OPERATION OF LONGITUDINAL SHOCK WAVE FERROELECTRIC GENERATORS IN THE RESISTANCE MODE

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Abstract

Results of systematic experimental investigations of operation of explosively driven longitudinal (shock wave propagates along the polarization vector \(\mathbf{P}\)) shock wave ferroelectric generators (FEGs) with active loads varied in a wide range of resistance (more than 4 orders of magnitude) are presented. One of the specific features of FEGs is direct electrical connection of the ferroelectric energy-carrying element to the load. The ferroelectric element is always a part of the load circuit during explosive and electrical operation of the FEG. Electrical parameters of the ferroelectric element change significantly under shock wave action during operation of the generator and those changes affect the electrical parameters of the FEG-Load system. It follows from our experimental results that the output voltage, current and power produced by the FEG across the resistance load depend on both the electrical parameters of the load and geometrical dimensions of the ferroelectric energy-carrying element of the FEG. It is experimentally demonstrated that a miniature FEG is capable of delivering to the active load a pulsed power with peak amplitude up to 0.35 MW.

I. INTRODUCTION

At ambient conditions, a solid solution of lead zirconate and lead titanate (PZT) in a Zr:Ti ratio of 95:5 with 2% doping with niobium [Pb\(_{\text{99.9}}\)(Zr\(_{\text{0.95}}\)Ti\(_{\text{0.05}}\))\(_{\text{0.98}}\)Nb\(_{\text{0.02}}\)O\(_{\text{3}}\)], denoted by PZT 95/5-2Nb or PZT 95/5, is a ferroelectric (FE) phase with a rhombohedral structure, but it is near the boundary of an antiferroelectric (AFE) phase having an orthorhombic structure [1]. At a hydrostatic pressure of approximately 0.4 GPa, the FE-to-AFE phase transition occurs [1].

If the PZT 95/5 ferroelectric sample was previously poled, the FE-to-AFE phase transition results in a sudden release of a bounded electric charge at the contact plates of the sample. This effect can be used for generation of primary electrical power. The first attempts to utilize the FE-to-AFE phase transition through the shock compression of the poled ferroelectric samples is strong enough to provide the release of bonded charges without an initiation of FE-to-AFE phase transition. In our opinion, it is almost not possible that anti-ferroelectric phase state (that is a specific kind of magnetic ordering of the ferroelectric state) can be created with a totally destructive shock-wave impact associated with highly intense shock heat and ultimate shock pressure. Our approach is based on the assumption that phase transformation in shocked ferroelectrics would be more like FE-to-non-FE. It means that ferroelectric materials having chemical compositions far from phase transition boundaries are capable to release its polarization charge under the shock wave action. If the PZT 95/5 is closed to FE-to-AFE phase boundary [8], the ferroceramics Pb(Zr\(_{0.52}\)Ti\(_{0.48}\))O\(_{3}\) (denoted by PZT 52/48) is exactly on the morphotronic phase boundary (MPB) (i.e. between the tetragonal ferroelectric phase and the rhombohedral ferroelectric phase). It should noted that all PZT compounds near the MPB have maximum coupling coefficient and maximum relative permittivity which are important for engineering applications of ferroceramics [8].

The mechanism of the release of the electric charge in shocked ferroelectric samples would include several physical and structural processes. For instance, this mechanism could definitely utilize ceramic porosity. It was recently demonstrated [9] that spherical micron size...
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**Subject Terms:**
- Ferroelectric generators
- Shock wave
- Explosive
- Active loads
- Electrical parameters
- Geometrical dimensions
- Pulsed power

**Supplementary Notes:**
pores in energetic materials are transformed into enormous growing fractal-type cracks behind the shock wave front. Similar effects may take place in the shocked ferroelectric ceramic samples. Thus, bounded charges could be quickly released in the compressed part of the ferroceramics.

Since the end of 1990s, we have been performing systematic studies of pulsed power generation with compact explosive driven ferroelectric generators utilizing longitudinal shock compression of poled PZT 52/48 ceramic samples.

In our previous work [10,11], we performed systematic experimental and modeling studies of pulsed power generation with the ferroelectric generators based on longitudinally shocked (shock wave propagated along the depolarization vector \( P \)) PZT 52/48 ceramic samples loaded with practical loads, capacitor banks that were prototypes of the miniature Marx generator capacitors bank.

In this work, we extended this research line and performed experimental studies of pulsed power generation with longitudinal shock wave ferroelectric generators (FEGs) loaded with ohmic loads over a wide range of load resistance (about 5 orders of magnitude).

II. RESULTS AND DISCUSSION

A schematic diagram of the experimental setup for studies of the operation of the longitudinal shock wave FEG in the resistance mode is shown in Fig. 1. It contains an explosively driven longitudinal FEG, a load circuit and a pulse measuring system.

![Figure 1. Schematic diagram of the experimental setup for investigating the operation of the explosive-driven FEG in the resistance mode.](image)

The load of the FEG was made of low-inductance 2-watt bulk carbon composition resistors. For each load, from three to five resistors were connected in series to avoid electrical breakdown along their surfaces. The inductance of the load units did not exceed 230 nH.

![Figure 2. Equivalent circuit of the FEG operating in the resistance mode.](image)

Pearson Electronics current monitors, models 411 and 110, were used for measurement of the pulsed current. A Tektronix P6015A high-voltage probe was used to monitor the FEG output voltage. Pulsed signals were recorded with an HP Agilent 54845A oscilloscope (bandwidth 1.5 GHz, 8 GSa/s) and a Tektronix TDS2024 oscilloscope (bandwidth 200 MHz, 2 GSa/s). The explosive driven FEGs were placed in a detonation chamber. The load, measuring circuits and pulse recording equipment were placed outside the detonation chamber. Other experimental details are described in [6, 10-13].

The equivalent circuit of the FEG operating in the resistance mode is shown in Fig. 2. The FEG-Load system is represented as an RC-circuit, but it is not a conventional RC-circuit. The ferroelectric energy-carrying element of the FEG is a dynamic capacitor that is charged due to shock wave depolarization of the ferromodule, and it is immediately discharged through the load. The capacitance of the shock-compressed part of the ferroelectric element is represented in the circuit as \( C_{\text{Shocked}} \) [Fig. 2(a)], and the capacitance of uncompressed part of element is as \( C_{\text{Unshocked}} \). Shock wave compression changes the electrical and physical properties of ferroelectric materials significantly. The permittivity (and the capacitance) of
shock-compressed ferroelectric materials is a function of the parameters of the shock wave. The electrical conductivity of shock-compressed part of the ferroelectric element can be higher than that of uncompressed part. The parameter $R_{\text{FEG}}$ represents the resistance of the shock-compressed part of the ferroelectric element in the equivalent circuit of the FEG-Load system [Fig. 2(a)]. $R_{\text{load}}$ and $L_{\text{load}}$ are resistance and inductance of the load, respectively. The E.M.F. represents the electric charge released at the contact plates of the ferroelectric element due to its shock wave depolarization.

**A. Low resistance loads**

To get information about operation of FEGs with low resistance loads we performed a series of experiments with FEGs containing thin PZT 52/48 element of 26.0 mm diameter ($D$) and 0.65 mm thickness ($h$). A typical waveform of the voltage pulse produced by an FEG containing a PZT 52/48 element of $D = 26.0 \text{ mm}/h = 0.65 \text{ mm}$ across a $0.7-\Omega$ load is shown in Fig. 3. The voltage oscillated with an obvious maximum in the voltage waveform. The peak amplitude of the voltage pulse was $U_{\text{max}} = 1.31 \text{ kV}$ with full width at half the maximum (FWHM) of 0.1 ms, and risetime $\tau = 0.1 \text{ ms}$.

Corresponding waveforms of the output current $I(t)$, voltage $U(t)$, and power $P(t)$ pulses produced by an FEG across a $0.7-\Omega$ load are shown in Fig. 4. The peak output current was $I_{\text{max}} = 12.6 \text{ μA}$.

The power dissipated by the load was calculated as the product of the instantaneous value of the output voltage $U(t)$ and the instantaneous current in the circuit, $I(t)$: $P(t) = U(t)I(t)$. So, the peak power delivered from the FEG to a $0.7-\Omega$ load was $P_{\text{max}} = 301 \text{ kW}$. This was more than seven times higher than the power delivered to the same load by an FEG containing a PZT 52/48 element of $D = 25.0 \text{ mm}/h = 2.5 \text{ mm}$. A thin PZT 52/48 element possessing higher initial capacitance provided significantly higher power to the low-resistance load. The average peak power delivered to the load in this series of experiments was $P_{\text{aver}} = 328\pm24 \text{ kW}$.

Integration of the $P(t)$ waveform from 0 to $t$ gives the momentary value of the energy, $W(t)$, delivered to the resistance load during explosive operation of the FEG:

$$W(t) = \int_{0}^{t} P(t) \cdot dt$$

The energy delivered from the FEG to the 0.7-Ω load was 41 mJ. Average energy delivered to the load in this series of experiments was $W_{\text{aver}} = 42\pm5 \text{ mJ}$.

**B. Medium resistance loads**

A typical waveform of the high-voltage pulse produced by an FEG containing a PZT 52/48 element of $D = 25.0 \text{ mm}/h = 2.5 \text{ mm}$ across a $40-\Omega$ load is shown in Fig. 5. The amplitude of the voltage pulse produced by an FEG across the load was $U_{\text{aver}} = 13.2 \text{ μA} = 3.63 \text{ kV}$. The FWHM of the pulse was 1.1 μs and risetime $\tau = 1.0 \text{ μs}$. The maximum electric field strength reached in the ferroelectric element in this experiment was 1.73 kV/mm. The high-voltage pulse amplitude averaged from the three experiments of this series was $U_{\text{aver}} = 3.6\pm0.07 \text{ kV}$. 

![Figure 3](image1.png)

**Figure 3.** A typical waveform of the high-voltage pulse produced by the FEG containing a PZT 52/48 element of $D = 26.0 \text{ mm}/h = 0.65 \text{ mm}$ across a $0.7-\Omega$ load.

![Figure 4](image2.png)

**Figure 4.** Corresponding (Fig. 3) waveforms of the output current, $I(t)$, (dark gray), voltage, $U(t)$, (light gray) and power, $P(t)$, (black) pulses produced by the FEG containing a PZT 52/48 element of $D = 26.0 \text{ mm}/h = 0.65 \text{ mm}$ across a $0.7-\Omega$ load.
A typical waveform of the high-voltage pulse produced by the FEG containing a PZT 52/48 element of \( D = 25.0 \text{ mm}/h = 2.5 \text{ mm} \) across 40-\( \Omega \) load is shown in Fig. 5. The waveforms of the output current \( I(t) \), high voltage \( U(t) \), and power \( P(t) \) pulses produced by an FEG across 40-\( \Omega \) load are shown in Fig. 6. The peak output current was \( I(13.3 \mu s)_{\text{max}} = 85.4 \text{ A} \). The peak power delivered to the 40-\( \Omega \) load was \( P(13.3 \mu s)_{\text{max}} = 321 \text{ kW} \), and the average peak power delivered to the load in this series of experiments was \( P_{\text{aver}} = 314\pm11 \text{ kW} \).

The maximum energy delivered to the 40-\( \Omega \) load in this experiment was \( W_{\text{max}} = 225 \text{ mJ} \). The average energy delivered to the load in experiments of this series was \( W_{\text{aver}} = 219\pm18 \text{ mJ} \). The specific energy density of the PZT 52/48 element in these experiments was \( W_{\text{spec aver}} = 182.5\pm15.0 \text{ mJ/cm}^3 \).

C. High resistance loads

Figures 7 and 8 presents a typical waveform of a high-voltage pulse produced by an FEG containing a PZT 52/48 element of \( D = 25.0 \text{ mm}/h = 5.1 \text{ mm} \) across a 300-\( \Omega \) load, and the corresponding waveforms of output current and power. The amplitude of the voltage pulse was \( U(8.7 \mu s)_{\text{max}} = 6.82 \text{ kV} \), FWHM was 1.52 \( \mu s \) and risetime \( \tau = 1.5 \mu s \). The maximum electric field strength reached in the ferroelectric element in this experiment was 1.34 kV/mm. The high-voltage pulse amplitude averaged from three experiments of this series was \( U(t)_{\text{aver}} = 6.77\pm0.71 \text{ kV} \).
The maximum energy delivered to the 300-Ω load in this experiment was \( W_{\text{max}} = 186 \text{ mJ} \). The energy averaged over the three experiments of this series was \( W_{\text{avg}} = 181.4\pm12.7 \text{ mJ} \). The specific energy density of the PZT 52/48 element in these experiments was \( W_{\text{spec avg}} = 72.4\pm5.1 \text{ mJ/cm}^3 \).

D. Experimental result summary

In addition to the experiments described above, extensive studies were also performed for FEGs with a 14-kΩ resistance load. Thus, in the series of experiments described in this paper, the resistance of the load was varied in the range from 0.7 Ω to 14 kΩ. Results of experiments with FEGs containing PZT 52/48 elements of \( D = 26.0 \text{ mm/h} = 0.65 \text{ mm} \), \( D = 25.0 \text{ mm/h} = 2.5 \text{ mm} \) and \( D = 25.0 \text{ mm/h} = 5.1 \text{ mm} \) are shown in Figs. 9 through 11.

Figure 9 presents the amplitudes of voltage pulses produced by FEGs versus resistance of the load. Because of the wide range of load resistances, the X-axis (Load Resistance) of the graph is a logarithmic scale. Our experimental results show that increasing the load resistance leads to an increase of the voltage produced by the FEG.

Figure 10 summarizes the amplitudes of current generated by FEGs in a load circuit. The current amplitude is inversely proportional to the load resistance. The maximum current of 308 A was reached with a load of resistance 0.7 Ω. In this resistance range, the FEG output current has inverse exponential dependence on the load resistance.

Figure 11 summarizes results of experiments concerning the energy delivered from the FEGs in the loads. It follows from our experimental results (Figs. 11) that there is an optimum load resistance at which the FEG provides the maximum output power and energy.
III. SUMMARY

Systematic experimental investigations of the operation of explosively driven longitudinal shock wave FEGs with active loads in a wide range (more than 4 orders of magnitude) of resistance were performed. The experimental results show that the output voltage, current, and power produced by the FEG across the resistance load depend on both the electrical parameters of the load and on the geometrical dimensions of the ferroelectric energy-carrying element of the FEG. We experimentally demonstrated that a miniature FEG is capable of delivering pulsed power with a peak amplitude up to 0.35 MW to an active load.

New fundamental experimental results revealing the logarithmic dependence of the voltage generated by the FEG containing PZT 52/48 ferroceramics across the active load, versus the resistance of the load, were obtained in this work.

IV. REFERENCES

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