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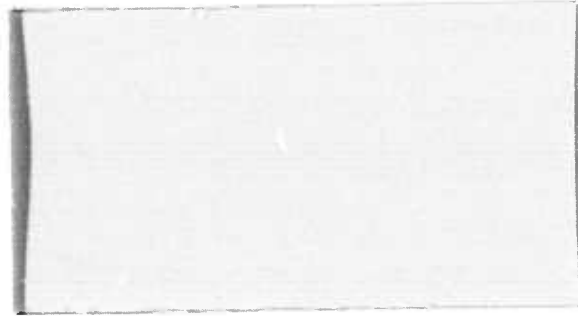
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# HYDRONAUTICS, incorporated research in hydrodynamics

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HYDRONAUTICS, Incorporated

TECHNICAL REPORT 349-1

AN ANALYTICAL STUDY OF THE  
HYDRODYNAMIC PERFORMANCE OF  
WINGED, HIGH-DENSITY TORPEDOES

By

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NOTATION

A	aspect ratio of wing = $\frac{4(b - \sqrt{1 - \gamma^2 R_b})^2}{S_w}$
A <sub>t</sub>	aspect ratio of the ring tail = $\frac{D_m}{C_{rt}}$
B	buoyancy force
b	distance from center of torpedo to tip of wing
t.c.	specific fuel consumption: lb-fuel/HP-Hr.
C	chord of wing
C <sub>A</sub>	total drag coefficient based on the wetted surface area of a body of revolution
C <sub>D</sub>	drag coefficient
C <sub>D<sub>o</sub></sub>	together with K defines the profile drag of the wing section
$\bar{C}_D$	drag coefficient based on $(V_w)^{\frac{2}{3}}$
C <sub>f</sub>	friction coefficient
C <sub>L</sub>	total lift coefficient based on exposed wing area
C <sub>L<sub>w</sub></sub>	lift coefficient developed on the wing
C <sub>La</sub>	lift curve slope
C <sub>pr</sub>	prismatic coefficient = $\frac{V_b}{\frac{\pi}{4} D_m^2 l}$
C <sub>rt</sub>	chord of ring tail
C <sub>s</sub>	surface coefficient = $\frac{S_b}{\pi D_m l}$



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$\bar{C}_w$  weight coefficient =  $\frac{W}{\rho V_w^{\frac{1}{3}}}$

D total drag

$D_m$  maximum diameter of torpedo

$\bar{D}_m = D_m / (V_w)^{\frac{1}{3}}$

$G(\gamma, R_b')$  algebraic function defined by Equation [30]

I moment of inertia

K,  $K_1$  constants

L lift

$l$  length of torpedo

$l_c$  length of central cylindrical portion of the torpedo

$l_t$  distance from the c.g. of torpedo to the c.p. of ring tail

M pitching moment

q dynamic pressure =  $\frac{1}{2} \rho U^2$

R buoyancy ratio =  $\frac{B}{W}$

$R_b$  radius of body

$R_b' = R_b / b$

$Re_l$  Reynolds number based on  $l$

$Re_t$  Reynolds number based on  $C_{rt}$

$Re_v$  Reynolds number based on  $V_w^{\frac{1}{3}}$

S range in miles

$S_b$  surface area of body

$S_w$	wing planform area
$S_v'$	ratio of the wetted area of the supporting vanes to area of ring tail
$S_t$	surface area of ring tail
$s$	maximum allowable stress
$s'$	$= sV_w^{\frac{2}{3}} W$
$T$	thrust
$t$	thickness ratio = $D_m/l$
$U$	uniform stream velocity
$V_b$	volume of the torpedo
$V_w$	volume of water whose weight is $W$ , $V_w = \frac{W}{\rho_w g}$
$W$	total weight of torpedo
$W_F$	total fuel weight
$\bar{x}$	distance from the nose of a body of revolution to the transition point
$y_{\max}$	distance from vertical axis to the outermost fiber
$\bar{z}$	nondimensional sectional modulus = $\frac{I}{y_{\max} C^3}$
$\alpha$	angle of attack
$\gamma$	$\gamma R_b$ is the distance from the centerline of the torpedo to a horizontally mounted wing.
$\eta$	propulsive efficiency

$\theta$	climbing angle
$\rho_b$	density of body
$\rho_w$	density of water

subscripts

b	body
r	wing root
t	tail, or wing tip
w	wing

## ABSTRACT

The hydrodynamic performance of winged torpedoes has been investigated. It is assumed that the wing is mounted such that its center of pressure coincides with the center of gravity of the body, and that a ring-tail stabilizer is used. The resulting overall lift-drag ratios are presented as functions of the buoyancy-weight ratio. The advantages of the winged torpedoes over those with neutral buoyancy become more pronounced as the nondimensional parameter  $\bar{C}_w$  becomes smaller, and as the buoyancy-weight ratio decreases.  $\bar{C}_w$  is defined as  $W / \frac{1}{2} \rho_w U^2 (V_w)^{\frac{2}{3}}$ , where  $W$  is the weight;  $\frac{1}{2} \rho_w U^2$ , the free stream dynamic pressure; and  $V_w$  is the volume of water with weight,  $W$ . Parametric studies of the lift-drag ratio obtainable have been carried out with respect to the following quantities: the Reynolds number based on  $(V_w)^{\frac{1}{3}}$ , the nondimensional strength factor of the wing material, and the maximum allowable diameter. In conclusion, the ranges obtainable for the ascending, level, and descending flights are calculated. It is found that if the fuel weight is assumed to be always one-half of the displacement, winged torpedoes have longer ranges than those with neutral buoyancy only for descending missions. If the fuel weight, however, is assumed to be one-half of the total weight, the winged torpedo has longer ranges for all missions except steep ascending ones.

## INTRODUCTION

Up to now, torpedoes have been generally designed with neutral buoyancy. If one departs from this concept and considers a winged torpedo, for which part of the weight is carried by the dynamic lift generated on the wings, a more efficient torpedo, depending on the design weight and speed, may be evolved. In this report, a preliminary investigation has been made on the overall lift-drag ratio obtainable, the size of the wing needed, and the range of travel for winged torpedoes at different values of buoyancy to weight ratios.

In the calculations, it is assumed that the wing is mounted such that its center of pressure coincides in axial position with that of the center of gravity of the torpedo. The assumption simplifies the tail selection for which considerations of stability must be made. We also assume that a ring tail is used to provide the required stability. Two types of bodies are considered: one is the optimum body for a given volume; the other is a diameter-limited body (i.e., limited to the maximum allowable size for use in existing torpedo tubes). In the following, the methods by which the component drags and the range are calculated are developed and the results of such calculations are presented and discussed.

## METHODS OF CALCULATION

### A. Drag

Let the weight of the torpedo be  $W$ ; let the drag due to the body, tail, and wing be denoted by  $D_b$ ,  $D_t$ , and  $D_w$  respectively. The overall lift to drag ratio is

$$\frac{W}{D} = \frac{W}{D_b + D_t + D_w} \quad [1]$$

The buoyancy to weight ratio, or in other words the ratio of the density of water  $\rho_w$ , to that of the torpedo,  $\rho_b$ , is denoted by R,

$$R = \frac{B}{W} = \frac{V_b \rho_w g}{V_w \rho_w g} = \frac{V_b}{V_w}; \quad R = \frac{B}{W} = \frac{V_b \rho_w g}{V_b \rho_b g} = \frac{\rho_w}{\rho_b}, \quad [2]$$

where B denotes the total buoyancy force. To normalize the forces, we use the dynamic pressure of the uniform stream,  $\frac{1}{2}\rho_w U^2$ , and  $(V_w)^{\frac{2}{3}}$ , where  $V_w$  is the volume of water whose weight is W:

$$V_w = \frac{W}{\rho_w g} \quad [3]$$

For a constant weight and constant forward speed U, the normalizing force,  $\frac{1}{2}\rho_w U^2 (V_w)^{\frac{2}{3}}$ , is constant. Let

$$\bar{C}_w \equiv \frac{W}{\frac{1}{2}\rho_w U^2 (V_w)^{\frac{2}{3}}}; \quad [4]$$

It then follows that

$$\frac{W}{D} = \frac{\bar{C}_w}{\bar{C}_{d_b} + \bar{C}_{d_t} + \bar{C}_{d_w}} \quad [5]$$

In the following, we examine each drag component separately.

(1) Body Drag

In the total drag of the body, (skin friction plus form drag), we use the results of Young (Reference 1). Young's calculation of total drag coefficients based on wetted surface area,  $C_A$ , are presented in graphical form. To facilitate computation by the IBM 1620 digital computer, the process of curve-fitting has been carried out to give the following formula:

$$C_A = 10^{-2} \times [.035(g - \log_{10} Re_\ell)^2 + .215 - .24 \bar{x}/\ell - (.2 - t)Y]. \quad [6]$$

$$Y = \begin{cases} .78 - .28(\log_{10} Re_\ell - 6) + .12(\log Re_\ell - 7)^2 & t > .2, \\ .37 - .12(\log_{10} Re_\ell - 6) + .04(\log Re_\ell - 7)^2 & t < .2, \end{cases} \quad [7]$$

in which  $Re_\ell$  denotes the Reynolds number based on body length  $\ell$ ;  $\bar{x}$ , distance from the nose to the transition point;  $t$ , the thickness ratio. In the optimum body,  $t = 0.2$ , and the expression for  $C_A$  is considerably simplified.

Since the comparisons will be carried out at constant speed and weight, the Reynolds number based on  $V_w^{\frac{1}{3}}$  is considered known:

$$Re_v = \frac{UV^{\frac{1}{3}}}{\nu} \quad [8]$$

To calculate  $Re_\ell$  from  $Re_v$ , we first define the (logitudinal) prismatic coefficient  $C_{pr}$  as

$$C_{pr} \equiv \frac{V_b}{\frac{\pi}{4} D_m^2 l}, \quad [9]$$

where  $V_b$  is the volume and  $D_m$  the maximum diameter of the body. By the definitions of the buoyancy — weight ratio and the thickness ratio, we obtain from [9]

$$V_w = \frac{\pi}{4R} C_{pr} t^2 l^3. \quad [10]$$

The Reynolds number based on body length is then

$$Re_l = \frac{Re_v}{\left(\frac{\pi}{4R} C_{pr} t^2\right)^{\frac{1}{3}}}. \quad [11]$$

To obtain  $\bar{C}_{D_b}$ , we define a surface coefficient  $C_s$

$$C_s \equiv \frac{S_b}{\pi D_m l}, \quad [12]$$

where  $S_b$  is the wetted area of the body. By simple algebra, we obtain

$$\bar{C}_{D_b} = C_A C_s \left[ \frac{16\pi R^2}{C_{pr}^2 t} \right]^{\frac{1}{3}}, \quad [13]$$

where  $C_A$  is obtainable from Equations [6] and [7].

For definiteness, we shall consider that the optimum body is a spheroid of thickness ratio 0.2, and the diameter-limited body



is made up of a central cylindrical section of length  $l_c$  and two semi-spheroidal noses. In such a composite body, the prismatic and surface coefficients are easily computed to be

$$C_{pr} = \frac{2 + l_c/l}{3} . \quad [14]$$

and

$$C_s = \frac{l_c}{l} + \frac{1}{2} \left[ \left(1 - \frac{l_c}{l}\right) (1 - t^2)^{-\frac{1}{2}} \sin^{-1}(1 - t^2)^{\frac{1}{2}} + t \right] . \quad [15]$$

For a spheroid,  $l_c/l = 0$ ,

$$C_{pr} = 2/3 , \quad [16a]$$

$$C_s = \frac{1}{2} \left[ (1 - t^2)^{-\frac{1}{2}} \sin^{-1}(1 - t^2)^{\frac{1}{2}} + t \right] . \quad [16b]$$

Let  $\bar{D}_m = D_m V_m^{-\frac{1}{3}}$  be the nondimensional maximum diameter. By the definition of the prismatic coefficient, we can write the thickness ratio  $t$  as

$$t = \frac{\pi}{12} (2 + l_c/l) \bar{D}_m^3 . \quad [17]$$

The volume of the body is

$$\begin{aligned} V_b &= \frac{\pi D_m^3}{12} l (2 + l_c/l) \\ &= \frac{\pi}{12} \bar{D}_m^3 l^3 \left( \frac{\pi}{4R} C_{pr} t^3 \right)^{\frac{2}{3}} (2 + l_c/l) . \end{aligned} \quad [18]$$

In the optimum body,  $t = 0.2$ , and  $C_{pr} = 2/3$ .  $C_s$  may be calculated according to [16b]. Equation [13] together with [6] gives the required value of  $\bar{C}_{D_b}$ . For a diameter-limited body,  $t_c/t$  and  $\bar{D}_m$  must be specified. From these values,  $C_{pr}$  and  $t$  are calculated according to [14] and [17] respectively.  $C_s$  may be obtained by [15], together with the value of  $C_A$  obtainable from [6] and [7], and  $\bar{C}_{D_b}$  can again be calculated.

### (2) Tail Drag

We assume that the position of the wing is such that it does not contribute to the moment when the entire configuration is pitched. According to experience, the static restoring moment generated by the tail is usually some fraction of the static destabilizing moment generated by the body. The configuration must be dynamically stable. We design the tail such that

$$M_t = K_1 M_b, \quad K_1 > 0, \quad [19]$$

where  $M_t$  and  $M_b$  denote moments due to the tail and the body respectively;  $K_1$  is a constant.  $K_1 > 0$  implies that the moments are opposite in sense. By slender body theory, at a pitch angle  $\alpha$

$$M_b = \rho_w U^2 V_b \alpha. \quad [20]$$

The moment generated by the tail may be written in terms of the lift curve slope of the tail,  $C_{Lat}$ , the dynamic pressure  $q$ , the

tail surface area,  $S_t$ , and the distance from the c.g. of the body to the tail center of pressure,  $l_t$ :

$$M_t = C_{Lat} q S_t l_t \alpha . \quad [21]$$

Equation [19] gives then

$$C_{Lat} = \frac{\pi K_1 C_{pr} t^2 l^3}{2 S_t l_t} . \quad [22]$$

For a ring tail

$$\begin{cases} S_t = \pi D_m C_{rt} , \\ A_t = \frac{D_m}{C_{rt}} , \end{cases} \quad [23]$$

in which  $C_{rt}$  is the chord of the ring tail. The diameter of the ring tail is taken as the maximum diameter of the body. Using the definition  $S_t$  and  $A_t$ , [22] becomes

$$\frac{C_{Lat}}{A_t} = \frac{1}{2} K_1 C_{pr} l/l_t . \quad [24]$$

Weissinger (Reference 2) gives the effectiveness of a ring wing approximately as

$$\frac{A_t}{C_{Lat}} \cong \frac{1}{2} + \frac{1}{\pi} \left( A_t + \tan^{-1} \frac{1.2}{A_t} \right) . \quad [25]$$

Solving [24] and [25] simultaneously, we obtain the aspect ratio of the tail  $A_t$ , thence

$$\left( A_t + \tan^{-1} \frac{1.2}{A_t} \right) = \frac{\pi}{2} \left( K_1 C_{pr} \ell / \ell_t - 1 \right). \quad [26]$$

To determine the frictional drag, we calculate the Reynolds number of the tail

$$Re_t = \frac{UC_{rt}}{v} = \frac{t}{A_t} Re_{\ell} \quad [27]$$

The drag of the tail non-dimensionalized with respect to  $qV_w^{\frac{2}{3}}$  is

$$\bar{C}_{D_t} = C_f \left\{ \frac{128\pi t^2 R^2}{C_{pr}^2} \right\}^{\frac{1}{3}} \left( \frac{1 + S_v'}{A_t} \right), \quad [28]$$

where  $S_v'$  is ratio of the wetted surface area of the supporting vanes to that of the tail, and  $C_f$  is the friction coefficient.

### (3) Wing Drag.

The drag of the wing can only be determined after the wing has been sized. Preliminary considerations show that the wings may be of small aspect ratio, say near 1, and of small span. The interference effects between the wing and the body must now be considered.

At the design condition, the body is considered to be at zero angle of attack, while the wing is set so that the desired

amount of lift is developed. Lawrence and Flax (Reference 3) have considered the interference lift generated on an infinite circular cylinder due to a finite lifting line of arbitrary lift distribution mounted therein. The problem is solved in the Trefftz plane by the use of Green's theorem. The interference lift generated on the body can be obtained by an integration along the wing of the product of the lift distribution and the velocity component normal to the wing due to a vertical translation of the cylinder. In their paper, Lawrence and Flax (Reference 3) calculated the interference lift on the cylinder due to a constant, elliptic, and optimum lift distribution on a centrally-mounted, horizontal lifting line. The results do not differ appreciably. Furthermore, they have shown that the lift on the body subsides in about two diameters in either direction from the lifting line; the idealization of an infinite cylinder for the body is thus not without justification. In the present case, we have calculated the total lift of the wing-body system (lift on wing + interference lift on body) for a horizontal lifting line of constant lift distribution, whose tip to tip distance is  $2b$ , mounted  $\gamma R_b$  above the center of the cylinder of radius  $R_b$ . Defining the lift coefficient with respect to the wing area  $S_w$ , we obtain

$$C_L = \frac{L}{qS_w} = C_{L_w} G(\gamma, R_b'), \quad [29]$$

$$G(\gamma, R_b') = \frac{1 - (1 - \gamma^2) R_b'^2}{[1 - (1 - \gamma^2)^{\frac{1}{2}} R_b'] (1 + \gamma^2 R_b'^2)}, \quad [30]$$

where  $R_b' = R_b/b$ . For wings of large span,  $R_b' \rightarrow 0$ ,  $G(\gamma, 0) = 1$ , then

$$C_L \approx C_{L_w}.$$

The function  $G$  is shown in Figure 1 for different values of  $\gamma$ . It is seen that centrally mounted wings are the most efficient in producing the interference lift on the body. However, for the present application, the wings will necessarily be stored within the body prior to and during the launch and a centrally mounted wing may not be feasible.

Before we select the wing which will carry the required lift while incurring the least amount of drag for our present winged torpedo system, it is instructive to consider briefly the optimum design of an isolated wing. In general, the drag coefficient of a wing may be written as

$$C_D = C_{D_0} + KC_L^2 + \frac{C_L^2}{\pi A} (1 + \delta), \quad [31]$$

in which the first two terms are the profile drag of the wing section and the last term is the induced drag;  $\delta$  is the factor introduced to take into account that the loading may not be elliptical. Dividing [31] through by  $C_L$ , and finding the minimum  $C_D/C_L$  we obtain

$$\left(\frac{C_D}{C_L}\right)_{\min} = 2 C_{D_0}^{\frac{1}{2}} \left(K + \frac{1 + \delta}{\pi A}\right)^{\frac{1}{2}}, \quad [32]$$

in which the optimizing components are

$$\left(C_L\right)_{\text{opt}} = \left(\frac{C_{D_0}}{K + \frac{1 + \delta}{\pi A}}\right)^{\frac{1}{2}} \quad [33]$$

and

$$\left(C_D\right)_{\text{opt}} = 2 C_{D_0} \quad [34]$$

It is seen that the larger the aspect ratio, the smaller the resulting drag for the same lift. However, the aspect ratio is limited by the bending stress allowable at the mid-span. For elliptic loading, the bending moment at the mid-span is

$$\frac{2}{3\pi} Lb = \frac{I_s}{y_{\text{max}}} , \quad [35]$$

in which  $I$  is the moment of inertia and  $y_{\text{max}}$  is the distance from the neutral axis to the outermost fiber, and  $s$  is the tensile stress at the outermost fiber. Rewriting and transposing, assuming a rectangular wing we obtain

$$C_L A^2 = 3\pi \bar{z} \frac{s}{q} , \quad [36]$$

in which  $\bar{z}$  is the nondimensional sectional modulus

$$\bar{z} = \frac{I}{y_{\text{max}} C^3} . \quad [37]$$

When the working stress of the wing material is given, Equations [33] and [36] determine the optimum aspect ratio and  $C_L$ .

Returning now to the winged torpedo, we follow the same procedure as above with the added complications that: (a) the profile drag is only found on the exposed wing, while the induced drag may be calculated according to the full span  $2b$ , (b) the maximum bending stress is at the wing-body juncture, (c) the lift developed by the wing is some fraction of the total lift required depending upon the position of the wing with respect to the center of the body, and (d) we allow the wing to be tapered. With these considerations, the counterpart of [33] is

$$C_{L_w} = \frac{C_{D_o}^{\frac{1}{2}}}{\left\{ K + \frac{1 + \delta}{\pi A} G(\gamma, R_b') [1 - (1 - \gamma^2)^{\frac{1}{2}} R_b'] \right\}^{\frac{1}{2}}} \quad [38]$$

and that of [36] is

$$C_{L_w} A^2 = \frac{24\pi}{(1 + C_t/C_r)^3} \bar{z}_r \frac{s}{q}, \quad [39]$$

where  $C_t$  and  $C_r$  denote the chord at the tip and the root respectively, and  $\bar{z}_r$  is the nondimensional sectional modulus of the root section. The aspect ratio  $A$  is that of the exposed wing. Let now the working stress be nondimensionalized with respect to  $WV_w^{-\frac{2}{3}}$ , and writing it as  $s'$ , [39] becomes



$$C_{L_w} A^2 = \frac{24\pi}{(1 + C_t/C_r)^3} \bar{z}_r s' \bar{C}_w . \quad [40]$$

Because of the added variable  $R_b'$ , another equation is needed.

This is obtained by considering the relation between  $C_{L_w}$  and  $W$ :

$$C_{L_w} = \frac{W(1 - R)}{G(\gamma, R_b') q S_w}$$

$$) = \frac{\bar{C}_w(1 - R)}{G(\gamma, R_b')} \frac{V_w^{\frac{2}{3}}}{S_w} . \quad [41]$$

Rewriting the wing area  $S_w$  in terms of aspect ratio and  $V_w$  according to [10], we obtain

$$C_{L_w} = \frac{\bar{C}_w(1 - R)}{G(\gamma, R_b')} \frac{R_b'^2 (C_{pr} \frac{\pi}{4R})^{\frac{2}{3}}}{[1 - (1 - \gamma^2)^{\frac{1}{2}} R_b']^2} A . \quad [42]$$

Equations [38], [39], and [42] determine  $C_{L_w}$ ,  $A$ , and  $R_b'$  for given values of  $\gamma$ ,  $C_{pr}$ ,  $t$ ,  $C_t/C_r$ ,  $\bar{z}_r$ ,  $\bar{C}_w$ ,  $R$ ,  $\delta$ ,  $K$ , and  $C_{D_o}$ .

Now it is an easy matter to determine the drag contribution due to the wing:

$$\bar{C}_{D_w} = \frac{2C_{D_o} S_w}{q V_w^{\frac{2}{3}}} . \quad [43]$$

By the use of [41], we obtain

$$\bar{C}_{D_w} = \frac{2C_{D_o}}{q} \frac{\bar{C}_w(1-R)}{C_{L_w} G(\gamma, R_b')} \quad [44]$$

These expressions have been programmed for computation on the IBM 1620 Computer for the following values of the constants:

$$\begin{aligned} K &= .012 \\ C_{D_o} &= .009 \\ \delta &= 0 \\ C_t/C_r &= .5 \\ l_c/l &= .5 \\ \bar{x} &= 0 \\ \gamma &= 0.7 \\ K_1 &= 0.7 \\ S_v' &= .5 \end{aligned}$$

The value of  $K$  and  $C_{D_o}$  determine the profile drag of the wing which should be a function of the Reynolds number. In the present calculation, they are assumed to be constant. Since the wing drag is usually one order of magnitude smaller than the body drag, the simplification should not incur too much of an error. In order to select a suitable range of values for  $\bar{C}_w$ , we have calculated  $\bar{C}_w$  for a 3000 pound and 6000 pound torpedo with forward

speeds of 10 to 100 knots. The results are shown in Figure 2. It is seen that the value of  $\bar{C}_w$  ranges from 0.01 (at about 100 knots) to 1 (at about 10 knots). The difference in the weight of the torpedo has no appreciable effect on the value of  $\bar{C}_w$ , since it is proportional to  $W^{\frac{1}{3}}$ .

The computation scheme is as follows: For assumed values of  $Re_v$ , the product  $s' \bar{z}$ , and  $\bar{D}_m$ , the value of  $\bar{C}_w$  is systematically varied. For each value of  $\bar{C}_w$ , the buoyancy ratio  $R$  is varied from 0.2 to 1.0. In each of these cases, the component drags, the overall lift-to-drag ratio  $W/D$ , the lift coefficient  $C_{L_w}$ , aspect ratio  $A$  and the radius-span ratio  $R_b'$  are calculated for both the optimum body ( $t = 0.2$  spheroid) and the diameter limited body. The following six cases have been computed:

	$Re_v$	$s' \bar{z}$	$\bar{D}_m$
1	$1.2 \times 10^8$	0.7	.481
2	$6 \times 10^6$	0.7	.481
3	$6 \times 10^6$	33.0	.383
4	$6 \times 10^6$	33.0	.481
5	$4 \times 10^7$	.7	-
6	$8 \times 10^7$	.7	-

In cases 5 and 6, only optimum bodies are calculated. The results from cases 1 and 2, together with 5 and 6 give the Reynolds number effect; cases 2 and 4 give the effect of  $s' \bar{z}$ ; cases 3 and 4 give the effect of  $\bar{D}_m$ .

B. Range

Let the torpedo be ascending at an angle  $\theta$  with respect to the horizontal. When in uniform motion, the thrust balances the drag and the component of the effective weight, i.e., weight less buoyancy, in the direction of flight:

$$T = (W - B) \sin \theta + D. \quad [45]$$

Let  $l.c.$  be the specific fuel consumption in weight of fuel per unit power output of the engine,  $\eta$  be the propulsive efficiency. The rate at which weight of fuel,  $W_F$ , is being spent is then

$$\frac{dW_F}{dt} = \frac{l.c. \cdot TU}{\eta} \quad [46]$$

Rewriting [46] and using [45], we obtain

$$\frac{l.c.}{\eta} U dt = \frac{dW_F}{(W - B) \sin \theta + D} \quad [47]$$

Assuming now both the specific fuel consumption,  $l.c.$ , and the propulsive efficiency,  $\eta$ , stay essentially constant, the left-hand side integrates out to be  $l.c. \cdot S/\eta$ , where  $S$  is the range. In torpedo applications, the weight of the torpedo is kept constant by using water to displace the fuel. If the density of the stored fuel is comparable to that of water, the buoyancy  $B$  stays constant; the total drag of the torpedo  $D$  is also a constant.

Then [47] gives

$$\frac{l.c.}{\eta} S = \frac{W_F}{W(1-R) \sin \theta + D}, \quad [48]$$

in which  $W_F$  is the total fuel weight. Writing in terms of the lift-drag-ratio, [48] becomes

$$\frac{l.c.}{\eta} S = \frac{W_F}{W} \frac{W/D}{\frac{W}{D} (1-R) \sin \theta + 1}. \quad [49]$$

It is seen from [49] that if  $\theta$  is the glide angle

$$\theta = - \sin^{-1} \frac{1}{\frac{W}{D} (1-R)}, \quad [50]$$

and the torpedo will travel on indefinitely without expending any fuel.

To facilitate calculation, we use the following units for the quantities on the left of Equation [49]:

$l.c.$  = lb fuel/horsepower - hour,

$S$  = range in miles.

Then the range expression becomes

$$\frac{l.c.S}{\eta} = 375 \frac{W_F}{W} \frac{W/D}{\frac{W}{D} (1-R) \sin \theta + 1} \text{ miles-lb fuel/horsepower-hour.}$$

[51]

Calculations of the range factor  $l.c. S/q$  have been made for the optimum body configuration at  $Re_v = 1.2 \times 10^8$  and  $s' \bar{z} = 0.7$  (corresponding to case 1). Two different assumptions have been made on the fuel weight: in the first case we assume that the fuel weight equals one-half of the displacement; in the second case, we assume that it equals one-half of the total weight.

## RESULTS AND DISCUSSIONS

### A. Lift-Drag Ratio

In Figure 3, we have presented the results of case 1; the lift-drag ratio is shown as a function of the buoyancy ratio with  $\bar{C}_w$  as a parameter. The results for the torpedo with the optimum body is shown in solid lines while that for the diameter-limited body is shown in dash lines. The lift-drag ratio,  $W/D$ , is plotted along a logarithmic scale, since in this way, irrespective of the values of  $W/D$  at  $R=1$ ,  $(W/D)_1$ , an  $x$ -fold increase therefrom will appear a constant linear distance  $(\log x)$  above  $(W/D)_1$ . The steeper the curves of  $W/D$ , the larger the relative increase of  $W/D$ . The smaller the  $\bar{C}_w$ , the larger the effect of decreasing the buoyancy ratio on the improvement of  $W/D$ . The effect of limiting the body diameter is always detrimental to the value of  $W/D$  obtainable. In Figure 4, we have shown the drag breakdown for this case of  $\bar{C}_w$ , which is quite typical. It is seen that a major portion of the drag is due to the body. If by some means the drag of the body can be reduced (e.g., by boundary layer suction, by the use of cavity running torpedoes or through the use of stabilizing additives), the resulting  $W/D$  can be further increased.

In Figures 5 and 6, only the results from the optimum body for cases 2 and 3 are presented. In Figure 5, intermediate values of  $\bar{C}_w = 0.75$  and  $0.5$  have been calculated and presented. It is seen that for  $\bar{C}_w$  greater than  $0.5$ , there is no advantage to be gained by using wings. However at the lower values of  $\bar{C}_w$ , say,  $0.01$  ( $\approx 3000$  pound torpedo at 90 knots, c.f. Figure 2), the value of  $W/D$  at  $R = .2$  is nearly 3 times that at  $R = 1.0$ .

Cross-comparing Figures 5 and 6, it is seen that the effect of  $s' \bar{z}$  on the resulting  $W/D$  is quite small. The larger value of  $s' \bar{z}$  permits the use of higher aspect-ratio wings with concomitant savings in the wing drag. However, the drag due to the wing constitutes only a small portion of the total drag, as shown in Figure 4, and the savings show up significantly only for  $\bar{C}_w \geq .1$ , and only at small  $R$ 's.

In Figure 7, the effect of the maximum allowable diameter is shown. The smaller diameter body, having a surface area larger than that of the bigger diameter body for enclosing the same volume, incurs larger drag. This explains the difference in  $W/D$  at  $R=1$ . However, the improvement on  $W/D$  can be made larger for the smaller diameter body.

Figures 8 and 9 refer to cases 5 and 6. Cross-comparing these two figures with Figures 3 and 5, we obtain the effect of the Reynolds number,  $Re_v$ . The  $W/D$  obtainable are smaller for smaller  $Re_v$ . However, as we shall see in Figure 13, the Reynolds number has little effect on the improvements attainable on  $W/D$ .

In Figures 10 through 13, we have shown the improvements on  $W/D$  attainable as a function of  $\bar{C}_w$ . We define the nondimensional increase in lift-drag ratio  $\Delta(W/D)$  as

$$\Delta(W/D) \equiv \frac{(W/D)_{R=.2} - (W/D)_{R=1}}{(W/D)_{R=1}} \quad [52]$$

When  $\Delta(W/D) = 1$ , the lift-drag ratio at buoyancy ratio  $R = 0.2$  is twice that at  $R = 1$ . In Figure 10,  $\Delta(W/D)$  is plotted vs. logarithm of  $\bar{C}_w$  for case 1. It is seen that for  $\bar{C}_w \geq 0.4$ , the winged torpedo is less efficient than the neutrally buoyant one. At low values of  $\bar{C}_w$ , the torpedo which consists of the diameter-limited body is not as efficient as that with the optimum body. In the same Figure, the aspect ratio of the wing  $A_w$  and the span-diameter ratio, or equivalently half-span-radius ratio,  $b/R_b$ , for the optimum-body torpedo at  $R = .2$  are also shown. It is seen that at  $\bar{C}_w \approx .01$ , the wing span as well as the aspect ratio are quite small;  $A_w \approx 0.5$ ,  $b/R_b \approx 0.8$ . We note here that the wing span may be smaller than the body diameter due to the location of the wing.

In Figure 11, the  $\Delta(W/D)$  for case 2 is shown; the general trend is quite similar to that of case 1. In Figure 12, cases 3 and 4 are shown. For these two cases, the strength factor,  $s'\bar{z}$ , is 33 which is about 50 times that of case 2. The aspect ratio of the wing is about six times that of case 2, although the resulting  $\Delta(W/D)$  is not too much different in these two cases. This is for the reason which has been stated before, that the



contribution of the wing to the total drag is quite small. The difference in the  $\bar{D}_m = 0.383$  and  $\bar{D}_m = 0.481$  is principally due to the drag of the body. The body volume decreases while the thickness ratio increases with decreasing buoyancy ratio. For  $\bar{D}_m = .383$ , the value of the body drag at  $R = .2$  is about 30% of that at  $R = 1$ , while the value for  $\bar{D}_m = 0.481$  is about 40%.

This fact accounts for the low values of  $\Delta(W/D)$  for the  $\bar{D}_m = 0.481$  case.

The Reynolds number effect on  $\Delta(W/D)$  is examined in Figure 12. It is seen that for  $Re_v$  range of  $.6$  to  $12 \times 10^7$ , the difference is small for practical  $\bar{C}_w \geq 0.1$ .

It may be of interest now to show schematically some winged-torpedo configurations. In Figure 14, we have shown a diameter limited torpedo ( $D_m = 21"$ ), and an optimum fineness ratio (5.1) torpedo both of which weigh 3000 pounds and have a forward speed of 45 knots when they are neutrally buoyant, and when the buoyancy ratio = 0.8 and 0.4. It is seen that even at  $R = 0.4$ , the wings needed in both cases are quite small. The small size of the wing panels makes the problem of retracting them when launching considerably simpler.

#### B. Range.

The results of the range calculations are shown in Figures 15 through 23. The range factor,  $l_c S/\eta$ , in miles-lb fuel/horsepower-hour is shown as a function of buoyancy ratio with the ascending

angle as a parameter. In the first four Figures (15 through 18), the fuel weight is equal to one-half of the displacement, while in the last four Figures (19 through 22) the fuel weight is equal to one-half of the total weight. Only the results for four practical  $\bar{C}_w$ 's are presented; they are  $\bar{C}_w = .01, .0204, .04, .0625$ .

For a torpedo of specified weight, in the case in which the fuel weight equals one-half of the displacement, since the volume of the torpedo decreases as the buoyancy ratio decreases, the fuel weight decreases with the buoyancy ratio. Although it has been shown that the overall lift-drag ratio increases with decreasing buoyancy ratio, the decrease in the amount of fuel available more than compensates for the effect with a resulting range which is always less than that obtainable by the neutrally buoyant torpedo except in descending missions. As the  $\bar{C}_w$  increases, the advantages of winged-torpedo over those which are neutrally buoyant becomes more pronounced.

When the fuel weight is half of the total weight (Figures 19 through 22), the winged-torpedo has longer ranges than those with neutral buoyancy except in steep ascending missions. It is noted that the vertical scales in these Figures are different so as to exhibit the graphs more clearly.

#### CONCLUSIONS

1. The overall lift-drag ratios of torpedoes may be improved by the use of wings for small  $\bar{C}_w$ 's, say less than 0.3.

2. For  $\bar{C}_w \approx 0.01$  (3000 pound torpedo at 90 knots) the winged-torpedo of .2 buoyancy ratio may give a lift-drag ratio 2.5 - 3 times of that obtainable with a neutrally buoyant torpedo.

3. The effect of limiting the body diameter is always detrimental to the lift-drag ratio obtainable.

4. Due to the small contribution of the wing to the total drag, an increase in the strength factor  $s'\bar{z}$  does not materially affect the lift-drag ratio, although it permits wings of larger aspect ratio and span.

5. The Reynolds number has little effect on the improvements attainable on the lift-drag ratio.

6. Assuming that the fuel weight equals one-half of the displacement, the winged-torpedo has longer ranges than those with neutral buoyancy only in descending missions.

7. If the fuel weight equals one-half of the total weight, the winged-torpedo has longer ranges than those with neutral buoyancy except in steep ascending missions -  $\theta > 30^\circ$ .

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3. Lawrence, H.R., and Flax, A.H., Wing-Body Interference at Subsonic and Supersonic Speeds - Survey and New Developments, Journal of Aeronautical Sciences, volume 21, No. 5, May 1954.

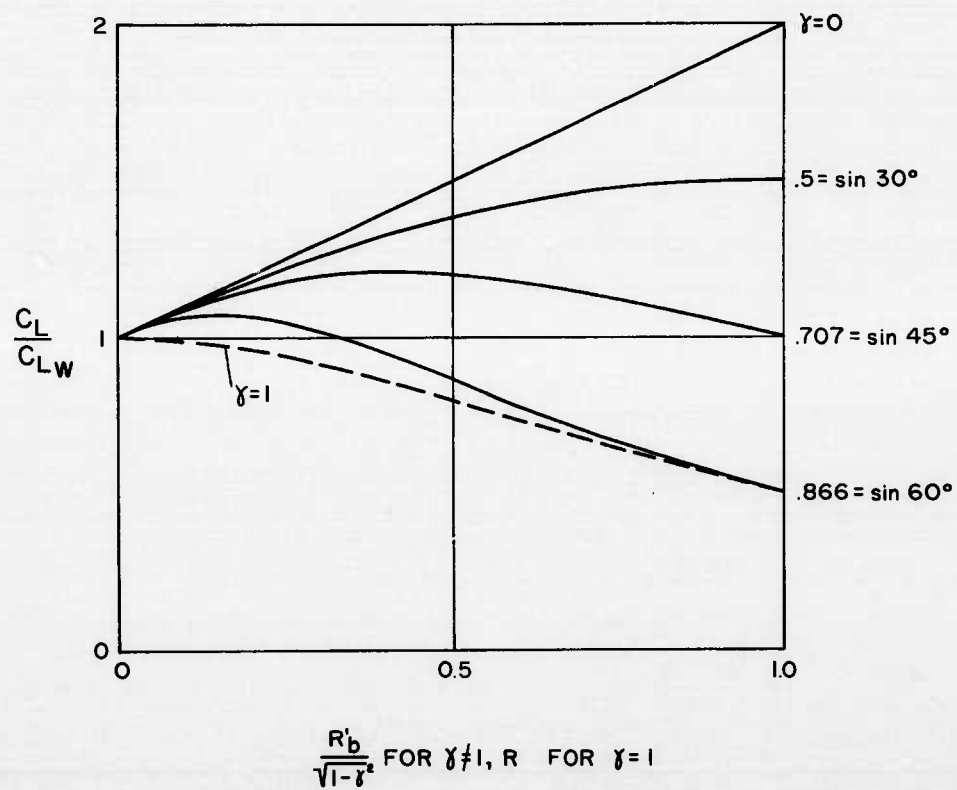
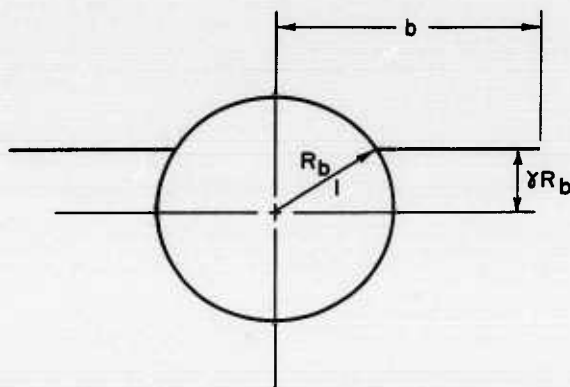


FIGURE 1-EFFECT OF WING-BODY INFLUENCE ON THE TOTAL LIFT

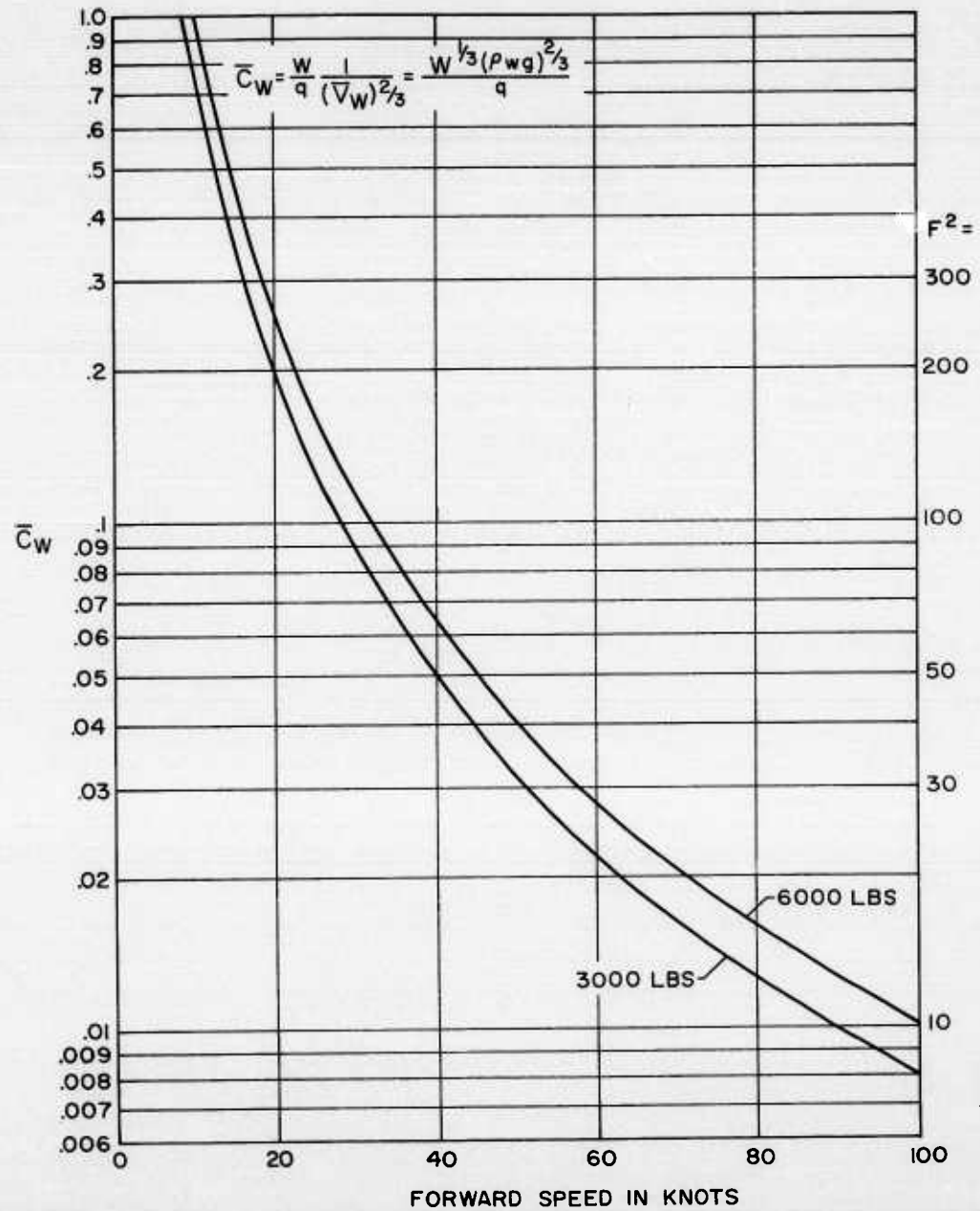


FIGURE 2-WEIGHT COEFFICIENT AS A FUNCTION OF FORWARD SPEED

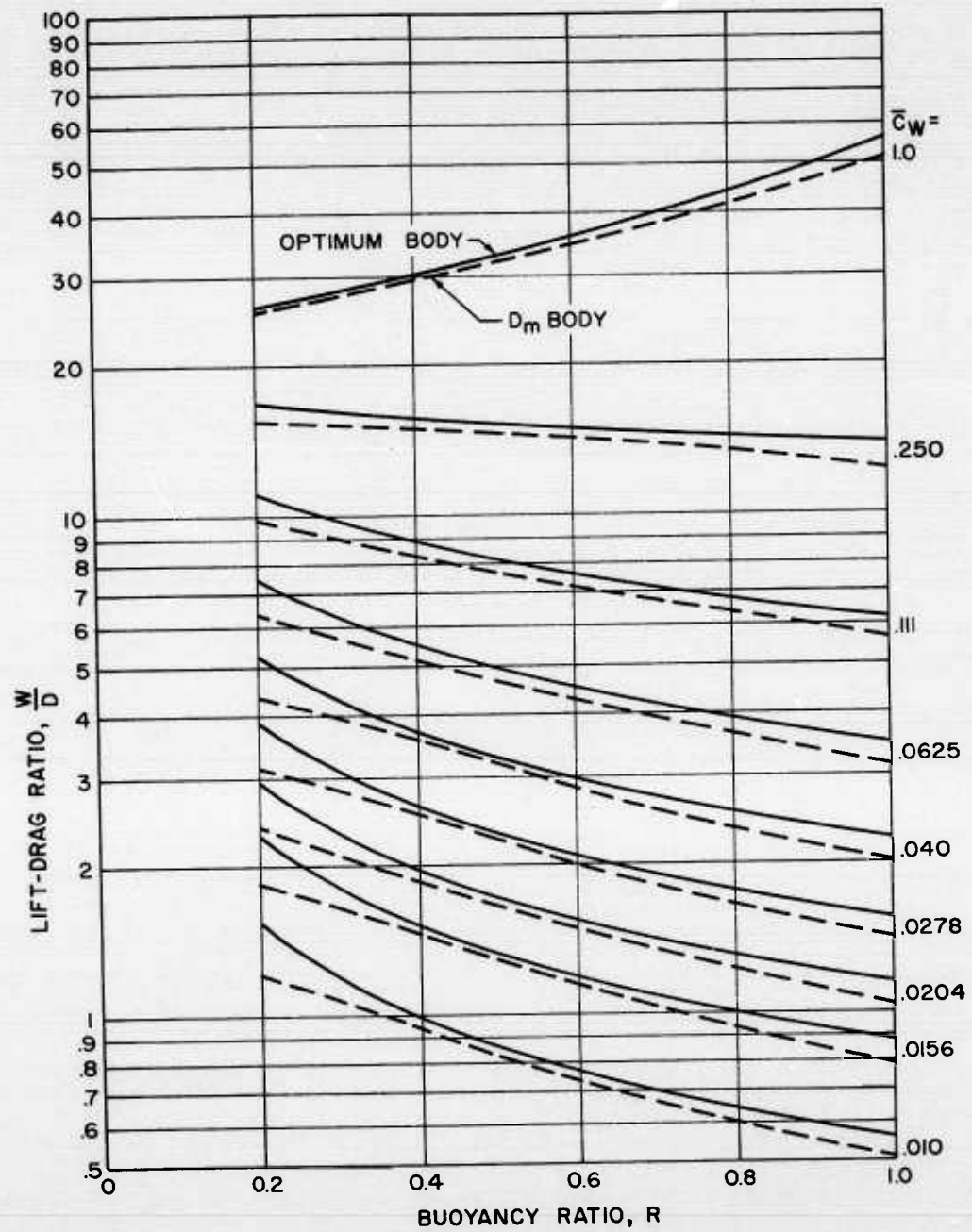


FIGURE 3-LIFT-DRAGE RATIO Vs. BUOYANCY RATIO  
 $Rev = 12 \times 10^8$ ,  $s\bar{Z} = 0.7$ ,  $\bar{D}_m = .481$



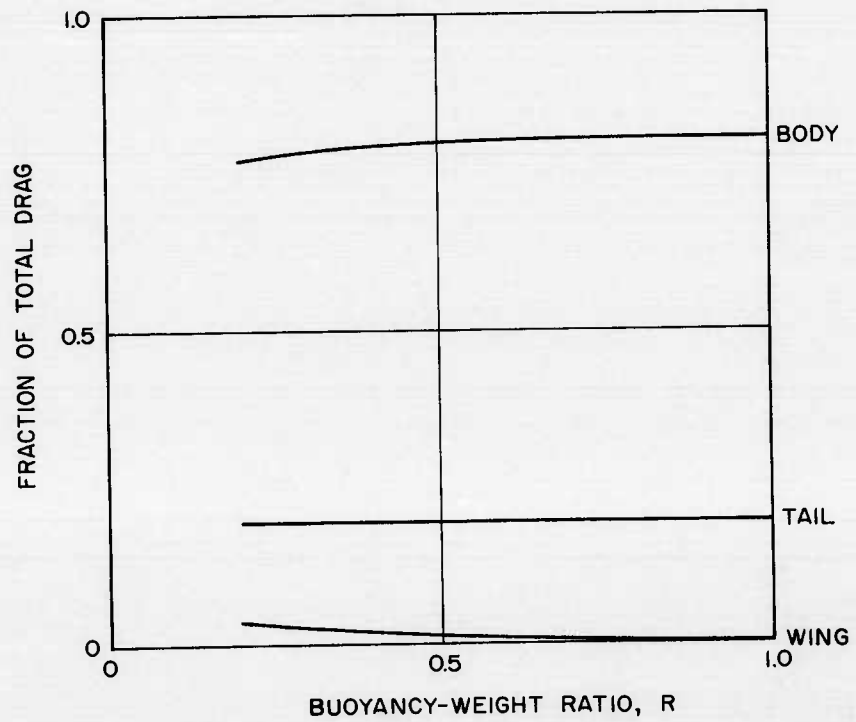


FIGURE 4-DRAG BREAK-DOWN FOR  $\bar{C}_w = 0.010$   
 $Re_v = 12 \times 10^7$ ,  $s'z = 0.7$  (OPTIMUM BODY)



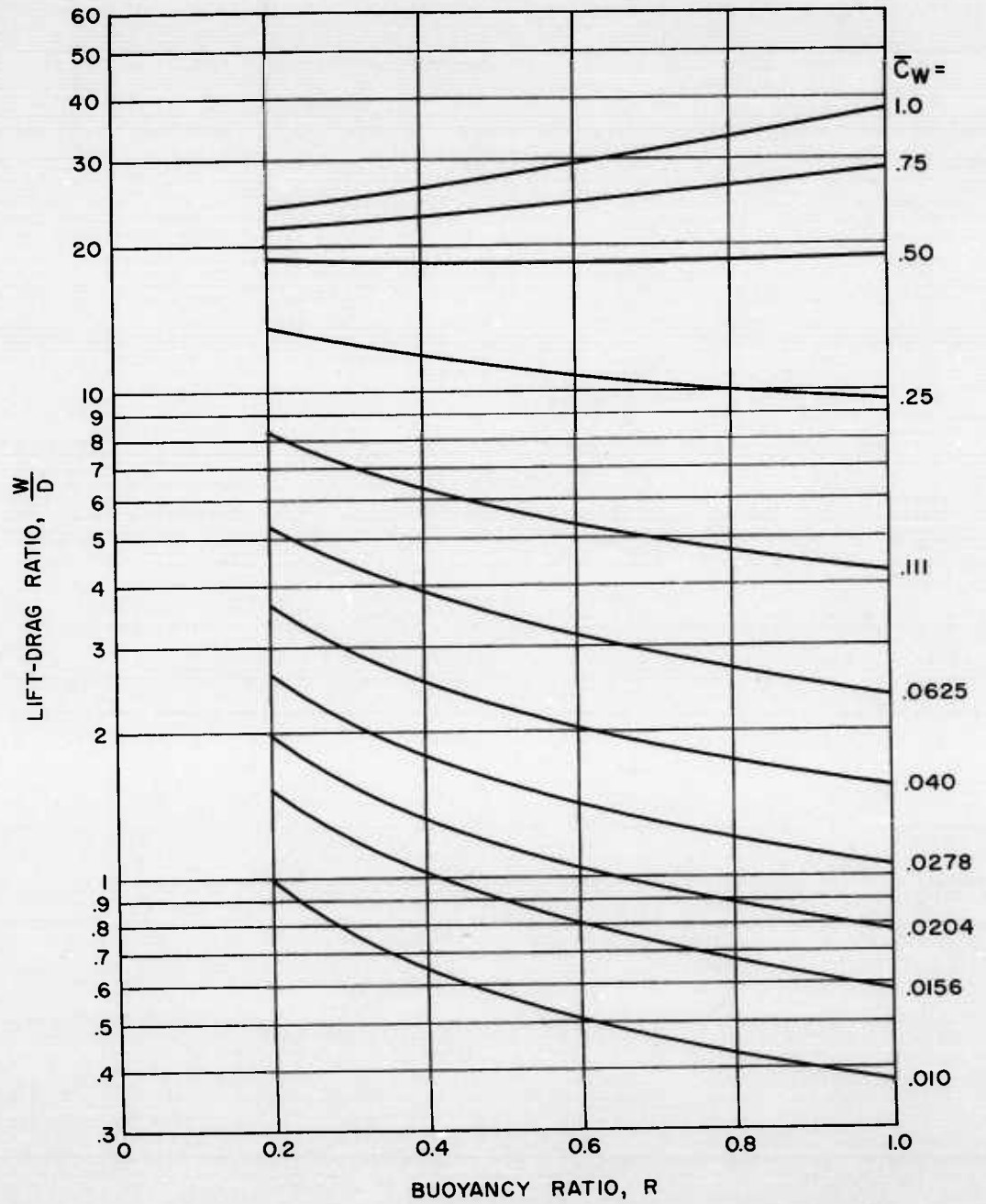


FIGURE 5-LIFT-DRAGE RATIO Vs BUOYANCY RATIO. (OPTIMUM BODY ONLY)  
 $Re_v = 6 \times 10^6$ ,  $s^*z = 0.7$

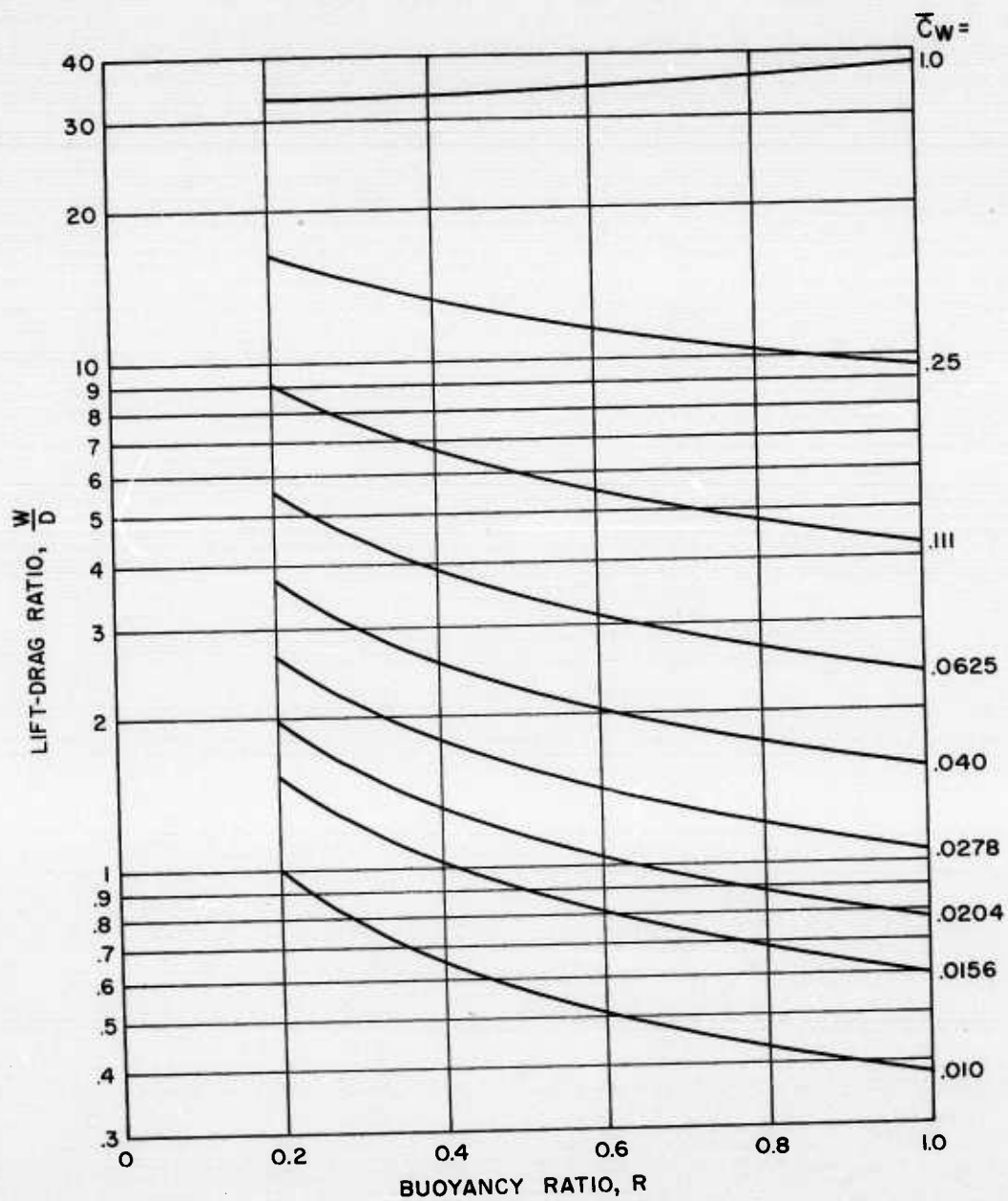


FIGURE 6-LIFT-DRAGE RATIO Vs BUOYANCY RATIO  
 Rev =  $6 \times 10^6$ ,  $s^2 Z = 33$

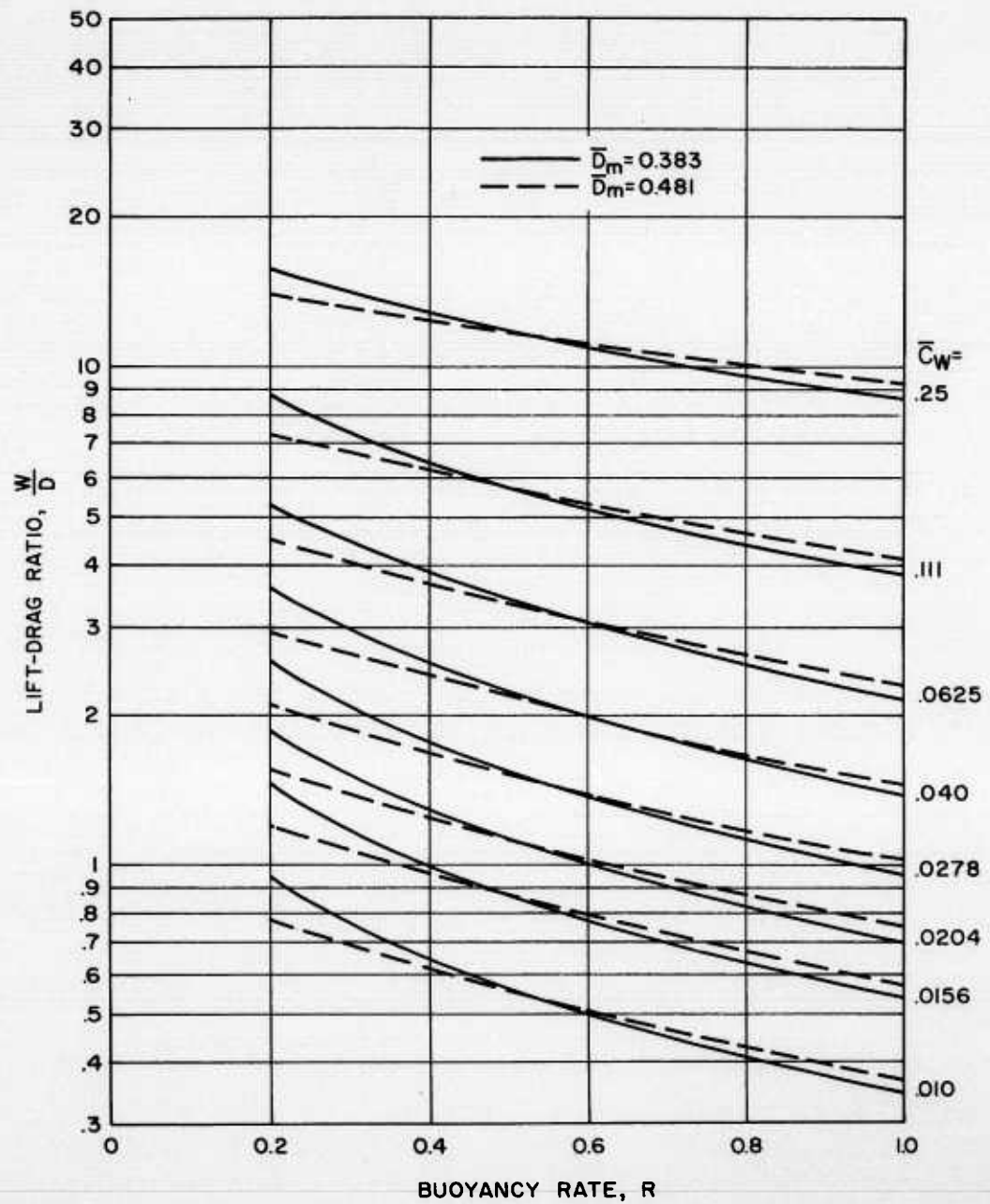


FIGURE 7-EFFECT OF  $\bar{D}_m$  ON LIFT-DRAGE RATIO  
 Rev =  $6 \times 10^6$ ,  $s^*Z = 33$

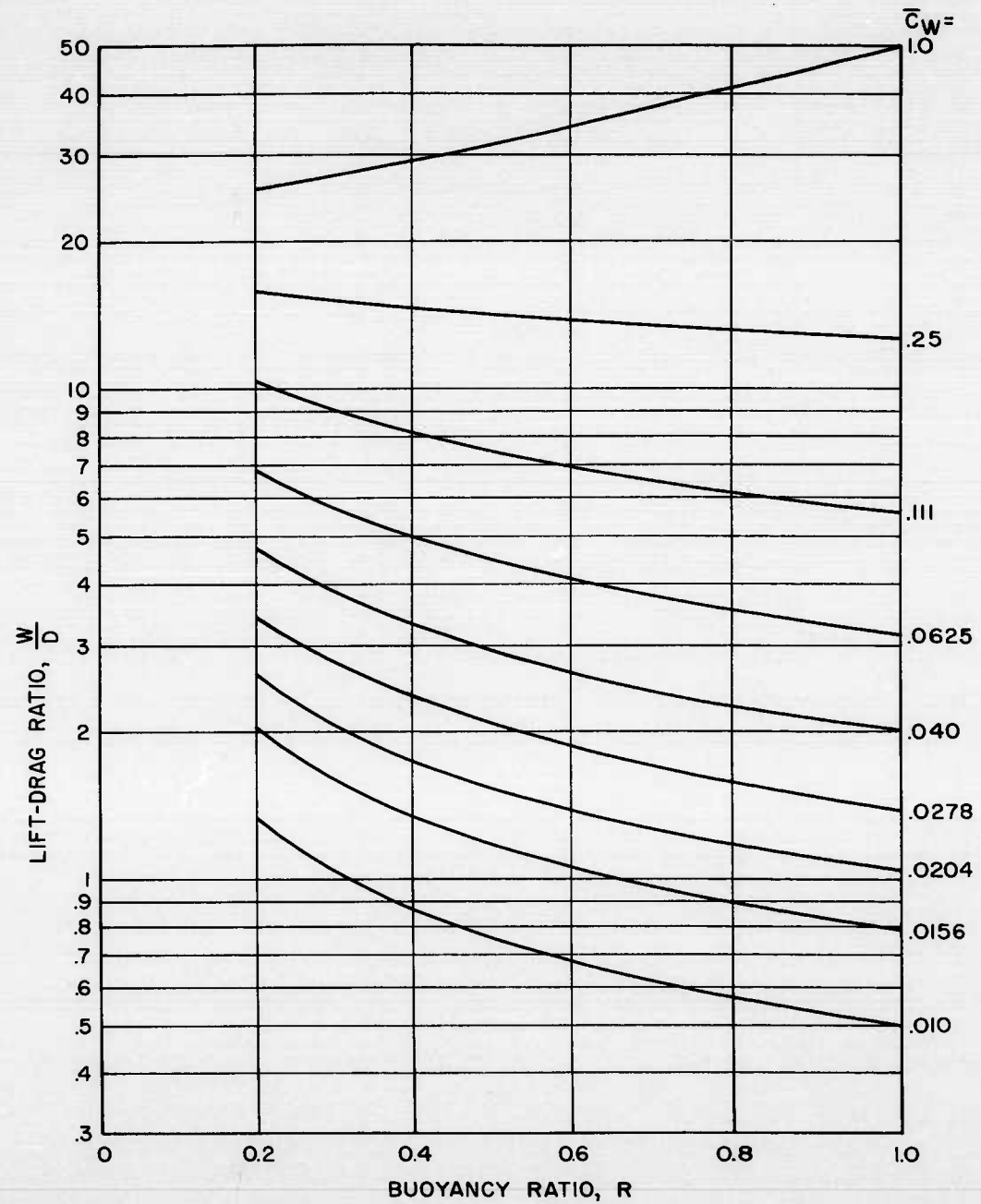


FIGURE 8-LIFT-DRAGE RATIO Vs BUOYANCY RATIO

Rev =  $4 \times 10^7$ ,  $s\bar{z} = .7$

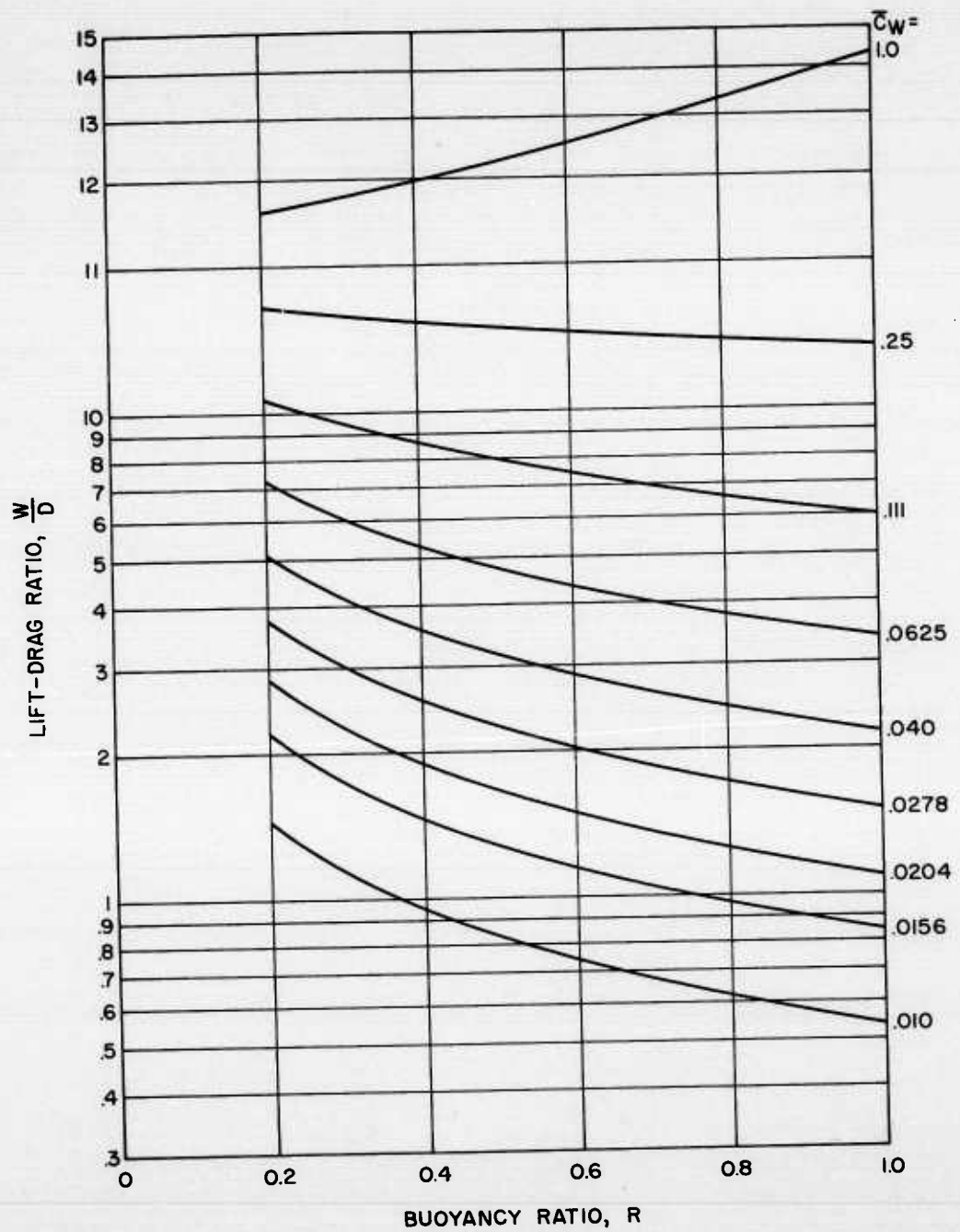


FIGURE 9-LIFT-DRAGE RATIO Vs BUOYANCY RATIO  
 Rev =  $8 \times 10^7$ ,  $s'Z = 0.7$

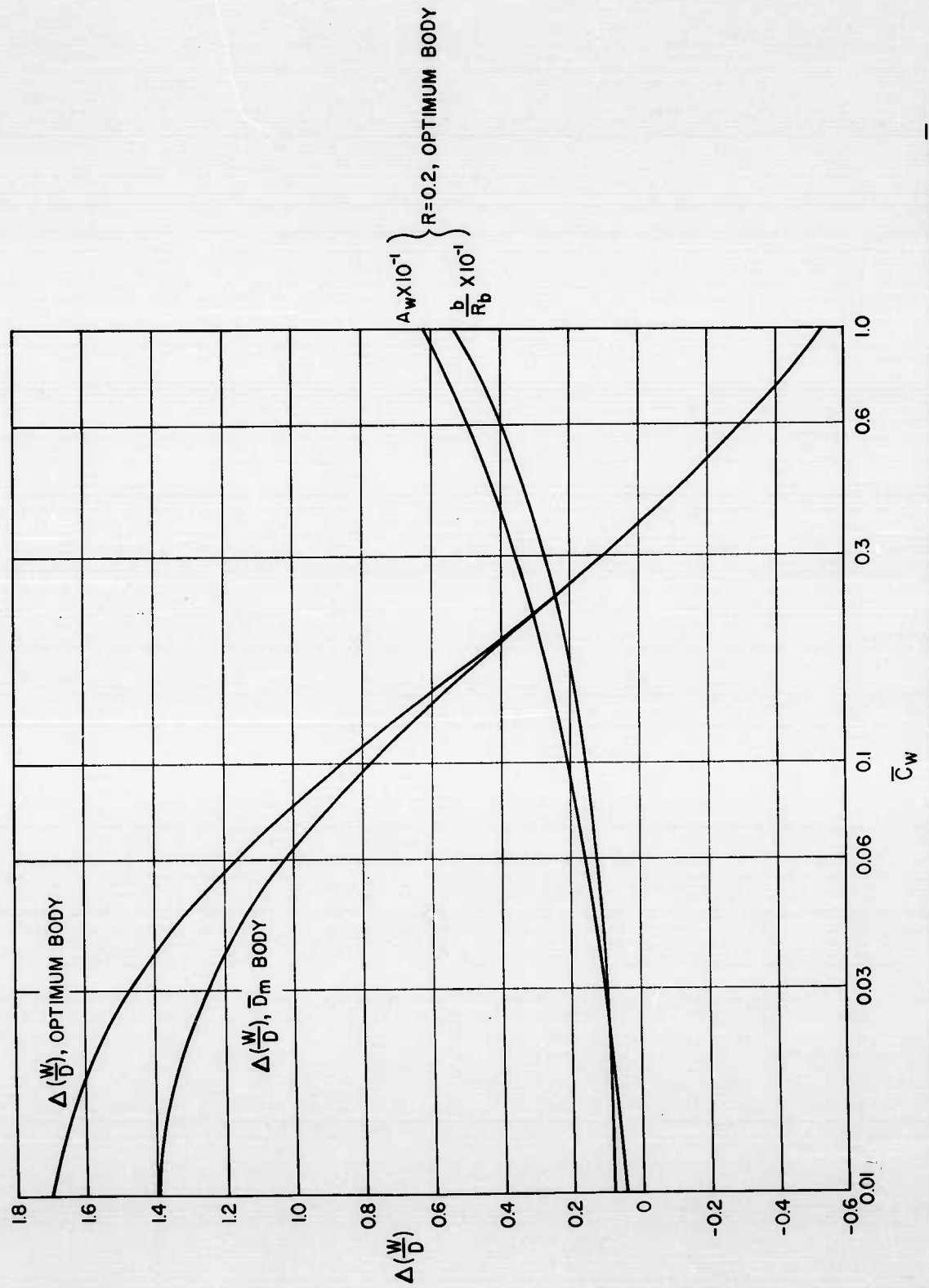


FIGURE 10-INCREASE IN LIFT-DRAG RATIO ATTAINABLE, WING ASPECT RATIO AND SPAN AS FUNCTIONS OF  $\bar{C}_w$   
 Rev =  $1.2 \times 10^6$ ,  $s\bar{z} = 0.7$ ,  $\bar{D}_m = 0.481$

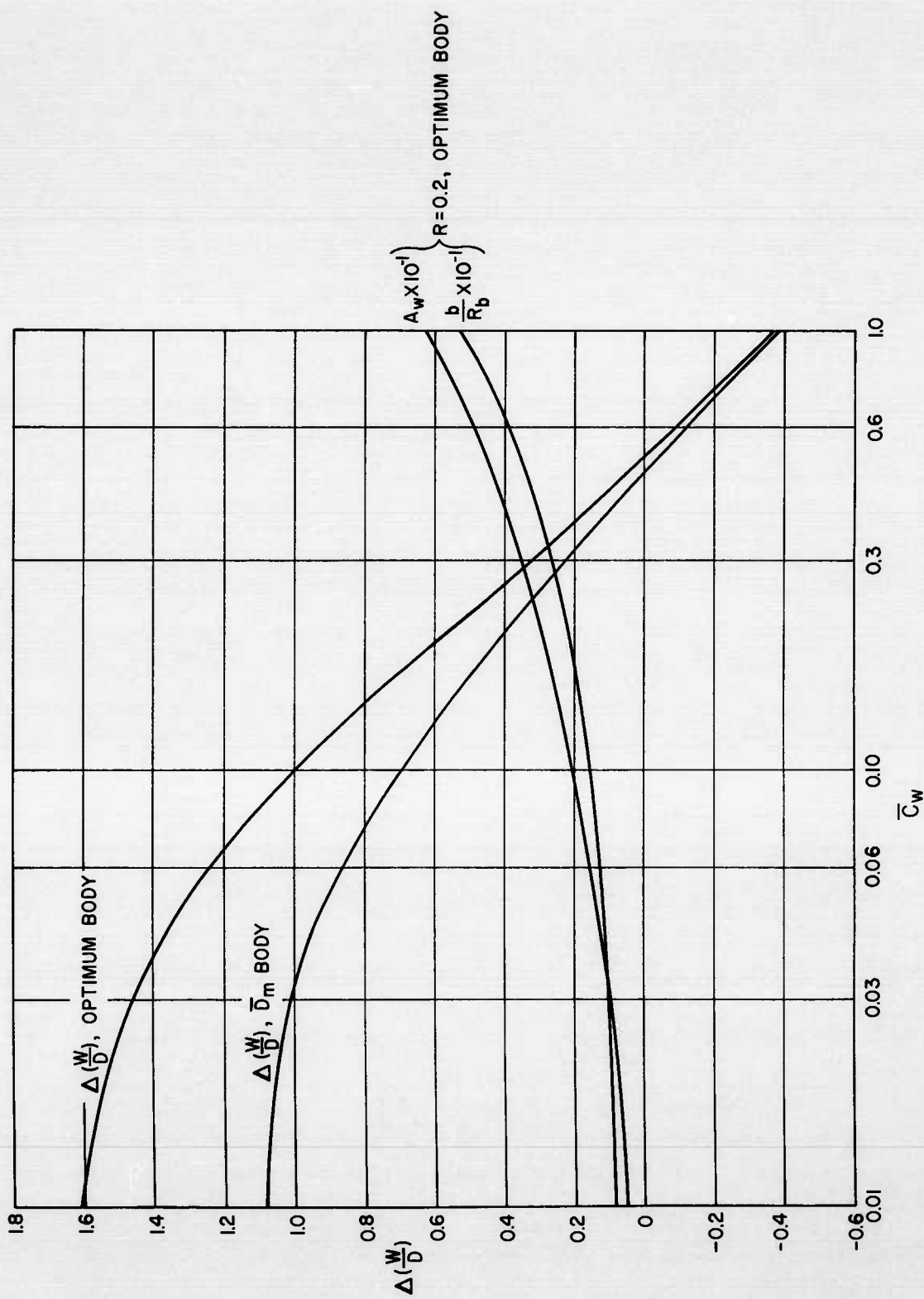


FIGURE II-INCREASE IN LIFT-DRAG RATIO ATTAINABLE, WING ASPECT RATIO AND SPAN AS FUNCTIONS OF  $\bar{C}_w$   
 Rev =  $6 \times 10^6$ ,  $s\bar{z} = 0.7$ ,  $\bar{D}_m = 0.481$



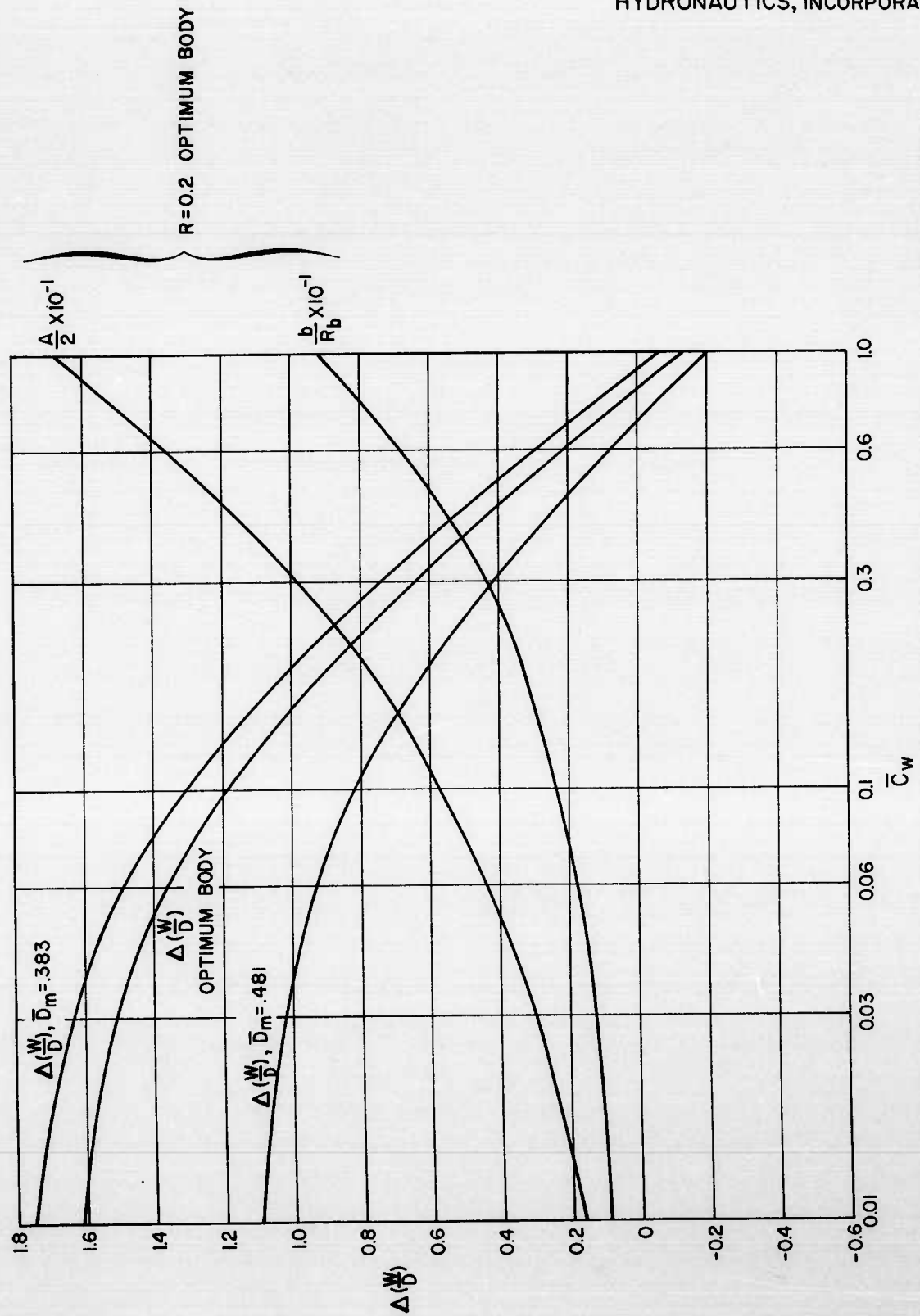


FIGURE 12-INCREASE IN LIFT-DRAG RATIO ATTAINABLE, WING ASPECT RATIO AND SPAN AS FUNCTIONS OF  $\bar{C}_w$   
 Rev = 6 X 10<sup>8</sup>,  $s\bar{Z} = 33$



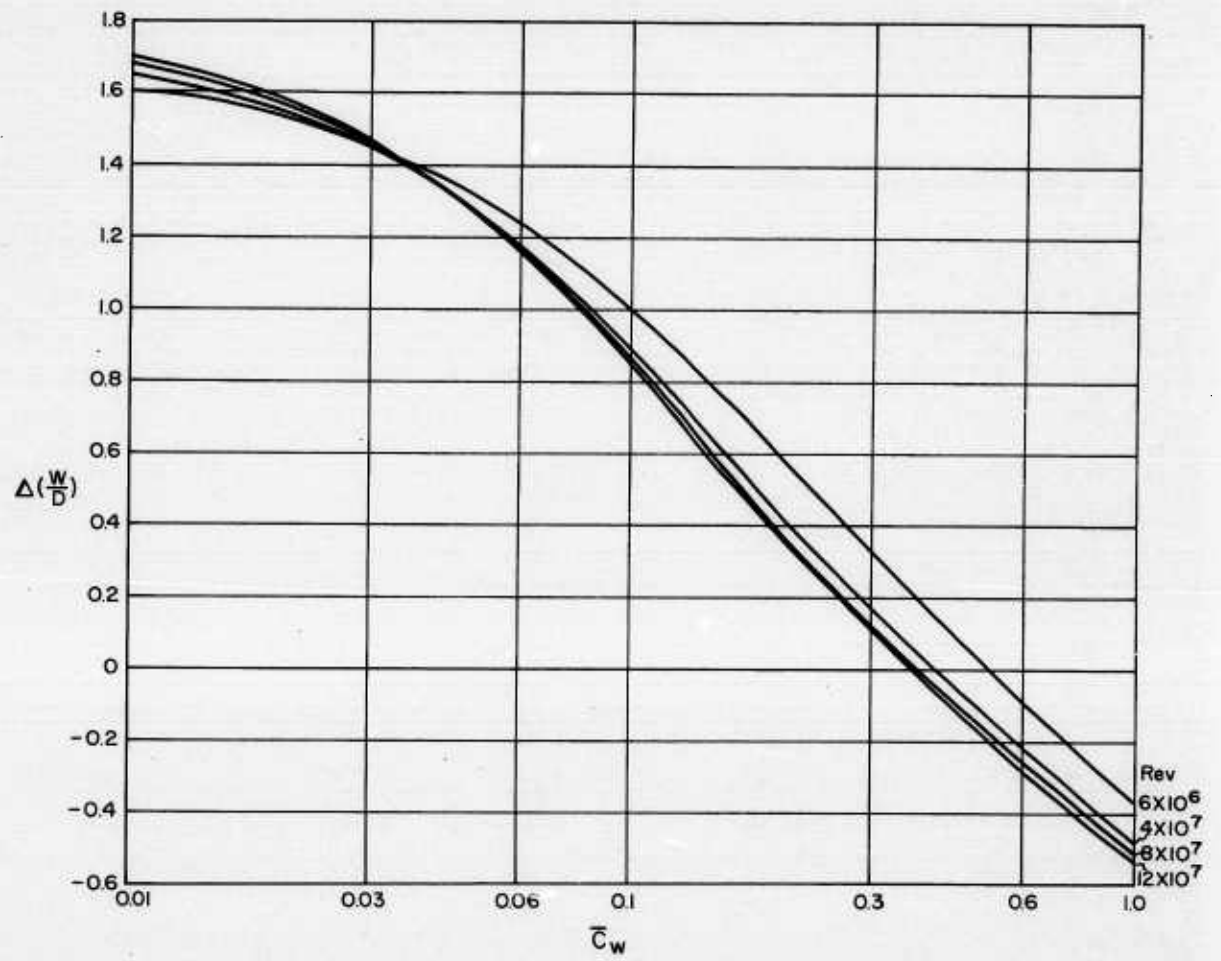


FIGURE 13-EFFECT OF Rev ON  $\Delta(\frac{W}{D})$

## 3000 POUND, 45 KNOT TORPEDOES

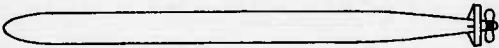

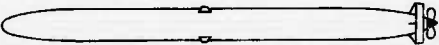

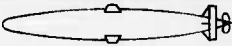
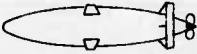
FIXED MAXIMUM DIAMETER OF 21"	OPTIMUM FINENESS RATIO OF 5
 <p data-bbox="784 641 992 717">R = 1.0 D = 1490 LBS.</p>	 <p data-bbox="1315 641 1523 717">R = 1.0 D = 1350 LBS.</p>
 <p data-bbox="784 1095 992 1171">R = .8 D = 1270 LBS.</p>	 <p data-bbox="1315 1095 1523 1171">R = .8 D = 1185 LBS.</p>
 <p data-bbox="784 1541 992 1616">R = .4 D = 850 LBS.</p>	 <p data-bbox="1315 1541 1523 1616">R = .4 D = 810 LBS.</p>

FIGURE 14

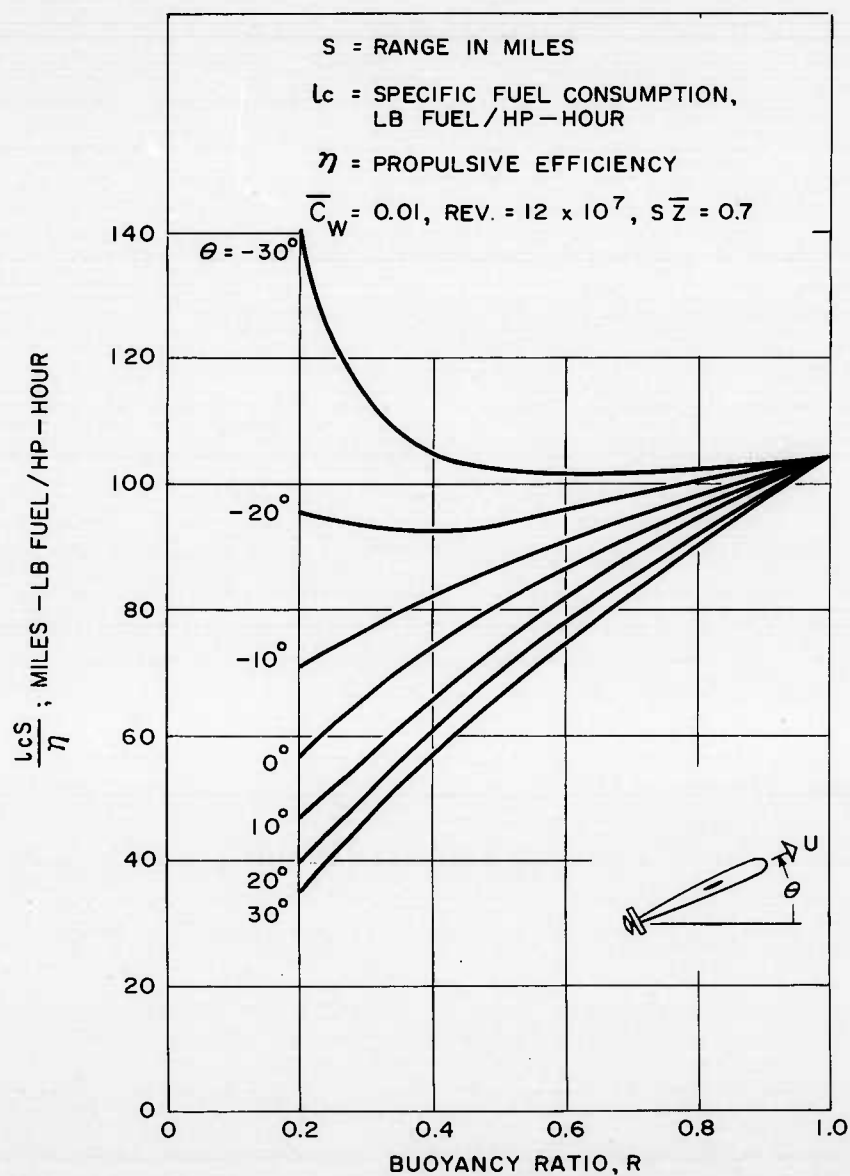


FIGURE 15 - THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
 (FUEL WEIGHT = .5 x DISPLACEMENT)

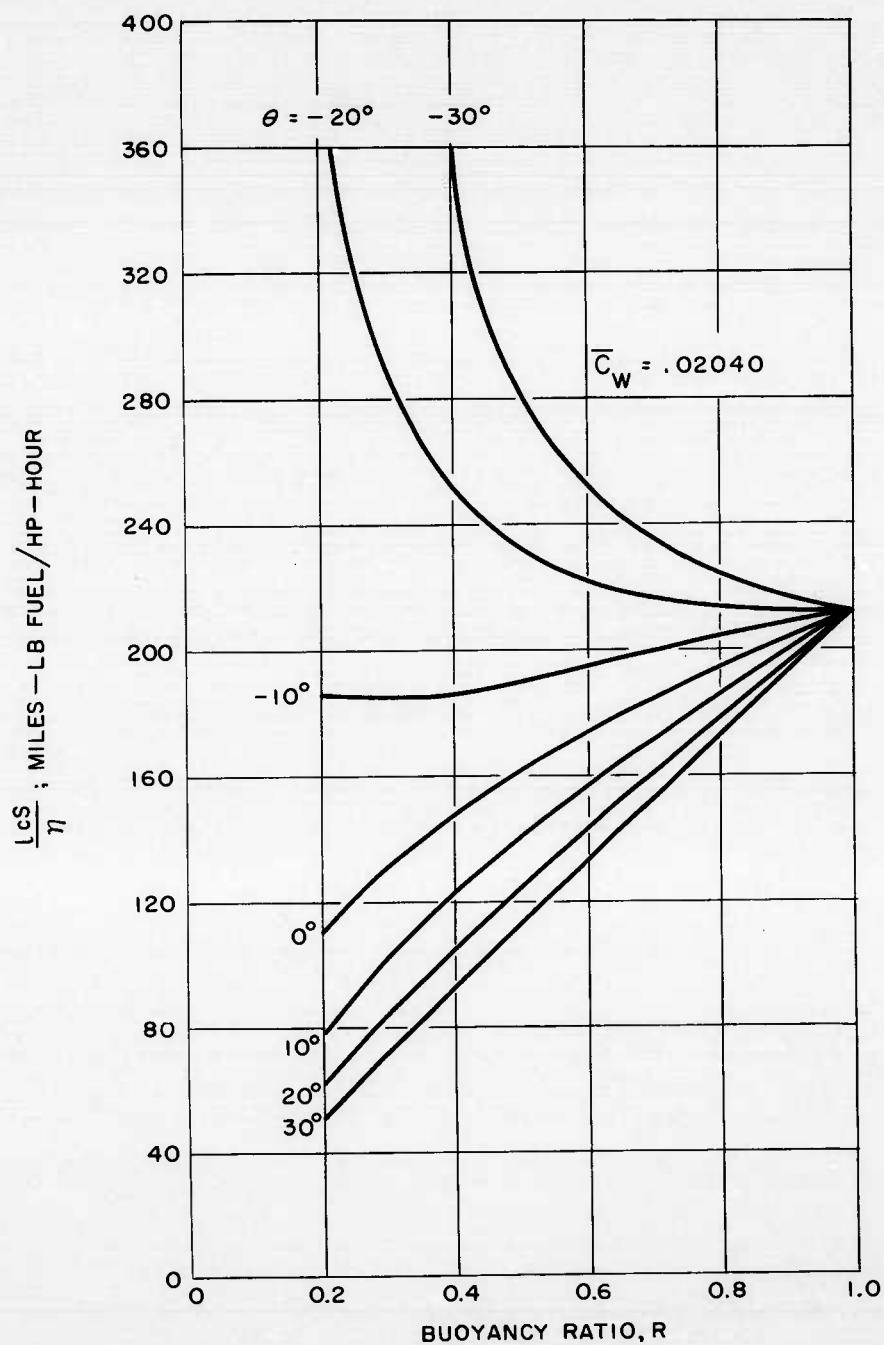


FIGURE 16— THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
( FUEL WEIGHT = .5 x DISPLACEMENT )

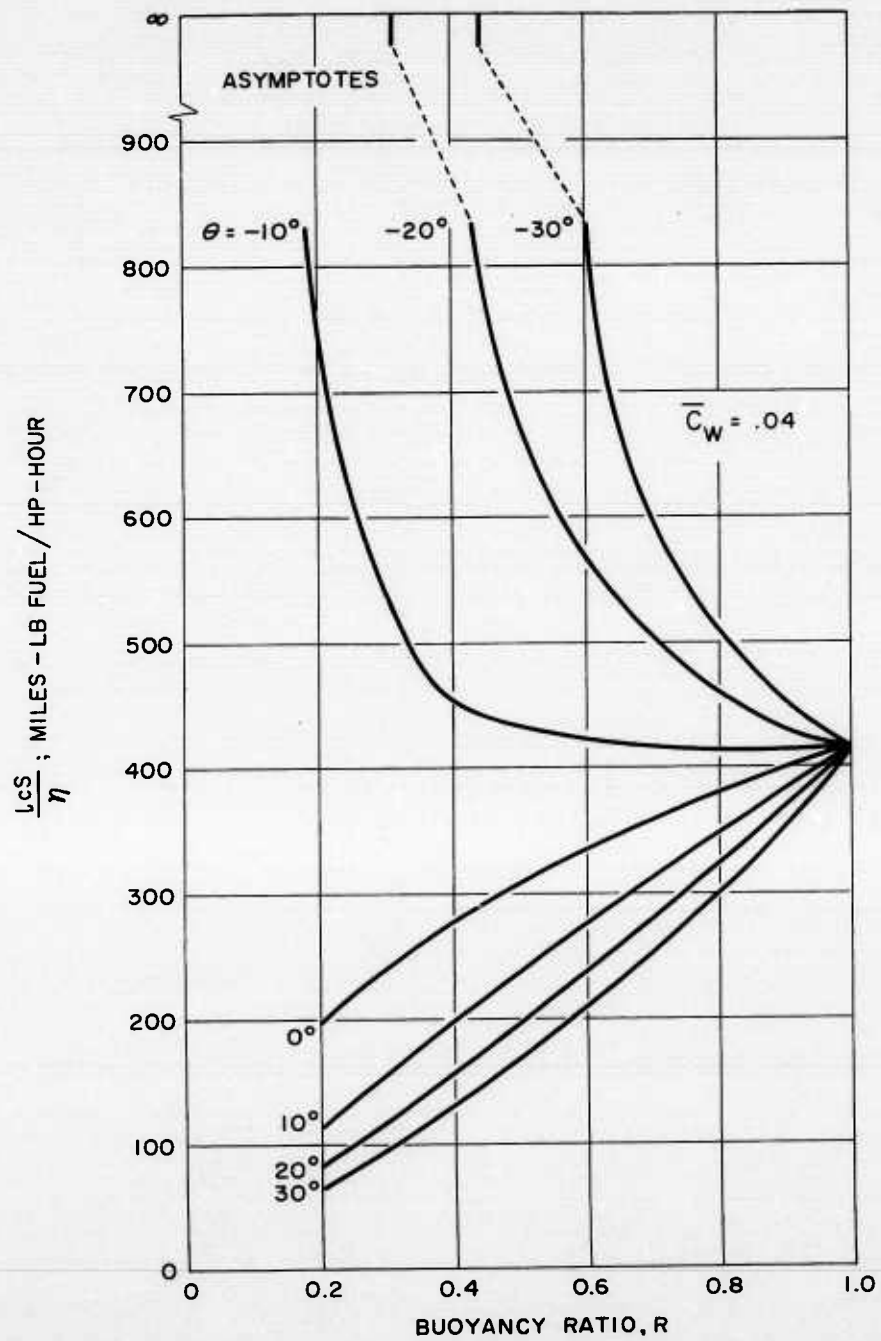


FIGURE 17- INFLUENCE OF BUOYANCY RATIO ON RANGE  
(FUEL WEIGHT = .5 x DISPLACEMENT)

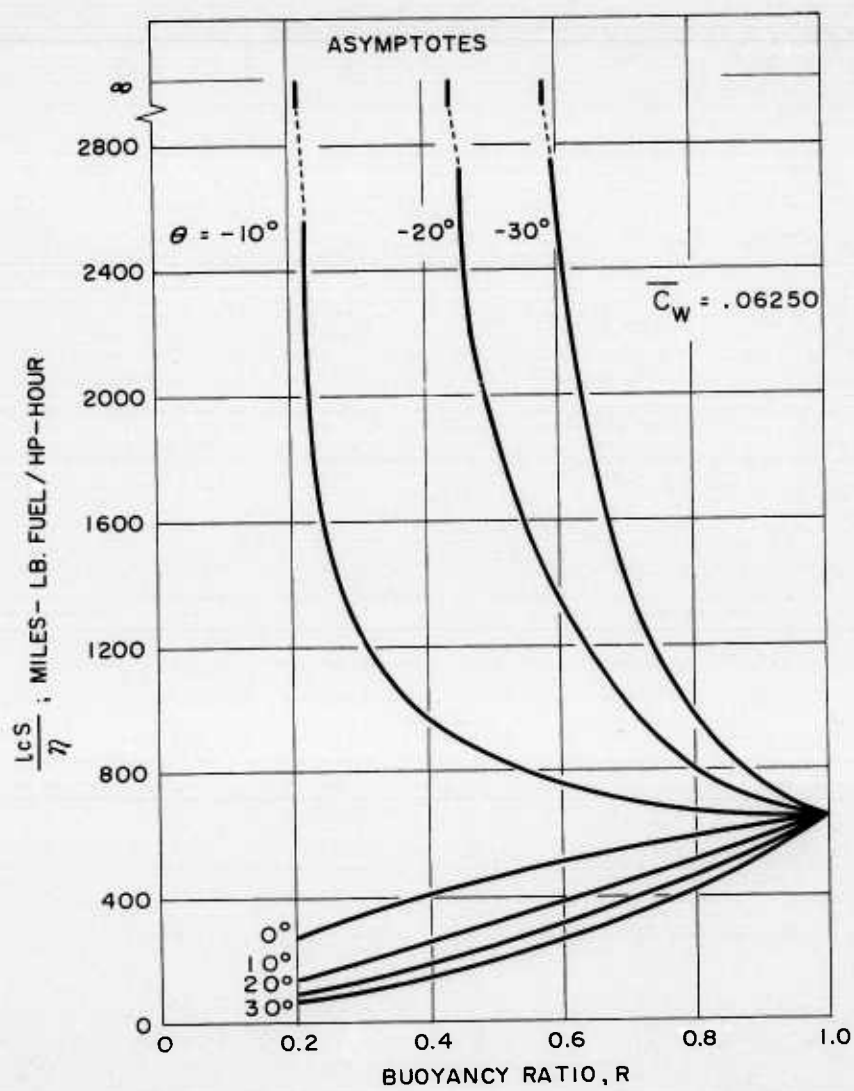


FIGURE 18— THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
( FUEL WEIGHT = .5 x DISPLACEMENT )

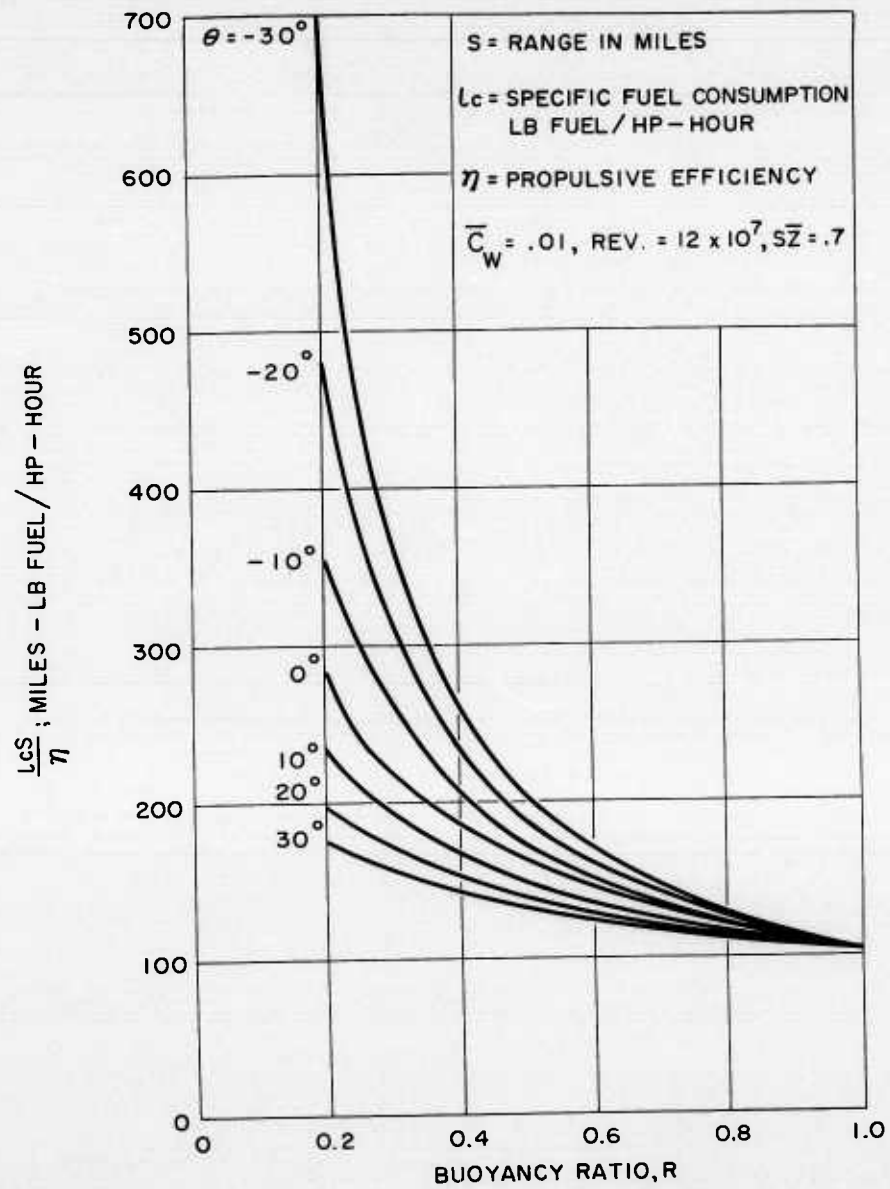


FIGURE 19— THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
 (FUEL WEIGHT = .5 W)

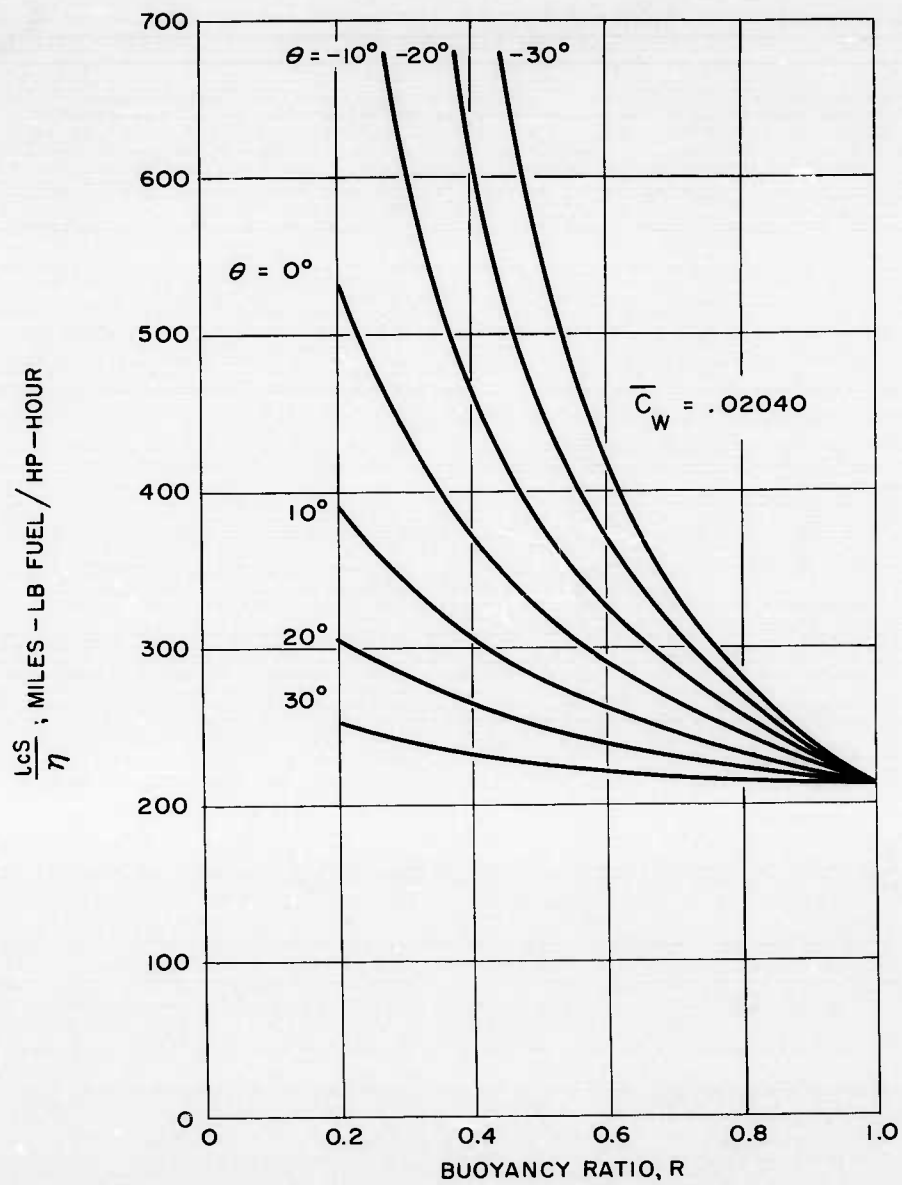


FIGURE 20- THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
( FUEL WEIGHT = .5W )



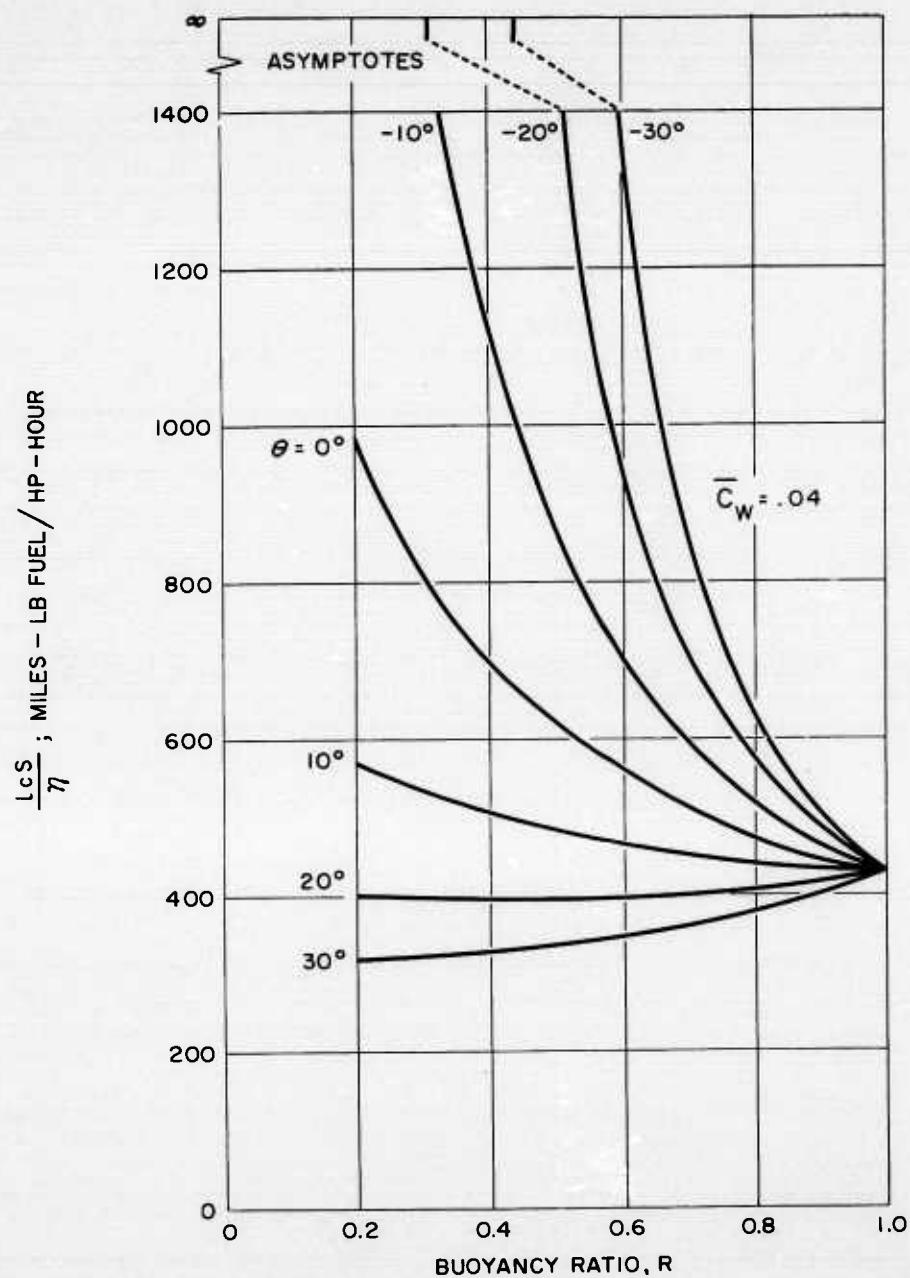


FIGURE 21- THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
(FUEL WEIGHT = .5W)

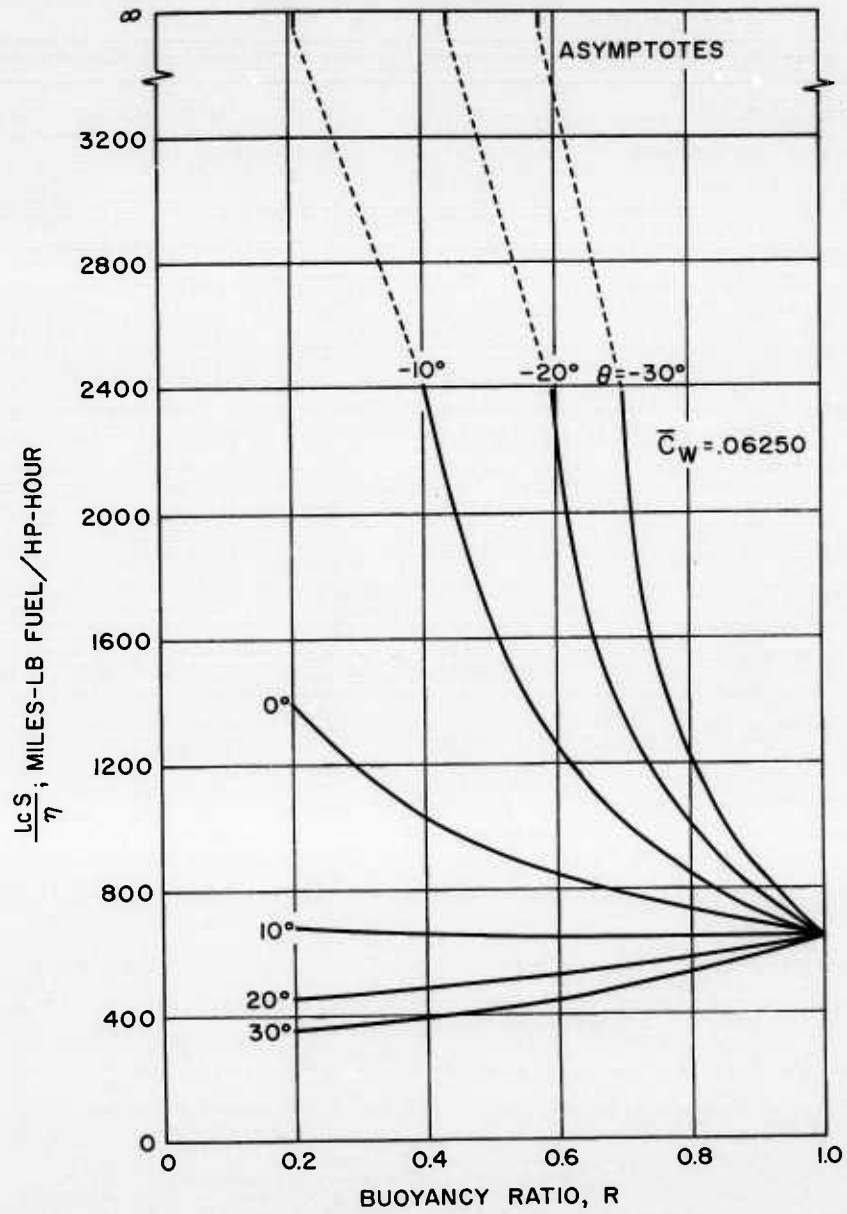


FIGURE 22-THE INFLUENCE OF BUOYANCY RATIO ON RANGE  
(FUEL WEIGHT = .5 W)

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