STRUCTURE AND OPTICAL PROPERTIES OF NANOCRYSTALLINE HAFNIUM OXIDE THIN FILMS (POSTPRINT)

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Interim Report

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Hafnium oxide (HfO$_2$) films were grown by sputter-deposition by varying deposition temperature (T$_s$) in a wide range of 25–700°C. The deposited HfO$_2$ films were characterized by studying their growth behavior, microstructure, and optical properties. Characterization of the films employing a wide range of analytical techniques indicates a clear functional relationship between processing conditions, structure, morphology, and optical properties. HfO$_2$ films were amorphous at T$_s$ = 600°C, at which point a structural transformation occurs. HfO$_2$ films grown at T$_s$ < 200°C were nanocrystalline, stabilized in a monoclinic structure. The nanocrystalline HfO$_2$ films exhibit a strong (111) texturing. The average crystallite size of HfO$_2$ films increased from ~10 nm to ~20 nm with increasing T$_s$. Electron and atomic force microscopy measurements also correlated with the crystalline behavior, as well as an evenly distributed network of spherical shaped crystallites for the nanocrystalline HfO$_2$ films. Density (p) of HfO$_2$ films probed using X-ray reflectivity and ellipsometry data analysis indicate that the q values are strongly dependent on T$_s$; p varied in the range of 7.36–9.14 g/cm$^3$. The higher end of p values were noted only for HfO$_2$ films grown at relatively higher T$_s$, indicating the crystalline nature accounts for the q improvement. The band gap values of the films varied in the range of 5.78–6.17(±0.03) eV for T$_s$ = 25–700°C. Index of refraction at 550 nm increased from 1.80 to 2.09, which also correlates with the characteristic feature of improved structural order, packing density of HfO$_2$ films with increasing T$_s$. Based on the observed results, a correlation between growth conditions, microstructure and optical constants is established.
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Structure and optical properties of nanocrystalline hafnium oxide thin films

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Hafnium oxide (HfO2) films were grown by sputter-deposition by varying deposition temperature (Ts) in a wide range of 25–700 °C. The deposited HfO2 films were characterized by studying their growth behavior, microstructure, and optical properties. Characterization of the films employing a wide range of analytical techniques indicate a clear functional relationship between processing conditions, structure, morphology, and optical properties. HfO2 films were amorphous at Ts ≤ 200 °C, at which point a structural transformation occurs. HfO2 films grown at Ts > 200 °C were nanocrystalline, stabilized in a monoclinic structure. The nanocrystalline HfO2 films exhibit a strong (1 1 1) texturing. The average crystallite size of HfO2 films increased from ~10 nm to ~20 nm with increasing Ts. Electron and atomic force microscopy measurements also correlated with the crystalline behavior, as well as an evenly distributed network of spherical shaped crystallites for the nanocrystalline HfO2 films. Density (ρ) of HfO2 films probed using X-ray reflectivity and ellipsometry data analysis indicate that the ρ values are strongly dependent on Ts; ρ varied in the range of 7.36–9.14 g/cm3. The higher end of ρ values were noted only for HfO2 films grown at relatively higher Ts indicating the crystalline nature accounts for the ρ improvement. The band gap values of the films varied in the range of 5.78–6.17(±0.03) eV for Ts = 25–700 °C. Index of refraction at 550 nm increased from 1.80 to 2.09, which also correlates with the characteristic feature of improved structural order, packing density of HfO2 films with increasing Ts. Based on the observed results, a correlation between growth conditions, microstructure and optical constants is established.

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1. Introduction

Hafnium oxide (HfO2) is a technologically important metal oxide, which is characterized by a unique combination of mechanical, chemical, electronic and optical properties [1–15]. HfO2 films exhibit high dielectric constant (k ~ 25) and wide band gap (Eg ~ 5.7 eV), which makes the material attractive for applications in the fields of electronics and opto-electronics [1–4]. HfO2 remains the leading candidate to replace SiO2 dielectrics in gate oxides due to a higher permittivity and reportedly lower electron tunneling effects [5,6].

Hafnium oxide exhibits various polymorphs on the basis of temperature and pressure. Monoclinic HfO2 (P21/c) is the most thermodynamically stable phase at ambient conditions of temperature and pressure [7,8]. At temperatures higher than 1700 °C, HfO2 transforms into the tetragonal (P42/mmc) phase [7]. A further increase to 2200 °C results in the cubic (Pm3m) phase formation [7]. In addition, monoclinic HfO2 may undergo a phase transition under pressures of the order of 12 GPa to a denser structure, orthorhombic I (Pbca), and a further increase in pressure to 28 GPa results in the orthorhombic II (Pnma) phase formation [7,8]. In view of the set of thermodynamic conditions resulting in specific phase formation and properties, the controlled growth and manipulation of specific crystal structures at the nanoscale dimensions have important implications for the design and applications of HfO2. The present work is focused towards the fabrication, structural analysis and optical property evaluation of nanocrystalline HfO2 films by sputter-deposition.

A large band gap coupled with low absorption provide optical transparency over a broad range in the electromagnetic spectrum; HfO2 optical films and coatings can operate efficiently down to 220 nm in the ultraviolet (UV) region and 10 μm in the infrared (IR) region [9,10]. There are not many contenders that are stable...
under UV considerations, therefore HfO2 is also a preferred high index material when high laser damage threshold is a requirement. As a result, HfO2 has been used in optical coating applications, including optical filters, ultraviolet heat mirrors, antireflection coatings and novel scintillation materials [1–12].

The objective of the present work is to derive a comprehensive understanding of the structure and optical properties of HfO2 thin films grown as a function of variable deposition temperature. Often, very specific film properties are required for optimal performance. It is evident, and well known, that the thermodynamically stability and phase existence depends on growth temperature and pressure conditions. In addition, the controlled growth and manipulation of specific HfO2 crystal structures at the nanoscale dimensions is the driving force for technological implications. Therefore, it is important to characterize and obtain a correlation between physico-chemical and optical properties in nanocrystalline HfO2 films as a function of growth conditions. Most importantly, determining the optical properties such as band gap (Eg) and index of refraction (n) is important for transparent oxides, such as HfO2 in this case. Furthermore, for thin films and nanomaterials, Eg and n values are sensitive to the microstructure; optical parameters are influenced by various factors such as surface/interface structure, crystal quality, packing density, lattice parameters, and defect structure. On the other hand, tailoring Eg and spectral behavior of n and the dispersion profiles allows for engineering modern electronic and optical devices. In this work, HfO2 films were produced by sputter-deposition in a wide range of growth temperature, which results in HfO2 films with a variable microstructure. The preliminary results of spectroscopic ellipsometry characterization of the index of refraction for HfO2 films has been reported elsewhere [13]. The effect of growth temperature on the optical properties is reported and a structure–property relationship is established in this paper for HfO2 sputter-deposited films.

2. Experimental

2.1. Film growth

Hafnium oxide films were deposited onto silicon (100) wafers and quartz substrates by radio frequency magnetron sputtering. All the substrates were thoroughly cleaned and dried with nitrogen before introducing them into the vacuum chamber, which was initially evacuated to a base pressure of ~10⁻⁶ Torr. A hafnium (Hf) target (Plasmaterials, Inc.) of 2 in. diameter and 99.95% purity was employed for sputtering. The Hf target was placed on a 2 in. sputter gun, which is placed at a distance of 8 cm from the substrate. The sputtering gas was high-purity (99.999%) argon (Ar), while oxygen (O₂), was introduced during deposition for reactive growth to form Hf-oxide. A power of 100 W was employed for reactive deposition. The ratio of Ar to O₂ was kept at 70:30 (28 sccm Ar mixed with 12 sccm of O₂) and the respective flow of each gas was monitored using an MKS mass flow meter. Before each deposition, the Hf target was pre-sputtered for 10 min with a shutter above the gun closed. The deposition time was carried out for 45 min. The thicknesses of the films were in the range ~33–60 nm. Film thickness measurements were made by three different methods as discussed under Section 3. Growth temperature (Tg) was varied in the range of room temperature (RT = 25 °C)–700 °C, the other variables such as sputtering power, pressure, and flow of Ar and O₂ and their ratio were kept constant.

2.2. Characterization

The grown HfO2 films were characterized by performing crystal structure, surface morphology, and optical measurements.

2.2.1. X-ray diffraction (XRD)

X-ray diffraction(XRD) measurements on HfO2 films grown on Si were performed using a Bruker D8 Advance X-ray diffractometer. All the measurements were made ex situ as a function of growth temperature. In order to avoid interference by the substrate and obtain diffraction pattern of the coatings, grazing incidence X-ray diffraction (GIXRD) were performed on the films. XRD patterns were recorded using Cu Kα radiation (λ = 1.54056 Å) at room temperature. High resolution scans were also performed on evident crystallization peaks with parameter of a step size of 0.01° per 1 s. The crystalline domain size was calculated through the use of the Scherrer relationship, after removal of background artifacts. The Scherrer equation is defined by,

\[ D_{hkl} = \frac{0.9\lambda}{\beta \cos \theta} \]

where \(D_{hkl}\) is the crystallite size, \(\lambda\) is the wavelength of the filament used in the XRD machine, \(\beta\) is the full width half maximum of the peak corrected for instrumental broadening, and \(\theta\) is the angle of the peak [16,17].

2.2.2. Scanning electron microscopy (SEM)

Surface imaging analysis was performed using a high-performance and ultra-high resolution scanning electron microscope (Hitachi S-4800). Secondary electron imaging was performed on HfO2 films grown on Si wafers using carbon paste at the ends to avoid charging problems.

2.2.3. Atomic force microscopy (AFM)

Surface morphology of the HfO2 films was also studied employing atomic force microscopy (AFM) using a Veeco Multimode scanning probe microscope with a Nanoscope V controller. AFM images were acquired using the ScanAsyst mode which utilizes a Bruker proprietary method for curve collection and sophisticated algorithms to continuously monitor image quality, and automatically make appropriate parameter adjustments [18]. Aluminum coated silicon cantilevers (Bruker, USA) were used to acquire ScanAsyst mode images. The cantilevers measure 115 μm long, 25 μm wide and 0.65 μm thick with a spring constant of 0.4 N/m a resonance frequency of 70 kHz. Tip quality was qualitatively assessed by the clarity and presence of artifacts in the acquired images. The calibration standard used to calibrate the scanner consisted of platinum-coated, 200 nm–tall silicon columns spaced at 10 μm intervals on centers. The columns have a length of 5 nm on a side. AFM images (512 scan lines & 512 pixels per scan line) were acquired with an integral gain of approximately 2, a proportional gain of approximately 50, and an amplitude setpoint of 200 mV. The drive amplitude varied between 30 and 180 mV. The images were then subjected to a 3rd order flattening procedure using the Veeco Nanoscope software to remove the non-linear background artifact introduced by the piezo scanner. Following the flattening procedure, the surface roughness was quantified over five areas of 1 μm × 1 μm on the 5 μm × 5 μm scan size images.

2.2.4. X-ray reflectivity (XRR)

X-ray reflectometry (XRR) measurements were performed on a Rigaku Smartlab X-ray diffractometer. A Cu Kα X-ray source is used by the Smartlab diffractometer. Scans were taken at a speed of 0.2° per minute and a step size of 0.005°. The total length of scans were taken at low angles from 0° to 6°. Experimental data was then fit with the software package GlobalFit associated with Rigaku Smartlab diffractometer.

2.2.5. Spectrophotometry measurements

Optical properties were evaluated using both spectrophotometric and ellipsometry measurements. Spectrophotometry measurements were attained by using a Cary 5000 UV–vis–NR
double-beam spectrophotometer. Films grown on optical grade quartz were employed for optical property measurements to probe the transparent nature and band gap analysis of the HfO2 films.

2.2.6. Spectroscopic ellipsometry (SE)

Spectroscopic ellipsometry (SE) was performed ex-situ on the films grown on silicon wafers using a J.A. Woollam V-VASE instrument. Measurements were done in the range of 300–1350 nm with a step size of 2 nm and at angles of incidence of 65°, 70°, and 75°, near the Brewster’s angle of silicon. The ellipsometry data analysis was performed using commercially available WVASE32 software.

3. Results and discussion

3.1. Crystal structure

X-ray diffraction patterns of HfO2 films are shown in Fig. 1a as a function of Ts. The patterns at Ts ≥ 200 °C exhibit crystalline nature oriented along the (111), designating a crystallization temperature of 200 °C for monoclinic HfO2. The film remains amorphous for Ts = RT. However, the peak corresponding to Ts = 200 °C is minor and broad. Perhaps, small crystallites being present in an amorphous matrix might be the reason for appearance of the broad peak. The intensity of the (111) peak increases with increasing growth temperature which indicates an increase in crystallite size with Ts. The films exhibit a strong (111) texturing which is expected based on phase-stability considerations [19–24]. It is well-known that (111) planes will primarily populate as they exhibit the lowest surface free energy, although minor peaks due to other orientations of monoclinic crystallites are also present at higher temperatures. High resolution scans of (111) texturing are shown in Fig. 1b. The high resolution scans were performed on (111) peaks for all the HfO2 films in order to obtain further information on the growth process, phase, and crystallite size at the nanoscale dimensions. It can be noted that the peak shifts to the higher diffracting angle for films grown from 200 °C to 400 °C. This trend continues for films grown at higher temperatures, however, at 500 °C the peak position retrogrades before continuing to increase. The shift in peak position is attributed to the lattice expansion and lattice mismatch between film and substrate. It is important to recognize the variation of d spacing for (111) planes with Ts which aids in obtaining quantitative information on the lattice expansion. The d spacing versus Ts for HfO2 films is shown in Fig. 2. The trend in d(111) is increasing for Ts ≤ 400 °C, after which the trend begins to slightly decline for Ts ≥ 500 °C. This leads to conclude that in this regime of Ts the lattice mismatch is at a maximum [20]. It is evident that at Ts ≥ 500 °C, the increase in grain size is affected more by the microstrain in the thin films, and slightly less by the effect of temperature. The average crystallite size increased from ~10 nm to ~20 nm (~2 nm) with increasing Ts from 200 to 700 °C. Furthermore, FWHM values decrease with Ts attributing to the increase in crystallite size (Fig. 2).

3.2. Film thickness and density

The XRR data of HfO2 films are shown in Fig. 3. Simulation of the XRR experimental data using appropriate models can provide physio-chemical information of HfO2 films. Specifically, the surface roughness, thickness and density of the HfO2 films can be obtained from XRR spectra [22]. The density can be calculated from the total reflection or critical edge, while film thickness can be derived from the period of the oscillations in the XRR spectra. In the present case, it is evident that the experimental and simulation curves are in excellent agreement for HfO2 films (Fig. 3). The stack model employed to simulate the XRR spectra contains, from top, HfO2 film, SiO2 interface and Si substrate. The surface and interface roughness were also considered in order to accurately fit the experimental XRR spectra of HfO2 films. A positive shift of the critical edge noted from XRR spectra indicates that the film density increases with Ts; further analysis was made with SE measurements as explained in the later portion of the discussion. The period of the oscillations present for the crystalline samples of the HfO2 films does not significantly change with Ts, which is in agreement with the deposition rate to obtain ~40 nm thicknesses;
thickness measurements will also be validated with SEM and SE measurements discussed below. Thickness measurements observed were for the fully crystallized films ($T_s = 300–700^\circ C$). Structural information obtained for the HfO$_2$ films is demonstrated in Fig. 4.

3.3. Surface morphology

The scanning electron microscopy (SEM) images of the HfO$_2$ films are shown in Fig. 5. The amorphous nature of the film is evident in the sample grown at RT. The crystalline samples ($T_s = 200–700^\circ C$) possess a uniform distribution of dense particles spherical in shape. Topographical features of the HfO$_2$ films are also correlated through AFM and shown in Fig. 6. Most importantly an evident decrease in peak to valley or surface height with increase in growth temperature yields a roughness profile. The root-mean-square (rms) roughness of HfO$_2$ films decreases as growth temperature increases as seen in Fig. 7. Roughness measurements are evidently related to the quality of the films. A smoother film will occupy fewer reaction sites and promote minimal interfacial reactions between the HfO$_2$ film and Si substrate. Fig. 7 demonstrates a correlation between XRR roughness measurements and AFM roughness profiling which are well in agreement with one another.

3.4. Spectral transmission characteristics and band gap

Having established the microstructural and physical qualities of the HfO$_2$ films, the attention is now directed to the optical nature of the films. The HfO$_2$ films were transparent and colorless under transmitted light down to the 200 nm wavelength range as seen in Fig. 8a. The highest transparency is observed by the amorphous film over a wide wavelength range (200–800 nm) ranging from 85% to 95% at lower wavelengths. The monoclinic polycrystalline films still employ transparencies of near 70% at lower wavelengths but significantly less than the amorphous film. A further analysis of the optical spectra is performed to better understand the effect of microstructure on the optical properties and to derive a quantitative structure–property relationship. The optical absorption coefficient, $\alpha$, of the films is evaluated using the relation:

$$\alpha = \frac{\ln R_T}{t}$$

where $T$ is the transmittance, $R$ is the reflectance, and $t$ is the film thickness [10,25–29]. Absorption data for the films grown at $T_s = RT–700^\circ C$ can be seen in Fig. 8b. An interesting observation to be made from the absorption data is the shoulder-like feature provided by the crystalline films. This feature is strongly correlated with the crystallization of amorphous HfO$_2$ [28].

Further absorption data analysis was made to understand the broad energy feature and determine band gap measurements. Band gap values for the HfO$_2$ films were measured by employing the power law of the form:

$$\alpha h\nu = B(h\nu - E_g)^n$$

where $h\nu$ is the incident photon, $\alpha$ is the absorption coefficient, $B$ is the absorption edge width parameter, $E_g$ is the band gap, and $n$ is the exponent dependent on direct or indirect intrinsic band gap behavior [10,25–29]. The indirect band gap value for HfO$_2$ is related...
to the electronic transition from the O 2p valence band to the Hf 5d conduction band between C and B points on the reciprocal lattice of monoclinic HfO$_2$ [27,28]. Indirect band gap measurements were made following the power law with $n = 1/2$ on the band that initiates at 5.6 eV for the crystalline films as seen in Fig. 9. The existence of the additional absorption band will initiate and saturate below $E_g$ of the films [27]. Extrapolating the linear region of the $(\alpha h\nu)^{1/2}$ plot to zero and regression analysis for $R^2$ values greater than 0.9 provide accurate indirect-$E_g$ values which ultimately reveal a decreasing trend with $T_s$. Looking at the absorption coefficient for the films exhibiting monoclinic orientations ($T_s = 200–600^\circ C$) at values higher than 6.00 eV (inset of Fig. 8b) the steepest increase in absorption is observed. The high energies coupled with high absorption behavior tailor to band-band transitions, and therefore $E_g$ has been measured by following the direct band gap power law with $n = 2$ [26,29–32]. Extrapolating the linear region of the plot to zero and regression analysis for $R^2$ values greater than 0.9 provide accurate $E_g$ values as seen in Fig. 10. The band gap values are increasing with increasing $T_s$ as observed in Fig. 10 in the range of 5.75–6.13 eV. The more notable factor is the impact of the amorphous to monoclinic transition which causes a significant change in band gap measurements.

3.5. Optical constants

Ultimately, the optical constants of the nanocrystalline, monoclinic HfO$_2$ films are considered and discussed. Optical constants
of the HfO₂ films were primarily probed by SE, which measures the relative changes in the amplitude and phase of the linearly polarized monochromatic incident light upon oblique reflection from the sample surface. The experimental parameters obtained by SE are the angles Ψ (azimuth) and Δ (phase change), which are related to the microstructure and optical properties, defined by:

\[ \rho = \frac{R_p}{R_s} = \tan \Psi \exp(i\Delta) \]  

where \( R_p \) and \( R_s \) are the complex reflection coefficients of the light polarized parallel and perpendicular to the plane of incidence, respectively [33–36]. In general, the fundamental equation of ellipsometry that relates the measurable with the accessible optical information is:

\[ \rho = \tan \Psi \exp(i\Delta) = \rho(N_0, N_1, N_2, L_1, \Phi_0, \lambda) \]  

where the middle term contains the measurable and the last term on the right contains all the accessible parameters of the measurement, namely, film thicknesses, optical properties, the wavelength of light, and the angle of incidence [35]. The spectral dependencies of ellipsometric parameters Ψ (azimuth) and Δ (phase change) can be fitted with appropriate models to extract film thickness and the optical constants i.e., the refractive index (n) and extinction coefficient (k), based on the best fit between experimental and simulated spectra [25,33–36]. In the present case, the Levenberg–Marquardt regression algorithm was used for minimizing the mean-squared error (MSE):

\[ \text{MSE} = \frac{1}{2N - M} \sum_{\tau=1}^{n} \left( \left( \frac{\Psi_{\text{exp}} - \Psi_{\text{calc}}}{\sigma_{\Psi_{\text{exp}}}} \right)^2 + \left( \frac{\Delta_{\text{exp}} - \Delta_{\text{calc}}}{\sigma_{\Delta_{\text{exp}}}} \right)^2 \right) \]  

where \( \Psi_{\text{exp}}, \Psi_{\text{calc}} \) and \( \Delta_{\text{exp}}, \Delta_{\text{calc}} \) are the measured (experimental) and calculated ellipsometry functions, \( N \) is the number of measured \( \Psi, \Delta \) pairs, \( M \) is the number of fitted parameters in the optical model and \( \sigma \) are standard deviations of the experimental data points [25,33].

In order to extract optimal data from SE experimental and simulated measurements, the construction of a multilayer optical model is essential. The model representation accounts for a number of distinct layers with individual optical dispersions and the interfaces between these layers are optical boundaries at which light is refracted and reflected according to the Fresnel relations. The dispersion relations of the optical constants of HfO₂ films are derived using a stack model composed of the Si substrate, interfacial SiO₂ layer, and HfO₂ film; the surface roughness was also considered to obtain precision during experimental fitting. Succeeding the construction of the optical layer model, the HfO₂ films were modeled with a conventional Cauchy dispersion model, because the films are transparent in the visible region the Cauchy model is optimal. The Cauchy equation can be expressed approximately as a refractive index \( n \) as a function of wavelength \( \lambda \):

\[ n(\lambda) = A + \frac{B}{\lambda^2} + \frac{C}{\lambda^4} \]  

where \( A, B, \) and \( C \) are the Cauchy coefficients and specific to the material, \( A \) is the constant that dominates \( n(\lambda) \) for long wavelengths, \( B \) controls the curvature of \( n(\lambda) \) in the middle of the visible spectrum, and \( C \) influences \( n(\lambda) \) to a greater extent in shorter wavelengths [31]. Note that this principle behind Cauchy’s polynomial is also used for the dispersion function \( k(\lambda) \):

\[ k(\lambda) = d + \frac{e}{\lambda^2} + \frac{f}{\lambda^4} \]  

where \( d, e, \) and \( f \) are constants specific to the material [26,37].

Microstructural information obtained from SE data for the HfO₂ films is film thickness, which is relative to the stack optical model. The variation of film thickness as a function of growth temperature for various crystalline HfO₂ films is shown in Fig. 11. It is evident that the film thickness is more or less constant with increasing growth temperature; this observation is consistent with XRR and SE for the crystalline samples. To validate the SE analysis and microstructure, the film thickness values obtained from SEM measurements are also plotted in Fig. 11. Distinct film properties are responsible for film thickness characterization, and ultimately it can be seen that the film thickness obtained from SE, XRR, and SEM are in reasonable agreement with respect to one another for
HfO$_2$ films are shown in Fig. 12. The films are slightly less than the reported bulk value for HfO$_2$ [38] from the results and analysis, the optical quality of the HfO$_2$ films is shown to be highly satisfactory in obtaining other film properties, such as the optical constants, or chemical inertness in the films.

Fig. 11. Thickness measurements obtained through XRR, RBS, and SE modeling. The measurements commensurate with one another and deposition rate. Characterization techniques are then concluded to be highly satisfactory in obtaining other film properties, such as the optical constants, or chemical inertness in the films.

The dispersion profiles of $n(\lambda)$ determined from SE data for the HfO$_2$ films are shown in Fig. 12. The $n(\lambda)$ dispersion curves indicate a sharp increase at shorter wavelengths corresponding to fundamental absorption of energy across the band gap. However, the effect of growth temperature is evident in the dispersion curves (Fig. 11), where there is an increase in ‘n’ with $T_s$. In order to further study the effect of growth temperature on the optical constants, the refractive index variation of the films at $\lambda = 550$ nm is shown in Fig. 13. At a $\lambda = 550$ nm, the ‘n’ values increase from 1.79 to 2.09 with increasing growth temperature from 25 to 700 °C. The temperature dependence on structure is evident in the measurements where ‘n’ values increase drastically with $T_s$ initially and begins to depend less at higher $T_s$. However, the values obtained for the films are slightly less than the reported bulk value for HfO$_2$ [38] which can be attributed to the method of growth; the sputtered films are well known to have a higher defect density than bulk HfO$_2$.

A simple model can be formulated to explain the effect of microstructure on the optical properties in HfO$_2$ films. Furthermore, increasing $T_s$ results in improved structural order and texturing of HfO$_2$ films along with an increase in the average crystallite size. The density of the film also increases, as evidenced by XRR analyses. It is well known that the refractive index is closely related to the physical properties and density of the films. Thus, the observed increase in ‘n’ values when HfO$_2$ films grown at higher $T_s$ can be attributed to the improved packing density of the films coupled with improved structural order. Improved structural order results in the formation of a dense network of nanocrystals leading to an enhancement in the packing density. This characteristic change in structure results in the observed enhancement in ‘n’. In order to further confirm the proposed physics and mechanism, the relative density of the film is also approximated using the Lorentz–Lorenz relation employing the measured ‘n’ values at 550 nm [39,40]. The functional dependence of the relative density of HfO$_2$ films on $T_s$ is shown in Fig. 14. The density measured for amorphous HfO$_2$ films at $T_s = RT$ is only 7.4 g/cm$^3$. However, the density increases to 9.1 g/cm$^3$ for nanocrystalline HfO$_2$ films deposited at $T_s = 300–700$ °C. XRR density measurements commensurate with the values derived from Lorentz–Lorenz relation as seen for the crystalline samples Fig. 14 (inset).

**Fig. 13.** Variation of ‘n’ ($\lambda = 550$ nm) with $T_s$ is shown in the insert. It is evident that the ‘n’ increases from 1.79 to 2.09 with increasing $T_s$ from 25 to 700 °C.

**Fig. 14.** Density measurements obtained from the Lorentz–Lorenz relation, as well as a correlation with XRR measurements.

The monoclinic HfO$_2$ films. This observation indicates that the model(s) and SE analysis adopted can reasonable simulate the microstructure and, hence, optical properties of the sputter-deposited HfO$_2$ films.

**Fig. 12.** The index of refraction profiles of HfO$_2$ films grown at various $T_s$. The effect of growth temperature is evident in the dispersion curves; ‘n’ values increase with $T_s$.

HfO$_2$ thin films were grown by sputter-deposition in a wide range of growth temperature, 25–700 °C. GIXRD studies revealed that the HfO$_2$ films deposited at $T_s < 200$ °C were amorphous while those grown at $T_s > 200$ °C were nanocrystalline and exhibit monoclinic structure. The detailed analyses based on XRD indicate that the average crystallite size of HfO$_2$ film increases from ~10 nm.
to ~20 nm with increasing $T_s$. The corresponding film roughness follows a decreasing trend with increasing $T_s$. The packing density and structural order of the HfO$_2$ films increases with increasing $T_s$. The band gap values of the HfO$_2$ films were found to be in the range of 5.78–6.17(±0.03) eV for $T_s = 25$–700 °C. The index of refraction and their dispersion profiles correlate with the microstructure.

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