INTERACTIONS OF ULTRACOLD IMPURITY PARTICLES WITH BOSE-EINSTEIN CONDENSATES

Georg Raithel
UNIVERSITY OF MICHIGAN

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Final Report
14. ABSTRACT

Research on interactions between quantum gases and impurities has become an active area of AMO. Here, two setups have been constructed and operated towards these goals. In the first, a metal tip (diameter 125 microns) is mounted close to a magneto-optic trap (MOT). Rydberg excitations are implanted in a cold-atom region (diameter about 10 microns, length about 50 microns). Interactions between the excitations cause excitation blockades, short- and medium-range order, as well as dynamics due to van-der-Waals interaction. All these topics were studied. The second setup is a double-trap system, in which magnetically trapped rubidium atom samples are prepared between 1 and 10 micro-Kelvin temperature and densities of about $10^12$ cm$^{-3}$. Cold circular Rydberg atoms have been prepared and trapped. The dynamics of these highly dipolar atoms in the magnetic trap was studied, and collision-induced loss was observed and traced back to collisions between the long-lived circular atoms and cold ground state atoms. Novel D-type molecules between Rydberg and ground-state atoms were realized. These molecules are due to an attractive triplet s-wave low-energy electron scattering interaction. Five papers were published [two Phys. Rev. Lett, 2 Phys. Rev. A] and one submitted to PRL.
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Abstract.

Research on interactions between quantum gases and impurities (ions, other atoms etc.) has become an active area of AMO research over the past couple of years. Among the topics of interest one finds the formation of mesoscopic ions, charge hopping and quantum transport, self trapping of impurities in Bose-Einstein Condensates (BECs), and the effect of impurity particles on the BEC density distribution. To study ion-BEC interactions, a method must be used that allows one to hold a cold ion in a BEC for a sufficiently long time that these phenomena become observable, in a way that does not heat the ion.

In the project two setups have been constructed and operated towards these goals. In the first, more basic one, a metal tip (diameter 125 microns) is mounted close to a magneto-optic trap (MOT). Rydberg excitations are implanted in a cold-atom region (diameter about 10 microns, length about 50 microns). Interactions between the excitations cause excitation blockades, short- and medium-range order, as well as dynamics due to van-der-Waals interaction. All these topics have been studied. Two papers were published [one PRL, one PRA, one submitted to PRL].

The second setup is a double-trap system, in which we prepare magnetically trapped rubidium atom samples between 1 and 10 micro-Kelvin and densities of about $10^{12}$ cm$^{-3}$. We have prepared and trapped, for the first time, cold circular Rydberg atoms in these traps. In addition to being able to study the dynamics of these highly dipolar atoms in the magnetic trap, we also observed a collision-induced loss we have traced back to collisions between the long-lived circular atoms and cold ground state atoms. These types of collisions are unexplored, to date. In this setup we also have prepared and studied D-type molecules between Rydberg and ground-state atoms. These are due to an attractive triplet s-wave low-energy scattering interaction between the Rydberg electron and a ground-state atom. We have published two papers, one in PRL, on in PRA.

Archival publications during reporting period (all attached):


**Activity (1):** We have imaged spatial correlations of Rydberg excitations in cold atom clouds. We use direct spatial imaging of cold 85Rb Rydberg atom clouds to measure the Rydberg-Rydberg correlation function. Initially obtained results were in qualitative agreement with theoretical predictions elsewhere. We determined the blockade radius for several D-level Rydberg states and investigated the dependence of the correlation behavior on excitation conditions and detection delay. Experimental data hinted at the existence of long-range order. We then extended the research to include light-shift potentials generated by an optical dipole trap. The optical dipole trap is used to prepare dense ground-state atom samples and to add light-shifts to the ground-Rydberg transition. We studied and interpreted the effects of laser detuning and light-shifts on the Rydberg pair-correlation function. The result showed an enhancement of the probability of exciting two Rydberg atoms at a particular separation distance, which is interpreted as a result of direct two-photon excitation of Rydberg atom pairs. In another experiment, we investigated the effect of the time delay between the excitation pulses and the read-out sequence. We observed a time dependence of the pair-correlation signal which is consistent with the effect of van-der-Waals forces acting between Rydberg-atom pairs. The results are significant because of the wide use of optically trapped Rydberg atoms in both ongoing and in proposed research. Three papers (one submitted, two published) are attached [*,3,5].

**Activity (2):** We have successfully prepared and trapped circular Rydberg atoms. Circular Rydberg atoms exhibit a unique combination of extraordinary properties: long lifetimes (~$n^5$), large magnetic moments and angular momenta $(|m|=l=n-1)$, and no first order Stark shift. Here, n, l and m are the principal, orbital and magnetic quantum numbers, respectively. These features have made circular Rydberg atoms attractive for a number of applications. We realized a magnetic trap for laser-cooled Rydberg atoms that are initially in a well-defined circular Rydberg state. The Rydberg-atom trap was characterized using state-selective electric-field ionization, direct spatial imaging of the atom distributions, and time-of-flight analysis of the ion signal. At room temperature, we observed 70 percent of the trapped atoms remaining after 6ms. We measured an enhancement of the center-of-mass trap oscillation frequency by the expected factor of $\sqrt{m}$. Simulations of the state-evolution of circular-state atoms in our magnetic trap, held at 300K radiation temperature, were performed and results were in good agreement with the observed phenomena. One published paper is attached [4].

**Activity (3):** One of the most prominent recent observations of impurities in dense cold atom clouds is that of Rydberg molecules. A recently discovered class of long-range Rydberg molecules generated through an attractive Fermi potential has generated a significant amount of theoretical and experimental interest. Here, we have observed long-range homonuclear diatomic nD Rydberg molecules photoassociated out of an ultracold gas of 87Rb atoms for $34<n<40$. We measured the ground-state binding energies of 87Rb (nD+5S_1/2) molecular states to be larger than those of their 87Rb(nS+5S_1/2) counterparts, showing the dependence of the molecular bond on the angular momentum of the Rydberg atom. We probed the transition of 87Rb(nD + 5S_1/2) molecules from the molecular-binding-dominant regime at low n [Hund's cases (a)] to a fine-structure-dominant regime at high n [Hund's case (c)]. A Fermi model that includes the fine structure of the nD Rydberg atom and hyper fine structure of the 5S_1/2 perturber is presented that describes this transition. In ongoing work, we include 3S, 3P, 1S and 1P scattering channels for accurate modeling of the molecular spectra. Two published papers are attached [1,2].
Measurement of van-der-Waals interaction by atom trajectory imaging

N. Thaicharoen*, A. Schwarzkopf†, and G. Raithel

Department of Physics, University of Michigan, Ann Arbor, MI 48109
(Dated: June 6, 2015)

We study the repulsive van der Waals interaction of $70S_{1/2}$ cold rubidium Rydberg atoms by analysis of time-delayed pair correlation functions. After excitation, Rydberg atoms are allowed to accelerate under the influence of the van der Waals force, before measuring their positions using a single-atom imaging technique. From the average pair correlation function of the atom positions we obtain the initial atom-pair separation and the terminal velocity, which yield the van der Waals interaction coefficient $C_6$. The measured $C_6$ value agrees well with calculations. The experimental method has been validated by simulations. The data hint at anisotropy in the overall expansion, caused by the shape of the excitation volume. Our measurement implies that the interacting entities are individual Rydberg atoms, not groups of atoms that coherently share a Rydberg excitation.

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The van der Waals interaction is important in the description and control of interactions in few- and many-body dynamics studies. This interaction has been critical in the observation of Rydberg excitation blockades and collective excitations [1–4], Rydberg crystals [5, 6], and Rydberg aggregates [7, 8]. Rydberg interactions have been used in quantum information processing [9–12]. The van der Waals interaction between two Rydberg atoms has been measured using spectroscopic methods [13, 14]. Several measurements have been performed near surfaces to observe radiative Rydberg-level shifts caused by image charge interaction near metal surfaces [15, 16]. The van der Waals interaction between excited cesium atoms and a dielectric surface has been measured using selective reflection spectroscopy [17].

Here, we develop a method to study the van der Waals interaction between Rydberg atoms using direct spatial imaging of their trajectories [18–21]. Pairs of $S_{1/2}$ rubidium Rydberg atoms are prepared with a well-defined initial separation by detuning an excitation laser and utilizing the $r^{-6}$ dependence of the van der Waals interaction [21, 22]. After preparation, the atoms are subject to van der Waals forces (which are repulsive in this case). The effect of the forces is observed by tracking the interatomic distance of the Rydberg atoms, after they have been allowed to move for selected wait times (see Fig. 1). The atom trajectories and thereby the van der Waals interaction coefficient $C_6$ are extracted from the pair correlation functions of the Rydberg atom positions.

The experimental setup is shown in Fig. 1(a). $^{85}$Rb ground-state atoms are prepared in a magneto-optical trap (MOT) at a density of $\gtrsim 10^{10}$ cm$^{-3}$. The two-photon Rydberg excitation to $70S_{1/2}$ is driven by simultaneous 780 nm and 480 nm laser pulses with a $5 \mu$s duration and $\approx 1$ GHz red-detuning from the $5P_{3/2}$ intermediate state. Both beams propagate in the $xy$ plane and are linearly polarized along $\hat{z}$. The 780 nm beam has a Gaussian beam parameter $w_0$ of 0.75 mm and the 480 nm beam is focused to $w_0 = 8 \mu$m. The Rydberg atoms are ionized by applying a high voltage to a tip imaging probe (TIP) with a rounded tip of diameter 125 $\mu$m. Ions are accelerated by the TIP electric field towards a microchannel plate (MCP). Ion impacts result in blips produced by the MCP-phosphor detector assembly, revealing the Rydberg atom positions. In each experimental cycle we record one image, taken by a CCD camera, that typically contains several blips. For more detail see reference [21].

The excitation volume is $\approx 170 \mu$m above the tip, which, in combination with the radial divergence of the TIP electric field and the MCP front voltage, results in a measured magnification of 155 with an uncertainty of 2%. We have calibrated the magnification by projecting a known double-slit interference pattern of 480 nm excitation light into the object plane and measuring the distribution of counts in the image (MCP) plane. The

![FIG. 1. Geometry (a) and timing sequence (b) of the experiment.](image-url)

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![FIG. 1. Geometry (a) and timing sequence (b) of the experiment.](image-url)
magnification uncertainty follows from the variation of the peak positions from an equidistant series (which one would expect for the double-slit). The resolution in the object plane is \( \approx 1 \mu m \); it follows from the magnification and the point spread function of the detector. We can easily resolve the correlation length between the Rydberg atoms, which is on the order of 10 \( \mu m \). The field of view typically contains 5 to 10 detected atoms. In the image processing sequence, we first extract ion impact positions on the MCP by using a peak detection algorithm [21]. Out of 10000 images taken in each dataset, we select the 5000 images with the highest numbers of detected ions. From this subset, we calculate the average pair correlation image and normalize it such that at large distances it approaches the value of one.

![FIG. 2. Pair correlation images from experiment (top row) and simulation (bottom row) for the selected wait times. The linear grayscale ranges from 0 (white) to 2 (black). Values of 1, <1, and >1 indicate no correlation, anticorrelation, and positive correlation, respectively.](image)

The excitation of the 70S1/2 Rydberg level is detuned by \( \delta \nu_L = 4 \pm 2 \) MHz with respect to the two-photon resonance. The positive excitation detuning is compensated by the (repulsive) van der Waals interaction. We preferentially excite Rydberg atoms in pairs at a separation at which the van der Waals interaction is 2\( \delta \nu_L = 8 \pm 4 \) MHz. We determine \( r_0 \) from pair-correlation images. After excitation, the Rydberg atoms are allowed to move within selected times before measuring their positions by applying a field ionization pulse [Fig. 1(b)]. The atom-position data are processed as explained above, yielding average pair correlation images. In Fig. 2, we present the pair correlation images for wait times 2.5 \( \mu s \), 10 \( \mu s \), 20 \( \mu s \), 30 \( \mu s \), and 40 \( \mu s \). The average interaction time of the Rydberg atoms is the wait time plus half the excitation pulse length (wait time + 2.5 \( \mu s \)). The pair correlation image at 2.5 \( \mu s \) exhibits strong correlation enhancement at a fairly well-defined radius. The initial correlation is critical for our trajectory experiment; it is sufficient to track Rydberg-pair trajectories out to approximately 40 \( \mu s \). With increasing wait time, the radius of enhanced pair correlation increases, reflecting an increase of interatomic separation due to the repulsive van der Waals interaction. At long wait times, the enhancement ring is blurred out due to initial thermal atom velocities in the MOT (temperature \( \sim 100 \) \( \mu K \)).

To determine the most probable separation \( r_p(t) \) between Rydberg-atom pairs at wait time \( t \), we first compute the angular integrals \( I(r) \) of the experimental pair correlation images in Fig. 2, as shown in Fig. 3(a). The values of \( r_p(t) \) are obtained from local parabolic fits centered approximately at the peak positions of the \( I(r) \) curves. We include 4 to 7 data points in the fit (depending on the shapes of the curves). The resulting separations \( r_p(t) \) are shown in Fig. 3(b).

![FIG. 3. (a) Angular integrals \( I(r) \) of the pair correlation images in Fig. 2 at wait times: 2.5 \( \mu s \) (red solid), 10 \( \mu s \) (orange dashed), 20 \( \mu s \) (green dotted), 30 \( \mu s \) (blue dot-dashed), and 40 \( \mu s \) (pink short-dashed). The \( y \) axis is for the red-solid curve; for clarity, the other curves are shifted down in equidistant intervals of 0.3. (b) Interatomic separations between Rydberg-atom pairs as a function of interaction time (left axis, blue circles), obtained from the peak positions in the \( I(r) \) curves. The blue dashed line represents a linear fit at long wait times (20-40 \( \mu s \)). The red solid line shows simulation results obtained for \( \delta \nu_L = 3 \) MHz. The pink hollow squares show the visibility of the experimental pair correlation enhancement (right axis) as defined in text.](image)

To extract the van der Waals \( C_6 \) coefficient, one may consider an isolated atom pair excited at an initial separation \( r_0 \). The initial van der Waals energy is

\[
W_0 = \frac{C_6}{r_0^6} = 2 \delta \nu_L. \quad (1)
\]

From Eq. 1, \( C_6 = 2 \delta \nu_L r_0^6 \) can, in principle, be obtained from spectroscopic measurement [14]. This method requires a well-defined \( r_0 \), a narrow laser linewidth, and accurate knowledge of \( \delta \nu_L \). In our work, the relative uncertainty in \( r_0^6 \) is about 12% (because the relative magnification uncertainty is 2%). In comparison, the uncertainty arising from \( \delta \nu_L = 4 \pm 2 \) MHz is much larger. Taking all uncertainties into account, Eq. 1 leads to values of \( C_6 \) ranging from \( 7 \times 10^{-38} \) Jm\(^6\) to \( 40 \times 10^{-38} \) Jm\(^6\). There-
fore, Eq. 1 only allows us to perform a crude order-of-magnitude estimate for $C_6$. The main weakness of Eq. 1 is that the $C_6$-values derived from it directly reflect our large relative uncertainty in $\delta v_L$.

A better way for us to obtain $C_6$ is to track the evolution of the Rydberg-atom trajectories. Over the experimentally investigated wait times, the entire initial van der Waals energy $W_0$ becomes converted into kinetic energy. With the reduced mass of the atom pair, $\mu$, and the terminal relative velocity, $v_t$, it is

$$W_0 = \frac{C_6}{r_0^6} = \frac{1}{2} \mu v_t^2, \quad (2)$$

To obtain $r_0$, we take the weighted average of the fit results $r_p(t)$ at the earliest times used in the experiment [the points in Fig. 3(b) at 250 ns and 2.5 $\mu$s]. The averaging is valid because during the first few microseconds after excitation the Rydberg atoms are frozen in place due to their inertia. The statistical weights are given by the inverse squares of the fitting uncertainties of $r_p$ at 250 ns and at 2.5 $\mu$s. We obtain $r_0 = 8.78$ $\mu$m with a net fitting uncertainty of 0.02 $\mu$m. To determine $v_t$, we perform a linear fit at long wait times (20-40 $\mu$s) and obtain $v_t = 0.182$ m/s with a fitting uncertainty of 0.008 m/s. It follows $C_6 = \frac{1}{2} \mu v_t^2 W_0 = (5.4 \pm 0.5) \times 10^{-58}$ J m$^6$. Including the 2% magnification uncertainty, the total uncertainty of $C_6$ becomes $1.0 \times 10^{-58}$ J m$^6$.

The final relative uncertainty of $C_6$ follows from three statistically independent contributions: the magnification uncertainty, the fit uncertainty for $v_t$, and the fit uncertainty for $r_0$. The respective powers at which these quantities enter into $C_6$ are 8, 2, and 6. Factoring in these powers, the three quantities contribute respective independent uncertainties of 16%, 8.7%, and 1.4% to the relative uncertainty of $C_6$, leading to the total relative uncertainty of 18%. In our method, achieving a small magnification uncertainty is particularly important.

A semi-classical 3D simulation of the dynamics of Rydberg atoms interacting by an isotropic van der Waals force has been performed to interpret the experiment. The simulation volume of $(140 \mu$m$)^3$ exceeds the experimentally relevant volume by about a factor of two in each dimension. The 480 nm excitation beam propagates along the $y$ direction. The excitation volume in the transverse directions ($x$ and $z$) is limited by the size of the excitation beam ($w_0 = 8 \mu$m). The number of simulations is 5000, in keeping with the number of images analyzed in the experiment. Rydberg-atom positions and velocities are then propagated using a Runge-Kutta integrator that includes all pair-wise interatomic forces. We use $C_6 = 5.7 \times 10^{-58}$ J m$^6$ [23] in the initialization and integration procedures. To avoid edge effects, we crop the $xy$ processing area in the images to $(70 \mu$m$)^2$ before calculating the average pair-correlation images and the radial functions $I(r)$.

In each simulation, we start by drawing the number of Rydberg atoms to be used, $n_{\text{Ryd}}$, from a Poissonian distribution. Initial trial positions of the Rydberg atoms are then drawn from a probability distribution that is Gaussian along $x$ and $z$, with a $w_0$ of 8 $\mu$m, and uniform along $y$ (in close analogy with the experiment). For an atom $i$ at a trial position $r_i$, the effective detuning $\delta_{\text{eff}}(r_i)$ due to all other atoms $j$ at positions $r_j$ which are already excited into the Rydberg state is

$$\delta_{\text{eff}}(r_i) = \sum_j \frac{C_6}{|r_i - r_j|^6} - \delta. \quad (3)$$

Since the detuning $\delta v_L$ is substantial, the first pair of Rydberg atoms is simultaneously excited via off-resonant excitation [21] (because the intermediate state in which there is only one Rydberg atom present is off-resonant). Therefore the value of $\delta$ in Eq. 3 for the first Rydberg-atom pair is set to be twice the laser detuning $\delta v_L$. For the excitation of additional atoms we use $\delta = \delta v_L$ to simulate the stepwise addition of those atoms, which can be a near-resonant process with other atoms already present [8]. Detunings due to the Doppler effect are about 300 kHz and are neglected. The excitation probability $P_{\text{ex}}(\delta_{\text{eff}})$ is a Gaussian centered at $\delta_{\text{eff}} = 0$ with a FWHM of 4 MHz (given by the excitation bandwidth) and $P_{\text{ex}}(\delta_{\text{eff}} = 0) = 1$. A new Rydberg atom at position $r_i$ is created if the excitation probability is larger than a number randomly drawn between 0 and 1. This procedure is repeated with new trial positions until the desired number of $n_{\text{Ryd}}$ Rydberg atoms has been reached. The initial center-of-mass velocities of the atoms are assigned using a Maxwell distribution at temperature 100 $\mu$K.

In the simulation, we record the atom positions at the same wait times as used in the experiment. The resulting pair correlation images are shown for the case $\delta v_L = 3$ MHz in the bottom row in Fig. 2. Black pixels along the left and right edges of each pair correlation are an artifact due to the normalization used in the image processing. From the simulated pair correlation images we calculate the $I(r)$ curves, as in the experiment, in order to obtain the most probable separations $r_p(t)$ between Rydberg-atom pairs at each interaction time [see solid curve in Fig. 3(b), which is for $\delta v_L = 3$ MHz]. The simulated and experimental results for $r_p(t)$ are in good agreement. In order to test how well our experimental procedure reproduces the $C_6$ coefficient that underlies the atomic interactions, we evaluate the simulated results for $r_p(t)$ using the same method that we also employ for the experimental data. The results for $r_0$, $v_t$ and $C_6$ extracted from the simulated $r_p(t)$ curves are shown in Table I for four choices of $\delta v_L$. These $C_6$ values agree, within the uncertainties, with the value that has been entered as a fixed input into the simulation. This finding validates the experimentally used procedure; in particular it is seen that the method is not very sensitive on $\delta v_L$.

The experimental, simulated, and expected values for $C_6$ in Table I are in reasonable agreement. Moreover, we observe that the entire simulated curve $r_p(t)$ for $\delta v_L =
TABLE I. Comparison of calculated, experimental, and simulated results for $C_6$, $r_0$, and $v_t$.

<table>
<thead>
<tr>
<th></th>
<th>$r_0$ (μm)</th>
<th>$v_t$ (m/s)</th>
<th>$C_6 \times 10^{-58}$ J m$^6$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calculation</td>
<td>5.7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Experiment</td>
<td>8.8 ± 0.2</td>
<td>0.18 ± 0.09</td>
<td>5.4 ± 1.0</td>
</tr>
<tr>
<td>Simulations</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\delta f_L = 2$ MHz</td>
<td>8.85 ± 0.06</td>
<td>0.17 ± 0.02</td>
<td>4.9 ± 1.0</td>
</tr>
<tr>
<td>$\delta f_L = 3$ MHz</td>
<td>8.14 ± 0.03</td>
<td>0.23 ± 0.005</td>
<td>5.5 ± 0.3</td>
</tr>
<tr>
<td>$\delta f_L = 4$ MHz</td>
<td>7.76 ± 0.05</td>
<td>0.278 ± 0.003</td>
<td>6.0 ± 0.3</td>
</tr>
<tr>
<td>$\delta f_L = 5$ MHz</td>
<td>7.51 ± 0.04</td>
<td>0.28 ± 0.01</td>
<td>4.9 ± 0.5</td>
</tr>
</tbody>
</table>

3 MHz matches the experimental result very well [see Figs. 2 and 3(b)]. Overall, our findings lend credibility to our method of measuring $C_6$.

We note that higher-order quadrupole-dipole and quadrupole-quadrupole interaction potentials, which scale as $r^{-7}$ and $r^{-8}$, are not important at the distances relevant in our work, at the current level of precision. We have verified this in a calculation of interaction potentials in which all terms up to the quadrupole-quadrupole interaction have been included [24].

A question of interest is whether the interatomic force is acting on “superatoms”, i.e., Rydberg excitations shared among a number of ground-state atoms, or on individual atoms. In our case, there are several tens of atoms within one blockade sphere. In our analysis, we have assumed that the effective mass of the interacting entities is half the rubidium atom mass, i.e., we have implied that the interacting entities are individual atoms and not superatoms. For our density and blockade radius, the total mass of a superatom equals that of several tens of atoms. The agreement between the $C_6$ coefficients in Table I demonstrates that the interacting entities are indeed individual atoms. The finding implies that, during the course of the van der Waals interaction, excitations within superatoms become projected onto individual atoms, which are then ejected from the initial superatom volumes. The phenomenon has been predicted in [25] for superatom clouds interacting via a dipole-dipole interaction. In our work, we arrive at a similar conclusion for van-der-Waals-interacting Rydberg atoms in a 3D system.

Close inspection of the pair correlation functions from the simulation presented in Fig. 2 reveals anisotropic expansion behavior: the radius of enhanced pair correlation is larger in $x$ than in $y$ direction. In several experimental data sets we see some evidence of anisotropic expansion, such as in the experimental result shown in Fig. 4(a). The anisotropic expansion is due to the cylindrical shape of the excitation volume (not the interatomic interaction, which is isotropic). Since the blockade radius is close to the transverse size of the excitation region, at most two atoms can be excited side-by-side in $x$ direction, leading to free, unimpeded expansion along that direction.

In contrast, more than two Rydberg atoms can be created along the $y$ direction. Therefore, along $y$ the expansion is slowed down due to multiple-atom repulsion. In our experiment, the overall Rydberg-atom density is high enough to sometimes observe this effect.

In summary, we have studied the trajectory of Rydberg-atom pairs interacting by repulsive, isotropic van der Waals interaction. We have extracted the $C_6$ coefficient from the experiment and compared it with simulations and calculations, and have observed good agreement. The result implies that the interaction occurs between individual atoms, not superatoms. We have observed indications of an anisotropic effect in the expansion, caused by the excitation geometry. Future work may involve atom-atom interactions that are anisotropic, such as the dipole-dipole interaction.

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*nithi@umich.edu
†Present address: zeroK NanoTech Corporation, Gaithersburg, MD 20878, USA
Measurement of van-der-Waals interaction by atom trajectory imaging

N. Thaicharoen, A. Schwarzkopf, and G. Raithel

Department of Physics, University of Michigan, Ann Arbor, MI 48109

Supplement

We have used the model presented in detail in [1] to calculate the interaction potential between a pair of 70S_{1/2} rubidium Rydberg atoms with dipole-dipole interaction terms only, as well as with dipole-dipole, dipole-quadrupole and quadrupole-quadrupole terms. The projection of the electron angular momenta onto the internuclear axis, M, can take the values 0 or +/-1. For M=0 there are two Rydberg-pair 70S_{1/2}-70S_{1/2} levels, labeled A and B, while for M=+/-1 there is only one (see table). QQ means all interactions up to and including quadrupole-quadrupole terms are included. DD means only dipole-dipole terms are included.

It is seen that all the atom pair has very similar shifts on all potentials, and that interaction terms beyond the dipole-dipole term are not important in the atom distance range of interest (R>7\mu m). The results also agree well with a perturbative level-shift calculation in [2].

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Spatial correlations between Rydberg atoms in an optical dipole trap

A. Schwarzkopf, D. A. Anderson, N. Thaicharoen, and G. Raithel
Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA
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We use direct spatial ion imaging of cold $^{85}$Rb Rydberg atom clouds to measure the Rydberg-Rydberg correlation function, with and without light-shift potentials generated by an optical dipole trap. We find that the blockade radius depends on laser detunings and spatially varying light shifts. At certain laser detunings the probability of exciting Rydberg atoms at particular separations is enhanced, which we interpret to be a result of direct two-photon excitation of Rydberg atom pairs. The results are in accordance with predictions [F. Robicheaux and J. V. Hernández, Phys. Rev. A 72, 063403 (2005)] and a model we develop that accounts for a one-dimensional dipole-trap potential.

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Rydberg-Rydberg interactions are essential in recently proposed [1,2] and demonstrated [3,4] neutral-atom quantum information processing schemes. They also play important roles in many-body Rydberg-atom physics [5–9] and specifically in proposals to produce Rydberg crystals [10–13]. Much recent work uses or assumes the presence of an optical trap for ground or Rydberg atoms. Indeed, in many quantum information schemes a trap is important to assist single-qubit addressability [14–16]. Nonetheless, to our knowledge the influence of the trap on the Rydberg blockade, a signature of the Rydberg-Rydberg interactions [17,18], has not been explicitly studied. In this work, we demonstrate that laser detunings and background optical potentials each have significant effects on the Rydberg blockade. We focus on the blockade-induced correlations between Rydberg atom positions.

We start with a magneto-optic trap (MOT) of $^{85}$Rb atoms (density $\gtrsim 10^{10}$ cm$^{-3}$) and, after switching off the MOT light, produce Rydberg atoms via a two-photon excitation from the $5\ell_2$ ground state by using 780- and 480-nm laser pulses. (The MOT magnetic field is always on.) The excitation is detuned from the intermediate $5P_{3/2}$ state by 1 GHz. We use crossed excitation beams, as shown in Fig. 1(a). The 780-nm beam has a Gaussian beam parameter of $w_0 = 0.75$ mm while the 480-nm beam is focused to $w_0 \approx 8 \mu$m. Beam powers are 2 and 36 mW, respectively. Each is linearly polarized along $\xi$, giving Rydberg atoms with $m_j = \pm 1/2$. In part of the work we excite the Rydberg atoms in an optical dipole trap (ODT) with 4 W of power and a focal spot of $w_0 = 23 \mu$m, crossed with the 480-nm beam focus. The ground-state atom density in the ODT is $\gtrsim 10^{11}$ cm$^{-3}$. We use Stark spectroscopy to reduce the electric field to $\lesssim 20$ V/cm. This is sufficient to avoid effects on the excitation blockade for the Rydberg states we excite [19].

We achieve spatially resolved detection of the Rydberg atoms by using a needle-shaped beryllium-copper field ionization electrode with a rounded tip of diameter 125 $\mu$m [Fig. 1(b)], referred to as the tip imaging probe (TIP) [18]. The photoexcitation region is $\approx 220 \mu$m above the TIP. The ions resulting from field ionization are accelerated along the radially divergent electric field lines produced by the TIP. The ions are detected $\approx 15$ cm away by a microchannel plate (MCP) spatially sensitive ion detector assembly. The magnification factor (the ratio between the ion separations in the MCP plane and the Rydberg-atom separations in the excitation plane) is $\approx 300$, providing submicron resolution (\approx 0.5 $\mu$m). This is comparable to existing [20,21] and proposed [22] diffraction-limited optical detection schemes and scanning electron microscope schemes [23].

To measure the Rydberg-Rydberg correlation function, we first acquire 10 000 CCD (charge-coupled device) images of the MCP phosphor screen, each image showing ion impact positions for a single experimental cycle of Rydberg excitation and ionization. We calculate the Rydberg pair correlation for each experimental cycle and then average these results. We use a peak detection algorithm to detect individual ion positions in each image; we then calculate the pair correlation from these discrete positions. Discrete peak detection is reliable because the minimum separation between Rydberg atoms (the blockade radius) is substantially larger than the imaging resolution.

We measure the Rydberg-Rydberg correlation function for excitation to states $59S_{1/2}$, $66S_{1/2}$, $74S_{1/2}$, $57D_{5/2}$, $64D_{5/2}$, and $72D_{3/2}$. Laser excitation pulse lengths are 5 $\mu$s for $S$ states and 1 $\mu$s for $D$ states, to account for differences in oscillator strength and to make count rates comparable. To eliminate

FIG. 1. (Color online) Experimental geometry: (a) A top view showing the crossed 780- and 480-nm excitation beams and the 1064-nm trap beam, with the $2w_0$ widths marked for the 480- and 1064-nm beams. The circle shows an estimate of the field of view of the microchannel plate (MCP) in the excitation plane (radius 25 $\mu$m). (b) A shadow image of the ODT above the tip imaging probe (TIP), and a sketch of the ion trajectories toward the MCP.
most images with fewer than two counts, we only use the
5 000 (of the 10 000 taken) that have the highest count numbers
for calculating the average pair correlation.

For each state, we adjust the 480-nm laser frequency to
excite at selected frequency points on the excitation spectra
without and with the ODT, as indicated by vertical lines
in Figs. 2(a) and 3(e), respectively. Resulting Rydberg pair
correlations are shown in Figs. 2(b), 2(c), and 3(a)–3(d).
Correlation values indicate the likelihood of finding Rydberg
atoms with a given projection of their separation vector into
the $xy$ plane. The linear grayscale is set such that white is
0 and black is 2. With the normalization used, a value of 1
indicates no correlation, i.e., the equivalent of random Rydberg
positions. Values $<1$ indicate anticorrelation and those $>1$
indicate positive correlation.

We first perform on-resonant excitation of state 66$S_{1/2}$
without ODT, with the result shown in Fig. 2(b). For Rydberg
separations $r < 8.5$ $\mu$m, correlation values are suppressed
due to the Rydberg excitation blockade. The single white pixel in
the center reflects the inability to resolve two Rydberg atoms
with a separation less than the imaging resolution. We next
detune the 480-nm laser frequency to the blue of resonance,
x exciting at the point where the count rate has dropped by
half [see Fig. 2(a)]. The resulting pair correlation is shown in
Fig. 2(c). The dark ring in Fig. 2(c) reflects a clear enhancement
of the probability of exciting two Rydberg atoms at a particular
separation distance, as predicted in Refs. [7,9]. One expects
this result for a detuning of the same sign as the van der Waals shift $V_{int}$ (positive for rubidium $S$ states, negative for
$D$ states [19,24]). The preferred separation is such that the
laser resonantly excites two ground-state atoms directly to
two Rydberg atoms, without populating an intermediate state
that carries a single Rydberg excitation. An energy level
diagram for this “two-photon” process is shown in Fig. 2(d).
(Experimentally, this is a four-photon transition because each
Rydberg transition involves both a 780- and 480-nm photon.)
For $S$ states we find that blue detunings yield these correlation
enhancements, while red detunings do not. For $D_{5/2}$ states we
observe the opposite behavior, since $V_{int} < 0$.

Our interpretation accords with the asymmetric broadening
of the excitation lines, such as the $S$ lines in Figs. 2(a) and 3(e)
dashed line). This indicates the presence of the two-photon
process shown in Fig. 2(d), with a positive $V_{int}/h$ of several
megahertz. $D_{5/2}$ lines (not shown) are broadened on the low-
frequency side, corresponding to a negative $V_{int}$.

In subsequent experiments, we excite Rydberg atoms in
the ODT at selected frequencies on the ODT spectrum, as
depicted in Fig. 3(e). Pair correlations for 59$S_{1/2}$ are shown
in Figs. 3(a)–3(d); Fig. 3(a) is for excitation without ODT,
shown for comparison with ODT results in Figs. 3(b)–3(d).
With increasing detuning, a ring of enhanced pair correlation
both grows in visibility and shrinks in radius. At 40-MHz
detuning a second ring emerges. We believe this is due to
exciting a string of three equally spaced Rydberg excitations,
with the middle excitation at the center of the ODT. The
second ring is seen especially well in the angular averages
$I(r)$ shown in Fig. 3(f). The error bars in Fig. 3(f) are obtained
by testing the variability of the results using subsets of the
data. The uncertainty increases significantly for datasets at
large laser detunings due to reduced count rates. A model for

FIG. 2. (a) Excitation spectrum without ODT for 66$S_{1/2}$. Note
the line asymmetry, with interaction-induced broadening for $\Delta > 0$.
The vertical lines show frequencies at which correlation functions
are measured. Panels (b) and (c): Pair correlations for excitation
of 66$S_{1/2}$ at the indicated detunings. (d) Level diagrams for off-
resonant excitation without ODT. The laser frequency is $f_0$ and
the frequency to excite one Rydberg atom without interactions is $f_0$.
Dotted lines indicate energy levels without interactions. Solid lines
are energy levels with interactions. The diagram is for the case of
blue detuning from $f_0$ ($\Delta > 0$). The “two-photon resonance” for the
direct excitation of two Rydberg atoms occurs when the interaction
energy $V_{int}/h = 2\Delta$.

FIG. 3. (Color online) (a) Correlation function for resonant excitation
of 59$S_{1/2}$ without ODT. Panels (b)–(d): Correlation functions
for excitation in the ODT, at the indicated detunings. (e) Spectra
for excitation of 59$S_{1/2}$ without ODT (black dashed curve) and with
ODT (red [gray] solid curve). Vertical lines indicate the excitation
frequencies used to acquire the correlation functions in panels (a)–(d).
The 0-MHz line is for excitation without ODT; for the other lines the
ODT is on. (f) Angular averages, $I(r)$, for the correlation functions
in panels (a)–(d). The curves correspond to correlation functions as
follows: black solid (a), red (gray) dashed (b), green (gray) dotted
(c), and purple (dark gray) dot-dash (d). The vertical scale is labeled
for the black solid curve; a vertical offset of 0.1 is applied between
subsequent curves to allow visual discrimination. For $r$ less than the
imaging resolution, each curve $I(r)$ drops to zero.
the excitation process, which explains the trends in Fig. 3, is presented below.

We measure the blockade radius \( r_b \) for each \( I(r) \) curve using the point closest to the origin where \( I(r) \) crosses its asymptotic value for large \( r \). This method is suggested by results of a stochastic, nonquantum simulation of the excitation-blockade process, which accounts for our geometry including the \( z \) projection during detection. The hard-sphere blockade radii entered as inputs, and the resulting asymptote crossings of the simulated \( I(r) \) curves, agree to within \( \pm 1 \) \( \mu \text{m} \).

In Fig. 4 we compare measurements and predictions of blockade radii for exciting on-resonance without ODT. One can estimate \( r_b \) by equating the Rydberg-Rydberg interaction strength with the laser excitation bandwidth \([18,19,25,26]\). Predictions in Fig. 4 are based on van der Waals interactions of the form \( V_{\text{int}} = C_6 / |R|^6 \), where \( R \) is the Rydberg-Rydberg separation vector. The coefficient \( C_6 \) is dependent on the interacting Rydberg states, \([n,\ell,j,m]_j\), as well as for \( D \) states the angle \( \theta \) between \( R \) and the quantization axis, \( \hat{z} \). Our calculations use interaction strengths from Ref. [19], where for \( D \) states we use \( C_6 \) for our experimental excitation conditions: \( \theta = \pi/2 \) and, for \( \hat{z} \) light polarizations, \( m_j = \pm 1/2 \). Power-broadening dominates the excitation bandwidths, which are therefore taken to be each state’s two-photon Rabi frequency (ranging from 500 kHz for \( 74S \) to 1.5 MHz for \( 57D \)). Agreement between these predictions and our measurements is quite good.

We further measure the blockade radius when exciting from the ODT. Results for \( 59S_{1/2} \) and \( 57D_{3/2} \) are shown in Fig. 5 as a function of \( \Delta \), the laser detuning from the trap-free transition. As the detuning \( \Delta \) increases, Rydberg atoms are excited deeper in the ODT. The data show an initial drop in \( r_b \) of several micrometers with the application of the ODT. With increasing \( \Delta \), \( r_b \) decreases for \( 59S_{1/2} \) and increases for \( 57D_{3/2} \). The trends of \( 59S_{1/2} \) and \( 57D_{3/2} \) also differ near the maximum light shift in the trap \( s_{\text{max}} \approx 30 \) MHz for our ODT parameters; see Fig. 5). For \( 59S_{1/2} \) we observe that Rydberg excitation is possible at detunings exceeding \( s_{\text{max}} \) by about 10 MHz [Figs. 3(e) and 5].

We model the system to predict the blockade radius, accounting for spatially dependent light shifts of the Rydberg transition. We consider the dimension with strongly varying light shifts \([x; \text{see Fig. 1(a)}]\). Our model uses ODT parameters as described for the experiment and has no free parameters.
excitation [see Fig. 6(c)]. The intermediate-state detuning, $\Delta = s_1$, is minimized by placing the first Rydberg atom at the center of the ODT. Energy conservation for the direct two-photon excitation of the Rydberg atom pair then requires

$$s_1 + s_2 + V_{\text{int}}/\hbar \pm \delta = 2\Delta.$$  \hspace{1cm} (3)

With $\Delta > s_{\text{max}}$ and $V_{\text{int}} > 0$, increasing $\Delta$ gives solutions for Eq. (3) with increasing $V_{\text{int}}$ (and thus diminishing $r_b$). Blockade radii predicted in this region agree well with data in Fig. 5. The described two-photon excitation process is similar to that seen earlier for excitation without ODT [Fig. 2(d)]. The two-photon excitation leads to the production of Rydberg atom pairs at well-defined separations, giving rise to ring structures in the pair correlations. We can estimate the relative importance of stepwise and two-photon excitation based on the visibility of these structures. Two-photon excitation gradually increases in importance as $\Delta$ approaches $s_{\text{max}}$, so the rings in Figs. 3(a)–3(d) smoothly shrink in radius and increase in visibility. The cusp in the solid curve in Fig. 5 is an artifact due to the model’s piecewise nature, assuming that two-photon excitation occurs only when the more efficient stepwise excitation is impossible.

For $D$ states ($V_{\text{int}} < 0$), the two-photon process described by Eq. (3) cannot occur for $\Delta > s_{\text{max}}$, as illustrated in Fig. 6(d). Thus the excitation spectra of $D$ lines in the ODT (not shown) do not extend beyond $\Delta = s_{\text{max}}$, which is why Fig. 5 does not show $D$ data for $\Delta > s_{\text{max}}$. However, we believe that two-photon processes are responsible for the low $r_b$ values measured in the range $5 \text{ MHz} < \Delta < 12 \text{ MHz}$. In this range, the laser is red-detuned from the Rydberg transitions of most atoms in the ODT (i.e., $\Delta < s$). Two-photon excitation is energetically allowed for pairs of such atoms, because a positive value of $s_1 + s_2 - 2\Delta$ can be balanced with a negative $V_{\text{int}}$. This situation can be described by a diagram similar to Fig. 6(d) but with $f < f_1, f_2$. The two-photon process causes the $r_b$ data to be smaller than predicted by the stepwise model.

With increasing $\Delta$ (range $12 \text{ MHz} < \Delta < s_{\text{max}}$) the number of atoms that are available to this process (i.e., atoms with $s > \Delta$) diminishes and the likelihood of direct two-photon excitation decreases. The data then approach the stepwise model (dashed line in Fig. 5). We note that excitation of a $D$-state atom at the center of the trap leads to a perfect blockade, as neither Eq. (2) nor Eq. (3) can be solved for $s_1 = 0$ and $V_{\text{int}} < 0$.

Our one-dimensional model in $x$ quantitatively explains our observations; we believe it captures the essential physics. In the experiment there is a perpendicular axis, $y$, along which there is no substantial light-shift gradient. Along this direction one might expect the trap-free blockade radius, but no clear anisotropy is observed in the experimental two-dimensional pair correlations.

In summary, we have measured the blockade radius for rubidium $S_{1/2}$ and $D_{3/2}$ Rydberg states and measured the effect of laser detunings and of light-shift potentials on the Rydberg pair correlation. We have observed a variation of the blockade radius as well as the appearance of additional structures in the pair-correlation functions, which we explain to be a result of direct two-photon excitation of Rydberg atom pairs at certain separations. Future studies may reveal the dynamics of these structures under the influence of decoherence and controlled shaping of the excitation pulses [10,29].

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Production and trapping of cold circular Rydberg atoms

D. A. Anderson,* A. Schwarzkopf, R. E. Sapiro, and G. Raithel
Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA
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Cold circular Rydberg atoms are produced and magnetically trapped. The trap is characterized by direct spatial imaging of ion distributions, ion counting, and state-selective field ionization. At room temperature, we observe about 70% of the trapped atoms remaining after 6 ms. We measure a trap oscillation frequency increase of the circular Rydberg atom trap relative to the ground-state atom trap due to the larger magnetic moment of the circular Rydberg atoms. Simulations of the center-of-mass and internal-state evolution of circular states in our magnetic trap are performed and results are in good agreement with experimental observations.

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Cylindrical Rydberg states [1] correspond to highly excited, Bohr-like electron trajectories with maximal orbital angular momenta. Circular-state (CS) atoms exhibit a unique combination of extraordinary properties: long lifetimes, large magnetic moments, and no first-order Stark shift. These features have made CS atoms attractive for cavity quantum electrodynamics (QED) precision measurements [4,5] benefit from the reduced nuclear and QED perturbations of these high-angular-momentum states. The large angular momenta also make CS atoms intriguing candidates for studies of interactions between Rydberg and ground-state atoms, such as the generation of Rydberg-ground molecules with GHz binding energies [6,7].

Several applications would benefit from trapping CS Rydberg atoms. While optical, electrostatic, and high-gradient magnetic trapping methods have been considered [8–10] and demonstrated [11–14] for atoms in other Rydberg states, cold, pure CS atoms have, to our knowledge, neither been prepared nor trapped. Additionally, magnetic Rydberg trapping has previously only been achieved for mixtures of Rydberg states, not for well-defined quantum states. In this Rapid Communication we describe the generation and trapping of cold, pure CS atoms in a conventional magnetic trap. We produce CS atoms at temperatures several orders of magnitude lower than in previous experiments (see, for example, [1,3,15,16]) and magnetically trap them. We employ the trapping force to measure their magnetic moments, which are the largest used in atom trapping to date. We characterize the trap using ion detection schemes that provide information on the center-of-mass (COM) oscillations in the trap, trap losses, and the atomic internal-state evolution.

We begin with a sample of $10^7 \ ^{87}$Rb atoms magnetically trapped in the $|F = 2, m_F = 2\rangle$ ground state at a temperature $\sim 100 \ \mu$K and density $\sim 10^{10} \ \text{cm}^{-3}$. The Ioffe-Pritchard-type magnetic trap is generated using a Z-shape wire [17]. The cigar-shaped trap has trap frequencies $(\omega_x, \omega_y, \omega_z) = 2\pi \times (7.9 \pm 0.3, 39.6 \pm 0.1, 37.4) \ \text{Hz}$, where $\omega_x$ and $\omega_y$ are measured and $\omega_z$ is calculated. The trap field minimum is measured to be $5.7 \pm 0.6 \ \text{G}$ and is located $3.5 \pm 0.2 \ \text{mm}$ from the surface of the Z wire. A schematic of the experiment and a plot of the magnetic field strength are shown in Fig. 1. The magnetic trapping region is enclosed by an electrode structure consisting of six individually addressable electrodes. Electric fields are controlled with an accuracy of $\leq 30 \ \text{mV/cm}$ in all coordinates using voltage-to-field calibration factors and field zeros obtained from Stark spectroscopy [18] on $85D$ Rydberg states. Electrode “T” is used for Rydberg-atom field ionization and electrode “B” produces an electric-field ramp required for the CS production. A microchannel plate (MCP) is located 10 cm from the excitation region, outside of the electrode package, and is used for ion detection (30% efficiency) and imaging.

We generate CS atoms with principal quantum number $n = 57$ by the crossed-fields method [19]. We first optically excite, in the presence of an electric field $E = -Ez$ from the B electrode (see Fig. 1), into the highest-lying state of the manifold of $n = 57$ states that exhibit the linear Stark effect (“hydrogenic states”). The excitation is done with counterpropagating 480 and 780 nm laser beams. The fixed-frequency 780 nm laser is 1 GHz off-resonance from the $5S_{1/2} \rightarrow 3P_{3/2}$ transition; the 480 nm laser is tunable to excite Rydberg levels. The combined excitation bandwidth is $\nu_L \approx 2 \ \text{MHz}$. The 480 nm beam is focused to a waist of $w_0 = 50 \ \mu$m and the 780 nm beam is collimated to $w_0 = 1.5 \ \text{mm}$, with powers of 35 and 2 mW, respectively. Both beams are linearly polarized perpendicular to the axis of the applied electric field. At a field of $\approx 1.8 \ \text{V/cm}$ the $60P$ states intersect with the $n = 57$ hydrogenic states. This field also mixes enough $S$ and $D$ character into the $P$ Rydberg states to enable two-photon excitation from the $5S_{1/2}$ ground state. Experimental and calculated two-photon excitation spectra are shown in Fig. 2. In the experimental spectrum the hydrogenic states appear only in regions where they intersect with $60P$ states. Due to the coupling between the states, the intersections are anticrossings with splittings of 20 MHz or more, as seen in Fig. 2(b). For our initial step in the CS production we excite to regions labeled I and II in Fig. 2(a).

After a 15 $\mu$s excitation pulse to region I, the electric field is ramped down over 40 $\mu$s from its initial value of 1.76 V/cm to 0 V/cm, within the residual electric-field uncertainty. This is slow enough to ensure adiabatic evolution of the Rydberg atoms within the anticrossings in Fig. 2. Regions labeled IV are not chosen because of state crossings at lower electric-field values that would cause state mixing during the electric-field ramp. The 5.7 G magnetic field at the bottom of the atom trap is always on and is perpendicular to the surface of the Z wire. A schematic of the experiment and a plot of the magnetic field strength are shown in Fig. 1. The
The hatched region indicates wire and the counterpropagating 480 and 780 nm beams for excitation location. An MCP is used for ion detection. The location of the Z trapped atom sample to control the electric fields at the excitation frequency. At the end of the ramp, the Larmor shift of one Bohr magneton, $\mu_B$, because in high-$\ell$ states the Zeeman effect dominates the fine structure. The magnetic field stabilizes the CS by lifting its degeneracy with any other hydrogenic state. The angular momentum of the trapped CS atom is parallel to the magnetic field at the trap minimum, which points along $\mathbf{x}'$ in Fig. 1. This CS is low-field seeking; the complementary $[n = 57, \ell = 56, m_t = -56, m_s = -0.5]$ CS is unsuitable for magnetic atom trapping because it is high-field seeking.

Due to their large magnetic moments, CS atoms in a magnetic trap experience significantly deeper confining potentials than ground-state atoms. The magnetically trapped $|F = 2, m_F = 2\rangle$ atoms (Landé factor $g_F = \frac{3}{2}$) have a magnetic moment of one Bohr magneton, $\mu_{GS} = -\mu_B$. The CS atoms described above have a magnetic moment $\mu_{CS} = -\mu_B(m_t + 0.3m_s) = -57\mu_B$, where $g_F \approx 2$. In a harmonic magnetic trap, the CS atom experiences a potential increase, $U_{CS} = (\ell_{CS}^2 \mu_{GS}^2)U_{GS} = 57U_{GS}$, and a corresponding trap frequency increase, $\omega_{CS} = \sqrt{57}\omega_{GS}$, where $U_{CS}$ and $U_{GS}$ are the CS and ground-state magnetic potentials, and $\omega_{CS}$ and $\omega_{GS}$ are the CS and ground-state trap frequencies, respectively.

The minimum of the ground-state trap is substantially shifted due to gravity, while in the much stronger CS trap gravity can be ignored. The displacement vector pointing from the minimum of the ground-state trap to the minimum of the CS trap is calculated to be $\delta r = (\delta x, \delta y, \delta z) = (710, 290, 0) \mu$m (using calculated force constants and the 12 ± 0.2 degree tilt of the trap with respect to gravity; see Fig. 1). This displacement allows us to initiate sloshing–mode oscillations of trapped CS atoms in the $\mathbf{x}'$ and $\mathbf{y}'$ directions.

To observe these oscillations we first generate the $|CS - 1\rangle = [n = 57, \ell = 56, m_t = 55, m_s = +0.5]$ near CS by initial excitation to region II in Fig. 2. We excite to II because it provides a stronger experimental signal than I; both regions result in high-$\ell$ states that exhibit quantitatively similar trapping behavior. The expected trap period for the near CS is $T_{CS-1} = \frac{2\pi}{\omega_{CS}}$, which equals 16.9 and 3.4 ms in $\mathbf{x}'$ and $\mathbf{y}'$, respectively. Since the excitation and circularization time interval of 55 $\mu$s is much smaller than $T_{CS-1}$, the atoms are prepared on the side of their trapping potential $U_{CS-1}$, at the location $-\delta r$. A field-ionization pulse is applied at varying time delays $t_d$ from the end of the $|CS - 1\rangle$ production. The ion positions are projected onto the MCP, where they generate spatially resolved light pulses on a phosphor screen, which is imaged by a CCD camera. The COM coordinates of the ion distributions in the MCP plane are obtained from sums of 2000 images at each $t_d$ [20]. Plots of the $\mathbf{x}$ and $\mathbf{y}$ COM coordinates as a function of $t_d$ are shown in Fig. 3. The $\mathbf{y}$ COM data [Fig. 3(a)] is fit to a sinusoid out to 4 ms from which we obtain an oscillation period of 3.4 ± 0.1 ms. This is in excellent agreement with the predicted value. The $\mathbf{y}$ COM data is only considered out to 4 ms because of distortions in the ion trajectories thereafter, as suggested by the $\mathbf{x}$ COM data. Since $\delta x \approx 2.5\delta y$, we expect a larger COM oscillation.
amplitude in \( x \). The \( x \) COM coordinate plotted in Fig. 3(b) develops a large displacement over about 4 ms. At \( t_d = 4 \) ms there is an apparent reversal in the direction of motion of the \( x \) COM coordinate, which occurs about a factor of 2 earlier than expected. We believe that the \( x \) COM oscillation amplitude is so large that it brings the ions produced by field ionization far enough off of the ion-imaging axis to cause distortion and obstruction [see Fig. 3(c) and discussion]. This prevents a direct measurement of the \( x \) COM oscillation period, as well as the \( y \) COM oscillation period after 4 ms.

To model the system, we perform Monte Carlo simulations of the internal-state evolution of a sample initially in the state |CS − 1⟩ in a \( T = 300 \) K radiation background; atom trajectories inside the magnetic trapping field are computed classically. The internal-state evolution and trajectories are coupled. The simulations account for all radiative transitions, including thermal photoionization, but no collisions. Typically, the rate of thermally induced transitions per atom is \( 6 \times 10^{3} \) s\(^{-1}\). (For comparison, in a \( T = 4 \) K cryogenic enclosure it would be \( 0.1 \times 10^{3} \) s\(^{-1}\).) The rapid state evolution from the |CS − 1⟩ due to the 300 K thermal radiation results in \( n, l, \) and \( m \) redistribution of the initially prepared sample, leading to a time dependence of the average magnetic dipole force as well as a diffusive component of that force. The change in average \( m \) amounts to less than 1% over the 10 ms observation time. The corresponding change in average oscillation frequency is too small to be seen in the experiment. The diffusive component of the \( m \) evolution is more significant, reaching an rms spread of \( \pm 15\% \) about the average \( m \) over 10 ms. This is large enough that we would expect some damping effect on the COM oscillations. From the simulations we obtain COM oscillation periods and decay constants of 16.5 and 36.2 ms in \( x' \) and 3.4 and 10.2 ms in \( y' \), respectively. In Fig. 3(a) we plot the simulated \( y' \) COM oscillation with a linear offset subtracted to match the experiment, accounting for ion-imaging abberations. We test the importance of thermally driven \( m \)-state diffusion by turning off all radiative transitions in the simulation, leaving anharmonicity-induced dephasing as the sole source of damping. We find that \( m \) diffusion and trap anharmonicity contribute in approximately equal parts to the decay of the COM oscillations over 10 ms.

To measure the magnetic trapping time we plot the number of detected Rydberg atoms as a function of \( t_d \). Figure 3(c) shows the fraction of Rydberg atoms detected relative to \( t_d = 0 \). We observe as much as 70% of the initially prepared sample remaining in the trap after 6 ms. If any \( 60P \) atoms remained after the circularization sequence, our simulations show that only a \( \sim 5 \times 10^{-3} \) fraction of them would survive after 6 ms. From this we conclude that our circularization procedure is very efficient. Between 7 and 13 ms we measure a rapid drop in signal, as well as a significant resurgence at about 16 ms. We believe that the rapid drop is due to atoms moving out of the ion-imaging field of view (in the \( x \) direction), while the resurgence occurs because of atoms moving back into view. This scenario is consistent with both the expected \( x \) oscillation period (16.5 ms) as well as the early reversal of the \( x \) COM in Fig. 3(b).

From Fig. 3(c) we estimate an overall loss rate of \( \gtrsim 50 \) s\(^{-1}\) for the trapped CS population. This loss rate cannot be explained at a quantitative level, as low-velocity CS atoms were not available until now and data on their collision cross sections are not available. However, the loss rate is consistent with collisions between Rydberg and ground-state atoms being the primary loss mechanism. This is determined from collisional cross sections between Rb low-\( \ell \) Rydberg and ground-state atoms provided in [21] and the estimated background Rb pressure. Losses from Rydberg-Rydberg collisions are not expected at the low Rydberg atom densities used (initially a few \( 10^{6} \) cm\(^{-3}\)). Our simulations of the state evolution show a loss rate of about 0.5 s\(^{-1}\) (at 300 K and accounting for all noncollisional loss channels), which is negligible in comparison to the measured loss rate.

Given the influence of the internal-state dynamics on the trapping behavior, we probe the internal-state evolution by performing state-selective field ionization (SSF) on the trapped Rydberg atom sample. A near-linear SSFI ramp is applied reaching a field of \( > 120 \) V/cm over the course of 50 \( \mu \)s. Different Rydberg states ionize at different points on the ramp, and can be distinguished by arrival time at the detector. Figure 4(a) shows SSFI traces for excitation to region III in Fig. 2, where only \( 60P_{1/2} \) atoms are excited. In this case, the electric-field ramp in the circularization procedure fails to populate any atoms in the CS; all atoms remain in \( 60P_{1/2} \). Figure 4(b) shows SSFI traces for excitation to region I in Fig. 2, where the CS generation procedure is expected to circularize most of the atoms. In both cases we obtain SSFI traces for \( t_d = 0 \) and 1 ms. We first compare the integrals of the SSFI curves. Excitation to region I produces a long-lived signal (0.59 remaining fraction), while excitation to III does not (0.09 remaining fraction), reaffirming the high yield of long-lived CS atoms.
Fig. 4. SSFI traces for an initial excitation into two different regions in Fig. 2: (a) into III, the 60P1/2 state and (b) into I, the first anticrossing at the 60P-manifold intersection to generate the CS after the circularization procedure. In both (a) and (b) the thin and thick traces correspond to the circularization procedure. In both (a) and (b) the thin and thick traces correspond to \( t_{\mu s} = 0 \) and 1 ms, respectively. Each trace is a sum of 20,000 experiments. The data are normalized such that for \( t_{\mu s} = 0 \) ms, the curves integrate to the same value. The dashed curve in (a) shows the field-ionization ramp used in both experiments.

Next we compare the structures of the SSFI curves. In both Figs. 4(a) and 4(b), with \( t_{\mu s} = 0 \), there are two distinct peaks: an early (22 \( \mu s \)) peak, which we attribute to adiabatic field-ionization events, and a later (29 \( \mu s \)) diabatic, high-field-ionizing peak [22]. In Fig. 4(b), the diabatic peak for \( t_{\mu s} = 1 \) ms arrives earlier than for \( t_{\mu s} = 0 \) ms, and is substantially broadened. This indicates a reduced average ionization field for the trapped sample at later times (corresponding to a higher average \( n \)) and rapid state diffusion, respectively. An additional peak emerges at an even earlier arrival time (18 \( \mu s \)). This peak is attributed to atoms accumulating in extremely high-\( n \) Rydberg states. The trends in Fig. 4 are in qualitative agreement with our simulations, which also show a thermally driven redistribution of population to longer-lived, very high-\( n \) states. For experimental reasons the field ionization is performed in crossed electric and magnetic fields; a detailed modeling of the SSFI curves in Fig. 4 is beyond the scope of this paper.

In summary, we have demonstrated a room-temperature magnetic trap for cold CS Rydberg atoms with \( n = 57 \). The trap oscillation period and trapping time have been measured and are in good agreement with predicted values and detailed simulations. The internal-state evolution of the atom sample was probed, showing the effect of the 300 K blackbody radiation background on the \( n \) distribution in the trap. Our trapping method could be employed in a 4 K cryogenic environment to suppress thermal transitions and provide a source of long-lived CS atoms for precision measurements [4,5]. Our work on cold, trapped CS Rydberg atoms paves the way for studies of exotic quantum states. For example, at sufficiently high ground-state atom density high-\( \ell \) Rydberg-ground molecules [6] may be produced in the generation of the CS. Due to their increased mass, these molecules would manifest as trailing signals in the COM oscillations of the CS in the magnetic trap. Another intriguing quantum object, which one could prepare in a setup similar to ours, would consist of a hollow electron wave function (that of the CS Rydberg atom) surrounding the ionic Rydberg-atom core and a Bose-Einstein condensate. This system would present an ideal platform to study interactions between ions and condensates [23–25].

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Imaging Spatial Correlations of Rydberg Excitations in Cold Atom Clouds

A. Schwarzkopf, R. E. Sapiro, and G. Raithel

FOCUS Center, Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA

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We use direct spatial imaging of cold $^{85}$Rb Rydberg atom clouds to measure the Rydberg-Rydberg correlation function. The results are in qualitative agreement with theoretical predictions [F. Robicheaux and J. V. Hernández, Phys. Rev. A 72, 063403 (2005)]. We determine the blockade radius for states $44D_{5/2}$, $60D_{5/2}$, and $70D_{5/2}$ and investigate the dependence of the correlation behavior on excitation conditions and detection delay. Experimental data hint at the existence of long-range order.

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When cold atoms are laser-excited to Rydberg states, the strong interactions between Rydberg excitations can lead to complex many-body entanglement in the system. The excitation process results in spatial correlations between excitations. In most cases, Rydberg excitation positions are anticorrelated such that no two excitations are within a "blockade radius" $r_b$ of each other. Such systems are well-suited for studying basic many-body physics [1–3], as well as for future technological applications such as quantum computation [4,5]. Theory for the laser excitation process that leads to the Rydberg blockade is considered in Refs. [6,7]. Previous experiments have shown the blockade effect to cause a suppression of excitation in an atom sample [8] and sub-Poissonian excitation-number statistics [9]. The underlying energy level shifts were measured spectroscopically [10].

We are presently interested in the spatial aspect of the blockade. In spatially resolved studies, the distance [11] and angle dependence [12] of Rydberg-Rydberg interactions were examined. The blockade effect was shown to be effective between spatially separated atom pairs in adjacent dipole traps [13,14]. In this Letter, we directly image a system containing multiple Rydberg excitations to obtain the Rydberg-Rydberg correlation function. We find evidence of the Rydberg excitation blockade and measure the blockade radius for several principal quantum numbers $n$.

The experimental setup is sketched in Fig. 1. The key feature enabling spatial resolution of the Rydberg sample is the ionization electrode: a beryllium-copper needle with a rounded tip of diameter $125 \mu m$. This tip imaging probe (TIP) is surrounded by a closed cage of electrodes whose voltages can be controlled to a precision of several millivolts. These electrodes allow independent control of the electric field in three orthogonal directions. To provide temporal and spatial electric-field stability, the apertures in the electrodes are covered with wire mesh, which has $0.51 \text{ mm}$ grid spacing and $88\%$ transparency.

The experiment runs at a repetition rate of $30 \text{ Hz}$. We collect $^{85}$Rb atoms for about $30 \text{ ms}$ in a magneto-optic trap (MOT) located $\sim 500 \mu m$ above the TIP. After turning off the MOT light, we optically pump the ground state atoms into the $5S_{1/2}[F = 3, m_F = 3]$ state, with the quantization axis along the beam direction. We then excite Rydberg atoms in a two-step process, using counterpropagating $480$ and $780 \text{ nm}$ beams. The excitation region is $\sim 360 \mu m$ above the TIP. The beams are $\sigma^+$ polarized and resonantly drive the transitions $5S_{1/2}[F = 3, m_F = 3] \rightarrow 5P_{3/2}[F' = 4, m_{F'} = 4] \rightarrow nD_{5/2}[F'' = 5, m_{F''} = 5]$.

The red beam has a Gaussian beam parameter of $w = 0.75 \text{ mm}$, while the blue beam is focused to $w_0 = 8 \mu m$ with a theoretical confocal parameter of $0.3 \text{ mm}$. Because of the much larger size of the red beam, the intermediate-state population is uniform across the width of the excitation region. We establish with CCD imaging that the intensity distribution of the blue focus is only weakly altered by diffraction from the mesh. Laser linewidths are on the order of $1 \text{ MHz}$. Typical Rydberg atom densities are $\sim 10^9 \text{ cm}^{-3}$, dependent on atomic state and laser power.

FIG. 1 (color online). (a) Overview of excitation region and ion detection. (b) Exploded view of electrodes that surround the excitation region, used for electric-field control. The purple, blue, and yellow electrodes allow electric-field control in the $z$, $y$, and $x$ directions, respectively. Green and red electrodes are grounded.
The system’s magnification factor is determined by the combined ion-lensing effects of the TIP, pulsed to about 400 V, and the MCP front plate, held at −800 V. To calibrate the magnification, we scan the focused 480 nm beam laterally across the MCP field of view by using a mirror with a piezo actuator on the horizontal axis. Using the known physical displacement of the beam, we determine the scale in the MCP picture. We find a linear magnification factor of $45 \times$ between the excitation region and the MCP front surface. 1 μm in the excitation region corresponds to 2.2 pixels in the digital CCD images, with an uncertainty of 10%.

The procedure of data acquisition and processing begins with taking 10,000 CCD images of the MCP phosphor screen, each image showing the ion impact positions for a single experimental cycle [as in Fig. 2(a)]. A CCD image consists of these blips plus background noise from the primary source. To eliminate the background, we determine the maximum background level and subtract it from the image, setting all negatives to zero. This procedure yields raw images, denoted by $A(i,j)$. The raw autocorrelation $A(i,j)$ is useful for qualitative analysis, as it is the easiest to interpret by eye. However, for quantitative analysis we must eliminate the shape of the beam. To do so we first sum the images [Fig. 2(b)] and take the autocorrelation of the sum of images, denoted by $A(i,j)$.

$$f(i,j,N,M) = \frac{NM}{(N-i)(M-j)},$$

where $N \times M$ is the image size, and $(i,j)$ is the displacement. The normalization factor $f$ eliminates finite-array effects in Eqs. (2) and (4), as it causes flat images to have flat autocorrelation functions rather than pyramidal ones.

The signal $A$ has three main structures: a central peak due to the correlation of a blip with itself, an overall cigar shape due to the geometry of the excitation region, and structure due to correlations between ion positions. It is this third structure that we wish to isolate in our analysis. The raw autocorrelation $A$ is useful for qualitative analysis, as it is the easiest to interpret by eye. However, for quantitative analysis we must eliminate the shape of the beam. To do so we first sum the images [Fig. 2(b)] and take the autocorrelation [Fig. 2(c)]:

$$B(i,j,N,M) = \sum_{n,m} \left( \sum_{\alpha} X_{n,m}^{\alpha} \right) \left( \sum_{\beta} X_{n-i,m-j}^{\beta} \right).$$

The autocorrelation $B$ does not contain any information about Rydberg-Rydberg correlations but still shows the overall shape of the excitation region. This allows us to divide out the beam shape by defining a normalized $A$:

$$\tilde{A}(i,j) = \sum_{\alpha} A_{i,j}^{\alpha},$$

where

$$f(i,j,N,M) = \frac{NM}{(N-i)(M-j)},$$

$N \times M$ is the image size, and $(i,j)$ is the displacement. The normalization factor $f$ eliminates finite-array effects in Eqs. (2) and (4), as it causes flat images to have flat autocorrelation functions rather than pyramidal ones.

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The autocorrelation $B$ does not contain any information about Rydberg-Rydberg correlations but still shows the overall shape of the excitation region. This allows us to divide out the beam shape by defining a normalized $A$:

$$\tilde{A}(i,j) = \sum_{\alpha} A_{i,j}^{\alpha},$$
\[ \vec{A}_{i,j}^1 = \vec{A}_{i,j} / N_p B_{i,j}, \]

where \( N_p \) is the number of pictures in the data set. The normalization of \( \vec{A}^1 \) is such that a value \( >1 \)\ (<1) should indicate a correlation (anticorrelation) of ion positions.

We take data at several combinations of red and blue laser powers. For the intensity of the lower transition beam we use intensities of 1.7I_{sat} and 3.4I_{sat}, where the saturation intensity \( I_{sat} = 1.6 \) mW/cm\(^2\). For each of these intensities we measure the atom number as a function of the intensity of the upper transition beam and observe saturation behavior as in Ref. [8]. To acquire images for the autocorrelation analysis described above, we select several intensities of the upper transition beam and observe saturation behavior.

Between 5 and \( 10 \) \( \mu \)m, each curve has a dip indicating an anticorrelation in Rydberg atom positions. Such dips are present in most of our data, with the degree of visibility depending on excitation parameters. The absence of dips in some data indicates that they are not artifacts of the imaging or image processing. We find that laser frequency fluctuations can make the dips change in depth and diameter. Furthermore, laser power affects the results, as described below.

To quantitatively compare the autocorrelations \( \vec{A}^1 \) of different states, in Fig. 4 we plot \( I(r) \), defined as the angular average of \( \vec{A}^1 \). \( I(r) \) is analogous to the radial autocorrelation function calculated in Ref. [6]. The self-term fills the region \( r < 5 \) \( \mu \)m. We do not remove the self-term due to the risk of producing a false blockade signal. Between 5 and \( 10 \) \( \mu \)m, each curve has a dip indicating an anticorrelation in Rydberg atom positions, as was qualitatively observed in Fig. 3. The minima of \( I(r) \) do not approach zero in part because we are projecting a three-dimensional sample onto the detector plane, which reduces the visibility for even a perfect blockade.

Figure 4 shows that the blockade radius increases with principal quantum number \( n \). However, there is no obvious choice for a method to measure a blockade radius from each curve, as the curve’s shape is determined by both the blockade-induced dip and the self-term. To determine a good measure for the blockade radius, we simulate the excitation-blockade process for our geometry and \( z \)-projection conditions, by using a stochastic, nonquantum model. We find that the inflection point after the minimum of each \( I(r) \) curve is close to the input hard-sphere blockade radius. We thus use this inflection point as our measure of the blockade radius. We note that in the simulations the self-term diminishes the dip depth and can shift the dip position. If the input blockade radius is close to the self-term width, the radius indicated by the inflection point is 1–2 \( \mu \)m higher than the blockade radius. When the blockade radius is much larger than the self-term width, the inflection point method underestimates the input blockade radius by \( \approx 1 \) \( \mu \)m.

For the states \( 44D_{5/2} \), \( 60D_{5/2} \), and \( 70D_{5/2} \) we measured the radii on nine, six, and nine curves. One additional curve was discarded for \( 70D_{5/2} \) although its dip minimum was consistent with other data, the position of its inflection point was unclear. Five additional curves for \( 44D_{5/2} \) were thrown out because there was no dip, as discussed below. The measured blockade radii are shown in Fig. 5. The error bars indicate the 10% uncertainty from the magnification calibration; this systematic uncertainty dominates the uncertainty due to measurement statistics by a factor of at least 2.

In Fig. 5, we compare the measurements to predictions based on an excitation bandwidth \( \delta \nu_L \) ranging from 5 to 12 MHz and interaction strengths as determined from Ref. [15]. The blockade radius for the van der Waals interaction has been calculated to be

\[ r_p = \left[ \frac{\Delta \bar{W}^{(2)}(n^*)}{\hbar (\delta \nu_L)} \right]^{1/6}, \]

where \( n^* = n - \delta_l \) is the effective principal quantum number, \( \delta_l \) is the quantum defect, and \( \Delta \bar{W}^{(2)} \) is a scaled, second-order, state-dependent van der Waals coefficient.
defined in Ref. [15], $\Delta W^{(2)}$ is scaled such that it would be independent of $n^*$ in the absence of resonant level shifts. The assumed value for $\delta \nu_L$ has little effect due to the sixth-root dependence.

Figure 5 shows that the measured blockade radii are within a factor of 2 of the predictions. Further, the amount by which the blockade radius increases between the probed $n$ levels is as expected. The measured blockade radii exceed the calculated radii by 2–3 $\mu$m. The difference may be because Eq. (6) models the interaction between two atoms and excludes many-body effects [3]. Ates et al. have previously seen evidence that theory based on pairwise interactions underestimates the blockade radius [7].

To test if atomic motion or the degree of excitation saturation modifies the observed correlation behavior, we vary laser powers, excitation pulse duration, and field extraction delays. In general, increasing the laser power, or the excitation duration at constant power, diminishes the dip depth (defined as the curve asymptote minus the dip minimum). For instance, increasing the excitation duration for state $70D_{5/2}$ from 100 to 400 ns causes the dip depth to decrease from 0.24 to 0.04. This behavior could be caused by an increased $z$ depth of the saturated part of the excitation region. In our simulations the degree to which the dip depth is diminished depends on the assumed beam focus quality. Adding wings to a Gaussian focus, as suggested by Fig. 2(c), yields better qualitative agreement with our data.

Laser power has a greater effect for the case of excitation to $44D_{5/2}$ than for the other states: In five $I(r)$ curves the dip disappeared entirely. We expect that this is partly due to saturating the atomic transition for $44D_{5/2}$ more strongly than for $60D_{5/2}$ or $70D_{5/2}$. It is also possible that, of the three states we studied, $44D_{5/2}$ is the most susceptible to laser parameters due to having the shallowest dip, closest to the radius of the self-term. Another possibility is that the blockade efficiency is diminished due to the proximity of the Förster resonance, as suggested by Refs. [3,16].

By varying the delay between excitation and field ionization, we test the longevity of the correlations. They are remarkably long-lived. The dip depth decreases by about half over 10 $\mu$s, despite possible atomic motion and ionization during this time [17,18]. This result awaits a future theoretical explanation.

Some of our data, using linear laser polarization and a few megahertz of detuning, show additional structures. The autocorrelation in Fig. 6(a) exhibits multiple rings, indicating long-range Rydberg-Rydberg correlations. The autocorrelation in Fig. 6(b) hints at multiple maxima in a ring about the center, indicating possible angular dependence of the Rydberg-Rydberg correlation function. There have been predictions of crystal-like structure in Rydberg systems [19], but the detailed excitation conditions are important in generating these structures. At present we are working to improve our experimental control in order to systematically study these effects.

In summary, we have obtained spatially resolved images of blockaded Rydberg atom samples and evaluated the Rydberg-Rydberg correlation function. Having observed a blockade, we measured the blockade radius for several quantum states. We have also tested the dependence of the blockade on parameters such as laser power, excitation duration, and detection delay. Future work could include investigation of long-range correlation structures, extending beyond one blockade radius, as in Fig. 6. One could further attempt to excite a Rydberg crystal as proposed in Ref. [19].

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FIG. 5 (color online). Comparison of blockade radius measurements (+) with predictions (×) based on Ref. [15].

FIG. 6. Some autocorrelations ($\bar{A}$) showing possible long-range and angular structure for state $44D_{5/2}$. 

103001-4
Angular-momentum couplings in long-range $^{87}$Rb$_2$ Rydberg molecules

D. A. Anderson, S. A. Miller, and G. Raithel

Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA

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We study angular-momentum couplings in $^{87}$Rb$_2$ Rydberg molecules formed between a Rydberg and $5S_{1/2}$ ground-state atom. We use a Fermi model that includes $S$-wave and $P$-wave singlet and triplet scattering of the Rydberg electron with the $5S_{1/2}$ atom, along with the fine-structure coupling of the Rydberg atom and hyperfine-structure coupling of the $5S_{1/2}$ atom. We discuss the effects of these couplings on the adiabatic molecular potentials. We obtain bound-state energies, lifetimes, and electric and magnetic dipole moments for the vibrational ground states of the $^{87}$Rb($nD + 5S_{1/2}$) molecules in all adiabatic potentials, with fine and hyperfine structure included. The hyperfine structure gives rise to mixed singlet-triplet potentials. We also study the effect of the hyperfine structure on the deep $^3S$-wave- and $^3P$-wave-dominated adiabatic molecular potentials, which support high-$\ell$ $^{87}$Rb$_2$ Rydberg molecules.

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I. INTRODUCTION

Rydberg molecules formed by the low-energy scattering of a Rydberg electron and a ground-state atom constitute a distinct class of molecular states that have in recent years become the subject of significant theoretical and experimental interest. Developments include studies of diatomic Rydberg molecules in low-angular-momentum Rydberg $S$ states [1, 2], $P$ states [3], and $D$ states [4, 5], the realization of coherent bonding and dissociation of $S$-type molecules [6], and the first observation of a permanent electric dipole moment in a homonuclear molecule [7]. Polyatomic Rydberg molecules have also been generated [8] and employed in a demonstration of the continuous transition between a few-body to many-body regime in an ultracold quantum gas [9].

The theoretical framework for these molecules is generally well established. The interaction between a low-energy Rydberg electron and ground-state atom can be described using a Fermi pseudopotential approach [10–12]. In the Fermi model, the ground-state atom is treated as a $\delta$-function perturber of the Rydberg-electron wave function, resulting in oscillatory potential curves with localized minima capable of sustaining bound molecular states. In alkali systems, the potential curves are strongly affected by low-energy $^3S$-wave and $^3P$-wave electron-atom scattering resonances [13–15]. The influence of these scattering resonances on the potentials has been studied in Rb$_2$. The $^3S$ interaction leads to so-called trilobite molecules [12], which are very long range (their size is on the order of $n^2$, where $n$ is the principal quantum number of the Rydberg level). The $^3P$ interaction produces potentials [16] that are about an order of magnitude deeper and about a factor of five shorter range than the trilobite potentials. The molecular potentials, wave functions, and electric dipole moments for both Rb$_2$ and Cs$_2$ have also been calculated using a Green’s function approach, accounting for the finite size of the perturbing ground-state atom via an effective short-range electron-atom interaction potential [17, 18].

In addition to the electron-atom scattering interaction, the molecular potentials and properties of long-range Rydberg molecules are dependent on the Rydberg-atom wave function as well as the angular-momentum couplings of the Rydberg- and ground-state constituents. Rydberg molecules exhibit a broad range of different angular momentum coupling schemes. For low-$\ell$ Rydberg molecules ($\ell \lesssim 2$ in rubidium), the angular-momentum coupling configurations span three Hund’s cases [(a)–(c)], dictated by the relative strength of the Rydberg atom’s fine-structure coupling compared to that of the $e^- + 5S_{1/2}$ scattering interaction. The Rb($nD + 5S_{1/2}$) molecules are unique among the low-$\ell$ molecules because their Rydberg fine-structure couplings are comparable to the scattering interaction strength, and they fall anywhere between two Hund’s cases (a) and (c) by a mere change in principal quantum number $n$. For high-$\ell$ Rydberg molecules, the molecular binding interaction is stronger than the fine-structure coupling, and is comparable to the hyperfine coupling of the ground-state perturber. Inclusion of the $5S_{1/2}$ hyperfine coupling in the model generates additional adiabatic potentials of mixed triplet and singlet character. For both high- and low-$\ell$ molecules, the hyperfine structure results in additional adiabatic potentials deep enough to sustain bound states.

In this work we present a study on the influence of angular-momentum couplings on the properties of long-range Rydberg molecules. We first describe a Fermi model for Rydberg molecules with the relevant angular-momentum couplings included. In our analysis we include singlet and triplet $S$- and $P$-wave scattering. By selectively enabling the different interactions in the model, the effects of each of these individual interactions on the adiabatic molecular potentials are revealed. Typical vibrational-state wave functions, binding energies, lifetimes, and dipole moments are discussed with an emphasis on the role of angular-momentum couplings. We conclude with describing hyperfine effects on the relatively deeply bound trilobite Rydberg molecules [12].

II. FERMI MODEL

We describe diatomic Rydberg molecules with a Fermi model [10, 11] taking into account the angular-momentum couplings in the Rydberg atom and perturbing ground-state atom system whose strengths are comparable to the Rydberg $e^- + $ perturber interaction. A schematic of the relevant couplings is shown in Fig. 1(a). The perturbing $^8$Rb $5S_{1/2}$ atom is located at a position $Z$ from the ionic core of the Rydberg atom,
Energy-dependent scattering phase shift. For the calculations in the present work we use nonrelativistic scattering phase shifts \( \delta_{\ell=0} \) and \( \delta_{\ell=1} \) provided by I. I. Fabrikant based on Ref. [17].

The electron momentum is given by \( k = \sqrt{-1/n_0^2 + 2/r} \) (atomic units) in the classically allowed range of the Rydberg electron and \( k = 0 \) elsewhere. Here, \( n_0^2 \) is the effective Rydberg quantum number of the level of interest. To account for configuration interactions, we employ basis sets \( |n, l_1, j_1, m_{l_1}, m_{j_1} \rangle \) that include all Rydberg levels with effective quantum numbers \( |n^* - n_0^2| \lesssim 2.5 \). For the Rydberg atom, all \( l_1, j_1, \) and \( m_{j_1} \) are included (as in Ref. [24]), and for the perturber atom all \( m_{j_2} \) and \( m_{l_2} \) are included. The singlet (S) and triplet (T) channels of the \( e^- + 5S_{1/2} \) scattering interaction include projectors \( \hat{I}_{S,T} \), defined as \( \hat{I}_S = \hat{S}_z + \frac{1}{2} \), which has an eigenvalue of one (zero) for the triplet (singlet) states, and \( \hat{I}_T = \hat{T}_z \). The operators \( \hat{S}_z \) and \( \hat{T}_z \) are the spins of the Rydberg electron and \( 5S_{1/2} \) atom, respectively, and \( \hat{I} \) is the identity operator. The last term in Eq. (1) accounts for the hyperfine interaction of the perturber. The \( 87Rb 5S_{1/2} \) perturber atom has nuclear spin \( I_2 \) with \( I_2 = 3/2 \), and hyperfine levels \( F_z = 1 \) and \( F_z = 2 \), with a hyperfine coupling parameter \( A = h \times 6.8 \text{GHz} / F_z = h \times 3.4 \text{GHz} \) (in SI units).

Only levels with \( m_{l_1} = 0, \pm 1 \) components have nonvanishing wave functions or wave function gradients on the internuclear axis. The S-wave interactions couple Rydberg states with \( m_{l_1} = 0 \) components. The P-wave interactions couple states with \( m_{l_1} = 0 \) components through the radial derivative of the Rydberg wave function, and states with \( m_{l_1} = \pm 1 \) components through the polar-angle derivative of the wave function. The electron scattering term in Eq. (1) conserves \( m_{l_1} + m_{l_2} \), while the hyperfine term conserves \( m_{l_2} + m_{l_2} \). The full Hamiltonian conserves \( m_2 := m_{l_1} + m_{l_2} + m_{l_2} \). Hence, the Hilbert space can be broken up into subspaces of fixed quantum numbers \( m_2 \). As an example, the subspace for \( m_2 = +1/2 \) and its couplings via the S-wave, P-wave, and hyperfine interactions is shown in Fig. 1(b). The gray bars in Fig. 1(b) illustrate that the couplings are organized in an interlaced block-diagonal structure in the magnetic quantum numbers. Since the couplings via the scattering terms require \( |m_{l_1}| \leq 3/2 \), the \( 87Rb_2 \) Rydberg molecules have \( |m_k| \leq 7/2 \).

### III. ADIABATIC POTENTIALS

Adiabatic molecular potentials \( V_i(Z) \) (i is an arbitrary label) are obtained by diagonalizing the Hamiltonian in Eq. (1) for a grid of perturber atom positions, \( Z \hat{z} \), through the extent of the Rydberg wave function. To highlight the effects of the different terms in Eq. (1) on \( V_i(Z) \), in Figs. 2 and 3 we show adiabatic potentials calculated for D-type Rydberg molecules with the different interaction terms in Eq. (1) selectively turned on.

First, we consider adiabatic potentials without hyperfine coupling. Figure 2(a) shows adiabatic potentials for the \( 31D + 5S_{1/2} \) molecule with only the S interaction turned on and no fine-structure coupling. This results in three degenerate oscillatory potentials, one corresponding to each triplet state, and a flat potential corresponding to the singlet state (which has no S interaction). The triplet potential curves are similar to those calculated in Ref. [12], in which the S-wave scattering length \( -\tan \delta / k \) is taken to first order in...
the electron momentum \cite{11}. With an appropriate choice of the zero-energy \( S \)-wave scattering length, the \( 3S \) interaction reproduces measured binding energies of vibrational ground states of \( S \)-type Rydberg molecules \cite{1}. Similarly, the \( 3S \) interaction with the addition of the fine structure reinforces vibrational ground states of \( D \)-type Rydberg molecules \cite{4}. The effect of the fine-structure coupling on the molecules is discussed further below.

IV. QUASIBOUND MOLECULAR STATES AND LIFETIMES

Due to the lack of an inner potential barrier, the molecular vibrational states have the character of metastable scattering resonances in potentials that are unbound on the inside. Figure 4 shows the (deep) adiabatic potential for the \( ^{87}\text{Rb}(31D_{1/2} + 5S_{1/2}, F = 2) \) molecule and its quasibound states. These are qualitatively similar to those of \( S \)-type molecules \cite{8}. The molecular wave functions consist of low-amplitude standing waves formed by outgoing and reflected ingoing waves in the region \( Z \lesssim 1000a_0 \), and a high-amplitude, resonantly enhanced portion in the outer adiabatic-potential wells at \( Z \sim 1500a_0 \). The latter are identified with quasi-bound molecular vibrational states that are metastable against tunneling-induced decay (decay into the region \( Z \lesssim 1000a_0 \)).

The resonances are found by computing the wave function phase at a fixed location in the unbound region (we use \( Z = 300a_0 \) as a function of energy \( W \)). The phase and its derivative are plotted as a function of energy in the right and middle panels of Fig. 4, respectively. The quasibound molecular states occur at energies at which the phase undergoes sudden changes of \( \Delta \Phi = \pi \), and are centered at energies where the derivative of the phase is maximal (circles in the middle panel of Fig. 4).
The resonances obey a single-level Breit-Wigner formula with frequency linewidths of the quasibound molecular states given by $\Gamma = 2/(\hbar \times d\Phi/dW)$ [25], corresponding to lifetimes of $\tau = (\hbar/2)d\Phi/dW$. The lifetimes scale as the Wigner tunneling time delay [26]. Resonances with larger slopes $d\Phi/dW$ in Fig. 4 correspond to longer-lived quasibound states. In addition to the sharp resonances there are broad resonances, as indicated by hatched regions in the middle panel of Fig. 4. While the broad resonances are not likely to cause observable effects in molecular spectra, they add to the total phase change over an energy range. For instance, within the energy range displayed in Fig. 4 the broad resonances account for a phase change of $3\pi$, and the quasibound molecular states for a change of $11\pi$, corresponding to a total change of $14\pi$. The distinction between broad and narrow resonances may, in practice, depend on experimental parameters such as excitation bandwidth and atom temperature (which affects Frank-Condon factors).

In Table I we give the binding energies, linewidths, decay times, and average internuclear separation of the scattering resonances shown in Fig. 4. Each quasibound state is assigned a vibrational quantum number $v$, sequentially increasing from 0 for the most strongly bound state in the outermost well to 10 for the most weakly bound state. Generally, one expects bound states furthest from the dissociation threshold to have the longest lifetimes. Here, the ground and first excited states of the outermost potential well (labeled $v = 0$ and 2, respectively) are well confined and have lifetimes in the range of hours and seconds, respectively. These lifetimes only reflect tunneling-induced decay. The actual lifetimes of these molecular states are, in fact, much shorter due to additional decay mechanisms, such as radiative decay of the Rydberg state and collisions with ground-state atoms [27]. An early dissociation process via the energy exchange between the Rydberg electron and ground-state atom has also been used to explain shorter molecular lifetimes observed in experiments [28]. Nevertheless, the relatively long lifetimes and large Frank-Condon factors associated with these outermost states make them the easiest to isolate experimentally [1,4,9]. There are also several resonances in the inner potential wells ($v = 1$ and 3) with lifetimes on the order of that of the Rydberg atom (which for $^{87}$Rb $31D_{1/2}$ is about 20 $\mu$s in a 300 K black-body radiation field). The resonances at higher energies ($v = 4 - 6$) exhibit shorter lifetimes because of the smaller potential barrier through which they more readily tunnel inward. Surprisingly, above these short-lived resonances additional resonances with longer lifetimes appear ($v = 7 - 10$). Here, the inner oscillatory wells act like an aperiodic Bragg reflector of the molecular wave functions, resulting in unexpectedly long-lived resonances near the dissociation threshold. The lifetime of these states is largest when a Bragg reflection condition is met. This occurs in a range of Rydberg principal quantum numbers $n$ at which the periodicity of the vibrational wave function approximately equals that of the Rydberg-electron wave function. This Bragg-reflection has previously been described as an internal quantum reflection process in $S$-type molecules [8].

V. HUND’S CASES FOR nD RYDBERG MOLECULES

Hund’s coupling cases are widely used for classification of angular momentum couplings in diatomic molecules [29]. Low-$\ell$ diatomic Rydberg molecules ($\ell \lesssim 2$ in rubidium) exhibit a variety of coupling cases, determined by the relative strength of the Rydberg atom’s fine-structure coupling to the $e^-p$ perturber scattering interaction. For $^{87}$Rb($nD_{1,2} + 5S_{1/2}$) molecules the fine-structure coupling is comparable to the scattering interaction strength. Due to this, $D$-type molecules trend from Hund’s case (c) at large $n$, where the fine-structure coupling exceeds the scattering interaction strength, to Hund’s case (a) for $n \lesssim 35$, where the scattering interaction strength exceeds the fine-structure coupling. In previous work, we observed $^{87}$Rb($nD_{1} + 5S_{1/2}, F = 2$)($v = 0$) molecules in transition between the two Hund’s coupling cases (a) and (c) [4].
In this section, we focus on the potentials and quasibound states of the $^{87}$Rb($nD_j + 5S_{1/2}$), $j = 3/2$ and $5/2$ molecules in the two limiting Hund’s cases and in the transition regime.

Figure 5(a) shows $V_1(Z)$ for the $j = 3/2$ and $5/2$ ($22D_{5/2} + 5S_{1/2}$) molecules (left) and $j = 3/2$ and $5/2$ ($40D_{5/2} + 5S_{1/2}$) molecules (right) calculated with all interaction terms in Eq. (1), excluding hyperfine-structure coupling. At high $n$, the molecules tend towards Hund’s case (c), where the dominant adiabatic molecular potentials are reduced by the product of two Clebsch-Gordan coefficients of the type $(n_t = 0, n_s = \pm 1/2)j, m_j = \pm 1/2$. This leads to adiabatic potentials whose depths carry spin-dependent factors $\ell/(2\ell + 1)$ for $j = \ell - 1/2$ and $(\ell + 1)/(2\ell + 1)$ for $j = \ell + 1/2$ [25]. For $nD_j$ ($\ell = 2$) molecules at high $n$, the depth ratio of the potentials for $j = 3/2$ and $j = 5/2$ approaches 2/3. This is seen in the depths of the outermost wells of the high-$n$ $j = 3/2$ and $5/2$ ($40D_{5/2} + 5S_{1/2}$) molecular potentials in Fig. 5(a). For decreasing $n$, the fine-structure splitting increases as $n^{-3}$ while the scattering interaction strength increases as $n^{-6}$, and the molecules tend towards Hund’s case (a). The $j = 3/2$ and $5/2$ ($22D_{5/2} + 5S_{1/2}$) molecular potentials in Fig. 5 exhibit this case, where the scattering interaction strength is large compared to the fine-structure splitting. In the low-$n$ limit, the $j = 3/2$ potential becomes notably deeper than the $j = 5/2$ potential.

The binding energies of the vibrational ground states in the outermost potential wells, $W_{\ell \rightarrow 0}$, closely track the depth of those wells and therefore mirror the transition of the molecule between the two Hund’s cases. In Fig. 5(b), we plot $W_{\ell \rightarrow 0}$ for the $j = 3/2$ and $5/2$ ($nD_j + 5S_{1/2}$) molecules for a range of $n$ from Hund’s case (a) (low-$n$) to Hund’s case (c) (high-$n$). In the high-$n$ limit, the molecular binding energies $W_{\ell \rightarrow 0}$ for both fine-structure levels approximately scale as $n^{-6}$, inversely with the atomic volume. In the low-$n$ limit, the lowest binding energy for the lower fine-structure level ($j = 3/2$) is larger and continues to scale as $\sim n^{-6}$, while that of the upper fine-structure level ($j = 5/2$) trends towards a $\sim n^{-3}$ scaling, approaching the scaling of the fine-structure splitting. For the $\text{Rb}(nD_j + 5S_{1/2})$ molecules, the binding energies of the vibrational ground states in the outermost potential wells for $j = 3/2$ and $j = 5/2$ are approximately equal at $n = 34$ [see Fig. 5(b)]. Further, due to the described Hund’s case behavior, at sufficiently low $n$ the inner wells of adiabatic potentials of the $nD_{3/2} + 5S_{1/2}$ molecule become deep enough to support vibrational states that are more deeply bound and long lived than the ground states of the outermost well of the $nD_{5/2} + 5S_{1/2}$ potentials.

VI. ELECTRIC AND MAGNETIC DIPOLE MOMENTS

Rydberg molecules present the only known case of homonuclear molecules with permanent electric dipole moments [7,12]. For high-$\ell$ Rydberg molecules dipole moments on the order of $10^6 a_0 e$ are predicted to exist [12]. Smaller permanent dipole moments arise in low-$\ell$ $S$, $P$, and $D$-type molecules from fractional admixing of high-$\ell$ state character. Permanent electric dipole moments of $\sim 5 - 50 a_0 e$ have previously been measured in rubidium $S$-type Rydberg molecules [7]. Dipolar cesium Rydberg molecules with electric dipole moments of $\sim 5 - 50 a_0 e$ have also been prepared. In this section we calculate both the electric and magnetic dipole moments for $nD$ Rydberg molecules, with all terms in the Hamiltonian in Eq. (1) included.

We obtain the adiabatic electric $|d_{i,\nu}(Z)|$ and magnetic $|\mu_{i,\nu}(Z)|$ dipole moments in the diagonalization of Eq. (1). The dipole moments of a molecular state $\nu$ follow from the expectation values of $d_{i,\nu}(Z)$ and $\mu_{i,\nu}(Z)$ over the vibrational wave function densities,

$$d_{i,\nu} = \int |\Psi_{i,\nu}(Z)|^2 d_{i,\nu}(Z) dZ$$

$$\mu_{i,\nu} = \int |\Psi_{i,\nu}(Z)|^2 \mu_{i,\nu}(Z) dZ.$$  (2)

Electric dipole moments for the ground vibrational states of the $j = 3/2$ and $5/2$ $^{87}$Rb($nD_j + 5S_{1/2}, F = 1,2$) deep (pure triplet) and shallow (mixed singlet-triplet) molecular potentials are shown in Fig. 6. In Figs. 6(a) and 6(b) we show the binding energies and representative potentials with wave functions, respectively, for all angular-momentum coupling cases that arise from Eq. (1). We note that for $^{87}$Rb($nD_j + 5S_{1/2}, F = 1,2$) molecules the hyperfine quantum numbers $F$ are well defined because the hyperfine coupling is much larger than the molecular binding. As seen in Figs. 6(a) and 6(b), the delineation between Hund’s cases (a) and (c) is shifted to lower $n$ for the shallow potentials (which are due to hyperfine-induced mixing of singlet and triplet states at the $5S_{1/2}$ atom). Essentially, the generally weaker scattering interaction
associated with the mixed singlet-triplet cases pushes those molecules more towards Hund’s case (c).

The electric dipole moments of the deep molecular potentials are eightfold degenerate when summed over all \( m_k \), and those of the shallow potentials are fourfold degenerate [see Fig. 6(c)]. It is noted that with decreasing \( n \) the degeneracies in energy and electric dipole moment become increasingly lifted. This may be attributed to a stronger configuration mixing at low \( n \) caused by the relative increase of the \( e^{-}+ \) perturber scattering term in Eq. (1). The only case in which the dipole moments of the \(^{87}\text{Rb}(n\,D_{\frac{1}{2}}+5S_{\frac{1}{2}}, F=1.2)\) molecules exhibit a clear scaling behavior in \( n \) is for the \( j=3/2 \) deep potentials (which are the same for \( F=1 \) and \( F=2 \)). A fit to the topmost data set in Fig. 6(c) gives an \( n^{-2.4} \) scaling,
similar to a result found previously for $^{87}$Rb$_2$ S-type Rydberg molecules [7]. Here, the scattering-induced mixing between the atomic Rydberg levels gives rise to a significant change in the electric dipole moments as a function of $n$. In the range $n \gtrsim 30$, the electric dipole moments for both types of shallow potentials of $^{87}$Rb($nD_{3/2} + 5S_{1/2}, F = 1, 2$) also approximately scale as $n^{-2.4}$. The electric dipole moments for the upper fine-structure component $j = 5/2$ have less clear scaling trends [squares in Fig. 6(c)]. In particular, the electric dipole moments for the deep $^{87}$Rb($nD_{3/2} + 5S_{1/2}, F = 1, 2$) potentials do not exhibit a clear scaling behavior. This is likely a result of the transition from Hund’s case (a) to Hund’s case (c).

The magnetic moments for the molecular states are shown in Fig. 6(d). The magnetic moments are nondegenerate due to the different $g$ factors of the involved types of spins. The $n$ dependence again reflects the transition in angular-momentum coupling behavior between the two Hund’s cases (a) and (c). We expect that experiments in weak electric and magnetic fields can reveal the electric and magnetic dipole moments of the vibrational states. The dipole moments computed in this work are for the weak-field limit, i.e., results are expected to be accurate as long as molecular Zeeman and Stark shifts are smaller than other relevant energy scales (such as the energy splitting between adjacent vibrational states).

VII. HYPERFINE-STRUCTURE EFFECTS IN DEEP $^3S$- AND $^3P$-DOMINATED POTENTIALS

The trilobite molecules [12] generated by the $^3S$ interaction are long range and on the order of 10 GHz deep, which is comparable to the hyperfine interaction of the $5S_{1/2}$ perturber. It is therefore of interest to explore hyperfine effects on the trilobite adiabatic potentials. In Figs. 7(a) and 7(b) we show these potentials without and with hyperfine coupling for $n = 30$, for all relevant values of $m_{j1} + m_{j2}$ and $m_{k} = m_{j1} + m_{j2} + m_{k2}$, respectively. While the hyperfine interaction does not affect the general shape and depth of the trilobite potentials, with hyperfine structure included there are three instead of only one. Since the number of $^3P$ potential curve also triples, the crossing pattern between $^3S$ and $^3P$ potentials becomes considerably more complex, as seen in Fig. 7. Considering that the modulations near the bottom of the trilobite potentials are several 100 MHz deep, which is sufficient to support individual bound vibrational states, the hyperfine structure is expected to have profound effects on the detailed vibrational level structure of these molecules. In Fig. 7(b), one may expect to find long-lived $^3S$-dominated states in the gray regions. Further, as indicated by the circles in Fig. 7(b), the crossing locations and the detailed coupling behavior of $\ell = 3$ Rydberg levels (which are optically accessible from low-lying atomic states) to molecular states in the long-range potentials also strongly depend on the hyperfine structure of the system under investigation.

In the present work we have not included the dependence of the $^3P$ $e^- +$Rb($5S_{1/2}$) scattering phase shift on $J$ (where $J = 0, 1, 2$) [17]. We have performed a preliminary calculation that indicates that the outermost several wells of the adiabatic potentials, which support the metastable molecular states, are not substantially altered by using $J$-dependent $^3P$ scattering phase shifts. We also find that the crossings between the $^3P$ potentials and the $^3S$ trilobite potentials shift in position by amounts up to about 50 a$_0$.

VIII. CONCLUSION

In summary, we have systematically explored the role of fine-structure and hyperfine-structure couplings in $^{87}$Rb$_2$ (Rydberg + $5S_{1/2}$) molecules formed between a Rydberg and $5S_{1/2}$ ground-state atom. As has been done extensively in previous work, we have treated the $e^- + 5S_{1/2}$ scattering with a Fermi model that includes $S$-wave and $P$-wave singlet and triplet scattering. The fine structure mostly influences the behavior of low-$\ell$ Rydberg molecules. We have explored in detail how $^{87}$Rb($nD + 5S_{1/2}$) molecules realize Hund’s cases (a) and (c). The hyperfine structure originates in the perturber atom and therefore has consequences for all types (low-$\ell$ and high-$\ell$) of Rydberg molecules. In the case of $^{87}$Rb($nD + 5S_{1/2}$) molecules, mixing of singlet and triplet potentials results in a set of shallow adiabatic potentials, whose quasibound states should be experimentally observable (in addition to those in the hyperfine-independent pure triplet potentials). We have obtained electric and magnetic dipole moments, which could, in future work, be measured spectroscopically in weak electric...
and magnetic fields. The hyperfine structure has also been seen to alter the deep, $^3S$-scattering-induced trilobite potentials as well as their crossing behavior with $\ell = 3$ Rydberg states; experimental spectroscopic studies should reveal these details. Since molecular level energies and properties are very sensitive to the scattering phase shifts used in the Fermi model, we expect that spectroscopy of Rydberg molecules can serve as a sensitive tool to provide measurement-based input to future theoretical studies in low-energy electron scattering.

The effects of the $J$ dependence of the $^3P$ scattering phase shifts could also be addressed in future work.

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Photoassociation of Long-Range $nD$ Rydberg Molecules

D. A. Anderson,* S. A. Miller, and G. Raithel
Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA
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We observe long-range homonuclear diatomic $nD$ Rydberg molecules photoassociated out of an ultracold gas of $^{87}$Rb atoms for $34 \leq n \leq 40$. The measured ground-state binding energies of $^{87}$Rb($nD + 5S_{1/2}$) molecular states are larger than those of their $^{87}$Rb($nS + 5S_{1/2}$) counterparts, which shows the dependence of the molecular bond on the angular momentum of the Rydberg atom. We exhibit the transition of $^{87}$Rb($nD + 5S_{1/2}$) molecules from a molecular-binding-dominant regime at low $n$ to a fine-structure-dominant regime at high $n$ [akin to Hund’s cases (a) and (c), respectively]. In the analysis, the fine structure of the $nD$ Rydberg atom and the hyperfine structure of the $5S_{1/2}$ atom are included.

Cold atomic systems have opened new frontiers at the interface of atomic and molecular physics. Of particular interest are a recently discovered class of long-range, homonuclear Rydberg molecules [1,2]. Formed via an attractive interaction between a Rydberg electron and a ground-state atom [1], these molecules are among the largest ever observed with internuclear separations of several thousand Bohr radii. Their distinctive binding mechanism, which is unlike conventional covalent, ionic, and van der Waals bonds between ground-state atoms, results in loosely bound molecules whose properties mimic those of their constituent Rydberg atoms. The discovery of these molecular bonds has been likened to a new ultracold chemistry [3] and has spurred a significant amount of theoretical [4,5] and experimental interest [6–9]. Nondegenerate, low angular momentum Rydberg states (orbital angular momentum $\ell \leq 2$ in rubidium) produce molecules with $\sim$ MHz binding energies and permanent electric dipole moments of a few Debye. The $\ell = 0$ molecules were first observed by photoassociation [10] of cold $^{87}$Rb atoms [2]. Recently, molecular states with $\ell = 1$ and high electron energies have also been excited via bound-bound transitions in $^{85}$Rb [9]. For high-$\ell$ Rydberg states, so-called trilobite molecules with giant permanent electric dipole moments of several kilo-Debye and $\sim$ GHz binding energies are predicted to exist [1]. These have yet to be observed, though dipolar molecules have been prepared in Rb [7] and Cs [8].

The relevant interaction was first described by Fermi [11] to help explain pressure-induced energy shifts of Rydberg absorption lines in a gas [12]. The de Broglie wavelength of the Rydberg electron (position $r$) is much larger than that of a heavy ground-state atom (position $R$) that lies within the Rydberg atom’s volume, and their interaction can be approximated as a low-energy $s$-wave scattering process (scattering length $a_s$). The interaction is described with a Fermi-type pseudopotential [1,13] $V_{\text{pseudo}}(r) = 2\pi a_s \delta^3(r - R)$, where $p$-wave and higher-order scattering [4] are neglected. For negative $a_s$, the interaction can lead to bound molecular states [1,13].

The bond strengths and electric and magnetic moments of Rydberg molecules are strongly dependent on the angular-momentum couplings in the Rydberg and ground-state atom constituents. In the present work, we focus on long-range $^{87}$Rb$_2$ molecules formed by an $nD$ Rydberg and a $5S_{1/2}$ ground-state atom. Within the low-$\ell$ class of these molecules, the $nD$ ones have the highest binding energies, which generally increase with $\ell$ due to the $\sqrt{2\ell + 1}$ scaling of the angular wave functions $Y^\ell_\ell(\theta = 0)$. The angular-momentum coupling spans three Hund’s cases as $\ell$ varies from 0 to 2. The $nS_{1/2} + 5S_{1/2}$ molecules are akin to Hund’s case (b), because they have $L = 0$ and total electron spin $S = 1$. The $nP_j + 5S_{1/2}$ molecules are akin to Hund’s case (c), because the fine structure coupling is larger than the scattering interaction energy. The $nD_j + 5S_{1/2}$ molecules present a unique system, because they transition from Hund’s case (c) at large $n$ to Hund’s case (a) at $n \lesssim 30$, where the scattering interaction energy becomes increasingly greater than the fine structure coupling. The $F$ and higher-$\ell$ states of Rb intersect with a sole, deeply bound (trilobite) potential which accumulates most of the level shifts [1], negating the existence of potential wells similar to those below the $S$, $P$, and $D$ asymptotes. In our model, we include the fine structure of the Rydberg atom and the hyperfine structure of the $5S_{1/2}$ perturber atom, both of which have observable effects.

To excite $nD$ Rydberg molecules, we first prepare a sample of $\sim 10^5$ magnetically trapped $^{87}$Rb atoms in their [$F = 2, m_F = 2$] ground state at a temperature $\lesssim 17$ $\mu$K and peak density $\gtrsim 5 \times 10^{14}$ cm$^{-3}$. Optical excitation to $nD$ Rydberg states is accomplished via a two-photon transition from the $5S_{1/2}$ ground state by using 780- and 480-nm laser beams. The 780-nm laser frequency is fixed $\sim 1$ GHz off resonance from the $5S_{1/2}$ to $5P_{3/2}$ transition, and the 480-nm laser frequency is scanned to excite either Rydberg atoms or...
molecules. The combined excitation bandwidth is $\approx 2 \text{ MHz}$. The 780-nm laser has a power of $\sim 500 \mu \text{ W}$ and is collimated to a full width at half maximum (FWHM) of 3.5 mm. The 480-nm beam has a power of $\sim 35 \text{ mW}$ and is focused to a FWHM of $89 \pm 5 \mu \text{ m}$ into the cigar-shaped atom sample, which has a FWHM diameter of $28 \mu \text{ m}$ and an aspect ratio of $\approx 1:3$. The atom sample is enclosed by six individually addressable electrodes used to control the electric field at the excitation location, described in previous work [14]. We zero the electric field to within $\lesssim 200 \text{ mV/cm}$ by Stark spectroscopy on $59D$ Rydberg states [15]. This ensures that quadratic Stark shifts of the $nD$ Rydberg levels in the $n$ range of interest are $\lesssim 2 \text{ MHz}$. In a single experiment, the atom sample is illuminated by $2-3 \mu \text{ s}$ long laser pulses followed by electric-field ionization of Rydberg atoms and molecules [16]. The signal ions are extracted and detected by a microchannel plate located 10 cm away. We use one ground-state atom sample for a series of 55 individual experiments at a single 480-nm frequency step; density loss during one series is negligible.

The photoassociation of a Rydberg atom and ground-state atom pair into a bound molecular state occurs when the excitation laser is detuned from the atomic Rydberg line by an amount equal to the molecular binding energy. In Fig. 1, we show an experimental spectrum in the vicinity of the atomic $35D_{5/2}$ Rydberg line. A prominent satellite line emerges at $-38 \pm 3 \text{ MHz}$, which is assigned to the $(35D_{5/2} + 5S_{1/2})(\nu = 0)$ molecule, where $\nu = 0$ denotes the vibrational ground state. This binding energy is $\approx 1.6$ times larger than that of the $(35S_{1/2} + 5S_{1/2})(\nu = 0)$ molecular state measured in previous experiments [2,6].

![35DS2 spectrum](image)

**FIG. 1.** Spectrum centered on the $35D_{5/2}$ atomic Rydberg line showing the $^{87}\text{Rb}(35D_{5/2} + 5S_{1/2})(\nu = 0)$ molecular line at $-38 \pm 3 \text{ MHz}$. The vertical error bars are the standard error of three sets of 55 individual experiments at each frequency step. The error in the binding energy is equal to the average long-term frequency drift observed over one full scan.

The larger binding energy reflects the deepening of the molecular potential with $\ell$.

A series of $nD_{5/2}$ Rydberg spectra for $34 \leq n \leq 42$ is shown in Fig. 2(a) (right). The lowermost, redshifted lines for $n = 40$ and below are assigned to the molecular states. Molecular lines are not discernable in the $n = 42$ and 41 spectra, because the line broadening due to residual fields and the laser linewidth exceeds the molecular binding energies for these states. Additional satellite lines are expected but are likely obscured in Figs. 1 and 2(a) by the broadening of the atomic lines as well as artificial signals at $\pm 20 \text{ MHz}$ due to weak, symmetric side peaks in the 480-nm laser spectrum (caused by a Pound-Drever-Hall stabilization loop). Features near $-20 \text{ MHz}$ are assigned to molecular lines only if they are significantly stronger than the artificial signal at $+20 \text{ MHz}$.

![Binding energies and peak number of detected ions](image)

**FIG. 2.** (a) Right: Spectra centered on $nD_{5/2}$ atomic Rydberg lines for the indicated values of $n$ and identified molecular lines (squares). Left: Selected spectra from the plot on the right for states with identified molecular lines. Error bars are obtained as in Fig. 1. (b) Binding energies obtained from Gaussian fits to the molecular lines identified in (a) vs $n$. An allometric fit (solid curve) to the experimental binding energies yields a $n^{-5.9 \pm 0.4}$ scaling. Also shown are theoretical binding energies for the $^{87}\text{Rb}(nD_{5/2} + 5S_{1/2})(\nu = 0)$ molecular states with $\alpha_0 = -14\alpha_0$ (hollow circles and dotted curve). (c) Peak number of detected ions on the $nD_{5/2}$ atomic Rydberg line (solid diamonds, left axis) and ratio of molecular and atomic line strengths (hollow diamonds, right axis) vs $n$.
Figure 2(b) shows the molecular binding energies measured in Fig. 2(a) vs. $n$. One may expect the binding energies to be proportional to the probability density of the Rydberg electron wave function, which scales as $\sim n^{-6}$. An allometric fit to the data in Fig. 2(b) qualitatively supports this expectation over the displayed range of $n$.

As shown in Fig. 2(c), the ratio of molecular and atomic line strengths ranges from $\approx 1\% - 5\%$. By taking our peak atomic density into consideration, this agrees quite well with the relative signal strengths found in Refs. [2,6]. One may expect the molecular-signal ratio to scale with the probability density of finding a $5S_{1/2}$ atom within the Rydberg-atom volume (which scales as $n^6$), corresponding to an increase of about a factor of 2.5 over the $n$ range in Fig. 2(c). The observed increase is about a factor of 5. This enhancement is likely due to a Rydberg excitation blockade caused by electrostatic Rydberg-atom interactions [17,18], which suppresses the atomic line strength. Since the blockade’s effectiveness increases with $n$, the molecular-signal ratio scales faster than $n^6$. This interpretation is corroborated by the atomic-signal strength, which drops by a factor of 4 over the $n$ range in Fig. 2(c). In the absence of an excitation blockade, the atomic signal would drop as $n^{-3}$, i.e., by only a factor of 2 in Fig. 2(c).

Molecular states of the $nD_j + 5S_{1/2}$ type exhibit a transition between Hund’s case (a) at low $n$ and Hund’s case (c) at high $n$. Most of our data trend towards Hund’s case (c), where the dominant molecular potentials carry spin-dependent factors $|\langle m_f = 0, m_s = \pm 1/2 | j, m_j = \pm 1/2 \rangle|^2$ (detailed model below); these factors are $\epsilon/(2\epsilon + 1)$ for $j = \ell + 1/2$ and $(\ell + 1)/(2\ell + 1)$ for $j = \ell - 1/2$. Hence, in Hund’s case (c) (high $n$) the $\nu = 0$ binding-energy ratio for $nD_j + 5S_{1/2}$ $j = 3/2$ and 5/2 molecules should be about 2/3. For decreasing $n$, the fine structure splitting increases as $n^{-3}$, while the molecular binding energy increases as $n^{-6}$. The system then trends towards Hund’s case (a), in which the $\nu = 0$ binding energy ratio changes from 2/3 to $\approx 1$ (see below). Therefore, the $\nu = 0$ binding energy ratio is a convenient experimental measure to characterize the system. Figure 3 shows spectra of the two fine structure components of $37D$. Molecular peaks are present for both $j = 3/2$ and 5/2, with binding energies of $24 \pm 3$ and $26 \pm 3$ MHz, respectively, corresponding to a ratio of 0.92 $\pm$ 0.15. Since this is significantly larger than 2/3, for $n = 37$ the system is in the transition regime between Hund’s cases (c) and (a).

Next we compare experimental data with a calculation. We consider $s$-wave triplet scattering and omit singlet scattering [1]. For low electron momenta $k$, the $s$-wave triplet scattering length is $a_T(k) \approx a_{s0} + \xi k^2$, where $a_{s0} = a_T^0(k = 0)$ is the zero-energy scattering length and $\alpha$ the Rb $5S_{1/2}$ polarizability [13]. We fit $a_{s0}$ to match the experimental data. In calculations not presented here we have verified that $p$-wave scattering strongly influences the inner part of the molecular potentials [20] but leaves the outermost well, where the bound states relevant to our work are found, largely unaffected. The Rydberg atom’s fine structure and the perturber’s hyperfine structure are included, because they are on the same order or larger than the molecular binding. The much smaller hyperfine structure of the Rydberg atom is ignored. We include configuration mixing with neighboring Rydberg manifolds [5]. For the $5S_{1/2}$ atom located at $\mathbf{R} = \mathbf{z}_e$, the Hamiltonian is

$$\hat{H}_0 + 2\pi a^s_0 |k(r)| \delta(r - \mathbf{z}_e) \left( \hat{S}_1 \cdot \hat{S}_2 + \frac{3}{4} \right) + A \hat{S}_2 \cdot \hat{I}_2,$$

(1)

where the unperturbed Hamiltonian $\hat{H}_0$ includes Rydberg quantum defects and fine structure [16]. The operators $\hat{S}_1$ and $\hat{S}_2$ are the spins of the Rydberg electron and $5S_{1/2}$ atom, respectively. The $^{87}$Rb $5S_{1/2}$ atom has $\ell' = 0$, a nuclear spin $I_2$ with $I_2 = 3/2$, and a hyperfine parameter $A = h \times 3.4$ GHz (in SI units). The projector $\hat{S}_1 \cdot \hat{S}_2 + \frac{3}{4}$ has the eigenvalue one (zero) for the triplet (singlet) states of $\hat{S}_1$ and $\hat{S}_2$, enabling only triplet scattering. In the classically allowed range of the Rydberg electron $k = \sqrt{-1/(n_{eff,1} n_{eff,2}) + 2/r}$ (atomic units), and $k = 0$ elsewhere. Here, $n_{eff,1}$ and $n_{eff,2}$ are the effective quantum numbers of the Rydberg states coupled by the scattering term. Since only states with $m_{j1} = m_{j2} = 0$ are nonvanishing on the internuclear axis, the relevant Hilbert space is limited to $\{m_{j1}, m_{j2} = \pm 1/2, m_{s1} = \pm 1/2, m_{s2} = \pm 1/2, \pm 3/2 \}$. Since the Hamiltonian in Eq. (1) conserves $m_{j1} = m_{j2} + m_{s1} + m_{s2}$, the space breaks up into separated subspaces with $m_{k} = \pm 5/2, \pm 3/2, \pm 1/2$, where the scattering term couples states with the same $m_{j1} + m_{s1}$, while the hyperfine term couples states with the same $m_{j2} + m_{s2}$.

The Hamiltonian in Eq. (1) is diagonalized, resulting in adiabatic potential surfaces $V_{ad,i}(Z)$ and electric $[d_i(Z)]$ and magnetic $[\mu_i(Z)]$ dipole moments of the adiabatic
states [i is an arbitrary label for the $V_{ad}(Z)$]. The vibrational states $W_{i,v}$ and their wave functions $\Psi_{i,v}(Z)$ are found by solving the Schrödinger equation with potential $V_{ad,i}(Z)$ and reduced mass $87 \text{ amu}/2$, and their electric and magnetic dipole moments are $d_{i,v} = \int |\Psi_{i,v}(Z)|^2 d_i(Z) dZ$ and $\mu_{i,v} = \int |\Psi_{i,v}(Z)|^2 \mu_i(Z) dZ$, respectively.

In Figs. 4(a) and 4(b), we show all potentials $V_{ad}(Z)$ for $35D_{3/2}$ and $35D_{3/2}$ that connect to the $F = 2$ hyperfine level of the $5S_{1/2}$ atom, as well as the vibrational states $\nu = 0, 1$ of the deeper potentials. The deep and shallow potentials and their states have degeneracies of 6 and 4, respectively. The shallow potentials are due to hyperfine-induced mixing between the electronic singlet and a triplet state. In Figs. 4(c) and 4(d), we show the vibrational energies $W_{i,v}$ for $\nu = 0, 1$ over a range of $n$ for $nD_{3/2} + 5S_{1/2}$ and $nD_{3/2} + 5S_{1/2}$ molecules.

In the experiment, we excite molecules below the $F = 2$ asymptote, for which the states in the deep potential $V_{ad}(Z)$ have the larger degeneracy and are easier to observe due to their larger binding energies. Hence, we adjust $a_{i0}$ so that the $\nu = 0$ levels in the deep $V_{ad}(Z)$ match the experimental data in Figs. 1–3 and find $a_{i0} = -14a_{00} \pm 0.5a_{00}$ [see Fig. 2(b)]. (For $37D_{5/2}$ the $\nu = 0$ binding energy increases by about 4 MHz when changing $a_{0}$ from $-13.5$ to $-14.5a_{0}$. This $a_{0}$ value lies within the range of published values $-13$ to $-19.48a_{0}$ [2,6,21–23]. The experimental signals at about half the $\nu = 0$ binding energies, seen in some of the plots in Fig. 2(a), may correspond to levels at about half the $\nu = 0$ binding energies in Figs. 4(c) and 4(d).

In the high-$n$ limit in Fig. 5(a), the $\nu = 0$ binding-energy ratio for $D_{5/2}$ and $D_{5/2}$ approaches $2/3$, as expected for Hund’s case (c), and both sets of binding energies approximately scale inversely with the atomic volume (i.e., as $n_{ad}^{-2}$). At low $n$, the system transitions into Hund’s case (a), where the binding-energy ratio changes from $2/3$ to $\gg 1$. Also, the $\nu = 0$ binding energies for the lower $(D_{3/2})$ fine structure level exceed the fine structure coupling and keep scaling as $a_{0}$, while those for the $D_{3/2}$ level approach the fine structure splitting and its scaling $(n_{ad}^{-2})$. The experimental data in Fig. 3 are in the transition regime between the two Hund’s cases.

For $nD$ Rydberg molecules the electric dipole moments $d_{i,v}$ are somewhat smaller than for $nS$ ones [see Fig. 5(b) and Ref. [7]]. As a result of the transition between two Hund’s cases, the $d_{i,v}$ of the $nD_{2}$-type molecules do not exhibit a clear scaling. Those for the $nD_{3/2}$-type molecules scale close to $n_{ad}^{-2}$, similar to $S$-type ones [7]. Noting that $d_{i,v} \approx 0.25a_{0}$ and that the stray electric field in our experiment is $\leq 200 \text{ mV/cm}$, the experimental permanent-electric-dipole shift is well below $1 \text{ MHz}$. The magnetic moments [Fig. 5(c)] exhibit a gradual change that reflects the change in angular-momentum coupling behavior between the two Hund’s cases. In our < 1 G magnetic field in the atom trap, the molecular lines could be broadened over a range $\leq 4 \text{ MHz}$, while the atomic lines have $|m_j| \leq 5/2$ and could be broadened over a range $\leq 8 \text{ MHz}$. These estimates agree well with the linewidths seen in the spectra.

In summary, we have observed polar Rydberg molecules of the type $nD_j + 5S_{1/2}$. The binding energies are larger than those of previously observed $nS_{1/2} + 5S_{1/2}$ molecules. The molecules undergo a transition between Hund’s case (a) at low $n$ to Hund’s case (c) at high $n$. With improved spectroscopic resolution, one should be able to measure the electric dipole moments and to assign higher-lying vibrational levels in the deep potentials in Fig. 4 as well as levels in the shallow potentials. Recently, we became...
aware of related work on \( nD \) molecular states in a highermagnetic-field regime [24].

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*anderda@umich.edu

Abstract
Research on interactions between quantum gases and impurities (ions, other atoms etc.) has become an active area of AMO research over the past couple of years. Among the topics of interest one finds the formation of mesoscopic ions, charge hopping and quantum transport, self trapping of impurities in Bose-Einstein Condensate (BECs), and the effect of impurity particles on the BEC density distribution. To study ion-BEC interactions, a method must be used that allows one to hold a cold ion in a BEC for a sufficiently long time that these phenomena become observable, in a way that does not heat the ion.

In the project two setups have been constructed and operated towards these goals. In the first, more basic one, a metal tip (diameter 125 microns) is mounted close to a magneto-optic trap (MOT). Rydberg excitations are implanted in a cold-atom region (diameter about 10 microns, length about 50 microns). Interactions between the excitations cause excitation blockades, short- and medium-range order, as well as dynamics due to van-der-Waals interaction. All these topics have been studied. Two papers were published [one PRL, one PRA, one submitted to PRL].

The second setup is a double-trap system, in which we prepare magnetically trapped rubidium atom samples between 1 and 10 micro-Kelvin and densities of about $10^{12}$ cm$^{-3}$. We have prepared and
trapped, for the first time, cold circular Rydberg atoms in these traps. In addition to being able to study the dynamics of these highly dipolar atoms in the magnetic trap, we also observed a collision-induced loss we have traced back to collisions between the long-lived circular atoms and cold ground state atoms. These types of collisions are unexplored, to date. In this setup we also have prepared and studied D-type molecules between Rydberg and ground-state atoms. These are due to an attractive triplet s-wave low-energy scattering interaction between the Rydberg electron and a ground-state atom. We have published two papers, one in PRL, on in PRA.

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**Change in AFOSR Program Manager, if any:**

None

**Extensions granted or milestones slipped, if any:**

There was a one-year additional funded period and a no-cost time extension.

**AFOSR LRIR Number**
### LRIR Title

### Reporting Period

### Laboratory Task Manager

### Program Officer

### Research Objectives

### Technical Summary

### Funding Summary by Cost Category (by FY, $K)

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