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A DIPOLE APPROXIMATION OF THE BACKSCATTERING FROM A CONDUCTOR IN A SEMI-INFINITE DISSIPATIVE MEDIUM WITH APPLICATION TO SUBMARINE DETECTION

Prepared by: Martin B. Kraichman

ABSTRACT: The backscattering of a uniform plane wave by a conductor in a semi-infinite dissipative medium is discussed. The conductor is assumed to act as both an electric and a magnetic dipole with moments which are obtained from the electric magnetic polarizabilities of the conductor, respectively. Using these induced moments, expressions are derived for the backscattered electric field at a point on the surface of the dissipative half-space directly above the dipoles. Both harmonic and transient excitation are considered. Numerical results are presented for the backscattered electric field from a perfectly conducting finite cylinder in sea water when the cylinder is excited by a single sferic pulse. The application of these results to the detection of submarines is discussed.

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The work reported herein was carried out in the Electromagnetics Division, Physics Research Department, under WepTask RU-222E000/ 212-1/RO04-03-01, ASW Oceanographic Research. The purpose of this task is to conduct an Oceanographic Research program that will provide an understanding of the effect and limitations imposed by the marine environment of the performance of weapons and weapon systems and the discovery of information which may lead to new concepts.

A portion of the work reported herein has been submitted for publication in the Journal of Research of the National Bureau of Standards, Sec. D.

This document is intended to serve as a progress report and is for information only.

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> R. E. ODENING Captain, USN Commander

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INTRODUCTION

1. The scattering of electromagnetic waves by conductors in an infinite homogeneous dissipative medium has been treated by various investigators in recent years. The classical problem of the scattering of a plane wave by a spherical object is reviewed by Stratton (1941). Wait (1951, 1960) has considered the response of a conducting sphere to a uniform time varying magnetic field and to the fields of electric and magnetic dipoles. The scattering by an infinite inhomogeneous conducting cylinder under the influence of a time varying magnetic field has been investigated by Negi (1962).

2. In many practical situations, it is of interest to consider the scattering of electromagnetic waves by conductors in a semi-infinite homogeneous dissipative medium. Recently, Galejs (1962), using a dipole approximation, treated the problem of the scattering from a conducting sphere in such a medium when the sphere is excited by a surface wave or by fields from vertical electric or horizontal magnetic dipoles in the lossless half-space. The analysis, however, is restricted to field points with horizontal ranges from the sphere which are much greater than a wavelength in the dissipative medium.

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3. The present paper considers the scattering of a uniform plane wave by a conductor of finite dimensions embedded in a semi-infinite dissipative medium. The frequency of excitation and the conductivity of the medium are such that the displacement current can be neglected. A dipole approximation, in which the electric and magnetic dipole moments of the conductor are obtained from the electric and magnetic polarizabilities, respectively, is used to evaluate the backscattered electric field in the interface directly above the conductor. The electric field step response is obtained from the response to harmonic excitation by transforming the Fourier integral into a convolution integral. Graphs of the electric field step responses are presented for the backscattering from both electric and magnetic dipoles. Numerical results are presented for the backscattered electric field from a perfectly conducting finite cylinder in sea water when the cylinder is excited by a single sferic pulse. The application of these results to the detection of submarines is discussed.

DIPOLE APPROXIMATION

4. A uniform plane wave is assumed to propagate vertically in a semi-infinite dissipative medium having a horizontal planar interface. The displacement current in the dissipative medium is considered to be negligible compared with the conduction current. The upper half-space is assumed to have the properties of free space. A perfectly conducting body (or one with negligible field penetration), which is embedded in the dissipative half-space, will have a surface current induced on it by the incident plane wave. The resulting scattered electromagnetic field may be approximated by that from a horizontal electric dipole and a horizontal magnetic dipole if the vertical dimension of the conductor is much smaller than a wavelength in the dissipative medium and if the dimensions of the conductor are small compared with the distance to a field point. In this approximation, the electric field of the plane wave induces a horizontal electric dipole moment in the conductor while the magnetic field induces a horizontal magnetic dipole moment. Both of these moments act as a source of electromagnetic field which can be determined from the propagation equations for horizontal electric and magnetic dipoles in a semi-infinite conducting medium.

Induced Electric Dipole Moment

5. Referring to the rectangular coordinates shown in Figure 1, the surface of a semi-infinite dissipative medium is located at z = o. A uniform plane wave, with harmonic variation $ej^{\omega t}$, propagates in the medium in the positive zdirection. The electric and magnetic fields are given by $E_x(z,\omega)$ and $H_y(z,\omega)$ respectively. If the incident electric field is substantially uniform over the height (z-dimension) of a perfect conductor at a depth z = d, the conductor will acquire an induced electric dipole moment, $P_x(d,\omega)$, which may be expressed as

$$P_{x}(d,\omega) = \left[\epsilon \left(i + \frac{\sigma}{j\omega \epsilon} \right) \right] \alpha_{e} E_{x}(d,\omega), \qquad (1)$$

where

- { = permittivity of the dissipative medium
- σ = conductivity of the dissipative medium
- a_e = electric polarizability of the perfectly conducting body

 $E_{M\omega}$ incident electric field at a depth d.

The quantity enclosed in brackets represents the complex permittivity of the dissipative medium. If the displacement current in the dissipative medium is neglected ($\sigma \gg \omega_{\ell}$), then (1) reduces to

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$$P_{\mathbf{x}}(d,\omega) = \frac{\sigma}{j\omega} \propto_{e} E_{\mathbf{x}}(d,\omega) . \qquad (2)$$

6. The current moment $P_{x}'(d,\omega)$ may be obtained by multiplying the right side of (2) by $j\omega$. Thus,

$$P'_{x}(a,\omega) = j\omega P_{x}(a,\omega) = \sigma \alpha_{e} E_{x}(a,\omega)$$
 (3)

and the induced electric current moment is seen to be in phase with the incident electric field. Multiple reflections between the conducting body and the surface of the half-space will be considered later in this section.

Induced Magnetic Dipole Moment

7. The permeability of the dissipative medium and the conducting body is assumed to be that of free space. If the incident magnetic field is substantially uniform over the height of the conductor at a depth d, then the conductor will acquire an induced magnetic dipole moment, $M_{y}(d,\omega)$, which is opposite in direction to the inducing magnetic field. The dipole moment is expressed as

$$M_{y}(d,\omega) = \alpha_{m} H_{y}(d,\omega) , \qquad (4)$$

where $\alpha_m = magnetic polarizability$

 $H_{v}(d,\omega)$ = incident magnetic field at depth d.

Since $M_y(d,\omega)$ is opposite in direction to $H_y(d,\omega)$, the polarizability α_m will be negative. The magnetic current moment, $M_y(d,\omega)$, is defined as

$$M'_{y}(d,\omega) = j\omega\mu_{o}M_{y}(d,\omega) = j\omega\mu_{o}\alpha_{m}H_{y}(d,\omega), \qquad (5)$$

where μ_0 = permeability of free space.

8. The polarizabilities, α_e and α_m , are functions of the volume and shape of the conductor and the relative orientation of the conductor with the inducing field. The expressions for the current moments given by (3) and (5) agree with those given by Galejs (1962) for a conducting sphere of volume v if the well known values $\alpha_e = 3v$ and $\alpha_m = -3/2v$ are used for the polarizabilities.

Perturbing Effect of Reflections

9. The incident plane wave at the conductor will be perturbed by reflections of the backscattered electric and magnetic fields from the surface of the dissipative half-space. The perturbing effect of a single reflection on the electric and magnetic current moments of spheres and certain cylinders will be approximated and shown to be small.

10. After a single reflection from the surface of the dissipative medium, the reflected electric and magnetic fields, $E_{xr}(d,\omega)$ and $H_{yr}(d,\omega)$, respectively, induce electric and magnetic current moments in the conductor. The moments are given by

$$P_{xr}(d,\omega) = \sigma \alpha_e E_{xr}(d,\omega)$$
 (6)

and

$$M'_{yr}(d,\omega) = j \, \omega \, \mu_0 \, \alpha_m \, H_{yr}(d,\omega) \, . \tag{7}$$

The reflected electric and magnetic fields in (6) and (7) may be expressed in terms of the current moments $P_{xi}(d,\omega)$ and $M_{yi}(d,\omega)$ which are induced in the conductor by the incident plane wave. Because of the large impedance mismatch at the surface of the dissipative medium, it is assumed that the backscattered electric field is totally reflected in opposite phase. In returning to the conductor at a depth d, the reflected wave will have experienced a spherical spreading over the distance 2d. Using these approximations, the reflected fields may be obtained from the well known propagation equations for the electromagnetic fields from electric and magnetic dipoles in an infinite dissipative medium. The electric dipole contributes to both the reflected electric and magnetic fields. Similarly, the magnetic dipole also contributes to both fields. The reflected fields are therefore written

$$E_{xr}(d,\omega) = -\frac{P_{xi}(d,\omega)}{32\pi\sigma d^{3}} (1+2Yd+4Y^{2}d^{2})e^{-2Yd}$$

$$-\frac{M'_{yi}(d,w)}{16\pi d^{2}}(1+2xd)e^{-2xd}$$
(8)

and

.

$$H_{yr}(d, w) = -\frac{P'_{xi}(d, w)}{16\pi d^{2}} (1 + 2rd) e^{-2rd} + \frac{M'_{yi}(d, w)}{32\pi j w \mu_{0} d^{3}} (1 + 2rd + 4r^{2}d^{2}) e^{-2rd}, \quad (9)$$

where $\gamma = (j \omega \mu_{e} \sigma)^{\frac{1}{2}}$.

For |7d| >> 1, the exponential attenuation factors in (8) and (9) will ensure the smallness of the perturbing electric and magnetic fields. For $|7d| \ll 1$, the perturbing moments in (6) and (7) may be expressed as

$$\frac{P_{xr}(d,\omega)}{P_{xi}(d,\omega)} \approx -\frac{1}{32\pi d^3} \left(\alpha_e + 2 \gamma d\alpha_m\right) \qquad (10)$$

and

$$\frac{M'_{yr}(d,\omega)}{M'_{yi}(d,\omega)} \approx \frac{1}{32\pi d^3} \left(\alpha_m - 2 \tau d \alpha_e \right), \qquad (11)$$

where use is made of the expressions in (8) and (9) and of the definitions in (3) and (5).

11. The ratios in (10) and (11) may readily by shown to be small for spherical conductors and for cylinders which are neither extremely needle hor extremely disc shaped. For a sphere of volume v and radius a, $\alpha_{e} = 3v = 4\pi a^{3}$ and $\alpha_{m} = -\frac{1}{2}\alpha_{e}$. The ratios in (10) and (11) then become

$$\frac{P_{xr}(d,\omega)}{P_{xi}(d,\omega)} \approx -\frac{1}{q} \frac{a^3}{d^3} (1-rd) \qquad (12)$$

and

$$\frac{M'_{yr}(d,\omega)}{M'_{yi}(d,\omega)} \approx -\frac{1}{16} \frac{a^3}{d^3} \left(1+4\gamma d\right). \qquad (13)$$

Since it has been assumed that $a \ll d$ and that $|\gamma d| \ll 1$, it follows that the perturbations in the electric and magnetic moments are small for a single reflection.

12. The electric and magnetic polarizabilities of a right circular cylinder are given in Table 1. The subscript l denotes longitudinal excitation, i.e., with the particular field vector of interest along the axis of the cylinder. The subscript t denotes an excitation which is transverse to the axis of the cylinder. The values in Table 1 are obtained from Taylor (1960a, 1960b). The entries for a/b = 0.1 represent values which have been extrapolated from the results in the above references. In the dipole approximation, the dimensions of the cylinder must be much smaller than the depth at which the cylinder is embedded, so that $v \ll d^3$. It is therefore

evident from (10), (11), and Table 1, that the moments due to the singly reflected electromagnetic field are small compared with the moments due to the incident plane wave for cylinders which are neither extremely needle nor extremely disc shaped.

13. Higher order perturbations, resulting from multiple reflections, will be even smaller than the perturbation due to a single reflection.

BACKSCATTERED ELECTRIC FIELD AT THE SURFACE

14. In this section, expressions will be derived for the backscattered electric field at the surface of the dissipative half-space for a field point directly above the conductor. The electric field contributions from the induced electric and magnetic dipoles will be treated separately and both harmonic and transient excitation will be considered.

Electric Field From an Induced Electric Dipole

Harmonic Excitation

15. Von Aulock (1952) has derived expressions for the electric field in a semi-infinite dissipative medium in a region directly above an embedded horizontal electric dipole. As is shown in Figure 1, the dipole is situated at the point (0,0,d) and is directed along the X-axis. The dipole is excited at an angular frequency ω . At the coordinate origin in the surface, the electric field E_x^{se} (0, ω), is directed along the X-axis and is written

$$E_{x}^{se}(o,\omega) = \frac{P_{x}(a,\omega)}{4\pi\sigma d^{3}} \left[Y^{2}d^{*}K_{x}(Yd) - 2e^{-Yd}(2+2Yd+Y^{2}d^{*}) \right], \qquad (14)$$

where $\gamma = (j \omega \mu_{\sigma} \sigma)^{\frac{1}{2}}$ and $K_2(\gamma d)$ is the modified Bessel function of the second kind. Using (3) and the plane wave relationship

$$E_{x}(\boldsymbol{a},\boldsymbol{\omega}) = \frac{\gamma}{\sigma} H_{y}(\boldsymbol{o},\boldsymbol{\omega}) e^{-\gamma \boldsymbol{a}}$$
(15)

which relates the electric field incident at the conductor to the magnetic field at the surface of the half-space, (14) may be written

$$E_{x}^{se}(0,\omega) = \frac{\alpha_{e}}{4\pi d^{3}} \frac{Y}{\sigma} H_{y}(0,\omega) e^{-Yd} \left[Y^{2}d^{3}K_{1}(Yd) - 2e^{-Yd} (2 + 2Yd + T^{2}d^{2}) \right].$$
 (16)

Transient Excitation

16. The backscattered electric field in the time domain , E_x^{se} (o,t), may be expressed as a Fourier integral and written

$$\overline{E}_{x}^{se}(o,t) = \frac{1}{2\pi t} \int_{-\infty}^{\infty} \overline{E}_{x}^{se}(o,w) e^{jwt} dw . \qquad (17)$$

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The Fourier integral may then be transformed into a convolution integral involving the backscattered electric field response at the surface of the half-space, directly above the dipole, when a unit step of magnetic field is applied at the surface in the y direction. The steps of the transformation are given in Appendix A. Equation (17) then reads

$$\bar{E}_{x}^{se}(o,t) = \int A_{x}^{e}(o,t-\lambda) H_{y}'(o,\lambda) d\lambda , \qquad (18)$$

where $A_X^e(o,t)$ = backscattered electric field step response at the surface from an induced electric dipole,

H' (o,t) = time derivative of the transient magnetic field applied at the surface. *(See insertion, page 8a) The step response may explicitly be written

$$A_{x}^{e}(o,t) = -\frac{\alpha_{e}}{4\pi\sigma d^{4}} \left[I(\beta) + \frac{2}{(\pi\beta)^{k_{2}}} \left(2 + \frac{3}{2\beta} + \frac{1}{\beta^{3}} \right) e^{-\frac{1}{\beta}} \right], \quad (19)$$

where $\beta = \frac{t}{\mu_0 \sigma d^2}$ and

$$I(\beta) = \int v^{2} \left[\cos v N_{2}(v) + \sin v J_{2}(v) \right] e^{\beta v^{2}} dv. \qquad (20)$$

*Since (17) includes all frequencies, the condition that the displacement current be negligible compared with the conduction current will no longer hold for the higher frequencies. However, in a medium with appreciable conductivity, the electromagnetic fields at these high frequencies will be so severely attenuated that their effect will be negligible at all but the most shallow depths. Since the approximation in (17) to the true $E_X^{se}(o,\omega)$ is also negligible at high frequencies, the results obtained by using (18) will be of practical value.

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The above expression for $I(\beta)$ is convenient for large values of β . With further manipulation, it can be shown that $I(\beta)$ may also be written

$$I(\beta) = -\frac{1}{\pi^{N}} \int \left[\frac{4v^{3}}{\beta^{N}} + \frac{3}{\beta^{N}v} + \frac{3}{\beta^{N}v^{3}} \right] (v^{2} - v)^{N} e^{-\frac{v^{2}}{\beta^{N}}} dv. \qquad (21)$$

This form is convenient for small values of s. The leading terms of an asymptotic expansion for small s obtainable from (21) are

$$I(\beta) = -\frac{e^{-\frac{1}{6}}}{2^{\frac{1}{2}}\beta^{\frac{1}{2}}} (1 + 1.68750\beta + 0.95508\beta^{2} + 0.16296\beta^{3} - 2.24885\beta^{4} + ...).$$
(22)

From the exponential factor $e^{-\frac{1}{p}}$ in (19) and 22), it is evident that the backscattered electric field, E_X^{ee} (o,t), is quite small for t $\ll d_1^2 \mu_0 \sigma$. For large β , it can be shown that A_X^{ee} (o,t) falls off as $t^{-\frac{1}{2}}$. A graph of the dimensionless quantity $-A_X^{ee}$ (o,t), $\frac{4\pi \sigma d^4}{\alpha e}$ is shown in Figure 2. The integrals were evaluated on the IBM 7090 using Gaussian integration.

Electric Field From an Induced Magnetic Dipole

Harmonic Excitation

17. Von Aulock (1952) has also derived expressions for the electric field directly above a horizontal magnetic dipole in a semi-infinite dissipative medium. As is shown in Figure 1, the magnetic dipole is situated at the point (0,0,d) and is directed along the Y-axis. The dipole is excited at angular frequency ω . At the coordinate origin in the surface, the electric field, E_X^{SM} (0, ω) is directed along the X-axis and is written

$$E_{x}^{sm}(o,\omega) = \frac{M_{u}(d,\omega)}{4\pi d^{2}} \left[r d K_{1}(rd) + 3K_{2}(rd) - 2e^{-rd} \left(rd + 2 + \frac{3}{rd} + \frac{3}{r^{2}d^{2}} \right) \right], \qquad (23)$$

where $Y = (j \omega \mu, \sigma)^{\frac{1}{2}}$ and $K_1(Yd)$, $K_2(Yd)$ are the modified Bessel functions of the second kind of the first second order, respectively. Using (5) and the plane wave relationship

$$H_{y}(d,\omega) = H_{y}(o,\omega) e^{-\gamma d}, \qquad (24)$$

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equation (23) may be written

$$E_{x}^{sm}(o,w) = \frac{jw\mu_{o}\alpha_{m}}{4\pi d^{2}} H_{y}(o,w) e^{-\gamma d} \left[\gamma d K_{1}(\gamma d) + 3 K_{2}(\gamma d) -2 e^{-\gamma d} (\gamma d + 2 + \frac{3}{\gamma d} + \frac{3}{\gamma d^{2}}) \right]. \quad (25)$$

Transient Excitation

18. The backscattered electric field in the time domain, E_x^{sm} (o,t), may be expressed as a Fourier integral similar to that in (17). The Fourier integral may then be transformed into a convolution integral of the form given in (18), where A_{m}^{m} (o,t) is now the backscattered electric field step response at the surface from an induced magnetic dipole. The steps of the transformation are given in Appendix B. The step response may be written explicitly as

$$A_{x}^{m}(a,t) = \frac{\alpha_{m}}{4\pi\sigma d^{4}} \left[3I_{x}(\beta) - I_{x}(\beta) - \frac{2}{(\pi\beta)^{\frac{1}{2}}} \left(3 + \frac{3}{2\beta} + \frac{1}{\beta^{\frac{1}{2}}} \right) e^{-\frac{1}{\beta}} + \frac{12}{\pi^{\frac{1}{2}}} e^{-\frac{1}{\beta}} \left(\frac{1}{\beta^{\frac{1}{2}}} \right) \right]$$
where $\beta = \frac{t}{2}$, (26)

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$$erf(x) = \int_{0}^{x} e^{-y^{2}} dy,$$

$$I_{i}(\theta) = \int_{0}^{\infty} v \left[\sin v N_{2}(v) - \cos v J_{2}(v) \right] e^{-\beta v^{2}} dv, \qquad (27)$$

and

$$I_{2}(\beta) = \int \mathcal{V}\left[\sin \nu N_{1}(\nu) - \cos \nu J_{1}(\nu)\right] e^{-\beta \nu} d\nu. \qquad (28)$$

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The above expressions for $I_1(\beta)$ and $I_2(\beta)$ are convenient for large values of β . With further manipulation, it can be shown that

$$I_{1}(\beta) = -2 + \frac{1}{4\pi} \int_{0}^{\infty} \left[\left(\frac{g}{\beta k} + \frac{H}{\beta^{k} (1+v^{k})^{2}} \right) e^{-\frac{(1+v^{k})^{2}}{\beta^{k}}} + \frac{20}{(1+v^{k})^{2}} e^{-fc} \left(\frac{1+v^{k}}{\beta^{k}} \right) \right] \frac{2v^{k}+1}{(1+v^{k})^{k}} dv \qquad (29)$$

and

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$$I_{1}(\beta) = -\frac{2}{\pi^{\frac{1}{2}}\beta^{\frac{1}{2}}} \int_{0}^{\infty} (1+v^{2})^{\frac{1}{2}} e^{-\frac{(1+v^{2})^{2}}{\beta}} dv, \qquad (30)$$

where $\operatorname{erfc}(x) = \int_{e}^{e^{-y^2}} dy$. These forms are convenient for small values of p? The leading terms of the asymptotic expansions obtainable from (29) and (30) are

$$I_{,}(\beta) = -2 + \frac{e^{-\beta}}{2^{k}\beta} (1 + 1.93750\beta + 0.43945\beta^{2} - 0.028687\beta^{3} + 1.97677\beta^{4} + ...) \quad (1)$$

and

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$$I_{s}(\beta) = -\frac{e^{-\frac{1}{2}}}{2^{\frac{1}{2}}\beta^{2}} (1 + 0.18750\beta - 0.076172\beta^{2} + 0.10071\beta^{3} - 0.23011\beta^{4} + ...). (32)$$

It can be shown that $A_{\mathbf{x}}^{\mathbf{m}}$ (o,t) behaves as $e^{-\frac{1}{\beta}}$ for small β and is thus very small for t << $d^{2}\mu$. σ . For large β , the step response can be shown to fall off as $t^{-3/2}$. A graph of the dimensionless quantity $-A_{\mathbf{x}}^{\mathbf{m}}$ (o,t), $\frac{4\pi \sigma d^{4}}{\alpha m}$ is shown in

.

Figure 3. The integrals were evaluated on the IBM 7090 computer using Gaussian integration.

RELATIVE IMPORTANCE OF THE ELECTRIC FIELD

Contributions From Electric and Magnetic Dipoles

19. The relative importance of the contributions by the induced electric and magnetic dipoles to the backscattered electric field at the surface will depend on the relative magnitudes of the electric and magnetic polarizabilities of the conductor. An estimate of the relative importance may be obtained by determining the ratio of the incident electric field at the surface from the magnetic dipole to that from the electric dipole. The incident electric field from the magnetic dipole, $E_{\rm m}^{\rm m}$ (o, ω), is

$$E_{x}^{m}(o,\omega) = -\frac{M_{u}(d,\omega)}{4\pi d^{2}} (1+rd)e^{-rd}$$
(33)

and that from the electric dipole, E_x^e (0,w), is

$$E_{x}^{e}(0,\omega) = -\frac{P_{x}(d,\omega)}{4\pi\sigma d^{3}} \left(1 + rd + r^{2}d^{2}\right) e^{-rd}.$$
 (34)

Using the definitions in (6) and (7), the ratio of the electric field contributions is written

$$\frac{\left|\frac{E_{x}^{m}(o,\omega)}{E_{x}^{e}(o,\omega)}\right| = \left|\frac{\alpha_{m}}{\alpha_{e}} \frac{8d+7^{2}d^{2}}{1+7d+7^{2}d^{2}}\right| \qquad (35)$$

When $|\gamma d| \ll 1$, the ratio is small, provided

$$\frac{\alpha_m}{\alpha_e} \ll \frac{1}{7d} \qquad (3c)$$

From (35), it is evident that

$$\frac{E_{x}^{m}(o,\omega)}{E_{x}^{e}(o,\omega)} < \left| \frac{\alpha_{m}}{\alpha_{e}} \right| . \tag{37}$$

The contribution of the magnetic dipole to the electric field will, therefore, also be small when $\left| \begin{array}{c} \alpha_m \\ \alpha_e \end{array} \right| \ll 1$. This is

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the case for a cylinder with a small diameter to length ratio when excited longitudinally by an electric field. On the other hand, when $\left| \frac{\alpha m}{\alpha e} \right|$ is sufficiently large, the contribution of

the magnetic dipole will be larger than that of the electric dipole. This is the case, for example, for a cylinder with a large diameter to length ratio when excited longitudinally by a magnetic field.

THE ELECTRIC FIELD SCATTERED BY A SUBMARINE

20. It is of interest to apply the results of the previous sections to the scattering of an electromagnetic field by a submarine in sea water. Since an electromagnetic field in sea water is exponentially attenuated with the frequency, the exciting field must contain sufficiently low frequencies in order to appreciably illuminate a deeply submerged conductor. Man-made sources which radiate efficiently in the ELF range are not at present very practical. However, the ELF energy radiated by lightning discharges and propagated as sferics could conceivably be used.

21. A typical sferic, consisting of a quasi-sinusoidal portion followed by a slow tail, is applied to the sea-air interface and is assumed to propagate vertically into the sea water as a uniform plane wave. This wave is then backscattered by a submarine at a depth of 150 meters. The submarine is approximated by a conducting cylinder with a diameter to length ratio of 1/10 and a volume of 10⁴ m³. The electric field of the incident wave is taken to be along the longitudinal axis of the cylinder. Since for this type of excitation $\left| \begin{array}{c} \propto m, t \\ \infty m, t \\ \infty m, t \end{array} \right| \ll 1$,

only the electric field contribution from the induced electric dipole is considered. Although neglected here, the induced ferromagnetic moment of a submarine will, in fact, oppose the induced diamagnetic moment, thus helping to make the contribution of the latter moment even smaller. While it is true that the dimensions of the submarine are not much smaller than the depth of submergence, the dipole approximation may be expected to give an order of magnitude estimate of the backscattered electric field in the interface directly above the submarine.

22. No attempt is made here to suggest a method for detecting the backscattered electric field. An example of such a method is discussed by Modavis (1962).

Specification of the Sferic Waveform and the Parameters of the Scattering Model

23. The choice of an analytical representation of the waveform of the applied sferic to be used in the numerical computations is based on the desire to approximate commonly observed waveforms by the simplest expression possible. Accordingly, the oscillatory portion is given by

$$H_{y}(o,t) = 0 \qquad \text{for } t < o ,$$

= $H_{o}e^{-at}sin(\omega_{o}t-bt^{2}) \text{ for } o \le t \le t_{c},$
= $0 \qquad \text{for } t > t_{c}$ (39)

where $H_0 = 3 \times 10^{-3} \text{ amp/m}$

a = 2.9 x 10^3 sec⁻¹ b = 1.8 x 10^7 sec⁻² ω_0 = 5.2 x 10^4 sec⁻¹ t_c = 8.6 x 10^{-4} sec.

A plot of the waveform specified in (38) is shown in Figure 4 for times greater than 10^{-4} sec. The slow tail following the oscillatory portion of the sferic is represented as a positive half-cycle consisting of two straight line portions joined by a section of a parabola. The duration of the slow tail is three times that of the oscillatory portion and the peak amplitude is 0.4 that of the maximum oscillatory amplitude. Thus,

$$H_{y}(o,t) = \alpha (t - t_{c}) \qquad \text{for } t_{c} \leq t \leq t_{1},$$

= h - $\beta (t - t_{2})^{2} \qquad \text{for } t_{1} < t < t_{3},$
= - $\alpha (t - t_{f}) \qquad \text{for } t_{3} \leq t \leq t_{f},$
= 0 for t > $t_{f},$
where $t_{1} = 2.3 t_{c}$
 $t_{2} = 2.5 t_{c}$,
 $t_{3} = 2 t_{2} - t_{1}$
$$\begin{pmatrix} 14 \\ \text{CONFIDENTIAL \end{pmatrix}$$
 (39)

$$t_{f} = 2 t_{2} - t_{c}$$

$$\alpha = \frac{2h}{t_{1} + t_{2} - 2t_{c}}$$

$$\beta = \frac{\alpha}{2(t_{2} - t_{1})}$$

$$h = 0.4 H_{0}$$

A plot of the above slow tail is shown in Figure 5.

24. The values of the other parameters are chosen as:

 σ , conductivity of sea = 4 mho/m μ_o , permeability of sea water = $4\pi \times 10^{-7}$ henries/m d, depth of scattering model = 150 meters $\frac{a}{b}$, diameter to length ratio of conducting cylinder = 1/10 v, volume of conducting cylinder = 10^4 m^3 $\propto e, \ell$, longitudinal electric polarizability = 60 $\times 10^4 \text{ m}^3$.

Numerical Results

25. Using (18) and the scattering model described in the previous section, numerical results have been computed on the IBM 7090 for the backscattered electric field at the sea surface. The background, against which this backscattered electric field must be detected, consists of the incident electric field at the sea surface. This field may be determined by an application of (18). The incident electric field step response may be obtained from the well known transmission line equations for an infinite, leakage free, non-inductive cable in which the voltage corresponds to the magnetic field and the current to the electric field. For example, see Goldman (1949). The result for the incident electric field step response at the sea surface, $E_{\mathbf{x}}^{\mathbf{x}}$ (o,t), is written

$$E_{x}^{i}(o,t) = \left(\frac{\mu_{o}}{\sigma}\right)^{\gamma_{a}} \frac{1}{(\pi t)^{\kappa}} \qquad (40)$$

26. Graphs of the backscattered electric field step response A_{x}^{e} (o,t), the incident electric field, E_{x} (o,t), and the backscattered electric field $\overline{E_{x}^{e}}$ (o,t), are presented in Figures 6, 7, and 8, respectively. Because of the exponential fall of the step response, A_{x}^{e} (o,t), for small values of t, the backscattered electric field at the sea surface for these times is negligible compared with the incident electric field at the surface. For this reason, numerical results for $t < 10^{-2}$ sec. are not presented for the backscattered electric field in Figure 8. The behavior of the incident field and the backscattered field for large t may be determined analytically from the convolution integral forms for these quantities. Both are found to fall off as $t^{-3/2}$ for large t. In Figure 8, the point marked ~ 3% of E_{x-1} (o,t) indicates the time at which the backscattered field is the maximum percentage (approximately 3%) of the incident field.

CONCLUSION

27. If submarines at a depth of 500 feet are to be detected in the example just given, a backscattered electric field of the order of 10-9 volts/meter must be measured at the sea surface directly above the submarine. Obviously, if the detector at the surface is much off to the side, the value of the scattered field will be even smaller. The backscattered field at the sea surface directly above the submarine amounts at most to about 3% of the incident electric field at the surface. Such requirements are rather severe and the detection of submarines in the case of single sferic excitation therefore appears to be quite difficult. For submarines at shallower depths and for different sferic excitations, the detection problem should be investigated further.

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Table 1

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Electric and Magnetic Polarizabilities of a Right Circular Cylinder of Diameter a, Length b, and Volume $v = \frac{\pi}{\gamma} a^2 b$

a 5		<u>Creit</u> V	<u>an l</u> v	<u>Q'm,t</u> V
0	~	2.00	-1.00	-2.00
$\frac{1}{10}$	60.00	2.13	-1.06	-1.94
$\frac{1}{4}$	15.1	2.32	-1.16	-1.85
17	7.10	2.61	-"31	-1.74
1	3.86	3.17	-1.59	-1.58
2	2.43	4.22	-2.11	-1.41
4	1.75	6.18	-3.09	-1.27
~	1.00	6	- 00	-1.00

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FIG.I A CONDUCTOR EMBEDDED IN A SEMI-INFINITE DISSIPATIVE MEDIUM





FIG.3 THE BACKSCATTERED ELECTRIC FIELD STEP RESPONSE AT THE SURFACE FROM AN INDUCED MAGNETIC DIPOLE

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FIG.4 WAVEFORM OF THE OSCILLATORY PORTION OF THE APPLIED SFERIC

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FIG. 6 BACKSCATTERED ELECTRIC FIELD STEP RESPONSE

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FIG. 7 INCIDENT ELECTRIC FIELD



FIG. 8 BACKSCATTERED ELECTRIC FIELD

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FIG.9 CONTOUR IN THE Z-PLANE

APPENDIX A

1. By substituting

$$H_{y}(o,\omega) = \int_{0}^{\infty} H_{y}(o,\lambda) e^{-j\omega\lambda} d\lambda = \frac{1}{j\omega} \int_{0}^{\infty} H_{y}(o,\lambda) e^{-j\omega\lambda} d\lambda \qquad (A1)$$

in (16), the inverse Fourier transform in (17) may, upon changing the order of integration, be written

$$\overline{E}_{x}^{se}(o,t) = \int_{0}^{\infty} A_{x}^{e}(o,t-\lambda) H_{y}'(o,\lambda) d\lambda , \qquad (A2)$$

where

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$$A_{x}^{e}(0,t) = \frac{\alpha_{e}\mu_{e}}{8\pi^{2}d^{3}} \int_{-\infty}^{\infty} \frac{e^{-\gamma d}}{\gamma} \left[\gamma_{d}^{*}K_{1}(\gamma_{d}) - 2e^{-\gamma d} (2 + 2\gamma d + \gamma^{2}d^{2}) \right] e^{j\omega t} d\omega, \quad (A3)$$

 $Y = (j \omega \mu_0 \sigma)^{\frac{1}{2}}$, and $K_2(Yd)$ is the modified Bessel function of the second kind. For convergence arg $\pm j\omega = \pm \frac{\pi}{2}$. Thus,

$$A_{x}^{e}(0,t) = \frac{\alpha_{e}\mu_{a}}{4\pi^{2}d^{3}} R_{a} \int \frac{e^{-rd}}{7} \left[r^{2} K_{1}(rd) - 2e^{-rd} (2 + 2rd + r^{2}) \right] e^{j\omega t} d\omega. \quad (A4)$$

When t > 0, ψ in (A4) is replaced by the complex variable $z = \psi + j u$, and the integration is performed around the contour shown in Figure 9. When $\epsilon \rightarrow \infty$,

$$A_{x}^{e}(o,t) = \frac{\alpha_{e}}{2\pi^{2}\sigma d^{\psi}} R_{a} \int_{0}^{\infty} e^{-jv} \left[-v^{2} K_{x}(jv) - 2e^{-jv} (2+2jv-v^{2}) \right] e^{-\frac{v^{2}t}{\mu \cdot \sigma d^{2}}} dv, \quad (A5)$$

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where $u = \frac{v^2}{\mu_0 \sigma d^2}$. Since

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$$K_{2}(jv) = \frac{\pi}{2} \left[N_{2}(v) + j J_{3}(v) \right],$$
 (A6)

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where $N_2(v)$ and $J_2(v)$ are the Neumann and Bessel functions of the second order, respectively, (A5) may be written ''

$$A_{x}^{e}(0,t) = -\frac{\alpha_{e}}{4\pi\sigma d^{4}} \int_{0}^{\infty} \left[\sin \nu J_{x}(\nu) + \cos \nu N_{x}(\nu) \right] e^{-\frac{\nu^{2}t}{\mu_{0}\sigma d^{2}}} d\nu$$

$$-\frac{\alpha e}{\pi^{2}\sigma d^{4}}\int_{0}^{\infty}\left[\left(2-\nu^{2}\right)\cos 2\nu+2\nu\sin 2\nu\right]e^{-\frac{\nu}{\mu\circ\sigma d^{2}}}d\nu \quad (A7)$$

when t > 0. Performing some of the integration, (A7) is written

$$A_{x}^{e}(o,t) = -\frac{\alpha_{e}}{4\pi\sigma d^{4}} \left[I(\beta) + \frac{2}{(\pi\beta)^{k_{2}}} \left(2 + \frac{3}{2\beta} + \frac{1}{\beta^{2}} \right) e^{-\frac{1}{\beta}} \right], \quad (As)$$

where $\beta = \frac{t}{\mu_0 \sigma d^2}$ and

$$I(\beta) = \int v^{*} \left[\sin v J_{\lambda}(v) + \cos v N_{\lambda}(v) \right] e^{-\beta v^{*}} dv. \qquad (A9)$$

Finally, since $A_X^{\epsilon}(o,t) = o$ for t < o,

$$\bar{E}_{x}^{se}(o,t) = \int_{0}^{t} A_{x}^{e}(o,t-\lambda) H_{y}(o,\lambda) d\lambda . \qquad (A10)$$

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APPENDIX B

1. By substituting

$$H_{y}(o,\omega) = \int_{0}^{\infty} H_{y}(o,\lambda) e^{-j\omega\lambda} d\lambda \qquad (B1)$$

in (25), the inverse Fourier transform may, upon changing the order of integration, be written

$$\tilde{E}_{x}^{sm}(o,t) = \int_{o}^{\infty} B_{x}^{m}(o,t-\lambda) H_{y}(o,\lambda) d\lambda, \qquad (B2)$$

where

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$$B_{X}^{m}(0,t) = \frac{\alpha_{m}}{8\pi^{3}\sigma d^{2}} \int_{0}^{\infty} \gamma^{2} e^{-\gamma d} \left[\gamma d K_{1}(\gamma d) + 3K_{1}(\gamma d) -2e^{-\gamma d} \left(\gamma d + 2 + \frac{3}{\gamma d} + \frac{3}{\gamma^{2} d^{2}}\right) \right] e^{j\omega t} d\omega, \quad (B3)$$

 $Y = (j \omega \mu, \sigma)^{\frac{1}{2}}$, and $K_1(Yd)$ and $K_2(Yd)$ are the modified Bessel functions of the second kind of the first and second order, respectively. Noting that arg $\pm j\omega = \pm \frac{\pi}{2}$ (B3) may be written

$$B_{x}^{m}(0,t) = \frac{\omega_{m}}{4\pi^{2}\sigma d^{2}} R_{e} \int_{0}^{\infty} e^{-Yd} \left[Yd K_{i}(Yd) + 3K_{2}(Yd) - 2e^{-Yd} (Yd + 2 + \frac{3}{7d} + \frac{3}{7^{2}d^{2}}) \right] e^{i\omega t} d\omega. \quad (B4)$$

When t < 0, the impulse response, B_X^m (0,t), is equal to zero since it is assumed that H_y (0,t) = 0 for t ≤ 0 . Integrating (B2) by parts, it follows that

$$\bar{E}_{x}^{sm}(o,t) = \int_{0}^{t} A_{x}^{m}(o,t-\lambda) H_{y}'(o,\lambda) d\lambda , \qquad (Bs)$$

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where

$$A_{x}^{m}(o,t) = \frac{\mu_{o} \propto_{m}}{4\pi^{2} d^{2}} k_{e} \int_{0}^{\infty} e^{-rd} \left[rdK_{1}(rd) + 3K_{2}(rd) - 2e^{-rd} \left(rd + 2 + \frac{3}{rd} + \frac{3}{r'd^{2}} \right) \right] e^{j\omega t} d\omega. \qquad (B6)$$

When t > 0, ω in (B6) is replaced by the complex variable $z = \omega + j\omega$, and the integration is performed around the contour shown in Figure 9. When $\epsilon \rightarrow 0$ and $R \rightarrow \infty$,

$$A_{x}^{m}(o,t) = \frac{\alpha_{m}}{2\pi^{2}\sigma d^{\psi}} R_{a} \int_{0}^{\infty} \sqrt{e^{-jv}} \left[jv K_{i}(jv) + 3K_{x}(jv) - 2e^{-jv} (jv + 2 + \frac{3}{jv} - \frac{3}{v^{2}}) \right] e^{-\frac{\sqrt{2}t}{N\sigma\sigma} d^{2}} dv, (B7)$$

where $u = \frac{v^2}{\mu_* \sigma d^2}$. Since

$$K_{i}(jv) = - \underbrace{\mp}_{i} \left[J_{i}(v) - j N_{i}(v) \right]$$
(BP)

and

$$K_{s}(iv) \cdot \prod_{n} \left[N_{s}(v) + j J_{s}(v) \right], \qquad (B9)$$

where $J_2(v)$ and $N_2(v)$ are the Bessel and Neumann functions of the second order, respectively, (B7) may be written

$$A_{x}^{m}(o,t) = \frac{\alpha_{m}}{\gamma \pi_{o} d^{4}} \int_{0}^{\infty} \left\{ 3\nu \left[\sin \nu N_{s}(\nu) - \cos \nu J_{s}(\nu) \right] - \nu^{2} \left[\sin \nu N_{s}(\nu) - \cos \nu J_{s}(\nu) \right] - \frac{4}{11} \left[\left(2\nu - \frac{3}{\nu} \right) \sin 2\nu - (\nu^{2} - 3) \cos 2\nu \right] \right\} e^{-\frac{\nu^{2} t}{\mu_{0} \cdot \sigma d^{2}}} d\nu.$$
(B10)

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Performing some of the integration, (BlO) is written

$$A_{x}^{\mathsf{M}}(o,t) = \frac{\omega_{\mathsf{M}}}{4\pi\sigma d^{\mathsf{M}}} \left[3 \mathbf{I}_{x}(\beta) - \mathbf{I}_{z}(\beta) - \frac{2}{(\pi\beta)^{\mathsf{K}}} \left(3 + \frac{3}{2\beta} + \frac{1}{\beta^{\mathsf{L}}} \right) e^{-\frac{1}{\beta}} + \frac{1^{\mathsf{L}}}{\pi^{\mathsf{K}}} \operatorname{erf}\left(\frac{1}{\beta^{\mathsf{K}}} \right) \right] , \qquad (\exists 1)$$
where $\beta = \frac{t}{\mu_{x}\sigma d^{\mathsf{L}}}$, $\operatorname{erf}(x) = \int_{0}^{x} e^{-\frac{y^{\mathsf{L}}}{y}} dy ,$

$$\mathbf{I}_{x}(\beta) = \int_{0}^{\infty} v \left[\sin v N_{z}(v) - \cos v \mathbf{J}_{z}(v) \right] e^{-\beta v^{\mathsf{L}}} dv , \qquad (B_{12})$$

and

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$$I_{2}(\mathbf{R}) = \int_{0}^{\infty} v^{*} \left[\sin v N_{1}(v) - \cos v J_{1}(v) \right] e^{-\beta v^{2}} dv . \qquad (B B)$$

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