Parametric Models of NIR Transmission and Reflectivity Spectra for Dyed Fabrics

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This study examines parametric modeling of near-infrared (NIR) transmission and reflectivity spectra for dyed fabrics, which provides for both their inverse and direct modeling. The dyes considered for prototype analysis are triarylamine, tetraaryldiamine, transition metal dithiolene, and indolium iodide. The fabrics considered are camouflage textiles characterized by color variations. The results of this study provide validation of the constructed parametric models, within reasonable error tolerances for practical applications, including NIR spectral characteristics in camouflage textiles, for purposes of simulating NIR spectra corresponding to various dye concentrations in host fabrics, as well as potentially to mixtures of dyes.

Parametric Modeling
Absorption coefficient
Inverse/direct analysis
NIR/SWIR absorbing dyes
Dielectric function
Reflection/transmission

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Parametric Models of NIR Transmission and Reflectivity Spectra for Dyed Fabrics

Introduction

Parametric models of NIR transmission and reflectivity spectra for dyed fabrics are presented, which provides for both their inverse and direct modeling [1]. The fabrics considered are camouflage textiles characterized by color variations. The dyes considered for prototype analysis are triarylamine (Dye 978), tetraaryldiamine (Dye 949), transition metal dithiolene (Dye 836) and indolium iodide (Dye 775) [2]. These dyes are within classes that are of interest to the U.S. Navy for the purpose of developing specific NIR spectral characteristics in camouflage textiles and other materials. The results of this study provide validation of the constructed parametric models, within reasonable error tolerances for practical applications, including NIR spectral characteristics in camouflage textiles, for purposes of simulating NIR spectra corresponding to various dye concentrations in host fabrics, as well as potentially to mixtures of dyes. Further, the results of this study demonstrate that absorption coefficients for dyes, which have been obtained previously by inverse analysis of transmission spectra for dyes in solution, can be validated as reasonable estimates of absorption coefficients for dyes in fabrics, which may be characterized as solid composite systems. Further, this study demonstrates proof of concept for parametric modeling of reflection from dyed fabrics by adopting a formalism similar to that of multicomponent analysis of spectra, which is typically for analysis of transmission through solutions containing varieties of solvents.
Parametric Models of NIR Spectra for Dyed Fabrics

Physically consistent parametric models provide a means for investigating the dielectric response characteristics of a given system that is characterized by a given material, or combination of materials, and geometry, in terms of both inverse and direct analysis [1]. For transmission through and reflection from a dyed fabric of finite and nonuniform thickness, whose material composition is heterogeneous, a general framework for parametric modeling of transmission and reflectivity spectra is given by

\[
T_{f+d,M}(\lambda) = \exp \left[ \sum_{j=1}^{N} C_{a,j} \alpha_{M,j}(\lambda) d \right] T_f(\lambda) \tag{1a}
\]

\[
T_{f+d,M}(\lambda) = \left[ 1 - \sum_{j=1}^{N} C_{a,j} \alpha_{M,j}(\lambda) d \right] T_f(\lambda) \tag{1b}
\]

\[
Z_T = \sum_{n=1}^{N} w_n \left( T_{f+d,M}(\lambda_n) - T_m(\lambda_n) \right)^2 \tag{2}
\]

\[
R_{f+d,M}(\lambda) = \exp \left[ \sum_{j=1}^{N} A_{a,j} \alpha_{M,j}(\lambda) \right] R_f(\lambda) \tag{3a}
\]

\[
R_{f+d,M}(\lambda) = \left[ 1 - \sum_{j=1}^{N} A_{a,j} \alpha_{M,j}(\lambda) \right] R_f(\lambda) \tag{3b}
\]

\[
Z_R = \sum_{n=1}^{N} w_n \left( R_{f+d,M}(\lambda_n) - R_m(\lambda_n) \right)^2 \tag{4}
\]

where \(d\) is the average thickness of the fabric layer, and \(\alpha\) is the absorption coefficient. The formal procedure underlying inverse analysis based on Eqs.(1)-(4) entails adjustment of the absorption coefficients defined over the entire wavelength region, if assumed unknown, and the concentration coefficients \(C_a\) and \(A_a\). This approach defines an optimization procedure where the transmission or reflectivity spanning the range of wavelengths is adopted as the quantity to be optimized. Constraint conditions are imposed on the transmission or reflectivity by minimizing the objective functions defined by Eqs. (2) and (4), respectively, where \(T_m(\lambda_n)\) and \(R_m(\lambda_n)\) are the measured or target transmission and reflectivity for wavelength \(\lambda_n\). The quantities \(w_n(n=1,...,N)\) are weight coefficients that specify relative levels of influence associated with constraint conditions \(T_m(\lambda_n)\) and \(R_m(\lambda_n)\).
The mathematical foundation of inverse analysis based on Eqs. (1)-(4) is that of least-squares parameter optimization [3, 4]. A significant aspect of least-squares parameter optimization is the choice of a sufficiently complete set of basis functions. This implies that all possible modes of a given process can be modeled parametrically by linear combinations of these functions. Accordingly, the parametric models defined by Eqs. (1a,b) and (3a,b) adopt absorption coefficients as basis functions. The general forms of Eqs. (1a,b) and (3a,b) are based on trend features following those of the Beer-Lambert law. Their parameterizations, however, are phenomenological in nature.

Direct modeling (or system simulation) based on Eqs. (1a,b) and (3a,b) provides a means for predicting the dielectric response characteristics of a layer of dyed fabric. For the case of a layer of dyed fabric, direct modeling assumes that material properties, e.g. absorption coefficients, have been estimated reasonably and that model parameters represent system response for the range of variation of quantities characterizing the system, e.g., dye concentration, as well as quantities or metrics associated with the dying process or with fabric characteristics.
Case Study: Analyses of NIR Spectra for Dyed Fabrics

In this section, prototype analyses of NIR transmission and reflectivity spectra for dyed fabrics are described. The fabrics considered are camouflage textiles characterized by color variations. The dyes considered for prototype analysis are triarylamine, tetraaryldiamine, transition metal dithiolene and indolium iodide [2]. For the spectra analyzed, our goal is to parametrically model the transmission and reflection characteristics of the dyes as a function of concentration.

First, we seek to parametrically model transmission characteristics of the dyes as a function of concentration. Shown in Figs. (1)-(4) are measured transmission spectra for dyed fabrics as a function of dye concentration. Accordingly, we define the quantity

\[ T_{d,E}(\lambda, C_a) = \frac{T_{f+\text{d,E}}(\lambda, C_a)}{T_{f,E}(\lambda)} = C_o \frac{T_{f+\text{d,E}}(\lambda, C_a)}{\langle T_{f,E}(\lambda) \rangle} \]  

where, because of small spectral variations for the untreated fabric associated with different colors (see Figs. (5) and (6)), we introduce the scaling parameter \( C_0 \), which represents small adjustments on the order of unity. This follows in that the transmission defined by Eq.(5) is based on background subtraction using an averaged transmission spectrum \( \langle T_{f,E}(\lambda) \rangle \) for the untreated fabric, which is shown in Fig. (7). Next, adopting the parametric model Eq.(1a), and assuming background subtraction with a scale factor \( C_o \), the modeled transmission component of the dyes as a function of concentration is given by

\[ T_{d,M}(\lambda, \beta) = C_o \frac{T_{f+\text{d,M}}(\lambda, C_a)}{T_{f}(\lambda)} = C_o \exp [C_a \alpha_M(\lambda) d] = C_o \exp [-\beta \alpha_M(\lambda)] \]  

where \( \beta = C_o d \). The transmission defined by Eq.(6) assumes that the quantities \( C_a \) and \( d \) are averaged quantities in that the dyed fabrics do not have uniform thickness and are heterogeneous in composition. Accordingly, their combined influence is represented by a single adjustable parameter. Proceeding, values of the parameters \( C_o \) and \( \beta \) as a function of dye concentration are determined. Estimates of the absorption coefficients \( \alpha_M(\lambda) \) for the dyes considered have been determined previously by inverse analysis of transmission spectra for these dyes in solution. For this analysis, we do not consider parameter optimization in the strict sense of objective function minimization, but rather a relaxed parameter adjustment with respect to qualitative agreement of measured and modeled spectra. It is important to note that a relaxed criterion for parameter optimization is consistent with the statistical nature of the measured spectra, which are for a nonuniform and irregular system. Shown in Figs. (8)-(11) are comparisons of experimental and modeled spectra, defined by Eqs. (5) and (6), respectively.

Next, we seek to parametrically model reflectivity characteristics of the dyes as a function of concentration. Shown in Figs. (12)-(15) are the reflectance spectra of untreated \( R_{f,E} \) and dyed fabric \( R_{f+\text{d,E}} \) as a function of dye concentration. Shown in Figs. (16)-(19) are scaled absorption coefficients as a function of dye concentration defined by

\[ A_a \alpha_E(\lambda) = 1 - \frac{R_{f+\text{d,E}}(\lambda, A_a)}{R_{f,E}(\lambda)} \]  

4
where the phenomenological coefficient $A_a$ is proportional to the density of dye molecules extending over a penetration depth of the fabric and inversely proportional to the level of scattering. The experimental quantity defined by Eq.(7) is modeled parametrically by the scaled absorption coefficient $C_{αM}(λ)$. Shown in Figs. (20)-(23) are comparisons of measured and modeled absorption spectra, defined by Eq. (7) and $C_{αM}(λ)$, respectively, where the absorption coefficients $α_M(λ)$ have been determined previously by inverse analysis of transmission spectra for these dyes in solution. Again, for this analysis, we do not consider parameter optimization formally by means of objective function minimization, but rather relaxed parameter adjustment based on qualitative agreement of measured and modeled spectra. Shown in Fig. (24) are values of $C_a$ as a function of dye concentration.

**Conclusion**

The fitting of modeled to experimental spectra shown in Figs. (8)-(11) and Figs. (20)-(23) for transmission and reflection, respectively, as well as the relatively good consistency of these fits, establishes proof of concept for constructing mappings from a process-parameter space, i.e., dye concentrations, to a model-parameter space, i.e., parameters $C_α$ and $β$ for transmission spectra and $C_a$ for reflectivity spectra. This in turn establishes that the parametric models defined by Eqs. (1a,b) and (3a,b) can be adopted for prediction of dyed fabric transmission and reflection characteristics for process parameters that can be mapped into a physically consistent range of values for model parameters.

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**References**

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