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Focusing of Dispersive Targets Using Synthetic Aperture Radar

by John McCorkle and Lam Nguyen

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Focusing of Dispersive Targets Using Synthetic Aperture Radar

by John McCorkle and Lam Nguyen
The focusing of synthetic aperture radar (SAR) data presents problems to the designer. This report addresses the SAR focusing problem with special attention to focusing an area in the near field of the synthetic aperture over a decade or more of bandwidth in a manner that preserves target resonance characteristics. A method for solving this image formation problem is described, along with a computationally efficient algorithm that is applicable to real-time processing with motion compensation. Simplified program examples are given, as well as a complete program listing that executes on several single-chip array processors simultaneously. An error analysis shows quantitatively when the depth of focus is adequate to preserve long-duration target resonance ringing effects for a given target Q, geometry, and bandwidth.
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1. Introduction

Over the past 40 years, studies have been made [1-4] of the process of obtaining images of the reflectivity or density of target areas that are rotating and translating with respect to a sensor such as a monostatic or bistatic radar, a sonar, or an x-ray CAT scanner. Ausherman et al [5] have written an excellent review of the work done in this area. Target areas that rotate and translate relative to a radar include, for example, planet surfaces observed from a satellite, ground terrain observed from airborne platforms, subsurface objects and voids observed from moving vehicles, and people scanned by a rotating x-ray system. Although the processing described is applicable to other systems, this report treats the topic from the point of view of a synthetic aperture radar (SAR).

In the SAR application, as the aspect angle between the sensor and a target changes with time, the sensor collects a sequence of signal records. After data are collected for $T$ seconds, the aspect angle has changed by $\theta$ degrees. These received signals are then coherently processed to produce the reflectivity profile of the target area. Down-range resolution into range bins is determined primarily by the bandwidth of the sensor. Cross-range resolution is obtained primarily by coherent processing of the received signals so that a very wide aperture is simulated: an aperture that is $\theta$ degrees wide.

Implementation and study of image formation processing have been limited in two ways. First, the image formation processing has assumed that targets are isotropic point scatterers, although many targets are anisotropic resonant scatterers. Treatment of resonant scattering becomes important when the sensor spectrum covers the Rayleigh, resonant, and optical regions of a family of targets. For example, discrimination between scatterers can be based on the unique signature of each target. But in order for the discrimination to work in the context of microwave reflectivity imaging, the information in the signature must be preserved during the image formation process.

The second limitation in previous work is that systems with relatively narrow bandwidth have been assumed. For example, the compressed pulse width of the sensor is assumed to be at least several and usually many cycles of an rf carrier frequency. So a single range bin is derived from several cycles of the carrier. Newer UWB (ultra-wide-bandwidth) sensors, however, have made it possible to make the image range-bin size roughly half the wavelength of the highest frequency in the sensor’s spectrum. The bin size is much smaller (1/10 or less) than the wavelength of the lowest frequency in the spectrum. This wide bandwidth exacerbates range walk and wavefront curvature errors to the point where conventional fast Fourier transform (FFT) based processing must be restricted to very small patches within an image area.
These two limitations are not independent. It is bandwidth that allows target discrimination based on signature analysis, and it is bandwidth that makes image formation more difficult. The purpose of this report is to examine image formation processing that preserves resonant target signatures and to present an efficient method of solving the microwave reflectivity imaging problem for UWB signals and resonant targets.
2. Background

2.1 Terminology

SAR systems depend upon collecting data coherently along a path. This path is referred to as the “synthetic aperture.” Figure 1 shows a sketch of the scenario projected onto a plane. An aircraft carrying the SAR system flies at some elevation $h$ above the ground, over a distance $L_y$ to form the synthetic aperture. The image area grid is referenced to the center of the aperture. Range is marked off by the parameter $i$. The parameter $k$ marks off azimuthal (bearing) lines. The sample points in the aperture are marked off by the parameter $j$. The distance between the $j^{th}$ point in the aperture and the $(i,k)^{th}$ position in the image area is denoted by $d_{i,j,k}$. Both the azimuthal lines and the range lines are referenced to the center of the aperture.

(Although nearly all operational SAR systems use a rectangular grid, the advantages of a polar grid are that for a ringing target, the grid provides equally spaced samples of the ring-down, and these samples are optimally focused and on a single bearing line. These features make it easy for postprocessors to look for specific ringing signatures.)

2.2 Approaches to Focusing

A “Doppler” paradigm is often used in discussions of SAR processing, or SAR focusing. Referring to figure 1, assume that the radar platform is moving at velocity $v$ as it collects data along the aperture. Therefore, the data collection points are spaced equally in time, occurring at a rate governed by $v$ and the PRF. (This sampling across the aperture is sometimes referred to

![Image of basic flight path and image area geometry](image)

* This grid is convenient for postprocessing. An x-y grid can also be computed with the techniques described.
The classic "polar formatting" [6] approach to computing a SAR image adjusts (time shifts) the data at each aperture point so that the new data set appears as if the platform had moved in a short circular path, with the circle at the center of the image area. Once this formatting is done, a target at the center point has the unique Doppler profile of zero over the entire aperture. Other points have other unique Doppler profiles.

A Fourier transform is typically used to recover the image from the Doppler profiles. This approach works well as long as the circular path is sufficiently short, the image area sufficiently small, the signal bandwidth sufficiently small, and the distance from the radar to the image center sufficiently long. This report addresses the case where none of these restrictions apply.
Although the Doppler paradigm has helped countless people to visualize SAR focusing, it is not necessary, nor always helpful, in solving the SAR focusing problem. For example, Doppler shift, which is defined as $2v/\lambda$, works fine when $\lambda$ varies by a few percentage points, but it becomes a stumbling block in the UWB case where $\lambda$ can vary by 10 or 100 to 1. Thus, although Doppler has proven to be a very convenient narrow-band concept, its convenience breaks down at wide relative bandwidths.

The focusing problem can also, however, be looked at as a stationary array of $N$ antennas whose outputs are digitally stored and combined in a computer to form beams. We believe that the focusing problem is easier to visualize and solve within this stationary array paradigm when neither the geometry nor the bandwidth are restricted. In this paradigm one can see that equation (1) coherently focuses the SAR data by summing across the array:

$$f_{i,k}(t) = \sum_j s_j (T_{i,k,l} + t) \text{ for } t \geq 0 .$$

Both the Doppler and stationary array approaches can be seen to be identical at the center point of the "polar format" patch. Notice that regardless of carrier frequency, the center point of the polar formatted data is always analyzed by the dc term of the Fourier transform, which is simply a summation of the data points. The summation shown in equation (1) is identical to finding the dc term of the polar formatted SAR data. But instead of formatting once and then finding many "Doppler" profiles via an FFT, equation (1) formats and "sums" the data many times; each formatting makes a different pixel the center, and then the dc term summation is used to calculate the value for that pixel. The result is that optimally focused beams are formed—beams taking full advantage of both the entire aperture and the entire signal bandwidth. The focusing is truly frequency independent.

How does the beam width compare with that obtained from "conventional" (far-field narrow-band) antenna theory? The rule-of-thumb half-power beamwidth of a line array is approximately $\lambda/L$, where $L$ is the length of the array. The beams formed by the processing described above follow this rule and have a width proportional to $\lambda$. Low frequencies have wide beams, and high frequencies have narrow beams. This fact has interesting consequences in the time domain as a source moves through a beam. Although the impulse response at the center of the beam is a narrow pulse, as one moves away from the center, the impulse response broadens. This time-domain broadening occurs because more and more high-frequency energy is lost as the source moves out of the narrowing high-frequency beam.

The switch from the Doppler to the stationary array approach may lead to thinking in "phased array" terms. Such an approach is a mistake when bandwidth and/or geometry are not restricted. Whenever the geometry is not restricted to the far field of an aperture, plane-wave simplifications
break down. This breakdown invalidates simple phase steering. Since a Fourier transform forms beams by simple phase steering, Fourier techniques becomes less and less useful as targets move into the near field. In a UWB system, phase becomes meaningless with regard to defining element positions or the beam-forming network. To speak of shifting one element 180° with respect to another element implies a fixed $\lambda$. If, for example, $\lambda$ changed by 2 to 1, then a delay line that provided 180° at one frequency would provide 360° at the other. Yet delay lines are precisely the element needed to build a wide-bandwidth “phased-array” antenna. When $\lambda$ varies several octaves, the best parameters to use in the equations defining the antenna are the time and distance: the time shift of the delay lines that form the beam-forming network, and distance between antenna elements. Thus it is best to think in “timed-array” terms. This time-based framework results in derivations that are frequency and geometry independent.

### 2.3 Null Steering, Pattern Forming, and Grating Lobes

Generally, an antenna designer would say that the most critical aspect of making desirable antenna patterns is forming nulls. A simple classic case is spacing two elements at 90° and phasing them by 90° to form an endfire beam in one direction and a null in the opposite direction. In the simplest case (where the element weighting is +1 and −1), to form a UWB null one could time-steer the array to where the null should be, and then invert half the elements before summing. Of course, using other weighting factors allows more freedom. An impulse signal $\delta(t)$ coming from a direction other than the null would produce in the receiver some array-induced waveform. If we ignore bandwidth effects from each element, that waveform would be a function of the + and − weighting and element spacing. By definition, that waveform is the antenna-array impulse response for that beam angle. Matched filtering to that waveform forms a main lobe in that direction.

Grating lobes are customarily defined as lobes whose gain is equal to the main beam. However, this definition leads to confusion in the UWB case. Are there grating lobes? That depends. If the response to the UWB signal is seen as an impulse, then the answer is no. Since the peak response on the main lobe is higher than the response at any other angle, the definition fails. On the other hand, the antenna is a linear system. It behaves just like an identical array operating at a single frequency. So, if the response is to a cw signal, the answer can be yes. If the elements are physically spaced more than $\lambda/2$ apart at the highest frequency component in the UWB waveform, then there certainly will be a grating lobe at that frequency component. All the insight gained from cw antenna analysis holds and remains useful. One must, however, be careful when applying terms like grating lobes that presuppose a narrow-band signal. For SAR, the element spacing (velocity/PRF) needed will be a function of what sidelobes are permissible at the various frequency components in the UWB waveform.
2.4 Target Resonance Effects

Historically, the relative bandwidth of radars has been sufficiently small that a target's echo is adequately modeled by a single number, $\sigma$, the radar cross section (RCS), usually given in square meters. When $\mu \geq 0.5$, however, a single number may no longer be adequate—$\sigma$ is a function of frequency. For example, figure 2 is a plot of the RCS of a sphere. In addition to the magnitude characteristic plotted, there is also a phase characteristic. These two frequency-domain characteristics can also be represented in the time domain by a ringing or resonant response. In either case—time domain or frequency domain—the waveform in the plots can be referred to as the impulse response of the target.

Since historical SAR systems have not been designed to respond to target ringing, no attention was paid to preserving the ringing information. This report describes and analyzes a procedure to focus a large array, over ultra-wide bandwidths, in such a way as to preserve the resonant response of targets, even when they are in the near field.

![Figure 2. Radar cross section of a sphere.](image)
3. Fundamental Time-Based Physical Array Approach

Consider an aperture looking at completely empty space except for an isotropic scatterer at position \((i,k)\). Also assume that an ideal impulse \(\delta(t)\) is broadcast. It is desirable to take advantage of all the echo energy across the aperture. To do that, one must sum the energy from all collection points along the synthetic aperture. However, this summation must be done so that the energy adds coherently at all frequencies. Frequency-independent adding is accomplished as

\[
f_{i,k}(t) = \sum_j s_j(T_{i,k,j} + t) w_j \quad \text{for } t \geq 0.
\]  

Here, \(f_{i,k}(t)\) would be the impulse response of the target located at position \((i,k)\). Note that the \(T_{i,k,j}\) term time shifts the received signals \(s_j\) so that the target impulse response starts at \(t = 0\) at all points in the aperture. The \(w_j\) term is simply an amplitude tapper across the aperture.

The above discussion assumes that a target's impulse response is sufficiently similar at all points along the aperture for equation (1) to be considered true. The response of a vertical dipole, for example, does not change depending on where the radar is positioned in the aperture. It is therefore an isotropic target.

Suppose we relax the isotropic requirement, and suppose that a complex scatterer is at position \((i,k)\) in the image area. A horizontal dipole, for example, is an anisotropic target. We could take advantage of the anisotropic behavior to extend the detection and target recognition performance of the radar by rewriting equation (1) as

\[
f_{i,k}(t) = \sum_j y_j(T_{i,k,j} + t) \quad \text{for } t \geq 0,
\]  

where \(y_j(t) = s_j(t) \otimes x_j(t)\) and the convolution step represents filtering. In this case, a set of filters \(X_j(\omega)\) would be needed, each one matched to the target response at the bearing of the \(j^{th}\) position in the aperture. In order to simplify the rest of this report, we use equation (1) as the fundamental equation. Nonetheless, one must recognize that real targets are complex anisotropic polarimetric scatterers; this fact should not be ignored for large arrays.
4. Short Impulse Response Approximation

A typical 2-D SAR image is simply the echo magnitude mapped to intensity. Equation (1) expands the typical 2-D image into a 3-D image with the target ringing along the third dimension. Given the heavy computational load of typical SAR processing, if it is required that an \( f(t) \) (rather than a single value) be computed for every pixel, then a massive computer would be needed. The impact of this computational load is even worse when one considers that the mass of resulting data must be analyzed in the target-detection/identification phase. This section defines an approximation that reduces the problem back to a 2-D case and presents an error analysis of the approximation.

4.1 Theory

The problem is that we have added a third dimension to measure target ringing. Note, however, that if there was only one aperture position, then ringing of the target would appear in pixels only behind the target. Even with an aperture of many positions, ringing will appear behind the target. But since the geometry is not constrained, and near-field operation is presumed, the antenna beam defocuses behind the target.

Equation (1) will perfectly focus ringing of unbounded duration. For practical purposes, however, the target rings only for a finite duration, say \( M \) range bins. The question is, given that the ringing is finite in duration, can the ring information be retained in a 2-D image? In other words, suppose that instead of calculating a time series \( f_{i,k}(t) \) for each pixel in the image, only one value is calculated, for example, \( f_{i,k}(\tau) \), where \( \tau \) is fixed for the image. If the ringing can be retained in this 2-D image, then computational load is greatly reduced. The aim of this section is to describe and quantify the error bounds when a 2-D image \( f_{i,k}(\tau) \) is used.

First, define \( \alpha \) to be the round-trip time it takes the radar pulse to traverse one range bin on the polar grid; that is,

\[
\alpha = t_{r,i,k,j} - t_{i,k,j}; \forall k, \text{ and } j = 0 .
\]  

Since the grid for the image has been defined to be referenced to the center of the aperture (the \( j = 0 \) position), the \( i \) parameter can be thought of as a quantized time \( t \) parameter. While \( t \) is in units of seconds, \( i \) is in units of range bins, and they are related by \( \alpha \)—one range bin equals \( \alpha \) seconds. Now we can write

\[
s_j(T_{i,k,j} + m\alpha) = s_j(T_{i,m,k,j}) \quad \text{for} \quad \begin{cases} \text{case 1:} & j = 0, \forall m, \forall i, \forall k \\ \text{case 2:} & m = 0, \forall j, \forall i, \forall k \end{cases}
\]  

(4)
We make an approximation to equation (4), generalizing it to include all aperture points over a limited range of \( m \) to arrive at

\[
s_j(T_{i,k,j} + m\alpha) = s_j(T_{i,m,k,j}) \quad \text{for } \forall i, \forall k, \forall j, m = -M \ldots M . \tag{5}
\]

The following may be said of the approximation in equation (5).

1. It is perfect at the center of the aperture (\( j = 0 \)) regardless of \( m \).
2. It is perfect at \( m = 0 \) regardless of \( j \).
3. It gets worse as \( m \) deviates further from zero.
4. It is worst at the end points of the aperture.

A solution is desired to equation (1) in the form of \( f_{i,k}(\tau) \), where \( \tau \) is a constant. In a practical system, \( \tau \) will be mapped to discrete range bins, so let

\[
\tau = n\alpha . \tag{6}
\]

Substituting equations (5) and (6) into (1), we define a 2-D "image" \( f(i,k) \) as

\[
f_{i,k}(\tau) = \sum_j s_j(T_{i,k,j}) = f_{i-n,k}(n\alpha) = \sum_j s_j(T_{i-n,k,j} + n\alpha) = f(i,k) . \tag{7}
\]

If one thinks of a ringing target, then equation (7) can be described as allowing the point of perfect focus to be adjusted to any depth \( n \) in the ring. For example, if \( n = 0 \), then the perfect focus point would be at the leading edge (the first sample) of the ringing response. If \( n \neq 0 \), say \( n = 3 \), then the third sample of the ringing response would be perfectly focused.

Next consider the indexing. The indexing is performed such that \( f(i,k) \) always represents the leading edge of the response from a target located at \( (i,k) \) regardless of whether it is perfectly focused or not. Once \( f(i,k) \) is found, we now wish to find the discrete samples of the target ringing. The samples will be counted as \( m = 0 \) for the first sample, \( m = 1 \) for the second, and so on. We obtain these samples by simply incrementing the \( i \) index. The \( m \)th value is just \( f(i + m,k) \), which follows from equations (5) and (7) as

\[
f_{i,k}(m\alpha) = f_{i-n,m,k}(n\alpha) = f(i + m,k) , \quad \text{or}
\]

\[
\sum_j s_j(T_{i,k,j} + m\alpha) = f_{i-n,m,k}(n\alpha) = f(i + m,k) . \tag{8}
\]

Clearly equation (8) is identical to equation (1) (i.e., perfect) when \( m = n \). So equation (8) gives perfect focus at \( m = n \). The name "short impulse response approximation" is used because the approximation needs to remain accurate only over the duration of a target's impulse response.
4.2 Examples of Applying Approximation

To illustrate the use of equation (8), we follow these steps:

1. Fix $n$.

2. Place a target (for the purposes of the illustration) at say $i = 237$ in range on the $k^{th}$ bearing.

3. Use equation (7) to calculate $f(i, k)$ for all $(i, k)$.

The cases of interest are where $n = 0$ and where $n \neq 0$. Let us consider each separately.

4.2.1 Case where $n = 0$

Where $n = 0$, use equation (8) to find the ringing response of the target. The response for the first three points of the focused impulse response is

\[ f_{237, i}(0) = f_{237, i+m, k}(0) = f_{238, k}(0) = f(237, k) \]  \quad \text{(case for } m = 0) ,
\[ f_{237, i}(\alpha) = f_{237, i+m, k}(\alpha) = f_{238, k}(\alpha) = f(238, k) \]  \quad \text{(case for } m = 1) ,
\[ f_{237, i}(2\alpha) = f_{237, i+m, k}(2\alpha) = f_{239, k}(2\alpha) = f(239, k) \]  \quad \text{(case for } m = 2) .

Since $n = 0$, the amplitude of the leading edge ($m = 0$) of the impulse response of that target is perfectly focused. As $m$ increases, the approximation gets worse. So the approximation is useful as long as the target resonance dies before the approximation gets too bad.

4.2.2 Case where $n \neq 0$

Where $n \neq 0$, perfect focus is $n\alpha$ seconds past the leading edge of the target impulse response. Suppose, for this example, $n = 2$. The first four data points for the impulse response are

\[ f_{237, i}(0) = f_{237, i+m, k}(n\alpha) = f_{238, k}(2\alpha) = f(237, k) \]  \quad \text{(case for } m = 0) ,
\[ f_{237, i}(\alpha) = f_{237, i+m, k}(n\alpha) = f_{238, k}(2\alpha) = f(238, k) \]  \quad \text{(case for } m = 1) ,
\[ f_{237, i}(2\alpha) = f_{237, i+m, k}(n\alpha) = f_{238, k}(2\alpha) = f(239, k) \]  \quad \text{(case for } m = 2) ,
\[ f_{237, i}(3\alpha) = f_{237, i+m, k}(n\alpha) = f_{238, k}(2\alpha) = f(240, k) \]  \quad \text{(case for } m = 3) .

Note that the leading edge is not perfectly focused, as it was when $n = 0$. The important point here is that one can choose $n \neq 0$ to allow the leading edge to defocus slightly for the sake of keeping later points in better focus.
5. Error of Short Impulse Response Approximation

Landt, Miller, and Van Blaricum [7] show the transient echo response of a thin (high-$Q$) dipole. Its ringing is damped after five cycles. This response allows one to gain an intuitive idea of the kind of range needed in the approximation. A 1/2-ft dipole should ring for five cycles at 1 GHz. If the A/D sampler collects data at 2 Gs/s and $\tau = 0$, then at $m = 10$, data for all five cycles will have been collected. If the dipole were 5 ft long, then it would ring for five cycles at 100 MHz. So at $m = 100$, data for the five cycles will be collected. Generally, high frequencies damp quickly and low frequencies damp slowly.

Figure 3 illustrates the geometry of the approximation. The discussion assumes this geometry. If a target is located at $(i,k) = (237,0)$, then $R$ is the distance from the center of the array to the target; $a_1$ is the distance from the end of the array to the target; and $f_{237,0}(t)$ is the perfectly focused data point for the impulse response of the target. The next point ($m = 1$) in the impulse response is approximated by $a_2 = a_1 + \alpha_d$, or in general $a_m = a_1 + m\alpha_d$. If $\varepsilon$ is the difference (error) between the approximation and the actual, then

$$\varepsilon = \left( a_1 + m\alpha_d \right) - a_2$$

$$= \sqrt{R^2 + \frac{L_2}{2} - L_zR \cos \theta + m\alpha_d} - \sqrt{(R + m\alpha_d)^2 + \frac{L_2}{2} - L_z(R + m\alpha_d)\cos \theta}. \quad (9)$$

As an example of finding the approximation error, suppose $R = 2$ km, $\theta = 90^\circ$, $L_z = 1$ km, and $m = 10$. How many degrees off (round trip) would the end point be at 1 GHz? Plugging these numbers into equation (9), we find $\varepsilon = 0.0447$ m. So the round trip phase error at 1 GHz is $107^\circ$. Figure 4 is a plot of the error as a function of the position in the aperture for $\theta = 90^\circ$, 76°, 50°, and 30°. A peculiar characteristic is that the error peaks at 76°. This peaking is a result of working at a range of only twice the aperture length. Figures 5 and 6 show the error as a function of the beam angle $\theta$, for $m = 5, 10, 15$, and 20 at two ranges.

Figure 7 is a plot of the error at the right end point of the aperture as a function of $m$, with $\tau = 0$. Since the error at the right end is greater than the error at the left end for $\theta$ angles below $90^\circ$, this is the worst case. Figure 8 is the same plot but with $\tau = n\alpha$ and $n = 4$. In this case, the leading edge of the impulse response (at $m = 0$) is out of focus by about $45^\circ$ at 1 GHz. Perfect focus occurs when $m = n = 4$.

Figures 4 through 8 give an indication of the bounds over which a five-cycle ring of a high-$Q$ scatterer is adequately captured by the approximation used in equation (4). These figures also show that making $\tau = 0$ can double the depth of focus on resonant targets. The optimum $\tau$, however, depends on the frequency and $Q$ of the resonance.
Figure 3. Geometry for calculation of approximation error.

Figure 4. Error as a function of position in aperture.

Figure 5. Error as a function of $\theta$ with $R/L_s = 2$.

Figure 6. Error as a function of $\theta$ with $R/L_s = 6$.

Figure 7. Error at right aperture end as a function of $m$, where $\tau = 0$.

Figure 8. Error at right aperture end as a function of $m$ where $\tau = 4\alpha$. 
6. Efficient Calculation

Fast focusing can be broken into three stages: (1) preprocessing raw data, where interpolation is performed; (2) computing a set of polynomial coefficients that will be used for fast index calculation; and (3) performing the focusing summation of equation (7) using the coefficients found in stage 2 to find the index corresponding to the proper time shift.

6.1 Preprocessing

A method to efficiently implement time shifting is needed. The SAR data are collected by an A/D converter that outputs a vector of $N$ numbers (voltages) at each aperture position. We call this vector $\tilde{s}_j(i)$. A time shift is, therefore, simply a shift in the index $\tilde{i}$.

Typically, the time shifting obtained by indexing on the original $N$-point vector is not fine enough. Finer resolution is gained by a two-stage interpolator. First, a high-quality interpolator is used to produce a new $K$-point vector $s_j(i)$. It is usually implemented by insertion of $Z - 1$ zeros between each data point in the original vector, after which the new sequence is passed through a low-pass FIR (finite impulse response) filter. The process results in a new vector with nearly the desired time-shift resolution. The length, in this case, is $K = ZN$. We can gain extra fine resolution by using a floating-point index with simple linear interpolation to find a value between any two data points in the interpolated data vector. For example, if the index $\tilde{i}$ were 6.3, then the interpolated value would just be $0.7s_j(6) + 0.3s_j(7)$.

The focusing algorithm that follows uses these techniques in the following sequence, which is typically referred to as back projection.

1. Read in one $N$-point vector $\tilde{s}_j(\tilde{i})$ of raw data.

2. Do an $Z$-point interpolation, to form a new $K$-point vector $s_j(i)$.

3. Iterate for all pixels:
   a. Find the floating point index needed for a pixel.
   b. Find the data value for that pixel either by rounding the index and grabbing the value, or by linearly interpolating between adjacent values.
   c. Sum into that pixel the data value obtained.
6.2 Fast Index Calculation

6.2.1 Approach

Typically, the greatest computational load in back-projection focusing is in finding the index. Let \( P(i,k,j) \) be the exact index needed. Then equation (7), the 2-D focusing equation, becomes

\[
f_{i,k} = \sum_j s_j(P(i,k,j)) .
\]

Calculating \( P(i,k,j) \) exactly involves 3-D trigonometric solutions for every pixel in the image at every position in the aperture. Such a calculation would be prohibitively large. For practical implementation, a secondary approximation is used to speed the computations. Extremely efficient computational methods exist for finding evenly spaced solutions to polynomials. Therefore, our approach is to define a polynomial in three variables \( G(i,k,j) \), where \( G(i,k,j) \approx P(i,k,j) \), and use \( G \) to compute the index.

The first issue that arises is choosing the order of the polynomial needed for each variable. To understand the method, suppose that a second-degree polynomial is adequate for each of the three variables \( i,k,j \). Now the problem can be restated as follows: for a given image pixel \((i,k)\), and a given aperture position \((j)\), find the coefficients \( a_m \) for \( m = 0...26 \) such that

\[
G(i,k,j) = P(i,k,j)
\]

\[
= g_{0,i,j} + g_{1,i,j} i + g_{2,i,j} i^2
\]

\[
= [c_{0,j} + c_{1,j} k + c_{2,j} k^2] + [c_{3,j} + c_{4,j} k + c_{5,j} k^2] j + [c_{6,j} + c_{7,j} k + c_{8,j} k^2] j^2
\]

\[
= [(a_0 + a_{1,j} i + a_{2,j} i^2) + (a_{3} + a_{4,j} + a_{5,j} j) k + (a_{6} + a_{7,j} + a_{8,j} j) k^2]
\]

\[
+ [(a_{9} + a_{10,j} i + a_{11,j} i^2) + (a_{12} + a_{13,j} + a_{14,j} j) k + (a_{15} + a_{16,j} + a_{17,j} j) k^2] j
\]

\[
+ [(a_{18} + a_{19,j} + a_{20,j} j^2) + (a_{21} + a_{22,j} + a_{23,j} j^2) k + (a_{24} + a_{25,j} + a_{26,j} j^2) k^2] j^2 .
\]

With the equation written in this format, it is easy to see that one can code the index calculation as loops nested three deep, with \( j \) as the outer loop, \( k \) as the middle loop, and \( i \) as the inner loop.
6.2.2 Solving for the Coefficients

The coefficients $a_m$ can be found numerically. The approach is to calculate the exact index required for $M$ points in the image at each of $H$ positions in the aperture, and do a least-squares fit to find the coefficients $a_m$ for $m = 0...26$. We can find a generic solution to this problem, for arbitrary image size, by using a pseudo-inverse operation to perform the least-squares fit. When matrix $A$ is not square but rectangular, then $A^{-1}$ is known as the pseudo inverse and is defined as

$$A^{-1} = (A^T \cdot A)^{-1} \cdot A^T.$$  \hspace{1cm} (12)

An example explains the method. To simplify the example, we find a solution for only a single position in the aperture at $j = 0$. So we find the $c_0$ through $c_8$ needed to calculate the index needed for $s_0(G(i,k,0))$. Take $M = 25$ points on a patch to be focused: five ranges (close in to far out: $i = 0, b, 2b, 3b, 4b$) on each of five azimuths (left side to right side: $k = 0, a, 2a, 3a, 4a$). The vector $\mathbf{B}$ is the exact (floating-point) calculated index needed for those 25 points in the image. The matrix $A$ is set up so that the width of the patch is $4a$ and the depth of the patch is $4b$. So we have

$$G(i,k,j)|_{j=0} = c_{0,0} + c_{1,0}k + c_{2,0}k^2 + c_{3,0}i + c_{4,0}ik + c_{5,0}ik^2 + c_{6,0}i^2k + c_{7,0}i^2k^2 + c_{8,0}i^2k^2 \hspace{1cm} (13)$$

or

$$G(i,k,j) = \begin{bmatrix} 1 & k & k^2 & i & ik & ik^2 & i^2 & i^2k & i^2k^2 \end{bmatrix} \cdot \mathbf{C}_j$$

with

$$\mathbf{A} \cdot \mathbf{C} = \mathbf{B},$$  \hspace{1cm} (14)
which is

\[
\begin{bmatrix}
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
1 & a & a^2 & 0 & 0 & 0 & 0 & 0 \\
1 & 2a & 4a^2 & 0 & 0 & 0 & 0 & 0 \\
1 & 3a & 9a^2 & 0 & 0 & 0 & 0 & 0 \\
1 & 4a & 16a^2 & 0 & 0 & 0 & 0 & 0 \\
1 & 0 & 0 & b & 0 & 0 & b^2 & 0 \\
1 & a & a^2 & b & ab & a^2b & b^2 & ab^2 & a^2b^2 \\
1 & 2a & 4a^2 & b & 2ab & 4a^2b & b^2 & 2ab^2 & 4a^2b^2 \\
1 & 3a & 9a^2 & b & 3ab & 9a^2b & b^2 & 3ab^2 & 9a^2b^2 \\
1 & 4a & 16a^2 & b & 4ab & 16a^2b & b^2 & 4ab^2 & 16a^2b^2 \\
1 & 0 & 0 & 2b & 0 & 0 & 4b^2 & 0 & 0 \\
1 & a & a^2 & 2b & 2ab & 2a^2b & 4b^2 & 4ab^2 & 4a^2b^2 \\
1 & 2a & 4a^2 & 2b & 4ab & 8a^2b & 4b^2 & 8ab^2 & 16a^2b^2 \\
1 & 3a & 9a^2 & 2b & 6ab & 18a^2b & 4b^2 & 12ab^2 & 36a^2b^2 \\
1 & 4a & 16a^2 & 2b & 8ab & 32a^2b & 4b^2 & 16ab^2 & 64a^2b^2 \\
1 & 0 & 0 & 3b & 0 & 0 & 9b^2 & 0 & 0 \\
1 & a & a^2 & 3b & 3ab & 3a^2b & 9b^2 & 9ab^2 & 9a^2b^2 \\
1 & 2a & 4a^2 & 3b & 6ab & 12a^2b & 9b^2 & 18ab^2 & 36a^2b^2 \\
1 & 3a & 9a^2 & 3b & 9ab & 27a^2b & 9b^2 & 27ab^2 & 81a^2b^2 \\
1 & 4a & 16a^2 & 3b & 12ab & 48a^2b & 9b^2 & 36ab^2 & 144a^2b^2 \\
1 & 0 & 0 & 4b & 0 & 0 & 16b^2 & 0 & 0 \\
1 & a & a^2 & 4b & 4ab & 4a^2b & 16b^2 & 16ab^2 & 16a^2b^2 \\
1 & 2a & 4a^2 & 4b & 8ab & 16a^2b & 16b^2 & 32ab^2 & 64a^2b^2 \\
1 & 3a & 9a^2 & 4b & 12ab & 36a^2b & 16b^2 & 48ab^2 & 144a^2b^2 \\
1 & 4a & 16a^2 & 4b & 16ab & 64a^2b & 16b^2 & 64ab^2 & 256a^2b^2 \\
\end{bmatrix} \begin{bmatrix}
c_{0,0} \\
c_{1,0} \\
c_{2,0} \\
c_{3,0} \\
c_{4,0} \\
c_{5,0} \\
c_{6,0} \\
c_{7,0} \\
c_{8,0} \\
\end{bmatrix} = \begin{bmatrix}
P(0,0,0) \\
P(0,a,0) \\
P(0,2a,0) \\
P(0,3a,0) \\
P(0,4a,0) \\
P(b,0,0) \\
P(b,a,0) \\
P(b,2a,0) \\
P(b,3a,0) \\
P(b,4a,0) \\
P(2b,0,0) \\
P(2b,a,0) \\
P(2b,2a,0) \\
P(2b,3a,0) \\
P(2b,4a,0) \\
P(3b,0,0) \\
P(3b,a,0) \\
P(3b,2a,0) \\
P(3b,3a,0) \\
P(3b,4a,0) \\
P(4b,0,0) \\
P(4b,a,0) \\
P(4b,2a,0) \\
P(4b,3a,0) \\
P(4b,4a,0) \\
\end{bmatrix}
The inverse of $A$ is found to be

$$\begin{bmatrix}
961 & -837 & 31 & -27 & & -31 & -27 & 1 \\
1225 & 1225a & 245a^2 & 1225b & 245a^2b & 245b & 245ab & 49a^2b^2 \\
279 & 403 & -31 & & -243 & -351 & 27 & 9 \\
1225 & 245a & 490a^2 & 1225b & 245ab & 490a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
-93 & 124 & -31 & & 81 & -108 & 27 & -3 & 9 \\
1225 & 245a & 245a^2 & 1225b & 245ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
-31 & 837 & -31 & & 81 & -108 & 27 & -3 & 9 \\
245 & 245a & 490a^2 & 245b & 245ab & 490a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
93 & 403 & -31 & & -81 & 351 & -27 & 3 & -13 & 1 \\
1225 & 1225a & 245a^2 & 1225b & 1225ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
279 & 243 & -9 & & 403 & -351 & 13 & -31 & 27 & -1 \\
1225 & 1225a & 245a^2 & 245b & 245ab & 245b^2 & 1225ab & 245ab^2 & 49a^2b^2 \\
81 & 117 & -9 & & 117 & 169 & -13 & -9 & -13 & 1 \\
1225 & 2450a & 490a^2 & 2450b & 2450ab & 490a^2b & 2450b^2 & 2450ab^2 & 490a^2b^2 \\
1225 & 245a & 245a^2 & 245b & 245ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
-9 & 243 & -9 & & -13 & 351 & -13 & 1 & -27 & 1 \\
245 & 2450a & 490a^2 & 2450b & 2450ab & 490a^2b & 2450b^2 & 2450ab^2 & 490a^2b^2 \\
27 & -117 & 9 & & 39 & -169 & 13 & -3 & 13 & -1 \\
1225 & 1225a & 245a^2 & 245b & 245ab & 245b^2 & 1225ab & 245ab^2 & 49a^2b^2 \\
-93 & 81 & -3 & & 124 & -108 & 4 & -31 & 27 & -1 \\
1225 & 1225a & 245a^2 & 245b & 245ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
-27 & 39 & 3 & & 36 & 26 & -2 & -9 & 13 & -1 \\
1225 & 2450a & 490a^2 & 2450b & 2450ab & 490a^2b & 2450b^2 & 2450ab^2 & 490a^2b^2 \\
-9 & 12 & 3 & & -12 & 16 & -4 & 3 & 13 & -1 \\
3 & 81 & 3 & & -4 & 54 & -2 & 3 & 13 & -1 \\
245 & 245a & 490a^2 & 245b & 245ab & 490a^2b & 245b^2 & 245ab^2 & 490a^2b^2 \\
-9 & 39 & -3 & & 12 & -52 & 4 & -3 & 13 & -1 \\
1225 & 1225a & 245a^2 & 245b & 245ab & 245b^2 & 1225ab & 245ab^2 & 49a^2b^2 \\
-31 & 27 & -1 & & 837 & -729 & 27 & -31 & 27 & -1 \\
245 & 1225a & 245a^2 & 245b & 245ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
-13 & 1 & & 243 & 351 & -27 & -9 & -13 & 1 \\
245 & 490a & 98a^2 & 2450b & 2450ab & 98a^2b & 2450b^2 & 2450ab^2 & 98a^2b^2 \\
3 & 4 & 1 & & -81 & 54 & -27 & 3 & -2 & 1 \\
245 & 49a & 49a^2 & 2450b & 245ab & 49a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
1 & -27 & 1 & & -27 & 729 & -27 & 1 & 13 & -1 \\
49 & 490a & 98a^2 & 490b & 490ab & 98a^2b & 98b^2 & 98ab & 196a^2b^2 \\
-3 & 13 & -1 & & 81 & -351 & 27 & -3 & 13 & -1 \\
245 & 245a & 49a^2 & 2450b & 245ab & 49a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
93 & -81 & 3 & & -403 & 351 & -13 & 31 & -27 & 1 \\
1225 & 1225a & 245a^2 & 1225b & 245ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
27 & -13 & 1 & & -117 & -169 & 13 & 9 & 13 & -1 \\
1225 & 2450a & 490a^2 & 1225b & 2450ab & 490a^2b & 2450b^2 & 2450ab^2 & 490a^2b^2 \\
-9 & 12 & -3 & & 39 & -52 & 13 & -3 & 4 & -1 \\
1225 & 245a & 490a^2 & 1225b & 245ab & 490a^2b & 245b^2 & 245ab^2 & 490a^2b^2 \\
-3 & 81 & -3 & & 13 & -351 & 13 & -1 & 27 & -1 \\
245 & 2450a & 490a^2 & 245b & 245ab & 490a^2b & 245b^2 & 245ab^2 & 490a^2b^2 \\
1225 & 1225a & 245a^2 & 1225b & 1225ab & 245a^2b & 245b^2 & 245ab^2 & 49a^2b^2 \\
\end{bmatrix}$$
Now $\mathbf{C}$ is calculated as $\mathbf{C} = \mathbf{A}^{-1}\mathbf{B}$, and is used for finding a floating-point index pointing into the data array. This floating-point index is either rounded, so that the nearest point is chosen, or is used for a linear interpolation between the two closest data points, so that a data value is found.

Two options are available for finding the coefficients $a_0 \ldots a_{26}$: The first method is to go through the same process as shown but for the full problem. That process would involve enlarging $\mathbf{C}$ to hold the 27 coefficients ($a_0 \ldots a_{26}$); enlarging $\mathbf{B}$ to hold the ideal values for more than one position in the aperture (say five positions); and enlarging $\mathbf{A}$ to match.

The second method is to solve for vector $\mathbf{C}$ (as shown) at a number of positions in the aperture. Then construct a polynomial in $j$ for each coefficient. This solution does not involve inverting the large $\mathbf{A}$ matrix but will result in a less than optimum solution in the least-squares sense.

One advantage of this second method is that it lends itself to correcting for airplane motion. Since $\mathbf{A}$ is independent of the airplane position, it is inverted once. The matrix multiplication to find the index polynomial coefficients can be applied at every aperture position or short subaperture if desired. The algorithm thus allows real-time UWB motion compensation.

### 6.2.3 Fast Polynomial Calculation

Now that we have a polynomial to find the index, we need a fast way to compute the polynomial. Directly calculating an $N$th degree polynomial usually requires $N$ adds and $N$ multiplies. If, however, a sequence of solutions is desired with the variable changed in fixed increments (the case we have here), more efficient means are available. An algorithm by Nuttall [8] describes a method that can be applied here, to calculate the index recursively without the multiplications. The procedure is as follows:

1. Let $X(i) = q_0 + q_1 i + q_2 i^2$ be the polynomial to be solved, where $i = 0, 1, 2, 3, \ldots$

2. Let $X_1(i) = X(i) - X(i - 1) = q_1 - q_2 + 2q_2 i$. Observe that $X_1(i) - X_1(i - 1) = 2q_2$.

3. Therefore a recursion can be set up where
   
   \[ X_1(i) = X_1(i - 1) + 2q_2, \text{ and} \]
   \[ X(i) = X_1(i - 1) + X_1(i) \]

   The starting values for the recursion are
   
   \[ X(0) = q_0 \text{ and} \]
   \[ X_1(0) = q_1 - q_2 + 2q_2 i = q_1 - q_2. \]
The same derivation can be applied to an arbitrary $N^{th}$ degree polynomial to produce a recursive formula that requires $N$ adds per step. The technique can also be expanded to multiple dimensions by nesting. Appendix B lists all routines used in the fast focusing algorithm. Subroutine poly2 in section B-5 of appendix B uses this technique directly.

### 6.2.4 Coefficient Generator Program

Figure 9 shows how the image is broken down, along with the names used in the subroutines.

The basic flow chart is shown in figure 10. In figure 10, the $Z_p$'s are the $a_0$ to $a_{26}$ coefficients. Each time the inner loop goes through all the $n$'s, the $Z_p$'s are calculated for the box (defined by $h$ and $m$) and the subaperture.
(defined by $l$). The flow chart shows that the polynomial degree for the $C_n$ is not always the same. The degree was optimized based on the errors caused when a lower degree was tried. Appendix A provides a complete listing of the program that generates the focusing coefficients from an input file with the geometry.

### 6.3 Fast Focusing Algorithm

The fast focusing algorithm simply applies the fast polynomial solution technique to find the indexing and does the signal summation into all the pixels in the image. As outlined above, the index calculation is done in three nested loops. To aid in explanation, we provide displays of subroutines Inner_Loop, Middle_Loop, and Outer_Loop as pseudo-coded examples of how the focusing routine is written using the recursive technique with nesting. A second-degree polynomial is used throughout for illustration purposes. These subroutines assume that the image is broken into a number of boxes where each box has its own set of coefficients. Inner_Loop (display 1) is the simplest subroutine and follows the derivation of the recursive formula directly. It essentially increments $i$ to focus a single line in a box.

<table>
<thead>
<tr>
<th>Display 1. Subroutine Inner_Loop</th>
<th>Code</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inner_Loop (f, s, s_max, q, i_pixels)</td>
<td>Inner loop subroutine</td>
<td></td>
</tr>
<tr>
<td>float *f;</td>
<td>Pointer to first pixel in a line; f(i_start,k)</td>
<td></td>
</tr>
<tr>
<td>float *s;</td>
<td>Pointer to signal-data vector from jth aperture position</td>
<td></td>
</tr>
<tr>
<td>float *q;</td>
<td>Pointer to coefficients vector for index calculation</td>
<td></td>
</tr>
<tr>
<td>int s_max;</td>
<td>s range is $s[0]..s[s_max] _s_max$.</td>
<td></td>
</tr>
<tr>
<td>int i_pixels;</td>
<td>Size of the box (pixels) along $i$ axis is $i_pixels$.</td>
<td></td>
</tr>
<tr>
<td>f_stop = f + i_pixels - 1;</td>
<td>Set up initial conditions.</td>
<td></td>
</tr>
<tr>
<td>T = q[2] + q[2];</td>
<td>Perform clipping when index &lt; 0 (before beginning of actual data).</td>
<td></td>
</tr>
<tr>
<td>R1 = q[1] - q[2];</td>
<td></td>
<td></td>
</tr>
<tr>
<td>R0 = q[0];</td>
<td></td>
<td></td>
</tr>
<tr>
<td>If R0 &lt; -0.5 then repeat</td>
<td></td>
<td></td>
</tr>
<tr>
<td>{f++;</td>
<td></td>
<td></td>
</tr>
<tr>
<td>R1 = R1 + T;</td>
<td></td>
<td></td>
</tr>
<tr>
<td>R0 = R0 + R1;</td>
<td></td>
<td></td>
</tr>
<tr>
<td>until R0 &gt; -0.5;}</td>
<td></td>
<td></td>
</tr>
<tr>
<td>If ($f &gt; f_stop$) then return;</td>
<td></td>
<td></td>
</tr>
<tr>
<td>index = Round(R0);</td>
<td>Perform first summation.</td>
<td></td>
</tr>
<tr>
<td>*f = *f + *(s + index);</td>
<td>Begin loop for a line in box.</td>
<td></td>
</tr>
<tr>
<td>repeat</td>
<td></td>
<td></td>
</tr>
<tr>
<td>{f++;</td>
<td>Increment pointer to next pixel.</td>
<td></td>
</tr>
<tr>
<td>R1 = R1 + 1;</td>
<td>Increment index R0 = R0 + R1.</td>
<td></td>
</tr>
<tr>
<td>index = Round(R0);</td>
<td>Clip when index is beyond actual data record length.</td>
<td></td>
</tr>
<tr>
<td>if index &gt; s_max return;</td>
<td></td>
<td></td>
</tr>
<tr>
<td>*f = *f + *(s + index);</td>
<td>Sum into pixel the new data.</td>
<td></td>
</tr>
<tr>
<td>until ($f = f_stop$);</td>
<td>END Inner_Loop</td>
<td></td>
</tr>
<tr>
<td>return;</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Nesting of the recursive approach means that the coefficients $q_0$, $q_1$, and $q_2$ are each formed by polynomials in $k$. Each polynomial is incrementally recursively in the subroutine Middle Loop (display 2). Thus, Middle Loop sums into a single box the data from a single aperture position.

### Display 2. Subroutine Middle Loop

<table>
<thead>
<tr>
<th>Code</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Middle Loop($f$, $s$, $c$, $s_{max}$, $i_{pixes}$, $k_{inc}$, $box_{offset}$);</td>
<td>Middle loop subroutine</td>
</tr>
<tr>
<td>float *f;</td>
<td>Pointer to first pixel of box</td>
</tr>
<tr>
<td>float *s;</td>
<td>Pointer to $j$th data vector</td>
</tr>
<tr>
<td>float *c;</td>
<td>Pointer to coefficients vector for index calculation</td>
</tr>
<tr>
<td>int $s_{max}$;</td>
<td>$s$ range is $s[0]$...$s[s_{max}]$</td>
</tr>
<tr>
<td>int $k_{inc}$;</td>
<td>( F[i,k] = *(f+i + k * k_{inc}) ) so $k_{inc}$ is total range line length.</td>
</tr>
<tr>
<td>int $i_{pixes}$;</td>
<td>Size of the box (pixels) along $i$ axis.</td>
</tr>
<tr>
<td>int box_offset;</td>
<td>Number to add to $f$ to move pointer to last line in box.</td>
</tr>
<tr>
<td>$f_{last} = f + box_{offset}$;</td>
<td>$f_{last}$ = address of the first pixel in last line of box.</td>
</tr>
<tr>
<td>( q0_{.T} = c[2]+c[2]; )</td>
<td>Set up initial conditions for $q_0$.</td>
</tr>
<tr>
<td>( q0_{.R1} = c[1]-c[2]; )</td>
<td></td>
</tr>
<tr>
<td>( q0[0] = c[0]; )</td>
<td></td>
</tr>
<tr>
<td>( q1_{.T} = c[5]+c[5]; )</td>
<td>Set up initial conditions for $q_1$.</td>
</tr>
<tr>
<td>( q1_{.R1} = c[4]-c[5]; )</td>
<td></td>
</tr>
<tr>
<td>( q1[1] = c[3]; )</td>
<td></td>
</tr>
<tr>
<td>( q2_{.T} = c[8]+c[8]; )</td>
<td>Set up initial conditions for $q_2$.</td>
</tr>
<tr>
<td>( q2_{.R1} = c[7]-c[8]; )</td>
<td></td>
</tr>
<tr>
<td>( q2[2] = c[6]; )</td>
<td></td>
</tr>
<tr>
<td>Call Inner Loop($f$, $s$, $c$..);</td>
<td>Perform summation on first line.</td>
</tr>
<tr>
<td>repeat</td>
<td>Start loop for rest of lines.</td>
</tr>
<tr>
<td>$f = f + k_{inc}$;</td>
<td>Increment pointer to next line in box.</td>
</tr>
<tr>
<td>( q0_{.R1} = q0_{.R1}+q0_{.T}; )</td>
<td>Iterate $q_0$.</td>
</tr>
<tr>
<td>( q0[0] = q0[0]+q0_{.R1}; )</td>
<td></td>
</tr>
<tr>
<td>( q1_{.R1} = q1_{.R1}+q1_{.T}; )</td>
<td>Iterate $q_1$.</td>
</tr>
<tr>
<td>( q1[1] = q1[1]+q1_{.R1} )</td>
<td></td>
</tr>
<tr>
<td>( q2_{.R1} = q2_{.R1}+q2_{.T}; )</td>
<td>Iterate $q_2$.</td>
</tr>
<tr>
<td>( q2[2] = q2[2]+q2_{.R1}; )</td>
<td></td>
</tr>
<tr>
<td>Call Inner Loop(..);</td>
<td>Perform summation on current line in box.</td>
</tr>
<tr>
<td>Until ($f = f_{last}$);</td>
<td>Loop until all lines done.</td>
</tr>
<tr>
<td>Return;</td>
<td></td>
</tr>
</tbody>
</table>
Again, nesting of the recursive approach means that the coefficients $c_0...c_8$ are each formed by polynomials in $j$. Each polynomial is incremented recursively in the subroutine Outer Loop (display 3). Outer Loop thus sums into each box the data from multiple aperture positions. Since it is desirable to read the signal data only once, Outer Loop will both call Middle Loop for each box and increment the coefficients for each box separately as it increments $j$ across the aperture.

Display 3. Subroutine Outer Loop

<table>
<thead>
<tr>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>Outer Loop(f,a,s_max,k_boxes,i_boxes, k_pixels,i_pixels,j_beg,j_end)</td>
</tr>
<tr>
<td>float *f;</td>
</tr>
<tr>
<td>float *a;</td>
</tr>
<tr>
<td>int s_max;</td>
</tr>
<tr>
<td>int</td>
</tr>
<tr>
<td>int</td>
</tr>
<tr>
<td>int k_pixels;</td>
</tr>
<tr>
<td>int</td>
</tr>
<tr>
<td>int j_beg;</td>
</tr>
<tr>
<td>int j_end;</td>
</tr>
<tr>
<td>k_inc = 1_pixels * i_boxes;</td>
</tr>
<tr>
<td>box_offset = k_inc * (k_pixels-1);</td>
</tr>
<tr>
<td>box_inc_k = i_pixels + box_offset;</td>
</tr>
<tr>
<td>j = j_start;</td>
</tr>
<tr>
<td>read s[0,s_max] for jth position;</td>
</tr>
<tr>
<td>f = f + (box inc k + box inc i);</td>
</tr>
<tr>
<td>box = -2;</td>
</tr>
<tr>
<td>for k_box = 0 to k_boxes-1;</td>
</tr>
<tr>
<td>box = box + 1;</td>
</tr>
<tr>
<td>f = f + box inc k;</td>
</tr>
<tr>
<td>for i_box = 0 to i_boxes-1;</td>
</tr>
<tr>
<td>box = box + 1;</td>
</tr>
<tr>
<td>f = f + box inc i;</td>
</tr>
<tr>
<td>$c_0_T[box] = a[2,box] + a[2,box];$</td>
</tr>
<tr>
<td>$c_0_R1[box] = a[1,box] - a[2,box];$</td>
</tr>
<tr>
<td>$c[0,box] = a[0,box];$</td>
</tr>
<tr>
<td>$c_1_T[box] = a[5,box] + a[5,box];$</td>
</tr>
<tr>
<td>$c_1_R1[box] = a[4,box] - a[5,box];$</td>
</tr>
<tr>
<td>$c[1,box] = a[3,box];$</td>
</tr>
<tr>
<td>$c_8_T[box] = a[27,box] + a[27,box];$</td>
</tr>
<tr>
<td>$c_8_R1[box] = a[26,box] - a[27,box];$</td>
</tr>
<tr>
<td>$c[8,box] = a[25,box];$</td>
</tr>
<tr>
<td>Call Middle Loop(f,s,c[box],...);</td>
</tr>
</tbody>
</table>
### Display 3. Subroutine Outer_Loop (cont'd)

<table>
<thead>
<tr>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>END (for i_box);</td>
</tr>
<tr>
<td>END (for k_box);</td>
</tr>
<tr>
<td>repeat</td>
</tr>
<tr>
<td>f = fo - (box_inc_k+box_inc_i);</td>
</tr>
<tr>
<td>for k_box = 0 to k_boxes-1;</td>
</tr>
<tr>
<td>box = box + 1;</td>
</tr>
<tr>
<td>f = f + box_inc_k;</td>
</tr>
<tr>
<td>for i_box = 0 to i_boxes-1;</td>
</tr>
<tr>
<td>box = box + 1;</td>
</tr>
<tr>
<td>f = f + box_inc_i;</td>
</tr>
<tr>
<td>c0_R1[box] = c0_R1[box]+c0_T[box];</td>
</tr>
<tr>
<td>c0[0,box] = c0[0,box]+c0_R1[box];</td>
</tr>
<tr>
<td>c1_R1[box] = c1_R1[box]+c1_T[box];</td>
</tr>
<tr>
<td>c1[1,box] = c1[1,box]+c1_R1[box];</td>
</tr>
<tr>
<td>Call Middle_Loop(f,s,c[box],...);</td>
</tr>
<tr>
<td>END (for i_box);</td>
</tr>
<tr>
<td>END (for k_box);</td>
</tr>
<tr>
<td>Until j = j_stop;</td>
</tr>
<tr>
<td>Return (END Outer_Loop)</td>
</tr>
</tbody>
</table>

**Comments**

- Loop through all boxes.
- Loop through all aperture positions.
- Increment aperture.
- Position read data for that aperture position.
- Initialize f.
- Set up to loop through all boxes.
- Iterate \( c_0 \) for current box.
- Iterate \( c_1 \) for current box.
- Iterate \( c_2...c_7 \) for current box.
- Iterate \( c_8 \) for current box.
- Sum into current box.
- Loop until all aperture positions are done.

### 6.4 Considerations for Fast Focusing Polynomial Order Selection

A study was conducted to determine the effect of polynomial order on the image size and aperture length. The worst-case position in the aperture \( f = 3 \) in fig. 3, p 17 and the worst-case area in the image \((i,k) = (237,3)\) in fig. 3) were chosen for the analysis. The sample rate was 4 Gs/s with a record length \( s_{\text{max}} \) of 4096 points. The elevation was 60 ft; otherwise the geometry was as in figure 3, with an aperture \( L_s = 384 \) ft, squint angle \( \theta = 85^\circ \), and slant range \( R = 550 \) ft. If the error in the floating-point index is restricted to \( \pm 0.5 \), then this geometry produces the following results:

<table>
<thead>
<tr>
<th>Polynomial degree</th>
<th>Maximum i_pixels</th>
<th>Maximum k_pixels</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>228</td>
<td>27</td>
</tr>
<tr>
<td>2</td>
<td>964</td>
<td>105</td>
</tr>
<tr>
<td>3</td>
<td>2191</td>
<td>315</td>
</tr>
<tr>
<td>4</td>
<td>-</td>
<td>657</td>
</tr>
</tbody>
</table>

By using the nested recursive technique as shown in the example subroutines, we compute the computational load as shown in table 2.
Grouping terms, we get

\[ L = \text{(inner loop adds)} + \text{(middle loop adds)} + \text{(outer loop adds)} \]

\[ = IKJB(i' + 1) + KJB(i' + 1)k' + JB(i' + 1)(k' + 1)j'. \]

From this equation, it is clear that a low-order polynomial is crucial in the inner loop. Conversely, the order of the polynomial in the outer loop can be high with little impact on the overall speed. Table 3 shows the computational load for various configurations with \( j' = 3 \) and \( J = 2304 \).

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i' )</td>
<td>Polynomial order for ( i ) index</td>
</tr>
<tr>
<td>( k' )</td>
<td>Polynomial order for ( k ) index</td>
</tr>
<tr>
<td>( j' )</td>
<td>Polynomial order for ( j ) index</td>
</tr>
<tr>
<td>( J )</td>
<td>Number of points in the aperture</td>
</tr>
<tr>
<td>( l )</td>
<td>Number of range bins (pixels) in box (i_pixes)</td>
</tr>
<tr>
<td>( K )</td>
<td>Number of azimuth bins (pixels) in box (k_pixes)</td>
</tr>
<tr>
<td>( B )</td>
<td>Number of boxes</td>
</tr>
<tr>
<td>( L_0 )</td>
<td>( i'(i' + 1); ) adds per Inner_Loop call</td>
</tr>
<tr>
<td>( L_1 )</td>
<td>( K[L_0 + (i' + 1)k']; ) adds per Middle_Loop call</td>
</tr>
<tr>
<td>( L )</td>
<td>( J[L_1 + (i' + 1)(k' + 1)j']; ) adds per Outer_Loop (adds per image)</td>
</tr>
</tbody>
</table>

Table 3. Matrix showing computational load versus partitioning for \( j' = 3 \) and \( J = 2304 \).

<table>
<thead>
<tr>
<th>( i' )</th>
<th>( j' )</th>
<th>Boxes across</th>
<th>Total pixels across</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>27</td>
<td>19</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>103</td>
<td>5</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
<td>256</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>4</td>
<td>512</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>19</td>
<td>513</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>515</td>
<td>512</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>512</td>
<td>512</td>
</tr>
<tr>
<td>2</td>
<td>4</td>
<td>512</td>
<td>512</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>19</td>
<td>19.711</td>
</tr>
<tr>
<td>3</td>
<td>2</td>
<td>14.51</td>
<td>21,888</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>14.53</td>
<td>S = 21,888</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>14.58</td>
<td>B = 342</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>19</td>
<td>19.769</td>
</tr>
<tr>
<td>4</td>
<td>2</td>
<td>14.51</td>
<td>S = 8640</td>
</tr>
<tr>
<td>4</td>
<td>3</td>
<td>14.53</td>
<td>B = 90</td>
</tr>
<tr>
<td>4</td>
<td>4</td>
<td>14.58</td>
<td>S = 4608</td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td>19</td>
<td>19.810</td>
</tr>
<tr>
<td>5</td>
<td>2</td>
<td>14.51</td>
<td>S = 2980</td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td>14.53</td>
<td>B = 36</td>
</tr>
<tr>
<td>5</td>
<td>4</td>
<td>14.58</td>
<td>S = 4608</td>
</tr>
</tbody>
</table>

\( L = \) total number of adds in giga-adds.

\( B = \) total number of boxes in the image.

\( S = \) bytes of storage needed for the coefficient tables = \( (i' + 1)(k' + 1)(j' + 1)B(4 \text{ bytes/word}). \)
6.5 Implementation Notes

The algorithm developed here requires no multiplication except in the pre­
processing (interpolation) stage. There already exist DSP (digital signal
processor) chips whose architecture is ideal for the FIR interpolation task.
The bulk of the computations, however, occur in the summing and index
calculation stage. Two facts make the summing algorithm attractive. First,
adders take considerably less area to implement in a VLSI (very-large-scale
integration) chip than multipliers. Second, parallel operation is extremely
simple; the image can simply be broken into boxes with a separate proces­
sor working independently on each box. In this case, only the coefficient
table would be different between processors, and a broadcast mode would
be needed to pass the signal data to each processor. Therefore, design of a
custom LSI chip appears practical and could result in real-time speeds.

If an off-the-shelf DSP chip with a parallel adder and multiplier is used to
perform this algorithm, then other options become available. For example,
the multiplier can be used in the summing algorithm to do interpolation on
the indexing rather than rounding. The multiplication required can be done
during other add cycles so that it takes zero time. Another possibility is to
calculate the index polynomial directly instead of recursively. Finally, since
all the operations can be fixed point, the address-generator ALU (arithmetic
logic unit) can sometimes be used in parallel with the floating-point units.
7. Beam Patterns and Sidelobe Structure

To develop an intuitive understanding for the beam shape, we assembled 16 figures to display, in the time domain, the main-lobe and sidelobe beam patterns. We simulated a resonant target by generating a data record for every position in the aperture. The simulated scene was a single-point target. The target bearing (see fig. 3) was squinted $15^\circ$ off broadside ($\theta = 105^\circ$). Range to the target $R$ was 750 ft, the aperture length $L_s$ was 385 ft, and the aperture height was 60 ft. The point target had an impulse response of

$$s(t) = \begin{cases} 
\sin(2\pi ft)(0.5 + 0.5\cos(4\pi ft)) & \text{for } 0 < t < \frac{1}{4f} \\
\sin(2\pi ft)\exp\left[\left(\frac{1}{4f - t}\right)0.23f\right] & \text{for } t \geq \frac{1}{4f}
\end{cases}$$

(15)

The data simulated a 2-GHz sample rate. A record length of 2048 samples was made for each aperture position. Each record was preprocessed with a times-8 interpolator, producing 16K records. Interpolation was done by the standard FIR filter method. A 255-tap Parks-McClellan low-pass filter with a 950-MHz cutoff was used to do the interpolation. Equation (7) (with $n = 0$) was used to produce the focused beams. A Hilbert transform was used to obtain the magnitude that is plotted in the figures. Plots were made on a decibel scale. Four 3-D plots were made, showing two viewing angles (on axis and above axis) and two aperture weighting functions (Hamming and rectangular) for each of four targets with different resonant frequencies (50, 200, 400, and 900 MHz). These are shown in figures 11 to 26.

The on-axis plots were made so that amplitude values could be easily read off the plots. The above-axis plots were made to reveal the sidelobe structure and the ring-down time of the target. The axis labels were shifted so that 0 range was at the point target and 0° was the bearing centered on the target. Notice that all plots are 3-D, even the on-axis plots. The various horizontal lines in the on-axis plots are the beam pattern on the $i^{th}$ range bin. These horizontal lines are identical to those shown in the above-axis plots; they are just being viewed "end on.”

These figures are unique in that they show how the sidelobes spread in time as one moves off the main beam. Because of the sharp rise time of the target echo, the contribution from the near and far ends of the aperture can be seen as the early and late peaks in the sidelobe structure. Hamming weighting was applied to the array so that one can see the effect of weighting on the sidelobe structure. It is interesting to note that although the peak sidelobe levels drop only marginally, the average or integrated sidelobe levels are significantly lower when tapered aperture weighting is used. The weighting also reduces the near and far peaks in the sidelobes since the weighting reduces the contribution of the array ends.
Since the antenna is a linear system, it is no surprise that the beam pattern behaves basically as classic antenna theory predicts. The aperture beam pattern is a function of (1) how long the aperture is relative to wavelength, and (2) what kind of weighting is used to sum the points in the aperture. If uniform aperture weighting is used (a straight summation), then the typical $\sin(\beta \psi)/(\beta \psi)$ pattern occurs, where $\psi$ is the angle off the main beam, and $\beta \propto L_S/\lambda$. $\beta$ establishes the width of the main beam. As the wavelength gets small, or as the aperture gets long, the beam gets narrow.

Figure 11. 50-MHz point reflector, equal weighting, end view.

Figure 12. 50-MHz point reflector, Hamming weighting, end view.
Figure 13. 50-MHz point reflector, equal weighting, above axis.

Figure 14. 50-MHz point reflector, Hamming weighting, above axis.
Figure 15. 200-MHz point reflector, equal weighting, end view.

Figure 16. 200-MHz point reflector, Hamming weighting, end view.
Figure 17. 200-MHz point reflector, equal weighting, above axis.

Figure 18. 200-MHz point reflector, Hamming weighting, above axis.
Figure 19. 400-MHz point reflector, Hamming weighting, end view.

Figure 20. 400-MHz point reflector, Hamming weighting, end view.
Figure 21. 400-MHz point reflector, equal weighting, above axis.

Figure 22. 400-MHz point reflector, Hamming weighting, above axis.
Figure 23. 900-MHz point reflector, equal weighting, end view.

Figure 24. 900-MHz point reflector, Hamming weighting, end view.
Figure 25. 900-MHz point reflector, equal weighting, above axis.

Figure 26. 900-MHz point reflector, Hamming weighting, above axis.
8. Summary

This report identifies a frequency-independent processing algorithm to get a perfectly focused impulse response from any object at any position from an ultra-wide-bandwidth synthetic aperture radar. The report also presents an approximation that reduces the computational complexity of the algorithm. An error analysis of this approximation demonstrates its applicability to focus even high-Q objects in the near field of an aperture. An implementation that is both computationally efficient and applicable to real-time motion compensation is also presented. Finally, plots are presented demonstrating the capability of the algorithm to focus ringing targets over an 18-to-1 bandwidth.
References


Appendix A. Coefficient Generator Program
# Appendix A

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<td>59</td>
</tr>
</tbody>
</table>
A-1. Main Program to Calculate Coefficients (main.c)

This is a listing of the code that calculates the coefficients needed by the fast focusing algorithm. It takes as inputs the geometry of the synthetic aperture radar (SAR) and image area, and it outputs the coefficient vectors required.

---

```c
#include <malloc.h>
#include <stdio.h>
#include <math.h>
#include "coefgen.const"
#include "coefgen.var"

main()
{
    long cacheset;
    FILE *fp,*tstart_fp;
    char fn[80];
    long i;
    ia=(BOX_SIZE_AZIMUTH-4)/4;
    ib=(BOX_SIZE_RADIAL-3)/4;
    /* initialize variables */
    coefgen_varinit();
    /* initialize pseudo inver matrix */
    initmat();

    printf("Enter coefficient a output file name ==> ");
    scanf("%s",fn);
    fp=fopen(fn,"w");
    if(fp==NULL)
    {
        printf("Error open output file 
");
        exit(1);
    }
    /*
    
    
    */
```
Appendix A

printf("Enter data acquisition timing file name ===> ");
scanf("%s", fn);
/*
tstart_fp=fopen("delaytime.dat","r");
if(tstart_fp==NULL)
{
    printf("Error open input file \n");
    exit(0);
}
read_delaytime(tstart_fp);
*/
coefgen(fp);
}

A-2. Main Coefficient Generator Routine (coefgen.c)

#include "coefgen.h"    /*geometry file*/
#include "coefgen.var"   /*list of variables*/
#include <stdio.h>
#include <math.h>
extern indexO;
extern mxmulO;
extern poly_fitO;
/* Note that Reference point is now taken at coordinate kpixel= n_azimuth/2-1 */
/* ipixel= n_radial/2 -1 */
/* At every position data were taken so that the reference point is at center */
/* data buffer */

void coefgen(fp)
FILE *fp;
{
    float input[NPOINT_APER/4];
    long i,j;
    long section,kbox,ibox,position,position_start,position_stop;
    long ipoint,kpoint;
    for(i=0;i<NPOINT_APER/n_section;i++)
    {
        input[i]=(float)i;
    }
    for(section=0;section<n_section;section++)
    {
        position_start=section*n_aper/n_section;
        position_stop=position_start+n_aper/n_section;

    46
for(kbox=0;kbox<NBOX_AZIMUTH;kbox++)
{
  for(ibox=0;ibox<NBOX_RADIAL;ibox++)
  {
    printf("processing section %d ibox %d kbox %d\n",section,ibox,kbox);
    for(position=position_start;position<position_stop;position++)
    {
      /* Calculating Actual index for all samples points in a box***********/
      i=0;
      for(ipoint=0;ipoint<NPOINT_BOXSAMPLE_RADIAL;ipoint++)
      {
        for(kpoint=0;kpoint<NPOINT_BOXSAMPLE_AZIMUTH;kpoint++)
        {
          ipixel=ibox*BOX_SIZE_RADIAL+ipoint*ib;
          jpixel=kbox*BOX_SIZE_AZIMUTH+kpoint*ia;
          d=((float)position-((float)n_afer/2.-1.))*(aper_length/((float)n_afer-1.)); /* distance from radar to center of aperture */
          x=sqrt(rcenter_ref*rcenter_ref-radar_height2);
          r_ref=sqrt(radar_height2+x*x*c_theta_center_ref*c_theta_center_ref+(d-x*s_theta_center_ref)*(d-x*s_theta_center_ref));
          rmin=r_ref-d_center*((float)n_radial/2.-1.);
          index(&ipixel,&jpixel,&findex[i]);
          i++;
        }
      }
      /* generate coef for this box at this position */
      mxmuls(mat,&mat_c_stride,&stride,findex,&findex_c_stride,&stride,coef,&coef_c_stride,
      &stride,&n_coef,&i_one,&n_boxsample);
      /* save in coefc[i][position] */
      for(i=0;i<COEF_SIZE;i++)
      {
        coefc[i][position-position_start]=coef[i];
      }
    }
  }
  /* for debug only */
  /* printf("pos= %d tstart= %.3e\n",position,2.0*rmin/c); */
  /* end debug */
}
} /* position */
for(i=0;i<COEF_SIZE;i++)
{
  printf("Doing polyfit for coef %d\n",i);
  poly_fit(input,&coefc[i][0],n_afer/n_section,deg[i],&coefa[i][0]);
Appendix A

for(j=0;j<(deg[i]+1);j++)
{
    fprintf(fp,"%e\n",coefa[i][j]); /* save a[i] to file */
}
}
/* inbox */
} /* kbox */
} /* section */

} /* subroutine */

A-3. Subroutine Find Ideal Index Vector (index.c)

*************************************************************************/

Subroutine: index.c

Input:
   ipixel  pixel radial coordinate
   jpixel  pixel angle coordinate
   a_span  angle spanned by the patch
   a_offset offset angle of the center line
   d       distance from middle position
   d_rcenter sampling range
   dr8     (sampling range)/8
   rmincenter  min range from center position
   hgt     height of building
   hgt2    square the height
   length  length of the building

Output:
   findex  floating point index to ivalue of that pixel

*************************************************************************/

#include "coefgen.const"
#include "coefgen.var"
#include <math.h>

index(ipixel,kpixel,findex)
int *ipixel,*kpixel;
float *findex;
{

    theta=a_offset-a_span/2.+(float)*kpixel*d_theta;
    c_theta=cos(theta);
    s_theta=sin(theta);
    rcenter=rmincenter+(float)*ipixel*d_rcenter;

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\[
\begin{align*}
x &= \sqrt{r_{\text{center}}^2 - \text{radar\_height}^2}; \\
r &= \sqrt{\text{radar\_height}^2 + x^2 \cdot c_{\theta}^2 + (d - x \cdot s_{\theta})^2 + (d - x \cdot s_{\theta})^2}; \\
*f_{\text{index}} &= (r - r_{\text{min}})/dr_8;
\end{align*}
\]

A-4. Geometry File — Declare All Global Constants (coefgen.h)

```c
#define NPOINT_AZIMUTH 600 /* number of bearing lines */
#define NPOINT_RADIAL 4095 /* number of radial lines */
#define NPOINT_APER 2304 /* # of positions in aperture */
#define NPOINT_DATA 2048 /* number of original data points */
#define NPOINT_DATA_INTER NPOINT_DATA*8 /* number of data points after interpolated */
#define PI 3.141592654
#define RADAR_HEIGHT 60. /* radar height in feet */
#define A_OFFSET -15.0 /* offset angle from center line */
#define A_SPAN 54.0 /* spanning angle of the patch */
#define RMINCENTER 550. /* range from center position to nearest point on the patch */
#define RCENTER_REF 802.0 /* range (ft) of ref. point from center pos. */
#define THETA_CENTER_REF -15.0 /* angle (deg) of ref. point from center pos. */
#define SAMPLING_RATE 2.0e09 /* sampling frequency of signal */
#define SAMPLING_PERIOD 5.0e-10 /* ts=1/fs */

#define BOX_SIZE_RADIAL 195
#define BOX_SIZE_AZIMUTH 100
#define NBOX_RADIAL NPOINT_RADIAL/BOX_SIZE_RADIAL
#define NBOX_AZIMUTH NPOINT_AZIMUTH/BOX_SIZE_AZIMUTH

#define SECTION_SIZE 4 /* # of sections for one aperture */
#define COEF_SIZE 6 /* # of coeffs for curve fit */
#define MAXDEG 3 /* maximum degree for poly. fit */
#define NPOINT_BOXSAMPLE_RADIAL 5 /* # of samples in a box in radial direction */
#define NPOINT_BOXSAMPLE_AZIMUTH 5 /* # of samples in azimuth direction for every box */
#define NPOINT_BOXSAMPLE NPOINT_BOXSAMPLE_RADIAL*NPOINT_BOXSAMPLE_AZIMUTH /* # of samples in a box for curve fit */
```

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A-5. Declare All Global Variables (coefgen.var)

```c
struct complex { float r,i; }; /* define a complex type */

/* Data Variables */
float pixel[NPOINT_AZIMUTH][NPOINT_RADIAL]; /* array of image */
float data[NPOINT_DATA]; /* original data buffer */
float data_inter[NPOINT_DATA_INTER]; /* interpolated data buffer */
struct complex data_inter_fft[NPOINT_DATA_INTER/2]; /* Real->Complex Forward FFT of data_inter */
float filter_coef[NPOINT_DATA_INTER]; /* filter coefficients */
struct complex filter_fft[NPOINT_DATA_INTER/2]; /* Real->Complex Forward FFT of filter_coef */
float nyquist_filter; /* value of FFT of filter at Nyquist point */
float nyquist_data; /* value of FFT of data at Nyquist Point */

/* Geometry Variables */
float a_offset; /* offset angle from the center line */
float a_span; /* spanning angle of the patch */
float d_theta; /* delta angle */
float x,theta; /* coordinate of a pixel */
float c_theta,s_theta; /* cosine and sine of theta */
float d; /* distance from radar to center position positive to the right, neg. to the left */
float rcenter,rmincenter,rmaxcenter; /* range from center position */
float rcenter_ref; /* range from center pos. to ref point */
float theta_center_ref; /* angle of ref. point from center position */
float r_ref; /* range from any pos. to ref. point */
float d_rcenter; /* sampling distance from center position */
float dr8; /* (sampling distance)/8 */
float r,rmin,rmax; /* range from any position */
float aper_length; /* length of aperture */
float radar_height; /* height of radar */
float radar_height2; /* square the height of radar */

/* Radar Variables */
float c; /* speed of wave */
float ts; /* sampling period of signal */
float fs; /* sampling frequency of signal */
long n_azimuth; /* # of points in azimuth direction */
long n_radial; /* # of points in radial direction */
long n_aper; /* # of positions in aperture */
long pix_size; /* # of points in pixel array */
```
A-6. Matrix Pseudo Inverse Coefficients (initmat.c)

#include <stdio.h>
#include <math.h>
#include "coefgen.const"
#include "coefgen.var"

initmat() 
{ 
  int i,j;
  float a,b;

  a=((float)BOX_SIZE_AZIMUTH-4.)/4.;
  b=((float)BOX_SIZE_RADIAL-3.)/4.;
Appendix A

mat[0][0]=93./175.;
mat[0][1]=27./175.;
mat[0][2]=(-9.)/175.;
mat[0][3]=(-3.)/35.;
mat[0][4]=9./175.;
mat[0][5]=62./175.;
mat[0][6]=18./175.;
mat[0][7]=(-6.)/175.;
mat[0][8]=(-2./35.;
mat[0][9]=6./175.;
mat[0][10]=31./175.;
mat[0][11]=9./175.;
mat[0][12]=(-3./175.;
mat[0][13]=(-1.)/35.;
mat[0][14]=3./175.;
mat[0][15]=0.;
mat[0][16]=0.;
mat[0][17]=0.;
mat[0][18]=0.;
mat[0][19]=0.;
mat[0][20]=(-31./175.;
mat[0][21]=(-9./175.;
mat[0][22]=3./175.;
mat[0][23]=1./35.;
mat[0][24]=(-3./175.;

mat[1][0]=(-81.)/(175.*a);
mat[1][1]=39./(350.*a);
mat[1][2]=12./(35.*a);
mat[1][3]=81./(350.*a);
mat[1][4]=(-39.)/(175.*a);
mat[1][5]=(-54.)/(175.*a);
mat[1][6]=13./(175.*a);
mat[1][7]=8./(35.*a);
mat[1][8]=27./(175.*a);
mat[1][9]=(-26.)/(175.*a);
mat[1][10]=(-27.)/(175.*a);
mat[1][11]=13./(350.*a);
mat[1][12]=4./(35.*a);
mat[1][13]=27./(350.*a);
mat[1][14]=(-13.)/(175.*a);
mat[1][15]=0.;
mat[1][16]=0.;
mat[1][17]=0.;
mat[1][18]=0.;
mat[1][19]=0.;
mat[1][20]=27./(175.*a);
mat[1][21]=(-13.)/(350.*a);
mat[1][22]=(-4.)/(35.*a);
mat[1][23]=(-27.)/(350.*a);
mat[1][24]=13./(175.*a);

mat[2][0]=3./(35.*pow(a,2.)));
mat[2][1]=(-3.)/(70.*pow(a,2.));
mat[2][2]=(-3.)/(35.*pow(a,2.));
mat[2][3]=(-3.)/(70.*pow(a,2.));
mat[2][4]=3./(35.*pow(a,2.));
mat[2][5]=2./(35.*pow(a,2.));
mat[2][6]=(-1.)/(35.*pow(a,2.));
mat[2][7]=(-2.)/(35.*pow(a,2.));
mat[2][8]=(-1.)/(35.*pow(a,2.));
mat[2][9]=2./(35.*pow(a,2.));
mat[2][10]=1./(35.*pow(a,2.));
mat[2][11]=(-1.)/(70.*pow(a,2.));
mat[2][12]=(-1.)/(35.*pow(a,2.));
mat[2][13]=(-1.)/(70.*pow(a,2.));
mat[2][14]=1./(35.*pow(a,2.));
mat[2][15]=0.;
mat[2][16]=0.;
mat[2][17]=0.;
mat[2][18]=0.;
mat[2][19]=0.;
mat[2][20]=(-1.)/(35.*pow(a,2.));
mat[2][21]=1./(70.*pow(a,2.));
mat[2][22]=1./(35.*pow(a,2.));
mat[2][23]=1./(70.*pow(a,2.));
mat[2][24]=(-1.)/(35.*pow(a,2.));

mat[3][0]=(-31.)/(175.*b);
mat[3][1]=(-9.)/(175.*b);
mat[3][2]=3./(175.*b);
mat[3][3]=1./(35.*b);
mat[3][4]=(-3.)/(175.*b);
mat[3][5]=(-31.)/(350.*b);
mat[3][6]=(-9.)/(350.*b);
mat[3][7]=3./(350.*b);
mat[3][8]=1./(70.*b);
mat[3][9]=(-3.)/(350.*b);
mat[3][10]=0.;
mat[3][11]=0.;
Appendix A

```
mat[3][12]=0.;
mat[3][13]=0.;
mat[3][14]=0.;
mat[3][15]=31./((350.*b);
mat[3][16]=9./((350.*b);
mat[3][17]=(-3.)/((350.*b);
mat[3][18]=(-1.)/(70.*b);
mat[3][19]=3./((350.*b);
mat[3][20]=31./((175.*b);
mat[3][21]=9./((175.*b);
mat[3][22]=(-3.)/(700.*b);
mat[3][23]=(-1.)/(35.*b);
mat[3][24]=3./((175.*b);

mat[4][0]=27./((175.*a*b);
mat[4][1]=(-13.)/((350.*a*b);
mat[4][2]=(-4.)/(35.*a*b);
mat[4][3]=(-27.)/((350.*a*b);
mat[4][4]=13./((175.*a*b);
mat[4][5]=27./((350.*a*b);
mat[4][6]=(-13.)/((700.*a*b);
mat[4][7]=(-2.)/(35.*a*b);
mat[4][8]=(-27.)/((700.*a*b);
mat[4][9]=13./((350.*a*b);
mat[4][10]=0.;
mat[4][11]=0.;
mat[4][12]=0.;
mat[4][13]=0.;
mat[4][14]=0.;
mat[4][15]=(-27.)/((350.*a*b);
mat[4][16]=13./((700.*a*b);
mat[4][17]=2./((35.*a*b);
mat[4][18]=27./((700.*a*b);
mat[4][19]=(-13.)/((350.*a*b);
mat[4][20]=(-27.)/((175.*a*b);
mat[4][21]=13./((350.*a*b);
mat[4][22]=4./((35.*a*b);
mat[4][23]=27./((350.*a*b);
mat[4][24]=(-13.)/((175.*a*b);

mat[5][0]=(-1.)/(35.*pow(a,2.)*b);
mat[5][1]=1./((70.*pow(a,2.)*b);
mat[5][2]=1./((35.*pow(a,2.)*b);
mat[5][3]=1./((70.*pow(a,2.)*b);
mat[5][4]=(-1.)/(35.*pow(a,2.)*b);
```
Appendix A

A-7. Initialize All Variables (varinit.c)

***************************************************************************
Subroutine: coefgen_varinit
Description: initialize all neccessary variables
***************************************************************************

#include <stdio.h>
#include <math.h>
#include "coefgen.const"
#include "coefgen.var"
coefgen_varinit()
{
    n_azimuth=NPOINT_AZIMUTH; /* # of points in azi. direction */
    n_radial=NPOINT_RADIAL;  /* # of points in rad. direction */
    pix_size=n_azimuth*n_radial; /* Pixel array size */
    n_data=NPOINT_DATA;      /* # of orig. data points */
    n_data_inter=NPOINT_DATA_INTER; /* # of interpolated. data points */
    n_data_inter_half=NPOINT_DATA_INTER/2; /* 1/2 # of inter. data points */
    mat[5][5]=(-1.)/(70.*pow(a,2.)*b);
    mat[5][6]=1./(140.*pow(a,2.)*b);
    mat[5][7]=1./(70.*pow(a,2.)*b);
    mat[5][8]=1./(140.*pow(a,2.)*b);
    mat[5][9]=(-1.)/(70.*pow(a,2.)*b);
    mat[5][10]=0.;
    mat[5][11]=0.;
    mat[5][12]=0.;
    mat[5][13]=0.;
    mat[5][14]=0.;
    mat[5][15]=1./(70.*pow(a,2.)*b);
    mat[5][16]=(-1.)/(140.*pow(a,2.)*b);
    mat[5][17]=(-1.)/(70.*pow(a,2.)*b);
    mat[5][18]=(-1.)/(140.*pow(a,2.)*b);
    mat[5][19]=1./(70.*pow(a,2.)*b);
    mat[5][20]=1./(35.*pow(a,2.)*b);
    mat[5][21]=(-1.)/(70.*pow(a,2.)*b);
    mat[5][22]=(-1.)/(35.*pow(a,2.)*b);
    mat[5][23]=(-1.)/(70.*pow(a,2.)*b);
    mat[5][24]=1./(35.*pow(a,2.)*b);
}
Appendix A

n_aper=NPOINT_APER; /* # of points in the aperture */
n_boxsample=NPOINT_BOXSAMPLE; /* # of samples in box for curve fit */
n_coef=COEF_SIZE; /* # of coeffs for curve fit */
n_section=SECTION_SIZE; /* # of sections for one aperture */

/* Radar Variables */
fs=SAMPLING_RATE; /* Sampling Frequency */
ts=SAMPLING_PERIOD; /* Sampling period */
c=3.e8; /* Speed of wave */

/* Geometry variables */
a_ofset=A_OFSET*PI/180.; /* Offset angle from center line */
a_span=A_SPAN*PI/180.; /* Spanning angle of the patch */
theta_center=theta_center+a_ofset-a_span/2.+( float) n_azimuth/2.-1.)*d_theta;
c Theta_center=cos(theta_center); s Theta_center=sin(theta_center);
rcenter_ref=rmincenter+d_rcenter*(( float) n_radial/2.-1.);

/* SSL Variables */
f_zero=0.; /* floating point zero */
strike=1; /* stride for ssl */
f_one=1.0; /* floating point 1 */
i_one=1; /* integer 1 */
mat_c_stride=n_boxsample; /* column stride for mat */
index_c_stride=1; /* column stride for index */
coef_c_stride=1; /* column stride for coeff */
deg[0]=3; /* degree for first coefc */
deg[1]=3;

A-8. Find Least Squares Polynomial Fit (poly_fit.c)

Subroutine: poly_fit.c
Description:
Perform data fit to polynomial
Input: x[n] input array
       y[n] input array
       n number of elements
       deg degree of poly.
output coeff[deg+1] coefficients of poly

#include <stdio.h>
#include <malloc.h>
#include <math.h>
void poly_fit(x,y,n,deg,coeff)
float x[], y[], coeff[];
long n,deg;
{
    double *dx,*dy,*dcoeff;
    double *dX,*dXtrans,*dA,*dB,*dC;
    long m,i,j,one;
    one=1;
    m=deg+1;
    dx=malloc(n*sizeof(double));
    if(dx==NULL)
    {
        printf("Memory allocation Error !!!\n");
        exit(1);
    }
    dy=malloc(n*sizeof(double));
    if(dy==NULL)
    {
        printf("Memory allocation Error !!!\n");
        exit(1);
    }
}
Appendix A

dcoeff=malloc(m*sizeof(double));
if (dcoeff==NULL)
{
    printf("Memory allocation Error !!!\n");
    exit(1);
}
dX=malloc(n*sizeof(double));
if (dX==NULL)
{
    printf("Memory allocation Error !!!\n");
    exit(1);
}
dXtrans=malloc(n*sizeof(double));
if (dXtrans==NULL)
{
    printf("Memory allocation Error !!!\n");
    exit(1);
}
dA=malloc(m*sizeof(double));
if (dA==NULL)
{
    printf("Memory allocation Error !!!\n");
    exit(1);
}
 dB=malloc(m*sizeof(double));
if (dB==NULL)
{
    printf("Memory allocation Error !!!\n");
    exit(1);
}
dC=malloc(m*sizeof(double));
if (dC==NULL)
{
    printf("Memory allocation Error !!!\n");
    exit(1);
}

for(i=0;i<n;i++)
{
    dx[i]=(double)x[i];
    dy[i]=(double)y[i];
}
for(i=0;i<n;i++)
{
    dX[i*m]=1.0;
A-9. Matrix Inverter (inverse.c)

```c
#include <stdio.h>

mat_inverse(source_mat,dest_mat,size_mat)
double source_mat[];
double dest_mat[];
long size_mat;
{
    long n,i,j,k,ki,count;
    double b,b1;
    double err=0.0001;
    double a[100][100];
    n=size_mat;
    count=0;
    for(j=1;j<m;j++)
    {
        for(i=0;i<n;i++)
        {
            dX[j+i*m]=pow(dx[i],(double)j);
        }
    }
    mxtrans(dX,n,m,dXtrans);
    mxmlp(dXtrans,&n,&one,dX,&m,&one,dA,&m,&one,&m,&m,&n);
    mat_inverse(dA,dB,m);
    mxmlp(dXtrans,&n,&one,dy,&one,&one,dC,&one,&one,&m,&one,&n);
    mxmlp(dB,&m,&one,dC,&one,&one,dcoeff,&one,&one,&m,&one,&m);
    for(i=0;i<m;i++)
    {
        coeff[i]=(float)dcoeff[i];
    }
    free(dx);
    free(dy);
    free(dA);
    free(dB);
    free(dC);
    free(dX);
    free(dXtrans);
    free(dcoeff);
}
```
Appendix A

for(i=0;i<size_mat;i++)
{
    for(j=0;j<size_mat;j++)
    {
        a[i+1][j+1]=source_mat[count++];
    }
}

for(i=1;i<=n;i++)
{
    for(j=n+1;j<=2*n;j++)
    {
        if((j-n-i)==0)
        {
            a[i][j]=1.0;
        }
        else
        {
            a[i][j]=0.0;
        }
    }
}

for(k=1;k<=n-1;k++)
{
    b=a[k][k];
    ki=k;
    for(i=k+1;i<=n;i++)
    {
        if((abs(b)-abs(a[i][k]))<0)
        {
            b=a[i][k];
            ki=i;
        }
    }
}

if((abs(b)-err)<0)
{
    printf("Error matrix inverse , matrix is singular\n");
    exit(1);
}

if((ki-k)!=0)
{
    for(j=ki;j<=2*n;j++)
    {

b1=a[k][j];
a[k][j]=a[ki][j];
a[ki][j]=b1;
}
}

for(j=k+1;j<=2*n;j++)
{
    a[k][j]=a[k][j]/b;
}

for(i=k+1;i<=n;i++)
{
    for(j=k+1;j<=2*n;j++)
    {
        a[i][j]=a[i][j]-a[i][k]*a[k][j];
    }
}

for(j=n+1;j<=2*n;j++)
{
    a[n][j]=a[n][j]/a[n][n];
}

for(k=n-1;k>=1;k=k-1)
{
    for(j=n+1;j<=2*n;j++)
    {
        for(i=k+1;i<=n;i++)
        {
            a[k][j]=a[k][j]-a[k][i]*a[i][j];
        }
    }
}

count=0;
for(i=0;i<size_mat;i++)
{
    for(j=0;j<size_mat;j++)
    {
        dest_mat[count++]=a[i+1][size_mat+j+1];
    }
}
Appendix B. UWB SAR Focusing Program
Appendix B

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B-1. Main Program for SUN Computer (focus.c)

This is a listing of the code that focuses the ultra-wideband (UWB) synthetic aperture radar (SAR) data. It takes as inputs the coefficient vectors generated by the code listed in appendix A and the SAR data, and it outputs a focused image.

```c
#include <stdio.h>
#include "focus.h"
#include "focus.var"

float data[NPOINT_DATA]; /* data buffer for host */
struct cstype *cs[NO_SUPERCARD];

main ()
{
    float tstart_err[NPOINT_APER]; /* tstart-tstart_trunc for each position */
    FILE *inputfile; /* input file contains radar data */
    FILE *outputfile; /* output file contains focused image */
    FILE *filterfile; /* input file contains filter coefficients */
    FILE *coefffile; /* input file contains back projection coefficients */
    FILE *tstart_err_file; /* input file contains tstart-tstart_trunc */
    FILE *junkfile;
    char inputname[80];
    char outputname[80];
    char filtername[80];
    char coefname[80];
    char tstart_err_name[80];
    char temp_string[20];
    long section,position,box,coefc_order,coefa_order;
    long i,j; /* just working variable */
```
Appendix B

float f_position;
long data_ready=1; /* mailbox to indicate data ready host --> SC */
long data_consumed=2; /* mailbox to indicate data consumed host <--- SC */
long msg; /* message read from mailbox */
long one=1; /* nonzero message to put in mailbox */
long cacheset=1; /* cacheset=0 turn off cache */
long numpar=1;
float pixel_zero[BOX_SIZE AZIMUTH][NPOINT_RADIAL];

/*** open supercards *********************************************/
for (i=0;i<NO_SUPERCARD;i++)
{
    cs[i]=(struct cstype*)xlubgn_(0,&cacheset,"sc.lo");
}

/*** initialize supercard variables ******************************
focus_varinit();

/*** initialize supercards' id ***********************************/
for(i=0;i<NO_SUPERCARD;i++)
{
    cs[i]->supercard_id=i;
}

/*** Enter Input ***********************************************
printf("Enter input file name (.raw) ==> ");
scanf("%s",inputname);
printf("Enter output file name (.focus) ==> ");
scanf("%s",outputname);
/*
printf("Enter back projection coefficient file name (coefa.dat) ==> ");
scanf("%s",coefname);
printf("Enter start time difference file name (delaytime_diff.dat) ==> ");
scanf("%s",tstart_err_name);
*/
strcpy(coefname,"coefa.dat");
strcpy(tstart_err_name,"delaytime_diff.dat");

printf("Do you want hamming weight across the aperture (y or n) ==> ");
scanf("%s",temp_string);

for(j=0;j<NO_SUPERCARD;j++)
{
    cs[j]->ham_flag=0;
}
if(temp_string[0]=='y')
{
    cs[j]->ham_flag=1;
}
}

strcpy(filtername,"filter.dat");
if((inputfile=fopen(inputname,"rb"))==NULL)
{
    printf("Error open input file\n");
    exit(1);
}
if((outputfile=fopen(outputname,"wb"))==NULL)
{
    printf("Error open output file\n");
    exit(1);
}
if((filterfile=fopen(filtername,"r"))==NULL)
{
    printf("Error open filter file\n");
    exit(1);
}
if((coeffile=fopen(coefname,"r"))==NULL)
{
    printf("Error open back projection coefficient file\n");
    exit(1);
}
if((tstart_err_file=fopen(tstart_err_name,"r"))==NULL)
{
    printf("Error open tstart difference file\n");
    exit(1);
}

/***
 Read filter coefficients ****************************
 /***/
 printf(">>> Reading filter coefficients\n");
 for(i=0;i<FILTER_LENGTH;i++)
 {
     fscanf(filterfile,"%f",&cs[0]->filter_coef[i]);
 }

 for(j=1;j<NO_SUPERCARD;j++)
 {
     for(i=0;i<FILTER_LENGTH;i++)
     {

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```c
  cs[j]->filter_coef[i]=cs[0]->filter_coef[i];
}
```
printf(">>> Starting supercard programs \n");
for(j=0;j<NO_SUPERCARD;j++)
{
    xrcall_("sc",&numpar,&cs[j]->dummy);
}

/*** For every position, the host computer reads data for that ***/ 
/*** position and copy data into each supercard memory. ***********/
/*** There are two mail boxes used between host and each ***********/
/*** supercard to provide synchronization ***************************/

for(section=0;section<SECTION_SIZE;section++)
{
    for(position=0;position<NPOINT_APER/SECTION_SIZE;position++)
    {
        printf(">>> processing section %d pos %d <<<<<<<<\n",section,position);

        /*** Read in data for a position ***********************/*/ 
        fread(data,sizeof(data),1,inputfile);

        for(j=0;j<NO_SUPERCARD;j++)
        {
            /*** Copy data in each supercard memory *******************/
            for(i=0;i<NPOINT_DATA;i++)
            {
                cs[j]->data_temp[i]=data[i];
            }

            /*** Send mail to supercard to inform data is ready *************/
            xlnwxmt_(cs[j],&data_ready,&one);
        }

        /*** Wait until data is consumed by supercards *******************/
        for(j=0;j<NO_SUPERCARD;j++)
        {
            xlwtrec_(cs[j],&data_consumed,&msg);
        }
        /* position */
    } /* section */

    /*** Check for supercards to finish all processing *******************/
    for(j=0;j<NO_SUPERCARD;j++)
    {
        xldone_(cs[j]);
    }
}
Appendix B

/*** Save resulting radar image ********************************************/
for(j=0;j<BOX_BASE_START;j++)
{
    printf(">>>Prepad zero to output file \n");
    fwrite(pixel_zero,sizeof(pixel_zero),1,outputfile);
}
printf(">>>Save image to output file \n");
for(j=0;j<NO_SUPERCARD;j++)
{
    fwrite(cs[j]->pixel,sizeof(float)*BOX_SIZE_AZIMUTH*NPOINT_RADIAL*NO_KBOX_PROCESS/NO_SUPERCARD,
    1,outputfile);
}
for(j=BOX_BASE_START+NO_KBOX_PROCESS;j<NBOX_AZIMUTH;j++)
{
    printf(">>>Postpad zero to output file \n");
    fwrite(pixel_zero,sizeof(pixel_zero),1,outputfile);
}
fclose(inputfile);
fclose(outputfile);

/*** Closing all supercards ********************************************/
for(j=NO_SUPERCARD-1;j>=0;j--)
{
    xlclos_(cs[j]);
}
} /* end main */

B-2. Main Program for Multiple Array Processors (sc.c)

/**************************************************
Program: sc.c
Description: This is the main program to be executed by each of
the CSPI i860 array processor.
**************************************************/
#include "focus.h"
#include "focus.var"
struct cstype *cs;
70
```c
void sc(dummy)
long *dummy;
{
    void focus_varinit();
    void filter_init();
    void haminit();
    void hamwt();
    void erase();
    void inter();
    void fix_data_pointer();
    void poly();
    void bp();
    void xwtrec();
    void xnwxmt();
    void xvmov();
    void xvclr();

    float *data_pointer; /* pointer to actual data */
    long section,position,box,coefficient_order,kbox,ibox;
    long data_ready=1; /* mailbox to indicate data ready host ---> SC */
    long data_consumed=2; /* mailbox to indicate data consumed host <--- SC */
    long msg; /* message read from mailbox */
    long one=1; /* nonzero message to put in mailbox */
    float fposition;
    long boxbase;

    /** initialize supercard pointer *******************************************/
    cs=0;

    /** initialize image with zeros ******************************************/
    xvclr_(cs->pixel,&cs->pixsize,&cs->i_one);

    /** initialize filter ******************************************************
    filter_init();

    /** initialize hamming weight coefficients ********************************
    haminit(cs->ham_coef,NPOINT_APER);

    /** Start forming image ******************************************************
    boxbase=BOX_BASE_START+cs->supercard_id*NO_KBOX_PROCESS/NO_SUPERCARD;

    for(section=0;section<SECTION_SIZE;section++)
    {
        for(position=0;position<NPOINT_APER/SECTION_SIZE;position++)
        {
```
Appendix B

```c
/* Wait for new data from host computer */
xwtrec(&data_ready,&msg);

/* Copy data to working buffer */
xvmov(cs->data,cs->data_temp,&cs->n_data,&cs->i_one,&cs->i_one);

/* Signal host computer that data are consumed */
xnwmt(&data_consumed,&one);

f_position=(float)position;

/* Hamming weight data if needed */
if(cs->ham_flag==1)
{
  hamwt(cs->data,cs->n_data,section*NPOINT_APER/SECTION_SIZE+position,
  cs->ham_coef);
}

/* zeros last portion of data for circular convolution */
erase(cs->data,cs->n_data,32);

/* Interpolate data */
inter(cs->data,cs->n_data,cs->data_inter,
  cs->n_data_inter,cs->filter_fft);

fix_data_pointer(&data_pointer,&cs->data_inter[0],
  cs->start_err[NPOINT_APER/SECTION_SIZE*section+position],
  cs->ts,8);

for(kbox=boxbase;kbox<(boxbase+NO_KBOX_PROCESS/NO_SUPERCARD);kbox++)
{
  for(ibox=IBOX_START;ibox<(IBOX_START+NO_IBOX_PROCESS);ibox++)
  {
    box=kbox*NBOX_RADIAL+ibox;
    /* Generate coefficients for back projection */
    for(coefc_order=0;coefc_order<COEF_SIZE;coefc_order++)
    {
      poly(&f_position,&cs->coef[coefc_order],1,
        &cs->coefa[section][box][coefc_order][0],
        cs->deg[coefc_order]);
    } /* coefc_order */

    /* Perform back projection */
    bp(cs->pixel,data_pointer,cs->n_data_inter,cs->coefc,
```
B-3. Routines Used to Interpolate (inter.c)

#include <math.h>
#include "focus.h"
#include "focus.var"

Subroutine: haminit.c
Description:
this subroutine initialize array of hamming weighting coeffs
across the aperture.
Input: float ham_coef[NPOINT_APER]
long npoint   Number of points for hamming coeffs
Output: float ham_coef[NPOINT_APER] is initialized
******************************************************************************
haminit(ham_coef,npoint)
float *ham_coef;
long npoint;
{
    long i;
    for(i=0;i<npoint;i++)
    {
        ham_coef[i]=.54-.46*cos(2.*3.1415927*(float)i/(float)npoint);
    }
}

******************************************************************************
Subroutine: hamwt.c
Description:
this subroutine takes the radar signal at a position and
multiplies the entire signal array with the hamming coef at
that position.
Appendix B

Input:
float data[NPOINT_DATA]
long npoint_data
long position
float ham_coef[];

Output:
float data[NPOINT_DATA]

****************************************************************************/
hamwt(data,npoint_data,position,ham_coef)
float *data,*ham_coef;
long npoint_data,position;
{
  long i;
  for(i=0;i<npoint_data;i++)
  {
    data[i]=data[i]*ham_coef[position];
  }
}
****************************************************************************/
Subroutine: inter.c
Description:
  This routine performs FIR interpolation by using convolution in the frequency domain. The input buffer contains 2K of data and is interpolated into 16K of data. The FIR filter has breakpoints at .95 Ghz and 1.05 Ghz
  # of taps = 255
  name of filter coeff. file : filter.dat
Input:  data[NPOINT_DATA]
        complex filter_fft[NPOINT_DATA_INTER/2]
        float nyquist_filter
Output: data_inter[NPOINT_DATA_INTER]
****************************************************************************/
inter()
{
  void xveir_();
  void xfrf_();
  void xcvmls_();
  void xcvms_();
  void xfri_();
}
extern struct cstype *cs;

int i;

/* clear data_inter buffer */
xvclr_(cs->data_inter,&cs->n_data_inter,&cs->i_one);

/* interleave data into data-inter buffer */
for(i=0;i<NPOINT_DATA;i++)
{
    cs->data_inter[i*8]=cs->data[i];
}

/* FFT of interleaved data */
xffr_(cs->data_inter_fft,&cs->nyquist_data,cs->data_inter,
     &cs->n_data_inter_half);

/* FFT of interpolated data (multiply with filter in freq. domain)*/
xcvmls_(cs->data_inter_fft,&cs->f_one,cs->data_inter_fft,
     cs->filter_fft,&cs->n_data_inter_half);

   cs->nyquist_data=cs->nyquist_data*cs->nyquist_filter;

/* inverse FFT to get interpolated data */
xffri_(cs->data_inter,&cs->nyquist_data,cs->data_inter_fft,
     cs->data_inter_fft,&cs->n_data_inter_half);

}

*************************************************************************
Subroutine: fix_data_pointer

Description: This subroutine fixes the pointer to the start of
data_inter buffer. The pointer needed to be adjusted
due to the following reasons:

(a) The linear FIR interpolation filter has phase
    shift and the actual data point starts at bin 127
    of the data_inter buffer (FIR has 255 coeffs)
(b) The actual time to start data acquisition has to
    be rounded of to 1 nsec resolution for the scope
    DSA602. However the backprojection algorithm uses
    the exact time since the indeces have to be smooth
    for curve fit.
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Input:
float *data_inter (address of data_inter buffer)
float tstart_err (tstart-tstart_trunc)
float ts (radar sampling period)
long inter_factor (interpolation factor)

Output:
float *data_pointer (actual start pointer for data)

**************************************************************************
fix_data yointer(pointer, data_inter, tstart_err, ts, inter_factor)
float **pointer;
float *data_inter;
float tstart_err;
float ts;
long inter_factor;
{
    long i;
    double float1, float2;
    unsigned long index_offset;
    float1 = modf(tstart_err * inter_factor / ts, &float2);
    if (float1 >= .5) float2 = float2 + 1.;
    index_offset = (unsigned long)127 + (unsigned long)float2;
    *pointer = data_inter + index_offset;

    /* zeros fill first 128 points of data_inter since phase shift from linear filter */
    for (i = 0; i < 128; i++)
    {
        data_inter[i] = 0.;
    }

    /* zeros fill the last 128 points of data_inter plus 8 points for tstart_err */
    for (i = 0; i < 136; i++)
    {
        data_inter[NPOINT_DATA_INTER + i] = 0.;
    }

    /* first point and last point of actual data array are zeros for backprojection */
    **pointer = 0.;
    *((pointer + NPOINT_DATA_INTER - 1)) = 0.;
}

**************************************************************************
Appendix B

Subroutine: erase

Description: Zero out the last nzero points of input buffer

***************************************************************************/

erase(buffer,ndata,nzero)
float *buffer;
long ndata,nzero;
{
    long i;
    for(i=ndata-nzero;i<ndata;i++)
    {
        buffer[i]=0.;
    }
}

B-4. Initialize Interpolation Filter (filtinit.c)

***************************************************************************/

#include <stdio.h>
#include "focus.h"
#include "focus.var"

extern struct cstype *cs;

void filter_init()
{
    void xfrf();
    long i;

    /* zero pad filter coeff */
    for(i=FILTER_LENGTH;i<NPOINT_DATA_INTER;i++)
    {
        cs->filter_coeff[i]=0.;
Appendix B

/* take fft of filter coef for each supercard */
for(i=0;i<NO_SUPERCARD;i++)
{
    xfrf_(cs->filter_fft,&cs->nyquist_filter,
            cs->filter_coef,&cs->n_data_inter_half);
}

B-5. Main Back Projection Focusing Routing (bp.c)

#include "math.h"
/****************************************************************************
Subroutine: poly.c
DESCRIPTION:
Calculates values of polynomials
Input: x[] input array
    n number of elements
    coeff[] coefficients of poly
    deg degree of poly
Output: y[] output array
****************************************************************************/
poly(x,y,n,coeff,deg)
float *x,*y,*coeff;
long n,deg;
{
    long i,j;
    for(i=0;i<n;i++)
    {
        y[i]=coeff[0];
        for(j=1;j<(deg+1);j++)
        {
            y[i]=y[i]+coeff[j]*pow(x[i],(float)j);
        }
    }
}  
/****************************************************************************
Subroutine: poly2.c
Description: calculate y=c0+c1*x+c2*x^2
            where x=[0,1,2,...,n-1]
Appendix B

Input:
float c[3]  coefficients
long n (max : 1000) number of points

Output:
float y[]  output vector

***************************************************************************/

#define MAX_ELEMENT 1000

void poly2(y,n,c)
float y[],c[];
long n;
{
    void xvrmp_();
    void xdintg_();
    float temp;
    float y1[MAX_ELEMENT];
    float y1_init,y1_inc;
    y1_init=c[1]-c[2];
    y1_inc=2.0*c[2];
    xvrmp_(y1,&temp,&y1_init,&y1_inc,&n);
    y1[0]=0.0;
    xdintg_(y,&c[0],y1,&temp,&n);
}

****************************************************************************

Two-dimensional back projection subroutine
using fast algorithm by Nuttal to calculates the index to data
array for each pixel on the ground in i_box,k_box positioned by i,k
k: azimuth (2nd order)
i: range (1st order)
The equation for index calculation is
index= c0+c1*k+c2*k^2 + (c3+c4*k+c5*k^2)*i
    = d0 + d1*i
where c(i) (i=0,5) is a set of coefficients for each box and
each position in the aperture

Input:
float *pixel  pointer to first point of the image
2-dimensional area
float *data  pointer to data array
Important: data[0]=0.0
            data[dat_size-1]=0.0
long  dat_size size of data buffer
Appendix B

float *c  pointer to six coefficients for index computation
long k_pix_size  size of the patch (pixels) in k axis
long i_pix_size  size of the patch (pixels) in i axis
long k_box  patch number in k axis
long i_box  patch number in i axis
long i_box_size  number of patches in i axis

Output:
index to data array is calculated and pixel is updated

*******************************************************************************
#define MAX_K_PIX_SIZE 1000
#define MAX_I_PIX_SIZE 1000

void bp(pixel, data, dat_size, c, k_box_base, k_box, i_box, k_pix_size,
        i_pix_size, i_box_size)

float *pixel;  /* array of pixels of the whole 2-dimentional area */
float *data;  /* data array */
long dat_size;  /* size of data array */
float *c;  /* pointer to six coefficients for index computation */
long k_box_base;  /* 0 for 1st SC, i*NBOX_AZIMUTH/NO_SUPERCARD for ith SC */
long k_box;  /* patch number in k axis */
long i_box;  /* patch number in i axis */
long k_pix_size;  /* size of the patch (pixels) in k axis */
long i_pix_size;  /* size of the patch (pixels) in i axis */
long i_box_size;  /* number of patches in i axis */
{
    void xvcclip_0;
    void vclip_0;
    void xvfx4_0;
    void fix4_0;
    void xvrmp_0;
    void vindex_0;
    void vramp_0;
    void vgathr_0;
    void vadd_0;
    void vtabi_0;

    float findex[MAX_I_PIX_SIZE];  /* data index value */
    long lindex[MAX_I_PIX_SIZE];  /* data index value (round to integer) */
    float pix_temp[MAX_I_PIX_SIZE];  /* temp buffer for back projection */
    float d0[MAX_K_PIX_SIZE];  /* d0= c0+c1*k+c2*k^2 */
    float d1[MAX_K_PIX_SIZE];  /* d1= c3+c4*k+c5*k^2 */
float *pix_index; /* pointer to current pixel */
long pix_index_inc; /* each time k is incremented, pixel pointer is jumped */
long k;  /* for k and i loops control */
float maxindex; /* maximum value for data index */
float zero=0.0;
float one=1.0;
long i_one=1;
float temp;

maxindex=(float)(dat_size-1);

pix_index=pix_index+(k_box-k_box_base)*k_pix_size*i_box_size*
    i_pix_size+i_box*i_pix_size;
    /* index of first point of the patch */
    /* with respect to pixel */
pix_index_inc=i_pix_size*i_box_size; /* index increment along k axis */

for(k=0;k<k_pix_size;k++)
{
    /* generate floating point index vector */
    vramp_( &d0[k], &d1[k], findex, &i_one, &i_pix_size);
    /* table look up and interpolate */
    /* this function replaces xvclip(),xvfxc(),vgathr() */
    /*
    vtabi_(findex, &i_one, &one, &zero, data, pix_temp, &i_one, &dat_size, &i_pix_size);
    */
    /* clip index */
    vclip_( findex, &i_one, &zero, &maxindex, findex, &i_one, &i_pix_size);
    /* convert to integer index */
    fix4_( findex, &i_one, lindex, &i_one, &i_pix_size);
    /* gather data into temporary buffer */
    vgathr_( data, lindex, &i_one, pix_temp, &i_one, &i_pix_size);
    /* update pixel array with data from temporary buffer */
    vadd_( pix_index, &i_one, pix_temp, &i_one, pix_index, &i_one, &i_pix_size);
    /* pix_index jumps along k axis */
    pix_index=pix_index+pix_index_inc;
Appendix B

} /* k loop */

} /* subroutine */

B-6. Declare All Global Constants (Focus.h)

#define NO_SUPERCARD 3      /* number of supercards */
#define NPOINT_AZIMUTH 600   /* number of bearing lines */
#define NPOINT_RADIAL 4095   /* number of radial lines */
#define NPOINT_APER 2304     /* # of positions in aperture */
#define NPOINT_DATA 2048     /* number of original data points */
#define NPOINT_DATA_INTER NPOINT_DATA * 8 /* number of data points after interpolated */
#define FILTER_LENGTH 255    /* length of FIR filter */
#define PI 3.141592654       /* PI */
#define RADAR_HEIGHT 60.    /* radar height in feet */
#define A_OFFSET -15.0       /* offset angle from center line */
#define A_SPAN 54.0          /* spanning angle of the patch */
#define RMINCENTER 550.      /* range from center position to reference point on the patch */
#define RCENTER_REF 802.0    /* range (ft) of ref. point from center pos. */
#define THETA_CENTER_REF -15.0 /* angle (deg) of ref. point from center pos. */
#define SAMPLING_RATE 2.0e09 /* sampling frequency of signal */
#define SAMPLING_PERIOD 5.0e-10 /* ts=1/fs */

#define BOX_SIZE_RADIAL 195
#define BOX_SIZE_AZIMUTH 100
#define NBOX_RADIAL NPOINT_RADIAL/BOX_SIZE_RADIAL
#define NBOX_AZIMUTH NPOINT_AZIMUTH/BOX_SIZE_AZIMUTH
#define BOX_BASE_START 2
#define NO_KBOX_PROCESS 3
#define IBOX_START 10
#define NO_IBOX_PROCESS 1

#define SECTION_SIZE 4      /* # of sections for one aperture */
#define COEF_SIZE 6          /* # of coeffs for curve fit */
#define MAXDEG 3             /* maximum degree for poly. fit */
#define NPOINT_BOXSAMPLE_RADIAL 5 /* # of samples in a box in radial direction */
#define NPOINT_BOXSAMPLE_AZIMUTH 5 /* # of samples in azimuth direction for every box */

#define NPOINT_BOXSAMPLE
B-7. Declare All Global Variables (Focus.var)

```c
struct complex { float r, i; }; /* define a complex type */

struct cstype {
    /* Data Variables */
    float pixel[NPOINT_AZIMUTH/NO_SUPERCARD][NPOINT_RADIAL]; /* array of image */
    float data_temp[NPOINT_DATA]; /* temp buffer for data */
    float data[NPOINT_DATA]; /* original data buffer */
    float filter_coef[NPOINT_DATA_INTER]; /* filter coefficients */
    float data_inter[NPOINT_DATA_INTER+136]; /* interpolated data buffer */
    float tstart_err[NPOINT_APER]; /* tstart-tstart_trunc for each position */
    struct complex data_inter_fft[NPOINT_DATA_INTER/2]; /* Real->Complex Forward FFT of data_inter */
    struct complex filter_fft[NPOINT_DATA_INTER/2]; /* Real->Complex Forward FFT of filter_coef */
    float nyquist_filter; /* value of FFT of filter at Nyquist point */
    float nyquist_data; /* value of FFT of data at Nyquist Point */
    long ham_flag; /* to indicate whether to use hamming or not */
    float ham_coef[NPOINT_APER]; /* hamming weight coefficients */

    /* Geometry Variables */
    float a_offset; /* offset angle from the center line */
    float a_span; /* spanning angle of the patch */
    float d_theta; /* delta angle */
    float x, theta; /* coordinate of a pixel */
    float c_theta, s_theta; /* cosine and sine of the theta */
    float d; /* distance from radar to center position */
    float rcenter, rmincenter, rmaxcenter; /* range from center position */
    float rcenter_ref; /* range from center pos. to ref point */
    float theta_center_ref; /* angle of ref. point from center position */
    float r_ref; /* range from any pos. to ref. point */
    float d_rcenter; /* sampling distance from center position */
    float dr8; /* (sampling distance)/8 */
    float r, rmin, rmax; /* range from any position */
    float aper_length; /* length of aperture */
    float radar_height; /* height of radar */
    float radar_height2; /* square the height of radar */
};
```
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/* Radar Variables */
float c; /* speed of wave */
float ts; /* sampling period of signal */
float fs; /* sampling frequency of signal */

long n_azimuth; /* # of points in azimuth direction */
long n_radial; /* # of points in radial direction */
long n_aper; /* # of positions in aperture */
long pix_size; /* # of points in pixel array */
long n_data; /* number of original data points */
long n_data_inter; /* number of interpolated data points */
long n_data_inter_half; /* 1/2 # of interpolated data points */
long n_boxsample; /* # of samples in a box for curve fit */
long n_coef; /* # of coefficients curve fit */
long n_section; /* # of sections for one aperture */
long k_pix_size; /* # of pixels of a box in azimuth direction */
long i_pix_size; /* # of pixels of a box in radial direction */
long k_box_size; /* # of boxes in azimuth direction */
long i_box_size; /* # of boxes in radial direction */

/* SSL Variables */
long supercard_id; /* to identify board number */
float f_zero; /* floating point zero */
float f_one; /* floating point 1 */
long i_one; /* integer 1 */
long stride; /* stride for supercard ssl */
long ierr; /* error message from lib call */
long dummy; /* just a dummy argument pass to SC program */

/* working variables */
long n_position;
float e_index,a_index,error,maxerror,minerror;
long ierr_max,jerr_max,ierr_min,jerr_min;
long column_max,row_max,column_min,row_min;
long ia,ib;
long ipixel,jpixel;
float coefc[COEF_SIZE]; /* c coefficients */
float
cofa[SECTION_SIZE][NBOX_RADIAL*NBOX_AZIMUTH][COEF_SIZE][MAXDEG+1];/* a coef. for each c */
long deg[COEF_SIZE]; /* degree for each coefc */
long mat_c_stride,findex_c_stride,coef_c_stride;
float tstart_diff[NPOINT_APER]; /* time difference between quantized and */
/* unquantized values from trigger to */
/* start data acq. at each position */
B-8. Initialize All Global Variables on Both Processors 
(varinit.c)

******************************************************************************
/* This subroutine performs the following: */
/* Initialize both host and Supercard Variables */
/* Output: */
/* All variables */
******************************************************************************
#include "focus.h"
#include "focus.var"

extern struct ctype *cs[NO_SUPERCARD];

focus_varinit()
{
    long j;

    for(j=0;j<NO_SUPERCARD;j++)
    {
        cs[j]->n_azimuth=NPOINT_AZIMUTH; /* # of points in azi. direction */
        cs[j]->n_radial=NPOINT_RADIAL; /* # of points in rad. direction */
        cs[j]->pix_size=cs[j]->n_azimuth*cs[j]->n_radial/NO_SUPERCARD;
        /* Pixel array size */
        cs[j]->n_data=NPOINT_DATA; /* # of orig. data points */
        cs[j]->n_data_inter=NPOINT_DATA_INTER;/* # of interpolated. data points*/
        cs[j]->n_data_inter_half=NPOINT_DATA_INTER/2;
        /* 1/2 # of inter. data points */
        cs[j]->n_aper=NPOINT_APER; /* # of points in the aperture */
        cs[j]->n_coef=COEF_SIZE; /* # of coeffs for curve fit */
        cs[j]->n_section=SECTION_SIZE; /* # of sections for one aperture*/
        cs[j]->i_pix_size=BOX_SIZE_RADIAL; /* # of pixels of a box in rad. dir.*/
        cs[j]->k_pix_size=BOX_SIZE_AZIMUTH; /* # of pixels of a box in az. dir. */
        cs[j]->i_box_size=NBOX_RADIAL; /* # of boxes in radial direction */
        cs[j]->k_box_size=NBOX_AZIMUTH; /* # of boxes in azimuth direction */

        /* Radar Variables */
        cs[j]->fs=SAMPLING_RATE; /* Sampling Frequency */
        cs[j]->ts=SAMPLING_PERIOD; /* Sampling period */
        cs[j]->c=3.e8; /* Speed of wave */
Appendix B

/* SSL Variables */
cs[j]->f_zero=0.;   /* floating point zero */
cs[j]->stride=1;   /* stride for ssl */
cs[j]->f_one=1.0;   /* floating point 1 */
cs[j]->i_one=1;    /* integer 1 */
cs[j]->mat_c_stride=cs[j]->n_boxsample; /* column stride for mat */
cs[j]->findex_c_stride=1;  /* column stride for findex */
cs[j]->coef_c_stride=1;   /* column stride for coeff */
cs[j]->deg[0]=3; /* degree for first coef */
cs[j]->deg[1]=3;
cs[j]->deg[2]=3;
cs[j]->deg[3]=3;
cs[j]->deg[4]=2;
cs[j]->deg[5]=2;

} /* end focus_varinit */
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I, the undersigned, am aware of the adversary's interest in DOD publications and in the subject matter of this material and that, to the best of my knowledge, the net benefit of this release outweigh the potential damage to the essential security of all ARL, AMC, Army, or other DOD programs of which I am aware.

John Costanza
OPSEC Reviewer (Printed name/signature)

Since this report was published 16 years ago, the technology described herein has become routine and is no longer critical technology.

**Final Release Clearances**

32. Public/Limited release information

a. Material has been reviewed for OPSEC policy.

ARL OPSEC Officer

b. The information contained in this material is ☒ / is not ☐ approved for public release/ has received appropriate tech/editorial review.

Division Chief

C. This information is accepted for public release.

Public Affairs Office

ARL Form 1
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