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REPORT 1522-11

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REPORT

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Investigation of Study Program Related to Shipboard Antenna System Environment

Subject of Report Far-Field Pattern Prediction for Shipboard Antennas

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Date

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31 March 1965

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ABSTRACT

Shipboard antennas operate in the vicinity of the ship's superstructure which consists of numerous metallic scatterers of various sizes and shapes. The far-field patterns of shipboard antennas are perturbed by these scatterers and are therefore difficult to predict. In this report a method is discussed for approximating the far-field pattern in the horizontal plane of a thin vertical antenna (e.g., a whip antenna) near cylindrical scatterers of arbitrary cross-section whose physical heights are at least that of the antenna. The method is based on approximating the antenna with ar. infinite line source and the scatterer with an array of thin infinite wires.

Some representative calculated and experimental results are presented which generally show very good agreement between the predicted and measured patterns. In addition, limitations of the method are discussed and the computer programs for calculating the far-field patterns are explained in some detail.

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FAR-FIELD PATTERN PREDICTION FOR SHIPBOARD ANTENNAS

I. INTRODUCTION

Radiation from shipboard antennas is complicated by the presence of the many varied objects that make up the ship's superstructure. This environment influences the far-field pattern of an antenna as well as its terminal impedance and can affect the mutual coupling between any two antennas. This report will be concerded only with the first problem, namely the effect of the superstructure on the far-field pattern in the horizontal plane of a thin vertical radiator, which is a good approximation for most MF and many HF antennas.

The technique used to predict the perturbed far-field pattern is essentially an extension of Richmond's [1] method for predicting the scattering pattern of an arbitrary array of infinitely long, thin, parallel wires. He has shown that a solid cylindrical conducting object can be approximated, for the purpose of pattern calculation, by replacing the object with thin parallel wires located at its periphery, if there are at least five wires per wavelength and one wire defines each corner. For a given form of the incident wave (e.g., plane waves, or cylindrical waves which will be used in this report) complex currents are induced on each of the wires. These induced currents are then assumed to radiate into free space to form a scattering pattern which can be calculated by the far-field radiation integral.

Essentially the same procedure is followed here, and a line source parallel to the wire array is used to approximate a thin vertical antenna as shown in Fig. 1. A computer program then gives the farfield pattern of the line source plus the field scattered by the wires, that is, the approximate pattern of the antenna in the presence of the scatterer.

The question naturally arises whether or not a technique which employs infinitely long wires and an infinitely long line source with uniform current can predict with acceptable accuracy the far-field of a finite antenna with a non-uniform current in the presence of a conducting cylinder of finite height. The answer is "yes" within certain restrictions. Justification for this positive answer was obtained experimentally; the correspondence between the predicted and measured patterns was generally quite good.



Fig. 1. Mathematical model for the case of a line source radiating in the presence of a cylindrical structure.

II. RESULTS

A. General

The results of this research consist of (1) a group of computer programs to calculate the patterns of the antenna (represented by a line source) and the cylindrical scatterers (represented by wire arrays), and (2) an extensive set of measurements to establish the range of validity of the calculations.

The mathematical formulation of the problem is given in Appendix A. The equations in this appendix are the equations on which the computer programs are based. The computer programs for use with a moderatesize (IBM 1620) computer are given and explained in Appendix B. Three passes through the computer are required; the output of the first pass is obtained on IBM cards and is used as the input to the second pass, and the output of this pass is similarly used as input for the third, which yields the desired results. A sample calculation is given in Appendix C to illustrate the use of these programs. The computer programs for use with a large (IBM 7094) computer are given in Appendix D. During the project it turned out efficient to use the smaller computer for initial investigations but the larger for "production" runs. The "production" program is being optimized further to allow the generation of a handbook of patterns with a reasonable use of computer time.

The experimental program was designed to test the calculations. Two types of approximations are involved in the calculations, and the

experimental program was designed to test these independently. One approximation consists of replacing finite antennas and obstacles with infinite ones to simplify the computations. To test this approximation, the models (described in more detail below) consisted of antennas and obstacles between two parallel plates, of which one could be removed. With the top plate in place, the patterns should be the same as for the infinite structure used in the calculations, except for finite groundplane effects. With the top plate removed, the structure approximates the practical finite case. Comparison of the two patterns shows the effect of the approximation. The second approximation involves replacing the solid scatterer with an array of wires and the numerical approximations of the programs. The errors involved here are estimated by the differences between the measured patterns with both plates in place and the calculated patterns. Finally, the overall accuracy can be evaluated by comparing the computed patterns with the measured patterns with the top plate removed.

B. Experimental Model

The model used for the measurements is shown in Figs. 2 and 3. At 2 Gc the structure is approximately 5 wavelengths in diameter, excluding the one-wavelength long flare. The feed is off center, being 2λ from the nearest portion of the flare. The styrofoam dielectric ring is onehalf wavelength thick and slightly less than one-half wavelength tall. The height of the ring was chosen so that the plate spacing would be less than $\lambda/2$. In order to obtain an omnidirectional pattern with the top plate in place and no obstacle present it was necessary to adjust the top of the exciling probe so that it terminated about $\frac{1}{16}$ "from the top plate. With the top plate on an experimental check was possible of the infinite case itself, whereas with the top plate absent the more practical finite case could be measured and checked against the patterns predicted and measured for the infinite case.

C. Comparison of Measurements and Calculations

Several solid metallic scattering objects were tested with the parallel-plate structure. These included circular cylinders with diameters from $\lambda / 4$ to λ and square cylinders whose sides were either $\lambda / 4$ or $\lambda / 2$. Patterns were measured and calculated for various distances between source and obstacle using these scatterers. In all cases good agreement between the measured and calculated patterns was obtained. Some representative results are discussed in the following paragraphs.

Figure 4 shows a cylinder of square cross-section positioned a distance d from a vertical source and Fig. 5 a,b,c,d show the associated



Fig. 2. Parallel-plate device as it would appear on an outdoor pattern range.





Fig. 4. Square cylinder near a line source.

far-field patterns for various values of d with $\ell = \lambda / 4$. The omnidirectional patterns shown as a reference for the calculated patterns correspond to the antenna without scattering obstacles. It can be seen that in general the measured patterns change little when the top plate is removed and also that the theoretical patterns are in good agreement with the experimental ones, especially for the smaller values of d. The reason for the small lobe in the forward scatter direction with the top-plate absent will be explained shortly. The theoretical pattern was determined by representing the cylinder by 5 wires on a side. Equally good results can be obtained with as few as three wires, that is, a wire at each corner and one in between. The effect of the number of wires on the calculated pattern is shown in Fig. 6. Because of symmetry only that part of the pattern between zero degrees and 180 degrees is shown. Essentially the same pattern is obtained using either 5 or 3 wires per side. If only 4 wires total (i.e., one at each corner) are used, the pattern deteriorates appreciably. On the other hand using 8 wires on a side (i.e., a density of 32 wires per wavelength) causes a slight shift in the pattern opposite to that when there were only 4 wires total. Also, increasing the wire density at the corners has negligible effect. Consequently, nothing is gained by using an excessive wire density and valuable storage space in the computer is wasted, a fact that may be of considerable importance in cases where large and/or numerous scatterers are present. In addition, the number of wires necessary to represent an object may be reduced by carefully eliminating those wires on the forward scatter side of the scatterer as shown in Fig. 7. The corresponding farfield pattern functions for the three cases of Fig. 7 are shown in Fig. 8. The pattern for the case where no wires are omitted is almost identically







Fig. 5b. Far-field patterns of a square cylinder, $l = \lambda / 4$. (b) $d = \lambda / 2$.







Fig. 5d. Far-field patterns of a square cylinder, $l = \lambda / 4$. (d) $d = \lambda$.



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Fig. 5 Effect of the number of wires on the calculated pattern, $d = \lambda$, $l = \lambda/4$.







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equal to pattern A while patterns B and C show differences mostly in the forward scatter direction. The reason some of the wires may be eliminated without seriously affecting the pattern is that the currents of those wires on the forward side are quite small compared to those on the back, and therefore they contribute insignificantly to the far-field pattern. When the square cylinder is rotated 45° about its center, it was found that almost half of the wires could be eliminated without seriously changing the pattern. This situation is illustrated in Fig. 9.

Several sets of patterns were taken for the square cylinder $\lambda/2$ on a side as shown in Fig. 9 except that calculations were made with wires on all four sides. Again agreement between experimental and theoretical patterns was good as shown in Figs. 10 a, b, c, d. It is interesting to note that the patterns in Fig. 10 and Fig. 5 are not too dissimilar for corresponding values of d even though the size and orientation of the scatterer are not the same. This fact is further supported by the case of a circular cylinder near a line source, as illustrated in Fig. 11. Figure 12 shows the predicted patterns for d equal to $\lambda/2$ and λ for cylinders whose diameters are $\lambda/2$ and λ . Thus it is seen that source-to-scatterer distance is the most sensitive parameter and that in general, for small objects, the size and shape of the scatterer are important but to a lesser degree.

The experimental patterns in Figs. 5 and 10 were recorded with the height of the source approximately equal to that of the scatterer; these patterns exhibit a small minor lobe in the forward-scatter direction that is neither predicted by theory nor measured when the top plate is in place.



Fig. 9. Wires omitted on the forward-scatter side of a square cylinder rotated 45°.





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Fig. 11. Circular cylinder near a line source.

The existence of this minor lobe is explained by Fig. 13. The orientation of the scatterer is the same as that in Fig. 9 with $l = \lambda/4$, $d = \lambda/4$ and the variable being the cylinder height h. The source antenna height h_s was just under $\lambda/2$ and the experimental scatterer was a solid cylinder. It is apparent from Fig. 13 that the small lobe in Figs. 5 and 10 is caused by diffraction over the top of the cylinder and that this does not take place if the cylinder height is on the order of twice that of the source. Also, for the case where the source is taller than the scatterer considerable energy is propagated over the top. Consequently, the method of farfield pattern prediction described in this report can not be expected to give very accurate results for situations where the antenna is taller than the scatterer. However, some insight into the shape of the pattern in back-scatter direction may be obtained depending on how much smaller the scatterer is than the source antenna.

III. CONCLUSIONS

It has been shown that the far-field pattern in the horizontal plane of a vertical antenna near cylindrical scattering objects of finite height can be predicted with reasonable accuracy by representing the scatterer by an array of infinitely-long parallel wires and the vertical antenna by an infinitely-long line source. The far-field predictions are valid so long as the scatterer is at least as tall as the antenna itself and at least 5 wires per wavelength are used to represent the object. The additional restriction is made that the number of wires used must sufficiently define the shape of the scatterer. Also, in situations where computer



















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Fig. 13b. Effect of relative heights of source antenna and scatterer. Source antenna height = $\lambda / 2$.

storage is at a premium it is possible to omit those wires on the forwardscatter side where induced currents are relatively small and only slightly affect the far-field pattern.

This technique for far-field pattern prediction should find considerable use for the preliminary evaluation of shipboard situations where a vertical antenna of one or more elements has in its environment cylindrical scatterers with arbitrary cross-sections.

The program presented here indicates the practicality of the preparation of a handbook of patterns for a vertical antenna in the presence of scatterers of various sizes and shapes which would facilitate the optimum location of many shipboard antennas.

ACKNOWLEDGEMENT

The author wishes to express his appreciation to Dr. Jack H. Richmond for his help in devising the computer programs.

APPENDIX A MATHEMATICAL DEVELOPMENT OF THE FORMULAS FOR THE FAR-FIELD PATTERNS

The problem of interest here is that of determining the far-field pattern in the horizontal plane due to a vertical antenna radiating near conducting cylinders of arbitrary cross-section. To obtain a mathematical model we approximate the conducting cylinder of arbitrary cross-section by an array of infinitely-long thin wires along the periphery and represent the vertical antenna by a vertical line source, as shown in Fig. 1.

The line source, whose current is directed in the positive z-direction, produces only a z-component of the electric field which is given by

(1)
$$E_z^{i} = -\frac{\omega\mu}{4} I H_0^{(2)}(k\rho)$$

where

(2)
$$k^2 = \omega^2 \mu \epsilon$$

and $H_0^{(2)}(k\rho)$ represents the zero-order Hankel function of the second kind. The current induced on wire n is uniform and produces a scattered field of the form

(3)
$$E_n^{s} = -\left(\frac{\omega \mu}{4}\right) I_n J_0 (ka_n) H_0^{(2)}(k\rho_n)$$

for
$$\rho_n \geq a_n$$
,

where $J_o(ka_n)$ is the zero order Bessel function, a_n is the radius of wire n, and ρ_n is the distance from wire n. For convenience a "modified current" I_n^{\dagger} is defined by

(4)
$$I_n^{t} = \left(\frac{\omega \mu}{4}\right) I_n J_0(k a_n).$$

Thus the field scattered from N wires at the surface of wire m can be written as

(5)
$$E_{z}^{s} = -\sum_{n=1}^{N} I_{n}^{*} H_{o}^{(2)}(k\rho_{mn})$$

where ρ_{mn} is the distance between wires m and n,

(6)
$$\rho_{mn} = \sqrt{(X_m - X_n)^2 + (Y_m - Y_n)^2}$$

and

(7)
$$\rho_{mm} = a_m$$
.

To obtain values for the complex current on each wire, we impose the condition that

$$(8) \qquad E_z^{i} + E_z^{s} = 0$$

at the surface of each wire. Actually we require that tangential E vanish at the center of each wire, which is an acceptable approximation for wires whose radii are much smaller than the wavelength. Substituting Eq.(1) and Eq.(5) with $\frac{\omega\mu}{4}$ I = -1 into Eq.(8) we obtain

(9)
$$\sum_{n=1}^{N} H_{o}^{(2)}(k\rho_{mn}) I_{n}^{*} = H_{o}^{(2)}(k\rho_{m})$$

The above equation then yields a set of N equations in the N unknowns I_n . Having determined the complex currents on each wire, the far-field pattern can then be determined from

(10)
$$E_{z}(\phi) = + \sum_{n=1}^{N} H_{o}^{(2)}(k\rho_{n}) I_{n}^{t} - H_{o}^{(2)}(k\rho)$$

When the observation point is at a great distance from the wires, it is said to be in the far-zone field. This permits some simplification of Eq.(10). For large arguments the Hankel function can be approximated by the asymptotic formula

(11)
$$H_0^{(2)}(X) = \sqrt{2j/\pi X} e^{-jX}, X >> 1.$$

The distance from wire n at (X_n, Y_n) to the observation point at (ρ, ϕ) can be expressed as

(12)
$$\rho_n \cong \rho - X_n \cos \phi - Y_n \sin \phi$$

Consequently the far-field is given by

(13)
$$E_{z}(\phi) = + \sqrt{\frac{2j}{\pi k \rho}} e^{-jk\rho} \left[-1 + \sum_{n=1}^{N} I_{n} e^{jk(X_{n}\cos\phi + Y_{n}\sin\phi)} \right]$$

A far-field pattern function is defined by the bracketed expression in Eq.(13), which can be written as

(14)
$$F(\phi) = \sum_{n=0}^{N} I_n' e^{jk(X_n \cos \phi + Y_n \sin \phi)}$$

where $I_0' = -1$ at the origin.

Appendix B gives three computer programs for implementing these calculations on a moderate-size (IBM-1620) computer. The first calculates the coefficients and excitation functions for the system of Eq.(9). The second solves the system for the modified currents I_n ¹. The last calculates the far field from these currents, according to Eq.(14). If only the scattered portion of the field is desired, the value of the current on the line source is set equal to zero in the input to this last program.

Appendix C gives a sample problem that illustrates the use of the three FORTRAN programs on the IBM 1620.

Appendix D gives a single, more efficient SCATRAN program for use on the IBM 7094 computer, which may be used in place of the three FORTRAN programs.

APPENDIX B

Figure 14 is a computer program in FORTRAN (Ohio State University Version 2) based on Eq.(9) for setting up the linear equations for the currents on the infinitely-long parallel wires. The line source is assumed to have a negative modified unit current. Included in the program is a subroutine for calculating the Bessel and Neumann functions. If the argument, $k\rho_{mn}$, is less than 4 the ascending power series is used and if it is greater than 4 the asymptotic series is used. The numbers in the "equals column" represent the incident electric field intensity at wire m due to the line source. Figure 15 gives a flow diagram for the program in Fig. 14. The output of the program in Fig. 14 is used as part of the input data for the program in Fig. 16. This program uses the method of Crout[2,3] to obtain the solution for an inhomogeneous system of linear equations with complex coefficients. The output of this program consists of the real and imaginary parts of the current on each wire.

Figure 17 gives a flow diagram for the program in Fig. 16. However, this program does not compute the elements in Crout's "auxiliary matrix" in the order called for by him in his article[2]. The order used here results in a more compact and efficient program.

The output of the program in Fig. 16, the various wire locations as used for input to the program of Fig. 14, and the magnitude of the line source current are used as the input for the program in Fig. 18. This latter program calculates the far-field pattern function of the parallel wire array excited by a line source whose "modified current" equals -1 + j0. If only the scattered field is desired, the input card for the magnitude of the line source current is omitted from the input deck. This program is based on Eq.(14). The output data gives the value of the pattern function at whatever values of ϕ are desired. Note that E(ϕ) in this program corresponds to the F(ϕ) defined by Eq.(14).

Figure 19 gives a flow diagram for the program in Fig. 18.

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с
     G THIELE. LINEAR EQUATIONS FOR SCATTERING PATTERN OF AN
     ARBITRARY ARRAY OF THIN WIRES, LINE SOURCE AT THE ORIGIN
С
     DIMENSION U(56), V(56), F(29), G(24)
    FORMAT (F1J+6+F10+6+F10+6+F1J+6+F10+6+F1J+6+F1J+6+F10+6)
  2
  3 FORMAT (110+F10+6+F10+6+F10+6+F10+6+F10+6+F10+6+F10+6)
     READ 3.N.BKJ.BKY.AAA.THETA
  READ2+U(1)+U(2)+U(3)+U(4)+U(5)+U(6)+U(7)+U(8)
  READ2 \cdot U(9) \cdot U(1 \cup ) \cdot U(11) \cdot U(12) \cdot U(13) \cdot U(14) \cdot U(15) \cdot U(16)
     READ2+U(17)+U(18)+U(19)+U(20)+U(21)+U(22)+U(23)
  READ2+V(1)+V(2)+V(3)+V(4)+V(5)+V(6)+V(7)+V(8)
  READ2.V(9).V(10).V(11).V(12).V(13).V(14).V(15).V(16)
     READ2+V(17)+V(18)+V(19)+V(20)+V(21)+V(22)+V(23)
      M = N
     NN = M+1
     THETA = .01745329*THETA
                                       Symbols for Input Data
     STHET = SIN(THETA)
     IF (AAA)8.5.8
                                  N
                                        Number of wires
  5 STHET = 6.2831853*STHET
                                        J_{0} (ka \sin \theta_{0})
N_{0} (ka \sin \theta_{0})
                                  EKJ
  8 DO 10 L = 1 • M
                                  BKY
     U(I) = STHET*U(I)
                                        0. if wire coordinates are x/\lambda and y/\lambda
                                  AAA
  10 V(I) = STHET*V(I)
                                        1. if wire coordinates are kx and ky
     STHET = SIN(THETA)
                                  THETA 90.
  11 \text{ D0 } 15 \text{ I} = 1.24
                                  U(N) x coordinate of wire N
     F(I) = 0.
                                  V(N) y coordinate of wire N
  15 G(1) = 0.
     DO 50 I = 1.M
     DO 17 K = 1 \cdot M
     F(K) = 0
  17 G(K) = 0.
     DO 30 J = 1.N
     L = J
     IF (M-J)24.25.25
  24 L = J-M
  25 IF (I=J)14+12+14
  12 F(J) = BKJ
     G(J) = -BKY
     GO TO 30
  14 R=SQRT((U(1)-U(J))*(U(1)-U(J))+(V(1)-V(J))*(V(1)-V(J)))
     IJK = 1
     GO TO 34
  20 F(L) = F(L) + B
     G(L) = G(L) - Y
  30 CONTINUE
     R = SQRT(U(1)*U(1)+V(1)*V(1))
     IJK = 2
     GO TO 34
```

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45 F(NN) = B
  G(NN) = −Y
  PUNCH2+F(1)+F(2)+F(3)+F(4)+F(5)+F(6)+F(7)+F(8)
  PUNCH2+F(9)+F(10)+F(11)+F(12)+F(13)+F(14)+F(15)+F(16)
  PUNCH2+F(17)+F(18)+F(19)+F(20)+F(21)+F(22)+F(23)+F(24)
  PUNCH2+G(1)+G(2)+G(3)+G(4)+G(5)+G(6)+G(7)+G(8)
  PUNCH2+G(9)+G(10)+G(11)+G(12)+G(13)+G(14)+G(15)+G(16)
5U PUNCH2+G(17)+G(18)+G(19)+G(20)+G(21)+G(22)+G(23)+G(24)
   STOP
34 IF (R-4.)35.35.40
35 W = R/2.
   W1 = W * W
   w2=w1*w1
   W3=W2*W1
   W4=W2*W2
    w5=w4*w1
   W6=W3*W3
    w7=w3*w4
    d=1.-W1+.25*W2-.J2777d*W3+.0017361*W4
    B=B-.6944E-4*W5+.1929E-5*W6-.394E-7*W7
    S=W1-.375*W2+.0509259*W3-.0036169*W4
   S=S++15856E-3*+5-+4726E-5*W6++1021E-6*W7
    Y=•63661977*(S+H*(•57721566+LOG(W)))
   GO TO 44
40 \ Z = 1.7R
   X=Z*Z
    Q=(•125-•J7324*X)*Z*•5641896
    B=((P-Q)*CUS(R)+(P+Q)*SIN(R))/SQRT(R)
    Y=((P+0 _ JIN(R)-(P+Q)*COS(R))/SQRT(R)
44 GO TO (20,45) . IJK
   END
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Fig. 14. Digital computer program for setting up the linear equations for the N unknown currents.

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С J RICHMOND, SOLUTION OF 15 (OR LESS) COMPLEX LINEAR EQUATIONS DIMENSION A(15+16)+B(15+16) FORMAT (F10+6+F10+6+F10+6+F10+6+F10+6+F10+6+F10+6+F10+6) 2 FORMAT (15+F15+6+F15+6) 24 READ I.N 00 5 I=1.N READ2+A(1+1)+A(1+2)+A(1+3)+A(1+4)+A(1+5)+A(1+6)+A(1+7)+A(1+8) $READ2 \bullet A(1 \bullet 9) \bullet A(1 \bullet 1 \cup) \bullet A(1 \bullet 11) \bullet A(1 \bullet 12) \bullet A(1 \bullet 13) \bullet A(1 \bullet 14) \bullet A(1 \bullet 15) \bullet A(1 \bullet 16)$ READ2+B(I+1)+B(I+2)+B(I+3)+B(I+4)+B(I+5)+B(I+6)+B(I+7)+B(I+8) 5 READ2+B(1+9)+B(1+10)+B(1+11)+B(1+12)+B(1+13)+B(1+14)+B(1+15)+B(1+16) NIN = N + 1DO 18 L = 1+N LLL = L-1DO 18 I = $L \cdot N$ 11 = 1+11F(LLL)5.4.3 DO 17 K = 1.LLL3 $A(I \bullet L) = A(I \bullet L) - A(I \bullet K) * A(K \bullet L) + d(I \bullet K) * B(K \bullet L)$ $B(I_{+}L) = B(I_{+}L) - A(I_{+}K) + B(K_{+}L) - A(K_{+}L) + B(I_{+}K)$ $A(L \bullet II) = A(L \bullet II) - A(L \bullet K) * A(K \bullet II) + B(L \bullet K) * B(K \bullet II)$ B(L+II) = B(L+II) - A(L+K)*B(K+II) - B(L+K)*A(K+II)17 $R = A(L \bullet L) * A(L \bullet L) + B(L \bullet L) * B(L \bullet L)$ 4 $S = A(L \cdot II)$ $T = B(L \cdot H)$ $A(L \bullet II) = (A(L \bullet L) * S + B(L \bullet L) * T) / R$ $B(L \bullet II) = (A(L \bullet L) * T - B(L \bullet L) * S) / R$ 18 PUNCH 24 +N+A(N+NN)+B(N+NN) $DO 23 L = 2 \cdot N$ I = NN-LII = I+1 $DO 22 K = II \cdot N$ $A(I \circ NN) = A(I \circ NN) - A(I \circ K) * A(K \circ NN) + B(I \circ K) * B(K \circ NN)$ 22 $B(I \bullet NN) = B(I \bullet NN) - A(I \bullet K) * B(K \bullet NN) - B(I \bullet K) * A(K \bullet NN)$ 23 PUNCH 24 + I + A (I + NN) + B (I + NN) STOP END Symbols for Input Data Symbols for Output Data N Number of Linear equations I Index of current I A(I,J) Real part of coefficient of I'_{i} A(I,NN) Real part of current I; in equation i B(I,J) Imaginary part of coefficient B(I,NN) Imaginary part of

of I' in equation i



current I



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C J RICHMOND + PATTERN OF ARRAY OF LINE SOURCES
     DIMENSION CR(3U) \cdot CI(3U) \cdot X(3U) \cdot Y(30)
  2 FORMAT (15+F15+8+F15+8+F15+8+F15+8+F15+8)
  3 FORMAT (F10+6+F10+6+F10+6+F10+6+F10+6+F10+6+F10+6+F10+6)
     READ 2+N+P+DP+FM+AAA+THETA
     READ 3 \times (1) \times (2) \times (3) \times (4) \times (5) \times (6) \times (7) \times (8)
     READ 3+X(9)+X(1)+X(11)+X(12)+X(13)+X(14)+X(15)+X(16)
     READ3+X(17)+X(18)+X(19)+X(20)+X(21)+X(22)+X(23)+X(24)
     READ 3+Y(1)+Y(2)+Y(3)+Y(4)+Y(5)+Y(6)+Y(7)+Y(8)
     READ 3+Y(9)+Y(10)+Y(11)+Y(12)+Y(13)+Y(14)+Y(15)+Y(16)
     READ3+Y(17)+Y(18)+Y(19)+Y(20)+Y(21)+Y(22)+Y(23)+Y(24)
      THETA = .01745329*THETA
                                               Symbols for Input Data
      STHET = SIN(THETA)
                                                   Number of wires
      IF (AAA)8,5,8
                                            N
P
                                                   Initial value of \phi in degrees
  5 STHET = 6.2831853*STHET
                                                   Increment in \emptyset in degrees
                                            DF
  8 DO 10 I = 1 .N
                                            FM
                                                   Number of values of \emptyset
      X(I) = STHET X(I)
                                            AAA
                                                   O. if coordinates are x/\lambda and y/\lambda.
  10 Y(I) = STHET*Y(I)
                                                   1. if coordinates are kx and ky
  12 \text{ DO } 20 \text{ I} = 1.00
                                            THETA
                                                   Angle of incidence \Theta_{0} with
     READ 2+J+U+V
                                                   respect to z axis
     CR(J) = U
                                            X(N)
                                                   x/\lambda or kx (coordinate of wire n)
     CI(J) = V
                                                   y/2, or ky (coordinate of wire n)
                                            Y(N)
     CS = U*U + V*V
      CM = SQRT(CS)
                                                   Index number of wire j
                                            J
                                            U
                                                   Real rart of current on wire j
  20 PUNCH 2.J.U.V.CS.CM
                                            V
                                                   Imaginary current on wire j
     M = FM
     DO 40 I = 1.M
                                                Symbols for Outrut Data
     PR = .U1745329*P
     C = COS(PR)
                                            P
                                                   Angle Ø in degrees
     S = SIN(PR)
                                                   Real part of E(\emptyset)
                                            ER
     ER = 0.
                                                   Imaginary pert of E(\emptyset)
                                            ΞI
     EI = 0.
                                                   Magnitude squared of \mathbf{E}(\emptyset)
                                            ES
     DO 3U J = 1.0
                                            E
                                                   Magnitude of \mathbf{E}(\emptyset)
     Z = X(J) * C + Y(J) * S
     CZ = COS(Z)
      SZ = SIN(Z)
     ER = ER + CR(J)*CZ - CI(J)*SZ
  30 EI = EI + CI(J)*CZ + CR(J)*SZ
     ES = ER + ER + EI + EI
     E = SORT(ES)
     PUNCH 2+1+P+ER+EI+ES+E
  40 P = P + DP
     STOP
     END
```

Fig. 18. Digital computer program for the far-field pattern of an arbitrary array of parallel wires.



Fig. 19. Flow graph for the program in Fig. 18.

APPENDIX C

The purpose of this appendix is to minimize the time required to gain proficiency in the utilization of the programs in Appendix B. As a sample calculation, the situation in Fig. 4 was used with $d = \lambda / 2$ and $l = \lambda / 4$. Three wires were used on a side as opposed to the five that were used to obtain the theoretical pattern in Fig. 5b.

The input cards to the program of Fig. 14 are shown in Fig. 20 and are self-explanatory except possibly for the four "zero" cards which are necessary because the program can accommodate up to 24 wires and only 8 are used in this instance. The output from this program consists of the real and imaginary parts of the coefficients of I_n' . Again, since the program provides for up to 24 wires but only 8 are used in this example, some of the output cards contain only zeros. These "zero cards" are removed before using the output as the input for the program of Fig. 16. The output of that computation is just the real and imaginary parts of the currents on each of the 8 wires. These cards are then used as part of the input to the program of Fig.18. Note that the same coordinate information used for Fig. 14 is also used for Fig. 18. Also note that the "current" -1 + i0 of the line source must be included in the input unless just the scattered field is desired. The output of the Fig. 18 program contains the desired far-field pattern information in the right-most column. These numbers may be used to generate the normalized pattern in Fig. 5b which was calculated using 5 wires per side and therefore has slightly deeper nulls. If in this example the only wire were the line source itself, the output of the last program (Fig. 18) would indicate that $F(\phi) = 1$. Hence the unit circle may be used as a reference.

*								
	C INPUT	CARDS FOR	PROGRAM IN	F16 14				
	8	.99937	-1-97931	0.0	900			
	0.500	0.530	J-625	0.75D	J. 750	1.75)	0.025	0.500
. .	0.0	00000	01025	00150	00750	01150	0.025	0.300
	0.0							
	0.000	0.125	0.125	0.125	1.000	-0.125	-0-125	-0.125
	0.000			00120		-00125	-00125	-00125
	0.0							
* • •	0.0							
	с <u>о</u> цтри			IN ELG 14				
•	+-999370	+-851631	+-714556	+.365432	+-472001	+.365432	+.714556	+-851631
		+.000000	+-0-000	++0000402	+++++++++++++++++++++++++++++++++++++++	+++0000000	++000.000	++000000
	+•000000	++0000000	+•0440046	+.000000	+-000000	+-000000	+.000000	+-000000
	+1.079310	+.101207	- 169601	467055	- 41 2003	+ 6000000	- 169601	+ 101207
•		+.0000000	+.000000	+.000000	+•000000	++000000	+•000000	++000000
	+.000000	+.0000000	+.000000	++000000	+.0000000	+ - 0000000	+.0000000	+.0000000
	+-851631	+.999370	+ 851631	++472001	+.365432	+ • 0 98474	+.365432	+ 472001
	- 329898	+.000000	+.000000	+.000000	+.000000	+ • 0 0 0 0 0 0	+.000000	+.000000
	+.000000	+.0000000	+.000000	+.000000	+.0000000	+.0000000	+.0000000	+.0000000
	+.101207	+1.979310	+.101207	- 410003	- 467056	- 520633	407056	- 410003
	- 292726	+.000000	+.000000	+.000000	+.000000	+.000000	+.00000	+.000000
	+.000000	+.000000	+.0.0000	+.000000	+.000000	+.000000	+.000000	+ - 000000
•	+ 714556	+.851631	+.999370	+.851631	+.714556	+.365432	+.472001	+.365432
	396862	+.0000000	+.000000	+.000000	+.000000	+.000000	+.000.00	+.000000
	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.0000000	+.000000
	169601	+.101207	+1.979310	+.101207	-+169601	- 467056	410003	- 467056
	+.018899	+.0000000	+.300003	+.000000	+.000000	+.000000	+.000000	+.000000
	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+.365432	+.472001	+.851631	++999370	+•851631	+ • 472001	+.365432	+.098474
	247116	+.0000000	+.000000	+.00000	+.000000	+.000000	+.000000	+.000000
	.+.000000	+.0000000	+.000000	+.030000	+.000000	+.000000	+.0000000	+.000000
	467056	410003	+.101207	+1.979310	+.131207	-•410003	467056	-•520633
	+.267421	+.JOUOUO	+.0.0000	+. 120000	+.000000	+.000000	+.0000000	+.000000
	+.000000	+•000000	+•000000	+•000000	+.000000	+.0000000	+.0000000	+•000000
	+•472JU1	+.365432	+.714505	+.851631	+.999370	+.851631	+.714556	+.365432
•	265847	+.000000	+•0000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+•000000	+•0000000	+.0000000	+.000000	+•000000	C000000+	+.000000	+.000000
	-•410003	467056	1696J1	+.101267	+1.979310	+•101207	-•169601	467056
	+.252423	+•0000000	+•0.0000	+•0000000	+• 000000	+.000000	+.000000	+.000000
	+.000000	+•000000	+•000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+.365432	+•098474	+•365432	+•472001	+.851631	֥999370	+.851631	+•472001
	247116	+.0000000	+•000000	+.000000	+.000000	+.000000	+•000000	+.000000
	+.000000	+•000000	+•000000	+.000000	+•000000	+•000000	+.000000	+.000000
	467056	-•52-633	467056	-•410003	+.1J12J7	+1.979310	+.101207	-•410003
	+•267421	+•000000	+•000000	+•000000	+•000000	+•000000	+.0000000	+•000000
	+•000000	+•100010	+•0,0000	+.000000	+•000000	+•000000	+.000000	+•000000
	+•714556	+•365432	+•472001	+•360432	+•714556	+•851631	+•999570	+•321631
	-•396862	+.000000	+.0000000	+•UJUQQQ	+.000000	+•00000	+.000000	+.000000
	+.000000	+.0000000	+•0000000	+•0000000	+•000000	+•000000	+•000000	+•000000
	169601	-•467056	410003	467056	169601	+.101237	+1.979310	+.101207
	+•018899	+.000000	+.000000	+.000000	+.300000	+.00000	+.0000000	+.000000
•	+.000000	+.000000	+•000000	+.000000	+.000000	+.000000	+.000000	+.0000000
	++851631	+.472001	+.305432	++098474	+•305432	+•472001	+.851631	+•999370
	329898	+.000000	+•0000000	+.000000	+•000000	+.000000	+.000300	+.000000
	+.000000	+.000000	+.000000	+.000000	+. 000000	+.000000	+.000000	+.000000
	+.101207	41.0003	467056		467055	- 410003	+.101207	+1.979310
	292726	+•000000	+	+*000000	+.000000	+.000000	+.000000	+•0000000
	+•000000	+•0000000	+•00000	+.00000	+•00000	+•000000	+•000000	+•000000

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Fig. 20. Inputs and outputs of the programs in appendices A, B, and C.

С	INPUT	CARDS FOR	PROGRAM H	N FIG 16				
	8							
	+.999370	+.851631	+•714556	+.365432	+.472001	+• 365432	+++714556	+.851631
	304243	+•000000	+•000000	+.000000	+.000000	+.000000	+.000000	+.003000
4	1.979310	+.101207	-•169601	467056	410003	467056	-•169601	+.101207
	++328366	+.000000	+•000000	+.000000	+.000000	+.000000	++000000	+.000000
	+.851631	+•999370	++851631	+.472001	+•365432	+.098474	+.365432	++472001
	329898	+.000000	+.000000	+.000000	+•000000	+.000000	+.0000000	+.000000
	+.101207	+1.979310	+.101207	410003	467056	520633	467056	410003
	292726	+.000000	+•000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+.714556	+.851631	+•999370	++851631	+.714556	+.365432	+•472001	+.365432
	396862	+.000000	+.000000	+.00000	+.000000	+.000000	+.000000	+.000000
	169601	+.101207	+1.979310	+.10.207	-•169601	-•467056	410003	~•467056
	+.018899	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+.365432	+.472001	+.851631	+.999370	+•851631	+•472001	+•365432	+.098474
	247116	+.000000	+•000000	+.000000	+.000000	+.000000	+•000000	+.000000
	-•467056	410003	+.101207	+1+979310	+.101207	410003	-•467056	520633
	+.267421	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+.472001	+,365432	+•714556	++851631	++999370	+.851631	+•714556	+.365432
	-•265847	+•000000	+•000000	+•000000	+.000000	+.000000	+.000000	+.000000
	~.410003	467056	169601	+•101207	+1.979310	+.101207	~•169601	467056
	+.252423	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+•365432	+.098474	+.365432	+•472001	+.851631	++999370	++851631	++472001
	247116	+.000000	+.000000	+•000000	+.000000	+.000000	+.000000	+.000000
	467056	520633	467056	410003	+.101207	+1.979310	+•101207	-•410003
	+.267421	+.000000	+•0000000	++000000	+.000000	++000000	+.000000	+.000000
	+•714556	+.365432	+.472001	+•365432	+•714556	+.851631	+•999370	+.851631
	396862	+•000000	+.000000	+•000000	+.000000	+.000000	+.000000	+.000000
	169601	467056	410003	467056	-•169601	++101207	+1+979310	++101207
	+.018899	+.000000	+•000000	+.000000	++000000	+.000000	+.000000	+.000000
	+.851631	+.472001	+•365432	+.098474	+.365432	+•472001	+.851631	+•999370
	329898	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000
	+.101207	410003	467056	-•520633	467056	410003	++101207	+1+979310
	-+292726	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000	+.000000

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с	OUTPUT	CARDS FROM	PROGRAM IN FIG 16
	+8	-•161631	-+018926
	+7	038466	+.028586
	+6	++005762	++019949
	+5	000098	++000905
	+4	+.005762	++019949
	+3	038466	++028586
	+2	161631	018926
	+1'	133808	062170

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с	INPUT 9	CARDS FOR 0.0	PROGRAM IN F	IG 18 0•0	36.0		0•0	90 •0
	0.50J 0.0	0.500	J ∙625	0.750	0 •7 50	0•750	0•625	0.500
	0.00.0 0.0 0.0	0.125	0.125	0.125	0.000	-0.125	-0.125	-0.125
	9	-1.0		0.0				
	+8	161631	0189	26				
	+7	038466	+.028	86				
	+6	+.005762	++0199	949	•			
	+5	000098	+•000	05				
	+4	+.005762	++0199	949				
	+3	038466	+.028	86				
	+2	-•161631	0189	26				
	+1	-•133808	-•062	70				

Fig. 20. Inputs and outputs of the programs in appendices A, B, and C.

с	OUTPUT CARDS FROM	PROGRAM IN FIG	18		
+	9 -1.00000000	+•00000000	+1.000000000	+1.00000000	
+	8 -•16163100	-•01892600	+.02648277	+•16273528	
+	-703846600	+•02858600	+.00229679	+•04792486	
+	6 +.00576200	+•01994900	+.00043116	+.02076447	
+	-500009800	+.0090500	+.00000082	+.00091029	
+	4 +.00576200	+•01994900	+.00043116	+.02076447	
+	3 -03846600	+.02858600	+.00229679	+.04792486	
+		01892600	+.02648277	+•16273528	
+	-113380800	-06217000	+.02176969	+•14754555	
+	1 +.000000000	40730116	+.10256843	+.17641451	+•42001727
+	2 +10.00000000	40757072	+.07192805	+•17128753	++41386897
+	3 +20.00000000	41717391	01696248	+•17432180	+•41751862
+	4 +30+00000000	45908866	15166895	+•23376587	+•48349340
+	5 +40.00000000		30378805	+.40543550	+.63673817
+	6 +50+00000000	-•73096286	42788042	+•71738835	+.84698780
+	-7 +60.00000000	-•95541772	47370881	+1+13722310	+1.06640660
+	8 +70.00000000	-1•18309290	40961800	+1.56749570	+1.25199660
+	9 +80.00000000	-1-35024300	24259704	+1.88200950	+1.37183350
+1	0 +90.00000000	-1+40873720	01939185	+1.98491650	+1.40887060
+ 1	1 +100.00000000	-1.34830170	+.19377559	+1.85546650	+1.36215500
+ 1	2 +110.0000000	-1.19848000	+.34034474	+1.55218880	+1.24586860
- +1	3 +120+00000000	-1.01133640	+.39454128	+1.17846410	+1.08557080
+1	4 +130.00000000	83707761	+.36484096	+.83380786	+•91313080
+ 1	5 +140.00000000	-•70644604	+.28205393	+•57862043	+•76067103
+ 1	6 +150+00000000	-•62652430	+.18230454	+•42576765	+•65250873
+1	7 +160+30000030	-•58741117	+.09461487	+•35400386	+•59498223
+ 1	8 +170+00000000	-•57292317	+.03666559	+.32958533	+•57409522
+ 1	9 +180.00000000	-•56976057	+.01562214	+•32490341	+•57000299
+2	0 +190. 00000000	-•57292313	+.03666538	+.32958526	+•57409516
+2	1 +500.00000000 1 +500.00000000	-•58741106	+.09461452	+•35400366	+•59498206
+2	2 +210.00000000	-•62652402	+.18230404	+•42576711	+•65250832
+2	3 +220.00000000	-•70644550	+.28205340	· +•57861936	+•76067033
+2	4 +230.00000000	83707676	+.36484062	+•83380618	+•91312988
+2	25 +240.000000000	-1.01133550	+.39454130	+1•17846230	+1.08557000
+2	26 +250•000000000	-1+19847910	+.34034526	+1•55218710	+1.24586800
+2	27 +260.0000JJJJJ	-1+34830110	+•19377658	+1.85546530	+1•36215460
+2	28 +270•00000000	-1.40873720	- •01939065	+1•98491650	+1+40887060
+2	29 +280.00000000	-1.35024360	24259598	+1.88201060	+1.37186390
+.3	30 +290.000000000	-1.18309400	40961738	+1•56749780	+1.25199750
+:3	31 +300.00000000	95541896	-•47370878	+1.13722540	+1.06640770
+3	32 +310.00000000	73096395	-•42788091	+•71739037	+•84698900
+3	33 +320.000000000	55959727	30378879	+•40543673	+•63673913
+:	34 +330.00000000	45908900	-•15166970	+•23376641	+•48349396
+0	35 +340+000000000	41717405	01696307	+.17432194	++41751878
+3	36 +350.00000000	40757074	+.07192772	++17128751	+•41386895

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Fig. 20. Inputs and outputs of the programs in appendices A, B, and C.

APPENDIX D

Figure 21 is a SCATRAN[4] program for use on the IBM 7090 computer at the Ohio State University. By combining the programs in Appendix B into a single SCATRAN program and utilizing the greater speed of the IBM 7090, this program achieves the same results in about 1/50 th the time it takes the IBM 1620. In addition, the IBM 7090 provides more storage capacity which is necessary for the solution of arrays with large numbers of wires.

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	THIELE	G. JOBN FGJ176	01/13/65
	SA	WRITE OUTPUT +S1-	0028
F	S1	(///78H SCATTERING BY ARBITRARY ARRAY OF THIN WIRES WITH A	0029
		LINE SOURCE AT THE ORIGIN///) -	0030
		IJK=62-	0031
		DIMENSION $(U(61))V(61)) =$	0032
		DIMENSION (A(3782+1JK)+8(3782+1JK))-	0033
F	52	(7F10.6) -	0034
		READ INPUT +55+(111)-	0035
		DO THROUGH $(S260) + JJJ=1+1+JJJ=LE+11I-$	0036
		READ INPUT +S2+(FN+BKJ+BKY+AAA+PHI)-	0037
		N=FN-	0038
		READ INPUT • \$2•((U(I)•I=1•1•I•LE•N))-	0039
		READ INPUT •52•((V(I)•I=1•1•I•I•LE•N))-	0040
		DO THROUGH (S4) + 1 = 1 + 1 + 1 + LE + N-	0041
		$\cup (1) = 6 \cdot 2831853 + \cup (1) =$	0042
	S4	V(1)=6•2831853*V(1)-	0043
		NN=N+1-	0044
		WRITE OUTPUT +S10-	0045
F	S5	(215+F15+8) -	0046
F	S10	(///27H INTERWIRE SPACING KR(I.J)///)	0047
		DO THROUGH (S50) $i = 1 \cdot 1 \cdot 1 \cdot 1 \cdot 1 \cdot 1$	0048
		DO THROUGH (S30)+J=1+1+J+LE+N-	0049
		TRANSFER TO (S14+S12+S14) PROVIDED (I-J)-	0050
	512	A(I+J)=BKJ-	0051
		B(1,J)=-BKY_	0052
		TRANSFER TO (\$30)-	0053
	S14	$R = SQRT \cdot ((U(1) - U(J)) * (U(1) - U(J)) + (V(1) - V(J)) * (V(1) - V(J))) -$	0054
		WRITE OUTPUT (SS((1)JR)-	0055
		TRANSFER TO (S16+S16+S18) PROVIDED (R-4+)-	0056
	516	W=R/2+-	0057
		W1=W*W_	0058
		w2=w1+w1-	6059
		W3=W2+W1~	0060
		W4=W2+W2-	0061
		WD#W4*W1-	0062
		W6=W3+W3-	0063
			0064
		DD=10-W1+025*W2+0U2//770*W3+00017361*W4-	0065
		50=00-•0944•X•-4*W5+•1929•X•-5*W6-•394•X•-7*W7-	0066
		5*W1***J/5#W2+*0509259#W3+*0036169#W4-	0067
		>=>+++++++++++++++++++++++++++++++++++	0068
		T < +03001777#(3+00#(+37721366+LN+(W)))~	0069
		· (MANDER 10 (520)-	0070

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Fig. 21. SCATRAN program for obtaining the far-field pattern of an arbitrary array with a line source at the origin.

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1	S18	Z=1+/R-	0071
		X=Z+Z-	0072
		P=(107031#X+.11215#X#X)#.5641896-	0073
		Q={•125-•07324*X}#Z*•5641896-	0074
		BB=((P-Q)*COS+(R)+(P+Q)*SIN+(R))/SQRT+(R)-	0075
		Y=((P-Q)*SIN+(R)-(P+Q)*COS+(R))/SQRT+(R)-	0076
1	S20	A(1+J)=BB-	0077
		B(1*1)=	0078
1	S3 0	CONTINUE -	0079
		$R = SQRT \cdot (U(1) + U(1) + V(1) + V(1)) -$	0080
		TRANSFER TO (S 36+S36+S38) PROVIDED (R-4+)-	0081
	S 36	₩≠R/2	0082
		W1=w*w_	0083
		W2=W1+W1-	0084
		₩3≖₩2*₩1-	0085
		₩4=₩2*₩2~	0086
		W5=W4*W1-	0087
		₩6=₩3 + ₩3~	0088
		₩7≖₩3₩₩4-	0089
		88=1•+W1+•25*W2+•0277778*W3+•0017361*W4-	0090
		₿₿=₿₽₽~•6944•X•-4*₩5+•1929•X•-5*₩6-• 3 94•X•-7*₩7~	0091
		S=W1-+375*W2++0509259*W3-+0036169*W4-	0092
		S=S++15856+X+-3*w5-+4726+X+-5*w6++1021+X+-6*w7-	0093
		Y=+03661977#(S+88#(+5772 1566+LN+(W))) -	0094
		TRANSFER TO (S49)-	0095
	S38	Z=1•/R-	6096
		x=z*z-	0097
		P=(1~.07031*X+.11215*X*X)*.5641896-	0098
		Q=(•125-•07324*X)*Z*•5641896-	0099
		BB=((P-Q)*COS+(R)+(P+Q)*S1N+(R))/SQRT+(R)-	0100
		Y=((P-Q)*SIN+(R)-(P+Q)*COS+(R))/SQRT+(R)-	0101
	549	B(I+NN)=-Y-	0102
	S50	A(1+NN)=BB-	0103
		WRITE OUTPUT +S2+(((A(I+J)+J=I+1+J+LE+NN)+I=I+I+I+LE+N))-	0104
		WRITE OUTPUT +52+(((B(I+J)+J+1+1+J+LE+NN)+I=1+1+LE+N})-	0105
		WRITE OUTPUT +S60-	0106
F	S60	(///46H REAL AND IMAGINARY PARTS OF CURRENT ON WIRE 1///)	0107
		-	0108
F	S8 0	(15,2715,8) -	0109
		DO THROUGH (S118)+L=1+1+L+LE+N-	0110
		DO THROUGH (S118)+1=L+1+1+L+N-	0112
		11=1+1-	0111
		TRANSFER TO (S104+S104+S103) PROVIDED (LLL)-	0114

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Fig. 21. SCATRAN program for obtaining the far-field pattern of an arbitrary array with a line source at the origin.

5103	DU THRUUGH (SII/)+K=I+I+K+LE+LLL-	0115
	A(I+L)=A(I+L)-A(I+K)#A(K+L)+B(I+K)#B(K+L)-	0116
	B(I+L)=B(I+L)~A(I+K)*B(K+L)~A(K+L)*B(I+K)~	0117
	A(L+II)=A(L+II)-A(L+K)*A(K+II)+B(L+K)*B(K+II)-	0118
5117	(•) ≠ (•) + A (• K) + B (K •) + B (• K) + A (K •) +	0119
S104	R=A(L+L)*A(L+L)+B(L+L)*B(L+L)-	0120
	S=A(L+II)-	0121
	T=B(L+11)-	0122
	A(1, 0, 1, 1) = (A(1, 0, 1) + S + B(1, 0, 1) + T) / R - 1	0123
SILB	B(1 + 11) = (A(1 + 1) + T - B(1 + 1) + S)/B =	0124
3110	WRITE OUTPUT AS80. (N.A(N.NN).B(N.NN)) =	0124
		0125
		0120
	1 = N/N = (,,	0127
		0128
	DO THROUGH (SIZZ) K=II · I · K · LE · N-	0129
	$A(I \circ NN) = A(I \circ NN) - A(I \circ K) * A(K \circ NN) + B(I \circ K) * B(K \circ NN) - A(I \circ N) + B(K \circ NN) - A(I \circ N) + B(K $	0130
S122	$B(1 \circ NN) = B(1 \circ NN) - A(1 \circ K) + B(K \circ NN) - B(1 \circ K) + A(K \circ NN) - \frac{1}{2}$	0131
S123	WRITE OUTPUT +S80+(I+A(I+NN)+B(I+NN))-	0132
	WRITE OUTPUT +S200-	0133
F 5200	(///18H FAR FIELD PATTERN///) -	0134
	READ INPUT +S2+(P+DP+FM)-	6135
	M#FM-	0136
	A(0,NN) = -1 -	0137
	B(0+NN)=+0-	0138
	U(Q) = QQ	0139
		0100
		0140
	DO 100000 (3240/01-101010LC0M-	0141
		0142
		0143
	5=51N•(PR)-	0144
	ER=0+-	0145
	E1=0•-	0146
	DO THROUGH (S230)+J=O+1+J+LE+N-	- 0147
	Z=U(J)*C+V(J)*S-	0148
	CZ=COS•(Z)-	0149
	SZ=SIN+(Z)-	0150
	ER=ER+A(J•NN)*CZ-B(J•NN)*SZ-	0151
\$230	EI=EI+B(J•NN)#CZ+A(J•NN)#SZ-	0152
0100	FS=ER+ER+E1+E1-	0153
	FESORTA (ES)-	0154
		0155
6240		0156
5270 F 5250	(5F14+8) -	0150
6260	WOITE OUTOUT ASIA	0124
3600	END DOGRAM (SA)_	0120
		W137

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Fig. 21. SCATRAN program for obtaining the far-field pattern of an arbitrary array with a line source at the origin.

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