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MASSACHUSETTS INSTITUTE OF TECHNOLOGY  
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AN APPROACH TO ESTIMATION  
IN SEISMIC EQUALIZATION

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## ABSTRACT

The "seismic equalization" problem is that of correcting the response at one station to match that at another station which may have different instrument characteristics and different (and unknown) local reverberation characteristics. In this note, the problem of seismic equalization is formulated mathematically, and that portion involving measurement or estimation of a transfer-function ratio is modeled and attacked on statistical terms, first by an ad hoc procedure and then by the method of maximum likelihood.

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correlation can so bias the measurement of  $H_1/H_2$  as to render it void. Fortunately, however, it is wholly reasonable to assume that the correlations, as well as the noise intensities at the two seismometer outputs, are known at all times. This of course requires additional data-processing beyond that implied by the development presented in the following Sections, but hardly more than is already employed at present in sophisticated array work.

We now proceed with a statistical analysis of the problem of measuring the ratio between a pair of transfer functions when noise disturbances are present.































where  $\rho_i = |\rho_i| \exp [j\theta_i]$  and  $E$  is given by (37). [That the asymptotic means are  $R$  and  $\theta$  is verified concurrently. These mean-and-variance results can no doubt be derived directly from (9) and (10) and the assumption of improving estimation conditions ( $E \rightarrow \infty$ ), without any appeal to asymptotic normality, and perhaps even without requiring  $N \rightarrow \infty$ .]













## REFERENCES

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