TWO-DIMENSIONAL WIND-TUNNEL INVESTIGATION OF LOW-DRAG
VERTICAL-TAIL, HORIZONTAL-TAIL, AND WING
SECTIONS EQUIPPED WITH SEALED INTERNALLY
BALANCED CONTROL SURFACES

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SUMMARY

A two-dimensional wind-tunnel investigation was made of three low-drag airfoil sections equipped with sealed internally balanced control surfaces designed for use as vertical-tail, horizontal-tail, and wing sections. The tests included determination of control-surface effectiveness and hinge moments and airfoil section drag characteristics. Balance pressures were also measured for use in estimating the hinge-moment characteristics of the control surfaces with any amount of sealed internal balance.

Sharp irregularities occurred in the variation of the control-surface section hinge-moment coefficient with airfoil section angle of attack, which were probably caused by sudden movements in transition along the surfaces of all three airfoils at the extremities of the low-drag range. Tests of the vertical-tail section indicated that these irregularities were reduced in magnitude when transition was fixed at a forward chord-wise position but were not entirely removed until transition was fixed at the airfoil leading edge. An estimated variation of aileron wheel force with wing-tip helix angle for an assumed airplane indicated that no unusual aileron wheel-force characteristics would be caused by the irregularities in the two-dimensional hinge-moment characteristics. Sudden movements in transition along the surfaces of vertical-tail or horizontal-tail sections, however, would probably cause sudden changes in rudder or elevator hinge moments.
INTRODUCTION

The recent trend toward the use of large high-speed airplanes has imposed upon the airplane designer the problem of obtaining adequate control effectiveness without excessive control forces while securing low values of airfoil drag and high values of critical Mach number. Data for use by the designer in the prediction of low-drag-wing characteristics are available but only a limited amount of data on two-dimensional aerodynamic characteristics of control surfaces on low-drag airfoils is available. An investigation was made in the Langley two-dimensional low-turbulence pressure tunnel of two NACA 64-series-type airfoils and one NACA 7-series-type airfoil equipped with sealed internally balanced control surfaces to provide additional data on two-dimensional characteristics of control surfaces on low-drag airfoils. The 64-series-type airfoils were intended for use as tail surfaces and were equipped with a rudder and elevator of 0.40 and 0.35 airfoil chord, respectively. The 7-series-type airfoil was fitted with an aileron of 0.22 airfoil chord.

The tests, which were made at Reynolds numbers of \(3 \times 10^6\), \(6 \times 10^6\), and \(9 \times 10^6\), included the determination of control-surface effectiveness and hinge moments and airfoil section drag characteristics. The pressure differences across the control-surface seals were also obtained for use in estimating the hinge-moment characteristics of the control surfaces with any amount of sealed internal balance.

SYMBOLS AND COEFFICIENTS

The symbols and coefficients used in the presentation of results are defined as follows:

- \(a_o\) airfoil section angle of attack, degrees
- \(c\) chord of airfoil with control surface neutral; measured along maximum length line
- \(c_x\) chord of control surface measured from hinge axis to trailing edge
$c_b$ chord of overhang from control-surface hinge axis to middle of gap seal

$\delta_x$ control-surface deflection with respect to airfoil; positive when trailing edge is deflected downward

$R$ Reynolds number

$q_o$ free-stream dynamic pressure

$b$ total wing span

$b_a$ span of one aileron

$c_a$ root-mean-square chord of aileron behind hinge axis

$V$ true airspeed

$V_i$ indicated airspeed

$p$ local static pressure; also, rolling velocity when used in parameter $p_b/2V$

$H_o$ free-stream total pressure

$S$ airfoil pressure coefficient $\frac{H_o - p}{q_o}$

$p_b/2V$ helix angle described by wing tip during roll, radians

$F_w$ wheel force

$\theta$ wheel deflection from neutral

$C_l\delta$ rate of change of rolling-moment coefficient with aileron deflection

$C_l^p$ rate of change of rolling-moment coefficient with $p_b/2V$

$c_l$ airfoil section lift coefficient

$\Delta c_l$ increment of $c_l$ caused by deflection of control surface from neutral

$c_d$ airfoil section drag coefficient
\( h \)  
control-surface hinge moment per unit span;  
positive when control surface tends to  
deflect downward

\( c_{h_x} \)  
control-surface section hinge-moment coefficient  
based on control-surface chord \( \left( \frac{h}{q_0 c_x^2} \right) \)

\( (c_{h_x})_{up} \)  
hinge-moment coefficient of upgoing aileron  
estimated for airplane during roll

\( (c_{h_x})_{down} \)  
hinge-moment coefficient of downgoing aileron  
estimated for airplane during roll

\( \Delta p/q_0 \)  
seal-pressure-difference coefficient (ratio  
of pressure difference across control-  
surface seal to free-stream dynamic  
pressure); positive when pressure below  
seal is greater than pressure above seal

\( \left( \frac{\partial c_l}{\partial \delta_x} \right)_{\alpha_0} \)  
rate of change of section lift coefficient  
with section angle of attack

\( \left( \frac{\partial c_l}{\partial \delta_x} \right)_{c_l} \)  
rate of change of section lift coefficient  
with control-surface deflection

\( \left( \frac{\delta \alpha_o}{\delta \delta_x} \right)_{c_l} \)  
control-surface section effectiveness parameter  
(absolute value); also designated as \( k \) for  
aileron

\( \left( \frac{\Delta \alpha_o}{\Delta \delta_a} \right)_{c_l} \)  
aileron section effectiveness parameter  
(ratio of increment of airfoil section  
angle of attack to increment of aileron  
deflection required to maintain a constant  
lift coefficient; absolute value)

\( \left( \frac{\delta c_{h_x}}{\delta \alpha_o} \right)_{h_x} \)  
rate of change of section hinge-moment  
coefficient with section angle of attack

\( \left( \frac{\delta c_{h_x}}{\delta \delta_x} \right)_{\alpha_0} \)  
rate of change of section hinge-moment coefficient  
with control-surface deflection
The subscript \(x\) is replaced herein with subscripts \(r\), \(e\), and \(a\) for the rudder, elevator, and aileron, respectively. The subscripts to the partial derivatives denote the variables held constant when the partial derivatives are taken. The derivatives are obtained at zero angle of attack and zero control-surface deflection except as noted.

MODELS AND APPARATUS

The three models, having chords of 24 inches, were two-dimensional airfoil sections designed for use as a vertical tail, a horizontal tail, and a wing and were constructed of laminated mahogany. Sketches of the models are presented as figure 1. Rubber seals were used along the complete span and at both ends of the control surfaces to prevent the flow of air through the gaps.

The pressure difference across the control-surface seals was measured with static-pressure orifices located above and below the balance plates. A manometer setup, which integrated the pressures along the floor and ceiling of the tunnel test section, was used to measure lift, and the wake survey method was used to measure drag. Hinge moments of the control surfaces were measured with electrical-resistance strain gages.

The vertical-tail section was a 0.155c thick symmetrical airfoil with a pressure distribution (fig. 2) similar to that of the NACA 64-series airfoils. The model was equipped with a 0.40c rudder with a sealed internal balance of 0.412c, that is, \(\frac{c_D}{c_r} = 0.412\).

The horizontal-tail section, which also had a pressure distribution (fig. 3) similar to that of the NACA 64-series airfoils, had a maximum thickness of approximately 0.13c. The angle of attack for this model was measured with respect to a reference line shown in figure 1. The model was equipped with a 0.35c elevator with a sealed internal balance of approximately 0.43c.

The wing profile had a maximum thickness of approximately 0.17c and a pressure distribution (fig. 4) similar to that of an NACA 7-series airfoil. The design section lift coefficient is 0.266, for which the position of
minimum pressure is approximately 0.35c on the upper surface and 0.50c on the lower surface. The airfoil section angle of attack was measured with respect to a reference line shown in figure 1. The model was equipped with a 0.22c aileron of true airfoil contour with a sealed internal balance of approximately 0.44c.

For the normal smooth condition of the models, the airfoil surfaces were sanded with No. 400 carborundum paper to produce an aerodynamically smooth finish. For the rough condition of the vertical-tail section, the model surfaces were the same as for the smooth condition but 0.002-inch carborundum grains were applied to a thin layer of shellac on both the upper and lower airfoil surfaces at various chordwise positions. The roughness strips were 1.2 inches wide at 0.45c, 0.5 inch wide at 0.30c, 0.15c, and 0.10c, and 3.75 inches wide at the leading edge (1.875 in. along each surface measured from the leading edge).

TESTS

Tests of the three models were made in the Langley two-dimensional low-turbulence pressure tunnel. The tests included measurements at a Reynolds number of approximately 6 × 10^6 of airfoil lift and drag, control-surface hinge moment, and balance pressure for each model with various deflections of the control surfaces. Observations of the airflow over the surfaces of both tail sections were made by means of tuft surveys. Lift and drag measurements were also made at Reynolds numbers of approximately 3 × 10^6 and 9 × 10^6 for the horizontal- and vertical-tail sections with the control surfaces neutral. In addition, the vertical-tail section was tested at a Reynolds number of 6 × 10^6 with roughness strips applied to both upper and lower airfoil surfaces at various chordwise positions. The Mach numbers corresponding to Reynolds numbers of 3 × 10^6, 6 × 10^6, and 9 × 10^6 were 0.11, 0.14, and 0.10, respectively.

The following formulas were used to correct the tunnel data to free-air conditions:

\[
C_l = \left[ 1 - 2\Lambda (\sigma + \xi) - \sigma \right] C_{l}'
\]
\[ c_d = \left[ 1 - 2\Lambda (\sigma + \xi) \right] c_d' \]
\[ c_o = (1 + \sigma) c_o' \]
\[ q_o = \left[ 1 + 2\Lambda (\sigma + \xi) \right] q_o' \]

where

\( \Lambda \) factor dependent on airfoil shape
\( \sigma \) factor dependent on ratio of airfoil size to tunnel height
\( \xi \) factor used for correcting effect of model upon velocity measured by static-pressure orifices

and the primed quantities represent the values measured in the tunnel.

The values of \( 2\Lambda (\sigma + \xi) \) were 0.0115, 0.00979, and 0.00792 for the wing, vertical-tail, and horizontal-tail sections, respectively. The value of \( \sigma \) was equal to 0.015 for all three airfoils.

**RESULTS AND DISCUSSION**

Values of the important aerodynamic parameters measured when \( \alpha_o \) and \( \delta_x \) are approximately 0 for the three models tested are presented in the following table:

<table>
<thead>
<tr>
<th>Airfoil section</th>
<th>Airfoil surface condition</th>
<th>( \frac{\partial c_l}{\partial \alpha_o} )</th>
<th>( \frac{\partial \alpha_o}{\partial \delta_x} )</th>
<th>( \frac{\partial c_l}{\partial \delta_x} )</th>
<th>( \frac{\partial c_l}{\partial \alpha_o} )</th>
<th>( \frac{\partial c_l}{\partial \delta_x} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rudder</td>
<td>Smooth</td>
<td>0.107</td>
<td>0.58</td>
<td>-0.0034</td>
<td>-0.0007</td>
<td></td>
</tr>
<tr>
<td></td>
<td>L.E. rough</td>
<td>0.107</td>
<td>0.58</td>
<td>-0.0009</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Elevator</td>
<td>Smooth</td>
<td>0.100</td>
<td>0.62</td>
<td>-0.0029</td>
<td>-0.0023</td>
<td></td>
</tr>
<tr>
<td>Aileron</td>
<td>Smooth</td>
<td>0.101</td>
<td>0.48</td>
<td>-0.0004</td>
<td>-0.0013</td>
<td></td>
</tr>
</tbody>
</table>
Vertical-Tail Section

Lift, hinge-moment, balance-pressure, and drag data for the vertical-tail section with the airfoil surfaces aerodynamically smooth and also with roughness strips applied at various chordwise positions are presented in figures 5 to 14.

Lift. - The lift characteristics of the vertical-tail section at a Reynolds number of approximately $6 \times 10^6$ are presented in figure 5 for the airfoil in a smooth condition. The values of $\frac{\alpha}{\alpha_o}$ and $\frac{c_l}{\alpha_o}$ are equal to 0.107 and 0.062, respectively, and the effectiveness parameter $\frac{\alpha}{\alpha_o}$ is equal to 0.58. The increment of section lift coefficient $\Delta c_l$ plotted against rudder deflection is presented in figure 6 for four section angles of attack from $0^\circ$ to $12^\circ$. These curves show that for small rudder deflections the effectiveness remains constant through this range of angle of attack. At rudder deflections more negative than $-2^\circ$, the increment of section lift coefficient increases with decreasing angle of attack until the air flow over the lower surface of the rudder begins to separate. This separation occurs at low angles of attack for high negative rudder deflections as shown in figures 5 and 6 and was observed by means of tuft surveys over the airfoil surfaces.

Scale effect on the lift characteristics is shown in figure 7. Lift measurements were made with the rudder neutral at Reynolds numbers of approximately $3 \times 10^6$, $6 \times 10^6$, and $9 \times 10^6$.

The effect of fixed transition on the lift characteristics at rudder deflections of $0^\circ$, $-5^\circ$, and $-10^\circ$ is shown in figure 8. Application of roughness to the airfoil leading edge caused an average reduction in maximum section lift coefficient of approximately 12 percent but had a negligible effect on the lift-curve slope with the rudder neutral. The values of $\Delta c_l$ with the rudder neutral.

The values of $\frac{\Delta c_l}{\alpha_o}$...
and \( \left( \frac{\partial \alpha_0}{\partial \delta_r} \right) \) that were obtained between rudder deflections of \(-5^\circ\) and \(0^\circ\) and at zero angle of attack remained the same as for the aerodynamically smooth condition, but the increment of \(c_l\) caused by rudder deflections of \(-5^\circ\) and \(-10^\circ\) decreased at low angles of attack when transition was induced at the airfoil leading edge (fig. 8); the sharp irregularity in the variation of \(\Delta c_l\) with \(\delta_r\) shown in figure 6 was thereby eliminated.

**Hinge moment.** The variation of rudder section hinge-moment coefficient \(c_{hr}\) with airfoil section angle of attack for the smooth airfoil is presented in figure 9 for rudder deflections between \(-19^\circ\) and \(19^\circ\) at a Reynolds number of approximately \(6 \times 10^6\). Corresponding curves of the pressure difference across the rudder balance seal \(\Delta p/\rho_0\) against \(\alpha_0\) are presented in figure 11. These data may be used to estimate the hinge-moment characteristics of a rudder of similar contour and chord by the methods of reference 1. For the 0.12-percent sealed internal balance, the values of \(\left( \frac{\partial c_{hr}}{\partial \alpha_0} \right) \delta_r\) and \(\left( \frac{\partial c_{hr}}{\partial \delta_r} \right) \alpha_0\) were equal to \(-0.0034\) and \(-0.0007\), respectively, for the airfoil surfaces in a smooth condition.

The sharp irregularities in the curves of \(c_{hr}\) against \(\alpha_0\) (fig. 9) correspond to the limits of the low-drag range as shown in figure 13 and are believed to be caused by the sudden movements in transition along the airfoil surfaces at the extremities of the low-drag range. The data of figure 10 were taken at rudder deflections of \(0^\circ\), \(-5^\circ\), and \(-10^\circ\) with transition strips placed on the airfoil surfaces at various chordwise positions to limit the movement of transition. As the fixed transition was moved forward of the 0.15c position the irregularities in \(\left( \frac{\partial c_{hr}}{\partial \alpha_0/\delta_r} \right) \) diminished in magnitude but were not entirely removed until transition was fixed.
at the airfoil leading edge. The value of \[ \left( \frac{\partial c_{hr}}{\partial \alpha_0} \right) \delta_r \]
with transition fixed at the airfoil leading edge was -0.0009 as compared with -0.0034 for the aerodynamically smooth airfoil. A forward position of transition had no significant effect on the variation of \( \Delta p/q_0 \) with \( \alpha_0 \) (fig. 12).

Drag. - Drag characteristics of the vertical-tail section in a smooth condition are presented in figure 13 at Reynolds number of approximately \( 3 \times 10^6 \), \( 6 \times 10^6 \), and \( 9 \times 10^6 \) with the rudder neutral and at a Reynolds number of approximately \( 6 \times 10^6 \) with rudder deflections between \(-5^\circ\) and \(5^\circ\). Through this range of rudder deflection the value of the minimum section drag coefficient and the range of lift coefficient for low-drag values remained substantially the same. Drag polars for the airfoil section with transition strips applied to the airfoil surfaces at various chordwise positions are presented in figure 14 for rudder deflections of \(0^\circ\) and \(-5^\circ\).

Horizontal-Tail Section

Lift, hinge-moment, balance-pressure, and drag data for the horizontal-tail section with the airfoil surfaces aerodynamically smooth are presented in figures 15 to 20.

Lift. - The lift characteristics of the horizontal-tail section at a Reynolds number of approximately \( 6 \times 10^6 \) are presented in figure 15 for various elevator deflections between \(-23^\circ\) and \(9^\circ\). The values of \( \left( \frac{\partial c_l}{\partial \alpha_0} \right) \delta_e \) and \( \left( \frac{\partial c_l}{\partial c_l} \right) \alpha_0 \)
are equal to 0.100 and 0.062, respectively, and the effectiveness parameter \( \left( \frac{\partial c_l}{\partial \delta_e} \right) \) is equal to 0.62. The variation of the increment of section lift coefficient \( \Delta c_l \) with elevator deflection is presented in figure 16 for four section angles of attack from \(-4^\circ\) to \(8^\circ\). Between elevator deflections of \(-3^\circ\) and \(3^\circ\) the effectiveness remains constant throughout this range of angle of attack. At elevator deflections more negative than \(-3^\circ\) the increment of section
lift coefficient increases with decreasing section angle of attack until, as in the case of the rudder, the air flow over the lower surface of the elevator begins to separate. This separation, which was observed by means of tuft surveys over the airfoil surfaces, causes the sharp breaks in the lift curves of figure 15 and results in the decreased value of $\Delta c_l$ at high negative elevator angles and low angles of attack (fig. 16). At positive elevator deflections greater than $4^\circ$, the value of $\Delta c_l$ decreases with increasing angle of attack.

The effect of Reynolds number between $3 \times 10^6$ and $9 \times 10^6$ on the lift characteristics of the horizontal-tail section with the elevator neutral is shown in figure 17.

Hinge moment. - The elevator section hinge-moment coefficients plotted against airfoil section angle of attack are presented in figure 18 for elevator deflections between $-23^\circ$ and $9^\circ$ at a Reynolds number of approximately $6 \times 10^6$. As in the case of the rudder tests, irregularities in the variation of $c_{h_e}$ with $\alpha_0$ correspond to the limits of the low-drag range as shown in figure 20 and are believed to be caused by the sudden movements in transition along the airfoil surfaces at the extremities of the low-drag range. The value of $\left( \frac{\partial c_{h_e}}{\partial \alpha_0} \right)_{\delta_e}$ is equal to $-0.0029$ and was obtained at an angle of attack of $-2^\circ$ because one of the jogs in the hinge-moment curve occurs at a section angle of attack of $0^\circ$. If transition occurs on the airfoil surfaces at a forward chordwise position because of surface irregularities or roughness, the magnitude of the jogs in the curve of the variation of hinge moment with angle of attack and the absolute value of $\left( \frac{\partial c_{h_e}}{\partial \alpha_0} \right)_{\delta_e}$ may be expected to decrease in a manner similar to that of the vertical-tail section. The value of $\left( \frac{\partial c_{h_e}}{\partial \delta_e} \right)_{\alpha_0}$ for the aerodynamically smooth horizontal-tail section is approximately $-0.0023$. 
The variation of the pressure difference across the elevator balance seal with $\alpha_o$ is presented in figure 19 at the same elevator deflections for which hinge-moment data are presented. The hinge-moment and seal-pressure data may be used to estimate the hinge-moment characteristics of an elevator of similar contour and chord with any amount of sealed internal balance by the methods of reference 1.

**Drag.**— Drag characteristics of the horizontal-tail section are presented in figure 20. These data include drag polars at Reynolds number of approximately $3 \times 10^6$, $6 \times 10^6$, and $9 \times 10^6$ with the elevator neutral and at a Reynolds number of $6 \times 10^6$ with the elevator deflected $\pm 20^\circ$.

**Wing Section**

Lift, hinge-moment, balance-pressure, and drag data for the wing section with the airfoil surfaces aerodynamically smooth are presented in figures 21 to 25.

**Lift.**— The lift characteristics of the airfoil section with an aileron are presented in figure 21. The values of $\frac{\delta c_l}{\delta \alpha_o}$ and $\frac{\delta c_l}{\delta \delta_a \alpha_o}$ are equal to 0.101 and 0.048, respectively. The effectiveness parameter $\frac{\delta \alpha_o}{\delta \delta_a c_l}$ is equal to 0.48 or 48 percent of the thin airfoil theoretical effectiveness (reference 2) and is approximately the same as the effectiveness obtained on the NACA 0009 airfoil section (reference 3).

In order to show the variation of aileron effectiveness with lift coefficient and aileron deflection, values of the effectiveness have been measured between definite aileron deflections. This effectiveness parameter is designated $\frac{\Delta \alpha_o}{\Delta \delta_a c_l}$. Curves of $\frac{\Delta \alpha_o}{\Delta \delta_a c_l}$ against $c_l$ for various aileron deflection limits are presented in...
figure 22. A comparison of the measured effectiveness between \( \delta_a = 0^\circ \) and \( 10^\circ \) and \( \delta_a = 0^\circ \) and \( -10^\circ \) shows that the aileron is more effective for negative aileron deflections. A comparison of the measured effectiveness between \( \delta_a = 0^\circ \) and \( 17^\circ \) and \( \delta_a = 0^\circ \) and \( -17^\circ \) also shows a higher effectiveness for negative aileron deflections except through an approximate range of section lift coefficient from 0 to 0.3 in which the effectiveness of the down aileron was about the same as that of the up aileron. At the section lift coefficients greater than approximately 0.4 the effectiveness of the aileron deflected down 17\(^\circ\) decreased appreciably. This large decrease in effectiveness at high positive aileron deflections and section angles of attack, probably caused by separation of the air flow over the upper surface of the aileron, is reflected in a decrease in the effectiveness from \( \delta_a = \pm 10^\circ \) to \( \delta_a = \pm 17^\circ \). At section lift coefficients from \(-0.4\) to 0.4, the effectiveness between the limits of \( \delta_a = \pm 17^\circ \) was almost the same as that measured between the limits of \( \delta_a = \pm 10^\circ \). The value of \( \frac{\Delta a_o}{\Delta \delta_a / c_l} \) when measured between \( \delta_a = \pm 10^\circ \) decreased from 0.50 at a section lift coefficient of 0 to 0.48 at a section lift coefficient of 0.70 or only 4 percent and, when measured between \( \delta_a = 17^\circ \) and \( \delta_a = -17^\circ \) decreased from 0.50 to 0.45 or 10 percent over the same lift-coefficient range.

Hinge moment. The variations of aileron section hinge-moment coefficient \( c_{h_a} \) with section angle of attack \( \alpha_o \) for all aileron deflections tested are presented in figure 23(a).

The irregularities in \( \frac{\partial c_{h_a}}{\partial \alpha_o / \partial \delta_a} \) shown by these curves are probably caused by the sudden movements in transition on the upper and lower airfoil surfaces at the extremities of the low-drag range. (See fig. 25.) No sharp irregularities are apparent, however, in the
variation of $c_{ha}$ with aileron deflection as shown by the curves of figure 23(b). The values of $\frac{\partial c_{ha}}{\partial \alpha_{a}}$ and $\frac{\partial c_{ha}}{\partial \delta_{a}}$ are 0.0004 and -0.0013, respectively, for the aerodynamically smooth airfoil.

The variation of the pressure difference across the aileron balance seal $\Delta p/q_0$ with $\alpha_a$ is presented in figure 24 for all aileron deflections tested. The basic data of figures 23(a) and 24 may be used to estimate the section characteristics of an aileron of similar contour and chord with any amount of sealed internal balance by the methods of reference 1.

Drag. - The variation of section drag coefficient with section lift coefficient at a Reynolds number of approximately $6 \times 10^6$ for aileron deflections of $0^\circ$, $5^\circ$, and $-5^\circ$ is presented in figure 25. The minimum section drag coefficient was approximately the same for the three aileron deflections, although the extent of the low-drag range was reduced with the aileron deflected $\pm 5^\circ$ to about one-half the range with the aileron neutral.

Effects of Sudden Movement of Transition on Airplane Control-Surface Characteristics

The two-dimensional data presented herein show sudden changes in the variation of control-surface section hinge-moment coefficient with airfoil section angle of attack when transition suddenly moves forward along the airfoil surfaces. The effect of sudden movements of transition on the airplane control forces was investigated. In order to determine whether the irregularities in the two-dimensional hinge-moment characteristics would cause unusual aileron wheel-force characteristics, the variation of wheel force $F_w$ with wing-tip helix angle $pb/2V$ for an assumed airplane was estimated for various indicated airspeeds (fig. 26). The values of $pb/2V$ were estimated from the following equation presented in reference 4:
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\[ \frac{pb}{2V} = \frac{C_{L_0}}{k} \frac{K \Delta \delta_a}{114.6 C_{L_p}} \]  (1)

Test values of \( \Delta \alpha_0 \) were substituted in equation (1) for the product \( k \Delta \delta_a \) and values of \( C_{L_0} \) and \( C_{L_p} \) equal to 0.331 and 0.495, respectively, were obtained from reference 4 by use of the following assumed airplane dimensions:

- Wing span, feet: 70.5
- Wing area, square feet: 55.4
- Wing loading, pounds per square foot: 45
- Aspect ratio: 9
- Taper ratio: 0.3
- Aileron span, feet: 11.5
- Aileron root-mean-square chord behind hinge axis, feet: 1.8
- Aileron location, fraction of semispan:
  - Inboard end: 0.668
  - Outboard end: 1.000
- Wheel diameter, feet: 1.083
- Maximum wheel deflection, degrees: 175°

Wheel forces were estimated from the equation

\[ F_w = \frac{q b \delta_a^2}{\text{Wheel radius}} \left[ \left( \frac{d \delta_a}{d \theta} \right)_{\text{up}} (c_{h_a})_{\text{up}} - \left( \frac{d \delta_a}{d \theta} \right)_{\text{down}} (c_{h_a})_{\text{down}} \right] \]  (2)

The aileron hinge-moment coefficients \((c_{h_a})_{\text{up}}\) and \((c_{h_a})_{\text{down}}\) were estimated from the section data for the airplane in a steady roll. Values of these coefficients were taken at given aileron angles and corrected for the change in angle of attack at the aileron midspan caused by the roll. Equal up and down aileron deflections and a maximum wheel deflection of 175° were used.

Because the values of \( pb/2V \) were not corrected for wing twist, control-system stretch, or adverse yaw and the section hinge-moment coefficients were not corrected for
aspect-ratio effects, the estimated values of \( \frac{pb}{2V} \) and \( F_w \) are not quantitatively accurate. The values are useful, however, to show the qualitative variation of wheel force with wing-tip helix angle.

No sudden changes in the estimated variation of \( F_w \) with \( \frac{pb}{2V} \) are apparent in figure 26, which indicates that inclusion of the hinge moments due to the deflection of both ailerons tends to eliminate the irregularities in the hinge-moment variation with angle of attack alone. If the angle of attack were varied with the ailerons neutral, however, both the right and left ailerons would tend to move in the same direction when the change in angle of attack causes transition to move forward suddenly, and the effect would be absorbed in the aileron rigging with no change in the wheel force.

Data recently obtained in the Langley stability tunnel indicate that sudden movements of transition cause irregularities in the variation of hinge-moment coefficient with angle of attack in three-dimensional flow as well as in two-dimensional flow. Sudden movements of transition along the surfaces of vertical-or horizontal-tail sections, therefore, will probably cause sudden changes in rudder or elevator hinge moments. The data obtained with transition fixed at various locations along the airfoil surfaces, however, indicate a decrease in the severity of the jogs in the variation of \( c_h \) with \( \alpha \) as the location of transition is moved toward the airfoil leading edge. Sudden changes in elevator and rudder forces, therefore, seem less likely to occur on an airplane since the full extent of laminar flow on production airplanes has not been realized because of manufacturing irregularities and surface deterioration in service and because transition is induced near or at the leading edge of tail surfaces that are located within the propeller slipstream or wing and fuselage wake.

**CONCLUDING REMARKS**

Results of a two-dimensional wind-tunnel investigation of a low-drag vertical-tail, horizontal-tail, and wing section equipped with sealed internally balanced control surfaces have been presented. Sharp irregularities occurred in the variation of the control-surface section
hinge-moment coefficient with section angle of attack, which were probably caused by sudden movements in transition along the surfaces of the airfoils at the extremities of the low-drag range. Tests of the vertical-tail section indicated that these irregularities were reduced in magnitude when transition was fixed at a forward chordwise position but were not entirely removed until transition was fixed at the airfoil leading edge. An estimated variation of aileron wheel force with wing-tip helix angle for an assumed airplane indicated that no unusual aileron wheel-force characteristics would be caused by the irregularities in the two-dimensional hinge-moment characteristics. Sudden changes in rudder or elevator hinge moments, however, would probably result from sudden movements in transition along the surfaces of the vertical- or horizontal-tail sections. If transition should occur at or near the leading edge of the tail surfaces, as is usually the case for tail surfaces located within the propeller slipstream or wing and fuselage wake, no sudden changes would occur in the control-surface hinge moments.

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National Advisory Committee For Aeronautics
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REFERENCES


Vertical-tail section

Horizontal-tail section

Wing section

Figure 1.- Vertical-tail, horizontal-tail, and wing sections.
Figure 2.- Theoretical pressure distribution at zero lift of the low-drag vertical-tail section.
Figure 3. – Theoretical pressure distribution at a section lift coefficient of -0.053 of the low-drag horizontal-tail section.
Figure 4.- Theoretical pressure distribution at a section lift coefficient of 0.266 of the low-drag wing section.
Figure 5.— Lift characteristics of a low-drag vertical-tail section equipped with a 0.400 sealed internally balanced rudder. Smooth condition; $R = 6 \times 10^6$ (approx.); test, TDT 582.
Figure 6.- Variation of $\Delta C_L$ with $\delta_r$ at constant $\alpha_0$ for a low-drag vertical-tail section equipped with a 0.40c sealed internally balanced rudder. Smooth condition; $R = 6 \times 10^6$ (approx.).
Figure 7. - Lift characteristics of a low-drag vertical-tail section equipped with a 0.40c sealed internally balanced rudder.
Smooth condition; $\delta_r = 0^\circ$; test, TDT 582.
Figure 8 - Lift characteristics of a low-drag vertical-tail section equipped with a 0.40c sealed internally balanced rudder. Strips of 0.002-inch carborundum grains on both airfoil surfaces at various chordwise positions; $R = 6 \times 10^6$ (approx.); test, TDT 585.
Figure 9.- Hinge-moment characteristics of a 0.40C sealed internally balanced rudder on a low-drag vertical-tail section. Smooth condition; $R = 6 \times 10^6$ (approx.); test, TDT 584.
Figure 10. - Concluded.
Figure 11—Variation of \( \frac{\Delta p}{\rho} \) with \( \alpha \) for a 0.4\( \alpha \) sealed internally balanced rudder on a low-drag vertical-tail section. Smooth condition; \( R = 6 \times 10^6 \) (approx.); test, TDT 584.
Figure 12.—Variation of $\frac{\Delta p}{\rho_0}$ with $\alpha_o$ for a 0.40c sealed internally balanced rudder on a low-drag vertical-tail section. Strips of 0.002-inch carborundum grains on both airfoil surfaces at various chordwise positions; $R = 6 \times 10^6$ (approx.); test, TDT 585.
Figure 14.- Drag characteristics of a low-drag vertical-tail section equipped with a 0.40c sealed internally balanced rudder. Strips of 0.002-inch carborundum grains on both airfoil surfaces at various chordwise positions; $Re = 6 \times 10^6$ (approx.); test, TDT 585.
Figure 15. - Lift characteristics of a low-drag horizontal-tail section equipped with a 0.350 sealed internally balanced elevator.

\[ R = 6 \times 10^6 \text{ (approx.)}; \text{ tests, TDT 581 and 589.} \]
Figure 16.- Variation of $\Delta c_l$ with $\delta_\epsilon$ at constant $\alpha_o$ for a low-drag horizontal-tail section equipped with a 0.35s sealed internally balanced elevator. $R = 6 \times 10^6$ (approx.).
Figure 17 - Lift characteristics of a low-drag horizontal-tail section equipped with a 0.35c sealed internally balanced elevator. $\delta_e = 0^\circ$; test, NDT 581.
Figure 18. - Hinge-moment characteristics of a 0.35o sealed internally balanced elevator on a low-drag horizontal-tail section.

\[ R = 6 \times 10^6 \text{ (approx.)}; \text{ tests, NDT 581 and 589}. \]
Figure 19.- Variation of ΔP with $\Delta \alpha_0$ for a 0.35s sealed internally balanced elevator on a low-drag horizontal-tail section. $R = 6 \times 10^6$ (approx.); tests, DTP 581 and 589.
Figure 20: Drag characteristics of a towed horizontal tail section equipped with a flap and an elevator.
Figure 21. - Lift characteristics of a low-drag wing section equipped with a 0.22-secret sealed internally balanced aileron.  $R = 6 \times 10^6$ (approx.); test, DT 585.
Figure 22.- Variation of $\frac{\Delta a_c}{\Delta \delta_a / c_l}$ with $c_l$ for a low-drag wing section equipped with a 0.220 sealed internally balanced aileron.

$R = 6 \times 10^6$ (approx.)
Figure 23. - Hinge-moment characteristics of a 0.22c sealed internally-balanced aileron on a low-drag wing section. 

$R = 6 \times 10^6$ (approx.); test, TDT 563.
Section hinge-moment correction, $c_{ha}$.
Figure 24. - Variation of $\frac{A_p}{q_o}$ with $\alpha_0$ for a 0.22c sealed internally balanced aileron on a low-drag wing section. $R = 6 \times 10^6$ (approx.); test, TDT 583.
Figure 25. - Drag characteristics of a low-drag wing section equipped with a 0.22c sealed internally balanced aileron. 
$R = 6 \times 10^6$ (approx.); test, NDT 583.
Figure 26.—Variation of aileron wheel force with wing-tip helix angle.