

AD 654906

# U. S. NAVAL AIR DEVELOPMENT CENTER

Johnsville, Westminster, Pennsylvania

Report No. NADC-AE-6719

1 June 1967

DETERMINATION OF NORMAL DRAG  
COEFFICIENTS FOR FLEXIBLE CABLES

PHASE REPORT  
AIRTASK NO. A37533000/2021/F101-13-07  
Work Unit No. 170

*Distribution of this document is unlimited.*



RECEIVED

JUL 25 1967

CFSTI



B



DEPARTMENT OF THE NAVY  
U. S. NAVAL AIR DEVELOPMENT CENTER  
JOHNSVILLE  
WARMINSTER, PA. 18974

Aero-Electronic Technology Department

REPORT NO. NADC-AE-6719

1 June 1967

205  
738

DETERMINATION OF NORMAL DRAG  
COEFFICIENTS FOR FLEXIBLE CABLES

PHASE REPORT  
AIRTASK NO. A37533000/2021/F101-13-07  
Work Unit No. 170

The determination of normal drag coefficients for flexible cables was developed to aid in a study of static cable drag dependence on cable strumming as related to underwater suspension cables used with airborne ASW sonar systems.

Reported by:

J. Dale M. McCandless  
J. Dale McCandless  
Sonar Sensor Division

Approved by:

H. Suter  
H. Suter, Superintendent  
Sonar Sensor Division

D. W. Mackiernan  
D. W. Mackiernan  
Technical Director

Distribution of this document is unlimited.

## SUMMARY

## INTRODUCTION

The determination of normal drag coefficients for flexible cables has been an art instead of a science because of the bizarre vibration modes of flexible cables in a fluid stream. These cable vibrations are commonly termed cable strumming. The difficulty arises because the drag is dependent on the amplitude and frequency of the cable vibration and an adequate understanding of the vibration modes is necessary to intelligently determine the cable drag. These modes have been studied<sup>1, 2</sup> and found to be basically defined by the classical vibrating string and Strouhal concepts.

A technique for the determination of the normal drag coefficient for a flexible cable is to be developed. The technique is to aid in a study of static cable drag dependence on cable strumming as related to underwater suspension cables used with airborne ASW sonar systems.

## RESULTS

Normal cable drag coefficients were determined from a static balance of coplanar fluid and gravity forces after measuring the cable drag angle of a towed streaming test cable with a terminal sphere standard. Cable strumming characteristics were determined and used to diagnose the cable vibration modes for selecting appropriate data points. Normal drag coefficients were determined for circular flexible cables from 0.057 to 0.140 inches in diameter, within the Reynolds number range 300 to 1300, and 0.2 to 1.2 kn velocity.

A parametric analysis was made of the estimated errors inherent in the technique. Maximum, limiting, and absolute error in the normal drag coefficient was predicted to fall between 10 and 20 percent. Probable experimental errors were between 5 and 10 percent.

## CONCLUSIONS

A general method for determination of the normal drag coefficient of a strumming flexible cable has been developed. The technique considers the cable drag dependence on the flow induced cable vibrations and is applicable to all flexible cable designs including faired and nonfaired types.

- 
1. Dale, J. R. and Menzel, H. R., Dec 1965; *Flow Induced Oscillations of Hydrophone Cables*; NAVAIRDEVCEM; 23rd Naval Underwater Sound Symposium Proceedings, ONR Rpt ACR-115, Paper 3A6, Pg 411.
  2. Dale, J. R. et. al. Sep 1966; *Dynamic Characteristics of Underwater Cables - Flow Induced Transverse Vibrations*; Report No. NADC-AE-6620.

TABLE OF CONTENTS

	Page
SUMMARY . . . . .	iii
Introduction . . . . .	iii
Results . . . . .	iii
Conclusions . . . . .	iii
LIST OF SYMBOLS . . . . .	v
DISCUSSION . . . . .	1
Background . . . . .	1
Cable Drag Coefficient . . . . .	1
Cable Strumming Force . . . . .	2
Data Acquisition . . . . .	2
Drag Coefficient Prediction . . . . .	3
Drag Coefficient Calculation . . . . .	3
Selection of Test Parameters . . . . .	5

LIST OF FIGURES

Figure	Title	Page
1	Instrumentation for Measurement of Cable Drag Angle and Strumming Accelerations . . . . .	7
2	Strumming and Drag Angle Signatures for a 0.107 In. Diameter Cable in a Gradually Decaying Flow . . . . .	8
3	Strumming Drag Coefficient and Force for a Smooth Cylindrical Cable 0.107 In. Diameter, 3 Ft Long . . . . .	9
4	Parametric Relations for the Streaming Flexible Cable . . . . .	10
5	Standard Data Sheet With Sample Calculation . . . . .	11
6	Estimate of Strumming Drag Coefficient . . . . .	12

L I S T O F S Y M B O L S

- A, B - Experimental constants
- $C_D$  - Dimensionless normal cable drag coefficient
- $C_{Ds}$  - Dimensionless normal cable drag coefficient based on  $d$  for normal flow past a strumming cable
- D - Terminal sphere diameter
- $d$  - Cable diameter
- F - Alternating periodic strumming force which accelerates the fixed end mass
- $F_u$  - Drag force on terminal sphere
- $f$  - Frequency of the transverse cable vibrations
- $f_c$  - Normal drag force per unit length of the cable
- $g$  - Gravitational constant
- $k$  - Spring constant of cable in transverse direction
- L - Cable length
- $l$  - Total moment arm of cable forces
- $M_o$  - Moment
- $m$  - Fixed end mass
- $m_c$  - Virtual cable mass per unit length (physical mass plus mass of an equivalent volume of water)
- $N_{Re}$  - Dimensionless Reynold's number =  $du_o/v$
- $n$  - Number of vibrating cable segments in the cable length L.  $n = L/l$
- $S_t$  - Dimensionless Strouhal number =  $fd/u_o$
- T - Tension in the cable

L I S T O F S Y M B O L S ( c o n t i n u e d )

- t - Time
- $u_n$  - Component of water velocity normal to the cable
- $u_o$  - Free stream water velocity
- W - Weight of the terminal sphere in water
- $w_c$  - Weight per unit length of cable in water
- y - Displacement of end mass
- $\ddot{y}$  - Acceleration of end mass
- $\alpha_1$  - Tangent angle at the tow point
- $\alpha_2$  - Tangent angle at the terminal mass
- v - Viscosity constant
- $\rho$  - Density of water
- $\theta$  - Cable angle with horizontal
- $\theta_c$  - Correction angle increment
- $\omega$  - Angular forcing frequency

## DISCUSSION

## BACKGROUND

To determine meaningful values for the normal drag coefficient of a flexible cable an understanding of the physics of cable strumming is essential. The results of two recent studies<sup>1 2</sup> are summarized below.

Transverse standing wave cable vibrations are excited by the interaction of the water flow relative to a flexible cable. When the flow velocity is gradually changed, transitions in amplitude and frequency occur at discrete velocities each time the number of standing wave segments changes by one. The frequency interval between successive transitions and a specific standing wave segment length characterizes a numbered partial vibration mode. (The term partial is used instead of harmonic because the frequencies are not even multiples of the fundamental.) The vibration modes are defined by the string equation

$$L = \frac{n}{2f} \sqrt{\frac{T}{m_c}} \quad (1)$$

where the forcing frequency is approximately defined by the Strouhal number,

$$S_t = fd/u_o \quad (2)$$

The amplitude of each standing wave vibration is a minimum near the transitional water velocity, frequently zero. Within each partial mode, a maximum amplitude is reached when the excitation frequency approximately equals the natural cable frequency of each vibrating segment. The normal drag coefficient is directly dependent on these amplitude variations.

## CABLE DRAG COEFFICIENT

An experimental technique has been developed to determine  $C_{Ds}$  by towing a test cable through water. The lower free end of the test cable was attached to a smooth surfaced sphere used as a standard, of known weight and known velocity dependent drag force. The cable drag angle at the tow point (fixed end) was measured and corrected for the bow in the streaming cable. The normal water force per unit cable length was then determined by summing the force moments about the tow point. Using this force and the cable diameter,  $C_{Ds}$  was computed.

- 
1. See pg iii.
  2. See pg iii.

The accuracy of the  $C_{Ds}$  determination is enhanced by a prudent selection of cable length and drag to weight ratio of the sphere standard. Cable lengths from 3 to 4 ft were used because longer cables generally are excited with multiple frequency beating effects which obscure the signature of the strumming signal. A 2-in. diameter smooth sphere weighing 0.504 lb (in water) was used as a standard.

#### CABLE STRUMMING FORCE

The periodic strumming forces, equivalent to cable tension oscillations, were determined by measuring the accelerations of a spring mounted mass. The mass and spring supported the cable at the tow point. The spring constant and mass were selected such that the spring restoring force was small compared to the force to accelerate the mass. Accordingly, the force determination is essentially the product, mass times acceleration.

#### DATA ACQUISITION

The instrumentation, mounted at the tow point, to determine  $C_{Ds}$  and  $F$  is illustrated in figure 1. The test cable was towed by a rotating arm with a 7-ft radius. During each test the angular velocity of the arm was varied such that the free stream tow velocity gradually decreased from about 1.2 to 0 kn in about 2 min. This provided data over the  $N_{Re}$  range of interest which spanned several partial vibration modes.

A segment of the raw data recording, for a 0.107 in. diameter cable, 36 in. long, is illustrated on figure 2. The water flow is decreasing uniformly from 1.0 to 0.2 kn. Observe the 3 partial vibration modes indicated by the 3 triangular forms of the acceleration signal. Starting from the high velocity end, these modes correspond to the fourth, third and second partials with half wave lengths of 9, 12, and 18 in., respectively. The trace of the cable drag angle is seen to hump during these partial vibrations, indicative of an increase in cable drag.

The  $C_{Ds}$  (based on 0.107-in. diameter) and the periodic strumming force are plotted against  $N_{Re}$  on figure 3. The normal drag coefficient for a nonstrumming circular cylinder is plotted for a reference. Each saw tooth form represents a discrete partial vibration. The minimum points are taken between the partials or near the transitions where the cable vibrations have decayed to a low level. Notice the minimum points approach the  $C_D$  reference plot.

The peak values correspond to the high level acceleration signals which are related to the transverse cable vibration amplitudes. For a specific partial mode, the highest  $C_{Ds}$  value is found at the velocity corresponding to these peak signals. The maximum and minimum points of these sawtooth characteristics will occur at different  $N_{Re}$  if the cable length is changed. This can be seen from equation No. 1 where a change in  $L$  will result in a different  $f$  for the same numbered partial,  $n$ . The

water forcing function will excite the cable at this new  $f$  at a different velocity or  $N_{Re}$ . The peak values of the parameters, therefore, describe an envelope which is independent of cable length. (Envelope values will be inferred with reference to  $C_{Ds}$  and  $F$  for the remainder of the report).

The drag angles that correspond to these envelope points, for a specific cable length, are usually found where the drag angle trace humps for each partial vibration mode. The humps usually correspond to peak values of the strumming signal. To aid in choosing envelope data the strumming signal should be recorded simultaneously with the cable drag angle signal. It is not necessary to calculate the strumming forces from the acceleration signals for the purpose of choosing envelope data. The velocities corresponding to the envelope data points can be selected using the acceleration trace. Therefore, a prerequisite for determining the drag coefficient envelope is to obtain continuous data of drag angle, strumming accelerations and water velocity over one or more partial vibration mode. The drag coefficient may be more sensitive to water velocity for unusual cross-sectional cable designs and it is good practice to evaluate the drag coefficient values over the velocity range of interest.

#### DRAG COEFFICIENT PREDICTION

Recent work relative to the dependence of cable drag on cable strumming has resulted in a scaling law to predict the  $C_{Ds}$ . The law is applicable to smooth flexible cables with circular sections. The  $C_{Ds}$  is equivalent to a factor times the nonstrumming coefficient or,

$$C_{Ds} = C_D [1 + 10 (d^2/\pi_c)^2] \quad (3)$$

This concept has been verified for cables from 0.057 to 0.140-inches in diameter over a  $N_{Re}$  range of 300 to 1300.

#### DRAG COEFFICIENT CALCULATION

The experimental technique employed to measure the  $C_{Ds}$  of a flexible cable is based on a balance of the static force moments acting on the cable and terminal sphere. Figure 4 illustrates the forces involved in the static balance where the cable is assumed to stream in a straight line between the fixed end and the sphere.

The moment associated with the normal drag force per unit length of cable is given by:

$$\curvearrowright M_c (f_c) = \int_{L-l}^L f_c y dy = f_c l (L - l/2) \quad (4)$$

The moment associated with the cable weight is given by:

$$\mathcal{M}_o (w_c) = \int_{L-l}^L w_c y \cos \theta dy = w_c \cos \theta (L-l/2) \quad (5)$$

Summing all the moments about point o, yields:

$$\Sigma M_o = 0 = F_u L \sin \theta + f_c l (L-l/2) - WL \cos \theta - \quad (6)$$

$$w_c l \cos \theta (L-l/2) f_c = w_c \cos \theta + \frac{W \cos \theta - F_u \sin \theta}{l(1-l/2L)}$$

Since the normal water force per unit length of cable, where the cable is at an angle  $\theta$  with the horizontal, is:

$$f_c = C_{Ds} d \frac{\rho}{2g} (u_o \sin \theta)^2 \quad (7)$$

then

$$C_{Ds} = \frac{f_c}{\frac{d\rho}{2g} (u_o \sin \theta)^2} \quad (8)$$

Since the tangent angle,  $\alpha$ , is measured, a correction angle increment  $\theta_c$  must be added to  $(90 - \alpha_1)$  to account for the bowing effect of the flexible cable, thereby obtaining a corrected value for  $\theta$ . By assuming the cable curvature to represent an arc length of a circle the value of  $\theta_c$  is derived from the angle relations illustrated on figure 4B.

A sample data sheet used to calculate  $C_{Ds}$  is illustrated in figure 5 along with a typical calculation taken from the data presented. The sequential calculation steps to be followed conform to the format of the data sheet and are outlined below.

1. After the setup constants are identified, the measured parameters for each selected data point are entered.
2. The angle correction tabulation is completed as identified by the column headings to obtain the angle  $\theta$ .
3. The  $C_{Ds}$  calculation tabulation is completed as indicated by the column headings to obtain the  $C_{Ds}$  value.

The periodic variation in the static tension is shown plotted as F in figure 3. As discussed previously, it is not necessary to calculate F since the recorded acceleration signal is proportional to F. Since the static tension oscillations are more meaningful than accelerations of a reference mass, the calculation is outlined as follows: The motion of the fixed end is considered to be a forced spring-mass system with negligible damping. The natural frequency is always less than the forcing frequencies. The equation of motion is:

$$m\ddot{y} + h_y = F \cos \omega t \quad (9)$$

Since  $\dot{y}$  will be maximum when  $\cos \omega t = +1$  and  $\dot{y}_{\max} = (2\pi f)^2 y_{\max}$ , equation 9 reduces to:

$$F = \pm \dot{y} \left[ \frac{k}{(2\pi f)^2} + m \right] \quad (10)$$

The acceleration level and signal frequency are taken at the selected data points.

#### SELECTION OF TEST PARAMETERS

Selection of the independent test parameters ( $L$ ,  $F_u$ ,  $W$ ,  $u_o$  and  $\theta$ ) was based on both the signal characteristics and the allowable error. The cable lengths used were less than 4 ft since longer cables are usually excited at multiple frequencies and the associated beat effects obscure the shape of each partial structure. When the partial structure is obscured, the selection of data points, corresponding to envelope values, is difficult. The cable must be long enough to be excited in at least 3 partial modes to adequately define the drag coefficient envelope. A cable length of 3 ft has been satisfactory for cables up to 0.2-in. diameter tested in the 0 to 1 kn velocity range. The sources of error inherent in the technique are:

1. Inaccuracy in measuring the physical system constants ( $w_c$ ,  $W$ ,  $F_u$ ,  $\lambda$ ,  $L$ , and  $d$ ).
2. Assumptions made regarding the drag angle correction concept.
3. Measurement error in the test variables  $u_o$  and  $\theta$ .

An estimate of the overall error was obtained by considering the magnitude of each of these sources. First, the precision of the physical system constants can be controlled by the experimenter to be a negligible weighted portion of the more dominant sources. The constants were generally considered good to 1 percent.

Secondly, an error in the drag angle correction concept is inherent because the bowed cable geometry departs from the assumed arc length of a true circle. The error is assumed to increase with the magnitude of  $\theta_c$  and is estimated as 5 percent of  $\theta_c$ .

Third, the error in the calculated value of  $C_{DS}$ , relative to the estimated individual errors in  $u_0$  and  $\theta$ , was analyzed by obtaining an expression for the total differential of equation 8. A measurement error of  $\pm 2$  percent of 1.0 kn was chosen as the overall measurement error in  $u_0$ . This is based on the error inherent in the measurement and readout of  $u_0$ . An estimated measurement error of 0.3 deg (2 percent of full scale-assumed as 15 deg), together with the stated 5 percent drag angle correction error comprise the total estimated error for  $\theta$ . Using these error values and the nominal physical values (figure 5) for the experimental setup, limiting error curves were drawn for the useful ranges of  $u_0$  and  $\theta$ . The curves are illustrated in figure 6. The curves represent upper limit errors in  $C_{DS}$  since the individual errors in  $\theta$  and  $u_0$  were always summed so as to give the maximum error in the drag coefficient. If a coefficient of 1.0 is computed for a given  $\theta$  and  $u_0$ , and the coordinate point  $(\theta, u_0)$  falls below the 10 percent curve, the experimental error is greater than 10 percent; if the point  $(\theta, u_0)$  is above the 20 percent curve, the error is less than 20 percent. The area above the respective curves, therefore, defines a  $C_{DS}$  error less than the limit indicated. The experimental data points were considered acceptable when they fell between the two limiting curves since the experimental error is probably between 5 and 10 percent of the drag coefficient value. The position of these plots is dependent on the choice of the physical system constants. Accordingly, the curves are valid only for the constants used (figure 5). An attempt was made to determine the position sensitivity of the curves to the cable diameter and the terminal sphere's drag to weight ratio.

1. Cable diameter, d: increasing the diameter resulted in lowering the limiting curves.

2. Drag to weight ratio: increasing the ratio again results in lowering the limiting curves; however, the normal velocity range would be reduced since the increased drag on the sphere results in higher tangent angles,  $\alpha_1$ , at the tow point. The 2 in. diameter 0.504 lb (water weight), smooth sphere was chosen as a suitable standard for the experimental setup employed.

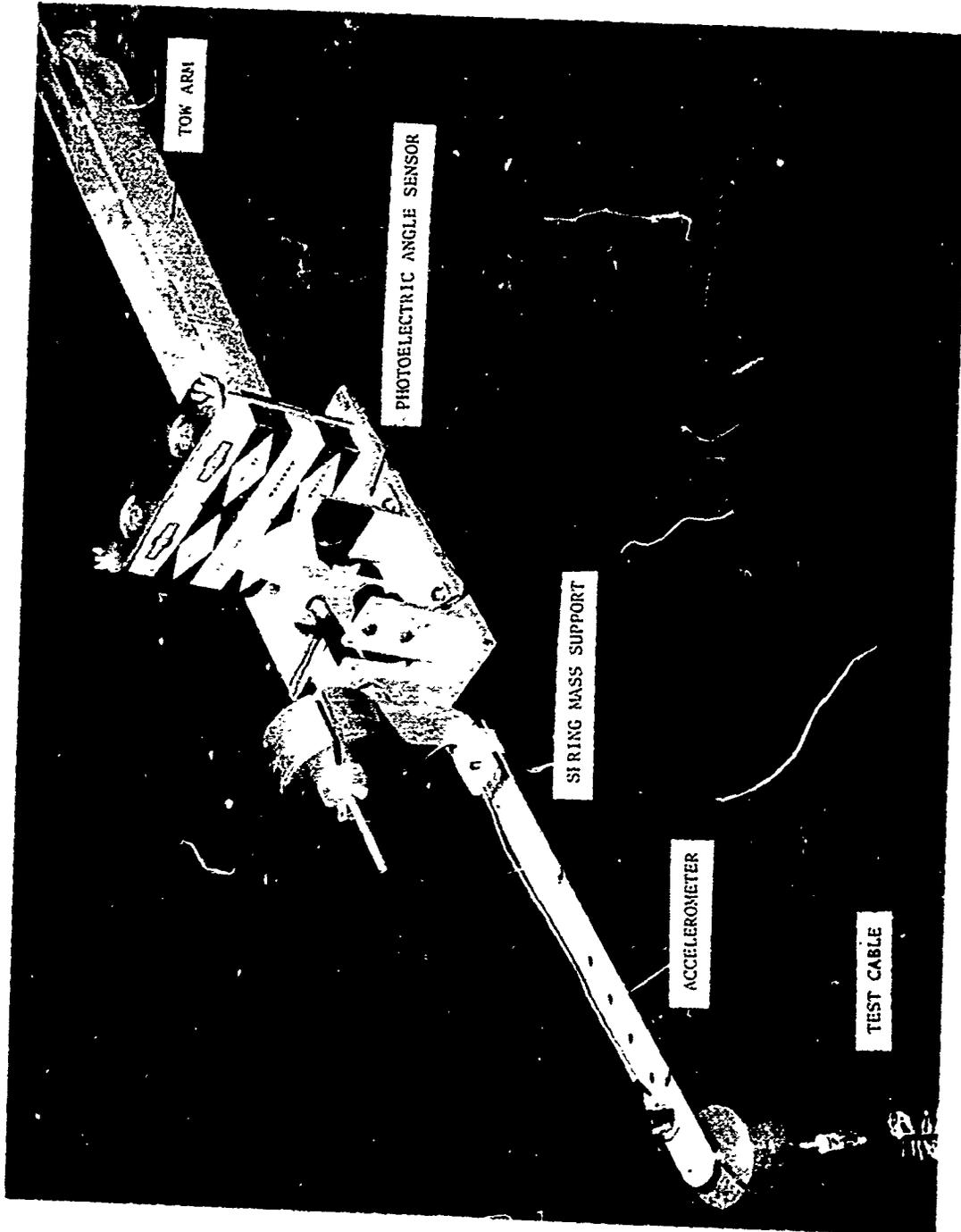


FIGURE 1 - Instrumentation for Measurement of Cable Drag Angle and Strumming Accelerations

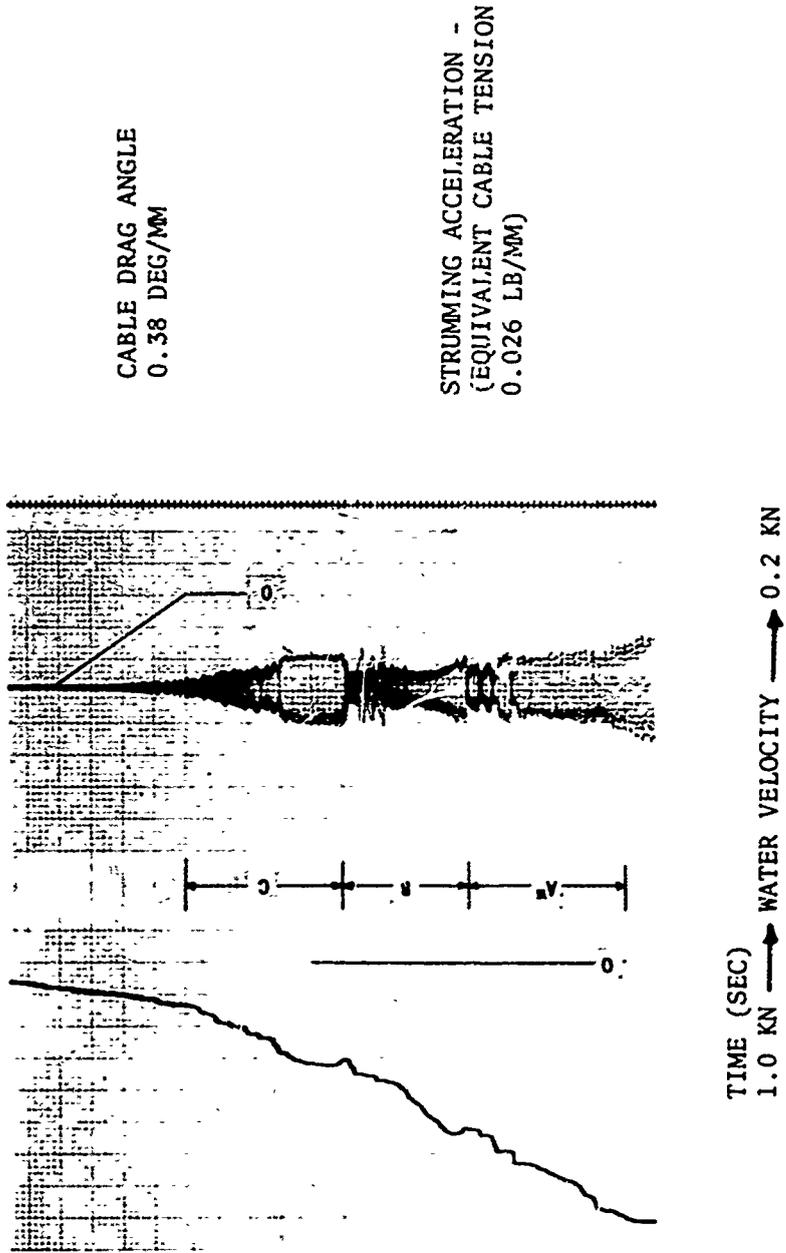


FIGURE 2 - Strumming and Drag Angle Signatures for a 0.107 In. Diameter Cable in a Gradually Decaying Flow

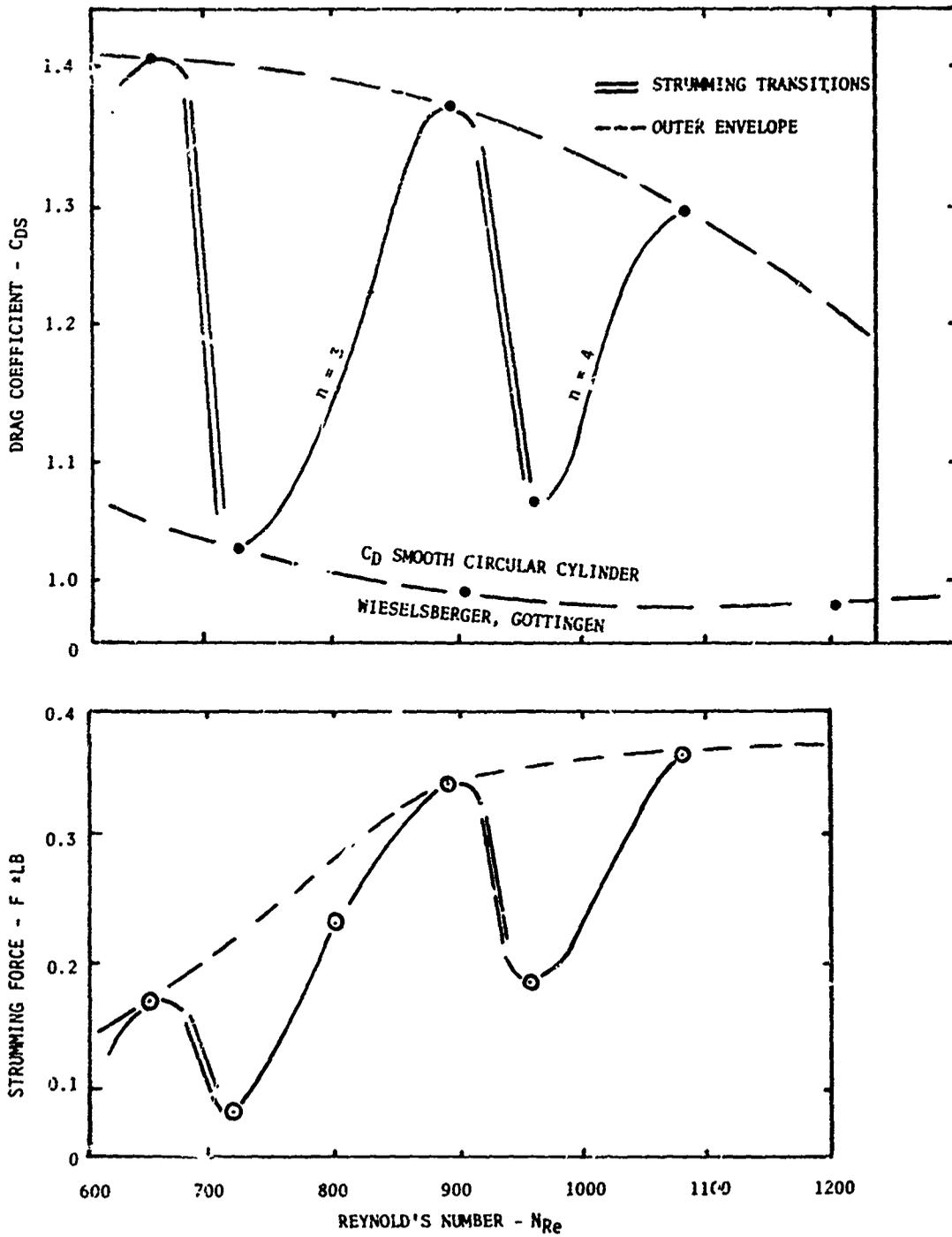
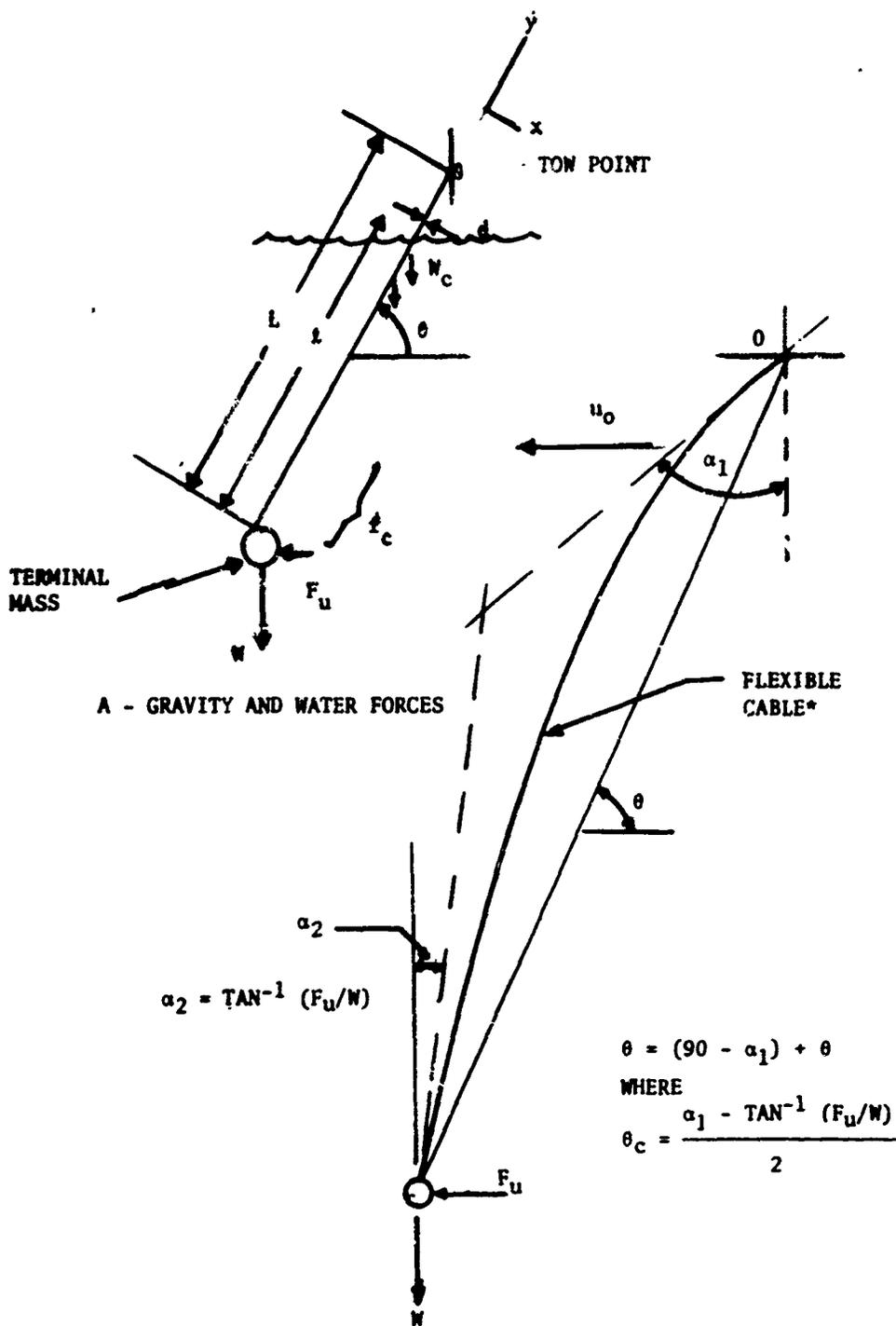


FIGURE 3 - Strumming Drag Coefficient and Force for a Smooth Cylindrical Cable 0.107 In. Diameter, 3 Ft Long



\* THE CABLE IS ASSUMED TO STREAM WITH THE CURVATURE OF A CIRCLE.  
 B - DRAG ANGLE CORRECTION

FIGURE 4 - Parametric Relations for the Streaming Flexible Cable

NADC-AE-6719

CABLE DRAG COEFFICIENT TEST CABLE 0.107 IN. DIA TEST NO. 1 DATE

EQUATIONS

$$f_c = W_c \cos \theta + \frac{W \cos \theta - F_u \sin \theta}{A} ; C_{DS} = \frac{f_c}{b (u_0 \sin \theta)^2}$$

$$F_u = C_D \frac{10^2 d^2}{8g} u_0^2 ; A = 1 (1 - \frac{1}{2L}) ; B = d \frac{D}{2z} (1.69)^2$$

SETUP CONSTANTS

W = 0.5075 LB (WATER WEIGHT)

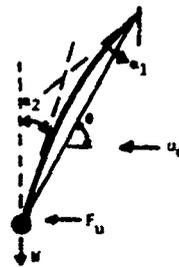
W<sub>c</sub> = 0.0019 LB/FT (WATER WEIGHT)

A = 1.79 FT    l = 3.00 FT  
L = 3.71 FT

B = 0.0247  $\frac{LB-SEC^2}{FT^3}$     d = 0.0089 FT

F<sub>u</sub> = 0.0444 u<sub>0</sub><sup>2</sup>    D = 0.167 FT  
C<sub>D</sub> = 0.73  
u<sub>0</sub>, KN

CABLE GEOMETRY



1. MEASURED PARAMETERS

$\alpha_1$	$u_0$ KN	$f_s$ C/S
10.5	0.77	52

2. ANGLE CORRECTION

$\alpha_1$	$u_0^2$	$F_u u_0^2$	$\tan^{-1} \frac{F_u}{W}$	$\alpha_2$	$\frac{\alpha_1 - \alpha_2}{2}$	$(90 - \alpha_1) + \theta_c$
10.50	0.595	0.0263	0.0518	3.00	3.70	83.20

3. C<sub>DS</sub> CALCULATION

	1		2	3	4	5	f <sub>c</sub>	6	C <sub>DS</sub>
cos θ	Ⓜ cos θ	sin θ	F <sub>u</sub> sin θ	1 - 2	$\frac{1}{A}$	Ⓝ cos θ	4 + 5	(u <sub>0</sub> sin θ) <sup>2</sup>	$\frac{C_{DS} f_c}{f_c}$
0.118	0.0599	0.993	0.0261	0.0336	0.0189	0.00085	0.6197	0.583	1.37

NOTE:

REPRESENT CALCULATION NUMBER

ENTER VALUE OF CONSTANT

FIGURE 5 - Standard Data Sheet With Sample Calculation

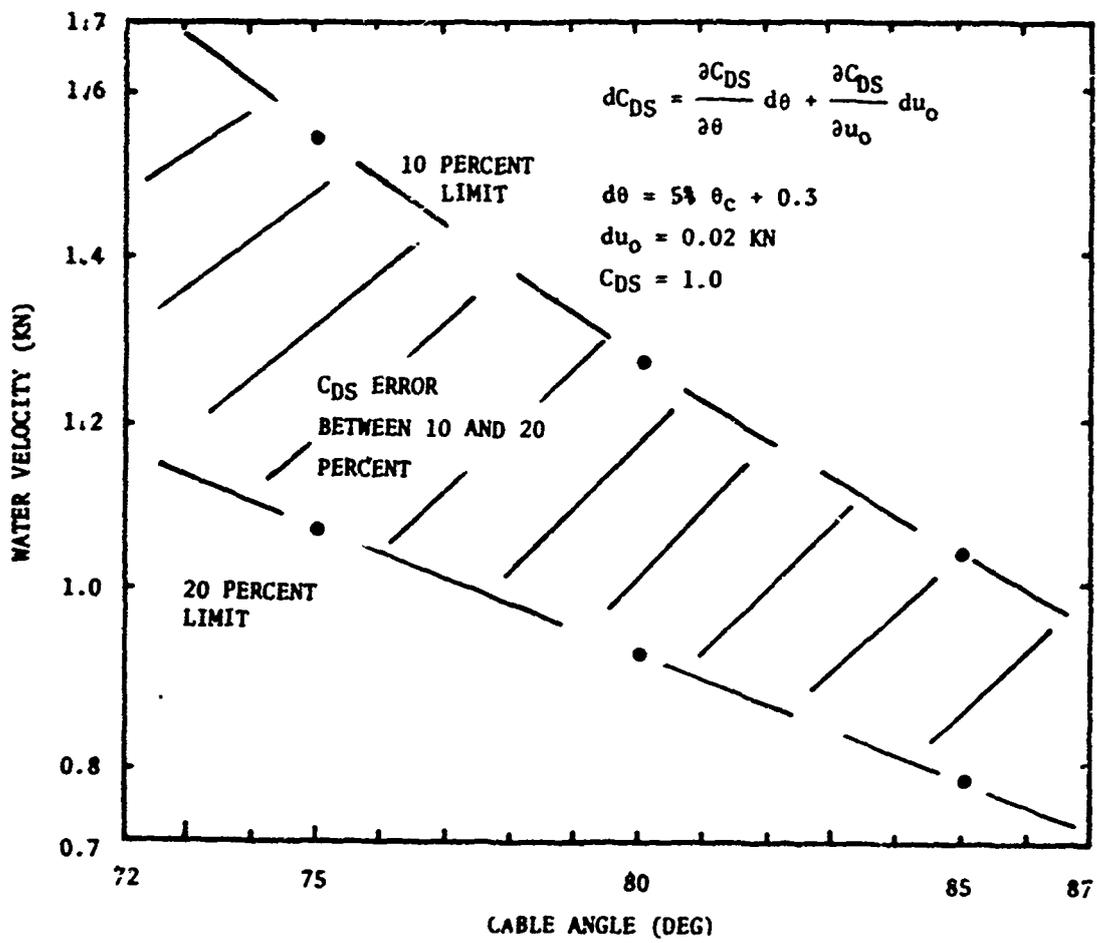


FIGURE 6 - Estimate of Strumming Drag Coefficient

**DOCUMENT CONTROL DATA - R & D**

*(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)*

1. ORIGINATING ACTIVITY (Corporate author) AERO-ELECTRONIC TECHNOLOGY DEPARTMENT NAVAL AIR DEVELOPMENT CENTER, JOHNSVILLE, WARMINSTER, PENNSYLVANIA 17094		2a. REPORT SECURITY CLASSIFICATION <b>UNCLASSIFIED</b>	
		2b. GROUP	
3. REPORT TITLE <b>DETERMINATION OF NORMAL DRAG COEFFICIENTS FOR FLEXIBLE CABLES</b>			
4. DESCRIPTIVE NOTES (Type of report and, inclusive dates) <b>PHASE REPORT</b>			
5. AUTHOR(S) (First name, middle initial, last name) <b>J. R. DALE AND J. M. McCANDLESS</b>			
6. REPORT DATE <b>1 JUNE 1967</b>		7a. TOTAL NO. OF PAGES <b>20</b>	7b. NO. OF REFS <b>2 (FOOTNOTES)</b>
8a. CONTRACT OR GRANT NO.		9a. ORIGINATOR'S REPORT NUMBER(S) <b>NADC-AE-6719</b>	
b. PROJECT NO. <b>AIRTASK NO. A37533000/2021/F101-13-07</b>		9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)	
c. WORK UNIT NO. 170			
d.			
10. DISTRIBUTION STATEMENT <b>DISTRIBUTION OF THIS DOCUMENT IS UNLIMITED.</b>			
11. SUPPLEMENTARY NOTES		12. SPONSORING MILITARY ACTIVITY <b>NAVAL AIR SYSTEMS COMMAND DEPARTMENT OF THE NAVY</b>	
13. ABSTRACT  The determination of normal drag coefficients for flexible cables was developed to aid in a study of static cable drag dependence on cable strumming as related to underwater suspension cables used with airborne ASW sonar systems.			

14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
FLEXIBLE CABLE DRAG COEFFICIENT STRUMING						