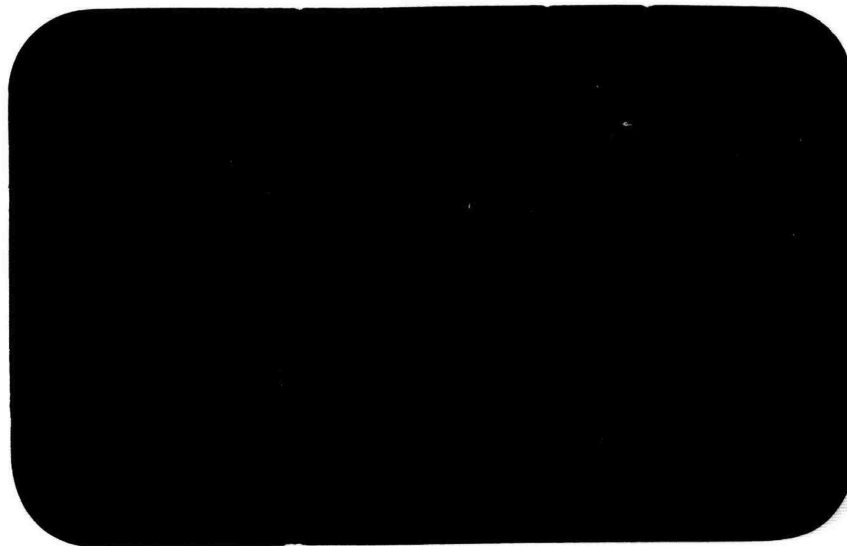


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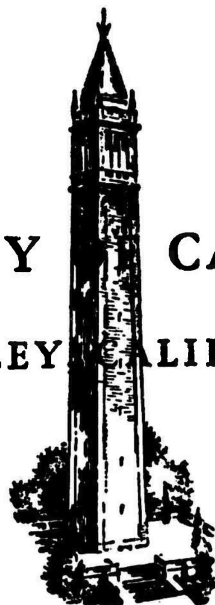
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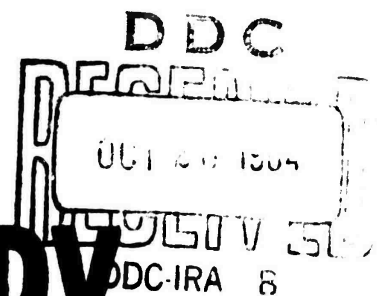
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COMPUTATION OF
GASEOUS DETONATION PARAMETERS

by
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COMPUTATION OF
GASEOUS DETONATION PARAMETERS *

by

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University of California, Berkeley

ABSTRACT

This report describes the development of a method programmed for a digital computer to evaluate one-dimensional detonation parameters in gaseous media. The calculations are based on the assumptions that the mixture is comprised of ideal gas constituents and that the wave process is governed by equilibrium end conditions.

Details of the analytical method of solution are presented including the IBM 7090 computer program, described in Fortran language. Sample input and output data with instructions for preparing the input data are given.

Finally, computations are performed for a number of hydrogen-oxygen mixtures from H_2+O_2 to $3H_2+O_2$ at several initial conditions covering a range in pressure from 0.1 to 760 mm Hg and in temperatures from -180 to +200°F and a comparison is made with calculations of other investigators for a stoichiometric mixture initially at NTP.

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NOMENCLATURE

Dimensional Variables:

- α - sound velocity
- B_{jk} - defined by eq. 6.1.17
- C_{p_i} - molar specific heat of i^{th} species
- C_p - mass specific heat of gaseous mixture
- f_i - defined by eq. 6.1.13
- g_i - molar Gibbs free energy at i^{th} species
- g° - molar Gibbs free energy at i^{th} species at one atmosphere
- h_i - molar enthalpy of i^{th} species
- h - enthalpy per unit mass of the gaseous mixture
- m_i - molecular weight of i^{th} species
- m - molecular weight of gaseous mixture
- n_i - number of moles of i^{th} species
- n - total number of moles of gaseous mixture
- P - pressure
- q_j - mole fraction of j^{th} component in hypothetical system
- R - universal gas constant
- R - specific gas constant
- S - molar entropy per unit mass of the gaseous mixture
- T - absolute temperature
- u - particle velocity relative to the wave
- v - volume per unit mass of the gaseous mixture
- x_i - mole fraction of i^{th} species
- Y_i - chemical symbol denoting the i^{th} species
- Z_j - iteration parameters defined by eq. 6.1.14
- β_{ij} - stoichiometric coefficients for i^{th} chemical reaction
- $\Delta_i h$ - enthalpy change for the i^{th} chemical reaction defined by eq. 6.2.3
- $\Delta_i g$ - Gibbs free energy change for the i^{th} chemical reaction defined by eq. 6.1.15
- γ - specific heat ratio
- μ_i - chemical potential of i^{th} species

Subscripts

- 1 - denotes initial properties upstream of the wave
- 2 - denotes final properties downstream of the wave
- f - denotes properties based on frozen composition
- e - denotes properties based on equilibrium composition

Dimensionless Variables:

$$C - C_p/R_1$$

$$\mathcal{H} - h/R_1 T_1$$

$$\mathcal{M} - m_2/m_1$$

$$M_1 - u_1/a_1$$

$$M_{e,2} - u_2/a_{e,2}$$

$$M_{t,2} - u_2/a_{t,2}$$

$$P - p_2/p_1$$

$$P_{CJ} - \text{pressure ratio at CJ state}$$

$$P_{vN} - \text{pressure ratio at von Neumann spike}$$

$$P_{v=1} - \text{pressure ratio in Hugoniot curve where } V = 1.0$$

$$\Theta = T_2/T_1$$

$$V = v_2/v_1 = u_2/u_1$$

$$V_H - V \text{ evaluated from Hugoniot equation at given } P \text{ and approximate } T$$

$$V_R - V \text{ evaluated on Rayleigh line at given } P$$

$$V_{RH} - V \text{ evaluated on Rankine-Hugoniot curve at given } P$$

$$V_s - V \text{ evaluated from equation of state at given } P \text{ and } \Theta$$

$$\Delta\Theta - \text{correction to } \Theta \text{ at specified } P \text{ on Hugoniot curve}$$

$$\Delta P_{CJ} - \text{correction to } P_{CJ}$$

$$\Delta P_{vN} - \text{correction to } P_{vN}$$

$$\Delta P_{v=1} - \text{correction to } P_{v=1}$$

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1. INTRODUCTION

The calculations of detonation parameters have been made by several investigators, notably Lewis and Friauf (1), Berets et al (2), Edse (3), Wolfson and Dunn (4), Luker et al (5), Eisen et al (6), Bollinger and Edse (7), Barrere's (8), Gordon and Zeleznik (9), and Bird et al (10).

The distinguishing features of the various analyses are summarized in Table 1. All have in common two basic assumptions, namely that complete thermodynamic and chemical equilibrium is established immediately downstream of the wave, so that dissipative effects and variations in chemical reaction rates can be disregarded, and that the constituents of both reactants and products behave as perfect gases.

The work in references (1), (2), (4), and (5) followed similar approaches and in particular, specified the CJ state as that for which the final Mach number, based on the frozen sound speed, was equal to unity. Lewis and Friauf made use of this condition in their equations and proceeded to calculate detonation properties by determining successive corrections to the assumed initial values of the independent variables, T_2 and v_2 using an iterative technique. Berets et al (2) used the same method, while Wolfson and Dunn (3) and Luker et al (4) performed the calculations in a similar manner but with T_2 and p_2 as the independent variables.

It was subsequently shown, however, that the correct specification of the CJ state must be based on the equilibrium sound speed. This problem was circumvented by Edse (3) and Bollinger and Edse (7) who determined the CJ state from the condition that the corresponding wave Mach number is a minimum. An initial estimate was made for the CJ value of the final temperature in both cases, the corresponding properties on the Hugoniot curve evaluated, and then corrections to the CJ temperature found. This is essentially the approach used by Eisen et al (6) who chose, however, M_1 as the independent

parameter. The latter method gave double-valued solutions for each value of M_1 , and the CJ state was determined when both solutions converged, yielding the minimum wave Mach number. In addition, Eisen et al (6) were the first to evaluate the final equilibrium Mach number as a check on their CJ calculations.

Barrere (8) developed a graphical method for calculating detonation properties which gave results in good agreement with those of Eisen et al (6). The CJ state in this instance was defined as the point on the Hugoniot curve at which the entropy was a minimum. Incorporating this into the conservation equations, T_2 and p_2 were used as the independent variables to evaluate the CJ properties.

Zelevnik et al (9) were the first to actually utilize in their computations the principle that at the CJ state the equilibrium Mach number is unity. On this basis initial estimates were made for the independent variables p_2 and T_2 and corrections found until the Hugoniot equation and equation of state were satisfied.

Bird et al (10) computed the CJ properties by finding the point of minimum wave Mach number. Since the thermodynamic properties are functions of the final temperature, T_2 , alone, this parameter was chosen as the independent variable, eliminating the need for re-evaluation of these properties at each iteration. The program is generalized to include the presence of condensed phases in the products of reaction.

In the present work, a method was developed for the determination of detonation and deflagration parameters including, in addition to the CJ state, solutions on both the deflagration and detonation branches of the Hugoniot curve. The procedure was programmed for an IBM 7090 digital computer in Fortran language. For detonations the calculations are terminated when states with pressure ratios corresponding to the von Neumann spike on the one end,

and the condition that the density ratio is equal to unity on the other, are attained. For deflagrations, the calculations are restricted, of course, to values of the pressure ratio equal to and less than unity. It should be noted also that since the allowable chemical reactions are specified in the input data, the parameters for other processes, such as non-reactive or dissociative waves, may be easily determined.

During the initial phases of this study, the wave velocity was chosen as the independent variable, following the approach used by several other investigators. For each specification of the velocity, then, solutions on both the strong and weak branches of the Hugoniot curve were obtained and the CJ state determined when the solutions converged at the minimum value of wave velocity. However, difficulties in obtaining convergence within a desired accuracy were encountered and it has been then found that the most convenient independent variable is the pressure ratio.

Since the thermodynamic properties of each constituent are uniquely functions of the temperature alone, the temperature ratio suggests itself as a convenient independent variable. However, as shown in Figs. 10 and 11, where temperature and pressure ratios are plotted respectively against the dimensionless entropy, the variation in the pressure ratio is about ten times greater than that in the temperature ratio along the Hugoniot curve, so that choosing the pressure ratio as the independent variable allows greater latitude in making an initial estimate of its value at the CJ state.

The CJ state was specified by the condition that the local equilibrium Mach number is equal to unity which, within the accuracy of calculations, corresponds exactly to the state of minimum wave velocity.

Calculations of detonation parameters were carried out for several hydrogen-oxygen mixtures over the range of initial conditions as follows:

Composition	Initial Pressure mmHg	Initial Temperature °F
$\text{H}_2 + \text{O}_2$	760	-180
		-50
	100	+60
		+200
	10	
$2\text{H}_2 + \text{O}_2$		-180
	1	+60
$3\text{H}_2 + \text{O}_2$		-180
	0.1	+60

The best available source of thermodynamic data, namely the JANAF Tables (11) prepared by the Dow Chemical Company, was used in the calculations. Within the accuracy of these data, the results for the CJ wave were found to be in good agreement with those of references 6, 8, and 9 obtained for similar conditions. In addition the CJ wave velocity exhibits an increase, independently of composition, of approximately 15 percent as the initial pressure was increased from 0.1 to 760 mmHg, and a decrease of approximately 3 percent as the initial temperature was increased from -180 to +200°F. Over the same range of initial conditions, the CJ pressure and temperature ratios were found to be more sensitive functions of the initial temperature than of the initial pressure.

2. DETERMINATION OF THE HUGONIOT CURVE

The detonation wave is considered to be a one-dimensional front and the process to take place in the absence of dissipative effects so that the simple continuity, momentum, and energy equations apply. The conditions of the initial gas mixture, including its composition, are assumed to be known, while the thermodynamic properties of each constituent of both the initial mixture and final products must be specified as input data. Each gas species is assumed to obey the ideal gas law so that the thermodynamic data of each species can be expressed conveniently in the form of a polynomial expansion in terms of the temperature. Any number of chemical reactions may be considered in the equilibrium system, including the case of no chemical reaction, corresponding to the Rankine-Hugoniot curve.

The final conditions of the wave are determined from a solution to the conservation equations and the equilibrium equation of state. The equations expressing conservation of mass, momentum, and energy respectively are:

$$\frac{u_1}{v_1} = \frac{u_2}{v_2} \quad 2.1$$

$$p_2 - p_1 = \frac{u_1^2}{v_1} - \frac{u_2^2}{v_2} \quad 2.2$$

$$h_2 - h_1 = \frac{1}{2}(u_1^2 - u_2^2) \quad 2.3$$

where u is the particle velocity, v the specific volume, p the pressure, and h the enthalpy while subscripts 1 and 2 denote initial and final states of the wave, respectively. The enthalpies in the energy equation are evaluated by means of a simple summation procedure:

$$h = \sum_i x_i h_i / m \quad 2.4$$

where the X_i , the mole fractions of the i^{th} species, are determined for state 1 from the specified composition of the initial mixture and for state 2 from the composition corresponding to local thermodynamic equilibrium. The mean molecular weight is a weighted average of the molecular weights, m_i , of the i^{th} species given by the relation:

$$m = \sum_i X_i m_i \quad 2.5$$

and h_i , the molar enthalpy of the i^{th} species, can be expressed as:

$$h_i = h_i^0 + \int_{T_0}^T c_{p_i} dT \quad 2.6$$

where h_i^0 is the enthalpy of formation at a reference temperature T_0 and c_{p_i} is the specific heat of the i^{th} species.

The conservation equations, eqs. (2.1), (2.2) and (2.3), can be combined to yield the well-known Hugoniot equation:

$$h_2 - h_1 = \frac{1}{2} (p_2 - p_1) (v_2 + v_1) \quad 2.7$$

which, expressed in dimensionless terms, has the form:

$$\mathcal{H}_2 - \mathcal{H}_1 = \frac{1}{2} (P - 1) (V + 1) \quad 2.8$$

where P is the pressure ratio, p_2/p_1 , V the volume ratio, v_2/v_1 and $\mathcal{H}$ is the dimensionless enthalpy defined as:

$$\mathcal{H} = \frac{h}{R_1 V_1} = \frac{h}{R_1 T_1} \quad 2.9$$

where T is the temperature and R , the specific gas constant, is expressed in terms of the universal gas constant $\mathcal{R}$ and the mean molecular weight:

$$R = \mathcal{R}/m \quad 2.10$$

The equation of state of the medium behind the wave can be written as:

$$P_2 V_2 = R_2 T_2 \quad 2.11$$

In dimensionless form, eq. (2.11) becomes

$$P V = \Theta / \mathcal{M} \quad 2.12$$

where Θ and $\mathcal{M}$ are respectively the temperature and molecular weight ratios, T_2/T_1 and m_2/m_1 , across the wave.

Since it is most convenient to work in the specific volume-temperature plane, eqs. (2.8) and (2.12) can be rearranged to yield the following expressions:

$$V = 2(\mathcal{K}_2 - \mathcal{K}_1) / (P - 1) - 1 \quad 2.13$$

$$V = \Theta / (P \mathcal{M}) \quad 2.14$$

Both $\mathcal{K}_2$ and $\mathcal{M}$ can be determined, of course, once P and Θ are known; hence, by specifying a value of P , solutions to eqs. (2.13) and (2.14) can be found as shown in Fig 1. The intersection of the equation of state (2.14) and the Hugoniot equation (2.13), which represents a solution point, i. e., a point on the Hugoniot curve corresponding to final conditions of the wave, is found in the following manner. An initial choice is made for Θ and, at the specified P , the equilibrium composition and corresponding thermodynamic properties are calculated. If the initial choice of Θ was correct, then eqs. (2.13) and (2.14) would be satisfied simultaneously within the prescribed accuracy. If not, a correction to Θ , $\Delta\Theta$, is obtained by expansion of eqs. (2.13) and (2.14) in terms of a Taylor series about the initial approximation to Θ . Equating the resulting expansions and retaining only first order terms, we obtain then:

$$\Delta\Theta = (V_H - V_S) / \left[\left(\frac{\partial V}{\partial \Theta} \right)_{P,S} - \left(\frac{\partial V}{\partial \Theta} \right)_{P,H} \right] \quad 2.15$$

where V_H and V_S are the volume ratios evaluated from the Hugoniot equation and equation of state respectively at the specified P and previous value of Θ . Differentiating eqs. (2.13) and (2.14) with respect to Θ at constant P yields, respectively:

$$\left(\frac{\partial V}{\partial \Theta}\right)_{P,H} = \frac{2C}{P-1} \quad 2.16$$

$$\left(\frac{\partial V}{\partial \Theta}\right)_{P,S} = \frac{M}{P} \left\{ 1 - \left(\frac{\partial \log M}{\partial \log \Theta}\right)_P \right\} \quad 2.17$$

where $C = \frac{C_p}{R_1}$ is the non-dimensional equilibrium specific heat at constant P and the subscripts H and S denote differentiation in the V - Θ plane along the path of the Hugoniot equation and along the path of the equation of state respectively. The derivation of equation (2.17) is given in section 6.5. Successive corrections are made to the temperature, Θ , until the values of V computed from eqs. (2.13) and (2.14) agree within a prescribed accuracy.

Eqs. (2.13) and (2.14) can also be solved by choosing Θ as the independent variable and iterating for the correct value of P .

Eq. (2.15) then becomes

$$\Delta \Theta = (V_H - V_S) \left[\left(\frac{\partial V}{\partial P}\right)_{\Theta,S} - \left(\frac{\partial V}{\partial P}\right)_{\Theta,H} \right] \quad 2.18$$

where the subscripts H and S now refer to differentiation in the V - P plane along the Hugoniot equation and the path of the equation of state respectively. For this case eqs. (2.16) and (2.17) become respectively

$$\left(\frac{\partial V}{\partial P}\right)_{\Theta,H} = 2 \left[(P-1) \left(V - \frac{\partial V}{\partial \ln \Theta} \right) - (\gamma_2 - \gamma_1) \right] / (P-1)^2 \quad 2.19$$

$$\left(\frac{\partial V}{\partial P}\right)_{\Theta,S} = - \frac{V}{P} \left\{ 1 + \left(\frac{\partial \log M}{\partial \log P}\right)_\Theta \right\} \quad 2.20$$

Eq. (2.19) is obtained by straightforward differentiation of eq. (2.13), while eq. (2.20) is derived in section 6.5. Fig. 2 shows the solution for a point on the Hugoniot curve in the V - P plane. The initial conditions are the same as those of Fig. 1 and the value of Θ , Fig. 2, was chosen so that both solutions correspond to some point on the Hugoniot curve. A comparison of Figs. 1 and 2 shows that the Hugoniot equation and equation of state are nearly orthogonal in the V - Θ (constant pressure) plane while in the V - P (constant temperature) plane they are almost parallel. Hence, in addition to a wider latitude for the initial choice of the independent parameter, choosing P , rather than Θ , as the dependent variable should minimize problems associated with convergence.

For purposes of illustration, Fig. 3 shows the Hugoniot curve for a $2H_2 + O_2$ mixture initially at $60^\circ F$ and 1 atmosphere in the P - V plane. Shown also is the CJ Rayleigh line whose intersection with the Rankine-Hugoniot curve defines the von Neumann spike.

3. DETERMINATION OF THE CHAPMAN JOUGUET STATE

The CJ state is defined as that state at which the final equilibrium Mach number is equal to unity. It is determined by finding the intersection of the Hugoniot curve with the line $M_{e,2} = 1$, in the $M_{e,2}$ - P plane. Fig. 4 shows the Hugoniot curve in the $M_{e,2}$ - P plane for a $2H_2 + O_2$ mixture initially at $60^\circ F$ and 1 atmosphere, and the line $M_{e,2} = 1$. The CJ state is determined by making an initial guess for the CJ pressure, P_{CJ} , linearizing the Hugoniot curve in the $M_{e,2}$ - P plane, and solving for corrections in the initial choice of P_{CJ} . At each approximate value of P_{CJ} , the corresponding properties on the Hugoniot curve are evaluated by the method described in the previous section.

While previously it was possible to find analytical expressions for the derivatives of the governing equations, a numerical method must be used here. The derivative of the Hugoniot curve in the $M_{e,2}$ - P plane is found by taking a small increment, δP , in the previous estimate of P_{CJ} and evaluating the corresponding incremental change in $M_{e,2}$, $\delta M_{e,2}$. Hence, to a good approximation, the derivative of the Hugoniot curve in the $M_{e,2}$ - P plane is given by $\frac{\delta M_{e,2}}{\delta P}$, and it can be easily verified that the correction ΔP_{CJ} is given by

$$\Delta P_{CJ} = (1 - M_{e,2}) / (\delta M_{e,2} / \delta P) \quad 3.1$$

It is advisable to overestimate the initial approximation to P_{CJ} in order to insure that the corresponding value of V on the Hugoniot curve will be less than one. The stability of the iteration procedure is improved by requiring that

$$|\Delta P_{CJ}| < 1 \quad 3.2$$

which should prevent the new approximation to P_{CJ} from becoming too small and yielding an imaginary wave velocity. The iteration is continued until the value of $M_{e,2}$ is sufficiently close to one, so that ΔP_{CJ} is less than a prescribed value.

4. DETERMINATION OF THE VON NEUMANN SPIKE

The von Neumann spike conditions correspond to the properties behind a non-reactive shock wave which propagates at a Mach number equal to that of the CJ detonation. In this report the von Neumann spike is used to establish the upper limit to the Hugoniot curve. The state in the P - V plane corresponding to the von Neumann spike is determined by the intersection of the Rayleigh line, which emanates from the initial state and is tangent to the Hugoniot curve, with the Rankine-Hugoniot curve. Fig. 3 illustrates the solution for the case of a $2\text{H}_2\text{O} + \text{O}_2$ mixture initially at 60°F and 1 atmosphere. The iterative technique used in the method of solution is similar to that outlined in section 3. An initial guess is made for P_{VN} , the von Neumann spike pressure ratio and the equations of the Rayleigh line and Rankine-Hugoniot curve are linearized permitting corrections to be found to the initial choice of P_{VN} .

It is necessary to know the value of the derivatives, $\frac{\partial V}{\partial P}$, along both the Rankine-Hugoniot curve and the Rayleigh line in the P - V plane, in order to linearize the equations describing these curves. The first, $\left(\frac{\partial V}{\partial P}\right)_{RH}$, is found by taking a small increment in P , δP , and evaluating the corresponding increment in V , δV ; the ratio $\frac{\delta V}{\delta P}$, yields, then, a sufficiently good approximation to the derivative, $\left(\frac{\partial V}{\partial P}\right)_{RH}$. The second, $\left(\frac{\partial V}{\partial P}\right)_R$, is invariant and may be found analytically. The dimensionless Rayleigh line equation is given by:

$$(P-1) = \gamma_1 M_1^2 (1-V) \quad 4.1$$

where γ_1 , and M_1 are, respectively, the initial specific heat ratio and Mach number. Since both γ_1 and M_1 remain constant along the Rayleigh line, differentiation of eq. (4.1) yields:

$$\left(\frac{\partial V}{\partial P}\right)_R = -\frac{1}{\gamma_1 M_1^2} \quad 4.2$$

An initial approximation to the von Neumann spike pressure, P_{VN} , is made and at this pressure, the required derivatives are evaluated as outlined above. It can easily be verified that the correction to the approximation of P_{VN} is given by:

$$\Delta P_{VN} = (V_R - V_{RH}) / \left(\left(\frac{\delta V}{\delta P} \right)_{RH} + \frac{1}{\gamma_i M_i^2} \right) \quad 4.3$$

where V_{RH} and V_R are, respectively, the values of the volume ratio evaluated from the equations for the Rankine-Hugoniot curve and Rayleigh line at the previous value of P_{VN} . The iteration is continued until V_{RH} is sufficiently close to V_R so that ΔP_{VN} is less than a prescribed value.

5. DETERMINATION OF THE POINT ON THE HUGONIOT CURVE AT $V = 1.0$

The pressure ratio, $P_{V=1}$, corresponding to the point on the Hugoniot curve where $V=1$ is used to establish the lower limit of the Hugoniot curve. It is determined by the intersection, in the $\mathcal{H}_2$ - P plane, of the Hugoniot curve with a line of 45° slope passing through the point $\mathcal{H}_2 = \mathcal{H}_1 - 1$, $P = 0$, corresponding to the Hugoniot equation with $V=1.0$. The two equations are then:

$$\mathcal{H}_2 = \mathcal{H}_1 + \frac{1}{2}(P - 1)(V + 1) \quad 5.1$$

$$\mathcal{H}_2 = \mathcal{H}_1 + (P - 1) \quad 5.2$$

Similar techniques are employed to solve eqs. (5.1) and (5.2) as that used in sections 2, 3, and 4. An initial approximation is made for $P_{V=1}$, the two equations (5.1) and (5.2) are linearized at this value of $P_{V=1}$, and a correction found for the initial guess.

The derivative of eq. (5.1) in the $\mathcal{H}$ - P plane is found by taking a small increment δP in the approximate $P_{V=1}$ and evaluating the corresponding increment in $\mathcal{H}_2$, $\delta \mathcal{H}_2$. Hence a good approximation to the derivative of eq. (5.1) is given by $\frac{\delta \mathcal{H}_2}{\delta P}$. The derivative of eq. (5.2) is obviously equal to one. It can be easily verified then that the correction to the initial approximation of $P_{V=1}$ is given by:

$$\Delta P_{V=1} = (\mathcal{H}_{2_H} - \mathcal{H}_{2_{V=1}}) / (1 - \frac{\delta \mathcal{H}_2}{\delta P}) \quad 5.3$$

where $\mathcal{H}_{2_H}$ and $\mathcal{H}_{2_{V=1}}$ are evaluated from eqs. (5.1) and (5.2) respectively at the approximate $P_{V=1}$.

The iteration is continued again until $\mathcal{H}_{2_{V=1}}$ is sufficiently close to $\mathcal{H}_{2_H}$, that $\Delta P_{V=1}$ is less than a prescribed value.

6. EVALUATION OF EQUILIBRIUM COMPOSITION AND EQUILIBRIUM THERMODYNAMIC DERIVATIVES

The preceding analysis requires the evaluation of the equilibrium composition of a multicomponent mixture of gases at a specified temperature and pressure. Brinkley (12) has developed a convenient method for equilibrium calculations for use in machine computation, and this procedure has been adopted for our work.

6.1 Equilibrium Composition

Following Brinkley (12) and Obert (14), we shall consider the products to consist of a certain number of species, referred to as constituents, of which a certain minimum number are components. The distinction between constituents and components is derived from the fact that in a closed system at a given pressure and temperature in which departures from equilibrium are considered, a component is defined as an independent variable while a constituent is defined as a dependent variable. (In an equilibrium system at a given pressure and temperature, the composition is fixed and hence the components may not be varied independently). For example, consider a closed system in which H_2 , O_2 , and H_2O are present at a given pressure and temperature. Any two of the three constituents may be considered as components. Formal rules for selecting components were given by Brinkley (13).

The constituents of the equilibrium system can be expressed symbolically in terms of the components in the following form:

$$Y_i = \sum_j \beta_{ij} Y_j \quad 6.1.1$$

where Y_i designates the chemical symbol of the i^{th} constituent, Y_j - the chemical symbol of the j^{th} component, and β_{ij} are the stoichiometric coefficients. In this section, i subscripts refer to constituents and j and k

subscripts refer to components. For example, consider the hydrogen-oxygen system in which six constituents are assumed present, namely, H_2 , O_2 , H_2O , OH , H , and O , and let the components be H_2O and O_2 . Then the matrix formed by the β_{ij} 's is:

Components ↓ Constituents →	H_2O	O_2
H_2	1.00	-0.50
O_2	0.00	1.00
H_2O	1.00	0.00
OH	0.50	0.25
H	0.50	0.25
O	0.00	0.50

The composition of the initial mixture determines the mole fraction of each component in a hypothetical system consisting of components only. The mass balance between the hypothetical system and the equilibrium constituents is expressed then by the relationship:

$$\sum \beta_{ij} n_i = q_j \quad 6.1.2$$

where n_i is the number of moles of the i^{th} constituent in the equilibrium system derived from the hypothetical system. The mass action relations for the system under consideration can be expressed as:

$$\mu_i = \sum_j \beta_{ij} \mu_j \quad 6.1.3$$

where μ_i and μ_j are the chemical potentials of the i^{th} constituent and j^{th} component respectively.

Dividing eq. (6.1.2) by n , where

$$n = \sum_i n_i \quad 6.1.4$$

leads to:

$$\sum_j \beta_{ij} x_i = q_{ij}/n \quad 6.1.5$$

which, when summed over the j components, becomes after rearrangement:

$$\frac{1}{n} = 1 + \sum_i (\beta_i - 1) x_i \quad 6.1.6$$

where β_i is defined by the relation:

$$\beta_i = \sum_j \beta_{ij} \quad 6.1.7$$

Substituting eq. (6.1.6) into eq. (6.1.5) yields finally:

$$\sum_i (\beta_{ij} - (\beta_i - 1) q_{ij}) x_i = q_{ij} \quad 6.1.8$$

A quantity G_j can be defined now as the residue of eq. (6.1.8), i.e.,

$$G_j = \sum_i (\beta_{ij} - (\beta_i - 1) q_{ij}) x_i - q_{ij} \quad 6.1.9$$

where G_j is identically zero when the correct set of x_i are substituted into eq. (6.1.9).

The chemical potential of the i^{th} ideal gas constituent may be written in the form:

$$\mu_i = \mu_i^\circ + RT \log(p x_i) \quad 6.1.10$$

where μ_i° is the chemical potential of the i^{th} constituent at the temperature in question and one atmosphere. Note that the chemical potential of a pure species is equal to the Gibbs free energy per mole. Hence, for this case:

$$\mu_i^o = g_i^o \quad 6.1.11$$

where g_i^o is the molar Gibbs free energy of the i^{th} constituent. Substituting eq. (6.1.10) into eq. (6.1.3) and rearranging terms yields:

$$\log(x_i) = f_i(p, T) - \sum_j \beta_{ij} z_j \quad 6.1.12$$

where

$$f_i(p, T) = -\log(p) - \Delta_i g^o / RT \quad 6.1.13$$

and z_j , the iteration parameter, has the formal definition:

$$z_j = -\log(p) - \log(x_j) \quad 6.1.14$$

The quantity, $\Delta_i g^o$, used in eq. (6.1.13) is defined by the relation:

$$\Delta_i g^o = g_i^o - \sum_j \beta_{ij} g_j^o \quad 6.1.15$$

Now an initial guess must be made for z_j . Then substituting the value of x_i from eq. (6.1.12) into eq. (6.1.9), expanding the resulting equation in a Taylor series about the approximate set of z_j , and retaining only first order terms, one obtains a set of linear equations of the form:

$$\sum_k B_{jk} \Delta z_k = G_j \quad 6.1.16$$

where

$$B_{jk} = \sum_i (\beta_{ij} - (\beta_i - 1) q_{ij}) \beta_{ik} x_i \quad 6.1.17$$

and Δz_k are the correction terms for the initial choice of z_j . With the new values of z_j , the procedure is repeated and the iteration continued to the desired accuracy.

6.2 Evaluation of the Derivatives $\left(\frac{\partial \log x_i}{\partial \log T}\right)_p$ and $\left(\frac{\partial \log x_i}{\partial \log p}\right)_T$

Differentiating eq. (6.1.12) with respect to $\log(T)$ at constant p one obtains:

$$\left(\frac{\partial \log x_i}{\partial \log T}\right)_p = \frac{\Delta_i h}{RT} - \sum_j \beta_{ij} \left(\frac{\partial z_j}{\partial \log T}\right)_p \quad 6.2.1$$

where we have made use of the thermodynamic relation

$$\left(\frac{\partial \Delta_i g^0/T}{\partial \log T}\right)_p = -\frac{\Delta_i h}{T} \quad 6.2.2$$

and $\Delta_i h$ is defined as:

$$\Delta_i h = h_i - \sum_j \beta_{ij} h_j \quad 6.2.3$$

Taking the derivative of eq. (6.1.8) with respect to $\log(T)$ at constant p , where the correct set of x_i have been used, and substituting eq. (6.2.1) into the resulting expression yields:

$$\sum_k B_{jk} \left(\frac{\partial z_k}{\partial \log T}\right)_p = \sum_i (\beta_{ij} - (\beta_i - 1)q_j) x_i \Delta_i h / (RT) \quad 6.2.4$$

which gives a set of simultaneous equations from which the set of derivatives $\left(\frac{\partial z_k}{\partial \log T}\right)_p$ may be determined, allowing, finally, the evaluation of the set of derivatives $\left(\frac{\partial \log x_i}{\partial \log T}\right)_p$ from eq. (6.2.1)

The set of derivatives $\left(\frac{\partial \log x_i}{\partial \log p}\right)_T$ may be derived in a similar manner.

Differentiating eq. (6.1.12) with respect to $\log(p)$ at constant T we have now:

$$\left(\frac{\partial \log x_i}{\partial \log p}\right)_T = -1 - \sum_j \beta_{ij} \left(\frac{\partial z_j}{\partial \log p}\right)_T \quad 6.2.5$$

while taking the derivative of eq. (6.1.8) with respect to p at constant T , where again the correct set of x_i have been used, and substituting eq. (6.2.5) into the resulting expression we obtain finally:

$$\sum_k B_{jk} \left(\frac{\partial z_k}{\partial \log p}\right)_T = -q_j \quad 6.2.6$$

This provides a set of simultaneous equations from which the set of derivatives

$$\left(\frac{\partial \bar{z}_i}{\partial \log p}\right)_T \quad \text{may be determined. Consequently, the derivatives } \left(\frac{\partial \log x_i}{\partial \log p}\right)_T$$

may be evaluated from eq. (6.2.5).

6.3 Partial Derivatives of Molecular Weight

The partial derivatives of the molecular weight can be expressed most conveniently in terms of the partial derivatives of the mole fractions. Making use of a mathematical identity, we can write:

$$\left(\frac{\partial \log m}{\partial \log T}\right)_p = \frac{1}{m} \left(\frac{\partial m}{\partial \log T}\right)_p \quad 6.3.1$$

With the use of eq. (2.5), where m_i is, of course, a constant, we obtain:

$$\left(\frac{\partial \log m}{\partial \log T}\right)_p = \sum_i \frac{m_i x_i}{m} \left(\frac{\partial \log x_i}{\partial \log T}\right)_p \quad 6.3.2$$

Similarly, it can be shown that:

$$\left(\frac{\partial \log m}{\partial \log p}\right)_T = \sum_i \frac{m_i x_i}{m} \left(\frac{\partial \log x_i}{\partial \log p}\right)_T \quad 6.3.3$$

6.4 Evaluation of Equilibrium Specific Heat

The equilibrium specific heat per unit mass is denoted by the expression $\left(\frac{\partial h}{\partial T}\right)_p$ where

$$h = \sum_i \frac{x_i h_i}{m} \quad 6.4.1$$

Performing the indicated differentiation yields then:

$$C_{pe} = \sum_i \frac{x_i}{m} \left(\frac{\partial h_i}{\partial T}\right)_p + \sum_i h_i x_i \left(\frac{\partial \log x_i}{\partial \log T}\right)_p + \sum_i \frac{h_i x_i}{m} \left(\frac{\partial \log x_i}{\partial \log p}\right)_p \quad 6.4.2$$

where the first term on the right hand side represents the frozen composition specific heat per unit mass, C_{pf} . Expressing the derivatives in logarithmic form we have:

$$C_{pe} = C_{pf} - \sum_i \frac{h_i x_i}{m T} \left(\frac{\partial \log m}{\partial \log T}\right)_p + \sum_i \frac{h_i x_i}{m T} \left(\frac{\partial \log x_i}{\partial \log T}\right)_p \quad 6.4.3$$

Note that for the case of frozen composition, the derivatives on the right hand side of eq. (6.4.3) vanish, leading to the identity that $C_{pe} = C_{pf}$.

6.5 Evaluation of Thermodynamic Derivatives $(\frac{\partial v}{\partial T})_p$ and $(\frac{\partial v}{\partial p})_T$

Differentiation of the ideal gas equation of state with varying molecular weight yields:

$$(\frac{\partial v}{\partial T})_p = \frac{R}{pm} (1 - (\frac{\partial \log m}{\partial \log T})_p) \quad 6.5.1$$

and

$$(\frac{\partial v}{\partial p})_T = -\frac{v}{p} (1 + (\frac{\partial \log m}{\partial \log p})_T) \quad 6.5.2$$

These relations are necessary to evaluate the equilibrium sound velocity and specific heat ratio, while eq. (6.5.1) has already been used in section 2.

The derivatives on the right hand side of the equations have been determined already in section 6.3.

6.6 Evaluation of the Equilibrium Specific Heat Ratio

The equilibrium specific heat ratio, γ_e , is defined as:

$$\gamma_e = \frac{C_{pe}}{C_{ve}} \quad 6.6.1$$

which upon substituting the well-known specific heat equation:

$$C_{pe} - C_{ve} = -T (\frac{\partial v}{\partial T})_p^2 / (\frac{\partial v}{\partial p})_T \quad 6.6.2$$

becomes:

$$\gamma_e = \frac{C_{pe}}{C_{pe} + T (\frac{\partial v}{\partial T})_p^2 / (\frac{\partial v}{\partial p})_T} \quad 6.6.3$$

Substituting now eqs. (6.5.1) and (6.5.2) into (6.6.3) and rearranging terms we obtain finally:

$$\gamma_e = \frac{C_{pe}}{C_{pe} - \frac{R}{m} [1 - (\frac{\partial \log m}{\partial \log T})_p]^2 / [1 + (\frac{\partial \log m}{\partial \log p})_T]} \quad 6.6.4$$

Note that for frozen composition, the derivatives of the molecular weight, m , vanish so that

$$\gamma_e = \gamma_f = \frac{c_{pf}}{c_{pf} - R/m} \quad 6.6.5$$

6.7 Evaluation of Equilibrium Sound Velocity

The equilibrium sound velocity is given by:

$$a_e^2 = \left(\frac{\partial p}{\partial \rho} \right)_s \quad 6.7.1$$

The above can be expressed in terms of p, v , and T and the specific heat data by a number of ways. One is by the use of the specific heat ratio

$$\gamma_e = \frac{c_{pe}}{c_{ve}} \quad 6.7.2$$

Now $c_{pe} = T \left(\frac{\partial s}{\partial T} \right)_p$ and $c_{ve} = T \left(\frac{\partial s}{\partial T} \right)_v$ so that eq. (6.7.2) becomes

$$\gamma_e = \left(\frac{\partial s}{\partial T} \right)_p / \left(\frac{\partial s}{\partial T} \right)_v \quad 6.7.3$$

Since, by the partial derivative relation between three variables,

$$\left(\frac{\partial s}{\partial T} \right)_p = - \left(\frac{\partial T}{\partial p} \right)_s \left(\frac{\partial s}{\partial p} \right)_T \quad 6.7.4$$

and

$$\left(\frac{\partial s}{\partial T} \right)_v = - \left(\frac{\partial v}{\partial T} \right)_s \left(\frac{\partial s}{\partial v} \right)_T \quad 6.7.5$$

Substituting eqs. (6.7.4) and (6.7.5) into eq. (6.7.3) and simplifying gives:

$$\gamma_e = \frac{\left(\frac{\partial p}{\partial T} \right)_s \left(\frac{\partial s}{\partial p} \right)_T}{\left(\frac{\partial v}{\partial T} \right)_s \left(\frac{\partial s}{\partial v} \right)_T} = \frac{\left(\frac{\partial p}{\partial T} \right)_s \left(\frac{\partial T}{\partial v} \right)_s}{\left(\frac{\partial p}{\partial s} \right)_T \left(\frac{\partial s}{\partial v} \right)_T} = \left(\frac{\partial p}{\partial v} \right)_s / \left(\frac{\partial p}{\partial v} \right)_T \quad 6.7.6$$

Hence

$$\left(\frac{\partial p}{\partial v} \right)_s = \gamma_e \left(\frac{\partial p}{\partial v} \right)_T \quad 6.7.7$$

Therefore the equilibrium sound velocity is given by the expression

$$a_e^2 = -v^2 \gamma_e \left(\frac{\partial p}{\partial v} \right)_T \quad 6.7.8$$

Substituting eqs. (6.5.2) and (6.6.4) into (6.7.8) yields after rearrangement

$$a_e^2 = \frac{RT/m}{\left[1 + \left(\frac{\partial \log m}{\partial \log p}\right)_T\right] - \frac{R/m}{c_{pe}} \left[1 - \left(\frac{\partial \log m}{\partial \log T}\right)_p\right]^2} \quad 6.7.9$$

for frozen composition, $\left(\frac{\partial \log m}{\partial \log p}\right)_T = \left(\frac{\partial \log m}{\partial \log T}\right)_p = 0$ and eq. (6.7.9) reduces to the classical thermodynamic relation

$$a_f^2 = \gamma_f RT/m \quad 6.7.10$$

It should be noted that the equilibrium velocity of sound is not equal to $\gamma_e RT/m$. If one wishes to use a similar expression it can be done by introducing a quantity Γ such that

$$a_e^2 = \Gamma RT/m \quad 6.7.11$$

Then by comparing eqs. (6.7.9) and (6.7.11)

$$\Gamma = \frac{1}{\left[1 + \left(\frac{\partial \log m}{\partial \log p}\right)_T\right] - \frac{R/m}{c_{pe}} \left[1 - \left(\frac{\partial \log m}{\partial \log T}\right)_p\right]^2} \quad 6.7.12$$

Clearly, if the molar mass m is constant

$$\Gamma = \frac{c_{pf}}{c_{pf} - R/m} = \gamma_f \quad 6.7.13$$

However if the molar mass is varying,

$$a_e^2 = \left(\frac{\partial p}{\partial \rho}\right)_s = \frac{p}{\rho} \left(\frac{\partial \log p}{\partial \log \rho}\right)_s = \left(\frac{\partial \log p}{\partial \log \rho}\right)_s RT/m$$

while from the temperature-entropy relations, with e the internal energy

$$\left(\frac{\partial h}{\partial e}\right)_s = -\left(\frac{\partial \log p}{\partial \log v}\right)_s = \left(\frac{\partial \log p}{\partial \log \rho}\right)_s \quad 6.7.14$$

Hence

$$\Gamma = \left(\frac{\partial h}{\partial e}\right)_s$$

which should be contrasted to γ_e used in eq. (6.7.8).

7. COMPUTER PROGRAM AND DATA

The program written for the IBM 7090 digital computer at the Computer Center, University of California, Berkeley, to evaluate the detonation parameters of gaseous mixtures consists of four programs and subprograms. The Fortran listings are given in Tables 2 - 7 which are discussed below. A flow diagram illustrating the operations performed by the four sub-routines and their interdependence is shown in Fig. 5.

Table 2 Source Program

This program loads the initial data into the computer and evaluates the upstream thermodynamic properties. These initial conditions are then printed out, and several constants are evaluated from the input data which are used later in the program.

Tables 3, 4, 5 Subroutine Spec

There are three Spec subroutines which shall be denoted by Spec(a), Spec(b), and Spec(c). The purpose of the subroutine in all three cases is either to specify the pressure at which properties are to be evaluated on the Hugoniot or Rankine-Hugoniot curve, or to converge to a particular pressure, e. g. P_{CT} , P_{VN} , or $P_{V=1}$.

The thermodynamic properties and equilibrium composition are printed out for each solution in this subroutine.

Table 6 Subroutine Main

Subroutine main is called by the Spec subroutine to determine the correct value of temperature on the Hugoniot (or Rankine-Hugoniot) curve corresponding to the given value of P . After converging to the correct Θ , the equilibrium sound velocity and specific heat ratio are evaluated and the subroutine returns to subroutine spec.

Table 7 Subroutine Brink

This subroutine is called by the subroutine main at each approximate value of T and P to evaluate the equilibrium composition and several thermodynamic properties.

Table 5 Input Data

The input data is given to the computer on IBM data cards. Instructions for putting the required data on the cards are given below. The format statement is given by each data card and the numbers on the left indicate the spaces on the card where the data must be inserted.

Data 1: 1 card (7E10.3)

- | | |
|--------|--|
| 1-10: | P , atmospheres |
| 11-20: | T , degrees Kelvin |
| 21-30: | convergence criterion for ΔZ_j |
| 31-40: | convergence criterion for ΔT , ΔP_{cJ} , ΔP_{vN} and $\Delta P_{v=1}$ |
| 41-50: | increment of P for Spec(a)
blank for Spec(b) and Spec(c) |
| 51-60: | initial value at P for Spec(a)
initial approximation of P_{cJ} for Spec(b)
initial approximation of P_{vN} for Spec(c) |
| 61-70: | initial approximation for T corresponding to the initial P |

Data 2: 1 card (7E10.3)

- | | |
|--------|--|
| 1-10: | blank |
| 11-20: | initial approximation for $P_{v=1}$ for Spec(b)
blank for Spec(a) and Spec(c) |

Data 3: 1 card (7I10)

- 1-10: number of pressures to be evaluated on Hugoniot curve
 for Spec(a)
 blank for Spec(b)and Spec(c)
- 11-20: number of constituents in downstream equilibrium system
- 21-30: number of components in downstream equilibrium system
- 31-40: number of species in upstream mixture
- 41-50: 1 if $P_{V=1}$ is to be computed for Spec(b)
 0 if $P_{V=1}$ is not to be computed for Spec(b)
 blank for Spec(a)and Spec(c)

Data 4: 1 or more cards (7I10)

- 1-10: subscripts of constituents appearing in initial mixture

Data 5

- 11-20: subscripts of constituents appearing in lists of components

Data 6: twice the number of cards as the number of constituents in downstream system

- 1-70: Data on each card is a line from Table 8: i. e., each
 card has coefficients for one species and for one
 temperature range. The cards with the coefficients for
 the constituents must appear in the order that the
 constituents appear in the β_{ij} , i. e., Data 8. The low
 temperature range coefficients must appear first
 followed by the high temperature range coefficients.

Data 7: 1 or more cards

- 10 spaces
per data: molecular weights of components in order

Data 8: 1 or more cards (7E10.3)

The matrix of the stoichiometric coefficients, β_{ij} , with one or more cards for each i . If j becomes greater than 7, use two cards for each i .

Data 9: 1 or more cards

10 spaces

per data: relative composition of upstream mixture in order of Data 4.

Data 10: 1 or more cards (7A10)

10 spaces

per data: symbols of constituents

Data 11: 1 or more cards (7E10.3)

Approximate mole fractions of components in equilibrium products.

Data 12: 1 card

blank for Spec(a) and Spec(b)

value of Mach number at which shock wave properties are to be computed for Spec(c)

Table 8 Preparation of Thermodynamic Data

A fifth degree polynomial was fitted to the specific heat data of each species so that the molar specific heats were given by:

$$\frac{C_{pi}}{R} = \sum_{n=0}^5 a_{ni} (T \cdot 10^{-3})^n \quad 100 \leq T \leq 1500$$

$$\frac{C_{pi}}{R} = \sum_{n=0}^5 b_{ni} (T \cdot 10^{-3})^n \quad 1500 \leq T \leq 5100$$

7.6.1

where two series expression were used to obtain a more accurate fit over the entire temperature range. The molar enthalpy of the i^{th} species was found then by integration of eq. (7.6.1), yielding thus:

$$\frac{h_i}{RT} = \sum_{n=0}^5 a_{ni} (T \cdot 10^{-3})^{n+1} / (n+1) + a_{6i} / (T) \quad 100 \leq T \leq 1500$$

$$\frac{h_i}{RT} = \sum_{n=0}^5 b_{ni} (T \cdot 10^{-3})^{n+1} / (n+1) + b_{6i} / (T) \quad 1500 \leq T \leq 5100$$

7.6.2

where the constants of integration a_{6i} and b_{6i} were adjusted so that the enthalpy computed from both eqs. (7.6.2) were identical to the value listed in the JANAF tables at 1500°K .

Dividing eq. (7.6.1) by the temperature and integrating the resulting expression yielded finally an equation for the molar entropy:

$$\begin{aligned}\frac{S_i}{R} &= a_{6i} \log T + \sum_{n=1}^5 a_{ni} (T \cdot 10^{-3})^{n/(n+1)} + a_{7i} & 100 \leq T \leq 1500 \\ \frac{S_i}{R} &= b_{6i} \log T + \sum_{n=1}^5 b_{ni} (T \cdot 10^{-3})^{n/(n+1)} + b_{7i} & 1500 \leq T \leq 5100\end{aligned}\tag{7.6.3}$$

where again the constants a_{7i} and b_{7i} were adjusted to provide an identical fit with the JANAF data at 1500°K .

Table 9 lists three sets of sample input data for the computer program using Spec(a), Spec(b), and Spec(c) respectively where each set is for a $2\text{H}_2+\text{O}$ mixture initially at 1 atm and 288.72°K (60°F). The corresponding computer output is then listed in Tables 10 - 12.

8. DISCUSSION OF RESULTS

Detonation parameters for the forty different initial conditions listed on page 4 were calculated using the computer program and the results are presented in Figs. 6 - 31.

Figs. 6 - 9 show the P - V representation of the Hugoniot curves computed for initial pressures of .1 and 760 mm Hg. Fig. 6 presents the Hugoniot curves for a $3H_2+O_2$ mixture initially at 200°F , Fig. 7 shows the Hugoniot curves for all three compositions at an initial temperature of 60°F , Fig. 8 illustrates the results for a $3H_2+O_2$ mixture initially at -50°F while, finally Fig. 9 displays the Hugoniot curves for all compositions at an initial temperature of -180°F . It is of interest to note that the Hugoniot curves are relatively independent of initial composition, and further that the CJ state in all cases has a volume, or velocity, ratio of approximately 0.54.

Figs. 10 and 11 show dimensionless temperature-entropy and pressure-entropy diagrams for the case of a $2H_2+O_2$ mixture initially at 1 atm and 60°F . They illustrate the classical condition that the entropy is a minimum at the CJ state. Further they indicate that the pressure variation is greater than that of the temperature over a given portion on the Hugoniot curve.

The effect of initial pressure on the CJ pressure and temperature ratios are shown respectively in Figs. 12 and 14. Fig. 13 is a cross plot of Fig. 12 for the $3H_2+O_2$ composition and illustrates the obviously greater effect of initial temperature on the CJ pressure ratio.

Figs. 15 and 17 show the effect of initial pressure on the CJ wave velocity and Mach number respectively. It is interesting to note that the CJ wave velocity is comparatively independent of initial temperature, while the Mach number is relatively independent of composition. Fig. 16, obtained from a

cross plot of Fig. 15 for the $3H_2 + O_2$ composition demonstrates the effect of initial temperature on wave velocity.

Figs. 18 - 25 show the equilibrium composition at the CJ state as a function of initial pressure for each initial composition and temperature. They reveal the interesting result that the equilibrium composition of H_2O is approximately the same for all conditions.

Figs. 26 and 27 indicate the effect of initial pressure on both frozen and equilibrium CJ specific heats for all three compositions at $-180^\circ F$ and $60^\circ F$. The frozen specific heat is seen to be independent of initial composition. More interesting yet is the comparison between the equilibrium and frozen specific heat, the former being about five times larger than the latter.

Fig. 28 illustrates the dependence of both frozen and equilibrium CJ specific heat ratios on the initial pressure. The equilibrium specific heat ratio, γ_e , is nearly independent of initial pressure and temperature, but shows a significant dependence on composition. The frozen composition specific heat ratio, γ_f , on the other hand, shows an obvious dependence on initial pressure, although it is relatively independent of initial temperature and composition.

The von Neumann spike values of P , Θ , and V are shown in Figs. 29, 30, and 31 as a function of initial pressure. It is interesting to note that the ratio of the VN pressure and temperature to the corresponding CJ values is nearly independent of the initial conditions.

The CJ properties for the initial conditions considered are tabulated in Table 13, while the von Neumann spike properties are presented in Table 14.

Finally, it is of interest to compare results of the present calculations with those obtained by other investigators together with some experimental

results. The data for CJ detonations presented in Table 15 indicate a good agreement between the various results based on the use of the equilibrium sound speed, which in general are slightly larger than both experimental measurements and those results based on frozen sound speed. The present results also agree quite well with those of Bollinger and Edse (7), which were obtained at 313°K.

REFERENCES

- 1) Lewis, B., and Friauf, J. B., Journal of the American Chemical Society 52, 1930.
- 2) Berets, D. J., Green, E. F., and Kistiakowsky, G. B., Journal of the American Chemical Society, 72, pp 1080-1086, March 1950.
- 3) Edse, R., Proceedings of the Propellant Thermodynamics and Handling Conference, Special report 12, Eng. Exp. Station, Ohio State University, June 1960.
- 4) Wolfson, B. T., and Dunn, G., Proceedings of the Propellant Thermodynamics and Handling Conference, Special Report 12, Eng. Exp. Station, Ohio State University, June 1960.
- 5) Luker, J. A., McGill, P. L., and Adler, L. B., Journal of Chemical and Engineering Data 4, pp 136-142, April 1959.
- 6) Eisen, C. L., Gross, R. A., and Rivlin, T. J., Combustion and Flame 4, pp 137-149, June 1960.
- 7) Bollinger, L. E., and Edse, R., ARS Journal 31, pp 251-256, February 1961.
- 8) Barrere S., and Barrere, M., La Recherche Aeronautique 87, pp 23-31, Mars-April, 1962.
- 9) Zeleznik, F. J., and Gordon, S., ARS Journal 32, pp 606-615, April 1962.
- 10) Bird, P. F., Duff, R. E., and Schott, G. L., A FORTRAN-FAP Code for Computing Normal Shock and Detonation Wave Parameters in Gases, Los Alamos Scientific Laboratory, University of California, September 11, 1963.
- 11) JANAF Thermochemical Data, compiled and calculated by the Dow Chemical Company, 1961.

- 12) Brinkley, S. R., "Calculation of the Thermodynamic Properties of Multi-component Systems and Evaluation of Propellant Performance Parameters" published in Kinetics, Equilibria and Performance of High Temperature Systems, The Proceedings of the First Conference, Western States Section, Combustion Institute, Butterworth and Co., London, 1959.
- 13) Brinkley, S. R., Journal of Chemical Physics 14, pp 563-565, 1946.
- 14) Obert, E. F., Concepts of Thermodynamics, McGraw-Hill, New York, 1960.

TABLE 1. Comparison of Various Methods of Analysis

AUTHOR	SYSTEM	SCOPE	INDEPENDENT VARIABLES	METHOD	REMARKS
Lewis & Friauf (1)	Hydrogen-Oxygen with inerts	CJ state	T_2, v_2	Iteration on T_2, v_2 , to satisfy conservation equations with CJ state determined from condition $M_2 = M_{2f} = 1$	Atomic oxygen not considered in the equilibrium system
Berets, et al (2)	Hydrogen, Oxygen	CJ state	T_2, v_2	Same as Lewis and Friauf	
Edse (3)	Arbitrary	Hugoniot curve and CJ state	T_2	Hugoniot curve determined by selecting arbitrary T_2 and iterating for the corresponding value of p_2 . CJ state determined when slope of Hugoniot curve is identical to slope of Rayleigh line.	
Wolfson & Durn (4)	Arbitrary	CJ state	T_2, p_2	Iterations on T_2 and p_2 to satisfy conservation equation with CJ point determined from condition $M_2 = M_{2f} = 1.0$	
Luker et al (5)	Hydrogen, Oxygen and Steam	CJ state	T_2, p_2	Same method as Reference 1	Van de Waal equations of state used for H_2O
Eisen et al (6)	C, H, O, N, A	Hugoniot curve and CJ state	M_1	For selected values of M_1 , iterations are performed to determine points along Hugoniot curve. CJ state specified by condition that M_1 is a minimum.	First to check CJ state with $M_{2e} = 1$
Bollinger & Edse (7)	Hydrogen-Oxygen	CJ state	T_2	Hugoniot curve found by selecting arbitrary T_2 , and determining corresponding p_2 by iteration. The CJ state is determined by finding the value of minimum M_1 .	Equilibrium equations are incorporated directly in the conservation equations
Barrere et al (8)	Arbitrary	CJ state	p_2, T_2	Computes equilibrium composition for several values of p and T in the neighborhood of the CJ state. Values of y_e and h are then evaluated from both the conservation equations and the equation of state. A cross plot technique yields the solution to the CJ state. The criteria for the CJ state is that of minimum entropy.	Graphical method
Zeleznik & Gordon (9)	Arbitrary	CJ state	p_2, T_2	Iteration on p_2 and T_2 with condition $M_2 = M_{2e}$ incorporated in conservation equations	Sound speed of products expressed by $a_g = \sqrt{\gamma R T}$ where $\gamma = \frac{p_{\text{prod}}}{\rho_{\text{prod}}} \frac{C_{pe}}{C_{ve}}$
Bird et al (10)	Arbitrary including condensed phase	Hugoniot curve & CJ state	T_2	p_2 is determined iteratively for specified T_2 to satisfy Hugoniot equation and equation of state. CJ state evaluated for M_1 minimum.	May include more than one phase in the chemical system
Present Work	Arbitrary	CJ state, von Neumann spike and Hugoniot curve	p_2	T_2 is determined iteratively for specified p_2 to satisfy Hugoniot equation and equation of state. CJ state evaluated for $M_{e,2} = 1$.	Sound speed of products expressed by $a_g = \sqrt{\gamma_e \frac{R}{v_e}}$ where: $\gamma_e = \frac{C_{pe}}{C_{ve}}$

TABLE 2. Fortran Listing - Source Program

```

*      LIST
*      LABEL
*      FORTRAN
      DIMENSION A(10,10),B(20,10),BB(20),BC(20,10),C(30,10),COMP(20),
      1CPM(20),AEQ(10,10),DZ(20),G(20),GG(10),H(20),HF(20),Q(10),UU(20),
      2UB(10),WMM(20),NB(10),NX(20),X(20),Z(10),WMC(10),WMP(20),CP(20),
      3STORE(50,20),BETA(20),DH(20)
      COMMON A,AA,AAA,B,BB,BBB,BC,C,CC,COMP,CDZ,CDV,CPM,CP1,CP2,D,DP,DT,
      1DT2,DZ,G,GAMMA1,GG,H,HF,H1,H2,MM,MP,NB,NCM,NCOM,NCON,NGO,NN,NX,P,
      2P1,P2,Q,QQ,R,SONIC,T,T1,T2,U1,UU,UB,V,V1,V2,WM,WMM,WMO,X,XN,Z,ZZ,
      3E,WM1,WMC,WMP,CONV,CON,CP,EMACH2,FMACH2,XMCH1,FRSON,EQSON,GAMM2R,
      4GAMM2E,CPR,CPE,H2,STORE,U2,CVE,CVR,BETA,DH,LSMFT,DS,DU,DELP,XX,YY,
      5LX,LY,LZ,LW,LV,LU,LT,LS,LR,LD,QLOSS,SOUND,CHECKV,CHECK,N,RR,RRM,SS
1000 FORMAT (7E10.6)
1001 FORMAT (7I10)
1003 FORMAT (7A10)
1004 FORMAT (6E12.5)
1005 FORMAT(8E10.3)
      R=1.98726
      CONV=4184.
      CON=41.84/1.0139
1050 READ 1000,P1,T1,CDZ,CDV,DP,P,T,QLOSS,CHECK
      NGO=0
      NN=0
      IF(P1) 1100,2000,1055
1100 PRINT 1110
1110 FORMAT (7H STOP 1)
      CALL EXIT
1055 PRINT 1060
      ARG6=0
1060 FORMAT(56H1HUGONIOT CURVE CALCULATIONS FOR GASEOUS MIXTURES---PROP
      162HULSION DYNAMICS LABORATORY--UNIVERSITY OF CALIFORNIA--BERKELEY)
1150 READ 1001,MP,NCON,NCOM,NCM,LR
      READ 1001, (NX(I),I=1,NCM)
      READ 1001, (NB(J),J=1,NCOM)
      N=NCON
      DO 1160 I=1,NCM
      IF (N-NX(I))1155,1160,1160
1155 N=NX(I)
1160 CONTINUE
      MC=2*N
      READ 1005,((C(I,J),J=1,8),I=1,MC)
1200 READ 1000, (WMC(J),J=1,NCOM)
      DO 1250 I=1,N
1250 READ 1000,(B(I,J),J=1,NCOM)
      READ 1000,(X(I),I=1,NCM)
      READ 1003,(COMP(J),J=1,N)
      QQ=0.0
      DO 1300 I=1,NCM
1300 QQ=QQ+X(I)
      DO 1350 I=1,NCM
1350 X(I)=X(I)/QQ
      QQ=0.0
      DO 1500 J=1,NCOM
      Q(J)=0.0
      DO 1450 K=1,NCM

```

TABLE 2 - Continued

```

      I=NX(K)
1450 Q(J)=Q(J)+B(I,J)*X(K)
1500 QQ=QQ+Q(J)
      DO 1550 J=1,NCOM
1550 Q(J)=Q(J)/QQ
      WMO=0
      DO 1560 J=1,NCOM
1560 WMO=WMO+WMC(J)*Q(J)
      WM1=WMO*QQ
      RR=R/WM1
      RRM=RR*T1
      DO 1690 I=1,NCON
      WMP(I)=0.
      DO 1690 J=1,NCOM
1690 WMP(I)=WMP(I)+B(I,J)*WMC(J)
      DO 1700 I=1,NCON
      BB(I)=0.0
      DO 1700 J=1,NCOM
1700 BB(I)=BB(I)+B(I,J)
      DO 1750 I=1,NCON
      DO 1750 J=1,NCOM
1750 BC(I,J)=B(I,J)-(BB(I)-1.)*Q(J)
      TK=T1/1000.
1760 IF(T1-1500.) 1770,1770,1772
1770 DO 1771 K=1,NCM
      I=NX(K)
1771 CPM(K)=((((C(I,6)*TK+C(I,5))*TK+C(I,4))*TK+C(I,3))*TK+C(I,2))*TK+
      IC(I,1))*R
      GO TO 1780
1772 DO 1773 K=1,NCM
      I=NX(K)
      J=I+N
1773 CPM(K)=((((C(J,6)*TK+C(J,5))*TK+C(J,4))*TK+C(J,3))*TK+C(J,2))*TK+
      IC(J,1))*R
1780 CP1=0.
      DO 1800 I=1,NCM
1800 CP1=CP1+CPM(I)*X(I)
      GAMMA1=CP1/(CP1-R)
      CP1=CP1/WM1
      SONIC=GAMMA1*R*T1/WM1
      U1=SQRTF(SONIC*CONV)
      V1=R*T1/(WM1*P1)
      V=V1*CON
      IF(T1-1500.) 1810,1810,1812
1810 DO 1811 K=1,NCM
      I=NX(K)
      HF(K)=((((C(I,6)*TK/5.+C(I,5)/4.)*TK+C(I,4)/3.)*TK+C(I,3)/2.)*TK+
      IC(I,2))*TK+C(I,1)*LOGF(T1))*R+C(I,8)*R
1811 H(K)=((((C(I,6)*TK/6.+C(I,5)/5.)*TK+C(I,4)/4.)*TK+C(I,3)/3.)*TK+
      IC(I,2)/2.)*TK+C(I,1))*T1*R+C(I,7)*R
      GO TO 1850
1812 DO 1813 K=1,NCM
      I=NX(K)
      J=N+I
      HF(K)=((((C(J,6)*TK/5.+C(J,5)/4.)*TK+C(J,4)/3.)*TK+C(J,3)/2.)*TK+
      IC(J,2))*TK+C(J,1)*LOGF(T1))*R+C(J,8)*R
1813 H(K)=((((C(J,6)*TK/6.+C(J,5)/5.)*TK+C(J,4)/4.)*TK+C(J,3)/3.)*TK+
      IC(J,2)/2.)*TK+C(J,1))*T1*R+C(J,7)*R
1850 H1=0.
      SS=0.

```

TABLE 2 - Continued

```

DO 1900 J=1,NCM
SS=SS+ X(J)*(HF(J)-R*LOGF(P1*X(J)))
1900 H1=H1+HH(J)*X(J)
H1=H1/WM1
SS=SS/R
HH=H1/RRM
HC=CP1/RR
PRINT 1950
1950 FORMAT(30H0 INITIAL CONDITION OF MIXTURE)
PRINT 1960,P1,T1,HH,U1
1960 FORMAT(4HOP1=E12.5, 14HATM      TEMP=F10.4,16H DEGK  ENTHALPY=F10
,1.2,16H      SD VEL=F10.4,5HMM/SEC)
PRINT 1961,V , HC,GAMMA1,WM1
1961 FORMAT(4H V1=E10.5,16HCM3/GM      CP1=F10.3,16H      GAMMA1=F10
1.3,16H      WM1=F10.3/)
PRINT 1959,SS
1959 FORMAT(9H ENTROPY=F10.4)
PRINT 1962
1962 FORMAT(23H0COMPOSITION OF MIXTURE/)
DO 1965 J=1,NCM
I=NX(J)
PRINT 1963,COMP(I),X(J)
1963 FORMAT(A7,2H =E12.5)
1965 CONTINUE
READ 1000, (X(J),J=1,NCOM)
1980 CONTINUE
CALL SPEC
GO TO 1050
2000 CALI. EXIT
END

```

**TABLE 3. Fortran Listing - Spec(a) Subroutine;
Hugoniot Curve Calculations**

```

* LIST
* LABEL
* FORTRAN
SUBROUTINE SPEC
  DIMENSION A(10,10),R(20,10),BB(20),BC(20,10),C(30,10),COMP(20),
  1CPM(20),AEQ(10,10),DZ(20),G(20),GG(10),H(20),HF(20),Q(10),UU(20),
  2UB(10),WMM(20),NB(10),NX(20),X(20),Z(10),WMC(10),WMP(20),CP(20),
  3STORE(50,20),BETA(20),DH(20)
  COMMON A,AA,AAA,B,BB,BBB,BC,C,CC,COMP,CDZ,CDV,CPM,CP1,CP2,D,DP,DT,
  1DT2,DZ,G,GAMMA1,GG,H,HF,H1,H2,MM,MP,NB,NCM,NCOM,NCON,NGO,NN,NX,P,
  2P1,P2,Q,QQ,R,SONIC,T,T1,T2,U1,UU,UB,V,V1,V2,WM,WMM,WMO,X,XN,Z,ZZ,
  3E,WM1,WMC,WMP,CONV,CON,CP,EMACH2,FMACH2,XMCH1,FRSON,EQSON,GAMM2R,
  4GAMM2E,CPR,CPE,H2,STORE,U2,CVE,CVR,BETA,DH,LSMFT,DS,DU,DELP,XX,YY,
  5LX,LY,LZ,LW,LV,LU,LT,LS,LR,LD,QLOSS,SOUND,CHECKV,CHECK,N,RR,RRM,SS
  1  FORMAT(1H )
  2  FORMAT(47H1THERMODYNAMIC PROPERTIES ON THE HUGONIOT CURVE)
  3  FORMAT(56H0 PRESS R TEMP R VEL R MACH1 FMACH2 FMACH2 FSDVEL2
  165HESDVEL2 FGAMM2 EGAMM2 FSPHT ESPHT ENTH2 MOLWT ENTROP
  2Y )
  4  FORMAT(F9.4,F8.4,F7.4,3F7.4,2F9.3,2F7.4,2F8.4,F10.3,F8.3,F9.4)
  5  FORMAT(F10.4,9E12.5)
  6  FORMAT(46H1EQUILIBRIUM COMPOSITION ON THE HUGONIOT CURVE)
  7  FORMAT(10H0 PRESS R 9A12)
    NGO=0
  2000 MM=5
    LSMFT=0
    K=NCON+1
    LV=0
    PRINT 2
    PRINT 1
    PRINT 3
    GO TO 2250
  2200 P=P+DP
  2250 P2=P*P1
    T2=T*T1
    CALL MAIN
    XX=XX/RR
    H2=H2/RRM
    CPE=CPE/RR
    CPR=CPR/RR
    IF(MM=5) 2300,2275,2275
  2275 PRINT 1
    MM=0
  2300 PRINT 4,P,T,V,XMCH1,FMACH2,EMACH2,FRSON,EQSON,GAMM2R,GAMM2E,
  1CPR,CPE,H2,WM,XX
    MM=MM+1
    NGO=NGO+1
    LSMFT=LSMFT+1
    STORE(LSMFT,1)=P
    DO 2700 I=1,NCON
      L=I+1
  2700 STORE(LSMFT,L)=X(I)
    IF(MP-NGO) 2800,2800,2750
  2750 IF(40-LSMFT) 2800,2800,2200
  2800 MM=5
    PRINT 6

```

TABLE 4 Fortran listing - Spec(b) Subroutine; CJ Calculations

```

*      LIST
*      LABEL
*      FORTRAN
      SUBROUTINE SPEC
      DIMENSION A(10,10),B(20,10),BB(20),BC(20,10),C(30,10),COMP(20),
      1CPM(20),AEQ(10,10),DZ(20),G(20),GG(10),H(20),HF(20),Q(10),UU(20),
      2UB(10),WMM(20),NB(10),NX(20),X(20),Z(10),WMC(10),WMP(20),CP(20),
      3STORE(50,20),BETA(20),DH(20)
      COMMON A,AA,AAA,B,BB,BBB,BC,C,CC,COMP,CDZ,CDV,CPM,CP1,CP2,D,DP,DT,
      1DT2,DZ,G,GAMMA1,GG,H,HF,H1,H2,MM,MP,NB,NCM,NCOM,NCON,NGO,NN,NX,P,
      2P1,P2,Q,QQ,R,SONIC,T,T1,T2,U1,UU,UB,V,V1,V2,W,WMM,WMO,X,XN,Z,ZZ,
      3E,WMI,WMC,WMP,CONV,CON,CP,EMACH2,FMACH2,XMCH1,FRSON,EQSON,GAMM2R,
      4GAMM2E,CPR,CPE,H2,STORE,U2,CVE,CVR,BETA,DH,LSMFT,DS,DU,DELP,XX,YY,
      5LX,LY,LZ,LW,LV,LU,LT,LS,LR,LD,QLOSS,SOUND,CHECKV,CHECK,N,RR,RRM,SS
      IF (LR) 5,5,4
4      PX=0.
      GO TO 2100
5      PP=P
      TT=T
      P=CHECK
      P2=P*P1
      T2=T*T1
      LV=1
10     CALL MAIN
      DS=H2
      DD=H2
      BBBB=H1+V1*(P2-P1)+QLOSS
      P=P+.05
      P2=P*P1
      CALL MAIN
      DS=(H2-DS)
      AAA=V1*P1
      CC=DS/.05
      DELP=(DD-BBBB)/(AAA-CC)
      IF (ABSF(DELP)-1.) 14,12,12
12     DELP=DELP/ABSF(DELP)
14     CONTINUE
      P=P-.05+DELP
      IF (ABSF(BBBB-DD)-CDV) 20,20,10
20     IF (ABSF(DELP)-CDV) 21,21,10
21     PX=P
      PRINT 22, PX
22     FORMAT(63H0 THE PRESSURE RATIO OF THE HUGONIOT CURVE AT V2=V1 IS E
      1QUAL TOF9.4)
      IF (PX-1.) 23,23,28
23     PRINT 25
25     FORMAT(48H0THERE IS NO CHAPMAN-JOUGUET POINT FOR THIS DATA)
      GO TO 3270
28     P=PP
      T=TT
      DO 2000 I=1,NCM
      K=NX(I)
2000  DH(I)=X(K)
      DO 2050 I=1,NCM
2050  X(I)=DH(I)
2100  PRINT 2200
2200  FORMAT(1H //)
      PRINT 2250
2250  FORMAT(54H THERMODYNAMIC PROPERTIES AT THE CHAPMAN-JOUGUET POINT)
      P2=P*P1
      T2=T*T1

```


TABLE 4 - Continued

```

LV=0
2300 CALL MAIN
      DU=EMACH2
      PP=P
      P=P+.05
      P2=P*P1
      SOUND=EMACH2
      CALL MAIN
      DU=(EMACH2-DU)/.05
      DELP=(1.-SOUND)/DU
      IF(ABSF(DELP)-1.) 2310,2308,2308
2308 DELP=DELP/ABSF(DELP)
2310 CONTINUE
      P=PP+DELP
      P2=P*P1
      IF(ABSF(SOUND-1.) -CDV) 2350,2350,2300
2350 IF(ABSF(DELP)-CDV) 2500,2500,2300
2500 CONTINUE
      CALL MAIN
      T=T2/T1
      PRINT 2520
2520 FORMAT(56H0 PRESS R  TEMP R  VEL R  MACH1 FMACH2 EMACH2  FSDVEL2
165HESDVEL2 FGAMM2 EGAMM2  FSPHT  ESPHT  ENTH2  MOLWT  ENTROP
2Y )
      PRINT 2560
      XX=XX/RR
      H2=H2/RRM
      CPE=CPE/RR
      CPR=CPR/RR
      PRINT 2550,P,T,V, XMCH1,FMACH2,EMACH2,FRSON,EQSON,GAMM2R,GAMM2E,
1CPR,CPE,H2,WM,XX
2550 FORMAT(F9.4,F8.4,F7.4,3F7.4,2F9.3,2F7.4,2F8.4,F10.3,F8.3,F9.4)
2560 FORMAT(1H )
      PRINT 2560
      PRINT 2600
2600 FORMAT(54H0 EQUILIBRIUM COMPOSITION AT THE CHAPMAN-JOUGUET POINT)
      PRINT 2560
      LFIRST=1
      IF(NCON-9) 3000,3000,2950
2950 LPRINT=9
      GO TO 3050
3000 LPRINT=NCON
3050 PRINT 3060,(COMP(J),J= LFIRST,LPRINT)
3060 FORMAT(9A12)
      PRINT 2560
      PRINT 3070,(X(I),I=LFIRST,LPRINT)
      IF(NCON-LPRINT) 3270,3270,3260
3070 FORMAT(9E12.5)
3260 LFIRST=LFIRST+9
      IF(NCON-LPRINT-9) 3262,3262,3264
3262 LPRINT=NCON
      GO TO 3266
3264 LPRINT=LPRINT+9
3266 PRINT 2560
      GO TO 3050
3270 RETURN
      END

```

TABLE 5. Fortran Listing - Spec (c) Subroutine, Shock Conditions at Given Mach Number

```

*      LIST
*      LABEL
*      FORTRAN
SUBROUTINE SPEC
  DIMENSION A(10,10),B(20,10),BB(20),BC(20,10),C(30,10),COMP(20),
  1CPM(20),AEQ(10,10),DZ(20),G(20),GG(10),H(20),HF(20),Q(10),UU(20),
  2UB(10),WMM(20),NB(10),NX(20),X(20),Z(10),WMC(10),WMP(20),CP(20),
  3STORE(50,20),BETA(20),DH(20)
  COMMON A,AA,AAA,B,BB,BBB,BC,C,CC,COMP,CDZ,CDV,CPM,CP1,CP2,D,DP,DT,
  1DT2,DZ,G,GAMMA1,GG,H,HF,H1,H2,MM,MP,NB,NCM,NCOM,NCON,NGO,NN,NX,P,
  2P1,P2,Q,QQ,R,SONIC,T,T1,T2,U1,UU,UB,V,V1,V2,WM,WMM,WMO,X,XN,Z,ZZ,
  3E,WM1,WMC,WMP,CONV,CON,CP,EMACH2,FMACH2,XMCH1,FRSON,EQSON,GAMM2R,
  4GAMM2E,CPR,CPE,H2,STORE,U2,CVE,CVR,BETA,DH,LSMFT,DS,DU,DELP,XX,YY,
  5LX,LY,LZ,LW,LV,LU,LT,LS,LR,LD,GLOSS,SOUND,CHECKV,CHECK,N,RR,RRM,SS
  1  FORMAT(8E10.3)
     LV=0
     READ 1, XMCH1
     ALPHA=GAMMA1*XMCH1**2
     T2=T*T1
  9000 P2=P*P1
     CALL MAIN
     VRH=V
     VALPH=1.-(P-1.)/ALPHA
     P=P+.05
     P2=P*P1
     CALL MAIN
     DVDP=(V-VRH)/.05
     DELP=(VALPH-VRH)/(DVDP+1./ALPHA)
     IF(ABSF(DELP)-1.) 9100,9100,9050
  9050 DELP=DELP/ABSF(DELP)
  9100 P=P-.05+DELP
     IF(ABSF(DELP)-CDV) 9200,9200,9000
  9200 P2=P*P1
     CALL MAIN
     PRINT 9400
  9400 FORMAT(29HOPROPERTIES BEHIND SHOCK WAVE)
     PRINT 9410
  9410 FORMAT(56H0 PRESS R  TEMP R  VEL R  MACH1 FMACH2 EMACH2  FSDVEL1
  165HESDVEL2 FGAMM2 EGAMM2  FSPHT  ESPHT      ENTH2  MOLWT  ENTROP
  2Y )
     PRINT 9430
     PRINT 9420,P,T,V, XMCH1,FMACH2,EMACH2,FRSON,EQSON,GAMM2R,GAMM2E,
  1CPR,CPE,H2,WM,XX
  9420 FORMAT(F9.4,F8.4,F7.4,3F7.4,2F9.3,2F7.4,2F8.4,F10.3,F8.3,F9.4)
     PRINT 9430
  9430 FORMAT(1H )
  3  PRINT 9440
  9440 FORMAT(30HOCOMPOSITION BEHIND SHOCK WAVE//)
     LFIRST=1
     IF(NCON-9) 9500,9500,9450
  9450 LPRINT=9
     GO TO 9550
  2  9500 LPRINT=NCON
  9550 PRINT 9560,(COMP(J),J=LFIRST,LPRINT)
  9560 FORMAT(9A12)
     PRINT 9430
     PRINT 9570,(X(I),I=LFIRST,LPRINT)
  1  9570 FORMAT(9E12.5)
     IF(NCON-LPRINT) 9770,9770,9760
  9760 LFIRST=LFIRST+9

```

TABLE 5 - Continued

```
          IF(NCON-LPRINT-9) 9762,9762,9764
9762 LPRINT=NCON
      GO TO 9766
9764 LPRINT=LPRINT+9
9766 PRINT 9768
9768 FORMAT(1H //)
      GO TO 9550
9770 RETURN
      END
```

TABLE 6. Fortran Listing - Main Subroutine.

```

*      LIST
*      LABEL
*      FORTRAN
      SUBROUTINE MAIN
      DIMENSION A(10,10),B(20,10),BB(20),BC(20,10),C(30,10),COMP(20),
1CPM(20),AEQ(10,10),DZ(20),G(20),GG(10),H(20),HF(20),Q(10),UU(20),
2UB(10),WMM(20),NB(10),NX(20),X(20),Z(10),WMC(10),WMP(20),CP(20),
3STORE(50,20),BETA(20),DH(20)
      COMMON A,AA,AAA,B,BB,BBB,BC,C,CC,COMP,CDZ,CDV,CPM,CP1,CP2,D,DP,DT,
1DT2,DZ,G,GAMMA1,GG,H,HF,H1,H2,MM,MP,NB,NCM,NCOM,NCON,NGO,NN,NX,P,
2P1,P2,Q,QQ,R,SONIC,T,T1,T2,U1,UU,UB,V,V1,V2,WM,WMM,WMO,X,XN,Z,ZZ,
3E,WM1,WMC,WMP,CONV,CON,CP,EMACH2,FMACH2,XMCH1,FRSON,EQSON,GAMM2R,
4GAMM2E,CPR,CPE,H2,STORE,U2,CVE,CVR,BETA,DH,LSMFT,DS,DU,DELP,XX,YY,
5LX,LY,LZ,LW,LV,LU,L1,LS,LR,LD,QLLOSS,SOUND,CHECKV,CHECK,N,RR,RRM,SS
4000 CALL BRINK
      PVTP=0.
      DO 4005 I=1,NCON
4005 PVTP=PVTP+WMP(I)*X(I)*BETA(I)
      PVTP=(1.-PVTP/WM)*R/(WM*P2)
      AAA=2.*CP2/(V1*(P2-P1))
      BBB=2.*(H2-H1-QLLOSS)/((P2-P1)*V1)-1.
      CC=PVTP/V1
      D=R*T2/(V1*P2*WM)
      DT2=(BBB-D)/(CC-AAA)
      IF(ABSF(DT2)-400.) 4008,4008,4007
4007 DT2=400.*(DT2/(ABSF(DT2)))
4008 T2=T2+DT2
      IF(ABSF(BBB-D)-CDV) 4010,4000,4000
4010 DT2=DT2/T1
      IF(ABSF(DT2)-CDV) 4150,4000,4000
4150 V=BBB
      T=T2/T1
      IF(LV) 4200,4200,4500
4200 U1=2.*(H2-H1-QLLOSS)/(1.-V**2)
      U2=(V**2)*U1
      XMCH1=SQRTF(U1/SONIC)
      GAMM2R=CPR/(CPR-R/WM)
      FRSON=GAMM2R*R*T2/WM
      FMACH2=SQRTF(U2/FRSON)
      FRSON=SQRTF(FRSON*CONV)
      DO 4300 J=1,NCOM
4300 GG(J)=-Q(J)
      ARG6=0
      LLL=ISIMEQ(10,NCOM,1,A,GG,ARG6,DZ)
      IF(LL-1) 4320,4320,4310
4310 PRINT 4311
4311 FORMAT(7H STOP 5)
      CALL EXIT
4320 DO 4350 I=1,NCON
      BETA(I)=0.
      DO 4340 J=1,NCOM
4340 BETA(I)=BETA(I)-B(I,J)*A(J,1)
4350 BETA(I)=BETA(I)-1.
      PVPT=0.
      DO 4400 I=1,NCON
4400 PVPT=PVPT+WMP(I)*X(I)*BETA(I)

```

TABLE 6 - Continued

```
PVPT=(1.+PVPT/WM)
GAMM2E=PVTP**2*WM*P2**2/(R*PVPT*CPE)
GAMM2E=1./(1.-GAMM2E)
EQSON=GAMM2E*R*T2/(PVPT*WM)
EMACH2=SQRTE(U2/EQSON)
EQSON=SQRTE(EQSON*CONV)
XX=0.
DO 4450 I=1,NCON
  IF(X(I)*10.**10-1.) 4450,4450,4430
4430 XX=XX+X(I)*(HF(I)-R*LOGF(X(I)*P2))
4450 CONTINUE
  XX=XX/WM
4500 RETURN
END
```

TABLE 7. Fortran Listing - Brink Subroutine.

```

*      LIST
*      LABEL
*      FORTRAN
      SUBROUTINE BRINK
      DIMENSION A(10,10),B(20,10),BB(20),BC(20,10),C(30,10),COMP(20),
1CPM(20),AEQ(10,10),DZ(20),G(20),GG(10),H(20),HF(20),Q(10),UU(20),
2UB(10),WMM(20),NB(10),NX(20),X(20),Z(10),WMC(10),WMP(20),CP(20),
3STORE(50,20),BETA(20),DH(20)
      COMMON A,AA,AAA,B,BB,BBB,BC,C,CC,COMP,CDZ,CDV,CPM,CP1,CP2,D,DP,DT,
1DT2,DZ,G,GAMMA1,GG,H,HF,H1,H2,MM,MP,NB,NCM,NCOM,NCON,NGO,NN,NX,P,
2P1,P2,Q,QQ,R,SONIC,T,T1,T2,U1,UU,UB,V,V1,V2,WM,WMM,WMO,X,XN,Z,ZZ,
3E,WM1,WMC,WMP,CONV,CON,CP,EMACH2,FMACH2,XMCH1,FRSON,EQSON,GAMM2R,
4GAMM2E,CPR,CPE,H2,STORE,U2,CVE,CVR,BETA,DH,LSMFT,DS,DU,DELP,XX,YY,
5LX,LY,LZ,LW,LV,LU,LT,LS,LR,LD,QLOSS,SOUND,CHECKV,CHECK,N,RR,RRM,SS
      L=0
      TK=T2/1000.
      IF(T2-1500.) 500,500,502
500  DO 501 I=1,NCON
      CP(I)=((((C(I,6)*TK+C(I,5))*TK+C(I,4))*TK+C(I,3))*TK+C(I,2))*TK+
1C(I,1))*R
      H(I)=((((C(I,6)*TK/6.+C(I,5)/5.)*TK+C(I,4)/4.)*TK+C(I,3)/3.)*TK+
1C(I,2)/2.)*TK+C(I,1))*T2*R+C(I,7)*R
      HF(I)=((((C(I,6)*TK/5.+C(I,5)/4.)*TK+C(I,4)/3.)*TK+C(I,3)/2.)*TK+
1C(I,2))*TK+C(I,1)*LOGF(T2))*R+C(I,8)*R
501  UU(I)=H(I)-T2*HF(I)
      GO TO 504
502  DO 503 J=1,NCON
      J=I+N
      CP(I)=((((C(J,6)*TK+C(J,5))*TK+C(J,4))*TK+C(J,3))*TK+C(J,2))*TK+
1C(J,1))*R
      H(I)=((((C(J,6)*TK/6.+C(J,5)/5.)*TK+C(J,4)/4.)*TK+C(J,3)/3.)*TK+
1C(J,2)/2.)*TK+C(J,1))*R*T2+C(J,7)*R
      HF(I)=((((C(J,6)*TK/5.+C(J,5)/4.)*TK+C(J,4)/3.)*TK+C(J,3)/2.)*TK+
1C(J,2))*TK+C(J,1)*LOGF(T2))*R+C(J,8)*R
503  UU(I)=H(I)-T2*HF(I)
504  DO 505 J=1,NCOM
      I=NB(J)
505  UB(J)=UU(I)
      DO 520 I=1,NCON
      G(I)=0.0
      DO 510 J=1,NCOM
510  G(I)=B(I,J)*UB(J)/(R*T2)+G(I)
520  G(I)=G(I)-LOGF(P2)-UU(I)/(R*T2)
      IF(NN) 523,523,521
521  DO 522 J=1,NCOM
522  X(J)=WMM(J)
523  DO 531 J=1,NCOM
531  Z(J)=-LOGF(X(J))-LOGF(P2)
      NN=1
540  DO 560 I=1,NCON
      X(I)=0.0
      DO 550 J=1,NCOM
550  X(I)=X(I)-B(I,J)*Z(J)
      X(I)=X(I)+G(I)
560  X(I)=EXP(X(I))
564  IF(L) 565,565,610

```

TABLE 7 - Continued

```
565 DO 575 J=1,NCOM
    GG(J)=0.0
    DO 570 I=1,NCON
570 GG(J)=GG(J)+BC(I,J)*X(I)
575 GG(J)=GG(J)-G(J)
    DO 580 J=1,NCOM
    DO 580 K=1,NCOM
    A(J,K)=0.0
    DO 580 I=1,NCON
    A(J,K)=A(J,K)+BC(I,J)*B(I,K)*X(I)
580 AEQ(J,K)=A(J,K)
    ARG6=0
    LLL=ISIMEQ(10,NCOM,1,AEQ,GG,ARG6,DH)
    IF (LLL-1) 585,585,583
583 PRINT 584
584 FORMAT(6H STOP 5)
585 ZZ=0.0
    DO 590 J=1,NCOM
    Z(J)=Z(J)+AEQ(J,1)
590 ZZ=ZZ+ABSF(AEQ(J,1))
    IF (ZZ-CDZ) 600,600,540
600 L=1
    GO TO 540
610 XN=0.
    DO 620 J=1,NCOM
    I=NB(J)
620 WMM(J)=X(I)
    DO 630 I=1,NCON
630 XN=XN+BR(I)*X(I)
    XN=1./XN
    WM=WMO/XN
    H2=0.0
    DO 640 I=1,NCON
640 H2=H2+H(I)*X(I)
    H2=H2/WM
705 CPR=0.
    DO 710 I=1,NCON
710 CPR=CPR+CP(I)*X(I)
    DO 730 I=1,NCON
    DH(I)=0.
    DO 720 J=1,NCOM
    K=NB(J)
720 DH(I)=DH(I)-B(I,J)*H(K)
730 DH(I)=DH(I)+H(I)
    DO 750 J=1,NCOM
    GG(J)=0.
    DO 750 I=1,NCON
750 GG(J)=GG(J)+BC(I,J)*X(I)*DH(I)/(R*T2)
    DO 752 I=1,NCOM
    DO 752 J=1,NCOM
752 AEQ(I,J)=A(I,J)
    ARG6=0
    LLL=ISIMEQ(10,NCOM,1,AEQ,GG,ARG6,DZ)
    IF (LLL-1) 760,760,758
758 PRINT 759
759 FORMAT(7H STOP 5)
    CALL EXIT
760 DO 775 I=1,NCON
    BETA(I)=0.
    DO 774 J=1,NCOM
```

TABLE 7 - Contined

```
774 BETA(I)=BETA(I)-B(I,J)*AEQ(J,I)
775 BETA(I)=BETA(I)+DH(I)/(R*T2)
    CPR=CPR/WM
    CPE=CPR
    PLNM=0.
    DO 777 I=1,NCON
777 PLNM=PLNM-WMP(I)*X(I)*BETA(I)
    PLNM=PLNM/(T2*WM**2)
    DO 780 I=1,NCON
780 CPE=CPE+H(I)*X(I)*BETA(I)/(WM*T2)+H(I)*X(I)*PLNM
    CP2=CPE
    RETURN
    END
```


TABLE 8. THERMODYNAMIC DATA: COEFFICIENTS

Temperature Range 100-1500°K

	a ₀	a ₁	a ₂	a ₃	a ₄	a ₅	a ₆	a ₇
H ₂	1.7747952	12.49660900	-33.0956990	40.6823270	-23.2540090	5.03878820	-863.80088	3.01377960
O ₂	3.3965745	-.30432267	3.4248489	-3.4348762	1.2359846	-.11996245	-1023.48720	5.27139980
H ₂ O	4.0821991	-1.11136900	4.0978967	-3.0581501	1.1289416	-.18128481	-30283.01300	-.38880032
OH	4.0067420	-2.41251140	4.5443704	-4.0708144	2.0592515	-.44010753	3574.81290	-.17879530
H	2.4999245						25472.76100	-.45946595
0	3.0439461	-2.25985070	3.9647901	-3.4822300	1.5042257	-.25417317	29134.00200	2.53859420

Temperature Range 1500-5100°K

	b ₀	b ₁	b ₂	b ₃	b ₄	b ₅	b ₆	b ₇
H ₂	2.8699448	.72232810	.063994338	-090722520	.020446865	-.00147682	-741.17471	-.57067430
O ₂	5.8411221	-3.04058980	2.248694500	-.72166208	.110180100	-.00652828	-2228.27820	-8.97833830
H ₂ O	8.0282346	-6.47261290	5.598213800	-1.98654050	.323502380	-.01995635	-32297.79100	-23.32421200
OH	4.3902840	-1.71685630	1.666016700	-.60766657	.100023230	-.00619887	3223.81870	-2.86444870
H	2.4999245						25472.76100	-.45946595
0	3.5206998	-1.76641330	1.179612700	-.381344800	.060163981	-.00367756	28790.13900	-.59613732

TABLE 9. Sample Input Data for Computer Program for
at 60°F and 760 mmHg.

Mixture Initially

Data for Spec(a) Subroutine

1.	288.72	.000001	.000001	20.	15.
	10.				
		6	2	2	
	1	2			
	3	2			
1.7747952	12.496609	-33.09569940	.682327	-23.2540095	.0387882
3.3965745	-.304322673	.4248489	-3.43487621	.2359846	-.11996245
4.0821991	-1.11136904	.0978967	-3.05813011	.1289416	-.18128401
4.0067420	-2.41251144	.5443704	-4.07081442	.0592515	-.440107533574
2.4999245					.8129
3.0439461	-2.25985073	.9647901	-3.48223001	.5042257	-.2541731729134
2.8699448	.72232810	.063994338	-.09072252	.020446865	-.00147682
5.8411221	-3.04058982	.2486945	-.72166208	.11018010	-.00652828
8.0282346	-6.47261295	.5982138	-1.9865405	.32350238	-.01997535
4.3902840	-1.71685631	.6660167	-.60766657	.10002323	-.006198875223
2.4999245					.8187
3.5206998	-1.76641331	.1796127	-.38134480	.060163981	-.0036775628790
18.016	32.				.139
1.	-.5				-.09613732
	1.				
1.					
.5	.25				
.5	-.25				
	.5				
2.	1.				
.45	.08				
		H2	O2	H2O	OH
				H	O

Data for Spec(b) Subroutine

1.	288.72	.000001	.000001	10.	10.
		2	2	2	
	1	2			
	1	2			
1.7747952	12.496609	-33.09569940	.682327	-23.2540095	.0387882
3.3965745	-.304322673	.4248489	-3.43487621	.2359846	-.11996245
2.8699448	.72232810	.063994338	-.09072252	.020446865	-.00147682
5.8411221	-3.04058982	.2486945	-.72166208	.11018010	-.00652828
2.016	32.				-.2228
1.					.2782
	1.				-8.9763383
2.	1.				
		H2	O2		
.666	.333				
5.					

TABLE 9 - Continued

Data for Spec(c) Subroutine

1.	288.72	.000001	.00001	1.	10.	10.
	40	6	2	2		
	1	2				
	3	2				
1.7747952	12.476607	-33.07569940	.682327	-23.2540095	.0387882	-863.800883.0137796
3.3965745	-.304322673	.4248487	-3.43487621	.2359846	-.11996245	-1023.48725.2713998
4.0821991	-1.11136904	.0978967	-2.05815011	.1289416	-.18128481	-30283.013-.38880032
4.0067420	-2.41251144	.5443704	-4.07081442	.0592515	-.440107533574	.8129 -.17879530
2.4999245					25472.761	-.45746595
3.0439461	-2.25985073	.9647901	-3.48223001	.5042257	-.2541731729134	.002-2.5385942
2.8699448	.72232810	.003974338	-.09072252	.020446865	-.00147682	-741.17471-.57067430
5.8411221	-3.04058982	.2486945	-.72166208	.11018010	-.00552828	-2278.2782-8.9783383
8.0282346	-6.47261295	.5982138	-1.9865405	.32350238	-.01995635	-32297.791-23.324212
4.3902840	-1.71685631	.6660167	-.60766657	.10002323	-.006198873223	.8187 -2.8644487
2.4999245					25472.761	-.45946595
3.5206998	-1.76641331	.1796127	-.36134430	.050163981	-.0036775628790	.139 -.59613732
18.016	32.					
1.	-.5					
	1.					
1.						
.5	.25					
.5	-.25					
	.5					
2.	1.					
	H2	O2	H2O	OH	H	O
.45	.08					

NOMENCLATURE FOR TABLES 10, 11, and 12

Initial Condition of Mixture

$P_1 - p_1, atm$
 $TEMP - T_1, ^\circ K$
 $ENTHALPY - \mathcal{H}_1$
 $SD\ VEL - a_1, m/sec$
 $V_1 - v_1, cm^3/gm$
 $CP_1 - c_{p1}/R_1$
 $GAMMA\ 1 - \gamma_1$
 $WM_1 - m$
 $ENTROPY - s_1/R_1$

Properties Downstream of Wave

$PRESS\ R - P$
 $TEMP\ R - \Theta$
 $VEL\ R - V$
 $MACH\ 1 - M_1$
 $EMACH\ 2 - M_{e,2}$
 $F\ MACH\ 2 - M_{f,2}$
 $ESDVEL\ 2 - a_{e,2}, m/sec$
 $FSDVEL\ 2 - a_{f,2}, m/sec$
 $F\ GAMM\ 2 - \gamma_f$
 $E\ GAMM\ 2 - \gamma_e$
 $FSPHT - c_{pf}/R_1$
 $ESPHT - c_{pe}/R_1$
 $ENTH\ 2 - \mathcal{H}_2$
 $MOLWT - m_2$
 $ENTROPY - s_2/R_1$

Table 10: Sample Output: Hugoniot Curve Computed Using Spec(a) Subroutine and Input Data in Table 9

HUGONIOT CURVE CALCULATIONS FOR GASEOUS MIXTURES---PROPELLION DYNAMICS LABORATORY--UNIVERSITY OF CALIFORNIA--SAN DIEGO

INITIAL CONDITION OF MIXTURE

P1= 0.16000E+01 ATM TEMPA= 288.720 DEGK ENTHALPY= -0.12 ID VEL= 529.7653M/SEC
V1= 19725E+00 CM3/GP CP1= 3.474 GAMMA1= 1.404 WPI= 12.011

COMPOSITION OF MIXTURE

M2 = 0.68687E+00
O2 = 0.33333E+00

THERMODYNAMIC PROPERTIES ON THE HUGONIOT CURVE

PRESS	TEMP	VEL	MACH1	MACH2	ENHALP2	FSOVEL2	ESOVEL2	FGAPP2	EGAPP2	FSPM7	ESPM7	ENTH2	PCAL7	ENTHCPY
10.0000	12.1812	0.994332	0.82711	0.95911	4.797	1554.7	1494.823	1.2187	1.2173	4.5933	24.1819	8.455	14.633	25.2279
11.0000	12.2489	0.9175	0.9186	2.7564	2.8846	1560.495	1527.733	1.2188	1.2136	4.5967	24.0514	9.435	14.665	25.1195
12.0000	12.3223	0.8407	1.1126	1.9938	2.0733	1566.476	1500.597	1.2189	1.2145	4.6000	23.9645	10.400	14.696	25.0174
13.0000	12.3720	0.7815	0.7536	1.4469	1.7121	1572.578	1512.257	1.2191	1.2155	4.6031	23.8573	11.371	14.627	24.9148
14.0000	12.4360	0.7306	0.6621	1.4382	1.4947	1577.593	1517.746	1.2193	1.2168	4.6060	23.7866	11.331	14.656	24.8131
15.0000	12.5024	0.6864	0.6381	1.2532	1.3467	1582.863	1523.388	1.2195	1.2177	4.6089	23.7298	11.687	14.685	24.7169
16.0000	12.5646	0.6476	0.6158	1.1894	1.2359	1588.295	1528.354	1.2197	1.2187	4.6116	23.6850	12.239	14.714	24.6178
17.0000	12.6239	0.6133	0.6085	1.1071	1.1502	1593.814	1533.410	1.2198	1.2198	4.6143	23.6506	12.787	14.743	24.5174
18.0000	12.6810	0.5828	0.5873	1.0426	1.0811	1598.762	1538.419	1.2199	1.2200	4.6171	23.6251	13.336	14.771	24.4174
19.0000	12.7370	0.5554	0.5699	0.9856	1.0238	1603.237	1543.343	1.2200	1.2219	4.6195	23.6006	13.881	14.796	24.3179
20.0000	12.7915	0.5308	0.5701	0.9390	0.9753	1608.148	1548.191	1.2201	1.2230	4.6220	23.5973	14.425	14.822	24.2174
21.0000	12.8446	0.5084	0.5830	0.8989	0.9336	1613.001	1552.971	1.2201	1.2241	4.6245	23.5929	14.967	14.849	24.1174
22.0000	12.8968	0.4881	0.6052	0.8639	0.8973	1617.803	1557.687	1.2201	1.2251	4.6269	23.5940	15.507	14.875	24.0174
23.0000	12.9474	0.4695	0.6366	0.8331	0.8652	1622.557	1562.351	1.2201	1.2262	4.6293	23.5999	16.047	14.901	23.9174
24.0000	12.9971	0.4526	0.6694	0.8056	0.8366	1627.269	1566.962	1.2201	1.2273	4.6316	23.6100	16.585	14.926	23.8174
25.0000	13.0460	0.4367	0.7010	0.7810	0.8113	1631.943	1571.527	1.2204	1.2284	4.6340	23.6245	17.123	14.951	23.7174
26.0000	13.0939	0.4222	0.7311	0.7587	0.7878	1636.580	1576.048	1.2207	1.2294	4.6362	23.6423	17.660	14.977	23.6174
27.0000	13.1410	0.4087	0.7596	0.7364	0.7647	1641.184	1580.531	1.2211	1.2304	4.6385	23.6642	18.198	14.992	23.5174
28.0000	13.1874	0.3962	0.7864	0.7198	0.7476	1645.759	1584.977	1.2214	1.2316	4.6407	23.6870	18.731	15.007	23.4174
29.0000	13.2330	0.3846	0.8123	0.7027	0.7297	1650.305	1589.389	1.2218	1.2328	4.6430	23.7134	19.266	15.021	23.3174
30.0000	13.2780	0.3737	0.8375	0.6870	0.7133	1654.825	1593.770	1.2221	1.2337	4.6452	23.7422	19.801	15.036	23.2174
31.0000	13.3224	0.3635	0.8617	0.6724	0.6981	1659.320	1598.122	1.2225	1.2348	4.6473	23.7721	20.335	15.051	23.1174
32.0000	13.3661	0.3539	0.8857	0.6588	0.6844	1663.794	1602.446	1.2229	1.2358	4.6495	23.8029	20.868	15.066	23.0174
33.0000	13.4093	0.3449	0.9093	0.6461	0.6720	1668.246	1606.745	1.2233	1.2369	4.6516	23.8345	21.401	15.081	22.9174
34.0000	13.4520	0.3365	0.9314	0.6342	0.6605	1672.678	1611.020	1.2236	1.2380	4.6538	23.8667	21.934	15.096	22.8174
35.0000	13.4941	0.3289	0.9529	0.6231	0.6489	1677.091	1615.272	1.2240	1.2390	4.6559	23.9144	22.467	15.111	22.7174
36.0000	13.5358	0.3219	0.9738	0.6126	0.6381	1681.487	1619.503	1.2244	1.2401	4.6580	23.9536	22.999	15.126	22.6174
37.0000	13.5770	0.3158	0.9942	0.6027	0.6278	1685.867	1623.715	1.2247	1.2412	4.6601	23.9936	23.531	15.141	22.5174
38.0000	13.6178	0.3107	0.1065	0.5934	0.6181	1690.231	1627.907	1.2251	1.2422	4.6622	24.0349	24.062	15.156	22.4174
39.0000	13.6582	0.3060	0.1205	0.5846	0.6097	1694.580	1632.081	1.2255	1.2433	4.6642	24.0772	24.594	15.171	22.3174
40.0000	13.6982	0.2965	0.2744	0.5762	0.5982	1698.915	1636.238	1.2259	1.2444	4.6663	24.1205	25.125	15.186	22.2174
41.0000	13.7378	0.2887	0.3283	0.5682	0.5903	1703.238	1640.380	1.2263	1.2454	4.6683	24.1645	25.656	15.201	22.1174
42.0000	13.7770	0.2831	0.3822	0.5606	0.5821	1707.547	1644.505	1.2267	1.2465	4.6704	24.2093	26.187	15.216	22.0174
43.0000	13.8159	0.2779	0.4357	0.5534	0.5746	1711.845	1648.617	1.2271	1.2476	4.6724	24.2548	26.717	15.231	21.9174
44.0000	13.8544	0.2730	0.4884	0.5465	0.5675	1716.132	1652.714	1.2275	1.2486	4.6744	24.3006	27.248	15.246	21.8174
45.0000	13.8926	0.2682	0.5420	0.5399	0.5607	1720.408	1656.799	1.2279	1.2497	4.6764	24.3475	27.778	15.261	21.7174
46.0000	13.9306	0.2636	0.5963	0.5336	0.5541	1724.674	1660.871	1.2283	1.2507	4.6784	24.3946	28.308	15.276	21.6174
47.0000	13.9682	0.2592	0.6489	0.5276	0.5479	1728.930	1664.930	1.2288	1.2518	4.6804	24.4421	28.838	15.291	21.5174
48.0000	14.0055	0.2547	0.7017	0.5218	0.5419	1733.177	1668.978	1.2292	1.2529	4.6824	24.4900	29.368	15.306	21.4174
49.0000	14.0425	0.2507	0.7543	0.5162	0.5361	1737.415	1673.016	1.2296	1.2539	4.6844	24.5383	29.898	15.321	21.3174

PRESS	M2	O2	M2C	CP	P	C
10.0000	0.15810E+00	0.48604E-01	0.95510E-01	0.12831E-00	0.75325E-01	0.34748E-01
11.0000	0.15870E+00	0.48368E-01	0.95279E-01	0.12947E-00	0.75448E-01	0.35044E-01
12.0000	0.15932E+00	0.48134E-01	0.95032E-01	0.13069E-00	0.75572E-01	0.35346E-01
13.0000	0.15995E+00	0.48339E-01	0.94782E-01	0.13196E-00	0.75699E-01	0.35652E-01
14.0000	0.16059E+00	0.48345E-01	0.94526E-01	0.13278E-00	0.75731E-01	0.35917E-01
15.0000	0.16123E+00	0.48342E-01	0.94264E-01	0.13384E-00	0.75754E-01	0.36148E-01
16.0000	0.16187E+00	0.48337E-01	0.93998E-01	0.13459E-00	0.75762E-01	0.36331E-01
17.0000	0.16254E+00	0.48319E-01	0.93727E-01	0.13592E-00	0.75741E-01	0.36470E-01
18.0000	0.16319E+00	0.48297E-01	0.93453E-01	0.13695E-00	0.75698E-01	0.36579E-01
19.0000	0.16385E+00	0.48301E-01	0.93176E-01	0.13795E-00	0.75643E-01	0.36662E-01
20.0000	0.16451E+00	0.48349E-01	0.92896E-01	0.13898E-00	0.75578E-01	0.36729E-01
21.0000	0.16517E+00	0.48400E-01	0.92614E-01	0.13994E-00	0.75504E-01	0.36779E-01
22.0000	0.16582E+00	0.48455E-01	0.92330E-01	0.14092E-00	0.75420E-01	0.36819E-01
23.0000	0.16648E+00	0.48512E-01	0.92044E-01	0.14188E-00	0.75328E-01	0.36851E-01
24.0000	0.16713E+00	0.48572E-01	0.91757E-01	0.14284E-00	0.75230E-01	0.36876E-01
25.0000	0.16778E+00	0.48633E-01	0.91469E-01	0.14378E-00	0.75128E-01	0.36895E-01
26.0000	0.16843E+00	0.48695E-01	0.91179E-01	0.14472E-00	0.75023E-01	0.36907E-01
27.0000	0.16908E+00	0.48759E-01	0.90889E-01	0.14565E-00	0.74917E-01	0.36913E-01
28.0000	0.16972E+00	0.48823E-01	0.90598E-01	0.14657E-00	0.74807E-01	0.36915E-01
29.0000	0.17036E+00	0.48888E-01	0.90307E-01	0.14748E-00	0.74695E-01	0.36913E-01
30.0000	0.17099E+00	0.48954E-01	0.90015E-01	0.14838E-00	0.74582E-01	0.36907E-01
31.0000	0.17162E+00	0.49021E-01	0.89723E-01	0.14927E-00	0.74468E-01	0.36897E-01
32.0000	0.17224E+00	0.49084E-01	0.89431E-01	0.15015E-00	0.74353E-01	0.36883E-01
33.0000	0.17286E+00	0.49149E-01	0.89139E-01	0.15103E-00	0.74238E-01	0.36865E-01
34.0000	0.17348E+00	0.49214E-01	0.88847E-01	0.15190E-00	0.74122E-01	0.36843E-01
35.0000	0.17409E+00	0.49279E-01	0.88555E-01	0.15275E-00	0.74006E-01	0.36818E-01
36.0000	0.17469E+00	0.49342E-01	0.88264E-01	0.15360E-00	0.73891E-01	0.36791E-01
37.0000	0.17529E+00	0.49406E-01	0.87973E-01	0.15443E-00	0.73775E-01	0.36762E-01
38.0000	0.17588E+00	0.49468E-01	0.87682E-01	0.15527E-00	0.73659E-01	0.36731E-01
39.0000	0.17646E+00	0.49529E-01	0.87392E-01	0.15609E-00	0.73543E-01	0.36698E-01
40.0000	0.17704E+00	0.49590E-01	0.87102E-01	0.15690E-00	0.73427E-01	0.36663E-01
41.0000	0.17761E+00	0.49650E-01	0.86813E-01	0.15771E-00	0.73311E-01	0.36627E-01
42.0000	0.17818E+00	0.49708E-01	0.86524E-01	0.15852E-00	0.73195E-01	0.36590E-01
43.0000	0.17874E+00	0.49766E-01	0.86236E-01	0.15932E-00	0.73079E-01	0.36552E-01
44.0000	0.17929E+00	0.49822E-01	0.85948E-01	0.16012E-00	0.72963E-01	0.36514E-01
45.0000	0.17984E+00	0.49877E-01	0.85662E-01	0.16091E-00	0.72847E-01	0.36475E-01
46.0000	0.18038E+00	0.49931E-01	0.85376E-01	0.16170E-00	0.72731E-01	0.36436E-01
47.0000	0.18091E+00	0.49983E-01	0.85092E-01	0.16248E-00	0.72615E-01	0.36396E-01
48.0000	0.18144E+00	0.50034E-01	0.84807E-01	0.16326E-00	0.72500E-01	0.36355E-01
49.0000	0.18196E+00	0.50084E-01	0.84524E-01	0.16404E-00	0.72384E-01	0.36314E-01

TABLE 11. Sample Output: Calculation of CJ State Using Spec (b) Subroutine and Input Data in Table 9.

HUGONIOT CURVE CALCULATIONS FOR GASEOUS MIXTURES---PROPULSION DYNAMICS LABORATORY---UNIVERSITY OF CALIFORNIA---BERKELEY

INITIAL CCNDITION OF MIXTURE

P1= 0.10000E 01 ATM TEMP= 288.720C DEGK ENTHALPY= / -0.12 SD VEL= 529.7653M/SEC
 V1= .19725E 04 CM3/GM CP1= 3.474 GAMMA1= 1.404 WM1= 12.011
 ENTRCPY= 19.2081

COMPOSITION OF MIXTURE

P2 = 0.66667E 00
 C2 = 0.33333E-00

THE PRESSURE RATIO OF THE HUGONIOT CURVE AT V2=V1 IS EQUAL TO 9.8845

THERMODYNAMIC PROPERTIES AT THE CHAPMAN-JOUQUET POINT

PRESS R. TEMP R VEL R MACH1 FMACH2 EMACH2 FSDVEL2 ESDVEL2 FGAMM2 EGAMM2 FSPHT ESPHT ENTH2 MOLWT ENTROPY
 19.4719 12.7629 7.5435 5.3682 0.9627 1.0000 1605.562 1545.640 1.2187 1.2224 4.6207 23.6020 14.138 14.485 25.1053

EQUILIBRIUM COMPOSITION AT THE CHAPMAN-JOUQUET POINT

H2 O2 H2C OH H O
 0.16416E-00 0.48523E-01 0.53044E 00 0.13843E-00 0.80365E-01 0.38083E-01

TABLE 12. Sample Output: Calculation of Shock Wave Parameters for Mach No. = 5.0 Using Spec (c) Subroutine and Input Data in Table 9.

HUGONIOT CURVE CALCULATIONS FOR GASEOUS MIXTURES---PROPULSION DYNAMICS LABORATORY--UNIVERSITY OF CALIFORNIA--BERKELEY

INITIAL CONDITION OF MIXTURE

P1=	0.10000E 01	ATM	TEMP=	288.7200	DEGK	ENTHALPY=	-0.12	SD	VEL=	529.7653	M/SEC
V1=	1.9725E 04	CM3/GM	CPI=	3.474		GAMMA1=	1.404		WMI=	12.011	
ENTROPY=			19.2081								

COMPOSITION OF MIXTURE

H2 = 0.66667E 00
D2 = 0.33333E-00

PROPERTIES BEHIND SHOCK WAVE

PRESS R	TEMP R	VEL R	MACH1	FNACH2	ESDVEL1	ESDVEL2	FGAMM2	EGAMM2	FSPHT	ESPHT	ENTH2	MOLWT	ENTROPY
29.6192	5.4713	0.1847	5.0000	0.4067	1202.980	1202.981	1.3233	1.3233	0.6772	0.6772	804.234	12.011	3.6617

COMPOSITION BEHIND SHOCK WAVE

42 02

0.66667E 00 0.33333E-00

TABLE 13. Computed Properties of CJ Detonations in Hydrogen-Oxygen Mixtures.

Initial Composition: $3H_2+O_2$

P_1	t_1	$a_1, m/sec$	M_1	$u_1, m/sec$	P	T	V	$a_{f,2}$	$a_{e,2}$	$U_{e,2}$	$\delta_{f,2}$	M_2
1 atm	-180°F	446.16	7.2603	3239.25	36.5907	23.8059	.5393	1807.518	1746.984	1.1986	1.2189	11.475
100 mm	-180°F	446.16	6.9991	3122.72	34.2422	21.6190	.5370	1751.861	1676.915	1.2009	1.2288	11.183
10 mm	-180°F	446.16	6.7048	2991.41	31.6546	19.4065	.5347	1688.182	1599.612	1.2028	1.2396	10.906
1 mm	-180°F	446.16	6.4249	2866.53	29.2600	17.5071	.5329	1627.183	1527.576	1.2041	1.2502	10.680
.1 mm	-180°F	446.16	6.1646	2750.40	27.0963	15.8922	.5315	1570.233	1461.721	1.2051	1.2602	10.497
1 atm	-50°F	532.19	6.0257	3206.81	24.6655	16.0074	.5422	1802.704	1738.678	1.2006	1.2214	11.386
100 mm	-50°F	532.19	5.8026	3088.08	23.0415	14.5256	.5402	1746.150	1668.072	1.2029	1.2314	11.101
10 mm	-50°F	532.19	5.5537	2955.62	21.2735	13.0406	.5383	1682.249	1590.967	1.2047	1.2422	10.832
1 mm	-50°F	532.19	5.3183	2830.35	19.6491	11.7715	.5363	1621.472	1519.514	1.2059	1.2528	10.615
.1 mm	-50°F	532.19	5.0999	2714.11	18.1863	10.6343	.5358	1564.921	1454.365	1.2069	1.2632	10.439
1 atm	60°F	595.49	5.3471	3184.14	19.2871	12.5069	.5448	1801.025	1734.677	1.2023	1.2232	11.322
100 mm	60°F	595.49	5.1447	3063.62	17.9942	11.3431	.5430	1743.856	1663.671	1.2046	1.2331	11.042
10 mm	60°F	595.49	4.9204	2930.05	16.5970	10.1837	.5415	1679.744	1586.602	1.2063	1.2440	10.778
1 mm	60°F	595.49	4.7089	2804.10	15.3187	9.1956	.5404	1619.025	1515.424	1.2075	1.2546	10.911
.1 mm	60°F	595.49	4.5130	2687.44	14.1698	8.3577	.5398	1562.648	1450.633	1.2084	1.2650	10.394
1 atm	200°F	668.056	4.7280	3158.57	15.0672	9.7704	.5483	1800.671	1731.837	1.2045	1.2252	11.250
100 mm	200°F	668.056	4.5445	3035.98	14.0364	8.8561	.5469	1742.815	1660.347	1.2067	1.2351	10.735
10 mm	200°F	668.056	4.3421	2900.76	12.9300	7.9504	.5458	1678.404	1583.214	1.2083	1.2460	10.716
1 mm	200°F	668.056	4.1520	2773.77	11.9226	7.1379	.5452	1617.665	1512.224	1.2095	1.2567	10.508
.1 mm	200°F	668.056	3.9760	2656.19	11.0196	6.5292	.5450	1561.393	1447.720	1.2103	1.2671	10.340

TABLE 13 - Continued

Initial Composition: 2H ₂ +O ₂												
P ₁	t ₁	a ₁ , m/sec	M ₁	u ₁ , m/sec	P	T	Y	a _{f,2}	a _{e,2}	Y _{e,2}	Y _{f,2}	m ₂
1 atm	-180°F	396.175	7.3100	2896.04	37.0324	24.3919	.5379	1612.874	1557.691	1.2187	1.2141	14.702
100 mm	-190°F	396.175	7.0347	2786.97	34.5105	21.9962	.5359	1560.775	1493.598	1.2216	1.2245	14.284
10 mm	-180°F	396.175	6.7318	2666.97	31.8188	19.6615	.5339	1502.532	1423.938	1.2237	1.2354	13.900
1 mm	-180°F	396.175	6.4474	2554.30	29.3713	17.6944	.5323	1447.493	1359.542	1.2257	1.2460	13.594
.1 mm	-180°F	396.175	6.1847	2450.22	27.1800	16.0389	.5309	1396.487	1300.903	1.2274	1.2564	13.349
1 atm	60°F	529.765	5.3682	2843.88	19.4719	12.7629	.5435	1605.562	1545.640	1.2224	1.2187	14.485
100 mm	60°F	529.765	5.1580	2732.53	18.1071	11.5150	.5421	1552.69	1481.19	1.2250	1.2289	14.091
10 mm	60°F	529.765	4.9291	2611.26	16.6674	10.3032	.5407	1494.462	1412.029	1.2271	1.2398	13.730
1 mm	60°F	529.765	4.7155	2498.11	15.3675	9.2854	.5398	1439.891	1348.540	1.2288	1.2504	13.444
.1 mm	60°F	529.765	4.5185	2393.74	14.2076	8.4293	.5393	1389.517	1290.92	1.2304	1.2607	13.213

Initial Composition: H₂+O₂

1atm	-180°F	331.505	7.1299	2363.60	34.9237	22.7884	.5388	1318.225	1273.395	1.1785	1.2159	20.600
100mm	-180°F	331.505	6.8969	2286.36	32.8918	20.9133	.5366	1281.020	1226.811	1.1790	1.2241	20.154
10mm	-180°F	331.505	6.6295	2197.71	30.6036	18.9482	.5344	1237.933	1174.512	1.1802	1.2335	19.595
1mm	-180°F	331.505	6.3706	2111.88	28.4396	17.2110	.5327	1196.018	1124.932	1.1818	1.2431	19.323
.1mm	-180°F	331.505	6.1262	2030.86	26.4501	15.7023	.5313	1156.334	1078.975	1.1837	1.2526	19.005
1atm	60°F	444.891	5.2267	2325.3	18.4466	12.0249	.5446	1314.931	1266.294	1.1810	1.2135	20.359
100mm	60°F	444.891	5.0456	2244.74	17.3177	11.0121	.5429	1276.50	1219.741	1.1819	1.2279	19.920
10mm	60°F	444.891	4.8414	2153.89	16.0712	9.9698	.5415	1232.65	1166.24	1.1834	1.2375	19.486
1mm	60°F	444.891	4.6455	2066.74	14.9074	9.0580	.5404	1190.895	1116.976	1.1853	1.2472	19.122
.1mm	60°F	444.891	4.4617	1984.97	13.8450	8.2701	.5398	1151.42	1071.56	1.1872	1.2567	18.819

TABLE 13 - Continued

Initial Composition: 3H ₂ +O ₂										Initial Composition: 2H ₂ +O ₂									
P ₁	t ₁	H ₂	O ₂	H ₂ O	OH	H	O			P ₁	t ₁	H ₂	O ₂	H ₂ O	OH	H	O		
1 atm	-180°F	.31933	.00665	.50747	.07179	.08414	.01062			1 atm	-180°F	.15952	.046174	.55264	.13717	.070604	.033889		
100 mm	-180°F	.31090	.00949	.47769	.075648	.11074	.015523			100 mm	-180°F	.16628	.052092	.51396	.13233	.092943	.042401		
10 mm	-180°F	.29959	.01258	.45335	.074144	.13974	.020594			10 mm	-180°F	.16879	.058170	.48293	.12185	.11783	.050437		
1 mm	-180°F	.28726	.01539	.43702	.068900	.16674	.024686			1 mm	-180°F	.16763	.063719	.46176	.10887	.14152	.056513		
.1 mm	-180°F	.27447	.017907	.42649	.061827	.19163	.027665			.1 mm	-180°F	.16408	.068829	.44737	.095236	.16378	.060698		
1 atm	-50°F	.31778	.00743	.49719	.074423	.09115	.012031			1 atm	60°F	.16416	.048523	.53044	.13843	.080365	.038083		
100 mm	-50°F	.30990	.010294	.46901	.076953	.11785	.016992			100 mm	60°F	.16902	.054213	.49580	.13155	.10306	.046348		
10 mm	-50°F	.29725	.013357	.44630	.074406	.14670	.021982			10 mm	60°F	.16999	.060096	.46827	.11973	.12798	.053923		
1 mm	-50°F	.28472	.016134	.43124	.068541	.17345	.02920			1 mm	60°F	.16777	.065499	.44961	.10612	.15152	.059479		
.1 mm	-50°F	.27182	.018606	.42164	.061138	.19808	.028723			.1 mm	60°F	.16350	.070494	.437000	.092277	.17357	.063157		
1 atm	60°F	.31671	.00799	.48981	.076281	.096122	.013077												
100 mm	60°F	.30754	.010865	.46267	.077947	.12291	.018078			Initial Composition: H ₂ +O ₂									
10 mm	60°F	.29566	.013915	.44100	.074724	.15168	.023022			1 atm	-180°F	.034511	.26595	.48994	.14204	.020248	.047316		
1 mm	60°F	.28298	.016673	.42673	.068452	.17829	.026864			100 mm	-180°F	.043211	.26006	.46256	.14153	.031890	.060756		
.1 mm	60°F	.27000	.019123	.41772	.060825	.20277	.029555			10 mm	-180°F	.051053	.25660	.43792	.1336	.047005	.073833		
1 atm	200°F	.31555	.0086284	.48142	.078368	.10173	.014302			1 mm	-180°F	.056588	.25578	.41929	.12130	.063062	.083973		
100 mm	200°F	.30605	.011512	.45535	.079127	.12861	.019349			.1 mm	-180°F	.060081	.25682	.40534	.10725	.079325	.091195		
10 mm	200°F	.29393	.014552	.43475	.075197	.15733	.024246			1 atm	60°F	.039008	.26140	.47370	.14630	.025344	.054254		
1 mm	200°F	.28110	.017291	.42131	.068492	.18382	.027993			100 mm	60°F	.047215	.25651	.44795	.14282	.038071	.067431		
.1 mm	200°F	.26802	.019725	.41291	.06021	.20815	.030569			10 mm	60°F	.054302	.25402	.42523	.13264	.054006	.079800		
										1 mm	60°F	.059089	.25394	.40823	.11910	.070550	.089089		
										.1 mm	60°F	.061928	.25551	.39554	.10447	.087085	.095470		

TABLE 15. Stoichiometric Hydrogen-Oxygen Detonation Parameters
Initial Pressure 1.0 ATM

SOURCE	INITIAL TEMP. K°	MEASURED VELOCITY m/sec.	CALCULATED PERAMETERS		
			Velocity m/sec.	P ₂ atm.	T ₂ °K
Lewis and Friauf (1)	291.00	2819	2806	18.05	3583
Berets et al (2)	298.16	2833	2852	18.06	3678
Luker et al (5)	298.16	-----	2845	18.10	3674
Eisen et al (6)	294.00	-----	2838	18.82	3675
Barrere et al (8)	298.16	-----	2848	18.93	3686
Zeleznik and Gordon (9)	298.15	-----	2840	18.82	3681
Present Work	298.00	-----	2840	18.84	3682

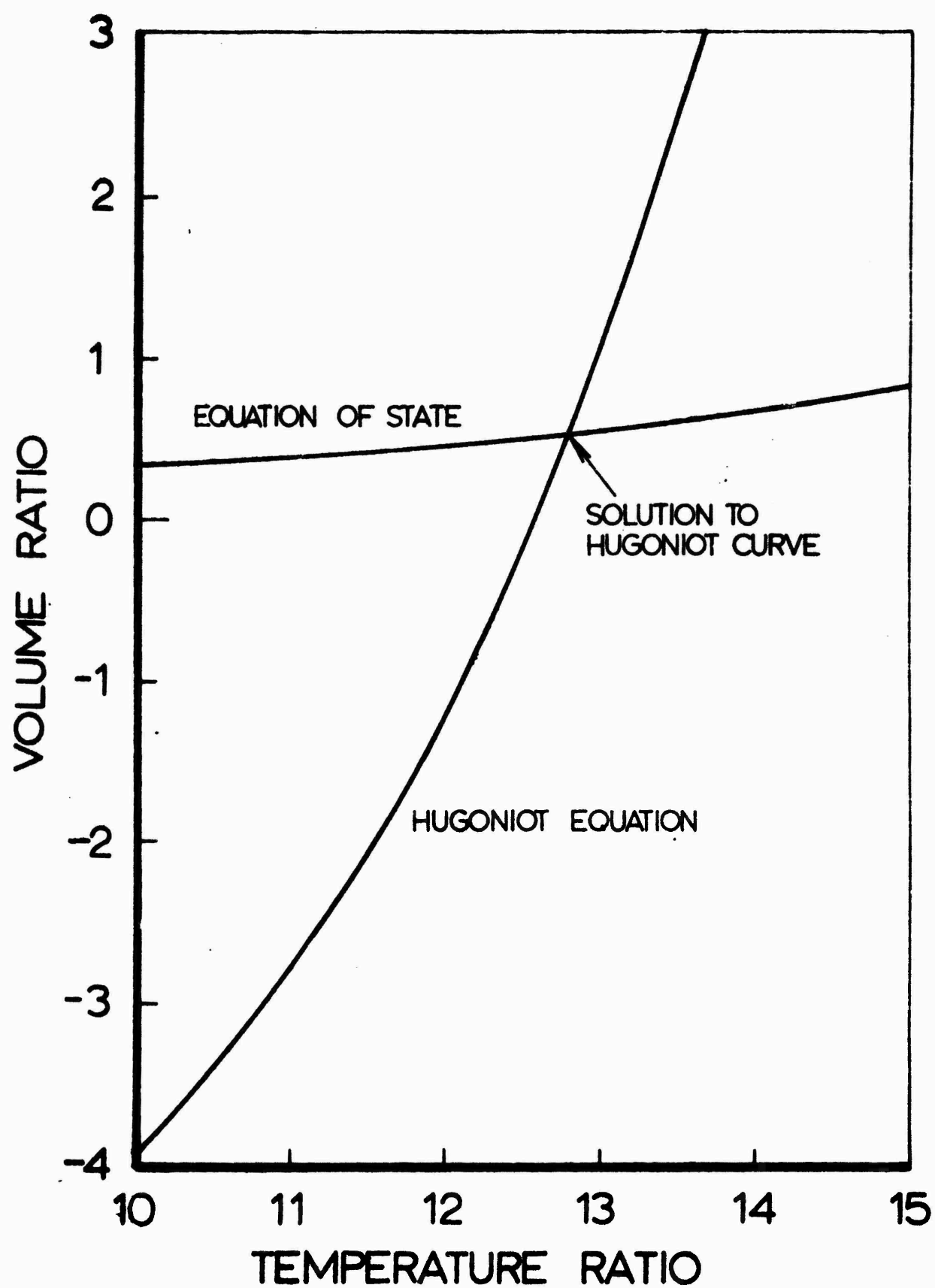


Fig. 1: Determination of a Point on the Hugoniot Curve in the V - P Plane

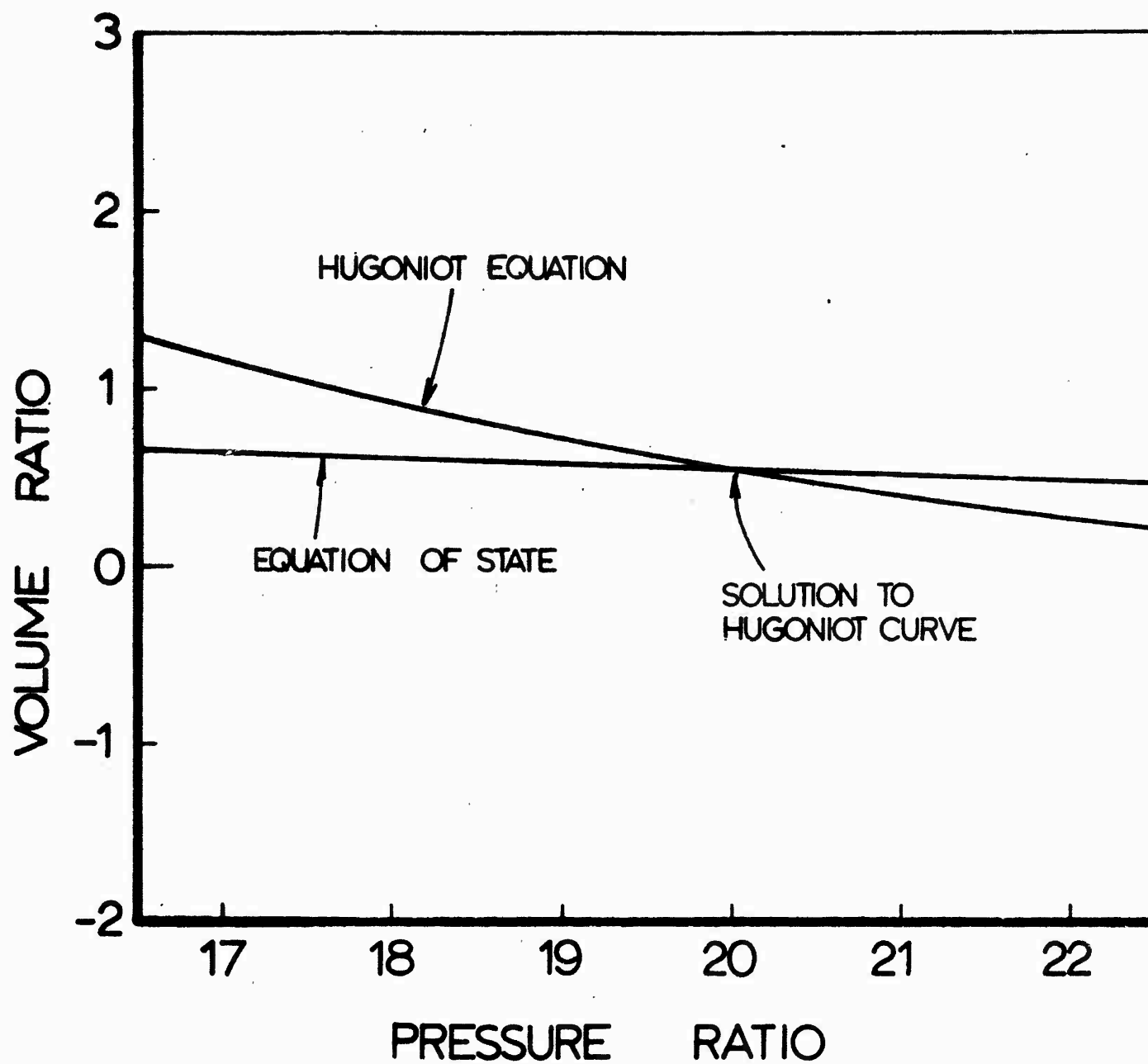


Fig. 2: Determination of a Point on the Hugoniot Curve in the $V-\theta$ Plane

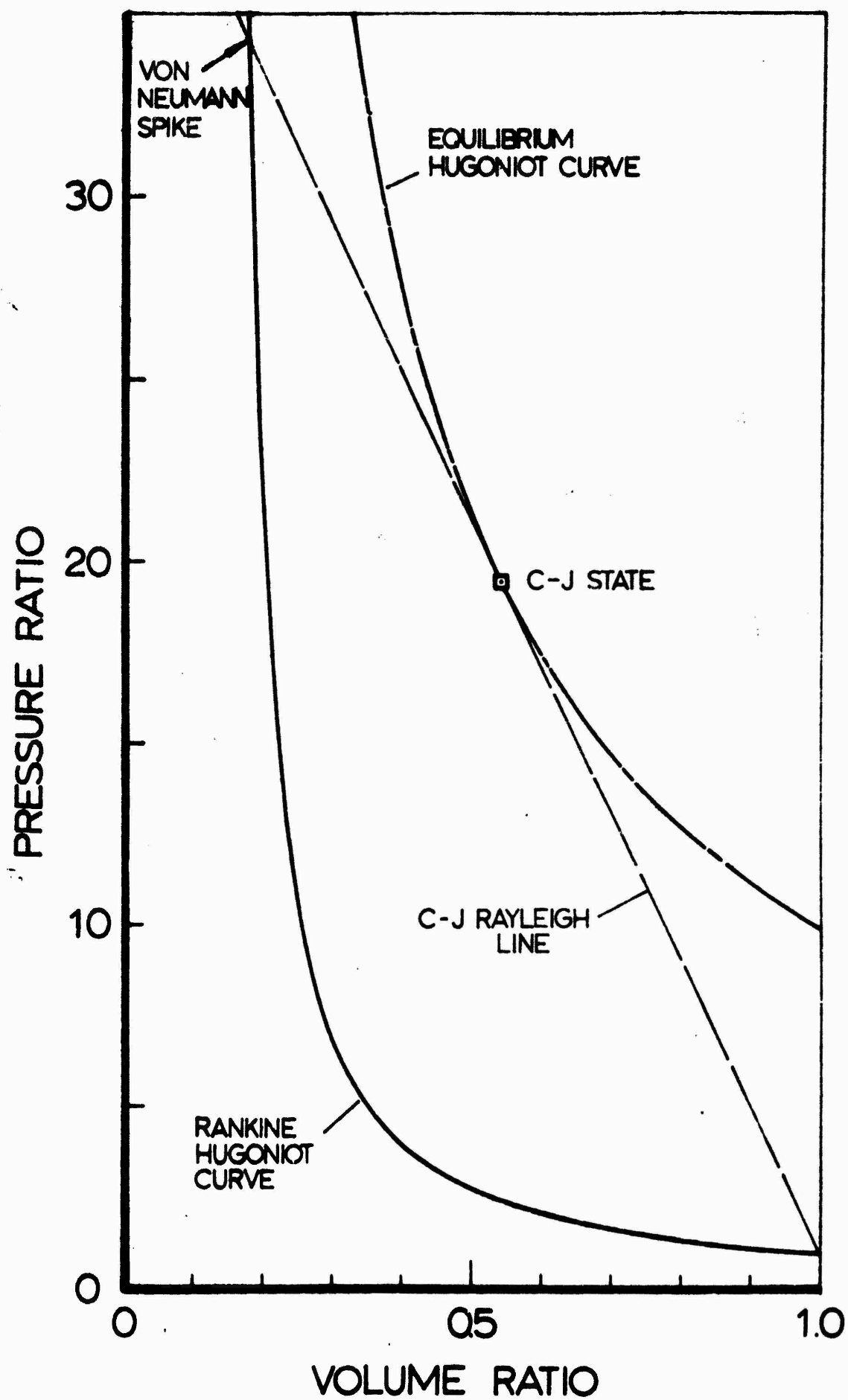


Fig. 3: Diagram Showing Hugoniot Curve, Rankine-Hugoniot Curve, and CJ Rayleigh Line for $2\text{H}_2 + \text{O}_2$ Mixture at 60°F , 760 mm Hg.

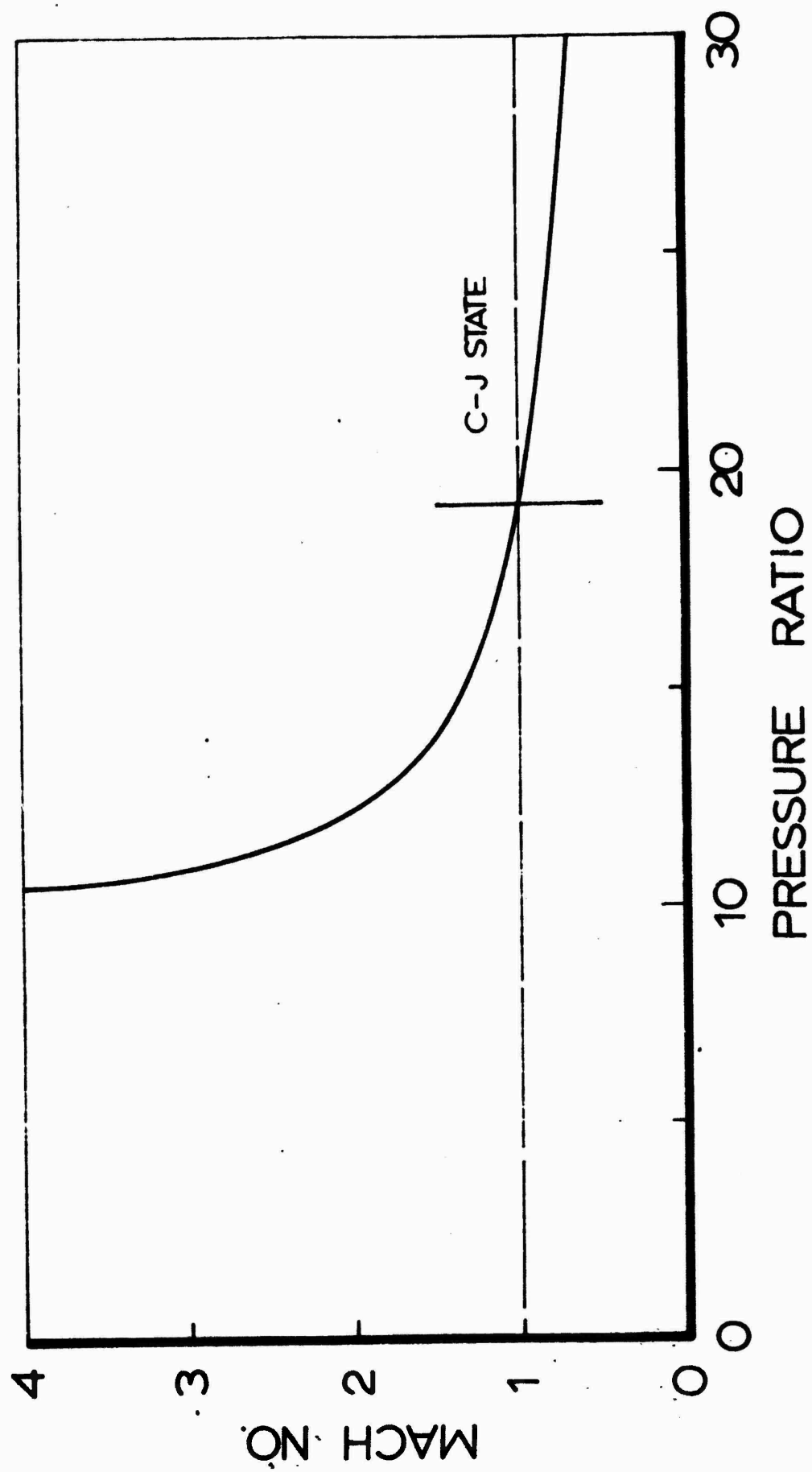


Fig. 4: Determination of the CJ State in the M_c - P Plane

FLOW DIAGRAM

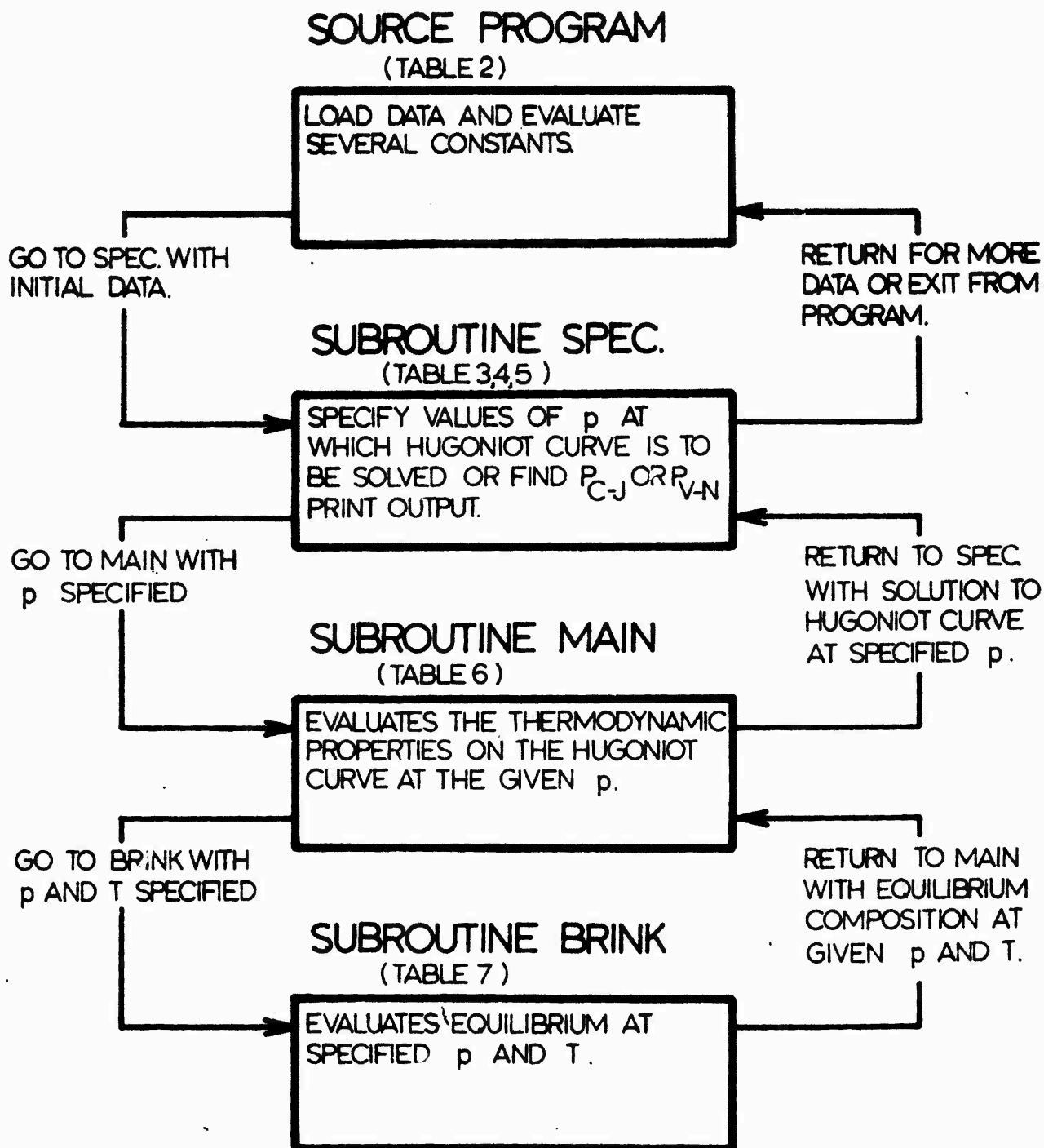


Fig. 5: Flow Diagram of Computer Program

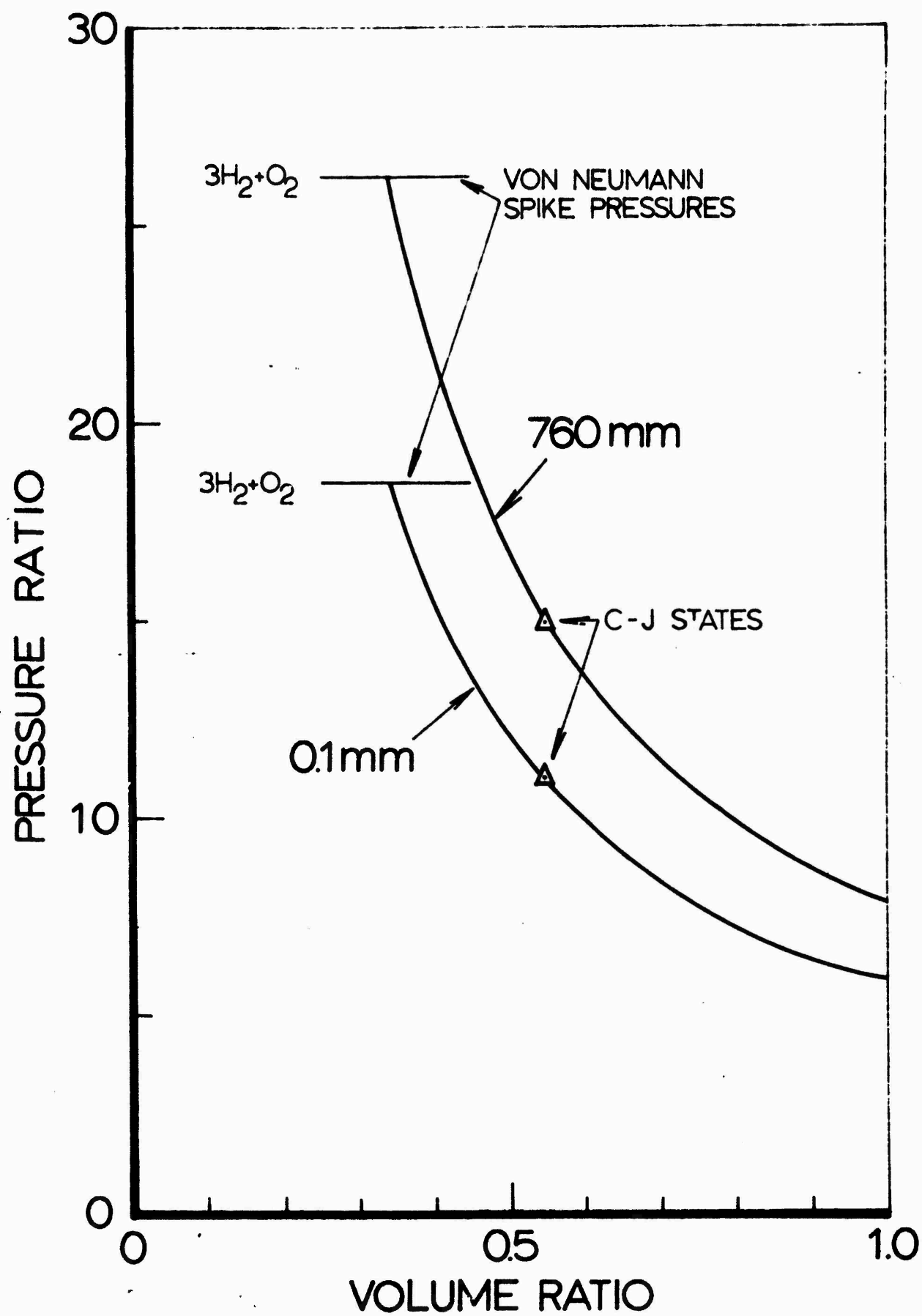


Fig. 6: Hugoniot Curves for $3\text{H}_2 + \text{O}_2$ Mixture Initially at 200°F

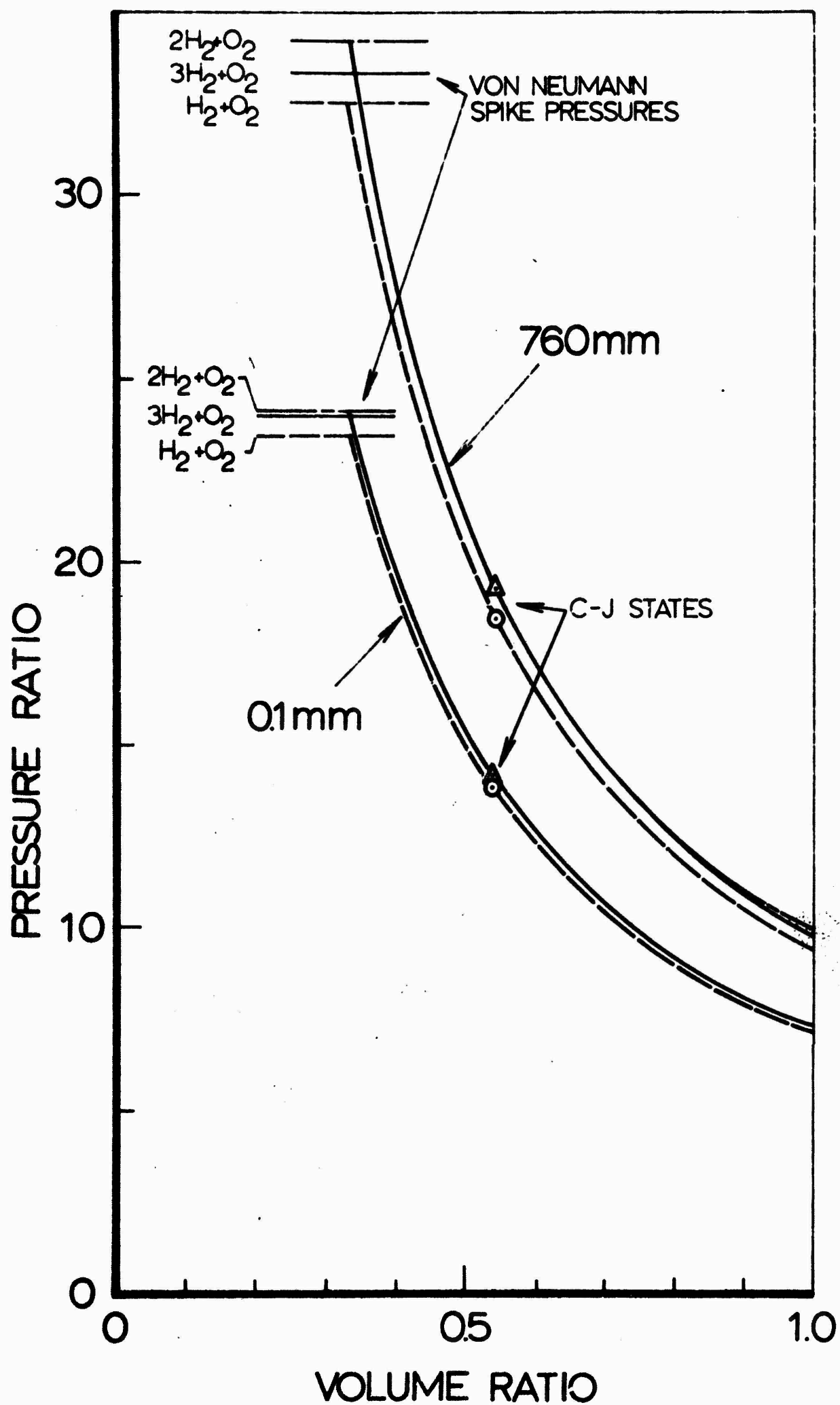


Fig. 7: Hugoniot Curves for Hydrogen-Oxygen Mixtures
Initially at 60°F

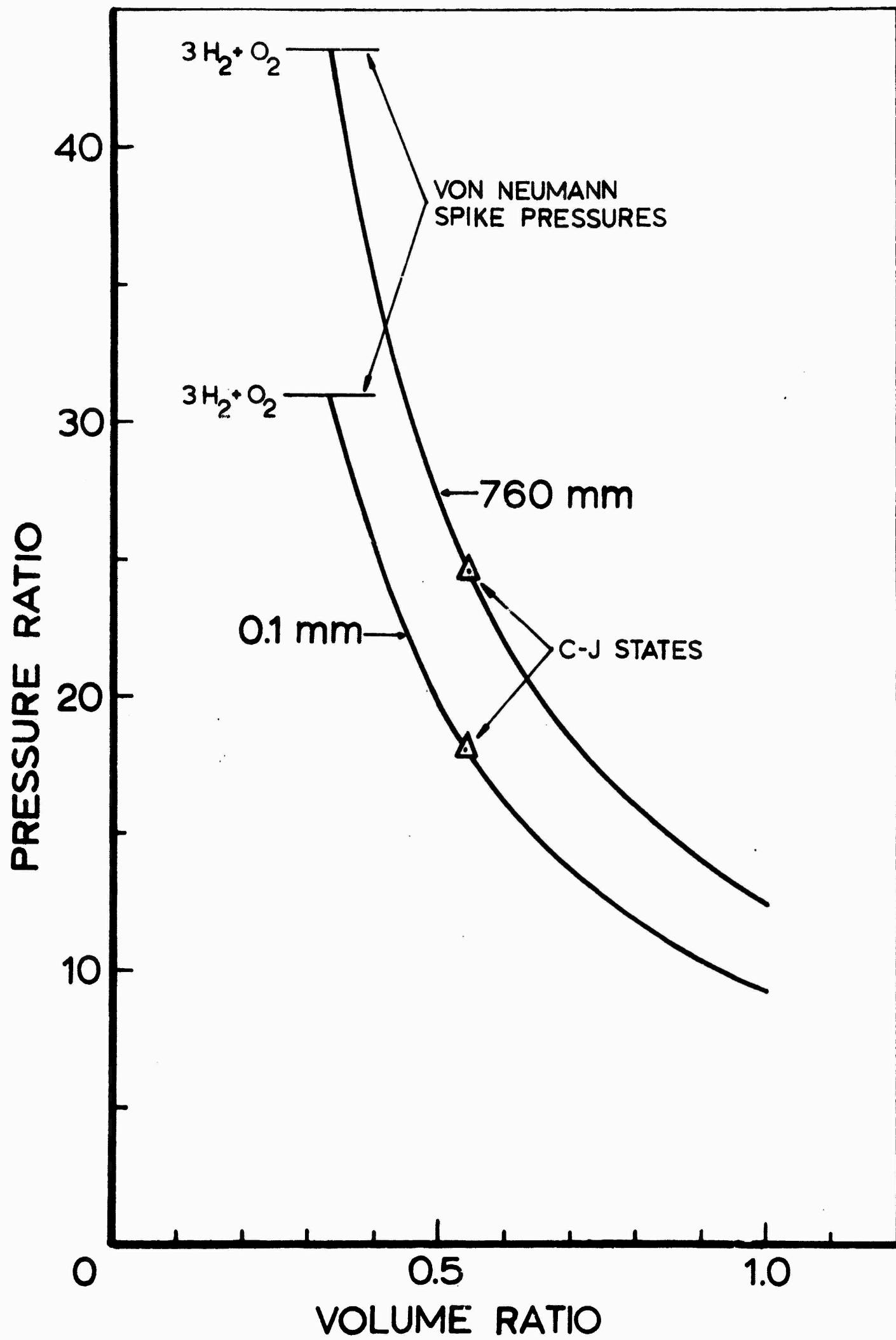


Fig. 8: Hugoniot Curves for $3\text{H}_2 + \text{O}_2$ Mixture Initially at -50°F

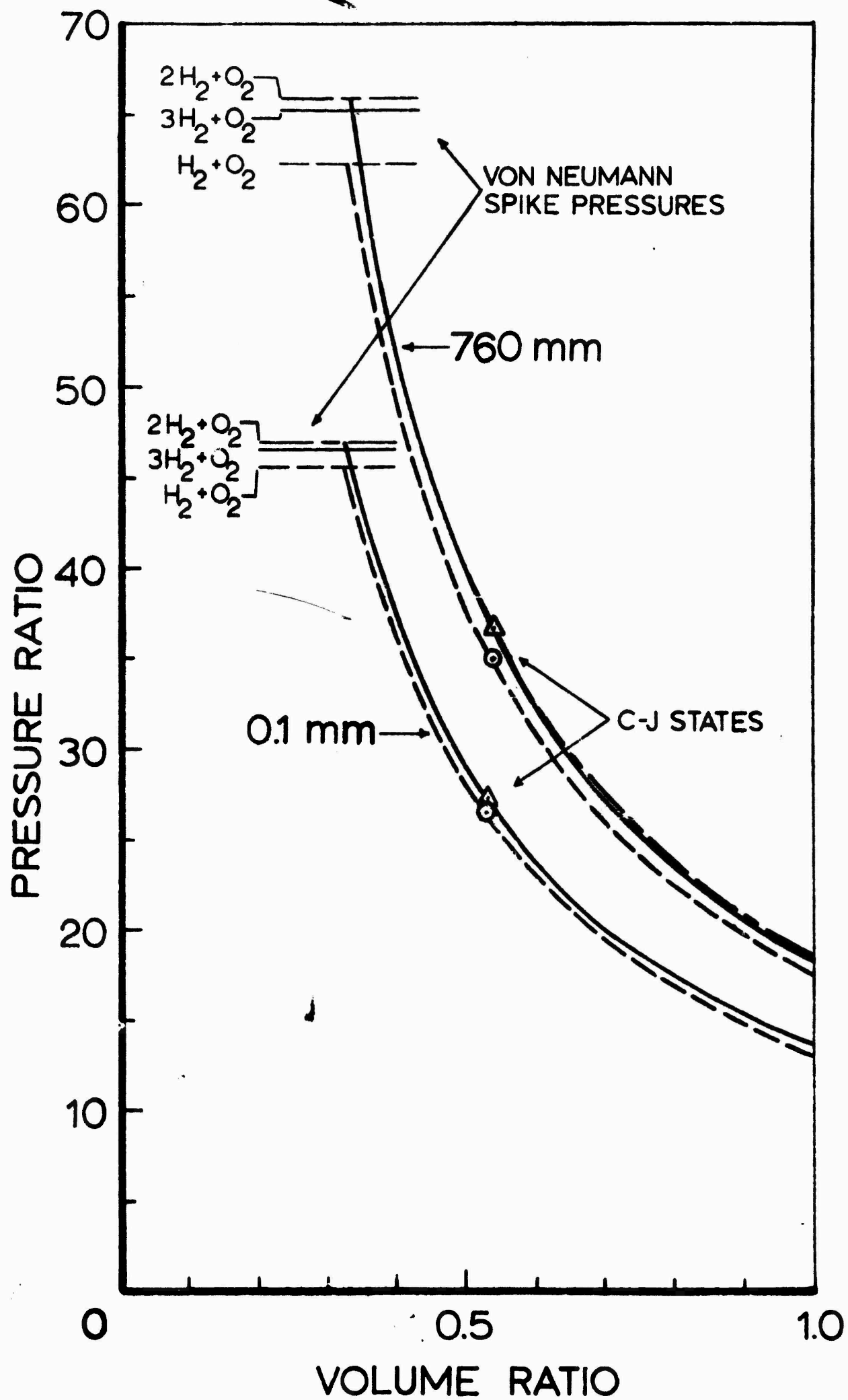


Fig. 9: Hugoniot Curves for Hydrogen-Oxygen Mixtures
Initially at -180°F

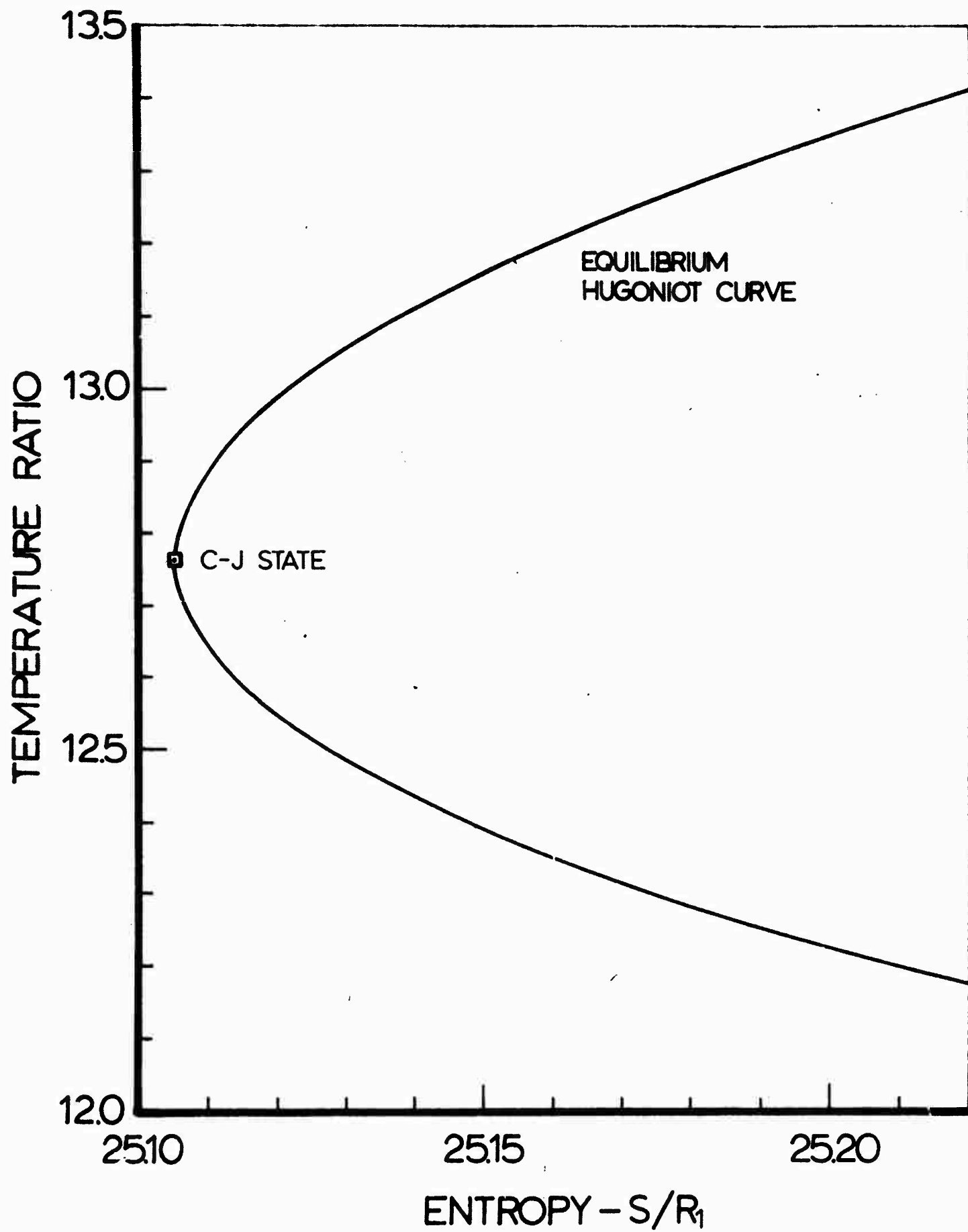


Fig. 10: Hugoniot Curve in Dimensionless Temperature-Entropy Diagram for $2\text{H}_2 + \text{O}_2$ Mixture Initially at 60°F , 760 mmHg.

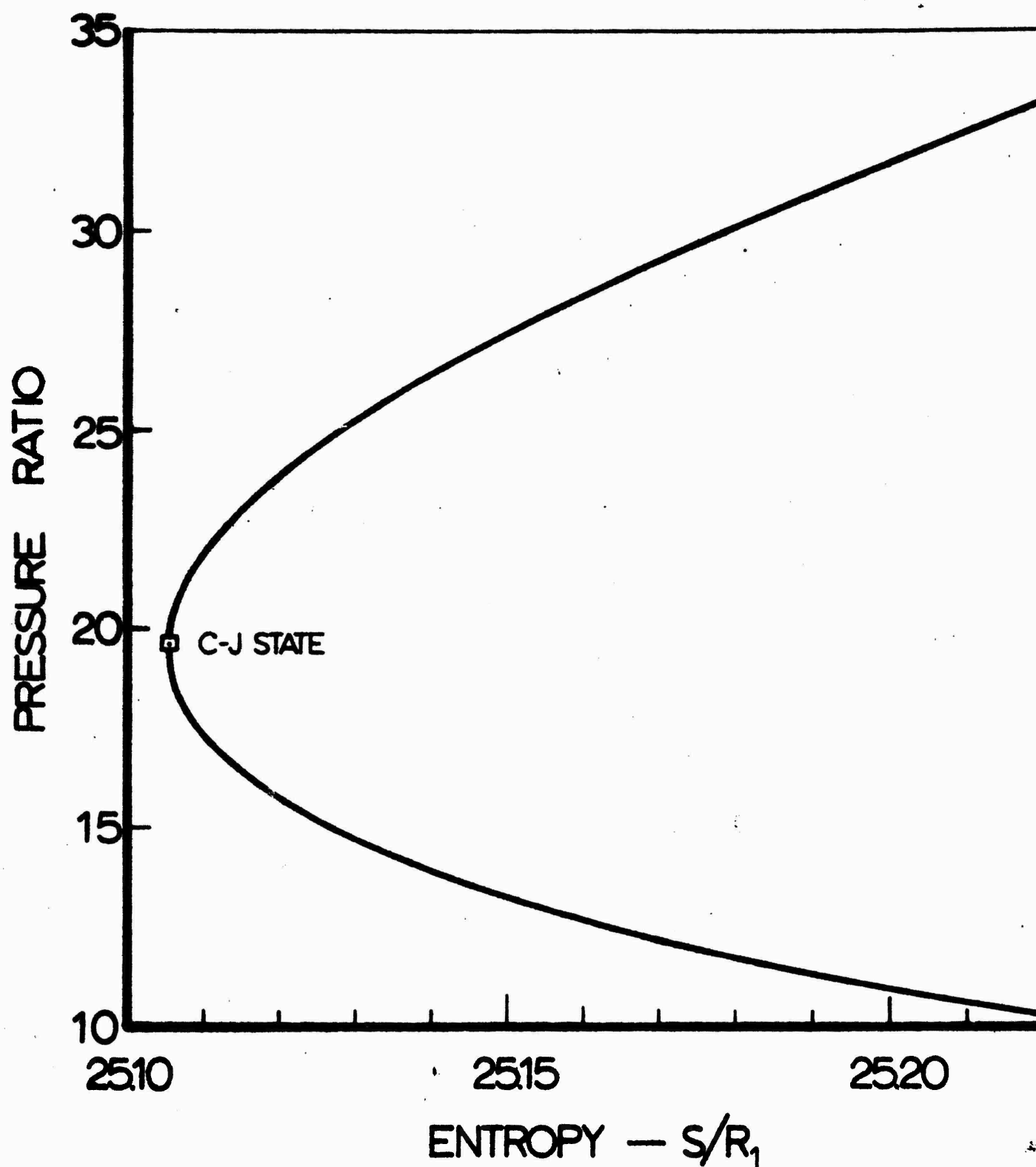


Fig. 11: Hugoniot Curve in Dimensionless Pressure-Entropy Diagram
for Mixture Initially at 60°F, 760 mmHg

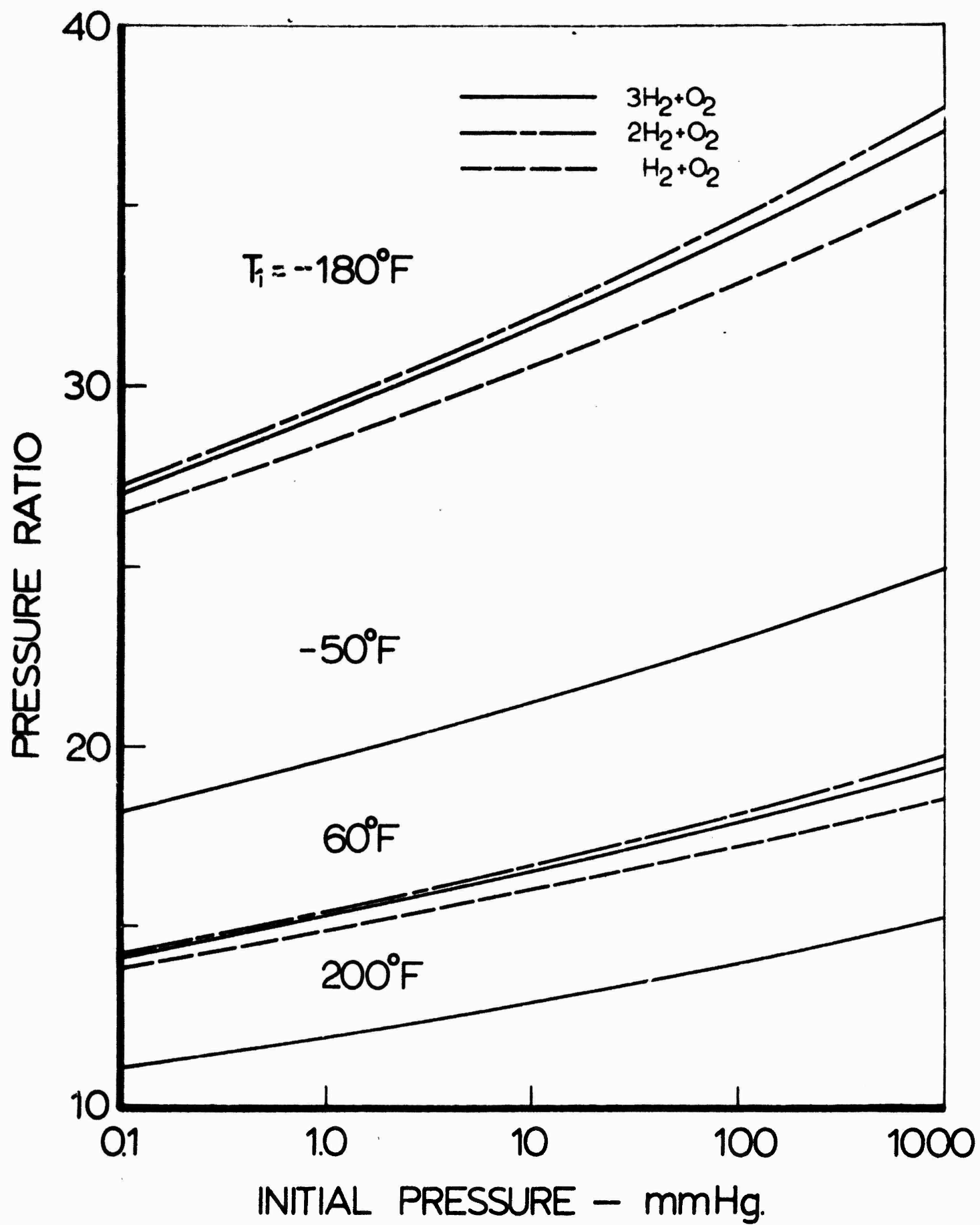


Fig. 12: Influence of Initial Pressure on CJ Pressure Ratio

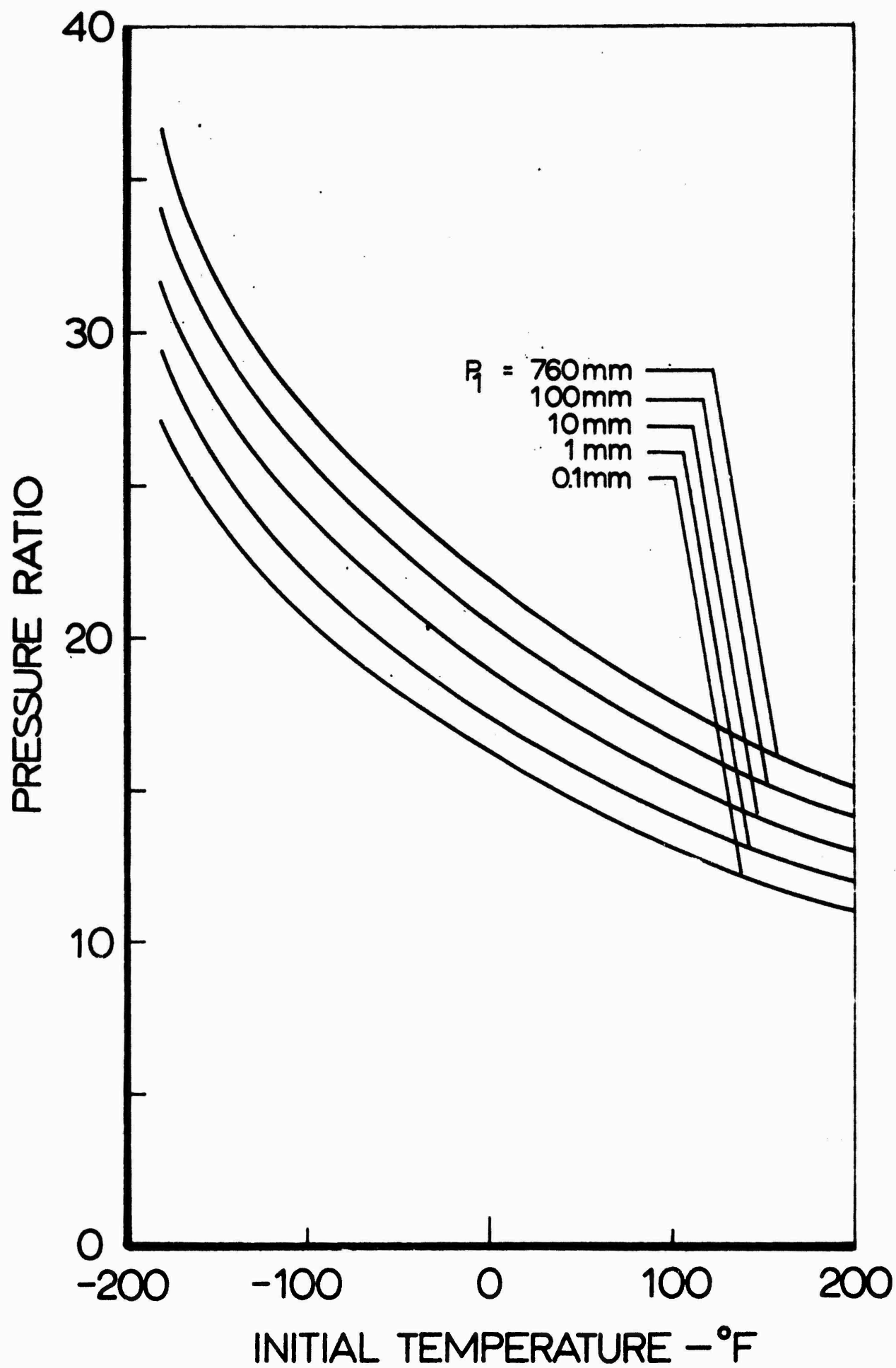


Fig. 13: Influence of Initial Temperature on CJ Pressure Ratio
for $3\text{H}_2 + \text{O}_2$ Mixture

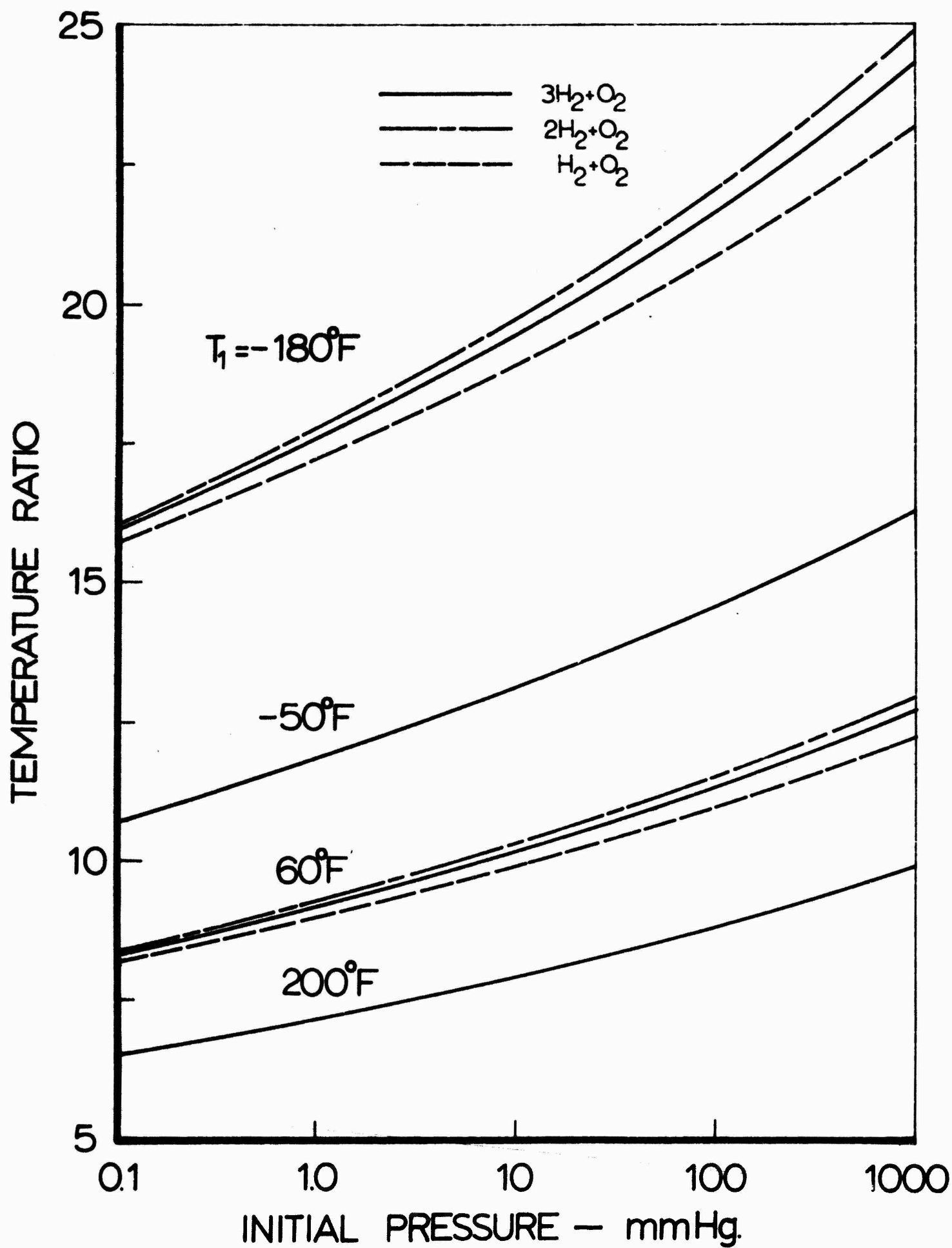


Fig. 14: Influence of Initial Pressure on CJ Temperature Ratio

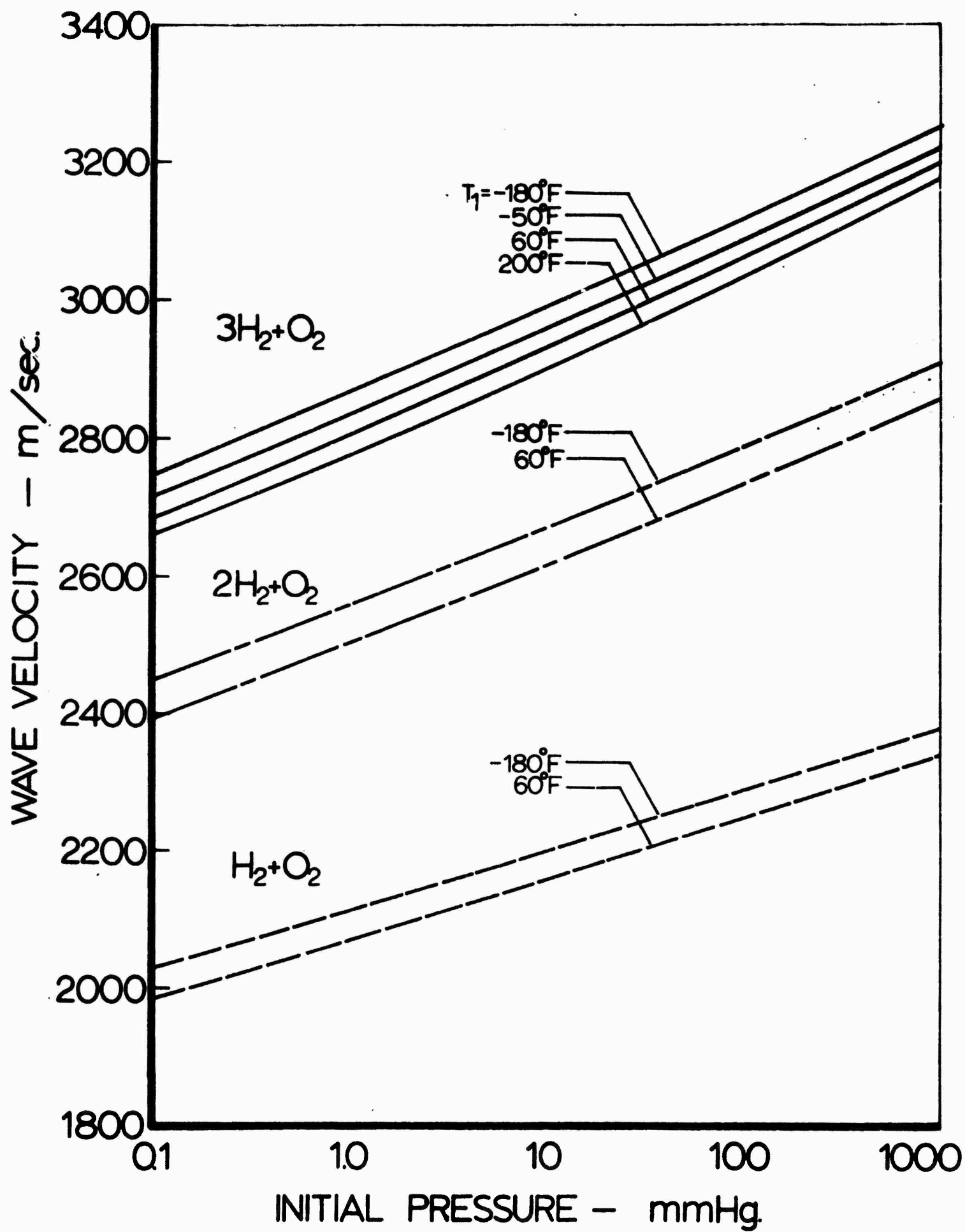


Fig. 15: Influence of Initial Pressure on CJ Detonation Velocity

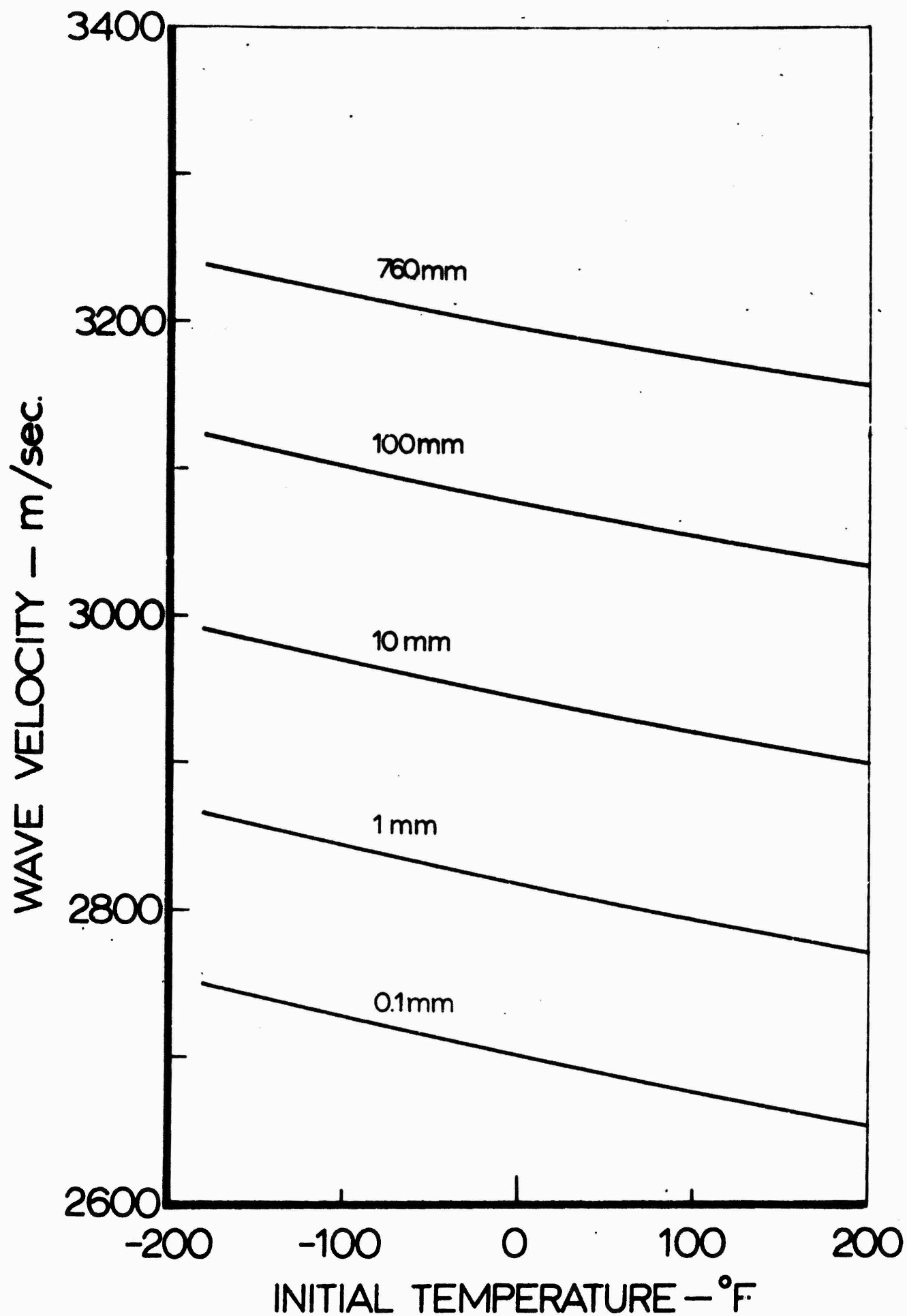


Fig. 16: Influence of Initial Temperature on CJ Detonation Velocity for $3\text{H}_2 + \text{O}_2$ Mixture

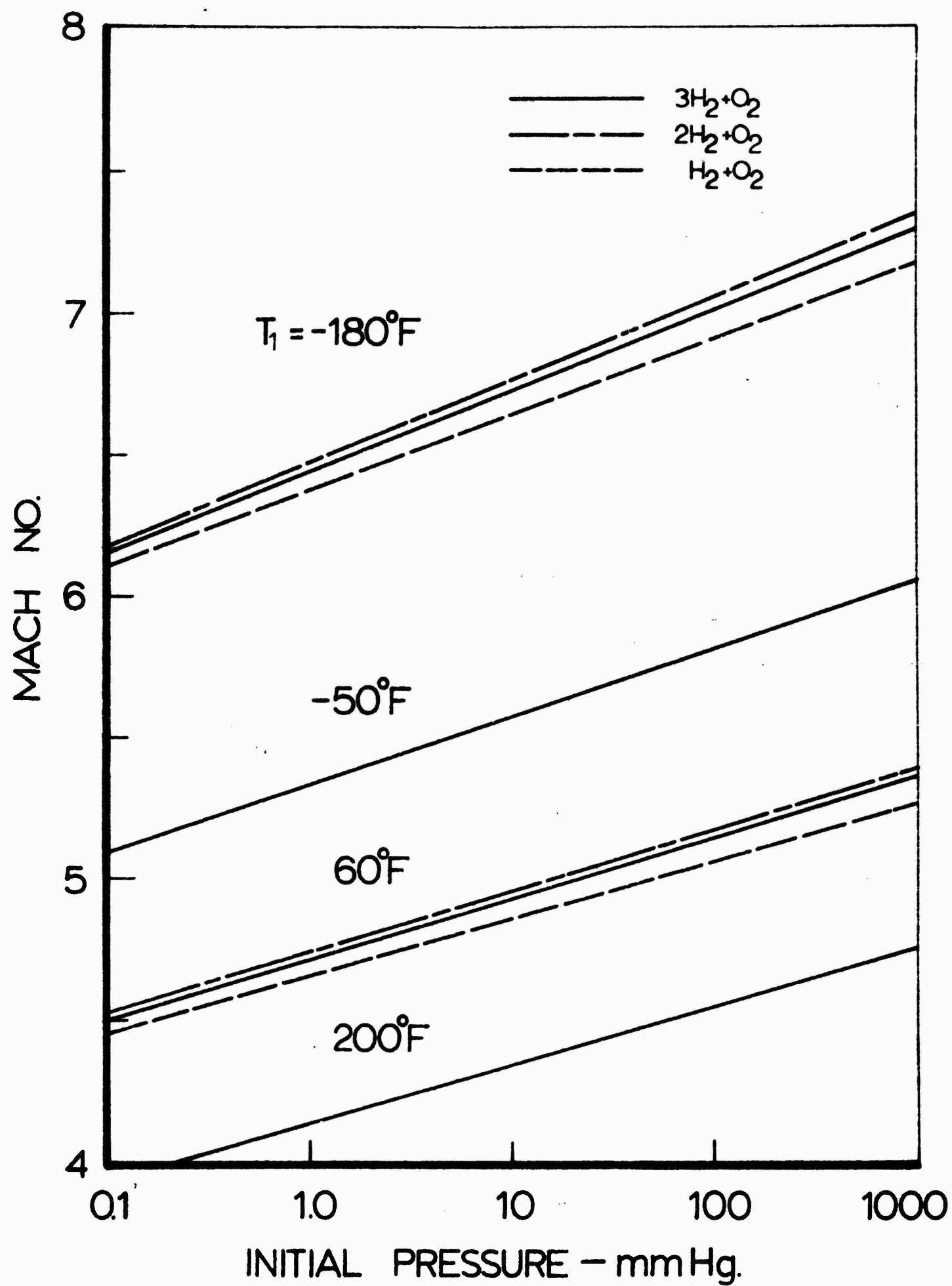


Fig. 17: Influence of Initial Pressure on CJ Detonation Mach Number

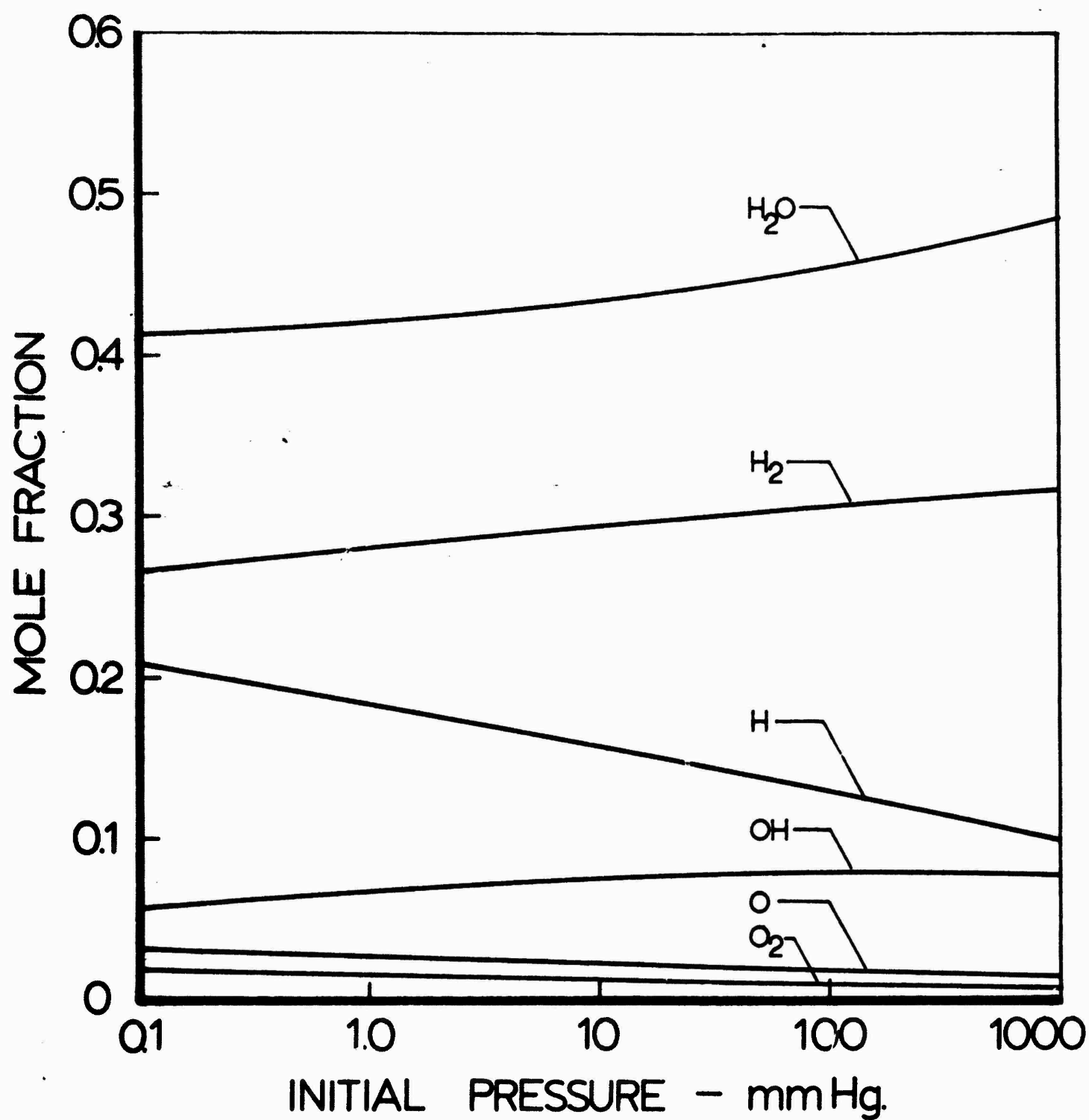


Fig. 18: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $3\text{H}_2 + \text{O}_2$ Mixture Initially at 200°F

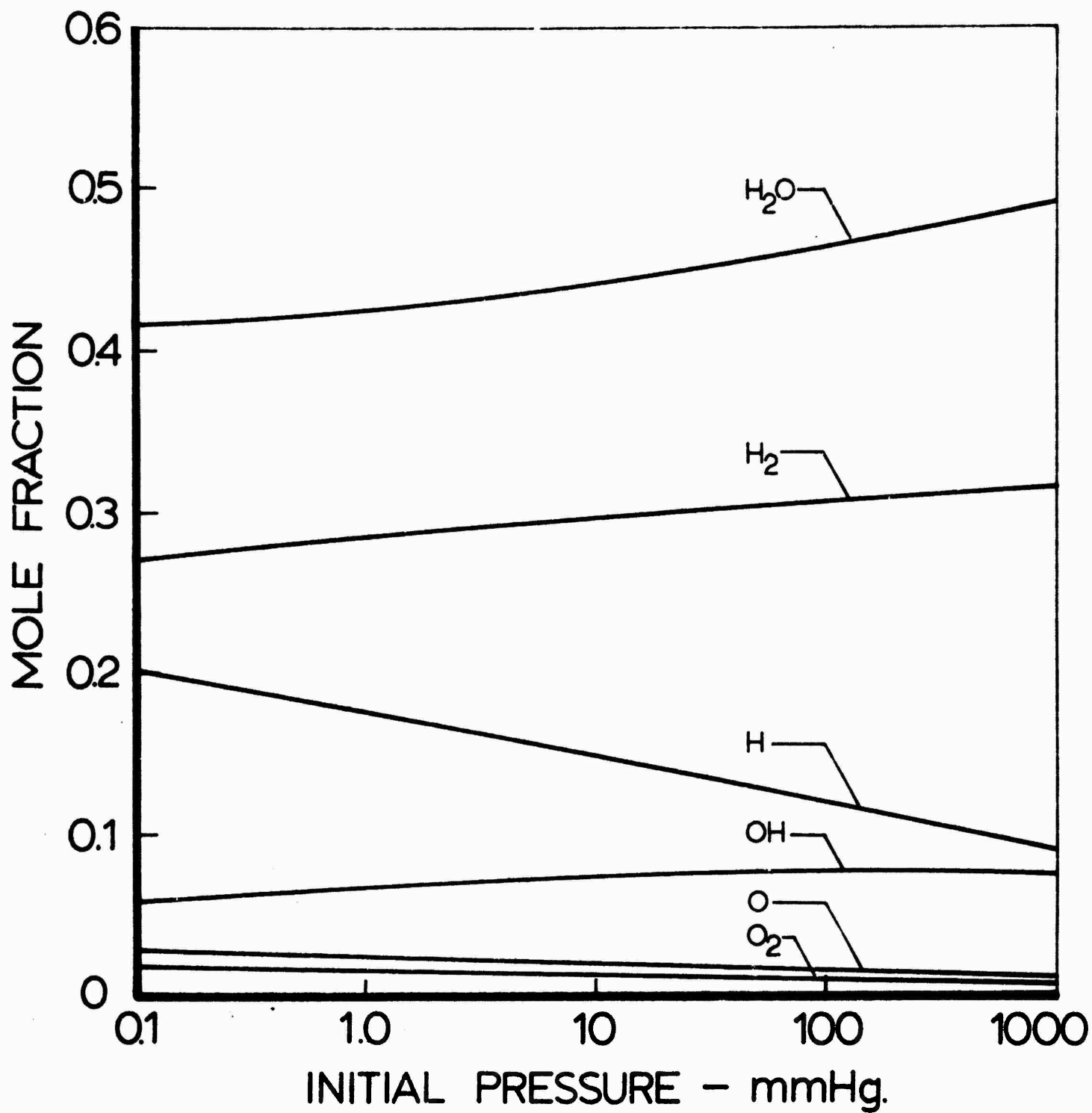


Fig. 19: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $3\text{H}_2 + \text{O}_2$ Mixture Initially at 60°F

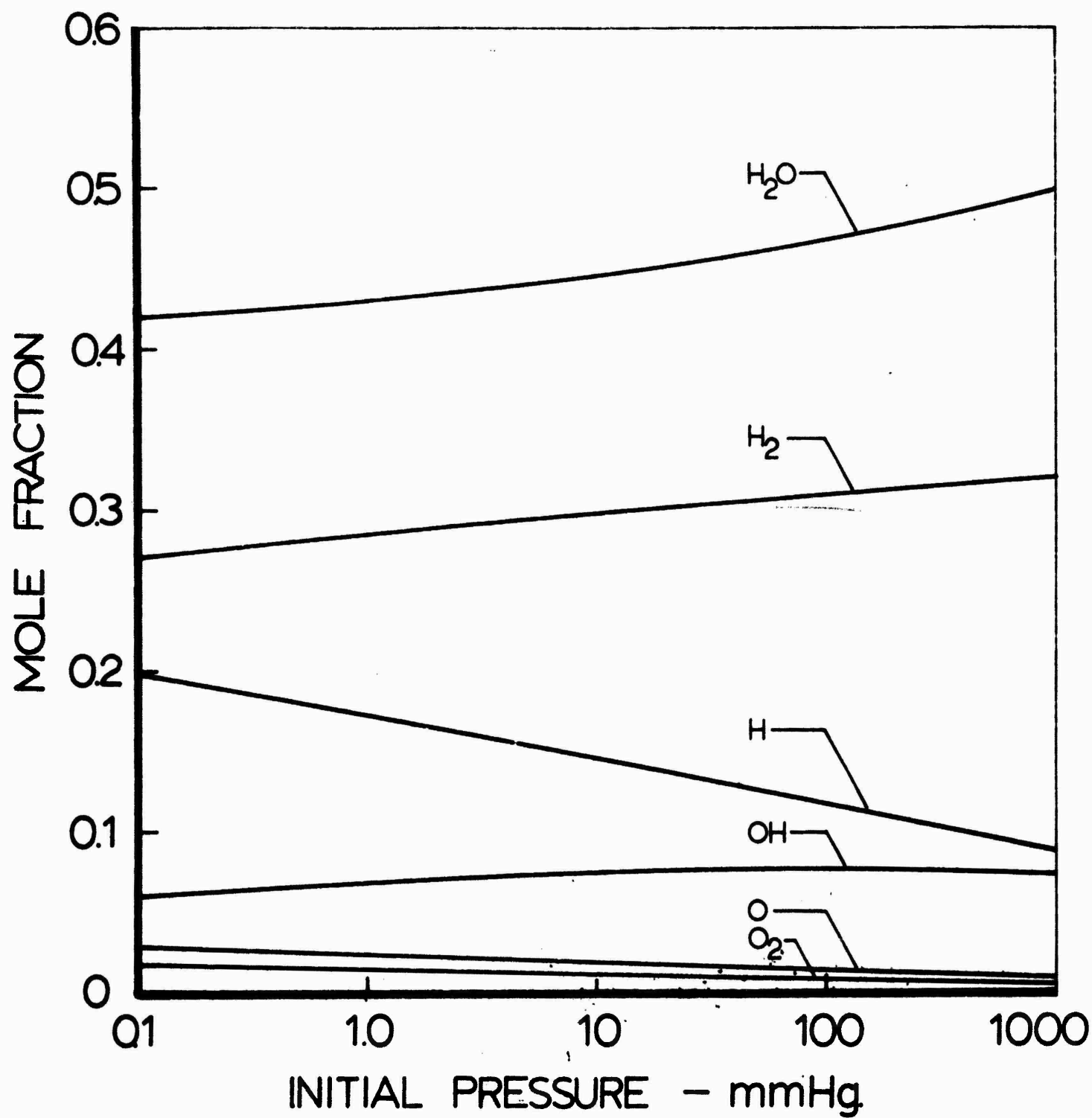


Fig. 20: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $3\text{H}_2 + \text{O}_2$ Mixture Initially at -50°F

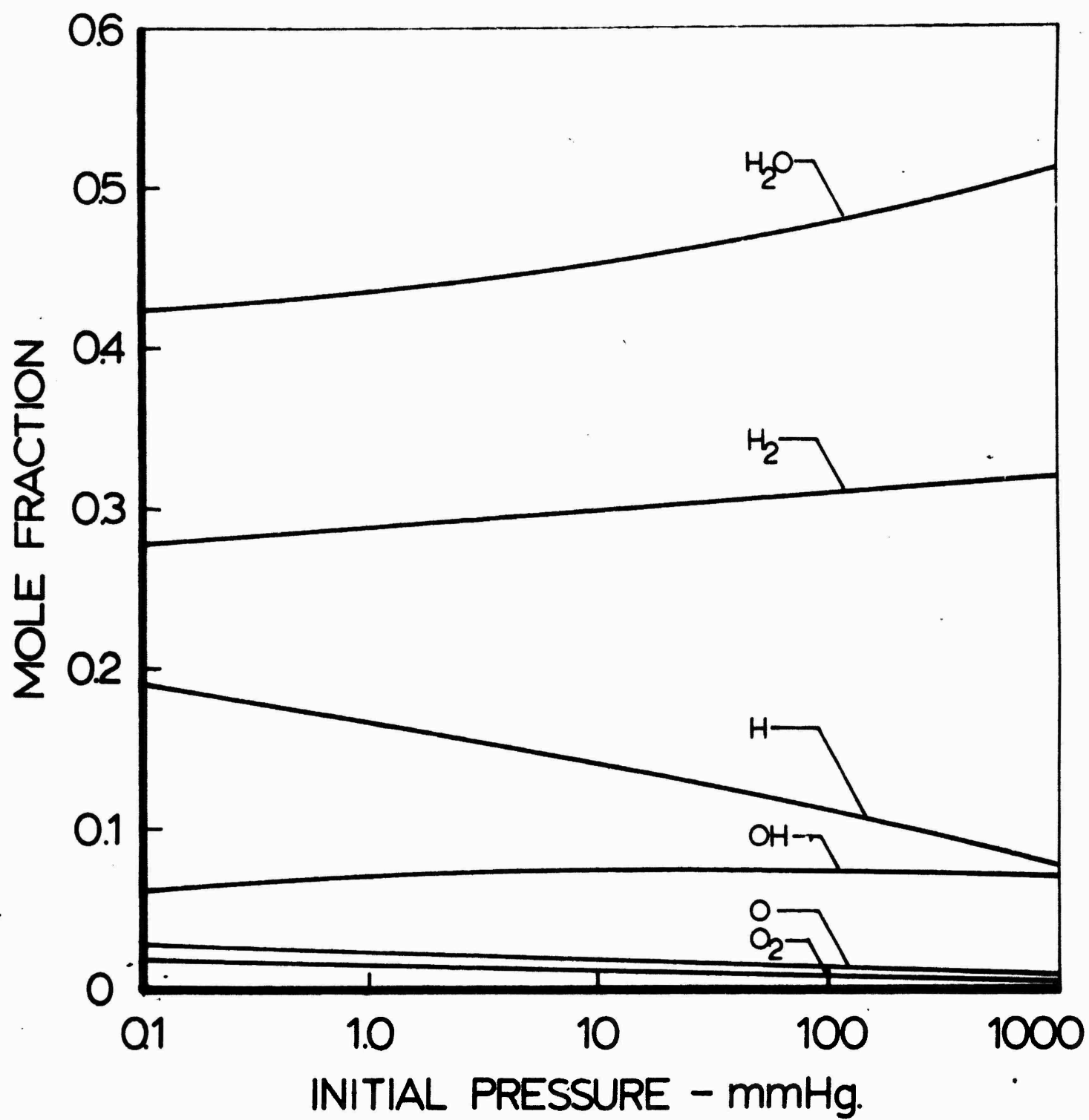


Fig. 21: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $3\text{H}_2 + \text{O}_2$ Mixture at -180°F

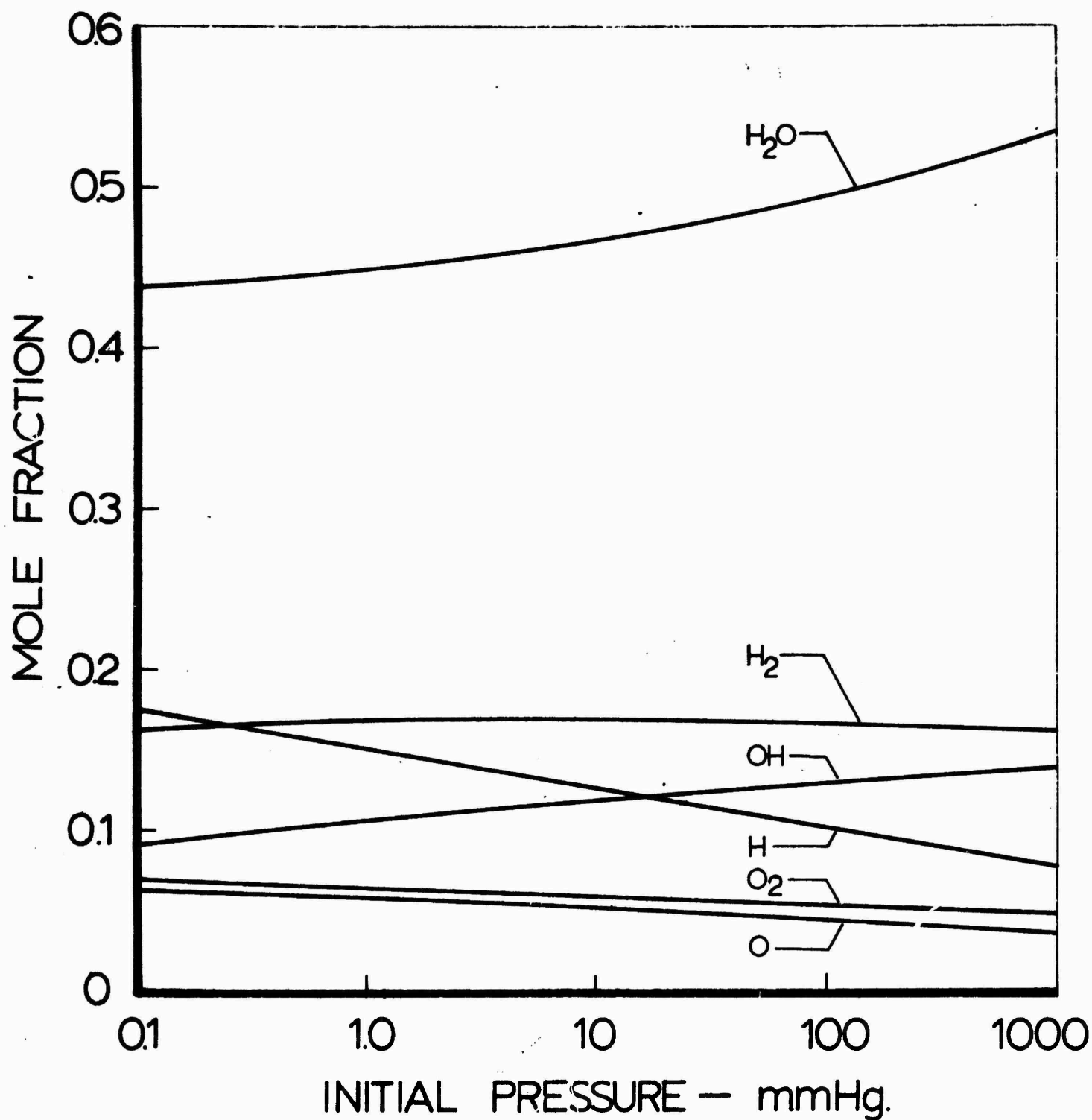


Fig. 22: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $2\text{H}_2 + \text{O}_2$ Mixture Initially at 60°F

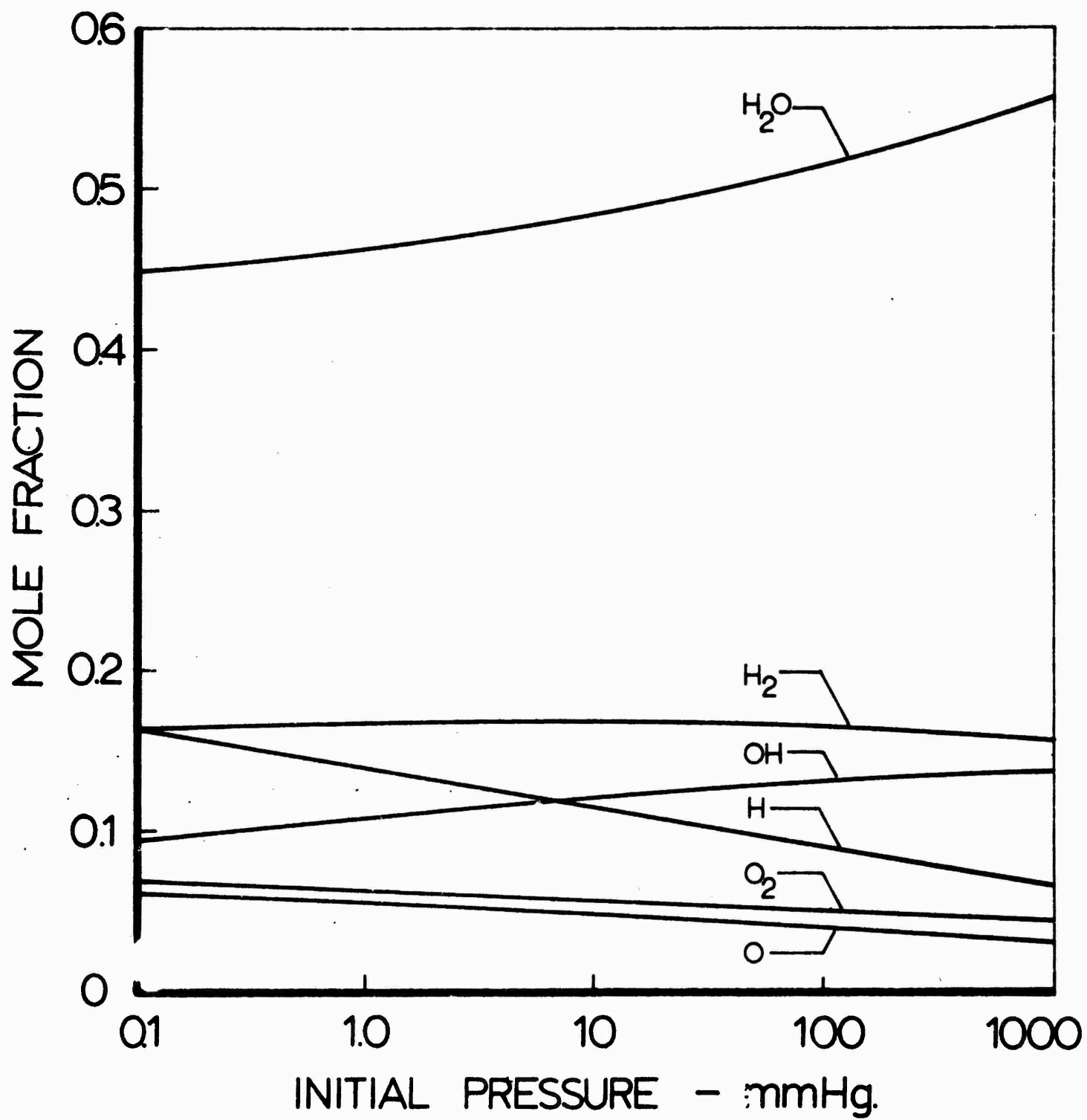


Fig. 23: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $2\text{H}_2 + \text{O}_2$ Mixture Initially at -180°F

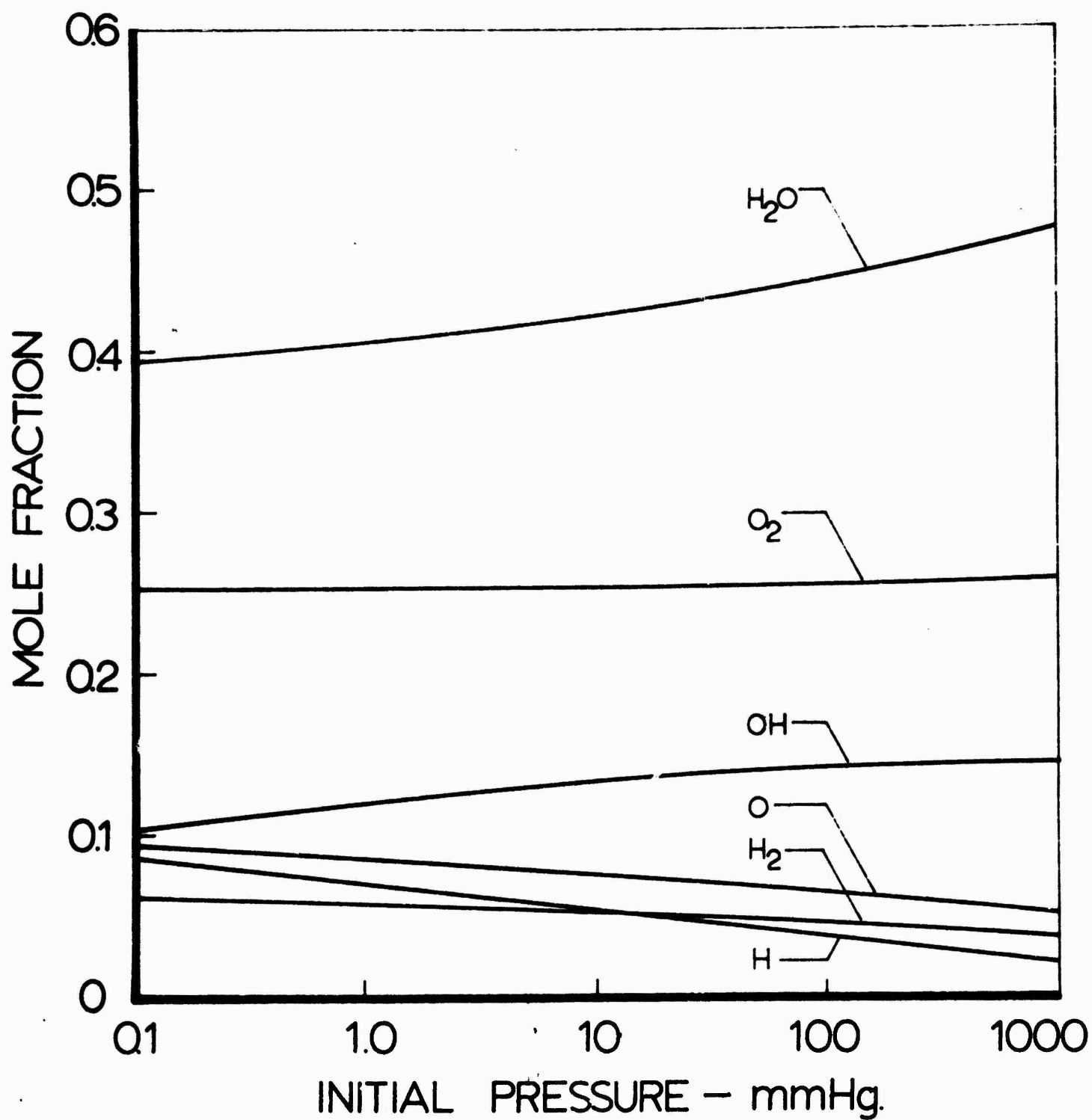


Fig. 24: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $H_2 + O_2$ Mixture Initially at $60^\circ F$

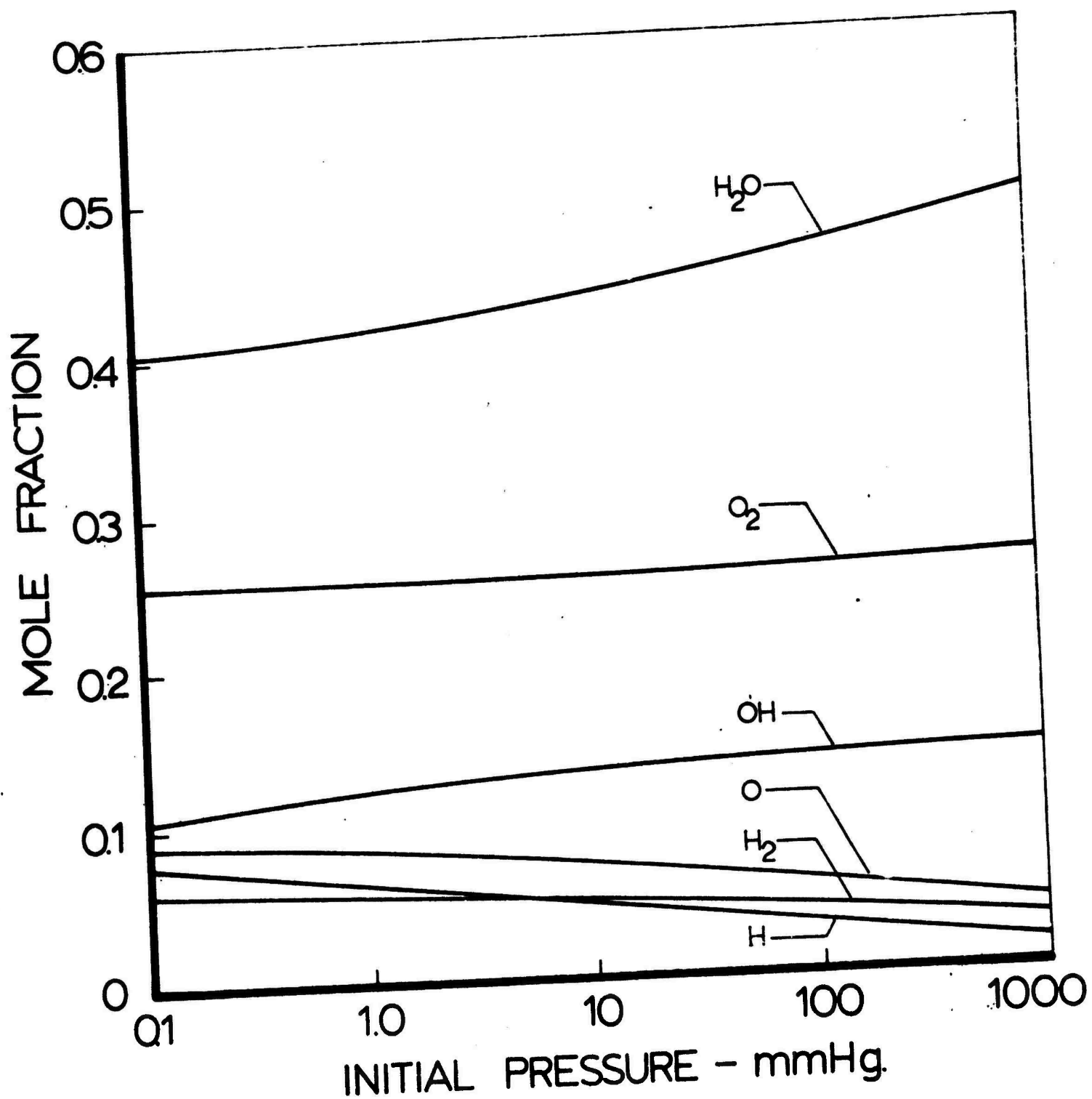


Fig. 25: Influence of Initial Pressure on Equilibrium Composition of Product Gases for $\text{H}_2 + \text{O}_2$ Mixture Initially at -180°F

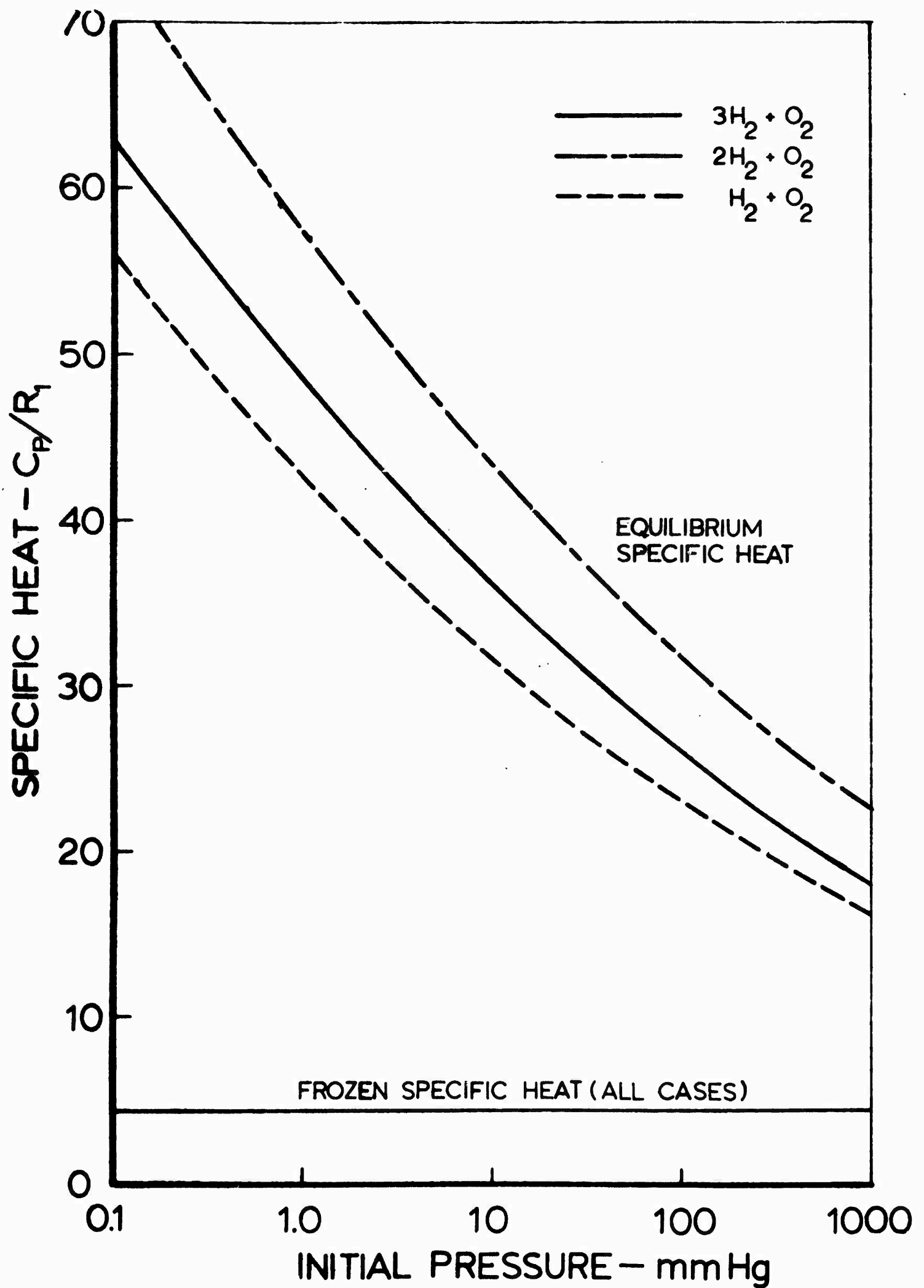


Fig. 26: Influence of Initial Pressure on Specific Heat at the Constant Pressure of Products at CJ State. Initial Temperature 60°F

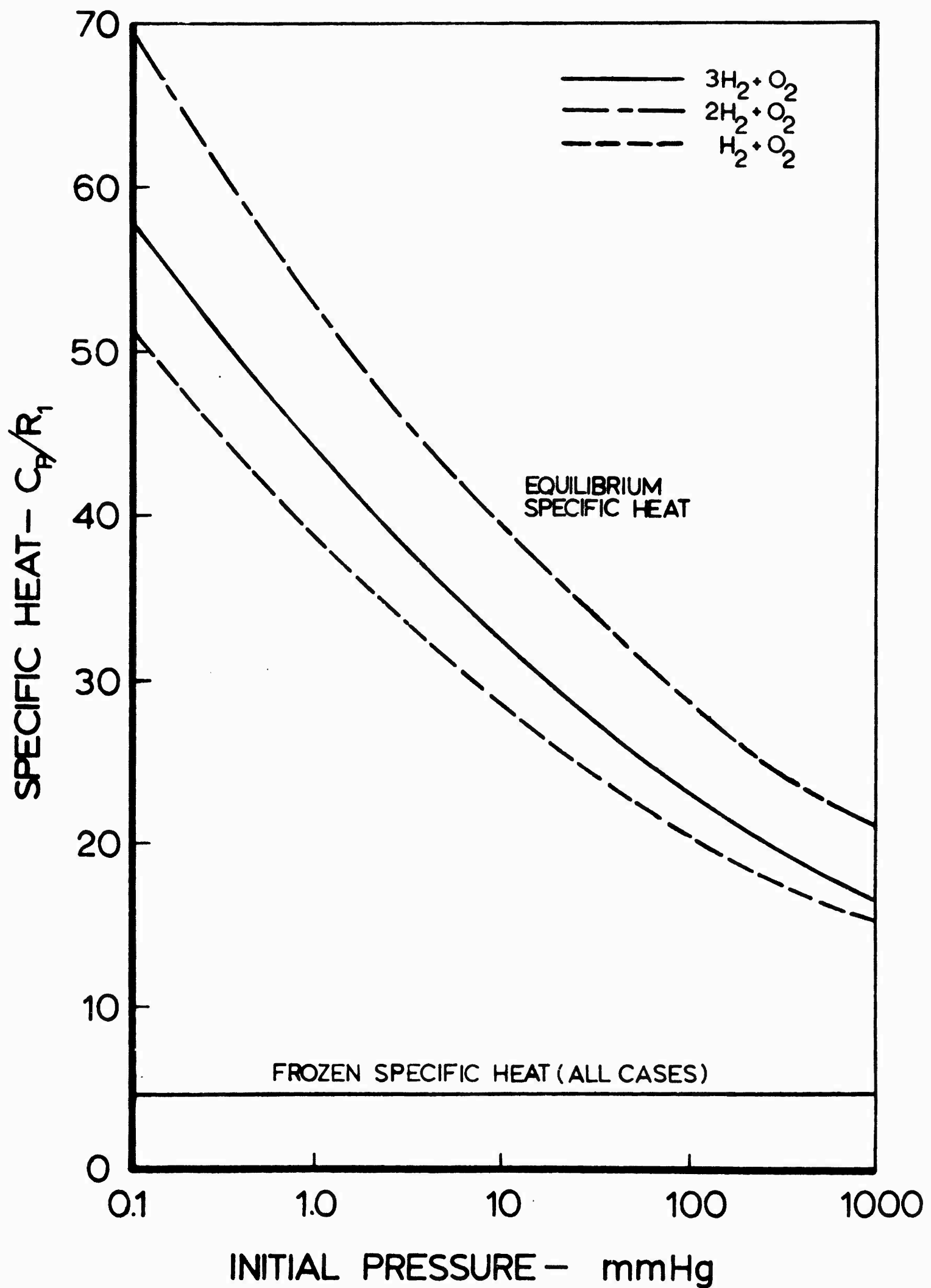


Fig. 27: Influence of Initial Pressure on Specific Heat at the Constant Pressure of Products at CJ State. Initial Temperature -180°F

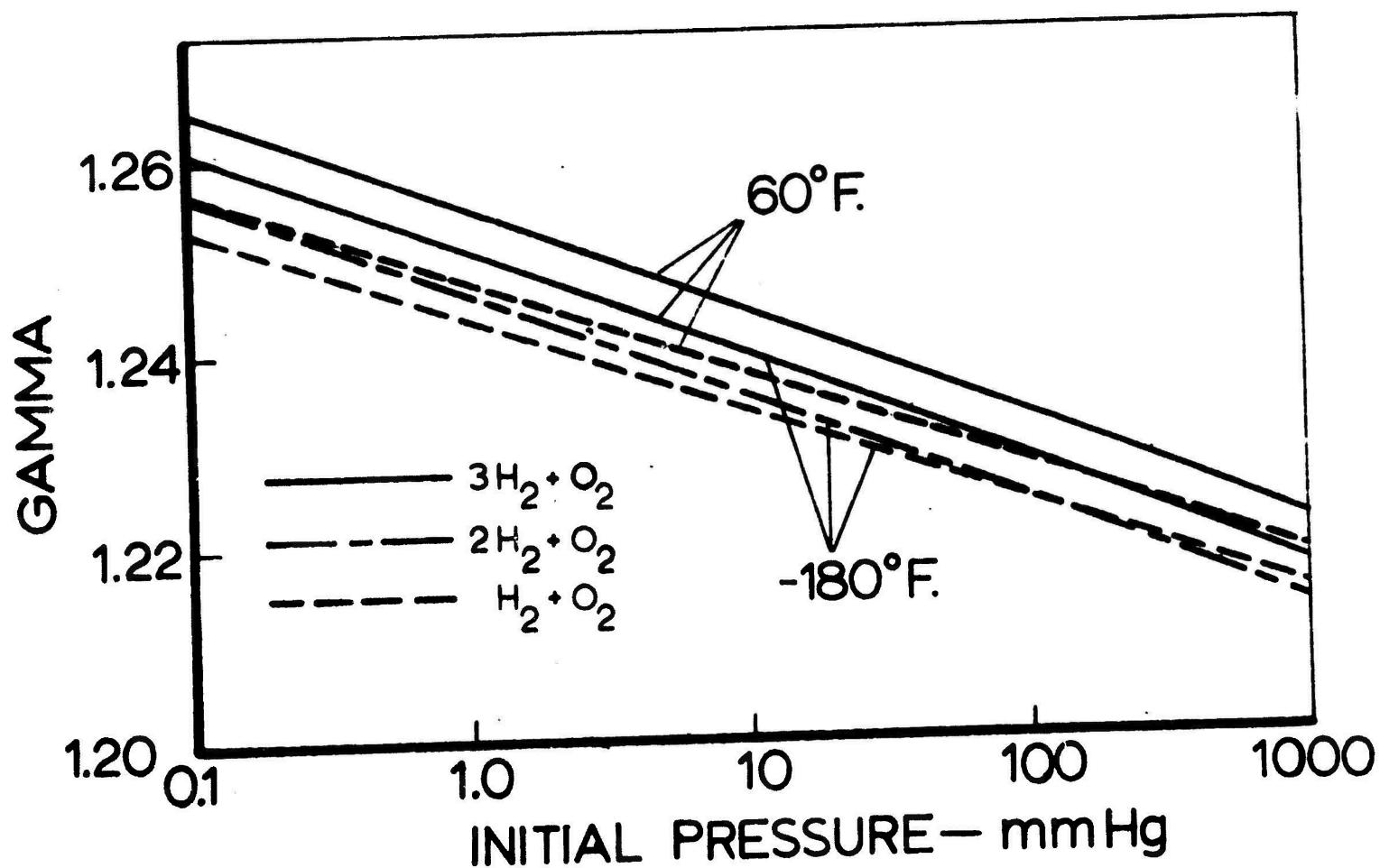
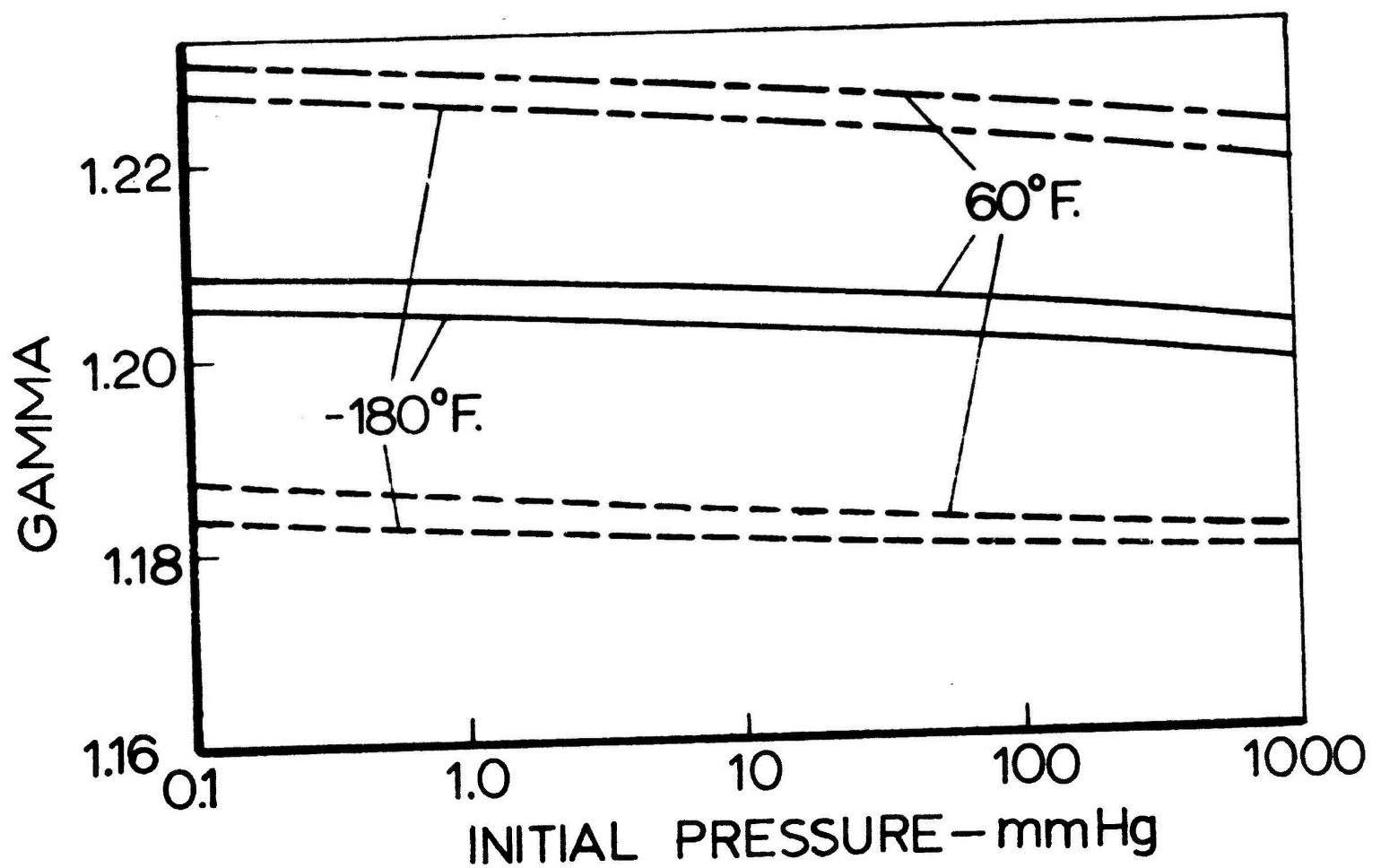


Fig. 28: Influence of Initial Pressure on Specific Heat Ratio of Products at CJ State. The Upper Graph is for Frozen Composition and the Lower Graph is for Equilibrium Composition.

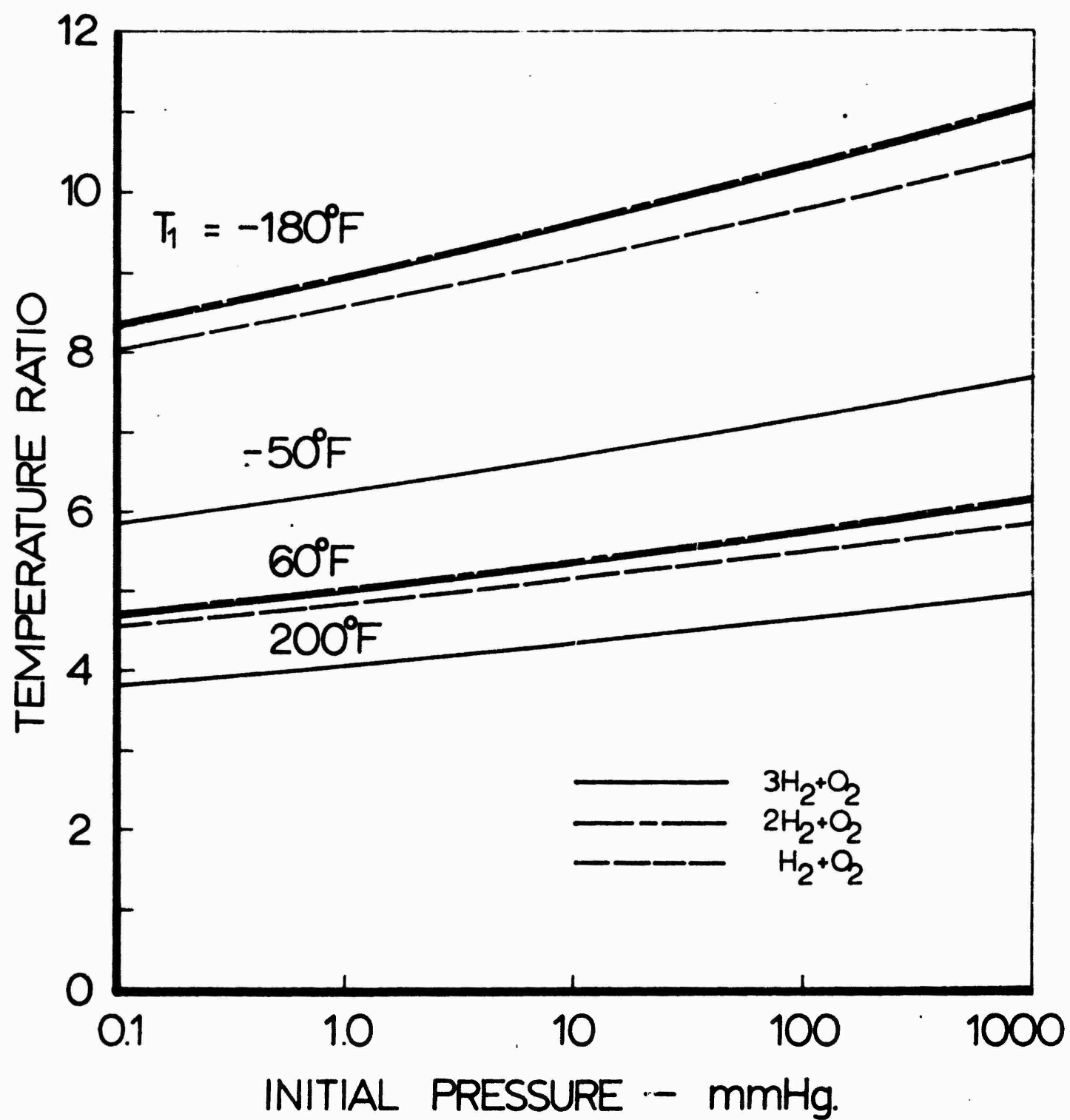


Fig. 29: Influence of Initial Pressure on Von Neumann Spike Pressure Ratio

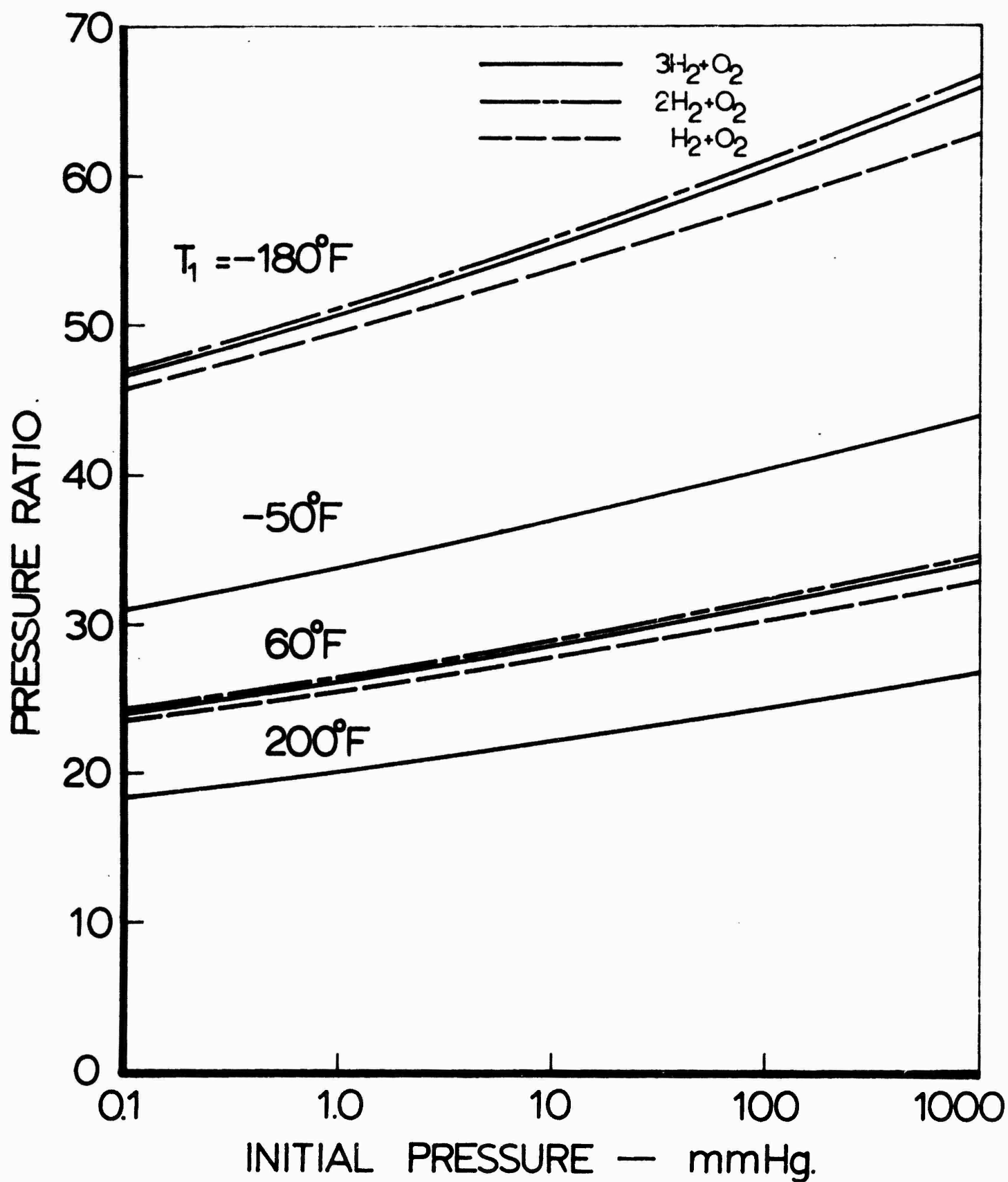


Fig. 30: Influence of Initial Pressure on Von Neumann Spike Temperature Ratio

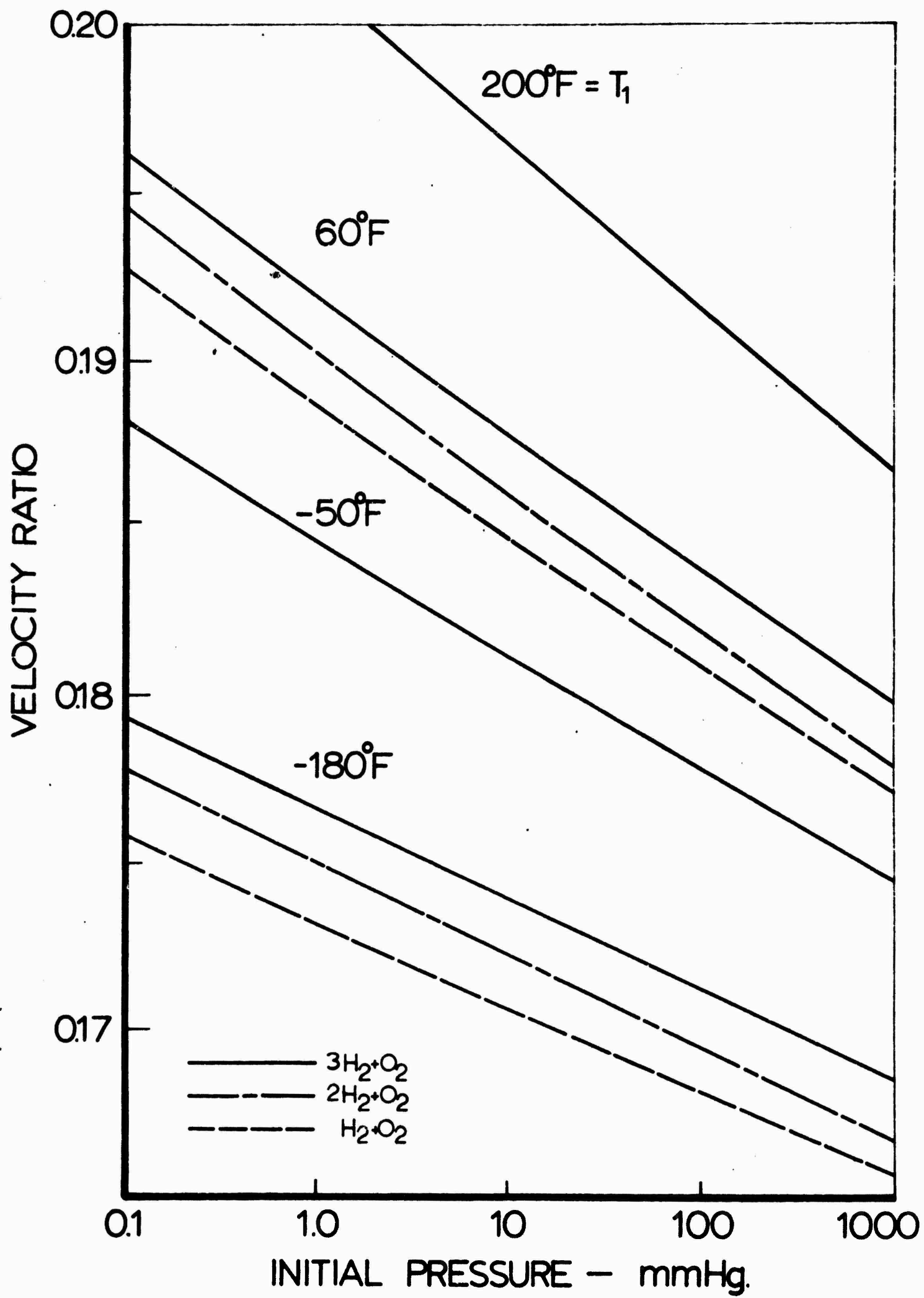


Fig. 31: Influence of Initial Pressure on Von Neumann Spike Velocity Ratio