BOEING
SCIENTIFIC RESEARCH LABORATORIES

Numerical Analysis and Related Literature for Scientific Computer Users

Second Edition

James F. Price

MATHEMATICS RESEARCH   **MARCH 1966**

NUMERICAL ANALYSIS AND RELATED LITERATURE FOR

SCIENTIFIC COMPUTER USERS

SECOND EDITION

by

James F. Price

PREFACE TO THE SECOND EDITION

Some idea of the book publishing explosion which has been occurring in these subjects in the last five years is obtained by considering that the May 1961 edition of this document listed 69 book titles. This new edition lists 151. In addition, the present list is not quite as complete as the earlier one, and several books reviewed in the earlier edition have now been dropped.

Perhaps the author should have omitted more books from this listing than he did, so that the reader wouldn't have such an imposing volume to look at. However, it is thought that anyone wishing a shorter list can just consider books which are listed with double *asterisks* (or in the index he can look at *underlined* page numbers).

The original edition had a section devoted to *Numerical Procedures in Recent Periodicals*. Such a section has not been included in the Second Edition. The abstracting journal, *Computing Reviews*, is now operating in a reasonably current manner, so that new literature may now be found quite easily. Periodically (perhaps every three years?), a Permuted (KWIC) Index to *Computing Reviews* is published which lists journal articles by subject matter (as well as by author and by review number).

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NUMERICAL ANALYSIS AND RELATED LITERATURE FOR

SCIENTIFIC COMPUTER USERS

. Second Edition

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ABSTRACT

The Second Edition of this annotated bibliography lists the contents of over 150 books in English on numerical analysis and related literature. It is meant for the general scientific computer user and not for the research numerical analyst; the descriptions and suggestions are given with this in mind.

It is expected that the most useful section will be the 27-page index which tells in which books various topics may be found. There is also a section describing how to look up further information on such topics which may be found in the literature.

INTRODUCTION

When someone plans to put a numerical problem on a digital computer, he may very likely look up the pertinent numerical analysis subject in the reference book on his desk. If this book does not cover the subject, he can go to the library. If the programmer knows the contents of the various reference works, he can run down a particular reference book even if someone else has it checked out at the time. However, most of the huge number of people programming for the digital computers are not specialists in numerical analysis. This document is written to aid such people by (1) listing what is in some of the books on this and related subjects, (2) giving one man's opinion of the relative reading difficulty of various works and of the relative usefulness in computer applications, and (3) explaining how to find out if what they want is available in the literature.

There has been no attempt to make this a complete listing of where information can be obtained on these subjects. Rather it is a listing of reference works which the author and analysts and computer programmers of the author's acquaintance use from time to time. No foreign language references have been given. Although the German, Russian, and French languages have their share of excellent references, and although in some cases the information is not available in English, the fact remains that a large majority of computer users and programmers do not know any other language and/or can never be induced to read foreign language references. This document is directed to such "English-limited" readers; we would not want to discourage the foreign language reader from obtaining his references from the most suitable source independent of language. A great many good Russian books have been translated into English and are listed here.

Part I lists books containing numerical analysis and related subjects. When a computer user has a new problem, he might wish to look up some of his favorite references in this list to see if they discuss this new problem or problems similar to it.

The listing contains a great majority of the English texts on numerical analysis, but only a very limited number on what we think of as "related literature." It was often very hard to decide which books to include and which to omit on such topics as (for example) linear programming, or linear algebra, or FORTRAN programming, which are represented in the literature by a very large number of titles. In many cases the actual choice was quite arbitrary.

Books listed by a double asterisk are recommended as references which the author has found to be of most use to computer people because of their content, their emphasis on computer applications, and/or to their clarity of exposition.

Part II consists of a general discussion of how one goes about looking up given subjects in the literature and how he can find whether or not certain tables are available.

Part III is a subject index. It is thought that this index may be useful either in the obvious way of finding a book which discusses the desired topic, or also in determining whether a certain reference work (which had previously been found especially useful) also is listed as discussing today's topic.

The formation of a really comprehensive index on numerical procedures and related subjects would have been a major undertaking. Many individual books themselves have only sketchy indes. In general,

this index contains quite specific listings in numerical analysis topics but usually only general listings on related topics. For example, there is no reference made to "Weinstein method," although there is a general reference to "Variational methods"; there is no reference to "Duality," although there are references to other linear programming topics such as "Simplex method."

Often a certain subject may be in a particular book under a different name or under no name at all. Then the question is whether this topic should be shown as being in the book (because it might be so hard to find there). In general, if there is a certain listing in our index, and if although the subject is discussed in a particular source, there is no similar listing in the source's index or paragraph headings, this reference will most often be omitted from our index.

A few general topics are listed with a great many references. The more detailed listings have been chosen quite arbitrarily, but it is hoped that enough such topics are represented in the index to make it of practical use.

Perhaps the most serious complaint about the index may be that while in some cases all of the sources which discuss a certain subject may not be listed, in other cases a source may be listed which only casually refers to the subject. For this reason, *when more than five references are given on any subject,* a few of them will be *underlined as especially recommended.*

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Many pages in this document are partially blank. It is recommended that when new reference works come out which seem useful, they be entered (along with a few comments) in one of the blank spaces; then the new references may be recalled at a later time if the need arises.

Finally, for those who feel that the list of references in this document is so long that it is frightening, it is suggested that a shorter list is easily obtained by considering only those titles which are *marked with a double asterisk*. These are references which are particularly popular with scientific computer users or which the present author feels *should* be popular. Similarly, the *underlined* references in Part III make up a smaller group of *subject* references.

PART I.

NUMERICAL PROCEDURES IN BOOKS

Alphabetical by Author

(A *double asterisk* ** by an author's name means
that the reference is considered *especially good and/or
popular* for the average scientific computer user who is
required to learn about the subject.)

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ACHIESER, N. I.: <u>Theory of Approximation</u>. Ungar (1956) 307 pp.

This quite advanced treatise was translated from the 1947 Russian edition. The language of functional analysis is used throughout, and the approximation techniques described have been kept as general as possible. This has been considered to be an excellent book, and it is still quoted extensively even though newer treatises are now available.

Contents

1. Approximation problems in Linear Normalized Spaces
   This includes the approximation of a function in terms of another function or functions which depend on certain parameters. The classical Weierstrass approximation theorem is an example
2. Tchebycheff's domain of ideas
   This includes various approximation problems in which it is desired to minimize the deviation of greatest absolute value
3. Elements of Harmonic Analysis
4. Certain extremal properties of integral transcendental functions of the exponential type
   Bernstein's inequality; the theorems of Fejér and Riesz; criterion for representation of continuous functions as Fourier-Stieltjes integrals
5. Questions regarding the best harmonic approximation of functions
6. Wiener's theorem on approximation

Various addenda and problems:
   A. Elementary extremal problems and certain closure criteria
   B. Szegö's theorem and some of its applications
   C. Further examples of closed sequences of functions
   D. Carathéodory-Fejér problem and similar problems
   E. Solotareff's problems and related problems
   F. The best harmonic approximation of the simplest analytic functions

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(A *double asterisk* ** by an author's name means that the reference is considered *especially good and/or popular* for the average scientific computer user who is required to learn about the subject.)

ADLER, B., FERNBACH, S., and ROTENBERG, M. (Ed.): <u>Methods in Computational</u>

<u>Physics</u>. Academic Press (1963) <u>1</u>, 304 pp.; (1964) <u>2</u>, 271 pp.; (1964)

<u>3</u>, 386 pp; (1965) <u>4</u>, 385 pp.

The authors state that the major aim of this series of books is to
describe various numerical techniques developed recently for the solution
of practical physical problems in certain fields by means of digital
computers. These books should be very welcome indeed to the computer
programmer-analyst who is discouraged by the fact that numerical analysis
textbooks usually contain only (and always the same) very simple examples
of numerical problems. At least if his field of work is one of those
discussed here, he now has some excellent reading material available.

Contents

Volume 1, Statistical Physics

Numerical theory of neutron transport. Monte Carlo methods for solving
various practical problems in statistical physics.

Volume 2, Quantum Mechanics

The Gaussian function in calculations of statistical mechanics and
quantum mechanics. Atomic self-consistent field calculators by the
expansion method. The evaluation of integrals by the Zeta-function
expansion. Integrals for diatomic molecular calculations. Nonseparable
theory of electron-hydrogen scattering. Estimating convergence rates
of variational calculations.

Volume 3, Fundamental Methods of Hydrodynamics

Two-dimensional Lagrangian hydrodynamic difference equations. Mixed
Eulerian-Lagrangian method. The strip code and the jetting of gas
between plates. CEL: a time-dependent, two-space dimensional, coupled
Eulerian-Lagrange code. The tensor code. Calculation of elastic-
plastic flow. Solution by characteristics of the equations of one-
dimensional unsteady flow. The solution of two-dimensional hydro-
dynamic equations by the method of characteristics. The particle-in-
cell computing methods for fluid dynamics. The time dependent flow
of an incompressible viscous fluid.

Volume 4, Applications in Hydrodynamics

Numerical simulation of the earth's atmosphere. Nonlinear effects
of the theory of a wind-driven ocean circulation. Analytic con-
tinuation using numerical methods. Numerical solution of complete
Krook-Boltzmann equation for strong shock waves. Computer experiments
for molecular dynamics problems. Computation of the stability of
laminar compressible boundary layer. Some computational aspects of
propeller design. Methods of automatic computation of stellar evo-
lution. Computations pertaining to the problem of propagation of a
seismic pulse in a layered solid.

AITKEN, A. C.: Determinants and Matrices, 8th ed. Interscience (1956)

This is a reasonably elementary text. Numerical procedures are not emphasized, but rather it tells about matrices and determinants in general. Explanations are clear. A ninth edition is supposed to be available now.

Contents

1. Definitions and fundamental operations of matrices

2. Definitions and properties of determinants

3. Adjugate and reciprocal matrices; solution of simultaneous equations; rank and linear dependence

4. Cauchy and Laplace expansions; multiplication theorems

5. Compound matrices and determinants; dual theorems

6. Special determinants; alternant, persymmetric, bigradient, centro-symmetric, Jacobian, Hessian, Wronskian

ALLEN, D. N. deG.: Relaxation Methods. McGraw-Hill (1954) 257 pp.

        This is a reasonably elementary explanation of "how to relax." The
author emphasizes that the computer using these methods "should not allow
himself to become a human computing machine." He says, "the relaxation
method is far from being a method carried out according to any set rules--
instead it could be more accurately described as a method of breaking
such rules as are necessary formally to explain it." Perhaps this gives
an indication as to why these kinds of relaxation methods are not placed on
digital computers so very often; certainly this author appears to discourage it.

<div align="center">Contents</div>

ALT, F. L.: Electronic Digital Computers. Academic Press (1958) 336 pp.

This is a generally expository book about digital computers and their use in science and engineering. In the part of the book on numerical analysis, various methods are described, often from the point of view of evaluating advantages and disadvantages of particular methods when they are to be carried out on the machine.

General Outline of Contents

1. Introduction (generalities concerning computing)
2. Automatic digital computers (how the machine works)
3. Coding and programming
4. Problem analysis:

   Errors

   Overflow and scaling

   Checking

   Evaluation of explicit functions

   Differentiation and integration

   Ordinary differential equations

   Partial differential equations

   Algebraic equations

   Nonlinear equations

   Characteristic roots of matrices

5. Matching problems and machines:

   Problems from science and engineering

   Problems from other areas

   Characteristics of machine computation laboratories

ALT, F. L. and RUBINOFF, M. (Ed.): <u>Advances in Computers</u>, Vol. 1. –

Academic Press (1960)

These volumes (which have been coming out yearly) are "intended to occupy a position intermediate between a technical journal and a collection of handbooks or monographs." Articles are written by experts in various fields, and they survey recent advances in the field. Each article is "intended to be a piece of technical writing intelligible and interesting to specialists in fields other than the writer's own"; in a majority of cases this is probably true.

General Outline of Contents

Volume 1. General purpose programming for business applications. Numerical weather prediction. Automatic translation of languages. Programming computers to play games. Machine recognition of spoken words. Binary arithmetic.

Volume 2. Parabolic partial differential equations. Orthonormalizing computation. Microelectronics using electron-beam-activated machining techniques. Linear programming. Theory of automata.

Volume 3. Computation of satellite orbit trajectors. Multiprogramming. Nonlinear programming. Alternating direction implicit methods. Combined analog-digital techniques in simulation. Information technology and the law.

Volume 4. Formulation of data processing problems for computers. All-magnetic circuit techniques. Computer education. Digital fluid logic elements. Multiple computer systems.

Volume 5. Role of computers in election night broadcasting. Automatic programming in eastern Europe. Artificial intelligence and self-organization. Automatic optical design. Computing problems and methods in X-ray chrystallography. Digital computers in nuclear reactor design. Procedure-oriented languages.

Volume 6. In preparation.

AMES, W. F.: <u>Nonlinear Partial Differential Equations in Engineering</u>.

Academic Press (1965) 511 pp.

This new book will probably be used quite extensively as a reference by engineers and computer programmers who are trying to obtain solutions to such problems. The book discusses the origin of certain equations of this type, some analytic methods, some approximate methods (such as asymptotic processes, perturbation procedures, etc.) and quite a few numerical methods. A book on such a subject is bound to be quite advanced, but theoretical aspects are not stressed, and many examples are given. There is a good list of references at the end of each chapter.

Contents

1. The origin of nonlinear differential equations

2. Transformation and general solutions

3. Exact methods of solution

4. Further analytic methods

5. Approximate methods (perturbation, asymptotic, and weighted residual methods)

6. Further approximate methods (integral methods, the maximum operation, series expansions, etc.)

7. Numerical methods (for parabolic, elliptic, hyperbolic, and mixed systems)

8. Some theoretical considerations (well-posed problems, existence and uniqueness, etc.)

ARDEN, B. W.: <u>An Introduction to Digital Computing</u>. Addison-Wesley

(1963) 389 pp.

This is a very elementary textbook introducing the subjects of
computing and numerical analysis. The MAD language is used throughout.
In the third of the text on numerical methods, "what to do" is empha-
sized rather than "why."

Contents

1. Language and notation

2. Elements of a practical language

3. Statements and flow charts

4. Functions and example programs

5. The design of a practical machine

6. Machine language and components

7. Number systems and arithmetic

8. Computational error

9. Taylor's series and divided differences

10. The solution of equations

11. Additional programming topics

12. Interpolation

13. Numerical integration

14. Simultaneous linear equations

15. Approximation

16. The numerical solution of differential equations

17. Non-numerical problems

18. A simple compiler

BALAKRISHNAN, A.V., and NEUSTADT, L.W. (Ed.): Computing Methods in

Optimization Problems. Academic Press (1964) 327 pp.

This book is based on papers given at a conference on the subject
in January 1964. The idea was to tell of recent research progress in the
area and in particular to indicate computing experience gained on specific
large-scale problems. If one were working on a problem similar to one
of these, he should certainly be familiar with what is said about it here.

Contents

BELLMAN, R. and KALABA, R. (Ed.): Modern Analytic and Computational

Methods in Science and Mathematics. Elsevier (1963) <u>1</u>, 358 pp.;

(1964) <u>2</u>, 270 pp.; (1965) <u>3</u>, 220 pp.; <u>4</u>, in preparation.

These books explain the application of invariant imbedding methods
to various practical problems in radiative transfer. The numerical
methods used can also be applied to other problems in engineering and
physics. A large proportion of the pages in the first two volumes are
taken up with giving the FORTRAN programs and the results obtained for
particular problems.

Contents

Volume 1, Invariant Imbedding and Radiative Transfer in Slabs of Finite
   Thickness (Bellman, Kalaba, and Prestrud)

   1. The physical model
   2. Gaussian quadrature, zeros of Legendre polynomials, approximate
      system of differential equations, computational details
   3. Analytic aspects: existence, uniqueness, convergence
   4. Computational results

Volume 2, Invariant Imbedding and Time Dependent Transport Processes
   (Bellman, Kalaba, Prestrud, Kagiwada)

   1. Numerical inversion of Laplace transforms
   2. One dimensional neutron multiplication process
   3. Time dependent diffuse reflection from a slab

Volume 3, Quasilinearization and Nonlinear Boundary Value Problems
   (Bellman and Kalaba)

   1. Application of quasilinearization to the study of the Riccati
      equation
   2. Two-point boundary value problems for second order differential
      equations
   3. Monotone behavior and differential inequalities
   4. Systems of differential equations, storage, and differential
      approximation
   5. Partial differential equations
   6. Applications in physics, engineering, and biology
   7. Dynamic programming and quasilinearization
   Appendices: Minimum time program; design and control program;
      radiative transfer program; Van der Pol equation program; orbit
      determination program; cardiology program.

Volume 4, Numerical Inversion of the Laplace Transform: with Applications
   to Biology, Economics, Engineering, and Physics (Bellman, Kalaba, and
   Lockett

   Outline: Elementary properties of the Laplace transform; numerical
      inversion of the Laplace transform; applications; nonlinear
      equations; dynamic programming and ill-conditioned systems; ap-
      pendices.

BEREZIN, I. S. and ZHIDKOV, N. P.: Computing Methods, two vols. Addison-

Wesley (1963) 464 pp. and 679 pp.

These two volumes are translations from 1959 Russian texts for a
two-year (third and fourth year Moscow University) introductory course
in numerical methods. In this country it would be senior and first year
graduate level. The language of functional analysis is used whenever the
authors feel it will help in the explanations, and hence the volumes may
be considered as more advanced than they really are. However, what func-
tional analysis they do use is explained from a very practical point of
view.

The size of the books and the title lead one to hope that this might
be the long awaited single general purpose reference on computing methods,
but actually the major portions of these books could have been written
before the advent of large scale computers; the title really should have
been "Classical Numerical Analysis."

Contents

Volume 1

    1. Operations on approximate quantities

    2. The theory of interpolation and certain applications

    3. Numerical differentiation and integration

    4. Approximations

    5. Least squares approximations

Volume 2

    6. The solution of sets of linear algebraic equations

    7. Numerical solution of high degree algebraic equations and tran-
scendental equations

    8. The evaluation of eigenvalues and eigenvectors of matrices

    9. Approximate methods of solving ordinary differential equations

    10. Approximate methods of solving partial differential and integral
equations

BERGE, C.: <u>The Theory of Graphs and Its Applications</u>. Wiley (1962) 247 pp.

      This reasonably elementary book is a translation from a 1958 French
edition. The theory of graphs concerns itself with problems which are
stated in terms of points and lines or arrows which join them. Examples
are communications networks, circuit diagrams, family trees, etc. In
addition to explaining underlying theory, this book also gives practical
computational algorithms.

<div align="center">Contents</div>

BICKLEY, W. G. and THOMPSON, R. S. H. G.: <u>Matrices, Their Meaning and</u>

<u>Manipulation</u>. English Univ. Press (1964) 168 pp.

This reasonably elementary text first presents some practical problems
which may be formulated in terms of matrices, and then some introductory
theory of matrices. The last half of the book is concerned with numerical
procedures. There are a wealth of problems, many with answers, so that
the text should be suitable for self-study. Most parts of the book are very
well written. The index contains only entries which are not mentioned in
the very complete table of contents.

Contents

BODEWIG, E.: <u>Matrix Calculus</u>, 2nd ed. Interscience (1959) 452 pp.

This is a reasonably elementary book. However, unless one is familiar with his notation, it may often strike one as being "advanced." The subject matter consists mainly of numerical methods in dealing with matrix problems. The author has in mind that digital computers will be used in the work. It is quite a complete exposition of the topics covered.

General Outline of Contents

Part 1. Matrix calculus (basic definitions and elementary discussion)

Part 2. Linear equations

  a. Direct methods of solution

    1. Exact solutions

    2. Approximate solutions: triangularization, diagonalization, decomposition, Gauss-Doolittle method, etc.

  b. Iterative methods of solution

Part 3. Inversion of matrices

  a. Direct methods

  b. Iterative methods

Part 4. Eigenproblems

  a. Iterative methods (Power method, Jacobi, Magnier's method, Givens' method, gradient method, Wielandt's method, etc.)

  b. Direct methods (Leverrier's method, Krylov-Duncan method, Hessenberg method, Samuelson method, etc.)

BOOLE, G.: Calculus of Finite Differences, 4th ed. Chelsea (1958)

336 pp.

The first edition of this classical test was published in 1860. A
reprint of the second (1872) edition is published by Dover. The third
edition (1926) and this so-called fourth edition are practically the
same. In the recent literature, references are still often made to this
source, although perhaps many times this is done for historical reasons.

Contents

1. Nature of the calculus of finite differences

2. Direct theorems of finite differences (the operators of finite
    difference calculus)

3. Interpolation and mechanical quadrature

4. Finite integration and the summation of series

5. The approximate summation of series

6. Bernoulli's numbers and factorial coefficients

7. Convergency and divergency of series

8. Exact theorems (remainder terms, etc.)

9. Difference equations of the first order

10. General theory of the solutions of difference and differential
    equations of the first order

11. Linear difference equations with constant coefficients

12. Further miscellaneous propositions and equations; simultaneous equations

13. Linear difference equations with variable coefficients

14. Mixed (difference-differential) and partial difference equations

15. The calculus of functions

16. Geometrical applications

BOOTH, A. D.: <u>Numerical Methods</u>, 2nd ed. Academic Press (1957) 195 pp.

This is a reasonably elementary text. A wide range of subjects is covered (usually not in any great detail), but an amazing amount of information is packed into these short chapters.

Contents

de BRUIJN, N. G.: <u>Asymptotic Methods in Analysis</u>. Interscience (1958)

   200 pp.

        The application of asymptotic methods to practical problems is quite
difficult for the nonspecialist; he will probably find this book to be
easier to read than most of the other literature on the subject. However,
the methods here are explained by example, and there are no "cook book"
formulas to enable one to apply these methods to similar problems without
really knowing much about the field.

                              Contents

1. Introduction (and definitions)

2. Implicit functions

3. Summation

4. The Laplace method for integrals

5. The saddle point method

6. Applications of the saddle point method

7. Indirect asymptotics

    Tauberian theorems

    Differentiation of an asymptotic formula

8. Iterated functions

9. Differential equations

BUCKINGHAM, R. A.: <u>Numerical Methods</u>. Pitman (1957) 597 pp.

This is a reasonably elementary textbook. The author says he is concerned mainly with the needs of those using desk computers, but he also has the electronic computers in mind in some cases.

General Outline of Contents

1. Interpolation

2. Difference methods

3. Solution of algebraic equations

4. Matrices and determinantal equations

5. Solution of ordinary differential equations (initial problems)

6. Solution of ordinary differential equations (boundary value problems)

7. Integral equations

8. Partial differential equations

9. Functions of two variables; interpolation, cubature, differentiation, functions of a complex variable

10. Fitting data by method of least squares

11. Appendices on:

    A. Relations between powers and factorials

    B. Summary of difference formulas, with remainders

    C. Lagrangian formulas for differentiation and integration

    D. Orthogonal polynomials for curve fitting

BUTLER, R. and KERR, E.: <u>An Introduction to Numerical Methods</u>.

   Pitman (1962) 386 pp.

   This elementary text could either be used as a self-study book or
as a college text in introductory numerical analysis for nonmathematics
majors. Although the authors often mention digital computers, their
treatment of the subject matter indicates that many times they do not
have them in mind.

General Outline of Contents

1. Introduction (discussion of errors, etc.)

2. The solution of algebraic and transcendental equations (including

    the solution of simultaneous linear algebraic equations)

3. Finite differences

4. Interpolation

5. Numerical differentiation and integration

6. Numerical solution of differential equations (including both initial-

    value and two-point boundary value problems)

CASHWELL, E. D., and EVERETT, C. J.: A Practical Manual on the Monte

Carlo Method for Random Walk Problems. Pergamon (1959) 153 pp.

This is a reasonably elementary discussion of the Monte Carlo method
as applied to problems in atomic physics. Computational details are
stressed. In an appendix is a summary of 20 problems which have been
coded and run on a digital computer at Los Alamos.

Contents

1. Basic principles (pseudo-random numbers)

2. The source routine

3. The mean free path and transmission

4. The collision or escape routine

·5. The collision routine for neutrons

6. Photon collisions

7. Direction parameters after collision

8. Terminal classification

9. Remarks on computation

10. Statistical considerations

Appendix: Summary of problems run on Maniac I.

**COLLATZ, L.: The Numerical Treatment of Differential Equations, 3rd

(English) ed. Springer (1960) 568 pp.

This is quite an advanced treatise on the subject. However, in most cases the author goes into some detail to explain the processes, and there are many worked examples. The translation of the earlier German edition is generally so good that one does not realize it is a translation.

Contents

1. Mathematical preliminaries and some general principles (finite difference and interpolation formulas, Green's functions; some error distribution principles; functional analysis)
2. Initial value problems in ordinary differential equations
3. Boundary value problems in ordinary differential equations
4. Initial and initial/boundary value problems in partial differential equations
5. Boundary value problems in partial differential equations
6. Integral and functional equations

Appendix: Tables of various types of finite difference formulas used in the solution of differential equations problems

**CONTE, S. D.:   Elementary Numerical Analysis: An Algorithmic Approach.

McGraw-Hill (1965) 278 pp.

This elementary (junior level) text differs from a majority of
such texts which have been swamping the market in that it is not just
a poor carbon copy of the older ones. Although it is basically a numeri-
cal analysis text, computer flow charts and FORTRAN IV programs are often
given in connection with algorithms for carrying out certain computations.

Contents

1.   Number systems and errors

2.   The solution of nonlinear equations

3.   Interpolation and approximation

4.   Differentiation and integration

5.   Matrices and systems of linear equations

6.   The solution of differential equations

7.   Boundary value problems in ordinary differential equations

CRANDALL, S. H.: <u>Engineering Analysis: A Survey of Numerical Procedures</u>.

McGraw-Hill (1956) 417 pp.

This is a reasonably elementary book, and it is excellent as a cross between an engineering and a numerical analysis book. It is not often that in one book you can find fairly careful mathematical formulations as well as clear engineering explanations.

Contents

1. Equilibrium problems in systems with a finite number of degrees of freedom (systems of linear equations)

2. Eigenvalue problems for systems with a finite number of degrees of freedom

3. Propagation problems in systems with a finite number of degrees of freedom

4. Equilibrium problems in continuous systems

5. Eigenvalue problems in continuous systems

6. Propagation problems in continuous systems

As the author points out, chapters 1-3 discuss the three topics, <u>equilibrium problems</u>, <u>eigenvalue problems</u>, and <u>propagation problems</u>, for <u>lumped parameter systems</u>. Chapters 4-6 discuss <u>the same three topics</u> for <u>continuous systems</u>. This careful classification should be a big aid to a computer programmer who is not very familiar with basic engineering course topics.

CURTISS, J. H. (Ed.): <u>Sixth Symposium in Applied Mathematics</u>. McGraw-

Hill (1956) 303 pp.

The subject of this symposium in 1953 was "Numerical Analysis." Nine-
teen papers were given at the time by various numerical analysists. A
majority of the papers are quite advanced. Many are of interest to computer
users.

Contents

1. Computational problems in the theory of dynamic programming (Bellman)
2. Some methods for solutions of boundary-value problems in linear
   partial differential equations (Bergman)
3. Computational aspects of certain combinatorial problems (Bruck)
4. Numerical results in the shock configuration in mach reflection
   (Clutterham and Taub)
5. Some applications of gradient methods (Fischbach)
6. Some qualitative comments on stability in partial differential equations
   (Frankel)
7. Approximations in numerical analysis (Hastings, Hayward, Wong)
8. The conjugate-gradient method for solving linear systems (Hestenes)
9. Number theory on the SWAC (Lehmer)
10. The assignment problem (Motzkin)
11. The method of steepest descent (Rosenbloom)
12. Function spaces and approximation (Sard)
13. Some computational problems in algebraic number theory (Taussky)
14. Machine attacks on problems whose variables are permutations (Thompkins)
15. Best-approximation polynomials of given degree (Walsh)
16. Recent results in numerical methods of conformal mapping (Warschawski)
17. On the asymptotic transformation of certain distributions into the
    normal distribution (Wasow)
18. Error bounds for eigenvalues of symmetric integral equations (Wielandt)
19. On the solution of linear systems by iteration (Young)

DANTZIG, G. B.: <u>Linear Programming and Extensions</u>. Princeton Univ. Press (1963) 621 pp.

This is probably the best known book on linear programming. The subject is taken up from a historial point of view first; then after the main body of the book, two final chapters deal especially with applications. Parts of the book might be considered elementary, but probably most would not. There is a 19-page bibliography.

Contents

1. The linear programming concept
2. Origins and influences
3. Formulating a linear programming model
4. Linear equation and inequality systems
5. The simplex method
6. Proof of the simplex algorithm and the duality theorem
7. The geometry of linear programs
8. Pivoting, vector spaces, matrices, and inverses
9. The simplex method using multipliers
10. Finiteness of the simplex method under perturbation
11. Variants of the simplex algorithm
12. The price concept in linear programming
13. Games and linear programs
14. The classical transportation problem
15. Optimal assignment and other distribution problems
16. The transshipment problem
17. Networks and the transshipment problem
18. Variables with upper bounds
19. Maximal flows in networks
20. The primal-dual method for transportation problems
21. The weighted distribution problem
22. Programs with variable coefficients
23. A decomposition principle for linear programs
24. Convex programming
25. Uncertainty
26. Discrete variable extremum problems
27. Stigler's nutrition problem; an example of formulation and solution
28. The allocation of aircraft to routes under uncertain demand

DAVIS, P.J.: <u>Interpolation and Approximation</u>. Blaisdell (Ginn) (1963) 393 pp.

This is a fairly advanced text on the subject. After studying such a book, the student should be able to read and understand most of the modern literature on interpolation and approximation.

General Outline of Contents

1. Introduction: topics from algebra and analysis
2. Interpolation
3. Remainder theory (dealing with the question of how good the approximations are which result from interpolation)
4. Convergence theorems for interpolatory processes
5. Some problems in infinite interpolation: infinite systems of linear equations in infinitely many unknowns
6. Uniform approximation: Weierstrass' approximation theorem and generalizations; Berstein polynomials; simultaneous approximation of functions and derivatives; simultaneous interpolation and approximation
7. Best approximation: normed linear spaces, convex sets; fundamental problem of linear approximation; uniqueness of best approximation; best uniform (Tschebyscheff) approximation of continuous functions; best approximation by nonlinear families
8. Least square approximation
9. Hilbert space
10. Orthogonal polynomials (both real and complex)
11. Theory of closure and completeness
12. Expansion theorems for orthogonal functions; Fourier series; Legendre series; complex orthogonal expansions; reproducing kernel functions
13. Degree of approximation
14. Approximation of linear functionals

DORFMAN, R., SAMUELSON, P.A., and SOLOW, R. M.: Linear Programming and

Economic Analysis. McGraw-Hill (1958) 525 pp.

This book contains a reasonably elementary exposition of some of the basic concepts of linear and nonlinear programming. It is written for the economist who wishes to learn something about linear programming, so all the emphasis is on applications to this field. However, the examples can be understood by all, and it is generally a popular book.

Contents

1. Introduction

2. Basic concepts of linear programming

3. The valuation problem; market solutions

4. The algebra of linear programming

5. The transportation problem

6. Linear programming analysis of the firm

7. Application to the firm; valuation and duality

8. Nonlinear programming

9. & 10.: The statical Leontief system

11. Dynamic aspects of linear models

12. Efficient programs of capital accumulation

13. Linear programming and the theory of general equilibrium

14. Linear programming and welfare analysis

15. Elements of game theory

16. Interrelations between linear programming and game theory

Appendices: Chance, utility and game theory; the algebra of matrices

DUSINBERRE, G. M.: Heat Transfer Calculations by Finite Differences.

International Textbook Co. (1961) 293 pp

This is a reasonably elementary book which has been written primarily for engineers. The author's previous text, "Numerical Analysis of Heat Flow" (which has been out of print for some time) was used for many years as their only numerical analysis reference book by many heat engineers. This newer text is recommended for a computer programmer who wishes to learn a little more of the physical background of the heat flow problems than he has found in standard numerical analysis texts. A text written from a more modern point of view should be consulted when desiring to learn more about stability of the finite difference equations of heat flow.

Contents

1. Thermal properties

2. Fundamental equations

3. Alternative formulations

4. Analytical and analog methods

5 & 6: One-dimensional transient problems

7. Multidimensional transient problems

8. Transient flow systems

9 & 10: Steady state problems

11. Variable properties

12. Digital computers

13. Miscellaneous examples

14. Problems

DWYER, P. S.: <u>Linear Computations</u>. Wiley (1951) 344 pp.

This is a quite elementary text on linear problems and on applications
to statistics. There is no emphasis on methods for digital computers.
Large numbers of worked out examples make it a very easy book to understand.

General Outline of Contents

1-3.   Introductory material on the use of desk calculators, significant

          figure theory, and general principles of good computational

          design

4-8.   solution of simultaneous linear equations by various methods

9-10.   Evaluation of determinants

11.   Evaluation of linear forms

12-14.   Matrices; the calculation of the adjoint and of the inverse of

          a matrix

15.   The characteristic equation, its roots, and the characteristic

          vectors

16.   Other methods of solving the problems of Chapters 4-15.

17.   The errors of linear computations

18.   Applications to statistics

19.   Application to nonlinear problems

ENGELI, M., GINSBURG, T., RUTISHAUSER, H., and STIEFEL, E.: <u>Refined</u>

<u>Iterative Methods for Computation of the Solution and the Eigenvalues</u>

<u>of Self-Adjoint Boundary Value Problems.</u> Birkhäuser (1959) 107 pp.

This is a very practical description of methods of solving such
problems written by four experts in the field. In addition to describing
various methods, they often give comparisons of machine times required.
The subject matter is not elementary, but the explanations are reasonably
clear.

General Outline of Contents

1. The self-adjoint boundary value problem. Problems of Dirichlet and
    Poisson type; energy on the boundary; eigenvalue problems; bihar-
    monic problems; modes of oscillation of a plate (Stiefel)

2. Theory of gradient methods (Rutishauser)

3. Experiments on gradient methods (Ginsburg)

    a. Survey of plate experiments

    b. Plate problem with coarse grid $(A\vec{x} + \vec{b} = 0)$
        Steepest descent; Tchebyscheff method; conjugate gradient
        methods; cgT method; combined method; elimination; computation
        of residuals

    c. Determination of eigenvalues of the matrix A; conjugate gradient
        methods with subsequent QD-algorithm; cgT method with subsequent
        QD-algorithm

    d. Same problems with fine grid

    e. A bar problem

4. Overrelaxation (Engeli)

    a. Theory (general relaxation, overrelaxation, "property A," Young's
        overrelaxation; different methods)

    b. Numerical results (plate problem)

    c. Numerical results (bar problem)

5. Conclusions (comparison of results)

**FADDEEV, D. K., and FADDEEVA, V. M.: <u>Computational Methods of Linear

<u>Algebra</u>. Freeman (1963) 621 pp.

This treatise is a translation from the Russian. Many parts of the book are reasonably elementary, but some parts are of intermediate difficulty. It discusses in detail most of the methods which are used by computer people in this field. A 1959 book by the second author on the same subject was much shorter, and this larger book can now be described as the leading reference book on the subject for scientific computer users. The main difficulties are translational (as for example, when the quotient-difference algorithm is described as the division and subtraction algorithm).

General Outline of Contents

1. Basic material from linear algebra

2. Exact methods for solving systems of linear equations

3. Iterative methods for solving systems of linear equations

4. The complete eigenvalue problem (finding all eigenvalues, and eigen-vectors associated with each eigenvalue)

5. The special eigenvalue problem (finding only a few of the eigenvalues and/or corresponding eigenvectors; for example, the power method finds one eigenvalue at a time)

6. The method of minimal interactions and other methods based on the idea of orthogonalization (for solving systems of equations or for solving the complete eigenvalue problem)

7. Gradient iterative methods (for solving systems of equations or for solving the complete eigenvalue problem)

8. Iterative methods for solving the complete eigenvalue problem

9. Universal algorithms (for solving systems of linear equations)

10. Fifty-nine pages of bibliography

FADDEEVA, V. N.: <u>Computational Methods of Linear Algebra</u>. Dover (1959)

  252 pp.

    This is a reasonably elementary book on matrices from the point of
view of computing. It is a translation from the Russian, and it dis-
cusses a majority of the methods which are used by computer people in
this field. The translator has used the terms "proper number" and "proper
vector" rather than the more common eigenvalue, eigenvector; or charac-
teristic number, characteristic value; or latent root, latent vector. The
much larger book by Faddeev and Faddeeva on the same subject (published
in 1963) is greatly to be preferred.

                    General Outline of Contents

1. Basic material about matrices

2. Systems of linear equations: Gauss' method; square-root method;

    inversion of matrices; partitioning methods; bordering method; esca-

    lator method; iteration methods (Seidel method); etc.

3. Proper numbers and proper vectors of a matrix (eigenvalues and eigen-

    vectors): methods of Krylov, Samuelson, Danilevsky, Leverrier,

    Faddeev; the escalator method; interpolation methods; determining the

    "first" proper number; finding proper numbers next in line

**FLETCHER, A., MILLER, J., and ROSENHEAD, L.: <u>An Index of Mathematical</u>

<u>Tables</u>, 2nd ed., two vols. Addison-Wesley (1962) 994 pp.

These volumes comprise an annotated bibliography of mathematical
tables which are available in various books and periodicals. From a
practical point of view, it can be considered as "complete," although such
a stupendous effort could never hope to be complete in any strict sense
of the work. In most cases the two volumes will be used together. A
particular table may be looked up in Volume 1, which gives the author's
name; then the actual reference may be found in the author index of Volume 2.

Contents

Volume 1.   Introduction (telling how the indexes are constructed)

    Part 1.   Index according to functions (and giving the author)

Volume 2.

    Part 2.   Bibliography (listed by author and giving the literature
             reference)

    Part 3.   Errors (which have been found in various tables)

    Part 4.   Index to Volume 1 (by author)

FORSYTHE, G. E. and ROSENBLOOM, P. C.: <u>Numerical Analysis and Partial</u>

<u>Differential Equations</u>. Wiley (1958) 204 pp.

These are survey articles which attempt in a broad manner to discuss the present state of knowledge (1958) in the two fields of the title. Each survey has an excellent bibliography attached. Since Rosenbloom's article on Linear Partial Differential Equations deals with theoretical aspects of the problems (no numerical methods are discussed), only Forsythe's article will be indexed here. Forsythe's article, entitled "Contemporary State of Numerical Analysis," is written for nonspecialists, and in a reasonably elementary manner. It tells about what is being done and it gives references, but it does not go into many details.

Paragraph Headings

1. What is numerical analysis? (4 pp.)

2. Areas of numerical analysis (1 p.)

3. An older Soviet view of numerical analysis (2 pp.)

4. A more recent Soviet view of numerical analysis (1 p.)

5. Automatic digital computers (3 pp.)

6. Two Soviet computers (1 p.)

7. Literature on numerical analysis (1 p.)

8. Numerical integration and interpolation (2 p.)

9. Approximations of functions (3 pp.)

10. Solving linear algebraic equations (6 pp.)

11. Solving matrix eigenvalue problems (4 pp.)

12. Difference methods for Laplace's equation (7 pp.)

Bibliography (5 pp.)

**FORSYTHE, G. E. and WASOW, W. R.: <u>Finite Difference Methods for</u>

<u>Partial Differential Equations.</u> Wiley (1960) 444 pp.

This book is generally quite advanced, although introductions to
various of the topics are given in quite elementary language. The
subject is developed from the point of view of the analyst who wishes
to "solve" partial differential equations on digital computers. At
the end is an excellent bibliography with references up to 1959.

Contents

Introduction to partial differential equations and computers

1. Hyperbolic equations in two independent variables (finite difference
   methods for (a) wave equation, (b) systems of equations, (c) quasi-
   linear equations; integration along characteristics; integration by
   Adams' method; shock waves)

2. Parabolic equations (simplest heat flow problems; linear problems
   in one and in two variables; convergence and stability; nonlinear
   problems)

3. Elliptic equations (problems from physics and engineering; varia-
   tional formulations; interface conditions; maximum principle;
   formulating elliptic difference equation problems; classical theory
   of solving elliptic difference equations; explicit and implicit
   overrelaxation methods; discretization and round-off errors; membrane
   eigenvalue problem; solving elliptic equations on an automatic
   digital computer)

4. Initial-value problems in more than two independent variables (the
   equation of wave propagation; characteristics in several dimensions;
   a meteorological forecast problem; Fourier method for difference
   and differential equations; method of Peaceman and Rachford)

FORT, T.: Finite Difference and Difference Equations in the Real Domain.

Oxford (1948) 251 pp.

This book is rather advanced, but probably most will find it easier to read than Milne-Thompson. A little more than half the book is on the topic of difference equations.

Contents

1. Direct difference operators

2. Elementary theory of summation

3. The Bernoulli and Euler polynomials and numbers

4. Summation formulas

5. Stirling's numbers and numerical differentiation

6. Interpolation and mechanical quadrature

7. The elementary theory of the linear recurrent relation

8. Maxima and minima of finite sums

9. The general boundary problem

10. Sturm-Liouville theory

11. The solution of a differential equation as the limit of the solution of a difference equation

12. The weighted vibrating string and its limit

13. The linear recurrent relation of the first order with periodic coefficients

14. The linear recurrent relation of the second order with periodic coefficients

15. Orthogonal sets and the development of an arbitrary function

16. Oscillatory and nonoscillatory linear difference equations of the second order

17. The linear difference equation in a continuous real independent variable

FOX, A.H.: <u>Fundamentals of Numerical Analysis</u>. Ronald Press (1963) 147 pp.

This standard short elementary text is really shorter than one would expect a 147-page book to be, because for some reason the author includes a 37-page table of squares of integers.

Contents

1. Introduction (concerning errors)
2. Systems of linear algebraic equations
3. Nonlinear equations
4. Polynomial equations
5. Numerical integration
6. Ordinary differential equations
7. Partial differential equations
8. Integral equations

Table of squares of integers 1000-9999

FOX, L.: <u>An Introduction to Numerical Linear Algebra</u>. Oxford (1965) 327 pp.

This fairly elementary text is a very good place for a computer user to look up various methods of solving systems of equations and of obtaining matrix eigenvalues and eigenvectors (which Fox calls latent roots and latent vectors). In addition to explaining the various methods, the author presents quite a few worked examples.

General Outline of Contents

1. Introduction (including a discussion of the use of computing machines)

2. Matrix algebra (theory)

3. Elimination methods of Gauss, Jordan, and Aitken

4. Compact elimination methods of Doolittle, Crout, Banachiewicz, and Cholesky

5. Orthogonalization methods

6. Condition, accuracy, and precision

7. Comparison of methods; measure of work

8. Iterative and gradient methods

9. Iterative methods for latent roots and vectors

10. Transformation methods for latent roots and vectors

11. Notes on error analysis for latent roots and vectors

**FOX, L.: <u>Numerical Solution of Two-Point Boundary Problems</u>. Oxford

(1957) 371 pp.

This is a reasonably elementary exposition of the subject of ordinary differential equations with two-point boundary conditions. However, some parts are quite advanced. The explanations are particularly clear. Digital computer methods are not stressed.

Partial List of Contents

1. The solution of algebraic equations which arise when solving differential equations numerically. Emphasis is on relaxation methods

2. Second order equations (various types of boundary conditions)

3. First order equations (applying boundary value techniques to problems which are essentially initial value problems)

4. Third and fourth order equations

5. Eigenvalue problems (including discussion of various differential equation eigenvalue problems as well as methods of solving the corresponding matrix eigenvalue problems)

6. Initial value techniques for boundary value problems

7. Accuracy and precision of boundary value methods

8. Miscellaneous methods: simultaneous differential systems; equations with discontinuous coefficients; deferred approach to a limit; nonlinear eigenvalue problems; semi-analytic methods (collation, least squares, Galerkin)

FOX, L. (Ed.): <u>Numerical Solution of Ordinary and Partial Differential</u>

<u>Equations</u>. Pergamon Press (1962) 509 pp.

This book contains a reasonably elementary introduction to the study of the numerical solution of ordinary differential equations, integral equations, and partial differential equations. In addition, there are discussions of many quite complicated practical problems and how to solve them numerically; thus for the computer user who complains that textbooks never consider problems as difficult as those he is faced with, this book should be an answer. Of course, in a book such as this which has many authors, the various sections are not uniformly good.

General Outline of Contents

1. Ordinary differential equations (initial value problems; boundary value problems; eigenvalue problems; Chebyshev solutions)

2. Integral equations (Fredholm equations of 1st, 2nd, and 3rd types; Volterra type equations; singular equations; integro-differential equations; Hartree-Fock equation)

3. Introduction to partial differential equations (hyperbolic, parabolic, and elliptic equations in two dimensions)

4. Practical problems in partial differential equations (nuclear reactor problems; one-dimensional unsteady flow; characteristics in 3 dimensions; quasi-linear parabolic equations in more than 2 dimensions; linear transport equation in 1 and 2 dimensions; Monte Carlo methods for neutronics problems; plasma physics problems; numerical weather prediction.

FRAZER, R. A., DUNCAN, W. J., and COLLAR, A. R.: Elementary Matrices.

Cambridge (1938) 416 pp.

This reasonably elementary book has probably been the most popular book on the subject among scientific computer users. More advanced topics are marked with asterisks and these paragraphs may be omitted by the beginner in the field. In the latter part of the book are many applications to problems in dynamics and particularly aerodynamics.

Contents

1. Funadmental definitions and elementary properties

2. Powers of matrices, series, and infinitesimal calculus

3. Lambda-matrices and canonical forms

4. Miscallaneous numerical methods: solving systems of equations; inverting matrices; finding latent roots and vectors (eigenvalues and eigenvectors)

5. & 6.: Linear ordinary differential equations with constant coefficients (systems of equations, boundary value problems, etc.)

7. Numerical solutions of linear ordinary differential equations with variable coefficients

8. Kinematics and dynamics of systems

9. Systems with linear dynamical equations

10. Iterative numerical solutions of linear dynamical problems

11. Dynamical systems with solid friction

12. Illustrative applications of friction theory to flutter problems

13. Pitching oscillations of a frictionally constrained aerofoil

FREIBERGER, W. and PRAGER, W. (Ed.): <u>Applications of Digital Computers</u>.

Ginn (1963) 244 pp.

This consists of a set of lectures given in 1961-62 at Brown University on the occasion of establishment of the Brown University Computing Laboratory by 16 well-known authors. Most of these lectures are quite general in nature. The book can be recommended to one who wishes he might have attended such a series of lectures or by one who wishes to get some general ideas of the problems of one of the specific fields discussed.

Contents

1. Computers and operations research (Morse)

2. How computers can learn from experience (Simon)

3. Recent developments in the science of diagnosis (Woodbury and Lipkin)

4. Recent trends in computer programming and numerical analysis (Carr)

5. Using computers to solve problems in physics (Thomas)

6. Computers and brains (Rosenblith)

7. Sorting on computers (Gotlieb)

8. The role of computers in astronomy (Davis)

9. Computers in fluid mechanics (Giese)

10. The use of digital computers in civil engineering (Massonnet)

11. Information theory and numerical analysis (Hamming)

12. Educational implications of the computer revolution (Forsythe)

13. The analysis and design of experiments with the help of computers (Hartley)

14. Automatic data processing in the legal profession (Kehl)

15. Automation and pure mathematics (Lehmer)

**FRÖBERG, CARL-ERIK: <u>Introduction to Numerical Analysis</u>. Addison-Wesley (1965) 340 pp.

This is a translation of a Swedish text published in 1962. It is suitable for a first (undergraduate or graduate) course in numerical analysis. This is not just a rehash of methods described in numerical analysis texts of earlier times, but some of the more useful of the newer advances on elementary topics are also considered. Although it may have lost something in its translation, it is still highly recommended. (One can remember, for example, when he is reading about matrices that "regular" means "non-singular," and "quadratic" means "square"). A glance at the contents will suggest, however, that it is not possible to have such a large list of topics covered in as great detail as one might wish if he were to use this only as a reference work.

Contents

1. Numerical computations (representation of numbers, errors, etc.)
2. Equations (methods of finding the roots of equations)
3. Matrices
4. Linear systems of equations
5. Matrix inversion
6. Algebraic eigenvalue problems
7. Linear operators
8. Interpolation
9. Numerical differentiation
10. Numerical quadrature
11. Summation
12. Multiple integrals
13. Difference equations
14. Ordinary differential equations
15. Partial differential equations
16. Approximation (least square, trigonometric, exponential, Chebyshev, continued fraction, rational)
17. The Monte Carlo method
18. Linear programming

GARABEDIAN, H. L. (Ed.): <u>Approximation of Functions</u>. Elsevier (1965) 220 pp.

This book contains papers presented at a symposium on the subject in 1964. Almost all are of an advanced nature. The paper by Davis consists mainly of an excellent bibliography compiled in the summer of 1964. Lorentz's paper discusses the Russian literature.

Contents

1. The convergence of sequences of rational functions of best approximation with some free poles (Walsh)
2. Uses of Hilbert space in approximation (Sard)
3. Applications of duality in approximation theory (Buck)
4. Inclusion theorems for the minimal distance in rational Tschebyscheff approximation with several variables (Collatz)
5. Rational approximation on finite point sets (Fox, Goldstein, and Lastman)
6. Phase methods for polynomial approximation (Stiefel)
7. Optimal and nearly-optimal linear approximation (Golomb)
8. Approximation by generalized rational functions (Cheney)
9. Nonlinear approximation (Rice)
10. Nonlinear sequence transformations (Bauer)
11. Approximation theory in the first two decades of electronic computers (Davis)
12. Piecewise polynomial interpolation and approximation (Birkhoff and de Boor)
13. Russian literature on approximation in 1958-1964 (Lorentz)

GARVIN, W. W.:   Introduction to Linear Programming.   McGraw-Hill (1960)

281 pp.

This is a reasonably elementary introduction to the subject.   There are a great many examples given, and the computational procedures which can be used on a digital computer are emphasized.   The author has made a special effort to use only very simple mathematics.

Contents

1. The general linear programming problem

2. The simplex method

3. The computational procedure

4. Sensitivity analysis

5. - 10.: Practical problems

11. Upper bounds

12. Statistical linear programming

13. Revised simplex method

14. Resolution of degeneracy

15. Parametric linear programming

16. A simple economic problem

17. Duality

18. The warehouse problem

GODUNOV, S. K. and RYABENKI, V. S.:   <u>Theory of Difference Schemes</u>.   North

  Holland Publ. Co. (1964) 289 pp.

    This quite advanced text is a translation from the Russian. Although
there is some more general introductory material, the main subject of
the book is the theory of difference schemes for partial differential
equations. There are many more examples given than in most other books
at this level. There is no index.

Contents

1. Elementary examples of difference schemes of first and second order
2. Approximations and stability (difference schemes for ordinary differ-
    ential equations)
3. Concepts of an approximation and stability for difference schemes for
    partial differential equations
4. On the solution of difference equations
5. Stability as the boundedness of the powers of a certain operator
6. Elements of the spectral theory of difference operators

Appendix I.   On difference schemes for the solution of the equation of
    thermal conductivity (Gelfond and Lokutsievski)
Appendix II.   The double sweep method for solution of difference equations
    (Gelfond and Lokutsievski)
Appendix III. The scope of the energy method (Lax)
Appendix IV.   On the estimate of the amount of computational labor
    necessary in approximate solutions (Bakhvalov)
Appendix V.   Difference schemes for parabolic equations and continuous
    integrals (Krylov)

GOULD, S. H.: <u>Variational Methods for Eigenvalue Problems.</u>   University

of Toronto Press (1957) 179 pp.

This is a fairly advanced book. It employs calculus of variations
methods to find bounds for eigenvalues. The theoretical engineering as-
pects of the subject are stressed, but computational methods are also
discussed (as the author states, "variational methods are particularly
well adapted to successive approximation").

Contents

1.   Systems vibrating with a finite number of degrees of freedom

2.   Variational principles for finite-dimensional systems

3.   Vibration of systems with infinitely many degrees of freedom

4.   Reproducing kernels and functional completion

5.   Vibrating rods, membranes, and plates

6.   The Weinstein method in its original form

7.   Linear operators in a Hilbert space

8.   The Weinstein-Aronszajn method for linear operators in Hilbert space

9.   Application of the preceding method to the differential problem of
     the vibrating plate

10. Application of the approximate methods to general differential problems

GRABBE, E. M., RAMO, S., and WOOLDRIDGE, D. E. (Ed.): <u>Handbook of</u>

<u>Automation, Computers, and Control</u>, Vol. 1. Wiley (1958)

This is one of a three-volume set to be used mainly as a reference
work. The various chapters have different authors. Many of the topics
at the first of the book are elementary, but often the discussions are
so sketchy that the beginner might have trouble learning about the subject
here. In the last half of the book the topics are covered in much greater
detail. It is written with computer people in mind, and it is certainly
a good ready reference for computer users on a variety of related subjects.
Adequate references are listed at the end of each chapter.

Contents

1. General mathematics (212 pp.): sets; algebraic equations; matrix
   theory; finite difference equations; differential equations; integral
   equations; complex variables; operational mathematics; Laplace trans-
   forms; conformal mapping; Boolean algebra; probability; statistics.
2. Numerical analysis (88 pp.): interpolation, curve fitting, differ-
   entiation, and integration; matrix inversion and simultaneous equations;
   eigenvalues and eigenvectors; digital techniques in statistical
   analysis of experiments; ordinary differential equations; partial dif-
   ferential equations
3. Operations research (124 pp.)
4. Information theory and transmission (108 pp.)
5. Feedback control (420 pp.)

GRAM, C. (Ed.): Selected Numerical Methods for Linear Equations, Poly-

nomial Equations, Partial Differential Equations, and Conformal

Mapping. Regnecentralen, Copenhagen (1962) 308 pp.

This collection of papers was prepared by a study group organized at the Danish Institute of Computing Machinery to investigate numerical methods in the areas indicated by the title. The purpose was to evaluate and compare various numerical methods. This has not been done in a complete manner at all (except for the conformal mapping work), but it is interesting to read of the results they did obtain. ALGOL programs are given in some cases. On pages 106-113 there is a nice summary of technical terms and key for classification of partial differential equation problems.

General Outline of Contents

1. Linear equations (Anderson and Krarup)
2. Partial differential equations (Gram, Naur, Poulsen)
    a. Linear elliptic equations of second order
        Dirichlet problem and other boundary value problems
        Eigenvalue problems
    b. The heat equation
        One-, two-, and three-dimensional problems
        Parabolic nonlinear equations
    c. Hyperbolic equations
        The wave equation and other second order equations of two independent variables
        Systems of first order equations with two or more independent variables
3. Conformal mapping (Anderson, Christiansen, Møller, and Tornehave)
    General theory; integral equation methods; application of the Lichtenstein-Gershgorin integral equation; conformal mapping of nearby circular regions onto the unit disc using expansions in powers of a "small parameter"
4. Polynomial equations (Busk and Svejgaard)

GRAVES, R. L. and WOLFE, P. (Ed.): Recent Advances in Mathematical

Programming. McGraw-Hill (1963) 347 pp.

The generally advanced papers which make up this book were presented
at a symposium on the subject in June, 1962. The first nine papers deal
with general theory; the next four deal with nonlinear programming; the
next five deal with stochastic programming. Papers 19 through 22 deal with
computational procedures for very large linear programming problems; the
next four concern themselves with detailed computational variations of the
simplex method for linear programs. Papers 27 through 33 are concerned
with applications; the next four papers deal with integer programming; the
last six papers are concerned with network flow problems.

Contents

Combinatorial theory underlying linear programs. A mutual primal-dual
simplex method. On cone functions. The maximum transform (abstract only).
Representations for the generalized inverse of matrices partitioned as
$A = [U,V]$ (abstract only). On unimodular sets of vectors. Dual programs.
Symmetric dual quadratic programs (abstract only). Orthogonality, duality,
and quadratic type problems in mathematical programming (abstract only).
Methods of nonlinear programming. On the gradient projection methods of
R. Frisch and J. B. Rosen (abstract only). The simplex method for local
separable programming. Minimization of indefinite quadratic functions with
linear constraints (abstract only). Linear programming under uncertainty.
A primal-dual algorithm for convex programming (abstract only). Characteri-
zations by chance-constrained programming. Programming with standard er-
rors in the constraints and the objective (abstract only). Inequalities
for stochastic nonlinear programming problems (abstract only). Compact
basis triangularization for the simplex method. The simplex method using
pseudo-basic variables for structured linear programming problems. Dual
and parametric methods in decomposition. Convex partition programming.
Experiments in linear programming. Parametric linear programming. Com-
putational efficiency in product form LP codes. Some new algorithms for
linear programming (abstract only). A formula for ranging the cost of
living (abstract only). A stochastic model for programming the supply of
a strategic material. Mathematical programming applied to short-term
scheduling of interconnected hydro-thermal electric power systems (abstract
only). An application of linear programming to the fairing of ships' lines.
The simulation of multi-component distillation. Optimal capacity scheduling
(abstract only). The personnel assignment problem (abstract only). An
algorithm for integer solutions to linear programs. Integer quadratic pro-
gramming. On diagonalization methods in integer programming (abstract only).
An accelerated Euclidean algorithm for integer linear programming. Flows
in networks. Multi-commodity network flows (abstract only). Transportation
problems with distributed loads (abstract only). Least cost estimating
and scheduling with limited resources (abstract only). Mathematical pro-
gramming solution of traveling salesman examples (abstract only). Network
algorithms for combinatorial and discrete variable optimization problems
(abstract only).

GREENSPAN, D.: Introductory Numerical Analysis of Elliptic Boundary

Value Problems. Harper and Row (1965) 164 pp.

This book could possibly be used as one of a series of specialized texts for a second year course in numerical analysis. The "lemma-proof, theorem-proof,..." method of exposition of thoretical parts of the subject may annoy the nonmathematician, but there are also many numerical examples which the scientific computer user might be glad to see. There is a 24-page bibliography.

Outline of Contents

1. Analytical preliminaries

2. The Dirichlet problem for the two-dimensional Laplace equation

3. The mixed problem for the two-dimensional Laplace equation

4. Dirichlet and mixed problems for more general two-dimensional linear elliptic equations

5. Three-dimensional problems with axial symmetry

6. Linear elliptic problems in three and more dimensions

7. Nonlinear problems

GRINTNER, L. E. (Ed.): <u>Numerical Methods of Analysis in Engineering</u>.

Macmillan (1949) 207 pp.

This book consists of a series of papers by well known practicing engineers on numerical methods which they use on practical (usually quite difficult) problems. The emphasis is on methods which depend somewhat on knowledge of the physical problem. Examples in the fields of heat flow and strength of materials are many.

Contents

1. Numerical methods based upon physical concepts

   a. Analysis of continuous frames by distributing fixed-end moments (Hardy Cross)

   b. Statistical state of stress studied by grid analysis (Grintner)

2. Numerical solutions of equations for state of stress

   c. Numerical solutions of boundary value problems by relaxation methods (Shaw)

   d. The quest for accuracy in computations using finite differences (Southwell)

   e. The new approach to the numerical solution of Laplace's equation (Frocht)

3. Applications of numerical methods to heat transfer

   f. Numerical solutions for thermal systems (Boeltner and Tribus)

   g. Two problems in building heating solved numerically (Dusinberre)

4. Surveys and bibliographies of numerical methods

   h. Successive corrections - a pattern of thought (Baron)

   i. Numerical methods of analysis of bars, plates, and elastic bodies (Newmark)

   j. A survey of the approximate solution of two-dimensional physical problems by variational methods and finite difference procedures (Higgins)

GRUENBERGER, F. and JAFFRAY, G.: <u>Problems for Computer Solution</u>.

   Wiley (1965) 401 pp.

     This paperback textbook contains 92 problems of varying difficulties
for possible computer solution. It is assumed that the reader has a
little basic knowledge of how to use a computer and is now ready to try
to place some simple problems on it. In a scientific computing center,
this book might be used in the introductory programming course as a source
for student problems.

     In most cases, a topic is introduced by a brief statement of a
problem, followed by some suggestions as to how to proceed. There are
quite a few flow charts, but complete FORTRAN programs are not given; the
reader is supposed to furnish these!

GUEST, P.G.: <u>Numerical Methods of Curve Fitting</u>. Cambridge (1961) 422 pp.

This quite elementary text is a sort of cross between a statistics book and a numerical methods book. It is written from the point of view of one who will be using desk calculators or no calculator at all.

General Outline of Contents

Single Variables:

1. General theory (probability and frequency; expectation and variance; estimation; weights; moments and cumulants)

2. The normal distribution

3. Some statistical tests

4. Discrete distributions (binomial, Poisson)

Regression Theory and the Straight Line

5. Regression curves and functional relationship

6. The straight line

Polynomials and Other Curves

7. Estimation of the polynomial coefficients

8. Standard deviations of the estimates

9. The grouping of observations

10. Functions which are not polynomials (linear functions; nonlinear functions; harmonic analysis; smoothing)

11. General regression and functional relationship problems in several variables

12. Further illustrative examples (various practical problems)

HADLEY, G. F.: <u>Linear Programming</u>. Addison-Wesley (1962) 520 pp.

HADLEY, G. F.: <u>Nonlinear and Dynamic Programming</u>. Addison-Wesley (1964) 484 pp.

These quite advanced texts are very popular amongst those who work regularly in these fields. The nonlinear programming book is a sequel to the other and assumes the reader is familiar with the earlier material.

Chapter Subjects in First Book

1. Introduction
2. Mathematical background
3 - 5: Simplex method
6. Resolution of the degeneracy problem
7. The revised simplex method
8. Duality theory and its ramifications
9. Transportation problems
10. Network flows
11. Special topics
12. Applications of linear programming to industrial problems
13. Applications of linear programming to economic theory

Chapter Subjects in Second Book

1. Introduction
2. Mathematical background
3. Classical optimization methods and properties of convex functions
4. Approximate methods for solving problems involving separable functions
5. Stochastic problems
6. Kuhn-Tucker theory
7. Quadratic programming
8. Integer linear programming
9. Gradient methods
10. & 11.: Dynamic programming

HAMMERSLEY, J. M. and HANDSCOMB, D. C.: <u>Monte Carlo Methods</u>. Wiley

(1964) 178 pp.

This is quite an advanced book. Direct simulations are discussed
in one chapter; but true Monte Carlo techniques are emphasized (in which,
for example, valid results may be obtained with less computation by
means of various variance reducing techniques). Both the theory and some
applications to specific problems are presented.

Contents

1. The general nature of Monte Carlo methods

2. Short resumé of statistical terms.

3. Random, pseudorandom, and quasirandom numbers

4. Direct simulation

5. General principles of the Monte Carlo method

6. Conditioned Monte Carlo

7. Solution of linear operator equations

8. Radiation shielding and reactor criticality

9. Problems in statistical mechanics

10. Long polymer molecules

11. Percolation processes

12. Multivariate problems

**HAMMING, R. W.: <u>Numerical Methods for Scientists and Engineers</u>. McGraw-Hill (1962) 411 pp.

Many senior or first year graduate numerical analysis texts look almost as if they might have been written starting from the same rough notes. It is not true of this book; the author's explanations and subject emphasis are sometimes quite novel. For a person who wishes to review an introductory numerical analysis course he had previously, this book might make the job much more interesting·than rereading the original text. The author has written the book with the idea in mind that the reader would be using digital computers to solve his practical numerical problems.

Contents

1. The difference calculus
2. Roundoff noise
3. The summation calculus
4. Evaluation of infinite series
5. Finite difference equations
6. The finite Fourier series
7. - 9.: Polynomial approximation introduction
10. A uniform method for finding formulas
11. On finding the error term of a formula
12. Formulas for definite integrals
13. Indefinite integrals
14. Introduction to differential equations
15. A general theory of predictor-corrector methods
16. Special methods of integrating ordinary differential equations
17. & 18.: Least squares theory and practice
19. Chebyshev polynomials
20. Rational functions
21. & 22.: Periodic functions - Fourier series
23. Nonperiodic functions - the Fourier integral
24. Linear filters - smoothing and differentiating
25. Integrals and differential equations
26. Exponential approximation
27. Singularities
28. On finding zeros
29. Simultaneous linear algebraic equations
30. Inversion of matrices and eigenvalues
31. Some examples of the simulation of situations and processes
32. Random numbers and Monte Carlo methods

Chapter N+1: The art of computing for scientists and engineers

HARRIS, L. D.: Numerical Methods Using FORTRAN. Merrill (1964) 244 pp.

   This very elementary book has been written by an Electrical Engineer.
A person with a quite limited mathematical background should have little
trouble understanding what is said about the various topics, but in many
cases he may easily obtain some wrong ideas because of what has not been
said. Only FORTRAN II is described in most parts of the book, although
one paragraph in Appendix I tells something of FORTRAN IV.

                    General Outline of the Contents

1. Solving numerical problems on the digital computer (very short des-
    cription of a computer)

2. The program (mainly an introductory discussion of the FORTRAN language).

3. Iteration in the program - subscripted variables and the DO statement.

4. Interpolation

5. Subdividing the program (subroutines and CALL statements)

6. Differentiation and integration

7. Numerical solution of ordinary differential equations

8. Finding the roots of an equation

9. Solutions of simultaneous linear equations

10. Appendices give more information about FORTRAN

HARTREE, D. R.: <u>Calculating Instruments and Machines</u>. University of

Illinois Press (1949) 138 pp.

This rather elementary book consists essentially of a set of lectures given in 1948 at the University of Illinois. The discussion is mainly about the machines, but scattered throughout are discussions of various types of problems to be placed on the machines. Any user of a digital (or of an analogue computer) should have some idea how problems similar to his might be solved on the other type of computer.

Contents

1. Introduction

2. The differential analyser

3. The differential analyser and partial differential equations

4. Some other instruments: solution of simultaneous linear algebraic equations, the isograph, Fourier synthesizers, integrating instruments, directors

5. Large automatic digital machines

6. Charles Babbage and the analytical engine

7. Historical development

8. Projects and prospects

9. High speed automatic digital machines and numerical analysis: iterative methods, simultaneous algebraic equations, ordinary differential equations with one-point boundary conditions, ordinary differential equations with two-point boundary conditions, partial differential equations

HARTREE, D. R.: <u>Numerical Analysis</u>, 2nd ed. Oxford (1958) 283 pp.

      This reasonably elementary text is carefully written. The author points the discussion more toward the desk calculator user than toward the digital computer user, but a final chapter has been included entitled "Organization of Calculations for an Automatic Machine."

Contents

1. Introduction
2. Tools of numerical work and how to use them (desk machines, tables, slide rule, graph paper, etc.)
3. Evaluation of formulas (difficulties which may arise and how to avoid them)
4. Finite differences
5. Interpolation
6. Integration (quadrature) and differentiation
7. Integration of ordinary differential equations
8. Simultaneous linear algebraic equations and matrices
9. Nonlinear algebraic equations
10. Functions of two or more variables (complex numbers, Laplacian operator; elliptic, parabolic, and hyperbolic partial differential equations)
11. Miscellaneous processes (summation of series, harmonic analysis, smoothing, etc.)
12. Organization of calculations for an automatic machine

HASTINGS, C.: <u>Approximations for Digital Computers</u>.   Princeton Univ.

Press (1955) 201 pp.

This is a reasonably elementary description of the subject of ap-
proximating various functions by functions which are relatively easy to
evaluate on digital computers. He deals with "best approximations" in
the sense of Chebyshev. Part 1 tells something about "how" the approxi-
mations listed in Part 2 were derived. Part 2 contains approximation
formulas for 23 functions which one might wish to evaluate in computer
problems (for example, arcsin x or

$$\frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} \, dt, \text{ etc.})$$

Contents of Part 1

1.   Concerning best fit

2.   Linear weights

3.   An iterative procedure

4.   Solution of equations

5.   Chebyshev polynomials

6.   Concerning weights

7.   Function with a peak

8.   Rates of convergence

9.   Choice of form

10.   A scoring-camera problem

**HENRICI, P.: Discrete Variable Methods in Ordinary Differential

Equations. Wiley (1962) 407 pp.

This book and its sequel, "Error Propagation for Difference
Methods," have become the most popular references on the theory of
the numerical solution of ordinary differential equations. The ex-
position is clear, and the subject matter could probably be considered
as of intermediate difficulty.

General Outline of Contents

Part 1. One-step methods for initial value problems

1. Euler's method for a single equation of first order

2. General methods for a single equation of first order

3. General methods for systems of equations of first order

4. Methods for systems of equations of higher order

Part 2. Multistep methods for initial value problems

1. Methods for equations of the first order

2. Methods for special equations of second order

Part 3. Boundary value problems

(Direct methods for a class of nonlinear boundary value problems

of second order)

**HENRICI, P.: <u>Elements of Numerical Analysis</u>. Wiley (1964) 328 pp.

This reasonably elementary text is written clearly and from a modern point of view. It should turn out to be a very popular introductory numerical analysis college text.

Contents

HENRICI, P.: Error Propagation for Difference Methods. Wiley (1963) 73 pp.

    This very well written book is of intermediate difficulty. It is a
sequel and companion volume to Henrici's book, "Discrete Variable Methods
in Ordinary Differential Equations." Here he extends the theory for
multi-step methods to the case of systems of equations. Specific formulas
with particular coefficients are not given; rather he discusses general
types of methods and their convergence and stability properties.

<div align="center">Contents</div>

1. & 2.: Introduction, definitions, and notations; definition of the class
    of systems of ordinary differential equations which are to be studied

3.   Stability, consistency, and convergence; necessary and sufficient con-
    ditions for convergence of a multi-step method

4.   Asymptotic behavior of discretization error; formulas for the error

5.   Asymptotic behavior of the round-off error; primary and secondary error;
    statistical analysis of errors

Appendix: Application to a simple linear problem and a simple nonlinear
    problem (both of these problems of circular motion have the same exact
    solution)

HERGET, P.: <u>The Computation of Orbits</u>. Published by Author (Cincinnati

Observatory) (1948; 2nd printing 1962) 177 pp.

This is a very readable text written by an outstanding authority
on the topic. Although only desk calculators are assumed, the author
has carried out so many extremely lengthy calculations on desk computers
that his methods usually turn out well on digital computers also. Thus
the book seems more modern than the 1948 publishing date would indicate.

General Outline of Contents

1. The problem and methods of orbit computation; numerical methods
   and practice
2. The calculus of finite differences
3. Problems in spherical astronomy. Precession; topocentric corrections
   and parallax; planetary aberration
4. The problem of two bodies. Integration of the equations of motion;
   vectorial methods; Kepler's laws; elements; position in the orbit,
   Kepler's equation; nearly parabolic orbits; Lambert's theorem
5. The method of Laplace. Solution by series; practical methods; deri-
   vation of elements and constants for the equator.
6. Methods of Gauss and Olbers. Circular orbits; triangle and sector-
   triangle ratios; Gibbs' formulas; solution for one or two geocentric
   distances; ephemeris computation; Lambert's equation; parabolic motion;
   Olbers' method; conditioned orbit
7. Improvement of the orbit. Fundamental equations; correction of position
   and velocity vectors; closed forms for df and dg; parabolic and
   conditioned solutions; correction of elements; least squares.
8. Special perturbations. Cowell's method; preliminary satellite orbit;
   approximate perturbations in the elements; ephemerides
9. Hansen's method of general perturbations. Series developments for re-
   ciprocals of mutual distances; harmonic analysis; multiplication of
   series; use of stencils; Besselian transformations; integration of
   T series; secular terms; constants of integration
10. Tables

HERRIOT, J. G.: Methods of Mathematical Analysis and Computation. Wiley

(1963) 198 pp.

This quite elementary text is supposed to be written especially for
structures engineers. However, there are almost no practical applications
cited; it is a mathematics and numerical analysis book with a choice of
topics which the author thinks should be of importance to engineers. It
should be quite useful for self-study.

General Outline of Contents

1. Interpolation

2. Numerical differentiation and integration

3. Roots of equations

4. Simultaneous linear equations and matrices

   (This 60-page chapter starts from scratch in discussing linear equations,

   vectors, and matrices; numerical methods of solving systems of equations

   and of obtaining eigenvalues and eigenvectors are emphasized)

5. Solution of ordinary differential equations

   (Theory of ordinary differential equations; Green's functions; numerical

   solution of ordinary differential equations)

6. Fourier series

   (Theory; applications to heat problems and to a rectangular plate

   problem)

7. Numerical solutions of partial differential equations

HILDEBRAND, F. B.: <u>Introduction to Numerical Analysis</u>. McGraw-Hill

(1956) 511 pp.

This reasonably elementary book is a popular text for first courses
in numerical analysis. It has a good bibliography as an appendix.

Contents

1. Introduction (significant figures, random errors, error bounds, etc.)

2. Interpolation with divided differences

3. Lagrangian methods

4. Finite-difference interpolation

5. Operations with finite differences

6. Numerical solution of ordinary differential equations

7. Least-squares polynomial approximation

8. Gaussian quadrature and related topics

9. Approximations of various types

10. Numerical solution of equations

Appendix: Justification of the Crout reduction

HOHN, F. E.:   Applied Boolean Algebra, an Elementary Introduction.

Macmillan (1960) 139 pp.

This is a reasonably elementary book written from the point of view
of applications to digital computer design. This (single) book on Boolean
algebra is included in the listing of '..'s in this docum..nt because com-
puter people often ask for a book on applied Boolean algebra and often
express disappointment in the somewhat more abstract volumes, of which
there are many. The book includes no index, but the table of contents is
very complete.

Contents

Introduction (definitions, basic identities, etc.)

1.   Boolean algebra as a model of combinational relay circuitry

2.   Boolean algebra as a model of propositional logic

3.   The Boolean algebra of the subsets of a set

4.   The minimization problem

Appendix 1.   The binary system of numeration (including binary-to-
     decimal and decimal-to-binary conversion)

Appendix 2.   Semiconductor logic elements

HOUSEHOLDER, A. S.: <u>Principles of Numerical Analysis</u>. McGraw-Hill

(1953) 274 pp.

This book is quite advanced. The author is particularly interested in numerical analysis as applied to problems solved on digital computers. Most people find the book hard reading, but it is considered a good reference book by numerical analysts.

General Outline of Contents

1. Discussion of various types of errors and of error analyses
2. Matrices and linear equations
3. Nonlinear equations and systems of equations
4. The proper values and vectors of a matrix (eigenvalues and eigen-vectors)
5. Polynomial, trigonometric, and exponential interpolation
6. More general methods of approximation (finite linear methods, Chebyshev expansions, etc.)
7. Numerical integration and differentiation
8. The Monte Carlo method

**HOUSEHOLDER, A. S.:   The Theory of Matrices in Numerical Analysis.

  Blaisdell (1964) 257 pp.

     The title of this book gives a perfect description of the contents.
It is written from a mathematical point of view, but all the subject
matter should be of real importance to the computer user who is trying
to solve systems of equations or to find matrix eigenvalues and eigen-
vectors on a computer (the author uses the terms Proper Values and Vectors).
The exposition is at a medium level of difficulty. There is an excellent
44-page bibliography.

General Outline of Contents

1. Some basic identities and inequalities

2. Norms, bounds, and convergence

3. Localization theorems and other inequalities (exclusion theorems;
    inclusion and separation theorems; minimax theorems; inequalities
    of Wielandt and Kantorovich)

4. The solution of linear systems: methods of successive approximation

5. Direct methods of inversion

6. Proper values and vectors: normalization and reduction of the matrix
    (methods of Krylov, Webber-Voetter, Danilevskii, Hessenberg, Lanczos,
    Samuelson and Bryan, Leverrier, etc.)

7. Proper values and vectors: successive approximation (methods of
    Jacobi, Collar and Jahn; power method; LR and QR transformations)

JACKSON, D.: The Theory of Approximation. Amer. Math. Soc. (1930) 178 pp.

This book is easier to read (less advanced) than most American Mathe-
matical Society Colloquium publications (of which this is Vol. 11). It
does not attempt to cover the whole subject; however, it covers theoretical
aspects of the topics chosen in a complete and rigorous manner.

Contents

1. Continuous functions (approximation by trigonometric sums and by
    polynomials)

2. Discontinuous functions; functions of limited variation; arithmetic
    means (convergence of Fourier series and Legendre series)

3. The principle of least squares and its generalizations (trigonometric
    and polynomial approximation)

4. Interpolation (trigonometric and polynomial cases; convergence and
    degree of convergence und r various hypotheses)

5. Introduction to the geometry of function space (a 30-year-old intro-
    duction into a field which has rapidly expanded in the meantime)

JENNINGS, W.: <u>First Course in Numerical Methods</u>. Macmillan (1963) 233 pp.

    ...e author feels that "most existing texts are far too voluminous for
a short introductory course." This small elementary book thus contains a
wide variety of topics with usually only a few short paragraphs about
each. Digital computer applications are discussed in the introduction,
but the remainder of the book does not appear to be slanted this way.

Contents

JORDÁN, C.: Calculus of Finite Differences, 2nd ed. Chelsea (1950) 652 pp.

     This is quite an advanced treatise, and it covers the subject
thoroughly. It is excellent as a reference work. Statistical appli-
cations are stressed. There is no essential difference beween this
edition and the original 1939 edition; thus one expects no emphasis on
computer applications.

Contents

1. On operations (forward, backward, central, and divided differences;
    generating functions; expansions of functions)

2. Functions (factorial, gamma, incomplete gamma, digamma, trigamma,
    beta, incomplete beta, exponential, tigonometric)

3. Inverse operation of differences and means. Sums (indefinite sums,
    summation by parts, determination of sums)

4. Stirling's numbers and applications

5. Bernoulli polynomials and numbers

6. Euler's and Boole's polynomials. Sums of reciprocal powers

7. Expansion of functions; interpolation; construction of tables

8. Approximation and graduation (orthogonal polynomials, trigonometric
    approximation, method of least squares)

9. Numerical resolution of equations; numerical integration

10. Functions of several independent variables (operations, interpolation)

11. Difference equations (various methods of solution)

12. Equations of partial differences

KANTOROVICH, L. V., and KRYLOV, V. I.: <u>Approximate Methods of Higher</u>

<u>Analysis</u>. Interscience (1958) 681 pp.

This is quite advanced. It is a translation of the 4th Edition of
the highly recommended Russian treatise. No thought is given to computer
methods, but rather the authors wish to show mathematically how one can
obtain approximate solutions to various types of partial differential
equation and integral equation problems.

General Outline of Contents

1. Methods based on representation of the solution as an infinite series
    (Fourier method; infinite systems of equations; use of nonorthogonal
    series; use of double series; improvement of the convergence of series)
2. Approximate solution of the integral equations of Fredholm
3. The method of nets (finite difference methods for numerical solution
    of ordinary and elliptic partial differential equations)
4. Variational methods
5. The conformal transformation of regions
6. Applications of conformal transformation (to Dirichlet problem,
    Neumann problem, etc.)
7. Schwarz's method (Dirichlet problem)

KHABAZA, I M.: <u>Numerical Analysis</u>. Pergamon Press (1965) 242 pp.

This elementary paperback text is one of five in a series entitled, "Higher Mathematics for Engineers and Scientists," which have been written for students with an introductory calculus background. The choice of topics and presentation are standard, with no special applications to problems in engineering.

General Outline of Contents

1. Digital computers (general description)

2. Desk machines; errors in computations

3. Finite difference methods

4. Recurrence relations: difference equations; summation of series; solution of algebraic equations

5. Numerical solution of ordinary differential equations (initial value problems)

6. Matrices; solutions of sets of linear equations; latent roots and vectors

7. Relaxation methods
   Solution of linear equations; second order ordinary differential equations with two-point boundary conditions; solution of partial differential equations of Poisson type

8. Numerical methods for unequal intervals
   Interpolation; curve fitting and method of least squares; orthogonal polynomials; integration (Gaussian quadrature)

KHOVANSKII, A. N.:   The Application of Continued Fractions and Their

Generalizations to Problems in Approximation Theory.   Noordhoff

(1963) 212 pp.

In addition to being carefully organized, this book has the added
advantage that the translator (Peter Wynn) has himself a very good
understanding of the subject; thus there is no roughness in the trans-
lation.   The original Russian edition came out in 1956.   If a computer
specialist is interested in learning something of the theory of con-
tinued fractions which could be of practical use, this book is probably
by far the best source.

General Outline of Contents

1.   Certain problems in the theory of continued fractions
     Convergents; transformations of continued fractions; transformations
     of series into continued fractions; convergence theory and tests
2.   Continued fraction expansions of certain functions
     Binomial functions; $\sqrt[x]{x}$; $\ln x$; e^x; inverse trigometric and hyperbolic
     functions; $\tan x$ and $\tanh x$; $\int_0^x \frac{dt}{1+t^k}$; hypergeometric functions; Prym's
     function; incomplete gamma function; etc.
3.   Further methods for obtaining rational function approximations
     Derivation of various rational function approximations to certain
     functions with the help of Obreschkoff's formula; derivation of
     rational function approximations by means of iteration; rational
     function approximations for many of the functions mentioned in para. 2
4.   Generalized continued fractions
     The computation of square roots or the solution of quadratic equations
     with the help of matrices of second order; the calculation of nth
     roots or the solution of nth order polynomial equations with the help
     of matrices of nth order

KOPAL, Z.: <u>Numerical Analysis</u>, 2r. i ed.   Wiley (1961) 594 pp.

   This is a reasonably elementary book. However, most of the subjects
considered are discussed quite fully, and there are many paragraphs which
are noted as being more advanced and which do not have to be read in order
to understand later paragraphs. The subject of mechanical quadratures is
covered thoroughly, and the chapters on ordinary differential equation
boundary value problems and on integral and integro-differential equations
give much more information than in most general books on numerical analysis.
Appendix 4 gives abscissas and weight coefficients of several formulas for
mechanical quadratures.

<div align="center">Contents</div>

1. Introduction

2. Polynomial interpolation

3. Numerical differentiation

4. Integration of ordinary differential equations

5. Boundary value problems: algebraic methods

6. Boundary value problems: variational, iterative, and other methods

7. Mechanical quadratures

8. Numerical solution of integral and integro-differential equations

9. Operational methods in numerical analysis

KOROVKIN, P. P.: Linear Operators and Approximation Theory. Hindustan

   Publishing Co. (1960) 222 pp.

   This advanced book is a poor translation from the 1959 Russian edition.
The language of functional analysis is used throughout.

Contents

1. Linear positive functionals and operators

2. Order of approximation of functions by means of polynomials

3. Characteristic of differential properties of a function with respect
    to the sequence of its best approximations

4. Order of approximation of functions by means of linear positive
    polynomial operators

5. Linear continuous polynomial operators

6. Fourier series

7. Interpolating polynomials

KRYLOV, V. I.: <u>Approximate Calculation of Integrals</u>. Macmillan (1962)

357 pp.

This fairly advanced book is a translation from a 1959 Russian text.
Technical terms are translated correctly (which often is not the case in
many other translations). Almost all the material is on the approximate
integration of functions of a single variable: both definite and indefinite
integrals are considered. Appendices give nodes and coefficients for
Gauss, Gauss-Hermite, and Gauss-Laguerre quadrature formulas.

Contents

Preliminary Information

1. Bernoulli numbers and Bernoulli operators

2. Orthogonal polynomials

3. Interpolation of functions

4. Linear normed spaces; linear operators

Approximate Calculation of Definite Integrals

5. Quadrature sums and problems related to them. The remainder in
   approximate quadrature

6. Interpolatory quadratures

7. Quadratures of the highest algebraic degree of precision

8. Quadrature formulas with least estimate of the remainder

9. Quadrature formulas containing pre-assigned nodes

10. Quadrature formulas with equal coefficients

11. Increasing the precision of quadrature formulas

12. Convergence of the quadrature process

Approximate Calculation of Indefinite Integrals

13. Introduction (error; convergence; stability)

14. Integration of functions given in tabular form

15. Calculation of indefinite integrals using a small number of values
    of the integrand

16. Methods which use several previous values of the integral

KUHN, H. W., and TUCKER, A. W. (Ed.): <u>Linear Inequalities and Related</u>

<u>Systems</u>. Princeton Univ. Press (1956) 322 pp.

This is a collection of 18 quite advanced papers on the theory of linear inequalities written by recognized authorities in the field. It is No. 38 in the <u>Annals of Mathematics Studies</u>. It includes a good sized bibliography, but no index.

Contents

1. Dual systems of homogeneous linear relations (Tucker)

2. Polyhedral convex cones (Goldman and Tucker)

3. Resolution and separation theorems for polyhedral convex sets (Goldman)

4. Theory of linear programming (Goldman and Tucker)

5. On systems of linear inequalities (Fan)

6. Infinite programs (Duffin)

7. A prime-dual algorithm for linear programs (Dantzig, Ford, and Fulkerson)

8. Marginal values of matrix games and linear programs (Mills)

9. Determinateness of polyhedral games (Wolfe)

10. On systems of distinct representatives (Hoffman and Kuhn)

11. Dilworth's theorem on partially ordered sets (Dantzig and Hoffman)

12. On the max-flow min-cut theorem of networks (Dantzig and Fulkerson)

13. Integral boundary points of convex polyhedra (Hoffman and Kruskal)

14. An extension of a theorem of Dantzig (Heller and Thompkins)

15. Neighboring vertices on a convex polyhedron (Gale)

16. On a theorem of Wald (Kuhn)

17. On the solution of a game-theoretic problem (Thompson)

18. The closed linear model of production (Gale)

KUNZ, K. S.: <u>Numerical Analysis</u>. McGraw-Hill (1957) 381 pp.

This is a reasonably elementary textbook. In addition to the standard topics covered in most beginning numerical analysis texts, the author has quite a discussion of numerical solution of partial differential and integral equations.

Contents

1. Real roots of an equation

2. Roots of polynomial equations

3. Finite difference tables and the theory of interpolation

4. Central difference interpolation formulas

5. Lagrange's interpolation formula and inverse interpolation

6. Summation of series

7. Numerical differentiation and integration

8. - 9.: Numerical solution of ordinary differential equations

10. Simultaneous equations and determinants

11. Interpolation in tables of two or more variables

12. - 14.: Numerical solution of partial differential equations

15. Integral equations

Appendix: Estimation of error in numerical computation

LANCE, G. N.: <u>Numerical Methods for High Speed Computers</u>. Iliffe (1960) 166 pp.

This reasonably elementary book discusses all the most important topics in numerical analysis for the average scientific computer programmer. With a small number of pages allotted to each topic, the discussion is limited in many cases to a few sentences. Also, in several cases, when a good method and another generally inferior method are discussed, there is nothing to indicate that the latter has any disadvantages.

General Outline of Contents

1. Introduction (a description of computers and their use)
2. Evaluation of functions (square roots; e^x; $\ln x$; trigonometric functions; arctangent; arcsine and arccosine; complete elliptic integrals; Jacobian elliptic functions; Bessel functions)
    Chebyshev polynomials and continued fractions are used in deriving formulas for the above
3. Solution of ordinary differential equations
4. Matrix methods
    Calculation of latent roots and vectors (eigenvalues and eigenvectors)
    Matrix interpretive scheme on a digital computer
    Inversion of matrices
5. Numerical solution of partial differential equations
6. Miscellaneous processes
    Solutions of polynomial equations; solution of real algebraic or transcendental equations; continued fractions; interpolation; numerical evaluation of definite integrals; inverse Laplace transforms; Aitken's δ^2 process

Appendix: Floating point arithmetic

**LANCZOS, C.: <u>Applied Analysis</u>. Prentice Hall (1957) 539 pp.

This reasonably elementary book emphasizes the use of vectors, matrices, and eigenvalues. Also stressed is the use of Chebyshev polynomials in a wide variety of problems. Explanations are unusually clear, and the author often emphasizes techniques which are particularly useful in digital computer applications.

Contents

1. Algebraic equations

2. Matrices and eigenvalue problems

3. Large-scale linear systems

4. Harmonic analysis

5. Data analysis (least squares, interpolation, smoothing, numerical differentiation, etc.)

6. Quadrature methods

7. Power expansions (telescoping power series, use of Chebyshev polynomials, use of the τ method, etc.)

LANGER, R. E. (Ed.): <u>On Numerical Approximation</u>. University of Wisconsin

Press (1959) 462 pp.

This is an advanced work. It consists of 21 articles presented by
invitation at a Numerical Analysis Symposium in 1958 by internationally
known numerical analysts. (Six of the 20 authors are from other countries.)
Many of the articles include excellent bibliographies on the topics dis-
cussed.

Titles of the Articles

1. On tr nds and problems in numerical approximation (Ostrowski)

2. Linear spaces and approximation theory (Buck)

3. Operational methods in numerical analysis based on rational ap-
proximations (Kopal)

4. On the numerical integration of periodic analytic functions (Davis)

5. Some new divided difference algorithms in two variables (Salzer)

6. Numerical evaluation of multiple integrals (Hammer)

7. Optimal approximation and error bounds (Golomb and Weinberger)

8. The rationale of approximation (Sard)

9. On extremal approximations (Walsh)

10. Numerical methods of Tchebycheff approximation (Stiefel)

11. Minimax methods in table construction (Fox)

12. Existence of essentially nonlinear families suitable for oscillatory
approximation (Motzkin)

13. On variation diminishing approximation methods (Schoenberg)

14. Approximation by functions of fewer variables (Golomb)

15. Extremal approximations--a summary (Miller)

16. Survey of recent Russian literature on approximation (Buck)

17. The quotient-difference and epsilon algorithms (Bauer)

18. Some sufficient conditions for the existence of an asymptotic formula
or an asymptotic expansion (Rosser)

19. The estimation of (power) spectra and related quantities (Tukey)

20. Approximation in partial differential equations (Collatz)

21. Special polynomials in numerical analysis (Todd)

LAPIDUS, L.: <u>Digital Computation for Chemical Engineers</u>. McGraw-Hill

(1962) 407 pp.

This is a reasonably elementary numerical analysis text written by a
Chemical Engineer. The examples are supposed to be directed toward problems
of direct chemical engineering interest; but usually the problem is origi-
nally stated in quite a mathematical form, so the computer programmer will
not find much on the background of chemical engineering problems. However,
the choice of topics and the degrees of emphasis placed on each indicate
their importance in the numerical solution of chemical engineering problems.
The number of topics covered is very large for a book of this size.

Contents

1. Concepts and history of digital computers

2. Polynomial approximation

3. Ordinary differential equations

4. Partial differential equations

5. Systems of linear algebraic equations

6. Roots of algebraic and transcendental equations

7. Further methods of approximation (least squares; orthogonal polynomials;
   telescoping power series; continued fractions)

8. Optimization and control (linear programming, etc.)

LARSSON, R. D.: <u>Equalities ana Approximations - with FORTRAN Programming</u>.

Wiley (1963) 158 pp.

This is a very elementary book, emphasizing concepts from "the new mathematics." The fact that numerical approximation and FORTRAN programming <u>are</u> discussed may make the other material more palatable to the parents of the students taking such an "enriched" course in high school or such a freshman liberal arts course in college.

<div align="center">Contents</div>

1. Groups

2. Matrices

3. FORTRAN programming

4. Sets with two operations: rings, integral domains, fields

5. Inequalities

6. Areas

7. Numerical and polynomial approximations

In all chapters after the second, sample FORTRAN programs are given

LEBEDEV, A. V. and FEDOROVA, R. M.: A Guide to Mathematical Tables.

Pergamon (1960) 586 pp.

BURUNOVA, N. M.: A Guide to Mathematical Tables, Supplement No. 1.

Pergamon (1960) 190 pp.

These two volumes (listing various mathematical tables which have been published throughout the world) are translations from the Russian. Only the words have been translated; tabular matter has been reproduced directly from the original. The main Russian edition was published in 1956, while the supplement references some material from sources as late as 1958. If one cannot find reference to a table he desires either in Fletcher, Miller, and Rosenhead, or in Schütte, or here, he might as well assume he is not going to find such a table published before 1960 or 1961.

Contents

Part 1. Description of the tables (given in chapters set up according to subject matter)

Part 2. References to subject material discussed in each of the chapters of Part 1.

Author index

(Both the original and the supplement have the above format)

LEVY, H. and BAGGOTT, E. A.: <u>Numerical Solutions of Differential Equations</u>.

   Dover (1955) 238 pp.

     For many years this book (published in 1934) was alone in its field.
It is reasonably elementary, and it discusses both graphical and numerical
solutions of initial value problems for ordinary differential equations. At
the time it was written, problems of stability of the finite difference for-
mulas had not worried workers in the field as they have more recently.

<div align="center">Contents</div>

Graphical methods

Numerical solution over a limited range

Forward integration of first order equations (7 different methods)

Simultaneous equations and equations of the second and higher orders

   (formulas are given for treating several special types of equations)

Special methods applicable to linear differential equations of the second

   order

LEVY, H. and LESSMAN, F.: <u>Finite Difference Equations</u>. Macmillan (1961)

   278 pp.

     The first part of this book is reasonably elementary, but some of the later topics are quite advanced. The subject matter has to do with solutions in closed form, the existence of solutions, etc.; the computation of numerical solutions and the stability problems which might arise in these cases are not discussed.

<div align="center">General Outline of Contents</div>

1. Elementary difference operations

2. Interpolation and extrapolation

3. The determination of difference equations (showing various ways in which difference equations arise)

4. Linear difference and functional equations with constant coefficients

5. The general difference equation of the first order

6. Linear difference equations with variable coefficients

7. Some applications of difference equations (a problem of continuous beams; problems of moving spheres; a problem of discs on a shaft; voltage drop in a chain of insulators; a problem in optics; a problem of masses on a string; permutation and combination problems; a problem of sequential tests in industrial statistics)

8. Difference equations associated with functions of two variables (partial difference equations with constant coefficients; some special cases of more general equations)

LINNIK, Y. V.: <u>Method of Least Squares and Principles of the Theory of</u>

<u>Observations</u>. Pergamon (1961) 360 pp.

This is a translation of a 1958 Russian text. It does not discuss much numerical detail, but rather it is written from a statistical point of view. For example, there is quite a discussion of the problem of determining the proper degree polynomial to use in fitting observed data. Most of the book is written in a fairly elementary manner. There is no index.

General Outline of Contents

1. Necessary knowledge of algebra (vectors; linear equations; matrices; determinants; quadratic forms)

2. Necessary knowledge of the theory of probability (random variables; correlation ellipsoid and ellipsoid of constant variance; distributions of random variables)

3. Necessary knowledge of mathematical statistics (estimation of parameters)

4. Direct measurements of equal accuracy (point estimates and estimates by confidence intervals; estimation of accuracy)

5. Direct observations of unequal accuracy (point estimation of mean and σ^2; estimation by confidence intervals)

6. Indirect unconditional measurements

7. The estimation of linear forms in fundamental parameters from indirect observations. Theorems of Neyman and David

8. Indirect conditional measurements

9. Reduction by means of correlates

10. Some examples of the analysis of observations in Geodesy

11. Estimation of results of direct and reverse bearings

12. Parabolic interpolation by the method of least squares

13. Some investigations of A. Wald. Line of orthogonal regression and its application

14. Miscellaneous additional results (confidence ellipsoids; dependent observations; non-normal error vector; Cauchy's method of reduction of observations)

LOWAN, A. N.: <u>The Operator Approach to Problems of Stability and</u>

<u>Convergence of Solutions of Difference Equations</u>. Scripta Mathe-

matica, New York (1957) 104 pp.

This is quite an advanced study of stability and convergence of the
solutions of various difference equations. However, the author uses the
same type of analysis on all his problems, so after one understands
thoroughly the methods applied to the first simple problem, the remainder
of the book is not too difficult. The appendices give alternate proofs
or more detailed proofs of the stability and convergence criteria of the
main text.

Contents

1. & 2.: Stability analysis of various difference schemes for the one-
   dimensional problem in heat conduction
3. Convergence of various iteration procedures
4. Stability analysis of various difference schemes for two-dimensional
   problems in heat conduction
5. Numerical treatment of the Laplace and Poisson differential equations
   in two dimensions
6. Convergence of solutions of difference equations to the solutions of
   the corresponding differential equations (for the one-dimensional dif-
   ferential equation of heat conduction)
7. Stability and convergence of difference analogs of the differential
   equation of wave motion
8. Stability analysis of difference analogs of the differential equation
   of heat conduction in case of variable coefficients

Appendices:
   1. Further applications of the theorems of Gershgorin and Brauer
   2. The roots of the determinantal equation
   3. Generalization of the Richardson iteration procedure to two-
      dimensional potential problems for regions bounded by lattice lines
   4. On high powers of matrices whose moduli of eigenvalues are smaller
      than unity
   5. On the stability of the Peaceman-Rachford scheme for arbitrary two-
      dimensional regions
   6. On Richardson's second order scheme

LYUSTERNIK, L. A., CHERVONENKIS, O. A., and YANPOL' SKII, A. R.: Handbook

for Computing Elementary Functions. Pergamon (1965) 251 pp.

This translation from a 1963 Russian book gives many methods of computing values for various elementary functions. It also gives the actual algorithms used on several particular Soviet computers. For computer programmers it should be a welcome supplement to the well-known book by Hastings, Approximations for Digital Computers, at least until the long-promised book by Hart, *et al*, Handbook of Computer Approximation, is actually published.

Contents

1. Rational and power functions

2. Exponential and logarithmic functions

3. Trigonometric, hyperbolic, inverse trigonometric, and inverse hyperbolic functions

4. Algorithms used for computing elementary functions on some Soviet computers (Strela, BESM, M-2, M-3, Ural)

Appendices

1. Special polynomials and other functions (Gudermannian, harmonic polynomials, hypergeometric function, orthogonal polynomials)

2. Numerical tables

MC CORMICK, J. M. and SALVADORI, M. G.: <u>Numerical Methods in FORTRAN</u>.

Prentice-Hall (1964) 324 pp.

This very elementary text is meant for a person who is beginning
numerical analysis as well as beginning to use a computer. After a brief
introduction to FORTRAN, several chapters of a standard numerical analysis
course follow; then the last 55 percent of the book presents actual
FORTRAN II programs, flow charts, etc. Their FORTRAN programming does
nothing to train the learner to write so as to conserve machine time.

Chapter Headings

1. Computers and programming

2. Approximate computations

3. Differentiation, integration, interpolation, and extrapolation

4. Solution of algebraic and transcendental equations

5. Simultaneous linear algebraic equations

6. Ordinary boundary value problems

7. Ordinary initial value problems

8. Two-dimensional problems

FORTRAN II Programs for Topics in Above Chapters

2. Evaluation of a polynomial; difference tables; Taylor series computation

3. First derivative of tabulated function; Simpson's rule; Richardson
   extrapolations; Lagrangian interpolation; Aitken-Neville interpolation

4. Quadratic equation; cubic equation; quartic equation: Newton's method
   (real or complex coefficients); bisection method.

5. Determinant by pivotal condensation; Gaussian elimination; Gauss-Seidel
   iteration; eigenvalues of 3rd order matrix; largest eigenvalue by iteration.

6. Second order boundary value programs; fourth order boundary value problems.

7. Euler method; Runge-Kutta method; Milne's method; simultaneous first order
   equations. Second order equations: Runge-Kutta, Milne, and a special
   method.

8. Laplace's equation; parabolic equation; hyperbolic equation; a two-
   dimensional boundary value problem

9. Further SUBROUTINES: Square root of a complex number; Bessel functions;
   simultaneous complex equations; matrix inversion; Simpson's rule with
   interval halving; two-dimensional Simpson's rule

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MC CRACKEN, D. D.: <u>A Guide to ALGOL Programming</u>. (1962) 106 pp. <u>A Guide</u>

<u>to FORTRAN IV Programming</u>. (1965) 151 pp. Wiley.

These two manuals explain the use of ALGOL and FORTRAN (respectively) in a manner more like a textbook than is the case with the basic reference manuals. There are more sample problems, and there are exercises for the student (with some answers at the back of the book).

The ALGOL is ALGOL-60 as defined in the May, 1960, issue of *Communications of the Association for Computing Machinery* in "Report on the Algorithmic Language ALGOL 60," edited by Peter Naur. The FORTRAN IV is as specified in IBM manuals.

Each of these books would be preferable for self study over the basic manuals. Particularly in the case of ALGOL, it is extremely useful to have the problems and examples with the answers.

MC CRACKEN, D. D. and DORN, W. S.: Numerical Methods and FORTRAN

Programming. Wiley (1964) 457 pp.

The FORTRAN in this elementary text is FORTRAN II. The topics of numerical analysis and FORTRAN programming are integrated very effectively, and it should be a very good book for a beginner who wishes to study on his own.

Chapter Headings

1. Fundamentals of FORTRAN computation

2. Errors

3. Practical evaluation of functions

4. Program development

5. Roots of equations

6. Numerical evaluation of integrals

7. Subscripted variables and the DO statement

8. Simultaneous linear algebraic equations

9. Functions and specification statements

10. Ordinary differential equations

11. Partial differential equations

Appendix 1. Summary of FORTRAN input and output methods

Appendix 2. Chebyshev polynomials; formulas for telescoping power series; approximations for some elementary functions; Gauss quadrature abscissas and coefficients.

MC MINN, S. J.: <u>Matrices for Structural Analysis</u>. E. & F. N. Spon. Ltd. (1964) 210 pp.

Other textbooks might offer a better first course in matrices. However, if one already possesses some elementary knowledge of the subject, he might wish to read this text to learn something of the problems in civil and mechanical engineering for which matrix methods are useful, and to learn something of the vocabulary used in structures problems by the practicing engineer.

<div align="center">Contents</div>

1. Determinants - algebraic theory

2. Matrices - algebraic theory

3. Determinants - arithmetic computations

4. Matrices - arithmetic computation (matrix multiplication and inversion)

5. Influence coefficients and energy theorems

6. & 7.: Statically indeterminate structures (flexibility method and stiffness method)

8. Matrices - theory of characteristic equations, latent roots, functions of matrices, etc.

9. Matrices - computation of latent roots

10. Stability of rigid frames

11. Further latent root applications

MACON, N.: <u>Numerical Analysis</u>. Wiley (1963) 161 pp.

This quite elementary text is designed for a one-semester Junior introductory course; it could also be used for self study.

Contents

1. Basic concepts

    Analog and digital computers; flow charts; error analysis
2. Approximation of functions by polynomials
3. Iterative methods of solving functional equations
4. Matrices and systems of linear equations
5. Computational methods with matrices
6. The characteristic values and characteristic vectors of a matrix
7. Interpolation
8. Differentiation and integration
9. Remainder terms for the integration formulas
10. Ordinary differential equations
11. Systems of first order (differential) equations
12. Difference equations

METROPOLIS, N. C., TAUB, A. H., TODD, J., THOMPKINS, C. B. (Ed.):

<u>Experimental Arithmetic, High Speed Computing and Mathematics</u>,

Proceedings of Symposia in Applied Mathematics, Vol 15. Amer.

Math. Soc. (1963) 396 pp.

        This volume contains 28 of the papers given at two April, 1962
symposia.   One symposium was entitled, "Experimental Airthmetic," and
the other was entitled, "Interactions Between Mathematical Research and
High Speed Computing."

<div align="center">Contents</div>

1. Purposeful and unpurposeful computing (Cohn)
2. Eliminating the irrelevant from mechanical proofs (Davis)
3. The mechanization of mathematical arguments (Wang)
4. Towards more versatile mechanical translators (Irons)
5. Information theory and decoding computations (Elias)
6. Adaptive neural networks as brain models (Block)
7. Computer investigation of orthogonal Latin squares of order ten (Parker)
8. Determination of division algebra with 32 elements (Walker)
9. How programming difficulties lead to theoretical advances (Dade and
    Zassenhaus)
10. Methods of successive restrictions in computational problems involving
    discrete variables (Tompkins)
11. An experimental study of the simplex method (Kuhn and Quandt)
12. Large and nonconvex problems in linear programming (Gomory)
13. Some high speed logic (Lehmer)
14. Stability questions for some numerical methods for ordinary differ-
    ential equations (Dahlquist)
15. Some applications of the quotient-difference algorithm (Henrici)
16. Plane-rotations in floating-point arithmetic (Wilkinson)
17. New aspects in numerical quadrature (Bauer, Rutishauser, and Stiefel)
18. On Jacobi rotation patterns (Rutishauser)
19. Automatic numerical integration of ordinary differential equations
    (Nordsieck)
20. Survey of stability of different schemes for solving initial value
    problems for hyperbolic equations (Lax)
21. Unexpected dividends in the theory of prime numbers (Rosser)
22. The particle-in-cell method for numerical solution of problems in
    fluid dynamics (Harlow)
23. Numerical experiments in atmospheric hydrodynamics (Charney)
24. The oscillations of the earth and of the atmosphere (MacDonald)
25. Few particle experiments in statistical mechanics (Alder)
26. An approach to the Ising problem using a large scale fast digital
    computer (Yang)
27. Applied mathematics as used in theoretical chemistry (Hirschfelder)
28. The mechanization of science (Hamming)

MEYER, H. A. (Ed.): <u>Symposium on Monte Carlo Methods</u>. Wiley (1956) 382 pp.

This consists of a series of papers given at a Somposium on Monte Carlo methods at the University of Florida in 1954. Many of the papers are quite advanced, but if one wishes to do more than merely simulate a physical problem on the computer (calling <u>this</u> Monte Carlo), he must be prepared to look into the possibilities of finding variance reducing techniques or other short cuts for his problem. The large bibliography contains also many abstracts of the books and articles listed.

Papers

1. An introductory note (Marshall)

2. Generation of pseudo-random numbers (Taussky and Todd)

3. Phase shifts, middle squares, wave equation (Metropolis)

4. A general theory of stochastic estimates of the Neumann series for the solution of certain Fredholm integral equations (Albert)

5. Neighbor sets for random walks and difference equations (Motzkin)

6. Monte Carlo computations (Dismuke)

7. Applications of Monte Carlo methods to tactical games (Ulam)

8. Conditional Monte Carlo for normal samples (Trotter and Tukey)

9. Monte Carlo techniques in a complex problem about normal samples (Arnold, Bucher, Trotter, and Tukey)

10. An application of the Monte Carlo metod to a problem in gamma ray diffusion (Berger)

12. Application of multiple stage sampling procedures to Monte Carlo problems (Marshall)

13. Questionable usefulness of variance for measuring estimate accuracy in Monte Carlo importance sampling problems (Walsh)

14. Experimental determination of eigenvalues and dynamic influence coefficients for complex structures such as airplanes (Vickery)

15. Use of different Monte Carlo sampling techniques (Kahn)

16. A theoretical comparison of the efficiencies of two classical methods and a Monte Carlo method for computing one component of the solution of a set of linear algebraic equations (Curtiss)

17. A description of the generation and testing of a set of random normal deviates (Lytle)

18. Machine sampling from given probability distributions (Butler)

19. A Monte Carlo technique for obtaining tests and confidence intervals for insurance mortality rates (Walsh)

20. Experiments and models for the Monte Carlo method (Walther)

MILLER, K. S.: <u>An Introduction to the Calculus of Finite Differences and</u>

<u>Difference Equations</u>. Holt, Rinehart, and Winston (1960) 167 pp.

This is a reasonably elementary text. It does not emphasize computational aspects of the subject.

Contents

1. The calculus of finite differences (factorial polynomials, Stirling numbers, the sum calculus, etc.)
2. Infinite products (gamma and beta functions)
3. Bernoulli numbers and polynomials (Euler-Maclaurin summation formula; asymptotic expansions)
4. Linear difference equations in the real domain

MILNE, W. E.: <u>Numerical Calculus</u>. Princeton Univ. Press (1954) 393 pp.

This reasonably elementary text is written in a particularly clear manner. It contains many worked examples.

Contents

1. Simultaneous linear equations
2. Solutions of equations by successive approximations (equation in one unknown or systems of equations; complex roots of algebraic equations; solutions of λ-determinants. Methods of successive substitutions)
3. Interpolation
4. Numerical differentiation and integration
5. Numerical solution of differential equations
6. - 8.: Finite differences (factorial polynomials, binomial coefficients; forward, backward, central, divided, and reciprocal differences; formulas using these differences)
9. Polynomial approximations by least squares
10. Other approximations by least squares (harmonic analysis, Gram-Charlier approximation, etc.)
11. Simple difference equations

MILNE, W. E.: <u>Numerical Solution of Differential Equations</u>. Wiley

   (1953) 275 pp.

      This is a reasonably elementary exposition of the subject. Worked
examples make the details of the numerical methods very clear. The author
has computer applications in mind. There is an excellent bibliography.

General Outline of Contents

Part 1. Ordinary equations

         Predictor-corrector methods (Adams, Milne, etc.)

         Runge-Kutta methods

         Methods based on higher order derivatives

         Analysis of error

         Systems of equations

         Higher order equations

         Two-point boundary problems

Part 2. Partial equations

         Explicit methods

               Simplest parabolic and hyperbolic equations

               Truncation error

               Nonlinear equations

               General boundary conditions

         Linear equations, matrices, eigenvalues (latent roots)

         Implicit methods

               Elliptic equations

               Analysis of errors

         Finding eigenvalues (characteristic numbers) of differential systems

MILNE-THOMPSON, L. M.: <u>The Calculus of Finite Differences</u>. Macmillan

   (1933) 558 pp.

         This quite advanced older treatise is often quoted by other authors
working in the field.

                              Contents

 1. Divided differences

 2. Difference operators

 3. Interpolation

 4. Numerical applications of differences

 5. Reciprocal differences

 6. The polynomials of Bernoulli and Euler

 7. Numerical differentiation and integration

 8. The summation problem

 9. The psi function and the gamma function

10. Factorial series

11. The difference equation of the first order

12. General properties of the linear difference equation

13. Linear difference equation with constant coefficients

14. & 15.: Linear difference equation with rational coefficients; operational
     methods; Laplace's transformation

16. Equations whose coefficients are expressible by factorial series

17. The theorems of Poincaré and Perron

**NATANSON, I. P.: <u>Constructive Function Theory</u>. Unger (3 vols.)

    Vol. 1: <u>Uniform Approximation.</u>(1964) 232 pp.

    Vol. 2: <u>Approximation in the Mean.</u>(1965) 176 pp.

    Vol. 3: <u>Interpolation and Approximation Quadratures.</u>(1965) 176 pp.

These quite advanced volumes are translations of the three parts of a 1949 Russian treatise. The subject deals with the theory behind the approximate representation of functions by simpler functions (as is done extensively on digital computers).

Contents

Volume 1.

    1. Weierstrass' approximation theorem
    2. Algebraic polynomials of the best approximation
    3. Trigonometric polynomials of the best approximation
    4. Interrelation between structural properties of functions and the degree of their approximation by trigonometric polynomials
    5. Characterization of the structural properties of a function by the behavior of its best approximation by trigonometric polynomials
    6. Interrelation between structural properties of functions and their approximation by algebraic polynomials
    7. Approximation by means of Fourier series
    8. The sums of Fejér and de la Vallée-Poussin
    9. The best approximation to analytic functions
   10. Properties of some analytic expressions as means of approximation

Volume 2.

    1. The space $L^2_{p(x)}$
    2. Orthogonal systems
    3. Linearly independent systems of functions
    4. General properties of orthogonal polynomials
    5. The Legendre polynomials
    6. The Jacobi polynomials
    7. The moment problem for finite intervals
    8. Infinite intervals

Volume 3.

    1. Various methods of interpolation
    2. Theorems of a negative character
    3. The convergence of interpolation processes
    4. Several convergence processes related to interpolation
    5. & 6.: Approximation quadratures

**NATIONAL PHYSICAL LABORATORY STAFF: Modern Computing Methods, 2nd ed.

Philosopical Library (1961) 170 pp.

This is a reasonably elementary resume of computational methods, both for hand computation and for high speed computer computation. It is considered to be excellent although rather brief, and it is often referred to in the literature. There is a very good bibliography.

Contents

NIELSEN, K. J.: <u>Methods in Numerical Analysis</u>, 2nd ed. Macmillan (1964)
384 pp.

This is an elementary text. There are many worked examples.

Contents

1. Fundamentals
2. Finite differences
3. Interpolation
4. Differentiation and integration
5. Lagrangian formulas
6. Ordinary equations and systems
7. Differential and difference equations
8. Least squares and their application
9. Periodic and exponential functions

NOBLE, B.: <u>Numerical Methods</u>, Vols. 1 and 2. Oliver and Boyd (1964) 372 pp.

These quite elementary volumes emphasize the practical use of numerical analysis without omitting entirely important concepts in an effort to simplify the presentation. If proofs are not given, the explanations are usually mathematically accurate, as far as they go, and the reader should not come away with erroneous impressions.

Contents

Volume 1 (156 pp.)

1. Accuracy and error

2. Iterative methods, with applications to the solution of equations

3. Elementary programming for digital computers

4. Simultaneous linear algebraic equations

5. Matrix methods

6. Eigenvalues and eigenvectors

Volume 2 (pp. 157-372)

7. Finite differences and the approximate representation of functions

8. Polynomial interpolation

9. Numerical integration and differentiation

10. Ordinary differential equations

11. Partial differential equations (only 34 pp.)

NORKIN, S. B. (Ed.): The Elements of Computational Mathematics.

This very elementary book is a translation of a Russian text published in 1960. The various chapters were written by six different authors. The text was written for correspondence course students, and it should be suitable for self-study at an elementary level.

Contents

1. Computation with approximate numbers, and assessment of errors

2. Construction of tables of functions

3. Approximate solution of equations

4. Systems of linear equations

5. Interpolation polynomials

6. Approximate computation of integrals

7. Approximate integration of differential equations

**OSTROWSKI, A. M.: <u>Solutions of Equations and Systems of Equations.</u>

Academic Press (1960) 202 pp.

This is a somewhat advanced book, although some parts discuss quite
elementary subjects. The author hopes to "bridge over the gap that still
exists between 'pure' and 'practical' mathematics." The computer user
will find that this book is much more "practical" than it looks at first
and probably more practical than many of the more elementary textbooks on
numerical analysis (many of the difficulties encountered in solving certain
equations on digital computers are explained clearly here).

A second, much enlarged edition is scheduled for publication in March,
1966.

Contents

Eleven appendices treat the following subjects: continuity and
relative continuity of the roots of algebraic equations; an explicit for-
mula for the nth derivative of the inverse function; analog of the Reguli
Falsi for two equations with two unknowns; Steffensen's improved iteration
rule; the Newton-Raphson algorithm for quadratic polynomials; some modifi-
cations and an improvement of the Newton-Raphson method; rounding off in
inverse interpolation; accelerating iterations with superlinear convergence;
roots of $f(z) = 0$ from the coefficients of the development of $1/f(z)$;
continuity of the fundamental roots as functions of the elements of the matrix.

PANOV, D. J.: <u>Formulas for the Numerical Solution of Partial Differential</u>

<u>Equations by the Method of Differences</u>. Ungar (1963) 133 pp.

This reasonably elementary text is a translation from the Russian
(probably the 1951 edition). Emphasis is on the numerical solution of
Laplace's equation. Although the book is somewhat old for one on the
subject, the wealth of worked examples should still be of interest. This
volume has the distinction of being the only one reviewed which has neither
a table of contents nor an index!

General Outline of Contents

1. Introduction
2. Interpolation formulas and difference formulas for the approximate
    calculation of derivatives; accuracy attainable
3. Laplace and Poisson equations
    a. Choice of networks; treatment of boundary; rectangular and
        triangular networks
    b. The Dirichlet problem: methods of improving values on the boundary;
        refinement of convergence; examples
    c. The Neumann problem and the third boundary value problem; examples
    d. Solution of Laplace's equation by use of a mapping of the region
    e. Solution of the Laplace and Poisson equations for an inhomogeneous
        medium
4. Biharmonic equation; reduction to a system of Poisson equations; direct
    solution; examples
5. Thermal conductivity equation (parabolic)
    Formulas for one and two space dimensional problems; mixed type bounda-
    ry conditions; examples
6. Wave and telegraph equations (hyperbolic); finite difference methods
7. Quasi-linear hyperbolic systems: the method of characteristics;
    Cauchy problem; Riemann problem; mixed problems. Approximate solutions
    by the method of characteristics; examples

PICC <u>Symposium on the Numerical Treatment of Ordinary Differential</u>
<u>Equations, Integral, and Integro-differential Equations</u>. Birkhaüser
(1960 679 pp.

This contains papers presented at an international symposium held
in Rome September, 1960. Some papers are in French, German, or Italian,
but a large majority of them are in English.

Papers in English Are on the Following Topics

Iterative methods for the numerical solution of ordinary differential
equations. Lyapunov-like functions and approximate solutions of ordinary
differential equations. Fourier transforms and analytic functions. The
solution of integro-differential equations occurring in nuclear collision
problems. An iterative method for solving nonlinear integral equations.
A numerical approach to some problems of continuum mechanics and related
questions of stability. The numerical solution of ordinary differential
equations in Chebyshev series. General problems confronting computer
centers. On existence, uniqueness, and numerical evaluation of solutions
of ordinary and hyperbolic differential equations. A new difference
method for solution of certain second order nonlinear differential
equations. Mathematical programming and integral equations. Some esti-
mates of spectra of matrices. On the asymptotic behavior of certain
one-dimensional flows. Some numerical solutions of two-point eigenvalue
equations with one boundary at infinity. On the general solution of
some nonlinear differential equations. Numerical integration of ordinary
differential equations by difference methods with automatic determination
of steplength. The propagation of round-off error in the numerical so-
lution of initial value problems involving ordinary differential equations
of the second order. The numerical solution of a singular integral
equation. Convergence of the discrete ordinate method for the aniso-
tropic scattering transport equation. On the numerical integration of
ordinary differential equations and the determination of error bounds.
Numerical solution of the differential equations governing the motion of
viscous fluid between two rotating discs. Solution of ordinary differ-
ential equations by trigonometric interpolation. Accumulation of errors
in approximate calculations. Stability of solutions of differential and
integral equations. Solution of integro-differential equations arising
in the theory of atomic scattering. Theory of numerical convergence of
iterative processes with applications to differential equations. Bistable
systems of differential equations. Iterative solution of boundary value
problems using remainder terms of Taylor expansion. Numerical solution
of the singular integral equation for the charge distribution on a flat
rectangular lamina. Solution of the Boltzmann Hilbert integral equation;
propagation of sound in a rarefied gas. An integrodifferential equation.
Application of computing techniques to nuclear physics. Error analysis
for the numerical solution of certain differential equations in gasdyna-
mics. Condition of certain integral equations. A self-consistent one
group method for the Boltzmann transport equation in neutronics. On
spectrum of a mono-energetic neutron transport operator. Perturbed
boundary-value problems and their approximate solution. General report
on the numerical treatment of integral and integro-differential equations.

PRAGER, W.: Introduction to Basic FORTRAN Programming and Numerical

Methods. Blaisdell (1965) 214 pp.

This is a very elementary paper-bound text which emphasizes the
teaching of FORTRAN programming. The numerical methods discussed are
incidental to the basic purpose. However, for a computer programmer
who wishes to learn some basic numerical analysis, this text will proba-
bly be much preferred over one of the older standard texts in which
digital computers are not considered at all.

Contents

In addition to the four chapters scattered through the text explaining
the various features of the FORTRAN language, and a chapter on flow charts,
there are chapters on each of the following topics in numerical analysis:

Error analysis and control

Computing with polynomials

Interpolation

Quadrature

Solution of systems of linear equations; solution of nonlinear equations

   or systems of nonlinear equations

Integration of ordinary differential equations (both initial and

   boundary value problems)

RALL, L. B. (Ed.):   Error in Digital Computation, Vols. 1 and 2.   Wiley

(1965) 336 pp. and 288 pp.

Each of these volumes contains the papers which were presented at symposia on the subject at the Mathematics Research Center, University of Wisconsin, in October 1964 and April 1965, respectively. The first volume also contains an excellent bibliography on the subject of error in digital computation.

A majority of the presentations are from a rather advanced standpoint. However, the actual numerical processes for which error analyses are being given are usually well known; thus it should be possible for the average computer programmer to study through and understand most of these papers quite well.

Contents

Volume 1

1. The problem of error in digital computation (Todd)
2. Techniques for automatic error monitoring and control (Ashenhurst)
3. The automatic analysis and control of error in digital computing based on the use of interval numbers (Moore)
4. Error in digital solution of linear problems (Albasiny)
5. The propagation of error in the digital integration of ordinary differential equations (Henrici)
6. Bibliography on error in digital computation (114 pp.)

Volume 2

1. Experimental investigation of unnormalized arithmetic (Ashenhurst)
2. Error bounds for computations with continued fractions (Henrici)
3. Error bounds for asymptotic expansions of special functions in the complex plane (Olver)
4. Error analysis for transformations based on the use of matrices of the form $I - 2ww^H$. (Wilkinson)
5. Automatic local coordinate transformations to reduce the growth of error bounds in interval computation of solutions of ordinary differential equations (Moore)
6. Differential inequalities and error bounds (Schröder)
7. Discrete representations of partial differential operators (Young and Dauwalder)
8. Upper and lower bounds for solutions of integral equations (Brown)
9. Convergence and error bounds for approximate solutions of integral and operator equations (Anselone)
10. Applications of functional analysis to error estimation (Collatz)
11. Error in the solution of linear programming problems (Wolfe)

**RALSTON, A.:   A First Course in Numerical Analysis.   McGraw-Hill (1965) 578 pp.

This new senior or first year graduate text will probably turn out to be very popular. The author seems to have made some real effort to leave out a lot of the standard classical numerical analysis that has lost its relative importance due to the advent of digital computers. These topics have been replaced by explanations of quite a few of the newer methods which are now being used extensively to solve practical problems on the computer. Each chapter has an up-to-date bibliography.

Contents

1. Introduction and preliminaries (concerning error and concerning digital computers

2. Polynomial approximation

3. Interpolation

4. Numerical differentiation, numerical quadrature, and summation

5 Numerical solution of ordinary differential equations

6. Functional approximation - least squares techniques

7. Functional approximation - minimum-maximum error techniques

8. The solution of nonlinear equations

9. The solution of simultaneous linear equations

10. The calculation of eigenvalues and eigenvectors of matrices

**RALSTON, A. and WILF, H. S. (Ed.): <u>Mathematical Methods for Digital</u>

<u>Computers</u>. Wiley (1960) 293 pp.

This book includes 26 expository articles on various topics of interest
to those who wish to place scientific problems on digital computers. Most
of the articles are reasonably elementary, although sometimes they cover
the subject rather sketchily. Since different authors have written different
chapters, there is a great diversity as to the excellence of the presen-
tations. However, there are many truly excellent chapters; since the author
even presents flow charts describing the particular process, this book
should be of very great use to anyone having anything to do with placing such
problems on the computer. it is written <u>for</u> computer programmers and <u>by</u>
experts who have actually worked with computers.

Contents

1. Generation of elementary functions (Kogbetliantz)
2. Matrix inversion by direct methods (Orden)
3. Solution of linear equations by Gauss-Seidel method (Van Norton)
4. Solution of linear equations by conjugate-gradient method (Beckman)
5. Matrix inversion by rank annihilation (Wilf)
6. Matrix inversion by Monte Carlo methods (Oswald)
7. Determination of characteristic roots of a matrix by Jacobi method
   (Greenstadt)
8. Numerical integration of ordinary differential equations (Ralston)
9. Runge-Kutta methods for the solution of ordinary differential equations
   (Romanelli)
10. Numerical solution of boundary value problems (Wachspress)
11. Solution of ordinary differential equations with large time constants
    (Certaine)
12. Numerical solution of parabolic partial differential equations (Keller)
13. Iterative methods for solution of elliptic partial differential
    equations (Sheldon)
14. Monte Carlo method for solution of elliptic partial differential
    equations (Klahr)
15. Numerical solution of hyperbolic partial differential equations by
    method of characteristics (Lister)
16. Numerical solution of hyperbolic partial differential equations by
    difference methods (Fox)
17. Multiple regression analysis (Efroymson)
18. Factor analysis (Harman)
19. Autocorrelation and spectral analysis (Southworth)
20. Analysis of variance (Hartley)
21. Numerical solution of polynomial equations (Wilf)
22. Methods of numerical quadrature (Ralston)
23. Multiple quadrature by Monte Carlo methods (Kahn)
24. Fourier analysis (Goertzel)
25. Solution of linear programming problems (Arden)
26. Network analysis (Bashkow)

REDISH, K. A.: <u>An Introduction to Computational Methods</u>. Wiley (1965)

    211 pp.

    The author has written this quite elementary book "for the occasional computer user." He thus attempts to present methods which are easy to understand--as opposed to more advanced methods which might be more efficient.

General Outline of Contents

1.   Introduction (sources of error, etc.)

2.   Simultaneous linear algebraic equations

3.   Nonlinear equations (locating roots)

4.   Finite differences

5.   Interpolation

6.   Numerical differentiation and integration

7. & 8.: Ordinary differential equations

    Isoclinals; graphical methods of solution; use of series

    First order equations: predictor-corrector methods; Fox-Goodwin

       methods, etc.

    Second order equations

    Initial value methods; boundary value methods

    Solution of simultaneous algebraic equations

    Boundary conditions at infinity

9.   Functions of two variables

    Interpolation (both "successive" and "simultaneous"); differentiation

       and integration; partial differential equations (with emphasis on

       elliptic equations)

10. Miscellanea (a few words concerning each topic)

    Approximating functions; difference equations; divided differences;

       Gauss integration formula; Lagrangian formula; latent roots and

       vectors; Runge-Kutta methods; singularities; summation of series

REMEZ, E. Ya.: <u>General Computational Methods of Chebyshev Approximation</u>.

<u>The Problems with Linear Real Parameters</u>. (2 vols.) U.S. Atomic Energy

Commission Translation Series, AEC-tr-4491 (original Russian ed., 1957),

740 pp.

    This is an advanced treatise on the subject. However, specific numeri-
cal algorithms are also described. The translation is not very smooth.
The index is located in the second book.

<div align="center">Outline of Contents</div>

Volume 1, Integral Methods of Effective Chebyshev Approximation and
    Properties of Solutions of the Generalized Chebyshev Problem

1. One dimensional problem of Chebyshev approximation by means of
    ordinary polynomials, and its direct generalization
2. Systems of incompatible linear equations (in the usual and genera-
    lized sense), and the general problem of the least deviation from
    zero for a function that depends linearly on a finite number of
    parameters
3. Certain cases of the Chebyshev problem, solved without successive
    computational approximation
4. Certain approximation methods and procedures, connected with
    Chebyshev problems

Volume 2, Finite Systems of Incompatible Linear Equations and Network
    Methods of Chebyshev Approximations

5. General introduction; α-algorithm of successive weighted quadratic
    approximations, and possible different applications of the algorithm
6. Method of successive equalizing descents
7. Method of prevailing deviations

Appendix 1: Convex sets in Euclidean n-space

Appendix 2: Solution of systems of linear inequalities

**RICE, J. R.: The Approximation of Functions. Vol. 1: Linear Theory.

Addison-Wesley (1964) 203 pp.

This fairly advanced text discusses the problem of the approximation
of a real continuous function by an approximating function which depends
on a fixed finite number of parameters. In most cases discussed, these
parameters occur in a linear manner, although "unisolvent" nonlinear ap-
proximating functons are also discussed (for example, rational approxi-
mations). Theory is emphasized, but computing applications are always in
mind, and the reader will often find answers to questions of a practical
nature as he goes along.

General Outline of Contents

1. Fundamentals

   Approximation problem; L_p norms; Tchebycheff norm and the Polya
   algorithm; linear spaces; choice of form and norm; existence theorems

2. Least squares and orthogonal functions

3. Tchebycheff approximation

   Characterization of Best approximations; uniqueness, continuous de-
   pendence; approximation on finite subsets; the de la Valleé-
   Pouissin algorithm; unisolvent functions; rational functions; limits
   of a Tchebycheff type theory

4. Approximation in the L_1 norm

   A convex set K in Euclidean (n+1) space; tangent planes to K; charac-
   terization of best L_1 approximations; uniqueness; polynomials and
   trigonometric sums; finite point sets

5. The Weierstrass theorem and degree of convergence (including topics
   on Fourier series and concerning kernels)

6. Computational methods

   Expansions from analysis; transformations of known expansions; tele-
   scoping procedures; method of descent; descent mapping; method of
   ascent for Tchebycheff approximation; approximation theory and pro-
   gramming

RICHARDSON, C. H.: An Introduction to the Calculus of Finite Differences.

Van Nostrand (1954) 142 pp.

This is a reasonably elementary textbook. There are many exercises
and illustrative examples.

Contents

1. Introduction (definitions and notation; operators)
2. Finite integration and applications (includes summation of series;
    Stirling numbers)
3. Bernoulli and Euler polynomials
4. Interpolation; approximate integration
5. Beta and gamma functions
6. Difference equations

RICHTMYER, R. D.: <u>Difference Methods for Initial Value Problems</u>.

Interscience (1957) 238 pp.

This is an advanced book. It is highly recommended, however, to anyone faced with putting such problems on computers.

Contents

1. Introduction: heat flow problem; finite difference equations; convergence; stability; etc.
2. Linear operators; Banach spaces; functional analysis
3. Linear difference equations
4. Pure initial-value problems with constant coefficients
5. Multi-level difference equations
6. Diffusion and heat flow (31 pp.): simplest heat equation; variable coefficients; nonlinear problems; problems in several space variables
7. Transport equation (44 pp.)
8. Sound waves (8 pp.)
9. Elastic vibrations (16 pp.)
10. Fluid dynamics in one space variable (41 pp.)

SALVADORI, M. G. and BARON, M. L.: <u>Numerical Methods in Engineering</u>,

2nd Ed. Prentice-Hall (1961) 258 pp.

This is a quite elementary text emphasizing the numerical solution of algebraic and transcendental equations and especially differential equations. The authors are engineers and have written the book for engineering students.

Contents of 1st Edition

1. The practical solution of algebraic and transcendental equations: real and complex roots of algebraic equations; transcendental equations; linear simultaneous algebraic equations (Gauss, Cholesky, Gauss-Seidel, and relaxation methods)

2. Finite differences and their applications

3. Numerical integration of initial value problems (Adams, Runge-Fox, Adams-Stormer, Fox methods)

4. Numerical integration of ordinary boundary value problems

5. Numerical solution of partial differential equations

    Partial differential operators in Cartesian coordinates

    Numerical double integration

    Solution of Laplace's and Poisson's equations

    Elastic and plastic torsion

    Problem involving $\nabla^4 z$

    Two-dimensional characteristic value problems

    Solution by separation of variables and finite differences

    Membrane vibrations

    Pivotal points near curved boundaries

    A transient problem in two-dimensional heat flow

    Laplacian operator in skew, polar, and triangular coordinates

SANGREN, W. C.: <u>Digital Computers and Nuclear Reactor Calculations</u>.

Wiley (1960) 208 pp.

This book is written to present the nuclear engineer with an intro-
duction to high-speed nuclear-reactor computations. Anyone with some
computer experience will probably find the parts of the book describing
machines and programming to be very elementary, while the parts dis-
cussing the specialized problems will seem much more difficult.

General Outline of Contents

1. Introduction (very general remarks concerning computers and reactors)

2. Digital computers (description of such machines)

3. Programming

4. Numerical analysis: approximations; interpolation; numerical dif-
   ferentiation and integration; algebraic and transcendental equations;
   ordinary differential equations; matrices and linear equations;
   partial differential equations; the treatment of interfaces

5. A code for fission-product poisoning

6. Diffusion and age-diffusion calculations: the criticality problem;
   the one-group problem and the wave equation; the two-group, two-region
   diffusion problem; one-, two-, and three-dimensional multigroup dif-
   ference equations; neutron balance; age-diffusion equation

7. Transport equation - Monte Carlo

8. Additional reactor calculations: kinetics; burnout; reactor physics
   and shielding; engineering

SARD, A.: <u>Linear Approximation</u>. Mathematical Surveys No. **9**. Amer. Math.

Soc. (1963) 544 pp.

This is an advanced treatise on topics which are much more general than
the word "linear" in the title might imply to some readers; for example,
an 11th degree Gaussian quadrature formula might not be thought of as a
linear approximation in one sense, but such formulas can be discussed readily
in the framework of approximating a linear (integral) operator by another
linear operator.

Contents

SAUL'YEV, V. K.:   Integration of Equations of Parabolic Type by the

Method of Nets. Macmillan (1964) 346 pp.

The title indicates that the whole 346 pages is concerned with the
solution of parabolic partial differential equations by finite difference
methods. However, implicit finite difference schemes for equations with
two space variables become (at a given time t) the same as would occur
in a two-dimensional elliptic problem; more than a third of the book dis-
cusses the numerical solution of these elliptic type problems.

The book is a translation from a Russian text published in 1960. An
elementary notation is used throughout, although of course much of the
subject matter is fairly advanced.

General Outline of Contents

1. Construction of the net equations (for parabolic problems)

    Stability; six-point equation; asymmetric net equations; alternating

    method; method of mean arithmetic; multi-nodal symmetric method;

    comparisons between explicit and implicit methods; spherical and

    cylindrical regions; fictitious nodes; bilateral approximations; two-

    dimensional and multi-dimensional equations; non-uniform nets; multi-

    step equations; variable and discontinuous coefficients; parabolic

    equations of higher than second order; nonlinear equations

2. Solution of the net equations

    "One-dimensional" elliptic net equations; direct methods; ill-conditioned

    net matrices; iterative methods of 1st, 2nd, and n^{th} degrees; variational

    methods; methods using Chebyshev polynomials; methods of successive

    displacements; block iteration

**SCARBOROUGH, J. B.: <u>Numerical Mathematical Analysis</u>, 5th ed.   Johns

Hopkins Press (1962) 594 pp.

     This is a very elementary text, and the later editions are excellent.
Large numbers of worked examples help to explain the processes. Answers
to suggested exercises are given at the end of the book. This book is
highly recommended for anyone with a very limited mathematical background.
The 5th edition has a new chapter on Newton's interpolation formula for
unequal intervals.

Contents of 4th Edition

1. The accuracy of approximate calculations

2. - 4.:   Interpolation

5. The accuracy of interpolation formulas

6. Interpolation with two independent variables and trigonometric
    interpolation

7. Numerical differentiation and integration

8. The accuracy of quadrature formulas

9. The solution of numerical algebraic and transcendental equations

10. Graeffe's root-squaring method for solving algebraic equations

11. The numerical solution of ordinary differential equations

12. The numerical solution of partial differential equations

13. The numerical solution of integral equations

14. The normal law of error and the principle of least squares

15. The precision of measurements

16. Empirical formulas (i.e., formulas whose form is inferred from the
    results of experiment or observation and in which the parameters are
    determined from experimental or observational data)

17. Harmonic analysis of empirical functions

18. Numerical solution of simultaneous linear equations

SCHÜTTE, K.: **Index of Mathematics Tables**. München, Oldenbourg (1955) 143 pp.

This bilingual index lists about 1200 tables; it is smaller than that of Fletcher, Miller, and Rosenhead, but Schütte says that nearly four-fifths of his tables are not shown in the 1946 edition of Fletcher, Miller, and Rosenhead.

Contents

1. Numerical and practical calculating

2. & 3.: Logarithms of natural and circular functions

4. Natural values of circular functions

5. Simple functions derived from ordinary functions

6. Primes; continued fractions; number theory

7. Factorials, gamma functions, exponential and hyperbolic functions, etc.

8. Elliptic functions and integrals; spherical, Bessel functions, etc.

9. Integral tables and other higher functions

10. Tables applicable to physics, chemistry, and other sciences

11. Astronomy and astrophysics

12. Geodesy and geophysics

13. Nautical and aeronautical determination of position

14. Meteorology

15. Astronautics

16. Miscellaneous; formulas and tables of measures, weights, etc.

SHAW, F. S.: <u>Relaxation Methods</u>. Dover (1953) 396 pp.

  This is a reasonably elementary exposition of relaxation methods.
These methods can be programmed for the digital computer, but the program
may become quite complicated if many of the very effective methods of
speeding convergence are introduced into the program. In some parts of
the book, engineering terminology is used, but in general the treatment
is mathematical. A bibliography of papers published from 1935-1949 is
included.

Contents

1. Linear algebraic simultaneous equations

2. Finite-difference approximations

3. Linear ordinary differential equations

4. - 6.: Second order linear partial differential equations

7. Fourth order linear partial differential equations

8. Eigenvalue problems

9. Free surface problems, integral equations, accuracy, nondimensional
   treatment

SINGER, J.:   <u>Elements of Numerical Analysis</u>.   Academic Press (1964)

   395 pp.

   This is a quite elementarv text in classical numerical analysis.   It
can be recommended for someone who wishes to solve numerical analysis
problems without the use of computers.   In particular, no other recent
numerical analysis text has so much space devoted to graphical methods of
solving equations and systems of equations.

Contents

1.   Significant figures and errors

2.   The approximating polynomial; approximation at a point

3.   The approximating polynomial; approximation in an interval

4.   The numerical solution of algebraic and transcendental equations
     in one unknown; geometric methods (construction of scales and rules,
     nomography, etc.)

5.   The numerical solution of algebraic and transcendental equations in
     one unknown; arithmetic methods

6.   The numerical solution of simultaneous algebraic and transcendendental
     equations

7.   Numerical differentiation and integration

8.   The numerical solution of ordinary differential equations

9.   Curve fitting

SMITH, G. D.: <u>Numerical Solution of Partial Differential Equations</u>.

Oxford (1965) 179 pp.

This carefully written text is probably the most elementary book which is devoted exclusively to the numerical solution of partial differential equations. There are many exercises and worked examples.

Contents

SOUTHWELL, R. V.: Relaxation Methods in Engineering Science. Oxford,

Clarendon Press.

SOUTHWELL, R. V.: Relaxation Methods in Theoretical Physics (2 vols).

These are a fairly advanced series of books which were published from 1940 to 1956 as treatises on relaxation methods. The emphasis is always on the solution of practical engineering problems. There are especially many examples from the fields of hydrodynamics and elasticity. These methods have been used more by workers using desk computers than by high speed computer people, probably because of the complexity of the suitable digital computer programs. There are good bibliographies given.

1940 Volume

Relaxation methods applied to pin jointed and continuous girders

Plane and space frameworks having rigid joints; block relaxations

Theoretical aspects of the relaxation method

Electrical networks; gyrostatic systems

Natural modes and frequencies of vibrating systems

Forced oscillations and the theory of dissipative forces

Continuous systems; problems of equilibrium; elastic stability

Nonlinear systems

Volume 1

Plane-potential and quasi-plane potential problems

The problem of conformal transformation

Problems involving boundaries or interfaces not initially known

Volume 2

Biharmonic problems

Two diagram technique

Eigenvalue problems; "normal" vibrations of mechanical and electrodynamic systems

Elastic stability of flat plate subjected to tractions

Nonlinear problems in elasticity, hydrodynamics, and plasticity

Three dimensional relaxation

Heat conduction and other transient problems

SOUTHWORTH, R. W. and DE LEEUW, S. L.: Digital Computation and

Numerical Methods. McGraw-Hill (1965) 508 pp.

This has been written as a textbook for a college freshman engineering course. It can be recommended over the rest of the present flood of books on computer programming and numerical analysis only because of its greater volume of material and because it gives some engineering applications. Ordinarily one would not expect to find so many somewhat more advanced topics in a freshman text. The programming language described is FORTRAN IV; the numerical analysis is classical.

Contents

1. Introduction to and history of computers
2. Flow charting
3. The FORTRAN language
4. Number systems and machine language
5. Rounding and truncation errors
6. Roots of equations
7. Simultaneous linear equations
8. Interpolation
9. Numerical differentiation and integration
10. Taylor's series
11. Numerical solution of ordinary differential equations
12. Empirical formulas and approximation

STANTON, R. G.: <u>Numerical Methods for Science and Engineering</u>. Prentice-

Hall (1961) 266 pp.

    This contains a standard elementary treatment of numerical analysis
for the college Junior; there are no particular applications to science
or engineering, as the title might imply. Most of the topics are covered
reasonably fully for the level to which the book is aimed, but (for ex-
ample) the treatment of numerical solution of ordinary differential equations
should have been modernized.

<div align="center">Contents</div>

1. Ordinary finite differences

2. Divided differences

3. Central differences

4. Inverse interpolation and the solution of equations

5. Computation with series and integrals

6. Numerical solution of differential equations

7. Linear systems and matrices

8. Solution of linear equations

9. Difference equations

10. Solution of differential equations by difference equation methods

11. The principles of automatic computation

STEFFENSEN, J. F.: Interpolation, 2nd ed. Chelsea (1950) 248 pp.

   This is a reasonably elementary text on interpolation formulas
and their use in numerical differentiation, integration, summation, etc.
It is a translation from the Danish edition, which came out in 1925.
The subjects covered are each covered in quite some detail.

Contents

1. Displacement symbols and differences

2. Divided differences

3. Interpolation formulas

4. Some applications

5. Factorial coefficients

6. Numerical differentiation

7. Construction of tables

8. Inverse interpolation

9. Elementary methods of summation

10. Repeated summation

11. Laplace's and Gauss' summation formulas

12. Bernoulli polynomials

13. Euler's summation formula

14. Lubbock's and Woolhouse's formulas

15. Mechanical quadrature

16. Numerical integration of differential equations

17. The calculus of symbols

18. Interpolation with several variables

19. Mechanical cubature

20. On differential coefficients of arbitrary order

**STIEFEL, E. L.: <u>An Introduction to Numerical Mathematics</u>. Academic Press (1963) 286 pp.

This reasonably elementary textbook should be very popular among computer programmers who wish to better understand some of the numerical procedures which are used to solve scientific problems on computers. The choice of topics is particularly good for a person who is interested in the applications of numerical analysis. It is a translation from the German, but it does not seem to suffer from the translation difficulties so often noticeable when the translators are not completely familiar with the subject matter.

General Outline of Contents

1. Linear algebra
2. Linear programming
3. Least-squares approximation and definite problems
4. Nonlinear algebra
5. Eigenvalue problems
6. Differential equations (numerical differentiation and integration; first order differential equations and systems; boundary value problems; partial differential equations)
7. Approximations

SZEGÖ, G.: Orthogonal Polynomials, revised ed., Amer. Math. Soc.,

Colloquium Publications, No. 23 (1959) 421 pp.

This is an advanced treatise dealing with the general theory of orthogonal polynomials as well as with the study of certain classes of these polynomials. Numerical aspects are seldom stressed. There is an excellent list of references given.

Contents

THOM, A. and APELT, C. J.: Field Computations in Engineering and Physics.

Van Nostrand (1961) 168 pp.

This book discusses in a reasonably elementary manner the method
of Squares, which has been used by Thom and others for nearly 40 years in
the numerical solution of partial differential equation boundary value
problems. The authors maintain that their methods of speeding convergence
of the iteration processes are easier to program on a digital computer than
are relaxation methods.

Contents

1. Finite difference formulas

2. Numerical solution of Laplace's equation

3. Symmetromorphic figures and free streamline problems

4. Numerical solution of Poisson's equation

5. Accuracy of solutions

6. Numerical solution of the equation for the flow of a compressible in-
    viscid fluid

7. The biharmonic equations

8. Numerical solution of Navier-Stokes equations

9. Solution of problems in three dimensions with axial symmetry

TIMAN, A. F.: <u>Theory of Approximation of Functions of a Real Variable.</u>

Macmillan (1963) 631 pp.

This advanced treatise is a translation from a Russian volume published in 1960. In general, the book is similar to those by Achieser (originally published in 1947) and by Natanson (originally published in 1949), but it includes newer Russian research which had not been available to the earlier authors.

Contents

1. Weierstrass' theorem

2. The best approximation

3. Some compact classes of functions and their structural characteristics

4. Some properties of algebraic polynomials and transcendental integral functions of exponential type

5. Direct theorems of the constructive theory of functions

6. Converse theorems. Constructive characteristics of some classes of functions

7. Further theorems connecting the best approximations of functions with their structural properties

8. Linear processes of approximation of functions by polynomials and some estimates connected with them

9. Some results from the theory of functions and functional analysis

TOCHER, K. D.: <u>The Art of Simulation</u>. Van Nostrand (1963) 184 pp.

This book is suggested for a computer user who wishes to learn more about the theory of the simulation and Monte Carlo problems which are to be carried out on the computer. The author assumes a basic knowledge of probability and statistics, but assuming this, the book could probably be classified as reasonably elementary.

Contents

TODD, J.: <u>Introduction to the Constructive Theory of Functions</u>.

Academic Press (1963) 127 pp.

This is a somewhat advanced book, and is probably used in first year
graduate courses. The title has reference to the approximate representa-
tion of functions in terms of simpler ones, but several other background
topics take up some of the space, so that the term "introduction" in the
title is really warranted. Also, pages 93 to 127 are taken up with solu-
tions to problems, bibliography, etc. If one were studying this topic for
the first time, he might wish to read this book and Natanson's books con-
currently.

Contents

1. Results from algebra and analysis

2. The theorems of Weierstrass

3. The Chebyshev theory

4. The theorems of the Markoffs

5. Orthogonal polynomials

6. Interpolation and interpolation processes

7. Bernoulli polynomials

8. Function spaces

9. Approximate quadrature

**TODD, J. (Ed.): Survey of Numerical Analysis. McGraw-Hill (1962) 589 pp.

This book is based upon a series of lectures by the various authors in a training program in numerical analysis for senior university staff members who had not previously specialized in numerical analysis. Some of the chapters are reasonably elementary, while others are quite advanced. Most chapters contain excellent bibliographies, and this book is used extensively as a general reference work on modern numerical analysis. The index is skimpy, but the table of contents has a lot of detail; both should be consulted before giving up on finding a particular subject.

Contents

1. Motivation for working in numerical analysis (Todd)
2. Classical numerical analysis (interpolation; quadrature and differentiation; differential equations; etc.) (Todd)
3. The constructive theory of functions (Todd)
4. Automatic computers (Newman and Todd)
5. Use and limitation of computers (Cohn)
6. Matrix computations (Newman)
7. Numerical methods for finding solutions of nonlinear equations (Hochstrasser)
8. Eigenvalues of finite matrices (Taussky and Marcus)
9. Numerical methods in ordinary differential equations (Antosiewicz, Gautschi)
10. Orthonormalizing codes in numerical analysis (Davis)
11. The numerical solution of elliptic and parabolic partial differential equations (Young)
12. Numerical methods for integral equations (Bückner)
13. Errors of numerical approximation for analytic functions (Davis)
14. Numerical analysis and functional analysis (Antosiewicz and Rheinboldt)
15. Discrete problems (block design; group theory problems) (Hall)
16. Number theory (Cohn and Taussky)
17. Linear estimation and related topics (Zelan)

TRAUB, J. F.: <u>Iterative Methods for the Solution of Equations</u>. Prentice-

Hall (1964) 310 pp.

This quite advanced book considers the problem of finding real roots
of algebraic or transcendental equations or systems of equations. The
author states that the extension of many of his results to the case of
complex roots would not be difficult. Although parts of the book seem quite
theoretical, the general tone is one of considering the efficiency of
various iterative root finding schemes which might be used on a digital
computer.

General Outline of Contents

1. Introduction and basic concepts and notations

2. General theorems on iteration functions (convergence theorems and the
    iteration calculus)

3. The mathematics of difference relations (intermediate theorems on
    solutions of certain difference equations and on the asymptotic be-
    havior of some solutions)

4. Iteration functions generated by direct or inverse hyperosculatory
    interpolation

5. One-point iteration functions

6. One-point iteration functions with memory (using old information con-
    cerning previous iterates)

7. Concerning multiple roots

8. & 9.: Multi-point iteration functions (there are no well known examples
    of such iteration functions)

10. Iteration functions which require no evaluation of derivatives

11. Systems of equations

12. A compilation of iteration functions

Appendices

   Interpolation

   On the jth derivative of the inverse function

   Significant figures and computational efficiency

   Acceleration of convergence

   Numerical examples

   Areas for future research

VAJDA, S.: <u>The Theory of Games and Linear Programming</u>. Wiley (1957) 106 pp.

VAJDA, S.: <u>Readings in Linear Programming</u>, 2rd ed. Wiley (1962) 130 pp.

These two books give quite an elementary introduction into the field of linear programming. The first named book has many worked examples, and the second book is practically a listing of various types of "practical" problems. Neither book requires much mathematics of the reader.

Contents of the First Book

1. An outline of the theory of games
2. Graphical representation
3. Algebra and theory of games
4. An outline of linear programming
5. Graphical representation of linear programming
6. Algebra of the simplex method
7. Degeneracy and other complications
8. Duality
9. The solution of games
10. The method of leading variables

Contents of the Second Book

Transportation problems, caterer problem, production scheduling, trans-shipment, bid evaluation, flow through a network, ship scheduling, personnel assignment (allocation), routing aircraft, investment; the simplex tableau; nutrition problem, airlift, blending of gasolines, smooth patterns of production; duality; selection of products, trim loss reduction, attendants' rota, warehousing, games.

**VARGA, R.: <u>Matrix Iterative Analysis</u>. Prentice-Hall (1962) 322 pp.

This somewhat advanced book discusses the numerical solution of matrix problems arising from discrete approximations to elliptic partial differential equations. Although the mathematical theory is there, the whole point of the book is to show how these particular large linear systems can be solved efficiently on large scale digital computers. There is also a chapter on matrix methods for problems arising from discrete approximations to parabolic partial differential equations. There is a 13-page bibliography.

Contents

1. Matrix properties and concepts

2. Non-negative matrices

3. Basic iterative methods and comparison theorems

4. Successive overrelaxation iterative methods

5. Semi-iterative methods

6. Derivation and solution of elliptic difference equations

7. Alternating direction implicit iterative methods

8. Matrix methods for parabolic partial differential equations

9. Estimation of acceleration parameters

VILENKIN, N. Ya.: Successive Approximation. Macmillan (1964) 70 pp.

This very elementary book is a translation from a 1961 Russian edition. Most methods are explained graphical means, so the book might be of some interest, even for those who could still understand a somewhat more difficult book. There is no index.

Contents

WALSH, J. L.: Interpolation and Approximation by Rational Functions in

the Complex Domain, 2nd ed. Amer. Math. Soc., Colloquium Publications

No. 20 (1956) 398 pp.

This is an advanced treatise. The theoretical aspects of the field
are well covered here.

Contents

1. & 2.: Possiblity of approximation; analytic functions

3. Interpolation and lemniscates

4. Degree of convergence of polynomials; overconvergence

5. Best approximation by polynomials

6. Orthogonality and least squares

7. Interpolation by polynomials

8. Interpolation by rational functions

9. Approximation by rational functions

10. Interpolation and functions analytic in the unit circle

11. Approximation with auxiliary conditions and to nonanalytic functions

12. Existence and uniqueness of rational functions of best approximations

WHITTAKER, E. T. and ROBINSON, G.: The Calculus of Observations, 3rd ed.

Blackie and Son (1940) 395 pp.

This treatise is a little more advanced in parts than some of the more modern texts, but generally it is quite readable. It is often quoted as a reference. There are several chapters discussing the numerical aspects of certain statistical subjects.

Contents

1. Interpolation with equal intervals of the argument
2. Interpolation with unequal intervals of the argument
3. Central differences formulas
4. Applications of difference formulas
5. Determinants and linear equations
6. Numerical solution of algebraic and transcendental equations
7. Numerical integration and summation
8. Normal frequency distributions
9. The method of least squares
10. Practical Fourier analysis
11. Graduation, or the smoothing of data
12. Correlation
13. The search for periodicities
14. The numerical solution of differential equations
15. Further problems

    Summation of slowly convergent series

    Prony's method of interpolation by exponentials

    Interpolation formulas for functions of two arguments

    Numerical computation of double integrals

    Numerical solution of integral equations

    Rayleigh-Ritz method for minimum problems

    Application to the determination of eigenvalues

**WILKINSON, J. H.:   The Algebraic Eigenvalue Problem.   Oxford (1965) 662 pp.

This new book has been eagerly awaited by those who are trying to
solve such problems on digital computers. The subject is rather advanced,
but explanations are in general unusually clear, and the book should be of
great value to knowledgeable engineers and computer programmers as well
as to specialists in the field. The author gives comparative assessments
of various techniques for solving the algebraic eigenvalue problem.

Contents

1. Theoretical background

2. Perturbation theory

3. Error analysis

4. Solution of linear algebraic equations

5. Hermetian matrices

6. Reduction of a general matrix to condensed form

7. Eigenvalues of matrices of condensed forms

8. The LR and QR algorithms

9. Iterative methods

**WILKINSON, J. H.:   <u>Rounding Errors in Algebraic Processes</u>.   Prentice-

Hall (1963) 161 pp.

This definitive text on the subject is of intermediate difficulty.
It is written in such a clear manner that a computer user with some slight
knowledge of numerical analysis could improve his intuitive knowledge on
the effect of round-off in various computing processes without actually
working through all the details of the various proofs. Upper bounds are
given in many cases; the more difficult problem of obtaining a (more
realistic) statistical bound is usually not covered.

<div align="center">Contents</div>

1. Rounding errors in arithmetic operations (for both fixed point and

    floating point cases); ill-conditioned problems

2. Computations involving polynomials

    Evaluation of polynomials; finding zeros of polynomials; ill-conditioned

    polynomials

3. Matrix computations

    Error analysis of simple matrix operations; orthogonalization of

    vectors; solution of systems of linear equations; matrix inversion.

    Error analysis of Gaussian elimination; both floating point and fixed

    point bounds.   Determinant evaluation; solutions of triangular equations;

    inversion of matrices; left-handed and right-handed inverses; use of

    an estimate for $\| A^{-1} \|$; calculation of Eigenvalues and Eigenvectors;

    ill-conditioned Eigenvalues

WILLERS, F. A.: <u>Practical Analysis.</u> Dover (1955) 422 pp.

This is a reasonably elementary treatise on graphical and numerical methods. It is a translation from the German of a 1928 text, but it does, however, have new sections describing American desk calculators, slide rules, etc. There is no discussion of high speed digital computers.

Contents

1. Numerical calculation and its aids (graphs, slide rules, nomograms, calculating machines)

2. Interpolation (interpolation formulas; numerical differentiation and integration; cubature)

3. Approximate integration and differentiation (graphical methods; the planimeter; numerical methods)

4. Practical equation theory (roots of equations and systems of equations)

5. Analysis of empirical function (approximations by linear functions, rational integral functions, periodic functions, and exponential functions)

6. Approximate integration of ordinary differential equations (graphical methods, numerical methods, and mechanical integrators)

ZAGUSKIN, V. L.: Handbook of Numerical Methods for the Solution of

Algebraic and Transcendendental Equations. Pergamon (1961) 195 pp.

This translation from the (1960) Russian edition presents an elementary
exposition of these topics. Digital computer applications are considered
in many of the choices of subject matter which have been made.

General Outline of Contents

1. Introductory material about polynomials and transcendental functions:

    Zeros of a function; basic properties of polynomials; changing the ar-

    gument of a polynomial; polynomials with complex coefficients; al-

    gorithms for multiplication and division of polynomials; Horner's

    method; position of zeros of a polynomial

2. Operations with approximate numbers

    Absolute and relative errors; round off; error in calculating value

    of a polynomial; solution of approximate equation; etc.

3. Methods for approximate determination of roots

    Graphical method; Viet's formulas; Lobachevskii method; Bernoulli

    method; method of iteration; Lin method; Paluver method; comparison

    of methods

4. Methods of increasing the accuracy of roots already found

    Method of linear interpolation; Newton's method; Berstoi's method;

    Belostotskii's method; iteration with quadratic convergence; methods

    of improving convergence; comparison of methods

5. Solution of equations of low orders and extraction of roots

    Quadratic, cubic, quartic, and quintic equations; Newton's method;

    iteration with quadratic convergence

6. Solution of simultaneous equations

    Method of elimination; graphical method; method of iteration; Newton's

    method; method of steepest descent; comparison of methods of solution

    of simultaneous nonlinear equations; methods of solution of simultaneous

    linear equations

ZOUTENDIJK, G.: <u>Methods of Feasible Directions</u>. Elsevier (1960) 127 pp.

     This fairly advanced book explains the author's particular method, which is sometimes used (perhaps in modified form) to solve nonlinear programming problems. There is also some preliminary discussion of other methods for linear or convex programming, but the main use of the book is in explaining the author's own methods.

<div align="center">Contents</div>

<u>Tracts for Computers</u>, I.-   . Cambridge Univ. Press (1919-   ).

These are a series of pamphlets published as "first aid" to the professional computer. They mostly consist of tables, but the five marked below with the symbol † are expository articles on the given subjects.

Titles

I.   Tables of Digamma and Trigamma functions (Pairman, 1919)

† II-III. On the construction of tables and on interpolation (Pearson, 1920)

IV.   Tables of logarithms of the complete Γ function to 12 figures. (Legendre, 1921)

V.   Table of coefficients of Everett's central difference formula (Thompson, 1921)

† VI.   Smoothing (Rhodes, 1921)

† VII.   Numerical evaluation of the incomplete β function or of the integral $\int_{0}^{x} x^{\rho-1}(1-x)^{q-1}\, dx$ for ranges of x between 0 and 1 (Soper, 1921)

VIII.   Table of logarithms of the complete Γ function (for arguments 2-1200, i.e., beyond Legendre's range). (Pearson, 1922)

IX.   Log Γ(x) from x = 1 to 50.9 by intervals of 0.01 (Brownlee, 1923)

†X.   On quadrature and cubature (Irwin, 1923)

XI.   Logarithmetica Britannica, being a standard table of logarithms to 20 decimal places. Part IX, No's. 90,000 to 100,000 (Thompson)

XII.   Tables of probable error of the coefficient of correlation as found by the product moment method (Holzinger, 1925).

XIII.   Biblioteca Tabularum Mathematicarum, being a descriptive catalog of mathematical tables. Part 1, Logarithmic tables (Henderson (1926)

XIV. & XVI. - XXII.: Logarithmetica Britannica, Parts I to VIII, No's. 10,000 to 90,000 (Thompson)

XXIII. Tables of $\tan^{-1}x$ and $\log(1+x^2)$. (Comrie, 1938)

XXIV.   Tables of random sampling numbers (Kendall and Smith, 1939)

XXV.   Random normal deviates (Wold, 1948)

XXVI.   Correlated random normal deviates (Fieller, Lewis, and Pearson (1955)

XXVII. Random negative exponential deviates (Barnett, 1965)

NATIONAL PHYSICAL LABORATORY: <u>Mathematical Tables Series 1 - </u>.   Her

Majesty's Stationery Office.   London (1956-   )

As the title indicates, these pamphlets are mostly tables. However,
the two marked below with the symbol * are mainly expository articles on
the subjects. Also, even if the major portion of a volume is a table,
there is some explanatory material given. The titles in the set are:

*1.   The use and construction of mathematical tables (Fox, 1956)

2.   Tables of Everett interpolation coefficients (Fox, 1958)

3.   Tables of generalized exponential integrals (Miller, 1960)

4.   Tables of Weber parabolic cylinder functions and other functions of
large arguments (Fox, 1960)

†5.   Chebyshev series for mathematical functions (Clenshaw, 1962)

6.   Tables of Bessel functions of moderate or large orders (Olver, 1963)

7.   Tables of Jacobian elliptic functions whose arguments are rational
functions of the quarter period (Curtis, 1964)

**NATIONAL BUREAU OF STANDARDS (U. S. Dept. Commerce): <u>Applied Mathematics</u>

<u>Series 1-58</u> (1948-1964).

These publications are mostly tables. However, No's. 12, 15, 18, 24, 29, 33, 38, 39, 42, 47, 49, 54, and 57 contain only expository articles, and several others (also marked with the symbol †) have considerable explanatory material. This series was set up as a continuation of the previous table series which went from MT1 to MT37. This series and its predecessor are of the highest popularity among computing people.

Titles

1. Tables of the Bessel Functions $Y_0(x), Y_1(x), K_0(x), K_1(x), 0 \leq x \leq 1$. 60 pp.

2. Table of coefficients for obtaining the first derivative without differences (Salzer) 20 pp.

3. Table of the confluent hypergeometric function $F(n/2, 1/2; x)$ and related functions. 73 pp.

4. Tables of scattering functions for spherical particles. 119 pp.

5. Tables of sines and cosines to 15 decimal places at hundredths of a degree. 95 pp.

6. Tables of the binomial probability distribution. 387 pp.

†7. Tables to facilitate sequential t-tests. 82 pp.

8. Table of powers of complex numbers (Salzer) 44 pp.

9. Tables of Chebyshev polynomials $S_n(x)$ and $C_n(x)$. 161 pp.

10. Tables for conversion of x-ray diffraction angles to interplanar spacing. 159 pp.

11. Tables of arctangents of rational functions (Todd) 105 pp.

†12. Monte Carlo method (Proceedings of a symposium conducted in 1949). 42 pp.

13. Tables for the analysis of beta spectra. 61 pp.

14. Tables of the exponential function e^x. 537 pp.

†15. Problems for the numerical analysis of the future (four papers from a 1948 symposium). 21 pp.

16. Tables of $n!$ and $\Gamma(n+1/2)$ for the first thousand values of n (Salzer) 10 pp.

†17. Tables of Coulomb wave functions I. 141 pp.

†18. Construction and application of conformal maps (Proceedings of a symposium conducted in 1949) 280 pp.

†19. Hypergeometric and Legendre functions with applications to integral equations of potential theory (Snow) 427 pp.

†20. Tables for rocket and comet orbits (Herrick) 128 pp.

†21. A guide to tables of the normal probability integral. 16 pp.

†22. Probability tables for the analysis of extreme-value data. 32 pp.

23. Tables of normal probability functions $\dfrac{1}{\sqrt{2\pi}}\,e^{-x/2}$ and $\dfrac{1}{\sqrt{2\pi}}\displaystyle\int_{-x}^{x} e^{-\alpha^2/2}d\alpha$

†24. Introduction to the theory of stochastic processes depending on a continuous parameter (Mann) 45 pp.

25. Tables of the Bessel functions $Y_0(x), Y_1(x), K_0(x), K_1(x), 0 \le x \le 1$. AMS1) 60 pp.

26. Table of arctan x. 17 pp.

27. Tables of 10^x. 543 p.

28. Tables of Bessel-Clifford functions of orders zero and one. 72 pp.

**†29. Simultaneous linear euqations and the determination of eigenvalues (Paige and Taussky) 126 pp.

30. Tables of coefficients for the numerical calculation of Laplace transforms (Salzer) 36 pp.

31. Table of natural logarithms for arguments between zero and five to sixteen decimal places. 501 pp.

32. Table of sine and cosine integrals for arguments from 10 to 100. 187 pp.

†33. The statistical theory of extreme values and some practical applications (Gumbel) 51 pp.

34. Table of the gamma function for complex arguments. 105 pp.

35. Tables of Lagrangian coefficients for sexagesimal interpolation. 157 pp.

36. Tables of circular and hyperbolic sines and cosines. 407 pp.

†37. Tables of functions and zeros of functions. 211 pp.

†38. Magnetic fields of cylindrical coils and annular coils (Snow) 29 pp.

**†39. Contributions to the solution of systems of linear equations and the determination of eigenvalues (Taussky) 139 pp.

40. Tables of secants and cosecants to nine significant figures at hundredths of a degree. 46 pp.

41. Tables of the error function and its derivative. 302 pp.

†42. Experiments in the computation of conformal maps (Todd) 61 pp.

43a. Tables of sines and cosines for radian arguments. 278 pp.

44. Table of salvo kill probabilities for square targets. 33 pp.

45. Table of hyperbolic sines and cosines $x = 2$ to $x = 10$. 81 pp.

46. Table of the descending exponential $x = 2.5$ to $x = 10$. 76 pp.

†47. Contributions on partially balanced incomplete block designs with two associate classes (Clatworthy) 76 pp.

†48. Fractional factorial experiment designs for factors at two levels. 85 pp.

**†49. Further contributions to the solution of simultaneous linear equations and the determination of eigenvalues.

50. Tables of the bivariate normal distribution function and related functions. 258 pp.

51. Tables of the exponential integral for complex arguments. 634 pp.

52. Integrals of airy functions

53. Table of natural logarithms for arguments between five and ten to sixteen decimal places. 506 pp.

†54. Fractional factorial experiment designs for factors at three levels (Conner and Zelen) 37 pp.

**†55. Handbook of Mathematical Functions (Abramowitz and Stegun). 1046 pp.

56. Tables of osculatory interpolation coefficients (Salzer) 25 pp.

**†57. Basic theorems in matrix theory (Marcus) 27 pp.

58. Fractional factorial designs for experiments with factors at two and three levels (Conner and Young, 65 pp.)

(A *double asterisk* ****** by an author's name means that the reference is considered *especially good and/or popular* for the average scientific computer user who is required to learn about the subject.)

PART II.   HOW TO FIND WHAT YOU WANT

These paragraphs are written for those who have had very little
experience in looking up scientific information in the literature, as
well as for the more experienced scientists who are newcomers to the
ranks of computer users. How does one find something in the literature
of this field? How does he find whether there is any literature on a
given numerical subject? How does he find whether or not certain desired
tables exist?

A.   BIBLIOGRAPHIES, LISTS OF BOOKS, ABSTRACTING JOURNALS

1.   General: If one knows absolutely nothing about a subject, he
probably should first see if he can find it discussed in a textbook.
Perhaps Part I of this document would help. For a less specialized but
older listing, one might consider

> PARKE III, N. G.:   Guide to the Literature of Mathematics and
> Physics, Including Related Works in Engi-
> neering Science, 2nd ed. Dover (1958) 436 pp.

This includes references to the periodical literature (in all languages)
as well as to books. There is a short discussion of the literature in
many of the subfields into which the basic subjects have been divided.
A still older list, which has been made up especially for a computer
laboratory, is

> FORSYTHE, G. E.:   "A Numerical Analyst's Fifteen-Foot Shelf,"
> M.T.A.C. 7 (1953) pp. 221-228.

This list includes 150 essential titles under the headings: (1) biblio-
graphies, (2) collections of formulas, (3) references on numerical
methods, (4) references on applied mathematics, (5) references on pure
mathematics. It includes outstanding foreign language references.

2. Abstracting Journals: The best way to be reasonably sure not to
miss out on any possible references is to look through the abstracting
journals in the field. The best known abstracting journals used by com-
puter people are listed on the following page.

**Mathematical Reviews*, Vol. 1- , Amer. Math. Soc., New York
(1940-)

Computer Abstracts, Vol. 1 - , Technical Information Co., Ltd.,
Chancery House, London (1957-)

**Computing Reviews*, Vol. 1 - , Association for Computing Machinery,
(1960-).

New books and periodical articles are reviewed in each of these periodicals. A complete reference as to where to find the article under review is given, and the reviewer tells a little bit about what is in the article or book. *Mathematical Reviews* covers all branches of mathematics and related fields. *Computer Abstracts* and *Computing Reviews* discuss references on computers and related fields. *Computing Reviews* publishes an extremely useful cumulative KWIC index periodically in which all reviewed articles are listed by review number, author, and by subject (key word in title). Some books or articles are reviewed in all three abstracting journals, while others may be reviewed in only one or two of them; it depends on the subject matter.

These abstracting journals are quite complete. For example, if in 1966 a person carefully looks through the yearly indexes of *Mathematical Reviews* for a certain mathematical topic, he has hopes that he has obtained most of the pertinent references to the subject which were published anywhere in the world in the 25-year period, 1939-1964. To make a thorough search of the earlier mathematical literature, one would have to go to the German abstracting journals

Jahrbuch über die Fortschritte der Mathematik, Vol. 1 - 60.
de Gruyter, Berlin (1868-1934)

Zentralblatt fur Mathematik, Vol. 1 - , Springer, Berlin (1931-).

Somewhat off the general subject of this document is the abstracting journal

Quality Control and Applied Statistics, Vol. 1 - . Interscience
and Executive Sciences Inst. (1956-).

This monthly publication includes reviews of some papers discussing linear programming and related subjects. Another similar monthly abstracting journal is

Operations Research/Management Science, Vol. 1 -   . Executive
Sciences Inst. (1961-   ).

3. <u>More Specialized Bibliographies and Annotated Bibliographies</u>. Many
of the books discussed in Part I have very complete bibliographies. There
is a 15-page bibliography on numerical analysis (emphasizing matrices) in
Householder's book (reviewed on p.   ). A supplementary list is given in
the article

> HOUSEHOLDER, A. S.: "Bibliography on Numerical Analysis," *J. of A.C.M.*
> *3,2* (1956) **pp.** 85-100.

A very specialized list is given in the reference,

> STROUD, A. H.: "A Bibliography on Approximate Integration," *Math of*
> *Comp.* *15,73* (1961) pp. 52-80.

This bibliography lists papers dealing with quadrature formulas (using
weighted linear sums of the values of the integrand and possibly deriva-
tives of the integrand) and with finite difference approximations. It
does not list papers on applications to the solution of differential equa-
tions or papers on graphical methods. Another specialized listing is
given in the article

> FORSYTHE, G. E.: "Tentative Classification of Methods and Biblio-
> graphy on Solving Systems of Linear Equations," Appl. Math.
> Series No. 29, <u>Simultaneous Linear Equations and the Determination</u>
> <u>of Eigenvalues</u>. National Bureau of Standards, Washington, D.C.
> (1953).

This 28-page article is an excellent place to start in the detailed study
of this subject. Another specialized listing is given in the book

> SHOHAT, J. A., HILLE, E., and WALSH, J. L.: <u>A Bibliography on</u>
> <u>Orthogonal Polynomials</u>. Bulletin of National Research Council,
> No. 103. Washington, D. C. (1940) 204 pp.

This very cleverly worked out bibliography uses a code symbol system so
as to indicate content and, in many cases, results of individual papers.
There is a short topical index.

The bibliography

YOUDEN, W. W.: Computer Literature Bibliography 1946-1963. National
     Bureau of Standards Misc. Publ. 266 (1965) 463 pp.

lists all papers in 9 journals, 100 proceedings, and 21 multi-author books.
They are listed in three ways: according to source, author, and subject.

A comprehensive earlier annotated bibliography on linear, nonlinear,
and dynamic programming is given in

RILEY, V. and GASS, S. I.: Linear Programming and Associated
     Techniques. Johns Hopkins Press (1958) 613 pp.

A quite recent 20-page listing which covers only the subjects of
Quadratic Programming, Nonlinear Programming, Programming under Uncertainty,
and Integer Programming (and which gives no discussion of the papers) is

COTTLE, R. W., and VAN SLYKE, R. M.: Bibliography on Mathematical
     Programming. Univ. Calif. Operations Research Center Report
     64-6 (RN). (March 1964).

Other works in related fields are reviewed in

BATCHELOR, J. H.: Operations Research, an Annotated Bibliography.
     (1959) 1; (1962) 2; (1963) 3; (1964) 4. St. Louis Acad. Press
     (Vol. 4 includes most references published in 1961).

An earlier bibliography (with no discussion of the papers) is

CASE INSTITUTE OPERATIONS GROUP: Comprehensive Bibliography on
     Operations Research (through 1956 with supplement for 1957).
     Wiley (1958) 188 pp.

A complete bibliography on symbolic logic is found in

CHURCH, A.: "A Bibliography of Symbolic Logic," *J. Sym. Logic 1*
     (1936) pp. 121-218. Additions and corrections, *Ibid. 3* (1938)
     pp. 178-212.

Reviews of later articles have been published each year in the same journal.

4. Indexes of Publications of Particular Groups. There are a large
number of such indexes. For example, there are several volumes (irregu-
larly issued) of

Index of NACA Technical Publications. 1915 - date.

For documents acquired by the Defense Documentation Center, this
organization publishes twice monthly a huge abstracting journal

Technical Abstract Bulletin (TAB).

Indexes and subject indexes to TAB are also available, so that one
has some chance of finding what he wants. We will only list two other
indexes of this general type:

RAND CORP.: Index of Selected Publications of the Rand Corporation,
        Vol. 1 (1946-62)

                Selected Rand Abstracts (yearly), Vol. 1 - . 1963- .

U.S. NATIONAL BUREAU OF STANDARDS: Publications 1901 - June 30, 1947.
        NBS Circular 460, U.S. Govt. Printing Office (1948) 375 pp.
        Supplementary List July 1, 1947 to June 30, 1957, 373 pp.
        Publications of NBS July 1, 1957 to June 30, 1960, 391 pp.
        Supplementary List July 1, 1960 to Feb. 26, 1965, 50 pp.

B. LOOKING FOR TABLES OF VARIOUS FUNCTIONS

There are two major sources where one can get information about
a huge number of tables. FLETCHER, MILLER, and ROSENHEAD (reviewed
on p. 33) is the "bible" in this regard. For the newer tables one
looks in the periodical

> *Mathematics of Computation,* Vol. 14 -   . (Formerly *Mathematical*
> *Tables and Other Aids to Computation (M.T.A.C.),* Vol. 1 - 13)
> National Research Council, Washington D. C. (1943-   ).

It of course takes quite a while to look through all the yearly volumes
of this periodical, but it is the best place to find about tables publi-
shed too recently to be listed in Fletcher, Miller, and Rosenhead.

Other good sources are LEBEDEV and FEDOROVA (reviewed on page 87)
and SCHÜTTE (reviewed on page 126).

For somewhat more specialized (statistical type) tables, one may
consult

> GREENWOOD, J. A. and HARTLEY, H. O.: Guide to Tables in Mathe-
> matical Statistics. Princeton Univ. Press (1962) 1014 pp.

C. KEEPING UP WITH SOME OF THE NEW LITERATURE

Quite often the author has been questioned as to what periodicals he would recommend to a computer programmer who would like to get a little knowledge of what is being done right now in the field of numerical analysis and related topics. This of course depends a lot upon his background and interests. However, we will list some periodicals which we think are most popular among such people. If there are any of these the reader has never seen, it is recommended that he at least look at one copy to see what it is like. Then perhaps he will want to regularly read or glance through one or more of these.

****Mathematics of Computation* (Quarterly)

***Numerische Mathematik* (Quarterly, with about half the articles in English)

***SIAM Journal on Applied Mathematics* (Quarterly)

***SIAM Journal on Numerical Analysis*

SIAM Review (Quarterly)

Journal of the Association for Computing Machinery (Quarterly)

Communications of the Association for Computing Machinery (Monthly)

Computer Journal (Quarterly)

Nordisk Tidskrift for Informations-Behandling (BIT) (Quarterly; with most articles in English)

U.S.S.R. Computational Mathematics and Mathematical Physics (Bimonthly; cover-to-cover translations of a Russian periodical on the subject)

Journal of Mathematics and Physics (Quarterly)

Journal of Research, U. S. National Bureau of Standards (Series B, Mathematics and Mathematical Physics) (Quarterly)

I.B.M. Journal of Research (Quarterly)

** *Mathematical Reviews* (Monthly)

Computer Abstracts (Monthly)

***Computing Reviews* (Bimonthly)

***Current Contents of Space and Physical Sciences* (Weekly)

Those journals marked with a double asterisk are especially recommended. If the author were limited to seeing four periodicals regularly, he would choose *Mathematics of Computation, Numerische*

Mathematik, Siam Journal on Numerical Analysis, and *Computing Reviews.* Many computer people might want to read *Mathematical Reviews* or *Computer Abstracts* as abstracting bibliographies, instead of *Computing Reviews.*

The weekly publication, *Current Contents of Space and Physical Sciences, 1961 -* , contains the contents pages of over 500 foreign and domestic journals. If one took the time to go through this every week, he would have all the new articles brought to his attention quicker than in any other way we know. Most of the magazines are of course on other fields, so it would usually only take five or ten minutes to look through one week's edition for articles of interest to computer people. Of course, the articles are not reviewed here (as they are in *Mathematical Reviews, Computer Abstracts,* or *Computing Reviews*), and one has to judge from the title whether he wants the library to get the actual periodical for him.

PART III.   INDEX

The numbers in this quite limited index refer to the pages of this document. Usually when more than five references are listed for a certain subject, some of the references are *underlined*. If one wishes a single general reference and is overwhelmed with the number of references given, the underlined references might be considered first: they generally contain quite a discussion of the given subject. For references consisting of more than one volume, this index usually includes the volume number. For example, 107v2 refers to vol. 2 of the reference listed on page 107 of this document. As another example, 156 (#39) means vol. 39 of the series described on page 156.

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