional directions from full scale values. The resulting stiffnesses are reduced from those of the aluminum model blades by a factor of 5.5, so that the reduced experimental velocities are $1/\sqrt{5.5}$ times the full scale velocities. For example, at an actual tunnel speed of 100 knots, the fiber glass rotor blades are dynamically similar to the full scale blades operating at $100\sqrt{5.5}$ or 235 knots, and this speed is referred to as the equivalent forward speed.

* The full scale S-56 main rotor blades are twisted -8 degrees

WIND TUNNEL

Testing was conducted in the United Aircraft Corporation's large subsonic wind tunnel. This is an atmospheric-density, closed-return tunnel powered by a 9000-horsepower motor and having a maximum speed of approximately 175 knots. The test section is octagonal in cross section, 18 feet across the opposite flats. Remotely controlled air exchangers are employed to maintain constant stagnation temperature during operation. Figure 6 is an artist's drawing depicting the general arrangement of the tunnel.

HELICOPTER ROTOR TEST RIG

The helicopter rotor test rig (HRTR) is equipped with a six-component strain gaged balance and is powered by a variable frequency electric motor rated at 375 horsepower at 6000 rpm. Figure 7 (a) shows an overall view of the HRTR mounted in the wind tunnel, and Figure 7 (b) shows the details of the hub and swash plate area. The coincident flapping and lagging hinges are located at the 5.6 percent radius station. Lagging motion is restrained by rotary viscous dampers having a nominal damping factor of 1.9 foot-pound-second for a lag motion amplitude of 1 degree. This value represents 55 percent critical damping. The model dampers have an adjustable damping feature which permits the selection of any desired damping factor within a moderate range determined by the working fluid in the damper. The dampers were set to the above value by calibrating them in a special calibration fixture which operates the damper at a specified frequency and amplitude and records the resulting torque output. The damper was adjusted in small increments until the proper combination of frequency, amplitude and torque was reached. There was a small phase difference between the application of the force to the damper and the minimum force output indicating the presence of spring force in the damper. This was taken into account in the calibration so the value stated above represents the pure damping output. Rotary transformers are used to sense flapping and lagging motion. A conventional swash plate is driven by three precision electric actuators. Collective and cyclic pitch are remotely set from a servo system in the wind tunnel control room, and the yaw table of the wind tunnel provides variation in shaft angle of attack.

The HRTR drive motor is supported by frictionless hydrostatic oil bearings. The motor case is restrained from rotation by a strain gage torque beam to measure rotor torque. Axial displacement of the motor-shaft system is limited by a strain gage thrust beam. The rotor head is supported by a four-component strain gage balance which was not used in

this test program, as this balance is sized for larger forces than were anticipated for this test. Electric signals are transmitted from the rotating system to the stationary system through a 100-channel slip ring assembly.

Dynamic data from the rotor test rig are recorded on a 20-channel EPSCO data acquisition system. Each channel is scanned 36 times per revolution for six revolutions. The information is received from the HRTR in analog form, digitized, and recorded on magnetic tape. These data are transmitted to an IBM 7094 data processing unit and reduced. The primary data reduction program reduces the performance data to dimensional and coefficient form in the wind and shaft axes systems. Tare forces and moments on the rotor hub, obtained with the blades removed, are subtracted from the measured data, so that the reduced performance data correspond to that from the rotor blades alone. Blade motions and bending moment data are reduced to average and peak-to-peak values. The secondary data reduction program performs a harmonic analysis on all 20 channels of information. The measured shear force and tangential moment data are further reduced to correct for calibration interactions and blades-off tares, and finally these data are corrected for the effects of hub flexibility, as discussed in the section on experimental procedures.

THEORETICAL METHOD

The theoretical method of Reference 3 was used to correlate the experimental data obtained in this program. This method is a fully coupled flatwise, edgewise, torsional aeroelastic analysis based on an extension of Myklestad's method for rotating beams. A variable inflow analysis, developed by the Cornell Aeronautical Laboratory, Inc. (CAL) and described in Reference 6, was combined with the blade aeroelastic analysis. The analytical procedure included an initial determination of flatwise and torsional rotor blade motion with a uniform inflow iteration to obtain required values of rotor lift and propulsive force. This information was used in the CAL analysis to obtain a distribution of induced velocity at ten radial blade stations and twenty-four azimuth locations. With this distribution, using the first flatwise shear force harmonic as a boundary condition, a second iteration was made on the rotor lift and propulsive force, which gave final values of blade motions and loadings.

SIGN CONVENTIONS

The sign convention used is that a positive sign indicates:

<u>Measurement</u>	<u>Direction</u>
Flatwise Shear Force	Upward
Edgewise Shear Force	In direction of rotor rotation
Radial Shear Force	Radially outward from rotor ζ
Flatwise Bending Moment	Upper surface in compression
Edgewise Bending Moment	Trailing edge in compression
Torsion Moment	Leading edge upward
θ	Leading edge upward
α_s	Rotor Shaft tilted downstream
A_{1s}	Pitch reduction at $\psi = 0$ degrees
B_{1s}	Pitch reduction at $\psi = 90$ degrees

EXPERIMENTAL PROCEDURE

HELICOPTER ROTOR TEST RIG IMPEDANCE

Since it is desirable to have vibratory shear force results which are independent of the particular rotor test rig employed, the measured shear forces must be corrected for the effects of the displacements of the hub, which induce extraneous forces in the instrumented section of the rotor head. These displacements are caused by the shear forces themselves; therefore, the correction factors must be determined from the test data in conjunction with predetermined properties of the rotor test rig.

The analytical background of this procedure is based on the fact that the deflections of the rotor hub can be predicted with a knowledge of the applied forces. Such deflections are determined by dividing the measured shear forces by an experimentally determined rotor hub impedance. The product of this quotient and the rotor blade impedance, determined analytically, yields the force induced on the blade by the hub motion. This force is then subtracted from the measured results to produce the final shear force, reflecting only the effects of the rotor blade loading and no effects of the supporting structure motion. The correction can be written in the form of a matrix equation, as follows:

$$\left\{ \text{corrected shear force} \right\} = \left\{ \text{measured shear force} \right\} - \left[\text{theoretical blade impedance} \right] \times \left[\text{experimental HRTR impedance} \right]^{-1} \times \left\{ \text{measured shear force} \right\}$$

To determine the rotor test rig impedance, a special rotor head was fabricated which matched the weight of the one to be used in the wind tunnel testing. This head was mounted on the HRTR in the wind tunnel, and to it was attached an electromagnetic shaker with appropriate instrumentation to measure forces and displacements. By taking measurements over a range of excitation frequencies in the axial and in-plane directions, the variation of HRTR impedance and principal axes was determined within the range of frequencies to which the rig would be subjected during actual testing. For a rotor with "n" blades, the nth harmonic of the flatwise root shear forces combine to produce an n/rev vertical excitation of the fuselage. The (n + 1) and (n - 1) harmonics of the flatwise root shears combine to form n/rev hub moments resulting in vibratory pitching and rolling moments of the airframe. The (n + 1) and (n - 1) harmonics of the edgewise root shear forces combine to form n/rev longitudinal and lateral in-plane forces at the rotor head. Since the

test rotor was a four-bladed configuration, only the third, fourth, fifth, seventh, eighth, and ninth shear force harmonics affected hub motions. Because in an "n" bladed rotor system only integer multiples of the $n\Omega$ frequency will be seen in the fixed system, the hub motion corrections were confined to the four-per-revolution and eight-per-revolution frequencies. The final test conditions were selected, whenever possible, so that the rotor speeds would correspond to frequencies away from those of low HRTR impedance, in order to minimize the correction factors on the measured data. The corrections of the shear forces based on this analysis were approximately 0.1 pound throughout the test, and the maximum correction was approximately 0.7 pound. It was determined prior to testing that the motion of the HRTR would not alter the rotor blade impedance characteristics by a significant amount, so that these characteristics were reduced to functions of rotor speed only. An example of the HRTR impedance matrix for a rotor speed of 636 rpm is given below.

	upstream direction		advancing blade direction	
	real	imaginary	real	imaginary
4 per rev.	- 1570 lb/in.	- 765 lb/in.	- 7050 lb/in.	- 2420 lb/in.
8 per rev.	- 3750 lb/in.	- 4920 lb/in.	- 4920 lb/in.	- 4750 lb/in.

The impedances in the rotor shaft direction were large enough to be considered infinite in comparison to the impedances shown in the above matrix.

WIND TUNNEL TESTING

The wind tunnel testing procedure was to set a desired rotor tip speed, shaft angle of attack, and tunnel speed and then to record data at each of a series of increasing collective pitch settings. The minimum value of collective pitch was that required for zero thrust; and at each collective pitch, longitudinal and lateral cyclic pitch were adjusted to eliminate first harmonic flapping in respect to the rotor shaft. This cyclic pitch condition was defined as trimmed. For some test conditions, the cyclic pitch values were set to yield longitudinal first harmonic flapping of -4 degrees (forward), while holding the lateral flapping at zero to determine the influence of out-of-trim flapping on the vibratory shear forces. The maximum collective pitch was determined by the limiting vibratory stress amplitude on the rotor head or blades. The tested rotor operating conditions are shown in Figure 8 and Table I. In the remainder of the report these conditions are referred to by the nominal advance ratio values, 0.2, 0.3, 0.4, 0.5, 0.7, and 1.0.

EXPERIMENTAL RESULTS

Table I is a listing of each test point in this program. Shaft and rotor angle of attack, non-dimensionalized thrust and torque, nominal collective pitch, and flapping and lagging motion are listed for each advance ratio. The flapping and lagging motion harmonic amplitudes are printed to three decimal places since the reproduction of the table was done directly from the test data through the data processing unit, but these amplitudes are only accurate to one decimal place or 0.1 degree.

The complete test results are presented in the appendices, and the most significant of these are presented again and discussed in the following section.

The first through tenth harmonic orthogonal components of flatwise and edgewise vibratory shear force obtained in the wind tunnel tests are presented in Appendix I. The flatwise force coefficients are shown as functions of rotor lift coefficient-solidity ratio, and the edgewise force coefficients as functions of rotor torque coefficient-solidity ratio. These data are grouped by advance ratio, each group covering a range of shaft angle of attack.

The first through fourth harmonic orthogonal components of radial shear force are presented in Appendix II. The first harmonic cosine coefficient is shown as a function of rotor angle of attack for constant collective pitch at each advance ratio. The variation of this coefficient with changes in trim and lag damping is indicated by flagged and double flagged symbols, respectively. None of the other harmonic coefficients of radial shear force reached magnitudes approaching those of the first cosine harmonic, instead, they were approximately one pound or 0.3 percent of the steady radial load. The radial shear force harmonics above the fourth did not exceed the one pound level at any test point and are not presented. The remaining radial shear force coefficients are given as functions of rotor lift coefficient-solidity ratio.

Flatwise rotor blade bending moments were measured at four radial stations on the blade at 21, 33, 47, and 64 percent radius. Throughout the range of test conditions, the flatwise moment at the inboard station, 21 percent radius, was consistently the largest measured moment. This fact is substantiated in the following section of the report. The radial locations of the largest measured edgewise and torsional moments are also verified in that section. Part (a) of the figures in Appendix III gives the one-half peak-to-peak values of the flatwise moment at 0.21R as it varies with rotor angle of attack for constant collective pitch and

advance ratio. A flatwise moment of 21 inch-pounds at this radial station on the blade corresponds to a stress of 10,000 psi on an equivalent rotor blade made of aluminum; i. e., it has the same unit strain. Edgewise bending moments were measured at 21, 33, and 47 percent radial stations on the blade. The location of the maximum measured value varied between the inboard and outboard stations within the range of test conditions. Part (b) of the figures in Appendix III presents the one-half peak-to-peak edgewise moment at the 21 percent station as a function of rotor angle of attack for constant collective pitch and advance ratio. An edgewise moment of 56 inch-pounds at this station on the blade corresponds to 10,000 psi edgewise stress on an equivalent aluminum blade. Part (c) of the same set of figures is a plot of the moments measured in the edgewise direction at the 47 percent radial station, with 29 inch-pounds giving the equivalent of 10,000 psi stress. The rotor blade torsional moment was measured at the 17.5, 38, and 90 percent radial stations. The inboard moment was largest at all test points, and its one-half peak-to-peak value is presented in part (d) of the figures of Appendix III in a manner identical to that of the other blade moments. A 35 inch-pound torsional moment at the 17.5 percent radial station corresponds to 10,000 psi on the equivalent aluminum blade. The change in each of the three blade bending moments resulting from out-of-trim operation is indicated by the flagged symbols on the plots for the advance ratio of 0.2. The change resulting from elimination of lag damping is indicated by double-flagged symbols on the plots for advance ratios 0.2 and 0.5.

Rotor control loads were measured on the push rod for the instrumented blade. The one-half peak-to-peak values of this load are presented in Appendix IV in a form identical to that of the blade bending moments.

EVALUATION OF EXPERIMENTAL RESULTS

OUT-OF-TRIM OPERATION

The effect of out-of-trim operation of the flatwise and edgewise vibratory shear forces can be seen by comparing parts (a) and (b) of Figure 9, which are taken directly from Appendix I. The only force harmonic which is significantly altered by adjusting the first harmonic flapping with respect to the shaft to -4 degrees in the longitudinal direction is the first harmonic, which produces a pitching moment in the fixed system of coordinates. In particular, the amplitude of the first harmonic shear in both the flatwise and edgewise directions takes on a value on the order of double that of trimmed operation. This behavior is what would be expected since a one per revolution forcing function is being introduced in the system. Figure 9 also shows that the phase of the first harmonic shear force becomes less sensitive to changes in rotor lift when the rotor is taken out-of-trim. The effect on the cosine component of the first radial shear force harmonic is not well defined, but the points in Figure 60 of Appendix II indicate that this component is generally increased by operation out-of-trim. The data in Figure 85 of Appendix III reveal that the principal effect of out-of-trim operation on blade bending moments is an increase in the one-half peak-to-peak flatwise moment approximately equivalent to that resulting from a 2-degree increase in collective pitch or roughly a 7500-pound increase in full-scale rotor lift. However, the edgewise and torsional moments are not significantly altered. It should be noted that because of the flapping and lagging motion of the blades, the blade bending, and the variation of the blade pitch over the rotor disk; the axis system in which the blade bending moments are measured is being continually displaced in both translational and rotational directions with respect to the axis system in which the root shear forces are measured. As a result, there is a large interaction between events occurring in any one direction of the blade axis system and the three directions of the shear force axis system. This effect is seen above where operation out-of-trim caused a change in the edgewise shear force with no significant change in the edgewise blade bending moment.

EFFECT OF LAG DAMPING

The effect of lag damping on the vibratory shear forces and blade moments must be evaluated in light of the proximity of the rotor operating condition to an edgewise blade natural frequency. For this reason two rotor speeds are considered. At the advance ratio of 0.2, the first edgewise bending frequency is very nearly three per revolution, whereas

at the higher advance ratio , 0.5, at which the rotor tip speed is reduced, the first edgewise bending frequency is farther removed from a resonance point, as shown in Figure 5. Comparing parts (a) and (b) of Figure 10, which is taken directly from Appendix I, it is seen that removal of the lag damping at the condition near the edgewise natural frequency results in an increase in the edgewise shear force harmonics shown, particularly the third; which displays an increase in maximum amplitude of about 25 percent. Removal of lag damping at the other condition results in a decrease in the edgewise shears, as seen by comparing parts (a) and (b) of Figure 11. The third harmonic amplitude decreases 20 percent at $C_Q/\sigma = 0.005$ for this case. The remaining shear force harmonics for these four test conditions, given in Appendix I, show that the edgewise force harmonics above the fourth behave essentially the same as those shown in Figures 10 and 11 and that the flatwise shear force increases with the removal of lag damping at both rotor speeds. The latter effect results from the increase in flatwise blade bending moments discussed below. The effect of lag damping on the radial shear force is not clearly indicated by the data taken from $\mu = 0.2$, but Figure 63 of Appendix II for $\mu = 0.5$ shows a definite pattern in which the first cosine harmonic is initially reduced but later reverses as the collective pitch is increased and eventually increases at the higher collective pitches.

The data in Appendix III show that removal of lag damping results in a slight increase in flatwise and torsional blade bending moments at both rotor speeds. This moment increase is largest at the high collective pitch settings and is essentially zero at the low settings. This effect is a result of the fact that, experimentally, more longitudinal cyclic pitch was required to maintain the rotor in a trimmed condition when the lag damping was removed than with full lag damping. It is not clear why this additional cyclic pitch is necessary, but the effect is consistent throughout the test. The edgewise bending moments at the inboard radial station are increased at both rotor speeds by an amount equivalent to a one degree increase in collective pitch or an increase in full scale lift of approximately 4000 pounds. At the outboard station the increment in edgewise moment due to the removal of lag damping is much larger at the higher rotor speed than it is at the lower speed. The increase at the lower speed at this station is of the same order of magnitude as the increases on the inboard station. This is seen in Figure 12, which is a plot of data extracted from Appendix IV. This effect of rotor speed on the edgewise response to changes in lag damping, is related to the effects of the rotor operating condition's being near an edgewise natural frequency, already discussed in connection with the edgewise shear force. It would be expected that the removal or reduction of lag damping at rotor speeds

remote from an edgewise natural frequency would cause a reduction rather than an increase in the edgewise bending moments because the restraining load on the blade root is reduced. For the rotor speed in question, however, Figure 5 shows that the test point is not sufficiently removed from the critical speed to preclude the presence of resonant excitation effects. The trend of reduction in edgewise bending moment and shear force with changes in rotor speed away from the critical value is clear, nevertheless, and for an advance ratio of 0.7, Figure 12 shows edgewise moments which are considerably lower than those measured with full lag damping.

EFFECT OF FORWARD SPEED

Figure 13 shows the effect of forward speed on the flatwise and edgewise shear forces. The amplitudes of the second through tenth harmonic coefficients, derived from the data presented in Appendix I, are presented as functions of advance ratio for a constant rotor lift coefficient - solidity ratio of 0.035 and a shaft angle of attack of -4 degrees with the rotor trimmed to zero flapping with respect to the shaft. The shear force amplitudes are nondimensionalized by the lift per blade to provide an indication of the magnitude of the vibratory loads relative to the steady loading on the rotor. The flatwise vibratory loading shows a general increase with forward speed in all harmonics. In some harmonics, particularly the third and fourth, the increase is very rapid as the advance ratio exceeds 0.5. The same pattern is evident in the edgewise vibratory loading, with the third and fourth harmonics again reaching very large values at $\mu = 0.7$. This flatwise and edgewise shear force response stems directly from the change in the behavior of the rotor blade in the edgewise direction as the forward speed is increased. This change is discussed below. The effect of forward speed on the first cosine harmonic of the radial shear force can be assessed from Figures 60 through 64 in Appendix II. In general, increasing forward speed causes this shear component to change from a nose down pitching moment component to a nose up component. The magnitude of this shear force was not anticipated and the cause of the measured behavior could not be determined without an extensive analytical effort, beyond the scope of the present study.

Figure 14 presents the one-half peak-to-peak blade bending moments as functions of advance ratio. The test points, listed in Table II, included those for $\alpha_s = -4$ degrees for $\mu = 0.2, 0.4, 0.5,$ and $0.7,$ and for $\mu = 0.3$ with $C_L/\sigma = 0.062$. The lift coefficient-solidity ratios are not constant for these five points but decrease with forward speed, as would be the case in compound helicopter operation, from

$C_L/\sigma = 0.071$ at $\mu = 0.2$ to $C_L/\sigma = 0.032$ at $\mu = 0.7$. The results shown represent a more realistic situation as compared, for instance, to the case with a constant C_L/σ equal to 0.032. The blade moments in all three directions increase with advance ratio. The edgewise and torsional moments are strongly influenced by the forward speed above the 0.5 advance ratio. It is notable that the maximum flatwise bending moment occurs at the inboard radial station throughout the forward speed range as does the maximum torsional moment, while the edgewise moment shifts from the inboard end of the blade to the outboard end as the forward speed is increased. The time histories of these moments can be seen in Figures 18, 21, 22, 23, and 24; and it is evident that the shift of the maximum edgewise bending moment station is a result of the change in the participation of edgewise bending modes. At the low advance ratios the first elastic mode predominates, but as the speed is increased additional modes become significant so the station of maximum bending moment is changed accordingly. It should also be noted that with the flatwise stiffness distribution given in Figure 4, the maximum bending stress tends to occur at the 64 percent radial station, which is in accord with flight measurements.

The time histories of the flatwise, edgewise, and radial shear forces at the same five test points are shown in Figures 15, 16, and 17; from them the change in harmonic content with forward speed can be observed. As the advance ratio is increased from 0.2 to 0.4, the first harmonic predominates in all three directions with some high harmonics of small amplitude appearing in no definite pattern. Above 0.4, all of the forces are predominately fourth harmonic. This effect would cause a change in the fuselage forcing functions from a steady moment at the low speeds to a four per revolution excitation at the high speeds. The cause of this variation of shear force harmonic content can be determined from the points in question shown in Figures 18 through 24, which present the azimuthal plots of blade bending moments at all seven points listed in Table II. The striking feature in these plots is the character of the edgewise bending moment at the high advance ratios. Essentially, it is composed of the fourth harmonic with an amplitude on the outboard station reaching 20 inch-pounds. Since the flatwise bending moment does not exhibit the same character, it can be concluded that at the 0.7 advance ratio the shear forces are primarily influenced by the edgewise blade bending through the mechanism of the displacement of the blade axis system from the shear force axes system.

Looking now at the change in harmonic content of the blade bending moments with forward speed in Figures 18, 21, 22, 23, and 24, the edgewise moment is seen to be essentially third harmonic at the lower

advance ratios as would be expected because of the nearness of the rotor speed to the edgewise natural frequency point. At the higher advance ratios, however, the rotor speed is reduced and moves away from the critical speed, but does not closely approach the four per revolution natural frequency. Therefore, the edgewise behavior at these high advance ratios cannot be categorically attributed to resonant excitation. The list of lag motion harmonics in Table I for the $\mu = 0.7$ data point shows a fourth harmonic amplitude larger than any others but the first, and a comparison in Table I with the lower speed points reveals that the first harmonic lag motion dominates all other harmonics in amplitude. Although the magnitudes being compared are on the borderline of the measuring system accuracy, an aerodynamic source of the high speed edgewise behavior is implied; but this has not been positively determined. It was observed during testing that removal of the lag damping at the high forward speeds resulted in a reduction of the fourth harmonic magnitude and in an increase in the third harmonic magnitude of the edgewise blade response. It should also be noted that the test data at $\mu = 1.0$ show the same effect: a large fourth harmonic with lag damping and a shift toward the third harmonic with reduced lag damping, even though the rotor speed is 15 percent lower at this condition than it is in the $\mu = 0.7$ condition. Investigation of this phenomenon is impeded by the shortage of experimental dynamic data at high forward speeds and by the complexity of the actual lag damper behavior. While the moment output is nominally pure damping linearly related to the velocity, as discussed in the section entitled "Helicopter Rotor Test Rig"; there is some spring content which varies in a complex manner with frequency and amplitude. The exact determination of these characteristics is beyond the scope of the present study. In this program, the structural limitations of the special rotor head precluded extensive data taking at the high advance ratios because of the very large vibratory forces involved. Designing for such large forces would have reduced measuring accuracy at lower values of advance ratio, μ .

The torsional moment in Figures 18 through 21 is essentially first harmonic in character at the low forward speeds, reflecting the cyclic pitch input. At the higher speeds, appearing first at an advance ratio of 0.4, the torsional moment has an increasing content of high harmonics, particularly at the inboard stations. At the two highest advance ratios, 0.5 and 0.7, presented in Figures 23 and 24, the eighth harmonic response can be traced to the proximity of a natural frequency at 580 rpm. The harmonic content of the flatwise bending moments is difficult to visualize because of the effects of high seventh, eighth, ninth, and tenth airload harmonics at all forward speeds. It is apparent, however, from Figures 18 through 24, that the third and fourth harmonics

show a large increase with increasing forward speed relative to the increases that take place in the high harmonics. None of this is attributable to resonant excitation of flatwise modes, but coupling with edgewise blade response undoubtedly contributes to this part of the flatwise response, particularly since both the collective and cyclic pitch settings are high under these conditions; i.e., $\theta = 12$ degrees, $B_{1s} = 13.7$ degrees at $\mu = 0.7$.

EFFECT OF ROTOR LIFT

Figures 25, 26, and 27 present the time histories of the flatwise, edgewise, and radial shear forces at a constant advance ratio of 0.3 for a range of rotor lift under trimmed conditions. A phase change in the first harmonic is readily apparent in all three components. In addition, the initial reduction and subsequent increase in this harmonic can be seen by comparing the middle load conditions with the high and low conditions. This comparison also reveals that the magnitude of the higher harmonics changes very little over the range of lift. It should be noted that the lowest equivalent forward speed in this program was approximately 75 knots, and due to the variation of wake-induced velocity effects with forward speed, the results discussed herein cannot generally be extrapolated to lower speeds.

The correlation between rotor thrust level and vibratory loading is shown in Figure 28. The amplitudes of the flatwise and edgewise shear force harmonics, obtained from Figure 50 of Appendix I, are presented as functions of rotor lift coefficient - solidity ratio at an advance ratio of 0.3 and a shaft angle of attack of -4 degrees. The amplitudes are nondimensionalized by the lift per blade, and data for C_L/σ below 0.04 are not plotted in order to avoid the distortion that takes place as the lift goes to zero. The low flatwise harmonics show an increase as the rotor lift increases. Except for the seventh and tenth, the harmonics above the fourth remain low throughout the range of lift. The rotor speed at this advance ratio, $\mu = 0.3$, yields an operating condition close to the seven per revolution natural frequency of the third flatwise blade bending mode and the ten per revolution natural frequency of the fourth flatwise mode, explaining the departure of the seventh and tenth harmonics from the pattern of the others. Looking at the harmonics of flapping motion for $\mu = 0.3$ and $\alpha_s = -4$ degrees, it is seen that the amplitudes of second, third, and fourth harmonic flapping increase with rotor lift. It is this effect which produces the increase in the flatwise shear force second, third, and fourth harmonics seen in Figure 28. The correlation between the rotor thrust level and the nondimensional edgewise shear force harmonic amplitudes is similar to that of the flatwise case for the

low harmonics although it is not as marked. The edgewise amplitudes above the fourth harmonic remain low throughout the lift range and do not exhibit even the small increase at the highest lift that was seen in the flatwise harmonic amplitudes.

The vibratory shear forces data presented in Figures 9, 10, 11, 13, 15, 17, and 25 through 28 are taken from only a very small number of the test conditions included in Appendix I. Sufficient information is given in Table I and Appendix I to enable the reader to replot the data of any of the 116 test conditions in any of the forms used herein and to evaluate specific operating conditions in more detail.

CORRELATION OF THEORY AND EXPERIMENT

The experimental data for the seven test points listed in Table II were correlated with the theoretical method of Reference 3.

Figures 29 through 35 present the measured and calculated shear force harmonic amplitudes. In Figures 29, 32, 33, and 35, the results of uniform inflow computations are also shown. In comparing the measured flatwise shear force harmonic amplitudes with the calculated variable inflow values, the second and fifth harmonics show the most consistent difference among the seven subject points. In all cases, except at $\mu = 0.7$, it was found that the fourth and/or fifth harmonic of induced velocity on the inboard segment of the blade, as computed in the variable inflow analysis, was higher than any other harmonics above the second. The effect of this on blade response can also be seen in the calculated flatwise blade bending moments at $\mu = 0.3, 0.4, 0.5$, shown in Figure 36. In the case of a large second harmonic difference, it was found that the calculated rotor wake produced a flatwise loading on the outboard portion of the blade which was essentially composed of a two per revolution load. This resulted in a blade flapping motion in which the primary component was second harmonic. For example, examination of the flapping coefficients given in Table I for the $\mu = 0.5$ point reveals a second harmonic magnitude of 0.8 degrees as opposed to the calculated value of 1.3 degrees.

Looking in particular at the $\mu = 0.2$ case, the flatwise bending moment presented in Figure 37 shows a sharp peak at the 165-degree azimuth in the calculated values that are present, but is greatly attenuated in the measured values. The cause of this peak was traced to the representation of the rotor wake, in which a tip vortex from one blade is passing under the inboard end of the following blade. Since the circulation is assumed to be concentrated at the vortex core, a rapid increase in induced velocity is felt by the blade, and the high peak in bending moment results. In the physical case with a finite vortex core, the increase in induced velocity is more gradual and the blade response is less drastic, as seen from the measured results in Figure 37. It was analytically determined that a peak such as that given by the calculations would cause an increase in the magnitudes of all harmonics, and it is seen that a downward shift of the calculated shear force harmonics in Figure 29 would yield a much better correlation in every harmonic. As the forward speed and rotor lift are increased and the wake is washed away from the rotor, this peaking effect is diminished as the subject vortex passes under the aft part of the rotor.

The remaining significant differences in the measured and calculated flatwise shear forces are in the seventh harmonic at $\mu = 0.2$ and the fourth harmonic at $\mu = 0.7$, as shown in Figures 29 and 35, respectively. The latter difference stems from the fact that the large fourth harmonic edgewise blade bending discussed earlier in conjunction with the measured shear force data is not predicted in the computations, even though the flatwise blade bending moment correlation is not unreasonable, as seen in Figure 37. The magnitude of the computed seventh harmonic at the low speed is a result of a resonant excitation of the third flatwise bending mode of the blade caused by a seventh harmonic-induced velocity component over the inboard blade segments having a value nearly equal to the steady induced velocity.

The flatwise shear force harmonics calculated with the assumption of uniform inflow show a steady decrease in magnitude as the harmonic order is increased. The measured results, however, do not follow this pattern, and it is evident that without the higher harmonic excitation provided by a variation in induced velocities, there is no possibility of accurately predicting the harmonic content of the vibratory shear forces. At the high advance ratio, $\mu = 0.7$, the difference between the uniform and variable inflow results is very small, but the analysis of wake-induced velocities used in this program was not developed for use at high speed. Therefore, the similarity of the two results does not necessarily imply that the effects of wake-induced velocities can be neglected at high speeds. Figure 39a, which shows the measured and calculated flatwise shear forces as functions of azimuth position, verifies that an accurate knowledge of harmonics is the key to vibratory shear force analysis.

Comparison of the measured values of edgewise shear force harmonic coefficients with the calculated variable inflow values, Figures 29 and 32 through 35, reveals a steady decrease in the degree of correlation as forward speed is increased. This is primarily evident in the low harmonics, where the measured values display a magnitude increase not matched by the theoretical values. The agreement of the higher harmonics is better, but only to the extent that both calculated and measured values remain small. It was shown earlier that all the harmonics of edgewise shear force tend to increase with forward speed, but no such trend is evident in the calculations. This absence, then, is the major deficiency in the edgewise shear force analysis. Since the nature of the blade edgewise behavior at the high advance ratios is not well understood because of the undefined effects of such things as the lag dampers and the blade counterweights, and even though calculated results compare favorably at an advance ratio as high as 0.5, as seen in Figure 38, very little can be said about the correlation of edgewise shear forces.

The results presented do, however, highlight the need for additional theoretical and experimental analyses of rotor behavior at high forward speeds.

The uniform inflow results and the comparative time histories of the edgewise shear forces, Figure 39b, add nothing to the understanding of the problem at hand. There is no significant difference between the uniform and variable inflow results, and both results differ from the measured values to a large extent. The induced velocity analysis does not account for variations of in-plane velocities, but whether or not the inclusion of these would effect the degree of correlation of the edgewise shear forces could not be determined within the scope of this investigation.

With respect to the overall correlation effort, it is felt that although there is considerable room for improvement, the results are encouraging in view of the fact that it has been impossible to even attempt such a correlation in the past for lack of detailed experimental data. The deficiencies in the flatwise shear force calculations clearly point to the areas in which improvements should be made. Namely, the especially restrictive comparison by harmonics demands that the wake-induced velocities be free of sudden large variations and that the rotor blade natural frequencies be well defined through the high modes. In addition, the strong influence of the aeroelastic behavior of the rotor blade in the edgewise direction necessitates a fundamental understanding of this behavior before a better degree of correlation can be achieved at high speeds.

CONCLUSIONS

The results of the experimental investigation of the vibratory shear forces generated by an individual helicopter rotor blade of a four bladed rotor system led to the following principal conclusions:

1) The harmonic content of vibratory shear forces can be accurately determined over a wide range of forward speeds and rotor lifts through the use of high sensitivity semiconductor strain gages.

2) The trim condition of the rotor exerts a strong influence on the amplitude and phase of the first harmonic flatwise and edgewise shear forces, but has no appreciable effect on other harmonics. The change in amplitude of the first harmonic forces is proportional to the amount of out-of-trim flapping. The trim condition exhibited no well defined effect on radial shear forces.

3) Removal of linear viscous lag damping results in a slight increase in the flatwise shear force and either an increase or a decrease in the edgewise shear force, depending on the nearness of the rotor speed to a rotor blade edgewise natural frequency.

4) Increasing forward speed over a range of from 75 to 300 knots results in a gradual increase in the flatwise shear force. The edgewise shear force remains essentially constant from 75 to 175 knots and then increases rapidly from 175 to 300 knots, becoming the predominate force at the highest speeds. At forward speeds above 200 knots, the edgewise bending of the blade dominates the shear forces in all three directions to result in a significant change in the harmonic content of the shear forces over the total speed range.

5) Increasing the rotor lift at constant forward speed produces a gradual increase in the flatwise vibratory shear force. A similar effect takes place in the edgewise shear force, but it is confined to the low harmonics.

6) The longitudinal first harmonic component of the radial shear force can take on values having a magnitude equal to those of the other shear forces under high rotor lift conditions at low forward speeds and under low rotor lift conditions at high forward speeds. The fundamental nature and significance of the radial shear force could not be determined within the scope of this investigation.

The comparison of experimental results and theoretical results obtained with a fully coupled aeroelastic analysis led to the following

principal conclusions:

- 1) The inclusion of the effects of wake-induced velocities alters the theoretical results in a direction which improves the correlation of the flatwise shear forces.
- 2) The natural frequencies of the rotor blade must be well defined through the high harmonic range, because the use of wake-induced velocities in the theoretical analysis necessarily introduces high harmonic forcing functions which excite a response in the blade that can be directly reflected in the vibratory shear force harmonics.
- 3) The theoretical distribution of induced velocities must be free of singular points having velocities greater by an order of magnitude than the surrounding points, because the singular points tend to introduce errors in all the harmonics of a force under consideration.
- 4) The deterioration of the degree of correlation of edgewise shear forces with increasing forward speed indicates the need for an improved theoretical and experimental definition of edgewise rotor blade aeroelastic behavior.
- 5) The inclusion of wake-induced velocities has no significant effect on the degree of correlation of edgewise shear forces.

RECOMMENDATIONS

A more complete understanding of the origin of fuselage excitation requires additional research in the following areas:

1) The existing model rotor should be tested through the low speed range in a wind tunnel having a larger cross section than that of the tunnel used in this investigation. Such a test will provide not only an indication of the magnitude of the effects of the tunnel-rotor diameter ratio (2:1 in this program) on the vibratory shear forces, but will also provide supplementary data at forward speeds below those evaluated herein.

2) A new rotor head having strengthened instrumented sections and fitted with the existing fiber glass blades should be tested to provide more data at forward speeds in the vicinity of 300 knots. Theoretical analyses should be made in conjunction with this experimental work so that specific questions can be answered, such as those arising in connection with the dominance of the edgewise rotor blade bending over the vibratory shear forces.

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TABLE I FLAPPING AND LAGGING MOTIONS AS FOURIER COEFFICIENTS, DEG.

LOVANCE RATIO = 0.181		ALPHA S = 0 CL/RIG = -0.000 THETA = -1 CO/SIC = 0.0001 ALPHA C = -0.1		ALPHA S = 0 CL/RIG = 0.018 THETA = 2 CO/SIC = 0.0002 ALPHA C = -1.0		ALPHA S = 0 CL/SIC = 0.004 THETA = 4 CO/SIC = 0.0008 ALPHA C = -2.0	
AD	-0.142	AD	1.923	AD	3.426	AD	3.426
A1	0.174	A1	-0.071	A1	-0.124	A1	-0.002
A2	0.298	A2	-0.186	A2	-0.007	A2	0.004
A3	0.442	A3	-0.024	A3	0.107	A3	-0.131
A4	0.443	A4	0.031	A4	0.038	A4	0.004
A5	-0.011	A5	-0.009	A5	0.011	A5	0.002
A6	0.004	A6	-0.009	A6	-0.012	A6	0.002
A7	0.002	A7	-0.003	A7	-0.012	A7	0.002
A8	0.005	A8	0.005	A8	0.012	A8	0.002
A9	0.004	A9	0.005	A9	0.005	A9	0.002
A10	0.004	A10	0.004	A10	0.004	A10	0.002
ALPHA S = 0 CL/RIG = 0.085 THETA = 6 CO/RIG = 0.0025 ALPHA C = -3.1							
AD	4.178	AD	-2.349	AD	-0.000	AD	-0.000
A1	0.037	A1	0.035	A1	-0.008	A1	-0.008
A2	-0.184	A2	-0.103	A2	0.016	A2	0.016
A3	0.071	A3	0.074	A3	-0.008	A3	-0.008
A4	0.038	A4	-0.027	A4	0.008	A4	0.008
A5	0.031	A5	-0.016	A5	0.004	A5	0.004
A6	0.038	A6	-0.028	A6	0.002	A6	0.002
A7	0.021	A7	-0.009	A7	0.004	A7	0.004
A8	0.007	A8	-0.008	A8	0.001	A8	0.001
A9	0.007	A9	-0.026	A9	0.001	A9	0.001
A10	0.007	A10	-0.026	A10	0.001	A10	0.001
ALPHA S = -4 CL/RIG = 0.044 THETA = 4 CO/SIC = 0.0010 ALPHA C = -5.9							
AD	-0.000	AD	-0.000	AD	-0.000	AD	-0.000
A1	0.100	A1	0.100	A1	0.100	A1	0.100
A2	-0.000	A2	-0.000	A2	-0.000	A2	-0.000
A3	0.000	A3	0.000	A3	0.000	A3	0.000
A4	-0.000	A4	-0.000	A4	-0.000	A4	-0.000
A5	0.000	A5	0.000	A5	0.000	A5	0.000
A6	-0.000	A6	-0.000	A6	-0.000	A6	-0.000
A7	0.000	A7	0.000	A7	0.000	A7	0.000
A8	-0.000	A8	-0.000	A8	-0.000	A8	-0.000
A9	0.000	A9	0.000	A9	0.000	A9	0.000
A10	-0.000	A10	-0.000	A10	-0.000	A10	-0.000
ALPHA S = -4 CL/RIG = 0.071 THETA = 6 CO/SIC = 0.0024 ALPHA C = -6.0							
AD	-0.000	AD	-0.000	AD	-0.000	AD	-0.000
A1	0.100	A1	0.100	A1	0.100	A1	0.100
A2	-0.000	A2	-0.000	A2	-0.000	A2	-0.000
A3	0.000	A3	0.000	A3	0.000	A3	0.000
A4	-0.000	A4	-0.000	A4	-0.000	A4	-0.000
A5	0.000	A5	0.000	A5	0.000	A5	0.000
A6	-0.000	A6	-0.000	A6	-0.000	A6	-0.000
A7	0.000	A7	0.000	A7	0.000	A7	0.000
A8	-0.000	A8	-0.000	A8	-0.000	A8	-0.000
A9	0.000	A9	0.000	A9	0.000	A9	0.000
A10	-0.000	A10	-0.000	A10	-0.000	A10	-0.000
ALPHA S = -4 CL/RIG = 0.002 THETA = 2 CO/SIC = 0.0003 ALPHA C = -8.8							
AD	-0.000	AD	-0.000	AD	-0.000	AD	-0.000
A1	0.100	A1	0.100	A1	0.100	A1	0.100
A2	-0.000	A2	-0.000	A2	-0.000	A2	-0.000
A3	0.000	A3	0.000	A3	0.000	A3	0.000
A4	-0.000	A4	-0.000	A4	-0.000	A4	-0.000
A5	0.000	A5	0.000	A5	0.000	A5	0.000
A6	-0.000	A6	-0.000	A6	-0.000	A6	-0.000
A7	0.000	A7	0.000	A7	0.000	A7	0.000
A8	-0.000	A8	-0.000	A8	-0.000	A8	-0.000
A9	0.000	A9	0.000	A9	0.000	A9	0.000
A10	-0.000	A10	-0.000	A10	-0.000	A10	-0.000
ALPHA S = -4 CL/SIC = 0.007 THETA = 8 CO/SIC = 0.0047 ALPHA C = -8.2							
AD	-0.000	AD	-0.000	AD	-0.000	AD	-0.000
A1	0.100	A1	0.100	A1	0.100	A1	0.100
A2	-0.000	A2	-0.000	A2	-0.000	A2	-0.000
A3	0.000	A3	0.000	A3	0.000	A3	0.000
A4	-0.000	A4	-0.000	A4	-0.000	A4	-0.000
A5	0.000	A5	0.000	A5	0.000	A5	0.000
A6	-0.000	A6	-0.000	A6	-0.000	A6	-0.000
A7	0.000	A7	0.000	A7	0.000	A7	0.000
A8	-0.000	A8	-0.000	A8	-0.000	A8	-0.000
A9	0.000	A9	0.000	A9	0.000	A9	0.000
A10	-0.000	A10	-0.000	A10	-0.000	A10	-0.000

NOTE: COEFFICIENTS ARE ALL LISTED AS -0 WHEN NO BLADE MOTION DATA WAS OBTAINED DUE TO INSTRUMENTATION DIFFICULTIES.

TABLE I CONTINUED.

<p>ADVANCE RATIO = 0.181</p> <p>ALPHA 5 = -4 CL/310 = 0.007 THETA = 10 CO/310 = 0.0081 ALPHA C = -9.1</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>	<p>ALPHA 5 = -8 CL/310 = 0.004 THETA = 2 CO/310 = 0.0001 ALPHA C = -8.7</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>	<p>ALPHA 5 = -8 CL/310 = 0.032 THETA = 4 CO/310 = 0.0010 ALPHA C = -9.4</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>
<p>ALPHA 5 = -8 CL/310 = 0.017 THETA = 4 CO/310 = 0.0024 ALPHA C = -18.9</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>	<p>ALPHA 5 = -8 CL/310 = 0.078 THETA = 8 CO/310 = 0.0044 ALPHA C = -11.4</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>	<p>ALPHA 5 = -8 CL/310 = 0.089 THETA = 10 CO/310 = 0.0074 ALPHA C = -13.5</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>
<p>ALPHA 5 = -8 CL/310 = 0.092 THETA = 11 CO/310 = 0.0089 ALPHA C = -13.7</p> <p>LAGGING</p> <p>AB -0.01 A1 -0.01 A2 -0.01 A3 -0.01 A4 -0.01 A5 -0.01 A6 -0.01 A7 -0.01 A8 -0.01 A9 -0.01 A10 -0.01</p> <p>FLIPPING</p> <p>B1 -0.01 B2 -0.01 B3 -0.01 B4 -0.01 B5 -0.01 B6 -0.01 B7 -0.01 B8 -0.01 B9 -0.01 B10 -0.01</p> <p>LAGGING</p> <p>C1 -0.01 C2 -0.01 C3 -0.01 C4 -0.01 C5 -0.01 C6 -0.01 C7 -0.01 C8 -0.01 C9 -0.01 C10 -0.01</p>	<p>OUT-OF-TRIM</p> <p>ALPHA 5 = 0 CL/310 = 0.007 THETA = 0 CO/310 = 0.0000 ALPHA C = -4.9</p> <p>LAGGING</p> <p>AB -0.281 A1 -0.278 A2 -0.275 A3 -0.272 A4 -0.269 A5 -0.266 A6 -0.263 A7 -0.260 A8 -0.257 A9 -0.254 A10 -0.251</p> <p>FLIPPING</p> <p>B1 0.329 B2 -0.228 B3 -0.038 B4 0.160 B5 0.362 B6 0.604 B7 0.846 B8 1.088 B9 1.330 B10 1.572</p> <p>LAGGING</p> <p>C1 0.043 C2 0.009 C3 -0.026 C4 -0.060 C5 -0.094 C6 -0.128 C7 -0.162 C8 -0.196 C9 -0.230 C10 -0.264</p>	<p>OUT-OF-TRIM</p> <p>ALPHA 5 = 0 CL/310 = 0.021 THETA = 2 CO/310 = 0.0005 ALPHA C = -3.0</p> <p>LAGGING</p> <p>AB 1.242 A1 1.148 A2 1.054 A3 0.960 A4 0.866 A5 0.772 A6 0.678 A7 0.584 A8 0.490 A9 0.396 A10 0.302</p> <p>FLIPPING</p> <p>B1 0.213 B2 -0.044 B3 -0.305 B4 -0.566 B5 -0.827 B6 -1.088 B7 -1.349 B8 -1.610 B9 -1.871 B10 -2.132</p> <p>LAGGING</p> <p>C1 0.009 C2 0.008 C3 -0.001 C4 -0.001 C5 -0.001 C6 -0.001 C7 -0.001 C8 -0.001 C9 -0.001 C10 -0.001</p>

TABLE I CONTINUED.

ADVANCE RATIO = 0.181		ZERO LAG DAMPING		OUT-OF-TRIM		ZERO LAG DAMPING	
OUT-OF-TRIM		ALPHA S = 0 CL/SIC = 0.047 THETA = 4 CO/SIC = 0.0012 ALPHA C = -0.2		ALPHA S = 0 CL/SIC = 0.071 THETA = 9 CO/SIC = 0.0025 ALPHA C = -7.2		ALPHA S = -4 CL/SIC = -0.004 THETA = 0 CO/SIC = 0.0001 ALPHA C = -4.0	
FLAPPING	LAGGING	FLAPPING	LAGGING	FLAPPING	LAGGING	FLAPPING	LAGGING
A0 2.022	A0 0.245	A0 4.084	A0 0.915	A0 0.008	A0 0.008	A0 0.008	A0 0.008
A1 0.182	A1 0.184	A1 4.207	A1 0.199	A1 0.213	A1 0.048	A1 0.213	A1 0.078
A2 0.122	A2 0.137	A2 0.295	A2 0.012	A2 0.060	A2 0.060	A2 0.060	A2 0.295
A3 0.180	A3 0.181	A3 0.181	A3 0.118	A3 0.039	A3 0.039	A3 0.039	A3 0.181
A4 0.150	A4 0.151	A4 0.012	A4 0.012	A4 0.012	A4 0.012	A4 0.012	A4 0.012
A5 0.021	A5 0.021	A5 0.021	A5 0.021	A5 0.021	A5 0.021	A5 0.021	A5 0.021
A6 0.014	A6 0.014	A6 0.014	A6 0.014	A6 0.014	A6 0.014	A6 0.014	A6 0.014
A7 0.011	A7 0.011	A7 0.011	A7 0.011	A7 0.011	A7 0.011	A7 0.011	A7 0.011
A8 0.001	A8 0.001	A8 0.001	A8 0.001	A8 0.001	A8 0.001	A8 0.001	A8 0.001
A9 0.001	A9 0.001	A9 0.001	A9 0.001	A9 0.001	A9 0.001	A9 0.001	A9 0.001
A10 0.001	A10 0.001	A10 0.001	A10 0.001	A10 0.001	A10 0.001	A10 0.001	A10 0.001
ZERO LAG DAMPING		ZERO LAG DAMPING		ZERO LAG DAMPING		ZERO LAG DAMPING	
ALPHA S = -4 CL/SIC = 0.025 THETA = 2 CO/SIC = 0.0006 ALPHA C = -5.0		ALPHA S = -4 CL/SIC = 0.048 THETA = 4 CO/SIC = 0.0012 ALPHA C = -9.1		ALPHA S = -4 CL/SIC = 0.048 THETA = 4 CO/SIC = 0.0012 ALPHA C = -9.1		ALPHA S = -4 CL/SIC = 0.015 THETA = 9 CO/SIC = 0.0024 ALPHA C = -9.7	
FLAPPING	LAGGING	FLAPPING	LAGGING	FLAPPING	LAGGING	FLAPPING	LAGGING
A0 1.777	A0 0.100	A0 5.597	A0 0.505	A0 5.597	A0 0.505	A0 5.037	A0 1.204
A1 0.181	A1 0.156	A1 0.212	A1 0.074	A1 0.212	A1 0.074	A1 0.189	A1 0.139
A2 0.140	A2 0.130	A2 0.285	A2 0.038	A2 0.285	A2 0.038	A2 0.452	A2 0.012
A3 0.125	A3 0.089	A3 0.194	A3 0.138	A3 0.194	A3 0.138	A3 0.245	A3 0.110
A4 0.040	A4 0.049	A4 0.054	A4 0.079	A4 0.054	A4 0.079	A4 0.107	A4 0.105
A5 0.012	A5 0.014	A5 0.051	A5 0.029	A5 0.051	A5 0.029	A5 0.077	A5 0.078
A6 0.022	A6 0.009	A6 0.015	A6 0.062	A6 0.015	A6 0.062	A6 0.049	A6 0.020
A7 0.011	A7 0.054	A7 0.024	A7 0.032	A7 0.024	A7 0.032	A7 0.064	A7 0.024
A8 0.014	A8 0.007	A8 0.025	A8 0.009	A8 0.025	A8 0.009	A8 0.021	A8 0.009
A9 0.011	A9 0.003	A9 0.017	A9 0.004	A9 0.017	A9 0.004	A9 0.009	A9 0.001
A10 0.017	A10 0.014	A10 0.008	A10 0.004	A10 0.008	A10 0.004	A10 0.001	A10 0.001
ZERO LAG DAMPING		ZERO LAG DAMPING		ZERO LAG DAMPING		ZERO LAG DAMPING	
ALPHA S = -4 CL/SIC = 0.009 THETA = 8 CO/SIC = 0.0048 ALPHA C = -8.0		ALPHA S = -4 CL/SIC = 0.009 THETA = 8 CO/SIC = 0.0048 ALPHA C = -8.0		ALPHA S = -4 CL/SIC = 0.009 THETA = 8 CO/SIC = 0.0048 ALPHA C = -8.0		ALPHA S = -4 CL/SIC = 0.009 THETA = 8 CO/SIC = 0.0048 ALPHA C = -8.0	
FLAPPING	LAGGING	FLAPPING	LAGGING	FLAPPING	LAGGING	FLAPPING	LAGGING
A0 0.140	A0 2.505	A0 0.140	A0 2.505	A0 0.140	A0 2.505	A0 0.140	A0 2.505
A1 0.044	A1 0.092	A1 0.044	A1 0.092	A1 0.044	A1 0.092	A1 0.044	A1 0.092
A2 0.042	A2 0.155	A2 0.042	A2 0.155	A2 0.042	A2 0.155	A2 0.042	A2 0.155
A3 0.295	A3 0.076	A3 0.295	A3 0.076	A3 0.295	A3 0.076	A3 0.295	A3 0.076
A4 0.181	A4 0.126	A4 0.181	A4 0.126	A4 0.181	A4 0.126	A4 0.181	A4 0.126
A5 0.092	A5 0.055	A5 0.092	A5 0.055	A5 0.092	A5 0.055	A5 0.092	A5 0.055
A6 0.017	A6 0.106	A6 0.017	A6 0.106	A6 0.017	A6 0.106	A6 0.017	A6 0.106
A7 0.015	A7 0.003	A7 0.015	A7 0.003	A7 0.015	A7 0.003	A7 0.015	A7 0.003
A8 0.014	A8 0.020	A8 0.014	A8 0.020	A8 0.014	A8 0.020	A8 0.014	A8 0.020
A9 0.013	A9 0.001	A9 0.013	A9 0.001	A9 0.013	A9 0.001	A9 0.013	A9 0.001
A10 0.013	A10 0.056	A10 0.013	A10 0.056	A10 0.013	A10 0.056	A10 0.013	A10 0.056

TABLE I CONTINUED.

ADVANCE RATIO • 0.283	ALPHA 5 = 0 CL/SIG = -0.023 THETA = 2 CG/SIG = 0.008 ALPHA C = 0.5	ALPHA 5 = 0 CL/SIG = -0.007 THETA = 0 CG/SIG = 0.007 ALPHA C = -0.5	ALPHA 5 = 0 CL/SIG = 0.015 THETA = 2 CG/SIG = 0.008 ALPHA C = -2.4					
<p>ALPHA 5 = 0 CL/SIG = 0.000 THETA = 0 CG/SIG = 0.003 ALPHA C = -3.5</p> <p>FLIPPING A0 -0.455 A1 -0.007 A2 -0.009 A3 -0.003 A4 -0.001 A5 -0.003 A6 -0.001 A7 -0.001 A8 -0.001 A9 -0.001 A10 -0.001 A11 -0.001 A12 -0.001 A13 -0.001 A14 -0.001 A15 -0.001 A16 -0.001 A17 -0.001 A18 -0.001 A19 -0.001 A20 -0.001</p> <p>LAGGING A0 2.334 A1 0.893 A2 0.009 A3 0.003 A4 0.001 A5 0.003 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10 0.001 A11 0.001 A12 0.001 A13 0.001 A14 0.001 A15 0.001 A16 0.001 A17 0.001 A18 0.001 A19 0.001 A20 0.001</p>	<p>ALPHA 5 = 0 CL/SIG = -0.007 THETA = 0 CG/SIG = 0.007 ALPHA C = -0.5</p> <p>FLIPPING A0 0.432 A1 -0.247 A2 -0.297 A3 0.003 A4 0.003 A5 -0.001 A6 -0.001 A7 -0.001 A8 -0.001 A9 -0.001 A10 -0.001 A11 -0.001 A12 -0.001 A13 -0.001 A14 -0.001 A15 -0.001 A16 -0.001 A17 -0.001 A18 -0.001 A19 -0.001 A20 -0.001</p> <p>LAGGING A0 2.517 A1 0.879 A2 -0.003 A3 -0.002 A4 -0.003 A5 -0.003 A6 -0.001 A7 -0.001 A8 -0.001 A9 -0.001 A10 -0.001 A11 -0.001 A12 -0.001 A13 -0.001 A14 -0.001 A15 -0.001 A16 -0.001 A17 -0.001 A18 -0.001 A19 -0.001 A20 -0.001</p>	<p>ALPHA 5 = 0 CL/SIG = 0.015 THETA = 2 CG/SIG = 0.008 ALPHA C = -2.4</p> <p>FLIPPING A0 1.038 A1 -0.224 A2 0.141 A3 -0.034 A4 -0.038 A5 0.009 A6 -0.240 A7 -0.001 A8 0.001 A9 0.001 A10 0.001 A11 0.001 A12 0.001 A13 0.001 A14 0.001 A15 0.001 A16 0.001 A17 0.001 A18 0.001 A19 0.001 A20 0.001</p> <p>LAGGING A0 2.925 A1 0.834 A2 0.001 A3 0.001 A4 0.001 A5 0.001 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10 0.001 A11 0.001 A12 0.001 A13 0.001 A14 0.001 A15 0.001 A16 0.001 A17 0.001 A18 0.001 A19 0.001 A20 0.001</p>	<p>ALPHA 5 = 0 CL/SIG = 0.000 THETA = 0 CG/SIG = 0.003 ALPHA C = -3.5</p> <p>FLIPPING A0 3.074 A1 0.134 A2 -0.003 A3 -0.014 A4 -0.212 A5 -0.177 A6 0.014 A7 0.045 A8 0.155 A9 0.111 A10 0.000 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p> <p>LAGGING A0 2.433 A1 0.043 A2 0.014 A3 -0.014 A4 -0.003 A5 0.014 A6 0.000 A7 0.000 A8 0.000 A9 0.000 A10 0.000 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p>	<p>ALPHA 5 = 0 CL/SIG = 0.009 THETA = 0 CG/SIG = 0.003 ALPHA C = -3.2</p> <p>FLIPPING A0 4.034 A1 -0.345 A2 -0.574 A3 -0.131 A4 0.041 A5 0.093 A6 0.153 A7 0.033 A8 0.014 A9 0.042 A10 -0.000 A11 -0.000 A12 -0.001 A13 -0.001 A14 -0.001 A15 -0.001 A16 -0.001 A17 -0.001 A18 -0.001 A19 -0.001 A20 -0.001</p> <p>LAGGING A0 3.290 A1 0.090 A2 -0.131 A3 0.033 A4 0.014 A5 0.042 A6 -0.000 A7 -0.000 A8 -0.001 A9 -0.001 A10 -0.001 A11 -0.001 A12 -0.001 A13 -0.001 A14 -0.001 A15 -0.001 A16 -0.001 A17 -0.001 A18 -0.001 A19 -0.001 A20 -0.001</p>	<p>ALPHA 5 = 0 CL/SIG = 0.045 THETA = 0 CG/SIG = 0.005 ALPHA C = -4.0</p> <p>FLIPPING A0 4.497 A1 -0.318 A2 -0.108 A3 -0.283 A4 0.157 A5 -0.197 A6 -0.185 A7 -0.000 A8 0.000 A9 0.000 A10 0.000 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p> <p>LAGGING A0 4.531 A1 -0.283 A2 -0.000 A3 0.000 A4 0.000 A5 0.000 A6 0.000 A7 0.000 A8 0.000 A9 0.000 A10 0.000 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p>	<p>ALPHA 5 = 0 CL/SIG = 0.074 THETA = 10 CG/SIG = 0.003 ALPHA C = -8.0</p> <p>FLIPPING A0 3.074 A1 -0.034 A2 -0.003 A3 0.181 A4 -0.174 A5 -0.608 A6 -0.033 A7 0.070 A8 0.151 A9 0.112 A10 0.015 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p> <p>LAGGING A0 4.033 A1 0.043 A2 -0.033 A3 0.033 A4 0.015 A5 0.042 A6 -0.000 A7 -0.000 A8 -0.000 A9 -0.000 A10 -0.000 A11 -0.000 A12 -0.000 A13 -0.000 A14 -0.000 A15 -0.000 A16 -0.000 A17 -0.000 A18 -0.000 A19 -0.000 A20 -0.000</p>	<p>ALPHA 5 = -5 CL/SIG = 0.010 THETA = 2 CG/SIG = 0.004 ALPHA C = -6.0</p> <p>FLIPPING A0 0.843 A1 -0.392 A2 -0.059 A3 0.043 A4 -0.047 A5 0.004 A6 -0.227 A7 -0.002 A8 0.001 A9 0.001 A10 0.001 A11 0.001 A12 0.001 A13 0.001 A14 0.001 A15 0.001 A16 0.001 A17 0.001 A18 0.001 A19 0.001 A20 0.001</p> <p>LAGGING A0 2.488 A1 0.843 A2 -0.002 A3 -0.002 A4 -0.001 A5 0.001 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10 0.001 A11 0.001 A12 0.001 A13 0.001 A14 0.001 A15 0.001 A16 0.001 A17 0.001 A18 0.001 A19 0.001 A20 0.001</p>	<p>ALPHA 5 = 0 CL/SIG = 0.000 THETA = 0 CG/SIG = 0.004 ALPHA C = -4.0</p> <p>FLIPPING A0 4.497 A1 -0.318 A2 -0.108 A3 -0.283 A4 0.157 A5 -0.197 A6 -0.185 A7 -0.000 A8 0.000 A9 0.000 A10 0.000 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p> <p>LAGGING A0 4.531 A1 -0.283 A2 -0.000 A3 0.000 A4 0.000 A5 0.000 A6 0.000 A7 0.000 A8 0.000 A9 0.000 A10 0.000 A11 0.000 A12 0.000 A13 0.000 A14 0.000 A15 0.000 A16 0.000 A17 0.000 A18 0.000 A19 0.000 A20 0.000</p>

TABLE I CONTINUED.

ADVANCE RATIO = 0.283		ALPHA S = -A CL/BIC = 0.041 THETA = 4 CQ/SIC = 0.0011 ALPHA C = -A.5		ALPHA S = -A CL/ZIO = 0.042 THETA = 4 CQ/SIC = 0.0022 ALPHA C = -7.9		ALPHA S = -A CL/SIC = 2.077 THETA = 0 CQ/SIC = 0.0062 ALPHA C = -10.0	
PLAPPING		LAGGING		PLAPPING		LAGGING	
A0	1.441	A0	2.787	A0	5.074	A0	5.769
A1	-0.358	A1	0.015	A1	-0.409	A1	0.044
A2	-0.135	A2	-0.001	A2	-0.122	A2	-0.210
A3	0.115	A3	0.005	A3	-0.190	A3	0.111
A4	0.282	A4	0.001	A4	0.009	A4	0.017
A5	-0.024	A5	-0.013	A5	-0.072	A5	0.012
A6	0.021	A6	0.001	A6	0.007	A6	0.004
A7	-0.027	A7	0.001	A7	-0.037	A7	-0.042
A8	0.007	A8	0.005	A8	0.051	A8	0.041
A9	0.007	A9	0.005	A9	0.007	A9	-0.024
A10	0.010	A10	0.002	A10	0.010	A10	0.002
A11	0.001	A11	0.001	A11	0.001	A11	0.001
A12	0.001	A12	0.001	A12	0.001	A12	0.001
A13	0.001	A13	0.001	A13	0.001	A13	0.001
A14	0.001	A14	0.001	A14	0.001	A14	0.001
A15	0.001	A15	0.001	A15	0.001	A15	0.001
A16	0.001	A16	0.001	A16	0.001	A16	0.001
A17	0.001	A17	0.001	A17	0.001	A17	0.001
A18	0.001	A18	0.001	A18	0.001	A18	0.001
A19	0.001	A19	0.001	A19	0.001	A19	0.001
A20	0.001	A20	0.001	A20	0.001	A20	0.001
A21	0.001	A21	0.001	A21	0.001	A21	0.001
A22	0.001	A22	0.001	A22	0.001	A22	0.001
A23	0.001	A23	0.001	A23	0.001	A23	0.001
A24	0.001	A24	0.001	A24	0.001	A24	0.001
A25	0.001	A25	0.001	A25	0.001	A25	0.001
A26	0.001	A26	0.001	A26	0.001	A26	0.001
A27	0.001	A27	0.001	A27	0.001	A27	0.001
A28	0.001	A28	0.001	A28	0.001	A28	0.001
A29	0.001	A29	0.001	A29	0.001	A29	0.001
A30	0.001	A30	0.001	A30	0.001	A30	0.001
A31	0.001	A31	0.001	A31	0.001	A31	0.001
A32	0.001	A32	0.001	A32	0.001	A32	0.001
A33	0.001	A33	0.001	A33	0.001	A33	0.001
A34	0.001	A34	0.001	A34	0.001	A34	0.001
A35	0.001	A35	0.001	A35	0.001	A35	0.001
A36	0.001	A36	0.001	A36	0.001	A36	0.001
A37	0.001	A37	0.001	A37	0.001	A37	0.001
A38	0.001	A38	0.001	A38	0.001	A38	0.001
A39	0.001	A39	0.001	A39	0.001	A39	0.001
A40	0.001	A40	0.001	A40	0.001	A40	0.001
A41	0.001	A41	0.001	A41	0.001	A41	0.001
A42	0.001	A42	0.001	A42	0.001	A42	0.001
A43	0.001	A43	0.001	A43	0.001	A43	0.001
A44	0.001	A44	0.001	A44	0.001	A44	0.001
A45	0.001	A45	0.001	A45	0.001	A45	0.001
A46	0.001	A46	0.001	A46	0.001	A46	0.001
A47	0.001	A47	0.001	A47	0.001	A47	0.001
A48	0.001	A48	0.001	A48	0.001	A48	0.001
A49	0.001	A49	0.001	A49	0.001	A49	0.001
A50	0.001	A50	0.001	A50	0.001	A50	0.001
A51	0.001	A51	0.001	A51	0.001	A51	0.001
A52	0.001	A52	0.001	A52	0.001	A52	0.001
A53	0.001	A53	0.001	A53	0.001	A53	0.001
A54	0.001	A54	0.001	A54	0.001	A54	0.001
A55	0.001	A55	0.001	A55	0.001	A55	0.001
A56	0.001	A56	0.001	A56	0.001	A56	0.001
A57	0.001	A57	0.001	A57	0.001	A57	0.001
A58	0.001	A58	0.001	A58	0.001	A58	0.001
A59	0.001	A59	0.001	A59	0.001	A59	0.001
A60	0.001	A60	0.001	A60	0.001	A60	0.001
A61	0.001	A61	0.001	A61	0.001	A61	0.001
A62	0.001	A62	0.001	A62	0.001	A62	0.001
A63	0.001	A63	0.001	A63	0.001	A63	0.001
A64	0.001	A64	0.001	A64	0.001	A64	0.001
A65	0.001	A65	0.001	A65	0.001	A65	0.001
A66	0.001	A66	0.001	A66	0.001	A66	0.001
A67	0.001	A67	0.001	A67	0.001	A67	0.001
A68	0.001	A68	0.001	A68	0.001	A68	0.001
A69	0.001	A69	0.001	A69	0.001	A69	0.001
A70	0.001	A70	0.001	A70	0.001	A70	0.001
A71	0.001	A71	0.001	A71	0.001	A71	0.001
A72	0.001	A72	0.001	A72	0.001	A72	0.001
A73	0.001	A73	0.001	A73	0.001	A73	0.001
A74	0.001	A74	0.001	A74	0.001	A74	0.001
A75	0.001	A75	0.001	A75	0.001	A75	0.001
A76	0.001	A76	0.001	A76	0.001	A76	0.001
A77	0.001	A77	0.001	A77	0.001	A77	0.001
A78	0.001	A78	0.001	A78	0.001	A78	0.001
A79	0.001	A79	0.001	A79	0.001	A79	0.001
A80	0.001	A80	0.001	A80	0.001	A80	0.001
A81	0.001	A81	0.001	A81	0.001	A81	0.001
A82	0.001	A82	0.001	A82	0.001	A82	0.001
A83	0.001	A83	0.001	A83	0.001	A83	0.001
A84	0.001	A84	0.001	A84	0.001	A84	0.001
A85	0.001	A85	0.001	A85	0.001	A85	0.001
A86	0.001	A86	0.001	A86	0.001	A86	0.001
A87	0.001	A87	0.001	A87	0.001	A87	0.001
A88	0.001	A88	0.001	A88	0.001	A88	0.001
A89	0.001	A89	0.001	A89	0.001	A89	0.001
A90	0.001	A90	0.001	A90	0.001	A90	0.001
A91	0.001	A91	0.001	A91	0.001	A91	0.001
A92	0.001	A92	0.001	A92	0.001	A92	0.001
A93	0.001	A93	0.001	A93	0.001	A93	0.001
A94	0.001	A94	0.001	A94	0.001	A94	0.001
A95	0.001	A95	0.001	A95	0.001	A95	0.001
A96	0.001	A96	0.001	A96	0.001	A96	0.001
A97	0.001	A97	0.001	A97	0.001	A97	0.001
A98	0.001	A98	0.001	A98	0.001	A98	0.001
A99	0.001	A99	0.001	A99	0.001	A99	0.001
A100	0.001	A100	0.001	A100	0.001	A100	0.001

TABLE I CONTINUED.

ADVANCE RATIO = 0.283		ALPHA S = -8 CL/SIG = 0.039 THETA = 6 CO/SIG = 0.0021 ALPHA C = -11.5		ALPHA S = -8 CL/SIG = 0.059 THETA = 8 CO/SIG = 0.0038 ALPHA C = -13.5			
FLAPPING		LAGGING		FLAPPING		LAGGING	
A0	2.238	A0	1.272	A0	3.365	A0	2.225
A1	-0.010	B1	0.399	A1	0.003	B1	-0.186
A2	-0.295	B2	-0.164	A2	-0.002	B2	0.244
A3	0.127	B3	0.199	A3	0.008	B3	-0.473
A4	0.087	B4	0.022	A4	0.002	B4	0.174
A5	0.022	B5	-0.001	A5	0.001	B5	0.083
A6	0.017	B6	0.008	A6	-0.001	B6	0.010
A7	-0.019	B7	0.031	A7	-0.002	B7	0.017
A8	-0.001	B8	0.003	A8	-0.001	B8	-0.002
A9	0.006	B9	0.006	A9	0.001	B9	0.002
A10	-0.002	B10	0.020	A10	0.001	B10	0.025
ALPHA S = -8 CL/SIG = 0.069 THETA = 10 CO/SIG = 0.0061 ALPHA C = -14.8		ALPHA S = -8 CL/SIG = 0.078 THETA = 11 CO/SIG = 0.0079 ALPHA C = -15.7					
FLAPPING		LAGGING		FLAPPING		LAGGING	
AC	4.269	AC	3.523	A0	4.634	A0	4.314
A1	0.309	B1	0.125	A1	0.710	B1	0.183
A2	-0.652	B2	-0.352	A2	-0.762	B2	-0.505
A3	0.223	B3	0.216	A3	0.280	B3	-0.195
A4	0.060	B4	0.105	A4	0.078	B4	0.119
A5	0.025	B5	0.032	A5	0.048	B5	0.062
A6	-0.005	B6	0.040	A6	-0.012	B6	0.061
A7	-0.029	B7	0.037	A7	-0.022	B7	0.005
A8	0.002	B8	0.007	A8	0.001	B8	-0.009
A9	0.007	B9	0.014	A9	0.007	B9	-0.001
A10	-0.021	B10	0.028	A10	-0.007	B10	0.006

TABLE I CONTINUED.

ADVANCE RATIO = 0.389		
<p>ALPHA 3 * A CL/BIG = -0.004 ALPHA C = 4.0 CC/SIG = 0.0003 ALPHA C = 4.0</p>		
<p>FLAPPING AO 0.128 A1 0.097 A2 0.427 A3 0.031 A4 -0.243 A5 -0.025 A6 -0.026 A7 -0.046 A8 -0.016 A9 0.001 A10-0.041</p>	<p>LAGGING AO 2.333 A1 0.048 A2 -0.011 A3 0.005 A4 0.072 A5 0.015 A6 0.015 A7 0.022 A8 0.008 A9 -0.002 A10-0.031</p>	<p>ALPHA 3 * A CL/SIG = 0.039 ALPHA C = 1.2 CC/SIG = -0.0006 ALPHA C = 1.2</p> <p>FLAPPING AO 2.131 A1 0.064 A2 -0.030 A3 0.051 A4 -0.018 A5 -0.023 A6 0.006 A7 0.006 A8 0.003 A9 0.008 A10-0.020</p> <p>LAGGING AO 2.089 A1 0.024 A2 -0.011 A3 0.016 A4 0.003 A5 0.001 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10-0.003</p>
<p>ALPHA 3 * A CL/BIG = 0.017 ALPHA C = 3.0 CC/SIG = -0.0004 ALPHA C = 3.0</p>		
<p>FLAPPING AO 1.166 A1 -0.088 A2 0.244 A3 0.030 A4 -0.128 A5 -0.017 A6 -0.002 A7 -0.002 A8 -0.004 A9 0.005 A10-0.043</p>	<p>LAGGING AO 2.187 A1 0.080 A2 -0.012 A3 0.004 A4 0.001 A5 0.001 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10-0.022</p>	<p>ALPHA 3 * A CL/SIG = 0.040 ALPHA C = 2 CC/SIG = 0.0002 ALPHA C = -1.7</p> <p>FLAPPING AO 3.363 A1 -0.023 A2 -0.429 A3 0.051 A4 0.012 A5 0.013 A6 0.012 A7 -0.012 A8 0.004 A9 0.021 A10-0.024</p> <p>LAGGING AO 2.315 A1 -0.075 A2 0.039 A3 0.016 A4 0.002 A5 0.002 A6 0.003 A7 0.003 A8 0.004 A9 0.001 A10-0.016</p>
<p>ALPHA 3 * A CL/SIG = 0.010 ALPHA C = 1.0 CC/SIG = 0.0001 ALPHA C = -1.0</p>		
<p>FLAPPING AO 3.176 A1 -0.281 A2 -0.291 A3 0.118 A4 -0.005 A5 0.026 A6 0.024 A7 -0.013 A8 0.005 A9 0.016 A10-0.021</p>	<p>LAGGING AO 2.370 A1 -0.025 A2 -0.005 A3 0.029 A4 0.002 A5 0.002 A6 0.003 A7 0.003 A8 0.002 A9 0.002 A10-0.021</p>	<p>ALPHA 3 * A CL/SIG = 0.040 ALPHA C = 2 CC/SIG = 0.0002 ALPHA C = -1.7</p> <p>FLAPPING AO 0.390 A1 -0.043 A2 0.190 A3 0.078 A4 -0.108 A5 -0.018 A6 0.004 A7 0.004 A8 0.008 A9 0.008 A10-0.029</p> <p>LAGGING AO 2.527 A1 0.084 A2 -0.007 A3 0.003 A4 0.003 A5 0.002 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10-0.001</p>
<p>ALPHA 5 * A CL/SIG = 0.004 ALPHA C = 1.0 CC/SIG = 0.0001 ALPHA C = -1.0</p>		
<p>FLAPPING AO 0.824 A1 0.115 A2 0.082 A3 0.098 A4 -0.013 A5 -0.021 A6 -0.021 A7 0.005 A8 0.004 A9 0.002 A10-0.025</p>	<p>LAGGING AO 2.310 A1 0.071 A2 -0.005 A3 0.004 A4 0.002 A5 0.001 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10-0.001</p>	<p>ALPHA 5 * A CL/SIG = 0.047 ALPHA C = 4 CC/SIG = 0.0010 ALPHA C = -3.1</p> <p>FLAPPING AO 2.034 A1 -0.045 A2 0.304 A3 0.100 A4 0.104 A5 0.065 A6 0.035 A7 0.003 A8 0.004 A9 0.008 A10-0.048</p> <p>LAGGING AO 2.021 A1 0.040 A2 -0.004 A3 0.024 A4 0.003 A5 0.003 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10-0.002</p>

TABLE I CONTINUED.

ADVANCE RATIO = 0.100		
<p>ALPHA 5 = 0 CL/SIC = 0.065 THETA = 6 C0/SIC = 0.0026 ALPHA C = -7.1</p> <p>FLAPPING</p> <p>AC 3-92Z A0 5-755 A1 -0.017 01 0.294 A1 -0.115 01 0.031 A2 -0.567 02 0.515 A2 0.006 02 0.023 A3 -0.192 03 -0.452 A3 0.035 03 -0.016 A4 0.184 04 0.113 A4 0.004 04 0.018 A5 0.042 05 0.036 A5 0.001 05 0.004 A6 0.021 06 0.070 A6 -0.001 06 0.001 A7 0.022 07 0.042 A7 0.005 07 -0.001 A8 -0.022 08 0.042 A8 -0.001 08 0.001 A9 -0.031 09 0.042 A9 -0.001 09 -0.002 A10-0.02C 010 0.021 A10 0.001 010-0.001</p>	<p>ALPHA 5 = 0.7 CL/SIC = 0.0000 ALPHA C = -6.0</p> <p>FLAPPING</p> <p>AO 0.61C 60 2-716 A1 -0.008 01 -0.077 A1 0.085 01 -0.050 A2 -0.001 02 -0.450 A2 0.015 02 -0.015 A3 0.004 03 -0.508 A3 0.004 03 -0.002 A4 0.093 04 -0.028 A4 0.004 04 0.001 A5 -0.006 05 3.000 A5 0.001 05 -0.005 A6 -0.023 06 2.001 A6 0.002 06 0.001 A7 0.001 07 0.011 A7 0.001 07 0.001 A8 -0.001 08 0.011 A8 0.001 08 0.001 A9 0.007 09 0.009 A9 -0.001 09 -0.001 A10-0.02Z 010 0.010 A10 0.001 010-0.001</p>	<p>ALPHA 5 = -4 CL/SIC = 0.0222 ALPHA C = -9.2</p> <p>FLAPPING</p> <p>AO 2-754 A0 3-575 A1 -0.276 01 -0.147 A1 -0.056 01 0.001 A2 -0.442 02 -0.389 A2 0.001 02 0.009 A3 -0.181 03 -0.385 A3 0.026 03 -0.008 A4 0.124 04 0.048 A4 0.008 04 0.004 A5 0.027 05 0.026 A5 -0.001 05 0.001 A6 -0.001 06 0.014 A6 -0.002 06 0.001 A7 0.031 07 0.004 A7 0.002 07 0.002 A8 -0.042 08 0.012 A8 0.001 08 -0.001 A9 -0.042 09 0.012 A9 0.001 09 -0.001 A10-0.01Z 010-0.015 A10-0.001 010-0.001</p>
<p>ALPHA 5 = -4 CL/SIC = 0.025 THETA = 4 C0/SIC = 0.0010 ALPHA C = -7.9</p> <p>FLAPPING</p> <p>AO 1-607 60 2-913 A1 -0.189 01 0.075 A1 0.028 01 -0.042 A2 -0.173 02 -0.158 A2 0.006 02 -0.002 A3 0.115 03 -0.220 A3 0.008 03 0.001 A4 0.128 04 -0.014 A4 0.002 04 -0.003 A5 -0.021 05 0.044 A5 0.001 05 -0.001 A6 0.018 06 -0.044 A6 0.001 06 -0.001 A7 0.018 07 0.019 A7 -0.001 07 0.001 A8 -0.001 08 0.012 A8 -0.002 08 -0.002 A9 -0.004 09 0.012 A9 -0.001 09 0.001 A10-0.02Z 010 0.008 A10-0.001 010 0.001</p>	<p>ALPHA 5 = -4 CL/SIC = 0.060 THETA = 8 C0/SIC = 0.0041 ALPHA C = -11.5</p> <p>FLAPPING</p> <p>AO 5-540 A0 4-562 A1 -0.081 01 -0.019 A1 -0.144 01 0.057 A2 -0.675 02 -0.501 A2 0.007 02 0.020 A3 0.248 03 0.502 A3 0.099 03 -0.019 A4 0.106 04 0.107 A4 0.002 04 0.005 A5 0.052 05 0.020 A5 0.001 05 0.005 A6 0.006 06 0.045 A6 -0.001 06 0.001 A7 1.067 07 0.007 A7 0.002 07 0.002 A8 -0.022 08 0.027 A8 0.001 08 0.002 A9 -0.022 09 0.027 A9 0.001 09 -0.001 A10 0.011 010 0.018 A10 0.001 010-0.001</p>	<p>ALPHA 5 = -8 CL/SIC = -0.007 THETA = 4 C0/SIC = 0.0003 ALPHA C = -10.6</p> <p>FLAPPING</p> <p>AO -0.019 40 2-755 A1 -0.082 01 -0.128 A1 0.043 01 -0.034 A2 -0.124 02 -0.140 A2 -0.005 02 -0.017 A3 0.100 03 -0.156 A3 -0.002 03 -0.007 A4 0.073 04 -0.315 A4 0.010 04 -0.001 A5 0.018 05 0.001 A5 0.004 05 0.001 A6 -0.014 06 0.021 A6 0.001 06 0.001 A7 0.014 07 0.021 A7 0.001 07 0.001 A8 0.001 08 0.004 A8 0.001 08 0.001 A9 0.005 09 0.004 A9 0.001 09 0.001 A10-0.014 010 0.014 A10-0.001 010-0.001</p>

TABLE I CONTINUED.

ADVANCE RATIO = 0.389		ALPHA S = -8 CL/SIG = 0.018 TME7A = 6 CO/SIG = 0.0015 ALPHA C = -12.6		ALPHA S = -8 CL/SIG = 0.027 TME7A = 7 CO/SIG = 0.0022 ALPHA C = -13.5			
FLAPPING		LAGGING		FLAPPING		LAGGING	
A0	0.183	A0	3.267	A0	1.454	A0	3.675
A1	0.127	A1	0.025	A1	0.027	A1	0.056
A2	-0.294	A2	-0.311	A2	0.005	A2	-0.31A
A3	0.111	A3	0.007	A3	-0.010	A3	0.125
A4	0.093	A4	-0.006	A4	0.004	A4	0.100
A5	0.044	A5	0.006	A5	-0.001	A5	0.047
A6	0.001	A6	0.006	A6	-0.001	A6	0.100
A7	0.025	A7	0.008	A7	0.001	A7	0.020
A8	0.004	A8	0.007	A8	-0.001	A8	0.006
A9	0.005	A9	0.009	A9	0.001	A9	-0.001
A10	-0.008	A10	0.008	A10	0.001	A10	-0.011

ADVANCE RATIO = 0.389		ALPHA S = -8 CL/SIG = 0.038 TME7A = 8 CO/SIG = 0.0032 ALPHA C = -14.6		ALPHA S = -8 CL/SIG = 0.042 TME7A = 9 CO/SIG = 0.0042 ALPHA C = -15.1			
FLAPPING		LAGGING		FLAPPING		LAGGING	
A0	2.073	A0	4.209	A0	2.304	A0	4.707
A1	-0.037	A1	-0.145	A1	-0.009	A1	-0.223
A2	-0.535	A2	-0.32J	A2	-0.437	A2	-0.363
A3	0.170	A3	-0.378	A3	0.021	A3	0.203
A4	0.095	A4	0.013	A4	0.009	A4	0.104
A5	0.061	A5	0.006	A5	0.001	A5	0.077
A6	0.003	A6	0.014	A6	-0.001	A6	0.007
A7	0.029	A7	-0.002	A7	-0.001	A7	0.030
A8	0.008	A8	0.013	A8	-0.001	A8	0.005
A9	-0.001	A9	0.010	A9	-0.001	A9	-0.003
A10	0.001	A10	-0.001	A10	0.001	A10	0.007

TABLE I CONTINUED.

ADVANCE RATIC = 0.488		
<p>ALPHA 5 = 0 CL/31C = 0.003 THETA = -2 CO/31C = 0.0001 ALPHA C = 0.0</p> <p>FLAPPING</p> <p>A0 2-015 A1 0.132 A2 0.110 A3 0.085 A4 0.060 A5 0.040 A6 0.025 A7 0.015 A8 0.005 A9 0.001 A10-0.001</p> <p>LAGGING</p> <p>A0 2-015 A1 0.132 A2 0.110 A3 0.085 A4 0.060 A5 0.040 A6 0.025 A7 0.015 A8 0.005 A9 0.001 A10-0.001</p>	<p>ALPHA 5 = 0 CL/31C = 0.015 THETA = 0 CO/31C = 0.0000 ALPHA C = -1.0</p> <p>FLAPPING</p> <p>A0 0.783 A1 -0.048 A2 -0.020 A3 -0.008 A4 0.014 A5 0.034 A6 0.053 A7 0.070 A8 0.085 A9 0.093 A10-0.093</p> <p>LAGGING</p> <p>A0 2-544 A1 0.110 A2 -0.007 A3 0.049 A4 0.082 A5 0.119 A6 0.152 A7 0.182 A8 0.210 A9 0.235 A10-0.254</p>	<p>ALPHA 5 = 0 CL/31C = 0.033 THETA = 2 CO/31C = 0.0001 ALPHA C = -3.5</p> <p>FLAPPING</p> <p>A0 1-726 A1 -0.466 A2 -0.115 A3 0.012 A4 0.000 A5 0.024 A6 0.040 A7 0.057 A8 0.072 A9 0.084 A10-0.084</p> <p>LAGGING</p> <p>A0 2-337 A1 0.087 A2 0.020 A3 0.011 A4 0.003 A5 0.004 A6 0.004 A7 0.002 A8 0.001 A9 0.001 A10-0.001</p>
<p>ALPHA 5 = 0 CL/31C = 0.044 THETA = 0 CO/31C = 0.0006 ALPHA C = -3.0</p> <p>FLAPPING</p> <p>A0 2-273 A1 0.180 A2 0.095 A3 0.048 A4 0.024 A5 0.012 A6 0.006 A7 0.003 A8 0.002 A9 0.001 A10-0.001</p> <p>LAGGING</p> <p>A0 2-273 A1 0.180 A2 0.095 A3 0.048 A4 0.024 A5 0.012 A6 0.006 A7 0.003 A8 0.002 A9 0.001 A10-0.001</p>	<p>ALPHA 3 = 0 CL/31C = 0.026 THETA = 6 CO/31C = 0.0022 ALPHA C = -7.5</p> <p>FLAPPING</p> <p>A0 5.078 A1 -0.070 A2 -0.015 A3 0.024 A4 0.044 A5 0.064 A6 0.080 A7 0.093 A8 0.100 A9 0.106 A10-0.106</p> <p>LAGGING</p> <p>A0 5-114 A1 -0.064 A2 0.017 A3 0.035 A4 0.048 A5 0.048 A6 0.018 A7 0.007 A8 0.001 A9 0.001 A10-0.001</p>	<p>ALPHA 5 = 0 CL/31C = 0.070 THETA = 8 CO/31C = 0.0042 ALPHA C = -9.0</p> <p>FLAPPING</p> <p>A0 3-873 A1 -0.340 A2 -0.095 A3 0.018 A4 0.007 A5 0.004 A6 0.002 A7 0.001 A8 0.001 A9 0.001 A10-0.001</p> <p>LAGGING</p> <p>A0 4-283 A1 0.034 A2 0.028 A3 0.021 A4 0.011 A5 0.004 A6 0.002 A7 0.001 A8 0.001 A9 0.001 A10-0.001</p>
<p>ALPHA 5 = 6 CL/31C = 0.008 THETA = 10 CO/31C = 0.0046 ALPHA C = -11.7</p> <p>FLAPPING</p> <p>A0 4-264 A1 -0.094 A2 -0.026 A3 0.031 A4 0.059 A5 0.076 A6 0.085 A7 0.091 A8 0.094 A9 0.097 A10-0.097</p> <p>LAGGING</p> <p>A0 5-001 A1 0.094 A2 0.031 A3 0.059 A4 0.076 A5 0.085 A6 0.091 A7 0.094 A8 0.097 A9 0.097 A10-0.097</p>	<p>ALPHA 5 = 0 CL/31C = 0.085 THETA = 11 CO/31C = 0.0077 ALPHA C = -12.8</p> <p>FLAPPING</p> <p>A0 4-553 A1 -0.460 A2 -0.094 A3 0.024 A4 0.014 A5 0.008 A6 0.004 A7 0.002 A8 0.001 A9 0.001 A10-0.001</p> <p>LAGGING</p> <p>A0 9-874 A1 0.026 A2 0.025 A3 0.015 A4 0.012 A5 0.008 A6 0.004 A7 0.002 A8 0.001 A9 0.001 A10-0.001</p>	<p>ALPHA 3 = -4 CL/31C = -0.008 THETA = 0 CO/31C = 0.0001 ALPHA C = -4.0</p> <p>FLAPPING</p> <p>A0 -0.616 A1 -0.460 A2 -0.380 A3 0.084 A4 0.024 A5 0.012 A6 0.004 A7 0.001 A8 0.001 A9 0.001 A10-0.001</p> <p>LAGGING</p> <p>A0 2-543 A1 0.135 A2 -0.002 A3 0.004 A4 0.004 A5 0.002 A6 0.001 A7 0.001 A8 0.001 A9 0.001 A10-0.001</p>

TABLE I CONTINUED.

GOVANCE RATIO = 0.488		
<p>ALPHA S = -4 CL/SIG = 0.003 THETA = 2 CO/SIG = 0.0004 ALPHA C = -3.9</p> <p>FLAPPING</p> <p>A0 0.214 A1 0.131 A2 2.373 A3 0.109 A4 -0.081 A5 -0.039 A6 -0.001 A7 -0.019 A8 0.072 A9 -0.097 A0 0.001 A1 -0.013 A2 0.014 A3 -0.013 A4 0.014 A5 0.002 A6 0.014 A7 0.021 A8 0.001 A9 0.004 A0 -0.014 A1 0.021 A2 0.001 A3 0.004 A4 0.002 A5 0.008 A6 0.002 A7 0.001 A8 0.002 A9 0.004 A0 0.001 A1 0.001 A2 0.001 A3 0.001 A4 0.001 A5 0.001 A6 0.001 A7 0.001 A8 0.001 A9 0.001</p>	<p>ALPHA S = -4 CL/SIG = 0.020 THETA = 4 CO/SIG = 0.0003 ALPHA C = -7.9</p> <p>FLAPPING</p> <p>A0 0.898 A1 -0.010 A2 2.730 A3 0.079 A4 -0.172 A5 -0.049 A6 0.009 A7 -0.079 A8 0.049 A9 -0.247 A0 0.003 A1 -0.023 A2 0.049 A3 -0.049 A4 0.018 A5 0.003 A6 0.049 A7 0.012 A8 0.002 A9 0.002 A0 -0.049 A1 0.012 A2 0.009 A3 0.002 A4 -0.049 A5 0.009 A6 0.002 A7 0.002 A8 0.012 A9 0.008 A0 0.001 A1 0.001 A2 0.007 A3 0.008 A4 0.001 A5 0.001 A6 0.003 A7 0.012 A8 0.001 A9 0.001</p>	<p>ALPHA S = -4 CL/SIG = 0.039 THETA = 6 CO/SIG = 0.0019 ALPHA C = -9.9</p> <p>FLAPPING</p> <p>A0 1.734 A1 -0.039 A2 3.132 A3 0.046 A4 -0.387 A5 -0.074 A6 0.009 A7 -0.046 A8 0.039 A9 -0.172 A0 0.014 A1 -0.046 A2 0.122 A3 -0.074 A4 0.028 A5 0.007 A6 0.041 A7 0.043 A8 0.002 A9 0.007 A0 -0.041 A1 0.043 A2 0.007 A3 0.002 A4 -0.041 A5 0.007 A6 0.002 A7 0.002 A8 0.013 A9 0.008 A0 0.002 A1 0.002 A2 0.004 A3 0.013 A4 0.001 A5 0.001 A6 0.004 A7 0.013 A8 0.001 A9 0.001 A0 0.019 A1 0.018 A2 0.002 A3 0.001</p>
<p>ALPHA S = -4 CL/SIG = 0.008 THETA = 8 CO/SIG = 0.0034 ALPHA C = -11.9</p> <p>FLAPPING</p> <p>A0 2.348 A1 0.011 A2 0.094 A3 0.011 A4 -0.244 A5 -0.027 A6 0.017 A7 0.019 A8 0.109 A9 -0.027 A0 0.048 A1 -0.048 A2 0.109 A3 -0.027 A4 0.019 A5 0.004 A6 0.048 A7 -0.027 A8 0.009 A9 0.002 A0 -0.048 A1 0.036 A2 0.003 A3 0.004 A4 0.014 A5 0.009 A6 -0.003 A7 0.001 A8 0.014 A9 0.009 A0 -0.003 A1 0.001 A2 0.002 A3 0.019 A4 -0.002 A5 0.001 A6 0.002 A7 0.019 A8 0.002 A9 0.001 A0 0.018 A1 0.008 A2 0.002 A3 0.001</p>	<p>ALPHA S = -4 CL/SIG = 0.061 THETA = 10 CO/SIG = 0.0093 ALPHA C = -14.1</p> <p>FLAPPING</p> <p>A0 3.242 A1 0.048 A2 0.232 A3 0.097 A4 -0.342 A5 -0.029 A6 0.029 A7 0.007 A8 0.199 A9 -0.029 A0 0.081 A1 -0.029 A2 0.227 A3 -0.029 A4 0.046 A5 0.003 A6 0.130 A7 0.048 A8 0.019 A9 0.002 A0 -0.048 A1 0.048 A2 0.002 A3 0.010 A4 0.048 A5 0.021 A6 0.001 A7 0.001 A8 0.048 A9 0.034 A0 0.009 A1 0.009 A2 0.007 A3 0.009 A4 0.009 A5 0.001 A6 0.024 A7 0.007 A8 0.004 A9 0.001</p>	<p>ALPHA S = -4 CL/SIG = 0.070 THETA = 12 CO/SIG = 0.0080 ALPHA C = -15.6</p> <p>FLAPPING</p> <p>A0 3.212 A1 0.017 A2 0.217 A3 0.177 A4 -0.321 A5 -0.021 A6 0.021 A7 0.017 A8 0.177 A9 -0.021 A0 0.110 A1 -0.021 A2 0.272 A3 -0.021 A4 0.084 A5 0.039 A6 0.148 A7 0.043 A8 0.023 A9 0.015 A0 -0.021 A1 0.043 A2 0.006 A3 0.012 A4 0.024 A5 0.198 A6 0.006 A7 0.019 A8 0.024 A9 0.033 A0 0.003 A1 0.002 A2 0.011 A3 0.026 A4 0.004 A5 0.005 A6 0.009 A7 0.033 A8 0.002 A9 0.001</p>
<p>ALPHA S = -8 CL/SIG = 0.073 THETA = 13 CO/SIG = 0.0059 ALPHA C = -16.8</p> <p>FLAPPING</p> <p>A0 3.712 A1 0.002 A2 0.009 A3 0.217 A4 -1.242 A5 -0.026 A6 0.047 A7 0.047 A8 0.423 A9 -0.026 A0 0.123 A1 -0.026 A2 0.213 A3 -0.026 A4 0.048 A5 0.019 A6 0.123 A7 -0.026 A8 0.033 A9 0.023 A0 -0.026 A1 0.104 A2 0.018 A3 0.001 A4 0.004 A5 0.249 A6 0.009 A7 0.022 A8 0.033 A9 0.038 A0 -0.018 A1 0.018 A2 0.017 A3 0.017 A4 0.013 A5 0.001 A6 0.004 A7 0.017 A8 0.006 A9 0.002 A0 0.004 A1 0.031 A2 0.006 A3 0.002</p>	<p>ALPHA S = -8 CL/SIG = 0.006 THETA = 4 CO/SIG = 0.0000 ALPHA C = -10.4</p> <p>FLAPPING</p> <p>A0 0.117 A1 0.103 A2 2.319 A3 0.098 A4 -0.177 A5 -0.049 A6 0.009 A7 -0.049 A8 0.101 A9 -0.216 A0 0.007 A1 -0.009 A2 0.043 A3 0.009 A4 0.010 A5 0.002 A6 0.024 A7 0.009 A8 0.002 A9 0.002 A0 -0.020 A1 0.018 A2 0.004 A3 0.001 A4 0.004 A5 0.007 A6 0.001 A7 0.001 A8 0.010 A9 0.008 A0 0.001 A1 0.001 A2 0.019 A3 0.021 A4 0.001 A5 0.001</p>	<p>ALPHA S = -8 CL/SIG = 0.010 THETA = 6 CO/SIG = 0.0011 ALPHA C = -12.2</p> <p>FLAPPING</p> <p>A0 0.311 A1 0.028 A2 1.001 A3 0.070 A4 -0.211 A5 -0.028 A6 0.008 A7 -0.070 A8 0.007 A9 -0.211 A0 0.004 A1 -0.019 A2 0.038 A3 -0.027 A4 0.014 A5 0.002 A6 0.003 A7 0.024 A8 0.002 A9 0.002 A0 -0.049 A1 0.004 A2 0.001 A3 0.001 A4 0.011 A5 0.008 A6 0.002 A7 0.001 A8 0.010 A9 0.007 A0 0.001 A1 0.001 A2 0.011 A3 0.018 A4 0.001 A5 0.001</p>

TABLE I CONTINUED.

ADVANCE RATIO = 0.400		ALPHA 5 = -8 CL/SIG = 0.021 THETA = 0 CO/SIG = 0.0023 ALPHA C = -14.8		ALPHA 5 = -8 CL/SIG = 0.039 THETA = 10 CO/SIG = 0.0043 ALPHA C = -16.1		ALPHA 5 = -8 CL/SIG = 0.050 THETA = 12 CO/SIG = 0.0067 ALPHA C = -18.2																							
AO	1.036	FLAPPING	AO -1.184	LAGGING	AO 2.034	FLAPPING	AO 2.408	LAGGING	AO 0.948																				
A1	0.131	81	0.074	A1	0.110	81	0.064	A1	-0.170	81	0.102	A1	-0.197	81	0.074														
A2	0.443	82	-0.328	A2	0.002	A2	0.001	A2	-0.721	82	-0.389	A2	0.006	82	0.015														
A3	0.101	83	-0.435	A3	0.822	A3	-0.642	A3	0.152	83	0.036	A3	0.045	83	-0.819														
A4	0.123	84	-0.049	A4	0.022	A4	0.033	A4	0.165	84	-0.537	A4	0.012	84	0.027														
A5	0.012	85	-0.050	A5	-0.084	A5	-0.033	A5	0.112	85	-0.078	A5	0.042	A5	-0.016	85	0.003												
A6	0.013	86	-0.002	A6	0.001	A6	-0.001	A6	0.004	86	-0.004	A6	-0.004	A6	0.001	86	-0.003												
A7	0.013	87	-0.002	A7	0.001	A7	-0.001	A7	0.004	87	-0.004	A7	-0.004	A7	0.001	87	-0.003												
A8	0.013	88	0.003	A8	-0.001	A8	0.001	A8	0.021	88	0.014	A8	0.003	A8	0.020	88	0.004												
A9	0.013	89	0.011	A9	0.001	A9	0.001	A9	0.008	89	0.014	A9	0.003	A9	0.015	89	0.004												
A10	-0.002	910	0.011	A10	0.002	A10	0.001	A10	-0.002	910	0.010	A10	0.002	A10	0.012	910	0.001												
ZERO LAG DAMPING										ZERO LAG DAMPING																			
ALPHA 5 = -8 CL/SIG = 0.022 THETA = 0 CO/SIG = 0.0017 ALPHA C = -10.8										ALPHA 5 = -4 CL/SIG = 0.035 THETA = 0 CO/SIG = 0.0029 ALPHA C = -12.9										ALPHA 5 = -4 CL/SIG = 0.051 THETA = 10 CO/SIG = 0.0049 ALPHA C = -16.6									
AO	2.825	FLAPPING	AO 2.428	LAGGING	AO 1.032	FLAPPING	AO 0.132	LAGGING	AO 0.034	FLAPPING	AO 1.013	LAGGING	AO 0.359																
A1	-0.401	81	0.027	A1	-0.340	81	0.127	A1	0.440	81	-0.213	A1	0.118	A1	-0.050	81	-0.049	A1	0.071	81	0.094								
A2	-1.267	82	-0.896	A2	-0.001	A2	0.027	A2	0.003	82	-0.847	A2	0.001	A2	-0.249	82	-0.519	A2	0.008	82	-0.042								
A3	0.424	83	-0.893	A3	0.073	A3	-0.040	A3	0.093	83	-0.893	A3	-0.014	A3	0.045	83	-0.284	A3	-0.008	83	-0.042								
A4	0.221	84	-0.095	A4	0.053	A4	0.041	A4	0.025	84	-0.013	A4	0.010	A4	0.028	84	-0.023	A4	0.043	84	-0.001								
A5	0.117	85	-0.024	A5	0.016	A5	-0.004	A5	-0.012	85	-0.012	A5	0.002	A5	-0.003	85	-0.017	A5	-0.002	85	0.001								
A6	0.010	86	-0.121	A6	0.010	A6	0.011	A6	0.072	86	-0.058	A6	0.002	A6	0.049	86	-0.050	A6	0.001	86	-0.002								
A7	0.010	87	-0.002	A7	-0.008	A7	0.008	A7	0.004	87	-0.004	A7	-0.002	A7	0.008	87	0.004	A7	0.001	87	-0.002								
A8	0.010	88	0.044	A8	-0.008	A8	0.008	A8	0.004	88	0.011	A8	-0.002	A8	0.008	88	0.004	A8	0.001	88	-0.002								
A9	0.010	89	0.011	A9	0.008	A9	0.005	A9	0.004	89	-0.002	A9	-0.002	A9	0.004	89	0.004	A9	0.001	89	0.003								
A10	0.010	910	0.010	A10	0.002	A10	0.001	A10	0.017	910	0.007	A10	-0.002	A10	0.014	910	0.010	A10	0.001	910	0.001								
ZERO LAG DAMPING										ZERO LAG DAMPING																			
ALPHA 5 = -4 CL/SIG = 0.022 THETA = 0 CO/SIG = 0.0017 ALPHA C = -10.8										ALPHA 5 = -4 CL/SIG = 0.035 THETA = 0 CO/SIG = 0.0029 ALPHA C = -12.9										ALPHA 5 = -4 CL/SIG = 0.051 THETA = 10 CO/SIG = 0.0049 ALPHA C = -16.6									
AO	1.483	FLAPPING	AO 0.787	LAGGING	AO 2.454	FLAPPING	AO 2.454	LAGGING	AO 1.509																				
A1	0.134	81	0.024	A1	0.011	A1	-0.049	A1	0.176	A1	-0.489	A1	0.003																
A2	0.502	82	-0.579	A2	0.014	A2	-0.611	A2	-0.444	A2	-0.368	A2	0.032	A2	0.050														
A3	0.045	83	-0.654	A3	0.017	A3	-0.681	A3	0.014	A3	-0.700	A3	0.034	A3	-0.114														
A4	0.123	84	-0.121	A4	0.019	A4	-0.080	A4	0.232	84	-0.244	A4	0.046	A4	0.014														
A5	0.059	85	-0.044	A5	0.002	A5	-0.007	A5	0.076	85	-0.071	A5	-0.008	A5	-0.004														
A6	0.014	86	-0.002	A6	-0.002	A6	-0.002	A6	0.071	86	-0.014	A6	-0.007	A6	0.002														
A7	0.012	87	-0.009	A7	-0.002	A7	-0.002	A7	0.020	87	-0.004	A7	-0.004	A7	0.004														
A8	0.012	88	0.011	A8	0.003	A8	0.003	A8	0.010	88	0.016	A8	0.004	A8	0.004														
A9	0.012	89	0.011	A9	0.003	A9	0.003	A9	0.010	89	0.016	A9	0.004	A9	0.004														
A10	0.021	910	0.017	A10	0.002	A10	0.001	A10	-0.002	910	0.003	A10	0.001	A10	0.001														

TABLE II SHEAR FORCE HARMONIC COEFFICIENTS, LB.

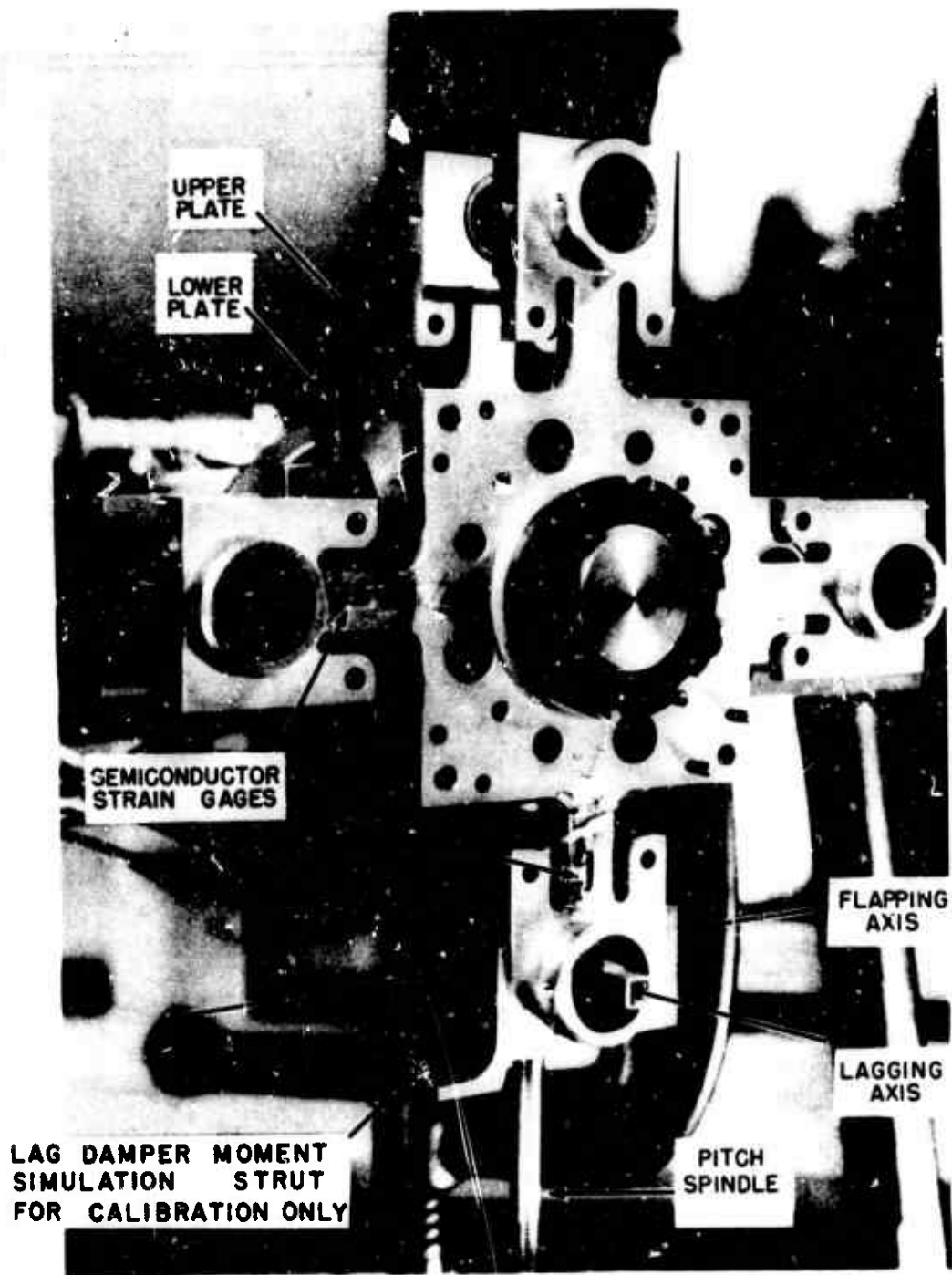
ADVANCE RATIO = 0.191						
ALPHA S = -4		ALPHA C = -6.9		THETA = 6		
CL/SIG = 0.071		CD/SIG = -0.0041		CQ/SIG = 0.0024		
FLATWISE		EDGEWISE		RADIAL		
N	COSINE	SINE	COSINE	SINE	COSINE	SINE
1	0.5	0.9	1.8	1.1	-7.9	0.9
2	-0.6	0.0	-0.3	0.0	0.4	1.1
3	1.6	0.0	-0.5	-0.5	0.6	1.2
4	-0.2	0.3	0.2	-0.2	-0.5	0.4
5	0.3	0.1	0.0	-0.1	0.3	0.0
6	0.1	0.0	-0.1	0.2	-0.2	0.2
7	0.2	0.1	-0.5	0.0	0.0	-0.1
8	0.0	-0.1	-0.2	0.0	0.0	0.0
9	-0.1	0.0	-0.2	0.1	-0.1	-0.0
10	0.2	0.1	-0.1	0.2	-0.2	0.2
ADVANCE RATIO = 0.283						
ALPHA S = -4		ALPHA C = -4.8		THETA = 2		
CL/SIG = 0.019		CD/SIG = 0.0007		CQ/SIG = 0.0004		
N	COSINE	SINE	COSINE	SINE	COSINE	SINE
1	-0.4	-3.3	2.3	1.1	-2.3	1.6
2	0.3	-0.3	-0.2	0.3	0.1	-0.7
3	0.4	-0.1	-0.4	-0.3	-0.0	0.4
4	0.2	0.0	0.2	-0.2	-0.2	0.0
5	0.0	-0.0	-0.1	-0.0	-0.0	0.1
6	0.0	0.1	-0.0	-0.1	0.0	0.0
7	-0.3	-0.0	-0.0	-0.0	-0.0	0.0
8	0.0	0.0	-0.0	-0.0	0.0	0.0
9	-0.1	0.1	-0.0	-0.0	-0.1	0.0
10	-0.3	-0.1	0.2	0.1	-0.1	-0.1
ALPHA S = -4 ALPHA C = -6.5 THETA = 4						
CL/SIG = 0.041		CD/SIG = -0.0008		CQ/SIG = 0.0011		
N	COSINE	SINE	COSINE	SINE	COSINE	SINE
1	-1.0	-2.3	0.5	-0.1	-1.2	0.1
2	-0.3	-0.3	-0.3	0.5	-0.0	-0.7
3	0.7	-0.2	0.0	0.2	-0.2	0.2
4	0.2	0.4	-0.2	0.1	-0.2	-0.1
5	0.1	-0.0	0.1	0.1	0.1	0.1
6	-0.0	0.1	0.0	-0.1	-0.0	0.0
7	-0.3	-0.1	-0.1	-0.0	-0.1	-0.0
8	0.0	-0.1	0.0	0.1	-0.1	-0.1
9	0.1	-0.2	-0.1	0.3	-0.2	-0.2
10	-0.3	-0.2	0.1	-0.0	-0.0	-0.1
ALPHA S = -4 ALPHA C = -7.9 THETA = 6						
CL/SIG = 0.062		CD/SIG = -0.0029		CQ/SIG = 0.0022		
N	COSINE	SINE	COSINE	SINE	COSINE	SINE
1	-2.4	-1.0	-2.2	-0.3	-0.5	-0.2
2	-0.7	-0.6	0.0	0.9	-0.2	-0.9
3	1.4	-0.7	0.5	0.8	-0.5	-0.1
4	0.0	0.4	-0.2	-0.1	0.1	-0.2
5	0.3	-0.2	0.3	0.3	0.2	-0.1
6	0.0	0.1	0.0	0.0	-0.0	-0.1
7	-0.6	-0.2	0.2	-0.0	-0.0	-0.1
8	-0.1	-0.4	0.1	0.2	-0.2	-0.2
9	0.2	0.1	-0.3	-0.0	0.1	0.1
10	0.4	-0.3	0.1	0.0	-0.0	-0.0

TABLE II CONCLUDED

ADVANCE RATIO = 0.389						
ALPHA S = -4		ALPHA C = -9.5		THETA = 6		
CL/SIG = 0.046		CD/SIG = -0.0018		CQ/SIG = 0.0022		
FLATWISE		EDGEWISE		RADIAL		
N	COSINE	SINE	COSINE	SINE	COSINE	SINE
1	-2.1	-1.5	-0.5	-0.2	-0.6	-0.2
2	-1.2	-1.8	-0.6	-1.2	0.0	1.0
3	1.0	-1.4	-0.9	0.5	0.8	0.5
4	0.7	0.3	-0.2	-0.4	-0.3	0.3
5	0.2	0.0	0.0	-0.3	0.4	0.2
6	-0.2	0.2	-0.2	0.1	-0.1	-0.1
7	0.2	0.3	0.1	0.1	-0.3	-0.1
8	-0.4	0.1	-0.1	-0.2	0.2	-0.1
9	-0.2	0.3	-0.2	-0.2	0.0	0.3
10	0.0	0.1	-0.1	-0.1	0.0	-0.0
ADVANCE RATIO = 0.488						
ALPHA S = -4		ALPHA C = -11.9		THETA = 8		
CL/SIG = 0.048		CD/SIG = -0.0024		CQ/SIG = 0.0034		
1	-0.5	-0.2	0.0	0.4	0.2	-0.3
2	-1.3	-2.4	-0.9	-1.5	0.5	1.4
3	0.0	-2.6	-1.3	1.2	0.6	0.3
4	0.6	-1.0	-0.7	-1.0	-0.3	0.5
5	0.4	-0.2	-0.1	0.0	0.4	-0.1
6	-0.2	0.2	0.0	0.3	-0.1	-0.0
7	0.3	-1.1	-0.3	-0.2	0.1	1.0
8	0.1	0.4	0.3	0.3	-0.4	-0.2
9	-0.2	0.3	0.0	0.3	0.1	-0.7
10	-0.3	-0.1	0.0	0.0	0.2	-0.2
ADVANCE RATIO = 0.683						
ALPHA S = -4		ALPHA C = -17.7		THETA = 12		
CL/SIG = 0.032		CD/SIG = 0.0033		CQ/SIG = 0.0042		
1	2.0	0.0	2.0	0.0	-1.0	-0.7
2	-2.9	-2.4	-2.9	2.4	2.3	1.1
3	-2.0	-2.7	-2.0	2.7	2.2	-1.0
4	-4.3	-4.3	-4.3	-4.3	4.6	2.9
5	0.3	0.0	0.0	0.3	0.3	-1.3
6	1.0	-0.1	1.0	-0.1	-0.7	0.1
7	0.0	0.4	0.0	0.4	0.1	0.3
8	0.4	-0.9	0.4	-0.8	-0.6	0.4
9	0.3	0.2	0.3	0.3	-0.1	-0.1
0	0.8	0.3	0.8	0.3	-0.4	-0.0

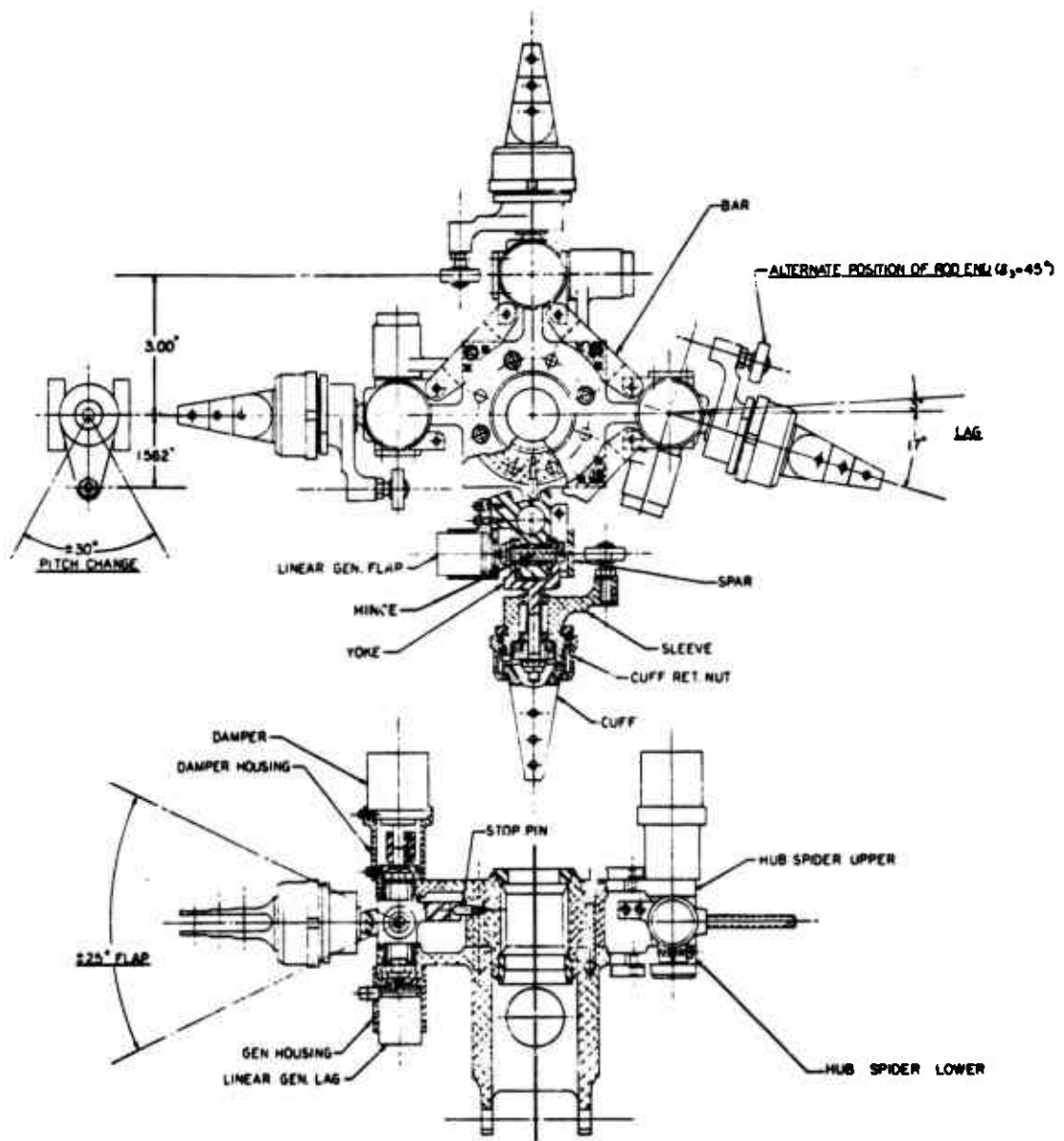
TABLE III - SCALING RATIOS

Model linear dimension = 1/S x full scale linear dimension	
Subscript m - model Subscript fs - full scale	
Parameter	Full Scale Blade
Radius & other linear dimensions R_m/R_{fs}	1/S
Areas- A_m/A_{fs}	1/S ²
Mass per unit length m_m/m_{fs}	1/S ²
Total mass M_{bm}/M_{bfs}	1/S ³
Stiffness EI_{xxm}/EI_{xxfs} , etc.	1/S ⁵
Angular velocity Ω_m/Ω_{fs}	\sqrt{S}
Linear velocities $(\Omega R)_m/(\Omega R)_{fs}$	1/ \sqrt{S}
Mach number M_m/M_{fs}	1/ \sqrt{S}
Froude number $(\Omega^2 R/g)_m/(\Omega^2 R/g)_{fs}$	1
Reynolds number RN_m/RN_{fs}	1/S ^{3/2}
Output forces F_m/F_{fs}	1/S ³
Output moments $Mom._m/Mom._{fs}$	1/S ⁴
Output elastic strains ϵ_m/ϵ_{fs}	1
Natural frequencies ω_m/ω_{fs}	\sqrt{S}



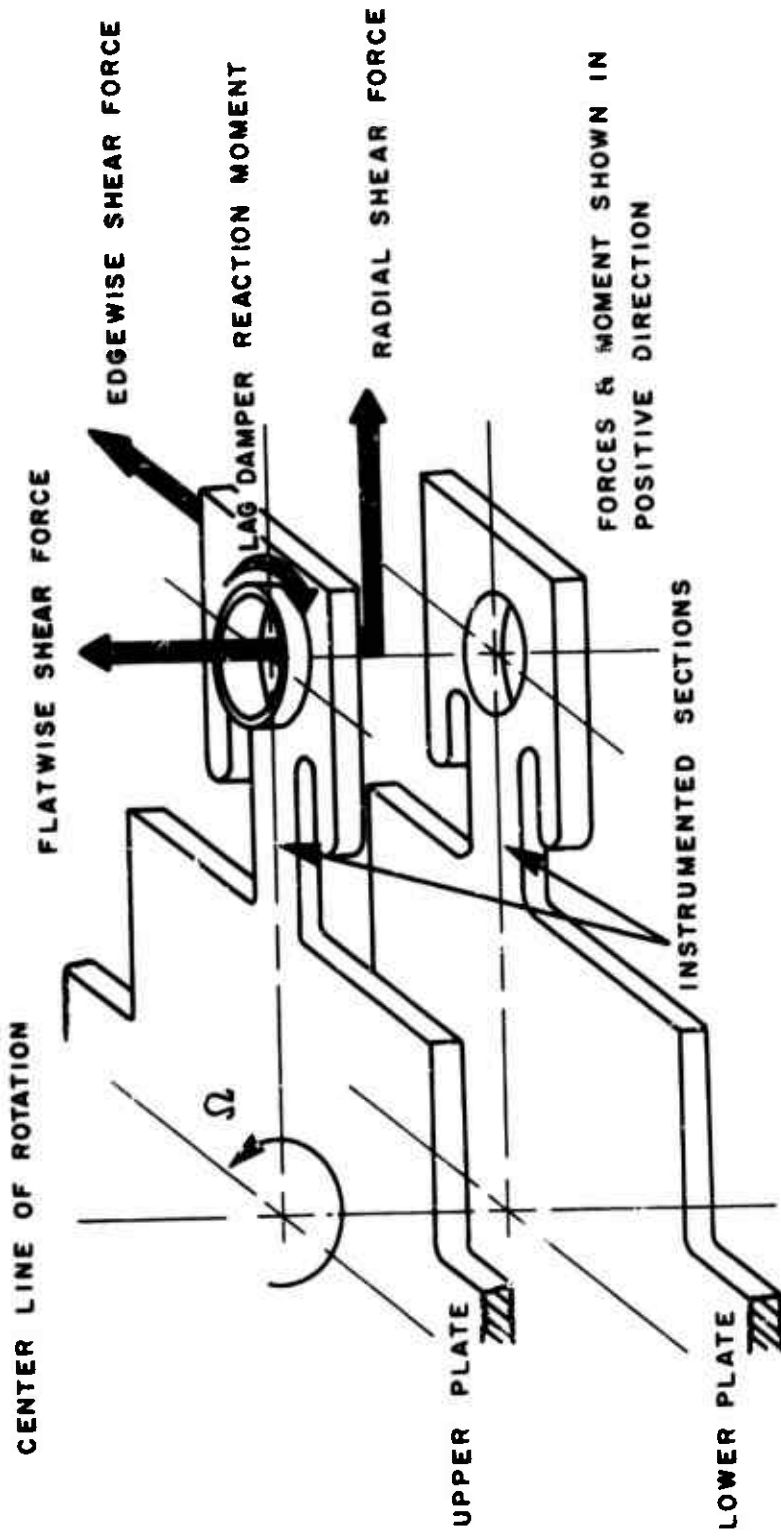
(a) BASIC INSTALLATION

Figure 1. Vibratory Shear Force Rotor Head.



(b) ASSEMBLY DRAWING

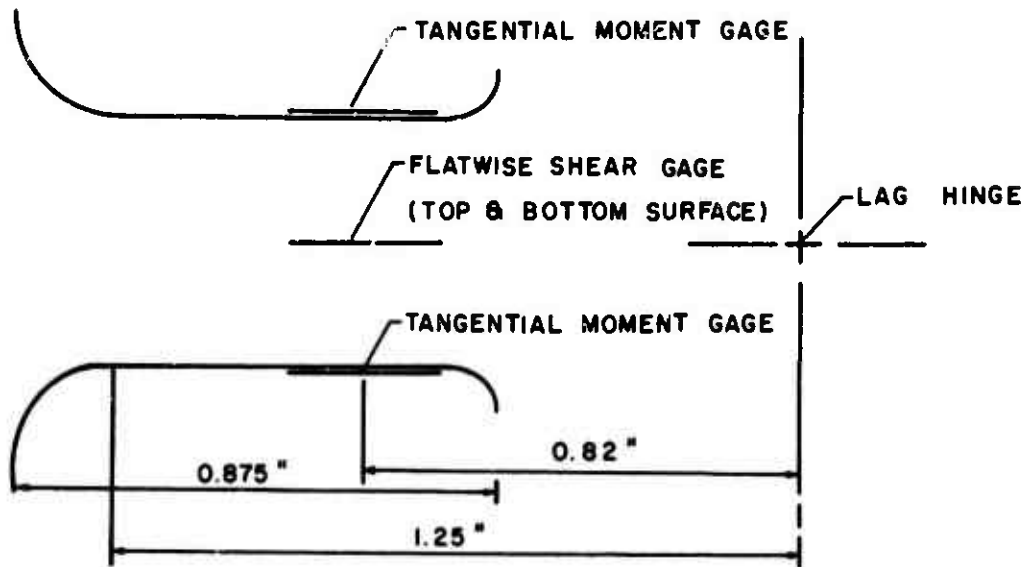
Figure 1. Concluded.



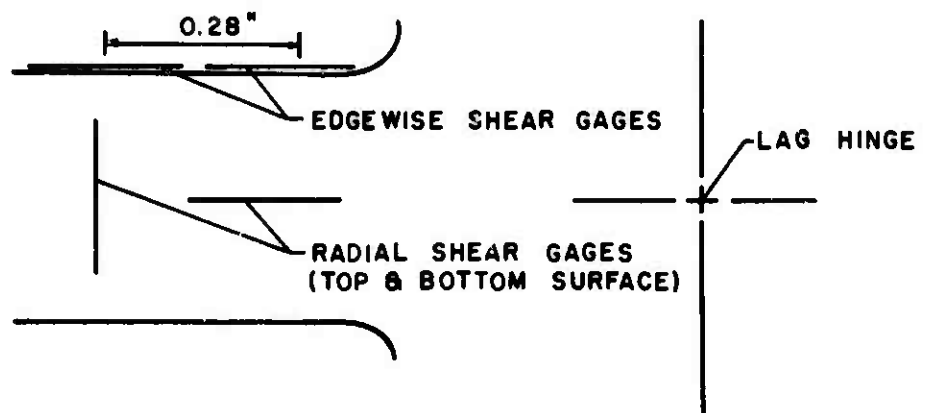
(a) DEFINITION OF SHEAR FORCES AND LAG DAMPER REACTION MOMENT

Figure 2. Vibratory Shear Force Rotor Head Details.

UPPER INSTRUMENTED SECTION - TOP VIEW



LOWER INSTRUMENTED SECTION - TOP VIEW



(b) SEMICONDUCTOR STRAIN GAGE LOCATIONS

Figure 2. Concluded.

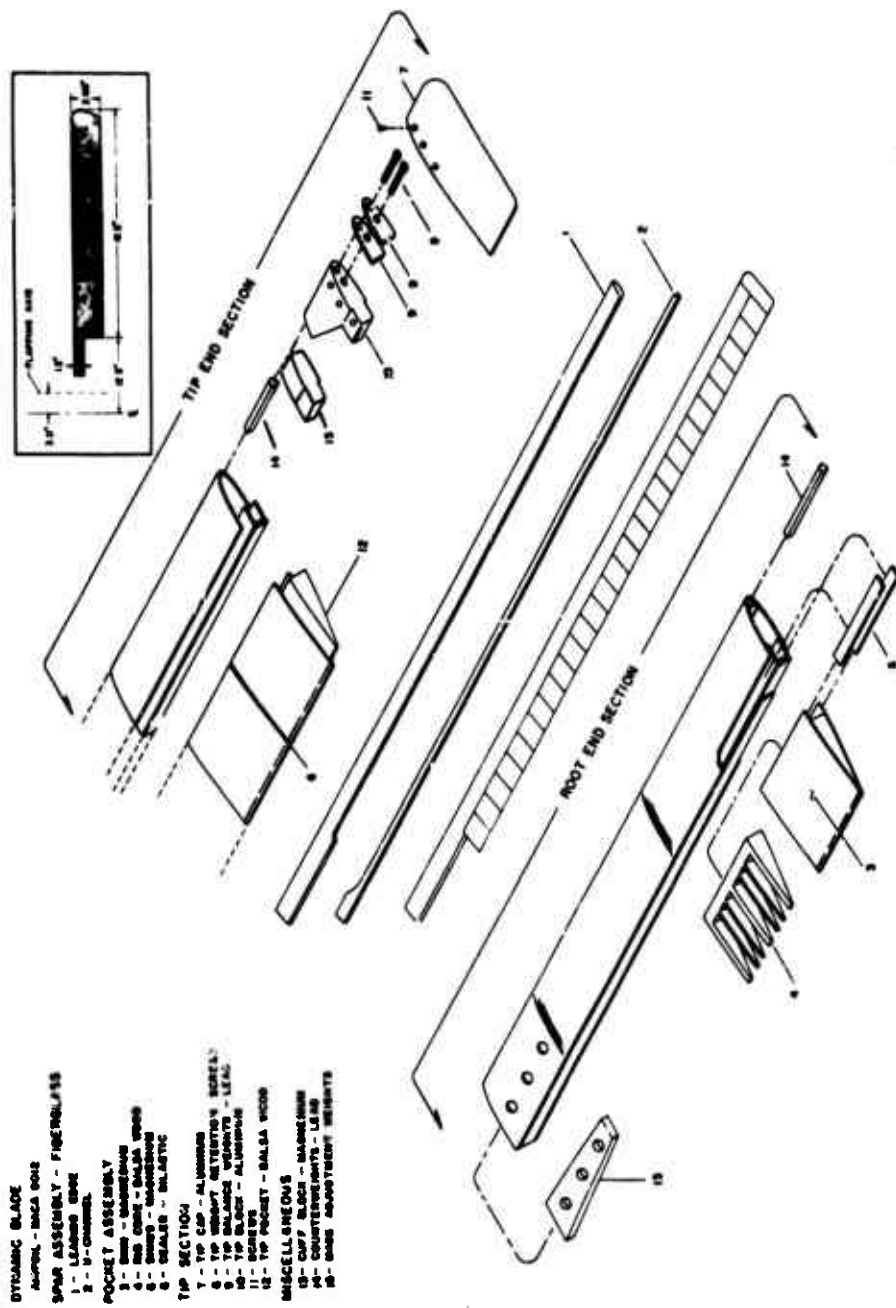


Figure 3. Dynamically Scaled Blade-Exploded View.

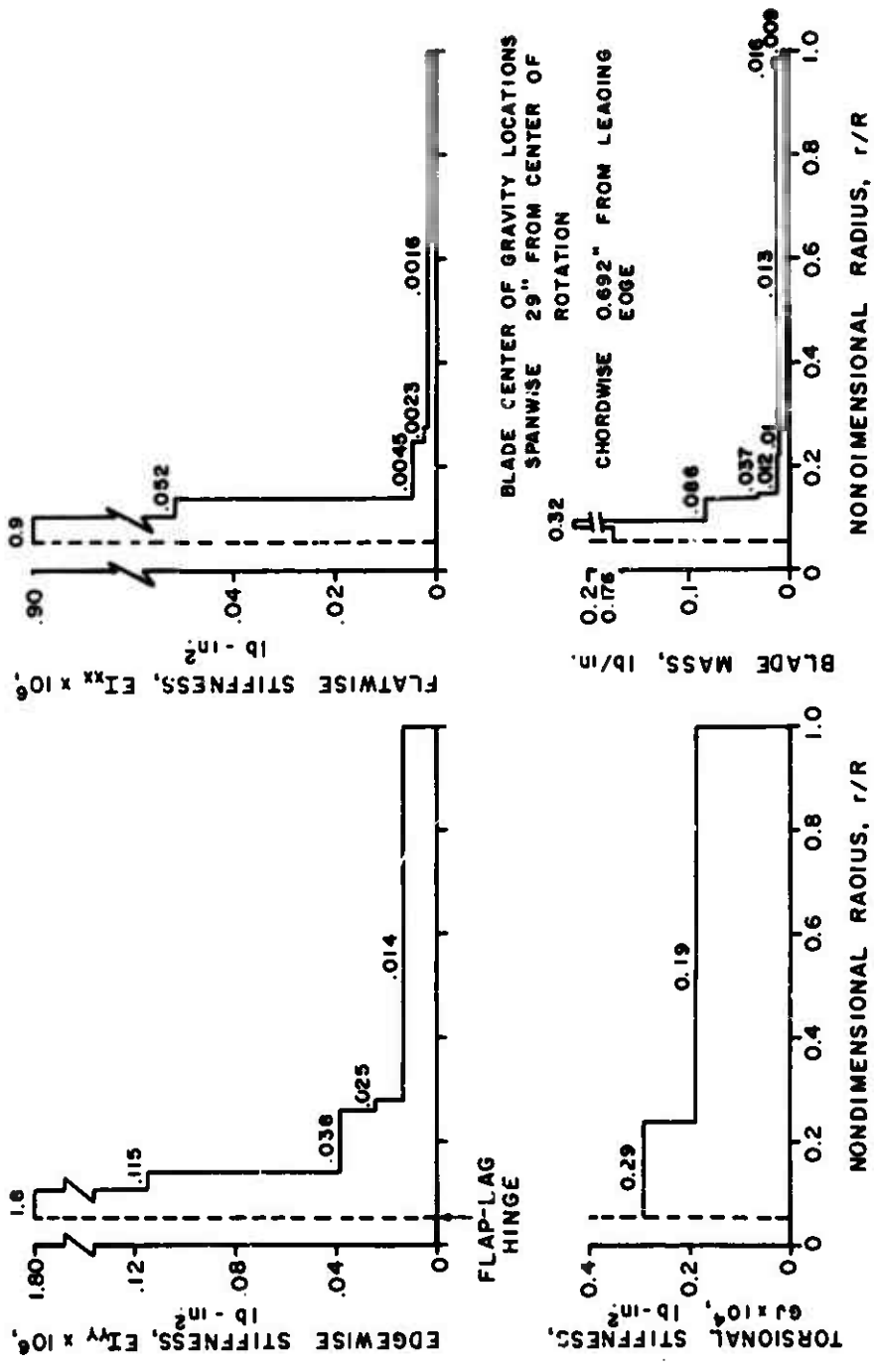


Figure 4. Dynamic Blade Physical Properties.

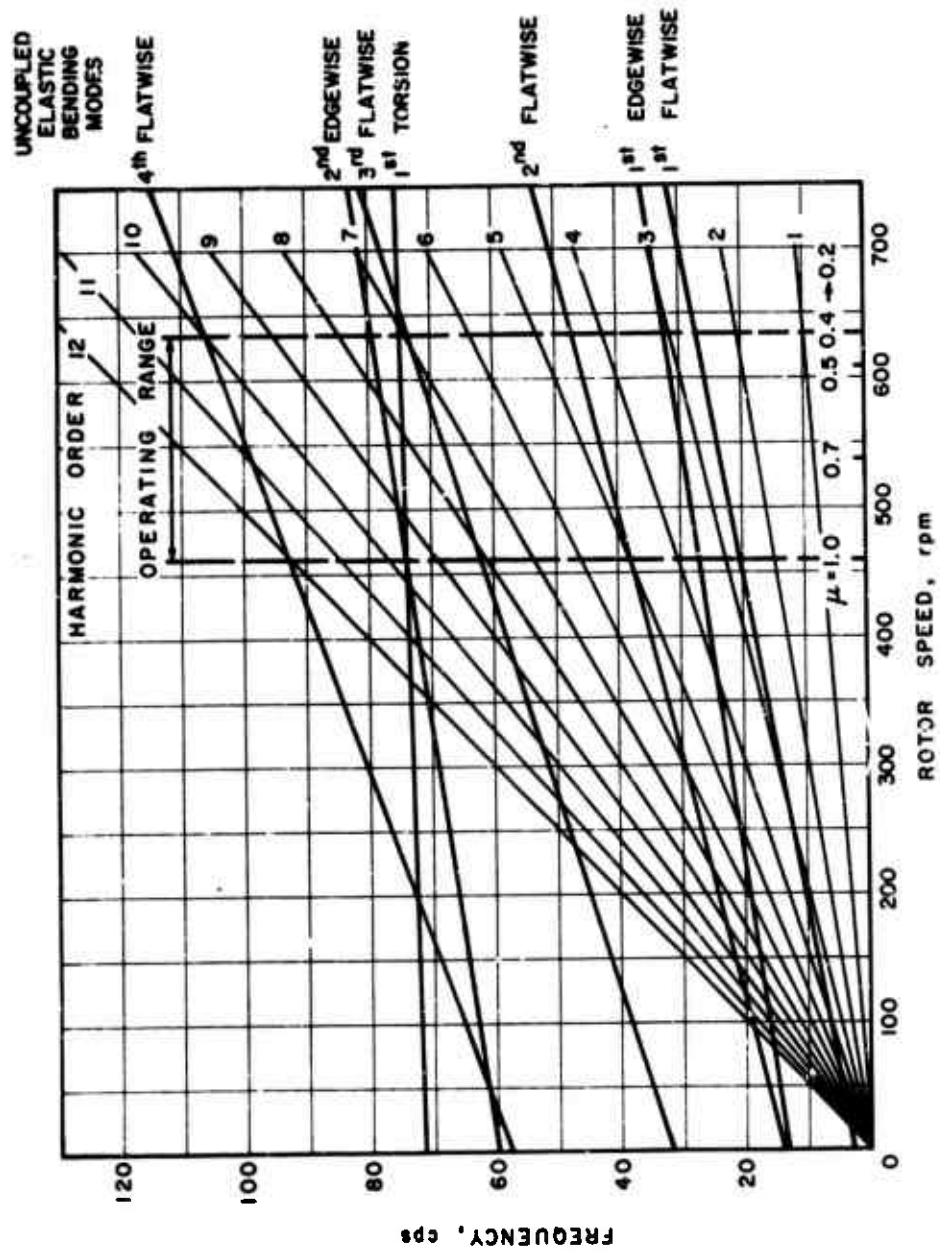


Figure 5. Model Rotor Blade Calculated Natural Frequencies.

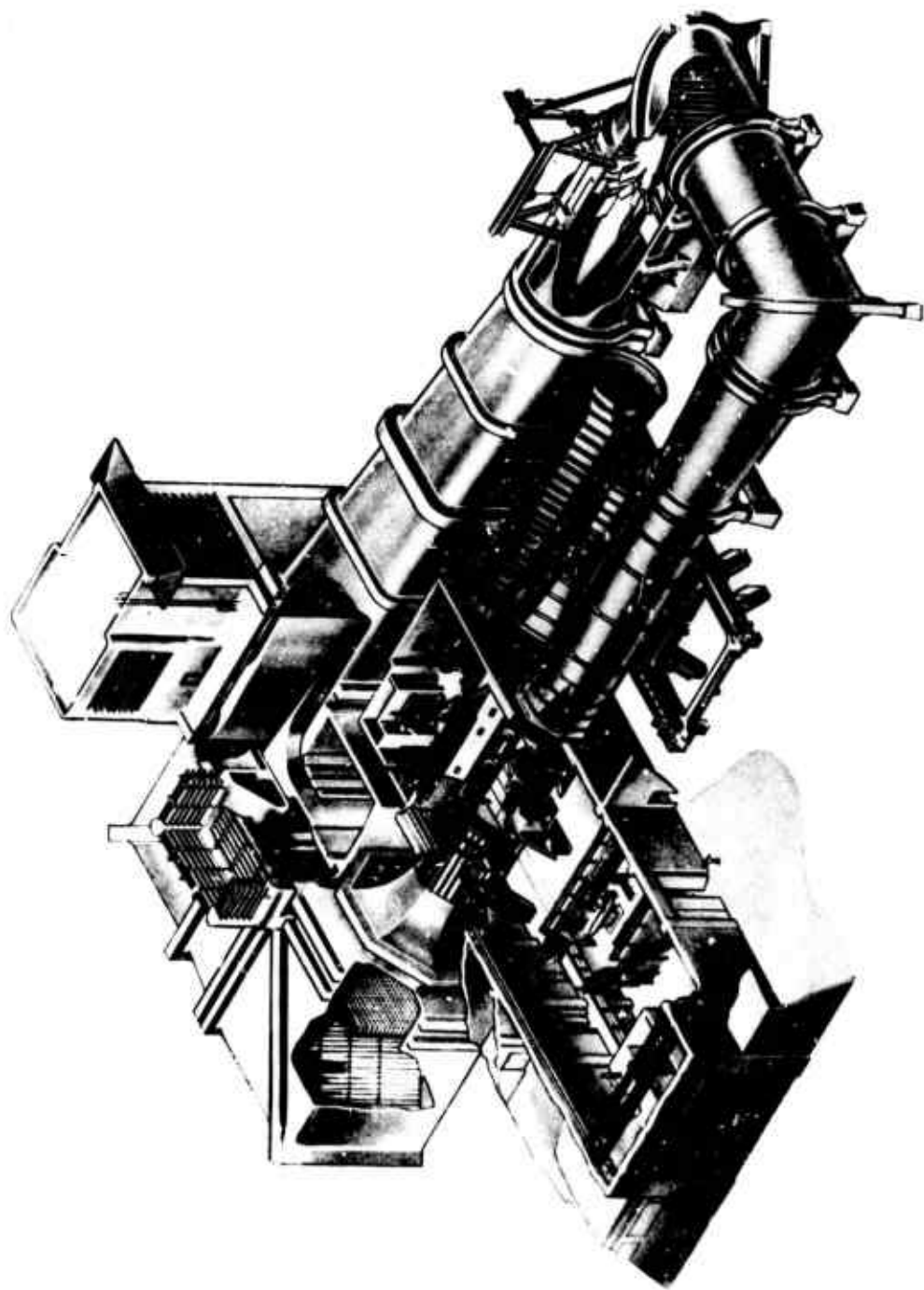
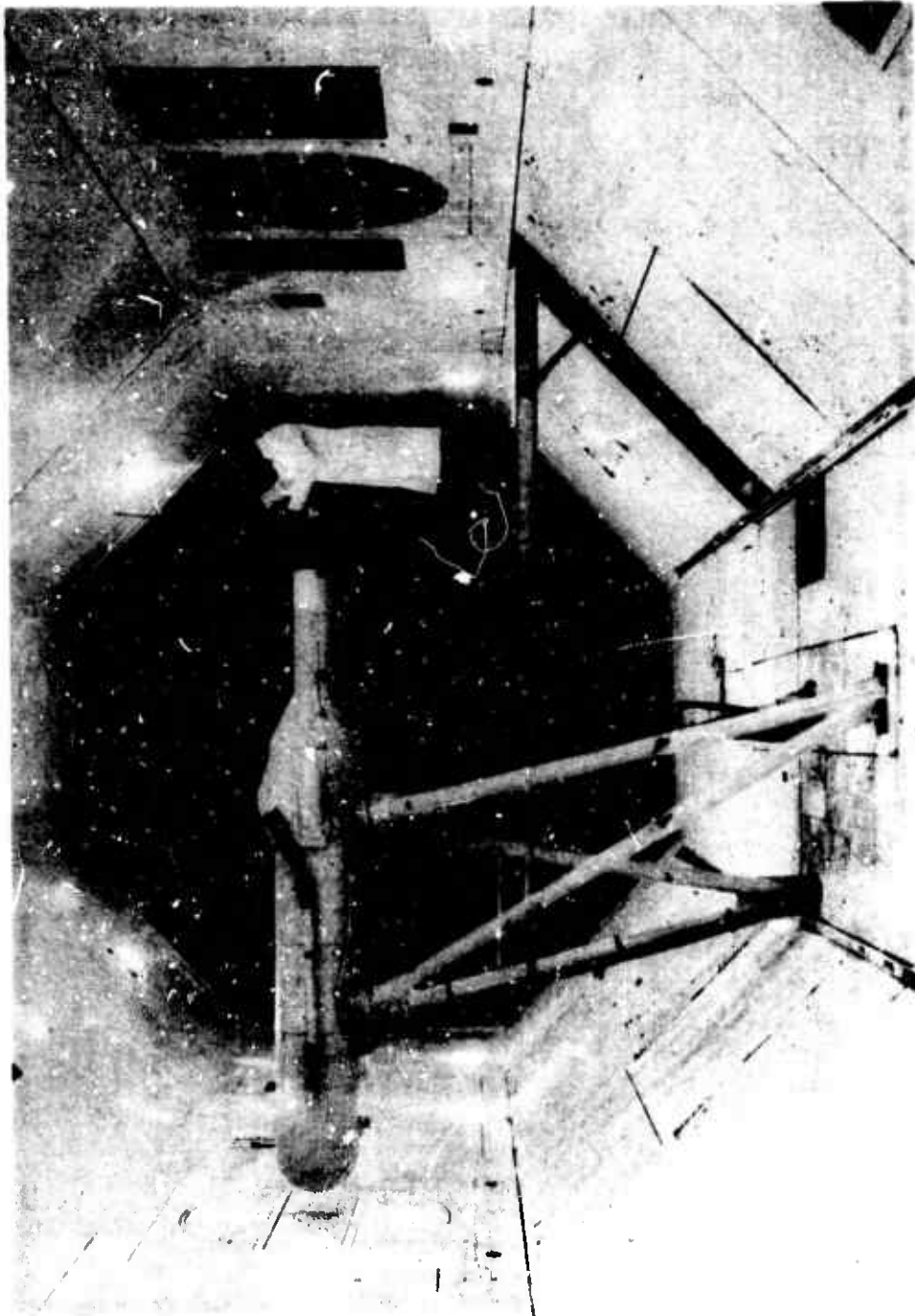
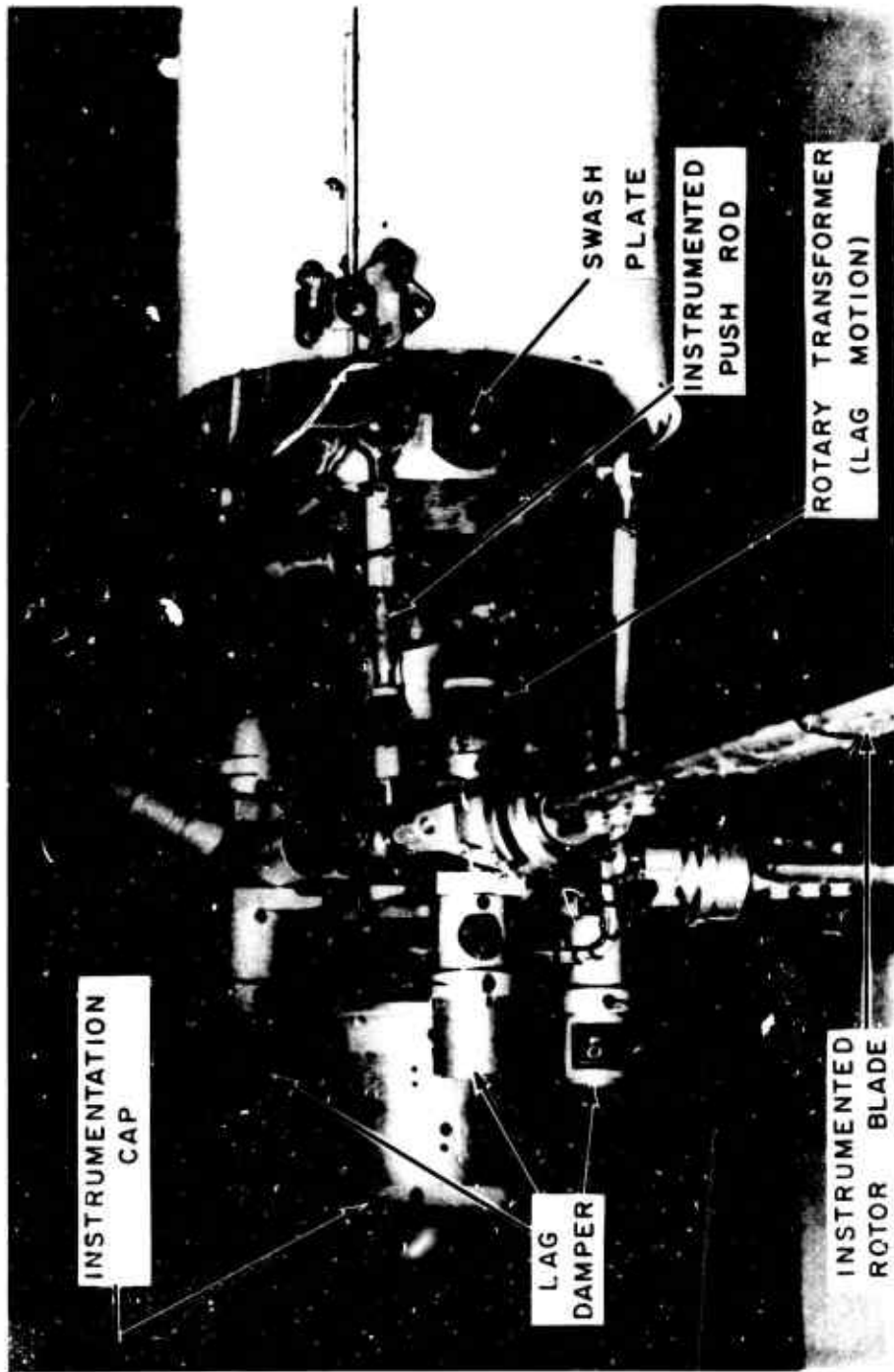


Figure 6. United Aircraft's Subsonic Wind Tunnel.



(a) GENERAL VIEW OF MODEL INSTALLATION IN WIND TUNNEL

Figure 7. Sikorsky Helicopter Rotor Test Rig.



(b) DETAILS OF HUB AND SWASH PLATE AREA

Figure 7. Concluded.

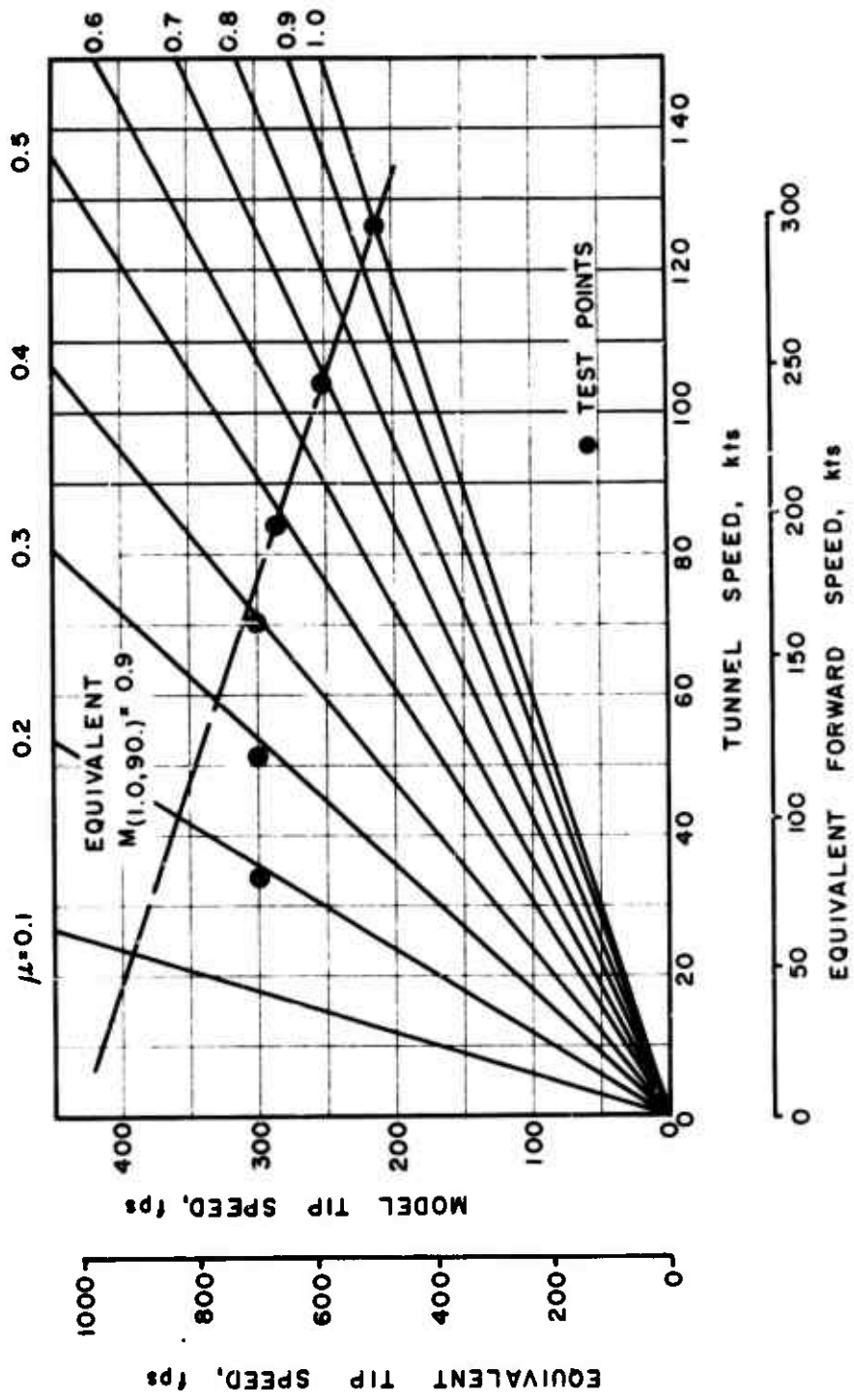
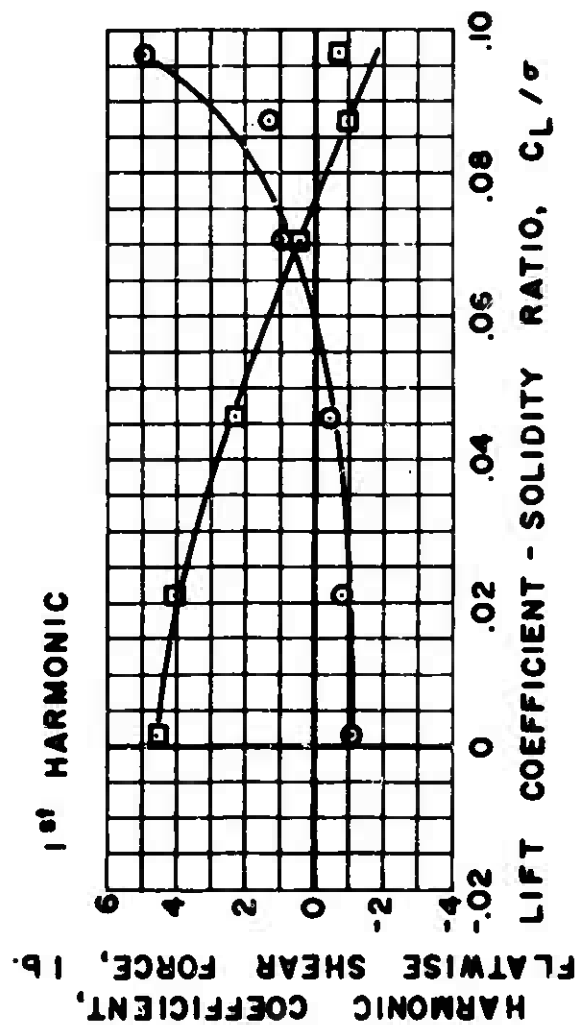


Figure 8. Wind Tunnel Test Conditions.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



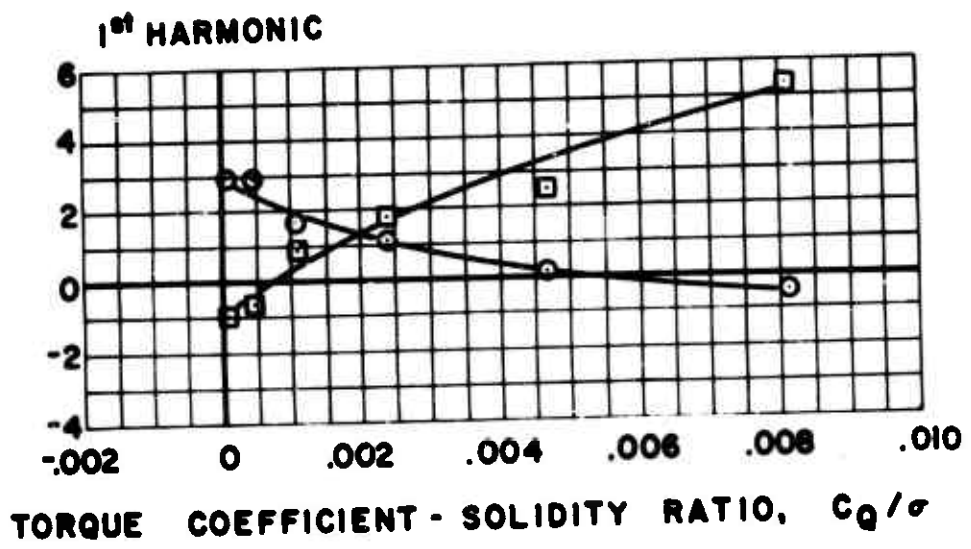
$\alpha_s = -4 \text{ deg. } \mu = 0.2$

(a) TRIMMED

Figure 9. Effect of Trim Condition on Shear Forces.

HARMONIC COEFFICIENT,
EDGEWISE SHEAR FORCE, lb.

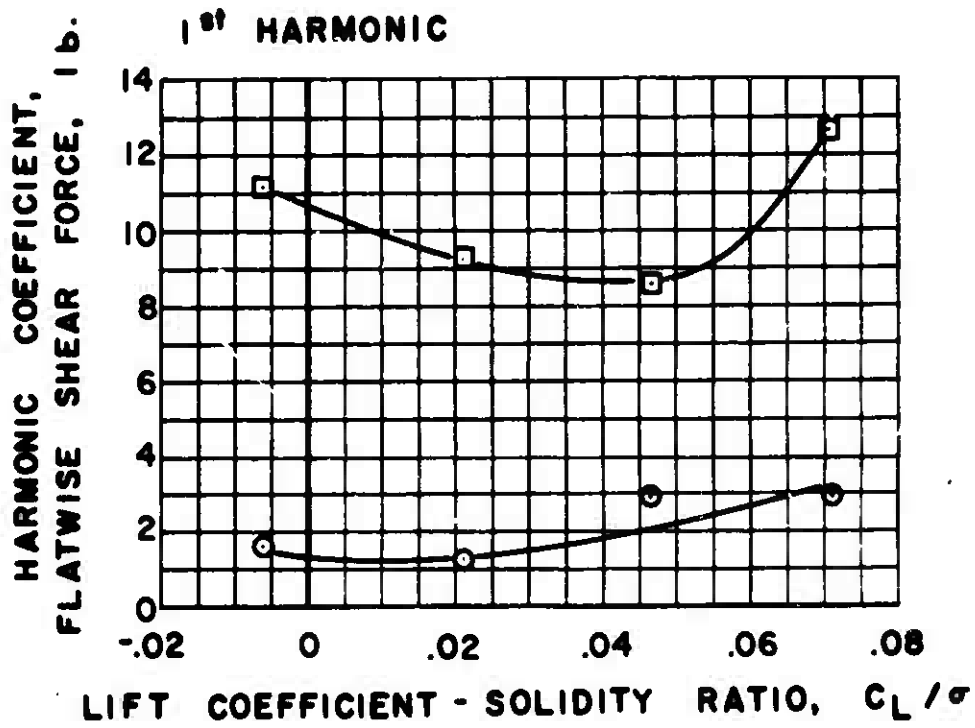
○ SINE COEFFICIENTS
□ COSINE COEFFICIENTS



$$\alpha_s = -4 \text{ deg.} \quad \mu = 0.2$$

Figure 9(a) Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



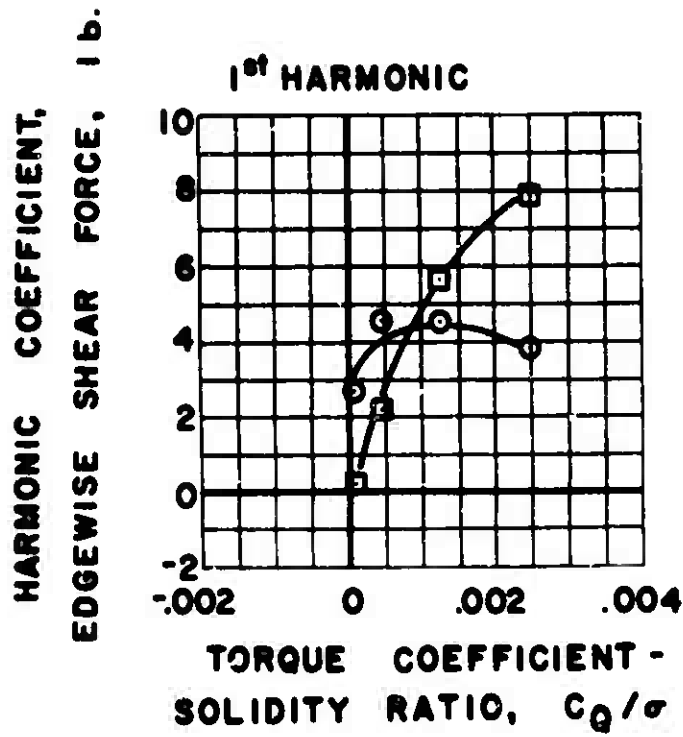
$$\alpha_s = 0 \text{ deg. } \mu = 0.2$$

-4 deg. FIRST HARMONIC LONGITUDINAL FLAPPING

(b) OUT-OF-TRIM

Figure 9. Continued.

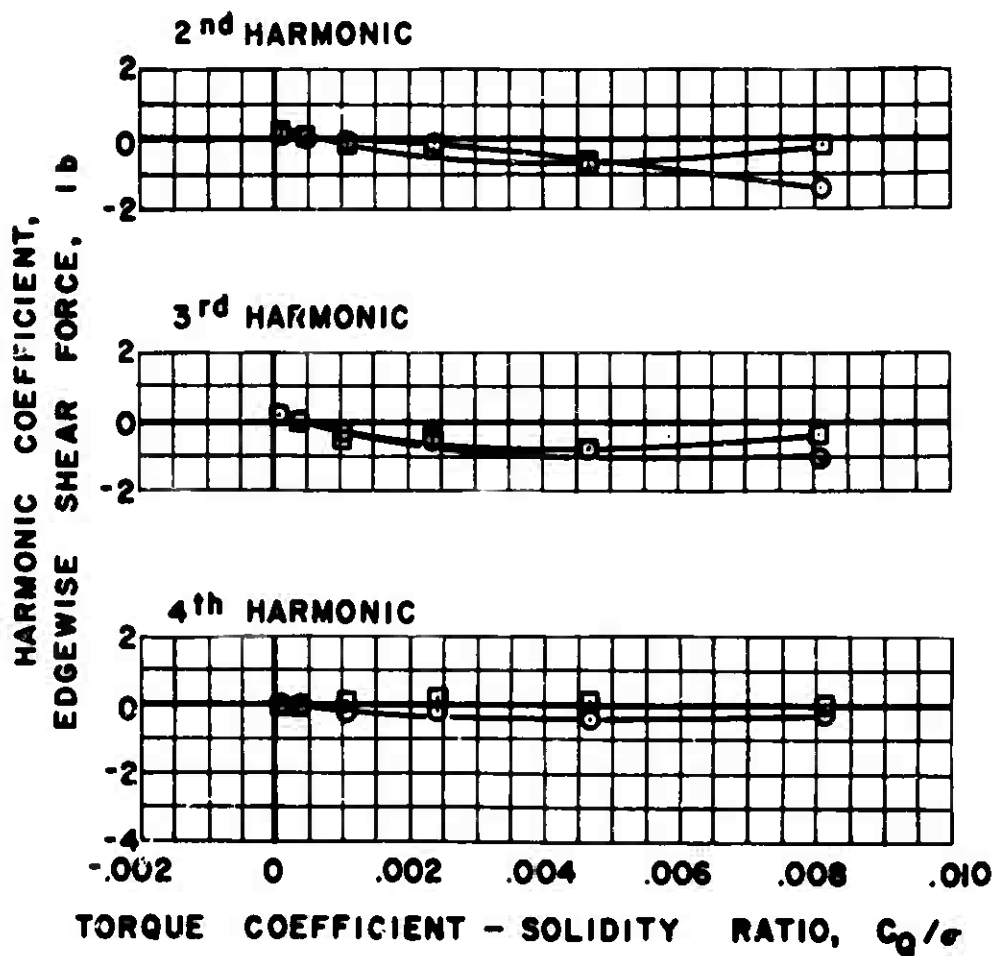
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\alpha_s = 0 \text{ deg.} \quad \mu = 0.2$

Figure 9(b) Concluded.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS

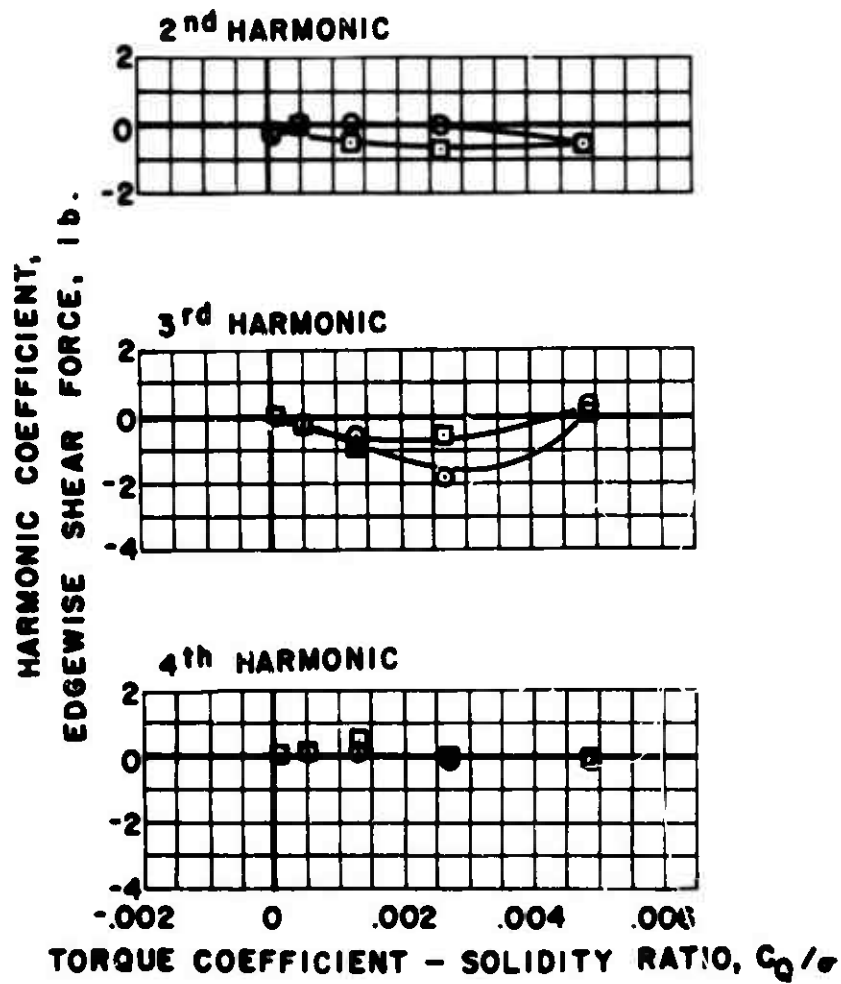


$\alpha_s = -4 \text{ deg. } \mu = 0.2$

(a) FULL LAG DAMPING

Figure 10. Effect of Lag Damping on Shear Forces.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\alpha_s = -4 \text{ deg.} \quad \mu = 0.2$

(b) ZERO LAG DAMPING

Figure 10. Concluded.

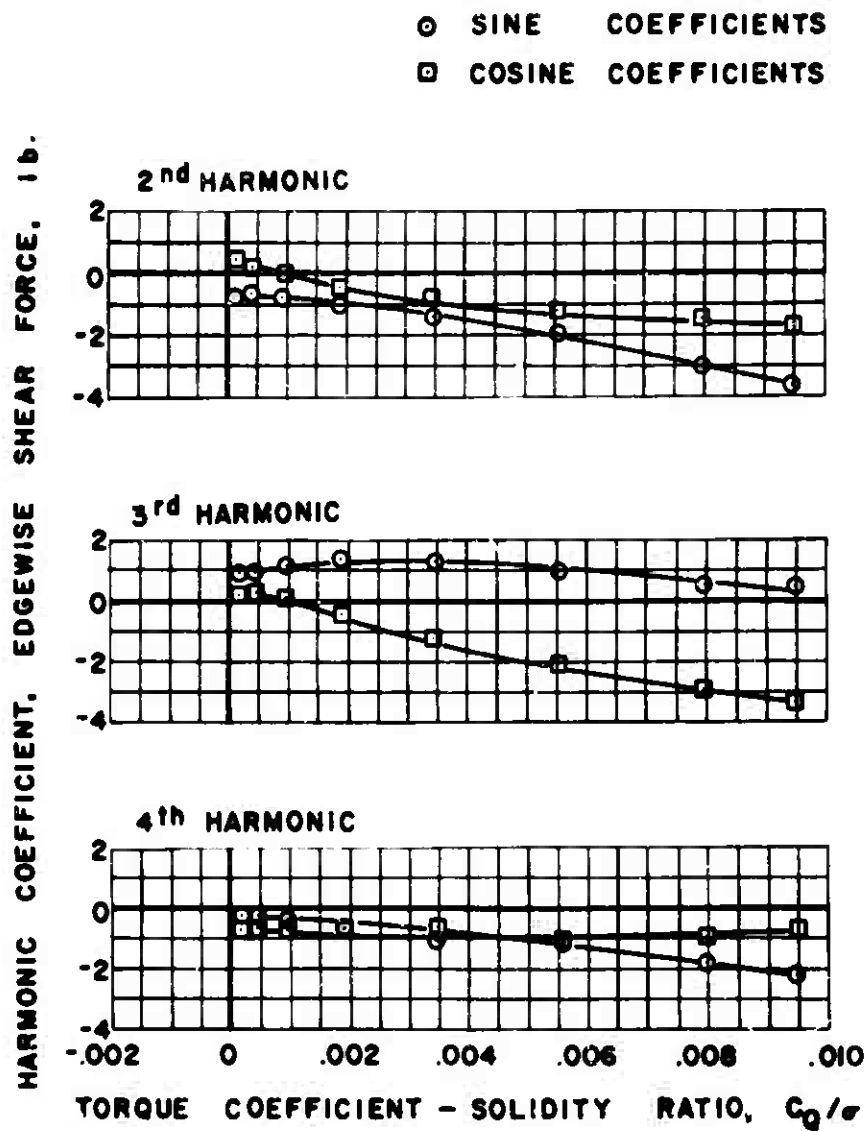
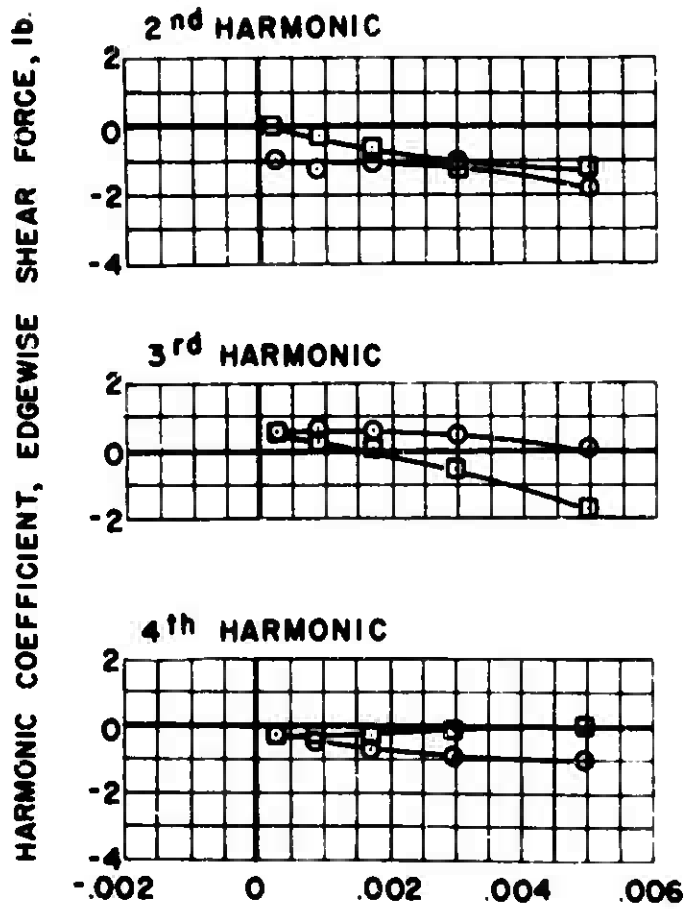


Figure 11. Effect of Lag Damping on Shear Forces.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS

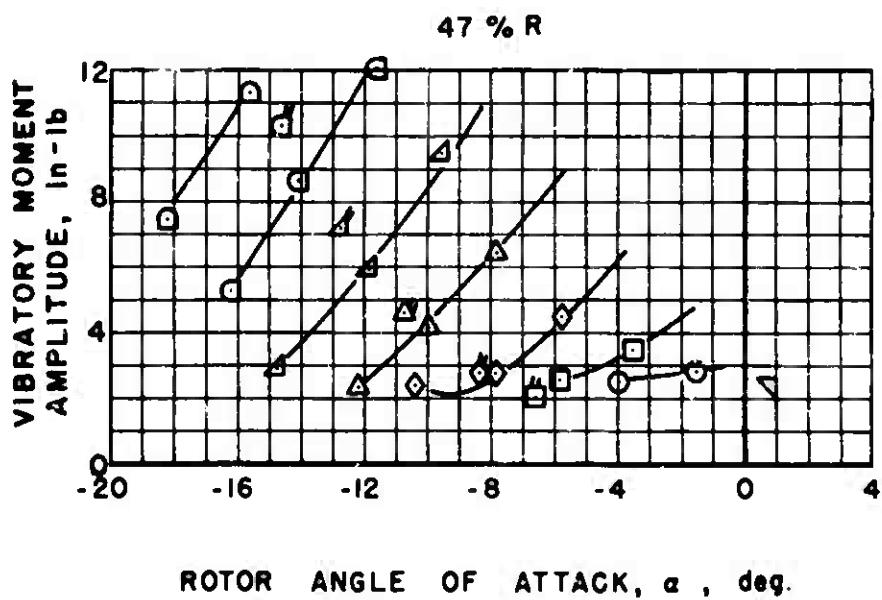
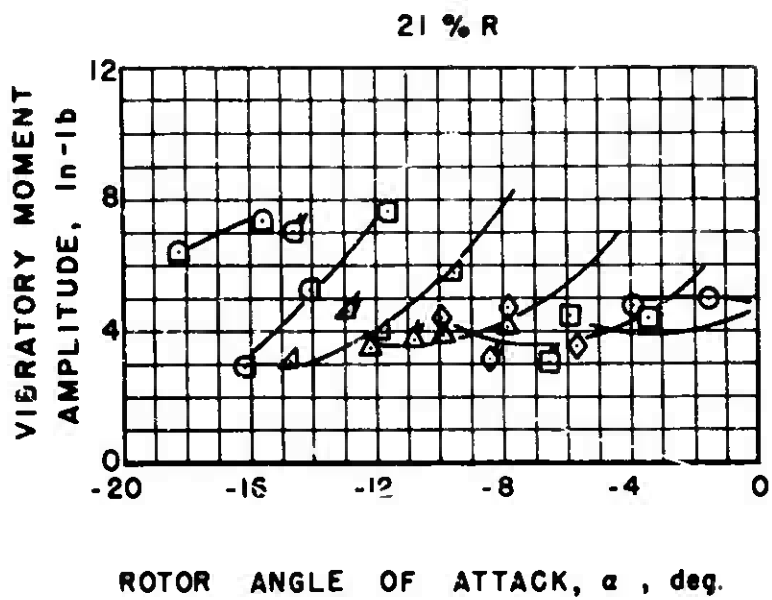


TORQUE COEFFICIENT - SOLIDITY RATIO, C_Q/σ

$$\alpha_s = -4 \text{ deg. } \mu = 0.5$$

(b) ZERO LAG DAMPING

Figure 11. Concluded.



(b) $\mu = 0.5$

Figure 12. Continued.

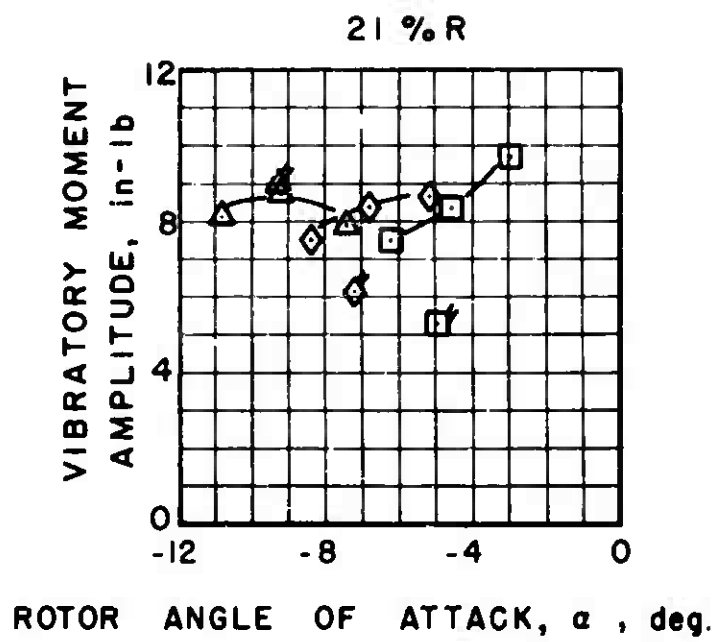
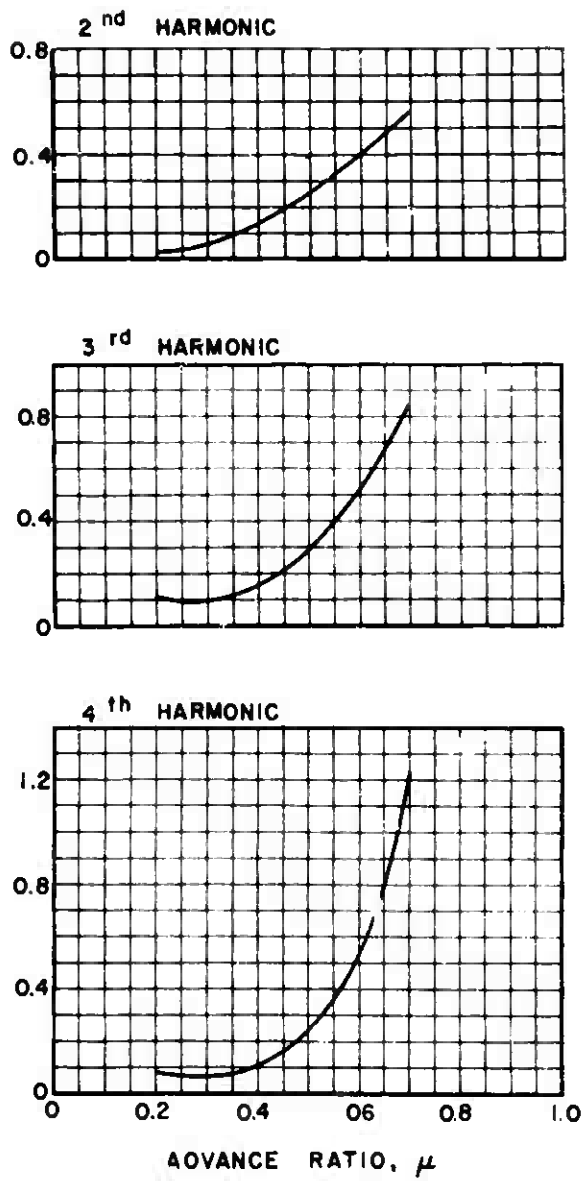


Figure 12. Concluded.

FLATWISE SHEAR FORCE HARMONIC AMPLITUDE
LIFT PER BLADE

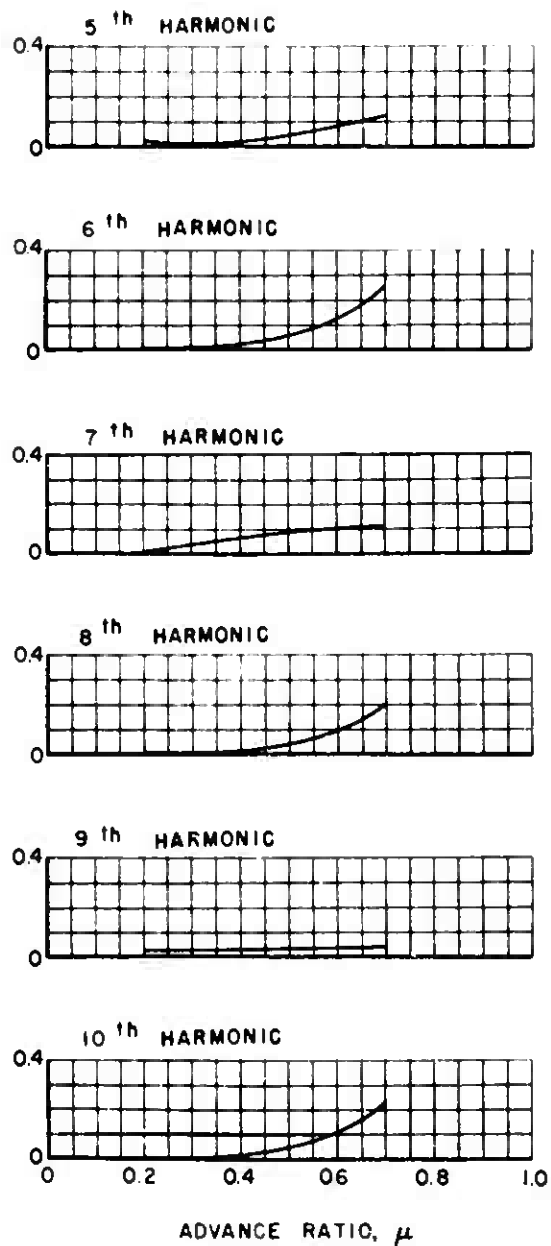


$C_L/\sigma = 0.035$, $\alpha_s = -4 \text{ deg.}$

(a) FLATWISE SHEAR

Figure 13. Effect of Advance Ratio on Nondimensional Shear Forces.

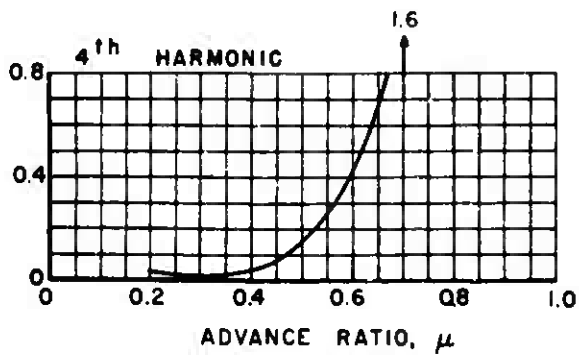
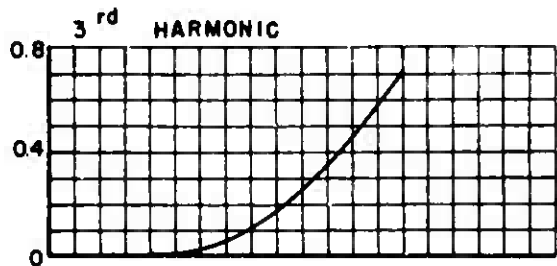
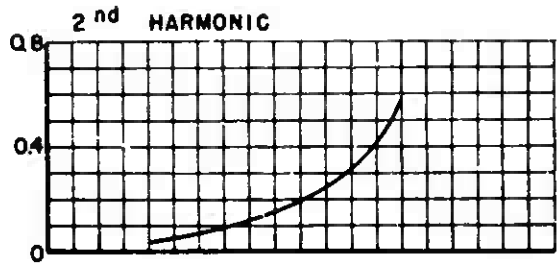
FLATWISE SHEAR FORCE HARMONIC AMPLITUDE
LIFT PER BLADE



$C_L/\sigma = 0.035$, $\alpha_s = -4$ deg.

Figure 13(a). Continued.

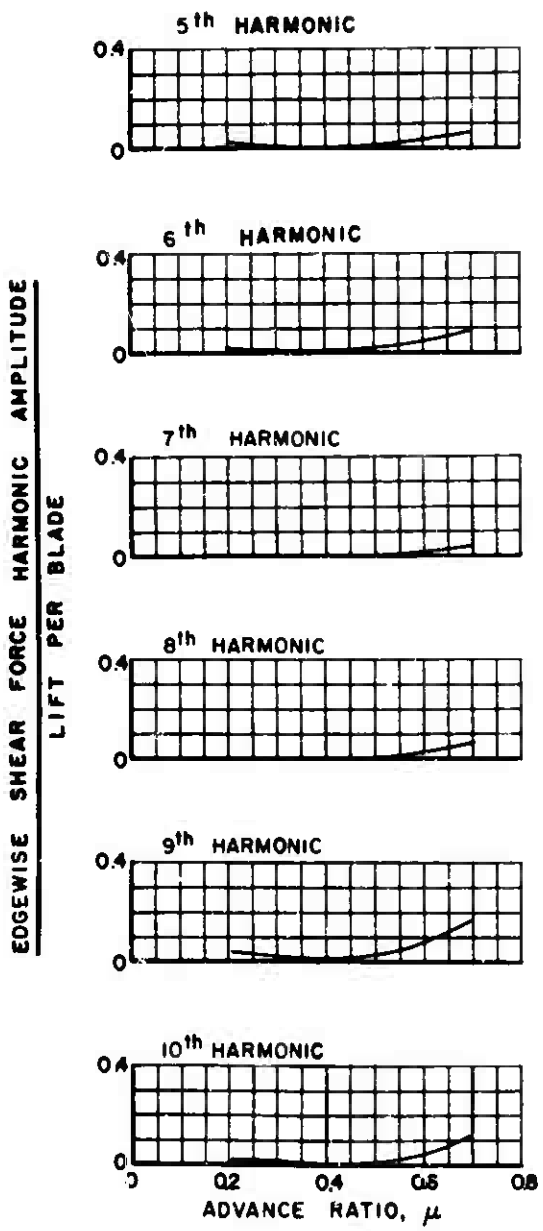
EDGEWISE SHEAR FORCE HARMONIC AMPLITUDE
LIFT PER BLADE



$C_L/\sigma = 0.035$, $\alpha_s = -4$ deg.

(b) EDGEWISE SHEAR

Figure 13. Continued.



$C_L/\sigma = 0.035$, $\alpha_s = -4$ deg.

Figure 13(b). Concluded.

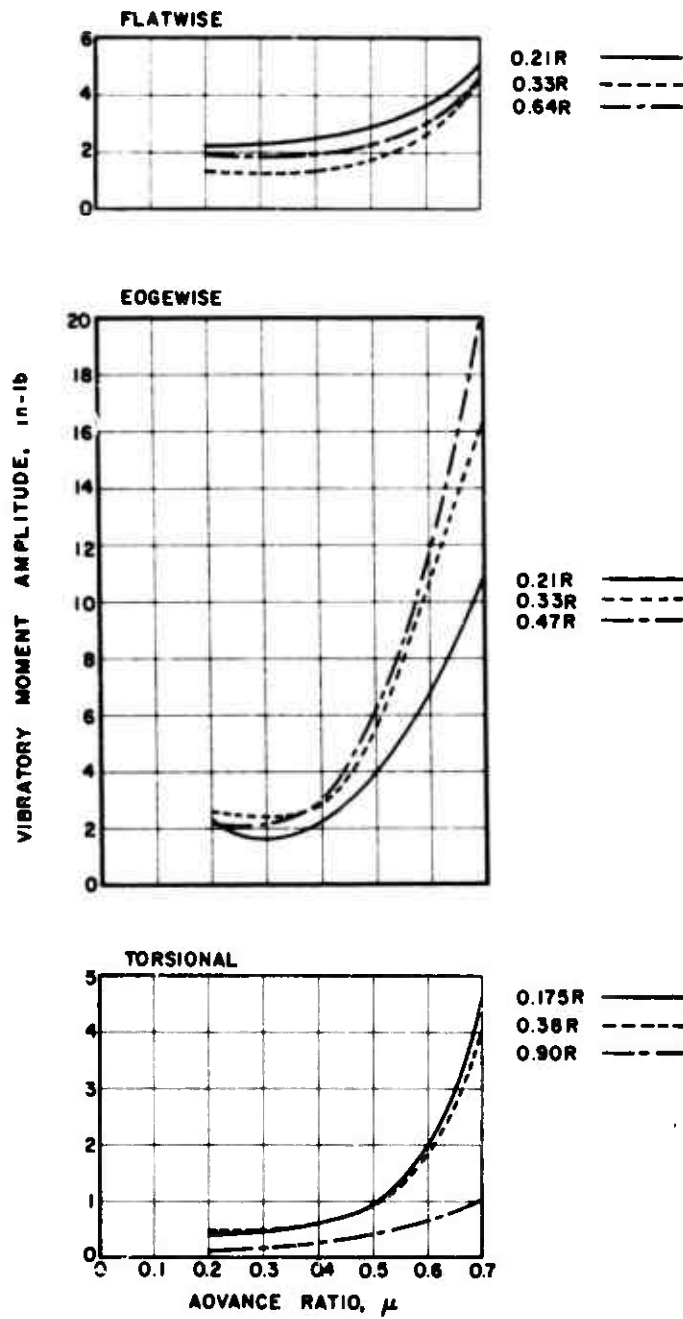


Figure 14. Effect of Advance Ratio on Rotor Blade Vibratory Moments.

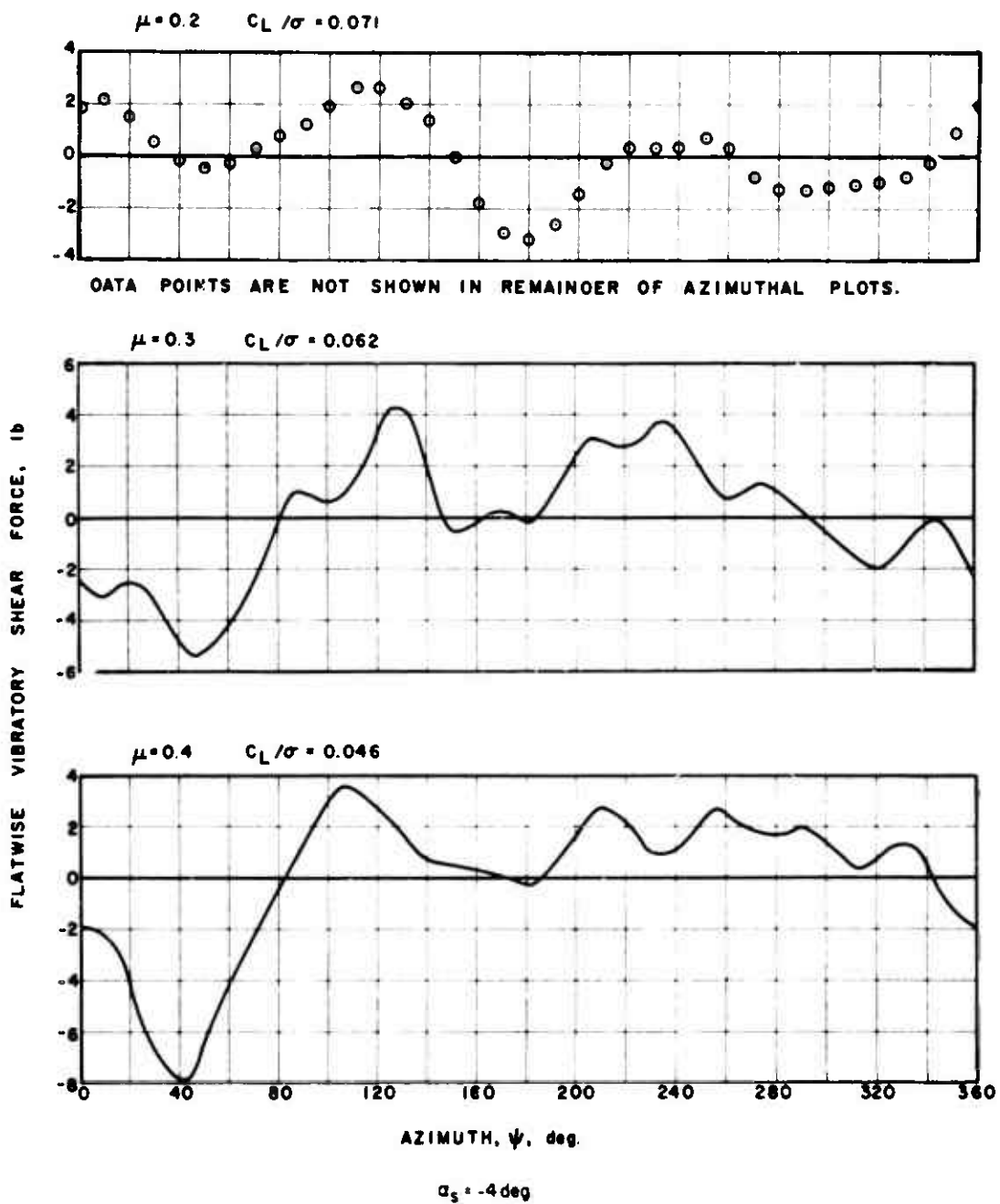


Figure 15. Experimental Flatwise Vibratory Shear Force.

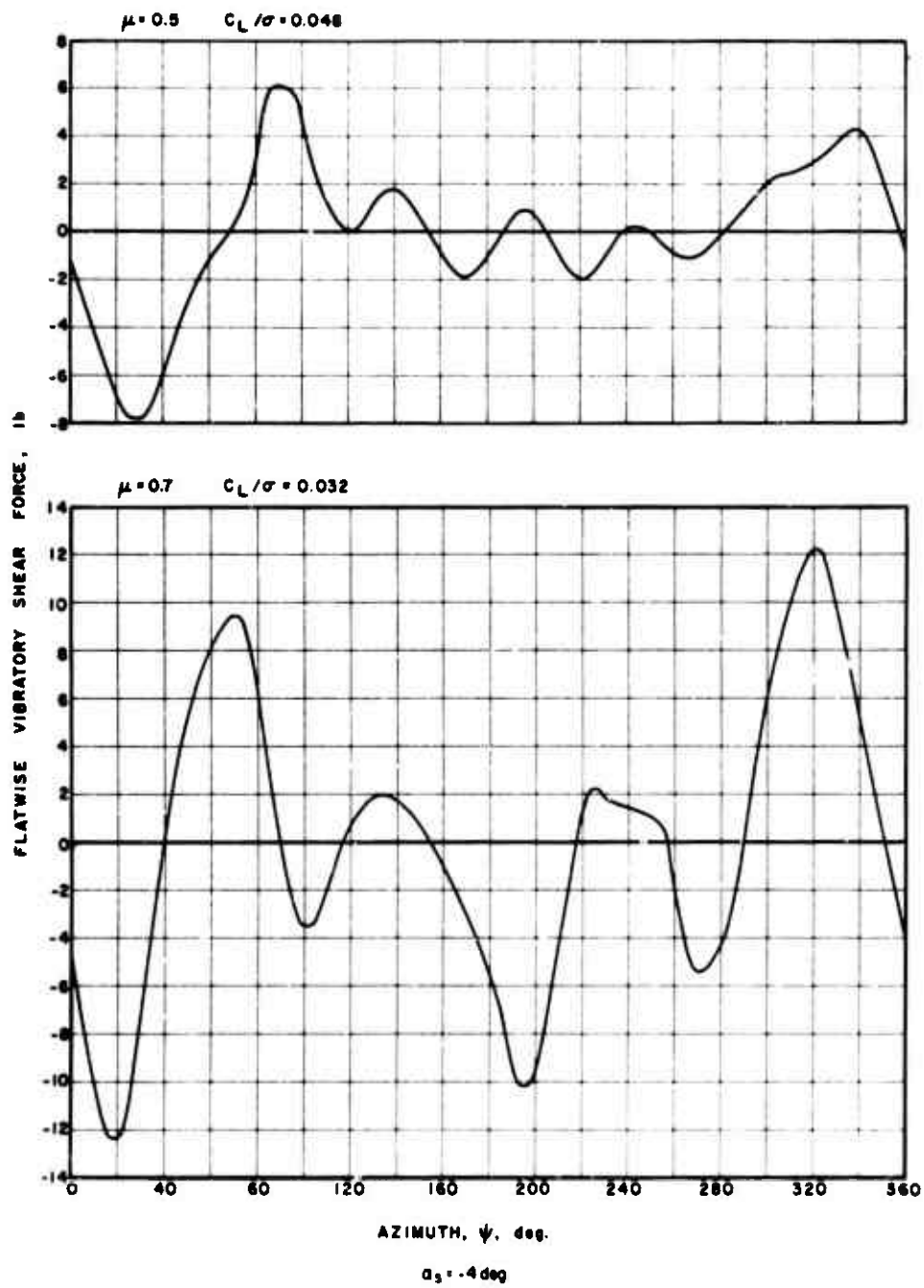


Figure 15. Concluded.

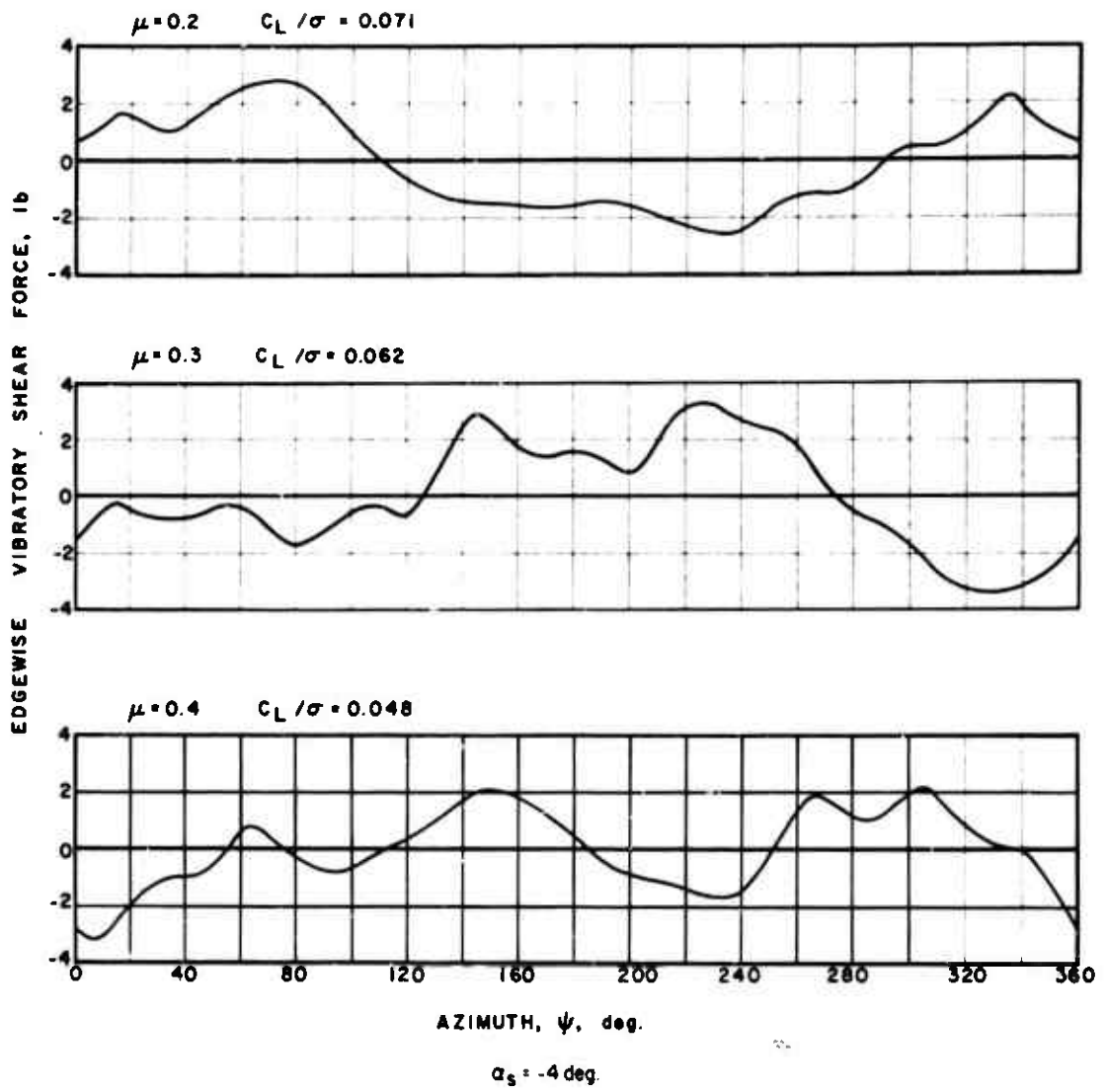


Figure 16. Experimental Edgewise Vibratory Shear Force.

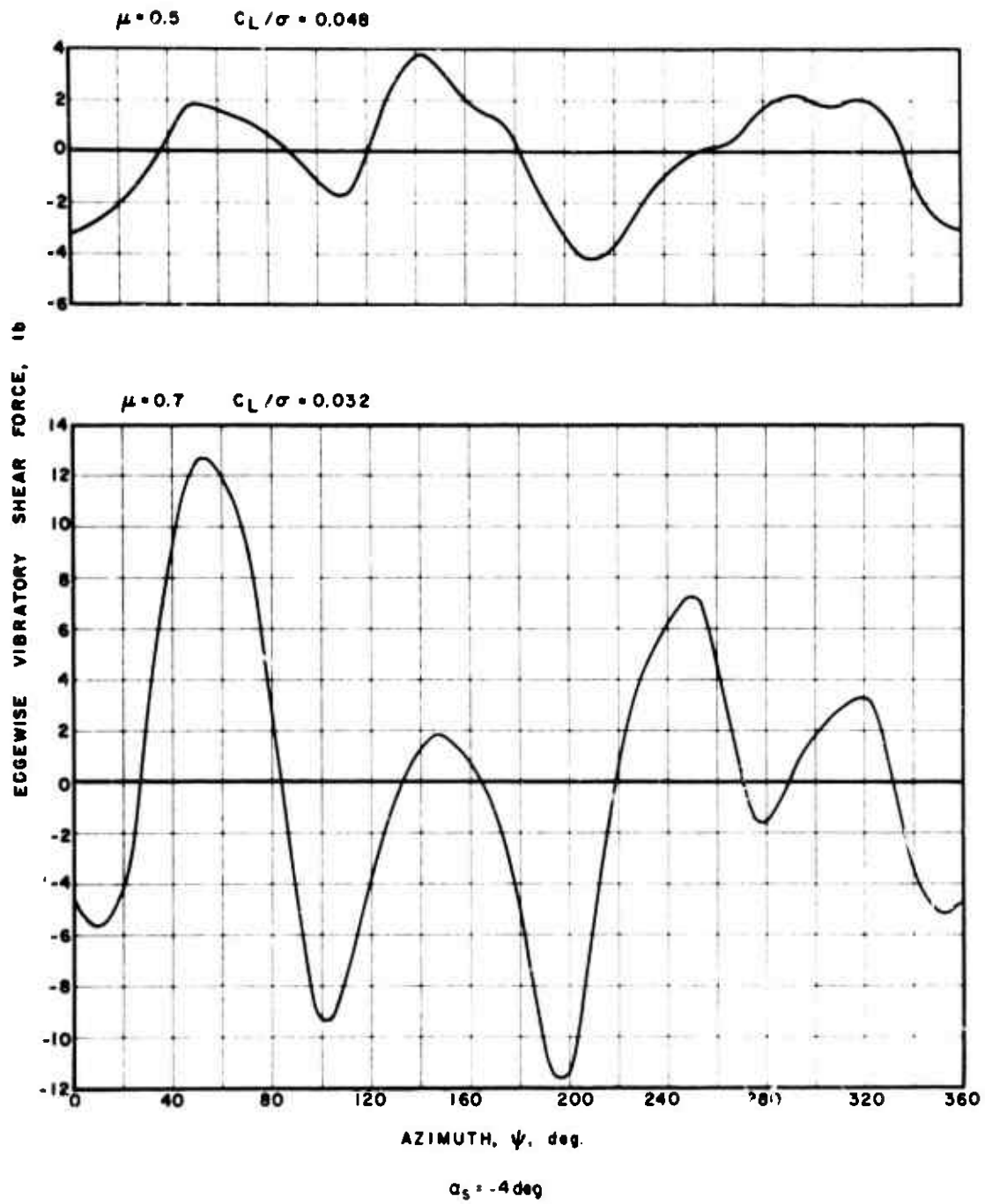


Figure 16. Concluded.

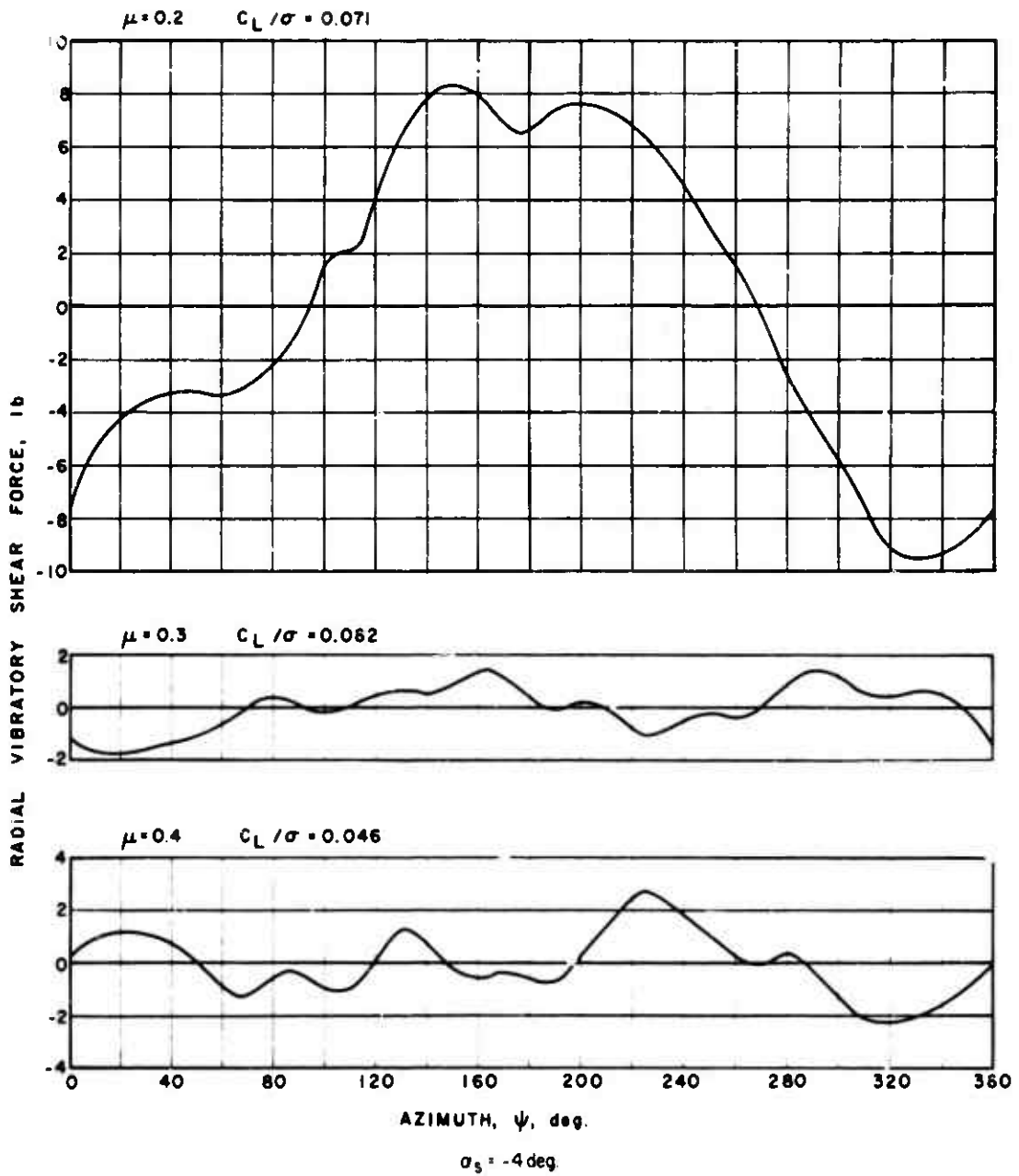


Figure 17. Experimental Radial Vibratory Shear Force.

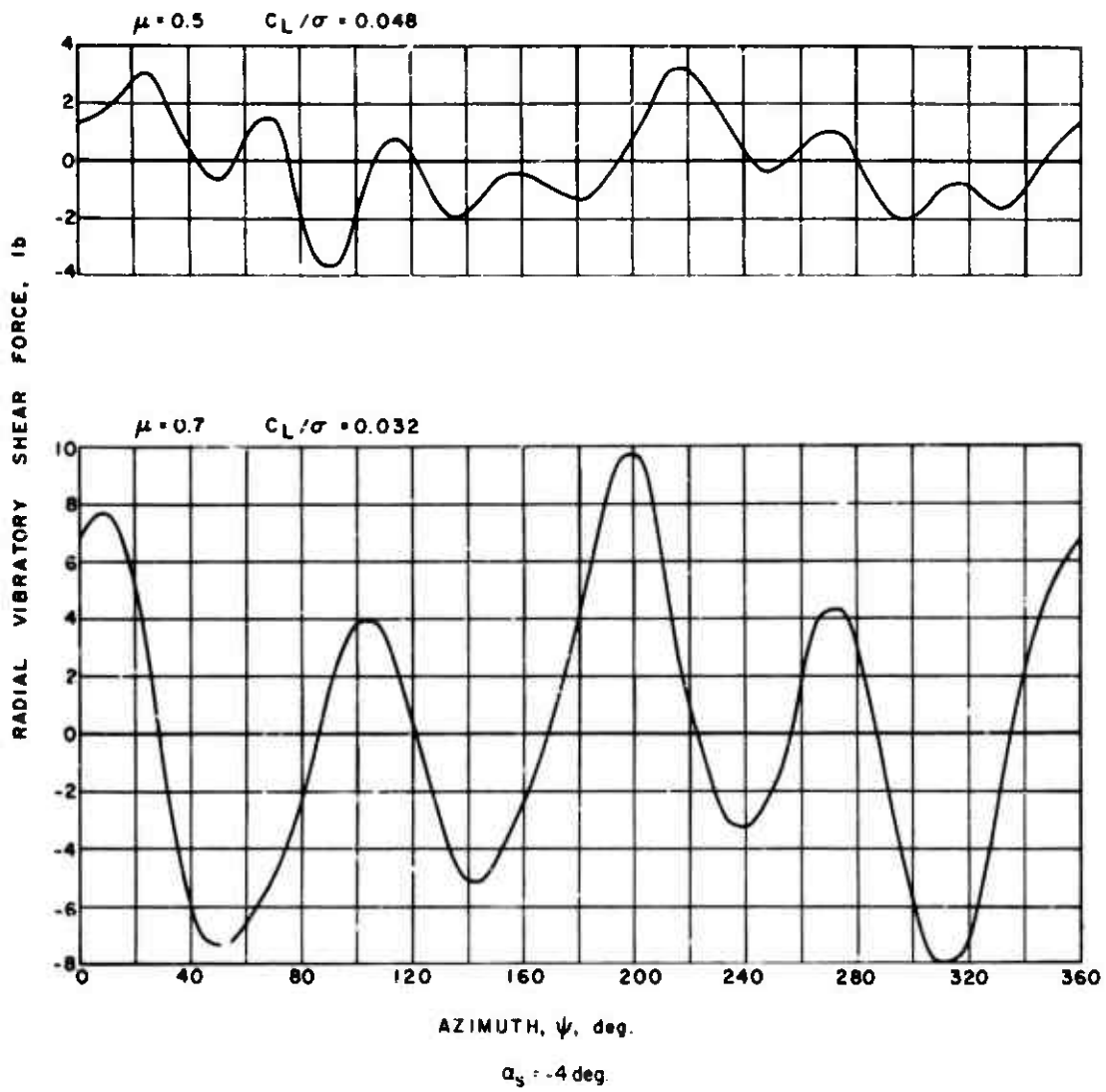
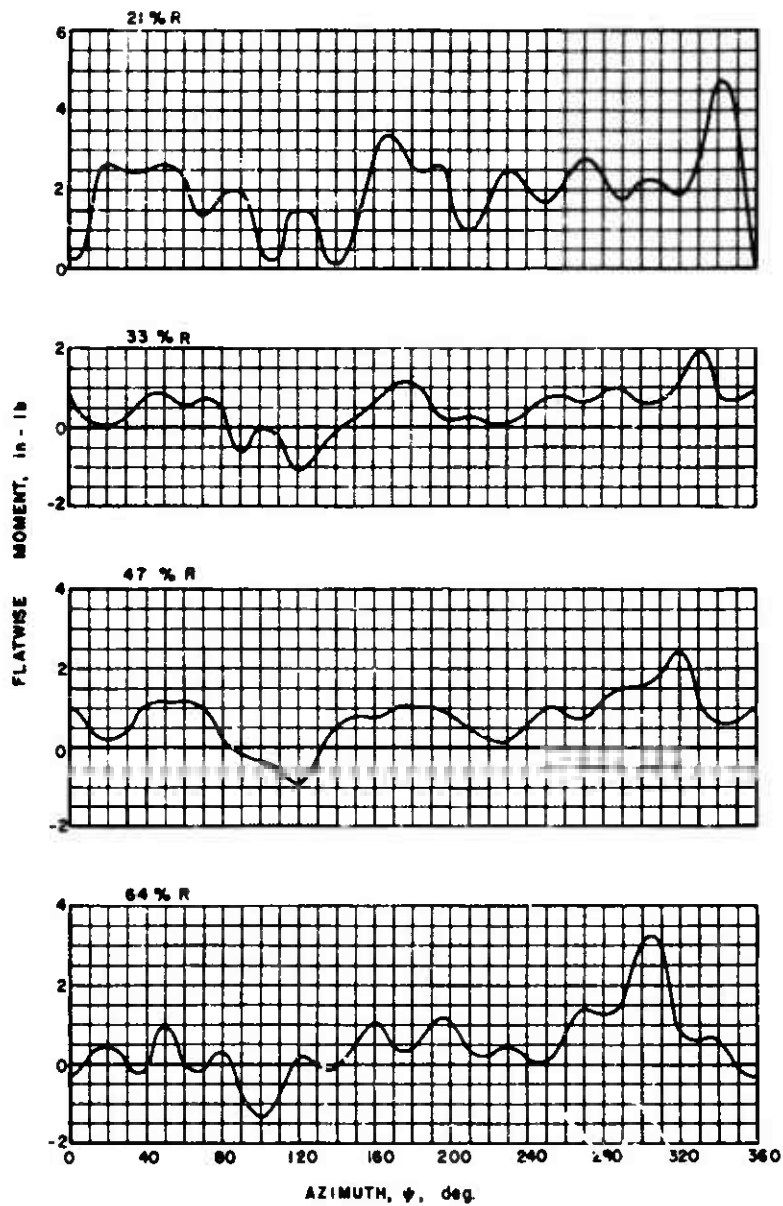


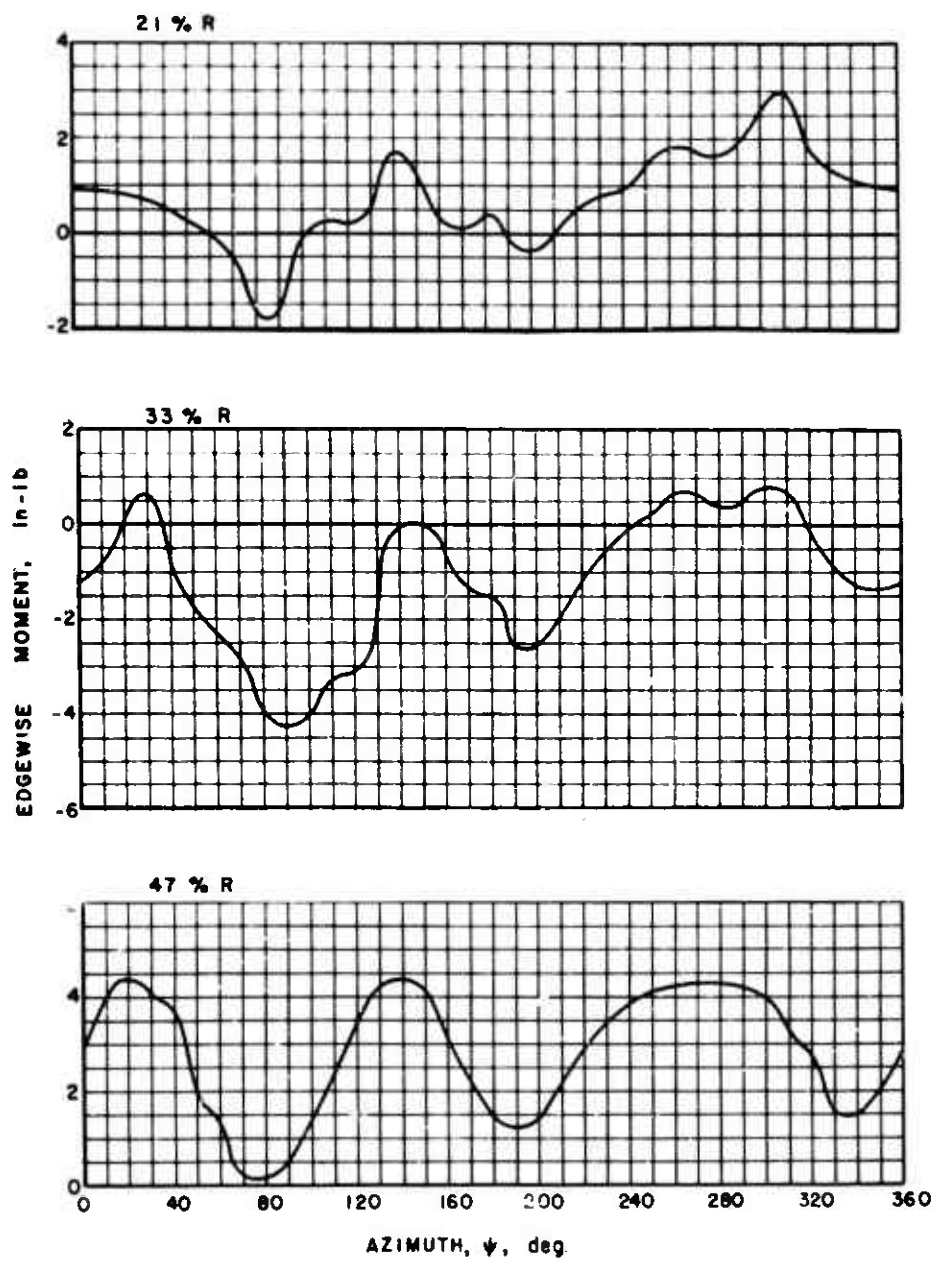
Figure 17. Concluded.



$\mu = 0.02$ $C_L / \sigma = 0.071$ $\alpha_g = -4 \text{ deg.}$

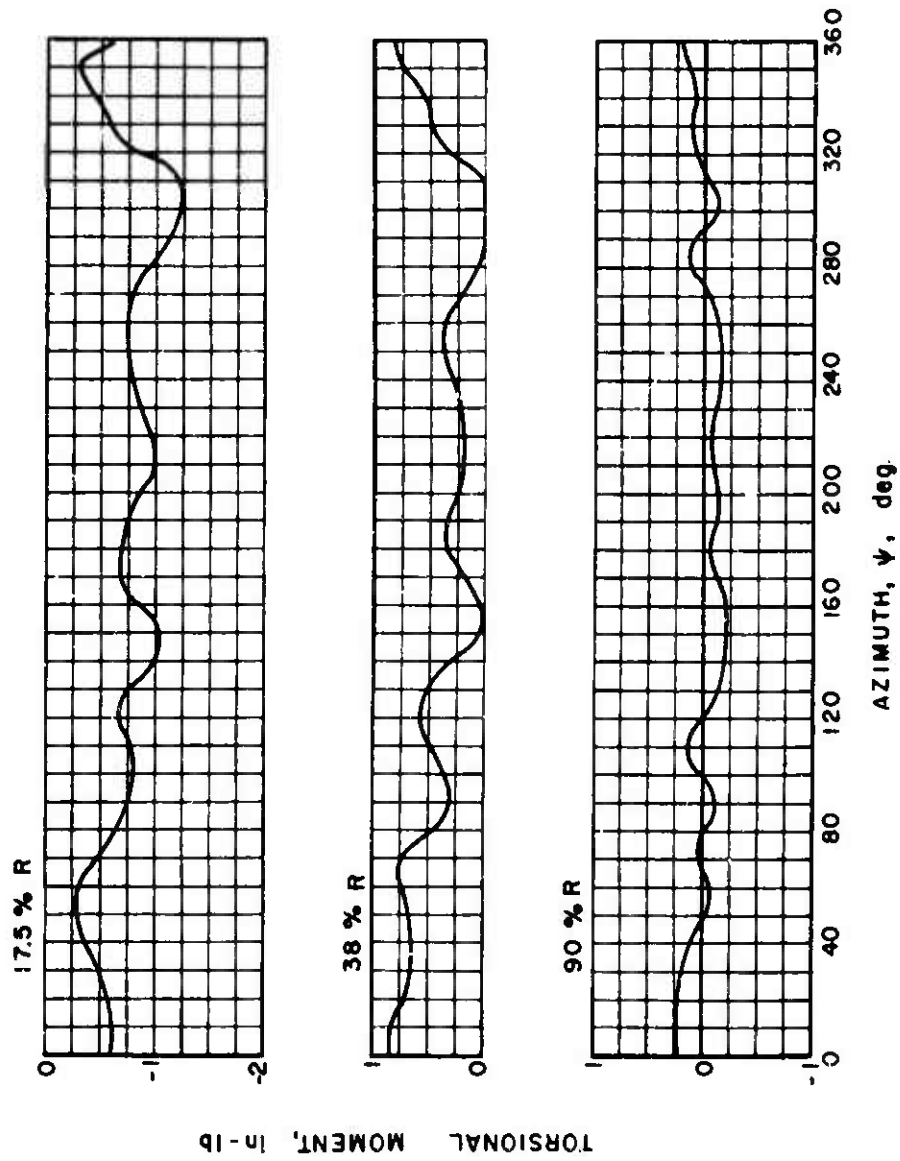
(a) FLATWISE MOMENTS

Figure 18. Experimental Blade Moments.



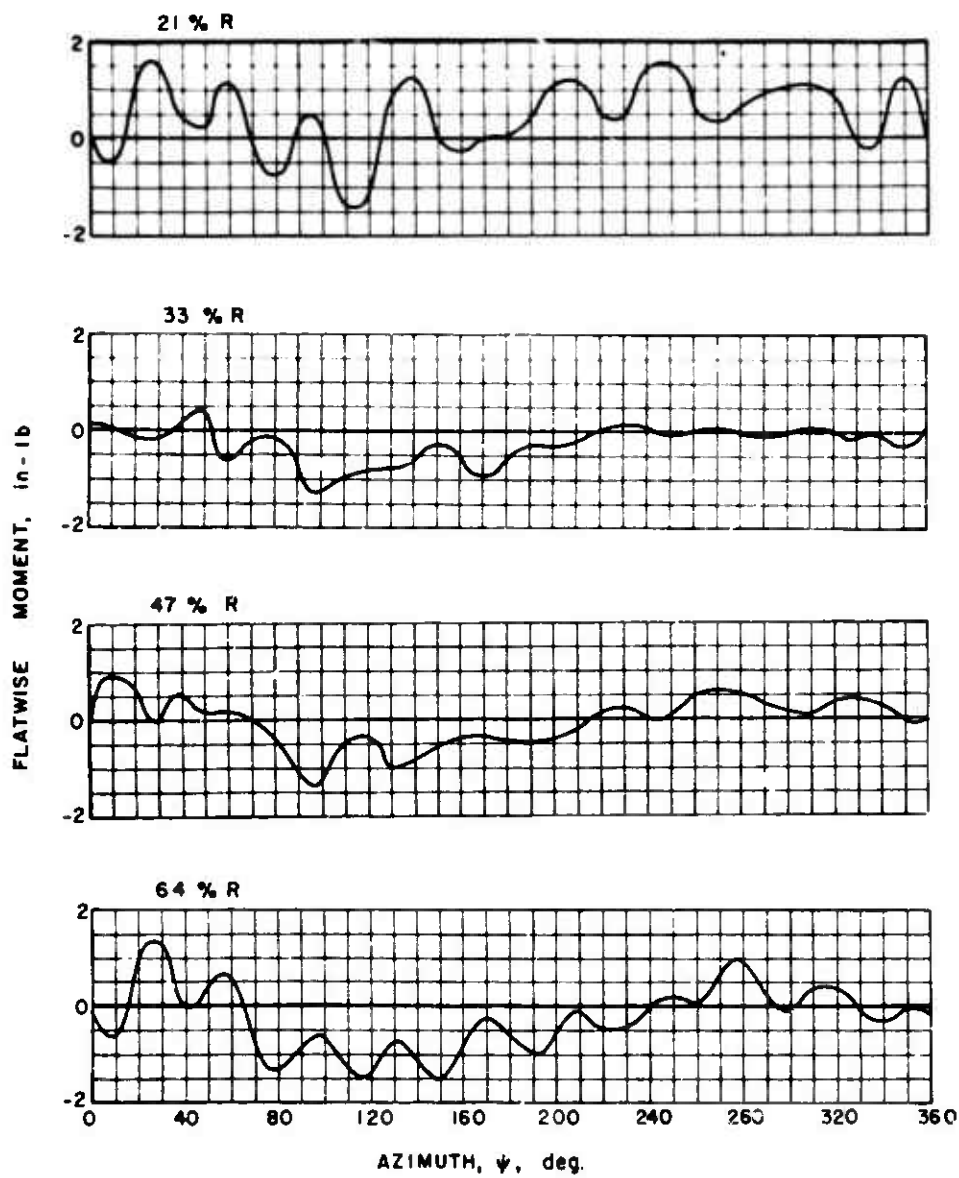
(b) EDGEWISE MOMENTS

Figure 18. Continued.



(c) TORSIONAL MOMENTS

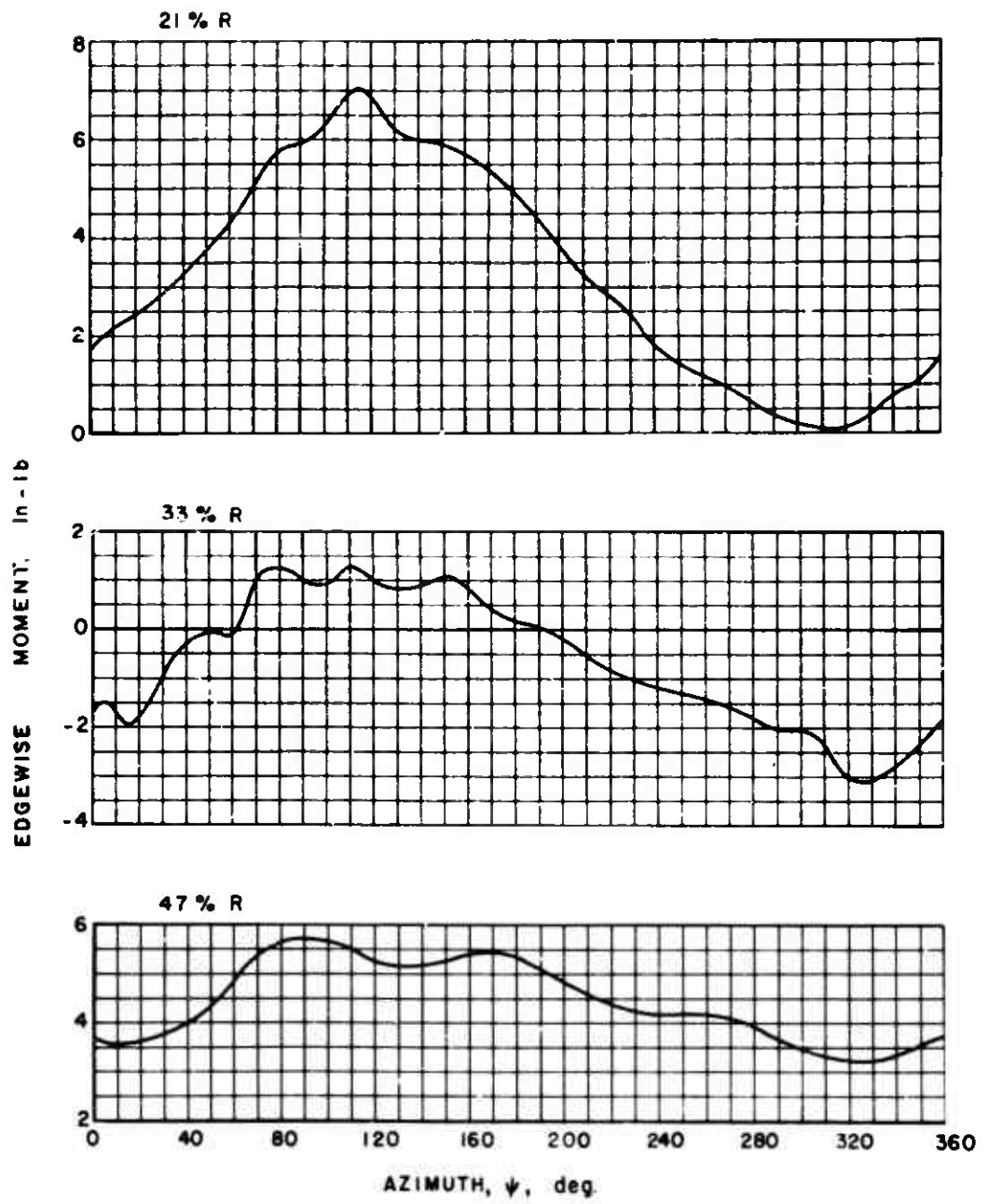
Figure 18. Concluded.



$$\mu = 0.3 \quad C_L / \sigma = 0.019 \quad \alpha_s = -4 \text{ deg.}$$

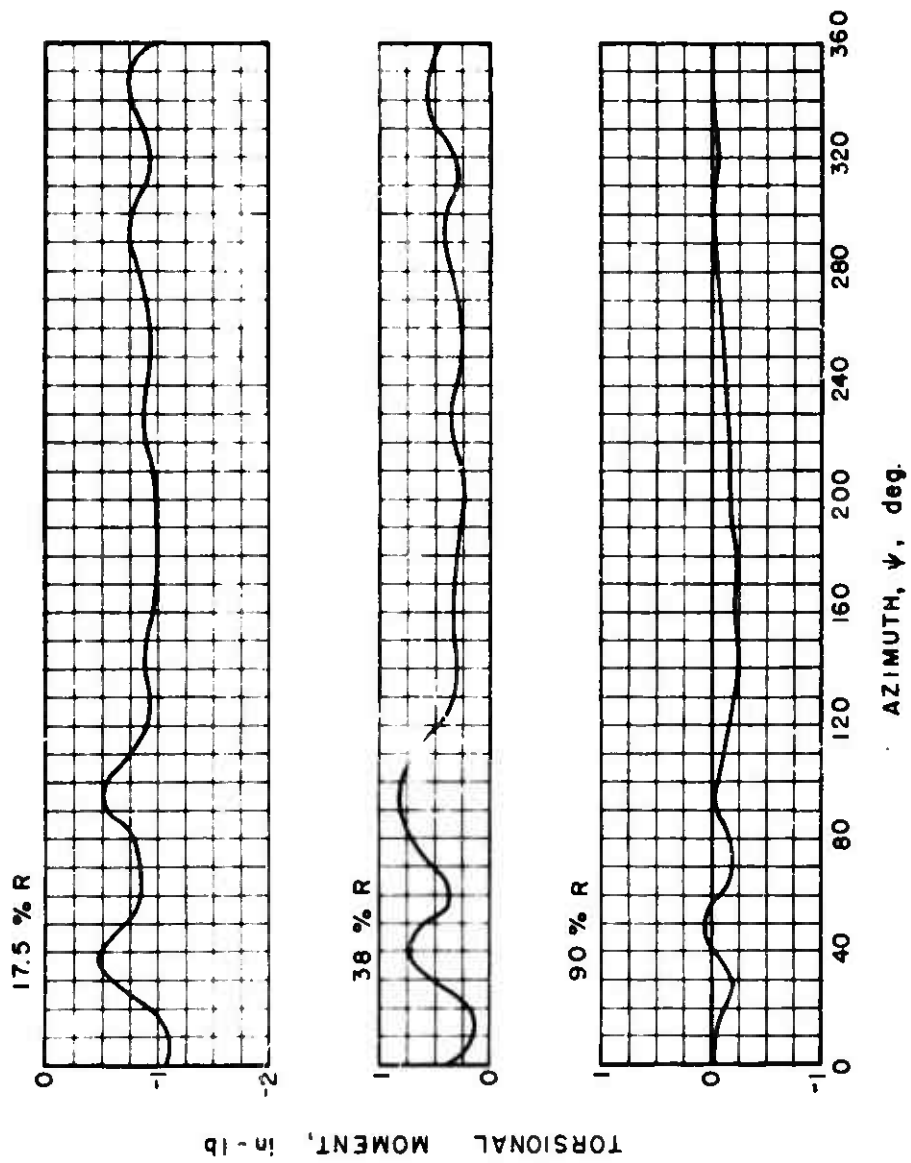
(a) FLATWISE MOMENTS

Figure 19. Experimental Blade Moments.



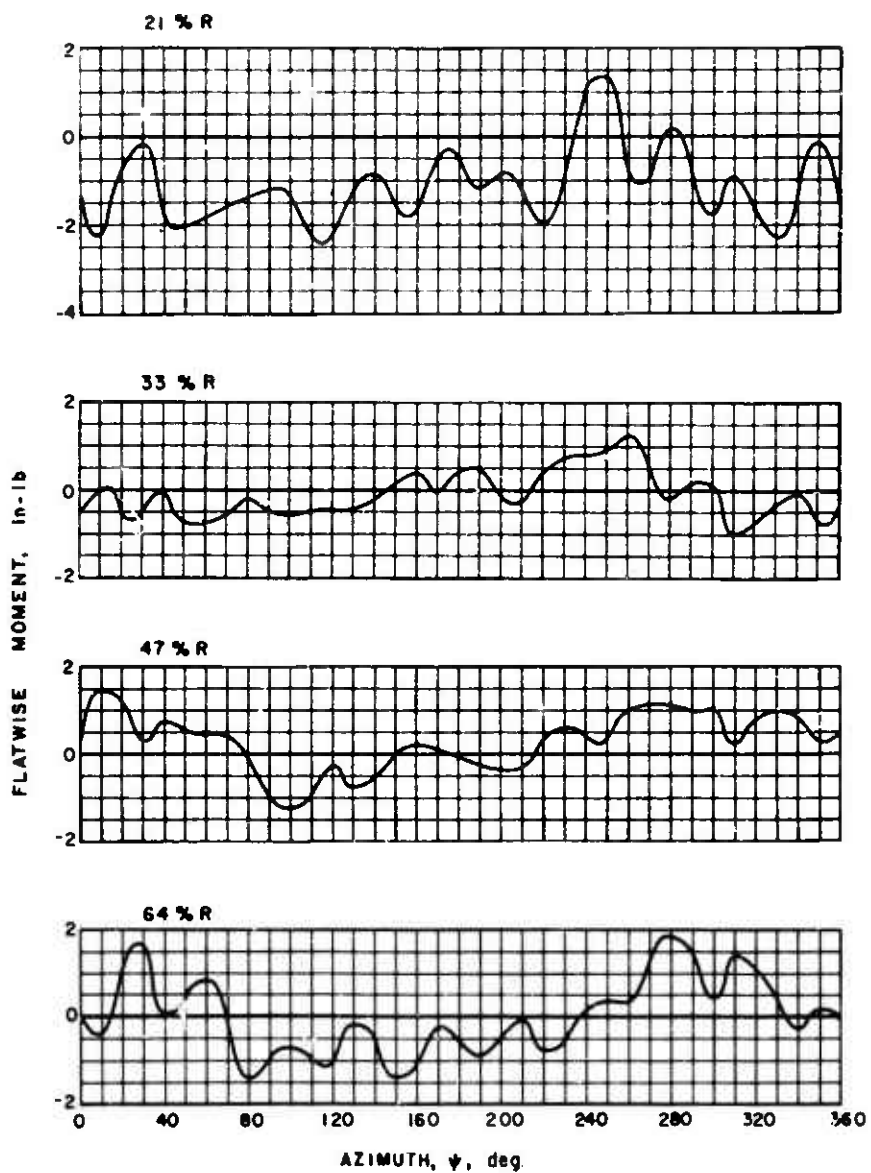
(b) EDGEWISE MOMENTS

Figure 19. Continued.



(c) TORSIONAL MOMENTS

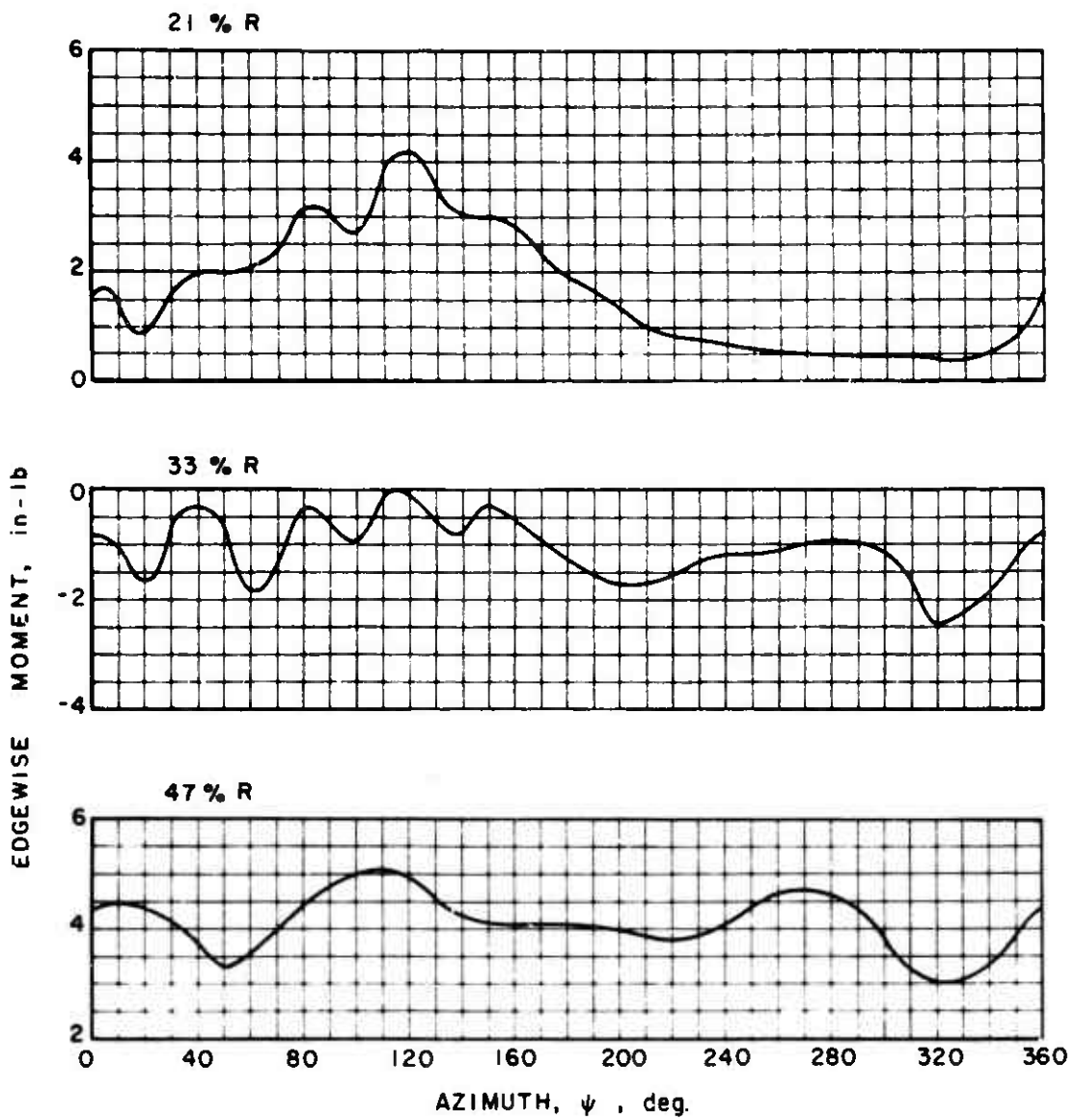
Figure 19. Concluded.



$$\mu = 0.3 \quad C_L / \sigma = 0.041 \quad \alpha_s = -4 \text{ deg.}$$

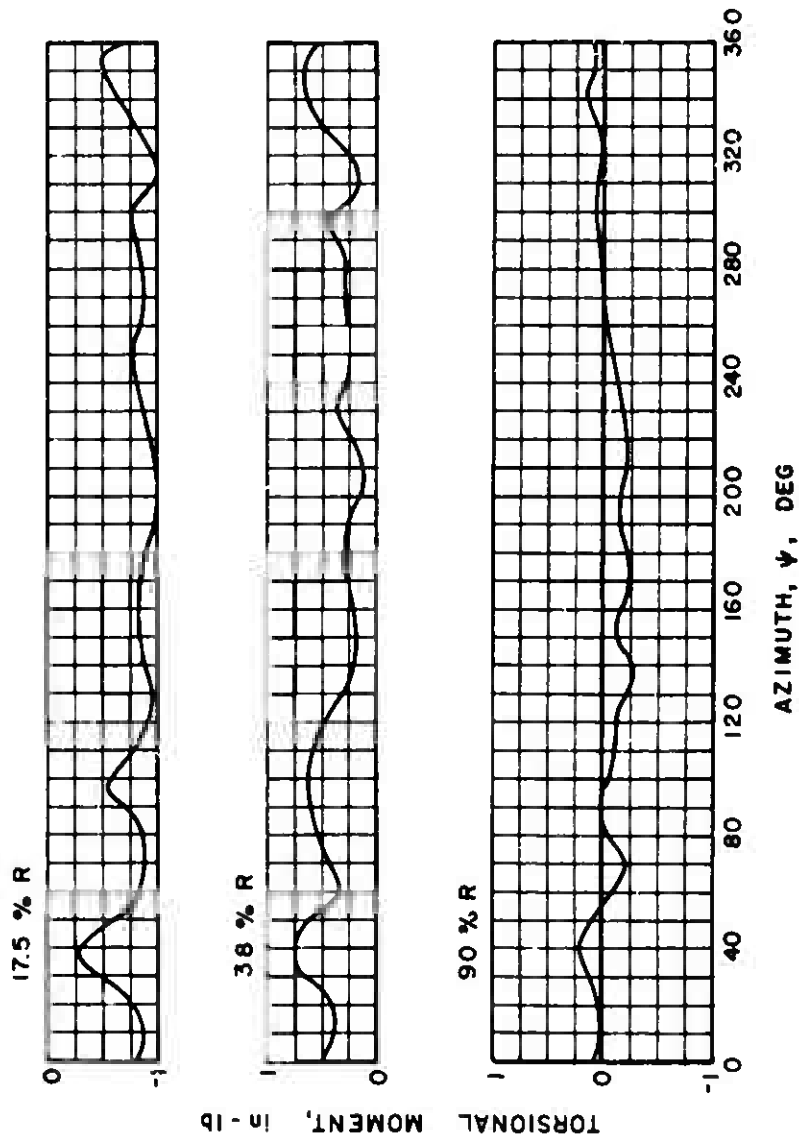
(o) FLATWISE MOMENTS

Figure 20. Experimental Blade Moments.



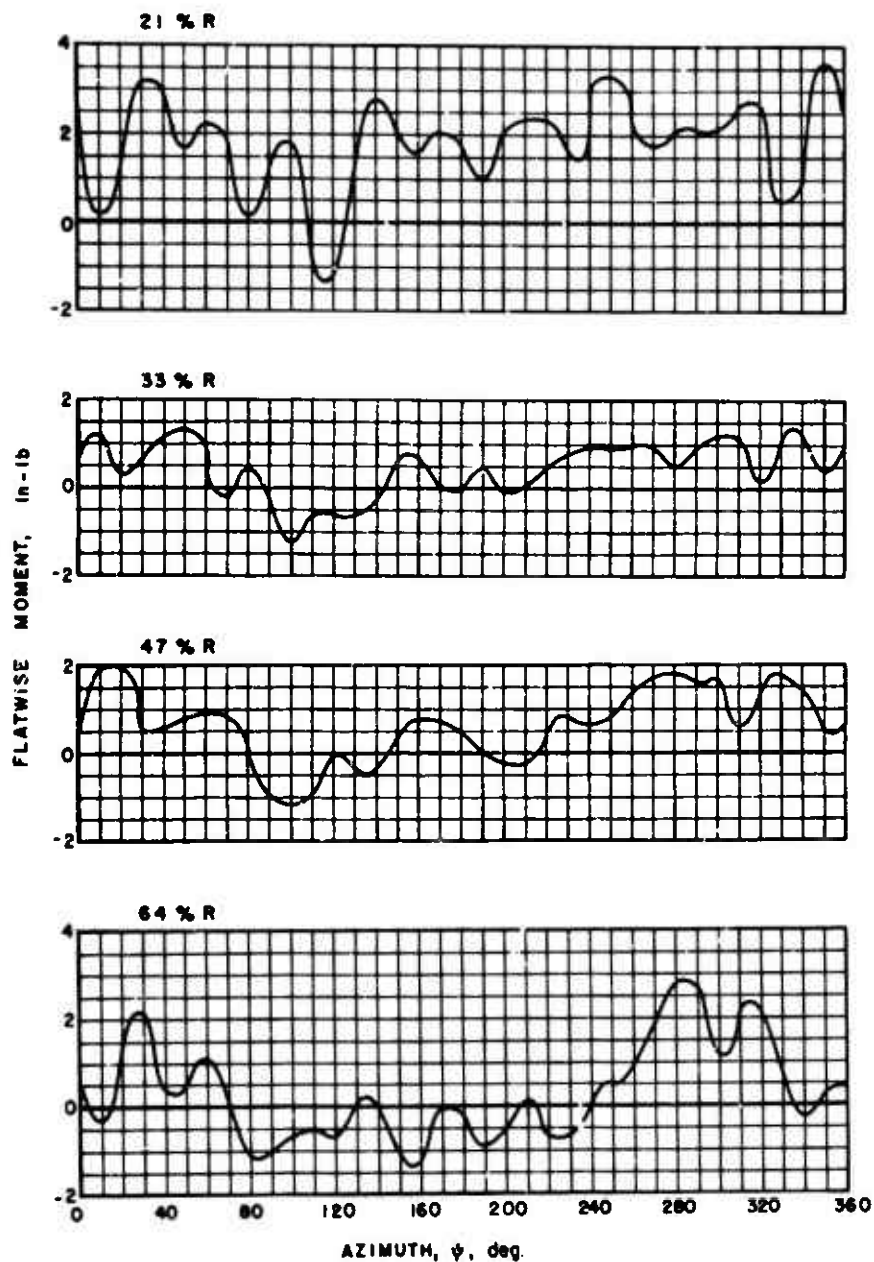
(b) EDGEWISE MOMENTS

Figure 20. Continued.



(c) TORSIONAL MOMENTS

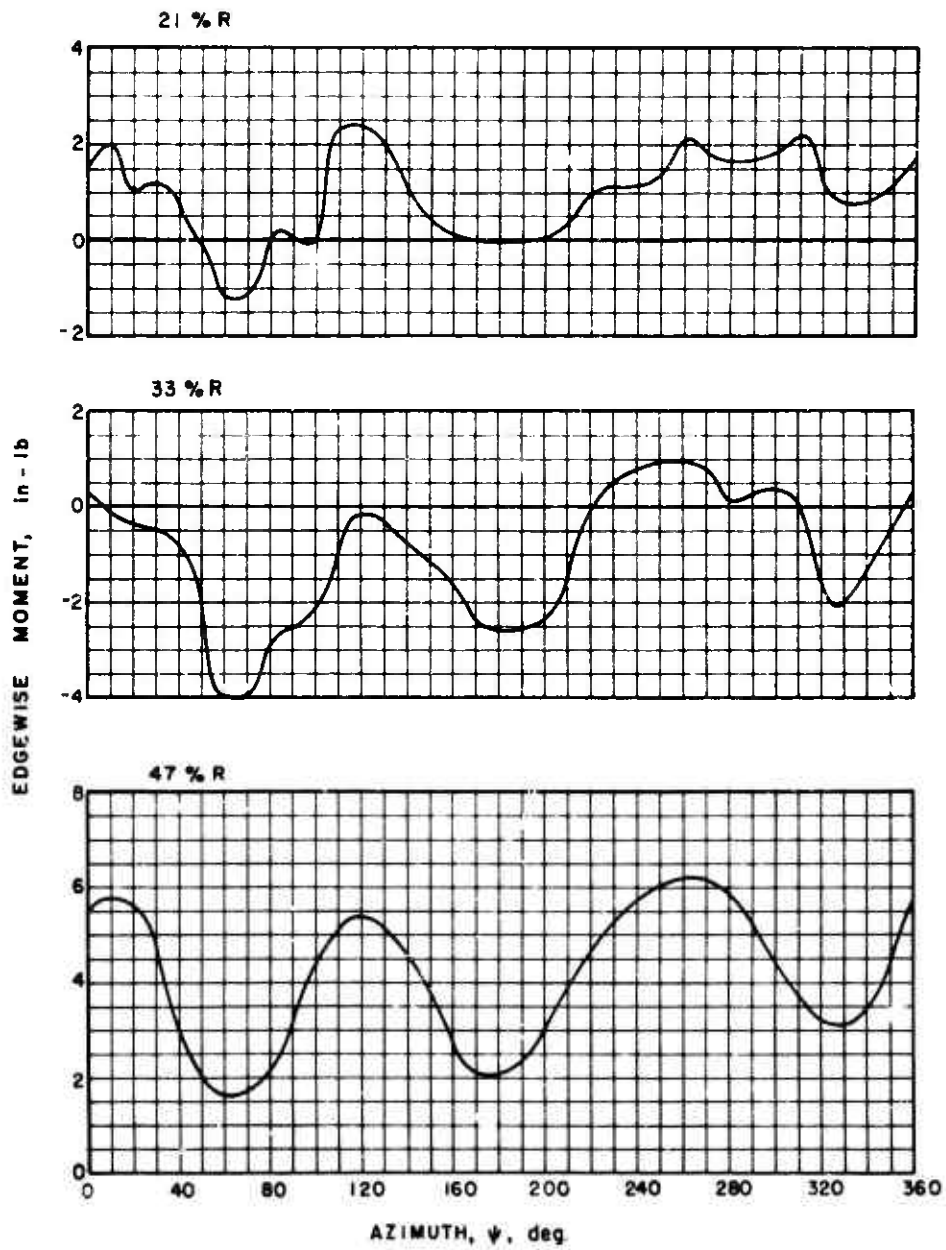
Figure 20. Concluded.



$\mu = 0.3$ $C_L / \sigma = 0.062$ $\alpha_s = -4 \text{ deg.}$

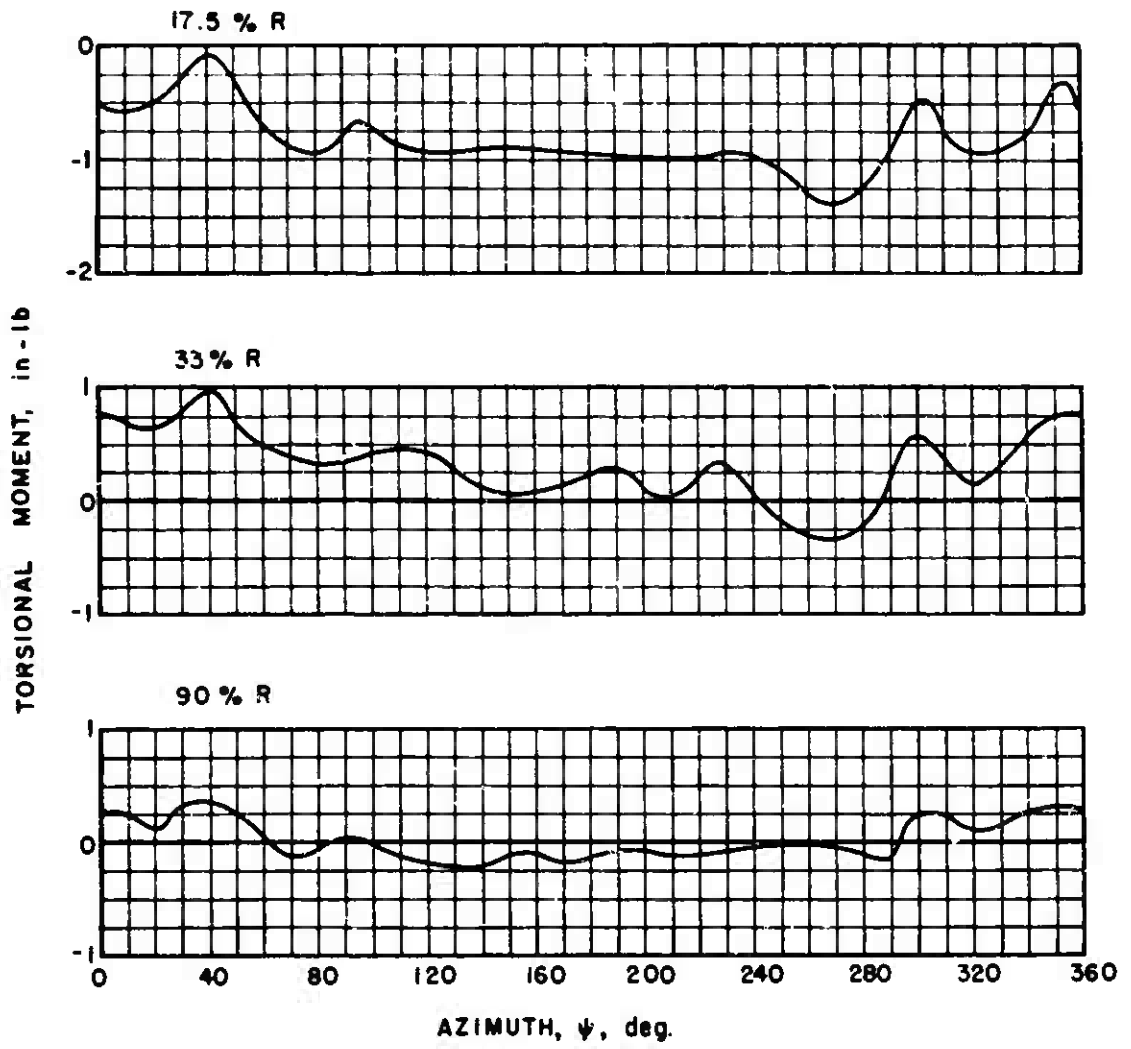
(a) FLATWISE MOMENTS

Figure 21. Experimental Blade Moments.



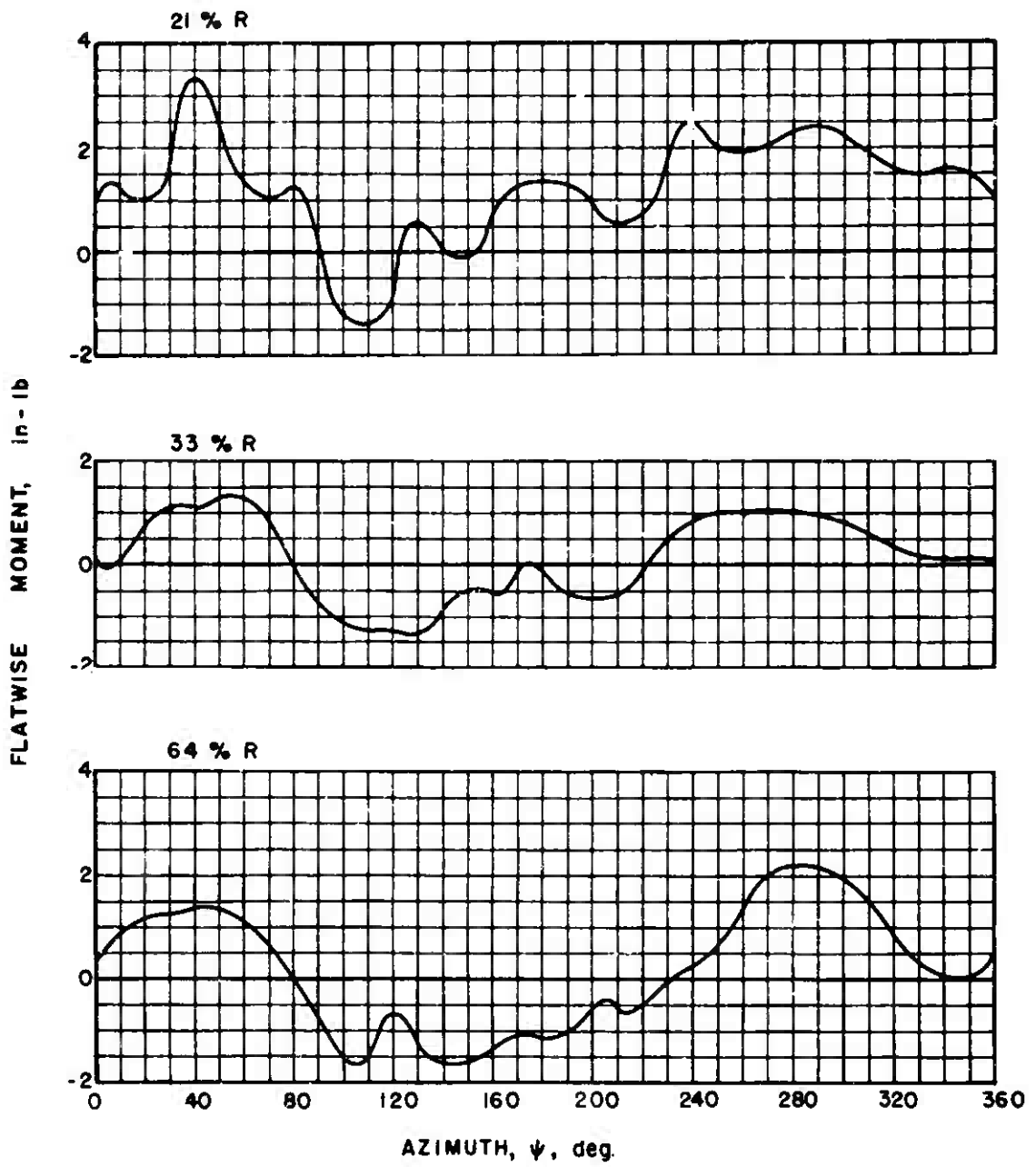
(b) EDGEWISE MOMENTS

Figure 21. Continued.



(c) TORSIONAL MOMENTS

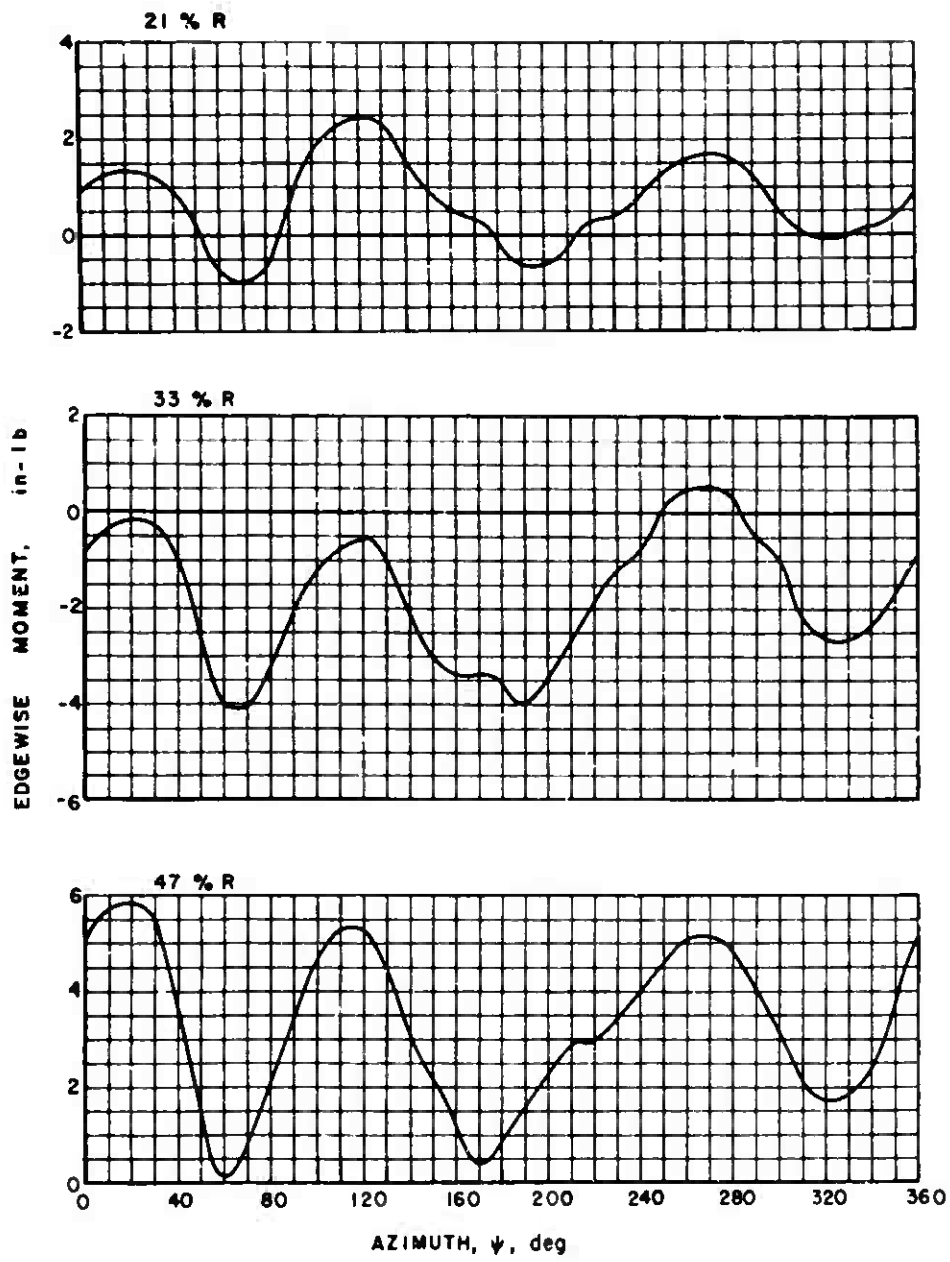
Figure 21. Concluded.



$$\mu = 0.4 \quad C_L / \sigma = 0.046 \quad \alpha_s = -4 \text{ deg.}$$

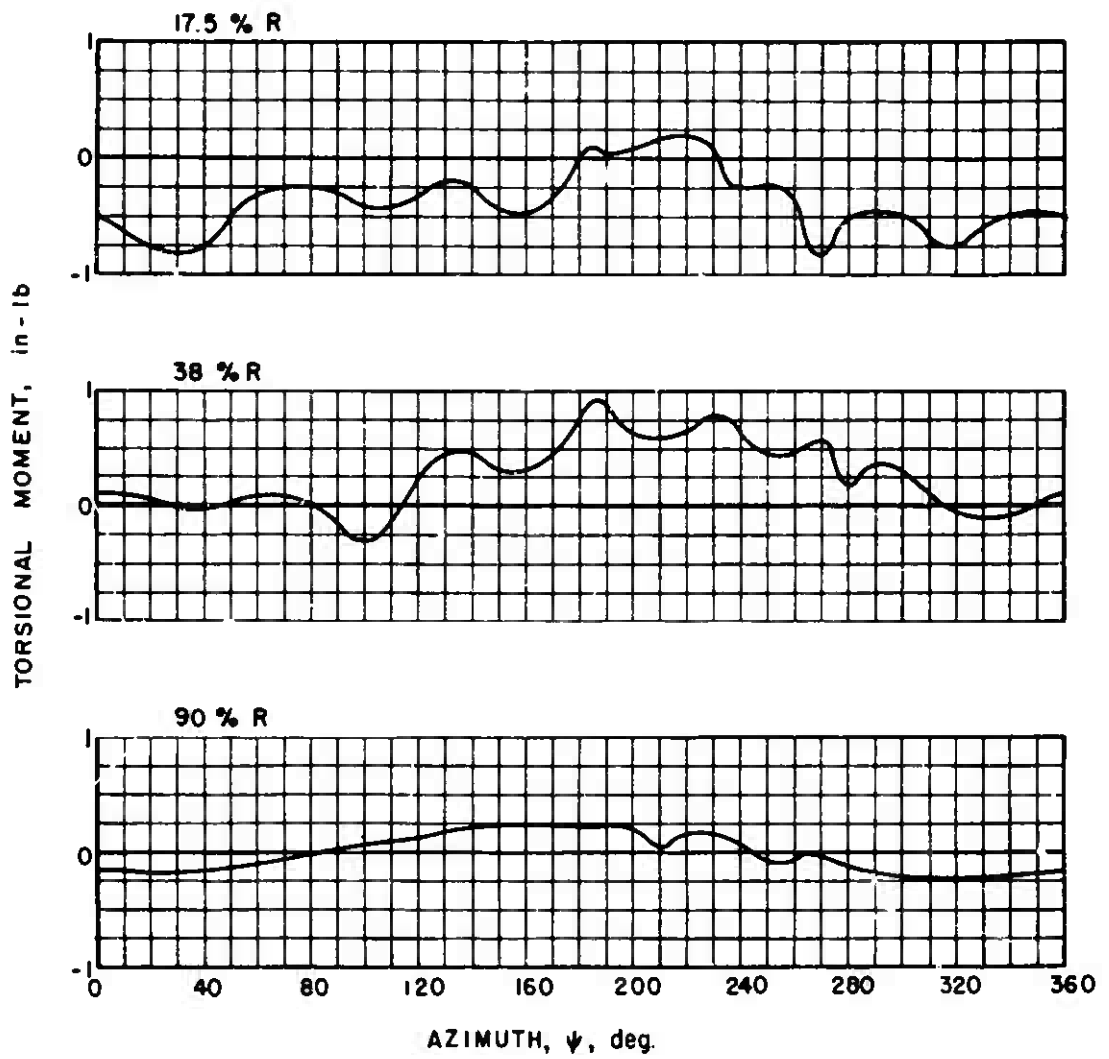
(a) FLATWISE MOMENTS

Figure 22. Experimental Blade Moments.



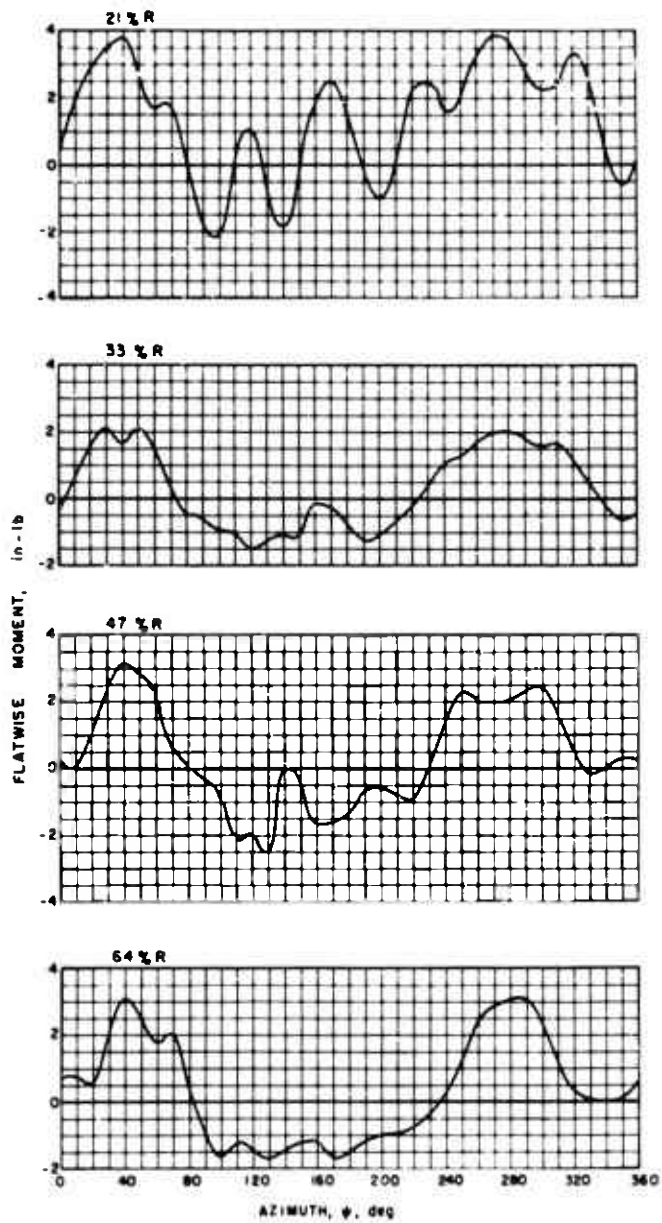
(b) EDGEWISE MOMENTS

Figure 22. Continued.



(c) TORSIONAL MOMENTS

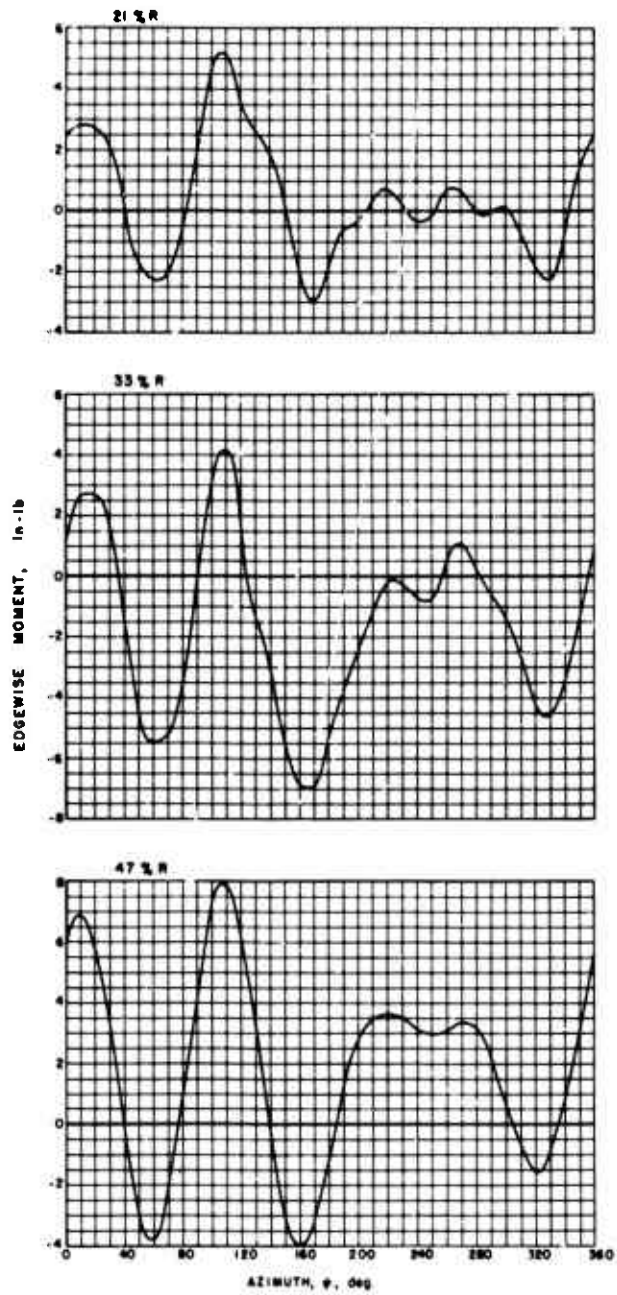
Figure 22. Concluded.



$\mu = 0.5$ $C_L / \sigma = 0.048$ $\alpha_s = -4 \text{ deg}$

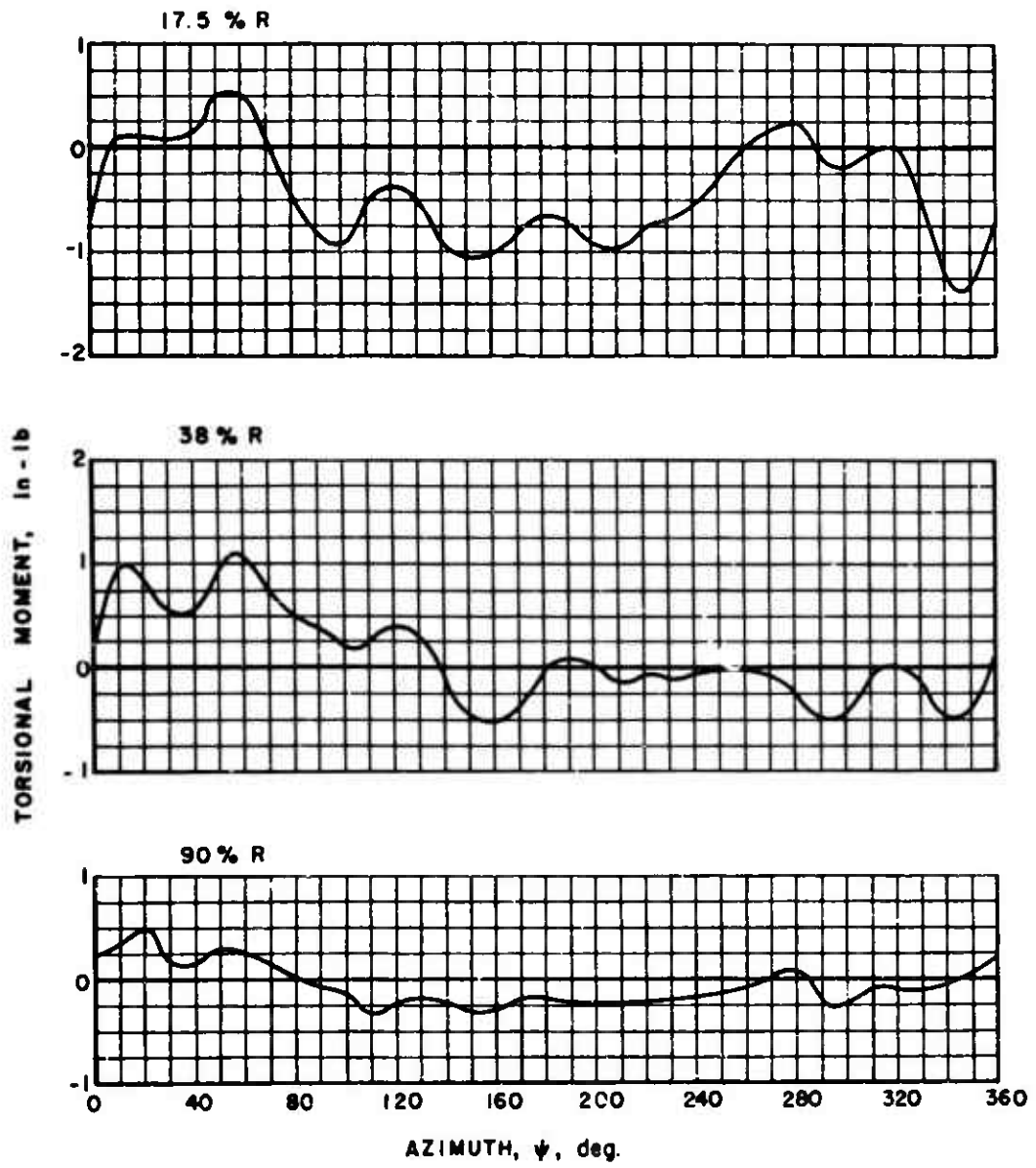
(a) FLATWISE MOMENTS

Figure 23. Experimental Blade Moments.



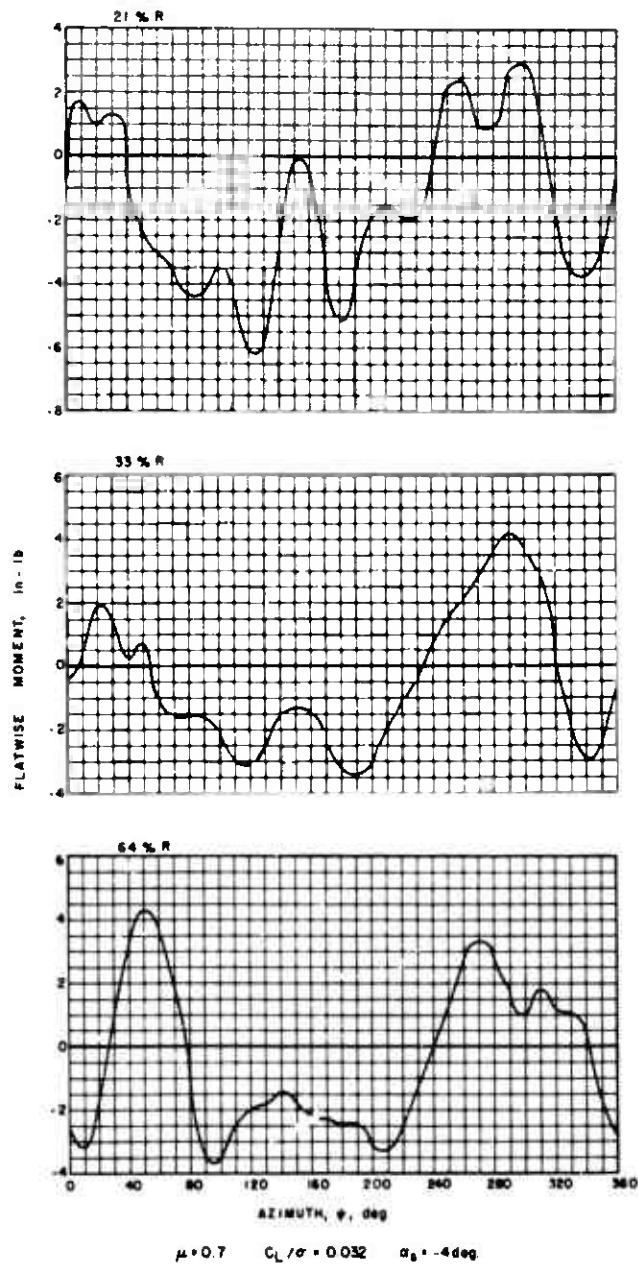
(b) EDGEWISE MOMENTS

Figure 23. Continued.



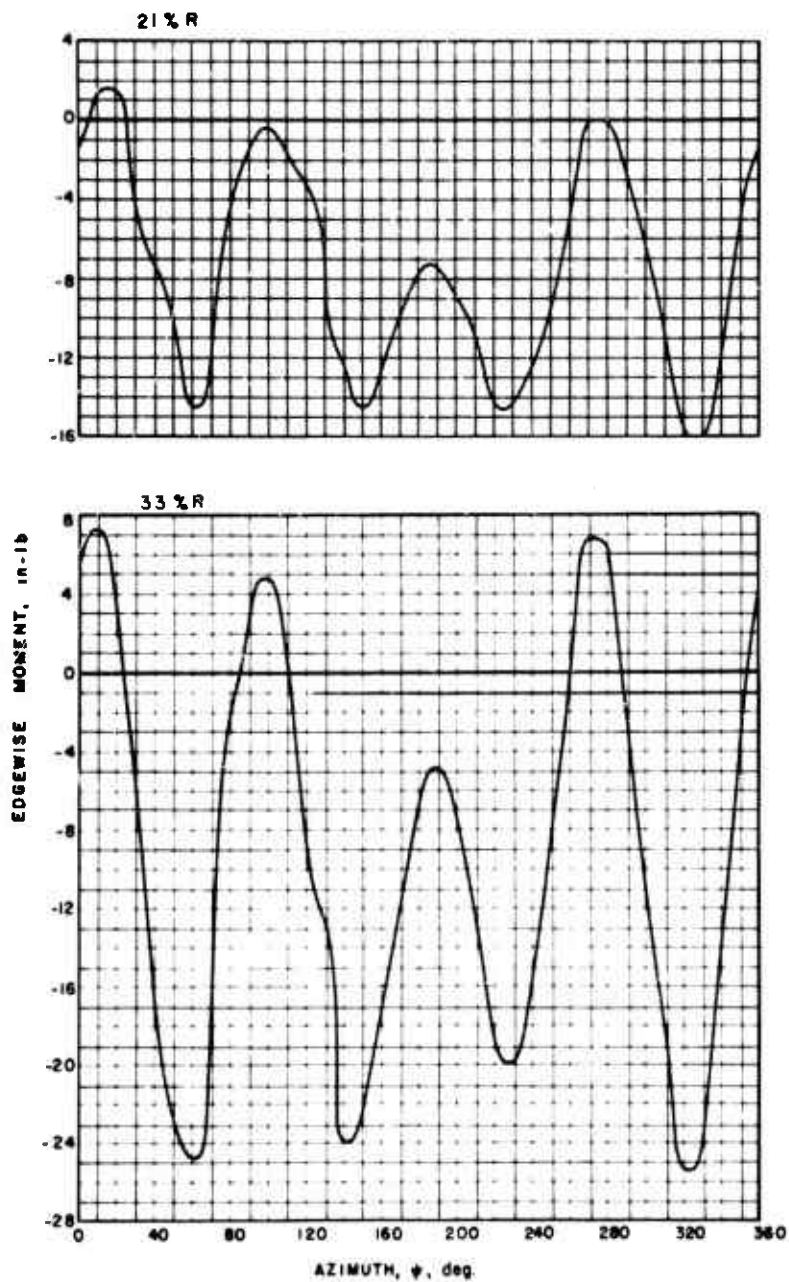
(c) TORSIONAL MOMENTS

Figure 23. Concluded.



(a) FLATWISE MOMENTS

Figure 24. Experimental Blade Moments.



(b) EDGEWISE MOMENTS

Figure 24. Continued.

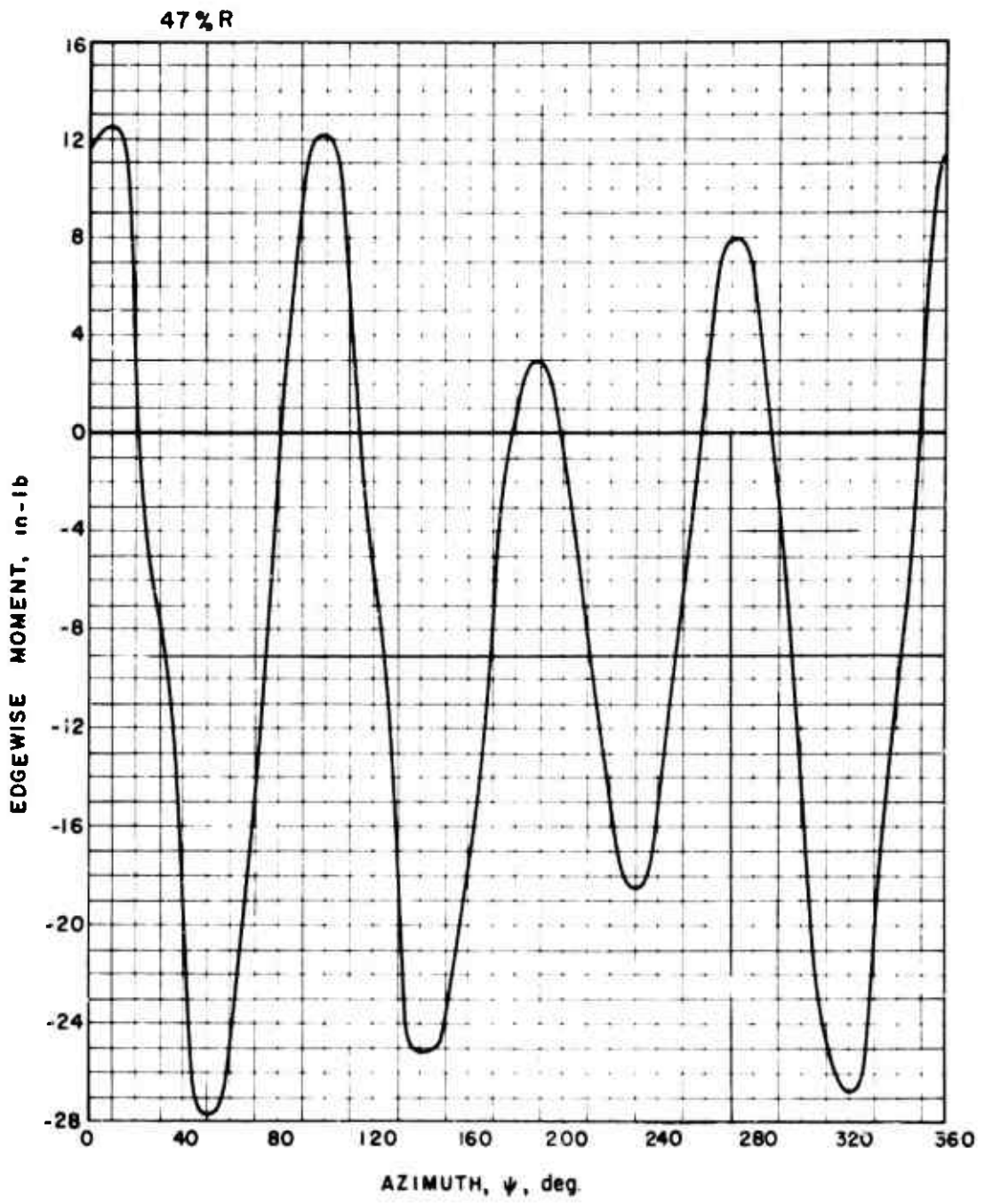
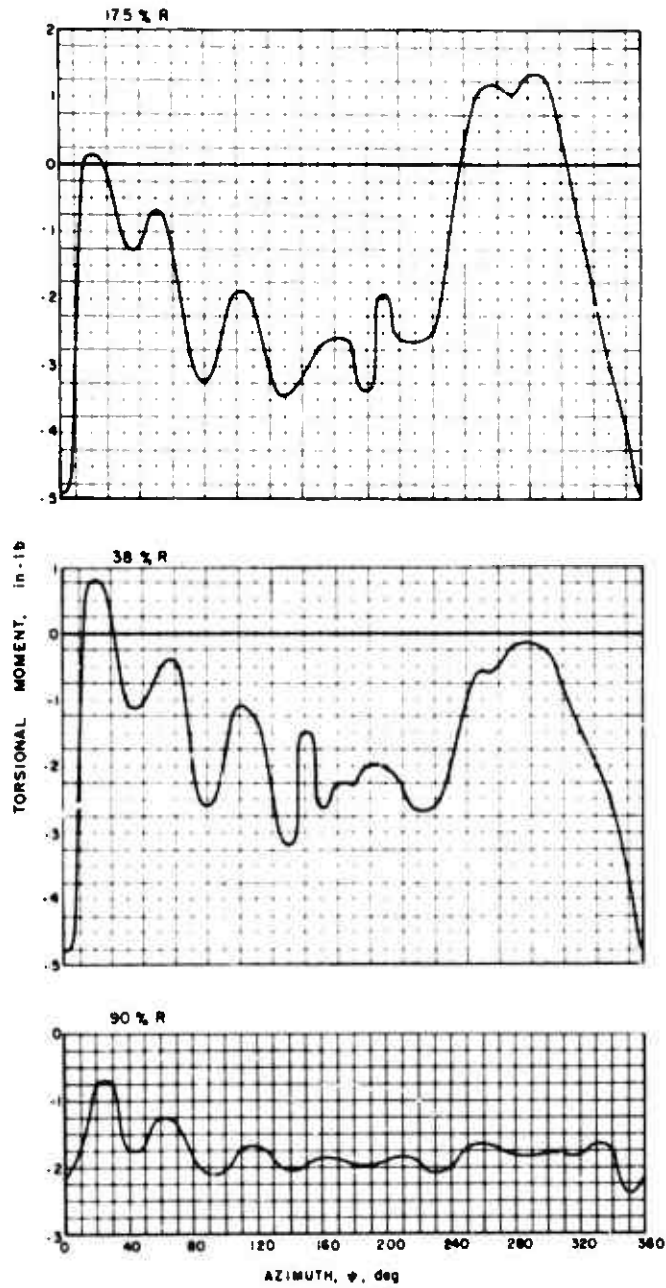


Figure 24(b). Continued.



(c) TORSIONAL MOMENTS

Figure 24. Concluded.

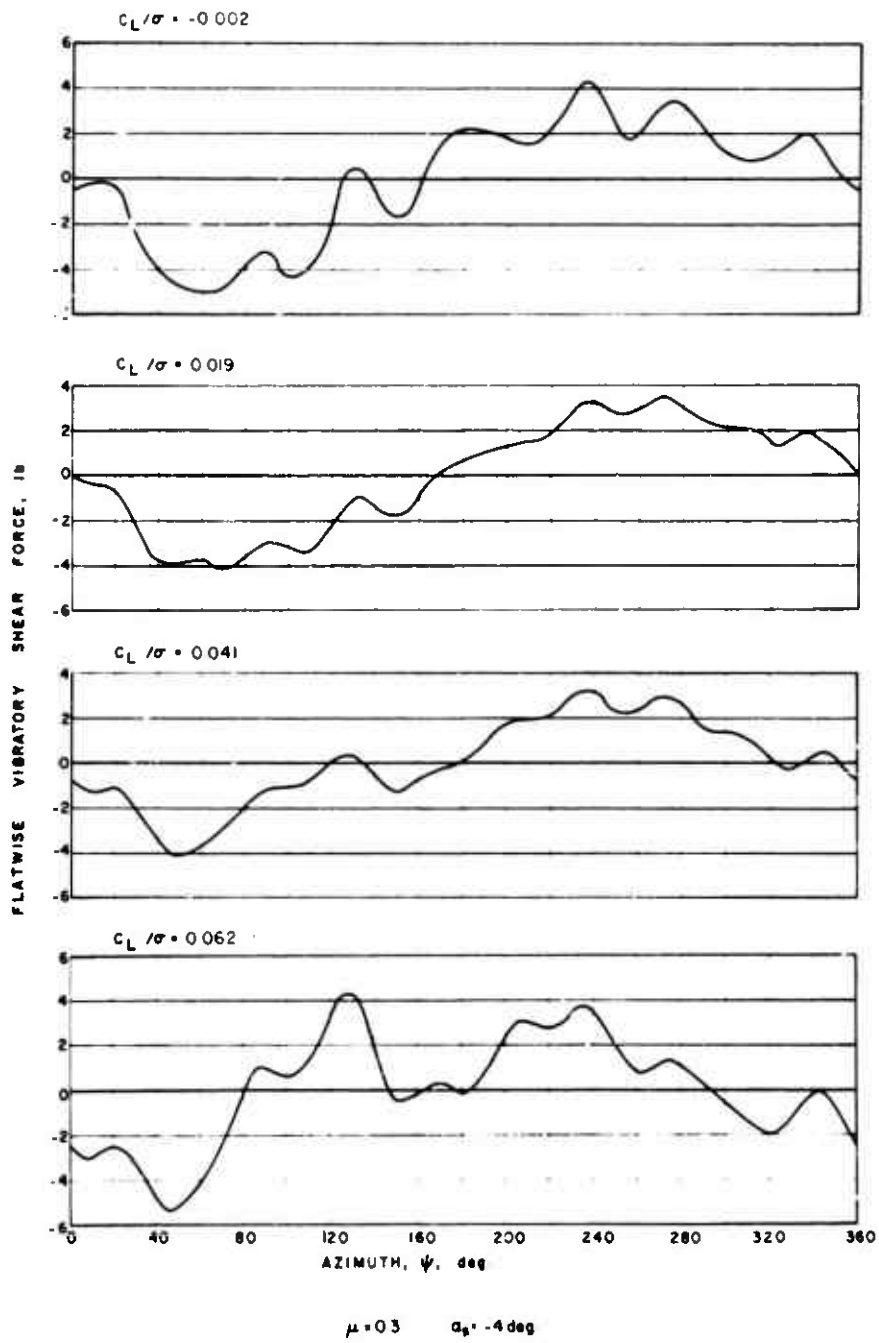
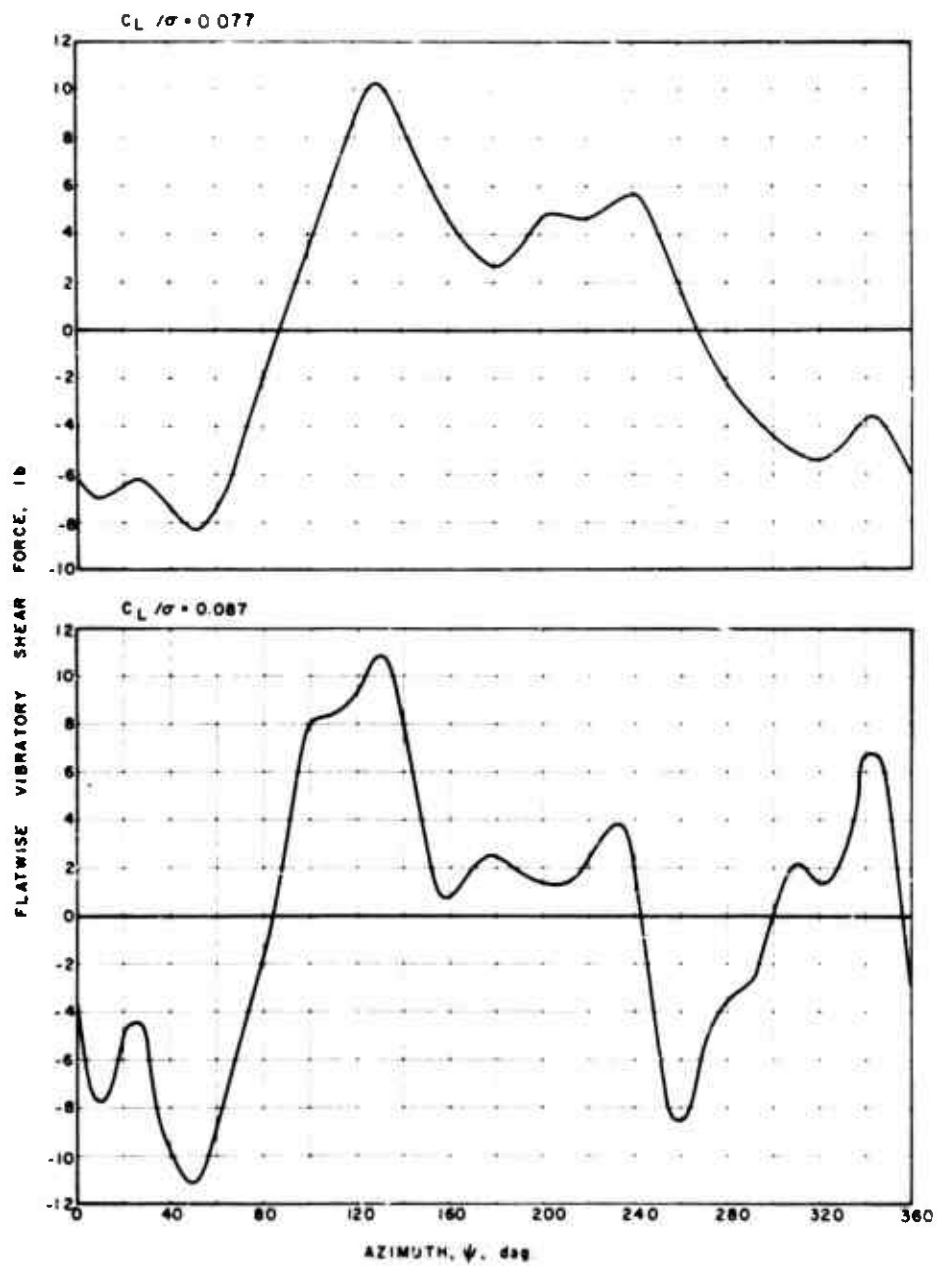


Figure 25. Effect of Rotor Lift on Flatwise Vibratory Shear Force.



$\mu = 0.3 \quad \alpha_q = -4 \text{ deg}$

Figure 25. Concluded.

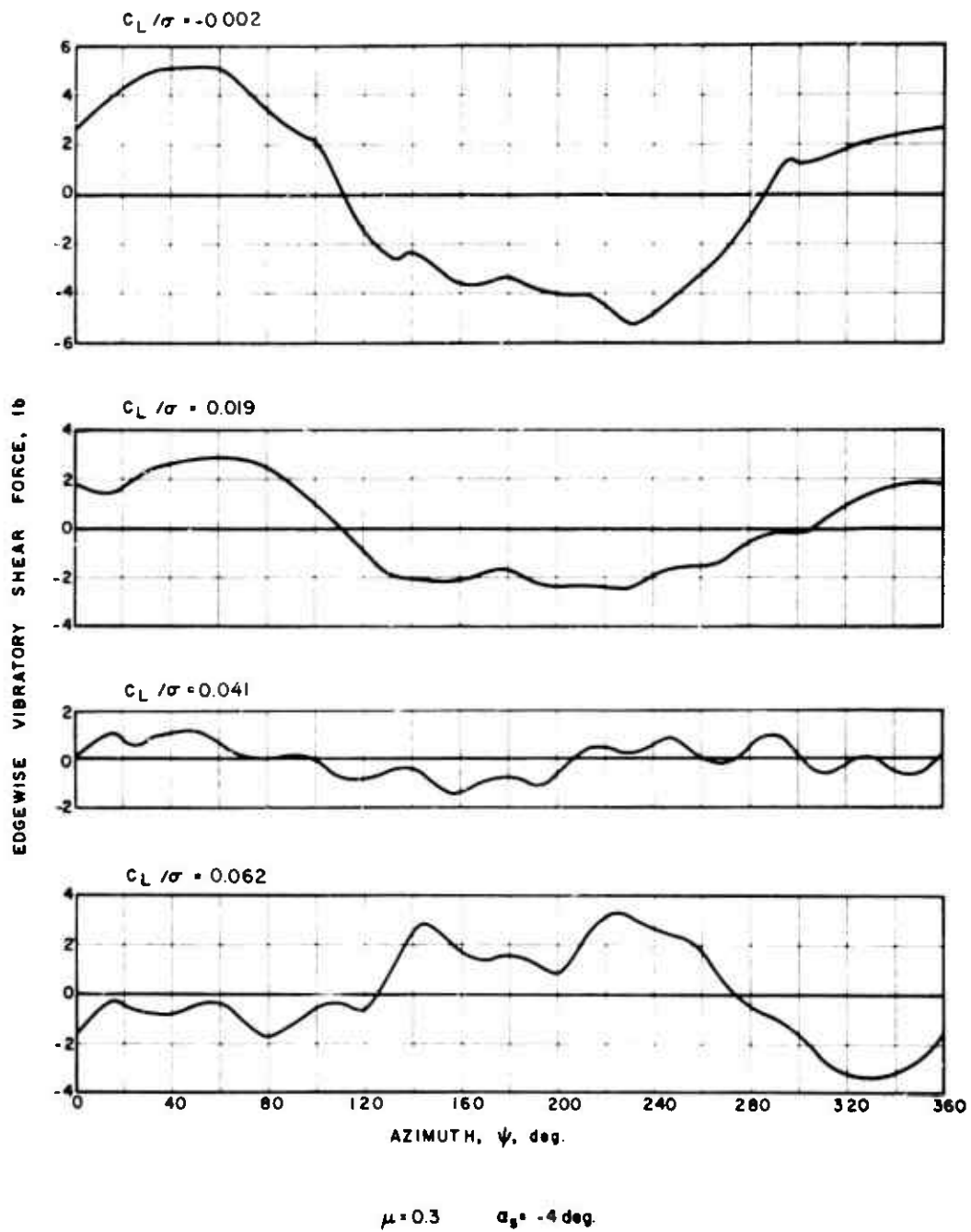


Figure 26. Effect of Rotor Lift on Edgewise Vibratory Shear Force.

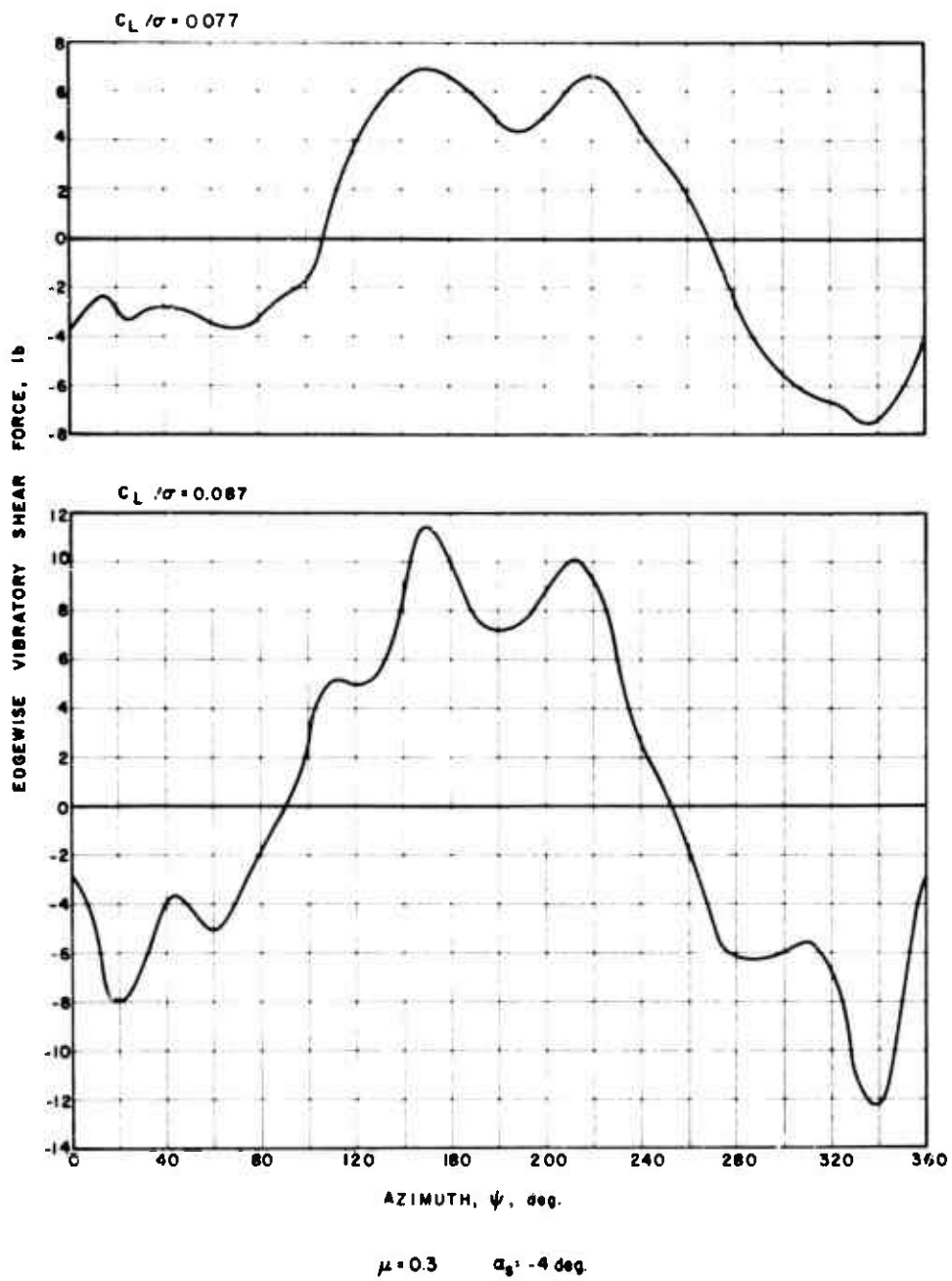


Figure 26. Concluded.

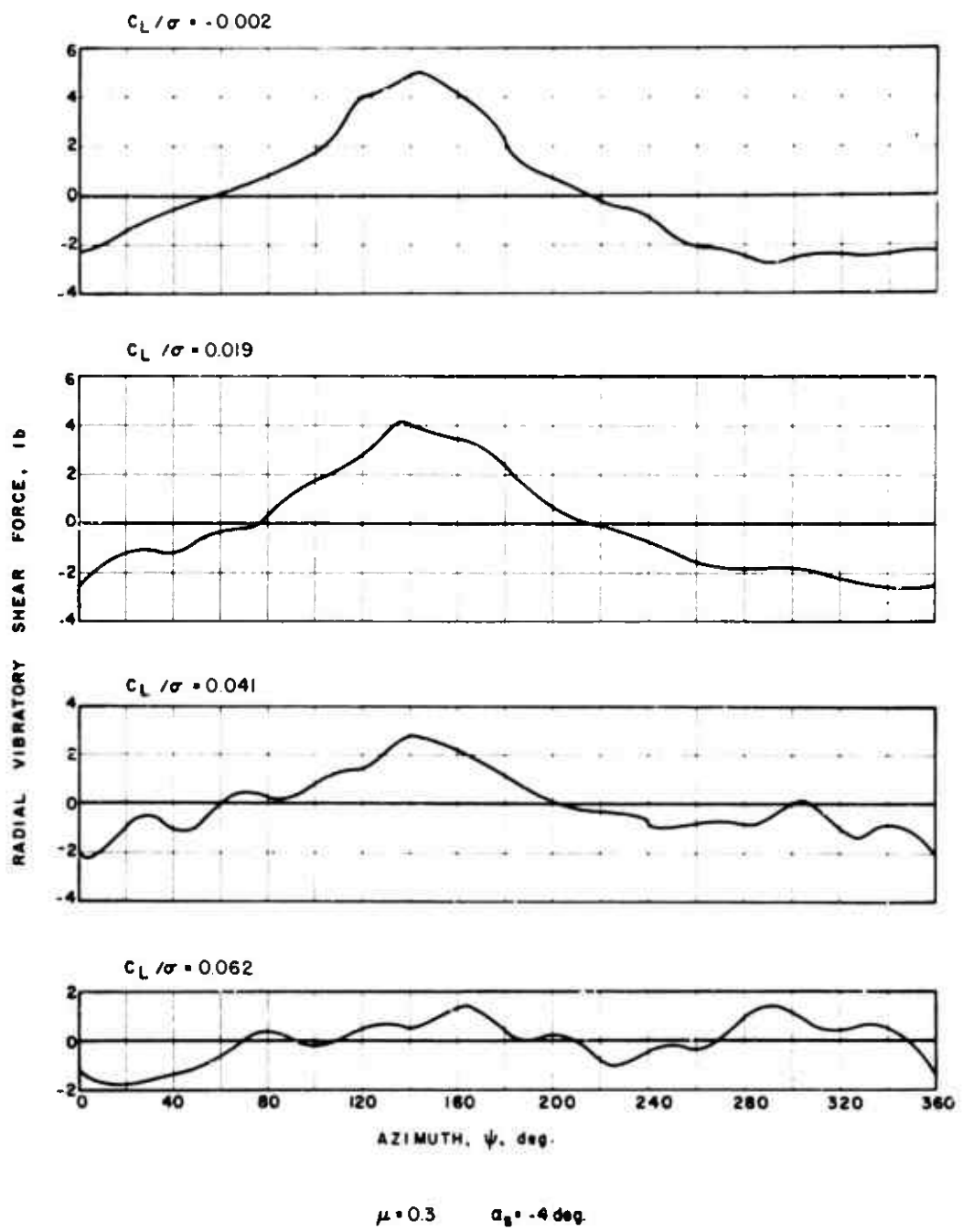


Figure 27. Effect of Rotor Lift on Radial Vibratory Shear Force.

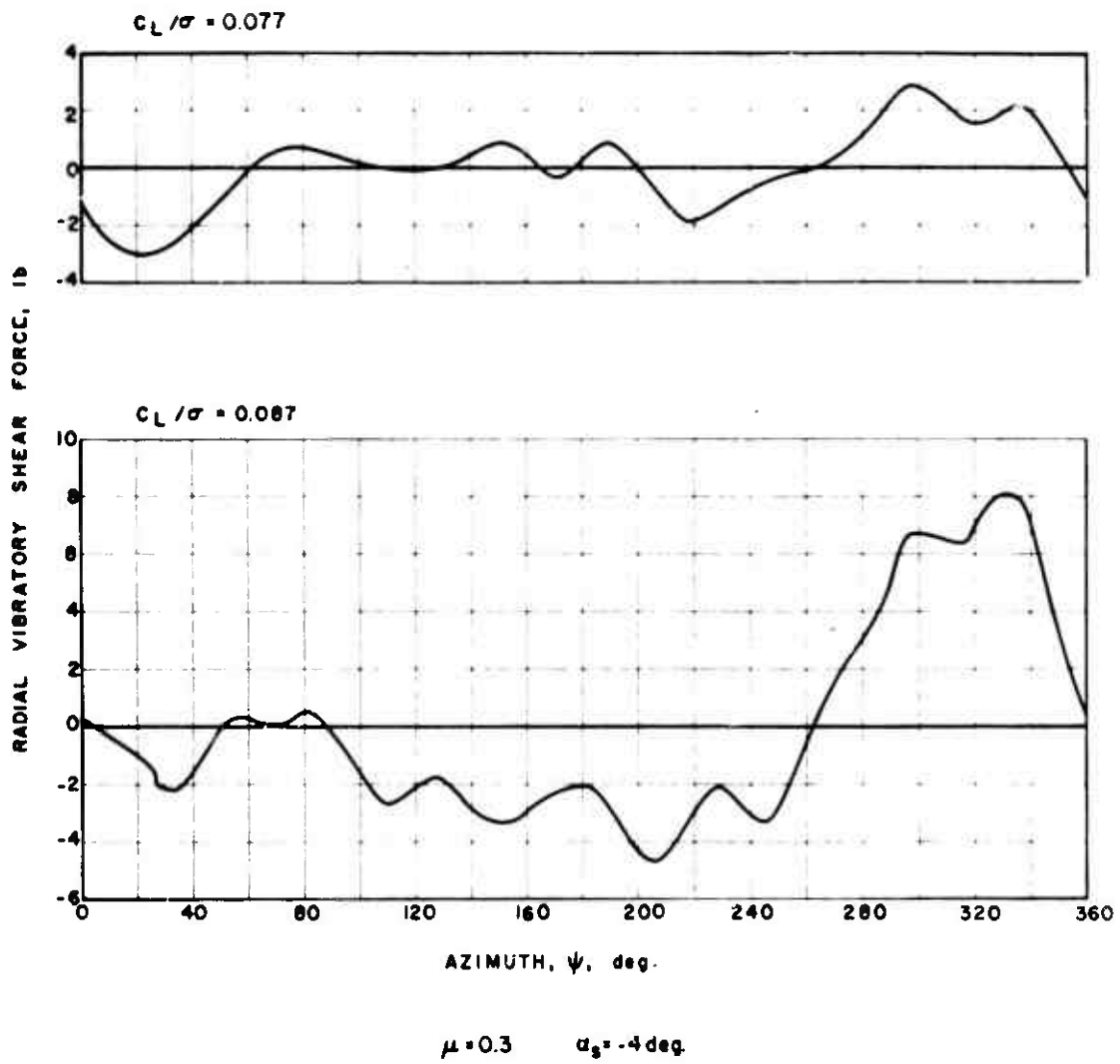
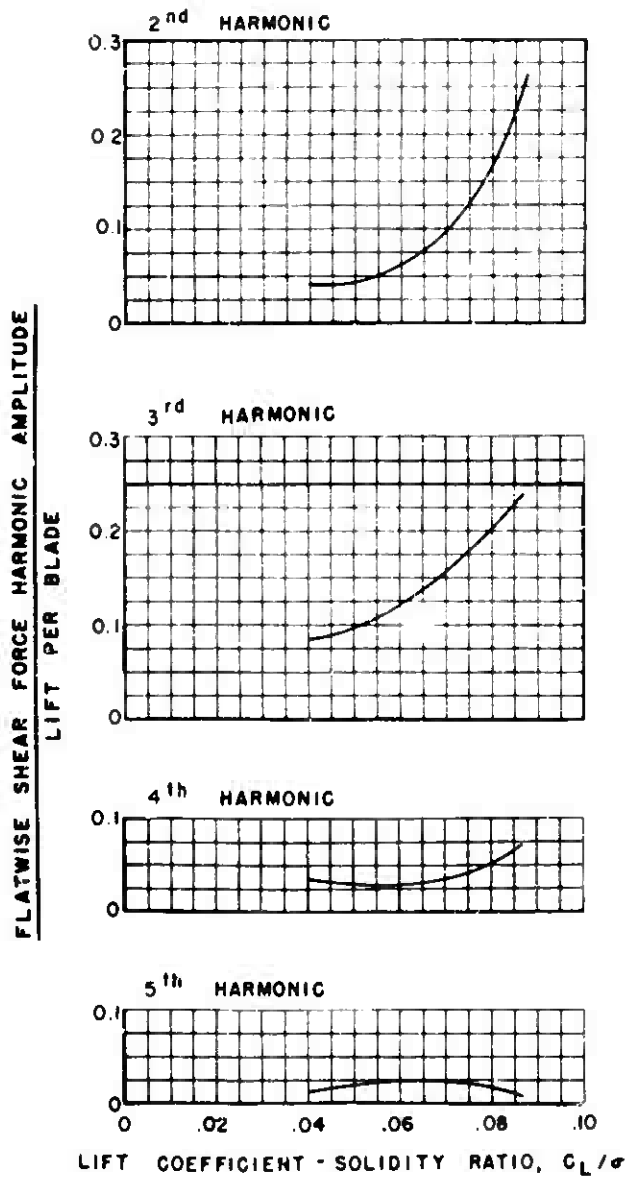


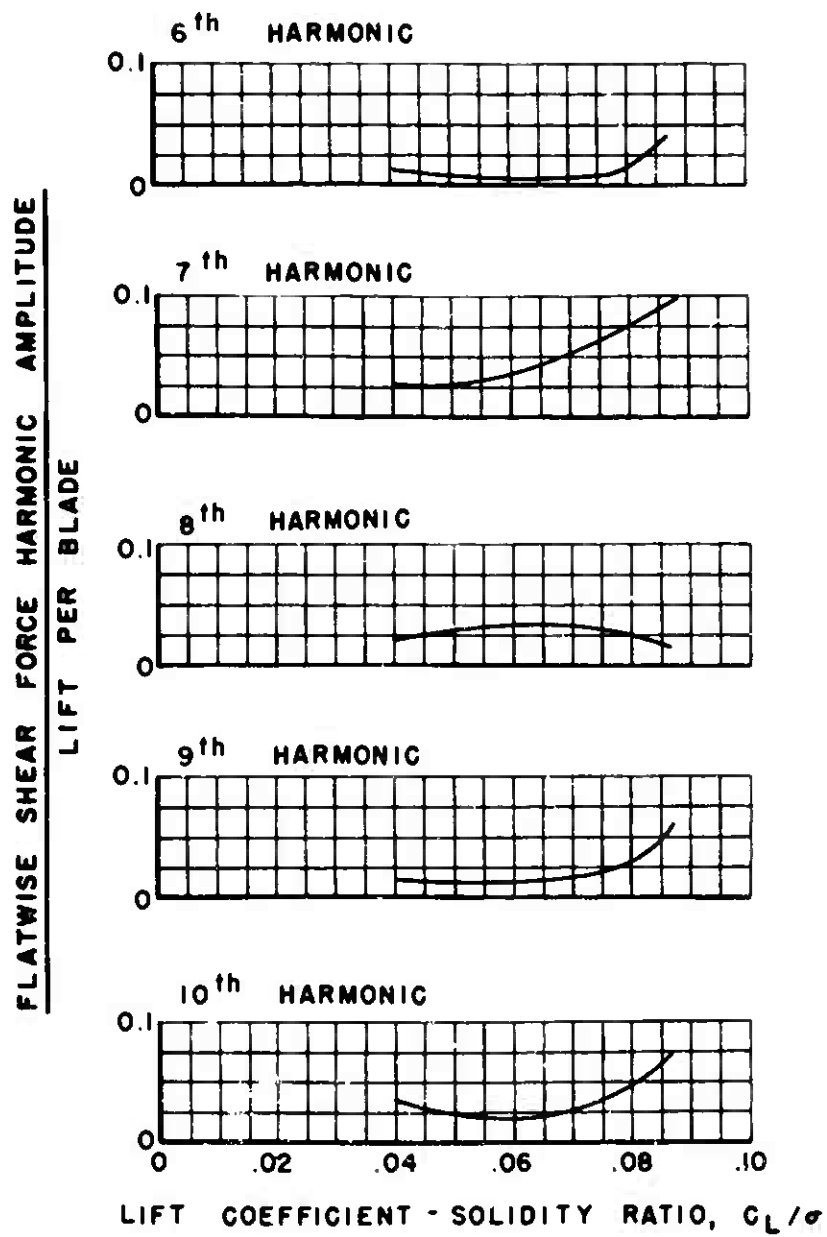
Figure 27. Concluded.



$\mu = 0.3, \alpha_s = -4 \text{ deg}$

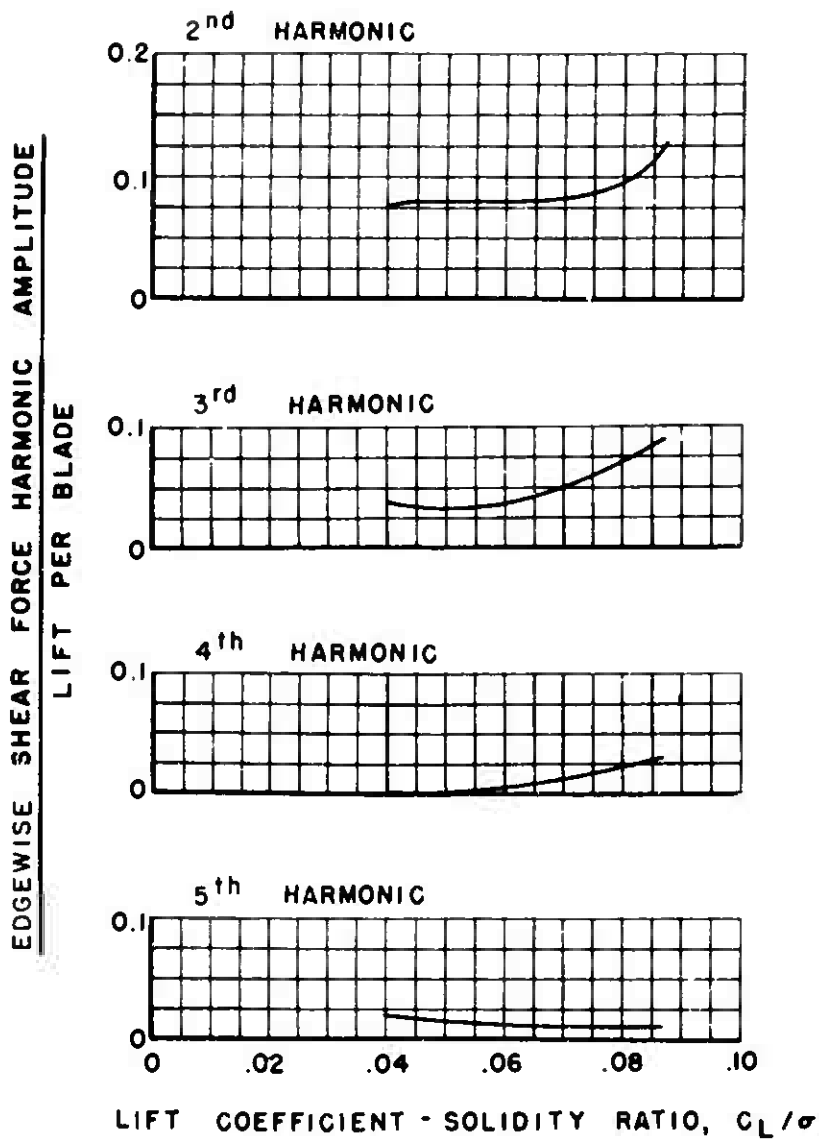
(a) FLATWISE

Figure 28. Effect of Rotor Lift on Nondimensional Shear Forces.



$\mu = 0.3, \alpha_s = -4 \text{ deg.}$

Figure 28(a). Continued.

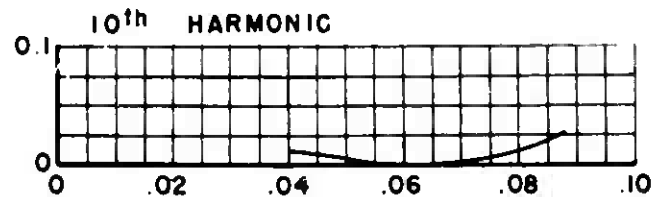
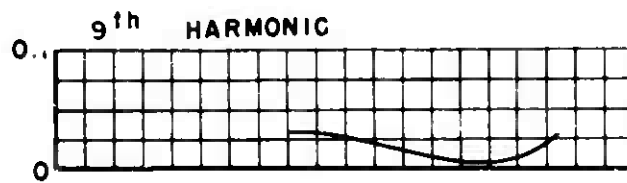
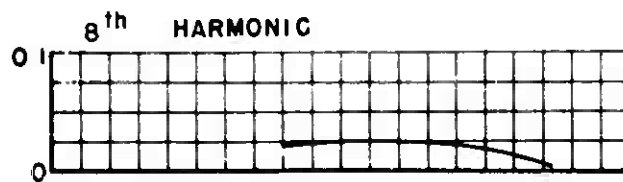
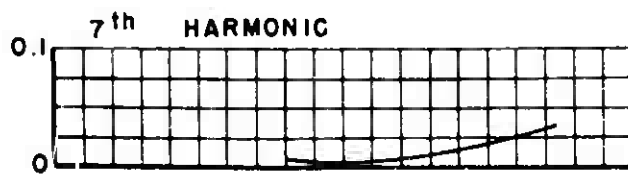
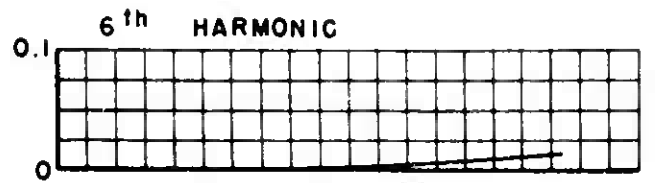


$$\mu = 0.3 \quad \alpha_s = -4 \text{ deg.}$$

(b) EDGEWISE

Figure 28. Continued.

EDGEWISE SHEAR FORCE HARMONIC AMPLITUDE
LIFT PER BLADE



LIFT COEFFICIENT - SOLIDITY RATIO, C_L/σ

$$\mu = 0.3 \quad \alpha_s = -4 \text{ deg}$$

Figure 28(b). Concluded.

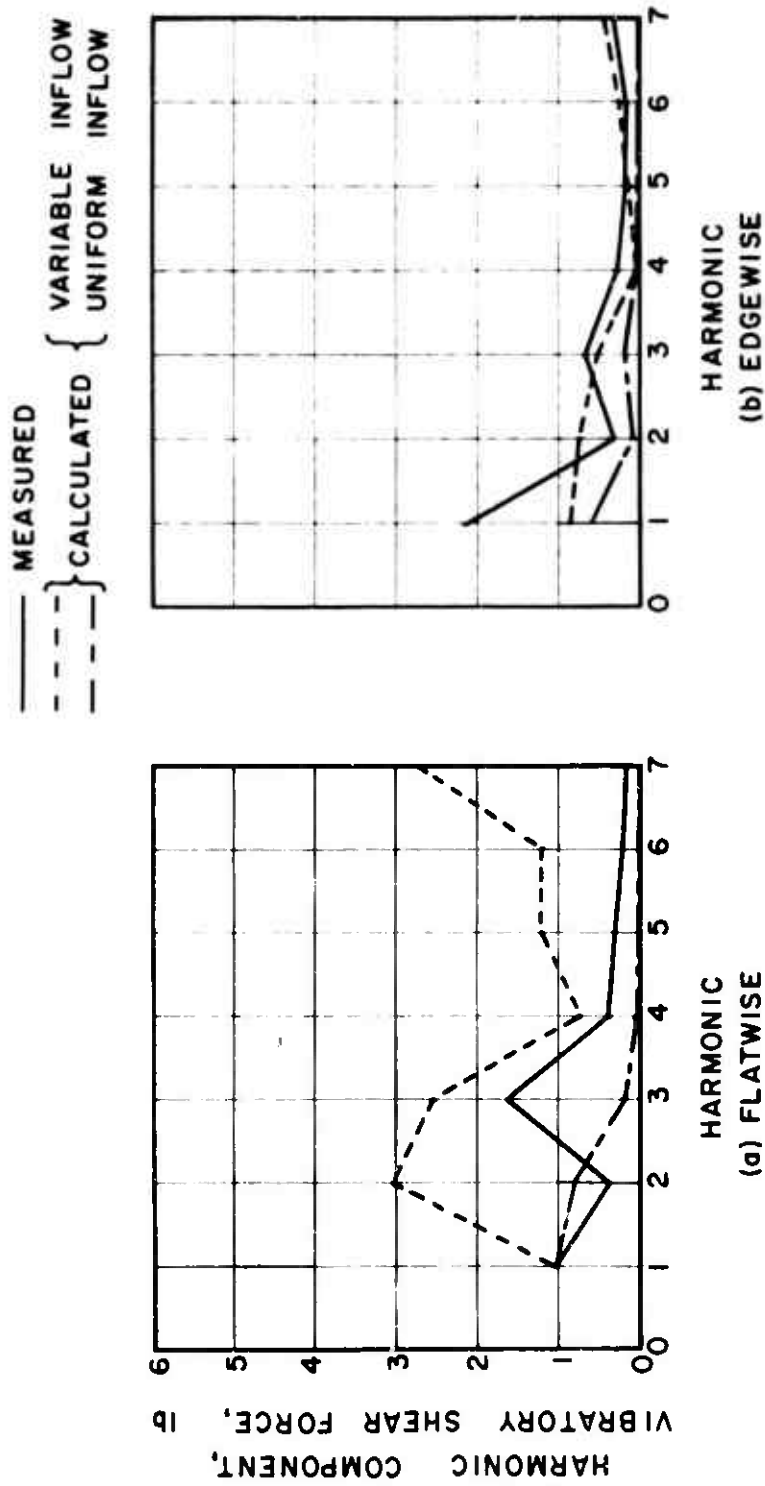
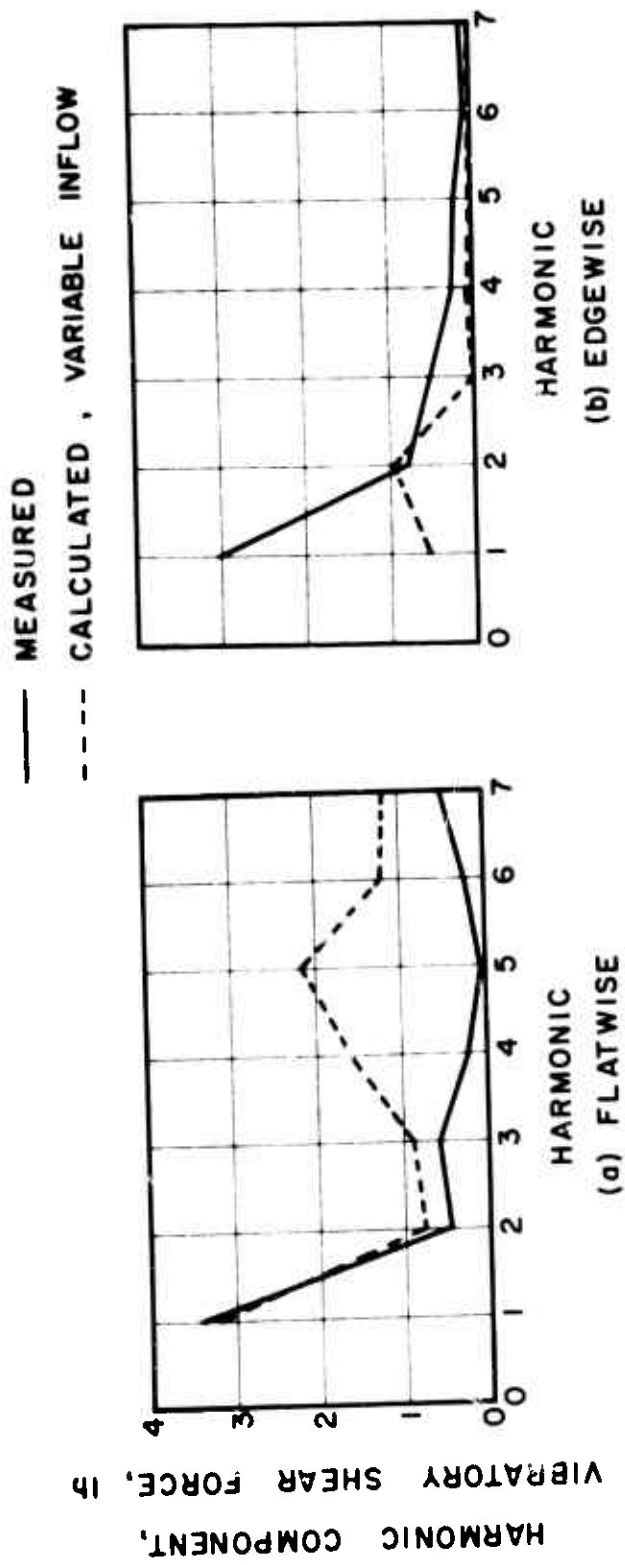
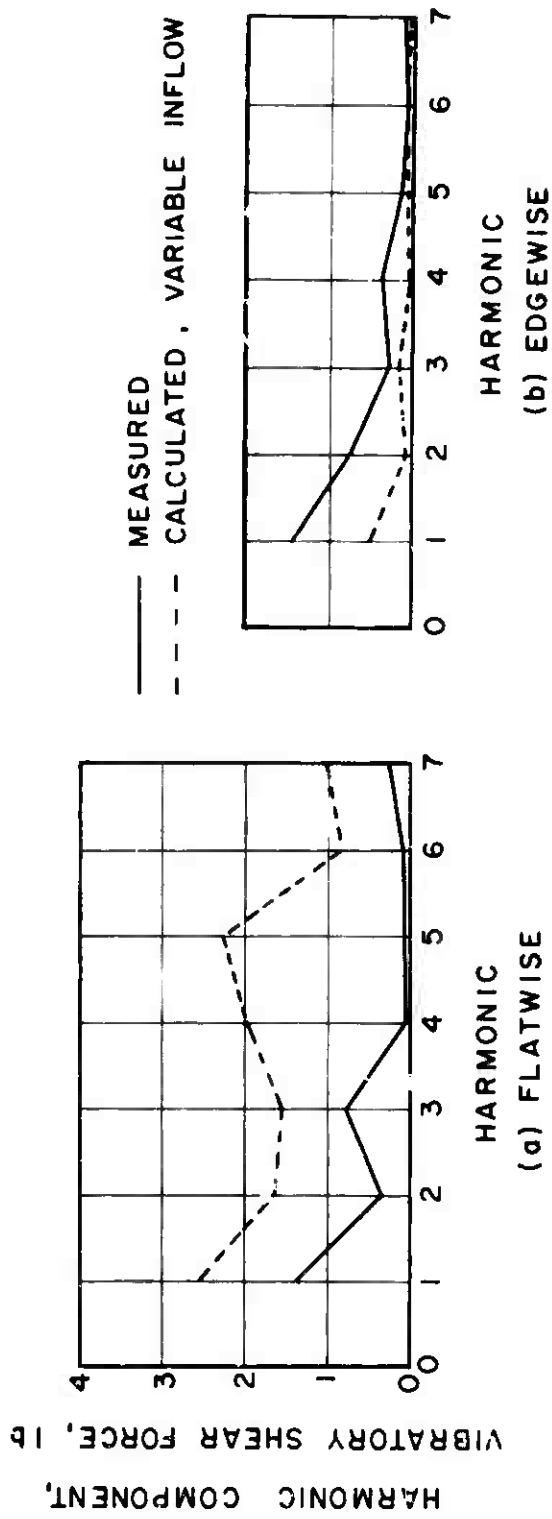


Figure 29. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.



$\mu = 0.3$ $C_L / \sigma = 0.019$ $\alpha_s = 4 \text{ deg.}$

Figure 30. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.

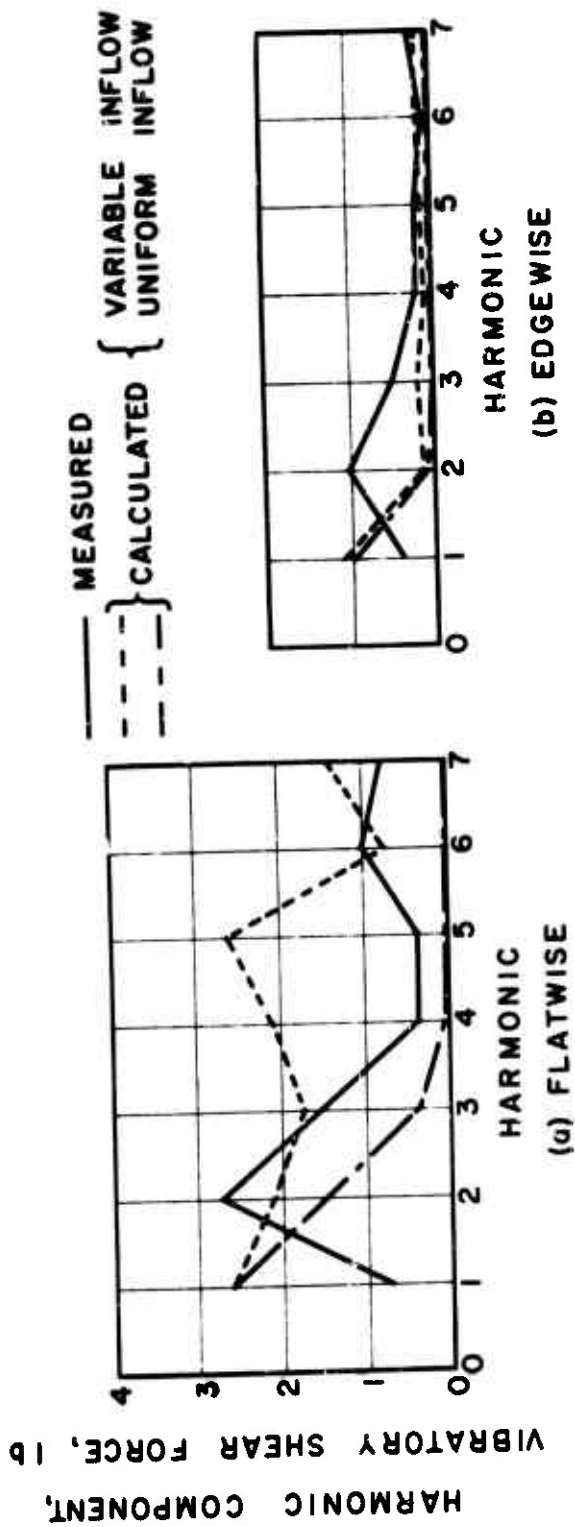


$\mu = 0.3$

$C_L/\sigma = 0.041$

$\alpha_s = -4 \text{ deg.}$

Figure 31. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.



$\mu = 0.3$ $c_L / \sigma = 0.062$ $\alpha_s = -4 \text{ deg.}$

Figure 32. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.

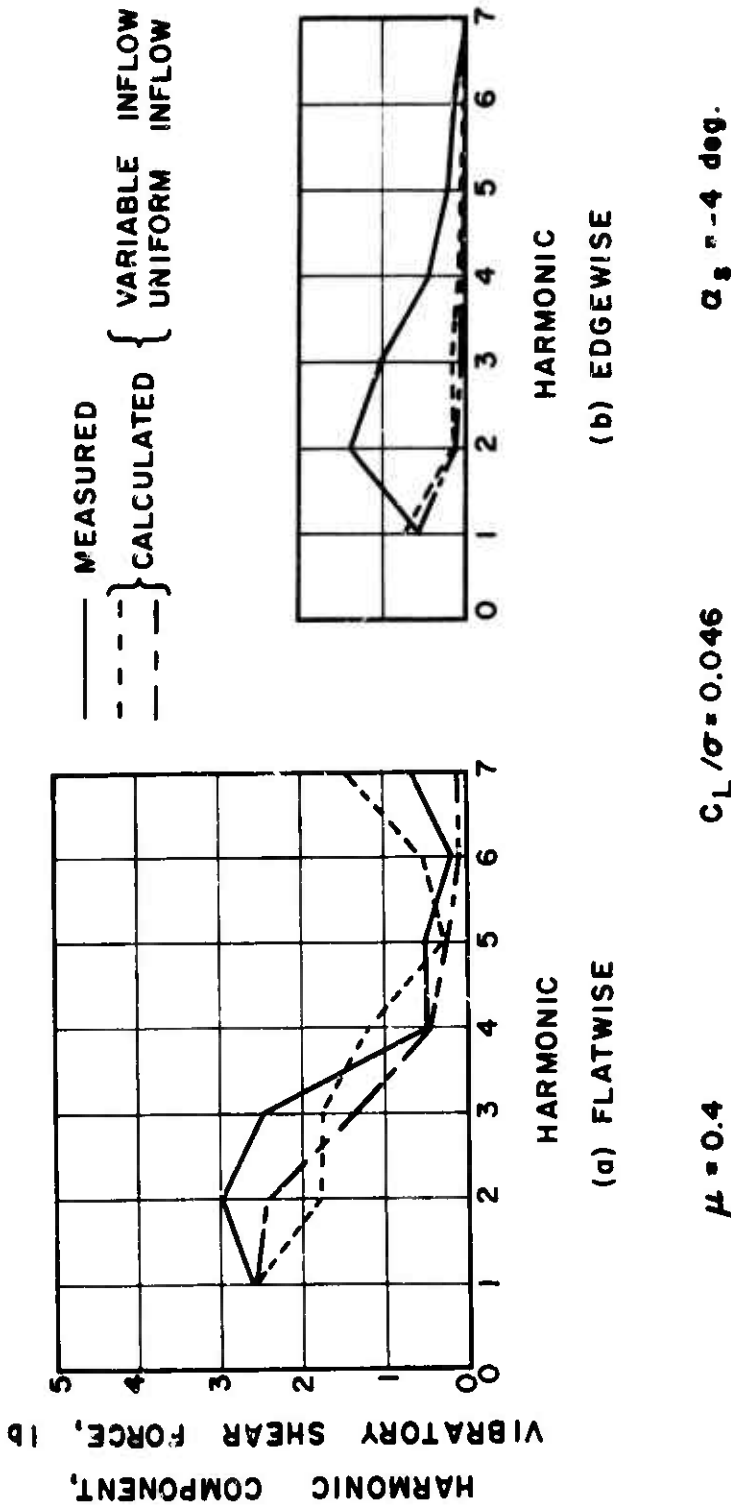


Figure 33. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.

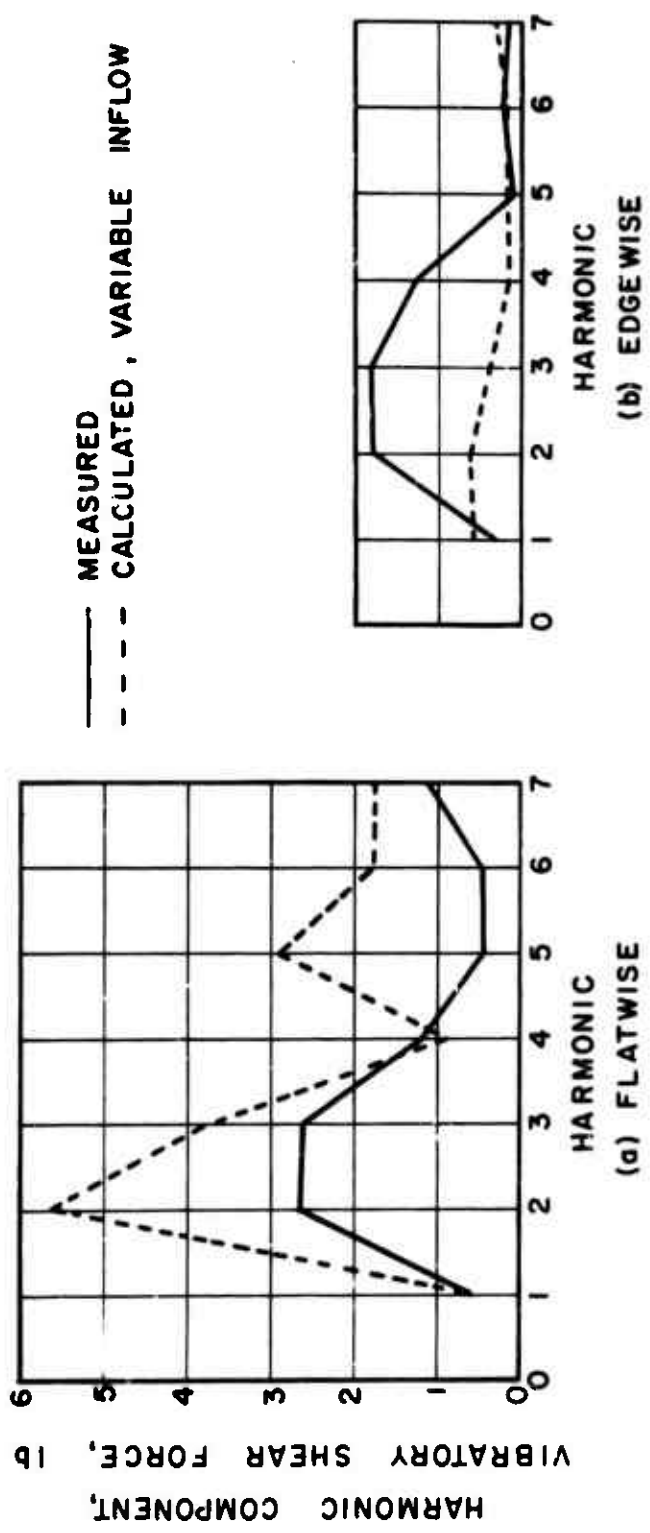


Figure 34. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.

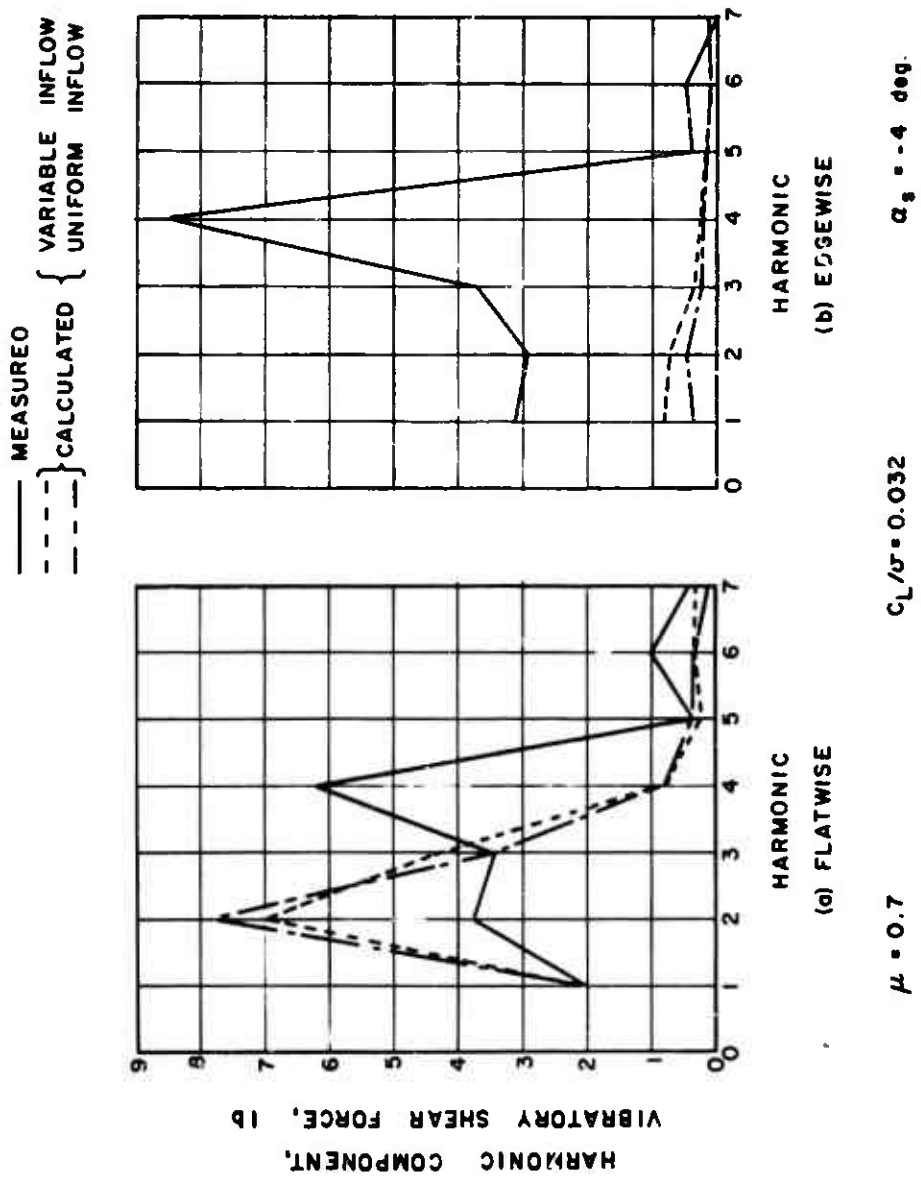


Figure 35. Comparison of Theoretical and Experimental Vibratory Shear Force Harmonic Amplitudes.

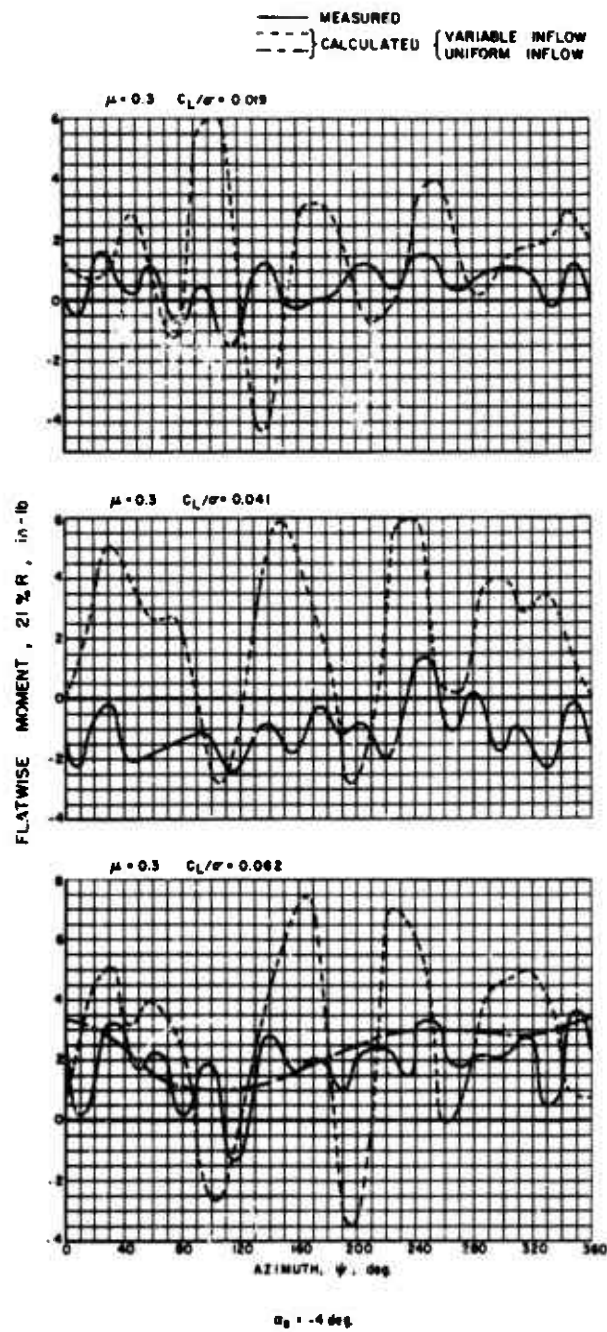


Figure 36. Comparison of Theoretical and Experimental Flatwise Rotor Blade Bending Moments.

— MEASURED
- - - CALCULATED { VARIABLE INFLOW
 UNIFORM INFLOW

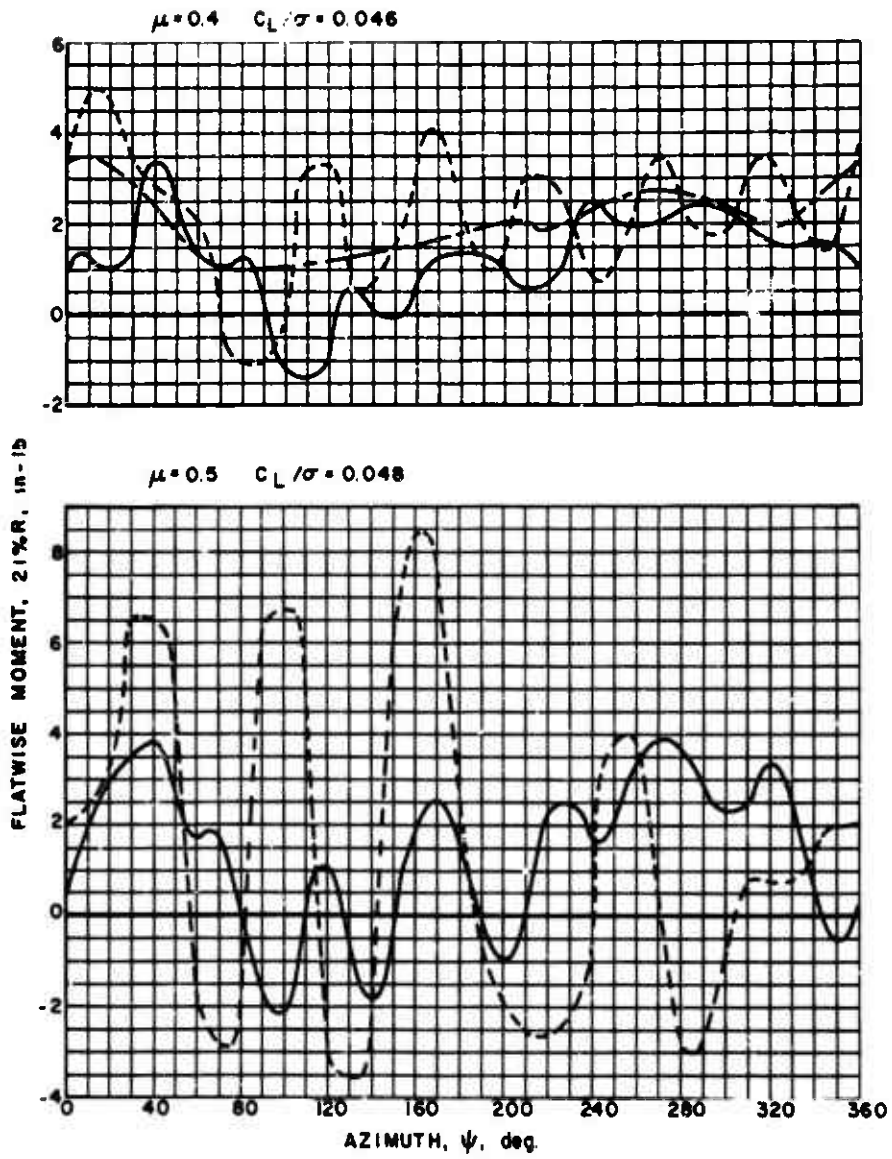


Figure 36. Concluded.

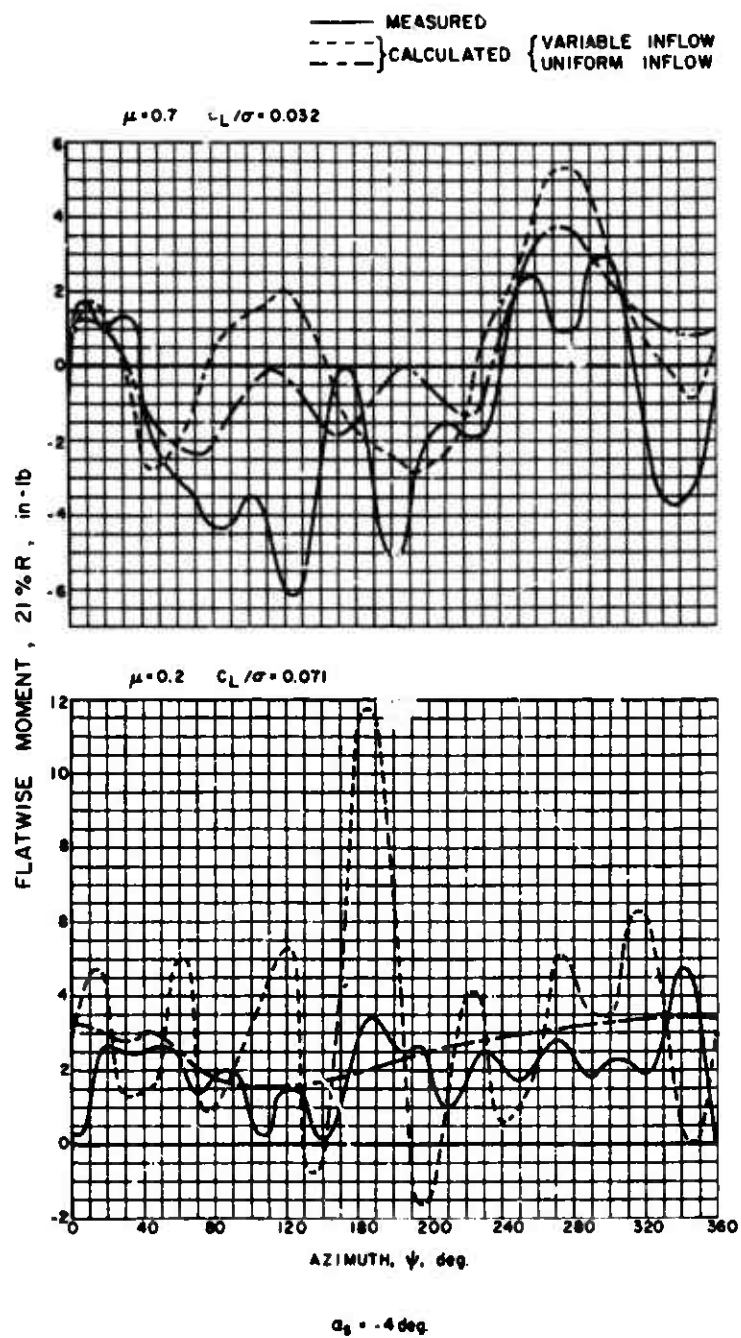
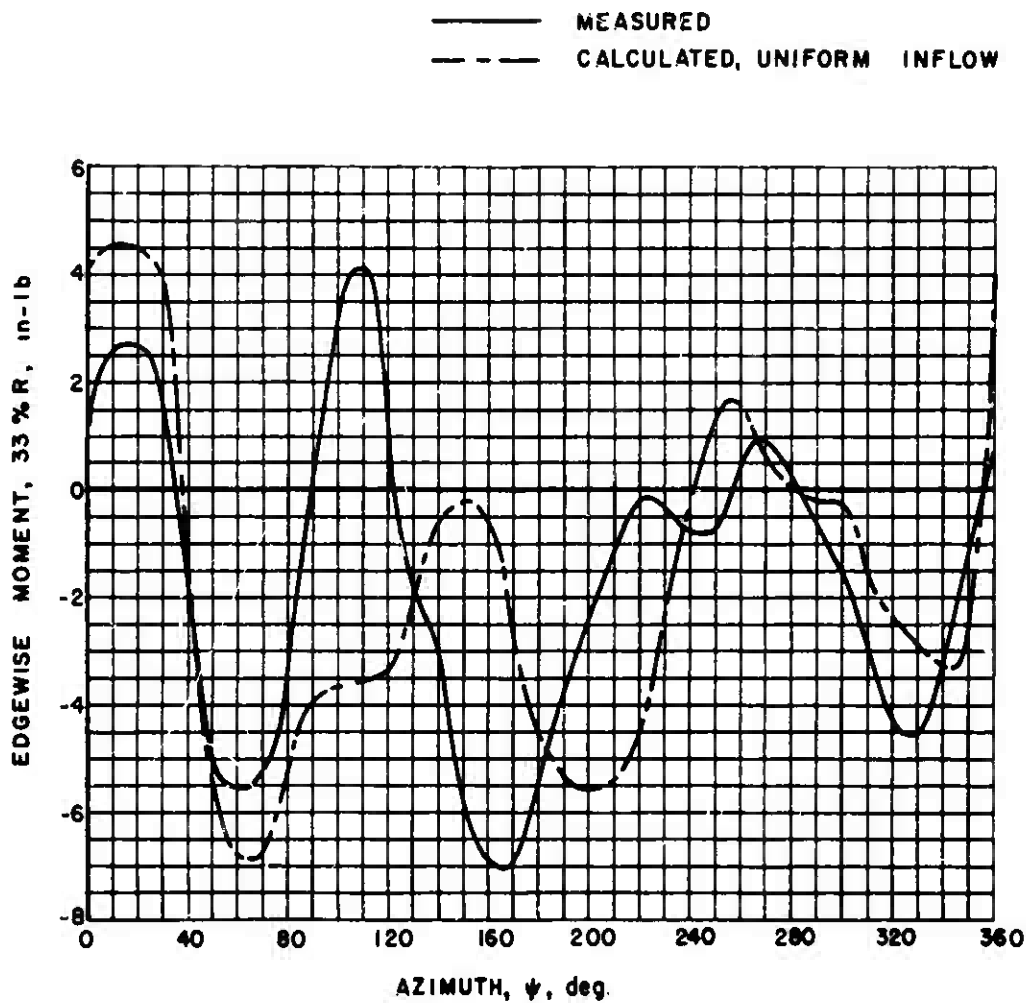


Figure 37. Comparison of Theoretical and Experimental Flatwise Rotor Blade Bending Moments.



$\mu = 0.5$

$C_L / \sigma = 0.048$

$\alpha_s = -4 \text{ deg.}$

Figure 38. Comparison of Theoretical and Experimental Edgewise Rotor Blade Bending Moments.

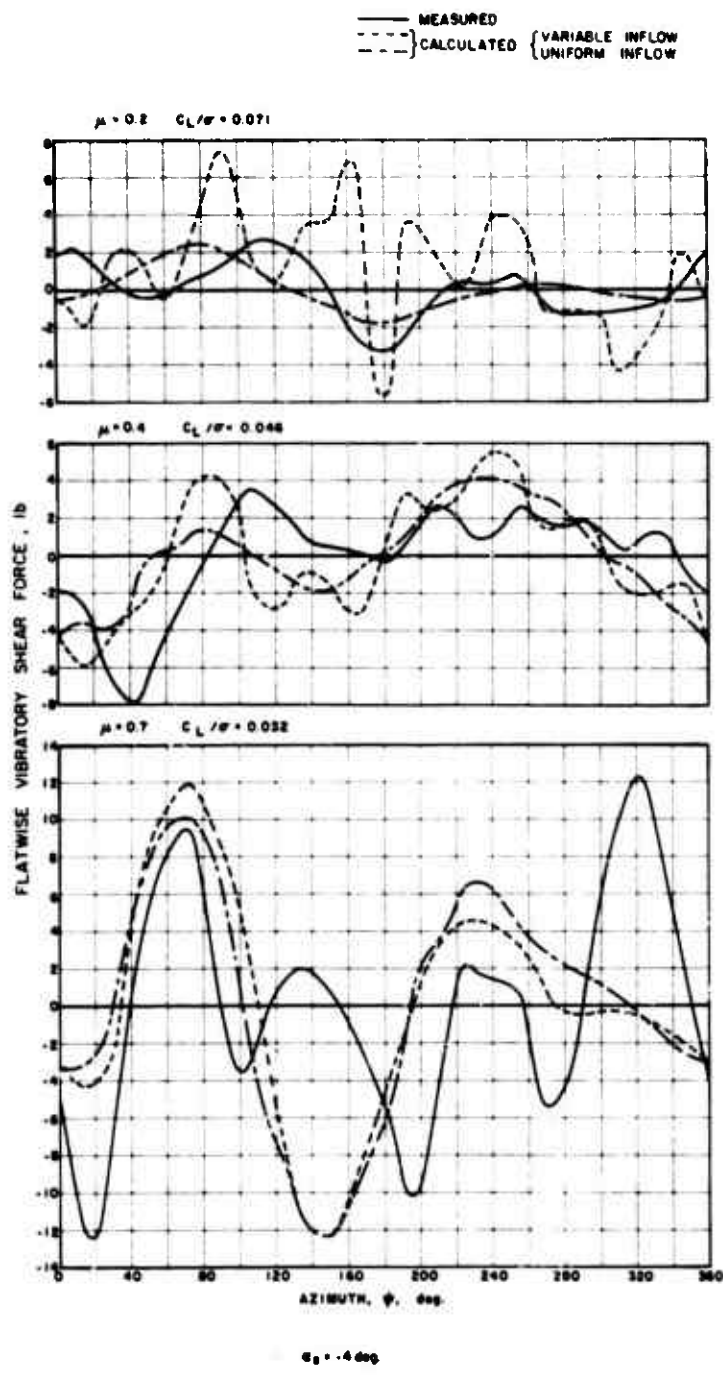


Figure 39. Azimuthal Variation of Vibratory Shear Force.

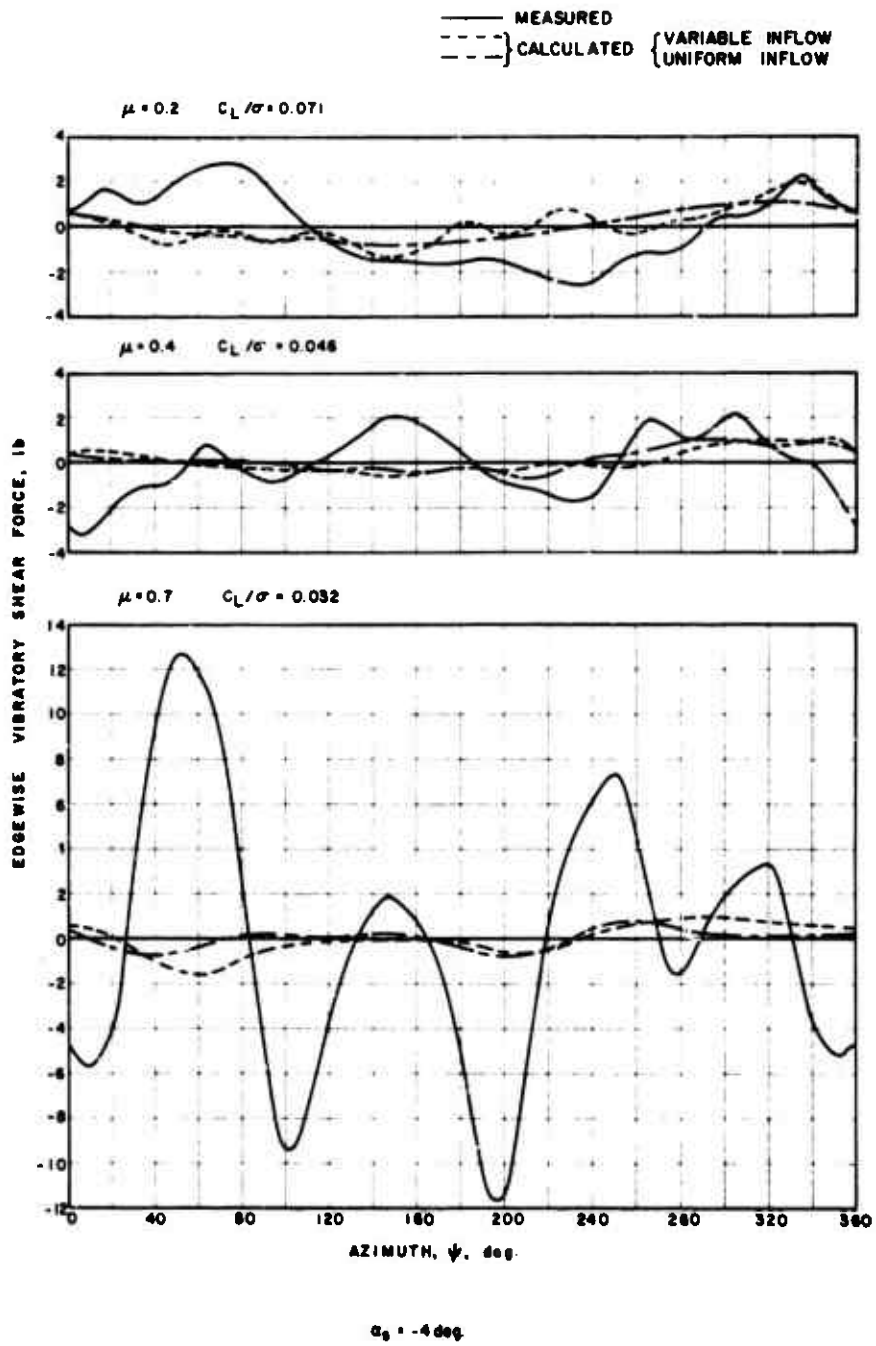


Figure 39. Concluded.

DISTRIBUTION

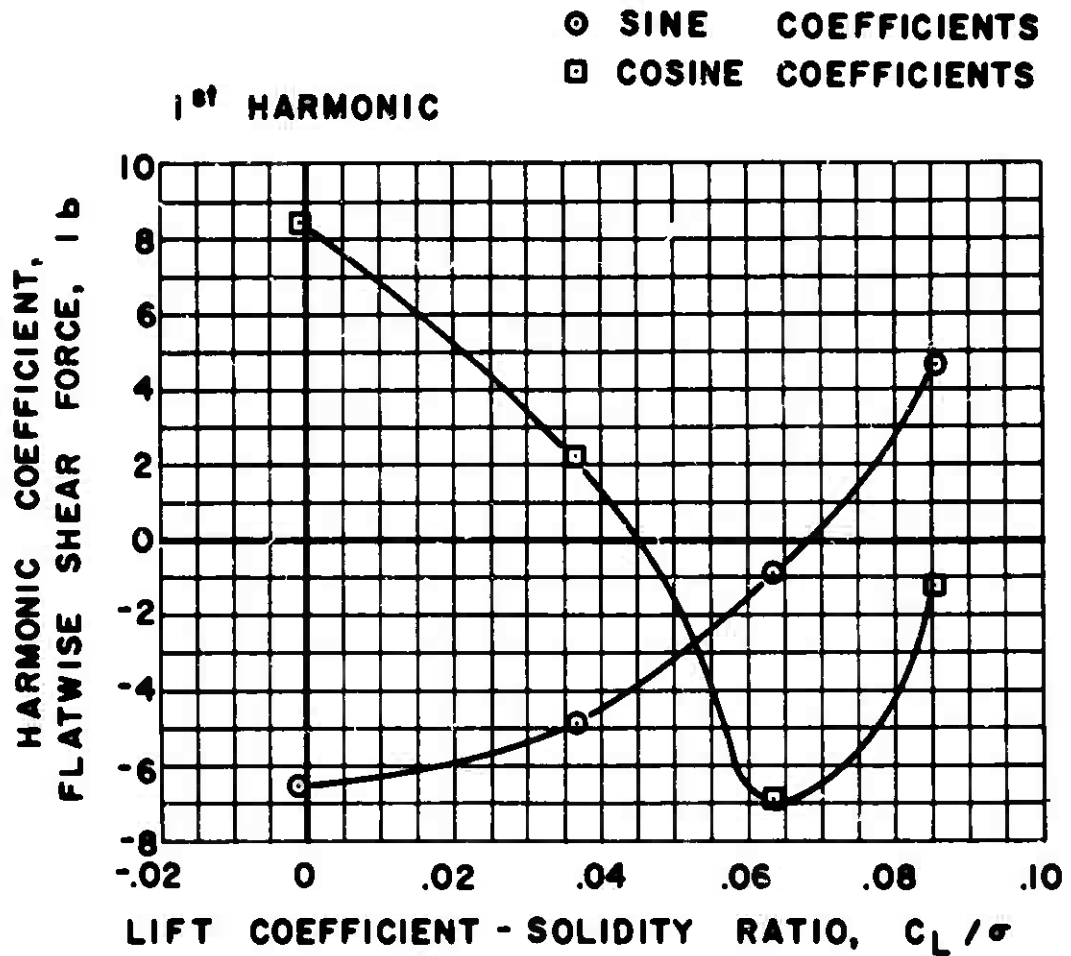
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US Army Aviation Materiel Command	5
United States Army, Pacific	1
Chief of R&D, DA	1
Director of Defense Research and Engineering	1
US Army R&D Group (Europe)	2
US Army Aviation Materiel Laboratories	28
Army Aeronautical Research Laboratory, Ames Research Center	1
US Army Research Office-Durham	1
Plastics Technical Evaluation Center	1
US Army Engineer Waterways Experiment Station	1
US Army Test and Evaluation Command	1
US Army Electronics Command	2
US Army Combat Developments Command Experimentation Command	1
US Army Aviation School	1
US Army Aviation Test Activity	2
Air Force Flight Test Center, Edwards AFB	2
Air Proving Ground Center, Eglin AFB	1
US Army Field Office, AFSC, Andrews AFB	1
Systems Engineering Group, Wright-Patterson AFB	1
Naval Air Systems Command, DN	7

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Manned Spacecraft Center, NASA	1
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NAFEC Library (FAA)	2
US Army Board for Aviation Accident Research	1
Bureau of Safety, Civil Aeronautics Board	2
US Naval Aviation Safety Center	1
Federal Aviation Agency, Washington, DC	2
US Army Medical R&D Command	1
US Government Printing Office	1
Defense Documentation Center	20

APPENDIX I

EXPERIMENTAL FLATWISE AND EDGEWISE SHEAR FORCE FIGURES

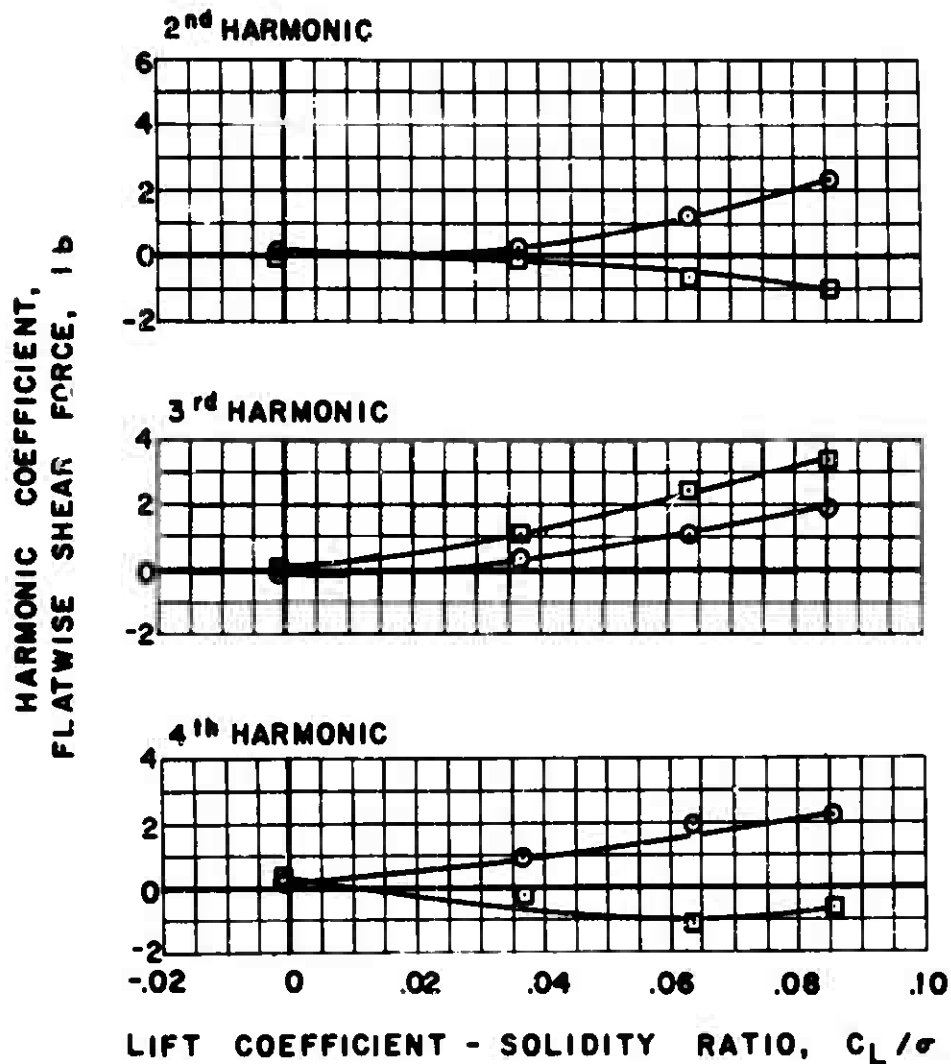


$\mu = 0.2 \quad \alpha_s = 0 \text{ deg.}$

(a) FLATWISE

Figure 40. Experimental Shear Force.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.2$ $\alpha_s = 0$ deg.

Figure 40(a). Continued.

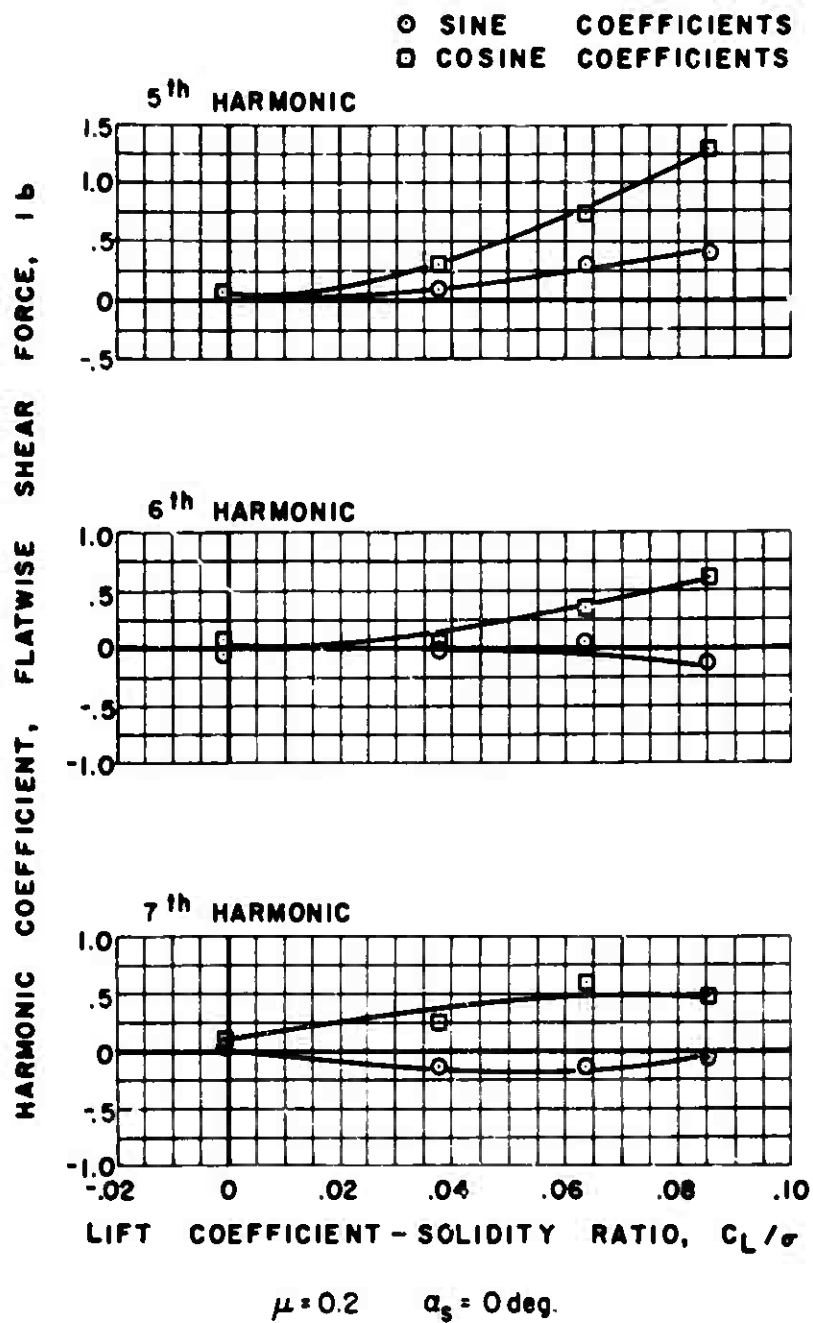


Figure 40(a). Continued.

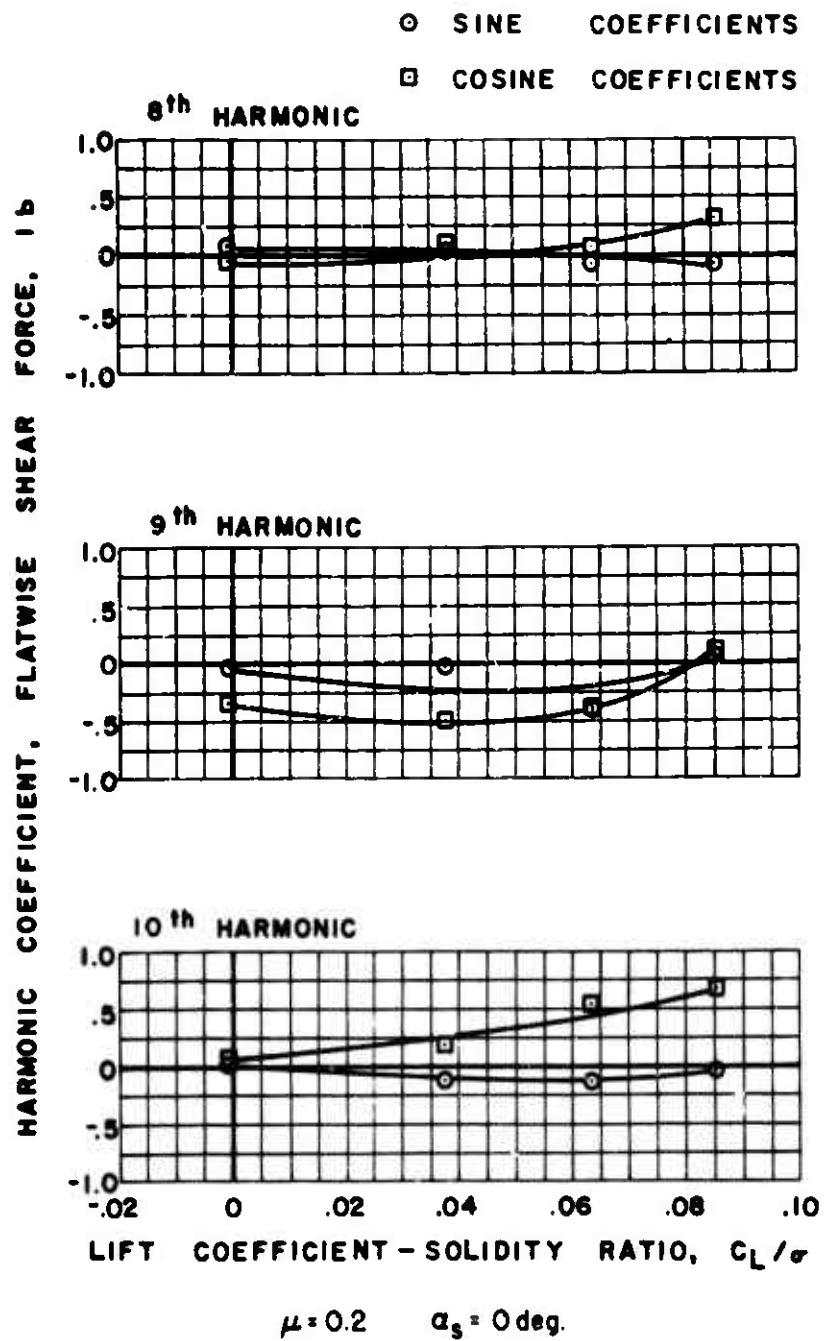
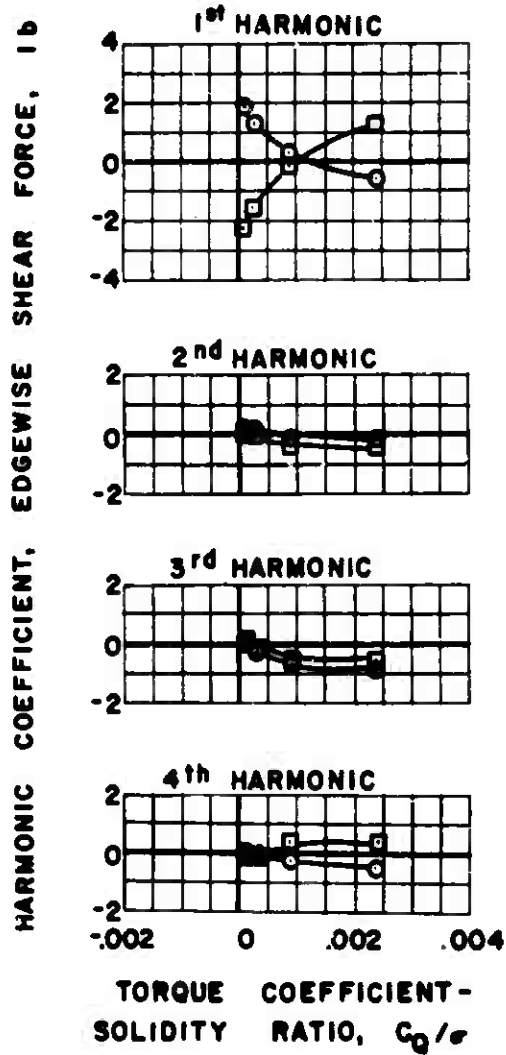


Figure 40(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.2$ $\alpha_s = 0 \text{ deg.}$

(b) EDGEWISE

Figure 40. Continued.

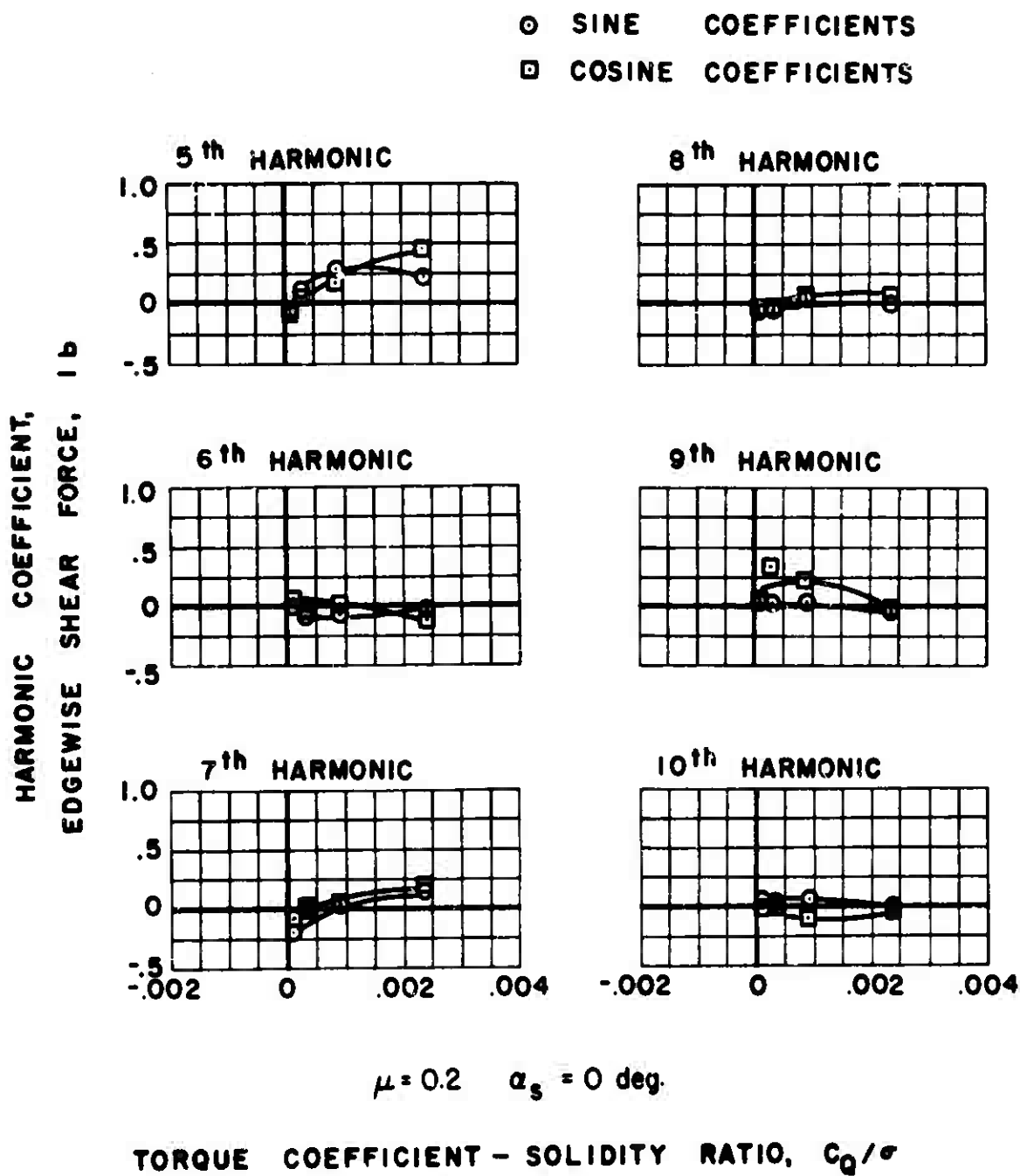


Figure 40(b). Concluded.

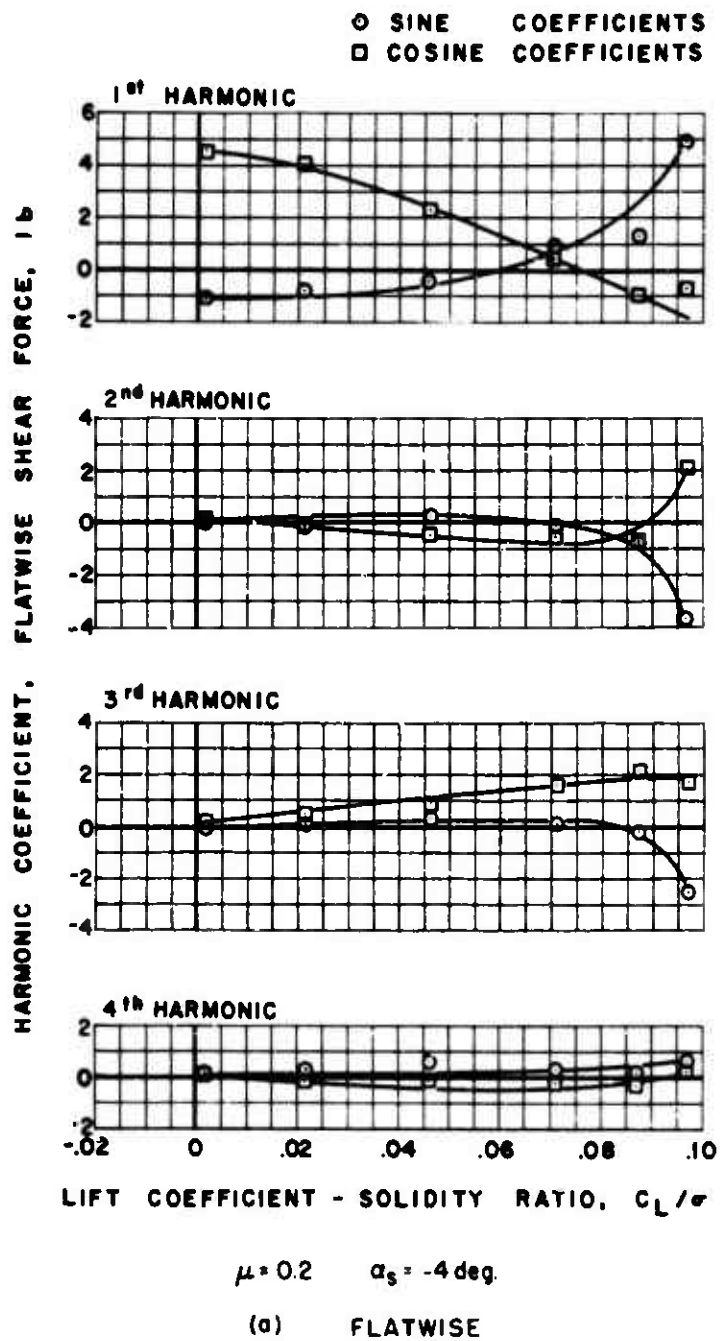


Figure 41. Experimental Shear Force.

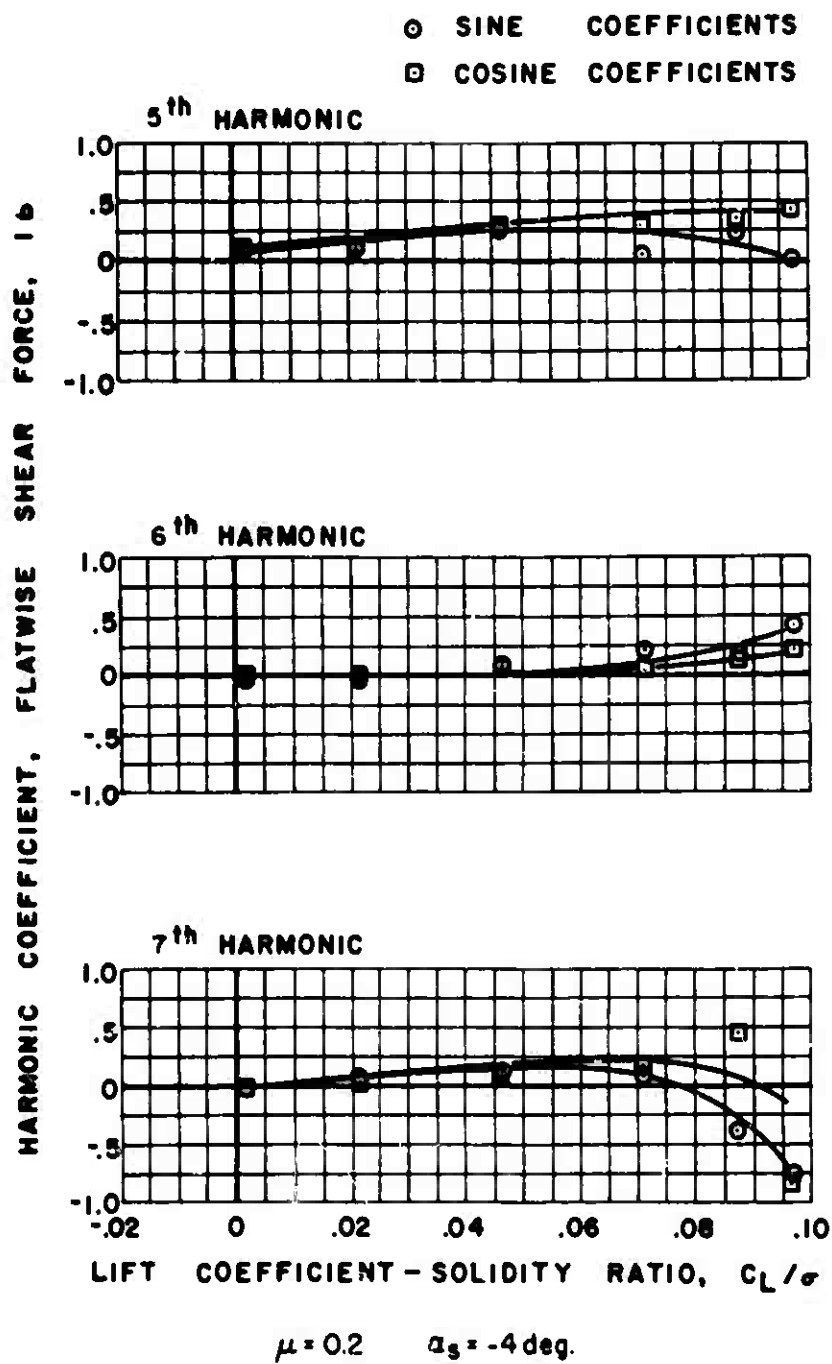


Figure 41(a). Continued.

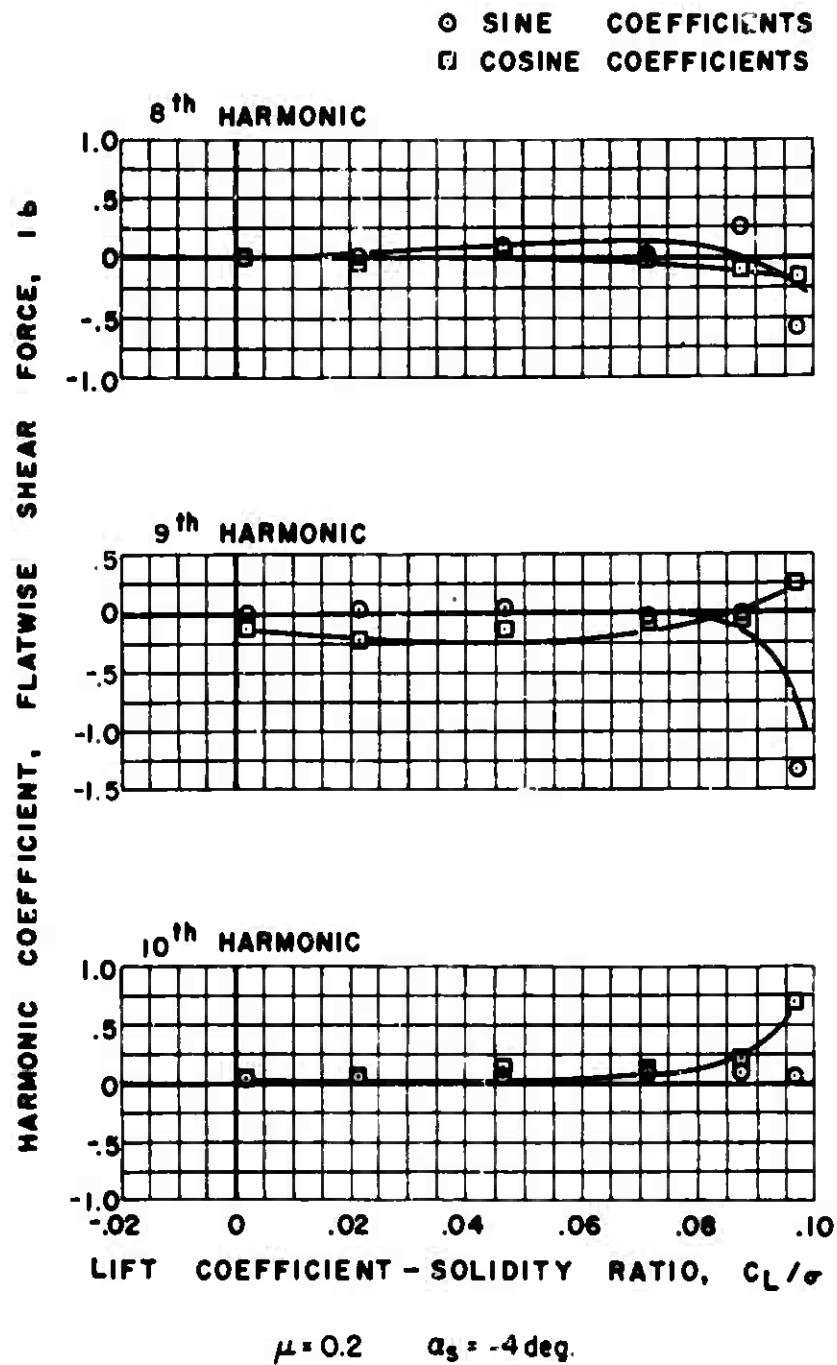
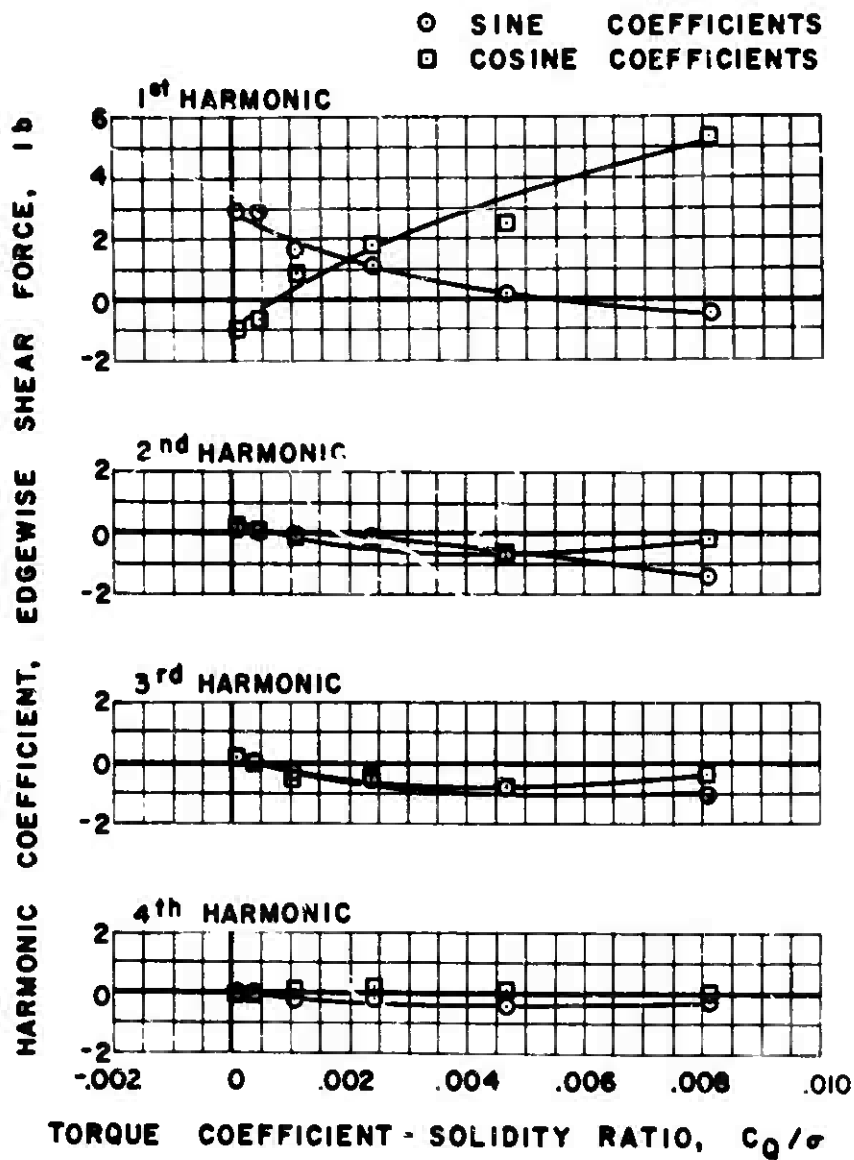


Figure 41(a). Continued.



$\mu = 0.2 \quad \alpha_s = -4 \text{ deg.}$

(b) EDGEWISE

Figure 41. Continued.

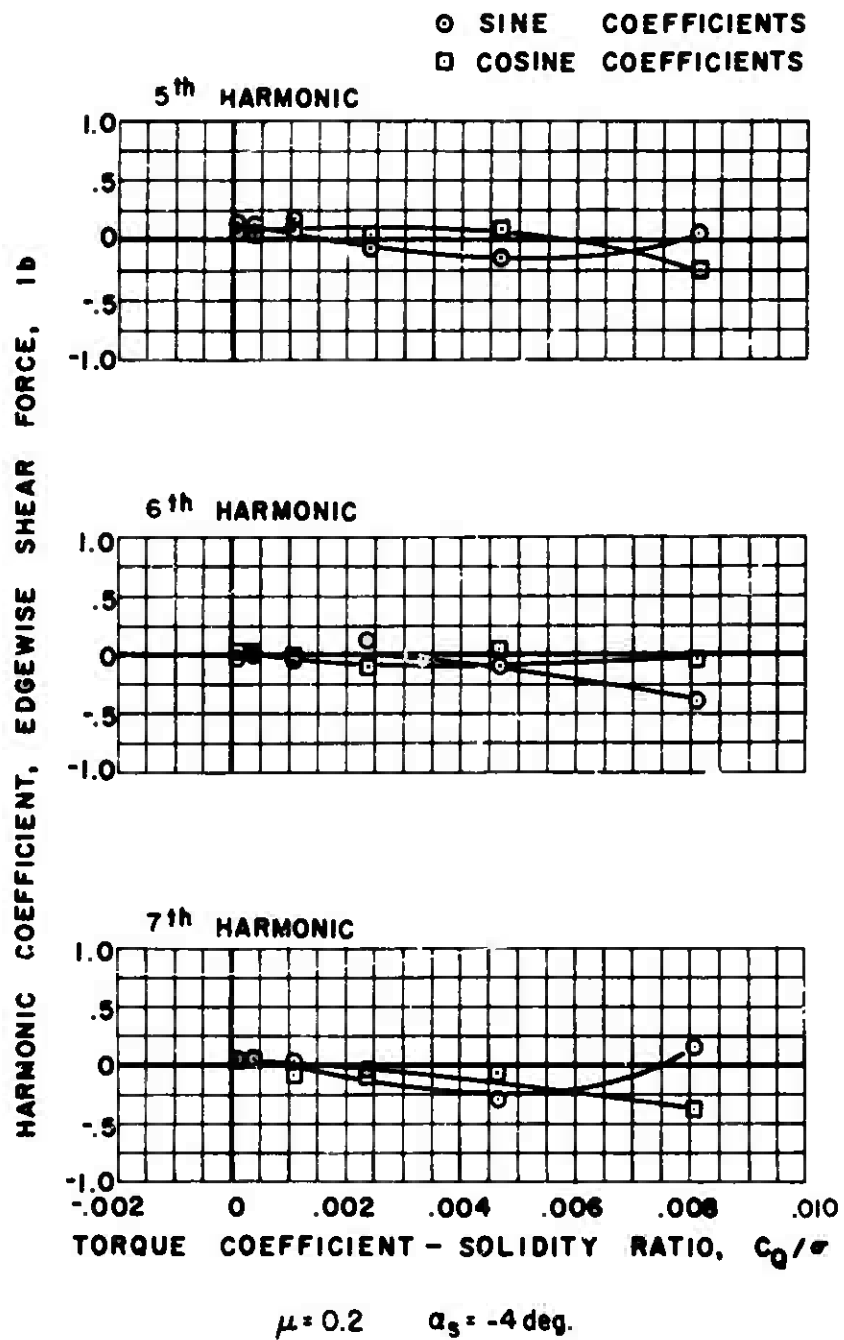
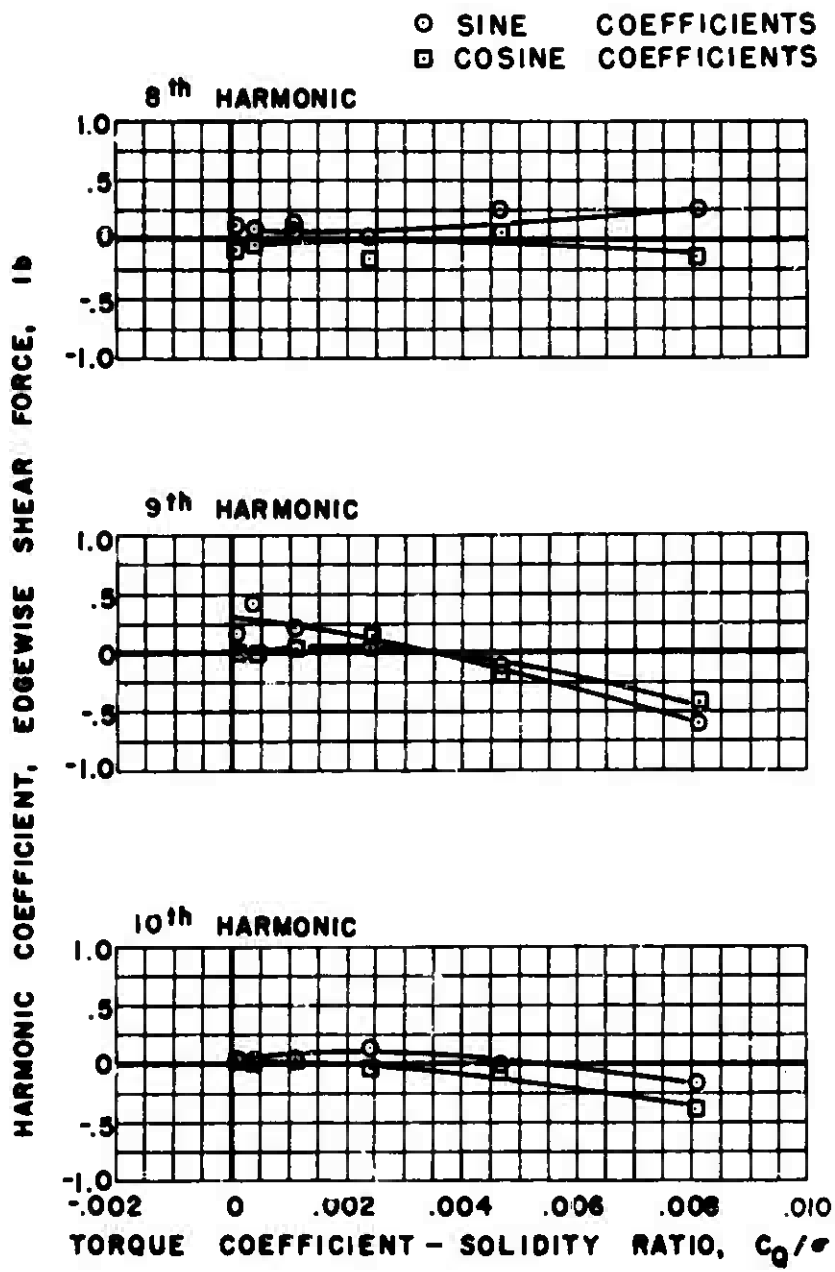
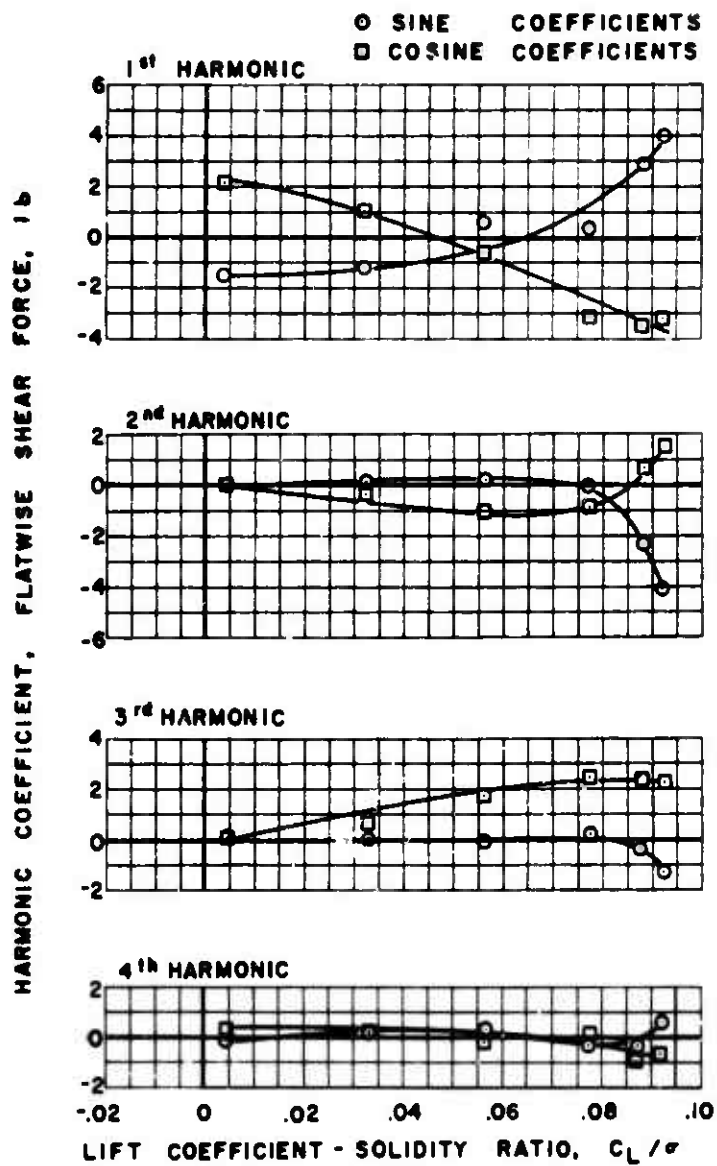


Figure 41(b). Continued.



$\mu = 0.2 \quad \alpha_s = -4 \text{ deg.}$

Figure 41(b). Concluded.



$\mu = 0.2 \quad \alpha_3 = -8 \text{ deg.}$

(a) FLATWISE

Figure 42. Experimental Shear Force.

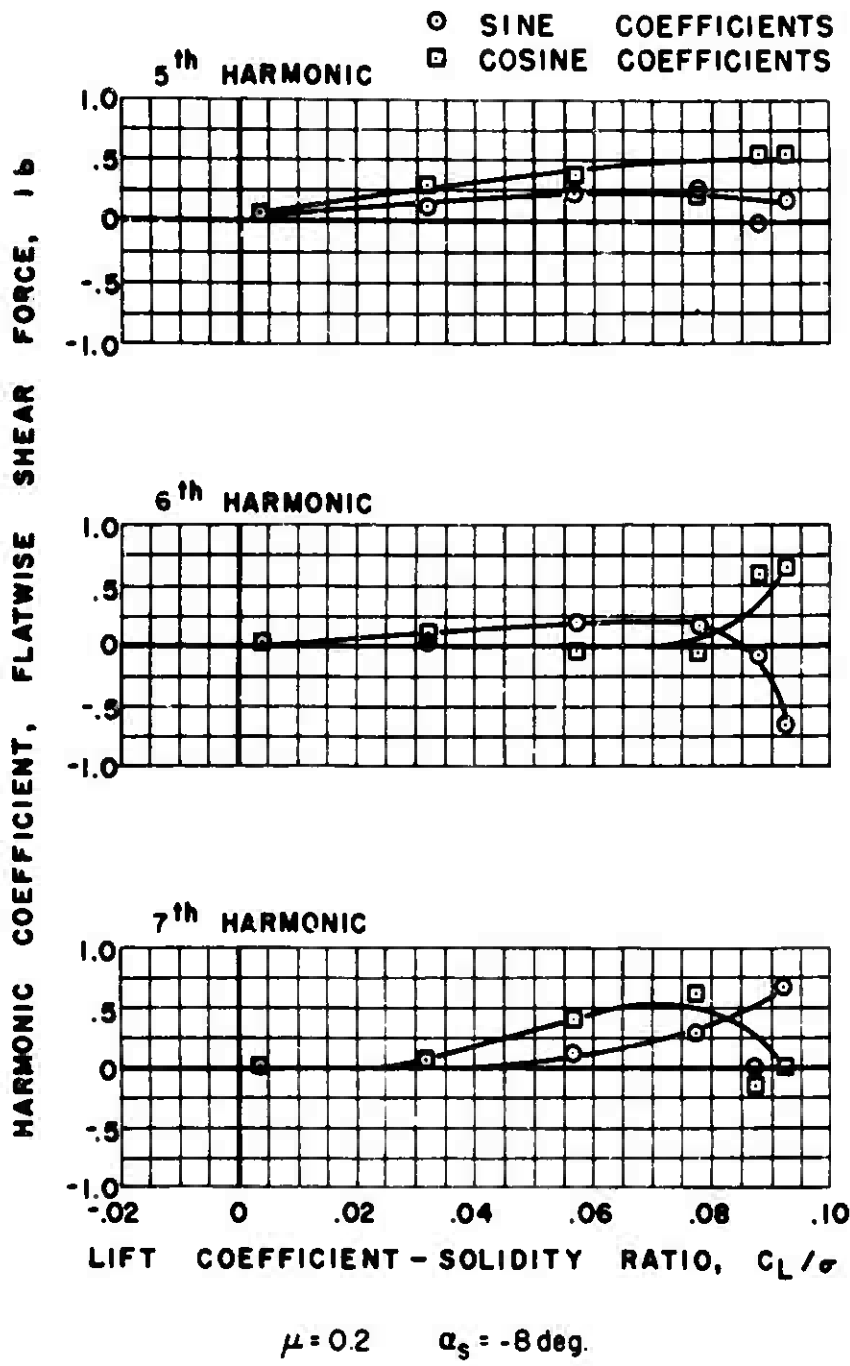
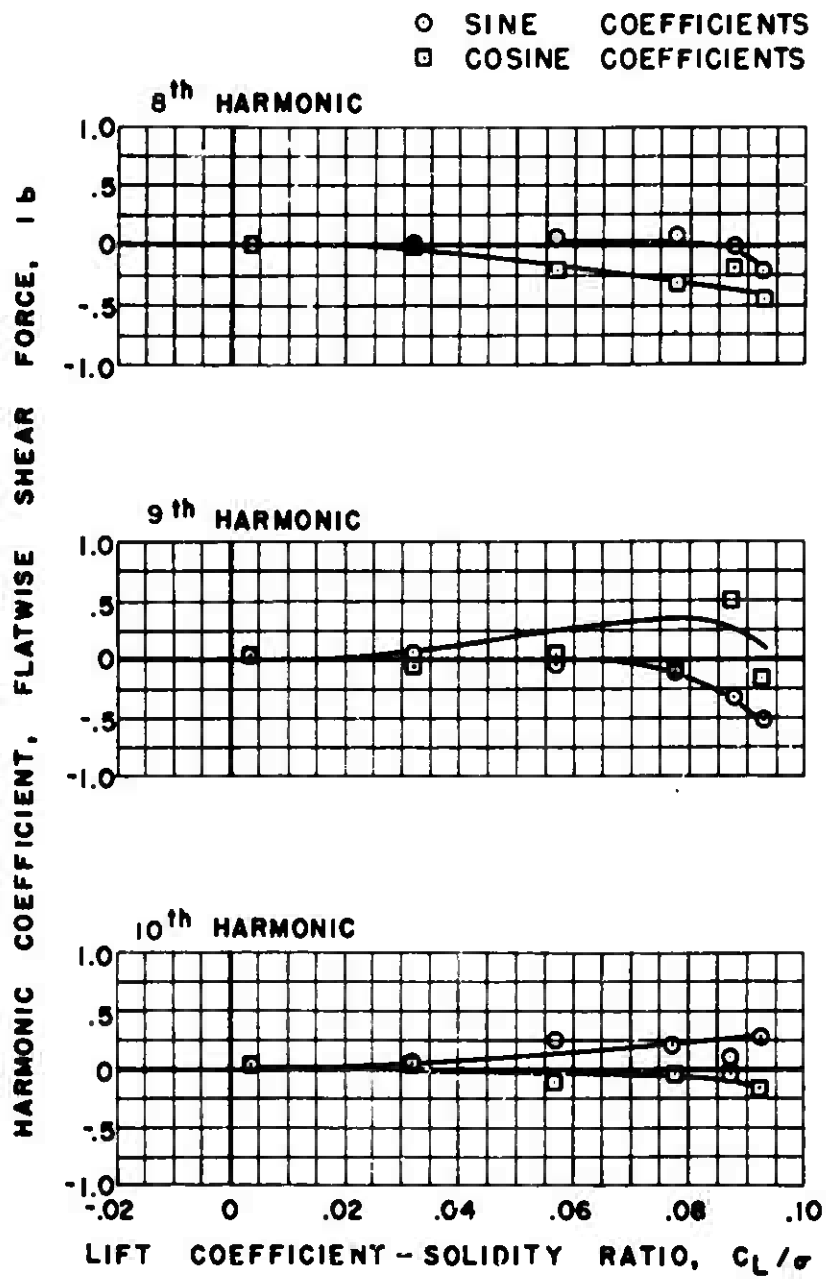
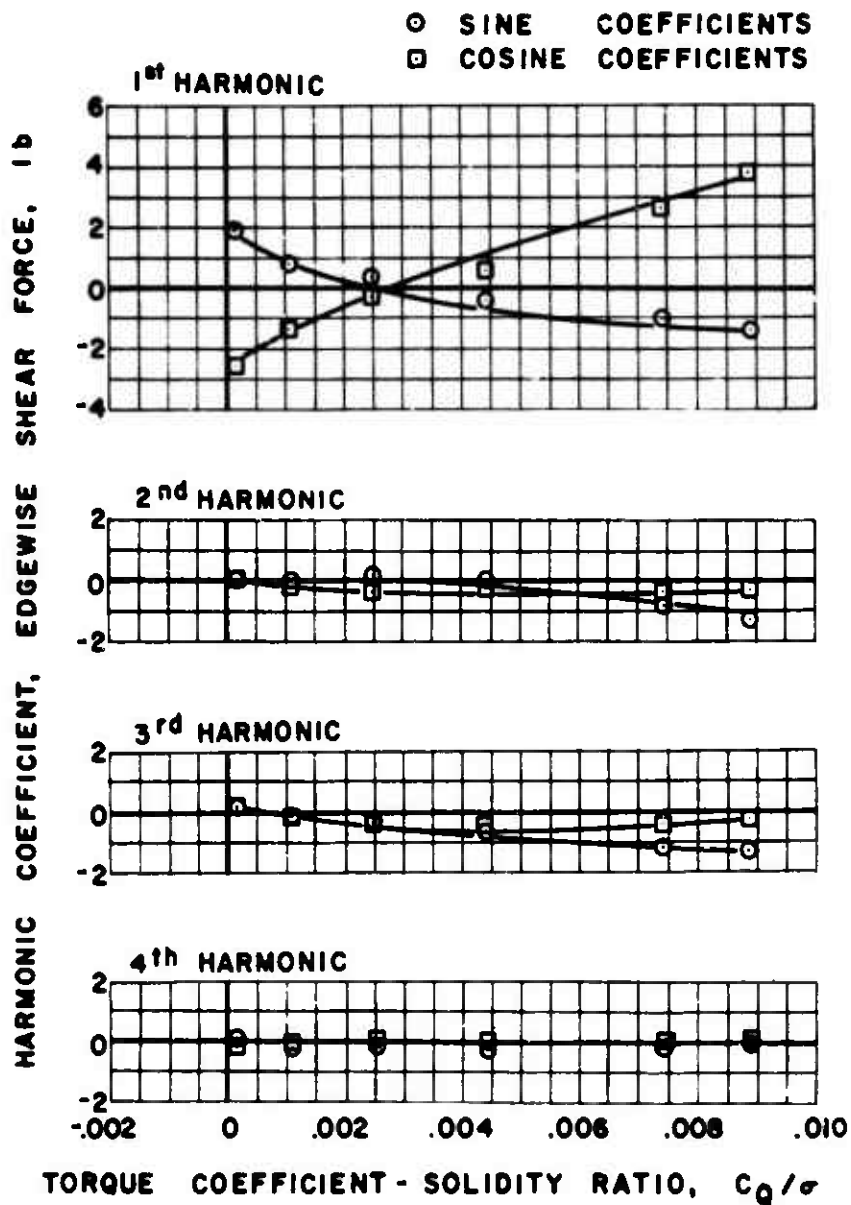


Figure 42(a). Continued.



$\mu = 0.2$ $\alpha_s = -8 \text{ deg.}$

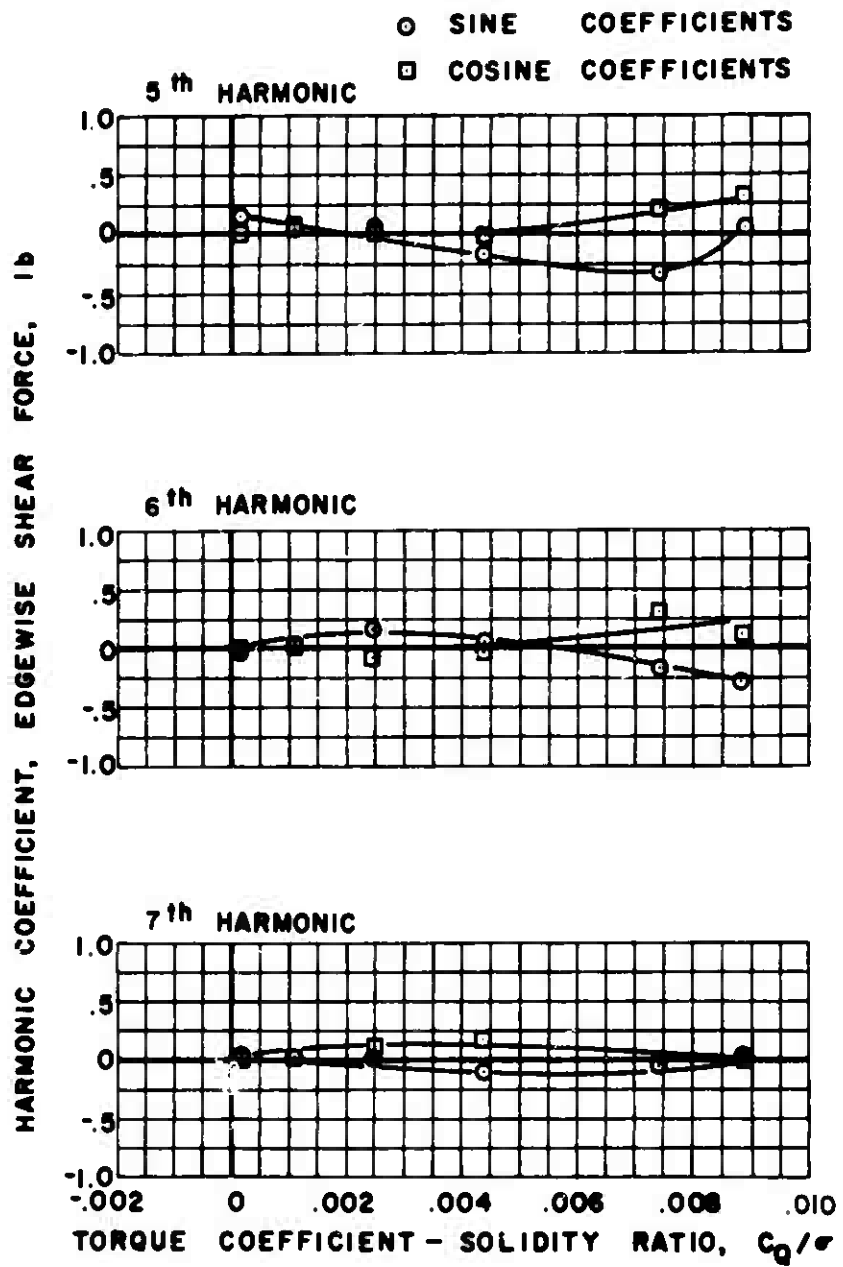
Figure 42(a). Continued.



$\mu = 0.2 \quad \alpha_s = -8 \text{ deg.}$

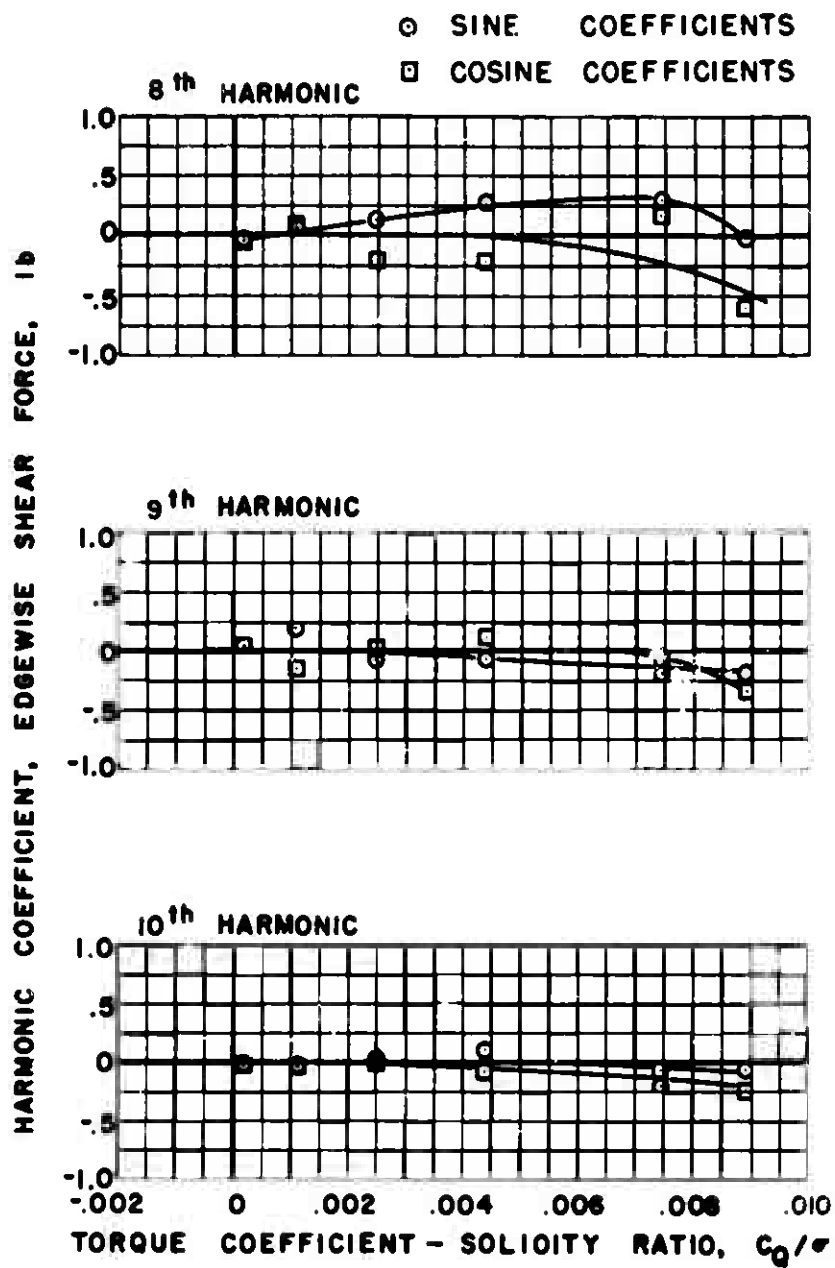
(b) EDGEWISE

Figure 42. Continued.



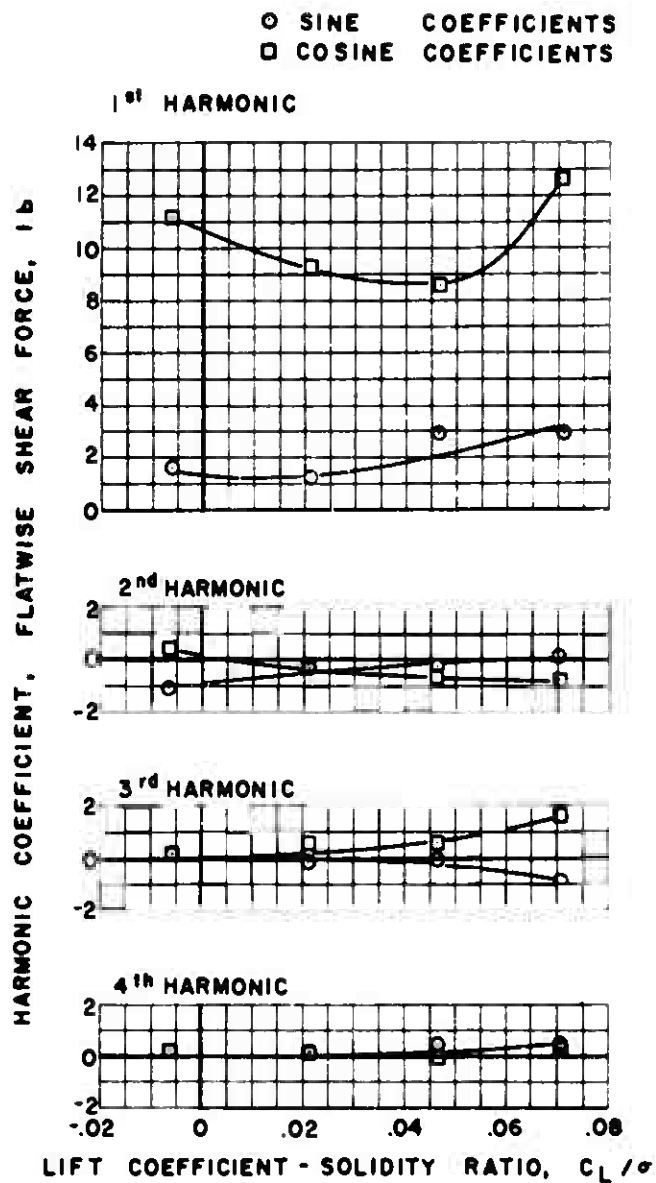
$\mu = 0.2 \quad \alpha_s = -8 \text{ deg.}$

Figure 42(b). Continued.



$\mu = 0.2 \quad \alpha_s = -8 \text{ deg.}$

Figure 42(b). Concluded.



$\mu = 0.2 \quad \alpha_s = 0 \text{ deg.}$

(a) FLATWISE

Figure 43. Experimental Shear Force, Out of Trim, -4 Degree Longitudinal Flapping.

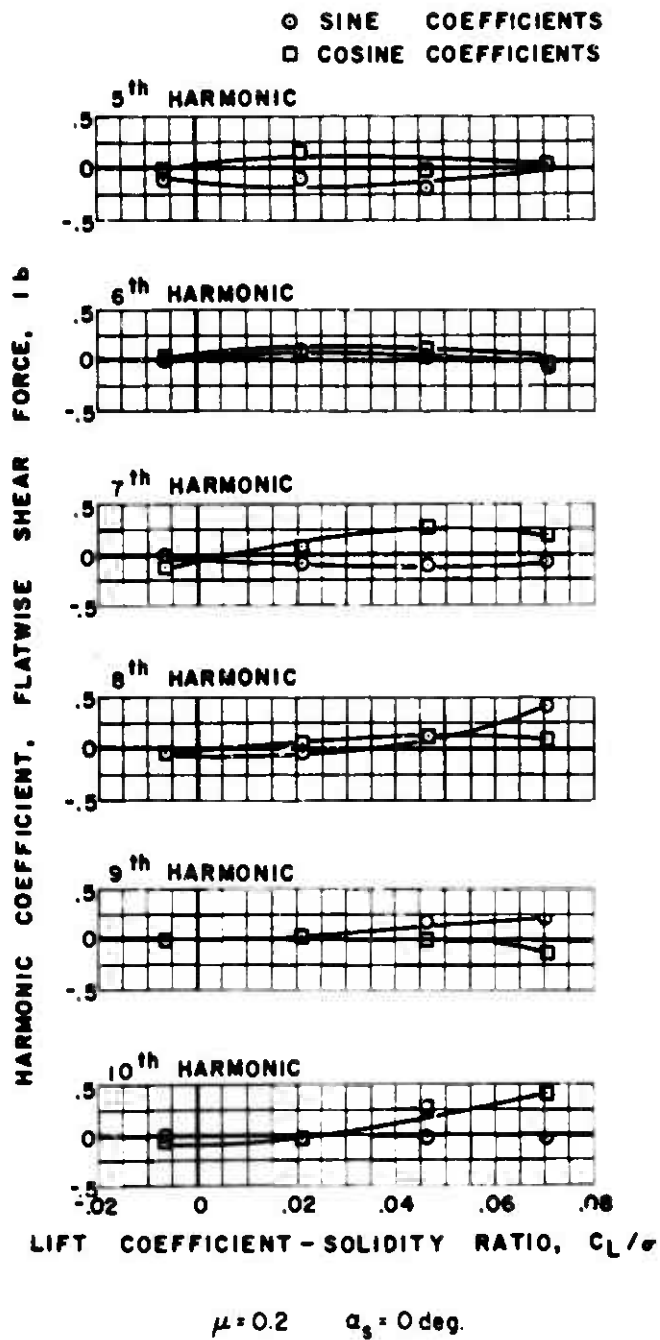
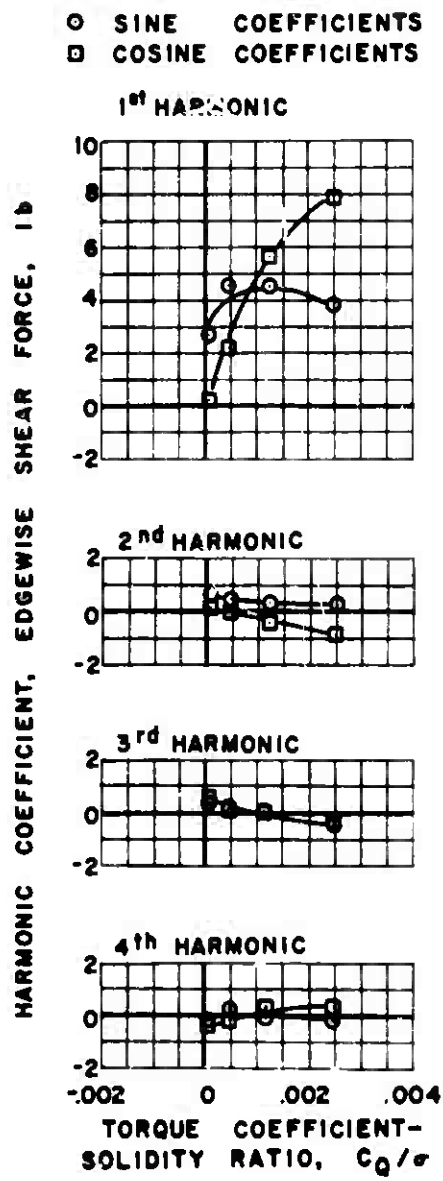


Figure 43(a). Continued

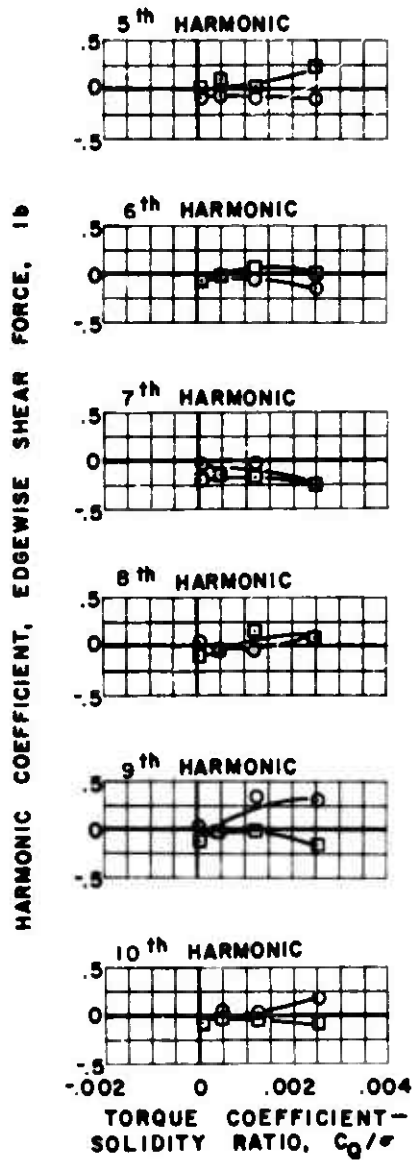


$\mu = 0.2 \quad \alpha_s = 0 \text{ deg.}$

(b) EDGEWISE

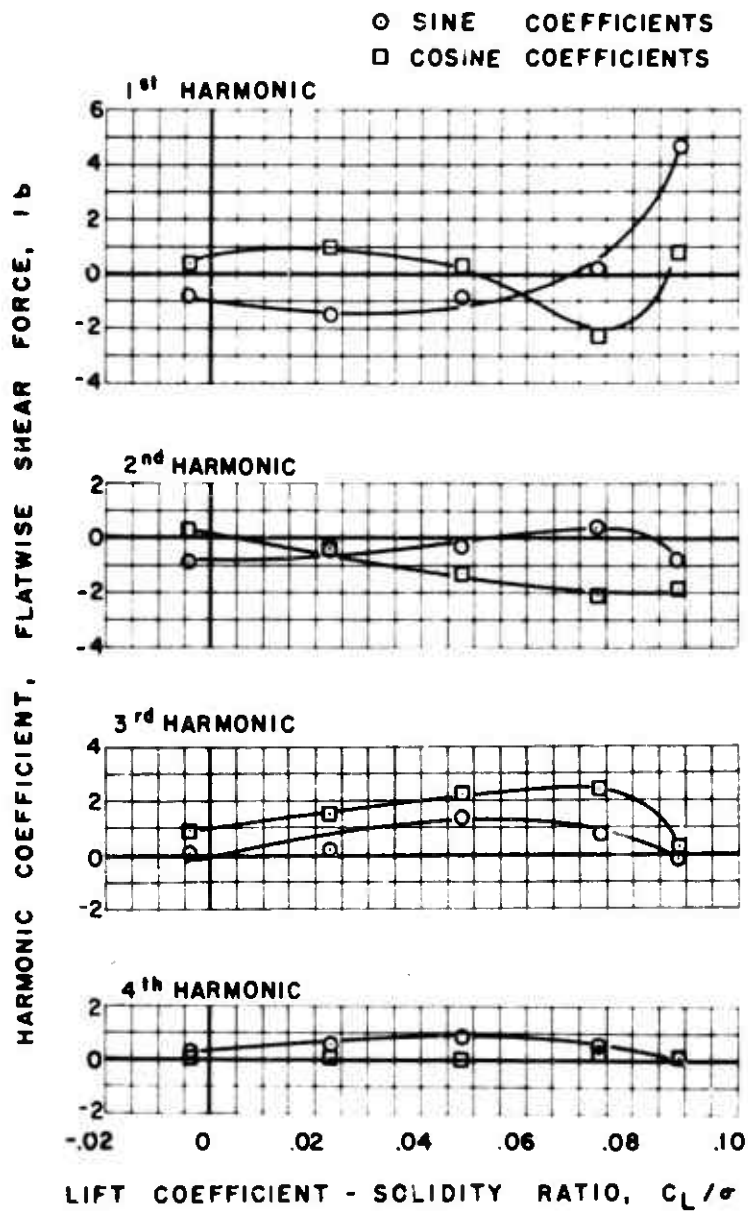
Figure 43. Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.2$ $\alpha_s = 0 \text{ deg.}$

Figure 43(b). Concluded.



$\mu = 0.2 \quad \alpha_s = -4 \text{ deg}$

(a) FLATWISE

Figure 44. Experimental Shear Force, Zero Lag Damping.

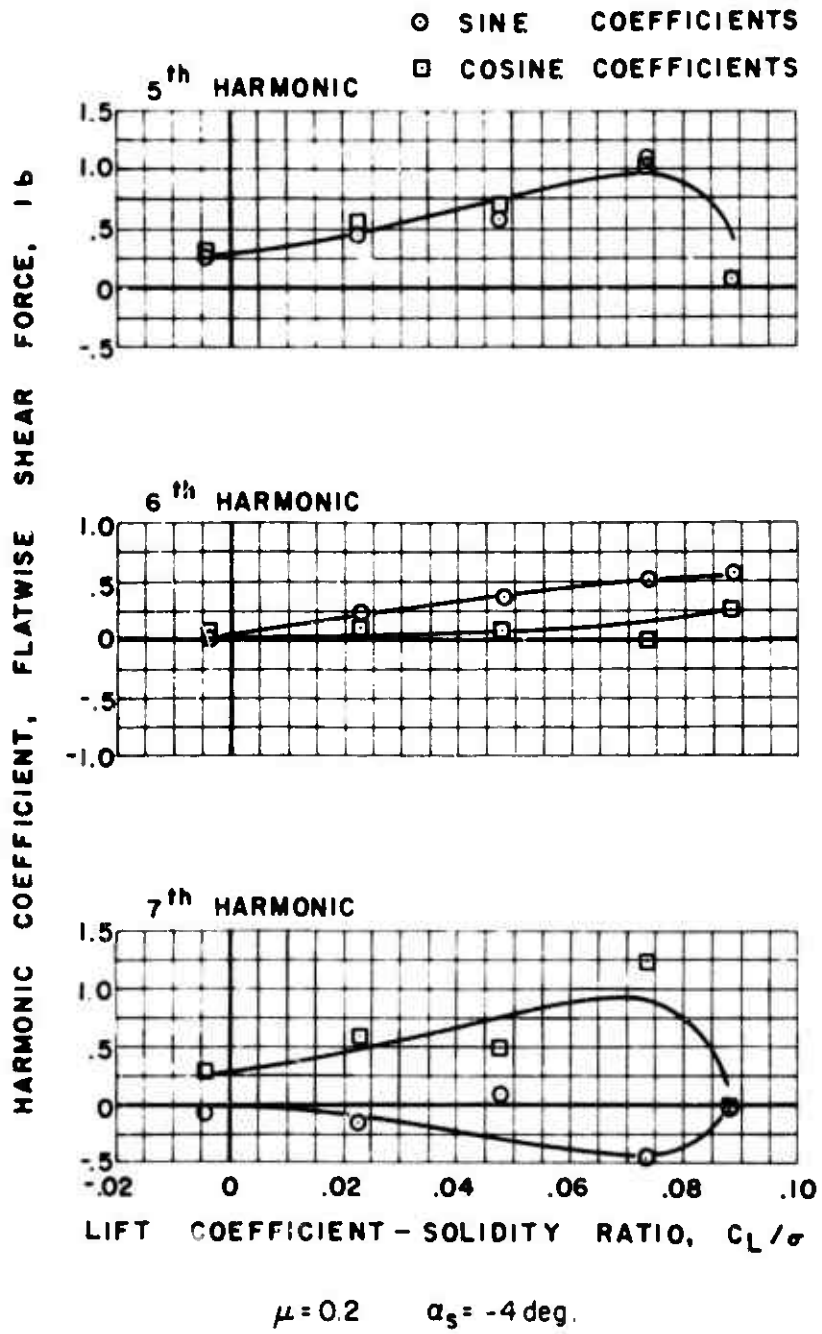


Figure 44(a). Continued.

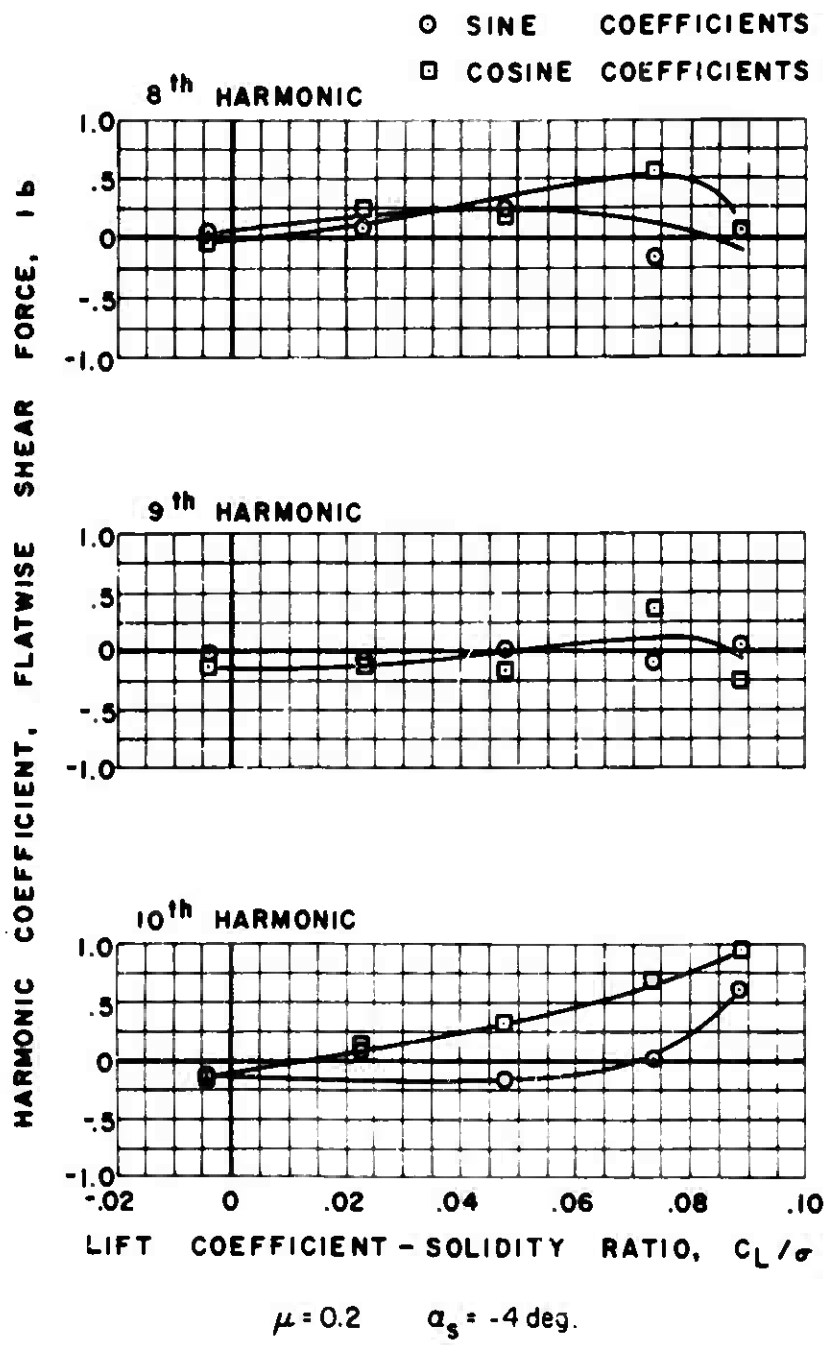
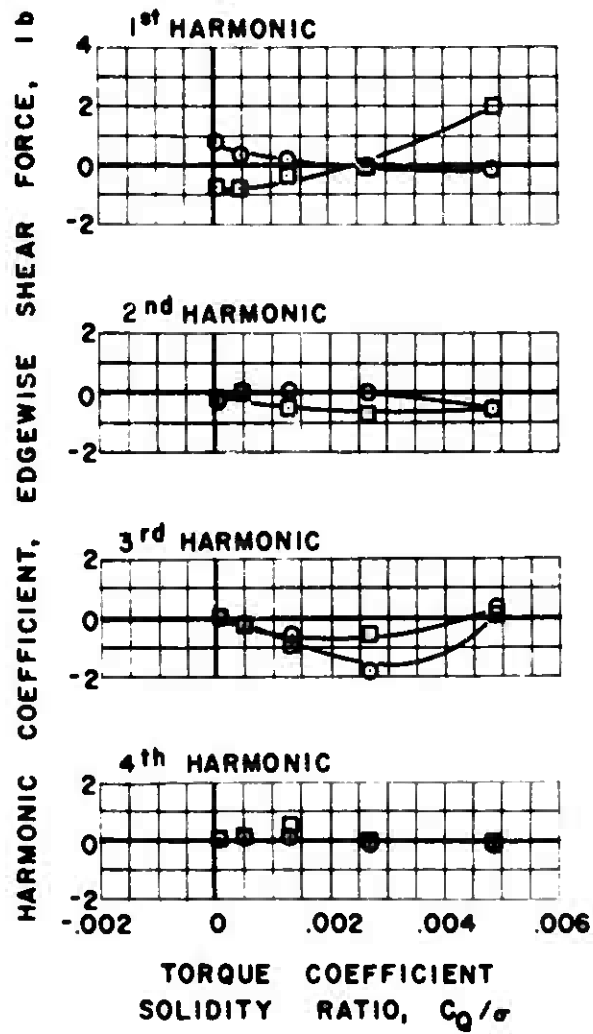


Figure 44(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.2$ $\alpha_s = -4$ deg.

(b) EDGEWISE

Figure 44. Continued.

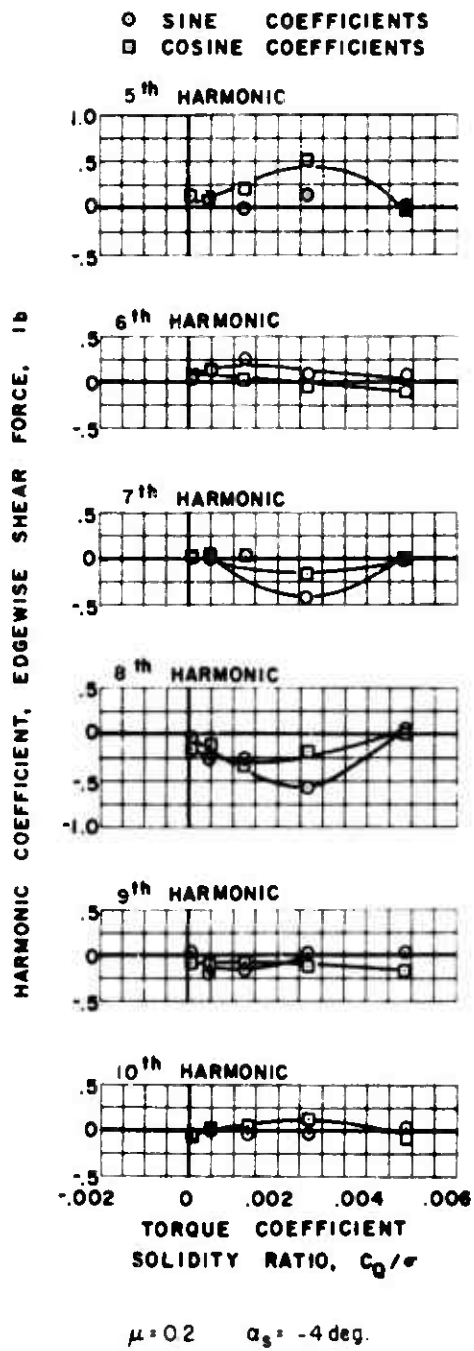
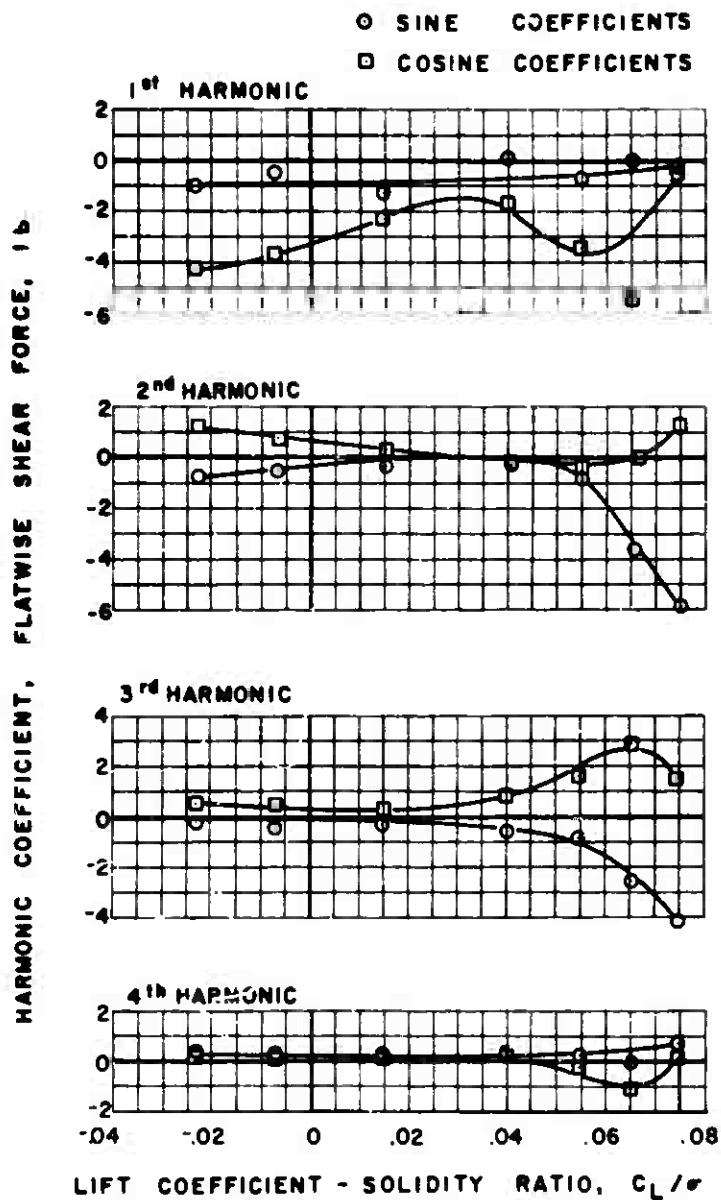


Figure 44(b). Concluded.



$\mu = 0.3 \quad \alpha_s = 0 \text{ deg.}$

(a) FLATWISE

Figure 45. Experimental Shear Force.

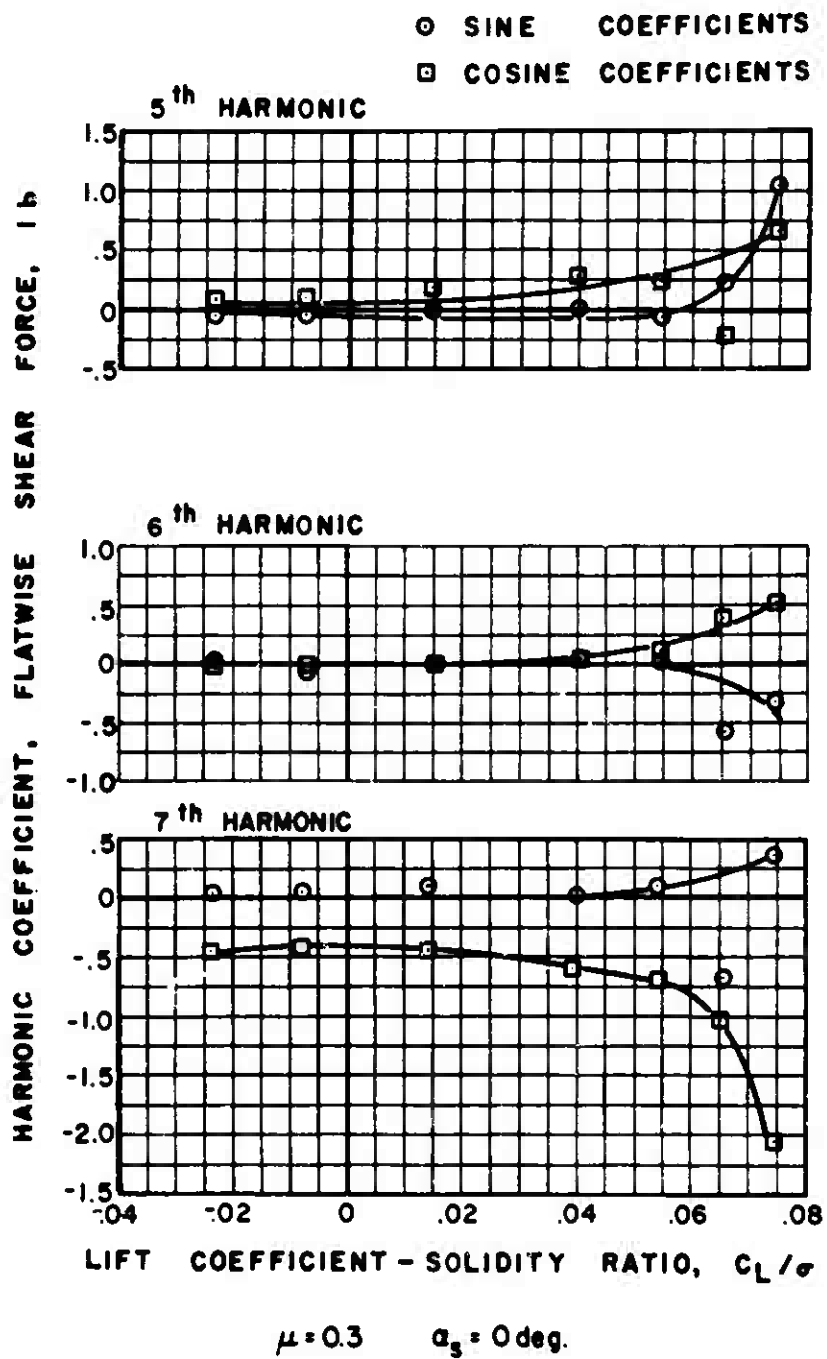


Figure 45(a). Continued.

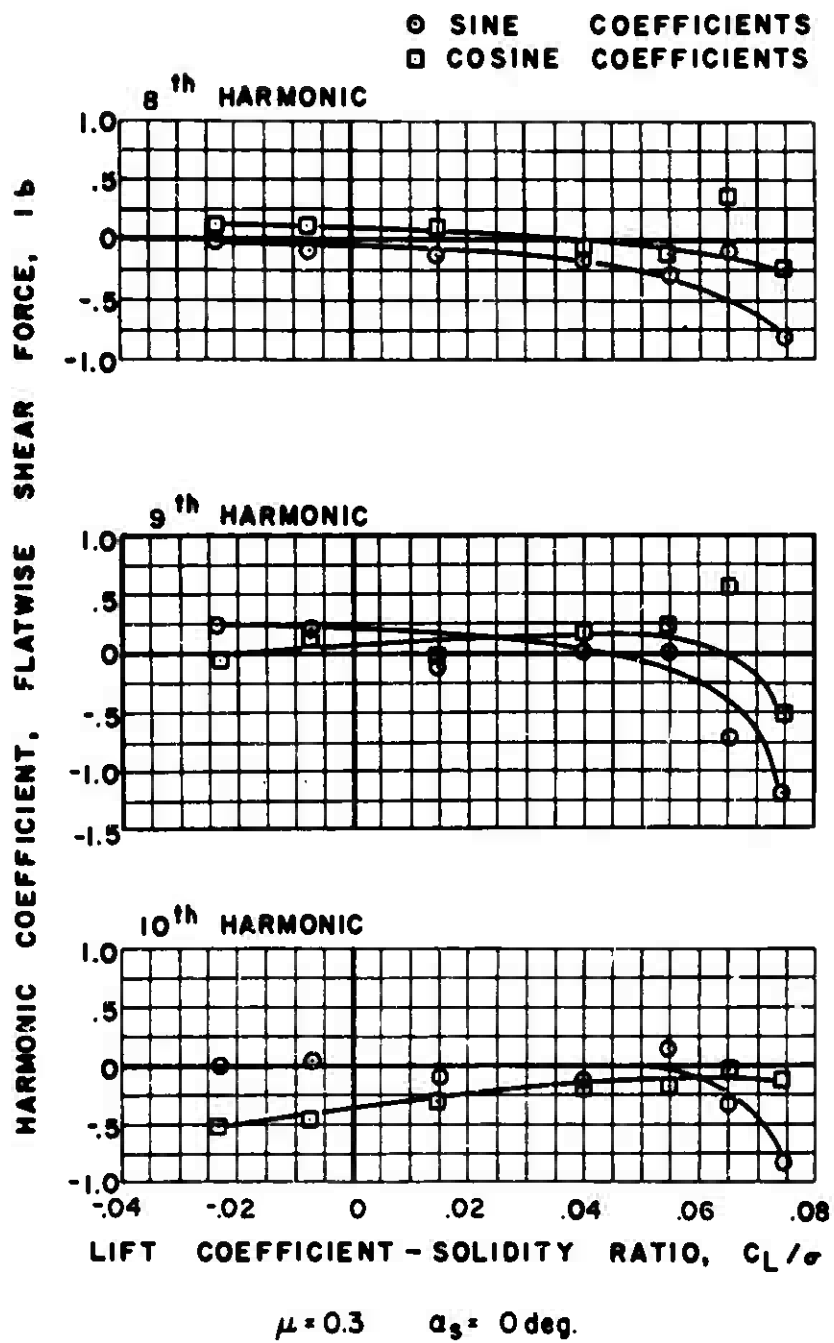
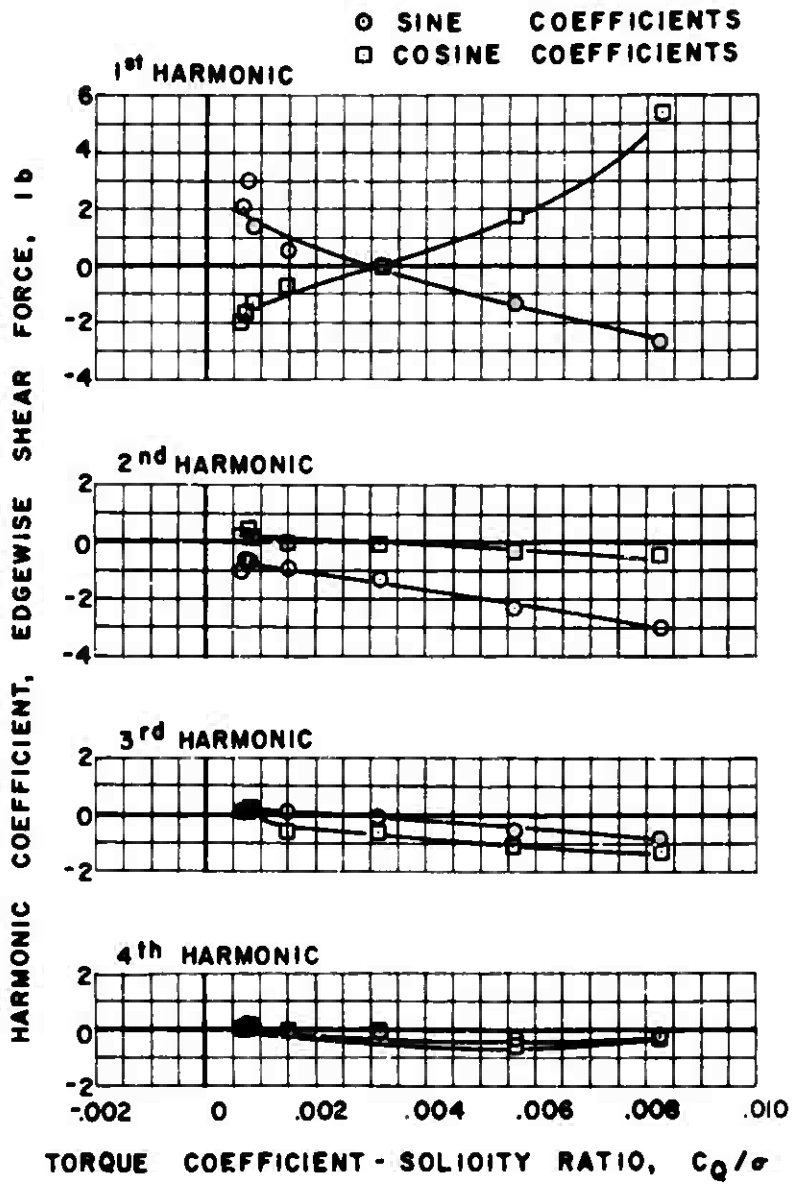


Figure 45(a). Continued.



$\mu = 0.3 \quad \alpha_s = 0 \text{ deg.}$

(b) EDGEWISE

Figure 45. Continued.

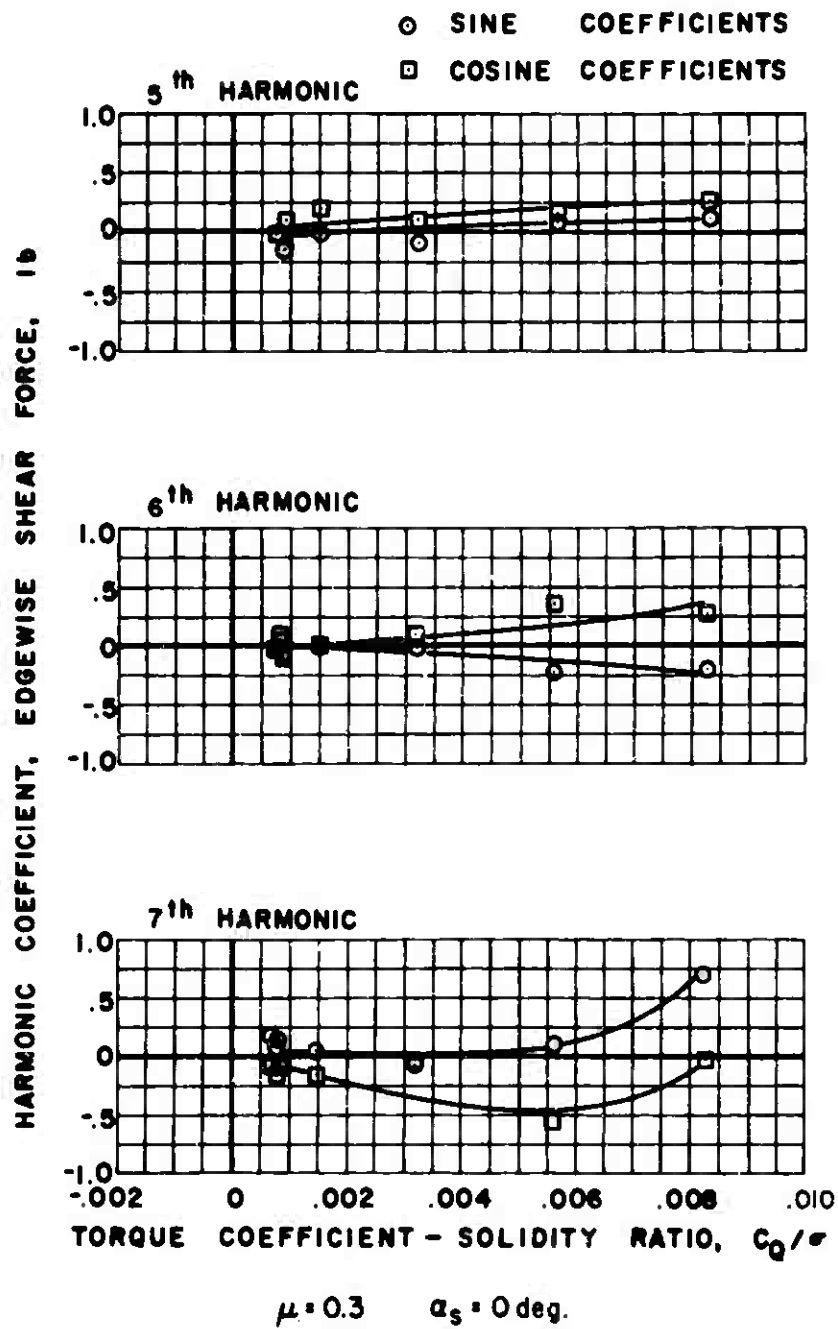


Figure 45(b). Continued.

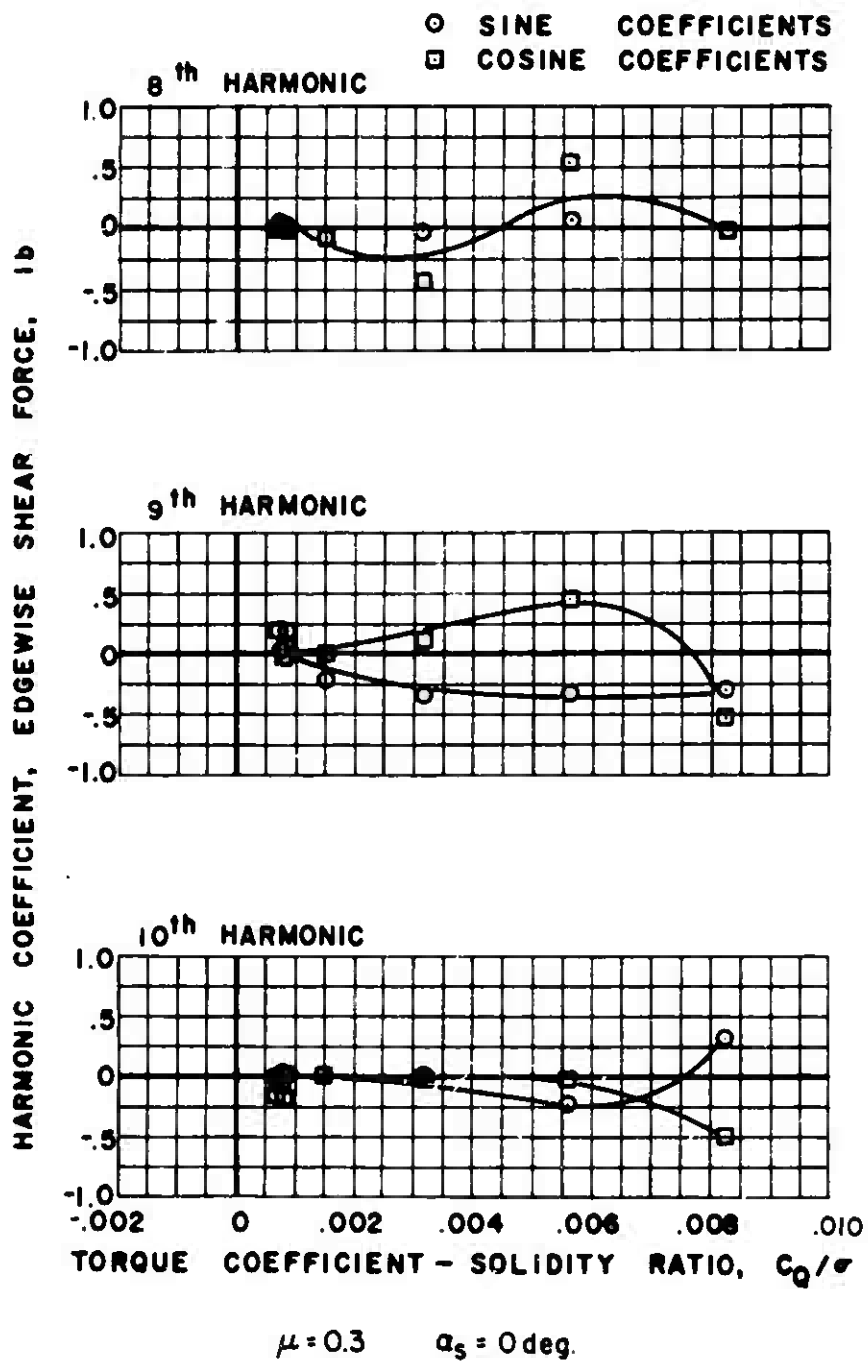
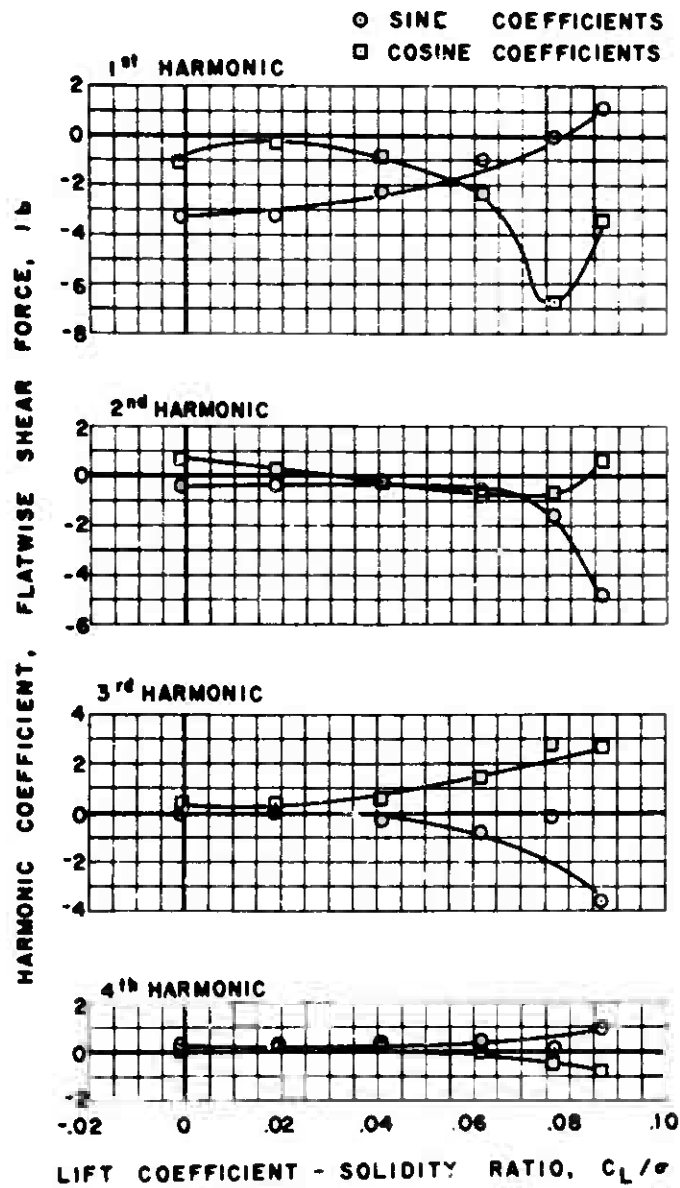


Figure 45(b). Concluded.



$\mu = 0.3 \quad \alpha_s = -4 \text{ deg.}$

(a) FLATWISE

Figure 46. Experimental Shear Force.

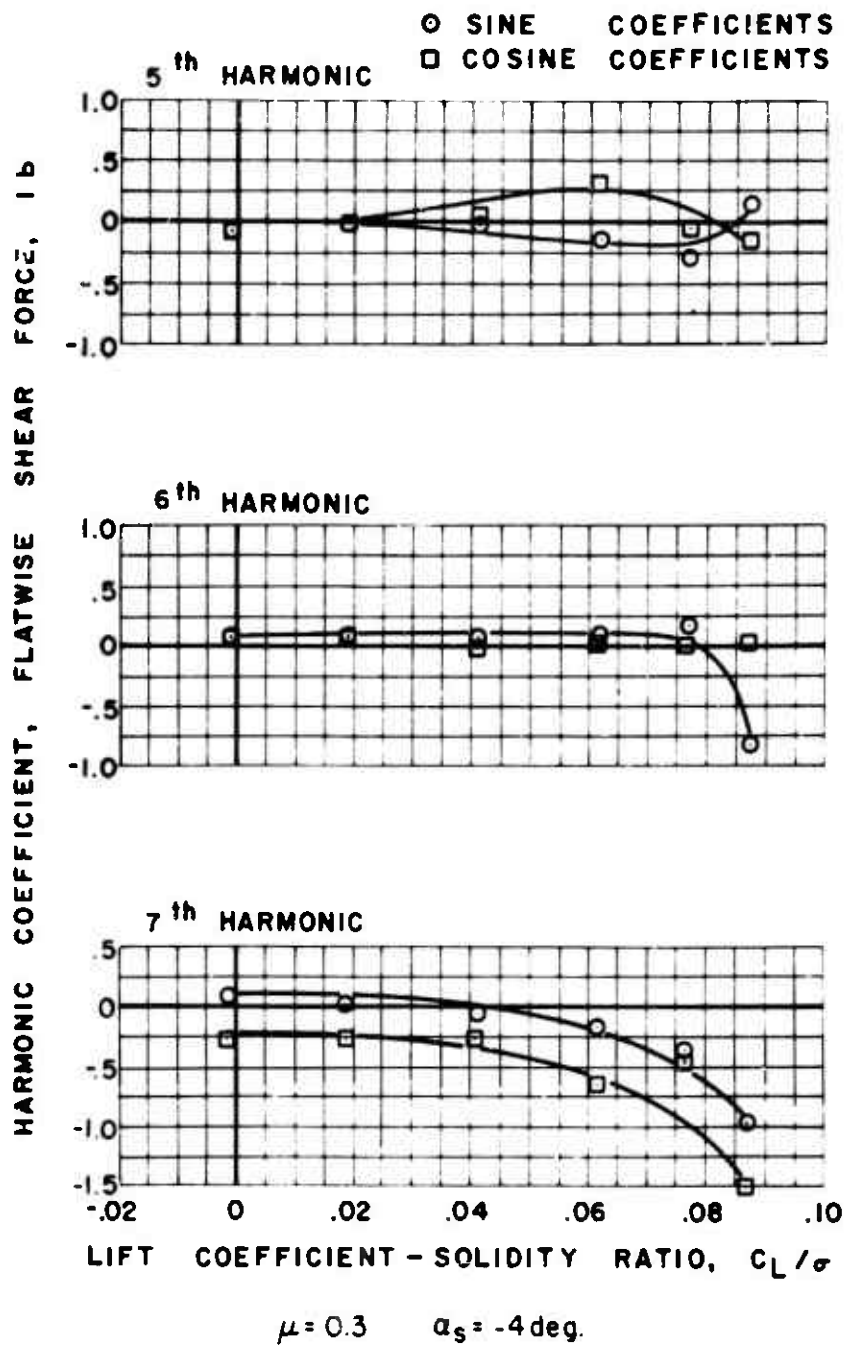


Figure 46(a). Continued.

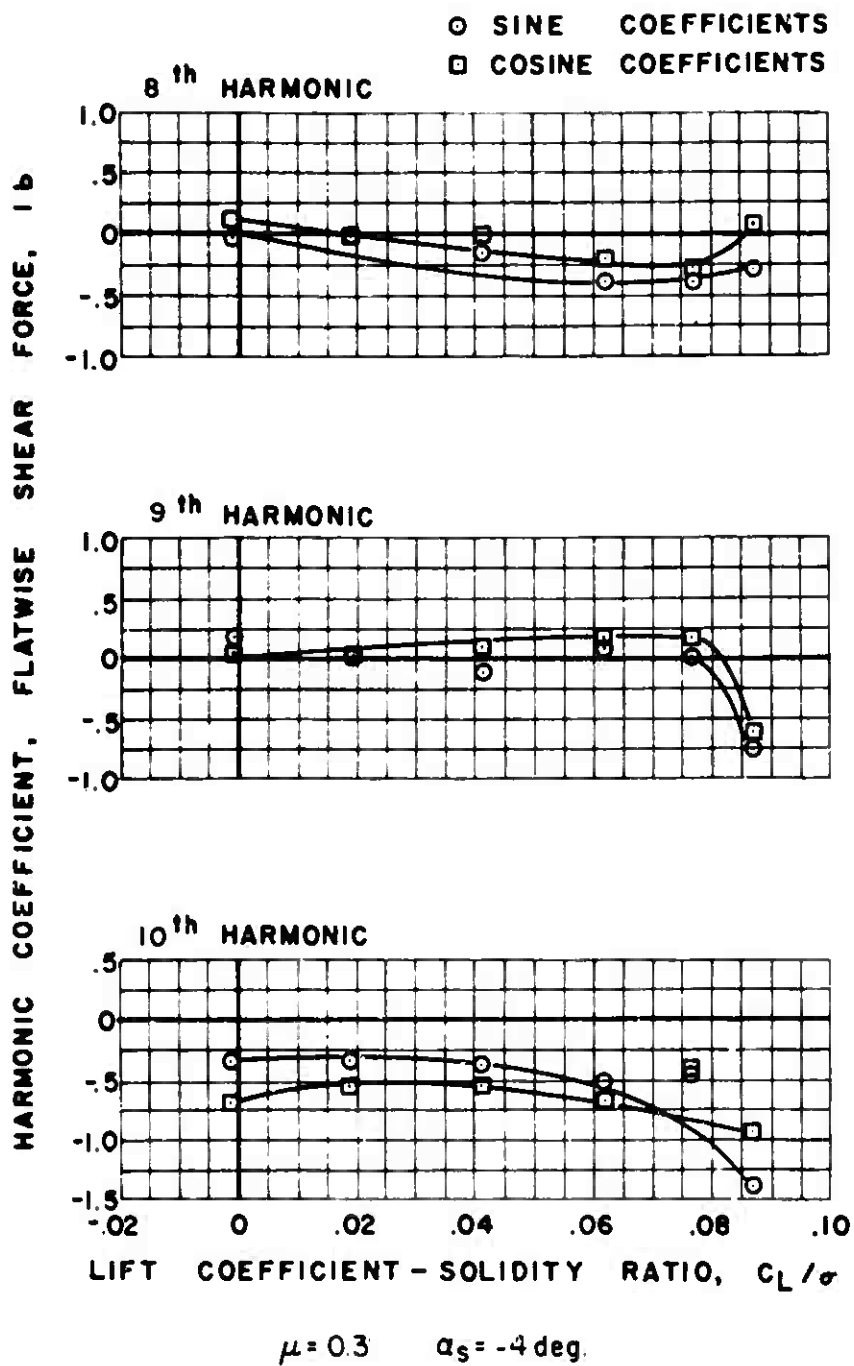
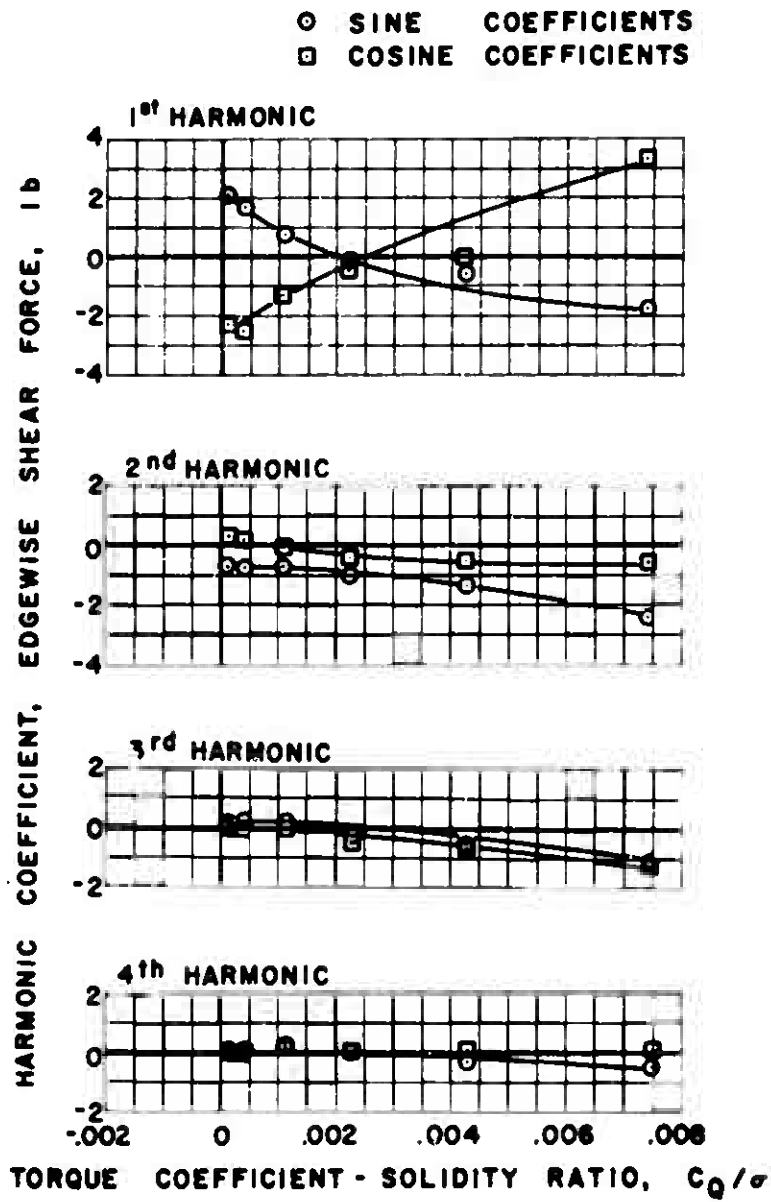


Figure 46(a). Continued.



$\mu = 0.3$ $\alpha_s = -4\text{deg.}$

(b) EDGEWISE

Figure 46. Continued.

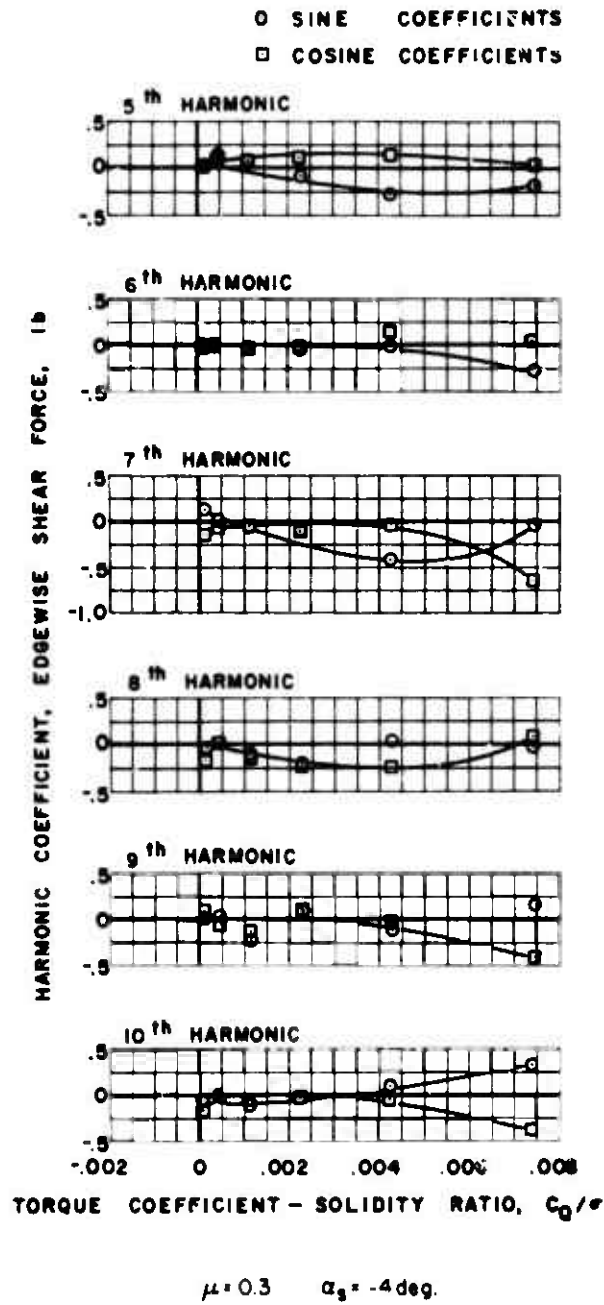


Figure 46(b). Concluded.

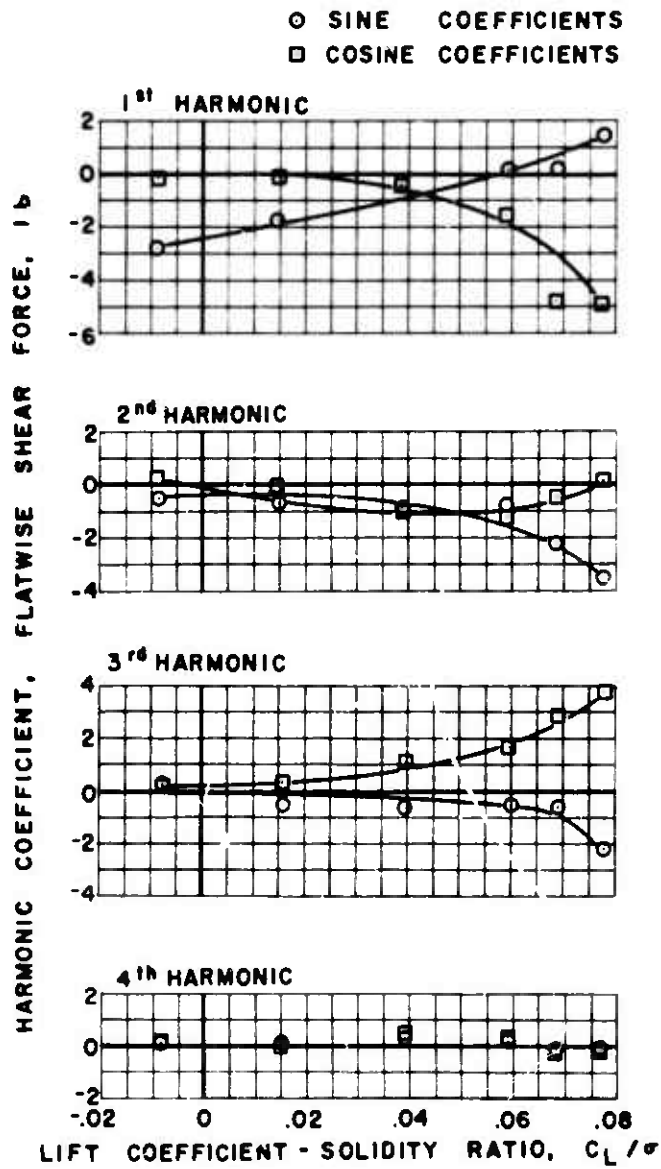
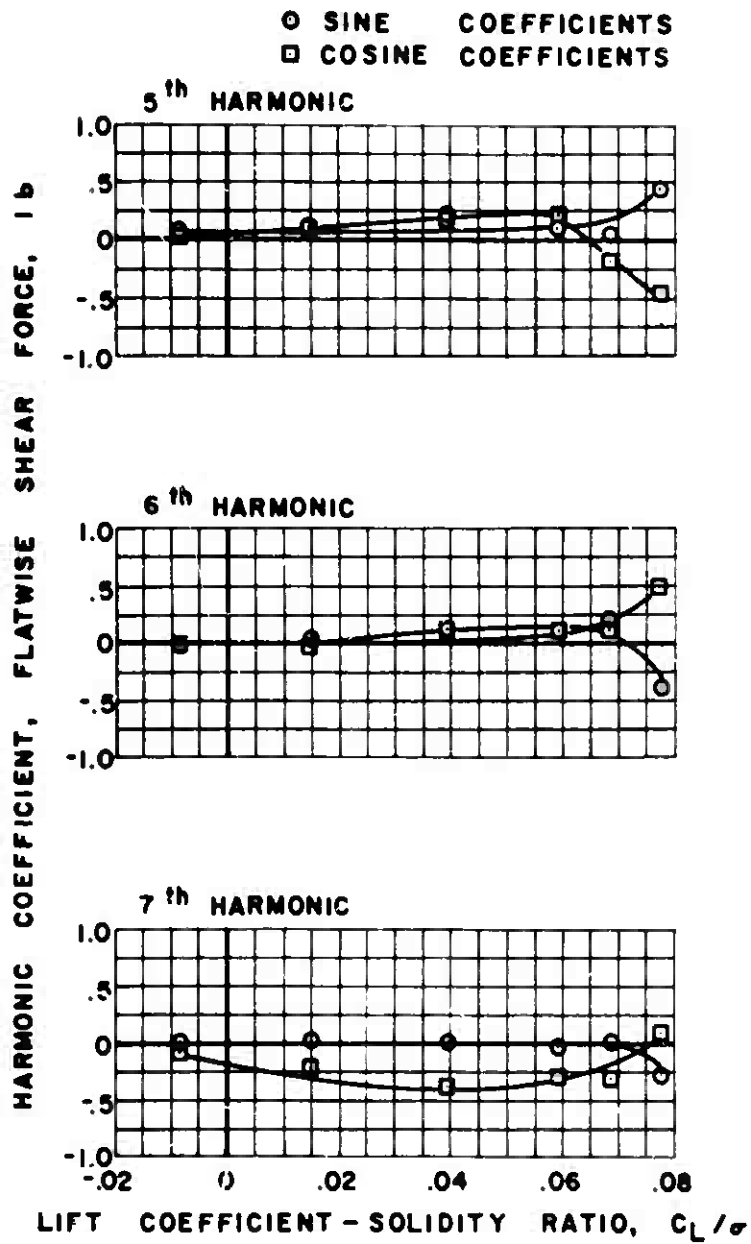
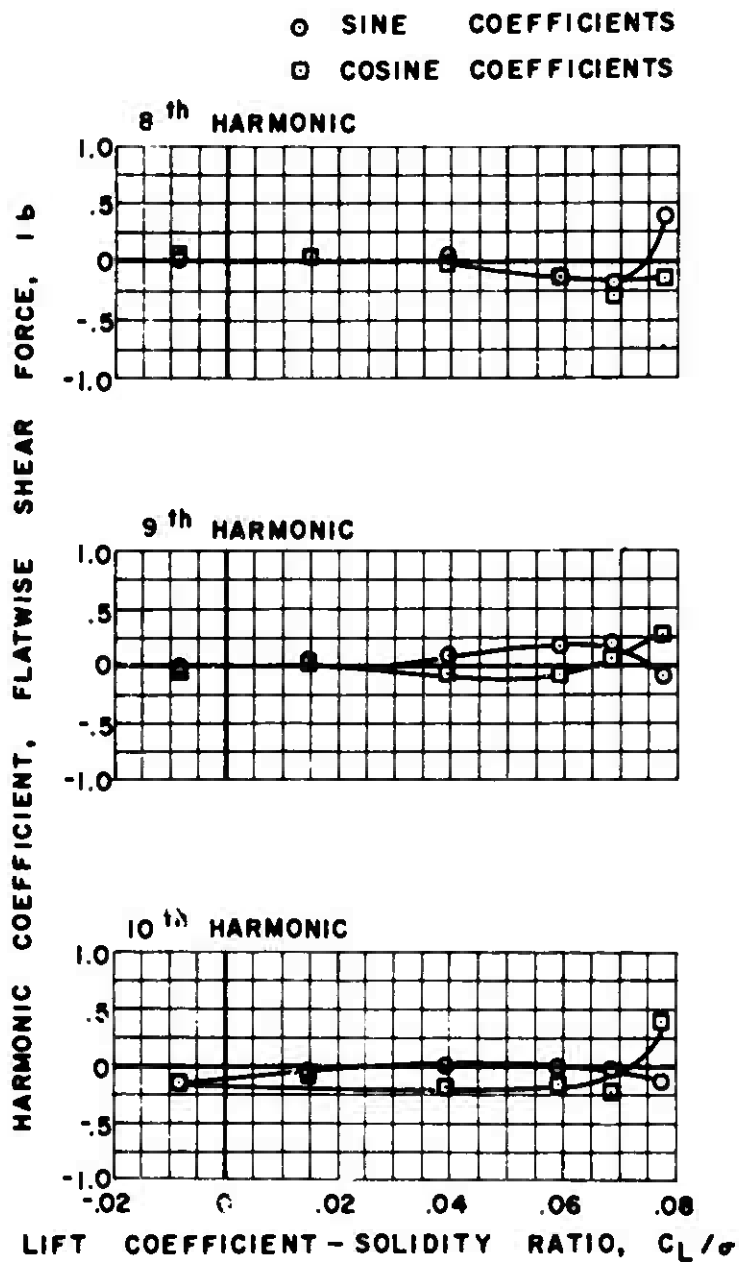


Figure 47. Experimental Shear Force.



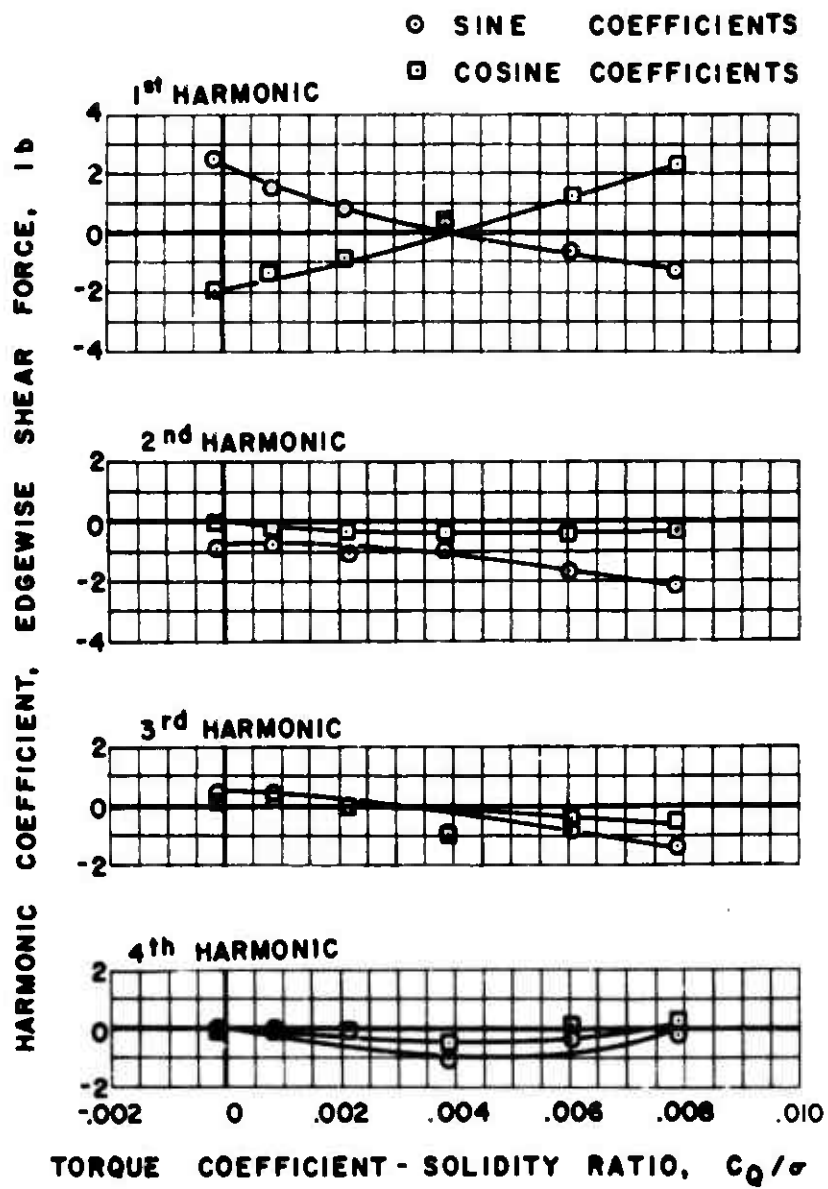
$\mu = 0.3 \quad \alpha_s = -8 \text{ deg.}$

Figure 47(a). Continued.



$\mu = 0.3 \quad \alpha_s = -8 \text{ deg.}$

Figure 47(a). Continued.



$\mu = 0.3 \quad \alpha_s = -8 \text{ deg.}$

(b) EDGEWISE

Figure 47. Continued.

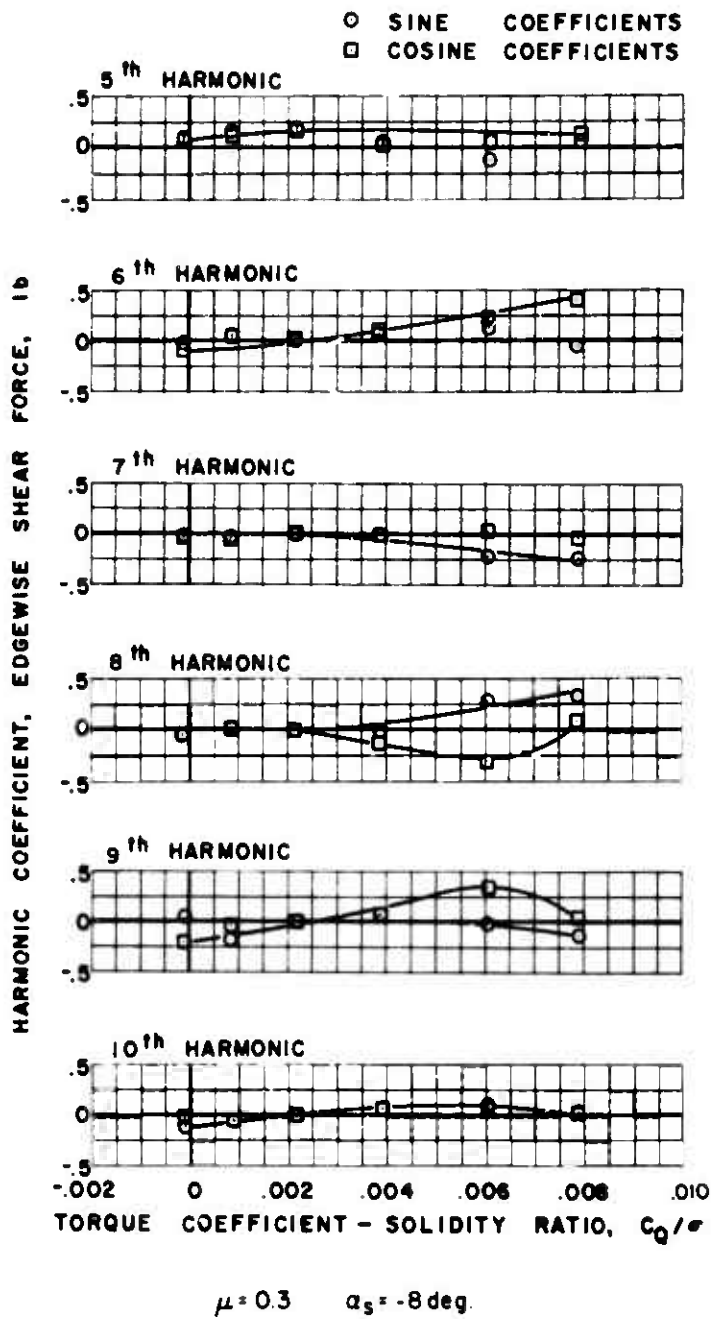
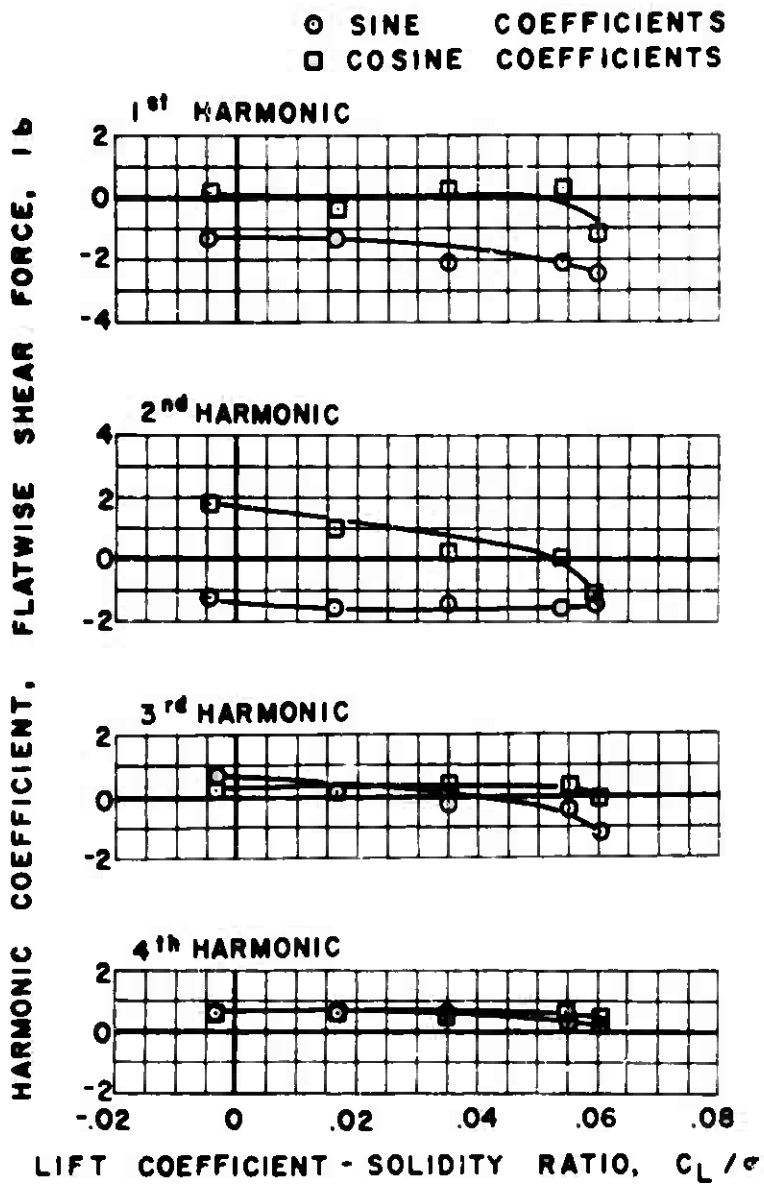


Figure 47(b). Concluded.



$\mu = 0.4 \quad \alpha_s = 4 \text{ deg.}$

(a) FLATWISE

Figure 48. Experimental Shear Force.

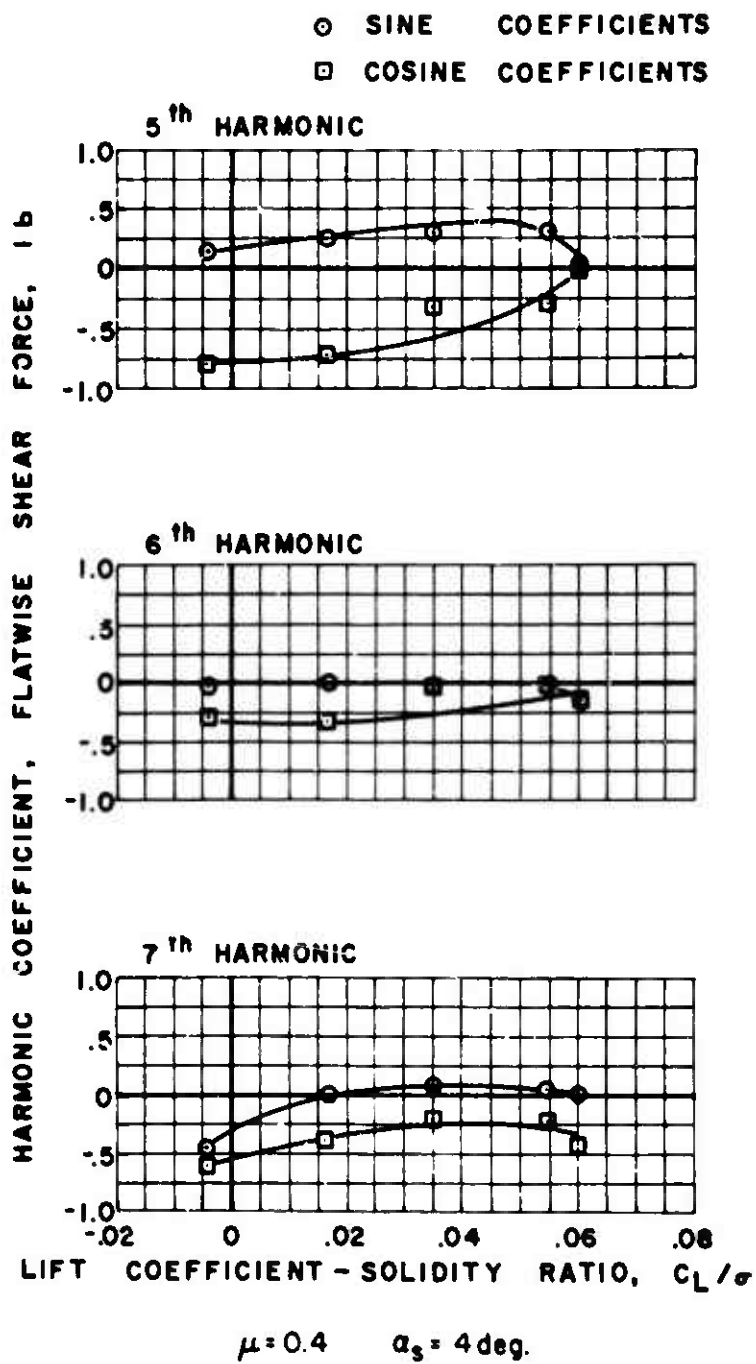


Figure 48(a). Continued.

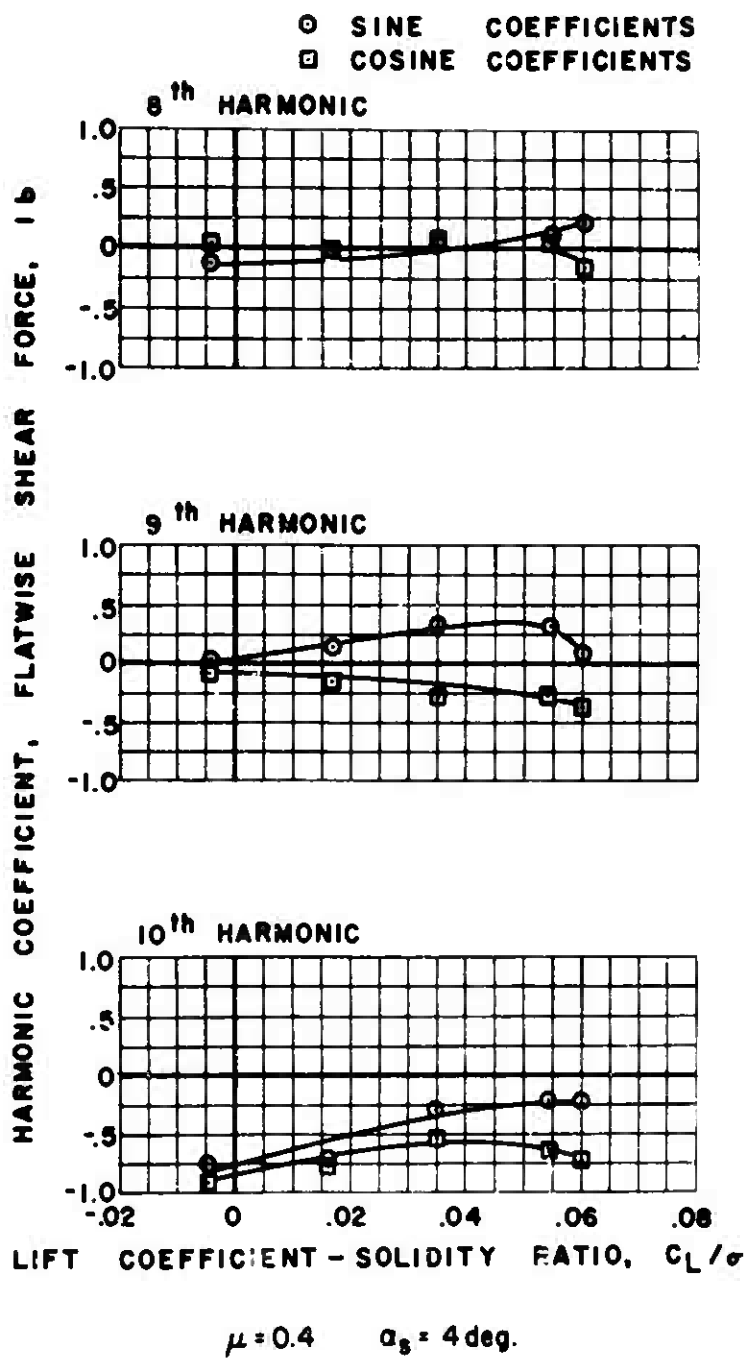
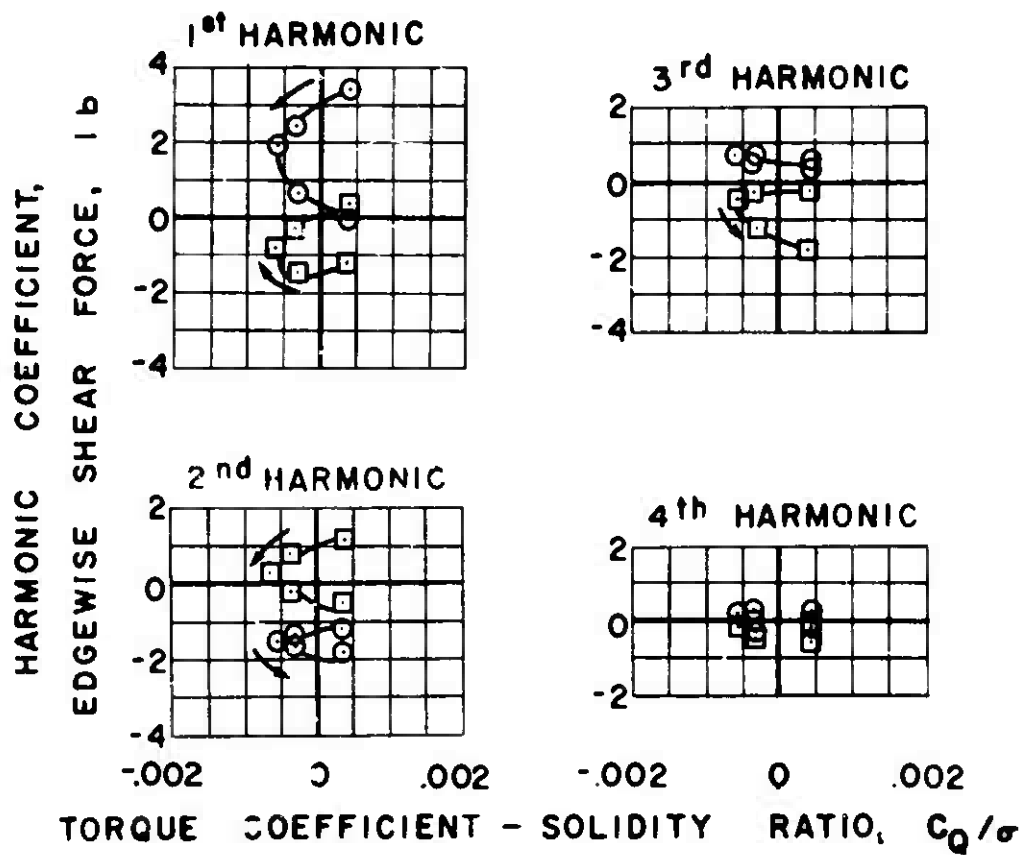


Figure 48(a). Continued.

ARROWS INDICATE DIRECTION OF
INCREASING COLLECTIVE PITCH

○ SINE COEFFICIENTS

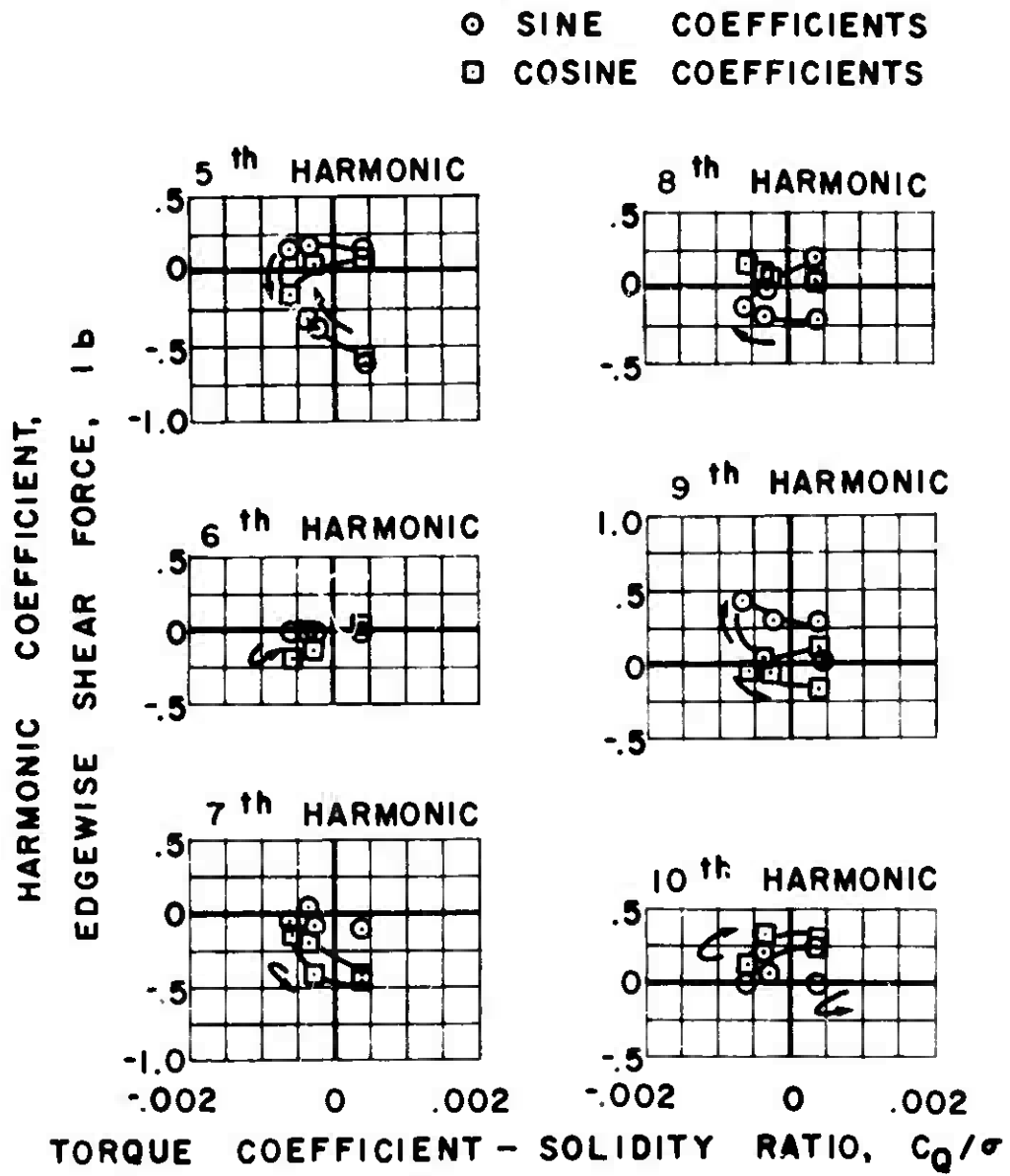
□ COSINE COEFFICIENTS



$$\mu = 0.4 \quad \alpha_s = 4 \text{ deg.}$$

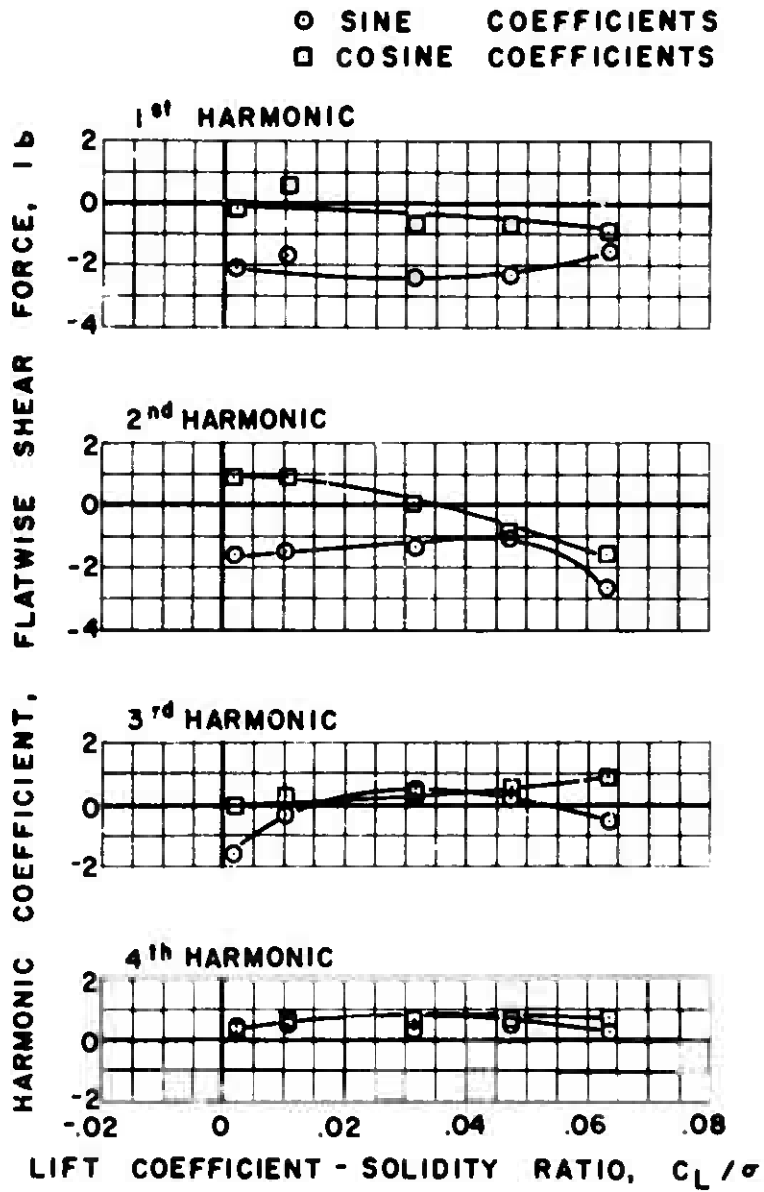
(b) EDGEWISE

Figure 48. Continued.



$\mu = 0.4 \quad \alpha_s = 4 \text{ deg.}$

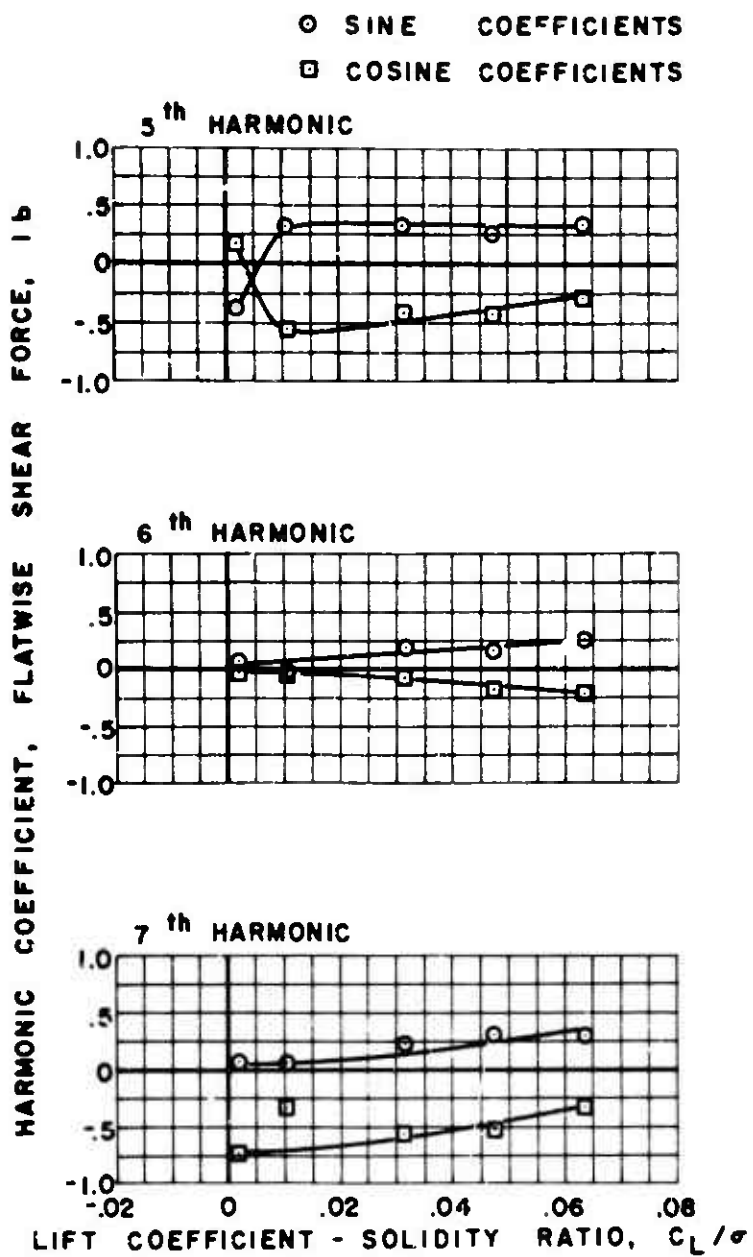
Figure 48(b). Concluded.



$\mu = 0.4 \quad \alpha_s = 0 \text{ deg.}$

(a) FLATWISE

Figure 49. Experimental Shear Force.



$\mu = 0.4 \quad \alpha_s = 0 \text{ deg.}$

Figure 49(a). Continued.

○ SINE COEFFICIENTS

□ COSINE COEFFICIENTS

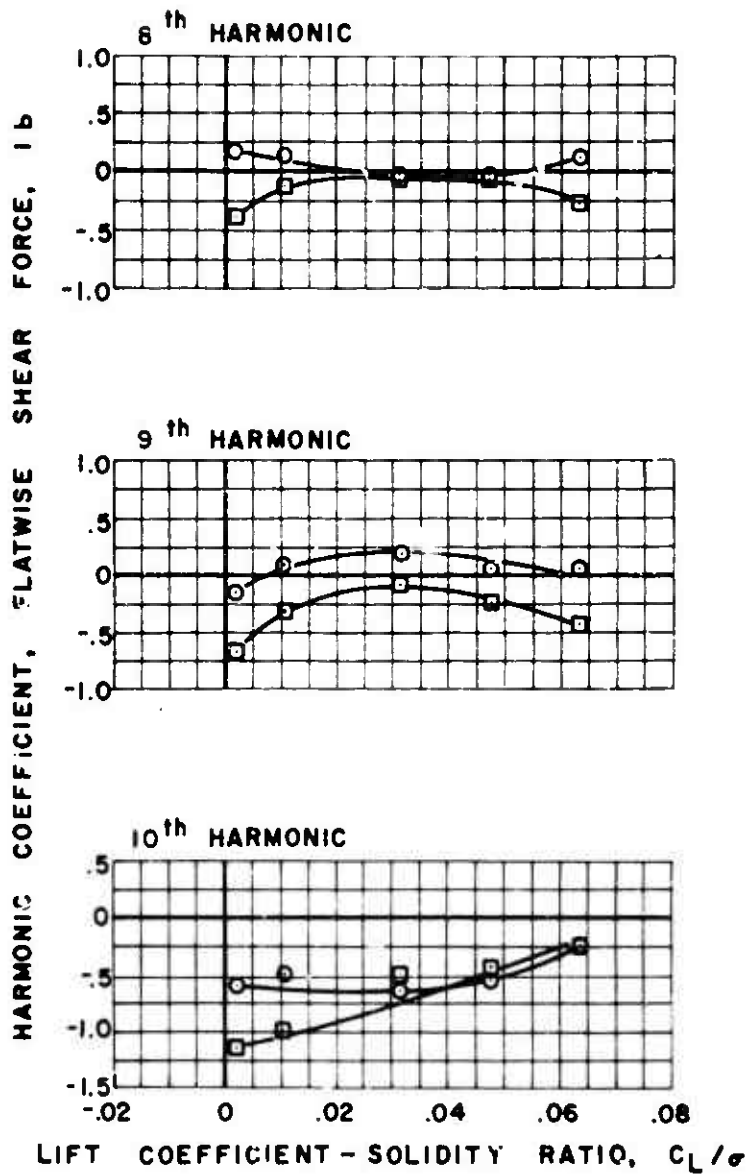
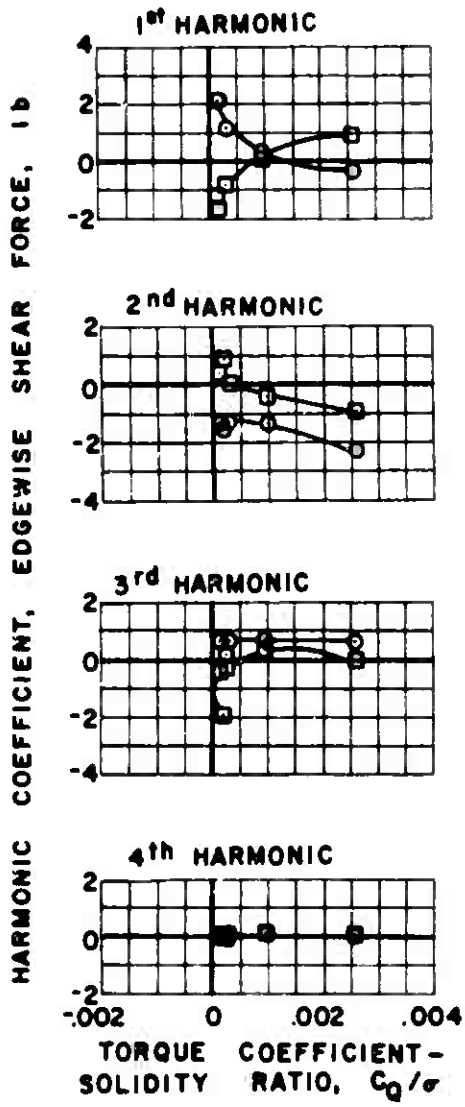


Figure 49(a). Continued.

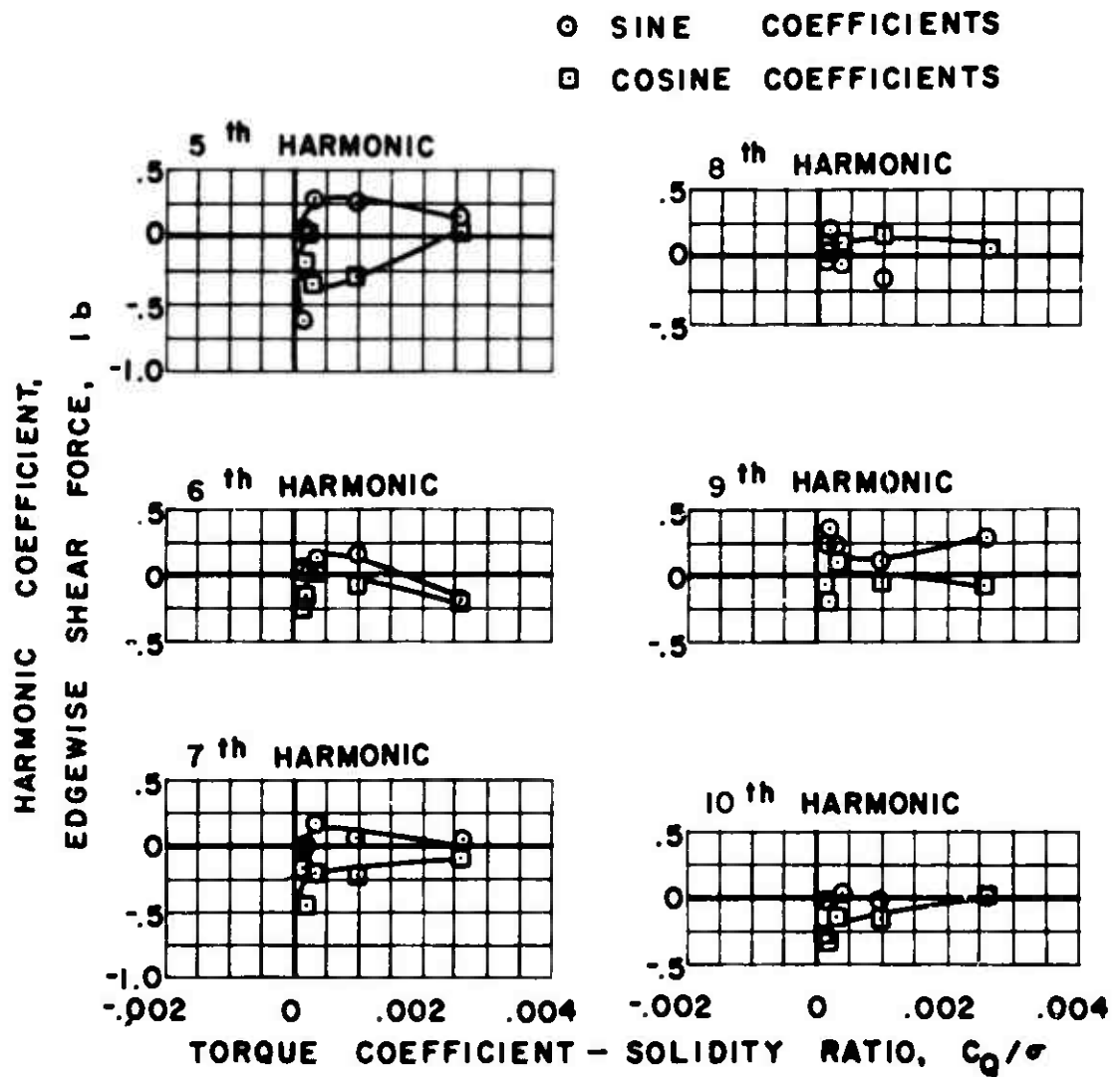
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.4$ $\alpha_s = 0$ deg.

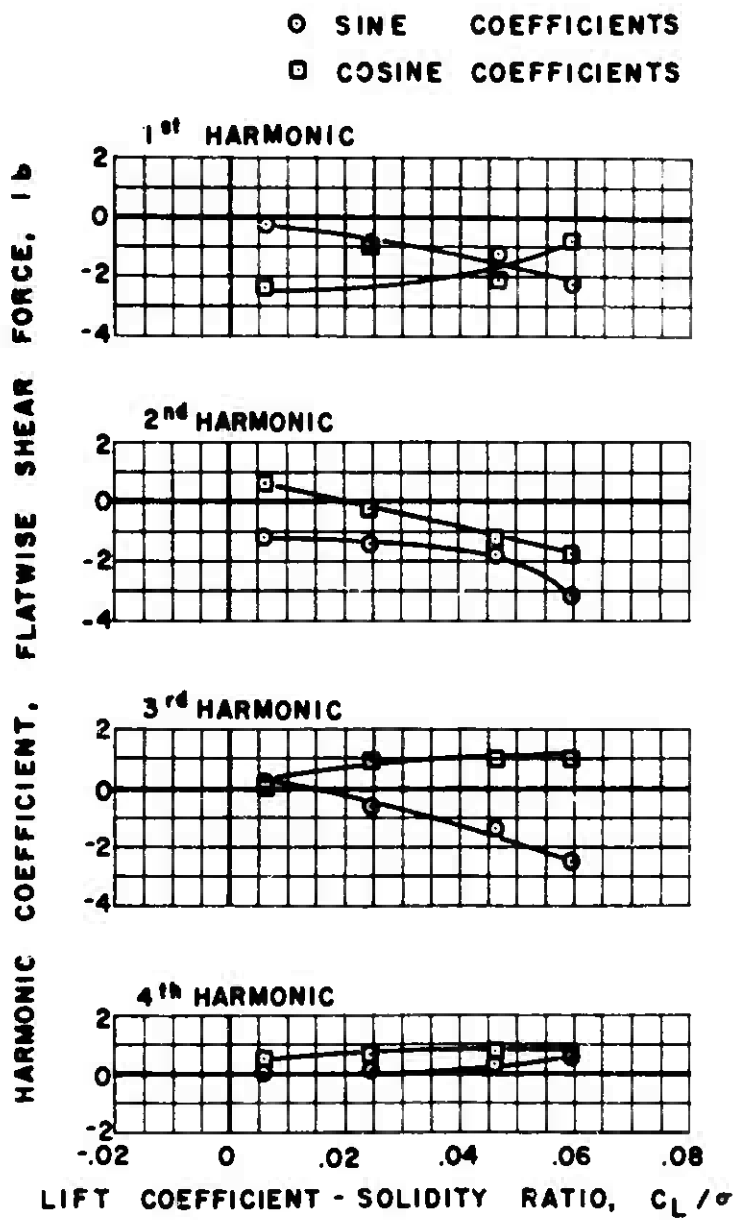
(b) EDGEWISE

Figure 49. Continued.



$\mu = 0.4 \quad \alpha_s = 0 \text{ deg.}$

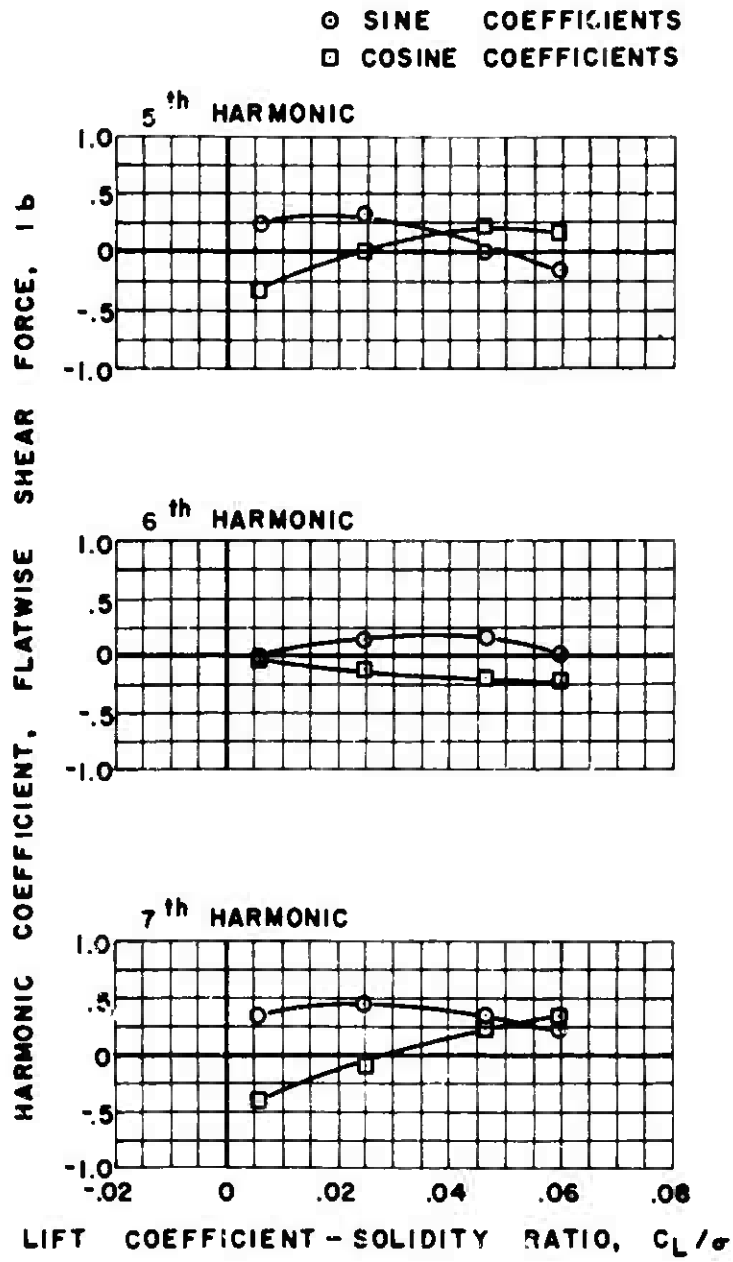
Figure 49(b). Concluded.



$$\mu = 0.4 \quad \alpha_s = -4 \text{ deg.}$$

(a) FLATWISE

Figure 50. Experimental Shear Force.



$\mu = 0.4 \quad \alpha_s = -4 \text{ deg.}$

Figure 50(a). Continued.

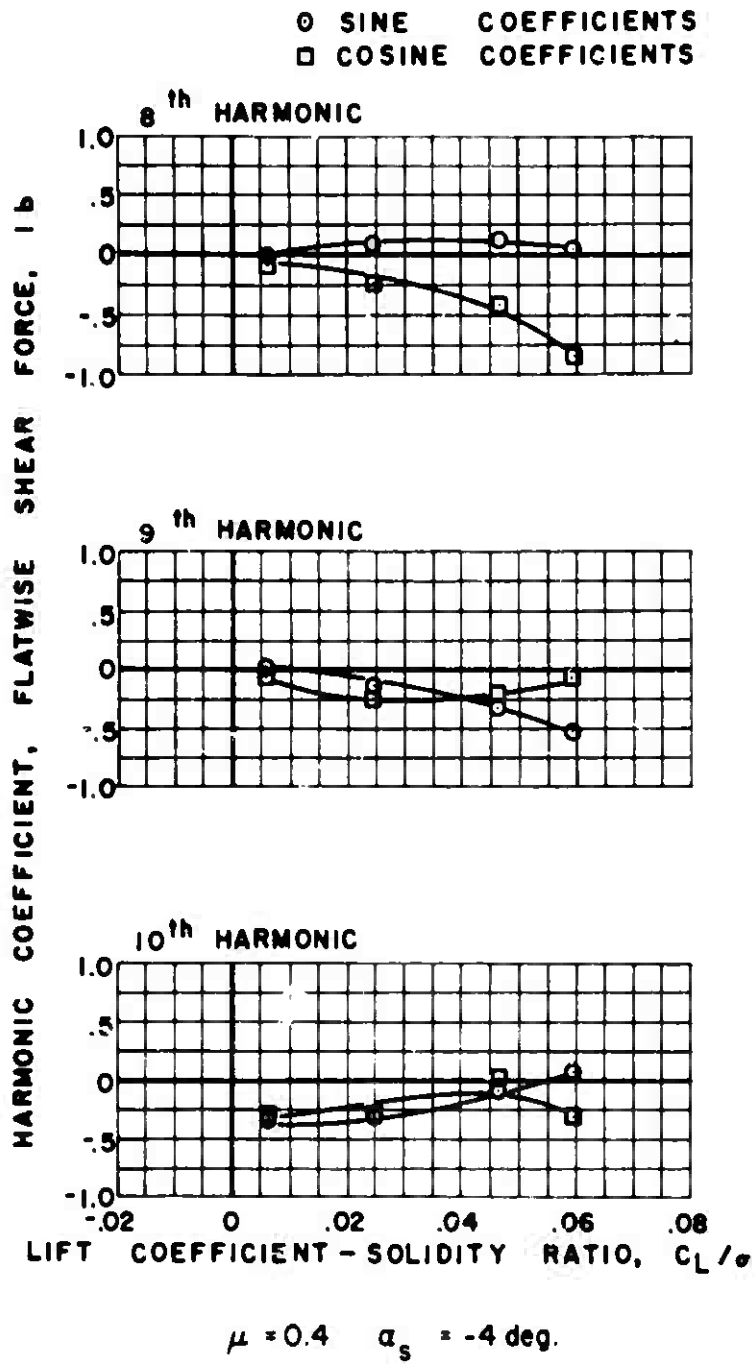
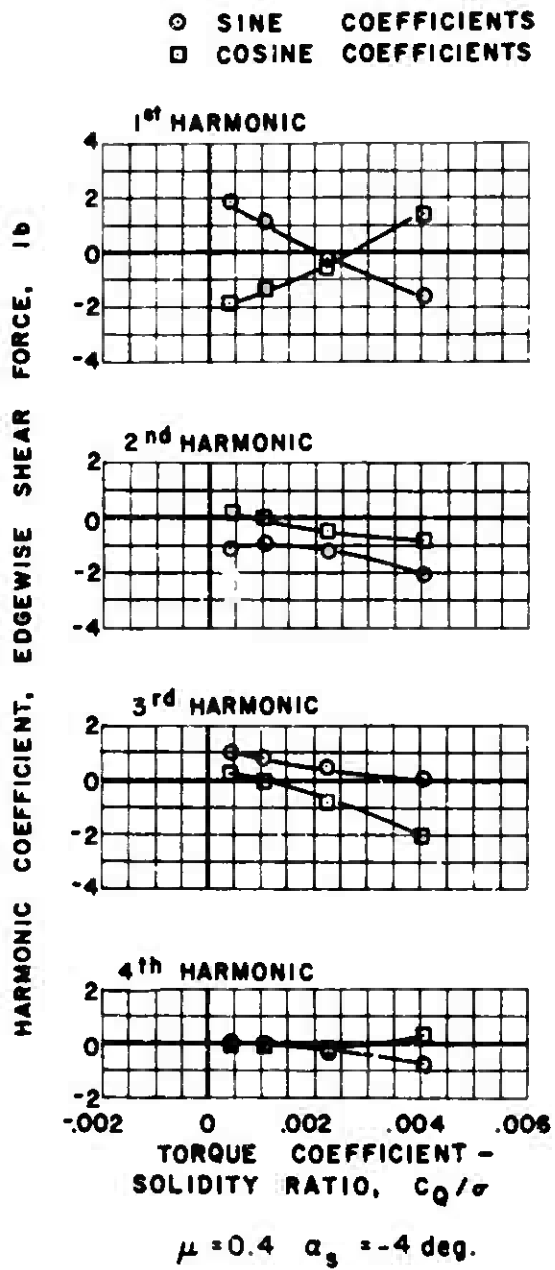


Figure 50(a). Continued.



(b) EDGEWISE

Figure 50. Continued.

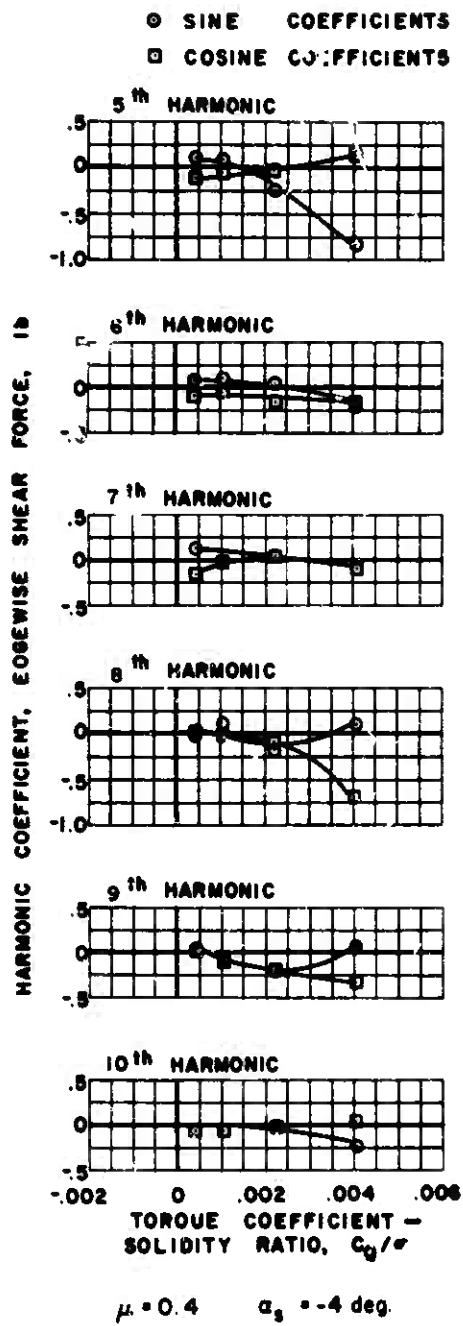
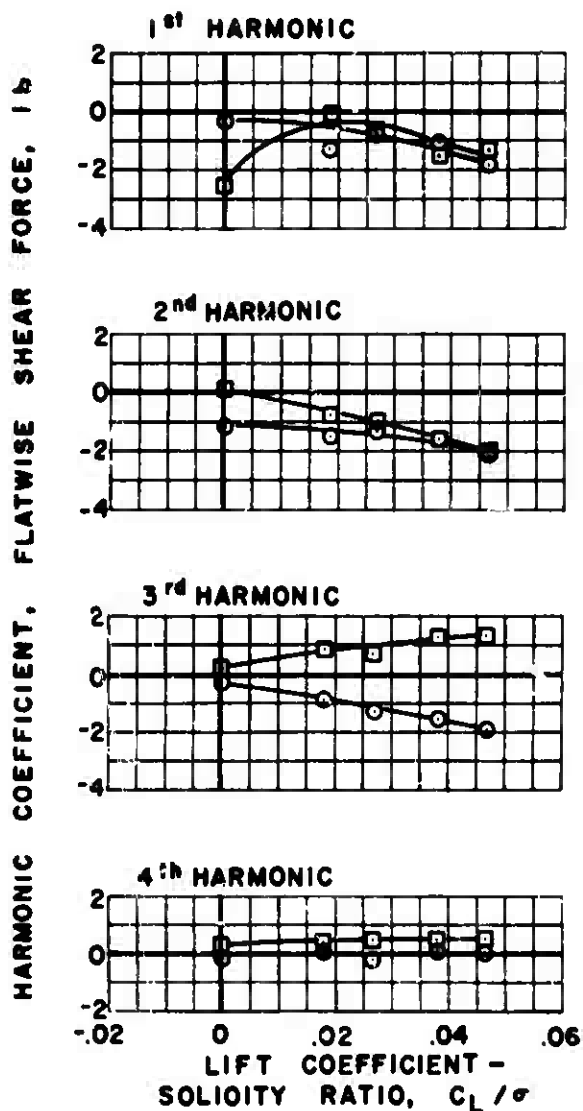


Figure 50(b). Concluded.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.4$ $\alpha_s = -8$ deg.

(a) FLATWISE

Figure 51. Experimental Shear Force.

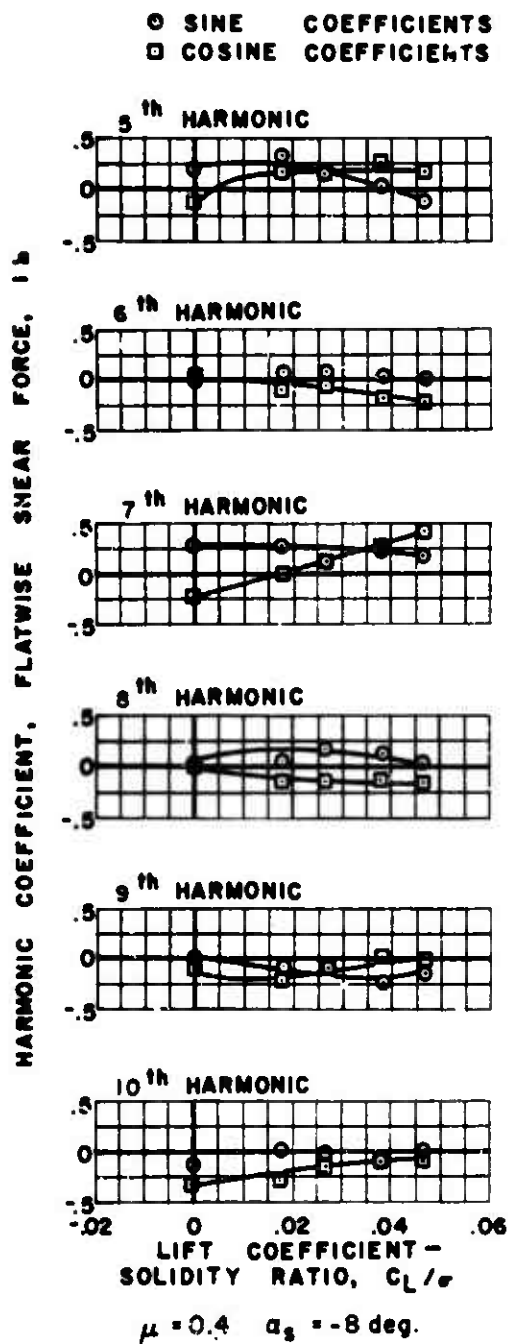
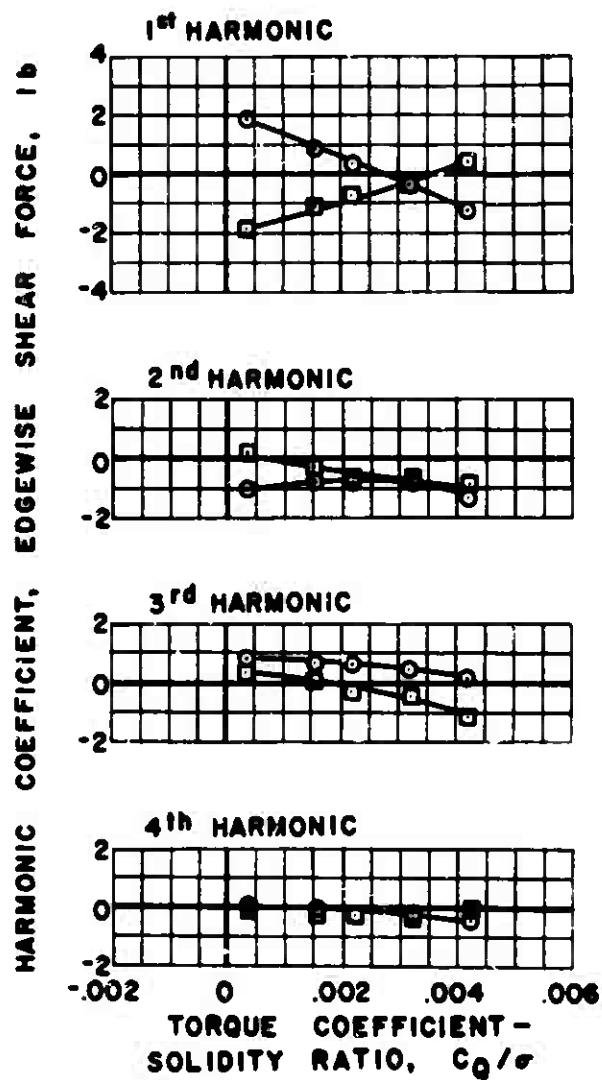


Figure 51(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS

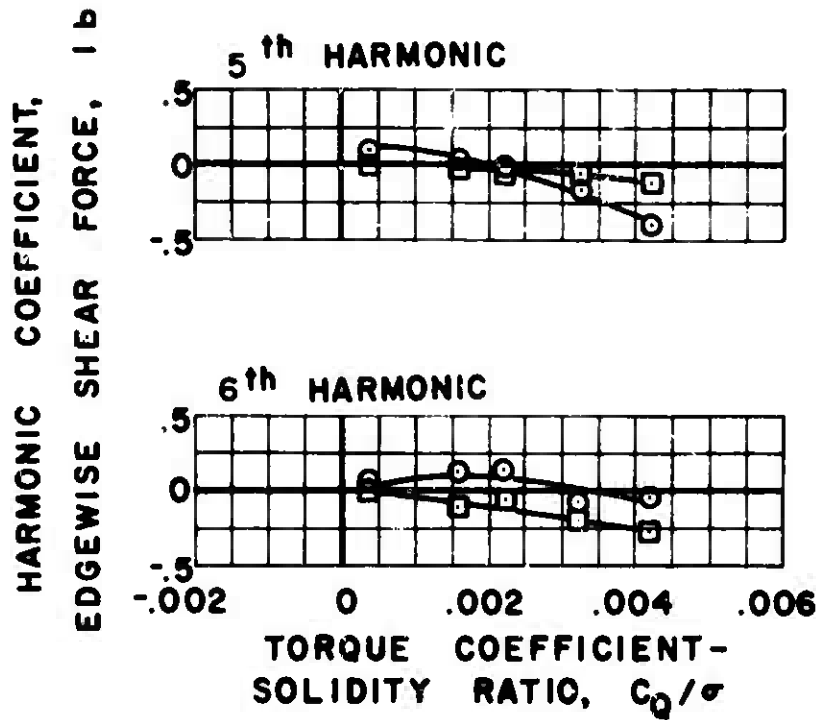


$\mu = 0.4$ $\alpha_s = -8$ deg.

(b) EDGEWISE

Figure 51. Continued.

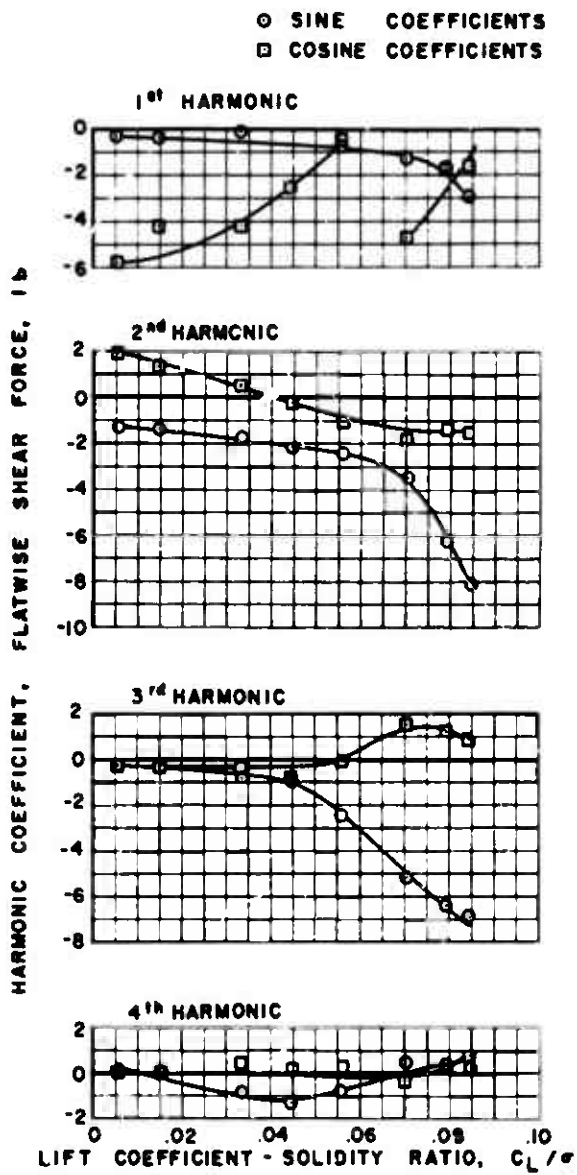
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



IN THIS TEST CONDITION THE MAGNITUDE OF THE EDGEWISE HARMONICS ABOVE THE SIXTH DID NOT EXCEED THE REPEATABILITY OF THE SYSTEM AND ARE NOT PRESENTED.

$$\mu = 0.4 \quad \alpha_s = -8 \text{ deg.}$$

Figure 51(b). Concluded.

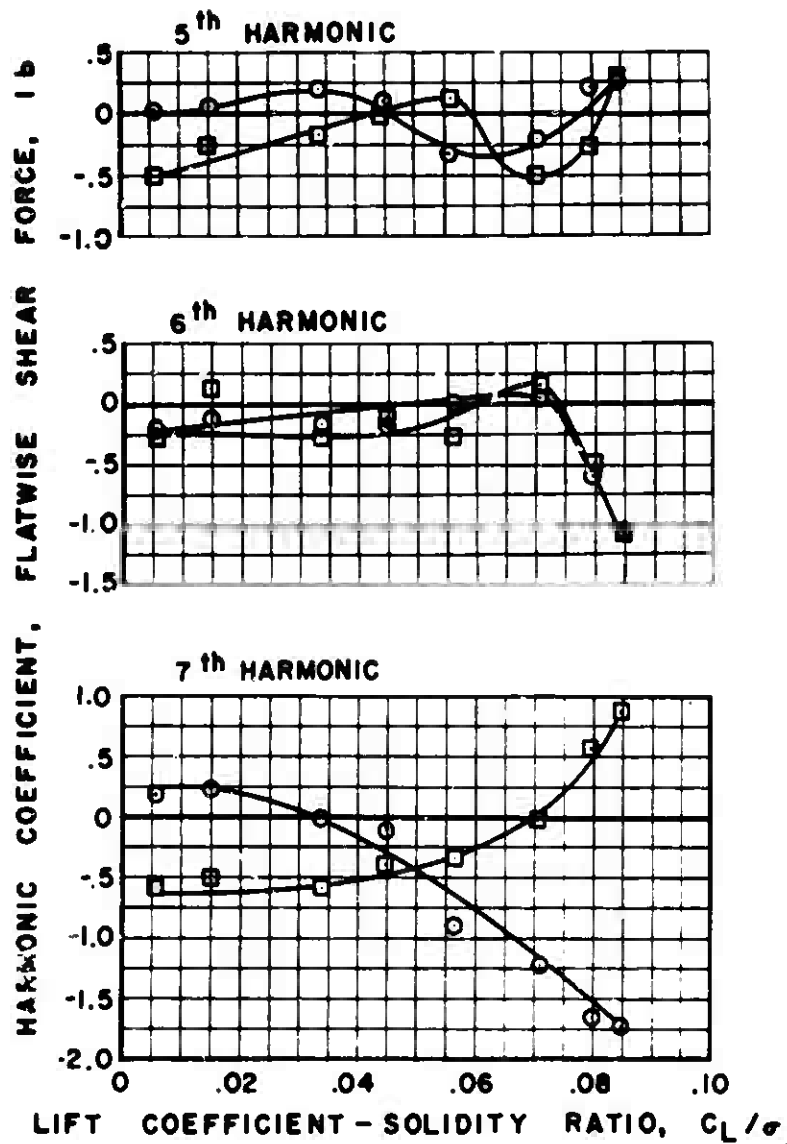


$\mu = 0.5 \quad \alpha_s = 0 \text{ deg.}$

(a) FLATWISE

Figure 52. Experimental Shear Force.

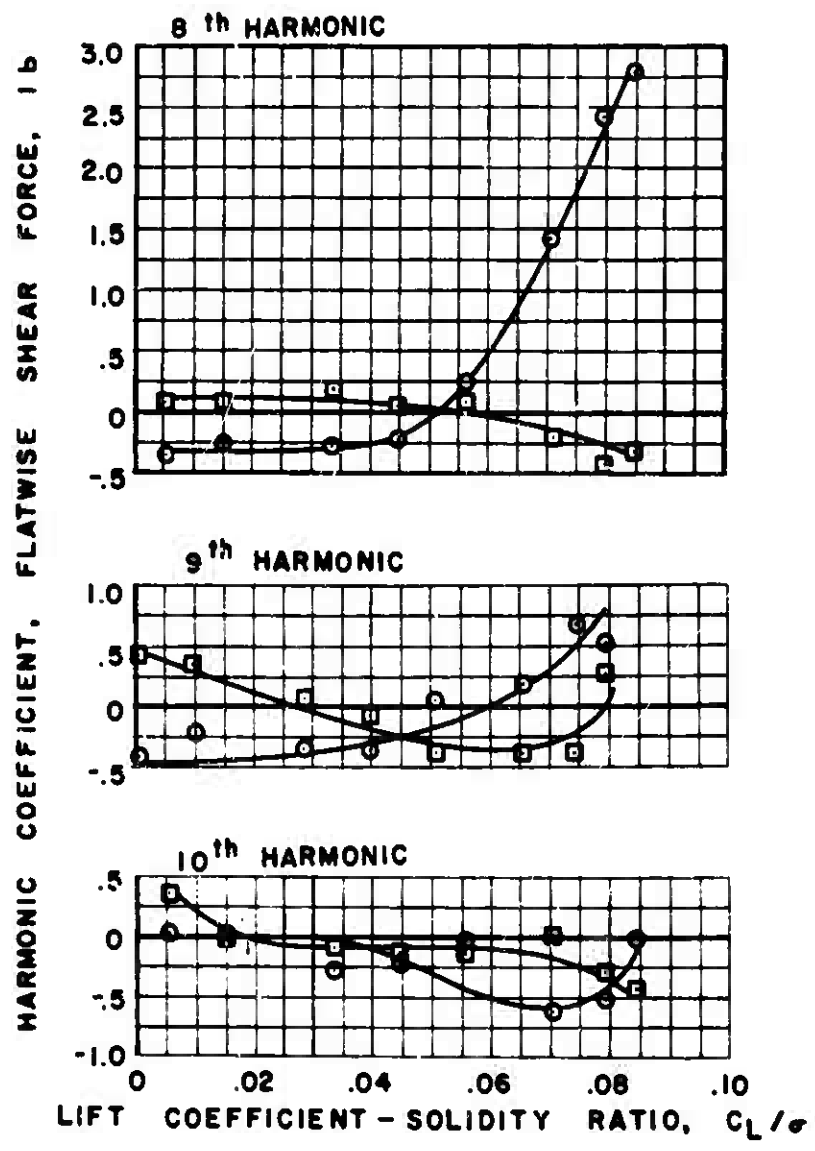
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = 0 \text{ deg.}$

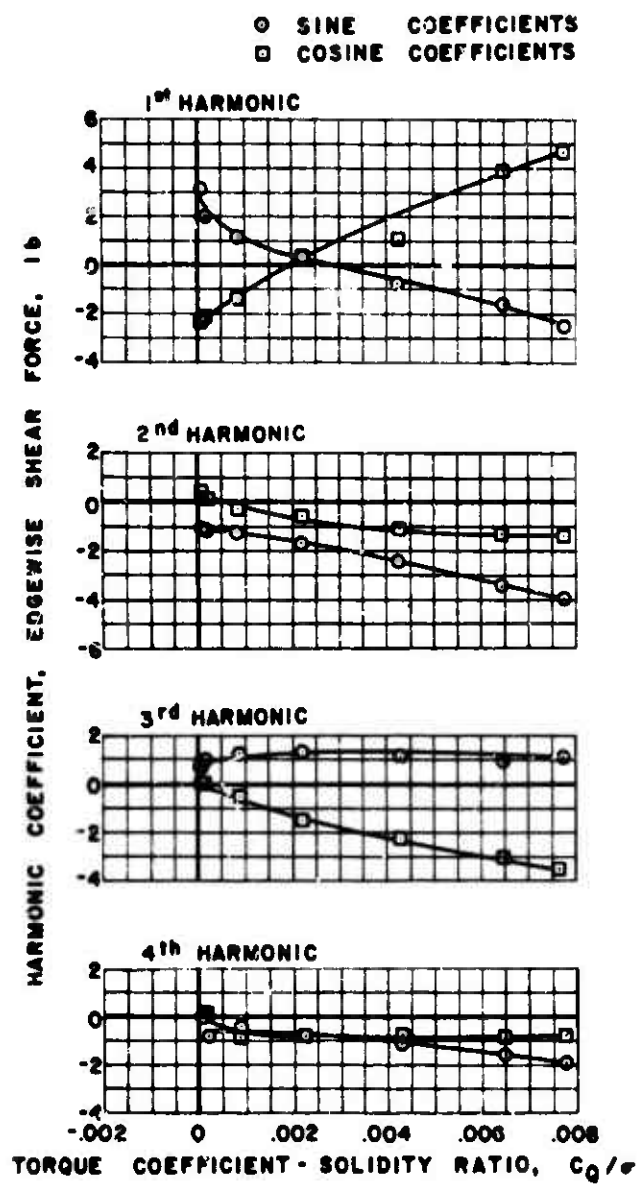
Figure 52(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = 0 \text{ deg.}$

Figure 52(a). Continued.

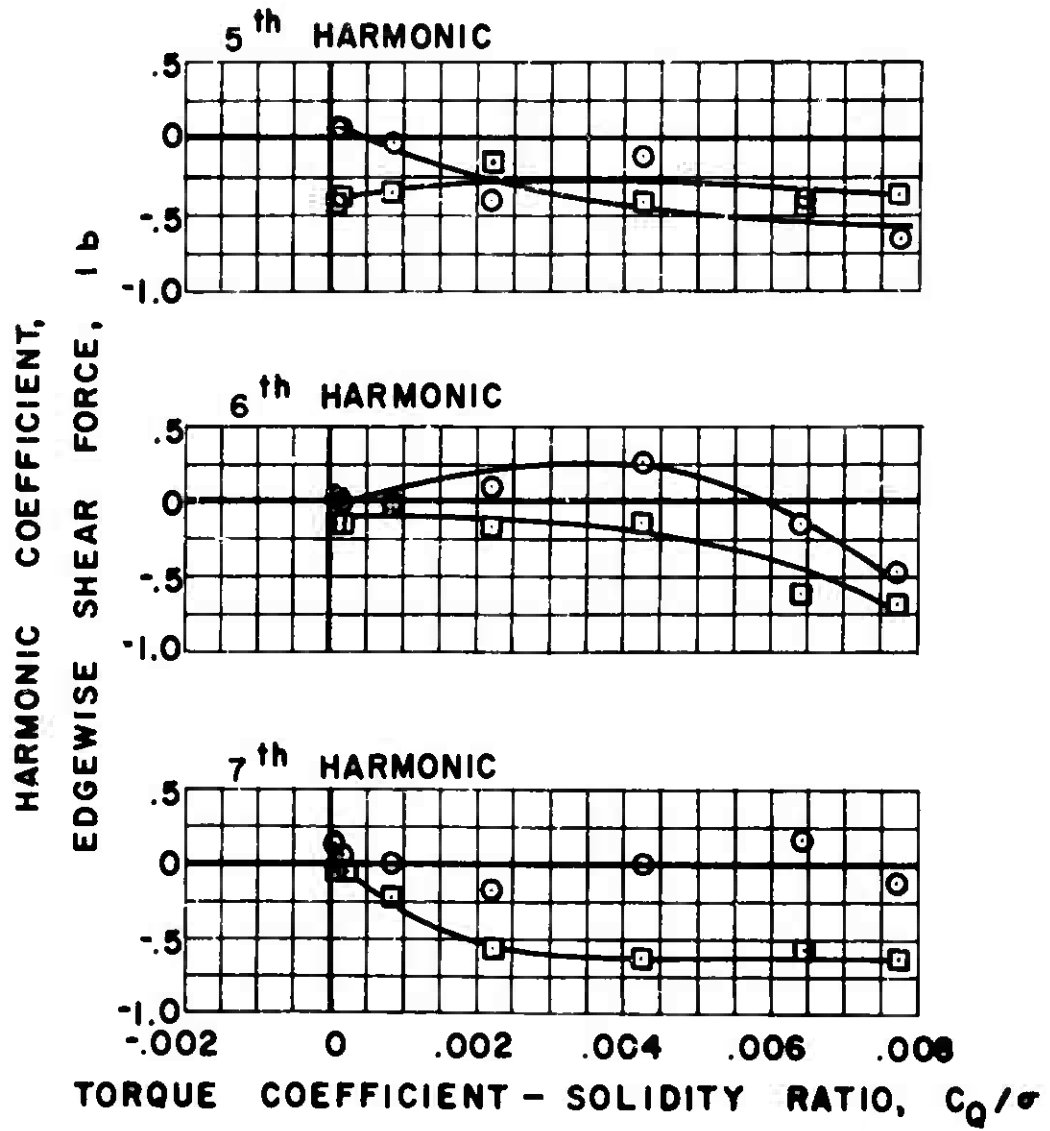


$\mu = 0.5 \quad \alpha_s = 0 \text{ deg.}$

(b) EDGEWISE

Figure 52. Continued.

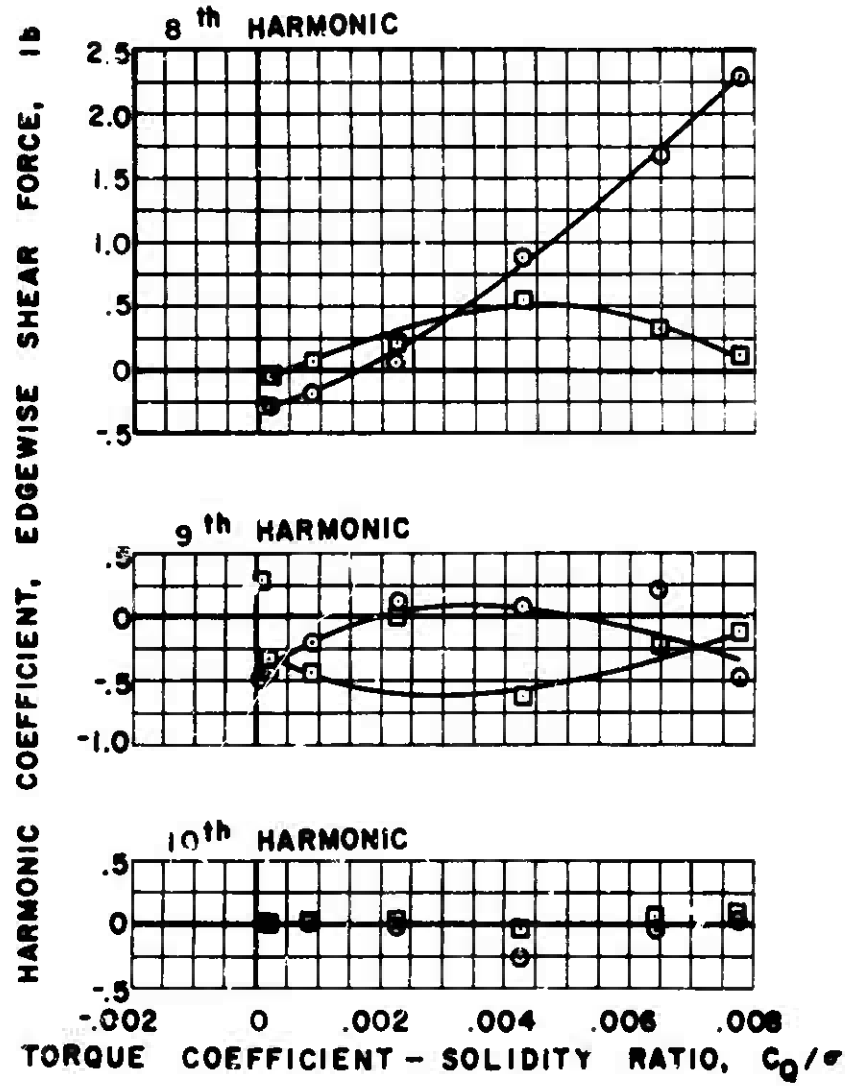
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = 0 \text{ deg.}$

Figure 52(b). Continued.

⊙ SINE COEFFICIENTS
 ⊠ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = 0 \text{ deg.}$

Figure 52(b). Concluded.

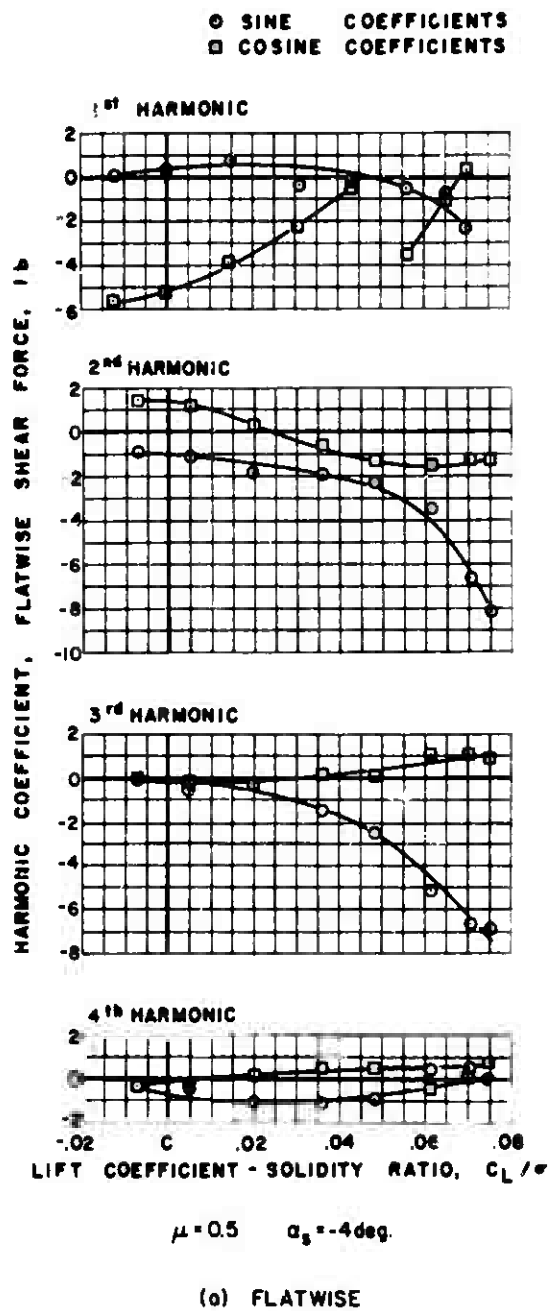
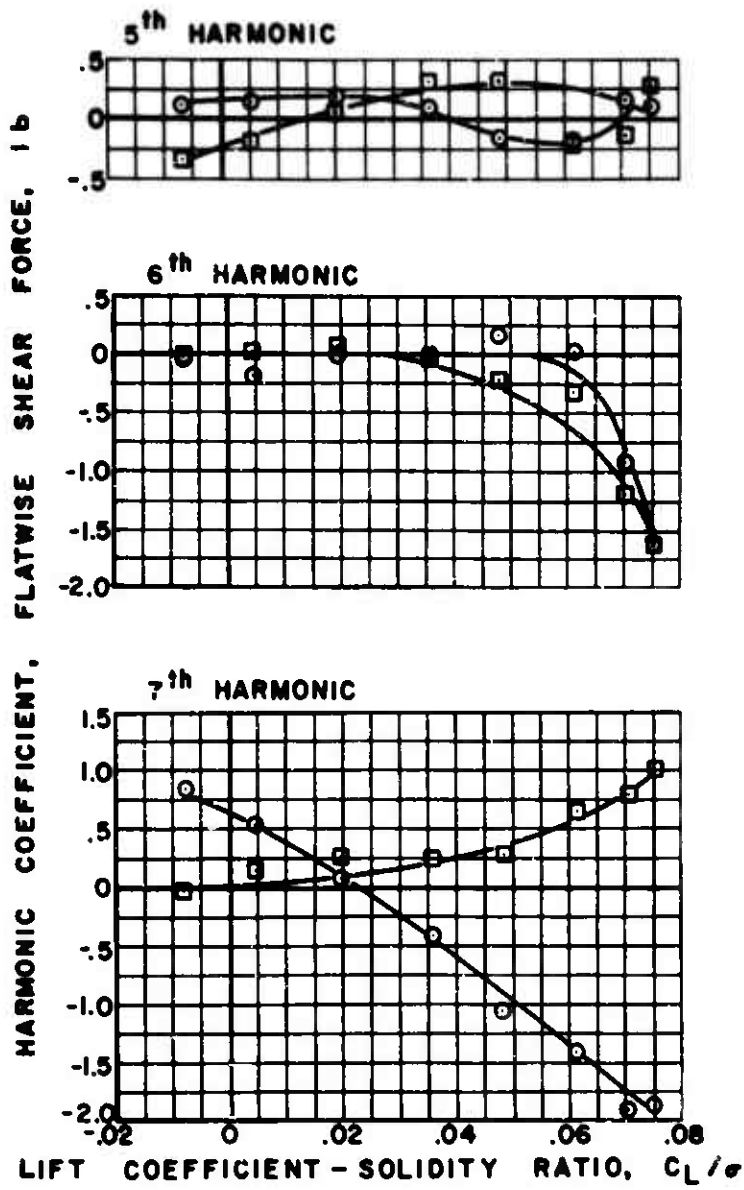


Figure 53. Experimental Shear Force.

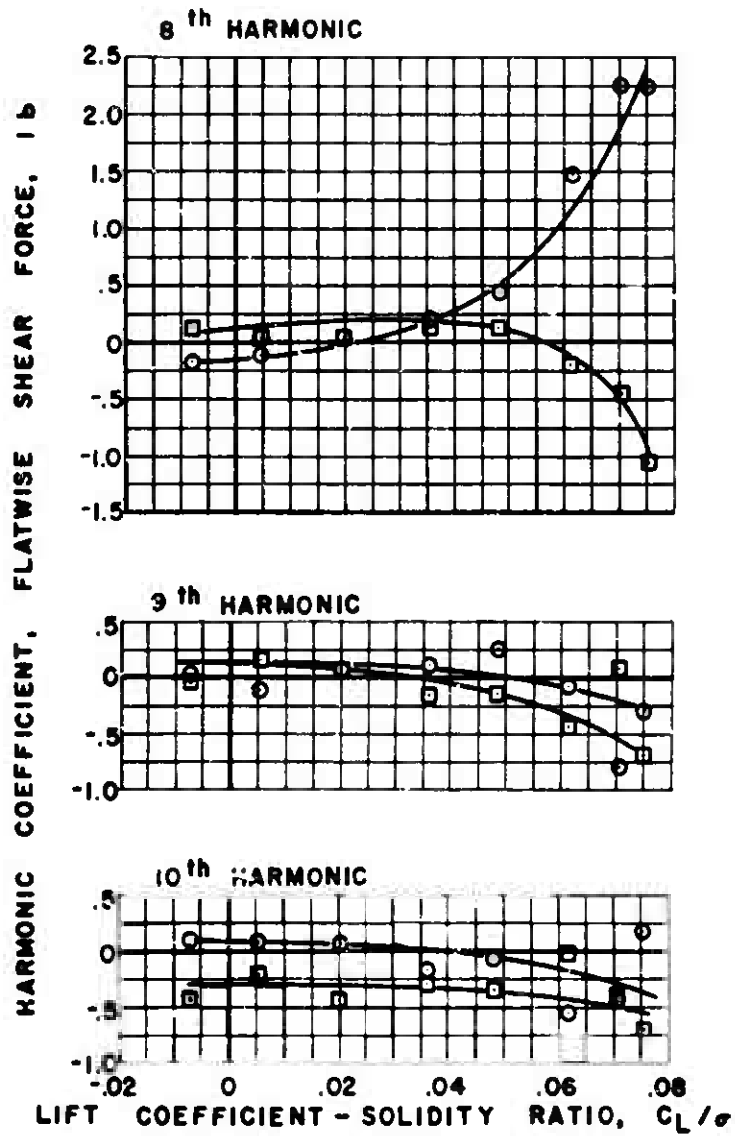
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4\text{deg.}$

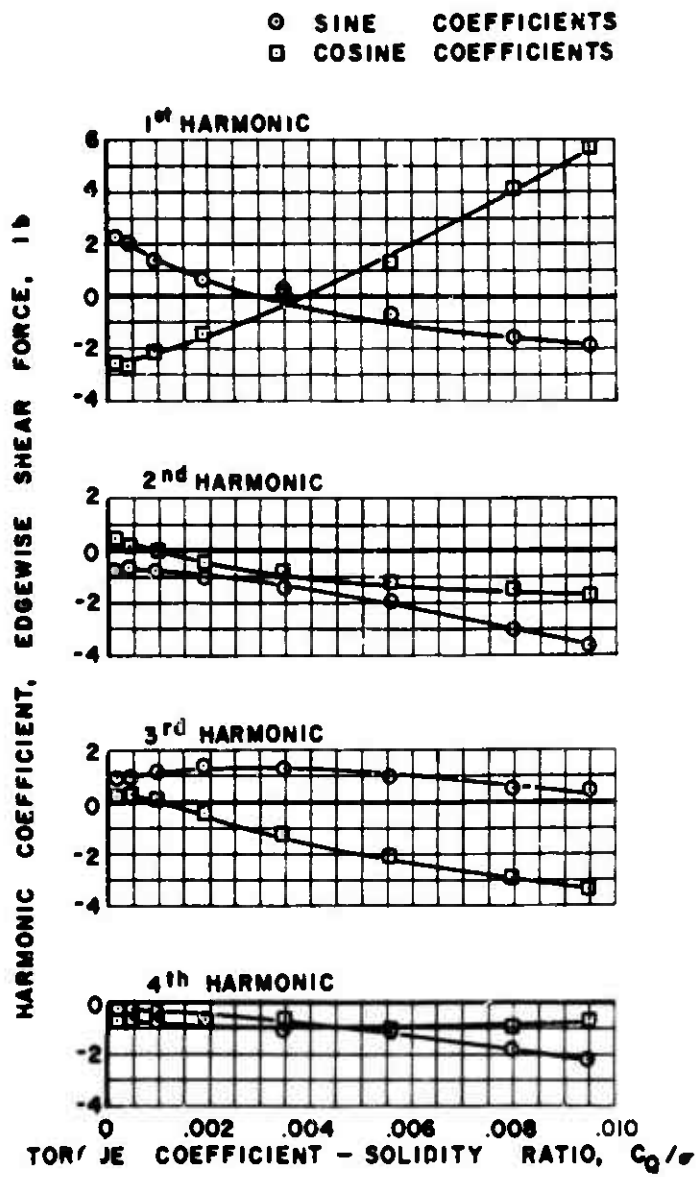
Figure 53(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4 \text{ deg.}$

Figure 53(a). Continued.

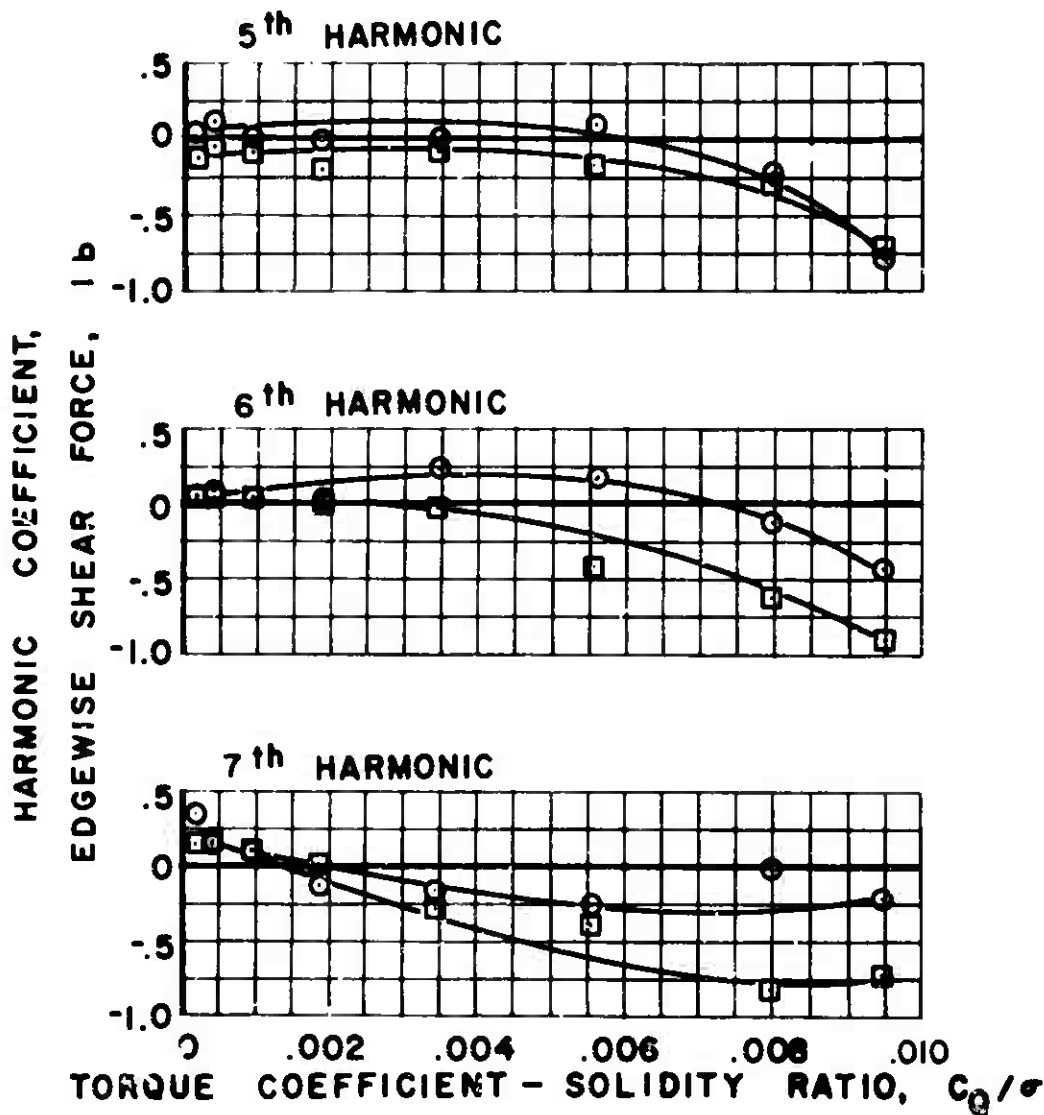


$\mu = 0.5$ $\alpha_s = -4$ deg.

(b) EDGEWISE

Figure 53. Continued.

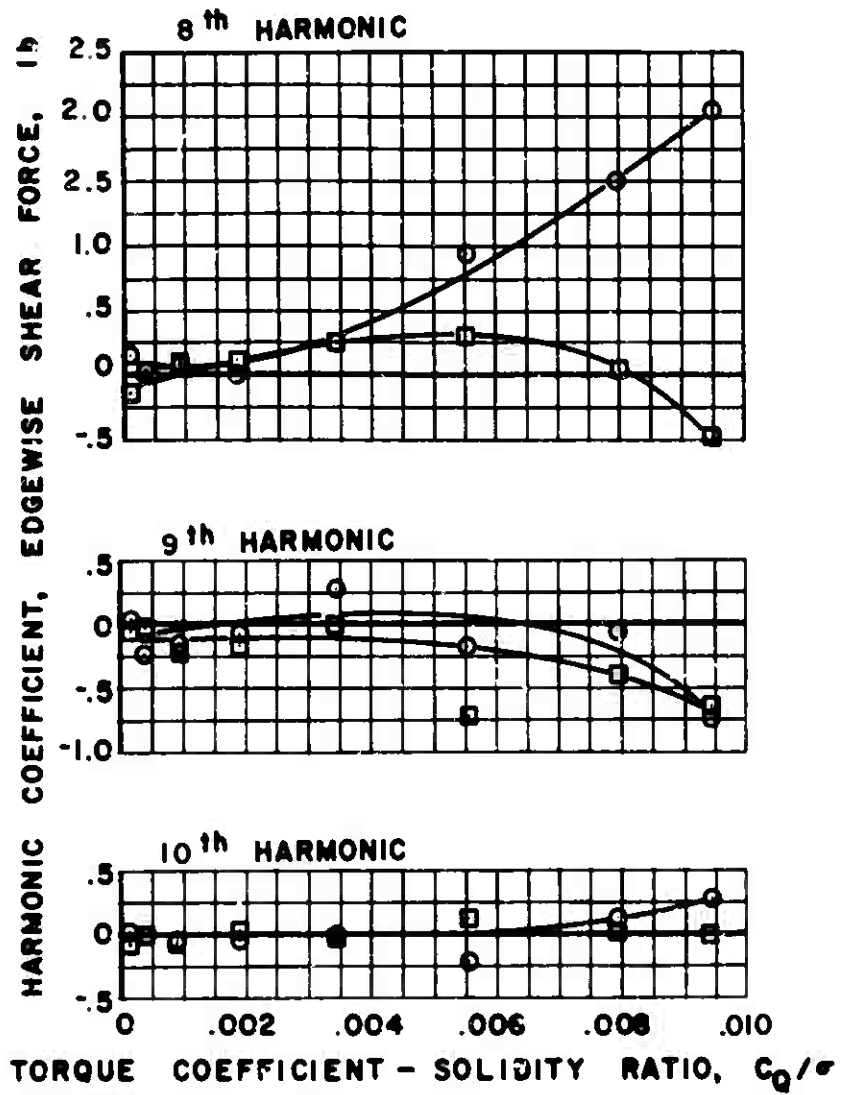
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4$ (deg).

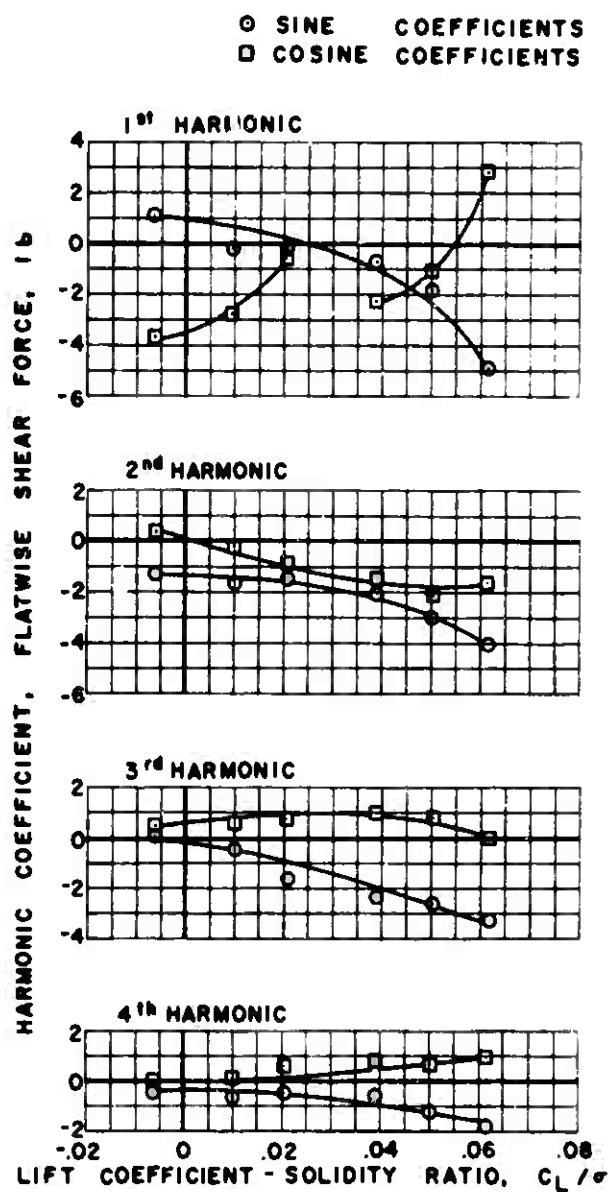
Figure 53(b). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4 \text{deg.}$

Figure 53(b). Concluded.

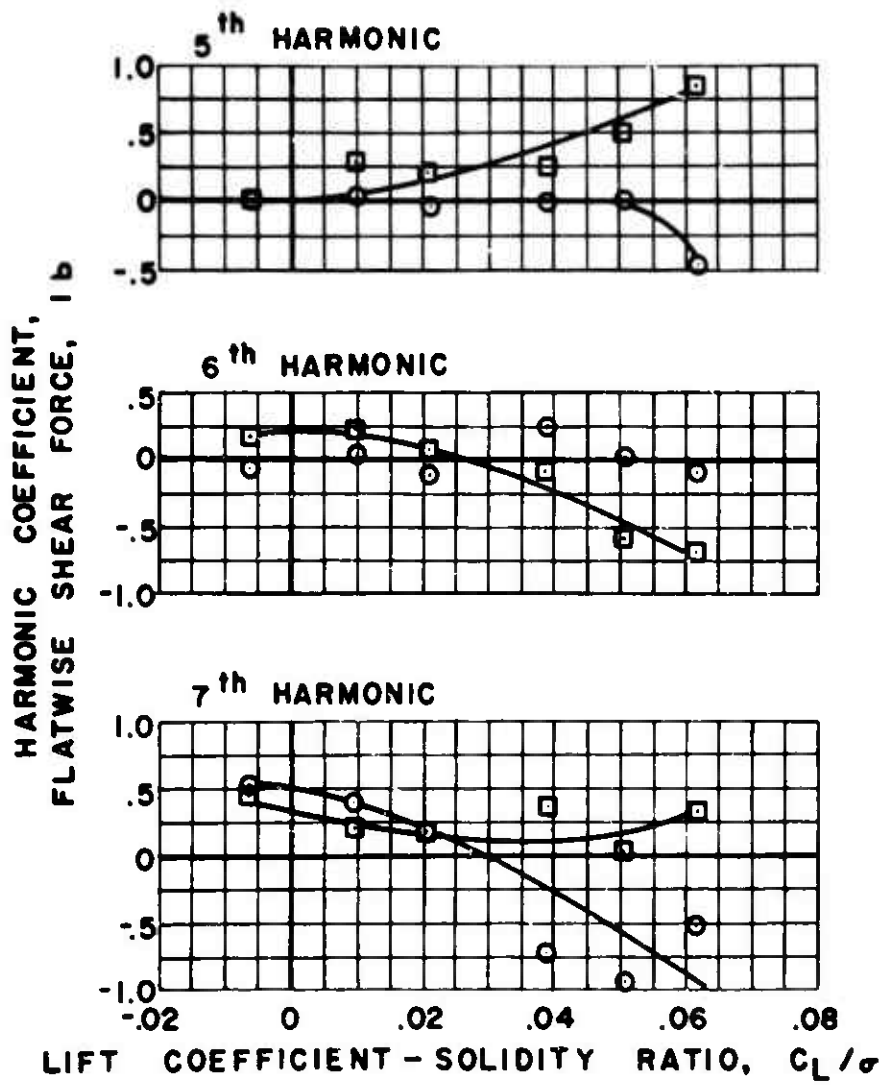


$\mu = 0.5 \quad \alpha_s = -8 \text{ deg.}$

(a) FLATWISE

Figure 54. Experimental Shear Force.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -8 \text{ deg.}$

Figure 54(a). Continued.

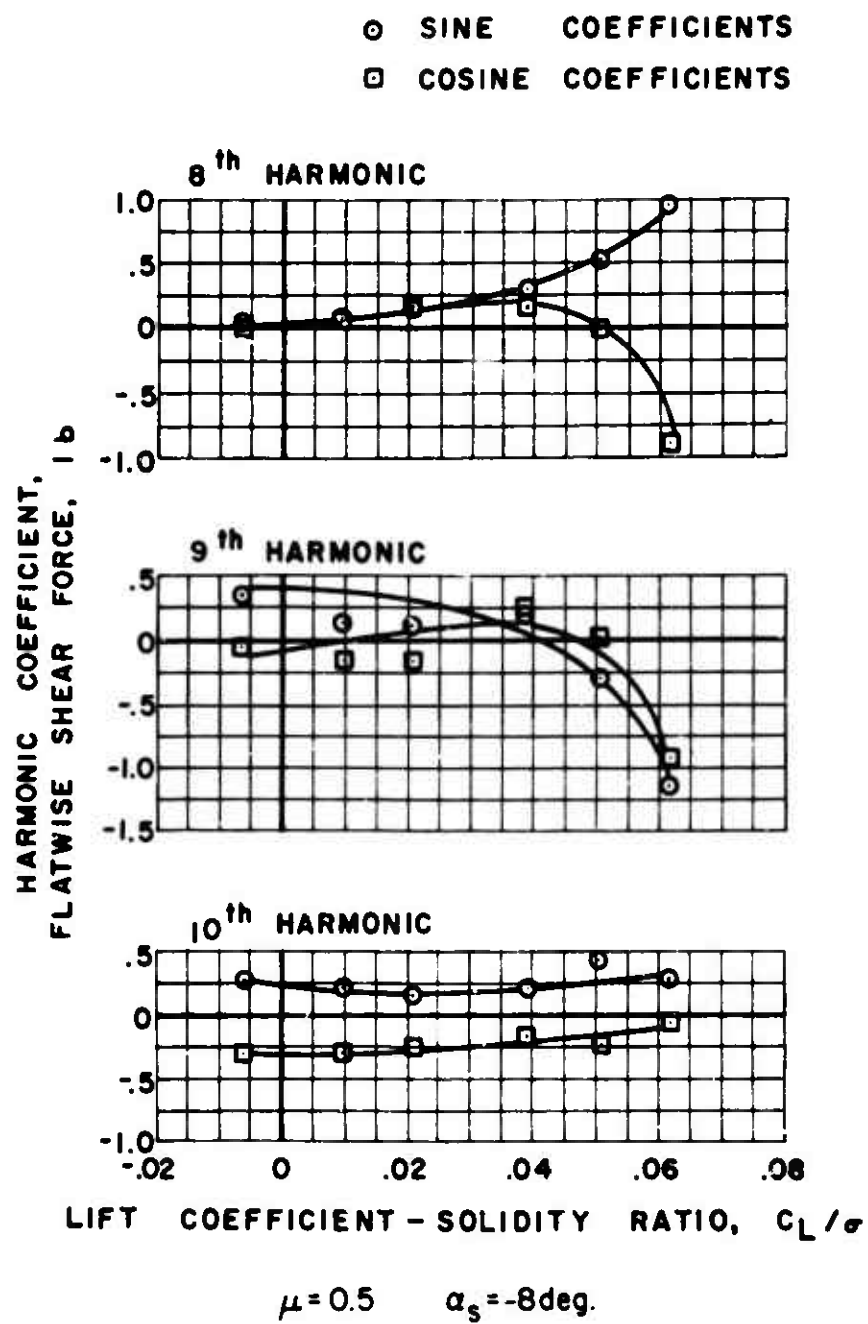
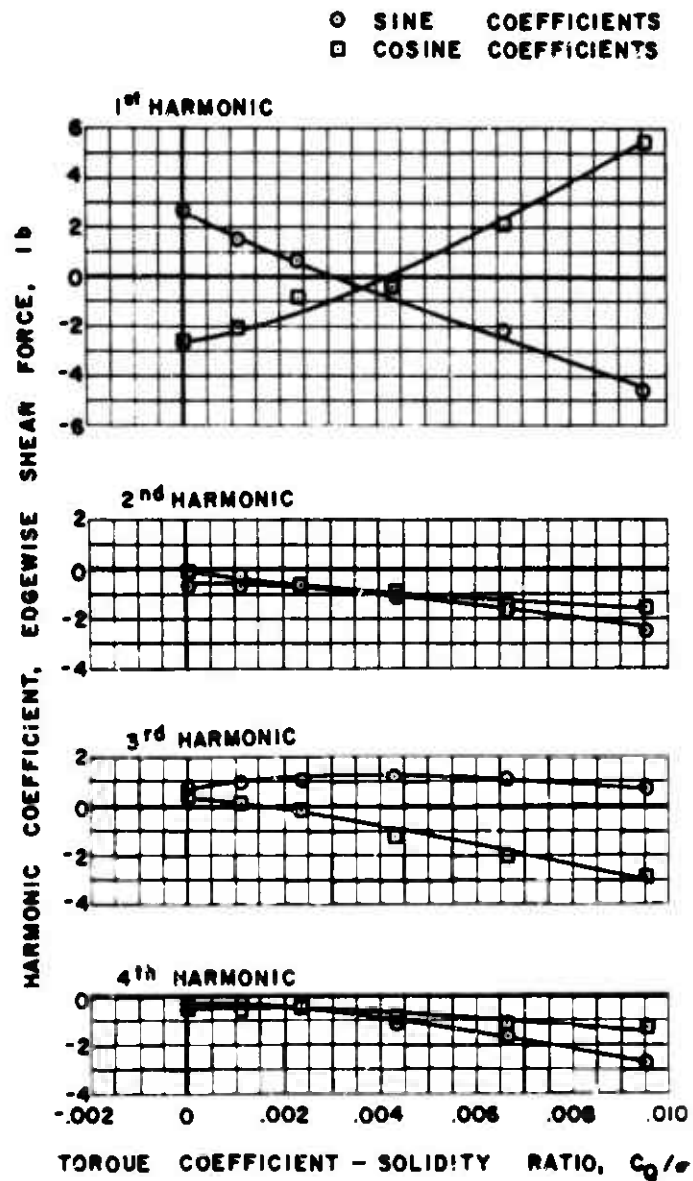


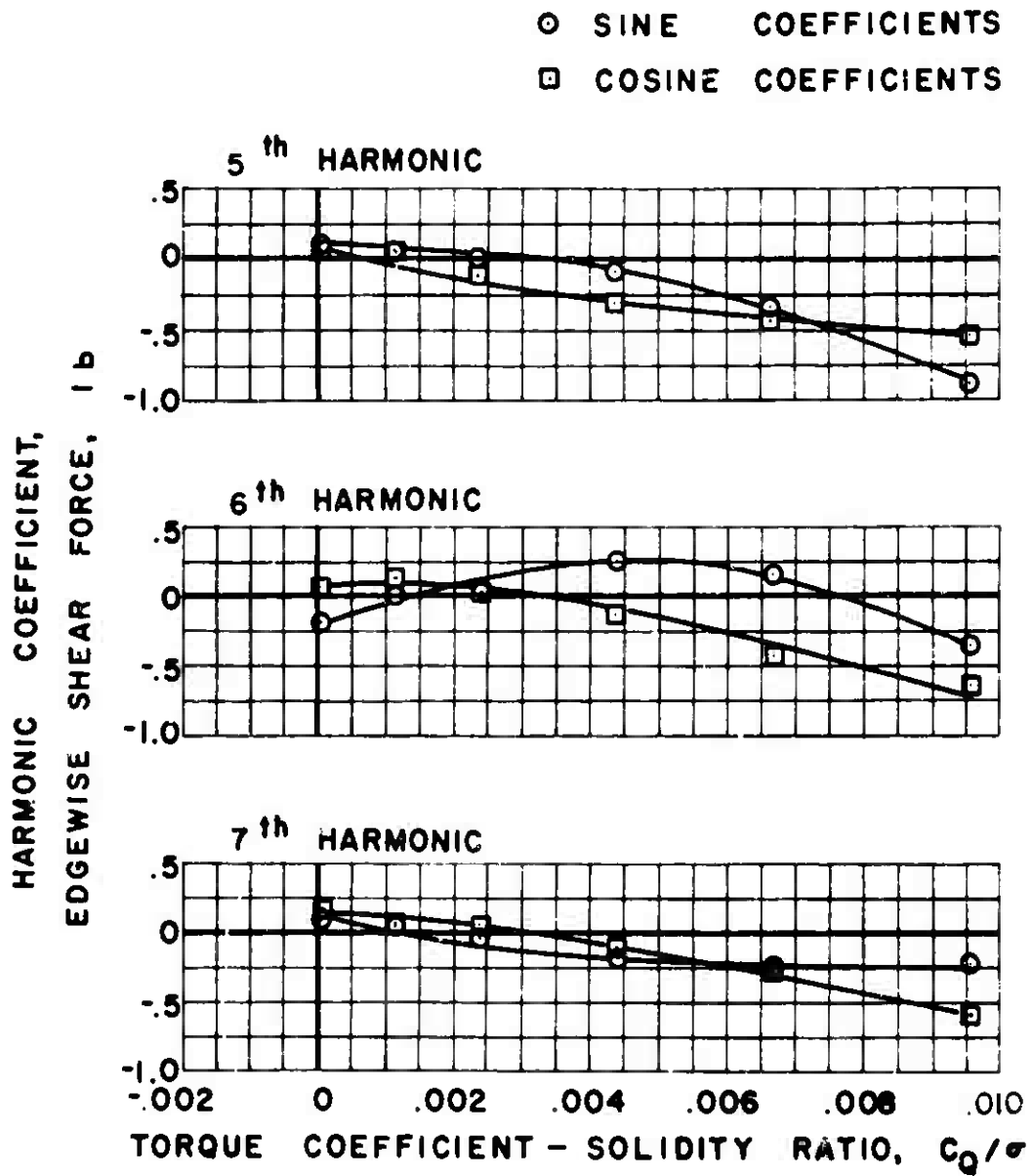
Figure 54(a). Continued.



$\mu = 0.5 \quad \alpha_s = -8\text{deg.}$

(b) EDGEWISE

Figure 54. Continued.



$\mu = 0.5$ $\alpha_s = -8 \text{ deg.}$

Figure 54(b). Continued.

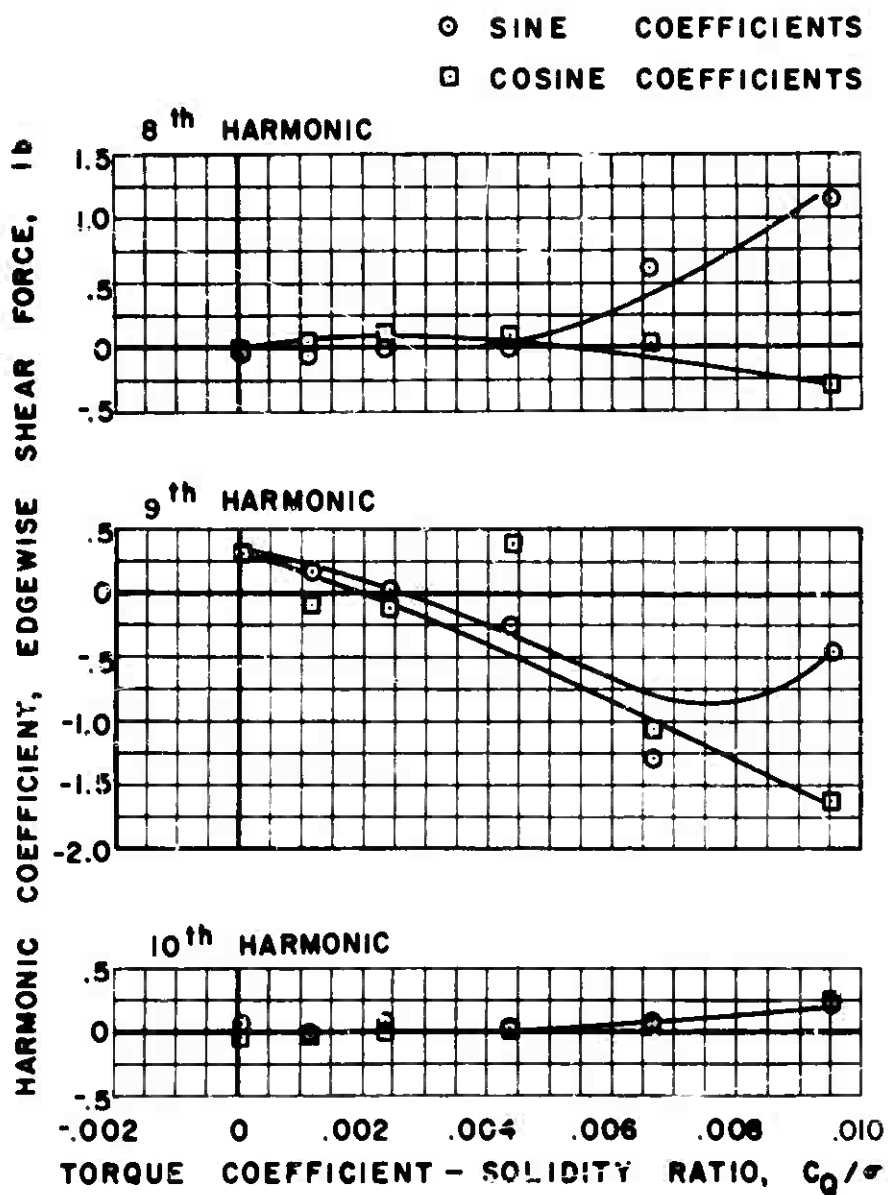
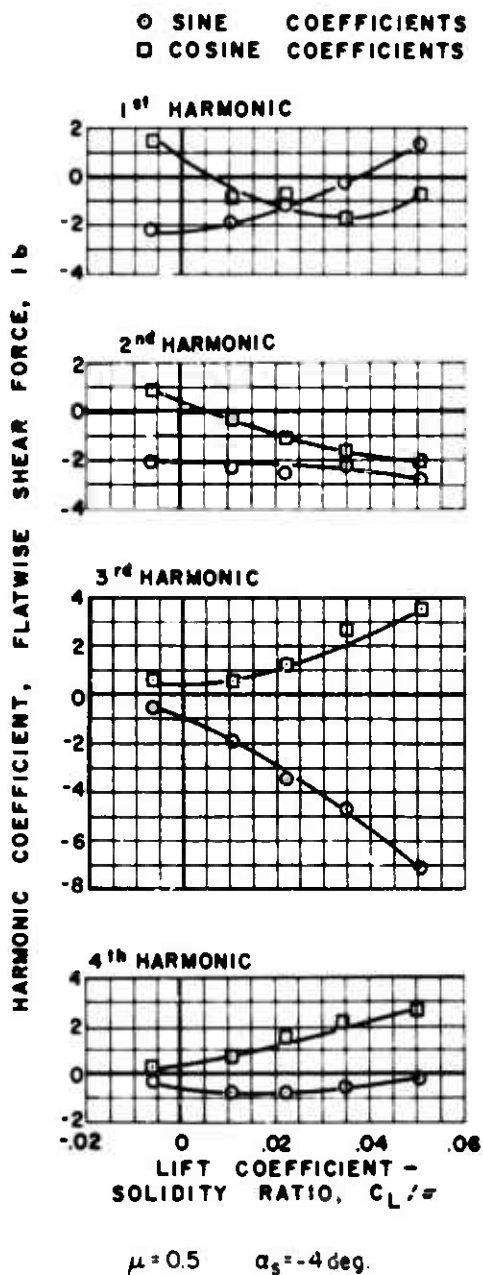


Figure 54(b). Concluded.



(a) FLATWISE

Figure 55. Experimental Shear Force, Zero Lag Damping.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS

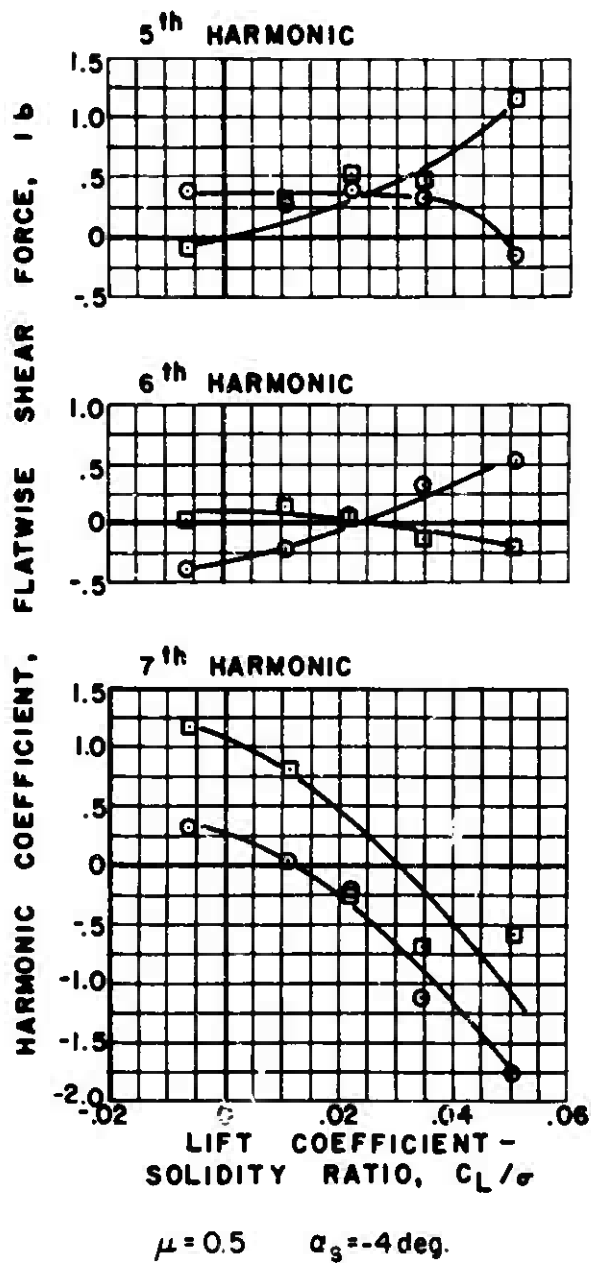
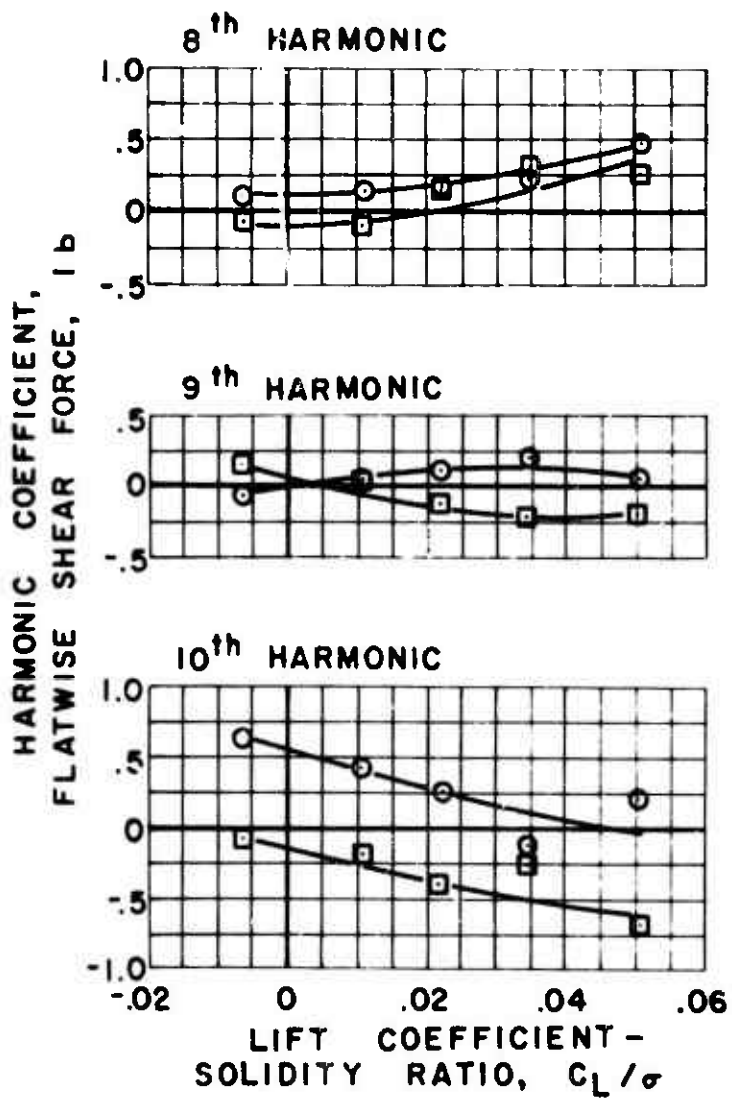


Figure 55(a). Continued.

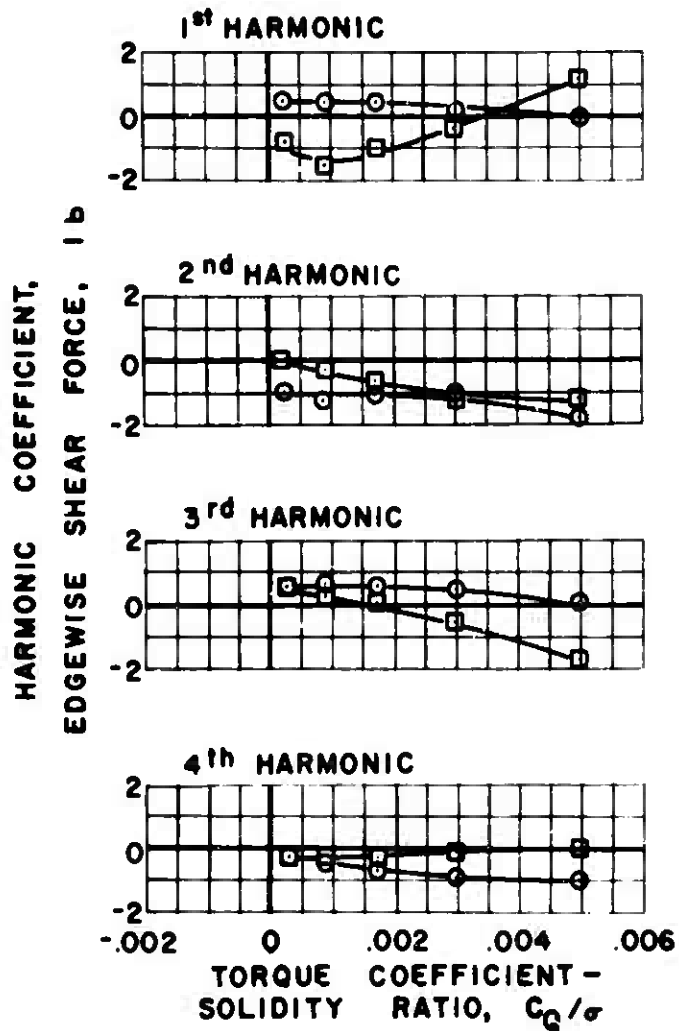
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4 \text{ deg.}$

Figure 55(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS

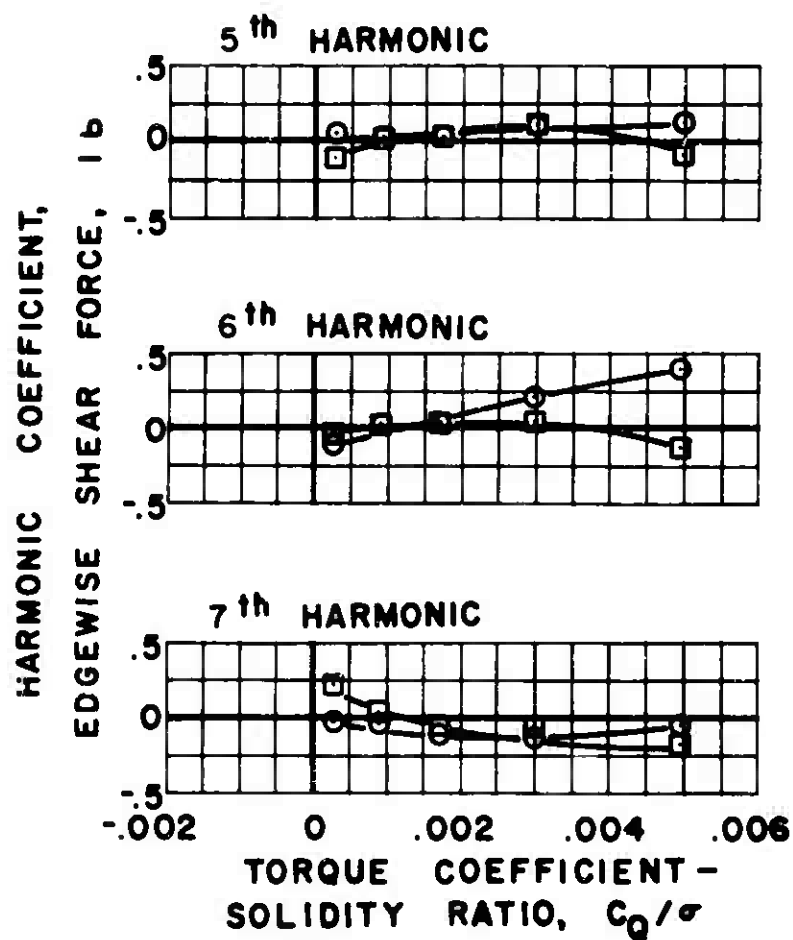


$\mu = 0.5$ $\alpha_s = -4 \text{ deg.}$

(b) EDGEWISE

Figure 55. Continued.

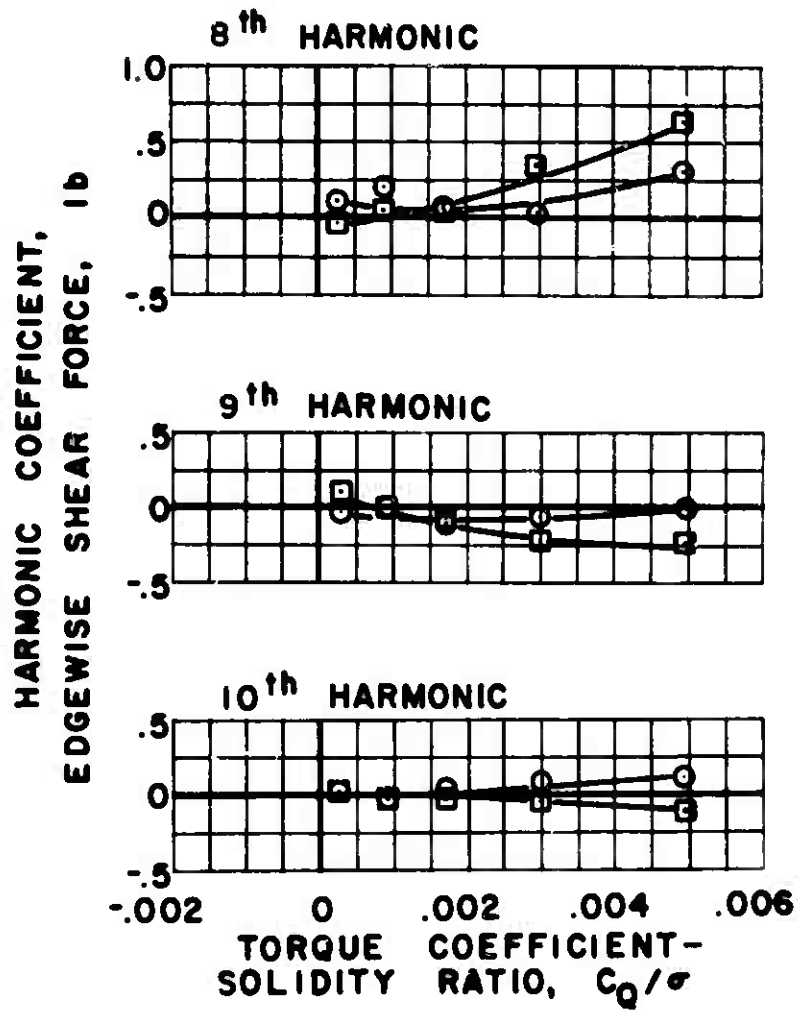
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4 \text{ deg.}$

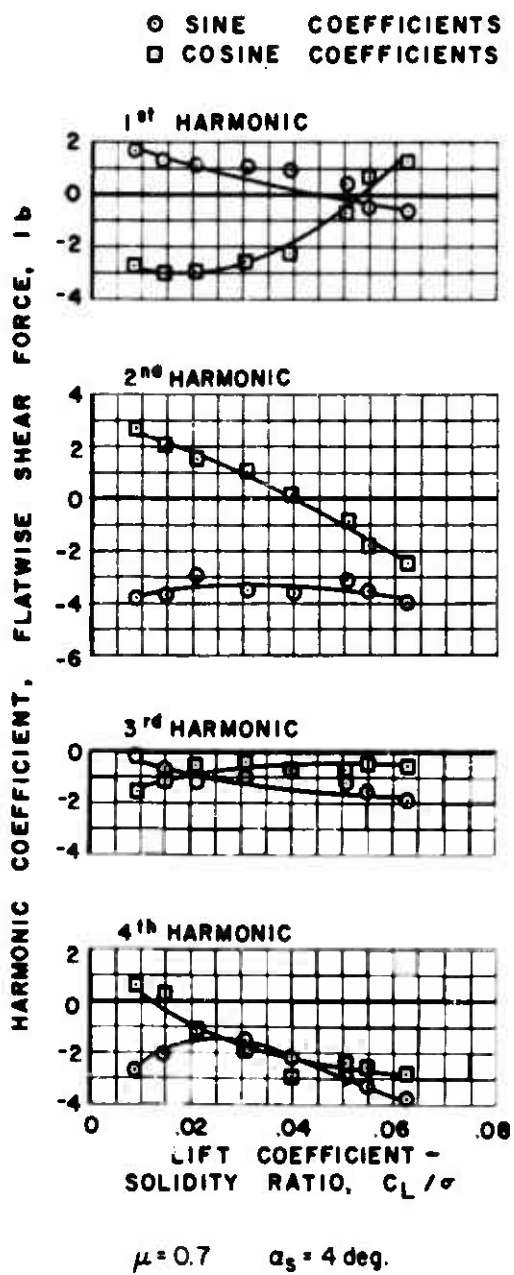
Figure 55(b). Continued.

⊙ SINE COEFFICIENTS
 ⊠ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4$ deg.

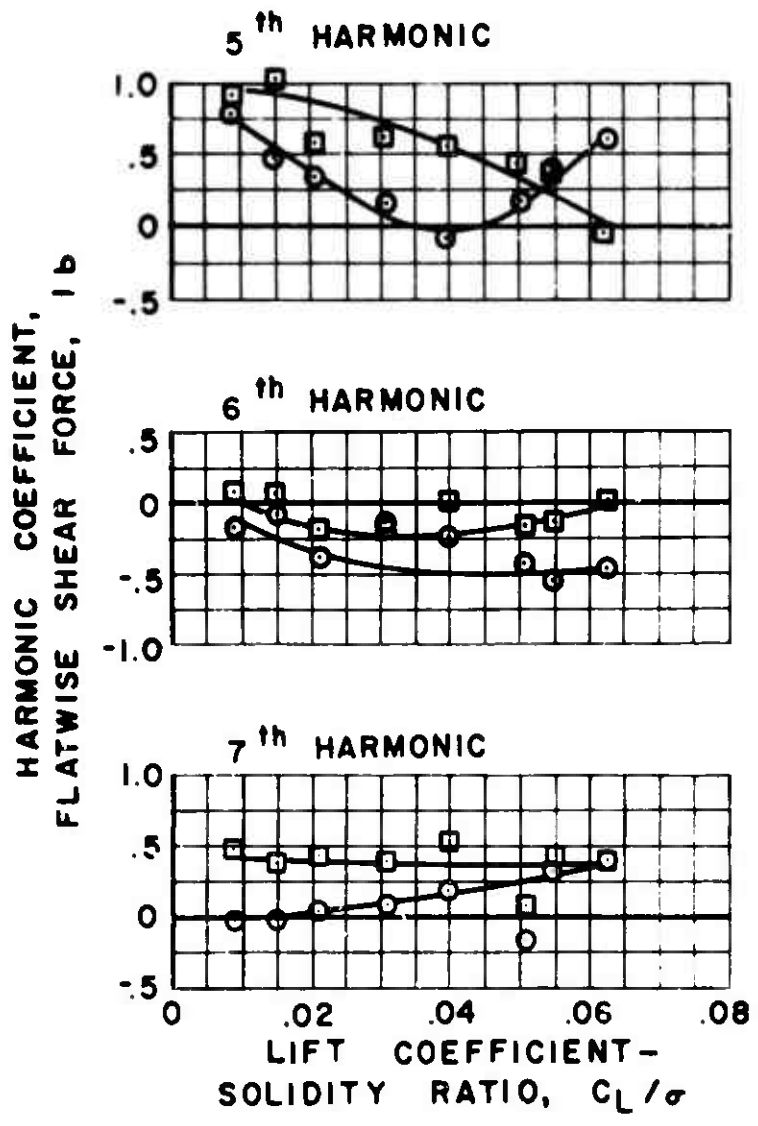
Figure 55(b). Concluded.



(a) FLATWISE

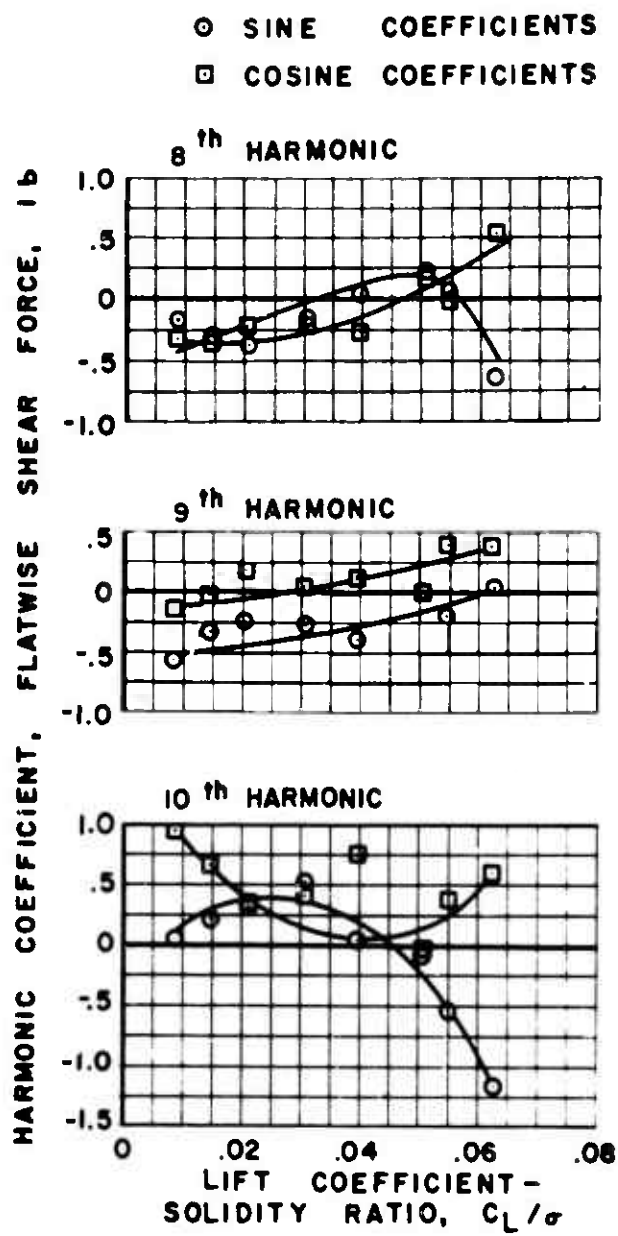
Figure 56. Experimental Shear Force.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



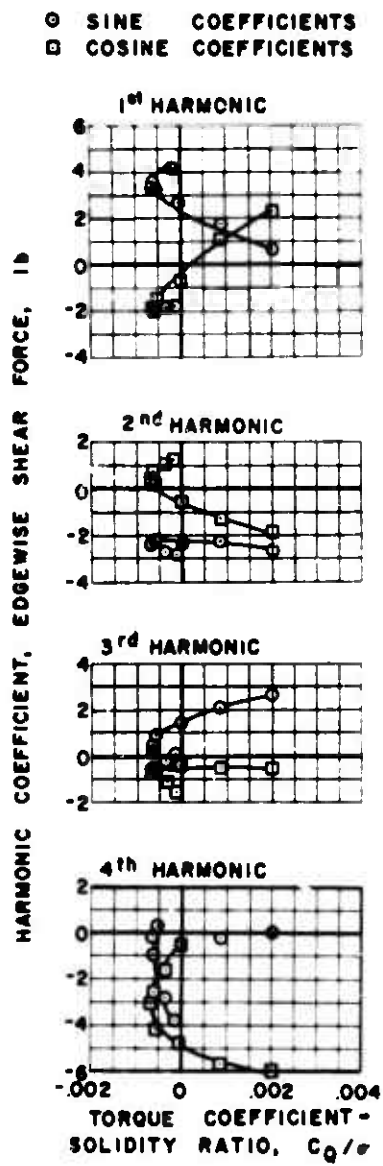
$\mu = 0.7$ $\alpha_s = 4$ deg.

Figure 56(a). Continued.



$\mu = 0.7$ $\alpha_s = 4 \text{ deg.}$

Figure 56(a). Continued.

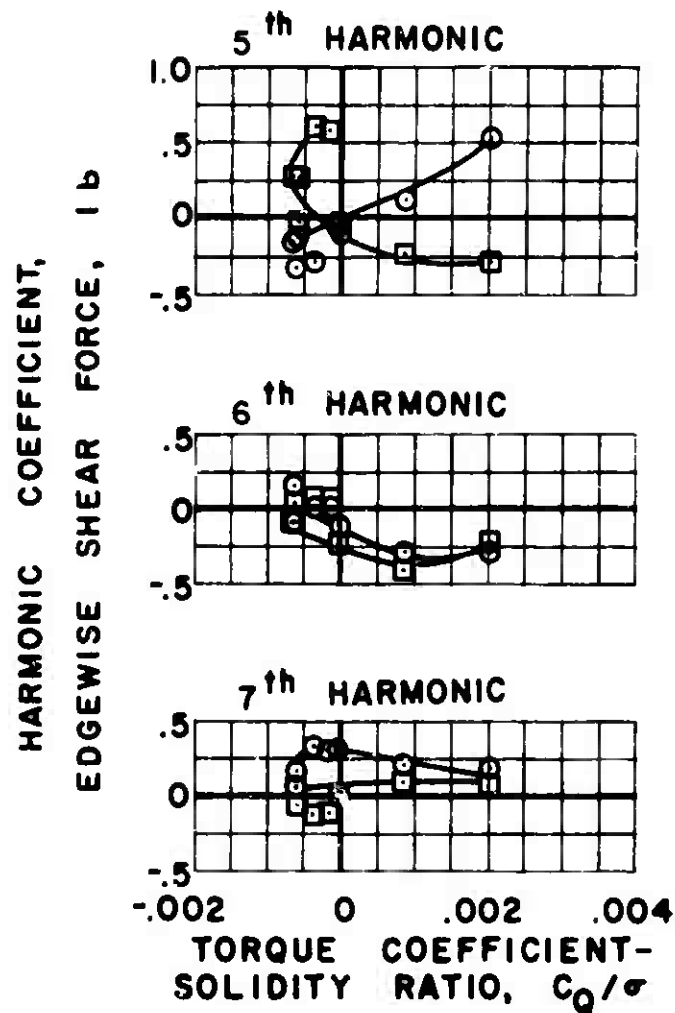


$\mu = 0.7$ $\alpha_s = 4 \text{ deg.}$

(b) EDGEWISE

Figure 56. Continued.

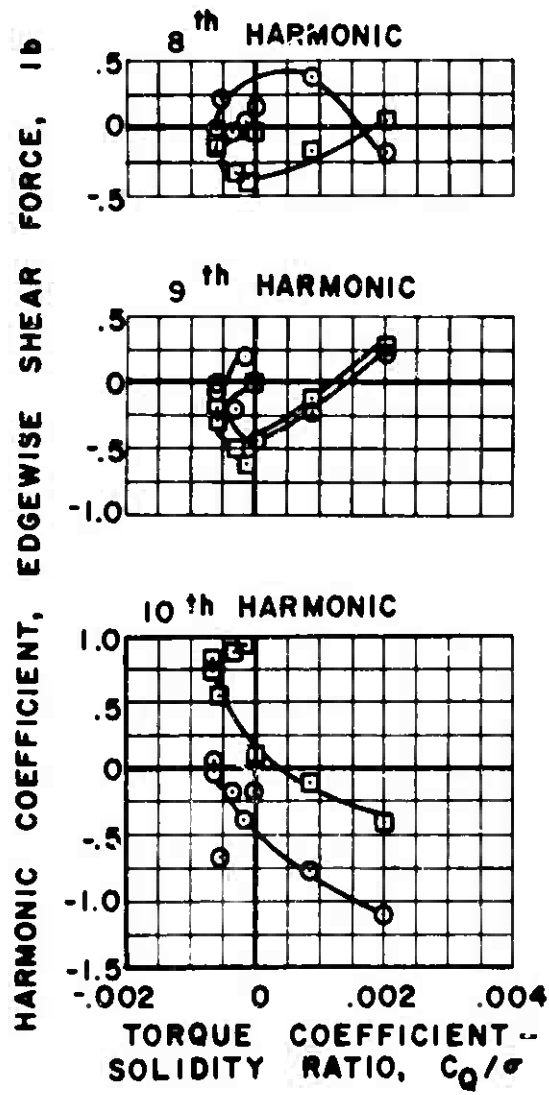
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = 4 \text{ deg.}$

Figure 56(b). Continued.

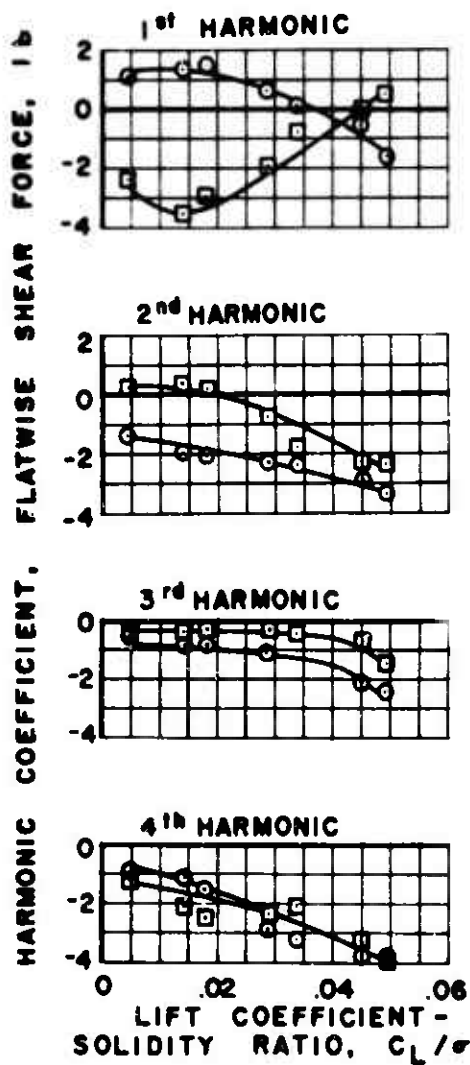
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = 4$ deg.

Figure 56(b). Concluded.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS

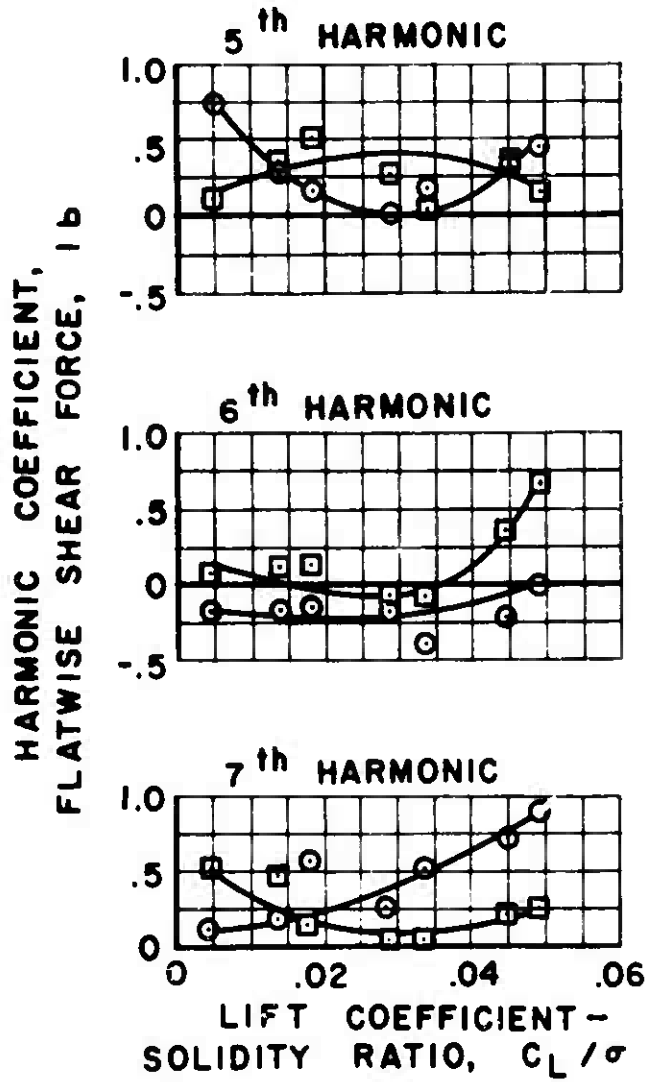


$\mu = 0.7$ $\alpha_s = 0$ deg.

(a) FLATWISE

Figure 57. Experimental Shear Force.

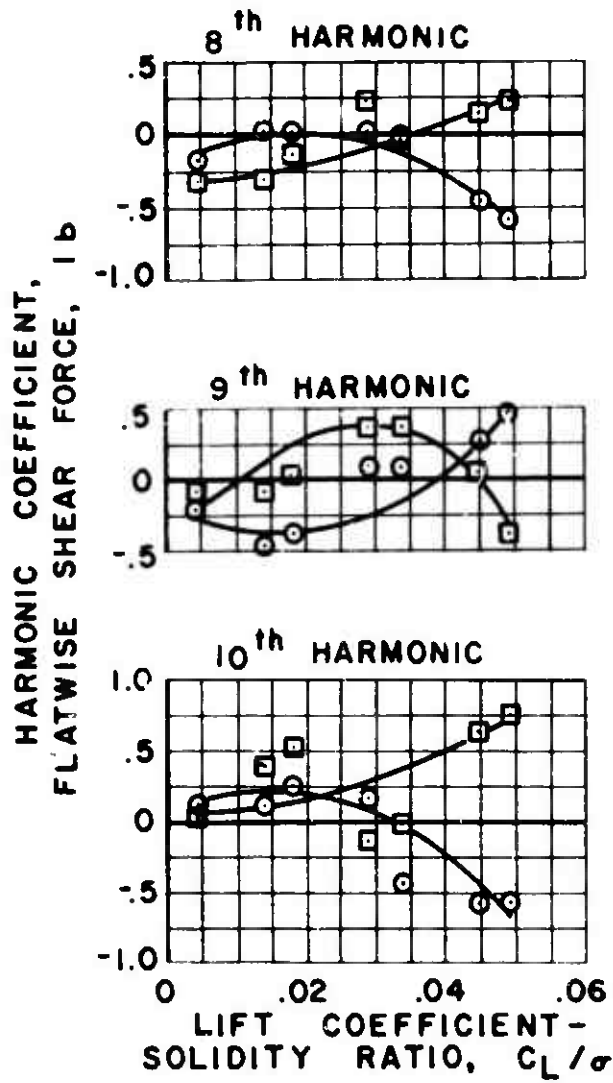
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = 0 \text{ deg.}$

Figure 57(a). Continued.

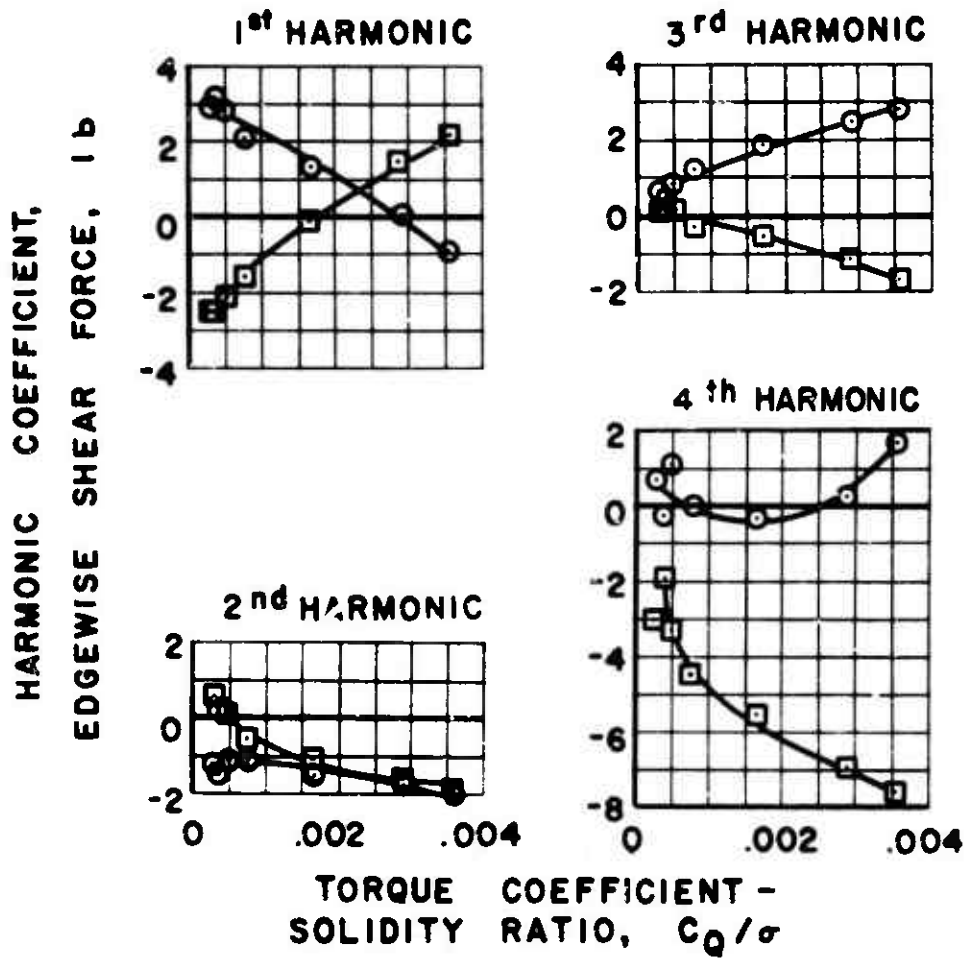
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = 0 \text{ deg.}$

Figure 57(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



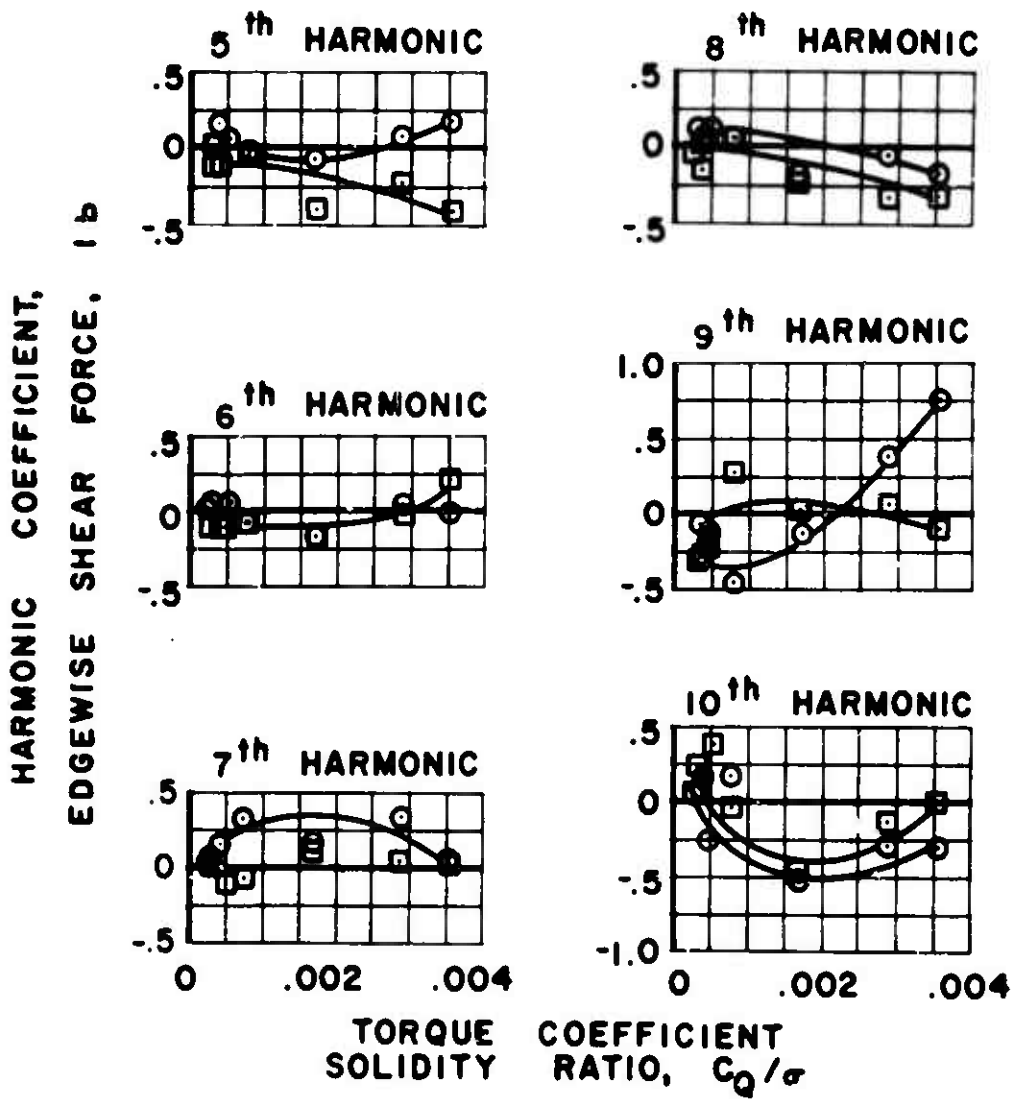
$\mu = 0.7$ $\alpha_s = 0 \text{ deg.}$

(b) EDGEWISE

Figure 57. Continued.

○ SINE COEFFICIENTS

□ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = 0 \text{ deg.}$

Figure 57(b). Concluded.

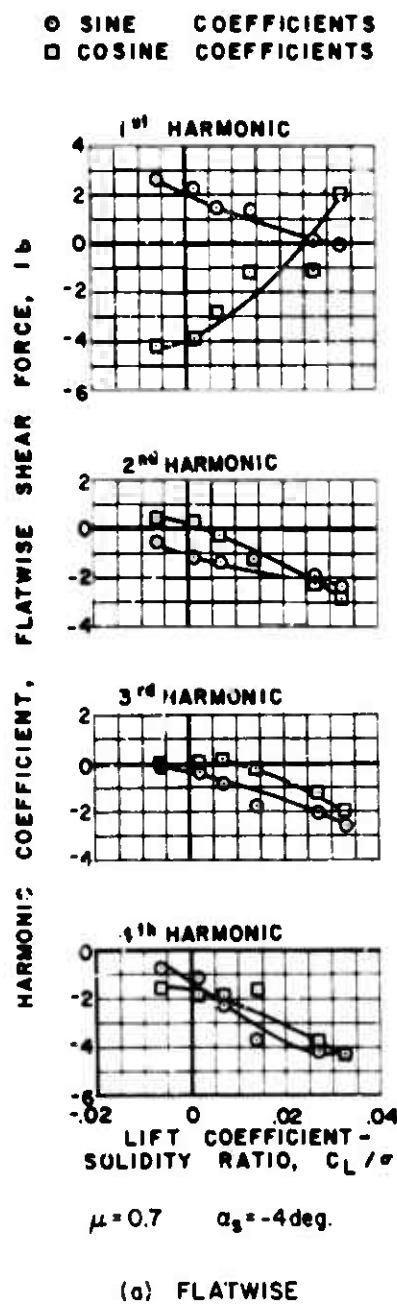
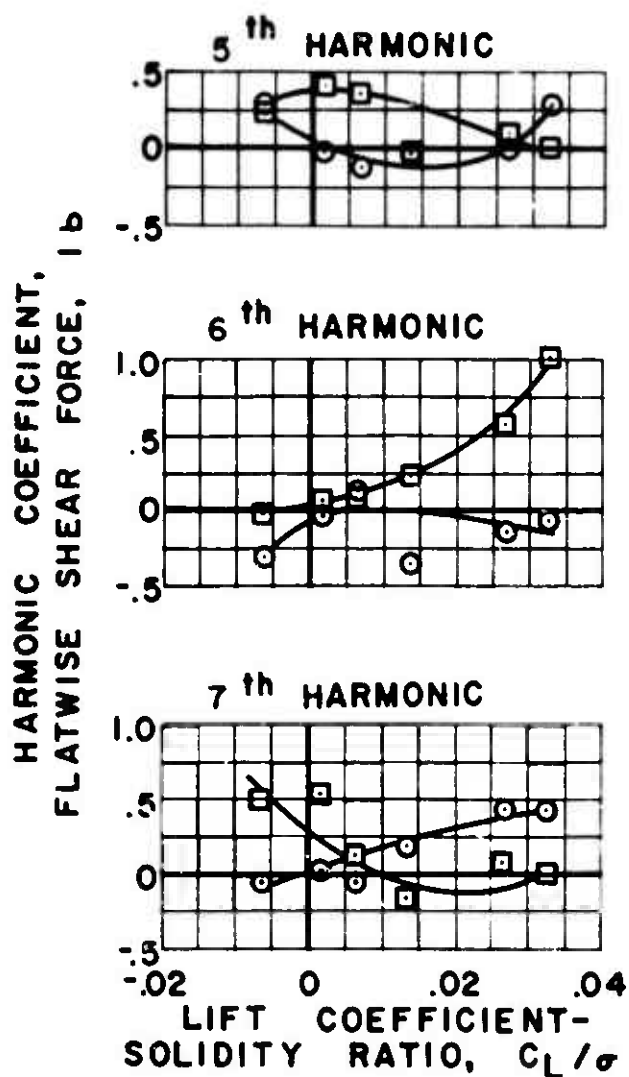


Figure 58. Experimental Shear Force.

⊙ SINE COEFFICIENTS
 ⊠ COSINE COEFFICIENTS

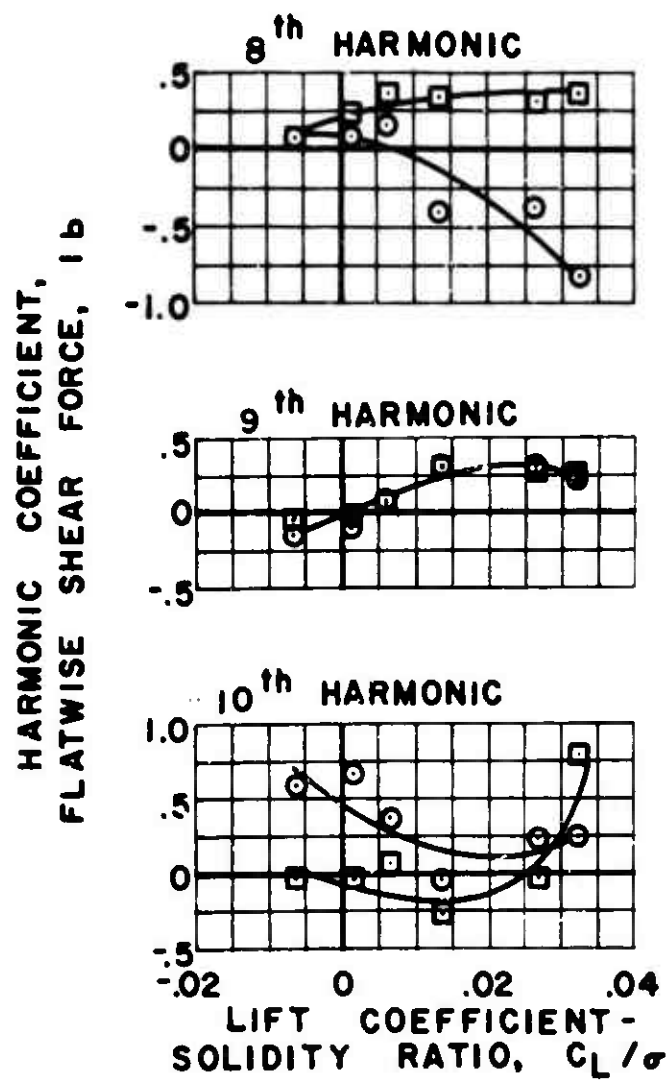


$\mu = 0.7$ $\alpha_s = -4 \text{ deg.}$

Figure 58(a). Continued.

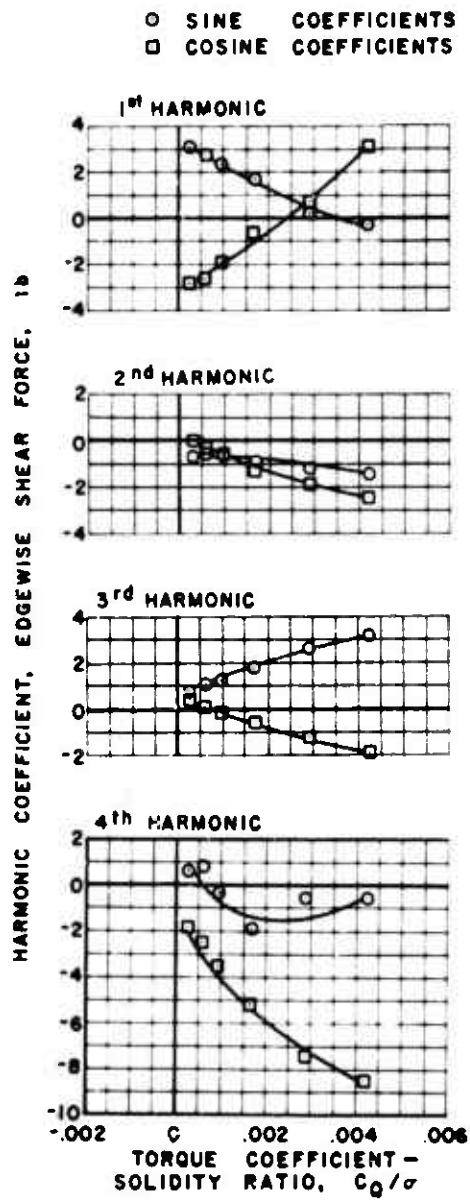
○ SINE COEFFICIENTS

□ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = -4$ deg.

Figure 58(a). Continued.

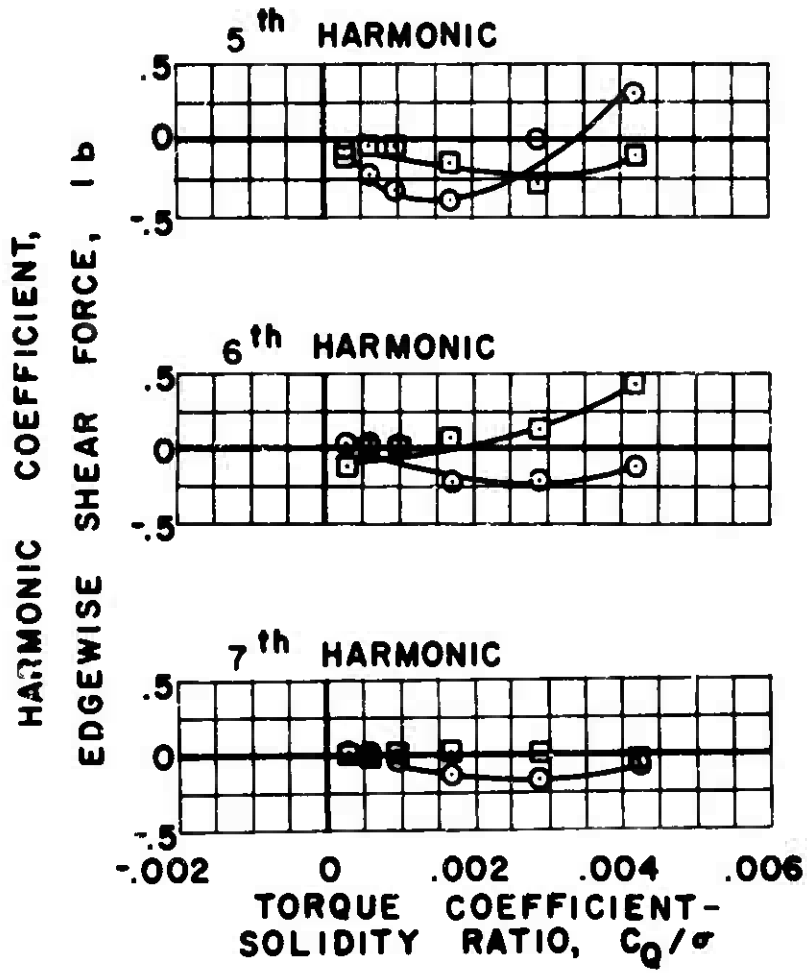


$\mu = 0.7$ $\alpha_s = -4 \text{ deg.}$

(b) EDGEWISE

Figure 58. Continued.

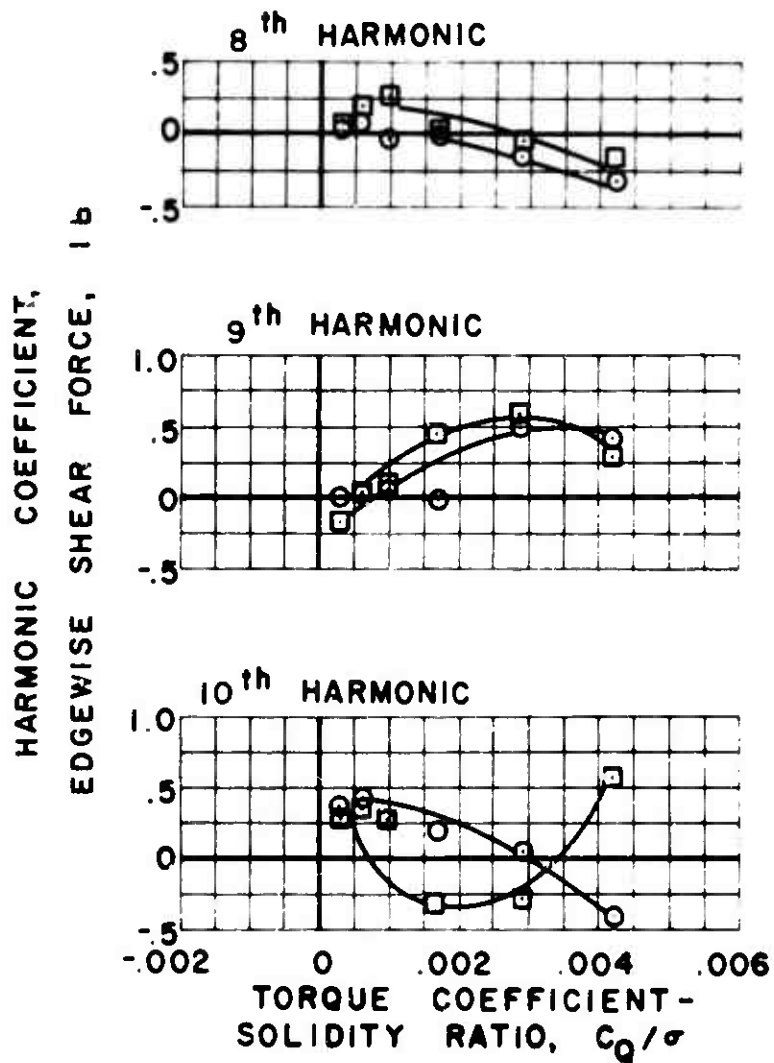
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = -4$ deg.

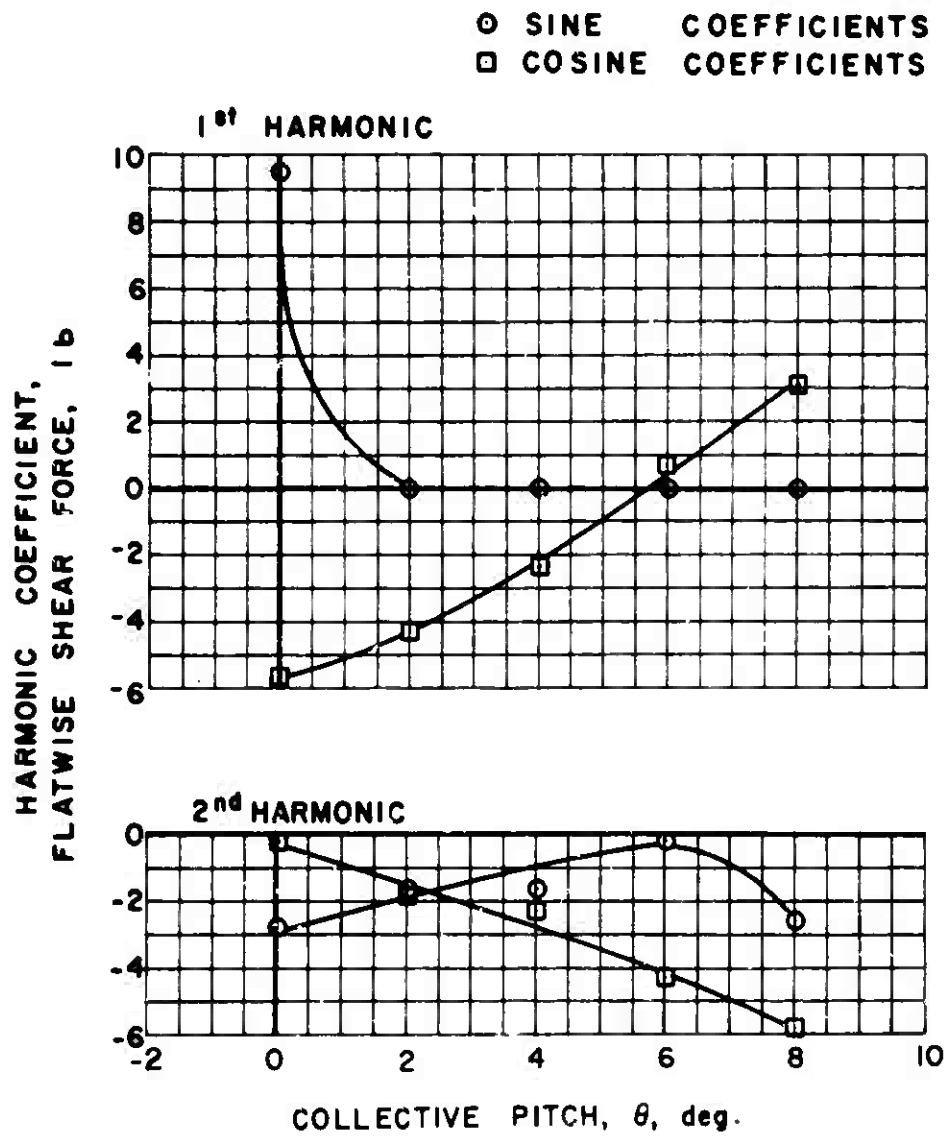
Figure 58(b). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_s = -4 \text{ deg.}$

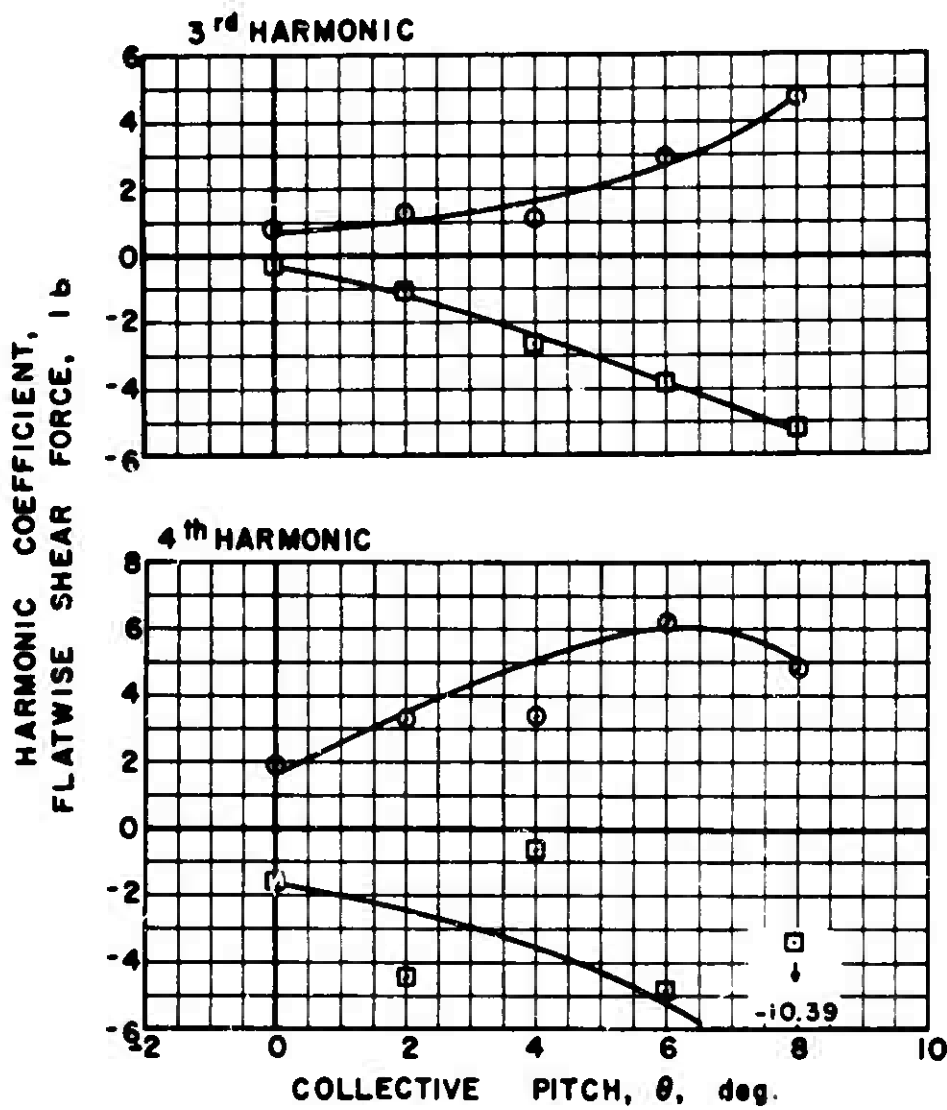
Figure 58(b). Concluded.



(a) FLATWISE

Figure 59. Experimental Shear Force.

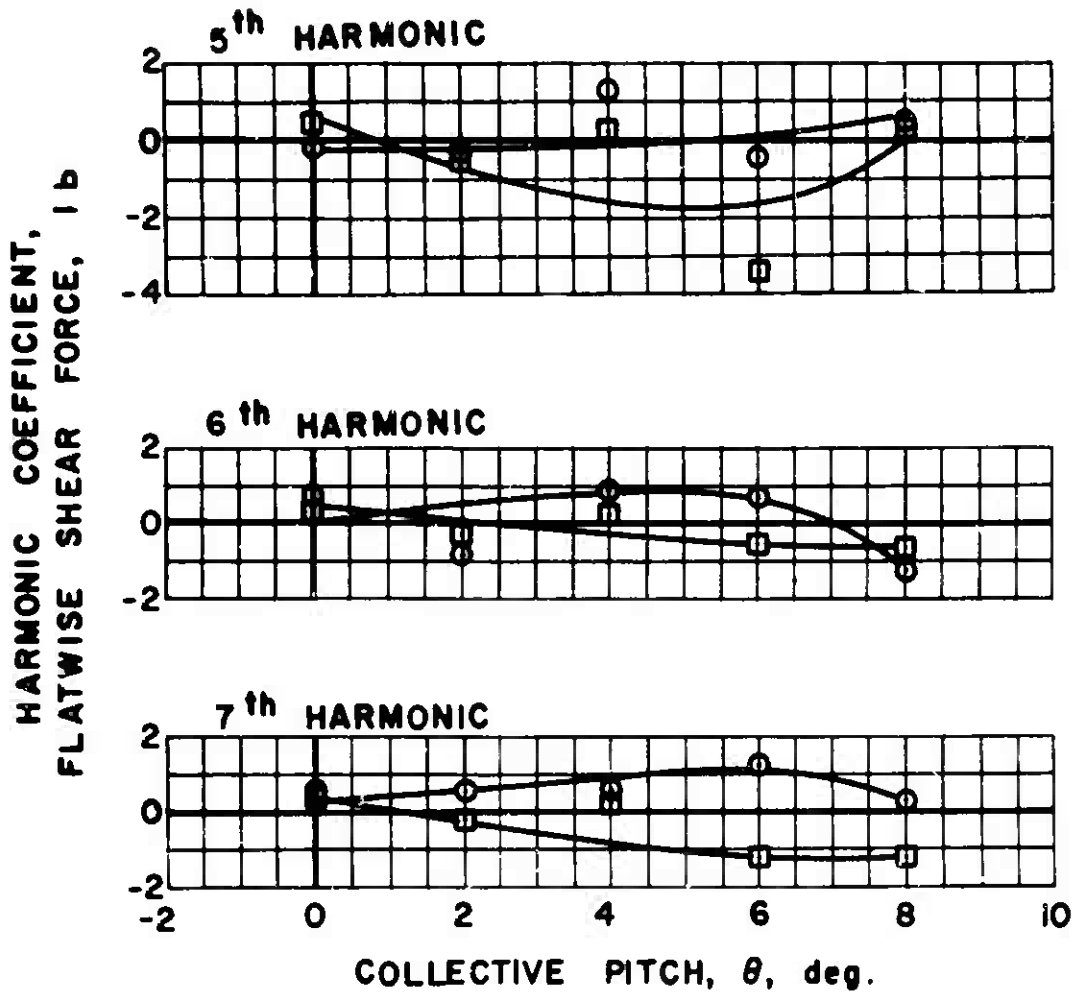
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 1.0$ $\alpha_s = 0$ deg.

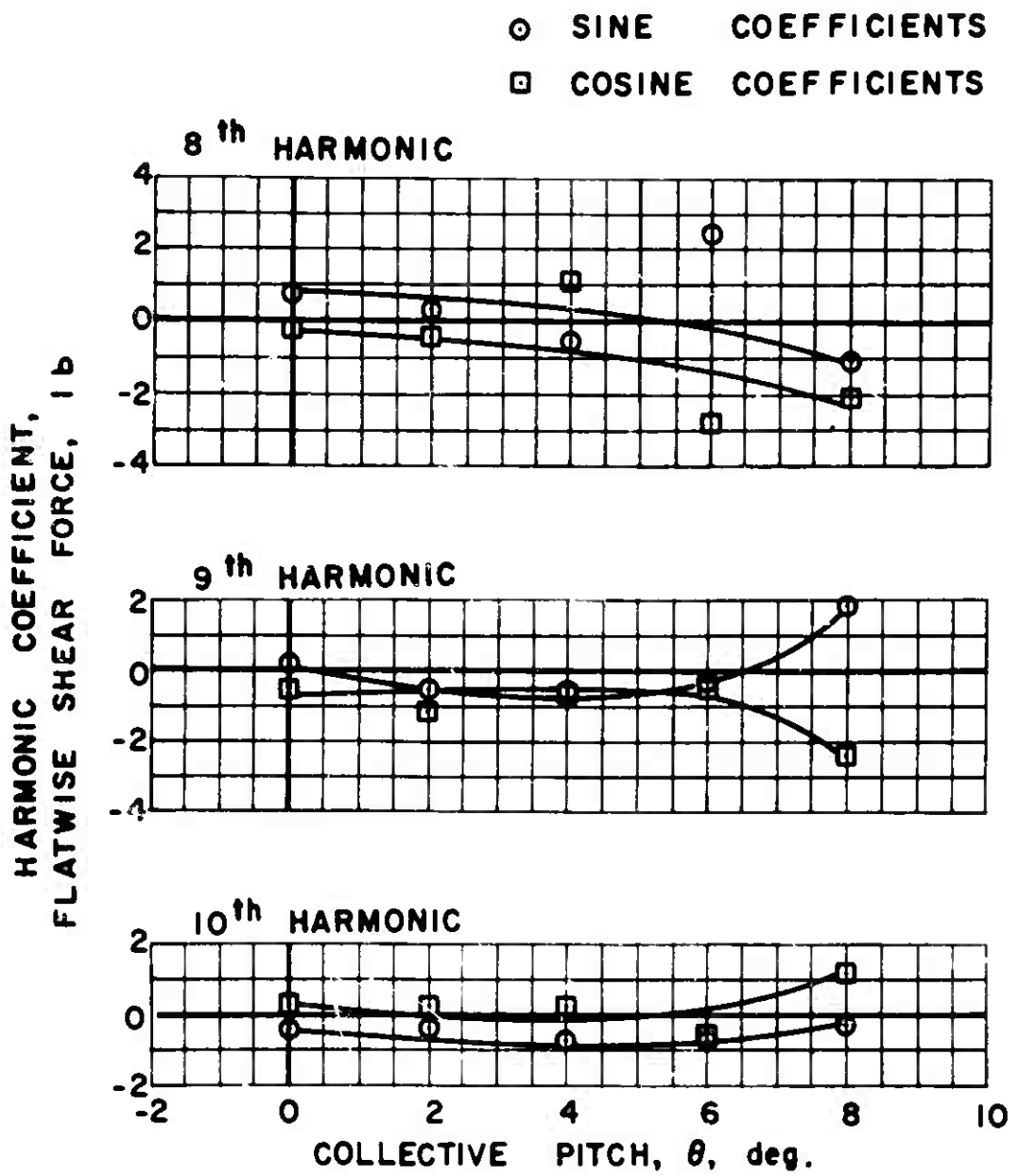
Figure 59(a). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 1.0$ $\alpha_s = 0 \text{ deg.}$

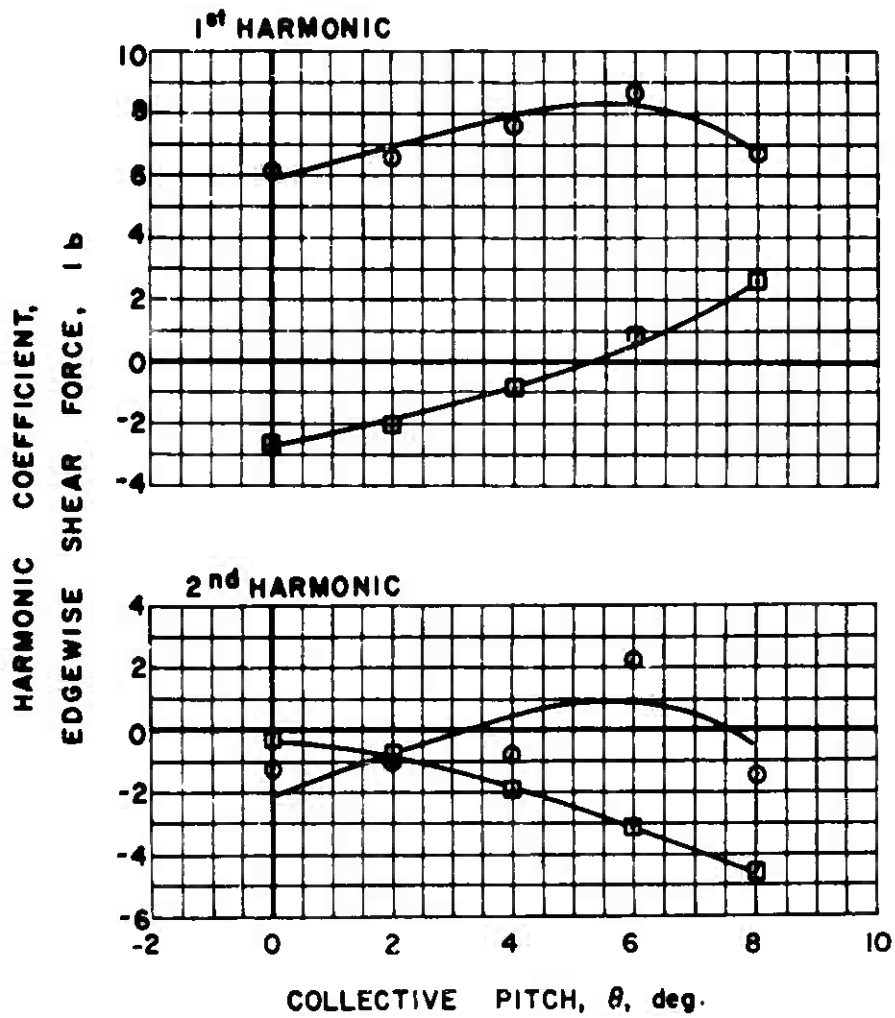
Figure 59(a). Continued.



$\mu = 1.0 \quad \alpha_s = 0 \text{ deg.}$

Figure 59(a). Continued.

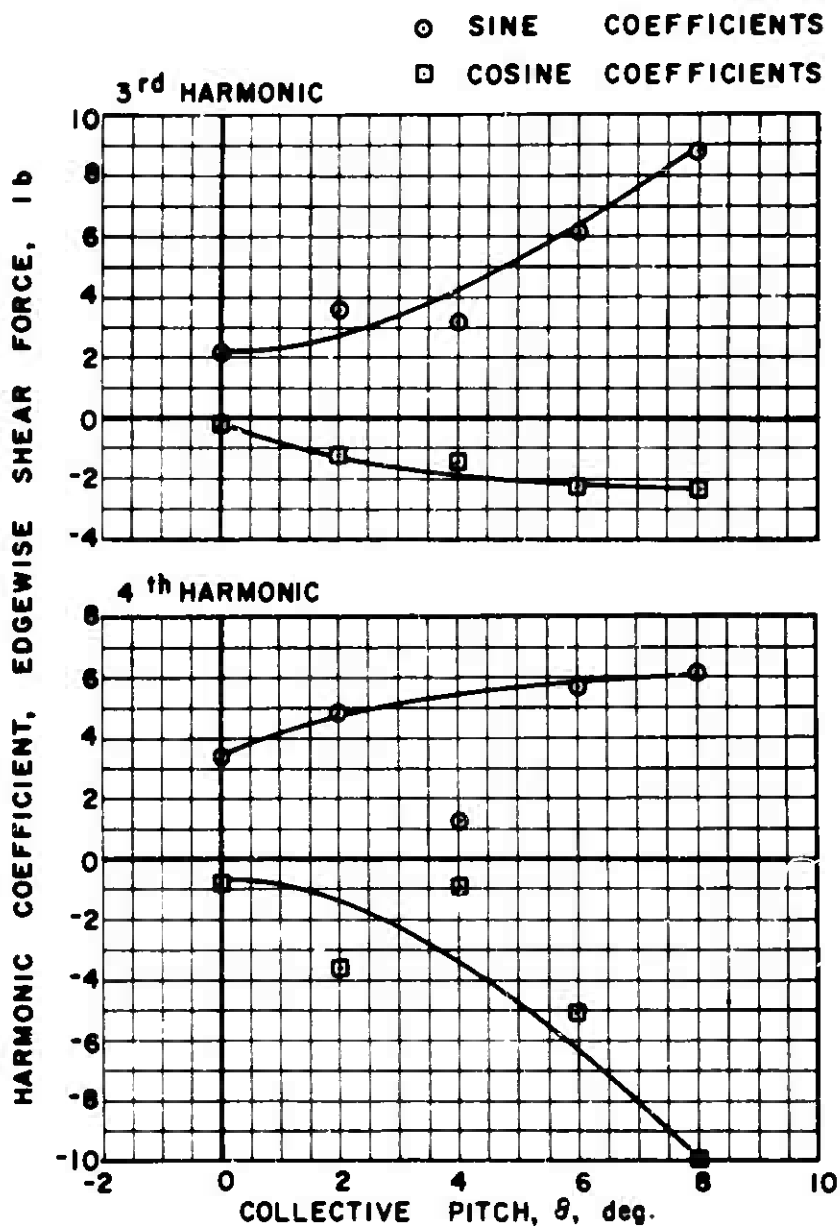
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 1.0$ $\alpha_s = 0$ deg.

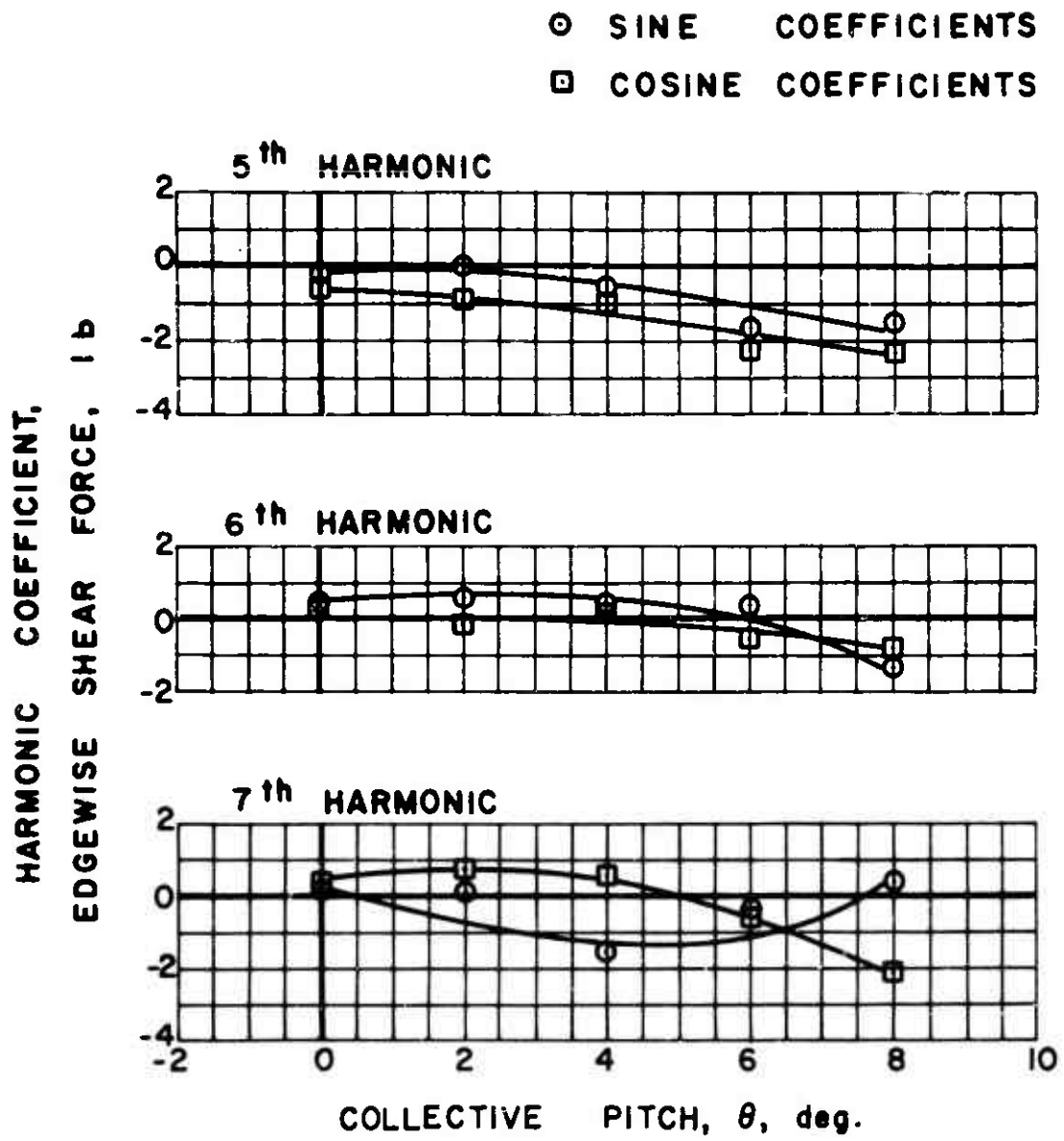
(b) EDGEWISE

Figure 59. Continued.



$\mu = 1.0$ $\alpha_s = 0 \text{ deg.}$

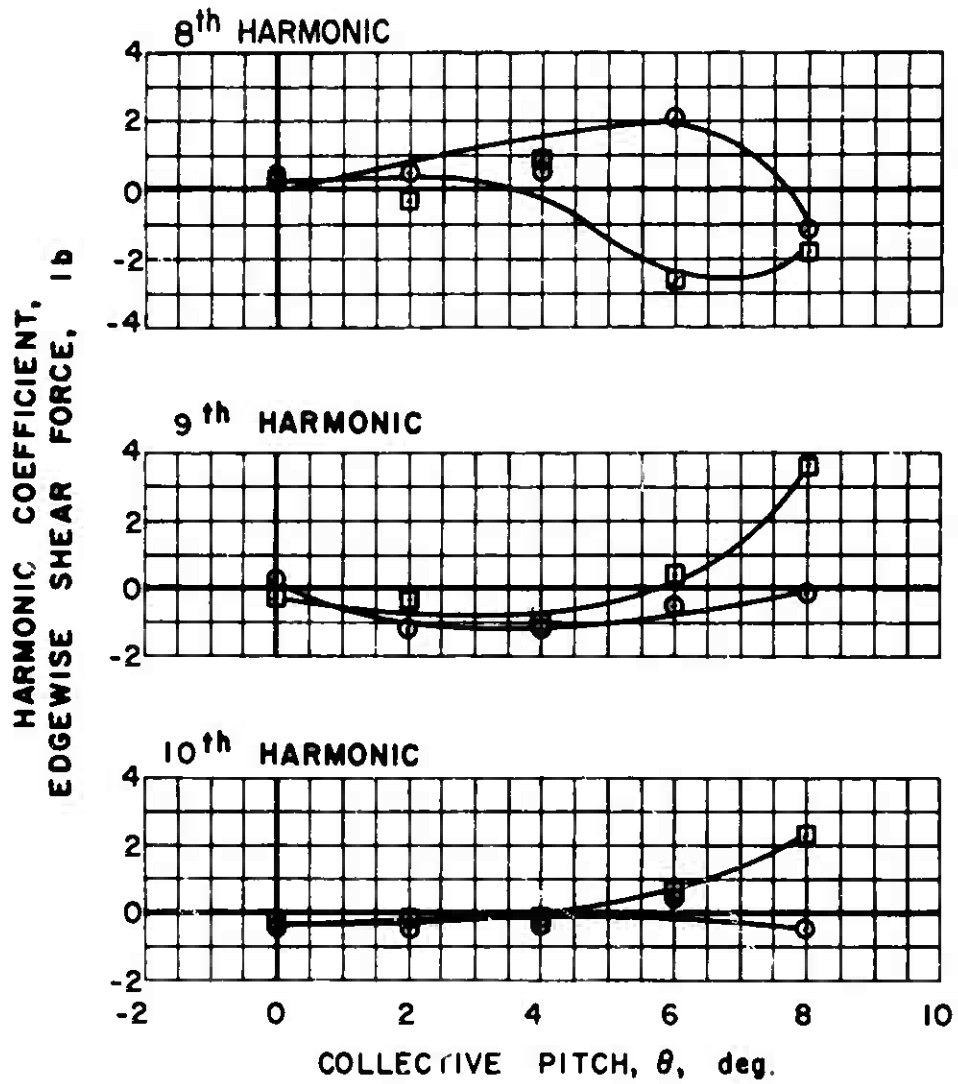
Figure 59(b). Continued.



$\mu = 1.0 \quad \alpha_s = 0 \text{ deg.}$

Figure 59(b). Continued.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 1.0$ $\alpha_s = 0 \text{ deg.}$

Figure 59(b). Concluded.

APPENDIX II
 EXPERIMENTAL RADIAL SHEAR FORCE FIGURES

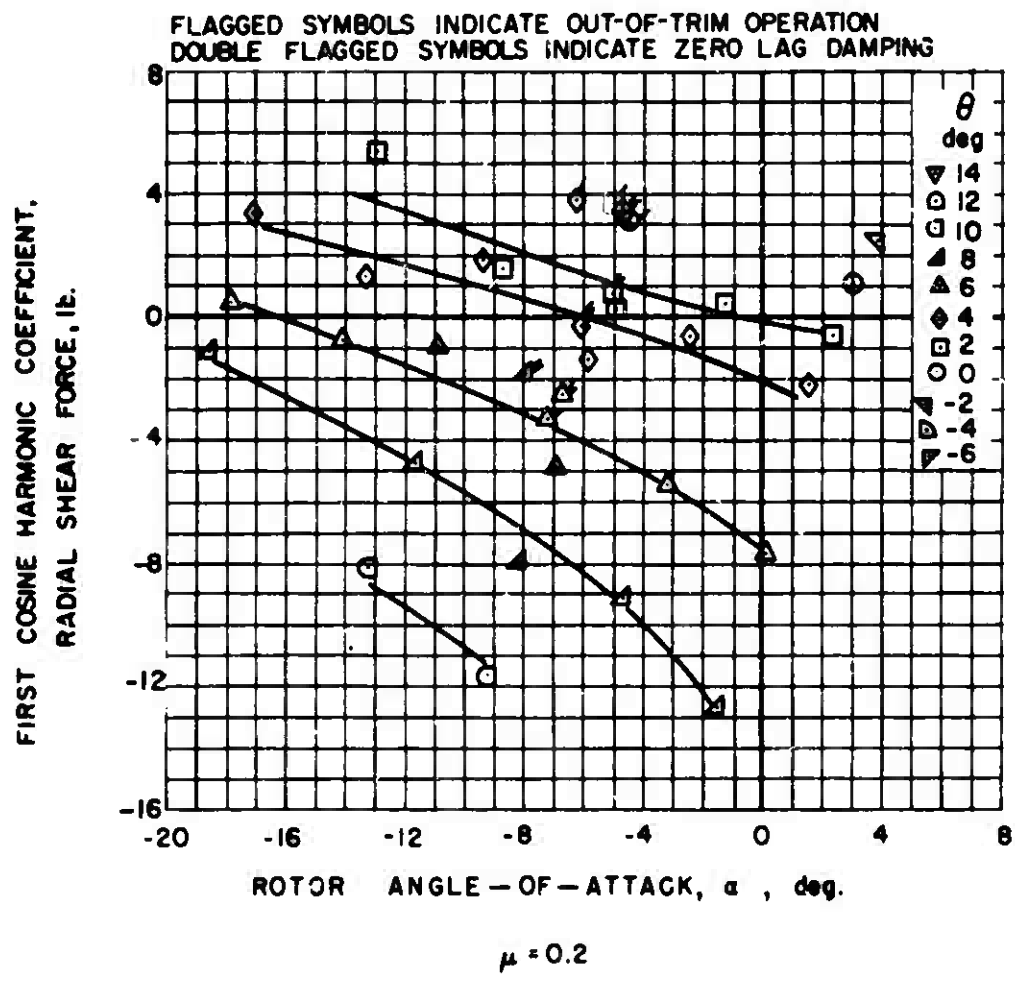


Figure 60. Experimental Radial Shear Force.

FIRST COSINE HARMONIC COEFFICIENT,
 RADIAL SHEAR FORCE, lb.

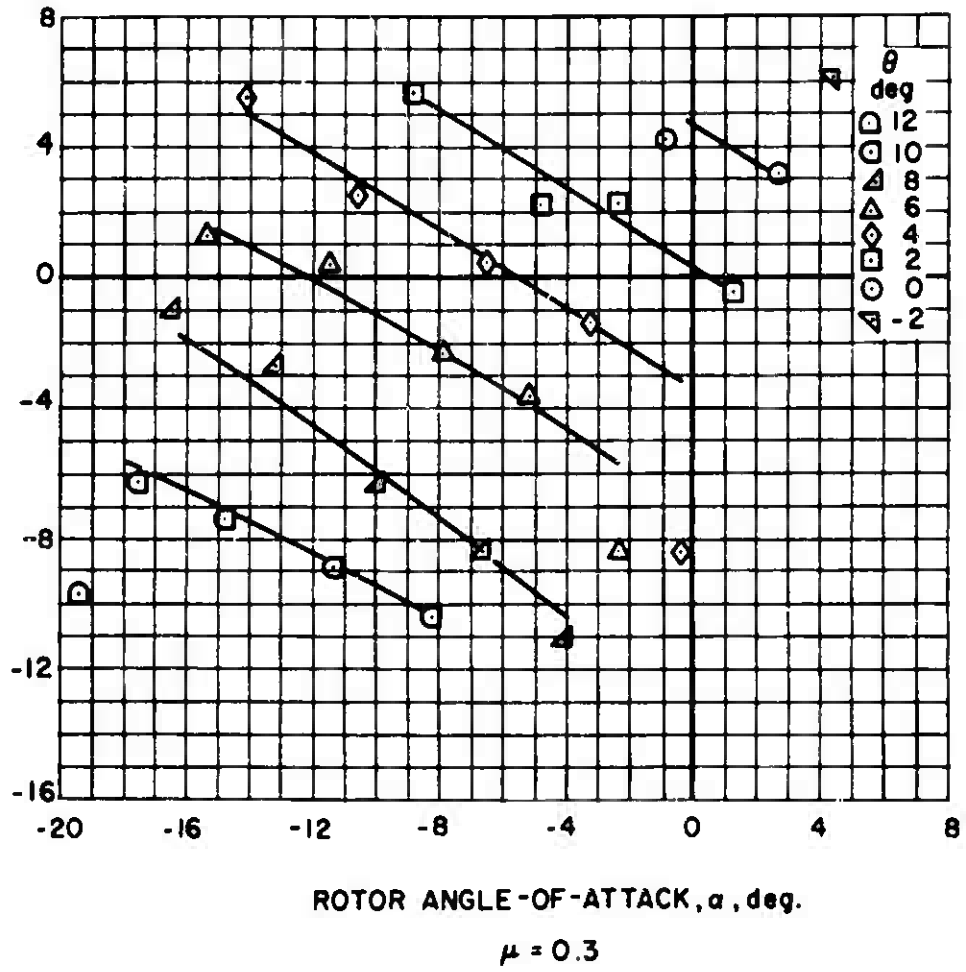


Figure 61. Experimental Radial Shear Force.

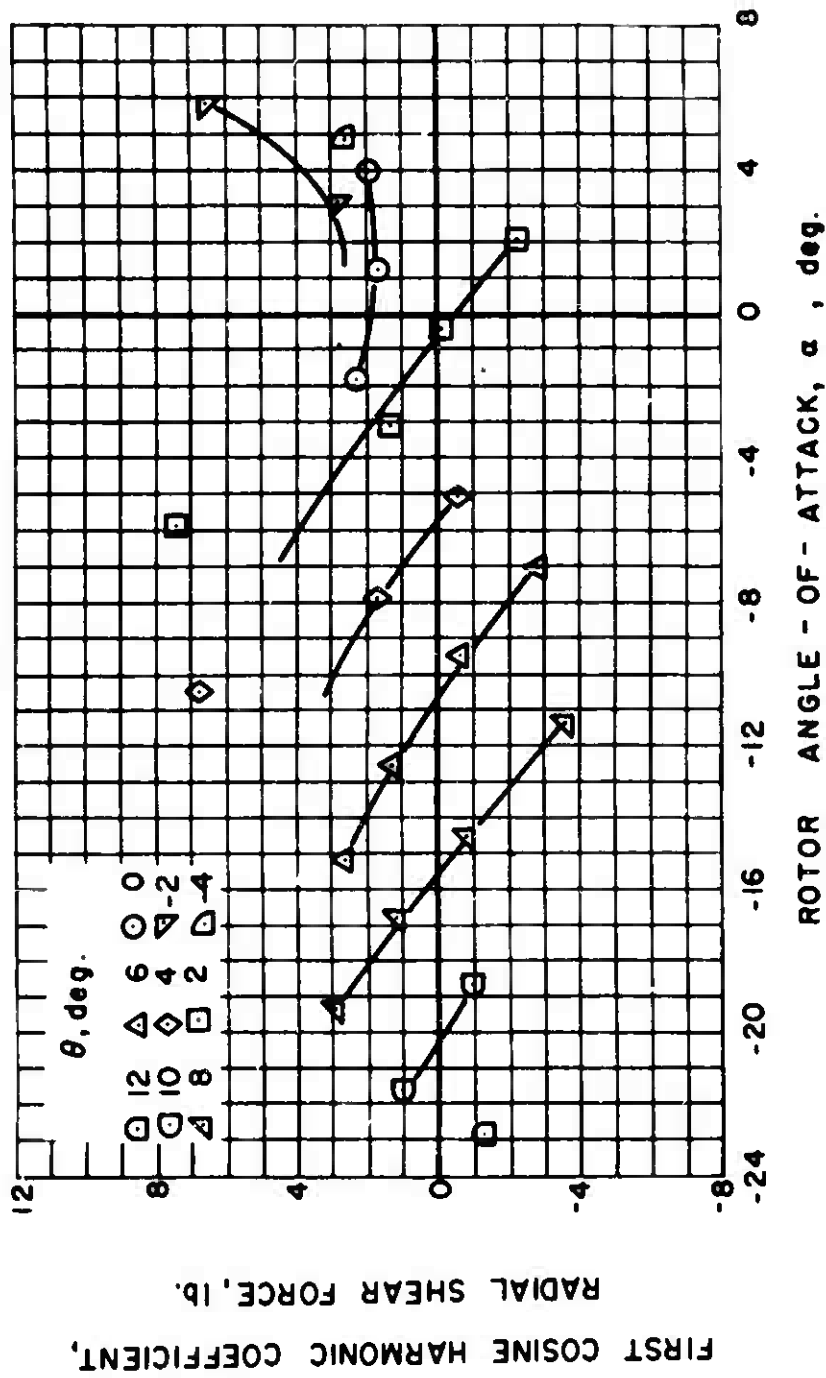


Figure 62. Experimental Radial Shear Force.

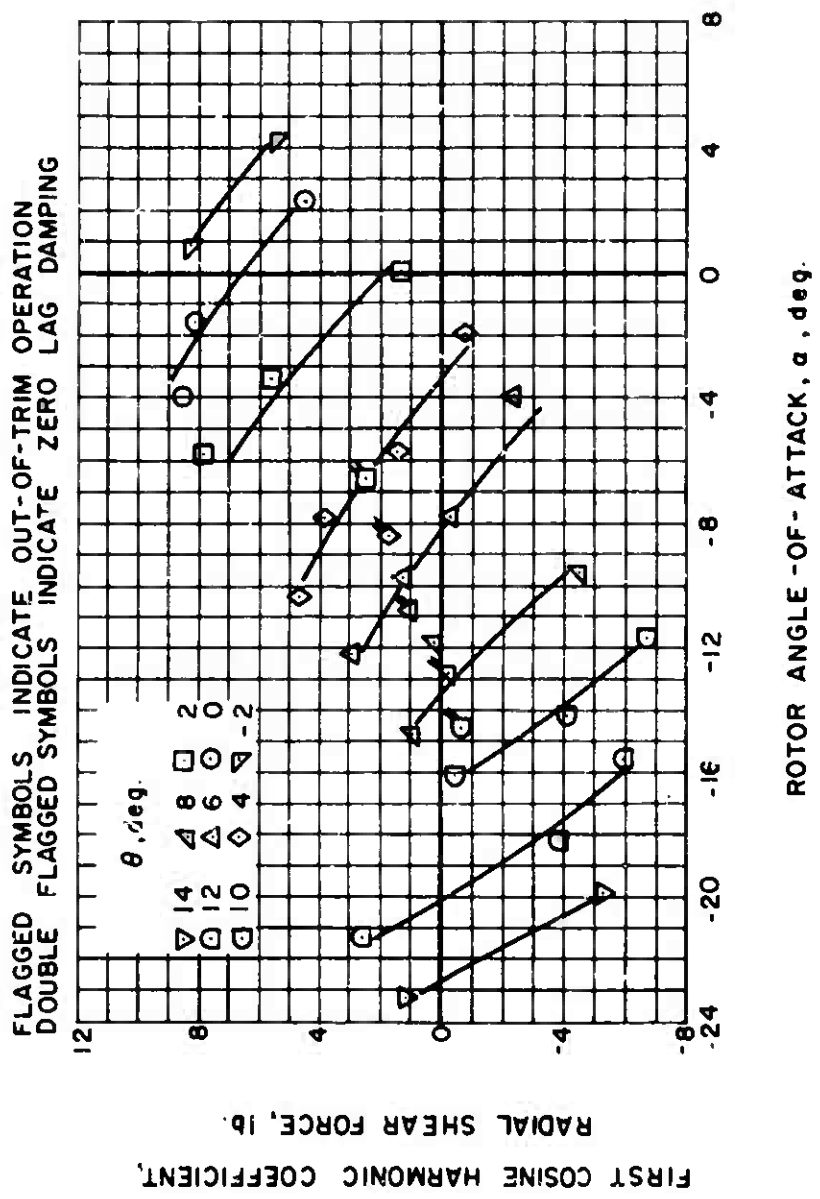


Figure 63. Experimental Radial Shear Force.

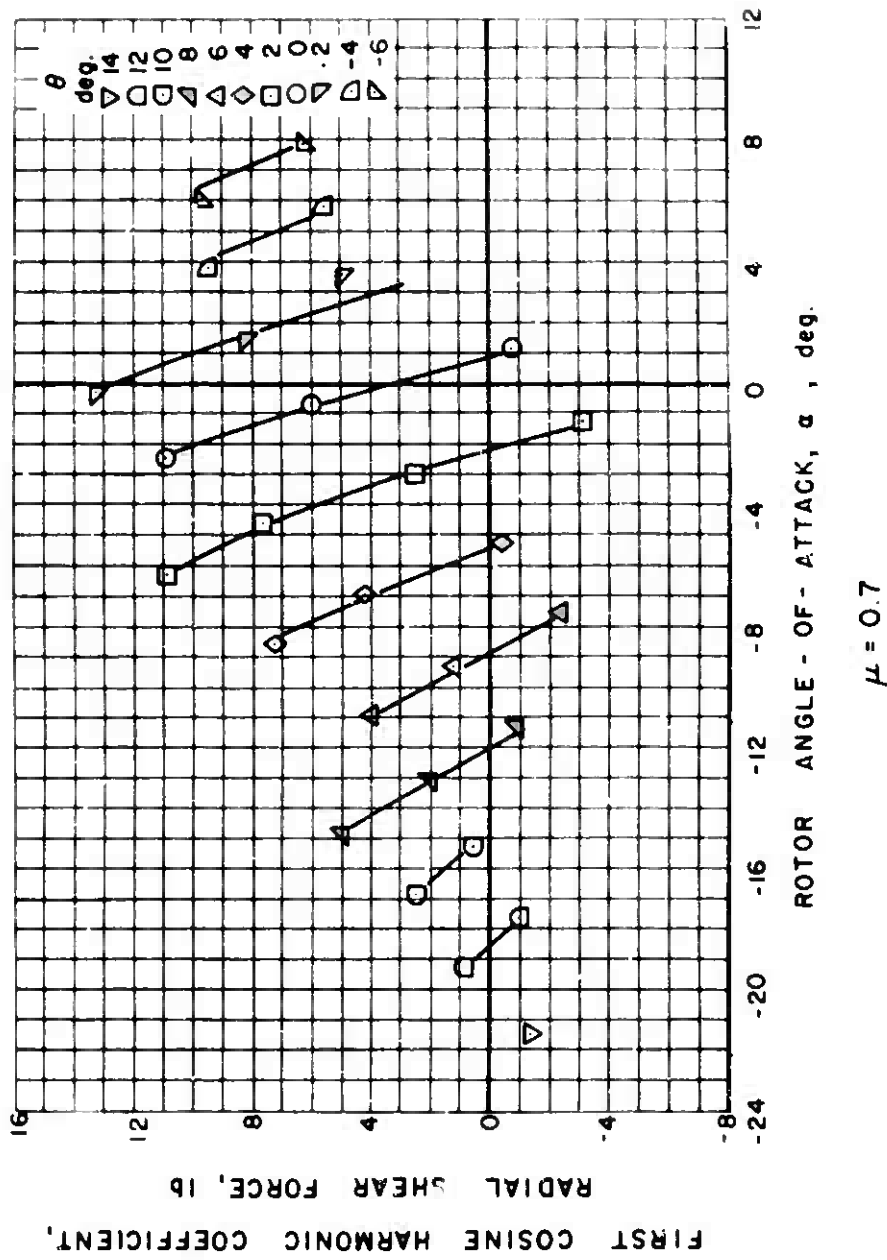


Figure 64. Experimental Radial Shear Force.

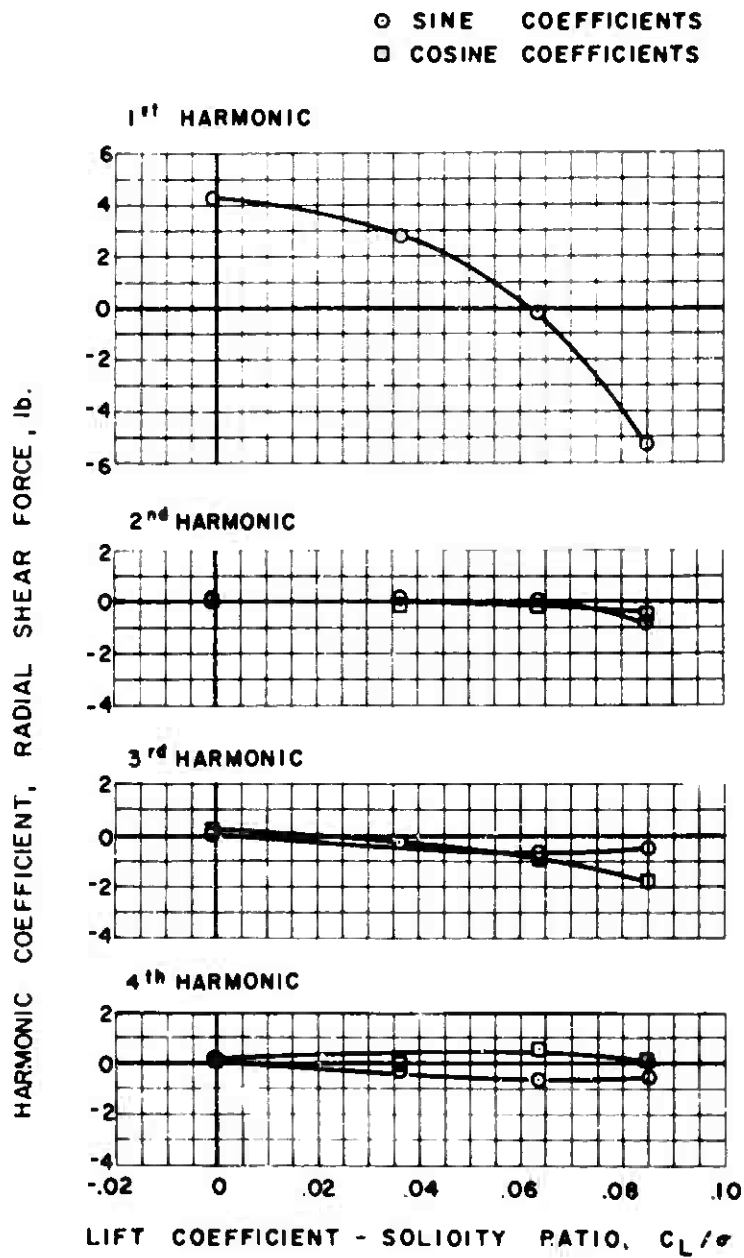
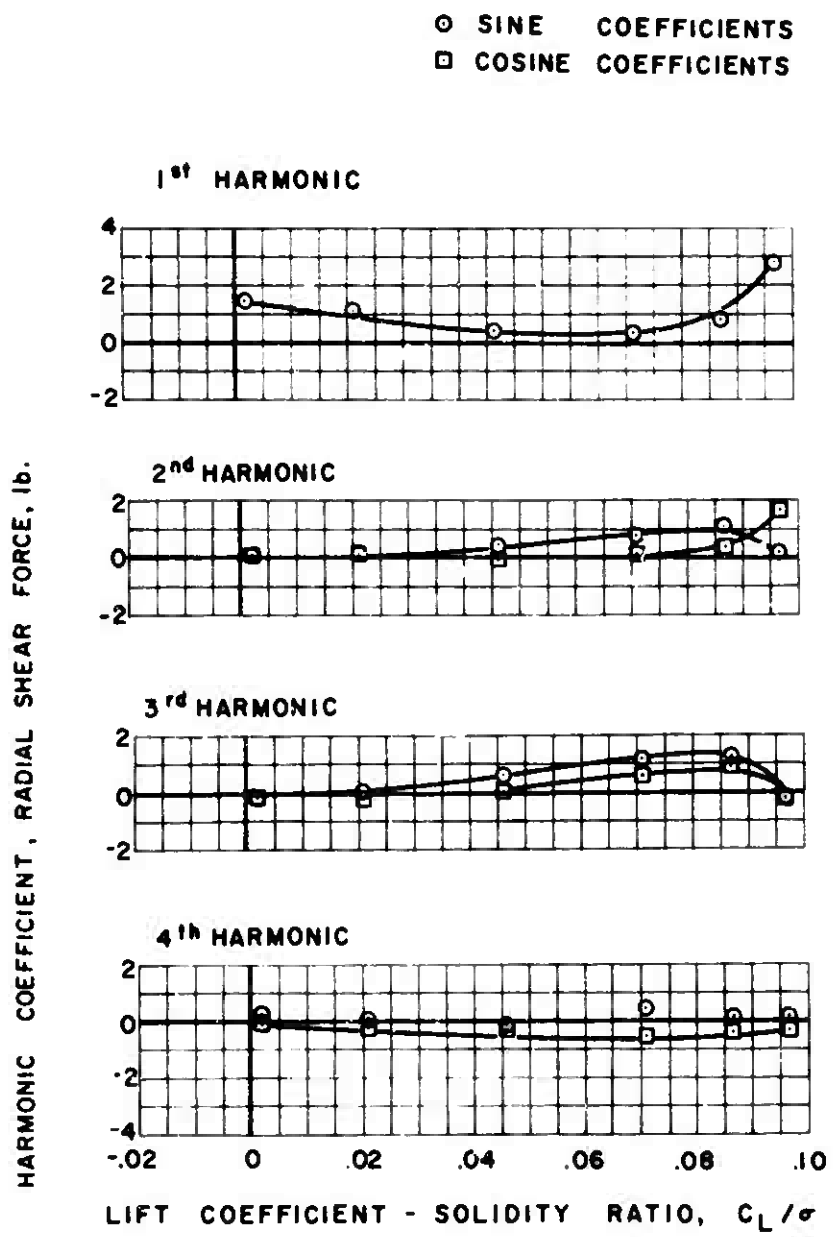
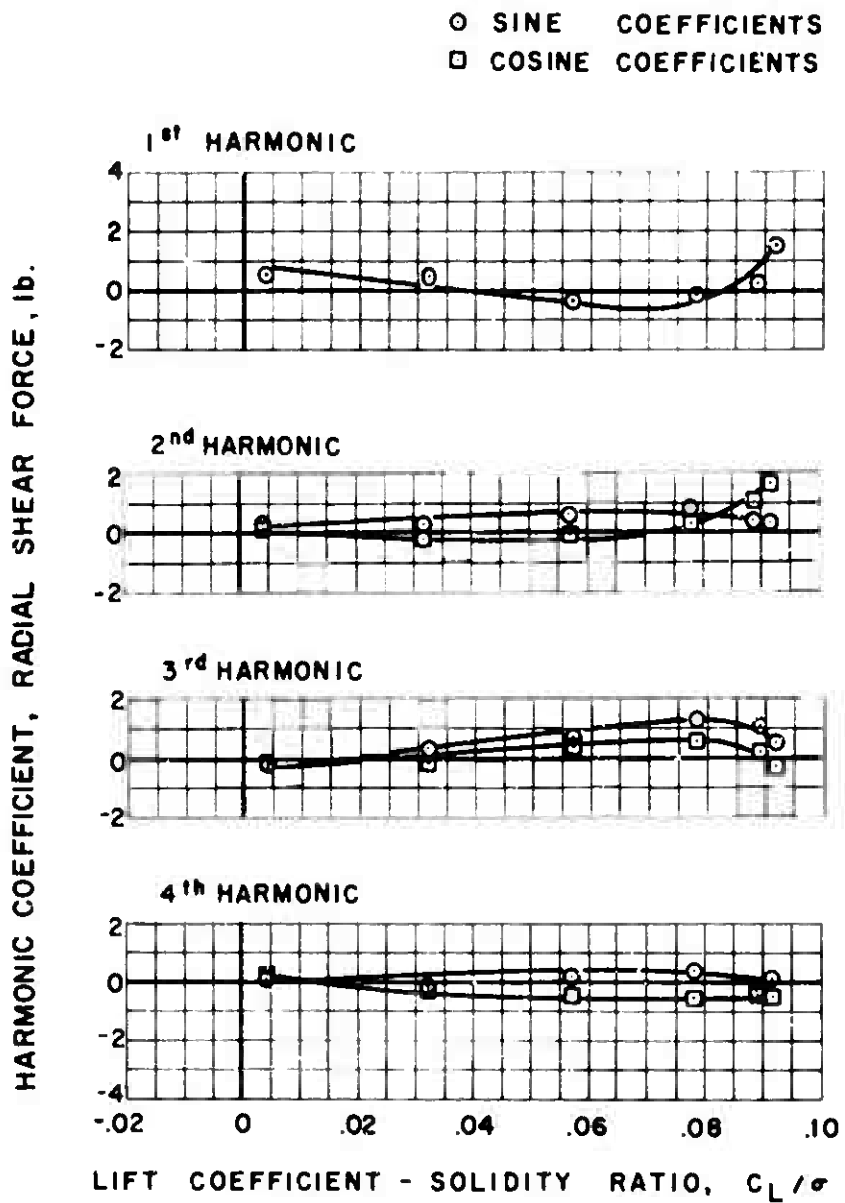


Figure 65. Experimental Radial Shear Force.



$\mu = 0.2 \quad \alpha_s = -4 \text{ deg.}$

Figure 66. Experimental Radial Shear Force.



$$\mu = 0.2 \quad \alpha_s = -8 \text{ deg.}$$

Figure 67. Experimental Radial Shear Force.

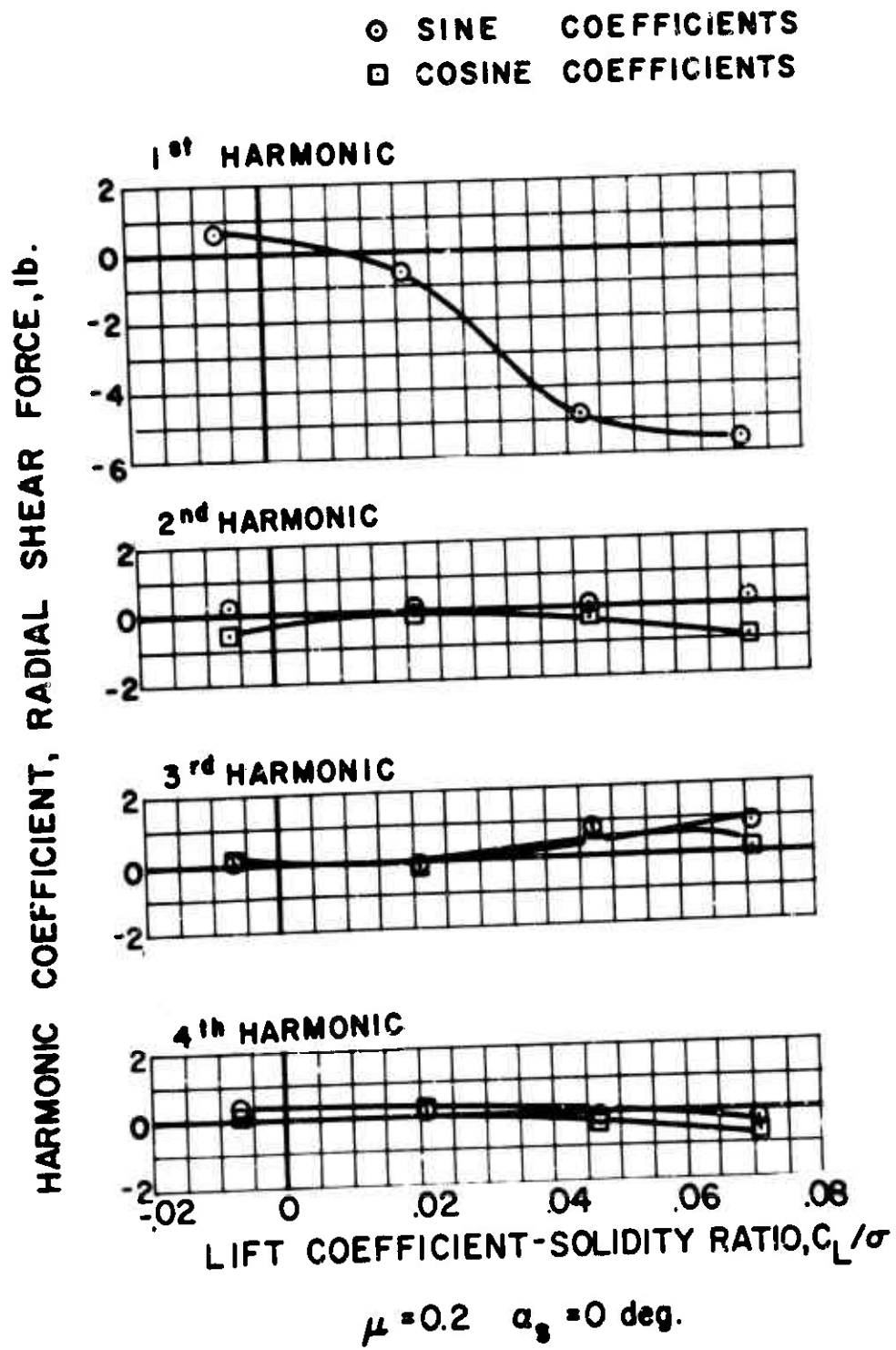
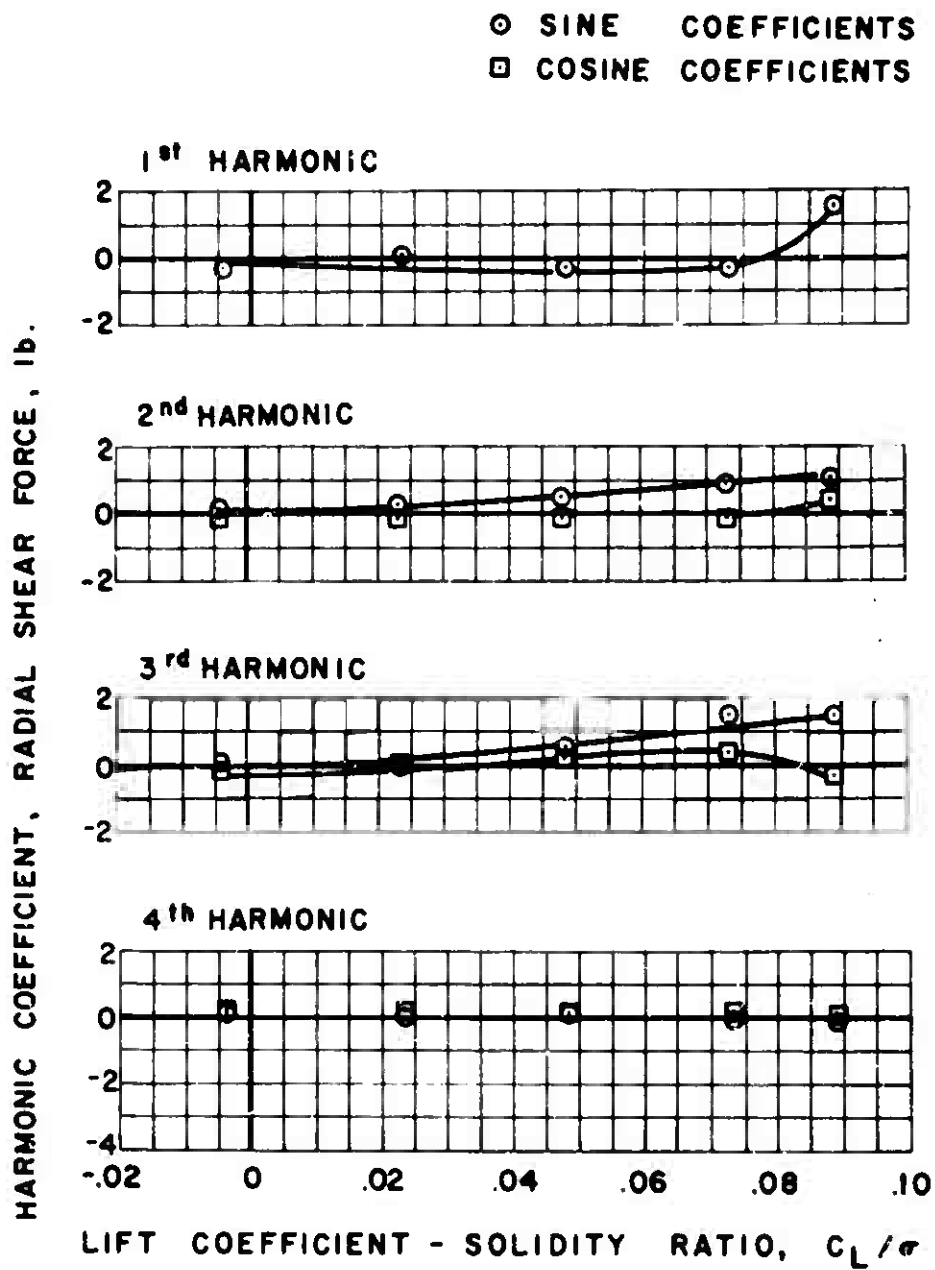
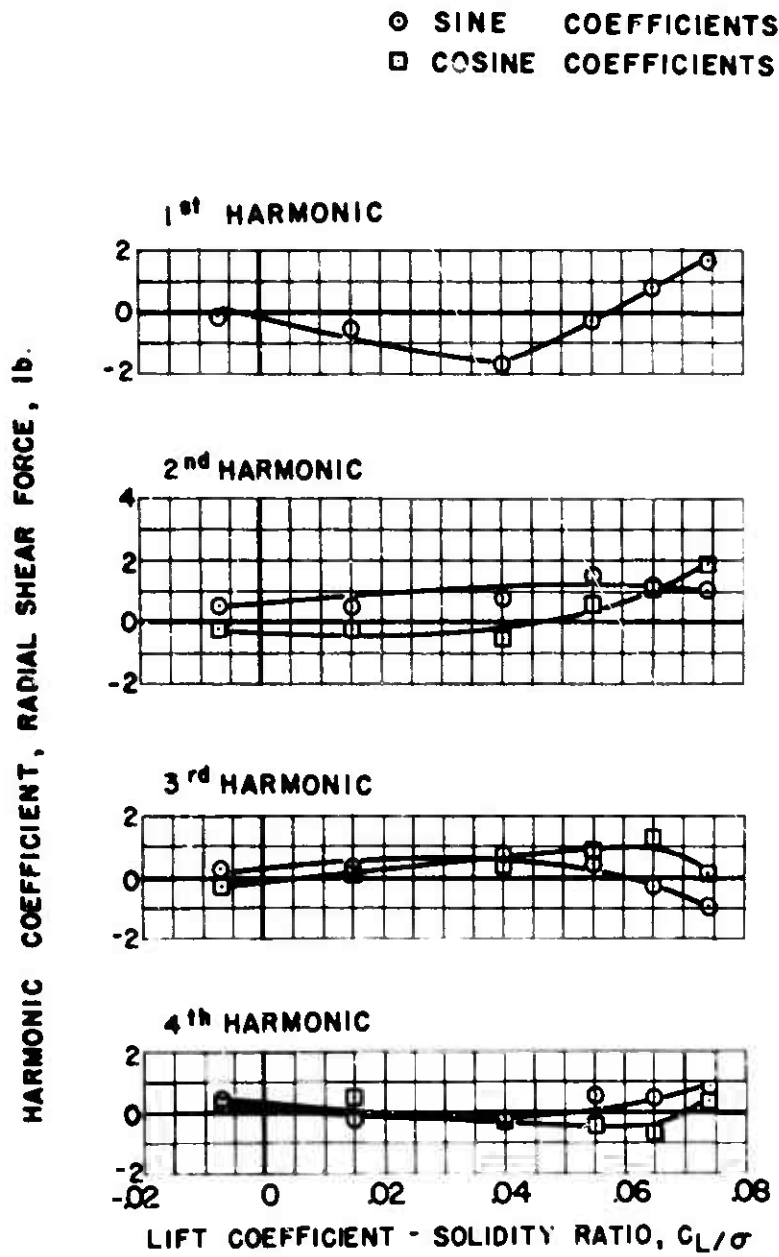


Figure 68. Experimental Radial Shear Force, Out of Trim, -4 Degree Longitudinal Flapping.



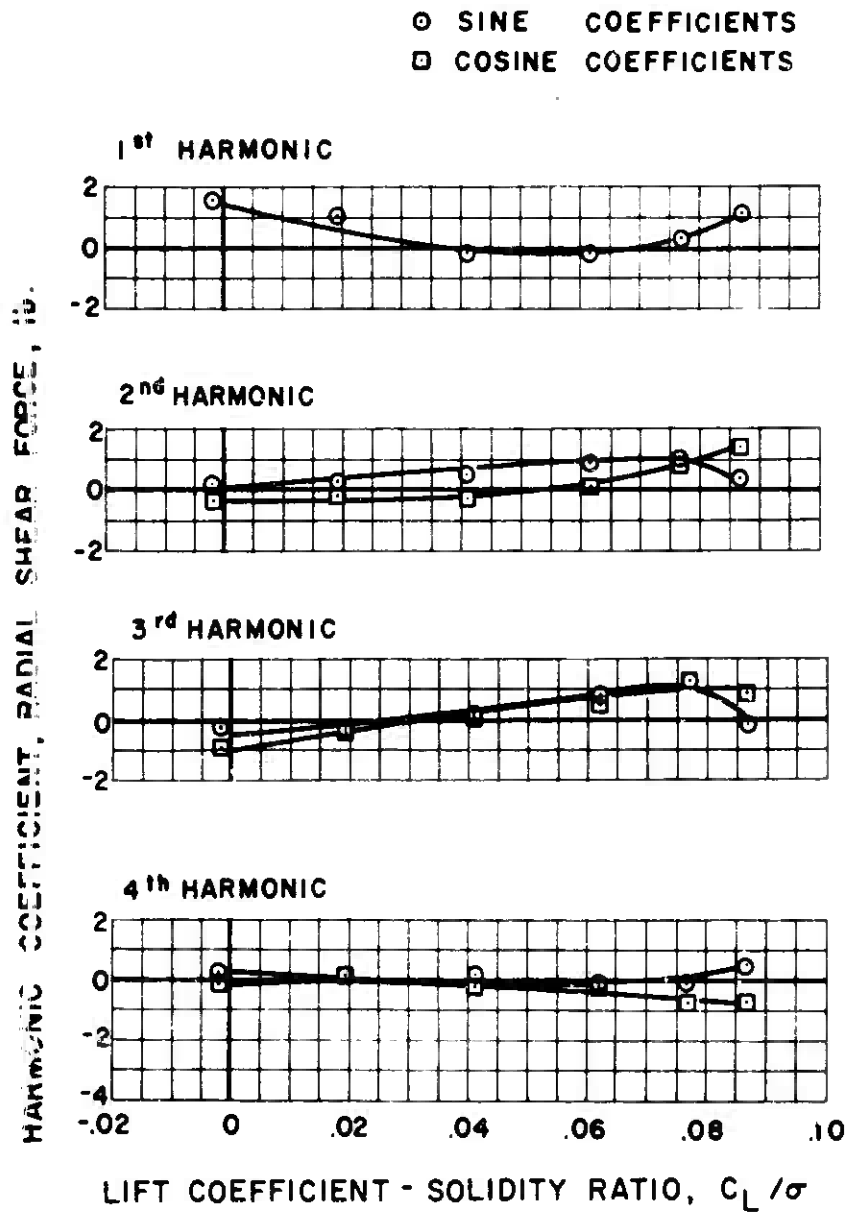
$$\mu = 0.2 \quad \alpha_s = -4 \text{ deg.}$$

Figure 69. Experimental Radial Shear Force, Zero Lag Damping.



$\mu = 0.3 \quad \alpha_s = 0 \text{ deg.}$

Figure 70. Experimental Radial Shear Force.



$$\mu = 0.3 \quad \alpha_s = -4 \text{ deg.}$$

Figure 71. Experimental Radial Shear Force.

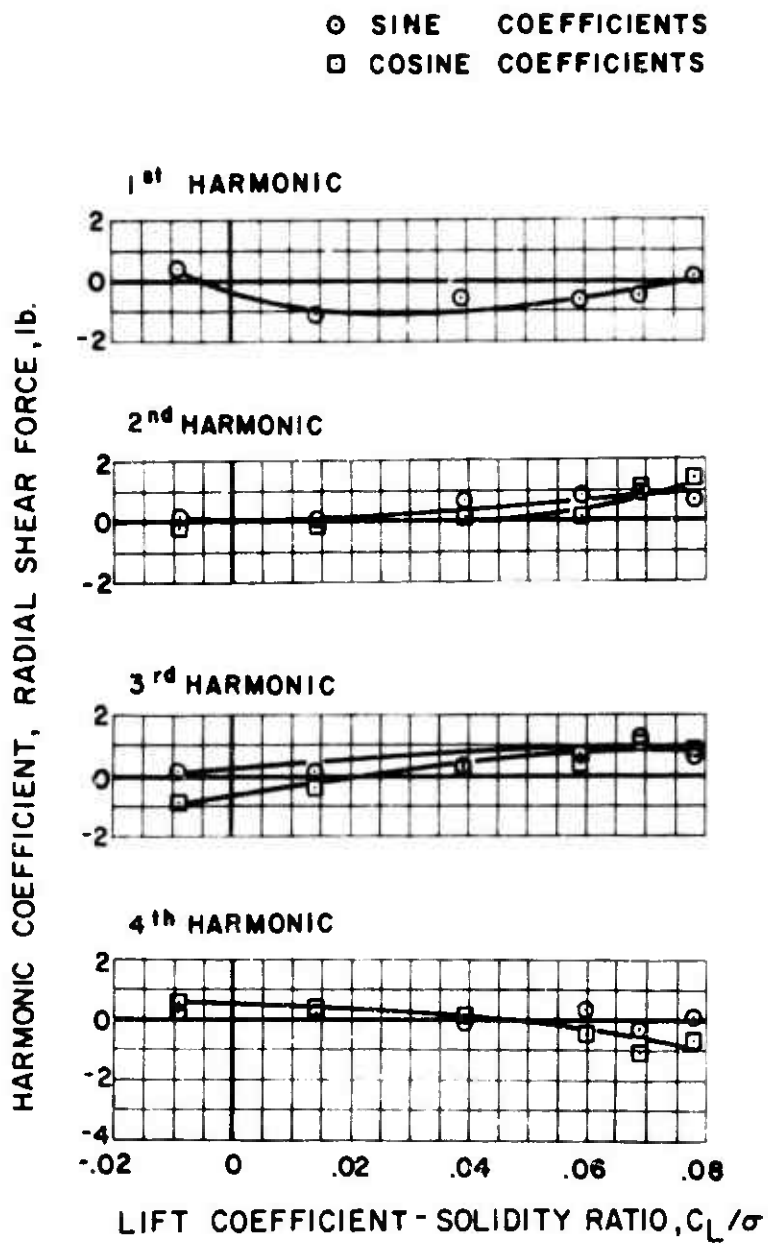
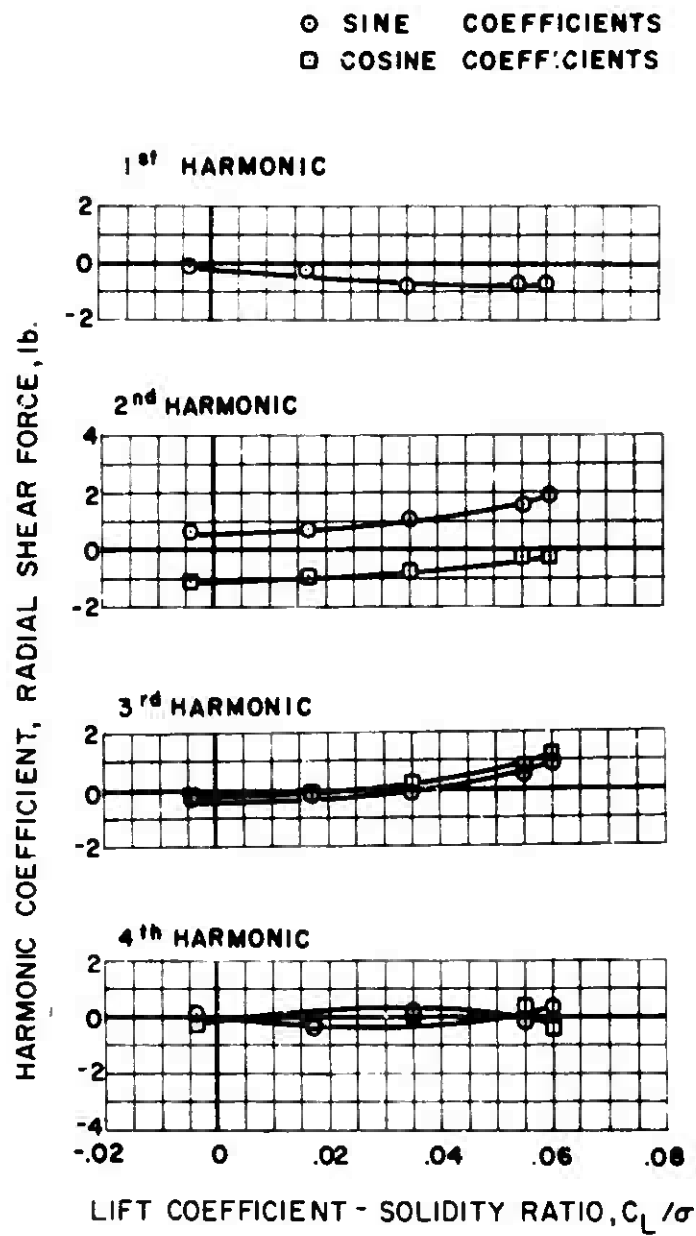


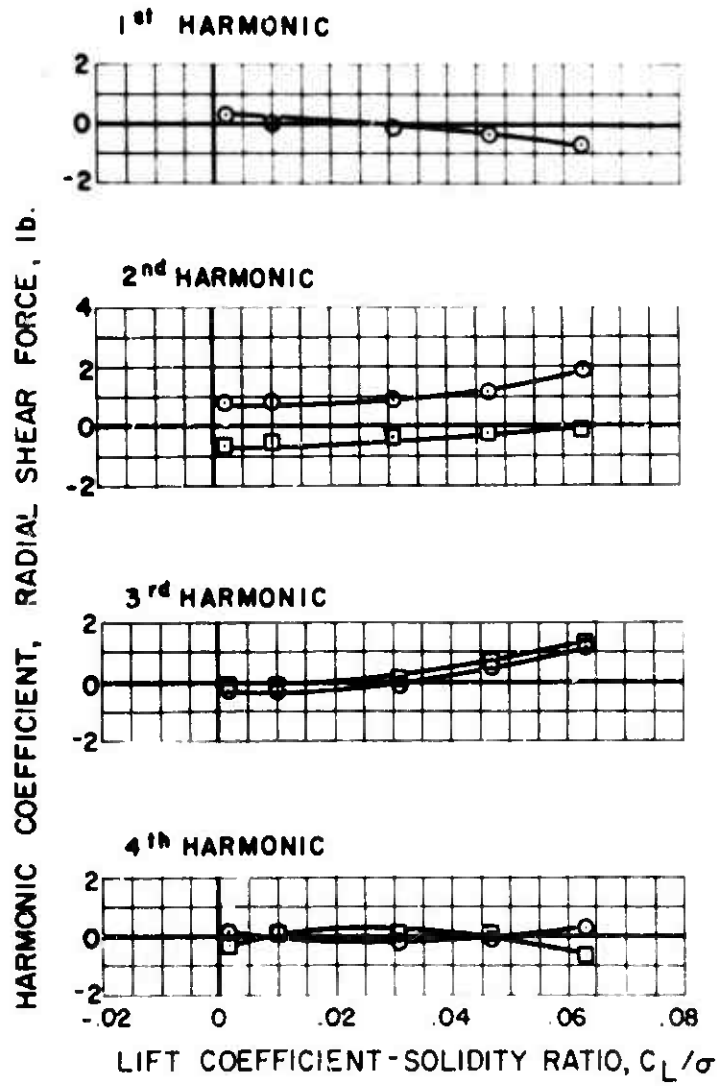
Figure 72. Experimental Radial Shear Force.



$\mu = 0.4 \quad \alpha_s = 4 \text{ deg.}$

Figure 73. Experimental Radial Shear Force.

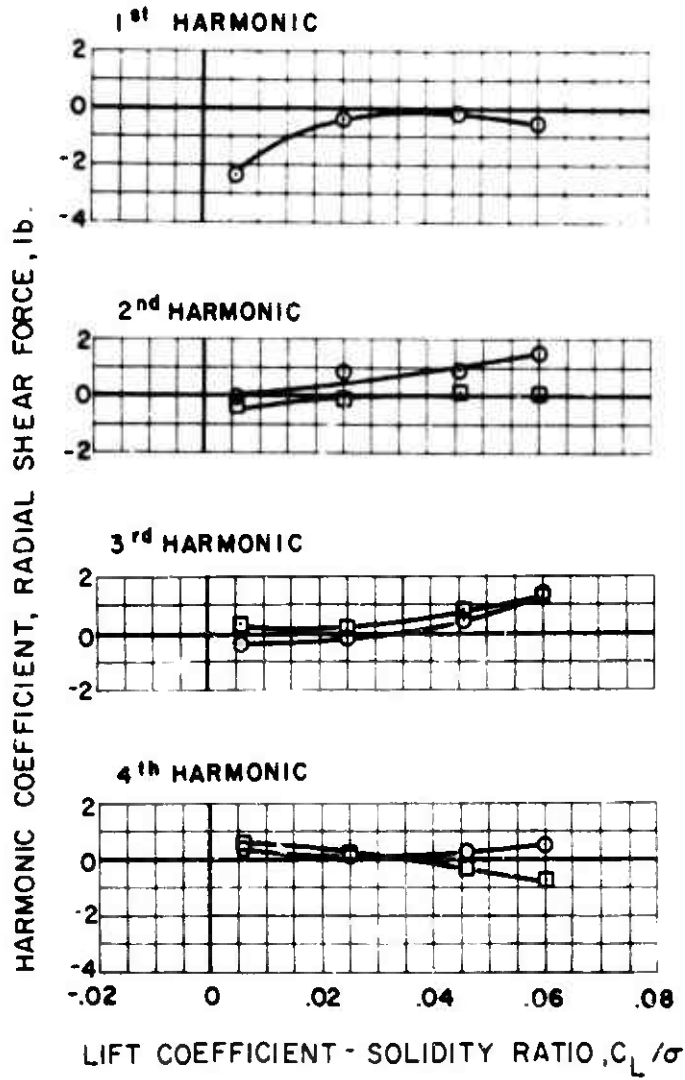
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.4$ $\alpha_s = 0$ deg.

Figure 74. Experimental Radial Shear Force.

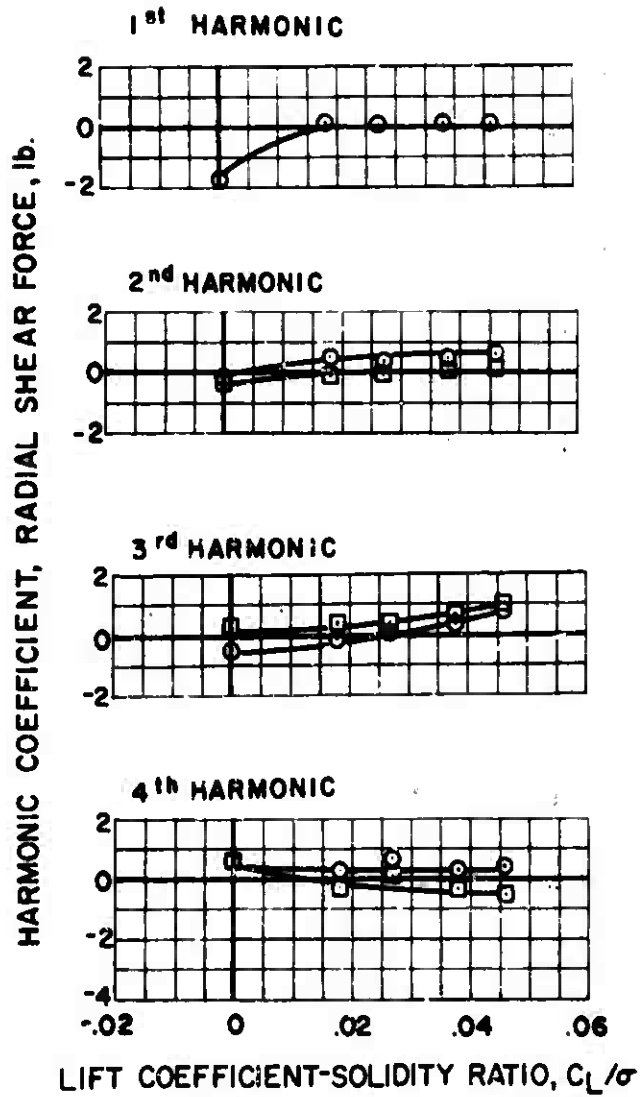
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.4$ $\alpha_s = -4\text{deg.}$

Figure 75. Experimental Radial Shear Force.

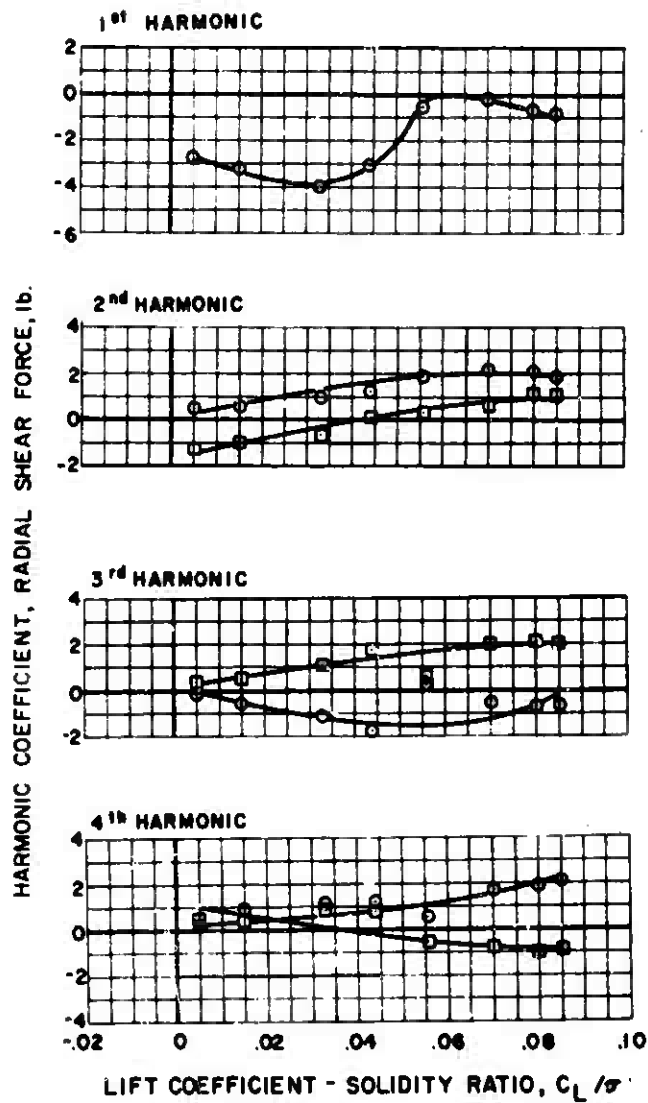
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.4$ $\alpha_s = -8$ deg.

Figure 76. Experimental Radial Shear Force.

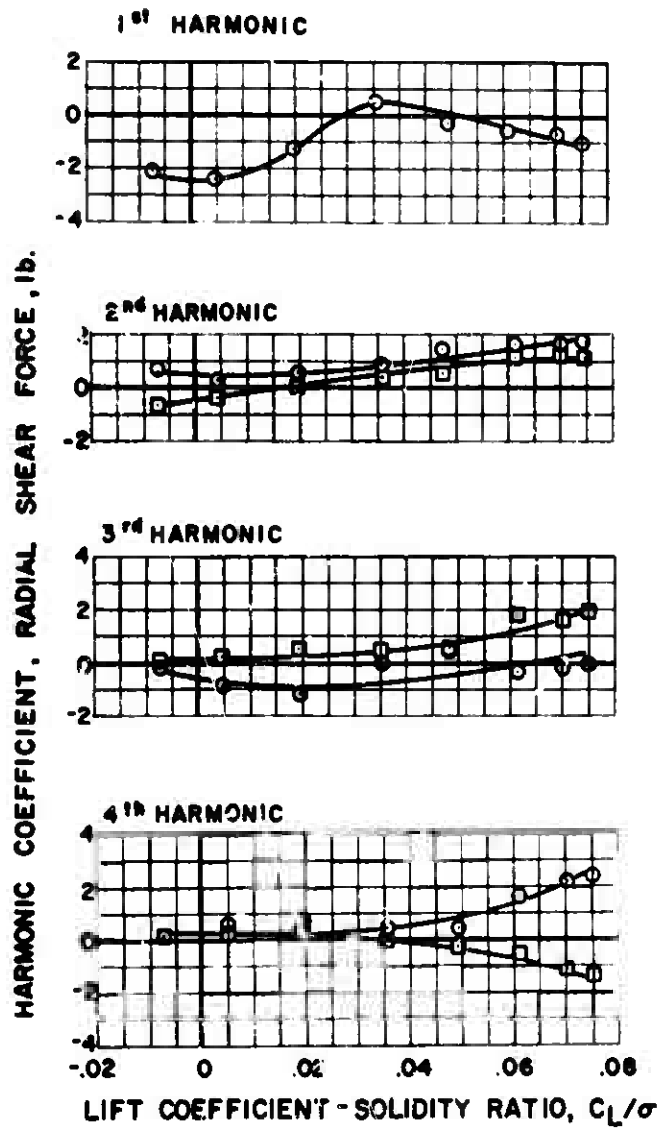
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = 0$ deg.

Figure 77. Experimental Radial Shear Force.

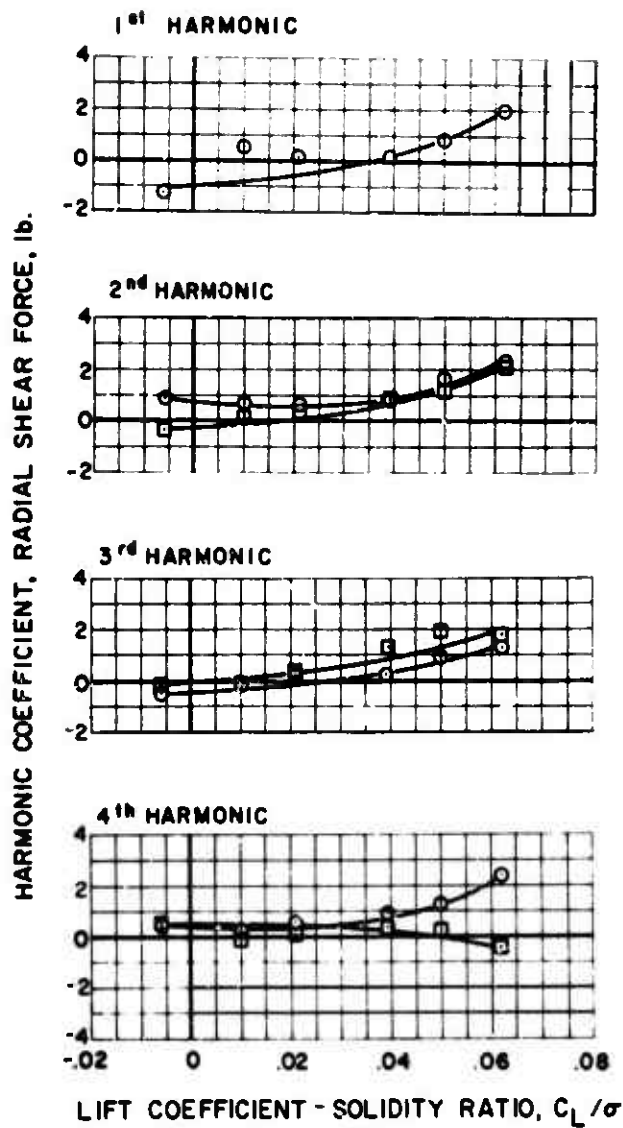
○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -4$ deg.

Figure 78. Experimental Radial Shear Force.

○ SINE COEFFICIENTS
 ○ COSINE COEFFICIENTS



$\mu = 0.5$ $\alpha_s = -8 \text{ deg.}$

Figure 79. Experimental Radial Shear Force.

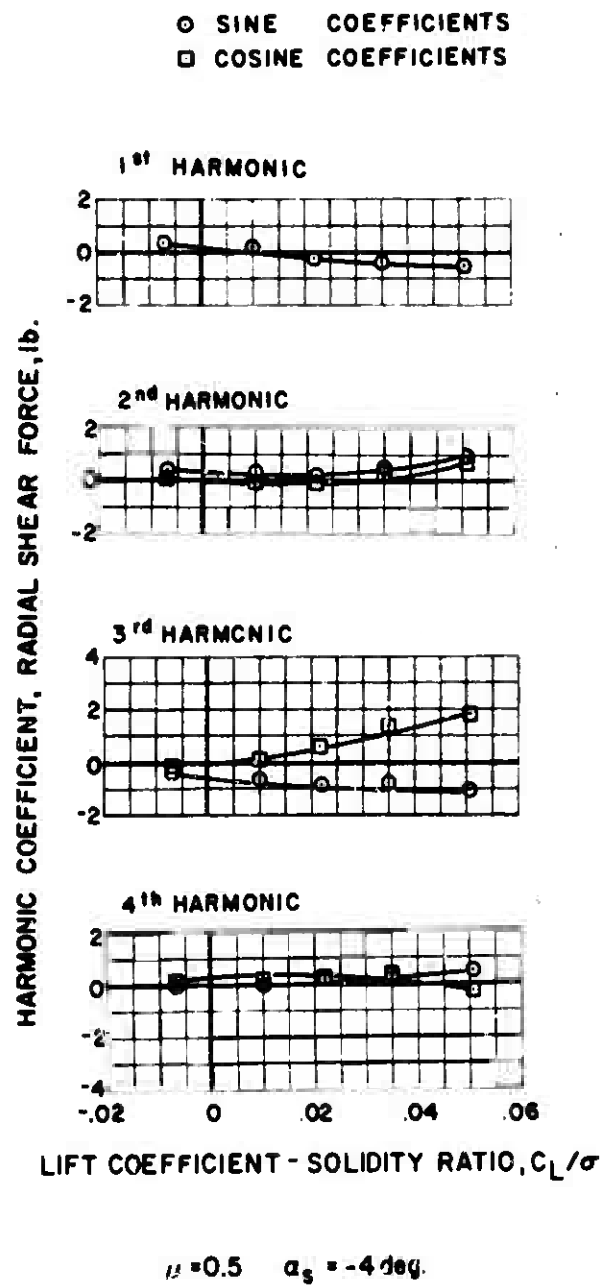
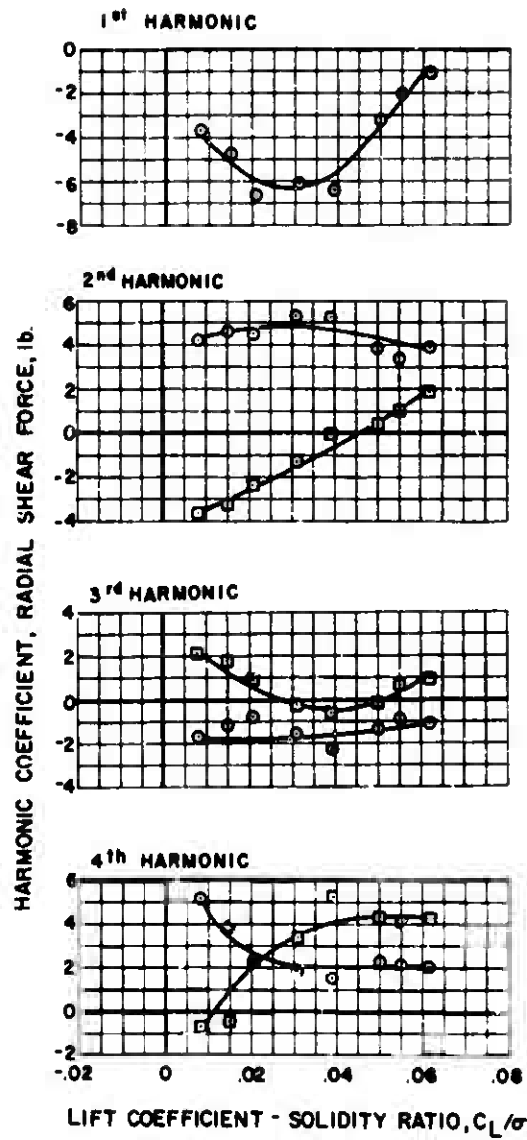


Figure 80. Experimental Radial Shear Force, Zero Lag Damping.

○ SINE COEFFICIENTS
 □ COSINE COEFFICIENTS



$\mu = 0.7$ $\alpha_0 = 4$ deg.

Figure 81. Experimental Radial Shear Force.

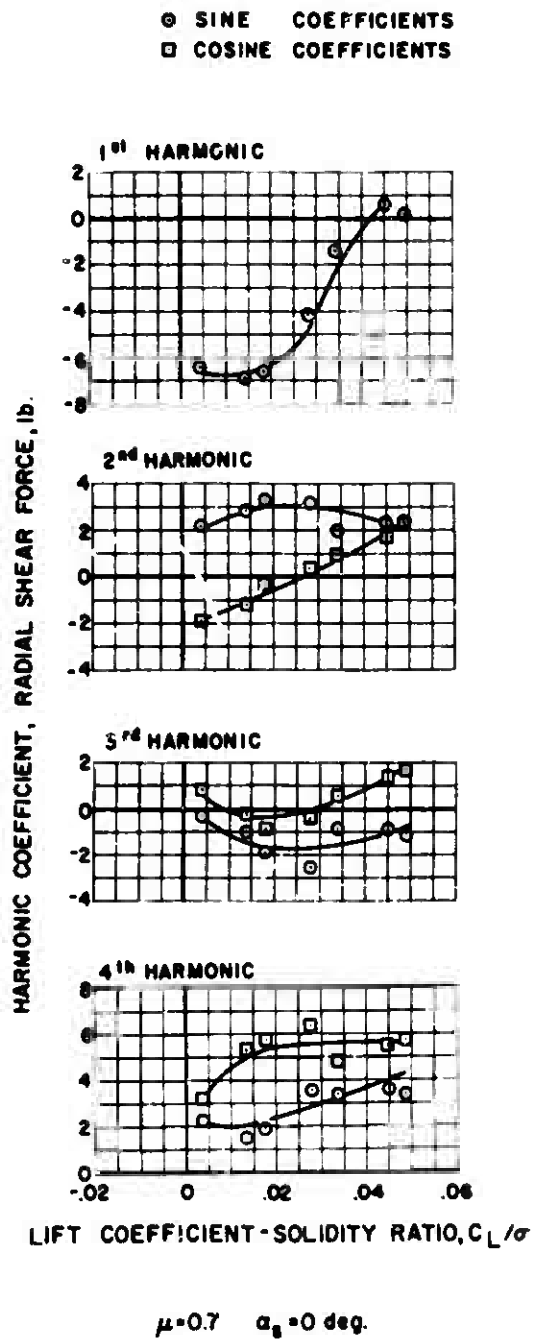
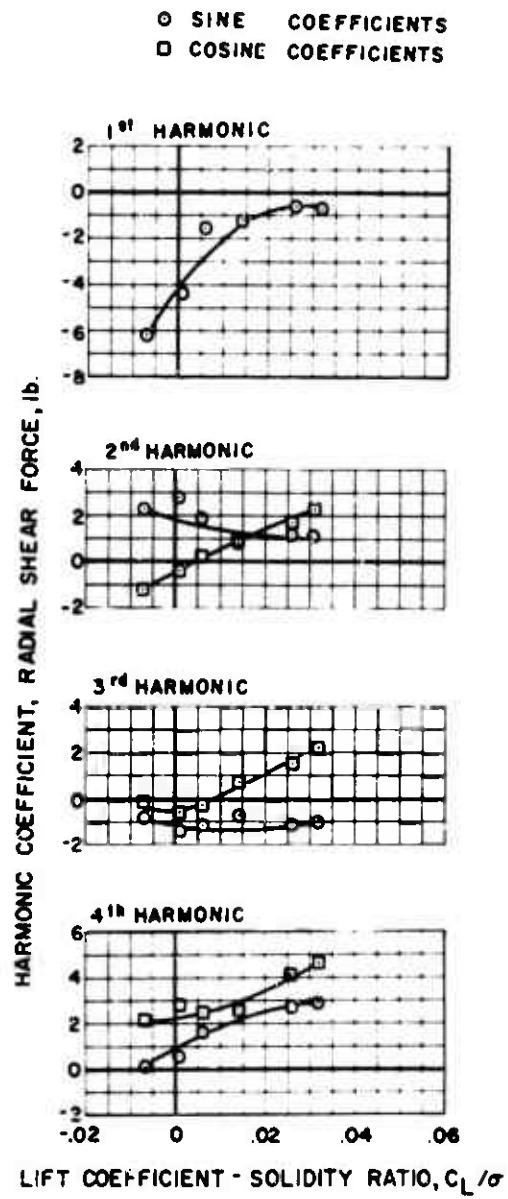
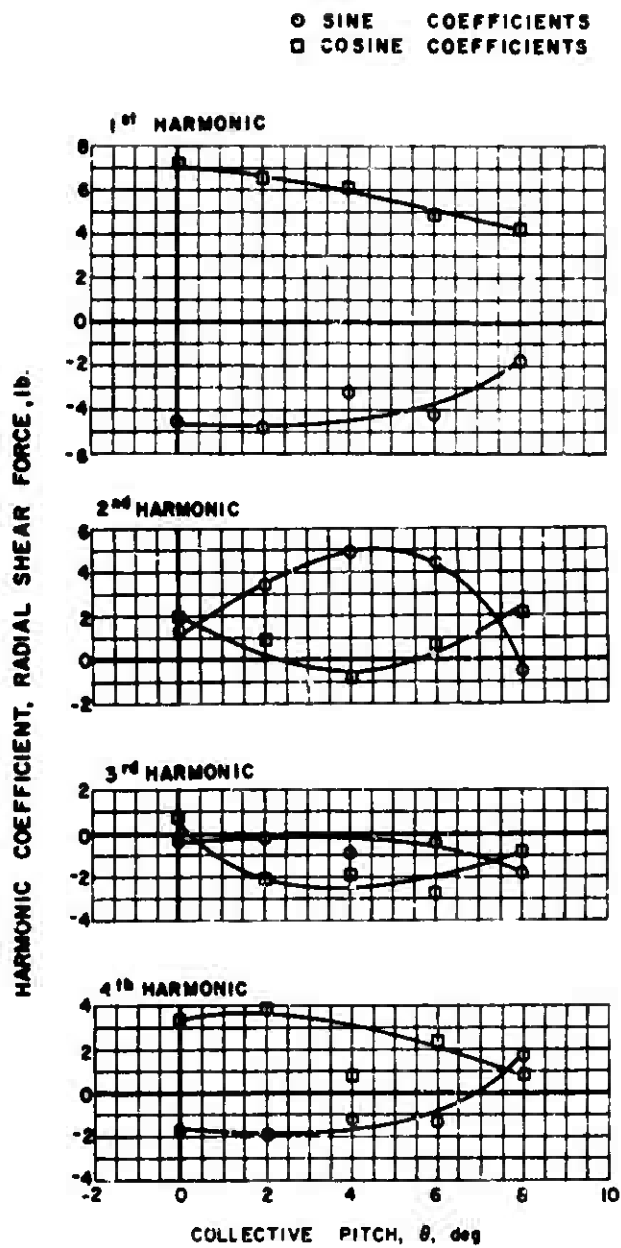


Figure 82. Experimental Radial Shear Force.



$\mu = 0.7 \quad \alpha_s = -4 \text{ deg.}$

Figure 83. Experimental Radial Shear Force.

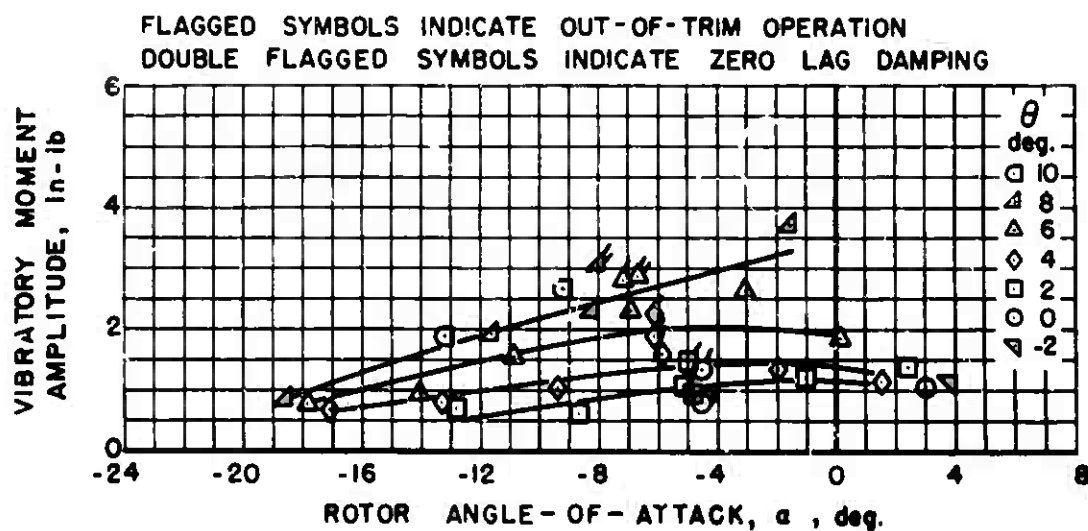


$\mu = 1.0 \quad \alpha_s = 0 \text{ deg.}$

Figure 84. Experimental Radial Shear Force.

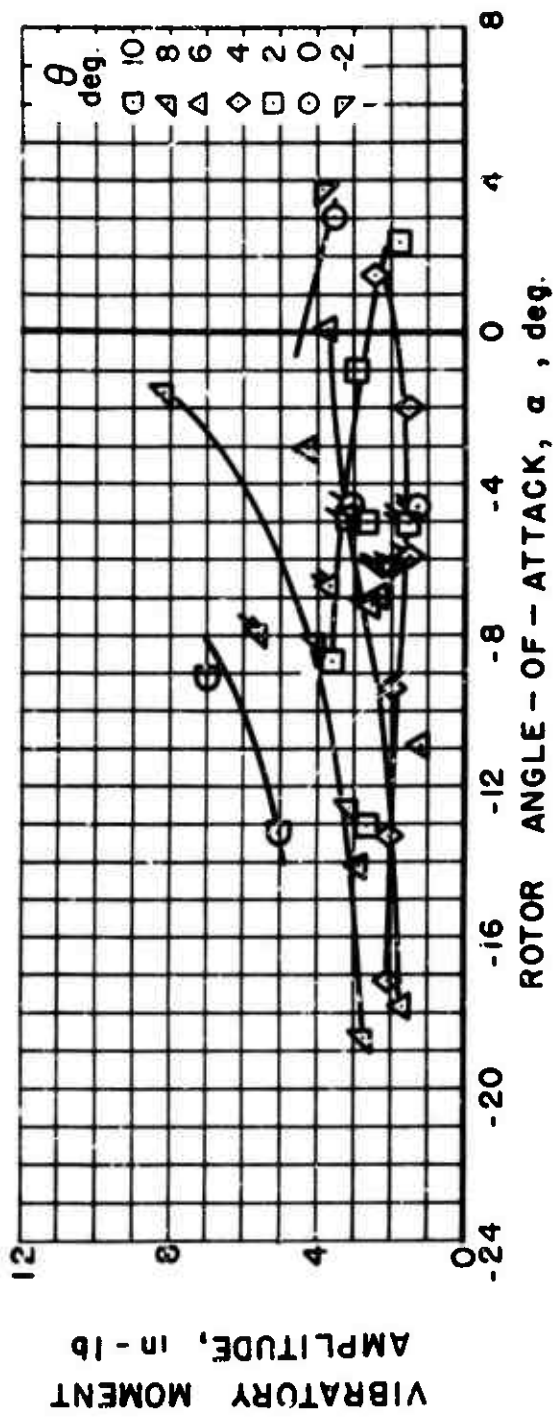
APPENDIX III

EXPERIMENTAL VIBRATORY MOMENT AMPLITUDE FIGURES



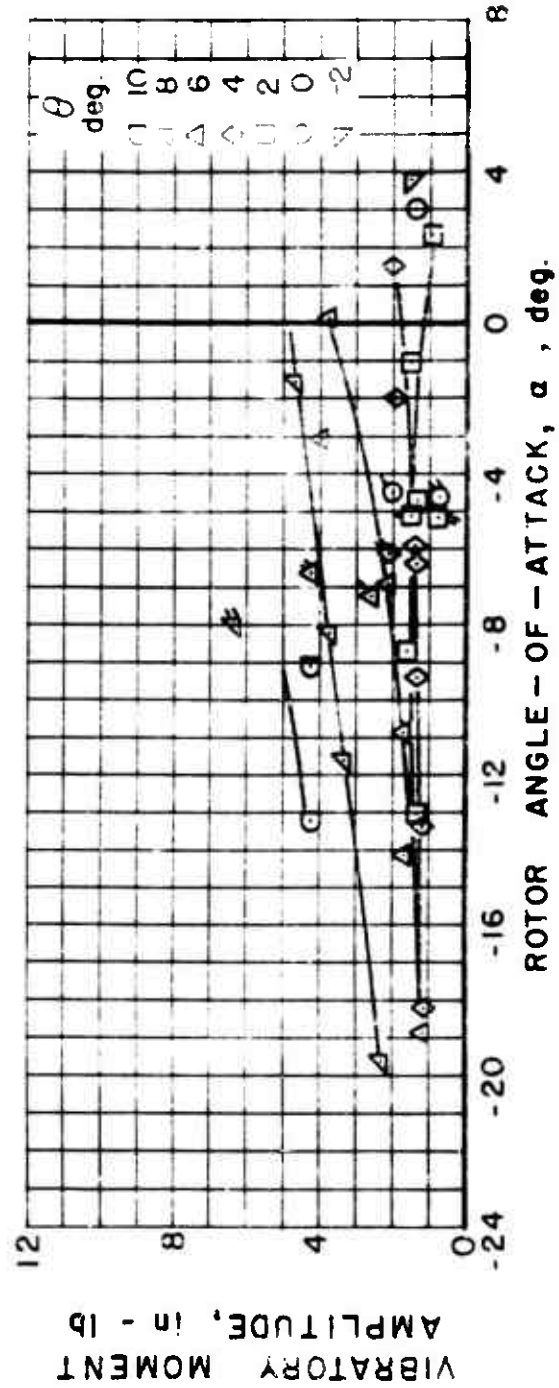
(a) FLATWISE BENDING MOMENT, 21 %R

Figure 85. Experimental Vibratory Moment Amplitude, $\mu = 0.2$.



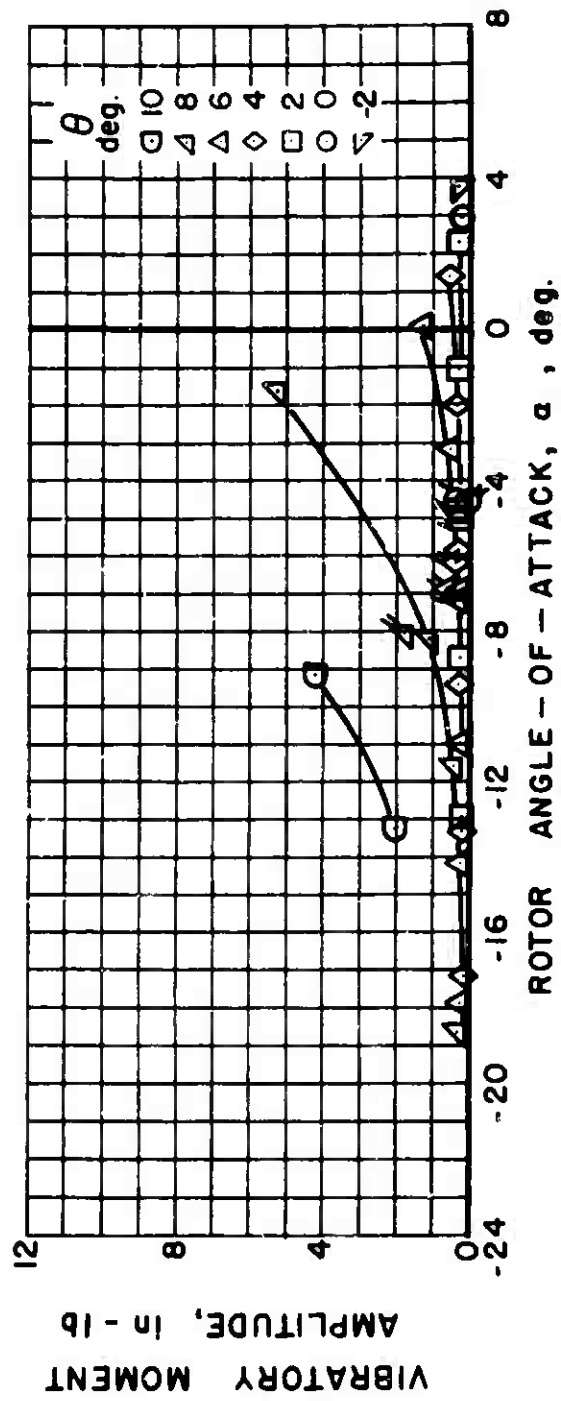
(b) EDGEWISE BENDING MOMENT, 21% R

Figure 85. Continued.



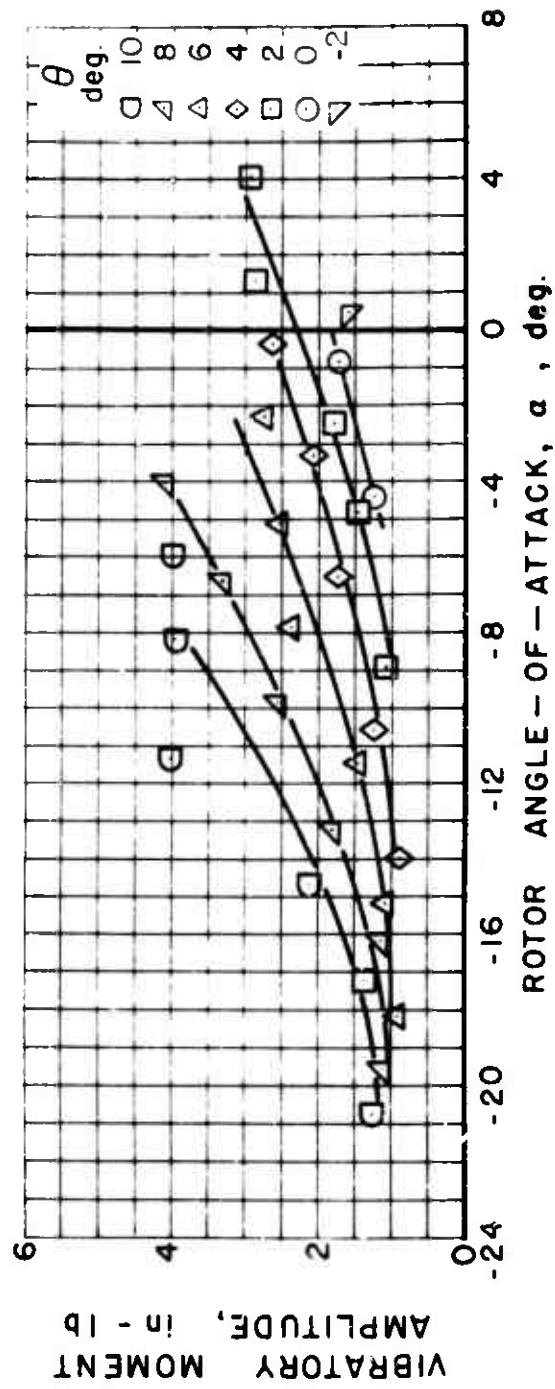
(c) EDGEWISE BENDING MOMENT, 47% R

Figure 85. Continued.



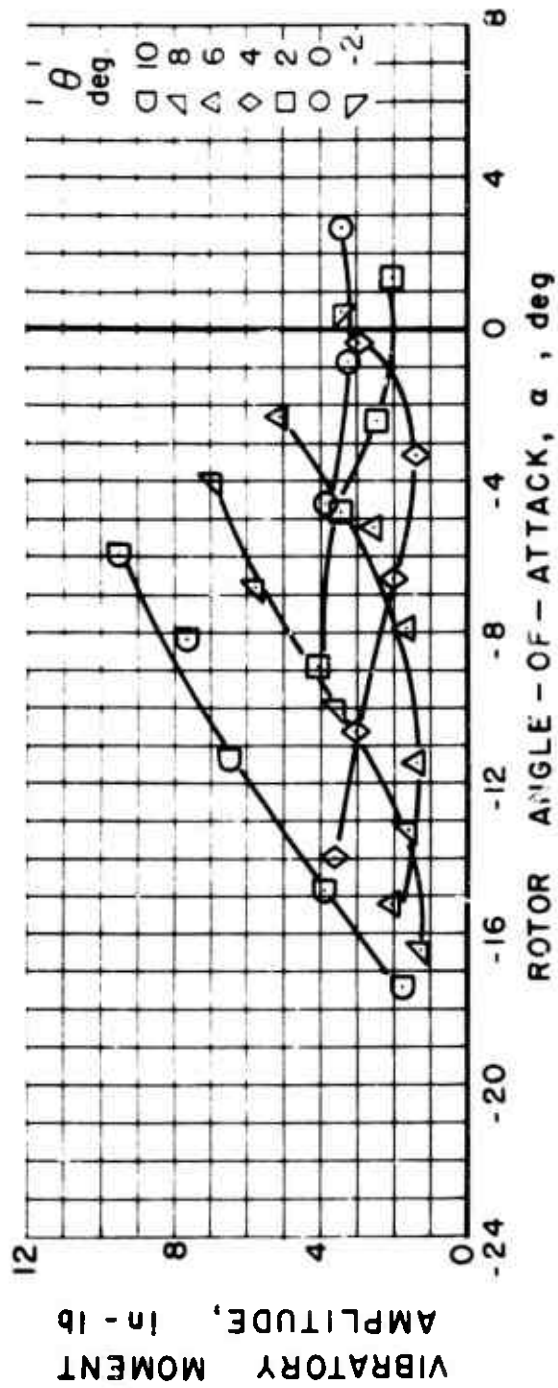
(d) TORSIONAL MOMENT, 17.5 % R

Figure 85. Concluded.



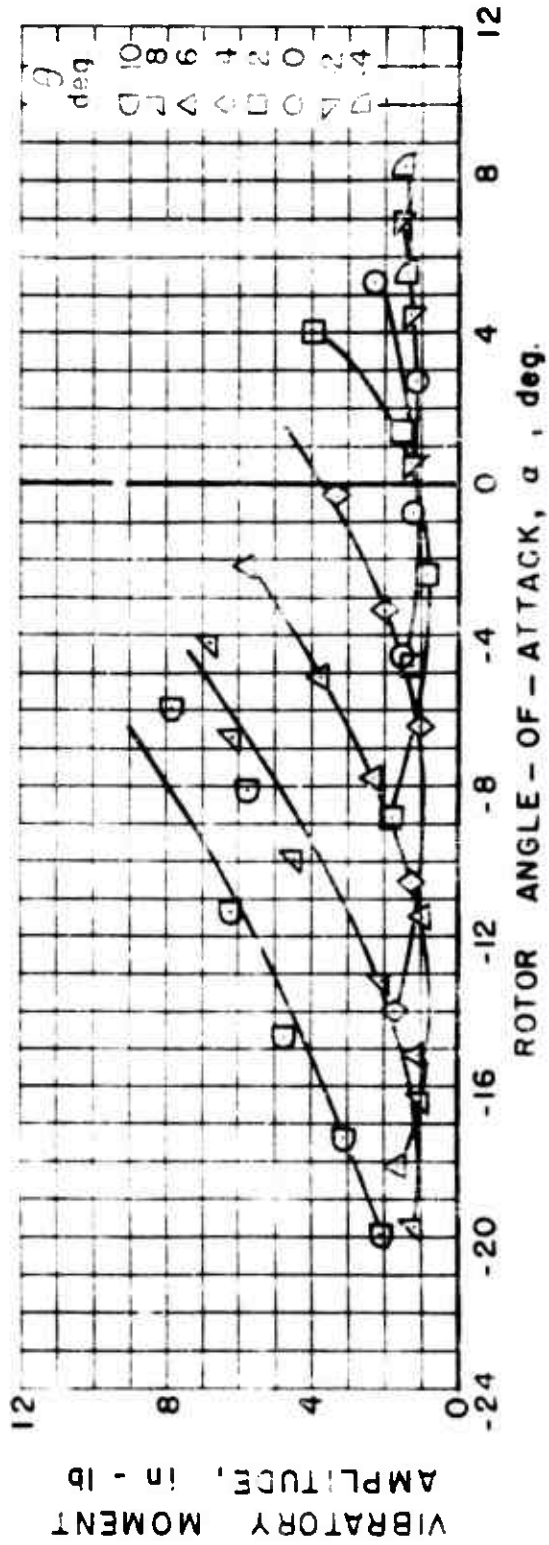
(a) FLATWISE BENDING MOMENT, 21% R

Figure 86. Experimental Vibratory Moment Amplitude, $\mu = 0.3$.



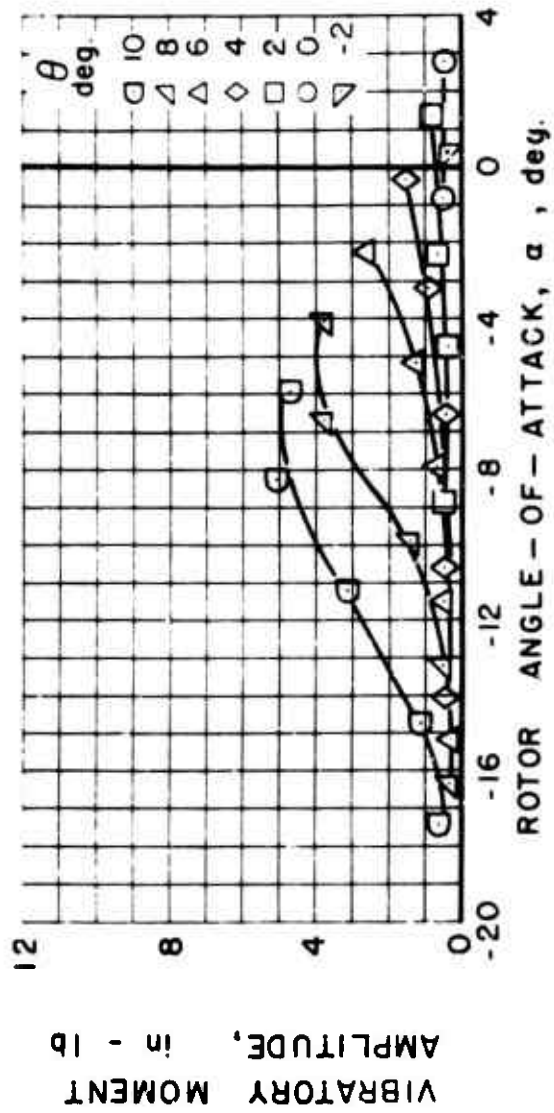
(b) EDGEWISE BENDING MOMENT, 21 % R

Figure 86. Continued.



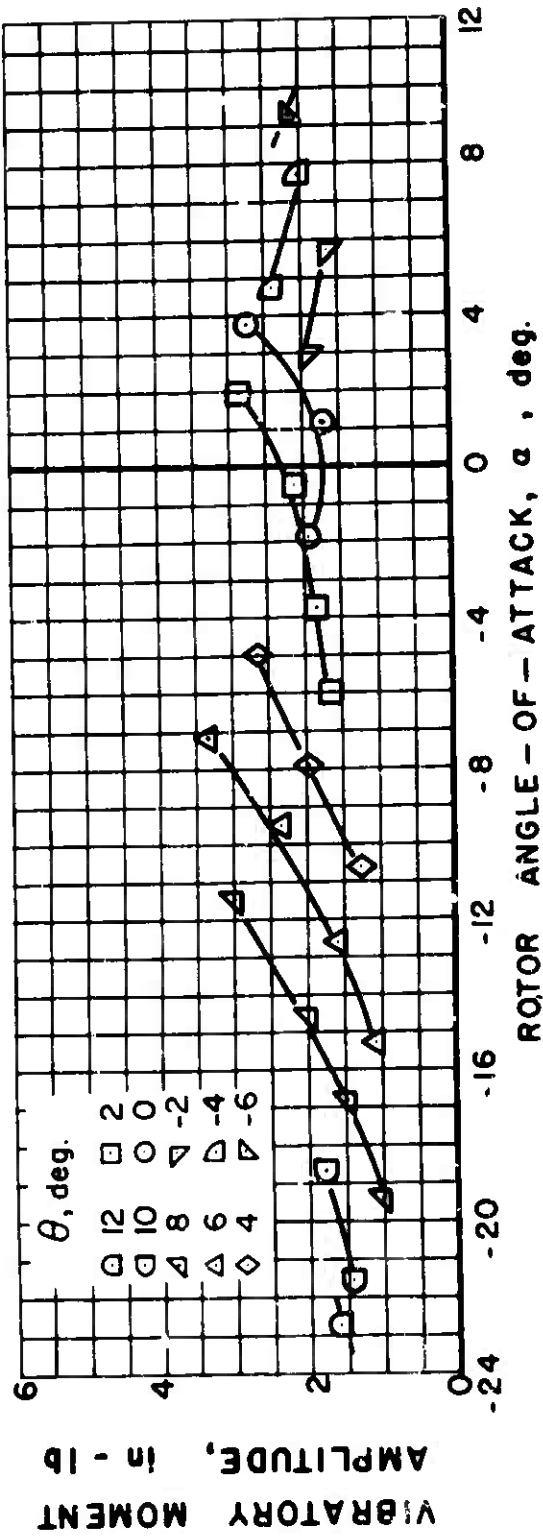
(c) EDGEWISE BENDING MOMENT, 47 % R

Figure 86. Continued.



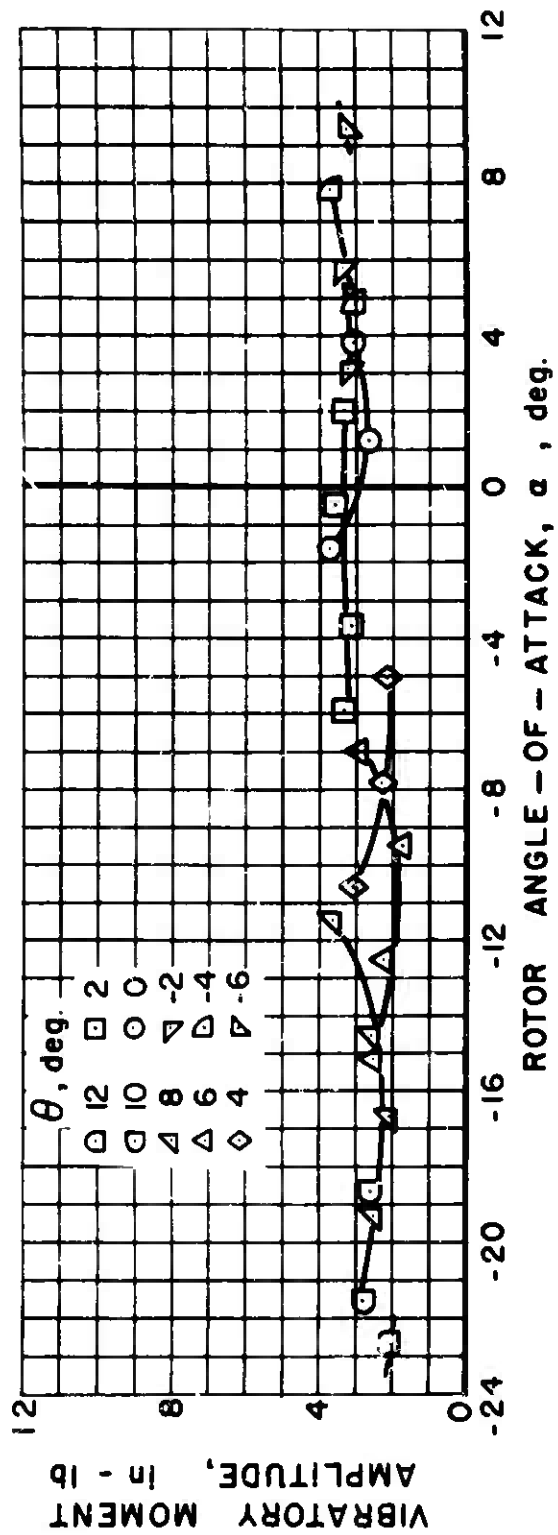
(d) TORSIONAL MOMENT, 17.5 % P.

Figure 86. Concluded.



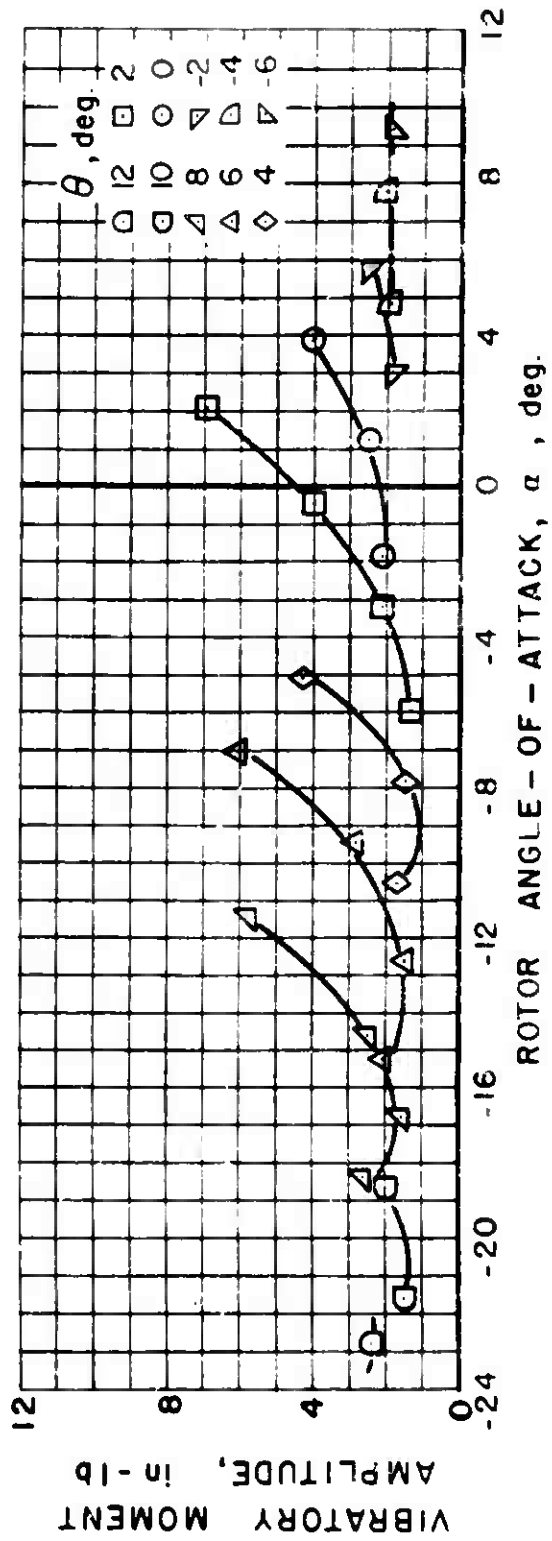
(a) FLATWISE BENDING MOMENT, 21% R

Figure 87. Experimental Vibratory Moment Amplitude, $\mu = 0.4$.



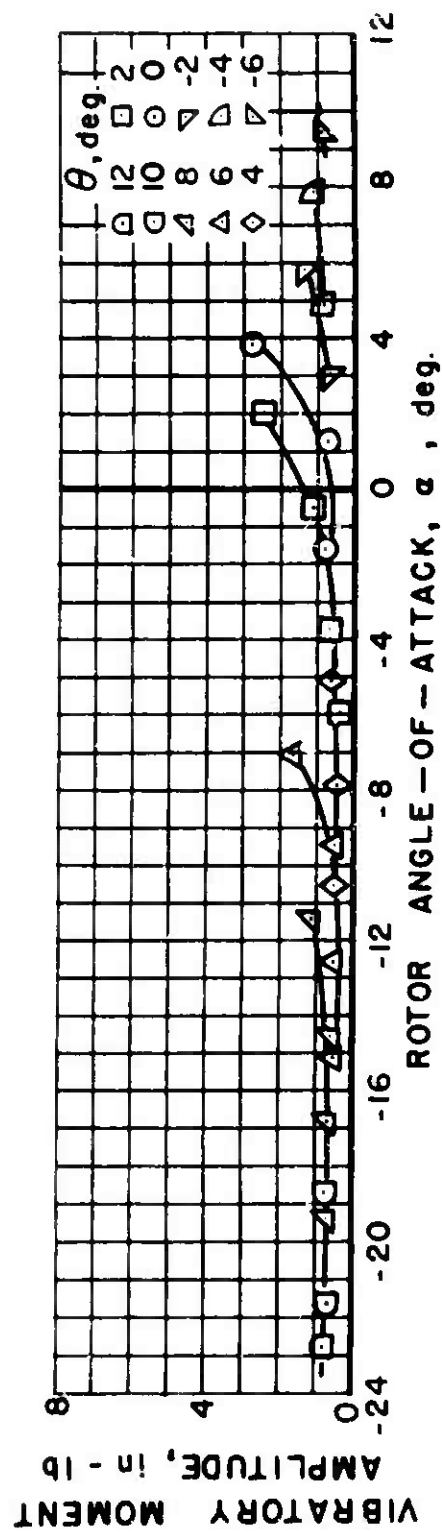
(b) EDGEWISE BENDING MOMENT, 21 %

Figure 87. Continued.



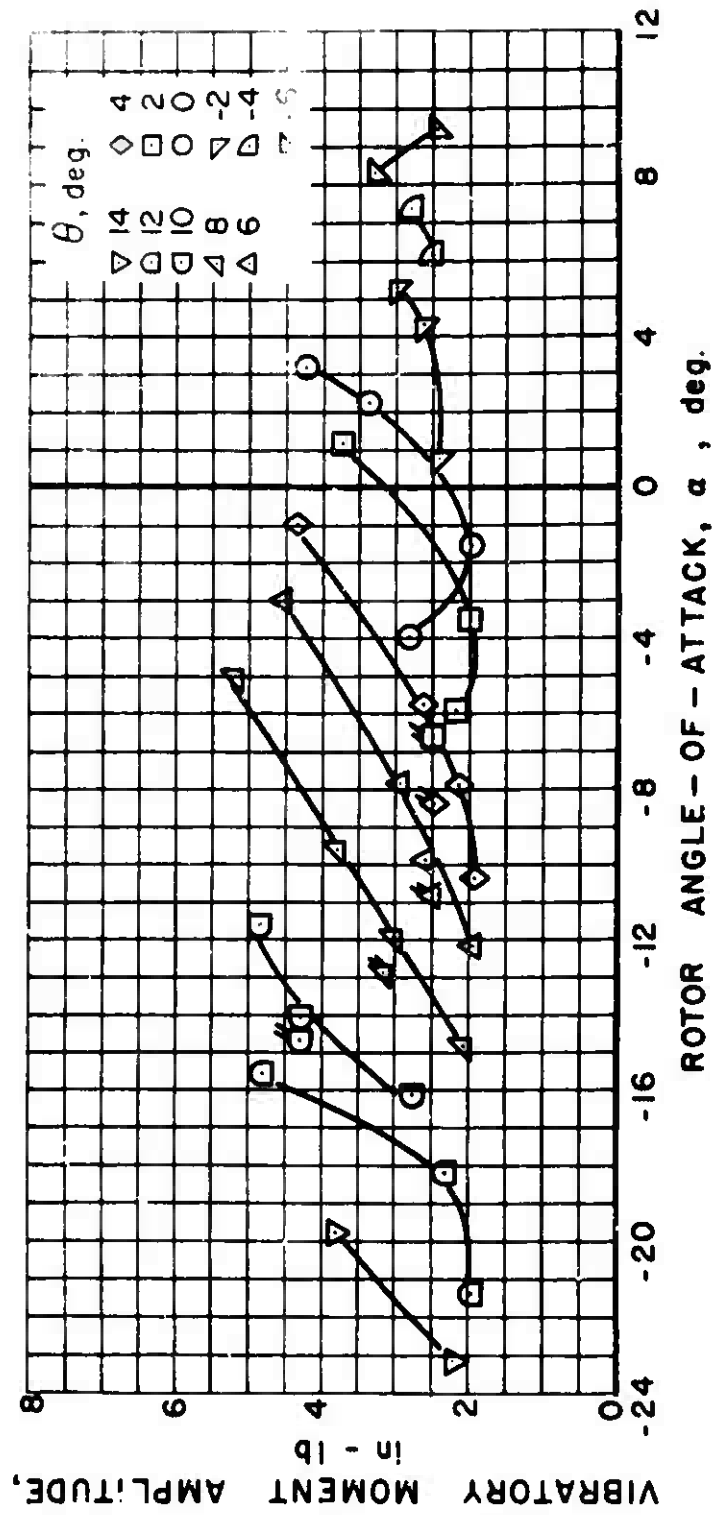
(c) EDGEWISE BENDING MOMENT, 47 % R

Figure 87. Continued.



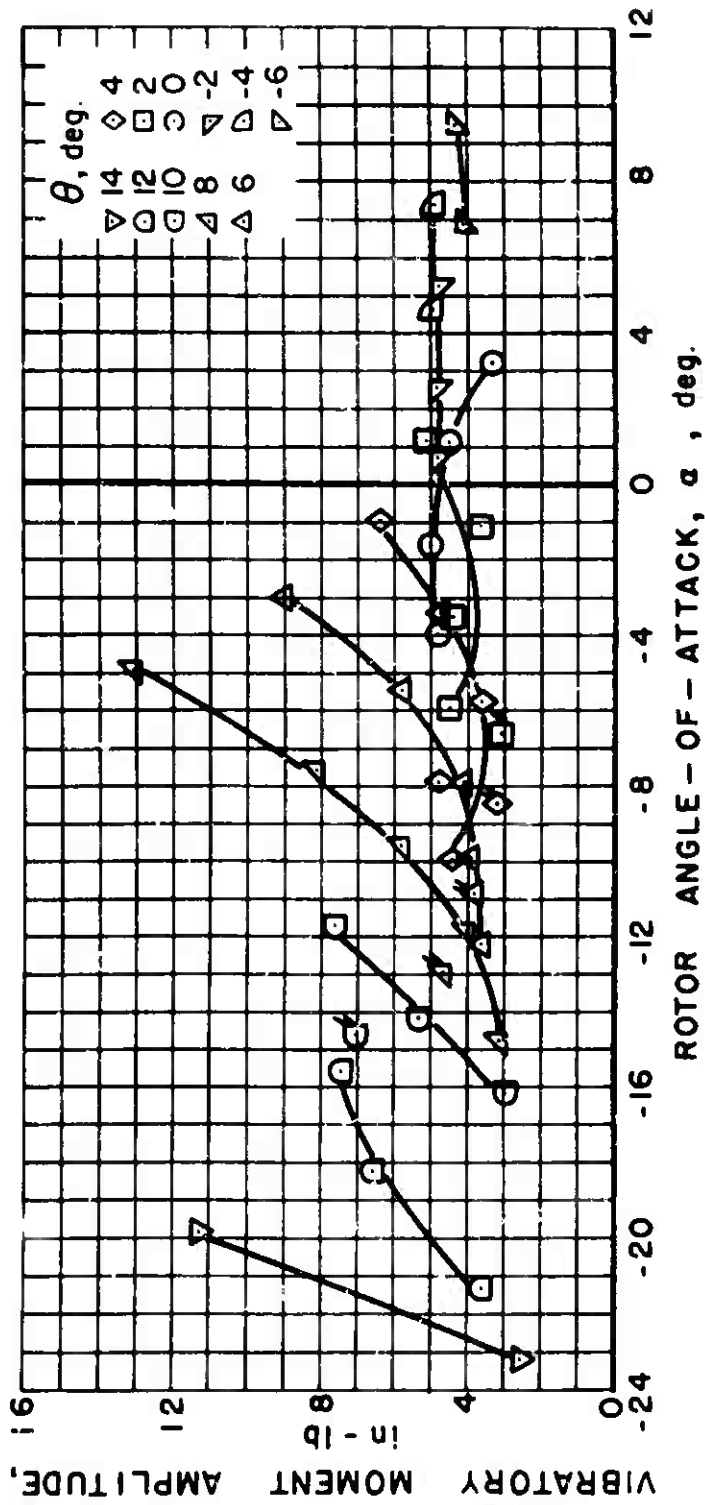
(d) TORSIONAL MOMENT, 17.5 % R

Figure 87. Concluded.



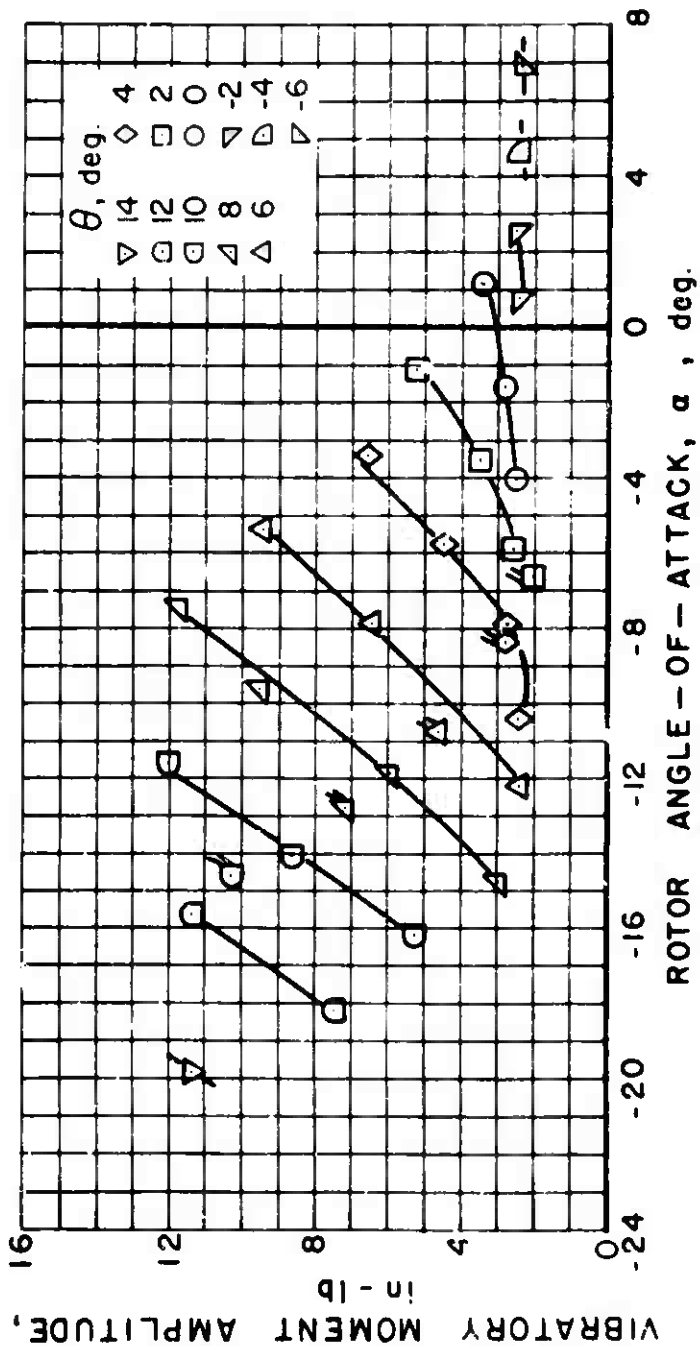
(a) FLATWISE BENDING MOMENT, 21% R

Figure 88. Experimental Vibratory Moment Amplitude, $\mu = 0.5$.



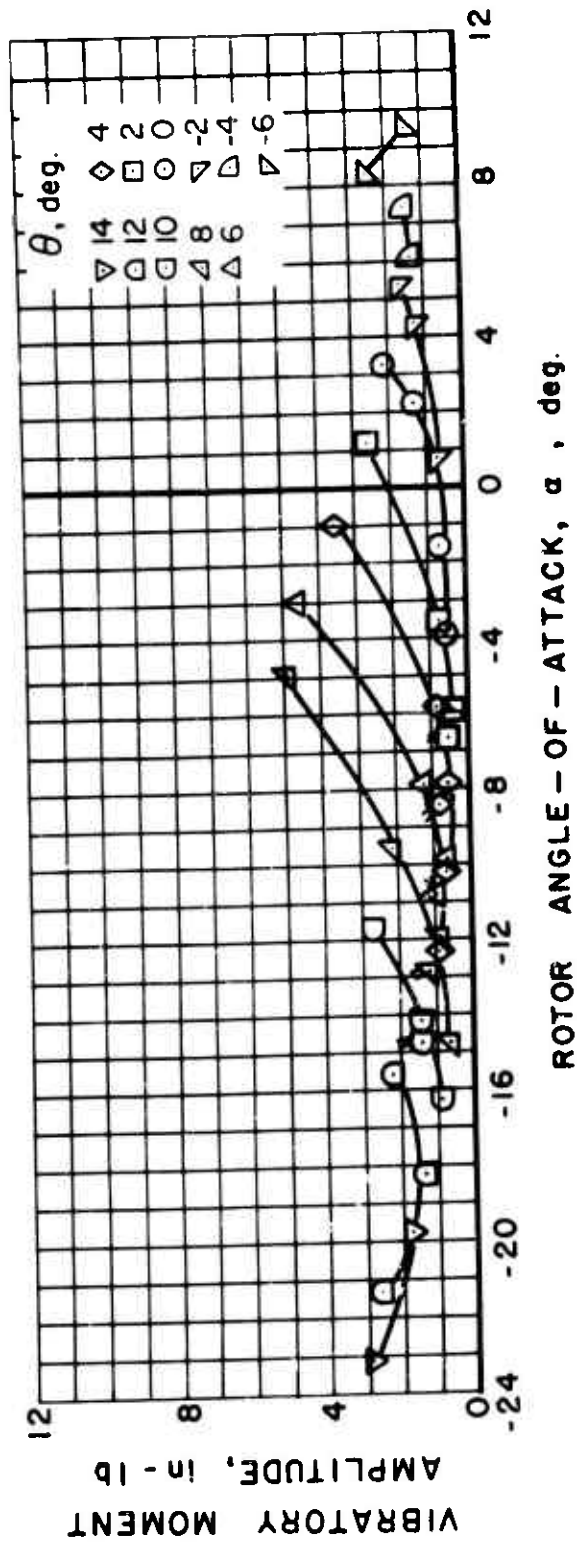
(b) EDGEWISE BENDING MOMENT, 21 % R

Figure 88. Continued.



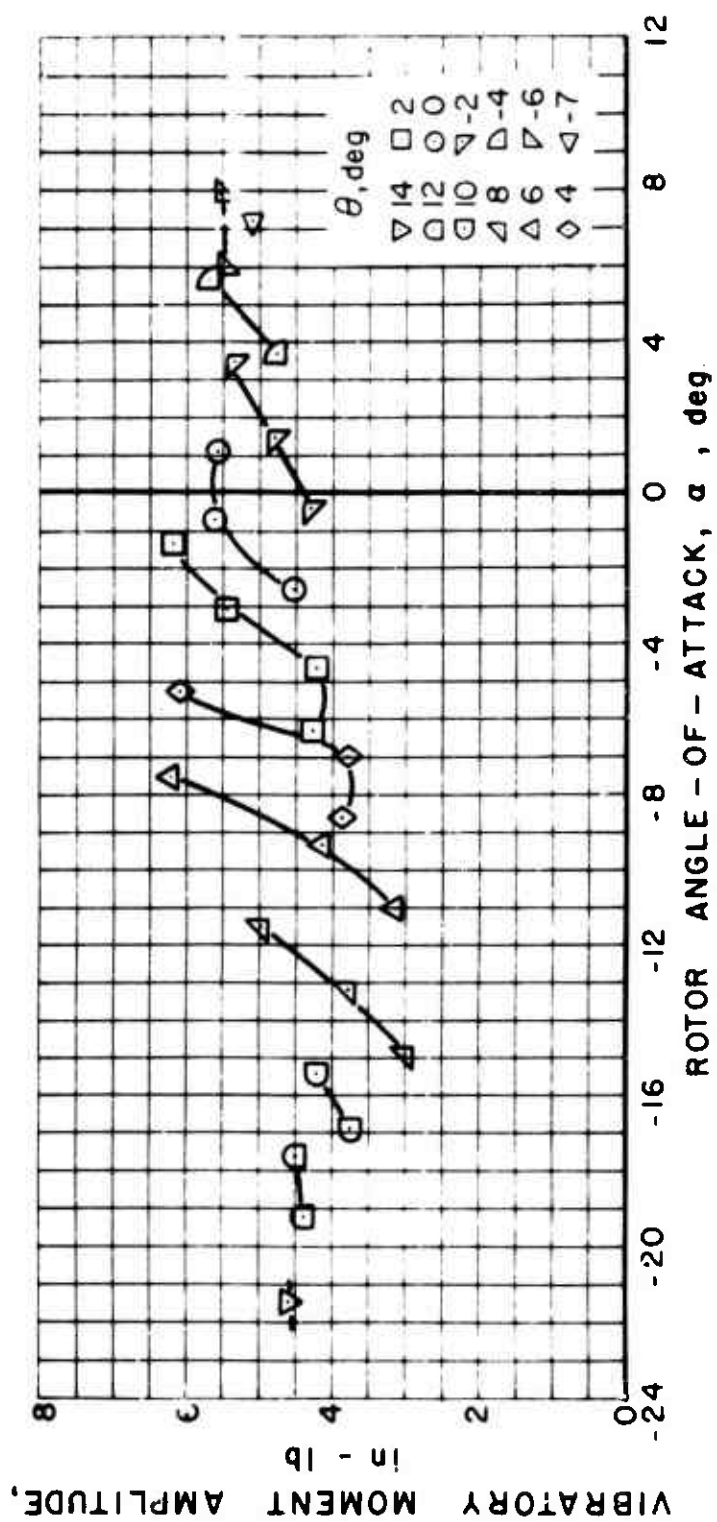
(c) EDGEWISE BENDING MOMENT, 47% R

Figure 88. Continued.



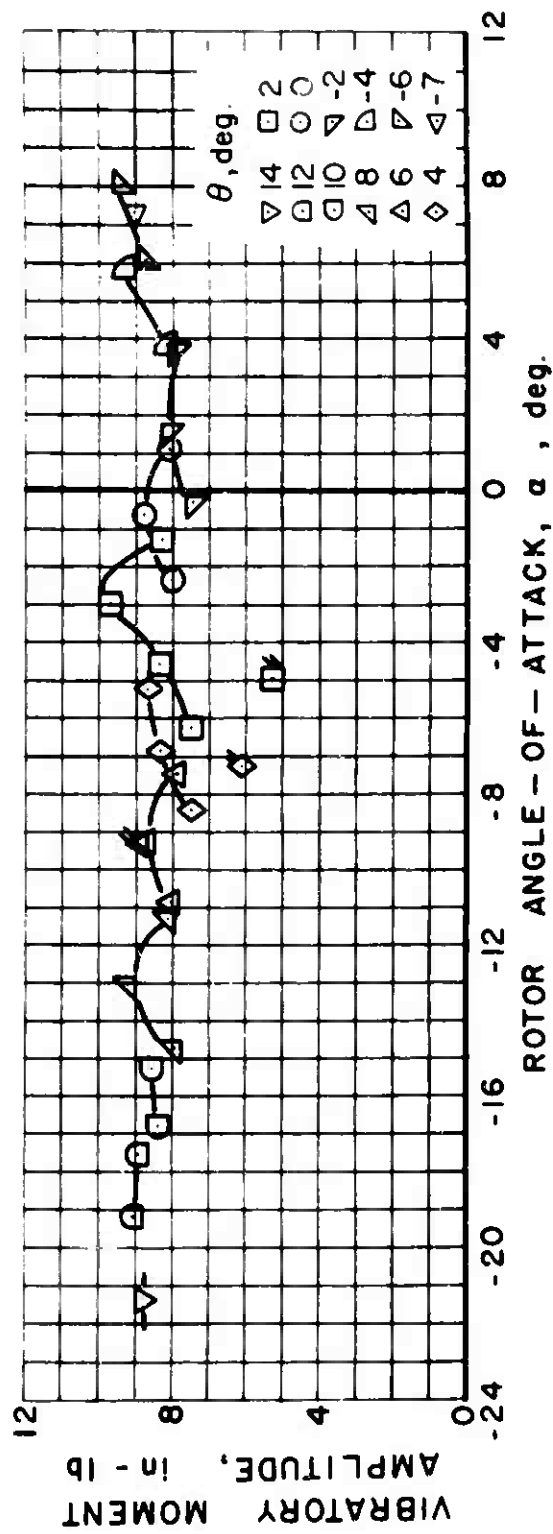
(d) TORSIONAL MOMENT, 17.5 % R

Figure 88. Concluded.



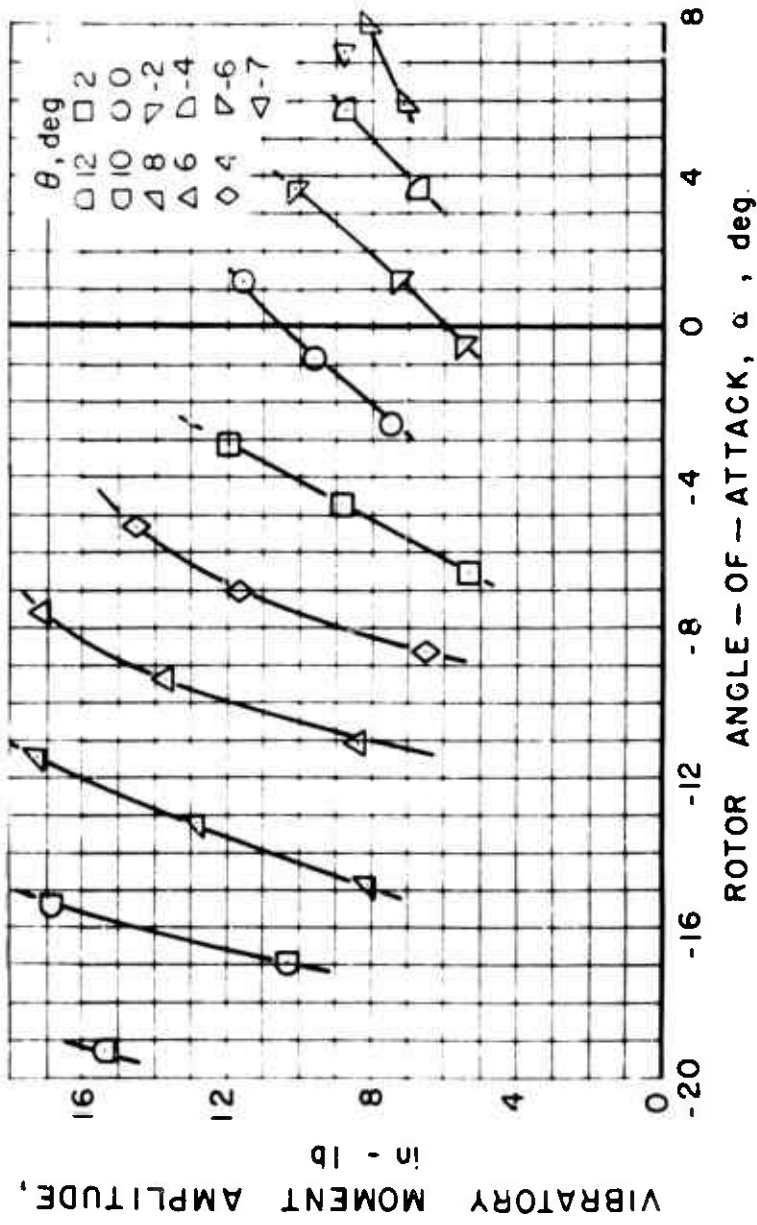
(a) FLATWISE BENDING MOMENT, 21% R

Figure 89. Experimental Vibratory Moment Amplitude, $\mu = 0.7$.



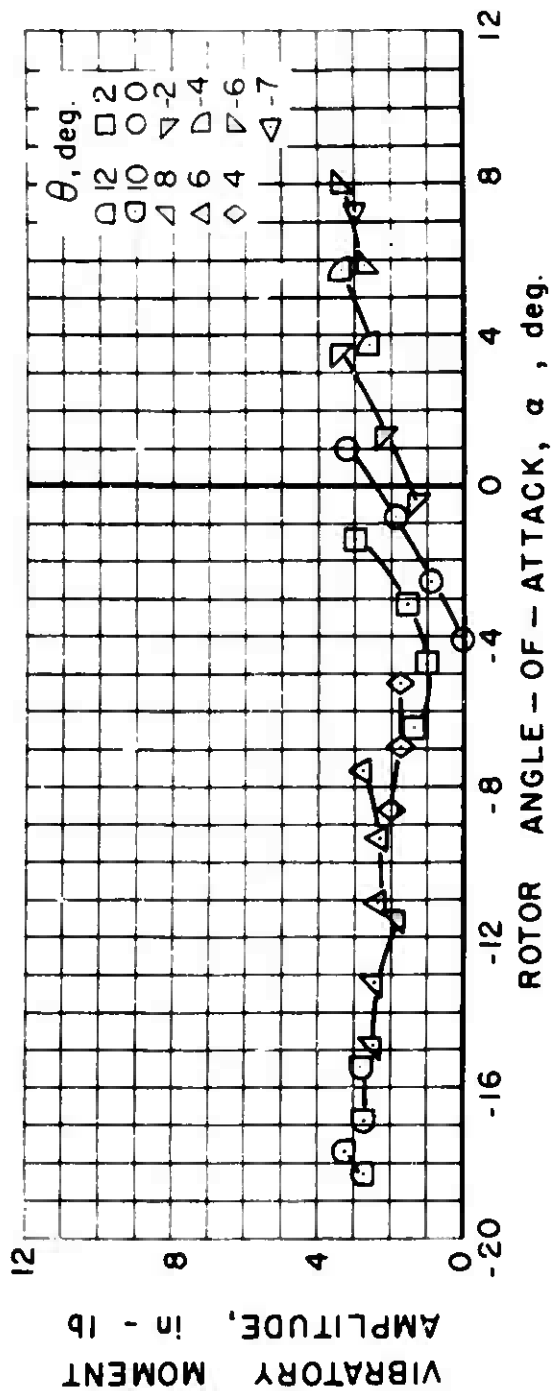
(b) EDGEWISE BENDING MOMENT, 21% R

Figure 89. Continued.



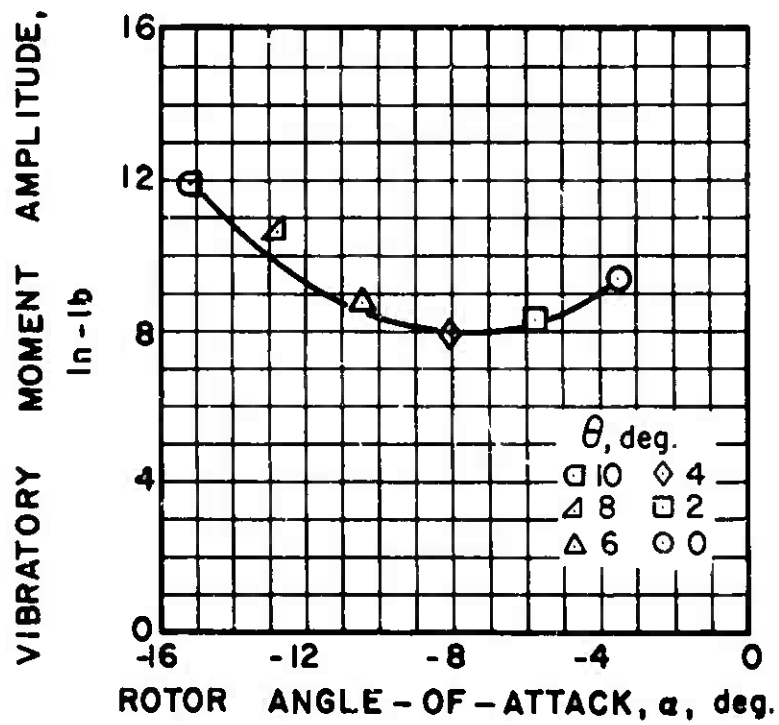
(c) EDGEWISE BENDING MOMENT, 47 % R

Figure 89. Continued.



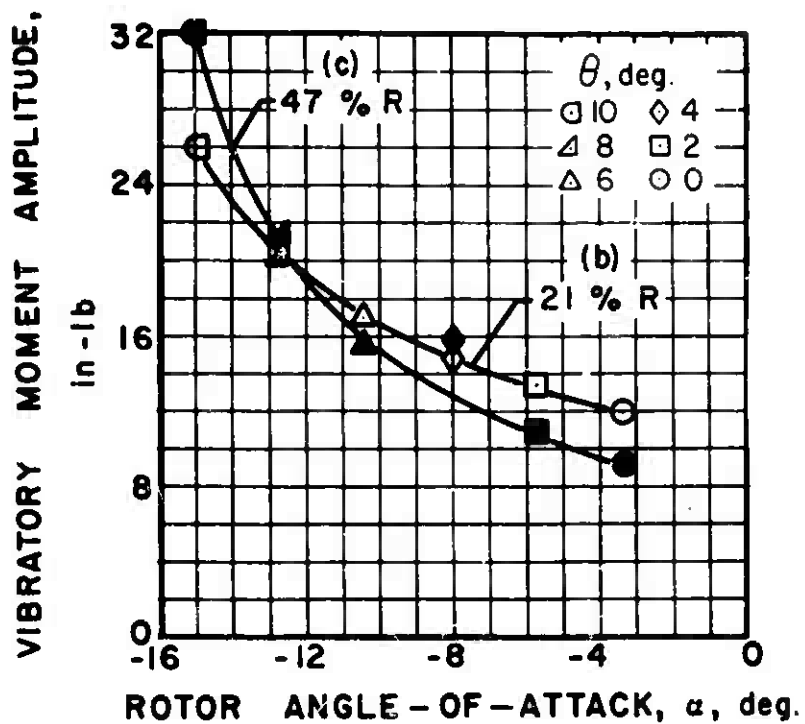
(d) TORSIONAL MOMENT, 17.5 % R

Figure 89. Concluded.



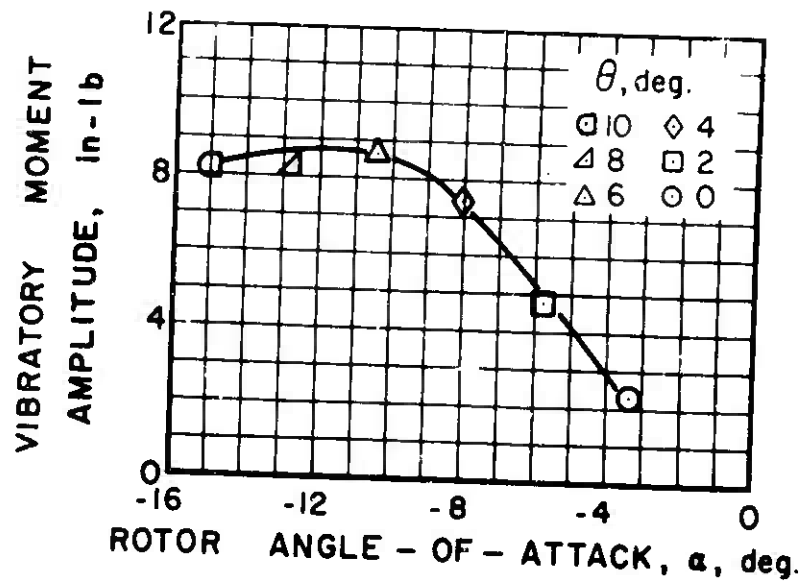
(d) FLATWISE BENDING MOMENT, 21% R

Figure 90. Experimental Vibratory Moment Amplitude, $\mu = 1.0$.



(b) & (c) EDGEWISE BENDING MOMENT

Figure 90. Continued.



(d) TORSIONAL MOMENT, 17.5 % R

Figure 90. Concluded.

APPENDIX IV

EXPERIMENTAL VIBRATORY CONTROL LOAD
AMPLITUDE FIGURES

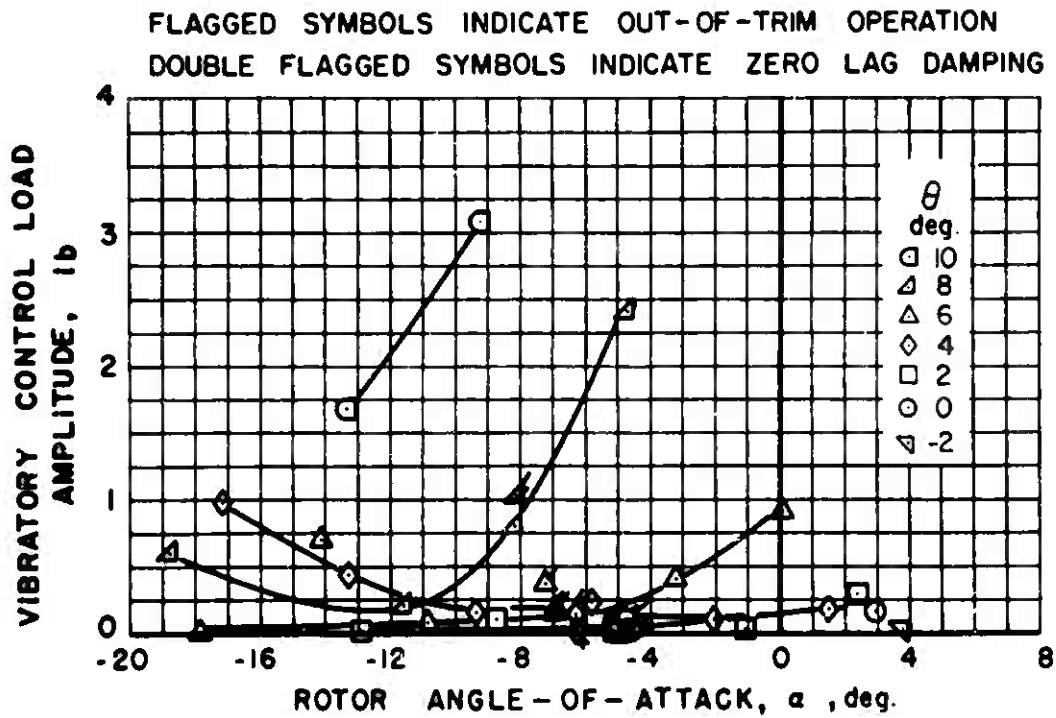


Figure 91. Experimental Vibratory Control Load Amplitude, $\mu = 0.2$.

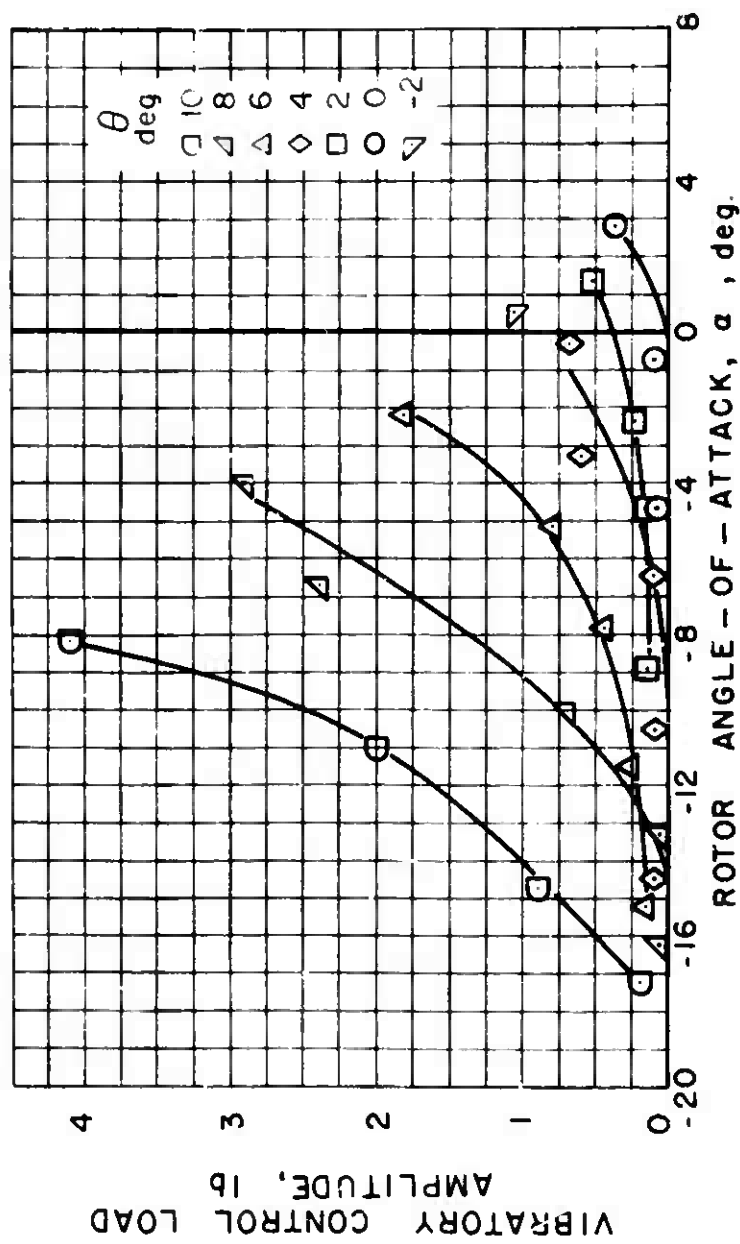


Figure 92. Experimental Vibratory Control Load Amplitude, $\mu = 0.3$.

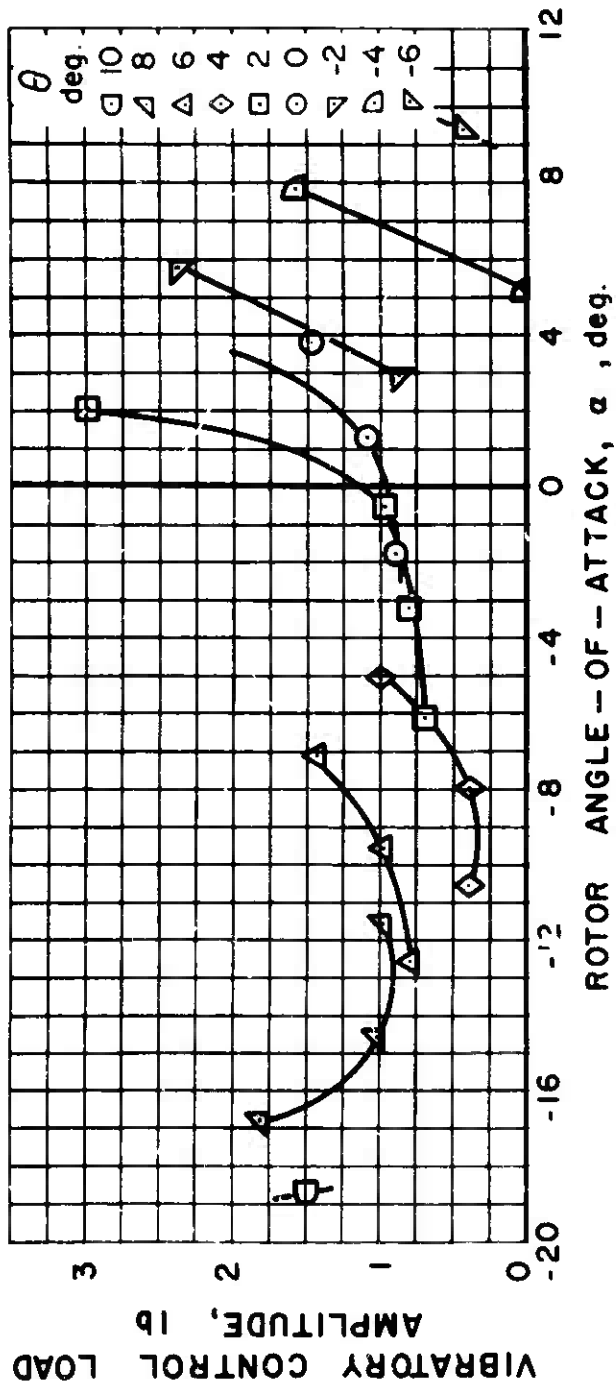


Figure 93. Experimental Vibratory Control Load Amplitude, $\mu = 0.4$.

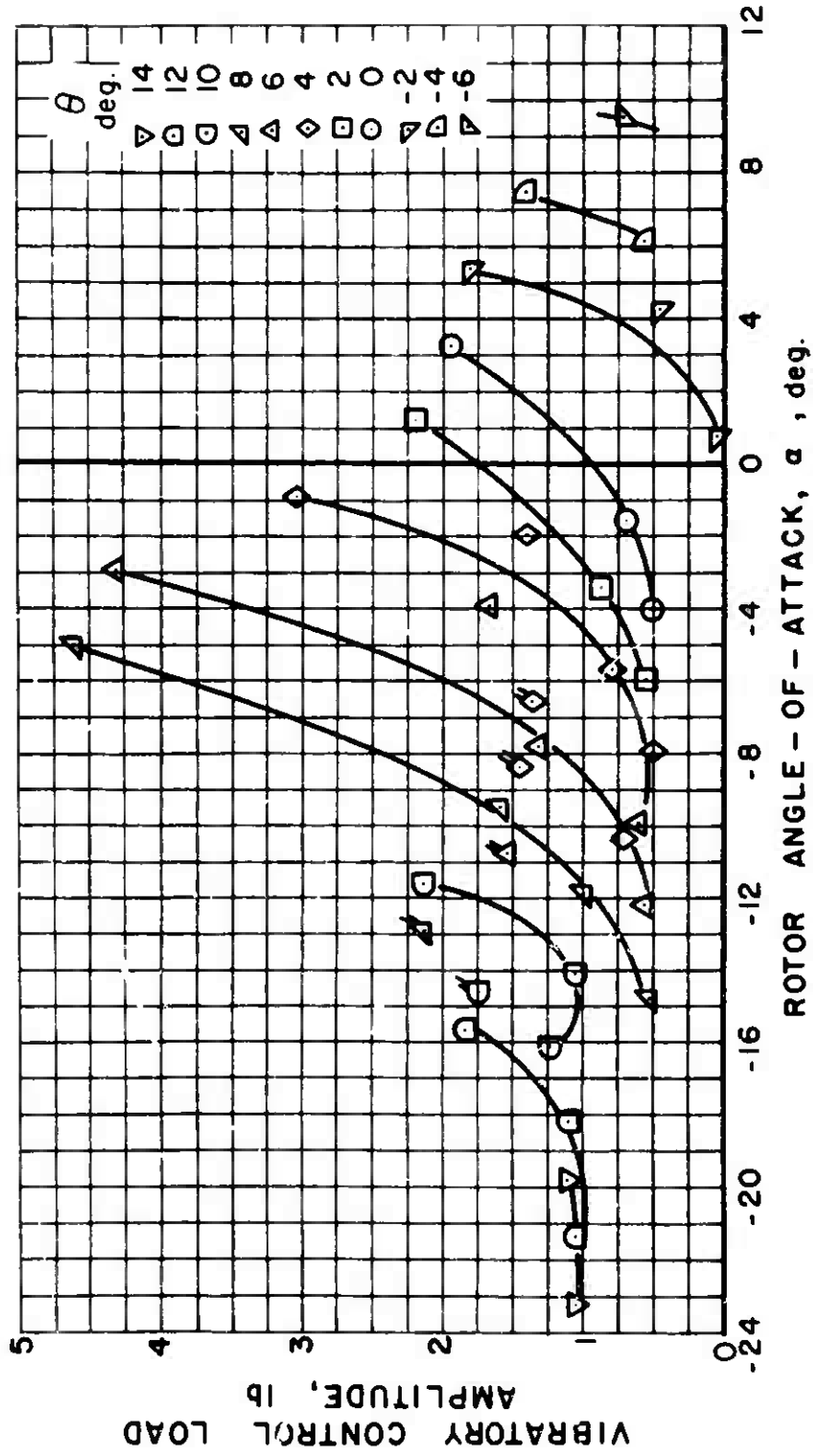


Figure 94. Experimental Vibratory Control Load Amplitude, $\mu = 0.5$.

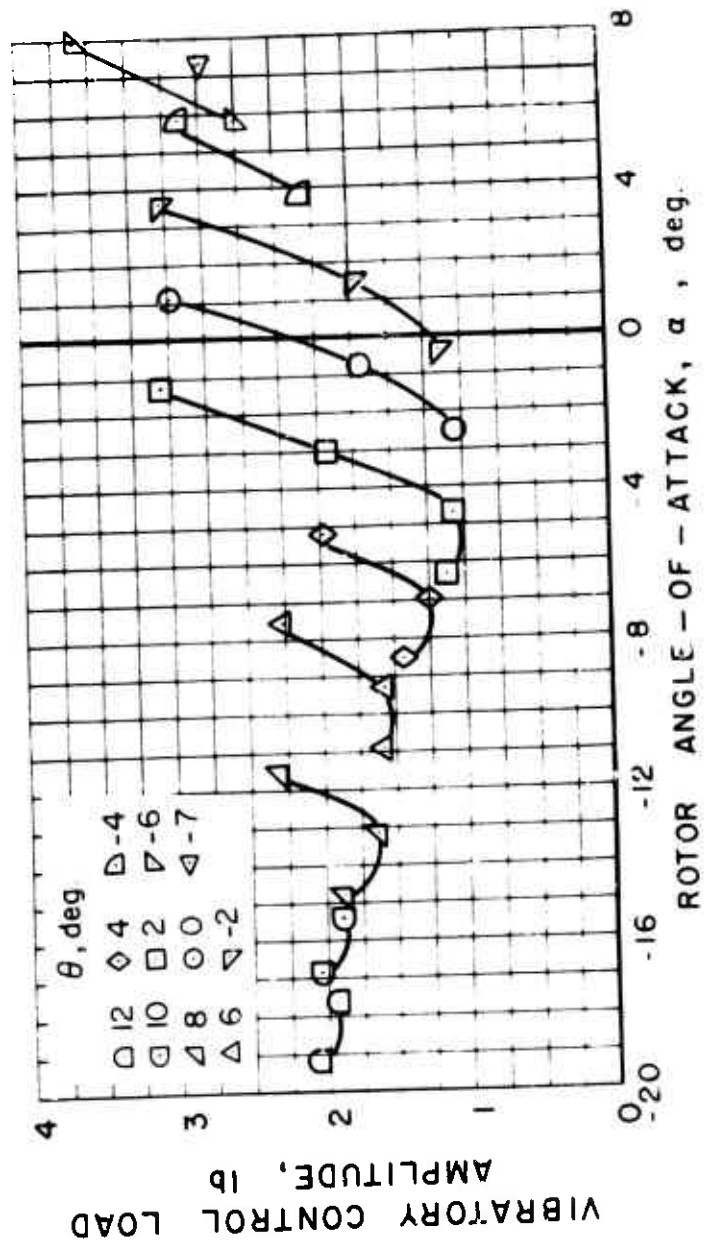


Figure 95. Experimental Vibratory Control Load Amplitude, $\mu = 0.7$.

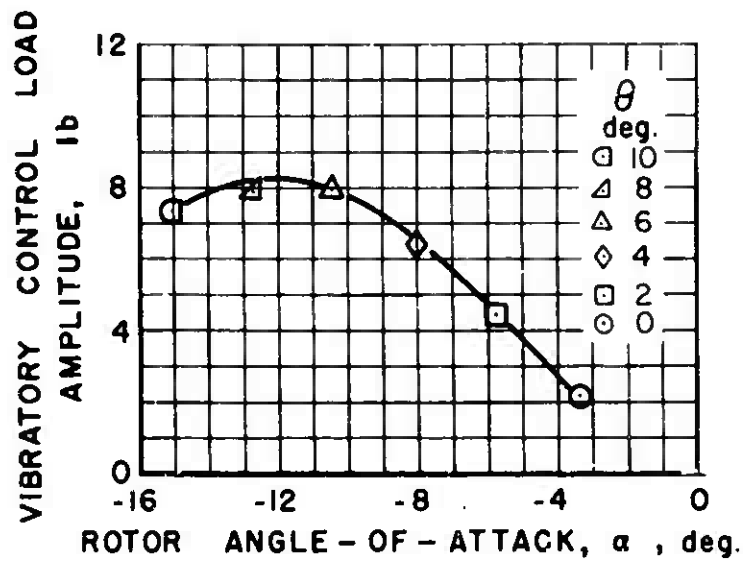


Figure 96. Experimental Vibratory Control Load Amplitude, $\mu = 1.0$.

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13. ABSTRACT An investigation was undertaken to obtain quantitative measurements of the vibratory forcing functions from the blades of rotary wing aircraft in the flight speed range encompassing both pure and compound helicopter operation. These measurements were made using dynamically scaled model rotor blades mounted on a specially instrumented rotor head. Testing was accomplished over a range of equivalent forward speeds from 75 to 300 knots and over a range of full-scale rotor lifts from zero to 40,000 lb. In addition to rotor performance, the final data include ten harmonics of the orthogonal blade root shear forces, rotor blade bending moments, and rotor control loads. A portion of the experimental results were correlated with a fully coupled aeroelastic analysis which included the effects of wake induced velocities. It was found that the inclusion of these effects improved the correlation of the flatwise shear forces over that obtained assuming uniform inflow.		

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